

Thesis
C78

Thesis
C78

Library
U. S. Naval Postgraduate School
Annapolis, Md.

AIR ISLETS FOR TURBOJET ENGINES
THROUGH THE TRANSONIC SPEED RANGE

A thesis
Submitted to the Graduate Faculty
of the
University of Minnesota

by
James J. Coyle

In Partial Fulfillment of the Requirements
For the Degree of
Master of Science

July 15, 1949

THE UNIVERSITY OF CHICAGO
LIBRARY

75-17
707

THE UNIVERSITY OF CHICAGO
LIBRARY
75-17
707

75-17
707

THE UNIVERSITY OF CHICAGO
LIBRARY
75-17
707

75-17
707

TABLE OF CONTENTS

Chapter	Page
I. Diffuser Analysis--Introduction	1
II. Performance of a Diffuser	5
1. Characteristics of Diffuser Flow.. . . .	5
2. Diffuser Efficiency	9
3. Diffuser Discharge Limitations	15
4. External Drag Considerations	18
III. Diffuser Losses	21
1. Shock Loss	22
2. Entrance Loss	28
3. Yawing Effect	32
4. Expansion Loss	33
A. Boundary Layer in a Diffuser	35
B. Point of Laminar Separation	38
C. Mixing Length	40
D. Point of Separation of the Turbulent Boundary Layer	40
E. Means of Delaying Separation	44
5. Friction Loss	47
6. Turning Loss	50
7. Obstructions in the Flow	53
8. Leakage Loss	56
9. Exit Loss	57
IV. Geometric Considerations	59
1. Inlet Duct Location	59
2. Area Ratios and Diffuser Length	63
3. Velocity Ratio	67
V. Typical Diffuser Problem	73
VI. Present Air Inlet Design Features	86
VII. Conclusions and Recommendations	97
Appendix I--Symbols	101
References	102

TABLE OF CONTENTS

Page	Chapter
1	1. Introduction
2	2. The importance of a library
3	3. The history of libraries
4	4. The functions of a library
5	5. The organization of a library
6	6. The collection of a library
7	7. The management of a library
8	8. The services of a library
9	9. The future of libraries
10	10. The role of libraries in society
11	11. The role of libraries in education
12	12. The role of libraries in research
13	13. The role of libraries in culture
14	14. The role of libraries in information science
15	15. The role of libraries in digital technology
16	16. The role of libraries in social media
17	17. The role of libraries in the digital age
18	18. The role of libraries in the 21st century
19	19. The role of libraries in the future
20	20. The role of libraries in the world
21	21. The role of libraries in the global village
22	22. The role of libraries in the information society
23	23. The role of libraries in the knowledge economy
24	24. The role of libraries in the digital economy
25	25. The role of libraries in the information age
26	26. The role of libraries in the digital age
27	27. The role of libraries in the information age
28	28. The role of libraries in the information age
29	29. The role of libraries in the information age
30	30. The role of libraries in the information age
31	31. The role of libraries in the information age
32	32. The role of libraries in the information age
33	33. The role of libraries in the information age
34	34. The role of libraries in the information age
35	35. The role of libraries in the information age
36	36. The role of libraries in the information age
37	37. The role of libraries in the information age
38	38. The role of libraries in the information age
39	39. The role of libraries in the information age
40	40. The role of libraries in the information age
41	41. The role of libraries in the information age
42	42. The role of libraries in the information age
43	43. The role of libraries in the information age
44	44. The role of libraries in the information age
45	45. The role of libraries in the information age
46	46. The role of libraries in the information age
47	47. The role of libraries in the information age
48	48. The role of libraries in the information age
49	49. The role of libraries in the information age
50	50. The role of libraries in the information age
51	51. The role of libraries in the information age
52	52. The role of libraries in the information age
53	53. The role of libraries in the information age
54	54. The role of libraries in the information age
55	55. The role of libraries in the information age
56	56. The role of libraries in the information age
57	57. The role of libraries in the information age
58	58. The role of libraries in the information age
59	59. The role of libraries in the information age
60	60. The role of libraries in the information age
61	61. The role of libraries in the information age
62	62. The role of libraries in the information age
63	63. The role of libraries in the information age
64	64. The role of libraries in the information age
65	65. The role of libraries in the information age
66	66. The role of libraries in the information age
67	67. The role of libraries in the information age
68	68. The role of libraries in the information age
69	69. The role of libraries in the information age
70	70. The role of libraries in the information age
71	71. The role of libraries in the information age
72	72. The role of libraries in the information age
73	73. The role of libraries in the information age
74	74. The role of libraries in the information age
75	75. The role of libraries in the information age
76	76. The role of libraries in the information age
77	77. The role of libraries in the information age
78	78. The role of libraries in the information age
79	79. The role of libraries in the information age
80	80. The role of libraries in the information age
81	81. The role of libraries in the information age
82	82. The role of libraries in the information age
83	83. The role of libraries in the information age
84	84. The role of libraries in the information age
85	85. The role of libraries in the information age
86	86. The role of libraries in the information age
87	87. The role of libraries in the information age
88	88. The role of libraries in the information age
89	89. The role of libraries in the information age
90	90. The role of libraries in the information age
91	91. The role of libraries in the information age
92	92. The role of libraries in the information age
93	93. The role of libraries in the information age
94	94. The role of libraries in the information age
95	95. The role of libraries in the information age
96	96. The role of libraries in the information age
97	97. The role of libraries in the information age
98	98. The role of libraries in the information age
99	99. The role of libraries in the information age
100	100. The role of libraries in the information age

LIST OF FIGURES

1. Effect of Ram Recovery Ratio on the Maximum Available Net Thrust of a Turbo-jet Engine at Sea Level.
2. Effect of Ram Recovery Ratio on Specific Fuel Consumption at Maximum Available Net Thrust of a Typical Turbo-jet Engine at Sea Level.
3. Change in Net Thrust and Specific Fuel Consumption for an Increase of Ram Recovery Ratio from 0.70 to 0.90.
4. Comparison of Test Results with Theoretical Expectations for Diffusers with Internal Shock.
5. Ram Recovery Ratio Across a Normal Shock.
6. Theoretical Pressure Recovery Ratio after "n" Compression Shocks, n - 1 oblique Shocks Plus One Normal Shock.
7. Effect of Exit Cone Angle on the Performance of Two Supersonic Diffusers.
8. Velocity Decrement Obtainable before Laminar Separation Occurs.
9. Improvement of Diffuser Efficiency with Suction.
10. Effect of Radius Ratio and Deflection Angle on Turning Losses in Ducts.
11. Influence of Aspect Ratio on Turning Losses in Ducts.
12. Effect of Gap/Chord Ratio on Resistance Coefficient.
13. Losses in Expanding Entries.
14. Obstruction Loss Coefficient in a Duct.
15. Length of Constant Area Duct Following a Diffuser Necessary for Complete Pressure Recovery.
16. Variation of Area Ratio with Entrance Mach Number to Give an Exit Mach Number of 0.3.
17. Length of Conical Diffuser Required for Various Entrance Mach Numbers.

18. Diffuser Geometry for Illustrative Problem.
19. Shape of Diffuser Entrance and Static Pressure Distribution.
20. Internal Conditions in the Diffuser.
21. Friction Effects in the Diffuser.
22. Friction Losses in the Duct Connecting the Diffuser and the Compressor
23. Variation of Velocity Ratio with Flight Mach Number.
24. Variation of Flow Density with Flight Mach Number and Altitude.

26. The following is a list of the most important factors which influence the rate of reaction between two reactants.
27. The rate of reaction between two reactants is influenced by the following factors:
 - (a) Concentration of the reactants
 - (b) Temperature
 - (c) Surface area of the reactants
 - (d) Nature of the reactants
 - (e) Presence of a catalyst
28. The rate of reaction between two reactants is influenced by the following factors:
 - (a) Concentration of the reactants
 - (b) Temperature
 - (c) Surface area of the reactants
 - (d) Nature of the reactants
 - (e) Presence of a catalyst
29. The rate of reaction between two reactants is influenced by the following factors:
 - (a) Concentration of the reactants
 - (b) Temperature
 - (c) Surface area of the reactants
 - (d) Nature of the reactants
 - (e) Presence of a catalyst
30. The rate of reaction between two reactants is influenced by the following factors:
 - (a) Concentration of the reactants
 - (b) Temperature
 - (c) Surface area of the reactants
 - (d) Nature of the reactants
 - (e) Presence of a catalyst

CHAPTER I

DIFFUSER ANALYSIS--INTRODUCTION

On September 15, 1948, a North American P-36A set a new world air speed record of 670.981 mph at Muroc, California. The average mach number of this speed trial was 0.87. The P-36A is powered by a General Electric-Allison J-35 turbojet engine. This was the fourth time in twenty seven months that the world air speed record was broken by a turbo-jet powered aircraft. On December 22, 1947, an aviation magazine published a report that the Bell XS-1, a rocket powered aircraft, had exceeded a flight mach number of 1.0 at altitude. Meanwhile, other experimental aircraft such as the Douglas D-558-II, the Bell XS-2, the Douglas XS-3, and the Northrop XS-4 are being developed for investigating transonic flight.

On the basis of this information it is obvious that rapid strides are being made in the field of aviation. As flight speeds approach and pass the speed of sound new problems arise which influence the design of aircraft and aircraft engines. Foremost among these problems is the phenomenon that air at these flight mach numbers is compressible, and behaves in a quite different manner than it does at relatively low speeds.

THE HISTORY OF THE UNITED STATES

The history of the United States is a story of a young nation that grew from a small group of colonies on the eastern coast of North America to a powerful superpower that spans across two continents. The story begins with the arrival of European explorers in the late 15th century, who discovered the New World. The first permanent English colony was established in Jamestown, Virginia, in 1607. Over the next century, more colonies were founded along the eastern coast, each with its own unique character and challenges. The colonies were united by a common language, culture, and a shared desire for self-governance. In 1776, the colonies declared their independence from Great Britain, and the United States was born. The new nation faced many challenges, including a weak central government and a series of wars with neighboring powers. However, through a series of compromises and a strong sense of national identity, the United States emerged as a powerful and influential nation. The 19th century was a time of rapid growth and expansion, as the United States moved westward across the continent. The Civil War, fought between 1861 and 1865, was a defining moment in the nation's history, as it resolved the issue of slavery and preserved the Union. The 20th century was a time of global leadership, as the United States emerged as a superpower and played a leading role in the world. The United States has a rich and diverse history, and its story continues to unfold in the present day.

The question also arises as to which type of propulsion system is best fitted for use at speeds near the speed of sound. The commonly recognized types of propulsion systems for airborne vehicles are the reciprocating engine driven propeller, the turbine driven propeller, the turbo-jet, the ram-jet, and the rocket. Only the last mentioned is independent of air supply for the generation of power.

At high speeds propeller efficiency declines rapidly so the use of a propeller driven aircraft near the speed of sound is not practical. This is further indicated by the present speed advantage of jet powered aircraft over propeller driven aircraft. The rocket, since it is independent of air supply, appears to have a big advantage, but it is so inefficient at low supersonic mach numbers that its fuel demands severely restrict the flight duration. Its use in present experimental type aircraft is based upon a desire to reach supersonic speeds, if only for a short duration, to obtain data to prove and develop aerodynamic designs for supersonic flight. It should be noted that auxiliary means are used to bring these aircraft up to high speed before the rocket power is utilized. The X8-1 is air launched from another aircraft, and the X-550-II has a turbo-jet engine for subsonic flight.

The ram-jet engine has a restricted use due to design limitations. It is efficient for only one flight

The question arises whether we should give up
 the right to work in order to avoid the
 possibility of being forced to work in
 some of the most dangerous and health-
 hazardous conditions in the world.
 It is a question of the right to
 work, and the right to work is
 not a luxury, it is a basic right.
 The right to work is the right to
 be able to support one's family
 and to participate in the life of
 the community. It is the right to
 be able to contribute to society
 and to be able to share in the
 benefits of the social system.
 The right to work is the right to
 be able to live with dignity and
 to be able to have a say in the
 decisions that affect one's life.
 It is the right to be able to
 work in conditions that are
 safe and sound, and to be able to
 work for a living wage.
 The right to work is the right to
 be able to work in a free and
 democratic society, and to be able
 to work for the betterment of
 the world.

mach number, and cannot develop sufficient thrust to reach this design point unaided. Furthermore, at flight mach numbers below 1.5 the turbo-jet is theoretically more efficient.

After considering the principal disadvantages of the other types of propulsion systems, the suitability of the turbo-jet for transonic operation will be considered. Fig. 1, which was obtained from Ref. 1, shows the variation of thrust with flight velocity at various values of ram recovery ratio. Ram recovery ratio is a measure of diffuser efficiency, and is defined thus:

$$\text{Ram recovery ratio} = \frac{P_2^0 - P_0}{P_0^0 - P_0}$$

As can be seen, thrust does vary with flight velocity, particularly with low values of ram recovery ratio. Thrust is even more sensitive to engine rpm. The turbo-jet's moving parts consist of a directly coupled turbine and compressor. The characteristics of these two units are such that peak efficiency occurs at a particular design engine speed, variations from this design point result in reduced engine performance. Fig. 1 reveals that the thrust decreases with flight velocity down to a minimum, and then increases with further speed increase if the ram recovery ratio is sufficiently high.

Fig. 2 shows the variation of specific fuel consumption with flight velocity with various ram recovery ratios. These curves are also a measure of the

the theory, the model is considered as a
 simple case of the general theory, and
 the theory is considered as a special case
 of the general theory.

After discussing the general theory, we
 will then discuss the special case, and
 the theory is considered as a special case
 of the general theory. The theory is
 considered as a special case of the
 general theory, and the theory is
 considered as a special case of the
 general theory.

$$\frac{a^2 - b^2}{a^2 + b^2} = \frac{a - b}{a + b}$$

It can be seen from the above equation
 that the theory is considered as a
 special case of the general theory, and
 the theory is considered as a special case
 of the general theory. The theory is
 considered as a special case of the
 general theory, and the theory is
 considered as a special case of the
 general theory.

The theory is considered as a special case
 of the general theory, and the theory is
 considered as a special case of the
 general theory. The theory is considered
 as a special case of the general theory,
 and the theory is considered as a special
 case of the general theory. The theory
 is considered as a special case of the
 general theory, and the theory is
 considered as a special case of the
 general theory.

efficiency of a turbo-jet unit. They show that for high ram recovery ratios, the specific fuel consumption increases with flight velocity but tends to level off after reaching some maximum value. From a study of Figs. 1 and 2 the conclusion can be drawn that the turbo-jet offers efficient operation from the static thrust condition to speeds near the speed of sound provided the diffuser ram recovery ratio is sufficiently high. These curves would show the same trends if they were extrapolated into the range of low supersonic mach numbers. The improvement in performance with increased ram recovery ratio is shown in Fig. 3. For example, it shows that for an airplane flying at 650 mph at sea level an increase in ram recovery ratio from 0.70 to 0.90 will result in an 15.9 per cent increase in net thrust and a 9.5 per cent decrease in specific fuel consumption. Such figures indicate the importance of high diffuser efficiency.

The first part of the document is a letter from the Secretary of the State Department to the Secretary of the War Department. The letter is dated August 1, 1918, and is addressed to the Secretary of the War Department, Washington, D.C. The letter is signed by the Secretary of the State Department, Robert Lansing.

The letter discusses the proposed transfer of the War Relocation Authority to the War Relocation Administration. The letter states that the War Relocation Authority was established by Executive Order on June 17, 1918, and is currently operating under the War Relocation Act. The letter proposes that the War Relocation Authority be transferred to the War Relocation Administration, which is currently operating under the War Relocation Act.

The letter also discusses the proposed transfer of the War Relocation Authority to the War Relocation Administration. The letter states that the War Relocation Authority was established by Executive Order on June 17, 1918, and is currently operating under the War Relocation Act. The letter proposes that the War Relocation Authority be transferred to the War Relocation Administration, which is currently operating under the War Relocation Act.

The letter concludes with a request for the Secretary of the War Department to approve the proposed transfer of the War Relocation Authority to the War Relocation Administration. The letter is signed by the Secretary of the State Department, Robert Lansing.

CHAPTER II
PERFORMANCE OF A DIFFUSER

1. Characteristics of Diffuser Flow.

Recognizing the advantages to be gained by efficient air induction into a turbojet engine, the mechanics of the air induction process will be investigated. For purposes of analysis it will be assumed that the engine is fixed in space and the air is flowing through and past it with an undisturbed free stream velocity equal to the flight velocity of the airplane. The velocity of flow at the entrance to the diffuser will not be the same as the undisturbed free stream velocity except at one flight velocity. The volume of airflow through the engine is a function of the engine speed. The flow velocity at the diffuser entrance depends upon this volume flow and the entrance area of the diffuser. Therefore, some process will occur before the air enters the diffuser. At low speeds, the air expands and accelerates into the diffuser; at high speeds, the air is compressed and decelerates into the diffuser. This process occurring before the air enters the diffuser is assumed to be isentropic.

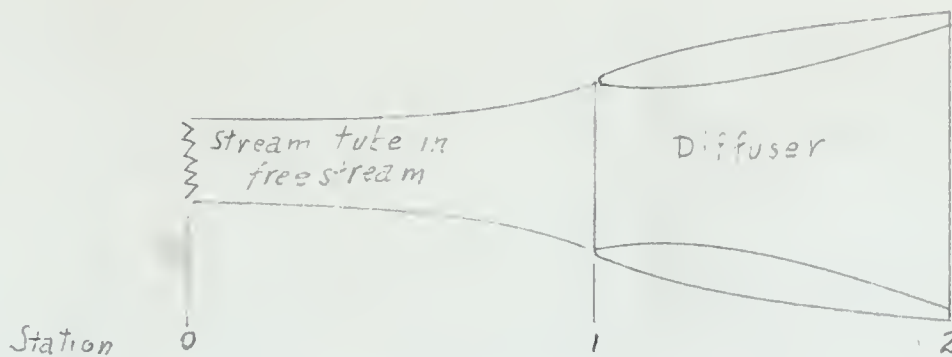
The following equations can be used to determine the state of the air at the entrance to the diffuser.

1. Introduction to the Report

The following information was obtained from the records of the Department of Health and Human Services, Office of the Assistant Secretary for Health, regarding the activities of the National Health and Medical Research Council (NH&MRC) during the period from 1970 to 1975. The information is presented in the following order: (1) a list of the members of the Council; (2) a list of the projects funded by the Council; (3) a list of the reports published by the Council; and (4) a list of the names of the individuals who have been associated with the Council in various capacities.

The Council was established in 1970 and is composed of representatives from the medical, nursing, and public health professions. Its primary function is to advise the Government on matters relating to health and medical research. The Council has been instrumental in the development of many of the health policies and programs currently in effect in Australia.

The following information was obtained from the records of the Department of Health and Human Services, Office of the Assistant Secretary for Health, regarding the activities of the National Health and Medical Research Council (NH&MRC) during the period from 1970 to 1975. The information is presented in the following order: (1) a list of the members of the Council; (2) a list of the projects funded by the Council; (3) a list of the reports published by the Council; and (4) a list of the names of the individuals who have been associated with the Council in various capacities.



$$\frac{A_0}{A_1} = \frac{M_1}{M_0} \left(\frac{1 + \frac{\gamma-1}{2} M_0^2}{1 + \frac{\gamma-1}{2} M_1^2} \right)^{\frac{\gamma+1}{2(\gamma-1)}}$$

$$\frac{P_0}{P_1} = \left(\frac{1 + \frac{\gamma-1}{2} M_1^2}{1 + \frac{\gamma-1}{2} M_0^2} \right)^{\frac{\gamma}{\gamma-1}} \quad P_0^0 = P_1^0 \text{ (Isentropic flow)}$$

$$\frac{T_0}{T_1} = \left(\frac{1 + \frac{\gamma-1}{2} M_1^2}{1 + \frac{\gamma-1}{2} M_0^2} \right) \quad T_0^0 = T_1^0 \text{ (Adiabatic flow)}$$

To consider the nature of the flow within the diffuser, let us write the following equations:

Euler's equation for one dimensional frictionless flow:

$$v dv + \frac{dp}{\rho} = 0 \quad (a)$$

Continuity equation:

$$\frac{d\rho}{\rho} + \frac{dA}{A} + \frac{dv}{v} = 0 \quad (b)$$

Definition of the speed of sound:

$$a^2 = \frac{dp}{d\rho} \quad (c)$$



$$\frac{+Y}{-Y} \cdot \left(\frac{+Y}{-Y} + \frac{-Y}{+Y} \right) = \frac{+Y}{-Y}$$

$$\frac{+Y}{-Y} \cdot \left(\frac{-Y}{+Y} + \frac{+Y}{-Y} \right) = \frac{+Y}{-Y}$$

$$\frac{-Y}{+Y} \cdot \left(\frac{+Y}{-Y} + \frac{-Y}{+Y} \right) = \frac{-Y}{+Y}$$

In finding the value of the sum of the terms of a geometric series, we use the following formula:

Let S_n be the sum of the first n terms of a geometric series with first term a and common ratio r .

$$S_n = \frac{a(1-r^{n+1})}{1-r}$$

Example:

$$S_4 = \frac{1(1-2^5)}{1-2} = \frac{1(1-32)}{-1} = \frac{-31}{-1} = 31$$

Find the sum of the first 5 terms of the geometric series.

$$S_5 = \frac{1(1-2^6)}{1-2} = \frac{1(1-64)}{-1} = \frac{-63}{-1} = 63$$

Substituting eq. (c) in (a), and combining eqs. (a) and (b), we arrive at the following expression:

$$\frac{dV}{V} (1-M^2) = - \frac{dA}{A} \quad (d)$$

This equation reveals that, for subsonic flow, velocity decreases with an increase in area; the reverse is true for supersonic flows. To decelerate a supersonic flow isentropically to subsonic would require a converging channel, followed by a diverging section. The velocity at the throat would be sonic.

