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A USER'S GUIDE TO THE OA3660 APL WORKSPACE

by

F. Russell Richards

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Instructions are given for the use of the APL Public Library Workspace, 2 OA3660, which was developed as an aid to interactive exploratory data analysis. The OA3660 workspace is accessible to all users of the computer time sharing system at the Naval Postgraduate School. The workspace contains various data analysis functions, data, and complete internal documentation. This report provides a primer on APL, documentation on each function contained in the workspace, examples of the use of each function, and program listings.

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I. INTRODUCTION

This report provides documentation for the OA3660 APL workspace that was developed during the summer and fall quarters of 1977 in conjunction with the offering of the OA3660 course, Data Analysis, at the Naval Postgraduate School. The OA3660 workspace contains APL functions, variables, and data sets that are useful for interactive exploratory data analysis. The APL functions include selected procedures from the STAT1O1 public library [6], and from Donald R. McNeil's textbook, Interactive Data Analysis: A Practical Primer [5] (with some modifications). The OA3660 workspace also includes functions written by myself and students in my class and various utility functions extracted from other public library workspaces. Documentation for each function is contained in this report and in the OA3660 Public Library Workspace.

The data sets include data contained in examples and exercises in the above mentioned book, data from John Tukey's Exploratory Data Analysis [8], data generated from test scores in the OA3660 class, and data extracted from a few other textbooks. The data are cross referenced with the sources in a variable named DATAMAP.

This report is intended for the user who has some experience with APL and who is taking a course in Data Analysis or one who is already familiar with the basic techniques of interactive exploratory data analysis as described in Tukey [8], McNeil [5], and Mosteller and Tukey [7]. This report will not attempt to explain the analysis techniques themselves, nor will it discuss detailed APL concepts. It will give a brief description of the construction of data arrays and transformations of data since those are key elements in interactive exploratory data analysis. It also includes a brief discussion of basic APL commands such as logging into the system, loading workspaces, etc. For further details on APL and the NPS time-sharing system, CP/CMS, the reader is referred to the Naval Postgraduate School Technical Note No. 0141-33, APL(CMS)-An Introduction [1]; the IBM report #GH20-0906-1, APL\360-OS and APL\360-DOS User's Manual [2]; APL-An Interactive Programming Language [3] by Gilman and Rose; and APL Programming and Computer Techniques [4] by Katzan.

Each function contained in the OA3660 workspace is discussed; the function syntax is given; the function parameters (if any) are described; APL listings of the functions are given; and at least one example is included to illustrate the use of each function. An attempt has been made to assure that every function in the workspace is completely debugged. However, should any problems be experienced, the user is urged to notify me of the problems. Users are also encouraged to submit to me interesting data and APL functions that are useful for interactive exploratory data analysis.

II. APL PRIMER

This chapter is written primarily for the user who is not familiar with the APL programming language. We attempt to provide only that material that the user needs to know about APL to use successfully the OA3660 APL Public Library. Therefore, we discuss in this chapter login procedures, basic APL workspace management, error recovery procedures, creation and storage of data, data transformations, function syntax, and logout procedures. A user conversant with APL should proceed to Chapter III.

A good understanding of APL would enhance the user's facility for working with data arrays and performing interactive exploratory data analysis. Therefore, we encourage th user to seek out more detailed information on APL. References [1,2,3,4] are all recommended.

A. Getting Started: Login

In order to use the OA3660 APL Public Library, the user must have access to a computer terminal that has APL capability linked to the Naval Postgraduate School IBM 360/67 computer. There are many different types of remote terminals available for use,* and each has its unique features of operation. Therefore, the user should check out the operating

*The IBM 2741 terminals with a special APL typing ball, the Intertec terminals, and some of the CRT terminals have APL capability. In addition, there are several school owned portable terminals with APL capability.

instructions for each terminal to augment the general instructions given here.

If the terminal is wired directly to the computer, the user need only turn it on to access the NPS CP/CMS Time Sharing System. If not, the user must link to the computer via an acoustic hookup. First, turn the terminal on to the correct settings. Then dial the appropriate telephone number for connection to CP/CMS.[*] When the shrill audible tone is received, place the telephone receiver into the acoustic coupler which is connected to the terminal. If all of the terminal settings are correct, and if the time sharing system is in operation, the user should receive the message "CP-67 ONLINE". At this point, the user must log onto the system by typing (with the non-APL character set):

```
        LOGIN XXXXPYY (CR)
```

where XXXX is the user's identification number assigned by the computer center, P indicates a private user ID (type G if a general user without private disk space), YY is the terminal number, and (CR) indicates a carriage return.[#] If the identification number is valid, the system will request the user's password.

[*] The telephone number and the terminal settings depend on the terminal being used. For ASCII terminals (nearly all terminals at NPS other than the IBM 2741 terminals) dial either x2611 (with speed setting at 110) or x3025 (with speed setting at 300). For EBCDIC terminals (IBM 2741), dial x2701.

[#] On some terminals the user must depress simultaneously the keys CONTROL and S in place of a carriage return even though there may be a key so labelled. We will use (CR) to indicate a carriage return for all terminals.

The assigned password should be typed followed by a carriage return:

```
PASSWORD CR
```

If the password is incorrect, the system will reject the login and ask the user to start over. If the password is correct, the system will request the user's four-digit project number to be followed by a four-character cost center code. The project number must be assigned by the computer center. The cost center code is the user's section identifier or department code.

```
PPPPCCCC CR
```

If the project number is acceptable the system will respond with a ready message indicating that the user is in the CMS subsystem of the CP/CMS Time Sharing System. Otherwise, the user must repeat the entire procedure.

Once the user has entered CMS he should switch on the APL character set* and type

```
APL CR
```

*Switching to the APL character set may consist of flipping a switch, changing a type ball or impact print set, or issuing a sequence of program instructions depending on the type of terminal.

to enter the APL subsystem. The system will then respond with the message:

```
        A * P * L \ N * P * S

LIBRARY DOCUMENTATION SYSTEM...   )LOAD 1 LIBDOC  TYPE DESCRIBE.*
```

The user is now in APL, and all of its powerful features are available to him. He may use APL in the calculator mode somewhat as he would use a hand held calculator; he may define his own functions to perform a sequence of operations; or he may access the public libraries which consist of commonly used preprogrammed functions that perform a variety of useful computations.

In the next section we describe briefly the use of APL in the calculator mode to generate, manipulate and store data. In later sections we describe the use of APL to transform the data, and the use of APL Public Library Workspaces. The user is directed to references [1,2,3,4] for information about writing functions in APL, and for more detailed information about primitive operations in APL.

*If any symbol other than the right parenthesis) appears before the word LOAD, the system is not properly translating the character set into the required APL characters. If this happens, the user should type the symbol that appears (represented here by ≠) followed by the word OFF as follows:

```
        ≠OFF  CR
```

This will get the user off the system at which time he should consult with the computer center staff as to the special requirements for his terminal. Do not proceed in APL until the character ")" appears before the word LOAD in the message typed when APL is entered.

B. Generating and Storing Data

Generation of data arrays is very simple in APL because one need not be concerned with format. One must, however, become familiar with the APL syntax. First is the assignment symbol ← which plays a role somewhat like the = sign in FORTRAN. It means to take the expression on the right and assign it to the variable named on the left. Suppose, for example, one wants to generate a vector of data named X[*] consisting of the four observations: 3.15 ¯12.57 8 6.003. One need only type:

```
X ← 3.15  ¯12.57  8  6.003  CR
```

with the decimal typed if needed and with one or more spaces serving as delimiters for the separate observed values. (Real numbers may be expressed in scientific format by use of the E notation. 2.5E5 means 2.5×10^5 or 250000.) Extra spaces before and after the assignment arrow, ←, are not needed, but they will not hurt anything. Additional values can be added to the vector by using the catenate operator (the comma)[#] as follows:

[*] Just about any name can be used for variables as long as the first character is alphabetic and the other characters are alphabetic or numeric. The character ∆ is also acceptable.

[#] One must take care to strike the characters for the APL character set. Several of the APL characters are identical in appearance on the terminal keyboards to non-APL characters, but different results are obtained. Among the characters that appear the same are) ' (- + × ÷ / : ; *.

```
        X ← X, 5.76  ¯4  1.47 CR
```

This statement says to catenate the three indicated values to the end of the old data vector X and to call the resulting vector X. The entire vector can be viewed by typing X followed by the CR

```
        X CR
3.15  ¯12.57  8  6.003  5.76  ¯4  1.47
```

In the above vector, the negative signs are typed using the negative symbol (upper shift 2), not the minus sign (upper shift +).

If one is entering many data values into a vector he may require several lines of input to do so. Additional values could be inserted, as above, using the catenate operator. However, a simpler way is to type a comma followed by the quad symbol ⎕ (upper shift L) and a carriage return at the end of a line if more values are to be continued on succeeding lines. The next line will automatically begin with the quad symbol prompting the user to continue entering values. This is illustrated below:

```
        DATA ← 4  6  8  12  6  ¯2  ¯4  0  0  1  22  36  29  18,⎕ CR
⎕: 4  2  12  9  ¯3  ¯17  9  9  2  ¯1  4
```

If a value is typed incorrectly and discovered before the CR is struck, the value can be corrected by backspacing to the incorrect entry and hitting the line feed key.[*] This will erase the incorrect value and everything to the right of the value. Then type the correct values.

Data correction or modification after a line has been terminated by a carriage return can be accomplished several ways. One way is to determine the index of an incorrect entry and assign a new value to that specific element of the data array. For example, suppose one wants to change the third element from 8 to 4.81 leaving all the other elements alone. This can be done by typing:

```
X[3] ← 4.81    CR
```

Multiple corrections can be made simultaneously as follows:

```
X[3, 4, 5] ← 4.81  5.9  ¯3.26   CR
```

The X vector would then contain:

```
3.15  ¯12.57  4.81  5.9  ¯3.26  1.47.
```

The index operator ι (upper shift I) is convenient for determining the index of a given value (or indices of a set of values) in an array of data. If X is the data array and B is a set of values in X, then X ι B will generate the set of

[*] On some terminals the line feed key is labelled LF. On others, the attention or break key must be struck.

indices of the values of B in X. If a value appears in more than one place in X, only the subscript of its first appearance is given. For example, if X ← 3.5 ¯12.57 4.81 5.9 ¯3.26 ¯4 1.47 the index of the value 5.9 is found as follows:

```
      X ⍳ 5.9
4
```

Let B ← ¯12.57 ¯3.26. The indices of B in X are given by:

```
      X ⍳ B
2  5
```

This operation could be useful for altering selected values in an array. To illustrate, assume that we want to change the values ¯12.57 and ¯3.26 in X to 80 and 83. The operation below will accomplish this change:

```
      X[X ⍳ ¯12.57  ¯3.26] ← 80  83
      X
3.15  80  4.81  5.9  83  ¯4  1.47
```

Additional values can be inserted at any position in the vector, and values can be deleted from the vector by using the take "↑", drop "↓", and catenate "," operations. The take operation with syntax

```
      r ↑ X,
```

selects the first r elements from the vector X if r is positive and the last |r| elements if r is negative. The drop operation with syntax

```
      r ↓ X
```

deletes the first r elements of X if r is positve and the last |r| elements if r is negative. If |r| is greater than the number of elements in X, r ↑ X will insert zeros to the right of the elements of X until |r| elements are obtained and r ↓ X will result in the empty vector. The examples below demonstrate the take and drop operations.

```
        X
3.15  ¯12.57  4.81  5.9  ¯3.26  ¯4  1.47

        3 ↑ X
3.15  ¯12.57  4.81

        ¯2 ↑ X
¯4  1.47

        9 ↑ X
3.15  ¯12.57  4.81  5.9  ¯3.26  ¯4  1.47  3.15  ¯12.57

        2 ↓ X
4.81  5.9  ¯3.26  ¯4  1.47

        ¯4 ↓ X
3.15  ¯12.57  4.81

        8 ↓ X
```

The take and drop operators can be used in conjunction with the catenate operator to edit data vectors. The examples below illustrate some ways this can be done.

Let

```
X ← 1  2  3  4  5  6  7  8  9  10.
```

Create a new vector Y consisting of the first four elements of X followed by the elements 11 12 and then the last three elements of X; i.e. Y = 1 2 3 4 11 12 8 9 10.

```
        Y ← (4 ↑ X), 11  12, (¯3 ↑ X)  CR
or      Y ← (4 ↑ X), 11  12, (7 ↓ X)   CR
```

Let W ← 0 ¯1 ¯2 ¯3 ¯4 ¯5. Create a new vector Y consisting of the first eight elements of X, followed by the number 25, followed by the middle four elements of W.

```
        Y ← (8 ↑ X), 25, (1 ↓ (5 ↑ W))  CR
```

A few comments about the above operation are in order. APL always operates from right to left except when parentheses are used to override the standard order of operation. Thus, (5 ↑ W) is the first operation executed. This results in the vector 0 ¯1 ¯2 ¯3 ¯4. The next operation is (1 ↓ 0 ¯1 ¯2 ¯3 ¯4) which gives ¯1 ¯2 ¯3 ¯4. This is catenated to 25 yielding 25 ¯1 ¯2 ¯3 ¯4 which is then catenated to (8 ↑ X) giving 1 2 3 4 5 6 7 8 25 ¯1 ¯2 ¯3 ¯4.

In data analysis one often wants to compare different groups of data or to relate one group to another group. Many of the functions in OA 3660 require the data arrays be matrices whose columns represent the different groups and whose rows represent the various observations for each group. Let us see how a data matrix can be created. Suppose for example that one wants to create the matrix:

$$A = \begin{pmatrix} 1 & 2 \\ 3 & 4 \\ 5 & 6 \\ 7 & 8 \end{pmatrix}$$

The easiest way to create A is to create a vector consisting of the eight elements and then reshape the vector into the desired 4 × 2 array. The reshape operator ρ can be used to reshape a vector into any specified size. The matrix A is created by the operation:

```
A ← (4,2)ρ  1  2  3  4  5  6  7  8   ⒸⓇ
```

The general syntax for the reshape operation is A ← (N,M)ρB where B is a vector, or scalar, M is the number of columns of the array A, and N is the number of rows of A. The first M elements of B will be used for row 1, the second M for row 2, etc. If there are less than M·N elements of B, the elements will be repeated from the beginning as many as are needed. If

B contains more than M·N elements, only the first M·N will be used. Try a few examples to see what reshape does.

Remember that the reshape operator fills up matrices row by row. Suppose that the user entered the data into the vector by columns; e.g. B ← 1 3 5 7 2 4 6 8. How can the 4 × 2 matrix A be generated? (4,2)⍴B will not work since that would give

$$\begin{pmatrix} 1 & 3 \\ 5 & 7 \\ 2 & 4 \\ 6 & 8 \end{pmatrix}$$

However, if one requested (2,4)⍴B one would obtain

$$\begin{pmatrix} 1 & 3 & 5 & 7 \\ 2 & 4 & 6 & 8 \end{pmatrix} .$$

What we need now is to transpose this to obtain A. The transpose operator is ⍉ (upper shift 0 overstruck with upper shift /).[*] This sequence of operations can be combined as follows:

```
A ← ⍉(2,4)⍴B      CR
```

The operator ⍴ is also useful for determining the dimension or shape of an arbitrary variable. When used for this purpose it is called the shape operator. The syntax is

```
⍴Z    CR
```

[*] Type shift O (oh), backspace, and type upper shift /.

Table 2.1 illustrates the results of the shape operator when applied to selected variables. The first entry is the scalar 3. APL considers all scalars to have no dimension (not dimension 0). Thus, ρZ is the empty vector. In the next to last case, the variable Z is defined to be ι0 (iota 0). (This represents a second use of the index operator ι where the operator has only a right argument. If K is any nonnegative integer, ιK is the vector consisting of the first K positive integers. For example, ι3 would be the vector 1 2 3.) The use of the index operator in Table 2.1 is a rather special one. APL interprets ι0 as a vector with 0 elements, hence the result 0 for ρZ. This probably is puzzling to the reader, but it is really quite handy. The reader should simply commit to memory the facts that scalars have no dimension and the empty vector has dimension 0. In the last entry of Table 2.1, Z is defined as the 1 × 3 array consisting of 1 2 3. This array appears to be identical to the vector Y ← 1 2 3, but APL makes a distinction between the two.

VARIABLE	ρZ
Z ← 3	–
Z ← 2 3 5	3
Z ← (2,2)ρ 1 2 3 4	2 2
Z ← ι0	0
Z ← (1,3)ρ 2 3 5	1 3

Table 2.1: THE SHAPE OPERATOR

The last APL operators discussed in this section are the grade up and grade down functions. These two functions, denoted ⍋ and ⍒,* give the indices of the elements in a vector in order of magnitude: ascending order for grade up and descending order for grade down. This is very useful for data analysis since much of our work requires us to sort the data. These operations accomplish this easily. Here are some examples:

```
      A ← 9  12  6  4  ¯2  3  7  ¯5  11
      ⍋A
8  5  6  4  3  7  1  9  2
      ⍒A
2  9  1  7  3  4  6  5  8
```

In the grade up of A the first element, 8, says that the eighth value of A should be taken first; the second element, 5, says that the fifth element of A should be taken next, etc., to sort A in increasing order. Similarly for grade down to sort in decreasing order. The sorted arrays can be written as follows:

```
      A[⍋A]
¯5  ¯2  3  4  6  7  9  11  12
      A[⍒A]
12  11  9  7  6  4  3  ¯2  ¯5
```

*These symbols are upper shift H and G, respectively, overstruck with upper shift M.

We have only scratched the surface of APL features useful for generating, modifying and storing data. The collection of operations discussed here will, nevertheless, enable a user to do most of the things that he requires to generate, correct, modify and store data. In the next section we discuss arithmetic operations in APL so that the user can perform calculations and transform data arrays.

C. Arithmetic Operations

In this section we discuss some of the basic arithmetic operations. We restrict attention to those operations most frequently used in data analysis.

The symbols used for the basic operations of adding, subtracting, multiplying, and dividing are the standard ones used in mathematics: (+, -, ×, ÷).* However, in APL these operations are more powerful than their equivalents in most programming languages since the operations can be applied to entire vectors or matrices. When used with vectors or arrays, the operations are applied componentwise. This requires that the vectors or arrays have the same size. An exception is made for the case where one of the arguments is a scalar. When this happens APL adds,

*The subtraction sign is upper shift +. Do not confuse this with the negative sign which is upper shift 2.

subtracts, multiplies or divides the scalar to each element of the vector or array. Of course, the operation can be applied to two or more scalars as with any other programming language. The examples below illustrate the basic operations:

```
        A ← 3  5  7  8      (CR)
        B ← ¯1  ¯2  1  2    (CR)
        A + B   (CR)
2  3  8  10
        A - B   (CR)
4  7  6  6
        A × B   (CR)
¯3  ¯10  7  16
        A ÷ B   (CR)
¯3  ¯2.5  7  4
        2 × A   (CR)
6  10  14  16
        3 + B   (CR)
2  1  4  5
        C ← (2,2)⍴A   (CR)
        C   (CR)
3  5
7  8
```

```
        D ← (2,2)ρ B   CR
        D   CR
¯1  ¯2
 1   2
        C + B   CR
 2  3
8  10
        C ÷ 2   CR
1.5  2.5
3.5  4.0
        3 × 4 + 5   CR
27
        12 ÷ 3 × 2   CR
2
```

The last two examples are included to re-emphasize the right-to-left order of operations in APL. Thus, 5 is added to 4 to give 9 which is then multiplied by 3 to yield 27. Similarly, in the last case, 2 is multiplied by 3 to give 6 which is then divided into 12 to yield 2. Unlike some other languages there is no hierarchy of operations other than right to left. Of course, parentheses may be used as in algebra to change the priority of operation.

```
        (3 × 4) + 5   CR
17
        (12 ÷ 3) × 2   CR
8
```

In addition to the four basic operations, data analysis frequently requires power, log, reciprocal, and exponential transformations. As with the four basic operations these can be applied to scalars, vectors, or matrices.

Table 2.2 presents the syntax for these operations.

Transformation	Syntax
X^a	X * a
$\ell n\ X$	⍟X [1]
$1/X$	÷X
e^X	*X

Table 2.2. SYNTAX FOR DATA TRANSFORMATIONS

Here we give examples of these transformations:

```
        X ← 1  2  3  4  5   (CR)
        X * 0.5  (CR)
1  1.41421  1.73205  2  2.23607
        X * 2  (CR)
1  4  9  16  25
        X * ¯3  (CR)
1  0.125  0.037037  0.015625  0.008
```

[1] The symbol for the logarithm is the upper shift O (oh) overstruck with the asterisk (upper shift P).

```
      ⍟X   (CR)
0  0.693147  1.098612  1.386294  1.609438
      ÷X   (CR)
1  0.5  0.333333  0.25  0.2
      X * ÷ ¯3   (CR)
1  0.793701  0.693361  0.629961  0.584804
```

(Recall that APL operates from right to left so that the operator above raises each element in X to the -1/3 power.)

```
      *X   (CR)
2.71828  7.389056  20.085537  54.598150  148.413159
```

The logarithm of a number N to an arbitrary base B can be determined by typing B ⍟ N; e.g.,

```
      10 ⍟ 1000
3
```

Three other useful arithmetic operations for scalars, vectors, and matrices are the ceiling ⌈, floor ⌊, and absolute value |. All of these can be used with a single right hand argument or with both left and right arguments.

