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- Tristimulus Specification of the Munsell Book of Color from Spectrophotometric Measurements**
..... KENNETH L. KELLY, KASSON S. GIBSON, AND DOROTHY NICKERSON 355
- Trichromatic Specifications for Intermediate and Special Colors of the Munsell System** . . .
..... WALTER C. GRANVILLE, DOROTHY NICKERSON, AND CARL E. FOSS 376
- Final Report of the O.S.A. Subcommittee on the Spacing of the Munsell Colors**
..... SIDNEY M. NEWHALL, DOROTHY NICKERSON, AND DEANE B. JUDD 385
- Psychological Color Solid** DOROTHY NICKERSON AND SIDNEY M. NEWHALL 419
- Necrology** 422

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Tristimulus Specification of the *Munsell Book of Color* from Spectrophotometric Measurements*

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The development of the Inter-Society Color Council-National Bureau of Standards (ISCC-NBS) system of color names, based on the standards in the *Munsell Book of Color*, made it necessary to specify the master standards of this book in fundamental terms. Accordingly, spectral reflection curves were run for each of the 421 master standards on the General Electric recording spectrophotometer at the National Bureau of Standards, using slit widths of approximately 4 millimicrons. Various corrections were applied to these spectrophotometric data in accordance with methods regularly used for such work at the bureau. Colorimetric computations were then made with these data, resulting in tristimulus specifications according to the 1931 ICI standard observer and coordinate system. Four illuminants were used: ICI Illuminants *A* and *C*, representative of incandescent-lamp light and

average daylight, respectively, Illuminant *D* (lightly overcast north sky), and Illuminant *S* (extremely blue sky). The colorimetric specifications of the Munsell standards for all four illuminants are thus given. The trilinear coordinates for the Munsell standards calculated for ICI Illuminant *C* have been plotted on large chromaticity (*x, y*) diagrams and constant Munsell chroma lines drawn in. (Similar values obtained by Glenn and Killian at the Massachusetts Institute of Technology in 1935 for Munsell color standards bearing the same hue-value-chroma designations have also been plotted on the diagram and differences between the two sets of data are discussed.) These diagrams serve as means for determining the Munsell notation and thereby the ISCC-NBS color name for any color whose trilinear coordinates and apparent reflectance are given.

I. INTRODUCTION

TWO of the official compendia of drugs and medicines, the United States Pharmacopoeia and the National Formulary, specify the purity and quality of drugs by a number of tests for which tolerance limits are set; with a crude drug, for example, these tests refer to ash, acid insoluble ash, size, chemical identification tests, taste, color, and so forth, these being indications

of purity or quality. All of the tests except color have been under continuous study by committees entrusted with their revision. Color, on the other hand, presented a different type of problem whose solution was not attempted until 1931. Previously the color terms used in the USP and NF had enjoyed no official definition but contained among others such confusing terms as brownish green or blackish white, with seldom any reference to a color chart or standard. In the monograph of a drug, the pharmacognocist describes the colors of the outside and the inside, the colors of the various microscopic elements, and

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finally the colors of the identification tests. In each instance, no mention is made of the normality of the observer's color vision (1),² or of the conditions of lighting or viewing.

Agitation toward research for the development of a suitable system of color terminology was begun in the twenties by E. N. Gathercoal, then a member of the USP Revision Committee (2). After the founding of the Inter-Society Color Council, of which he was the first chairman, studies were made of the then existing color systems, and in 1933 the report (3) was submitted which became the basis of the system of color names now known as the ISCC-NBS system of color names (4). Procedures were developed at the same time for the application of these color names to the description of the colors of crude drugs, powdered drugs, chemicals, liquids, precipitates, microscopic structures, and fluorescent materials (5). The central notations of the color-name blocks were determined for the application of these color names to the description of the colors of soils (6). Recently these names have also been used to describe the colors of illuminants and a description of this method of use is in preparation.

In all of this work, the boundaries of the separate color-name blocks have been specified in terms of the Munsell color standards (7), (8). It was realized early in the project that in order to be placed on a sound basis the individual boundaries must be specified in fundamental terms. The accuracy of the system of color names would then be independent of the existence or stability of the individual system of material color standards in terms of which the system is used in practice. Since the Munsell color system provided a very satisfactory means of determining which color name best described the color of an object, it was decided to measure the spectral reflectances of all of the color standards in the *Munsell Book of Color*. The specification of the trilinear coordinates and apparent reflectances of each of the Munsell samples would provide an invariable specification of the color of that sample and thereby of a definite point in the

framework of the system by which the relative position of each color name is indicated.

Tristimulus specifications of the *Munsell Book of Color* have been published by Glenn and Killian (8) and were available for some time before that date. Instead of using the Glenn-Killian data, however, it seemed preferable to define the ISCC-NBS system of color names by way of the Munsell samples actually used in the color-names work. This involved a nominal repetition of the spectrophotometric and colorimetric work carried out by Glenn and Killian, but avoided uncertainties arising out of the possible differences between the respective Munsell samples bearing the same color designation as well as those arising from the unknown history and usage of the Glenn-Killian samples prior to their measurement. Furthermore, the present authors desired to use in the spectrophotometric measurements certain methods of calibration regularly used at the National Bureau of Standards for such work. The measurements and computations described below were accordingly undertaken, and the diagrams and tables included in the present paper provide a means by which a color may be named without reference to a color chart, or by which the boundaries of the color-name blocks may be specified in terms of a fundamental color system. It is now possible to select the appropriate color name for a color when the fundamental specifications for that color are given.

Since the application of this system of color names will be made in the plant or in the field where the illumination used will usually be daylight, all of the techniques and computations both for the color names and for the Munsell system have primarily been made on the basis of ICI Illuminant C. However, colorimetric data on the Munsell standards for other illuminants are also of interest. Accordingly, based on the same spectrophotometric data, tristimulus values have been computed for four illuminants—ICI Illuminant C (9) (representative of average daylight), ICI Illuminant A (9) (2842°K) (10), representative of incandescent illuminants, Illuminant D (11), (12) (representative of lightly overcast north sky), and Illuminant S (13), (14) (representative of extremely blue sky).

² Figures in parentheses indicate the literature references at the end of this paper.

II. SAMPLES MEASURED

Prior to his death, Walter T. Spry, then manager of the Munsell Color Company, deposited one or more samples of all of the original paintings of the standards in the *Munsell Book of Color* with the Colorimetry Section of the Bureau. He also deposited repaints of all colors the original paintings of which had become depleted, together with new colors prepared up to 1935. In selecting the samples of each color to be measured, that painting was chosen which matched the color chip of the same designation in the *Munsell Book of Color*. In most instances the color differences between the originals and their repaints were negligible but in several it was important to specify which painting was used. Therefore, for the purpose of accuracy and as a matter of record, the painting number of each sample measured is given.

The 2-value 2-chroma samples for the intermediate hues (10R, 10YR, 10Y, etc.) were painted independently of the other 2-value 2-chroma samples and the colors and the data are not as congruent with the other samples as they are with each other. These samples, as well as several 8-value 2-chroma samples for the intermediate hues, are not included in the *Munsell Book of Color*, but they were measured and the data are included in the present paper for the sake of completeness. One new sample, 10YR 8/8, recently received, is included. The complete list of samples measured is given in Table II.

The samples in the *Munsell Book of Color* were inspected under a strong source of ultraviolet radiant energy and also under a strong yellowish green light for fluorescence which might vitiate the spectrophotometric measurements (15). No fluorescence was observed under either illuminant.

III. METHODS OF MEASUREMENT AND COMPUTATION

Spectral reflection curves of all of the samples noted and listed in Table II were run on the General Electric recording spectrophotometer at the National Bureau of Standards. The samples were run relative to magnesium oxide (16), with approximately 4- $m\mu$ slits and over a wave-length range from 400 to 750 $m\mu$. The samples were backed with black paper for these measurements. Calibration curves were run on each sheet

enabling corrections to be applied to the data for wave-length errors, for 100 percent and zero curve deviations, and for aging of the magnesium oxide comparison surface, in accordance with methods regularly used at the National Bureau of Standards (17), (18).

As already noted, the colorimetric computations were made for four different illuminants. ICI Illuminants A and C have become well

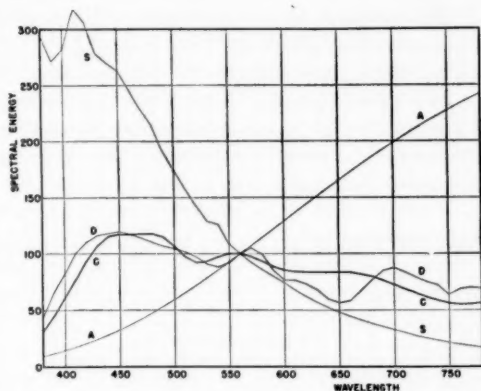


FIG. 1. Spectral energy distributions of the four illuminants used in deriving the colorimetric data on the Munsell standards. Note: ICI Illuminant A, 2842°K, representative of incandescent illuminants. ICI Illuminant C, representative of average daylight. Illuminant D, representative of lightly overcast sky. Illuminant S, representative of "limit blue sky."

established in colorimetric work. Illuminant A is the Plankian radiator or blackbody at 2842°K ($C_2=14,320$ micron-degrees, or 2848°K with $C_2=14,350$); the color temperatures of common incandescent illuminants vary from about 2600°K to about 3100°K. Illuminant C is that produced by a source at 2842°K combined with a certain Davis-Gibson daylight liquid filter (19). On the "OSA excitations" basis (used in the design of the Davis-Gibson filters) the resulting color matched that of a Plankian radiator at 6500°K. On the basis of the ICI data the approximate color temperature of this lamp-and-filter combination is 6800°K. The color and spectral energy distribution of ICI Illuminant C satisfactorily match those of overcast sky or average daylight for colorimetric use. Illuminant D is that produced by an illuminant at 3000°K combined with a Macbeth (Corning) daylight glass filter giving a color temperature of approximately

7500°K. The color of Illuminant *D*, found to be the optimum color for cotton grading, is also being widely used for agricultural grading and textile color matching. Its color closely matches that of the lightly overcast north sky most desired for such work. Illuminant *S* was designed as the blue end point for a series of illuminants representing the range from fully overcast to maximally clear sky. It was devised by weighting Abbot's "sun-outside-atmosphere" energy data by the inverse λ^4 scattering relation. Illuminant *S* has been designated as "limit blue sky."

The colorimetric data on the Munsell samples for ICI Illuminant *C*, representative of average daylight, are of primary interest and the computations were carried out both at the National Bureau of Standards and in the U. S. Depart-

ment of Agriculture. Those for the other three illuminants were made in the Department of Agriculture. All of the computations in the Department of Agriculture were done by using Hollerith cards and automatically punching sums obtained by the method of progressive digitizing. The authors are indebted to Lila F. Knudsen, mathematical statistician of the Food and Drug Administration, for suggesting this rapid method of computation (20). All of the computations were made by the weighted ordinate method.

The spectral energy distributions of the four illuminants are shown in Fig. 1, and in Table I are given the tristimulus data for the spectrum of each of the four illuminants used in the computations of *X*, *Y*, *Z* and *x*, *y*, *z*.

TABLE I. ICI tristimulus data for the four illuminants, *A*, *C*, *D*, and *S*, used in deriving the colorimetric data on the Munsell standards.

Wave-length (m μ)	For Illuminant <i>A</i>			For Illuminant <i>C</i>			For Illuminant <i>D</i>			For Illuminant <i>S</i>		
	$\bar{x}E$	$\bar{y}E$	$\bar{z}E$	$\bar{x}E$	$\bar{y}E$	$\bar{z}E$	$\bar{x}E$	$\bar{y}E$	$\bar{z}E$	$\bar{x}E$	$\bar{y}E$	$\bar{z}E$
380	1		6	4		20	6		30	36		165
390	5		23	19		89	27	1	128	99	3	473
400	19	1	93	85	2	404	119	3	567	349	10	1658
410	71	2	340	329	9	1570	446	12	2125	1199	33	5719
420	262	8	1256	1238	37	5949	1504	45	7223	3567	107	17137
430	649	27	3167	2997	122	14628	3373	138	16461	6852	280	33442
440	926	61	4647	3975	262	19938	4202	277	21077	8143	538	40845
450	1031	117	5435	3915	443	20638	4100	463	21613	7652	865	40332
460	1019	210	5851	3362	694	19299	3476	717	19952	6194	1278	35554
470	776	362	5116	2272	1058	14972	2274	1059	14982	3870	1803	25503
480	428	622	3636	1112	1618	9461	1070	1556	9099	1742	2533	14815
490	160	1039	2324	363	2358	5274	347	2258	5049	530	3444	7703
500	27	1792	1509	52	3401	2864	52	3451	2906	74	4871	4102
510	57	3080	969	89	4833	1520	96	5214	1640	127	6870	2160
520	425	4774	525	576	6462	712	626	7023	774	781	8757	965
530	1214	6322	309	1523	7934	388	1533	7986	391	1847	9618	471
540	2313	7600	162	2785	9149	195	2610	8574	182	2958	9717	207
550	3732	8568	75	4282	9832	86	4062	9324	82	4070	9343	81
560	5510	9222	36	5880	9841	39	6072	10162	40	5148	8615	34
570	7571	9457	21	7322	9147	20	8160	10194	22	6092	7610	16
580	9719	9228	18	8417	7992	16	9310	8840	17	6798	6454	13
590	11579	8540	12	8984	6627	10	8946	6599	10	7090	5229	7
600	12704	7547	10	8949	5316	7	8343	4956	6	6798	4038	5
610	12669	6356	4	8325	4176	2	7800	3913	2	5871	2945	2
620	11373	5071	3	7070	3153	2	6372	2841	1	4585	2044	1
630	8980	3704		5309	2190		4477	1847		3160	1303	
640	6558	2562		3693	1443		2732	1067		2030	793	
650	4336	1637		2349	886		1640	619		1183	447	
660	2628	972		1361	504		988	365		636	236	
670	1448	530		708	259		603	221		313	114	
680	804	292		369	134		367	133		155	56	
690	404	146		171	62		197	71		69	25	
700	209	75		82	29		102	37		32	11	
710	110	40		39	14		49	18		15	5	
720	57	19		19	6		23	8		7	3	
730	28	10		8	3		11	4		3	1	
740	14	6		4	2		5	2		2	1	
750	6	2		2	1		2	1		1		
760	4	2		1	1		1	1		1		
770	2			1			1					
$\Sigma =$	109828	100000	35547	98041	100000	118103	96124	100000	124379	100078	100000	231410
$x, y, z =$.44759	.40754	.14487	.31012	.31631	.37357	.29992	.31201	.38807	.23194	.23176	.53630

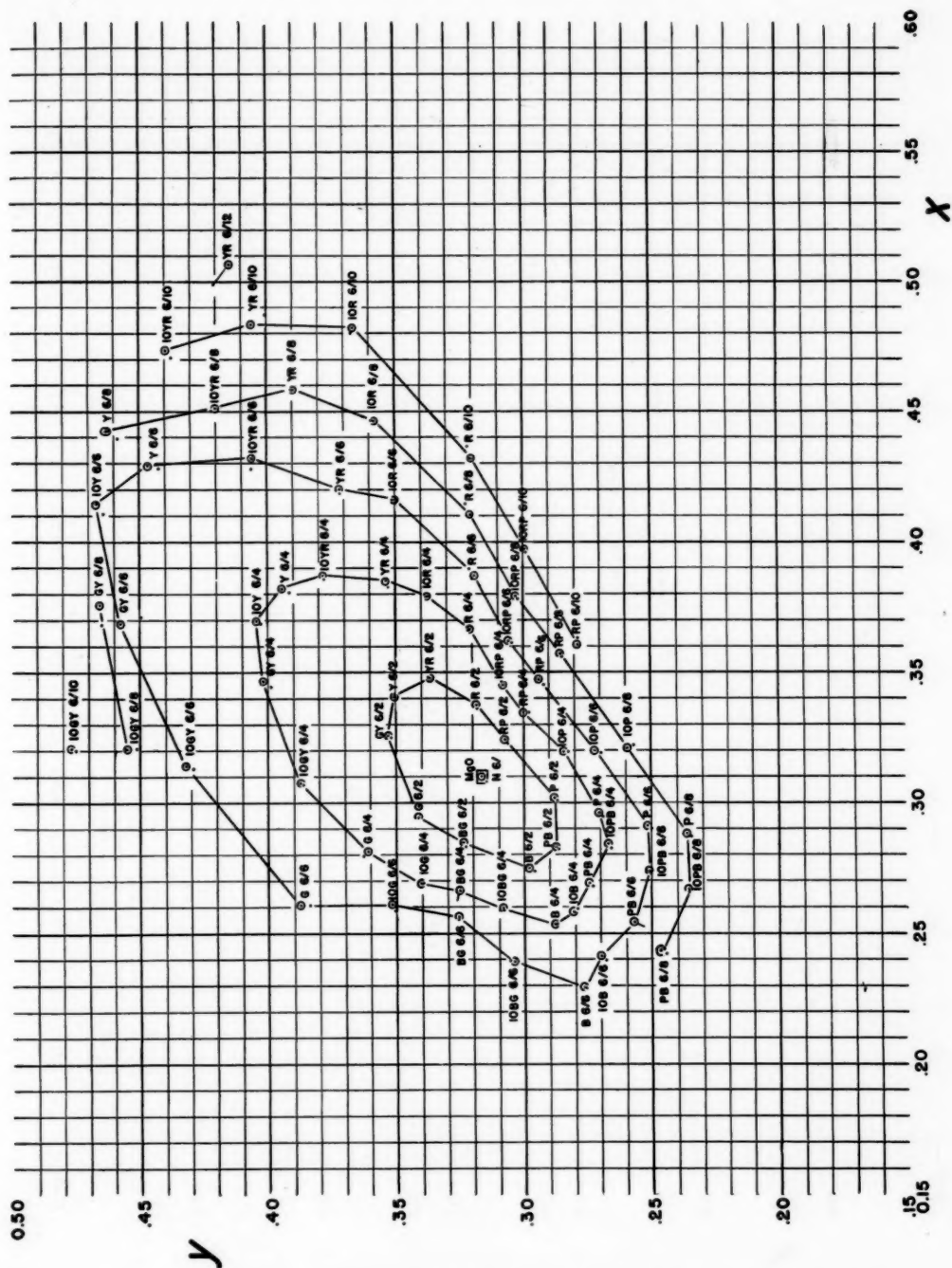


Fig. 6. ICI chromaticity diagram showing values of x and y for ICI Illuminant C for Munsell standards of value level 6/.

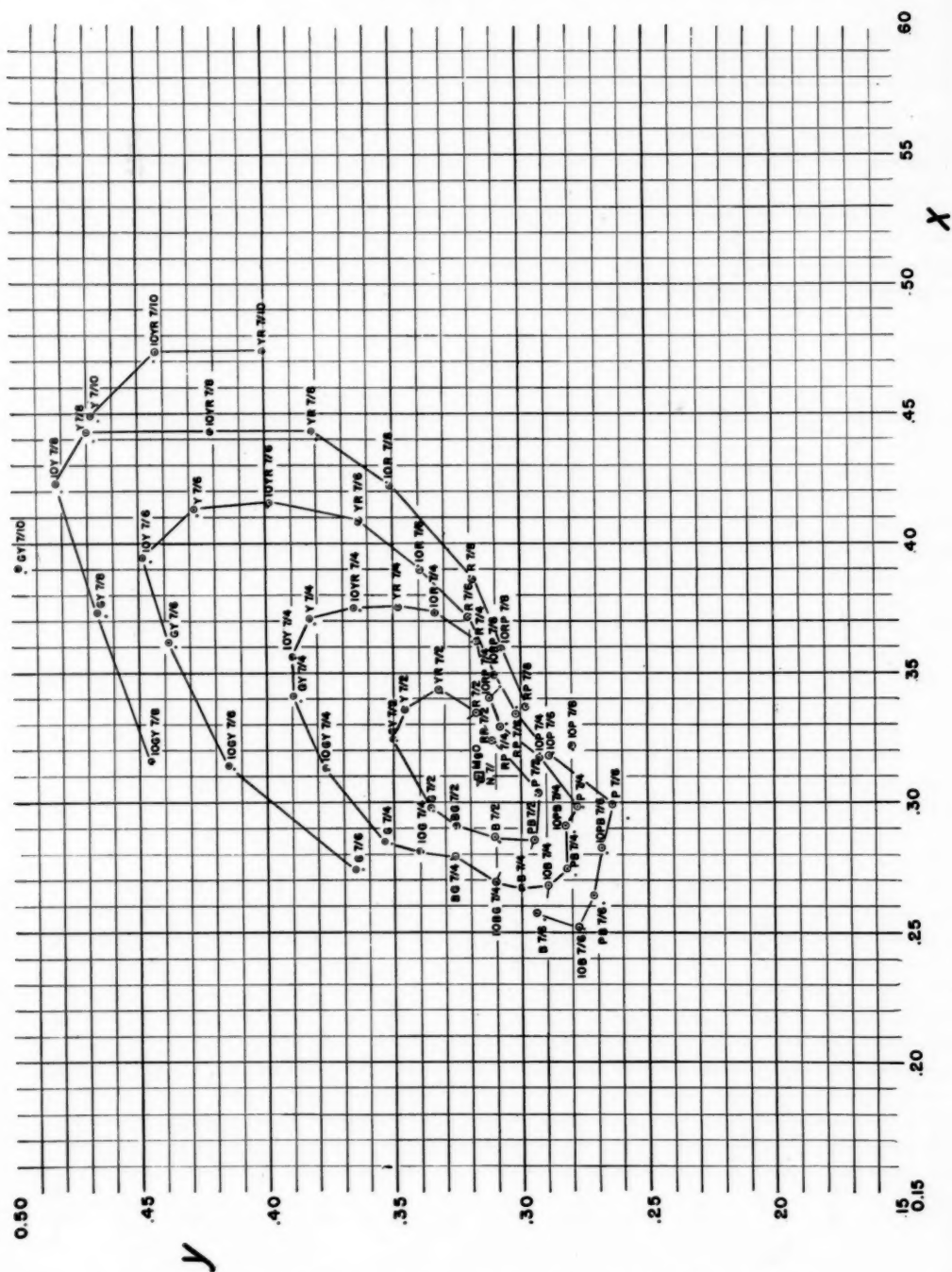


Fig. 7. ICI chromaticity diagram showing values of x and y for ICI Illuminant C for Munsell standards of value level 7/.

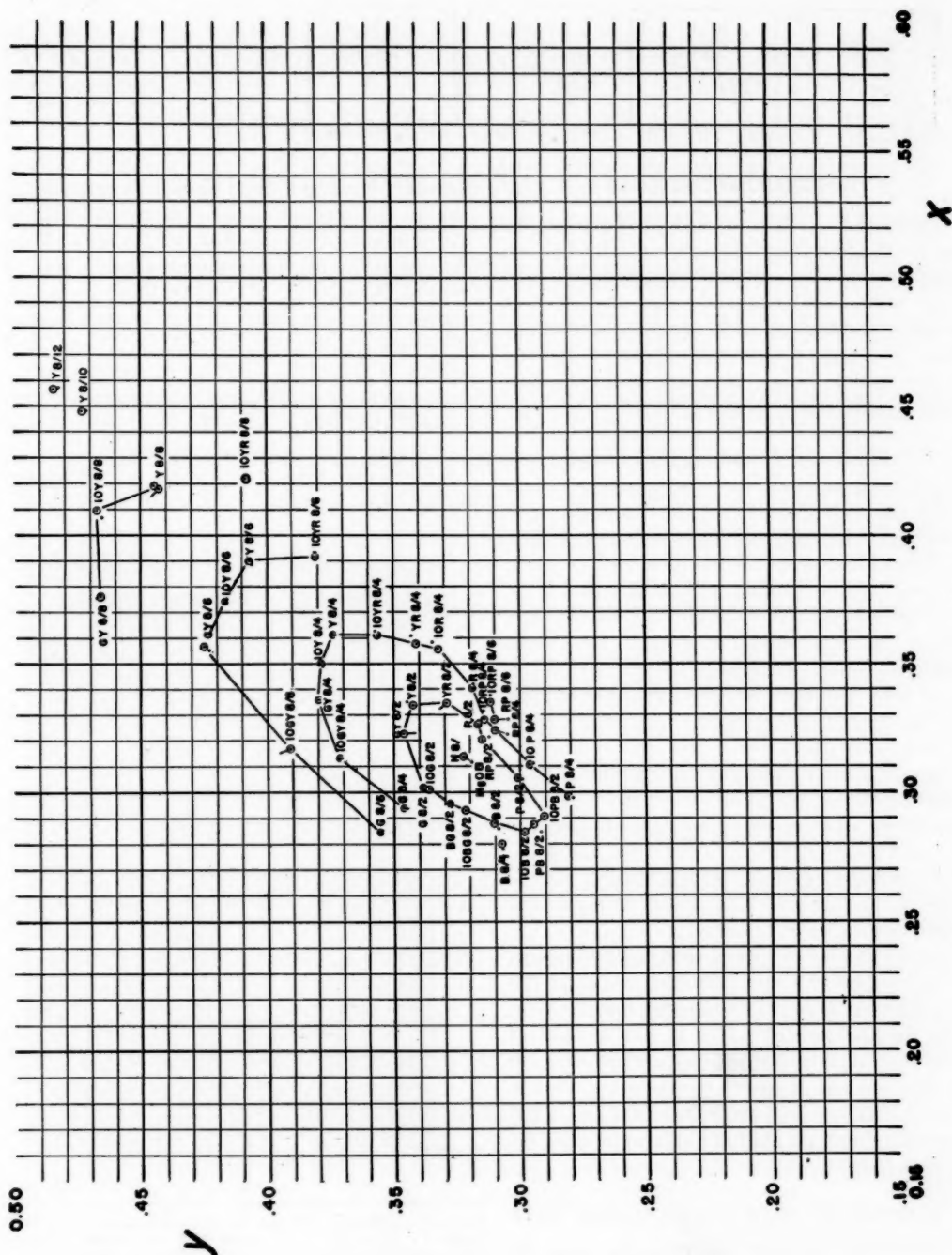


Fig. 8. ICI chromaticity diagram showing values of x and y for ICI Illuminant C for Munsell standards of value level $8/$.

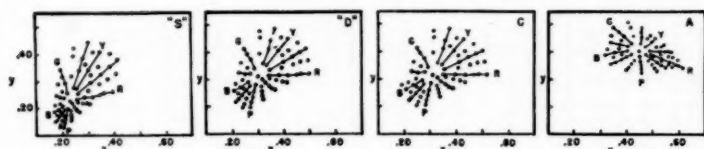


FIG. 9. Values of x and y for samples of Munsell value 5/ for illuminants A, C, D, and S. This graph shows the effect of illuminant on the location and shape of the Munsell network.

IV. COLORIMETRIC DATA

Values of X , Y , Z , x , and y for all of the samples and for the four illuminants, as explained above, together with the Munsell notations, H V/C (hue, value, and chroma), and the Munsell painting number for each sample, are given in Table II. Values for the neutrals are at the end of the table. Values of z are omitted, since $z = 1 - x - y$.

Values of the trilinear coordinates, x and y , for ICI Illuminant C, are plotted in Figs. 2 to 8 for Munsell values 2 to 8, respectively. The x and y values for ICI Illuminant C, and therefore for magnesium oxide and for any other spectrally non-selective sample, are given in each diagram at $x = 0.3101$, $y = 0.3163$. Values of x and y for the Munsell samples obtained at the National Bureau of Standards are plotted as circled points. The data obtained by Glenn and Killian (8) at the Massachusetts Institute of Technology in 1935 are plotted as uncircled points for comparison with the present data. When the two points for a sample coincide, the combination is plotted as a circled point with a short line attached; in many cases, to avoid confusion, the two points are joined by a fine line. Lines are drawn connecting all of the NBS points of constant chroma on each diagram, resulting in the spiderweb-like figures shown.

Graphs similar to Figs. 2 to 8 could of course be plotted for the other illuminants using the data given in Table II. While this has not been done for the present paper it has seemed of interest to show the effect of the illuminant on the location and shape of the network. This is done in Fig. 9, where the values of x and y for Munsell value 5 are plotted to the same scale for the four illuminants.

V. COMPARISON WITH GLENN-KILLIAN DATA

Differences between the methods used by Glenn and Killian and those used at the National Bureau of Standards are understood to be as

follows: 1. The Glenn-Killian spectrophotometric data were obtained with samples backed by "a standard white substance," the National Bureau of Standards data with samples backed with black paper. 2. The calibration curves (see above) run on each sheet at the National Bureau of Standards were not used by Glenn and Killian. 3. The Glenn-Killian colorimetric computations were made by the selected-ordinate method, the NBS data by the weighted ordinate method.

Spectrophotometric differences caused by the backing are illustrated in Fig. 10, in which are

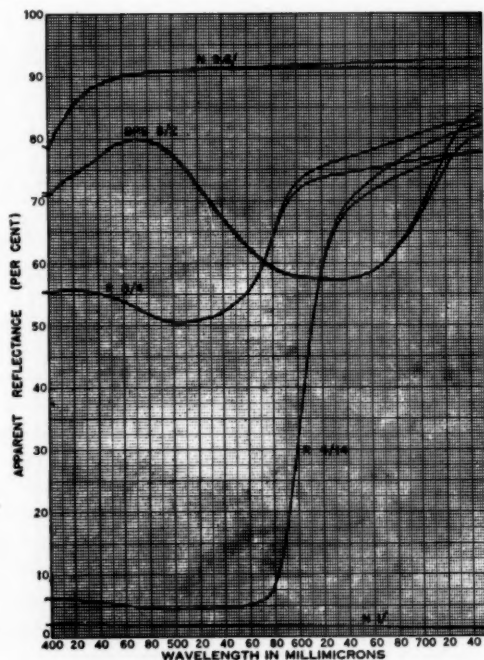


FIG. 10. Effect of backing on the spectral apparent reflectance of Munsell samples. The upper curve of each pair was obtained with the sample backed with a white paper (N 9.6/), the lower curve with the sample backed with a black paper (N 1/). Note that no difference in curves caused by difference in backing is apparent for values of reflectance less than 0.6 or at the shorter wavelengths.

TRISTIMULUS SPECIFICATION

TABLE II. The tristimulus specifications and trilinear coordinates of the Munsell standards for the four illuminants, A, C, D, and S, based on spectrophotometric data obtained at the National Bureau of Standards.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell designation number		
	X	Y	Z	x	y	z	X	Y	Z	x	y	z			
8/4	7.432	6.147	1.874	4.809	3.978	6.261	5.862	6.264	3.405	3.188	6.044	5.667	1.2317	2516	2.358
2	7.160	6.179	2.036	4.657	4.019	6.199	6.021	3.624	3.261	3.167	6.147	5.908	1.3338	2.421	2.327
7/8	6.654	4.769	1.168	5.251	3.815	5.144	4.244	3.936	3.861	3.154	4.614	3.903	1.7794	2.829	2.393
6	6.445	4.886	1.276	5.112	3.876	5.157	4.452	4.279	3.713	3.206	4.722	4.167	1.8437	2.725	2.405
2	5.856	4.876	1.485	4.746	3.993	4.763	4.521	4.095	3.343	3.134	4.652	4.309	1.9765	2.471	2.336
6/10	5.912	3.874	0.740	5.616	3.681	4.469	3.236	2.514	3.108	3.198	4.102	3.146	2.662	3.139	2.443
8	5.461	3.758	0.804	5.448	3.749	4.142	3.236	2.717	3.103	3.180	3.920	3.167	2.622	3.013	2.443
6	5.121	3.721	0.903	5.255	3.818	4.013	3.308	3.053	3.668	3.189	3.831	3.259	3.329	3.064	2.834
4	4.673	3.611	0.958	5.056	3.907	3.798	3.313	3.228	3.667	3.208	3.510	3.106	3.693	2.698	2.888
6	4.007	3.348	1.037	4.776	3.987	3.396	3.205	3.464	3.374	3.184	3.298	3.190	3.651	3.253	3.146
5/12	4.675	2.596	0.293	6.181	3.432	3.149	1.938	0.995	5.872	3.187	2.858	1.825	3.989	3.990	2.628
2	4.099	2.477	0.388	5.886	3.557	2.900	1.963	1.315	6.694	3.178	2.684	1.884	3.191	4.504	2.738
6	3.713	2.407	0.488	5.639	3.656	2.736	1.998	1.574	6.338	3.178	2.567	1.940	3.663	4.161	3.144
4	3.074	2.183	0.510	5.331	3.785	2.379	1.915	1.715	5.959	3.176	2.264	1.881	4.180	3.801	3.159
4/14	2.604	2.084	0.610	4.915	3.934	2.158	1.915	2.041	5.507	3.171	2.087	1.941	4.210	3.378	3.141
6	3.653	1.882	0.166	6.408	3.301	2.360	1.334	0.550	5.561	3.143	2.104	1.231	5.981	5.373	3.144
12	3.580	1.984	0.187	6.339	3.333	2.341	1.360	0.653	5.444	3.135	2.100	1.231	5.981	5.348	3.135
6	1.933	0.870	0.178	5.576	3.829	1.664	1.022	0.865	5.847	3.186	1.974	1.022	5.068	5.847	3.186
18	2.890	1.683	0.245	5.997	3.493	2.004	1.306	0.831	4.839	3.155	1.837	1.243	5.078	4.642	3.140
6	2.023	1.418	0.330	5.565	3.634	1.734	1.247	0.955	4.406	3.167	1.622	1.207	4.100	4.225	3.144
4	1.748	1.377	0.388	4.976	3.920	1.559	1.236	1.115	3.987	3.161	1.481	1.212	3.178	3.825	3.131
3/10	1.799	0.991	0.126	6.168	3.400	1.433	1.280	1.299	3.572	3.190	1.383	1.269	3.169	3.439	3.156
6	1.662	0.958	0.142	6.017	3.468	1.143	0.744	0.431	5.065	3.124	1.088	0.698	3.047	4.851	3.113
6	1.933	0.870	0.178	5.576	3.829	1.143	0.744	0.431	4.824	3.125	1.041	0.704	3.512	4.613	3.120
6	1.933	0.870	0.178	5.576	3.829	1.143	0.744	0.431	4.824	3.125	1.041	0.704	3.512	4.613	3.120
2	1.022	0.780	0.216	5.067	3.863	0.824	0.716	0.722	3.643	3.164	0.911	0.713	3.032	4.045	3.155
2/6	0.885	0.558	0.124	5.647	3.859	0.653	0.461	0.434	4.219	2.977	0.609	0.445	4.062	4.019	2.934
4	0.885	0.453	0.105	5.522	3.639	0.516	0.384	0.359	4.094	3.053	0.484	0.373	3.381	3.907	3.015
2	0.598	0.442	0.123	5.143	3.803	0.479	0.400	0.420	3.686	3.083	0.457	0.394	3.045	3.529	3.041
10R	7.899	6.491	1.724	4.902	4.028	6.539	6.115	5.744	3.554	3.324	6.339	6.087	1.293	2639	2.504
7/6	6.605	5.044	1.085	5.187	3.961	5.272	4.550	4.635	3.895	3.394	5.018	4.508	1.389	3.755	2.615
4	6.288	4.937	1.194	5.064	3.976	5.075	4.537	3.997	3.334	3.373	4.634	4.236	1.781	2.903	2.617
6/10	5.891	3.948	0.404	5.751	3.854	4.268	3.243	1.345	3.820	3.662	4.031	3.181	1.422	4.668	3.684
6	5.585	3.931	0.547	5.550	3.902	4.170	3.345	1.828	4.463	3.580	3.965	3.295	1.934	4.313	3.584
6	4.556	3.569	0.871	5.096	3.991	4.022	3.384	2.261	4.161	3.501	3.843	3.344	2.389	4.014	3.492
4	4.710	3.673	0.802	5.128	3.975	3.755	3.262	2.743	3.789	3.426	3.521	3.195	2.697	3.944	3.407
5/18	3.990	2.653	0.288	5.761	3.830	2.884	2.175	0.943	4.806	3.624	2.519	2.016	3.916	4.033	3.407
4	3.591	2.465	0.339	5.615	3.855	2.650	2.073	1.130	4.522	3.542	2.719	2.035	3.100	4.652	3.644
6	3.102	2.297	0.442	5.311	3.932	2.409	2.028	1.484	4.069	3.425	2.309	2.035	2.168	3.924	3.411
4/10	3.031	1.891	0.172	5.950	3.712	2.127	1.493	0.571	5.075	3.563	1.981	1.446	3.663	4.916	3.587
8	2.811	1.786	0.176	5.890	3.742	1.989	1.428	0.580	4.976	3.573	1.858	1.446	3.663	4.916	3.587
4	2.627	1.734	0.209	5.749	3.794	1.897	1.424	0.693	4.726	3.549	1.783	1.392	3.740	4.567	3.563
4	2.158	0.920	0.269	5.398	3.898	1.636	0.728	0.646	3.446	3.418	1.636	0.728	0.646	3.446	3.418
3/4	1.250	0.866	0.151	5.515	3.820	0.935	0.741	0.502	3.913	3.402	0.984	0.726	0.472	4.428	3.449
2/2	0.711	0.515	0.119	5.288	3.828	0.551	0.458	0.399	2.913	3.252	0.523	0.450	0.421	3.753	3.226
YR 8/4	7.567	6.314	1.590	4.891	4.081	6.255	5.970	5.271	3.575	3.412	6.068	5.950	5.557	3.453	3.386
2	7.041	6.096	1.824	4.706	4.075	6.007	5.917	6.039	3.434	3.260	5.849	5.904	6.358	3.230	3.260
7/10	6.736	4.888	0.415	5.395	4.060	4.941	4.178	1.309	4.738	4.007	4.896	4.129	1.378	4.603	4.047
6	6.059	4.857	0.488	4.949	4.042	4.703	4.180	2.635	4.083	3.629	4.504	4.140	2.776	3.944	3.626
8	6.194	4.746	0.627	5.269	4.035	4.787	4.262	2.676	4.083	3.635	4.584	4.223	2.817	3.944	3.626
4	5.867	4.724	1.052	5.039	4.057	4.521	4.376	3.484	3.478	3.327	4.556	4.349	3.674	3.622	3.357
2	5.362	4.561	1.287	4.783	4.069	4.253	4.375	3.433	3.322	3.289	4.396	4.362	4.505	3.315	3.289

TABLE II.—Continued.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number	
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z		
10V 8/8	8119	6627	4804	5221	4262	3419	6249	6049	2514	4219	4084	6004	6004	4104
6	7891	6583	1118	5061	4222	3611	6282	6114	3648	3916	3811	6067	6090	3846
6	7339	6279	1436	4875	4171	3565	6048	5972	4732	4610	3565	5868	5955	4989
7/10	5991	4740	0264	3449	4311	4171	4470	4179	0793	4734	4426	4288	4157	0834
6	5817	4763	0628	5190	4250	3984	4674	4397	1876	4187	4036	4374	4340	4187
6	5817	4809	0994	4967	4184	3656	4531	4347	2029	4155	3966	4567	4588	3448
6/10	5214	4084	0245	5464	4280	4280	4873	4602	3268	3747	3656	4567	4588	3448
8	4912	3887	0342	5374	4252	3713	3457	3457	1060	4512	4201	3569	3443	1114
8	4721	3770	0425	5295	4229	3611	3392	1352	4322	4059	4287	3468	3373	1425
4	4011	3376	0596	5024	4229	3218	3149	1952	3869	3786	3116	3116	3141	2060
4	2999	2379	0166	3409	4292	2266	2099	0807	4651	4306	2191	2099	0532	4344
5/8	2719	2256	0331	5143	4240	1848	1676	0476	4676	4384	2078	2078	2045	1137
4	2719	2256	0331	5143	4240	1848	1676	0476	4676	4384	2078	2078	2045	1137
4/4	1819	1467	0171	5243	4243	1413	1318	0548	4309	4019	1372	1320	0577	4198
3/2	0915	0755	0130	5084	4195	0730	0696	0421	3953	3768	0709	0696	0443	3836
2/2	0650	0537	0124	4956	4098	0529	0505	0410	3664	3496	0511	0502	0432	3538
Y 8/12	7051	6199	0257	5220	4589	5374	5706	0697	4563	4845	5178	5685	0731	4466
12	6855	5924	0285	5247	4535	5178	5443	0744	4536	4789	5178	5443	0744	4536
12	6855	5924	0285	5247	4535	5178	5443	0744	4536	4789	5178	5443	0744	4536
8	7015	6109	0625	5102	4443	5406	5723	1804	4177	4420	5205	5722	1883	4063
8	7093	6177	0917	5108	4448	5457	5794	1770	4192	4450	5253	5783	1847	4078
6	6938	6110	0904	4973	4379	5539	5784	2874	3902	4074	5253	5783	1847	4078
4	6626	5888	0901	4953	4374	5305	5566	2834	3871	4061	5136	5640	2978	3785
4	6526	5871	1239	4824	4162	5455	5651	4007	3609	3739	5293	5640	2978	3785
6	6357	5680	1610	4658	4162	5427	5570	5265	3337	3537	5293	5640	2978	3785
7/10	5246	4259	0278	4520	3520	4015	4199	0788	4492	4683	3881	4183	0825	4273
6	3715	3299	0828	4944	4305	3191	3110	2828	3907	3505	3882	4153	1628	4018
6	5124	4455	0500	5084	4270	4014	4158	1549	4129	4278	3882	4153	1628	4018
4	5079	4479	0856	4877	4301	4143	4282	2756	3630	3830	4022	4278	2901	3820
4	5054	4546	1250	4658	4190	4326	4454	4113	3356	3454	4225	4453	4334	3247
6/8	3880	3410	0220	5167	4540	3009	3145	0649	4423	4623	2922	3151	0681	3247
6	3994	3513	0224	5166	4544	3095	3242	0658	4425	4635	3006	3247	0690	3247
6	3954	3429	0298	5148	4465	3055	3179	0888	4289	4464	2951	3177	0933	3180
4	3715	3299	0828	4944	4305	3191	3110	2828	3907	3505	3881	4183	0825	4273
5/6	2406	2136	0180	5095	4523	1893	1984	0854	4271	4479	1846	1993	0583	3175
4	2432	2101	0314	4956	4389	1910	1987	0998	3902	4059	1860	1991	1081	3794
4	2376	2177	0549	4720	4217	2057	2117	1795	3446	3548	2005	2116	1889	3336
4/4	1495	1322	0180	4989	4411	1200	1243	0566	3988	4131	1172	1247	0594	3888
4	1628	1461	0351	4733	4247	1369	1419	1145	3481	3609	1335	1419	1205	3371
3/2	0788	0707	0183	4698	4213	0668	0689	0596	3419	3529	0652	0689	0627	3421
2/2	0557	0489	0117	4793	4204	0461	0472	0374	3528	3610	0449	0472	0392	3420
Y 8/12	4218	5167	1288	3952	4841	4038	4958	1333	3909	4800	5487	5958	1533	3909
12	4058	5058	1333	3909	4800	4409	5373	3358	3355	4089	4409	5373	3358	3355
8	4438	5429	3284	3375	4128	4438	5429	3284	3375	4128	4438	5429	3284	3375
5/8	4798	5429	5572	3031	3449	4602	5273	5459	5572	3031	3449	4602	5273	5459
12/1	4974	5440	7781	2734	2990	5224	5469	10233	2496	2614	4974	5440	7781	2734
6	4812	5302	1037	3747	4576	3196	3802	1037	3747	4576	3196	3802	1037	3747
7/10	3354	3861	2974	3292	3789	3354	3861	2974	3292	3789	3354	3861	2974	3292
4	3720	4091	5357	2825	3107	3720	4091	5357	2825	3107	3720	4091	5357	2825
6/8	4172	4361	8053	2515	2630	4172	4361	8053	2515	2630	4172	4361	8053	2515
6	2424	2858	1228	3723	4390	2400	2948	1240	3729	4414	2400	2948	1240	3729
6	2487	2932	1686	3501	4126	2487	2932	1686	3501	4126	2487	2932	1686	3501
12/1	2977	3113	5514	2557	2695	2977	3113	5514	2557	2695	2977	3113	5514	2557
5/6	1561	1815	1066	3514	4086	1561	1815	1066	3514	4086	1561	1815	1066	3514
3/4	1943	2059	3501	2590	2744	1943	2059	3501	2590	2744	1943	2059	3501	2590
4/4	1031	1156	1089	3146	3529	1031	1156	1089	3146	3529	1031	1156	1089	3146
4	1284	1377	2233	2624	2813	1284	1377	2233	2624	2813	1284	1377	2233	2624
3/2	0634	0671	1161	2870	2723	0634	0671	1161	2870	2723	0634	0671	1161	2870
2/2	0425	0456	0721	2653	2849	0425	0456	0721	2653	2849	0425	0456	0721	2653

