Think Python

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1 Preface

1.1 Chapter 0: Preface

1.1.1 The strange history of this book

(This section was written by Allen B. $Downey^{12}$)

In January 1999, I was preparing to teach an introductory programming class in Java. I had taught it three times and I was getting frustrated. The failure rate in the class was too high and, even for students who succeeded, the overall level of achievement was too low.

One of the problems I saw was the books. They were too big, with too much unnecessary detail about Java, and not enough high-level guidance about how to program. And they all suffered from the "trapdoor effect": they would start out easy, proceed gradually, and then somewhere around Chapter 5 the bottom would fall out. The students would get too much new material, too fast, and I would spend the rest of the semester picking up the pieces.

Two weeks before the first day of class, I decided to write my own book.

My goals were:

- Keep it short. It is better for students to read 10 pages than read 50 pages.
- Be careful with vocabulary. I tried to minimize the jargon and define each term at first use.
- Build gradually. To avoid trapdoors, I took the most difficult topics and split them into a series of small steps.
- Focus on programming, not the programming language. I included the minimum useful subset of Java and left out the rest.

I needed a title, so on a whim I chose How to Think Like a Computer Scientist.

My first version was rough, but it worked. Students did the reading, and they understood enough that I could spend class time on the hard topics, the interesting topics and (most important) letting the students practice.

I released the book under the GNU Free Documentation License, which allows users to copy, modify, and distribute the book.

What happened next is the cool part. Jeff Elkner, a high school teacher in Virginia, adopted my book and translated it into Python. He sent me a copy of his translation, and I had the unusual experience of learning Python by reading my own book.

 $\frac{1}{2}$

[&]quot;The strange history of this book" ^{http://www.greenteapress.com/thinkpython/html/book001. html} by Allen B. Downey

Jeff and I revised the book, incorporated a case study by Chris Meyers, and in 2001 we released *How to Think Like a Computer Scientist: Learning with Python*, also under the GNU Free Documentation License. As Green Tea Press, I published the book and started selling hard copies through Amazon.com and college book stores. Other books from Green Tea Press are available at greenteapress.com³.

In 2003, I started teaching at Olin College and I got to teach Python for the first time. The contrast with Java was striking. Students struggled less, learned more, worked on more interesting projects, and generally had a lot more fun.

Over the last five years I have continued to develop the book, correcting errors, improving some of the examples and adding material, especially exercises. In 2008 I started work on a major revision—at the same time, I was contacted by an editor at Cambridge University Press who was interested in publishing the next edition. Good timing!

The result is this book, now with the less grandiose title *Think Python*. Some of the changes are:

- I added a section about debugging at the end of each chapter. These sections present general techniques for finding and avoiding bugs, and warnings about Python pitfalls.
- I removed the material in the last few chapters about the implementation of lists and trees. I still love those topics, but I thought they were incongruent with the rest of the book.
- I added more exercises, ranging from short tests of understanding to a few substantial projects.
- I added a series of case studies—longer examples with exercises, solutions, and discussion. Some of them are based on Swampy, a suite of Python programs I wrote for use in my classes. Swampy, code examples, and some solutions are available from thinkpython.com⁴.
- I expanded the discussion of programming development plans and basic design patterns.
- The use of Python is more idiomatic. The book is still about programming, not Python, but now I think the book gets more leverage from the language.

I hope you enjoy working with this book, and that it helps you learn to program and think, at least a little bit, like a computer scientist.

Allen B. Downey

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³ http://www.greenteapress.com/

⁴ http://www.thinkpython.com

1.1.2 Acknowledgements

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1.1.3 Contributor List

More than 100 sharp-eyed and thoughtful readers have sent in suggestions and corrections over the past few years. Their contributions, and enthusiasm for this project, have been a huge help.

If you have a suggestion or correction, please send email to feedback@thinkpython.com. If I make a change based on your feedback, I will add you to the contributor list (unless you ask to be omitted).

If you include at least part of the sentence the error appears in, that makes it easy for me to search. Page and section numbers are fine, too, but not quite as easy to work with. Thanks!

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1.1.4 The further strange adventures of this book

In September of 2008, Whiteknight converted the HTML version of "Think Python" at Green Tea $Press^5$ to a Wikitext version at Wikibooks⁶. Now anyone can improve the text.

^{5 &}quot;Think Python" at Green Tea Press ^{http://thinkpython.com/}

⁶ Wikibooks: Think Python ^{http://en.wikibooks.org/wiki/Think_Python}

2 The way of the program

The goal of this book is to teach you to think like a computer scientist. This way of thinking combines some of the best features of mathematics, engineering, and natural science. Like mathematicians, computer scientists use formal languages to denote ideas (specifically computations). Like engineers, they design things, assembling components into systems and evaluating tradeoffs among alternatives. Like scientists, they observe the behavior of complex systems, form hypotheses, and test predictions.

The single most important skill for a computer scientist is **problem solving**. Problem solving means the ability to formulate problems, think creatively about solutions, and express a solution clearly and accurately. As it turns out, the process of learning to program is an excellent opportunity to practice problem-solving skills. That's why this chapter is called, "The way of the program."

On one level, you will be learning to program, a useful skill by itself. On another level, you will use programming as a means to an end. As we go along, that end will become clearer.

2.0.5 The Python programming language

The programming language you will learn is Python. Python is an example of a **high-level language**; other high-level languages you might have heard of are C, C++, Perl, and Java.

There are also **low-level languages**, sometimes referred to as "machine languages" or "assembly languages." Loosely speaking, computers can only execute programs written in low-level languages. So programs written in a high-level language have to be processed before they can run. This extra processing takes some time, which is a small disadvantage of high-level languages.

The advantages are enormous. First, it is much easier to program in a high-level language. Programs written in a high-level language take less time to write, they are shorter and easier to read, and they are more likely to be correct. Second, high-level languages are **portable**, meaning that they can run on different kinds of computers with few or no modifications. Low-level programs can run on only one kind of computer and have to be rewritten to run on another.

Due to these advantages, almost all programs are written in high-level languages. Low-level languages are used only for a few specialized applications.

Two kinds of programs process high-level languages into low-level languages: **interpreters** and **compilers**. An interpreter reads a high-level program and executes it, meaning that it does what the program says. It processes the program a little at a time, alternately reading lines and performing computations.

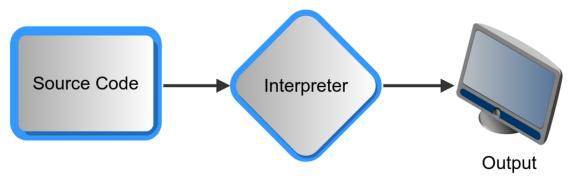


Figure 1

A compiler reads the program and translates it completely before the program starts running. In this context, the high-level program is called the **source code**, and the translated program is called the **object code** or the **executable**. Once a program is compiled, you can execute it repeatedly without further translation.

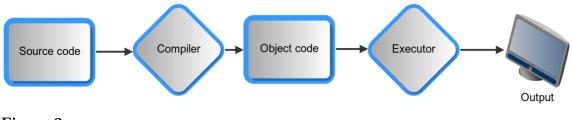


Figure 2

Python is considered an interpreted language because Python programs are executed by an interpreter. There are two ways to use the interpreter: **interactive mode** and **script mode**. In interactive mode, you type Python programs and the interpreter prints the result:

The chevron, >>>, is the **prompt** the interpreter uses to indicate that it is ready. If you type 1 + 1, the interpreter replies 2.

Alternatively, you can store code in a file and use the interpreter to execute the contents of the file, which is called a **script**. By convention, Python scripts have names that end with .py.

To execute the script, you have to tell the interpreter the name of the file. In a UNIX command window, you would type python dinsdale.py. In other development environments, the details of executing scripts are different. You can find instructions for your environment at the Python Website python.org.

Working in interactive mode is convenient for testing small pieces of code because you can type and execute them immediately. But for anything more than a few lines, you should save your code as a script so you can modify and execute it in the future.

2.0.6 What is a program?

A **program** is a sequence of instructions that specifies how to perform a computation. The computation might be something mathematical, such as solving a system of equations or finding the roots of a polynomial, but it can also be a symbolic computation, such as searching and replacing text in a document or (strangely enough) compiling a program.

The details look different in different languages, but a few basic instructions appear in just about every language: **input**: Get data from the keyboard, a file, or some other device.**output**: Display data on the screen or send data to a file or other device.**math**: Perform basic mathematical operations like addition and multiplication.**conditional execution**: Check for certain conditions and execute the appropriate sequence of statements.**repetition**: Perform some action repeatedly, usually with some variation. Believe it or not, that's pretty much all there is to it. Every program you've ever used, no matter how complicated, is made up of instructions that look pretty much like these. So you can think of programming as the process of breaking a large, complex task into smaller and smaller subtasks until the subtasks are simple enough to be performed with one of these basic instructions.

That may be a little vague, but we will come back to this topic when we talk about **algorithms**.

2.0.7 What is debugging?

Programming is error-prone. For whimsical reasons, programming errors are called **bugs** and the process of tracking them down is called **debugging**.

Three kinds of errors can occur in a program: syntax errors, runtime errors, and semantic errors. It is useful to distinguish between them in order to track them down more quickly.

Syntax errors

Python can only execute a program if the syntax is correct; otherwise, the interpreter displays an error message. **Syntax** refers to the structure of a program and the rules about that structure. For example, parentheses have to come in matching pairs, so (1 + 2) is legal, but 8) is a **syntax error**.

In English readers can tolerate most syntax errors, which is why we can read the poetry of E. E. Cummings without spewing error messages. Python is not so forgiving. If there is a single syntax error anywhere in your program, Python will display an error message and quit, and you will not be able to run your program. During the first few weeks of your programming career, you will probably spend a lot of time tracking down syntax errors. As you gain experience, you will make fewer errors and find them faster.

Runtime errors

The second type of error is a runtime error, so called because the error does not appear until after the program has started running. These errors are also called **exceptions** because they usually indicate that something exceptional (and bad) has happened.

Runtime errors are rare in the simple programs you will see in the first few chapters, so it might be a while before you encounter one.

Semantic errors

The third type of error is the **semantic error**. If there is a semantic error in your program, it will run successfully in the sense that the computer will not generate any error messages, but it will not do the right thing. It will do something else. Specifically, it will do what you told it to do.

The problem is that the program you wrote is not the program you wanted to write. The meaning of the program (its semantics) is wrong. Identifying semantic errors can be tricky because it requires you to work backward by looking at the output of the program and trying to figure out what it is doing.

Experimental debugging

One of the most important skills you will acquire is debugging. Although it can be frustrating, debugging is one of the most intellectually rich, challenging, and interesting parts of programming.

In some ways, debugging is like detective work. You are confronted with clues, and you have to infer the processes and events that led to the results you see.

Debugging is also like an experimental science. Once you have an idea about what is going wrong, you modify your program and try again. If your hypothesis was correct, then you can predict the result of the modification, and you take a step closer to a working program. If your hypothesis was wrong, you have to come up with a new one. As Sherlock Holmes pointed out, "When you have eliminated the impossible, whatever remains, however improbable, must be the truth." (A. Conan Doyle, *The Sign of Four*)

For some people, programming and debugging are the same thing. That is, programming is the process of gradually debugging a program until it does what you want. The idea is that you should start with a program that does *something* and make small modifications, debugging them as you go, so that you always have a working program.

For example, Linux is an operating system that contains thousands of lines of code, but it started out as a simple program Linus Torvalds used to explore the Intel 80386 chip. According to Larry Greenfield, "One of Linus's earlier projects was a program that would switch between printing AAAA and BBBB. This later evolved to Linux." (*The Linux Users' Guide* Beta Version 1).

Later chapters will make more suggestions about debugging and other programming practices.

2.0.8 Formal and natural languages

Natural languages are the languages people speak, such as English, Spanish, and French. They were not designed by people (although people try to impose some order on them); they evolved naturally. **Formal languages** are languages that are designed by people for specific applications. For example, the notation that mathematicians use is a formal language that is particularly good at denoting relationships among numbers and symbols. Chemists use a formal language to represent the chemical structure of molecules. And most importantly:

Programming languages are formal languages that have been designed to express computations.

Formal languages tend to have strict rules about syntax. For example, 3 + 3 = 6 is a syntactically correct mathematical statement, but 3 + = 3 \$ 6 is not. H2O is a syntactically correct chemical formula, but 2Zz is not.

Syntax rules come in two flavors, pertaining to **tokens** and structure. Tokens are the basic elements of the language, such as words, numbers, and chemical elements. One of the problems with 3 + = 3 \$ 6 is that \$ is not a legal token in mathematics (at least as far as I know). Similarly, 2Zz is not legal because there is no element with the abbreviation Zz.

The second type of syntax error pertains to the structure of a statement; that is, the way the tokens are arranged. The statement 3 + = 3 \$ 6 is illegal because even though + and = are legal tokens, you can't have one right after the other. Similarly, in a chemical formula the subscript comes after the element name, not before. **Exercise 1** Write a well-structured English sentence with invalid tokens in it. Then write another sentence with all valid tokens but with invalid structure. When you read a sentence in English or a statement in a formal language, you have to figure out what the structure of the sentence is (although in a natural language you do this subconsciously). This process is called **parsing**.

For example, when you hear the sentence, "The penny dropped," you understand that "the penny" is the subject and "dropped" is the predicate. Once you have parsed a sentence, you can figure out what it means, or the semantics of the sentence. Assuming that you know what a penny is and what it means to drop, you will understand the general implication of this sentence.

Although formal and natural languages have many features in common—tokens, structure, syntax, and semantics—there are some differences:

ambiguity: Natural languages are full of ambiguity, which people deal with by using contextual clues and other information. Formal languages are designed to be nearly or completely unambiguous, which means that any statement has exactly one meaning, regardless of context.**redundancy:** In order to make up for ambiguity and reduce misunderstandings, natural languages employ lots of redundancy. As a result, they are often verbose. Formal languages are less redundant and more concise.**literalness:** Natural languages are full of idiom and metaphor. If I say, "The penny dropped," there is probably no penny and nothing dropping¹. Formal languages mean exactly what they say. People who grow up speaking a natural language—everyone—often have a hard time adjusting to formal languages. In some ways, the difference between formal and natural language is like the difference between poetry and prose, but more so:

Poetry: Words are used for their sounds as well as for their meaning, and the whole poem together creates an effect or emotional response. Ambiguity is not only common but

¹ This idiom means that someone realized something after a period of confusion.

often deliberate.**Prose:** The literal meaning of words is more important, and the structure contributes more meaning. Prose is more amenable to analysis than poetry but still often ambiguous.**Programs:** The meaning of a computer program is unambiguous and literal, and can be understood entirely by analysis of the tokens and structure. Here are some suggestions for reading programs (and other formal languages). First, remember that formal languages are much more dense than natural languages, so it takes longer to read them. Also, the structure is very important, so it is usually not a good idea to read from top to bottom, left to right. Instead, learn to parse the program in your head, identifying the tokens and interpreting the structure. Finally, the details matter. Small errors in spelling and punctuation, which you can get away with in natural languages, can make a big difference in a formal language.

2.0.9 The first program

Traditionally, the first program you write in a new language is called "Hello, World!" because all it does is display the words, "Hello, World!" In Python, it looks like this:

print ,Hello, World!,

This is an example of a **print statement**², which doesn't actually print anything on paper. It displays a value on the screen. In this case, the result is the words

Hello, World!

The quotation marks in the program mark the beginning and end of the text to be displayed; they don't appear in the result.

Some people judge the quality of a programming language by the simplicity of the "Hello, World!" program. By this standard, Python does about as well as possible.

2.0.10 Debugging

It is a good idea to read this book in front of a computer so you can try out the examples as you go. You can run most of the examples in interactive mode, but if you put the code into a script, it is easier to try out variations.

Whenever you are experimenting with a new feature, you should try to make mistakes. For example, in the "Hello, world!" program, what happens if you leave out one of the quotation marks? What if you leave out both? What if you spell print wrong?

This kind of experiment helps you remember what you read; it also helps with debugging, because you get to know what the error messages mean. It is better to make mistakes now and on purpose than later and accidentally.

Programming, and especially debugging, sometimes brings out strong emotions. If you are struggling with a difficult bug, you might feel angry, despondent or embarrassed.

² In Python 3.0, print is a function, not a statement, so the syntax is print('Hello, World!'). We will get to functions soon!

There is evidence that people naturally respond to computers as if they were people³. When they work well, we think of them as teammates, and when they are obstinate or rude, we respond to them the same way we respond to rude, obstinate people.

Preparing for these reactions might help you deal with them. One approach is to think of the computer as an employee with certain strengths, like speed and precision, and particular weaknesses, like lack of empathy and inability to grasp the big picture.

Your job is to be a good manager: find ways to take advantage of the strengths and mitigate the weaknesses. And find ways to use your emotions to engage with the problem, without letting your reactions interfere with your ability to work effectively.

Learning to debug can be frustrating, but it is a valuable skill that is useful for many activities beyond programming. At the end of each chapter there is a debugging section, like this one, with my thoughts about debugging. I hope they help!

2.0.11 Glossary

problem solving: The process of formulating a problem, finding a solution, and expressing the solution. high-level language: A programming language like Python that is designed to be easy for humans to read and write. **low-level language:** A programming language that is designed to be easy for a computer to execute; also called "machine language" or "assembly language." **portability:** A property of a program that can run on more than one kind of computer. **interpret**: To execute a program in a high-level language by translating it one line at a time. **compile:** To translate a program written in a high-level language into a low-level language all at once, in preparation for later execution. source code: A program in a high-level language before being compiled. **object code:** The output of the compiler after it translates the program. executable: Another name for object code that is ready to be executed. **prompt**: Characters displayed by the interpreter to indicate that it is ready to take input from the user. script: A program stored in a file (usually one that will be interpreted). **interactive mode:** A way of using the Python interpreter by typing commands and expressions at the prompt. script mode: A way of using the Python interpreter to read and execute statements in a script. program: A set of instructions that specifies a computation. algorithm: A general process for solving a category of problems. bug: An error in a program. debugging: The process of finding and removing any of the three kinds of programming errors. syntax: The structure of a program. syntax error: An error in a program that makes it impossible to parse (and therefore impossible to interpret). exception: An error that is detected while the program is running. semantics: The meaning of a program. semantic error: An error in a program that makes it do something other than what the programmer intended. **natural language:** Any one of the languages that people speak that evolved naturally. formal language: Any one of the languages that people have designed for specific purposes, such as representing mathematical ideas or computer programs; all programming languages are formal languages. token: One of the basic elements of the syntactic structure of a program, analogous to a word in a natural language. **parse:** To examine a program and analyze the syntactic structure. **print**

³ See Reeves and Nass, The Media Equation: How People Treat Computers, Television, and New Media Like Real People and Places.

statement: An instruction that causes the Python interpreter to display a value on the screen.

2.0.12 Exercises

Exercise 2

Use a web browser to go to the Python website, http://python.org/. This page contains information about Python and links to Python-related pages, and it gives you the ability to search the Python documentation. For example, if you enter print in the search window, the first link that appears is the documentation of the print statement. At this point, not all of it will make sense to you, but it is good to know where it is.

Exercise 3

Start the Python interpreter and type 'help()' to start the online help utility. Or you can type help('print') to get information about the 'print' statement. If this example doesn't work, you may need to install additional Python documentation or set an environment variable; the details depend on your operating system and version of Python.

Exercise 4

Start the Python interpreter and use it as a calculator. Python's syntax for math operations is almost the same as standard mathematical notation. For example, the symbols '+', '-' and '/' denote addition, subtraction and division, as you would expect. The symbol for multiplication is '*'. If you run a 10 kilometer race in 43 minutes 30 seconds, what is your average time per mile? What is your average speed in miles per hour? (Hint: there are 1.61 kilometers in a mile).

2.1 References

3 Variables, expressions and statements

3.0.1 Values and types

A value is one of the basic things a program works with, like a letter or a number. The values we have seen so far are 1, 2, and 'Hello, World!'.

These values belong to different **types**: 2 is an integer, and 'Hello, World!' is a **string**, so-called because it contains a "string" of letters. You (and the interpreter) can identify strings because they are enclosed in quotation marks.

The print statement also works for integers.

```
>>> print 4
4
```

If you are not sure what type a value has, the interpreter can tell you.

```
>>> type(,Hello, World!,)
<type ,str,>
>>> type(17)
<type ,int,>
```

Not surprisingly, strings belong to the type str and integers belong to the type int. Less obviously, numbers with a decimal point belong to a type called float, because these numbers are represented in a format called **floating-point**.

```
>>> type(3.2)
<type _float,>
```

What about values like '17' and '3.2'? They look like numbers, but they are in quotation marks like strings.

```
>>> type(,17,)
<type ,str,>
>>> type(,3.2,)
<type ,str,>
```

They're strings.

When you type a large integer, you might be tempted to use commas between groups of three digits, as in 1,000,000. This is not a legal integer in Python, but it is legal:

>>> print 1,000,000 1 0 0

Well, that's not what we expected at all! Python interprets 1,000,000 as a comma-separated sequence of integers, which it prints with spaces between.

This is the first example we have seen of a semantic error: the code runs without producing an error message, but it doesn't do the "right" thing.

3.0.2 Variables

One of the most powerful features of a programming language is the ability to manipulate **variables**. A variable is a name that refers to a value.

An assignment statement creates new variables and gives them values:

>>> message = ,And now for something completely different,
>>> n = 17
>>> pi = 3.1415926535897931

This example makes three assignments. The first assigns a string to a new variable named message; the second gives the integer 17 to n; the third assigns the (approximate) value of π to pi.

A common way to represent variables on paper is to write the name with an arrow pointing to the variable's value. This kind of figure is called a **state diagram** because it shows what state each of the variables is in (think of it as the variable's state of mind). This diagram shows the result of the previous example:

message	\rightarrow	'And now for something completely different'
n	\rightarrow	17
pi	\rightarrow	3.1415926535897931

To display the value of a variable, you can use a print statement:

```
>>> print n
17
>>> print pi
3.14159265359
```

The type of a variable is the type of the value it refers to.

```
>>> type(message)
<type ,str,>
>>> type(n)
<type ,int,>
>>> type(pi)
<type ,float,>
```

Exercise 1

If you type an integer with a leading zero, you might get a confusing error:

Other number seem to work, but the results are bizarre:

```
>>> zipcode = 02132
>>> print zipcode
1114
```

Can you figure out what is going on? Hint: print the values 01, 010, 0100 and 01000.

3.0.3 Variable names and keywords

Programmers generally choose names for their variables that are meaningful—they document what the variable is used for.

Variable names can be arbitrarily long. They can contain both letters and numbers, but they have to begin with a letter. It is legal to use uppercase letters, but it is a good idea to begin variable names with a lowercase letter (you'll see why later).

The underscore character (_) can appear in a name. It is often used in names with multiple words, such as my_name or airspeed_of_unladen_swallow.

If you give a variable an illegal name, you get a syntax error:

```
>>> 76trombones = 'big parade'
SyntaxError: invalid syntax
>>> more@ = 1000000
SyntaxError: invalid syntax
>>> class = 'Advanced Theoretical Zymurgy'
SyntaxError: invalid syntax
```

76trombones is illegal because it does not begin with a letter. more@ is illegal because it contains an illegal character, @. But what's wrong with class?

It turns out that class is one of Python's **keywords**. The interpreter uses keywords to recognize the structure of the program, and they cannot be used as variable names.

Python has 31 keywords:

and	del	from	not	while
as	elif	global	or	with
assert	else	if	pass	yield
break	except	import	print	
class	exec	in	raise	
continue	finally	is	return	
def	for	lambda	try	

You might want to keep this list handy. If the interpreter complains about one of your variable names and you don't know why, see if it is on this list.

If you write your code in a text editor that understands Python, you may find that it makes it easy for you to spot such keyword clashes by displaying keywords in a different color to ordinary variables. This feature is called *syntax highlighting*, and most programmers find it indispensable. This book uses syntax highlighting for its example code, so in the following example: ok variable = 42 yield = 42

you can see that yield has been recognized as a keyword and not as an ordinary variable, since it is colored orange.

3.0.4 Statements

A statement is a unit of code that the Python interpreter can execute. We have seen two kinds of statements: print and assignment.

When you type a statement in interactive mode, the interpreter executes it and displays the result, if there is one.

A script usually contains a sequence of statements. If there is more than one statement, the results appear one at a time as the statements execute.

For example, the script

```
print 1
x = 2
print x
```

produces the output

1 2

The assignment statement produces no output.

3.0.5 Operators and operands

Operators are special symbols that represent computations like addition and multiplication. The values the operator is applied to are called **operands**.

The operators +, -, *, / and ** perform addition, subtraction, multiplication, division and exponentiation, as in the following examples:

20+32 hour-1 hour*60+minute minute/60 5**2 (5+9)*(15-7)

In some other languages, ^ is used for exponentiation, but in Python it is a bitwise operator called XOR. I won't cover bitwise operators in this book, but you can read about them at wiki.python.org/moin/BitwiseOperators.

The division operator might not do what you expect:

```
>>> minute = 59
>>> minute/60
0
```

The value of minute is 59, and in conventional arithmetic 59 divided by 60 is 0.98333, not 0. The reason for the discrepancy is that Python is performing **floor division**.¹

When both of the operands are integers, the result is also an integer; floor division chops off the fraction part, so in this example it rounds down to zero.

If either of the operands is a floating-point number, Python performs floating-point division, and the result is a float:

>>> minute/60.0 0.983333333333333333

3.0.6 Expressions

An **expression** is a combination of values, variables, and operators. A value all by itself is considered an expression, and so is a variable, so the following are all legal expressions (assuming that the variable x has been assigned a value):

17 x x + 17

If you type an expression in interactive mode, the interpreter **evaluates** it and displays the result:

>>> 1 + 1 2

But in a script, an expression all by itself doesn't do anything! This is a common source of confusion for beginners.

Exercise 2

Type the following statements in the Python interpreter to see what they do:

5 x = 5 x + 1

Now put the same statements into a script and run it. What is the output? Modify the script by transforming each expression into a print statement and then run it again.

3.0.7 Order of operations

When more than one operator appears in an expression, the order of evaluation depends on the **rules of precedence**. For mathematical operators, Python follows mathematical convention. The acronym **PEMDAS** is a useful way to remember the rules:

¹ In Python 3.0, the result of this division is a float. The new operator // performs integer division.

- Parentheses have the highest precedence and can be used to force an expression to evaluate in the order you want. Since expressions in parentheses are evaluated first, 2 * (3-1) is 4, and (1+1)**(5-2) is 8. You can also use parentheses to make an expression easier to read, as in (minute * 100) / 60, even if it doesn't change the result.
- Exponentiation has the next highest precedence, so $2^{**}1+1$ is 3, not 4, and $3^{*}1^{**}3$ is 3, not 27.
- Multiplication and Division have the same precedence, which is higher than Addition and Subtraction, which also have the same precedence. So 2*3-1 is 5, not 4, and 6+4/2 is 8, not 5.
- Operators with the same precedence are evaluated from left to right. So in the expression degrees / 2 * pi, the division happens first and the result is multiplied by pi. To divide by 2 π , you can reorder the operands or use parentheses.

3.0.8 String operations

In general, you cannot perform mathematical operations on strings, even if the strings look like numbers, so the following are illegal:

'2'-'1' 'eggs'/'easy' 'third'*'a charm'

The + operator works with strings, but it might not do what you expect: it performs **concatenation**, which means joining the strings by linking them end-to-end. For example:

first = 'throat'
second = 'warbler'
print first + second

The output of this program is throatwarbler.

The * operator also works on strings; it performs repetition. For example, 'Spam'*3 is 'SpamSpamSpam'. If one of the operands is a string, the other has to be an integer.

This use of + and * makes sense by analogy with addition and multiplication. Just as 4*3 is equivalent to 4+4+4, we expect 'Spam'*3 to be the same as 'Spam'+'Spam'+'Spam', and it is. On the other hand, there is a significant way in which string concatenation and repetition are different from integer addition and multiplication. Can you think of a property that addition has that string concatenation does not?

3.0.9 Comments

As programs get bigger and more complicated, they get more difficult to read. Formal languages are dense, and it is often difficult to look at a piece of code and figure out what it is doing, or why.

For this reason, it is a good idea to add notes to your programs to explain in natural language what the program is doing. These notes are called **comments**, and they start with the # symbol:

compute the percentage of the hour that has elapsed percentage = (minute * 100) / 60

In this case, the comment appears on a line by itself. You can also put comments at the end of a line:

percentage = (minute * 100) / 60 # percentage of an hour

Everything from the **#** to the end of the line is ignored—it has no effect on the program.

Comments are most useful when they document non-obvious features of the code. It is reasonable to assume that the reader can figure out *what* the code does; it is much more useful to explain *why*.

This comment is redundant with the code and useless:

This comment contains useful information that is not in the code:

v = 5 # velocity in meters/second.

Good variable names can reduce the need for comments, but long names can make complex expressions hard to read, so there is a tradeoff.

3.0.10 Debugging

At this point the syntax error you are most likely to make is an illegal variable name, like class and yield, which are keywords, or odd~job and US\$, which contain illegal characters.

If you put a space in a variable name, Python thinks it is two operands without an operator:

>>> bad name = 5 SyntaxError: invalid syntax

For syntax errors, the error messages don't help much. The most common messages are SyntaxError: invalid syntax and SyntaxError: invalid token, neither of which is very informative.

The runtime error you are most likely to make is a "use before def;" that is, trying to use a variable before you have assigned a value. This can happen if you spell a variable name wrong:

>>> principal = 327.68
>>> interest = principle * rate
NameError: name 'principle' is not defined

Variables names are case sensitive, so LaTeX is not the same as latex.

At this point the most likely cause of a semantic error is the order of operations. For example, to evaluate $1/2 \pi$, you might be tempted to write

>>> 1.0 / 2.0 * pi

But the division happens first, so you would get $\pi / 2$, which is not the same thing! There is no way for Python to know what you meant to write, so in this case you don't get an error message; you just get the wrong answer.

3.0.11 Glossary

value: One of the basic units of data, like a number or string, that a program manipulates. type: A category of values. The types we have seen so far are integers (type int), floatingpoint numbers (type float), and strings (type str). integer: A type that represents whole numbers. floating-point: A type that represents numbers with fractional parts. string: A type that represents sequences of characters. **variable:** A name that refers to a value. statement: A section of code that represents a command or action. So far, the statements we have seen are assignments and print statements. **assignment:** A statement that assigns a value to a variable. state diagram: A graphical representation of a set of variables and the values they refer to. **keyword:** A reserved word that is used by the compiler to parse a program; you cannot use keywords like if, def, and while as variable names. operator: A special symbol that represents a simple computation like addition, multiplication, or string concatenation. operand: One of the values on which an operator operates. floor division: The operation that divides two numbers and chops off the fraction part. expression: A combination of variables, operators, and values that represents a single result value. evaluate: To simplify an expression by performing the operations in order to yield a single value.rules of precedence: The set of rules governing the order in which expressions involving multiple operators and operands are evaluated.

concatenate: To join two operands end-to-end. **comment:** Information in a program that is meant for other programmers (or anyone reading the source code) and has no effect on the execution of the program.

3.0.12 Exercises

Exercise 3

Assume that we execute the following assignment statements:

```
width = 17
height = 12.0
delimiter = ...
```

For each of the following expressions, write the value of the expression and the type (of the value of the expression).

- 'width/2'
- 'width/2.0'
- 'height/3'
- '1 + 2 * 5'
- 'delimiter * 5'

Use the Python interpreter to check your answers.

Exercise 4

Practice using the Python interpreter as a calculator:

• The volume of a sphere with radius 'r' is $'4/3' \pi$ r3.

What is the volume of a sphere with radius 5? Hint: 392.6 is wrong!

• Suppose the cover price of a book is \$24.95, but bookstores get a

40% discount. Shipping costs \$3 for the first copy and 75 cents for each additional copy. What is the total wholesale cost for 60 copies?

• If I leave my house at 6:52 am and run 1 mile at an easy pace

(8:15 per mile), then 3 miles at tempo (7:12 per mile) and 1 mile at easy pace again, what time do I get home for breakfast?

3.0.13 Notes

4 Functions

4.1 Function calls

In the context of programming, a **function** is a named sequence of statements that performs a computation. When you define a function, you specify the name and the sequence of statements. Later, you can "call" the function by name. We have already seen one example of a **function call**:

>>> type(32)
<type ,int,>

The name of the function is type. The expression in parentheses is called the **argument** of the function. The result, for this function, is the type of the argument.

It is common to say that a function "takes" an argument and "returns" a result. The result is called the **return value**.

4.2 Type conversion functions

Python provides built-in functions that convert values from one type to another. The int function takes any value and converts it to an integer, if it can, or complains otherwise:

```
>>> <u>int(</u>,32,)
32
>>> <u>int(</u>,Hello,)
ValueError: invalid literal for <u>int(</u>): Hello
```

int can convert floating-point values to integers, but it doesn't round off; it chops off the fraction part:

```
>>> <u>int</u>(3.99999)
3
>>> <u>int</u>(-2.3)
-2
```

float converts integers and strings to floating-point numbers:

```
>>> float(32)
32.0
>>> float(,3.14159,)
3.14159
```

Finally, str converts its argument to a string:

>>> str(32)
,32,
>>> str(3.14159)
,3.14159,

4.3 Math functions

Python has a math module that provides most of the familiar mathematical functions. A **module** is a file that contains a collection of related functions.

Before we can use the module, we have to import it:

>>> import math

This statement creates a **module object** named math. If you print the module object, you get some information about it:

>>> print math
<module ,math, from ,/usr/lib/python2.5/lib-dynload/math.so,>

The module object contains the functions and variables defined in the module. To access one of the functions, you have to specify the name of the module and the name of the function, separated by a dot (also known as a period). This format is called **dot notation**.

```
>>> ratio = signal_power / noise_power
>>> decibels = 10 * math.log10(ratio)
>>> radians = 0.7
>>> height = math.sin(radians)
```

The first example computes the logarithm base 10 of the signal-to-noise ratio. The math module also provides a function called log that computes logarithms base e.

The second example finds the sine of radians. The name of the variable is a hint that sin and the other trigonometric functions (cos, tan, etc.) take arguments in radians. To convert from degrees to radians, divide by 360 and multiply by 2 π :

```
>>> degrees = 45
>>> radians = degrees / 360.0 * 2 * math.pi
>>> math.sin(radians)
0.707106781187
```

The expression math.pi gets the variable pi from the math module. The value of this variable is an approximation of π , accurate to about 15 digits.

If you know your trigonometry, you can check the previous result by comparing it to the square root of two divided by two:

>>> math.sqrt(2) / 2.0 0.707106781187

4.4 Composition

So far, we have looked at the elements of a program—variables, expressions, and statements—in isolation, without talking about how to combine them.

One of the most useful features of programming languages is their ability to take small building blocks and **compose** them. For example, the argument of a function can be any kind of expression, including arithmetic operators:

```
x = math.sin(degrees / 360.0 * 2 * math.pi)
```

And even function calls:

x = math.exp(math.log(x+1))

Almost anywhere you can put a value, you can put an arbitrary expression, with one exception: the left side of an assignment statement has to be a variable name. Any other expression on the left side is a syntax error.

>>> minutes = hours * 60 # right
>>> hours * 60 = minutes # wrong!
SyntaxError: can,t assign to operator

4.5 Adding new functions

So far, we have only been using the functions that come with Python, but it is also possible to add new functions. A **function definition** specifies the name of a new function and the sequence of statements that execute when the function is called.

Here is an example:

```
def print_lyrics():
    print "I,m a lumberjack, and I,m okay."
    print "I sleep all night and I work all day."
```

def is a keyword that indicates that this is a function definition. The name of the function is print_lyrics. The rules for function names are the same as for variable names: letters, numbers and some punctuation marks are legal, but the first character can't be a number. You can't use a keyword as the name of a function, and you should avoid having a variable and a function with the same name.

The empty parentheses after the name indicate that this function doesn't take any arguments.

The first line of the function definition is called the **header**; the rest is called the **body**. The header has to end with a colon and the body has to be indented. By convention, the indentation is always four spaces (see Section). The body can contain any number of statements.

The strings in the print statements are enclosed in double quotes. Single quotes and double quotes do the same thing; most people use single quotes except in cases like this where a single quote (which is also an apostrophe) appears in the string.

If you type a function definition in interactive mode, the interpreter prints ellipses (...) to let you know that the definition isn't complete:

```
>>> def print_lyrics():
... print "I,m a lumberjack, and I,m okay."
... print "I sleep all night and I work all day."
...
```

To end the function, you have to enter an empty line (this is not necessary in a script).

Defining a function creates a variable with the same name.

```
>>> print print_lyrics
<function print_lyrics at 0xb7e99e9c>
>>> print type(print_lyrics)
<type ,function,>
```

The value of print_lyrics is a function object, which has type 'function'.

The syntax for calling the new function is the same as for built-in functions:

```
>>> print_lyrics()
I,m a lumberjack, and I,m okay.
I sleep <u>all</u> night and I work <u>all</u> day.
```

Once you have defined a function, you can use it inside another function. For example, to repeat the previous refrain, we could write a function called repeat_lyrics:

```
def repeat_lyrics():
    print_lyrics()
    print_lyrics()
```

And then call repeat_lyrics:

```
>>> repeat_lyrics()
I,m a lumberjack, and I,m okay.
I sleep <u>all</u> night and I work <u>all</u> day.
I,m a lumberjack, and I,m okay.
I sleep <u>all</u> night and I work <u>all</u> day.
```

But that's not really how the song goes.

4.6 Definitions and uses

Pulling together the code fragments from the previous section, the whole program looks like this:

```
def print_lyrics():
    print "I,m a lumberjack, and I,m okay."
    print "I sleep all night and I work all day."
def repeat_lyrics():
    print_lyrics()
    repeat_lyrics()
```

This program contains two function definitions: print_lyrics and repeat_lyrics. Function definitions get executed just like other statements, but the effect is to create function objects. The statements inside the function do not get executed until the function is called, and the function definition generates no output.

As you might expect, you have to create a function before you can execute it. In other words, the function definition has to be executed before the first time it is called.

4.6.1 Exercise 1

Move the last line of this program to the top, so the function call appears before the definitions. Run the program and see what error message you get.

4.6.2 Exercise 2

Move the function call back to the bottom and move the definition of print_lyrics after the definition of repeat_lyrics. What happens when you run this program?