The examples below illustrate the use of these operators:

Monadic (one argument)

```
      ⌈2.75  6  0.08  ¯3.6
3  6  1  ¯3           (Gives smallest integer ≥ argument.)

      ⌊2.75  6  0.08  ¯3.6
2  6  0  ¯4           (Gives largest integer ≤ argument.)

      |2.75  6  0.08  ¯3.6
2.75  6  0.08  3.6    (Gives absolute value of each element.
```

Dyadic (two arguments)

```
        3  5  ⌈  2  8
3  8         (Gives the maximum of each component.)
        3  5  ⌊  2  8
2  5         (Gives the minimum of each component.)
        3  |  7  6  8  ¯2
1  0  2  1   (Gives the remainder after dividing each element by 3.)*
```

Clearly, the floor and ceiling operators are useful for rounding values. One can select any number of significant digits. If one wants to round values to the nearest integer, one should type ⌊0.5 + N. If, say, four significant digits are wanted, one could type (⌊.5 + N × 1E4) ÷ 1E4. The examples below illustrate the use of ⌊ for rounding:

```
        N ← 0.0835126  12.51877623  1.33333333  5.25
        ⌊.5 + N
0  13  1  5
        (⌊.5 + N × 1E4) ÷ 1E4
0.0835  12.5188  1.3333  5.2500
```

Another operator, the reduction operator /, allows the operations discussed above to be applied to all the elements of a vector or to the rows or columns of a matrix. The syntax is

[*] All remainders of K|N are expressed as positive integers in the set 0, ιK-1. If a remainder is negative, K is added to it.

f/A where f can be any of the arithmetic operations discussed above and A is a vector or a matrix. The result of this operation when applied to a vector A of size n is the scalar A[1] fA[2]f ··· fA[n]. When applied to a matrix M having r rows and c columns, the result is the vector B of dimension r where B[i] = A[i;1] fA[i;2] f ··· fA[i;c] for i = 1,2,...,r (column reduction). The matrix M can be reduced over its rows by typing f/[1]M. The examples below illustrate the reductio operation:

```
        + /1  3  7  4
15           (the sum of all the elements)
        ×/1  3  7  4
84           (the product of all the elements)
        ⌈/1  3  7  4
7            (the largest element)
        M ← (3,2)⍴3  1  2  6  5  4
        M
3  1
2  6
5  4
        -/M
2  ¯4  1     (differences of elements in rows 1, 2, and 3)
        ⌊/M
1  2  4      (minimum values in rows 1, 2, and 3)
```

```
        +/[1]M
10  1    (sums of elements in columns 1 and 2)
        ⌈/[1]M
5  6     (maximum values in columns 1 and 2)
```

Finally, we describe the inner product operation and the matrix inverse. The inner product, like the reduction operation can be applied with any general APL operators. The syntax is Af.gB, where A and B are vectors or matrices (which must satisfy certain size restrictions) and f and g are any general APL operators. For vector arguments, A and B must be the same size, say n, and the result is given by f/A[1]gB[1] A[2]gB[2] ... A[n]gB[n]. For matrix arguments the number of columns of A must be the same as the number of rows of B. The result is a matrix of size n × m where ⍴A = (n,k) and ⍴B = (k,m). The (i,j)th element of the result is f/A[i;1]gB[1;j] A[i;2]gB[2;j] ... A[i;k]gB[k;j]. The reader should recognize the operation above as matrix multiplication when f is + and g is ×. The examples below illustrate the inner product.

```
        X ← 1  4  3  2
        Y ← 2  3  1  2
        X + . × Y
21  ((1 × 2) + (4 × 3) + (3 × 1) + (2 × 2))
        X × . + Y
336 ((1 + 2) × (4 + 3) × (3 + 1) × (2 + 2))
```

```
        A ← 3  2  ρ  ι  6
        A
1  2
3  4
5  6
        B ← 2  3 ρ 3  5  2  3  1  1
        B
3  5  2
3  1  1
        A + . × B
 7   7   4    (the matrix product of  A  and  B)
21  19  10
33  31  16
```

The domino operator ⌹ (type ⎕, backspace, ÷) is used to solve for the matrix inverse of a nonsingular square matrix. The inverse of a nonsingular square matrix C is found by typing ⌹C. For example,

```
        C ← 2  2  ρ  1  1  0  2
        C
1  1
0  2
        ⌹C
1  -0.5
0   0.5
        C  +  .  ×  ⌹C
1  0
0  1
```

D. Workspace Management

In the previous sections we have seen how data are input and variables are transformed. In this section we describe how the user manages his APL workspace so that he can save data for use from one session to the next; he can load public library workspaces; and he can use functions available in the public library workspaces. For information about writing functions the user should see references [2,3,4].

When a user types APL he is put into a clear APL workspace. In this clear workspace data can be created and any of the operations described in the earlier chapters can be performed. If the user wishes to maintain the data or results for future use he must save the workspace. This is done by typing

```
        )SAVE WSNAME
```

where WSNAME is an arbitrary name (first letter alphabetic, eleven characters or less) that the user selects for the workspace. This private workspace can subsequently be loaded into the user's active workspace by typing

```
        )LOAD WSNAME
```

This causes the active workspace to be cleared and a copy of the named workspace to be written into the active workspace. Alternatively, if the user does not want to clear out the contents of the active workspace to bring in the named workspace, he can type

```
)COPY WSNAME
```

This will simply augment the existing contents of the active workspace with the contents of workspace WSNAME. However, if an existing variable or function in the active workspace has the same name as a function or variable in workspace WSNAME the latter will replace the former.

Any modifications, additions, deletions, corrections, etc. that the user makes to a copy of a workspace will affect the active workspace, but will not affect the permanent copy of the workspace maintained on his private files unless the user saves the so modified active workspace. This can be accomplished by typing)SAVE WSNAME (or simply)SAVE if workspace WSNAME were LOADed).

The user can determine the name of the active workspace at any time by typing)WSID (for WorkSpace IDentification). Similarly, he can change the name of the active workspace by typing)WSID NEWNAME. A list of all the user's private APL workspaces is obtained by typing)LIB. Entire workspaces can be permanently destroyed by typing)DROP WSNAME. (Be careful with this one!)

Within an active workspace, a user can obtain a list of all of the functions contained in the workspace by typing)FNS. The functions will be listed alphabetically so that all functions from those beginning with a certain letter, LETTER, onward can be obtained by typing)FNS LETTER. Similarly, a list of variables in the workspace can be obtained by typing)VARS or)VARS LETTER. Typeout can be terminated at any point by hitting the BREAK or the ATTN key. Variables and/or functions can be deleted from the active workspace by typing)ERASE LIST where LIST is a single function or variable or a list of functions and variables to be deleted. Names in the list should be separated by one or more blanks. Two other system commands allow the user some control over his APL environment. These commands control the number of digits printed out and the width of a typed line. They are)DIGITS N and)WIDTH N, where N is the number of digits to be printed or the desired line width, respectively.

In addition to his own private APL workspaces, the user also has access to all of the APL public libraries available at NPS. These libraries have numbers between 1 and 999 and are intended to hold workspaces of general interest. See [1] for a list of the public library numbers. The contents of a public library can be displayed using the)LIB command followed by the library number. For example,

```
              )LIB 1

         A-DISK       R/0
         IOFNS        17.25       7/09
         PLOTFORM     17.25       7/09
         NEWS         15.54       8/27
         WSFNS        17.25       7/09
         TEXTEDIT     17.26       7/09
         FORMAT       17.26       7/09
         CATALOG      15.17       7/14
         MAILBOX      12.50       7/14
         MULTIPLO     14.06       7/18
         FILEFNS      17.18       8/14
```

The list contains the workspace name and the time and date that it was last modified.

A copy of a public library workspace can be put into the user's active workspace by typing)LOAD n WSNAME or)COPY n WSNAME where n is the library number and WSNAME the workspace name. (Recall the differences in LOAD and COPY; LOAD will first clear the contents of the active workspace.) Selected functions and variables from a workspace (either public or private) can be copied by typing

```
                 )COPY n WSNAME OBJECT
         or
                 )COPY n WSNAME GROUP
```

where OBJECT is a single variable or function that the user wants to copy into his active workspace and GROUP is a group of variables and/or functions that has previously been defined for WSNAME.*

When a public library workspace is brought into the user's active workspace, documentation can usually be obtained by typing the word DESCRIBE. It is somewhat standard procedure to document public library workspaces with a DESCRIBE variable giving general information and with each function in the workspace being documented by a "HOW" variable. Type the name of the function followed by HOW with no intervening spaces. For example, documentation for the function STEMLEAF in public library 2 OA3660 is obtained by typing STEMLEAFHOW. "HOW" variables generally describe the function syntax, parameters, input/output requirements, etc. Of course, the user can determine if a workspace contains this sort of internal documentation by typing)VARS.

When the user has completed his work session he can logout by typing)OFF. If he wants to get out of APL but not logout, he should type)OFF CMS. Then, he should switch back to the standard keyboard.

*The group structure for the OA3660 workspace is discussed in Chapter III.

E. Error Recovery

This section describes recovery procedures that the user can employ if he receives error messages during execution of functions contained in a workspace. Usually, error messages received when functions in public library workspaces are executed are the result of improper syntax or problems with the shapes of the arguments. As soon as an error is detected, execution of the function is suspended, the number of the line containing the error is typed, a caret is inserted at the position in the line that the error occurred, and an explanatory error message is printed out. When the function is suspended the values of all variables determined up to the point of suspension can be obtained by simply typing the variable name. All of this makes error discovery and correction quite simple. From the point of suspension the user can branch to any line of the function by typing → n, where n is the desired line number. If n is omitted a branch is made outside of the function. Many types of calculations can be performed while a function is suspended, including the execution of other functions. However, the function will remain suspended until a branch is made as described above. Suspended functions tend to clutter up the user's workspace so that suspended functions should not be left pending. A list of all suspended functions can be displayed at any time by typing)SI (state indicator). If several functions are listed as being suspended, the user should type as many branch arrows (→), one per line, as there are asterisks displayed in the list.

Since the functions contained in the public library workspaces have been tested extensively, most of the errors that are encountered result from improper function syntax or the use of arguments that are not conformable or of improper size. The documentation contained in the next chapter shows the proper syntax for each function, and gives the requirements placed on the arguments.

III. THE OA3660 WORKSPACE

This chapter provides documentation for the public library workspace, 2 OA3660. General workspace documentation is contained in the DESCRIBE variable and in the lists of functions, variables, and groups. Short writeups are given for each function in the workspace via "HOW" variables, and examples of the use of each function are provided. Data are contained in the workspace to provide easy illustration of the functions. The data are described in the DATAMAP variable. Finally, the actual APL programs are displayed.

A. General Documentation

The OA3660 APL workspace is contained in public library 2. Therefore, the user must type)LOAD 2 OA3660 or)COPY 2 OA3660 to create a copy of the OA3660 workspace in his active workspace area. The functions and variables contained in OA3660 are displayed by typing)FNS and)VARS as shown below.

```
      )FNS
AND      ANOVA    A3R      A3RSR    BOXPLOT  CHISQUARE         CODERRS
COMPARE  CONDENSE          CONTINGENCY       CORRELATION       FILL     FM
INPUT    KS       LINE     LIT      LSLINE   MEDPOLISH         MSTATS   NU
ONEH     ONE3     PARTIAL  REGRESS  SCAT     SHOWRES  SPLIT    STATISTICS
STEMLEAF          SUMSQ    TWICE    UTCOND
```

```
      )VARS
AGES     ANDHOW   ANOVAHOW          A3RHOW   A3RSRHOW          BOXPLOTHOW
CHICKWTS          CHISQUAREHOW      COAL     CODERESHOW        COMPAREHOW
CONDENSEHOW       CONSUMPTION       CONTINGENCYHOW  CORRELATIONHOW  CI
CRIMES   DATAMAP  DEATHS   DEP      DEPTH    DESCRIBE          DISCOVERIES
DRAPER   EPSILON  GRADES1  GRADES2  HYDROPLANTS      INSECTS  KSHOW
LANDAREAS         LENGTH   LINEHOW  LSLINEHOW        MEDPOLISHHOW      MISS
MORTALITY         MSTATSHOW         NDIVX    NDIVY   NGAP     NORMEFFECTS
NUM      NUMSUMHOW         ONEHHOW  ONE3HOW  OPTION  PARTIALHOW
PRECIPITATION     PRESRATING        REGRESSHOW       RESIDS   RIVERS
RSELECT  SCALE    SCATHOW  SHOWRESHOW        SPLITHOW          STATISTICSHOW
STEMLEAFHOW       TESTX    TESTY    TWICEHOW         USPOP    VOLCANO
WARPBREAKS        WID      WIDTH    ∆INTERCEPT       CH
```

Notice that there is a variable called DESCRIBE. This variable gives general documentation about the workspace.

```
      ⍝THE DESCRIBE VARIABLE PROVIDES GENERAL DOCUMENTATION
      ⍝FOR THE ENTIRE WORKSPACE.  SIMPLY TYPE 'DESCRIBE' TO
      ⍝OBTAIN THE INFORMATION.



      DESCRIBE
                          OA3660-DATA ANALYSIS

     DATE:  JANUARY 1978
     PROGRAMMER:  F. RUSSELL RICHARDS

     THIS WORKSPACE CONTAINS FUNCTIONS AND VARIABLES  USEFUL  FOR
EXPLORATORY INTERACTIVE DATA ANALYSIS.  FOR  INFORMATION  ON  THE
USE OF THE FUNCTIONS TYPE THE FUNCTION NAME FOLLOWED BY  'HOW'.
FOR EXAMPLE, TYPE STEMLEAFHOW FOR DOCUMENTATION ON  THE  FUNCTION
STEMLEAF.  SOME FUNCTIONS ARE USED ONLY AS SUBPROGRAMS FOR  OTHER
FUNCTIONS AND WILL NOT HAVE A 'HOW' VARIABLE.  FOR MORE  DETAILED
DOCUMENTATION SEE THE NPS TECHNICAL REPORT, A USER'S GUIDE TO THE
OA3660 APL  WORKSPACE,  BY  F.  RUSSELL  RICHARDS  OR  DONALD  R.
MCNEIL'S BOOK, INTERACTIVE DATA ANALYSIS.
     THE WORKSPACE ALSO CONTAINS  VARIOUS  SMALL  DATA  SETS  FOR
ILLUSTRATION  OF  THE  FUNCTIONS.   TYPE  DATAMAP  TO  OBTAIN
IDENTIFICATION OF THE DATA ARRAYS.
     THE USER CAN SAVE SPACE IN HIS ACTIVE WORKSPACE  BY  COPYING
ONLY THOSE  FUNCTIONS  AND  VARIABLES  NEEDED  TO  PERFORM  THE
NECESSARY  TASKS.   FUNCTIONS  AND  VARIABLES  ARE  CONVENIENTLY
COLLECTED  INTO  GROUPS  WHICH  ARE  IDENTIFIED  IN  THE  'HOW'
VARIABLES.  FOR EXAMPLE, IF THE USER WANTS TO  GENERATE  STEMLEAF
OR BOXPLOT DISPLAYS HE CAN COPY THE DISPLAY GROUP AS FOLLOWS:
                         )COPY 2 OA3660 DISPLAY
     THE GROUP CONTAINS NOT  ONLY  THE  FUNCTIONS  BUT  ALSO  ALL
REQUIRED PARAMETERS AND DOCUMENTATION.
```

There is also a variable named DATAMAP which describes the data contained in OA3660 and provides a reference to the data source. This is shown below.

```
⍝THE VARIABLE DATAMAP PROVIDES INFORMATION ABOUT THE
⍝DATA SETS CONTAINED IN THE WORKSPACE.  IT GIVES THE
⍝SOURCE OF EACH DATA SET AND THE SIZE OF THE DATA ARRAY.
⍝SIMPLY TYPE 'DATAMAP' FOR DATA DOCUMENTATION.
```

```
      DATAMAP
THIS WORKSPACE CONTAINS SEVERAL DATA SETS THAT  CAN  BE  USED  TO
ILLUSTRATE THE FUNCTIONS OR TO SERVE AS HOMEWORK PROBLEMS.   THE
ENTIRE COLLECTION OF DATA ARRAYS IS CONTAINED IN THE GROUP  NAMED
DATA.  THE DATA CAME FROM THE FOLLOWING SOURCES:
     (1)DRAPER, N.R. AND H. SMITH, APPLIED  REGRESSION  ANALYSIS,
     WILEY AND SONS.
     (2)MCNEIL, D.R., INTERACTIVE DATA ANALYSIS, ADDISON-WESLEY.
     (3)MILLER, I. AND J.E. FREUND,  PROBABILITY  AND  STATISTICS
     FOR ENGINEERS, PRENTICE-HALL.
     (4)RICHARDS, F.R., CLASSROOM GRADES.
     (5)TUKEY, JOHN, EXPLORATORY DATA ANALYSIS, ADDISON-WESLEY.
THE TABLE BELOW LISTS EACH DATA ARRAY, THE DIMENSION, THE  SOURCE
(USING AUTHOR ABBREVIATIONS), AND PAGE OR CHAPTER NUMBERS.
          DATA                ⍴DATA         SOURCE

          AGES                  42        MC(P.17)
          CHICKWTS            14 6        MC(P.30)
          COAL                  49        TU
          CONSUMPTION          5 5        MC(P.100)
          CRIMES              50 4        MC(P.132)
          DEATHS               5 4        MC(P.94)
          DISCOVERIES          100        MC(P.121)
          DRAPERX             13 4        DS(P.178)
          DRAPERY               13        DS(P.178)
          GRADES1             15 5        RI
          GRADES2             15 5        RI
          HYDROPLANTS           34        TU(CH.3)
          INSECTS             12 6        MC(P.12,36)
          LANDAREAS             48        MC(P.9)
          MORTALITY            5 4        TU(CH.16)
          PRECIPITATION         69        MC(P.3)
          PRESRATING           114        MC(P.126)
          RIVERS               141        MC(P.14)
          TESTX               10 2        MF(P.253)
          TESTY                 10        MF(P.253)
          USPOP               19 2        TU(CH.8)
          VOLCANO              219        TU
          WARPBREAKS           9 6        MC(P.28)
```

Finally, notice that there are "HOW" variables for most of the functions contained in the workspace. (The only functions without "HOW" variables are utility functions which are used by other functions, but which are transparent to the user.) These variables provide documentation on the use of the functions. For example, documentation on the function SCAT is obtained by typing SCATHOW.

```
      SCATHOW
SYNTAX:  SCAT ARRAY
PARAMETERS:
          (1) WID- CONTROLS THE HORIZONTAL SIZE  OF  THE  DISPLAY
          (DEFAULT=30 CHARACTERS).
          (2) DEP- CONTROLS THE  VERTICAL  SIZE  OF  THE  DISPLAY
          (DEFAULT=15 LINES).
          (3) NDIVX, NDIVY- NUMBER OF UNITS  ON  X-  AND  Y-AXES,
          RESPECTIVELY (DEFAULT=4,4).
GROUP:  RELATIONS, SMOOTH, COMPARISONS
DESCRIPTION:  SCAT PRODUCES A SCATTER PLOT OF THE DATA  CONTAINED
IN ARRAY. THE ARGUMENT ARRAY CAN BE A VECTOR OR A MATRIX WITH  AS
MANY AS 9 COLUMNS. IF A  VECTOR  OF  SIZE  N,  THOSE  VALUES  ARE
PLOTTED VS. THE INTEGERS 1 TO N; IF A MATRIX, THE SECOND,  THIRD,
ETC. COLUMNS ARE  PLOTTED  VS.  COLUMN  1  ON  THE  SAME  AXES.
DIVISIONS ON THE AXES OF THE PLOT  ARE  NOT  EXPLICITLY  PRINTED,
EXCEPT AT THE EXTREMES OF THE PLOT.  THE  USER  CAN  CONTROL  THE
RESOLUTION OF THE PLOT BY  MODIFYING  THE  PARAMETERS  WID,  DEP,
NDIVX AND NDIVY.   PRINTING  TIME  INCREASES  DRAMATICALLY  WITH
RESOLUTION; THEREFORE, OTHER PLOT PROGRAMS SHOULD BE USED IF HIGH
RESOLUTION IS DESIRED. FOR A SINGLE GROUP OF DATA, THE  NUMBER  N
(2≤N≤9) WILL BE PRINTED IF N POINTS LIE  CLOSE  TOGETHER  ON  THE
DISPLAY.  FOR MULTIPLE PLOTS ON THE SAME DISPLAY,  THE  LETTER  A
REPRESENTS GROUP 1, B REPRESENTS GROUP 2,  ETC.    FOR  2  POINTS
CLOSE TOGETHER THE LETTER WILL BE PRINTED WITH  AN  UNDERSCORE.
THE DISPLAY CANNOT HANDLE 3 OR  MORE  POINTS  CLOSE  TOGETHER  IF
THERE ARE MULTIPLE PLOTS.
```

The format of SCATHOW is followed for every function. The function syntax, the user controlled parameters, the group (or groups) containing the functions, the subroutines used by the function, and a brief description of the use of the function are displayed.