TABLE II.—Continued.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number					
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z		x	y			
10Y 8/8	.6737	.6292	.0563	.4956	.4629	.5283	.6035	.5877	.0637	.1656	.3093	.4173	.4340	.5727	.2932	.3339	.4406	591
6	.6019	.6171	.0971	.4810	.4485	.5380	.5996	.5902	.3742	.3742	.4676	.4676	.4725	.5781	.2747	.2907	.3557	588
6	.6540	.6119	.1313	.4580	.4358	.5291	.5997	.5924	.3574	.3574	.4515	.4515	.4725	.5830	.2830	.2963	.3603	578
7/8	.6423	.6093	.1243	.4680	.4463	.5409	.5974	.5907	.3626	.3626	.4566	.4566	.4725	.5830	.2830	.2963	.3603	579
6	.4723	.4497	.0493	.4863	.4629	.5389	.6044	.5971	.4341	.4341	.5283	.5283	.5341	.6088	.3081	.3165	.3925	604
6	.4832	.4541	.0895	.4706	.4422	.5055	.4439	.2894	.3561	.3561	.3898	.3880	.3733	.4296	.2648	.2729	.3141	608
6/6	.3665	.3437	.0291	.4957	.4649	.5299	.3278	.0830	.1145	.1145	.4671	.4671	.2938	.3072	.1536	.1623	.1885	617
6	.3671	.3393	.0583	.4800	.4437	.5007	.3291	.1842	.3094	.3094	.4043	.4043	.2681	.3170	.1359	.1449	.1709	615
5/6	.2480	.2345	.0245	.4892	.4626	.5096	.2250	.0736	.1066	.1066	.4536	.4536	.1687	.2119	.1395	.1449	.1709	619
4	.2431	.2292	.0342	.4800	.4525	.5089	.2224	.1059	.1373	.1373	.4219	.4219	.1745	.2131	.1402	.1456	.1716	610
4	.2843	.2680	.0182	.4740	.4537	.5185	.2185	.1468	.1792	.1792	.4394	.4394	.1843	.2231	.1482	.1536	.1796	612
3/2	.0383	.0383	.0119	.4666	.4399	.5053	.0493	.0493	.0493	.0493	.3313	.3313	.0483	.0772	.1302	.1356	.1616	932
2/2	.0535	.0493	.0119	.4666	.4399	.5053	.0484	.0484	.0484	.0484	.3331	.3331	.0424	.0473	.0737	.0791	.1051	939
GY 8/8	.5994	.6050	.0728	.4693	.4737	.4857	.6022	.2046	.3758	.3758	.4684	.4684	.4731	.5903	.3753	.3900	.4279	433
6	.6046	.5941	.1017	.4650	.4568	.4977	.5929	.3048	.3567	.3567	.4249	.4249	.4432	.5858	.2741	.2760	.3657	432
4	.6293	.6035	.1436	.4572	.4384	.5341	.6041	.5522	.3358	.3358	.3799	.3781	.5015	.6008	.3675	.3746	.4650	434
2	.6266	.5850	.1727	.4527	.4226	.5451	.5851	.5006	.3224	.3224	.3461	.3461	.5343	.5856	.3891	.3923	.4628	435
7/6	.4413	.4413	.0540	.4657	.4474	.5094	.4816	.4816	.3619	.3619	.4665	.4665	.3104	.4419	.2892	.2987	.3233	442
8	.4523	.4518	.0684	.4588	.4434	.5094	.4816	.4816	.3619	.3619	.4665	.4665	.3104	.4419	.2892	.2987	.3233	443
6	.4507	.4518	.0684	.4640	.4651	.4716	.4509	.3023	.3408	.3408	.3896	.3896	.3625	.4324	.2879	.2879	.3829	441
4	.4523	.4372	.0964	.4588	.4434	.5094	.4816	.4816	.3619	.3619	.4665	.4665	.3104	.4419	.2892	.2987	.3233	444
4	.4539	.4260	.1224	.4528	.4250	.5044	.4261	.3970	.3239	.3239	.3500	.3500	.3860	.4326	.2710	.2710	.3166	439
6/8	.3183	.3257	.0380	.4667	.4776	.2612	.3238	.1104	.3756	.3756	.4657	.4657	.2554	.3253	.1153	.1153	.1369	437
2	.3296	.3223	.0644	.4601	.4601	.2772	.3217	.2013	.3644	.3644	.4020	.4020	.2708	.3225	.1113	.1113	.1366	440
2	.3248	.3248	.0644	.4601	.4601	.2772	.3217	.2013	.3644	.3644	.4020	.4020	.2708	.3225	.1113	.1113	.1366	441
5/8	.1948	.2097	.0208	.4582	.4529	.1621	.2100	.0612	.3742	.3742	.4846	.4846	.1593	.2110	.0643	.0643	.0856	450
6	.1900	.2062	.0298	.4575	.4741	.1669	.2066	.0915	.3589	.3589	.4443	.4443	.1636	.2075	.0962	.0962	.1140	448
4	.2078	.2074	.0379	.4587	.4576	.1756	.2070	.1196	.3497	.3497	.4121	.4121	.1720	.2077	.1190	.1190	.1408	449
4/6	.2201	.2098	.0555	.4535	.4323	.1908	.2097	.1804	.3284	.3284	.3611	.3611	.1868	.2101	.1900	.1900	.2184	448
4	.1219	.1248	.0202	.4568	.4677	.1031	.1249	.0626	.3547	.3547	.4298	.4298	.1013	.1256	.0658	.0658	.0822	445
4	.1307	.1311	.0257	.4546	.4560	.1117	.1313	.0814	.3442	.3442	.4048	.4048	.1098	.1320	.0856	.0856	.1031	446
3/2	.0743	.1354	.0352	.4515	.4327	.1229	.1357	.1376	.3396	.3396	.3607	.3607	.1248	.1360	.1438	.1438	.1608	445
2/2	.0780	.0747	.0187	.4533	.4399	.0673	.0748	.0604	.3323	.3323	.3694	.3694	.0646	.0741	.1175	.1229	.1472	459
2/2	.0466	.0457	.0115	.4489	.4399	.0402	.0461	.0363	.3278	.3278	.3762	.3762	.0394	.0463	.0379	.0379	.0488	462
10GY 8/6	.5302	.5600	.1396	.4312	.4554	.4695	.5793	.4334	.3168	.3168	.3908	.3908	.4629	.5828	.4526	.3089	.3890	863
4	.5840	.6002	.1659	.4326	.4446	.5203	.6181	.5252	.3128	.3128	.3715	.3715	.5126	.6211	.5498	.3045	.3689	861
7/8	.3503	.4147	.0810	.4141	.4902	.3115	.4399	.2359	.3155	.3155	.4455	.4455	.3085	.4439	.2447	.3094	.4452	635
4	.3201	.4433	.0913	.4307	.4502	.3709	.4407	.3488	.3128	.3128	.3770	.3770	.3741	.4594	.3051	.3094	.4738	616
6/10	.2321	.2845	.0459	.4125	.5058	.2037	.3032	.1284	.3207	.3207	.4772	.4772	.2015	.3060	.1331	.1345	.1777	634
8	.2597	.3049	.0558	.4186	.4914	.2273	.3224	.1594	.3206	.3206	.4548	.4548	.2243	.3190	.1649	.1649	.2141	625
6	.2604	.3000	.0618	.4185	.4822	.2301	.3168	.1861	.3139	.3139	.4322	.4322	.2270	.3190	.1648	.1648	.2141	624
4	.2738	.2969	.0773	.4225	.4582	.2461	.3101	.2438	.3076	.3076	.3876	.3876	.2431	.3120	.1751	.1751	.2297	621
5/8	.1421	.1785	.0288	.4068	.5107	.1260	.1910	.0833	.3147	.3147	.4772	.4772	.1244	.1925	.0869	.0869	.1081	628
4	.1699	.2016	.0371	.4158	.4935	.1490	.2141	.1081	.3161	.3161	.4544	.4544	.1469	.2158	.1129	.1129	.1389	628
4/6	.1074	.1268	.0271	.4109	.4852	.0985	.1355	.0803	.3066	.3066	.4343	.4343	.0941	.1365	.0837	.0837	.1094	722
3/4	.1128	.1264	.0323	.4154	.4656	.1016	.1337	.0902	.3028	.3028	.3985	.3985	.1003	.1345	.0950	.0950	.1251	630
2/2	.0411	.0425	.0119	.4307	.4447	.0364	.0440	.0375	.3087	.3087	.3731	.3731	.0357	.0442	.0393	.0393	.0488	937
8/6	.5243	.5243	.1810	.4025	.4442	.4479	.5595	.5677	.2844	.2844	.3552	.3552	.4443	.5635	.5006	.2780	.3526	214
5/6	.5626	.5626	.1912	.4192	.4385	.5003	.5681	.6123	.2917	.2917	.3486	.3486	.5009	.6079	.6449	.2921	.3319	213
7/6	.3333	.4019	.1402	.3878	.4536	.3296	.4328	.2739	.3652	.3652	.4418	.4418	.3264	.4418	.2496	.2681	.3628	755
4	.3703	.4072	.1403	.4035	.4436	.3491	.4340	.2847	.3540	.3540	.4340	.4340	.3462	.4370	.2642	.2780	.3509	184
2	.4095	.4095	.1424	.4260	.4259	.3755	.4231	.4626	.2977	.2977	.3355	.3355	.3703	.4248	.2853	.2894	.3317	182
6/6	.2084	.2707	.0925	.3645	.4736	.2043	.3040	.2765	.2604	.2604	.3873	.3873	.2043	.3070	.2858	.2557	.3855	206
4	.2587	.2929	.0997	.3972	.4497	.2453	.3151	.3128	.2809	.2809	.3699	.3699	.2436	.3175	.3262	.2745	.3578	202
2	.2834	.2909	.1001	.4203	.4314	.2614	.3032	.3237	.2943	.2943	.3413	.3413	.2584	.3046	.3398	.2862	.3374	204

TABLE II.—Continued.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number											
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z												
G	5/8	1158	1631	0528	3492	4916	1134	1875	1521	2503	4139	1128	1896	1568	2457	4128	1182	2067	2747	3044	3045	3182	3447	
	6	1298	1666	0581	3703	4755	1234	1869	1626	2626	3943	1235	1896	1694	2565	3917	1304	2029	2644	2645	2845	3182	3447	
	2	1749	1807	0623	4184	4660	1618	1898	2017	2929	3419	1607	1896	1749	2617	3153	1435	1941	2617	2618	2818	3153	3447	
	4/4	0958	1170	0383	3816	4060	0914	1291	1183	2698	3810	0908	1302	1240	2633	3774	0964	1383	2263	2692	3002	3002	3402	3774
	3/4	0581	1218	0414	4138	4368	0545	0803	0682	2685	3956	0532	0810	0712	2823	3426	0563	0869	1281	2077	2702	3022	3022	3426
	2/2	0608	0661	0222	4080	4432	0360	0703	0396	2859	3467	0557	0707	0741	2779	3527	0310	0735	1361	2184	2711	2711	3184	3527
	8/2	5883	5799	1993	4302	4341	5340	5965	6447	3008	3360	5357	5984	6754	2921	3326	5448	6075	12407	2377	2539	2539	3539	3539
	7/4	4088	4389	1629	4045	4344	3864	4672	5197	2813	3402	3864	4672	5197	2813	3402	4067	4879	9906	2157	2157	2589	2589	3539
	6/6	2669	3193	1259	3748	4480	2623	3538	3901	2607	3517	2608	3568	4051	2551	3488	2938	3805	7290	2029	2733	2733	3539	3539
	4	2810	3179	1237	3889	4400	2720	3458	3935	2690	3420	2700	3480	4118	2622	3379	2938	3674	7534	2029	2737	2737	3539	3539
	5/6	1285	1738	0743	3413	4615	1315	2013	2210	2375	3635	1555	2063	2409	2580	3423	1701	2191	4405	2050	2641	2641	3539	3539
	4/4	0941	1149	0457	3696	4310	0933	1283	1429	2560	3520	0929	1294	1493	2580	3483	1025	1392	2715	1997	2713	2713	3539	3539
	4/4	0941	1149	0457	3696	4310	0933	1283	1429	2560	3520	0929	1294	1493	2580	3483	1025	1392	2715	1997	2713	2713	3539	3539
	2/2	0626	0369	0148	3864	4378	0311	0407	0463	2852	3445	0307	0409	0485	2587	3411	0334	0439	0879	2021	2659	2659	3539	3539
	8/2	5955	5887	2146	4257	4208	5473	6082	6981	2953	3281	5394	6101	7318	2867	3243	5673	6219	13470	2237	2452	2452	3539	3539
	7/4	4169	4367	1736	4058	4251	3963	4634	5613	2789	3261	3924	4657	5880	2713	3221	4240	4839	10803	2133	2434	2434	3539	3539
	2	4559	4549	1716	4212	4203	4224	4729	5575	2908	3255	4167	4746	5881	2824	3217	4416	4863	10742	2206	2429	2429	3539	3539
	6/6	2738	3143	1406	3757	4313	2731	3473	4458	2561	3257	2716	3498	4650	2500	3220	3034	3743	8460	1991	2456	2456	3539	3539
	2	2868	3156	1344	3893	4284	2801	3425	4304	2660	3253	2781	3447	4501	2592	3213	3066	3640	8238	2052	2436	2436	3539	3539
	5/6	1397	1807	0915	3366	4385	1619	2117	2955	2248	3247	1471	2117	2955	2248	3247	1760	2354	5854	2163	2416	2416	3539	3539
	4	1667	1908	0874	3747	4289	1667	2112	2773	2545	3224	1659	2112	2893	2483	3185	1862	2281	5270	1978	2423	2423	3539	3539
	4/6	0868	1147	0634	3278	4328	0934	1354	1937	2211	3205	0933	1368	2003	2168	3179	1098	1538	3574	1769	2476	2476	3539	3539
	4	1087	1267	0591	3690	4230	1100	1413	1876	2506	3218	1095	1423	1958	2447	3179	1240	1456	3558	2088	2393	2393	3539	3539
	3/6	0482	0640	0380	3209	4262	0525	0767	1165	2135	3123	0524	0775	1210	2088	3090	0635	0886	2179	1716	2394	2394	3539	3539
	4	0942	0644	0258	3848	4245	0589	0727	0953	2602	3202	0586	0743	0998	2533	3158	0650	0780	1831	2608	2388	2388	3539	3539
	2/4	0296	0344	0180	3610	4198	0293	0395	0550	2367	3190	0289	0398	0572	2299	3159	0331	0444	1030	1834	2462	2462	3539	3539
	2/2	0323	0347	0155	3912	4204	0308	0379	0492	2613	3216	0304	0381	0514	2533	3178	0336	0410	0939	1996	2432	2432	3539	3539
	8/2	6173	6057	2293	4251	4171	5695	6258	7475	2931	3221	5614	6277	7834	2846	3182	5940	6406	14423	2219	2393	2393	3539	3539
	7/4	4052	4256	1892	3972	4173	3953	4555	5179	2692	3102	3924	4579	6481	2619	3056	4362	4795	1954	2668	2274	2274	3539	3539
	6/6	2518	2983	1389	3552	4208	2653	3375	4059	2590	3041	2751	3402	5289	2538	3000	3106	3663	1887	2254	2254	3539	3539	
	4	1453	1833	1174	3260	4108	1627	2160	3099	2173	2886	1631	2180	3846	2384	2847	2004	2454	6996	1754	2148	2148	3539	3539
	5/6	1644	1853	0957	3260	4160	1691	2062	3090	2469	3010	1688	2076	3246	2407	2962	1965	2241	5977	1930	2201	2201	3539	3539
	4/6	0891	1135	0730	3233	4118	0992	1349	2276	2149	2922	0993	1361	2361	2355	2887	1216	1543	4256	1733	2199	2199	3539	3539
	4/4	0991	1146	0603	3617	4183	1027	1290	1933	2416	3036	1025	1300	2023	2357	2991	1200	1417	4275	1895	2238	2238	3539	3539
	3/6	0427	0584	0446	2930	4006	0503	0727	1365	1940	2801	0505	0735	1412	1903	2773	0648	0864	2527	1604	2139	2139	3539	3539
	2/2	0355	0669	0405	3399	4111	0359	0728	1276	2246	2937	0354	0784	1329	2195	2897	0717	0878	2414	1788	2190	2190	3539	3539
	8/2	5768	5749	2457	4128	4114	5481	6025	8080	2798	3076	5419	6046	8484	2716	3031	5934	6522	15691	2129	2243	2243	3539	3539
	7/6	3851	4085	2067	3850	4004	3877	4436	6773	2570	2941	3857	4460	7103	2502	2892	4433	4737	13110	1990	2126	2126	3539	3539
	4	4159	4283	2011	3979	4099	4077	4575	6605	2672	2998	4297	4731	6444	2717	3058	4548	4819	12809	2051	2173	2173	3539	3539
	6/6	2370	2739	1726	3467	4008	2595	3128	5595	2293	2764	2600	3152	5849	2241	2717	3177	3473	10730	1828	1998	1998	3539	3539
	4	2811	3175	1575	3816	4046	2898	3254	4661	2661	2981	2901	3245	4876	2665	2931	3281	3371	9048	2098	2147	2147	3539	3539
	5/6	1331	1632	1212	3187	3910	1553	1940	3881	2106	2631	1562	1972	4046	2689	2879	1996	2222	7385	1720	1915	1915	3539	3539
	4/6	1539	1737	1057	3182	4008	1652	1959	3485	2349	2768	1664	1977	4616	2294	2719	2015	2153	6658	1862	1989	1989	3539	3539
	2	0760	0949	0865	4023	4053	0946	1172	2747	1945	2409	0954	1183	2855	1911	2370	1947	2012	5493	2060	2129	2129	3539	3539
	8	0735	0906	0823	2983	3677	0900	1119	2610	1945	2418	0907	1131	2710	1910	2382	1206	1328	4908	1620	1785	1785	3539	3539
	6	0868	1067	0877	3087	3795	1045	1287	2806	2033	2506	1045	1299	2921	1995	2464	1375	1493	5522	1679	1823	1823	3539	3539
	4	1163	1278	0805	3583	3937	1237	1447	2621	2351	2728	1236	1457	2749	2271	2677	1505	1666	5076	1858	1962	1962	3539	3539

TRISTIMULUS SPECIFICATION

TABLE II.—Continued.

Munsell notation	For JCI Illuminant A			For JCI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number						
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z		x	y				
B 4/2	1.250	1.282	0.624	1.231	1.374	2.057	2.640	2.947	1.231	1.380	2.162	2.564	2.897	1.388	1.455	4.007	2.026	2.124	777
3/6	0.059	0.044	0.886	0.026	0.082	1.830	1.920	2.463	0.028	0.089	1.894	1.886	2.430	0.833	0.954	3.411	1.603	1.835	494
4	0.027	0.024	0.886	0.014	0.045	1.840	1.915	2.463	0.014	0.045	1.840	1.915	2.463	0.722	0.785	2.937	1.055	1.931	495
2	0.037	0.058	0.844	0.034	0.078	1.140	2.557	2.872	0.034	0.078	1.140	2.557	2.872	0.426	0.456	2.017	1.615	1.791	496
2/2	0.035	0.049	0.180	0.030	0.038	0.583	2.552	2.946	0.032	0.038	0.611	2.474	2.900	0.374	0.412	1.124	1.960	2.157	779
10B 8/2	0.610	0.802	2.745	0.628	0.814	9.106	2.844	2.984	0.612	0.826	9.575	2.785	2.937	0.609	0.706	1.770	2.149	2.151	942
7/6	4.053	4.205	2.348	4.150	4.576	7.761	2.517	2.776	4.133	4.599	8.145	2.449	2.725	4.851	4.906	1.507	2.154	1.954	673
4	2.885	2.992	4.026	4.186	4.526	6.921	2.678	2.895	4.148	4.542	7.271	2.599	2.846	4.693	4.757	1.3474	2.047	2.075	780
6/6	2.806	2.995	1.924	2.960	3.320	6.015	2.413	2.699	2.965	3.339	6.310	2.351	2.647	3.571	3.612	1.1668	1.894	1.916	675
5/6	1.714	1.877	1.319	1.907	2.132	3.468	2.278	2.543	1.913	2.145	3.554	2.221	2.491	2.395	2.363	0.8423	1.814	1.906	676
4	1.894	1.959	1.131	1.963	2.134	3.768	2.495	2.714	1.957	2.145	3.964	2.427	2.659	2.329	2.292	0.7371	1.942	1.911	640
4/8	0.903	1.064	1.009	1.063	1.292	3.271	1.986	2.260	1.141	1.303	3.410	1.949	2.226	1.539	1.510	0.6239	1.658	1.626	669
6	1.022	1.132	0.924	1.196	1.316	3.081	2.150	2.366	1.141	1.303	3.196	2.101	2.315	1.567	1.491	0.5901	1.749	1.664	782
3/8	1.142	1.185	0.715	1.198	1.299	2.384	2.454	2.661	1.196	1.305	2.599	2.387	2.605	1.440	1.402	0.4668	1.918	1.867	652
6	0.587	0.632	0.596	0.673	0.765	1.929	1.998	2.273	0.704	0.820	2.267	1.765	2.054	0.907	0.990	4.454	1.547	1.537	661
2/2	0.326	0.345	0.237	0.349	0.396	0.618	2.311	2.577	0.673	0.771	2.009	1.959	2.230	0.907	0.894	3.669	1.659	1.635	659
	0.326	0.345	0.237	0.349	0.396	0.618	2.311	2.577	0.673	0.771	2.009	1.959	2.230	0.907	0.894	3.669	1.659	1.635	660
	0.326	0.345	0.237	0.349	0.396	0.618	2.311	2.577	0.673	0.771	2.009	1.959	2.230	0.907	0.894	3.669	1.659	1.635	943a
	0.326	0.345	0.237	0.349	0.396	0.618	2.311	2.577	0.673	0.771	2.009	1.959	2.230	0.907	0.894	3.669	1.659	1.635	943b
PB 7/6	0.675	0.623	2.709	0.618	0.630	9.034	2.875	2.949	0.612	0.630	9.509	2.781	2.900	0.606	0.635	1.7686	2.163	2.114	808
4	4.482	4.311	2.329	4.430	4.556	7.802	2.639	2.714	4.390	4.567	8.211	2.557	2.660	5.074	4.794	1.5282	2.017	1.906	506
2	4.800	4.551	2.232	4.614	4.743	7.466	2.743	2.819	4.559	4.751	7.860	2.655	2.767	5.138	4.930	1.4635	2.080	1.996	786
6/8	3.079	4.771	2.097	4.757	4.907	6.988	2.857	2.947	4.688	4.914	7.354	2.765	2.898	5.137	5.037	1.3678	2.154	2.112	807
6	3.174	3.059	1.036	3.214	3.310	6.601	2.475	2.549	3.200	3.322	7.225	2.483	2.544	4.900	4.958	1.2655	1.923	1.775	1307
6	3.297	3.184	1.918	3.364	3.404	6.472	2.541	2.574	3.345	3.413	6.818	2.464	2.514	4.986	4.962	1.2727	1.960	1.780	512
4	3.608	3.426	1.779	3.520	3.589	5.973	2.691	2.744	3.483	3.596	6.293	2.605	2.689	4.987	4.971	1.1756	2.048	1.926	787
2	3.587	3.338	1.532	3.432	3.432	2.831	2.831	2.847	3.336	3.436	5.407	2.739	2.821	3.684	3.528	1.0078	2.135	2.039	784
5/10	1.867	1.969	1.681	2.188	2.263	5.620	2.173	2.247	2.202	2.277	5.899	2.122	2.194	2.887	2.846	1.0945	1.763	1.554	1303
8	2.056	2.094	1.598	2.293	2.345	5.378	2.289	2.341	2.299	2.356	5.659	2.229	2.284	2.929	2.887	1.0544	1.824	1.611	517
6	2.090	2.063	1.347	2.202	2.241	4.551	2.448	2.492	2.198	2.250	4.797	2.377	2.434	2.687	2.614	0.9965	1.910	1.717	516
2	2.137	2.013	0.973	2.153	2.160	3.277	2.703	2.658	2.029	2.040	3.457	2.678	2.759	2.287	2.186	0.6464	2.096	1.975	785
4/10	1.142	1.219	1.253	1.184	1.184	4.202	2.035	2.039	1.460	1.456	4.409	1.993	1.987	2.009	1.968	0.8182	1.694	1.406	532
6	1.173	1.211	1.065	1.384	1.387	3.597	2.174	2.178	1.395	1.395	3.784	2.122	2.122	1.846	1.858	0.7053	1.766	1.490	522
8	1.227	1.232	0.908	1.353	1.364	3.078	2.334	2.354	1.356	1.370	3.245	2.271	2.295	1.716	1.493	0.6070	1.850	1.609	521
4	1.313	1.268	0.762	1.344	1.355	2.583	2.544	2.569	1.338	1.358	2.727	2.467	2.505	1.600	1.439	0.5109	1.964	1.766	520
2	1.350	1.268	0.612	1.296	1.313	2.064	2.774	2.809	1.282	1.315	2.179	2.684	2.753	1.446	1.356	0.4080	2.011	1.970	519
3/12	0.574	0.627	0.907	0.832	0.802	2.983	1.803	1.737	0.847	0.808	3.109	1.778	1.697	1.246	0.977	0.700	1.573	1.233	3037
6	0.653	0.692	0.836	0.871	0.874	2.790	1.934	1.873	0.884	0.850	2.921	1.899	1.825	1.257	0.995	0.5400	1.643	1.300	3038
10	0.653	0.692	0.836	0.871	0.874	2.790	1.934	1.873	0.884	0.850	2.921	1.899	1.825	1.257	0.995	0.5400	1.643	1.300	534
8	0.621	0.649	0.686	0.768	0.768	2.406	2.036	1.990	0.796	0.773	2.421	1.994	1.938	1.099	0.886	0.4500	1.695	1.366	532
6	0.661	0.663	0.568	0.749	0.749	1.923	2.222	2.180	0.768	0.753	2.021	2.166	2.123	1.007	0.834	0.3784	1.790	1.483	530
4	0.659	0.643	0.441	0.779	0.779	1.500	2.422	2.409	0.702	0.701	1.533	2.352	2.348	0.871	0.755	0.2968	1.896	1.642	528
4	0.698	0.660	0.345	0.810	0.810	1.168	2.695	2.711	0.679	0.690	1.284	2.608	2.652	0.783	0.718	0.2315	2.052	1.882	526
2/6	0.326	0.337	0.309	0.412	0.405	1.251	1.993	1.959	0.416	0.406	1.310	1.950	1.916	0.577	0.475	0.2421	1.662	1.367	804
4	0.330	0.334	0.309	0.388	0.385	1.033	2.150	2.129	0.389	0.387	1.085	2.096	2.070	0.518	0.376	0.2151	1.645	1.469	805
2	0.362	0.333	0.269	0.378	0.378	0.876	2.459	2.490	0.378	0.384	0.817	2.384	2.433	0.487	0.413	1.1524	1.910	1.724	806
10PB 8/2	7.035	6.393	2.801	6.499	6.937	9.576	2.907	2.907	6.384	6.946	9.846	2.809	2.858	6.949	6.625	1.8314	2.179	2.078	945
7/6	4.889	4.300	2.155	4.598	4.565	7.316	2.825	2.681	4.519	4.537	7.171	2.723	2.626	5.077	4.463	4.440	2.117	1.861	796
4	5.023	4.454	2.019	4.634	4.498	6.798	2.969	2.824	4.547	4.491	7.163	2.807	2.772	4.982	4.571	3.366	2.174	1.994	790
6/8	3.680	3.152	1.952	4.199	3.874	3.623	3.200	2.654	3.577	3.190	7.053	2.567	2.720	4.253	3.510	3.520	2.017	1.570	900
6	3.887	3.600	1.781	3.447	3.161	3.988	2.732	2.409	3.542	3.082	6.923	2.732	2.480	4.324	3.676	1.1278	2.133	1.852	791a
5/10	2.291	1.933	1.503	2.401	2.413	3.291	2.483	2.072	2.401	2.009	5.616	2.395	2.004	3.024	3.465	1.1278	2.133	1.852	791b
6	2.291	1.933	1.503	2.401	2.413	3.291	2.483	2.072	2.401	2.009	5.616	2.395	2.004	3.024	3.465	1.1278	2.133	1.852	803
4	2.419	2.050	1.464	2.476	2.126	5.110	2.550	2.181	2.469	2.121	5.415	2.547	2.123	3.029	2.230	1.0244	1.954	1.439	801

TABLE II.—Continued.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number					
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z						
10PB 4/4	1468	1264	0732	4239	3649		1426	1288	2526	2721	2458		1644	1326	5046	2051	1655	793
3/10	0868	0659	0577	3769	2859		1031	0693	2843	2258	1517		1465	0750	5864	1813	0929	864
8	0874	0703	0599	4019	3230		0936	0724	2143	2461	1903		1208	0760	4365	1908	1201	701
6	0855	0696	0628	4114	3348		0883	0711	1874	2546	2032		1100	0741	3801	1950	1313	700
4	0841	0700	0469	4184	3483		0841	0711	1643	2630	2253		1009	0739	3308	1996	1461	794
2/6	0833	0351	0277	4081	3306		0453	0358	0988	2529	1985		0574	0372	2002	1947	1261	707
4	0447	0370	0281	4071	3369		0466	0380	0992	2535	2067		0581	0397	2005	1949	1331	878
P 8/4	7006	5974	2643	4484	3824		6318	5940	8897	2986	2808		6671	5984	7480	2214	1986	282
7/6	6706	5915	2313	4490	3961		5992	5897	7723	3055	3007		5858	5884	5143	2272	2176	284
4	5314	4492	2133	4577	3673		4972	4381	7256	2994	2638		4824	4341	4333	2198	1830	1337
2	4740	4129	1685	4491	3912		4256	4108	5658	3035	2940		4674	4287	3380	2211	1956	274
6/8	4211	3252	1848	4533	3479		3846	3157	6363	3277	2362		4441	4123	1132	2255	2093	278
6	4044	3280	1693	4570	3602		3681	3177	5748	3014	2514		4246	3187	3633	2116	1388	268
4	3984	3380	1503	4489	3751		3522	3181	6111	2789	2146		4009	3211	1485	2149	1025	2037
2	3764	3257	1368	4487	3882		3610	3170	5296	2958	2704		3863	3329	10460	2188	1886	264
5/10	3004	2129	1422	4583	3248		2768	2039	5008	2820	2078		3563	3253	9092	2240	2045	262
8	2930	2177	1313	4564	3391		2682	2107	4574	2864	2250		3156	2949	10065	2067	1342	228
6	2612	2018	1094	4563	3526		2368	1965	3774	2921	2454		2998	2120	9150	2102	1486	226
4	2313	1904	0964	4518	3677		2188	1934	3297	2950	2606		2591	1974	7520	2144	1633	224
4	2177	1662	1054	4740	2966		1960	1650	3748	2823	1977		2362	1945	6845	2176	1792	222
4/12	2177	1362	1054	4740	2966		1960	1650	3748	2823	1977		2362	1945	6845	2176	1792	222
12	2381	1474	1060	4844	2999		2101	1336	3802	2902	1845		1885	1212	5976	2665	1715	693
10	2027	1373	0930	4681	3171		1832	1292	3276	2863	2019		2007	1292	4044	2733	1759	250
8	1851	1339	0829	4605	3332		1704	1278	2954	2871	2153		1763	1261	3471	2714	1942	258
6	1700	1282	0721	4590	3463		1539	1240	2503	2914	2348		1655	1258	3146	2732	2076	816
4	1668	1322	0654	4578	3628		1496	1289	2240	2977	2566		1492	1223	2649	2781	2281	246
3/10	1481	1262	0585	4506	3837		1337	1248	1850	3015	2814		1458	1233	2367	2851	2505	244
6	1189	0896	0579	4626	3133		1105	0759	2072	2807	1929		1070	0743	2204	2664	1850	298
2/6	0966	0730	0414	4579	3460		0909	0744	1778	2837	2113		0970	0732	1889	2701	2039	296
2	0909	0749	0341	4546	3746		0881	0705	1446	2906	2325		0856	0696	1533	2774	2257	294
4	0503	0373	0223	4577	3398		0511	0346	0955	2820	1911		0797	0731	1232	2887	2650	292
4	0851	0410	0248	4558	3563		0467	0358	0796	2879	2208		0485	0353	0849	1024	2676	1824
2	0842	0428	0248	4558	3563		0512	0354	0885	2869	1996		0502	0382	1808	1113	1412	1313
2	0803	0390	0208	4564	3544		0460	0378	0733	2930	2406		0450	0362	1669	1246	1483	249
8/4	7343	6280	2446	4570	3908		6490	6182	8230	3180	2958		6637	6158	8677	2990	2935	810
7/8	6373	4972	1983	4782	3731		5445	4675	6745	3217	2798		5251	4679	7121	3079	2744	1974
6	5944	4839	1886	4692	3820		5152	4675	6383	3178	2884		4995	4602	6207	2342	2342	1540
6	5797	4799	1837	4662	3860		5048	4657	6210	3172	2926		4907	4628	6554	3050	2877	1539
6/6	5544	4387	1447	4795	3679		4847	4301	5951	3090	2723		4745	4313	5768	3078	2688	1537
5/10	4220	3372	1332	4729	3779		3637	3238	4515	3193	2843		3518	3209	4764	3062	2792	1536
6	3908	2520	1140	5164	3370		3161	2226	3999	3368	2371		2979	2154	4244	3178	2292	296
8	3559	2406	1052	5072	3429		2905	2174	3644	3331	2492		2751	2116	3858	3153	2425	1535
6	3236	2315	0955	4974	3558		2688	2129	3299	3312	2623		2568	2088	3494	3151	2562	1534
4/10	2542	1546	0759	5244	3190		2534	2143	3098	3259	2186		2441	2116	3274	3117	2702	1532
6	2332	1548	0678	5006	3472		2045	1331	2713	3359	2166		1920	1278	2890	3154	2100	1530
6	2031	1525	0627	4855	3646		1860	1428	2377	3295	2426		1775	1373	2425	3128	2426	1529
3/10	1328	0765	0461	5199	2996		1730	1420	2170	3247	2680		1668	1408	2299	3102	2620	1528
8	1331	0810	0431	5175	3149		1101	0648	1694	3198	1883		1038	0614	1814	2990	1784	1527
6	1191	0798	0406	4972	3332		1011	0722	1448	3179	2270		1034	0674	1666	3065	1996	1526
4	1117	0795	0354	4927	3510		0948	0731	1245	3242	2500		0960	0704	1543	3007	2191	1525
2/6	0670	0426	0244	4999	3178		0579	0377	0898	3123	2032		0555	0362	0864	2985	1941	1524
4	0601	0407	0216	4910	3327		0521	0370	0779	3119	2215		0501	0366	0834	2984	2133	1523
RP 8/6	7512	6268	2126	4723	3951		6411	6058	7081	3240	3009		6215	6019	7454	3157	3057	1369
4	7344	6219	2144	4676	3959		6321	6050	7136	3240	3150		6140	6019	7511	3122	3060	1368
2	7511	6548	2244	4607	4017		6540	6435	7454	3201	3150		6375	6417	7844	3089	3110	1367

TRISTIMULUS SPECIFICATION

TABLE II.—Continued.

Munsell notation	For ICI Illuminant A			For ICI Illuminant C			For Illuminant D			For Illuminant S			Munsell painting number									
	X	Y	Z	X	Y	Z	X	Y	Z	X	Y	Z										
RP 7/8	6536	5137	1760	4866	3824	3724	5474	4845	5937	3367	2980	4792	6264	4231	2934	5346	4690	11712	2458	2157	1366	
6	6500	5070	1719	4819	3945	3864	5482	4955	5975	3340	3019	4910	6301	3209	2974	5373	4814	11771	2447	2192	1365	
4	5671	4851	1660	4655	3982	3724	4913	4727	5547	3235	2811	4786	6107	3068	3038	5151	4777	11319	2424	2248	1364	
6/10	5504	3810	1278	5197	3597	3582	4384	3389	4388	3605	3173	4160	5307	3444	3370	4139	3173	8747	2577	1976	1362	
8	5213	3715	1229	5132	3658	3582	4186	3349	4197	3568	2855	3987	5282	3438	2804	3963	3152	8344	2563	2039	575	
8	4852	3642	1207	4829	3852	3852	4150	3456	4294	3414	2998	3794	5272	3416	2821	3769	3142	8102	2520	2114	1360	
4	4851	3642	1207	4829	3852	3852	4150	3456	4294	3414	2998	3794	5272	3416	2821	3769	3142	8102	2520	2114	1360	
5/10	4308	2724	1133	4470	3957	3724	3337	3169	3799	3238	3075	3250	4119	3031	2631	3335	3117	7476	2395	2133	1358	
8	3813	2537	1084	4316	3536	3460	2984	2266	2858	3708	2741	2818	4143	3025	2682	2778	2029	5739	2634	1924	1356	
8	3330	2346	1072	4164	3639	3570	2670	2099	2661	3593	2826	2542	3820	3428	2771	2531	1964	5327	2577	1999	1355	
4	2968	2271	1068	4941	3780	3780	2470	2110	2623	3429	2929	2379	2080	3287	2879	2406	2017	5222	2494	2091	1354	
2	2692	2225	1062	4740	3918	3818	2304	2138	2559	3291	3054	2237	2125	2698	3169	2280	2089	5035	2425	2221	1353	
4/12	2756	1654	1057	5583	3118	3118	2072	1326	1934	3862	2534	1796	2089	3634	2640	1832	1540	3034	2612	1921	1352	
8	2503	1577	1050	5429	3421	3421	1921	1341	1874	3862	2612	1796	2089	3634	2640	1832	1540	3034	2612	1921	1352	
4	2365	1598	1053	5236	3539	3539	1881	1406	1918	3614	2701	1784	2194	1995	3532	1778	1212	3812	2612	1782	1350	
4	2104	1550	1058	5019	3698	3698	1734	1418	1855	3464	2833	1665	1397	1966	3311	1688	1344	3846	2572	1881	554	
4	1847	1509	1058	4755	3886	3886	1582	1445	1785	3288	3003	1536	1435	1885	3163	1575	1408	3531	2418	2161	1348	
3/10	1654	1493	1031	4570	3217	3217	1209	1074	1726	3928	2413	1110	1073	1206	3677	1084	1064	3327	2674	1583	1346	
8	1445	1485	1028	4576	3312	3312	1082	1076	1033	3836	2592	1003	10674	1103	3607	1082	10623	2120	2646	1671	1345	
8	1087	1075	1025	5171	3602	3602	883	8674	1085	3762	2762	883	10660	10952	3401	883	10660	10952	3401	2702	1344	
8	1087	1075	1025	5171	3602	3602	883	8674	1085	3762	2762	883	10660	10952	3401	883	10660	10952	3401	2702	1344	
2	0884	0695	1024	4851	3816	3816	0749	0654	0831	3351	2930	0725	0648	0880	3217	0742	0631	1657	2448	2081	1343	
2	0843	0520	1019	5397	3328	3328	0656	0440	0721	3609	2421	0615	0424	0773	3395	0630	0397	1493	2500	1576	1342	
2/6	0736	0476	1017	5327	3445	3445	0577	0411	0605	3621	2582	0543	0399	0646	3421	0549	0376	1239	2537	1736	1341	
4	0565	0420	1015	5002	3715	3715	0465	0386	0499	3442	2859	0445	0386	0529	3287	0452	0367	1099	2484	1844	1340	
10RP 8/6	7907	6533	2106	4779	3949	3949	6712	6351	7048	3351	3121	6513	6215	7456	3227	6079	6066	13929	2471	2284	883	
8	7400	6000	2088	4701	3984	3984	6378	6051	6748	3282	3072	6108	5818	7150	3072	5818	6820	13929	2471	2284	883	
7/8	6363	4810	1415	5055	3871	3871	5152	4412	4777	3593	3077	4941	4354	5045	3445	4830	4169	9450	2618	2259	1391	
6	6237	4877	1415	4951	3871	3871	5129	4551	4983	3498	3104	4935	4502	5257	3359	4673	4350	9820	2559	2284	1390	
6/10	5586	4632	1458	4833	3930	3930	4789	4397	4896	3401	3122	4639	4368	5166	3273	4082	4639	4244	9653	2503	2290	1389
8	5182	3668	1004	5259	3722	3722	4255	3210	3256	3994	2994	4009	3123	3447	3790	2952	3764	2902	6492	2861	2205	1388
8	4751	3553	1039	5085	3803	3803	3835	3240	3521	3620	3057	3676	3195	3721	3471	3016	3589	3049	6983	2635	2238	1386
8	4356	2690	1059	5743	3482	3482	3208	2180	2948	4315	2931	2974	2688	2755	3108	2887	2649	1888	4115	2697	2233	1385
5/16	4005	2540	1059	5344	3560	3560	2966	2111	2251	4168	2966	2771	2039	2165	3973	2923	2549	1856	4103	2906	2182	1383
6	3638	2512	10657	5344	3691	3691	2819	2191	2251	3882	3018	2673	2143	2386	3712	2976	2536	1956	4504	2806	2210	1382
4/10	2988	2463	1071	5038	3843	3843	2634	2260	2435	3594	3083	2537	2235	2376	3452	3042	2484	2130	4843	2627	2252	1381
8	2649	1625	1040	5665	3475	3475	1948	1332	1400	4163	2846	1943	1289	1431	4167	2764	1754	1151	2728	3114	2044	1380
6	2310	1495	10379	5521	3574	3574	1740	1262	1312	4356	2924	1840	1278	1488	3955	2793	1678	1164	2829	2959	2053	1379
3/10	1756	1090	10337	5932	3246	3246	1223	0735	0849	4356	2621	1107	0690	0902	4094	2552	1010	0612	1744	3000	1818	1376
8	1502	0875	10210	5805	3383	3383	1074	0698	0742	4273	2776	0986	0664	0791	4039	2719	0904	0597	1513	3000	1979	1375
6	1371	0856	10219	5603	3500	3500	1016	0712	0765	4075	2855	0945	0685	0814	3867	2803	0885	0628	1550	2889	2051	1374
2/6	1057	0743	10215	5247	3686	3686	0834	0658	0741	3745	2945	0799	0644	0787	3566	2896	0771	0607	1489	2689	2118	1373
4	0844	0506	10152	5620	3367	3367	0626	0416	0544	3949	2621	0579	0397	0581	3718	2551	0558	0364	1115	2740	1788	1372
6	0676	0403	10140	5326	3571	3571	0526	0395	0491	3726	2799	0496	0385	0475	3274	2444	0486	0361	0991	2643	1966	1371
N 0/6/	9974	9083	3158	4489	4089	4089	8863	9076	10461	3121	3196	8684	9087	11006	3019	3155	9066	20429	2335	2356	60	
N 0/5/	9166	8344	2867	4498	4095	4095	8123	8329	9476	3133	3212	7955	8328	9966	3034	3155	8201	8313	18482	2343	2376	1486
N 0/4/	9171	8333	2859	4504	4092	4092	8119	8311	9455	3137	3211	7950	8310	9944	3034	3171	8193	8292	18445	2346	2374	1486
N 0/3/	7994	7266	2329	4494	4085	4085	7095	7256	8367	3123	3194	6948	7254	8801	3021	3153	7183	7247	16330	2335	2356	1177
N 0/2/	6315	5759	1966	4498	4102	4102	5591	5751	6484	3136	3226	5474	5750	6815	3035	3188	5632	5741	12625	2347	2392	1176
N 0/1/	4839	4424	1590	4459	4077	4077	4337	4433	5285	3086	3154	4257	4434	5565	2986	3121	4444	4438	10349	2311	2308	1175
N 0/0/	3324	3032	1076	4473	4079	4079	2972	3032	3579	3102	3164	2916	3033	3768	3001	3121	3036	3030	7010	2322	2317	1071
N 0/0/	1985	1207	1068	4457	4062	4062	1189	1209	1415	3080	3131	1185	1209	1415	2976	3089	1222	1209	2891	2306	2278	1070
N 0/0/	0717	0651	10237	4469	4054	4054	0															

TABLE III. Effect of backing on colors of Munsell samples. Values are computed from the spectrophotometric curves shown in Fig. 10.

