AN ANALYTICAL AND EXPERIMENTAL STUDY OF BLOOD OXYGENATORS AND PULMONARY MASS TRANSFER IN LIQUID BREATHING

Еу

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NOMENCLATURE

A	=	interfacial surface area
C	=	concentration
Ci	=	concentration of component i in a mixture
C [*] i	==	concentration of component i in the liquid phase that is in equilibrium with component i in a second phase
(C ₁)	=	n-dimensional column matrix containing the concentrations of the blood constituents at the entrance of the bubble oxygenator
C _M :	72	the amount of component k bound to component M
C ^f i	æ	concentration of the ith component in a liquid film
C ^{out} i		concentration of the ith component in the liquid phase between two discs
c ^{ia}	=	concentration of component i in the inlet stream to a mixing stage
D	735	binary diffusion coefficient
[D]	=	n x n matrix of multicomponent diffusion coefficients
D _b	==	diffusivity of oxygen in blood
DB	gart a Accode	bubble diameter
Di	=	diffusivity of component i into a mixture
$D_{\mathbf{p}}$	2.5	diffusivity of oxygen into plasma
e i		obnicentration of dye in the alveoli of the ith stage in the lung
fM	****	equilibrium relationship which equates the total amount of component k to the concentrations of the remaining constituents
G_{M}	12	equilibrium relationship which equates the amount of component k, bound to component M, to the remaining species concentrations in the mixture

```
volume fraction of red cells in the blood, i.e., hematocrit
               diffusion flux of component i
J,
K
              binary mass transfer coefficient
              n x n matrix of multicomponent mass transfer coefficients
[K]
K
               equilibrium constant
               mass transfer coefficient of species i into species j
K_{\underline{i},j}
               mass flux of component i
Nai
Р
               pressure
P;
               partial pressure of component i
               radius
r
           = radius of a bubble
R
           = n-dimensional column matrix of reaction rates
(R)
            = rate of reaction of the ith component
R_{\downarrow}
              fractional oxygen saturation
S
Sr
              reduced fractional saturation
                \begin{bmatrix} arterial & 0 \\ 2 \end{bmatrix} saturation - venous \begin{bmatrix} 0 \\ 2 \end{bmatrix} saturation
                 saturation at P_{0_2} = 760 \text{ mm} - \text{venous } 0_2 \text{ saturation}
               time
              temperature
               volume flow rate into alveoli in the ith mixing stage
v
            = volume
            = velocity
```

= volume in the lung at which transport becomes diffusion-

= volume flow rate

= volume of a stagnant film

controlled

```
V<sub>H</sub> = gas holdup volume
```

$$V_{TOT}$$
 = total lung volume

$$V_0$$
 = initial volume of the lungs

x = distance parameter

y = mole fraction of oxygen saturation

Greek Latters

 α_i = Henry's law constant of component i in a solvent

γ = ratio of gas to liquid flow rate in the bubble oxygenator

 δ = boundary layer thickness

μ = viscosity

t = residence time

6 = residence time of a film at the blood membrane interface

 χ = effective residence time as defined in Equation 3.3-4

 ψ = effective residence time as defined in Equation 3.3-3

 ω = angular velocity

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Ву

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Chairman: Professor Robert D. Walker, Jr. Major Department: Chemical Engineering

Mathematical models for blood oxygenation in bubble and disc oxygenators have been proposed. In the case of the bubble oxygenator, a single-stage, perfectly mixed absorber model was tested and confirmed by a saline simulation experiment which approximated oxygenator use in open-heart surgery. From data taken during sixteen open-heart operations, oxygen and carbon dioxide mass transfer coefficients were estimated as

$$K_{O_2,B} = 0.00528 \frac{cm}{sec}$$

$$K_{CO_2,B} = 0.0131 \frac{cm}{sec}$$

With these results, a computer program was written to simulate the operation of the bubble oxygenator over a wide range of oxygen and blood flow rates. During the simulation experiment, it was found that for each of the four sizes of oxygenators tested, an optimal

ratio of gas to liquid flow rate was obtained. Furthermore, the oxygenation rate was reduced when gas flow rates exceeded 7 to 8 liters per minute in all four models.

In the case of the disc oxygenator, the equilibrium relationships and other physical constants have been put into subroutine form for easy substitution in other systems.

The problem of gas transport in liquid-filled lungs was also considered. It was proposed that oxygen and carbon dioxide transport through the bulk of the lung by convective mixing instead of by diffusion as proposed by Kylstra. A transient breathing experiment measuring dye penetration into saline- and fluorocarbon-filled lungs was devised and carried out. From the data obtained, it was determined that gas transfer through the bulk of the lung was by convective mixing; the lung was approximated by ten perfect mixing stages in series when fluorocarbon was used and twenty perfect mixing stages in series when saline was used.

CHAPTER 1

THE DEVELOPMENT OF ARTIFICIAL BLOOD OXYGENATORS

1.1 Historical Development

Attempts to oxygenate blood artificially date back to the nineteenth century. The oxygenation of blood by shaking with air was reported by Ludwig and Schmidt (1) in 1868, while the first continuous process for blood oxygenation was attempted by Schorder (2) in 1882, who showed that blood could be oxygenated by bubbling air through it. Zeller (3) in 1908, improved the rate of oxygenation by using pure oxygen in place of air.

Continued improvement in this method of oxygenation eventually led to the development of the bubble oxygenator by De Wall and co-workers (4) in 1956. It is probably the most widely used oxygenator at this time cwing to its relatively low cost, simplicity of operation and complete disposability.

Another early method of ovygenating blood, which eventually evolved into a successful design, was the thin film transfer unit; it was studied by Hooker (5) in 1915, and by Drinker and co-workers (6). The basic design consisted of a glass cylinder through which exygen was passed. A thin film of blood was distributed on the cylinder wall, the direction of blood flow induced bring countercurrent to the direction of oxygen flow. This type of design eventually evolved into the screen oxygenator developed by Miller et al. (7) in 1951. In the Miller and Gibbon oxygenator, a series of parallel screens replace a set of concentric cylinders as the blood-filming surface,

but the essential idea of oxygen transfer into a thin blood film is still the main feature of the design.

Bjork (3) developed an alternate thin film oxygenator in 1948. His oxygenator consisted of a series of rotating discs, exposed to a stream of oxygen, which dip into a blood reservoir. This method of oxygenation is based on oxygen transfer into a thin film which is constantly being renewed with fresh blood.

These three types of oxygenators, the bubble, screen, and disc, have been tested experimentally and used clinically. These oxygenators, which might be termed first-generation oxygenators, have two features and disadvantages in common. Firstly, all of them require direct contact between gaseous oxygen and blood, and thus protein denaturation becomes a problem after extended periods of operation.

Secondly, these methods of oxygenation attempt to minimize resistance to mass transfer of oxygen into the blood by minimizing diffusional resistance in the blood phase.

To date, the principal application of blood exygenators has been as cardiac bypass units in open-heart surgery. The three exygenators discussed above have been used for short term (up to approximately three hours) by-pass of the heart and lungs during either surgical repair or replacement of sections of the heart. The current limitation on operating time is the rate of hemolysis, or red blood cell destruction, and the rate of protein denaturation. In an effort to minimize protein denaturation new exygenators, which might be termed second-generation exygenators, are in development. All of these

new designs eliminate the direct contact of gaseous oxygen and blood. It is anticipated that elimination of the blood-gas interface will reduce protein denaturation and increase the possible bypass time to the order of days rather than hours. Such a development would be of value in the treatment of heart and lung damage which cannot be corrected by surgery.

There have been a number of different schemes proposed to accomplish the oxygenation of blood without direct contact between gaseous oxygen and blood, two of which appear to be promising. Research on the use of membranes through which gaseous oxygen can diffuse into blood has been underway for approximately the last fifteen years.

Kottf and Balzer (9) attempted to oxygenate blood by flowing blood in polyethylene tubes while oxygen was passed over the tubes. Bodell and co-workers (10) tried the reverse experiment of immersing tubes, through which oxygen flowed, in blood. Others (11,12) have attempted to use these two methods with different membrane materials. The material that appears to be most promising at this time is Silastic (a silicone rubber) tubing. Pierce (13) has also tested a membrane oxygenator which has blood flow channels embedded in spaced layers of membranes through which oxygen is passed.

The second method of blood oxygenation which would eliminate the direct contact of gasecus oxygen with blood involves the use of inert fluorocarbons as an exchange medium. Basically, the process works as follows: a fluorocarbon (or other inert, water-insoluble liquid) is oxygenated by bubbling oxygen through it, then the oxygenated

fluorocarbon is brought into contact with venous blood. Oxygen is transferred from the saturated fluorocarbon into the blood and carbon dioxide is transferred from the blood into the fluorocarbon. Since fluorocarbon is insoluble in blood, the blood-fluorocarbon mixture can be separated and the fluorocarbon can be recycled for decarbonation and reoxygenation. Research in this area is quite recent and the literature on this method of oxygenation is sparse. Nose and co-workers (14) have designed a thin film oxygenator using fluorocarbon (FX-80) as a transfer medium. Dundas (15) has performed similar experiments with FX-80 as well as DC-200 silicone oil. Results so far are promising, but this method of oxygenation will require a great deal of further research before a working fluorocarbon oxygenator can be developed.

Although the bubble, disc and screen oxygenators have been in use for over a decade, no mathematical models have been developed which describe their operation adequately. Furthermore, only in the case of the screen oxygenator (16) has there been an attempt to describe mathematically the rate-limiting process in oxygen transfer. Significantly, the initial work done thus far with fluorocarbon oxygenators does not involve mathematical models. It was the original goal of this research to develop and test mathematical models for the disc and bubble oxygenators in the hope that these models would provide a basis for similar modelling of fluorocarbon oxygenators. Furthermore, such mathematical models should prove useful in developing in vitro experiments to determine the effects of anesthetics and other drugs on blood oxygenation, and should provide a clinical tool for open-heart surgery.

The development of models for membrane oxygenators, in contrast to other oxygenators, has been the subject of a number of research studies. Bradley (17) has done a thorough study of gas exchange through silastic tubes through which blood is pumped. Lightfoot (18), and Weisman and Mockros (19) have also constructed models for the design of membrane oxygenators.

1.2 The Cardiovascular-Pulmonary System

Since blood oxygenators are designed to take over the functions normally performed by the heart and lungs, the evaluation of such artificial oxygenators requires a thorough understanding of the human cardiovascular-pulmonary system. This system consists of the heart, lungs and a network of veins, arteries and capillary beds. The function of the kidneys is also important to consider as some of the problems that arise in artificial blood oxygenation are directly attributable to these organs. A schematic diagram of the cardiovascular system is shown in Figure 1.2.1.

The heart serves as a pump to circulate blood through the network of veins and arteries to the various points in the body where oxygen, carbon dioxide, and other blood constituents are exchanged. It is a four-chambered vessel: Venous blood flows into the right atrium and thence into the right ventricle which acts as a positive displacement pump to force the blood through the pulmonary system and into the left atrium. Arterial blood flows into the left ventricle which in turn pumps blood through the arteries and veins which compose the circulatory system.

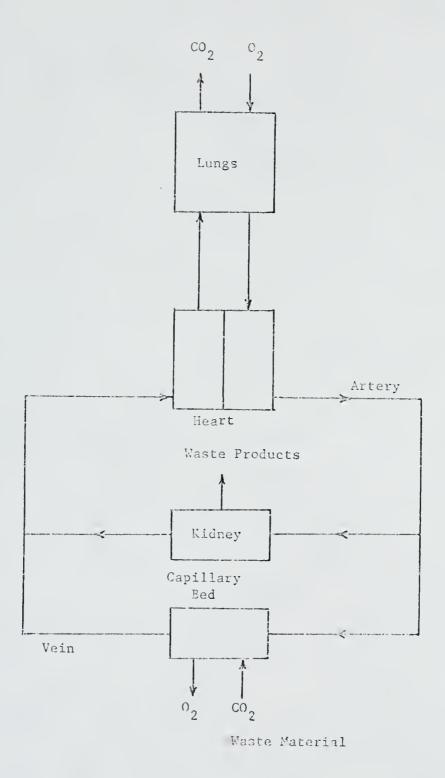


Figure 1.2-1. The Cardiovascular System.

The arteries are a network of flow channels which transport blood to the pulmonary capillary bed and to systemic capillary beds which are distributed throughout the body tissues. Gas exchange takes place in these capillary beds. In the case of pulmonary capillaries, oxygen is transferred into the blood while carbon dioxide is transferred out, and in the case of the systemic capillaries, carbon dioxide is transferred into the blood while oxygen is transferred into the tissue. Upon exiting from the systemic capillaries the blood is transported back to the heart through a network of veins.

The function of the kidneys is to remove waste material from the blood stream. About 25% of the total blood flow passes through the renal arteries into these two bean-shaped organs. Once in the kidney, blood is distributed to approximately 1 million transfer units called nephrons. A nephron consists of an entrance called Bowman's capsule and a series of transfer units in which four processes occur. The first unit, the glomerulus, is an ultrafilter which separates erythroctes, lipids and plasma proteins from the remaining plasma constituents. The second unit consists of the proximal tubule, Henle's loop, and distal tubule. This section is basically a long tubule folded and looped in sections in which some plasma constituents and water are reabsorbed and other constituents are secreted into the tubule. The final unit is the collecting duct in which, as its name implies, waste products and water are collected to be eventually excreted from the body.

The details of the phenomena which occur in the kidneys are

quite complex and numerous, and a comprehensive discussion of them is beyond the scope of this work. There are a number of text and papers which treat the kidneys, among which is a recent and concise summary by Pitts (20).

The lung, of course, also forms an important part of the cardiovascular-pulmonary system supplying oxygen to the blood and facilitating carbon dioxide removal from the same. Since it is an oxygenator in its own right, we have chosen to discuss it in comparison with artificial oxygenators in Section 1.5 rather than in connection with the cardiovascular-pulmonary system.

1.3 The Properties of Blood

Blocd has been the subject of much research, generally concentrating on either biochemical interactions or rheology. In the following paragraphs we have drawn heavily from texts by Ferguson (21), and Whitmore (22) to collect a pertinent summary.

Whole blood is essentially a suspension of red blood cells in plasma. Other formed elements in the plasma include white blood cells and platelets. The plasma is an aqueous solution containing about 7% proteins, 0.9% inorganic selt, and 2.1% organic substances other than proteins.

As stated in Section 1.2, blood is distributed throughout the body through a network of veins and arteries. In addition to supplying all body tissues with oxygen and removing carbon dickide and waste materials, blood also carries nutrients to the tissues, and it also serves as a heat transfer medium to control temperature within the

more, blood regulates the fluid balance throughout the body and provides a defense mechanism against diseases.

The red blood cells, or eyrthrocytes, which carry most of the oxygen in the blood stream are biconcave discoids. The dimensions of the human eyrthrocytes quoted by Lehman (23), and Britton (24) are as follows:

dimmeter = 7.8 microns
thickness = 1.84 - 2.06 microns
volume = 88 cubimicrons.

The red cell is quite flexible and thus easily distorted. It is this property that permits the cells to pass through capillaries that are smaller in diameter than themselves. It is interesting to note that the eyrthrocytes pass through the capillaries in slip flow. Although a number of studies on microcirculation have been reported by Gopley (25), Lew (26), Wells (27,28), and Goldsmith (29), a mathematical model based upon slip flow has not been proposed or tested at this time. Since good microcirculation is necessary for alequate oxygenation of cell tissue and since microcirculation is affected by hemolysis, that is, cell breakage, during cardiac bypass, it appears that an understanding of the slip flow mechanism in capillaries would provide valuable insight into the development of better blood oxygenators.

An erythrocyte consists of a membrane enclosing fluid without a nucleus. The membrane is formed of a bimolecular layer of lipids and the coll fluid contains approximately 33% hemoglobin. Hemoglobin is

the constituent which is responsible for the large oxygen-carrying capacity of blood, vide infra.

White blood cells, or leucoytes, provide a defense mechanism against disease. They are classified into three groups according to size, ranging from 7 to 22 microns. From the smallest to the largest the three types of leucocytes are lymphocytes, granulocytes, and monocytes. The total concentration of these cells in normal blood is negligible compared to red cell concentration, the ratio of eysthocyte to leucocyte cells being approximately 1000 to 1. The white cell is more rigid than the red cell, but it has a gelatinous membrane which easily deforms to adjust to local conditions.

Platelets are disc-shaped cell remnants much smaller in size than other formed elements and having a diameter between 0.5 and 3 microns as reported by Bell (30), Merrill (31), and Britton (24). Platelets play an important role in the blood coagulation process, which we shall discuss shortly.

Plasma, the fluid in which all of these formed elements are suspended, is both a molecular and ionic solution. The major ions which are dissolved in the solution are sodium, potassium, calcium, magnesium, chlorine, and bicarbonate. The principal molecular proteins in the solution are fibrinogen, α , β , and γ globulins, and albumin. Fibrinogen, which polymerizes to fibrin during coagulation, is one of the largest of the protein molecules. The globulins, whose specific functions are not understood, are extremely important as carriers of lipids and other water soluble substance. Albumin, the plasma pretair in highest concentration, is important in maintaining the balance of water metabolism.

Having described the constituents of the blood we are now . prepared to venture into a discussion of how these various components in the blood combine with oxygen and carbon dioxide, transport these two gases to the appropriate locations in the body, and then release them to the body tissue and lungs, respectively. Of major importance are the reactions hemoglobin undergo but we will also comment on thrombosis, protein denaturation, and hemolysis which are three serious problems which may occur during or shortly after cardiac bypass. Hemoglobin is a large protein molecule with a molecular weight of 67,000 containing approximately 10,000 atoms (32) and an effective diameter of 50 to 64 Å (33). It is a tetramer, each polymeric chain containing an iron atom combined with a heme group connected to a polypeptide chain. The heme group is an iron porphyrin complex which reversibly binds oxygen. It is important to note that heme iron bound to oxygen remains in the ferrous state (i.e., oxidation of iron by oxygen does not take place), and consequently the oxygen molecule maintains its identity. Both oxygen and hemoglobin are paramagnetic, but oxyhemoglobin is diamagnetic, indicating a covalent bond between iron and oxygen. This bond is, in fact, very weak, and the reaction can be shifted by a slight charge in pH. Consider a dissociable hydrogen ion attached to a hemoglobin molecule.

$$H \cdot Hb^{+} + O_{2} \stackrel{>}{\sim} HbO_{2} + H^{+}$$
 (1.3-1)

If the pH of the hemoglobin environment decreases, i.e., the hydrogen ion concentration increases, the reaction is shifted to the left with a release of oxygen. If the pH increases, the reaction will shift to

the right and oxygen will be taken up. In the body the pH decreases when carbon dioxide is released into the blood stream in the form of bicarbonate ion

$$CO_2 + H_2O ? H_2CO_3 ? H^+ + HCO_3^-$$
 (1.3-2)

Thus, oxygen release to body tissue is facilitated by carbon dioxide absorption into the blood. In the lungs, where carbon dioxide is released, the pH increases and oxygen binding to hemoglobin is facilitated again by the CO₂ transfer.

The kinetics of hemoglobin-oxygen reactions have been the subject of a number of research studies and several models have been proposed for the mechanism of reaction. Among the earliest is the mechanism proposed by Hill (34)

$$Hb + nO_2 \stackrel{?}{=} Hb(O_2)n$$
 (1.3-3)

for which it can be easily shown that the mole fraction of hemoglobin saturated is

$$y = \frac{\hat{K}P^n}{1 + \hat{K}P^n} \tag{1.3-4}$$

where \hat{K} is the equilibrium constant and P is the partial pressure of oxygen in the mixture. Since each hemoglobin molecule combines with 4 oxygen molecules, the value of n should be equal to 4, but experimental values range between 1.4 and 2.9 and they depend on the ionic strength of the solution. Although this fact undermines the theoretical basis for Fill's equation, Equation 1.3-4 is still used because of its simplicity. \hat{K} , of course, is a function of both ionic strength and pH.

Adair (35), in 1925, proposed a four-parameter model for hemoglobin oxygenation involving the following series of steps:

$$Hb_{4} + o_{2} \stackrel{?}{=} Hb_{4}o_{2}$$

$$Hb_{4}o_{2} + o_{2} \stackrel{?}{=} Hb_{4}o_{4}$$

$$Hb_{4}o_{4} + o_{2} \stackrel{?}{=} Hb_{4}o_{6}$$

$$Hb_{4}o_{6} + o_{2} \stackrel{?}{=} Hb_{4}o_{8}$$

$$(1.3-5)$$

It can be shown after a fair amount of algebra that the fractional saturation is

$$y = \frac{\hat{K}_{1}P + 2\hat{K}_{1}\hat{K}_{2}P^{2} + 3\hat{K}_{1}\hat{K}_{2}\hat{K}_{3}P^{3} + 4\hat{K}_{1}\hat{K}_{2}\hat{K}_{3}\hat{K}_{4}P^{4}}{4(1 + \hat{K}_{1}P + \hat{K}_{1}\hat{K}_{2}P^{2} + \hat{K}_{1}\hat{K}_{2}\hat{K}_{3}P^{3} + \hat{K}_{1}\hat{K}_{2}\hat{K}_{3}\hat{K}_{4}P^{4})}$$
(1.3-6)

where \hat{K}_1 through \hat{K}_4 are the equilibrium constants for the reactions shown in Equation 1.3-5. Note that Equation 1.3-6 does not take into account pH or ionic concentration and thus the equilibrium constants must be functions of these two variables in addition to temperature.

In 1935, Pauling (17) developed a model which did take into account pH effects and assumes a heme-heme interaction. His resulting equilibrium relationship

$$y = \frac{\hat{K}P + (2a+1)\hat{K}^2P^2 + 3a^2\hat{K}^3P^3 + a^4\hat{K}^4P^4}{1 + 4\hat{K}P + (4a+2)\hat{K}^2P^2 + 4a^2\hat{K}^3P^3 + a^4\hat{K}^4P^4}$$
(1.3-7)

where PTlna is the decrease in free energy due to the interaction of two groups ${\rm HbO}_2$. If RTlnb is the difference in the change free

energies of hydrogen ion dissociation from oxyhemoglobin and from nemoglobin, the pH dependency of K is given by

$$\hat{K} = \hat{K}' \frac{(1 + bA/[H^+])^2}{(1 + A/[H^+])^2}$$
(1.3-8)

where A is the acid ionization constant. A modification of Pauling's model was proposed by Margaria (36) in 1963. His final result is

$$y = \frac{\left(\frac{1 + \hat{K}P}{KP}\right)^3 + m - 1}{\left(\frac{1 + \hat{K}P}{\hat{K}P}\right)^4 + m - 1}$$
(1.3-9)

where m is constant found experimentally to be equal to 125.

It should be noted that Margaria's equation is a one-parameter model and that \hat{K} is a function of pH as well as ionic concentration again.

There are a number of other possible models which have been summarized by Adecdato de Souza (37). We have chosen to use an updated version of Adair's equation developed by Kelman (38) to approximate the saturation curve. The modified Adair equation including temperature, pH, and carbon dioxide concentration corrections has been written as a subroutine for convenient computer solution by Kelman. It is thus particularly swited for this work. The actual equations used along with the subroutine are listed in Appendix A. Typical saturation curves as functions of oxygen partial pressure, carbon dioxide partial pressure, temperature, and pH are shown in Figures 1.3-1, 1.3-2, and 1.3-3. It should be noted that as pH increases, the saturation curve

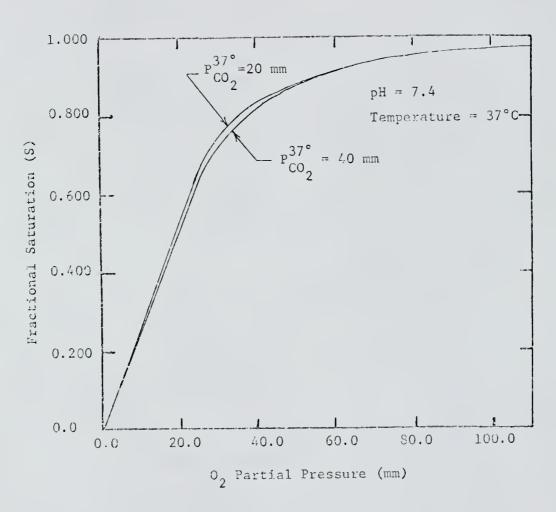


Figure 1.3-1. The Effect of Carbon Dioxide Partial Pressure on Oxygen Saturation in Whole Blood.

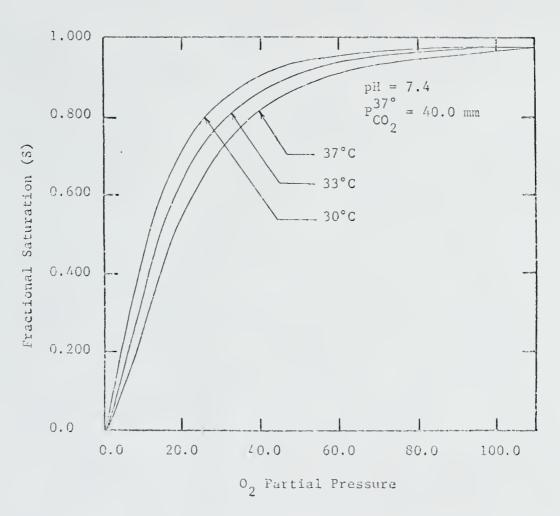


Figure 1.3-2. The Effect of Temperature on Oxygen Saturation.

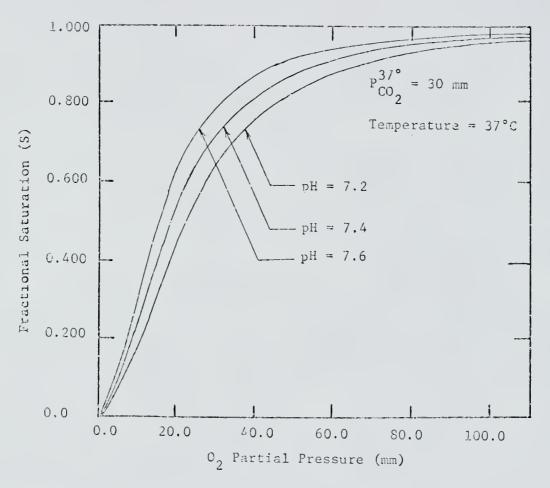


Figure 1.3-3. Effect of pH on Oxygen Saturation in Whole Blood.

shifts towards lower partial pressures of oxygen. This effect, known as the Bohr effect, plays a vital role in facilitating the exchange and transport of oxygen in the body as stated earlier in this section.

Carbon dioxide also interacts with blood in a number of ways. The majority of carbon dioxide is carried in both the plasma and red cells in the form of bicarbonate ions. The reaction of ${\rm CO}_2$ with water to form carbonic acid, and subsequently bicarbonate ions, takes place mainly within the red cell, where the reaction is catalyzed by carbonic anhydrose. The hydrogen ion released when ${\rm H_2CO}_3$ dissociates reacts with the nitrogen of the imidazole group of the hemoglobin molecule. This reaction buffers the blood and regulates the pH within a narrow range for large changes in ${\rm CO}_2$ concentration. ${\rm CO}_2$ also reacts directly with the amine groups of hemoglobin as well as proteins in general. These reactions can be summarized as follows:

$$CO_2 + Bb \cdot NH_2 \neq Bb \cdot NH \cdot COOH$$
 $Bb \cdot NH \cdot COOH \neq Bb \cdot NH \cdot COO^- + B^+$
 $Carbonic$
 $CO_2 \neq B_2O \neq B_2CO_3$
 $CO_3 \neq B_2CO_3 \neq B_2CO_3$

Bradley (17) suggested that ${\rm CO}_2$ concentrations can be represented by a two-parameter model

$$C = 0.373 - 0.07/85S + 0.00456 P_{CO_{S}}$$
 (1.3-11)

where C is the total concentration of carbon dioxide, S is the fractional saturation of hemoglobin by oxygen, and P_{CO_2} is the partial pressure of carbon dioxide. Since the total CO_2 concentration is not a function of total hemoglobin concentration and does not equal zero at zero CO_2 partial pressure, Equation 1.3-11 must be viewed as semiempirical; it is valid for CO_2 partial pressures ranging from approximately 30 to 60 mm. We note in passing that there is a variation in the CO_2 saturation curve with respect to hemoglobin saturation, similar to the Bohr effect for oxygen saturation. This is shown in Figure 1.3-4 and is known as the Haldane effect.

In addition to blood-gas chemistry, we are interested in a series of reactions triggered by trauma which induce blood clotting and, more generally, thrombosis. Thrombosis is always triggered by either chemically or physically induced trauma. The first step in the process is aggregation of platelets; the next step involves the polymerization of fibrinogen to fibrin, which forms a matrix for the thrombus. During the physiological changes, a series of chemical reactions occurs for which a cascade mechanism has been proposed (39,40). The reaction is an activation of an enzyme called Hageman factor. This enzyme acts as a catalyst to activate another enzyme, etc., finally forming thrombin which catalyzes the polymerization of tibringgen to fibrin (Figure 1.3-5). The formation as growth of thrombi is enhanced by a feedback mechanism as shown in Figure 1.3-6. Since adenosine diphosphate and thrombin cause aggregation, their formation during the cascade reaction provides a feedback mechanism for further growth and formation.

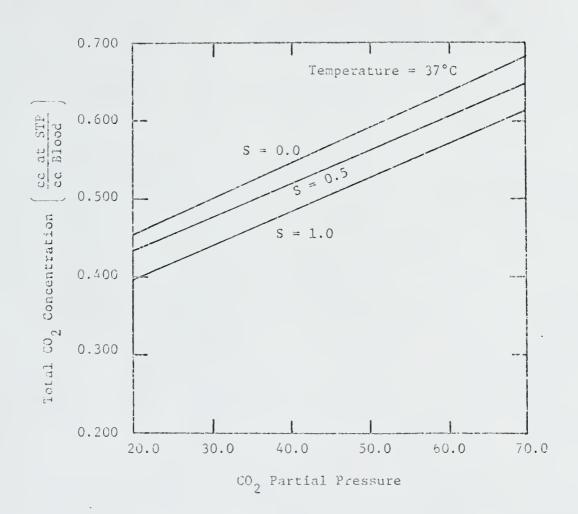


Figure 1.3-4. The Effect of $\mathbf{0}_2$ Saturation on Carbon Dioxide Concentration.

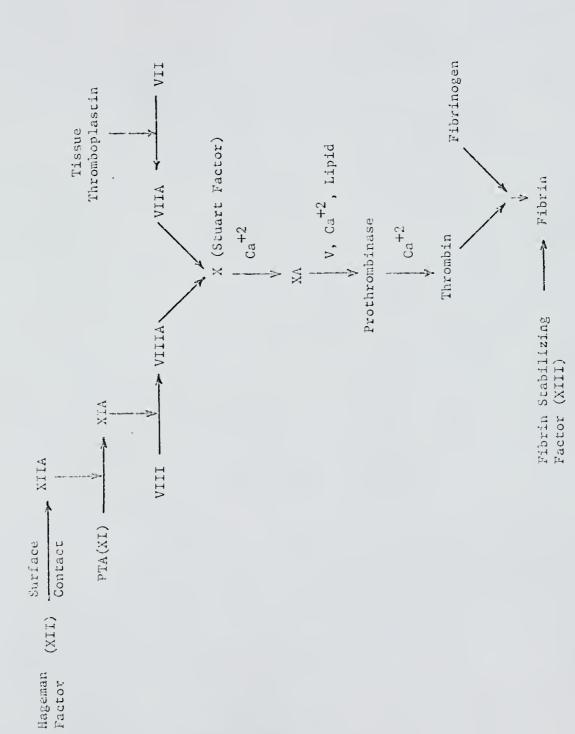


Figure 1.3-5. Cascade Mechanism for Thrombosis.

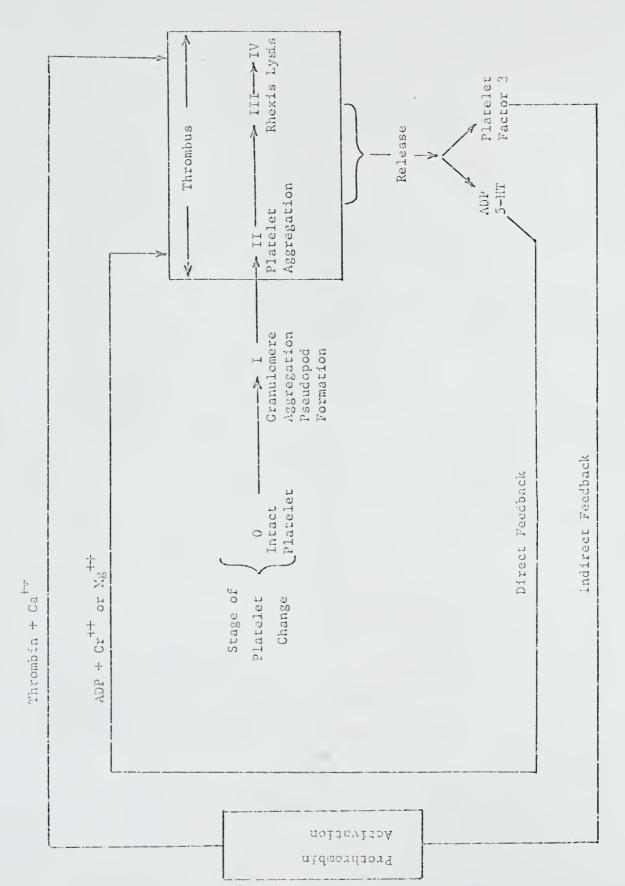


Figure 1.3-6. Feedback Mechanism for the Growth of Thrombi.

The problem of eliminating blood clots is currently surmounted by the use of anticoagulants such as ACD (acid, Citrate, Dextrose), and heparin. These anticoagulants do not completely eliminate the problem as poor oxygen distribution, indicative of embolism and clot formation, is sometimes observed both during and after surgery.

Research to provide a better understanding of clotting and thrombosis mechanisms appears to be a prerequisite for improved clinical techniques in this area.