4.7 Flow of execution

In order to ensure that a function is defined before its first use, you have to know the order in which statements are executed, which is called the **flow of execution**.

Execution always begins at the first statement of the program. Statements are executed one at a time, in order from top to bottom.

Function definitions do not alter the flow of execution of the program, but remember that statements inside the function are not executed until the function is called.

A function call is like a detour in the flow of execution. Instead of going to the next statement, the flow jumps to the body of the function, executes all the statements there, and then comes back to pick up where it left off.

That sounds simple enough, until you remember that one function can call another. While in the middle of one function, the program might have to execute the statements in another function. But while executing that new function, the program might have to execute yet another function! Fortunately, Python is good at keeping track of where it is, so each time a function completes, the program picks up where it left off in the function that called it. When it gets to the end of the program, it terminates.

What's the moral of this sordid tale? When you read a program, you don't always want to read from top to bottom. Sometimes it makes more sense if you follow the flow of execution.

4.8 Parameters and arguments

Some of the built-in functions we have seen require arguments. For example, when you call math.sin you pass a number as an argument. Some functions take more than one argument: math.pow takes two, the base and the exponent.

Inside the function, the arguments are assigned to variables called **parameters**. Here is an example of a user-defined function that takes an argument:

```
def print_twice(bruce):
    print bruce
    print bruce
```

This function assigns the argument to a parameter named bruce. When the function is called, it prints the value of the parameter (whatever it is) twice.

This function works with any value that can be printed.

```
>>> print_twice(,Spam,)
Spam
Spam
>>> print_twice(17)
17
17
17
>>> print_twice(math.pi)
3.14159265359
3.14159265359
```

The same rules of composition that apply to built-in functions also apply to user-defined functions, so we can use any kind of expression as an argument for print_twice:

```
>>> print_twice(,Spam ,*4)
Spam Spam Spam Spam
Spam Spam Spam
>>> print_twice(math.cos(math.pi))
-1.0
-1.0
```

The argument is evaluated before the function is called, so in the examples the expressions 'Spam '*4 and math.cos(math.pi) are only evaluated once.

You can also use a variable as an argument:

>>> michael = _Eric, the half a bee.,

```
>>> print_twice(michael)
Eric, the half a bee.
Eric, the half a bee.
```

The name of the variable we pass as an argument (michael) has nothing to do with the name of the parameter (bruce). It doesn't matter what the value was called back home (in the caller); here in print_twice, we call everybody bruce.

4.9 Variables and parameters are local

When you create a variable inside a function, it is **local**, which means that it only exists inside the function. For example:

```
def cat_twice(part1, part2):
    cat = part1 + part2
    print_twice(cat)
```

This function takes two arguments, concatenates them, and prints the result twice. Here is an example that uses it:

```
>>> line1 = ,Bing tiddle ,
>>> line2 = ,tiddle bang.,
>>> cat_twice(line1, line2)
Bing tiddle tiddle bang.
Bing tiddle tiddle bang.
```

When cat_twice terminates, the variable cat is destroyed. If we try to print it, we get an exception:

>>> print cat NameError: name ,cat, is not defined

Parameters are also local. For example, outside print_twice, there is no such thing as bruce.

4.10 Stack diagrams

To keep track of which variables can be used where, it is sometimes useful to draw a **stack diagram**. Like state diagrams, stack diagrams show the value of each variable, but they also show the function each variable belongs to.

Each function is represented by a **frame**. A frame is a box with the name of a function beside it and the parameters and variables of the function inside it. The stack diagram for the previous example looks like this:

../images/3.png

Figure 3

The frames are arranged in a stack that indicates which function called which, and so on. In this example, print_twice

was called by cat_twice, and cat_twice was called by __main__, which is a special name for the topmost frame. When you create a variable outside of any function, it belongs to __main__.

Each parameter refers to the same value as its corresponding argument. So, part1 has the same value as line1, part2 has the same value as line2, and bruce has the same value as cat.

If an error occurs during a function call, Python prints the name of the function, and the name of the function that called it, and the name of the function that called *that*, all the way back to __main__.

For example, if you try to access cat from within

print_twice, you get a NameError:

```
Traceback (innermost last):
   File "test.py", line 13, in __main__
      cat_twice(line1, line2)
   File "test.py", line 5, in cat_twice
      print_twice(cat)
   File "test.py", line 9, in print_twice
      print cat
NameError: name _cat, is not defined
```

This list of functions is called a **traceback**. It tells you what program file the error occurred in, and what line, and what functions were executing at the time. It also shows the line of code that caused the error.

The order of the functions in the traceback is the same as the order of the frames in the stack diagram. The function that is currently running is at the bottom.

4.11 Fruitful functions and void functions

Some of the functions we are using, such as the math functions, yield results; for lack of a better name, I call them **fruitful** functions. **Other functions**, **like print_twice**, **perform an** action but don't return a value. They are called **void** functions.

When you call a fruitful function, you almost always want to do something with the result; for example, you might assign it to a variable or use it as part of an expression:

```
x = math.cos(radians)
golden = (math.sqrt(5) + 1) / 2
```

When you call a function in interactive mode, Python displays the result:

>>> math.sqrt(5) 2.2360679774997898

But in a script, if you call a fruitful function all by itself, the return value is lost forever!

math.sqrt(5)

This script computes the square root of 5, but since it doesn't store or display the result, it is not very useful.

Void functions might display something on the screen or have some other effect, but they don't have a return value. If you try to assign the result to a variable, you get a special value called None.

```
>>> result = print_twice(,Bing,)
Bing
Bing
>>> print result
None
```

The value None is not the same as the string 'None'. It is a special value that has its own type:

>>> print type(None)
<type ,NoneType,>

The functions we have written so far are all void. We will start writing fruitful functions in a few chapters.

4.12 Why functions?

It may not be clear why it is worth the trouble to divide a program into functions. There are several reasons:

- Creating a new function gives you an opportunity to name a group of statements, which makes your program easier to read and debug.
- Functions can make a program smaller by eliminating repetitive code. Later, if you make a change, you only have to make it in one place.
- Dividing a long program into functions allows you to debug the parts one at a time and then assemble them into a working whole.
- Well-designed functions are often useful for many programs. Once you write and debug one, you can reuse it.

4.13 Debugging

If you are using a text editor to write your scripts, you might run into problems with spaces and tabs. The best way to avoid these problems is to use spaces exclusively (no tabs). Most text editors that know about Python do this by default, but some don't.

Tabs and spaces are usually invisible, which makes them hard to debug, so try to find an editor that manages indentation for you.

Also, don't forget to save your program before you run it. Some development environments do this automatically, but some don't. In that case the program you are looking at in the text editor is not the same as the program you are running.

Debugging can take a long time if you keep running the same, incorrect, program over and over!

Make sure that the code you are looking at is the code you are running. If you're not sure, put something like print 'hello' at the beginning of the program and run it again. If you don't see hello, you're not running the right program!

4.14 Glossary

• function: A named sequence of statements that performs some

useful operation. Functions may or may not take arguments and may or may not produce a result.

• function definition: A statement that creates a new function,

specifying its name, parameters, and the statements it executes.

• function object: A value created by a function definition.

The name of the function is a variable that refers to a function object.

- header: The first line of a function definition.
- body: The sequence of statements inside a function definition.
- parameter: A name used inside a function to refer to the value

passed as an argument.

• function call: A statement that executes a function. It

consists of the function name followed by an argument list.

• argument: A value provided to a function when the function is called.

This value is assigned to the corresponding parameter in the function.

• local variable: A variable defined inside a function. A local

variable can only be used inside its function.

• return value: The result of a function. If a function call

is used as an expression, the return value is the value of the expression.

- fruitful function: A function that returns a value.
- void function: A function that doesn't return a value.
- module: A file that contains a

collection of related functions and other definitions.

• import statement: A statement that reads a module file and creates

a module object.

• module object: A value created by an import statement

that provides access to the values defined in a module.

• dot notation: The syntax for calling a function in another

module by specifying the module name followed by a dot (period) and the function name.

• composition: Using an expression as part of a larger expression,

or a statement as part of a larger statement.

• flow of execution: The order in which statements are executed during

a program run.

• stack diagram: A graphical representation of a stack of functions,

their variables, and the values they refer to.

• frame: A box in a stack diagram that represents a function call.

It contains the local variables and parameters of the function.

• traceback: A list of the functions that are executing,

printed when an exception occurs.

4.15 Exercises

4.15.1 Exercise 3

Python provides a built-in function called len that returns the length of a string, so the value of len('allen') is 5.

Write a function named *right_justify* that takes a string named s as a parameter and prints the string with enough leading spaces so that the last letter of the string is in column 70 of the display.

```
''>>> right_justify('allen')
allen
''
```

4.15.2 Exercise 4

A function object is a value you can assign to a variable or pass as an argument. For example, do_twice is a function that takes a function object as an argument and calls it twice:

''def do_twice(f): f() f()

Here's an example that uses do_twice to call a function named print_spam twice.

```
''def print_spam():
print 'spam'
```

- do_twice(print_spam)
 ''
 - 1. Type this example into a script and test it.
 - 2. Modify do_twice so that it takes two arguments, a function object and a value, and calls the function twice, passing the value as an argument.
 - 3. Write a more general version of print_spam, called print_twice, that takes a string as a parameter and prints it twice.

- 4. Use the modified version of do_twice to call print_twice twice, passing 'spam' as an argument.
- 5. Define a new function called do_four that takes a function object and a value and calls the function four times, passing the value as a parameter. There should be only two statements in the body of this function, not four.

You can see my solution at thinkpython.com/code/do_four.py.

4.15.3 Exercise 5

This exercise' **can be** done using only the statements and other features we have learned so far.

1. Write a function that draws a grid like the following:

```
1
           1
                      1
           1
           1
          +
1
           1
           1
           1
+
, ,
^{\prime }\,^{\prime }\text{Hint:} to print more than one value on a line, you can print a
 comma-separated sequence:'' ''print '+', '-' ''  ''If
 the sequence ends with a comma, Python leaves the line unfinished, so
 the value printed next appears on the same line.'' ''print
 '+', print '-' '' ' 'The output of these statements is <code>'+ -'</code>.'' ''A print statement all by itself ends the
 current line and goes to the next line.''
# ''Use the previous function to draw a similar grid with four rows
 and four columns.'
''You can see my solution at thinkpython.com/code/grid.py.''
We will see exceptions to this rule
later.
Based on an exercise in Dualline, ''Practical C Programming, Third
Edition'', O'Reilly (1997)
= Case study: interface design =
```

4.15.4 TurtleWorld

To accompany this book, I have written a suite of modules called Swampy. One of these modules is TurtleWorld, which provides a set of functions for drawing lines by steering turtles around the screen.

You can download Swampy from thinkpython.com/swampy; follow the instructions there to install Swampy on your system.

Move into the directory that contains TurtleWorld.py, create a file named polygon.py and type in the following code:

from TurtleWorld import *
world = TurtleWorld()
bob = Turtle()
print bob
wait for user()

The first line is a variation of the import statement we saw before; instead of creating a module object, it imports the functions from the module directly, so you can access them without using dot notation.

The next lines create a TurtleWorld assigned to world and a Turtle assigned to bob. Printing bob yields something like:

<TurtleWorld.Turtle instance at 0xb7bfbf4c>

This means that bob refers to an **instance** of a Turtle as defined in module TurtleWorld. In this context, "instance" means a member of a set; this Turtle is one of the set of possible Turtles.

wait_for_user tells TurtleWorld to wait for the user to do something, although in this case there's not much for the user to do except close the window.

TurtleWorld provides several turtle-steering functions: fd and bk for forward and backward, and lt and rt for left and right turns. Also, each Turtle is holding a pen, which is either down or up; if the pen is down, the Turtle leaves a trail when it moves. The functions pu and pd stand for "pen up" and "pen down."

To draw a right angle, add these lines to the program (after creating bob and before calling wait_for_user):

fd(bob, 100) rt(bob) fd(bob, 100)

The first line tells bob to take 100 steps forward. The second line tells him to turn right.

When you run this program, you should see bob move east and then south, leaving two line segments behind.

Now modify the program to draw a square. Don't turn the page until you've got it working!

4.15.5 Simple repetition

Chances are you wrote something like this (leaving out the code that creates TurtleWorld and waits for the user):

fd(bob, 100) lt(bob) fd(bob, 100) lt(bob)

```
fd(bob, 100)
lt(bob)
fd(bob, 100)
```

We can do the same thing more concisely with a for statement. Add this example to polygon.py and run it again:

for i in range(4):
 print 'Hello!'

You should see something like this:

Hello! Hello! Hello! Hello!

This is the simplest use of the for statement; we will see more later. But that should be enough to let you rewrite your square-drawing program. Don't turn the page until you do.

Here is a for statement that draws a square:

```
for i in range(4):
    fd(bob, 100)
    lt(bob)
```

The syntax of a for statement is similar to a function definition. It has a header that ends with a colon and an indented body. The body can contain any number of statements.

A for statement is sometimes called a **loop** because the flow of execution runs through the body and then loops back to the top. In this case, it runs the body four times.

This version is actually a little different from the previous square-drawing code because it makes another left turn after drawing the last side of the square. The extra turn takes a little more time, but it simplifies the code if we do the same thing every time through the loop. This version also has the effect of leaving the turtle back in the starting position, facing in the starting direction.

4.15.6 Exercises

The following is a series of exercises using TurtleWorld. They are meant to be fun, but they have a point, too. While you are working on them, think about what the point is.

The following sections have solutions to the exercises, so don't look until you have finished (or at least tried).

• Write a function called square that takes a parameter

named t, which is a turtle. It should use the turtle to draw a square. Write a function call that passes bob as an argument to square, and then run the program again.

• Add another parameter, named length, to square.

Modify the body so length of the sides is length, and then modify the function call to provide a second argument. Run the program again. Test your program with a range of values for length.

• The functions lt and rt make 90-degree turns by

default, but you can provide a second argument that specifies the number of degrees. For example, lt(bob, 45) turns bob 45 degrees to the left. Make a copy of square and change the name to polygon. Add another parameter named n and modify the body so it draws an n-sided regular polygon. Hint: The angles of an n-sided regular polygon are 360.0 / n degrees.

• Write a function called circle that takes a turtle, t,

and radius, r, as parameters and that draws an approximate circle by invoking polygon with an appropriate length and number of sides. Test your function with a range of values of r.

Hint: figure out the circumference of the circle and make sure that length * n = circumference.

Another hint: if bob is too slow for you, you can speed him up by changing bob.delay, which is the time between moves, in seconds. bob.delay = 0.01 ought to get him moving.

• Make a more general version of circle called arc

that takes an additional parameter angle, which determines what fraction of a circle to draw. angle is in units of degrees, so when angle=360, arc should draw a complete circle.

4.15.7 Encapsulation

The first exercise asks you to put your square-drawing code into a function definition and then call the function, passing the turtle as a parameter. Here is a solution:

```
def square(t):
    for i in range(4):
        fd(t, 100)
        lt(t)
```

square(bob)

The innermost statements, fd and lt are indented twice to show that they are inside the for loop, which is inside the function definition. The next line, square(bob), is flush with the left margin, so that is the end of both the for loop and the function definition.

Inside the function, t refers to the same turtle bob refers to, so lt(t) has the same effect as lt(bob). So why not call the parameter bob? The idea is that t can be any turtle, not just bob, so you could create a second turtle and pass it as an argument to square:

ray = Turtle()
square(ray)

Wrapping a piece of code up in a function is called **encapsulation**. One of the benefits of encapsulation is that it attaches a name to the code, which serves as a kind of documentation. Another advantage is that if you re-use the code, it is more concise to call a function twice than to copy and paste the body!

4.15.8 Generalization

The next step is to add a length parameter to square. Here is a solution:

```
def square(t, length):
    for i in range(4):
        fd(t, length)
        lt(t)
square(bob, 100)
```

Adding a parameter to a function is called **generalization** because it makes the function more general: in the previous version, the square is always the same size; in this version it can be any size.

The next step is also a generalization. Instead of drawing squares, polygon draws regular polygons with any number of sides. Here is a solution:

```
def polygon(t, n, length):
    angle = 360.0 / n
    for i in range(n):
        fd(t, length)
        lt(t, angle)
polygon(bob, 7, 70)
```

This draws a 7-sided polygon with side length 70. If you have more than a few numeric arguments, it is easy to forget what they are, or what order they should be in. It is legal, and sometimes helpful, to include the names of the parameters in the argument list:

polygon(bob, n=7, length=70)

These are called **keyword arguments** because they include the parameter names as "keywords" (not to be confused with Python keywords like while and def).

This syntax makes the program more readable. It is also a reminder about how arguments and parameters work: when you call a function, the arguments are assigned to the parameters.

4.15.9 Interface design

The next step is to write circle, which takes a radius, r, as a parameter. Here is a simple solution that uses polygon to draw a 50-sided polygon:

```
def circle(t, r):
    circumference = 2 * math.pi * r
    n = 50
    length = circumference / n
    polygon(t, n, length)
```

The first line computes the circumference of a circle with radius r using the formula 2 π r. Since we use math.pi, we have to import math. By convention, import statements are usually at the beginning of the script.

n is the number of line segments in our approximation of a circle, so length is the length of each segment. Thus, polygon draws a 50-sides polygon that approximates a circle with radius r.

One limitation of this solution is that n is a constant, which means that for very big circles, the line segments are too long, and for small circles, we waste time drawing very small segments. One solution would be to generalize the function by taking n as a parameter. This would give the user (whoever calls circle) more control, but the interface would be less clean.

The **interface** of a function is a summary of how it is used: what are the parameters? What does the function do? And what is the return value? An interface is "clean" if it is "as simple as possible, but not simpler. (Einstein)"

In this example, r belongs in the interface because it specifies the circle to be drawn. n is less appropriate because it pertains to the details of how the circle should be rendered.

Rather than clutter up the interface, it is better to choose an appropriate value of n depending on circumference:

```
def circle(t, r):
    circumference = 2 * math.pi * r
    n = int(circumference / 3) + 1
    length = circumference / n
    polygon(t, n, length)
```

Now the number of segments is (approximately) circumference/3, so the length of each segment is (approximately) 3, which is small enough that the circles look good, but big enough to be efficient, and appropriate for any size circle.

4.15.10 Refactoring

When I wrote circle, I was able to re-use polygon because a many-sided polygon is a good approximation of a circle. But arc is not as cooperative; we can't use polygon or circle to draw an arc.

One alternative is to start with a copy of polygon and transform it into arc. The result might look like this:

```
def arc(t, r, angle):
    arc_length = r * math.radians(angle)
    n = int(arc_length / 3) + 1
    step_length = arc_length / n
    step_angle = float(angle) / n
    for i in range(n):
        fd(t, step_length)
        lt(t, step_angle)
```

The second half of this function looks like polygon, but we can't re-use polygon without changing the interface. We could generalize polygon to take an angle as a third argument, but then polygon would no longer be an appropriate name! Instead, let's call the more general function polyline:

```
def polyline(t, n, length, angle):
    for i in range(n):
        fd(t, length)
        lt(t, angle)
```

Now we can rewrite polygon and arc to use polyline:

```
def polygon(t, n, length):
    angle = 360.0 / n
    polyline(t, n, length, angle)
def arc(t, r, angle):
    arc_length = r * math.radians(angle)
    n = int(arc_length / 3) + 1
    step_length = arc_length / n
    step_angle = float(angle) / n
    polyline(t, n, step_length, step_angle)
```

Finally, we can rewrite circle to use arc:

def circle(t, r):
 arc(t, r, 360)

This process—rearranging a program to improve function interfaces and facilitate code re-use—is called **refactoring**. In this case, we noticed that there was similar code in arc and polygon, so we "factored it out" into polyline.

If we had planned ahead, we might have written polyline first and avoided refactoring, but often you don't know enough at the beginning of a project to design all the interfaces. Once you start coding, you understand the problem better. Sometimes refactoring is a sign that you have learned something.

4.15.11 A development plan

A **development plan** is a process for writing programs. The process we used in this case study is "encapsulation and generalization." The steps of this process are:

- Start by writing a small program with no function definitions.
- Once you get the program working, encapsulate it in a function

and give it a name.

- Generalize the function by adding appropriate parameters.
- Repeat steps 1–3 until you have a set of working functions.

Copy and paste working code to avoid retyping (and re-debugging).

• Look for opportunities to improve the program by refactoring.

For example, if you have similar code in several places, consider factoring it into an appropriately general function.

This process has some drawbacks—we will see alternatives later—but it can be useful if you don't know ahead of time how to divide the program into functions. This approach lets you design as you go along.

4.15.12 docstring

A **docstring** is a string at the beginning of a function that explains the interface ("doc" is short for "documentation"). Here is an example:

```
def polyline(t, length, n, angle):
    """Draw n line segments with the given length and
    angle (in degrees) between them. t is a turtle.
    """
    for i in range(n):
        fd(t, length)
        lt(t, angle)
```

This docstring is a triple-quoted string, also known as a multiline string because the triple quotes allow the string to span more than one line.

It is terse, but it contains the essential information someone would need to use this function. It explains concisely what the function does (without getting into the details of how it does it). It explains what effect each parameter has on the behavior of the function and what type each parameter should be (if it is not obvious).

Writing this kind of documentation is an important part of interface design. A well-designed interface should be simple to explain; if you are having a hard time explaining one of your functions, that might be a sign that the interface could be improved.

4.15.13 Debugging

An interface is like a contract between a function and a caller. The caller agrees to provide certain parameters and the function agrees to do certain work.

For example, polyline requires four arguments. The first has to be a Turtle (or some other object that works with fd and lt). The second has to be a number, and it should probably be positive, although it turns out that the function works even if it isn't. The third argument should be an integer; range complains otherwise (depending on which version of Python you are running). The fourth has to be a number, which is understood to be in degrees.

These requirements are called **preconditions** because they are supposed to be true before the function starts executing. Conversely, conditions at the end of the function are **postconditions**. Postconditions include the intended effect of the function (like drawing line segments) and any side effects (like moving the Turtle or making other changes in the World).

Preconditions are the responsibility of the caller. If the caller violates a (properly documented!) precondition and the function doesn't work correctly, the bug is in the caller, not the function. However, for purposes of debugging it is often a good idea for functions to check their preconditions rather than assume they are true. If every function checks its preconditions before starting, then if something goes wrong, you will know which function to blame.

4.15.14 Glossary

instance: A member of a set. The TurtleWorld in this chapter is a member of the set of TurtleWorlds. **loop:** A part of a program that can execute repeatedly. **encapsulation:** The process of transforming a sequence of statements into a function definition. **generalization:** The process of replacing something unnecessarily specific (like a number) with something appropriately general (like a variable or parameter). **keyword argument:** An argument that includes the name of the parameter as a "keyword."

interface: A description of how to use a function, including the name and descriptions of the arguments and return value. **development plan:** A process for writing programs. **docstring:** A string that appears in a function definition to document the function's interface. **precondition:** A requirement that should be satisfied by the caller before a function starts. **postcondition:** A requirement that should be satisfied by the function before it ends.

4.15.15 Exercises

Exercise 1 Download the code in this chapter from 'thinkpython.com/code/polygon.py'.

• Write appropriate docstrings for 'polygon', 'arc' and

'circle'.

• Draw a stack diagram that shows the state of the program

while executing 'circle(bob, radius)'. You can do the arithmetic by hand or add 'print' statements to the code.

• The version of 'arc' in Section '4.7' is not

very accurate because the linear approximation of the circle is always outside the true circle. As a result, the turtle ends up a few units away from the correct destination. My solution shows a way to reduce the effect of this error. Read the code and see if it makes sense to you. If you draw a diagram, you might see how it works.

Exercise 2 Write an appropriately general set of functions that can draw flowers like this: You can download a solution from 'thinkpython.com/code/flower.py'.

Exercise 3 Write an appropriately general set of functions that can draw shapes like this: You can download a solution from 'thinkpython.com/code/pie.py'. Exercise 4 '' The letters of the alphabet can be constructed from a moderate number of basic elements, like vertical and horizontal lines and a few curves. Design a font that can be drawn with a minimal number of basic elements and then write functions that draw letters of the alphabet.

You should write one function for each letter, with names draw_a, draw_b, etc., and put your functions in a file named 'letters.py'. You can download a "turtle typewriter" from 'thinkpython.com/code/typewriter.py' to help you test your code.

You can download a solution from 'thinkpython.com/code/letters.py'.

5 Conditional and recursion

5.0.16 Modulus operator

The **modulus operator** works on integers and yields the remainder when the first operand is divided by the second. In Python, the modulus operator is a percent sign (%). The syntax is the same as for other operators:

```
>>> quotient = 7 / 3
>>> print quotient
2
>>> remainder = 7 % 3
>>> print remainder
1
```

So 7 divided by 3 is 2 with 1 left over.

The modulus operator turns out to be surprisingly useful. For example, you can check whether one number is divisible by another—if x % y is zero, then x is divisible by y.

Also, you can extract the right-most digit or digits from a number. For example, x % 10 yields the right-most digit of x (in base 10). Similarly x % 100 yields the last two digits.

5.0.17 Boolean expressions

A **boolean expression** is an expression that is either true or false. The following examples use the operator ==, which compares two operands and produces True if they are equal and False otherwise:

```
>>> 5 == 5
True
>>> 5 == 6
False
```

True and False are special values that belong to the type bool; they are not strings:

```
>>> type(True)
<type 'bool'>
>>> type(False)
<type 'bool'>
```

The == operator is one of the **comparison operators**; the others are:

Although these operations are probably familiar to you, the Python symbols are different from the mathematical symbols. A common error is to use a single equal sign (=) instead of a double equal sign (==). Remember that = is an assignment operator and == is a comparison operator. There is no such thing as =< or =>.

5.0.18 Logical operators

There are three **logical operators**: and, or, and not. The semantics (meaning) of these operators is similar to their meaning in English. For example, x > 0 and x < 10 is true only if x is greater than 0 and less than 10.

n%2 == 0 or n%3 == 0 is true if *either* of the conditions is true, that is, if the number is divisible by 2 or 3.

Finally, the not operator negates a boolean expression, so not (x > y) is true if x > y is false, that is, if x is less than or equal to y.

Strictly speaking, the operands of the logical operators should be boolean expressions, but Python is not very strict. Any nonzero number is interpreted as "true."

```
>>> 17 and True True
```

This flexibility can be useful, but there are some subtleties to it that might be confusing. You might want to avoid it (unless you know what you are doing).

5.0.19 Conditional execution

In order to write useful programs, we almost always need the ability to check conditions and change the behavior of the program accordingly. **Conditional statements** give us this ability. The simplest form is the if statement:

```
if x > 0:
    print ,x is positive,
```

The boolean expression after the if statement is called the **condition**. If it is true, then the indented statement gets executed. If not, nothing happens.

if statements have the same structure as function definitions: a header followed by an indented block. Statements like this are called **compound statements**.

There is no limit on the number of statements that can appear in the body, but there has to be at least one. Occasionally, it is useful to have a body with no statements (usually as a place keeper for code you haven't written yet). In that case, you can use the pass statement, which does nothing.

5.0.20 Alternative execution

A second form of the if statement is **alternative execution**, in which there are two possibilities and the condition determines which one gets executed. The syntax looks like this:

```
if x%2 == 0:
    print ,x is even,
else:
    print ,x is odd,
```

If the remainder when x is divided by 2 is 0, then we know that x is even, and the program displays a message to that effect. If the condition is false, the second set of statements is executed. Since the condition must be true or false, exactly one of the alternatives will be executed. The alternatives are called **branches**, because they are branches in the flow of execution.

5.0.21 Chained conditionals

Sometimes there are more than two possibilities and we need more than two branches. One way to express a computation like that is a **chained conditional**:

```
if x < y:
    print 'x is less than y'
elif x > y:
    print 'x is greater than y'
else:
    print 'x and y are equal'
```

elif is an abbreviation of "else if." Again, exactly one branch will be executed. There is no limit on the number of elif statements. If there is an else clause, it has to be at the end, but there doesn't have to be one.

```
if choice == 'a':
    draw_a()
elif choice == 'b':
    draw_b()
elif choice == 'c':
    draw_c()
```

Each condition is checked in order. If the first is false, the next is checked, and so on. If one of them is true, the corresponding branch executes, and the statement ends. Even if more than one condition is true, only the first true branch executes.

5.0.22 Nested conditionals

One conditional can also be nested within another. We could have written the trichotomy example like this:

```
if x == y:
    print 'x and y are equal'
else:
    if x < y:
        print 'x is less than y'
```

```
else:
print 'x is greater than y'
```

The outer conditional contains two branches. The first branch contains a simple statement. The second branch contains another if statement, which has two branches of its own. Those two branches are both simple statements, although they could have been conditional statements as well.

Although the indentation of the statements makes the structure apparent, **nested condi-tionals** become difficult to read very quickly. In general, it is a good idea to avoid them when you can.

Logical operators often provide a way to simplify nested conditional statements. For example, we can rewrite the following code using a single conditional:

```
if 0 < x: 
 if x < 10: 
 print 'x is a positive single-digit number.'
```

The print statement is executed only if we make it past both conditionals, so we can get the same effect with the and operator:

```
if 0 < x and x < 10: print 'x is a positive single-digit number.'
```

5.0.23 Recursion

It is legal for one function to call another; it is also legal for a function to call itself. It may not be obvious why that is a good thing, but it turns out to be one of the most magical things a program can do. For example, look at the following function:

```
def countdown(n):
    if n <= 0:
        print 'Blastoff!'
    else:
        print n
        countdown(n-1)</pre>
```

If n is 0 or negative, it outputs the word, "Blastoff!" Otherwise, it outputs n and then calls a function named countdown—itself—passing n-1 as an argument.

What happens if we call this function like this?

```
>>> countdown(3)
```

The execution of countdown begins with n=3, and since n is greater than 0, it outputs the value 3, and then calls itself...

The execution of countdown begins with n=2, and since n is greater than 0, it outputs the value 2, and then calls itself... The execution of countdown begins with n=1, and since n is greater than 0, it outputs the value 1, and then calls itself... The execution of countdown begins with n=0, and since n is not greater than 0, it outputs the word, "Blastoff!" and then returns.

The countdown that got n=1 returns.

The countdown that got n=2 returns.

The countdown that got n=3 returns.

And then you're back in <u>main</u>. So, the total output looks like this:

3 2 1 Blastoff!

A function that calls itself is **recursive**; the process is called **recursion**.

As another example, we can write a function that prints a string n times.

```
def print_n(s, n):
    if n <= 0:
        return
    print s
    print_n(s, n-1)</pre>
```

If $n \le 0$ the return statement exits the function. The flow of execution immediately returns to the caller, and the remaining lines of the function are not executed.

The rest of the function is similar to countdown: if n is greater than 0, it displays s and then calls itself to display s n-1 additional times. So the number of lines of output is 1 + (n - 1), which adds up to n.

For simple examples like this, it is probably easier to use a for loop. But we will see examples later that are hard to write with a for loop and easy to write with recursion, so it is good to start early.

5.0.24 Stack diagrams for recursive functions

In Section 3.10, we used a stack diagram to represent the state of a program during a function call. The same kind of diagram can help interpret a recursive function.

Every time a function gets called, Python creates a new function frame, which contains the function's local variables and parameters. For a recursive function, there might be more than one frame on the stack at the same time.

This figure shows a stack diagram for countdown called with n = 3:

As usual, the top of the stack is the frame for <u>main</u>. It is empty because we did not create any variables in <u>main</u> or pass any arguments to it.

The four countdown frames have different values for the parameter n. The bottom of the stack, where n=0, is called the **base case**. It does not make a recursive call, so there are no more frames.

Draw a stack diagram for print_n called with s ='Hello' and n=2.

Write a function called do_n that takes a function object and a number, n as arguments, and that calls the given function n times.

5.0.25 Infinite recursion

If a recursion never reaches a base case, it goes on making recursive calls forever, and the program never terminates. This is known as **infinite recursion**, and it is generally not a good idea. Here is a minimal program with an infinite recursion:

```
def recurse():
    recurse()
```

In most programming environments, a program with infinite recursion does not really run forever. Python reports an error message when the maximum recursion depth is reached:

This traceback is a little bigger than the one we saw in the previous chapter. When the error occurs, there are 1000 recurse frames on the stack!

5.0.26 Keyboard input

The programs we have written so far are a bit rude in the sense that they accept no input from the user. They just do the same thing every time.

Python provides a built-in function called raw_input that gets input from the keyboard¹. When this function is called, the program stops and waits for the user to type something. When the user presses Return or Enter, the program resumes and raw_input returns what the user typed as a string.

```
>>> input = raw_input()
What are you waiting for?
>>> print input
What are you waiting for?
```

Before getting input from the user, it is a good idea to print a prompt telling the user what to input. raw_input can take a prompt as an argument:

```
>>> name = raw_input('What...is your name?\n')
What...is your name?
Arthur, King of the Britons!
>>> print name
Arthur, King of the Britons!
```

The sequence \n at the end of the prompt represents a **newline**, which is a special character that causes a line break. That's why the user's input appears below the prompt.

If you expect the user to type an integer, you can try to convert the return value to int:

¹ In Python 3.0, this function is named input

```
>>> prompt = 'What...is the airspeed velocity of an unladen
swallow?\n'
>>> speed = raw_input(prompt)
What...is the airspeed velocity of an unladen swallow?
17
>>> int(speed)
17
```

But if the user types something other than a string of digits, you get an error:

```
>>> speed = raw_input(prompt)
What...is the airspeed velocity of an unladen swallow?
What do you mean, an African or a European swallow?
>>> int(speed)
ValueError: invalid literal for int()
```

We will see how to handle this kind of error later.

5.0.27 Debugging

The traceback Python displays when an error occurs contains a lot of information, but it can be overwhelming, especially when there are many frames on the stack. The most useful parts are usually:

- What kind of error it was, and
- Where it occurred.

Syntax errors are usually easy to find, but there are a few gotchas. Whitespace errors can be tricky because spaces and tabs are invisible and we are used to ignoring them.

```
>>> x = 5
>>> y = 6
File "<stdin>", line 1
y = 6
SyntaxError: invalid syntax
```

In this example, the problem is that the second line is indented by one space. But the error message points to y, which is misleading. In general, error messages indicate where the problem was discovered, but the actual error might be earlier in the code, sometimes on a previous line.

The same is true of runtime errors. Suppose you are trying to compute a signal-to-noise ratio in decibels. The formula is $SNRdb = 10 \log 10$ (Psignal / Pnoise). In Python, you might write something like this:

```
import math
signal_power = 9
noise_power = 10
ratio = signal_power / noise_power
decibels = 10 * math.log10(ratio)
print decibels
```

But when you run it, you get an error message:

```
Traceback (most recent call last):
    File "snr.py", line 5, in ?
```

```
decibels = 10 * math.log10(ratio)
OverflowError: math range error
```

The error message indicates line 5, but there is nothing wrong with that line. To find the real error, it might be useful to print the value of ratio, which turns out to be 0. The problem is in line 4, because dividing two integers does floor division. The solution is to represent signal power and noise power with floating-point values.

In general, error messages tell you where the problem was discovered, but that is often not where it was caused.

5.0.28 Glossary

modulus operator: An operator, denoted with a percent sign (%), that works on integers and yields the remainder when one number is divided by another.

boolean expression: An expression whose value is either True or False.

comparison operator: One of the operators that compares its operands: ==, !=, >, <, >=, and <=.logical operator: One of the operators that combines boolean expressions: and, or, and not.conditional statement: A statement that controls the flow of execution depending on some condition.

condition: The boolean expression in a conditional statement that determines which branch is executed. **compound statement:** A statement that consists of a header and a body. The header ends with a colon (:). The body is indented relative to the header. **body:** The sequence of statements within a compound statement. **branch:** One of the alternative sequences of statements in a conditional statement. **chained conditional:** A conditional statement with a series of alternative branches.

nested conditional: A conditional statement that appears in one of the branches of another conditional statement.

recursion: The process of calling the function that is currently executing. **base case:** A conditional branch in a recursive function that does not make a recursive call. **infinite recursion:** A function that calls itself recursively without ever reaching the base case. Eventually, an infinite recursion causes a runtime error.

5.0.29 Exercises

Exercise 1 Fermat's Last Theorem says that there are no integers 'a', 'b', and 'c' such that an + bn = cn

for any values of $\mathbf{'n'}$ greater than 2.

• Write a function named check_fermatthat takes four

parameters—'a', 'b', 'c' and 'n'—and that checks to see if Fermat's theorem holds. If 'n' is greater than 2 and it turns out to be true that a''n'' + b''n'' = c''n''' ' the program should print, "Holy smokes, Fermat was wrong!" Otherwise the program should print, "No, that doesn't work."'

• 'Write a function that prompts the user to input values

for a, b, c and n, converts them to integers, and uses "check_fermat" to check whether they violate Fermat's theorem.'

Exercise 2 If you are given three sticks, you may or may not be able to arrange them in a triangle. For example, if one of the sticks is 12 inches long and the other two are one inch long, it is clear that you will not be able to get the short sticks to meet in the middle. For any three lengths, there is a simple test to see if it is possible to form a triangle: "If any of the three lengths is greater than the sum of the other two, then you cannot form a triangle. Otherwise, you can²."

• Write a function named is_trianglethat takes three

integers as arguments, and that prints either "Yes" or "No," depending on whether you can or cannot form a triangle from sticks with the given lengths.

• Write a function that prompts the user to input three stick

lengths, converts them to integers, and uses is_triangle to check whether sticks with the given lengths can form a triangle.

The following exercises use TurtleWorld from Chapter 4:

Exercise 3 Read the following function and see if you can figure out what it does. Then run it (see the examples in Chapter '4').

```
''def draw(t, length, n):
    if n == 0:
        return
    angle = 50
    fd(t, length*n)
    lt(t, angle)
    draw(t, length, n-1)
    rt(t, 2*angle)
    draw(t, length, n-1)
    lt(t, angle)
    bk(t, length*n)
```

Exercise 4

The Koch curve is a fractal that looks something like this: To draw a Koch curve with length 'x', all you have to do is

- Draw a Koch curve with length 'x/3'.
- Turn left 60 degrees.
- Draw a Koch curve with length 'x/3'.
- Turn right 120 degrees.
- Draw a Koch curve with length 'x/3'.
- Turn left 60 degrees.
- Draw a Koch curve with length 'x/3'.

² If the sum of two lengths equals the third, they form what is called a "degenerate" triangle.