Munsell sample	Values obtained with white backing minus values obtained with black backing		
	ΔY	Δx	Δy
R 4/14	+0.0007	+0.0010	-0.0002
R 8/4	+0.0043	+0.0023	+0.0001
BPB 8/2	+0.0000 ₁	+0.0000 ₁	.0000 ₀
N 9.6/	+0.0034	+0.0007	+0.0003

shown the curves obtained on four Munsell samples, each sample being run first with white backing and then with black backing. The spectral reflections of the backings used for Fig. 10 are shown in the figure. It will be noted that the effect of backing becomes appreciable at wave-lengths greater than 550 m μ , approximately, if the values of apparent reflectance are greater than 0.60 or 0.65. (The slight separation of the curves for BPB 8/2 between 480 and 600 millimicrons is not considered significant. It is probably caused by non-uniformity of the sample. Differences of this magnitude can be obtained when a sample is re-run with the same backing if the sample and backing have been removed and reinserted between runs.)

The effects of such spectrophotometric differences on the computed values of Y , x , and y are shown in Table III. Since these samples probably illustrate the maximum effects to be expected from the two backings it is apparent that the differences in color caused by measurement with white or with black backing are mostly unimportant.

The use of calibration curves on each record sheet—those enabling corrections of wave-length errors, 100 percent and zero curve deviations, and aging of the MgO comparison surface, as used at the National Bureau of Standards—enables spectrophotometric data to be obtained with much less care and worry regarding certain details of operation than if these calibration curves were omitted. Omission of the curves makes it necessary for the operator to take great care, for example, in the insertion of the graph sheet in the instrument, in continually checking the wave-length calibration of the instrument and in controlling or watching the graph paper for expansion or shrinkage with change of hu-

midity. A new MgO comparison surface must be prepared each day and the question of reproducibility of such surfaces thus enters. The possibility of erratic differences in results between the two investigations is thus present but since different actual samples were measured no further conclusions can be reached regarding the erratic differences between the Glenn-Killian and the National Bureau of Standards data.

With respect to differences between values of X , Y , Z , x , y , and z resulting from differences in computational procedure—30 selected ordinates as against weighted ordinates at every 10 m μ —it has been shown (21) that such differences are small for samples such as those considered here, much less than some of the differences shown. Only small and unimportant errors are therefore to be expected from this difference in computational procedure.

Detailed comparison of the values of x and y obtained by Glenn and Killian with those obtained at the National Bureau of Standards may be made by inspection of Figs. 2 to 8 or by study of the published data. Only two additional points will be noted here.

1. Certain consistent differences in the respective chromaticities are apparent when the (x, y) -data for certain groups of samples having the same hue designations (Figs. 2 to 8) are replotted in a single graph regardless of value level. This is particularly noticeable for the 10GY, GY, P, 10RP, and R samples. However, although the maximum (x, y) difference³ between the Glenn-Killian and the National Bureau of Standards data is $\Delta x=0.0143$ and $\Delta y=0.0156$, inspection of Figs. 2 to 8 shows that in the great

TABLE IV.

Munsell value	Average differences in Y , Glenn-Killian values minus National Bureau of Standards values
8	+0.0031
7	+0.0019
6	-0.0006
5	+0.0018
4	+0.0020
3	+0.0029
2	+0.0039
Average	+0.002

³ For YR 2/2. As is to be expected the discrepancies in chromaticity are greatest at the lowest value level.

majority of cases there is good agreement between the two sets of data. Further effort to resolve the differences would seem unwarranted.

2. Differences in the average values of Y obtained in the two investigations are shown in Table IV. The greatest differences are at the extremes. That for Munsell value 8 may be caused partially by the differences in backing. That for Munsell value 2 may indicate a real instrumental difference relating to the zero readings of the respective instruments; none of the 33 individual differences going into this average is negative. While the individual differences on which the values of Table IV are based reached a maximum of 0.036 (sample P 7/2), the final average value of +0.002 for all of the data is very small.⁴

VI. DERIVATION OF ISCC-NBS COLOR NAMES FROM ICI TRISTIMULUS DATA

The Munsell notations for chroma and hue may be determined from Figs. 2 to 8 for any color whose chromaticity falls within these diagrams by plotting its trilinear coordinates on the appropriate value-level diagrams and estimating the relative position of this point with respect to the points representing the nearest samples of constant hue and the nearest lines of constant chroma. The Munsell value of the color is found by interpolation or extrapolation between the values of apparent reflectance (Y) of the Munsell standards for Illuminant C in Table II. By referring to the color-name charts in RP 1239, the ISCC-NBS color name descriptive of that color will be found. Likewise in disk colorimetry (21), given percentages of a certain set of disks may be transformed into trilinear coordinates, plotted in a similar-manner, and the corresponding color name found. Thus the ISCC-NBS color name for a color may be found by the use of any spectrophotometer or colorimeter (22), (23) whose resultant values may be transformed into data

⁴ Differences in Munsell value corresponding to the average differences in Y shown in Table IV are significant only at the lowest values. The difference, $\Delta Y = 0.0039$, corresponds to $\Delta V = 0.15$ at value level 2. It is believed that the NBS data are more reliable than the Glenn-Killian data at these low value levels. For the neutral samples $N1/$, $N2/$, and $N3/$, the Glenn-Killian values of Y are from 0.005 to 0.006 higher than the NBS values given in Table II. Independent check of these samples visually on the Priest-Lange reflectometer gave values lower than the Glenn-Killian values by 0.004, and closely agreeing with the NBS data of Table II.

based on the ICI standard observer and coordinate system. Likewise, any color system may be used as a comparison standard if the trilinear coordinates of each sample in that system are plotted on the (x, y) -diagrams and the ISCC-NBS color name determined through conversion to the Munsell notation.

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Trichromatic Specifications for Intermediate and Special Colors of the Munsell System*

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THE Munsell concept of hue, value, and chroma (1), (2),¹ and the Munsell notation for recording colors in terms of numerical scales of these three attributes, are daily proving themselves useful in color work (3), (4). The usefulness of the Munsell charts in color measurement grows in direct ratio to the accuracy and availability of standard colorimetric data that become available regarding the colors on those charts. Actually no one color is more a "Munsell color" than any other, but the charts are devised so that selected points of intersection in the color solid are illustrated, and these are often called "Munsell colors."

The 1929 edition of the *Munsell Book of Color* (5) contained chips representing 10 major hues on value levels 2/ to 8/, at all even steps of chroma, and 10 hues intermediate between these major hues on value levels 2/ to 8/, at even steps of chroma beginning with /4 chroma. These are the standard colors for which I.C.I. tristimulus values and trilinear coordinates have been reported for Illuminant C by Glenn and Killian (6), for Illuminants A, C, Macbeth

7500°K, and a limit blue sky by Kelly, Gibson, and Nickerson (7).

Because many people find that direct reference to color charts is the simplest method for obtaining color notations, and because many people are not able satisfactorily to interpolate between hues that are as far apart as one-twentieth of the hue circuit, "Munsell colors" now appear in an additional series of 20 hues, each of the 20 new hues being intermediate between a pair of the earlier standard 20 hues. All /2 chromas omitted in the 1929 edition have been added. These colors total 561 samples (in addition to the 421 samples of the standard series). In addition to these colors for new charts to be inserted in the early series, several other series of colors have been made available for special purposes. Thus, there is a series of 100 hues at 5/5, 50 hues at their maxima chromas, a 50-step value scale, a 20-step value scale, a series of pinks, of browns, and others. Each of these series becomes more useful as standard I.C.I. colorimetric data become available for it.

The authors have therefore measured these colors spectrophotometrically and have com-

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¹ Numbers in parentheses refer to literature cited.

TABLE I. Trichromatic specification, dominant wave-length, and excitation purity for intermediate 20 Munsell hues, and for /2 chromas omitted in (6) and (7).

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.	Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.		
	X	Y	Z	x	y					X	Y	Z	x	y					
2.5R	8/4	.5997	.5656	.6190	.336	.317	611.0	7.0	1593**	2.5YR	7/10	.5024	.4041	.1597	.471	.379	590.5	60.0	1555
		.5926	.5738	.6323	.330	.319	602.0	6.0	1899*		8	.4703	.4004	.2271	.428	.365	590.0	44.5	1553
	7/8	.5023	.4243	.4315	.370	.312	631.0	15.0	1584	6	.4765	.4229	.3041	.396	.351	589.9	32.3	1554	
		.5025	.4424	.4625	.357	.314	625.0	12.0	1583	4	.4726	.4372	.3740	.368	.341	589.0	22.2	1872**	
	6/10	.5061	.4666	.4909	.346	.319	609.0	10.2	1898**	2	.4656	.4491	.4380	.344	.332	588.0	13.5	1871**	
		.4648	.4448	.4897	.332	.318	609.0	6.2	1897**	6/13	.4240	.3250	.0613	.523	.401	590.3	80.1	1578	
	8	.4172	.3102	.2804	.414	.308	638.0	25.5	1582	12	.4102	.3173	.0745	.511	.396	590.5	75.2	1546	
		.3870	.3062	.2938	.392	.310	634.0	20.4	1581	10	.3992	.3170	.1103	.483	.384	590.6	64.2	1550	
	6	.3810	.3216	.3282	.370	.312	633.0	14.8	1580	8	.3742	.3063	.1372	.458	.375	590.4	55.2	1549	
		.3739	.3342	.3482	.354	.316	617.0	11.8	1896	6	.3644	.3121	.1854	.423	.362	589.9	42.3	1548	
	2	.3320	.3100	.3404	.338	.316	620.0	7.5	1895	4	.3702	.3326	.2576	.386	.346	590.0	28.8	1870	
										2	.3304	.3157	.2944	.351	.336	588.0	16.2	1869	
5/10	.3043	.2064	.1713	.446	.303	650.0	32.8	1586	5/10	.2634	.2004	.0592	.504	.383	592.0	70.0	1551		
	.2779	.1957	.1713	.431	.304	660.0	29.0	1585	8	.2585	.2040	.0819	.475	.375	591.8	59.7	1532A		
4	.2672	.2039	.1917	.403	.308	646.0	22.5	1579	6	.2448	.2002	.0998	.449	.367	591.3	51.0	1533A		
	.2516	.2083	.2088	.376	.312	635.0	16.5	1894	4	.2321	.1980	.1340	.412	.351	592.2	36.2	1868		
2	.2218	.2004	.2130	.349	.316	620.0	10.4	1893	2	.2302	.2142	.1910	.362	.337	590.0	19.8	1867		
									4/8	.1802	.1384	.0524	.486	.373	593.0	62.0	1547		
4/10	.1972	.1261	.1074	.458	.293	492.8c	37.2	1587	6	.1747	.1386	.0662	.460	.365	592.9	53.5	1545		
	.1866	.1263	.1124	.439	.297	492.6c	32.0	1588	4	.1703	.1444	.0968	.414	.351	593.2	37.0	1866		
6	.1682	.1228	.1145	.415	.303	492.5c	25.2	1589	2	.1461	.1320	.1120	.374	.338	592.2	23.1	1865		
	.1575	.1248	.1246	.387	.306	700.0	19.0	1892	3/6	.1123	.0876	.0380	.472	.368	593.0	57.5	1886		
2	.1427	.1248	.1333	.356	.311	670.0	11.0	1891	4	.0933	.0769	.0485	.427	.351	593.8	40.6	1552		
									2	.0851	.0761	.0632	.379	.339	592.5	24.8	1864		
3/10	.1261	.0771	.0701	.461	.282	493.7c	42.0	1592	2/3	.0632	.0538	.0431	.395	.336	590.7	28.0	1556		
	.1079	.0714	.0650	.442	.292	493.2c	34.3	1591	2	.0481	.0438	.0402	.364	.332	594.5	18.5	1863		
8	.1057	.0749	.0730	.417	.295	493.3c	28.4	1590	7.5YR	8/6	.6079	.5792	.3883	.386	.368	583.0	34.0	1565	
	.0926	.0712	.0713	.394	.303	492.8c	21.5	1890	4	.5922	.5796	.5004	.354	.347	583.0	20.0	1849		
2	.0814	.0693	.0738	.363	.309	492.0c	13.0	1889	2	.5705	.5684	.5494	.338	.337	582.0	13.0	1848**		
									7/10	.4533	.4023	.1039	.472	.419	584.0	71.0	1564		
2/6	.0647	.0460	.0493	.404	.287	494.6c	29.5	1596	8	.4605	.4178	.1635	.442	.401	583.8	58.0	1563		
	.0566	.0436	.0489	.380	.292	495.0c	22.5	1888	6	.4533	.4195	.2292	.411	.381	584.0	44.4	1562		
2	.0491	.0408	.0461	.361	.300	495.0c	16.2	1887	4	.4427	.4267	.3399	.366	.353	584.0	25.0	1847		
									2	.4274	.4228	.4029	.341	.337	583.0	14.0	1846		
7.5R	8/4	.5982	.5548	.5477	.352	.326	596.0	14.0	1543**	6/10	.3645	.3207	.0773	.478	.420	584.3	73.0	1561	
		.5703	.5517	.5635	.338	.327	590.5	10.5	1911*		8	.3689	.3298	.1134	.454	.406	584.2	62.8	1560
7/8	.4912	.4040	.3118	.407	.335	599.3	30.8	1544	6	.3425	.3140	.1503	.424	.389	583.9	50.2	1559		
	.4942	.4257	.3715	.383	.330	599.8	23.0	1542A	4	.3409	.3243	.2459	.374	.356	584.5	26.0	1845		
6	.4742	.4328	.4071	.361	.329	595.8	17.1	1910**	2	.3235	.3168	.2908	.348	.340	583.8	16.5	1844		
	.4577	.4373	.4423	.342	.327	592.5	11.4	1909**	5/8	.2318	.2036	.0600	.468	.411	584.8	67.8	1558		
6/10	.4033	.3030	.1791	.456	.342	599.9	46.0	1531A	6	.2204	.1974	.0813	.441	.395	584.7	56.4	1557		
	.3867	.3049	.2057	.431	.340	599.0	38.5	1530A	4	.2058	.1916	.1198	.398	.370	584.3	38.0	1843		
8	.3791	.3156	.2454	.403	.336	598.2	30.1	1529A	2	.2002	.1935	.1740	.353	.341	585.5	18.0	1842		
	.3614	.3194	.2849	.374	.331	597.5	21.0	1908	4/4	.1522	.1367	.0677	.427	.383	585.3	49.5	1594		
2	.3326	.3115	.3113	.348	.326	595.9	12.7	1907	2	.1313	.1252	.0950	.374	.356	584.0	27.5	1841		
									3/2	.0792	.0734	.0485	.394	.365	585.0	35.0	1840		
5/12	.2974	.1911	.0669	.535	.344	603.5	67.8	1537A	10YR	8/2	.5684	.5718	.5685	.333	.335	573.0	8.4	1855*	
	.2830	.1946	.0933	.496	.341	603.0	56.1	1536A		7/2	.4461	.4479	.4134	.341	.343	580.0	15.5	1754*	
8	.2697	.1934	.1084	.472	.338	602.5	49.2	1535A	5/2	.2864	.2843	.2499	.349	.346	581.0	18.5	1755*		
	.2580	.1961	.1331	.439	.334	602.5	39.2	1534A	2	.2170	.2143	.1780	.356	.352	581.0	22.0	1756*		
4	.2459	.2045	.1687	.397	.330	600.3	27.2	1906	4/2	.1387	.1349	.0995	.372	.362	581.8	28.5	1851*		
	.2242	.2029	.1968	.359	.325	599.6	15.7	1905	3/2	.0851	.0819	.0543	.384	.370	582.2	34.2	1758*		
4/12	.2208	.1370	.0505	.541	.335	606.8	67.0	1541A	2/2	.0538	.0515	.0411	.367	.352	584.3	25.0	934*		
	.2011	.1337	.0653	.503	.334	606.4	56.3	1540A	2.5Y	9 ^{ab} /4	.8208	.8353	.7147	.346	.352	578.0	19.5	1752	
6	.1857	.1272	.0694	.486	.333	605.8	51.5	1539A	2	.7996	.8166	.7907	.332	.339	577.0	12.0	1751		
	.1762	.1302	.0817	.454	.335	602.8	43.6	1538A	9/8	.7321	.7401	.3639	.399	.403	577.8	47.0	1730		
4	.1585	.1266	.0983	.413	.330	602.8	31.4	1904	6	.7049	.7142	.4749	.372	.377	578.0	33.0	1729		
	.1476	.1295	.1220	.370	.324	602.0	18.0	1903	4	.7212	.7352	.5770	.355	.362	577.5	24.0	1728		
3/10	.1380	.0894	.0408	.514	.333	607.0	59.2	1525A	2	.7070	.7242	.7116	.330	.338	576.5	11.5	1727		
	.1226	.0840	.0478	.482	.330	607.0	49.8	1527A	8/12	.5789	.5783	.0897	.464	.464	578.3	81.0	1577		
6	.1080	.0797	.0557	.444	.327	607.0	38.8	1528A	10	.5930	.5981	.1489	.443	.446	577.8	70.4	1567		
	.1015	.0786	.0614	.420	.325	607.0	32.0	1902	8	.5797	.5816	.2200	.420	.421	578.1	57.6	1566		
2/4	.0869	.0741	.0709	.375	.320	609.8	18.1	1901	6	.5526	.5579	.3036	.391	.395	578.0	42.5	1568		
	.0631	.0491	.0447	.402	.313	623.0	23.8	1526A	4	.5665	.5761	.4101	.365	.371	577.5	29.5	1733		
2	.0485	.0418	.0420	.366	.316	612.0	15.6	1900	2	.5627	.5728	.5564	.333	.339	578.0	12.0	1732		
									7/10	.4079	.4084	.0723	.459	.460	578.2	78.5	1576		
10R	8/2	.5946	.5795	.5842	.338	.330	588.0	11.0	1862*	8	.4101	.4108	.1121	.440	.440	578.2	68.0	1575	
		.4766	.4516	.4544	.345	.327	593.5	12.0	1861*	6	.4216	.4212	.1760	.414	.413</				

TABLE I.—Continued.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wavelength	Excitation purity	Munsell production no.			
	X	Y	Z	x	y						
2.5Y	6/8	.3263	.3273	.0850	.442	.443	578.1	69.5	1573		
		.3210	.3180	.1071	.430	.426	578.8	61.8	1572		
		.3310	.3347	.1867	.388	.393	578.0	41.5	1737		
	2	.3137	.3185	.2685	.348	.354	578.0	20.0	1736		
		5/6	.2124	.2096	.0577	.443	.437	578.9	67.9	1571	
			.2058	.2072	.1115	.392	.395	578.5	43.5	1739	
	.2073		.2094	.1789	.348	.352	579.0	19.8	1738		
	4/4	.1294	.1272	.0604	.408	.401	579.5	49.0	1570		
		.1257	.1260	.1006	.357	.358	579.0	23.5	1740		
		.0827	.0828	.0604	.366	.366	579.0	28.2	1741		
	5Y	9 ¹⁰ /6	.7541	.7956	.5137	.366	.386	574.6	33.6	1713	
			.7532	.7864	.6448	.345	.360	574.3	21.0	1712	
.7694			.7936	.7566	.332	.341	575.5	12.5	1711		
9/14		.6168	.6597	.0760	.456	.488	575.4	85.2	1705		
		.6283	.6688	.1773	.426	.454	575.3	68.0	1704		
		.6317	.6706	.2289	.413	.438	575.2	60.0	1703		
		.6375	.6728	.3090	.394	.416	575.2	49.1	1702		
		.6443	.6826	.4031	.372	.395	574.8	37.8	1701		
		.6523	.6851	.4911	.357	.375	574.8	28.0	1700		
2		.6824	.7018	.6844	.330	.339	575.0	11.5	1699		
		7.5Y	9 ¹⁰ /8	.7686	.8404	.3232	.398	.435	573.5	55.0	1726
				.7754	.8370	.4670	.373	.403	573.2	40.0	1725
.7929	.8440			.6182	.352	.374	573.0	26.7	1724		
2	.7823	.8160	.7698	.330	.345	573.0	13.0	1723			
	9/10	.6029	.6786	.1174	.431	.485	573.0	78.0	1718		
		.6097	.6730	.2529	.397	.438	573.0	56.0	1717		
.6165		.6668	.3841	.370	.400	573.0	38.1	1716			
6	.6490	.6894	.5222	.349	.370	573.5	25.0	1715			
	.6679	.6968	.6677	.329	.343	573.0	12.0	1714			
	8/10	.5076	.5688	.0763	.440	.493	573.4	82.3	1710		
.5077		.5597	.1898	.404	.445	573.0	60.0	1709			
.5367		.5821	.3189	.373	.405	573.0	40.8	1708			
4	.5447	.5810	.4135	.354	.378	573.5	28.0	1707			
	.5568	.5826	.5381	.332	.347	572.8	14.2	1706			
	7/10	.4030	.4457	.0685	.439	.486	573.9	80.0	1722		
.4031		.4415	.1210	.417	.458	573.9	66.4	1884			
.3979		.4284	.1791	.396	.426	574.1	52.2	1721			
6	.3997	.4233	.2700	.366	.387	574.2	34.0	1720			
	.4155	.4324	.3956	.334	.348	574.0	15.0	1719			
	6/8	.2719	.3005	.0597	.430	.475	573.9	74.4	1883		
.2899		.3134	.1170	.402	.435	574.2	56.5	1882			
.2984		.3188	.1889	.370	.396	574.0	37.5	1881			
4	.3048	.3177	.2783	.338	.353	574.0	17.5	1880			
	5/6	.1987	.2168	.0590	.419	.457	574.0	66.5	1879		
		.1955	.2088	.1110	.380	.405	574.2	42.5	1878		
.1876		.1969	.1599	.344	.362	574.0	21.5	1877			
4/4	.1213	.1313	.0533	.397	.429	574.0	53.5	1876			
	.1181	.1247	.0960	.349	.368	573.8	24.0	1875			
	.0655	.0690	.0452	.365	.384	577.0	35.5	1874			
10Y	8/2	.5529	.5850	.5486	.328	.347	570.5	13.0	2133		
		.4168	.4414	.3926	.333	.353	571.5	16.0	2132		
		.3112	.3310	.2840	.336	.357	571.3	18.0	2131		
	5/2	.2135	.2292	.1798	.343	.368	571.8	22.8	2130		
		.1390	.1501	.1144	.344	.372	571.0	24.2	2129		
		.0684	.0743	.0596	.338	.367	569.8	21.2	2128*		
	2/2	.0495	.0535	.0408	.344	.372	571.0	24.2	2127*		
		2.5GY	8/10	.5010	.6088	.1096	.411	.499	569.8	76.2	2205
				.4962	.6021	.1452	.399	.484	569.2	69.0	2204
	.5122			.5989	.2686	.371	.434	569.0	48.0	2203	
	2	.5277	.5880	.4086	.346	.386	569.1	28.3	2202		
		.5585	.5986	.5295	.331	.355	569.7	16.0	2201		
7/8		.3516	.4317	.0894	.403	.495	569.1	72.8	2200		
	.3692	.4376	.1655	.380	.450	569.1	56.0	2199			
	.3883	.4385	.2833	.350	.395	568.7	31.8	2198			
2	.3960	.4263	.3835	.328	.354	568.4	15.0	2197			
	6/8	.2725	.3290	.0647	.409	.494	569.9	74.1	2196		
		.2701	.3232	.1028	.388	.464	569.2	60.6	2195		
.2800		.3195	.1735	.362	.413	569.5	40.0	2194			
2	.2815	.3041	.2496	.337	.364	570.2	20.0	2193			
	5/6	.1784	.2101	.0715	.388	.457	569.8	58.5	2192		
		.1800	.2091	.1011	.367	.427	569.0	45.0	2191		
.1953		.2145	.1560	.345	.379	569.8	26.3	2190			
2.5GY	4/4	.1167	.1344	.0641	.370	.426	569.7	45.7	2189		
		.1233	.1350	.1008	.343	.376	570.0	25.0	2188		
		.0677	.0748	.0576	.338	.374	568.4	23.0	2187		
	7.5GY	8/8	.4553	.5828	.2857	.344	.440	562.3	42.5	2185	
			.4798	.5892	.3614	.336	.411	562.3	32.5	2184	
			.4931	.5786	.4286	.329	.386	563.2	23.7	2183	
		2	.5357	.5853	.5576	.319	.349	562.5	11.1	2182	
			7/10	.3336	.4628	.1425	.355	.493	561.8	59.7	2181
				.3318	.4460	.1756	.348	.468	561.5	50.9	2180
	.3503	.4504		.2240	.342	.440	561.8	41.7	2179		
	6	.3745	.4474	.3067	.332	.396	562.2	27.5	2178		
		.3909	.4310	.4070	.318	.351	561.0	11.5	2177		
6/10		.2355	.3274	.0947	.358	.498	562.0	61.7	2176		
	.2422	.3253	.1184	.353	.474	562.3	54.2	2175			
	.2369	.3110	.1404	.344	.452	561.7	45.7	2174			
4	.2527	.3105	.2034	.330	.405	560.5	29.1	2173			
	.2753	.3088	.2754	.320	.359	561.1	14.3	2172			
	5/6	.1568	.2100	.0887	.344	.461	561.1	48.2	2171		
.1601		.1979	.1256	.331	.409	560.8	30.6	2170			
.1887		.2137	.1842	.322	.364	561.2	16.0	2169			
4/6	.1032	.1348	.0711	.334	.436	559.8	38.7	2168			
	.1082	.1353	.0870	.327	.409	559.4	29.8	2167			
	.1278	.1461	.1219	.323	.369	561.2	17.7	2166			
	3/4	.0631	.0799	.0515	.324	.411	558.0	29.5	2165		
		.0633	.0742	.0585	.323	.379	559.9	20.0	2164		
		.0458	.0524	.0458	.318	.364	558.3	15.0	2163		
10GY	8/2	.5124	.5667	.5601	.313	.346	556.0	8.8	2107		
		.3847	.4279	.4257	.311	.346	553.0	8.2	2106		
		.2642	.2995	.2874	.310	.352	551.0	9.8	2105		
	5/2	.1766	.2017	.1873	.312	.357	553.8	11.5	2104		
		.1139	.1312	.1215	.311	.358	552.0	11.5	2103		
		.0611	.0731	.0620	.311	.373	552.0	15.6	2102		
	2/2	.0424	.0496	.0454	.308	.361	549.2	11.8	2101*		
		2.5G	8/6	.4626	.5869	.5002	.298	.379	539.0	14.2	2162
				.5047	.6007	.5540	.304	.362	543.5	11.0	2161
	.5255			.5922	.5939	.307	.346	546.0	7.2	2160	
	7/8	.3217	.4637	.3355	.287	.414	536.0	21.3	2159		
		.3335	.4475	.3627	.292	.391	535.8	16.2	2158		
.3498		.4348	.3933	.297	.369	535.8	11.3	2157			
2	.3746	.4473	.4410	.297	.354	528.0	7.6	2156			
	6/8	.1886	.3047	.1912	.276	.445	533.8	27.5	2155		
		.2142	.3076	.2252	.287	.412	535.5	20.5	2154		
.2479		.3162	.2780	.294	.376	534.0	12.6	2153			
2	.2746	.3168	.3170	.302	.349	536.0	7.0	2152			
	5/8	.1217	.2002	.1193	.276	.454	535.2	29.7	2151		
		.1435	.2087	.1437	.289	.421	539.0	23.6	2150		
.1580		.2106	.1672	.295	.393	538.5	17.4	2149			
2	.1774	.2075	.2035	.302	.353	536.0	8.0	2148			
	4/6	.0869	.1366	.0906	.277	.435	432.3	24.8	2147		
		.0978	.1352	.1068	.288	.398	533.0	17.2	2146		
.1169		.1401	.1298	.302	.362	540.2	10.6	2145			
3/4	.0562	.0828	.0591	.284	.418	534.0	21.8	2144			
	.0667	.0839	.0717	.300	.378	541.0	14.2	2143			
	.0398	.0477	.0459	.298	.357	532.0	8.5	2142			
7.5G	8/4	.4785	.5634	.6287	.286	.337	502.0	7.8	2126**		
		.5215	.5800	.6413	.299	.333	510.0	3.8	2125**		
		.3401	.4465	.4644	.272	.357	504.5	12.4	2124		
	2	.3527	.4336	.4768	.279	.343	503.0	10.2	2123**		
		.3975	.4488	.5000	.295	.333	506.0	4.8	2122		
		6/6	.2244	.3226	.3274	.257	.369	503.5	17.4		

TABLE I.—Continued.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wavelength	Excitation purity	Munsell production no.
	X	Y	Z	x	y			
7.5G 3/4	.0557	.0814	.0823	.254	.371	503.2	18.3	2112
	.0572	.0733	.0757	.277	.356	506.2	10.6	2111
2/2	.0334	.0431	.0480	.268	.346	499.8	13.8	2110
10G 8/2	.5333	.5892	.6519	.301	.332	512.8	3.3	2067*
	.3942	.4427	.5039	.294	.330	502.0	5.2	2066
	.2793	.3188	.3644	.290	.331	500.3	6.5	2065
	.1776	.2060	.2336	.288	.334	500.9	7.3	2064
	.1120	.1325	.1528	.282	.334	498.7	9.5	2063
	.0572	.0720	.0810	.272	.343	499.4	12.5	2062
2/2	.0347	.0428	.0495	.274	.337	497.7	12.3	2061*
2.5BG 8/2	.5348	.5897	.6637	.299	.330	507.4	3.6	2084
	.3880	.4598	.5338	.281	.333	498.0	10.0	2083
2	.4170	.4698	.5370	.293	.330	501.0	5.7	2082**
6/6	.2610	.3428	.4047	.259	.340	496.6	17.5	2081
	.2718	.3376	.4063	.268	.332	496.2	14.6	2080
2	.2965	.3411	.3991	.286	.329	495.5	8.2	2079
5/6	.1480	.2151	.2647	.236	.343	495.2	25.8	2078
	.1574	.2027	.2473	.259	.334	495.0	17.7	2077
2	.1781	.2083	.2442	.282	.330	497.1	9.3	2076
4/6	.0938	.1389	.1785	.228	.338	494.1	29.0	2075
	.1038	.1388	.1732	.250	.334	494.5	21.2	2074
2	.1106	.1331	.1592	.275	.330	495.8	12.2	2073
3/6	.0519	.0762	.1001	.228	.334	493.5	29.4	2072
	.0623	.0860	.1104	.241	.332	493.7	24.6	2071
2	.0602	.0757	.0936	.262	.330	494.5	16.8	2070
2/4	.0359	.0467	.0626	.248	.322	491.9	22.9	2069
	.0337	.0410	.0528	.264	.322	492.3	16.5	2068
7.5BG 8/4	.4924	.5621	.7137	.279	.318	491.5	11.5	2029A**
	.5156	.5641	.6865	.292	.319	493.0	6.5	2029
7/4	.3884	.4549	.5943	.270	.316	491.0	14.7	2028
	.4085	.4474	.5507	.290	.318	492.0	7.0	2027
6/6	.2794	.3512	.4834	.251	.315	490.8	22.1	2026
	.2877	.3406	.4559	.265	.314	490.5	16.7	2025
2	.2994	.3304	.4143	.287	.317	491.0	8.5	2024
5/6	.1525	.2089	.3197	.224	.307	489.5	32.8	2023
	.1654	.2060	.2939	.249	.310	489.5	23.5	2022
2	.1879	.2111	.2730	.280	.314	490.0	11.5	2021
4/6	.0962	.1371	.2202	.212	.302	489.3	37.5	2020
	.1124	.1412	.2148	.240	.301	488.2	27.5	2019**
2	.1180	.1337	.1826	.272	.308	488.3	15.3	2018**
3/4	.0567	.0751	.1187	.226	.300	488.5	32.2	2017**
	.0638	.0745	.1026	.265	.309	489.0	17.5	2016**
2/2	.0356	.0417	.0582	.263	.308	488.5	18.2	2015
10BG 8/2	.5332	.5794	.7117	.292	.318	492.0	6.5	2014*
	.4053	.4423	.5658	.287	.313	489.0	8.7	2013
7/2	.2888	.3192	.4169	.282	.312	488.5	11.0	2012
6/2	.1820	.2043	.2790	.274	.307	488.0	14.5	2011
4/2	.1119	.1254	.1724	.273	.306	487.8	14.5	2010**
3/2	.0647	.0746	.1042	.266	.306	488.2	17.5	2009
2.5B 8/4	.5638	.6238	.8148	.282	.312	488.6	11.0	2049**
	.5617	.6005	.7696	.291	.311	488.0	7.8	2048**
7/6	.3858	.4571	.7012	.250	.296	486.8	24.1	2047
	.4120	.4673	.6605	.268	.304	487.3	16.8	2293*
2	.4301	.4662	.6193	.284	.308	487.0	10.5	2045
6/6	.2499	.3066	.5161	.233	.286	486.0	31.5	2044
	.2792	.3201	.4900	.256	.294	485.6	22.0	2043
2	.2919	.3174	.4378	.279	.303	486.0	12.8	2042
5/6	.1567	.1984	.3686	.217	.274	485.5	38.5	2041
	.1689	.1977	.3187	.246	.289	485.6	26.0	2040
2	.1792	.1952	.2801	.274	.298	484.7	15.2	2039
4/8	.0949	.1304	.2735	.190	.261	485.3	49.5	2038
	.1051	.1349	.2547	.212	.273	485.5	40.0	2037
2	.1144	.1357	.2213	.243	.288	485.8	27.5	2036
2	.1157	.1275	.1813	.273	.300	485.8	15.2	2035
3/6	.0640	.0831	.1772	.197	.256	484.4	47.5	2034
	.0699	.0849	.1618	.221	.268	484.2	37.6	2033**
2	.0680	.0746	.1182	.261	.286	483.5	21.0	2032
2/2	.0385	.0479	.0824	.228	.284	486.1	33.6	2031*
7.5B 8/4	.5315	.5744	.8460	.272	.294	483.6	16.0	2008
	.5399	.5738	.7643	.288	.306	485.0	9.5	2007
7/6	.3784	.4245	.6917	.253	.284	484.0	24.3	2006
	.3975	.4372	.6499	.268	.294	484.6	17.8	2297*
2	.4242	.4494	.6026	.287	.304	484.5	9.5	2004
6/6	.2741	.3148	.5638	.238	.273	483.0	30.5	2003
	.2924	.3198	.5042	.262	.286	483.0	20.8	1999
2	.2985	.3164	.4366	.284	.301	483.5	11.5	1998
5/6	.1837	.2122	.4296	.223	.257	482.3	38.0	1997
	.1963	.2176	.3813	.247	.274	482.5	27.5	1996
2	.1981	.2110	.3122	.275	.292	482.2	15.5	1995
4/6	.1112	.1287	.2998	.206	.238	481.4	46.2	1994
	.1228	.1362	.2594	.237	.263	481.5	32.5	1993
2	.1258	.1348	.2158	.264	.283	482.0	21.0	1992
3/4	.0701	.0800	.1678	.220	.252	481.8	39.5	1991
	.0754	.0821	.1374	.256	.278	482.0	24.0	1990
2/2	.0357	.0390	.0692	.248	.271	481.7	27.5	2296*
10B 8/4	.5423	.5802	.8396	.276	.296	483.0	14.5	1988
	.5418	.5682	.7541	.291	.305	483.0	8.0	1987*
7/2	.4103	.4305	.5980	.285	.299	482.0	10.8	1986
	.3159	.3353	.4842	.278	.295	482.5	14.0	1985
5/2	.2121	.2229	.3292	.278	.292	481.0	14.5	1984
	.1253	.1316	.2013	.273	.287	480.5	16.5	1983
3/2	.0700	.0732	.1157	.270	.283	480.0	18.0	1982
	.0378	.0416	.0890	.224	.247	480.5	38.5	1981
2	.0338	.0361	.0676	.246	.262	480.0	29.5	1980**
2.5PB 8/4	.5730	.5980	.8849	.279	.291	480.0	14.2	1978
	.5622	.5798	.7852	.292	.301	480.0	8.2	1977
7/6	.4204	.4407	.7702	.258	.270	479.5	24.0	1976
	.4175	.4329	.6964	.270	.280	479.0	19.0	1975
2	.4294	.4429	.6043	.291	.300	480.0	9.0	1974
6/8	.3231	.3444	.7268	.232	.247	479.5	36.0	1973
	.3186	.3326	.6271	.249	.260	478.5	28.2	1972
2	.3221	.3356	.5620	.264	.275	479.2	21.5	1971
2	.3246	.3342	.4755	.286	.295	479.0	11.0	1970
5/10	.2140	.2313	.5725	.210	.227	479.2	46.2	1969
	.2135	.2272	.5349	.219	.233	479.0	42.5	1968
6	.2030	.2126	.4350	.239	.250	478.5	33.5	1967
	.2045	.2129	.3749	.258	.269	478.5	24.0	1966
2	.1972	.2032	.2989	.282	.290	478.5	13.2	1965
4/10	.1313	.1405	.4053	.194	.208	478.5	54.2	1964
	.1357	.1435	.3689	.209	.221	478.5	47.5	1963
6	.1233	.1286	.2942	.226	.236	478.2	40.0	1962
	.1257	.1305	.2511	.248	.257	478.5	29.5	1961
2	.1287	.1313	.2179	.269	.275	477.0	19.8	1960
3/8	.0755	.0806	.2284	.196	.210	478.5	53.6	1959
	.0735	.0769	.2024	.208	.218	478.0	48.2	1958
4	.0716	.0741	.1614	.233	.241	477.9	36.5	1957
	.0694	.0711	.1232	.263	.270	477.6	22.4	1956
2/4	.0404	.0419	.0994	.222	.231	477.9	41.8	1955
	.0374	.0384	.0748	.248	.255	477.8	29.5	1954
7.5PB 8/4	.5881	.5949	.8600	.288	.291	477.0	11.0	1681
	.5744	.5834	.7524	.301	.305	475.0	4.8	1680**
7/8	.4579	.4555	.8100	.266	.264	475.0	22.2	1675
	.4581	.4524	.7753	.272	.268	473.0	19.9	1674
6	.4460	.4461	.6737	.285	.285	473.0	13.1	1673**
	.4388	.4455	.5963	.296	.301	473.0	6.8	1672**
6/10	.3376	.3207	.7289	.243	.231	475.0	34.8	1671
	.3344	.3215	.6643	.253	.244	472.0	29.6	1670
8	.3202	.3110	.5834	.264	.256	472.0	24.3	1669
	.3238	.3182	.5188	.279	.274	471.0	16.4	1668
2	.3224	.3234	.4598	.292	.292	473.0	9.8	1667**
5/14	.2202	.1966	.5978	.217	.194	471.8	49.0	1666
	.2219	.1996	.5672	.224	.202	47		