1.4 Description of Oxygenators

The title "oxygenator" for artificial heart-lungs is a misnomer, since both ${\rm CO}_2$ and ${\rm O}_2$ are exchanged in these units; gas exchangers would appear to be a more descriptive term. In all of the direct contact exchangers, three processes occur:

- Oxygen is transported to the blood-gas interface and carbon dioxide is transported away from this interface by convection;
- 2. Oxyger and ${\rm CO}_2$ are transported through the blood by diffusion and convective mixing;
- 3. Chemical reactions involving ${\rm CO}_2$ and oxygen take place within the red blood cell.

In the design of blood oxygenators, it is desirable to oxygenate as much blood as possible in as short a time as possible, and consequently, various resistances to mass transfer in both gas and liquid phases should be minimized. The gas-phase resistance is essentially eliminated in all current direct contact oxygenators by supplying a

very high gas to liquid volume flow rate (in fact much more oxygen is supplied than required for complete saturation of the blood). This leaves the liquid-phase resistance to be dealt with. In mathematical form, the rate of mass transfer of a gas through a liquid can be written as (41)

rate of accumulation = net flux of component i by diffusion of component i

- + net flux of component i by convection
- + rate of formation of component i by reaction

(1.4-1)

OT

$$\frac{\partial C_{i}}{\partial t} = -\nabla \cdot J_{i} - \nabla \cdot (C_{i} \nabla) + R_{i}$$
(1.4-2)

Using a multicomponent generalization of Fick's law and assuming incompressibility, we obtain

$$\frac{\Im\left(\mathcal{C}\right)}{\Im\left(\mathbf{t}\right)} = \left[\mathsf{D}\right]\mathsf{V}^{2}(\mathsf{C}) - \mathbf{v}\cdot\mathbf{v}(\mathsf{C}) + (\mathsf{R}) \tag{1.4-3}$$

Since diffusion is, in general, a much slower process than convection, the major resistance to mass transfer occurs in regions which are stagnant. The minimization of these diffusion layers is the major design consideration in all oxygenators. In this stagnant boundary layer, Equation 1.4-3 reduces to

$$\frac{\partial (C)}{\partial t} = [D] \nabla^2 (C) \div (R) \tag{1.4-4}$$

oxygen are pumped cocurrently into the bottom of the oxygenation chamber. Oxygen enters through a sparger and apparently bubbles through the chamber in plug flow. Oxygen diffuses into the blood from the gas bubbles, and CO_2 diffuses into the bubbles from the blood. There is a stagnant layer of blood which surrounds each gas bubble through which both gases must diffuse. After passing through the oxygenation chamber, the arterial blood flows through a stainless steel mesh which defoams the blood and then through a collecting reservoir.

The major advantages of this type of oxygenator are as follows:

- the bubble oxygenator is inexpensive and completely disposable;
- the entire system requires a small blood priming volume;
- the cocurrent flow of oxygen and blood minimizes the pressure drop across the system;
- 4. the equipment is easy to operate;
- 5. the large number of bubbles provides a large blood-gas interfacial area for gas exchange.

The major disadvantage of bubble cxygenators is that the turbulent motion of blood in the oxygenation causes hemolysis and thus limits the time bypass can be sustained.

The disc oxygenator, as shown in Figure 1.4-2, consists of a series of discs mounted in a horizontal cylinder. Venous blood is pumped into one end of the cylinder, the flow rates being regulated at both ends by two pumps to maintain the blood level at a depth of

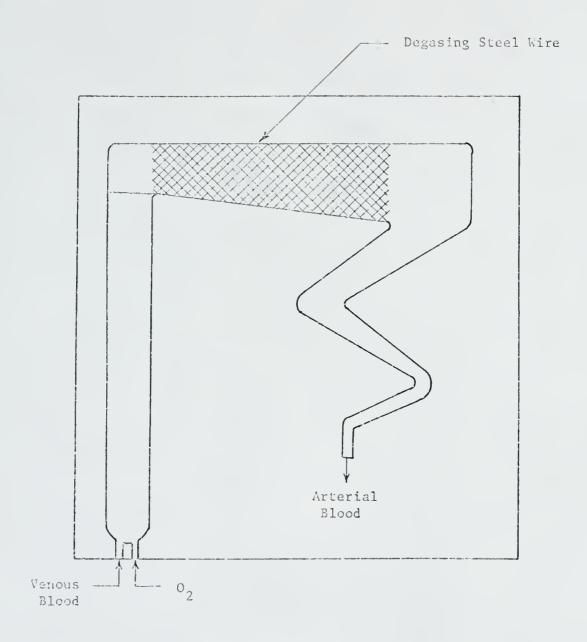


Figure 1.4-1. The Bubble Oxygenator.

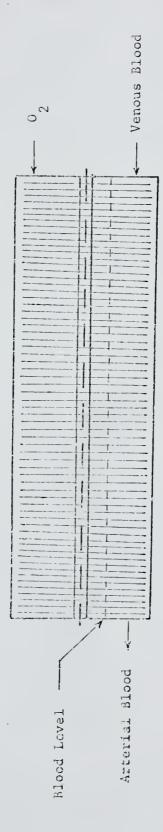


Figure 1.4-2. The Disc Oxygenator.

che-third the diameter of the cylinders. As the blood flows through the chamber, a portion of it is picked up on the rotating discs as thin films. As the film is carried around by the rotating disc, oxygen is absorbed from the surrounding atmosphere, and carbon dioxide is released. It can be shown that blood flow between each of the discs is turbulent when the equipment is operated at the conditions normal for surgery.

The diffusion layer which limits gas transfer, in this case, is the thin blood film on the surface of the discs. This surface is renewed once every revolution by blood in which the discs are partially submerged.

The main advantage of the disc oxygenator is that turbulence is restricted to the spaces between rotating discs. This minimizes hemolysis due to mechanical breakage of blood cells via turbulence. The major disadvantages of this oxygenator are as follows:

- equipment and required resterilization procedures are expensive;
- 2. a large blood priming volume is required.

The screen oxygenator has evolved from a set of concentric cylinders to an arrangement of parallel screens. Blood is pumped to a fixture at the top of the screens where it is distributed. It then flows down both sides of each screen contacting oxygen. The thin film provides efficient gas transfer, particularly if the blood flow is turbulent.

The major advantage of the screen exygenator is that small scale turbulence minimizes hemolysis. The major disadvantages are

large holdup volumes and intermittent channelling blood flow which causes variations in oxygen and carbon dioxide transfer.

These three direct contact oxygenators have two limitations which restrict their operating time as we have stated previously. Hemolysis, or release of hemoglobin from the red blood cell into the plasma, occurs in cardiac bypass using any of the three oxygenators now in clinical use. There are two ways in which hemoglobin release can occur. If red blood cells are placed in distilled water, they swell, loosing their discoid shape, and become spherical. The cell membrane expands until it ruptures, releasing hemoglobin into the surrounding distilled water. The driving force for cell expansion is osmotic pressure, which is caused by the impermeability of the cell membrane to various electrolytes and proteins.

The other cause of hemolysis is mechanical breakage. This type of hemolysis is generally due to turbulent flow and mechanical pumping. It appears that since turbulence in pumps is severe, this particular problem will be overcome largely by better pump designs.

The problem of protein denaturation is also common to all clinically used direct contact oxygenators. Protein denaturation is the alteration of the molecular structure of the protein molecule which leads to changes in the properties of the molecules. The most likely explanation for the denaturation caused by exposure of blood to direct contact with oxygen is the influence of interfacial forces on the protein molecules and the subsequent reaction of these molecules with oxygen (42). The protein molecule is a surface active agent owing to the fact that parts of its molecular chain are hydrophobic and other

parts are hydrophilic. In solution, the hydrophobic sections tend to align themselves in the interior of a molecular coil while the hydrophilic sections tend to lie exposed to the water. At an interface, the protein molecule tends to unfold or unravel so that the hydrophobic sections orient themselves toward the gas phase, and the hydrophilic sections orient themselves toward the liquid phase. This orientation exposes protein bends to attack by the gaseous oxygen and thus alters the protein structure.

The membrane and fluorocarbon oxygenators are supposed to minimize this problem by eliminating the blood-gas interface.

Although there are a number of feasible designs for both types of oxygenators, none have been put into clinical use to our knowledge. The experimental designs all conform to the thin film model. In the case of the membrane oxygenator, it appears that the most successful models have employed small diameter tubes or flow channels surrounded by flowing oxygen. The tube diameter or cross-sectional area of the flow channel must be minimized since near the membrane wall gas transport is diffusion-controlled in a stagnant layer of blood. Also of importance is resistance to gas transport in the membrane. † In

Bradley (17) has presented a discussion on the effect of silicone membrane thickness and has shown that resistance to ${\rm CO}_2$ transport through the membrane becomes the rate-limiting step as wall thickness is increased. The opposite is true in direct contact expensions in which exygen transport is the limiting rate process.

along with a simple example to illustrate resistance to transfer in series.

The major drawback to membrane oxygenators is that the transport of gases through the membrane and stagnant blood boundary layer is diffusion-controlled; hence a large priming volume is required to generate the surface area needed for adequate oxygenation and decarbonation. Attempts to increase efficiency by reducing the diameter of the tubes must be balanced against increased pumping and resultant hemolysis. Further increases in efficiency of gas transport by reducing membrane thickness are also limited by structural requirements.

The fluorocarbon oxygenator has promise as a long term artificial blood-gas exchanger. As stated earlier, current experimental designs are limited to the thin film types. Other, more efficient, methods of contacting oxygen-saturated fluorocarbon and venous blood are available, and these should be tested. The principal drawback of these possible methods, including the thin film process, is that there is some indication that a blood fluorocarbon emulsion forms which is difficult to break. Since more than trace amounts of fluorocarbon in the blood can cause embolisms (15), any such emulsion must be scrupulously removed.

1.5 The Lung as an Oxygenator

The lung, of course, is an exygenator supplying oxygen to the blood and removing carbon dioxide from the same. The respiratory system consists of the trachea (air intake and exist), and the right and left bronchi. Each bronchus branches in tree-like fashion into

20 to 23 subdivisions, or about 10⁶ terminal tubes. At the end of each tube are terminal sacks called alveoli of which there are approximately 3 x 10⁸ in the entire lung. It is in the alveoli, which range from 20 to 30 microns in diameter, that gas exchange with blood occurs. Each of the alveoli are surrounded by thin-walled capillary beds through which blood passes. The diameter of these capillaries ranges from 7 to 10 microns and the wall thickness is less than 0.1 micron.

The amount of gas the lung can transport is extremely large, ranging up to approximately 5.5 l/min of oxygen during heavy exercise. In normal breathing, air is pumped in and out of the lungs by movement of the diaphragm, which movement causes high and low pressures in the thorax resulting in alternate contractions and expansions of the alveoli.

The transport of gases from the alveoli to the blood is accomplished by diffusion through the alveolar membranes, which are less than 0.1 micron thick, and the capillary walls. Under normal conditions, the volume of air inhaled and exhaled in one breath is approximately 450 ml in a healthy adult. This volume is known as the tidal volume. Upon normal expiration, the lungs still retain about 2.4 a of gas. This volume is termed the expiratory reserve capacity and residual volume. The volume of the conducting airways leading to the alveoli is approximately 150 ml; this is called dead space

All dimenions, data and physical constants reported in this section were taken from Comroe (43).

since these airways do not participate to any significant extent in gas exchange.

The mode of oxygen transport in the lung to the membrane wall is by convective mixing. Comroe (43) implies that air passes through the lung airways in plug flow and then perfectly mixes with the alveolar gases. Seagrave (44), in a model of the entire respiratory system, describes the entire lung as a perfectly mixed stage, thus neglecting plug flow in the dead space region.

Our interest in the lung is mainly in a liquid-breathing application. While studying blood oxygenation by artificial means, we became aware of attempts to oxygenate blood adequately with the natural lungs but employing oxygen-saturated liquids instead of air as an exchange medium. In liquid breathing, the lungs are filled with an oxygen-saturated liquid, and breathing is accomplished by pumping fresh liquid into and out of the lungs periodically. There are a number of clinical uses to which such a technique could be applied, the most important of which appears to be the treatment of hypoxemia, specifically in cystic fibrosis.

The earliest experiments involving liquid breathing were performed using normal saline or Ringer's solution saturated with oxygen. West and co-workers (45) filled canine Jungs with degassed normal saline. After breathing the dogs a sufficient number of times to ensure removal of all gas, a step-change in the concentration of a tracer gas was introduced into the lung. One more inspiration was permitted before breathing was terminated to force some of the tracer into the lung. The expanded lung was then held fixed for various periods of time before it was drained and the concentration of the tracer was measured as a function of volume drained. From these

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concentration profiles, West concluded that oxygen is transported through liquid-filled lungs by diffusion.

Kylstra (46) performed steady-state liquid breathing experiments using oxygenated Ringer's solution, saturated at a partial pressure of oxygen of 3000 mm. In Kylstra's experiments, canine lungs were filled with oxygen-saturated Ringer's solution and breathed until steady-state conditions were obtained. Concentration profiles of 0_2 and 0_2 were then measured as a function of lung volume by draining the lung. Kylstra fitted these data to a spherical diffusion model assuming the core of the sphere to be fed by liquid at the entrance composition. He assumed that the flow of liquid through the airways was in plug flow. To provide a reasonable agreement between theory and experimental results, Kylstra adjusted the size and number of hypothetical diffusion spheres and noted that the diameter of spheres thus obtained compared favorably within size with the primary lobules of the lung.

More recently Modell and co-workers (47,48,49) and Lowenstein and co-workers (50) have used fluorocarbon (FX80 and P1D) to ventilate dogs. The major advantage of fluorocarbon is that its extremely high exygen solubility facilitates the exygenation of blood at atmospheric pressure.

The description of gas transport through the lung by diffusion alone appears to be quite unsatisfactory and we shall show that diffusion capnot account for the amounts of oxygen and carbon diexide transferred in liquid-filled lungs. Turthermore we shall develop an

A similar diffusion model has been proposed for gas-filled lungs by LaForce (51), and supporting data have been quoted by Kylstra (46). The assumption of diffusion-controlled transport in gas-filled lungs is further from reality than in the case of liquid-filled lungs and arguments for a more realistic model are presented in Appendix C.

alternate model, based upon imperfect mixing theory, which we believe will describe the functioning of the lung more accurately than models proposed previously.

CHAPTER 2

SIMULATION OF THE BUBBLE OXYGENATOR

2.1 Mathematical Models

open-heart surgery, we concluded that both blood and gas were in turbulent flow in the oxygenation chamber. We were also able to ascertain that oxygen gas bubbles passed through the chamber in essentially plug flow. The blood flow patterns, however, could not be determined precisely; thus a saline simulation experiment was devised to investigate liquid flow patterns in the oxygenation chamber. It was decided to simulate blood with a normal saline solution to which was added a small amount of carboxy-methyl-cellulose (C.M.C.) to increase the viscosity of saline to that of whole blood. Since oxygen does not react or physically bind with saline, it was felt that the flow characteristics of blood could be obtained by measuring the rate of absorption of oxygen into saline, i.e., fluid mechanical effects would effectivel; be separated from chemical kinetic effects.

In such an absorption process, occurring in a turbulent flow channel, there are two limiting cases which are of physical significance. The first case is plug flow of a liquid through the column. In such a column, liquid and oxygen, entering the bottom and flowing cocurrently, would pass through the oxygenating chamber in a slug, and any mixing

As we discovered in the simulation, this is not always the case when the oxygenator is operated incorrectly.

which occurred in the liquid phase would be local. In such a situation, a mass balance across a slug of infinitesimal volume V would predict the rate of mass transfer as

$$\frac{d(VC_{O_{2}})}{dt} = -KA(C_{O_{2}} - C_{O_{2}})$$
 (2.1-1)

where C_{0_2} = concentration of the oxygen in the saline solution $C_{0_2}^*$ = concentration of oxygen at the gas-liquid interface

K = mass transfer coefficient

 $A = 0_2$ bubble-saline interfacial area

V = volume of the slug.

If we further assume that the liquid density is constant and that the range of absorption is small compared to the flow rate of gas,

Equation 2.1-1 becomes

$$\frac{d(C_{O_2} - C_{O_2}^*)}{dt} = -\frac{KA}{V}(C_{O_2} - C_{O_2}^*)$$
 (2.1-2)

Upon integration of this equation, we obtain

$$(C_{0_2} - C_{0_2}^*) = (C_{0_2}^I - C_{0_2}^*) \exp\left(-\frac{KA}{V}t\right)$$
 (2.1-3)

where the initial condition

$$C_{0_2}(0) = C_{0_2}^{I}$$

has been used. Equation 2.1-3 can be written in reduced form as

$$x = \exp\left(-\frac{KA}{V}t\right)$$
 (2.1-4)

where

$$x = \frac{c_{0_2} - c_{0_2}^*}{c_{0_2}^1 - c_{0_2}^*}$$

Now, t is the residence time of a slug of liquid, i.e., the time that a slug or element of fluid remains in the oxygenation column, and since these elements are in plug flow, the residence time of any element of fluid is equal to the average residence time of the liquid, τ , or

$$\tau = \frac{V}{\dot{V}}$$

where \dot{V} is the volume flow rate of saline. Thus the final form of Equation 2.1-3 is

$$x = \exp - \left(\frac{KA}{v}\right) \tag{2.1-5}$$

The other limiting case is a single perfectly mixed stage. In this model, an element of fluid entering the bottom of the oxygenator is immediately distributed throughout the oxygenation chamber. Thus, all of the liquid in the column is at the exit composition \mathbf{C}_0 . Of course, the instantaneous mixing of entering liquid is a hypothetical case which cannot be physically realized; if, however, the time required for distribution of liquid is small compared to the average residence time, the above assumption predicts accurately the physical behavior of the system. A mass balance across the oxygenator in this case yields

$$\dot{\mathbf{v}}(\mathbf{C}_{0_{2}} - \mathbf{C}_{0_{2}}^{\mathbf{I}}) = \mathbf{A}\mathbf{K}(\mathbf{C}_{0_{2}} - \mathbf{C}_{0_{2}}^{*})$$
 (2.1-6)

or following analogous steps to those taken in the plug flow case

$$x = \frac{1}{1 + \frac{AK}{\dot{V}}} \tag{2.1-7}$$

We had originally expected that mixing in the oxygenator would lie between these two extremes and that the best mathematical model for the system would be n perfectly mixed stages in series for which it can be shown by extension of Equation 2.1-6 that

$$x = \left(\frac{1}{1 + \frac{AK}{nV}}\right)^{n} = \left(\frac{1}{1 + \frac{A}{V}K\tau}\right)^{n}$$
 (2.1-8)

Although the results of our experiments indicated that 1 perfectly mixed stage described the system accurately, we have included a comparison of our results with n=2 for illustrative purposes.

There is an alternate derivation of Equation 2.1-7 which parallels Kramer and Westerterp's (52) analysis of a 1st order chemical reaction carried out in a continuously stirred tank reactor (CSTR). In this development, it is noted the rate of change in concentration of an element of fluid which remains in the oxygenator for a given length of time, τ , is given by Equation 2.1-2 and the concentration of this element is given by

$$x = \exp\left[-\frac{KA}{V}\tau\right] \tag{2.1-9}$$

Now, the elements which constitute the liquid in the oxygenation column

remain in the column for different periods of time. The probability of an element remaining in the column for a given time, τ , is given by the residence time distribution function which, for a CSTR, can be calculated as follows: Since an element of fluid entering the chamber mixes perfectly with the bulk liquid, its current position is independent of its previous history. Consequently, the probability of it remaining in the column longer than a specified time $\tau \div \Delta \tau$, is the product of the probability of the element remaining longer than time τ and the probability of the element remaining longer than $\Delta \tau$. If $F(\tau)$ is the volume fraction in the outlet stream having a residence time less than τ , then this probability is given by

$$1 - F(\tau + \Delta \tau) = [1 - F(\tau)][1 - F(\Delta \tau)]$$
 (2.1-10)

Now, since element position is independent of past history, all elements have an equal chance of leaving the column in the time period $\Delta \tau$, namely,

$$F(\Delta \tau) = \frac{\dot{V}}{V} \Delta \tau = \frac{\Delta \tau}{t}$$
 (2.1-11)

Substituting this equation into Equation 2.1-10 gives

$$\frac{dF(\tau)}{d\tau} + \frac{1}{t} F(\tau) = \frac{1}{t}$$
 (2.1-12)

Recognizing that at τ = 0, no fluid element has left the oxygenator, i.e.,

$$F(0) = 0 (2.1-13)$$

Equation 2.1-12 becomes, upon integration,

$$F(\tau) = 1 - \exp[-\tau/t]$$

Furthermore, since the change in the bulk concentration between the entrance and exit of the oxygenation chamber is simply the volume average of the various elements, the bulk concentration is

$$x = \int_{\tau=0}^{\tau=\infty} \exp\left(-\frac{KA}{V}\tau\right) \cdot dF(\tau)$$

or

$$x = \int_{\tau=0}^{\tau=\infty} \exp\left(-\frac{KA}{V}\tau\right) \cdot \frac{1}{t} \exp[-\tau/t] d\tau \qquad (2.1-14)$$

Upon integration of Equation 2.1-12, one obtains the result

$$x = \frac{1}{1 + \frac{KA}{V} t}$$
 (2.1-15)

which is identical to Equation 2.1-7. This second derivation reveals more about the physical phenomenon of ideal mixing than the first development since it not only predicts bulk exit concentration but also the residence time distribution function.

A graphical comparison in Figures 2.1-1 and 2.1-2, shows the differences between the three cases under condition. It can be seen easily from Figure 2.1-1 that, for a given residence time, the greater the number of mixing stages, the smaller the value of x, i.e., oxygenation is more efficiently accomplished by a larger number of mixing stages. The second salient feature that should be noted is that as a approaches infinity the resulting x curve approaches the plug flow curve.

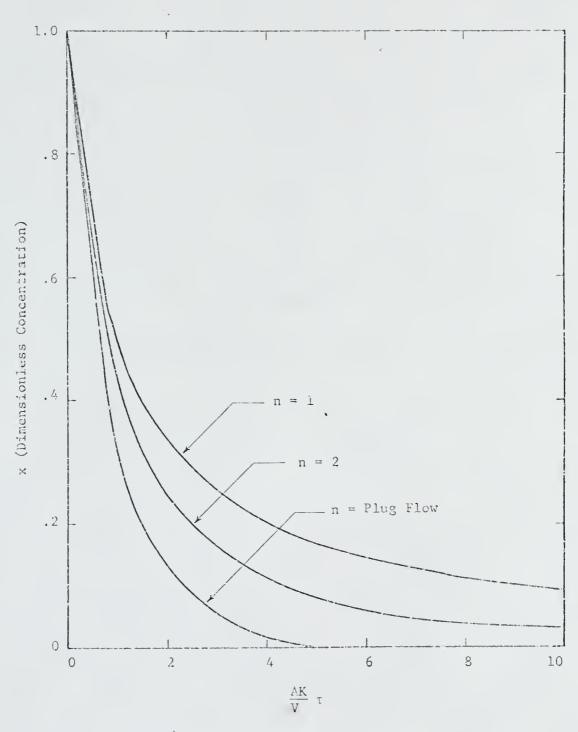


Figure 2.1-1. Comparison of Concentration Profiles as a Function of Number of Stages in Series.

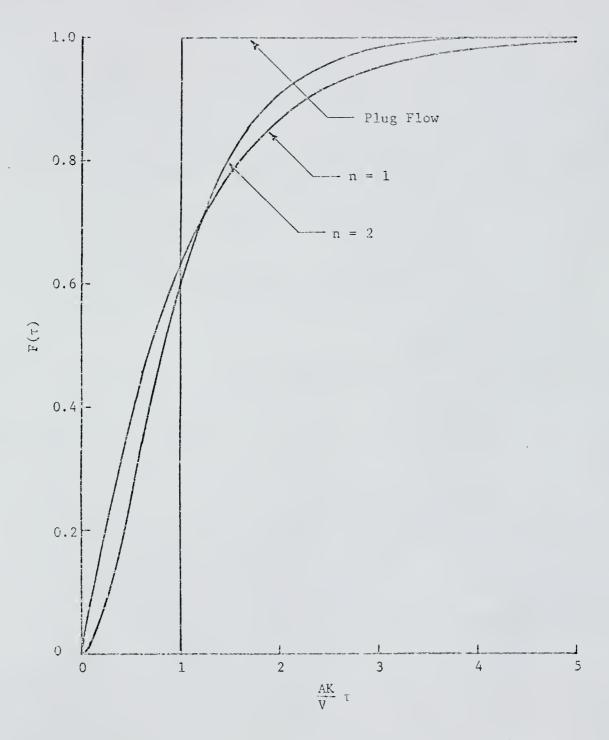


Figure 2.1-2. Comparison of Residence Time Distribution Functions for Varying Number of Stages in Series.

2.? Experimental Equipment and Procedure

The simulation experiments performed were designed primarily to determine the extent of mixing which occurred in the oxygenator; secondly, they were designed to yield data from which the mass transfer coefficient of oxygen in normal saline could be calculated. It was anticipated that this mass transfer coefficient would be a good estimate of the mass transfer coefficient of oxygen in blood plasma.

To accomplish these experimental goals two experiments were attempted. The first experiment was concerned with measurement of the size of bubbles ejected from the sparger. The second experiment was designed to ascertain which flow model best described the physical behavior of the system, and to determine an O_2 -saline mass transfer coefficient.

In both experiments, normal saline, with small additions of CMC, was used to simulate whole blood. The solutions were prepared as follows: To each liter of distilled water 9 gms of commercial grade sodium chloride and 2.23 gms of DuPont sodium CMC (2 WxH grade) were added and dissolved. This amount of CMC increased the viscosity of the saline to that of whole blood as is shown in Figure 2.2-1. The values shown were obtained by measuring the viscosity of test samples of saline with varying amounts of CMC. All measurements were made with a Brookfield variable speed viscosimeter at a temperature of 23°C.

The experimental apparatus, shown in Figure 2.2-2, used to measure bubble diameters consisted of a 2-liter Miniprime Disposable oxygenator (Travenol Laboratories, Inc.), a high pressure air source,

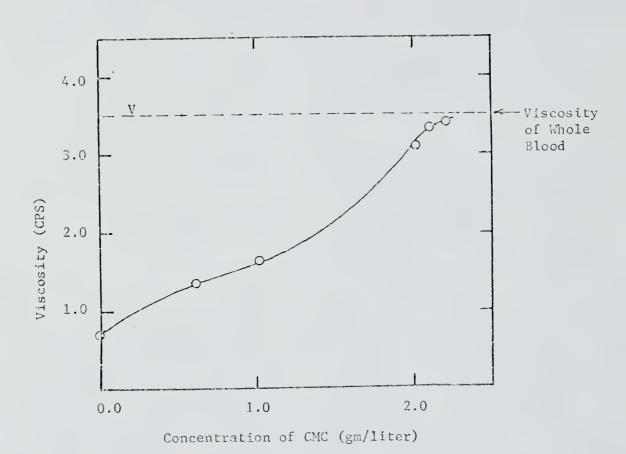


Figure 2.2-1. Viscosity of Saline-CMC Solution As a Function of Composition.

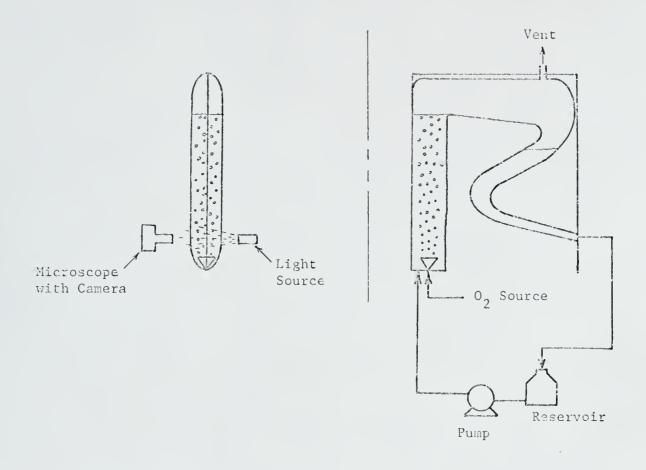


Figure 2.2-2. Experimental Apparatus Used to Measure Bubble Diameters.

a 12-liter capacity saline reservoir, and a multiple finger variable drive pump. Accessories included calibrated gas and liquid flow meters, a pressure-reducing valve, and a thermocouple. Photographs of rising bubbles were taken using a Unitron Series N Metallograph with Polaroid camera attachment and auxiliary light source. The magnification was set at 5X. As it was found that the saline solution corroded metallic surfaces, Tygon tubing connected by glass and plastic joints was used exclusively.

The experimental procedure used to measure bubble diameters was as follows:

- 1. Saline was pumped through the oxygenator at a flow rate of 1.4 ℓ/\min .
- Air flow through the oxygenator was regulated at 5.9 l/min.
- 3. Three sets of photographs were taken of rising bubbles at 10, 17, and 30 cm above the sparger entrance. The camera was focused as closely as possible on the center of the oxygenation chamber to minimize the distortion of the rounded surface. Measurements were taken at 23°C (room temperature) and 1 atmosphere pressure.

The experimental apparatus used to determine the mixing model and to measure θ_2 -saline mass transfer coefficient is shown in Figure 2.2-3. It consisted of two Miniprime oxygenators in series, three rumps, high pressure oxygen and nitrogen sources, plus all the accessory equipment used in the bubble measurement experiment with the exception of the microscope and camera. The first oxygenator was used

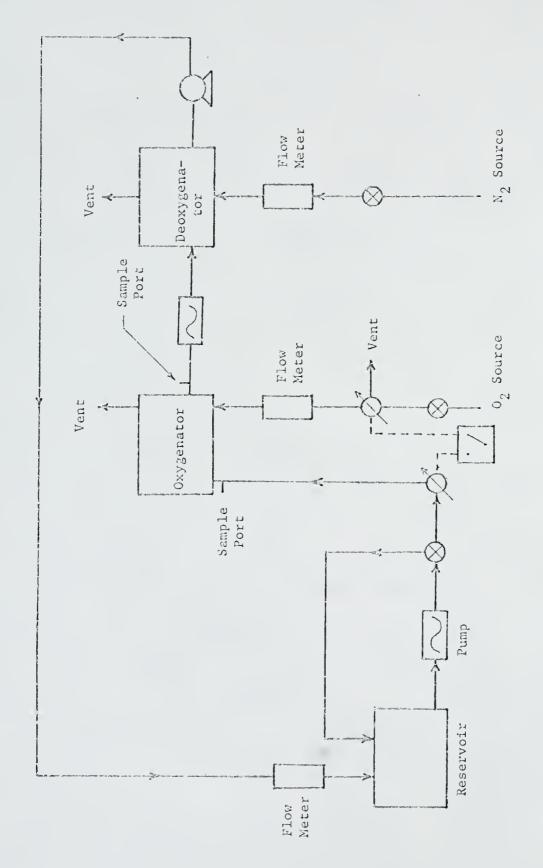


Figure 2.2-3. Blood Simulation Experiment Apparatus.

to saturate the saline solution with oxygen, and the second was used as an oxygen stripper. A bypass was installed between the saline reservoir and the first oxygenator to vary liquid flow through the system. Two solenoid valves were also installed between the high pressure oxygen source and the sparger entrance, and between the saline reservoir and the oxygenator entrance. These solenoids were used to stop simultaneously the flow of oxygen and saline for the purpose of measuring holdup volumes. Sampling ports were installed at the entrance and exit of the first oxygenator in order to measure the change in oxygen content across the oxygenation chamber. A drain was also provided at the bottom of the oxygenation chamber to facilitate the measurement of holdup volumes.

A galvanic cell oxygen analyzer was used to measure oxygen concentration of liquid samples. As the name implies the analyzer is a galvanic cell with a lead anode and a silver cathode. An aqueous KOH solution is used as an electrolyte and together with anode and cathode it is enclosed by a polyethylene membrane which is permeable to oxygen.

The experimental procedure for testing each of the four oxygenators (1-, 2-, 3- and 6-liter capacity units) was as follows:

- 1. Oxygen flow rate was adjusted to 3 %/min.
- 2. Saline flow rate was adjusted to a predetermined value.
- 3. Oxygen flow rate was adjusted to predetermined value.
- 4. Nitrogen flow rate was set at a value not less than 7.0 1/min.

- 5. After waiting 10 minutes to allow the system to come to steady state, a 50 ml sample was drawn from the entrance to the oxygenator and analyzed for oxygen concentration.
- 6. 50 ml samples were then taken and analyzed until two successive oxygen readings were recorded which varied less than 0.6% of the full scale.
- 7. 50 ml samples were then taken from the oxygenator exit and analyzed until two successive oxygen readings were recorded which varied less than 0.6% of the full scale.
- 8. The temperature of the saline in the oxygenator was recorded immediately after each 50 ml sample was drawn.

The oxygen analyzer was calibrated at the beginning of each day in saline solution saturated with air. The analyzer was also recalibrated at the end of each day for a period of two to three days after the probe membrane had been changed and electrodes cleaned.

2.3 Experimental Results--Bubble Diameter Measurements

The results of the bubble measurement experiment are shown in Figures 2.3-1 and 2.3-2. Actual data are given in Appendix D. From the photographs taken, it was determined that the rising bubbles were not perfect spheres but tended to be ellipsoidal in shape. Consequently, the formulas used to calculate the surface area and volume of each bubble were, respectively,

$$S = 2\pi \left(b^2 + \frac{ab}{\epsilon} \sin^{-1} \epsilon \right)$$

$$V = \frac{4}{3} \pi a b^2$$

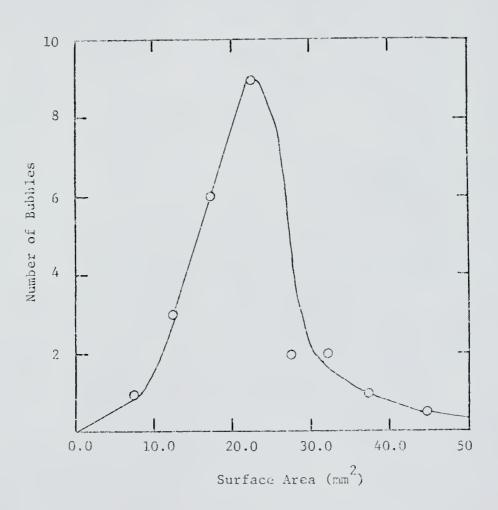


Figure 2.3-1. Distribution of Bubble Sizes by Surface Area.