However, the flow in a channel is not isentropic, but it is essentially adiabatic, therefore the result of an entropy increase can be determined from the definition of entropy increase as given in Ref. 2, p. 11.

$$ds = c_p \frac{dT}{T} - R \frac{dp}{p}$$

$$T^0 = T \left(1 + \frac{\gamma-1}{2} M^2 \right)$$

$$p^0 = p \left(1 + \frac{\gamma-1}{2} M^2 \right)^{\frac{\gamma}{\gamma-1}}$$

$$\frac{ds}{R} = \frac{\gamma}{\gamma-1} \frac{dT^0}{T^0} - \frac{dp^0}{p^0}$$

And since the process is adiabatic, $ds = 0$, and

$$\frac{dT^0}{T^0} = - \frac{dp^0}{p^0}$$

$$\frac{p_2^0}{p_1^0} = e^{-\frac{\Delta s}{R}}$$

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.
Find $(f+g)(x)$ and $(f-g)(x)$.

$$(f+g)(x) = (x^2 + 2x + 1) + (x^2 - 2x + 1)$$

Combine like terms:
 $(f+g)(x) = x^2 + 2x + 1 + x^2 - 2x + 1$
 $(f+g)(x) = 2x^2 + 2$
 $(f-g)(x) = (x^2 + 2x + 1) - (x^2 - 2x + 1)$
 $(f-g)(x) = x^2 + 2x + 1 - x^2 + 2x - 1$
 $(f-g)(x) = 4x$

$$(f+g)(x) = 2x^2 + 2$$

$$(f-g)(x) = 4x$$

$$f(x) = x^2 + 2x + 1$$

$$g(x) = x^2 - 2x + 1$$

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.

$$\begin{aligned} f(x) &= x^2 + 2x + 1 \\ g(x) &= x^2 - 2x + 1 \end{aligned}$$

The quantities p° and T° are defined as total pressure and total temperature. They are the values which would be obtained if the flow were slowed isentropically until it had zero velocity. Since according to the second law of thermodynamics, $dS > 0$, then $p_1^{\circ} > p_2^{\circ}$, or in a non-isentropic process a decrease in total pressure accompanies an entropy increase. The conditions of flow at the diffuser exit are given by the following equations, M_2 being found as an implicit function of the entrance conditions.

$$\frac{M_2}{\left(1 + \frac{\gamma-1}{2} M_2^2\right)^{\frac{\gamma+1}{2(\gamma-1)}}} = \frac{A_1}{A_2} \frac{p_1^{\circ}}{p_2^{\circ}} \frac{M_1}{\left(1 + \frac{\gamma-1}{2} M_1^2\right)^{\frac{\gamma+1}{2(\gamma-1)}}}$$

$$\frac{p_2}{p_1} = \frac{p_2^{\circ}}{p_1^{\circ}} \left(\frac{1 + \frac{\gamma-1}{2} M_1^2}{1 + \frac{\gamma-1}{2} M_2^2} \right)^{\frac{\gamma}{\gamma-1}}$$

$$\frac{T_2}{T_1} = \left(\frac{1 + \frac{\gamma-1}{2} M_1^2}{1 + \frac{\gamma-1}{2} M_2^2} \right)$$

The above equations show that diffuser losses have the effect of increasing the exit Mach number for a given area ratio, and decreasing the static pressure recovery. Where the diffuser is being designed for a given exit Mach number, suitable for use in the compressor, the effect of the loss is to require use of a larger area ratio, increasing the diffuser length or increasing the rate of pressure recovery.

The condition for the existence of a solution is that the determinant of the system is not zero. This is satisfied if the matrix is invertible. The condition for the existence of a solution is that the determinant of the system is not zero. This is satisfied if the matrix is invertible.

$$\frac{1}{\sqrt{1-x^2}} = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{1}{\sqrt{1-x^2}} = \frac{1}{\sqrt{1-x^2}}$$

$$\frac{1}{\sqrt{1-x^2}} = \frac{1}{\sqrt{1-x^2}}$$

The above condition is satisfied for all values of x. The condition for the existence of a solution is that the determinant of the system is not zero. This is satisfied if the matrix is invertible.

2. Diffuser Efficiency.

Diffuser efficiency is defined in many different ways. Some of these definitions have advantages in defining a particular aspect of diffuser performance, others may be more applicable to low velocity flows. In general, for the definition to be suitable it should fulfill certain requirements. Ref. 1 lists the following requirements for a diffuser efficiency parameter:

1. It should be readily measured.
2. Have a maximum value of unity to indicate the best possible diffuser performance, no pressure loss.
3. Remain essentially constant for the subsonic speed range (provided there are no energy losses due either to shock formation or separation resulting from changes in Reynold's number).

The third requirement mentioned above might be subjected to the criticism that we are interested not only in a device for energy conversion in subsonic flows, but also for use with supersonic flows. Also, why is it necessary that it remain constant? What interests us most in evaluating the diffuser is what is the relative energy remaining in the flow at the exit compared to the energy available in the flow ahead of the diffuser. More than one efficiency parameter may satisfy these requirements. Since no standard definition

THE UNIVERSITY OF CHICAGO

THE UNIVERSITY OF CHICAGO LIBRARY

500 EAST 57TH STREET, CHICAGO, ILL. 60637

TEL: 773-936-3000

FAX: 773-936-3000

WWW.CHICAGO.LIBRARY.EDU

CHICAGO, ILL. 60637

LIBRARY

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

CHICAGO, ILL. 60637

of diffuser efficiency has been decided upon, it is best to be acquainted with the various definitions which may be encountered.

Ram recovery ratio. This has been discussed previously in connection with the improved performance of a turbojet engine with efficient pressure recovery. This parameter was chosen by the authors of Ref. 1 as best fulfilling the requirements which they set forth for a satisfactory diffuser efficiency parameter. It is defined as follows:

$$\text{Ram recovery ratio} = \frac{P_2^0 - P_0}{P_1^0 - P_0}$$

Exponential form. This form of expressing diffuser efficiency has more appeal to the thermodynamicist or mathematician. This parameter expresses the fraction of the kinetic energy increment which is converted into pressure. Ref. 2, p. 83, presents the development of this definition in the following manner.

$$\eta_D v dv = - \frac{dp}{\rho} \quad (a)$$

From the energy equation:

$$v dv = - c_p dT = \frac{-\gamma}{\gamma-1} d \left(\frac{P}{\rho} \right) \quad (b)$$

Combining eq. (a) and (b), and integrating produces:

to discuss with you the various definitions of the word "probability" as used in the text.

The main idea of this chapter is to show that the concept of probability is not a simple one, and that it is not a simple matter to give a definition of it. The author shows that the concept of probability is a very broad one, and that it is not a simple matter to give a definition of it. The author shows that the concept of probability is a very broad one, and that it is not a simple matter to give a definition of it.

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

Probability is a measure of the likelihood of an event occurring. It is a number between 0 and 1, inclusive. The probability of an event occurring is the ratio of the number of favorable outcomes to the total number of possible outcomes. This is the classical definition of probability. The author shows that the concept of probability is a very broad one, and that it is not a simple matter to give a definition of it.

(a)

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

(b)

$$P(A|B) = \frac{P(A \cap B)}{P(B)}$$

The author shows that the concept of probability is a very broad one, and that it is not a simple matter to give a definition of it.

$$\frac{P_2}{P_0} = \left(\frac{P_2}{P_0}\right)^{1 - \frac{\gamma-1}{\eta_D \gamma}} \quad (c)$$

$$\text{or } \left(\frac{P_2}{P_0}\right)^{\eta_D \frac{\gamma}{\gamma-1}} = \frac{P_2}{P_0} \quad (d)$$

Since the process is polytropic, and the pressure-temperature relationship for a polytropic process is:

$$\left(\frac{T_2}{T_0}\right)^{\frac{\eta}{\eta-1}} = \frac{P_2}{P_0} \quad (e)$$

Then,

$$\eta_D = \frac{\eta/\eta-1}{\gamma/\gamma-1} \quad (f)$$

For incompressible flow:

$$\eta_D = \frac{P_2 - P_0}{\Delta q}$$

Dynamic pressure recovery ratio. This quantity is defined in the following manner:

$$\text{Dynamic pressure recovery ratio} = \frac{P_2^0 - P_0}{q_0}$$

$$= \text{Ram recovery ratio} \times (1 + \eta)$$

$$(1 + \eta) = 1 + \frac{\eta^2}{4} + \frac{\eta^4}{40} + \frac{\eta^6}{1600} + \dots$$

At low subsonic mach numbers this parameter is the same as ram recovery ratio, but since it ignores the compressibility factor $(1 + \eta)$, it diverges rapidly as mach number increases. With very high efficiency of pressure recovery it can exceed one, and so it is not desirable for measuring the efficiency of a compressible flow.

11

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

12

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

13

These two cases are identical, and the result is the same. The result is that the result is the same.

14

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

15

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

The result is that the result is the same.

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

The result is that the result is the same. The result is that the result is the same.

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

The result is that the result is the same.

$$\frac{Y}{Y^{\Delta}} = \frac{Y^{\Delta}}{Y^{\Delta}} = 1$$

The result is that the result is the same. The result is that the result is the same.

The result is that the result is the same. The result is that the result is the same.

The result is that the result is the same. The result is that the result is the same.

The result is that the result is the same. The result is that the result is the same.

Total pressure ratio. This parameter has direct application in turbojet performance calculations. It is the ratio of the total pressure at the diffuser outlet to the free stream total pressure. It is important because it is a direct measure of the entropy increase in the compression process. It is considerably affected by the mach number of the flow.

$$\text{Total pressure ratio} = \frac{p_2^0}{p_0^0} = e^{-\frac{\Delta s}{R}}$$

Pressure ratio. This parameter is given in most turbojet engine performance manuals and is directly applicable for the computation of net thrust, air flow, and specific fuel consumption. It is the ratio of the total pressure at the diffuser outlet to the free stream static pressure. Since it will be almost always greater than one, it is not too useful as a measure of the diffuser efficiency.

$$\text{Pressure ratio} = \frac{p_2^0}{p_0}$$

Energy ratio. This efficiency parameter is defined as the kinetic energy recovered by the air induction system, divided by the kinetic energy available in the airstream. It is derived in the following manner:

From the energy equation

$$c_p T_0 + \frac{V_0^2}{2gJ} = c_p T_0^0$$

The first part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. The second part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow 0$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow 0$.

$$\Delta u = \frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2}$$

The third part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. The fourth part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow 0$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow 0$.

$$\frac{\partial u}{\partial x} = \frac{\partial u}{\partial y} + \frac{\partial u}{\partial z}$$

The fifth part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. The sixth part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow 0$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow 0$.

$$\frac{\partial^2 u}{\partial x^2} + \frac{\partial^2 u}{\partial y^2} + \frac{\partial^2 u}{\partial z^2} = 0$$

and the pressure temperature relationship

$$\frac{T_0}{T_0^0} = \left(\frac{p_0}{p_0^0}\right)^{\frac{\gamma-1}{\gamma}}$$

the following expression for the kinetic energy available is obtained,

$$\frac{V_0^2}{2gJ} = c_p \left[T_0^0 - T_0 \left(\frac{p_0}{p_0^0}\right)^{\frac{\gamma-1}{\gamma}} \right]$$

As the exit from the diffuser the total pressure is p_2^0 and the total temperature is T_2^0 . If these quantities are reconverted to free stream conditions where the free stream static pressure is p_0 , and the air velocity V_0' is less than V_0 because of the pressure losses involved, then

$$\frac{(V_0')^2}{2gJ} = c_p \left[T_2^0 - T_0' \left(\frac{p_0}{p_2^0}\right)^{\frac{\gamma-1}{\gamma}} \right]$$

The above equation represents the kinetic energy which was recovered from the airstream. Since the process is adiabatic, T_0^0 equals T_2^0 , and the energy ratio equation can be written:

$$\text{Energy Ratio} = \frac{T_2^0 - T_0' \left(\frac{p_0}{p_2^0}\right)^{\frac{\gamma-1}{\gamma}}}{T_0^0 - T_0' \left(\frac{p_0}{p_0^0}\right)^{\frac{\gamma-1}{\gamma}}}$$

or

$$\text{Energy Ratio} = 1 - \frac{2}{(\gamma-1) \frac{V_0^2}{c_p T_0^0}} \left[\left(\frac{p_0}{p_2^0}\right)^{\frac{\gamma-1}{\gamma}} - 1 \right]$$

THE UNIVERSITY OF CHICAGO PRESS

$$\left[\frac{1}{Y} \left(\frac{1}{Y} - 1 \right) \right] = \frac{1}{Y}$$

THE UNIVERSITY OF CHICAGO PRESS

CHICAGO, ILLINOIS

$$\left[\frac{1}{Y} \left(\frac{1}{Y} - 1 \right) \right] = \frac{1}{Y}$$

THE UNIVERSITY OF CHICAGO PRESS
 CHICAGO, ILLINOIS
 THE UNIVERSITY OF CHICAGO PRESS
 CHICAGO, ILLINOIS

$$\left[\frac{1}{Y} \left(\frac{1}{Y} - 1 \right) \right] = \frac{1}{Y}$$

THE UNIVERSITY OF CHICAGO PRESS
 CHICAGO, ILLINOIS
 THE UNIVERSITY OF CHICAGO PRESS
 CHICAGO, ILLINOIS

$$\frac{\frac{1}{Y} - 1}{\frac{1}{Y}} = \frac{1}{Y} - 1$$

$$\left[\frac{1}{Y} \left(\frac{1}{Y} - 1 \right) \right] = \frac{1}{Y} - 1$$

Power Ratio. This definition of diffuser efficiency is used in Ref. 3, and is the ratio of the power transformed to pressure energy to the power supplied for transformation.

Power supplied for transformation =

$$\int_{A_1} \frac{1}{2} \rho w^2 u dA - \int_{A_2} \frac{1}{2} \rho w^2 u dA$$

u - axial flow velocity.

w - air stream velocity.

$$\text{Power transformed} = \int_{A_2} p u dA - \int_{A_1} p u dA$$

If the airflow is axial only, and the flow is one-dimensional, then

$$\text{Power ratio} = \frac{P_2 u_2 A_2 - P_1 u_1 A_1}{\frac{1}{2} \rho u_1^3 A_1 - \frac{1}{2} \rho u_2^3 A_2}$$

For incompressible flow, $u_1 A_1 = u_2 A_2$, and the power ratio can be written,

$$\text{Power ratio} = \frac{P_2 - P_1}{\frac{1}{2} \rho u_1^2 \left(1 - \frac{\rho_2 u_2^2}{\rho_1 u_1^2}\right)} = \frac{P_2 - P_1}{q_1 \left(1 - \left(\frac{A_1}{A_2}\right)^2\right)}$$

Since this definition of diffuser efficiency is based upon the assumption of incompressible flow, it is of little value for the types of flow which will be considered.

Diffuser efficiency based on static pressure rise.

This definition of diffuser efficiency is the ratio of

THESE RESULTS... THE DEFINITION OF...
... IS GIVEN IN THE...
... OF THE...
... THE...

... THE...

$$10^2 - 9^2 = 19$$

$$a = 10, b = 9$$

$$a^2 - b^2 = 19$$

$$10^2 - 9^2 = 19$$

IT IS EASY TO SEE THAT...

...

$$\frac{10^2 - 9^2}{10 - 9} = 19$$

THE DEFINITION...

...

$$\frac{10^2 - 9^2}{10 - 9} = 19$$

...

...

...

...

...

...

the static pressure rise obtained to the sum of the static pressure rise obtained plus the total pressure loss in the diffuser.

$$\eta_D = \frac{P_2 - P_0}{(P_2 - P_0) - (P_0^0 - P_2^0)}$$

This definition of diffuser efficiency is not unlike ram recovery ratio, which may be written in the following manner:

$$\text{Ram recovery ratio} = \frac{(P_0^0 - P_0) - (P_0^0 - P_2^0)}{P_0^0 - P_0}$$

Ram recovery ratio when written in this manner is the ratio of the maximum possible pressure rise less the total pressure loss in the diffuser to the maximum possible pressure rise. The simplicity of ram recovery ratio would make it preferable to the diffuser efficiency based on static pressure rise if the selection of a definition were a matter of choice.

3. Diffuser Discharge Limitations.

The main air intake duct of a turbojet engine is designed as a diffuser because at present flight velocities the velocity of the incoming air must be reduced before the air is introduced into the compressor. The desired velocity of the air at the diffuser exit depends upon the compressor design. Present types of compressors operate with subsonic velocities because their capacity and efficiency would fall if supersonic relative

The first part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions tend to zero as $t \rightarrow \infty$ if and only if the matrix A is stable.

$$\frac{dx}{dt} = Ax, \quad x(0) = x_0$$

The second part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions tend to zero as $t \rightarrow \infty$ if and only if the matrix A is stable.

$$\frac{dx}{dt} = Ax, \quad x(0) = x_0$$

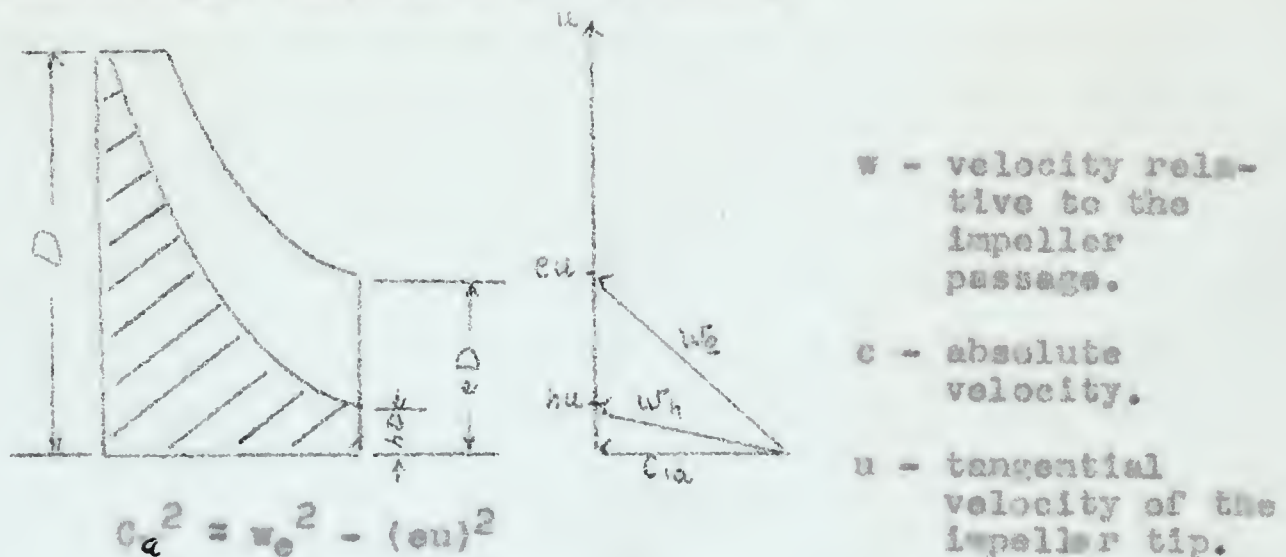
The third part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions tend to zero as $t \rightarrow \infty$ if and only if the matrix A is stable.

3. Asymptotic behavior of the solutions

The first part of this section is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions tend to zero as $t \rightarrow \infty$ if and only if the matrix A is stable.