TABLE I.—Continued.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.	Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.				
	X	Y	Z	x	y					X	Y	Z	x	y							
7.5PB 4/16	14	.1591	.1297	.5233	.196	.160	470.5	61.0	1659	7.5P 2/6	4	.0578	.0391	.0952	.301	.204	555.5c	43.5	1821		
	12	.1606	.1337	.5080	.200	.167	470.5	58.3	1658		4	.0512	.0373	.0800	.304	.221	554.5c	37.0	1820		
	10	.1514	.1296	.4380	.211	.180	470.5	53.2	1657		2	.0434	.0360	.0597	.312	.259	549.5c	23.8	1819		
	8	.1478	.1299	.3921	.221	.194	470.0	47.9	1656		10P	8/2	.6515	.6383	.7896	.313	.307	537.0c	5.8	2140	
	6	.1437	.1296	.3469	.232	.209	471.0	42.0	1655			7/2	.4845	.4692	.5918	.314	.304	533.0c	5.8	2139	
	4	.1365	.1266	.2948	.245	.227	470.5	35.0	1654			6/2	.3481	.3293	.4309	.314	.297	538.0c	8.4	2138	
	2	.1319	.1254	.2433	.264	.250	470.0	25.2	1653			5/2	.2256	.2092	.2751	.318	.295	527.0c	10.1	2137	
					.282	.269	468.0	14.8	1652			4/2	.1502	.1376	.1888	.315	.289	540.3c	12.0	2136	
					.283	.277	468.0	14.8	1652			3/2	.0793	.0694	.1002	.319	.279	536.7c	16.7	2135	
											2/2	.0517	.0417	.0661	.324	.261	534.5c	14.5	2134		
	3/14	10	.0998	.0732	.3631	.186	.136	468.5	68.0		1645	2.5SRP	8/4	.6539	.6075	.7833	.320	.297	517.0c	9.5	1818
		8	.0944	.0728	.3154	.196	.151	469.0	62.6		1644		2	.6035	.5851	.7267	.315	.306	520.0c	5.3	1817*
6		.0861	.0674	.2734	.202	.158	468.2	59.9	1643	7/6	7/6		.5434	.4750	.6325	.329	.288	510.0c	15.2	1816	
4		.0815	.0679	.2316	.214	.178	469.0	52.4	1642		4		.5061	.4582	.5909	.325	.295	510.0c	11.6	1815	
2		.0793	.0686	.1972	.230	.199	468.2	44.1	1641		2		.4903	.4709	.5822	.318	.305	510.0c	5.9	1814	
					.249	.226	467.5	33.8	1640		6/8		6/8	.4407	.3478	.5050	.341	.269	511.0c	24.8	1812
					.275	.265	467.5	20.0	1639				6	.4135	.3412	.4830	.334	.276	513.0c	20.8	1811
													4	.3710	.3251	.4339	.328	.288	511.4c	15.0	1809
										2			.3390	.3197	.4074	.318	.300	518.0c	8.2	1808	
										5/10			5/10	.3302	.2290	.3580	.360	.250	508.1c	36.2	1807
													8	.3107	.2293	.3415	.352	.260	508.0c	30.5	1806
											6		.2786	.2189	.3115	.344	.271	508.1c	24.7	1805	
									4		.2424	.2062	.2788	.333	.284	509.0c	17.6	1804			
									2		.2195	.2021	.2603	.322	.296	513.0c	10.2	1803			
									4/10		4/10	.2194	.1403	.2514	.359	.230	514.3c	44.1	1802		
										8	.2067	.1388	.2413	.352	.236	515.8c	40.0	1801			
										6	.1826	.1342	.2116	.346	.254	514.0c	31.7	1800			
										4	.1607	.1319	.1876	.335	.275	513.0c	21.3	1799			
										2	.1459	.1297	.1718	.326	.290	512.3c	13.7	1798			
										3/10	3/10	.1231	.0720	.1446	.362	.212	517.1c	51.9	1796		
									8		.1161	.0749	.1395	.351	.227	519.5c	43.8	1795			
									6		.1072	.0758	.1252	.348	.246	515.5c	35.6	1794			
									4		.0888	.0688	.1044	.339	.262	516.0c	27.0	1793			
									2		.0769	.0681	.0913	.326	.288	515.0c	14.0	1792			
									2/8		2/8	.0722	.0452	.0914	.346	.216	527.0c	46.8	1791		
										6	.0688	.0447	.0902	.338	.219	532.2c	44.2	1790			
										4	.0591	.0411	.0747	.334	.236	531.2c	36.5	1789			
										2	.0461	.0378	.0592	.322	.264	536.1c	23.2	1788			
										7.5SRP	8/4	.6678	.6214	.7301	.331	.303	496.0c	7.5	1787**		
											2	.5806	.5663	.6502	.323	.315	492.0c	3.3	1786*		
									7/6		7/6	.5444	.4765	.5584	.345	.302	496.0c	12.4	1785		
											4	.5175	.4778	.5612	.332	.307	496.0c	8.0	1784		
											2	.4656	.4491	.5181	.325	.313	493.5c	4.0	1783		
											6/10	6/10	.4357	.3326	.3807	.380	.289	495.8c	24.0	1782	
										8		.4213	.3361	.3841	.369	.294	495.7c	19.5	1781		
										6		.3763	.3186	.3706	.353	.299	494.9c	15.0	1780		
									4	.3586		.3214	.3706	.341	.306	495.0c	10.0	1779			
									2	.3245		.3091	.3604	.326	.311	495.0c	5.1	1778			
									5/10	5/10		.3320	.2327	.2715	.397	.278	496.3c	31.8	1777		
										8	.2884	.2100	.2439	.389	.283	496.1c	28.2	1776			
										6	.2626	.2052	.2430	.369	.289	496.6c	22.3	1775			
										4	.2435	.2059	.2411	.353	.298	496.2c	15.4	1774			
										2	.2238	.2062	.2419	.333	.307	496.0c	8.0	1773			
										4/10	4/10	.2181	.1398	.1730	.411	.263	497.3c	40.2	1772		
									8		.2092	.1438	.1756	.396	.272	497.2c	34.0	1771			
									6		.1866	.1393	.1666	.379	.283	496.9c	26.5	1770			
									4		.1701	.1395	.1626	.360	.295	496.0c	18.0	1769			
									2		.1506	.1347	.1589	.339	.303	496.8c	10.9	1768			
									3/10		3/10	.1358	.0801	.1107	.416	.245	499.2c	48.4	1767		
										8	.1188	.0760	.0994	.404	.258	498.5c	40.8	1766			
										6	.1099	.0773	.0982	.385	.271	498.4c	32.4	1765**			
										4	.0928	.0735	.0902	.362	.287	498.0c	21.6	1764			
										2	.0897	.0788	.0940	.342	.300	497.0c	12.6	1763			
										2/6	2/6	.0644	.0415	.0632	.381	.246	503.5c	41.8	1762		
									4		.0595	.0417	.0602	.369	.258	503.5c	34.3	1761			
									2		.0483	.0386	.0519	.348	.278	503.8c	22.6	1760			
									10RP		8/2	.6151	.6024	.6690	.326	.319	599.0	5.0	1918*		
											7/2	.4777	.4574	.5039	.332	.318	608.0	6.3	1917**		
											6/2	.3306	.3109	.3507	.333	.313	700.0	5.5	1916		
										5/2	.2426	.2229	.2453	.341	.314	642.0	7.8	1915			
										4/2	.1578	.1394	.1537	.350	.309	493.0c	10.4	1914			
										3/2	.0802	.0692	.0776	.353	.305	493.5c	12.8	1913			
									2/2	.0530	.0430	.0542	.353	.286	499.7c	20.1	1912				

TABLE II. Trichromatic specification, dominant wavelength, and excitation purity for neutral grays; half-steps of Munsell value, and a special series of small value steps.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wavelength	Excitation purity	Munsell production no.
	X	Y	Z	x	y			
Neutrals								
N 8.5/	.6205	.6365	.7266	.313	.321	570	2.0	2228*
7.5/	.4860	.4993	.5716	.312	.321	567	1.7	2227*
6.5/	.3634	.3732	.4379	.309	.318	515	0.4	2211*
5.5/	.2419	.2483	.2889	.310	.319	558	0.8	2210*
4.5/	.1579	.1614	.1905	.310	.317	550	0.2	2224*
3.5/	.0948	.0964	.1135	.311	.316	700	0.2	2223*
2.5/	.0524	.0531	.0609	.315	.319	700	2.0	2222*
1.5/	.0245	.0250	.0295	.310	.316	—	0.0	2221*
Special "60-step" value scale								
	.8696	.8953	1.0158	.313	.322	568	2.2	60
	.8843	.9058	1.0418	.312	.320	568	1.5	58
	.8177	.8399	.9367	.315	.324	572	3.5	57
	.7804	.7996	.9154	.313	.320	570	1.8	56*
	.7451	.7641	.8658	.313	.322	572	2.3	55
	.7059	.7239	.8280	.313	.321	570	2.0	54
	.6735	.6895	.7973	.312	.319	570	1.2	53
	.6686	.6851	.7890	.312	.320	568	1.5	52
	.6422	.6580	.7619	.311	.319	565	1.2	51
	.6196	.6345	.7394	.311	.318	570	0.8	50
	.5912	.6048	.7064	.311	.318	570	3.5	49
	.5853	.5985	.6981	.311	.318	570	0.8	48
	.5637	.5767	.6916	.309	.316	490	0.5	47
	.5216	.5340	.6260	.310	.318	555	0.4	45
	.5255	.5384	.6260	.311	.319	565	1.2	44
	.5216	.5340	.6213	.311	.318	570	0.8	43
	.4849	.4959	.5835	.310	.317	550	0.2	42
	.4706	.4816	.5658	.310	.317	550	0.2	41
	.4461	.4566	.5398	.309	.316	490	0.5	40
	.4255	.4344	.5197	.309	.315	470	0.6	39
	.4049	.4134	.4855	.311	.317	580	0.2	37 old 37 new
	.4049	.4159	.4819	.311	.319	565	1.2	37
	.3794	.3882	.4548	.310	.318	555	0.4	36
	.3373	.3452	.4075	.309	.317	500	0.2	34
	.3186	.3258	.3851	.310	.316	—	0.0	33
	.3049	.3107	.3697	.310	.315	400	0.3	32
	.2892	.2956	.3485	.310	.317	550	0.2	31
	.2794	.2859	.3319	.311	.319	565	1.2	30
	.2627	.2682	.3107	.312	.319	570	1.2	28
	.2480	.2529	.2941	.312	.318	580	1.0	27
	.2274	.2326	.2693	.312	.319	570	1.2	26
	.1941	.1978	.2270	.314	.320	578	2.0	24
	.1782	.1820	.2081	.314	.320	578	2.0	23
	.1710	.1744	.2001	.314	.320	578	2.0	22
	.1610	.1642	.1908	.312	.318	580	1.0	21
	.1553	.1584	.1831	.313	.319	578	1.4	20
	.1345	.1372	.1585	.313	.319	578	1.4	18
	.1332	.1358	.1571	.313	.319	578	1.4	17
	.1186	.1208	.1412	.312	.317	590	0.8	16
	.1106	.1126	.1310	.312	.318	580	1.0	15
	.0967	.0984	.1162	.311	.316	700	0.2	14
	.0939	.0956	.1117	.312	.317	590	0.8	13
	.0861	.0878	.1025	.312	.318	580	1.0	12
	.0755	.0768	.0905	.311	.316	700	0.2	11
	.0726	.0738	.0864	.312	.317	590	0.8	10
	.0667	.0678	.0791	.312	.317	590	0.8	8A
	.0596	.0608	.0716	.310	.317	550	0.2	8
	.0520	.0528	.0616	.312	.317	590	0.8	6
	.0457	.0464	.0536	.314	.318	585	1.5	5
	.0394	.0400	.0472	.311	.316	700	0.2	4
	.0277	.0280	.0328	.313	.316	650	0.8	61
	.0237	.0240	.0283	.312	.316	680	0.5	63
	.0255	.0260	.0305	.311	.317	580	0.2	62
	.0184	.0188	.0224	.309	.316	490	0.5	64
	.0173	.0174	.0212	.309	.311	560	1.7	65

* More than one lot of this color has been made (March, 1943).

puted colorimetric values for the curves.² About 1000 colors were involved.

Spectral apparent reflectance curves were made on the General Electric Recording Spectrophotometer. The standard of reflectance was the surface of a freshly prepared layer, 0.06 inch thick, of magnesium oxide. All samples were

² Mimeographed tables for portions of these data have been available since 1938-39.

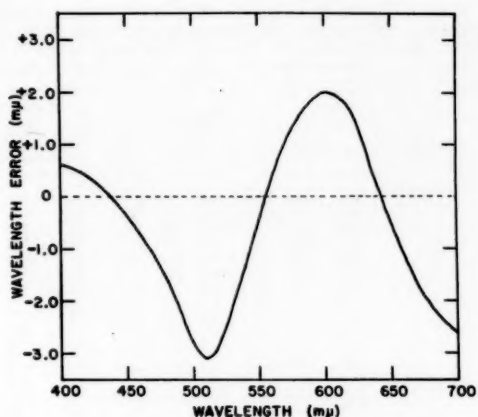


FIG. 1. Wave-length calibration of the spectrophotometer.

backed by a non-selective diffusing surface having an apparent reflectance of 0.005.

The wave-length calibration of the spectrophotometer is shown by the curve in Fig. 1. This curve was obtained by drawing a smooth line through the mean of points representing the wave-length error as determined by observation of a mercury discharge tube, and measurements on two filters calibrated by the National Bureau of Standards and the Color Measurements Laboratory at the Massachusetts Institute of Technology. It is believed that this calibration was maintained within $\pm 0.5 \text{ m}\mu$ in the wave-length region used for the colorimetric computations.

The General Electric Recording Spectrophotometer as originally manufactured allows the sample and standard to be irradiated normally and viewed diffusely, except that approximately one-half of the specular component is lost by being reflected through the entrance apertures. During the course of this work, the viewing geometry was changed to permit total inclusion or exclusion of the specular component. This change allowed the sample and standard to be irradiated at 5° from the normal, and viewed diffusely, with provision to include or exclude the specular component.

Therefore, some of the reflectance curves were made with the original viewing geometry, while the remainder were run with the new viewing geometry,³ specular component included. Experi-

³ This is the type of viewing geometry adopted several years ago by the Color Measurements Laboratory at the Massachusetts Institute of Technology.

TABLE III. Trichromatic specification, dominant wave-length, and excitation purity for several series of special Munsell samples: 100 hues at 5/5; 50 hues at maximum chroma; a series of "Pinks;" of "Browns;" odd chromas at value levels of maximum chroma for 10 hues; high value series (9/) for 5 hues; weak chromas (/1), values 2/ to 8/ for 5 hues; a series specially produced in strong chromas; and glossy surface papers for matching tomato colors.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.	Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.
	X	Y	Z	x	y					X	Y	Z	x	y			
100 hues at 5/5¹																	
5R	2794	2308 ¹	1966	.395	.325	603.8	25.6	101	6	.3014	2668	4067	.309	.274	552.0c	17.1	182
6	2840	2335	1874	.403	.331	600.7	28.8	102	7	2909	2517	3867	.313	.271	547.7c	18.9	183
7	2697	2228	1758	.404	.333	599.5	29.7	103	8	2949	2546	3836	.316	.273	543.2c	18.7	184
8	2654	2209	1657	.407	.339	597.0	32.0	104	9	2898	2489	3654	.321	.275	535.0c	19.4	185
9	2648	2209	1564	.412	.344	595.0	34.9	105	10	2918	2485	3616	.323	.275	529.2c	19.0	186
10	2652	2241	1505	.414	.350	592.9	37.2	106	1RP	2927	2465	3484	.330	.278	517.3c	19.2	187
1YR	2512	2142	1353	.419	.357	591.1	39.8	107	2	3000	2529	3454	.334	.282	509.8c	18.5	188
3	2513	2167	1313	.419	.362	589.7	41.5	108	3	3088	2589	3411	.340	.285	504.9c	18.2	189
4	2473	2144	1202	.425	.368	588.6	44.8	109	4	2965	2454	3041	.350	.290	499.0c	18.1	190
5	2412	2121	1102	.428	.376	587.0	47.9	110	5SRP	2841	2341	2943	.350	.288	499.7c	18.6	191
6	2452	2213	1126	.423	.382	585.2	48.1	111	6	2992	2454	2996	.354	.291	498.1c	18.6	192
7	2382	2156	1042	.427	.386	584.7	50.2	112	7	3027	2467	2953	.358	.292	496.9c	18.9	193
8	2391	2184	0994	.429	.392	584.0	52.4	113	8	3042	2472	2876	.363	.295	496.0c	18.5	194
9	2370	2205	0918	.431	.401	582.6	55.4	114	9	3018	2455	2760	.367	.298	494.8c	17.8	195
10	2459	2333	0944	.429	.407	581.4	56.1	115	10	2876	2350	2479	.373	.305	493.0c	16.3	196
1Y	2424	2343	0910	.427	.413	580.2	57.2	116	1R	2971	2428	2489	.377	.308	492.5c	16.0	197
2	2539	2508	0908	.426	.421	579.1	59.4	117	3	2851	2330	2115	.391	.319	610.8	22.4	199
3	2492	2488	0878	.425	.425	578.5	60.0	118	4	2870	2345	2050	.395	.323	607.5	24.3	200
4	2430	2462	0862	.422	.428	577.7	60.0	119	50 hues at maximum chroma								
5	2523	2605	0882	.420	.433	576.7	60.8	120	1R	3044	2030	1834	.441	.294	493.0c	33.8	999
6	2500	2639	0943	.411	.434	575.6	58.7	121	3	3148	2115	1618	.458	.307	629.0	37.2	998
7	2536	2690	1019	.406	.431	575.2	56.3	122	5	3107	2095	1263	.481	.324	610.0	47.8	1008
8	2598	2791	1090	.403	.431	574.5	55.1	123	5	3648	2491	1112	.503	.344	602.2	59.2	893
9	2518	2766	1175	.394	.427	573.9	52.1	124	7	4092	2928	1036	.508	.363	596.6	65.8	892
10	2539	2841	1295	.380	.425	571.8	48.2	126	1YR	4328	3234	0882	.512	.383	592.8	72.0	891
1GY	2496	2867	1328	.373	.428	570.0	47.1	127	3	4325	3339	0581	.525	.405	589.8	81.2	890
2	2350	2730	1337	.366	.425	569.0	44.3	128	5	4278	3483	0621	.510	.416	587.4	80.1	870
3	2403	2831	1422	.361	.425	567.8	43.0	129	7	4099	3553	0619	.496	.430	584.5	80.0	884
4	2378	2829	1533	.353	.420	566.4	39.3	130	9	4282	3913	0609	.486	.445	582.0	81.8	883
5	2288	2742	1644	.344	.411	564.6	34.1	131	1Y	4671	4488	0634	.471	.458	579.8	82.8	946
6	2347	2850	1709	.340	.413	563.4	34.0	132	3	5107	5177	0710	.465	.471	572.6	82.9	945A
7	2335	2870	1807	.333	.409	561.4	31.3	133	5	4951	5274	0822	.448	.477	575.5	80.2	1128*
8	2313	2891	1892	.326	.407	558.9	28.8	134	7	4450	4907	0780	.439	.484	574.0	79.8	1130
9	2323	2909	2008	.321	.402	556.8	26.1	135	9	4296	4890	0826	.429	.488	572.7	78.1	1131*
10	2364	2986	2152	.315	.398	554.2	23.4	136	1GY	3909	4559	0850	.420	.489	571.5	76.0	1132*
1G	2305	2944	2234	.308	.393	549.7	20.4	137	3	3586	4293	0914	.408	.488	570.1	72.2	952
2	2190	2849	2218	.302	.393	545.0	18.8	138	5	3321	4218	0957	.391	.496	567.3	70.1	1105
3	2301	2994	2462	.297	.386	539.1	15.9	139	7	2792	3599	1072	.374	.482	565.6	62.0	960
4	2123	2804	2398	.290	.383	530.5	13.7	140	9	2342	3224	1194	.347	.477	560.8	53.0	961
5	2019	2646	2434	.283	.373	520.0	11.0	141	1G	1889	2808	1324	.314	.466	552.3	41.8	1103
6	2033	2682	2539	.280	.370	514.4	11.0	142	3	1480	2224	1435	.285	.439	538.2	27.5	1102
7	2087	2746	2711	.277	.364	509.6	11.2	143	5	1202	2059	1706	.257	.406	513.2	18.9	1101
8	2076	2739	2810	.272	.359	505.5	12.3	144	7	1271	1944	1934	.247	.378	503.0	20.9	1100
9	2050	2716	2889	.268	.355	502.3	13.9	145	9	1231	1869	2015	.241	.365	499.7	23.0	1099
10	2102	2778	3074	.264	.349	499.8	15.2	146	1BG	1320	1971	2269	.237	.354	497.4	24.8	1098
1BG	2030	2689	3096	.260	.344	497.8	17.2	147	3	1339	1982	2520	.229	.339	492.4	28.3	1097
2	2009	2660	3184	.256	.339	495.9	18.8	148	5	1263	1865	2577	.221	.327	492.4	32.1	1096
3	2080	2720	3380	.254	.333	494.4	19.5	149	7	1172	1694	2551	.216	.313	490.5	35.0	1095
4	2142	2789	3614	.251	.326	493.0	21.4	150	9	1065	1513	2422	.213	.303	489.3	37.3	1094
5	1994	2557	3384	.251	.322	492.2	21.5	151	1B	1008	1396	2458	.207	.287	487.6	40.4	1093
6	2117	2719	3642	.250	.321	491.9	22.1	152	3	0998	1329	2681	.199	.265	485.3	45.7	1092
7	2076	2643	3730	.246	.313	490.3	24.2	153	5	0957	1198	2806	.193	.241	482.8	50.9	1087
8	2027	2569	3700	.244	.310	489.8	25.0	154	7	0868	1067	2705	.187	.230	482.0	54.0	1086
9	2106	2617	3836	.246	.306	489.0	24.6	155	9	0777	0931	2519	.184	.220	481.2	56.5	1063
10	2200	2720	4090	.244	.302	488.2	25.7	156	1PB	0770	0876	2553	.183	.209	480.0	58.1	1061
1B	2211	2688	4201	.243	.295	487.1	26.6	157	3	0816	0871	2756	.184	.196	478.3	59.5	1060*
2	2135	2555	4224	.240	.287	485.8	29.0	158	5	0869	0836	2981	.185	.178	475.7	61.5	1059
3	2160	2554	4295	.240	.282	485.2	29.2	159	7	1080	0888	3404	.201	.165	470.1	58.5	1133*
4	2116	2486	4254	.239	.281	484.7	29.9	160	9	1241	0924	3416	.222	.165	460.0	52.7	1134*
5	2054	2355	3992	.245	.280	484.1	27.7	161	1P	1483	1035	3535	.245	.171	420.0	47.0	1135
6	2200	2502	4364	.243	.276	483.3	28.9	162	3	1758	1200	3553	.270	.184	563.4c	45.8	1136
7	2237	2510	4423	.244	.274	482.8	28.7	163	5	2021	1310	3776	.284	.184	559.6c	48.2	1007
8	2255	2513	4459	.244	.272	482.4	28.6	164	7	2140	1412	3587	.300	.198	555.5c	46.0	1006
9	2342	2563	4532	.248	.272	481.7	27.3	165	9	2265	1487	3378	.318	.209	547.2c	44.8	1005
10	2369	2550	4541	.250	.270	480.8	26.8	166	1RP	2444	1658	3195	.335	.227	532.7c	40.6	1004
1PB	2417	2568	4615	.252	.267	480.1	26.4	167	3	2721	1886	3008	.357	.248	510.0c	36.5	1003
2	2453	2567	4619	.254	.266	479.1	25.8	168	5	28							

TABLE III.—Continued.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wavelength	Excitation purity	Munsell production no.	Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wavelength	Excitation purity	Munsell production no.
	X	Y	Z	x	y					X	Y	Z	x	y			
"Pinks"									Odd chromas								
3RP 7/8	.5305	4729	.6170	.327	.292	509.5c	13.2	1052	R 4/13	.2187	.1283	.0631	.533	.313	619.5	58.8	895
6	.5195	4705	.5962	.328	.297	505.0c	11.0	1028	11	.2057	.1256	.0722	.510	.311	621.0	52.1	1614*
4	.5062	4740	.5827	.324	.303	503.0c	8.0	1020	9	.1944	.1235	.0791	.490	.311	622.0	46.6	38
7RP 8/6	.6597	6186	.7165	.331	.310	496.0c	6.3	1045	7	.1734	.1195	.0885	.455	.313	619.5	38.0	1613*
4	.6083	.5891	.6605	.327	.317	496.0c	4.8	1037	5	.1608	.1222	.1071	.412	.313	621.0	26.5	1612*
7/8	.5284	4691	.5471	.342	.304	496.0c	11.0	1053	3	.1457	.1225	.1216	.374	.314	621.0	16.8	1610*
6	.5190	4671	.5526	.337	.304	497.0c	10.2	1029	1	.1377	.1318	.1463	.331	.317	610.0	6.0	1611*
4	.4947	4590	.5357	.332	.308	496.0c	7.5	1021	YR 6/11	.3928	3253	.0719	.497	412	587.0	75.9	898
9RP 8/6	.6651	6220	.7049	.334	.312	493.5c	6.2	1046	9	.3703	.3155	.1047	.468	.309	586.6	64.8	897*
4	.6105	.5883	.6500	.330	.318	606.0	6.0	1038	7	.3629	.3159	.1492	.438	.382	587.0	52.0	380
7/8	.5158	4482	4947	.354	.307	493.5c	12.0	1054	5	.3415	.3096	.2039	.399	.362	586.9	36.2	378
6	.4922	4445	5080	.344	.306	494.5c	10.5	1030	3	.3084	.2909	.2454	.365	.344	587.0	22.3	376
4	.4827	4430	5080	.337	.309	494.0c	8.0	1022	1	.2998	.2974	.3132	.329	.327	580.0	8.0	374
1R 8/6	.6246	.5851	.6476	.336	.315	630.0	6.5	1047	Y 8/11	.5378	.5690	.0878	.450	.476	575.8	80.3	906
4	.6179	.5923	.6432	.333	.320	600.0	7.0	1039	9	.5341	.5642	.1197	.438	.463	575.8	74.0	905
7/8	.5142	4415	4764	.359	.308	493.5c	12.8	1055	7	.5214	.5492	.2182	.405	.426	575.5	54.8	860
6	.4922	4378	4749	.350	.312	650.0	9.5	1031	5	.5288	.5528	.3390	.372	.389	575.4	36.1	874
4	.4820	4371	4764	.345	.313	645.0	8.6	1023	3	.5246	.5432	.4364	.349	.361	574.8	22.3	873
3R 8/6	.6327	5880	6375	.340	.316	620.0	8.0	1048	1	.5211	.5389	.5425	.325	.336	574.0	9.8	872
4	.5974	.5656	.6009	.339	.321	600.0	9.0	1040	GY 7/9	.3485	4421	1.303	.378	.480	566.5	62.5	901*
7/8	.5005	4256	4385	.367	.312	636.0	14.0	1056	7	.3635	4444	1.809	.368	.449	567.0	51.3	900
6	.4982	4384	4450	.360	.317	615.0	13.5	1032	5	.3705	4363	2.462	.352	.414	566.8	37.6	926
4	.4775	4274	4481	.353	.316	620.0	11.5	1024	3	.3734	4150	3.396	.331	.368	566.0	19.2	925
5R 8/6	.6295	5817	6018	.347	.321	604.0	11.0	1074	1	.3982	4188	4.330	.319	.335	568.0	7.5	924
7R 8/6	.6192	.5681	.5885	.355	.325	599.0	14.3	1049	G 5/7	.1166	.1850	.1559	.255	.404	512.0	19.1	922
4	.6041	.5662	.5725	.347	.325	597.0	12.0	1041	5	.1275	.1839	.1655	.267	.386	512.0	14.8	175
7/8	.4927	4117	3463	.394	.329	601.5	26.0	1057	3	.1523	.1895	.1899	.286	.356	513.0	8.4	173
6	.5004	4352	3961	.376	.327	601.5	20.2	1033	1	.1722	.1874	.2111	.302	.328	510.0	3.0	171
4	.4834	4257	4060	.368	.324	603.0	17.5	1025	BG 4/7	.0887	.1320	.1852	.218	.325	492.2	33.0	927
9R 8/6	.6367	5880	5518	.358	.331	593.0	16.5	1050	5	.0989	.1342	.1820	.238	.323	492.2	26.0	479
4	.6064	.5676	.5514	.352	.329	593.0	14.5	1042	3	.1140	.1384	.1779	.265	.322	492.4	16.3	481
7/8	.4795	4018	2870	.410	.344	595.0	34.2	1058	1	.1234	.1378	.1682	.287	.321	493.2	8.0	923*
6	.5038	4392	3683	.384	.335	596.0	24.8	1034	B 4/7	.1054	1.297	2.913	.200	.246	482.9	47.4	930*
4	.4898	4372	3963	.370	.330	596.5	20.0	1026	5	.1105	1.313	2.589	.221	.262	483.4	38.2	929*
"Browns"									3	.1255	1.434	2.346	.249	.285	484.3	15.5	932*
7R 4/6	.1774	1.306	.0803	.457	.336	602.7	44.3	988A	1	.1252	1.334	1.789	.286	.305	484.8	10.0	928*
4	.1592	1.294	1.051	.404	.329	602.8	28.5	979	PB 3/11	.0842	.0805	.2841	.188	.179	475.5	60.3	535
3/6	.1118	.0810	.0574	.447	.324	609.6	38.5	974	9	.0825	.0804	2.483	.201	.196	475.7	53.8	533
4	.1008	.0775	.0613	.421	.323	608.2	31.7	972	7	.0784	.0762	2.085	.216	.210	475.2	47.0	531
9R 4/6	.1745	1.320	.0745	.458	.346	598.4	47.8	987A	5	.0710	.0697	1.613	.235	.231	475.0	37.5	529
4	.1540	1.264	.0908	.415	.341	597.0	34.3	980	3	.0724	.0725	1.386	.255	.256	475.8	26.8	527
3/6	.1098	.0816	.0521	.451	.335	602.5	42.8	975	1	.0699	.0706	1.025	.288	.290	475.0	11.2	525
4	.0971	.0761	.0561	.423	.332	602.4	34.3	970	P 4/11	.1835	1.222	3.540	.278	.185	561.5c	46.5	252
1YR 4/6	.1762	1.364	.0659	.465	.360	594.8	53.7	989A	9	.1773	1.295	3.114	.287	.210	560.6c	38.2	943*
4	.1569	1.312	.0818	.424	.355	592.5	41.0	981	7	.1590	1.241	2.658	.290	.226	560.9c	32.2	944*
3/6	.0989	.0773	.0421	.453	.354	595.3	49.0	995*	5	.1501	1.257	2.379	.292	.245	561.5c	25.3	245
4	.0915	.0736	.0500	.425	.342	597.0	38.0	971	3	.1370	1.235	1.988	.298	.269	561.5c	17.0	243
3YR 4/6	.1712	1.394	.0639	.457	.372	591.0	54.6	990	1	.1285	1.255	1.676	.305	.298	563.0c	6.3	241
4	.1597	1.376	.0790	.424	.366	589.2	44.0	982	RP 4/11	.2267	1.440	2.134	.388	.246	502.2c	42.5	937A*
3/6	.1066	.0866	.0418	.454	.368	591.5	52.4	996*	9	.2108	1.437	2.073	.375	.256	502.6c	36.5	939A
4	.0897	.0746	.0453	.428	.356	592.5	42.0	990A*	7	.1920	1.396	1.938	.365	.266	503.3c	30.6	938A
7YR 4/6	.1664	1.455	.0583	.450	.393	586.0	58.0	991A	5	.1744	1.372	1.849	.351	.276	503.8c	22.8	940A
4	.1587	1.411	.0693	.430	.382	585.9	50.0	983	3	.1615	1.407	1.795	.335	.292	503.0c	14.2	941A
3/4	.0872	.0775	.0441	.418	.371	587.0	43.6	991*	1	.1491	1.421	1.756	.319	.304	507.0c	6.3	942A
9YR 4/6	.1598	1.451	.0528	.447	.406	583.5	60.3	992A	High value series (9) for 5 hues ²								
4	.1568	1.416	.0673	.429	.387	584.8	51.0	984	5R 9/3	.7294	7.110	.8012	.325	.317	609.5	4.3	2237
3/4	.0863	.0796	.0441	.411	.379	584.3	44.0	992*	2	.7274	7.203	8.239	.320	.317	608.0*	2.9	2236
1Y 4/4	.1394	1.331	.0596	.420	.401	581.2	52.0	985	1	.7183	7.184	8.277	.317	.317	604.0	2.2	2235
3/4	.0848	.0782	.0449	.408	.376	584.5	42.2	993*	0.5	.7084	7.187	8.163	.316	.320	582.0	2.6	2234
3Y 4/4	.1295	1.285	.0592	.408	.405	579.0	50.0	986	5Y 9/3	.6642	6.920	5.742	.344	.358	574.5	20.4	2290
3/4	.0780	.0771	.0473	.385	.381	579.8	37.5	994*	2	.6717	6.910	6.650	.331	.341	575.6	12.2	1699
5Y 3/4	.0744	.0767	.0451	.379	.391	576.5	38.5	973	1	.6910	7.108	7.398	.323	.332	574.5	7.6	2239
									0.5	.6994	7.191	7.751	.319	.328	573.3	5.4	2238
									5G 9/3	.6370	7.164	7.793	.299	.336	513.8	4.1	2244
									2	.6634	7.231	8.043	.303	.330	516.0	2.8	2243
									1	.6918	7.334	8.224	.308	.326	537.0	2.2	2242
									0.5	.6871	7.147	8.135	.310	.323	550.0	1.7	2241

TABLE III.—Continued.

Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.	Munsell notation	Tristimulus values			Trilinear coordinates		Dominant wave-length	Excitation purity	Munsell production no.										
	X	Y	Z	x	y					X	Y	Z	x	y													
Weak chromas																											
5R	/1), values 2/ to 8/, for 5 hues																										
8/1	.5607	.5516	.6246	.323	.318	602.0	3.7	2260	A series specially produced in strong chromas ^b																		
7/1	.4382	.4330	.4902	.322	.318	602.0	3.6	2259	4 R	3.4/10.4	.1479	.0846	.0491	.525	.300	635.0	53.5	2325									
6/1	.3134	.3082	.3504	.322	.317	609.0	3.6	2258	4.5R	4.0/13.1	.2223	.1203	.0552	.559	.302	628.2	62.8	2299									
5/1	.2008	.1927	.2103	.333	.319	604.0	6.8	2257	8.5R	4.8/14.7	.3020	.1759	.0370	.587	.342	606.0	80.8	2300									
4/1	.1283	.1219	.1319	.336	.319	606.0	7.7	2256	8.5R	5.0/14.5	.3307	.1980	.0458	.576	.345	604.8	78.6	2301									
3/1	.0758	.0705	.0755	.342	.318	610.0	8.9	2255	10 R	5.7/14.6	.4002	.2623	.0458	.565	.370	598.0	82.7	2302									
2/1	.0414	.0376	.0408	.346	.314	635.0	9.0	2254	5 YR	6.6/13.9	.4726	.3718	.0474	.530	.417	588.3	86.2	2303									
									0.5Y	7.7/13.0	.5750	.5335	.0698	.488	.453	581.3	84.3	2304									
									4.5Y	8.4/13.3	.6468	.6708	.0745	.464	.482	576.7	86.0	2305									
5Y	8/1	.5440	.5622	.5651	.326	.336	574.0	9.5	2267	9.5Y	8.8/12.2	.6547	.7476	.1150	.432	.493	572.6	80.0	2320								
	7/1	.4253	.4390	.4339	.328	.338	574.6	10.5	2266	0.5GY	9.2/10.8	.7193	.8326	.1835	.414	.480	571.6	71.8	2306								
	6/1	.3034	.3133	.3013	.330	.341	574.7	12.2	2265	3 GY	7.5/11.2	.4052	.5079	.0771	.409	.513	568.7	79.5	2307								
	5/1	.2011	.2076	.1966	.332	.343	575.0	13.0	2264	8 GY	7.1/10.4	.3090	.4515	.1451	.341	.498	558.8	57.5	2308								
	4/1	.1312	.1352	.1282	.333	.343	575.4	13.2	2263	4.5G	5.5/11.5	.1280	.2491	.1804	.230	.447	512.0	28.0	2309								
	3/1	.0709	.0735	.0647	.339	.351	575.0	17.2	2262	6 G	2.7/5.6	.0324	.0531	.0469	.245	.401	507.6	21.5	2321								
	2/1	.0386	.0400	.0381	.330	.343	574.0	12.7	2261	4.5BG	3.3/8.4	.0410	.0778	.1209	.171	.324	491.7	51.1	2310								
5G	8/1	.5155	.5499	.6109	.308	.328	537.0	2.7	2274	1.5B	3.1/7.3	.0453	.0695	.1624	.164	.251	485.4	60.2	2311								
	7/1	.4015	.4302	.4890	.304	.326	512.0	2.1	2273	8.5B	3.0/6.8	.0567	.0672	.1941	.178	.211	480.7	59.3	2322								
	6/1	.2845	.3092	.3503	.301	.328	508.0	2.9	2272	3 PB	3.1/10.7	.0706	.0689	.3149	.155	.152	476.4	75.2	2312								
	5/1	.1805	.1962	.2247	.300	.326	503.6	3.3	2271	7 PB	3.5/19.4	.1339	.0777	.5833	.168	.098	466.2	80.1	2313								
	4/1	.1212	.1333	.1500	.300	.330	507.7	3.5	2270	1 P	2.2/12.9	.0692	.0364	.2058	.222	.117	400.0	64.0	2323								
	3/1	.0604	.0686	.0731	.299	.340	518.0	4.5	2269	2 P	2.6/14.3	.0985	.0496	.2670	.237	.120	565.2c	65.7	2314								
	2/1	.0353	.0401	.0444	.295	.335	507.0	5.0	2268	5 P	3.2/14.6	.1430	.0749	.3102	.271	.142	560.8c	62.9	2315								
									2 RP	3.3/15.3	.1706	.0784	.2107	.371	.171	522.5c	70.0	2316									
									4.5RP	2.8/9.3	.0996	.0557	.1004	.390	.218	507.0c	54.6	2324									
5B	8/1	.5385	.5659	.7118	.296	.312	487.0	5.4	2282	8 RP	3.4/12.1	.1649	.0866	.1013	.467	.245	496.4c	58.0	2317								
	7/1	.4241	.4451	.5618	.296	.311	486.0	5.5	2281	1 R	3.7/11.8	.1881	.1002	.0821	.508	.270	473.8c	55.4	2318								
	6/1	.2965	.3137	.4088	.291	.308	485.5	7.8	2280	Glossy surface papers for matching tomato colors ^a																	
	5/1	.1923	.2052	.2756	.286	.305	485.1	10.1	2279	R ⁵	.1427	.0961	.0599	.478	.322	612.0	46.3	2208*									
	4/1	.1218	.1308	.1815	.281	.301	484.5	12.2	2278	R ⁶	.1192	.0704	.0292	.545	.322	613.2	64.4	2208*									
	3/1	.0638	.0692	.0983	.276	.299	484.7	14.2	2276	YR ⁵	.3350	.2549	.0826	.498	.379	592.6	67.2	2207*									
	2/1	.0377	.0404	.0580	.277	.297	483.0	14.2	2275	YR ⁶	.3231	.2422	.0690	.509	.382	592.8	71.0	2207*									
5P	8/1	.5503	.5505	.6922	.307	.307	564.4c	3.2	2289	N 1/5	.0431	.0439	.0530	.308	.314	473.0	1.2	2209*									
	7/1	.4466	.4423	.5657	.307	.304	561.9c	4.3	2288	N 1/6	.0128	.0130	.0161	.305	.311	477.0	2.3	2209*									
	6/1	.3286	.3207	.4286	.305	.298	562.8c	6.6	2287																		
	5/1	.2160	.2100	.2787	.306	.298	560.0c	6.8	2286																		
	4/1	.1435	.1366	.1872	.307	.292	557.0c	9.0	2285																		
	3/1	.0795	.0742	.1083	.303	.283	560.0c	12.2	2284																		
	2/1	.0419	.0373	.0597	.302	.269	559.0c	17.7	2283																		

^a All but seven of the following 26 papers are made from different pigments; seven are mixtures in order to fill up wide hue gaps. This series is particularly useful in disk colorimetry.

^b These papers have semi-gloss surfaces as evidenced by the difference in the Y tristimulus values for the two conditions of viewing, and as a result, the corresponding values of P_s for the R and YR papers differ considerably. If these papers were very glossy, a difference in the Y

values as great as 0.04 would be obtained for the two conditions of viewing, with a correspondingly greater difference in P_s . Thus, viewing and illuminating geometry become increasingly critical as surfaces depart from non-specularity, and if the geometry is not known, measurements on glossy chromatic samples are subject to misinterpretation.

^c Specular component included in spectrophotometric measurement.
* Specular component excluded in spectrophotometric measurement.

ments have indicated that the viewing geometries of the spectrophotometer as originally manufactured, as well as the new geometry with specular component both included and excluded, give similar values of reflectance for samples of matt surfaces. Since the usual Munsell color chips have nearly matt surfaces, the two methods of viewing geometry are believed to give values of apparent reflectance that differ by less than 0.002. A few "special" papers possessed glossy surfaces, and are so noted in the tables. They were measured with the specular component both included and excluded.⁴

Some of the samples also exhibit a slight iridescence which often has been termed as "bronze." As bronze increases, viewing and illuminating geometry become increasingly critical.