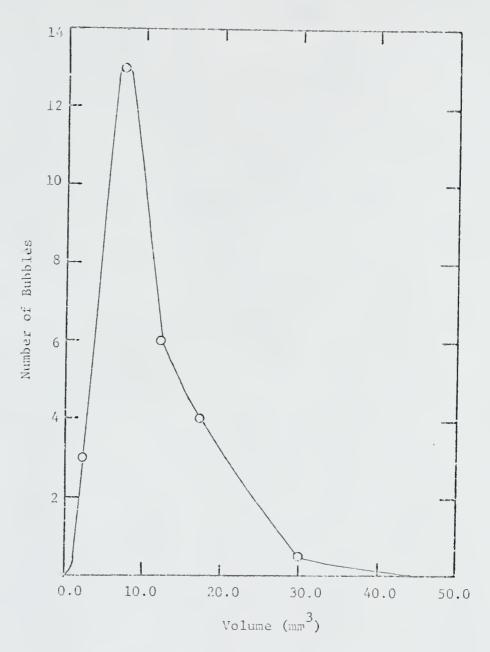


Figure 2.3-2. Distribution of Bubble Sizes by Volume.

where a = major radius

b = minor radius

 ε = eccentricity

As can be seen, both distribution curves for volume and surface area are skew symmetric. Graphical integration of the distribution curve for volume gives an average bubble volume of 1.3.69 mm and an apparent average spherical diameter of 2.97 mm. Graphical integration of the surface area distribution function gives an average bubble surface area of 26.9 mm² and an apparent average spherical diameter of 2.93 mm. Since the apparent spherical diameters calculated from the average volume and average surface area were virtually identical, it was assumed that the effective spherical diameter of the bubbles was the average of these two values, i.e., 2.95 mm, in all following calculations involving blood and saline. Analysis of photographs of bubbles taken at various heights in the oxygenation chamber indicated little change in bubble size throughout the column. There appeared to be a slight increase in the average diameter of approximately 10% from the bottom to the top of the column, but data points were too few, pasticularly at the top of the column, to definitely confirm this trend. Furthermore a calculation of maximum hydrostatic pressure drop across the oxygenation columns of all four Miniprime oxygenator models predicts a maximum gas volume change of 7%. During normal operation of the oxygenators even this small change will not be obtained since a fraction of the oxygenation chamber volume is occupied by gas thus reducing the hydrostatic head. Finally, it is the total surface of the bubbles in the exygenator that is important;

including bubble variation as a function of position in the calculation of the average diameter, as has been done, should give a valid estimate of the surface area for mass transfer coefficient estimation.

A more serious source of error could arise from the assumption that the bubble diameter is independent of change in gas and liquid flow rate. The most concrete evidence to support this assumption is that the term KA was found to be directly proportional to the gas hold-up volume in the experiments performed to measure the mass transfer coefficient. If the average bubble diameter varied, this would not have been the case.

An attempt was made to correlate bubble diameter data with the single-bubble regime model summarized by Perry (53) which predicts

$$D_{B} = \left(\frac{6D\sigma}{g\rho_{I}}\right)^{1/2} \tag{2.3-1}$$

where D_{p} = bubble diameter

D = orifice diameter

c = gas-liquid interfacial surface tension

 $\rho_{\tau} = \text{liquid density.}$

The average bubble diameter size, using Equation 2.3-1, was calculated to be 7.64 mm which is about twice as large as the estimated value.

The experimentally obtained average diameter was also compared with the empirical correlation

$$D_{B} = 0.18 D^{0.5} N_{Rc}^{0.33}$$
 (2.3-2)

which was developed by Leibson and co-workers (54). Equation 2.3-2

predicts the average bubble diameter to be 0.310 mm or an order of magnitude too small.

The range of Reynolds numbers for which Equation 2.3-2 is valid covers flow rates above the single bubble range to Reynolds numbers below 2000, and this region is known as the transition region. There is no clear division between the single bubble region and the transition region, but the low gas Reynolds numbers at which the exygenator is operated,

$$N_{Re} = 30$$
 to $N_{Re} = 80$

probably lie in the region in which surface tension effects are important. In such a region, the variation of bubble diameter with respect to $N_{\rm Re}$, and thus with flow rate, would be a secondary effect, no effect at all according to Equation 2.3-1.

2.4 Experimental Results--Oxygenator Simulation

Representative results of the oxygenator simulation experiments are shown in Figure 2.4-1 and a complete data listing is given in Appendix D. The variables plotted are % oxygenation, or 1-x, versus a reduced residence time

$$\tau = \frac{V}{V} \epsilon \tag{2.4-1}$$

The variable $V_{\rm g}$, the holdup volume of oxygen, was chosen since it was assumed that average bubble diameter was independent of flow rates. Thus $V_{\rm g}$ is related to the interfacial surface area A by the proportionality

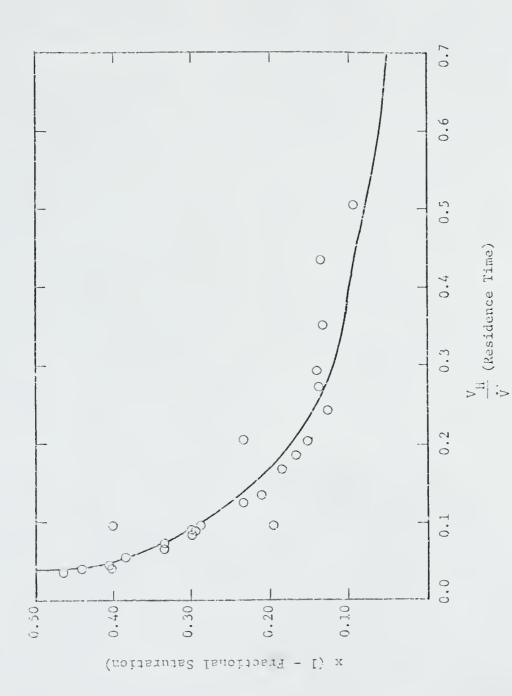


Figure 2.4-1. Experimental Results of the Saline Simulation Experiment.

$$A = V_g \frac{6}{D_g}$$

A least squares fit of the data to a 1 CSTR, 2 CSTR, and plug flow model was performed. The linear method outlined by Mickley, Sherwood, and Reed (55) was used by rewriting Equations 2.1-5, 2.1-7, and 2.1-8 as

$$Y = \frac{1}{x} = 1 + \left(K \frac{Vg}{V} \cdot \frac{6}{D_B} \right) t$$
 (2.4-2)

$$Y = \left(\frac{1}{x}\right)^{1/2} = 1 + \left(K \frac{Vg}{V} \cdot \frac{6}{D_B}\right)t \tag{2.4-3}$$

$$Y = \ln_{x} = -\left(K \frac{Vg}{V} \cdot \frac{6}{D_B}\right) t \qquad (2.4-4)$$

The results of these operations are summarized in Table 2.4-1.

As can be seen, the standard deviations for the 2 CSTR and plug flow models are almost twice as large as for the 1 CSTR model.

Furthermore, although an F-test indicates nonrandom errors in all three analyses, a qualitative inspection of the data suggests that the nonrandom error is greater for the 2 CSTR and plug flow models than for the 1 CSTR model. It was concluded, therefore, that the oxygenator could be approximated by a 1 CSTR model for all four sizes of oxygenators.

There appears to be some discrepancy between the model and the data for smallest size bag, the 1-liter capacity oxygenator. The data suggest that the oxygenation of saline was less than would be obtained if the system were perfectly mixed. Since both the sparger

TABLE 2.4-1

COMPARISON OF PROPOSED MODELS WITH EXPERIMENTAL RESULTS

Mode1	$K\left(\frac{cm}{sec}\right)$	$\frac{\frac{6K}{D_B} (sec^{-1})}{\frac{1}{2}}$	Standard Deviation
1 CSTR	2.29×10^{-2}	4.65×10^{-1}	4.7% (5.4%°)
2 CSTR	4.53×10^{-3}	9.22×10^{-2}	8.5%
Plug Flow	8.51×10^{-3}	1.73×10^{-1}	8.5%

Data from the 1-liter capacity oxygenator were deleted from final estimation of K. The value in brackets indicates the standard deviation with these data omitted.

and chamber for the 1- and 2-liter bags are the same geometrically and, in fact, identical dimensionally, we cannot attribute this phenomenon to scale up factors, i.e., change in mass transfer coefficient or bubble diameter. It was noted in later experiments, that any tilting of the oxygenation chamber caused channelling flow in certain portions of the oxygenator while in other regions, stagnation and back mixing occurred. Accompanying this type of unstable flow was a marked reduction in oxygenation of saline.

as a function of gas flow rate divided by liquid flow rate for each size oxygenator. These reduced data for each case were then fitted to 10th degree polynomials which were subsequently written in the form of a computer subroutine to be used in blood data analysis. These results are shown graphically in Figures 2.4-2, 2.4-3, 2.4-4, and 2.4-5. The final values of the mass transfer coefficients, obtained by the method of Gauss elimination (56) applied to a least squares fit, are tabulated in Table 2.4-2. The experimental data are also listed in Appendix D. The relatively constant value of gas holdup volumes at high gas flow races is due to fact that as the volume flow rate increases the velocity of the bubbles increases, and thus, the increase in the number of bubbles generated per unit time is offset by the speed at which the bubbles move.

It was also noted that at very high flow rates, bubbles coalesced into large pockets of gas which rose rapidly through the oxygenation chamber. This effect could also reduce gas holdup volume, and, in addition, reduce the surface area available for mass transfer.

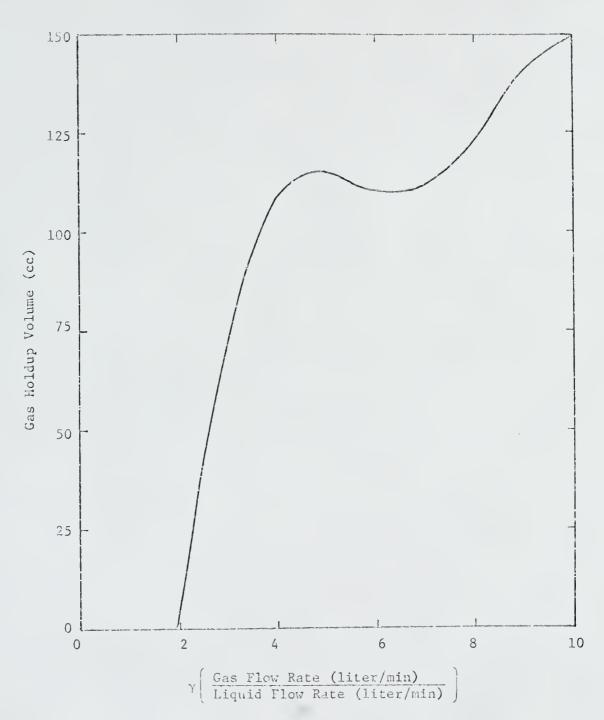


Figure 2.4-2. Gas Holdup Volume as a Function of Gas to Liquid Volume Flow Rate Ratio in the 1LF Bubble Oxygenator.

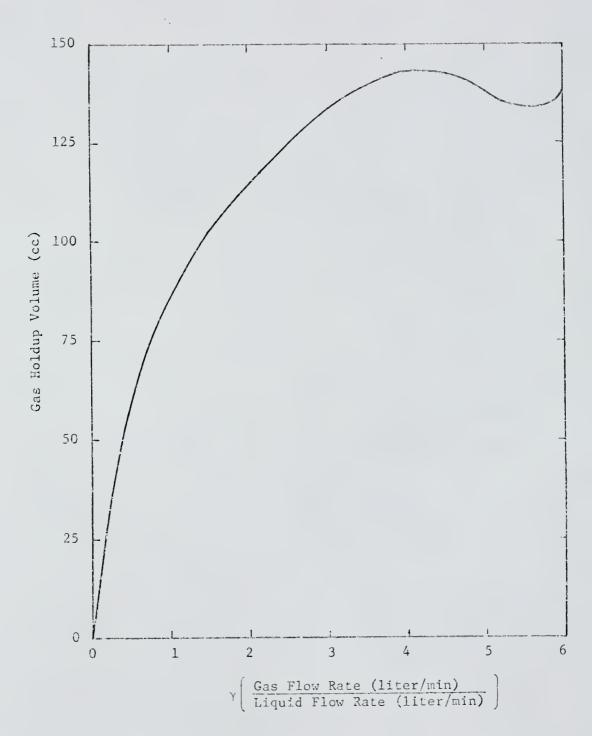


Figure 2.4-3. Gas Holdup Volume as a Function of Gas to Liquid Volume Flow Rate Ratio in the 2LF Bubble Oxygenator.

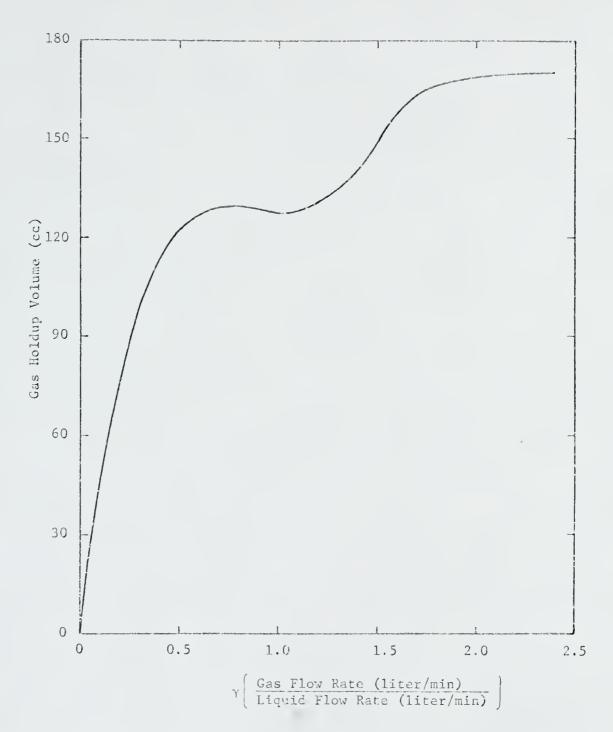


Figure 2.4-4. Gas Holldup Volume as a Function of Gas to Liquid Volume Flow Rate Ratio in the 3LF Bubble Oxygenator.

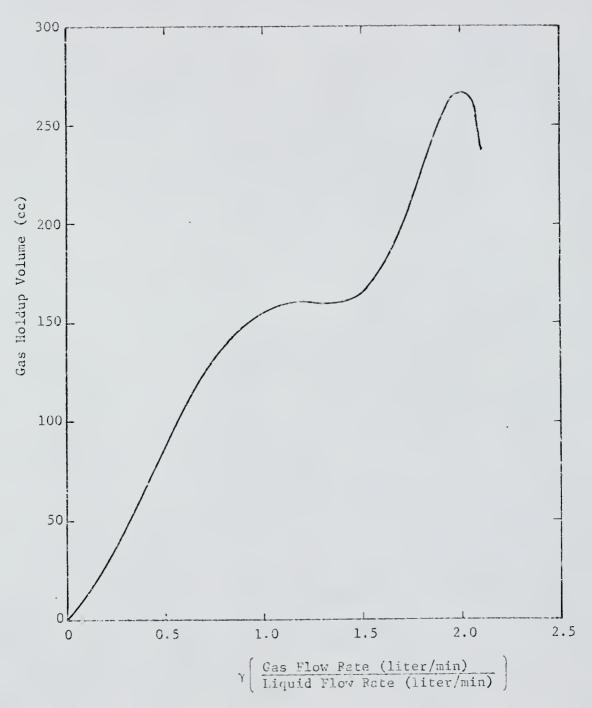


Figure 2.4-5. Gas Holdup Volume as a Function of Gas to Liquid Volume Flow Rate Ratio in the 6LF Bubble Oxygenator.

TABLE 2.4-2

FRACTIONAL GAS HOLDUP VOLUME VS. FUNCTION OF \boldsymbol{o}_2 AND BLOCD FLOW RATES

Fractional Hoidup Volume =	+ ೮ [–]	$c_2 \gamma + c_3 \gamma^2 + c_4 \gamma^3 + c_5 \gamma^4 + c_6 \gamma^5 + c_7 \gamma^6 + c_8 \gamma^7 + c_9 \gamma^8 + c_{10} \gamma^9 + c_{11} \gamma^{10}$	$_{6}^{7} + c_{7}^{7} + c_{8}^{7} + c_{5}^{2}$	$^{8}_{9}$ + $^{6}_{10}$ + $^{9}_{11}$ + $^{10}_{11}$
Oxygenator Modei	C	c_2	C_3	C.4
	-7.26151×10^{-3}	-4.974657 x 10 ⁻¹	3.99882 x 10 ⁻¹	-8.60446 x 10 ⁻²
	6.654732 × 10 ⁻⁴	4.87973 × 10 ⁻¹	-2.634624 x 10 ⁻¹	9.48690 x 10 ⁻¹
	3.499880 × 10 ⁻⁶	1.208610	-1.101016	6.00549 x 10 ⁻²
	9.73307 × 10 ⁻⁵	1.039137 x 10 ⁻¹	2.391992 x 10 ⁻¹	-8.84271×10^{-2}
	S	Co	C ₇	్రా
	5.78214 × 10 ⁻³	3.69494 x 10 ⁻⁵	1.71899 x 10 ⁻⁵	-4.02937 x 10 ⁻⁶
	1.83593 x 10 ⁻¹	2.28350×10^{-3}	-2.01014 × 10 ⁻⁴	-1.24458 x 10 ⁻⁵
	1.940979 x 10 ⁻¹	2.55293×10^{-2}	9.87895 × 10 ⁻³	-2.09601×10^{-2}
	-1.07494 x 10 ⁻³	-1.458537×10^{-1}	8.21756×10^{-2}	3.34081×10^{-3}

 * * ratio of Ω_2 volume flow rate to blood volume flow rate

TABLE 2.4-2 (Continued)

	0	∞	3	n
C ₁₁	-5.2657×10^{-10}	-8.50442×10^{-8}	1.42629 × 10 ⁻³	-3.82683×10^{-3}
c ₁₀	1.61250 × 10 ⁻⁸	7.96349 × 10 ⁻⁷	-2.68215×10^{-3}	1.04377×10^{-2}
65	2.46891 :: 10-8	1.50754 × 10 ⁻⁶	4.31817 × 10 ⁻⁴	-9.81349×10^{-3}
Orygenator Model	llF	21.F	3LF	CLF

It was found that this phenomenon occurred at a gas flow rate of 7.0 to 8.0 %/min depending on the size of oxygenator used.

The starting point of our analysis of this absorption process was Equation 2.1-6. This equation itself is based upon the more primitive model of diffusion through a thin film or boundary layer. To derive Equation 2.1-6, it is assumed that the process is diffusion-controlled, i.e., the rate is controlled by a diffusion resistance in a thin layer close to the gas-liquid interface; and, furthermore, that the concentration profile across this boundary layer is linear. A schematic representation of this model is shown in Figure 2.4-6.

A mass balance across the diffusion layer gives

$$\frac{d^{2}C_{0_{2}}}{dt} = +AJ_{r} \Big|_{R+\delta}$$

$$\frac{d^{2}C_{0_{2}}}{dt} = -\frac{A}{V}D_{0_{2}} = -\frac{A}{V}D_{0_{$$

or

Suppose that the bulk concentration changes slowly in time in comparison with the rate of change in concentration profile within the boundary layer, then, for any small interval of time, ${\rm C_0}_2$ can be assumed as independent of time and the diffusion of oxygen through the layer can be described by

$$\frac{\partial C}{\partial t} = \frac{1}{r^2} \frac{\partial}{\partial r} \left(\frac{2}{r^2} \frac{\partial c}{\partial r} \right)$$
 (2.4-6)

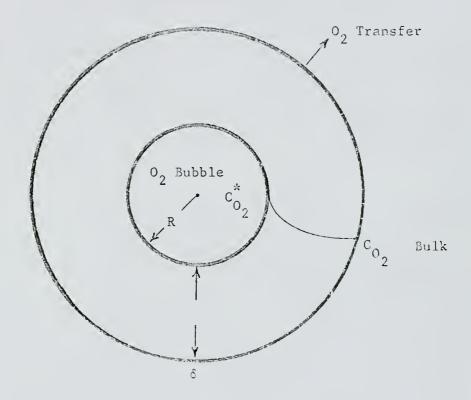


Figure 2.4-6. Thin Film Diffusion Model for Oxygen Absorption.

with the boundary corditions

$$C(0,r) = C_0$$

$$a \le r \le a + \delta$$

$$C(t,a) = C^*$$

$$C(t,\delta) = C_0$$

$$(2.4-7)$$

The solution to this set of equations has been given by Crank (57) as

$$C = \frac{aC^{*}}{r} + \frac{[(a + \delta)C_{0} - aC^{*}](r - a)}{r\delta} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=1}^{\infty} \frac{(a+\delta)(C_{0} - C^{*})\cos n\pi - a(C^{*} - C_{0})}{n} + \frac{2}{r\pi} \sum_{n=$$

For values of δ approaching zero all of the terms in the right-hand size of Equation 2.4-8 except the first two approach zero. Differentiating these remaining terms gives

$$\frac{2(C - C^*)}{\delta r} = \frac{-a}{r^2} C^* + \frac{[(a + \delta)C_0 - ac^*]}{\delta} \left(\frac{1}{r} - \frac{r - a}{r^2}\right)$$
 (2.4-9)

Moreover, if δ is much smaller than r,

$$r \approx a$$
 $a \leq c \leq b$

and Equation 2.4-9 can be approximated by

$$\frac{\partial \left(C - C^{*}\right)}{\partial r} = \frac{C_{0} - C^{*}}{\delta} \tag{2.4-10}$$

It should thus be noted that the assumption of a small boundary layer thickness, such that

$$\delta << r$$
 and $\delta^2 < D_{0} 2^{\pi^2}$ (2.4-11)

yields the linear concentration profile which we required. Substituting Equation 2.4-10 into Equation 2.4-5 gives

$$\frac{d(C_{0_2} - C_{0_2}^*)}{dt} = -\frac{A}{V} D_{0_2} \frac{(C_{0_2} - C_{0_2}^*)}{\delta}$$
 (2.4-12)

and comparison of this equation with 2.1-6 yields

$$K = \frac{{}^{D}O_{2}}{\delta}$$
 (2.4–13)

Using a value of 2.5×10^{-5} cm²/sec for the diffusivity of oxygen into saline (53), we obtain a boundary layer thickness of 1.1×10^{-3} cm. This boundary layer thickness fits the criterion as stated in Equation 2.4-11 for our proposed assumption quite well as shown in Table 2.4-3.

. TABLE 2.4-3
BOUNDARY LAYER THICKNESS AND PROFILE PARAMETERS

Parameter	Value
S	1.1×10^{-3} cm
$\frac{2\delta}{D_B}$	1.1×10^{-2}
³ / _{π²D} ο ₂	$4.9 \times 10^{-3} \text{ sec}$

CHAPTER 3

OBSERVATIONS DURING OPEN-HEART SURGERY

3.1 Theory of Gas Transfer Through Blood

In Chapter 2, oxygen transfer into saline during operation of the bubble oxygenator was discussed, and it was determined that the oxygenator could be best characterized, in fact, as a perfectly mixed stage. This is also true for blood in the oxygenation chamber, but in this case the oxygen absorption process is more complex owing to the reactions which take place as discussed in Chapter 1, Section 3. This circumstance increases the complexity of the system and invalidates the second derivation presented in Chapter 2 of Equation 2.1-7 except for the case of first order reactions.

Since oxygen and carbon dioxide transport must be accounted for both as dissolved gas and in the chemically bound form, a mass balance including all of these species must be written. In matrix form this mass balance is

$$\dot{V}\{(C) - (C^{I})\} = -A[K]\{(C) - (C^{*})\} + (R)$$
 (3.1-1)

where (C) is the column matrix of chemically distinct species concentrations at the exit of the oxygenator, (C^I) is the column matrix of chemically distinct species concentrations at the oxygenator entrance, (C^X) is the column matrix of chemically distinct species concentrations in equilibrium with the gas phase, and (R) is the column matrix of chemical reaction coefficients. We shall dismiss out of hand all of the off-diagonal elements of the matrix [K] arguing that the solution

is dilute in ${\rm CO}_2$ and ${\rm O}_2$, therefore these gases diffuse into the blood as binary ${\rm O}_2$ -blood and ${\rm CO}_2$ -blood pairs. In these circumstances, Equation 3.1-1 reduces to

$$(C_{0_2} - C_{0_2}^{I}) = -\frac{A}{V} K_{0_2,B} (C_{0_2} - C_{0_2}^*) + \frac{1}{V} R_{0_2}$$
 (3.1-2a)

$$(C_{HbO_2} - C_{HbO_2}^{I}) = -\frac{A}{V} K_{HB,O_2} (C_{HBO_2} - C_{HBO_2}^*) + \frac{1}{V} R_{HBO_2}$$
 (3.1-2b)

$$(C_{CO_2} - C_{CO_2}^{I}) = -\frac{A}{\dot{v}} K_{CO_2, B} (C_{CO_2} - C_{CO_2}^*) + \frac{1}{\dot{v}} R_{HBO_2}$$
 (3.1-2c)

$$(C_{HCO_3} - C_{HCO_3}^{I}) = -\frac{A}{\dot{V}} K_{HCO_3,B} (C_{HCO_3} - C_{HCO_3}^{*}) + \frac{1}{\dot{V}} R_{HBO_2}$$
 (3.1-2d)

$$(C_{\text{HbCO}_2} - C_{\text{HbCO}_2}^{\text{I}}) = -\frac{A}{\dot{v}} K_{\text{HbCO}_2} (C_{\text{HbCO}_2} - C_{\text{HbCO}_2}^{*}) + \frac{1}{\dot{v}} R_{\text{HbCO}_2}$$

$$(3.1-2e)$$

where $C_{\rm HbO}_2$, $C_{\rm HCO}_3$ and $C_{\rm HbCO}_2$ are the concentration of oxygen and carbon dioxide bound to each of these chemical species. Addition of Equations 3.1-2a, 3.1-2b, and 3.1-2c leads to the total oxygen transport

$$(C_{O_{2}} - C_{O_{2}}^{I})_{TOT} = -\frac{\Lambda}{\dot{v}} \Big((K_{O_{2}, B} (C_{O_{2}} - C_{O_{2}}^{*}) + K_{HbO_{2}, B} (C_{HbO_{2}}) + (R_{HbO_{2}} + R_{O_{2}}) + (R_{HbO_{2}} + R_{O_{2}}) \Big)$$
(3.1-3)

We further assume that the system is in local equilibrium, i.e.,

$$R_{HbO_2} = -R_{O_2}$$
 (3.1-4)

and, consequently, the amount of θ_2 bound to hemoglobin can be related

to the concentration (partial pressure) of dissolved unbound oxygen by the equilibrium relationship, Equation 1.3-6. Since the red blood cell has a specific gravity of 1.091 and contains 0.34 weight fraction hemoglobin, the concentration of hemoglobin in whole blood is

$$C_{Hb} = (.34)(1.091) \cdot H$$
 (3.1-5)

where H = hematocrit = volume fraction of red cells in blood.

Furthermore, since each gram of hemoglobin can bind 1.34 standard cc of exygen at saturation, the amount of bound oxygen in the blood is related to the partial pressure of oxygen by

$$C_{\text{HbO}_2} = (.34)(1.091)(1.34) \text{H*S}(\text{PO}_2)$$
 (3.1-6)

Finally, we assume that the transport of oxygen bound to hemoglobin by diffusion is negligible, i.e.,

$$K_{\text{HbO}_2} \approx 0$$
 (3.1-7)

This assumption is based upon the fact that the hemoglobin molecule is quite large; consequently, it diffuses very slowly through the blood (58). Incorporating Equations 3.1-4, 3.1-6 and 3.1-7 into Equation 3.1-5 gives the final results, namely,

$$\frac{(c_{0_{2}}^{2} - c_{0_{2}}^{*})_{TOT}}{(c_{0_{2}}^{1} - c_{0_{2}}^{*})_{TOT}} = \frac{1}{AK_{0_{2},B}} \frac{(P_{0_{2}} - P_{0_{2}}^{*})}{(c_{0_{2}}^{2} - c_{0_{2}}^{*})_{TOT}}$$

$$(3.1-8)$$

where Henry's law has been used to relate the partial pressure of oxygen to the consentration of dissolved gas by

$${}^{C}_{O_{2}} = {}^{\alpha}_{O_{2}} {}^{P}_{O_{2}}$$
 (3.1-9)

 α_{0_2} being the Henry's law constant.

The equations for transport of carbon dioxide through blood are similar to those developed for oxygen. A total mass balance of ${\rm CO}_2$ across the oxygenation chamber gives the result

$$(c_{CO_{2}} - c_{CO_{2}}^{I})_{TOT} = -\frac{A}{\dot{v}} \left((k_{CO_{2}, B} (c_{CO_{2}} - c_{CO_{2}}^{*}) + k_{HbCO_{2}, B} (c_{HbCO_{2}}) + k_{HbCO_{2}, B} (c_{HbCO_{2}, B}) + k_{HbC$$

where it has already been assumed that all reactions are in local equilibrium, i.e.,

$$R_{CO_2} + R_{HCO_3} + R_{HbCO_2} = 0$$
 (3.1-11)

The assumption of negligible transfer by diffusion of hamoglobin-bound CO₂ appears to be valid for the same reason given for HbO₂ diffusion. The problem of bicarbonate ion transfer is not so easily handled. It was the original intent of this work to determine or at least make a fair estimate of the bicarbonate diffusivity, but data taken during open-heart surgery gave differences in inlet and outlet CO₂ concentration amounting to only a few millimeters partial pressure, a quantity far too small to make any but an order of magnitude estimate of the mass-transfer coefficient. Thus, we assumed

$$K_{HCO_3}, B = 0$$
 (3.1-12)

Incorporating this last result into Equation 3.1-10 gives

$$\frac{(c_{CO_{2}} - c_{CO_{2}}^{*})_{TOT}}{(c_{CO_{2}}^{\mathsf{I}} - c_{CO_{2}}^{*})_{TOT}} = \frac{1}{1 + \frac{AK_{CO_{2}, B}^{\alpha}CO_{2}}{\dot{v}} \frac{(P_{CO_{2}} - P_{CO_{2}}^{*})}{(c_{CO_{2}} - c_{CO_{2}}^{*})_{TOT}}}$$
(3.1-13)

which is the same result as obtained in the case of oxygen transfer.

3.2 Experimental Procedure

Sixteen open-heart operations were observed at Shands

Teaching Hospital, the University of Florida, Gainesville, Florida

during the period from June 18, 1970 to October 3, 1970. In each case

normal operating procedures were followed with the exception that

venous as well as arterial blood samples were drawn from the patient.

In all cases the Miniprime Oxygenators produced by Travenol Corporation

with pumps and a heat exchanger were used, and data were obtained for

each size oxygenator as shown in Table 3.2-1.

A schematic diagram of the operational setup, which was the same in all of the operations observed, is shown in Figure 3.2-1. The procedure used in open-heart surgery can be separated into two parts; (1) the preparation of and surgery on the patient, and (2) the startup and operation of the exygenator. The procedure for preparation of the patient and the surgery is as follows.

1. Before the patient is moved into the operating room a

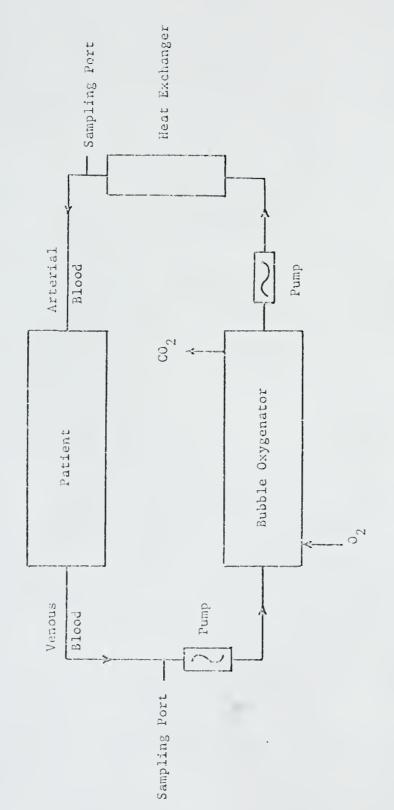


Figure 3.2-1. Schematic of Surgical Operating Setup.

TABLE 3.2-1
SUMMARY OF DATA TAKEN DURING OPEN-HEART SURGERY

Model	Maximum Blood Flow Capacity (liter/min)	No. of Operations	No. of Data Points
1LF	1.0	2	3
2LF	2.0	5	12
3LF	3.0	3	6
6LF	6.0	4	12

- sedative, generally Nembutal, and atropine, is administered.
- Before surgery is begun, an anesthetic such as Pentothal
 is administered to the patient. Other anesthetic agents
 used are halothane, morphine, and nitrous oxide.
- 3. Surgery is begun by cannulating the femoral artery located in the thigh. This artery serves as the arterial return from the blood oxygenator.
- 4. Next, the chest cavity is opened and both superior and inferior vena cava are cannulated. These two veins serve as the venous supply to the oxygenator.
- 5. The patient is now placed on 60% bypass, i.e., 60% of total blood flow is bypassed through the oxygenator. At this point an anticoagulant, heparin, is administered.
- 6. The heart is then defibrillated either by electric shock or by surging cold blood through it.
- 7. The bypass flow is brought to 100% body perfusion rate and surgical repairs are made.
- 8. After surgery on the heart is completed, the bypass flow rate is reduced to 60% and the heart is fibrillated by electric shock.
- The patient is taken off bypass completely and all wounds are closed.