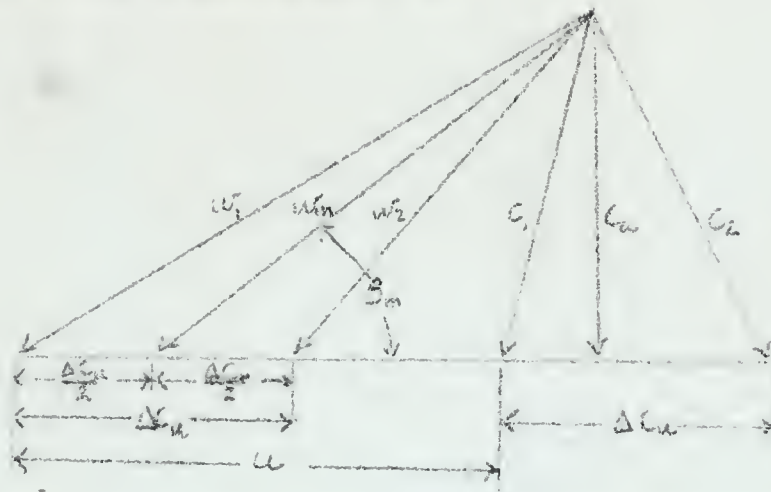
velocities are attained and shock waves develop within the compressor. Compressors which take advantage of this phenomenon are in the process of development, but are not yet in actual use. Since we are concerned primarily with present designs, and since information on supersonic compressors is restricted, nothing further will be said about them.

From Ref. 4, the entrance velocity diagram for a centrifugal compressor is as shown.



According to Ref. 4, M_e , the Mach number corresponding to w_e , should not exceed 0.75 approximately, and eu should not exceed $0.65D$. If we assume these maximum values, and assume the impeller tip velocity to be sonic, the Mach number corresponding to the axial velocity is 0.374. This seems to be a fairly high value, and certainly it should be much lower than that if a double faced impeller is used. With the double faced impeller the airflow must turn through 180 degrees to enter the rear side, and the head loss resulting from this reversal would be high with such a large flow velocity.

From Ref. 4, the entrance velocity diagram for an axial flow compressor is:



For an axial flow compressor the blading efficiency is a maximum when β_m is about 45 deg. Subscript 1 indicates the velocity ahead of a moving blade; subscript 2 indicates a velocity leaving a moving blade. The relative velocity, w_1 , at any station on the blade should not exceed sonic velocity or shock losses will result. Since with an axial flow compressor there is no flow reversal as occurs with a double faced centrifugal compressor, the allowable axial flow velocity can be greater. For very high speed aircraft the trend seems to be toward the turbojet engine with the axial flow compressor. One important factor influencing this trend is the fact that the permissible airflow velocity entering the compressor is higher with the axial flow type. A reasonable value to assume for this compressor entrance velocity, or diffuser exit velocity, would be one corresponding to a mach number of 0.3 to 0.4. Of course, as we have seen, this is a function of the compressor design.

There will be the following chapters during the
 1944-1945 season.



The first part of the project is to
 establish a central office in
 the city of London. This
 office will be responsible for
 all the work of the project.
 The second part is to
 establish a series of regional
 offices in the various
 parts of the country. These
 offices will be responsible
 for the work of the project
 in their respective regions.
 The third part is to
 establish a series of sub-
 regional offices in the
 various parts of the country.
 These offices will be
 responsible for the work
 of the project in their
 respective sub-regions.

4. External Drag Considerations.

The design of an efficient diffuser entails a two-fold consideration. First, the design must be such that the pressure recovery within the diffuser must be accomplished with a minimum loss; second, the flow over the outside surfaces in the vicinity of the diffuser inlet must not be disturbed to such an extent that the drag is increased. It is due to this latter consideration that a lower limit on velocity ratio is imposed.

In subsonic flows the total drag of a body shape can be considered to be composed of two components, skin friction drag and wake drag. The two components are inter-related and have their counterparts in the internal diffuser flow. In the consideration of drag we are more concerned with the resistance of the air to the motion of the body through it; with internal flow we are more concerned with the pressure loss in the flow.

A body in a subsonic, non-viscous, ideal flow has zero drag forces acting on it. The flow comes to a stagnation point on the leading edge of the body with the kinetic energy of the flow being transformed into pressure. As the flow continues around the body it is accelerated up to the widest dimension with the pressure decreasing as the velocity increases. Beyond the widest dimension the flow decelerates to a rear stagnation point. A summation of the pressure forces in the direction of flow is zero.

A. *Administrative and Financial*

The Commission on the Administration of the Government of the District of Columbia has been organized to study the present and proposed methods of administering the Government of the District of Columbia. The Commission is composed of representatives of the Executive, Legislative, and Judicial Branches of the Government of the District of Columbia, and of representatives of the public. The Commission is authorized to hold public hearings and to report to the Board of Commissioners on or before the first day of January, 1955.

The Commission is organized into three subcommittees: (1) Administrative Organization, (2) Financial Administration, and (3) Personnel Administration. The subcommittees are authorized to hold public hearings and to report to the Commission on or before the first day of January, 1955. The Commission is authorized to employ such personnel as it may deem necessary and appropriate, and to incur such expenses as it may deem necessary and appropriate, within the limits of the appropriation therefor.

The Commission is authorized to hold public hearings and to report to the Board of Commissioners on or before the first day of January, 1955. The Commission is authorized to employ such personnel as it may deem necessary and appropriate, and to incur such expenses as it may deem necessary and appropriate, within the limits of the appropriation therefor.

Approved: _____
 Date: _____

The real flow of a subsonic, viscous fluid tries to follow the pattern of the ideal flow, but viscosity causes some deviations. Due to viscous forces a boundary layer is formed, a thin layer of fluid at the surface of the body where a strong velocity gradient normal to the body surface exists. This velocity gradient is the result of viscous interaction, friction, between the body and the fluid. Friction tends to impede the progress of the body through the fluid. The drag due to friction is usually rather small, but with streamline bodies it may be the most significant component of the total drag.

The second component of drag is the one which causes most concern. As the flow progresses around the body the boundary layer grows. In the positive pressure gradient at the rear of the body the boundary layer is unstable and the flow tends to separate from surface. When the flow separates there is a pressure loss. The summation of the pressure forces about the body is no longer zero and a drag due to the unbalanced pressure forces results. Pressure drag increases with forward movement of the separation point. With poorly designed shapes the pressure or wake drag can amount to several times the skin friction drag. This is comparable with the separation loss which may occur in the internal flow through the diffuser. At low velocity ratios separation of the flow over the outside surface of

The first step in a systematic approach to the study of the history of the United States is to determine the period and the subject to be studied. The period may be determined by the date of the event or by the date of the author's writing. The subject may be determined by the nature of the event or by the nature of the author's writing. The next step is to collect the material. This may be done by consulting the library, the archives, or the field. The third step is to analyze the material. This may be done by comparing the material with other material, by examining the material in detail, or by applying the material to a theory. The fourth step is to synthesize the material. This may be done by combining the material into a coherent whole, by identifying the main themes, or by developing a new theory. The fifth step is to present the material. This may be done by writing a book, by giving a lecture, or by publishing an article.

The second step in a systematic approach to the study of the history of the United States is to determine the period and the subject to be studied. The period may be determined by the date of the event or by the date of the author's writing. The subject may be determined by the nature of the event or by the nature of the author's writing. The next step is to collect the material. This may be done by consulting the library, the archives, or the field. The third step is to analyze the material. This may be done by comparing the material with other material, by examining the material in detail, or by applying the material to a theory. The fourth step is to synthesize the material. This may be done by combining the material into a coherent whole, by identifying the main themes, or by developing a new theory. The fifth step is to present the material. This may be done by writing a book, by giving a lecture, or by publishing an article.

the diffuser is more likely to occur with attendant high drag losses.

Further complications are introduced with supersonic flows, and subsonic flows near the sonic velocity. For a body in a supersonic flow, a drag force exists even in a perfect fluid. The drag with which we are concerned, however, is not this form drag, but the added drag resulting from the appearance of a shock wave on the surface of the body.

The critical Mach number of a body is defined as that Mach number at which a Mach number of one appears in the flow around the body. When the flow is at a Mach number greater than the critical, there is always the possibility of a shock wave existing on the body. Since a shock wave causes an abrupt change in the flow with a high degree of turbulence in the vicinity of the shock, the results of this disturbance are transmitted to the boundary layer. The boundary layer is thickened and the added turbulence increases the likelihood of early flow separation and wake drag.

When evaluating diffuser performance the effects of drag increase due to a particular configuration must be balanced against the gain in engine performance resulting from the improved internal flow. This is probably an important factor in the choice of the flush type air inlet for some present high speed airplane designs.

The following is a list of the names of the persons who have been

admitted to the office of the Secretary of the State since the

year 1850, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

appointed, and the date of their admission, and the name of the

person to whom they have been appointed, and the date of their

admission, and the name of the person to whom they have been

CHAPTER III

DIFFUSER LOSSES

We have seen that the purpose of a diffuser is to reduce the velocity of the incoming air to a level suitable for use in the engine compressor, and, further, to recover as much as possible of the kinetic energy of the airstream and convert it into pressure energy. It was shown that when the ram recovery ratio was high the performance of the jet engine increased. Let us now investigate some of the factors which decrease the diffuser efficiency. If we appreciate what things affect diffuser performance, we can incorporate into our diffuser design features which minimize these effects.

The principal types of losses encountered in diffuser flow are:

1. Shock loss.
2. Entrance loss.
3. Yawing effect.
4. Expansion loss.
5. Friction loss.
6. Turning loss.
7. Obstructions in the flow.
8. Leakage loss.
9. Exit loss.

Some of these losses can be approximated by simple analysis while others are so complex and dependent upon the conditions of a particular installation that only general rules for evaluating their magnitude can be given. The losses listed above are discussed in the following paragraphs.

THE REPORT

GENERAL PRINCIPLES

The first part of the report deals with the general principles of the work.

The second part of the report deals with the results of the work.

The third part of the report deals with the conclusions of the work.

The fourth part of the report deals with the recommendations of the work.

The fifth part of the report deals with the appendixes of the work.

The sixth part of the report deals with the bibliography of the work.

The seventh part of the report deals with the index of the work.

The eighth part of the report deals with the list of figures of the work.

The ninth part of the report deals with the list of tables of the work.

The tenth part of the report deals with the list of references of the work.

The eleventh part of the report deals with the list of abbreviations of the work.

The twelfth part of the report deals with the list of symbols of the work.

The thirteenth part of the report deals with the list of units of the work.

1. General principles of the work.

2. Results of the work.

3. Conclusions of the work.

4. Recommendations of the work.

5. Appendixes of the work.

6. Bibliography of the work.

7. Index of the work.

8. List of figures of the work.

9. List of tables of the work.

10. List of references of the work.

11. List of abbreviations of the work.

1. Shock Loss.

The shock loss is a problem which is peculiar to supersonic speeds. A shock wave is a region across which sudden and finite changes in pressure, density and velocity of the flow occur. It is a non-isentropic compression. The pressure and density increase while the velocity decreases. Since the shock wave is accompanied by an entropy increase, there is a decrease in total pressure. This loss increases with increase of flow Mach number before the shock wave. The width of the shock wave in the direction of flow is very small. Shock waves may be classified into two categories, normal and oblique. These descriptions specify the orientation of the wave with respect to the flow direction. The normal shock is characterized by a jump from supersonic to subsonic velocity; the oblique shock, on the other hand, may cause a velocity jump from supersonic to a lesser supersonic, or subsonic velocity. The velocity jump from supersonic to a lesser supersonic velocity is more likely. The total head loss across a normal shock wave is greater than that across an oblique shock wave.

The relationships across either type of shock wave are given by the following equations.

β - angle between the direction of flow and the shock wave, 90° for a normal shock.

Subscripts:

THE STATE OF TEXAS

County of ... State of Texas

I, the undersigned, Clerk of the County of ... State of Texas

do hereby certify that the following is a true and correct copy

of the original as the same appears in the records of the County

of ... State of Texas

at this office on the ... day of ... 19...

Witness my hand and the seal of the County of ... State of Texas

this ... day of ... 19...

at ... State of Texas

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

...

x - condition before a shock.

y - condition after the shock.

$$M_y^2 = \frac{1 + \frac{\gamma-1}{2} M_x^2}{\gamma M_x^2 \sin^2 \beta - \frac{\gamma-1}{2}} - \frac{M_x^2 \cos^2 \beta}{1 + \frac{\gamma-1}{2} M_x^2 \sin^2 \beta}$$

$$\frac{P_0^y}{P_0^x} = \left[\frac{2\gamma}{\gamma+1} M_x^2 \sin^2 \beta - \frac{\gamma-1}{\gamma+1} \right]^{\frac{1}{\gamma-1}}$$

$$\times \left[\frac{(\gamma-1) M_x^2 \sin^2 \beta + 2}{(\gamma+1) M_x^2 \sin^2 \beta} \right]^{\frac{\gamma}{\gamma-1}}$$

$$\frac{P_y}{P_x} = \frac{2\gamma}{\gamma+1} M_x^2 \sin^2 \beta - \frac{\gamma-1}{\gamma+1}$$

Further information on shock waves can be found in Ref. 2, and the relationships across the shock wave can be found in Ref. 5.

Shockless compression from supersonic speed to subsonic speed is theoretically possible. The diffuser shape for such a flow would be that of a reversed Laval nozzle designed for one particular inlet mach number. With such shockless compression occurring, the mach number at the diffuser throat is one, and the mass flow is a maximum. Now, consider a slight variation in the mach number of the incoming flow. If it is less than the design mach number, the mass flow will be less than maximum, the throat mach number will have to be less than one, but isentropic compression from supersonic to subsonic flow demands sonic velocity at the diffuser throat. The flow becomes unstable and a detached shock

u = constant
v = constant

$$\frac{\partial u}{\partial x} + \frac{\partial v}{\partial y} = 0$$

$$\left[\frac{\partial}{\partial x} \left(\frac{u}{1+\gamma} - \delta \right) + \frac{\partial v}{\partial y} \right] = 0$$

$$\left[\frac{\partial}{\partial x} \left(\frac{u(1-\gamma)}{1+\gamma} + \delta \right) + \frac{\partial v}{\partial y} \right] = 0$$

$$\frac{\partial u}{\partial x} - \delta = \frac{\partial v}{\partial y}$$

The following text is extremely faint and mostly illegible. It appears to be a detailed derivation or explanation related to the mathematical equations shown above. Some discernible fragments include: "The following text...", "The constant...", "The...", "The...", "The...", "The...", "The...", "The...", "The...".

forms ahead of the diffuser entrance. Flow through the diffuser becomes wholly subsonic. On the other hand, if the entrance mach number is greater than the design value, the value of the throat mach number will never get as low as one. Supersonic flow will start into the diverging part of the diffuser and transition to subsonic flow can only occur through a shock wave in the diverging part of the diffuser.

We have considered what happens when variations in flow occur with a reversed Laval nozzle flowing full. Actually, we should consider what happens when we have subsonic flow through such a diffuser, and the entrance mach number is increased to supersonic values. At entrance mach numbers below the design value a detached shock occurs ahead of the diffuser because a mach number of one tries to occur in the converging part of the diffuser, an unstable flow condition. At some flow mach number, the contraction ratio of the converging part of the diffuser is such that a mach number of one occurs in the diffuser throat. This contraction ratio can be determined from the following relationship:

$$\begin{aligned} \text{Contraction ratio for sonic velocity at diffuser} \\ \text{throat} &= \text{area ratio for isentropic deceleration} \\ &\text{of flow to sonic velocity at the throat} \\ &= \frac{p_x^0}{p_y^0} \end{aligned}$$

At this point the diffuser is able to swallow the detached shock, supersonic flow starts into the diffuser,

and the shock forms in the diverging part of the diffuser, its location dependent upon the pressure ratios across the diffuser. We can see, therefore, that shockless diffusion is impossible, but we can move the detached shock into the diverging part of the diffuser.

In Ref. 6 the theoretical maximum efficiency attainable with the type of diffuser described above is given, as well as the results of actual experiments. This data is shown in Fig. 4. Actually, with an adjustable throat one hundred per cent efficiency is theoretically possible. If, after supersonic flow has started through the diffuser throat, the throat area is reduced, then the throat Mach number approaches one. By adjusting the pressure ratio across the diffuser the position of the shock wave can be moved into the throat of the diffuser, and there is no loss when the Mach number at the throat is one. Such a procedure presupposes that conditions across the diffuser can be closely controlled. In the evaluation of the theoretical maximum efficiencies of Fig. 4, the shock had been located in the diffuser throat by adjusting the pressure ratios across the diffuser. However, the pressure ratio across the diffuser depends upon the ambient pressure, in this case, and the volume flow through the compressor, a function of compressor speed. It is not advisable to vary the compressor speed over too wide a range, because the efficiency of the engine will decrease. Also, the

mechanical difficulties of an adjustable throat would not be offset by the improved diffuser performance which would result. A third objection to this diffuser design is that for flight Mach numbers greater than that for which the diffuser was designed, the volume flow through the diffuser increases with the Mach number. To accommodate this flow the compressor speed would have to increase which would affect the overall engine performance.

As the free stream Mach number increases, the losses occurring through a detached shock wave increase very rapidly, as can be seen in Fig. 5. Ref. 7 presents an analytical study of one method of reducing these shock losses. Since the losses through an oblique shock are less than those through a normal shock, it was proposed to reduce the initial Mach number of the flow through a series of oblique shocks, and finally through a normal shock wave. The results of this analysis, shown in Fig. 6, would seem to indicate that pressure recovery would be considerably improved over that possible with one normal shock, particularly at high Mach numbers.

From the foregoing discussion it would appear that shock free compression from supersonic to subsonic velocities is unlikely. Some shock system will occur, either normal or oblique, and located either within or external to the diffuser. Even though the shock

The first part of the document is a list of names and titles, including the names of the members of the committee and the names of the organizations they represent. The list is organized in a table-like format with columns for names and titles.

The second part of the document is a letter or report addressed to the members of the committee. It discusses the work of the committee and the results of its investigations. The text is written in a formal, professional style and includes several paragraphs of text.

The third part of the document is a list of references or sources used in the report. It includes the names of the authors, the titles of the works, and the publishers or sources of the information.

The fourth part of the document is a list of appendices or additional information. It includes the names of the documents or materials that are included in the report and a brief description of each.

The fifth part of the document is a list of footnotes or endnotes. It includes the names of the authors and the titles of the works cited in the report.

The sixth part of the document is a list of acknowledgments. It includes the names of the individuals and organizations that provided assistance or support during the course of the investigation.

The seventh part of the document is a list of indexes or tables of contents. It includes the names of the sections of the report and the page numbers where they can be found.

The eighth part of the document is a list of glossary or definitions. It includes the names of the terms used in the report and their meanings.

The ninth part of the document is a list of bibliography or references. It includes the names of the authors, the titles of the works, and the publishers or sources of the information.

The tenth part of the document is a list of appendices or additional information. It includes the names of the documents or materials that are included in the report and a brief description of each.

may be external to the diffuser proper it is only right that the losses incurred across the shock be attributed to the diffuser. In all our discussion of diffuser flow we have referred to free stream conditions of flow with the subscript "o"; with a shock located ahead of the diffuser entrance, this condition will be that on the downstream side of the shock.

The detached shock ahead of a diffuser entrance is of a complicated structure. In the region of the stream tube which ultimately enters the diffuser entrance, it is essentially a normal shock, or at least the assumption of a normal shock will give a reasonable approximation of the conditions downstream of the shock. Proceeding outward, normal to the direction of flow, the shock progresses through the whole family of strong and weak oblique shocks, and finally degenerates into a Mach line. This complicates the flow pattern around the outside of the diffuser because of the resulting velocity gradient normal to the direction of flow. Also, the location of the shock wave ahead of the diffuser is difficult to determine, except when the Mach number immediately downstream of the shock wave corresponds to the entrance Mach number of the diffuser as determined by the volume flow and diffuser geometry. In this latter case, the shock wave will probably attach itself to the entrance lip of the diffuser.

The first part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The second part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The third part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The fourth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The fifth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The sixth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The seventh part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The eighth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The ninth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

The tenth part of the report is devoted to a description of the
 general situation in the country. It is then followed by a
 detailed account of the various departments and their
 activities. The report concludes with a summary of the
 main findings and recommendations.

In some respects the detached shock wave is advantageous. It will accommodate a wider range of flow conditions through the diffuser. At relatively low supersonic mach numbers the loss occurring through the shock wave is not excessive, and additional compression of the flow can be made before the flow enters the diffuser. Further, the flow turbulence occasioned by the shock can be wholly or partially damped out before the flow enters the diffuser. That this turbulence caused by the shock wave is of some importance can be seen from Fig. 7, which shows the loss in pressure recovery occasioned by increasing the exit cone angle of the diffuser from 3 degrees to 5 degrees. For a diffuser without shock the optimum exit cone angle of the diffuser is about 3 degrees. This indicates that the pressure recovery within the diffuser must be more gradual because of this shock induced turbulence. Although the internal flow within a diffuser benefits from a detached shock wave, the effect of the external flow on the drag of the engine nacelle may be seriously increased. This particular problem merits experimental investigation.