Tristimulus values and trilinear coordinates have been determined for I.C.I. Illuminant C,

⁴ See Table III, reference 4.

using the 30 selected ordinate method. The graph paper on which the spectrophotometric curve was recorded had the selected ordinates printed thereon. Dominant wave-length and purity were read from large-scale sections of the I.C.I. mixture diagram in the *Handbook of Colorimetry* (8). Trilinear coordinates are reported to three decimal places, instead of the usual four, in order to call attention to the fact that the fourth place is accurate only when corrections for all instrumental and recording errors are applied.

The spectrophotometric measurements were made in the Interchemical Corporation Research Laboratories, and a complete set of calculations were compiled in the laboratories of the Food Distribution Administration. Each of the authors has had a part in checking the data.

This work was started in order to supply hue sensibility data for surface colors (9), also in

connection with the work of the Newhall subcommittee (OSA Colorimetry Committee) on Review of Spacing of the Munsell Colors (10), (11). It was completed in order to make full information available to all color workers who may have use for any of the Munsell papers. The data for the 20 new hues, and the $\frac{1}{2}$ chromas originally omitted in the 10 intermediates of the regular 20 hue series, are placed in order by hue in Table I. Data for half-value step and special neutrals are assembled in Table II. Data for other special series are placed together by title in Table III.

The authors are indebted to the Munsell Color Company for supplying samples and production numbers, and to their respective laboratories for permission to carry on and publish this work.

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Final Report of the O.S.A. Subcommittee on the Spacing of the Munsell Colors*

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This report presents the characteristics of a modified and enlarged Munsell solid which has been evolved from the 1940 visual estimates of the *Munsell Book of Color* samples. All three dimensions have been carefully reviewed and extensively revised. The newly defined loci of constant hue have been extended closer to the extremes of value while the loci of constant chroma have been extrapolated to the pigment maximum. The dimension of value has been redefined without substantial departure from the Munsell-Sloan-Godlove scale. By the above changes a solid is achieved which approaches more closely to A. H. Munsell's dual ideal of psychological equispacing and precise applicability. The new solid is defined in terms of the I.C.I. standard coordinate system and Illuminant C.

TABLE OF CONTENTS

	Page		Page
Introduction	385	Hue adjustments	414
Recommendations	386	Value adjustments	416
Conversion Charts, Munsell hue and chroma vs. I.C.I. chromaticity	387	Summary	417
Conversion Table, Munsell hue and chroma vs. I.C.I. chromaticity	897		
Conversion Table, Munsell value vs. I.C.I. luminous reflectance	406		
Conversion Table, Munsell samples in terms of the recommended Munsell notation	408		
Revision Procedures	407		
Chroma adjustments	407		

INTRODUCTION

THE original purpose of the subcommittee¹ was to reduce the psychological irregu-

* Paper presented at the meeting of the Optical Society of America, New York, New York, March 5-6, 1943.

¹ This subcommittee was appointed by L. A. Jones in 1937 as a Subcommittee of the Colorimetry Committee of the Optical Society of America. It includes H. P. Gage, D. B. Judd, Dorothy Nickerson, W. B. VanArsdel, and

larities in the spacing of the samples of the *Munsell Book of Color*. To this end, constant-value and constant-hue charts of the form found in the standard library edition of the *Book of Color* (25)² were systematically examined by 40 observers using the ratio method (27) and totaling some 3,000,000 color judgments. The data were summarized in the form of averaged visual estimates of the correct notations of the hue, value, and chroma of each sample. These estimates were then published in Table II of the preliminary report of 1940 (28).

The present report is concerned with the remaining aim of the subcommittee which was to produce a psychophysical system of surface colors which should be based upon the above data and which should correspond as closely to the ideal psychological color solid as is consonant with practical usefulness. The general method for achieving this aim was: (a) To eliminate minor variations in the averaged visual estimates by drawing through plotted points representing them, smooth curves defining new loci of constant hue and constant chroma; (b) to extrapolate the chroma loci beyond the Munsell samples and out to the theoretical pigment maximum (22); (c) to extrapolate the hue loci as far as feasible, that is, to the 1/ and 9/ value levels; (d) to adjust the value dimension by applying a new formula which eliminates irregularities in the Munsell-Sloan-Godlove function (24); (e) to express in terms of the I.C.I. notation (15) (Illuminant C) enough surface colors corresponding to this recommended psychophysical system to define it adequately; and finally, (f) for the sake of comparison, to redesignate all current samples with the revised Munsell notation.

RECOMMENDATIONS

The charts and tables in this report constitute the definition and standards of the new system. These tables and charts are recommended for general use in determining the Munsell *renotation* of a given color sample when the I.C.I. (Y and x, y) specification is known, or for determining the I.C.I. specification when the

S. M. Newhall, chairman, Dr. Gage and Mr. VanArsdel have been unable to participate in the work of reducing the data to this form, but both have indicated approval of the report.

² Italic numbers in parentheses refer to literature cited.

Munsell notation is given. If the chromaticity of the given color is specified in terms of dominant wave-length and purity, the I.C.I. trichromatic coordinates (x, y) must be found first, and then with reflectance given (Y), the Munsell value, hue, and chroma may be obtained.

Figures 1-9 present 40 hue loci corresponding to the full complement of samples in the latest edition of the *Book of Color* (25) together with the locus for every even chroma. Standard I.C.I. Illuminant C, which approximates 6700°K, has been taken as neutral origin for both the hue and chroma loci. The aim has been to make, as nearly as feasible, both series of loci perceptually equispaced. Of course, the spacing of the hue loci is not even approximately the same as that of the chroma loci, nor for that matter of the value loci. While some data on the subject are available (29), (4), no attempt was made in this study to equate the dimensional scales. It was felt that the greatly altered notation would detract seriously from the utility of the proposed system.

The charts presented are located at the recommended value levels indicated on the figures and presently to be described. It should be noted that Figs. 1-9 do not extend at all points to the theoretical pigment limit. It seemed more useful to include here only the more frequently used portions of color space, and thus obtain the advantage of a correspondingly larger scale. Table I was read from large unpublished charts which extend to the pigment limits at all points and from which the fourth place could be estimated.³ The Y entries in this table must be multiplied by 100 to obtain Y percentages, as in Table II.

Table II presents the I.C.I. luminous reflectance Y equivalents (percent form) of the recommended Munsell value scale. For convenience in computation the value-step intervals are given to 0.01. It should be noted that the reflectances indicated are not absolute but relative to magnesium oxide; whereas the maximum at value 10/ was formerly 100 percent, it is now 102.57. Use of this relation facilitates results and also avoids the somewhat dubious conversion to absolute scale, by permitting Y determinations with a MgO standard to be converted directly to

³ This table can be used for plotting complete charts.

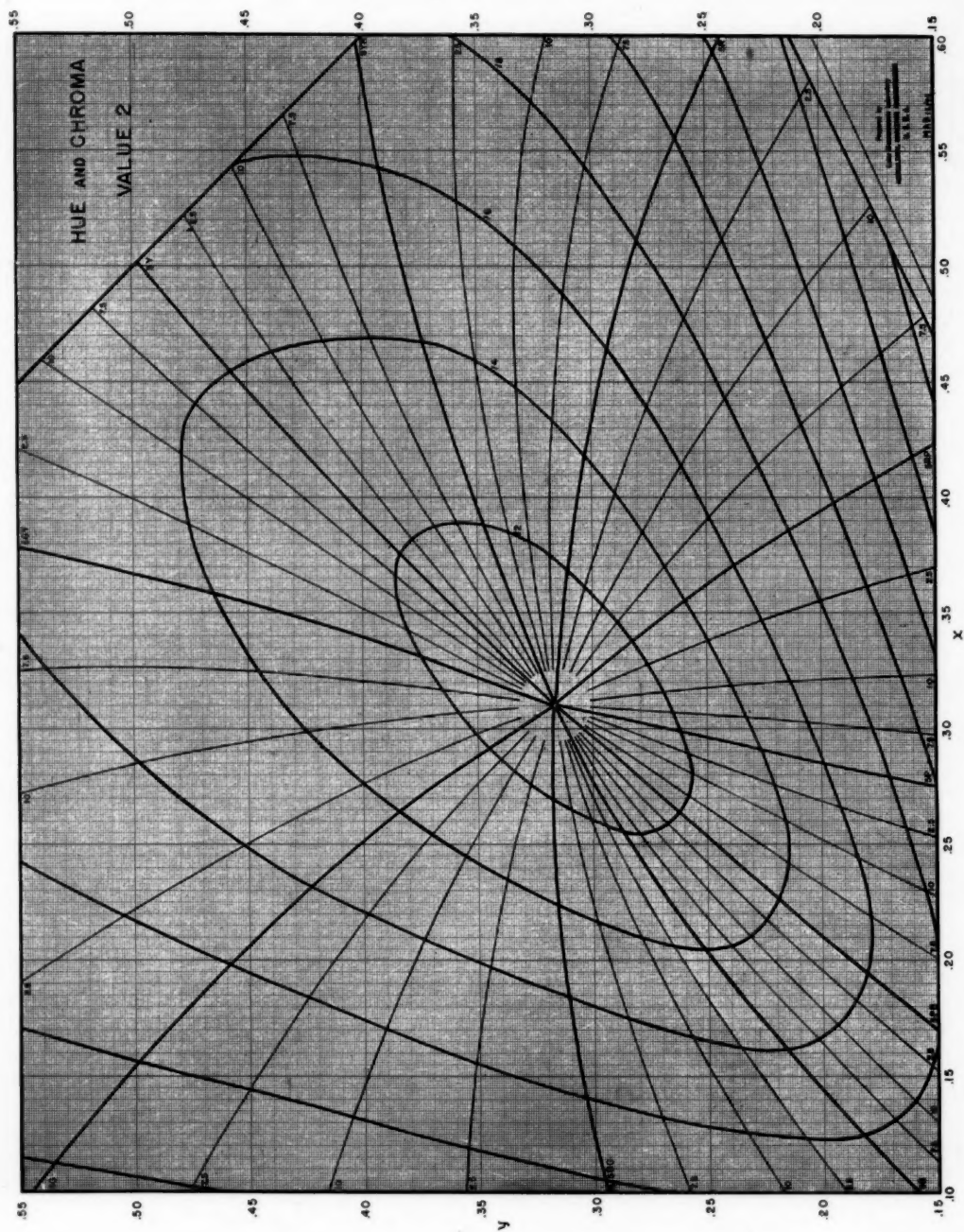


FIG. 2. Loci of constant hue and constant chroma in I.C.I. (x, y)-coordinates, at value 2/.

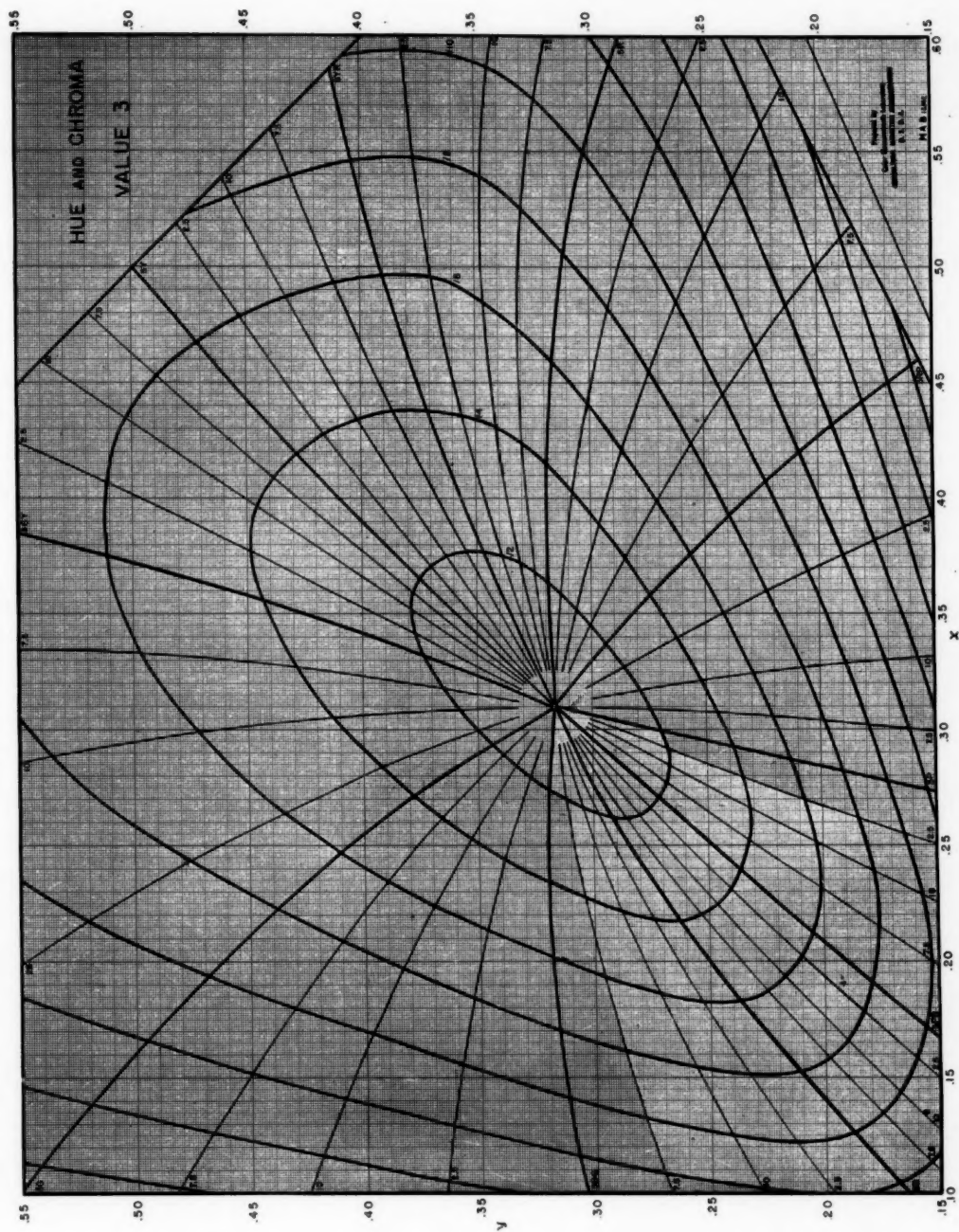


FIG. 3. Loci of constant hue and constant chroma in I.C.I. (x, y)-coordinates, at value $3/$.

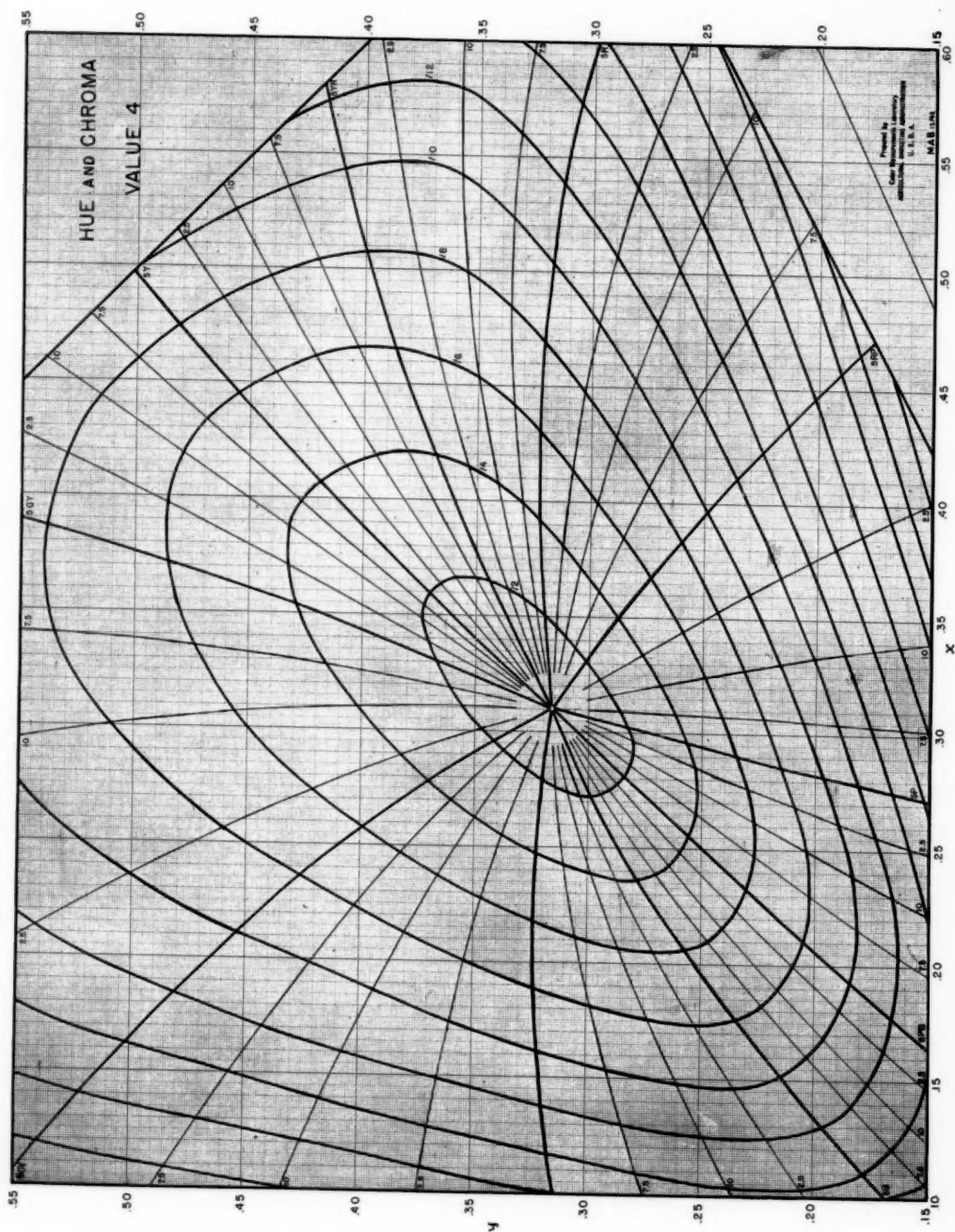


FIG. 4. Loci of constant hue and constant chroma in I.C.I. (x, y) -coordinates, at value 4/.

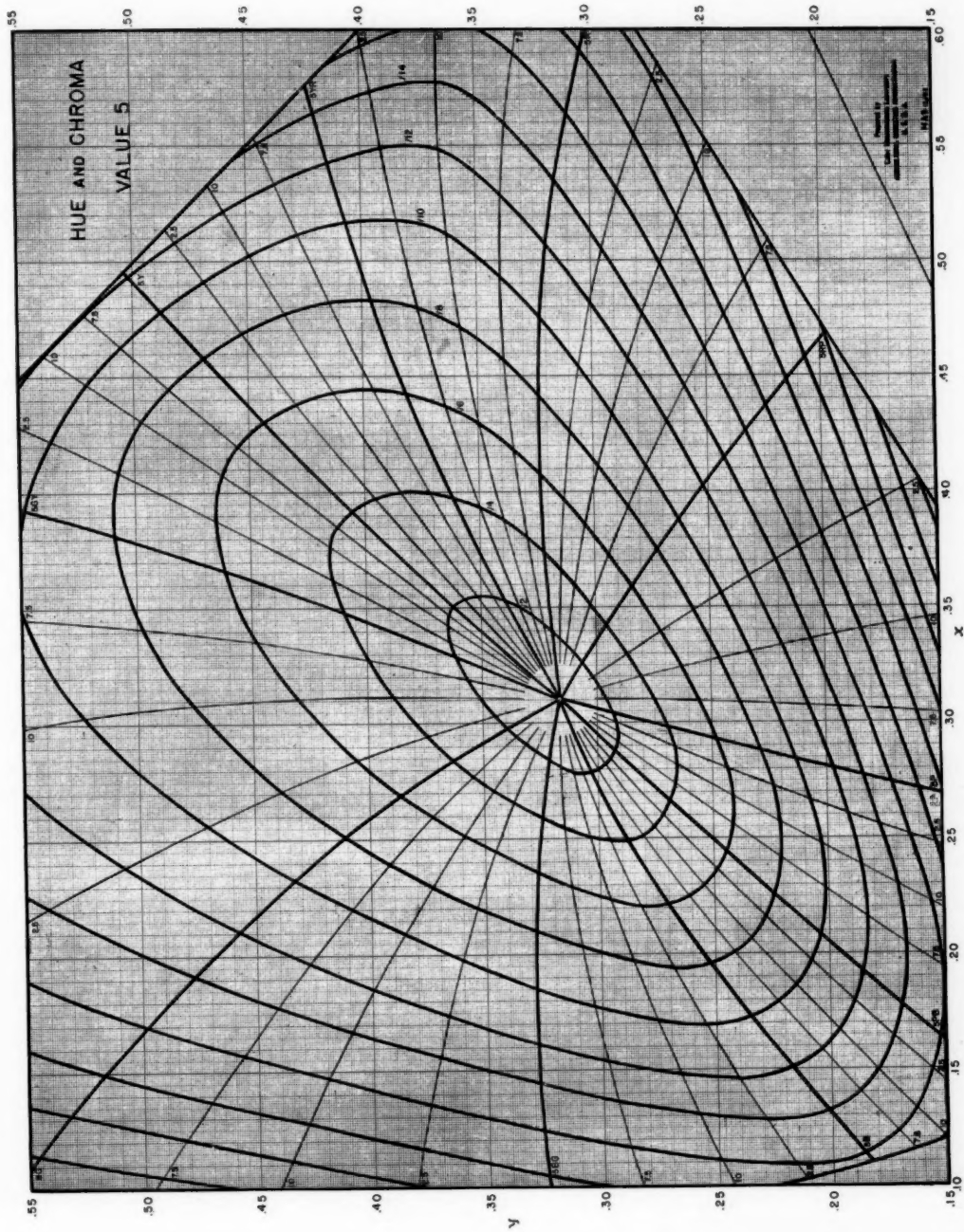


FIG. 5. Loci of constant hue and constant chroma in I.C.I. (x, y)-coordinates, at value 5/.

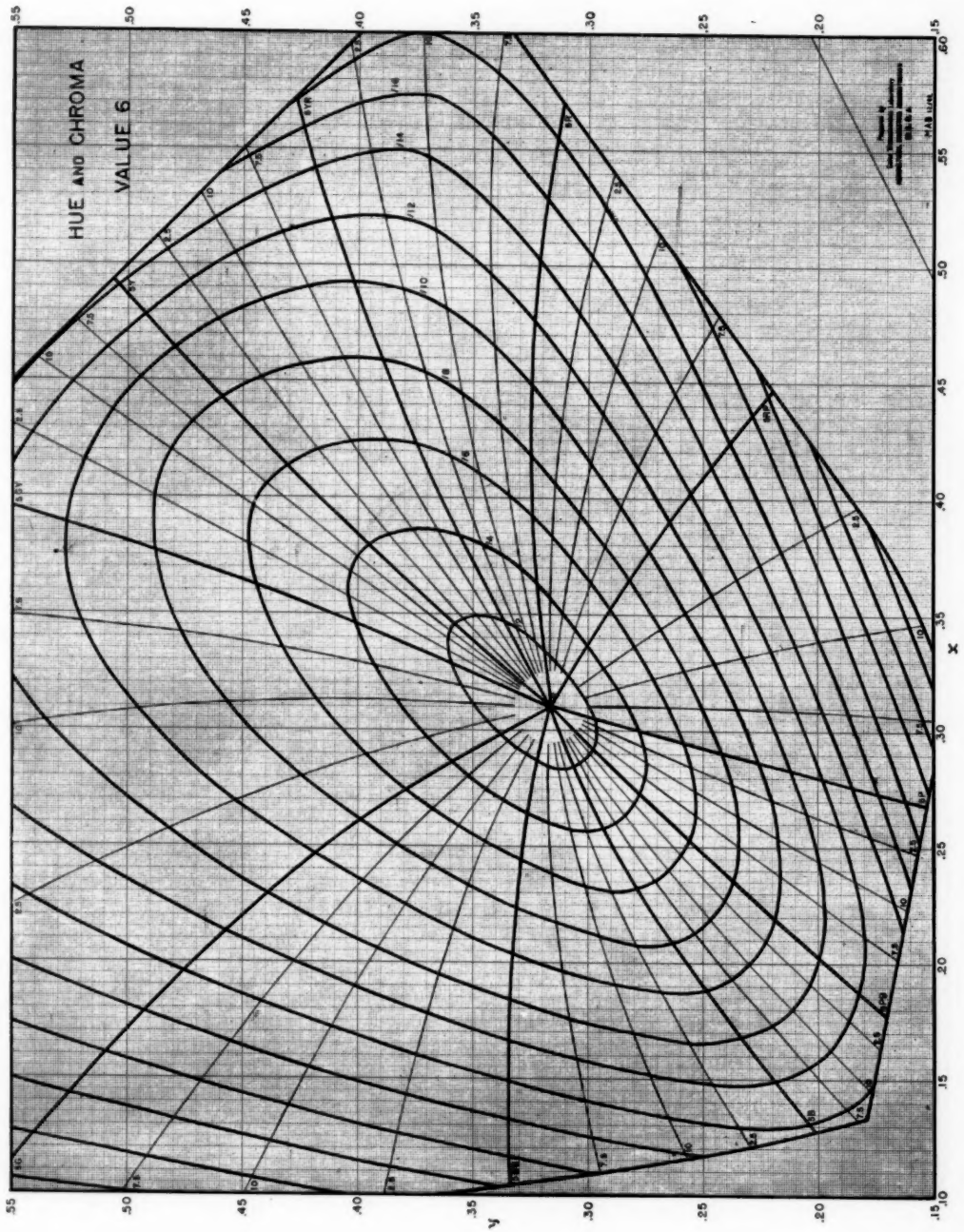


FIG. 6. Loci of constant hue and constant chroma in I.C.I. (x, y) -coordinates, at value 6/.

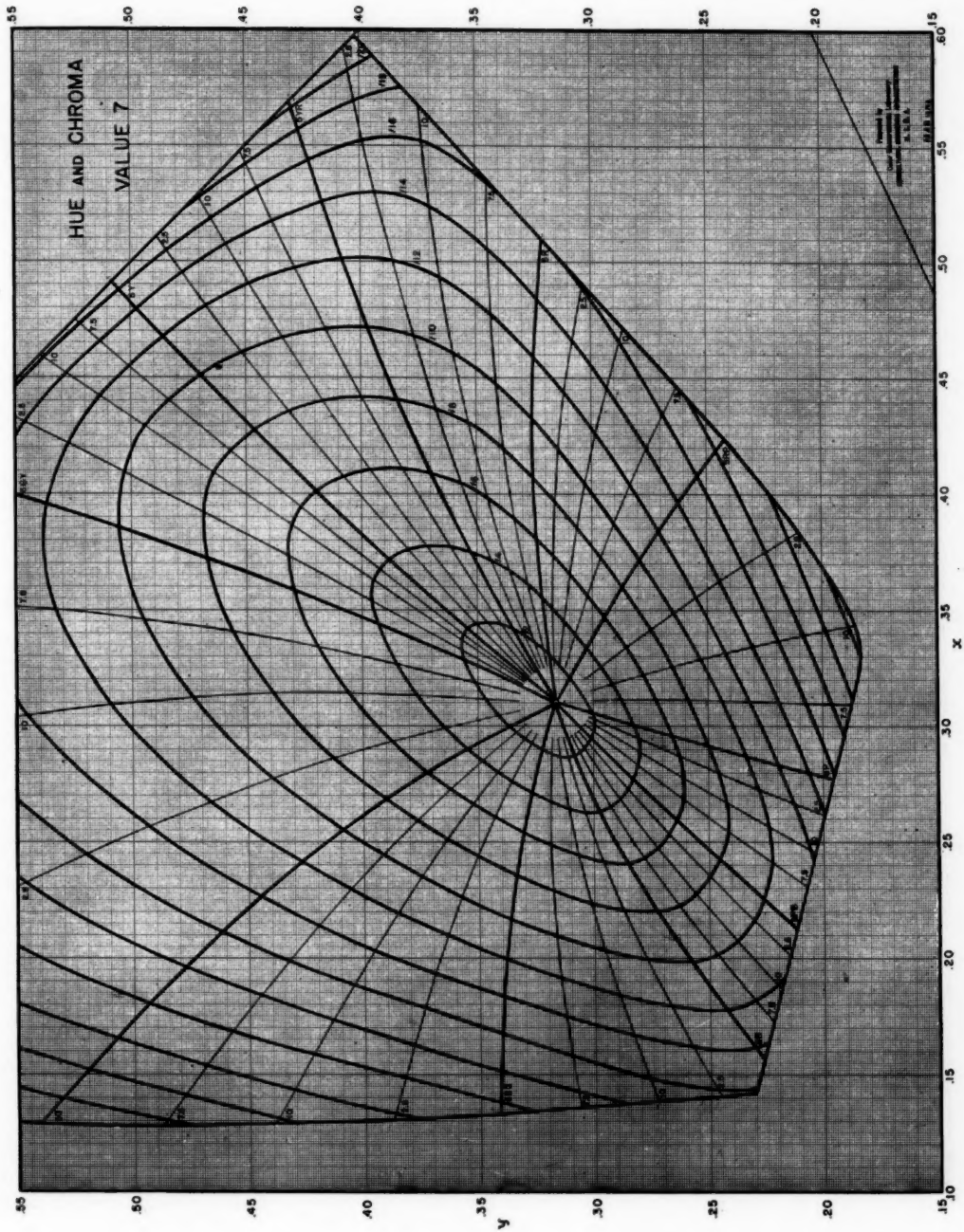


FIG. 7. Loci of constant hue and constant chroma in I.C.I. (x, y)-coordinates, at value 7/.

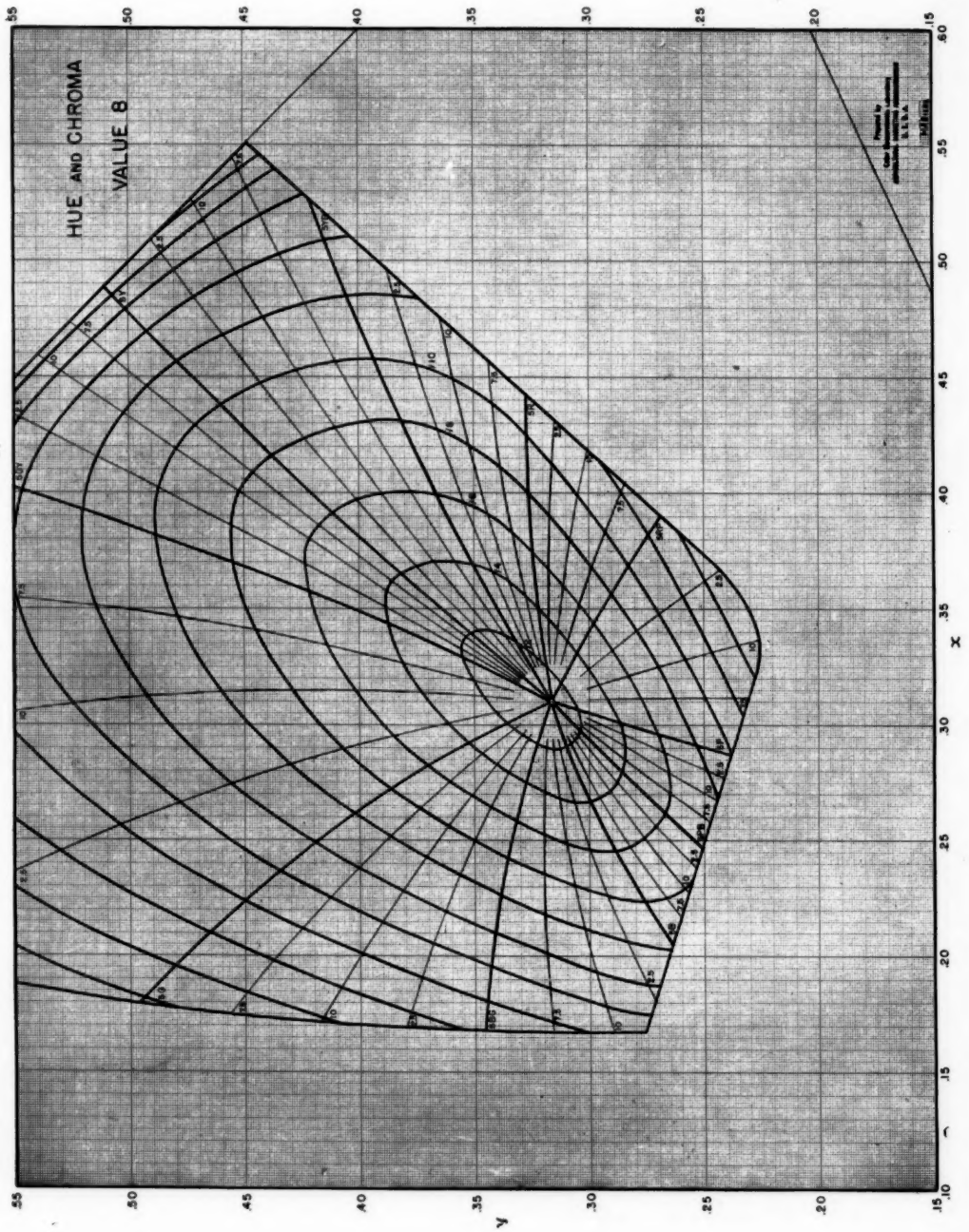


FIG. 8. Loci of constant hue and constant chroma in I.C.I. (x, y) -coordinates, at value $8/$.

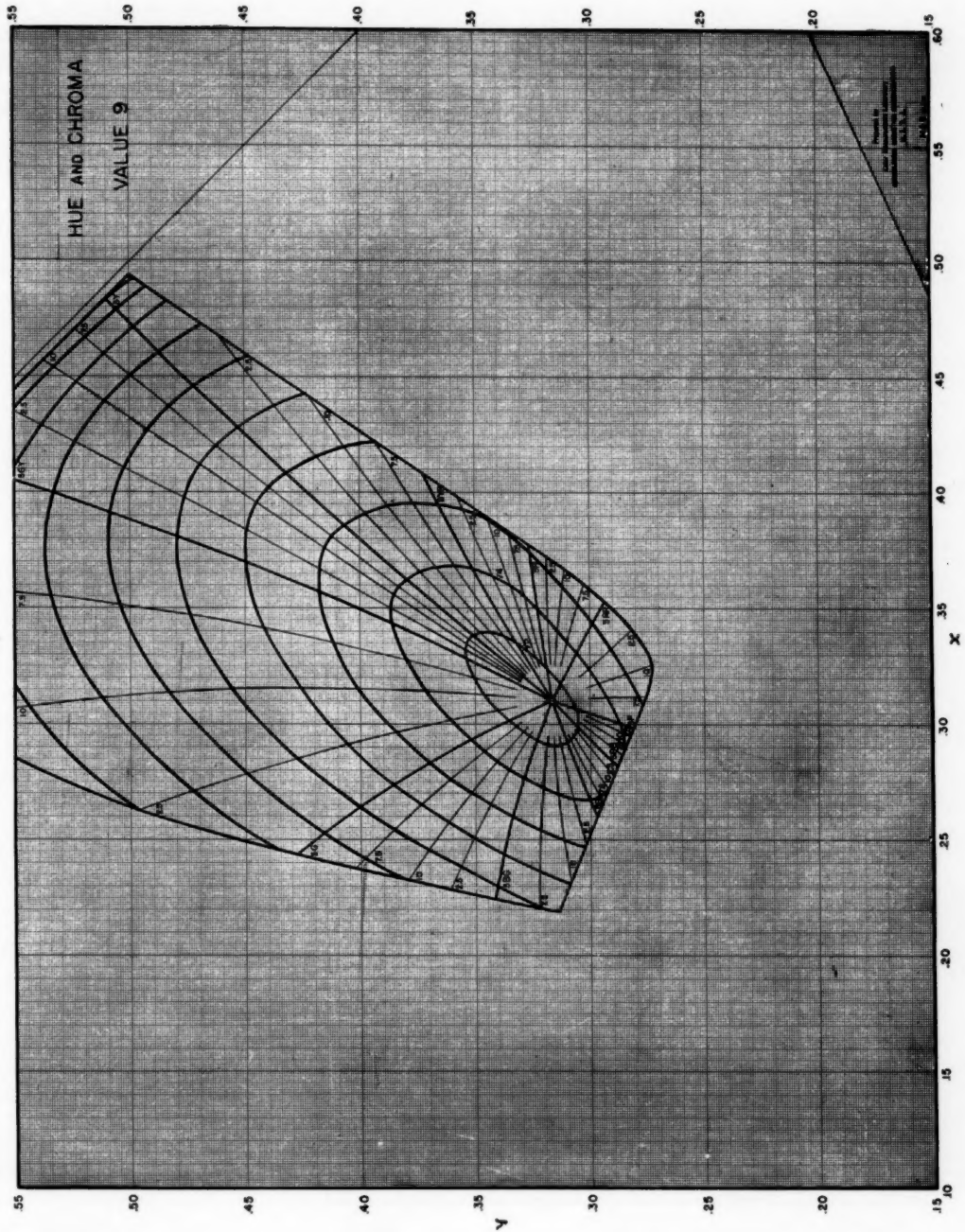


FIG. 9. Loci of constant hue and constant chroma in I.C.I. (x, y)-coordinates, at value 9/.

Munsell value. The reflectances corresponding to the principal value steps are seen to be somewhat different from the Munsell-Sloan-Godlove data (24).

Table I, or Figs. 1-9, together with Table II provide the means of complete specification of the given surface color sample. When the sample falls, as it usually does, between adjacent value levels and off the intersection of hue and chroma loci, interpolation is required. First the particular value (or luminous reflectance) is read from Table II. Then hue and chroma (or x, y) are spotted on both the adjacent value-level charts. Finally the hue and chroma (or x, y) for the sample are found by linear interpolation. For instance, to obtain Munsell equivalents for $Y=0.4602$, $x=0.500$, $y=0.454$:

- (1) From Table II it is found that for $Y=46.02$ percent, Munsell value (V) = 7.20/.
- (2) Since $V=7.20/$, Munsell hue and chroma will be found by interpolation between the charts for values 8/ and 7/. On Fig. 8, for $x=0.500$, $y=0.454$, the Munsell hue is just redder than 10.0YR. Since the difference is less than ± 0.25 hue step, it usually will be read as 10.0YR. The chroma lies between /14 and /16 at /14.6. On Fig. 7, for $x=0.500$, $y=0.454$, the hue falls at 10.0YR, the chroma between /12 and /14, at /13.1.
- (3) Since 7.20 is 0.2 of the distance between 7.00 and 8.00, the interpolated hue will be that of value 7/ plus 0.2 of the difference between the hues read from Figs. 8 and 7. Since the hue on Fig. 8 is 10.0YR, and on Fig. 7 is 10.0YR, the interpolated hue will be $10.0YR + [0.2(10.0YR - 10.0YR)] = 10.0YR$. Obviously, in this case, the interpolation formula was unnecessary, for hue could be read by inspection. The interpolated chroma will be the chroma at 7/ plus 0.2 of the difference between the chromas as read from Figs. 8 and 7. Since the chroma on Fig. 8 is /14.6, and on Fig. 7 is /13.1, the interpolated chroma will be $13.1 + [0.2(14.6 - 13.1)] = 13.4$.
- (4) The complete notation for the sample is 10.0YR 7.2/13.4.

The Munsell hues at the higher values are generally so little different on adjacent value

levels that they can be read by inspection. Chroma, however, varies considerably at all value levels, and interpolation usually will be required. The hues at the lower values—particularly in the red and red-purple region—will vary considerably between adjacent value levels. An example for this region is given below.

To obtain Munsell equivalents for $Y=0.0428$, $x=0.550$, $y=0.280$:

- (1) From Table II it is found that for $Y=4.28$ percent, Munsell value (V) = 2.40/.
- (2) Since $V=2.40/$, hue and chroma are found by interpolation between charts for values 3/ and 2/. On Fig. 3, for $x=0.550$, $y=0.280$, the hue is between 2.5R and 5.0R at 3.25R. The chroma lies between /10 and /12 at /11.2. On Fig. 2, for $x=0.550$, $y=0.280$, the hue falls between 5.0R and 7.5R at 6.0R, the chroma between /8 and /10 at /9.0.
- (3) Since 2.40 is 0.4 of the distance from 2.00 toward 3.00, the interpolated Munsell hue will be that of value 2/ plus 0.4 of the difference resulting when the hue read from Fig. 2 is subtracted from the hue read from Fig. 3. Since the hue on Fig. 3 is 3.25R and that on Fig. 2 is 6.0R, the interpolated hue will be $6.0R + 0.4(3.25R - 6.0R) = 4.9R$. Usually it is sufficient to report hue to the nearest 0.5 hue step. Thus, this figure would be rounded to 5.0R. The interpolated chroma will be the chroma at 2/ plus 0.4 of the difference between the chromas read from Figs. 3 and 2. Since the chroma on Fig. 3 is /11.2 and on Fig. 2 is /9.0, the interpolated chroma will be

$$9.0 + [0.4(11.2 - 9.0)] = 9.9.$$

- (4) The complete Munsell notation for the sample is 5.0R 2.4/9.9.

The protractor adapted for linear measurement which is illustrated in Fig. 10 is convenient for reading between the hue and chroma loci on Figs. 1-9.

The following example is included to illustrate the reverse conversion, that is, from Munsell notation to I.C.I.

To obtain I.C.I. (Y, x, y) equivalents for Munsell hue (H) = 5.0R, value (V) = 2.4, and chroma (C) = /9.9:

TABLE I. The I.C.I. (Y, x, y) equivalents of the recommended Munsell notation for 40 hues and 9 values (V), at every second chroma (C) step from zero to the theoretical pigment maximum.