The startup and operating procedure for the oxygenator is as follows:

- The oxygenator, including all tubing, is primed with Ringer's solution and then whole blood.
- 2. The blood pumps are started and the oxygen flow valve is

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opened while the priming solution is circulated around the oxygenator and heat exchanger in a closed loop. This is to insure the initial blood entering the patient's body is saturated with oxygen and at the desired temperature.

- 4. The blood flow rates are adjusted to 60% desired flow as the patient is placed on partial cardiac bypass.

 Simultaneously a maximum 5% (by volume) flow rate of halothane is introduced into the oxygen inlet stream.
- 5. The blood flow rate through the oxygenator is gradually increased to 100% of desired flow.
- 6. Venous and arterial blood samples are taken at approximate 20-minute intervals or upon request of the operating surgeon. These samples are analyzed for oxygen and carbon dioxide partial pressure, plasma pH, hematocrit, and plasma bicarbonate concentration. At the time blood samples are drawn, and blood and oxygen flow rates, as well as temperature, are recorded.
- 7. The blood temperature is gradually increased to normal body temperature, and bypass flow is reduced to 60% of normal flow.
- 8. The patient is removed from bypass system.

 In addition to these procedures blood hemolysis is also monitored at various time intervals.

The device used to analyze blood samples was an Asterup Type AME1.
Estimated accuracy of the Asterup equipment for various measured
quantities is shown in Table 3.2-2. Blood hematocrits were measured

TABLE 3.2-2

ACCURACY OF EXPERIMENTAL DATA TAKEN DURING OPEN-HEART SURGERY

Parameter	Range of Data	Accuracy
O ₂ Partial Pressure	32-590 mm	± 0.5 mm
CO ₂ Partial Pressure	16-38.5 mm	± 0.02 mm
Temperature	28-37°C	± 1.0°C
рН	7.2-7.6	± 0.007
Hematocrit	0.280-0.385	± 2%

by centrifuging two blood samples drawn in capillary tubes for a period of not less than three minutes and then measuring the volume fraction of the separated red cells and plasma. The estimated accuracy of these measurements is shown in Table 3.2-2.

3.3 Experimental Results

Data taken during the 16 operations referred to above are listed in Appendix D. Of the 32 data points taken approximately one-half or 15 were at ratios of oxygen flow to blood flow which exhibited channelling and stagnating flow in the saline simulation experiment. These data points were consequently disregarded in a least square fit to calculate mass transfer coefficients. As previously stated, a linear least squares fit (56) of the data was made with Equations 3.1-8 and 3.1-13 written in the form

$$x_{O_{2}} = \frac{(c_{O_{2}}^{I} - c_{O_{2}}^{*})_{TOT}}{(c_{O_{2}} - c_{O_{2}}^{*})_{TOT}} = 1.0 + K_{O_{2},B} \frac{6}{D_{B}} \cdot \chi$$
 (3.3-1)

and

$$x_{CO_2} = \frac{(c_{CO_2}^{I} - c_{CO_2}^{*})_{TOT}}{(c_{CO_2} - c_{CO_2}^{*})_{TOT}} = 1.0 + K_{CO_2}, B \frac{6}{D_B} \cdot \chi$$
 (3.3-2)

where

$$\chi = \frac{v_{H}}{\dot{v}} \alpha_{O_{2}} \frac{(P_{O_{2}} - P_{O_{2}}^{*})}{(C_{O_{2}} - C_{O_{2}}^{*})_{TOT}}$$
(3.3-3)

and

$$x = \frac{v_{H}}{\dot{v}} \alpha_{CO_{2}} \frac{(P_{CO_{2}} - P_{CO_{2}}^{*})}{(C_{CO_{2}} - C_{CO_{2}}^{*})_{TCT}}$$
(3.3-4)

Both Henry's law constant and the mass transfer coefficient are functions of temperature and hematocrit, and both of these varied from data point to data point. The temperature dependence of Henry's law constants was accounted for by fitting data reported by Sendroy et al. (59), and Davenport (60). For temperatures ranging between 25°C and 37° C, it was found that the 0_2 and 0_2 solubilities could be predicted accurately by

$$\alpha_{0_2} = (8.971448 - 0.02566618.T) \cdot \alpha_{0_2,37^{\circ}C}$$
 (3.3-5)

and

$$\alpha_{\text{CO}_2} = (9.26475738 - 0.026607855.\text{T}) \cdot \alpha_{\text{CO}_2,37^{\circ}\text{C}}$$
 (3.3-6)

where T is the temperature of the blood in degrees Kelvin. The variation of these constants with respect to hematocrit was also reported by Sendroy and Davenport as

$$\alpha_{38^{\circ}C} = \alpha_{rc} \cdot H + \alpha_{p}(1 - H)$$
 (3.3-7)

where $\alpha_{\rm rc}$ is the solubility of 0_2 or 0_2 in the red cell and $\alpha_{\rm p}$ is the solubility of these gases in plasma and H is the volume fraction of red cells in whole blood. For oxygen, values of 0.0258 cc (STP)/cc-atm and 0.0209 cc (STP)/cc-atm, were reported for $\alpha_{\rm rc}$ and $\alpha_{\rm p}$, respectively. For carbon dioxide, values of 0.423 cc (STP)/cc-atm and 0.509 cc (STP/cc-atm, were reported for $\alpha_{\rm rc}$ and $\alpha_{\rm p}$, respectively.

A correction for the variation in mass transfer coefficient due to fluctuations in hematocrit was made based on the diffusivity correction used by Bradley (17). Bradley, noting that blood was a suspension of red cells in plasma, drew an analogy for oxygen and carbon dioxide diffusion into blood to electrical conduction in a suspension of noninteracting ellipsoids (61). From this analogy he suggested that the diffusivity of gases in whole blood could be related to the diffusivity of the same gases in plasma by the equation

$$D_{b}/D_{p} = \frac{1 - H(0.65)}{1 + 0.49H}$$
 (3.3-8)

where $\mathbf{D}_{\mathbf{b}}$ is the diffusivity of the gas in whole blood and $\mathbf{D}_{\mathbf{p}}$ is the diffusivity of the gas in plasma. Now, we have already noted that the mass transfer coefficient is simply

$$K = \frac{D}{L} \tag{3.3-9}$$

where L is the length of the diffusion path. Substituting Equation 3.3-9 into 3.3-8 gives the desired result

$$\frac{K_b}{K_p} = \frac{1 - H(0.65)}{1 \div 0.49H}$$
 (3.3-10)

It was assumed further, that the relationships developed for gas holdup volume as a function of the ratio of the gas flow rate to the liquid flow rate in the saline experiment was valid for the blood experiments.

Using Equations 3.3-1 and 3.3-2 and correcting for temperature

and hematocrit variations, it was found that the best least squares fit of the 17 data points analyzed predicted an oxygen mass transfer coefficient of

$$K_{O_2,B} \cdot \frac{6}{D_B} = 6.44 \text{ min}^{-1}$$

and a carbon dioxide mass transfer coefficient of

$$K_{CO_2,B} \cdot \frac{6}{D_B} = 15.96 \text{ min}^{-1}$$

A graph based on these results of percent oxygenation versus residence time ψ is shown in Figure 3.3-1.

The standard of deviation for $K_{O_2,B}$ was $\stackrel{t}{=}$ 21%, and the standard deviation for $K_{CO_2,B}$ was $\stackrel{t}{=}$ 73.3%. The large standard of deviation in the case of $K_{CO_2,B}$ should not be surprising since very small changes in carbon dioxide partial pressure correspond to a relatively large change in total carbon dioxide concentration. Since data reported were to the nearest 0.5 mm, the calculations made could only predict order of magnitude values for $K_{CO_2,B}$. In addition, we have neglected the transport of bicarbonate ion, and this could be a serious source of error. The 20% standard deviation of the mass transfer coefficient for oxygen is probably due partly to the variation in mass transfer coefficient with temperature, which ranged from 29°C to 37°C, and to inaccuracies in flow rate measurements.

The oxygen flow meter used in the open-heart surgery was graduated to the nearest liter/min which gave at best a \pm 0.25 liter/min estimate of the actual flow rate (as compared to \pm 0.05 liter/min

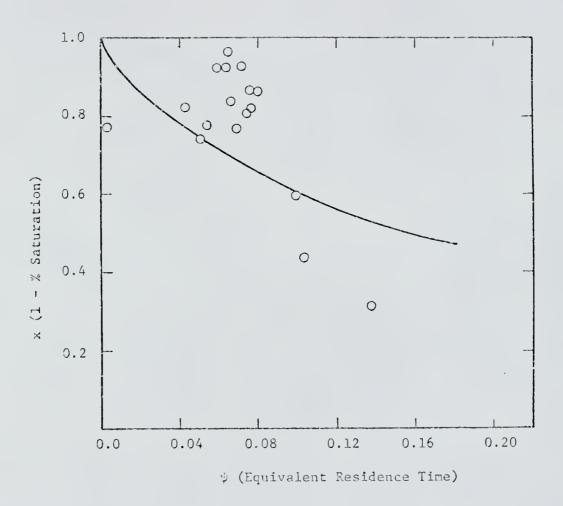


Figure 3.3-1. Data Taken During Open-Heart Surgery.

estimates obtained in the saline simulation). Although the blood flow meter was calibrated to \pm .02 liter/min, readings were reported by the medical staff to the nearest \pm 0.2 liter/min (as opposed to readings of \pm 0.1 liter/min obtained in the saline experiments). If we consider the variation of the diffusivity of oxygen in plasma for temperature changes of the order of 29°C to 37°C, we find a similar deviation of slightly more than 20%. Finally, it should be noted that slight deviations of the oxygenation chamber from the vertical also cause marked differences in the oxygenator performance.

As was done for the saline experiment, a check for the model of diffusion through a stagnant boundary layer with a linear profile surrounding each bubble was made. As a test case a representative hematocrit of 0.30 and a temperature of 32°C was chosen. Since the limiting case near total saturation is the situation encountered in the system when operated normally, it was assumed that Equation 2.4-8 described the transient problem accurately. Using a diffusivity of 1.149 x 10^{-5} cm²/sec, the calculated boundary layer thickness and time constant obtained are shown in Table 3.3-1. The results, of course, assume the same average bubble diameter as was measured in the saline experiment.

The somewhat larger boundary layer, estimated at the blood- $\mathbf{0}_2$ interface as compared with the saline- $\mathbf{0}_2$ interface, is to be expected since red cells and the other formed elements of the blood at the blood:gas interface would tend to "drag" more fluid with the rising bubble than the molecular saline solution. Even though the time constant for the blood system (2.57 sec⁻¹) is smaller than the saline system time

TABLE 3.3-1 $\begin{tabular}{llllll} \hline EXPERIMENTAL VALUES OF O_2 & MASS TRANSFER \\ \hline COEFFICIENT AND OTHER PERTINENT PARAMETERS \\ \hline \end{tabular}$

Parameter	Value
6K _{O₂,B} D _B	0.107 sec ⁻¹
^К о ₂ ,в	$5.28 \times 10^{-3} \text{ cm/sec}$
GKCO ₂ ,B	0.266 sec ⁻¹
K _{CO2} ,B	$1.31 \times 10^{-2} \text{ cm/sec}$
δ	$2.1 \times 10^{-3} \text{ cm}$
$\frac{\delta^2}{\pi^2 p_{0_2}}$	$3.89 \times 10^{-2} \text{ sec}$

constant, it is still large enough to insure a linear diffusion profile across the boundary layer for any reasonable residence time.

The large ${\rm CO}_2$ mass transfer coefficient is probably at least in part due to the neglected transport of bicarbonate ion. Since the majority of carbon dioxide in the blood is carried in this form, a very large mass transfer coefficient would result from neglecting transport due to bicarbonate concentration gradients. It is interesting to note that Bradley (17) obtained a conservative estimate of carbon dioxide transfer by assuming no significant bicarbonate diffusion and he suggested that this result implies that bicarbonate diffusion is significant. If, instead of directly measuring ${\rm K}_{{\rm CO}_2,{\rm B}}$, the ${\rm CO}_2$ mass transfer coefficient is calculated using the equation

$$K = \frac{D_{CO_2, b}}{\delta}$$

we would reach the same conclusions.

The performance of the oxygenator during open-heart surgery at high gas flow rates appears to parallel the performance of the saline simulation. As blood is opaque, it is difficult to confirm the formation of gas pockets at these high flow rates, but the actual reduction in the rate of mass transfer suggests this is the case. Originally we analyzed all 32 data points to fit a mass transfer coefficient. On this basis, the oxygen mass transfer coefficient was calculated to be $6.67 \times 10^{-1} \, \mathrm{min}^{-1}$, a number which is an order of magnitude smaller than our previous estimate. Assuming that the mass transfer coefficient $\mathrm{K}_{\mathrm{O}_2,\mathrm{B}} = 6.44 \, \mathrm{min}^{-1}$, the gas holdup volumes were calculated for these

high flow rate cases. These calculated holdup volumes were extremely scattered and did not appear to be a function of gas and blood flow rate. In general, the values obtained were smaller than would be predicted by our correlations at lower flow rates, thus implying a reduction in the rate of oxygenation. Again, it should be emphasized that the reduction in holdup volume is really a measure of the reduction in interfacial surface area due to coalescence of bubbles; the actual holdup volume may increase.

Having estimated the mass transfer coefficient of oxygen in blood and having obtained at least an order of magnitude estimate of the mass transfer coefficient of carbon dioxide in blood, we can predict the concentration of oxygen and carbon dioxide in arterial blood given the blood and oxygen flow rates, the temperature of the system, and the oxygen, carbon dioxide, and hydrogen ion concentration in venous blood. To accomplish this a computer program was written incorporating the following: 1) Equations 3.3-1 through 3.3-10, 2) the equilibrium relation for total carbon dioxide and oxygen concentrations, 3) Equations 1.3-11 and 1.3-6, and 4) the relationship for holdup volumes listed in Table 2.4-2. This program is listed in Appendix A and is a straightforward arrangement of these equations. Representative results are shown in the figures which follow.

rigures 3.3-2 through 3.3-5 show the effect of temperature on the mass transfer of oxygen in the four sizes of oxygenators studied. The advantage of cooling the blood is obvious from these graphs. For any given flow rate, the percent oxygenation of blood is higher at the lower temperature, other parameters being held constant. This increase

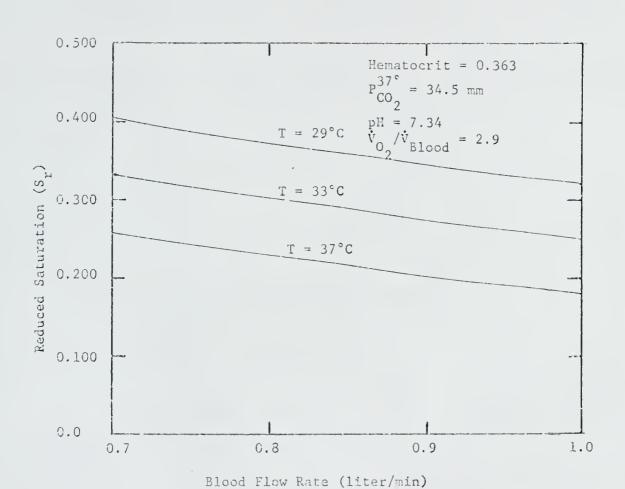


Figure 3.3-2. The Effect of Temperature on Oxygen Absorption in the 1LF Bubble Oxygenator.

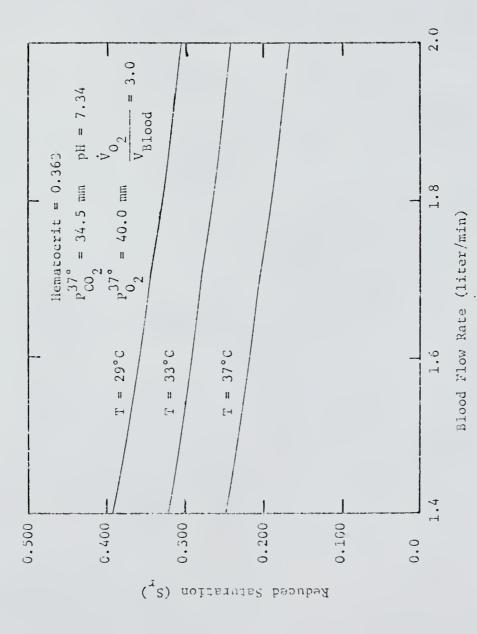


Figure 3.3-3. The Effect of Temperature on Oxygen Absorption in the 2LF Bubble Oxygenator.

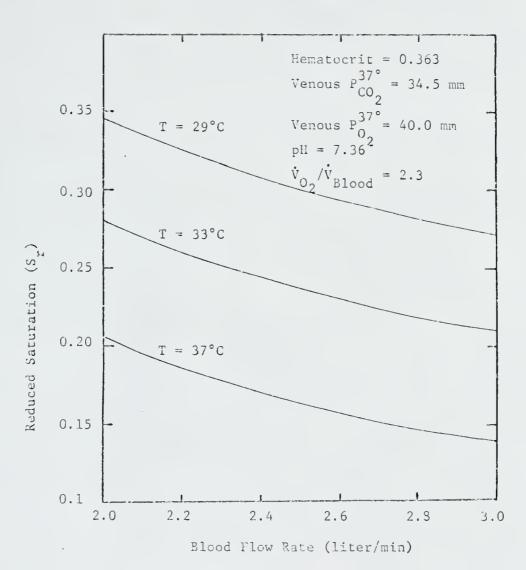
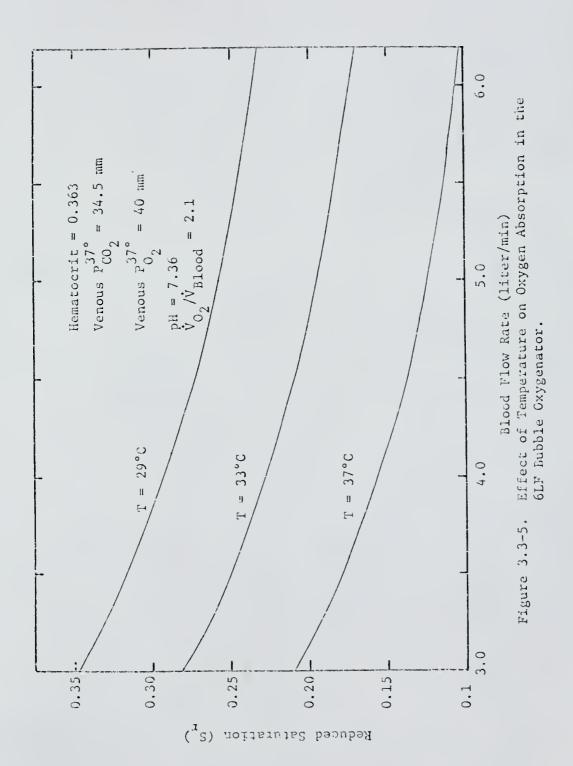


Figure 3.3-4. Effect of Temperature on Oxygen Absorption in the 3LF Bubble Oxygenator.



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in saturation is due to the shift in the equilibrium between oxygenbound hemoglobin and oxygen toward increased saturation at lower temperatures. To a lesser extent the increase in relative saturation is due to the increase in solubility of oxygen in blood at lower temperatures.

Figures 3.3-6 through 3.3-9 show the effects of blood flow rate and the ratio of gas flow rate to blood flow rate on arterial oxygen partial pressure for each of the oxygenators. Figures 3.3-10 through 3.3-13 show the influence of these same parameters on arterial carbon dioxide partial pressure. As can be seen, an optimal value of the ratio of oxygen to blood flow rate is obtained by all of the oxygenators. For the 1-liter bag this ratio is 8.5, for the 2-liter bag it is 3.6, for the 3-liter bag 1.9, and for the 6-liter bag it is 1.7. For ratios greater than these, the holdup volume remains constant until a gas flow rate of about 7-8 liters/min is reached at which point the effective holdup volume decreases with the onset of bubble coalescence.

Figures 3.3-14 through 3.3-17 show the effect of venous oxygen partial pressure on the arterial oxygen partial pressure. The small slope of these curves at low venous partial pressures is due to the fact that a large amount of oxygen added to the blood in this pressure range combines with hemoglobin and thus does not contribute to increase the partial pressure of dissolved elemental oxygen.

3.4 Conclusions and Recommendations

In summarizing the results of the blood oxygenator experiments, the main features of oxygen and carbon dioxide transport are as follows:

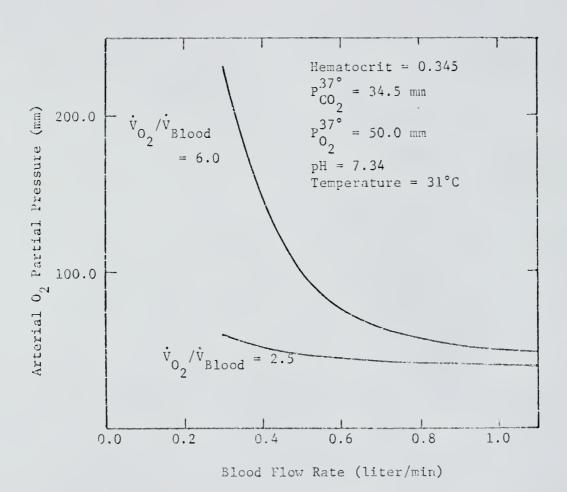


Figure 3 3-6. The Effect of $\mathbf{0}_2$ to Blood Flow Rate Patio on Arterial $\mathbf{0}_2$ Partial Pressure in the 1LF Bubble Oxygenator.

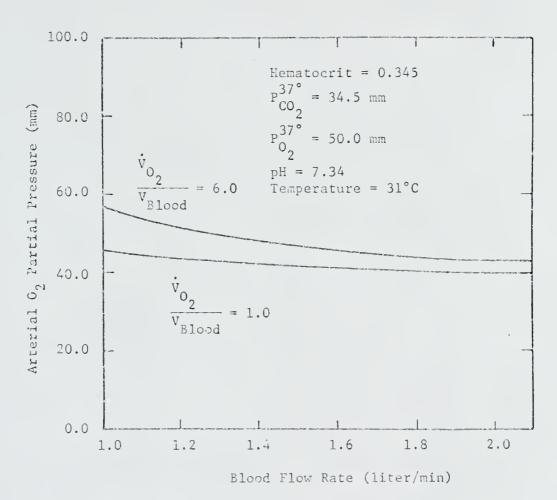


Figure 3.3-7. The Effect of $\mathbf{0}_2$ to Blood Flow Rate Ratio on Arterial $\mathbf{0}_2$ Partial Pressure in the 2LF Bubble Oxygenator.

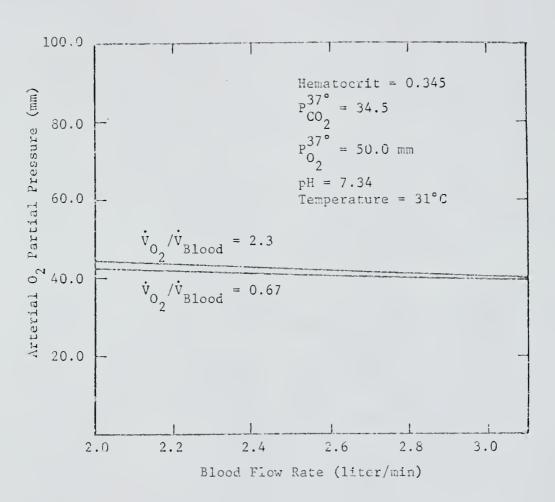


Figure 3.3-8. The Effect of O_2 to Blood Flow Rate Ratio on Arterial O_2 Partial Pressure in the 3LF Bubble Oxygenator.

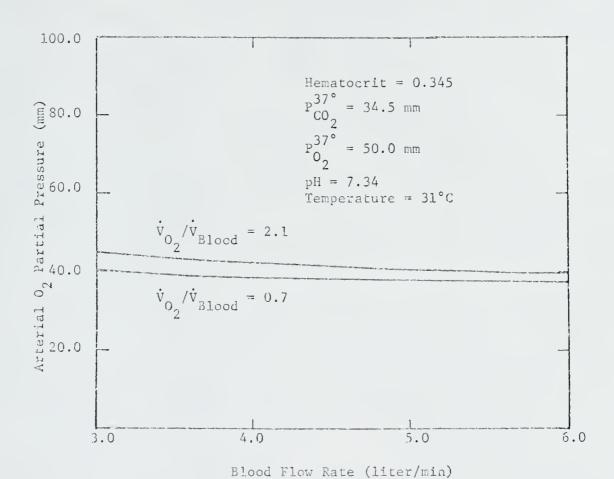


Figure 3.3-9.

The Effect of O_2 to Blood Flow Rate on

Arterial 0_2 Partial Pressure in the 6LF Bubble Oxygenator.

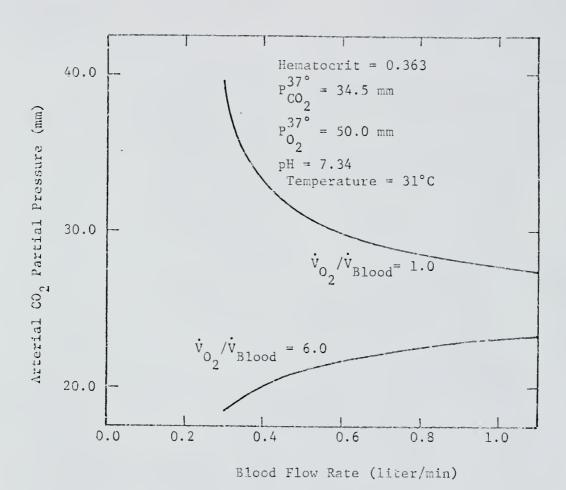


Figure 3.3-10. The Effect of $\mathbf{0}_2$ to Blood Flow Ratio on Arterial $\mathbf{C0}_2$ Partial Pressure in the lLF Bubble Oxygenator.

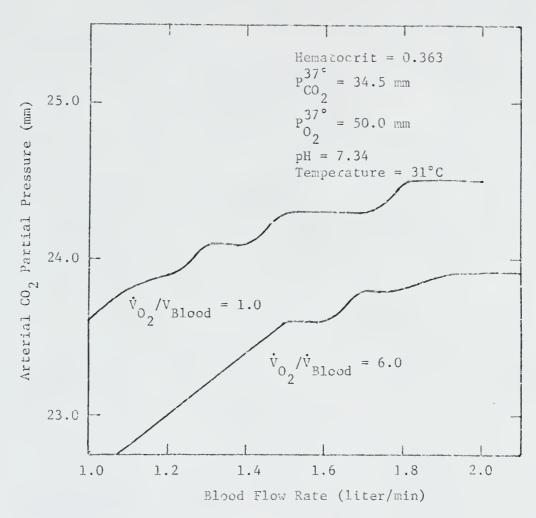


Figure 3.3-11. The Effect of $\rm O_2$ to Blood Flow Ratio on the Arterial $\rm CO_2$ Partial Pressure in a 2LF Bubble Oxygenator.

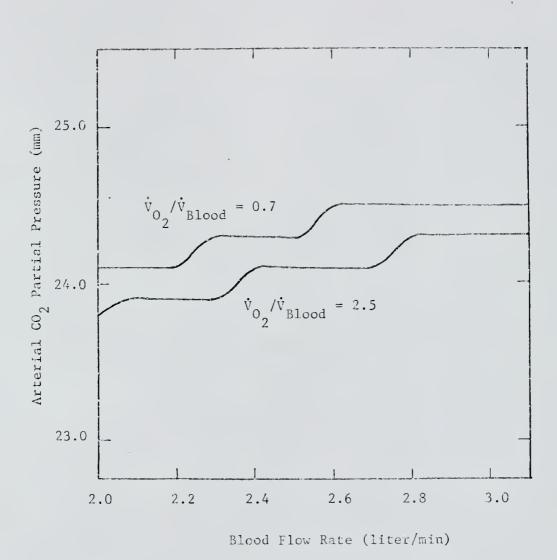


Figure 3.3-12. The Effect of $\rm O_2$ to Blood Flow Ratio on the Arterial $\rm CO_2$ Partial Pressure in the 3LF Eubble Oxygenator.

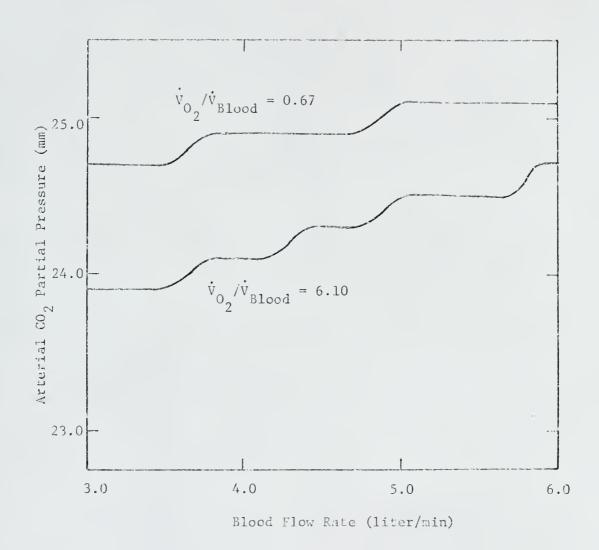


Figure 3.3-13. The Effect of C_2 to Blood Flow Ratio on the Arterial CO_2 Partial Pressure in the 6LF Bubble Oxygenator.

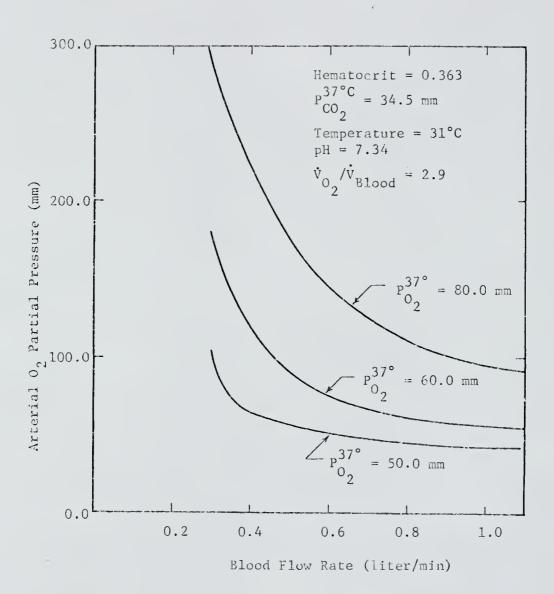


Figure 3.3-14. The Effect of Venous $\mathbf{0}_2$ Partial Pressure on Oxygen Absorption in the 1LF Bubble Oxygenator.

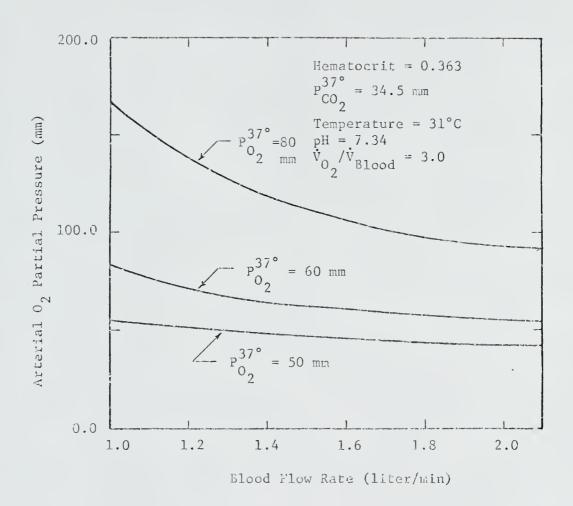


Figure 3.3-15. The Effect of Venous θ_2 Partial Pressure on Oxygen Absorption in the 2LF Bubble Oxygenator.

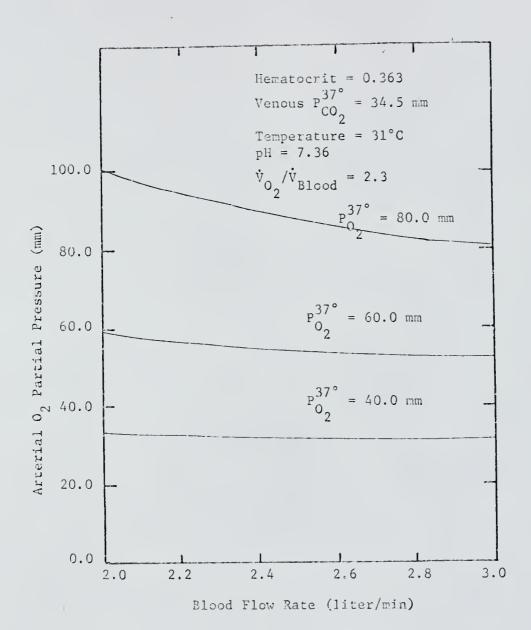


Figure 3.3-16. Effect of Venous $\mathbf{0}_2$ Partial Pressure on Oxygen Absorption in the 3LF Bubble Oxygenator.

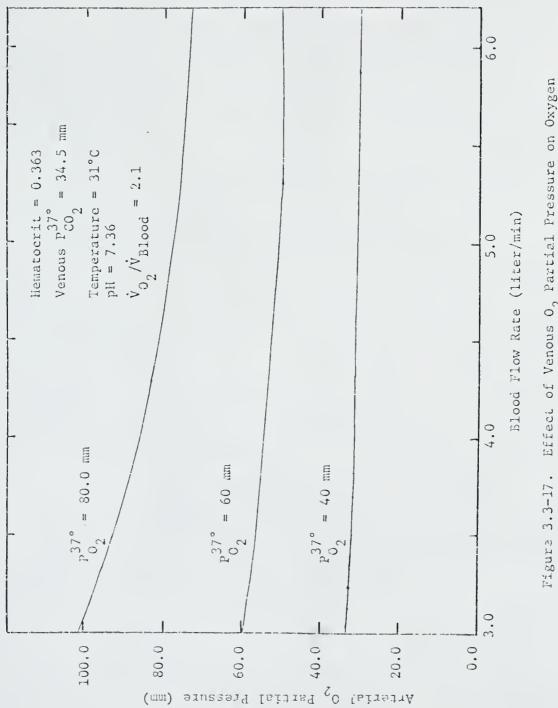


Figure 3.3-17. Effect of Venous o_2 Partial Pressure on Oxygen Absorption in the 6LF Bubble Oxygenator.

