

COMPARISON OF NUMERICAL AND HYDRAULIC
OCEANOGRAPHIC PREDICTION MODELS

Leopoldo Salas Römer

Library
Naval Postgraduate School
Monterey, California 93940

NAVAL POSTGRADUATE SCHOOL

Monterey, California



THESIS

COMPARISON OF NUMERICAL AND HYDRAULIC
OCEANOGRAPHIC PREDICTION MODELS

by

Leopoldo Salas Römer

Thesis Advisor:

E.B. Thornton

September 1972

Approved for public release; distribution unlimited.

T152287

Comparison of Numerical and Hydraulic
Oceanographic Prediction Models

by

Leopoldo Salas Römer
Commander, Venezuelan Navy

Submitted in partial fulfillment of the
requirements for the degree of

MASTER OF SCIENCE IN OCEANOGRAPHY

from the

NAVAL POSTGRADUATE SCHOOL
September 1972

ABSTRACT

The Hydro-Numerical Prediction Model developed by Hansen is applied to San Diego Bay, and the results compared both with the hydraulic model and the real data obtained by field measurements. This allows one of the few good comparisons between numerical and hydraulic models for the prediction of actual conditions.

The bay was divided into two sections that were run separately in order to obtain the desirable spatial resolution. This division required solving the problems of proper tuning and matching techniques between both portions. The solution involved the addition of an appended pseudo-bay to the first section of the model in order to compensate for the correct tidal prism. The effects of a proposed second open entrance in the southern part of the bay were studied. This resulted in an increase of flushing in the southern portion of the bay but caused the currents in the center of the bay to be small which decreased dispersion in the central portion of the bay. In general, both models produced similar and reliable results, but there was a considerable reduction of cost and time with the numerical model.

TABLE OF CONTENTS

I.	INTRODUCTION -----	11
	A. REVIEW -----	11
	B. OBJECTIVES -----	12
II.	HYDRAULIC MODEL OF SAN DIEGO BAY -----	14
	A. DESCRIPTION OF SAN DIEGO BAY -----	14
	B. PURPOSE OF THE U.S. CORPS OF ENGINEERS MODEL STUDY -----	16
	C. THE HYDRAULIC MODEL -----	16
	D. RESULTS OF THE HYDRAULIC MODEL -----	21
III.	THE HANSEN HYDRODYNAMICAL-NUMERICAL MODEL -----	27
	A. SELECTION OF THE GRID -----	35
	B. TIDE INPUT IN THE MODEL (1) -----	37
	C. ADDITION OF AN APPENDED PSEUDO-BAY-----	40
	D. MODEL (2) -----	54
	E. MODEL (3) -----	63
IV.	MERITS OF HYDRAULIC AND NUMERICAL MODELS -----	79
V.	CONCLUSIONS -----	83
	APPENDIX A. NUMERICAL PROGRAMS -----	87
	BIBLIOGRAPHY -----	133
	INITIAL DISTRIBUTION LIST -----	135
	FORM DD 1473 -----	140

LIST OF FIGURES

1.	SAN DIEGO BAY -----	15
2-1.	HEIGHT IN THE PROTOTYPE AND IN THE HYDRAULIC MODEL -----	23
2.	A. CURRENT AT A-2 U.S. CORPS OF ENGINEER RESULTS -	25
	B. CUURENT AT B-2 U.S. CORPS OF ENGINEER RESULTS -	25
3.	A. CURRENT AT C-2 U.S. CORPS OF ENGINEER RESULTS -	26
	B. CURRENT AT D-2 U.S. CORPS OF ENGINEER RESULTS -	26
4.	A. SCHEME OF THE GRID NET -----	33
	B. COMPUTATION GRID -----	33
5.	A. INPUT BOUNDARY AND FREE BOUNDARY WITHOUT CONTINUATION -----	39
	B. LEVELING OF THE EDGES (LUBRICATED WALL) AT BOUNDARIES -----	39
	C. CONTINUATION OF CURRENT AT THE FREE OPEN BOUNDARY WITH THE GRADIENT CORRECTED BY A CONSTANT -----	39
6.	A. VALUES OF Z ALONG MODEL (1) FOR DIFFERENT CONSTANTS IN THE CONTINUATION OF THE FREE BOUNDARY AFTER 1 HOUR OF REAL TIME -----	41
7.	VALUES OF VELOCITY AT M-3 AND N-45 TO 53 IN THE FREE OPEN BOUNDARY FOR DIFFERENT CONSTANTS IN THE CONTINUATION AFTER 1 HOUR OF REAL TIME -----	41
8.	APPENDED AREAS IN MODEL (1) -----	42
9.	CIRCULATION IN MODEL (1) WITH THE APPENDED AREAS --	43
10.	A. HEIGHT AT NAVY PIER MODEL (1) FOR DIFFERENT APPENDED AREAS -----	45
	B. HEIGHT AT PIER N. 2 MODEL (1) FOR DIFFERENT APPENDED AREAS -----	45
11.	A. CURRENT AT A-2 MODEL (1) FOR DIFFERENT APPENDED AREAS -----	46

	B.	CURRENT AT C-2 MODEL (1) FOR DIFFERENT APPENDED AREAS -----	46
12.	A.	VOLUME TRANSPORT IN SECTION AA1 MODEL (1) -----	47
	B.	VOLUME TRANSPORT IN SECTION AA2 MODEL (1) -----	47
13.	A.	CURRENT AT A-2 MODEL (1) -----	48
	B.	CURRENT AT B-1 MODEL (1) -----	48
14.	A.	CURRENT AT C-2 MODEL (1) -----	49
	B.	NET VOLUME TRANSPORT MODEL (1) -----	49
15.	A.	HEIGHT AT NAVY PIER MODEL (1) -----	50
	B.	HEIGHT AT PIER N. 2 MODEL (1) -----	50
16.		CURRENT DISTRIBUTION IN MODEL (1) AT TIME = 0 Hr ---	51
17.		CURRENT DISTRIBUTION IN MODEL (1) AT TIME = 3 Hr ---	52
18.		CURRENT DISTRIBUTION IN MODEL (1) AT TIME = 9 Hr ---	53
19.	A.	CURRENT AT C-2 MODEL (2) FOR DIFFERENT VALUES OF R -----	55
	B.	CURRENT AT D-2 MODEL (2) FOR DIFFERENT VALUES OF R -----	55
20.	A.	HEIGHT AT PIER N. 2 MODEL (2) FOR DIFFERENT VALUES OF R -----	56
	B.	HEIGHT AT SOUTH BAY MODEL (2) FOR DIFFERENT VALUES OF R -----	56
20-1.		ENERGY DENSITY SPECTRUM -----	58
21.	A.	CURRENT AT C-2 FOR DIFFERENT MINIMUM DEPTHS ----	60
	B.	HEIGHT AT PIER N. 2 FOR DIFFERENT MINIMUM DEPTHS -----	60
22.	A.	CURRENT AT C-2 MODEL (2) -----	61
	B.	CURRENT AT D-2 MODEL (2) -----	61
23.	A.	HEIGHT AT PIER N. 2 MODEL (2) -----	62
	B.	HEIGHT AT SOUTH BAY MODEL (2) -----	62

24.	CURRENT DISTRIBUTION IN MODEL (2) AT TIME = 3 Hr --	64
25.	CURRENT DISTRIBUTION IN MODEL (2) AT TIME = 9 Hr --	65
26.	CURRENT DISTRIBUTION IN MODELS (1) and (2) AT TIME = 9 Hr -----	66
27.	CURRENT DISTRIBUTION IN MODELS (1) and (2) AT TIME = 3 Hr -----	67
28.	CURRENT DISTRIBUTION IN MODELS (1) and (2) AT TIME = 15 Hr -----	68
29.	CURRENT DISTRIBUTION HYDRAULIC MODEL (BASE TEST) AT TIME = 12 Hr -----	70
30.	CURRENT DISTRIBUTION HYDRAULIC MODEL (BASE TEST) AT TIME = 18 Hr -----	71
31.	A. CURRENT AT C-2 MODEL (3) -----	72
	B. CURRENT AT D-2 MODEL (3) -----	72
32.	A. CURRENT AT CROWN CAVE MODEL (3) -----	73
	B. HEIGHT AT SOUTH BAY MODEL (3) -----	73
33.	NET VOLUME TRANSPORT MODEL (3) -----	74
34.	CURRENT DISTRIBUTION MODEL (3) -----	75
35.	CURRENT DISTRIBUTION MODEL (3) -----	76
36.	CURRENT DISTRIBUTION HYDRAULIC MODEL (PROPOSED SECOND ENTRANCE) AT TIME = 12 Hr -----	77
37.	CURRENT DISTRIBUTION HYDRAULIC MODEL (PROPOSED SECOND ENTRANCE) AT TIME = 18 Hr -----	78

TABLE OF SYMBOLS AND ABBREVIATIONS

C	Phase wave speed
C_m	Velocity in the model
C_p	Velocity in the prototype
d	Total difference
F	Friction force
f	Coriolis parameter
F_r	Froude number
g	Acceleration of gravity
g_m	Gravity in the model
g_p	Gravity in the prototype
H	Total depth ($h + \eta$)
h	Depth of the water at mean sea level
h_m	Depth in the model
h_p	Depth in the prototype
HTU HTV	Depth at U and V grid points
HTZ	Depth at Z grid points
J	Dimensionalless constant
K	Coefficient of horizontal kinematic eddy viscosity
\vec{k}	Vertical unit vector
km	Kilometer
L	Characteristic length
L_m	Characteristic length in the model
L_p	Characteristic length in the prototype

ℓ	Length of mesh
M,N	Grid co-ordinates (also m,n)
m	Meter
cm	Centimeter
MEH NEH	Near border grid points
p	Hydrostatic pressure
R	Bottom roughness coefficient
R_g	Gravity ratio. Gravity scale
R_c	Velocity ratio. Velocity scale
R_h	Depth ratio. Vertical scale
R_L	Length ratio. Horizontal scale
R_t	Time ratio. Time scale
R_{vd}	Discharge ratio. Discharge scale
R_v	Volume ratio. Volume scale
r	Coefficient of friction
t	Time
u,v	Components of horizontal velocity
\vec{V}	Total velocity vector
V_c	Characteristic velocity
\bar{V}, \bar{U}	Mean u and v components
$W()$	Wind speed component
X,Y	Space co-ordinates
Z,U,V	Grid points
α	Smoothing parameter
β	$1 - \alpha$

δ	Partial difference
γ	Specific weight
λ	Drag coefficient
η	Sea level anomaly
ρ	Density of the fluid
τ	Wind stress
$\vec{\Omega}$	Earth angular velocity
∇	$\frac{\partial}{\partial x} + \frac{\partial}{\partial y}$
τ^b	Bottom stress
Δ	Difference

ACKNOWLEDGEMENTS

I wish to express my sincere thanks to everyone who has assisted in the preparation of this study. In particular, I extend my gratitude to Dr. T. Laevastu of the Environmental Prediction Research Facility, to Mr. Sheldon Lazanoff of Fleet Numerical Weather Central, and to Miss Sharon Raney of the Computer Center for their helpful suggestions, encouragement, and programming assistance. Finally to Dr. Edward B. Thornton, my thesis advisor, my sincere thanks for his patience, understanding, and constructive criticism that contributed greatly to the completion of this project.

I. INTRODUCTION

A. REVIEW

The study of bays, estuaries and other semi-restricted areas is difficult because these masses of water are subject to constant movement with short time irregular periodicities. The important mechanism driving the circulation in these areas generally is the tide. The water is partially renewed and mixed during each tidal cycle due to the interchange of water between such areas and the ocean. The shape and depth of the area governs the direction and speed of the currents generated during this interchange. The constant flow of water causes a constant state of non-equilibrium of constituents, temperature and potential energy inside the bays or estuaries.

The study of such areas by field observations is extremely laborious requiring large expenditures of manpower and money. Another approach to the solution of the problem is to reproduce the physical characteristics of these areas by the use of hydraulic models. Hydraulic models have been used for many decades and have proven to be a reliable method for studying an area although space and operating problems make them a relatively expensive tool of investigation.

With the advent of high speed computers, the numerical solution of the differential equations used to describe

flow was made possible. Oceans, seas, gulfs and other water masses have been described by the use of this technique. It transforms a physical model into a program which can be modified to simulate different conditions more easily, can be stored for future uses and alterations, is faster and allows solutions to be obtained at reasonable cost.

The U. S. Army Corps of Engineers made a study of San Diego Bay by means of a hydraulic model based on field measurements made in early 1967. The results have been reported in a Technical Report [10] and published in a paper [1] by the U. S. Corps of Engineers.

The Hydro-Numerical Prediction Model developed by Hansen is applied to San Diego Bay, and the results compared both with the hydraulic model and the data obtained by field measurements. This allows one of the few good comparisons between numerical and hydraulic models for the prediction of actual conditions.

B. OBJECTIVES

The objective of this thesis is to reproduce by means of the Hansen hydrodynamic-numerical model the existing conditions in San Diego Bay and compare them with conditions produced in the hydraulic model operated by the U. S. Corps of Engineers. This comparison will result in a proper evaluation of the merits and limitations of both models.

The division of the bay into two separate models is attempted in order to obtain comparable resolution in the numerical model. This division requires solving problems in the method of running numerical models in series and of transferring boundary conditions from one section to another.

II. HYDRAULIC MODEL OF SAN DIEGO BAY

A. DESCRIPTION OF SAN DIEGO BAY

San Diego Bay is located on the southern coast of California, U.S.A. The bay is long, curved, has an area of approximately 90 sq. km. and a maximum width of 3.1 km.

[Fig. 1]. It is connected with the ocean by the narrow Zuniga Channel at its northern end.

The inflow of fresh water can be considered negligible except during local heavy rainfall. The circulation of the entire bay is driven by the tide at its unique entrance. The tidal circulation can be perturbed by local wind conditions.

The tide is of the mixed type with a period of 24.83 hours and maximum range of about 1.89 meters. Field measurements indicate that tidal variations become larger in the bay increasing to 1.98 meters at the center portion of the bay and 2.1 meters near the southern end. Currents have a maximum speed of about 0.7 meters/second in Zuiga Channel.

A channel is maintained for navigation starting at Zuniga Channel and continuing throughout San Diego Bay. The channel depth is 12.8 meters below MLLW from the ocean to the vicinity of the South Bay gage. Other channels of minor importance exist in the southern portion of the bay.

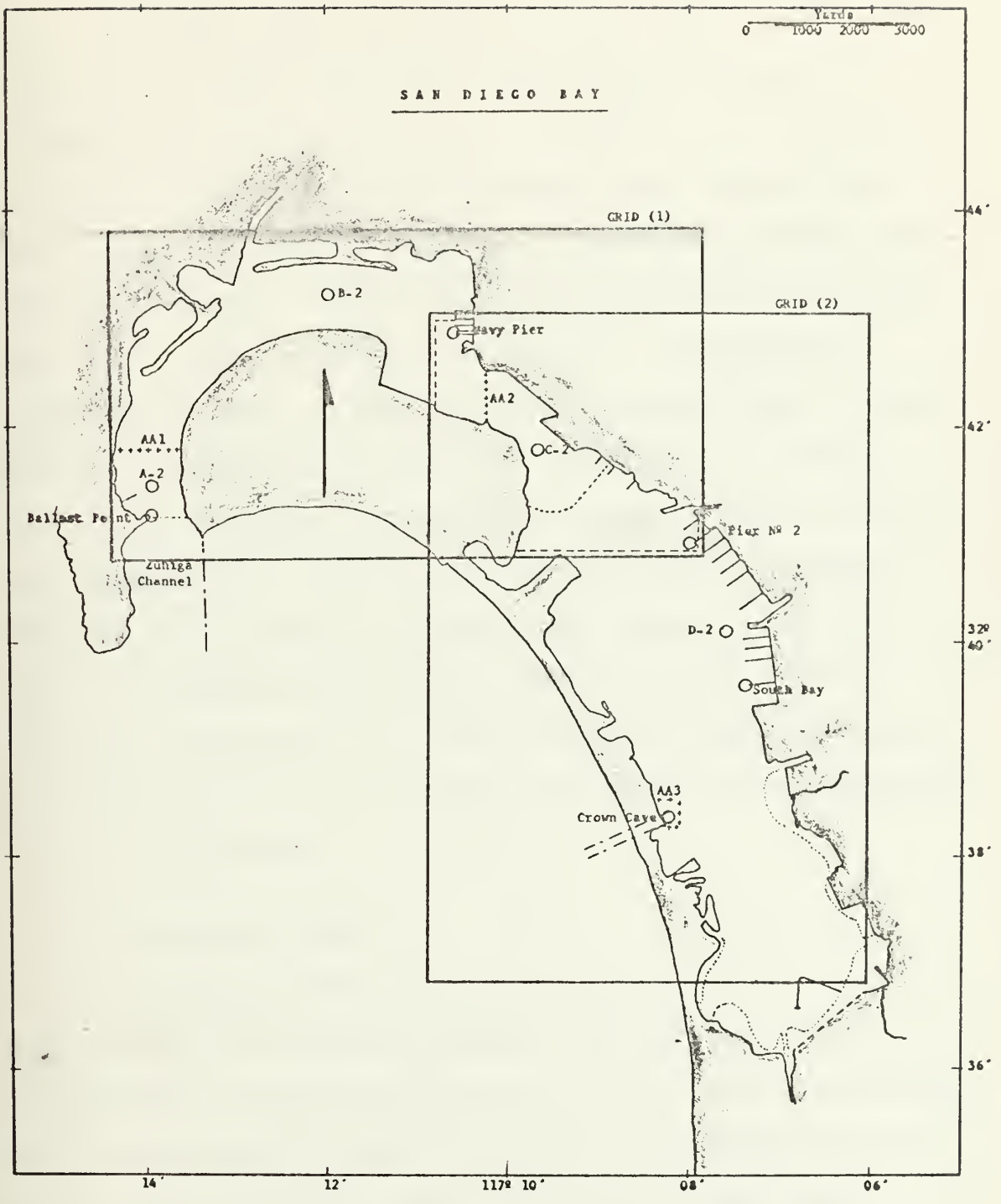


FIGURE 1

B. PURPOSE OF THE U.S. CORPS OF ENGINEERS MODEL STUDY

The natural shape of San Diego Bay and its only entrance at the northern end, its use as a Naval Base, and the influence of a large community surrounding the Bay, have brought into consideration the construction of a second navigation entrance somewhere along Silver Strand Beach. This second entrance is expected to cause decreasing ship traffic throughout Zuniga Channel and increasing flushing rate of the Bay, possibly improving the environmental conditions within the bay. A major consideration in evaluating the overall benefits of a second entrance depend heavily on assessing the extent to which it would increase the flushing rate. These effects could not be computed reliably by the available analytical methods [10], so a physical hydraulic model of the bay, in which several suggested locations for a second entrance could be tested, was constructed to investigate the effects of each proposed location, in detail.

C. THE HYDRAULIC MODEL

The dominant forces in rivers, narrow estuaries and some lakes, are pressure gradient forces driving circulations which are opposed by friction [12]. In large scales of circulations, the opposing forces are combinations of friction and Coriolis force, or Coriolis force alone.

Similarity can be considered as being graded from geometrical through kinematic to dynamic in the attempt to

reproduce the existing conditions in a scale model. A model has geometric similarity if the ratios of all homologous dimensions are equal. The model is said to have kinematic similarity if the paths and patterns of motion are geometrically similar to those of homologous occurrences in the prototype, and the ratios of homologous velocities are equal at all times. Dynamic similarity is achieved when the ratios of homologous masses and forces affecting motion are equal at all times. Complete dynamical similarity is difficult to achieve in fluid models and, kinematic similarity, of necessity, involves elements of dynamic similarity.

The general equation of motion can be written in the form:

$$\rho \frac{d\vec{V}}{dt} = -\rho 2\vec{\Omega} \times \vec{V} - \nabla p + \rho \vec{k}g + F$$

Where:

$$\rho \frac{d\vec{V}}{dt} = \text{inertial force}$$

$$\rho 2\vec{\Omega} \times \vec{V} = \text{coriolis force}$$

$$\nabla p = \text{pressure gradient force}$$

$$\rho \vec{k}g = \text{gravity force}$$

$$F = \text{friction force}$$

Each term of the equations of motion represents the forces present in a prototype and what is to be represented

in a model. Since the totality of forces cannot be easily reproduced in hydrodynamic models, a few important terms are usually singled out.

In scaling a model, each quantity and dimension of those particular terms of the equation of motion used to describe a flow must be reduced to the model scale. Dimensionless ratios of terms are used to achieve correct model scales. The numerical value of the dimensional ratio must be the same for the model as for the prototype for simiarity to prevail.

Several dimensionless ratios of terms are common to oceanographic modeling, and each one is used depending on the characteristics of the flow in the prototype. The Froude number is generally used in models of estuaries because it involve the ratio of inertial to gravity forces. These forces are, with friction, the dominant forces. The direction of flow is primarily down the gradient of pressure.

The Froude number is defined as:

$$Fr = \frac{\text{inertial term}}{\text{gravitational term}} = \frac{V_c}{(L\gamma/\rho)^{1/2}}$$

Where:

V_c = characteristic velocity

L = characteristic length

γ = specific weight

ρ = fluid density

As a preliminary step in scaling a phenomenon down to model size, it is useful to construct a ratio of units which by convention is:

$$R = \frac{A_m}{A_p}$$

where A_m is a number representing the dimensions of a certain property of the model and A_p the dimensions of the homologous property in the prototype.

The length ratio is fixed first in order to match the available space or equipment. The numerical value of each dimensionless group constant can be held altering the ratios of the other units included in a dimensionless group. By these procedures, time and other unit dimensions of other related properties may have to be altered to permit the fluid motion in the model to be regarded as behaving in the same physical manner as that in the prototype.

The ratio of inertial (velocity and length) and gravity is of concern for the Froude Number. Shallow-water gravity waves, such as tides, propagate at a speed $C = \sqrt{gh}$. The velocity ratio (R_c) is satisfied using the length ratio (R_L), where

$$R_c = \frac{C_m}{C_p} = \sqrt{\frac{g_m h_m}{g_p h_p}} = \sqrt{R_g R_h} = \sqrt{R_h}$$

which assumes that the gravity ratio (R_g) is one. Therefore, the length ratio and velocity ratio are left as adjustable parameters

$$R_c = \sqrt{R_h} = \frac{R_L}{R_t}$$

It can be seen from this equation that R_c shortens with increasing R_h and lengthens with increasing R_L .

A distinction between the vertical length (h) and the horizontal length (L) is often made. If the Froude model is geometrically similar to its prototype, $R_h = R_L$.

The vertical scale (R_h) generally must be chosen so that the least depth of water in which the flow is to be studied is approximately one cm. to prevent capillary effects from being important. Then, it may be necessary to depart from similarity by distorting vertical dimensions such that $R_h > R_L$. One is led to a choice of scales by a path which touches first the minimum depth requirement and then an adjustment of the R_L and R_t such that either one becomes constant, leaving the others to be adjusted.

The R_t (time ratio) is usually the most flexible parameter available and determines the frequencies of the simulated tides.

The effects of wind stress on the circulation in estuaries and bays are often important and sometimes dominate the tide. To scale it in a model requires more knowledge

of the dynamics of momentum transfer across the air-sea interface than is now available. Empirical procedures must be made to suffice.

For the U.S. Corps of Engineers hydraulic model, the following characteristics and scales were used:

Area: 280 sq. km.

Horizontal scale (R_L) = 1:500

Vertical scale (R_h) = 1:100

Velocity scale (R_c) = 1:10

Time scale (R_t) = 1:50

Discharge scale (R_{vd}) = 1:500 000

Volume scale (R_v) = 1:25 000 000

Physical dimensions = 35 x 40 meters

D. RESULTS OF THE HYDRAULIC MODEL

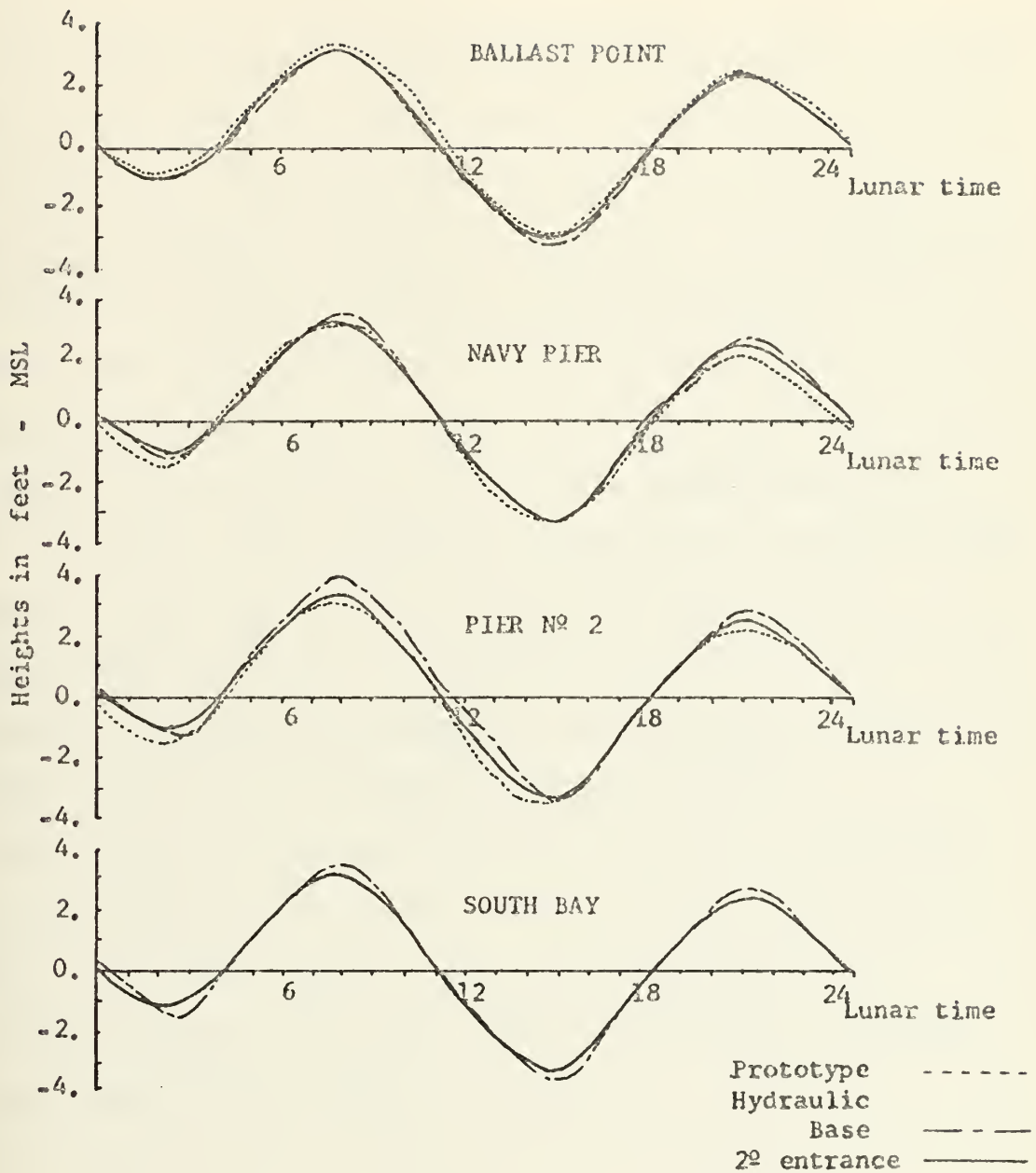
The type of flow being studied determines the predominant forces to consider for dynamic similarity. The San Diego Bay model used a Froude number scaling criteria. After determining the dynamic scaling, a hydraulic model is constructed to match the scaled geometry of the prototype. After reproducing the geometry as closely as possible, kinematic similarity must be obtained. This is accomplished by matching the hydraulic head and flow patterns at various locations in the model over the tidal cycle. This matching is generally accomplished by using roughness elements which can consist of concrete blocks or metal strips. The roughness elements have the effect of increasing turbulence and

changing mean flow patterns. This is a rather laborious and tedious procedure and usually is the most time consuming aspect of hydraulic model building. After the kinematic similarity is satisfactorily accomplished, the model is presumed to be calibrated.

Tests of existing conditions were made under carefully controlled conditions of tides, currents, and simulated pollution input [1]. The results of these calibration tests, called Base Tests, were used to evaluate the effects of navigation openings. Thus, any differences noted during the tests of the proposed second entrances were attributed to influences of the plan being tested and not to errors in the construction of the model.

The wind conditions on the day of observations can introduce large modifications to the normal surface and current characteristics in a bay such as San Diego Bay. Differences from day to day in the values of a mixed tide make a one-day observation a non-periodic function. Therefore, modifications of the field measurements were introduced in order to make them periodic and comparable to a non-wind situation.

The effects of the south entrance on tides throughout the bay are shown by comparative tide curves for measured, base and planned conditions in figure 2-1. The second entrance caused a reduction in the tide range at the southern



HEIGHTS IN THE PROTOTYPE AND IN THE HYDRAULIC MODEL

FIGURE 2-1

end of the bay by lowering high water and raising low water. At the south bay gage, the reduction in tide range was about 15 cm.

The effects of the second entrance on mid-depth current velocity are shown in figures 2 and 3. The opening reduced the maximum mid-depth current velocities at all stations on gauges "A" through "D" by 15 to 75 cm./sec. The flushing of the southern portion of the bay became governed by the new entrance and there seemed to be little interchange of water between the northern and southern portion of the bay with the area in the vicinity of Pier No. 2 gauge having very small currents. Under those new conditions, the entire bay appears to have two completely different circulation systems driven by tides at Zuniga Channel and at the second entrance. The flushing appears to be increased in the southern portion by including a second entrance.

The pictorial representations of the flow in the bay under both conditions [1] are shown in figures 29, 30, 36 and 37. In these figures, the flow is represented at different stages of the tide, and its intensity is scaled by the length of the lines.