The only exception is if \mathbf{x}' is less than 3. In that case, you can just draw a straight line with length \mathbf{x}' .

• Write a function called 'koch' that takes a turtle and

a length as parameters, and that uses the turtle to draw a Koch curve with the given length.

• Write a function called 'snowflake' that draws three

Koch curves to make the outline of a snowflake. You can see my solution at 'thinkpython.com/code/koch.py'.

• The Koch curve can be generalized in several ways. See

'wikipedia.org/wiki/Koch_snowflake' for examples and implement your favorite.

5.0.30 Notes

6 Fruitful functions

6.1 Return values

Some of the built-in functions we have used, such as the math functions, produce results. Calling the function generates a value, which we usually assign to a variable or use as part of an expression.

```
e = math.exp(1.0)
height = radius * math.sin(radians)
```

All of the functions we have written so far are void; they print something or move turtles around, but their return value is None.

In this chapter, we are (finally) going to write fruitful functions. The first example is area, which returns the area of a circle with the given radius:

```
def area(radius):
    temp = math.pi * radius**2
    return temp
```

We have seen the return statement before, but in a fruitful function the return statement includes an expression. This statement means: "Return immediately from this function and use the following expression as a return value." The expression can be arbitrarily complicated, so we could have written this function more concisely:

```
def area(radius):
    return math.pi * radius**2
```

On the other hand, temporary variables like temp often make debugging easier.

Sometimes it is useful to have multiple return statements, one in each branch of a conditional:

```
def absolute_value(x):
    if x < 0:
        return -x
    else:
        return x</pre>
```

Since these return statements are in an alternative conditional, only one will be executed.

As soon as a return statement executes, the function terminates without executing any subsequent statements. Code that appears after a return statement, or any other place the flow of execution can never reach, is called **dead code**.

In a fruitful function, it is a good idea to ensure that every possible path through the program hits a return statement. For example:

```
def absolute_value(x):
    if x < 0:
        return -x
    if x > 0:
        return x
```

This function is incorrect because if x happens to be 0, neither condition is true, and the function ends without hitting a return statement. If the flow of execution gets to the end of a function, the return value is None, which is not the absolute value of 0.

>>> print absolute_value(0)
None

By the way, Python provides a built-in function called abs that computes absolute values.

6.1.1 Exercise 1

Write a 'compare' function that returns '1' if $\mathbf{x} > \mathbf{y}$ ', '0' if ' $\mathbf{x} == \mathbf{y}$ ', and '-1' if ' $\mathbf{x} < \mathbf{y}$ '.

6.2 Incremental development

As you write larger functions, you might find yourself spending more time debugging.

To deal with increasingly complex programs, you might want to try a process called **incre-mental development**. The goal of incremental development is to avoid long debugging sessions by adding and testing only a small amount of code at a time.

As an example, suppose you want to find the distance between two points, given by the coordinates (x1, y1) and (x2, y2). By the Pythagorean theorem, the distance is:

distance = $\sqrt{(x_2 - x_1)^2 + (y_2 - y_1)^2}$

The first step is to consider what a distance function should look like in Python. In other words, what are the inputs (parameters) and what is the output (return value)?

In this case, the inputs are two points, which you can represent using four numbers. The return value is the distance, which is a floating-point value.

Already you can write an outline of the function:

```
def distance(x1, y1, x2, y2):
    return 0.0
```

Obviously, this version doesn't compute distances; it always returns zero. But it is syntactically correct, and it runs, which means that you can test it before you make it more complicated.

To test the new function, call it with sample arguments:

>>> distance(1, 2, 4, 6) 0.0 I chose these values so that the horizontal distance is 3 and the vertical distance is 4; that way, the result is 5 (the hypotenuse of a 3-4-5 triangle). When testing a function, it is useful to know the right answer.

At this point we have confirmed that the function is syntactically correct, and we can start adding code to the body. A reasonable next step is to find the differences $x^2 - x^1$ and $y^2 - y^1$. The next version stores those values in temporary variables and prints them.

```
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    print _dx is,, dx
    print _dy is,, dy
    return 0.0
```

If the function is working, it should display 'dx is 3' and 'dy is 4'. If so, we know that the function is getting the right arguments and performing the first computation correctly. If not, there are only a few lines to check.

Next we compute the sum of squares of dx and dy:

```
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    dsquared = dx**2 + dy**2
    print ,dsquared is: ,, dsquared
    return 0.0
```

Again, you would run the program at this stage and check the output (which should be 25). Finally, you can use math.sqrt to compute and return the result:

```
def distance(x1, y1, x2, y2):
    dx = x2 - x1
    dy = y2 - y1
    dsquared = dx**2 + dy**2
    result = math.sqrt(dsquared)
    return result
```

If that works correctly, you are done. Otherwise, you might want to print the value of result before the return statement.

The final version of the function doesn't display anything when it runs; it only returns a value. The print statements we wrote are useful for debugging, but once you get the function working, you should remove them. Code like that is called **scaffolding** because it is helpful for building the program but is not part of the final product.

When you start out, you should add only a line or two of code at a time. As you gain more experience, you might find yourself writing and debugging bigger chunks. Either way, incremental development can save you a lot of debugging time.

The key aspects of the process are:

- Start with a working program and make small incremental changes. At any point, if there is an error, you should have a good idea where it is.
- Use temporary variables to hold intermediate values so you can display and check them.

• Once the program is working, you might want to remove some of the scaffolding or consolidate multiple statements into compound expressions, but only if it does not make the program difficult to read.

6.2.1 Exercise 2

Use incremental development to write a function called 'hypotenuse' that returns the length of the hypotenuse of a right triangle given the lengths of the two legs as arguments. Record each stage of the development process as you go.

6.3 Composition

As you should expect by now, you can call one function from within another. This ability is called **composition**.

As an example, we'll write a function that takes two points, the center of the circle and a point on the perimeter, and computes the area of the circle.

Assume that the center point is stored in the variables xc and yc, and the perimeter point is in xp and yp. The first step is to find the radius of the circle, which is the distance between the two points. We just wrote a function, distance, that does that:

radius = distance(xc, yc, xp, yp)

The next step is to find the area of a circle with that radius; we just wrote that, too:

result = area(radius)

Encapsulating these steps in a function, we get:

```
def circle_area(xc, yc, xp, yp):
    radius = distance(xc, yc, xp, yp)
    result = area(radius)
    return result
```

The temporary variables radius and result are useful for development and debugging, but once the program is working, we can make it more concise by composing the function calls:

```
def circle_area(xc, yc, xp, yp):
    return area(distance(xc, yc, xp, yp))
```

6.4 Boolean functions

Functions can return booleans, which is often convenient for hiding complicated tests inside functions. For example:

```
def is_divisible(x, y):
    if x % y == 0:
        return True
    else:
```

return False

It is common to give boolean functions names that sound like yes/no questions; is_divisible returns either True or False to indicate whether x is divisible by y.

Here is an example:

```
>>> is_divisible(6, 4)
False
>>> is_divisible(6, 3)
True
```

The result of the == operator is a boolean, so we can write the function more concisely by returning it directly:

```
def is_divisible(x, y):
    return x % y == 0
```

Boolean functions are often used in conditional statements:

```
if is_divisible(x, y):
    print 'x is divisible by y'
```

It might be tempting to write something like:

```
if is_divisible(x, y) == True:
    print 'x is divisible by y'
```

But the extra comparison is unnecessary. **Exercise 3** Write a function is_between(x, y, z) that returns 'True' if ' $x \le y \le z$ ' or 'False' otherwise.

6.5 More recursion

We have only covered a small subset of Python, but you might be interested to know that this subset is a *complete* programming language, which means that anything that can be computed can be expressed in this language. Any program ever written could be rewritten using only the language features you have learned so far (actually, you would need a few commands to control devices like the keyboard, mouse, disks, etc., but that's all).

Proving that claim is a nontrivial exercise first accomplished by Alan Turing, one of the first computer scientists (some would argue that he was a mathematician, but a lot of early computer scientists started as mathematicians). Accordingly, it is known as the Turing Thesis. For a more complete (and accurate) discussion of the Turing Thesis, I recommend Michael Sipser's book *Introduction to the* Theory of Computation.

To give you an idea of what you can do with the tools you have learned so far, we'll evaluate a few recursively defined mathematical functions. A recursive definition is similar to a circular definition, in the sense that the definition contains a reference to the thing being defined. A truly circular definition is not very useful: **frabjuous:** An adjective used to describe something that is frabjuous. If you saw that definition in the dictionary, you might be annoyed. On the other hand, if you looked up the definition of the factorial function, denoted with the symbol !, you might get something like this: $\langle TD | ALIGN=right | NOWRAP \rangle \langle TD | ALIGN=center NOWRAP \rangle \langle TD | ALIGN=left | NOWRAP \rangle | = 1 \langle TD | ALIGN=right | NOWRAP \rangle \langle TD | ALIGN=center | NOWRAP \rangle \langle TD | ALIGN=left | NOWRAP \rangle | = n (n-1)!$

This definition says that the factorial of 0 is 1, and the factorial of any other value, n, is n multiplied by the factorial of n-1.

So 3! is 3 times 2!, which is 2 times 1!, which is 1 times 0!. Putting it all together, 3! equals 3 times 2 times 1 times 1, which is 6.

If you can write a recursive definition of something, you can usually write a Python program to evaluate it. The first step is to decide what the parameters should be. In this case it should be clear that factorial takes an integer:

```
def factorial(n):
```

If the argument happens to be 0, all we have to do is return 1:

```
def factorial(n):
    if n == 0:
        return 1
```

Otherwise, and this is the interesting part, we have to make a recursive call to find the factorial of n-1 and then multiply it by n:

```
def factorial(n):
    if n == 0:
        return 1
    else:
        recurse = factorial(n-1)
        result = n * recurse
        return result
```

The flow of execution for this program is similar to the flow of countdown in Section 5.8. If we call factorial with the value 3:

Since 3 is not 0, we take the second branch and calculate the factorial of n-1...

Since 2 is not 0, we take the second branch and calculate the factorial of n-1... Since 1 is not 0, we take the second branch and calculate the factorial of n-1... Since 0 is 0, we take the first branch and return 1 without making any more recursive calls.

The return value (1) is multiplied by n, which is 1, and the result is returned.

The return value (1) is multiplied by n, which is 2, and the result is returned.

The return value (2) is multiplied by n, which is 3, and the result, 6, becomes the return value of the function call that started the whole process.

Here is what the stack diagram looks like for this sequence of function calls:

The return values are shown being passed back up the stack. In each frame, the return value is the value of result, which is the product of n and recurse.

In the last frame, the local variables recurse and result do not exist, because the branch that creates them does not execute.

6.6 Leap of faith

Following the flow of execution is one way to read programs, but it can quickly become labyrinthine. An alternative is what I call the "leap of faith." When you come to a function call, instead of following the flow of execution, you *assume* that the function works correctly and returns the right result.

In fact, you are already practicing this leap of faith when you use built-in functions. When you call math.cos or math.exp, you don't examine the bodies of those functions. You just assume that they work because the people who wrote the built-in functions were good programmers.

The same is true when you call one of your own functions. For example, in Section 6.4, we wrote a function called is_divisible that determines whether one number is divisible by another. Once we have convinced ourselves that this function is correct—by examining the code and testing—we can use the function without looking at the body again.

The same is true of recursive programs. When you get to the recursive call, instead of following the flow of execution, you should assume that the recursive call works (yields the correct result) and then ask yourself, "Assuming that I can find the factorial of n-1, can I compute the factorial of n?" In this case, it is clear that you can, by multiplying by n.

Of course, it's a bit strange to assume that the function works correctly when you haven't finished writing it, but that's why it's called a leap of faith!

6.7 One more example

After factorial, the most common example of a recursively defined mathematical function is fibonacci, which has the following definition¹: <TD ALIGN=right NOWRAP> <TD ALIGN=center NOWRAP> <TD ALIGN=left NOWRAP>fibonacci(0) = 0 <TD ALIGN=right NOWRAP> <TD ALIGN=center NOWRAP> <TD ALIGN=left NOWRAP>fibonacci(1) = 1 <TD ALIGN=right NOWRAP> <TD ALIGN=center NOWRAP> <TD ALIGN=left NOWRAP> fibonacci(n) = fibonacci(n-1) + fibonacci(n-2);

Translated into Python, it looks like this:

```
def fibonacci (n):
    if n == 0:
        return 0
    elif n == 1:
        return 1
    else:
        return fibonacci(n-1) + fibonacci(n-2)
```

¹ See wikipedia.org/wiki/Fibonacci_number.

If you try to follow the flow of execution here, even for fairly small values of n, your head explodes. But according to the leap of faith, if you assume that the two recursive calls work correctly, then it is clear that you get the right result by adding them together.

6.8 Checking types

What happens if we call factorial and give it 1.5 as an argument?

>>> factorial(1.5) RuntimeError: Maximum recursion depth exceeded

It looks like an infinite recursion. But how can that be? There is a base case—when n == 0. But if n is not an integer, we can *miss* the base case and recurse forever.

In the first recursive call, the value of n is 0.5. In the next, it is -0.5. From there, it gets smaller (more negative), but it will never be 0.

We have two choices. We can try to generalize the factorial function to work with floatingpoint numbers, or we can make factorial check the type of its argument. The first option is called the gamma function² and it's a little beyond the scope of this book. So we'll go for the second.

We can use the built-in function is instance to verify the type of the argument. While we're at it, we can also make sure the argument is positive:

```
def factorial (n):
    if not isinstance(n, int):
        print 'Factorial is only defined for integers.'
        return None
    elif n < 0:
        print 'Factorial is only defined for positive integers.'
        return None
    elif n == 0:
        return 1
    else:
        return n * factorial(n-1)</pre>
```

The first base case handles nonintegers; the second catches negative integers. In both cases, the program prints an error message and returns None to indicate that something went wrong:

```
>>> factorial('fred')
Factorial is only defined for integers.
None
>>> factorial(-2)
Factorial is only defined for positive integers.
None
```

If we get past both checks, then we know that n is a positive integer, and we can prove that the recursion terminates.

² See wikipedia.org/wiki/Gamma_function.

This program demonstrates a pattern sometimes called a **guardian**. The first two conditionals act as guardians, protecting the code that follows from values that might cause an error. The guardians make it possible to prove the correctness of the code.

6.9 Debugging

Breaking a large program into smaller functions creates natural checkpoints for debugging. If a function is not working, there are three possibilities to consider:

• There is something wrong with the arguments the function

is getting; a precondition is violated.

• There is something wrong with the function; a postcondition

is violated.

• There is something wrong with the return value or the

way it is being used.

To rule out the first possibility, you can add a print statement at the beginning of the function and display the values of the parameters (and maybe their types). Or you can write code that checks the preconditions explicitly.

If the parameters look good, add a print statement before each return statement that displays the return value. If possible, check the result by hand. Consider calling the function with values that make it easy to check the result (as in Section 6.2).

If the function seems to be working, look at the function call to make sure the return value is being used correctly (or used at all!).

Adding print statements at the beginning and end of a function can help make the flow of execution more visible. For example, here is a version of factorial with print statements:

```
def factorial(n):
    space = ' ' * (4 * n)
    print space, 'factorial', n
    if n == 0:
        print space, 'returning 1'
        return 1
    else:
        recurse = factorial(n-1)
        result = n * recurse
        print space, 'returning', result
        return result
```

space is a string of space characters that controls the indentation of the output. Here is the result of factorial(5):

```
factorial 5
factorial 4
factorial 3
factorial 2
factorial 1
factorial 0
returning 1
returning 1
```

```
returning 2
returning 6
returning 24
returning 120
```

If you are confused about the flow of execution, this kind of output can be helpful. It takes some time to develop effective scaffolding, but a little bit of scaffolding can save a lot of debugging.

6.10 Glossary

temporary variable: A variable used to store an intermediate value in a complex calculation.

dead code: Part of a program that can never be executed, often because it appears after a return statement. **None:** A special value returned by functions that have no return statement or a return statement without an argument.

incremental development: A program development plan intended to avoid debugging by adding and testing only a small amount of code at a time. scaffolding: Code that is used during program development but is not part of the final version. guardian: A programming pattern that uses a conditional statement to check for and handle circumstances that might cause an error.

6.11 Exercises

6.11.1 Exercise 4

Draw a stack diagram for the following program. What does the program print?

```
def b(z):
    prod = a(z, z)
    print z, prod
    return prod
def a(x, y):
    x = x + 1
    return x * y
def c(x, y, z):
    sum = x + y + z
    pow = b(sum)**2
    return pow
x = 1
y = x + 1
print c(x, y+3, x+y)
```

6.11.2 Exercise 5

The Ackermann function, 'A(m, n)' is defined³⁴:

6.12 Multiple assignment

As you may have discovered, it is legal to make more than one assignment to the same variable. A new assignment makes an existing variable refer to a new value (and stop referring to the old value).

bruce = 5
print bruce,
bruce = 7
print bruce

The output of this program is 5 7, because the first time bruce is printed, its value is 5, and the second time, its value is 7. The comma at the end of the first print statement suppresses the newline, which is why both outputs appear on the same line.

Here is what **multiple assignment** looks like in a state diagram:

With multiple assignment it is especially important to distinguish between an assignment operation and a statement of equality. Because Python uses the equal sign (=) for assignment, it is tempting to interpret a statement like a = b as a statement of equality. It is not!

First, equality is a symmetric relation and assignment is not. For example, in mathematics, if a = 7 then 7 = a. But in Python, the statement a = 7 is legal and 7 = a is not.

Furthermore, in mathematics, a statement of equality is either true or false, for all time. If a = b now, then a will always equal b. In Python, an assignment statement can make two variables equal, but they don't have to stay that way:

a = 5
b = a # a and b are now equal
a = 3 # a and b are no longer equal

The third line changes the value of a but does not change the value of b, so they are no longer equal.

Although multiple assignment is frequently helpful, you should use it with caution. If the values of variables change frequently, it can make the code difficult to read and debug.

6.13 Updating variables

One of the most common forms of multiple assignment is an **update**, where the new value of the variable depends on the old.

³ See

⁴ wikipedia.org/wiki/Ackermann_function

x = x+1

This means "get the current value of x, add one, and then update x with the new value."

If you try to update a variable that doesn't exist, you get an error, because Python evaluates the right side before it assigns a value to x:

```
>>> x = x+1
NameError: name 'x' is not defined
```

Before you can update a variable, you have to **initialize** it, usually with a simple assignment:

>>> x = 0 >>> x = x+1

Updating a variable by adding 1 is called an **increment**; subtracting 1 is called a **decrement**.

6.14 The while statement

Computers are often used to automate repetitive tasks. Repeating identical or similar tasks without making errors is something that computers do well and people do poorly.

We have seen two programs, countdown and print_n, that use recursion to perform repetition, which is also called **iteration**. Because iteration is so common, Python provides several language features to make it easier. One is the for statement we saw in Section 4.2. We'll get back to that later.

Another is the while statement. Here is a version of countdown that uses a while statement:

```
def countdown(n):
    while n > 0:
        print n
        n = n-1
    print 'Blastoff!'
```

You can almost read the while statement as if it were English. It means, "While n is greater than 0, display the value of n and then reduce the value of n by 1. When you get to 0, display the word Blastoff!"

More formally, here is the flow of execution for a while statement:

- Evaluate the condition, yielding True or False.
- If the condition is false, exit the while statement and continue execution at the next statement.
- If the condition is true, execute the body and then go back to step 1.

This type of flow is called a **loop** because the third step loops back around to the top.

The body of the loop should change the value of one or more variables so that eventually the condition becomes false and the loop terminates. Otherwise the loop will repeat forever, which is called an **infinite loop**. An endless source of amusement for computer scientists is the observation that the directions on shampoo, "Lather, rinse, repeat," are an infinite loop.

In the case of countdown, we can prove that the loop terminates because we know that the value of n is finite, and we can see that the value of n gets smaller each time through the loop, so eventually we have to get to 0. In other cases, it is not so easy to tell:

The condition for this loop is n != 1, so the loop will continue until n is 1, which makes the condition false.

Each time through the loop, the program outputs the value of n and then checks whether it is even or odd. If it is even, n is divided by 2. If it is odd, the value of n is replaced with n*3+1. For example, if the argument passed to sequence is 3, the resulting sequence is 3, 10, 5, 16, 8, 4, 2, 1.

Since n sometimes increases and sometimes decreases, there is no obvious proof that n will ever reach 1, or that the program terminates. For some particular values of n, we can prove termination. For example, if the starting value is a power of two, then the value of n will be even each time through the loop until it reaches 1. The previous example ends with such a sequence, starting with 16.

The hard question is whether we can prove that this program terminates for all positive values of n. So far1, no one has been able to prove it or disprove it! **Exercise 1** Rewrite the function print_n from Section '5.8' using iteration instead of recursion.

6.15 break

Sometimes you don't know it's time to end a loop until you get half way through the body. In that case you can use the break statement to jump out of the loop.

For example, suppose you want to take input from the user until they type done. You could write:

```
while True:
    line = raw_input('> ')
    if line == 'done':
        break
    print line
print 'Done!'
```

The loop condition is True, which is always true, so the loop runs until it hits the break statement.

Each time through, it prompts the user with an angle bracket. If the user types done, the break statement exits the loop. Otherwise the program echoes whatever the user types and goes back to the top of the loop. Here's a sample run:

> not done not done > done Done!

This way of writing while loops is common because you can check the condition anywhere in the loop (not just at the top) and you can express the stop condition affirmatively ("stop when this happens") rather than negatively ("keep going until that happens.").

6.16 Square roots

Loops are often used in programs that compute numerical results by starting with an approximate answer and iteratively improving it.

For example, one way of computing square roots is Newton's method. Suppose that you want to know the square root of a. If you start with almost any estimate, x, you can compute a better estimate with the following formula: y = x + a/x

 $\mathbf{2}$

For example, if a is 4 and x is 3:

```
>>> a = 4.0
>>> x = 3.0
>>> y = (x + a/x) / 2
>>> print y
2.166666666667
```

Which is closer to the correct answer ($\sqrt{4} = 2$). If we repeat the process with the new estimate, it gets even closer:

```
>>> x = y
>>> y = (x + a/x) / 2
>>> print y
2.00641025641
```

After a few more updates, the estimate is almost exact:

```
>>> x = y
>>> y = (x + a/x) / 2
>>> print y
2.00001024003
>>> x = y
>>> y = (x + a/x) / 2
>>> print y
2.00000000003
```

In general we don't know ahead of time how many steps it takes to get to the right answer, but we know when we get there because the estimate stops changing:

```
>>> x = y
>>> y = (x + a/x) / 2
>>> print y
2.0
>>> x = y
>>> y = (x + a/x) / 2
>>> print y
2.0
```

When y == x, we can stop. Here is a loop that starts with an initial estimate, x, and improves it until it stops changing:

```
while True:
    print x
    y = (x + a/x) / 2
    if y == x:
        break
    x = y
```

For most values of a this works fine, but in general it is dangerous to test float equality. Floating-point values are only approximately right: most rational numbers, like 1/3, and irrational numbers, like $\sqrt{2}$, can't be represented exactly with a float.

Rather than checking whether x and y are exactly equal, it is safer to use the built-in function abs to compute the absolute value, or magnitude, of the difference between them:

```
if abs(y-x) < epsilon:
    break</pre>
```

Where epsilon has a value like 0.0000001 that determines how close is close enough. **Exercise 2** ' *Encapsulate this loop in a function called square_root* that takes 'a' as a parameter, chooses a reasonable value of 'x', and returns an estimate of the square root of 'a'.

6.17 Algorithms

Newton's method is an example of an **algorithm**: it is a mechanical process for solving a category of problems (in this case, computing square roots).

It is not easy to define an algorithm. It might help to start with something that is not an algorithm. When you learned to multiply single-digit numbers, you probably memorized the multiplication table. In effect, you memorized 100 specific solutions. That kind of knowledge is not algorithmic.

But if you were "lazy," you probably cheated by learning a few tricks. For example, to find the product of n and 9, you can write n-1 as the first digit and 10-n as the second digit. This trick is a general solution for multiplying any single-digit number by 9. That's an algorithm!

Similarly, the techniques you learned for addition with carrying, subtraction with borrowing, and long division are all algorithms. One of the characteristics of algorithms is that they do not require any intelligence to carry out. They are mechanical processes in which each step follows from the last according to a simple set of rules.

In my opinion, it is embarrassing that humans spend so much time in school learning to execute algorithms that, quite literally, require no intelligence.

On the other hand, the process of designing algorithms is interesting, intellectually challenging, and a central part of what we call programming.

Some of the things that people do naturally, without difficulty or conscious thought, are the hardest to express algorithmically. Understanding natural language is a good example. We

all do it, but so far no one has been able to explain how we do it, at least not in the form of an algorithm.

6.18 Debugging

As you start writing bigger programs, you might find yourself spending more time debugging. More code means more chances to make an error and more place for bugs to hide.

One way to cut your debugging time is "debugging by bisection." For example, if there are 100 lines in your program and you check them one at a time, it would take 100 steps.

Instead, try to break the problem in half. Look at the middle of the program, or near it, for an intermediate value you can check. Add a print statement (or something else that has a verifiable effect) and run the program.

If the mid-point check is incorrect, the problem must be in the first half of the program. If it is correct, the problem is in the second half.

Every time you perform a check like this, you halve the number of lines you have to search. After six steps (which is much less than 100), you would be down to one or two lines of code, at least in theory.

In practice it is not always clear what the "middle of the program" is and not always possible to check it. It doesn't make sense to count lines and find the exact midpoint. Instead, think about places in the program where there might be errors and places where it is easy to put a check. Then choose a spot where you think the chances are about the same that the bug is before or after the check.

6.19 Glossary

multiple assignment: Making more than one assignment to the same variable during the execution of a program.

update: An assignment where the new value of the variable depends on the old. **initialize:** An assignment that gives an initial value to a variable that will be updated.**increment:** An update that increases the value of a variable (often by one). **decrement:** An update that decreases the value of a variable. **iteration:** Repeated execution of a set of statements using either a recursive function call or a loop. **infinite loop:** A loop in which the terminating condition is never satisfied.

6.20 Exercises

6.20.1 Exercise 3

To test the square root algorithm in this chapter, you could compare it with **'math.sqrt**'. Write a function named test_square_root that prints a table like this:

```
''1.0 1.0
                   1.0
                                  0.0
2.0 1.41421356237 1.41421356237 2.22044604925e-16
3.0 1.73205080757 1.73205080757 0.0
4.0 2.0
                 2.0
                               0.0
5.0 2.2360679775 2.2360679775 0.0
6.0 2.44948974278 2.44948974278 0.0
7.0 2.64575131106 2.64575131106 0.0
8.0 2.82842712475 2.82842712475 4.4408920985e-16
9.0 3.0
                 3.0
                                0.0
. .
```

The first column is a number, 'a'; the second column is the square root of 'a' computed with the function from Exercise '7.2'; the third column is the square root computed by 'math.sqrt'; the fourth column is the absolute value of the difference between the two estimates.

6.20.2 Exercise 4

The built-in function 'eval' takes a string and evaluates it using the Python interpreter. For example:

```
''>>> eval('1 + 2 * 3')
7
>>> import math
>>> eval('math.sqrt(5)')
2.2360679774997898
>>> eval('type(math.pi)')
<type 'float'>
''
```

Write a function called eval_loopthat iteratively prompts the user, takes the resulting input and evaluates it using 'eval', and prints the result.

It should continue until the user enters **done**, and then return the value of the last expression it evaluated.

6.20.3 Exercise 5

The brilliant mathematician Srinivasa Ramanujan found an infinite series 2 that can be used to generate a numerical approximation of π :

 $\frac{1}{\pi} = \frac{2\sqrt{2}}{9801} \sum_{k=0}^{\infty} \frac{(4k)!(1103+26390k)}{(k!)^4396^{4k}}$

Write a function called estimate_pithat uses this formula to compute and return an estimate of ' π '. It should use a 'while' loop to compute terms of the summation until the last term is smaller than '1e-15' (which is Python notation for '10-15). You can check the result by comparing it to 'math.pi'.

You can see my solution at 'thinkpython.com/code/pi.py'.

1See wikipedia.org/wiki/Collatz_conjecture. 2See wikipedia.org/wiki/Pi.

7 Strings

7.1 A string is a sequence

A string is a **sequence** of characters. You can access the characters one at a time with the bracket operator:

```
>>> fruit = 'banana'
>>> letter = fruit[1]
```

The second statement selects character number 1 from fruit and assigns it to letter.

The expression in brackets is called an **index**. The index indicates which character in the sequence you want (hence the name).

But you might not get what you expect:

```
>>> print letter
a
```

For most people, the first letter of 'banana' is b, not a. But for computer scientists, the index is an offset from the beginning of the string, and the offset of the first letter is zero.

```
>>> letter = fruit[0]
>>> print letter
b
```

So b is the 0th letter ("zero-eth") of 'banana', a is the 1th letter ("one-eth"), and n is the 2th ("two-eth") letter.

You can use any expression, including variables and operators, as an index, but the value of the index has to be an integer. Otherwise you get:

```
>>> letter = fruit[1.5]
TypeError: string indices must be integers
```

7.2 len

len is a built-in function that returns the number of characters in a string:

```
>>> fruit = 'banana'
>>> len(fruit)
6
```

To get the last letter of a string, you might be tempted to try something like this:

```
>>> length = len(fruit)
>>> last = fruit[length]
IndexError: string index out of range
```

The reason for the IndexError is that there is no letter in 'banana' with the index 6. Since we started counting at zero, the six letters are numbered 0 to 5. To get the last character, you have to subtract 1 from length:

```
>>> last = fruit[length-1]
>>> print last
a
```

Alternatively, you can use negative indices, which count backward from the end of the string. The expression fruit[-1] yields the last letter, fruit[-2] yields the second to last, and so on.

7.3 Traversal with a for loop

A lot of computations involve processing a string one character at a time. Often they start at the beginning, select each character in turn, do something to it, and continue until the end. This pattern of processing is called a **traversal**. One way to write a traversal is with a while loop:

```
index = 0
while index < len(fruit):
    letter = fruit[index]
    print letter
    index = index + 1</pre>
```

This loop traverses the string and displays each letter on a line by itself. The loop condition is index < len(fruit), so when index is equal to the length of the string, the condition is false, and the body of the loop is not executed. The last character accessed is the one with the index len(fruit)-1, which is the last character in the string. **Exercise 1** Write a function that takes a string as an argument and displays the letters backward, one per line. Another way to write a traversal is with a for loop:

```
for char in fruit:
print char
```

Each time through the loop, the next character in the string is assigned to the variable char. The loop continues until no characters are left.

The following example shows how to use concatenation (string addition) and a for loop to generate an abecedarian series (that is, in alphabetical order). In Robert McCloskey's book *Make* Way for Ducklings, *the names of the ducklings are Jack, Kack, Lack, Mack, Nack, Ouack, Pack, and Quack.* This loop outputs these names in order:

```
prefixes = 'JKLMNOPQ'
suffix = 'ack'
for letter in prefixes:
    print letter + suffix
```

The output is:

Jack Kack Lack Mack Nack Oack Pack Qack

Of course, that's not quite right because "Ouack" and "Quack" are misspelled.

7.3.1 Exercise 2

Modify the program to fix this error.

7.4 String slices

A segment of a string is called a **slice**. Selecting a slice is similar to selecting a character:

```
>>> s = 'Monty Python'
>>> print s[0:5]
Monty
>>> print s[6:13]
Python
```

The operator [n:m] returns the part of the string from the "n-eth" character to the "m-eth" character, including the first but excluding the last. This behavior is counterintuitive, but it might help to imagine the indices pointing *between* the characters, as in the following diagram:

If you omit the first index (before the colon), the slice starts at the beginning of the string. If you omit the second index, the slice goes to the end of the string:

```
>>> fruit = 'banana'
>>> fruit[:3]
'ban'
>>> fruit[3:]
'ana'
```

If the first index is greater than or equal to the second the result is an **empty string**, represented by two quotation marks:

```
>>> fruit = 'banana'
>>> fruit[3:3]
```

An empty string contains no characters and has length 0, but other than that, it is the same as any other string.

7.4.1 Exercise 3

Given that 'fruit' is a string, what does 'fruit[:]' mean?

7.5 Strings are immutable

It is tempting to use the [] operator on the left side of an assignment, with the intention of changing a character in a string. For example:

```
>>> greeting = 'Hello, world!'
>>> greeting[0] = 'J'
TypeError: object does not support item assignment
```

The "object" in this case is the string and the "item" is the character you tried to assign. For now, an **object** is the same thing as a value, but we will refine that definition later. An **item** is one of the values in a sequence.

The reason for the error is that strings are **immutable**, which means you can't change an existing string. The best you can do is create a new string that is a variation on the original:

```
>>> greeting = 'Hello, world!'
>>> new_greeting = 'J' + greeting[1:]
>>> print new_greeting
Jello, world!
```

This example concatenates a new first letter onto a slice of greeting. It has no effect on the original string.

7.6 Searching

What does the following function do?

```
def find(word, letter):
    index = 0
    while index < len(word):
        if word[index] == letter:
            return index
        index = index + 1
    return -1
```

In a sense, find is the opposite of the [] operator. Instead of taking an index and extracting the corresponding character, it takes a character and finds the index where that character appears. If the character is not found, the function returns -1.

This is the first example we have seen of a return statement inside a loop. If word[index] == letter, the function breaks out of the loop and returns immediately.

If the character doesn't appear in the string, the program exits the loop normally and returns -1.

This pattern of computation—traversing a sequence and returning when we find what we are looking for—is a called a **search**.

7.6.1 Exercise 4

Modify 'find' so that it has a third parameter, the index in 'word' where it should start looking.

7.7 Looping and counting

The following program counts the number of times the letter a appears in a string:

```
word = 'banana'
count = 0
for letter in word:
    if letter == 'a':
        count = count + 1
print count
```

This program demonstrates another pattern of computation called a **counter**. The variable count is initialized to 0 and then incremented each time an a is found. When the loop exits, count contains the result—the total number of a's. **Exercise 5** Encapsulate this code in a function named 'count', and generalize it so that it accepts the string and the letter as arguments. **Exercise 6** Rewrite this function so that instead of traversing the string, it uses the three-parameter version of 'find' from the previous section.

7.8 string methods

A **method** is similar to a function—it takes arguments and returns a value—but the syntax is different. For example, the method upper takes a string and returns a new string with all uppercase letters:

Instead of the function syntax upper(word), it uses the method syntax word.upper().

```
>>> word = 'banana'
>>> new_word = word.upper()
>>> print new_word
BANANA
```

This form of dot notation specifies the name of the method, upper, and the name of the string to apply the method to, word. The empty parentheses indicate that this method takes no argument.

A method call is called an **invocation**; in this case, we would say that we are invoking upper on the word.

As it turns out, there is a string method named find that is remarkably similar to the function we wrote:

```
>>> word = 'banana'
>>> index = word.find('a')
>>> print index
1
```

In this example, we invoke find on word and pass the letter we are looking for as a parameter.

Actually, the find method is more general than our function; it can find substrings, not just characters:

>>> word.find('na')
2

It can take as a second argument the index where it should start:

```
>>> word.find('na', 3)
4
```

And as a third argument the index where it should stop:

```
>>> name = 'bob'
>>> name.find('b', 1, 2)
-1
```

This search fails because b does not appear in the index range from 1 to 2 (not including 2). **Exercise 7** ' There is a string method called 'count' that is similar to the function in the previous exercise. Read the documentation of this method and write an invocation that counts the number of 'a's in *banana*.

7.9 The in operator

The word in is a boolean operator that takes two strings and returns True if the first appears as a substring in the second:

```
>>> 'a' in 'banana'
True
>>> 'seed' in 'banana'
False
```

For example, the following function prints all the letters from word1 that also appear in word2:

```
def in_both(word1, word2):
    for letter in word1:
        if letter in word2:
            print letter
```

With well-chosen variable names, Python sometimes reads like English. You could read this loop, "for (each) letter in (the first) word, if (the) letter (appears) in (the second) word, print (the) letter."

Here's what you get if you compare apples and oranges:

```
>>> in_both('apples', 'oranges')
a
e
s
```

7.10 String comparison

The comparison operators work on strings. To see if two strings are equal:

if word == ,banana,:
 print ,All right, bananas.,

Other comparison operations are useful for putting words in alphabetical order:

```
if word < ,banana,:
    print ,Your word,, + word + ,, comes before banana.,
elif word > ,banana,:
    print ,Your word,, + word + ,, comes after banana.,
else:
    print ,All right, bananas.,
```

Python does not handle uppercase and lowercase letters the same way that people do. All the uppercase letters come before all the lowercase letters, so:

Your word, Pineapple, comes before banana.

A common way to address this problem is to convert strings to a standard format, such as all lowercase, before performing the comparison. Keep that in mind in case you have to defend yourself against a man armed with a Pineapple.

7.11 Debugging

When you use indices to traverse the values in a sequence, it is tricky to get the beginning and end of the traversal right. Here is a function that is supposed to compare two words and return True if one of the words is the reverse of the other, but it contains two errors:

```
def is_reverse(word1, word2):
    if len(word1) != len(word2):
        return False
    i = 0
    j = len(word2)
    while j > 0:
        if word1[i] != word2[j]:
            return False
        i = i+1
        j = j-1
    return True
```

The first if statement checks whether the words are the same length. If not, we can return False immediately and then, for the rest of the function, we can assume that the words are the same length. This is an example of the guardian pattern in Section 6.8.

i and j are indices: i traverses word1 forward while j traverses word2 backward. If we find two letters that don't match, we can return False immediately. If we get through the whole loop and all the letters match, we return True.

If we test this function with the words "pots" and "stop", we expect the return value True, but we get an IndexError:

```
>>> is_reverse('pots', 'stop')
...
File "reverse.py", line 15, in is_reverse
if word1[i] != word2[j]:
IndexError: string index out of range
```

For debugging this kind of error, my first move is to print the values of the indices immediately before the line where the error appears.

Now when I run the program again, I get more information:

>>> is_reverse('pots', 'stop')
0 4
...
IndexError: string index out of range

The first time through the loop, the value of j is 4, which is out of range for the string 'pots'. The index of the last character is 3, so the initial value for j should be len(word2)-1.