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- When operated under normal conditions all four models of the Miniprime oxygenator act as a perfectly mixed single stage absorber.
- 2. The mass transfer coefficient of oxygen in blood over the temperature range of 29°C to 37°C is 0.00528 cm/sec.
- 3. The mass transfer coefficient of carbon dioxide in blood over the temperature range of 29°C to 37°C is 0.0131 cm/sec.
- 4. The optimal interfacial surface area is obtained at a ratio of oxygen to blood flow rate of
 - 8.5 in the 1LF Miniprime Oxygenator;
 - 3.6 in the 2LF Miniprime Oxygenator;
 - 1.9 in the 3LF Miniprime Oxygenator; and
 - 1.7 in the 6LF Miniprime Oxygenator.
- 5. Above a gas flow rate of 7 to 8 liter/min, oxygenator performance is variable and rate of oxygenation is reduced owing to coalescence of bubbles into gas pockets and concomitant reduction in interfacial area. Also contributing to this reduction is the channelling and stagnation flow which occur at these high gas flow rates.
- 6. Tilting of the oxygenator from the vertical causes channelling and stagnation flows which reduce the rate of oxygenation.

Our recommendations lie in two areas; modification of current operating procedures and further research on blood oxygenators. With regard to alteration of current procedures, the following changes

are suggested:

- Every reasonable precaution should be taken to insure that the oxygenation column is in the vertical position and under no circumstances should it be intentionally tilted.
- 2. Gas flow rates should be set to a value corresponding to the ratios listed in item 4 of the conclusions to insure that the maximum interfacial area is available for gas transport.
- 3. Gas flow rates should not be increased beyond 8 liters/min as no increase in the rate of oxygenation will result and the increased flow rate will probably cause increased hemolysis.

Our recommendations for further research are as follows:

- A detailed study of carbon dioxide reactions and equilibrium with blood should be made in order to predict accurately the total amount of carbon dioxide in the blood.
- 2. An effort should be made to measure the diffusivity of bicarbonate ion in the blood.
- 3. In vitro experiments with canine blood paralleling the saline simulation should be made to obtain an accurate value of the carbon dioxide mass transfer coefficient.

 A better estimate of the oxygen mass transfer coefficient could also be obtained by these in vitro experiments.

CHAPTER 4

THE DISC OXYGENATOR

4.1 Description of the Disc Model

The disc oxygenator has only limited use in open-heart surgery and consequently, a mathematical description of its operation has limited value to medicine. However, the principle used in the disc oxygenator to oxygenate blood has been successfully applied to other transport problems (62), and thus placed into a more general context, the investigation of blood oxygenation in the disc oxygenator should provide insight into processes which involve mass transport of reactive gases on a series of rotating discs on which the transport is diffusion-controlled. Since the approach is to be general, we shall derive the disc model for a broad class of problems treating the disc oxygenator as a specific example in Section 2. Referring to Figure 1.4-2, we begin by making a number of assumptions which will be used henceforth:

- the bulk liquid phase occupying the space between any two discs is perfectly mixed;
- 2) reactive gases are supplied to the system in such an excess that their concentration everywhere in the system is equal to their inlet concentration;
- 3) the liquid film which is picked up on the rotating disc is in rigid motion;
- 4) the exposure time of the blood on a disc is short enough, i.e., the rotational speed is high enough, so that the penetration of the gases into the film by diffusion can be assumed to be a penetration into an infinite medium;

[More simply stated, the penetration thickness is much smaller than the film thickness.]

- 5) the process is diffusion-controlled, i.e., all reactions are locally in equilibrium;
- 6) the concentrations of all solutes in the liquid phase are small.

The problem can now be separated into two parts, 1) the mass transfer in the disc liquid film and, 2) the mass transfer in the bulk liquid phase. The liquid film transfer is complex and will be dealt with first. The bulk transfer, which is the transfer from the thin film to the bulk phase, is straightforward and will be dealt with last.

Consider a small segment of the liquid film as shown in Figure 4.1-1. Assuming that mass is transferred in the x-direction alone, (the concentration gradients in the radial and angular directions being small) leads to

$$\frac{\Im(C)}{\Im t} = \frac{[D]\Im^2 C}{\Im x^2} + (R) \tag{4.1-1}$$

with the boundary conditions

$$(C) = (C)^{*}$$
 $x = 0$ $t > 0$
 $(C) = (C)_{c}$ $x \ge 0$ $t = 0$ $(4.1-2)$
 $(C) = (C)_{c}$ $x = \infty$ $t \ge 0$

Using the Boltzmann similarity transformation

$$n = \frac{x}{2\sqrt{t}} \tag{4.1-3}$$

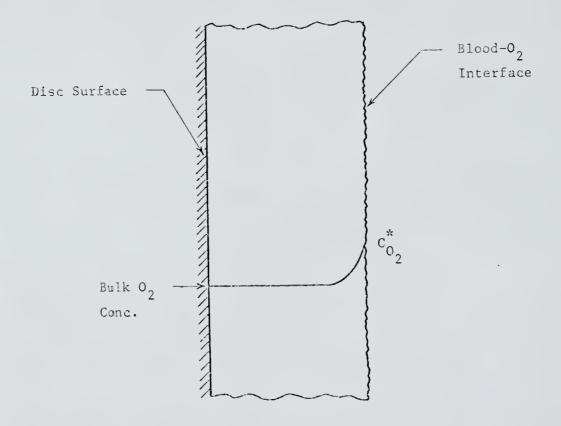


Figure 4.1-1. θ_2 Transfer on a Blood Film.

we obtain the result

$$-2\eta \frac{d(C)}{d\eta} = \frac{[D]d^{2}(C)}{d\eta^{2}} + (R)$$
 (4.1-4)

and the boundary conditions become

$$(C) = (C)^*$$
 $\eta = 0$ (4.1-5)
 $(C) = (C)_0$

We have reduced the system of second order partial differential equations with one initial and two boundary conditions to a system of second order ordinary differential equations with two boundary conditions. In component form, Equation 4.1-5 becomes

$$-2\eta \frac{d^{2}}{d\eta} = \sum_{j=1}^{n} D_{ij} \frac{d^{2}C}{d\eta^{2}} + R_{i}$$
 (4.1-6)

Recognizing that the cross terms, D_{ij} ($i \neq j$) are small for dilute solutions, Equation 4.1-6 can be simplified to

$$-2\eta \frac{dC_{i}}{d\eta} = D_{ii} \frac{d^{2}C_{i}}{d\eta^{2}} + R_{i}$$
 (4.1-7)

At this point the conditions on the problem must be further specified to eliminate the reaction term R_i and to utilize the assumption of local equilibrium. If a chemical species is denoted by the subscript k and total amount of this species per unit volume in both reacted and unreacted forms is summed in Equation 4.1-6, the results are

$$-2\eta - \frac{d \sum_{M} C_{Mk}}{d\eta} = \sum_{M} D_{MM} - \frac{d^{2}C_{Mk}}{d\eta^{2}}$$
 (4.1-8)

and
$$\sum_{i=1}^{n} R_{ijk} = 0$$

The result that the summation of the reaction rates involving the component k must be equal to zero is due to the conservation of mass, not the assumption of local equilibrium. The assumption of local equilibrium is now invoked using the equilibrium relationships

$$\sum_{M} C_{Mk} = \hat{r}_{M}(C_{i}, C_{j}, C_{k}, \dots, C_{n}, T, P)$$
(4.1-9)

i.e., the amount of component k per unit volume is a function of the concentration of component k, the concentrations of all the components reacting with component k, the temperature, and the pressure. At constant temperature and pressure we obtain

$$\frac{d\sum_{Mk}^{C}}{d\eta} = \sum_{i} \frac{df_{M}}{\partial C_{i}} \frac{dC_{i}}{d\eta}$$
 (4.1-10)

Furthermore, viewing the inverse relationship of Equation 4.1-9, the concentration of k bound to any one component is a function of the concentration of component k bound to the remaining species and the total concentration or

$$^{\mathbf{C}}_{\mathbf{Mk}} = G_{\mathbf{M}}(C_{\mathbf{i}}, C_{\mathbf{i}}, C_{\mathbf{i}}, C_{\mathbf{i}}, \dots, \sum_{C_{\mathbf{Mk}}}, \Gamma, P)$$
(4.1-11)

Therefore,

$$\frac{d^{2}C_{Mk}}{dn^{2}} = \sum_{i} \sum_{j} \frac{\partial^{2}G_{M}}{\partial C_{i}} \frac{dC_{j}}{\partial n^{j}} + \sum_{i} \frac{\partial G_{M}}{\partial C_{i}} \frac{d^{2}C_{i}}{dn^{2}}$$
(4.1-J2)

Substituting Equations 4.1-11 and 4.1-10 into Equation 4.1-8 gives the final result

$$\sum_{i} \frac{\partial f_{M}}{\partial C_{i}} \frac{dC_{i}}{d\eta} = \sum_{M} D_{MM} \left[\sum_{i} \left[\sum_{j} \frac{\partial^{2} G_{M}}{\partial C_{i}} \frac{dC_{j}}{d\eta} \frac{dC_{j}}{d\eta} + \sum_{i} \frac{\partial G_{M}}{C_{i}} \cdot \frac{d^{2} C_{i}}{d\eta^{2}} \right] \right]$$
(4.1-13)

Equation 4.1-13 is the starting point for any analysis of thin film mass transfer on a disc. In theory, it can be solved for a wide range of functional forms of the nonlinearities $G_{\widetilde{M}}$ and $f_{\widetilde{M}}$ by numerical techniques, but the cost of computation becomes prohibitive if more than a few coupled components are considered. Consequently, it is advantageous to model processes as simply as possible, retaining the important physical characteristics of the system and deleting those features which have only minor influence.

There are many limiting cases of Equation 4.1-13 which are of practical significance, one of which will be demonstrated in the discussion of the disc oxygenator in the next section. A very simple limiting case arises when the diffusivities of all the components are equal. In this case Equation 4.1-8 becomes

$$-2\eta \frac{d \sum_{M} C_{Mk}}{d\eta} = D_{MM} \frac{d^2 \sum_{M} C_{Mk}}{d\eta^2}$$
 (4.1-14)

This, of course, is a linear differential equation which has the simple solution

$$\sum_{M} C_{Mk} = \left(\sum_{M} C_{Mk}(\infty) - \sum_{M} C_{Mk}(0)\right) \operatorname{erf}\left(\frac{\eta}{\sqrt{D_{MM}}}\right) + \sum_{M} C_{Mk}(0) \qquad (4.1-15)$$

where

$$\sum_{M} C_{Mk}(\infty) = \sum_{M} C_{Mk} \qquad \qquad n \to \infty$$

and

$$\sum_{M} C_{Mk}(0) = \sum_{M} C_{Mk} \qquad \eta = 0$$

Assuming that a solution of $C_{\bf i}$ as a function of n can be found, the mass transfer in the bulk liquid phase can now be determined. Writing a mass balance across one ideal mixing stage (see Figure 4.1-1) we obtain the equation

$$\dot{\mathbf{v}}(\mathbf{C}_{\mathbf{i}}^{\text{out}} - \mathbf{C}_{\mathbf{i}}^{\text{in}}) = \omega \int_{\mathbf{R}_{1}}^{\mathbf{R}_{2}} \int_{\mathbf{R}_{1}}^{\infty} 2\pi \mathbf{r}(\mathbf{C}_{\mathbf{i}}^{f}(\mathbf{r}, \mathbf{x}) - \mathbf{C}_{\mathbf{i}}^{\text{out}}) d\mathbf{x} d\mathbf{r}$$
 (4.1-16)

where

. v = volume flow rate of liquid through the ideal mixing stage $C_{\,\,i}^{\,\,i\,n} \,=\, \text{inlet concentration of component i}$

Cout = concentration of component i in the bulk liquid phase in the mixing stage

 $C_i^f(r,x)$ = concentration of component i re-entering the bulk phase after 1 revolution around the disc

and ω = the angular rotational speed of the disc.

It should be noted that $C_{\bf i}^{\rm f}$ is a function of both radial position on the disc and of the depth below the surface of the film. The radial position, r, can be related to the time parameter, t, in Equation 4.1-3. Referring to Figure 4.1-2, the length of time t that an element of a liquid film at radius r is exposed to the gas phase is given by the equation

$$t = \frac{2 \arcsin\left(\frac{R_1}{r}\right) + \pi}{2\pi}$$

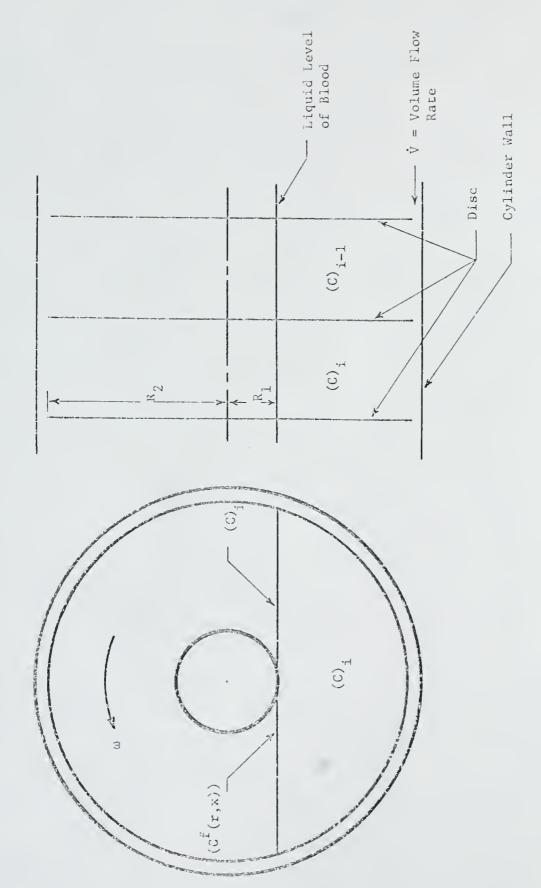


Figure 4.1-2. Schematic of Perfectly Mixed Stages in a Disc Oxygenator.

where R_1 is the radius to which the disc is immersed in the bulk phase. Thus, if C_i^f is known as a function of η , it can be calculated as a function of x and r, and the analytical or numerical integration of Equation 4.1-16 can be carried out. It should also be noted that

$$C_i^f \rightarrow C_i^{out}$$
 as $x \rightarrow \delta$ (4.1-17)

where δ is some finite penetration thickness. Incorporating Equation 4.1-17 into 4.1-16 gives the final result

$$C_{i}^{out} = \frac{\int_{R_{1}}^{R_{2}} \int_{0}^{\delta} 2\pi r C_{i}^{f}(r,x) dxdr + vC_{i}^{in}}{\omega \pi (R_{2}^{2} - R_{1}^{2}) + v}$$

If these stages are arranged in series, calculations can be done for each stage in stepwise fashion with the inlet concentration for the i+lth stage being set equal to the outlet concentration of the ith stage.

4.2 Analytical Results -- Computer Simulation

example of diffusion-controlled mass transfer with chemical reaction in a thin film. The chemical reactions involved in this process were outlined in Chapter 1, Section 3. The equilibrium relationship used for oxygen binding is given in Equation 1.3-6. Thus, the equation for total oxygen transport obtained by substituting Equation 4.3-6 into Equation 4.1-8 is

$$-2\tau \left(\alpha_{0_{2}} + \frac{\sigma S}{\partial P_{0_{2}}}\right) \frac{dP_{0_{2}}}{d\eta} = \alpha_{0_{2}}^{D_{0_{2}}} + D_{0_{2}} + D_{0_{2}} \left(\frac{d^{2}HBO_{2}}{d\eta^{2}}\right)$$
(4.2-1)

Since the hemoglobin molecule is large and has a high molecular weight, its diffusivity is small; consequently, mass transport of oxygen due to the diffusion of oxyhemoglobin is negligible. Setting the last term in Equation 4.2-1 equal to zero gives the desired result

$$-2\eta \left(\alpha_{0_{2}} + \frac{3S}{3P_{0_{2}}}\right) - \frac{dP_{0_{2}}}{d\eta} = \alpha_{0_{2}} D_{0_{2}} - \frac{d^{2}P_{0_{2}}}{d\eta^{2}}$$
 (4.2-2)

with the boundary conditions

$$P_{O_2} = P_{O_2}^{int} \qquad \eta = \infty$$

$$P_{O_2} = P_{O_2}^* \qquad \eta = 0$$

Equation 4.2-2 can be solved numerically as a function of n if the diffusivity and solubility of oxygen are known. We have already discussed the solubility of oxygen in blood as a function of hematocrit and temperature in Chapter 3, and we have pointed out that the diffusivity of both carbon dioxide and oxygen can be represented by Equation 3.3-8 as a function of hematocrit. It remains then to calculate the diffusivities of these two gases in plasma as a function of temperature. Spacth (63) showed that the ratio of the diffusivity of oxygen in plasma to the diffusivity in water was 0.58 at all temperatures studied. Using data taken from Bradley (17), Foust (64), and Perry (53), the diffusion coefficient of oxygen in water can be represented by

$$D_{0_2, H_20} = -677.2838 \times 10^{-5} + 4.458846 \times 10^{-5} \cdot T + 7.307692 \times 10^{-8} T^2$$
(4.2-3)

where T = temperature (°K)

$$D_{O_2,H_2O} = diffusivity (cm^2/sec)$$

Thus

$$D_{O_2,HE} = D_{O_2,H_2O} \cdot (0.58)$$
 (4.2-4)

Reliable data on the diffusivity of carbon dioxide in blood plasma are not available; consequently, as Mackros (19) also assumed, the ratio of carbon dioxide diffusivity to oxygen diffusivity in blood was set equal to the ratio of these diffusivities in water. Again correlating existing data (17), (19), (52), it was found that this ratio is predicted by the empirical equation

$$R = 1.0169 + 6.94355985 \times 10^{-2} \cdot (310 - T) - 3.54312 \times 10^{-3} (310 - T)^{2}$$

$$(4.2-5)$$

where T = temperature (°K)

and thus

$$^{D}CO_{2}, HB = ^{D}O_{2}, HB/R$$
 (4.2-6)

Having calculated all pertinent physical constants, only the equilibrium equation for carbon dioxide remains to be incorporated into the equation for CO₂ transfer to completely define the problem. Unfortunately Equation 1.3-10 is applicable only over a restricted pressure range whose minimum value is greater than 30 mm. Since one of the boundary

conditions for the CO₂ transport equation is

$$P_{CO_2} = 0 \qquad \eta = 0$$

Equation 1.3-11 cannot be used. In its place, the Henderson-Hasselbalch equation for the equilibrium of bicarbonate ion with carbon dioxide has been used. This equation is based on the two reactions which take place in the plasma

$$co_2 + H_2 o \neq H_2 co_3$$

and

$$H_2 CO_3 \stackrel{?}{\leftarrow} H^+ + HCO_3^-$$
 (4.2-7)

The corresponding equilibrium equations for these two reactions are

$$\hat{K}_{1} = \frac{[CO_{2}][H_{2}O]}{[H_{2}CO_{3}]}$$
 (4.2-8)

and

$$\hat{K}_2 = \frac{[H_2CO_3]}{[H^+][HCO_3]}$$

Combining Equations 4.2-8 gives the desired result

$$\hat{K}_{1}\hat{K}_{2} = \frac{[\text{CO}_{2}][\text{H}_{2}\text{O}]}{[\text{H}^{+}][\text{HCO}_{3}^{-}]}$$
(4.2-9)

Furthermore since the concentration of water is essentially constant, $[H_20]$ can be incorporated into the term $\hat{K_1} \cdot \hat{K_2}$, giving the result

$$pH = p\hat{K} + log \left(\frac{[HCO_3]}{CO_2} \right)$$
 (4.2-10)

$$p\hat{K} = \log\left(\frac{[H_2O]}{\hat{K}_1\hat{K}_2}\right) \tag{4.2-11}$$

Thus, the concentration of bicarbonate ion in the plasma is given by the equation

$$[HCO_3^-] = \alpha_{CO_2}^P CO_2^- 10^{(pH-p\hat{K})}$$
 (4.2-12)

and the total concentration of carbon dioxide in plasma is given by

$$[CO_2]_{TOT} = \alpha_{CO_2}^{P}_{CO_2} (1 + 10^{pH-p\hat{K}})$$
 (4.2-13)

Equation 4.2-13 involves the assumption that the amount of undissociated carbonic acid is negligible. The value of $p\hat{K}$ at 37°C is 6.1 (65), and temperature corrections have been calculated for temperatures to as low as 25°C (66). It has been reported (67) that the concentration of carbon dioxide in whole blood is related to the concentration of carbon dioxide in plasma by the relationship

$$[CO_2]_{TOT, Blood} = \frac{[CO_2]_{TOT, plasma}}{1.2}$$
 (4.2-14)

Substitution of Equations 4.2-13 and 4.2-14 into 4.1-8 gives

$$-2\eta \frac{\alpha_{\text{CO}_2}}{1.2} \left[1 + 10^{(pH-p\hat{K})}\right] \frac{d^{\text{P}}_{\text{CO}_2}}{d\eta} = \alpha_{\text{CO}_2}^{\text{D}}_{\text{CO}_2} \frac{d^{2}P_{\text{CO}_2}}{d\eta^{2}} + D_{\text{HCO}_3}^{\text{D}} \frac{d^{2}[\text{HCO}_3]}{d\eta^{2}}$$
(4.2-15)

Although there is less justification for assuming megligible bicarbonate transfer than for assuming negligible exphemoglobin transfer, this assumption will be made since values of $D_{\mbox{HCO}_3^-}$ are not currently

available. Eliminating the last term in Equation 4.2-15 by this assumption leads to

$$\frac{-2n}{1.2} \left[1 + 10^{(pH-p\hat{K})}\right] \frac{d^{p}_{CO_{2}}}{dn} = D_{CO_{2}} \frac{d^{2}p_{CO_{2}}}{dn^{2}}$$
(4.2-16)

with the boundary conditions

$$P_{CO_{2}} = 0 \qquad \eta = 0$$

$$P_{CO_{2}} = P_{CO_{2}}^{int} \qquad \eta = \infty$$

$$P_{CO_2} = P_{CO_2}^{int}$$
 $\eta = \infty$

Equation 4.2-16 is a linear differential equation the solution of which is

$$P_{CO_2} = P_{CO_2}^{int} erf \left(n \frac{1 + 10^{(pH-p\hat{K})}}{1.2 D_{CO_2}} \right)$$
 (4.2-17)

The solution for the oxygen concentration profile is more complicated owing to the nonlinearity of the differential equation. A computer program was written to solve Equation 4.2-2. The technique used in the program to solve this equation is the Adams Bashforth predictor-corrector method for numerical integration which has been written in a convenient subroutine package by Dr. T. C. Bullock, Department of Electrical Engineering, University of Florida.

A plot of oxygen concentration profiles versus n at different initial $\mathbf{0}_{2}$ partial pressures is shown in Figure 4.2-1. It should be noted that the concentration gradients steepen, and the peretration thickness decreases, as the initial partial pressure decreases due to

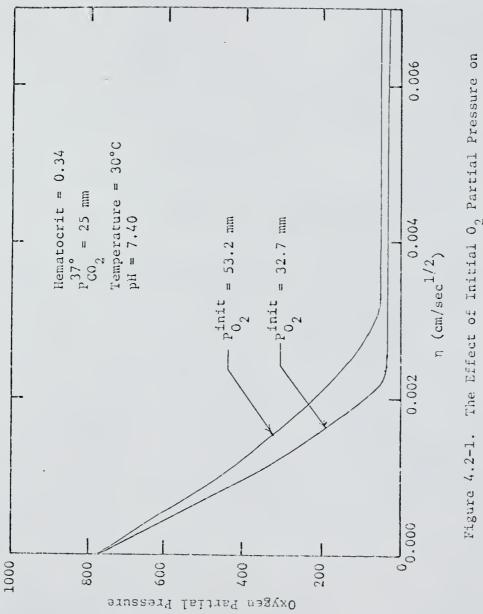


Figure 4.2-1. The Effect of Initial $\mathbf{0}_2$ Partial Pressure on the Boundary Layer Concentration Profile.

the nonlinearity introduced into the differential equation by oxygen binding to hemoglobin. The effect of temperature is shown in Figure 4.2-2; the advantage of operating at a lower temperature is illustrated clearly. The carbon dioxide partial pressure profile is shown in Figure 4.2-3. Since the differential equation describing this process is linear, the profile is independent of initial partial pressure. The temperature effects are shown in Figure 4.2-4.

With the concentration profile across the diffusion layer specified, Equation 4.1-18 can be employed to calculate the bulk concentration of the ith stage for both CO, and oxygen. Typical results for a series of 5 stages are shown in Figures 4.2-5, 4.2-6 and 4.2-7. These reveal that the largest amount of transfer takes place in the first few stages, an effect which is caused by the reduction in the difference between bulk phase concentration of gases and the concentration of these gases at the blood-gas interface, and the corresponding reduction in concentration gradients of these components across the diffusion layer in succeeding stages. It should be noted that the inlet concentration of the oxygen in blood entering the disc film was set equal to the known inlet concentration of the blood entering the ith stage rather than the unknown bulk concentration of the ith stage. If the differential equations for oxygen transport were linear, this assumption would not be necessary since the concentration provile is independent of initial concentration when written in dimensionless form. Since Equation 4.2-2 is nonlinear, however, this approximation is made to reduce computational time required to solve the problem. Moreover, as the increase in concentration of oxygen

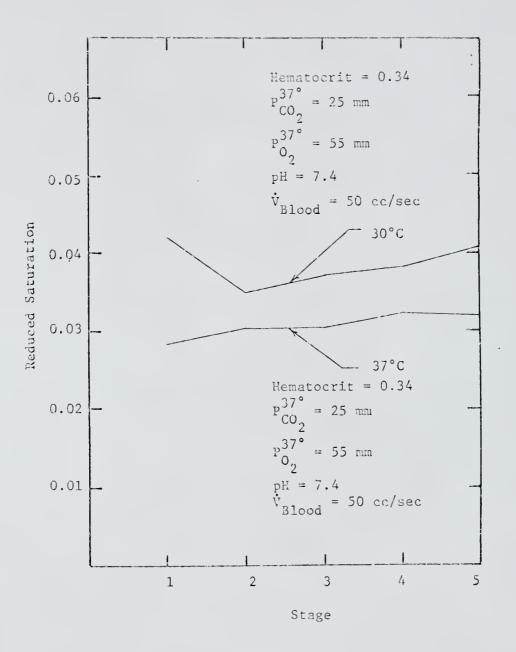


Figure 4.2-2. The Effect of Temperature on ${\it O}_2$ Absorption in the Disc Oxygenator.

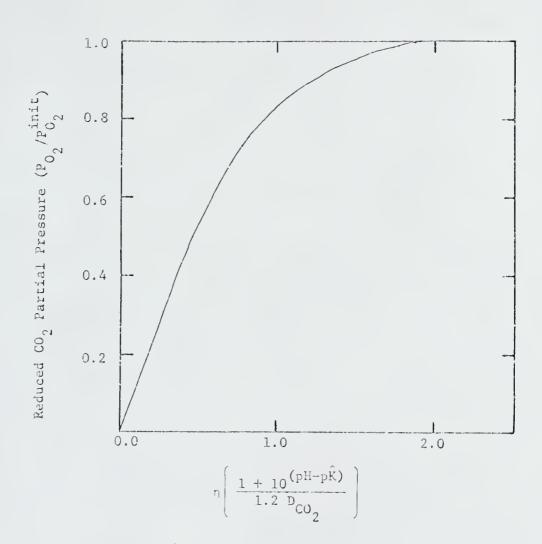


Figure 4.2-3. Carbon Dioxide Boundary Layer Profile.

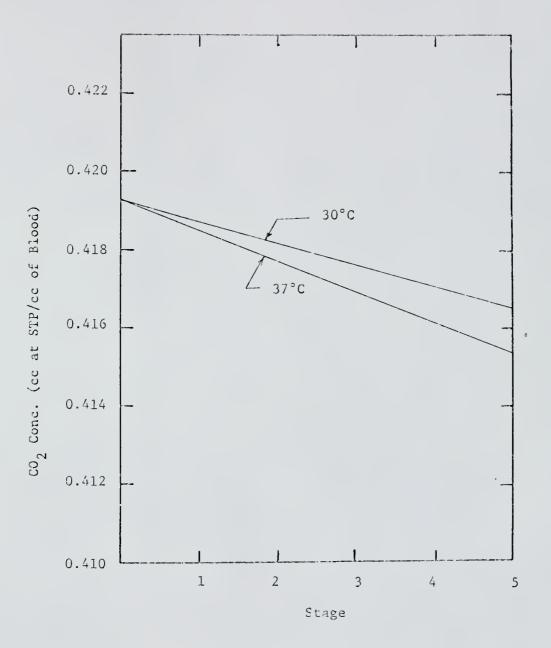


Figure 4.2-4. The Effect of Temperature on ${\rm CO}_2$ Desorption in the Disc Oxygenator.

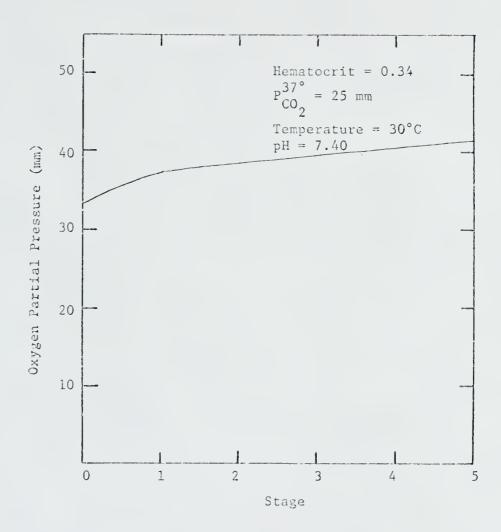


Figure 4.2-5. $\rm O_2$ Partial Pressure as a Function of Stage No. for a Blood Flow of 40 cc/sec.

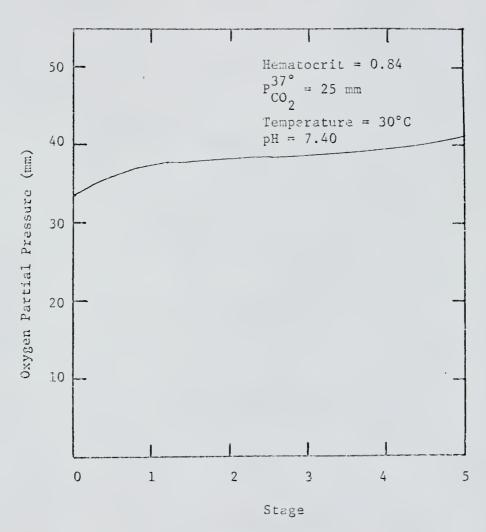


Figure 4.2-6. O₂ Partial Pressure as a Function of Stage No. for a Blood Flow of 30 cc/sec.

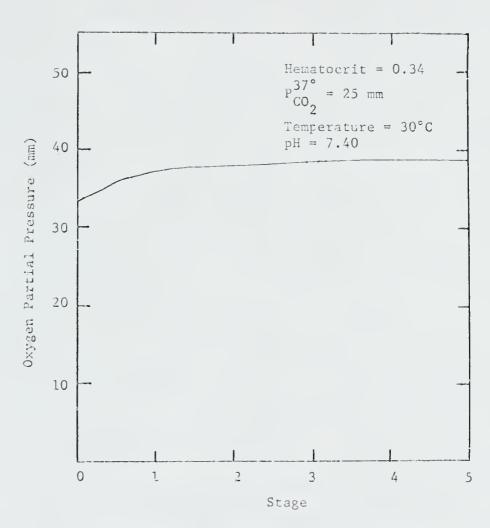


Figure 4.2-7. θ_2 Partial Pressure as a Function of Stage No. for a 3100d Flow of 75 cc/sec.

across any one stage is small, this assumption should not lead to serious errors.

4.3 Conclusion and Recommendations

The model proposed for the diffusion-controlled transport gives reasonable estimates of blood oxygenation in disc oxygenators. The method of solving the pertinent nonlinear equations by numerical integration gives a satisfactory solution, but the computation time required to solve the equation is excessive. This problem is further aggravated by the fact the boundary values are given at two different values of η , one of which is infinite. Consequently, an initial guess of the derivative at $\eta=0$ was made to transform the problem into a one-point boundary value problem instead of a two-point boundary value problem. The numerical integration was carried out and the asymptotic value as $\eta\to\infty$ was checked against the second boundary condition. If the values did not match, the initial derivative was adjusted accordingly and the process was repeated.

It is suggested that a variable integration step size be introduced into the subroutine involving the Adams-Bashforth numerical integration. This addition to the program could save a significant amount of time now wasted by the stringent requirement of constant step size over the entire integration range. It would also be helpful if a more accurate method of predicting and correcting the initial derivative (outlined in Appendix A) could be found.

It is recommended that oxygenation data either from the operating room, in vivo experiments with animals, or in vitro

experiments be taken and analyzed to test the validity of the proposed model.

It is also suggested that this model be applied to biooxidation of waste water by the BIO-DISC developed by Allis-Chalmers
for secondary waste treatment. The chemical kinetics of this system
will have to be developed for this application.

Finally, it is suggested that a membrane oxygenator design incorporating the principle of the disc oxygenator be investigated as a means to oxygenate blood for long perfusion times.