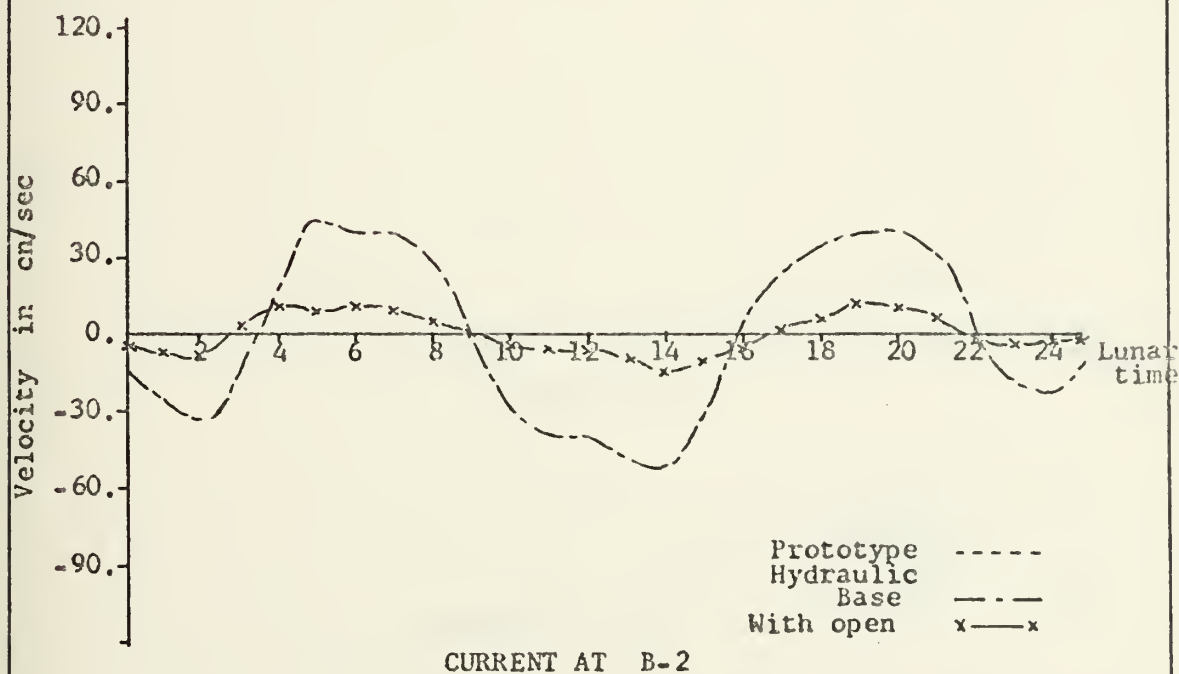
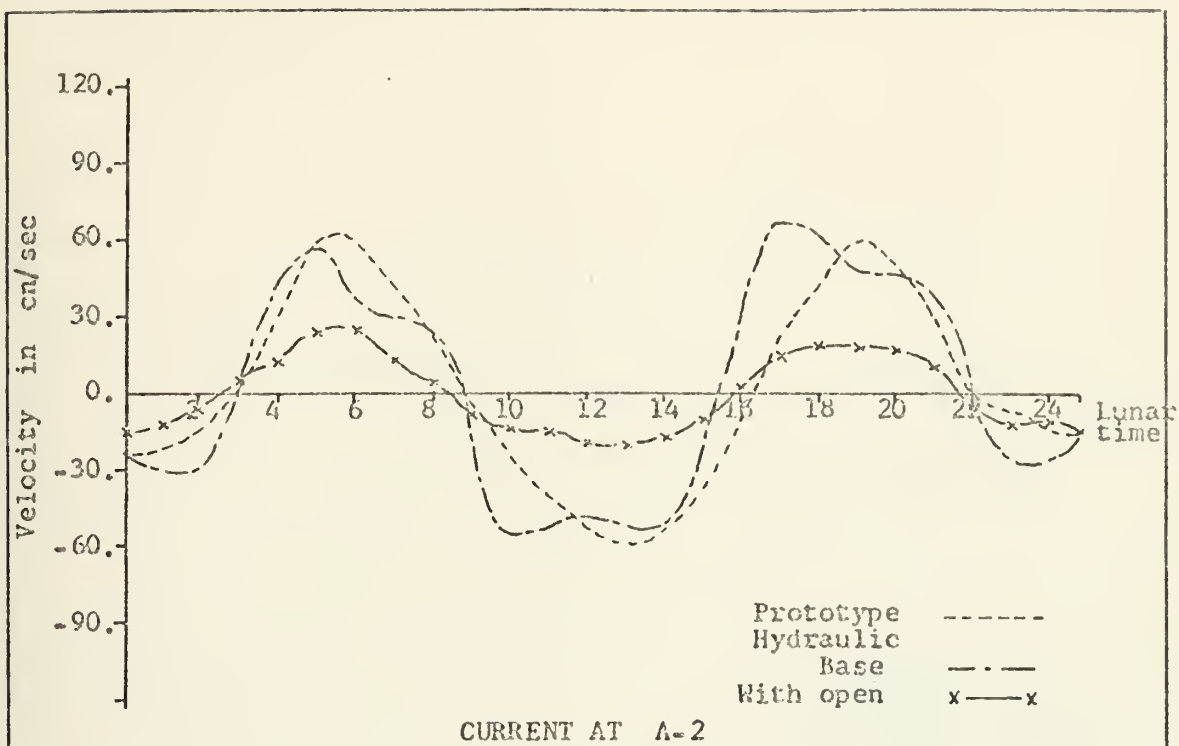


FIGURE 2

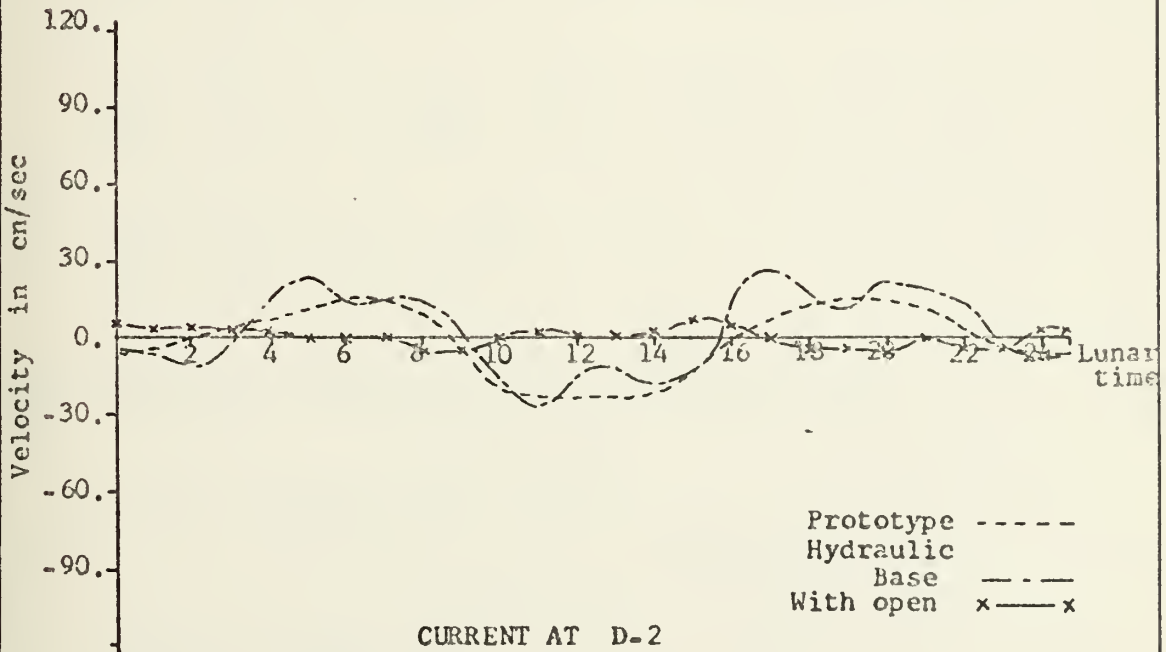
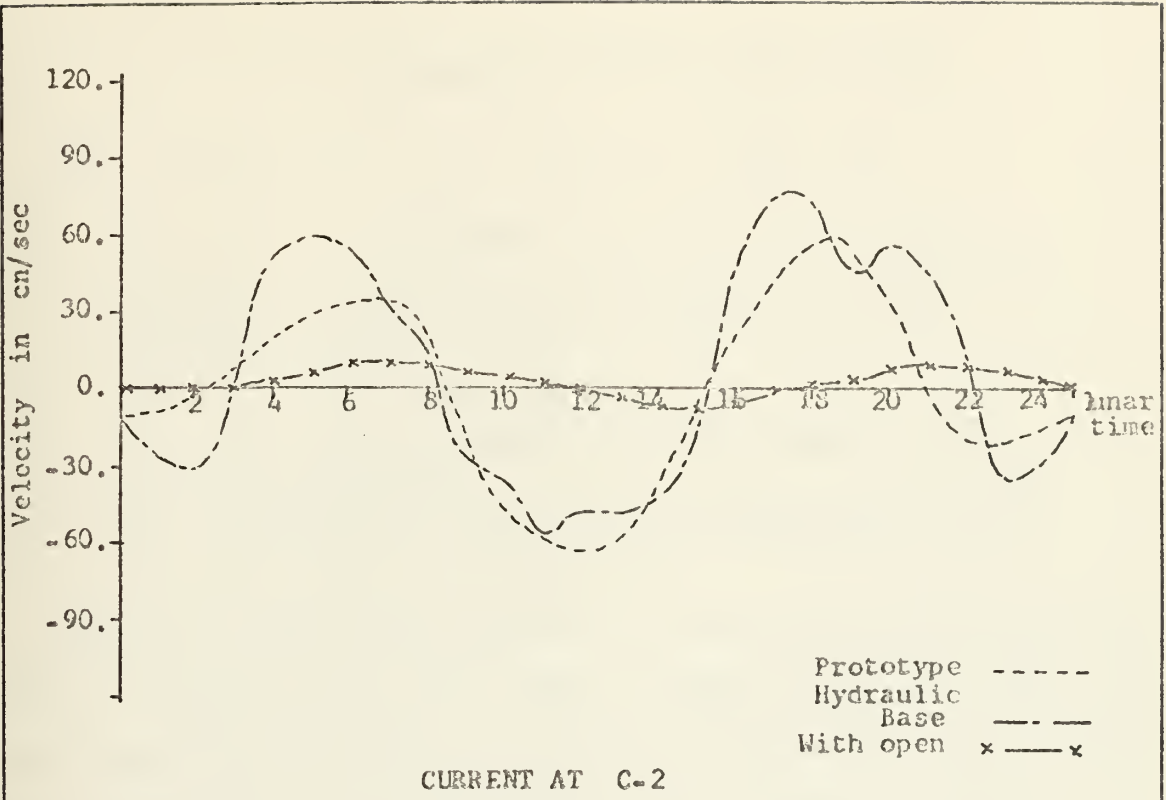


FIGURE 3

III. THE HANSEN HYDRODYNAMICAL MODEL

The assumptions of the numerical model are:

1. The fluid is homogeneous and incompressible.
2. Pressure is hydrostatic and thus, the changes in pressure are due solely to changes in water surface elevation.
3. Advection terms are ignored.
4. The fluid is in hydrostatic equilibrium in the vertical direction.
5. The geographical and vertical variations of the Coriolis force are neglected.

Applying these assumptions to the equations of conservation of momentum and mass, basic equations are obtained for the single-layer model developed by Hansen [6]. Horizontal momentum equations are integrated over depth to give

$$\frac{\partial u}{\partial t} - fv = -g \frac{\partial \eta}{\partial x} + Kv^2 u - \tau^b(x) + \tau(x)$$

$$\frac{\partial v}{\partial t} + fu = -g \frac{\partial \eta}{\partial y} + Kv^2 v - \tau^b(y) + \tau(y)$$

$$\frac{\partial \eta}{\partial t} + \frac{\partial}{\partial x} (Hu) + \frac{\partial}{\partial y} (Hv) = 0.$$

The wind stress components are represented by

$$\tau(x) = \frac{\lambda}{H} W_x \sqrt{W_x^2 + W_y^2},$$

$$\tau(y) = \frac{\lambda}{H} W_y \sqrt{W_x^2 + W_y^2}$$

and the bottom stress components are represented by

$$\tau^b(x) = \frac{r}{H} u \sqrt{u^2 + v^2} \quad \text{and}$$

$$\tau^b(y) = \frac{r}{H} v \sqrt{u^2 + v^2} .$$

The various terms of the equations are defined as:

K = coefficient of horizontal kinematic eddy viscosity

λ = drag coefficient

$W(\)$ = wind speed component

η = surface elevation

H = total depth = $h + \eta$

x, y = space coordinates

u, v = velocity components

g = acceleration of gravity

f = coriolis parameter

$$\nabla = \frac{\partial}{\partial x} + \frac{\partial}{\partial y}$$

Both the wind stress and bottom stress equations are empirically developed. The wind stress terms, as used in the model, are assumed to be a quadratic expression in wind speed, where λ is the wind drag coefficient with a typical value of 0.65. The bottom stress is assumed to be non-linearly dependent on u and v , and its formulation, like the wind stress, have been derived by empirical means. It was originally formulated for shallow water application. Over deep water, its value becomes small and its applicability is questionable.

An implicit central difference scheme is used for achieving time dependent solutions of the equations. At the boundaries, the values of η , u and v are taken at the actual points rather than from the surrounding points as shown in Figure 4.

The driving forces are tides input at the open boundaries, and wind at the surface over the entire grid. The tide values are computed at each time step and introduced as new values of η at each point of the boundaries.

The finite approximations are given below. The water surface elevations are first calculated using the conservation of mass equation.

$$\begin{aligned} \eta^{t+\frac{\Delta t}{2}}(n,m) &= \eta^{t-\frac{\Delta t}{2}}(n,m) - \frac{\Delta t}{\Delta \rho} \{ H_u^t(n,m) U^t(n,m) \\ &\quad - H_u^t(n,m-1) U^t(n,m-1) + H_v^t(n-1,m) V^t(n-1,m) \\ &\quad - H_v^t(n,m) V^t(n,m) \} \end{aligned}$$

The horizontal and vertical velocity components are then determined from respective horizontal and vertical momentum equations.

$$\begin{aligned}
 U^{t+\Delta t}(n,m) &= \{1 - [\Delta t \ r/Hu^{t+\Delta t}(n,m)]\sqrt{\bar{U}^t(n,m)^2 + V^{*t}(n,m)}\}\bar{U}^t(n,m) \\
 &+ \Delta t \ f \ V^{*t}(n,m) - \frac{\Delta t/2g}{\Delta z} \{n^{t+\frac{\Delta t}{2}}(n,m+1) \\
 &- n^{t+\frac{\Delta t}{2}}(n,m)\} + \Delta t \ X^{t+\Delta t}(n,m)
 \end{aligned}$$

$$\begin{aligned}
 V^{t+\Delta t}(n,m) &= \{1 - [\Delta t \ r/Hv^{t+\frac{\Delta t}{2}}(n,m)]\sqrt{\bar{V}^t(n,m)^2 + U^{(t)}(n,m)}\}\bar{V}^t(n,m) \\
 &- \Delta t \ f \ U^{*t}(n,m) - \frac{\Delta t/2g}{\Delta z} \{n^{t+\frac{\Delta t}{2}}(n,m) \\
 &- n^{t+\frac{\Delta t}{2}}(n+1,m)\} + \Delta t \ Y^{t+\Delta t}(n,m)
 \end{aligned}$$

where

$$\bar{U}^t(n,m) = \alpha U^t(n,m) + \frac{1-\alpha}{4} \{U^t(n-1,m) + U^t(n+1,m) + U^t(n,m+1) + U^t(n,m-1)\},$$

$$\bar{V}^t(n,m) = \alpha V^t(n,m) + \frac{1-\alpha}{4} \{V^t(n-1,m) + V^t(n+1,m) + V^t(n,m+1) + V^t(n,m-1)\},$$

$$U^{*t}(n,m) = \frac{1}{4} \{U^t(n,m-1) + U^t(n+1,m-1) + U^t(n,m) + U^t(n+1,m)\}, \text{ and}$$

$$V^{*t}(n,m) = \frac{1}{4} \{V^t(n,m-1) + V^t(n+1,m-1) + V^t(n,m) + V^t(n+1,m)\}.$$

The factor α can be interpreted as related to the horizontal kinematic viscosity parameter. In the program it is treated as a tuning parameter and is related to the eddy viscosity coefficient by:

$$\frac{K\Delta t}{\Delta l^2} = \frac{1-\alpha}{4} = \frac{\beta}{4}$$

The total depth of water is calculated by:

$$Hu^{t+\Delta t}(n,m) = hu(n,m) + \frac{1}{2} \{u^{t+\frac{\Delta t}{2}}(n,m) + u^{t+\frac{\Delta t}{2}}(n,m+1)\}$$

$$Hv^{t+\Delta t}(n,m) = hv(n,m) + \frac{1}{2} \{v^{t+\frac{\Delta t}{2}}(n,m) + v^{t+\frac{\Delta t}{2}}(n,m+1)\}$$

The effects of wind are computed by:

$$X^t = \frac{\lambda W_x^t \sqrt{(W_x^t)^2 + (W_y^t)^2}}{H} - \frac{1}{\rho} \frac{\partial P_o}{\partial x} \quad \text{and}$$

$$Y^t = \frac{\lambda W_y^t \sqrt{(W_x^t)^2 + (W_y^t)^2}}{H} - \frac{1}{\rho} \frac{\partial P_o}{\partial y} .$$

where P_o is the barometric pressure. Its gradient is assumed to be zero for small areas and normal conditions.

The stability of the model is governed by the Courant-Friedrichs-Levy criterion which says that the maximum length of the time step is determined by the grid size and maximum depth in the area,

$$\Delta t \leq \frac{\ell}{\sqrt{2gH_{\max}}} .$$

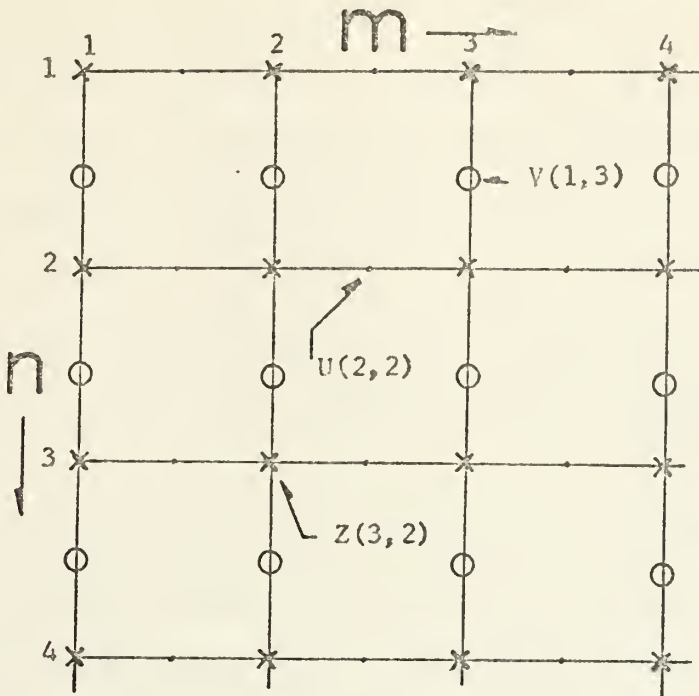
For this particular grid, a Δt (half-time step) of 5 seconds was adopted.

If the computational area contains small sections of greater depths [4], a "false bottom" can sometimes be assumed in these areas. (E.g., areas deeper than 500 meters can be assumed to be 500 meters deep.) This will often result in a considerable increase in the time step, or a decrease of the grid length if total computation time is a critical factor. Experiments have shown that the error introduced with the above procedure is acceptable in some cases for practical applications of the model.

The grid net consists of three different sets of grid points shown in Figure 4-a; the water elevation (z), the u -velocity component and the v -velocity component. Each of these three points have the same coordinate designation (n,m). The coastline must pass through u and v points and not through z points and the values of depths at any of these particular points are read in the program as HTU and HTV.

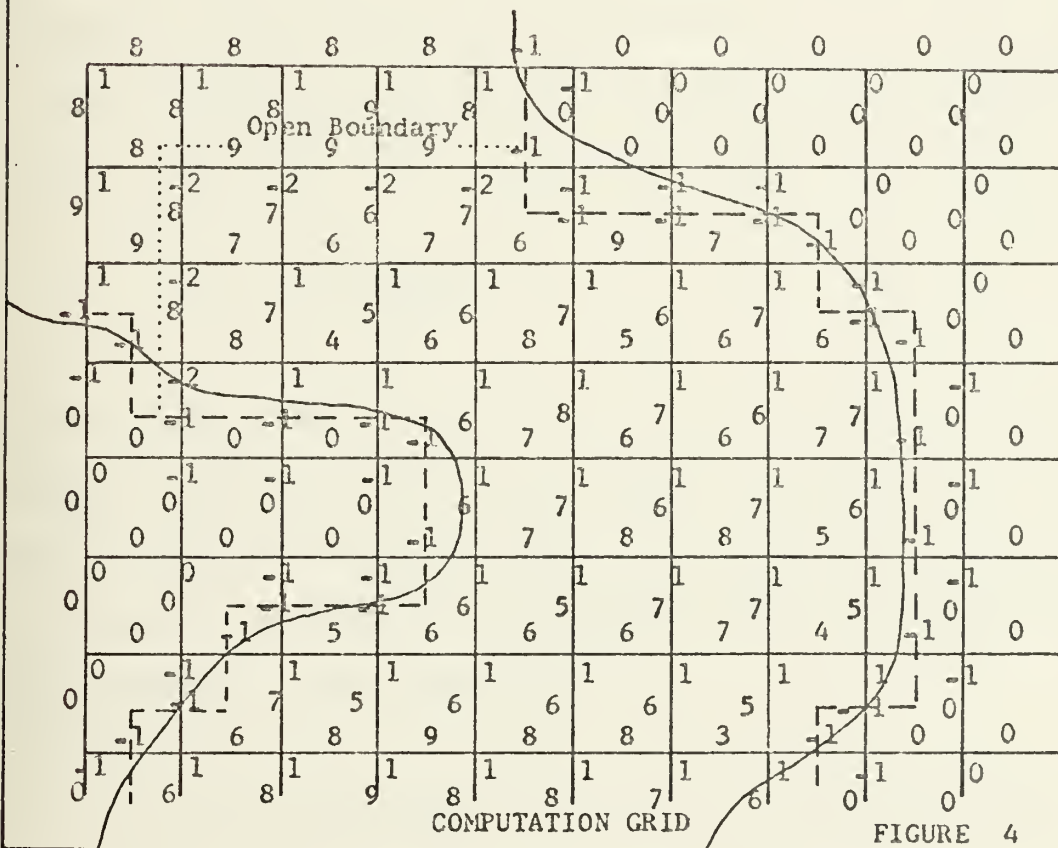
The HTZ points act as water-coast-land designators having values of 1, -1, and 0 respectively. The HTU and HTV show the depth values (in cm.), the coastline as -1, and land as 0, depending on their location in the grid [Figure 4-b].

At the input open boundaries, HTZ points have values of -2 (and -3) for the first and second open boundaries (if applicable). Outside of the input boundaries, values of zero for HTZ are prescribed.



x Z-points • U-points ○ V-points

SCHEME OF THE GRID NET



The coefficient of horizontal kinematic eddy viscosity is interpreted as related to the values of the u and v current components. Hansen states that the computations are always stable for values of Beta (1- α) larger than zero and the normal value used is 0.01. However, this coefficient can also be used as a tuning factor. If a higher value is used, the current speed is generally decreased.

In areas where the depth distribution is irregular, accelerations and surface irregularities appear in the model. This abnormality can be solved by means of a proper smoothing of the bottom or the sea surface. This is accomplished in this model by the smoothing of the sea surface elevation which is a numerical artifact of the model. This is done to insure numerical convergence.

The coefficient of horizontal kinematic eddy viscosity in the finite solution, is represented by the relation

$$K = \frac{\Delta l^2(1-\alpha)}{4\Delta t}$$

For the values of Δl (100 m), Δt (5 sec.) of this specific model, and alpha (0.992) recommended by Laevastu for estuaries (personal communication), K becomes 0.9×10^5 cm²/sec.

Bowden [2] suggests for estuaries with a tidal current amplitude of V and a depth of h,

$$K = 0.15 Vh$$

This relation gives a value of $K = 0.25 \times 10^5 \text{ cm}^2/\text{sec.}$ for the northern portion of San Diego Bay. This corresponds to an α value of 0.995. For the southern part, this equation gives a value of $K = 0.3 \times 10^4$ with a corresponding value of $\alpha = 0.999$.

The use of these high values for α must be done with caution because the low smoothing can allow undesirable oscillations in the model. If a too low value of α is used in order to obtain good smoothing, the resolution of current could be affected.

As was pointed out in the assumptions of the Hansen Model, the advection terms, $u_j \frac{\partial u_i}{\partial x_j}$ have been neglected. If a value of 50 cm/sec. (about one knot) is assumed for both u_j and u_i , and if the distance between grid points is 200 m, then, the advection terms are of the order of 10^{-2} cm/sec. A representative value of the local velocity change $\frac{\partial u_i}{\partial t}$, is calculated using a Δt of a quarter tidal cycle of 3 hours during which time the velocity changes from a maximum represented by 50 cm/sec. to zero. This term then is of the same order of magnitude as the advection terms. The coefficient of horizontal eddy viscosity (K) is deduced from the horizontal advection terms; then, in the model, what is partially done by the tuning process is accounted in K for the values of the neglected advection terms.

A. SELECTION OF THE GRID

The selection of the grid size is usually based on requirements of details and accuracy, and availability

of computer core memory and time. For open areas and round shaped smooth bays, where the expected velocities and direction fields are smooth, it is not necessary to use a fine mesh. In areas where topography is of primary importance a fine mesh is necessary for reliable results.

The flow in San Diego Bay is governed by the topography of the area; therefore, a small grid size must be introduced. To cover the entire area, a large array would be necessary which would require a large amount of core and computation time.

On the other hand, due to deficiencies in the boundary conditions of the model, inaccuracies of the computations are found near land grid points; therefore, if acceptable results are desirable in narrow channels, the grid must provide enough grid points across these areas.

A small grid of 100 x 100 array was laid over San Diego Bay. Because of the difficulty of handling by the computer, the area was divided in two regions with sufficient overlap to insure proper calibration.

The way the boundary conditions are set at the open boundaries produce errors which propagate throughout the adjacent grid points; therefore, the overlap area must be of considerable size in order that the match section be distant enough from both open boundaries that these influences are negligible. For this specific model, a long

and narrow portion of the bay in front of Coronado was chosen, assuming that in this area flow is parallel to the coastline and free of big eddies.

This division gives two grids: a northern grid of 53 x 30 designated as grid (1), and a second southern grid of 58 x 40 and designated as grid (2) [Figure 1].

The second portion of the bay was run under two different conditions: first under existing conditions (model (2)) and, secondly, with a second open boundary at Crown Cove (model (3)). The division of the bay into two different models will not allow for computation of velocity at the northern entrance for the case of the model (3), but it will give a good indication of what the future conditions will be in the northern channel as the point C-2 (see Fig. 1) will be computed in the second and third models.

B. TIDE INPUT IN THE MODEL (1)

In the northern model referred to as model (1) (the one with two open boundaries), tidal values at both openings was first introduced. The time inaccuracies of the prototype measurements forced water in and out of the bay at the two ends simultaneously. This procedure causes a non-equilibrium state in the bay with corresponding erroneous answers.

A new procedure was tried by leaving the second boundary open without a driving force, letting the water flow in and out according to the propagation of the tidal wave

from the first boundary. Continuation of the surface of the water and currents for each point in the free open boundary was prescribed to insure the flow of water throughout this end. For the values of height, this continuation was obtained by leveling the edges using the concept of a "lubricated wall",

$$Z(\text{NEH},M) = Z(\text{NEH}-1,M)$$

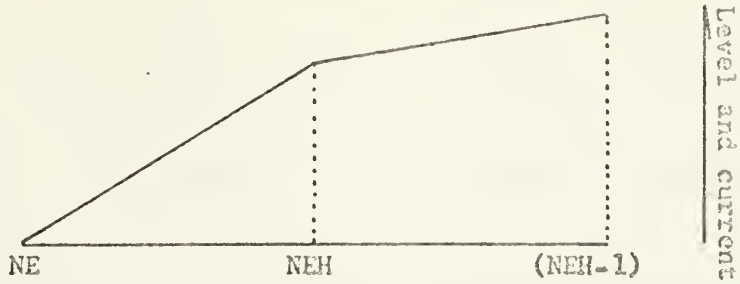
Attempts to continue the surface slope resulted in disturbances being generated in the model,

$$Z(\text{NEH},M) = Z(\text{NEH}-1,M) + [Z(\text{NEH}-1,M) - Z(\text{NEH}-2,M)].$$

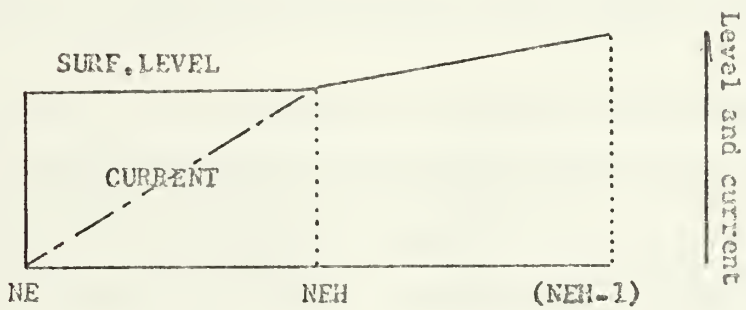
Leveling the edges and letting the model compute the values of currents itself resulted in too severe a decay of the values of velocity at the second boundary; this resulted in no flow through the free open boundary.

To obtain the correct flow of water throughout the free open boundary, a continuation of current (u and v) was prescribed with the assumption that calibration of the model could be obtained modifying the values of this slope by means of applying a smoothing constant (J) to its value [Figure 5],

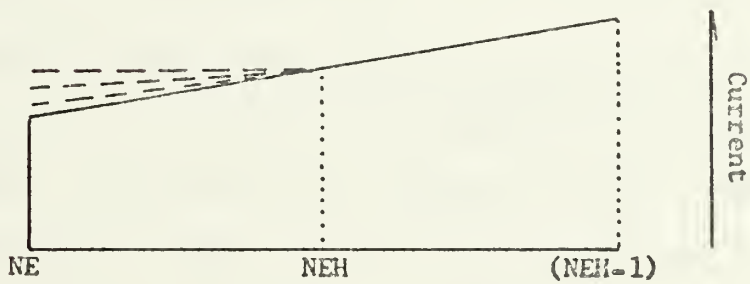
$$V(\text{NEH},M) = V(\text{NEH}-1,M) + J[V(\text{NEH}-1,M) - V(\text{NEH}-2,M)].$$



INPUT BOUNDARY AND FREE BOUNDARY WITHOUT CONTINUATION



LEVELING OF THE EDGES (LUBRICATED WALL) AT BOUNDARIES



CONTINUATION OF CURRENT AT THE FREE OPEN BOUNDARY
WITH THE GRADIENT CORRECTED
BY A CONSTANT

FIGURE 5

Variations of the values of the currents in the entire model were obtained, but great disturbances in the water surface were introduced up to a point that back-flux was obtained. Figures 6 and 7 show different results obtained for different values of J in the continuation of current used at the free open boundary.

These disturbances in the surface can be reduced by applying an inverse correction to the slope of the surface at the edge

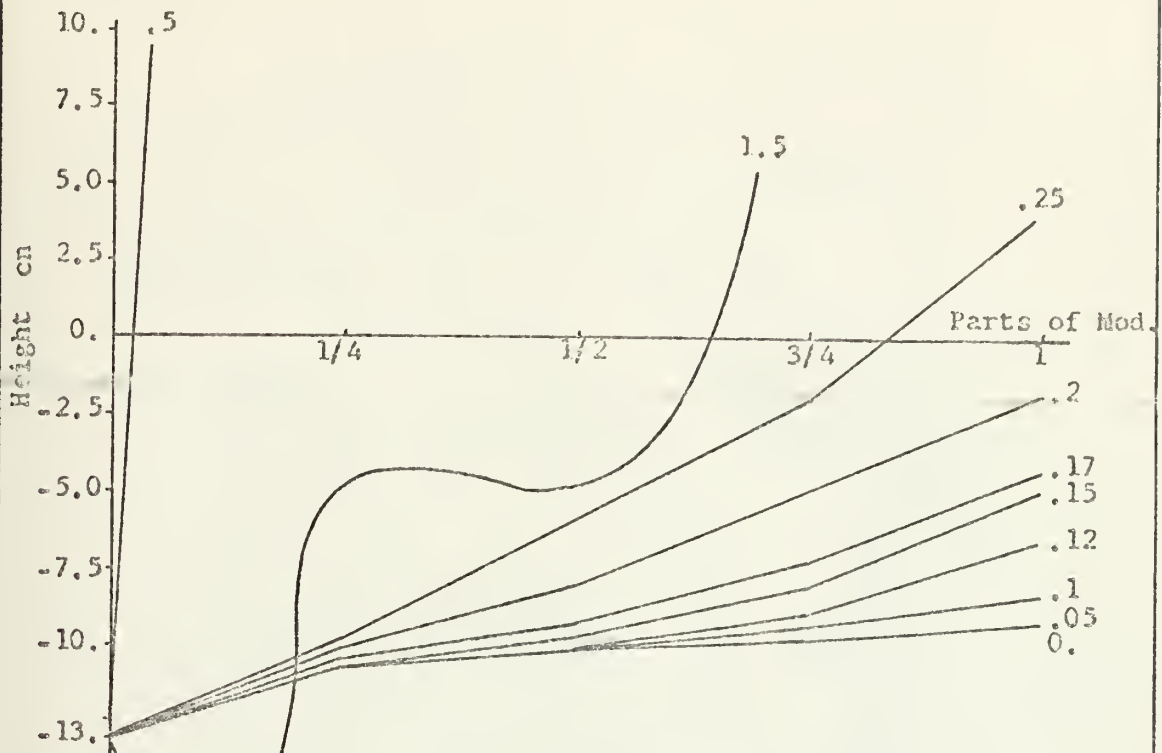
$$Z(\text{NEH},M) = Z(\text{NEH}-1,M) - C(Z(\text{NEH}-1,M) - Z(\text{NEH}-2,M)).$$

No further calibration was attempted because this procedure is not realistic, but a proper calibration may give a good result with savings in computation time.

Because no satisfactory answer was obtained from a free open boundary, the idea was abandoned and the addition of an appended pseudo-bay was tried.

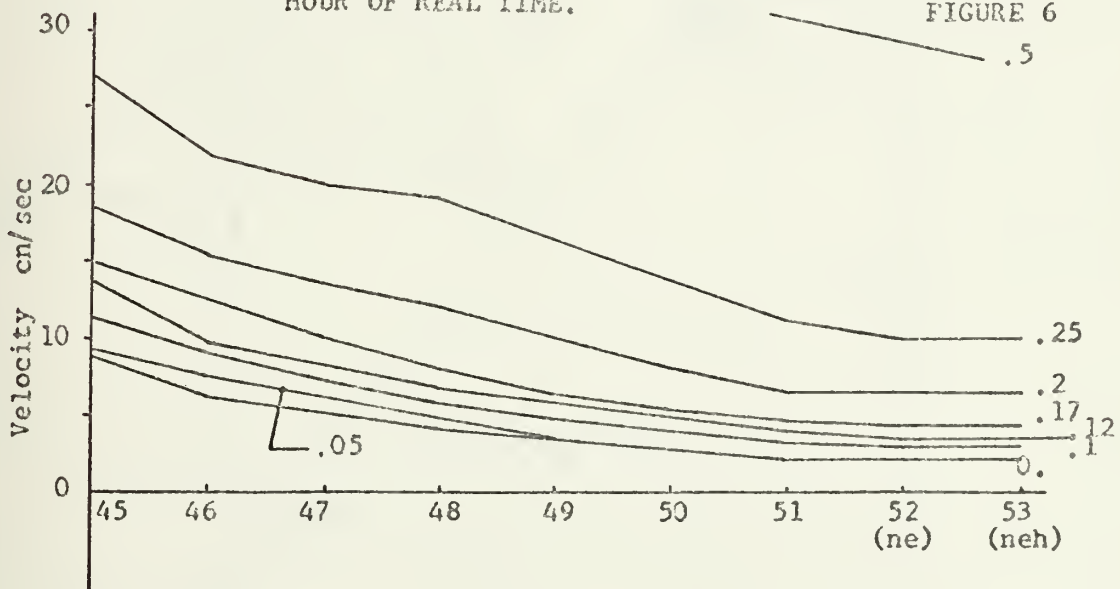
C. ADDITION OF AN APPENDED PSEUDO-BAY

The addition of an appended area at the end of the model (1) creates an additional tidal prism which will force the volume of water passing throughout the first model to increase. This new area, Figures 8 and 9, was obtained by filling the empty spaces of the grid and connecting them to the end of the model. This procedure does not increase the core in the program, but increases the time of computation by about 30% for this specific case.