If I fix that error and run the program again, I get:

```
>>> is_reverse('pots', 'stop')
0 3
1 2
2 1
True
```

This time we get the right answer, but it looks like the loop only ran three times, which is suspicious. To get a better idea of what is happening, it is useful to draw a state diagram. During the first iteration, the frame for is_reverse looks like this:

I took a little license by arranging the variables in the frame and adding dotted lines to show that the values of i and j indicate characters in word1 and word2. Exercise 8 ' Starting with this diagram, execute the program on paper, changing the values of 'i' and 'j' during each iteration. Find and fix the second error in this function.

7.12 Glossary

object: Something a variable can refer to. For now, you can use "object" and "value" interchangeably. **sequence:** An ordered set; that is, a set of values where each value is identified by an integer index. **item:** One of the values in a sequence. **index:** An integer value used to select an item in a sequence, such as a character in a string. **slice:** A part of a string specified by a range of indices. **empty string:** A string with no characters and length 0, represented by two quotation marks. **immutable:** The property of a sequence

whose items cannot be assigned. **traverse:** To iterate through the items in a sequence, performing a similar operation on each. **search:** A pattern of traversal that stops when it finds what it is looking for.

counter: A variable used to count something, usually initialized to zero and then incremented. **method:** A function that is associated with an object and called using dot notation. **invocation:** A statement that calls a method.

7.13 Exercises

7.13.1 Exercise 9

A string slice can take a third index that specifies the "step size;" that is, the number of spaces between successive characters. A step size of 2 means every other character; 3 means every third, etc.

```
''>>> fruit = 'banana'
>>> fruit[0:5:2]
'bnn'
''
```

A step size of -1 goes through the word backwards, so the slice [::-1] generates a reversed string.

Use this idiom to write a one-line version of is_palindrome from Exercise '6.6'.

7.13.2 Exercise 10

Read the documentation of the string methods at 'docs.python.org/lib/stringmethods.html'. You might want to experiment with some of them to make sure you understand how they work. 'strip' and 'replace' are particularly useful.

The documentation uses a syntax that might be confusing. For example, in find(sub[, start[, end]]), the brackets indicate optional arguments. So 'sub' is required, but 'start' is optional, and if you include 'start', then 'end' is optional.

7.13.3 Exercise 11

The following functions are all *intended* to check whether a string contains any lowercase letters, but at least some of them are wrong. For each function, describe what the function actually does.

```
''def any_lowercase1(s):
    for c in s:
        if c.islower():
            return True
        else:
            return False

def any_lowercase2(s):
    for c in s:
        if 'c'.islower():
```

```
return 'True'
        else:
            return 'False'
def any_lowercase3(s):
    for c in s:
        flag = c.islower()
    return flag
def any_lowercase4(s):
    flag = False
    for c in s:
        flag = flag or c.islower()
    return flag
def any_lowercase5(s):
    for c in s:
        if not c.islower():
            return False
   return True
. .
```

7.13.4 Exercise 12

ROT13 is a weak form of encryption that involves "rotating" each letter in a word by 13 places¹. To rotate a letter means to shift it through the alphabet, wrapping around to the beginning if necessary, so 'A' shifted by 3 is 'D' and 'Z' shifted by 1 is 'A'.

Write a function called rotate_word that takes a string and an integer as parameters, and that returns a new string that contains the letters from the original string "rotated" by the given amount.

For example, "cheer" rotated by 7 is "jolly" and "melon" rotated by -10 is "cubed".

You might want to use the built-in functions 'ord', which converts a character to a numeric code, and 'chr', which converts numeric codes to characters.

Potentially offensive jokes on the Internet are sometimes encoded in ROT13. If you are not easily offended, find and decode some of them.

7.14 Notes

¹ See wikipedia.org/wiki/ROT13

8 Case study: word play

8.1 Reading word lists

For the exercises in this chapter we need a list of English words. There are lots of word lists available on the Web, but the one most suitable for our purpose is one of the word lists collected and contributed to the public domain by Grady Ward as part of the Moby lexicon project¹. It is a list of 113,809 official crosswords; that is, words that are considered valid in crossword puzzles and other word games. In the Moby collection, the filename is 1138090f.fic; I include a copy of this file, with the simpler name words.txt, along with Swampy.

This file is in plain text, so you can open it with a text editor, but you can also read it from Python. (You may need to move the file from the swampy folder into the main python folder) The built-in function open takes the name of the file as a parameter and returns a **file object** you can use to read the file.

>>> fin = open('words.txt')
>>> print fin
<open file 'words.txt', mode 'r' at 0xb7f4b380>

fin is a common name for a file object used for input. Mode 'r' indicates that this file is open for reading (as opposed to 'w' for writing).

The file object provides several methods for reading, including readline, which reads characters from the file until it gets to a newline and returns the result as a string:

```
>>> fin.readline()
'aa\r\n'
```

The first word in this particular list is "aa," which is a kind of lava. The sequence $\r\n$ represents two whitespace characters, a carriage return and a newline, that separate this word from the next.

The file object keeps track of where it is in the file, so if you call readline again, you get the next word:

```
>>> fin.readline()
'aah\r\n'
```

The next word is "aah," which is a perfectly legitimate word, so stop looking at me like that. Or, if it's the whitespace that's bothering you, we can get rid of it with the string method strip:

```
>>> line = fin.readline()
>>> word = line.strip()
```

¹ wikipedia.org/wiki/Moby_Project

>>> print word aahed

You can also use a file object as part of a for loop. This program reads words.txt and prints each word, one per line:

```
fin = open('words.txt')
for line in fin:
    word = line.strip()
    print word
```

Exercise 1 Write a program that reads 'words.txt' and prints only the words with more than 20 characters (not counting whitespace).

8.2 Exercises

There are solutions to these exercises in the next section. You should at least attempt each one before you read the solutions. **Exercise 2** In 1939 Ernest Vincent Wright published a 50,000 word novel called *Gadsby* that does not contain the letter "e." Since "e" is the most common letter in English, that's not easy to do. *In fact, it is difficult to construct a solitary thought without using* that most common symbol. It is slow going at first, but with caution and hours of training you can gradually gain facility.

All right, I'll stop now.

Write a function called has_no_ethat returns '**True**' if the given word doesn't have the letter "e" in it.

Modify your program from the previous section to print only the words that have no "e" and compute the percentage of the words in the list have no "e."

Exercise 3 Write a function named **'avoids'** that takes a word and a string of forbidden letters, and that returns **'True'** if the word doesn't use any of the forbidden letters. *Modify your program to prompt the user to enter a string* of forbidden letters and then print the number of words that don't contain any of them. Can you find a combination of 5 forbidden letters that excludes the smallest number of words? **Exercise 4** Write a function named uses_only that takes a word and a string of letters, and that returns **'True'** if the word contains only letters in the list. Can you make a sentence using only the letters **'acefhlo'**? Other than "Hoe alfalfa?" *Exercise 5* Write a function named uses_all that takes a word and a string of required letters, and that returns **'True'** if the word uses all the required letters at least once. How many words are there that use all the vowels **'aeiou'**? How about **'aeiouy'**? *Exercise 6* Write a function called is_abecedarian that returns **'True'** if the letters in a word appear in alphabetical order (double letters are ok). How many abecedarian words are there?

8.3 Search

All of the exercises in the previous section have something in common; they can be solved with the search pattern we saw in Section 8.6. The simplest example is:

```
def has_no_e(word):
    for letter in word:
        if letter == 'e':
            return False
    return True
```

The for loop traverses the characters in word. If we find the letter "e", we can immediately return False; otherwise we have to go to the next letter. If we exit the loop normally, that means we didn't find an "e", so we return True.

You can write this function more concisely using the in operator, but I started with this version because it demonstrates the logic of the search pattern.

avoids is a more general version of has_no_e but it has the same structure:

```
def avoids(word, forbidden):
    for letter in word:
        if letter in forbidden:
            return False
    return True
```

We can return False as soon as we find a forbidden letter; if we get to the end of the loop, we return True.

uses_only is similar except that the sense of the condition is reversed:

```
def uses_only(word, available):
    for letter in word:
        if letter not in available:
            return False
        return True
```

Instead of a list of forbidden words, we have a list of available words. If we find a letter in word that is not in available, we can return False.

uses_all is similar except that we reverse the role of the word and the string of letters:

```
def uses_all(word, required):
    for letter in required:
        if letter not in word:
            return False
    return True
```

Instead of traversing the letters in word, the loop traverses the required letters. If any of the required letters do not appear in the word, we can return False.

If you were really thinking like a computer scientist, you would have recognized that uses_all was an instance of a previously-solved problem, and you would have written:

```
def uses_all(word, required):
    return uses_only(required, word)
```

This is an example of a program development method called **problem** recognition, which means that you recognize the problem you are working on as an instance of a previously-solved problem, and apply a previously-developed solution.

8.4 Looping with indices

I wrote the functions in the previous section with for loops because I only needed the characters in the strings; I didn't have to do anything with the indices.

For is_abecedarian we have to compare adjacent letters, which is a little tricky with a for loop:

```
def is_abecedarian(word):
    previous = word[0]
    for c in word:
        if c < previous:
            return False
        previous = c
    return True</pre>
```

An alternative is to use recursion:

```
def is_abecedarian(word):
    if len(word) <= 1:
        return True
    if word[0] > word[1]:
        return False
    return is_abecedarian(word[1:])
```

Another option is to use a while loop:

```
def is_abecedarian(word):
    i = 0
    while i < len(word)-1:
        if word[i+1] < word[i]:
            return False
        i = i+1
    return True
```

The loop starts at i=0 and ends when i=len(word)-1. Each time through the loop, it compares the ith character (which you can think of as the current character) to the i+1th character (which you can think of as the next).

If the next character is less than (alphabetically before) the current one, then we have discovered a break in the abecedarian trend, and we return False.

If we get to the end of the loop without finding a fault, then the word passes the test. To convince yourself that the loop ends correctly, consider an example like 'flossy'. The length of the word is 6, so the last time the loop runs is when i is 4, which is the index of the second-to-last character. On the last iteration, it compares the second-to-last character to the last, which is what we want.

Here is a version of is_palindrome (see Exercise 6.6) that uses two indices; one starts at the beginning and goes up; the other starts at the end and goes down.

```
def is_palindrome(word):
    i = 0
    j = len(word)-1
    while i<j:
        if word[i] != word[j]:
            return False
        i = i+1
```

j = j-1 return True

Or, if you noticed that this is an instance of a previously-solved problem, you might have written:

```
def is_palindrome(word):
    return is_reverse(word, word)
```

Assuming you did Exercise 8.8.

8.5 Debugging

Testing programs is hard. The functions in this chapter are relatively easy to test because you can check the results by hand. Even so, it is somewhere between difficult and impossible to choose a set of words that test for all possible errors.

Taking has_no_e as an example, there are two obvious cases to check: words that have an 'e' should return False; words that don't should return True. You should have no trouble coming up with one of each.

Within each case, there are some less obvious subcases. Among the words that have an "e," you should test words with an "e" at the beginning, the end, and somewhere in the middle. You should test long words, short words, and very short words, like the empty string. The empty string is an example of a **special case**, which is one of the non-obvious cases where errors often lurk.

In addition to the test cases you generate, you can also test your program with a word list like words.txt. By scanning the output, you might be able to catch errors, but be careful: you might catch one kind of error (words that should not be included, but are) and not another (words that should be included, but aren't).

In general, testing can help you find bugs, but it is not easy to generate a good set of test cases, and even if you do, you can't be sure your program is correct.

According to a legendary computer scientist:

Program testing can be used to show the presence of bugs, but never to show their absence! — Edsger W. Dijkstra

8.6 Glossary

file object: A value that represents an open file.

problem recognition: A way of solving a problem by expressing it as an instance of a previously-solved problem. **special case:** A test case that is atypical or non-obvious (and less likely to be handled correctly).

8.7 Exercises

8.7.1 Exercise 7

This question is based on a Puzzler that was broadcast on the radio program $Car Talk^2$: Give me a word with three consecutive double letters. I'll give you a couple of words that almost qualify, but don't. For example, the word committee, c-o-m-m-i-t-t-e-e. It would be great except for the 'i' that sneaks in there. Or Mississippi: M-i-s-s-i-s-s-i-p-p-i. If you could take out those i's it would work. But there is a word that has three consecutive pairs of letters and to the best of my knowledge this may be the only word. Of course there are probably 500 more but I can only think of one. What is the word?

Write a program to find it. You can see my solution at 'thinkpython.com/code/cartalk.py'.

8.7.2 Exercise 8

Here's another *Car Talk Puzzler³*: "I was driving on the highway the other day and I happened to notice my odometer. Like most odometers, it shows six digits, in whole miles only. So, if my car had 300,000 miles, for example, I'd see 3-0-0-0-0-0. "*Now, what I saw that day was very interesting. I noticed that the* last 4 digits were palindromic; that is, they read the same forward as backward. For example, 5-4-4-5 is a palindrome, so my odometer could have read 3-1-5-4-4-5.

"One mile later, the last 5 numbers were palindromic. For example, it could have read 3-6-5-4-5-6. One mile after that, the middle 4 out of 6 numbers were palindromic. And you ready for this? One mile later, all 6 were palindromic!

"The question is, what was on the odometer when I first looked?"

Write a Python program that tests all the six-digit numbers and prints any numbers that satisfy these requirements. You can see my solution at 'thinkpython.com/code/cartalk.py'.

8.7.3 Exercise 9

Here's another *Car Talk* Puzzler you can solve with a search⁴: "Recently I had a visit with my mom and we realized that the two digits that make up my age when reversed resulted in her age. For example, if she's 73, I'm 37. We wondered how often this has happened over the years but we got sidetracked with other topics and we never came up with an answer. "When I got home I figured out that the digits of our ages have been reversible six times so far. I also figured out that if we're lucky it would happen again in a few years, and if we're really lucky it would happen one more time after that. In other words, it would have happened 8 times over all. So the question is, how old am I now?"

 $^{2 \}qquad www.cartalk.com/content/puzzler/transcripts/200725$

³ www.cartalk.com/content/puzzler/transcripts/200803

 $^{4 \}qquad www.cartalk.com/content/puzzler/transcripts/200813$

Write a Python program that searches for solutions to this Puzzler. Hint: you might find the string method 'zfill' useful.

You can see my solution at 'thinkpython.com/code/cartalk.py'.

8.8 Notes

9 Lists

9.1 A list is a sequence

Like a string, a **list** is a sequence of values. In a string, the values are characters; in a list, they can be any type. The values in list are called **elements** or sometimes **items**.

There are several ways to create a new list; the simplest is to enclose the elements in square brackets ([and]):

[10, 20, 30, 40] ['crunchy frog', 'ram bladder', 'lark vomit']

The first example is a list of four integers. The second is a list of three strings. The elements of a list don't have to be the same type. The following list contains a string, a float, an integer, and (lo!) another list:

['spam', 2.0, 5, [10, 20]]

A list within another list is **nested**.

A list that contains no elements is called an empty list; you can create one with empty brackets, [].

As you might expect, you can assign list values to variables:

```
>>> cheeses = ['Cheddar', 'Edam', 'Gouda']
>>> numbers = [17, 123]
>>> empty = []
>>> print cheeses, numbers, empty
['Cheddar', 'Edam', 'Gouda'] [17, 123] []
```

9.2 Lists are mutable

The syntax for accessing the elements of a list is the same as for accessing the characters of a string—the bracket operator. The expression inside the brackets specifies the index. Remember that the indices start at 0:

```
>>> print cheeses[0]
Cheddar
```

Unlike strings, lists are mutable. When the bracket operator appears on the left side of an assignment, it identifies the element of the list that will be assigned.

```
>>> numbers = [17, 123]
>>> numbers[1] = 5
```

>>> print numbers
[17, 5]

The one-eth element of numbers, which used to be 123, is now 5.

You can think of a list as a relationship between indices and elements. This relationship is called a **mapping**; each index "maps to" one of the elements. Here is a state diagram showing cheeses, numbers and empty:

Lists are represented by boxes with the word "list" outside and the elements of the list inside. cheeses refers to a list with three elements indexed 0, 1 and 2. numbers contains two elements; the diagram shows that the value of the second element has been reassigned from 123 to 5. empty refers to a list with no elements.

List indices work the same way as string indices:

- Any integer expression can be used as an index.
- If you try to read or write an element that does not exist, you get an IndexError.
- If an index has a negative value, it counts backward from the end of the list.

The in operator also works on lists.

```
>>> cheeses = ['Cheddar', 'Edam', 'Gouda']
>>> 'Edam' in cheeses
True
>>> 'Brie' in cheeses
False
```

9.3 Traversing a list

The most common way to traverse the elements of a list is with a for loop. The syntax is the same as for strings:

```
for cheese in cheeses: print cheese
```

This works well if you only need to read the elements of the list. But if you want to write or update the elements, you need the indices. A common way to do that is to combine the functions range and len:

```
for i in range(len(numbers)):
    numbers[i] = numbers[i] * 2
```

This loop traverses the list and updates each element. len returns the number of elements in the list. range returns a list of indices from 0 to n-1, where n is the length of the list. Each time through the loop i gets the index of the next element. The assignment statement in the body uses i to read the old value of the element and to assign the new value.

A for loop over an empty list never executes the body:

```
for x in empty:
    print 'This never happens.'
```

Although a list can contain another list, the nested list still counts as a single element. The length of this list is four:

['spam', 1, ['Brie', 'Roquefort', 'Pol le Veq'], [1, 2, 3]]

9.4 List operations

The + operator concatenates lists:

>>> a = [1, 2, 3]
>>> b = [4, 5, 6]
>>> c = a + b
>>> print c
[1, 2, 3, 4, 5, 6]

Similarly, the * operator repeats a list a given number of times:

>>> [0] * 4 [0, 0, 0, 0] >>> [1, 2, 3] * 3 [1, 2, 3, 1, 2, 3, 1, 2, 3]

The first example repeats [0] four times. The second example repeats the list [1, 2, 3] three times.

9.5 List slices

The slice operator also works on lists:

```
>>> t = ['a', 'b', 'c', 'd', 'e', 'f']
>>> t[1:3]
['b', 'c']
>>> t[:4]
['a', 'b', 'c', 'd']
>>> t[3:]
['d', 'e', 'f']
```

If you omit the first index, the slice starts at the beginning. If you omit the second, the slice goes to the end. So if you omit both, the slice is a copy of the whole list.

>>> t[:] ['a', 'b', 'c', 'd', 'e', 'f']

Since lists are mutable, it is often useful to make a copy before performing operations that fold, spindle or mutilate lists.

A slice operator on the left side of an assignment can update multiple elements:

```
>>> t = ['a', 'b', 'c', 'd', 'e', 'f']
>>> t[1:3] = ['x', 'y']
>>> print t
['a', 'x', 'y', 'd', 'e', 'f']
```

9.6 List methods

Python provides methods that operate on lists. For example, append adds a new element to the end of a list:

```
>>> t = ['a', 'b', 'c']
>>> t.append('d')
>>> print t
['a', 'b', 'c', 'd']
```

extend takes a list as an argument and appends all of the elements:

```
>>> t1 = ['a', 'b', 'c']
>>> t2 = ['d', 'e']
>>> t1.extend(t2)
>>> print t1
['a', 'b', 'c', 'd', 'e']
```

This example leaves t2 unmodified.

sort arranges the elements of the list from low to high:

```
>>> t = ['d', 'c', 'e', 'b', 'a']
>>> t.sort()
>>> print t
['a', 'b', 'c', 'd', 'e']
```

List methods are all void; they modify the list and return None. If you accidentally write t = t.sort(), you will be disappointed with the result.

9.7 Map, filter and reduce

To add up all the numbers in a list, you can use a loop like this:

```
def add_all(t):
    total = 0
    for x in t:
        total += x
    return total
```

total is initialized to 0. Each time through the loop, x gets one element from the list. The += operator provides a short way to update a variable:

```
total += x
```

is equivalent to:

total = total + x

As the loop executes, total accumulates the sum of the elements; a variable used this way is sometimes called an **accumulator**.

Adding up the elements of a list is such a common operation that Python provides it as a built-in function, sum:

```
>>> t = [1, 2, 3]
>>> sum(t)
6
```

An operation like this that combines a sequence of elements into a single value is sometimes called **reduce**.

Sometimes you want to traverse one list while building another. For example, the following function takes a list of strings and returns a new list that contains capitalized strings:

```
def capitalize_all(t):
    res = []
    for s in t:
        res.append(s.capitalize())
    return res
```

res is initialized with an empty list; each time through the loop, we append the next element. So res is another kind of accumulator.

An operation like capitalize_all is sometimes called a **map** because it "maps" a function (in this case the method capitalize) onto each of the elements in a sequence.

Another common operation is to select some of the elements from a list and return a sublist. For example, the following function takes a list of strings and returns a list that contains only the uppercase strings:

```
def only_upper(t):
    res = []
    for s in t:
        if s.isupper():
            res.append(s)
    return res
```

is support is a string method that returns True if the string contains only upper case letters.

An operation like only_upper is called a **filter** because it selects some of the elements and filters out the others.

Most common list operations can be expressed as a combination of map, filter and reduce. Because these operations are so common, Python provides language features to support them, including the built-in function map and an operator called a "list comprehension."

9.7.1 Exercise 1

Write a function that takes a list of numbers and returns the cumulative sum; that is, a new list where the 'i'th element is the sum of the first 'i+1' elements from the original list. For example, the cumulative sum of '[1, 2, 3]' is '[1, 3, 6]'.

9.8 Deleting elements

There are several ways to delete elements from a list. If you know the index of the element you want, you can use pop:

```
>>> t = ['a', 'b', 'c']
>>> x = t.pop(1)
>>> print t
['a', 'c']
>>> print x
b
```

pop modifies the list and returns the element that was removed. If you don't provide an index, it deletes and returns the last element.

If you don't need the removed value, you can use the del operator:

```
>>> t = ['a', 'b', 'c']
>>> del t[1]
>>> print t
['a', 'c']
```

If you know the element you want to remove (but not the index), you can use remove:

```
>>> t = ['a', 'b', 'c']
>>> t.remove('b')
>>> print t
['a', 'c']
```

The return value from remove is None.

To remove more than one element, you can use del with a slice index:

```
>>> t = ['a', 'b', 'c', 'd', 'e', 'f']
>>> del t[1:5]
>>> print t
['a', 'f']
```

As usual, the slice selects all the elements up to, but not including, the second index.

9.9 Lists and strings

A string is a sequence of characters and a list is a sequence of values, but a list of characters is not the same as a string. To convert from a string to a list of characters, you can use list:

```
>>> s = 'spam'
>>> t = list(s)
>>> print t
['s', 'p', 'a', 'm']
```

Because list is the name of a built-in function, you should avoid using it as a variable name. I also avoid l because it looks too much like 1. So that's why I use t.

The list function breaks a string into individual letters. If you want to break a string into words, you can use the split method:

```
>>> s = 'pining for the fjords'
>>> t = s.split()
>>> print t
['pining', 'for', 'the', 'fjords']
```

An optional argument called a **delimiter** specifies which characters to use as word boundaries. The following example uses a hyphen as a delimiter:

```
>>> s = 'spam-spam-spam'
>>> delimiter = '-'
>>> s.split(delimiter)
['spam', 'spam', 'spam']
```

join is the inverse of split. It takes a list of strings and concatenates the elements. join is a string method, so you have to invoke it on the delimiter and pass the list as a parameter:

```
>>> t = ['pining', 'for', 'the', 'fjords']
>>> delimiter = ' '
>>> delimiter.join(t)
'pining for the fjords'
```

In this case the delimiter is a space character, so join puts a space between words. To concatenate strings without spaces, you can use the empty string, , as a delimiter.

9.10 Objects and values

If we execute these assignment statements:

```
a = 'banana'
b = 'banana'
```

We know that a and b both refer to a string, but we don't know whether they refer to the *same* string. There are two possible states:

In one case, a and b refer to two different objects that have the same value. In the second case, they refer to the same object.

To check whether two variables refer to the same object, you can use the is operator.

```
>>> a = 'banana'
>>> b = 'banana'
>>> a is b
True
```

In this example, Python only created one string object, and both a and b refer to it.

But when you create two lists, you get two objects:

```
>>> a = [1, 2, 3]
>>> b = [1, 2, 3]
>>> a is b
False
```

So the state diagram looks like this:

In this case we would say that the two lists are **equivalent**, because they have the same elements, but not **identical**, because they are not the same object. If two objects are identical, they are also equivalent, but if they are equivalent, they are not necessarily identical.

Until now, we have been using "object" and "value" interchangeably, but it is more precise to say that an object has a value. If you execute a = [1,2,3], a refers to a list object whose value is a particular sequence of elements. If another list has the same elements, we would say it has the same value.

9.11 Aliasing

If a refers to an object and you assign b = a, then both variables refer to the same object:

>>> a = [1, 2, 3] >>> b = a >>> b is a True

The state diagram looks like this:

The association of a variable with an object is called a **reference**. In this example, there are two references to the same object.

An object with more than one reference has more than one name, so we say that the object is **aliased**.

If the aliased object is mutable, changes made with one alias affect the other:

```
>>> b[0] = 17
>>> print a
[17, 2, 3]
```

Although this behavior can be useful, it is error-prone. In general, it is safer to avoid aliasing when you are working with mutable objects.

For immutable objects like strings, aliasing is not as much of a problem. In this example:

a = 'banana' b = 'banana'

It almost never makes a difference whether a and b refer to the same string or not.

9.12 List arguments

When you pass a list to a function, the function gets a reference to the list. If the function modifies a list parameter, the caller sees the change. For example, delete_head removes the first element from a list:

```
def delete_head(t):
del t[0]
```

Here's how it is used:

>>> letters = ['a', 'b', 'c']
>>> delete_head(letters)
>>> print letters

['b', 'c']

The parameter t and the variable letters are aliases for the same object. The stack diagram looks like this:

Since the list is shared by two frames, I drew it between them.

It is important to distinguish between operations that modify lists and operations that create new lists. For example, the append method modifies a list, but the + operator creates a new list:

```
>>> t1 = [1, 2]
>>> t2 = t1.append(3)
>>> print t1
[1, 2, 3]
>>> print t2
None
>>> t3 = t1 + [3]
>>> print t3
[1, 2, 3]
>>> t2 is t3
False
```

This difference is important when you write functions that are supposed to modify lists. For example, this function *does not* delete the head of a list:

def bad_delete_head(t):
 t = t[1:] # WRONG!

The slice operator creates a new list and the assignment makes t refer to it, but none of that has any effect on the list that was passed as an argument.

An alternative is to write a function that creates and returns a new list. For example, tail returns all but the first element of a list:

```
def tail(t):
    return t[1:]
```

This function leaves the original list unmodified. Here's how it is used:

```
>>> letters = ['a', 'b', 'c']
>>> rest = tail(letters)
>>> print rest
['b', 'c']
```

9.12.1 Exercise 2

Write a function called '**chop**' that takes a list and modifies it, removing the first and last elements, and returns '**None**'.

Then write a function called **'middle**' that takes a list and returns a new list that contains all but the first and last elements.

9.13 Debugging

Careless use of lists (and other mutable objects) can lead to long hours of debugging. Here are some common pitfalls and ways to avoid them:

• Don't forget that most list methods modify the argument and

return None. This is the opposite of the string methods, which return a new string and leave the original alone. If you are used to writing string code like this: word = word.strip()

1.0

It is tempting to write list code like this:

t = t.sort() # WRONG!

Because sort returns None, the next operation you perform with t is likely to fail.

Before using list methods and operators, you should read the documentation carefully and then test them in interactive mode. The methods and operators that lists share with other sequences (like strings) are documented at docs.python.org/lib/typesseq.html. The methods and operators that only apply to mutable sequences are documented at docs.python.org/lib/typesseq-mutable.html.

• Pick an idiom and stick with it.

Part of the problem with lists is that there are too many ways to do things. For example, to remove an element from a list, you can use pop, remove, del, or even a slice assignment.

To add an element, you can use the append method or the + operator. But don't forget that these are right:

t.append(x)t = t + [x]

And these are wrong:

WRONG!
WRONG!
WRONG!
WRONG!

Try out each of these examples in interactive mode to make sure you understand what they do. Notice that only the last one causes a runtime error; the other three are legal, but they do the wrong thing.

• Make copies to avoid aliasing.

If you want to use a method like sort that modifies the argument, but you need to keep the original list as well, you can make a copy.

orig = t[:]
t.sort()

In this example you could also use the built-in function sorted, which returns a new, sorted list and leaves the original alone. But in that case you should avoid using sorted as a variable name!

9.14 Glossary

list: A sequence of values. **element:** One of the values in a list (or other sequence), also called items. **index:** An integer value that indicates an element in a list. **nested list:** A list that is an element of another list. **list traversal:** The sequential accessing of each element in a list. **mapping:** A relationship in which each element of one set corresponds to an element of another set. For example, a list is a mapping from indices to elements. **accumulator:** A variable used in a loop to add up or accumulate a result.

reduce: A processing pattern that traverses a sequence and accumulates the elements into a single result.

map: A processing pattern that traverses a sequence and performs an operation on each element.

filter: A processing pattern that traverses a list and selects the elements that satisfy some criterion.

object: Something a variable can refer to. An object has a type and a value. **equivalent:** Having the same value. **identical:** Being the same object (which implies equivalence). **reference:** The association between a variable and its value. **aliasing:** A circumstance where two variables refer to the same object. **delimiter:** A character or string used to indicate where a string should be split.

9.15 Exercises

9.15.1 Exercise 3

Write a function called is_sorted that takes a list as a parameter and returns '**True**' if the list is sorted in ascending order and '**False**' otherwise. You can assume (as a precondition) that the elements of the list can be compared with the comparison operators '<', '>', etc.

For example, is_sorted([1,2,2])should return '**True**' and is_sorted(['b','a']) should return '**False**'.

9.15.2 Exercise 4

Two words are anagrams if you can rearrange the letters from one to spell the other. Write a function called is_anagram that takes two strings and returns **'True'** if they are anagrams. **Exercise 5** The (so-called) Birthday Paradox:

Write a function called has_duplicatesthat takes a list and returns '**True**' if there is any element that appears more than once. It should not modify the original list.

• If there are 23 students in your class, what are the chances

that two of you have the same birthday? You can estimate this probability by generating random samples of 23 birthdays and checking for matches. Hint: you can generate random birthdays with the **'randint**' function in the **'random'** module.

You can read about this problem at 'wikipedia.org/wiki/Birthday_paradox', and you can see my solution at 'thinkpython.com/code/birthday.py'. Exercise 6

Write a function called remove_duplicates that takes a list and returns a new list with only the unique elements from the original. Hint: they don't have to be in the same order.

9.15.3 Exercise 7

Write a function that reads the file 'words.txt' and builds a list with one element per word. Write two versions of this function, one using the 'append' method and the other using the idiom ' $\mathbf{t} = \mathbf{t} + [\mathbf{x}]$ '. Which one takes longer to run? Why?

You can see my solution at 'thinkpython.com/code/wordlist.py'.

9.15.4 Exercise 8

To check whether a word is in the word list, you could use the 'in' operator, but it would be slow because it searches through the words in order.

Because the words are in alphabetical order, we can speed things up with a bisection search, which is similar to what you do when you look a word up in the dictionary. You start in the middle and check to see whether the word you are looking for comes before the word in the middle of the list. If so, then you search the first half of the list the same way. Otherwise you search the second half.

Either way, you cut the remaining search space in half. If the word list has 113,809 words, it will take about 17 steps to find the word or conclude that it's not there.

Write a function called 'bisect' that takes a sorted list and a target value and returns the index of the value in the list, if it's there, or 'None' if it's not.

Or you could read the documentation of the 'bisect' module and use that!

9.15.5 Exercise 9

Two words are a "reverse pair" if each is the reverse of the other. Write a program that finds all the reverse pairs in the word list.

9.15.6 Exercise 10

Two words "interlock" if taking alternating letters from each forms a new word1. For example, "shoe" and "cold" interlock to form "schooled."

• Write a program that finds all pairs of words that interlock.

Hint: don't enumerate all pairs!

• Can you find any words that are three-way interlocked; that is,

every third letter forms a word, starting from the first, second or third?

1This exercise is inspired by an example at puzzlers.org.

10 Dictionaries

A **dictionary** is like a list, but more general. In a list, the indices have to be integers; in a dictionary they can be (almost) any type.

You can think of a dictionary as a mapping between a set of indices (which are called **keys**) and a set of values. Each key maps to a value. The association of a key and a value is called a **key-value pair** or sometimes an **item**.

As an example, we'll build a dictionary that maps from English to Spanish words, so the keys and the values are all strings.

The function dict creates a new dictionary with no items. Because dict is the name of a built-in function, you should avoid using it as a variable name.

```
>>> eng2sp = dict()
>>> print eng2sp
{}
```

The squiggly-brackets, {}, represent an empty dictionary. To add items to the dictionary, you can use square brackets:

```
>>> eng2sp['one'] = 'uno'
```

This line creates an item that maps from the key 'one' to the value 'uno'. If we print the dictionary again, we see a key-value pair with a colon between the key and value:

>>> print eng2sp
{'one': 'uno'}

This output format is also an input format. For example, you can create a new dictionary with three items:

>>> eng2sp = {'one': 'uno', 'two': 'dos', 'three': 'tres'}

But if you print eng2sp, you might be surprised:

```
>>> print eng2sp
{'one': 'uno', 'three': 'tres', 'two': 'dos'}
```

The order of the key-value pairs is not the same. In fact, if you type the same example on your computer, you might get a different result. In general, the order of items in a dictionary is unpredictable.

But that's not a problem because the elements of a dictionary are never indexed with integer indices. Instead, you use the keys to look up the corresponding values:

```
>>> print eng2sp['two']
'dos'
```

The key 'two' always maps to the value 'dos' so the order of the items doesn't matter.

If the key isn't in the dictionary, you get an exception:

```
>>> print eng2sp['four']
KeyError: 'four'
```

The len function works on dictionaries; it returns the number of key-value pairs:

```
>>> len(eng2sp)
3
```

The in operator works on dictionaries; it tells you whether something appears as a *key* in the dictionary (appearing as a value is not good enough).

```
>>> 'one' in eng2sp
True
>>> 'uno' in eng2sp
False
```

To see whether something appears as a value in a dictionary, you can use the method values, which returns the values as a list, and then use the in operator:

```
>>> vals = eng2sp.values()
>>> 'uno' in vals
True
```

The in operator uses different algorithms for lists and dictionaries. For lists, it uses a search algorithm, as in Section 8.6. As the list gets longer, the search time gets longer in direct proportion. For dictionaries, Python uses an algorithm called a **hashtable** that has a remarkable property: the in operator takes about the same amount of time no matter how many items there are in a dictionary. I won't explain how that's possible, but you can read more about it at wikipedia.org/wiki/Hash_table.

10.0.7 Exercise 1

Write a function that reads the words in 'words.txt' and stores them as keys in a dictionary. It doesn't matter what the values are. Then you can use the 'in' operator as a fast way to check whether a string is in the dictionary.

If you did Exercise '10.8', you can compare the speed of this implementation with the list 'in' operator and the bisection search.

10.1 Dictionary as a set of counters

Suppose you are given a string and you want to count how many times each letter appears. There are several ways you could do it:

- You could create 26 variables, one for each letter of the alphabet. Then you could traverse the string and, for each character, increment the corresponding counter, probably using a chained conditional.
- You could create a list with 26 elements. Then you could convert each character to a number (using the built-in function ord), use the number as an index into the list, and increment the appropriate counter.
- You could create a dictionary with characters as keys and counters as the corresponding values. The first time you see a character, you would add an item to the dictionary. After that you would increment the value of an existing item.

Each of these options performs the same computation, but each of them implements that computation in a different way.

An **implementation** is a way of performing a computation; some implementations are better than others. For example, an advantage of the dictionary implementation is that we don't have to know ahead of time which letters appear in the string and we only have to make room for the letters that do appear.

Here is what the code might look like:

```
def histogram(s):
    d = dict()
    for c in s:
        if c not in d:
            d[c] = 1
        else:
            d[c] += 1
    return d
```

The name of the function is **histogram**, which is a statistical term for a set of counters (or frequencies).

The first line of the function creates an empty dictionary. The for loop traverses the string. Each time through the loop, if the character c is not in the dictionary, we create a new item with key c and the initial value 1 (since we have seen this letter once). If c is already in the dictionary we increment d[c].

Here's how it works:

```
>>> h = histogram('brontosaurus')
>>> print h
{'a': 1, 'b': 1, 'o': 2, 'n': 1, 's': 2, 'r': 2, 'u': 2, 't': 1}
```

The histogram indicates that the letters 'a' and 'b' appear once; 'o' appears twice, and so on.

10.1.1 Exercise 2

Dictionaries have a method called 'get' that takes a key and a default value. If the key appears in the dictionary, 'get' returns the corresponding value; otherwise it returns the default value. For example:

```
''>>> h = histogram('a')
>>> print h
{'a': 1}
```

```
>>> h.get('a', 0)
1
>>> h.get('b', 0)
0
```

Use 'get' to write 'histogram' more concisely. You should be able to eliminate the 'if' statement.

10.2 Looping and dictionaries

If you use a dictionary in a for statement, it traverses the keys of the dictionary. For example, print_hist prints each key and the corresponding value:

```
def print_hist(h):
    for c in h:
        print c, h[c]
```

Here's what the output looks like:

```
>>> h = histogram('parrot')
>>> print_hist(h)
a 1
p 1
r 2
t 1
o 1
```

Again, the keys are in no particular order.

10.2.1 Exercise 3

Dictionaries have a method called 'keys' that returns the keys of the dictionary, in no particular order, as a list.

Modify print_histo print the keys and their values in alphabetical order.

10.3 Reverse lookup

Given a dictionary d and a key k, it is easy to find the corresponding value v = d[k]. This operation is called a **lookup**.

But what if you have v and you want to find k? You have two problems: first, there might be more than one key that maps to the value v. Depending on the application, you might be able to pick one, or you might have to make a list that contains all of them. Second, there is no simple syntax to do a **reverse lookup**; you have to search.

Here is a function that takes a value and returns the first key that maps to that value:

```
def reverse_lookup(d, v):
    for k in d:
        if d[k] == v:
            return k
```

raise ValueError

This function is yet another example of the search pattern, but it uses a feature we haven't seen before, raise. The raise statement causes an exception; in this case it causes a ValueError, which generally indicates that there is something wrong with the value of a parameter.

If we get to the end of the loop, that means v doesn't appear in the dictionary as a value, so we raise an exception.