2. Entrance Loss.

The importance of the entrance conditions of a diffuser is not due to any particular loss occurring in the diffuser itself, but the effect of the entrance

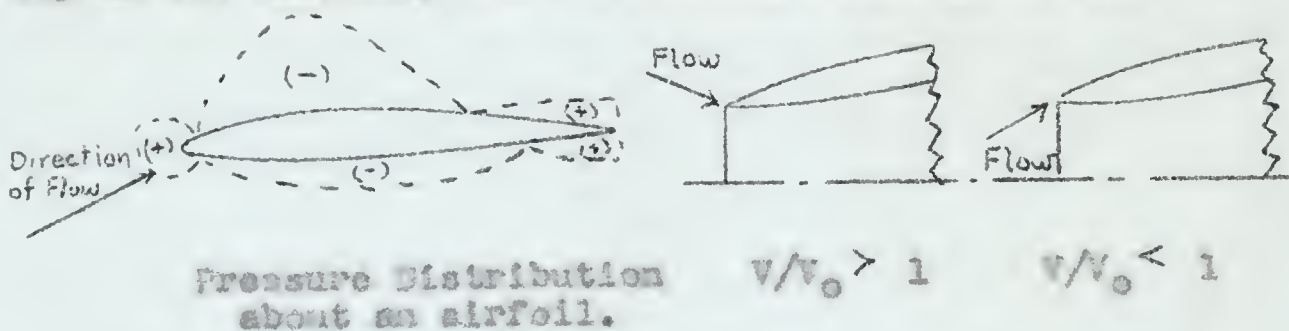
The first part of the document is a general introduction to the project. It describes the objectives and the scope of the work. The second part is a detailed description of the methodology used in the study. This includes a discussion of the data sources, the sampling method, and the statistical techniques employed. The third part presents the results of the study, which are organized into several sections corresponding to the different variables analyzed. The final part is a conclusion that summarizes the main findings and discusses their implications for future research.

APPENDIX A

The following table provides a summary of the data used in the study. It includes information on the number of observations, the range of values, and the distribution of the data for each variable. This information is useful for understanding the characteristics of the dataset and for identifying any potential issues with the data.

conditions on other diffuser losses. For example, one turbojet engine manufacturer specifies that the engine performance is not guaranteed unless the airflow variation across the compressor inlet is less than five per cent. One plane using this engine achieves this result by having constant velocity head at the diffuser entrance. Obtaining uniform flow conditions at the diffuser entrance may be complicated by some entrance duct locations.

If we can conceive the idea that the lip of the diffuser entrance is an airfoil shape, we can picture what happens as the airflow approaches and passes it. Assume that the external surface of the diffuser is the top of the airfoil, and the internal surface is the



bottom. With a velocity ratio (v/v_0) greater than one the diffuser airfoil shape is at a negative angle of attack, a negative pressure area due to this flow forms inside the diffuser. The lowest pressure will occur at the throat of the diffuser. The flow in the diverging part of the diffuser is progressing against a positive pressure gradient due to the diffuser design. This increased negative pressure at the diffuser throat increases the pressure gradient and makes separation of the internal flow more likely.

With a velocity ratio less than one the diffuser lip is at a positive angle of attack. The increased negative pressure area occurs external to the diffuser. Some limiting velocity ratio will be attained where the entrance lip stalls, and the flow separates from the outside surface of the diffuser with external drag increasing accordingly.

If a sharp leading edge had been selected for the diffuser lip, the effects described above would have been aggravated, considering subsonic flow at the diffuser entrance. A sharp nosed airfoil stalls at lower angles of attack than those with rounded leading edges due to the difficulty of the flow around such a corner. With supersonic flow into the diffuser a sharp edged profile might prove beneficial because supersonic flow can change direction sharply in following contours. Where the normal shock is located at the diffuser entrance, and there is subsonic flow in the diffuser and supersonic flow outside, a sharp leading edge would be preferable because it would have less effect on the external flow, and no effect on the internal flow because the velocity ratio in this case is one. However, at conditions other than that at which the shock sits on the nose of the diffuser, the sharp leading edge would be detrimental.

In the entrance of a diffuser with a rounded leading edge, there is a region where the flow will be

expanding. A point of minimum diffuser cross-sectional area will occur. This region of contraction has its advantages and disadvantages. It provides a region of favorable pressure gradient where stream turbulence, such as that following a shock wave, may be damped out. On the other hand, the flow is accelerating in this region and more compression is required in the diverging part of the diffuser. At entry Mach numbers near one it does not require much of a change in area ratio to cause considerable change in flow Mach number. Some reasonable compromise must be effected.

Because the flow at the entrance to the diffuser is not parallel to the diffuser axis, some question may arise as to what is the effective entrance area of the diffuser. The stagnation point of the flow, from which the boundary layer starts, will tend to move into the diffuser as velocity ratio decreases below one. It will move to the outside of the diffuser for velocity ratios increasing above one. This will affect the contraction ratio to the diffuser throat which may reach measurable magnitude with high subsonic entrance Mach numbers.

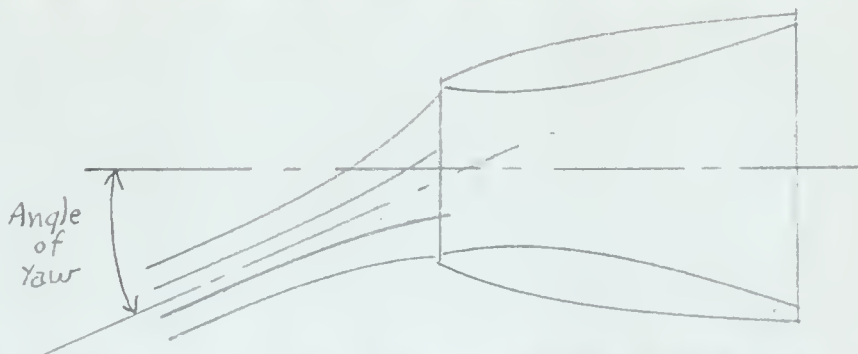
Realizing the effect of the diffuser entrance on the internal flow through the diffuser, it should be carefully designed to cause the least disturbance possible. In this case the only loss in the diffuser entrance will be the friction loss which should be very

The first part of the report is devoted to a general
 description of the work done during the year. It
 is followed by a detailed account of the various
 projects which have been carried out. The first
 of these is the study of the properties of the
 new material which has been developed. This
 work has been carried out in collaboration with
 the other members of the group. The results
 of this work are given in the following
 sections. The first section is devoted to a
 description of the material and its properties.
 The second section is devoted to a description
 of the methods used for the study of the
 material. The third section is devoted to a
 description of the results of the study. The
 fourth section is devoted to a discussion of
 the results and their significance. The fifth
 section is devoted to a summary of the work
 done during the year. The sixth section is
 devoted to a list of references. The seventh
 section is devoted to a list of symbols and
 abbreviations. The eighth section is devoted
 to a list of figures. The ninth section is
 devoted to a list of tables. The tenth section
 is devoted to a list of appendices. The
 eleventh section is devoted to a list of
 errata. The twelfth section is devoted to a
 list of acknowledgments. The thirteenth
 section is devoted to a list of authors. The
 fourteenth section is devoted to a list of
 sponsors. The fifteenth section is devoted to
 a list of distributors. The sixteenth section
 is devoted to a list of agents. The
 seventeenth section is devoted to a list of
 publishers. The eighteenth section is devoted
 to a list of printers. The nineteenth section
 is devoted to a list of binders. The
 twentieth section is devoted to a list of
 distributors. The twenty-first section is
 devoted to a list of agents. The twenty-
 second section is devoted to a list of
 publishers. The twenty-third section is
 devoted to a list of printers. The twenty-
 fourth section is devoted to a list of
 binders. The twenty-fifth section is
 devoted to a list of distributors. The
 twenty-sixth section is devoted to a list of
 agents. The twenty-seventh section is
 devoted to a list of publishers. The
 twenty-eighth section is devoted to a list of
 printers. The twenty-ninth section is
 devoted to a list of binders. The thirtieth
 section is devoted to a list of distributors.

small. If the diffuser entrance is poorly designed the internal losses in the diffuser will be increased. Although this additional loss is directly attributable to the diffuser entrance it is difficult to assess the extent of the loss so occasioned.

3. Yawing Effect.

Closely allied with entrance loss is the loss occasioned when the axis of the diffuser is not parallel to the axis of the initial airflow. Under such



circumstances the flow at the diffuser inlet will be complex. Such a condition could occur with yawing or pitching motion of an aircraft, or when landing and a high angle of attack results. Some aircraft designers allow for this last case by extending the upper lip of the air entrance duct. A good example of this configuration is the air entrance duct of the P-56.

In the plane containing the duct axis and the maximum yawing angle, this effect is greatest. The duct lip will have a higher angle of attack than normally on one side, and a lower angle of attack on the other side. Since the volume of airflow through the duct is a

The first part of the report deals with the general situation of the country and the progress of the work done during the year. It is followed by a detailed account of the various projects and the results achieved. The report concludes with a summary of the work done and the prospects for the future.

3. Technical Details

The following section contains a detailed description of the technical details of the work done during the year. It is divided into several parts, each dealing with a different aspect of the work.



The diagram illustrates the technical details of the work done during the year. It shows a cross-section of a structure with various components and dimensions. The diagram includes a central vertical column, a horizontal beam, and a sloped section. Dimensions are indicated by lines and arrows, and there are labels for different parts of the structure.

The following section contains a detailed description of the technical details of the work done during the year. It is divided into several parts, each dealing with a different aspect of the work.

function of the engine speed, the average air velocity across the face of the duct, parallel to the duct axis will be unaffected by this condition. The velocity distribution across the face of the duct will not be uniform, however. The lip in the direction of the flow will have a lower pressure internally than the lip away from the direction of flow. A higher velocity will accompany the lower pressure to satisfy the flow equilibrium. This will be the maximum velocity across the face of the duct. Diametrically opposite a minimum velocity will occur. In other radial planes around the duct entrance the flow will vary from a maximum at one lip to a minimum at the other, except that there will be a lesser degree of difference. In a bend in a duct, which is not unlike the situation in this case, it has been found that a secondary flow in a plane normal to the main flow axis sometimes occurred. This could also take place in this instance. The net result of the yawing effect is a disturbed entrance flow into the diffuser which may result in sufficient turbulence to cause a loss in pressure potential, and will result in decreased diffuser performance. Since the resulting flow will vary in all three dimensions, and vorticity will be introduced, it will be difficult to analyze.

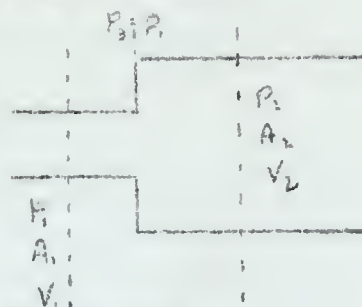
h. Expansion Loss.

It has been recognized that diffuser flow is unstable by its very nature. In the diverging part of a

The first of the three conditions is that the
 system must be in a state of equilibrium. This
 condition is satisfied if the system is in a
 state of equilibrium. The second condition is
 that the system must be in a state of
 equilibrium. This condition is satisfied if
 the system is in a state of equilibrium. The
 third condition is that the system must be
 in a state of equilibrium. This condition is
 satisfied if the system is in a state of
 equilibrium. The fourth condition is that
 the system must be in a state of equilibrium.
 This condition is satisfied if the system is
 in a state of equilibrium. The fifth
 condition is that the system must be in a
 state of equilibrium. This condition is
 satisfied if the system is in a state of
 equilibrium. The sixth condition is that
 the system must be in a state of equilibrium.
 This condition is satisfied if the system is
 in a state of equilibrium. The seventh
 condition is that the system must be in a
 state of equilibrium. This condition is
 satisfied if the system is in a state of
 equilibrium. The eighth condition is that
 the system must be in a state of equilibrium.
 This condition is satisfied if the system is
 in a state of equilibrium. The ninth
 condition is that the system must be in a
 state of equilibrium. This condition is
 satisfied if the system is in a state of
 equilibrium. The tenth condition is that
 the system must be in a state of equilibrium.
 This condition is satisfied if the system is
 in a state of equilibrium.

diffuser the flow is advancing against a positive pressure gradient, and it has been found that if this gradient is too severe the flow will separate from the diffuser wall. The result of this separation is a sudden expansion from the point of separation to the end of the diffuser. The loss caused by a sudden expansion is calculated in Ref. 3.

The loss due to a sudden expansion yields to analysis in the following manner:



From Bernoulli's equation:

$$\frac{p_1}{\rho} + \frac{v_1^2}{2g} = \frac{p_2}{\rho} + \frac{v_2^2}{2g} + h_f \quad (a)$$

h_f - head loss due to sudden enlargement.

$$h_f = \frac{v_1^2 - v_2^2}{2g} - \frac{(p_2 - p_1)}{\rho} \quad (b)$$

Now, the momentum principle states that the resulting force acting on a body equals the change of momentum of the body per second.

$$\text{Rate of change of momentum} = \frac{\rho A_2 v_2}{g} (v_1 - v_2)$$

$$\text{Force acting} = (p_2 - p_1) A_2$$

$$(p_2 - p_1) A_2 = \frac{\rho A_2 v_2}{g} (v_1 - v_2) \quad (c)$$

... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...

... the ... of ...



... the ... of ...

$$y = \frac{a}{9} + \frac{b}{9} + \frac{c}{9} + \frac{d}{9} + \frac{e}{9}$$

... the ... of ...

$$\frac{100 - 100}{9} = \frac{100 - 100}{9} + \frac{100 - 100}{9}$$

... the ... of ...
 ... the ... of ...
 ... the ... of ...

$$\frac{100 - 100}{9} = \frac{100 - 100}{9} + \frac{100 - 100}{9}$$

$$100 - 100 = 100 - 100$$

$$100 - 100 = 100 - 100$$

... the ... of ...

$$\frac{p_2 - p_1}{\rho} = \frac{V_2}{5} (V_1 - V_2) \quad (4)$$

Substituting in eq. (b) yields:

$$h_f = \frac{(V_1 - V_2)^2}{2g}$$

In our case V_1 will be the velocity at the point of separation, and V_2 , the velocity with which the flow re-establishes itself. It is evident that the loss will be least if the point of flow separation is near the exit of the diffuser, increasing as the point of separation moves toward the throat. An incompressible flow analysis was made in this instance, and is acceptable because it is hoped that the flow will be slowed to the point where it can be considered incompressible before separation occurs. If such is not the case the diffuser is much too inefficient.

The next points to be considered are the cause of flow separation, how the point of flow separation can be determined, and what experimental results have been obtained. The cause of flow separation is linked with the growth of the boundary layer, and some characteristics of the boundary layer must be reviewed first.

A. Boundary Layer in a Diffuser.

The boundary layer is a region in a fluid flow adjacent to a solid surface where strong velocity gradients normal to the surface exist. It is caused

$$\frac{d^2x}{dt^2} + \gamma \frac{dx}{dt} = -\frac{dV}{dx}$$

where γ is the friction coefficient.

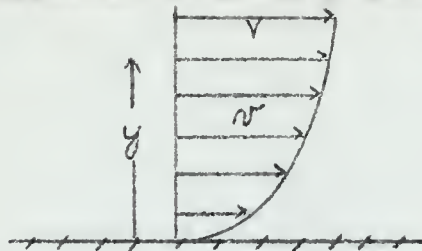
$$\frac{d^2x}{dt^2} + \gamma \frac{dx}{dt} = -\frac{dV}{dx}$$

The first term on the right-hand side of the equation is the force of the spring, which is proportional to the displacement x . The second term is the force of friction, which is proportional to the velocity \dot{x} . The third term is the force of the external field, which is the negative gradient of the potential energy $V(x)$. The equation of motion can be written in the form of a second-order differential equation. The solution of this equation is given by the following expression:

The general solution of the equation of motion is given by the following expression:

The boundary conditions are given by the following expression:

by friction, the viscous reaction of a fluid at the solid surface. At the point of contact of the fluid with the surface the velocity of the flow is zero, increasing normal to the surface until it reaches the free stream velocity. A typical velocity pattern would be:

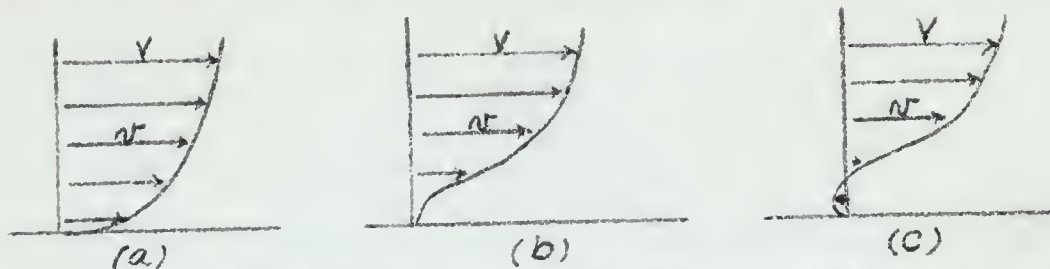


V - free stream velocity.

v - Velocity at any point in the boundary layer.

Generally, boundary layers may be classified into two types, the laminar and the turbulent boundary layers. The velocity distribution in these two types is quite different. In the laminar boundary layer there is no flow of the fluid particles normal to the main axis of the flow. In the turbulent boundary layer small velocity variations normal to the main flow do exist. Both types of boundary layer increase in thickness in the direction of flow, but at different rates. Boundary layer growth is a function not only of the axial distance in the direction of flow, but also of the pressure gradient which may exist in the flow. A boundary layer which is initially laminar may go through a transition point where laminar flow can no longer be maintained. The flow may even separate from the surface and re-establish itself downstream as a turbulent boundary layer.

As the turbulent boundary layer grows it loses some of the kinetic energy initially present due to friction losses. The development of the turbulent boundary layer can be visualized thus:



In state (c) a reversal of flow has started next to the wall. This condition is unstable. A vortex will develop and the flow will ultimately separate from the surface.

The development of the boundary layer in a diffuser is probably somewhat like the following pattern. At the entrance lip of the diffuser a stagnation point occurs. At this point the boundary layer has zero thickness. From this point to the throat of the diffuser a negative pressure gradient exists. A negative pressure gradient has a stabilizing effect on the boundary layer so it grows in the laminar fashion. In the diverging part of the diffuser a positive pressure gradient exists. A positive pressure gradient has a destabilizing effect on the boundary layer. The laminar boundary layer will persist for a short distance into this unfavorable pressure gradient, then transition to a turbulent boundary layer will occur. The turbulent boundary layer will continue to the separation point

or the end of the diffuser if separation does not occur.

There is a considerable fund of information on both laminar and turbulent boundary layer growth, transition, and separation. Ref. 9 reviews the field and contains several pages of further references for those interested in pursuing the subject further. Most of the work done in boundary layer research is confined to two dimensional cases. The flow in a diffuser, or any duct for that matter, is further complicated by three dimensional effects. The flow outside the boundary layer in a duct is not uniform. It, too, may be either laminar or turbulent. Further complications in a duct of varying cross-section, like a diffuser, are added by the fact that the pressure recovery across any cross-section is not uniform.

For purposes of analysis some assumptions, however erroneous, are necessary. In this particular case it will be assumed that the main flow in the duct is one dimensional, and that the boundary layer behaves as it would in a simple two dimensional flow. This will probably be not too far from the truth if the boundary layer thickness remains small in comparison with the duct diameter.

A. Point of Laminar Separation.

Ref. 10 gives the following method of determining the point of separation of the laminar boundary layer.

... the way of the ...

... the way of the ...

... the way of the ...

... the way of the ...



$$\text{Velocity gradient} = P = \frac{s_0}{V_0} \frac{dV}{ds} = \frac{-s_0}{2(1 + 1m)} \frac{dP}{ds}$$

s_0 = equivalent flat plate length from the entrance of the duct to the point at which the adverse pressure gradient is applied
 $= s_1 + s_2$

$$s_1 = 0.376 s_m \left(\frac{\Delta p}{q_m} \right)^{-0.164}$$

s_2 = the distance from s_m to the point at which an adverse gradient is applied.

s_m = point of minimum pressure.

$$P = \text{pressure coefficient} = \frac{(p - p_\infty)}{q}$$

p = static pressure at any point.

p_∞ = free stream static pressure.

q_m = dynamic pressure at s_m .