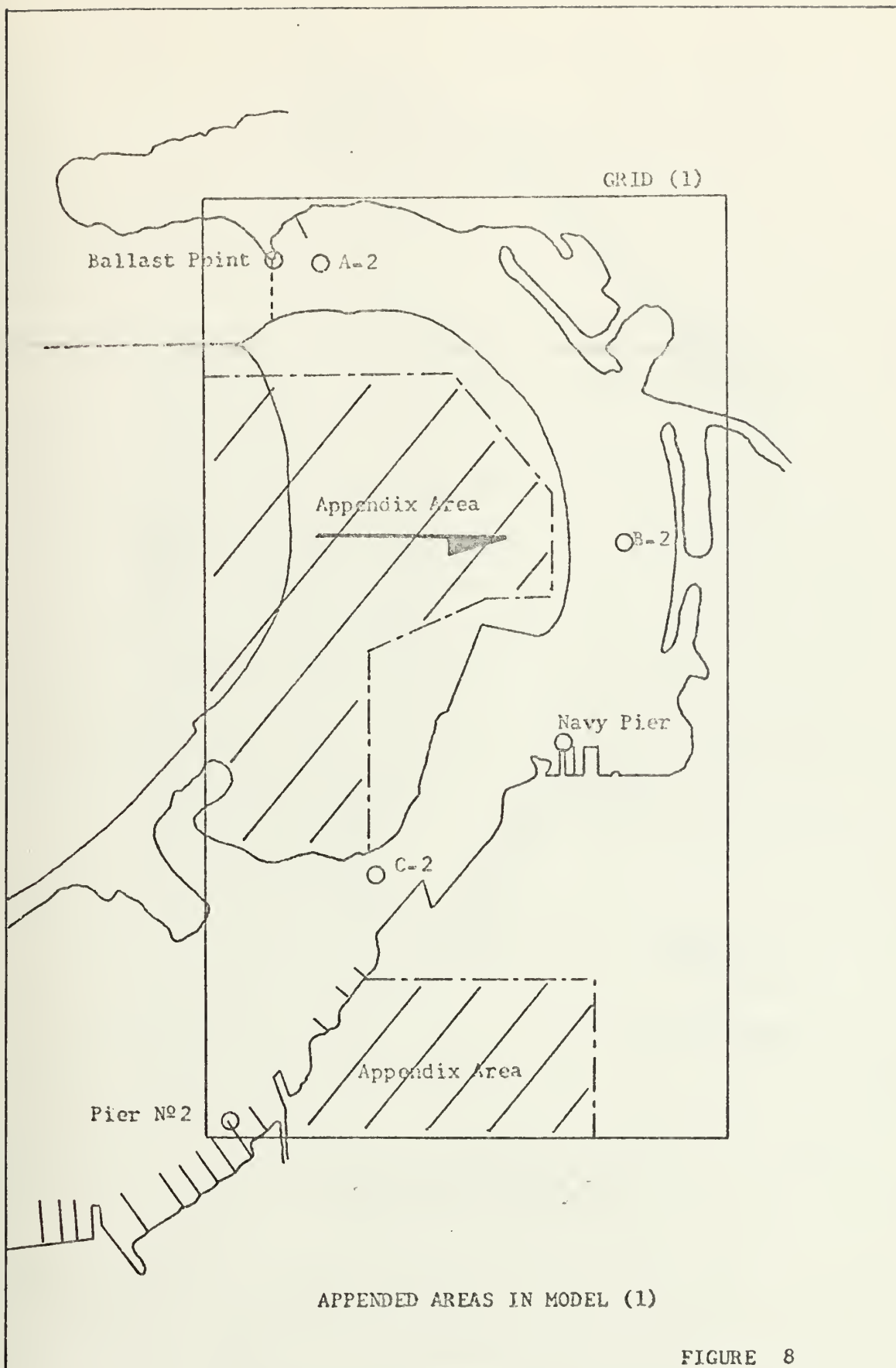
VALUES OF Z ALONG THE MODEL (1) FOR DIFFERENT CONSTANTS IN THE CONTINUATION OF THE FREE BOUNDARY AFTER 1 HOUR OF REAL TIME.

FIGURE 6



VALUES OF VELOCITY AT $N=3$ AND $N=45$ to 53 IN THE FREE OPEN BOUNDARY FOR DIFFERENT CONSTANTS IN THE CONTINUATION AFTER 1 HOUR OF REAL TIME.

FIGURE 7



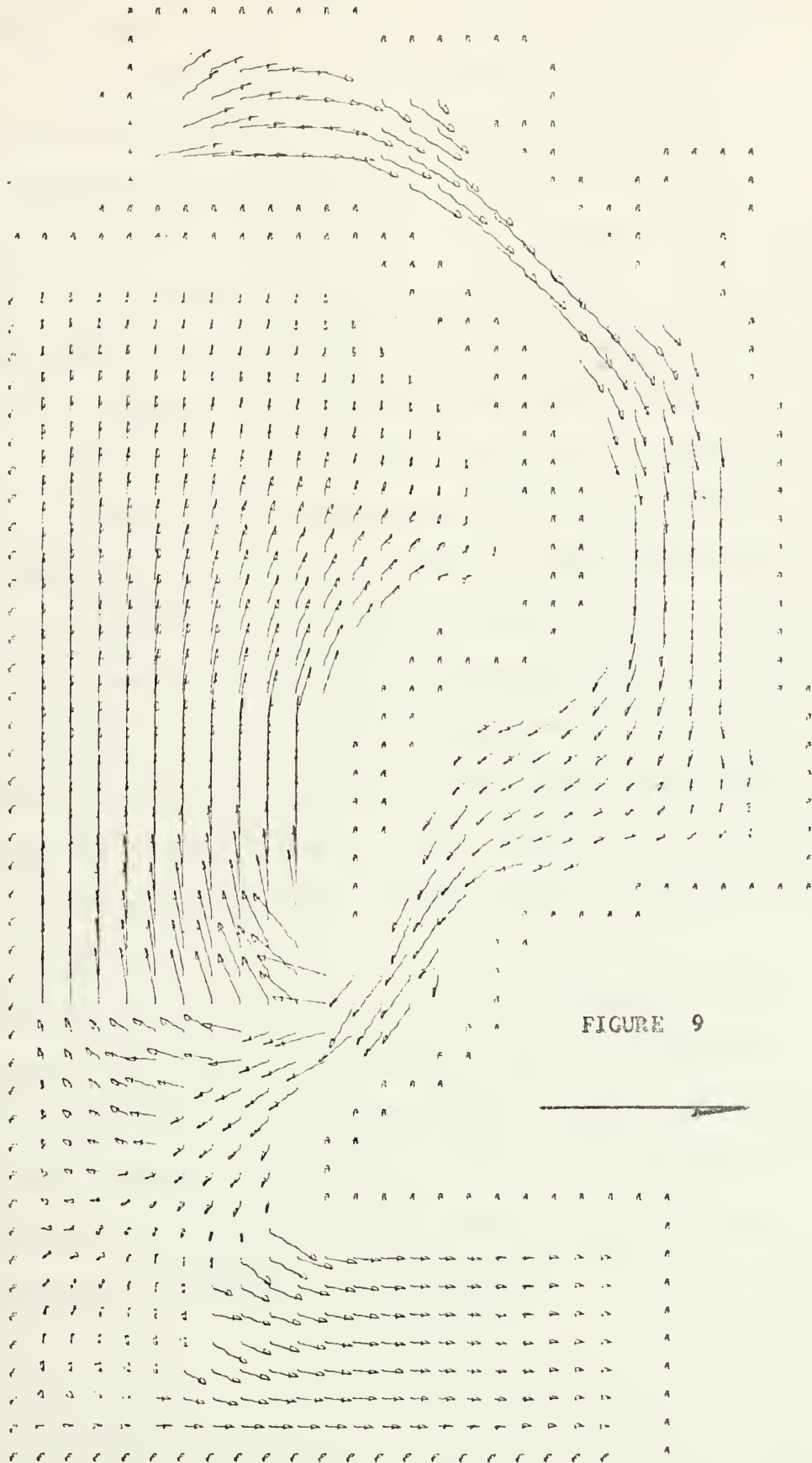


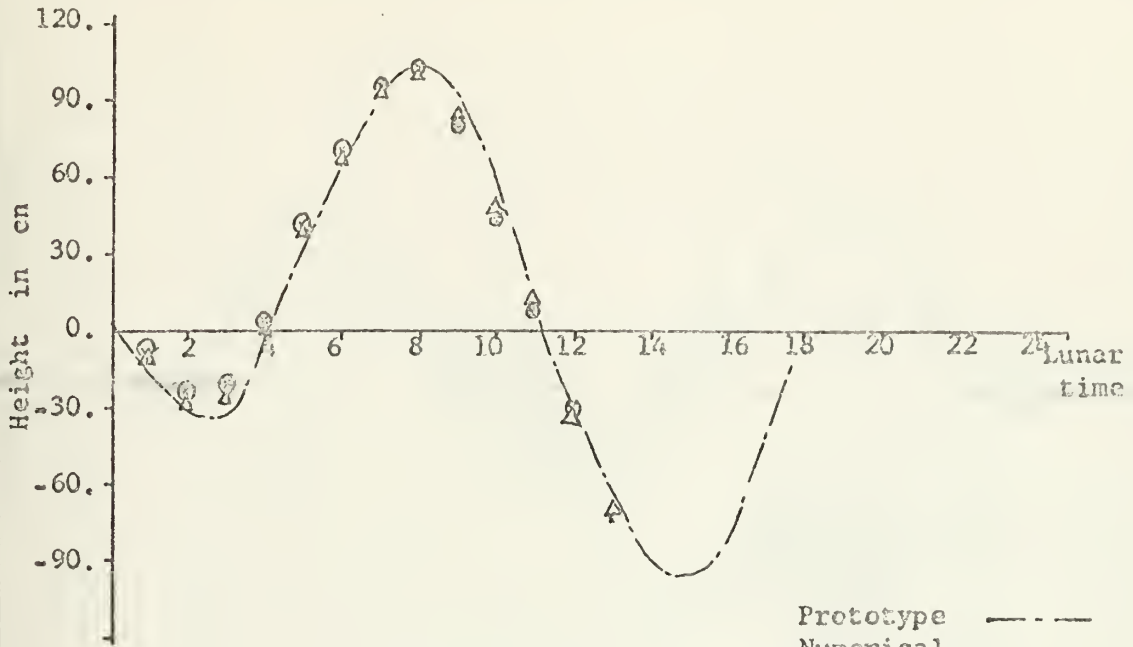
FIGURE 9

CIRCULATION IN MODEL (1) WITH APPENDED AREAS

Areas corresponding to 82% and 100% of the remaining area of the bay were tried. The results, Figures 10, 11, and 12 show an increase of water transport and current values with no appreciable modifications to the values of the water surface. The increase in volume transport and currents were proportional to the increased areas. The values of height remain stable for the different cases.

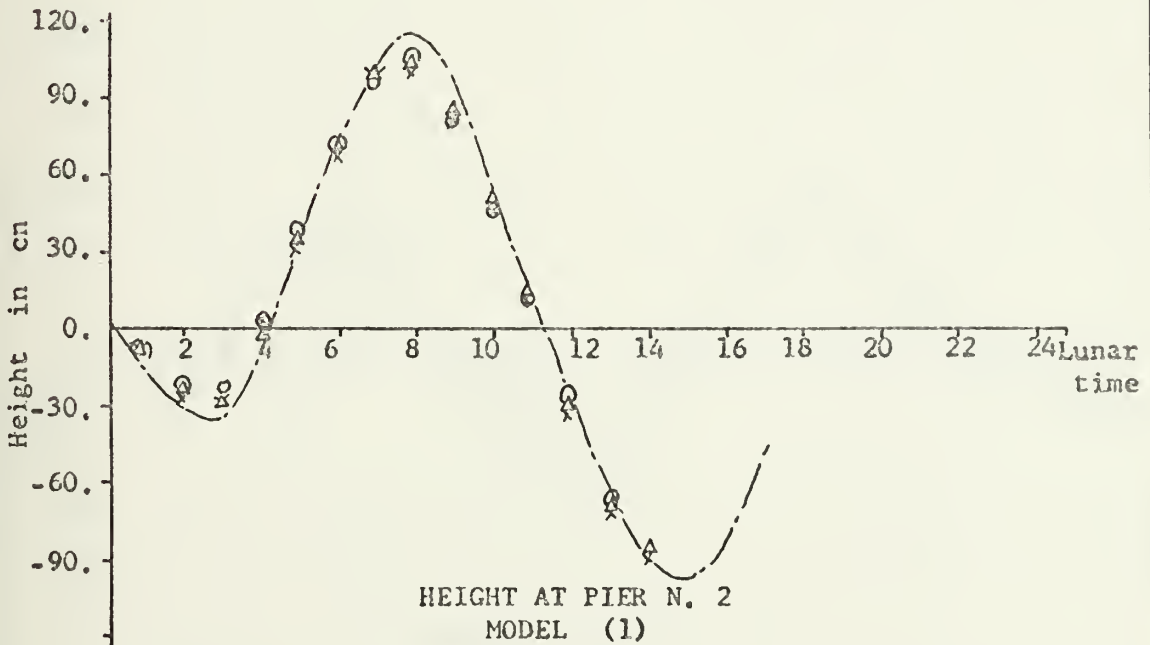
Different values of R (0.003, 0.0028 and 0.002) were applied to the model. The results show that the model is not very sensitive to the variations of this parameter. After comparing the results obtained at the points A-2, B-2 and C-2 for each of the values of R , 0.003 was adopted because it seemed to better fit the measurements at these points in the prototype. The discrepancies at A-2 were attributed to the inaccuracies of the Hansen numerical model near the open boundaries. The results of the model (1) in current, water height and net volume transport are shown in figs. 13, 14, 15.

A pictorial description of the flow throughout the entire model (1), with the appended areas, is shown in Figure 9. The real part of this model and the times of 0., 3., and 9 hours are shown in Figures 16, 17 and 18. The direction of the flow is indicated by the arrows, and its magnitude is scaled by the length.



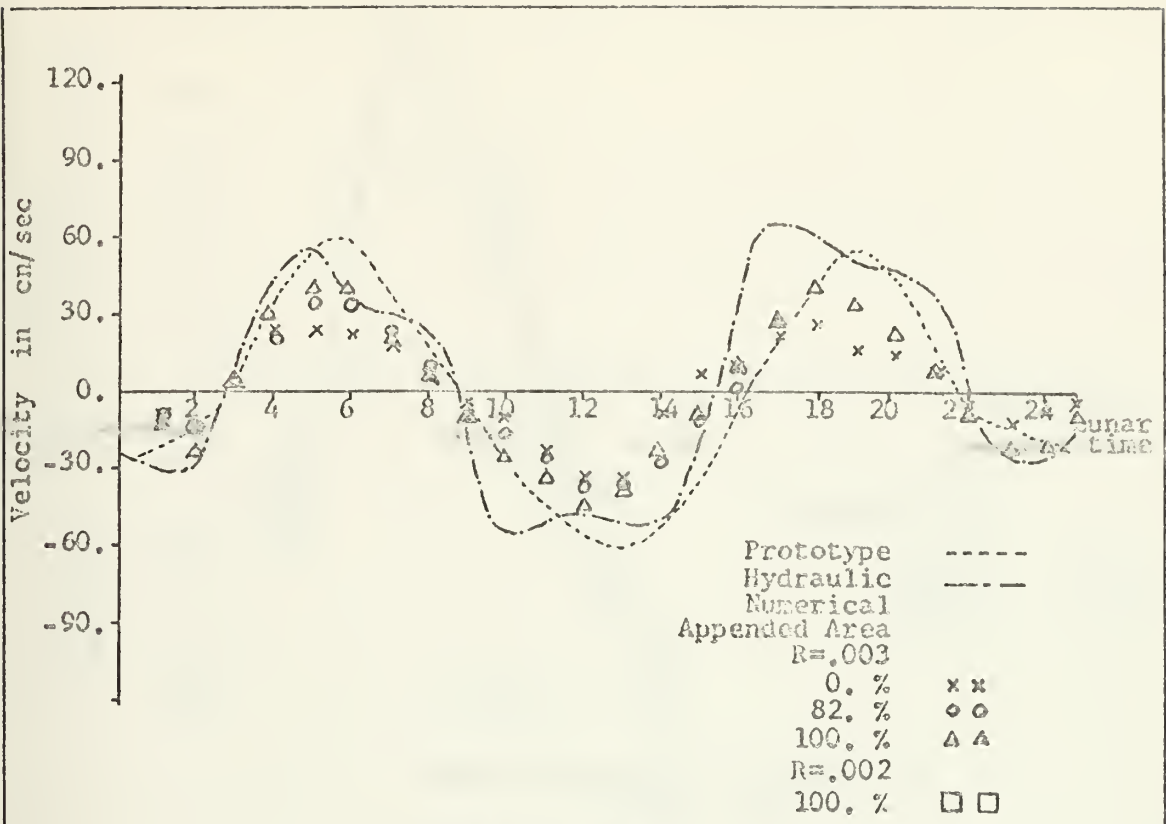
HEIGHT AT NAVY PIER
MODEL (1)

Prototype	---
Numerical	
Appended Area	
R=.003	
0. %	o o
82. %	Δ Δ
100. %	x x

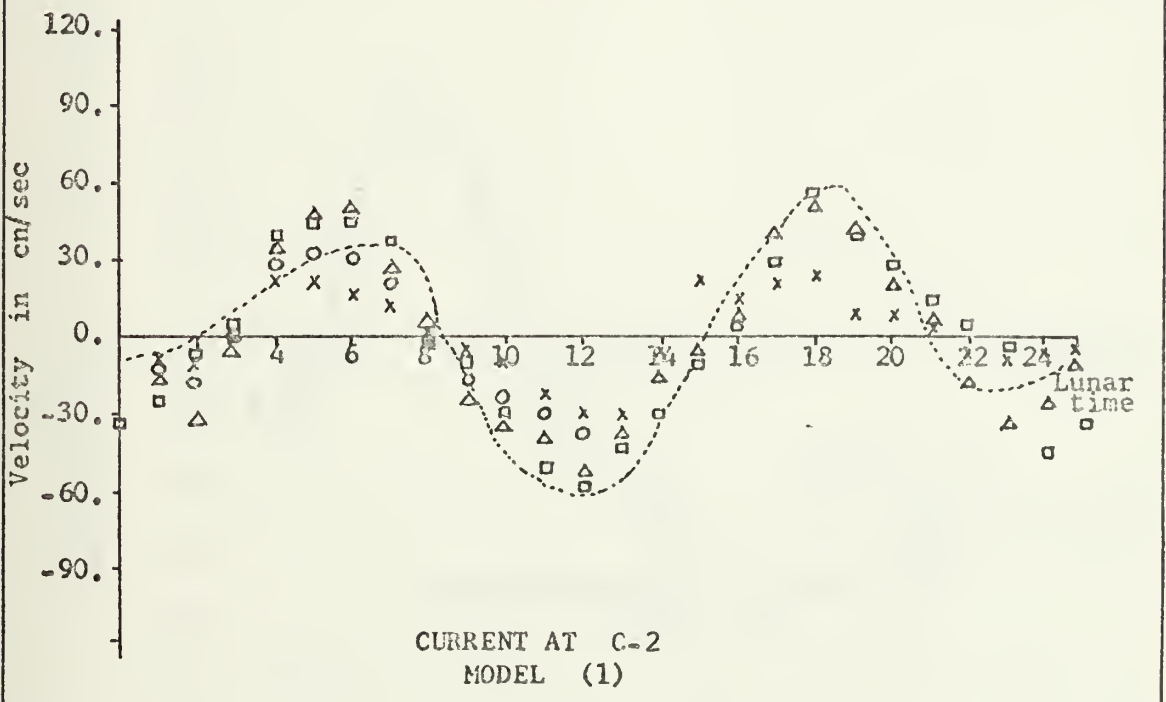


HEIGHT AT PIER N. 2
MODEL (1)

FIGURE 10



CURRENT AT A-2
MODEL (1)



CURRENT AT C-2
MODEL (1)

FIGURE 11

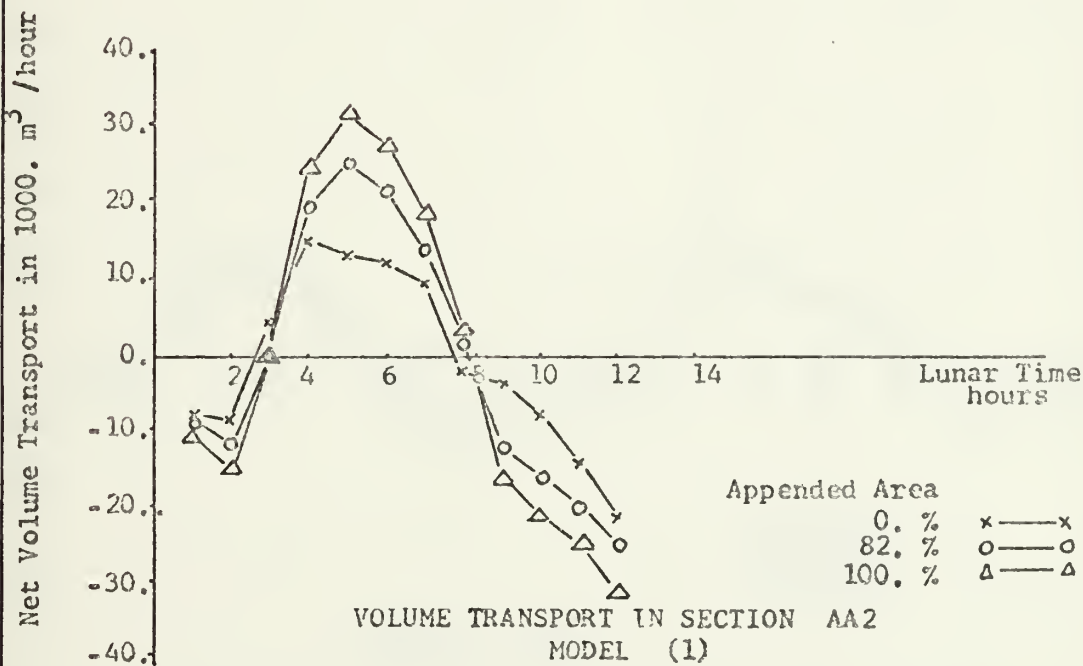
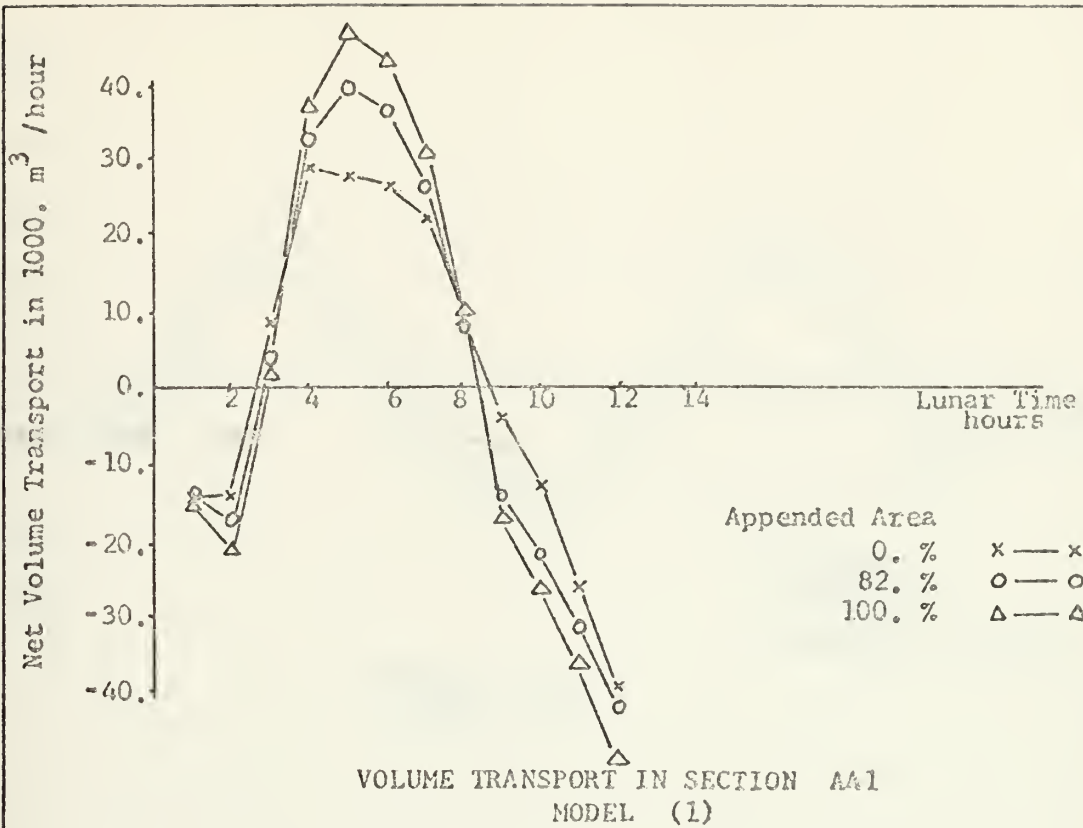


FIGURE 12

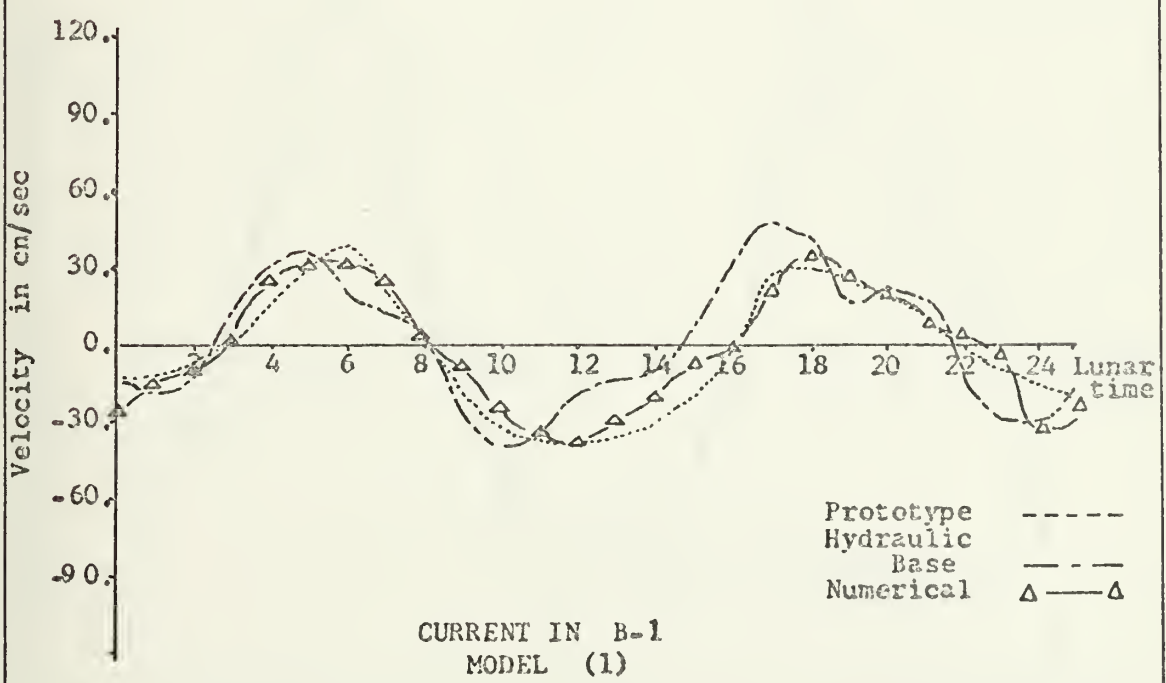
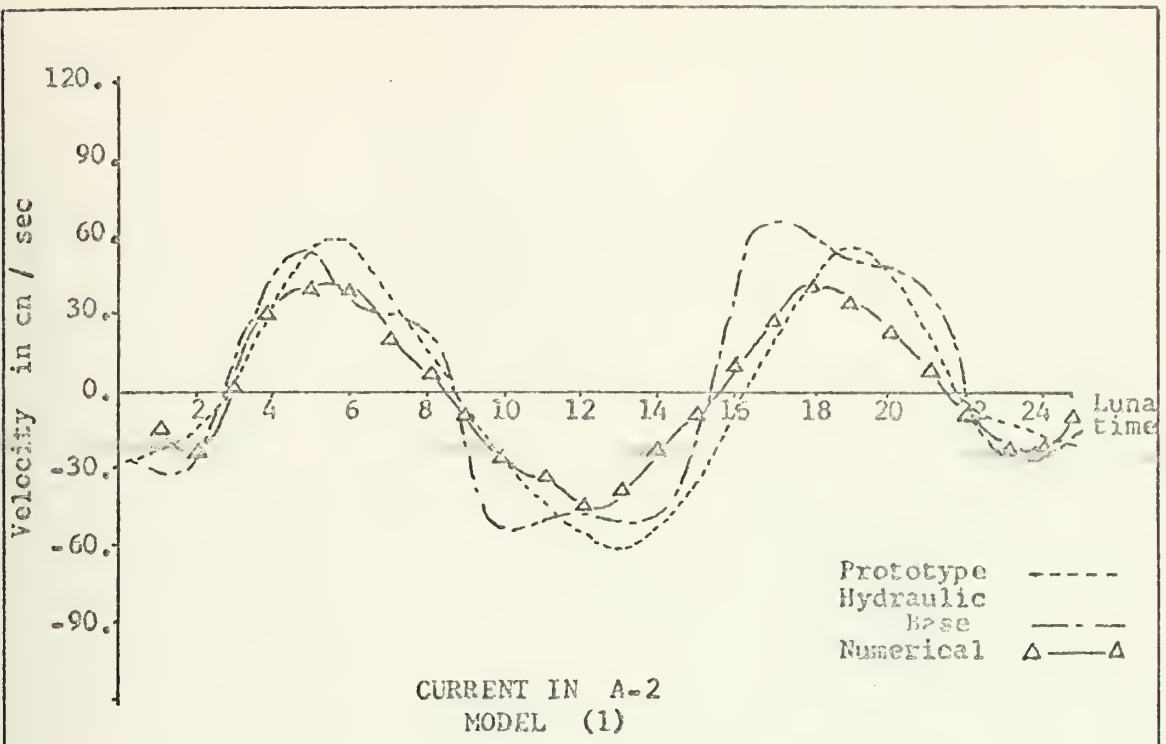