Here is an example of a successful reverse lookup:

```
>>> h = histogram('parrot')
>>> k = reverse_lookup(h, 2)
>>> print k
r
```

And an unsuccessful one:

```
>>> k = reverse_lookup(h, 3)
Traceback (most recent call last):
   File "<stdin>", line 1, in ?
   File "<stdin>", line 5, in reverse_lookup
ValueError
```

The result when you raise an exception is the same as when Python raises one: it prints a traceback and an error message.

The raise statement takes a detailed error message as an optional argument. For example:

```
>>> raise ValueError, 'value does not appear in the dictionary'
Traceback (most recent call last):
   File "<stdin>", line 1, in ?
ValueError: value does not appear in the dictionary
```

A reverse lookup is much slower than a forward lookup; if you have to do it often, or if the dictionary gets big, the performance of your program will suffer. **Exercise 4** Modify reverse_lookup so that it builds and returns a list of *all* keys that map to 'v', or an empty list if there are none.

10.4 Dictionaries and lists

Lists can appear as values in a dictionary. For example, if you were given a dictionary that maps from letters to frequencies, you might want to invert it; that is, create a dictionary that maps from frequencies to letters. Since there might be several letters with the same frequency, each value in the inverted dictionary should be a list of letters.

Here is a function that inverts a dictionary:

```
def invert_dict(d):
    inv = dict()
    for key in d:
        val = d[key]
        if val not in inv:
            inv[val] = [key]
        else:
            inv[val].append(key)
```

return inv

Each time through the loop, key gets a key from d and val gets the corresponding value. If val is not in inv, that means we haven't seen it before, so we create a new item and initialize it with a **singleton** (a list that contains a single element). Otherwise we have seen this value before, so we append the corresponding key to the list.

Here is an example:

```
>>> hist = histogram('parrot')
>>> print hist
{'a': 1, 'p': 1, 'r': 2, 't': 1, 'o': 1}
>>> inv = invert_dict(hist)
>>> print inv
{1: ['a', 'p', 't', 'o'], 2: ['r']}
```

And here is a diagram showing hist and inv:

A dictionary is represented as a box with the type dict above it and the key-value pairs inside. If the values are integers, floats or strings, I usually draw them inside the box, but I usually draw lists outside the box, just to keep the diagram simple.

Lists can be values in a dictionary, as this example shows, but they cannot be keys. Here's what happens if you try:

```
>>> t = [1, 2, 3]
>>> d = dict()
>>> d[t] = 'oops'
Traceback (most recent call last):
File "<stdin>", line 1, in ?
TypeError: list objects are unhashable
```

I mentioned earlier that a dictionary is implemented using a hashtable and that means that the keys have to be **hashable**.

A hash is a function that takes a value (of any kind) and returns an integer. Dictionaries use these integers, called hash values, to store and look up key-value pairs.

This system works fine if the keys are immutable. But if the keys are mutable, like lists, bad things happen. For example, when you create a key-value pair, Python hashes the key and stores it in the corresponding location. If you modify the key and then hash it again, it would go to a different location. In that case you might have two entries for the same key, or you might not be able to find a key. Either way, the dictionary wouldn't work correctly.

That's why the keys have to be hashable, and why mutable types like lists aren't. The simplest way to get around this limitation is to use tuples, which we will see in the next chapter.

Since dictionaries are mutable, they can't be used as keys, but they can be used as values.

10.4.1 Exercise 5

Read the documentation of the dictionary method 'setdefault' and use it to write a more concise version of invert_dict.

10.5 Memos

If you played with the fibonacci function from Section 6.7, you might have noticed that the bigger the argument you provide, the longer the function takes to run. Furthermore, the run time increases very quickly.

To understand why, consider this **call graph** for fibonacci with n=4:

A call graph shows a set of function frames, with lines connecting each frame to the frames of the functions it calls. At the top of the graph, fibonacci with n=4 calls fibonacci with n=3 and n=2. In turn, fibonacci with n=3 calls fibonacci with n=2 and n=1. And so on.

Count how many times fibonacci(0) and fibonacci(1) are called. This is an inefficient solution to the problem, and it gets worse as the argument gets bigger.

One solution is to keep track of values that have already been computed by storing them in a dictionary. A previously computed value that is stored for later use is called a **memo**¹. Here is an implementation of fibonacci using memos:

```
known = {0:0, 1:1}
def fibonacci(n):
    if n in known:
        return known[n]
res = fibonacci(n-1) + fibonacci(n-2)
    known[n] = res
    return res
```

known is a dictionary that keeps track of the Fibonacci numbers we already know. It starts with two items: 0 maps to 0 and 1 maps to 1.

Whenever fibonacci is called, it checks known. If the result is already there, it can return immediately. Otherwise it has to compute the new value, add it to the dictionary, and return it.

10.5.1 Exercise 6

Run this version of **'fibonacci'** and the original with a range of parameters and compare their run times.

10.6 Global variables

In the previous example, known is created outside the function, so it belongs to the special frame called <u>main</u>. Variables in <u>main</u> are sometimes called **global** because they can be accessed from any function. Unlike local variables, which disappear when their function ends, global variables persist from one function call to the next.

¹ See wikipedia.org/wiki/Memoization

It is common to use global variables for **flags**; that is, boolean variables that indicate ("flag") whether a condition is true. For example, some programs use a flag named verbose to control the level of detail in the output:

```
verbose = True
def example1():
    if verbose:
        print 'Running example1'
```

If you try to reassign a global variable, you might be surprised. The following example is supposed to keep track of whether the function has been called:

```
been_called = False
def example2():
    been_called = True  # WRONG
```

But if you run it you will see that the value of been_called doesn't change. The problem is that example2 creates a new local variable named been_called. The local variable goes away when the function ends, and has no effect on the global variable.

To reassign a global variable inside a function you have to **declare** the global variable before you use it:

```
been_called = False
def example2():
    global been_called
    been_called = True
```

The global statement tells the interpreter something like, "In this function, when I say been_called, I mean the global variable; don't create a local one."

Here's an example that tries to update a global variable:

```
count = 0
def example3():
    count = count + 1  # WRONG
```

```
If you run it you get:
```

UnboundLocalError: local variable 'count' referenced before assignment

Python assumes that count is local, which means that you are reading it before writing it. The solution, again, is to declare count global.

```
def example3():
    global count
    count += 1
```

If the global value is mutable, you can modify it without declaring it:

known = {0:0, 1:1}
def example4():

```
known[2] = 1
```

So you can add, remove and replace elements of a global list or dictionary, but if you want to reassign the variable, you have to declare it:

```
def example5():
    global known
    known = dict()
```

10.7 Long integers

If you compute fibonacci(50), you get:

```
>>> fibonacci(50)
12586269025L
```

The L at the end indicates that the result is a long integer², or type long.

Values with type int have a limited range; long integers can be arbitrarily big, but as they get bigger they consume more space and time.

The mathematical operators work on long integers, and the functions in the math module, too, so in general any code that works with int will also work with long.

Any time the result of a computation is too big to be represented with an integer, Python converts the result as a long integer:

>>> 1000 * 1000 1000000 >>> 100000 * 100000 1000000000L

In the first case the result has type int; in the second case it is long.

10.7.1 Exercise 7

Exponentiation of large integers is the basis of common algorithms for public-key encryption. Read the Wikipedia page on the RSA algorithm³ and write functions to encode and decode messages.

10.8 Debugging

As you work with bigger datasets it can become unwieldy to debug by printing and checking data by hand. Here are some suggestions for debugging large datasets: **Scale down the input:** If possible, reduce the size of the dataset. For example if the program reads a text file, start with just the first 10 lines, or with the smallest example you can find. You can

² In Python 3.0, type long is gone; all integers, even really big ones, are type int.

³ wikipedia.org/wiki/RSA

either edit the files themselves, or (better) modify the program so it reads only the first n lines. If there is an error, you can reduce n to the smallest value that manifests the error, and then increase it gradually as you find and correct errors. **Check summaries and types:** Instead of printing and checking the entire dataset, consider printing summaries of the data: for example, the number of items in a dictionary or the total of a list of numbers. A common cause of runtime errors is a value that is not the right type. For debugging this kind of error, it is often enough to print the type of a value. **Write self-checks:** Sometimes you can write code to check for errors automatically. For example, if you are computing the average of a list of numbers, you could check that the result is not greater than the largest element in the list or less than the smallest. This is called a "sanity check" because it detects results that are "insane."

Another kind of check compares the results of two different computations to see if they are consistent. This is called a "consistency check." **Pretty print the output:** Formatting debugging output can make it easier to spot an error. We saw an example in Section 6.9. The pprint module provides a pprint function that displays built-in types in a more human-readable format.

Again, time you spend building scaffolding can reduce the time you spend debugging.

10.9 Glossary

dictionary: A mapping from a set of keys to their corresponding values. key-value pair: The representation of the mapping from a key to a value. item: Another name for a key-value pair. key: An object that appears in a dictionary as the first part of a key-value pair. value: An object that appears in a dictionary as the second part of a key-value pair. This is more specific than our previous use of the word "value." implementation: A way of performing a computation. hashtable: The algorithm used to implement Python dictionaries. hash function: A function used by a hashtable to compute the location for a key. hashable: A type that has a hash function. Immutable types like integers, floats and strings are hashable; mutable types like lists and dictionaries are not. lookup: A dictionary operation that takes a key and finds the corresponding value. reverse lookup: A dictionary operation that takes a value and finds one or more keys that map to it. singleton: A list (or other sequence) with a single element. call graph: A diagram that shows every frame created during the execution of a program, with an arrow from each caller to each callee.

histogram: A set of counters. **memo:** A computed value stored to avoid unnecessary future computation. **global variable:** A variable defined outside a function. Global variables can be accessed from any function. **flag:** A boolean variable used to indicate whether a condition is true. **declaration:** A statement like global that tells the interpreter something about a variable.

10.10 Exercise-8

```
$\ensuremath{\mathsf{Dictionaries}}\xspace have a method called 'keys' that returns the keys of the dictionary, in
```

no particular order, as a list. Modify print_hist to print the keys and their values in alphabetical order.

10.10.1 Exercise 9

Two words are "rotate pairs" if you can rotate one of them and get the other (see rotate_word in Exercise '8.12').

Write a program that reads a wordlist and finds all the rotate pairs.

10.10.2 Exercise 10

Here's another Puzzler from Car Talk⁴: This was sent in by a fellow named Dan O'Leary. He came upon a common one-syllable, five-letter word recently that has the following unique property. When you remove the first letter, the remaining letters form a homophone of the original word, that is a word that sounds exactly the same. Replace the first letter, that is, put it back and remove the second letter and the result is yet another homophone of the original word. And the question is, what's the word? Now I'm going to give you an example that doesn't work. Let's look at the five-letter word, 'wrack.' W-R-A-C-K, you know like to 'wrack with pain.' If I remove the first letter, I am left with a four-letter word, 'R-A-C-K.' As in, 'Holy cow, did you see the rack on that buck! It must have been a nine-pointer!' It's a perfect homophone. If you put the 'w' back, and remove the 'r,' instead, you're left with the word, 'wack,' which is a real word, it's just not a homophone of the other two words.

But there is, however, at least one word that Dan and we know of, which will yield two homophones if you remove either of the first two letters to make two, new four-letter words. The question is, what's the word?

You can use the dictionary from Exercise '11.1' to check whether a string is in the word list.

To check whether two words are homophones, you can use the CMU Pronouncing Dictionary. You can download it from 'www.speech.cs.cmu.edu/cgibin/cmudict' or from 'thinkpython.com/code/c06d' and you can also download 'thinkpython.com/code/pronounce.py', which provides a function named read_dictionary that reads the pronouncing dictionary and returns a Python dictionary that maps from each word to a string that describes its primary pronunciation.

Write a program that lists all the words that solve the Puzzler. You can see my solution at 'thinkpython.com/code/homophone.py'.

10.11 Notes

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 $^{4 \}qquad www.cartalk.com/content/puzzler/transcripts/200717$

11 Tuples

11.1 Tuples are immutable

A tuple is a sequence of values. The values can be any type, and they are indexed by integers, so in that respect tuples are a lot like lists. The important difference is that tuples are immutable.

Syntactically, a tuple is a comma-separated list of values:

>>> t = 'a', 'b', 'c', 'd', 'e'

Although it is not necessary, it is common to enclose tuples in parentheses:

```
>>> t = ('a', 'b', 'c', 'd', 'e')
```

To create a tuple with a single element, you have to include the final comma:

>>> t1 = ('a',) >>> type(t1) <type 'tuple'>

Without the comma, Python treats ('a') as a string in parentheses:

```
>>> t2 = ('a')
>>> type(t2)
<type 'str'>
```

Another way to create a tuple is the built-in function tuple. With no argument, it creates an empty tuple:

```
>>> t = tuple()
>>> print t
()
```

If the argument is a sequence (string, list or tuple), the result is a tuple with the elements of the sequence:

```
>>> t = tuple('lupins')
>>> print t
('l', 'u', 'p', 'i', 'n', 's')
```

Because tuple is the name of a built-in function, you should avoid using it as a variable name.

Most list operators also work on tuples. The bracket operator indexes an element:

>>> t = ('a', 'b', 'c', 'd', 'e') >>> print t[0] 'a'

And the slice operator selects a range of elements.

>>> print t[1:3] ('b', 'c')

But if you try to modify one of the elements of the tuple, you get an error:

>>> t[0] = 'A'
TypeError: object doesn't support item assignment

You can't modify the elements of a tuple, but you can replace one tuple with another:

>>> t = ('A',) + t[1:] >>> print t ('A', 'b', 'c', 'd', 'e')

11.2 Tuple assignment

It is often useful to swap the values of two variables. With conventional assignments, you have to use a temporary variable. For example, to swap a and b:

>>> temp = a >>> a = b >>> b = temp

This solution is cumbersome; **tuple assignment** is more elegant:

>>> a, b = b, a

The left side is a tuple of variables; the right side is a tuple of expressions. Each value is assigned to its respective variable. All the expressions on the right side are evaluated before any of the assignments.

The number of variables on the left and the number of values on the right have to be the same:

>>> a, b = 1, 2, 3 ValueError: too many values to unpack

More generally, the right side can be any kind of sequence (string, list or tuple). For example, to split an email address into a user name and a domain, you could write:

```
>>> addr = 'monty@python.org'
>>> uname, domain = addr.split('@')
```

The return value from split is a list with two elements; the first element is assigned to uname, the second to domain.

>>> print uname
monty
>>> print domain
python.org

11.3 Tuples as return values

Strictly speaking, a function can only return one value, but if the value is a tuple, the effect is the same as returning multiple values. For example, if you want to divide two integers and compute the quotient and remainder, it is inefficient to compute x/y and then x%y. It is better to compute them both at the same time.

The built-in function divmod takes two arguments and returns a tuple of two values, the quotient and remainder. You can store the result as a tuple:

```
>>> t = divmod(7, 3)
>>> print t
(2, 1)
```

Or use tuple assignment to store the elements separately:

```
>>> quot, rem = divmod(7, 3)
>>> print quot
2
>>> print rem
1
```

Here is an example of a function that returns a tuple:

```
def min_max(t):
    return min(t), max(t)
```

max and min are built-in functions that find the largest and smallest elements of a sequence. min_max computes both and returns a tuple of two values.

11.4 Variable-length argument tuples

Functions can take a variable number of arguments. A parameter name that begins with * **gathers** arguments into a tuple. For example, printall takes any number of arguments and prints them:

```
def printall(*args):
    print args
```

The gather parameter can have any name you like, but args is conventional. Here's how the function works:

```
>>> printall(1, 2.0, '3')
(1, 2.0, '3')
```

You can combine the gather operator with required and positional arguments:

```
def pointless(required, optional=0, *args):
    print required, optional, args
```

Run this function with 1, 2, 3 and 4 or more arguments and make sure you understand what it does.

The complement of gather is **scatter**. If you have a sequence of values and you want to pass it to a function as multiple arguments, you can use the * operator. For example, divmod takes exactly two arguments; it doesn't work with a tuple:

```
>>> t = (7, 3)
>>> divmod(t)
TypeError: divmod expected 2 arguments, got 1
```

But if you scatter the tuple, it works:

>>> divmod(*t) (2, 1)

11.4.1 Exercise 1

Many of the built-in functions use variable-length argument tuples. For example, **'max'** and **'min'** can take any number of arguments:

```
''>>> max(1,2,3)
3
''
But 'sum' does not.
''>>> sum(1,2,3)
TypeError: sum expected at most 2 arguments, got 3
```

Write a function called 'sumall' that takes any number of arguments and returns their sum.

11.5 Lists and tuples

zip is a built-in function that takes two or more sequences and "zips" them into a list1 of tuples where each tuple contains one element from each sequence.

This example zips a string and a list:

```
>>> s = 'abc'
>>> t = [0, 1, 2]
>>> zip(s, t)
[('a', 0), ('b', 1), ('c', 2)]
```

The result is a list of tuples where each tuple contains a character from the string and the corresponding element from the list.

If the sequences are not the same length, the result has the length of the shorter one.

>>> zip('Anne', 'Elk') [('A', 'E'), ('n', 'l'), ('n', 'k')]

You can use tuple assignment in a for loop to traverse a list of tuples:

```
t = [('a', 0), ('b', 1), ('c', 2)]
for letter, number in t:
    print number, letter
```

Each time through the loop, Python selects the next tuple in the list and assigns the elements to letter and number. The output of this loop is:

0 a 1 b 2 c

If you combine zip, for and tuple assignment, you get a useful idiom for traversing two (or more) sequences at the same time. For example, has_match takes two sequences, t1 and t2, and returns True if there is an index i such that t1[i] == t2[i]:

```
def has_match(t1, t2):
    for x, y in zip(t1, t2):
        if x == y:
            return True
    return False
```

If you need to traverse the elements of a sequence and their indices, you can use the built-in function enumerate:

```
for index, element in enumerate('abc'):
    print index, element
```

The output of this loop is:

0 a 1 b 2 c

Again.

11.6 Dictionaries and tuples

Dictionaries have a method called items that returns a list of tuples, where each tuple is a key-value pair2.

```
>>> d = {'a':0, 'b':1, 'c':2}
>>> t = d.items()
>>> print t
[('a', 0), ('c', 2), ('b', 1)]
```

As you should expect from a dictionary, the items are in no particular order.

Conversely, you can use a list of tuples to initialize a new dictionary:

>>> t = [('a', 0), ('c', 2), ('b', 1)]
>>> d = dict(t)
>>> print d
{'a': 0, 'c': 2, 'b': 1}

Combining dict with zip yields a concise way to create a dictionary:

```
>>> d = dict(zip('abc', range(3)))
>>> print d
{'a': 0, 'c': 2, 'b': 1}
```

The dictionary method update also takes a list of tuples and adds them, as key-value pairs, to an existing dictionary.

Combining items, tuple assignment and for, you get the idiom for traversing the keys and values of a dictionary:

```
for key, val in d.items():
    print val, key
```

The output of this loop is:

0 a 2 c 1 b

Again.

It is common to use tuples as keys in dictionaries (primarily because you can't use lists). For example, a telephone directory might map from last-name, first-name pairs to telephone numbers. Assuming that we have defined last, first and number, we could write:

```
directory[last,first] = number
```

The expression in brackets is a tuple. We could use tuple assignment to traverse this dictionary.

```
for last, first in directory:
    print first, last, directory[last,first]
```

This loop traverses the keys in directory, which are tuples. It assigns the elements of each tuple to last and first, then prints the name and corresponding telephone number.

There are two ways to represent tuples in a state diagram. The more detailed version shows the indices and elements just as they appear in a list. For example, the tuple ('Cleese', 'John') would appear:

But in a larger diagram you might want to leave out the details. For example, a diagram of the telephone directory might appear:

Here the tuples are shown using Python syntax as a graphical shorthand.

The telephone number in the diagram is the complaints line for the BBC, so please don't call it.

11.7 Comparing tuples

The comparison operators work with tuples and other sequences; Python starts by comparing the first element from each sequence. If they are equal, it goes on to the next elements, and so on, until it finds elements that differ. Subsequent elements are not considered (even if they are really big).

>>> (0, 1, 2) < (0, 3, 4) True >>> (0, 1, 200000) < (0, 3, 4) True

The sort function works the same way. It sorts primarily by first element, but in the case of a tie, it sorts by second element, and so on.

This feature lends itself to a pattern called **DSU** for **Decorate** a sequence by building a list of tuples with one or more sort keys preceding the elements from the sequence,**Sort** the list of tuples, and**Undecorate** by extracting the sorted elements of the sequence.

For example, suppose you have a list of words and you want to sort them from longest to shortest:

```
def sort_by_length(words):
    t = []
    for word in words:
        t.append((len(word), word))
    t.sort(reverse=True)
    res = []
    for length, word in t:
        res.append(word)
    return res
```

The first loop builds a list of tuples, where each tuple is a word preceded by its length.

sort compares the first element, length, first, and only considers the second element to break ties. The keyword argument reverse=True tells sort to go in decreasing order.

The second loop traverses the list of tuples and builds a list of words in descending order of length.

11.7.1 Exercise 2

In this example, ties are broken by comparing words, so words with the same length appear in alphabetical order. For other applications you might want to break ties at random. Modify this example so that words with the same length appear in random order. Hint: see the **'random'** function in the **'random'** module.

11.8 Sequences of sequences

I have focused on lists of tuples, but almost all of the examples in this chapter also work with lists of lists, tuples of tuples, and tuples of lists. To avoid enumerating the possible combinations, it is sometimes easier to talk about sequences of sequences.

In many contexts, the different kinds of sequences (strings, lists and tuples) can be used interchangeably. So how and why do you choose one over the others?

To start with the obvious, strings are more limited than other sequences because the elements have to be characters. They are also immutable. If you need the ability to change the characters in a string (as opposed to creating a new string), you might want to use a list of characters instead. Lists are more common than tuples, mostly because they are mutable. But there are a few cases where you might prefer tuples:

- In some contexts, like a return statement, it is syntactically simpler to create a tuple than a list. In other contexts, you might prefer a list.
- If you want to use a sequence as a dictionary key, you have to use an immutable type like a tuple or string.
- If you are passing a sequence as an argument to a function, using tuples reduces the potential for unexpected behavior due to aliasing.

Because tuples are immutable, they don't provide methods like sort and reverse, which modify existing lists. But Python provides the built-in functions sorted and reversed, which take any sequence as a parameter and return a new list with the same elements in a different order.

11.9 Debugging

Lists, dictionaries and tuples are known generically as **data** structures; in this chapter we are starting to see compound data structures, like lists of tuples, and dictionaries that contain tuples as keys and lists as values. Compound data structures are useful, but they are prone to what I call shape errors; that is, errors caused when a data structure has the wrong type, size or composition. For example, if you are expecting a list with one integer and I give you a plain old integer (not in a list), it won't work.

To help debug these kinds of errors, I have written a module called structshape that provides a function, also called structshape, that takes any kind of data structure as an argument and returns a string that summarizes its shape. You can download it from thinkpython.com/code/structshape.py

Here's the result for a simple list:

```
>>> from structshape import structshape
>>> t = [1,2,3]
>>> print structshape(t)
list of 3 int
```

A fancier program might write "list of 3 ints," but it was easier not to deal with plurals. Here's a list of lists:

>>> t2 = [[1,2], [3,4], [5,6]]
>>> print structshape(t2)
list of 3 list of 2 int

If the elements of the list are not the same type, structshape groups them, in order, by type:

>>> t3 = [1, 2, 3, 4.0, '5', '6', [7], [8], 9]
>>> print structshape(t3)
list of (3 int, float, 2 str, 2 list of int, int)

Here's a list of tuples:

```
>>> s = 'abc'
>>> lt = zip(t, s)
>>> print structshape(lt)
list of 3 tuple of (int, str)
```

And here's a dictionary with 3 items that map integers to strings.

>>> d = dict(lt)
>>> print structshape(d)
dict of 3 int->str

If you are having trouble keeping track of your data structures, structshape can help.

11.10 Glossary

tuple: An immutable sequence of elements. **tuple assignment:** An assignment with a sequence on the right and a tuple of variables on the left. The right is evaluated and then its elements are assigned to the variables on the left.

gather: The operation of assembling a variable-length argument tuple. scatter: The operation of treating a sequence as a list of arguments. **DSU**: Abbreviation of "decorate-sort-undecorate," a pattern that involves building a list of tuples, sorting, and extracting part of the result. data structure: A collection of related values, often organized in lists, dictionaries, tuples, etc. shape (of a data structure): A summary of the type, size and composition of a data structure.

11.11 Exercises

11.11.1 Exercise 3

Write a function called most_frequent that takes a string and prints the letters in decreasing order of frequency. Find text samples from several different languages and see how letter frequency varies between languages. Compare your results with the tables at 'wikipedia.org/wiki/Letter_frequencies'.

11.11.2 Exercise 4

More anagrams!

• Write a program

that reads a word list from a file (see Section '9.1') and prints all the sets of words that are anagrams. *Here is an example of what the output might look like:*

```
''['deltas', 'desalt', 'lasted', 'salted', 'slated', 'staled']
['retainers', 'ternaries']
['generating', 'greatening']
['resmelts', 'smelters', 'termless']
```

Hint: you might want to build a dictionary that maps from a set of letters to a list of words that can be spelled with those letters. The question is, how can you represent the set of letters in a way that can be used as a key?

• Modify the previous program so that it prints the largest set

of anagrams first, followed by the second largest set, and so on.

• In Scrabble a "bingo" is when you play all seven tiles in

your rack, along with a letter on the board, to form an eight-letter word. What set of 8 letters forms the most possible bingos? Hint: there are seven.

• 'Two words form a "metathesis pair" if you can transform one

into the other by swapping two letters''3''; for example, "converse" and "conserve." Write a program that finds all of the metathesis pairs in the dictionary. Hint: don't test all pairs of words, and don't test all possible swaps.' 'You can download a solution from *thinkpython.com/code/anagram_sets.py.*'

11.11.3 Exercise 5

Here's another Car Talk Puzzler4: What is the longest English word, that remains a valid English word, as you remove its letters one at a time? Now, letters can be removed from either end, or the middle, but you can't rearrange any of the letters. Every time you drop a letter, you wind up with another English word. If you do that, you're eventually going to wind up with one letter and that too is going to be an English word—one that's found in the dictionary. I want to know what's the longest word and how many letters does it have?

I'm going to give you a little modest example: Sprite. Ok? You start off with sprite, you take a letter off, one from the interior of the word, take the r away, and we're left with the word spite, then we take the e off the end, we're left with spit, we take the s off, we're left with pit, it, and I.

Write a program to find all words that can be reduced in this way, and then find the longest one.

This exercise is a little more challenging than most, so here are some suggestions:

• You might want to write a function that takes a word and

computes a list of all the words that can be formed by removing one letter. These are the "children" of the word.

• Recursively, a word is reducible if any of its children

are reducible. As a base case, you can consider the empty string reducible.

• The wordlist I provided, 'words.txt', doesn't

contain single letter words. So you might want to add "I", "a", and the empty string.

• To improve the performance of your program, you might want

to memoize the words that are known to be reducible.

You can see my solution at 'thinkpython.com/code/reducible.py'.

1In Python 3.0, zip returns an iterator of tuples, but for most purposes, an iterator behaves like a list. 2This behavior is slightly different in Python 3.0. 3This exercise is inspired by an example at puzzlers.org. 4 www.cartalk.com/content/puzzler/transcripts/200651

```
= Case study: data structure selection}
```

11.12 Word frequency analysis

As usual, you should at least attempt the following exercises before you read my solutions.

11.12.1 Exercise 1

Write a program that reads a file, breaks each line into words, strips whitespace and punctuation from the words, and converts them to lowercase.

Hint: The 'string' module provides strings named 'whitespace', which contains space, tab, newline, etc., and 'punctuation' which contains the punctuation characters. Let's see if we can make Python swear:

```
>>> import string
>>> print string.punctuation
!"#$%&,()*+,-./:;<=>?@[\]^___{|}~
```

Also, you might consider using the string methods 'strip', 'replace' and 'translate'.

11.12.2 Exercise 2

Go to Project Gutenberg ('gutenberg.org') and download your favorite out-of-copyright book in plain text format.

Modify your program from the previous exercise to read the book you downloaded, skip over the header information at the beginning of the file, and process the rest of the words as before.

Then modify the program to count the total number of words in the book, and the number of times each word is used.

Print the number of different words used in the book. Compare different books by different authors, written in different eras. Which author uses the most extensive vocabulary?

11.12.3 Exercise 3

Modify the program from the previous exercise to print the 20 most frequently-used words in the book.

11.12.4 Exercise 4

Modify the previous program to read a word list (see Section '9.1') and then print all the words in the book that are not in the word list. How many of them are typos? How many of them are common words that *should* be in the word list, and how many of them are really obscure?

11.13 Random numbers

Given the same inputs, most computer programs generate the same outputs every time, so they are said to be **deterministic**. Determinism is usually a good thing, since we expect the same calculation to yield the same result. For some applications, though, we want the computer to be unpredictable. Games are an obvious example, but there are more.

Making a program truly nondeterministic turns out to be not so easy, but there are ways to make it at least seem nondeterministic. One of them is to use algorithms that generate **pseudorandom** numbers. Pseudorandom numbers are not truly random because they are generated by a deterministic computation, but just by looking at the numbers it is all but impossible to distinguish them from random.

The random module provides functions that generate pseudorandom numbers (which I will simply call "random" from here on).

The function random returns a random float between 0.0 and 1.0 (including 0.0 but not 1.0). Each time you call random, you get the next number in a long series. To see a sample, run this loop:

```
import random
for i in range(10):
    x = random.random()
    print x
```

The function randint takes parameters low and high and returns an integer between low and high (including both).

```
>>> random.randint(5, 10)
5
>>> random.randint(5, 10)
9
```

To choose an element from a sequence at random, you can use choice:

```
>>> t = [1, 2, 3]
>>> random.choice(t)
2
>>> random.choice(t)
3
```

The random module also provides functions to generate random values from continuous distributions including Gaussian, exponential, gamma, and a few more.

11.13.1 Exercise 5

Write a function named choose_from_histhat takes a histogram as defined in Section '11.1' and returns a random value from the histogram, chosen with probability in proportion to frequency. For example, for this histogram:

```
''>>> t = ['a', 'a', 'b']
>>> h = histogram(t)
>>> print h
{'a': 2, 'b': 1}
''
```

your function should "a" with probability '2/3' and b with probability '1/3'.

11.14 Word histogram

Here is a program that reads a file and builds a histogram of the words in the file:

```
import string
```

```
def process_file(filename):
    h = dict()
    fp = open(filename)
    for line in fp:
        process_line(line, h)
    return h
def process_line(line, h):
    line = line.replace('-', ' ')
    for word in line.split():
        word = word.strip(string.punctuation + string.whitespace)
        word = word.lower()
        h[word] = h.get(word, 0) + 1
hist = process_file('emma.txt')
```

This program reads emma.txt, which contains the text of *Emma* by Jane Austen.

process_file loops through the lines of the file, passing them one at a time to process_line. The histogram h is being used as an accumulator.

process_line uses the string method replace to replace hyphens with spaces before using split to break the line into a list of strings. It traverses the list of words and uses strip and lower to remove punctuation and convert to lower case. (It is a shorthand to say that strings are "converted;" remember that string are immutable, so methods like strip and lower return new strings.)

Finally, process_line updates the histogram by creating a new item or incrementing an existing one.

To count the total number of words in the file, we can add up the frequencies in the histogram:

```
def total_words(h):
    return sum(h.values())
```

The number of different words is just the number of items in the dictionary:

def different_words(h):
 return len(h)

Here is some code to print the results:

```
print 'Total number of words:', total_words(hist)
print 'Number of different words:', different_words(hist)
```

And the results:

```
Total number of words: 161073
Number of different words: 7212
```

11.15 Most common words

To find the most common words, we can apply the DSU pattern; most_common takes a histogram and returns a list of word-frequency tuples, sorted in reverse order by frequency:

```
def most_common(h):
    t = []
    for key, value in h.items():
        t.append((value, key))
    t.sort(reverse=True)
    return t
```

Here is a loop that prints the ten most common words:

t = most_common(hist)
print 'The most common words are:'
for freq, word in t[0:10]:
 print word, '\t', freq

And here are the results from *Emma*:

The most common words are: 5242 to the 5204 and4897 4293 of i 3191 3130 а it 2529 her 2483 was 2400 she 2364

11.16 Optional parameters

We have seen built-in functions and methods that take a variable number of arguments. It is possible to write user-defined functions with optional arguments, too. For example, here is a function that prints the most common words in a histogram

```
def print_most_common(hist, num=10)
   t = most_common(hist)
   print 'The most common words are:'
   for freq, word in t[0:num]:
        print word, '\t', freq
```

The first parameter is required; the second is optional. The **default value** of num is 10.

If you only provide one argument:

print_most_common(hist)

num gets the default value. If you provide two arguments:

print_most_common(hist, 20)

num gets the value of the argument instead. In other words, the optional argument **overrides** the default value.

If a function has both required and optional parameters, all the required parameters have to come first, followed by the optional ones.

11.17 Dictionary subtraction

Finding the words from the book that are not in the word list from words.txt is a problem you might recognize as set subtraction; that is, we want to find all the words from one set (the words in the book) that are not in another set (the words in the list).

subtract takes dictionaries d1 and d2 and returns a new dictionary that contains all the keys from d1 that are not in d2. Since we don't really care about the values, we set them all to None.

```
def subtract(d1, d2):
    res = dict()
    for key in d1:
        if key not in d2:
        res[key] = None
    return res
```

To find the words in the book that are not in words.txt, we can use process_file to build a histogram for words.txt, and then subtract:

```
words = process_file('words.txt')
diff = subtract(hist, words)
print "The words in the book that aren't in the word list are:"
for word in diff.keys():
    print word,
```

Here are some of the results from *Emma*:

```
The words in the book that aren't in the word list are:
rencontre jane's blanche woodhouses disingenuousness
friend's venice apartment ...
```

Some of these words are names and possessives. Others, like "rencontre," are no longer in common use. But a few are common words that should really be in the list!

11.17.1 Exercise 6

Python provides a data structure called 'set' that provides many common set operations. Read the documentation at 'docs.python.org/lib/types-set.html' and write a program that uses set subtraction to find words in the book that are not in the word list.

11.18 Random words

To choose a random word from the histogram, the simplest algorithm is to build a list with multiple copies of each word, according to the observed frequency, and then choose from the list:

```
def random_word(h):
    t = []
    for word, freq in h.items():
        t.extend([word] * freq)
    return random.choice(t)
```

The expression [word] * freq creates a list with freq copies of the string word. The extend method is similar to append except that the argument is a sequence.

11.18.1 Exercise 7

This algorithm works, but it is not very efficient; each time you choose a random word, it rebuilds the list, which is as big as the original book. An obvious improvement is to build the list once and then make multiple selections, but the list is still big.

An alternative is:

- Use 'keys' to get a list of the words in the book.
- Build a list that contains the cumulative sum of the word

frequencies (see Exercise '10.1'). The last item in this list is the total number of words in the book, 'n'.

• Choose a random number from 1 to 'n'. Use a bisection search

(See Exercise '10.8') to find the index where the random number would be inserted in the cumulative sum.

• Use the index to find the corresponding word in the word list.

Write a program that uses this algorithm to choose a random word from the book.

11.19 Markov analysis

If you choose words from the book at random, you can get a sense of the vocabulary, you probably won't get a sentence:

this the small regard harriet which knightley's it most things

A series of random words seldom makes sense because there is no relationship between successive words. For example, in a real sentence you would expect an article like "the" to be followed by an adjective or a noun, and probably not a verb or adverb.

One way to measure these kinds of relationships is Markov analysis, which characterizes, for a given sequence of words, the probability of the word that comes next. For example, the song *Eric*, the Half a Bee begins:

Half a bee, philosophically,

Must, ipso facto, half not be.

But half the bee has got to be

Vis a vis, its entity. D'you see?

But can a bee be said to be

Or not to be an entire bee

When half the bee is not a bee

Due to some ancient injury?

In this text, the phrase "half the" is always followed by the word "bee," but the phrase "the bee" might be followed by either "has" or "is".

The result of Markov analysis is a mapping from each prefix (like "half the" and "the bee") to all possible suffixes (like "has" and "is").

Given this mapping, you can generate a random text by starting with any prefix and choosing at random from the possible suffixes. Next, you can combine the end of the prefix and the new suffix to form the next prefix, and repeat.

For example, if you start with the prefix "Half a," then the next word has to be "bee," because the prefix only appears once in the text. The next prefix is "a bee," so the next suffix might be "philosophically," "be" or "due."

In this example the length of the prefix is always two, but you can do Markov analysis with any prefix length. The length of the prefix is called the "order" of the analysis.

11.19.1 Exercise 8

Markov analysis:

- Write a program to read a text from a file and perform Markov analysis. The result should be a dictionary that maps from prefixes to a collection of possible suffixes. The collection might be a list, tuple, or dictionary; it is up to you to make an appropriate choice. You can test your program with prefix length two, but you should write the program in a way that makes it easy to try other lengths.
- Add a function to the previous program to generate random text based on the Markov analysis. Here is an example from Emmawith prefix length 2:

He was very clever, be it sweetness or be angry, ashamed or only amused, at such a stroke. She had never thought of Hannah till you were never meant for me?" "I cannot make speeches, Emma:" he soon cut it all himself.

For this example, I left the punctuation attached to the words. The result is almost syntactically correct, but not quite. Semantically, it almost makes sense, but not quite.

- What happens if you increase the prefix length? Does the random text make more sense?
- Once your program is working, you might want to try a mash-up: if you analyze text from two or more books, the random text you generate will blend the vocabulary and phrases from the sources in interesting ways.

11.20 Data structures

Using Markov analysis to generate random text is fun, but there is also a point to this exercise: data structure selection. In your solution to the previous exercises, you had to choose:

- How to represent the prefixes.
- How to represent the collection of possible suffixes.
- How to represent the mapping from each prefix to the collection of possible suffixes.

Ok, the last one is the easy; the only mapping type we have seen is a dictionary, so it is the natural choice.

For the prefixes, the most obvious options are string, list of strings, or tuple of strings. For the suffixes, one option is a list; another is a histogram (dictionary).

How should you choose? The first step is to think about the operations you will need to implement for each data structure. For the prefixes, we need to be able to remove words from the beginning and add to the end. For example, if the current prefix is "Half a," and the next word is "bee," you need to be able to form the next prefix, "a bee."