The functions and variables are grouped into APL groups for ease of handling and to conserve space. The group structure is described below.

```
      )GRPS
COMPARISONS     DATA    DISPLAY DOC     ESSENTIALS      GEIT
RELATIONS       SMOOTH  STATS   TWOWAY
```

```
      )GRP COMPARISONS
CONDENSE        CONDENSEHOW     NUM     MISS    UTCOND  FMT     SC
SCATHOW LINE    LINEHOW NDIVX   NDIVY   WID     DEP     DEPTH   G
COMPARE COMPAREHOW      FILL    NUMSUM  NUMSUMHOW       RSELECT AN
ANDHOW  LSLINE  LSLINEHOW
```

```
      )GRP DATA
AGES    CHICKWTS        COAL    CONSUMPTION     CRIMES  DEATHS
DISCOVERIES     DRAPERX DRAPERY GRADES1 GRADES2 HYDROPLANTS
INSECTS LANDAREAS       MORTALITY       PRECIPITATION   PRESRATING
RIVERS  TESTX   TESTY   USPOP   WARPBREAKS      VOLCANO
```

```
      )GRP DISPLAY
STEMLEAF        STEMLEAFHOW     WIDTH   SCALE   LIT     BOXPLOT
BOXPLOTHOW      LENGTH  FILL    NUMSUM  NUMSUMHOW       MISS
CR
```

```
      )GRP DOC
ANDHOW  ANOVAHOW        A3RHOW  A3RSRHOW        BOXPLOTHOW
CHISQUAREHOW    CODERESHOW      COMPAREHOW      CONDENSEHOW
CONTINGENCYHOW  CORRELATIONHOW  DATAMAP DESCRIBE        KSHOW
LINEHOW LSLINEHOW       MEDPOLISHHOW    MSTATHOW        NUMSUMHOW
ONEHHOW ONE3HOW PARTIALHOW      REGRESSHOW      SCATHOW SHOWRESHOW
SPLITHOW        STATISTICSHOW   STEMLEAFHOW     TWICEHOW
```

```
      )GRP ESSENTIALS
AND     ANOVA   A3R     A3RSR   BOXPLOT CHISQUARE       [illegible]
COMPARE CONDENSE        CONTINGENCY     CORRELATION     [illegible]
DEPTH   EPSILON FILL    FMT     INPUT   KS      LENGTH  [illegible]     [illegible]
LSLINE  MEDPOLISH       MISS    NDIVX   NDIVY   NORMEFFECTS             [illegible]
NUMSUM  ONEH    ONE3    OPTION  REGRESS RESIDS  SCALE   SCAT
SHOWRES SPLIT   STEMLEAF        SUMSQ   TWICE   [illegible] WID         [illegible]
CR      MSTATS  PARTIAL STATISTICS              RSELECT ΔINTERCEPT




      )GRP GFIT
 KS      KSHOW   CHISQUARE       CHISQUAREHOW




      )GRP RELATIONS
LINE    LINEHOW LSLINE  LSLINEHOW       REGRESS REGRESSHOW
ANDHOW  RSELECT SCAT    SCATHOW WID     DEP     NDIVX   NDIVY
ΔINTERCEPT      FMT     CR




      )GRP SMOOTH
SPLIT   ONE3    ONEH    A3R     A3RSR   TWICE   SCAT    SPLITHOW
A3RHOW  A3RSRHOW        ONE3HOW ONEHHOW TWICEHOW        SCATHOW NDIVX
NDIVY   WID     DEP




      )GRP STATS
 CORRELATION     CR      FMT     MSTATS  PARTIAL STATISTICS      CR
 CORRELATIONHOW  MSTATSHOW       PARTIALHOW      STATISTICSHOW



      )GRP TWOWAY
MEDPOLISH       MEDPOLISHHOW    LINE    LINEHOW LSLINE  LSLINEHOW
RESIDS  EPSILON NORMEFFECTS     SHOWRES CODERES RSELECT SHOWRESHOW
CODERESHOW      AND     ANDHOW  CONTINGENCY     CONTINGENCYHOW  ANOVA
ANOVAHOW        OPTION  INPUT   SUMSQ
```

The user can conserve space in his active work area by selectively loading or copying only the required functions or groups. We have attempted to anticipate the type of analyses that the user will attempt, and the group structure has been selected with the objective to combine functions and parameters which naturally go hand-in-hand. A specific group can be selected by typing

```
)COPY 2 OA3660 GROUPNAME
```

where GROUPNAME is any one of the groups listed above. Two of the groups, ESSENTIALS and DOC, are especially useful. The ESSENTIALS group contains all of the functions and default values of all of the required parameters. Documentation and data are not included. The DOC group contains all of the documentation (DESCRIBE, DATAMAP, and "HOW" variables). The user may want to load the entire OA3660 workspace, check on some of the documentation, and then erase the group DOC to make room for user generated data and other functions or variables. The DOC group can be erased by typing)ERASE DOC. Similarly, any group can be erased by typing)ERASE GROUPNAME.

The following sections give brief descriptions (the writeups contained in the "HOW" variables) and examples of the functions contained in the OA3660 library. Each function description gives the syntax, a list of the parameters, a list of the groups which contain the function, a list of subroutines (other functions) used by the function, and a narrative about the use of the function. The narrative tells what the function does, describes any restrictions on the function arguments, and indicates how the function parameters affect the output. The order of presentation of the functions follows what appears to me to be a natural sequence of exposure to tools of data analysis.

The HOW variables are listed alphabetically in Appendix A, and the APL program listings are given in Appendix B.

B. Function Descriptions and Examples

```
      )GRP DISPLAY
STEMLEAF         STEMLEAFHOW      WIDTH   SCALE   LIT       BOXPLOT
BOXPLOTHOW       LENGTH   FILL    NUMSUM  NUMSUMHOW         MISS      B
CH



      STEMLEAFHOW
SYNTAX:  STEMLEAF VECTOR
GROUP:  DISPLAY
PARAMETERS:
         (1)  WIDTH- CONTROLS THE WIDTH (CHARACTERS PER LINE) OF
         THE DISPLAY (DEFAULT=70).
         (2)  SCALE- VARIES THE DEPTH  (STEM  INTERVAL)  OF  THE
         DISPLAY IN UNITS OF 1, 2, OR 0.5 TIMES A POWER OF 10.
         SELECT AN INTEGER FROM 1 TO 3 (DEFAULT=1).
SUBPROGRAM:  LIT
DESCRIPTION:  STEMLEAF GENERATES A STEM AND  LEAF  DISPLAY  OF  A
VECTOR OF OBSERVATIONS.  THE FUNCTION  AUTOMATICALLY  SCALES  THE
DATA USING A SCALING ROUTINE BASED ON THE RANGE AND SIZE  OF  THE
DATA VECTOR.  BY VARYING THE SCALE PARAMETER THE USER CAN  CHANGE
THE SIZE OF THE STEM, BUT IT WILL NOT NECESSARILY  BE  SCALED  BY
THE AMOUNT SPECIFIED.  TRY VARIOUS VALUES LIKE 1,2, AND 3 TO  SEE
WHICH CHOICE YIELDS THE BEST DISPLAY.  IF  A  LEAF  CONTAINS  TOO
MANY CHARACTERS TO BE  PRINTED  ON  A  LINE,  THE  LINE  WILL  BE
TRUNCATED AND THE NUMBER OF TRUNCATED CHARACTERS WILL BE  WRITTEN
AT THE END OF THE LINE.  IF THE STEM  INTERVAL  IS  TWO  TIMES  A
POWER OF TEN, THE LEAVES MAY CONTAIN THE  CHARACTERS  A,B,C,...,*
IN ADDITION  TO  THE  DIGITS  0,1,...,9.   IN  THIS  CASE,  THE
CHARACTERS A TO * REPRESENT THE NUMBERS 10 TO 19.



      SCALE
1
```

```
      STEMLEAF VOLCANO
00|25666799
01|0001366799
02|0011222444556667788999
03|01122445555667899
04|0111233333444678899999
05|001122234455666666677799
06|00114455666677788 9
07|00001112334555678889
08|1222233335679
09|0001233445566779
10|0112233445689
11|0112334669
12|11244456
13|03478
14|00
15|667
16|25
17|29
18|5
19|03379


      SCALE←.5

      STEMLEAF VOLCANO
00|25666799AAABDGGH··
02|0011222444556667788999ABBCCEEEFFGGGHI
04|0111233333444678899999AABBCCCDEEFFGGGGGHHH
06|001144556666777889AAAABBBCDDEFFFGHIII-
08|122223335679AAABCDDEEEFGHH·
10|0112233445689ABBCDDEGG·
12|11244456ADEHI
14|00GGH
16|25C-
18|5ADDH·




      ⍝ CHANGING SCALE TO .5 REDUCED THE NUMBER OF STEMS.
      ⍝ INCREASING SCALE WILL ALWAYS RESULT IN MORE STEMS OR
      ⍝ THE SAME NUMBER.
      BOXPLOTHOW
SYNTAX:  BOXPLOT VECTOR
PARAMETER:
          LENGTH- CONTROLS THE HORIZONTAL  SIZE  OF  THE  DISPLAY
          (DEFAULT=50  CHARACTERS).
GROUP:  DISPLAY
SUBPROGRAM:  FILL
DESCRIPTION:  BOXPLOT GENERATES A BOX PLOT DISPLAY FOR  A  VECTOR
OF DATA.  A RECTANGULAR BOX WITH ENDS CORRESPONDING TO LOWER  AND
UPPER QUARTILES IS PRESENTED  WITH  THE  MEDIAN  MARKED  WITH  AN
ASTERISK.  WHISKERS ARE DRAWN  ON  EACH  SIDE  OF  THE  BOX  WITH
CROSSES MARKING THE LOWEST AND  HIGHEST  DATA  VALUES  WITHIN  AN
INTERQUARTILE DISTANCE OF THE QUARTILES.  DATA VALUES OUTSIDE THE
CROSSES (OUTLIERS) ARE MARKED WITH CIRCLES AND  THOSE  MORE  THAN
1.5 INTERQUARTILE DISTANCES GET HEAVY CIRCLES.
```

```
      BOXPLOT VOLCANO
2                                               199
             |-------------|
 ××××××××|        *        |×××××××××××××× ○○○○ ○  ⊛⊛⊛⊛
             |_____________|                          22
```

```
      ⍝ WE CAN SQUEEZE THE BOXPLOT IN OR STRETCH IT OUT BY
      ⍝ CHANGING LENGTH.
```

```
      LENGTH←30

      BOXPLOT VOLCANO
2                           199
         |--------|
 ××××|      *      |×××××    ○○○○⊛⊛⊛
         |________|          32    32
```

```
      LENGTH←70
      BOXPLOT VOLCANO
2
      199
                 |---------------------|
 ×××××××××××|          *           |××××××××××××××      ○ ○○   ○ ○ ⊛  ⊛⊛⊛
                 |_____________________|                    3               2
      NUMSUMHOW
SYNTAX: NUMSUM VECTOR      OR      NUMSUM ARRAY
PARAMETER:
          MISS← NUMBER USED TO INDICATE MISSING VALUE IN THE DATA
          ARRAY (DEFAULT=¯99999).
GROUP:  COMPARISONS
SUBPROGRAM:  FMT
DESCRIPTION:  NUMSUM OPERATES ON EITHER A VECTOR OR AN ARRAY BUT,
IN ALL CASES, THE DATA ARE TREATED AS A  SINGLE  BATCH.   NUMSUM
PRODUCES A NUMERICAL SUMMARY WHICH GIVES THE SAMPLE  SIZE  (AFTER
DELETION OF MISSING  VALUES),  THE  EIGHTHS,  THE  EXTREMES,  THE
SPREADS, AND THE  MIDPOINTS IN TABULAR FORM.   THIS  SUMMARY  IS
USEFUL FOR TESTING THE SYMMETRY OF A DATA SET,  AND  TO  EVALUATE
THE EFFECTIVENESS OF DATA TRANSFORMATIONS IN PRODUCING SYMMETRY.



      NUMSUM VOLCANO


              NUMERICAL SUMMARY
---------------------------------------------------------------------
SAMPLE SIZE = 219
---------------------------------------------------------------------
    MIDPTS    LOQ/8/MIN          MEDIAN    UPQ/8/MAX        SPREADS
     65.00 |             |        65.00 |             |             |
     66.50 |       37.00 |              |       96.00 |       59.00 |
     72.50 |       24.00 |              |      121.00 |       97.00 |
    100.50 |        2.00 |              |      199.00 |      197.00 |
---------------------------------------------------------------------


      ⍝ THE STEMLEAF, THE BOXPLOT, AND THE NUMERICAL SUMMARY ALL
      ⍝ SUGGEST THAT THE VOLCANO DISTRIBUTION IS POSITIVELY
      ⍝ SKEWED.  TRY A LOG TRANSFORM TO SEE IF THAT WILL MAKE
      ⍝ THE DISTRIBUTION MORE NEARLY SYMMETRIC.

      NUMSUM ⍟ VOLCANO


              NUMERICAL SUMMARY
---------------------------------------------------------------------
SAMPLE SIZE = 219
---------------------------------------------------------------------
    MIDPTS    LOQ/8/MIN          MEDIAN    UPQ/8/MAX        SPREADS
      4.17 |             |         4.17 |             |             |
      4.09 |        3.61 |              |        4.56 |        0.95 |
      3.99 |        3.18 |              |        4.80 |        1.62 |
      2.99 |        0.69 |              |        5.29 |        4.60 |
---------------------------------------------------------------------
```

```
      ⍝ THERE IS NOW A DECREASING TREND IN THE MIDPTS COLUMN.
      ⍝ THAT SUGGESTS THAT THE LOG IS TOO EXTREME A TRANSFORMATION.
      ⍝ TRY SQUARE ROOT.

      NUMSUM VOLCANO*.5

                NUMERICAL SUMMARY
------------------------------------------------------------------------
SAMPLE SIZE = 219
------------------------------------------------------------------------
   MIDPTS     LOQ/8/MIN        MEDIAN    UPQ/8/MAX        SPREADS
      8.06 |             |        8.06 |             |             |
      7.94 |        6.08 |             |        9.80 |        3.72 |
      7.95 |        4.90 |             |       11.00 |        6.10 |
      7.76 |        1.41 |             |       14.11 |       12.69 |
------------------------------------------------------------------------


      ⍝ THAT LOOKS A LOT BETTER.  LET US OBTAIN THE BOXPLOT
      ⍝ AND STEMLEAF PLOT OF THE SQUARE ROOT TRANSFORMED DATA.


      BOXPLOT VOLCANO*.5
1.4
      14.1
                         |---------------------|
O   O  xxxxxxxxxxxxxxxxxx|          *          |xxxxxxxxxxxxxxxxxx OOO
                         |---------------------|                     2

      LENGTH←50


      BOXPLOT VOLCANO*.5
1.4                                            14.1
                  |-------------|
O  O xxxxxxxxxxxxx|      *      |xxxxxxxxxxxxx OO
                  |-------------|               3

      ⍝ THE BOXPLOT LOOKS A LOT MORE SYMMETRIC.  NOW FOR THE
      ⍝ STEMLEAF PLOT:
```

```
      STEMLEAF VOLCANO*.5
01|4
02|24446
03|0022236
04|001445566777999
05|00111223344456677889999
06|00012223444566666666 8999
07|0000011112223334455555555577778 8
08|0011111122222344444445556777788889
09|01111111233455556667777888 9
10|00011112223445556667889
11|00011122456 7788
12|55578
13|146899
14|01
```

```
      )GRP COMPARISONS
CONDENSE        CONDENSEHOW     NUM     MISS    UTCOND  FMT     SCAT
SCATHOW LINE    LINEHOW NDIVX   NDIVY   WID     DEP     DEPTH   NGAP
COMPARE COMPAREHOW      FILL    NUMSUM  NUMSUMHOW       RSELECT AND
ANDHOW  LSLINE  LSLINEHOW
```

```
      ANDHOW
SYNTAX:  X  AND  Y
GROUPS:  RELATIONS, TWOWAY, COMPARISONS
DESCRIPTION:  THE FUNCTION 'AND' IS USED TO  CREATE  A  NEW  DATA
ARRAY CONSISTING OF X AUGMENTED BY Y AS ADDITIONAL  COLUMNS.    X
AND Y CAN BE SCALARS, VECTORS, OR MATRICES  BUT  CANNOT  BOTH  BE
SCALARS.  IF AN ARGUMENT IS A SCALAR, A COLUMN IS GENERATED  EACH
ELEMENT OF WHICH IS THE SCALAR.  IF THE ARGUMENTS ARE VECTORS  OR
MATRICES, THEY MUST BE CONFORMABLE.


      ⍝ THE FUNCTION 'AND' IS USEFUL FORDATA ENTRY AND MANIPULA-
      ⍝ TION.


      X←3 4 5
      Y←9 10 12
      X AND Y
  3   9
  4  10
  5  12
      Z←3 2⍴⍳6
      X AND Z
 3  1  2
 4  3  4
 5  5  6
      50 AND Z
 50   1   2
 50   3   4
 50   5   6
      50 AND X
 50   3
 50   4
 50   5


      ⍝ EXCEPT WHEN ONE ARGUMENT IS A SCALAR, THE ARGUMENTS OF
      ⍝ AND MUST BE CONFORMABLE IN SIZE.

      W←4 6 8 10
      X AND W
ARGUMENTS OF  AND  ARE NOT CONFORMABLE.
      W AND Z
ARGUMENTS OF  AND  ARE NOT CONFORMABLE.
```

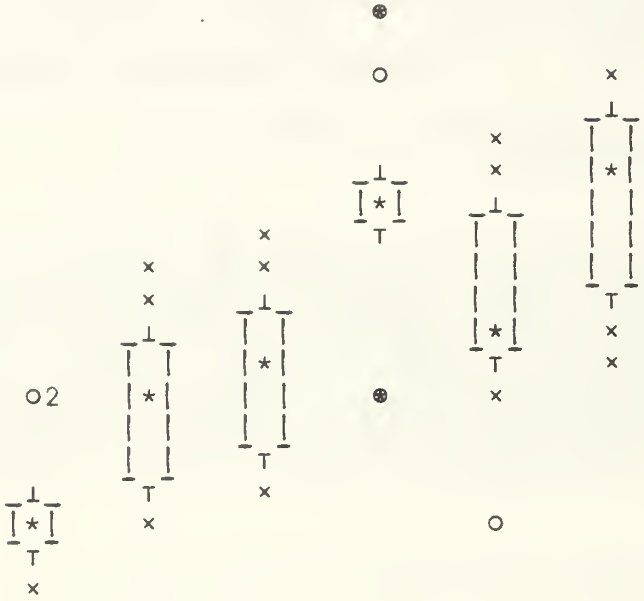
```
      COMPAREHOW
SYNTAX: COMPARE MATRIX
PARAMETERS:
           (1) DEPTH- VERTICAL HEIGHT OF DISPLAY (DEFAULT=20
           LINES).
           (2) MISS- NUMBER USED TO INDICATE MISSING VALUES
           (DEFAULT =¯99999)
           (3) NGAP- NUMBER OF HORIZONTAL SPACES BETWEEN THE
           BOXPLOT DISPLAYS (DEFAULT=3).
GROUP: COMPARISONS
SUBPROGRAM: FILL
DESCRIPTION: COMPARE OPERATES ON AN N BY K MATRIX TO PRODUCE K
VERTICAL BOX PLOTS PLACED NEXT TO EACH OTHER TO ALLOW VISUAL
COMPARISON OF THE CENTERS, SPREADS, AND OUTLIERS OF THE BATCHES
(COLUMNS) OF THE MATRIX. THE USER MUST FILL UP THE MATRIX SO
THAT THERE ARE N OBSERVATIONS FOR EACH BATCH.  THE PARAMETER,
MISS, SHOULD BE USED TO FILL IN MISSING VALUES. THE USER SHOULD
ASSURE THAT MISS IS DIFFERENT FROM ALL VALID ENTRIES IN THE DATA
ARRAY.



      DEPTH
20
      MISS
¯99999
      NGAP
3


      ⍝ WE WILL DEMONSTRATE COMPARE WITH THE CHICKWT DATA.
      ⍝ SINCE WE USED 0 TO INDICATE MISSING VALUES IN THAT
      ⍝ DATA, WE MUST FIRST ALTER THE PARAMETER MISS.


      MISS←0
      COMPARE CHICKWTS
423
108
```



```
      ⍝ THE DIAGRAM REVEALS RATHER LARGE DIFFERENCES IN THE
      ⍝ MIDSPREADS OF THE CHICKWT DATA.  WE SHOULD TRANSFORM
      ⍝ THE DATA TO TRY TO ACHIEVE HOMOGENIETY IN THE SPREADS.
      ⍝  FIRST LETS GET A NUMERICAL SUMMARY OF THE DIFFERENT COLUMNS.


      CONDENSEHOW
SYNTAX:  CONDENSE MATRIX OR R←CONDENSE MATRIX
PARAMETERS:
        (1)  NUM: CONTROLS WHAT STATISTICS ARE INCLUDED IN  THE
        SUMMARY.  NUM∊[1,2,5,7] (DEFAULT=2).
        NUM=1 GIVES MEDIANS OF EACH COLUMN OF THE MATRIX
        NUM=2 GIVES MEDIANS AND INTERQUARTILE RANGES
        NUM=5 GIVES MIN,QUARTILES,MAX, AND SIZE
        NUM=7 GIVES MIN,EIGHTHS,MAX AND SIZE
        (2)    MISS:  NUMBER  USED  TO  CODE   MISSING   VALUES
        (DEFAULT=¯99999).
GROUP:  COMPARISONS
SUBPROGRAMS:  UTCOND, FMT
DESCRIPTION:  CONDENSE  GENERATES  SUMMARY  STATISTICS  FOR  EACH
GROUP OF DATA REPRESENTED BY THE COLUMNS OF THE ARGUMENT MATRIX.
SINCE THE ARGUMENT IS A MATRIX, THE USER MUST FILL UP THE MISSING
VALUES IN THE MATRIX WHENEVER THE GROUPS (COLUMNS) HAVE DIFFERENT
NUMBERS OF OBSERVATIONS.  THE PARAMETER, MISS, SHOULD BE USED  TO
FILL THE MATRIX SINCE THE FUNCTION WILL RECOGNIZE THOSE VALUES AS
MISSING DATA AND WILL IGNORE THEM IN ALL CALCULATIONS.        THE
RESULT FROM CONDENSE  CAN  BE  USED  AS  THE  ARGUMENT  OF  OTHER
FUNCTIONS SUCH AS SCAT OR LINE IF AND ONLY IF NUM=2.
```

```
      NUM
2
      MISS
0


      CONDENSE CHICKWTS
    151.5                43
    221                  83.5
    248                  72
    328                  33
    263                  83
    342                 102

      ⍝ THE ABOVE DATA ARE THE MEDIANS AND MIDSPREADS FOR EACH
      ⍝ OF THE 6 BATCHES (COLUMNS) OF CHICKWT DATA.  ZERO WAS
      ⍝ ENTERED INTO THE PARAMETER MISS EARLIER.  THE MIDSPREADS
      ⍝ SHOW QUITE A DISPERSION, FROM AS SMALL AS 151.5 TO AS LARGE
      ⍝ AS 342.


      ⍝ WE CAN GET MORE INFORMATION ABOUT THE INDIVIDUAL COLUMNS
      ⍝ OF CHICKWTS BY CHANGING NUM AS FOLLOWS:



      NUM←5
      CONDENSE CHICKWTS
      MIN        LOQ       MEDIAN        UPQ        MAX         SIZE
    108.00     136.00     151.50     179.00     227.00        10.00
    141.00     175.00     221.00     258.50     309.00        12.00
    158.00     199.00     248.00     271.00     329.00        14.00
    226.00     307.50     328.00     340.50     423.00        12.00
    153.00     242.00     263.00     325.00     380.00        11.00
    216.00     271.50     342.00     373.50     404.00        12.00


      ⍝ IN SEEKING OUT AN APPROPRIATE TRANSFORMATION TO EVEN OUT
      ⍝ THE MIDSPREADS, IT IS OFTEN USEFUL TO PLOT THE LOG OF THE
      ⍝ MIDSPREADS VS. THE LOG OF THE MEDIANS.
      ⍝ IN MANY CASES WE NEED TO LOOK AT A SCATTER PLOT OF OUR
      ⍝ DATA, OR AT SCATTER PLOTS OF FUNCTIONS OF OUR DATA.
      ⍝ LET US INTRODUCE A FUNCTION SCAT THAT WILL PROVIDE THE
      ⍝ NEEDED SCATTER PLOT.
      SCATHOW
SYNTAX: SCAT ARRAY
PARAMETERS:
          (1) WID- CONTROLS THE HORIZONTAL SIZE OF THE DISPLAY
          (DEFAULT=30 CHARACTERS).
          (2) DEP- CONTROLS THE VERTICAL SIZE OF THE DISPLAY
          (DEFAULT=15 LINES).
          (3) NDIVX, NDIVY- NUMBER OF UNITS ON X- AND Y-AXES,
          RESPECTIVELY (DEFAULT=4,4).
GROUP: RELATIONS, SMOOTH, COMPARISONS
DESCRIPTION: SCAT PRODUCES A SCATTER PLOT OF THE DATA CONTAINED
IN ARRAY. THE ARGUMENT ARRAY CAN BE A VECTOR OR A MATRIX WITH AS
MANY AS 9 COLUMNS. IF A VECTOR OF SIZE N, THOSE VALUES ARE
PLOTTED VS. THE INTEGERS 1 TO N; IF A MATRIX, THE SECOND, THIRD,
ETC. COLUMNS ARE PLOTTED VS. COLUMN 1 ON THE SAME AXES.
DIVISIONS ON THE AXES OF THE PLOT ARE NOT EXPLICITLY PRINTED,
EXCEPT AT THE EXTREMES OF THE PLOT. THE USER CAN CONTROL THE
RESOLUTION OF THE PLOT BY MODIFYING THE PARAMETERS WID, DEP,
NDIVX AND NDIVY.  PRINTING TIME INCREASES DRAMATICALLY WITH
RESOLUTION; THEREFORE, OTHER PLOT PROGRAMS SHOULD BE USED IF HIGH
RESOLUTION IS DESIRED. FOR A SINGLE GROUP OF DATA, THE NUMBER N
(2≤N≤9) WILL BE PRINTED IF N POINTS LIE CLOSE TOGETHER ON THE
DISPLAY. FOR MULTIPLE PLOTS ON THE SAME DISPLAY, THE LETTER A
REPRESENTS GROUP 1, B REPRESENTS GROUP 2, ETC.  FOR 2 POINTS
CLOSE TOGETHER THE LETTER WILL BE PRINTED WITH AN UNDERSCORE.
THE DISPLAY CANNOT HANDLE 3 OR MORE POINTS CLOSE TOGETHER IF
THERE ARE MULTIPLE PLOTS.


      WID
30
      DEP
15
      NDIVX
4
      NDIVY
4


      X←ι10
      Y1←2 3 5 6 8 10 11 13 15 18
      Y2←20 20 17 24 21 26 31 30 37 33
      SCAT X AND Y1
RANGE OF X: 0  10
RANGE OF Y: 0  20
|
|                        o
|
|                      o
|                   o
|                 o
|              o
|            o
|         o
|       o
|    o
|  o
|¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯
```

```
      SCAT X AND Y1 AND Y2
RANGE OF X: 0  10
RANGE OF Y: 0  40
|
|                      B B
|                 B B
|         B    B
|  B B       B           A
|       B           A  A
|            A A  A
|    A  A A
|¯¯A¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯
```

```
      ⍝ IF THE ARGUMENT OF SCAT IS A VECTOR, SCAT WILL CREATE
      ⍝ ABSCISSA VALUES TO BE THE POSITIVE INTEGERS 1 TO ⍴ARGUMENT.
```