FIGURE 13

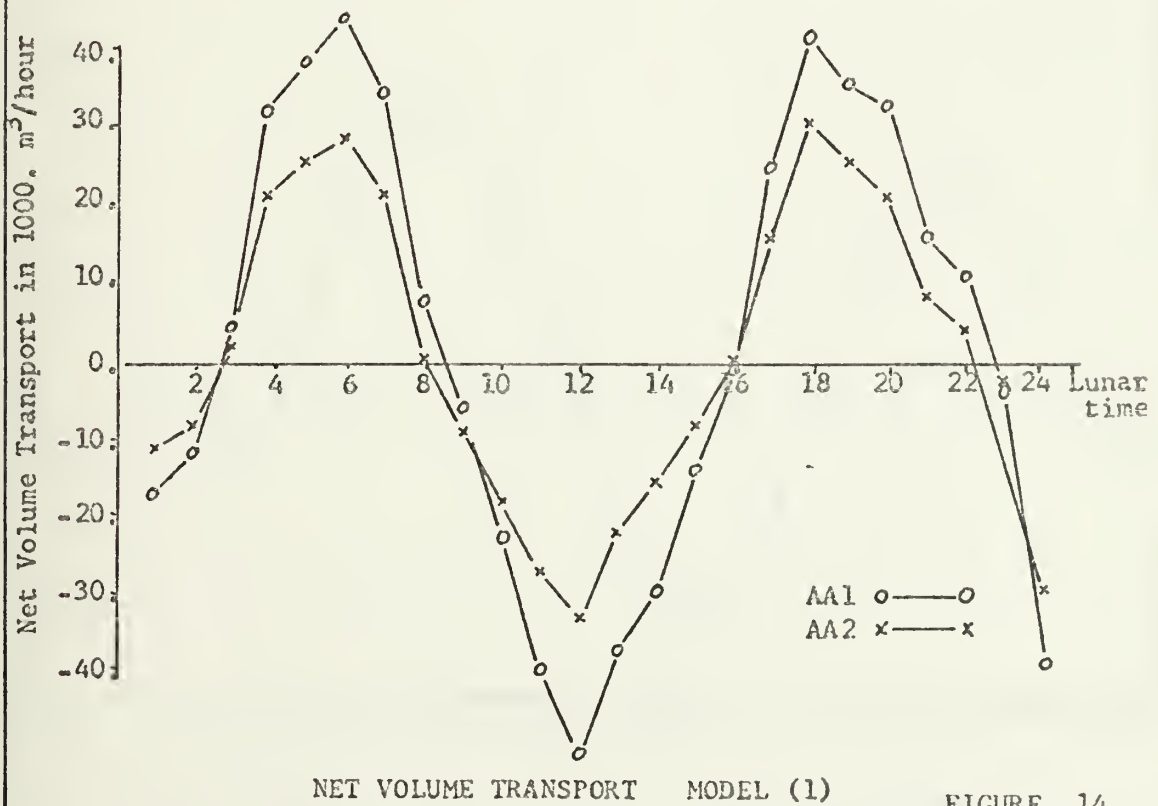
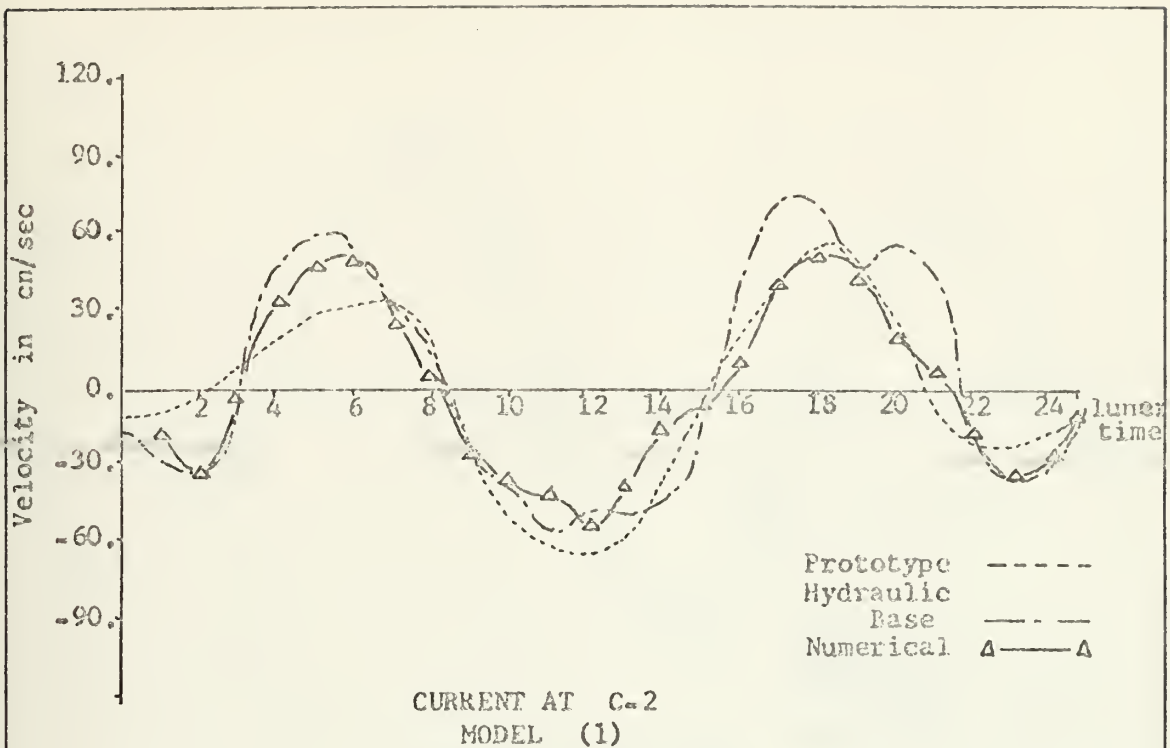
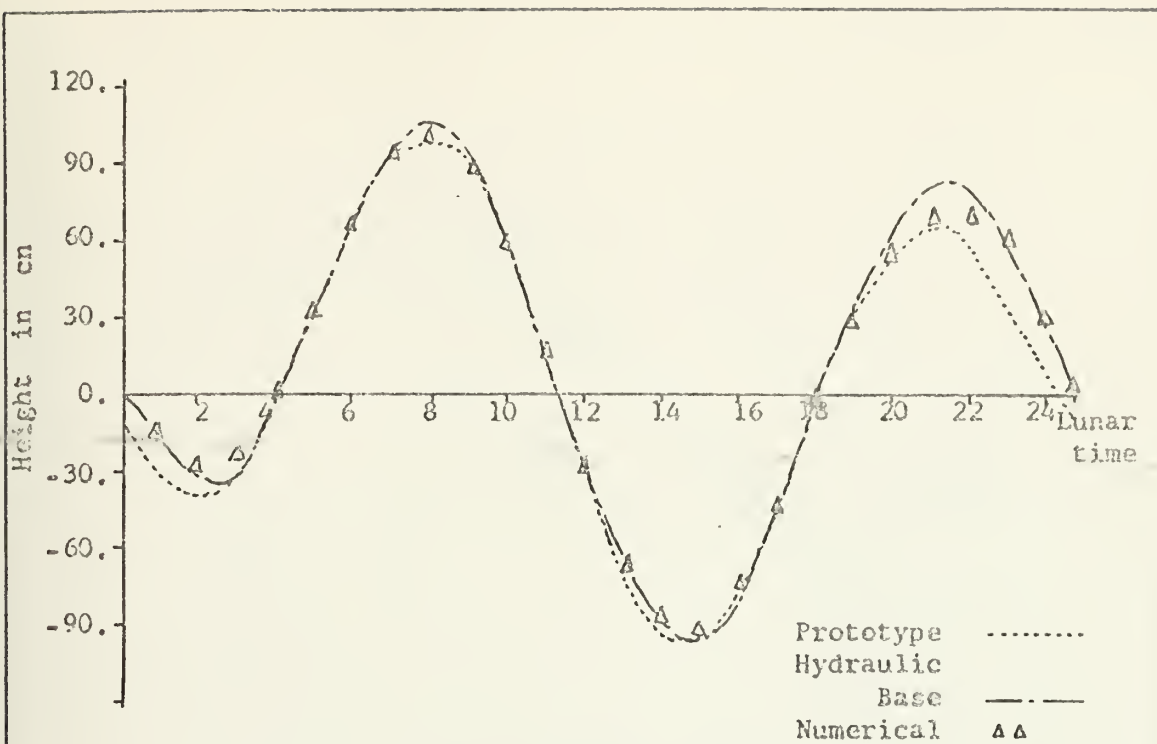
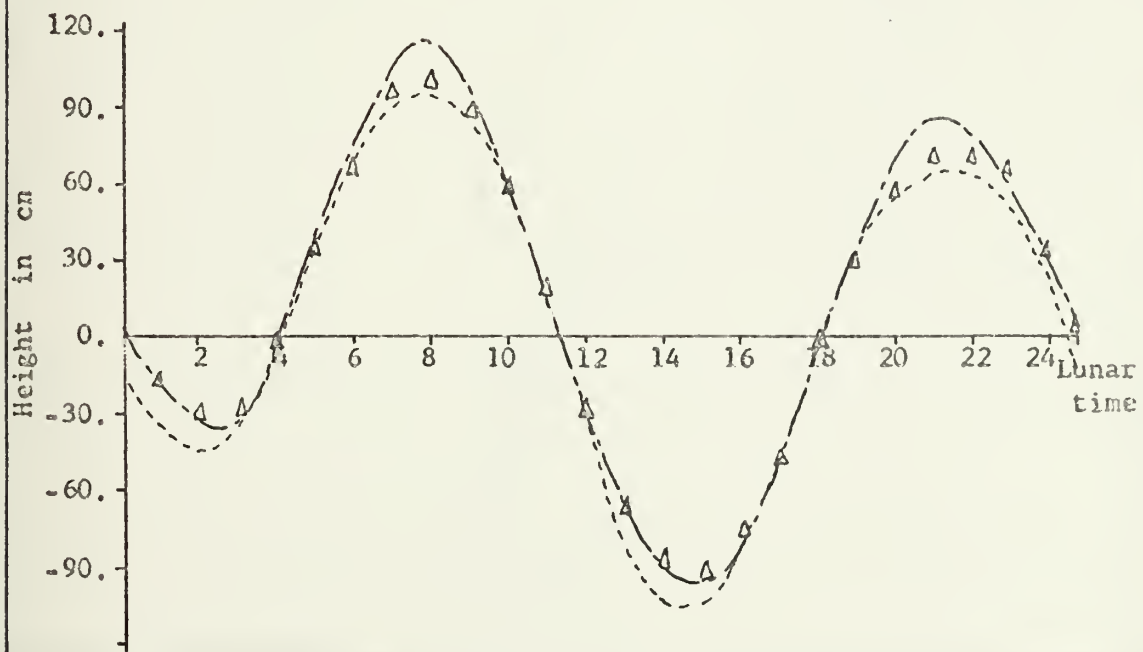


FIGURE 14

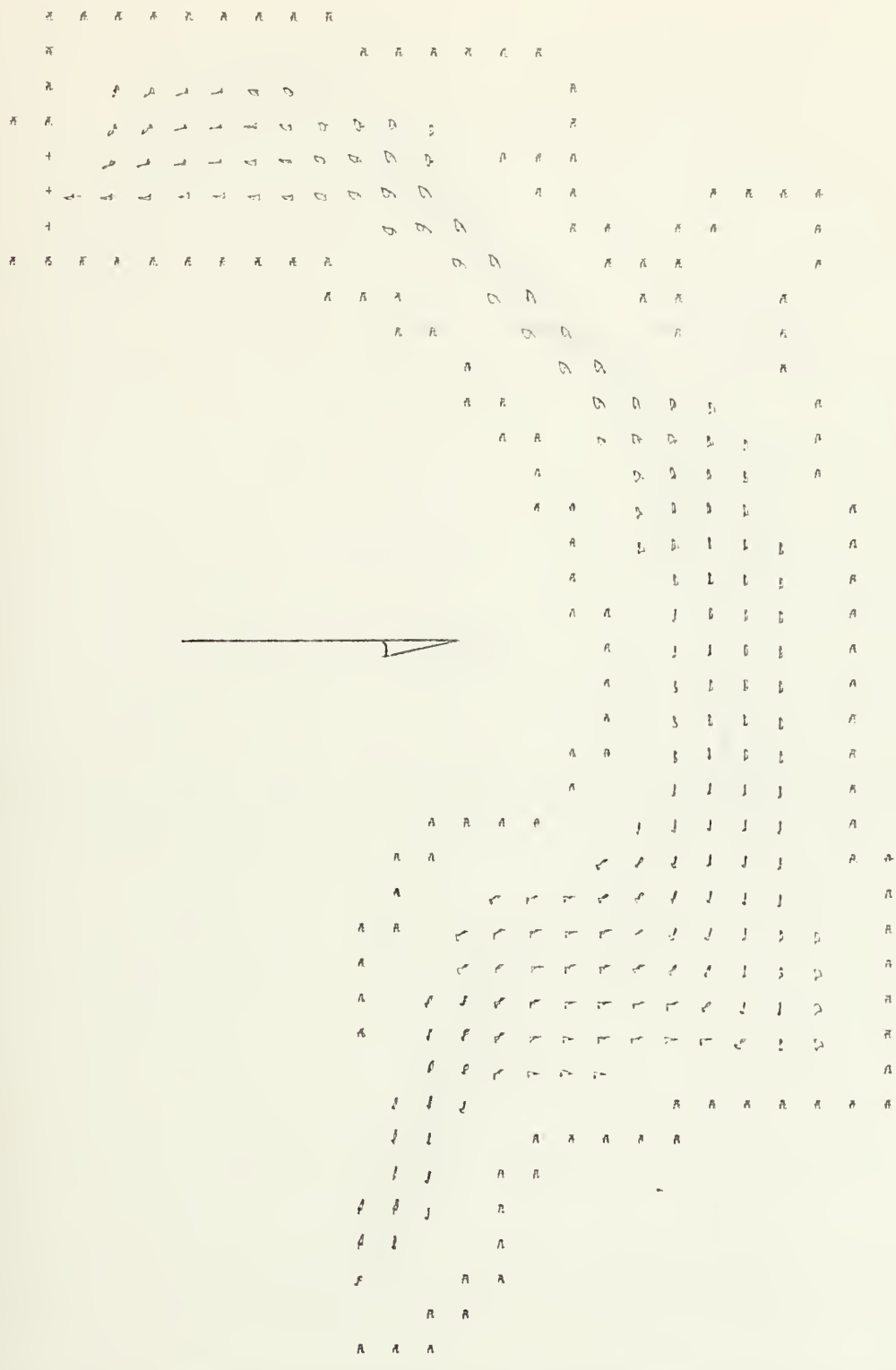


HEIGHT AT NAVY PIER
MODEL (1)



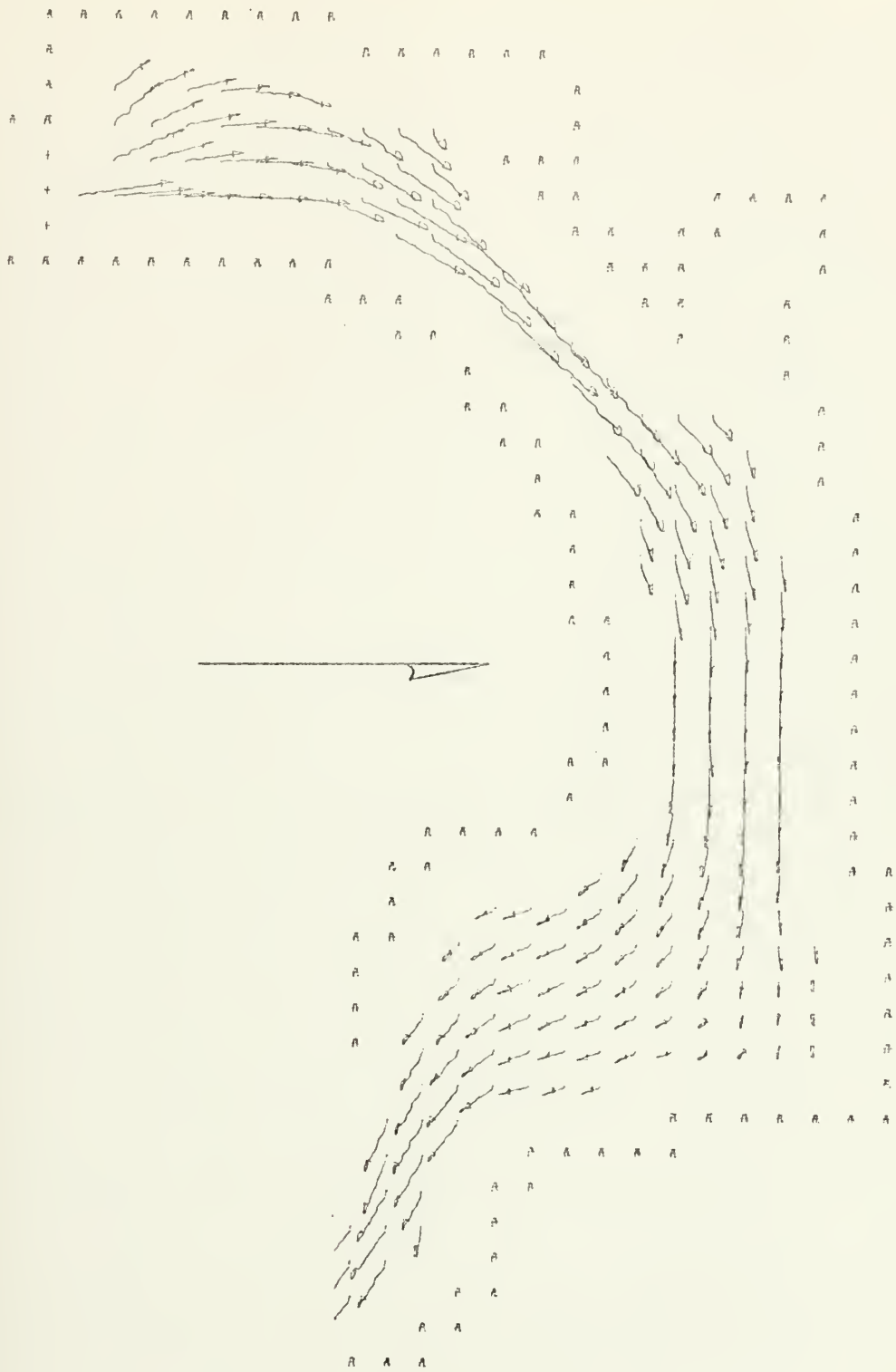
HEIGHT AT PIER N. 2
MODEL (1)

FIGURE 15



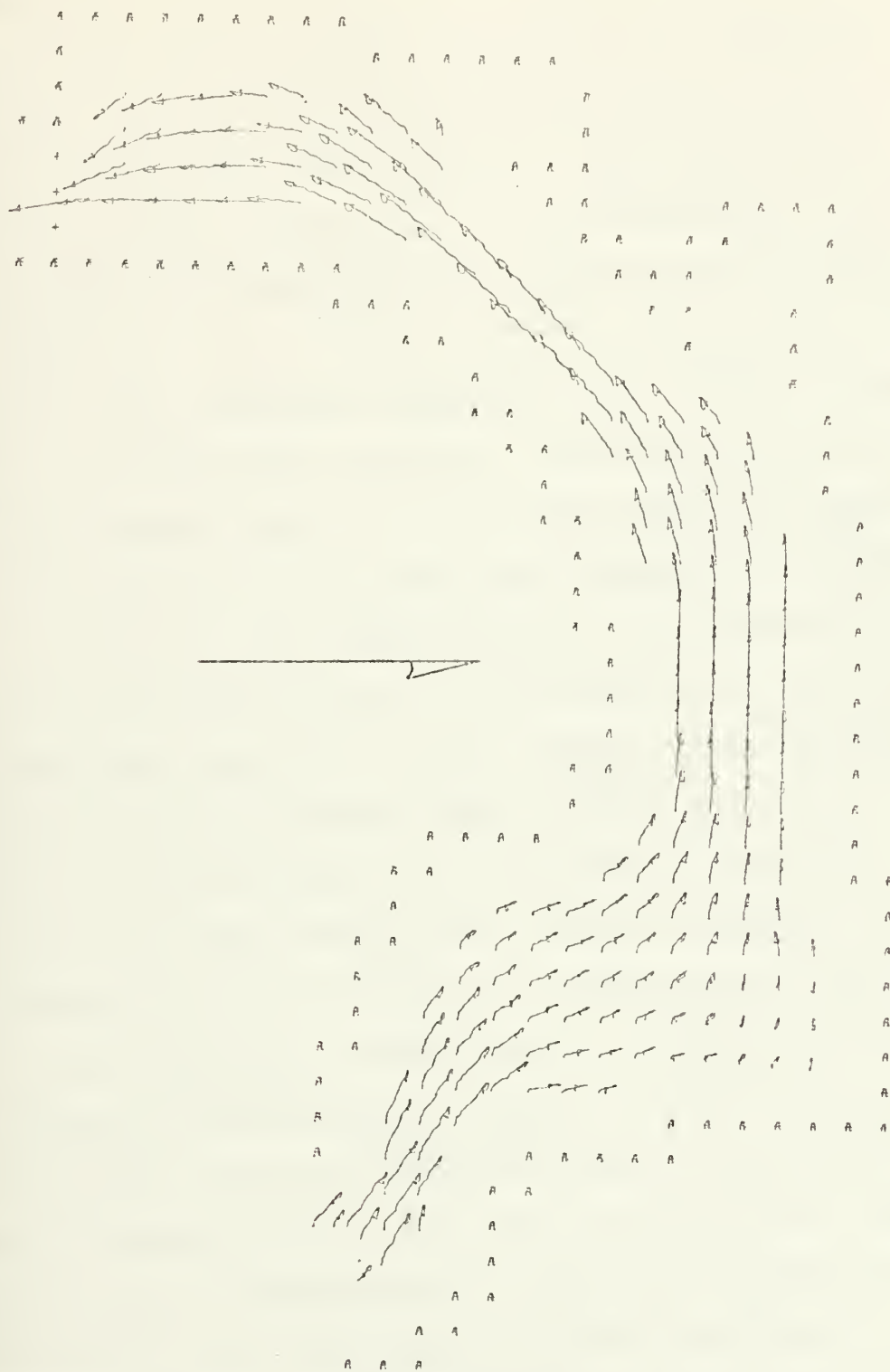
CURRENT DISTRIBUTION IN MODEL (1)
 TIME = 0. hr.

FIGURE 16



CURRENT DISTRIBUTION IN MODEL (1)
 TIME = 3 hr.

FIGURE 17



CURRENT DISTRIBUTION IN MODEL (1)
 TIME = 9 hr.

FIGURE 18

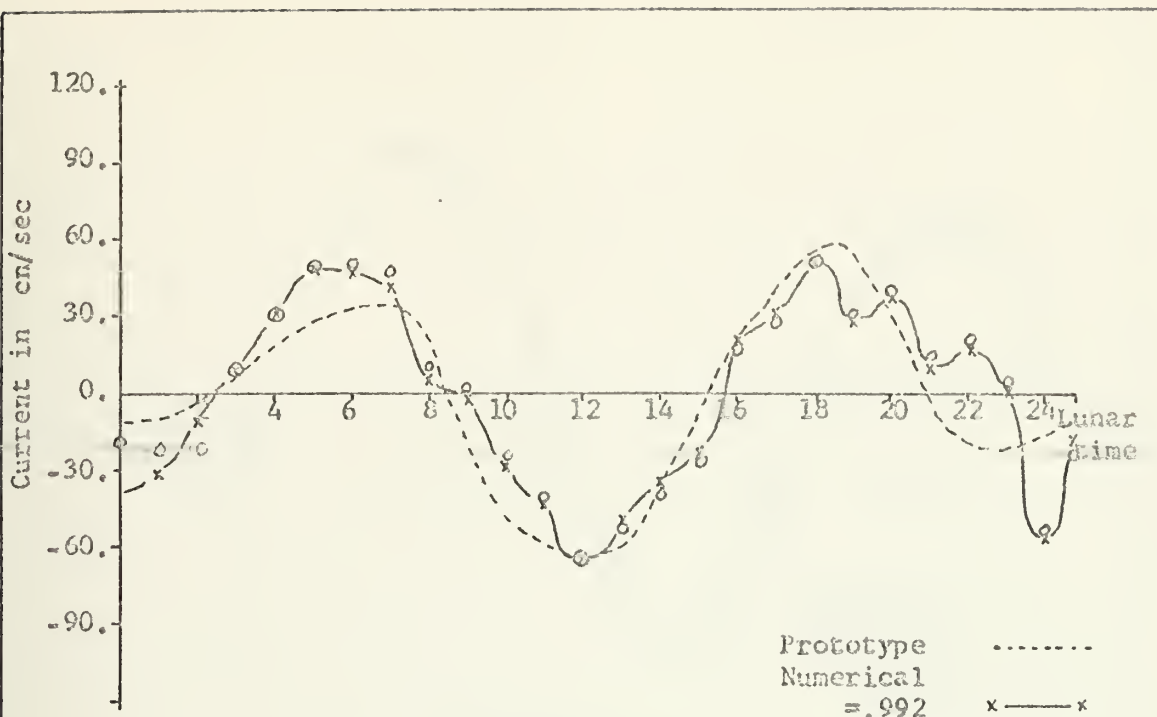
D. MODEL (2)

From the results of model (1), tidal values were obtained for a point at the middle of the channel in the vicinity of Navy Pier Tidal Station. These values were introduced as input to model (2). The computations were attempted with the same values of R (0.003) and α (0.992) as in model (1).

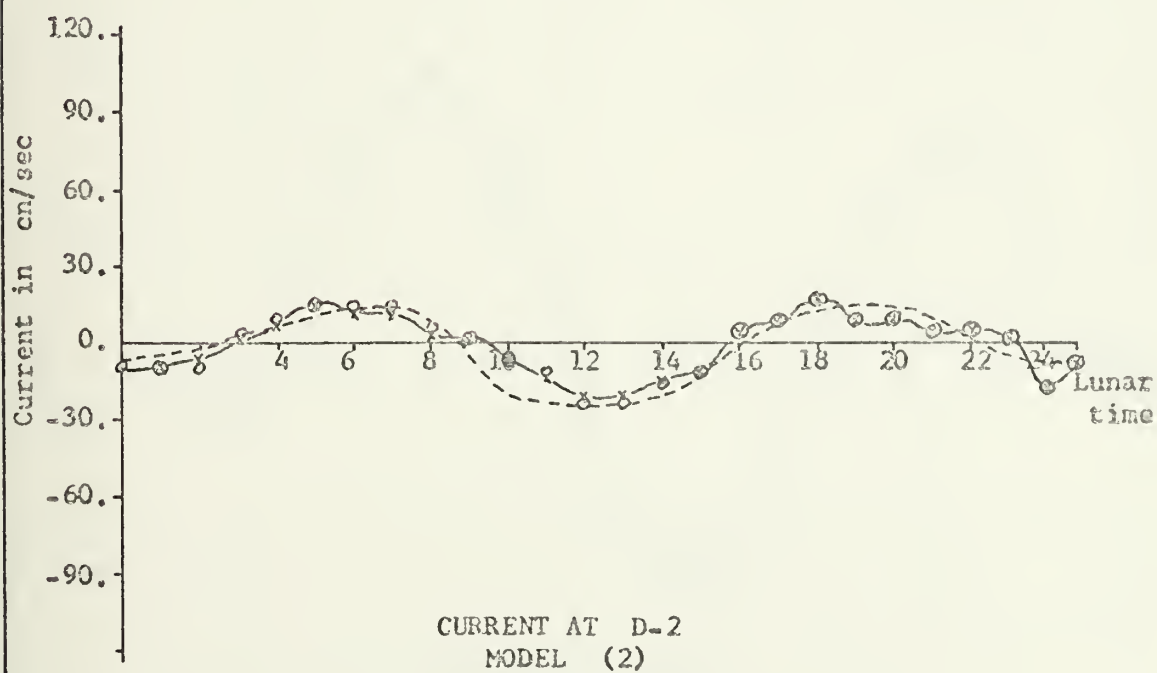
Using these prescribed conditions, oscillations in the current and tidal values developed (see Figures 19 and 20). These oscillations appear to be in phase and their magnitudes increase from zero at the open boundary to a maximum value of about 30 cm/sec. and 15 cm/sec. respectively at the end of the deeper channel at the near end of the bay, and from there, the values of the current reduce proceeding to the shallower and southern part of the bay.

The oscillations seem to be activated as the tide approaches the LLW, increase their values throughout the next HW and die out by the next LW, repeating the cycle 12 hours later when LLW is reached again. The period of the oscillations is greater than 2 hours.

The causes of the oscillations could be some kind of seiching manifestations in the model, shallow water tide or oscillations characteristic of the model produced by attempting to work in extremely shallow water without introducing special prescribed conditions for these small values [8].



CURRENT AT C-2
MODEL (2)



CURRENT AT D-2
MODEL (2)

FIGURE 19

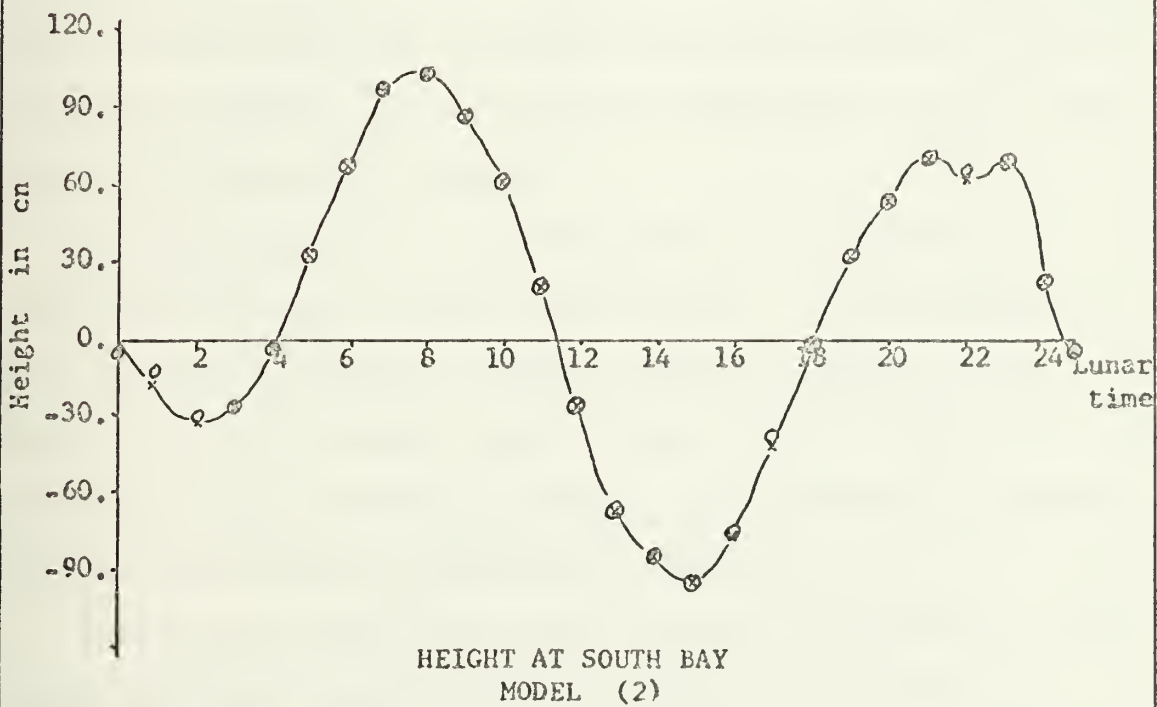
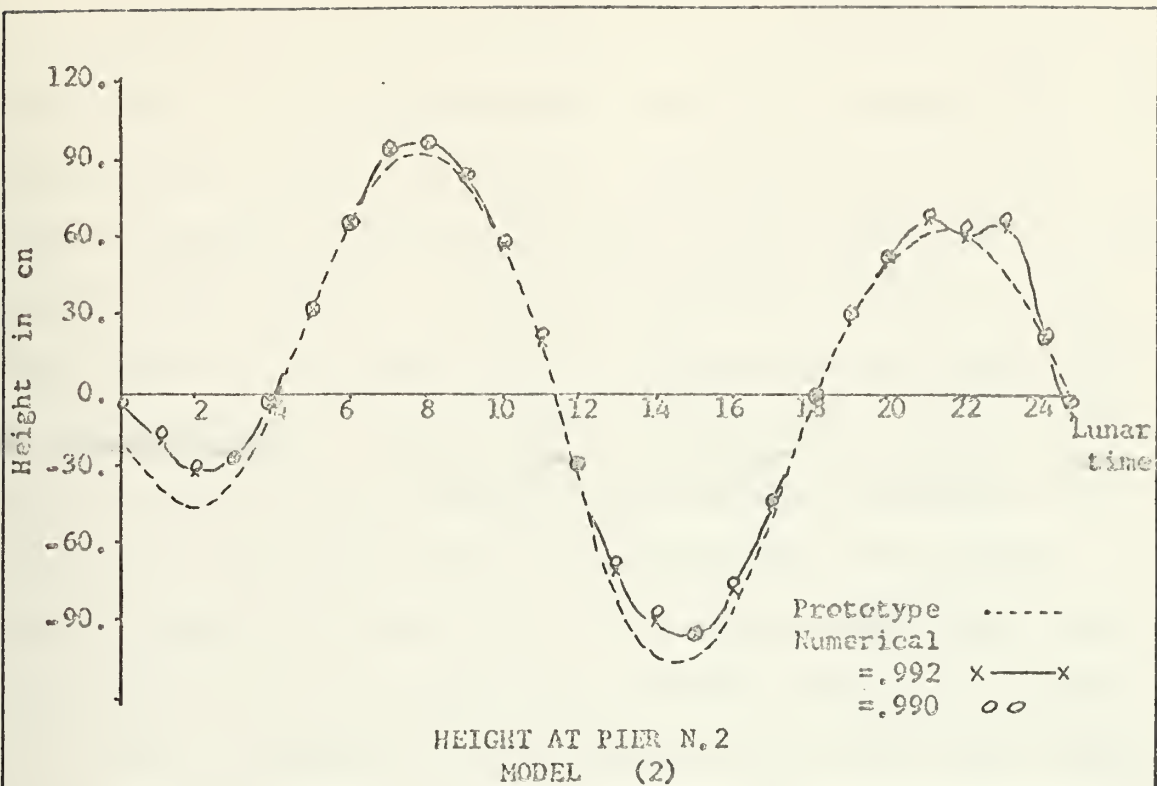
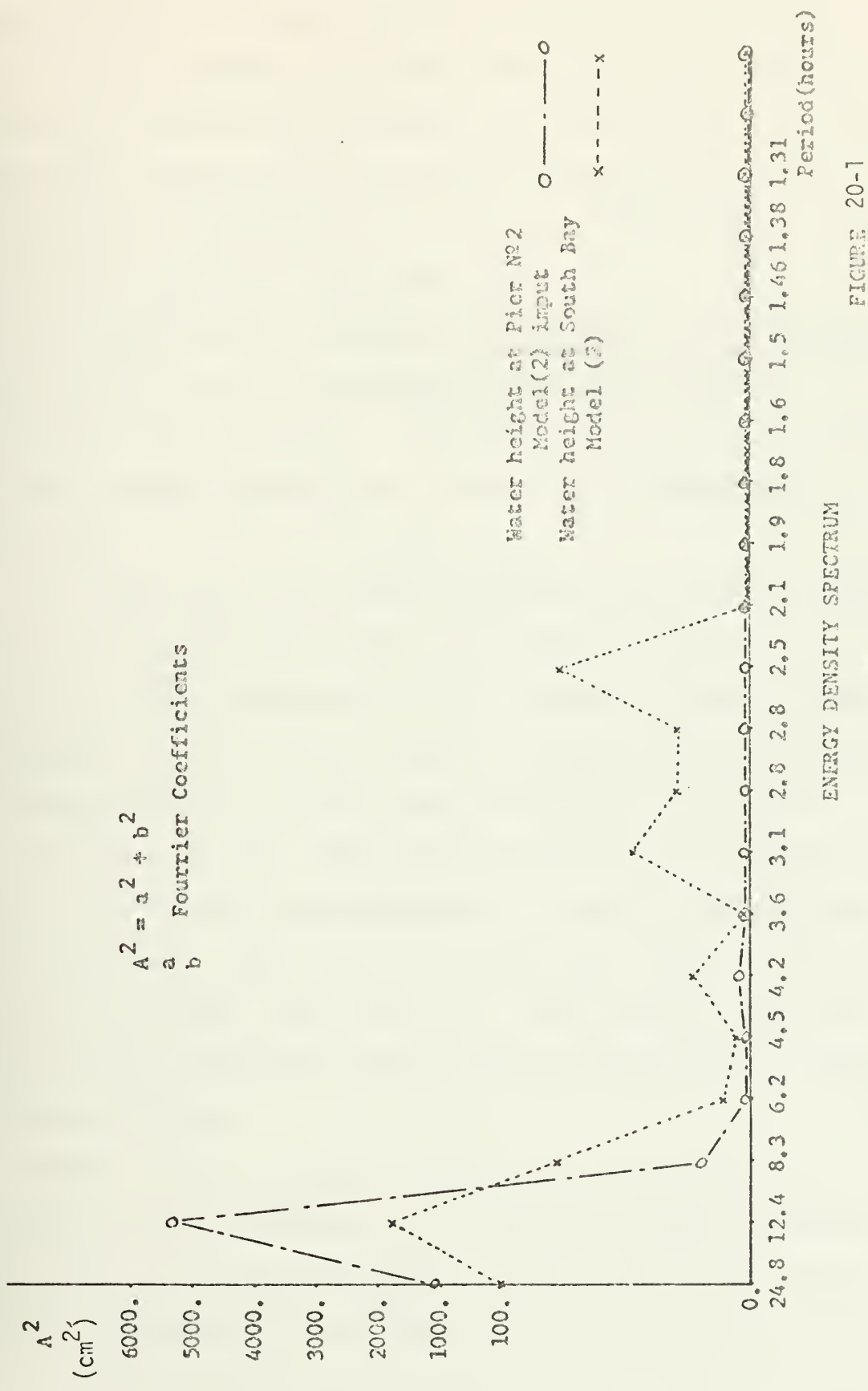


FIGURE 20

A possible mode of seiching can be calculated assuming that model (2) is an independent bay with a length of 14. km and a medium depth of 4. meters. This bay will oscillate with a fundamental period of about 2.3 hr. which agrees with the resulting values. A Fourier analysis was made of the tidal input of the model (2) and the calculated water height at South Bay Gage. Calculation of the Energy Density Spectrum was performed to compare both and see if energy from some of the harmonics from the tidal input have excited the oscillations in the bay. The spectrum shows (see Fig. 23-1) that the oscillations have periods between 2.06 and 3.55 (with a maximum at 2.3) hours and that the tidal input has negligible energy in these periods. This seiching may be activated at the LLW and damped out by the smoothing parameter α . The existence of such anomalies are not shown in the published records of the observations and its appearance depends, in case of its existence, on the time spacing of the data obtained.