$\frac{dP}{ds}$ = slope of line approximating the pressure distribution back of the point of minimum pressure.

$$\Delta p = \frac{(p_{s_m} - p_{s_m})}{2}$$

The permissible velocity decrement with a given velocity gradient is shown in Fig. 6.



$$\frac{1}{2} \rho v^2 + \rho g h + p = \frac{1}{2} \rho v'^2 + \rho g h' + p'$$

we are interested in the case where the height of the fluid is the same on both sides of the pipe so the pressure is the same on both sides.

$$p = p'$$

$$\frac{1}{2} \rho v^2 = \frac{1}{2} \rho v'^2$$

we can simplify this to $v = v'$ and we see that the velocity is the same on both sides of the pipe.

$$\frac{1}{2} \rho v^2 = \frac{1}{2} \rho v'^2$$

we can simplify this to $v = v'$ and we see that the velocity is the same on both sides of the pipe.

we can simplify this to $v = v'$ and we see that the velocity is the same on both sides of the pipe.

$$v = v'$$

we can simplify this to $v = v'$ and we see that the velocity is the same on both sides of the pipe.

C. Mixing Length.

After the separation of the laminar boundary layer there exists a transition region in which the flow in the boundary layer is neither laminar nor turbulent. According to Ref. 11 the extent of this region has been experimentally determined to be:

$$\frac{x}{c} = \frac{70,000}{c} \frac{\nu}{V_s}$$

x = the extent of the transition region, the distance from the point of laminar separation to the point at which a fully developed turbulent profile is observed.

V_s = velocity outside the boundary layer at the laminar separation point.

ν = Kinematic viscosity at the point of laminar separation

c = a characteristic length, in this case, the length of the diffuser.

D. Point of Separation of the Turbulent Boundary Layer.

A method of determining the point of separation of the turbulent boundary layer is given in Ref. 12. It was found that the variables controlling the development of the turbulent boundary layer were (1) the ratio of the non-dimensional pressure gradient, expressed in terms of the local dynamic pressure outside the boundary layer ^{and boundary layer} thickness, to the local skin friction coefficient,

2. *Linear Equations*

After the completion of the linear equations chapter, the student should be able to solve linear equations in one variable, linear equations in two variables, and linear inequalities in one variable. The student should also be able to solve word problems involving linear equations in one variable and linear inequalities in one variable.

$$\frac{1}{2}x + \frac{3}{4}y = 12$$

The student should be able to solve linear equations in one variable and linear inequalities in one variable. The student should also be able to solve word problems involving linear equations in one variable and linear inequalities in one variable.

The student should be able to solve linear equations in two variables and linear inequalities in two variables. The student should also be able to solve word problems involving linear equations in two variables and linear inequalities in two variables.

The student should be able to solve linear equations in three variables and linear inequalities in three variables. The student should also be able to solve word problems involving linear equations in three variables and linear inequalities in three variables.

and boundary lines

and (2) the shape of the boundary layer. An empirical equation was developed in terms of these variables which, when used with the momentum equation and the skin friction relation, makes it possible to trace the development of the turbulent boundary layer to the separation point.

At this point it is well to review some definitions which will be used subsequently. Boundary layer thickness, δ , is the distance normal to a solid boundary in a fluid flow in which a velocity gradient exists. For a laminar boundary layer, Ref. 13 gives the equation for this thickness.

$$\delta = 5.48 \sqrt{\frac{\nu x_0}{V}}$$

Other references give essentially the same equation with some variations in the numerical factor.

The velocity distribution in the laminar boundary layer, according to Ref. 14 is:

$$\frac{v}{V} = 2\left(\frac{y}{\delta}\right) - 2\left(\frac{y}{\delta}\right)^3 + \left(\frac{y}{\delta}\right)^4 \quad (\text{Prandtl-Blasius Equation})$$

This equation for velocity distribution is satisfactory if the stream turbulence is low and the Reynolds number is less than 500,000.

The actual boundary layer thickness is difficult to determine, however, and other thickness parameters are used. One of these is the displacement thickness which is defined as the amount the general flow is

... (1) ... the ... of ...
... the ... of ...
... the ... of ...
... the ... of ...

... the ... of ...
... the ... of ...
... the ... of ...
... the ... of ...

$$\delta = \sqrt{\frac{2}{\rho \omega^2}}$$

... the ... of ...
... the ... of ...
... the ... of ...

$$\frac{1}{\rho} \left(\frac{\partial^2 \sigma}{\partial x^2} + \frac{\partial^2 \tau}{\partial y^2} - \frac{\partial^2 \nu}{\partial z^2} \right) = \frac{\partial^2 \xi}{\partial t^2}$$

... the ... of ...
... the ... of ...
... the ... of ...
... the ... of ...

displaced outward by the boundary layer. It may be written

$$\delta^* = \int_0^{\delta} \left(1 - \frac{v}{V}\right) dy$$

Another boundary layer thickness parameter is the momentum thickness. The difference between the actual flow of momentum in the boundary layer, and that of the same quantity of fluid flowing with velocity V is $\rho V^2 \theta$. From this relation momentum thickness gets its name. It is defined as:

$$\theta = \int_0^{\delta} \frac{v}{V} \left(1 - \frac{v}{V}\right) dy$$

This definition is quite frequently used in boundary layer calculations. It should be noted that, although boundary layer thickness does change in transition from laminar to turbulent flow, momentum thickness does not, according to Ref. 15.

Another parameter which makes an appearance in boundary layer calculations is the shape parameter. This is defined as the ratio of the displacement thickness to the momentum thickness

$$H = \frac{\delta^*}{\theta}$$

The equation that gives the rate of change of the momentum in a boundary layer, originally derived by von Karman, may be written in the following form for two dimensional flow:

... ..

...

$$a \left(\frac{1}{b} - 1 \right) \frac{1}{c} = \frac{1}{c}$$

... ..

...

$$a \left(\frac{1}{b} - 1 \right) \frac{1}{c} = \frac{1}{c}$$

... ..

$$\frac{1}{c} = \frac{1}{c}$$

... ..

$$\frac{d\theta}{dx} + \frac{(\eta + 2)}{2} \frac{\theta}{q} \frac{dq}{dx} = \frac{\tau_0}{2q}$$

$$\frac{\tau_0}{q} = \text{local skin friction coefficient.}$$

$$\frac{\theta}{q} \frac{dq}{dx} = \text{non-dimensional pressure gradient.}$$

The value of the skinfriction coefficient was determined by the Squire and Young formula (Ref. 16), which states:

$$\frac{2q}{\tau_0} = \left[5.090 \log_{10} (4.075 R_0) \right]^2$$

$$R_0 = \frac{\rho u V}{\mu}$$

This skin friction formula gives good agreement with experimental results on airfoils.

The variation of the shape parameter, H , along the surface was determined by von Doenhoff and Tetervin to be:

$$\theta \frac{dH}{dx} = e^{4.630 (H - 2.975)} \left[-\frac{\theta}{q} \frac{dq}{dx} \frac{2q}{\tau_0} - 2.035 (H - 1.236) \right]$$

To calculate the characteristics of the turbulent boundary layer, it is always required to know the initial values of θ and H , the pressure distribution, and the Reynolds number. With this information and the three equations above a solution can be obtained. Separation may be considered to have occurred when H reaches a value of 2.6. According to Ref. 12 if the calculation is begun in a region where the ratio of the non-dimensional

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2}$$

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2}$$

$$\frac{1}{2} = \frac{1}{2} + \frac{1}{2}$$

The value of the function is constant for all values of x. The value of the function is 1/2.

$$\left[\frac{1}{2} \right] = \frac{1}{2}$$

$$\frac{1}{2} = \frac{1}{2}$$

This value is constant for all values of x. The value of the function is 1/2. The value of the function is 1/2.

$$\left[\frac{1}{2} \right] = \frac{1}{2}$$

The value of the function is constant for all values of x. The value of the function is 1/2. The value of the function is 1/2.

pressure coefficient to the skin friction coefficient is very small or positive, the boundary layer is not very sensitive to the initial value of H . For example, if dq/dx is zero, H will eventually have the value of 1.236 regardless of its initial value.

Some criticism of the above method of determining the point of separation of the turbulent boundary layer is given in Ref. 15. These criticisms are:

1. To determine the separation point within 4 per cent of the chord, the value of H immediately after transition must be known within ± 0.05 .
2. There is evidence that skin friction increases violently through the adverse pressure gradient preceding separation.
3. The empirical equation is derived entirely from data at low Reynolds number, $0.35 - 4.18 \times 10^6$. It may be proved ultimately that certain constants in the equation may vary appreciably with Reynolds number.
4. The mean value of H after transition is nearer 1.4. In von Koenhoff's momentum equation $(H - 1.4)$ would be better than $(H - 1.236)$.

E. Means of Delaying Separation.

Ref. 17 suggests the following methods of artificially delaying separation:

1. Provide motion of the solid boundary in the direction of the stream.

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

2. Increase the momentum of the retarded fluid by jets.

3. Prevent the accumulation of retarded fluid by suction.

The first method of delaying separation suggested is impractical in a duct. The shape of a diffuser does not lend itself to such a device, and secondly, the additional mechanism involved would cause more serious penalties in performance than the expected loss due to separation. The idea is of purely academic interest.

The second method is a decided possibility and Ref. 3 claims that the expansion loss can be reduced 40 to 50 per cent at expansion angles greater than 50° by the use of deflectors. These deflectors essentially provide a jet in the boundary layer region by reducing the pressure gradient near the wall, or even accelerating the flow in that region. Such large divergence angles



are not necessary for a diffuser to be used as the entrance duct of a jet engine, however. If a jet discharging into the boundary layer from an outside source is contemplated, the additional power required to furnish the jet must be accounted for in the computation of diffuser efficiency. Also, the increased mass flow must be allowed for in the calculation of diffuser performance.

2. The first part of the document is the

Part of the

3. The second part of the document is the

Part of the

The first part of the document is the

is described in a way that is very

and that is to say that the

first part of the document is the

that is to say that the

second part of the document is the

the first part of the document is the

the second part of the document is the

the third part of the document is the

the fourth part of the document is the

the fifth part of the document is the

the sixth part of the document is the

the seventh part of the document is the

the eighth part of the document is the



the ninth part of the document is the

the tenth part of the document is the

the eleventh part of the document is the

the twelfth part of the document is the

the thirteenth part of the document is the

the fourteenth part of the document is the

the fifteenth part of the document is the

19

The third method of preventing boundary layer separation seems the most inviting. Ref. 3 claims that diffuser efficiencies of the order of 80 per cent, based on power ratios, are possible with divergence angles greater than 50 degrees. Some results of experiments using this principle are shown in Fig. 9. The definition of efficiency is corrected for the power expended in raising the pressure of the fluid removed to the diffuser exit pressure, assuming a pump efficiency of 75 per cent.

$$\eta_s = \frac{p_2 - p_1}{\frac{1}{2} \rho u_1^2 \left[1 - \left(\frac{A_1}{A_2} \right)^2 \right] + \frac{Q_s p_s}{.75}}$$

Q_s = quantity of fluid sucked away per unit time.

p_s = required increase in pressure from the suction slit to p_2 , diffuser discharge pressure.

Still a fourth method of reducing expansion loss is suggested in Ref. 3. In this method a solid body rotation is imposed on the flow by curved vanes at the diffuser entrance. This motion has the effect of decreasing the rate of compression by increasing the mean distance travelled by the flow through the diffuser. Other methods of reducing the rate of compression suggested by the same article are the use of an annular duct and the use of a dividing vane in the flow. In

The first method of determining the
 concentration of a solution is by
 using a standard solution of known
 concentration and comparing it with
 the unknown solution. This is done
 by measuring the volume of the
 standard solution required to react
 with a known volume of the
 unknown solution. The volume of
 the standard solution required is
 proportional to the concentration
 of the unknown solution.

$$C_1 V_1 = C_2 V_2$$

This is a simple equation and can be
 used to find the concentration of
 a solution if the volume of the
 standard solution and the volume
 of the unknown solution are known.
 For example, if 10 ml of a 0.1 M
 standard solution is required to
 react with 20 ml of an unknown
 solution, then the concentration
 of the unknown solution is 0.05 M.
 This is because the volume of the
 standard solution is twice that of
 the unknown solution, so its
 concentration must be half that
 of the unknown solution.

both of these latter cases the divergence angle is decreased with the same diffuser length. In Ref. 1⁰ it was found that the use of the dividing vane in a flow reduced the losses in wide angled diffusers, but the efficiency was not as high as for a longer diffuser with the same divergence angle as each of the separate passages into which the shorter diffuser was divided.

5. Friction Loss.

Skin friction is one of the major losses encountered in the flow of a viscous fluid over a surface. Prandtl in 1904 introduced the concept of the boundary layer, a region of small thickness near the surface of an object immersed in a fluid stream, or moving through a fluid, within which the speed of the fluid relative to the surface rises within a comparatively short distance from zero at the surface to a value comparable to the relative speed of the body and the fluid at a great distance. The frictional force exerted by the body on the fluid is proportional to the velocity gradient normal to the body and can be expressed:

$$\tau_0 = \mu \frac{dv}{dy} \quad (1)$$

The effect of skin friction is such as to cause a pressure drop in the fluid in the direction of flow. Considering a filament of flow upon which frictional forces are acting:

The first part of the paper is devoted to a study of the
 properties of the function $f(x)$ defined by the
 equation $f(x) = \int_0^x f(t) dt$. It is shown that
 this function is the only solution of the equation
 $f'(x) = f(x)$ which satisfies the condition
 $f(0) = 1$. The second part of the paper is
 devoted to a study of the function $g(x)$ defined
 by the equation $g(x) = \int_0^x g(t) dt$. It is
 shown that this function is the only solution of
 the equation $g'(x) = g(x)$ which satisfies the
 condition $g(0) = 1$.

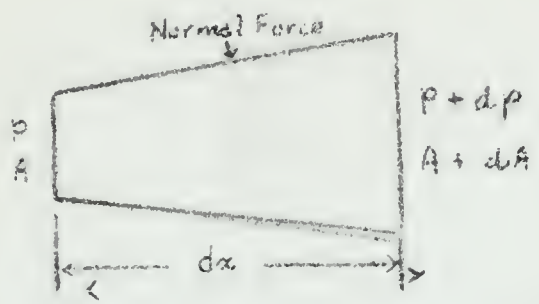
REFERENCES

1. E. T. Whittaker, *A Course of Pure Mathematics*,
 Cambridge University Press, 1927.
2. G. H. Hardy, *An Introduction to the Theory of
 Numbers*, Oxford University Press, 1921.
3. L. E. Dickson, *History of the Theory of Numbers*,
 Interscience Publishers, 1919.
4. J. E. Littlewood, *An Introduction to the Theory of
 Functions*, Cambridge University Press, 1940.
5. R. V. Churchill, *Operational Mathematics*, McGraw-
 Hill, 1958.
6. I. S. Gradshteyn and I. M. Ryzhik, *Table of
 Integrals, Series, and Products*, Butterworths, 1962.
7. E. W. Hobson, *The Theory of Functions*, Cambridge
 University Press, 1931.
8. E. C. Titchmarsh, *The Theory of Functions*,
 Cambridge University Press, 1939.
9. G. E. Hardy and J. E. Littlewood, *Some
 Problems of Geometric Analysis*, Cambridge University
 Press, 1926.
10. G. E. Hardy and J. E. Littlewood, *Some
 Problems of Geometric Analysis*, Cambridge University
 Press, 1926.

$$\int_0^x f(t) dt = f(x)$$

The author wishes to express his appreciation to the
 National Science Foundation for the support of this
 research.

JOHN D. COLEMAN



$$\text{Pressure force} = pA - (p + dp)(A + dA) = -Adp - pdA \quad (2)$$

$$\text{Normal force} = (p + \frac{dp}{2})(A + dA - A) = pdA \quad (3)$$

$$\text{Friction force} = -\tau_0 \pi (D + \frac{dD}{2})(v + \frac{1}{2}dv)dt \quad (4)$$

According to Newton's law of motion:

$$dF = dm \frac{dv}{dt} \quad (5)$$

Now, summing the forces in the direction of motion:

$$F = \text{Pressure force} + \text{normal force component} + \text{friction force} \quad (6)$$

$$dF = -Adp - pdA + pdA - \tau_0 \pi (vdt + \frac{1}{2}Dvdt + \frac{1}{2}vDvdt) \quad (7)$$

$$dm = \rho A dx / g \quad (8)$$

Substituting in the equation of motion:

$$\begin{aligned} -Adp - \tau_0 \pi vdt &= \frac{\rho}{g} A dx \frac{dv}{dt} \\ -dp - 4 \frac{\tau_0 \pi}{D} \frac{dx}{4} \frac{dt}{dt} &= \frac{\rho}{g} \frac{dx}{dt} dv \\ -dp - 4 \tau_0 \frac{dx}{D} &= \frac{\rho}{g} vdv \end{aligned} \quad (9)$$

This equation has also been written:

$$dp + \frac{\rho}{g} d(v^2) + \frac{\rho}{g} v^2 f \frac{dx}{D} = 0 \quad (10)$$



$$S = \frac{1}{2}(a+b)h$$

$$= \frac{1}{2}(a+b)h$$

$$S = \frac{1}{2}(a+b)h$$

$$= \frac{1}{2}(a+b)h$$

$$S = \frac{1}{2}(a+b)h$$

$$= \frac{1}{2}(a+b)h$$

To find the friction loss in terms of total pressure:

$$\frac{dp}{p} + \frac{1}{g} \frac{d(v^2)}{p} + \frac{4}{p} \frac{\tau_0}{D} dx = 0 \quad (11)$$

$$v^2 = g \gamma M^2 \tau^2$$

$$d(v^2) = g \gamma M^2 d(\tau^2) + g \gamma \tau^2 dM^2 \quad (12)$$

$$\frac{\tau_0}{\tau} = 1 + \frac{\gamma-1}{2} M^2$$

$$\frac{d\tau_0}{\tau_0} = \frac{d\tau}{\tau} + \frac{\frac{\gamma-1}{2} d(M^2)}{1 + \frac{\gamma-1}{2} M^2}$$

$d\tau_0 = 0$ (Adiabatic process)

$$d\tau = - \frac{\frac{\gamma-1}{2} \tau d(M^2)}{1 + \frac{\gamma-1}{2} M^2} \quad (13)$$

$$\frac{p_0}{p} = \left(1 + \frac{\gamma-1}{2} M^2\right)^{\frac{\gamma}{\gamma-1}}$$

$$\frac{dp}{p} = \frac{dp_0}{p_0} - \frac{\frac{\gamma}{2} d(M^2)}{1 + \frac{\gamma-1}{2} M^2} \quad (14)$$

Substituting eq. 13 in eq. 12, and eqs. 12 and 14 in eq. 11 gives:

$$\frac{dp_0}{p_0} + \frac{4}{p} \frac{\tau_0}{D} dx = 0 \quad (15)$$

$$\ln \frac{p_2^0}{p_1^0} + \int_1^2 \frac{4}{p} \frac{\tau_0}{D} dx = 0 \quad (16)$$

$$\ln \frac{p_2^0}{p_1^0} + \int_1^2 \frac{2}{q} \frac{\tau_0}{\gamma M^2} dx = 0 \quad (17)$$

The skin friction coefficient for the laminary boundary layer on a thin flat plate is: (Ref. 13.)

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

(11)
$$y' + P(x)y = Q(x)$$

$$y' + \frac{1}{x}y = \frac{1}{x^2}$$

$$y' + P(x)y = Q(x)$$

(12)
$$y' + P(x)y = Q(x)$$

$$y' + P(x)y = Q(x)$$

$$y' + P(x)y = Q(x)$$

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

$$y' + P(x)y = Q(x)$$

$$y' + P(x)y = Q(x)$$

$$y' + P(x)y = Q(x)$$

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

(13)
$$y' + P(x)y = Q(x)$$

(14)
$$y' + P(x)y = Q(x)$$

(15)
$$y' + P(x)y = Q(x)$$

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

THE LINEAR DIFFERENTIAL EQUATION IN STANDARD FORM

$$\frac{\tau_0}{\rho} = 0.730 \sqrt{\frac{\nu}{Vx}}$$

For the turbulent boundary layer, the skin friction coefficient is given by the Squire and Young formula (Ref. 16.) previously given:

$$\frac{\tau_0}{\rho} = \frac{2}{[5.490 \log (4.375 R_e)]^2}$$

Although neither one of these skin friction coefficient equations have been obtained for flow in a duct, it is believed that they will be reasonably accurate if the boundary layer thickness remains small compared with the duct diameter.