V/C			Y			Reds						Yellow-Reds									
						2.5R		5.0R		7.5R		10.0R		2.5VR		5.0VR		7.5VR		10.0VR	
x	y	Y	x	y	Y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y
9/6	4	0.7866	0.3665	0.3183	0.3256	0.3734	0.3256	0.3812	0.3348	0.3880	0.3439	0.3880	0.3439	0.3927	0.3450	0.3948	0.3659	0.4220	0.3930	0.4199	0.4069
4			0.3445	0.3179	0.3226	0.3495	0.3226	0.3551	0.3283	0.3600	0.3348	0.3600	0.3348	0.3641	0.3422	0.3668	0.3509	0.3679	0.3585	0.3941	0.3877
2			0.3210	0.3168	0.3188	0.3240	0.3188	0.3263	0.3210	0.3284	0.3233	0.3284	0.3233	0.3320	0.3273	0.3353	0.3325	0.3480	0.3377	0.3392	0.3430
8/10	0.5910		0.4125	0.3160	0.3270	0.4249	0.3270	0.4388	0.3419	0.4490	0.3589	0.4490	0.3589	0.4852	0.3847	0.5088	0.4145	0.5191	0.4518	0.5245	0.4709
8			0.3900	0.3171	0.3263	0.4001	0.3263	0.4118	0.3385	0.4212	0.3526	0.4212	0.3526	0.4552	0.3761	0.4849	0.4050	0.5025	0.4338	0.4940	0.4530
6			0.3671	0.3175	0.3248	0.3743	0.3248	0.3830	0.3353	0.3910	0.3442	0.3910	0.3442	0.4275	0.3662	0.4576	0.3938	0.4816	0.4100	0.4527	0.4268
4			0.3420	0.3177	0.3224	0.3520	0.3224	0.3610	0.3319	0.3621	0.3412	0.3621	0.3412	0.3960	0.3487	0.3988	0.3663	0.4000	0.3770	0.3994	0.3896
2			0.3236	0.3169	0.3186	0.3254	0.3186	0.3277	0.3211	0.3301	0.3237	0.3301	0.3237	0.3697	0.3259	0.3719	0.3330	0.3895	0.3516	0.3407	0.3634
7/16	0.4306		0.4885	0.3039	0.3288	0.4848	0.3288	0.5341	0.3452	0.5519	0.3729	0.5519	0.3729	0.5824	0.4046	0.5657	0.4298	0.5417	0.4492	0.5276	0.4700
14			0.4660	0.3082	0.3238	0.4648	0.3238	0.5059	0.3450	0.5234	0.3700	0.5234	0.3700	0.5522	0.3989	0.5437	0.4228	0.5119	0.4449	0.5188	0.4650
12			0.4435	0.3119	0.3252	0.4477	0.3252	0.4777	0.3435	0.4930	0.3659	0.4930	0.3659	0.5297	0.3938	0.5252	0.4168	0.5174	0.4381	0.5074	0.4581
10			0.4210	0.3156	0.3266	0.4252	0.3266	0.4552	0.3416	0.4700	0.3628	0.4700	0.3628	0.5007	0.3861	0.5007	0.4081	0.4970	0.4282	0.4900	0.4480
8			0.3985	0.3193	0.3280	0.4027	0.3280	0.4327	0.3397	0.4471	0.3600	0.4471	0.3600	0.4834	0.3804	0.4834	0.4116	0.4716	0.4428	0.4540	0.4163
6			0.3760	0.3170	0.3294	0.3805	0.3294	0.3888	0.3336	0.3984	0.3452	0.3984	0.3452	0.4347	0.3715	0.4347	0.4021	0.4115	0.3996	0.4309	0.4163
4			0.3535	0.3171	0.3308	0.3577	0.3308	0.3661	0.3282	0.3671	0.3360	0.3671	0.3360	0.4053	0.3570	0.4053	0.3701	0.4107	0.3820	0.4102	0.3960
2			0.3310	0.3170	0.3325	0.3352	0.3325	0.3411	0.3282	0.3671	0.3360	0.3360	0.3360	0.3715	0.3439	0.3715	0.3530	0.3772	0.3613	0.3778	0.3719
6/18	0.3005		0.5262	0.2928	0.3138	0.5552	0.3138	0.5829	0.3396	0.6009	0.3720	0.6009	0.3720	0.6297	0.4021	0.6297	0.4270	0.5715	0.4478	0.5200	0.4623
16			0.4990	0.2971	0.3172	0.5260	0.3172	0.5560	0.3420	0.5743	0.3747	0.5743	0.3747	0.6037	0.3919	0.6037	0.4169	0.5273	0.4478	0.5000	0.4536
14			0.4765	0.3012	0.3234	0.5020	0.3234	0.5320	0.3448	0.5503	0.3774	0.5503	0.3774	0.5791	0.3857	0.5791	0.4119	0.5145	0.4331	0.5050	0.4536
12			0.4540	0.3053	0.3306	0.4778	0.3306	0.5078	0.3476	0.5261	0.3800	0.5261	0.3800	0.5548	0.3946	0.5548	0.4201	0.5022	0.4004	0.4843	0.4416
10			0.4315	0.3094	0.3378	0.4536	0.3378	0.4836	0.3504	0.5019	0.3822	0.5019	0.3822	0.5306	0.4006	0.5306	0.4269	0.4900	0.4596	0.4570	0.4249
8			0.4090	0.3135	0.3462	0.4294	0.3462	0.4594	0.3530	0.4777	0.3844	0.4777	0.3844	0.5064	0.4183	0.5064	0.4446	0.4522	0.4242	0.4240	0.4030
6			0.3865	0.3176	0.3549	0.4052	0.3549	0.4352	0.3556	0.4539	0.3866	0.4539	0.3866	0.4826	0.4321	0.4826	0.4584	0.4262	0.3876	0.4240	0.4030
4			0.3640	0.3217	0.3622	0.3809	0.3622	0.3992	0.3583	0.4176	0.3895	0.4176	0.3895	0.4464	0.4314	0.4464	0.4568	0.4242	0.3876	0.4240	0.4030
2			0.3415	0.3258	0.3700	0.3592	0.3700	0.3881	0.3671	0.3960	0.3879	0.3960	0.3879	0.4258	0.4364	0.4258	0.4373	0.4046	0.3876	0.4240	0.4030
5/20	0.1977		0.5784	0.2719	0.3192	0.6142	0.3192	0.6388	0.3216	0.6388	0.3216	0.6388	0.3216	0.6634	0.3321	0.6634	0.3530	0.6373	0.4887	0.5491	0.4883
18			0.5540	0.2804	0.3038	0.5918	0.3038	0.6161	0.3277	0.6297	0.3642	0.6297	0.3642	0.6543	0.3753	0.6543	0.3953	0.6297	0.4887	0.5491	0.4883
16			0.5300	0.2880	0.3102	0.5697	0.3102	0.5950	0.3331	0.6037	0.3657	0.6037	0.3657	0.6283	0.3763	0.6283	0.3989	0.6037	0.4887	0.5491	0.4883
14			0.5060	0.2950	0.3158	0.5477	0.3158	0.5730	0.3370	0.5811	0.3664	0.5811	0.3664	0.6057	0.3800	0.6057	0.4022	0.5811	0.4887	0.5491	0.4883
12			0.4820	0.3020	0.3194	0.5258	0.3194	0.5510	0.3409	0.5591	0.3690	0.5591	0.3690	0.5837	0.3837	0.5837	0.4064	0.5591	0.4887	0.5491	0.4883
10			0.4580	0.3088	0.3240	0.5038	0.3240	0.5290	0.3448	0.5371	0.3671	0.5371	0.3671	0.5617	0.3866	0.5617	0.4101	0.5371	0.4887	0.5491	0.4883
8			0.4340	0.3156	0.3286	0.4818	0.3286	0.5068	0.3487	0.5140	0.3694	0.5140	0.3694	0.5389	0.3904	0.5389	0.4138	0.5140	0.4887	0.5491	0.4883
6			0.4100	0.3224	0.3330	0.4598	0.3330	0.4848	0.3526	0.4920	0.3727	0.4920	0.3727	0.5167	0.3914	0.5167	0.4175	0.4920	0.4887	0.5491	0.4883
4			0.3860	0.3292	0.3400	0.4378	0.3400	0.4628	0.3564	0.4700	0.3800	0.4700	0.3800	0.4939	0.3994	0.4939	0.4212	0.4700	0.4887	0.5491	0.4883
2			0.3620	0.3360	0.3470	0.4158	0.3470	0.4408	0.3602	0.4470	0.3879	0.4470	0.3879	0.4718	0.4064	0.4718	0.4295	0.4470	0.4887	0.5491	0.4883
4/20	0.1200		0.5898	0.2622	0.2881	0.6329	0.2881	0.6806	0.2988	0.6806	0.2988	0.6806	0.2988	0.7283	0.3506	0.7283	0.3953	0.7033	0.5506	0.6445	0.5514
18			0.5620	0.2724	0.2978	0.6039	0.2978	0.6538	0.3100	0.6409	0.3533	0.6409	0.3533	0.6926	0.3617	0.6926	0.4064	0.6776	0.5506	0.6445	0.5514
16			0.5340	0.2826	0.3032	0.5750	0.3032	0.6257	0.3151	0.6121	0.3586	0.6121	0.3586	0.6603	0.3669	0.6603	0.4175	0.6454	0.5506	0.6445	0.5514
14			0.5060	0.2928	0.3084	0.5471	0.3084	0.5990	0.3192	0.5840	0.3624	0.5840	0.3624	0.6289	0.3774	0.6289	0.4286	0.6121	0.5506	0.6445	0.5514
12			0.4780	0.3030	0.3136	0.5192	0.3136	0.5711	0.3233	0.5560	0.3664	0.5560	0.3664	0.5949	0.3855	0.5949	0.4397	0.5711	0.5506	0.6445	0.5514
10			0.4500	0.3132	0.3238	0.4913	0.3238	0.5434	0.3274	0.5282	0.3705	0.5282	0.3705	0.5671	0.3946	0.5671	0.4508	0.5434	0.5506	0.6445	0.5514
8			0.4220	0.3234	0.3340	0.4634	0.3340	0.5155	0.3315	0.5003	0.3736	0.5003	0.3736	0.5442	0.4017	0.5442	0.4619	0.5155	0.5506	0.6445	0.5514
6			0.3940	0.3336	0.3442	0.4355	0.3442	0.4876	0.3356	0.4724	0.3857	0.4724	0.3857	0.5171	0.4188	0.5171	0.4730	0.4876	0.5506	0.6445	0.5514
4			0.3660	0.3438	0.3544	0.4076	0.3544	0.4597	0.3396	0.4444	0.3848	0.4444	0.3848	0.4893	0.4309	0.4893	0.4841	0.4597	0.5506	0.6445	0.5514
2			0.3380	0.3540	0.3646	0.3797	0.3646	0.4318	0.3437	0.4164	0.3900	0.4164	0.3900	0.4609	0.4456	0.4609	0.4889	0.4597	0.5506	0.6445	0.5514

TABLE I.—Continued.

		Reds (continued)										Yellow-Reds (continued)														
		2.5R		5.0R		7.5R		10.0R		Y		V/C		2.5YR		5.0YR		7.5YR		10.0YR						
V/C	Y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y					
3/16	0.06555	6116	2466	6530	2660	6817	2872	7003	3249	0.06555	3/10	5941	3818	5456	4040	5390	4306	5305	4559	6302	2287	6791	2520	7165	2734	
12		5326	2579	5704	2789	6092	3015	6322	3361		8	5475	3771	4966	3908	4930	4116	4872	4326	6300	2465	6930	2704	7432	2937	
10		5191	2691	5584	2904	6158	3240	6710	3440		6	4954	3692	4666	3715	4378	3865	4341	4018	5995	2874	6247	3129	6848	3068	
8		4821	2918	5064	3114	5251	3297	5393	3477		4	4738	3467	4854	3477	4584	3412	4208	3549	5390	2874	6247	3129	6848	3068	
6		4409	3009	4592	3168	4738	3316	4854	3477		2	4240	3302	4308	3412	4008	3314	3757	3391	4676	3688	5280	3581	5426	3925	
4		4021	3076	4148	3190	4240	3302	4308	3412			3757	3391	3771	3476	3371	3549	3446	3982	4676	3688	5280	3581	5426	3925	
2/14	0.03126	5734	2083	6302	2287	6791	2520	7165	2734	0.03126	2/8	5995	3590	5426	3925	5475	4271	5390	4306	5305	4559	6302	2287	6791	2520	7165
12		5438	2254	5930	2465	6392	2704	6732	2937		6	5280	3581	4676	3688	4676	3688	4676	3688	4676	3688	5280	3581	4676	3688	
10		5122	2428	5557	2633	5952	2874	6247	3129		4	4598	3508	4674	3738	4690	3964	3859	3590	4676	3688	5280	3581	4676	3688	
8		4776	2593	5143	2800	5433	3027	5713	3259		2	3852	3365	3880	3476	3889	3590	4446	3982	4676	3688	5280	3581	4676	3688	
6		4490	2760	4642	2934	4875	3123	5095	3331			6721	4058	5660	3795	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	
4		4021	2900	4184	3032	4335	3169	4481	3330		2	4258	3344	4377	3580	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	
2		3614	3033	3692	3111	3751	3181	3811	3274			6721	4058	5660	3795	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	
1/10	0.01210	5058	1900	5604	2100	6111	2290	6661	2499	0.01210	1/8	6721	4058	5660	3795	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	
8		4812	2103	5282	2297	5722	2487	6178	2713		6	6048	3270	6048	3270	6048	3270	6048	3270	6048	3270	6048	3270	6048	3270	
6		4515	2329	4885	2515	5235	2698	5584	2921		4	5311	3371	5311	3371	5311	3371	5311	3371	5311	3371	5311	3371	5311	3371	
4		4166	2569	4420	2728	4660	2888	4933	3068		2	4258	3344	4377	3580	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	
2		3768	2816	3908	2929	4020	3034	4128	3154			6721	4058	5660	3795	4430	3775	4446	3982	4676	3688	5280	3581	4676	3688	

		Yellows										Green-Yellows									
		2.5Y		5.0Y		7.5Y		10.0Y		Y		V/C		2.5GY		5.0GY		7.5GY		10.0GY	
V/C	Y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y
9/20	0.7866	0.4569	0.4527	0.4830	0.5092	0.4663	0.5188	0.4540	0.5320	0.7866	9/18	0.4354	0.5508	0.4108	0.5699	0.3602	0.5920	0.3032	0.5748	0.4569	0.4527
18		4711	4977	4711	4977	4595	5104	4477	5225		16	4288	5383	4058	5541	3581	5654	3079	5440	4569	4527
16		4602	4869	4602	4869	4503	4993	4393	5101		14	4212	5237	3993	5329	3551	5339	3115	5129	4569	4527
14		4425	4719	4425	4719	4369	4829	4271	4920		12	4108	5028	3911	5082	3518	5042	3139	4829	4569	4527
12		4275	4529	4275	4529	4201	4622	4120	4694		10	3973	4761	3810	4791	3471	4735	3152	4558	4569	4527
10		4080	4319	4080	4319	4019	4392	3957	4450		8	3834	4490	3698	4497	3414	4415	3157	4259	4569	4527
8		3811	4161	3811	4161	3751	4261	3681	4352		6	3681	4261	3581	4352	3314	4306	3164	4006	4569	4527
6		3623	3790	3623	3790	3591	3832	3558	3852		4	3499	3866	3437	3866	3274	3791	3184	3706	4569	4527
4		3378	3504	3378	3504	3365	3527	3349	3537		2	3321	3539	3284	3534	3198	3500	3124	3454	4569	4527
2		3091	4900	3091	4900	3079	5200	3061	5366		8/24	0.5910	0.5910	0.5910	0.5910	0.5910	0.5910	0.5910	0.5910	0.5910	0.5910
18		3035	4855	3035	4855	3027	5152	3018	5306		22	4371	5577	4127	5855	3592	6235	2846	6564	5910	5910
16		2847	4712	2847	4712	2840	5062	2832	5181		20	4261	5444	4011	5668	3546	6006	2987	6255	5910	5910
14		2678	4589	2678	4589	2674	5062	2662	5181		18	4154	5313	3924	5199	3511	5144	3091	5747	5910	5910
12		2469	4423	2469	4423	2463	4712	2450	5020		16	4021	4869	3816	4879	3463	4791	3140	4926	5910	5910
10		2231	4231	2231	4231	2224	4466	2210	4791		14	3858	4550	3696	4542	3408	4452	3149	4601	5910	5910
8		1969	4009	1969	4009	1962	4175	1948	4520		12	3690	4230	3573	4214	3359	4129	3150	4284	5910	5910
6		1684	3751	1684	3751	1676	3861	1658	4216		10	3504	3887	3433	3872	3266	3809	3140	3727	5910	5910
4		1394	3484	1394	3484	1385	3540	1366	3883		8	3327	3555	3284	3542	3194	3502	3121	3459	5910	5910
2		1091	3216	1091	3216	1082	3272	1063	3552		6	3154	3327	3118	3327	3154	3327	3118	3327	5910	5910

SPACING OF THE MUNSELL COLORS

TABLE I.—Continued.

V/C	Y	Greens (continued)										Blue-Greens (continued)									
		2.5G		5.0G		7.5G		10.0G		V/C	Y	2.5BG		5.0BG		7.5BG		10.0BG			
		x	y	x	y	x	y	x	y			x	y	x	y	x	y	x	y		
5/26	0.1977	0794	7385	0699	5898	0585	5224	0572	4590	5/24	0.1977	0738	3851	0781	3211	0982	2828	1108	2489		
26		0092	7185	0784	5761	0730	5131	0690	4542	22		1005	3814	0904	3231	1046	2828	1108	2489		
24		1188	6918	0953	5628	0878	5039	0811	4491	22		1165	3785	0944	3231	1167	2828	1108	2489		
22		1377	6674	1144	5463	1050	4927	0958	4428	20		1359	3708	1048	3275	1364	2932	1485	2662		
20		1579	6392	1318	5321	1212	4817	1120	4360	18		1589	3668	1148	3280	1537	2976	1485	2662		
18		1782	6095	1489	5171	1372	4705	1275	4288	16		1735	3606	1248	3280	1776	3032	1716	2760		
16		2005	5759	1695	4971	1571	4591	1469	4192	16		1980	3506	1380	3280	2030	3082	1970	2860		
14		2258	5405	1951	4721	1771	4351	1699	4022	14		2248	3452	1540	3270	2292	3125	2234	2840		
12		2545	5071	2104	4578	1966	4219	1852	3992	12		2589	3369	1720	3246	2550	3150	2512	3040		
10		2865	4705	2329	4331	2200	4082	2095	3853	10		2880	3270	1910	3210	2812	3161	2796	3111		
8		3210	4380	2511	4107	2395	3915	2297	3730	8											
6		3584	4045	2690	3860	2598	3724	2519	3587	6											
4		3943	3735	2841	3628	2775	3545	2711	3455	4											
2		4300	3445	2978	3392	2945	3355	2910	3310	2											
4/26	0.1200	0528	7502	0407	6010	0392	5288	0400	4545	4/24	0.1200	0510	3800	0675	3075	0768	2667	0888	2298		
26		0760	7250	0614	5857	0581	5131	0553	4492	22		0636	3788	0675	3075	0922	2718	1033	2376		
24		1009	6975	0841	5684	0770	5040	0702	4440	20		0768	3773	0922	3141	1092	2774	1033	2376		
22		1230	6706	1018	5543	0928	4942	0850	4380	18		0915	3754	0922	3141	1170	2868	1170	2694		
20		1446	6431	1188	5400	1086	4842	1006	4330	16		1102	3720	0992	3141	1258	2946	1258	2694		
18		1682	6111	1402	5214	1293	4703	1212	4245	16		1263	3688	1170	3170	1346	2946	1448	2694		
16		1909	5779	1627	5015	1500	4562	1398	4168	14		1438	3640	1346	3219	1438	2910	1480	2730		
14		2158	5455	1845	4822	1672	4419	1572	4033	12		1618	3600	1518	3249	1540	2910	1620	2730		
12		2455	5097	2115	4652	1892	4219	1827	3799	10		1800	3540	1800	3234	1815	2985	1760	2730		
10		2735	4215	2381	4262	2232	4022	2124	3655	8		2006	3480	2182	3240	2113	3052	2065	2863		
8		3012	3470	2699	3992	2467	3822	2374	3655	6		2278	3463	2480	3232	2429	3108	2384	2984		
6		3340	3111	2978	3704	2702	3602	2628	3498	4		2552	3375	2799	3208	2764	3148	2740	3091		
4		3612	2959	3417	3417	2919	3371	2880	3327	2		2840	3270	2799	3208	2764	3148	2740	3091		
3/22	0.06555	0390	7468	0340	6011	0332	5206	0333	4444	3/20	0.06555	0482	3695	0580	2940	0691	2559	0798	2151		
22		0620	7250	0505	5805	0498	4954	0498	4340	18		0636	3682	0735	2979	0874	2627	0986	2151		
20		0840	6975	0682	5605	0678	4818	0678	4340	16		0843	3667	0940	3027	1086	2706	1018	2281		
18		1049	6766	0882	5414	0878	4684	0878	4340	14		1051	3648	1158	3071	1258	2784	1258	2411		
16		1341	6420	1120	5414	1023	4667	1023	4340	12		1288	3620	1410	3118	1552	2872	1551	2571		
14		1626	6052	1382	5197	1262	4505	1262	4340	10		1485	3531	1703	3159	1820	2872	1820	2571		
12		1902	5642	1660	4948	1516	4340	1516	4340	8		1685	3486	1910	3106	2046	2872	2046	2571		
10		2170	5211	1935	4682	1800	4101	1800	4340	6		1890	3406	2182	3106	2272	3046	2272	2682		
8		2435	4752	2228	4380	2088	4101	2088	4340	4		2100	3346	2443	3106	2443	3046	2443	2682		
6		2682	4342	2471	4100	2346	3997	2346	4340	2		2327	3286	2734	3106	2734	3046	2734	2682		
4		2910	3886	2711	3886	2616	3597	2616	4340	2		2552	3227	2983	3106	2983	3046	2983	2682		
2		3160	3500	2999	3500	2890	3391	2890	4340	2		2799	3271	2742	3192	2699	3120	2660	3050		
2/16	0.03126	0329	7358	0277	5986	0276	5285	0285	4327	2/14	0.03126	0555	3588	0769	2880	0724	2478	0920	2133		
16		0820	6860	0688	5691	0629	4973	0599	4270	14		0851	3576	0969	2880	1046	2592	1258	2411		
14		1307	6308	1120	5358	1022	4759	0934	4183	12		1190	3551	1258	2932	1346	2682	1448	2571		
12		1773	5698	1560	4981	1442	4505	1321	4059	10		1485	3531	1540	3110	1747	2853	1669	2570		
10		2245	5143	2046	4682	1800	4340	1800	4340	8		1735	3506	1843	3110	2046	2981	2096	2790		
8		2735	4522	2318	4331	2200	3983	2092	3730	6		1971	3457	2182	3150	2318	2981	2162	2981		
6		3210	3998	2640	3845	2540	3705	2442	3559	4		2243	3378	2443	3150	2612	2981	2318	2981		
4		3612	3507	2918	3450	2869	3400	2820	3341	2		2512	3271	2697	3175	2651	3098	2606	3010		
2		3978	3057	3160	3160	3050	3160	3050	3341	2		2765	3271	2697	3175	2651	3098	2606	3010		
1/8	0.01210	0620	6896	0559	5710	0530	4943	0511	4158	1/8	0.01210	0476	3458	1093	2860	1059	2485	1074	2129		
8		1711	5619	1468	4996	1344	4505	1249	4019	6		1169	3452	1483	2860	1169	2485	1258	2411		
6		2484	4489	2290	4218	2159	3967	2089	3702	4		1600	3406	1800	3021	1702	2493	1669	2570		
4		2910	3634	2833	3564	2738	3484	2689	3407	2		1880	3389	2300	3141	2430	2602	2362	2882		

TABLE I.—Continued.

		Blues										Purple-Blues									
V/C	Y	2.5B		5.0B		7.5B		10.0B		V/C	Y	2.5PB		5.0PB		7.5PB		10.0PB			
		x	y	x	y	x	y	x	y			x	y	x	y	x	y	x	y		
9/4	0.7866	0.2680	0.3073	0.2675	0.3005	0.2688	0.2961	0.2712	0.2924	9/4	0.7866	0.2975	0.3063	0.2991	0.3057	0.3015	0.3052	0.2910	0.2850		
8/12	0.5910	0.2909	0.3125	0.2919	0.3102	0.2937	0.3087	0.2949	0.3076	8/8	0.5910	0.2562	0.2709	0.2614	0.2670	0.2702	0.2648	0.2677	0.2643		
10		0.1877	0.2752	0.2237	0.2761	0.2252	0.2668	0.2294	0.2587	6		0.2758	0.2879	0.2798	0.2861	0.2856	0.2846	0.2702	0.2648		
8		0.2066	0.2839	0.2457	0.2888	0.2472	0.2821	0.2512	0.2760	6		0.2957	0.3047	0.2974	0.3039	0.3003	0.3034	0.2856	0.2846		
6		0.2462	0.3000	0.2457	0.2998	0.2688	0.2956	0.2718	0.2911	4								0.3011	0.2848		
4		0.2668	0.3067	0.2671	0.3096	0.2922	0.3077	0.2935	0.3062	2								0.2952	0.2801		
2		0.2897	0.3124	0.2908	0.3096	0.2922	0.3077	0.2935	0.3062	2								0.2932	0.2801		
7/16	0.4306	0.1435	0.2472	0.1615	0.2307	0.1818	0.2303	0.1883	0.2303	7/12	0.4306	0.2162	0.2309	0.2254	0.2267	0.2410	0.2224	0.2465	0.2058		
14		0.2384	0.2872	0.2672	0.2872	0.2672	0.2872	0.2672	0.2872	14		0.2538	0.2677	0.2596	0.2643	0.2687	0.2612	0.2563	0.2240		
12		0.1797	0.2775	0.1778	0.2530	0.1818	0.2303	0.1883	0.2303	12		0.2729	0.2848	0.2773	0.2828	0.2833	0.2809	0.2686	0.2240		
10		0.1994	0.2775	0.1986	0.2579	0.2016	0.2466	0.2078	0.2382	8		0.2833	0.2952	0.2883	0.2931	0.2982	0.2909	0.2776	0.2425		
8		0.2208	0.2871	0.2204	0.2854	0.2436	0.2787	0.2478	0.2728	8		0.2932	0.3025	0.2952	0.3011	0.2982	0.2909	0.2833	0.2425		
6		0.2418	0.2960	0.2410	0.2854	0.2633	0.2927	0.2685	0.2886	6		0.3025	0.3111	0.3011	0.3077	0.3048	0.2974	0.2886	0.2425		
4		0.2629	0.3038	0.2633	0.2972	0.2651	0.2927	0.2685	0.2886	4								0.2886	0.2425		
2		0.2867	0.3110	0.2875	0.3078	0.2888	0.3058	0.2908	0.3039	2								0.2932	0.2425		
6/16	0.3005	0.1294	0.2348	0.1310	0.2048	0.1376	0.1879	0.1454	0.1778	6/16	0.3005	0.1754	0.1868	0.1873	0.1822	0.2119	0.1799	0.2365	0.1671		
14		0.1480	0.2459	0.1496	0.2193	0.1556	0.2043	0.1629	0.1947	14		0.1913	0.2038	0.2026	0.1999	0.2241	0.1975	0.2440	0.1830		
12		0.1660	0.2561	0.1685	0.2339	0.1734	0.2203	0.1803	0.2114	12		0.2095	0.2225	0.2197	0.2188	0.2378	0.2168	0.2540	0.1976		
10		0.1879	0.2682	0.1883	0.2487	0.1934	0.2374	0.2000	0.2298	10		0.2274	0.2406	0.2360	0.2365	0.2505	0.2347	0.2637	0.2352		
8		0.2080	0.2789	0.2088	0.2635	0.2132	0.2537	0.2189	0.2468	8		0.2465	0.2599	0.2533	0.2558	0.2638	0.2531	0.2740	0.2533		
6		0.2312	0.2899	0.2320	0.2789	0.2352	0.2708	0.2399	0.2650	6		0.2684	0.2804	0.2734	0.2778	0.2798	0.2752	0.2863	0.2747		
4		0.2571	0.3008	0.2579	0.2938	0.2602	0.2881	0.2637	0.2840	4		0.2897	0.2991	0.2923	0.2978	0.2955	0.2963	0.2968	0.2863		
2		0.2835	0.3097	0.2842	0.3063	0.2854	0.3037	0.2871	0.3012	2								0.2897	0.2961		
5/18	0.1977	0.1090	0.2166	0.1132	0.1863	0.1230	0.1711	0.1203	0.1505	5/22	0.1977	0.1363	0.1410	0.1518	0.1365	0.1794	0.1239	0.2082	0.1225		
16		0.1283	0.2292	0.1320	0.2021	0.1404	0.1878	0.1492	0.1632	18		0.1495	0.1559	0.1638	0.1521	0.1945	0.1365	0.2121	0.1239		
14		0.1461	0.2406	0.1505	0.2172	0.1584	0.2042	0.1666	0.1964	16		0.1642	0.1728	0.1773	0.1689	0.2042	0.1661	0.2299	0.1444		
12		0.1649	0.2519	0.1693	0.2285	0.1776	0.2152	0.1858	0.2173	14		0.1793	0.1874	0.1924	0.1836	0.2187	0.1860	0.2440	0.1555		
10		0.1837	0.2632	0.1881	0.2400	0.1962	0.2267	0.2067	0.2344	12		0.1943	0.2028	0.2079	0.2004	0.2356	0.2030	0.2637	0.1698		
8		0.1947	0.2827	0.1991	0.2586	0.2077	0.2417	0.2067	0.2344	10		0.2117	0.2204	0.2255	0.2240	0.2417	0.2204	0.2712	0.1837		
6		0.2210	0.2823	0.2215	0.2701	0.2248	0.2612	0.2299	0.2548	8		0.2365	0.2448	0.2449	0.2449	0.2563	0.2417	0.2866	0.2412		
4		0.2492	0.2954	0.2493	0.2879	0.2511	0.2808	0.2547	0.2757	6		0.2600	0.2720	0.2662	0.2687	0.2739	0.2666	0.2821	0.2659		
2		0.2791	0.3071	0.2794	0.3032	0.2803	0.3000	0.2821	0.2966	2		0.2847	0.2942	0.2882	0.2923	0.2918	0.2908	0.2821	0.2959		
4/16	0.1200	0.0908	0.1973	0.1098	0.1785	0.1204	0.1655	0.1155	0.1416	4/30	0.1200	0.1288	0.1288	0.1288	0.1288	0.1288	0.1288	0.1288	0.1288		
14		0.1027	0.2057	0.1063	0.1963	0.1153	0.1655	0.1310	0.1580	18		0.1218	0.1208	0.1392	0.1167	0.1798	0.1185	0.2075	0.1256		
12		0.1247	0.2159	0.1293	0.1963	0.1393	0.1655	0.1310	0.1580	16		0.1336	0.1349	0.1504	0.1317	0.1861	0.1316	0.2120	0.1256		
10		0.1461	0.2272	0.1517	0.2022	0.1607	0.1655	0.1310	0.1580	14		0.1473	0.1513	0.1627	0.1479	0.1941	0.1468	0.2220	0.1303		
8		0.1675	0.2387	0.1731	0.2127	0.1821	0.1655	0.1310	0.1580	12		0.1604	0.1688	0.1823	0.1633	0.2152	0.1631	0.2487	0.1417		
6		0.1889	0.2502	0.1945	0.2242	0.2035	0.1655	0.1310	0.1580	10		0.1731	0.1815	0.2023	0.1833	0.2388	0.1831	0.2838	0.1567		
4		0.2103	0.2617	0.2169	0.2381	0.2252	0.1655	0.1310	0.1580	8		0.1955	0.2094	0.2103	0.2050	0.2404	0.2023	0.2977	0.2038		
2		0.2360	0.2872	0.2436	0.2572	0.2470	0.1655	0.1310	0.1580	6		0.2235	0.2343	0.2325	0.2300	0.2471	0.2266	0.2618	0.2263		
		0.2727	0.3038	0.2723	0.2992	0.2733	0.2947	0.2753	0.2910	4		0.2487	0.2597	0.2562	0.2540	0.2657	0.2528	0.2759	0.2522		
										2		0.2782	0.2876	0.2816	0.2842	0.2861	0.2819	0.2911	0.2842		

TABLE I.—Continued.

			Purples										Red-Purples									
			2.5P		5.0P		7.5P		10.0P		V/C	Y	2.5RP		5.0RP		7.5RP		10.0RP			
V/C	Y		ε	γ	ε	γ	ε	γ	ε	γ			ε	γ	ε	γ	ε	γ	ε	γ		
9/6	0.7866		0.2963	0.2865	0.3003	0.2870	0.3120	0.2788	0.3218	0.2845	9/6	0.7866	0.3322	0.2910	0.3431	0.2988	0.3512	0.3052	0.3590	0.3118		
4			.3050	.3051	.3067	.3060	.3107	.2928	.3176	.2966	4		.3234	.3301	.3060	.3350	.3099	.3400	.3140			
2											2		.3149	.3108	.3172	.3126	.3141	.3205	.3155			
8/14	0.5910										8/14	0.5910	0.3621	0.3818	0.4002	0.4289	0.4579	0.4866	0.5155	0.5444		
10											10		.3496	.3742	.4002	.4289	.4579	.4866	.5155			
12											12		.3496	.3742	.4002	.4289	.4579	.4866	.5155			
8											8		.3496	.3742	.4002	.4289	.4579	.4866	.5155			
6											6		.3496	.3742	.4002	.4289	.4579	.4866	.5155			
4											4		.3496	.3742	.4002	.4289	.4579	.4866	.5155			
7/22	0.4306										7/22	0.4306	0.3811	0.4186	0.4579	0.4986	0.5400	0.5818	0.6240	0.6666		
20											20		.3811	.4186	.4579	.4986	.5400	.5818	.6240			
18											18		.3751	.4186	.4579	.4986	.5400	.5818	.6240			
16											16		.3688	.4186	.4579	.4986	.5400	.5818	.6240			
14											14		.3620	.4186	.4579	.4986	.5400	.5818	.6240			
12											12		.3555	.4186	.4579	.4986	.5400	.5818	.6240			
10											10		.3496	.4186	.4579	.4986	.5400	.5818	.6240			
8											8		.3431	.4186	.4579	.4986	.5400	.5818	.6240			
6											6		.3372	.4186	.4579	.4986	.5400	.5818	.6240			
4											4		.3313	.4186	.4579	.4986	.5400	.5818	.6240			
2											2		.3254	.4186	.4579	.4986	.5400	.5818	.6240			
6/26	0.3005										6/26	0.3005	0.3170	0.3206	0.3242	0.3278	0.3314	0.3350	0.3386	0.3422		
24											24		.3170	.3206	.3242	.3278	.3314	.3350	.3386			
20											20		.3111	.3206	.3242	.3278	.3314	.3350	.3386			
18											18		.3052	.3206	.3242	.3278	.3314	.3350	.3386			
16											16		.2993	.3206	.3242	.3278	.3314	.3350	.3386			
14											14		.2934	.3206	.3242	.3278	.3314	.3350	.3386			
12											12		.2875	.3206	.3242	.3278	.3314	.3350	.3386			
10											10		.2816	.3206	.3242	.3278	.3314	.3350	.3386			
8											8		.2757	.3206	.3242	.3278	.3314	.3350	.3386			
6											6		.2698	.3206	.3242	.3278	.3314	.3350	.3386			
4											4		.2639	.3206	.3242	.3278	.3314	.3350	.3386			
2											2		.2580	.3206	.3242	.3278	.3314	.3350	.3386			
5/30	0.1977										5/30	0.1977	0.3188	0.3232	0.3276	0.3320	0.3364	0.3408	0.3452	0.3496		
28											28		.3188	.3232	.3276	.3320	.3364	.3408	.3452			
26											26		.3129	.3232	.3276	.3320	.3364	.3408	.3452			
24											24		.3070	.3232	.3276	.3320	.3364	.3408	.3452			
22											22		.3011	.3232	.3276	.3320	.3364	.3408	.3452			
20											20		.2952	.3232	.3276	.3320	.3364	.3408	.3452			
18											18		.2893	.3232	.3276	.3320	.3364	.3408	.3452			
16											16		.2834	.3232	.3276	.3320	.3364	.3408	.3452			
14											14		.2775	.3232	.3276	.3320	.3364	.3408	.3452			
12											12		.2716	.3232	.3276	.3320	.3364	.3408	.3452			
10											10		.2657	.3232	.3276	.3320	.3364	.3408	.3452			
8											8		.2598	.3232	.3276	.3320	.3364	.3408	.3452			
6											6		.2539	.3232	.3276	.3320	.3364	.3408	.3452			
4											4		.2480	.3232	.3276	.3320	.3364	.3408	.3452			
2											2		.2421	.3232	.3276	.3320	.3364	.3408	.3452			
4/32	0.1200										4/32	0.1200	0.4011	0.4048	0.4085	0.4122	0.4159	0.4196	0.4233	0.4270		
30											30		.4011	.4048	.4085	.4122	.4159	.4196	.4233			
28											28		.3952	.4048	.4085	.4122	.4159	.4196	.4233			
26											26		.3893	.4048	.4085	.4122	.4159	.4196	.4233			
24											24		.3834	.4048	.4085	.4122	.4159	.4196	.4233			
22											22		.3775	.4048	.4085	.4122	.4159	.4196	.4233			
20											20		.3716	.4048	.4085	.4122	.4159	.4196	.4233			
18											18		.3657	.4048	.4085	.4122	.4159	.4196	.4233			
16											16		.3598	.4048	.4085	.4122	.4159	.4196	.4233			
14											14		.3539	.4048	.4085	.4122	.4159	.4196	.4233			
12											12		.3480	.4048	.4085	.4122	.4159	.4196	.4233			
10											10		.3421	.4048	.4085	.4122	.4159	.4196	.4233			
8											8		.3362	.4048	.4085	.4122	.4159	.4196	.4233			
6											6		.3303	.4048	.4085	.4122	.4159	.4196	.4233			
4											4		.3244	.4048	.4085	.4122	.4159	.4196	.4233			
2											2		.3185	.4048	.4085	.4122	.4159	.4196	.4233			

TABLE II. I.C.I. (Y) equivalents (in per cent relative to MgO) of the recommended Munsell value scale (V) from 0/ to 10/.