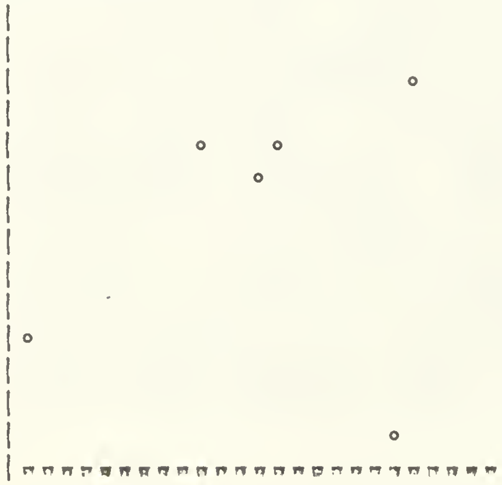
```
      SCAT Y2
RANGE OF X: 0  10
RANGE OF Y: 15  40
|
|                      o
|
|                        o
|                 o o
|
|         o    o
|
|  o o       o
|       o
|¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯¯
```

```
      ⍝ BACK TO THE PROBLEM OF NONHOMOGENEOUS MIDSPREADS IN THE
      ⍝ CHICKWT DATA.  LET US LOOK AT A SCATTER PLOT OF THE
      ⍝ LOG MIDSPREADS V. LOG MEDIANS.

      ⍝ FIRST WE RESET PARAMETER NUM TO 2, SO IT WILL GIVE
      ⍝ MEDIANS AND MIDSPREADS.

      NUM←2

      SCAT ⍟CONDENSE CHICKWTS
RANGE OF X: 5   6
RANGE OF Y: 3.4   4.8
```



```
      ⍝ THE SCATTER PLOT SUGGESTS A RELATIONSHIP BETWEEN MIDSPREADS
      ⍝ AND MEDIANS.  PERHAPS SOME ROOT OF THE DATA WOULD MAKE
      ⍝ THE MIDSPREADS MORE HOMOGENEOUS.  TRY SQUARE ROOT.

      CONDENSE CHICKWTS*.5
   12.30368569        1.717184371
   14.86363273        2.851055496
   15.74801575        2.355341653
   18.11001266        0.9195158937
   16.21727474        2.471407191
   18.4912651         2.852064545

      ⍝ THAT IS BETTER (RATIO OF MAX MIDSPREAD TO MIN MIDSPREAD
      ⍝ IS ABOUT 1.5.  MORE WORK NEEDS TO BE DONE THOUGH.
      )GRP RELATIONS
LINE    LINEHOW LSLINE  LSLINEHOW        REGRESS REGRESSHOW        AND
ANDHOW  RSELECT SCAT    SCATHOW WID      DEP     NDIVX   NDIVY
ΔINTERCEPT      FMT     CR
```

```
      LINEHOW
SYNTAX:  LINE ARRAY      OR      Z←LINE ARRAY
PARAMETER:
          RSELECT- SELECTS  THE  OUTPUT  MATRIX  OF  RESIDUALS.
          RSELECT=1 GIVES ABSCISSA VS.  RESIDUALS  (DEFAULT=1).
          RSELECT≠1 GIVES FITTED VALUES VS. RESIDUALS
GROUP:  RELATIONS
DESCRIPTION:  LINE FITS A STRAIGHT LINE TO A SET OF (X,Y)  POINTS
BY DIVIDING THE POINTS INTO 3 REGIONS AND USING  THE  MEDIANS  OF
THE X AND Y VALUES IN THE OUTER REGIONS TO DETERMINE THE SLOPE.
THE INTERCEPT IS THE MEDIAN OF THE DIFFERENCES Y-SLOPE×X.    LINE
ALSO COMPUTES THE RESIDUALS AND GIVES AN N BY 2 MATRIX CONTAINING
EITHER THE X-VALUES  VS.  RESIDUALS  OR  THE  FITTED  VALUES  VS.
RESIDUALS DEPENDING ON THE PARAMETER, RSELECT.  IF THE USER  DOES
NOT WANT RESIDUALS TYPED OUT, HE SHOULD USE THE SYNTAX:
                         Z←LINE ARRAY
THE ARGUMENT ARRAY CAN BE EITHER A VECTOR OR A 2-COLUMN MATRIX.
IF THE ARGUMENT  IS  A  VECTOR  OF  SIZE  N,  THE  X-VARIABLE  IS
CONSTRUCTED TO BE THE FIRST N POSITIVE INTEGERS.  IF THE ARGUMENT
IS A 2-COLUMN MATRIX, THE FIRST COLUMN IS TAKEN TO BE THE SET  OF
X-VALUES AND THE SECOND COLUMN THE SET OF Y-VALUES.  LINE CAN  BE
USED IN CON■UNCTION WITH THE FUNCTION SCAT TO  PRODUCE THE SLOPE,
THE INTERCEPT, AND A PLOT OF THE RESIDUALS.  TO DO THIS, ENTER:
                         SCAT LINE ARRAY
      X←2 3 4 3 5 6 7 6 7 5 9 8 10 11 12 14
      ρX
16
      ARRAY←X AND Y
      LINE ARRAY
SLOPE: 1.375 Y-INTERCEPT: 0.0625
    2                    0.1875
    3                   ¯0.1875
    4                   ¯1.5625
    3                    0.8125
    5                    1.0625
    6                   ¯2.3125
    7                   ¯5.6875
    6                   ¯0.3125
    7                   ¯0.6875
    5                    3.0625
    9                   ¯0.4375
    8                    3.9375
   10                    2.1875
   11                   ¯1.1875
   12                    1.4375
   14                    0.6875
      RSELECT←0
      LINE ARRAY
SLOPE: 1.375 Y-INTERCEPT: 0.0625
    2.8125               0.1875
    4.1875              ¯0.1875
    5.5625              ¯1.5625
    4.1875               0.8125
    6.9375               1.0625
    8.3125              ¯2.3125
    9.6875              ¯5.6875
    8.3125              ¯0.3125
    9.6875              ¯0.6875
    6.9375               3.0625
   12.4375              ¯0.4375
   11.0625               3.9375
   13.8125               2.1875
   15.1875              ¯1.1875
   16.5625               1.4375
   19.3125               0.6875
      RSELECT←1
      SCAT LINE ARRAY
SLOPE: 1.375 Y-INTERCEPT: 0.0625
RANGE OF X: 2  14
RANGE OF Y: ¯6  4
|                          o
|             o
|                                    o
|    o        o                                o        o
o----o------------o--------------o----------------------
|                      o                  o
|        o        o
|
|
|                      o
```

```
      Y
3  4  4  5  8  6  4  8  9  10  12  15  16  14  18  20
      ρY
16
      LINE Y
SLOPE: 1.090909091 Y→INTERCEPT: 0.6818181818
   1                    1.227272727
   2                    1.136363636
   3                    0.04545454545
   4                   ¯0.04545454545
   5                    1.863636364
   6                   ¯1.227272727
   7                   ¯4.318181818
   8                   ¯1.409090909
   9                   ¯1.5
  10                   ¯1.590909091
  11                   ¯0.6818181818
  12                    1.227272727
  13                    1.136363636
  14                   ¯1.954545455
  15                    0.9545454545
  16                    1.863636364
      X←ι16
      ARRAY←X AND Y
      LINE ARRAY
SLOPE: 1.090909091 Y→INTERCEPT: 0.6818181818
   1                    1.227272727
   2                    1.136363636
   3                    0.04545454545
   4                   ¯0.04545454545
   5                    1.863636364
   6                   ¯1.227272727
   7                   ¯4.318181818
   8                   ¯1.409090909
   9                   ¯1.5
  10                   ¯1.590909091
  11                   ¯0.6818181818
  12                    1.227272727
  13                    1.136363636
  14                   ¯1.954545455
  15                    0.9545454545
  16                    1.863636364

      SCAT LINE Y
SLOPE: 1.090909091 Y→INTERCEPT: 0.6818181818
RANGE OF X: 0  20
RANGE OF Y: ¯6  2
|              o                              o
|   o  o                           o o
|                                          o
| ¬¬¬¬¬¬¬o¬¬o¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬¬
|                               o
|                 o    o  o  o
|                                       o
|
|                    o
|
      RSELECT←1
      Z←LINE Y2
SLOPE: 1.857142857 Y-INTERCEPT: 17.42857143


      LSLINEHOW
SYNTAX:  LSLINE ARRAY     OR     Z←LSLINE ARRAY
GROUP:  RELATIONS
DESCRIPTION:  LSLINE  DETERMINES  THE  LEAST  SQUARES  SOLUTION,
Y=YI+SLOPE×X.  THE ARGUMENT ARRAY CAN BE A VECTOR OR  A  2-COLUMN
MATRIX.  IF THE ARGUMENT IS A VECTOR, THE X-VALUES ARE  TAKEN  TO
BE THE INTEGERS 1 TO N WHERE N=⍴ARRAY.   IF  THE  ARGUMENT  IS  A
2-COLUMN MATRIX, COLUMN 1 CONSISTS OF THE X-VALUES AND  COLUMN  2
THE Y-VALUES. RESIDUALS ARE DETERMINED AND  STORED  IN  A  MATRIX
WHOSE FIRST COLUMN IS THE SET OF X-VALUES AND WHOSE SECOND COLUMN
IS THE SET OF RESIDUALS.  IF THE USER WANTS TO SUPPRESS  PRINTOUT
OF THE RESIDUALS, HE MUST ASSIGN  THE  RESULTS  OF  LSLINE  TO  A
VARIABLE; I.E., TYPE Z←LSLINE ARRAY.


      SCAT LSLINE X AND Y2
SLOPE: 1.933333333  Y-INTERCEPT: 16.86666667
RANGE OF X: 0  10
RANGE OF Y: ¯4  4
|
|
|              o       o
|
|  o    o
|                   o
|-------------------------
|    o       o
|                 o
|                        o
|
|         o
|


      ⍝IF THE USER WANTS TO REGRESS A RESPONSE VARIABLE ON
      ⍝ A SET OF CARRIERS, HE CAN USE THE PROGRAM REGRESS.
      ⍝ THIS LEAST SQUARES MULTIPLE REGRESSION PROGRAM IS
      ⍝ VERY POWERFUL AND FLEXIBLE.
      REGRESSHOW
SYNTAX:  Z←Y REGRESS X
PARAMETER:
            ΔINTERCEPT- DETERMINES WHETHER OR NOT AN INTERCEPT TERM
            IS TO BE INCLUDED.  ΔINTERCEPT=1  GIVES  AN  INTERCEPT
            TERM, AND ΔINTERCEPT=0 GIVES NO INTERCEPT. (DEFAULT  IS
            1.)
GROUP:  RELATIONS
SUBPROGRAMS:  FMT AND SCAT
DESCRIPTION:    REGRESS  DOES  A  MULTIPLE  REGRESSION   ANALYSIS
RELATING THE DEPENDENT VARIABLE Y TO A SET  OF  CARRIERS  X.  THE
LEFT ARGUMENT Y IS A VECTOR OF SIZE N.  THE RIGHT ARGUMENT  X  IS
AN N BY K MATRIX CONSISTING  OF  N  OBSERVATIONS  ON  EACH  OF  K
VARIABLES OR A VECTOR OF SIZE N IF K=1.  OUTPUT  CONSISTS  OF  AN
ANOVA TABLE, R-SQUARE, STD. ERROR, REGRESSION  COEFFICIENTS  (THE
FIRST COEFFICIENT  IS  THE  CONSTANT  TERM  IF  ΔINTERCEPT=1.),
T-STATISTICS,    VARIANCE-COVARIANCE    MATRIX,    DURBIN-WATSON
STATISTIC, AND A VECTOR OF  PREDICTED  Y  VALUES  AND  RESIDUALS.
THERE IS AN OPTION THAT ALLOWS THE USER TO INPUT A  VECTOR  OF  X
VALUES AND USE THE REGRESSION EQUATION TO FORECAST Y VALUES.  THE
USER CAN ALSO OBTAIN A SCATTER  PLOT  OF  THE  RESIDUALS.   WHEN
EXECUTION TERMINATES, THE PREDICTED Y VALUES  AND  THE  RESIDUALS
RESIDE IN THE N BY 2 MATRIX Z.

      ΔINTERCEPT
1

      ⍴DRAPERX
13  4
      ⍝LETS REGRESS A RESPONSE VARIABLE DRAPERY ON THE FOUR
      ⍝ CARRIERS IN THE MATRIX DRAPERX.
      Z←DRAPERY REGRESS DRAPERX

                              ANOVA

    SOURCE  DF      SUM SQUARES      MEAN SQUARE          F-RATIO
REGRESSION   4        2.6679E3         6.6697E2          1.1148E2
  RESIDUAL   8        4.7864E1         5.9830E0
TOTAL       12        2.7158E3

R SQUARE:  0.9823756203
STD ERROR: 2.446007963
   COEFFICIENTS   T STATISTICS
        62.4054          0.8906
         1.5511          2.0827
         0.5102          0.7049
         0.1019          0.135
        ¯0.1441         ¯0.2032
DO YOU WANT A PRINTOUT OF THE VARIANCE-COVARIANCE MATRIX?
Y
VARIANCE-COVARIANCE MATRIX:
   4.9099E+3  ¯5.0507E+1  ¯5.0603E+1  ¯5.1660E+1  ¯4.9597E+1
  ¯5.0507E+1   5.5468E¯1   5.1266E¯1   5.5425E¯1   5.0529E¯1
  ¯5.0603E+1   5.1266E¯1   5.2387E¯1   5.2570E¯1   5.1213E¯1
  ¯5.1660E+1   5.5425E¯1   5.2570E¯1   5.6959E¯1   5.1688E¯1
  ¯4.9597E+1   5.0529E¯1   5.1213E¯1   5.1688E¯1   5.0275E¯1
DURBIN-WATSON: 2.052596933
DO YOU WANT TO FORECAST A VALUE FOR Y?
20 30 15 40
DO YOU WANT TO SCAT RESIDUALS VS. PREDICTED Y?
Y
RANGE OF X: 70  120
RANGE OF Y: ¯4  4
|                 o
|
|
|     o
|o         o
|                    o
|---o--------o---------o--
|
|                o
|         o       o  o
|
|  o
|
      )GRP SMOOTH
SPLIT   ONE3    ONEH    A3R     A3RSR   TWICE   SCAT    SPLITHOW
A3RHOW  A3RSRHOW        ONE3HOW ONEHHOW TWICEHOW        SCATHOW NDIVX
NDIVY   WID     DEP




      ONE3HOW
SYNTAX:  ONE3 VECTOR
GROUP:  SMOOTH
DESCRIPTION:  ONE3 SMOOTHS A VECTOR OF DATA  USING  ONE  PASS  OF
RUNNING MEDIANS OF 3 WITH TUKEY'S END-POINT RULE.  WHEN SMOOTHING
(X,Y) PAIRS, THE USER SHOULD USE AS THE  ARGUMENT  VECTOR  THE  Y
VALUES ORDERED ACCORDING TO THE MAGNITUDE OF THE X VALUES:
                              VECTOR←Y[⍋X]
IT IS ASSUMED  THAT  THE  X  VALUES  ARE  EQUISPACED.   REPEATED
SMOOTHING BY MEDIANS OF 3 CAN BE ACCOMPLISHED WITH A3R.   OUTPUT
CONSISTS OF THE SMOOTHED  SEQUENCE.   A  PLOT  OF  THE  SMOOTHED
SEQUENCE IS GIVEN BY TYPING:
                           SCAT ONE3 VECTOR



      X
3  2  3  7  4  3  2  15  4  5  3  6

      ONE3 X
2  3  3  4  4  3  3  4  5  4  5  3

      SPLITHOW
SYNTAX:  SPLIT A3R VECTOR
GROUP:  SMOOTH
DESCRIPTION:  SPLIT DOES ONE PASS AT  DIVIDING  MESAS  (PAIRS  OF
AD■ACENT POINTS WITH A COMMON VALUE WHICH IS A LOCAL MAX OR  MIN)
USING TUKEY'S END-POINT RULE.  IT IS  USED  IN  CON^UNCTION  WITH
A3R.



      SPLIT ONE3 X
2  3  3  3  3  4  3  4  5  4  5  3



      A3RHOW
SYNTAX:  A3R VECTOR
GROUP:  SMOOTH
SUBPROGRAM:  ONE3
DESCRIPTION: A3R DOES REPEATED SMOOTHINGS OF RUNNING MEDIANS OF 3
UNTIL THERE ARE NO CHANGES IN  THE  SMOOTHED  SEQUENCE  FROM  ONE
ITERATION TO THE NEXT.  SEE ONE3HOW.
```

```
      A3R X
3  3  3  4  4  3  3  4  4  4  4  4
```

```
      A3RSRHOW
SYNTAX:  A3RSR VECTOR
GROUP:  SMOOTH
SUBPROGRAMS:  A3R, ONE3, SPLIT
DESCRIPTION:  A3RSR DOES REPEATED SMOOTHINGS BY  RUNNING  MEDIANS
OF 3 FOLLOWED BY SPLITTING MESAS AND REPEATING UNTIL CONVERGENCE.
 SEE A3R AND SPLIT.
```

```
      A3RSR X
3  3  3  3  3  4  4  4  4  4  4  4
```

```
      ONEHHOW
SYNTAX:  ONEH VECTOR
GROUP:  SMOOTH
DESCRIPTION:  ONEH DOES A SINGLE HANNING OF A SEQUENCE OF DATA.
IT IS USED IN CON-UNCTION WITH THE OTHER SMOOTHING FUNCTIONS AS A
FINAL TOUCH-UP TO A SEQUENCE OF SMOOTHED DATA.  THE I-TH RESPONSE
IS REPLACED BY 0.25×Y[I-1] + 0.5×Y[I] + 0.25×Y[I+1].  SEE A3R AND
A3RSR.
```

```
      ONEH X
3  2.5  3.75  5.25  4.5  3  5.5  9  7  4.25  4.25  6
```

```
      TWICEHOW
SYNTAX:  TWICE VECTOR
GROUP:  SMOOTH
SUBPROGRAMS:  ONE3, SPLIT, A3RSR
DESCRIPTION:  TWICE SMOOTHS A SEQUENCE OF DATA, THEN SMOOTHS  THE
RESIDUALS AND ADDS THE SMOOTHED RESIDUALS BACK  TO  THE  SMOOTHED
DATA TO OBTAIN THE FINAL SMOOTH.  THE  SMOOTHING  IS  DONE  USING
A3RSR.
```

```
      TWICE X
3  3  3  3  3  4  4  4  4  4  4  4



      ⍝NOW LET US LOOK AT SOME PLOTS WITH SOME MORE INTERESTING
      ⍝ DATA THAT SHOWS THE EFFECTS OF SMOOTHING.
      ⍝WE WILL USE THE PRESRATING DATA.


      WID←45
      DEP←20
      SCAT PRESRATING
RANGE OF X: 0  120
RANGE OF Y: 0  100
|
|
|o
|o             o o     o2  o
|o          2o2o2o   o 2 2ooo
|     o        oo    o    o 22    o2    o
| o o oo    o2o   3o2o3  ooo oo   o o  o
| o 2  o            o         o o  o22
|      oo          2          o2ooo  o2 o
| o  o  2                       o       o
|  2 o   2 2                     2
|        oo                              32
|         o
|
|
o----oo----o---------------------------2---


      ⍝IT IS HARD TO TELL MUCH FROM THIS.  LETS SEE IF SMOOTHING
      ⍝ HELPS ANY.

      SCAT A3RSR PRESRATING
RANGE OF X: 0  120
RANGE OF Y: 20  90
|
|
o2                     o2o
|o             23        o
|           233o o    22 oo23o
| o              oo  oo   2o 2    o2
|           o     2 o2        o   oo
| 22333o           oo         o     2
|      o           2o               o322
|      oo                     o233o    oo
|       2                               2
|        822                             22
|------------------------------------------
```

```
      ⍝THAT IS A LOT SMOOTHER.  THE PEAKS AND VALLEYS ARE A LOT
      ⍝ CLEARER NOW.  AS A FINAL TOUCHUP, LETS USE TWICE TO
      ⍝ SMOOTH THE RESIDUALS AND ADD BACK TO THE SMOOTHED SEQUENCE,
      ⍝ AND THEN USE ONER AS A FINAL POLISH.


      SCAT ONER TWICE PRESRATING
RANGE OF X: 0  120
RANGE OF Y: 20  90
|
|
o2                      2
|o             23      2 2
|           233o o    2o oo23o
| o              oo  3o   2o 2    o2
|                 2 o         o    o
| 222 3o    o      o2         o   o 2