The possibility of a shallow water tide seems to be reasonable because in each tidal cycle, the oscillations seem to be activated by the tide when the depth of the water is at its minimum value. This shallow water tide produces a high frequency harmonic [3] which can be amplified by the model and damped out later by α .

Because the model has linear terms only (except in the bottom and wind friction terms), it is not possible to transfer energy from one harmonic to another; then, the



amplification of a high harmonic from the shallow water tide is questionable. One last possibility can be a deficiency of the difference scheme. As the tide is a continuous wave type propagation, errors are introduced in the time differential computation that could produce a harmonic that could be amplified by the same model.

An α of 0.99 was introduced in an attempt to eliminate the oscillations by increasing the smoothing, but no improvement was obtained. Lower values were not introduced because larger smoothing may affect other parameters in the model.

The need for a low value of Alpha in the model to damp out these oscillations makes the previous estimation of 0.999 of α not applicable for the southern portion of San Diego Bay. In the model 2 and 3, a minimum depth of 4. ft is established to prevent that portion of the bay from becoming dry at LLW. This minimum depth was increased up to 12. ft. to test the probability of shallow water tide with the result that similar oscillations appeared but with larger amplitudes, (see fig. 21). This new test made the possibility of seiching the most feasible mechanism causing the oscillations.

Model (3) was finally run with an α of 0.992 and an R of 0.003 and the results of current and height of water are shown in Figures 22 and 23. A pictorial description of the circulation of the Model (2) at the hours 3 and 9

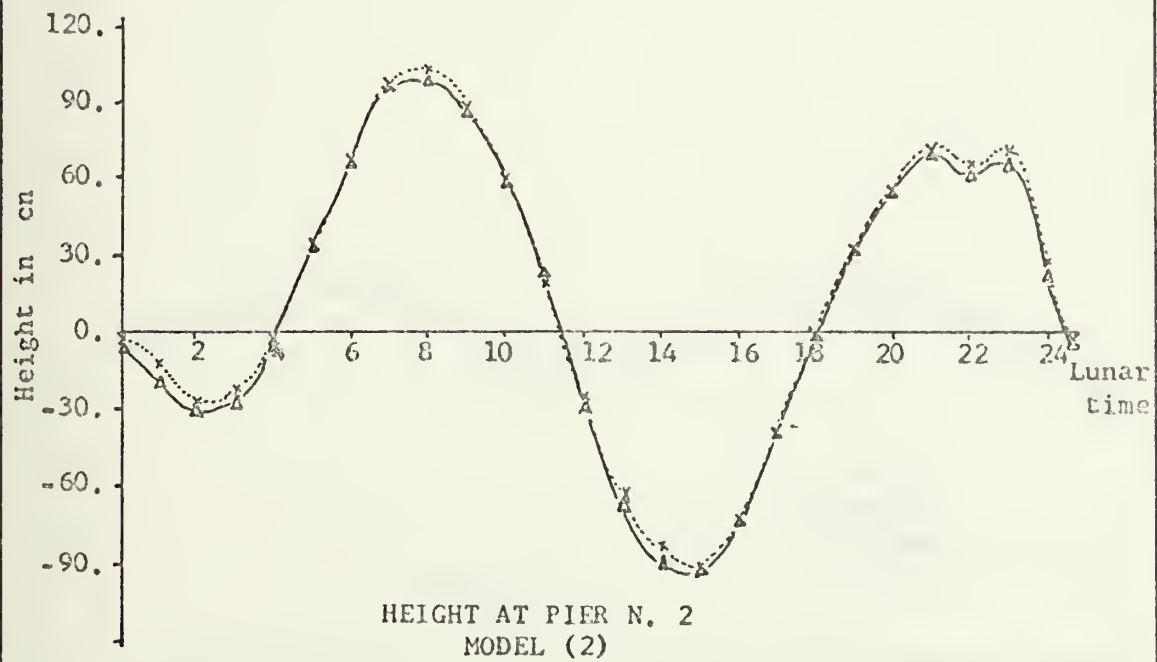
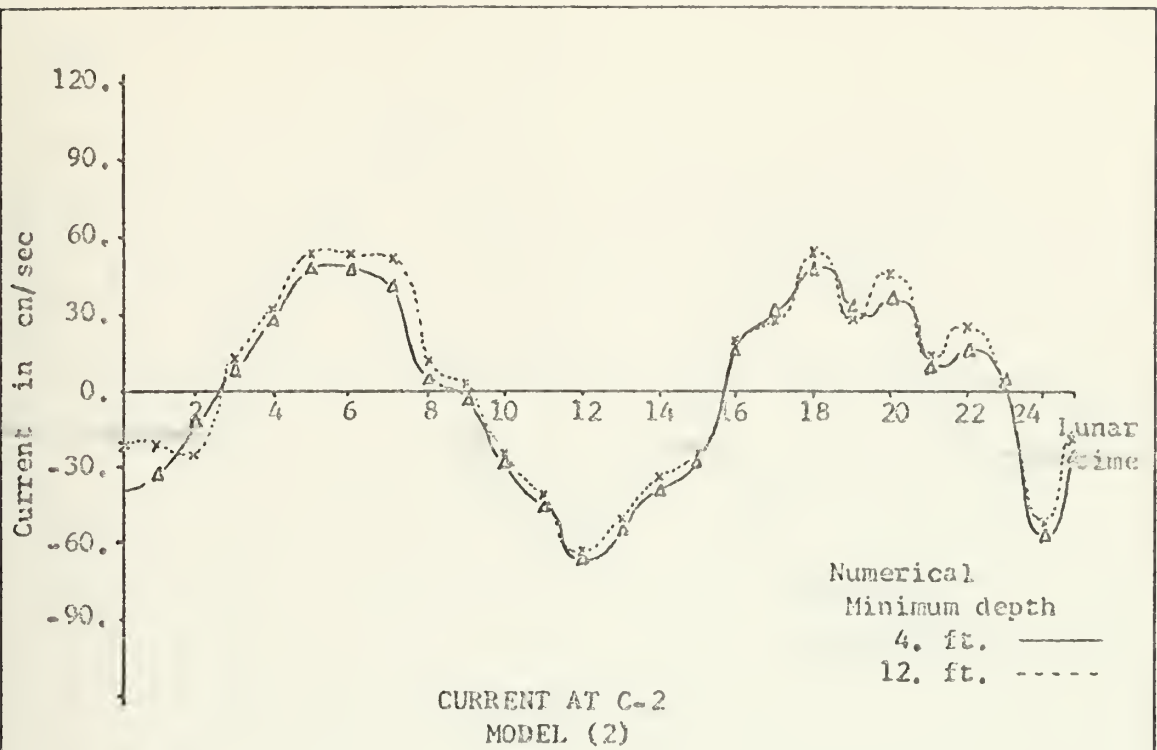
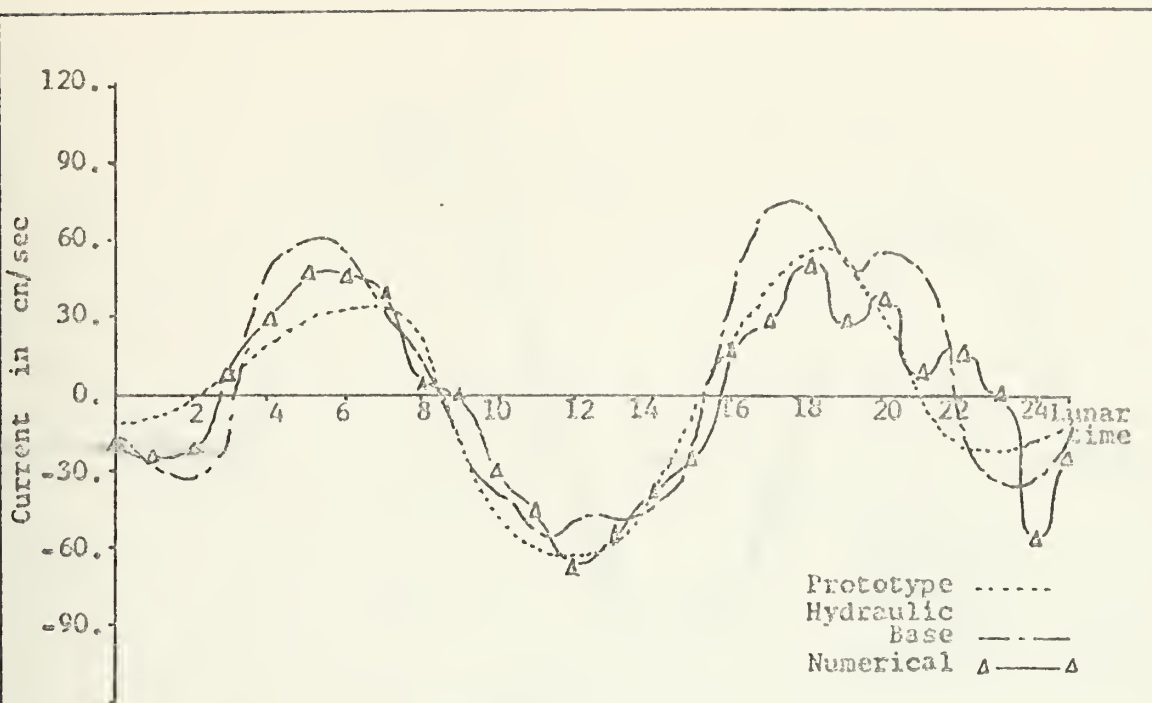
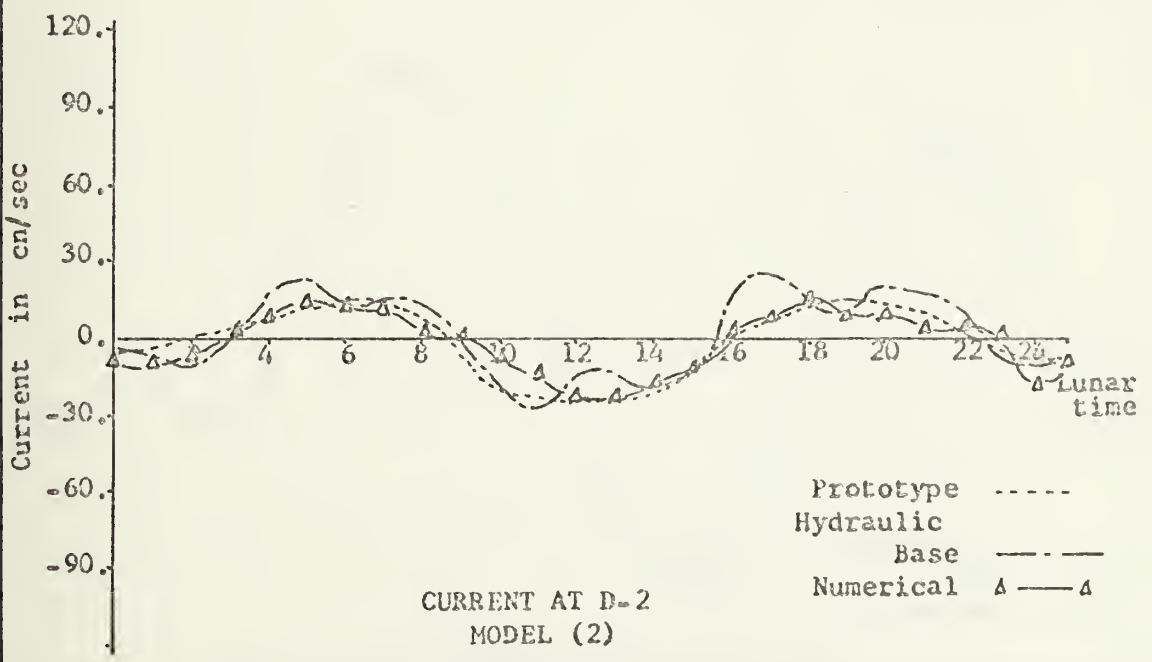


FIGURE 21

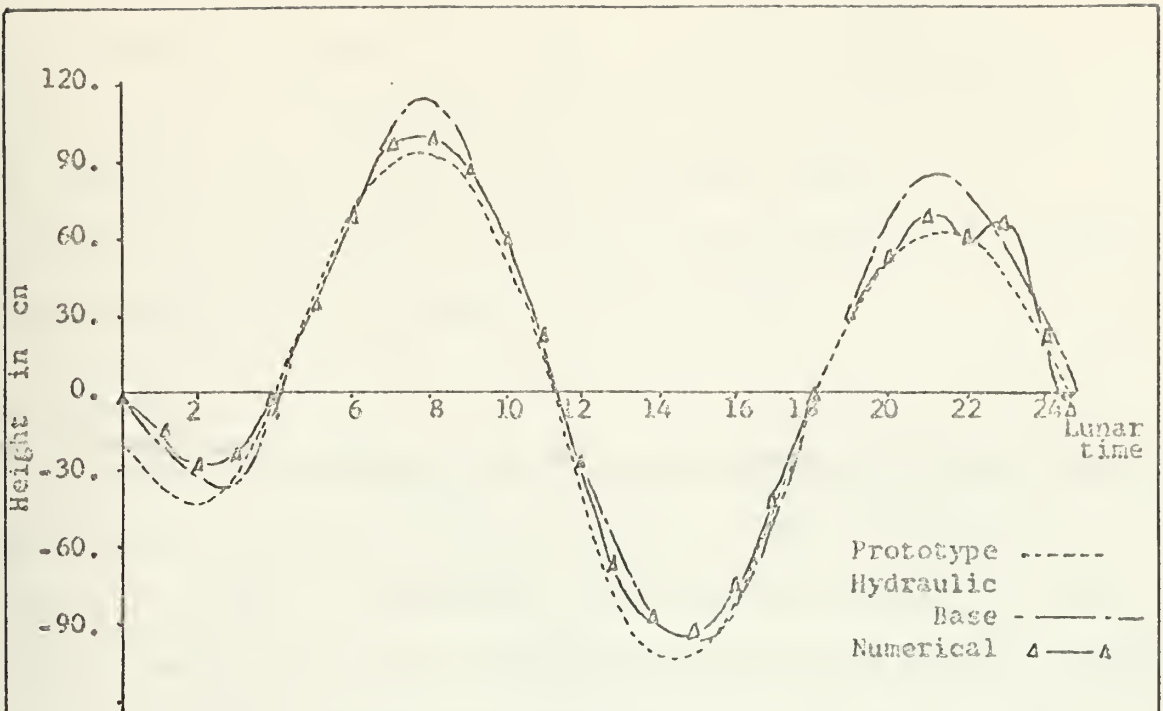


CURRENT AT C-2
MODEL (2)

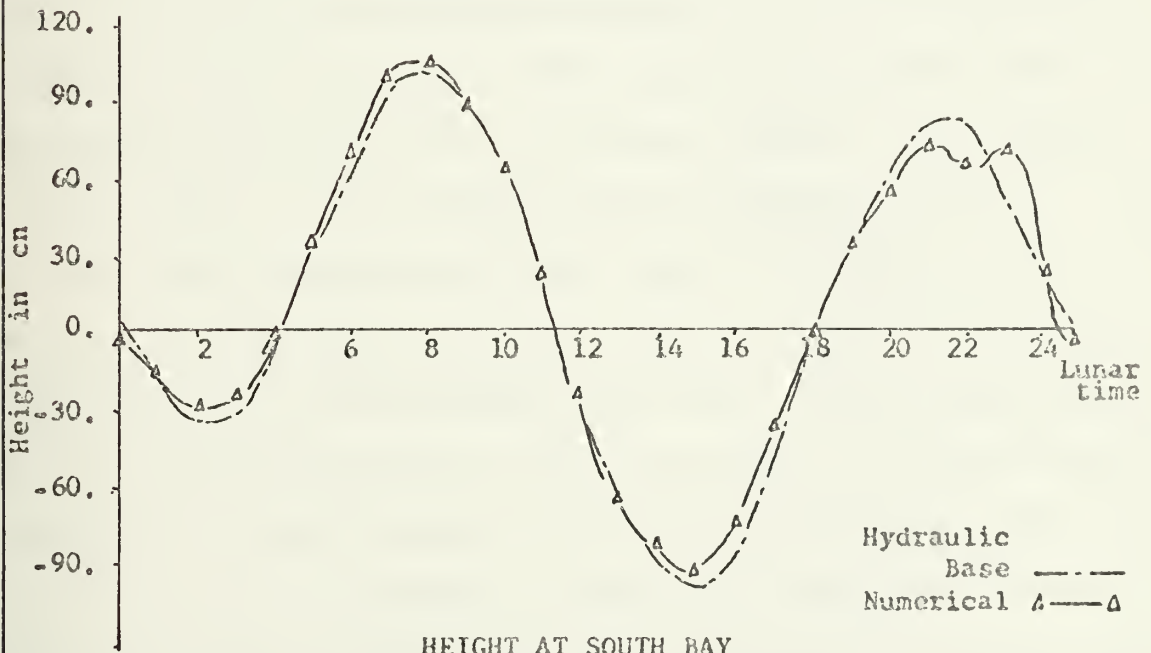


CURRENT AT D-2
MODEL (2)

FIGURE 22



HEIGHT AT PIER N. 2
 MODEL (2)



HEIGHT AT SOUTH BAY
 MODEL (2)

FIGURE 23

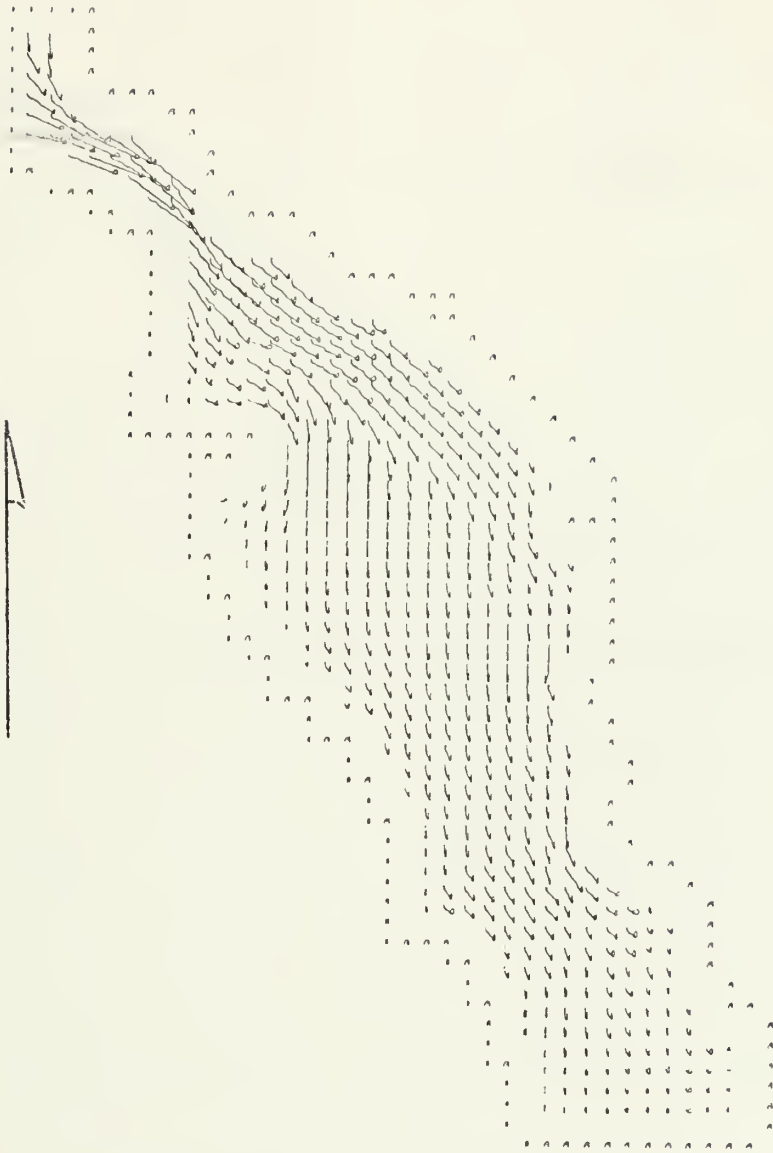
are shown in figures 24 and 25, and of the entire bay in which model (1) and model (2) have been matched is shown in Figures 26, 27, 28. In all of these figures, the direction and magnitude of the flow are represented by the direction and scaled length of the arrows.

E. MODEL (3)

Several alternatives of a second entrance and diffusion were tested by means of the hydraulic model conducted by the U. S. Corps of Engineers. Because the purpose of this work is mainly to make a comparison between different models, only one of the alternate second entrances was examined in the numerical model, and no diffusion study was made.

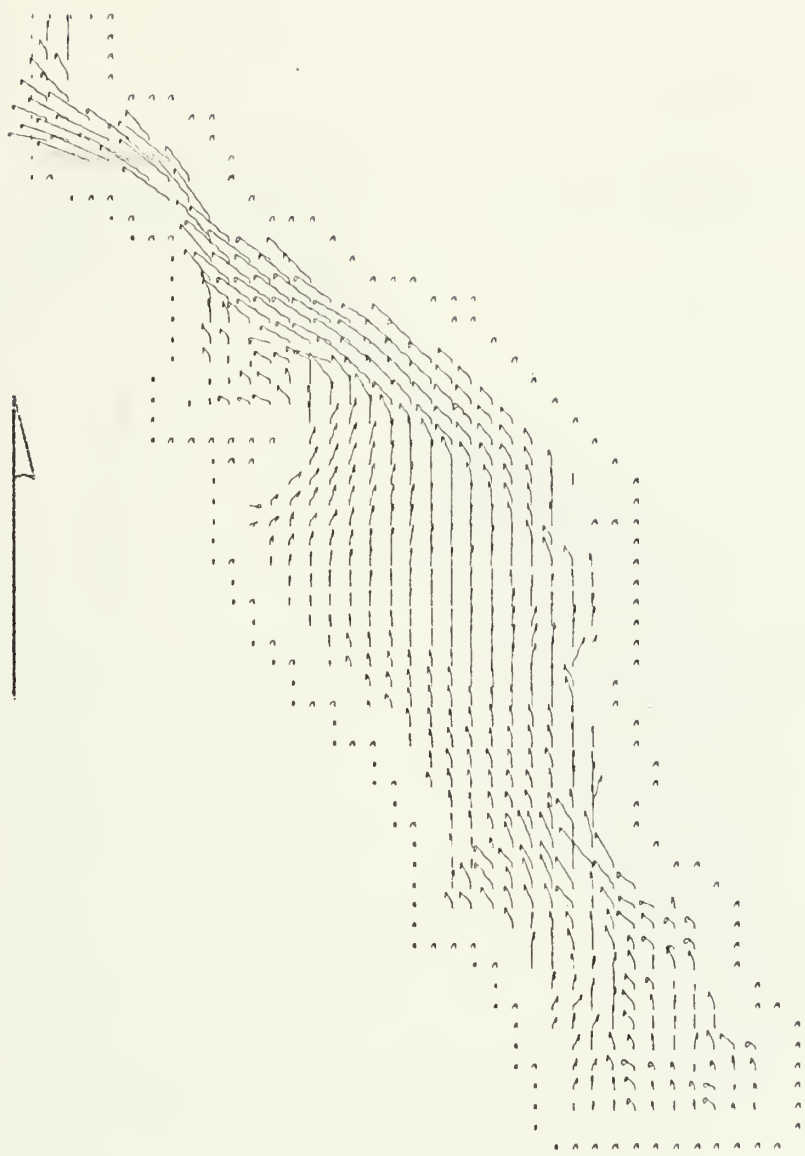
Model (3), with the proposed second open boundary at Crown Cove, was run in a similar manner to model (2). The input for the northern open boundary was obtained from the results of the model (1). The same oceanic tidal values measured at Ballast Point, in Zuniga channel, were chosen for the input at the proposed second channel entrance.

The same currents and tidal values developed in the model (2) using the prescribed conditions with α and R of 0.992 and 0.003 respectively were used. Their characteristics and interpretations were discussed in the previous section. No other values of the tuning parameters were tested because the purpose of this last model is to test model (2) with an additional open entrance.



CURRENT DISTRIBUTION IN MODEL (2)
TIME = 3 hr.

FIGURE 24



CURRENT DISTRIBUTION IN MODEL (2)
TIME = 9 hr.

FIGURE 25



CURRENT DISTRIBUTION IN MODELS (1) and (2)
TIME = 9 hr.

FIGURE 26



CURRENT DISTRIBUTION IN MODELS (1) and (2)
TIME = 3 hr.

FIGURE 27



CURRENT DISTRIBUTION IN MODELS (1) and (2)
TIME = 15 hr.

FIGURE 28

The results obtained by the U. S. Corps of Engineers shown in Figures 29 and 30 are compared to the results in currents and height of water for this model shown in Figures 31, 32 and 33. Pictorial representations of the current distributions are shown in Figures 34 and 35. The same representation obtained from the U. S. Corps of Engineers Hydraulic model for the complete Bay with the second open boundary are shown in Figures 36 and 37. In both groups, the flow of water throughout the proposed open entrance seems to be the dominating factor of the circulation in the southern portion of the bay. The northern portion is dominated by the northern circulation and a very definite rest area is located between the two systems.



CURRENT DISTRIBUTION HYDRAULIC MODEL (BASE TEST)
TIME = 12 hr.

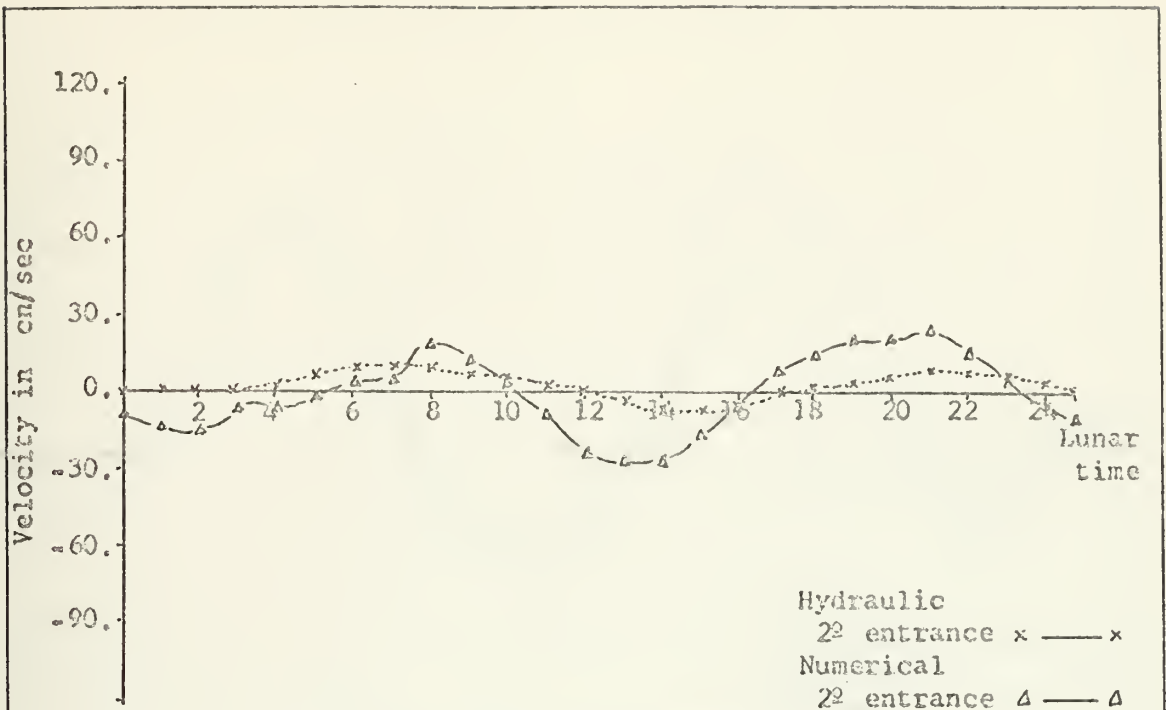
FIGURE 29)



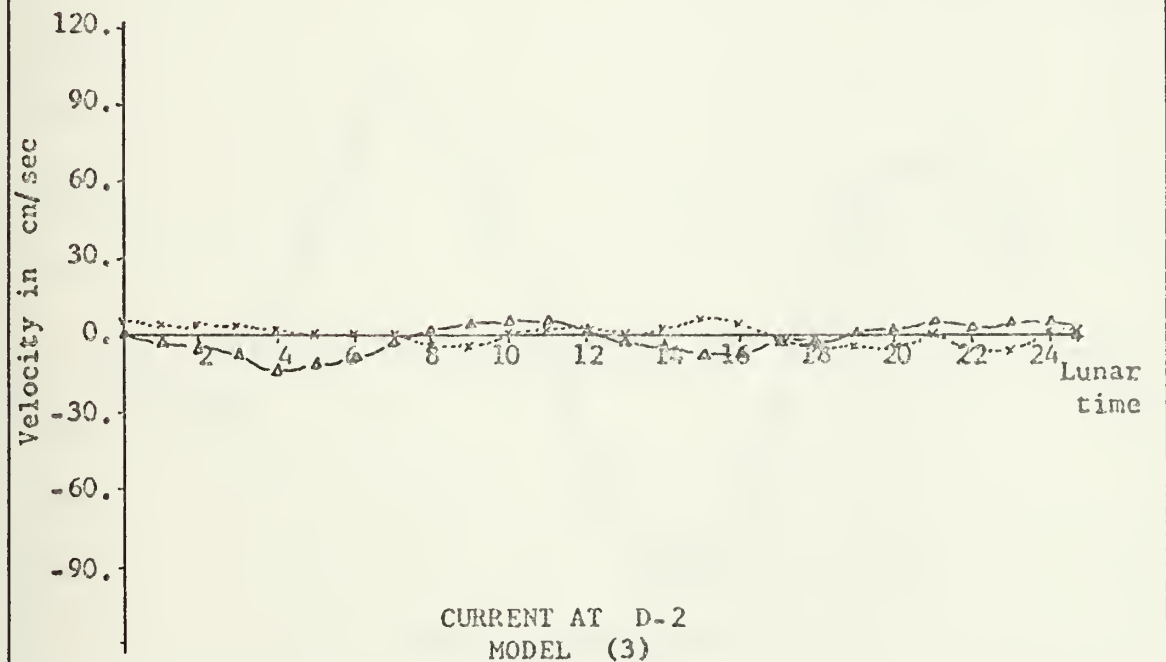
CURRENT DISTRIBUTION HYDRAULIC MODEL (BASE TEST)

TIME = 18 hr.