Your first choice might be a list, since it is easy to add and remove elements, but we also need to be able to use the prefixes as keys in a dictionary, so that rules out lists. With tuples, you can't append or remove, but you can use the addition operator to form a new tuple:

```
def shift(prefix, word):
    return prefix[1:] + (word,)
```

shift takes a tuple of words, prefix, and a string, word, and forms a new tuple that has all the words in prefix except the first, and word added to the end.

For the collection of suffixes, the operations we need to perform include adding a new suffix (or increasing the frequency of an existing one), and choosing a random suffix.

Adding a new suffix is equally easy for the list implementation or the histogram. Choosing a random element from a list is easy; choosing from a histogram is harder to do efficiently (see Exercise 13.7).

So far we have been talking mostly about ease of implementation, but there are other factors to consider in choosing data structures. One is run time. Sometimes there is a theoretical reason to expect one data structure to be faster than other; for example, I mentioned that the in operator is faster for dictionaries than for lists, at least when the number of elements is large.

But often you don't know ahead of time which implementation will be faster. One option is to implement both of them and see which is better. This approach is called **benchmarking**. A practical alternative is to choose the data structure that is easiest to implement, and then see if it is fast enough for the intended application. If so, there is no need to go on. If not, there are tools, like the profile module, that can identify the places in a program that take the most time.

The other factor to consider is storage space. For example, using a histogram for the collection of suffixes might take less space because you only have to store each word once, no matter how many times it appears in the text. In some cases, saving space can also make your program run faster, and in the extreme, your program might not run at all if you run out of memory. But for many applications, space is a secondary consideration after run time.

One final thought: in this discussion, I have implied that we should use one data structure for both analysis and generation. But since these are separate phases, it would also be possible to use one structure for analysis and then convert to another structure for generation. This would be a net win if the time saved during generation exceeded the time spent in conversion.

11.21 Debugging

When you are debugging a program, and especially if you are working on a hard bug, there are four things to try: **reading:** Examine your code, read it back to yourself, and check that it says what you meant to say.**running:** Experiment by making changes and running different versions. Often if you display the right thing at the right place in the program, the problem becomes obvious, but sometimes you have to spend some time to build scaffolding.**ruminating:** Take some time to think! What kind of error is it: syntax, runtime, semantic? What information can you get from the error messages, or from the output of the program? What kind of error could cause the problem you're seeing? What did you change last, before the problem appeared?**retreating:** At some point, the best thing to do is back off, undoing recent changes, until you get back to a program that works and that you understand. Then you can starting rebuilding. Beginning programmers sometimes get stuck on one of these activities and forget the others. Each activity comes with its own failure mode.

For example, reading your code might help if the problem is a typographical error, but not if the problem is a conceptual misunderstanding. If you don't understand what your program does, you can read it 100 times and never see the error, because the error is in your head.

Running experiments can help, especially if you run small, simple tests. But if you run experiments without thinking or reading your code, you might fall into a pattern I call "random walk programming," which is the process of making random changes until the program does the right thing. Needless to say, random walk programming can take a long time.

You have to take time to think. Debugging is like an experimental science. You should have at least one hypothesis about what the problem is. If there are two or more possibilities, try to think of a test that would eliminate one of them.

Taking a break helps with the thinking. So does talking. If you explain the problem to someone else (or even yourself), you will sometimes find the answer before you finish asking the question.

But even the best debugging techniques will fail if there are too many errors, or if the code you are trying to fix is too big and complicated. Sometimes the best option is to retreat, simplifying the program until you get to something that works and that you understand.

Beginning programmers are often reluctant to retreat because they can't stand to delete a line of code (even if it's wrong). If it makes you feel better, copy your program into another file before you start stripping it down. Then you can paste the pieces back in a little bit at a time.

Finding a hard bug requires reading, running, running, and sometimes retreating. If you get stuck on one of these activities, try the others.

11.22 Glossary

deterministic: Pertaining to a program that does the same thing each time it runs, given the same inputs. **pseudorandom:** Pertaining to a sequence of numbers that appear to be random, but are generated by a deterministic program. **default value:** The value given to an optional parameter if no argument is provided. **override:** To replace a default value with an argument. **benchmarking:** The process of choosing between data structures by implementing alternatives and testing them on a sample of the possible inputs.

11.23 Exercises

11.23.1 Exercise 9

The "rank" of a word is its position in a list of words sorted by frequency: the most common word has rank 1, the second most common has rank 2, etc.

Zipf's law describes a relationship between the ranks and frequencies of words in natural languages 1. Specifically, it predicts that the frequency, 'f', of the word with rank 'r' is: f = c r - s

where \mathbf{s}' and \mathbf{c}' are parameters that depend on the language and the text. If you take the logarithm of both sides of this equation, you get:

11.24 Persistence

Most of the programs we have seen so far are transient in the sense that they run for a short time and produce some output, but when they end, their data disappears. If you run the program again, it starts with a clean slate.

Other programs are **persistent**: they run for a long time (or all the time); they keep at least some of their data in permanent storage (a hard drive, for example); and if they shut down and restart, they pick up where they left off.

Examples of persistent programs are operating systems, which run pretty much whenever a computer is on, and web servers, which run all the time, waiting for requests to come in on the network.

One of the simplest ways for programs to maintain their data is by reading and writing text files. We have already seen programs that read text files; in this chapters we will see programs that write them.

An alternative is to store the state of the program in a database. In this chapter I will present a simple database and a module, pickle, that makes it easy to store program data.

11.25 Reading and writing

A text file is a sequence of characters stored on a permanent medium like a hard drive, flash memory, or CD-ROM. We saw how to open and read a file in Section 9.1.

To write a file, you have to open it with mode 'w' as a second parameter:

```
>>> fout = open('output.txt', 'w')
>>> print fout
<open file 'output.txt', mode 'w' at 0xb7eb2410>
```

If the file already exists, opening it in write mode clears out the old data and starts fresh, so be careful! If the file doesn't exist, a new one is created.

The write method puts data into the file.

```
>>> line1 = "This here's the wattle,\n"
>>> fout.write(line1)
```

Again, the file object keeps track of where it is, so if you call write again, it adds the new data to the end.

>>> line2 = "the emblem of our land.\n"
>>> fout.write(line2)

When you are done writing, you have to close the file.

>>> fout.close()

11.26 Format operator

The argument of write has to be a string, so if we want to put other values in a file, we have to convert them to strings. The easiest way to do that is with str:

>>> x = 52 >>> f.write(str(x))

An alternative is to use the **format operator**, %. When applied to integers, % is the modulus operator. But when the first operand is a string, % is the format operator.

The first operand is the **format string**, and the second operand is a tuple of expressions. The result is a string that contains the values of the expressions, formatted according to the format string.

As an example, the **format sequence** '%d' means that the first expression in the tuple should be formatted as an integer (d stands for "decimal"):

```
>>> camels = 42
>>> '%d' % camels
'42'
```

The result is the string '42', which is not to be confused with the integer value 42.

A format sequence can appear anywhere in the format string, so you can embed a value in a sentence:

```
>>> camels = 42
>>> 'I have spotted %d camels.' % camels
'I have spotted 42 camels.'
```

The format sequence '%g' formats the next element in the tuple as a floating-point number (don't ask why), and '%s' formats the next item as a string:

```
>>> 'In %d years I have spotted %g %s.' % (3, 0.1, 'camels') 'In 3 years I have spotted 0.1 camels.'
```

The number of elements in the tuple has to match the number of format sequences in the string. Also, the types of the elements have to match the format sequences:

```
>>> '%d %d %d' % (1, 2)
TypeError: not enough arguments for format string
>>> '%d' % 'dollars'
TypeError: illegal argument type for built-in operation
```

In the first example, there aren't enough elements; in the second, the element is the wrong type.

The format operator is powerful but difficult to use. You can read more about it at docs.python.org/lib/typesseq-strings.html.

11.27 Filenames and paths

Files are organized into **directories** (also called "folders"). Every running program has a "current directory," which is the default directory for most operations. For example, when you open a file for reading, Python looks for it in the current directory.

The os module provides functions for working with files and directories ("os" stands for "operating system"). os.getcwd returns the name of the current directory:

```
>>> import os
>>> cwd = os.getcwd()
>>> print cwd
/home/dinsdale
```

cwd stands for "current working directory." The result in this example is /home/dinsdale, which is the home directory of a user named dinsdale.

A string like cwd that identifies a file is called a **path**. A **relative path** starts from the current directory; an **absolute path** starts from the topmost directory in the file system.

The paths we have seen so far are simple filenames, so they are relative to the current directory. To find the absolute path to a file, you can use os.path.abspath:

```
>>> os.path.abspath('memo.txt')
'/home/dinsdale/memo.txt'
```

os.path.exists checks whether a file or directory exists:

```
>>> os.path.exists('memo.txt')
True
```

If it exists, os.path.isdir checks whether it's a directory:

```
>>> os.path.isdir('memo.txt')
False
>>> os.path.isdir('music')
True
```

Similarly, os.path.isfile checks whether it's a file.

os.listdir returns a list of the files (and other directories) in the given directory:

```
>>> os.listdir(cwd)
['music', 'photos', 'memo.txt']
```

To demonstrate these functions, the following example "walks" through a directory, prints the names of all the files, and calls itself recursively on all the directories.

```
def walk(<u>dir</u>):
    for name in os.listdir(<u>dir</u>):
        path = os.path.join(<u>dir</u>, name)
        if os.path.isfile(path):
            print path
        else:
            walk(path)
```

os.path.join takes a directory and a file name and joins them into a complete path.

11.27.1 Exercise 1

Modify 'walk' so that instead of printing the names of the files, it returns a list of names. *Exercise 2* The 'os' module provides a function called 'walk' that is similar to this one but more versatile. Read the documentation and use it to print the names of the files in a given directory and its subdirectories.

11.28 Catching exceptions

A lot of things can go wrong when you try to read and write files. If you try to open a file that doesn't exist, you get an IOError:

```
>>> fin = open('bad_file')
IOError: [Errno 2] No such file or directory: 'bad_file'
```

If you don't have permission to access a file:

```
>>> fout = open('/etc/passwd', 'w')
IOError: [Errno 13] Permission denied: '/etc/passwd'
```

And if you try to open a directory for reading, you get

>>> fin = open('/home')
IOError: [Errno 21] Is a directory

To avoid these errors, you could use functions like os.path.exists and os.path.isfile, but it would take a lot of time and code to check all the possibilities (if "Errno 21" is any indication, there are at least 21 things that can go wrong).

It is better to go ahead and try, and deal with problems if they happen, which is exactly what the try statement does. The syntax is similar to an if statement:

```
try:
    fin = open('bad_file')
    for line in fin:
        print line
    fin.close()
except:
    print 'Something went wrong.'
```

Python starts by executing the try clause. If all goes well, it skips the except clause and proceeds. If an exception occurs, it jumps out of the try clause and executes the except clause.

Handling an exception with a try statement is called **catching** an exception. In this example, the except clause prints an error message that is not very helpful. In general, catching an exception gives you a chance to fix the problem, or try again, or at least end the program gracefully.

11.29 Databases

A **database** is a file that is organized for storing data. Most databases are organized like a dictionary in the sense that they map from keys to values. The biggest difference is that the database is on disk (or other permanent storage), so it persists after the program ends.

The module anydom provides an interface for creating and updating database files. As an example, I'll create a database that contains captions for image files.

Opening a database is similar to opening other files:

```
>>> import anydbm
>>> db = anydbm.open('captions.db', 'c')
```

The mode 'c' means that the database should be created if it doesn't already exist. The result is a database object that can be used (for most operations) like a dictionary. If you create a new item, anydbm updates the database file.

>>> db['cleese.png'] = 'Photo of John Cleese.'

When you access one of the items, anydbm reads the file:

```
>>> print db['cleese.png']
Photo of John Cleese.
```

If you make another assignment to an existing key, anydbm replaces the old value:

```
>>> db['cleese.png'] = 'Photo of John Cleese doing a silly walk.'
>>> print db['cleese.png']
Photo of John Cleese doing a silly walk.
```

Many dictionary methods, like keys and items, also work with database objects. So does iteration with a for statement.

for key in db: print key

As with other files, you should close the database when you are done:

>>> db.close()

11.30 Pickling

A limitation of anydbm is that the keys and values have to be strings. If you try to use any other type, you get an error.

The pickle module can help. It translates almost any type of object into a string suitable for storage in a database, and then translates strings back into objects.

pickle.dumps takes an object as a parameter and returns a string representation (dumps is short for "dump string"):

```
>>> import pickle
>>> t = [1, 2, 3]
>>> pickle.dumps(t)
'(lp0\nI1\naI2\naI3\na.'
```

The format isn't obvious to human readers; it is meant to be easy for pickle to interpret. pickle.loads ("load string") reconstitutes the object:

```
>>> t1 = [1, 2, 3]
>>> s = pickle.dumps(t1)
>>> t2 = pickle.loads(s)
>>> print t2
[1, 2, 3]
```

Although the new object has the same value as the old, it is not (in general) the same object:

```
>>> t == t2
True
>>> t is t2
False
```

In other words, pickling and then unpickling has the same effect as copying the object.

You can use pickle to store non-strings in a database. In fact, this combination is so common that it has been encapsulated in a module called shelve.

Exercise 3

If you did Exercise '12.4', modify your solution so that it creates a database that maps from each word in the list to a list of words that use the same set of letters.

Write a different program that opens the database and prints the contents in a human-readable format.

11.31 Pipes

Most operating systems provide a command-line interface, also known as a **shell**. Shells usually provide commands to navigate the file system and launch applications. For example, in Unix, you can change directories with cd, display the contents of a directory with ls, and launch a web browser by typing (for example) firefox.

Any program that you can launch from the shell can also be launched from Python using a **pipe**. A pipe is an object that represents a running process.

For example, the Unix command ls -l normally displays the contents of the current directory (in long format). You can launch ls with os.popen:

>>> cmd = 'ls -l' >>> fp = os.popen(cmd)

The argument is a string that contains a shell command. The return value is a file pointer that behaves just like an open file. You can read the output from the ls process one line at a time with readline or get the whole thing at once with read:

```
>>> res = fp.read()
```

When you are done, you close the pipe like a file:

```
>>> stat = fp.close()
>>> print stat
None
```

The return value is the final status of the ls process; None means that it ended normally (with no errors).

A common use of pipes is to read a compressed file incrementally; that is, without uncompressing the whole thing at once. The following function takes the name of a compressed file as a parameter and returns a pipe that uses gzip to decompress the contents:

```
def open_gzip(filename):
    cmd = 'gunzip -c ' + filename
    fp = os.popen(cmd)
    return fp
```

If you read lines from fp one at a time, you never have to store the uncompressed file in memory or on disk.

11.32 Writing modules

Any file that contains Python code can be imported as a module. For example, suppose you have a file named wc.py with the following code:

```
def linecount(filename):
    count = 0
    for line in open(filename):
        count += 1
    return count
```

```
print linecount('wc.py')
```

If you run this program, it reads itself and prints the number of lines in the file, which is 7. You can also import it like this:

>>> import wc 7 Now you have a module object wc:

>>> print wc <module 'wc' from 'wc.py'>

That provides a function called linecount:

```
>>> wc.linecount('wc.py')
7
```

So that's how you write modules in Python.

The only problem with this example is that when you import the module it executes the test code at the bottom. Normally when you import a module, it defines new functions but it doesn't execute them.

Programs that will be imported as modules often use the following idiom:

```
if __name__ == '__main__':
    print linecount('wc.py')
```

_____name____is a built-in variable that is set when the program starts. If the program is running as a script, _____name____has the value ____main____; in that case, the test code is executed. Otherwise, if the module is being imported, the test code is skipped. Exercise 4 Type this example into a file named 'wc.py' and run it as a script. Then run the Python interpreter and 'import wc'. What is the value of ______ when the module is being imported? Warning: If you import a module that has already been imported, Python does nothing. It does not re-read the file, even if it has changed.

If you want to reload a module, you can use the built-in function 'reload', but it can be tricky, so the safest thing to do is restart the interpreter and then import the module again.

11.33 Debugging

When you are reading and writing files, you might run into problems with whitespace. These errors can be hard to debug because spaces, tabs and newlines are normally invisible:

```
>>> s = '1 2\t 3\n 4'
>>> print s
1 2 3
4
```

The built-in function repr can help. It takes any object as an argument and returns a string representation of the object. For strings, it represents whitespace characters with backslash sequences:

>>> print repr(s) '1 2\t 3\n 4'

This can be helpful for debugging.

One other problem you might run into is that different systems use different characters to indicate the end of a line. Some systems use a newline, represented n. Others use a return

character, represented \r. Some use both. If you move files between different systems, these inconsistencies might cause problems.

For most systems, there are applications to convert from one format to another. You can find them (and read more about this issue) at wikipedia.org/wiki/Newline. Or, of course, you could write one yourself.

11.34 Glossary

persistent: Pertaining to a program that runs indefinitely and keeps at least some of its data in permanent storage. **format operator:** An operator, %, that takes a format string and a tuple and generates a string that includes the elements of the tuple formatted as specified by the format string. **format string:** A string, used with the format operator, that contains format sequences. **format sequence:** A sequence of characters in a format string, like %d, that specifies how a value should be formatted. **text file:** A sequence of characters stored in permanent storage like a hard drive. **directory:** A named collection of files, also called a folder. **path:** A string that identifies a file. **relative path:** A path that starts from the current directory. **absolute path:** A path that starts from the topmost directory in the file system. **catch:** To prevent an exception from terminating a program using the try and except statements. **database:** A file whose contents are organized like a dictionary with keys that correspond to values.

11.35 Exercises

Exercise 5 The 'urllib' module provides methods for manipulating URLs and downloading information from the web. The following example downloads and prints a secret message from 'thinkpython.com':

```
import urllib
conn = urllib.urlopen(,http://thinkpython.com/secret.html,)
for line in conn.fp:
    print line.strip()
```

Run this code and follow the instructions you see there.

Exercise 6

In a large collection of MP3 files, there may be more than one copy of the same song, stored in different directories or with different file names. The goal of this exercise is to search for these duplicates.

• Write a program that searches a directory and all of its

subdirectories, recursively, and returns a list of complete paths for all files with a given suffix (like '.mp3'). Hint: 'os.path' provides several useful functions for manipulating file and path names.

• To recognize duplicates, you can use a hash function that

reads the file and generates a short summary of the contents. For example, MD5 (Message-Digest algorithm 5) takes an arbitrarily-long "message" and returns a 128-bit "checksum." The probability is very small that two files with different contents will return the same checksum. You can read about MD5 at 'wikipedia.org/wiki/Md5'. On a Unix system you can use the program 'md5sum' and a pipe to compute checksums from Python.

Exercise 7

The Internet Movie Database (IMDb) is an online collection of information about movies. Their database is available in plain text format, so it is reasonably easy to read from Python. For this exercise, the files you need are 'actors.list.gz' and 'actresses.list.gz'; you can download them from 'www.imdb.com/interfaces#plain'.

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I have written a program that parses these files and splits them into actor names, movie titles, etc. You can download it from **'thinkpython.com/code/imdb.py**'.

If you run 'imdb.py' as a script, it reads 'actors.list.gz' and prints one actor-movie pair per line. Or, if you 'import imdb' you can use the function process_file to, well, process the file. The arguments are a filename, a function object and an optional number of lines to process. Here is an example:

''import imdb

```
def print_info(actor, date, title, role):
    print actor, date, title, role
imdb.process_file('actors.list.gz', print_info)
```

When you call process_file, it opens 'filename', reads the contents, and calls print_info once for each line in the file. print_info takes an actor, date, movie title and role as arguments and prints them.

• Write a program that reads 'actors.list.gz' and 'actresses.list.gz' and uses 'shelve' to build a database

that maps from each actor to a list of his or her films.

• Two actors are "costars" if they have been in at least one

movie together. Process the database you built in the previous step and build a second database that maps from each actor to a list of his or her costars.

• Write a program that can play the "Six Degrees of Kevin

Bacon," which you can read about at 'wikipedia.org/wiki/Six_Degrees_of_Kevin_-Bacon'. This problem is challenging because it requires you to find the shortest path in a graph. You can read about shortest path algorithms at 'wikipedia.org/wiki/Shortest_path_problem'.

12 Classes and objects

12.1 User-defined types

We have used many of Python's built-in types; now we are going to define a new type. As an example, we will create a type called Point that represents a point in two-dimensional space.

In mathematical notation, points are often written in parentheses with a comma separating the coordinates. For example, (0, 0) represents the origin, and (x, y) represents the point x units to the right and y units up from the origin.

There are several ways we might represent points in Python:

- We could store the coordinates separately in two variables, x and y.
- We could store the coordinates as elements in a list or tuple.
- We could create a new type to represent points as objects.

Creating a new type is (a little) more complicated than the other options, but it has advantages that will be apparent soon.

A user-defined type is also called a **class**. A class definition looks like this:

```
class Point(object):
    """represents a point in 2-D space"""
```

This header indicates that the new class is a Point, which is a kind of object, which is a built-in type.

The body is a docstring that explains what the class is for. You can define variables and functions inside a class definition, but we will get back to that later.

Defining a class named Point creates a class object.

```
>>> print Point
<class '__main__.Point'>
```

Because Point is defined at the top level, its "full name" is _____.Point.

The class object is like a factory for creating objects. To create a Point, you call Point as if it were a function.

```
>>> blank = Point()
>>> print blank
<__main__.Point instance at 0xb7e9d3ac>
```

The return value is a reference to a Point object, which we assign to blank. Creating a new object is called **instantiation**, and the object is an **instance** of the class.

When you print an instance, Python tells you what class it belongs to and where it is stored in memory (the prefix 0x means that the following number is in hexadecimal).

12.2 Attributes

You can assign values to an instance using dot notation:

```
>>> blank.x = 3.0
>>> blank.y = 4.0
```

This syntax is similar to the syntax for selecting a variable from a module, such as math.pi or string.whitespace. In this case, though, we are assigning values to named elements of an object. These elements are called **attributes**.

As a noun, "AT-trib-ute" is pronounced with emphasis on the first syllable, as opposed to "a-TRIB-ute," which is a verb.

The following diagram shows the result of these assignments. A state diagram that shows an object and its attributes is called an **object diagram**:

The variable blank refers to a Point object, which contains two attributes. Each attribute refers to a floating-point number.

You can read the value of an attribute using the same syntax:

```
>>> print blank.y
4.0
>>> x = blank.x
>>> print x
3.0
```

The expression blank.x means, "Go to the object blank refers to and get the value of x." In this case, we assign that value to a variable named x. There is no conflict between the variable x and the attribute x.

You can use dot notation as part of any expression. For example:

```
>>> print '(%g, %g)' % (blank.x, blank.y)
(3.0, 4.0)
>>> distance = math.sqrt(blank.x**2 + blank.y**2)
>>> print distance
5.0
```

You can pass an instance as an argument in the usual way. For example:

def print_point(p):
 print '(%g, %g)' % (p.x, p.y)

print_point takes a point as an argument and displays it in mathematical notation. To invoke it, you can pass blank as an argument:

>>> print_point(blank)
(3.0, 4.0)

Inside the function, p is an alias for blank, so if the function modifies p, blank changes.

12.2.1 Exercise 1

Write a function called 'distance' that it takes two Points as arguments and returns the distance between them.

12.3 Rectangles

Sometimes it is obvious what the attributes of an object should be, but other times you have to make decisions. For example, imagine you are designing a class to represent rectangles. What attributes would you use to specify the location and size of a rectangle? You can ignore angle; to keep things simple, assume that the rectangle is either vertical or horizontal.

There are at least two possibilities:

- You could specify one corner of the rectangle (or the center), the width, and the height.
- You could specify two opposing corners.

At this point it is hard to say whether either is better than the other, so we'll implement the first one, just as an example.

Here is the class definition:

```
class Rectangle(object):
    """represent a rectangle.
    attributes: width, height, corner.
    """
```

The docstring lists the attributes: width and height are numbers; corner is a Point object that specifies the lower-left corner.

To represent a rectangle, you have to instantiate a Rectangle object and assign values to the attributes:

```
box = Rectangle()
box.width = 100.0
box.height = 200.0
box.corner = Point()
box.corner.x = 0.0
box.corner.y = 0.0
```

The expression box.corner.x means, "Go to the object box refers to and select the attribute named corner; then go to that object and select the attribute named x."

The figure shows the state of this object:

An object that is an attribute of another object is **embedded**.

12.4 Instances as return values

Functions can return instances. For example, find_center takes a Rectangle as an argument and returns a Point that contains the coordinates of the center of the Rectangle:

```
def find_center(box):
    p = Point()
    p.x = box.corner.x + box.width/2.0
    p.y = box.corner.y + box.height/2.0
    return p
```

Here is an example that passes box as an argument and assigns the resulting Point to center:

```
>>> center = find_center(box)
>>> print_point(center)
(50.0, 100.0)
```

12.5 Objects are mutable

You can change the state of an object by making an assignment to one of its attributes. For example, to change the size of a rectangle without changing its position, you can modify the values of width and height:

box.width = box.width + 50
box.height = box.width + 100

You can also write functions that modify objects. For example, grow_rectangle takes a Rectangle object and two numbers, dwidth and dheight, and adds the numbers to the width and height of the rectangle:

```
def grow_rectangle(rect, dwidth, dheight) :
    rect.width += dwidth
    rect.height += dheight
```

Here is an example that demonstrates the effect:

```
>>> print box.width
100.0
>>> print box.height
200.0
>>> grow_rectangle(box, 50, 100)
>>> print box.width
150.0
>>> print box.height
300.0
```

Inside the function, rect is an alias for box, so if the function modifies rect, box changes.

12.5.1 Exercise 2

Write a function named move_rectangle that takes a Rectangle and two numbers named 'dx' and 'dy'. It should change the location of the rectangle by adding 'dx' to the 'x' coordinate of 'corner' and adding 'dy' to the 'y' coordinate of 'corner'.

12.6 Copying

Aliasing can make a program difficult to read because changes in one place might have unexpected effects in another place. It is hard to keep track of all the variables that might refer to a given object.

Copying an object is often an alternative to aliasing. The copy module contains a function called copy that can duplicate any object:

```
>>> p1 = Point()
>>> p1.x = 3.0
>>> p1.y = 4.0
>>> import copy
>>> p2 = copy.copy(p1)
```

p1 and p2 contain the same data, but they are not the same Point.

```
>>> print_point(p1)
(3.0, 4.0)
>>> print_point(p2)
(3.0, 4.0)
>>> p1 is p2
False
>>> p1 == p2
False
```

The is operator indicates that p1 and p2 are not the same object, which is what we expected. But you might have expected == to yield True because these points contain the same data. In that case, you will be disappointed to learn that for instances, the default behavior of the == operator is the same as the is operator; it checks object identity, not object equivalence. This behavior can be changed—we'll see how later.

If you use copy.copy to duplicate a Rectangle, you will find that it copies the Rectangle object but not the embedded Point.

```
>>> box2 = copy.copy(box)
>>> box2 is box
False
>>> box2.corner is box.corner
True
```

Here is what the object diagram looks like:

This operation is called a **shallow copy** because it copies the object and any references it contains, but not the embedded objects.

For most applications, this is not what you want. In this example, invoking grow_rectangle on one of the Rectangles would not affect the other, but invoking move_rectangle on either would affect both! This behavior is confusing and error-prone.

Fortunately, the copy module contains a method named deepcopy that copies not only the object but also the objects it refers to, and the objects *they* refer to, and so on. You will not be surprised to learn that this operation is called a **deep copy**.

```
>>> box3 = copy.deepcopy(box)
>>> box3 is box
False
```

```
>>> box3.corner is box.corner False
```

box3 and box are completely separate objects.

12.6.1 Exercise 3

Write a version of move_rectangle that creates and returns a new Rectangle instead of modifying the old one.

12.7 Debugging

When you start working with objects, you are likely to encounter some new exceptions. If you try to access an attribute that doesn't exist, you get an AttributeError:

```
>>> p = Point()
>>> print p.z
AttributeError: Point instance has no attribute 'z'
```

If you are not sure what type an object is, you can ask:

```
>>> type(p)
<type '__main__.Point'>
```

If you are not sure whether an object has a particular attribute, you can use the built-in function hasattr:

```
>>> hasattr(p, 'x')
True
>>> hasattr(p, 'z')
False
```

The first argument can be any object; the second argument is a *string* that contains the name of the attribute.

12.8 Glossary

class: A user-defined type. A class definition creates a new class object. **class object:** An object that contains information about a user-defined type. The class object can be used to create instances of the type. **instance:** An object that belongs to a class. **attribute:** One of the named values associated with an object.

embedded (object): An object that is stored as an attribute of another object.

shallow copy: To copy the contents of an object, including any references to embedded objects; implemented by the copy function in the copy module. **deep copy:** To copy the contents of an object as well as any embedded objects, and any objects embedded in them, and so on; implemented by the deepcopy function in the copy module. **object diagram:** A diagram that shows objects, their attributes, and the values of the attributes.

12.9 Exercises

12.9.1 Exercise 4

World.py', which is part of Swampy (see Chapter '4'), contains a class definition for a user-defined type called 'World'. If you run this code:

```
''from World import *
world = World()
wait_for_user()
''
```

A window should appear with a title bar and an empty square. In this exercise we will use this window to draw Points, Rectangles and other shapes. Add the following lines before wait_for_user and run the program again

```
''canvas = world.ca(width=500, height=500, background='white')
bbox = [[-150,-100], [150, 100]]
canvas.rectangle(bbox, outline='black', width=2, fill='green4')
''
```

You should see a green rectangle with a black outline. The first line creates a Canvas, which appears in the window as a white square. The Canvas object provides methods like **'rectangle'** for drawing various shapes.

bbox' is a list of lists that represents the "bounding box" of the rectangle. The first pair of coordinates is the lower-left corner of the rectangle; the second pair is the upper-right corner.

You can draw a circle like this:

```
''canvas.circle([-25,0], 70, outline=None, fill='red')
''
```

The first parameter is the coordinate pair for the center of the circle; the second parameter is the radius.

If you add this line to the program, the result should resemble the national flag of Bangladesh (see 'wikipedia.org/wiki/Gallery_of_sovereign-state_flags').

• Write a function called draw_rectanglethat takes a

Canvas and a Rectangle as arguments and draws a representation of the Rectangle on the Canvas.

• Add an attribute named 'color' to your Rectangle objects and

modify draw_rectangle so that it uses the color attribute as the fill color.

• Write a function called draw_pointthat takes a

Canvas and a Point as arguments and draws a representation of the Point on the Canvas.

• Define a new class called Circle with appropriate attributes and

instantiate a few Circle objects. Write a function called draw_circle that draws circles on the canvas.

• Write a program that draws the national flag of of the Czech Republic¹.

Hint: you can draw a polygon like this:

''points = [[-150,-100], [150, 100], [150, -100]] canvas.polygon(points, fill='blue') ''

I have written a small program that lists the available colors; you can download it from 'thinkpython.com/code/color_list.py'.

¹ http://en.wikipedia.org/wiki/File:Flag_of_the_Czech_Republic.svg

13 Classes and functions

13.1 Time

As another example of a user-defined type, we'll define a class called Time that records the time of day. The class definition looks like this:

```
class Time(object):
    """represents the time of day.
    attributes: hour, minute, second"""
```

We can create a new Time object and assign attributes for hours, minutes, and seconds:

```
time = Time()
time.hour = 11
time.minute = 59
time.second = 30
```

The state diagram for the Time object looks like this:

13.1.1 Exercise 1

Write a function called print_time that takes a Time object and prints it in the form hour:minute:second.

Hint: the format sequence %.2d prints an integer using at least two digits, including a leading zero if necessary.

13.1.2 Exercise 2

Write a boolean function called is_after that takes two Time objects, t1 and t2, and returns True if t1 follows t2 chronologically and False otherwise.

Challenge: don't use an if statement.

13.2 Pure functions

In the next few sections, we'll write two functions that add time values. They demonstrate two kinds of functions: pure functions and modifiers. They also demonstrate a development plan I'll call **prototype and patch**, which is a way of tackling a complex problem by starting with a simple prototype and incrementally dealing with the complications.

Here is a simple prototype of add_time:

```
def add_time(t1, t2):
    sum = Time()
    sum.hour = t1.hour + t2.hour
    sum.minute = t1.minute + t2.minute
    sum.second = t1.second + t2.second
    return sum
```

The function creates a new Time object, initializes its attributes, and returns a reference to the new object. This is called a **pure function** because it does not modify any of the objects passed to it as arguments and it has no effect, like displaying a value or getting user input, other than returning a value.

To test this function, I'll create two Time objects: start contains the start time of a movie, like *Monty Python and the* Holy Grail, *and duration contains the run time of the movie*, which is one hour 35 minutes.

add_time figures out when the movie will be done.

```
>>> start = Time()
>>> start.hour = 9
>>> start.minute = 45
>>> start.second = 0
>>> duration = Time()
>>> duration.hour = 1
>>> duration.minute = 35
>>> duration.second = 0
>>> done = add_time(start, duration)
>>> print_time(done)
10:80:00
```

The result, 10:80:00 might not be what you were hoping for. The problem is that this function does not deal with cases where the number of seconds or minutes adds up to more than sixty. When that happens, we have to "carry" the extra seconds into the minute column or the extra minutes into the hour column.

Here's an improved version:

```
def add_time(t1, t2):
    sum = Time()
    sum.hour = t1.hour + t2.hour
    sum.minute = t1.minute + t2.minute
    sum.second = t1.second + t2.second
    if sum.second >= 60:
        sum.second -= 60
        sum.minute += 1
    if sum.minute >= 60:
        sum.minute -= 60
        sum.hour += 1
    return sum
```

Although this function is correct, it is starting to get big. We will see a shorter alternative later.

13.3 Modifiers

Sometimes it is useful for a function to modify the objects it gets as parameters. In that case, the changes are visible to the caller. Functions that work this way are called **modifiers**.

increment, which adds a given number of seconds to a Time object, can be written naturally as a modifier. Here is a rough draft:

```
def increment(time, seconds):
    time.second += seconds
    if time.second >= 60:
        time.second -= 60
        time.minute += 1
    if time.minute >= 60:
        time.minute -= 60
        time.hour += 1
```

The first line performs the basic operation; the remainder deals with the special cases we saw before.

Is this function correct? What happens if the parameter seconds is much greater than sixty?

In that case, it is not enough to carry once; we have to keep doing it until time.second is less than sixty. One solution is to replace the if statements with while statements. That would make the function correct, but not very efficient. **Exercise 3** Write a correct version of **'increment'** that doesn't contain any loops. Anything that can be done with modifiers can also be done with pure functions. In fact, some programming languages only allow pure functions. There is some evidence that programs that use pure functions are faster to develop and less error-prone than programs that use modifiers. But modifiers are convenient at times, and functional programs tend to be less efficient.

In general, I recommend that you write pure functions whenever it is reasonable and resort to modifiers only if there is a compelling advantage. This approach might be called a **functional** programming style.

Exercise 4 Write a "pure" version of **'increment**' that creates and returns a new Time object rather than modifying the parameter.

13.4 Prototyping versus planning

The development plan I am demonstrating is called "prototype and patch." For each function, I wrote a prototype that performed the basic calculation and then tested it, patching errors along the way.

This approach can be effective, especially if you don't yet have a deep understanding of the problem. But incremental corrections can generate code that is unnecessarily complicated—since it deals with many special cases—and unreliable—since it is hard to know if you have found all the errors.

An alternative is **planned development**, in which high-level insight into the problem can make the programming much easier. In this case, the insight is that a Time object is really a three-digit number in base 60 (see wikipedia.org/wiki/Sexagesimal)! The second attribute is the "ones column," the minute attribute is the "sixties column," and the hour attribute is the "thirty-six hundreds column."

When we wrote add_time and increment, we were effectively doing addition in base 60, which is why we had to carry from one column to the next.

This observation suggests another approach to the whole problem—we can convert Time objects to integers and take advantage of the fact that the computer knows how to do integer arithmetic.

Here is a function that converts Times to integers:

```
def time_to_int(time):
    minutes = time.hour * 60 + time.minute
    seconds = minutes * 60 + time.second
    return seconds
```

And here is the function that converts integers to Times (recall that divmod divides the first argument by the second and returns the quotient and remainder as a tuple).

```
def int_to_time(seconds):
    time = Time()
    minutes, time.second = divmod(seconds, 60)
    time.hour, time.minute = divmod(minutes, 60)
    return time
```

You might have to think a bit, and run some tests, to convince yourself that these functions are correct. One way to test them is to check that time_to_int(int_to_time(x)) == x for many values of x. This is an example of a consistency check.

Once you are convinced they are correct, you can use them to rewrite add_time:

```
def add_time(t1, t2):
    seconds = time_to_int(t1) + time_to_int(t2)
    return int_to_time(seconds)
```

This version is shorter than the original, and easier to verify. **Exercise 5** Rewrite 'increment' using time_to_int and int_to_time. In some ways, converting from base 60 to base 10 and back is harder than just dealing with times. Base conversion is more abstract; our intuition for dealing with time values is better.

But if we have the insight to treat times as base 60 numbers and make the investment of writing the conversion functions (time_to_int and int_to_time), we get a program that is shorter, easier to read and debug, and more reliable.

It is also easier to add features later. For example, imagine subtracting two Times to find the duration between them. The naïve approach would be to implement subtraction with borrowing. Using the conversion functions would be easier and more likely to be correct.

Ironically, sometimes making a problem harder (or more general) makes it easier (because there are fewer special cases and fewer opportunities for error).

13.5 Debugging

A Time object is well-formed if the values of minutes and seconds are between 0 and 60 (including 0 but not 60) and if hours is positive. hours and minutes should be integral values, but we might allow seconds to have a fraction part.

These kind of requirements are called **invariants** because they should always be true. To put it a different way, if they are not true, then something has gone wrong.

Writing code to check your invariants can help you detect errors and find their causes. For example, you might have a function like valid_time that takes a Time object and returns False if it violates an invariant:

```
def valid_time(time):
    if time.hours < 0 or time.minutes < 0 or time.seconds < 0:
        return False
    if time.minutes >= 60 or time.seconds >= 60:
        return False
    return True
```

Then at the beginning of each function you could check the arguments to make sure they are valid:

```
def add_time(t1, t2):
    if not valid_time(t1) or not valid_time(t2):
        raise ValueError, 'invalid Time object in add_time'
    seconds = time_to_int(t1) + time_to_int(t2)
    return int_to_time(seconds)
```

Or you could use an assert statement, which checks a given invariant and raises an exception if it fails:

```
def add_time(t1, t2):
    assert valid_time(t1) and valid_time(t2)
    seconds = time_to_int(t1) + time_to_int(t2)
    return int_to_time(seconds)
```

assert statements are useful because they distinguish code that deals with normal conditions from code that checks for errors.