|   o  o           2          o   o o322
|    o oo                      233     oo
|    2  2  o                            o
|        o                              o
|        o o                             o
|        o2o                             22
|------------------------------------------
```

```
      )GRP TWOWAY
MEDPOLISH       MEDPOLISHHOW    LINE    LINEHOW LSLINE  LSLINEHOW
RESIDS  EPSILON NORMEFFECTS     SHOWRES CODERES RSELECT SHOWRESHOW
CODERESHOW      AND     ANDHOW  CONTINGENCY     CONTINGENCYHOW  ANOVA
ANOVAHOW        OPTION  INPUT   SUMSQ
```

```
      MEDPOLISHHOW
SYNTAX: MEDPOLISH MATRIX      OR      Z←MEDPOLISH MATRIX
PARAMETERS:
          (1) RESIDS- CONTROLS OUTPUT OF RESIDUALS.   IF 1,
          RESIDUALS ARE PRODUCED IN A TWO-WAY TABLE;   IF 2,
          COMPARISON VALUES, (RE∘.×CE)÷TV AND RESIDUALS ARE
          PRODUCED IN A TWO COLUMN MATRIX (DEFAULT=1).
          (2) EPSILON- PROPORTION BY WHICH THE SUM OF THE
          ABSOLUTE VALUES OF THE RESIDUALS MUST BE REDUCED AT
          EACH ITERATION TO CONTINUE POLISHING (DEFAULT=0.01).
          (3) NORMEFFECTS- DETERMINES WHETHER OR NOT NORMALIZED
          EFFECTS ARE OUTPUT. THE DEFAULT OF 0 SUPPRESSES OUTPUT
          OF NORMALIZED VALUES. NORMEFFECTS=1 CAUSES NORMALIZED
          VALUES TO BE PRINTED.
GROUP:- TWOWAY
DESCRIPTION: MEDPOLISH ITERATIVELY SWEEPS OUT MEDIANS FROM THE
ROWS AND COLUMNS OF A TWO-WAY TABLE TO YIELD THE MODEL:
      OBS = MEDIAN + ROW EFFECT + COLUMN EFFECT + RESIDUAL
IT YIELDS RESIDUALS FOR TESTING THE ADEQUACY OF THE MODEL (SEE
SHOWRES AND CODERES). THE FUNCTION CONTINUES POLISHING UNTIL THE
STOPPING RULE CONTROLLED BY EPSILON IS ACTIVATED.   THE OVERALL
MEDIAN, THE ROW- AND COLUMN-EFFECTS, AND THE SUM OF ABSOLUTE
VALUES OF THE RESIDUALS ARE GIVEN.   THE USER CAN SUPPRESS
RESIDUAL PRINTOUT BY ASSIGNING THE FUNCTION TO A VARIABLE, I.E.,
BY WRITING:
                         Z← MEDPOLISH MATRIX
```

```
      RESIDS
1
      EPSILON
0.01
      NORMEFFECTS
0
```

```
      DEATHS
    11.7                 8.7                 15.4                 8.4
    18.1                11.7                 24.3                13.6
    26.9                20.3                 37                  19.3
    41                  30.9                 54.6                35.1
    66                  54.3                 71.1                50


      Z←MEDPOLISH DEATHS
315.4
40.3
38.25
37.575
TYPICAL VALUE: 25.6
ROW EFFECTS: ¯15.3625  ¯10.1  ¯1.4  12.6375  32.875
COLUMN EFFECTS: 2.7  ¯3.9  12.625  ¯3.1375


      ⍝THE RESIDUALS ARE STORED IN Z.  THE FIRST VALUES
      ⍝ PRINTED OUT ARE THE SUMS OF THE ABSOLUTE VALUES
      ⍝ OF THE RESIDUALS. ITERATION CEASES WHEN TWO
      ⍝ CONSECUTIVE VALUES ARE WITHIN EPSILON.


      Z
  ¯1.2375              2.3625              ¯7.4625              1.3
  ¯0.1                 0.1                 ¯3.825               1.2375
   0                   0                    0.175              ¯1.7625
   0.0625             ¯3.4375               3.7375              0
   4.825              ¯0.275                0                  ¯5.3375



      +/+/|Z
37.2375


      SHOWRESHOW
SYNTAX:  SHOWRES MATRIX      OR      SHOWRES MEDPOLISH MATRIX
SUBPROGRAM:  AND
GROUP:  TWOWAY
DESCRIPTION:  SHOWRES AIDS IN  THE  ANALYSIS  OF  RESIDUALS  FROM
MEDIAN POLISHING A TWO-WAY TABLE.  THE USER SHOULD  SET  RESIDS=1
IN MEDPOLISH IF SHOWRES IS TO BE USED.  THE OUTPUT OF SHOWRES  IS
A MATRIX CONSISTING OF THE SYMBOLS O○∘×X DEPENDING ON  THE  SIZES
OF THE RESIDUALS.  LET R REPRESENT THE RESIDUAL, M THE  MIDSPREAD
OF ALL RESIDUALS, L THE LOWER QUARTILE, AND U THE UPPER QUARTILE.
 THE CODES ARE PRINTED AS FOLLOWS:
          O: R<L-1.5M
          ○: L-1.5M≤R≤L-M
          ∘: L-M<R<U+M
          ×: U+M≤R≤U+1.5M
          X: R>U+1.5M
      SHOWRES Z
o o O o
o o O o
o o o o
o o × o
X o o O


      CODERESHOW
SYNTAX: CODERES MATRIX      OR      CODESRES MEDPOLISH MATRIX
SUBPROGRAM:  AND
GROUP:  TWOWAY
DESCRIPTION:  CODERES PRODUCES A DIAGNOSTIC ARRAY  FOR  ANALIZING
THE RESIDUALS FROM MEDIAN POLISHING OF A TWO-WAY TABLE.  THE USER
SHOULD SET RESIDS=1 IN MEDPOLISH  WHEN  CODERES  IS  USED.   THE
OUTPUT MATRIX CONSISTS OF THE SYMBOLS -o+ DEPENDING ON  THE  SIZE
OF THE RESIDUALS.
          -:  VALUE BELOW LOWER QUARTILE
          o:  VALUE BETWEEN QUARTILES
          +:  VALUE LARGER THAN UPPER QUARTILES



      CODERES Z
o + - +
o o - +
o o o -
o - + o
+ o o -


      ⍝ LETS SEE WHAT HAPPENS WHEN RESIDS=2.

      RESIDS←2

      Z←MEDPOLISH DEATHS
315.4
40.3
38.25
37.575
TYPICAL VALUE: 25.6
ROW EFFECTS: ¯15.3625  ¯10.1  ¯1.4  12.6375  32.875
COLUMN EFFECTS: 2.7  ¯3.9  12.625  ¯3.1375
```

```
      SCAT Z
RANGE OF X: ¯10  20
RANGE OF Y: ¯8  6
        |
        |  o
        |    o
        |
        | o
        |oo
----o--322-------------o---
       o|
        o
      o |
    o   |
     o  |
        |
  o     |
        |
```

```
      ⍝ THERE SEEMS TO BE A RELATIONSHIP BETWEEN THE RESIDUALS
      ⍝ AND THE COMPARISON VALUES, (RE∘.×CE)÷TV.
```

```
      A←LINE Z
SLOPE: 0.6216761995 Y-INTERCEPT: ¯0.1348011389
```

```
      ANOVAHOW
SYNTAX:  ANOVA
PARAMETER:
        OPTION- SELECTS THE TYPE OF ANOVA PERFORMED.  OPTION=1
        GIVES A ONE-WAY ANOVA  AND  OPTION=2  GIVES  A  TWO-WAY
        ANOVA (TREATMENTS WITH BLOCKING).  (DEFAULT=1)
GROUP:  TWOWAY
SUBPROGRAMS:  INPUT, SUMSQ, FMT
DESCRIPTION:  ANOVA DOES A  ONE-WAY  OR  A  TWO-WAY  ANALYSIS  OF
VARIANCE DEPENDING ON THE VALUE OF THE  OPTION  PARAMETER.  ANOVA
WILL INTERACT WITH THE USER TO OBTAIN  THE  REQUIRED  INFORMATION
AND DATA.  WHEN ENTERING DATA, SEPARATE THE DATA POINTS  WITH  AT
LEAST ONE BLANK AND USE NO OTHER DELIMITERS.  OUTPUT CONSISTS  OF
AN ANOVA TABLE, ESTIMATES OF THE OVERALL MEAN, AND  ESTIMATES  OF
THE TREATMENT (AND,IF OPTION=2, BLOCK) EFFECTS.
```

```
      OPTION
1


      ANOVA
ENTER NUMBER OF TREATMENTS.
⎕:
      4
ENTER VECTOR OF NUMBER OF OBS. FOR TREATMENTS 1 TO 4
⎕:
      3 3 3 3
ENTER 3 OBSERVATIONS FOR TREATMENT 1
⎕:
      45 46 51
ENTER 3 OBSERVATIONS FOR TREATMENT 2
⎕:
      42 44 50
ENTER 3 OBSERVATIONS FOR TREATMENT 3
⎕:
      36 41 48
ENTER 3 OBSERVATIONS FOR TREATMENT 4
⎕:
      49 47 54
                    ANOVA TABLE
  SOURCE        DF         SS          MS        F
  TREATMENT      3       110.92      36.97     1.92
  ERROR          8       154.00      19.25
  TOTAL         11       264.92
R-SQUARE = 0.419
OVERALL MEAN =      46.08
TREATMENT EFFECTS   1.25 ¯0.75 ¯4.42  3.92
```

```
      ⍝ LET US TAKE THE SAME DATA AND DO A TWO WAY ANOVA.


      OPTION←2


      ANOVA
ENTER NUMBER OF TREATMENTS.
⎕:
      4
ENTER VECTOR OF NUMBER OF OBS. FOR TREATMENTS 1 TO 4
⎕:
      3 3 3 3
ENTER 3 OBSERVATIONS FOR TREATMENT 1
⎕:
      45 46 51
ENTER 3 OBSERVATIONS FOR TREATMENT 2
⎕:
      42 44 50
ENTER 3 OBSERVATIONS FOR TREATMENT 3
⎕:
      36 41 48
ENTER 3 OBSERVATIONS FOR TREATMENT 4
⎕:
      40 47 54
                     ANOVA TABLE
  SOURCE       DF         SS          MS        F
  TREATMENT     3        60.67       20.22     5.56
  BLOCKS        2       204.17      102.08    28.05
  ERROR         6        21.83        3.64
  TOTAL        11       286.67
R▪SQUARE = 0.924
OVERALL MEAN =      45.33
TREATMENT EFFECTS   2.00  0.00 ¯3.67  1.67
BLOCK EFFECTS   ¯4.58 ¯0.83  5.42
```

```
      CONTINGENCYHOW
SYNTAX:  CONTINGENCY MATRIX
GROUP:  TWOWAY
DESCRIPTION:  CONTINGENCY TAKES A TWO-WAY TABLE  AND  PERFORMS  A
TEST OF  INDEPENDENCE  OF  ROWS  AND  COLUMNS.    THE  CHI-SQUARE
STATISTIC AND ITS DEGREES OF FREEDOM ARE OUTPUT.



      CONTINGENCY DEATHS
CHI-SQUARE VALUE= 2.920832627  DF= 12


      ⍝ COMPARE THE ABOVE VALUE WITH THOSE IN CHI-SQUARE
      ⍝ TABLES FOR 12 DF TO DETERMINE IF THE HYPOTHESIS
      ⍝ STATING THAT THE ROWS AND COLUMNS ARE INDEPENDENT
      ⍝ CAN BE REJECTED AT THE SELECTED SIGNIFICANCE LEVEL.
      )GRP STATS
CORRELATION     CR        FMT      MSTATS  PARTIAL STATISTICS      CH
CORRELATIONHOW  MSTATSHOW          PARTIALHOW      STATISTICSHOW



      STATISTICSHOW
SYNTAX:  STATISTICS VECTOR
GROUP:  STATS
SUBPROGRAM:  FMT
DESCRIPTION:  STATISTICS DETERMINES THE MEAN, VARIANCE,  STANDARD
DEVIATION, COEFFICIENT OF VARIATION, LOWER AND  UPPER  QUARTILES,
MEDIAN,  TRIMEAN,  MIDMEAN,  MIDRANGE,   RANGE,   MEAN   ABSOLUTE
DEVIATION, INTERQUARTILE RANGE, SKEWNESS, AND  KURTOSIS  FOR  THE
DATA IN VECTOR.



      STATISTICS VOLCANO
MEAN: 70.24657534
VARIANCE: 1850.562775
STD. DEV.: 43.01816796
COEFF. OF VARIATION: 0.6123881165
LOWER QUARTILE: 37
UPPER QUARTILE: 96
MEDIAN: 65
TRIMEAN: 65.75
MIDMEAN: 64.47747748
RANGE: 197
MIDRANGE: 100.5
MEAN ABSOLUTE DEVIATION: 33.68493151
INTERQUARTILE RANGE: 59
COEFF. OF SKEWNESS: 0.8325767059
COEFF. OF KURTOSIS: 0.4281831164



      CORRELATIONHOW
SYNTAX:  R←CORRELATION W
GROUP:  STATS
SUBPROGRAM:  FMT
DESCRIPTION:  CORRELATION DETERMINES THE SIMPLE  PEARSON  PRODUCT
MOMENT CORRELATIONS BETWEEN EACH PAIR OF VARIABLES REPRESENTED BY
THE C COLUMNS OF W.  THE OUTPUT IS A C BY C CORRELATION MATRIX.
```

```
      CORRELATION GRADES1
              1.00     2.00     3.00     4.00     5.00
     1.00     1.00     0.34     0.50     0.25     0.64
     2.00     0.34     1.00    ¯0.07     0.54     0.68
     3.00     0.50    ¯0.07     1.00     0.52     0.64
     4.00     0.25     0.54     0.52     1.00     0.87
     5.00     0.64     0.68     0.64     0.87     1.00


      ⍝ IN THE CORRELATION OUTPUT, THE TOP ROW AND THE FIRST
      ⍝ COLUMN ARE LABELS FOR THE CORRELATIONS.  FOR EXAMPLE,
      ⍝ THE CORRELATION BETWEEN THE SECOND AND FOURTH COLUMNS
      ⍝ OF GRADES1 IS 0.54.


      ρGRADES1
15  5


      MSTATSHOW
SYNTAX:  MSTATS W
GROUP:  STATS
SUBPROGRAM:  EMT
DESCRIPTION:  MSTATS  DETERMINES  CORRELATIONS,  MEANS,  STANDARD
DEVIATIONS, LOWER QUARTILES, MEDIANS, AND UPPER QUARTILES FOR THE
COLUMNS OF THE ARGUMENT MATRIX W.  THE CORRELATIONS ARE DISPLAYED
IN AN N BY N MATRIX, WHERE N IS THE NUMBER OF COLUMNS OF W.


      THE OUTPUT FROM MSTATS IS MUCH LIKE THAT OF CORRELATION.


      MSTATS GRADES1
              1.00     2.00     3.00     4.00     5.00
     1.00     1.00     0.34     0.50     0.25     0.64
     2.00     0.34     1.00    ¯0.07     0.54     0.68
     3.00     0.50    ¯0.07     1.00     0.52     0.64
     4.00     0.25     0.54     0.52     1.00     0.87
     5.00     0.64     0.68     0.64     0.87     1.00
MEANS         0.86     0.81     0.88     0.81     0.84
STD.DEV       0.09     0.11     0.10     0.10     0.07
L. QRTLS      0.82     0.69     0.82     0.74     0.78
MEDIANS       0.85     0.83     0.88     0.79     0.83
U. QRTLS      0.94     0.92     0.98     0.91     0.90
```

```
      PARTIALHOW
SYNTAX:  PARTIAL W
GROUP:  STATS
SUBPROGRAMS:  CORRELATION, FMT
DESCRIPTION:  PARTIAL  DETERMINES  PARTIAL  CORRELATIONS  OF  ANY
SPECIFIED ORDER FOR THE COLUMNS OF THE MATRIX W. THE USER WILL BE
ASKED FOR THE COLUMNS TO BE PARTIALLED OUT.  THE USER'S RESPONSES
MUST BE INTEGERS BETWEEN 1 AND  C,  WHERE  C  IS  THE  NUMBER  OF
COLUMNS OF W.



      PARTIAL GRADES1
ENTER COLUMNS OF MATRIX TO BE PARTIALLED OUT.
⎕:
      1
            1.00     2.00     3.00     4.00
    1.00    1.00    ¯0.29     0.50     0.64
    2.00   ¯0.29     1.00     0.47     0.49
    3.00    0.50     0.47     1.00     0.95
    4.00    0.64     0.49     0.95     1.00


      ⍝ BE CAREFUL WITH INTERPRETING THE LABELS IN THE OUTPUT
      ⍝ OF PARTIAL.  ABOVE, LABEL 1 DOES NOT MEAN COLUMN ONE,
      ⍝ BUT THE FIRST COLUMN REMAINING AFTER THE SELECTED VARIABLES
      ⍝ HAVE BEEN PARTIALED OUT.  SIMILARLY, 2 REFERS TO THE
      ⍝ SECOND REMAINING COLUMN.


      PARTIAL GRADES1
ENTER COLUMNS OF MATRIX TO BE PARTIALLED OUT.
⎕:
      2 3
            1.00     2.00     3.00
    1.00    1.00    ¯0.45     0.23
    2.00   ¯0.45     1.00     0.77
    3.00    0.23     0.77     1.00


      ⍝ THE ABOVE EXAMPLE SHOWS THAT MORE THAN ONE VARIABLE
      ⍝ CAN BE PARTIALED OUT.  LABEL 2 ABOVE REFERS TO THE
      ⍝ SECOND COLUMN REMAINING AFTER THE SELECTED VARIABLES
      ⍝ HAVE BEEN PARTIALED OUT. IN THIS EXAMPLE 2 REFERS TO
      ⍝ COLUMN 4.
      )GRP GFIT
KS        KSHOW   CHISQUARE        CHISQUAREHOW



      CHISQUAREHOW
SYNTAX:  T CHISQUARE X
GROUP:  GFIT
DESCRIPTION:     CHISQUARE   COMPARES   A   THEORETICAL   DISCRETE
PROBABILITY MASS FUNCTION T HAVING  N  POSSIBLE  VALUES  WITH  AN
EMPIRICAL FREQUENCY FUNCTION X OVER THE SAME N VALUES TO TEST HOW
WELL THE  PROBABILITIES  T  FIT  THE  DATA  X.   THE  CHI-SQUARE
GOODNESS-OF-FIT STATISTIC IS  PRINTED  OUT  WITH  THE  NUMBER  OF
DEGREES OF FREEDOM.



      ⍝ THE THEORETICAL PROBABILITY MASS FUNCTION T AND THE
      ⍝ EMPIRICAL FREQUENCY FUNCTION X MUST BE OF THE SAME
      ⍝ SIZE; I.E., ⍴T=⍴X.  THE ACTUAL OBSERVED VALUES ARE
      ⍝ IMPLICIT IN THE POSITION OF THE VECTORS.


      T←.1 .2 .3 .2 .1
      X← 5 20 38 32 12


      ⍝ THE VALUES IN T REPRESENT PROBABILITIES.  THE VALUES IN
      ⍝ X REPRESENT OBSERVED FREQUENCIES.  THE ACTUAL OBSERVATIONS
      ⍝ ARE NOT STATED EXPLICITLY, BUT IT IS UNDERSTOOD THAT
      ⍝ THE POSITIONS OF X AND T REFER TO THE SAME VALUES.  FOR
      ⍝ EXAMPLE, IN THE CASE ABOVE, THE FIRST POSITION MAY REFER
      ⍝ TO THE VALUE ¯1, THE SECOND 0, ETC.


      T CHISQUARE X
CHI-SQUARE VALUE = 9.620872274  DF = 4


      ⍝ TO DETERMINE IF ONE SHOULD REJECT THE HYPOTHESIS THAT
      ⍝ THE DATA WERE DRAWN FROM A POPULATION WITH PROBABILITY
      ⍝ MASS FUNCTION T, COMPARE THE VALUE ABOVE WITH THOSE
      ⍝ IN CHI-SQUARE TABLES WITH 4 DF.
      KSHOW
SYNTAX:  F KS G
GROUP:  GFIT
DESCRIPTION:  KS DOES A KOLMOGOROV-SMIRNOV GOODNESS OF FIT TEST
OF THE EQUALITY OF TWO DISCRETE EMPIRICAL PROBABILITY
DISTRIBUTIONS. THE ARGUMENTS F AND G ARE EACH VECTORS OF
OBSERVATIONS. THEY NEED NOT BE SORTED, NOR MUST THEY BE THE SAME
SIZE.  OUTPUT OF KS ARE THE VALUES:
                        MAX F(X)-G(X) AND MIN F(X)-G(X)



      F←3 2 5 9 10 16 3 5 7 19 20 12 6 3 8 8 9 7 7 7 7 2 10 7

      G←4 2 10 20 18 3 6 7 4 2 1 10 8 6 3 31 7

      F KS G
MAX F(X)-G(X) =0.1274509804
MIN F(X)-G(X) =¯0.3137254902


      ⍝ TO DETERMINE IF THE TWO SAMPLES OF DATA WERE TAKEN FROM
      ⍝ THE SAME POPULATION (OR POPULATIONS WITH THE SAME CDF'S)
      ⍝ COMPARE THE MAX AND MIN VALUES WITH THE DELTA STATISTICS
      ⍝ IN TABLES FOR THE TWO SAMPLE KS TEST.
```