V	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)	Y	Y _F (%)						
10.00	102.56																						
9.99	102.30	9.14	81.73	8.29	64.38	7.44	49.72	6.59	37.38	5.74	27.12	4.89	18.79	4.04	12.26	3.19	7.27	2.34	4.092	1.49	2.002	0.64	0.747
8	102.04	3	81.50	8	64.19	3	49.56	8	37.25	3	27.02	8	18.70	3	12.19	8	7.35	3	4.060	8	1.983	3	.735
7	101.78	2	81.28	7	64.01	2	49.41	7	37.12	2	26.91	7	18.62	2	12.12	7	7.328	2	4.029	7	1.965	2	.723
6	101.52	1	81.06	6	63.82	1	49.25	6	36.99	1	26.80	6	18.53	1	12.06	6	7.281	1	3.998	6	1.947	1	.711
5	101.25	0	80.84	5	63.63	0	49.09	5	36.86	0	26.69	5	18.44	0	12.00	5	7.234	0	3.968	5	1.929	0	.699
9.94	100.99	9.09	80.62	8.24	63.45	7.39	48.93	6.54	36.72	5.69	26.58	4.84	18.36	3.99	11.935	3.14	7.177	2.29	3.938	1.44	1.910	0.59	.687
3	100.73	8	80.40	3	63.26	8	48.78	3	36.59	8	26.48	3	18.27	8	11.870	3	7.140	8	3.907	3	1.892	8	.675
2	100.47	7	80.18	2	63.08	7	48.62	2	36.46	7	26.37	2	18.19	7	11.805	2	7.094	7	3.877	2	1.874	7	.663
1	100.21	6	79.97	1	62.89	6	48.47	1	36.33	6	26.26	1	18.10	6	11.740	1	7.048	6	3.847	1	1.856	6	.651
0	99.95	5	79.75	0	62.71	5	48.31	0	36.20	5	26.15	0	18.02	5	11.675	0	7.002	5	3.817	0	1.838	5	.640
9.89	99.69	0.04	79.53	8.19	62.52	7.34	48.16	6.49	36.07	5.64	26.05	4.79	17.93	3.94	11.611	3.09	6.956	2.24	3.787	1.39	1.821	0.54	.628
8	99.44	3	79.31	3	62.34	3	48.00	3	35.94	3	25.94	3	17.85	3	11.547	3	6.911	3	3.758	3	1.803	3	.617
7	99.18	2	79.10	2	62.16	2	47.85	2	35.81	2	25.84	2	17.76	2	11.483	2	6.866	2	3.729	2	1.786	2	.605
6	98.92	1	78.88	1	61.98	1	47.69	1	35.68	1	25.73	1	17.68	1	11.419	1	6.821	1	3.700	1	1.769	1	.593
5	98.66	0	78.66	0	61.79	0	47.54	0	35.56	0	25.62	0	17.60	0	11.356	0	6.776	0	3.671	0	1.752	0	.581
9.84	98.41	8.99	78.45	8.14	61.61	7.29	47.38	6.44	35.43	5.59	25.52	4.74	17.51	3.89	11.292	3.04	6.731	2.19	3.642	1.34	1.735	0.49	.570
3	98.15	8	78.23	3	61.43	8	47.23	3	35.30	8	25.41	3	17.43	8	11.229	3	6.687	8	3.613	3	1.718	8	.559
2	97.90	7	78.02	2	61.25	7	47.08	2	35.17	7	25.31	2	17.34	7	11.167	2	6.643	7	3.585	2	1.701	7	.547
1	97.64	6	77.80	1	61.07	6	46.92	1	35.04	6	25.20	1	17.26	6	11.104	1	6.599	6	3.557	1	1.684	6	.535
0	97.39	5	77.59	0	60.88	5	46.77	0	34.92	5	25.10	0	17.18	5	11.042	0	6.555	5	3.529	0	1.667	5	.524
9.79	97.14	8.94	77.38	8.09	60.70	7.24	46.62	6.39	34.79	5.54	25.00	4.69	17.10	3.81	10.980	2.99	6.511	2.14	3.501	1.29	1.650	0.44	.513
8	96.88	3	77.16	8	60.52	3	46.47	8	34.66	3	24.89	8	17.02	3	10.918	8	6.468	3	3.473	8	1.634	3	.501
7	96.63	2	76.95	7	60.35	2	46.32	7	34.54	2	24.79	7	16.93	2	10.856	7	6.425	2	3.445	7	1.618	2	.489
6	96.38	1	76.74	6	60.17	1	46.17	6	34.41	1	24.69	6	16.85	1	10.795	6	6.382	1	3.418	6	1.601	1	.478
5	96.13	0	76.53	5	59.99	0	46.02	5	34.28	0	24.58	5	16.77	0	10.734	5	6.339	0	3.391	5	1.585	0	.467
9.74	95.88	8.89	76.32	8.04	59.81	7.19	45.87	6.34	34.16	5.49	24.48	4.64	16.69	3.79	10.673	2.94	6.296	2.09	3.364	1.24	1.569	0.39	.455
3	95.63	8	76.11	3	59.63	8	45.72	3	34.03	8	24.38	3	16.61	8	10.612	3	6.254	8	3.337	3	1.553	8	.444
2	95.38	7	75.90	2	59.45	7	45.57	2	33.91	7	24.28	2	16.53	7	10.551	2	6.212	7	3.310	2	1.537	7	.432
1	95.13	6	75.69	1	59.28	6	45.42	1	33.78	6	24.17	1	16.45	6	10.491	1	6.170	6	3.283	1	1.521	6	.421
0	94.88	5	75.48	0	59.10	5	45.27	0	33.66	5	24.07	0	16.37	5	10.431	0	6.128	5	3.256	0	1.506	5	.409
9.69	94.63	8.84	75.27	7.99	58.92	7.14	45.12	6.29	33.54	5.44	23.97	4.59	16.29	3.74	10.371	2.89	6.086	2.04	3.230	1.19	1.490	0.34	.398
8	94.38	3	75.06	8	58.74	3	44.97	8	33.41	3	23.87	8	16.21	3	10.311	8	6.045	3	3.204	8	1.475	3	.386
7	94.14	2	74.85	7	58.57	2	44.82	7	33.29	2	23.77	7	16.13	2	10.252	7	6.003	2	3.178	7	1.459	2	.375
6	93.89	1	74.64	6	58.39	1	44.67	6	33.16	1	23.67	6	16.05	1	10.193	6	5.962	1	3.152	6	1.444	1	.363
5	93.64	0	74.44	5	58.22	0	44.52	5	33.04	0	23.57	5	15.97	0	10.134	5	5.921	0	3.126	5	1.429	0	.352
9.64	93.40	8.79	74.23	7.94	58.04	7.09	44.38	6.24	32.92	5.39	23.47	4.54	15.89	3.69	10.075	2.84	5.881	1.99	3.100	1.14	1.413	0.29	.341
3	93.15	8	74.02	3	57.87	8	44.23	3	32.80	8	23.37	3	15.81	8	10.017	3	5.841	8	3.075	3	1.398	8	.329
2	92.91	7	73.82	2	57.69	7	44.08	2	32.67	7	23.27	2	15.74	7	9.959	2	5.800	7	3.050	2	1.383	7	.318
1	92.66	6	73.61	1	57.52	6	43.94	1	32.55	6	23.17	1	15.66	6	9.901	1	5.760	6	3.025	1	1.368	6	.306
0	92.42	5	73.40	0	57.35	5	43.79	0	32.43	5	23.07	0	15.57	5	9.843	0	5.720	5	3.000	0	1.354	5	.295
9.59	92.18	8.74	73.20	7.89	57.17	7.04	43.64	6.19	32.31	5.34	22.97	4.49	15.49	3.64	9.785	2.79	5.680	1.94	2.975	1.09	1.339	0.24	.283
8	91.93	3	72.99	8	57.00	3	43.50	8	32.19	3	22.87	8	15.42	3	9.728	8	5.641	3	2.950	8	1.324	3	.272
7	91.69	2	72.79	7	56.83	2	43.35	7	32.07	2	22.78	7	15.34	2	9.671	7	5.602	2	2.925	7	1.310	2	.260
6	91.45	1	72.59	6	56.66	1	43.21	6	31.95	1	22.68	6	15.26	1	9.614	6	5.563	1	2.901	6	1.295	1	.248
5	91.21	0	72.38	5	56.48	0	43.06	5	31.83	0	22.58	5	15.18	0	9.557	5	5.524	0	2.877	5	1.281	0	.237
9.54	90.97	8.69	72.18	7.84	56.31	6.99	42.92	6.14	31.71	5.29	22.48	4.44	15.11	3.59	9.501	2.74	5.485	1.89	2.853	1.04	1.267	0.19	.225
3	90.73	8	71.98	3	56.14	8	42.77	3	31.59	8	22.38	3	15.03	8	9.445	3	5.447	8	2.829	3	1.253	8	.214
2	90.49	7	71.78	2	55.97	7	42.63	2	31.47	7	22.29	2	14.96	7	9.389	2	5.408	7	2.805	2	1.238	7	.202
1	90.25	6	71.57	1	55.80	6	42.49	1	31.35	6	22.19	1	14.88	6	9.333	1	5.370	6	2.781	1	1.224	6	.191
0	90.01	5	71.37	0	55.63	5	42.34	0	31.23	5	22.09	0	14.81	5	9.277	0	5.332	5	2.758	0	1.210	5	.179
9.49	89.77	8.64	71.17	7.79	55.46	6.94	42.20	6.09	31.11	5.24	22.00	4.39	14.73	3.54	9.222	2.69	5.295	1.84	2.735	0.99	1.196	0.14	.167
8	89.53	3	70.97	8	55.29	3	42.06	8	30.99	3	21.90	8	14.66	3	9.167	8	5.257	3	2.718	8	1.182	3	.155
7	89.30	2	70.77	7	55.12	2	41.92	7	30.87	2	21.81	7	14.58	2	9.112	7	5.220	2	2.688	7	1.168	2	.143
6	89.06	1	70.57	6	54.95	1	41.77	6	30.75	1	21.71	6	14.51	1	9.058	6	5.183	1	2.665	6	1.154	1	.131
5	88.82	0	70.37	5	54.78	0	41.63	5	30.64	0	21.62	5	14.43	0	9.003	5	5.146	0	2.642	5	1.141	0	.120
9.44	88.59	8.59	70.17	7.74	54.62	6.89	41.49	6.04	30.52	5.19	21.52	4.34	14.36	3.49	8.949	2.64	5.109	1.79	2.620	0.94	1.128	0.09	.108
3	88.35	8	69.97	3	54.45	8	41.35	3	30.40	8	21.43	3	14.28	8	8.895	3	5.072	8	2.598	3	1.114	8	.096
2	88.12	7	69.78	2	54.28	7	41.21	2	30.28	7	21.33	2	14.21	7	8.841	2	5.036	7	2.575	2	1.101	7	.084
1	87.88	6	69.58	1	54.11	6	41.07	1	30.17	6	21.24	1	14.14										

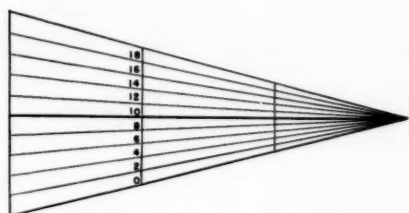


FIG. 10. Illustration of transparent scale for reading fractional hue or chroma between adjacent loci in Figs. 1-9.

- (1) From Table II it is found that for $V=2.4$, I.C.I. $Y=4.28$ percent.
- (2) Since $V=2.4/$, x and y will be found by interpolation between the charts for values $3/$ and $2/$. On Fig. 3 for $5.0R\ 3.0/9.9$, I.C.I. $x=0.548$ and $y=0.303$. On Fig. 2 for $5.0R\ 2.0/9.9$, I.C.I. $x=0.553$ and $y=0.264$.
- (3) Since 2.4 is 0.4 of the distance from 2.0 toward 3.0 , the interpolated chromaticity (x, y) will be that of value $2/$ plus 0.4 of the difference resulting when the chromaticity read from Fig. 2 is subtracted from that of Fig. 3. Since x on Fig. 2 is 0.553 and on Fig. 3 is 0.548 , the interpolated x will be

$$0.553 + [0.4 (0.548 - 0.553)] = 0.551.$$

Similarly, the interpolated y will be

$$0.264 + [0.4 (0.303 - 0.264)] = 0.280.$$

- (4) The complete notation for the sample is $Y=0.043$ (or 4.3 percent); $x=0.551$, $y=0.280$.

Still another illustration of the use of the above data is shown in Table III. This table shows the effect of the revision on the notation of the Munsell samples by presenting revised designations for them. The entries for this table were obtained as follows: (a) Given the Munsell sample, the I.C.I. data for them were taken from reports of the National Bureau of Standards (21), Glenn-Killian (9), and Granville-Nickerson-Foss (10); (b) then the value was read from the subcommittee's Table II and the hue and chroma were interpolated by use of the large originals of Figs. 1-9.⁴ There are larger irregularities in the

⁴ The National Bureau of Standards and Glenn-Killian data provided a good check on the samples of the standard 20 hues. When there was doubt because of a large dis-

crepancy, National Bureau of Standards data were used because special calibration precautions had been taken to obtain accurate wave-length and photometric values. The National Bureau of Standards data were used for all value conversions. For the 20 intermediate hues only one set of data was available. It is important to recognize that the table depends upon the accuracy of the I.C.I. colorimetric data supplied for the samples.

chroma series than in the hue or value series, presumably because of the special difficulties in recognizing chroma and in producing a painted series to represent it.

Color samples are often evaluated by direct reference to charts of the *Munsell Book of Color*. This evaluation may be sufficient; if not, conversion to the recommended notation may be made directly by use of Table III or, when interpolations are necessary, by use of Figs. 1-9 on which points representing the *Book of Color* samples have first been spotted (21), (9), (10).

REVISION PROCEDURES

Details of the various procedures employed in arriving at the recommendations⁵ above may now be summarized conveniently in relation to each of the Munsell attributes taken separately.

Chroma Adjustments

The chromaticity surface provided by the I.C.I. coordinates themselves is far from perceptual equi-spacing, as several investigators (16), (23), (30) have shown. Even when Nickerson published the first smoothed chroma loci for Munsell colors, the smoothing of averaged visual estimates directly in such a system was recognized as a difficult task. The present smoothing operations demand more guidance for they involve the added complication of extrapolating beyond the published samples.

While an ideal system for psychological smoothing is not available, Adams' coordinates of chromatic-value afford some of the needed guidance. Plots of Munsell chroma loci on his charts at values $2/$ to $8/$, inclusive (2), evince sufficient approximation to circularity to facilitate considerably the actual smoothing operation. Once the smooth loci of chroma are located in the Adams' coordinates they remain smooth when converted to the (x, y) -coordinates.

A given point in chromatic-value is defined by

⁵ These recommendations provide smoothed curves that supersede those given in references 10 and 11 in ASA War Standard (3).

TABLE III. Re-notations for the *Munsell Book of Color* samples in accordance with the recommended spacing and smoothing adjustments.

Munsell Book Notation			Munsell Re-notation According to Recommended Curves			Munsell Book Notation			Munsell Re-notation According to Recommended Curves			Munsell Book Notation			Munsell Re-notation According to Recommended Curves			Munsell Book Notation			Munsell Re-notation According to Recommended Curves				
H	V	C	H	V	C	H	V	C	H	V	C	H	V	C	H	V	C	H	V	C	H	V	C		
2.5R	8/4		2.0R	7.8	3.1	7.5R	5/12		8.0R	4.9	11.9	5YR	8/4		4.0YR	8.0	3.5	2.5Y	9.2 ^{3/4}		1.5Y	9.2	2.5		
	2		4.0R	7.9	2.4	(cont'd)	10		7.5R	5.0	10.1		2		4.0YR	8.0	2.0		2		2.0Y	9.1	1.5		
	7/8		1.0R	7.0	6.2		8		7.5R	5.0	8.9		7/10		5.5YR	6.9	10.1		9/8		2.5Y	8.8	6.5		
	6		1.0R	7.1	5.0		6		7.0R	5.0	7.2		8		4.5YR	7.0	8.2		6		2.0Y	8.6	4.4		
	4		3.5R	7.2	3.5		4		7.0R	5.1	5.0		6		3.5YR	6.9	5.9		4		2.0Y	8.8	3.2		
	2		3.0R	7.1	2.3		2		7.0R	5.1	2.9		6		3.5YR	7.0	6.0		2		2.5Y	8.7	1.4		
	6/10		1.5R	6.1	9.2		4/12		7.5R	4.2	11.4		4		3.0YR	7.0	4.1		8/12		3.5Y	7.9	11.9		
	8		1.5R	6.0	7.3		10		7.5R	4.2	9.4		2		3.0YR	7.0	2.1		10		3.5Y	8.0	9.9		
	6		1.0R	6.2	5.5		8		7.0R	4.1	8.4		6/12		6.0YR	6.2	11.5		8		2.5Y	8.0	7.8		
	4		2.5R	6.3	4.0		6		7.5R	4.2	6.7		10		6.0YR	6.3	9.8		6		2.5Y	7.8	5.5		
	2		2.5R	6.1	2.5		4		7.5R	4.1	4.7		8		5.0YR	6.2	8.3		4		2.0Y	7.9	3.7		
	5/10		2.0R	5.1	10.1		2		7.0R	4.1	2.8		6		4.5YR	6.2	6.0		2		1.5Y	7.9	1.6		
	8		1.5R	5.0	8.9		3/10		7.5R	3.5	8.5		4		4.0YR	6.1	4.0		7/10		3.5Y	6.8	10.0		
	6		1.5R	5.1	6.8		8		7.5R	3.4	7.1		2		4.5YR	6.1	2.0		8		3.0Y	6.9	8.3		
	4		2.0R	5.1	5.0		6		7.0R	3.3	5.4		6		5.5YR	5.1	9.0		6		2.5Y	6.9	6.4		
	2		2.5R	5.0	2.9		4		6.5R	3.3	4.3		8		5.0YR	5.1	7.7		4		2.5Y	6.9	4.2		
	4/10		1.5R	4.1	9.4		2		5.0R	3.2	2.6		6		5.0YR	5.0	6.2		2		1.5Y	7.0	1.8		
	8		1.5R	4.1	8.2		2/4		4.5R	2.6	3.5		4		4.5YR	4.9	4.6		6/8		3.5Y	6.2	7.8		
	6		1.5R	4.0	6.3		2		5.5R	2.4	1.9		2		4.0YR	4.9	2.1		6		2.5Y	6.2	6.8		
	4		1.5R	4.1	4.6		10R	8/4	10.0R	8.1	3.7		4/8		6.0YR	4.2	6.3		4		3.0Y	6.3	4.4		
	2		1.5R	4.1	2.6		2		2.5YR	7.9	2.2		6		5.0YR	4.4	5.8		2		2.5Y	6.2	2.0		
	3/10		1.0R	3.2	8.3		4		5.0YR	4.3	4.6		2		4.0YR	4.1	2.3		5/6		3.0Y	5.1	6.5		
	8		1.5R	3.1	6.7		6		9.0R	7.2	5.7		4		5.0YR	3.3	4.1		4		3.0Y	5.1	3.9		
	6		1.0R	3.2	5.6		4		8.5R	7.2	4.7		2		5.0YR	3.1	2.0		2		2.5Y	5.1	1.7		
	4		1.5R	3.1	4.1		2		9.0R	7.1	2.7		3/4		5.0YR	3.3	4.1		4/4		2.5Y	4.1	3.9		
	2		1.5R	3.1	2.3		6/10		0.5YR	6.2	10.1		2		5.0YR	3.1	2.1		2		2.0Y	4.1	1.7		
	2/6		0.5R	2.5	4.8		8		0.5YR	6.3	8.2		2/2		4.5YR	2.4	1.8		3/2		2.5Y	3.4	1.9		
	4		0.5R	2.4	3.5		6		0.5YR	6.3	6.5		7.5YR	8/6	7.5YR	7.9	5.1		5Y	9.2 ^{3/6}	5.5Y	9.0	4.4		
	2		0.5R	2.3	2.3		4		9.0R	6.2	4.2		4		7.5YR	7.9	2.9		2		4.0Y	9.0	2.6		
							2		1.0YR	6.3	2.5		2		8.0YR	7.9	1.9		4		3.5Y	9.0	1.5		
5R	8/4		3.5R	8.0	3.6	5/10	10.0R	5.0	9.9	7/10	8.0YR	6.8	9.9		7.5YR	6.9	8.0		9/14		6.0Y	8.4	13.0		
	2		2.0R	8.1	2.2	8	10.0R	5.2	8.7	8	7.5YR	6.9	8.0		6		7.5YR	6.9	6.0		12		6.0Y	8.4	9.5
	7/8		3.5R	7.0	7.0	6	10.0R	5.1	7.1	6	7.5YR	6.9	6.0		8		7.5YR	6.8	6.0		10		5.0Y	8.4	8.2
	6		3.5R	7.1	5.7	4	9.5R	5.1	4.9	4	7.0YR	7.0	3.4		6		7.5YR	6.1	6.1		8		5.0Y	8.4	6.5
	4		3.0R	7.1	5.2	2	10.0R	5.2	2.6	2	6.5YR	7.0	1.8		4		7.0YR	6.2	3.5		6		6.0Y	8.5	4.8
	2		2.5R	7.2	2.6	4/10	9.5R	4.4	9.0	6/10	8.0YR	6.2	9.5		2		6.5YR	6.1	2.0		2		3.5Y	8.6	1.4
	6/10		4.0R	6.2	9.7	8	10.0R	4.3	8.4	8	7.5YR	6.2	8.0		8/12		5.5Y	7.9	12.3		10		5.5Y	7.9	11.1
	8		4.0R	6.2	8.1	6	10.0R	4.3	7.3	6	7.5YR	6.2	8.0		8		5.5Y	7.9	8.2		8		5.5Y	7.9	8.2
	6		3.5R	6.2	6.3	4	10.0R	4.2	4.7	4	7.0YR	6.2	3.5		6		4.5Y	7.9	8.3		6		4.5Y	7.9	5.8
	4		4.5R	6.3	4.5	2	10.0R	4.2	2.7	2	6.5YR	6.1	2.0		4		4.0Y	7.8	3.5		4		4.0Y	7.8	3.5
	2		4.0R	6.2	2.3	3/6	10.0R	3.3	5.4	4	10.0R	3.2	4.1		2		3.5Y	7.8	1.6		2		3.5Y	7.8	1.6
	5/12		5.5R	5.0	12.8	4	10.0R	3.2	4.1	2/2	8.5R	2.5	2.6		4/4		7.5YR	4.2	4.5		7/10		5.0Y	6.9	9.7
	10		5.0R	5.2	10.9	2	9.0R	3.3	2.2		8.5R	2.5	2.3		2		8.0YR	4.1	2.3		8		6.0Y	6.9	9.5
	8		4.5R	5.0	10.0	2.5YR	8/4		3.5YR	7.9	3.7		3/2		7.5YR	3.2	2.6		6		4.5Y	6.9	6.6		
	6		4.0R	5.0	8.0	7/10	2.5YR	6.8	10.0	4	4.0YR	7.9	2.3		6		8.0YR	4.1	2.3		4		4.0Y	7.0	3.8
	4		4.0R	4.9	5.3	8	2.5YR	6.8	7.2	2	2.0YR	7.0	3.9		2		9.0YR	7.9	1.5		2		4.0Y	7.1	1.6
	2		4.0R	5.0	2.8	6	2.0YR	7.0	5.6	6/13	3.5YR	6.2	12.5		4		2.0YR	7.0	3.9		6		5.0Y	6.2	7.2
	4/14		5.5R	4.2	13.2	12	3.5YR	6.1	11.5	10	3.0YR	6.1	9.8		2		2.5YR	7.1	2.3		4		4.5Y	6.1	4.0
	12		5.5R	4.2	13.2	8	3.0YR	6.1	9.8	8	3.0YR	6.0	8.2		6		2.0YR	7.0	5.6		2		4.0Y	6.2	1.7
	10		5.0R	4.2	12.6	6	2.5YR	6.8	7.2	6	2.5YR	6.1	6.4		4		2.0YR	7.0	3.9		6		5.0Y	6.2	7.2
	8		4.5R	4.2	10.8	4	2.0YR	7.0	5.6	4	2.0YR	6.3	4.5		2		2.0YR	7.0	3.9		4		4.5Y	6.1	4.0
	6		4.5R	4.2	9.4	2	2.5YR	7.1	2.3	2	3.5YR	6.1	2.4		2		3.5YR	6.1	2.4		2		4.0Y	6.2	1.7
	4		4.5R	4.1	6.8	12	3.5YR	6.2	12.5	10	3.0YR	6.1	9.8		8		3.0YR	6.0	8.2		6		6.0Y	6.0	5.0
	2		4.0R	4.1	2.6	8	3.0YR	6.0	8.2	6	2.5YR	6.1	6.4		4		2.0YR	6.3	4.5		4		5.0Y	5.0	3.9
	3/10		5.0R	3.2	8.3	4	2.0YR	6.3	4.5	2	3.5YR	6.1	2.4		2		3.5YR	6.1	2.4		2		4.5Y	5.2	1.7
	8		5.0R	3.2	7.4	5/10	2.5YR	5.0	9.3	8	2.5YR	5.1	7.8		6/10		10.0YR	6.5	9.8		4/4		5.0Y	4.1	3.6
	6		4.5R	3.4	6.2	8	2.5YR	5.1	9.3	6	2.5YR	5.1	7.8		8		9.5YR	6.4	8.0		2		3.5Y	4.3	1.7
	4		5.0R	3.2	4.6	4	2.5YR	5.0	6.6	4	0.5Y	6.1	4.1		6		0.5Y	6.3	6.7		6		6.0Y	5.0	6.0
	2		3.5R	3.1	2.1	4	1.5YR	5.0	4.9	2	9.0YR	5.9	2.0		4		9.0YR</								

TABLE III.—Continued.

Munsell Book Notation		Munsell Re-notation According to Recommended Curves			Munsell Book Notation		Munsell Re-notation According to Recommended Curves			Munsell Book Notation		Munsell Re-notation According to Recommended Curves			Munsell Book Notation		Munsell Re-notation According to Recommended Curves			
H	V/C	H	V	C	H	V/C	H	V	C	H	V/C	H	V	C	H	V/C	H	V	C	
2.5B (cont'd)	6/6 4 2	3.5B 4.5B 5.5B	6.0 6.2 6.1	5.9 4.2 2.4	10B (cont'd)	3/8 6 4 2	9.0B 9.5B 9.5B	3.3 3.2 3.1	7.1 5.6 3.9	7.5PB (cont'd)	5/14 12 10 8 6 4	7.0PB 7.0PB 7.0PB 7.5PB 7.5PB 7.5PB	5.0 5.0 5.0 5.0 5.0 5.0	10.8 10.0 8.7 7.3 5.8 4.0	2.5P (cont'd)	3/10 8 6 4 2	2.0P 2.5P 3.0P 3.5P 2.5P	3.3 3.2 3.2 3.2 3.1	11.6 9.7 8.1 6.4 3.5	
	5/6 4 2	3.5B 4.0B 6.5B	5.0 5.0 5.0	6.3 4.2 2.3		2/4 2	9.5B (0.5PB)	2.4 2.2	3.5 2.6		4/16 14 12 10	7.0PB 7.0PB 7.0PB 7.5PB	4.2 12.9 12.1 9.1		2/8 6 4 2	2.5P 2.5P 3.5P 5.5P	2.3 2.3 2.2 2.1	8.2 6.4 4.2 3.2		
	4/8 6 4 2	2.5B 2.5B 3.0B 4.5B	4.0 4.2 4.2 4.1	7.2 5.8 3.8 2.0	2.5PB	8/4 2	2.5PB 3.5PB	8.0 7.9	3.6 2.4		8 6 4 2	7.5PB 7.5PB 7.5PB 7.5PB	4.1 6.1 4.1 2.4	5P	8/4 2	4.5P 5.0P	8.0 8.0	4.8 2.5		
	3/6 4 2	3.5B 4.5B 7.5B	3.4 3.4 3.2	5.7 4.1 2.2		7/6 4 2	3.0PB 3.5PB	7.1 7.0	5.6 4.4 2.2		3/14 12 10 8 6 4 2	7.5PB 7.5PB 7.5PB 7.5PB 7.5PB 7.5PB	3.2 3.2 3.0 3.1 3.1 3.0		7/6 4 2	5.5P 5.0P 4.5P	7.0 7.1 6.9	6.4 4.8 2.7		
	2/2	1.5B	2.6	3.5		6/8 6 4 2	2.5PB 2.5PB 2.5PB	6.4 6.3 6.3	7.7 6.1 2.5		5/10 8 6 4 2	1.5PB 2.5PB 2.5PB 2.5PB	5.4 5.3 5.2 5.1		6/8 6 4 2	5.0P 4.5P 4.5P	6.1 6.2 6.2	9.1 7.1 3.0		
5B	8/4 2	4.0B 4.0B	8.1 8.2	2.9 2.2		5/10 8 6 4 2	1.5PB 2.5PB 2.5PB 3.5PB	5.4 5.3 5.2 5.1	8.8 8.0 6.0 2.3		2/10 8 6 4 2	6.5PB 7.0PB 7.0PB 7.0PB	2.4 10.4 9.1 3.7		5/10 8 6 4 2	5.0P 5.0P 5.0P 4.5P	5.1 5.1 5.0 5.0	10.9 8.9 6.8 4.7 2.5		
	6/6 4 2	5.5B 6.5B 7.5B	6.1 6.2 6.2	6.4 4.5 3.0		4/10 8 6 4 2	2.0PB 2.5PB 2.5PB 3.5PB	4.3 4.1 4.2 4.2	8.9 6.1 4.2 2.9		10PB	8/2	7.5PB 10.0PB	8.3 8.0	3.4 2.5		4/12 10 8 6 4 2	5.5P 5.0P 5.0P 5.0P 5.0P	4.1 4.1 4.1 4.1 4.1	12.6 10.1 8.2 6.1 4.2 2.2
	4/8 6 4 2	6.5B 5.5B 6.0B 5.0B	4.0 4.1 4.4 4.3	6.9 6.4 4.6 2.7		2/4 2	2.5PB 2.5PB	2.4 2.3	4.0 2.7		7/6 4 2	10.0PB 10.0PB 0.5P	7.0 7.1 7.0	5.3 4.0 2.4		3/10 8 6 4 2	5.0P 5.0P 4.5P 5.0P	3.3 3.2 3.2 3.2	11.2 8.4 6.4 2.2	
	3/6 4 2	5.0B 4.5B 5.5B	3.3 3.1 2.1	5.9 4.2 2.3	5PB	8/2	5.0PB	8.3	3.2		6/8 6 4 2	0.5P 10.0PB 10.0PB	6.2 6.1 6.3 6.4	8.0 6.3 4.8 3.0		2/6 4 2	5.0P 5.0P 5.5P	2.1 2.2 2.1	6.8 4.6 2.9	
	2/2	2.0B	2.2	2.2		7/6 4 2	4.0PB 4.0PB 3.5PB	7.2 7.3 7.4	5.6 4.5 3.0		5/10 8 6 4 2	10.0PB 10.0PB 10.0PB 10.0PB 10.0PB	5.0 5.2 5.2 5.2 5.2	9.6 8.4 6.8 5.0 3.1		7.5P	8/2	7.5P	8.0	3.3
7.5B	8/4 2	9.0B 7.5B	7.9 7.9	3.8 2.3		6/8 6 4 2	5.0PB 5.0PB 5.0PB	6.3 6.3 6.4	7.4 6.2 3.2		4/10 8 6 4 2	10.0PB 10.0PB 10.0PB 10.0PB 10.0PB	4.0 4.1 4.2 4.2 4.2	9.7 8.5 6.6 4.6 2.4		7/4 2	7.0P 7.5P	7.2 7.2	4.9 3.0	
	7/6 4 2	8.0B 9.0B 8.5B	7.0 7.1	5.1 4.2 2.2		5/10 8 6 4 2	3.5PB 4.0PB 4.0PB 4.5PB 5.0PB	5.3 5.4 5.3 5.2 5.1	8.6 7.9 6.2 4.4 3.1		3/10 8 6 4 2	10.0PB 10.0PB 10.0PB 1.0P	3.1 3.2 3.1 3.1	10.6 7.4 6.1 4.7 2.7		6/6 4 2	7.5P 7.5P 7.0P	6.2 6.2 6.0	7.3 5.5 2.8	
	6/6 4 2	7.5B 8.5B 8.5B	6.1 6.2 6.1	5.9 4.1 2.2		4/10 8 6 4 2	4.0PB 4.5PB 4.5PB 5.0PB	4.4 4.3 4.2 4.2	8.9 7.4 6.0 2.5		2/6 4 2	10.0PB 10.0PB 1.0P	2.2 2.2 2.2	5.5 4.8 3.5		5/8 4 2	8.0P 8.5P 9.0P	5.0 5.0 5.1	10.0 7.5 5.3 2.6	
	5/6 4 2	8.0B 8.5B 10.0B	5.2 5.2 5.2	6.5 4.6 2.6		3/12 10 8 6 4 2	4.0PB 4.5PB 4.5PB 5.0PB 5.0PB	3.3 3.4 3.2 3.1 3.1	9.4 8.5 7.0 5.6 2.1		2/6 4 2	10.0PB 10.0PB 1.0P	2.2 2.2 2.2	5.5 4.8 3.5		4/8 6 4 2	8.5P 8.5P 9.0P 8.5P	4.1 4.0 4.1 4.1	10.3 7.0 4.7 2.4	
	4/6 4 2	8.5B 9.0B 9.5B	4.1 4.2 4.2	6.6 4.5 2.7		7.5PB	8/4 2	6.5PB 7.5PB	8.0 8.0	3.4 1.8		8/4 2	3.5P 4.0P	7.8 7.9	4.1 2.4		3/8 6 4 2	7.5P 7.5P 8.0P	3.1 3.1 3.0	9.1 7.1 4.4 2.2
	3/4 2	8.0B 9.0B	3.3 3.4	4.4 2.5		2/6 4 2	4.0PB 4.0PB 4.5PB	2.3 2.3 2.2	5.9 4.8 2.6		7/6 4 2	3.0P 3.5P 3.5P	7.1 7.2 7.2	6.0 4.3 2.1		2/6 4 2	7.5P 7.5P 8.5P	2.3 2.2 2.2	6.4 5.1 2.5	
10B	8/4 2	9.5B (1.0PB) 9.5B	7.9 8.3 7.9	3.5 3.0 2.2		7/8 6 4 2	6.5PB 7.0PB 7.0PB 6.5PB	7.2 7.2 7.1 7.1	5.8 5.3 3.6 2.0		5/10 8 6 4 2	2.5P 2.5P 2.5P 2.5P	5.1 5.0 5.0 5.0	12.1 10.2 7.6 5.4 3.2		8/8 6 4 2	9.5P 9.5P 10.0P 10.0P	7.3 7.2 7.2 7.3	6.0 4.6 4.0 2.3	
	7/6 4 2	9.5B 9.0 1.0PB	7.2 7.2 7.0	5.7 4.0 2.5		6/10 8 6 4 2	7.0PB 7.0PB 7.5PB 7.5PB	6.2 6.2 6.1 6.2	8.6 7.1 5.9 4.2 2.5		4/10 8 6 4 2	2.5P 2.5P 2.5P 2.5P	4.1 4.2 4.1 4.0	11.5 9.5 8.0 5.6 3.5		6/8 6 4 2	9.0P 9.5P 10.0P 9.0P	6.2 6.2 6.2 6.2	8.0 8.0 4.6 2.8	

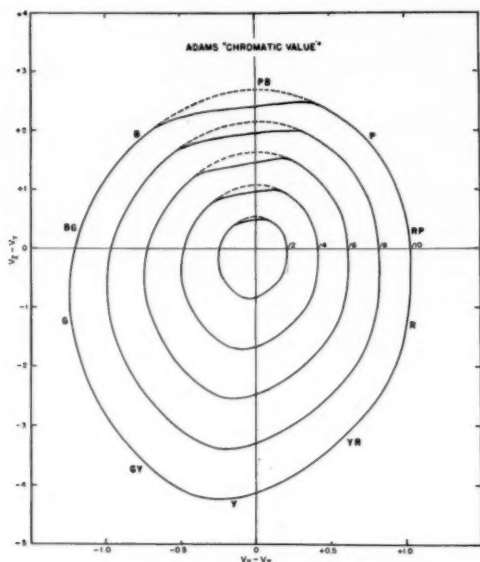


FIG. 11. The recommended loci for constant chroma $1/2$ to $1/10$ as plotted in Adams' chromatic-value coordinates. Dotted lines indicate original contour in the purple-blue region.

falls at $(V_X - V_Y) = 0.06$; $(V_Z - V_Y) = 0.085$; and from $5/$ up to $9/$ which falls at $(V_X - V_Y) = -0.10$; $(V_Z - V_Y) = -0.235$. Figure 11 shows the appearance of the family of concentric constant chroma loci at the region of the $5/$ value level in the Adams' coordinates. Each chroma locus is seen to be not only of the same shape but also at the same distance from adjacent loci as measured along any radius.

The achievement of these relations not only involved the adoption of the decentering expedient but also some considerable local departures from the data. On the other hand, the specification of chroma is greatly simplified and a much needed basis is provided for its extrapolation beyond the data through much used areas to the theoretical maximum (22). This extrapolation was accomplished as follows: First a listing was made of the I.C.I. (x, y) -figures for the MacAdam limits corresponding to 40 hues at each of nine values. Approximations to these limits are given in Table IV. Then the new chroma loci were extended at equal intervals (in Adams' space), up to the last even step which would come within the MacAdam limit (Table I).

When the system of ovoids established in

Adams' space was transformed into I.C.I. (x, y) -space, the results at the various value levels⁶ were as shown in Fig. 12. All the loci are seen to be smoothly transitional at a given value level or from one value to another. The chroma loci in Figs. 1-9 and Table I are adjusted for the differences required by the recommended value scale as compared to the Munsell-Sloan-Godlove value scale.

The spacing on the I.C.I. diagram is drastically affected by the major departures from perceptual uniformity of the I.C.I. system. The marked bunching of the chroma loci in the purple region emphasizes the difficulty which was avoided by smoothing in the more regular space employed.

After charts for $1/$ to $9/$ value levels had been completed, visual comparisons of chromatic samples were found to agree very well with the new chroma loci. There was, however, a marked exception in the blue and purple-blue region, especially at the lower and intermediate value levels. Although the sample comparisons pointed to real discrepancies between $5.0B$ and $7.5PB$, on either side of this rather narrow range the agreement was good. The most pronounced bulge in the entire sweep of the chroma loci occurred at

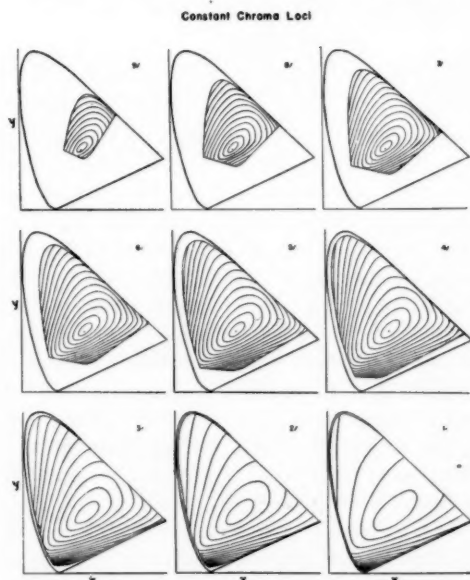


FIG. 12. Master chroma chart in the I.C.I. standard coordinate system showing the recommended loci of constant chroma for every second chroma step from zero to the theoretical maximum at every value level from $1/$ through $9/$.

about the middle of this range, but reference to the corresponding part of the ovoid developed in Adams' space showed that it was flattest there. Furthermore, the ovoid would need not only to be more flat, but actually concave in order to produce agreement with visual observation. The plots of the data in the Adams' space originally had suggested concavity in this one limited region, but the evidence had seemed insufficient to justify such a drastic localized departure from what the Adams' space was believed to represent. The low chromas indicated the type of curve first used (dotted line, Fig. 11) but higher chromas indicated concavity. In the original smoothing, the curve was pushed to the limit of the data in this region in order to afford some agreement with the rest of the curve. Now, however, visual

check on the result provided reason for giving the strong-chroma data more weight, and so the ovoid pattern was reduced to virtually a straight line (Fig. 11) in the region under discussion. Transformation to the I.C.I. (x, y)-diagram now resulted in chroma loci which partially correct the observed discrepancy; and the corresponding revisions were made in Figs. 1 to 9 and Table I. But the loci still are not really satisfactory in this region. Why, one might ask, should very sudden transitions be required in this particular region and nowhere else? This exception may be due, not to the Munsell samples or to the Adams' conversion, but to the I.C.I. system itself. The chromatic data, on which the standard observer is based, were taken with a 2° field centrally fixated. The luminosity data probably represent

TABLE IV. The I.C.I. (x, y) equivalents of the theoretical pigment maxima for 40 hues on nine value levels.*

Hue	Munsell Value																	
	9		8		7		6		5		4		3		2		1	
	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y	x	y
2.5R	0.372	0.318	0.432	0.315	0.490	0.304	0.540	0.289	0.585	0.269	0.613	0.253	0.627	0.238	0.580	0.204	0.526	0.172
5.0	.378	.326	.442	.327	.510	.322	.570	.311	.624	.294	.659	.278	.668	.259	.632	.228	.581	.198
7.5	.384	.335	.458	.344	.535	.345	.604	.336	.658	.315	.690	.294	.703	.277	.680	.251	.628	.220
10.0	.390	.344	.476	.364	.567	.374	.627	.372	.635	.364	.647	.353	.677	.322	.721	.271	.679	.244
2.5YR	.399	.358	.497	.388	.593	.407	.596	.403	.600	.400	.605	.394	.617	.382	.646	.353	.713	.287
5.0	.409	.373	.527	.422	.569	.431	.572	.427	.576	.423	.581	.419	.586	.413	.598	.402	.616	.384
7.5	.423	.393	.545	.455	.547	.452	.550	.449	.553	.446	.556	.443	.560	.439	.566	.434	.581	.418
10.0	.442	.422	.527	.472	.529	.471	.530	.468	.533	.466	.536	.463	.539	.460	.543	.456	.550	.449
2.5Y	.468	.461	.509	.490	.511	.489	.512	.487	.514	.485	.516	.483	.519	.480	.522	.477	.526	.473
5.0	.484	.510	.488	.510	.491	.508	.493	.506	.495	.504	.498	.502	.500	.500	.502	.497	.504	.495
7.5	.470	.523	.474	.526	.475	.524	.476	.523	.478	.522	.479	.520	.480	.519	.482	.517	.484	.515
10.0	.457	.537	.460	.540	.459	.539	.460	.540	.459	.540	.459	.540	.459	.540	.459	.540	.459	.540
2.5GY	.438	.555	.439	.560	.438	.561	.437	.562	.435	.563	.434	.565	.432	.567	.430	.570	.424	.575
5.0	.413	.576	.413	.586	.410	.588	.407	.591	.404	.594	.401	.597	.396	.602	.390	.607	.380	.618
7.5	.361	.603	.360	.632	.356	.640	.349	.648	.342	.655	.333	.663	.322	.673	.311	.683	.292	.701
10.0	.303	.579	.278	.686	.267	.711	.257	.726	.247	.740	.238	.747	.222	.760	.188	.785	.147	.810
2.5G	.263	.497	.202	.615	.149	.682	.105	.724	.066	.753	.042	.762	.027	.759	.019	.750	.013	.737
5.0	.244	.428	.180	.496	.129	.541	.085	.574	.047	.600	.023	.614	.012	.617	.008	.612	.006	.605
7.5	.238	.403	.175	.456	.128	.488	.086	.513	.049	.528	.027	.532	.017	.529	.014	.522	.012	.513
10.0	.232	.380	.172	.417	.129	.439	.091	.454	.057	.459	.036	.456	.028	.446	.025	.433	.024	.417
2.5BG	.229	.361	.170	.380	.130	.388	.097	.389	.068	.386	.048	.380	.040	.370	.037	.359	.037	.345
5.0	.225	.342	.168	.346	.133	.342	.104	.334	.078	.321	.062	.306	.056	.294	.053	.280	.053	.267
7.5	.221	.323	.168	.316	.136	.306	.110	.295	.086	.280	.072	.265	.065	.254	.062	.244	.063	.227
10.0	.232	.309	.168	.290	.138	.273	.116	.257	.095	.241	.082	.226	.076	.213	.073	.200	.074	.190
2.5B	.248	.302	.181	.272	.141	.246	.121	.230	.102	.212	.090	.197	.084	.185	.082	.175	.082	.166
5.0	.259	.297	.205	.264	.156	.226	.127	.202	.110	.183	.100	.170	.094	.158	.090	.149	.090	.143
7.5	.265	.295	.217	.260	.172	.222	.132	.183	.115	.164	.106	.151	.100	.141	.096	.133	.096	.127
10.0	.271	.292	.227	.257	.186	.219	.144	.177	.120	.150	.111	.137	.105	.127	.102	.119	.101	.114
2.5PB	.277	.290	.238	.254	.201	.215	.163	.173	.127	.130	.119	.117	.113	.107	.110	.099	.109	.093
5.0	.281	.288	.246	.251	.213	.212	.177	.170	.140	.122	.127	.100	.121	.087	.119	.078	.119	.071
7.5	.286	.286	.258	.247	.230	.207	.202	.166	.177	.118	.164	.078	.160	.046	.162	.026	.168	.013
10.0	.290	.284	.268	.244	.245	.204	.224	.161	.205	.115	.195	.076	.191	.048	.191	.032	.192	.022
2.5P	.295	.283	.277	.241	.261	.200	.247	.157	.234	.112	.226	.075	.223	.053	.222	.040	.225	.035
5.0	.298	.281	.287	.238	.277	.196	.268	.152	.261	.109	.257	.079	.255	.062	.256	.052	.259	.048
7.5	.312	.275	.312	.230	.309	.187	.305	.146	.301	.108	.296	.088	.292	.075	.288	.065	.283	.059
10.0	.325	.273	.336	.226	.343	.186	.347	.154	.250	.126	.344	.108	.335	.092	.323	.081	.306	.070
2.5RP	.340	.282	.366	.243	.383	.211	.396	.183	.405	.158	.406	.141	.403	.126	.380	.108	.337	.083
5.0	.352	.294	.390	.268	.423	.242	.447	.220	.469	.197	.472	.176	.461	.155	.434	.133	.383	.105
7.5	.360	.302	.404	.284	.446	.263	.479	.243	.509	.222	.522	.203	.519	.185	.478	.154	.431	.128
10.0	.367	.311	.419	.301	.471	.286	.514	.269	.551	.248	.571	.230	.579	.215	.526	.178	.470	.146

* The figures for these limit colors were obtained from a diagram supplied by Dr. MacAdam (22). They are approximations which depend upon the accuracy with which it was possible to interpolate and read curves representing Munsell values 1/ through 9/.

an admixture of a slight degree of rod vision. The Munsell samples, on the other hand, have been observed under a degree of light adaptation insuring a greater approach to pure cone vision, but with fields so greatly exceeding two degrees that the macular pigment probably exerted little influence. Perhaps these differences in observing conditions account for the peculiarity in the purple-blue region. Since definite justification for a sudden transition is lacking, the curves were not altered as radically as they might otherwise have been.

