

Trigonometry: Finding an Unknown Angle

June 10, 2014

Review: 4.06 Q14

A hot air balloon is anchored to the ground by a rope. When it drifts 20 m sideways, it makes an angle of 75° with the ground. How long is the rope (to one decimal place)?

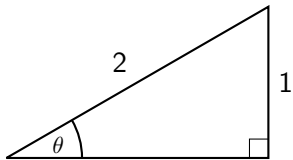
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Finding unknown angles

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Notation: if $\sin(\theta) = \frac{a}{b}$, we write

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