13.6 Glossary

prototype and patch: A development plan that involves writing a rough draft of a program, testing, and correcting errors as they are found. **planned development:** A development plan that involves high-level insight into the problem and more planning than incremental development or prototype development. **pure function:** A function that does not modify any of the objects it receives as arguments. Most pure functions are fruitful. **modifier:** A function that changes one or more of the objects it receives as arguments. Most modifiers are fruitless. **functional programming style:** A style of program design in which the majority of functions are pure. **invariant:** A condition that should always be true during the execution of a program.

13.7 Exercises

13.7.1 Exercise 6

Write a function called mul_time that takes a Time object and a number and returns a new Time object that contains the product of the original Time and the number. *Then use mul_timeto write a function that takes a Time* object that represents the finishing time in a race, and a number that represents the distance, and returns a Time object that represents the average pace (time per mile).

13.7.2 Exercise 7

Write a class definition for a Date object that has attributes 'day', 'month' and 'year'. Write a function called increment_date that takes a Date object, 'date' and an integer, 'n', and returns a new Date object that represents the day 'n' days after 'date'. Hint: "Thirty days hath September..." Challenge: does your function deal with leap years correctly? See 'wikipedia.org/wiki/Leap_year

13.7.3 Exercise 8

The 'datetime' module provides 'date' and 'time' objects that are similar to the Date and Time objects in this chapter, but they provide a rich set of methods and operators. Read the documentation at 'docs.python.org/lib/datetime-date.html'.

- Use the 'datetime' module to write a program that gets the current date and prints the day of the week.
- Write a program that takes a birthday as input and prints the user's age and the number of days, hours, minutes and seconds until their next birthday.

14 Classes and methods

14.1 Object-oriented features

Python is an **object-oriented programming language**, which means that it provides features that support object-oriented programming.

It is not easy to define object-oriented programming, but we have already seen some of its characteristics:

• Programs are made up of object definitions and function

definitions, and most of the computation is expressed in terms of operations on objects.

• Each object definition corresponds to some object or concept

in the real world, and the functions that operate on that object correspond to the ways real-world objects interact.

For example, the Time class defined in Chapter 16 corresponds to the way people record the time of day, and the functions we defined correspond to the kinds of things people do with times. Similarly, the Point and Rectangle classes correspond to the mathematical concepts of a point and a rectangle.

So far, we have not taken advantage of the features Python provides to support objectoriented programming. These features are not strictly necessary; most of them provide alternative syntax for things we have already done. But in many cases, the alternative is more concise and more accurately conveys the structure of the program.

For example, in the Time program, there is no obvious connection between the class definition and the function definitions that follow. With some examination, it is apparent that every function takes at least one Time object as an argument.

This observation is the motivation for **methods**; a method is a function that is associated with a particular class. We have seen methods for strings, lists, dictionaries and tuples. In this chapter, we will define methods for user-defined types.

Methods are semantically the same as functions, but there are two syntactic differences:

- Methods are defined inside a class definition in order to make the relationship between the class and the method explicit.
- The syntax for invoking a method is different from the syntax for calling a function.

In the next few sections, we will take the functions from the previous two chapters and transform them into methods. This transformation is purely mechanical; you can do it simply by following a sequence of steps. If you are comfortable converting from one form to another, you will be able to choose the best form for whatever you are doing.

14.2 Printing objects

In Chapter 16, we defined a class named Time and in Exercise 16.1, you wrote a function named print_time:

```
class Time(object):
    """represents the time of day.
    attributes: hour, minute, second"""

def print_time(time):
    print '%.2d:%.2d' % (time.hour, time.minute, time.second)
```

To call this function, you have to pass a Time object as an argument:

```
>>> start = Time()
>>> start.hour = 9
>>> start.minute = 45
>>> start.second = 00
>>> print_time(start)
09:45:00
```

To make print_time a method, all we have to do is move the function definition inside the class definition. Notice the change in indentation.

```
class Time(object):
    def print_time(time):
        print '%.2d:%.2d' % (time.hour, time.minute,
    time.second)
```

Now there are two ways to call print_time. The first (and less common) way is to use function syntax:

```
>>> Time.print_time(start)
09:45:00
```

In this use of dot notation, Time is the name of the class, and print_time is the name of the method. start is passed as a parameter.

The second (and more concise) way is to use method syntax:

```
>>> start.print_time()
09:45:00
```

In this use of dot notation, print_time is the name of the method (again), and start is the object the method is invoked on, which is called the **subject**. Just as the subject of a sentence is what the sentence is about, the subject of a method invocation is what the method is about.

Inside the method, the subject is assigned to the first parameter, so in this case start is assigned to time.

By convention, the first parameter of a method is called self, so it would be more common to write print_time like this:

```
class Time(object):
    def print_time(self):
        print '%.2d:%.2d' % (self.hour, self.minute,
```

```
self.second)
```

The reason for this convention is an implicit metaphor:

• The syntax for a function call, print_time(start),

suggests that the function is the active agent. It says something like, "Hey print_time! Here's an object for you to print."

• In object-oriented programming, the objects are the active

agents. A method invocation like start.print_time() says "Hey start! Please print yourself."

This change in perspective might be more polite, but it is not obvious that it is useful. In the examples we have seen so far, it may not be. But sometimes shifting responsibility from the functions onto the objects makes it possible to write more versatile functions, and makes it easier to maintain and reuse code.

14.2.1 Exercise 1

Rewrite time_to_int (from Section '16.4') as a method. It is probably not appropriate to rewrite int_to_time as a method; it's not clear what object you would invoke it on!

14.3 Another example

Here's a version of increment (from Section 16.3) rewritten as a method:

```
# inside class Time:
```

```
def increment(self, seconds):
    seconds += self.time_to_int()
    return int_to_time(seconds)
```

This version assumes that time_to_int is written as a method, as in Exercise 17.1. Also, note that it is a pure function, not a modifier.

Here's how you would invoke increment:

>>> start.print_time()
09:45:00
>>> end = start.increment(1337)
>>> end.print_time()
10:07:17

The subject, start, gets assigned to the first parameter, self. The argument, 1337, gets assigned to the second parameter, seconds.

This mechanism can be confusing, especially if you make an error. For example, if you invoke increment with two arguments, you get:

```
>>> end = start.increment(1337, 460)
TypeError: increment() takes exactly 2 arguments (3 given)
```

The error message is initially confusing, because there are only two arguments in parentheses. But the subject is also considered an argument, so all together that's three.

14.4 A more complicated example

is_after (from Exercise 16.2) is slightly more complicated because it takes two Time objects as parameters. In this case it is conventional to name the first parameter self and the second parameter other:

```
# inside class Time:
    def is_after(self, other):
        return self.time_to_int() > other.time_to_int()
```

To use this method, you have to invoke it on one object and pass the other as an argument:

```
>>> end.is_after(start)
True
```

One nice thing about this syntax is that it almost reads like English: "end is after start?"

14.5 The init method

The init method (short for "initialization") is a special method that gets invoked when an object is instantiated. Its full name is _____init____(two underscore characters, followed by init, and then two more underscores). An init method for the Time class might look like this:

```
# inside class Time:
```

```
def __init__(self, hour=0, minute=0, second=0):
    self.hour = hour
    self.minute = minute
    self.second = second
```

It is common for the parameters of _______ to have the same names as the attributes. The statement

```
self.hour = hour
```

stores the value of the parameter hour as an attribute of self.

The parameters are optional, so if you call Time with no arguments, you get the default values.

```
>>> time = Time()
>>> time.print_time()
00:00:00
```

If you provide one argument, it overrides hour:

```
>>> time = Time (9)
>>> time.print_time()
```

09:00:00

If you provide two arguments, they override hour and minute.

```
>>> time = Time(9, 45)
>>> time.print_time()
09:45:00
```

And if you provide three arguments, they override all three default values.

14.5.1 Exercise 2

Write an init method for the 'Point' class that takes ' \mathbf{x} ' and ' \mathbf{y} ' as optional parameters and assigns them to the corresponding attributes.

14.6 The <u>str</u> method

_____is a special method, like _____init____, that is supposed to return a string representation of an object.

For example, here is a str method for Time objects:

```
# inside class Time:
    def __str__(self):
        return '%.2d:%.2d' % (self.hour, self.minute,
    self.second)
```

When you print an object, Python invokes the str method:

```
>>> time = Time(9, 45)
>>> print time
09:45:00
```

When I write a new class, I almost always start by writing <u>____init___</u>, which makes it easier to instantiate objects, and <u>____str___</u>, which is useful for debugging.

14.6.1 Exercise 3

Write a 'str' method for the 'Point' class. Create a Point object and print it.

14.7 Operator overloading

By defining other special methods, you can specify the behavior of operators on user-defined types. For example, if you define a method named _____add____for the Time class, you can use the + operator on Time objects.

Here is what the definition might look like:

Classes and methods

```
# inside class Time:
```

```
def __add__(self, other):
    seconds = self.time_to_int() + other.time_to_int()
    return int_to_time(seconds)
```

And here is how you could use it:

```
>>> start = Time(9, 45)
>>> duration = Time(1, 35)
>>> print start + duration
11:20:00
```

When you apply the + operator to Time objects, Python invokes ____add____. When you print the result, Python invokes ____str____. So there is quite a lot happening behind the scenes!

Changing the behavior of an operator so that it works with user-defined types is called **operator overloading**. For every operator in Python there is a corresponding special method, like <u>___add___</u>. For more details, see docs.python.org/ref/specialnames.html.

14.7.1 Exercise 4

Write an 'add' method for the Point class.

14.8 Type-based dispatch

In the previous section we added two Time objects, but you also might want to add an integer to a Time object. The following is a version of ____add___that checks the type of other and invokes either add_time or increment:

inside class Time:

```
def __add__(self, other):
    if isinstance(other, Time):
        return self.add_time(other)
    else:
        return self.increment(other)
def add_time(self, other):
    seconds = self.time_to_int() + other.time_to_int()
    return int_to_time(seconds)
def increment(self, seconds):
    seconds += self.time_to_int()
    return int_to_time(seconds)
```

The built-in function is instance takes a value and a class object, and returns True if the value is an instance of the class.

If other is a Time object, <u>___add___</u>invokes add__time. Otherwise it assumes that the parameter is a number and invokes increment. This operation is called a **type-based dispatch** because it dispatches the computation to different methods based on the type of the arguments.

Here are examples that use the + operator with different types:

```
>>> start = Time(9, 45)
>>> duration = Time(1, 35)
>>> print start + duration
11:20:00
>>> print start + 1337
10:07:17
```

Unfortunately, this implementation of addition is not commutative. If the integer is the first operand, you get

```
>>> print 1337 + start
TypeError: unsupported operand type(s) for +: 'int' and 'instance'
```

The problem is, instead of asking the Time object to add an integer, Python is asking an integer to add a Time object, and it doesn't know how to do that. But there is a clever solution for this problem: the special method <u>radd</u>, which stands for "right-side add." This method is invoked when a Time object appears on the right side of the + operator. Here's the definition:

```
# inside class Time:
```

```
def __radd__(self, other):
    return self.__add__(other)
```

And here's how it's used:

>>> print 1337 + start 10:07:17

14.8.1 Exercise 5

Write an 'add' method for Points that works with either a Point object or a tuple:

- If the second operand is a Point, the method should return a new Point whose 'x' coordinate is the sum of the 'x' coordinates of the operands, and likewise for the 'y' coordinates.
- If the second operand is a tuple, the method should add the first element of the tuple to the 'x' coordinate and the second element to the 'y' coordinate, and return a new Point with the result.

14.9 Polymorphism

Type-based dispatch is useful when it is necessary, but (fortunately) it is not always necessary. Often you can avoid it by writing functions that work correctly for arguments with different types.

Many of the functions we wrote for strings will actually work for any kind of sequence. For example, in Section 11.1 we used histogram to count the number of times each letter appears in a word.

```
def histogram(s):
    d = dict()
```

```
for c in s:
    if c not in d:
        d[c] = 1
    else:
        d[c] = d[c]+1
return d
```

This function also works for lists, tuples, and even dictionaries, as long as the elements of s are hashable, so they can be used as keys in d.

```
>>> t = ['spam', 'egg', 'spam', 'spam', 'bacon', 'spam']
>>> histogram(t)
{'bacon': 1, 'egg': 1, 'spam': 4}
```

Functions that can work with several types are called **polymorphic**. Polymorphism can facilitate code reuse. For example, the built-in function sum, which adds the elements of a sequence, works as long as the elements of the sequence support addition.

Since Time objects provide an add method, they work with sum:

```
>>> t1 = Time(7, 43)
>>> t2 = Time(7, 41)
>>> t3 = Time(7, 37)
>>> total = sum([t1, t2, t3])
>>> print total
23:01:00
```

In general, if all of the operations inside a function work with a given type, then the function works with that type.

The best kind of polymorphism is the unintentional kind, where you discover that a function you already wrote can be applied to a type you never planned for.

14.10 Debugging

It is legal to add attributes to objects at any point in the execution of a program, but if you are a stickler for type theory, it is a dubious practice to have objects of the same type with different attribute sets. It is usually a good idea to initialize all of an objects attributes in the init method.

If you are not sure whether an object has a particular attribute, you can use the built-in function hasattr (see Section 15.7).

```
>>> p = Point(3, 4)
>>> print p.__dict__
{'y': 4, 'x': 3}
```

For purposes of debugging, you might find it useful to keep this function handy:

```
def print_attributes(obj):
    for attr in obj.__dict__:
        print attr, getattr(obj, attr)
```

print_attributes traverses the items in the object's dictionary and prints each attribute name and its corresponding value.

The built-in function getattr takes an object and an attribute name (as a string) and returns the attribute's value.

14.11 Glossary

object-oriented language: A language that provides features, such as user-defined classes and method syntax, that facilitate object-oriented programming. **object-oriented programming:** A style of programming in which data and the operations that manipulate it are organized into classes and methods. **method:** A function that is defined inside a class definition and is invoked on instances of that class. **subject:** The object a method is invoked on. **operator overloading:** Changing the behavior of an operator like + so it works with a user-defined type.

type-based dispatch: A programming pattern that checks the type of an operand and invokes different functions for different types. **polymorphic:** Pertaining to a function that can work with more than one type.

14.12 Exercises

14.12.1 Exercise 6

This exercise is a cautionary tale about one of the most common, and difficult to find, errors in Python.

• Write a definition for a class named 'Kangaroo' with the following

methods:

- An ____init___method that initializes an attribute named pouch_contents o an empty list.
- A method named put_in_pouchthat takes an object of any type and adds it to pouch_contents.
- A <u>_____str___</u>method that returns a string representation of the Kangaroo object and the contents of the pouch.

Test your code by creating two *Kangaroo* objects, assigning them to variables named *kanga* and *roo*, and then adding *roo* to the contents of *kanga*'s pouch.'

• 'Download thinkpython.com/code/BadKangaroo.py. It contains

a solution to the previous problem with one big, nasty bug. Find and fix the bug.' 'If you get stuck, you can download *thinkpython.com/code/GoodKangaroo.py*, which explains the problem and demonstrates a solution.'

14.12.2 Exercise 7

Visual is a Python module that provides 3-D graphics. It is not always included in a Python installation, so you might have to install it from your software repository or, if it's not there, from 'vpython.org'.

The following example creates a 3-D space that is 256 units wide, long and high, and sets the "center" to be the point '(128, 128, 128)'. Then it draws a blue sphere.

''from visual import *
scene.range = (256, 256, 256)
scene.center = (128, 128, 128)
color = (0.1, 0.1, 0.9) # mostly blue
sphere(pos=scene.center, radius=128, color=color)

color' is an RGB tuple; that is, the elements are Red-Green-Blue levels between 0.0 and 1.0 (see 'wikipedia.org/wiki/RGB_color_model').

If you run this code, you should see a window with a black background and a blue sphere. If you drag the middle button up and down, you can zoom in and out. You can also rotate the scene by dragging the right button, but with only one sphere in the world, it is hard to tell the difference.

The following loop creates a cube of spheres:

```
''t = range(0, 256, 51)
for x in t:
    for y in t:
        for z in t:
            pos = x, y, z
                 sphere(pos=pos, radius=10, color=color)
''
```

• Put this code in a script and make sure it works for

you.

• Modify the program so that each sphere in the cube

has the color that corresponds to its position in RGB space. Notice that the coordinates are in the range 0–255, but the RGB tuples are in the range 0.0–1.0.

Download 'thinkpython.com/code/color_list.py'

and use the function read_colors to generate a list of the available colors on your system, their names and RGB values. For each named color draw a sphere in the position that corresponds to its RGB values.

You can see my solution at 'thinkpython.com/code/color_space.py'.

14.13 Further reading

- Wikipedia: VPython¹
- Wikipedia: RGB color model²

¹

http://en.wikipedia.org/wiki/%20VPython http://en.wikipedia.org/wiki/%20RGB%20color%20model 2

15 Inheritance

In this chapter we will develop classes to represent playing cards, decks of cards, and poker hands. If you don't play poker, you can read about it at wikipedia.org/wiki/Poker¹, but you don't have to; I'll tell you what you need to know for the exercises.

If you are not familiar with Anglo-American playing cards, you can read about them at wikipedia.org/wiki/Playing_cards².

15.1 Card objects

There are fifty-two cards in a deck, each of which belongs to one of four suits and one of thirteen ranks. The suits are Spades, Hearts, Diamonds, and Clubs (in descending order in bridge). The ranks are Ace, 2, 3, 4, 5, 6, 7, 8, 9, 10, Jack, Queen, and King. Depending on the game that you are playing, an Ace may be higher than King or lower than 2.

If we want to define a new object to represent a playing card, it is obvious what the attributes should be: rank and suit. It is not as obvious what type the attributes should be. One possibility is to use strings containing words like 'Spade' for suits and 'Queen' for ranks. One problem with this implementation is that it would not be easy to compare cards to see which had a higher rank or suit.

An alternative is to use integers to **encode** the ranks and suits. In this context, "encode" means that we are going to define a mapping between numbers and suits, or between numbers and ranks. This kind of encoding is not meant to be a secret (that would be "encryption").

For example, this table shows the suits and the corresponding integer codes:

Spades	\mapsto	3
Hearts	\mapsto	2
Diamonds	\mapsto	1
Clubs	\mapsto	0

This code makes it easy to compare cards; because higher suits map to higher numbers, we can compare suits by comparing their codes.

The mapping for ranks is fairly obvious; each of the numerical ranks maps to the corresponding integer, and for face cards:

 \mapsto

Jack

11

¹ http://en.wikipedia.org/wiki/Poker

² http://en.wikipedia.org/wiki/Playing_cards

Queen	\mapsto	12
King	\mapsto	13

I am using the \mapsto symbol to make is clear that these mappings are not part of the Python program. They are part of the program design, but they don't appear explicitly in the code.

The class definition for Card looks like this:

```
class Card:
    """represents a standard playing card."""
    def __init__(self, suit=0, rank=2):
        self.suit = suit
        self.rank = rank
```

As usual, the init method takes an optional parameter for each attribute. The default card is the 2 of Clubs.

To create a Card, you call Card with the suit and rank of the card you want.

```
queen_of_diamonds = Card(1, 12)
```

15.2 Class attributes

In order to print Card objects in a way that people can easily read, we need a mapping from the integer codes to the corresponding ranks and suits. A natural way to do that is with lists of strings. We assign these lists to **class** attributes:

Variables like suit_names and rank_names, which are defined inside a class but outside of any method, are called class attributes because they are associated with the class object Card.

This term distinguished them from variables like suit and rank, which are called **instance attributes** because they are associated with a particular instance.

Both kinds of attribute are accessed using dot notation. For example, in _____str____, self is a Card object, and self.rank is its rank. Similarly, Card is a class object, and Card.rank_names is a list of strings associated with the class.

Every card has its own suit and rank, but there is only one copy of suit_names and rank_names.

Putting it all together, the expression Card.rank_names[self.rank] means "use the attribute rank from the object self as an index into the list rank_names from the class Card, and select the appropriate string."

The first element of rank_names is None because there is no card with rank zero. By including None as a place-keeper, we get a mapping with the nice property that the index 2 maps to the string '2', and so on. To avoid this tweak, we could have used a dictionary instead of a list.

With the methods we have so far, we can create and print cards:

```
>>> card1 = Card(2, 11)
>>> print card1
Jack of Hearts
```

Here is a diagram that shows the Card class object and one Card instance:

Card is a class object, so it has type type. card1 has type Card. (To save space, I didn't draw the contents of suit_names and rank_names).

15.3 Comparing cards

For built-in types, there are conditional operators (<, >, ==, etc.) that compare values and determine when one is greater than, less than, or equal to another. For user-defined types, we can override the behavior of the built-in operators by providing a method named ____cmp____.

_____takes two parameters, self and other, and returns a positive number if the first object is greater, a negative number if the second object is greater, and 0 if they are equal to each other.

The correct ordering for cards is not obvious. For example, which is better, the 3 of Clubs or the 2 of Diamonds? One has a higher rank, but the other has a higher suit. In order to compare cards, you have to decide whether rank or suit is more important.

The answer might depend on what game you are playing, but to keep things simple, we'll make the arbitrary choice that suit is more important, so all of the Spades outrank all of the Diamonds, and so on.

With that decided, we can write <u>_____</u>cmp____:

```
# inside class Card:
```

```
def __cmp__(self, other):
    # check the suits
    if self.suit > other.suit: return 1
    if self.suit < other.suit: return -1
    # suits are the same... check ranks
    if self.rank > other.rank: return 1
    if self.rank < other.rank: return -1
    # ranks are the same... it's a tie
    return 0</pre>
```

You can write this more concisely using tuple comparison:

```
# inside class Card:
    def __cmp__(self, other):
        t1 = self.suit, self.rank
        t2 = other.suit, other.rank
        return cmp(t1, t2)
```

The built-in function cmp has the same interface as the method <u>_____</u>: it takes two values and returns a positive number if the first is larger, a negative number of the second is larger, and 0 if they are equal.

15.3.1 Exercise 1

Write a <u>_____</u> method for Time objects. Hint: you can use tuple comparison, but you also might consider using integer subtraction.

15.4 Decks

Now that we have Cards, the next step is to define Decks. Since a deck is made up of cards, it is natural for each Deck to contain a list of cards as an attribute.

The following is a class definition for Deck. The init method creates the attribute cards and generates the standard set of fifty-two cards:

class Deck:

```
def __init__(self):
    self.cards = []
    for suit in range(4):
        for rank in range(1, 14):
            card = Card(suit, rank)
            self.cards.append(card)
```

The easiest way to populate the deck is with a nested loop. The outer loop enumerates the suits from 0 to 3. The inner loop enumerates the ranks from 1 to 13. Each iteration creates a new Card with the current suit and rank, and appends it to self.cards.

15.5 Printing the deck

Here is a _____str___method for Deck:

```
#inside class Deck:
```

```
def __str__(self):
    res = [str(card) for card in self.cards]
    return '\n'.join(res)
```

This method demonstrates an efficient way to accumulate a large string: building a list of strings and then using join. The built-in function str invokes the ____str___method on each card and returns the string representation.

Since we invoke join on a newline character, the cards are separated by newlines. Here's what the result looks like:

```
>>> deck = Deck()
>>> print deck
Ace of Clubs
2 of Clubs
3 of Clubs
...
10 of Spades
Jack of Spades
Queen of Spades
King of Spades
```

Even though the result appears on 52 lines, it is one long string that contains newlines.

15.6 Add, remove, shuffle and sort

To deal cards, we would like a method that removes a card from the deck and returns it. The list method pop provides a convenient way to do that:

```
#inside class Deck:
```

```
def pop_card(self):
    return self.cards.pop()
```

Since pop removes the *last* card in the list, we are dealing from the bottom of the deck. In real life bottom dealing is frowned upon1, but in this context it's ok.

To add a card, we can use the list method append:

```
#inside class Deck:
```

```
def add_card(self, card):
    self.cards.append(card)
```

A method like this that uses another function without doing much real work is sometimes called a **veneer**. The metaphor comes from woodworking, where it is common to glue a thin layer of good quality wood to the surface of a cheaper piece of wood.

In this case we are defining a "thin" method that expresses a list operation in terms that are appropriate for decks.

As another example, we can write a Deck method named shuffle using the function shuffle from the random module:

```
# inside class Deck:
```

```
def shuffle(self):
    random.shuffle(self.cards)
```

Don't forget to import random.

15.6.1 Exercise 2

Write a Deck method named 'sort' that uses the list method 'sort' to sort the cards in a 'Deck'. 'sort' uses the _____ method we defined to determine sort order.

15.7 Inheritance

The language feature most often associated with object-oriented programming is **inheritance**. Inheritance is the ability to define a new class that is a modified version of an existing class.

It is called "inheritance" because the new class inherits the methods of the existing class. Extending this metaphor, the existing class is called the **parent** and the new class is called the **child**.

As an example, let's say we want a class to represent a "hand," that is, the set of cards held by one player. A hand is similar to a deck: both are made up of a set of cards, and both require operations like adding and removing cards.

A hand is also different from a deck; there are operations we want for hands that don't make sense for a deck. For example, in poker we might compare two hands to see which one wins. In bridge, we might compute a score for a hand in order to make a bid.

This relationship between classes—similar, but different—lends itself to inheritance.

The definition of a child class is like other class definitions, but the name of the parent class appears in parentheses:

```
class Hand(Deck):
    """represents a hand of playing cards"""
```

This definition indicates that Hand inherits from Deck; that means we can use methods like pop_card and add_card for Hands as well as Decks.

Hand also inherits <u>init</u> from Deck, but it doesn't really do what we want: instead of populating the hand with 52 new cards, the init method for Hands should initialize cards with an empty list.

If we provide an init method in the Hand class, it overrides the one in the Deck class:

```
# inside class Hand:
```

```
def __init__(self, label=''):
    self.cards = []
    self.label = label
```

So when you create a Hand, Python invokes this init method:

```
>>> hand = Hand('new hand')
>>> print hand.cards
[]
>>> print hand.label
new hand
```

But the other methods are inherited from Deck, so we can use pop_card and add_card to deal a card:

```
>>> deck = Deck()
>>> card = deck.pop_card()
>>> hand.add_card(card)
>>> print hand
King of Spades
```

A natural next step is to encapsulate this code in a method called move_cards:

#inside class Deck:

```
def move_cards(self, hand, num):
    for i in range(num):
        hand.add_card(self.pop_card())
```

move_cards takes two arguments, a Hand object and the number of cards to deal. It modifies both self and hand, and returns None.

In some games, cards are moved from one hand to another, or from a hand back to the deck. You can use move_cards for any of these operations: self can be either a Deck or a Hand, and hand, despite the name, can also be a Deck. **Exercise 3** Write a Deck method called deal_hands that takes two parameters, the number of hands and the number of cards per hand, and that creates new Hand objects, deals the appropriate number of cards per hand, and returns a list of Hand objects. Inheritance is a useful feature. Some programs that would be repetitive without inheritance can be written more elegantly with it. Inheritance can facilitate code reuse, since you can customize the behavior of parent classes without having to modify them. In some cases, the inheritance structure reflects the natural structure of the problem, which makes the program easier to understand.

On the other hand, inheritance can make programs difficult to read. When a method is invoked, it is sometimes not clear where to find its definition. The relevant code may be scattered among several modules. Also, many of the things that can be done using inheritance can be done as well or better without it.

15.8 Class diagrams

So far we have seen stack diagrams, which show the state of a program, and object diagrams, which show the attributes of an object and their values. These diagrams represent a snapshot in the execution of a program, so they change as the program runs.

They are also highly detailed; for some purposes, too detailed. A class diagrams is a more abstract representation of the structure of a program. Instead of showing individual objects, it shows classes and the relationships between them.

There are several kinds of relationship between classes:

• Objects in one class might contain references to objects in another class. For example, each Rectangle contains a reference to a Point, and each Deck contains references to many Cards. This kind of relationship is called **HAS-A**, as in, "a Rectangle has a Point."

- One class might inherit from another. This relationship is called **IS-A**, as in, "a Hand is a kind of a Deck."
- One class might depend on another in the sense that changes in one class would require changes in the other.

A **class diagram** is a graphical representation of these relationships2. For example, this diagram shows the relationships between Card, Deck and Hand.

The arrow with a hollow triangle head represents an IS-A relationship; in this case it indicates that Hand inherits from Deck.

The standard arrow head represents a HAS-A relationship; in this case a Deck has references to Card objects.

The star (*) near the arrow head is a **multiplicity**; it indicates how many Cards a Deck has. A multiplicity can be a simple number, like 52, a range, like 5..7 or a star, which indicates that a Deck can have any number of Cards.

A more detailed diagram might show that a Deck actually contains a *list* of Cards, but built-in types like list and dict are usually not included in class diagrams.

15.8.1 Exercise 4

Read 'TurtleWorld.py', 'World.py' and 'Gui.py' and draw a class diagram that shows the relationships among the classes defined there.

15.9 Debugging

Inheritance can make debugging a challenge because when you invoke a method on an object, you might not know which method will be invoked.

Suppose you are writing a function that works with Hand objects. You would like it to work with all kinds of Hands, like PokerHands, BridgeHands, etc. If you invoke a method like shuffle, you might get the one defined in Deck, but if any of the subclasses override this method, you'll get that version instead.

Any time you are unsure about the flow of execution through your program, the simplest solution is to add print statements at the beginning of the relevant methods. If Deck.shuffle prints a message that says something like Running Deck.shuffle, then as the program runs it traces the flow of execution.

As an alternative, you could use this function, which takes an object and a method name (as a string) and returns the class that provides the definition of the method:

```
def find_defining_class(obj, meth_name):
    for ty in type(obj).mro():
        if meth_name in ty.__dict__:
        return ty
```

Here's an example:

```
>>> hand = Hand()
>>> print find_defining_class(hand, 'shuffle')
<class 'Card.Deck'>
```

So the shuffle method for this Hand is the one in Deck.

find_defining_class uses the mro method to get the list of class objects (types) that will be searched for methods. "MRO" stands for "method resolution order."

Here's a program design suggestion: whenever you override a method, the interface of the new method should be the same as the old. It should take the same parameters, return the same type, and obey the same preconditions and postconditions. If you obey this rule, you will find that any function designed to work with an instance of a superclass, like a Deck, will also work with instances of subclasses like a Hand or PokerHand.

If you violate this rule, your code will collapse like (sorry) a house of cards.

15.10 Glossary

encode: To represent one set of values using another set of values by constructing a mapping between them. **class attribute:** An attribute associated with a class object. Class attributes are defined inside a class definition but outside any method.

instance attribute: An attribute associated with an instance of a class.

veneer: A method or function that provides a different interface to another function without doing much computation. **inheritance:** The ability to define a new class that is a modified version of a previously defined class. **parent class:** The class from which a child class inherits. **child class:** A new class created by inheriting from an existing class; also called a "subclass." **IS-A relationship:** The relationship between a child class and its parent class. **HAS-A relationship:** The relationship between two classes where instances of one class contain references to instances of the other. **class diagram:** A diagram that shows the classes in a program and the relationships between them.

multiplicity: A notation in a class diagram that shows, for a HAS-A relationship, how many references there are to instances of another class.

15.11 Exercises

15.11.1 Exercise 5

The following are the possible hands in poker, in increasing order of value (and decreasing order of probability): **pair**:two cards with the same rank 'two pair:' two pairs of cards with the same rank 'three of a kind:' three cards with the same rank 'straight:' five cards with ranks in sequence (aces can be high or low, so 'Ace-2-3-4-5' is a straight and so is '10-Jack-Queen-King-Ace', but 'Queen-King-Ace-2-3' is not.) 'flush:' five cards with the same suit 'full house:' three cards with one rank, two cards with another 'four of a kind:' four cards with the same rank 'straight flush:' five cards in sequence (as defined above) and

with the same suit The goal of these exercises is to estimate the probability of drawing these various hands.

• Download the following files from 'thinkpython.com/code': Card.py: A complete version of the 'Card', 'Deck' and 'Hand' classes in this chapter.'PokerHand.py': An incomplete implementation of a class

that represents a poker hand, and some code that tests it.

• 'If you run *PokerHand.py*, it deals six 7-card poker hands

and checks to see if any of them contains a flush. Read this code carefully before you go on.'

• 'Add methods to *PokerHand.py*named "has_pair",

"has_twopair", etc. that return True or False according to whether or not the hand meets the relevant criteria. Your code should work correctly for "hands" that contain any number of cards (although 5 and 7 are the most common sizes)."

• 'Write a method named *classify*that figures out

the highest-value classification for a hand and sets the *label* attribute accordingly. For example, a 7-card hand might contain a flush and a pair; it should be labeled "flush".'

• 'When you are convinced that your classification methods are

working, the next step is to estimate the probabilities of the various hands. Write a function in *PokerHand.py* that shuffles a deck of cards, divides it into hands, classifies the hands, and counts the number of times various classifications appear.'

• 'Print a table of the classifications and their probabilities.

Run your program with larger and larger numbers of hands until the output values converge to a reasonable degree of accuracy. Compare your results to the values at *wikipedia.org/wiki/Hand_rankings.*'

15.11.2 Exercise 6

This exercise uses TurtleWorld from Chapter '4'. You will write code that makes Turtles play tag. If you are not familiar with the rules of tag, see 'wikipedia.org/wiki/Tag_(game)'.

• Download 'thinkpython.com/code/Wobbler.py' and run it. You

should see a TurtleWorld with three Turtles. If you press the ' \mathbf{Run} ' button, the Turtles wander at random.

• Read the code and make sure you understand how it works.

The 'Wobbler' class inherits from 'Turtle', which means that the 'Turtle' methods 'lt', 'rt', 'fd' and 'bk' work on Wobblers. *The 'step' method gets invoked by TurtleWorld. It invokes* 'steer', which turns the Turtle in the desired direction, 'wobble', which makes a random turn in proportion to the Turtle's clumsiness, and 'move', which moves forward a few pixels, depending on the Turtle's speed.

• Create a file named 'Tagger.py'. Import everything from

'Wobbler', then define a class named 'Tagger' that inherits from 'Wobbler'. Call make_world passing the 'Tagger' class object as an argument.

• Add a 'steer' method to 'Tagger' to override the one in

'Wobbler'. As a starting place, write a version that always points the Turtle toward the origin. Hint: use the math function 'atan2' and the Turtle attributes 'x', 'y' and 'heading'.

• Modify 'steer' so that the Turtles stay in bounds.

For debugging, you might want to use the ${\bf 'Step'}$ button, which invokes ${\bf 'step'}$ once on each Turtle.

• Modify 'steer' so that each Turtle points toward its nearest

neighbor. Hint: Turtles have an attribute, 'world', that is a reference to the TurtleWorld they live in, and the TurtleWorld has an attribute, 'animals', that is a list of all Turtles in the world.

• Modify 'steer' so the Turtles play tag. You can add methods

to **'Tagger'** and you can override **'steer'** and <u>init</u>, but you may not modify or override **'step'**, **'wobble'** or **'move'**. Also, **'steer'** is allowed to change the heading of the Turtle but not the position. *Adjust the rules and your 'steer'* method for good quality play; for example, it should be possible for the slow Turtle to tag the faster Turtles eventually.

You can get my solution from 'thinkpython.com/code/Tagger.py'.

1See wikipedia.org/wiki/Bottom_dealing. 2The diagrams I am using here are similar to UML (see wikipedia.org/wiki/Unified_Modeling_Language), with a few simplifications.

16 Debugging

Different kinds of errors can occur in a program, and it is useful to distinguish among them in order to track them down more quickly:

- Syntax errors are produced by Python when it is translating the source code into byte code. They usually indicate that there is something wrong with the syntax of the program. Example: Omitting the colon at the end of a def statement yields the somewhat redundant message SyntaxError: invalid syntax.
- Runtime errors are produced by the interpreter if something goes wrong while the program is running. Most runtime error messages include information about where the error occurred and what functions were executing. Example: An infinite recursion eventually causes the runtime error "maximum recursion depth exceeded."
- Semantic errors are problems with a program that runs without producing error messages but doesn't do the right thing. Example: An expression may not be evaluated in the order you expect, yielding an incorrect result.

The first step in debugging is to figure out which kind of error you are dealing with. Although the following sections are organized by error type, some techniques are applicable in more than one situation.

16.1 Syntax errors

Syntax errors are usually easy to fix once you figure out what they are. Unfortunately, the error messages are often not helpful. The most common messages are SyntaxError: invalid syntax and SyntaxError: invalid token, neither of which is very informative.

On the other hand, the message does tell you where in the program the problem occurred. Actually, it tells you where Python noticed a problem, which is not necessarily where the error is. Sometimes the error is prior to the location of the error message, often on the preceding line.

If you are building the program incrementally, you should have a good idea about where the error is. It will be in the last line you added.

If you are copying code from a book, start by comparing your code to the book's code very carefully. Check every character. At the same time, remember that the book might be wrong, so if you see something that looks like a syntax error, it might be.

Here are some ways to avoid the most common syntax errors:

- Make sure you are not using a Python keyword for a variable name.
- Check that you have a colon at the end of the header of every

compound statement, including for, while, if, and def statements.

• Make sure that any strings in the code have matching

quotation marks.

• If you have multiline strings with triple quotes (single or double), make

sure you have terminated the string properly. An unterminated string may cause an invalid token error at the end of your program, or it may treat the following part of the program as a string until it comes to the next string. In the second case, it might not produce an error message at all!

• An unclosed opening operator—(, {, or

[—makes Python continue with the next line as part of the current statement. Generally, an error occurs almost immediately in the next line.

• Check for the classic = instead of == inside

a conditional.

• Check the indentation to make sure it lines up the way it

is supposed to. Python can handle space and tabs, but if you mix them it can cause problems. The best way to avoid this problem is to use a text editor that knows about Python and generates consistent indentation.

If nothing works, move on to the next section...

16.1.1 I keep making changes and it makes no difference.

If the interpreter says there is an error and you don't see it, that might be because you and the interpreter are not looking at the same code. Check your programming environment to make sure that the program you are editing is the one Python is trying to run.