APPENDIX A

ANDHOW

SYNTAX: X AND Y

GROUPS: RELATIONS, TWOWAY, COMPARISONS

DESCRIPTION: THE FUNCTION 'AND' IS USED TO CREATE A NEW DATA ARRAY CONSISTING OF X AUGMENTED BY Y AS ADDITIONAL COLUMNS. X AND Y CAN BE SCALARS, VECTORS, OR MATRICES BUT CANNOT BOTH BE SCALARS. IF AN ARGUMENT IS A SCALAR, A COLUMN IS GENERATED EACH ELEMENT OF WHICH IS THE SCALAR. IF THE ARGUMENTS ARE VECTORS OR MATRICES, THEY MUST BE CONFORMABLE.

ANOVAHOW

SYNTAX: ANOVA

PARAMETER:

OPTION- SELECTS THE TYPE OF ANOVA PERFORMED. OPTION=1 GIVES A ONE-WAY ANOVA AND OPTION=2 GIVES A TWO-WAY ANOVA (TREATMENTS WITH BLOCKING). (DEFAULT=1)

GROUP: TWOWAY

SUBPROGRAMS: INPUT, SUMSQ, FMT

DESCRIPTION: ANOVA DOES A ONE-WAY OR A TWO-WAY ANALYSIS OF VARIANCE DEPENDING ON THE VALUE OF THE OPTION PARAMETER. ANOVA WILL INTERACT WITH THE USER TO OBTAIN THE REQUIRED INFORMATION AND DATA. WHEN ENTERING DATA, SEPARATE THE DATA POINTS WITH AT LEAST ONE BLANK AND USE NO OTHER DELIMITERS. OUTPUT CONSISTS OF AN ANOVA TABLE, ESTIMATES OF THE OVERALL MEAN, AND ESTIMATES OF THE TREATMENT (AND,IF OPTION=2, BLOCK) EFFECTS.

A3RHOW

SYNTAX: A3R VECTOR

GROUP: SMOOTH

SUBPROGRAM: ONE3

DESCRIPTION: A3R DOES REPEATED SMOOTHINGS OF RUNNING MEDIANS OF 3 UNTIL THERE ARE NO CHANGES IN THE SMOOTHED SEQUENCE FROM ONE ITERATION TO THE NEXT. SEE ONE3HOW.

A3RSRHOW

SYNTAX: A3RSR VECTOR

GROUP: SMOOTH

SUBPROGRAMS: A3R, ONE3, SPLIT

DESCRIPTION: A3RSR DOES REPEATED SMOOTHINGS BY RUNNING MEDIANS OF 3 FOLLOWED BY SPLITTING MESAS AND REPEATING UNTIL CONVERGENCE. SEE A3R AND SPLIT.

BOXPLOTHOW

SYNTAX: BOXPLOT VECTOR

PARAMETER:

LENGTH- CONTROLS THE HORIZONTAL SIZE OF THE DISPLAY (DEFAULT=50 CHARACTERS).

GROUP: DISPLAY

SUBPROGRAM: FILL

DESCRIPTION: BOXPLOT GENERATES A BOX PLOT DISPLAY FOR A VECTOR OF DATA. A RECTANGULAR BOX WITH ENDS CORRESPONDING TO LOWER AND UPPER QUARTILES IS PRESENTED WITH THE MEDIAN MARKED WITH AN ASTERISK. WHISKERS ARE DRAWN ON EACH SIDE OF THE BOX WITH CROSSES MARKING THE LOWEST AND HIGHEST DATA VALUES WITHIN AN INTERQUARTILE DISTANCE OF THE QUARTILES. DATA VALUES OUTSIDE THE CROSSES (OUTLIERS) ARE MARKED WITH CIRCLES AND THOSE MORE THAN 1.5 INTERQUARTILE DISTANCES GET HEAVY CIRCLES.

CHISQUAREHOW

SYNTAX: T CHISQUARE X

GROUP: GFIT

DESCRIPTION: CHISQUARE COMPARES A THEORETICAL DISCRETE PROBABILITY MASS FUNCTION T HAVING N POSSIBLE VALUES WITH AN EMPIRICAL FREQUENCY FUNCTION X OVER THE SAME N VALUES TO TEST HOW WELL THE PROBABILITIES T FIT THE DATA X. THE CHI-SQUARE GOODNESS-OF-FIT STATISTIC IS PRINTED OUT WITH THE NUMBER OF DEGREES OF FREEDOM.

CODERESHOW

SYNTAX: CODERES MATRIX OR CODESRES MEDPOLISH MATRIX

SUBPROGRAM: AND

GROUP: TWOWAY

DESCRIPTION: CODERES PRODUCES A DIAGNOSTIC ARRAY FOR ANALYZING THE RESIDUALS FROM MEDIAN POLISHING OF A TWO-WAY TABLE. THE USER SHOULD SET RESIDS=1 IN MEDPOLISH WHEN CODERES IS USED. THE OUTPUT MATRIX CONSISTS OF THE SYMBOLS -∘+ DEPENDING ON THE SIZE OF THE RESIDUALS.

-: VALUE BELOW LOWER QUARTILE

∘: VALUE BETWEEN QUARTILES

+: VALUE LARGER THAN UPPER QUARTILES

COMPAREHOW

SYNTAX: COMPARE MATRIX

PARAMETERS:

(1) DEPTH- VERTICAL HEIGHT OF DISPLAY (DEFAULT=20 LINES).

(2) MISS-_ NUMBER USED TO INDICATE MISSING VALUES (DEFAULT =¯99999)

(3) NGAP- NUMBER OF HORIZONTAL SPACES BETWEEN THE BOXPLOT DISPLAYS (DEFAULT=3).

GROUP: COMPARISONS

SUBPROGRAM: FILL

DESCRIPTION: COMPARE OPERATES ON AN N BY K MATRIX TO PRODUCE K VERTICAL BOX PLOTS PLACED NEXT TO EACH OTHER TO ALLOW VISUAL COMPARISON OF THE CENTERS, SPREADS, AND OUTLIERS OF THE BATCHES (COLUMNS) OF THE MATRIX. THE USER MUST FILL UP THE MATRIX SO THAT THERE ARE N OBSERVATIONS FOR EACH BATCH. THE PARAMETER, MISS, SHOULD BE USED TO FILL IN MISSING VALUES. THE USER SHOULD ASSURE THAT MISS IS DIFFERENT FROM ALL VALID ENTRIES IN THE DATA ARRAY.

CONDENSEHOW

SYNTAX: CONDENSE MATRIX OR R←CONDENSE MATRIX

PARAMETERS:

(1) NUM- CONTROLS WHAT STATISTICS ARE INCLUDED IN THE SUMMARY. NUM∊[1,2,5,7] (DEFAULT=2).
NUM=1 GIVES MEDIANS OF EACH COLUMN OF THE MATRIX
NUM=2 GIVES MEDIANS AND INTERQUARTILE RANGES
NUM=5 GIVES MIN,QUARTILES,MAX, AND SIZE
NUM=7 GIVES MIN,EIGHTHS,MAX AND SIZE

(2) MISS- NUMBER USED TO CODE MISSING VALUES (DEFAULT=¯99999).

GROUP: COMPARISONS

SUBPROGRAMS: UTCOND, FMT

DESCRIPTION: CONDENSE GENERATES SUMMARY STATISTICS FOR EACH GROUP OF DATA REPRESENTED BY THE COLUMNS OF THE ARGUMENT MATRIX. SINCE THE ARGUMENT IS A MATRIX, THE USER MUST FILL UP THE MISSING VALUES IN THE MATRIX WHENEVER THE GROUPS (COLUMNS) HAVE DIFFERENT NUMBERS OF OBSERVATIONS. THE PARAMETER, MISS, SHOULD BE USED TO FILL THE MATRIX SINCE THE FUNCTION WILL RECOGNIZE THOSE VALUES AS MISSING DATA AND WILL IGNORE THEM IN ALL CALCULATIONS. THE RESULT FROM CONDENSE CAN BE USED AS THE ARGUMENT OF OTHER FUNCTIONS SUCH AS SCAT OR LINE IF AND ONLY IF NUM=2.

CONTINGENCYHOW

SYNTAX: CONTINGENCY MATRIX

GROUP: TWOWAY

DESCRIPTION: CONTINGENCY TAKES A TWO-WAY TABLE AND PERFORMS A TEST OF INDEPENDENCE OF ROWS AND COLUMNS. THE CHI-SQUARE STATISTIC AND ITS DEGREES OF FREEDOM ARE OUTPUT.

KSHOW

SYNTAX: F KS G

GROUP: GFIT

DESCRIPTION: KS DOES A KOLMOGOROV-SMIRNOV GOODNESS OF FIT TEST OF THE EQUALITY OF TWO DISCRETE EMPIRICAL PROBABILITY DISTRIBUTIONS. THE ARGUMENTS F AND G ARE EACH VECTORS OF OBSERVATIONS. THEY NEED NOT BE SORTED, NOR MUST THEY BE THE SAME SIZE. OUTPUT OF KS ARE THE VALUES:

MAX F(X)-G(X) AND MIN F(X)-G(X)

LINEHOW

SYNTAX: LINE ARRAY OR Z←LINE ARRAY

PARAMETER:

RSELECT- SELECTS THE OUTPUT MATRIX OF RESIDUALS.
RSELECT=1 GIVES ABSCISSA VS. RESIDUALS (DEFAULT=1).
RSELECT≠1 GIVES FITTED VALUES VS. RESIDUALS

GROUP: RELATIONS

DESCRIPTION: LINE FITS A STRAIGHT LINE TO A SET OF (X,Y) POINTS BY DIVIDING THE POINTS INTO 3 REGIONS AND USING THE MEDIANS OF THE X AND Y VALUES IN THE OUTER REGIONS TO DETERMINE THE SLOPE. THE INTERCEPT IS THE MEDIAN OF THE DIFFERENCES Y-SLOPE×X. LINE ALSO COMPUTES THE RESIDUALS AND GIVES AN N BY 2 MATRIX CONTAINING EITHER THE X-VALUES VS. RESIDUALS OR THE FITTED VALUES VS. RESIDUALS DEPENDING ON THE PARAMETER, RSELECT. IF THE USER DOES NOT WANT RESIDUALS TYPED OUT, HE SHOULD USE THE SYNTAX:

Z←LINE ARRAY

THE ARGUMENT ARRAY CAN BE EITHER A VECTOR OR A 2-COLUMN MATRIX. IF THE ARGUMENT IS A VECTOR OF SIZE N, THE X-VARIABLE IS CONSTRUCTED TO BE THE FIRST N POSITIVE INTEGERS. IF THE ARGUMENT IS A 2-COLUMN MATRIX, THE FIRST COLUMN IS TAKEN TO BE THE SET OF X-VALUES AND THE SECOND COLUMN THE SET OF Y-VALUES. LINE CAN BE USED IN CONJUNCTION WITH THE FUNCTION SCAT TO PRODUCE THE SLOPE, THE INTERCEPT, AND A PLOT OF THE RESIDUALS. TO DO THIS, ENTER:

SCAT LINE ARRAY

LSLINEHOW

SYNTAX: LSLINE ARRAY OR Z←LSLINE ARRAY

GROUP: RELATIONS

DESCRIPTION: LSLINE DETERMINES THE LEAST SQUARES SOLUTION, Y=YI+SLOPE×X. THE ARGUMENT ARRAY CAN BE A VECTOR OR A 2-COLUMN MATRIX. IF THE ARGUMENT IS A VECTOR, THE X-VALUES ARE TAKEN TO BE THE INTEGERS 1 TO N WHERE N=ρARRAY. IF THE ARGUMENT IS A 2-COLUMN MATRIX, COLUMN 1 CONSISTS OF THE X-VALUES AND COLUMN 2 THE Y-VALUES. RESIDUALS ARE DETERMINED AND STORED IN A MATRIX WHOSE FIRST COLUMN IS THE SET OF X-VALUES AND WHOSE SECOND COLUMN IS THE SET OF RESIDUALS. IF THE USER WANTS TO SUPPRESS PRINTOUT OF THE RESIDUALS, HE MUST ASSIGN THE RESULTS OF LSLINE TO A VARIABLE; I.E., TYPE Z←LSLINE ARRAY.

MEDPOLISHHOW

SYNTAX: MEDPOLISH MATRIX OR Z←MEDPOLISH MATRIX

PARAMETERS:

(1) RESIDS- CONTROLS OUTPUT OF RESIDUALS. IF 1, RESIDUALS ARE PRODUCED IN A TWO-WAY TABLE; IF 2, COMPARISON VALUES, (RE∘.×CE)÷TV AND RESIDUALS ARE PRODUCED IN A TWO COLUMN MATRIX (DEFAULT=1).

(2) EPSILON- PROPORTION BY WHICH THE SUM OF THE ABSOLUTE VALUES OF THE RESIDUALS MUST BE REDUCED AT EACH ITERATION TO CONTINUE POLISHING (DEFAULT=0.01).

(3) NORMEFFECTS- DETERMINES WHETHER OR NOT NORMALIZED EFFECTS ARE OUTPUT. THE DEFAULT OF 0 SUPPRESSES OUTPUT OF NORMALIZED VALUES. NORMEFFECTS=1 CAUSES NORMALIZED VALUES TO BE PRINTED.

GROUP: TWOWAY

DESCRIPTION: MEDPOLISH ITERATIVELY SWEEPS OUT MEDIANS FROM THE ROWS AND COLUMNS OF A TWO-WAY TABLE TO YIELD THE MODEL:

OBS = MEDIAN + ROW EFFECT + COLUMN EFFECT + RESIDUAL

IT YIELDS RESIDUALS FOR TESTING THE ADEQUACY OF THE MODEL (SEE SHOWRES AND CODERES). THE FUNCTION CONTINUES POLISHING UNTIL THE STOPPING RULE CONTROLLED BY EPSILON IS ACTIVATED. THE OVERALL MEDIAN, THE ROW- AND COLUMN-EFFECTS, AND THE SUM OF ABSOLUTE VALUES OF THE RESIDUALS ARE GIVEN. THE USER CAN SUPPRESS RESIDUAL PRINTOUT BY ASSIGNING THE FUNCTION TO A VARIABLE, I.E., BY WRITING:

Z← MEDPOLISH MATRIX

```
      CORRELATIONHOW
SYNTAX:  R←CORRELATION W
GROUP:  STATS
SUBPROGRAM:  FMT
DESCRIPTION:  CORRELATION DETERMINES THE SIMPLE  PEARSON  PRODUCT
MOMENT CORRELATIONS BETWEEN EACH PAIR OF VARIABLES REPRESENTED BY
THE C COLUMNS OF W.  THE OUTPUT IS A C BY C CORRELATION MATRIX.
```

```
      MSTATSHOW
SYNTAX:  MSTATS W
GROUP:  STATS
SUBPROGRAM:  FMT
DESCRIPTION:  MSTATS  DETERMINES  CORRELATIONS,  MEANS,  STANDARD
DEVIATIONS, LOWER QUARTILES, MEDIANS, AND UPPER QUARTILES FOR THE
COLUMNS OF THE ARGUMENT MATRIX W.  THE CORRELATIONS ARE DISPLAYED
IN AN N BY N MATRIX, WHERE N IS THE NUMBER OF COLUMNS OF W.
```

```
      PARTIALHOW
SYNTAX:  PARTIAL W
GROUP:  STATS
SUBPROGRAMS:  CORRELATION, FMT
DESCRIPTION:  PARTIAL  DETERMINES  PARTIAL  CORRELATIONS  OF  ANY
SPECIFIED ORDER FOR THE COLUMNS OF THE MATRIX W. THE USER WILL BE
ASKED FOR THE COLUMNS TO BE PARTIALLED OUT.  THE USER'S RESPONSES
MUST BE INTEGERS BETWEEN 1 AND  C,  WHERE  C  IS  THE  NUMBER  OF
COLUMNS OF W.
```

NUMSUMHOW

SYNTAX: NUMSUM VECTOR OR NUMSUM ARRAY

PARAMETER:

MISS- NUMBER USED TO INDICATE MISSING VALUE IN THE DATA ARRAY (DEFAULT=¯99999).

GROUP: COMPARISONS

SUBPROGRAM: FMT

DESCRIPTION: NUMSUM OPERATES ON EITHER A VECTOR OR AN ARRAY BUT, IN ALL CASES, THE DATA ARE TREATED AS A SINGLE BATCH. NUMSUM PRODUCES A NUMERICAL SUMMARY WHICH GIVES THE SAMPLE SIZE (AFTER DELETION OF MISSING VALUES), THE EIGHTHS, THE EXTREMES, THE SPREADS, AND THE MIDPOINTS IN TABULAR FORM. THIS SUMMARY IS USEFUL FOR TESTING THE SYMMETRY OF A DATA SET, AND TO EVALUATE THE EFFECTIVENESS OF DATA TRANSFORMATIONS IN PRODUCING SYMMETRY.

ONEHHOW

SYNTAX: ONEH VECTOR

GROUP: SMOOTH

DESCRIPTION: ONEH DOES A SINGLE HANNING OF A SEQUENCE OF DATA. IT IS USED IN CONJUNCTION WITH THE OTHER SMOOTHING FUNCTIONS AS A FINAL TOUCH-UP TO A SEQUENCE OF SMOOTHED DATA. THE I-TH RESPONSE IS REPLACED BY 0.25×Y[I-1] + 0.5×Y[I] + 0.25×Y[I+1]. SEE A3R AND A3RSR.

ONE3HOW

SYNTAX: ONE3 VECTOR

GROUP: SMOOTH

DESCRIPTION: ONE3 SMOOTHS A VECTOR OF DATA USING ONE PASS OF RUNNING MEDIANS OF 3 WITH TUKEY'S END-POINT RULE. WHEN SMOOTHING (X,Y) PAIRS, THE USER SHOULD USE AS THE ARGUMENT VECTOR THE Y VALUES ORDERED ACCORDING TO THE MAGNITUDE OF THE X VALUES:

```
VECTOR←Y[⍋X]
```

IT IS ASSUMED THAT THE X VALUES ARE EQUISPACED. REPEATED SMOOTHING BY MEDIANS OF 3 CAN BE ACCOMPLISHED WITH A3R. OUTPUT CONSISTS OF THE SMOOTHED SEQUENCE. A PLOT OF THE SMOOTHED SEQUENCE IS GIVEN BY TYPING:

```
SCAT ONE3 VECTOR
```

REGRESSHOW

SYNTAX: Z←Y REGRESS X

PARAMETER:

∆INTERCEPT- DETERMINES WHETHER OR NOT AN INTERCEPT TERM IS TO BE INCLUDED. ∆INTERCEPT=1 GIVES AN INTERCEPT TERM, AND ∆INTERCEPT=0 GIVES NO INTERCEPT. (DEFAULT IS 1.)

GROUP: RELATIONS

SUBPROGRAMS: FMT AND SCAT

DESCRIPTION: REGRESS DOES A MULTIPLE REGRESSION ANALYSIS RELATING THE DEPENDENT VARIABLE Y TO A SET OF CARRIERS X. THE LEFT ARGUMENT Y IS A VECTOR OF SIZE N. THE RIGHT ARGUMENT X IS AN N BY K MATRIX CONSISTING OF N OBSERVATIONS ON EACH OF K VARIABLES OR A VECTOR OF SIZE N IF K=1. OUTPUT CONSISTS OF AN ANOVA TABLE, R-SQUARE, STD. ERROR, REGRESSION COEFFICIENTS (THE FIRST COEFFICIENT IS THE CONSTANT TERM IF ∆INTERCEPT=1.), T-STATISTICS, VARIANCE-COVARIANCE MATRIX, DURBIN-WATSON STATISTIC, AND A VECTOR OF PREDICTED Y VALUES AND RESIDUALS. THERE IS AN OPTION THAT ALLOWS THE USER TO INPUT A VECTOR OF X VALUES AND USE THE REGRESSION EQUATION TO FORECAST Y VALUES. THE USER CAN ALSO OBTAIN A SCATTER PLOT OF THE RESIDUALS. WHEN EXECUTION TERMINATES, THE PREDICTED Y VALUES AND THE RESIDUALS RESIDE IN THE N BY 2 MATRIX Z.