CHAPTER 5

GAS TRANSPORT IN LIQUID-FILLED LUNGS

5.1 Introduction

The problem of gas transport in liquid-filled lungs was originally brought to our attention by Dr. J. H. Modell, Chairman of the Department of Anesthesiology at the University of Florida and members of his staff. In their attempts to provide adequate oxygen and carbon dioxide exchange in canine lungs, they found that the fluorocarbons PLD and FX-80 provided adequate oxygen transfer but did not provide efficient carbon dioxide elimination from the blood.

Comparing their data with a diffusion model similar to Kylstra's (46), they suggested that the limited CO₂ transport could be due to the small differences in partial pressures of carbon dioxide between the blood and the fluorocarbon entering the lung; thus the correspondingly small diffusion flux resulted in only a small net mass transfer of carbon dioxide.

After investigating the problem and determining the flow rate of fluorocarbon in the lungs (approximately 1.8 liters per minute) and the total volume of the lungs (approximately 0.8 liters), it was suggested that the mode of mass transfer of dissolved gases through the liquid-filled lungs could be by convective mixing as opposed to molecular diffusion. To test these two hypothesyses, a series of experiments was proposed. In brief, the experiments consisted of filling a dog's lungs with solution containing a known dye concentration and then breathing the dog using the same solution but with higher dye

concentration for a specified number of respirations. After the specified number of respirations, the liquid would then be drained from the lungs and the concentration of the dye measured as a function of volume drained. It was anticipated that from the resulting dye concentration profiles as a function of lung volume, one could discriminate between the diffusion and convective transport models.

5.2 Theory of Diffusion

In setting up a theoretical model of the transient response in the lungs to a step change in dye concentration at the lung entrance during liquid breathing, there are two diffusion-controlled cases to be considered. In both cases, the lung as a transport unit will be arbitrarily separated into two parts: 1) a region in which convective transport dominates and 2) a region in which diffusion dominates. In the first limiting case, it will be assumed that in the region in which transfer is dominated by convection, the motion of the fluid is described by plug flow. In the second limiting case, it will be assumed that the region in which transfer is dominated by convection, the liquid is perfectly mixed.

In the first case, the concentration of the dye at the boundary of the diffusion-dominated region is the same as the inlet concentration, the problem is reduced to transient diffusion of a dye into a finite slab with a step in dye concentration at some initial time, t=0, at one of the boundaries of the slab. Writing the continuity equation for such a system, we obtain

$$\frac{\partial C}{\partial t} = -\nabla \cdot J \tag{5.2-1}$$

where C = the contentration of the dye and J = mass flux of the dye.

Substituting Fick's diffusion law for J into Equation 5.2-1 gives the result

$$\frac{\partial C}{\partial t} = -\nabla \cdot (Cv) + D\nabla^2 C \qquad (5.2-2)$$

As we are interested in the limiting case of diffusion-controlled transport, it will be assumed that the fluid velocity is equal to zero, and, furthermore, that the problem is one-dimensional, i.e., the concentration across any cross-sectional area of the slab is constant. With these assumptions, Equation 5.2-2 becomes

$$\frac{\partial C}{\partial r} = D \frac{\partial^2 C}{\partial x^2}$$
 (5.2-3)

with the boundary conditions

$$C = C_1$$
 $x = 0, t > 0$
 $C = C_0$ $t = 0$

The solution to Equation 5.2-3 is straightforward; and it can be written as

$$\frac{C - C_1}{C_0 - C_1} = \sum_{n=0}^{\infty} \frac{4}{(2n+1)\pi} \left(\exp - \left(\frac{(2n+1)\pi}{2} \right)^2 \frac{Dt}{\ell^2} \right)$$

$$\cdot \text{ sir. } \frac{(2n+1)\pi}{2} \left(\frac{V - V_0}{V_{\text{tot}} - V_D} \right)$$
(5.2-4)

where C = concentration of the dye

 C_1 = concentration of the dye at the entrances to the lungs

 C_{Ω} = concentration of the dye initially in the lungs

= length of the diffusion path

V = volume of the slab (in this case the volume of the lungs)

 $V_{\mathrm{D}}^{}=\mathrm{volume}$ of the lung at which diffusion becomes the dominant mode of mass transfer

 V_{tot} = total volume of the lungs.

The dye concentration profiles which would result in the lungs if such a two-regime mass transfer process occurred are shown in Figure 5.2-1, where it has been assumed that the volume of the convection-dominated region is one-half the total volume of the lungs. It should be noted that the parameters plotted in Figure 5.2-1 are dimensionless quantities

$$\phi = \left(\frac{(2n+1)\pi}{2\lambda} \right)^2 Dt$$

Therefore, these curves are independent of the magnitude of the diffusivity and diffusion length of the system.

In the second case, the concentration C_0 will be a function of time, since, with each breath, the newly inspired liquid will mix with the liquid already in the convection-dominated region. At the end of each inspiration, the concentration in this region will be perfectly mixed, consequently, C_0 will be

$$c_{0} = \frac{v_{1}c_{init} + v_{2}c_{R}}{v_{1} + v_{2}}$$

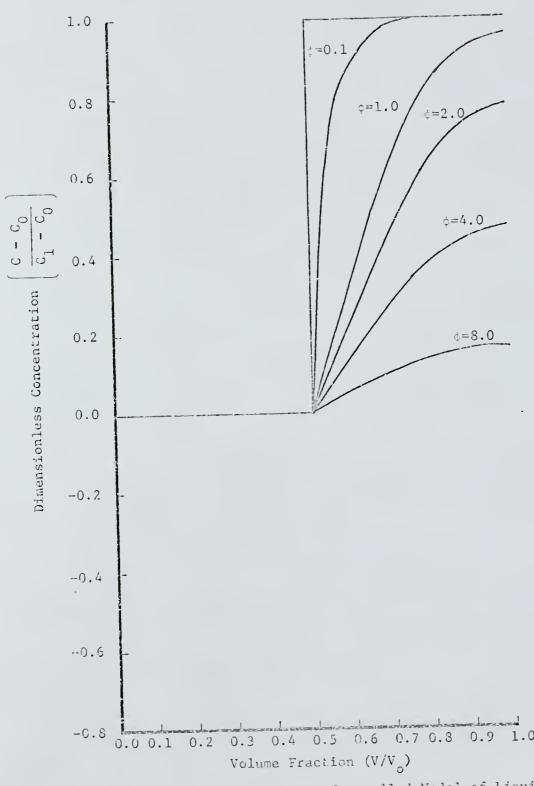


Figure 5.2-1. Diffusion-Controlled Model of Liquid Breathing with Plug Flow.

where C_{init} = concentration of the dye in the convective region at the start of an inspiration

 $C_{R}^{}$ = concentration of dye in the inspired liquid

 ${
m V}_1$ = volume of liquid in the convective region at the beginning of an inspiration

 $V_2 = tidal volume of the lung*$

Since the process of diffusion is relatively slow, it will be assumed that the concentration of the perfectly mixed region reaches the limiting value of the inlet concentration before significant diffusion takes place. Granting this to be the case, Equations 5.2-3 and 5.2-4 are applicable again, and the solution can be represented graphically as shown in Figure 5.2-2, where once again reduced parameters have been plotted. In making these calculations it has also been assumed that the volume of the convection-dominated region is equal to one-half of the total lung volume, and the tidal volume was set equal to one-third the total volume of the lung.

It should be noted that the lung has been modelled as a rectangular geometry. Other geometries, such as spheres and cylinders, have been used which may reflect the geometry of the lung more realistically, but it should be emphasized that, regardless of the geometrical configuration, we should still observe the same qualitative behavior in the experiments, namely, the sharp rise in $\frac{C-C_1}{C_0-C_1}$ at $\frac{V}{V_{\rm tot}} = \frac{V_D}{V_{\rm tot}}$ if there exists a region within the lung in which mass transport is diffusion-controlled.

It should be recalled from Chapter 1, that the tidal volume is defined as the volume inspired or expired during one breath.

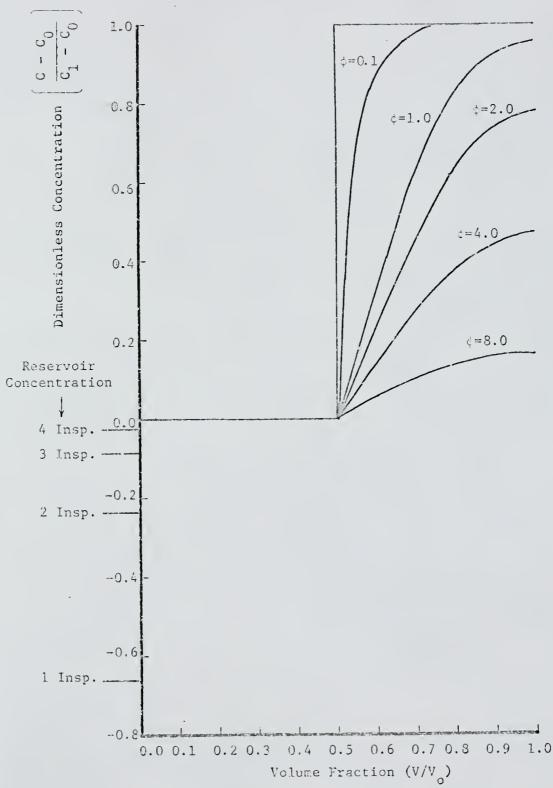


Figure 5.2-2. Diffusion-Controlled Model of Liquid Breathing with Perfect Mixing.

5.3 Theory of Imperfect Convective Mixing

As opposed to the diffusion models developed in the previous section, concentration profiles can occur in the lung, or any mixing vessel, owing to imperfect mixing. Such cases arise in flow patterns which lie between the limiting cases of plug flow and perfect mixing; these are treated in general, by one of two analyses:

- 1) the system is modeled a series of perfectly mixed stages;
- 2) the system is treated as a dispersion problem for which relation of the form of Equation 5.2-2 is developed but with the diffusivity replaced by a dispersion coefficient.

We have chosen to model the lung as a system of perfectly mixed stages in order to avoid any confusion which might develop due to the similarity between the equations for diffusion-controlled and convective mass transport. The dispersion model is a plausible alternative description of convective mixing in the lung, and should be investigated in the future.

In the imperfect mixing model, the initial assumption is made that the lung can be divided into n perfectly mixed stages in series with a fixed number of alveoli attached to each stage as shown in Figure 5.3-1. These stages could be of different volumes but, for the sake of simplicity, it will be assumed that they are all of equal size; thus, the volume of the ith stage can be written as

$$V = \frac{V_{\text{tot}}}{n} \tag{5.3-1}$$

Writing a mass balance across the ith stage for the dye component at

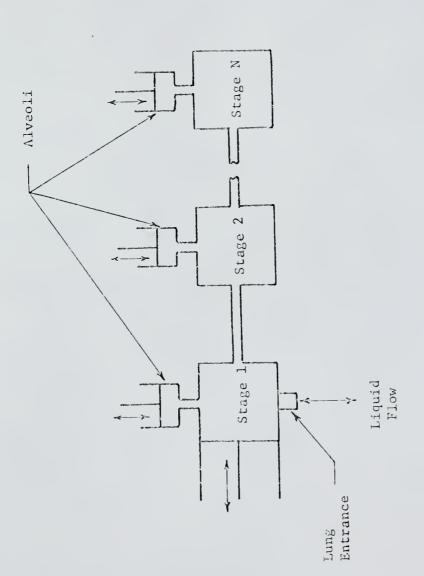


Figure 5.3-1. A Model of the Lung as a Series of CSTRs.

some time t after a step change in dye concentration has been introduced into the lung entrance gives the results

1) during inspiration

$$V \frac{dC_{i}}{dt} = \dot{V}_{i-1}C_{i-1} - \dot{V}_{i}C_{i} - vC_{i}$$
 (5.3-2)

where C_i = concentration of the dye in the ith stage

 \dot{V}_{i} = volume flow rate of the liquid out of the ith stage

v = volume flow rate of liquid into the alveolar sacs connected to the ith stage

2) during expiration

$$V = \dot{V}_{i+1}^{C} + v_{i+1}^{C} + v_{i}^{C}$$
 (5.3-3)

where e = concentration of the dye in the alveolar sacs connected to the ith stage.

Both Equations 5.3-2 and 5.3-3 assume that the flow rates of liquid into and out of the alveolar are the same in all stages and, furthermore, that all volume flow rates are constant.

If at the beginning of an inspiration or expiration the concentration of the dye concentration in the ith stage is C_{10} , Equations 5.3-2 and 5.3-3 can be written, respectively, in matrix form as

$$\frac{d(C)}{dt} = [A](C)$$
(C) = (C)₀ t = 0

and

$$\frac{d(C)}{dt} = [K](C) + [B](e)$$
 (5.3-5)

$$(C) = (C)_0 t = 0$$

[A] is an n+1 by n+1 matrix whose elements are defined by

and

 $A_{i,j} = 0$ for all i and j not specified in previous equations.

 $[\overline{K}]$ is an n x n matrix whose elements are defined by

$$\overline{K}_{ii} = -\frac{V_i}{V}$$

$$i = 1,n$$

$$\overline{K}_{i+1,i} = \frac{V_{i+1}}{V}$$

$$i = 1,n-1$$

$$\overline{K}_{i,j} = 0$$
for all i and j not specified in previous equations.

[B] is an n x n matrix whose elements are defined by

$$[E] = \frac{v}{V} [I] \tag{5-3-8}$$

The solutions to Equations 5.3-5 and 5.3-6 for the inspiration part of the breathing cycle are

(C) =
$$\exp\{[A]t\}(C)_{O}$$
 (5.3-9)

and for the expiration part

(C) =
$$e^{\{[\overline{K}]t\}}((C)_{0}^{+[\overline{K}]^{-1}}[B](e)) - [\overline{K}]^{-1}(B)(e)$$
 (5.3-10)

The dye concentration profile can be determined after any arbitrary number of respirations by solving Equations 5.3-9 and 5.3-10 in step-wise fashion. For the first inspiration, after a step change in inlet dye concentration, the initial concentration profile is essentially constant and equal to some known value (C)₀. For the first and succeeding expirations, the initial concentration profile is set equal to the final value of the concentration of dye in each stage at the end of the previous inspiration. After the first inspiration, the initial concentration of the dye for each inspiration is set equal to the final value obtained during the previous expiration. A graphical representation of resulting dye concentration profiles is given in Figure 5.3-2.

5.4 Transient Dye Penetration in the Lung Experimental Procedure

In this section, the experimental apparatus and procedure used to introduce a step change in dye concentration and observe its penetration into the lung as a function of time will be discussed. Two sets of experiments were performed using two different liquids, normal saline and fluorocarbon FX-80, to liquid-breathe dogs. The experimental procedure in each case was the same, except for the number of respirations completed before draining the lungs. In the case of FX-80, only one experiment was completed because of the scarcity of fluorocarbon dye.

The experimental setup used in all experiments is shown in Figure 5.4-1. It consisted of a one-liter liquid reservoir, an

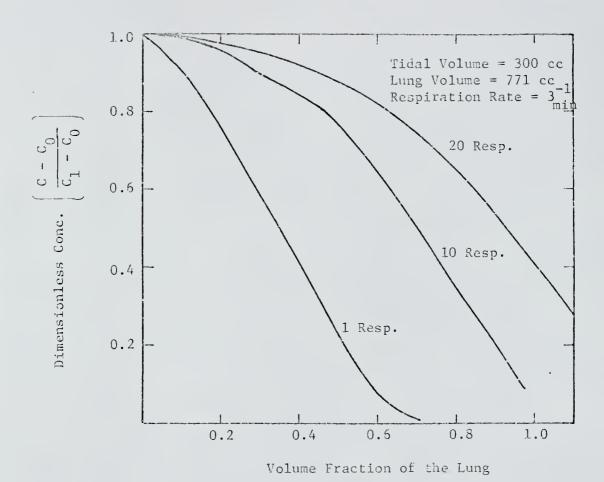


Figure 5.3-2. Response of the Lung to a Step Change in Dye Conc. for CSTR Limiting Case.

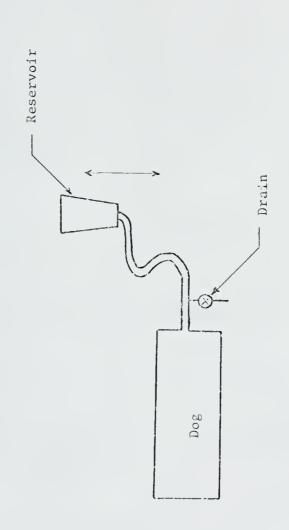


Figure 5.4-1. Experimental Apparatus for the Liquid-Breathing Experiment.

endotracheal tube with a bypass drain and a 6 to 8 kilogram dog.

The experimental procedure used in all experiments was as follows:

- A live dog was placed on the operating table and anesthetized with Nembutal (administered in dosages of 0.25 mg/Kg).
- 2. The dog was intubated with an endotracheal tube which was connected to the liquid reservoir.
- Potassium chloride was administered in a dosage of
 milliliters in order to defibrilate the heart.
- 4. The reservoir and the dog's lungs were filled with liquid (either saline or FX-80) and the lungs were respired by raising and lowering the reservoir until all trapped air was removed.
- 5. When the lungs were completely filled with liquid, 300 cc of saline (350 cc of fluorocarbon) were withdrawn, and the tubing connection to the reservoir was clamped.
- 6. The reservoir was emptied and refilled with saline (or fluorocarbon) containing a known dye concentration.
- 7. 300 cc of the dyed saline (350 cc of the dyed fluorocarbon)
 was introduced into the lung through the endotracheal
 tube.
- 8. 300 cc of saline (350 cc of fluorocarbon) was expired from the lung.
- 9. Steps 6, 7 and 8 were repeated until desired number of respirations had been achieved.

- 10. On final expiration, the lung was drained in 50 cc : aliquots until no more liquid could be drawn out of the lungs by gravity.
- 11. Each 50 cc aliquot of lung fluid was then analyzed for dye concentration.

Each respiration of the dog's lungs required about 20 seconds, 10 seconds for inspiration and 10 seconds for expiration. Approximately 40 seconds were required to replace the dye solution in the reservoir after each breath in the saline experiment, so that the breathing rate was approximately 1 respiration per minute. From experience gained in the saline experiments, we were able to reduce the time required to exchange reservoir liquid to approximately 15 seconds in the fluorocarbon experiment. Thus the breathing rate was increased to 1.7 respirations per minute in the fluorocarbon experiment.

In both fluorocarbon and saline experiments, dye concentrations were measured photometrically with a Klett-Summerson Photoelectric Color meter. A green filter with transmission in the wavelength range of 500 to 570 millimicrons was used in measuring the concentration of Dupont potamine copper blue dye in the saline experiment. A red filter with transmission in the vavelength range of 640 to 700 millimicrons was used to measure the concentration of the fluorocarbon dye produced by Allied Chemical Corporation in the fluorocarbon experiment. In all cases, 10 cc samples were taken for color analysis from each 50 cc aliquot drawn from the lung.

5.5 Results and Conclusions

Figure 5.5-1 shows the experimental dye concentration profile observed in our experiments after one inspiration. Also shown are data taken by West (45) using CO_2 , O_2 and albumin. It should be emphasized that, as shown in Figure 5.5-1, the dyes in our experiment, as well as West's, penetrated to the extremity of the lungs. observation is a strong indication that diffusion is not the ratecontrolling mechanism of mass transport through the bulk of the lung. Furthermore, one cannot match the change in dye profiles as a function of number of respirations (Figure 5.5-2) with the diffusion curves shown in Figure 5.2-1 for then the results of the matching are inconsistent with experimental observations. If a value of the diffusion resistance $\frac{D}{\phi}$ is estimated from the concentration profile after one breath, the diffusion model predicts that the dye concentration throughout the lung will be equal to the inlet dye concentration after ten breaths. If a value of $\frac{D}{\varrho}$ is estimated from the concentration profiles after ten or twenty breaths, the diffusion model predicts that the dye concentration in the lung beyond the total volume will be essentially zero immediately after the first breath. Neither of these conclusions is consistent with our experimental observations.

Comparing the dye penetration curve as a function of the number of respirations with the convective mixing model, it can be seen that if the number of mixing stages is set equal to 20, the experimental results correlate well with the model. In comparing the experimental data with the model, it was assumed that during draining the lung, the

1.00 0.8 0.6 Albumin 0.4 - Blue Dye 0.2 0.0 0.0 0.2 0.4 0.6 0.8 1.0 Tracer

Figure 5.5-1. Concentration Profiles After 1 Inspiration.

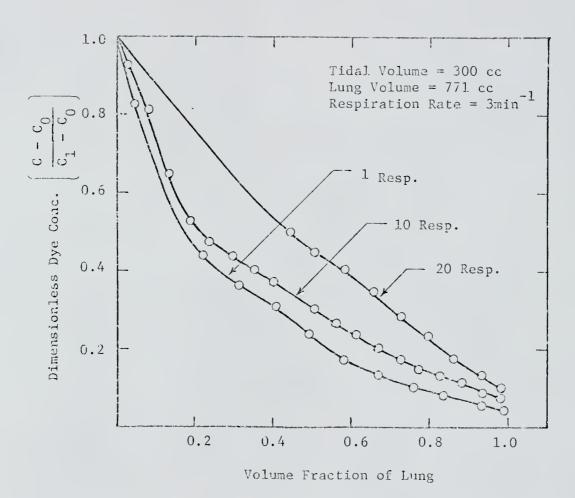


Figure 5.5-2. Results of Saline Liquid-Breathing Experiment.

equations given in Section 3 were valid until the tidal volume had been removed. After this point it was assumed that the lung was drained in plug flow. These assumptions were based upon the fact that initially the volume flow rate at which the lung was drained was approximately equal to that obtained during respiration. As lung draining was continued, the drain rate decreased; thus reducing convective mixing.

Figure 5.5-3 shows the concentration profile in fluorocarbon-filled lungs after 3 respirations. Fitting these data to the convective mixing model, it was determined that 10 perfect mixing stages described the transport process with good accuracy. The fewer mixing stages for the fluorocarbon experiment as compared to the saline experiment are probably due to the shorter time required to change reservoir fluid between each breath. This reduction in time between inspirations most likely increases the agitation (mixing) of fluid in the lung with the result more dye will penetrate into the extremity of the lungs in a given period of time.

The conclusion we have reached from these experiments is that in both saline— and fluorocarben—filled lungs, the mode of mass transfer through the bulk of the lung be it dye, oxygen, or carbon dioxide, is by convective mixing. This is not to say that oxygen and carbon dioxide transport into the blood is not diffusion—centrolled. In fact, it is expected that, in a small layer immediately adjacent to the alveolar walls, gas transport is diffusion—controlled. What must be clarified is that in calculating the rate of oxygen and carbon dioxide exchange in liquid—filled lungs, both diffusional and convective mixing must be

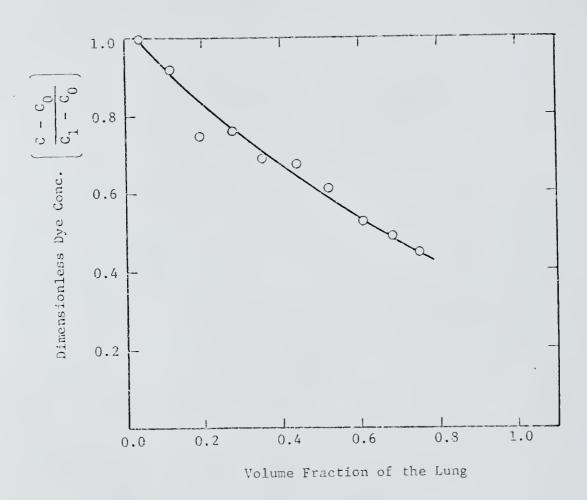


Figure 5.5-3. Results of Fluorocarbon (FX-80)
Breathing Experiment.

accounted for; diffusion alone cannot describe accurately the physical phenomena which occur.

Our recommendations for further research in this area are as follows:

- 1. Extensive liquid breathing experiments with dyes or other tracer materials should be carried out with fluorocarbon, varying respiration rates and tidal volumes to determine the effects these parameters have on convective mixing (i.e., the number of mixing stages).
- 2. The amount of oxygen and carbon dioxide exchange that can be accommodated by convective mixing should be estimated and compared with experimental data.
- 3. In experiments performed in 1 above, a continuous reservoir exchange system should be provided to supply dye solution of a constant concentration without stopping the experiment after each breath to replace reservoir fluid.
- 4. A mechanical device should be employed in all breathing experiments to provide both constant tidal volume and respiration rate during liquid breathing.



APPENDIX A

COMPUTER SIMULATION

In this appendix, the computer programs used in various simulations are listed. An attempt has been made to document the program and instructions are supplied in each of them. Subroutines have been supplied wherever possible to permit easy substitution of relationships to broaden the scope of problems to which the programs can be applied.

The programs in the order in which they appear are:

- 1. Bubble Oxygenator
- 2. Disc Oxygenator
- 3. Convective Model for Liquid Breathing.

The program, Bubble Oxygenator, simulates the operation of the .

Miniprime Bubble Oxygenator. The program, Disc Oxygenator, simulates the operation of the disc oxygenator. Lastly, the program, Convective Model for Liquid Breathing, simulates liquid breathing in the lungs.

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                           N= O IF MASS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            INPUT VARIABLES
IMPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         REALIS, 10) HEME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    FUREAT (F5.3)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           IF(Y) 2,2,1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        BERF= 0.34
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   NED DEM
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AT PRESSURE=P AND TEMPERATURE=I
                         ALPHAE= HENRY'S LAW CONSTANT FOR OZ AT TEMPERATURE=
                                                                                   ALPHAIR REPARTS LAW CONSTANT FOR 02 AT TEMPERATURE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IAU= ALPHAE*VH*(1.0-0.65*HI)*CKU2/((1.0+0.49*HI)*VB)
                                                      PERATUCRITE FI (CC AT STP///CC OF RLUOD)*MM))
                                                                                                                HEMATOCRITE FI (CC AT STR//(CC OF BLOOD)*MM))
                                                                                                                                                                                                                                                                                                                                                                                                                           CALL SATRN(PUZI, PHI, PCOZI, 310., DPYDP, SAIR
                                                                                                                                                                                                                                                                                                                                                                                                CALCULATE TOTAL 02 CONCENTRATION AT INLET
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CALL SATRA(PO2:T, PHI, PCOTI, I, DPYUP, SATIT)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALCULATE ARTERIAL PUZ AT TEMPERATURE= T
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             CALL SATRN(PS, PFI, PCOTI, T, DPYOP, SAIT)
                                                                                                                                                                                                                                                                                                       SATRN(P, PHI, PCUTI, T, DPYDP, SATR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALCULATE ANTERIAL OZ CONCENTRATION
CALL FOLEUP(VB, VGI, ISIZE, VH)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SAT (POZI, PCZIT, T, SATI)
                                                                                                                                                                                                                                           CALCULATE D2 CENCENTEATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CBI= FETS*SATR+ALPHAI*PUZI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            CALL SCLITALPHAI, 310., HI)
                                                                                                                                                                                                          FEM3= HEME#1.091*1.34*HT
                                                                                                                                                                                                                                                                        CALL SATCIPCCTI, PCRII, T.)
VH= GAS ACLUUR VOLUME
                                                                                                                                                                                                                                                                                                                                                                     CREE LEMBASATRAALPHAEAP
                                                                                                                                                                                                                                                                                                                                      SOL1(ALPHAE, T, FI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      IF(1JK-50) 26,7 57)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PS= (PT-P1)/2.3+Pt
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      EC0-180 =803
                                                                                                                                                                                                                                                                                                                                                                                                                                                             SATIE SATR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    --- CJ
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IAU1= ALPHAC*VP*(1.0-C.65*HI)*CKCO2/((1.0+6.49*HI)*VB)
                                                                                                                                                                                                                                                                                                                                                                     CALL PC2(PS: CBC, PHI, FEMB, PCU2I, PU2U, SATU, ALPHAI)
                                                                                    CCN1 - - - OCB* TAU/ (1.0+TAU* (PS-P)/(GBU-CBE))**2
               CBT= UC3/(1.0+TAU*(PS-P)/(CBU+CBE))+CBE
                                                                                                                                                                                                                                                                                                                                                     CALL SAIRN(PO2T, PHI, PCO21,T, DPYDP, SAIDT)
                                                                                                                    DCIDP= CCN1/((CRO-CRE)»(1.0+CON1*CON2))
                                                                                                                                                                                                                                                                                                                                                                                                                         CALCULATE ANTERIAL COZ CONCENTRATION
                                                                                                                                                                                                                                                                                                                                                                                       CALCULATE VENGUS CO2 CONCENTRATION CALL CIO1 (CTUTI, SATI, PCD21)
                                IF(ABS(CBC-CBT)-ALPEAE ) 7,7,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALL CTOT(CTGTG, SATO, PCG20)
                                                                                                     CHN2= (PS-P)/(CBG-CBE)**2
                                                                   COULP= ALPHAE+DBYRP#FFMB
CBUS ALPHAE *PS+FEMB*SATT
                                                                                                                                        PS=PS-DELC/(CCBCP-CCTDP)
                                                                                                                                                                                                                                                                                                 MMITE (6,1010) PS,PT,PL
                                                                                                                                                                                                                                                                                                                                                                                                                                           CALL SCLC(ALPHAC, T, HI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PCC2C= PCC20+DELTA1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PCC2U= PCC20+0ELTA
                                                                                                                                                        IF(25-PT) 5,4,4
                                                                                                                                                                                                           (F(PL-PS) 2,6,6
                                                  DELC= CBJ-CBT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               CFL FA= -0.25
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                DELIAI= 0.25
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              PCC2E= PCG2I
                                                                                                                                                                                                                                                                                                                                    SAFCI= SATT
                                                                                                                                                                                                                                                                                                                   PC2T= PS
                                                                                                                                                                                                                                                                  CONTINUE
                                                                                                                                                                                                                                                                                60 TC 71
                                                                                                                                                                           PL= PST
                                                                                                                                                                                                                              TSG =1d
                                                                                                                                                                                                                                              00 10 1
                                                                                                                                                                                           0.00
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1002 FCRNAT (* ','VENDUS CO2 CONC.= ',E10.4,' ARTERIAL CO2 CONC.= ',E10.4)
1510.4,' VENDOS C2 COMC.= ',LIO.4,' ARTERIAL O2 CONC.= ',E10.4)
1603 FCRMAT (' ','TEMPERATURE ','VENDUS CO2 TENSION ','ARTERIAL CC2 TEN
151CN ','VENSION C2 TENSION ','ARTERIAL O2 TENSION')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1005 FURMAT (* *,4X,F4.0 ,9X,F5.l,1X, MM *,6X,F5.l,1X,*MM*,12X,F5.l,1X,
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1304 FORMAT(* *,4X, *316. *,9A,F5.1,1X, *MM *,8X,F5.1,1X, *MM*,12X,F5.1,1X,
                                                                                                                                                                                                                                                                                                                                                                                                                                 100G FCRMAT ('0','UXYCENAFUR SIZE= ',11,' BLUGD FLOW RAIE= ',F8.2,' CC/
IMIN ','GAS FLOW KATE= ',F3.2,' CC/MIN')
1001 FORKAT ('','HEMATOCKIT= ',F5.3,' PH= ',F5.2,' TEMPERATURE= ',F6.1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        1006 FURMAT (* *, TEMPERATURE *, VENDUS UZ SATURATION *, ARTERIAL OZ
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    1010 FORMATI'O', 'PRUGRAM WILL NOT CONVERGE BEST ESTIMATE OF ARTERIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              FORMAT (* ** * * * * ALL CONCENTRATIONS IN CC AT SIPZEC OF BLCOD*)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        1007 FURMAT (* *,4%,*310. *,12%,F7.5,17%,F7.5)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      (* *,4X, F4.0:13X, F1.5:17X, F7.5)
                                                                                                                                                                                                                                                                                                                      T, PCUII, PCUTU, PUZII, PUZI
                                                                                                                                                                                                                                                                                            PCC21, PCC20, PU21, PU20
                                                         IF(ADS(CTOTU-CTI)-0.30152) 12,12,11
                                                                                                                                                                                                                                    CIOII, CIUIO, CUI, CBO
                         CTT= ECHZ(1.0+FAU1*PCOTO/CTOTO)
                                                                                                                                                                                                                                                                                                                                                                                                                WRITE(6,1008) T,SATIT,SATUT
                                                                                                                                                   ISIZE, VB, VGI
CALL SATCIPCOZU, PCGTO, T)
                                                                                                                                                                                                                                                                                                                                                                                      SATI, SATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        I.P.M. 113%, F5.1,11, 'MM.')
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 1 * NM * + 23X , F5 - 1 , 2X , * MN * 1
                                                                                                                                                                           HI, PHI, T
                                                                                        IF(CTCTO-CTT) 9,9,8
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  1, * DEGREES K*)
                                                                                                                                                                                                                                                                                                                                                                                      WRITE(0,1007)
                                                                                                                                                   MAITE(6,1000)
                                                                                                                                                                                                                                                                                                   WRITE(6,1094)
                                                                                                                                                                                                                                                                                                                             MRITE(c, 1005)
                                                                                                                                                                                                                                        XRITE(6, 1092)
                                                                                                                                                                              WRITE(6,1001)
                                                                                                                                                                                                                                                                                                                                                            MRIFE(6):000)
                                                                                                                                                                                                                                                                     WRITE(6, 1003)
                                                                                                                                                                                                            MRITE(6, 1009)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     LIURATION :)
                                                                                                                         CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               1000
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X= PC2*10.0**10.0*40.024*(310.-TEMP)+0.40*(PH-7.4)+0.06*(ALOCIO(40.0)-A
                                                                                                                                                                                                                                                                                                                                                                                         PARTIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      SATURATION WITH RESPECT TO DXYGEN
                                                                                                                                                                                                                                                                                                                                                                                   PURPESSE TO CALCULATE 02 SATURATION AS A FUNCTION OF 02
                                                                                                                                                                                                                                      CICTI= IGTAL GG2 CONCENTRATION (GC AT STP/CC OF BLOOD)
                                                                                                                                                                                                                                                                                                                                                         SUBRCUTINE SATRN(PDZ,PH,PCD2,TEMP,DPYDP,SATR)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PCG2= CARSON DICKIDE PARTIAL PRESSURG
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PP= -LGG( PYEROCEW ION CONCENTRATION)
                                                                                                                                                                                                                                                                   CTCTI= 0.373-0.0748*SATI+0.00456*PC02I
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              TEMP = TEMPERATURE (DESREES KELVIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       PC2= CXYCEN PARTIAL PRESSURE (MM)
12 15' F7.2' LIMITS ARE' F7.2. F7.2)
                                                                                         SUBBLUTINE CTOT (CTOTI, SATI, PCC21
                                                                                                                                                                                                                                                                                                                                                                                                                                              METHUDO MUDIFIED ADAIR EQUATION.
                                                                                                                                                  PCG21= CGZ PARTIAL PRESSURE
                                                                                                                                                                            SATIL 02 SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CPYCP = DERIVATIVE OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SATRE SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PARTIAL PRESSURE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PUT VARIABLES
                                                                                                                                                                                                      CUIPLE VARIABLES
                                                                                                                     INPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                          INPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         2,12140163
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      A3= 6.707359E;
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               3.15462654
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             3.50222983
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    9.30960915
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              2,39616713
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                ILCGIS(PCC2)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    エヤマ
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125×X+24)-(Xx+4+13×Xxx3+12-Xxxxx+1xx)*(4.0xxxx3+3.0*47*Xx*2+2.*20*A
                                                                                                                                                                                                                                                                                          METHODO EMPIRICAL EQUATION-PHO DISSERTATION, UNIVERSITY OF FLORIDA
(Xx(Xx(Xx(Xxb3)+42)+42))/(Xx(Xx(Xx(Xxx))+A6)+A5)+A4
                                                                            CPYDX= (4.0 xxxx313.0 xA3 x42x2.2.0 xA2xX+A1)/(Xxx4+A7xXxx3+A6xXxx2+
                       EXEP= 10.0**(.024*(310.-TEMP)+0.40*(PH-7.4)*.06*(ALGG10(40.0)-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FOR GAS HOLDUP VOLUME, HOLDUP VOLUME
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          31000 FLOW IS LARGER THAN RANGE OF
                                                                                                                                                                                                                                                                      FURPUSED TO CALCULATE GAS HULDUP VOLUME
                                                                                                                                  2+45)/(Xxx44+A7+Xxx3+A6xXxx2+A5xX+A4)4+2
                                                                                                                                                                                                                                                                                                                                                                                                                                    ISIZE= SIZE CF OXYGENATOR (1,2,3,6)
                                                                                                                                                                                                                                            SUBRCUTINE HULDUPIVB, VGI, ISIZE, VH)
                                                                                                                                                                                                                                                                                                                                                                                VER BECOE FLOW RATE (ML/MIN)
                                                                                                                                                                                                                                                                                                                                                                                                           VOIT GAS FLOW RATE (ML/MIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             1. JE RAFIO CE CAS TO
FMPIRICAL CORRELATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         VES GAS HOLDUP VOLUME
                                                                                                                                                                                                                                                                                                                        , J. W. FALCO, 1971.
                                                                                                                                                                CPYCF= BXCP*CPYCX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        IF(ISI/E-1)1,1,1,10
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      -0.402937 H-5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   5−∃
                                                                                                                                                                                                                                                                                                                                                                                                                                                               CUTPUT VARJABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        0.578214 [-2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   0,246891 E-7
                                                                                                                                                                                                                                                                                                                                                       INPUT VARIABLES
                                                      1 ALCG10(PCU2)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           19942576-
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 -0.726151
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               -0.856446
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      0,399882
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   55T = C.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             VE= VGI/VP
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CONTRACO
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 A1=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            A2=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 コック
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   ,-4
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Alu = C.161250 E-7

Alu = -0.526570 E-9

VICT=360.