6. Turning Loss.

In a turbojet installation it is not always feasible to duct the airflow from the diffuser entrance to the compressor without the use of bends in the ducting. A loss of head results from this change in the direction of the airflow, but with proper design the loss can be kept to a very low value. The loss of head in a turn is caused by the tendency of the flow to separate from the inside wall of the bend. At the entrance to the bend, the velocities in the duct are rectilinear. After entering the bend, the velocities distribution tends to change. The flow on the inside of the bend, turning through a shorter radius, is accelerated faster than the flow on the outside of the turn. Conditions become

$$\frac{1}{2} \sqrt{1 + 4x} = \frac{1}{2} \sqrt{1 + 4x}$$

The first step in the derivation is to take the square root of both sides of the equation. This is done by taking the square root of the left side and the square root of the right side. The result is:

$$\frac{1}{2} \sqrt{1 + 4x} = \frac{1}{2} \sqrt{1 + 4x}$$

Although the two sides of the equation are identical, this is not the case if we consider the domain of the function. The function is defined for all real numbers, but the square root function is only defined for non-negative numbers. Therefore, the domain of the function is $x \geq -\frac{1}{4}$.

The Inverse Function

In a previous section, we saw that the function $f(x) = \frac{1}{2} \sqrt{1 + 4x}$ is a one-to-one function. This means that for every value of y in the range of the function, there is exactly one value of x in the domain of the function such that $f(x) = y$. This property allows us to define the inverse function $f^{-1}(y)$ of the function $f(x)$. The inverse function is defined by the equation $f^{-1}(y) = x$ if and only if $f(x) = y$. In other words, the inverse function "undoes" the action of the original function. For example, if $f(x) = \frac{1}{2} \sqrt{1 + 4x}$, then $f^{-1}(y) = \frac{1}{4}(4y^2 - 1)$. This means that if we take a value y in the range of the function and apply the inverse function to it, we will get the value x in the domain of the function such that $f(x) = y$.

similar to those for a free vortex, and the pressure on the inside of the turn is less than that on the outside. This redistribution of velocity results in increased turbulence throughout the bend. Upon leaving the bend, conditions are reversed, and the approximate free vortex motion established in the bend must be changed back to rectilinear flow. For a 90° turn the length of duct following the corner should be about 4 x the diameter of the duct.

According to Ref. 19, the turning loss is a function of the following:

1. the radius ratio, the ratio of the radius of curvature of the duct (R) to the diameter or width of the duct (D), measured in the same plane as R.
2. the aspect ratio, or ratio of the height of the duct (H) to its width (D).
3. the angle (θ) through which the air is deflected by the corner.
4. the local Reynold's number.

The pressure loss involved in turning the airflow can be expressed in the form of a resistance coefficient:

$$K_c = \frac{\Delta h_c}{\frac{1}{2} \rho V^2}$$

Fig. 10 shows the effect of radius ratio and deflection angle upon the resistance coefficient. It should also be realized that the turning loss is proportional to the

... the ... of the ...

... the ... of the ...

... the ... of the ...

... the ... of the ...

... the ... of the ...

... the ... of the ...

... the ... of the ...

... the ... of the ...

$$\frac{\Delta}{\Gamma} = \frac{\Delta}{\Gamma} = \frac{\Delta}{\Gamma}$$

... the ... of the ...

... the ... of the ...

square of the velocity. Some representative values of the resistance coefficient for various duct shapes and turning angles are given below. In this particular series of tests the Reynolds number was between 10^5 and 10^6 based upon duct diameter.



$\theta = 30^\circ$	$k_c = 0.15$	0.10	0.02
$\theta = 60^\circ$	1.10	0.40	0.05
$\theta = 90^\circ$	1.60	1.05	0.20

The advantage of the circular duct without too small a value of radius ratio and with small turning angles is readily apparent from the above listed values of resistance coefficient. However, the efficiency of the rectangular duct can be made to approach that of the circular duct by increasing the aspect ratio, W/D . The influence of aspect ratio with varying radius ratio to give a resistance coefficient of 0.15 is shown in Fig. 11.

Sharp bends may also be improved by the use of curved vanes in the bend. These have the effect of creating high aspect ratio passages. The gap/chord ratio, s/c , of these vanes is important as shown in Fig. 12. Resistance coefficient reduces to a minimum at a gap/chord ratio of about 0.3, and then increases as the gap/chord ratio is raised or lowered. This data

was obtained in a 90 degree bend with vanes shaped as quarter circles. The angle of incidence of the flow was 45 degrees, and the Reynolds number based on the chord of the vane was between 10^4 and 10^5 . It was also found that the angle of incidence was not particularly critical as long as the vanes did not stall. The primary requisite of the vanes is to have the flow parallel to the duct wall when it leaves the vanes. The angle of incidence of the vanes is defined as the angle which the chord of the vane makes with the direction of the incoming flow.

Some data on the losses involved when a turn is made in an expanding entry was obtained from Ref. 20 and is shown in Fig. 13. In this test the duct was rectangular with two diverging and two parallel walls. It was found that fairly high resistance coefficients were encountered particularly with increasing expansion ratios. Since the loss occurring in a bend involves flow separation from the wall, and since the danger of separation is always encountered in the diffusion process with increasing area ratios, it might be expected that the combination of these two unstable flow processes would result in fairly high losses.

7. Obstructions in the Flow.

It would be desirable to eliminate all obstructions from air intake ducts, but it is not always possible. In

The first part of the report deals with the general situation of the country and the progress of the work done during the year. It is followed by a detailed account of the various projects and schemes which have been undertaken. The report concludes with a summary of the work done and a statement of the progress made.

The second part of the report deals with the financial statement of the organization. It shows the income and expenditure for the year and the balance sheet at the end of the year. It also shows the details of the various projects and schemes which have been undertaken. The report concludes with a summary of the financial statement and a statement of the progress made.

The third part of the report deals with the general remarks and conclusions. It discusses the various projects and schemes which have been undertaken and the progress made. It also discusses the financial statement and the balance sheet at the end of the year. The report concludes with a summary of the work done and a statement of the progress made.

many cases the diffuser is not a simple conical shape, but may be an annular duct with a central cone. The central cone must be supported in some manner, usually by struts to the outer cone structure. The central cone may also house apparatus requiring leads from the outside of the engine. In some instances, screens may be placed in the duct ahead of the compressor inlet to prevent the entry of foreign matter into the engine. All of these obstructions are potential sources of pressure loss due to turbulent flow about them. The magnitude of the loss depends upon the location and shape of the obstruction. It would be impossible to give general rules covering all possible cases, but some estimate of the loss may be made for a particular case.

Let us consider one of the worst cases, an obstruction which is not streamlined. The loss occasioned by this shape can be considered to be caused by a sudden contraction, followed by a sudden expansion of the flow. Ref. B gives the general form of these losses.

Loss due to a sudden contraction:

$$\Delta p = \frac{k \rho v_b^2}{2g}$$

v_b/v_a	0.6	0.7	0.8	0.9	1.0
k	0.28	0.21	0.14	0.06	0.0

Loss due to a sudden expansion:

$$\Delta p = \rho \frac{(v_b - v_c)^2}{2g}$$

The first part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $\epsilon \rightarrow 0$. It is shown that the solutions of (1) converge to the solutions of the system (2) in the limit. The convergence is proved in the L^2 norm. The second part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $\epsilon \rightarrow 0$. It is shown that the solutions of (1) converge to the solutions of the system (2) in the limit. The convergence is proved in the L^2 norm.

The third part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $\epsilon \rightarrow 0$. It is shown that the solutions of (1) converge to the solutions of the system (2) in the limit. The convergence is proved in the L^2 norm. The fourth part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $\epsilon \rightarrow 0$. It is shown that the solutions of (1) converge to the solutions of the system (2) in the limit. The convergence is proved in the L^2 norm.

Let us consider the case of a linear boundary value problem.

$$\frac{\partial u}{\partial x} + u = f(x)$$

$x=0$	$x=L$	$x=0$	$x=L$	$x=0$	$x=L$
$u=0$	$u=0$	$u=0$	$u=0$	$u=0$	$u=0$

where $f(x)$ is a given function.

$$\frac{\partial u}{\partial x} + u = f(x)$$

Subscripts:

- a - position ahead of obstruction.
- b - position of minimum cross-sectional area.
- c - Position after obstruction.

Loss due to an obstruction:

Assume that $v_a = v_c$

$$\Delta p = k \frac{\rho v_b^2}{2g} + \frac{\rho (v_b - v_a)^2}{2g}$$

$$\Delta p = q_b \left(k + \left(1 - \frac{v_a}{v_b} \right)^2 \right)$$

Assume that the flow is incompressible in the vicinity of the obstruction. This assumption is justified because the obstruction will probably be located in a region in which the flow has already been considerably slowed down. Since the loss is a function of the square of the velocity it would not be logical to have an obstruction in the high speed flow region.

$$v_a/v_b = A_b/A_a = (D_b/D_a)^2$$

$$\Delta p = q_b \left(k + \left(1 - A_b/A_a \right)^2 \right)$$

Now the loss coefficient of sudden contraction is based on flow from a larger pipe to a smaller one, but let us assume that the same coefficient is satisfactory based on area ratios, then a new loss coefficient based on area ratios can be calculated.

$$\Delta p = k q_b$$

PROBLEM 1

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.

Find the sum of the roots of the equation $f(x) = g(x)$.

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.

Then the equation $f(x) = g(x)$ is

$$x^2 + 2x + 1 = x^2 - 2x + 1$$

$$\frac{x^2 + 2x + 1}{x^2} = \frac{x^2 - 2x + 1}{x^2} \implies 1 + \frac{2}{x} + \frac{1}{x^2} = 1 - \frac{2}{x} + \frac{1}{x^2}$$

$$\frac{2}{x} + \frac{1}{x^2} = -\frac{2}{x} + \frac{1}{x^2}$$

Subtracting $\frac{1}{x^2}$ from both sides, we get

$\frac{2}{x} = -\frac{2}{x}$, which implies $4 = 0$, a contradiction.

Therefore, the only solution is $x = 0$.

Since the sum of the roots is 0 , the answer is 0 .

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.

Then the equation $f(x) = g(x)$ is

$$x^2 + 2x + 1 = x^2 - 2x + 1$$

$$\frac{x^2 + 2x + 1}{x^2} = \frac{x^2 - 2x + 1}{x^2} \implies 1 + \frac{2}{x} + \frac{1}{x^2} = 1 - \frac{2}{x} + \frac{1}{x^2}$$

Subtracting $\frac{1}{x^2}$ from both sides, we get

$\frac{2}{x} = -\frac{2}{x}$, which implies $4 = 0$, a contradiction.

Therefore, the only solution is $x = 0$.

Since the sum of the roots is 0 , the answer is 0 .

Let $f(x) = x^2 + 2x + 1$ and $g(x) = x^2 - 2x + 1$.

$$\frac{x^2 + 2x + 1}{x^2} = \frac{x^2 - 2x + 1}{x^2}$$

where $C = k + (1 - A_1/A_2)^2$

This new coefficient is plotted in Fig. 14 for various area ratios.

If the obstruction is large, the losses will be large, but for most obstructions which might be encountered the loss is low, but of significant magnitude when trying to keep efficiency high. The loss due to an obstruction in the flow can be further reduced by the use of a fairing or streamline shape around the obstruction. In this case the only loss to be expected would be that due to friction which should be very small.

8. Leakage Loss.

At the exit of a diffuser the internal pressure may be considerably above the pressure of the surrounding air. Unless care has been taken in making the joints, particularly where the diffuser joins the compressor, the air will leak into the region of lower pressure. This consideration militates against the use of long ducts from the diffuser exit to the compressor entrance.

Depending upon the number and size of the leaks themselves, leakage can have a serious effect on diffuser efficiency. Leakage results in a two-fold loss. First, there is a loss in the mass flow into the compressor; and, secondly, there is a loss in pressure resulting from the loss in fluid. To make an estimate

$$x_{ij}^2 = x_i + x_j + c$$

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

of the extent of loss due to leakage would serve no useful purpose. Leakage is inexcusable, and if it should occur, the first thought should not be what is the effect of the loss, but how can the leak be stopped.

9. Exit Loss.

It has been found (Ref. 21 and Ref. 3) that complete pressure recovery does not occur entirely within the diffuser for a given diffuser area ratio. Ref. 21 was the source of Fig. 15 which shows the length of ducting necessary for a turbulent velocity profile to develop in the duct. The velocity profile leaving the diffuser proper is parabolic in shape due to the fact that pressure recovery is not uniform in a plane normal to the diffuser axis.

Ref. 3 claims that the required length of ducting following a diffuser can be reduced by suction slots in the vicinity of the diffuser exit, or inducing a solid body rotation in the flow in the diffuser. Suction slots, therefore, which were used to reduce the likelihood of flow separation now serve a two fold purpose and reduce the required length of exit ducting. The extent of rotation induced in the flow at the diffuser exit by the rotary motion of the compressor is not known, but it is felt that some rotation does occur. This, too, would have the beneficial effect of shortening the length of exit ducting required. Generally

speaking, an annular type diffuser has a more desirable exit velocity profile than does a plain conical diffuser and would require a shorter length of exit ducting for complete pressure recovery.

CHAPTER IV

GEOMETRIC CONSIDERATIONS

1. Inlet Duct Location.

The aircraft designer has the choice of many different locations for his engine air inlet, limited, of course, by the engine location which may be:

1. Submerged in the fuselage.
2. Partially submerged in the fuselage.
3. Submerged in the wing root.
4. Located in a nacelle in the wing structure.
5. Located in a nacelle supported by a pylon from the wing structure.

The air inlet may be located at a stagnation point in the flow about the airplane, or may be of the scoop type, with or without boundary layer control, or it may be a flush type opening in the fuselage. The choice of design is a compromise between internal flow considerations, external drag considerations, and structural considerations.

The stagnation point inlet has the advantage of giving a good velocity distribution across the inlet face without artificial flow control. When the stagnation point is the nose of the fuselage, however, long ducts are required to lead the flow back to the engine. At high speeds the pressure differential between the

THE HISTORY OF THE

CHAPTER V

The history of the

CHAPTER VI

The history of the

CHAPTER VII

The history of the

CHAPTER VIII

The history of the

CHAPTER IX

The

The history of the

The history of the

The history of the

The history of the

The history of the

The history of the

The

The history of the

The history of the

The history of the

The history of the

The history of the

inside and outside of the duct requires substantially constructed ducts with well sealed joints to prevent leakage. Valuable fuselage space is sacrificed to the ducting, and bends in the ducting are generally required to guide the flow around obstructions.

In multi-engine installations, the trend is to locate the jet engines in or supported from the wings. This type of engine installation permits stagnation point air inlet ducts with short diffusers required because of space limitations. Expansion angles greater than optimum may be required. Additional problems are also present. For supersonic plane designs the effect of the shock wave, originating at the fuselage nose, on the flow ahead of the air inlet must be considered, and may limit the engine location. The shock wave forming ahead of the air inlet duct itself will undoubtedly influence the flow over the wing of the plane, and may cause such a loss in the wing performance that such a configuration would not be permissible. For subsonic flows care must be taken where several air inlets are adjacent that the flow into one duct does not affect the velocity distribution across the face of another, or cause the critical Mach number of the wing to be lowered.

The scoop type of inlet has poor velocity distribution across the face of the duct because it is located next to a surface where a boundary layer exists. The

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

...the ... of the ...
...the ... of the ...
...the ... of the ...

velocity distribution can be improved by boundary layer bleeds at the duct entrance until conditions comparable to the stagnation point inlet exist. The added feature of the boundary layer bleed and its control add to the design complexity, however. For scoop inlets to an engine submerged in the fuselage the flow must negotiate two turns and join in a Y-duct at the compressor entrance in most instances. This problem is not unique to the scoop type of inlet, though. Many designs with the inlet in the nose of the fuselage have a similar configuration where the ducting is divided at the nose of the airplane, and the ducts follow the sides of the fuselage and meet at the engine entrance.

The scoop type of inlet has advantages also. Shorter lengths of ducting are required which mean a weight saving and reduce the probability of leakage loss. Less fuselage space is required for the ducting, and improved visibility for the pilot due to more desirable nose shapes results. For military aircraft better armament arrangement can be obtained when there is no ducting in the nose of the fuselage. Where the scoop is located at the wing-fuselage juncture the critical Mach number of this section can be improved. This particular point is also a source of drag which may be reduced considerably by the inlet and exit duct location there.

With the coming of supersonic plane designs several examples of the flush type of air inlet duct have

appeared. The flush air inlet located at some point on the fuselage sacrifices ram compression ahead of the air inlet and has an entrance velocity distribution problem, but the decrease in resulting drag and wall effect on the flow around the fuselage contour must offer greater benefits than the reduced performance due to incomplete ram recovery.

The inlet ducts under discussion are the main air inlet ducts for high speed operation. Some aircraft have auxiliary air inlet ducts for low speed operation and take-off conditions. At low speeds the velocity ratio is so high that diffuser performance suffers. Ram recovery is not of much significance at these low speeds, and so the auxiliary air inlets provide a means of getting a large volume of air to the engine in the quickest possible manner. These auxiliary ducts are usually spring loaded doors opening directly into the plenum chamber at the compressor entrance. When the pressure in the plenum chamber is below atmospheric the auxiliary air inlet opens; when the pressure gets up to atmospheric the auxiliary air inlet closes due to the spring action, and a flush exterior surface results.

The choice of air inlet duct location is subject to many compromises. It would be impossible to reach a definite conclusion as to which is unreservedly better than any other. Present airplane designs show a great variety of inlet duct locations and types of entrances,

... the first part of the ...
 ... the second part of the ...
 ... the third part of the ...
 ... the fourth part of the ...
 ... the fifth part of the ...

... the sixth part of the ...
 ... the seventh part of the ...
 ... the eighth part of the ...
 ... the ninth part of the ...
 ... the tenth part of the ...

... the eleventh part of the ...
 ... the twelfth part of the ...
 ... the thirteenth part of the ...
 ... the fourteenth part of the ...
 ... the fifteenth part of the ...

... the sixteenth part of the ...
 ... the seventeenth part of the ...
 ... the eighteenth part of the ...
 ... the nineteenth part of the ...
 ... the twentieth part of the ...

... the twenty-first part of the ...
 ... the twenty-second part of the ...
 ... the twenty-third part of the ...
 ... the twenty-fourth part of the ...
 ... the twenty-fifth part of the ...

some of these particular instances will be discussed later. It appears that in some cases the location of the entrance duct was a result of the airframe configuration; in other cases it would appear that the airframe configuration resulted from a choice in the location of the air entrance duct. In the future it is believed that the latter approach will be more prevalent.

2. Area Ratios and Diffuser Length.

If a diffuser exit mach number is assumed, the required area ratio to obtain it can be computed for various entrance mach numbers and diffuser efficiencies. An exit mach number of 0.3 will be assumed, which is a reasonable value for the airflow to be supplied to the compressor. A range of entrance mach numbers from 0.3 to 1.0 will be investigated. Mach numbers greater than one will not occur in the diffuser because it is preferable to have the shock wave located outside the diffuser. Instead of diffuser efficiency the variation of area ratio and diffuser length with total pressure ratio, which is a measure of diffuser efficiency, will be investigated.

First, the area ratio necessary to accelerate a flow isentropically from its present mach number to a mach number of one can be determined from continuity considerations.

$$\frac{p_{01}}{\rho_1} = \frac{p^* A^*}{\rho^*}$$

$$\frac{A}{A^*} = \frac{M^*}{M} \frac{p^*}{p} \left(\frac{T}{T^*}\right)^{\frac{1}{2}}$$

$$M^* = 1$$

$$\frac{p^*}{p} = \left(\frac{1 + \frac{\gamma-1}{2} M^2}{\frac{\gamma+1}{2}}\right) \frac{\gamma}{\gamma-1}$$

$$\frac{T}{T^*} = \left(\frac{1 + \frac{\gamma-1}{2} M^2}{\frac{\gamma+1}{2}}\right)^{-1}$$

$$\frac{A}{A^*} = \frac{1}{M} \left(\frac{1 + \frac{\gamma-1}{2} M^2}{\frac{\gamma+1}{2}}\right) \frac{\gamma+1}{2(\gamma-1)}$$

If the process is isentropic, $A_1^* = A_2^*$

$$\frac{A_2}{A_1} = \frac{A_2/A_2^*}{A_1/A_1^*} = \frac{M_1}{M_2} \left(\frac{1 + \frac{\gamma-1}{2} M_2^2}{1 + \frac{\gamma-1}{2} M_1^2}\right) \frac{\gamma+1}{2}$$

If the process is adiabatic, but non-isentropic

$$\frac{A_2}{A_1} = \frac{A_2^*}{A_1^*} \frac{M_1}{M_2} \left(\frac{1 + \frac{\gamma-1}{2} M_2^2}{1 + \frac{\gamma-1}{2} M_1^2}\right) \frac{\gamma+1}{2(\gamma-1)}$$

$$\frac{A_2^*}{A_1^*} = \frac{p_1^0}{p_2^0} \frac{\Delta S}{R}$$

$$\frac{A_2}{A_1} = \frac{p_1^0}{p_2^0} \frac{M_1}{M_2} \left(\frac{1 + \frac{\gamma-1}{2} M_2^2}{1 + \frac{\gamma-1}{2} M_1^2}\right) \frac{\gamma+1}{2(\gamma-1)}$$

The required area ratios to accomplish compression to an exit Mach number of 0.3 with various entrance Mach numbers and total pressure ratios are shown in Fig. 16.