FIGURE 30

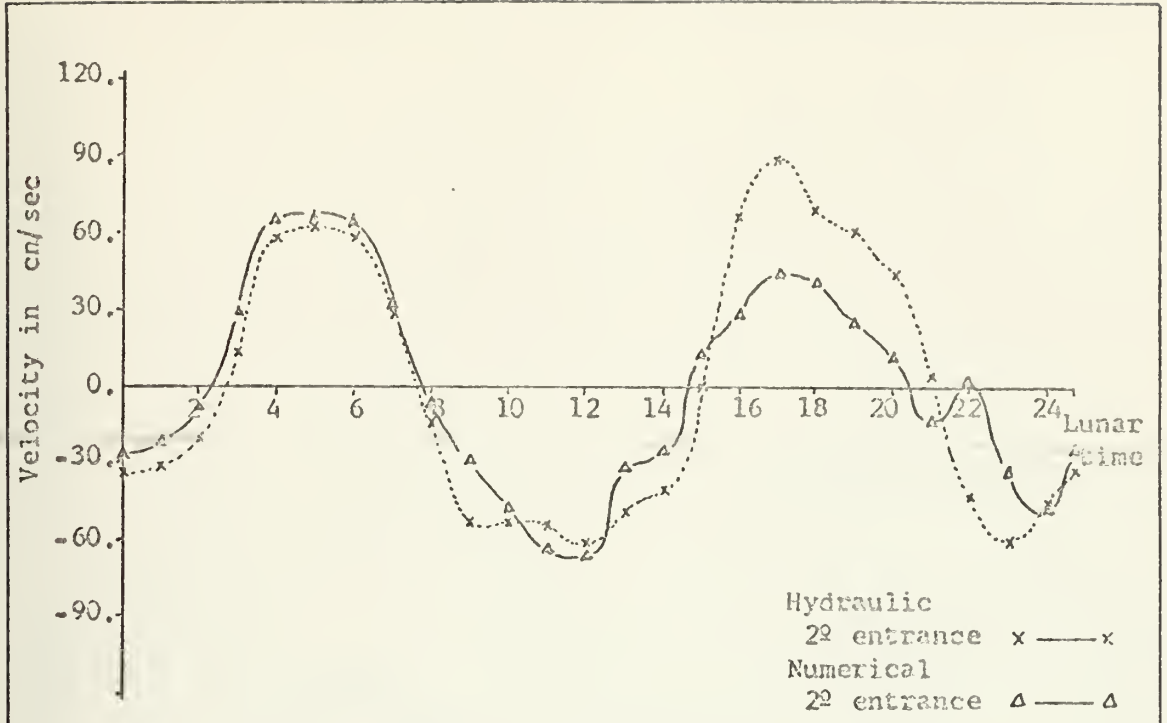


CURRENT AT C-2
MODEL (3)

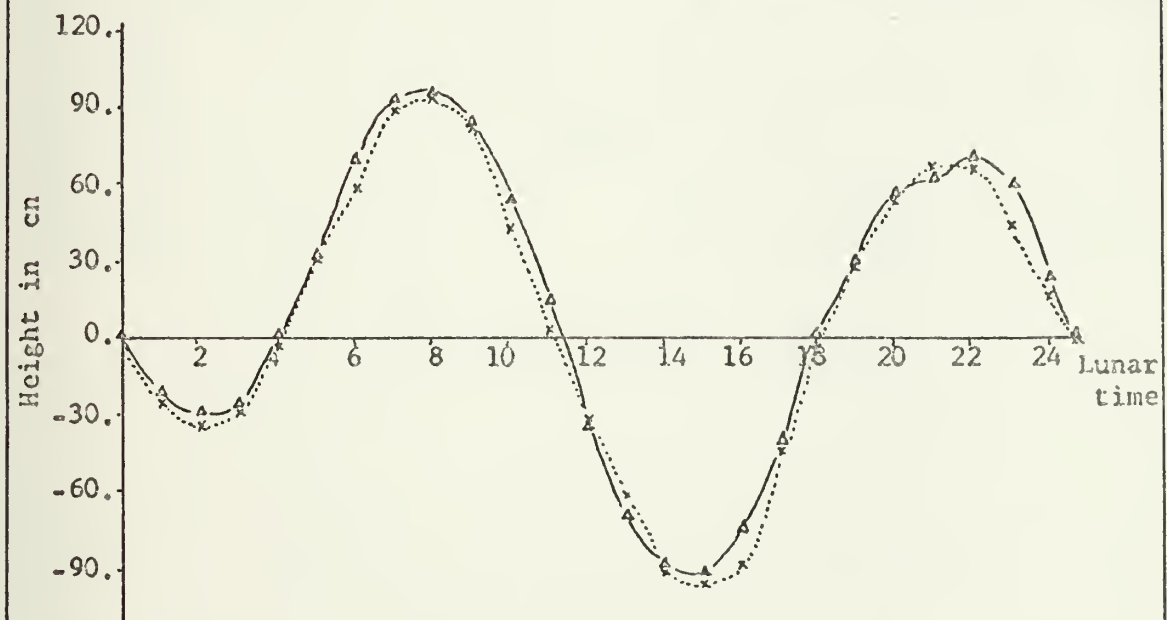


CURRENT AT D-2
MODEL (3)

FIGURE 31

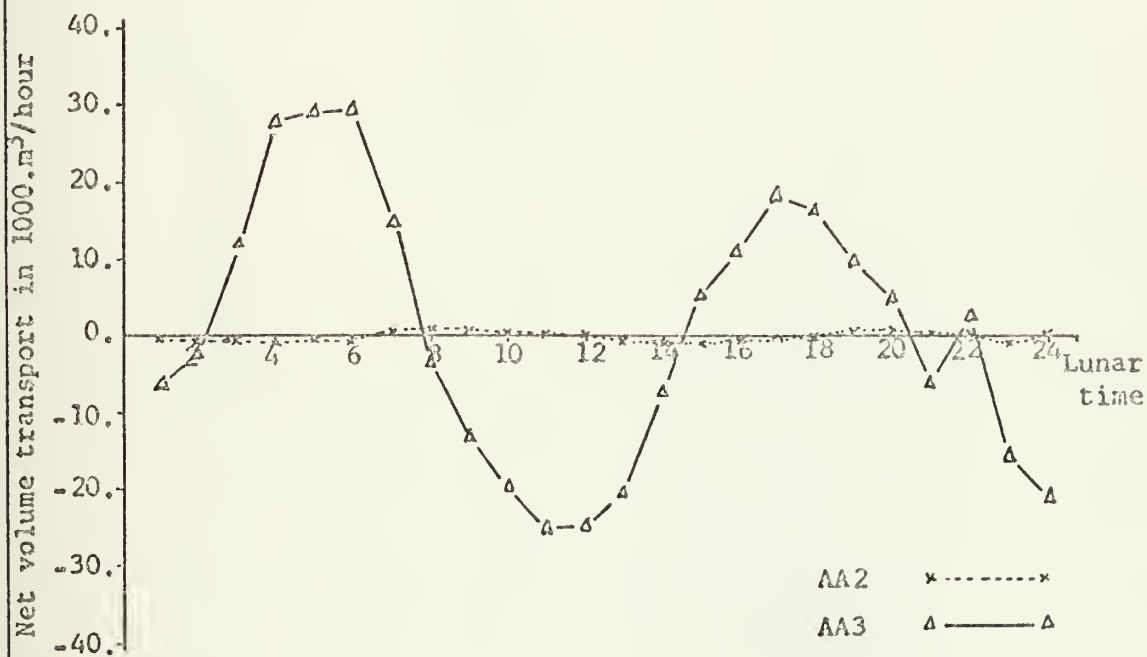


CURRENT AT CROWN CAVE
MODEL (3)



HEIGHT AT SOUTH BAY
MODEL (3)

FIGURE 32



NET VOLUME TRANSPORT MODEL (3)

FIGURE 33



CURRENT DISTRIBUTION MODEL (3)
TIME = 3 hr

FIGURE 34



CURRENT DISTRIBUTION MODEL (3)
 TIME = 9 hr

FIGURE 35



CURRENT DISTRIBUTION HYDRAULIC MODEL (PROPOSED SECOND ENTRANCE)

TIME = 12 hr

FIGURE 36



CURRENT DISTRIBUTION HYDRAULIC MODEL (PROPOSED SECOND ENTRANCE)

TIME = 18 hr

FIGURE 37

IV. MERITS OF BOTH THE HYDRAULIC AND NUMERICAL MODELS

A comparison between both models cannot be made without the results of a proper test of the models under the same conditions and on an area where accurate measurements of actual conditions have been made to compare with their results. The merits of each have previously been enumerated and the goal of this work is to evaluate them.

Before ordering the merits of the numerical and hydraulic models, it is good to recall that for this specific case, the numerical model in discussion (Hansen Model), by definition, is a barotropic ($\rho = \text{constant}$) single-layer model, and the hydraulic model used a constant density fluid. The hydraulic model was based on the Froude similarity concept (inertial and gravitational forces predominate). Although the discussion is restricted by these conditions and are not applicable to general numerical and hydraulic models, these are the most commonly applied types of models.

The spatial resolution of the hydraulic model depends on the length scale and the measuring capability. In the numerical model, topographic features are represented in terms of grid points. To obtain a good representation of bathymetry, small grid size is needed that results in an extremely large array. A compromise between spatial resolution and core size must be reached.

The time resolution in the hydraulic model depends on the similitude criteria and can be scaled to obtain a reliable result. In the numerical model, it is governed by the availability of computer time, i.e., the smaller the time step, the more computer time required.

The scaling in the hydraulic model is given by the similitude criteria. As was pointed out in the section dealing with the hydraulic model, these criteria compromise scales causing distortions in the model and oblige the use of some specific dimensionless number for each specific case. The introduction of distortions in the model limits its uses because some other terms ignored in the selection of the dimensionless number may become important.

In the numerical models, the flow is described by the solution of the equations of motion which includes terms of different orders and degrees. Each term describes some specific characteristic of the flow. The characteristics of the flow will depend on the shape, location, external forces applied, bathymetry, and properties of the fluid. In describing these flows by the equations of motion, some of the terms become dominant and some others can be considered negligible or included in some coefficients. In the case of the Hansen Model, this was accomplished by neglecting the non-linear momentum flux terms. The choosing of the proper terms becomes invalid if improper considerations are done. Then, an improper scaling can invalidate these selected portions of the equation.

Furthermore, the finite solution of this equation does not permit the continuous computation of the flow. The computation is done by time and spatial steps that may cause large errors in the model if proper precautions are not taken. For example, the coefficient of Eddy Diffusion is defined in the finite solution in terms of spatial and time steps. Then, its value becomes affected by the grid size and time step.

Obtaining data from a hydraulic model is difficult and limited by the instruments and the distortion in the scale of the model. Sizes and numbers of the measurement instruments are limited, and the region where these instruments can perform a measurement in the model is restricted by their sizes. In the numerical models, the characteristics of the flow is computed at each grid point; thus, it is available at each point and at each time step. Deficiencies in the differential solutions introduce errors in these grid points in the vicinities of the coast lines and input boundaries. In the hydraulic model, equivalent errors exist in the input boundaries; good resolutions have been claimed for near shore regions that can be questionable because difficulties in the measurements of quantities, such as current speed, in these regions makes it a not always tested assumption. Besides, surface tension becomes important in these regions that compromises the model.

The cost and time are some of the larger limitations in programs and research. Hydraulic models are expensive

and take months and sometimes years to achieve a satisfactory calibration. The use of the numerical models generally decreases considerably these limiting factors. A limitation of numerical models is that they require large computers that are not always available.

Simulated diffusion or dispersion of pollutants has been accomplished in both types of models with comparable results [1 and 5]. In the hydraulic models, this is achieved by direct measurements of dye materials introduced into the model. The conservation of mass equation is used for this computation in the numerical model. All the previous measurement and computation problems are taken into consideration for a proper evaluation of these factors.

V. CONCLUSIONS

The comparisons between the hydraulic and numerical models dealing with the modeling of San Diego Bay and its proposed modifications, are considered separately for general cases and for each of the different tests involved in this study. The Hansen Hydro-numerical Model was applied to the Bay to compare its solution against the U. S. Army Corps of Engineers hydraulic model. The description of both models and the manner of how these numerical and hydraulic models were applied to San Diego Bay has been discussed in detail.

In general, the numerical model is more easily handled for topographic changes than the hydraulic. The latter cannot be stored for future uses after being run as is done with the numerical model because of space limitation. A comparison of time and cost is not possible because no data are available for the model of the U. S. Corps of Engineers. The three numerical models consumed for final runs a total of 7 hours 15 minutes CPU time in the IBM 360/67. Adding an average of three times this amount for calibration, the cost becomes approximately \$21,000 (U.S. dollars). It would take about three weeks for a trained programmer to obtain the complete answer for this specific case.

The added easier possibility of including the input of wind gives to the numerical model better ability to represent

the prevailing conditions. The same numerical model can include the wind. Usually completely different hydraulic models must be built to simulate wind because of similitude considerations.

The hydraulic model has better space resolution than the numerical model. A method was tested for transferring boundary values from one numerical model to another to give the model the ability to divide long estuaries into smaller areas improving in this way the resolution of the numerical model. With the use of this method, two different but dependent models were run to represent the complete bay. A constriction in the configuration of the bay was chosen for the overlapping region. A similar procedure is used in the hydraulic model to save space in long hydraulic models. To achieve it, the bay is distorted in a narrow location in a fold-like procedure. The model is calibrated at both sides of the curve. This procedure gives the possibility of dealing with a model of a smaller scale that gives more details of the area, but special care must be taken so as not to introduce errors in the time scale. A similar procedure can be done in the numerical model if the excess area is small and can be accommodated in the free space of the first grid. The possibility of running two completely different hydraulic models seems to be impracticable because of economics.

The numerical model reproduced very well the sea level and currents for the cases tested, provided boundary

treatments are correct. The boundary treatments sometimes are not easily achieved and are a matter of decision in order to represent properly the coast line and channels in the grid. Representation of sea level seems to be equally correct in both models, but the current results seem to be better in the numerical model except near boundaries and shorelines. The seich-like oscillations developed in the numerical model must be taken into consideration if the model is to be representative of the total bay. If only a part of the bay is under consideration (for example model (2)), the seiche oscillations should be smoothed out because they are not representative of the bay.

No comparison can be made of net volume transport because no evaluation in the hydraulic model is available. These computations were made in the numerical model based on the computed velocities. The computed values seem to be reliable enough.

It was pointed out in the section dealing with model (2), that the boundary conditions in the numerical model must be given special treatment when the area becomes dry during low tide. A minimum depth of 120 cm was fixed in the numerical model in order to prevent any problem, and the southern extreme of the bay was eliminated because its depth was below 50 cm. No special problem seems to appear in hydraulic models, for the case of portions of the area becoming dry, but special care must be taken if areas become shallower than 1 cm. because then surface tension is important. This

minimum depth had not been discussed in previous literature for numerical models, and no attempt to evaluate these conditions was made in this study.

In the model with the proposed second entrance, the initial assumption of increasing the flushing of the bay seems to be reasonable. The circulation of the southern portion of San Diego Bay will be almost entirely governed by the second entrance. But, from the computed net volume transport in the section AA2, it is shown that the interchange of water between the northern and southern portion of the bay at this section will be almost negligible. Comparing the pictorial representations of both models for this special case, an area of decrease of current speed can be noticed between Pier No. 2 and D-2 gages where both models indicate that the flow of the bay will be divided into two separate systems and the projected second entrance will provide the water for the southern system. This would result in decreased dispersion of pollutants introduced to the bay in this region.

APPENDIX A
 NUMERICAL PROGRAMS

HANSEN'S HYDRODYNAMICS MODEL

SAN DIEGO BAY (1)

CF LEOPOLDO SALAS R.

LIST OF PARAMETERS IN THE PROGRAM

```

M
N
Z(N,M)
U(N,M)
V(N,M)
RAD(N,M)
ANG(N,M)
QU(N,M)
QV(N,M)
REST(N,M)
DIR(N,M)
ZM(N,M)
ZST(N,M)
HTZ(N,M)
HTU(N,M)
HTV(N,M)

GRID INDEX(PARALLEL TO ENTRANCE)
GRID INDEX(PERPENDICULAR TO ENTRANCE)
WATER ELEVATION (CM)
U-COMPONENT OF VELOCITY (CM/SEC)
V-COMPONENT OF VELOCITY (CM/SEC)
RESULTANT CURRENT SPEED (CM/SEC)
ANGLE (FROM GEOGRAPHIC NORTH) OF RESULTANT CURRENT
SPEED (THE CURRENT DIRECTION)

FIELDS FOR SUMMATION OF U AND V COMPONENTS OF CURR
ENTS FOR COMPUTATION OF REST CURRENTS
AVERAGE SPEED OF REST CURRENT (CM/SEC)
DIRECTION OF REST CURRENT (IN GEOGRAPHIC COORDINAT
ES)
USED IN J05 AS INTERMEDIATE FOR SMOOTHING
USED IN J05 AS INTERMEDIATE FOR AVERAGING
SYMBOLIC WATER DEPTHS AT WATER ELEVATION (Z) POINT
HTZ = 1- INNER POINT (OVER WATER)
HTZ = 0- OUTER POINT (OVER LAND)
HTZ = -1- NORMAL BOUNDARY POINT
HTZ = -2- POINT ON OPEN (ENTRANCE) BOUNDARY

WATER DEPTH AT U POINTS
WATER DEPTH AT V POINTS
INNER POINT HTU, HTV = DEPTH (CM)
OUTER POINT HTU, HTV = 0
BOUNDARY POINT HTU, HTV = -1
  
```


HGU(N, M)	ACTUAL WATER DEPTH AT U POINTS (HGU = HTU+Z)
HGV(N, M)	ACTUAL WATER DEPTH AT V POINTS (HGV = HTV+Z)
XK(N, M)	U COMPONENT OF WIND CURRENT DIVIDED BY DEPTH
YK(N, M)	V COMPONENT OF WIND CURRENT DIVIDED BY DEPTH
Q(N, M)	FIELDS USED FOR A SPECIAL COMPUTATION (NOT SHOWN
VAC(N, M)	IN THE PROGRAM)
A(I)	CHARACTERISTICS OF THE WIND FIELD
A(1)	TIME WHEN WIND STARTS (SEC)
A(2)	WIND SPEED (M/SEC)
A(3)	WIND DIRECTION (DEGREES COUNTED COUNTERCLOCKWISE
	FROM 0 GRID COORDINATE)
MU(I)	WIND FIELD DELIMITERS (N AND M COORDINATES OF THE
MN(I)	UPPER AND LOWER LEFT CORNERS OF THE WIND FIELD)
NZ(I)	COORDINATES (N, M) OF OPEN (ENTRANCE) BOUNDARY POIN
MZ(I)	TS (I=1, II) SELECTED POINTS (I=12; 24)
NA(I)	COORDINATES (N, M) OF THE BOUNDARY POINTS AT THE SE
MA(I)	COND OPEN BOUNDARY
Z1(I)	AMPLITUDES OF FOUR DIFFERENT TIDAL COMPONENTS AT
Z2(I)	THE OPEN BOUNDARY (CM)
U1(I)	
U2(I)	
Z3(I)	AMPLITUDES OF FOUR DIFFERENT TIDAL COMPONENTS AT
Z4(I)	THE SECOND OPEN BOUNDARY (CM)
U3(I)	
U4(I)	
X(I)	INTERMEDIATE PARAMETERS IN JOB3 AND JOB5 FOR COMPUTA
ARG(I)	TION OF ASTRONOMICAL TIDES AT OPEN (ENTRANCE) BOUN
	DARY
Y(I)	INTERMEDIATE PARAMETERS FOR TIDAL COMPUTATIONS AT
CON(I)	THE OPEN BOUNDARY
V1(I)	NAMES OF SELECTED POINTS
V2(I)	WATER ELEVATION AT SELECTED SPECIAL POINTS
V3(I)	SPEED OF CURRENT AT SPECIAL POINTS
V4(I)	DIRECTION OF CURRENT AT SPECIAL POINTS
AFGN	ARBITRARY PROBLEM NUMBER

F	CORIOLIS PARAMETER (SEC-1)
G	GRAVITY ACCELERATION (CM SEC2)
SIGMA	ANGULAR VELOCITY OF M2 - TIDE (RADIAN/SEC) (USED IN COMPUTATIONS WHERE M2 TIDE ONLY IS ENTERED AT THE OPEN BOUNDARY)
ALPHA	SMOOTHING PARAMETER (USUALLY 0.92 TO 0.99)
R	FRICTIION COEFFICIENT (0.003)
ROL	DENSITY OF THE AIR (GM CM-3) (1-162(X 10-3)
RBETA	COEFFICIENT OF GEOSTROPHIC WIND (JSUALLY 0.65)
C	DRAG COEFFICIENT (3.2X10-6)
DL	1/2 STEP IN SPACE (CM) (1/2 OF GRID SIZE)
DT	1/2 STEP IN TIME (SEC)
T	TIME (SEC)
T1	TIME INTERVAL BETWEEN FIELD PRINTOUTS (SEC)
T2	FIELD OUTPUT COUNT (SEC)
T3	INITIAL TIME COUNT FOR PLOT PROGRAM
ME	INITIAL TIME OF ENTIRE FIELD (THE GRID SIZE) DELIMITERS
TE	END TIME OF COMPUTATION (SEC)
KE	NUMBER OF A(I) (NUMBER OF WIND FIELDS)
KKE	NUMBER OF OPEN (ENTRANCE) BOUNDARY POINTS
IZE	NUMBER OF POINTS AT SECOND OPEN BOUNDARY
NG	TWICE THE NUMBER OF WIND FIELDS
IUE	TIME WHEN THE WIND STARTS (SEC)
ITW	
TIC	COUNTERS
LEN	SUMMATION OF TRANSPORT THROUGH A SPECIFIED SECTION
PCC	
TRAN	
BETA	(1-ALFA) / 4
A1	2(DT)
A2	F(A1)
A3	R(A1)
A4	DT/DL
A5	G(A4)
CI	0 FI NO WIND, ELSE ANY VALUE DIFFERENT THAN 0
CE	C(A(2))X(10000)
NOTE	10000 IS UNIT CONVERSION FACTOR. A(2) IS READ IN AS M/SEC AND MUST BE CHANGED TO CM/SEC AFTER BEING SQUARED
SI	TIME WHEN WIND STOP
NURU	NUMBER OF SELECTED POINTS
NURV	PRINTOUT LINE LINE COUNTER USED IN SOB
JA	INDICATOR JA DIFF. 0 READ INITIAL VALUES JA EQUAL 0 SET Z,U,V=0

INTERMEDIATE PARAMETERS

NE-1
ME-1
NE-2
ME-2

NEH
MEH
NEHH
MEHH

USED IN J05 AS INTERMEDIATE STORAGE LOCATIONS FOR U
AND V VALUES DURING SMOOTHING AND AVERAGING OPERATIO
NS

WERTU
WERTL
WERTR
WERTOL
WERTOR
WERTUL
WERTUR
WURZEL
GRZ

SQRT(ZM**2+ZST**2)
A3(WURZEL)

T3, T4, STV, ETV, I INCV, STH, ETH, T INCH ARE PARAMETERS USED IN THE
PLOTTING PROGRAM

T2 START TIME FOR STORING SPECIAL VALUES ON CYLINDER
T3 USUALLY SET TO ZERO. WHEN JA=1, SET TO STARTING TIME
ETH START TIME FOR PRINTING VALUE ARRAYS HORIZONTALLY
ETV TIME OF THE LAST WATER HEIGHT PLOT
I INCV TIME OF THE LAST VECTOR PLOT HEIGHT PLOT
T INCH TIME INCREMENT BETWEEN WATER HEIGHT PLOTS
STH TIME OF THE FIRST BETWEEN VECTOR PLOTS. MUST BE GREATER
THAN T2 AND LESS THAN (T+T1+T1/2)
STV TIME OF THE FIRST VECTOR PLOT. MUST BE GREATER THAN T2
HT AND LESS THAN (T+T1+T1/2)
VEC PLOT FLAG FOR WATER HEIGHTS
PLOT 0 = DO NOT PLOT
I = PLOT
PLOT FLAG FOR VECTOR PLOTS AND A CONTROL FLAG FOR D01
PLOT 0 = DO NOT PLOT
I = PLOT

NALL COUNT OF THE NUMBER OF PLOTS EXPECTED
TEI TIME SAVED FOR START AND END OF THE PROGRAM

AA1 PROFILES FOR MASS COMPUTATIONS
AA2

THE DATA INPUT CARDS

CARD 1 FORMAT 24I3

JA, NE, ME, IZ, IUE, KKE, NURU, NG

CARD 2 FORMAT 9F8.3

AFGN, G, ALPHA, RBETA, C1

CARD 3 FORMAT 9F8.0

DT, TE, TW, T1, T2, SI, T, T3

DT 102 TIME STEP (SEC)
 TE LENGTH OF THE COMPUTATION
 TW TIME WHEN WIND STARTS
 T1 TIME INTERVAL BETWEEN PRINTPOINTS DESIRED FROM START
 T2 FIELD OUTPUT COUNTER (0 IF OUTPUT OTHERWISE DELAYED
 OF THE COMPUTATION, OTHERWISE ANY OTHER DELAYED
 STARTING TIME, MUST BE GRATER OR EQUAL THAN T+AI
 SI TIME WHEN WIND STOP
 T TIME (INITIALIZED 0. IF PREVIOUS COMPUTATIONS MADE
 AND Z, U, V, READ FROM TAPE, GIVE THE TIME PREVIOUS
 COMPUTATION ENDED.)
 T3 IF PLOT DESIRED, TIME WHEN FIELD APF REQUIRED FOR
 PLOTING

CARD 4 FORMAT 6E12.4

DL, F, SIGMA, R, ROL, C

CARD 5 FORMAT 24I3

NZ, MZ (FIRST BOUNDARY)

CARD 6 FORMAT 24I3

NZ, MZ (SECOND BOUNDARY)

CARD 7 FORMAT 24I3


```

NU, MU
CARD 8      FORMAT 26I3
NA, MA
CARD 9      FORMAT 10A4
V1(I)
CARD 10     FORMAT 9F8.2
A(I)
CARD 11     FORMAT 12F6.0
HTZ
CARD 12     FORMAT 12F6.0
HTU
CARD 13     FORMAT 12F6.0
CARD 14     FORMAT 9F8.3
Z1, Z2, U1, U2
CARD 15     FORMAT 9F8.3
Z3, Z4, U3, U4
CARD 16     FORMAT (A8, 2X, 3F10.0)
HEAD, STV, ETV, TINC
CARD 17     FORMAT (A8, 2X, 3F10.0)
HEAD1, STH, ETH, TINC
Z3( ) Z4( ) TIDE COEFF.
Z5( ) Z6( ) TIDE COEFF.
Z7( ) Z8( ) TIDE COEFF.
Z9( ) Z10( ) TIDE COEFF.
BALAST POINT
PIER N, 2
NAVY PIER
SOUTH BAY

```

SAN DIEGO BAY AREA PROGRAM 1

```

COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZST(53,30),
1 HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HTZ(53,30),XK(53,30),
2 YK(53,30),RAD(53,30),ANG(53,30),Q(53,30)
COMMON/B/A(60),NZ(90),MZ(90),MU(60),Z1(60),Z2(60),V1(60),
1 V2(60),U1(60),U2(60),V3(60),X(4),ARG(4),NA(60),MA(60),
2 Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/ AFGN,F,AA1,AA2
3 G,SIGMA,ALPHA,R,ROL,RBETA,C,DL,DT,T,T1,T2,NE,ME,TE,KKE,IZE,IUE,TW
4 ,BETA,A1,A2,A3,A4,A5,C1,C3,S1,NURJ,NURV,JA,NEH,MEH,NEHH,MEHH,NG
5 ,T3,STV,FTV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TEI
REAL*8 V1
REWIND 1
REWIND 2
REWIND 3
REWIND 8
NALL=0
CALL J02
CALL J03
CALL DB1
IF(JA)2,21,2
21 CONTINUE
CALL J04
CALL DB2
T2=T+1
T=T+A1
CALL J05
IF(T-TE) 3,5,5
3 IF(ABS(T-T2)-A1/2.) 1,1,4
4 GO TO 2
5 CONTINUE
CALL J04
CALL DB2
CALL S08
CALL J06
STOP
END

```



```

715 READ(5,701)(HTV(N,M),M=13,24)
   READ(5,702)(HTV(N,M),M=25,ME)
   CONTINUE
   SET THE MINIMUM DEPTH
   DO 50 N=1,NE
   DO 50 M=1,ME
   IF(HTU(N,M).LT.4..AND..HTU(N,M).GT.0.)HTU(N,M)=4.
   IF(HTV(N,M).LT.4..AND..HTV(N,M).GT.0.)HTV(N,M)=4.
50 CONTINUE

```

PRINT CONTROL DATA

```

1 PRINT 110,AFGN
2 PRINT 112,DT,DL
3 PRINT 113,ALPHA,R
4 IF(C1)2,1,2
5 GO TO 5
6 PRINT 116,TW,ROL
7 PRINT 117,PRTA,C
8 PRINT 3,(A(I),I=1,KKE)
9 IF(IZE)6,6,7
10 GO TO 8
11 PRINT 120,(NZ(I),MZ(I),I=1,IZE)
12 PRINT 125,(NA(I),MA(I),I=1,NG)
13 PRINT 121,(N,N=1,18)

```

PRINT THE FIELDS

```

130, (N, (HTZ(N,M),M=1,18),N=1,NE)
131, (N,N=19,30)
132, (N, (HTZ(N,M),M=19,30),N=1,NE)
133, (N,N=1,18)
130, (N, (HTU(N,M),M=1,18),N=1,NE)
131, (N,N=19,30)
132, (N, (HTU(N,M),M=19,30),N=1,NE)
124, (N,N=1,18)
130, (N, (HTV(N,M),M=1,18),N=1,NE)
131, (N,N=19,30)
132, (N, (HTV(N,M),M=19,30),N=1,NE)

```

WRITING OUT DEPTH GRID AT U, V POINTS SIMULTANEOUSLY

```

PRINT 142,(M,M= 1, 9)

```



```

DO 21 N=1, NE
PRINT 140,(N, (HTZ(N,M), HTU(N,M), M=1, 9))
PRINT 141,(N, (HTV(N,M), M= 1, 9))
CONTINUE
21 PRINT 142,(M, M=10, 18)
DO 22 N=1, NE
PRINT 140,(N, (HTZ(N,M), HTU(N,M), M=10, 18))
PRINT 141,(N, (HTV(N,M), M=10, 18))
CONTINUE
22 PRINT 142,(M, M=19, 27)
DO 23 N=1, NE
PRINT 140,(N, (HTZ(N,M), HTU(N,M), M=19, 27))
PRINT 141,(N, (HTV(N,M), M=19, 27))
CONTINUE
23 PRINT 142,(M, M=28, 30)
DO 24 N=1, NE
PRINT 140,(N, (HTZ(N,M), HTU(N,M), M=28, 30))
PRINT 141,(N, (HTV(N,M), M=28, 30))
CONTINUE
24 BETA=(1.-ALPHA)/4.
A1=2.*DT
A2=F*A1
A3=R*A1
A4=DT/DL
A5=G*A4
C3=C*A1*10000.
AA1=0.
AA2=0.
REWIND 4
WRITE(4) HTZ, V1, NURU, ME, NE
ENDFILE 4
RETURN
END

```


SUBROUTINE J03

J03 READING THE BEGINNING VALUES

```

COMMON/A,Z(53,30),U(53,30),V(53,30),W(53,30),ZST(53,30),
1HSV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HTZ(53,30),XK(53,30),
2YK(53,30),PAD(53,30),ANG(53,30),O(53,30)
COMMON/B/A(60),NZ(90),MZ(90),NJ(60),MJ(60),Z1(60),Z2(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/ AFGN,F,AA1,AA2
3G,SIGMA,ALPHA,R,ROL,RBETA,C,DL,DT,T,I1,I2,NE,ME,TE,KKE,IZE,IJE,TW
4,BETA,A1,A2,A3,A4,A5,C1,C3,SI,NUPU,NURV,JA,NEH,MEH,NEHH,MEHH,NG
5,I3,STV,ETV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TEI
REAL*8 V1
100 FORMAT(9F8.3)
113 FORMAT(18F4.1)
2000 I = ,F10.0, SECONDS,////)

```

CONVERT THE DEPTH'S CHART IN FEET TO CENTIMETERS

```

DO 3 N=1,NE
D3 3 M=1,ME
IF(HTU(N,M).LE.0)GO TO 21
HTU(N,M)=HTU(N,M)*30.48
21 CONTINUE
IF(HTV(N,M).LE.0)GO TO 22
HTV(N,M)=HTV(N,M)*30.48
22 CONTINUE
3 CONTINUE

```

READ CONTINUATION VALUES WHEN PREVIOUS COMPUTATION EXIST

```

IF(JA)2,7,2
2 READ(8) ((Z(N,M),M=1,ME),N=1,NE),
1 ((U(N,M),M=1,ME),N=1,NE),
2 ((V(N,M),M=1,ME),N=1,NE),
3 ((HGU(N,M),M=1,ME),N=1,NE),
4 ((HGV(N,M),M=1,ME),N=1,NE),
5 TEI
WRITE(6,2000)TEI
GO TO 14

```

CLEAN THE ARRAYS

SET INITIAL WATER ELEVATIONS

```

7 DO 12 N=1,NE
DO 12 M=1,ME
Z(N,M)=0.
U(N,M)=0.
V(N,M)=0.
12 CONTINUE

```

SET SMALL VALUES TO PREVENT UNDERFLOW

```

DO 30 N=1,NE
DO 30 M=1,ME
IF(HTZ(N,M))30,30,31.
31 Z(N,M)=0.2
30 CONTINUE
DO 32 N=1,NE
DO 32 M=1,ME
IF(HTU(N,M))24,34,33
33 U(N,M)=0.2
34 IF(HTV(N,M))32,32,35
35 V(N,M)=0.2
32 CONTINUE

```

INITIALIZATION OF ACTUAL DEPTH.

```

15 DO 14 N=1,NE
DO 14 M=1,ME
IF(HTU(N,M))5,5,4
4 HGU(N,M)=HTU(N,M)+(Z(N,M)+Z(N,M+1))/2.
GO TO 13
5 HGV(N,M)=0.
13 IF(HTV(N,M))8,8,6
6 HGV(N,M)=HTV(N,M)+(Z(N,M)+Z(N+1,M))/2.
GO TO 14
8 HGU(N,M)=0.
14 CONTINUE