IF(VF-11.1) 30,30,31

IF(ISIZE-2) 11,11,20

Alu C.654732 E-3

Alu C.654732 E-3

Alu C.654732 E-3
                                                                                                                                                                                                                                                                                                                                                                   IF(VE-2.42, 30,30,3
Al= 0.973307 E-4
                                                                                                                                                                                                  IF(VC-6.3) 30.30,31
IF(ISIZE-3) 21,21,2
                                                                                                                                                                                                                                                                                                                                  Alu= -0.268215 E-2
All= 0.142629 C-2
VTCT= 470.
                                                                                                                                                                            Ali= -0.850442 E-7
                                                                                                                                                   A9= 0.160734 E-5
A10= 0.796249 E-6
                                                                                                                                                                                                                         0.349850 E-5
1.20860967
-1.1010163
                                                                                                                              A7= -0.201014E-3
A8= -0.124458 E-4
                                                                                                                                                                                                                                                                                               A7= 0.987895 E-2
A8= -0.209601 E-
                                                                                                                                                                                                                                                                                                                       49= 0.431817 E-3
                                                                                 C.600549 E-1
                                                                                                                  0.223350 6-2
                                                                                                      1-30508-1-0-
                                                                                                                                                                                                                                                                        0.19409794
                                                                                                                                                                                                                                                                                    0.255293
                                                                                                                                                                                        VTCT-375.
                                                                                                      75m
                                                                                                                                                                                                                           114
                                                                                                                                                                                                                                      A2=
                                                                                                                                                                                                                                                  13=
                                                                                                                                                                                                                                                              24=
                                                                                                                                                                                                                                                                         11 07 <
                                                                                                                                                                                                                                                                                      # 97
                                                                                                                                                                                                                20 21
                                                                                                                                                                                                                                                                                                                                                                                  25
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30 VF= A1:42*VC+A3*(VO**2)+A4*(VO**3)+A5*(VO**4)+A6*(VO**5)+A7*(VO**6
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      D2 CONC. ,
                                                                                                                                                                                                                                                                                                                                                                  CICTO = TOTAL CO2 CONCENTRATION (CC AT STP/CC OF SLCOD)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    PURPESED TO CALCULATE UZ PARTIA! PRESSURE GIVEN TOTAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        EMPERATURE, PH, CO2 PARTIAL PRESSURE AND HEMATOCRIT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SUBSCUIINE PU2(PS, CB, PH, PEMB, PC021, PU20, SATU, ALPHA)
                                                                                                                                                                                                            1)+A8*(VD**7)+A9*(VD**8)+ A1C*(VD**9)+A11*(VD**10)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  OF UZ PARTIAL PRESSURE
                                                                                                                                                                                                                                                                                                                                                                                                                                            PCU2C= (CTDFU-0.373*0.0743*SAT0170.00458
                                                                                                                                                                                                                                                                                                                             SUBACUTINE PCOZ(CTOTO, SATO, PCOZO)
                                                                                                                                                                                                                                                                                                                                                                                                                           PCG20= CO2 PARTIAL PRESSURE
                                                                                                                                                                                                                                                                                                                                                                                       SATC= 02 SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PS= INITIAL ESTIMATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CE TOTAL DZ CONC.
                                                                                                                                                                                                                               VH= VTCT *VEZ(1.C*VF)
                                                                                                                                                                        IF(VE-2.2) 30,50,31
元
十
山
                                                                                                               1
1
                                                                                                                                 All=-0.582683 E-2
                                                                                                                                                                                                                                                                                                                                                                                                         CUTPUT VARIABLES
                                                       0.821756 E-1
                                                                         A8= 0.334081 E-2
                                                                                                                                                                                                                                                                                                                                                INPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  INPUT VARIABLES
                                      -0.1458537
                  A5= -0.107454
-0.534271
                                                                                              A9= -C.981349
                                                                                                               A10= 0.104377
                                                                                                                                                      VTCT= 980.
                                                                                                                                                                                                                                                                      VH= C.O
                                                                                                                                                                                                                                                                                          23
                                                                                                                                                                                                                                                                        31
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           000000
                                                                                                                                                                                                                                                                                                                                                    00000
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0.2391992

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1010 FORMATI'O', 'PROGRAM WILL HOT CONVERGE BEST ESTIMATE OF ARTERIAL 12 IS', F7.2, 'LIMITS AKE', F7.2, F7.2)
                                                                     HEMB= CONC. OF HEMBCLUBIN IN BLOOM (GM/CC)
                                                                                                                                                                                                                                                                                         CALL SATRK(PS, PF, PCO2I, 313., DPYDP, SATO)
                 PCCZI - CCZ PARTIAL PRESSURE
SAIO- FRACTICMAL SATURATION OF UZ
                                                   ALPHA = SOLUGILITY OF G2 IN BLOOD
                                                                                                          POZU= PARTIAL PRESSURE UF OXYGEN
                                                                                                                                                                                                                                                                                                                                             PS= PS+; CB-CS]/(LPYDP#HEMB+ALPHA)
                                                                                                                                                                                                                                                                                                                            IF(ABS(CB-CS)-0.000003) 10,10,3
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SCLI(ALPFAO, T, HU)
PER TENSOR I'M CONC.)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     70 WRITE (6%1010) PS.PT.PL
10 Pt.2C= PS
                                                                                                                                                                                                                                                                                                           CS= SATO*PEMB+ALPHA*PS
                                                                                                                                                                                                                                                                        IF(IJK-50) 20,20,70
                                                                                                                                                                                                                  PS= (P1-PL)/2.04PL
                                                                                        CUTPUT VARIABLES
                                                                                                                          NEW TONS
                                                                                                                                                                                                                                                                                                                                                              IF(PI-PS) 4,4,5
FL= PST
                                                                                                                                                                                                                                                                                                                                                                                                                    IF(PS-PL) 6,6,2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  SUBRCUTINE
                                                                                                                                                                                                                                                       1JK= 1JK+1
                                                                                                                            FLT1-CD0 :
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    VARIABLES
                                                                                                                                                              PT = 800.
                                                                                                                                                                                                                                                                                                                                                                                                                                     PT= PST
                                                                                                                                                                                                                                                                                                                                                                                                                                                        GC TC 1
                                                                                                                                                                                                                                     PST= PS
                                                                                                                                                                                                 5 37 00
                                                                                                                                                                                                                                                                                                                                                                                                  GC 1C 1
                                                                                                                                                                                IJK= O
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ALPHACE HENRY'S LAW CONSTANT AT FEMPERATURE I AND HEMATOCRITE
                                                                                                                                                                                                           ALPHACH HENRY'S LAW CONSTANT AT TEMPERATURE I AND HEMATOCRITH
                                                                                                                                                                                                                                                                                                                                                                                                                                                 37 DEGREES C (MM)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              (NN)
                                                                                                                                                                                                                                                                                                                                                                                                                                             PUZU= G2 PARTIAL PRESSURE AT TEMPERATURE=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             AT TEMPERATURE=
                                                                                                                                                                                                                                                        KELVIN
                                                                                                                                                                                                                                                                                                                                                                                                                                                                  TH CHERATING TEMPERATURE (DEGREES KELVIN)
                                           KELVIN)
                                                                                                                                                                                                                                                                                                                  ALPHIC=(4.26475738-0.026607855*T)*ALPHAC
                                                                                0.0000339*HB+0.0000275*(1.0-HB)
                                                                                                    ALPHAC= (8.971488-0.02566618+T)*ALPHAD
                 (CC OF O2 AT STRZCC OF BLOOD)

T= OPERATING TEMPERATURE (DEGREES
                                                                                                                                                                                                                                                     T= CPERATING TEMPERATURE (DECREES
                                                                                                                                                                                                                                                                                            ALPHAC= 0.000557*HG+C.00067*(1.0-HO)
                                                           FC= HEMATCCRIT (VOLUME FRACTION)
                                                                                                                                                                                                                                                                           HC# HEMATUCRIT (VCLUME FAACTION)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                PUZI= PUZO*(10.0**(.0313*(I-316.1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PG27= P020*(10.0**(.0237*(7-310.)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   PC27=PC26*(10.0**(.0367*(T-316.)))
                                                                                                                                                                                                                               (CC JF CU2 AT STP/CC OF BLOOD)
                                                                                                                                                                                                                                                                                                                                                                                  SUBRUDILLE SAT(POZO, POZI, I, SATW)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           PIZT = C2 PARTIAL PRESSURE
                                                                                                                                                                   SUBRUUTINE SCLC(ALPHAC, T, HO)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               IF(SATN+3.90) 1000,2000,2000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            IF(Sain-0,95) 3000,4000,4000
                                                                                                                                                                                                                                                                                                                                                                                                                         SATN# 02 SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CUTPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                     INPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        GO TC 5000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     GC 1C 5060
                                                                                                                                                                                       VARIABLES
                                                                                 ALPHAC=
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            2000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 3000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      1000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           4000
0000
                                                                                                                                                                                         00000
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SUBROUTINE SATC(PCUZC,PCDTO,T)

VARIABLES

FCC2U= CO2 PARTIAL PRESSURE AT 37 DEGREES C

PCLTG= CO2 PARTIAL PRESSURE AT TEMPERATURE=

T= TEMPERATURE (DEGREES MELVIN)

PCGTC= PCG2O*(10.0**(.0221*(T-310.)))

RETURN

ENU

* ш ш <u>n</u> GIVEN NUMBER DIMENSION X(120),XZ(20),XEXIT(570),ZEXIT(500) Unmwen q,T,N,XZ,XEXIT,ZEXIT,TEMP,PHI,PARI,CONI,CONZ,CON3,Tl - 1 IF VOLUME FRACTION OF HEMOGLOBIN IN THE RED CFLL IS EDUAL TU 0.34 ~[CALCULATE DXYGENATION OF BLCOD FOR TEMPE OPERATING TEMPERATURE (DECREES KELVIN 138 ш С PC2I= VENGUS D2 TENSION (MM)
PCC2I= VENGUS COZ TENSION (MM)
ONEGA= AOTATICNAL SPEED OF THE DISCS V= VOLUME OF PLOOD IN THE (TH STACE = 0 IF THIS VOLUME FRACTION IS TO AT= LUMBER OF STAGES VS= VCLUME FLUW OF BLOOD (GC/SPC) PH 02 PRESSUREH USUALLY 760 MB DISC DXYGENATOR RIM INDER RADIUS OF THE DISC RZM BUTER RADIUS OF THE BISC ME DECISION VARIABLE READ IN AS DATA TH SHOUNDA HEAD COLPUT VARIABLES PUT VARIABLES TXTERNAL FOUR FUNPUSED TO DISC STAGES

PCZ= UZ TEMSIČN IN THE 11B STAGE (MM) SATC= 02 SATUPATION IN THE ITH STAGE PCCTU= COZ TENSION IN THE ITH STAGE CTGTO= CUZ GONGANTRATION IN THE ITH STAGE

THE NUMBER OF PEACE

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CALCULATE TEMPERATURE CORRECTION , GAMMA, FOR PCOZ
PERFORMS DIFFERENTIAL CALCULATION FOR ADDUM
STOPES JUTPUT FROM SUBREUTINE ADDUM
                                                                                                                                                                                                                                                               CURFECTS COZ TENSIONS TO TEMPERATORES OTHER THAN
                                                                                                                                                                                                                           CURRECTS OF TELSIONS TO TEMPERATURES CTHER THAN
                                                                                          CALCULATE COZ TENSION SIVEN COZ CONCENTRATION
                                                                      CALCULATE UZ TENSION GIVEN OZ CONCENTRATION
                                  CALCULATE IST DEMIVATIVE OF SATUKATION WITH
                                                                                                                                                                                                        CALCULATES COD CONC. AT A GIVEN COD TENSION
                                                                                                                                                                                                                                                                                                                          0.02
                                                                                                                                                                                                                                                                                                       05
                                                                                                                                                                                                                                                                                                       FOR
                                                                                                                                                                                                                                                                                                                         F C X
                                                                                                                                                                                                                                                                                                   CALCULATES HEMRY'S LAW COFFFICIENT CALCULATES HEMRY'S LAW COFFFICIENT
                   SATURATION
                                                                                                                                                                  CALCULATES CO2 DIFFUSIVITY
                                                                                                                                                                                    CALCULATES OF DIFFUSIVITY
                                                                                                                                                                                                                                                                                                                                        FINITE DIFFERANCE ROUTING
                                                     375PECF 10 02 3ENSION
                 CALCULATE TRACTIONAL
                                                                                                                                                                                                                                                                                                                                                                                                 P, PEI, HI, PUZI, PCUZI
                                                                                                                                                                                                                                             37 DUCREES C
                                                                                                                                                                                                                                                                                  37 PECREES C
                                                                                                                                                                                                                                                                                                                                                                                                                 CMECA, VF, V, K1, K7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  CALL SCLI(ALP: AI, ICAP, AI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     SCLI(ALPHAR, 317., HI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       SCLC(ALPHAC, TEMP, HI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             PENE= 0.34
FIMP= 1.34*1.09[*HEME*HI
                                                                                                                                                                                                                                                                                                                                                                                                                                   W, NI, TEKP
SUBRCUTINES USEC
                                                                                                                                                                                                                                                                                                                                                                                            REALIS, 102) (
REALIS, 102) (
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PE/C(5,103)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                      18(7) 2,2,1
                                                                                                                                                                                   CIFFO
                 12 17 17 5
                                   CERVO
                                                                                                           SCHER.
                                                                                                                                                                  CIFFC
                                                                                                                                                                                                                                                                                                                                      ALDUK
                                                                                          102
                                                                                                                                                                                                                                                                                                   255
                                                                                                                                                                                                       CICT
                                                                                                                                                                                                                                                                                                                      SULC
                                                                                                                                                                                                                                                               SATL
                                                                                                                                                  JALL
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XZI2)= ((CPTSP/(3.1416*LU2))**0.5)*(PO2[I-P)*2.0
                                                                                                                              CCN3= ((1.0+10.0**(PFI-PK))/(1.21/*0C02))**0.5
                                                                                                                                                                                                                                                                     CALL SATC(PCC21,PCUTI,TEMP)
VTEW2= ALPHAP*PCOTI*(1.0+10.0**(PHI-PK))/1.217
                                                                                                                                                      CALL SATINIPOPI, PHI, POUZI, 310., SATI)
                                                                                                                                                                                                                                                                                                                                                                                                            MPIRE(5, 106) 90271, SATI, PCJII, CTOTI
                                                                                                                                                                                                                                                                                                                CALL SATRN(P,PHI,PCCTI,TEMP,SATE)
CBd= SATE*HEMB+ALPHAI*PC2TI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CALL DENVC(P, PHI, P.C, TEMP, OPYDP)
                                                                                                                                                                                                                         CALL SAT(POZI,PCZTI,FEMP,SATI)
CALL GTOT(CTUTI,SATI,PCOZI)
                                                                                                                                                                             CUI= SATI*PEMB*ALPPAE*PU2I
SCLC(ALPHAP, TEAP, D.C)
                                                                                     PK= 6.1-3.000*(310.-TENP)
                 DIRECTORCY, TEMP, FI)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                 PPTOP= OPYDP*PARITIO
                                                                                                                                                                                                                                                                                                                                                               MRITTE(0,154) VB, TEHP
                                                                                                                                                                                                                                                                                                                                                                                                                                VFER3= PG2FT
TMAX= 2.5*(002)**0.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FELTAH (R2-31)/20.
                                                                 FARIT HEMBIALPHAI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  X1(2)= X1(2)*1.5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         (2)/2/ = SIBOX
                                                                                                        CCVI- -2.07002
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               EG 99 I=1,NT
CG 999 IPK=1,1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                              F= TYAX/333.33
                                                                                                                                                                                                                                                                                                                                                                                     NKI FE(6, 105
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CONZE POUTI
                                                                                                                                                                                                     VTEMI= COI
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    TZ : 38 7.0
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                           ITC= 16
                  1.01.6
                                         CALI
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TILIN- (2.0*ARSIN(RE)+3.1416)/(2.0*3.1416)
                                                                                                                                                                                                                DENON= (X5X11(20)-YGUES)/(X2(2)-XGUES)
                                 CALL ADDUM(H, ITC, TZEND, THAX, XZ, F, UUT)
                                                                                                                                                                                                                                                 XZ(2)= (7(2)+(PC2TI-XEXIT(2C))/DENUM
                                                  IF (APS (KEXIT (20)-PU2TI)-1.0)11,5,5
                                                                                    IS(XEXIT(20)-PG2TI) 8,11,7
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CELTA1= TM*+0.5*Th4X/10.0
 PENTER TEMPS JARRA
                                                                                                       %2(2)= %2(2)+C.1*%2(2)
%0015= %0X1F(20)
                                                                                                                                                            X2(2) = X2(2) - 0.1 * X7(2)
                                                                                                                                                                             YGUTS= XLXII(20)
                                                                                                                                                                                                                                                                   COCULIXUX FOUNDA
                                                                                                                                                                                                                                (2)7X =SEODX
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     TWE THETAZUATECA
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        UX= UXIDELIAL
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          PCZ= XEXII(J)
                                                                   IF(AJ) 6,6,9
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        US 15 3×1,20
                                                                                                                                                                                                                                                                                                                                                                                                                               BC 13 K=1,29
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 以上了一日 中日 中日
                                                                                                                                                                                                                                                                                                                                                         0.
                                                                                                                                                                                                                                                                                                                                                                          VCC18= 0.0
VCC21= 0.0
                                                                                                                                                                                                                                                                                                                                       "CLUJ"
                                                                                                                                                                                             77 21 29
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  S / 5 3 - 1 8
                                                                                                                                                                                                                                                                                                                                                                                                                                                 いっては大山
                                                                                                                                                                                                                                                                                                                      CLNTINUL
                                                                                                                                                                                                                                                                                     NU= NU+1
                                                                                                                                                                                                                                                                                                    5 JT 30
                                                                                                                                                                                                                                                                                                                                                          VCC20=
CALL
                                                                                                                                                                                                                                                                                                                                                                                                             7 50
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SATURATION . "CO2 TENS
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FURNAT ('1:, '3LCCO FLOW RATES ', F7.1,' CC/MIN ', 'TEMPERATURES
                                                                                                                                                                                                                                                                                              , SAIO, POZ, ALPHAI, P, HEMB
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              IICN (MM) ","CUL CONC. (CC/CU)")

10 FORKAT (" ",3X,"F",6X,F5.1,11X.F6.4,FX,F5.1,13X,L13.7)

17 FURMAT (" ",1X,12,5X,F5.1,11X,F6.4,8A,F5.1,15X,F13.7)
                                                                                                                                                                                                                                                                                                                                                                          VTEM2= ALPHAP*PCGTO*(1.0+1C.0**(PHI-PK))/1.217
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         105 FURNAT (*1: , STAGE ', 'UZ Teasion (MM) ', 'DZ
                                                                                                                    CCC2= ALPFAP*PCC2*(1.6+16.6**(PHI-PK))/1.217
                                                                                                                                                                     VCC:Xx VCGIN*4.0*3.1416*R*VTEN1*DELTA*DELTAI
                                                                                                                                                                                        VCL2. = VCO2I*4, 0*3.1416*8*VIEM2*DELTA*DELIAL
                                                                                                                                            VCU2C+ VCR2U+4.0*3.1416*R*CUJZ*DELFA*DELFA
                                                                                            VCCOT= VCOUT+4.0*3.1416*R*CU2*D*L1A*DEL1A1
                                                                                                                                                                                                                                                                                                                       CALL BC02(CFCTO, TEMP, SATO, PCUTO, GAMNA)
                                                                                                                                                                                                                                                                                               CALL O2(CSO, TEMP, PCOTI, PHI, VTEM3, CB!
                                                                                                                                                                                                                                                                                                                                                                                                   WRITE(6,107) I, PC2, SATG, PCUTO, CTDTO
                                                                                                                                                                                                                                                                         CTCTC= CTDTI+OMEGA*(VCD20-Vu021)/VB
                                           CALL SAIRN(PL2, FPI, PCO2, TEMP, SATJ)
CO2= SATJ*HEME+ALPHAI*PU2
                                                                                                                                                                                                                                                  CEL= CRI+UMBCA*(VCUUT-VCGIA)/VB
CENERCONSECTION CONTRACTOR
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             SCRNAT (TIPIO,2510.0)
                    PCC2= PCCTI*ERF(PPE)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     1.8 8333930 .41.631
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FORMAT (SFLO.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               FORMAT (SF10.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      FCKPAT (FIG. 0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CIUTIS CTOTU
                                                                                                                                                                                                                                                                                                                                                                                                                                                        פררונ= הכנור
                                                                                                                                                                                                                                                                                                                                                                                                                               FL2TI= PC?
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                SATI= SATE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   VTLYS= PLZ
                                                                                                                                                                                                                                                                                                                                                         VIENI= COU
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              CONTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                      CBI= CBO
                                                                                                                                                                                                                            CUNTINUE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                001
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SOUNTINE (A,F)
DIVENSION A(A) NO (1201,XZ(ZC),XCYIT(VUC),ZEXIT(500)
GUYNER VII,K,K,K,YENII,ZEXII,FERP,PHI,PARI,CONI,CONZ,CON3,TI
                                        SUBREUTINE UZ (CPL, T, PCUZ, PH, PUZI, CBI, SATO, PUZ, ALPHA, P, HEMB)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                        SUJREUTINE SCUZ(CTUI,T,SNT,PCD2,GAMMA)
PCL2= ((CTUT-Oug/3*SUD748*SNT)/C.f0456)*(1.0/GAMMA)
                                                                                                                                     FUZ= (CGC-CGK)/(FFRF#D-YDP+ALPEA)*POZR
                                                                                                                                                                                                          IF(AES((GBO-CBR)/GEB)+P.SCBUI)15,10,2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    CALT DERVOLX (1), PHI, CONZ, TEMP, SPYDP)
                                                                                                                  CALL BEYYO(PU28, Pr. POUZ, T. DPYCP)
                                                                                                                                                            CALL SATEN (PC2, 28, PCU2, 1, Salut
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         SUBSCUTINE POWER (T.CANRA)
                                                                                                                                                                                                                                                                                                                                  PO23= (PU28-PO21)/2.3(PU21
                                                                                                                                                                                     CARE PERCASATOANEPERA
                                                                                                                                                                                                                                                         PO2R= (P-PO2R)/2. CPU2R
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         0.1+12.00 dCAdC 401161
                                                                                                                                                                                                                                                                                                             IF(PU2-PO21) 5,6,6
                                                                                                                                                                                                                                    IF (PC2-P) 4,3,3
                                                                                            PC28= FU21
                                                                    CENT CRI
                                                                                                                                                                                                                                                                                                                                                                                                        (1)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         22.07.55
                                                                                                                                                                                                                                                                                                                                                                                                                                  RETURE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             KETURA
11/10
                                                                                                                                                                                                                                        01.0
                                                                                                                                                                                                                                                                                                              J 5
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LH2C= -677.23381-5+4.4588465-5*TEMP-7.307692E-8*TEMP**2
CP= 0.58*D420
                                                CIMENSION X(120), N2 (20), KEXIT(500), ZCXIT(500)
                                                                                                                                                                                                                                                                                                                                                                                                  PURPOSE O TO CALCULATE CG2 LIFFUSIVITY
                                                                                                                                                                                                                                                                                                                                                                                                                                                         TEMPE TEMPERATURE DECRESS KELVIN
                                                                                                                                                                                                                                                             TEMPE TEMPERATURE DEGREES KELVIA
                                                                                                                                                                                                                   PURPUSEU TO CALCULATE UZ DIFFUSIVITY
                                                                                                                                                                                                                                                                        FI= HEMATOCAIT (VOLUME FRACTION)
                                                                                                                                                                                                                                                                                                                                EC2= CP*(1.0-HI*P.69)/(1.0+6.49*HI)
                                                                                                                                                                                                                                                                                                                                                                        SUBREUTINE DIFFE(PC22, TEMP, FI)
                                                                                                                                                                                          SUBRCUTINE DIFFCICO2, TEMP, HI)
                                                                COMMENT, X, XZ, NEXIT, ZEXIT
                                                                                                                                                                                                                                                                                        CC2= C2 DIFFUSIVITY
A(Z)= CONIFTEDPICP*X(Z)
                                        SUBACUTINE OUT(K)
                                                                                IF(K) 1,2,1
                                                                                                                                                                                                                                                                                                                                                                                                                                               VARIABLES
                                                                                                                                      XEXIT(J)=
                                                                                                                                                     =(f)11X37
                                                                                                           GO 1: 10
                                                                                                                                                                                                                                                                                                                                                 RETURN
                                                                                                                           J= J+1
                                                                                                                                                                   RUTURN
               RETURA
                                                                                                                                                                    O FI
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PURG = 02 PARTIAL PRESSURE AT TEMPERATURE = 37 DEGREUS C (MM)
                                                                                                                                                                                                                                                                                            81000)
                                                                                             CH2C= -677.2039.-5+4.458846c-5*TEMP-7.307592E-8*TEMP**2
                                                                                                                                                                                                                                                                                            STP/CC OF
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     AT TEMPERATURES T (PM)
                                                                           CD= 1.0169+1.0694355985*DENP-0.003543120*DENP**2
                                                                                                                                                                                                                                                                                           CTOTI= TOTAL CO2 CONCENTRATION (CC AT
                                                                                                                                                                                                                                                                                                            CTC11= 0.373-0.0744*SATI+0.00456*PCU21
                                                                                                                                    [CC2= CP*(1.0+)[*0.69]/(1.0+0.49*H])
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  PC2T= PJ2G*(10.0**(.0313*(T-310.)))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         PO2T= PO20*(17.0**(.0237*(T-310.)))
HIE HEMATONAIT IVOLUME FRACTION
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     IF(SATN-U.90) 1000,2000,2000
POZT=PC2U*(19.0**(.0307*(T-310.)))
                                                                                                                                                                                            SULACUTIAE CTOT (CTOTI, SATI, PCO21)
                                                                                                                                                                                                                                                                                                                                                                       SUERCUTINE SAT (PCZU, POZI, I, SAIN)
                                                                                                                                                                                                                                   PCC21 = CO2 PARTIAL PRESSURE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                     PURTS CR PARTIAL PRECSURE
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                TELSATINHO, 950 3000, 4000, 4000
                  CCC2= COP BIFFUSIVITY
                                                                                                                                                                                                                                                    SATI= 02 SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                             SATING OR SATURATION
                                                                                                                                                                                                                                                                                                                                                                                                                                                 CUTPUT VARIABLES
                                                                                                                                                                                                                                                                       CUTPLT YARIYBLES
                                                                                                                 CF- 0.53*CH20/UE
                                                                                                                                                                                                                                                                                                                                                                                          INPUT VARIABLES
                                                                                                                                                                                                               INPUT VARIABLES
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                               6C 1C 5000
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     COS4 01 00
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T AND HEMATOCRIT=
                                                                                                                                                                                                                                                   AND HEMATOCRIT=
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                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         ALPHAC= HENRY * S LAW CONSTANT AT TEMPERATURE
                                                                    PCCIO- CO2 PARTIAL PRESSURE AT TEMPERATURE=
                                                                                                                                                                                                                                                   ALPHACE HEMRY'S LAW CONSTANT AT TEMPERATURE
                                              37 DEGREES C
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ALPFAC= (9.26475738-1.0266076554114ALPHAC
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                SUBPCUTINE SATRA (PO2, PH, PCO2, TEMP, SATR)
                                                                                                                                                                                                                                                                                                                                                     ALPHACE 0.0300329*HC+0.0000275*(1.0-HO)
                                                                                                                                                                                                                                                                                                                                                                             ALMEAC= 18.971488-0.02566618*T)*ALPHAD
                                                                                                                    PCUTU= PCC23*(10.0**(.0221*(T-310.1))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ALPEACE 0.000557*FH+0.000067*(1.0-H0)
                                                                                              TH THASE (DECRETS KALVIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    HIT HEMATUCHIT (VOLUME FRACTION)
                                                                                                                                                                                                                                                                                                                              FOR MEMATOCKIT (VOLUME FRACTION)
                                                                                                                                                                                                                                                                                                   IN TEMPERATURE (DEGREES KALVIN)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          TH TEMPERATURE (CEGNELS KALVIN)
                                               PCC20= CO2 PARTIAL PRESSURE AT
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    (CC OF CUZ AT STP/CC OF BLOOD)
                                                                                                                                                                                                                                                                           ICC OF 02 AT STRYCE OF BLOSO!
SATC (PCG20, PCGT0, I
                                                                                                                                                                                                                                                                                                                                                                                                                                                           SULC (ALPMAC, T, HO)
                                                                                                                                                                                                   SCLI(ALPHAO, 19HU)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        3.53222c3
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                                                                                                                                                                                                   SUBRECTIVE
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SUCACUTINE
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                                                                                                                                                RETURN
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3 X= PC2*10.0**(0.024*(310.-)EMP)*(.49*(PH-7.4)*0.06*(ALOG10(40.0)-A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             X= PC2*10.0**(0.024*(310.-FEMP)*0.40*(PH-7.4)*0.06*(ALOG10(47.0)-A
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                        PPYEX=114.0×X3+2.0×A3*X2+2.0×A2*X+A1)-(X4+A3*X3*A2*X2+A1*X)*14.0*X
                                                                                                                                                                            (X+(X+(X+A3)+A2)+A1))/(Xx(Xx(X+A7)+A2)+A6)+A6)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                         CAUP= 10.0**(.074*(310.-TEMP)+0.40*(PH-7.4)+.06*(ALUG10(40.0)
                                                                                                                                                                                                                                             SUBRCUTINE DERVETPUZ, PH, PCUZ, TEMP, DPYDP)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                              13+3.0+27+X2+2.0+A6+X+A5)/P1)/P1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    Pl= X4+A7+X3+A6+X2+A5+X4A4
                                        IF(PCC2-4.0) 1,1,2
                                                                                                                                                                                                                                                                                                                                                                                                                        IF (1'CC2-4.0) 1.1,2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    ロアソロドー ロスロドキロコイロス
AC= 2.396167.3
A7= 6.716443.01
                                                                                                                                                                                                                                                               A3= 8.532229E3
                                                                                                                                                                                                                                                                                       2.121401E3
                                                                                                                                                                                                                                                                                                                                                                              2.39616/23
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                                                                                                                                                                                                                                                                                                                                                                                                   A7= 6.71044121
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                             ALCELOIVARB));
                                                                                                                                                      ILCG10(VARB)))
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                                                                                     CC TC 3
VARB= PUC2
                                                                                                                                                                                                                                                                                                                                                                                                                                                                 CC TC ?
VAR Ja PCC2
                                                                VAR3= 4.0
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              ACDUME SIFFERENTIAL COUATION SOLVER IN FURTRAN IV. SOLVES A 20
ORDLA DIFFICRENTIAL EQUATION USING FOURH ORDER RUNGE-RUTTA TO
START AND ADAMS-BASHFORTE PREDICTOR CORRECTOR TO RUN, MUST
CEAUGE DIMENSION OF X, XZ, AND C TO CHANGE ORDER, CALLS F TO GIVEN
CERTVATIVE OF THE STATES IN TERMS OF THE STATES X(1) AND TO
ALSO CALLS OUTPUT RUSTIVE OUT(R) EVERY ITO INTEGRATION STEPS.
                                                                                     T & BULLCCK REVISED 1/15/66,5/17/69,8/14/69,10/24/70 EIMENSION XZ(20),6(20,6),X(20,6)
       SUBRCUTINE ACTURIALICH, ITU, IZERO, TMAK, XZ, F, JUI)
                                                                                                                                                                                                                                                                                                                                              X(K,1) + C(K,1
                                                                                                                                                                                                                                                                                                                          = X(K,5)*FH
= X(K,1)
                                                                                                                                                                                                                                                                                                           CALL JUT(1)
                                                                                                                                                                                                                                                             X(1,6)=X7(1)
CALL F(X(1,5),1)
CALL F(X(1,2),0)
                                                                                                                                                                                                                                                                                                                                                                                  K=1, N
                                                                                                                             F = ARS(AITCH)
                                                                                                                                                                                                                                                                                                 IF(ITC)5,5,4
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                                                                                                                  COMPON NOTAX
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X(K,1)
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                                                                                  X(K,1)=X(K,4)f(C(K,1)+2.0*C(k,2)+C(K,3)+0.5*C(K,4))*0.33333333ADCU
X(K,6) = X(K,1)
                  ACDU
                           ACDU
                                    ACEU
                                                                     ADDU
                                                                              ABBU
                                                                                                                                                  ABBU
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                                                                                                                                                                                                               X(K, 1) = X(K, 6) + D*(55.0*X(K, 5) - 59.0*X(K, 4) + 37.0*X(K, 3) - 9.0*X(K, 2)
                                                                                                                                                                                                                                                                 X(K,6)=X(P,6)+[x(9.0*X(K,5)+19.0*X(K,4)-5.0*X(K,3)+X(K,2))
LIK(2) = PC.C(h,2)
XIK,1) = X(K,6) + C
L F(C(1,3),3)
                                             X(K,6) *
                                                                               1 C(K,4)*F
                                    H T*C(K, 3)
                                                                                                        1SUT = 1SET*1
6C TC (10,12,17),1SET
CALL F(<(1,5),0)</pre>
                                                                                                                                                                                                                                                         16 8 = 2,
                                                                                                                                                                                                                                                                          X(K, 1) = X(X, 6)
                                                                                                                                 11 K = 1:A
                                                                                                                                                                                                                                        CALL 1 (< (1, 5); 1)
                                                                                                                                                           F(X(1,5);0)
                            大口による
                                                             CALL F(C(1.4),1)
                                                                                                                                                                   FC 13 K=1,N
X(K,4)=Y(K,5)
                                                                                                                                                                                                       15 K-1, R
                                                                                                                                          X(K,S) = X(K,S)
                                                                                                                                                                                                                        X(K, Z)=X(K, 3)
                                                                                                                                                                                                                                1(K,3)=4(K,4)
                                             11
                                   N(X, V)
                                                                              C(K,4)
                                                                                                                                                                                              + 11
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                                                                                                                                                                                                                                                 CALL
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12
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14
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ABBU 690
ABBU 690
ABBU 700
ABBU 720
ABBU 730
ABBU 730
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N= NUMBER OF PERFECT MIXING STAGES INTO WHICH THE LUNG IS DIVIDED 1,1 a 1,2 ı,t STEP CHANGE IN 프 = 1 IF IT IS ASSUMED THAT ALL STAGES ARE OF EQUAL VOLUME AND VS(I)= VOLUME OF THE ITH STAGE VF(I)= VOLUME FLOW RATE INTO THE ITH STAGE ALVEOLI DURING AN ALVEDLAR SACS OF ⋖ STAGE AFTER AFTER CH CONC. OF THE COMSTITUENT AT THE LUNG ENTRANCE AFTER TV= TIDAL VOLUME V= TUTAL EXPANDED VOLUME OF THE LUNG -TIDAL VGLUME V= DECISION VARIABLE S146E =-2 If BOTH VP(I) AND VS(I) ARE TO BE READ AS DATA =-1 IF VP(I) IS TO BE READ IN AS DATA TOA CONVECTIVE NODEL FOR LIQUID BREATHING FLOW PATES TO ALVEDUL ARE FOUND IN ALL STAGES II H PURPOSED TO SIMPLATE THE RESPONCE OF THE LUNG THE SCNC. OF A CONSTITUENT IN THE LUNG FLUID. CC= INITIAL CONSTITUENT CONC. IN THE LUNG 二二 H CONE(I)= CONC. OF THE CONSTITUENT IN THE CONSTITUENT IN ATE TOTAL NUMBER OF INSPIRATIONS RE RESPIRATORY RATE (BREATHS/MIN.) =0 IF VS(I) IS TO SE READ AS DATA CONSTITUENT ITH STAGE AFTER AN INSPIRATION 11 OF THE CONTAINS CONC. OF CCCT(1) = CDNC. CUTPUT VARIABLES INPUT VARIABLES INSPIRATION NOT LEY LESVI