Hue Adjustments

Originally it was believed that the chromatic-value charts would also simplify the smoothing of the constant-hue lines by permitting them to be drawn with a straightedge. The number of irregularities to be contended with, however, soon made it apparent that the simplest thing to do was to smooth directly in the I.C.I. (x, y)-diagram. Accordingly, the visual estimates for the 20 principal hues, corresponding to the 1929 Munsell samples, were plotted in vector arrow notation with respect to both the National Bureau of Standards and the Glenn-Killian points; and then tentative loci of constant hue were drawn in for each value level.

An attempt was made in the first smoothing to hold to lines of constant dominant wave-length, but degrees of curvature which could not be ignored were soon apparent in some hue lines. When the curved smoothed lines of hue for separate value levels were put together, a picture of fairly regular progression emerged (Fig. 13). In numerous instances it was necessary to extrapolate the hue lines far beyond the Munsell data to reach the theoretical pigment limit. One working rule was to carry to the limit the trend of the curve which seemed best to fit the data. Another rule was to err in the direction of straightness rather than of curvature. Of course, the loci for a given hue on different value levels had to be smoothed and adjusted to provide smooth inter-value-level transitions. Tracings of the several loci for a given hue were compared and adjusted, after which the smoother reviewed the arrangement at each value level. Thus, as in the chroma smoothing, by reverting back and forth from the intra-value to the inter-value

operation, discrepancies were progressively reduced until the optimal hue lines were eventually approximated.

In certain extended regions beyond the Munsell data, the problem of determining the exact courses of the hue loci is formidable. In some instances, fortunately, the results of other studies were available to supplement the visual estimates, and proved helpful in reaching or confirming a decision. In spite of our practical precept favoring straightness, observations of strong colors by Judd (17), and by Kelly and Judd (20) made it clear that a number of our provisional curved loci should be increased in curvature toward their extremes. In particular, the PB line was kept nearly straight while the 7.5PB line was altered from nearly straight to considerable curvature toward its limit on the basis of Judd's previous data and check observations by Judd, Nickerson, and Newhall. The greatest curvature occurs immediately following the PB, and is not shown since it lies between the PB and 7.5PB lines. Hue lines between 7.5PB and 5.0P were adjusted toward their ends to conform with a curvature gradient decreasing toward P, as observed by Kelly and Judd. Their observations are also responsible for increased curvature of the line ending at 620 $m\mu$ on the spectrum locus. This line represents a local curvature maximum, the loci on either side being altered slightly to conform to a progressive change in curve.

There is also older evidence that the loci of constant hue cannot be expected to coincide with those of dominant wave-length, even when luminance is constant. This question has been considered by Müller (33), Abney (1), Schrödinger (34), and Judd (18). Hue appears to be an imperfectly known function of purity when luminance and dominant wave-length are constant. Around the spectrum locus the effect seems to be in different directions in different regions, with several hues invariable, or nearly invariable in this regard. In Fig. 13 an invariable (straight line) at 10Y and another between 5P and 7.5P may be noted.

The recommended hue loci also seem to be affected by the well-established Bezold-Brücke phenomenon (5), (6), (14), (35), (32), that is, the hue shift with luminance, apart from purity and

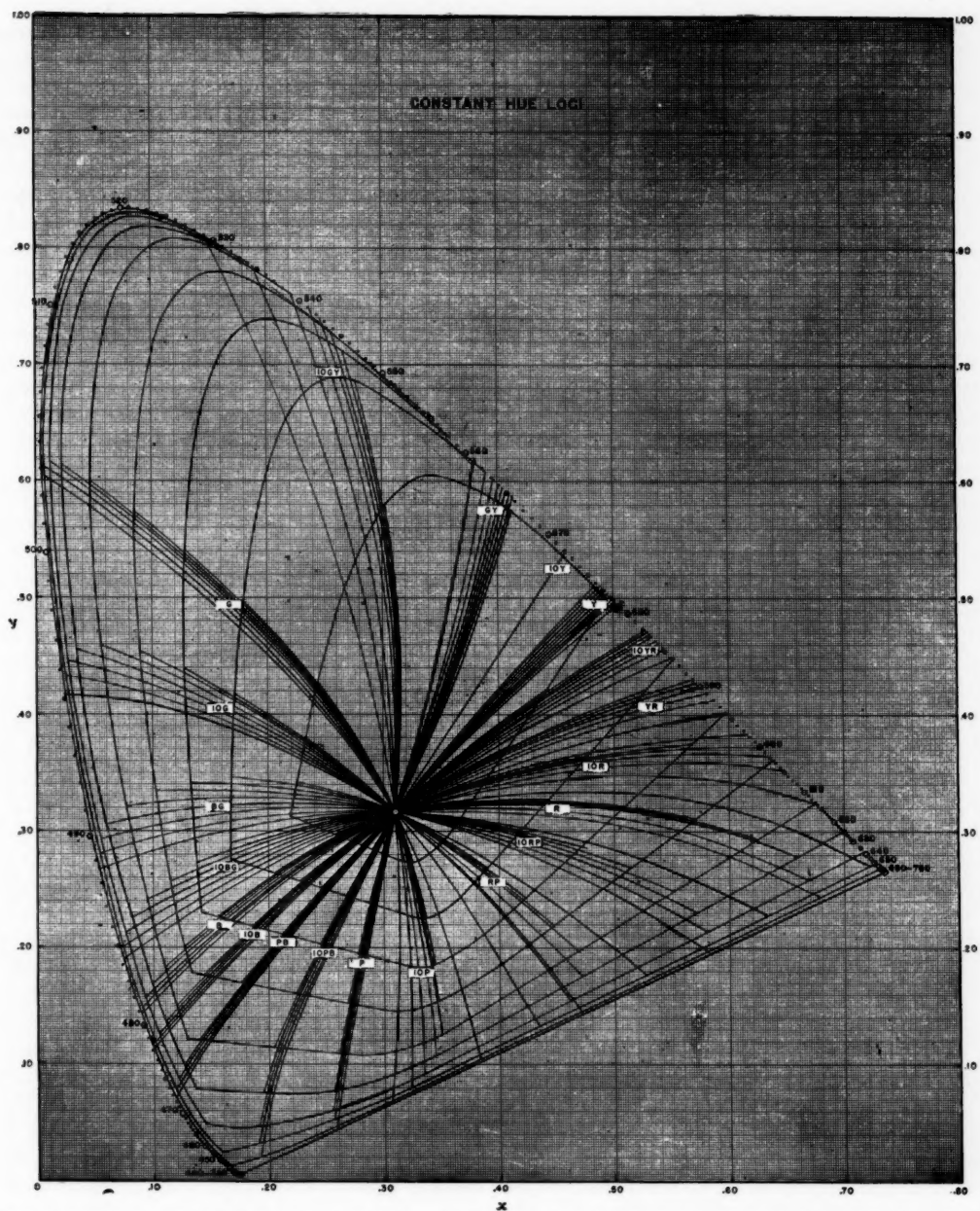


FIG. 13. Master hue chart in the I.C.I. standard coordinate system showing the recommended loci of constant hue for the 20 standard hues at value levels 1/ through 9/.

wave-length. Reference to Fig. 13 shows that the loci representing the same hue at different values are in some regions much more closely grouped than in others. The 10Y line, for example, is

nearly the same at all value levels. This agrees with findings of Purdy (32) and of Exner (7) in their investigations of the Bezold-Brücke effect. Figure 13 also suggests invariables of this type at

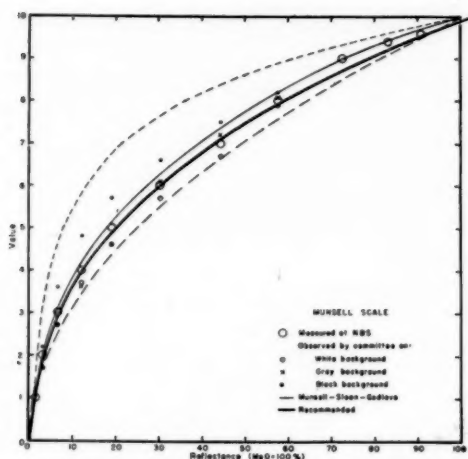


FIG. 14. Munsell value (*Book of Color* samples) as a function of reflectance. This figure shows the curve of the recommended value scale (heavy line) in comparison with the Munsell-Sloan-Godlove value function (fine line); and also with the subcommittee's observations on white (open circles), on gray (crosses), and on black (closed circles) grounds. The large open circles indicate National Bureau of Standards measurements of the samples. Nearly all of these results are seen to fall within the limits of $R = V^2$ (lower dashed curve) and $R = k \text{ anti-log } V$ (upper dashed curve). Note: The three solid dots which appear below the heavy line should be open circles with crosses in the center.

5PB; between 5P and 7.5P; and near 5G, probably toward 10GY. The averages of these hue lines cut the spectrum locus at 572.2, 505, 473.5 $m\mu$, and the purples at 559 ϵ . Purdy reported invariables at 571, 506, and 474 $m\mu$ and Exner at 577, 508, and 475 $m\mu$. Evidence of this changing relation between hue and dominant wave-length is found in the earliest Munsell papers [(8), Fig. 5], and the observations on which this report is based (28) emphasize it.

As a precautionary measure, it seems well to emphasize the fact that the establishment of standard hue loci was a difficult problem. Considerable judgment and inference were necessarily relied upon, and the complete result is not to be regarded as more than a first approximation to uniform hue spacing. The problem was especially difficult at the 1/ and the 9/ value levels to which it seemed very desirable to try to extrapolate but at which there were no chromatic Munsell samples. Such extrapolation is hazardous and tentative as sudden changes may readily occur in these extreme regions of the solid; however, it seemed best to make a beginning and thus provide some basis for future refinement.

After the 20 principal hue lines had been established at all value levels, the final step of drawing in 20 more intermediate lines to correspond approximately to the recently released third intermediate hues was a simple one. The latter 20 were drawn in simply to fit into the sequences of the original 20 which are based upon the visual estimates of the 1929 samples. The interpolated 20 fit the corresponding data fairly well. This latter group of hue lines was plotted in a figure—not shown—similar to Fig. 13. The entries in Table I were read from large master charts on which the extrapolated hue and chroma lines had been carefully traced. Then check readings were made from the originals of the charts shown in Figs. 1–9. The entries were read from the original penciled charts before inking.

The tables and charts of the chroma and hue loci were worked out so that they would be correct for the new value-reflectance relations given in Table II. The procedure for determining the latter is described in the next section.

Value Adjustments

The hue and chroma adjustments were made on the basis of visual estimates which had been averaged for all three observing grounds. This average was taken because under our conditions of observation the influence of background reflectance on hue and saturation comparisons was neither systematic nor dependable, and is therefore to be regarded as insignificant. The influence of background reflectance on value estimates, however, was found to be significant. The general nature of this effect is evident from intercomparison of the three curves in Fig. 14 which correspond to the observations on the white, gray, and black grounds. In some of the more extreme cases encountered in practice it will be worth while to make an adjustment for this effect of simultaneous contrast, and this can be done by reference to the corresponding graph. In general and for intermediate reflectances, however, it seemed desirable to standardize on a single value function suitable for use with a light ground, otherwise complications would arise in the hue and chroma dimensions. This decision was supported further by the discovery that only the function for the black background was greatly out of line.

The value adjustments were made on the neutral or near-neutral samples with the assumption that a constant value-reflectance (V to Y) relation holds for all colors regardless of chroma.

The heavy curve in Fig. 14 represents the recommended value function, while the other curves have been at some time or for some reason considered indicative of the relation between reflectance and value. It should be noted that the Munsell-Sloan-Godlove scale, which is represented by the finer line, is not far from the curve of the recommended value scale. A double adjustment was made, the nature of which deserves some explanation.

The recent National Bureau of Standards (21) measurements of the neutral samples indicate reflectances higher by 6 percent or more than the averages of Munsell-Sloan-Godlove. This considerable discrepancy may be due in part to the use of different reflectance standards but is not yet completely explained. Investigation has revealed that it was not due to failure by the painter of the samples to reproduce to a narrow tolerance the specifications furnished him. The indicated double adjustment consisted in (a) increasing the reflectances reported by Munsell-Sloan-Godlove by 6 percent for values 2/ to 8/, inclusive, and (b) making the reflectance scale relative to magnesium oxide taken as 97.5 percent (26). This adjustment amounts to multiplying the Munsell-Sloan-Godlove reflectances from 0/ to 9/ by 1.0871 and then smoothing to 10/ which is set at 102.56 percent in order that value 10/ be equivalent to 100 percent absolute reflectance. On such a scale Y values, in terms of MgO at 100 percent, may be read directly.

Despite these adjustments and its superficially smooth appearance a curve drawn through these points was found still to contain a number of inflections. By trial and error, a quintic parabola was found which fits closely the adjusted Munsell-Sloan-Godlove reflectances and has but one trivial inflection. This equation is:

$$R_Y = 1.2219V - 0.23111V^2 + 0.23951V^3 \\ - 0.021009V^4 + 0.0008404V^5.$$

This formula was employed in computing the various reflectances in Table II which presents I.C.I. Y (or percent reflectance relative to magnesium oxide) as a function of value.

SUMMARY

A psychophysical system of surface colors has been developed from the extended observations by numerous observers of the *Munsell Book of Color* samples. This system is aimed toward the double ideal of practicability and perceptual uniformity. The necessity of considerable reliance on color judgment, the scattered data, and extrapolation make it clear that this system is to be regarded only as an approximation to the ideal.

The visual conditions appropriate to the employment of the system are evident from the procedure followed in taking the basic data. The observers made their color comparisons by looking at groups of related samples on the Munsell type of constant hue and constant value charts. Thus, at the time of an observation, the observer's eyes were adapted to the chart as a whole rather than to, for example, I.C.I. Illuminant C . This is the usual situation in the visual specification of a color sample by reference to a standard chart, a type of situation which has been discussed by Helmholtz (11), Helson (12), and Judd (18).

During the experimental investigation of the subcommittee, no simultaneous comparisons were made of samples on backgrounds of different reflectance. White, gray, and black grounds were used at different times, but a single ground was always used in observations of a given set of samples. This uniformity of background is, also, a fairly usual situation for color comparisons. The separate use of the several achromatic grounds explains the lack of influence of ground evident in the hue and saturation estimates of our observers. The striking effects of ground under other viewing conditions (18), (12), (13), were absent here, presumably because of the relativity of the judgments and the tendency toward constancy from adaptation (19). Lightness, of course, was significantly affected by ground in our work, for the comparison of lightnesses always included the achromatic ground itself. Even here most of the effect was due to the black ground while the white and the gray were in fair agreement.

The question whether to make the system right for trained or untrained observers was raised in the preliminary report. The possibility of significant differences in the dimensional relations reported by visual color experts as compared with others seemed worthy of consideration. It

was felt in particular that inexperienced observers either might not notice or be reluctant to indicate significant points and might possibly, therefore, mask more valid indications of experts. To check this matter, the data from several visual color experts who participated in the preliminary study were analyzed and summarized separately. Comparison with the results from the main group showed no systematic trends which could justify the fractionation of the results in the final report.

The point of view of the subcommittee has changed considerably during the course of more than five years' work on its problem. The problem now seems more complicated than at first; and it may be that greater compromises with the ideal of perceptual uniformity have been made in order to secure a workable system than was anticipated.

The specific recommendations of the subcommittee are presented in the form of standard tables and charts (Tables I and II, Figs. 1-9), defining the new loci for Munsell hue, chroma, and value in terms of the I.C.I. system. It is expected that these forms will prove useful until such time as the whole problem may be vigorously reinvestigated and a closer approximation toward the double ideal realized.

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A Psychological Color Solid*

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VARIOUS geometrical solids have been designed in an attempt to describe the color space of normal human perception. Such solids, it should be emphasized, are concerned exclusively with the conscious color responses of the organism and have nothing to do with the stimuli except insofar as psychophysical equivalents may prove useful for standardization or conversion purposes.

The most familiar and promising procedure has been to represent the principal dimensions of perceived color by the coordinate axes of a cylindrical system in which lightness is indicated by altitude on the central axis, hue by angle about the axis, and saturation by distance from the axis (1)-(3).†

The ideal psychological solid in cylindrical coordinates would fulfill the following requirements: The dimensional scales would be calibrated in perceptually uniform steps; the units of the several scales would be equated; the surface of the solid would represent all colors of maximum saturation; the volume would be representative of all colors which are perceptibly different; the conditions of stimulation or viewing would be prescribed; and finally, the scales would be standardized in terms of a generally recognized psychophysical system.

In the preparation of a report on the smoothing of the Munsell colors (4), (5), data became available which permit, for the first time, an approximate fulfillment of all of these requirements. By reference to Adams' plots of "chromatic value" (6) and MacAdam's theoretical pigment limits (7), it was possible to lay down loci for constant chromas from zero to maximum. Table I presents (to the nearest half step) the maximum Munsell chromas corresponding to nine equispaced value levels and 40 equi-spaced hues. These figures serve to define the surface of the new solid.

Two models have been constructed, one to portray the proportions of a solid when the lightness and saturation dimensions have been equated at a supraliminal level of color difference, and the other when they have been equated at the liminal level. Thus the relatively short model, Fig. 1a, represents color as perceived under more or less usual conditions when no special tax is imposed upon the discriminatory power of the normal observer; the proportions are about right for readily perceived differences of the order of a chroma or value step (δ). The taller model,

TABLE I. Chromas¹ at theoretical pigment limits for 40 hues, Munsell values 1/ through 9/.

Hue	Munsell value								
	9	8	7	6	5	4	3	2	1
2.5 R	6.5	12.0	16.0	19.5	21.0	20.0	17.5	15.0	12.0
5	6.5	11.5	16.0	19.5	21.0	20.0	17.0	14.0	11.5
7.5	6.0	11.5	16.0	19.5	21.5	20.5	17.5	14.0	11.0
10	6.0	11.5	17.0	20.0	18.5	16.5	14.5	14.0	10.5
2.5 YR	6.5	13.0	22.0	18.5	16.5	13.5	11.0	9.5	9.5
5	7.0	16.0	21.0	18.0	15.5	12.5	10.0	7.5	4.0
7.5	8.0	22.0	19.5	16.5	15.5	11.5	9.0	6.5	3.0
10	10.0	21.0	18.0	15.5	13.5	11.0	8.0	6.0	3.0
2.5 Y	13.0	20.0	17.5	15.0	13.0	10.5	8.0	5.0	3.0
5	20.0	19.5	17.0	14.5	12.5	10.0	7.5	5.0	3.0
7.5	20.0	19.0	16.5	14.0	12.0	9.5	7.0	5.0	3.0
10	19.5	19.0	16.5	14.0	12.0	9.5	7.0	5.0	3.5
2.5 GV	19.0	19.0	16.5	14.5	12.0	10.0	8.0	5.5	3.5
5	19.0	20.0	18.0	15.0	13.0	10.5	8.5	6.5	4.0
7.5	18.5	20.5	20.0	17.5	15.0	12.5	11.0	8.5	6.0
10	18.0	24.0	23.0	21.5	19.0	16.5	15.0	12.0	7.5
2.5 G	16.0	25.0	28.0	29.0	29.5	27.5	23.0	16.5	9.0
5	13.5	22.0	27.5	28.5	29.5	28.0	23.5	17.0	8.5
7.5	12.5	21.5	26.0	28.0	29.0	27.5	23.0	16.5	8.5
10	12.0	20.0	24.0	26.5	28.0	26.5	22.5	16.0	8.5
2.5 BG	11.5	19.0	22.5	24.0	23.5	24.0	21.0	15.0	8.5
5	11.0	18.0	20.5	22.0	22.0	21.0	18.0	14.0	8.0
7.5	10.0	16.5	19.0	20.0	19.5	19.0	16.5	12.5	7.5
10	7.5	16.0	17.5	18.5	17.5	17.0	14.5	11.5	7.0
2.5 B	6.0	13.0	16.5	17.5	17.0	16.0	13.5	11.0	7.0
5	5.0	10.0	15.0	16.5	16.5	15.0	13.5	10.5	8.0
7.5	4.5	9.0	13.5	17.0	17.5	16.0	13.5	11.0	8.0
10	4.0	8.0	12.0	17.0	18.0	17.0	14.0	12.0	9.0
2.5 PB	4.0	8.0	11.5	16.5	19.0	18.5	16.0	13.0	10.0
5	4.0	7.5	11.5	16.0	19.5	20.5	18.5	15.5	12.0
7.5	4.0	7.5	11.5	15.5	21.0	27.0	35.0	40.0	38.5
10	4.0	8.0	12.0	16.5	23.5	30.5	35.5	35.0	31.0
2.5 P	4.5	9.0	14.0	19.0	26.5	32.5	34.0	31.0	26.0
5	5.0	10.0	16.0	21.5	29.0	33.0	32.5	28.0	23.0
7.5	6.5	13.0	19.5	26.0	32.0	33.5	30.0	26.0	21.0
10	8.0	16.0	22.5	27.0	31.5	30.0	27.5	23.5	19.0
2.5 RP	8.0	15.0	21.0	26.0	28.0	26.5	23.0	20.0	17.5
5	7.5	13.5	19.0	22.5	24.0	23.5	21.0	18.0	15.5
7.5	7.5	12.5	18.0	21.0	23.0	22.0	19.0	17.0	14.0
10	7.0	12.0	16.5	20.0	22.0	20.5	18.0	16.0	13.0

¹ To nearest 0.5 step of chroma.

* Paper presented at the meeting of the Optical Society of America, New York, New York, March 5-6, 1943.

† Numbers in parentheses refer to literature cited.

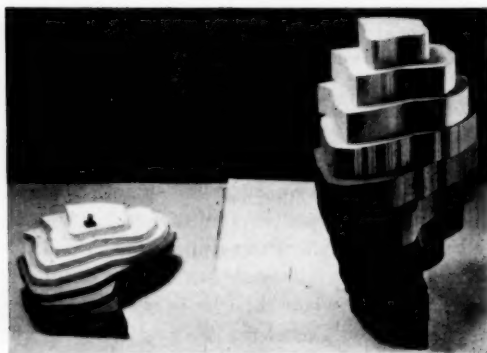


FIG. 1. Psychological color solid: (a) *Left*, for colors perceived under good visual color matching conditions such as those of a textile color matcher; (b) *Right*, for colors perceived under supraliminal conditions, as when using a good instrument.

Fig. 1b, has the same horizontal dimensions as the shorter one; but the vertical dimension has been increased by a factor of 4 to take account of the relatively greater lightness valence at the limen. Thus this model is designed to suggest the equation of the scales for the smallest, or just perceptible, color differences (9). Just why different equations should be required for perceived color steps of different orders of magnitude is still an unsettled question.

It may be noted that the conditions of viewing or method of observation were taken into account in the design of these models of a psychological, or "equal-sense-step," color solid. Much as a single standard observer with standard observing conditions is assumed for all I.C.I. diagrams, so a normal observer with a set of standard observing conditions is required for the psychological color solid.

There is an important difference between the psychological solid presented in Fig. 1 and the analogous psychophysical solid in I.C.I. color space described and illustrated by MacAdam (7). The conditions for the psychological solid must be realizable in practice because this solid by definition represents real conscious responses. The I.C.I. system, on the other hand, fulfills its valuable functions of specification and transformation without the necessity of realizing its standard observer.

Figure 2 shows horizontal sections through the solid at Munsell value levels 1/ to 9/. The

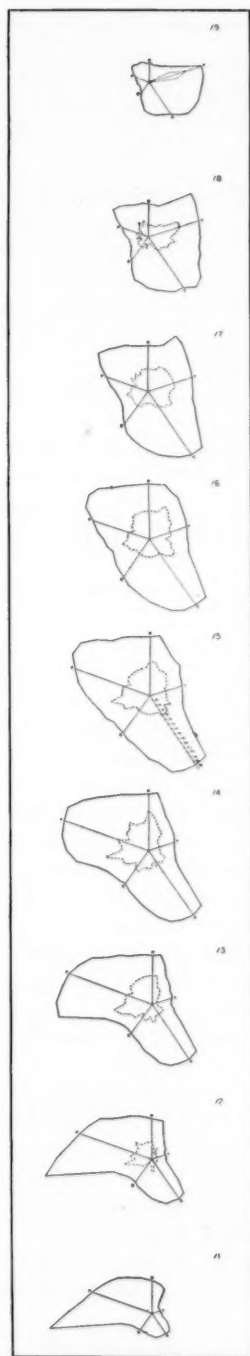


FIG. 2. Horizontal sections through the psychological color solid at Munsell values 1/ to 9/.

shapes of these sections appear strange, but those at the lower value levels make some suggestion of the shape of the plane to which Spencer (10) reduced the MacAdam data from the Nutting observations (11). Figure 3 shows five plane vertical sections spaced, roughly, according to the five principal Munsell hues and their complementaries. The dotted lines on the planes in Fig. 2 and Fig. 3 give a good idea of size and shape relative to the solid that can be constructed of available Munsell samples.

Estimates have been made of the total number of perceptibly different colors, that is, the volume of the psychological solid graduated in terms of the differential threshold or of the just noticeable difference. In general, the size of the estimate has increased with the passage of time. Titchener's figure in 1896 was about 33,000 (12) while Boring's in 1939 was 300,000 (13). Since these writers did not distinguish between solids for

surface colors and for illuminant colors, their estimates may be taken as maxima. Judd (2) recently estimated that about 10,000,000 surface colors are distinguishable in daylight by a trained observer.

The present model for liminal differences, Fig. 1b, would seem to provide a fair basis for a new estimate. Table I shows numbers that total 5836 full chroma steps for 40 hues spaced 2.5 hue steps apart, and nine values spaced one value step apart. Representative difference limen figures for chroma, hue, and value, are 0.2, 0.5, and 0.02 (9), respectively. Since these figures are in terms of the corresponding scale units: 1 chroma step \approx 5 just perceptible increments, 2.5 hue steps \approx 5 just perceptible increments, and 1 value step \approx 50 just perceptible increments. Multiplying the given number of chroma steps by these products, we have: $5836 \times 50 \times 5 \times 5 = 7,295,000$ which does not include the extreme space near 0/ and 10/ value. If this result is increased somewhat to include the extremes, and rounded to 7,500,000, we have an estimate of the number of surface-colors that may be distinguished under the best observational conditions (Fig. 1b). If this number is divided by 4, the result will be 1,875,000, which roughly corresponds to the number expected to be distinguished under the more usual observational conditions of visual color matching work (Fig. 1a).

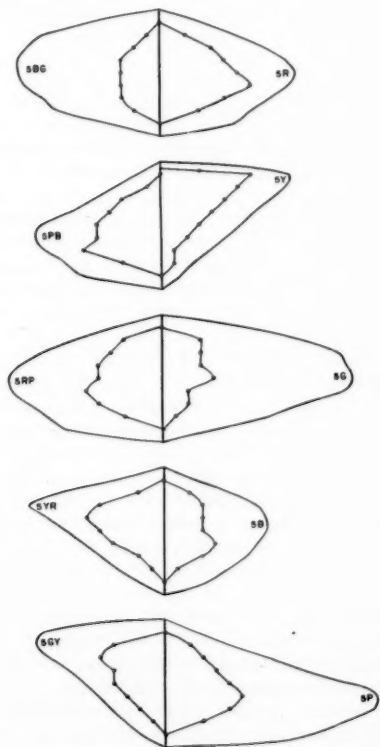


FIG. 3. Vertical sections through the psychological color solid for five hues and their complementaries.

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Necrology

Robert E. Oltman

DR. ROBERT E. OLTMAN, Chief Chemist with the Minnesota Valley Canning Company, died on July 25, 1942, at his home, 517 South Second Street, Le Sueur, Minnesota, as a result of pulmonary embolism. Dr. Oltman was born in Cleveland, Ohio, December 5, 1908, and received most of his education in the East Cleveland schools, graduating from Shaw High School. He was awarded the Bachelor of Arts degree, with major in botany, from Oberlin College in 1932. The following year he went to the University of Minnesota as a teaching assistant in plant physiology and received the Doctor of Philosophy degree there in 1936. Immediately after his graduation he entered the employ of the Minnesota Valley Canning Company and has been with that company ever since. During this time he resided in Le Sueur, with the exception of two years spent in Toronto, Canada, as Director of Research with Fine Foods of Canada, Limited.

Dr. Oltman was a member of Sigma Xi, and was a Fellow of the Canadian Institute of Chemistry and a member of the Canadian Society of Technical Agriculturists, the American Chemical Society, the American Association for the Advancement of Science, and the Optical Society of America. He leaves a wife, formerly Miss Sophia Ann Krenik of Montgomery, and a son, Eric, six years old.

—G. C. SCOTT

Carl Pfanstiehl

CARL PFANSTIEHL, Vice President and Director of Research of the Pfanstiehl Chemical Company of Waukegan, Illinois, was born in Columbia, Missouri, September 17, 1888. He was founder of the present Fansteel Metallurgical Corporation of North Chicago, Illinois. Granted well over a hundred patents, it is possible to touch only the highlights of his inventions: the first efficient "pancake" wound spark coil for gasoline engines; the process of making tungsten malleable, for the first time commercially available, and thus releasing the precious metal platinum during the World War; the first bar of tantalum made ductile by forging . . . the beginning of the tantalum industry; a means of welding tungsten to steel from which came the tungsten points used for contacts in magnetos; the single calibrated dial for radios; the development and manufacture of a line of rare chemicals, previously made only in Germany, vital in medical research and imperative in time of war; countless valuable developments in the pen field; and shortly before his

death, a completely new type of precious metal alloy now being used for phonograph needles and precision instrument parts.

His inspired and untiring pioneer work in powder metallurgy and diffusion, particularly with the rare metals, in electricity and welding techniques, in rare chemicals and the phenomenon of fluorescence, have opened unlimited and as yet untouched fields for application and development.

Mr. Pfanstiehl was a member of the American Chemical Society, the Electrochemical Society, the American Association for the Advancement of Science, the New York Academy of Science, the American Physical Society, the Optical Society of America, the American Institute of Mining and Metallurgical Engineers, and the American Society for Metals. He was a recipient of the 1940 Modern Pioneer Award for invention and discovery.

—B. G. FRANCIS

Charles W. Frederick

CHARLES W. FREDERICK, research scientist at the Hawk-Eye Works of the Eastman Kodak Company in Rochester, New York, who pioneered in the design of lenses for aerial photography and the development of a new type of optical glass, died on November 29, 1942.

Mr. Frederick had been associated with Eastman Kodak Company from 1914 to 1939 as head of the scientific and lens-designing staff of the Hawk-Eye Works. In 1939, Mr. Frederick withdrew from active industrial research, but continued as head of the research division of the Hawk-Eye scientific staff.

Mr. Frederick was born in Des Moines, Iowa, in 1870. After graduating from Kansas State University, he was for thirteen years a civilian scientist and teacher with the Navy before joining the Hawk-Eye Works. He served as a computer at the Naval Observatory in Washington and was assistant astronomer assigned to the Observatory's equatorial telescope from 1902 to 1904.

During the two years following he took part in supervising the construction of an observatory at Tutuila, Samoa. In 1906 he returned to the mainland and spent several years in research at the Washington Naval Observatory, later going to the Naval Academy at Annapolis where he taught mathematics for five years.

Mr. Frederick designed some of the first aerial lenses used for military photography in the first World War, and during the last three years has evolved several new types of lenses used in the present conflict. His study of the possibilities of non-silica glass led to the development

by Kodak researchers of the first new optical glass discovered since the 1880's, and this was subsequently adopted for manufacturing purposes by the Eastman Kodak Company.

Clarence Errol Ferree

CLARENCE ERROL FERREE was born in Sidney, Ohio, March 11, 1877. He received the degrees of B.S., M.A., and M.S. from Ohio Wesleyan University in 1900 and 1901; of Ph.D. from Cornell University in 1909; and of D.Sc. (hon.) from Ohio Wesleyan in 1938. From 1907 to 1928 he was a member of the Faculty of Bryn Mawr College, serving as Associate Professor of Experimental Psychology 1912-1917 and Professor 1917-1928. He was also Director of the Psychological Laboratory 1912-1928 and succeeded in building up a very active department of his chosen subject in those pioneer days, creating among his students a group of able and enthusiastic researchers. His early interests lay in the fields of attention, audition, and vision, but in later years he devoted himself almost entirely to the last-named field, extending his scientific studies to their applications in ophthalmology and lighting. From 1928-1935 he was Director of the Laboratory of Physiological Optics, Wilmer Ophthalmological Institute, The Johns Hopkins University School of Medicine, and held the additional title of Adjunct Professor of Physiological Optics. Forced by poor health to retire from active service in 1935, he was able to continue research, writing, and consultation work from his private laboratory. His sudden death of coronary occlusion occurred at his home on July 26, 1942. He is survived by his wife and collaborator, Dr. Gertrude Rand.

Ferree was an intensive worker, publishing more than 250 articles. He possessed a constructive and inventive mind, and it may be fairly said that his chief interest in teaching and research lay in the development of methods and the devising of apparatus to carry out these methods. In 1911, in collaboration with Gertrude Rand, he was the first to use stimuli, whose physical energy was directly measured, in the study of visual processes and the determination of sensitivities in any part of the retina. Various spectro-radiometric instruments were devised for this work and a number of quantitative studies were made under his direction using this technique. Among these instruments is a quantitative color-mixer with which 2, 3, or 4 spectrum colors can be mixed and the energy of the colors used and of the mixture can be measured. He was also one of the first to recognize the need for a systematic study of light and lighting in relation to the eye, and the first to show by test, in 1912, that one system of lighting is better than another for the eye. His many studies on lighting in relation to the comfort and hygiene of the eye culminated in the devising of a series of glareless lighting units and devices, prominent among which are the Ferree-Rand hospital ward light used in leading hospitals throughout the country, the louvered direct-indirect type of fixture in current use, and the Ferree-Rand variable illuminator. He invented also a number of optical and ophthalmological instruments. Also may be mentioned

his studies on the light and color sense, central and peripheral; normal and pathologic perimetry and scotometry; theory of flicker photometry in relation to the rise of visual sensation; the refraction of the peripheral retina; visual acuity and the construction of a standard visual acuity and astigmatism test chart for testing and rating vision; and dynamic speed of vision in testing fitness for aviation and for general and ocular fatigue—another of the researches conducted during the last war and for which the multiple-exposure tachistoscope was constructed. Ferree was the holder of 12 U. S. patents.

Ferree's work was aptly summed up in the following citation by Acting-President Edward L. Rice on the occasion of the award of the degree of Doctor of Science by Ohio Wesleyan University: "By your intensive theoretical study you have brought light into the borderland where physics, physiology, and psychology meet; by the application of your studies in practical invention you have aided oculists and opticians to bring light to defective eyesight."

—GERTRUDE K. RAND

Hans Georg Beutler

HANS GEORG BEUTLER was born in Reichenbach, Germany in 1896. He received his Ph.D. in 1922 at the University of Greifswald. From 1923 to 1933 he was associated with Dr. F. Haber at the Kaiser Wilhelm Institute of Physical Chemistry. From 1930 to 1936 he was Privat-dozent and Dozent at the University of Berlin. From 1936 to 1937 he was Research Physicist and Lecturer at the University of Michigan, and from 1937 on, Research Associate in Physics at the University of Chicago. He devoted the years from 1923 to 1927 to problems of highly diluted flames, from 1927 to 1932 to elementary processes of atoms and molecules, and, perhaps his most important work, from 1932 to 1936, to the inner spectra of atoms. While at Ryerson Laboratory he developed a generalized theory of the concave grating, a masterly and exhaustive treatment leaving little to be added in detail. He also spent a great deal of time improving the performance of the 30-foot grating spectrograph. Much other equipment at Ryerson bears the stamp of his expert direction. All his research was exhaustive in detail; he could bear with nothing short of completeness, accuracy, precision. At the time of his death he was finishing, in collaboration with R. A. Sawyer, a much needed volume on spectroscopic technique. During the short time he was with us, his comprehensive knowledge of spectroscopy was freely and courteously at the disposal of everyone. His early death is a serious loss to the field of spectroscopy. He was a member of Sigma Xi, the Optical Society of America, and a Fellow of the American Physical Society.

—GEORGE S. MONK

E. H. Anthes

E. H. ANTHES, manager of the New York Branch of the Bausch & Lomb Optical Company since 1933, died on August 3, 1942 following a short illness. He had been associated with the company for 33 years. Prior to

coming to the United States he was associate manager of the London Office. He was widely known in educational and industrial circles as an authority on the use and history of the microscope.

Alfred Nelson Finn

ALFRID NELSON FINN, Chief of the Glass Section of the National Bureau of Standards, Washington, D. C., died at the home of his brother in Lincoln, Nebraska, on September 21, 1942. Because of continued serious illness he had withdrawn from active work about one year earlier.

Mr. Finn was born in Denver, Colorado, on August 10, 1882. He attended the University of Denver where he received a bachelor's degree in chemistry and mathematics in 1909. He was Instructor in Chemistry at that university until 1911 when he received an appointment to the National Bureau of Standards.

As chemist in the Structural Materials Laboratory of the Bureau, Mr. Finn tested and analyzed cement, paints, oils, varnishes, coated metals, non-ferrous alloys, boiler waters, boiler compounds, and protective coatings for metals. He resigned from the National Bureau of Standards in 1919 to become Chief Chemist and Metallurgist for the Hydraulic Steel Company, Cleveland, Ohio. In 1920, he returned to the Bureau to assume the position he held until the time of his death.

At the beginning of the first World War this country had no satisfactory domestic source of optical glass. The resulting difficulty in producing military optical instruments focused attention upon the desirability of having a government-controlled source of supply for optical glass, and it was during Mr. Finn's tenure of office that the Glass Section of the National Bureau of Standards was expanded into a glass plant of sufficient capacity to produce an important part of the optical glass required to meet present war needs. Mr. Finn and his associates made the seventy-inch glass disk for the telescope mirror now in use at Ohio Wesleyan University, Delaware, Ohio. The annealing and cooling required more than eight months, and at the time of its production (1927-28) this disk was the largest that had been produced in this country and the second largest for the entire world. Although interested in all phases of glass technology, Mr. Finn was particularly active in improving the quality of optical glass. In this work he made a careful study of annealing procedures and of tests for freedom from strain. Under his direction, important fundamental research was done on the properties of glass, many of his later papers dealing with the relations between density, index of refraction, dispersion, and chemical composition of optical glasses. A complete list of his publications will be found in *The Bulletin of the American Ceramic Society*.¹

Mr. Finn was a member of the Optical Society of America, Washington Academy of Sciences, American Chemical Society, American Ceramic Society, American Society for Testing Materials, and American Institute of Chemists.

—I. C. GARDNER

¹ Bull. Am. Ceram. Soc. 21, 299-300 (1942).

Orrin W. Pineo

ORRIN W. PINEO, physicist, died September 5, 1942, at his home in Milo, Maine. He was born at Katahdin Iron Works, Maine, on September 28, 1908. He graduated from Massachusetts Institute of Technology with a S.B. degree in 1929. From 1929 to 1933 he worked with Professor A. C. Hardy at Massachusetts Institute of Technology on the development of an automatic recording visual range spectrophotometer which was later commercialized by the General Electric Company. During 1932-33 he held the Textile Foundation's senior fellowship. From 1933 to 1934 he worked independently on the development of automatic spectrophotometers with Adam Hilger, Ltd., in London and contributed to a book published by this company on the subject of "The Practice of Absorption Spectrophotometry."

From 1935 to 1940 he was employed by the Calco Chemical Division, American Cyanamid Company, at Bound Brook, New Jersey, where he did further work on the development of spectrophotometers, taking out many patents and publishing a paper on "Residual photometric errors in the commercial recording spectrophotometer."

During the last two years Mr. Pineo was engaged in work for the war effort, being located in Washington, D. C., and Princeton, New Jersey.

He was a member of the following scientific organizations: American Association for the Advancement of Science, Optical Society of America, American Association of Textile Colorists and Chemists, and the Society of Dyers and Colorists.

—G. L. ROYER

Harry John McNicholas

HARRY JOHN McNICHOLAS was born in 1892. He was graduated from Ripon College in 1915 with an A.B. degree. He came to the National Bureau of Standards in 1916, entering the Colorimetry Section under Irwin G. Priest. He remained in that Section until 1926, getting his M.A. degree in 1925 and his Ph.D. degree in 1926, both from Johns Hopkins University. Since 1926 he has been a member of the Photometry Section and of the pH Standards Section at the Bureau, being in this latter Section at the time of his death on July 23, 1942.

Dr. McNicholas was the author of a series of important research papers in the optical field, all published in the Bureau of Standards Journal of Research since 1928. Although he was perhaps best known for his development of the concept of apparent reflectance,¹ which is basic to present practice in the measurement of gloss and color of surfaces, Dr. McNicholas has also contributed importantly to visual and photographic spectrophotometry (RP30, RP33, and RP704), to choice of the colors of signal lights (RP956), to basic data on vegetable pigments and oils (RP337, RP815), and to the use of the diffraction method for the grading of wool and other fibers. Dr. McNicholas' work was marked throughout by care in the design of equipment, by painstaking treatment of data, and by penetrating analysis thereof.

—K. S. GIBSON

¹ Bur. Stand. J. Research, RP 3.