```

INITIALIZATION OF VARIOUS PARAMETERS

```

DO 10 N=1,NE
DO 10 M=1,ME
Q(N,M)=0.
XC(N,M)=0.
ZST(N,M)=0.
ZM(N,M)=0.
10 YK(N,M)=0.
RETURN
END

```


SUBROUTINE J04

```

J04      WRITING OF THE VALUE FIELDS
COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZSI(53,30),
1HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HTZ(53,30),XK(53,30),
2YK(53,30),RAD(53,30),ANG(53,30),Q(53,30),
COMMON/B/A(60),NZ(90),MU(60),MJ(60),Z1(60),Z2(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/AFGN,F,AA1,AA2
3G,SICMA,ALPHA,R,ROL,RBETA,C,DL,DT,T,T1,T2,NE,ME,TE,KKE,IZE,IUE,TW
4BETA,A1,A2,A3,A4,A5,C1,C3,SI,NURU,NURV,JA,NEH,MEH,NEHH,MEHH,NG
5I3,SIV,ETV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TEL
REAL*8 VI
50  FORMAT(' WROTE(1) SUBROUTINE J04 T = ',F10.0,'T,V2,V3,V4',/)
224  FORMAT(IH1,14X,21HWATER HEIGHT AFTER T =,F9.0,9H SEC (CM)/7X,I7,18I
17//)
228  FORMAT(I(17,18F7.0/))
229  FOPMAT(I(18,3F8.0//))
230  FOPMAT(I(2X,F4.0,1X,F4.0),/)
232  FOPMAT(5(2X,F4.0,1X,F4.0),/)
233  FOPMAT(' SPECIAL POINT WATER ELEVATION SPEED(CM/SEC) DIRECT
1 HIGH CURRENT TIME = ',F10.0,/,10(3X,A8,10X,F8.2,7X,F8.2,8X,F8.2
1,/,/)
298  FORMAT(' 14X,RESULTANT CURRENT VELOCITY MAGNITUDE(CN/SEC)
1 AND DIRECTION(DEGREES) AFTER T = ',F9.0,')
328  FOPMAT(I(17,17F7.0/))
404  FOPMAT(//7X,I7,18I7//)
405  FOPMAT(//8X,I7,2I8)
406  FOPMAT(' ',/,5X,I3,11I11,/,/)
1228 FOPMAT(I(17,12F7.0/))
PRINT OF Z VALUES
PRINT 224,T,(N,N=1,18)
PRINT 228,(N,(Z(N,M),M=1,18),N=1,NE)
PRINT 404,(N,(V=19,30)
PRINT 1228,(N,(Z(N,M),M=19,30),N=1,NE)
PIR=180.73.1415926
COMPUTATION OF CURRENT DIRECTION
DO 432 N=1,NE
DO 432 M=1,ME
IF(V(N,M)**2+U(N,M)**2.EQ.0.)GO TO 101

```



```

100 PAD(N,M)=SQRT(V(N,M)**2+U(N,M)**2)
    GO TO 102
101 RAD(N,M)=0.
    ANG(N,M)=999.
    GO TO 432
102 ABC=ABS(V(N,M))/RAD(N,M)
    ABC1=ABC*(10**10)
    IF(ABC1.LT.0)GO TO 1
    ANG(N,M)=ARSIN(ABC)
    ANG(N,M)=ANG(N,M)*PI
    GO TO 2
1   ANG(N,M)=0.0
2   IF(V(N,M).GE.0..AND.U(N,M).GE.0.)GO TO 433
    IF(V(N,M).GE.0..AND.U(N,M).LT.0.)GO TO 500
    IF(V(N,M).LT.0..AND.U(N,M).LE.0.)GO TO 501
    GO TO 502
500 ANG(H,M)=180.-ANG(N,M)
    GO TO 433
501 ANG(N,M)=180.+ANG(N,M)
    GO TO 433
502 ANG(N,M)=360.-ANG(N,M)
433 ANG(N,M)=90.-ANG(N,M)
432 IF(AUC(N,M).LT.0.)ANG(N,M)=360.+ANG(N,M)
    CONTINUE
DO 10 N=1,NE
DO 10 M=1,ME
    IF(Q(N,M).EQ.0.)GO TO 10
    RAD(N,M)=-1.
    ANC(N,M)=666.
    Q(N,M)=0.
10 CONTINUE

    WRITING THE SPETIAL POINTS
    IF(NURU.EQ.0)GO TO 12
    DO 9 I=1,NURU
    M = MZ(I+IZE)
    N = NZ(I+IZE)
    V2(I)=Z(N,M)
    V3(I)=PAD(N,M)
    V4(I)=ANG(N,M)
    NALL=NALL+1
    WRITE(I)T,(V2(I),I=1,NURU),
1      (V3(I),I=1,NURU),
2      (V4(I),I=1,NURU)
    PRINT 50,T
12 CONTINUE

```


PRINTING OF CURRENTS AND DIRECTION

```
WRITE(6,298) T  
WRITE(6,406) (N, N=1, 12)  
PRINT 230, ((RAD(N, M), ANG(N, M), M=1, 12), N=1, NE)  
WRITE(6,406) (N, N=13, 24)  
PRINT 230, ((RAD(N, M), ANG(N, M), M=13, 24), N=1, NE)  
WRITE(6,406) (N, N=25, ME)  
PRINT 232, ((RAD(N, M), ANG(N, M), M=25, ME), N=1, NE)  
PRINT 233, T, (V1(I), V2(I), V3(I), V4(I), I=1, NURU)  
RETURN  
END
```



```

SUBROUTINE J05
COMPUTATION AND MANIPULATION
COMMON/A,Z(53,30),U(53,30),V(53,30),ZM(53,30),ZST(53,30),
1HSV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),XK(53,30),
2YK(53,30),RAD(53,30),ANG(53,30),Q(53,30),
COMMON/B/A(60),MZ(90),MZ(90),NU(60),NU(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/ AFGN,F,AA1,AA2
3,G,SIGMA,ALPHA,R,ROL,RBETA,C,DL,DT,T,T1,T2,NE,ME,TE,KKE,IZE,IUE,TW
4,BETA,A1,A2,A3,A4,A5,C1,C3,SI,NUPU,NURV,JA,NEH,MEH,MEHH,NG
5,T3,STV,ETV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TFI
REAL*8 VI

```

SET TIDE VALUES AT OPEN BOUNDARIES

```

IF(IZE.EQ.0)GO TO 709
PER=24.833333*3600.
PI = 3.1415927
TT=T+0.
DO 77 I = 1,IZE
N = NZ(I)
M = MZ(I)
SUM=0.
DO 10 L=1,11
ZTIDE=Z3(L)*COS((L)*2.*PI*TT/PER)+Z4(L)*SIN((L)*2.*PI*TT/PER)
SUM=SUM+ZTIDE
10 Z(N,M)=SUM+Z3(12)
77 CONTINUE
172 IE(NG.EQ.0)GO TO 709
DO 78 I=1,NG
N=NA(I)
M=MA(I)
SUM=0.
DO 20 L=1,3
ZTIDE=Z7(L)*COS((L)*2.*PI*TT/PER)+Z8(L)*SIN((L)*2.*PI*TT/PER)
SUM=SUM+ZTIDE
20 Z(N,M)=SUM+Z7(4)
78 CONTINUE

```

CONTINUATION OF Z IN THE OPEN BOUNDARIES

```

709 DO 30 N=6,8
Z(N,4)=Z(N,5)

```


30 CONTINUE

SMOOTHING OF Z VALUES

```

DO 470 N=2,NEH
DO 470 M=2,MEH
IF (HTZ(N,M)) 710,470,75
IF (HTZ(N,M)+2) 470,75,470
710 IF (1-N) 28,6,28
28 IF (HTZ(N-1,M)) 57,6,57
57 WERTO=Z(N-1,M)
GO TO 7

```

```

6 WERTO=Z(N,M)
7 IF (NE-M) 18,9,18
18 IF (HTZ(N+1,M)) 58,9,58
58 WERTU=Z(N+1,M)
GO TO 5

```

```

9 WERTU=Z(N,M)
5 IF (1-M) 29,12,29
29 IF (HTZ(N,M-1)) 59,12,59
59 WERTL=Z(N,M-1)
GO TO 13

```

```

12 WERTL=Z(N,M)
13 IF (ME-M) 17,15,17
17 IF (HTZ(N,M+1)) 60,15,60
60 WERTR=Z(N,M+1)
GO TO 22

```

```

15 WERTP=Z(N,M)
22 ZM(N,M)=ALPHA*Z(N,M)+BETA*(WERTO+WERTU+WERTL+WERTR)
470 CONTINUE

```

```

DO 70 N=2,NEH
DO 70 M=2,MEH
IF ((HGV(N,M).GT.900000.) .OR. (HGU(N,M).GT.900000.)) GO TO 91
IF ((V(N,M).GT.100000.) .OR. (U(N,M).GT.100000.)) GO TO 92
IF (HTZ(N,M)) 70,70,3355

```

CONTINUITY EQUATION FOR COMPUTATION OF Z

```

3355 DHV = HGV(N-1,M)*V(N-1,M)-HGV(N,M)*V(N,M)
355 DHU = HGU(N,M)*U(N,M)-HGU(N,M-1)*U(N,M-1)
361 Z(N,M) = ZM(N,M) - A4*(DHU+DHV)
70 CONTINUE

```

CONTINUATION OF THE OPEN BOUNDARIES

```

DO 71 M=2,23
Z(52,M)=Z(52,M)
71 CONTINUE

```



```

DO 171 N=11,53
Z(N,1)=Z(N,2)
CONTINUE
171 DO 271 N=6,8
Z(N,4)=Z(N,5)-(Z(N,6)-Z(N,5))
271 CONTINUE

ACTUAL DEPTH COMPUTATION

72 DO 82 N=1,NEH
DO 82 M=2,MEH
IF(HTU(N,M))76,76,81
81 HGU(N,M)=HTU(N,M)+(Z(N,M)+Z(N,M+1))/2.
76 IF(HTV(N,M))82,82,87
87 HGV(N,M)=HTV(N,M)+(Z(N,M)+Z(N,M+1,M))/2.
82 CONTINUE
DO 1001 M=2,6
HGU(53,M)=HGU(52,M)
HGV(53,M)=HGV(52,M)
1001 DO 1002 N=43,53
HGU(N,1)=HGU(N,2)
1002 HGV(N,1)=HGV(N,2)
IF(C1.EQ.0.)GO TO 103
IF(I.LT.TW)GO TO 103

```

```

CALL WIND SUBROUTINE
CALL S01

```

```

SMOOTHING OF U

```

```

103 DO 512 N=2,NEH
DO 512 M=2,MEH
IF(HTU(N,M))512,512,128
128 IF(HTU(N-1,M))157,106,157
157 WERTQ=U(N-1,M)
GO TO 118
106 WERTQ=U(N,M)
118 IF(HTU(N+1,M))158,109,158
158 WERTU=U(N+1,M)
GO TO 129
109 WERTU=U(N,M)
129 IF(HTU(N,M-1))159,112,159
159 WERTL=U(N,M-1)
GO TO 117
112 WERTL=U(N,M)
113 IF(ME-M)117,115,117
117 IF(HFU(N,Y+1))160,115,160
160 WERTR=U(N,M+1)

```



```

GO TO 23
WERTR=U(N,M)
ZM(N,M)=ALPHA*U(N,M)+BETA*(WERTO+WERTU+WERTL+WERTR)
AVERAGING OF U
IF(HTV(N-1,M))61,32,61
WERTOL=V(N-1,M)
IF(HTV(N-1,M+1))62,35,62
WERTOR=V(N-1,M+1)
GO TO 36
WERTOL=V(N-1,M+1)
WERTOR=WERTOL
IF(HTV(N,M))63,38,63
WERTUL=V(N,M)
IF(HTV(N,M+1))64,41,64
WERTUR=V(N,M+1)
GO TO 42
WERTUL=V(N,M+1)
WERTUR=WERTUL
ZST(N,M)=(WERTOL+WERTUL+WERTOR+WERTUR)/4.
CONTINUE

```

COMPUTATION OF U

```

DO 412 N=2,NEH
DO 412 M=2,MEH
IF(HTU(N,M))412,412,513
IF(ZM(N,M).EQ.0)GO TO 514
WURZEL=SQRT(ZM(N,M)**2+ZST(N,M)**2)
GRZ=A3*WURZEL
GO TO 515
WURZEL=0.0
GRZ=0.0
IF(HGU(N,M)-GRZ)94,94,702
IF(HTU(N,M)-9999.)14,700,700
ZM(N,M)=ZM(N,M)+A2*ZST(N,M)-A5*(Z(N,M+1)-Z(N,M))
ZM(N,M)=ZM(N,M)+XK(N,M)
ZM(V,M)=(1.-GRZ/HGU(N,M))*ZM(N,M)-A5*(Z(N,M+1)-Z(N,M))
1+XK(N,M)
GO TO 412
O(N,M)=1.
CONTINUE

```

AVERAGING OF U

```

DO 528 N=1,NEH
DO 528 M=2,MEH
IF(HTV(N,M))528,528,429

```



```

429 IF(HTU(N,M-1))65,44,65
65 WERTOL=U(N,M-1)
66 IF(HTU(N+1,M-1))66,46,66
66 WERTUL=U(N+1,M-1)
GO TO 47
44 WERTOL=U(N+1,M-1)
46 WERTUL=WERTOL
47 IF(HTU(N,M))67,49,67
67 WERTOR=U(N,M)
68 IF(HTU(N+1,M))68,52,68
68 WERTUP=U(N+1,M)
GO TO 53
49 WERTOP=U(N+1,M)
52 WERTUP=WERTOR
53 ZST(N,M)=(WERTOL+WERTUL+WERTOR+WERTUR)/4.
528 CONTINUE

```

SMOOTHING OF V

```

4101 DO 4100 N=2,NEH
4100 M=2,MEH
IF(HTU(N,M))4100,4100,4101
U(N,M)=ZM(N,M)
CONTINUE
DO 431 N=1,NEH
431 M=2,MEH
IF(HIV(N,M))431,431,432
432 IF(1-N)228,206,228
228 IF(HTV(N-1,M))257,206,257
257 WERTC=V(N-1,M)
GO TO 218
206 WERTO=V(N,M)
218 IF(HTV(N+1,M))258,209,258
258 WERTU=V(N+1,M)
GO TO 229
209 WERTU=V(N,M)
229 IF(HTV(N,M-1))259,212,259
259 WERTL=V(N,M-1)
GO TO 217
212 WERTL=V(N,M)
217 IF(HTV(N,M+1))260,215,260
260 WERTR=V(N,M+1)
GO TO 25
215 WERTR=V(N,M)
25 ZM(N,M)=ALPHA*V(N,M)+BETA*(WERTO+WERTU+WERTL+WERTR)
431 CONTINUE

```

COMPUTATION OF V


```

DO 428 N=2, NEH
DO 428 M=2, MEH
IF (HTV(N,M)) 428, 428, 529
IF (ZM(N,M).EQ.0.AND.ZST(N,M).EQ.0) GO TO 530
WURZEL=SQRT(ZM(N,M)**2+ZST(N,M)**2)
GRZ=A3*WURZEL
GO TO 531
WURZEL=0.0
GRZ=0.0
531 IF (HGV(N,M)-GRZ) 300, 300, 703
703 IF (HTV(N,M)-0999.) 415, 701, 701
701 V(N,M) = ZM(N,M)-A2*ZST(N,M)-A5*(Z(N,M)-Z(N+1,M)) +YK(N,M)
415 V(N,M)= (1.-GRZ/HGV(N,M))*ZM(N,M)-A2*ZST(N,M)-A5*(Z(N,M)-Z(N+1,M)) +
1 YK(N,M)
GO TO 428
300 Q(N,M)=1.
428 CONTINUE

```

COMPUTATION OF MASS TRANSPORT

```

11 IF (I-I2) 400, 5250, 5250
5250 IF (T-ETH) 5251, 5251, 400
5251 AA1=AA1+(U(3,10)*HTU(3,10)*A1**2**DL+
1 U(4,10)*HTU(4,10)*A1**2**DL+
1 U(5,10)*HTU(5,10)*A1**2**DL+
1 U(6,10)*HTU(6,10)*A1**2**DL+
1 U(7,10)*HTU(7,10)*A1**2**DL+
1 U(8,10)*HTU(8,10)*A1**2**DL)/1000000.
AA2=AA2-(V(34,14)*HTV(34,14)*A1**2**DL+
1 V(34,15)*HTV(34,15)*A1**2**DL+
1 V(34,16)*HTV(34,16)*A1**2**DL+
1 V(34,17)*HTV(34,17)*A1**2**DL+
1 V(34,18)*HTV(34,18)*A1**2**DL)/1000000.
400 RETURN
91 PRINT 1
92 PRINT 2, T, N, M, ERROR, HGU
1 FORMAT (IX, 9HEPROR, V)
2 FORMAT (IX, 7HEPROR, V)
3 FJRMAT (F11.0, 5X, IH(, I2, 1H, , I2, 2H) )
END

```


SUBROUTINE S01

```

S01 VARIABLE WIND IN SUBAREAS, INTERMITANTLY
COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZSI(53,30),
1 HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HK(53,30),
2 YK(53,30),RAD(53,30),ANG(53,30),O(53,30)
3 COMMON/B/A(60),NZ(90),NU(60),MU(60),Z1(60),Z2(60),V1(60),
4 V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
5 Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
6 COMMON/C/AFGN,F,AA1,AA2
7 SIGMA,ALPHA,R,ROL,BETA,C,DL,DT,T,I1,T2,NE,ME,TE,KK5,IZE,IUE,TW
8 BETA,A1,A2,A3,A4,A5,C1,C3,SI,NURU,NURV,JA,NFH,MEH,NEHH,MEHH,NG
9 T3,SV,ETV,STH,ETH,TINCH,HT,VEC,NALL,TEI
10 REAL*8 V1
11 IF(SI-T)12,10,2
12 KF=IUE/2
13 DO 9 I=1,KF
14 IF(T-A(I))9,4,9
15 N1=MU(2*I-1)
16 N2=MU(2*I)
17 M1=MU(2*I-1)
18 M2=MU(2*I)
19 DO 8 N=N1,N2
20 DO 8 M=M1,M2
21 IF(T-A(I))9,4,4
22 DO 8 N=1,NE
23 DO 8 M=1,ME
24 IF(HGU(N,M))1,1,5
25 IF(HGV(N,M))1,1,5
26 XK(N,M)=C3*A(8,8)
27 IF(HTV(N,M))8,8,6
28 IF(HCV(N,M))8,8,7
29 YK(N,M)=C3*A(2,2)**2*SIN(A(3)*0.017453)/2000.
30 CONTINUE
31 YK(N,M)=C3*A(2,2)**2*COS(A(3)*0.017453)/2000.
32 CONTINUE
33 GO TO 12
34 DO 11 N=1,NE
35 DO 11 M=1,ME
36 XK(N,M)=0.
37 YK(N,M)=0.
38 RETURN
39 END

```

for differences

SUBROUTINE S08

S08 OUTPUT FOR SPECIAL POINTS

```

COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZST(53,30),
1HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HTZ(53,30),XK(53,30),
2YK(53,30),RAD(53,30),ANG(53,30),Q(53,30)
COMMON/R/A(60),NZ(90),MZ(90),NU(60),MJ(60),Z1(60),Z2(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/ AECN,F,AAL,AA2
3,C,SIGMA,ALPHA,R,RCL,RBETA,C,CL,DT,T,T1,T2,ME,ME,TE,KKF,IZF,IUE,TW
4,BETA,A1,A2,A3,A4,A5,C1,C3,SI,NURU,NURV,JA,NEH,MEH,NEHH,MEHH,NG
5,I3,SIV,FTV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TE1
DEAL#8 V1
130 FORMAT(/,7X,4HNAME,4X,15(2X,A6)/15X,14(2X,A6)/)
131 FORMAT(1H1,5X,114HWATER ELEVATION(CM) AND CURRENT VELOCITY RESULTS
1INT(MAGNITUDE IN CM/SEC AND DIRECTION IN DEGREES) AT SPECIAL POINTS
2//7X,4HNAME,4X,15(2X,A6)/15X,14(2X,A6)/)
132 FORMAT(6X,5HCOORD,4X,15(2X,I2,1H,I2,1X)/15X,14(2X,I2,1H,I2,1X)//
1)
133 FORMAT(' TIME OF COMPUTATION = ',F10.0,' SECONDS',/,6X,'HFIGHT
1',4X,14F8.2/14X,14F8.2//)
134 FORMAT(5X,14HEND OF PROGRAM,////////)
135 FORMAT(' VELOC,DIP',2X,F7.0,1H,F4.0,14(F4.0,1H,,F4.0)//
114X,14(F4.0,1H,,F4.0)/)
TE1=I
NURV=0
PRINT 131,(V1(I),I=1,NURU)
PRINT 132,(NZ(I+IZE),MZ(I+IZE),I=1,NURU)
ENDIF 1
REWIND 1
1 READ(1),I=1,NURU),
1 (V2(I),I=1,NURU),
2 (V3(I),I=1,NURU),
(V4(I),I=1,NURU)
NURV=NUPV+1
IF(NURV-50)3,3,4
4 PRINT 130,(V1(I),I=1,NURU)
3 NURV=1
PRINT 133,I,(V2(I),I=1,NURU)
PRINT 135,(V3(I),V4(I),I=1,NURU)
WRITE(?,I,(V2(I),I=1,NURU)
,(V3(I),I=1,NURU)
,(V4(I),I=1,NURU)
1
2 IF(I-I)2,2,1
2 ENDFILE 2
PRINT 134
RETURN

```


END

SUBROUTINE DB1

```
COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZST(53,30),
1HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HZ(53,30),XK(53,30),
2YK(53,30),RAD(53,30),ANG(53,30),O(53,30)
COMMON/B/A(60),NZ(90),AMZ(90),NU(60),MU(60),Z1(60),Z2(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/ AFGN,F,AA1,AA2
3,G,SIGMA,ALPHA,R,ROL,RBETA,C,DL,DT,T,I1,T2,ME,ME,TE,KKE,IZE,IUF,TW
4,BETA,AL1,A2,A3,A4,A5,C1,C3,SI,NURV,J,A,NEH,MEH,NEHH,MEHH,NG
5,I3,STV,FTV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TEI
REAL*8 VI
REAL*8 HEAD,HEAD1
111 FORMAT(' CHECK PARAMETERS IN DB1 ',/,'STH = ',F7.0)
1 I = 1, F7.0, I1 = 1, F7.0, STV = 1, F7.0
400 FORMAT(' WRITE (3) SUBROUTINE DB2 T = ',F10.0,'T,VEC,HT,RAD,ANG,Z
1',/,')
401 FORMAT(' MASS TRANSPORT AT T = ',F10.0,'DURING THE LAST HOUR PE
1R',/,') AA1 = F10.2, M3/HOUR
1000 FORMAT(A8,2X,3F10.0)
1001 FORMAT(//,20X,A8,2X,3F10.0)

ENTRY TO READ VECTOR + HEIGHT CARDS

READ 1000,HEAD,STV,FTV,TINCV
READ 1000,HEAD1,STH,ETH,TINCH
PRINT 1001,HEAD,STV,FTV,TINCV
PRINT 1001,HEAD1,STH,ETH,TINCH
RETURN

ENTRY TO WRITE DATA IN DISK FILE 3 FOR VVECTOR AND WATER HEIGHT
PLOTS

ENTRY DB2
HT=0.
VEC=0.
WRITE(6,111)T,I1,STV,STH
IF(ABS(T-STV).GT.11/2.)GO TO 100
STV=STV+TINCV
VEC=1.
100 IF(ABS(T-STH).GT.11/2.)GO TO 200
STH=STH+TINCH
HT=1.
```



```

200 IF(HT+VEC.EQ.0.)GO TO 300
WRITE(3) T,VEC,HT,RAD,ANG,Z
WRITE(6,400) T
PRINT 401,T,AA1,AA2
AA1=0.
AA2=0.
RETURN
300 END

```

SUBROUTINE J06

SOBRROUTINE FOR WRIGTING IN TAPES FOR FUTURE USES OF COMPUTATIONS

```

COMMON/A/Z(53,30),U(53,30),V(53,30),ZM(53,30),ZSI(53,30),
1HGV(53,30),HGU(53,30),HTU(53,30),HTV(53,30),HTZ(53,30),XK(53,30),
2YK(53,30),RAD(53,30),ANG(53,30),O(53,30)
COMMON/R/A(80),NZ(90),MZ(90),NU(60),MJ(60),Z1(60),Z2(60),V1(60),
1V2(60),U1(60),U2(60),V3(60),V4(60),X(4),ARG(4),NA(60),MA(60),
2Z3(12),Z4(12),Z5(8),Z6(8),Z7(8),Z8(8),Z9(8),Z10(8)
COMMON/C/AEGN,F,AA1,AA2
3,G,SIGMA,ALPHA,R,RPOL,BETA,C,DL,DT,T,T1,T2,NE,ME,TE,KKE,IZE,IUE,TW
4,BETA,A1,A2,A3,A4,A5,C1,C3,SI,NURJ,NURV,JA,NEH,MEH,NEHH,MEHH,NG
5,I3,STV,ETV,TINCV,STH,ETH,TINCH,HT,VEC,NALL,TEI
PEAL*8 V1
ENDFILE 3
REWIND 2
REWIND 3
REWIND 4
REWIND 8
REWIND 9
READ(4) HTZ,V1,NURU,ME,NE
WRITE(9)HTZ,V1,NURU,ME,NE,NALL

```



```

11 PRINT 11
12 FORMAT(1,T) WRITE (9) SUBROUTINE J06 HTZ,V1,NURU,ME,NE,NALL,/)
WRITE(2) T,(V2(I),I=1,NURU),(V3(I),I=1,NURU),(V4(I),I=1,NURU)
WRITE(9) T,(V2(I),I=1,NURU),(V3(I),I=1,NURU),(V4(I),I=1,NURU)
10 PRINT 10,T WRITE (9) SUBROUTINE J06 T =',F10.0,'T,V2,V3,V4',/)
FORMAT(1,4,2)
14 IF(TE-T)4,VFC,HT,RAD,ANG,Z
4 READ(3) T,VEC,HT,RAD,ANG,Z
WRITE(9) T,VEC,HT,RAD,ANG,Z
12 PRINT 12,T WRITE (9) SUBROUTINE J06 T =',F10.0,'T,VEC,HT,RAD,ANG,Z
FORMAT(1,5,4)
1 IF(TE-T)5,(Z(N,M),M=1,ME),N=1,NE),
5 WRITE(8) ((U(N,M),M=1,ME),N=1,NE),
1 ((V(N,M),M=1,ME),N=1,NE),
2 ((HGU(N,M),M=1,ME),N=1,NE),
3 ((HGV(N,M),M=1,ME),N=1,NE),
4 TFI
1 PRINT 1,TEI
FORMAT(1,1,SECONDS,/) PARTIAL RESULTS HAD BEEN WRITTEN IN TAPE 8 AT TIME
1',F10.0,SECONDS,/)
6 PRINT 6,NALL - NUMBER OF PLOT ORDERED = ',I3,/)
FORMAT(1,8)
ENDFILE 8
REWIND 8
ENDFILE 9
REWIND 9
RETURN
END

```

HANSEN PROGRAM PLOTS

PLOTS OF TIDE AND VELOCITY CURVES

CARD 1

THMIN
THMAX
YPN
XPN
SKIP

MINIMUM VALUE OF WATER HEIGHT ON Y AXIS SCALE
MAXIMUM VALUE OF WATER HEIGHT ON Y AXIS SCALE
SCALE OF Y AXIS IN UNITS/INCH
SCALE OF TIME AXIS IN UNITS/INCH
NO. OF TIME STEPS TO BE SKIPPED OVER BETWEEN PLOTTED PO

CARD 2

TMIN
TMAX
TINC
TLEN
XPN
YPN
ZPN

START TIME OF FIRST WATER HEIGHT VECTOR PLOT
START TIME OF LAST WATER HEIGHT VECTOR PLOT
TIME INTERVAL BETWEEN START TIMES
TIME INTERVAL TO BE PLOTTED
TIME AXIS SCALE IN UNITS/INCH
WATER HEIGHT SCALE UNIT/INCH (MIN. QMAX VALUES ARE
THOSE ON THE TIDE CARD CYCLE)
VECTOR SCALE IN UNITS/INCH

MAIN PROGRAM

```

COMMON/A/ V1(60), V2(60), V3(60), V4(60), HTZ(53,30), RAD(53,30),
1 ANG(53,30), Z(53,30), X(3), Y(3), NURU, ME, NE, T, VEC, HT
REAL*8 V1
REWIND 2
REWIND 3
REWIND 4
REWIND 9
READ(9) HTZ, V1, NURU, ME, NE, NALL
PRINT 11, NALL, NURU
11 FORMAT( ' ', I3, /) HTZ, V1, NURU, ME, NE, NALL, NALL = ' , I3, '
1 NURU = ' , I3, /)
PRINT 1, ((HTZ(N,M), M=1,20), N=1, NE)
PRINT 7, ((HTZ(N,M), M=21, ME), N=1, NE)
PRINT 2, (V1(I), I=1, NURU)
PRINT 3, ME, ME
PRINT 4, NURU
1 FORMAT(20F6.1)
2 FORMAT(10A10)
3 FORMAT( ' ', I2, ' ', I2, ' ', /)
4 FORMAT( ' ', I2, ' ', /)
DO 5 K=1, NALL
READ(9) T, (V2(I), I=1, NURU), (V3(I), I=1, NURU), (V4(I), I=1, NURU)
WRITE(2) T, (V2(I), I=1, NURU), (V3(I), I=1, NURU), (V4(I), I=1, NURU)
WRITE(3) T, (V2(I), I=1, NURU), (V3(I), I=1, NURU), (V4(I), I=1, NURU)
PRINT 20, T
20 FORMAT( ' ', T, V2, V3, V4, AT T = ' , F10.0, /)
PRINT 21, (V2(I), V3(I), V4(I), I=1, NURU)
31 FORMAT( ' ', I0X, 'V3(I)', I0X, 'V4(I)', /, 5X, 3F10.0, /)
5 CONTINUE
DO 6 I=1, NALL
READ(9) T, VEC, HT, RAD, ANG, Z
WRITE(4) T, VEC, HT, RAD, ANG, Z
PRINT 12, T
12 FORMAT( ' ', T, VEC, HT, PAD, ANG, Z, AT T = ' , F10.0, /)
PRINT 1, ((RAD(N,M), M=1,20), N=1, ME)
PRINT 7, ((RAD(N,M), M=21, ME), N=1, NE)
PRINT 1, ((ANG(N,M), M=1,20), N=1, NE)
PRINT 7, ((ANG(N,M), M=21, ME), N=1, NE)
PRINT 1, ((Z(N,M), M=1,20), N=1, NE)
PRINT 7, ((Z(N,M), M=21, ME), N=1, NE)
6 CONTINUE
ENDFILE 2
ENDFILE 3
ENDFILE 4

```



```

REWIND 2
REWIND 3
REWIND 4
REWIND 9
PRINT 101, NURU, ME, NE, T, VEC, HT
FORMAT(, NURU, ME, NE, T, VEC, HT BEEFORE PASSED TO SUBROUTINE T01', /)
101 1, 10X, I5, I5, I5, F10.0, F10.0, F10.0, /)
CALL T01
CALL TEST(NALL, NURU)
STOP
END

```



```

SUBROUTINE T01
COMMON/A/ V1(60), V2(60), V3(60), V4(60), V4(60), HTZ(53,30), RAD(53,30),
1 ANGC(53,30), Z(53,30), X(3), Y(3), NUPU, ME, NE, T, VEC, HT
DIMENSION VV2(10000), VV3(10000), VV4(10000), TT(1500)
REAL*8 V1
DIMENSION VV2(10000), VV3(10000), VV4(10000), TT(1500)
COMPUTE UPPER BOUNDS OF STORAGE AREA. DATA WILL BE STORED IN
THE FOLLOWING ORDER; AREA(TIME, NURU)
KK = 10000/NURU
CALL PLOTS
PRINT 9000, NURU, ME, NE, T, VEC, HT
KK = 10000/NURU
READ TYPE CYCLE CARD
PEAD 1000, THMIN, THMAX, YPN, XPN, SKIP
PRINT 1001, THMIN, THMAX, YPN, XPN, SKIP
M=SKIP
DO 110 I = 1, KK
KKK = (NURU-I)*KK+I
1 READ(2, END=200) TT(I), (VV2(J), J=I, <KK, KK), (VV3(J), J=I, KKK, KK),
150 (VV4(J), J=I, KKK, KK)
PRINT 8000, I, TT(I)
IF (M.EQ.0) GO TO 110
DO 100 J=1, M
READ(2, END=210)
CONTINUE
110 CONTINUE
KKK=KK
GO TO 250
KKK=I-1
GO TO 250
KKK=I
READ IDEVECTOR CARD
READ 1000, TMIN, TMAX, TINC, TLEN, XPN, YPN, ZPN
250 PRINT 1002, TMIN, TMAX, TINC, TLEN, XPN, YPN, ZPN
PLCT WATER HEIGHTS FOR ENTIRE RUN FOR EACH SPECIAL POINT
DO 300 I = 1, NURU
K = K*(I-1)+1
300 CALL TIMPL (TT, VV3(K), VV4(K), VV2(K), KKK, V1(I), 10, XPN, THMIN, YPN,
350 THMAX, 0, ZPN, I, TT, TT(KKK), .07, 7200.)
DO 400 M=1, KKK
IF (TT(M).GE. TMIN) GO TO 500
400 CONTINUE
M=KKK
GO TO 900
500 TIMFND = THIN+TLEN
DO 600 J = M, KKK
IF (TIMFND .LT. TT(J)) GO TO 700
600 CONTINUE