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FOR JRH 1,3,5,19, AND 20, COMP(U)= CONG. OF THE CONSTITUENT IN THE EXIT STACE FOR 175 OF THE TIDAL VOLUME DRAINED

F= TIME REQUIRED FOR 1 INSPIRATION OR EXPIRATION VLOT= VOLUME FLOW RATE INTO THE LUNG VI= VOLUME OF ALYEOLI IN THE ITH GTAGE AT THE START OF AN INSPIRATION CIPEN VARIABLES OF INTEREST

PURPUSE SUBRCUTINES USEC

EXP(MATRIX#T) TO GENERATE CAUSE OF EARDRS IN THE SOLUTION IF ANY WILL MOST LIKELY PRUCKAM IS DIMENSIONED FOR A MAXIMUM OF 25 STAGES. 35 DUE TO LIMITATIONS OF EXP GENERATED IN GENE. CONMENTSO

IMPLICIT REAL*8(A,B,E,X,T) DIMENSION A(25,25),VF(25),VS(25),VSF(25),XIN(25,25),XOUT(25,25), 100(25), CUNE(15), CON(25), EXH(25, 25), EXHI(25, 25), EXHIV(25, 25),

25CCNC(25), CONT(25), COUT(25), BACT(25, 25), COMP(25)

JK=0

READ(S, 100) N, NT, TV, R, CO, C, V Y1= 0.0

VUCTE TV#2.0*R IF (F + 1) 1,3,5

FC 2 [=1,N READ(5,101) VF(I),VS(I) -4 C

REAC (5, 102) CC 4 Jelyn GC TC 10 \hat{m}

IF(N) 10,6,8 *

ſΔ)

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EXE(1, 1) = 45F(1+1)/VS(1
                                                                                                                                                                                                                                                                                                                                         EC 22 J=1,N
1F(1-3) 19,18,19
EXH(1,J) = -VSF(1)/VS(I)
                                                                                                                                                        IF(I-J) 13,12,13
A(I,J)= -VSF(I)/VS(I
                                                                                                                                                                                           IF((1-1)-J) 15,14,15

3(1,J)= VSF(1)/VS(1)
                                                                                                                    VSF(1) = VSF(J) + VF(J)

CC 16 i=1,N

CD 16 J=1,N
CC 7 J=1+N
REAL(5,102) VS(1)
VF(1)= VCOT/N
CC 1C 10
                                                                                                                                                                                                                                                                                                                                                                            GC TC 22
IF(I*:-J)21,20,21
                                            CC 9 I=1,N
VS(I)= V/N
VF(I)= V-0T/N
VSF(I)- V-0T/N
                                                                                                                                                                                                                                                      T= 0.5/3
TAB= T/5.0
FC 1/ T=1,N
COUT(1)=C
                                                                                            EC 11 1=2,N
                                                                                                                                                                                                                                                                                                                              EC 22 1=1+N
                                                                                                                                                                                                                   CC Tt 16
A(I,J)= 0.0
                                                                                                                                                                                                                                                                                                     CO - (1) = C-CO
                                                                                                                                                                                                                                                                                                                 CENELI'S C
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CCN(I) = CCM(I) + VP(I) *EXFI(I, J) *(CONC(J) -CG(J))
                                                                                                                                                                                                                                                                                                      CCNC(I) = 1,N
CCNC(I) = 0.0
CU 30 J = 1,N
CCNC(I) = XIN(I,J)*CG(J)+CONC(I)
                                                                                                                                                                                                                       CALL GENE(A,XIN,1,N,T)
CALL GENE(EXH,XCUT,1,N,T)
CALL GENE(EXH,3ACT,1,N,TAB)
                                                                                            ((J) HSA/(C)SA) - - (C'I) ALLXE
                                                                                                                                     EC 28 J=1,N
IF(I-1) 27,26,26
EXHI(1,J)= -VS(J)/VSF(J)
                                                                                                                                                                                                                                                             KRITE(6, 103) N, V, TV, K, CU
                                                                                                                                                                                                                                                                                                                                                               CCNT(I)= CONC(I)+CO
                                                                                                                                                                                                                                                                                                                                                                                         IF (JK-NT) 32,50,50
                                                                                                                                                                                                                                                                                                                                                                                                                     ([])= ([)+1+0)
                                                    IF(J-1) 23,24,24
FXHIV(1,J)= 0.C
                                                                                                                                                                                                                                                                                           WRITE(6,107) JK
                                                                                                                                                                                            57FI([,J)= 0.0
                                                                                                                                                                                                                                                                                                                                                                                                        CC 33 I= 1,N
                                      CO 25 J= 1,4
                                                                                                                                                                                                                                                                                                                                                                                                                                   CO 33 J=1,N
                         EC 25 I=1,h
                                                                                                                        EC 28 I=1,N
EXH(1,0)=
                                                                                                                                                                                                                                                                                                                                                                             CCALINUE
                                                                                                                                                                                                         CCATINUE
             CCNTINUE
                                                                                                                                                                                                                                                                               JK= JK+1
                                                                                                          CONTINUE
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CCUT(1)= CGUT(1)+BACT(1,J)*COMP(J)-EXHIV(1,J)*VF(J)*CONE(J)/VS(J)
                                                                                                                                                                                                                                                                                                                                                                                                                                                 CCUT(1) = COUT(1) + XOUF(1, J) + CSNT(J) - EXHIV(1, J) + VF(J) + CCNE(J) / VS(J)
                                                                                                                                                                                                      CCUT(1)= COUT(1)+BACT(1,J)*EXHIV(J,K)*VF(K)*CONE(K)/VS(K)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     CCLI(I) = COUT(I) *XOUT(I,J) * EXHIV(J,K) *VF(K) *CONF(K) /VS(K)
                 CCNE(1)= (CON(1)+COME(I)*V1)/((V1+TV/N))
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                          MRETE(0, 104) I, CCUT(I), CONT(I), CONE(I)
                                                                                                                                                                                                                                                             ARITE (6,108) CCUT(1), ILL
                                                                                                                                                                                                                                                                                                                                                      IF( JM-10) 340,300,340
IF( JM-20) 350,300,350
                                   IF ( JK-1) 310,300,310
                                                                                                                                                                                                                                                                                                                  IF( JK-3) 320,300,320
                                                                                                                                                                                                                                                                                                                                   IF UK-51 330,300,330
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                  FORMAT(12,13,5610.0)
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                            COTID= CCUT(I)+CC
                                                                       COMP(1)= COMP(1)
                                                                                                                                                                                                                                          CCMP(I)= COUT(I)
                                                                                         EC 307 ILL=1,5
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                     FORMAT(2F10.0)
                                                     CU 304 1=1,%
                                                                                                          60 305 Tal, N
                                                                                                                                                                                                                       M#1=1 908 00
                                                                                                                              CCUT([]= 0.0
                                                                                                                                                PG 305 J=1, V
                                                                                                                                                                                   CC 305 K=1, N
                                                                                                                                                                                                                                                                                                                                                                                          CCUT(I)= 0.0
16 34 lelyn
                                                                                                                                                                                                                                                                                                                                                                                                                               FO 35 J=1,N
                                                                                                                                                                                                                                                                                                                                                                                                                                                                   CC 35 K=1,1
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                                       CC 37 1=1,N
                                                                                                                                                                                                                                                                                                 SC TC 300
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11 Volume=',F10.3,' Respiration Rate=',F5.2,' Inlet Dyg Conc.=',F8.
                                                                                 104 FCPPAT(* *, *STACE=*, 12, * EXPINED CONC.=*, F10.5, * INSPIRED CONC.=*,
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C=Y(K,J)
U= CADS(D)
CE= CADS(C)
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APPENDIX B

SOME OBSERVATIONS ON MEMBRANE OXYGENATORS

B.1 One-dimensional Laminar Flow Model

This research study was intended to provide a basis for advanced design of blood oxygenators, including membrane oxygenators. Although we have not presented a membrane design, preliminary studies are currently underway. The comments that we make here are views and conclusions which were drawn from the literature survey on membrane oxygenators. We will restrict these comments to design principles pertinent to membrane oxygenator designs, a more complete understanding of which would, in our opinion, be of great assistance to those using these devices. The reader is invited, therefore, to "take the wheat and throw away the chaff."

As discussed in Chapter 1, Section 4, several membrane models have been proposed for blood flow in tubes and between parallel plates made of membrane material. These models are, in one way or another, boundary layer problems. In the case of laminar flow in tubes, it is usually assumed that transport in the radial direction is diffusion—controlled, and that transport in the axial direction is by convective mixing. Writing the flux of component i in the general form leads to

$$N_{i} = vC_{i} + J_{i}$$
(B.1-1)

and the two assumptions stated above require

$$v_{i} = 0$$
 and $J_{i} = 0$ (B.1-2)

The partial differential equation and boundary conditions for this problem are

$$\frac{\partial c_{i}}{\partial t} = D_{i} \nabla^{2} c_{i} - \nabla \cdot (c_{i} \nabla) + R_{i}$$
 (B.1-3)

and

$$C_{\underline{i}} = C_{\underline{i}}^{0} \qquad z = 0$$

$$J_{ir}\Big|_{r=R_1} = J_{ir}^{M}\Big|_{r=R_1}$$

where $J_{ir} = diffusion flux of component i in the blood in the radial direction$

 J_{ir}^{M} = diffusion flux of component i in the membrane

 R_1 = internal radius of the tubing

and $R_i = reaction rate of component i.$

The velocity component in the z-direction, $v_z(r)$, can be found by solving the equation of motion (41); for a Newtonian fluid the solution is

$$v_z(r) = 1 - \left(\frac{r}{R_1}\right)^2 - \frac{\Delta P}{4uL} (R_1)^2$$

where \(\text{LP} = - pressure drop across the length of the tube

 $\mu = viscosity$ of the blood

L = length of the tube.

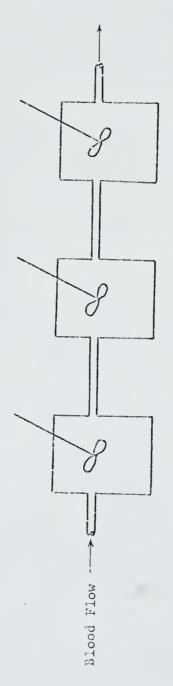
Non-Newtonian fluids give somewhat different velocity profiles. With ${\bf v_z}$ specified, Equation B.1-3 can be solved numerically if not analytically.

These models implicitly make use of the assumption of a stagnant layer of fluid immediately adjacent to the tube wall, and they describe the motion of the fluid quite well as long as there is no secondary and turbulent flow. It is Equations B.1-1 and B.1-2 which point to the limitations of membrane oxygenators. Noting that the axial velocity is zero in the vicinity of the wall, it should be obvious that gas transport at the wall is diffusion-controlled. This is the rate-limiting step in the transport of gas in the blood phase. Furthermore, if the membrane does not offer significant resistance to mass transfer, diffusion of gas into the blood near the membrane wall is the rate-limiting step for the entire process.

If secondary flow or turbulence occurs (which is desirable to increase gas exchange), either a more complicated form of the equation of motion has to be solved or a new model has to be proposed. For secondary flow due to coiling of tubes, Mackros (19) has chosen the first option. An attempt to model turbulent transfer as a CSTR has also been made (67), but, unfortunately, the mechanism of transfer proposed does not appear to be realistic. It is this model that we will discuss in hopes that a more realistic approach to turbulent transport will result.

B.2 The CSTR Model

Consider a length of tubing in which blood flow is turbulent. If the tube is relatively long, i.e., the ratio of length to diameter is large, the mining of constituents due to turbulent motion can be described as a series of CSTR's as shown in Figure B.2-1. Since the



CSTR Model for Turbulent Mass Transfer in Membrane Oxygenators. Figure B2-1.

stage-to-stage calculations for such a series of perfectly mixed absorbers were discussed in Chapter 4 and are applicable to this situation, we will consider only one stage here. The model presented by Gille et al. (67) for absorption of gases through membranes is called a surface renewal model. As shown in Figure B.2-2, blood enters a perfectly mixed reservoir, and is immediately mixed with the blood already in the container.

Absorption is modeled by assuming that a thin film of blood moves to the membrane-blood interface, becomes saturated with oxygen, and is then replaced by a new film. If the residence time of the film is 9, the rate of gas transfer is

$$\frac{d(VC_i)}{dt} = \frac{V_f C_i^*}{\theta}$$
 (B.2-1)

where VC; = mass of component i transferred

 $V_f = \text{volume of the film}$

 C_{i}^{*} = equilibrium concentration of component i in the blood.

The concept of a renewable surface is an idea taken from direct-contact absorbers. In these absorbers gas is brought into direct contact with a well-mixed liquid, and since by mixing, the materials at the gas-liquid interface are being replaced constantly, the surface renewal model is an acceptable description.

It must be remembered that at the interface in a membrane oxygenator a thin film of stagnant blood clings to the membrane; consequently, it is never replaced. For such a film, a stagnant boundary layer model would be a much more realistic description of the

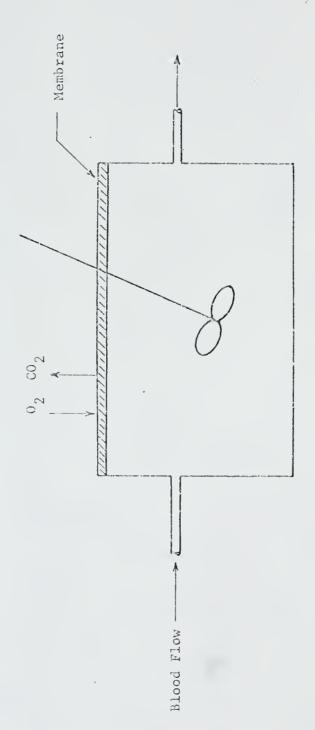


Figure B2-2. Membrane Oxygenator Gas Exchange in CSTR Model.

phenomenon occurring in a well-mixed stage. In this case, the rate of mass transfer would be given by the equation

$$\frac{d(VC_i)}{dt} = -KA(C_i - C_i^*)$$
(B.2-2)

instead of Equation B.2-1.

Finally, it should be noted that the diffusivity of carbon dioxide is low in Silastic which is currently considered the best membrane material. This fact leads to the possible consequence of transport limitations occurring in the membrane rather than in the blood. In any design, the consequences of carbon dioxide transport limitation in the membrane must be considered to maintain an acceptable respiratory ratio (ratio of oxygen to carbon dioxide exchange).

APPENDIX C

GAS EXCHANGE IN ALR BREATHING

Our comments on air breathing parallel our discussion of the membrane oxygenator. Once again, we have not expended a large effort to pursue the study of mechanisms of gas exchange in air-filled lungs, and again, our observations and interpretations are limited to areas already investigated but which merit further discussion. As might be expected, the mechanisms proposed for gas exchange during air breathing have been diffusion and convective mixing models. It is the role of diffusion that needs to be clarified.

Most models of gas exchange with which we are familiar treat the lung as a single perfectly mixed stage. At the alveolar walls it is assumed that a thin stagnant layer is present in which mass transport is diffusion-controlled. For such a system the rate of oxygen or carbon dioxide transport across the lung can be described by

$$\frac{dC_{i}}{dt} = \frac{\dot{V}(C_{i}^{o} - C_{i}) - K_{i}A(C_{i} - C_{i}^{*})}{V_{o} + \int \dot{V}dt}$$
(C-1)

where

- C_{i} = bulk concentration of the ith component in the lungs
- C_i^0 = concentration of the ith component in the gas entering the lungs
- * = the concentration of the ith component that would be in equilibrium with the concentration of the same component in the blood capillaries
- V_{c} = initial volume of the lungs

 \dot{V} = volume flow rate of gas into the lungs

K, = mass transfer coefficient

A = surface area available for gas transfer across the alveolar walls.

Although many refinements to it have been made, Equation C-1 is the starting point for convection mixing models for gas transport in the lungs. The model which leads to it reflects accurately the transport phenomena taking place in the lung.

Attempts to use a diffusion model for gas transport in the lung have not met with any considerable success. A typical case is a study made by La Force and Lewis (51). These investigators modelled the lungs as a diffusion-controlled transport unit. A computer program was developed to calculate oxygen concentration as a function of distance from the lung entrance and in terms of time elapsed after a step change in the entrance oxygen concentration had occurred. The conclusions they drew from the resulting concentration profiles are quite revealing.

Among the variables of interest is the length of the diffusion path. To consistently match computer results with experimental data, Conley concluded that a "thumb tack" model should be used to describe the lung. In the thumb tack model, it is assumed that gas diffuses through a relatively long, narrow entrance, thence into almost innumerable branches in a short distance. Such a model predicts an extremely short diffusion path, which is clearly the case, but it once again misses the correct interpretation of the physical phenomenon occurring, namely, the diffusion-controlled region is confined to a thin stagnant layer at the alveolar walls and this gives rise to the apparent short diffusion path.

In terms of calculational convenience, diffusion-controlled models such as the one presented by Conley may provide reasonable results in terms of prediction of oxygen and carbon dioxide transport in the lungs, but these models provide little insight into the actual workings of the lungs. Consequently, they are of minimal long term interest.

APPENDIX D

EXPERIMENTAL DATA

The data taken for the three different types of experiments performed in this study are listed as follows:

- data taken during air bubble measurements are shown in Table D-1;
- data taken during the saline simulation of blood oxygenators are shown in Table D-2;
- data of actual blood oxygenation parameters during openheart surgery are shown in Table D-3;
- 4. data taken during the saline liquid-breathing experiment are shown in Table D-4;
- 5. data taken during the fluorocarbon liquid-breathing experiment are shown in Table D-5.

DATA TAKEN DURING BUBBLE MEASUREMENT EXPERIMENT

Saline Flow Rate = 1.4 liter/min Air Flow Rate = 5.9 liter/min

Bubble No.	Major Diameter (mm)	Minor Diameter (mm)	Distance From the Sparger (cm)
1A	1 02	1 02	0.0
2A	1.83 2.39	1.83	9.0
3A	2.18	2.39 2.18	9.0
4A	3.45	2.39	9.0 9.0
5A	3.20	2.54	9.0
6A	3.66	3.05	9.0
7A	3.05	2.54	9.0
8A	3.56	3.05	9.0
9A	3.66	2.08	9.0
10A	3.71	1.43	9.0
11A	2.29	2.29	9.0
1.2A	3.96	1.63	9.0
13A	4.67	2.29	9.0
144	1.83	1.83	9.0
15A	3.45	1.93	9.0
18	3.05	2.29	9.0
2B	2.64	2.49	9.0
3B	3.05	2.29	9.0
4B	3.15	2.90	9.0
5B	4.47	4.06	9.0
63	3.15	2.54	9.0
7B	2.79	2.54	9.0
SB	3.61	3.25	9.0
98	2.59	2.13	9.0
10B	2.08	1.52	9.0
10	3.66	3.05	20.0
2C	3.61	2.54	20.0
3C	3.30	3.30	20.0
4C	4.01	3.81	20.0
5C	3.81	2.84	20.0
6C	2.13	2.13	20.0
7C	2.03	2.03	20.0
80	3.66	3.56	20.0
9G	2.13	2.13	20.0
10C	2.29	2.08	20.0
11C	3.66	2.90	20.0
12C	3.66	2.90	20.C

TABLE D-1 (Continued)

			Distance
	Major Diameter	Minor Diameter	From the Sparger
m 111 - N-	(mm)	(mm)	(cm)
Bubble No.	(IIIII)		
1.20	3.81	2.79	20.0
13C	4.06	2.54	20.0
14C		2.95	20.0
15C	4.06	3.56	20.0
16C	4.42	2.39	20.0
17C	4.06	•	20.0
18C	3.05	2.54	20.0
19C	4.06	3.56	20.0
	•		20 5
1D	4.67	3.45	30.5
2D	4.57	4.52	30.5
3D	3.30	2.79	30.5
4D	2.64	2.03	30.5
	2.64	2.28	30.5
5D	3.61	3.30	30.5
6D		2.54	30.5
7D	3.56	2.18	30.5
8D	2.18	3.40	30.5
9 D	4.47		30.5
10D	2.49	2.79	30.5
110	5.59	2.79	30.5
12D	5.08	1.78	30.3

CABLE D-2

SALINE SIMULATION OF A BLOOD OXYGENATCR

Oxygenator Model	1 LF	2 L F
×	0.219 0.150 0.158 0.235 0.235 0.189 0.160 0.138 0.160	0.547 0.127 0.138 0.142 0.212 0.187 0.187 0.194 0.160
O ₂ Holdup	124 195 189 189 216 264 125	263 200 239 210 227 239 197 163 216
Saline Holdup	236 165 181 171 171 156 235 171	170 136 126 165 178 178 159
0 ₂ Flow Rate (ce/min)	3400 4300 4300 4300 5600 5600 4500 6700 8000	4500 5500 6500 4500 6500 5500 6500
Saline Flow Race (cc/min)	911 952 933 916 971 562 580 603 374	816 816 882 1539 1429 1968 1981 2022

(Continued)
TABLE D-2

	Oxygenator Model	3LF	6LF
	×	0.199 0.240 0.234 0.308 0.402 0.343 0.343	0.501 0.480 0.445 0.418 0.479 0.479 0.461 0.464 0.386 0.386 0.338
led)	O ₂ Holdup	208 248 283 176 236 187 285	130 165 228 188 130 210 201 170 195 245
TABLE D-2 (Continued)	Saline Holdup	262 222 187 294 . 234 . 216 222 185	850 815 752 792 850 760 770 779 810 755 810 735
	0 ₂ Flow Rate (cc/min)	3400 4400 5500 3500 4500 5500 4500 5500	3500 4500 3500 3500 4500 4500 6500 6500 6500 6500 6500
	iine Flow Rate (cc/min)	2270 2460 2270 2610 2650 2650 2880 2930	5680 5980 5680 5750 4880 4850 4010 4160 4020 4020 3050 3030

TABLE D-3

OXYGENATION DATA FROM OPEN-HEART SURGERY

Experiment		Venous Po2	Arterial P_{0}	0, Flow Rate
No.	рН	(mm)	(mm)	(cc/min)
L	7.34	32.0	59.0	6300
2.	7.36	40.0	92.0	6900
. 3	7.43	32.0	82.0	6800
4	7.44	70.0	485.0	8200
5	7.43	55.0	240.0	7500
6	7.49	68.0	170.0	9300
7	7.58	47.0	180.0	9300
8	7.46	47.0	248.0	5900
9	7.39	32.0	170.0	5800
1.0	7.38	50.0	235.0	6100
11	7.38	88.0	220.0	9000
12	7.43	61.0	470.0	9300
13	7.44	41.0	480.0	4700
14	7.44	53.0	610.0	4850
15	7.47	102.0	590.0	10,000
16	7.28	82.0	150.0	4800
17	7.49	55.0	245.0	6100
18	7.48	38.0	87.0	6100
19	7.43	39.0	162.0	4000
20	7.35	70.0	172.0	5600
21	7.30	67.0	210.0	6000
22	7.47	48.0	230.0	9700
23	7.54	48.0	280.0	9500
24	7.56	56.0	330.0	9700
25	7.57	66.0	360.0	9600
26	7.54	156.0	240.0	9500
27	7.46	33.0	370.0	7700
28	7.32	55.0	158.0	6000
29	7.42	61.0	380.0	9200
30	7.43	130.0	230.0	10,000
31	7.35	65.0	240.0	600C
32	7.34	100.0	240.0	6000
33	7.35	48.0	1.64.0	6000

TABLE D-3 (Continued)

T	Venous P _{CO2}	Arterial P _{CO2}	Venous	Arterial
Experiment No.	(mm)	(mm) _	Hematocrit	Hematocrit
		And the second s		0.005
1	38.8	31.0	0.285	0.285
2	34.5	25.0	0.363	0.363
3	35.0	29.5	0.344	0.344
4	18.6	17.6	0.245	0.245
5	25.2	22.0	0.290	0.290
5	27.0	23.0	0.373	0.373
7	22.5	16.0	0.315	0.315
8	28.5	25.0	0.306	0.306
9	32.5	30.0	0.324	0.324
10	34.0	30.0	0.356	0.356
11	35.0	31.0	0.267	0.267
12	28.5	20.2	0.306	0.306
13	34.5	23.5	0.344	0.344
14	33.0	25.0	0.352	0.352
15	25.7	20.5	0.277	0.277
16	38.5	35.5	0.336	0.336
1.7	33.0	27.5	0.335	0.335
1.8	31.0	26.5	0.372	0.372
19	37.0	28.5	0.324	0.324
20	26.0	19.0	0.351	0.351
21	27.5	26.0	0.367	0.367
22	33.0	28.5	0.374	0.374
23	27.5	24.5	0.358	0.358
24	24.0	24.0	0.376	0.376
25	24.5	23.0	0.368	0.368
26	24.5	20.5	0.368	0.368
27	28.5	24.0	0.260	0.260
28	27.0	25.0	0.360	0.380
29	20.5	28.5	0.337	0.337
30	28.5	2.7.5	0.322	0.342
31.	30.5	25.3	0.282	0.278
32	29.5	24.0	0.281	0.257
33	27.0	25.0	0.253	0.254

TABLE D-3 (Continued)

Experiment No.	Oxygenator Model	Temperature (°C)	Blood Flow Rate (cc/min)
1	2LF	30.0	1606
2	2LF	31.0	1445
. 3	2LF	33.0	1285
4	3LF	30.0	2442
5	3LF	32.0	2442
6	6LF	30.0	3934
7	6LF	32.0	3934
8	3LF	29.0	2474
9	3LF	30.0	2227
10	3LF	30.0	2474
11	6LF	28.5	3872
12	6LF	34.5	2923
13	1LF	34.0	871
14	1LF	30.0	871
15	6LF	34.15	2710
16	2LF	34.0	1694
17	2LF	30.0	1540
18	2LF	35.0	1540
19	1LF	37.0	990
20	21.F	30.0	1320
21	2LF	31.0	1320
22	6LF	34.0	3600
23	6LF	35.0	3780
24	6LF	34.0	3870
25	6LF	34.5	3870
26	6LF	37.0	3600
2.7	3LF	30.0	1555
28	2LF	30.0	1409
29	6LF	32.0	4500
30	6LF	32.0	450 0
31	2LF	32.0	1373
32	2LF	30.0	1200
33	6LF	34.0	858

TABLE D-4

TRANSIENT LIQUID-BREATHING EXPERIMENT WITH SALINE

Total Volume of the Expanded Lung = 771 cc
Tidal Volume = 300 cc
Respiratory Rate = 3 Breaths/min

Volume Fraction Drained	$ \begin{pmatrix} C - C_{int} \\ C_{inlet} - C_{int} \end{pmatrix} $	Number of Respirations
0.0448	0.8284	1
0.1352	0.6110	1
0.2256	0.4394	î
0.3152	0.3661	1
0.4038	0.3113	1
0.4921	0.2425	1
0.5803	0.1762	1
0.6686	0.1304	1
0.7577	0.1030	1
0.8464	0.0847	1
0.9350	0.0618	1
0.9899	0.0458	1.
3.3035		
0.0259	0.9298	10
0.0789	0.8152	10
0.1316	0.6421	10
0.1843	0.5251	10
0.2384	0.4690	10
0.2925	0.4339	10
0.3455	0.4012	10
0.3984	0.3661	10
0.4524	0.3333	1.0
0.5067	0.3053	10
0.5610	0.2632	10
0.6155	0.2327	10
0.6698	0.2047	10
0.7233	0.1749	10
0.7771	0.1485	10
0.8305	0.1251	10
0.8832	0.1146	10
0.9367	0.0877	10
0.9820	0.0819	3.0

TABLE D-4 (Continued)

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TABLE D-5

TRANSIENT LIQUID-BREATHING EXPERIMENT WITH FLUOROCARBON (FX-80)

Total Volume of the Expanded Lung = 640 cc Tidal Volume = 350 cc Respiratory Rate = 3 Breaths/min

Concentration

Volume Fraction Drained	$\left(\begin{array}{c} C - C_{int} \\ \hline C_{inlet} - C_{int} \end{array}\right)$	Number of Respirations
0.0828	1.000	3
0.1563	0.921	3
0.2336	0.744	3
0.3180	0.766	3
0.3992	0.691	3
0.4836	0.675	3
0.5648	0.612	3
0.6445	0.518	3
0.7227	0.491	3
0.7758	0.447	3

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I certify that I have read this study and that in my opinion it conforms to acceptable standards of scholarly presentation and is fully adequate, in scope and quality, as a dissertation for the degree of Doctor of Philosophy.

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