If a conical diffuser with a divergence angle of 8 deg. is assumed, the resultant ^{ing} diffuser length is a function of the mass flow to be digested and the area ratios previously determined.

$$\frac{1}{x^2} = x^{-2}$$

$$\frac{d}{dx} x^{-2} = -2x^{-3} = -\frac{2}{x^3}$$

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

is the answer to the problem, the derivative of $\frac{1}{x^2}$ is $-\frac{2}{x^3}$.

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

is the answer to the problem, the derivative of $\frac{1}{x^2}$ is $-\frac{2}{x^3}$.

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

$$\frac{d}{dx} \left(\frac{1}{x^2} \right) = -\frac{2}{x^3}$$

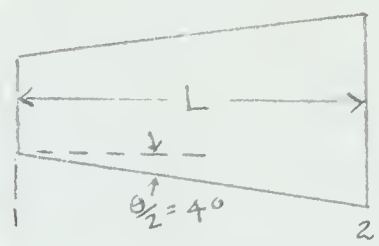
The derivative of $\frac{1}{x^2}$ is $-\frac{2}{x^3}$. This result can be obtained by using the power rule for differentiation. The power rule states that if $f(x) = x^n$, then $f'(x) = nx^{n-1}$. In this case, $n = -2$, so $f'(x) = -2x^{-2-1} = -2x^{-3} = -\frac{2}{x^3}$. Another way to verify this result is by using the definition of the derivative. The derivative of $f(x)$ is defined as $f'(x) = \lim_{h \rightarrow 0} \frac{f(x+h) - f(x)}{h}$. For $f(x) = \frac{1}{x^2}$, we have $f'(x) = \lim_{h \rightarrow 0} \frac{\frac{1}{(x+h)^2} - \frac{1}{x^2}}{h}$. Simplifying the numerator, we get $\frac{x^2 - (x+h)^2}{(x+h)^2 x^2} = \frac{x^2 - (x^2 + 2xh + h^2)}{(x+h)^2 x^2} = \frac{-2xh - h^2}{(x+h)^2 x^2}$. Dividing the numerator and denominator by h , we get $\frac{-2x - h}{(x+h)^2 x^2}$. Taking the limit as $h \rightarrow 0$, we get $\frac{-2x}{x^2 x^2} = -\frac{2}{x^3}$. Therefore, the derivative of $\frac{1}{x^2}$ is $-\frac{2}{x^3}$.

$$w = P AV = 49.1 P A M \sqrt{\sigma}$$

$$\sigma = P/P_{SL} \quad \theta = \gamma/\gamma_{SL}$$

$$A_1 = \frac{\pi}{4} D_1^2 = \frac{w \sqrt{\sigma}}{49.1 P_{SL} M \sqrt{\sigma}}$$

$$D_1 = \sqrt{\frac{w \sqrt{\sigma}}{67 M}}$$



$$\tan \frac{\theta}{2} = \frac{D_2 - D_1}{2L}$$

$$L = \frac{D_1 (\sqrt{A_2/A_1} - 1)}{2 \tan 40}$$

Fig. 17 shows the variation of diffuser length with different values of the weight flow parameter and total pressure ratios for various entrance mach numbers.

Figure 16 reveals that relatively small area ratios will reduce any expected diffuser entrance mach number to an exit mach number of 0.3, even with large internal losses in the diffuser. Large internal losses in the diffuser are not to be expected, however, with such small area ratios. Ref. 3 shows high diffuser efficiencies with small area ratios, and a diffuser divergence angle of 6 to 8 deg.

In Fig. 17 the effect of entrance mach number and weight flow upon the diffuser length can be seen with an exit mach number of 0.3 and a diffuser divergence angle of 8 degrees. It is interesting to note that the greatest

$$r = \frac{9}{10} = 0.9$$

$$r = 0.9$$

$$r = \frac{9}{10}$$

$$\frac{r}{1-r} = \frac{0.9}{1-0.9} = \frac{0.9}{0.1} = 9$$

$$\frac{r}{1-r} = 9$$



$$\frac{r}{1-r} = 9$$

$$\frac{r}{1-r} = 9$$

The following text is extremely faint and appears to be bleed-through from the reverse side of the page. It contains several paragraphs of text, but the content is illegible due to the low contrast and blurriness of the scan.

diffuser length does not occur with the largest diffuser entrance Mach number, but occurs at an entrance Mach number of about 0.62. This is due to the small change in area ratio required at these high entrance Mach numbers in comparison to the change in entrance area required to maintain the given weight flow. As was to be expected, diffuser length increases with increased mass flow and decreased diffuser efficiency.

Whether these diffuser lengths are tolerable depends upon the engine location and the size of the airplane. For an engine located in the fuselage, and with the diffuser entrance located in the nose, it is hardly likely that such diffuser lengths would be critical even with large weight flows. The weight flow of 150 pounds of air per second, using the thumb rule that one pound of air per second corresponds to 50 pounds of thrust, would be the equivalent of a 7,500 pound thrust unit. For an engine installation in the wing, or in a pylon attached to the wing, such diffuser lengths as have been calculated might be impractical. These lengths could be decreased by increasing the divergence angle, but reduced diffuser performance could be expected since the divergence angle used in the computations is just about the optimum. Such problems, however, should be considered in the selection of an engine and its installation.

The first thing I noticed when I stepped out of the plane was the
 humidity. It was a sticky, oppressive heat that clung to my skin.
 I had heard that the weather in the tropics was unbearable, and
 now I knew why. The sun was a merciless giant, pouring down its
 rays with a relentless intensity. I had to shield my eyes as I
 stepped onto the tarmac. The air was thick with the scent of
 tropical flowers and the distant hum of machinery. I felt a
 sense of awe and wonder as I took in the sights and sounds of
 this new world. The vibrant colors of the buildings and the
 lush greenery of the surrounding landscape were a stark
 contrast to the grey and brown of my home. I had come to a
 place where nature was in full, unbridled glory.

As I walked through the terminal, I noticed the diverse
 mix of people. There were men in traditional attire, women
 in modern fashion, and children of all ages. The atmosphere
 was one of excitement and anticipation. I had heard that the
 people here were friendly and hospitable, and now I was
 beginning to see why. The smiles and waves I received from
 the staff and other passengers were a warm welcome. I
 felt a sense of belonging and a desire to explore this
 beautiful land. I had come to a place where the world was
 truly at its best.

The journey had been long and tiring, but it was
 worth every moment. I had seen the world from a new
 perspective, and I had discovered a place that was
 truly amazing. I had come to a place where the
 sun was always shining, and the life was always
 full. I had come to a place where the world was
 truly at its best.

3. Velocity Ratio.

A. Effect of velocity ratio on a diffuser.

Velocity ratio is defined as the ratio of the diffuser entrance velocity to the free stream velocity of the airflow. For subsonic flows NACA has determined experimentally that this ratio should be within the range of 0.3 to 0.6 for optimum performance. It was found that at very low velocity ratios the flow tended to separate from the outside lip of the diffuser and increase the external drag of the engine nacelle. At higher velocity ratios the flow tended to separate from the diffuser wall and the pressure recovery and diffuser efficiency decreased.

The volume flow through a turbojet tends to remain constant for a given engine speed, and so, at any one flight velocity, the required inlet area for a diffuser is a function of the velocity ratio.

$$A_1 = \frac{Q}{V_0}$$

Therefore, a bigger entrance area is required for low velocity ratios than for high velocity ratios.

At flight velocities greater than the diffuser inlet velocity a stream tube ahead of the diffuser inlet starts expanding. The flow velocity in the stream tube is decelerated to the desired inlet velocity and in the process is compressed isentropically.

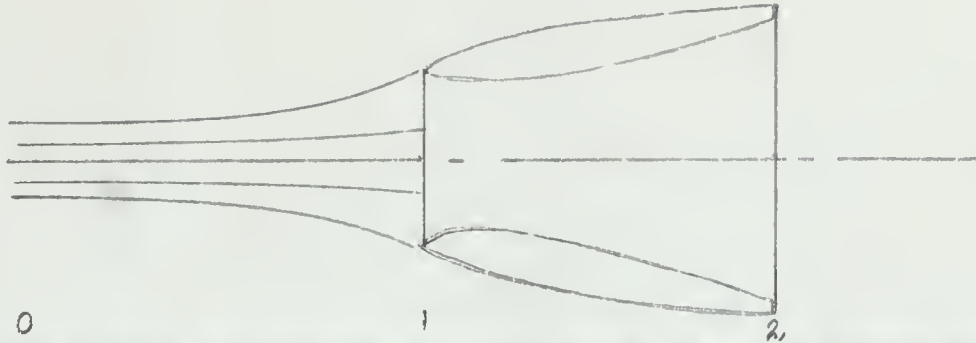
3. Results

The first part of the analysis is a descriptive statistics of the data. The second part is a regression analysis. The third part is a sensitivity analysis. The fourth part is a conclusion.

The descriptive statistics show that the data is normally distributed. The regression analysis shows that there is a significant relationship between the variables. The sensitivity analysis shows that the results are robust to changes in the parameters. The conclusion is that the findings are consistent with the hypothesis.

$$y = \beta_0 + \beta_1 x + \epsilon$$

The regression results are presented in Table 1. The coefficients are all statistically significant. The adjusted R-squared is 0.45. The F-statistic is 12.34. The p-value is 0.001. The confidence interval for the slope coefficient is [0.5, 1.5].



At the lower velocity ratios more of the compression is accomplished outside the diffuser than at higher velocity ratios.

Since compression outside the diffuser is accomplished at greater efficiency than compression in the diffuser, it would seem to be more practical to keep the velocity ratio as low as possible. However, it should be noted that as the flow approaches the diffuser entrance it has a velocity component normal to the diffuser axis. This is equivalent to increasing the angle of attack of the diffuser lip in the air stream. At very low velocity ratios the diffuser lip stalls and the flow separates from the outside surface of the diffuser increasing the drag of the nacelle. For this reason, a lower limit of permissible velocity ratios is established.

At the higher velocity ratios more of the compression must be accomplished in the diffuser. For the same length of diffuser and exit velocity the pressure gradient is greater, and the danger of internal flow separation from the wall of the diffuser is increased. If the length of the diffuser is increased to permit the same pressure gradient as could be obtained with the lower



The drawing shows a tapered shaft or pipe. The shaft is shown in a perspective view, tapering from left to right. The left end is wider than the right end. There are several horizontal lines representing the profile of the shaft, and a vertical line indicating a specific cross-section or feature. The drawing is a technical illustration, likely for a patent or engineering document.

velocity ratio, the boundary layer has a greater distance in which to grow thicker. Separation of flow is also a function of the boundary layer thickness. In view of these reasons the upper limit on desirable velocity ratios is established.

B. Variation of velocity ratio with range of operation.

Once the geometry of a diffuser has been established for desirable operation at a particular design condition, the velocity ratio will vary with departure from the design point,

$$r = \frac{V_1}{V_0} = \frac{Q}{49.1 A_1 \sqrt{T_0}}$$

This equation indicates that the velocity ratio varies inversely as the flight mach number and the square root of the ambient temperature. It also varies directly with the volume of airflow. Particularly critical are the static thrust and take-off conditions. At the static thrust condition the velocity ratio is infinite, and at take-off velocity the velocity ratio is considerably greater than one for an entrance duct designed for efficient operation at high speed, unless auxiliary air inlets are provided into the plenum chamber.

C. Effect of supersonic speed on velocity ratio.

At supersonic speeds with a shock wave ahead of the diffuser entrance, the values of V_0 , V_0' , and T_0

... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...

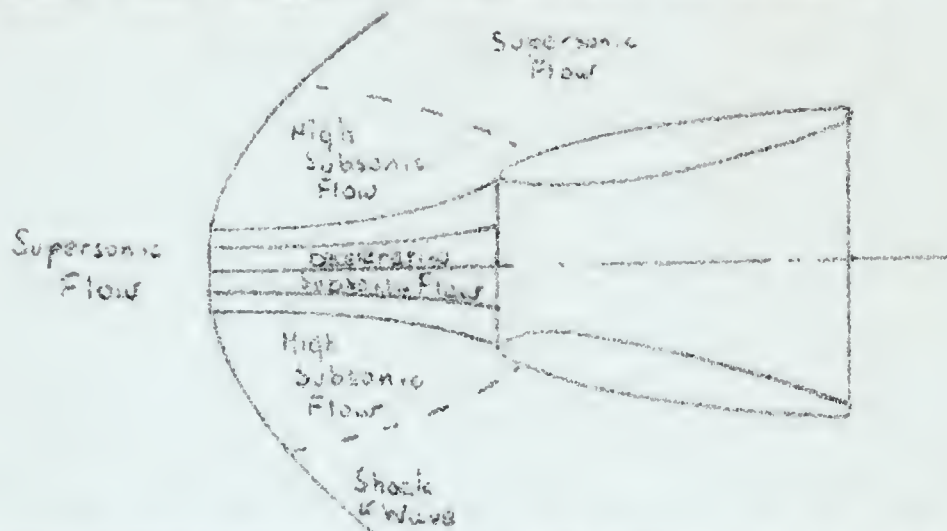
... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...

$$\frac{1}{\sqrt{1-\beta^2}} = \frac{1}{\sqrt{1-\frac{v^2}{c^2}}}$$

... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...

... the ... of ...
 ... the ... of ...
 ... the ... of ...
 ... the ... of ...

used in the computation of velocity ratio are the free stream conditions immediately following the shock wave. Other values would have little significance. Since it is assumed that a normal plane shock occurs in the region of flow through which the stream tube entering the diffuser passes, the conditions immediately following the shock are uniform. Whether or not the limits for velocity ratio which have been established for subsonic flow are applicable is a question of great importance. Although the stream velocity directly ahead of the diffuser inlet is subsonic, the adjacent flow is not. The velocities in the region about the diffuser entrance are of some such complicated pattern as shown.



Low velocity ratios will move the position of the shock wave to greater distances from the diffuser inlet. The effect of this position of the shock wave on the nacelle drag, and the exact position of the shock wave is not known. It would seem likely that positioning the shock wave on the diffuser lip with a velocity ratio of one would cause the least drag. In this case, the external

flow field would be supersonic, and the internal flow subsonic. Of course, this would require a large percentage of the pressure recovery to be effected by the diffuser, and diffuser efficiency decreases with increased demands upon the diffuser. A further complication introduced by positioning the shock on the diffuser lip is the effect on the boundary layer.

The deceleration of flow through a shock wave is accomplished with some degree of turbulence accounting for the entropy increase through the shock. With a detached shock this turbulence tends to be damped out in the free stream flow. If the shock is positioned on the diffuser lip, the ensuing turbulence is transmitted to the boundary layer. Up to the throat of the diffuser there is a favorable negative pressure gradient tending to damp the turbulence, and establish laminar flow conditions in the boundary layer. This favorable region is of very short length, however, and the turbulence may carry over into the unfavorable positive pressure gradient region in the divergent part of the diffuser, and hasten flow separation, seriously affecting the diffuser efficiency. This should be thoroughly investigated.

Thus, we are confronted with a situation where a decision must be made as to which is the more critical factor, the powerplant performance or the aerodynamic performance of the airplane. Before a decision can be

The first part of the document is a letter from the
 author to the editor of the journal. The letter
 discusses the author's interest in the subject
 and the reasons for writing the paper. The author
 mentions that the paper is based on a study
 conducted in the field of psychology. The author
 states that the study was conducted over a
 period of six months and involved a total
 of 100 participants. The author describes the
 methodology used in the study and the results
 that were obtained. The author concludes the
 letter by expressing the author's hope that
 the journal will find the paper interesting
 and useful to its readers.

reached, the magnitude of the effects of shock wave position must be determined.

The first part of the document is a preface, which is written in a very simple and direct style. It explains the purpose of the document and the reasons for its publication. The preface is followed by a list of the contents, which is also written in a simple and direct style. The list of contents is followed by the main body of the document, which is divided into several sections. Each section is written in a simple and direct style, and is followed by a list of references. The document concludes with a final section, which is also written in a simple and direct style.

CHAPTER V

TYPICAL DIFFUSER PROBLEMS

1. The Geometry of the Diffuser.

The first consideration in the design of a diffuser is its size and shape. The size is controlled by the desired volume of airflow through the diffuser, and its shape by the desired characteristics of the internal flow. An infinite number of shapes and sizes could be considered, but for practical reasons only one configuration will be analyzed. It is hoped that the method of analysis used will be applicable to other designs with necessary modifications.

A representative modern turbo-jet engine develops 4,000 pounds of static thrust with an airflow of 73 pounds of air per second. The compressor of this engine will consume a constant volume of air for a given engine speed. The turbo-jet engine is characterized by giving its best performance at its design engine speed which is 100 per cent RPM. The volumetric capacity of the given engine can then be calculated from the continuity equation, and the diffuser will be designed accordingly. The density of the entering airflow will be assumed to be that of the standard sea level atmosphere.

$$w = \rho AV = 73 \text{ lb./sec.}$$

THE UNIVERSITY OF CHICAGO

PH.D. THESIS

The first consideration in the design of a program is the choice of the language. The choice is determined by the nature of the problem to be solved. For example, if the problem is one of numerical calculation, a language such as Fortran or Algol would be appropriate. If the problem is one of symbolic manipulation, a language such as Lisp or Pascal would be more suitable. The choice of language is also influenced by the availability of hardware and software. Once the language has been chosen, the next step is to design the program. This involves the choice of data structures, the design of algorithms, and the writing of code. The design of data structures is particularly important, as it can have a significant impact on the efficiency of the program. The design of algorithms is also crucial, as it determines the complexity of the program. Finally, the writing of code is the final step in the design process. This involves the translation of the design into a form that can be executed by the computer. The quality of the code is also important, as it can affect the reliability and performance of the program.

THE UNIVERSITY OF CHICAGO

$$Q = AV = \frac{W}{\rho} = \frac{73}{.0765} = 954.2 \text{ cu. ft./sec.}$$

w = weight flow, lb./sec.

Q = volume flow, cu. ft./sec.

A = cross-sectional area of flow, sq. ft.

V = flow velocity, ft./sec.

ρ = specific weight of fluid, lb./cu.ft.

The three critical design conditions of a turbo-jet powered airplane are the static thrust condition, take-off and maximum speed. In the first two conditions a diffuser is of little use, and it would be better if some device was used to bypass the diffuser. The condition of maximum speed, however, is the point at which diffuser performance is desired. The design operating condition of the diffuser is then decided upon. Our selection is a flight Mach number of 1.5 at 40,000 feet altitude.

The diffuser will be conical with a rounded entrance lip to reduce entrance losses. The velocity ratio desired is 0.6. For flight Mach numbers greater than one a detached normal shock will occur ahead of the diffuser, and the total pressure loss accompanying this shock will be accepted. Where shock occurs, the free stream velocity following the shock will be used to determine the velocity ratio of the diffuser. The velocity of flow from the exit of the diffuser will be that corresponding to a Mach number of 0.3. With

... .. ?

... ..

... ..

... ..

... ..

... .. ?

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

this information the size of the diffuser can be determined.

First, the conditions across the shock front have to be determined. The initial conditions are for the standard atmosphere, and the conditions across the normal shock are found in Ref. 5, Table 48. It is then assumed that the flow is slowed isentropically from the free stream condition to the condition at the diffuser entrance. This gives the following conditions:

Station	θ	$T^{\circ}R$	a -ft/sec	p -lb/ft ²	ρ -slugs/ft ³
x	1.5	392.4	970.7	391.9	.000532
y/x		1.320		2.458	1.9621
y	.7011	518	1117.5	960.5	.001084

Station	M	M^2	V
y	.7011	.733	783.6
1	.409	.440	470

a - velocity of sound, ft./sec.

p - static pressure, lb./sq.ft.

T - static temperature, deg. R.

M - mach number, V/a .

x - condition before the shock.

y - condition after the shock.

1 - diffuser entrance.

2 - diffuser throat.

3 - diffuser exit.

* - reference state where each number is one.