STATISTICSHOW

SYNTAX: STATISTICS VECTOR

GROUP: STATS

SUBPROGRAM: FMT

DESCRIPTION: STATISTICS DETERMINES THE MEAN, VARIANCE, STANDARD DEVIATION, COEFFICIENT OF VARIATION, LOWER AND UPPER QUARTILES, MEDIAN, TRIMEAN, MIDMEAN, MIDRANGE, RANGE, MEAN ABSOLUTE DEVIATION, INTERQUARTILE RANGE, SKEWNESS, AND KURTOSIS FOR THE DATA IN VECTOR.

SCATHOW

SYNTAX: SCAT ARRAY

PARAMETERS:

(1) WID- CONTROLS THE HORIZONTAL SIZE OF THE DISPLAY (DEFAULT=30 CHARACTERS).

(2) DEP- CONTROLS THE VERTICAL SIZE OF THE DISPLAY (DEFAULT=15 LINES).

(3) NDIVX, NDIVY- NUMBER OF UNITS ON X- AND Y-AXES, RESPECTIVELY (DEFAULT=4,4).

GROUP: RELATIONS, SMOOTH, COMPARISONS

DESCRIPTION: SCAT PRODUCES A SCATTER PLOT OF THE DATA CONTAINED IN ARRAY. THE ARGUMENT ARRAY CAN BE A VECTOR OR A MATRIX WITH AS MANY AS 9 COLUMNS. IF A VECTOR OF SIZE N, THOSE VALUES ARE PLOTTED VS. THE INTEGERS 1 TO N; IF A MATRIX, THE SECOND, THIRD, ETC. COLUMNS ARE PLOTTED VS. COLUMN 1 ON THE SAME AXES. DIVISIONS ON THE AXES OF THE PLOT ARE NOT EXPLICITLY PRINTED, EXCEPT AT THE EXTREMES OF THE PLOT. THE USER CAN CONTROL THE RESOLUTION OF THE PLOT BY MODIFYING THE PARAMETERS WID, DEP, NDIVX AND NDIVY. PRINTING TIME INCREASES DRAMATICALLY WITH RESOLUTION; THEREFORE, OTHER PLOT PROGRAMS SHOULD BE USED IF HIGH RESOLUTION IS DESIRED. FOR A SINGLE GROUP OF DATA, THE NUMBER N ($2 \le N \le 9$) WILL BE PRINTED IF N POINTS LIE CLOSE TOGETHER ON THE DISPLAY. FOR MULTIPLE PLOTS ON THE SAME DISPLAY, THE LETTER A REPRESENTS GROUP 1, B REPRESENTS GROUP 2, ETC. FOR 2 POINTS CLOSE TOGETHER THE LETTER WILL BE PRINTED WITH AN UNDERSCORE. THE DISPLAY CANNOT HANDLE 3 OR MORE POINTS CLOSE TOGETHER IF THERE ARE MULTIPLE PLOTS.

SHOWRESHOW

SYNTAX: SHOWRES MATRIX OR SHOWRES MEDPOLISH MATRIX

SUBPROGRAM: AND

GROUP: TWOWAY

DESCRIPTION: SHOWRES AIDS IN THE ANALYSIS OF RESIDUALS FROM MEDIAN POLISHING A TWO-WAY TABLE. THE USER SHOULD SET RESIDS=1 IN MEDPOLISH IF SHOWRES IS TO BE USED. THE OUTPUT OF SHOWRES IS A MATRIX CONSISTING OF THE SYMBOLS O○∘×X DEPENDING ON THE SIZES OF THE RESIDUALS. LET R REPRESENT THE RESIDUAL, M THE MIDSPREAD OF ALL RESIDUALS, L THE LOWER QUARTILE, AND U THE UPPER QUARTILE. THE CODES ARE PRINTED AS FOLLOWS:

O: $R<L-1.5M$
○: $L-1.5M\leq R\leq L-M$
∘: $L-M<R<U+M$
×: $U+M\leq R\leq U+1.5M$
X: $R>U+1.5M$

SPLITHOW

SYNTAX: SPLIT A3R VECTOR

GROUP: SMOOTH

DESCRIPTION: SPLIT DOES ONE PASS AT DIVIDING MESAS (PAIRS OF ADJACENT POINTS WITH A COMMON VALUE WHICH IS A LOCAL MAX OR MIN) USING TUKEY'S END-POINT RULE. IT IS USED IN CONJUNCTION WITH A3R.

STEMLEAFHOW

SYNTAX: STEMLEAF VECTOR

GROUP: DISPLAY

PARAMETERS:

(1) WIDTH- CONTROLS THE WIDTH (CHARACTERS PER LINE) OF THE DISPLAY (DEFAULT=70).

(2) SCALE- VARIES THE DEPTH (STEM INTERVAL) OF THE DISPLAY IN UNITS OF 1, 2, OR 0.5 TIMES A POWER OF 10. SELECT AN INTEGER FROM 1 TO 3 (DEFAULT=1).

SUBPROGRAM: LIT

DESCRIPTION: STEMLEAF GENERATES A STEM AND LEAF DISPLAY OF A VECTOR OF OBSERVATIONS. THE FUNCTION AUTOMATICALLY SCALES THE DATA USING A SCALING ROUTINE BASED ON THE RANGE AND SIZE OF THE DATA VECTOR. BY VARYING THE SCALE PARAMETER THE USER CAN CHANGE THE SIZE OF THE STEM, BUT IT WILL NOT NECESSARILY BE SCALED BY THE AMOUNT SPECIFIED. TRY VARIOUS VALUES LIKE 1,2, AND 3 TO SEE WHICH CHOICE YIELDS THE BEST DISPLAY. IF A LEAF CONTAINS TOO MANY CHARACTERS TO BE PRINTED ON A LINE, THE LINE WILL BE TRUNCATED AND THE NUMBER OF TRUNCATED CHARACTERS WILL BE WRITTEN AT THE END OF THE LINE. IF THE STEM INTERVAL IS TWO TIMES A POWER OF TEN, THE LEAVES MAY CONTAIN THE CHARACTERS A,B,C,...,J IN ADDITION TO THE DIGITS 0,1,...,9. IN THIS CASE, THE CHARACTERS A TO J REPRESENT THE NUMBERS 10 TO 19.

TWICEHOW

SYNTAX: TWICE VECTOR

GROUP: SMOOTH

SUBPROGRAMS: ONE3, SPLIT, A3RSR

DESCRIPTION: TWICE SMOOTHS A SEQUENCE OF DATA, THEN SMOOTHS THE RESIDUALS AND ADDS THE SMOOTHED RESIDUALS BACK TO THE SMOOTHED DATA TO OBTAIN THE FINAL SMOOTH. THE SMOOTHING IS DONE USING A3RSR.

```
      ⍝DEFAULT VALUES OF THE PARAMETERS:


      DEP
15
      DEPTH
20
      EPSILON
0.01
      LENGTH
50
      MISS
¯99999
      NDIVX
4
      NDIVY
4
      NGAP
3
      NORMEFFECTS
0
      NUM
2
      OPTION
1
      RESIDS
1
      SCALE
1
      RSELECT
1
      WID
30
      WIDTH
70
      ΔINTERCEPT
1
      C̲H̲
```