```



```

J=KKK+1
700 PRINT 9999, J, M, KKK, TMIN, TIMEND, TT(M), TT(J)
J = J-M
DO 800 I = 1, NURU
K = KK*(I-1)+M
800 CALL TIMPL (TT(M), VV3(K), VV4(K), VV2(K), J, V1(I), 8, XPN, THMIN, YPN,
1 THMAX, I, ZPN, 0, TT(M), TT(M)+TLEN, .07, 7200.)
TIMIN=TIMIN+TTINC
IF( TIMIN.LT. TMAX) GO TO 350
900 CALL PLOTE
RETURN
1000 FFORMAT (10X, 7F10.0)
1001 FFORMAT (, 7F10.0, /)
1002 FFORMAT (, 7F10.0)
8000 FFORMAT (, READ 2, TT(, I2, ,) = , F10.0, /)
9000 FFORMAT (, NURU, ME, NE, T, VFC, HT PASSED TO THE SUBROUTINE T01: , /)
110X, I5, I5, F10.0, F10.0, /)
9999 FFORMAT (3I10, 4F10.0)
END

```



```

SUBROUTINE TIMPL (TIME, VELOC, DIREC, HEIGHT, MAXDIM, PLNAM, N, XPN,
1 THMIN, YPN, THMAX, SKIP, ZPN, NAROW, TST, TEND, H, TINC)
INTEGER SKIP
REAL*8 VI
DIMENSION (1), NAM1(4), NAM2(3), NAM3(9)
1 DATA NAM1/,'TIME', 'IN', 'SECO', 'NDS', /
DATA NAM2/'HEIG', 'HT I', 'N CM', /
DATA NAM3/'L.SA', 'LAS', 'HA', 'NSEN', 'MOD', 'EL', 'SAN', 'DIEG',
1:0(I), /
X = (TEND-TST)/XPN
CALL PLOT (0, 0, 3)
PX = X/2 - 6.7 * H * FLOCAT(N)
CALL SYMBOL (PX, -1, H*2, NAM3, 0, 0, 37)
CALL SYMBOL (PX, -5, H*2, PLNAM, 0, 0, N)
CALL CXIS2 (TST, 25, NAM1,
1 XPN, XPN, 6, TEND, 6, -1, .07)
ZERLIN = THMIN/YPN
CALL PLOT (X, ZERLIN, 3)
CALL PLOT (0, 0, ZERLIN, 2)
CALL CXIS2 (TST, THMIN, NAM2,
1 270, THMIN, YPN, 50, 4, THMAX, 4, -1, .07)
DUM1 = (TIME(I) - TST) / XPN
DUM2 = (HEIGHT(I) - THMIN) / YPN
DP 300 I = 1, MAXDIM
CALL PLOT (DUM1, DUM2, 3)
Y = (HEIGHT(I) - THMIN) / YPN
X = (TIME(I) - TST) / XPN
IF (SKIP.NE.0) GO TO 210
CALL PLOT (X, Y, 3)
200 GO TO 215
CALL PLOT (X, Y, 2)
210 IF (NAPW.EQ.0) GO TO 300
215 DIST = VELOC(I) / ZPN
IF (DIPEC(I) .GT. 360.) GO TO 300
SI = AMOD ( 450.0 - DIPEC(I)
CC = COS(SI)
SI = SIN(SI)
VX = DIST * CO + X
VY = DIST * SI + Y
CALL PLOT (VX, VY, 2)
CALL ARWPT (VX, VY, CO, SI)
IF (SKIP.EQ.0) GO TO 300
CALL PLOT (X, Y, 3)
CONTINUE
250 CALL PLOT (0, Y+6., -3)
300 RETURN
END

```

, 360.) * .0174532925


```

SUBROUTINE CXIS2 (X,Y,XNAME,NLET,XMIN,XPN,YMIN,YPN,THETA,
1 ZVAL,ZPN,ZINT,ZNUM,ZMAX,NC,NS,H)
REAL*8 V1 XNAME(2)
DIMENSION XNAME(2)
XX = THETA*.0174532925
SI = -SIN(XX)
CO = COS(XX)
XINT = CO*ZINT/ZPN
YINT = SI*ZINT/ZPN
XTIC = SI*.05
YTIC = CO*.05
YY = H*1.5
XX = 3./7.*H*FLOAT(NC)
XLET = -SI*YY-CO*XX
YLET = -CO*YY+SI*XX
XLI = ZNUM*XINT
YLI = ZNUM*YINT
XX = 6./7.*H*FLOAT(NLET)
YY = H*5
XTIT = SI*YY-CO*XX
YTIT = -CO*YY+SI*XX
XX = (X-XMIN)/XPN
YY = (Y-YMIN)/YPN
CENT = ZVAL+(ZMAX-ZVAL)/2.
XTIT = XX+XTIT+(CENT-ZVAL)/ZPN*CO
YTIT = YY+YTIT+(CENT-ZVAL)/ZPN*SI
Z=ZVAL
ZZ=Z
CALL PLOT (XX,YY,3)
XLET = XLET+XX
YLET = YLET+YY
100 IF( NC.LE.0.OR. ABS(ZZ-Z).GT.ZINT/2.)
CALL NUMBER (XLET,XLI
XLET = XLET+XLI
YLET = YLET+YLI
200 ZZ = ZZ+ZNUM*ZINT
CALL PLOT (XX,YY,3)
XX = XX+XINT
YY = YY+YINT
ZZ = ZZ+ZINT
CALL PLOT (XX,YY,2)
IF (Z.GE.ZMAX) GO TO 500
CALL PLOT (XX+XTIC,YY+YTIC,2)
CALL PLOT (XX,YY,2)
IF (Z.GT.CENT .AND. NLET.GT.0)GO TO 400
GO TO 200

```



```

400 GO TO 100
    CALL SYMBOL (XTIIT, YTIIT, H*2., XNAME, THETA, NLET)
    CALL PLOT (XX, YY, 3)
    CENT = 3.*ZMAX
    GO TO 100
500 IF (NC.LE.0 .OR. ZZ.NF.Z) RETURN
    CALL NUMBER (XLET, YLET, H, ZZ, THETA, NS)
    RETURN
END

```

```

SUBROUTINE ROT(X, Y, DEG, MM)
DIMENSION X(MM), Y(MM)
SI = DEG*0.01745329
CC = COS(SI)
SI = SIN(SI)
DO 100 I = 1, MM

```



```

X1=X(I)
Y1=Y(I)
X(I) = Y1*CO + X1*SI
Y(I) = Y1*CO - X1*SI
100 RETURN
END

```

```

SUBROUTINE ARWPT (X,Y,CO,SI)
REAL*8 V1
DATA H/.07/
YY = SI*H
XX = CO*H
XXY=YY*.25
YYX=XX*.25
XX=X-XX
YY=Y-YY
CALL PLOT (XX-XXX,YY+YYY,2)
CALL PLOT (XX+XXX,YY-YYY,2)
CALL PLOT (X,Y,2)
CALL PLOT (X,Y,3)
RETURN
END

```

```

SUBROUTINE TEST(NALL,NURU)
DIMENSION VA2(50,50),VA3(50,50),V2(50),VD3(50),V2(50),V3(50),V4(5
10),VE2(50),VE3(50),TA(50)
REAL*8 NAME
REAL*8 V1
COMMON/C/ VR2(8),VB3(16),VC2,VC3,TB

```



```

REAL#8 ITATLF(12)/,VALUES 0,,F WATER,,HEIGHT M,,EASSURE,,D AN
ID CA,,LCULATED,,
2DIEG,,O BAY( )//
REAL#8 ITETLE(12)/,VALUES 0,,F CJRREN,,T M,,EASSURE,,D AN
ID CA,,LCULATED,,
2DIEG,,O BAY( )//
REAL#8 LABEL(2)/8HMSSURED ,8HMSSURED /
REAL* 8 LABEL(2)/8HMODEL ,8HMODEL /
DO 1 I=1,NALL
READ(3) I,(V2(K),K=1,NURU),(V3(K),K=1,NURU),(V4(K),K=1,NURU)
PRINT 600,T
TA(I)=T
DO 2 K=1,NURU
VA2(I,K)=V2(K)
VA3(I,K)=V3(K)
IF(V4(K).GT.180.)VA3(I,K)=-VA3(I,K)
2 CONTINUE
DO 3 K=1,NURU
CALL RECI
READ 21,NAME
DO 4 I=1,NALL
TB=TA(I)
CALL REC2
VD2(I)=VC2
VD3(I)=VC3
VE2(I)=VA2(I,K)
VE3(I)=VA3(I,K)
4 CONTINUE
CALL DRAW(NALL,TA,VD2,1,0,LABEL,ITATLE,0.0,0.0,0.0,4,2,2,2,8,8,1,LAST)
PRINT 750,NAME
PRINT 900,LAST
CALL PLOT(0,0,0,3)
CALL SYMBOL(3,0,0,5,0.14,NAME,0.0,8)
CALL PLOT(0,0,-3)
CALL DRAW(NALL,TA,VE2,3,1,LEBEL,ITATLE,0.0,0.0,0.0,4,2,2,2,8,8,1,LAST)
PRINT 750,NAME
PRINT 900,LAST
CALL DRAW(NALL,TA,VD3,1,0,LABEL,ITETLE,0.0,0.0,0.0,4,2,2,2,8,8,1,LAST)
PRINT 750,NAME
PRINT 900,LAST
CALL PLOT(0,0,0,3)
CALL SYMBOL(3,0,0,5,0.14,NAME,0.0,8)
CALL PLOT(0,0,-3)
CALL DRAW(NALL,TA,VE3,3,1,LEREL,ITETLE,0.0,0.0,0.0,4,2,2,2,8,8,1,LAST)
PRINT 750,NAME
PRINT 900,LAST
3 CONTINUE

```



```

21 RETURN
600 FORMAT (A8)      READED IN TEST DISC(3)  T = ,F10.0,/)
750 FORMAT(,A8,/)
900 FORMAT(,I1,/)
END

```

```

SUBROUTINE REC
COMMON/C/ VB2(8), VB3(16), VC2, VC3, TB
ENTRY REC1
READ 20, (VB2(I), I=1,6), VB2(7)
READ 20, (VB3(I), I=1,3)
READ 20, (VB3(I), I=4,6), VB3(7)
GO TO 10
ENTRY REC2
PER=24.*3600.
PI=3.1415927
TB=TB+39800.
SUM=0.
DO 1 L=1,3
ZTIDE=VB2(L)*COS((L)*2.*PI*TB/PER)+VB2(L+3)*SIN((L)*2.*PI*TB/PER)
1+VB2(7)
1 SUM=SUM+ZTIDE
VC2=SUM
SUM=0.
DO 2 L=1,3
ZCURR=VB3(L)*COS((L)*2.*PI*TB/PER)+VB3(L+3)*SIN((L)*2.*PI*TB/PER)
1+VB3(7)
2 SUM=SUM+ZCURR
VC3=SUM
10 RETURN
20 FORMAT (8F10.5)
END

```

HANSEN PROGRAM PLOTS

GPPI GRID POINTS PER INCH ON VECTOR AND HEIGHT PLOTS
 VVS VELOCITY VECTOR SCALE UNITS/INCH
 WWS WATER HEIGHT SCALE
 ROT DEG RIGHT ANGLE FROM NORTH TO Y AXIS OF HANSE PROG GRID
 NS NO. OF STRIPES
 X(I), I=1,3 STRIP ORIGIN IN TENS OF GRID POINTS
 NTHPT DISTANCE BETWEEN PLOTTED POINTS
 LAND DISTANCE FROM LAND

CARD 2

TITLE OF THE PROGRAM

CARD 3

THMIN MINIMUM VALUE OF WATER HEIGHT ON Y AXIS SCALE
 THMAX MAXIMUM VALUE OF WATER HEIGHT ON Y AXIS SCALE
 YPN SCALE OF Y AXIS IN UNITS/INCH
 XPN SCALE OF TIME AXIS IN UNITS/INCH
 SKIP NO. OF TIME STEPS TO BE SKIPPED OVER BETWEEN PLOTTED PO

CARD 4

TMIN START TIME OF FIRST WATER HEIGHT VECTOR PLOT
 TMAX START TIME OF LAST WATER HEIGHT VECTOR PLOT
 TINC TIME INTERVAL BETWEEN START TIMES
 TLEN TIME INTERVAL TO BE PLOTTED
 XPN TIME AXIS SCALE IN UNITS/INCH (MIN.QMAX VALUES ARE
 YPN WATER HEIGHT SCALE UNIT/INCH (MIN.QMAX VALUES ARE
 ZPN THOSE ON THE TIDE CARD CYCLE)
 VECTOR SCALE IN UNITS/INCH

COMMON/A, V1(60), V2(60), V3(60), V4(60), HTZ(53,30), RAD(53,30),
 IANG(53,30), Z(53,30), X(3), Y(3), NURU, ME, NE, T, VEC, HT
 REAL*8 V1
 REWIND 2
 REWIND 3
 REWIND 4
 REWIND 9
 READ(9) HTZ, V1, NURU, ME, NE, NALL
 PRINT 11, NALL, NURU


```

SUBROUTINE P01
COMMON/A/ V1(60), V2(60), V3(60), V4(60), HTZ(53,30), RAD(53,30),
1  COMON(53,30), Z(53,30), X(3), Y(3), NURU, ME, NE, T, VEC, HT
DIMENSION SMBOL(3), TITLE(20), XCOORD(53,30), YCOORD(53,30)
1, TATLE(20)
REAL*8 V1
INTEGER SMBOL, TITLE, TATLE
DATA SMBOL/'*', '+', '-', '/',
CALL PLOTS
READ 1000, GPPI, VVS, WHS, ROTDEG, NS, (X(I), Y(I), I=1,3), NTHPT, LAND
PRINT 1001, GPPI, VVS, WHS, ROTDEG, NS, (X(I), Y(I), I=1,3), NTHPT, LAND
READ 2000, (TITLE(I), I=1,20)
READ 2000, (TATLE(I), I=1,20)
READ 1002, THMIN, THMAX, YPN, XPN, SKIP
READ 1002, THIN, TMAX, TINC, TLEN, XPN, YPN, ZPN
VVS=ZPN
WHS=YPN
SET UP X, Y GRID
DO 100 J=1, ME
DO 100 I=1, NE
XCOORD(I, J)=J
DO 150 I=1, NS
Y(I)=-Y(I)
ROTATE ORIGIN POINTS
CALL ROT(X, Y, ROTDEG, NS)
ROTATE GRID POINTS
CALL ROT(XCOORD, YCOORD, ROTDEG, ME*NE)
READ(4, END=900) T, VEC, HT, RAD, ANG, Z
PRINT 8000, T
IF(T.LT.THMIN.OR.T.GT.TMAX)GO TO 270
TMIN=TMIN+TINC
GO TO 260
IF(T.EQ.TMAX)GO TO 260
GO TO 400
PRINT 4000, (TITLE(MM), MM=1,20), T)
IF( VEC.EQ.0.) GO TO 300
CALL VECTOR(.07, SMBOL, NTHPT, NTHPT, TITLE, LAND, ME, NE, HTZ, X, Y, NS,
1 XCOORD, YCOORD, RAD, ANG, VVS, T)
300 IF(HT.EQ.0.)GO TO 200
IF(HT.4000, (TATLE(MM), MM=1,20), T)
CALL WATHT (.07, SMBOL, NTHPT, GPPI, TATLE, LAND, ME, NE, HTZ, X, Y, NS,
1 XCOORD, YCOORD, Z, WHS, T)
400 GO TO 200
900 CALL PLOTE
RETURN
1000 FORMAT(10X
1001 FORMAT(: PARAMETER', F10.0, 3F6.0, 4X, I1, 6F3.0, I3, 4X, I1)

```



```

1002 FORMAT(10X
2000 FORMAT(20A4)
3000 FORMAT(1 READED 4 T = ,F10.0,/)
3000 FORMAT(6H TIME F10.0,4H SEC)
4000 FORMAT(10H PLUT FOR ,20A4,F10.0)
END

```

```

SUBROUTINE VECTOR(SSIZE, SMBOL, NTHPT, GPPI, TITLE, LAND, ME, NE,
1HTZ, X, Y, NS, XCOORD, YCOORD, VELOC, ANG, VVS, T)
DIMENSION ION HTZ(53,30), VELOC(53,30), ANG(53,30), XCOORD(53,30),
1YCOORD(53,30), X(NS), Y(NS), TITLE(20), SMBOL(3)
1, TATLE(20)
REAL*8 V1
INTEGER SMBOL, TITLE, TATLE
DO 400 I=1,NS
NN=MAXO(NE,ME)
CALL PLOT(O,0,0,3)
CALL PLOT(O,2,-3)
CALL SYMBOL(O,0,-0.5,0.14, TITLE,0.0,80)
CALL NUMBER(8.5,-.5,0.14,T,0.0,0)
DO 300 J=1,NE
DO 300 K=1,ME
TOPOG=HTZ(J,K)
IF( TOPOG.EQ.0.) GO TO 300
IF( TOPOG.EQ.1.)AND.(MOD(J,NTHPT).NE.0 .OR.MOD(K,NTHPT) .NE.0))
1GO TO 300
200 YJK=(YCOORD(J,K)-Y(I))/GPPI
IF( YJK.LT.0.)OR.YJK.GT.15.) GO TO 300
XJK=(XCOORD(J,K)-X(I))/GPPI
IF( XJK.LT.-1.) GO TO 300
IF( TOPOG+1.) 210,220,230

```



```

210 CONTINUE
211 CALL SYMBOL (XJK,YJK,SSIZE ,SMBOL (2),0.,1)
    GO TO 300
220 CONTINUE
221 CALL SYMBOL (XJK,YJK,SSIZE ,SMBOL (1),0.,2)
    GO TO 300
230 IF(LAND.EQ.0) GO TO 260
    J1=J-LAND
    K1=K-LAND
    J2=J+LAND
    K2=K+LAND
    DO 240 L=J1,J2
      DO 240 M=K1,K2
        IF (HTZ(L,M).EQ.-1.) GO TO 300
240 CONTINUE
260 DIST=VELOC(J,K)/VVS
    IF (ANG(J,K).GT.360.) GO TO 300
    SI=(450.-ANG(J,K)
    CO=COS(SI)
    SI=SIN(SI)
    CALL PLOT (XJK,YJK,3)
    XJK=XJK+DIST#CO
    YJK=YJK+DIST#SI
    CALL PLOT (XJK,YJK,2)
    CALL ARWPT (XJK,YJK,CO,SI)
300 CONTINUE
400 CALL PLOT(0.,NN/GPPI+3.,-3)
    RETURN
    END

```



```

SUBROUTINE WATHT (SSIZE ,SMBOL ,NTHPT,GPPI ,TATLE,LAND,ME,NE,
1HTZ,X,Y,NS ,XCOORD ,YCOORD ,Z,WHS,T)
DIMENSION SMBOL (3),TITLE(20),HTZ(53,30),X(NS),Y(NS),XCOORD(53,30)
1,TATLE(20)
1,YCOORD(53,30),Z(53,30)
REAL*8 V1
INTEGER SMBOL,TITLE,TATLE
DO 400 I=1,NS
NN=MAXO(NE,ME)
CALL PLOT(0,0,3)
CALL PLOT(0,2,-3)
CALL SYMBOL(0,0,5,0,14,TATLE,0,0,80)
CALL NUMBER(8,5,-.5,0,14,1,0,0,0)
DO 300 J=1,NE
DO 300 K=1,ME
TOPOG=HTZ(J,K)
IF( TOPOG.EQ.0.) GO TO 300
IF( TOPOG.EQ.1..AND.(MOD(J,NTHPT).NE.0 .OR.MOD(K,NTHPT) .NE.0))
1GO TO 300
200 YJK=(YCOORD(J,K)-Y(I))/GPPI
IF( YJK.LT.0..OR.YJK.GT.15.) GO TO 300
XJK=(XCOORD(J,K)-X(I))/GPPI
IF( XJK.LT.-1.) GO TO 300
IF( TOPOG+1.) 210,220,230
CONTINUE
210 CALL SYMBOL (XJK,YJK,SSIZE ,SMBOL (2),0.,1)
211 GO TO 300
CONTINUE
220 CALL SYMBOL (XJK,YJK,SSIZE ,SMBOL (1),0.,2)
221 GO TO 300
230 IF(LAND.EQ.0) GO TO 260
J1=J-LAND
K1=K-LAND
J2=J+LAND
K2=K+LAND
DO 240 L=J1,J2
DO 240 M=K1,K2
IF( HTZ(L,M).EQ.-1.) GO TO 300
CONTINUE
240 CALL SYMBOL (XJK,YJK,SSIZE ,SMBOL (3),0.,2)
260 IF( Z(J,K).EQ.0.) GO TO 300
CALL PLOT (XJK,YJK,3)
YJK=YJK+ Z(J,K)/WHS
CALL PLOT (XJK,YJK,2)
UP=1
IF( Z(J,K).LT.0.) UP=-1.
CALL ARWPT (XJK,YJK,0.,UP)
CONTINUE
300

```



```

400 CALL PLOT(0., NN/GPPI+3., -3)
RETURN
END

```

```

SUBROUTINE ROT(X, Y, DEG, MM)
DIMENSION X(MM), Y(MM)
REAL*8 V1
SI=DEG*.01745329
CO=COS(SI)
SI=SIN(SI)
DO 100 I = 1, MM
XI=X(I)
YI=Y(I)
X(I) = XI*CO + YI*SI
Y(I) = YI*CO - XI*SI
100 RETURN
END

```

```

SUBROUTINE ARWPT (X, Y, CO, SI)
REAL*8 V1
DATA H/.06/
YY = SI*H
XX = CO*H
YYY=YY*.25
XX=X-XX
YY=Y-YY
CALL PLOT (XX-XXX, YY+YYY, 2)
CALL PLOT (XX+XXX, YY-YYY, 2)
CALL PLOT (X, Y, 2)
CALL PLOT (X, Y, 3)
RETURN
END

```



```

SUBROUTINE WATLV(NALL)
DIMENSION Z(58,40),CL(11)
LOGICAL*1 LTG(3)
REAL*8 TITLE(12),WATER,HE,IGHT CON,TOURS
100 BAY( ),,TIME
200
    LTG(1)=.TRUE.
    LTG(2)=.TRUE.
    LTG(3)=.TRUE.
    CL(1)=-125.
    DO 200 KKK=2,11
    CL(KKK)=CL(KKK-1)+25.
200 CONTINUE
    DO 100 KK=1,NALL
    READ(3) T,Z
    CALL CONTUR(Z,58,40,58,CL,11,TITLE,8,8,LTG)
    CONTINUE
100 RETURN

```


BIBLIOGRAPHY

1. U.S. Army Engineer District, Los Angeles (Preliminary) Summary Report. San Diego Bay Model Study. Hydraulic Model Study. U. S. Army Engineer Waterways Experiment Station. Corps of Engineers, Vicksburg, Mississippi, June 1971.
2. Bowden, K. F., "The Mixing Processes in a Tidal Estuary," J. Air and Water Pollution, Pergamon Press 1963, Vol. 7, pp. 343-356.
3. Doodson, A. T., and Warburg, H. D., Admiralty Manual of Tides, Her Majesty's Stationery Office, 1941.
4. Dr. Laevastu, T., and Rabe, K., A Description of the EPRE Hydrodynamical-Numerical Model, U. S. Navy Environmental Prediction Research Facility, Technical Paper No. 3 - 72, March 1972.
5. Dr. Laevastu, T., and CDR Hamilton, G. D., Computation of Flushing and Dispersion of Pollutants in the Pearl Harbor and in San Diego Bay with Hydrodynamical-Numerical Models, U. S. Navy Environmental Prediction Research Facility, Monterey, Calif. 1972.
6. Dr. Laevastu, T., and Stevens, P., Application of Numerical-Hydrodynamical Model in Ocean Analysis/Forecast. Rrt 1; The Single-Layer Models of W. Hansen, Fleet Numerical Weather Central, Monterey, Calif., Technical Note No. 51, July 1969.
7. Dr. Laevastu, T., and CDR Hamilton, G. D., Reproduction of Current in the Strait of Florida with a Hydrodynamical-Numerical (HM) Model, U. S. Navy Environmental Prediction Research Facility, Monterey, Calif., April 1972.
8. Ramming, H. G., Investigation of Motion Processes in Shallow Water Areas and Estuaries, Institut Für Meereskunde Der Universität, Hamburg, Proceedings Symp. on Coastal Geodesy, Munich, July 1970, pp. 439-452.
9. Ramming, H. G., Hydrodynamical-Numerical Investigations and Horizontal Dispersion of Seston in the River Elbe, Institut Für Meereskunde Der Universität Hamburg, Report No. 18, Feb. 1971, 72 pgs. 31 figs.

10. Simmons, H. S. and Herrmann, F. A., Influences of Proposed Second Entrance on the Flushing Characteristics of San Diego Bay, Calif., FAO Technical Conference on Marine Pollution and its Effects on Living Resources and Fishing, Rome, Italy, 9-18 December 1970.
11. Sverdrup, H. Q., Johnson, M. W., and Fleming, R. H., The Oceans, Prentice-Hall, Inc. 1942.
12. Von Arx, W. S., An Introduction to Physical Oceanography, Addison Wesley Publishing Co. Inc. 1962.

INITIAL DISTRIBUTION LIST

	No. copies
1. Defense Documentation Center Cameron Station Alexandria, Virginia. 22314	2
2. Library, Code 0212 Naval Postgraduate School Monterey, California 93940	2
3. Department of Oceanography Naval Postgraduate School Monterey, California 93940	3
4. CDR Leopoldo Salas R. Dirección de Hidrografía y Navegación Apartado 6745 Caracas, Venezuela	5
5. Escuela Naval de Venezuela Escuela de Posgrado Meseta de Mamo, Catia la Mar Venezuela	1
6. Dr. Edward B. Thornton Department of Oceanography Naval Postgraduate School Monterey, California 93940	5
7. Dr. Taivo Laevastu Environmental Prediction Agency Fleet Numerical Weather Center Monterey, California 93940	2
8. Lt. Jose Saldanha Instituto Hidrografico Ministerio de Marinha Lisboa, Portugal	1
9. Mr. F. A. Herrmann Estuaries Branch U. S. Army Waterways Experiment Station Corps of Engineers, PO Box 631 Vicksburg, Mississippi 39180	2
10. Mr. Edward Koehm Engineering Division Corps of Engineers 300 N. Los Angeles Los Angeles, Calif.	1

11. Mr. George M. Fisackerly 1
Harbor Entrance Section
U.S. Army Corps of Engineers
P.O. Box 631
Vicksburg, Mississippi 39180
12. Mr. Stuart L. Kufferman 1
College of Marine Studies
University of Delaware
Newark, Delaware 19711
13. Mr. Dennis F. Polio 1
College of Marine Studies
University of Delaware
Newark, Delaware 19711
14. Mr. Sheldon M. Lazanoff 1
Fleet Numerical Weather Central
Monterey, California 93940
15. Dr. J. A. Galt 1
Department of Oceanography
Naval Postgraduate School
Monterey, California 93940
16. Dr. D. J. Baumgartner 1
Federal Water Quality Administration
Northwest Region
Pacific Northwest Water Laboratory
200 Southwest 35th street
Corvallis, Oregon 97330
17. Dr. R. G. Dean 1
Coastal and Oceanographic Engineering Department
University of Florida
Gainesville, Florida 32601
18. Environmental and Fishery Forecasting Center 1
National Marine Fisheries Service
National Oceanic and Atmospheric Administration
U. S. Department of Commerce
C/O Fleet Numerical Weather Central
Monterey, California 93940
19. Dr. John Huth 1
Special Assistant to Director of Navy Laboratory
Code 034
Naval Ship System Command
Washington, D. C. 20350

20. LCDR Charles A. Farrel 1
 Ocean Services
 Naval Undersea Research and Development Center
 San Diego, California 92132
21. CDR Richard D. Fasing 1
 Pollution Control Office
 11th Naval District
 San Diego, California 92132
22. CDR Joseph D'Emidio 1
 OP 45
 Director of the Environmental Protection Div.
 Pentagon Building, Room 4B516
 Washington, D. C. 20350
23. Mr. R. L. Reisbig 1
 Mechanical Engineering School
 University of Missouri
 Rolla, Mo. 65401
24. Mr. H. G. Ramming 1
 Institut für Meereskunde
 Universität Hamburg
 Hamburg, Germany
25. Dr. W. Hansen 1
 Institut für Meereskunde
 Universität Hamburg
 Hamburg, Germany
26. Director Instituto Nacional de Canalizaciones 1
 Av. Andrés Bello
 Edificio Atlantic 6º
 Los Palos Grandes
 Caracas, Venezuela
27. Division de Ingeniería 1
 Instituto Nacional de Canalizaciones
 Av. El Milagro
 Maracaibo, Venezuela
28. Departamento de Oceanografía 1
 Universidad Simón Bolívar
 Caracas, Venezuela
29. Departamento de Oceanografía 1
 Universidad de Oriente
 Cumaná, Venezuela

30. Director 1
National Oceanic and Atmospheric Administration
U.S. Department of Commerce
Washington, D.C. 20235
31. Division of Oceanography 1
Environmental Science Service Administration
Silver Springs, Maryland 20910
32. Commanding Officer 1
Office of Naval Research Branch Office
Box 39
Fleet Post Office
New York 09510
33. Chief of Naval Research 1
Ocean Science and Technology Group
Code 480
Office of Naval Research
Washington, D.C. 20360
34. Chief of Naval Research, Code 480 1
Attn: Dr. Ostenso
Office of Naval Research
Washington, D.C. 20360
35. Oceanographer of the Navy 1
Office of the Oceanographer of the Navy
732 North Washington St.
Alexandria, Virginia 22314
36. Director 1
Coastal Engineering Research Center
Corps of Engineers, U.S. Army
5201 Little Falls Road, N.W.
Washington, D.C. 20315
37. Commandant 1
U.S. Coast Guard
Headquarters
Washington, D.C. 20591
38. Director, Naval Research Laboratory 1
Attn: Technical Information Officer
Washington, D.C. 20390
39. Director 1
Office of Naval Research Branch Office
1030 East Green St.
Pasadena, California 91101

40. Sr. Presidente 1
Comite de Hidrografía
Instituto Panamericano de Geografía e Historia
Ex-Arzobispado 29
Mexico 18, D.F. Mexico
41. Dirección de Hidrografía y Navegación 1
Camandancia General de la Marina
Apartado 6745
Caracas, Venezuela
42. LTjg Rafael Steer 1
Calle 70. Nº 59-15
Barranguilla, Colombia
43. Dr. Noel Boston 1
Department of Oceanography
Naval Postgraduate School
Monterey, California 93940
44. CDR Karl L. Schriener 1
Headquarters, Fifth Naval District
Norfolk, Virginia 23511

(Security classification of title, body of abstract and indexing annotation must be entered when the overall report is classified)

ORIGINATING ACTIVITY (Corporate author)

Naval Postgraduate School
Monterey, California 93940

2a. REPORT SECURITY CLASSIFICATION

Unclassified

2b. GROUP

REPORT TITLE

Comparison of Numerical and Hydraulic Oceanographic Prediction
Models

DESCRIPTIVE NOTES (Type of report and, inclusive dates)

Master's Thesis: September 1972

AUTHOR(S) (First name, middle initial, last name)

Leopoldo Salas R.

REPORT DATE

September 1972

7a. TOTAL NO. OF PAGES

141

7b. NO. OF REFS

12

CONTRACT OR GRANT NO.

9a. ORIGINATOR'S REPORT NUMBER(S)

PROJECT NO.

9b. OTHER REPORT NO(S) (Any other numbers that may be assigned
this report)

DISTRIBUTION STATEMENT

Approved for public release; distribution unlimited.

SUPPLEMENTARY NOTES

12. SPONSORING MILITARY ACTIVITY

Naval Postgraduate School
Monterey, California 93940

ABSTRACT

The Hydro-Numerical Prediction Model developed by Hansen is applied to San Diego Bay, and the results compared both with the hydraulic model and the real data obtained by field measurements. This allows one of the few good comparisons between numerical and hydraulic models for the prediction of actual conditions.

The bay was divided into two sections that were run separately in order to obtain the desirable spatial resolution. This division required solving the problems of proper tuning and matching techniques between both portions. The solution involved the addition of an appended pseudo-bay to the first section of the model in order to compensate for the correct tidal prism. The effects of a proposed second open entrance in the southern part of the bay were studied. This resulted in an increase of flushing in the southern portion of the bay but caused the currents in the center of the bay to be small which decreased dispersion in the central portion of the bay. In general, both models produced similar and reliable results, but there was a considerable reduction of cost and time with the numerical model.

KEY WORDS	LINK A		LINK B		LINK C	
	ROLE	WT	ROLE	WT	ROLE	WT
Numerical Oceanographic Model Hydraulic Model San Diego Bay						

26 AUG 74
20 JUN 75
29 JAN 76

23452
22660
26406

Thesis

141363

S1526 Salas Römer

c.1 Comparison of numerical and hydraulic oceanographic prediction models..

26 AUG 74
20 JUN 75
29 JAN 76

23452
22660
26406

Th
S1

Thesis

141353

S1526 Salas Römer

c.1 Comparison of numerical and hydraulic oceanographic prediction models.

thes1526

Comparison of numerical and hydraulic oc



3 2768 001 97694 7

DUDLEY KNOX LIBRARY