If you are not sure, try putting an obvious and deliberate syntax error at the beginning of the program. Now run it again. If the interpreter doesn't find the new error, you are not running the new code.

There are a few likely culprits:

• You edited the file and forgot to save the changes before

running it again. Some programming environments do this for you, but some don't.

• You changed the name of the file, but you are still running

the old name.

• Something in your development environment is configured

incorrectly.

• If you are writing a module and using import,

make sure you don't give your module the same name as one of the standard Python modules.

• If you are using import to read a module, remember

that you have to restart the interpreter or use reload to read a modified file. If you import the module again, it doesn't do anything.

If you get stuck and you can't figure out what is going on, one approach is to start again with a new program like "Hello, World!," and make sure you can get a known program to run. Then gradually add the pieces of the original program to the new one.

16.2 Runtime errors

Once your program is syntactically correct, Python can compile it and at least start running it. What could possibly go wrong?

16.2.1 My program does absolutely nothing.

This problem is most common when your file consists of functions and classes but does not actually invoke anything to start execution. This may be intentional if you only plan to import this module to supply classes and functions.

If it is not intentional, make sure that you are invoking a function to start execution, or execute one from the interactive prompt. Also see the "Flow of Execution" section below.

16.2.2 My program hangs.

If a program stops and seems to be doing nothing, it is "hanging." Often that means that it is caught in an infinite loop or infinite recursion.

• If there is a particular loop that you suspect is the

problem, add a print statement immediately before the loop that says "entering the loop" and another immediately after that says "exiting the loop." Run the program. If you get the first message and not the second, you've got an infinite loop. Go to the "Infinite Loop" section below.

• Most of the time, an infinite recursion will cause the program

to run for a while and then produce a "RuntimeError: Maximum recursion depth exceeded" error. If that happens, go to the "Infinite Recursion" section below. If you are not getting this error but you suspect there is a problem with a recursive method or function, you can still use the techniques in the "Infinite Recursion" section.

• If neither of those steps works, start testing other

loops and other recursive functions and methods.

• If that doesn't work, then it is possible that

you don't understand the flow of execution in your program. Go to the "Flow of Execution" section below.

Infinite Loop

If you think you have an infinite loop and you think you know what loop is causing the problem, add a print statement at the end of the loop that prints the values of the variables in the condition and the value of the condition.

For example:

```
while x > 0 and y < 0 :
    # do something to x
    # do something to y
    print "x: ", x
    print "y: ", y
    print "condition: ", (x > 0 and y < 0)</pre>
```

Now when you run the program, you will see three lines of output for each time through the loop. The last time through the loop, the condition should be false. If the loop keeps going, you will be able to see the values of x and y, and you might figure out why they are not being updated correctly.

Infinite Recursion

Most of the time, an infinite recursion will cause the program to run for a while and then produce a Maximum recursion depth exceeded error.

If you suspect that a function or method is causing an infinite recursion, start by checking to make sure that there is a base case. In other words, there should be some condition that will cause the function or method to return without making a recursive invocation. If not, then you need to rethink the algorithm and identify a base case.

If there is a base case but the program doesn't seem to be reaching it, add a print statement at the beginning of the function or method that prints the parameters. Now when you run the program, you will see a few lines of output every time the function or method is invoked, and you will see the parameters. If the parameters are not moving toward the base case, you will get some ideas about why not.

Flow of Execution

If you are not sure how the flow of execution is moving through your program, add print statements to the beginning of each function with a message like "entering function foo," where foo is the name of the function.

Now when you run the program, it will print a trace of each function as it is invoked.

16.2.3 When I run the program I get an exception.

If something goes wrong during runtime, Python prints a message that includes the name of the exception, the line of the program where the problem occurred, and a traceback.

The traceback identifies the function that is currently running, and then the function that invoked it, and then the function that invoked *that*, and so on. In other words, it traces the sequence of function invocations that got you to where you are. It also includes the line number in your file where each of these calls occurs.

The first step is to examine the place in the program where the error occurred and see if you can figure out what happened. These are some of the most common runtime errors: **NameError:** You are trying to use a variable that doesn't exist in the current environment. Remember that local variables are local. You cannot refer to them from outside the function where they are defined. **TypeError:** There are several possible causes:

• You are trying to use a value improperly. Example: indexing

a string, list, or tuple with something other than an integer.

• There is a mismatch between the items in a format string and

the items passed for conversion. This can happen if either the number of items does not match or an invalid conversion is called for.

• You are passing the wrong number of arguments to a function or method.

For methods, look at the method definition and check that the first parameter is self. Then look at the method invocation; make sure you are invoking the method on an object with the right type and providing the other arguments correctly.

KeyError: You are trying to access an element of a dictionary using a key that the dictionary does not contain.

AttributeError: You are trying to access an attribute or method that does not exist. Check the spelling! You can use dir to list the attributes that do exist. If an AttributeError indicates that an object has NoneType, that means that it is None. One common cause is forgetting to return a value from a function; if you get to the end of a function without hitting a return statement, it returns None. Another common cause is using the result from a list method, like sort, that returns None.

IndexError: The index you are using to access a list, string, or tuple is greater than its length minus one. Immediately before the site of the error, add a print statement to display the value of the index and the length of the array. Is the array the right size? Is the index the right value?

The Python debugger (pdb) is useful for tracking down Exceptions because it allows you to examine the state of the program immediately before the error. You can read about pdb at docs.python.org/lib/module-pdb.html.

I added so many print statements I get inundated with output.

One of the problems with using print statements for debugging is that you can end up buried in output. There are two ways to proceed: simplify the output or simplify the program.

To simplify the output, you can remove or comment out print statements that aren't helping, or combine them, or format the output so it is easier to understand.

To simplify the program, there are several things you can do. First, scale down the problem the program is working on. For example, if you are searching a list, search a *small* list. If the program takes input from the user, give it the simplest input that causes the problem.

Second, clean up the program. Remove dead code and reorganize the program to make it as easy to read as possible. For example, if you suspect that the problem is in a deeply nested part of the program, try rewriting that part with simpler structure. If you suspect a large function, try splitting it into smaller functions and testing them separately.

Often the process of finding the minimal test case leads you to the bug. If you find that a program works in one situation but not in another, that gives you a clue about what is going on.

Similarly, rewriting a piece of code can help you find subtle bugs. If you make a change that you think doesn't affect the program, and it does, that can tip you off.

16.3 Semantic errors

In some ways, semantic errors are the hardest to debug, because the interpreter provides no information about what is wrong. Only you know what the program is supposed to do.

The first step is to make a connection between the program text and the behavior you are seeing. You need a hypothesis about what the program is actually doing. One of the things that makes that hard is that computers run so fast.

You will often wish that you could slow the program down to human speed, and with some debuggers you can. But the time it takes to insert a few well-placed print statements is often short compared to setting up the debugger, inserting and removing breakpoints, and "stepping" the program to where the error is occurring.

16.3.1 My program doesn't work.

You should ask yourself these questions:

• Is there something the program was supposed to do but

which doesn't seem to be happening? Find the section of the code that performs that function and make sure it is executing when you think it should.

• Is something happening that shouldn't? Find code in

your program that performs that function and see if it is executing when it shouldn't.

• Is a section of code producing an effect that is not

what you expected? Make sure that you understand the code in question, especially if it involves invocations to functions or methods in other Python modules. Read the documentation for the functions you invoke. Try them out by writing simple test cases and checking the results.

In order to program, you need to have a mental model of how programs work. If you write a program that doesn't do what you expect, very often the problem is not in the program; it's in your mental model.

The best way to correct your mental model is to break the program into its components (usually the functions and methods) and test each component independently. Once you find the discrepancy between your model and reality, you can solve the problem.

Of course, you should be building and testing components as you develop the program. If you encounter a problem, there should be only a small amount of new code that is not known to be correct. A.3.2 I've got a big hairy expression and it doesn't do what I expect.

Writing complex expressions is fine as long as they are readable, but they can be hard to debug. It is often a good idea to break a complex expression into a series of assignments to temporary variables.

For example:

self.hands[i].addCard(self.hands[self.findNeighbor(i)].popCard())

This can be rewritten as:

```
neighbor = self.findNeighbor(i)
pickedCard = self.hands[neighbor].popCard()
self.hands[i].addCard(pickedCard)
```

The explicit version is easier to read because the variable names provide additional documentation, and it is easier to debug because you can check the types of the intermediate variables and display their values.

Another problem that can occur with big expressions is that the order of evaluation may not be what you expect. For example, if you are translating the expression $x/2 \pi$ into Python, you might write:

y = x / 2 * math.pi

That is not correct because multiplication and division have the same precedence and are evaluated from left to right. So this expression computes x π / 2.

A good way to debug expressions is to add parentheses to make the order of evaluation explicit:

y = x / (2 * math.pi)

Whenever you are not sure of the order of evaluation, use parentheses. Not only will the program be correct (in the sense of doing what you intended), it will also be more readable for other people who haven't memorized the rules of precedence. A.3.3 I've got a function or method that doesn't return what I expect.

If you have a return statement with a complex expression, you don't have a chance to print the return value before returning. Again, you can use a temporary variable. For example, instead of:

```
return self.hands[i].removeMatches()
```

```
you could write:
count = self.hands[i].removeMatches()
return count
```

Now you have the opportunity to display the value of count before returning.

16.3.2 I'm really, really stuck and I need help.

First, try getting away from the computer for a few minutes. Computers emit waves that affect the brain, causing these symptoms:

- Frustration and rage.
- Superstitious beliefs ("the computer hates me") and

magical thinking ("the program only works when I wear my hat backward").

• Random walk programming (the attempt to program by writing

every possible program and choosing the one that does the right thing).

If you find yourself suffering from any of these symptoms, get up and go for a walk. When you are calm, think about the program. What is it doing? What are some possible causes of that behavior? When was the last time you had a working program, and what did you do next?

Sometimes it just takes time to find a bug. I often find bugs when I am away from the computer and let my mind wander. Some of the best places to find bugs are trains, showers, and in bed, just before you fall asleep.

16.3.3 No, I really need help.

It happens. Even the best programmers occasionally get stuck. Sometimes you work on a program so long that you can't see the error. A fresh pair of eyes is just the thing.

Before you bring someone else in, make sure you are prepared. Your program should be as simple as possible, and you should be working on the smallest input that causes the error. You should have print statements in the appropriate places (and the output they produce should be comprehensible). You should understand the problem well enough to describe it concisely.

When you bring someone in to help, be sure to give them the information they need:

• If there is an error message, what is it

and what part of the program does it indicate?

• What was the last thing you did before this error occurred?

What were the last lines of code that you wrote, or what is the new test case that fails?

• What have you tried so far, and what have you learned?

When you find the bug, take a second to think about what you could have done to find it faster. Next time you see something similar, you will be able to find the bug more quickly.

Remember, the goal is not just to make the program work. The goal is to learn how to make the program work.

17 Answers

17.1 Chapter 1

17.1.1 Exercise 1.4

If you run a 10 kilometer race in 43 minutes 30 seconds, what is your average time per mile? What is your average speed in miles per hour? (Hint: there are 1.61 kilometers in a mile).

```
>>> 10/1.61 # Convert kilometers to miles
6.2111801242236018
>>> (43*60)+30 # Convert time to seconds
2610
>>> 2610/6.2111801242236018 # what is your average time (seconds) per
mile
420.21000000000004
>>> 420.2100000000000460 # what is your average time (minutes) per
mile
7.0035000000000007
>>> 60/7.003500000000007 # Miles per hour
8.5671449989291055
```

Comment: This is not valid, it **ONLY** works for 43min and 30 seconds to 10km's. Python should have a way to do this the proper way.

In order to do this the proper way, a person must do something like this.

 $43*60 \rightarrow$ convert the minutes to seconds.

 $2580+30 \rightarrow add$ the seconds

 $2610/10 \rightarrow$ divide by distance

 $261/60 \rightarrow$ change seconds into minutes

4.35 -> is the answer, now you must

 $.35{}^{*}60$ -> multiply the number after the decimal with 60

21 seconds..

End result = 4.21 minutes per KM, this technique works for all distances and times.

17.2 Chapter 2

17.2.1 Exercise 2.1

If you type an integer with a leading zero, you might get a confusing error:

Other number seem to work, but the results are bizarre:

```
>>> zipcode = 02132
>>> print zipcode
1114
```

So python is assuming you want to convert an octal number to a decimal number. In the base 8 numbering system where valid numbers are 0, 1, 2, 3, 4, 5, 6 and 7.

```
Base 8: 00 01 02 03 04 05 06 07 10 11 12 13 14 15 16 17 20 21 22 23
24
Base 10: 00 01 02 03 04 05 06 07 08 09 10 11 12 13 14 15 16 17 18 19
20
```

Every 8 numbers we increment the left hand columns. This means that the left most column is the number of 'ones'. The one to the right of that is a tally of the number of 'eights', the one next to that is a tally of a full column of 'eight' times the 'eight column' - 64. The one next to that is 64*8 - 512 and so on. For more information read http://www4.ncsu.edu/unity/lockers/users/f/felder/public/kenny/papers/bases.html Base Eight math¹.

That is why zipcode = 02492 is invalid as the digit 9 is not a valid octal number. We can do the conversion manually as follows:

```
>>> print 02132
1114
>>> (2*512)+(1*64)+(3*8)+(2*1)
1114
>>>
```

17.2.2 Exercise 2.4

The volume of a sphere with radius **r** is $4/3 \pi r3$. What is the volume of a sphere with radius 5?

¹ http://en.wikibooks.org/wiki/%20Base%20Eight%20math

```
>>> pi = 3.1415926535897931
>>> r = 5
>>> 4/3*pi*r**3 # This is the wrong answer
392.69908169872411
>>> r = 5.0 # Radius can be a float here as well, but is not
_necessary_.
>>> 4.0/3.0*pi*r**3 # Using floats give the correct answer
523.59877559829886
>>>
```

Suppose the cover price of a book is \$24.95, but bookstores get a 40% discount. Shipping costs \$3 for the first copy and 75 cents for each additional copy. What is the total wholesale cost for 60 copies?

```
$24.95 Cost
 $9.98 Discount per book
 $14.97 Cost per book after discount
 60
       Total number of books
$898.20 Total cost not inc delivery
 $3.00 First book delivery
 59
       Remaining books
 $0.75 Delivery cost for extra books
 $44.25 Total cost for extra books
 $47.25 Total Delivery cost
$945.45
          Total Bill
This answer is wrong because 40.0/100.0 return wrong value
Floating-Point Arithmetic)
>>> (24.95-24.95*40.0/100.0)*60+3+0.75*(60-1)
945.44999999999993
>>> 24.95*0.6*60+0.75*(60-1)+3
945.45
```

If I leave my house at 6:52 am and run 1 mile at an easy pace (8:15 per mile), then 3 miles at tempo (7:12 per mile) and 1 mile at easy pace again, what time do I get home for breakfast?

Answer: 7:30 am

How I did it:

```
>>> start = (6*60+52)*60
>>> easy = (8*60+15)*2
>>> fast = (7*60+12)*3
>>> finish_hour = (start + easy + fast)/(60*60.0)
>>> finish_floored = (start + easy + fast)/(60*60) #int() function
can also be used to get integer value, but isn't taught yet.
>>> finish_minute = (finish_hour - finish_floored)*60
>>> print 'Finish time was %d:%d' % (finish_hour,finish_minute)
Finish time was 7:30
>>>
```

17.3 Chapter 3

17.3.1 Exercise 3.3

Python provides a built-in function called *len* that returns the length of a string, so the value of len('allen') is 5. Write a function named right_justify that takes a string named *s* as a parameter and prints the string with enough leading spaces so that the last letter of the string is in column 70 of the display.

```
>>> def right_justify(s):
... print (' '*(70-len(s))+s)
...
>>> right_justify('allen')
allen
>>>
```

17.3.2 Exercise 3.4

You can see my solution at http://thinkpython.com/code/grid.py http://thinkpython.com/code/grid.py²http://.

```
.....
Solution to Exercise X.X on page X of Think Python
Allen B. Downey
.....
# here is a mostly-straightforward solution to the
# two-by-two version of the grid.
def do_twice(f):
   f()
    f()
def do_four(f):
    do_twice(f)
    do_twice(f)
def print_beam():
   print ,+ - - - -,,
def print_post():
   print ,|
                    .,
def print_beams():
    do_twice(print_beam)
   print ,+,
def print_posts():
   do_twice(print_post)
    print ,|,
def print_row():
   print_beams()
    do_four(print_posts)
```

² http://en.wikibooks.org/wiki/%20

```
def print_grid():
    do_twice(print_row)
    print_beams()
print_grid()
# here is a less-straightforward solution to the
# four-by-four grid
def one_four_one(f, g, h):
    f()
    do_four(g)
    h()
def print_plus():
    print ,+,,
def print_dash():
    print ,-,,
def print_bar():
    print ,|,,
def print_space():
    print , ,,
def print_end():
    print
def nothing():
    "do nothing"
def print1beam():
    one_four_one(nothing, print_dash, print_plus)
def print1post():
    one_four_one(nothing, print_space, print_bar)
def print4beams():
    one_four_one(print_plus, print1beam, print_end)
def print4posts():
    one_four_one(print_bar, print1post, print_end)
def print_row():
    one_four_one(nothing, print4posts, print4beams)
def print_grid():
    one_four_one(print4beams, print_row, nothing)
print_grid()
comment = """
After writing a draft of the 4x4 grid, I noticed that many of the
functions had the same structure: they would do something, do
something else four times, and then do something else once.
So I wrote one_four_one, which takes three functions as arguments; it
calls the first one once, then uses do_four to call the second one
four times, then calls the third.
Then I rewrote print1beam, print1post, print4beams, print4posts,
print_row and print_grid using one_four_one.
Programming is an exploratory process. Writing a draft of a program
often gives you insight into the problem, which might lead you to
```

rewrite the code to reflect the structure of the solution. --- Allen """ print comment

17.4 Chapter 9

17.4.1 Exercise 9.1

```
fin = open(,words.txt,)
for line in fin:
    word = line.strip()
    if len(word) >= 20:
        print (word)
```

17.5 Chapter 10

17.5.1 Exercise 10.1

Write a function that takes a list of numbers and returns the cumulative sum; that is, a new list where the ith element is the sum of the first i+1 elements from the original list. For example, the cumulative sum of [1, 2, 3] is [1, 3, 6].

```
def cumulative(a):
    cumulative = []
    <u>sum</u> = 0
    for i in a:
        <u>sum</u> += i
        cumulative.append(<u>sum</u>)
    return cumulative
a = [1, 2, 3]
print(cumulative(a))
```

17.5.2 Exercise 10.2

Write a function called chop that takes a list and modifies it, removing the first and last elements, and returns None.

>>> def chop(x): del x[:1] del x[-1:]

Then write a function called middle that takes a list and returns a new list that contains all but the first and last elements.

>>> def middle(x):

This can also be done simply with a slice.

```
>>> def middle(x):
    return x[1:-1]
```

17.6 Chapter 11

17.6.1 Exercise 11.1

```
>>>englishdictionary = dict()
>>>fin = open(,words.txt,)
>>>line = fin.readline()
>>>word = line.strip()
>>>def engdicdefine():
    index = 0
    while index <= 1000:
        englishdictionary[index] = word
        i += 1
    return englishdictionary</pre>
```

17.6.2 Exercise 11.2

```
def histogram(s):
    d = dict()
    for c in s:
        d[c] = 1 + d.get(c, 0)
    return d
```

17.6.3 Exercise 11.4

17.7 Chapter 12

17.7.1 Exercise 12.1

```
numbers = (1,2,3)
def sumall(numbers):
```

```
x = 0
for i in numbers:
    x = x + i
print x
sumall(numbers)
Or
def sumall(*t):
    x = 0
    for i in range(len(t)):
        x += t[i]
    return x
Or
```

```
def sumall(*args):
    t = <u>list(args)</u>
    return <u>sum(t)</u>
```

17.7.2 Exercise 12.2

```
import random
```

```
def sort_by_length(words):
         t = []
         for word in words:
                  t.append((<u>len</u>(word),word))
         t.sort(reverse=True)
         res = []
         for length, word in t:
                  res.append(word)
         i=0
         final = []
         while i <= \underline{len}(res)-2:
                  if \overline{\underline{len}}(res[i]) == \underline{len}(res[i+1]):
                            y_list = [res[i], res[i+1]]
                            random.shuffle(y_list)
                            final = final + y_list
                            i += 2
                  else:
                            final.append(res[i])
                            i += 1
         if i == \underline{len}(res)-1:
                  final.append(res[i])
         return final
```

or

17.7.3 Exercise 12.3

import string

```
def most_frequent(s):
    d = dict()
    inv = dict()
    for char in s:
        if char in string.ascii_letters:
            letter = char.lower()
            d[letter] = d.get(letter, 0) + 1
    for letter, freq in d.items():
            inv.setdefault(freq, []).append(letter)
    for freq in <u>sorted(inv, reverse=True):</u>
        print(,{:.2%}:,.format(freq/(<u>sum(list(inv)*len(inv[freq])))</u>),
    ,, .join(inv[freq]))
```

17.8 Chapter 13

17.8.1 Exercise 13.7

```
from string import punctuation, whitespace, digits
from random import randint
from bisect import bisect_left
def process_file(filename):
        h = \underline{dict}()
        fp = open(filename)
        for line in fp:
                process_line(line, h)
        return h
def process_line(line, h):
        line = line.replace(,-,, , ,)
for word in line.split():
                 word = word.strip(punctuation + whitespace + digits)
                 word = word.lower()
                 if word != ...:
                         h[word] = h.get(word, 0) + 1
hist = process_file(,emma.txt,)
def cum_sum(list_of_numbers):
        cum_list = []
        for i, elem in <u>enumerate(list_of_numbers):</u>
                 if i == 0:
                         cum_list.append(elem)
                 else:
                         cum_list.append(cum_list[i-1] + elem)
        return cum_list
def random_word(h):
        word_list = list(h.keys())
        num_list = []
        for word in word_list:
                num_list.append(h[word])
        cum_list = cum_sum(num_list)
        i = randint(1, cum_list[-1])
        pos = bisect_left(cum_list, i)
```

return word_list[pos]

print(random_word(hist))

17.9 Chapter 14

17.9.1 Exercise 14.3

```
import shelve
```

```
def dict_of_signatures_and_words(filename=,words.txt,):
        d = dict()
        for line in open(filename):
                word = line.lower().strip()
                signature = ,,.join(sorted(word))
                d.setdefault(signature, []).append(word)
        return d
def db_of_anagrams(filename=,anagrams,,
 d=dict_of_signatures_and_words()):
        db = shelve.open(filename)
        for key, values in d.items():
                if <u>len(values)>1:</u>
                         for index, value in <u>enumerate(values):</u>
                                 db[value]=values[:index]+values[index+1:]
        db.close()
def print_contents_of_db(filename=,anagrams,):
        db = shelve.open(filename, flag=,r,)
        for key in <u>sorted</u>(db):
                print(key.rjust(12), _\t<==>\t, _, _, _.join(db[key]))
        db.close()
```

```
db_of_anagrams()
print_contents_of_db()
```

17.9.2 Exercise 14.5

```
# Replace urllib.request with urllib if you use Python 2.
# I would love to see a more elegant solution for this exercise,
possibly by someone who understands html.
import urllib.request
def check(zip_code):
        if zip_code == ,done,:
                return break
        if len(zip_code) != 5:
                print(,\nThe zip code must have five digits!,)
                return continue
def get_html(zip_code):
        gibberish = urllib.request.urlopen(,http://www.uszip.com/zip/, +
zip_code)
        less_gib = gibberish.read().decode(,utf-8,)
        return less_gib
def extract_truth(code, key, delimiter):
```

```
pos = code.find(key) + len(key)
       nearly_true = code[pos:pos+40]
       truth = nearly_true.split(delimiter)[0]
       return truth
while True:
       zip_code = input(,Please type a zip code (5 digits) or "done" if
want to stop:\n,)
        check(zip_code)
        code = get_html(zip_code)
        invalid_key = (0 results),
        if invalid_key in code:
               print(,\nNot a valid zip code.,)
                continue
       name_key = ,zip code of <strong>,
       name_del = ,<,</pre>
       name = extract_truth(code, name_key, name_del)
       pop_key = ,Population:</b>
       pop_del = , <,
       name = extract_truth(code, pop_key, pop_del)
        if not 1 < \underline{len}(pop) < 9:
                pop = ,not available,
       print(,\n, + name)
       print(,Population:,, pop, ,\n,)
```

17.10 Chapter 15

17.10.1 Exercise 15.1

```
import math
class Point(object):
    """represents a point in 2-D space"""
def distance(p1, p2):
    distance = math.sqrt((p2.x - p1.x)**2 + (p2.y - p1.y)**2)
    return distance
p1 = Point()
p2 = Point()
p1.x = 3
p1.y = 2
p2.x = 4
p2.y = 3
print(distance(p1, p2))
```

17.11 Chapter 16

17.11.1 Exercise 16.1

```
def print_time(t):
    print ,%.2d:%.2d, % (t.hour, t.minute, t.second)
```

or

```
# Solution for Python3
# More on string formatting:
http://docs.python.org/py3k/library/string.html#formatspec
```

```
def print_time(t):
    # 0 is a fill character, 2 defines the width
    print(,{}:{:02}:{:02},.<u>format(t.hour, t.minute, t.second</u>))
```

17.11.2 Exercise 16.2

```
def is_after(t1, t2):
    return (t1.hour, t1.minute, t1.second) > (t2.hour, t2.minute,
    t2.second)
```

17.11.3 Exercise 16.3

```
# Comment not by the author: This will give a wrong result, if (time.second + seconds \%~60) > 60
```

```
def increment(time, seconds):
```

n = seconds/60
time.second += seconds - 60.0*n
time.minute += n

```
m = time.minute/60
time.minute -= m*60
time.hour += m
```

or

```
# Solution for Python3
# Replace ,//, by ,/, for Python2
```

def increment(time, seconds):
 time.second += seconds
 time.minute += time.second//60
 time.hour += time.minute//60
 time.second %= 60
 time.minute %= 60
 time.hour %= 24

17.11.4 Exercise 16.4

```
# Solution for Python3
# Replace ,//, by ,/, for Python2
from copy import deepcopy
def increment(time, seconds):
    r = deepcopy(time)
    r.second += seconds
    r.minute += r.second//60
    r.hour += r.minute//60
    r.second %= 60
    r.minute %= 60
    r.hour %= 24
    return r
```

17.11.5 Exercise 16.5

```
class Time(object):
    """represents the time of day.
        attributes: hour, minute, second"""
time = Time()
time.hour = 11
time.minute = 59
time.second = 30
def time_to_int(time):
    minutes = time.hour * 60 + time.minute
    seconds = minutes * 60 + time.second
    return seconds
def int_to_time(seconds):
    time = Time()
    minutes, time.second = <u>divmod</u>(seconds, 60)
    time.hour, time.minute = <u>divmod</u>(minutes, 60)
    return time
def increment(time, addtime):
    seconds = time_to_int(time)
    return int_to_time(seconds + addtime)
def print_time (x):
    print ,The time is \%.2d : \%.2d : \%.2d , \% (x.hour, x.minute,
 x.second)
print_time (time)
newtime = increment (time, 70)
print_time (newtime)
```

17.11.6 Exercise 16.6

```
def time_to_int(time):
    minutes = time.hour * 60 + time.minute
```

```
seconds = minutes * 60 + time.second
return seconds
def int_to_time(seconds):
    time = Time()
    minutes, time.second = <u>divmod</u>(seconds, 60)
    time.hour, time.minute = <u>divmod</u>(minutes, 60)
    return time
def mul_time(time, factor):
    seconds = time_to_int(time)
    seconds = time_to_int(time)
    seconds *= factor
    seconds = <u>int</u>(seconds)
    return int_to_time(seconds)
def average_pace(time, distance):
    return mul_time(time, 1/distance)
```

17.11.7 Exercise 16.7

Write a class definition for a Date object that has attributes *day*, *month* and *year*. Write a function called *increment_date* that takes a Date object, *date*, and an integer, *n*, and returns a new Date object that represents the day *n* days after *date*. Hint: "Thirty days hath September..." Challenge: does your function deal with leap years correctly? See *wikipedia.org/wiki/Leap_year*.

```
class Date(object):
        """ represents a date.
        attributes: day, month, year"""
def print_date(date):
        # German date format
        print(,{}.{}.{}..format(date.day, date.month, date.year))
def is_leap_year(year):
        # http://en.wikipedia.org/wiki/Leap_year#Algorithm
        if year % 4 == 0:
                if year % 100 == 0:
                        if year % 400 == 0:
                                return True
                        return False
                return True
        return False
def month_list(year):
        if is_leap_year(year):
                return [31, 29, 31, 30, 31, 30, 31, 31, 30, 31, 30, 31]
        return [31, 28, 31, 30, 31, 30, 31, 31, 30, 31, 30, 31]
def days_of_year(year):
        if is_leap_year(year):
                return 366
        return 365
def date_to_int(date):
        days = 0
        for year in range(1, date.year):
                days += days_of_year(year)
        month_days = month_list(date.year)
        for month in range(1, date.month):
```

```
days += month_days[month - 1]
        days += date.day - 1
        return days
def int_to_date(days):
        date = Date()
        date.year = 1
        next_days = 365
        while days >= next_days:
                date.year += 1
                days -= next_days
                next_days = days_of_year(date.year)
        date.month = 1
        next_days = 31
        month_days = month_list(date.year)
        while days >= next_days:
                date.month += 1
                days -= next_days
                next_days = month_days[date.month - 1]
        date.day = days + 1
        return date
def increment_date(date, n):
        days = date_to_int(date)
        return int_to_date(days + n)
d1 = Date()
d1.day, d1.month, d1.year = 8, 3, 2012
print_date(d1)
d2 = increment_date(d1, 7)
print_date(d2)
```

17.11.8 Exercise 16.8

1. Use the *datetime* module to write a program that gets the current date and prints the day of the week.

```
from datetime import date

def current_weekday():
        i = date.today().weekday()
        print([,Monday,, ,Tuesday,, ,Wednesday,, ,Thursday,, ,Friday,,
        ,Saturday,, ,Sunday,][i])

current_weekday()
```

17.12 Chapter 3.5

17.12.1 calculator

#recursion or recursive			
print "\n	INDEX\n""\n	C=1 for addition\n""\n	C=2 for
substraction\n""\n			
C=3 for multiplication\n""\n		C=4 for division\n""\n	C=5 for to

```
find modulus\n""\n
                          C=6 to find factorial\n"
C=input("Enter your choice here: ")
def add(x,y):
        c=x+y
        print x,"+",y,"=",c
def sub(x,y):
        c=x-y
        print x, "-", y, "=", c
def mul(x,y):
        c=x*y
        print x,"*",y,"=",c
def div(x,y):
        c=x/y
        print x,"/",y,"=",c
def mod(x,y):
        c=x%y
       print x,"%",y,"=",c
if C==6:
        def f(n):
                if n==1:
                        print n
                        return n
                else:
                        print n,"*",
                        return n*f(n-1)
        n=input("enter your no here: ")
        print f(n)
if C==1:
        a=input("Enter your first no here: ")
        b=input("Enter your second no here: ")
        add(a,b)
elif C==2:
        a=input("Enter your first no here: ")
        b=input("Enter your second no here: ")
        sub(a,b)
elif C==3:
        a=input("Enter your first no here: ")
        b=input("Enter your second no here: ")
        mul(a,b)
elif C==4:
        a=input("Enter your first no here: ")
        b=input("Enter your second no here: ")
        div(a,b)
elif C==5:
        a=input("Enter your first no here: ")
        b=input("Enter your second no here: ")
        mod(a,b)
```

17.12.2 palindrome

```
else:
print "not palindrome"
```

```
word=raw_input("Enter the string:")
palindrome(word)
```

17.12.3 sum of all digits

```
def sum_of_n_numbers(number):
        if(number==0):
                 return 0
         else:
                 return number + sum_of_n_numbers(number-1)
num = raw_input("Enter a number:")
num=int(num)
sum = sum_of_n_numbers(num)
print <u>sum</u>
\#\#\#another answer in case of while loops
def sum_of_Digits(number):
        sum=0
        while number>0:
                 digit=number%10
                 <u>sum</u>=<u>sum</u>+digit
                 number=number/10
        return <u>sum</u>
num=raw_input("enter the number")
num=<u>int(num)</u>
sum_of_digits=sum_of_Digits(num)
print sum_of_digits
```

17.12.4 Exercise 18.5

```
class Card(object):
        suit_names = [,Clubs,, ,Diamonds,, ,Hearts,, ,Spades,]
       rank_names = [None, Ace, 2, 3, 4, 5, 6, 7, 8, 8, 9, 10, Jack, Queen, King]
       def __init__(self, suit = 0, rank = 2):
                self.suit = suit
                self.rank = rank
        def __str__(self):
                return ,%s of %s, % (Card.rank_names[self.rank],
                                                        Card.suit_names[self.suit])
       def __cmp__(self, other):
                c1 = (self.suit, self.rank)
                c2 = (other.suit, other.rank)
                return cmp(c1, c2)
       def is_valid(self):
                return self.rank > 0
class Deck(object):
       def __init__(self, label = _Deck_):
                self.label = label
                self.cards = []
               for i in range(4):
```

```
for k in range(1, 14):
                                card = Card(i, k)
                                self.cards.append(card)
        def __str__(self):
               res = []
                for card in self.cards:
                        res.append(<u>str</u>(card))
                print self.label
                return _\n.join(res)
        def deal_card(self):
                return self.cards.pop(0)
        def add_card(self, card):
                self.cards.append(card)
        def shuffle(self):
                import random
                random.shuffle(self.cards)
        def sort(self):
                self.cards.sort()
        def move_cards(self, other, num):
                for i in range(num):
                        other.add_card(self.deal_card())
        def deal_hands(self, num_hands, num_cards):
                if num_hands*num_cards > 52:
                        return ,Not enough cards.,
                1 = []
                for i in range(1, num_hands + 1):
                        hand_i = Hand(,Hand %d, % i)
                        self.move_cards(hand_i, num_cards)
                        l.append(hand_i)
                return 1
class Hand(Deck):
        def __init__(self, label = ','):
                self.cards = []
                self.label = label
# 18-6, 1-4:
class PokerHand(Hand):
        def suit_hist(self):
                self.suits = {}
                for card in self.cards:
                        self.suits[card.suit] = self.suits.get(card.suit, 0) + 1
                return self.suits
        def rank_hist(self):
                self.ranks = {}
                for card in self.cards:
                        self.ranks[card.rank] = self.ranks.get(card.rank, 0) + 1
                return self.ranks
        def P(self):
                self.rank_hist()
                for val in self.ranks.values():
                        if val >= 2:
                                return True
```

```
return False
def TP(self):
        self.rank_hist()
        count = 0
        for val in self.ranks.values():
                if val == 4:
                        return True
                elif val >= 2 and val < 4:
                        count += 1
        return count >= 2
def TOAK(self):
        self.rank_hist()
        for val in self.ranks.values():
                if val >= 3:
                        return True
        return False
def STRseq(self):
        seq = []
1 = STRlist()
        self.rank_hist()
        h = self.ranks.keys()
        h.sort()
        if <u>len</u>(h) < 5:
                return []
        # Accounts for high Aces:
        if 1 in h:
                h.append(1)
        for i in range(5, <u>len(h)+1):</u>
                if h[i-5:i] in 1:
                        seq.append(h[i-5:i])
        return seq
def STR(self):
        seq = self.STRseq()
        return seq != []
def FL(self):
        self.suit_hist()
        for val in self.suits.values():
                if val >= 5:
                        return True
        return False
def FH(self):
        d = self.rank_hist()
        keys = d.keys()
        for key in keys:
                if d[key] >= 3:
                         keys.remove(key)
                         for key in keys:
                                 if d[key] >= 2:
                                         return True
        return False
def FOAK(self):
        self.rank_hist()
        for val in self.ranks.values():
                if val >= 4:
                        return True
        return False
def SFL(self):
```

```
seq = self.STRseq()
                if seq == []:
                        return False
                for <u>list</u> in seq:
                        list_suits = []
                         for index in <u>list</u>:
                                 for card in self.cards:
                                         if card.rank == index:
                                                 list_suits.append(card.suit)
                         list_hist = histogram(list_suits)
                         for key in list_hist.keys():
                                 if list_hist[key] >= 5:
                                         return True
                return False
        def classify(self):
                self.scores = []
                hands = [,Pair,, ,Two-Pair,,
                 ,Three of a Kind,, ,Straight,,
                 ,Flush,, ,Full House,,
                 ,Four of a Kind,, ,Straight Flush,]
                if self.P():
                        self.scores.append(1)
                if self.TP():
                        self.scores.append(2)
                if self.TOAK():
                         self.scores.append(3)
                if self.STR():
                         self.scores.append(4)
                if self.FL():
                        self.scores.append(5)
                if self.FH():
                         self.scores.append(6)
                if self.FOAK():
                         self.scores.append(7)
                if self.SFL():
                         self.scores.append(8)
                if self.scores != []:
                         return hands[max(self.scores)-1]
def STRlist():
        s = []
        for i in range(0,9):
                s.append(range(1,14)[i:i+5])
        s.append([10,11,12,13,1])
        return s
def histogram(1):
        d = \underline{dict}()
        for k in range(<u>len(l)):</u>
               d[l[k]] = 1 + d.get(l[k],0)
        return d
# 18-6, 5:
def p(config = ,,, trials = 10000, n = 1):
        """Estimates probability that the
        nth dealt hand will be config. A hand
        consists of seven cards."""
        successes = 0
        for i in range(1, trials + 1):
                deck = Deck(,Deck %d, % i)
                deck.shuffle()
                box = Hand()
                deck.move_cards(box, (n-1)*7)
```

```
hand = PokerHand(,Poker Hand %d, % i)
                deck.move_cards(hand, 7)
                if hand.classify() == config:
                        successes += 1
        return 1.0*successes/trials
#Iterate until first desired config.:
if __name__ == ,__main__,:
        c = 1
        while True:
                deck = Deck()
                deck.shuffle()
                hand = PokerHand(,Poker Hand %d, % c)
                deck.move_cards(hand, 5)
                print hand
                print hand.SFL()
                if hand.SFL():
                        print hand.STRseq()
                        break
                print ..
                c += 1
Code by Victor Alvarez
= Index =
```

17.13 Index

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