APPENDIX B

```
        ∇AND[⎕]∇
     ∇ L←A AND B;C;D
[1]     →(((2<ρρA)∨3<ρρB),0≠ρρB)/ 17 3
[2]     B←,B
[3]     →(((3=ρρB)∧1≠1ρρB),2=ρρA)/ 17 7
[4]     A←,A
[5]     →(∧/((ρA)≠1,D),1≠D←1ρ¯2ΦρB)/16
[6]     A←(((D×ρA)⌊D⌈ρA),1)ρA
[7]     →(1≠ρρB)/9
[8]     B←(((ρB)⌈(1=ρB)×1ρρA),1)ρB
[9]     →((∧/D≠1,1ρρA),1≠D←1ρ¯2ΦρB)/ 16 11
[10]    B←(((3=ρρB)ρ1),(1ρρA),1ρΦρB)ρB
[11]    →(3=ρρB)/14
[12]    L←(((C←1ρΦρA)ρ0),(1ρΦρB)ρ1)\B
[13]    →0×ρρL[;ιC]←A
[14]    L←(1,((C←1ρΦρA)ρ0),(¯1+1ρΦρB)ρ1)\B
[15]    →0×ρρL[;;1+ιC]←A
[16]    →0=ρ⍞←'ARGUMENTS OF  AND  ARE NOT CONFORMABLE.'
[17]    'AN ARGUMENT OF  AND  IS OF IMPROPER RANK.'
     ∇
```

```
        ∇ANOVA[⎕]∇
     ∇ ANOVA;Y;K;BTSS;MSR;R;MAX;BLSS;MSBL;MSE;WTSS;EDF;TDF;TSS;YBAR;N;
        T;BLOCK
[1]     INPUT
[2]     SUMSQ
     ∇
```

```
        ∇A3R[⎕]∇
     ∇ Z←A3R X;Y1;Y2;X1;X2;N;C
[1]     Z←ONE3 X
[2]     →1×(ρρρX←Z)×0≠+/|Z-X
     ∇
```

```
        ∇A3RSR[⎕]∇
     ∇ Z←A3RSR X
[1]     X←A3R X
[2]     Z←A3R SPLIT X
[3]     →2×(ρρρX←Z)×0≠+/|Z-X
     ∇
```

```
      ∇BOXPLOT[⎕]∇
    ∇ Z←BOXPLOT X;L;U;B
[1]   X←(÷1E¯20+U-L)×((U←⌈/,X)-LENGTH×L←⌊/,X)+,X×LENGTH-1
[2]   0.1×⌊0.5+10×L;(0⌈LENGTH-6)ρ' ';0.1×⌊0.5+10×U
[3]   →9×ι0=U-L
[4]   Z←LENGTH FILL X
[5]   B←' ¯|⌈||¯                       '[1+Z]
[6]   B←B,' *|*|* -×  OOOOOOOOO ⊛⊛⊛⊛⊛⊛⊛⊛⊛'[1+Z]
[7]   B←B,' _|⌊||_     23456789  23456789'[1+Z]
[8]   →0×ρρZ←(3,LENGTH)ρB
[9]   'RANGE OF DISTRIBUTION IS ZERO'
    ∇
```

```
      ∇CHISQUARE[⎕]∇
    ∇ T CHISQUARE X;DF;C
[1]   →3×ι((ρX)=ρT)
[2]   →0×ρ⎕←'LENGTH ERROR: X AND T MUST BE THE SAME SIZE.'
[3]   C←+/((X-T)*2)÷T←T×+/X
[4]   'CHI-SQUARE VALUE = ';C;'  DF = ';(ρX)-1
    ∇
```

```
      ∇CODERES[⎕]∇
    ∇ Z←CODERES X;Y;N;Q;LW;UW
[1]   N←ρY←Y[⍋Y←,X]
[2]   Q←0.5×Y[⌊0.25×3+N×ι3]+Y[⌈0.25×1+N×ι3]
[3]   LW←Q[1]-D←Q[3]-Q[1]
[4]   UW←Q[3]+D
[5]   Y←(X>LW)+(X>Q[1])+(X>Q[3])+X>UW
[6]   Z←'--○++'[1+Y]
[7]   Z←((ρZ[;1]),2×ρZ[1;])ρ(,Z) AND,(ρZ)ρ' '
    ∇
```

```
      ∇COMPARE[⎕]∇
    ∇ Z←COMPARE X;U;L;Y;M;C;J;P
[1]   X←(÷1E¯20+U−⎕←L)×((⎕←U←⌈/Y)−DEPTH×L←⌊/Y←(MISS≠,X)/,X)+X×DEPTH−1
[2]   M←(÷1E¯20+U−L)×(U−DEPTH×L)+MISS×DEPTH−1
[3]   Z←(DEPTH,6×C←⍴X[1;])⍴' '
[4]   J←0
[5]   J←J+1
[6]   P←DEPTH FILL P[⍋P←(P≠M)/P←X[;J]]
[7]   Z[;¯2+6×J]←' |¯⊥_⊤|                       '[1+P]
[8]   Z[;¯1+6×J]←' *⊤=⊥= |×  ooooooooo ⊛⊛⊛⊛⊛⊛⊛⊛⊛'[1+P]
[9]   Z[;6×J]←' |¯⊥_⊤|     23456789  23456789'[1+P]
[10]  →5×⍳J<C
[11]  Z←⊖Z
    ∇
```

```
      ∇CONDENSE[⎕]∇
    ∇ R←CONDENSE X;I;N;NR;U;Q;Z
[1]   R←⍳0
[2]   UTCOND X
[3]   →0×⍳(NUM≠2)
[4]   R←(NR,2)⍴Z
    ∇
```

```
      ∇CONTINGENCY[⎕]∇
    ∇ CONTINGENCY F;R;C;T;E;CHI2;DF
[1]   R←+⌿F
[2]   T←+/C←+/F
[3]   E←C∘.×R÷T
[4]   CHI2←+/,((F−E)*2)÷E
[5]   DF←×/(⍴F)−1
[6]   'CHI−SQUARE VALUE= ';CHI2;'  DF= ';DF
    ∇
```

```
     ∇CONDENSE[⎕]∇
     ∇ R←CONDENSE X;I;N;NR;U;Q;Z
[1]    R←⍳0
[2]    UTCOND X
[3]    →0×⍳(NUM≠2)
[4]    R←(NR,2)⍴Z
     ∇
```

```
       ∇CONTINGENCY[⎕]∇
     ∇ CONTINGENCY F;R;C;T;E;CHI2;DF
[1]    R←+⌿F
[2]    T←+/C←+/F
[3]    E←C∘.×R÷T
[4]    CHI2←+/,((F-E)*2)÷E
[5]    DF←×/(⍴F)-1
[6]    'CHI-SQUARE VALUE= ';CHI2;'  DF= ';DF
     ∇
```

```
       ∇CORRELATION[⎕]∇
     ∇ R←CORRELATION W;Z;C;S;C̲H̲;MEANS;VAR
[1]    C←(⍉Z)+.×Z←W-(⍴W)⍴(MEANS←+⌿W)÷1↑⍴(¯2↑1,1,⍴W)⍴W+⍴C̲H̲←''
[2]    R←'BF8.2' FMT(0,⍳⍴S),[1](⍳⍴S),C÷S∘.×S←(VARS←+⌿Z*2)*
       0.5
     ∇
```

```
      ∇FMT[⎕]∇
    ∇ OL←E̲ FMT R;S;W;Δ;G;X;T;K;J;M;Q;P;D;N;O;L;B;V;CH;H
[1]    N←Q←1↓M←ρR←(1⌈¯2↑ρR)ρR
[2]    OL←((1=1↑M)↓ 1 0 ×M←M+2↑H←1<ρCH←C̲H̲,',')ρΔ←'0123456789.'
[3]    →E×ι(N←0=N)∨V←1≥ρS←,E̲
[4]   L0:→~ιV∨(×P←4×Q=ρK←ρX←' ')∧∨/('A',O←'⍞')∊S
[5]    →(L0+(V←0=ρS←J↓S)+ιB=M[2]←1),L̲-(ι×B←O+.=K),P×~'A'∊K←K,(J←Sι',')
       ↑S
[6]    →E+×ρS←'TEXT DELIMITER'
[7]    →L3-3××(ρG←K=K←(K∊¯1↓Δ)/K)⌊W←ρX←(ρK←(KιO)↑K)↓(-(⌽K)ιO)↓K
[8]   L̲:→(D←~1↑G←K∊Δ)/L3-2×(ρK)≠W←1↑O←'XA'∊K←(~K∊' ,')/K
[9]    →L3×ι(B≠+/G)⍲×M[2]←10⊥|1-Δι(B←|1-Gι0)↑K
[10]   →L3-⌽O,-(L←'EFI'∊K)/×W←10⊥|1-Δι(|1-G←Bι'.')↑B←(1-(⌽G)ι0)↑K
[11]   A̲←(1↓ρX←((1⌈ρA̲)⌊(M[1]-H),W)↑A̲)⌽A̲
[12]  L3:→(HD×ιH∧~'X'∊K),E-ρX←-W,D←0ρP←((M-H,0)×1,W)ρX
[13]   →L4-ι~1↑L,Q←1↓ρR←(0 1 ×ρP←R[;ιM[2]←Q⌊M[2]⌈Q×V∧D])↓R
[14]   P←P÷10*L←⌊10⍟|P+0=P
[15]   →L3×ι0=J←+/B←('B'∊K)⍲0=P←(⌊0.5+N×,P)÷N←10*D←10⊥|1-ΔιG↓B
[16]  L4:→(ρ1↓ρL)/F-ρρX←(1 0 ×ρG←JρT\'¯')ρJ←J,O←∨/T←0>P←B/P
[17]   →(×L←(O⌈L×J←'Z'∊K)⌈.×~T←(T+O←1+⌊10⍟1⌈|P)>O+L←W-D+O+~2↓L)/L/F,E,
       I
[18]   →E+×ρS←'FIELD WIDTH'
[19]   →L4+1+ι((J[2]←L∨.<0)+O←1+10⌈.≤|L←(B/,L)+T←10=|P)>W-D+O+
       3
[20]   T←~J←P[T/ι1↑J]←L←ρ1ρX←'E','+0¯'[Jρ2-×L],Δ[1+⍉(Oρ10)⊤|L]
[21]  F:→(J∨2≥D×~'T'∊K)/I,N←ρX←Δ[11,1+⍉(Dρ10)⊤⌈N×1||P],X
[22]   D←,(-N)↑(D⌈.×⍉X[;2+D]≠1↑Δ)∘.<D←ιD-1
[23]   X←NρX,X[D/ιρX←,X]←' '
[24]  I:→(J←J∨0=+/O←0⌈L-O)/I+ρD←ρP←G,Δ[1+⍉(Lρ10)⊤⌊|P]
[25]   P←Dρ(,O←G⌽O)\(,O←O∘.<(-G)⌽ιL+G←1↓ρG)/,P
[26]   →HD-ιJ∨L←~'L'∊K,P[T/ιD←1↑X←ρP←P,X;]←'*'
[27]   P←Xρ(,⌽O)\(,O←~X↑~O)/,P
[28]   →(~H)/E-N←1,D←0ρP←B⍀(D,X←W×1-2×L)↑P
[29]  HD:CH←(ρK←(¯1↑D←0,(M[2]⌊ρD)ρD←(','=CH)/ιρCH)ρCH)⌽CH
[30]   D←,(M[2],X)↑ 0 ¯1 ↓(M[2],B)ρ(,⌽D∘.≥ιB←⌈/D←1↓D-¯1⌽D)\K
[31]   →(L0-V∧×Q),ρOL←OL,((1=1↑M)↓M×1,W)ρD,,P
[32]  E:K←'NO VALID E, I, OR F PHRASE'
[33]   'FMT PROBLEM       ',K;(1,ρS)ρS
    ∇
```

```
      ∇FILL[⎕]∇
    ∇ Z←W FILL X;N;D;X1;X2;X3;X4;Y;I;J;S
[1]   N←ρX←X[⍋X←,X]
[2]   Z←0.5×X[⌊0.25×3+N×ι3]+X[⌈0.25×1+N×ι3]
[3]   S←(Z[1]-0.5+1.5×D),(Z[1]-0.5+D←Z[3]-Z[1]),Z[1]
[4]   S←⌊0.5+S,Z[2],Z[3],(Z[3]+0.5+D),Z[3]+0.5+
      1.5×D
[5]   X1←(X2≤S[1])/X2←(X≤S[2])/X←⌊0.5+X
[6]   X2←(X2>S[1])/X2
[7]   X4←(X3≥S[7])/X3←(X≥S[6])/X
[8]   X3←(X3<S[7])/X3
[9]   Y←((X>S[2])×X<S[6])/X
[10]  Z←Wρ0
[11]  Z[I]←20+9⌊+⌿(¯1,X1)∘.=I←ι(S←0⌈S⌊W)[1]
[12]  Z[I]←10+9⌊+⌿(¯1,X2)∘.=I←S[1]+ι1+S[2]-S[1]
[13]  Z[I]←10+9⌊+⌿(¯1,X3)∘.=I←¯1+S[6]+ι1+S[7]-S[6]
[14]  Z[I]←20+9⌊+⌿X4∘.=I←¯1+S[7]+ι1+W-S[7]
[15]  →18×ι0=ρY
[16]  Z[J←¯1↑Y]←Z[I←1↑Y]←9
[17]  Z[I+ι0⌈J-I+1]←8
[18]  Z[S[3]+ι0⌈S[5]-S[3]+1]←6
[19]  Z[S[3],S[5]]←0
[20]  Z[S[4]]←1
[21]  Z[S[3],S[5]]←Z[S[3],S[5]]+ 2 4
    ∇
```

```
      ∇INPUT[⎕]∇
    ∇ INPUT;J;M;Z
[1]   'ENTER NUMBER OF TREATMENTS.'
[2]   J←0×K←⎕
[3]   'ENTER VECTOR OF NUMBER OF OBS. FOR TREATMENTS 1 TO ';K
[4]   Y←((MAX←⌈/N←⎕),K)ρ0
[5]   →7×ι(K=ρN)
[6]   →4×ρρ⎕←'RE-ENTER COUNT VECTOR, ONE ELEMENT PER TREATMENT.'
[7]   →0×ι(K<J←J+1)
[8]   'ENTER ';N[J];' OBSERVATIONS FOR TREATMENT ';J
[9]   →7×ρρρY[;J]←(MAX,1)ρZ,(M←MAX-ρZ←⎕)ρ0
    ∇
```

```
      ∇KS[⎕]∇
    ∇ F KS G;Z;N;X;NF;NG;MAX;SIGN;M
[1]   D←NF←ιM←0×N←ρZ←Z[⍋Z←F,G]
[2]   →A1×ι(N<M←M+1)
[3]   NF←NF,(+/F≤X←Z[M])÷ρF
[4]   NF←NF,(+/F<X)÷ρF
[5]   NG←(+/G≤X)÷ρG
[6]   SIGN←×NF←,NF∘.-NG,(+/G<X)÷ρG
[7]   D←D,MAX×1↑((NF=MAX←⌈/NF←|NF)/SIGN)
[8]   →2,NF←ι0
[9]  A1:'MAX F(X)-G(X) =';⌈/D
[10]  'MIN F(X)-G(X) =';⌊/D
    ∇


      ∇LINE[⎕]∇
    ∇ Z←LINE W;X;Y;N;M;P;I;J;K;X1;Y1;X2;Y2;F;SL;YI
[1]   →3×ι2=ρρW
[2]   W←⍉(2,ρW)ρ(ιρW),W
[3]   F←(N←ρX←X[P←⍋X←W[;1]])ρK←SL←0
[4]   X1←0.5×X[I←⌊0.5×M+1]+X[J←⌈0.5×1+M←⌊0.5+N÷3]
[5]   X2←0.5×X[N+1-I]+X[N+1-J]
[6]   Y1←0.5×Z[I]+(Z←Z[⍋Z←M↑Y←W[P;2]-F])[J]
[7]   Y2←0.5×Z[I]+(Z←Z[⍋Z←(-M)↑Y])[J]
[8]   F←(SL←SL+(Y2-Y1)÷X2-X1)×X
[9]   K←K+1
[10]  →6×ιK<2
[11]  YI←0.5×Y[⌊0.5×N+1]+(Y←Y[⍋Y←W[P;2]-F])[⌈0.5×N+1]
[12]  'SLOPE: ';SL;' Y-INTERCEPT: ';YI
[13]  Z←W[;2]-F←YI+SL×W[;1]
[14]  →16×ιKSELECT=1
[15]  →0,,Z←⍉(2,N)ρF,Z
[16]  Z←⍉(2,N)ρW[;1],Z
    ∇


      ∇LIT[⎕]∇
    ∇ R←LIT A
[1]   R←,'0123456789'[1+((1+⌊10⍟A)ρ10)⊤A]
    ∇
```

```
        ∇LSLINE[⎕]∇
      ∇ Z←LSLINE X;N;B
[1]     →A1×⍳2=⍴⍴X
[2]     X←⍉(2,N)⍴X←(⍳N←⍴X),X
[3]    A1:B←X[;2]⌹(⍉(2,N)⍴(,X[;1]),(N←1↑⍴X)⍴1)
[4]     'SLOPE: ';B[1];'  Y-INTERCEPT: ';B[2]
[5]     Z←⍉(2,N)⍴(X[;1]),X[;2]-(B[2]+X[;1]×B[1])
      ∇
```

```
        ∇MEDPOLISH[⎕]∇
      ∇ Z←MEDPOLISH X;k;C;N;RI;CI;RA;CA;S;RG;RE;CE;TV
[1]     R←⍴X[;1]
[2]     N←R×C←⍴X[1;]
[3]     X←X-TV←0.5×Z[⌊0.5×N+1]+(Z←Z[⍋Z←,X])[⌈0.5×N+1]
[4]     RE←R⍴0
[5]     CE←C⍴0
[6]     ⎕←S←+/|,X
[7]     Z←(R,C)⍴(,X)[⍋,X+(⍳R)∘.×C⍴1×RG←(⌈/,X)-⌊/,X]
[8]     X←X-(RI←+/0.5×Z[;⌊0.5×C+1]+Z[;⌈0.5×C+1])∘.×C⍴1
[9]     RE←RE+RI
[10]    Z←⍉(C,R)⍴(,⍉X)[⍋,⍉X+(R⍴1)∘.×(⍳C)×RG]
[11]    X←X-(R⍴1)∘.×CI←+⌿0.5×Z[⌊0.5×R+1;]+Z[⌈0.5×R+1;]
[12]    CE←CE+CI
[13]    →6×⍳EPSILON<1-+/|,X÷S
[14]    Z←X
[15]    →17×⍳RESIDS≠2
[16]    Z←⍉(2,N)⍴((,RE∘.×CE)÷TV),,Z
[17]    →21×⍳NORMEFFECTS=0
[18]    RE←RE-RA←(+/RE)÷R
[19]    CE←CE-CA←(+/CE)÷C
[20]    TV←TV+RA+CA
[21]    'TYPICAL VALUE: ';TV
[22]    'ROW EFFECTS: ';RE
[23]    'COLUMN EFFECTS: ';CE
      ∇
      ∇MSTATS[⎕]∇
    ∇ MSTATS W;Z;C;S;C̲H̲;MEANS;VARS;N;J
[1]   C←(⍉Z)+.×Z←W-(ρW)ρMEANS←(+⌿W)÷N←1↑ρ(¯2↑1,1,ρW)ρW+ρC̲H̲←''
[2]   'BF8.2' FMT(0,⍳ρS),[1](⍳ρS),C÷S∘.×S←(VARS←+⌿Z*2)*
      0.5
[3]   '⍞MEANS    ⍞,BF8.2' FMT MEANS
[4]   '⍞STD.DEV ⍞,BF8.2' FMT S←S÷(N-1)*0.5
[5]   Z←⍳J←0
[6]   →END×⍳(ρS)<J←J+1
[7]   C←X[⍋X←W[;J]]
[8]   →6,Z←Z,C←0.5×C[⌊0.25×3+N×⍳3]+C[⌈0.25×1+N×⍳3]
[9]  END:Z←((ρS),3)ρZ
[10]  '⍞L. QRTLS⍞,BF8.2' FMT Z[;1]
[11]  '⍞MEDIANS ⍞,BF8.2' FMT Z[;2]
[12]  '⍞U. QRTLS⍞,BF8.2' FMT Z[;3]
    ∇
```

```
      ∇NUMSUM[⎕]∇
    ∇ NUMSUM X;N;Q;T1;C̲H̲
[1]   CR
[2]   '                   NUMERICAL SUMMARY'
[3]   70ρ'-'
[4]   N←ρX←X[⍋X←(X≠MISS)/X←,X]
[5]   'SAMPLE SIZE = ';N
[6]   70ρ'-'
[7]   Q←0.5×X[⌊0.125×7+N×⍳7]+X[⌈0.125×1+N×⍳7]
[8]   T1←Q[4],0,Q[4],0,0,((Q[2]+Q[6])÷2),Q[2],0
[9]   T1←T1,Q[6],(Q[6]-Q[2]),((Q[1]+Q[7])÷2)
[10]  T1←T1,Q[1],0,Q[7],(Q[7]-Q[1]),((X[1]+X[N])÷2)
[11]  T1←T1,X[1],0,X[N],X[N]-X[1]
[12]  T1← 4 5 ρT1
[13]  C̲H̲←'MIDPTS,,LOQ/8/MIN,,MEDIAN,,UPQ/8/MAX,,SPREADS,'
[14]  'BF10.2,⍞ | ⍞' FMT T1
[15]  70ρ'-'
    ∇
```

```
      ∇ONEH[⎕]∇
    ∇ H←ONEH X;A;B;C
[1]   A←0,X,0
[2]   B←X,0,0
[3]   C←0,0,X
[4]   H←¯2↓(C+B+2×A)÷4
[5]   H←X[1],2↓H,X[ρX]
    ∇
```

```
      ∇ONE3[⎕]∇
    ∇ Z←ONE3 X;Y1;Y2;X1;X2;N;C
[1]   Y1←(3×X[2])-2×X[3]
[2]   Y2←(3×X[N-1])-2×X[¯2+N←⍴X]
[3]   X1←Y1,¯1↓X
[4]   X2←1↓X,Y2
[5]   Z←(Y1,X,Y2)[(⍳N)+1+(C=X1<X)-(X≤X2)=C←X1<X2]
    ∇
```

```
      ∇PARTIAL[⎕]∇
    ∇ P←PARTIAL W;C;CIN;M;Y;X;BETA
[1]   M←⍳1↓⍴W
[2]   'ENTER COLUMNS OF MATRIX TO BE PARTIALLED OUT.'
[3]  A1:→A2×⍳0≠+/~(C←⎕)∊M
[4]   Y←W[;CIN←(~M∊C)/M]
[5]   →0,⍴P←CORRELATION R←Y-X+.×BETA←Y⌹X←1,(2↑(⍴W[;C]),1)⍴W[;C]
[6]  A2:→A1,⍴'UNACCEPTABLE VALUES, ENTER INTEGERS FROM 1 TO ';M
    ∇
```

```
      ∇SHOWRES[⎕]∇
    ∇ Z←SHOWRES X;Y;N;Q;D;LW;LF;UW;UF
[1]   N←⍴Y←Y[⍋Y←,X]
[2]   Q←0.5×Y[⌊0.25×3+N×⍳3]+Y[⌈0.25×1+N×⍳3]
[3]   LW←Q[1]-D←Q[3]-Q[1]
[4]   UW←Q[3]+D
[5]   LF←LW-D÷2
[6]   UF←UW+D÷2
[7]   Y←(X>LF)+(X>LW)+(X>Q[1])+(X>Q[2])+(X>Q[3])+(X>UW)+X>UF
[8]   Z←'O○∘∘∘∘×X'[1+Y]
[9]   Z←((⍴Z[;1]),2×⍴Z[1;])⍴(,Z) AND,(⍴Z)⍴' '
    ∇
```

```
      ∇REGRESS[⎕]∇
    ∇ Z←Y REGRESS X;N;K;C;XPXINV;XPY;BETA;RSS;TSS;S2;ESS;WID;DEP
[1]   X←(2↑(ρX),1)ρX
[2]   X←(0,1-ΔINTERCEPT)↓1,X
[3]   XPXINV←⌹(⍉X)+.×X
[4]   BETA←XPXINV+.×XPY←(⍉X)+.×Y
[5]   RSS←((⍉BETA)+.×XPY)-C←((+⌿Y)*2)÷N←ρ,Y
[6]   ESS←(TSS←((⍉Y)+.×Y)-C)-RSS
[7]   S2←,ESS÷(N-1)-K←(ρ,BETA)-ΔINTERCEPT
[8]   CR
[9]   '                          ANOVA'
[10]  C̲H̲←'SOURCE,DF,SUM SQUARES,MEAN SQUARE,F-RATIO'
[11]  ' '
[12]  '⍞REGRESSION⍞,I4,BE16.4' FMT(K),(,RSS),(,RSS÷K),(,RSS÷K)÷S2
[13]  C̲H̲←''
[14]  '⍞  RESIDUAL⍞,I4,BE16.4' FMT((N-1)-K),(,ESS),S2,0
[15]  '⍞TOTAL     ⍞,I4,BE16.4' FMT(N-1),(,TSS),0,0
[16]  ' '
[17]  'R SQUARE:  ';,RSS÷TSS
[18]  'STD ERROR: ';,S2*0.5
[19]  C̲d̲←'COEFFICIENTS,T STATISTICS'
[20]  'F15.4' FMT⍉(2,ρ,BETA)ρ(,BETA),(,BETA)÷(1 1 ⍉V←S2×XPXINV)*
      0.5
[21]  'DO YOU WANT A PRINTOUT OF THE VARIANCE-COVARIANCE MATRIX?'
[22]  →A1×ι'Y'≠1↑⍞
[23]  'VARIANCE-COVARIANCE MATRIX: ',C̲H̲←''
[24]  'E12.4' FMT V
[25] A1:'DURBIN-WATSON: ';(+/((1↓,C)-(¯1↓,C))*2)÷+/(,C←Y-X+.×BETA)*
      2
[26]  Z←⍉(2,N)ρ(,X+.×BETA),,C
[27] B1:'DO YOU WANT TO FORECAST A VALUE FOR Y?'
[28]  →C1×ι'Y'≠1↑⍞
[29]  'ENTER X VECTOR (';K;' VALUES)'
[30]  'FORECAST OF Y VALUE: ';(C←(1-ΔINTERCEPT)↓1,⎕)+.×BETA
[31]  'VARIANCE OF FORECAST ERROR: ';S2×1+C+.×XPXINV+.×⍉C
[32]  →B1
[33] C1:'DO YOU WANT TO SCAT RESIDUALS VS. PREDICTED Y?'
[34]  →0×ι'N'=1↑⍞
[35]  DEP←0.5×WID←⌊/70,(⌈/((0.75×N),30))
[36]  SCAT Z
    ∇
```

```
      ∇SCAT[⎕]∇
    ∇ W←SCAT Z;N;X;Y;C;R;U;S;L;I;J;K;UT;CL;G;D;B;A;O;V
[1]   →3×⍳(2=+/2=N)∨(×/N)>+/N←⍴Z
[2]   Z←⍉(2,⍴Z)⍴(⍳⍴Z),Z←,Z
[3]   Y←Z[;1+⍳C←¯1+(⍴Z)[2]]
[4]   R←⍴Z←X←,Z[;1]
[5]   L←U←S←2⍴0
[6]   J←1+0×⍴(D←NDIVX,NDIVY),B←WID,DEP
[7]   UT←10*⌊10⍟CL←1E¯20+((U[J]←⌈/Z)-S[J]←⌊/Z)÷D[J]
[8]   S[J]←UT×⌊S[J]÷UT←UT[1↑⍋|CL-UT←(1 2 5)×UT]
[9]   U[J]←UT×⌈U[J]÷UT
[10]  L[J]←1+G×⌊(B[J]-1)÷G←(U[J]-S[J])÷UT
[11]  Z←,Y
[12]  →7×⍳3>J←J+1
[13]  A←(⌽L)⍴0
[14]  X←1+⌊0.5+(L[1]-1)×(X-S[1])÷U[1]-S[1]
[15]  Y←1+⌊0.5+(L[2]-1)×(Y-S[2])÷U[2]-S[2]
[16]  I←1
[17]  →20×⍳1<C
[18]  A[Y[I;1];X[I]]←10⌊A[Y[I;1];X[I]]+1
[19]  →18+6×R<I←I+1
[20]  J←1
[21]  D←0=V←A[Y[I;J];X[I]]
[22]  A[Y[I;J];X[I]]←(10×V>K+1)+((K+1)×K=V)+(K←35-2×J)×D
[23]  →21×⍳R≥I←I+1
[24]  →21×⍳C≥J←J+I←1
[25]  O←(⌽⍴A)⌊1⌈1+⌊0.5+(L-1)×S÷S-U
[26]  A[;O[1]]←A[;O[1]]+36×0=A[;O[1]]
[27]  A[O[2];]←A[O[2];]+35×0=A[O[2];]
[28]  W←' ∘23456789⌹LL̲KK̲JJ̲II̲HH̲GG̲FF̲EE̲DD̲CC̲BB̲AA̲-|'[1+⊖A≥
]
[29]  'RANGE OF X: ';S[1],U[1]
[30]  'RANGE OF Y: ';S[2],U[2]
    ∇
```

```
       ∇SPLIT[⎕]∇
     ∇ Z←SPLIT X;P;Q;R;S;T;N;I;J;C
[1]    P←¯3↓X
[2]    Q←¯2↓1↓X
[3]    R←¯1↓2↓X
[4]    S←3↓X
[5]    I←(((P<Q)×R>S)+(P>Q)×R<S)×Q=R
[6]    Q←(X←X[1],X,X[N])[1+I←(I≠0)/I←I×⍳¯3+N←⍴X]
[7]    R←(3×Q)-2×X[I]
[8]    P←X[I+2]
[9]    T←(3×S←X[I+4])-2×X[I+5]
[10]   X[I+2]←(R×1=J)+(P×¯1=J)+Q×0=J←(C=P<Q)-(Q≤R)=C←P<R
[11]   X[I+3]←(T×1=J)+(P×¯1=J)+S×0=J←(C=P<S)-(S≤T)=C←P<T
[12]   Z←1↓¯1↓X
     ∇
```

```
       ∇STATISTICS[⎕]∇
     ∇ STATISTICS R;XBAR;VAR;N;Q;S;Z
[1]    XBAR←(+/R)÷N←⍴,R
[2]    VAR←(+/((R-XBAR)*2))÷N-1
[3]    S←R[⍋R]
[4]    Q←0.5×S[⌊0.25×3+N×⍳3]+S[⌈0.25×1+N×⍳3]
[5]    'MEAN: ';XBAR
[6]    'VARIANCE: ';VAR
[7]    'STD. DEV.: ';S←VAR*0.5
[8]    'COEFF. OF VARIATION: ';S÷|XBAR
[9]    'LOWER QUARTILE: ';Q[1]
[10]   'UPPER QUARTILE: ';Q[3]
[11]   'MEDIAN: ';Q[2]
[12]   'TRIMEAN: ';0.25×Q[1]+Q[3]+2×Q[2]
[13]   'MIDMEAN: ';(÷⍴Z)×+/Z←((R≥Q[1])∧(R≤Q[3]))/R
[14]   'RANGE: ';(⌈/R)-⌊/R
[15]   'MIDRANGE: ';((⌈/R)+⌊/R)÷2
[16]   'MEAN ABSOLUTE DEVIATION: ';(+/|R-Q[2])÷N
[17]   'INTERQUARTILE RANGE: ';Q[3]-Q[1]
[18]   'COEFF. OF SKEWNESS: ';((+/(R-XBAR)*3)÷N-1)÷S*3
[19]   'COEFF. OF KURTOSIS: ';(((+/(R-XBAR)*4)÷N-1)÷S*4)-3
     ∇
```

```
      ∇STEMLEAF[⎕]∇
    ∇ Z←STEMLEAF X;C;R;S;SI;I;J;F;A;W;L;WW;AA;XW
[1]   C←10*1-⌊10⍟R←1E¯20+(X[ρX]-(X←X[⍋X←,X])[1])÷SCALE
[2]   SI←(1+3×+/(R×C)> 25 50)++/(ρX)> 25 100
[3]   X←⌊0.5+X×C×10*+/SI= 2 3 6
[4]   F←+/(SI=⍳9)/ 0.5 2 1 1 0.5 2 2 1 0.5
[5]   A←20ρ'0123456789ABCDEFGHIJ',Z←''
[6]   I←F×⌊X[1]÷10×F
[7]   XW←8+WW←WIDTH-4
[8]   S←'- '[1+J←X[1]≥0]
[9]   L←1+(|W←(X≤(10×I)+J×¯1+10×F)/X)-10×⌊|I
[10]  AA←A[1+(10 10)⊤|⌊I]
[11]  →((ρA[L])≤WW)/L1
[12]  Z←Z,XWρS,AA,'|',(WW↑A[L]),'+',(LIT(ρA[L])-WW),2ρ' '
[13]  →L2
[14] L1:Z←Z,XWρS,AA,'|',A[L],XWρ' '
[15] L2:I←I+F×1-(I=0)×X[1]<0
[16]  →8×⍳0<ρX←(ρW)↓X
[17]  Z←((⌊(ρZ)÷XW),XW)ρZ
    ∇
```

```
      ∇SUMSQ[⎕]∇
    ∇ SUMSQ;C;NUMBER;B;BLDF
[1]   T←+⌿Y
[2]   TSS←(+/(+/Y*2))-C←((+/T)*2)÷NUMBER←+/N
[3]   BLSS←(+/(((B←+/Y)*2)÷K))-C
[4]   MSBL←BLSS÷BLDF←MAX-1
[5]   →7×⍳(OPTION=2)
[6]   BLSS←BLDF←0
[7]   WTSS←TSS-BLSS+BTSS←(+/((T*2)÷N))-C
[8]   MSR←BTSS÷K-1
[9]   TDF←NUMBER-1
[10]  F←MSR÷MSE←WTSS÷EDF←TDF-BLDF+K-1
[11]  BLOCK←(B÷K)-YBAR←(+/T)÷NUMBER
[12]  '                          ANOVA TABLE'
[13]  '  SOURCE       DF            SS            MS         F'
[14]  CH←''
[15]  '⍞  TREATMENT⍞,I5,F13.2,F11.2,F8.2' FMT(K-1),BTSS,MSR,F
[16]  →(OPTION=1)/L5
[17]  '⍞  BLOCKS⍞,I8,F13.2,F11.2,F8.2' FMT(MAX-1),BLSS,MSBL,(MSBL÷MSE
      )
[18] L5:'⍞  ERROR⍞,I9,F13.2,F11.2' FMT EDF,WTSS,MSE
[19]  '⍞  TOTAL⍞,I9,F13.2' FMT TDF,TSS
[20]  '⍞R-SQUARE = ⍞,F5.3' FMT(BTSS+BLSS)÷TSS
[21]  '⍞OVERALL MEAN = ⍞,F10.2' FMT YBAR
[22]  '⍞TREATMENT EFFECTS ⍞,F6.2' FMT(T÷N)-YBAR
[23]  →(OPTION=1)/0
[24]  '⍞BLOCK EFFECTS ⍞,F6.2' FMT BLOCK
    ∇
```

```
      ∇TWICE[⎕]∇
    ∇ Z←TWICE X;Y
[1]   Z←Y+A3RSR X-Y←A3RSR X
    ∇
```

```
      ∇UTCOND[⎕]∇
    ∇ UTCOND X
[1]   X←(2⍴(⍴X),1)⍴X
[2]   Z←''
[3]   I←0×NR←(⍴X)[2]
[4]   N←⍴U←U[⍋U←(U≠MISS)/U←X[;I+1]]
[5]   Q←0.5×U[⌊0.125×7+N×⍳7]+U[⌈0.125×1+N×⍳7]
[6]   →7+2×⌊NUM÷2
[7]   Z←Z,Q[4]
[8]   →4+11×NR=I←I+1
[9]   Z←Z,Q[4],Q[6]-Q[2]
[10]  →4×NR>I←I+1
[11]  Z←Z,U[1],Q[2],Q[4],Q[6],U[N],N
[12]  →4+13×NR=I←I+1
[13]  Z←Z,U[1],Q[1 2 4 6 7],U[N],N
[14]  →4+16×NR=I←I+1
[15]  CH←'MEDIANS'
[16]  →0×⍴⎕←'F10.2' FMT Z←(NR,1)⍴Z
[17]  Z←(NR,6)⍴Z
[18]  CH←'MIN,LOQ,MEDIAN,UPQ,MAX,SIZE'
[19]  →0×⍴⎕←'F10.2' FMT Z
[20]  Z←(NR,8)⍴Z
[21]  CH←'MIN,LO8,LOQ,MEDIAN,UPQ,UP8,MAX,SIZE'
[22]  ⎕←'F9.2' FMT Z
    ∇
```

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