Knowing the velocity at the entrance of the diffuser, and knowing the volume rate of flow the area of the diffuser entrance can be calculated.

$$V_1 = 0.6 \times V_y = 470 \text{ ft./sec.}$$

$$A_1 = \frac{Q}{V_1} = \frac{951.2}{470} = 2.025 \text{ sq. ft.}$$

$$D_1 = 1.605 \text{ ft.} = 19.25 \text{ in.}$$

$$A_3 = A_1 \times \frac{A_3/A^*}{A_1/A^*} = 2.025 \times \frac{2.0351}{1.563} = 2.635 \text{ sq. ft.}$$

$$D_3 = 1.83 \text{ ft.} = 21.95 \text{ in.}$$

A_3 was calculated from Table 30 of the "Gas Tables", knowing the desired exit mach number, and assuming an isentropic process. This assumption will be corrected later to allow for the fact that the process will not be isentropic. Next, with a contraction ratio of 1.184 between the diffuser entrance and throat, and rounding the entrance lip, the mach number at the throat was found to be 0.51, throat area - 1.71 sq. ft., throat diameter - 17.75 in. A divergence angle of 8 deg. from the throat to the exit was assumed, and the diffuser length determined. The dimensions of the diffuser are now known and the shape is as shown in the accompanying figure.

$$4 = \text{distance from } 0$$

$$3 = \text{distance from } 0$$

$$2 = \text{distance from } 0$$

$$1 = \text{distance from } 0$$

$$0 = \text{distance from } 0$$

$$-1 = \text{distance from } 0$$

$$-2 = \text{distance from } 0$$

$$-3 = \text{distance from } 0$$

$$-4 = \text{distance from } 0$$

$$-5 = \text{distance from } 0$$

$$-6 = \text{distance from } 0$$

$$-7 = \text{distance from } 0$$

$$-8 = \text{distance from } 0$$

$$-9 = \text{distance from } 0$$

$$-10 = \text{distance from } 0$$

$$-11 = \text{distance from } 0$$

$$-12 = \text{distance from } 0$$

$$-13 = \text{distance from } 0$$

$$-14 = \text{distance from } 0$$

$$-15 = \text{distance from } 0$$

$$-16 = \text{distance from } 0$$

$$-17 = \text{distance from } 0$$

$$-18 = \text{distance from } 0$$

$$L = \frac{21.95 - 17.75}{2 \times \sin 4^\circ} = 30.1 \text{ in.}$$

2. Conditions of Internal Flow.

Now that the geometry of the diffuser has been determined, the character of the internal flow can be determined for any given condition of inflow. The volume rate of flow for the design operating condition of the engine has been calculated, and the velocity at the diffuser entrance has been established. The compression or expansion of the flow from the free stream condition to the condition at the diffuser entrance has been assumed to be an isentropic process, except across the shock front when such occurs. The compression of the flow within the diffuser will also be assumed to be isentropic, and when the diffuser losses have been determined, the geometry of the diffuser will be corrected accordingly to allow for variation from the isentropic condition.

The character of the internal flow can be determined from Table 30 of the Gas Tables, and the resulting flow for the design operating condition of a flight Mach number of 1.5 at 40,000 feet altitude is shown in Table I, and Fig. 20.

3. Separation of Laminar Flow.

Since a diffuser in a free stream has a boundary layer of zero thickness at the stagnation point of the

flow, and since the rounded entrance lip has the effect of producing a favorable pressure gradient up to the point of the diffuser throat, the initial boundary layer in the entrance of the diffuser will be laminar. Due to the adverse pressure gradient in the diverging part of the diffuser, however, this laminar boundary layer will separate, there will be a transition zone, and then a turbulent boundary layer will establish itself if the pressure gradient is not too great. The point of separation of the laminar boundary layer can be determined by the method of Ref. 10, previously mentioned.

$$\text{Velocity gradient} = F = \frac{-s_0}{2(1 + f_m)} \frac{dP}{ds}$$

$$s_0 = s_1 + s_2$$

$$s_1 = 0.376 s_m \frac{(P_{sm}/2 - P_{sm})^{-0.164}}{Q_m}$$

$$s_1 = 0.376 \times 1.90 \times \frac{(1134.5 - 1116)}{204} = 1.105 \text{ in.}$$

$$s_2 = 0$$

$$s_0 = 1.105 \text{ in.}$$

$$P_m = -.523$$

$$\frac{dP}{ds} = .0554$$

$$F = -.0041$$

$$\frac{V_m - V_s}{V_s} = .0465 \text{ (From Fig. 81)}$$

$$V_s = 553.9 \text{ ft./sec. at } x/c = .1325$$

They will also be required to show that the function is continuous at the origin. To do this, we must show that $\lim_{(x,y) \rightarrow (0,0)} f(x,y) = f(0,0)$. The function is defined as $f(x,y) = \frac{x^2 + y^2}{x^2 + y^2 + 1}$ for $(x,y) \neq (0,0)$ and $f(0,0) = 0$. We can use the polar coordinate system to evaluate this limit. Let $x = r \cos \theta$ and $y = r \sin \theta$. Then $x^2 + y^2 = r^2$ and the function becomes $f(r, \theta) = \frac{r^2}{r^2 + 1}$. As $(x,y) \rightarrow (0,0)$, $r \rightarrow 0$ and $f(r, \theta) \rightarrow \frac{0}{0+1} = 0$. Therefore, the function is continuous at the origin.

$$\frac{\partial f}{\partial x} = \frac{2x}{x^2 + y^2 + 1} - \frac{2x^2}{(x^2 + y^2 + 1)^2}$$

$$= \frac{2x}{(x^2 + y^2 + 1)^2}$$

$$\frac{\partial f}{\partial y} = \frac{2y}{x^2 + y^2 + 1} - \frac{2y^2}{(x^2 + y^2 + 1)^2}$$

$$= \frac{2y}{(x^2 + y^2 + 1)^2}$$

$$f_x = 0$$

$$f_y = 0$$

$$f_{xx} = -\frac{4x}{(x^2 + y^2 + 1)^3}$$

$$f_{yy} = -\frac{4y}{(x^2 + y^2 + 1)^3}$$

$$f_{xy} = 0$$

$$\Delta^2 f = f_{xx} + f_{yy} = -\frac{4(x^2 + y^2)}{(x^2 + y^2 + 1)^3}$$

$$\Delta^2 f(0,0) = 0$$

k. Mixing Length.

After the separation of the laminar boundary layer, there exists a transition region in which the flow in the boundary layer is neither laminar nor turbulent. Ref. 11 gives this length as:

$$x/c = \frac{70,000}{c} \frac{\nu}{V_s}$$

For the particular condition under investigation separation occurred at $x/c = .1325$ where the following conditions existed:

$$V_s = 553.9 \text{ ft./sec.}$$

$$c = 32.08 \text{ in.}$$

$$\nu = .000297 \text{ ft.}^2/\text{sec.}$$

$$\text{Mixing length} = x/c = .01405$$

This indicates that turbulent flow is established soon after laminar separation at $x/c = .1466$.

5. Separation of the Turbulent Boundary Layer.

The possibility of separation of the turbulent boundary layer was investigated by the method of von Doenhoff and Tetervin described in Ref. 12, and previously discussed. Since it was found that laminar separation would occur very soon after the flow progressed into the region of positive pressure gradient, it was believed that it should be satisfactory to assume that the turbulent boundary was established at the throat

THE THEORY OF THE...

After the separation of the...

$$\frac{1}{2} \frac{d^2 x}{dt^2} + \dots = 0$$

For the particular solution...

$$\begin{aligned} x &= A \cos(\omega t) + B \sin(\omega t) \\ \dot{x} &= -A\omega \sin(\omega t) + B\omega \cos(\omega t) \end{aligned}$$

This indicates that...

THE THEORY OF THE...

The stability of the...

of the diffuser. An initial value of the shape parameter H was assumed as 1.286 because at the throat the pressure gradient would be zero. The initial value of momentum thickness, θ , was computed in the following manner. The boundary layer thickness at the throat was computed, and using the Prandtl - Blasius equation, which was previously given, for the velocity distribution in the boundary layer, the momentum thickness of the boundary layer was computed. This momentum thickness does not change when there is a transition from laminar to turbulent flow in the boundary layer, and so this value is suitable for the initial momentum thickness of the turbulent boundary layer.

$$\delta = 5.2 \sqrt{\frac{\nu x_0}{V}}$$

$$\delta = 5.2 \sqrt{\frac{3.615 \times 10^{-7} \times 1.105}{1.205 \times 10^{-3} \times 581 \times 12}} = .001135 \text{ ft.}$$

$$\frac{v}{V} = 2\left(\frac{y}{\delta}\right) - 2\left(\frac{y}{\delta}\right)^3 + \left(\frac{y}{\delta}\right)^4$$

$$\theta = \int_0^{\delta} \frac{v}{V} \left(1 - \frac{v}{V}\right) dy$$

$$\theta = .118 \delta = .000134 \text{ ft.}$$

$$R_{\theta} = \frac{V\theta}{\nu} = \frac{581 \times .000134}{3 \times 10^{-4}} = 260$$

The initial boundary layer conditions have been established, and the computation for the growth of the turbulent boundary layer is shown in Table II. From the computations it appears that the boundary layer will not separate.

The displacement thickness of the boundary layer at the exit of the diffuser can be determined from the relation between it, the momentum thickness and the shape parameter.

$$\text{Shape parameter} = \frac{\text{displacement thickness}}{\text{momentum thickness}}$$

$$\text{Displacement thickness} = 1.586 \times .00401 = .00635 \text{ ft.}$$

The exit diameter of the diffuser will have to be increased by twice the displacement thickness to allow for the thickness of the boundary layer.

6. Skin Friction.

The skin friction in the diffuser will cause a pressure loss which can be calculated from the following equation which was developed earlier:

$$\ln \frac{p_2^0}{p_1^0} = - \int_0^1 \frac{\tau_0}{2q} \frac{cc}{p^0} d(x/c)$$

The skin friction coefficient was determined as previously explained. The pressure loss equation can be graphically integrated. A plot of the integrand is shown in Fig. 21. The graphical integration yields the following result:

$$p_1^0/p_2^0 = e^{.0025} = 1.0025$$

$$p_1^0 - p_2^0 = 3.33 \text{ lb./sq.ft.}$$

These computations show the loss due to friction to be very small which might have been suspected with such a

The first part of the paper is devoted to the study of the asymptotic behavior of the solutions of the system (1) as $t \rightarrow \infty$. It is shown that the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$ if the matrix A is stable. In the case of a non-stable matrix A , the solutions of (1) are unbounded and tend to infinity as $t \rightarrow \infty$.

2. Asymptotic behavior of the solutions of the system (1)

Let us consider the system (1) with a constant matrix A . The characteristic equation of the matrix A is $\Delta(\lambda) = \det(\lambda I - A) = 0$. The roots of this equation are the eigenvalues of the matrix A . If all the eigenvalues of A have negative real parts, then the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. If at least one eigenvalue of A has a positive real part, then the solutions of (1) are unbounded and tend to infinity as $t \rightarrow \infty$.

3. Asymptotic behavior of the solutions of the system (1) with a time-varying matrix $A(t)$

Let us consider the system (1) with a time-varying matrix $A(t)$. The characteristic equation of the matrix $A(t)$ is $\Delta(\lambda, t) = \det(\lambda I - A(t)) = 0$. The roots of this equation are the eigenvalues of the matrix $A(t)$. If all the eigenvalues of $A(t)$ have negative real parts for all t , then the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. If at least one eigenvalue of $A(t)$ has a positive real part for some t , then the solutions of (1) are unbounded and tend to infinity as $t \rightarrow \infty$.

$$\Delta(\lambda) = \det(\lambda I - A) = 0$$

The asymptotic behavior of the solutions of the system (1) with a time-varying matrix $A(t)$ is determined by the asymptotic behavior of the eigenvalues of the matrix $A(t)$. If all the eigenvalues of $A(t)$ have negative real parts for all t , then the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. If at least one eigenvalue of $A(t)$ has a positive real part for some t , then the solutions of (1) are unbounded and tend to infinity as $t \rightarrow \infty$.

$$\Delta(\lambda, t) = \det(\lambda I - A(t)) = 0$$

$$\Delta(\lambda, t) = \det(\lambda I - A(t)) = 0$$

It is shown that the asymptotic behavior of the solutions of the system (1) with a time-varying matrix $A(t)$ is determined by the asymptotic behavior of the eigenvalues of the matrix $A(t)$. If all the eigenvalues of $A(t)$ have negative real parts for all t , then the solutions of (1) are bounded and tend to zero as $t \rightarrow \infty$. If at least one eigenvalue of $A(t)$ has a positive real part for some t , then the solutions of (1) are unbounded and tend to infinity as $t \rightarrow \infty$.

small L/D ratio as the duct has. Since this was the only loss which could be attributed to the internal flow in the diffuser, the exit area of the diffuser must be increased by a factor of 1.0625 to achieve the desired exit conditions.

We have been able to make estimates of the shock loss, the separation loss and the friction loss in a typical diffuser. For the particular configuration chosen, it was found that the pressure loss across the shock wave was considerable, but was accompanied by a considerable pressure recovery, and speed decrease which facilitated the work of further compression. It was found that separation did not occur for the particular geometric configuration selected, and the expansion loss was non-existent. The loss due to friction was very small because of the short length of diffuser required. Further frictional losses in the ducting between the exit of the diffuser and the compressor entrance are shown in Fig. 22.

The method of obtaining the pressure loss due to friction in the length of constant area duct between the diffuser exit and the entrance to the compressor was the following:

Conditions at diffuser exit.

$$V = 3\frac{1}{8} \text{ ft./sec.} \quad q = 79.2 \text{ lb./sq.ft.}$$

$$\rho = 1.310 \times 10^{-3} \text{ slugs/ft.}^3$$

$$\mu = 3.71 \times 10^{-7} \text{ lb.sec./ft.}^2$$

D (uncorrected) - 1.83 ft.

Boundary layer displacement thickness - .00635 ft.

D (corrected) - $(1.83 + (2 \times .00635)) \times (1.0025)^{1/2} =$
1.843 ft.

Reynolds number - 2.27×10^6

The friction factor, f , for the length of ducting was obtained from the Moody equation which is:

$$f = .0055 \left(1 + \left(20,000 \frac{\epsilon}{D} + \frac{10^6}{Re} \right)^{1/3} \right)$$

$$\epsilon = .00015 \text{ ft.}$$

$$f = .0125$$

$$\Delta p = f q L/D = .99 L/D \text{ lb./sq.ft.}$$

If we assume an exit length equal to three times the exit diameter which should assure complete pressure recovery, then we can make an estimate of the pressure recovery ratio of the diffuser under investigation.

Total pressure loss due to the shock wave.

$$p_0 = 391.9 \text{ lb./sq.ft.}$$

$$p_0^0 = 1437 \text{ lb./sq.ft.}$$

$$p_y^0/p_x^0 = .930$$

$$p_x^0 - p_y^0 = 100.5 \text{ lb./sq.ft.}$$

Total pressure loss due to friction in the diffuser.

$$\Delta p^0 = 3.33 \text{ lb./sq.ft.}$$

Total pressure loss due to friction in the constant area duct following the diffuser.

Let $\alpha = \sqrt{2} + \sqrt{3}$

Find the minimal polynomial of α over \mathbb{Q} .

Let $\alpha = \sqrt{2} + \sqrt{3}$. Then $\alpha - \sqrt{2} = \sqrt{3}$ and squaring both sides gives

$$\alpha^2 - 2\alpha\sqrt{2} + 2 = 3$$

$$\alpha^2 - 2\alpha\sqrt{2} - 1 = 0$$

Thus $\alpha^2 - 1 = 2\alpha\sqrt{2}$. Squaring both sides again gives

$$(\alpha^2 - 1)^2 = 8\alpha^2$$

$$\alpha^4 - 2\alpha^2 + 1 = 8\alpha^2$$

$$\alpha^4 - 10\alpha^2 + 1 = 0$$

$$f(x) = x^4 - 10x^2 + 1$$

$$\Delta = 4^3 - 4^2 \cdot 10 \cdot 1 = 4(4 - 10) = -24$$

Since $\Delta < 0$, $f(x)$ has no rational roots.

By the Rational Root Theorem, any rational root of $f(x)$ must be of the form $\pm \frac{p}{q}$ where p divides 1 and q divides 1.

Thus the only possible rational roots are ± 1 .

Since $f(1) = 1 - 10 + 1 = -8 \neq 0$ and $f(-1) = 1 - 10 + 1 = -8 \neq 0$,

$f(x)$ has no rational roots and is irreducible over \mathbb{Q} .

$$f(x) = x^4 - 10x^2 + 1$$

$$f(x) = (x^2 - 2\sqrt{2}x + 1)(x^2 + 2\sqrt{2}x + 1)$$

$$f(x) = (x^2 - 2\sqrt{2}x + 1)(x^2 + 2\sqrt{2}x + 1)$$

$$f(x) = (x^2 - 2\sqrt{2}x + 1)(x^2 + 2\sqrt{2}x + 1)$$

Thus the minimal polynomial of α over \mathbb{Q} is $x^4 - 10x^2 + 1$.

$$f(x) = x^4 - 10x^2 + 1$$

Since $f(x)$ is irreducible over \mathbb{Q} , it is the minimal polynomial of α .

Thus the minimal polynomial of α over \mathbb{Q} is $x^4 - 10x^2 + 1$.

$$\Delta p = 2.97 \text{ lb./sq.ft.}$$

$$\frac{\Delta p}{p} \sim \frac{\Delta p^0}{p^0} \text{ (at low subsonic Mach numbers.)}$$

$$\Delta p^0 = 3.17 \text{ lb./sq.ft.}$$

$$p_2^0 = 1437 - 100.7 - 3.33 - 3.17 = 1330 \text{ lb./sq.ft.}$$

$$\text{Ram recovery ratio} = \frac{p_2^0 - p_0}{p_0 - p_0} = \frac{1330 - 391.9}{1437 - 391.9} =$$

.898

It appears that the ram recovery ratio of the chosen diffuser configuration is fairly high, and that the principal pressure loss occurs through the shock wave. No attempt was made to assess entrance loss, yawing loss, turning loss, loss due to obstructions, exit loss or leakage loss because these are factors which can be minimized with proper design. It would appear from this analysis that ram recovery ratio can be kept to a reasonable value even through a normal shock precede^{ing} the entrance of the flow into the diffuser.

Fig. 23 shows the variation of velocity ratio with flight mach number. As is to be expected, velocity ratio decreases with increasing flight mach number up to the sonic velocity. Due to a shock occurring in the flow ahead of the diffuser, velocity ratio increases with increasing supersonic flight velocities since the strength of the shock and the velocity decrease across

$$\Delta \approx 2.7 \times 10^{-10} \text{ s}$$

$$\frac{\Delta}{\tau} \approx \frac{2.7 \times 10^{-10}}{1.5 \times 10^{-8}} \approx 0.018$$

$$\Delta \approx 2.7 \times 10^{-10} \text{ s}$$

$$\Delta \approx 2.7 \times 10^{-10} \text{ s}$$

$$\frac{\Delta}{\tau} \approx \frac{2.7 \times 10^{-10}}{1.5 \times 10^{-8}} \approx 0.018$$

etc.

It appears that the two values of the time
 interval distribution in fairly close and that the
 first values are about 10% of the total
 always are also in some other cases. This
 means that the first values are about 10%
 of the total values. It would seem that
 the first values are about 10% of the total
 values. It would seem that the first values
 are about 10% of the total values.

pmi

of the two values of the time interval

It is seen that the two values of the time
 interval distribution are in fairly close and
 that the first values are about 10% of the
 total values. It would seem that the first
 values are about 10% of the total values.
 It would seem that the first values are
 about 10% of the total values. It would
 seem that the first values are about 10%
 of the total values. It would seem that
 the first values are about 10% of the
 total values. It would seem that the first
 values are about 10% of the total values.

the shock increase with increasing Mach number. Velocity ratio increases with altitude as flight Mach number increases because of the variation of Mach number with temperature. Temperature decreases with altitude, sonic velocity decreases, and a lesser flight velocity gives the same Mach number.

Fig. 24 shows the increase of density ratio with flight Mach number. This ratio is also a measure of the mass flow through the engine. The entrance area and entrance velocity are fixed. The former is fixed due to diffuser design; the latter due to the engine speed and permissible volume flow. The mass flow through the engine, therefore, with a fixed engine speed varies directly with the flow density at the diffuser entrance. Entrance density increases with flight Mach number because of the recovery of ram pressure ahead of the diffuser entrance. The reduction in entrance density with increasing altitude is due to the reduced ambient air density at altitude.

The first section of the document is devoted to a general introduction of the subject. It discusses the importance of the study and the scope of the work. The second section deals with the methodology used in the research. It describes the data sources, the sampling technique, and the statistical methods employed. The third section presents the results of the study. It includes a detailed analysis of the data and a discussion of the findings. The final section concludes the report and offers some suggestions for further research.

The first part of the report is a general introduction to the subject. It discusses the importance of the study and the scope of the work. The second part deals with the methodology used in the research. It describes the data sources, the sampling technique, and the statistical methods employed. The third part presents the results of the study. It includes a detailed analysis of the data and a discussion of the findings. The final part concludes the report and offers some suggestions for further research.

The first part of the report is a general introduction to the subject. It discusses the importance of the study and the scope of the work. The second part deals with the methodology used in the research. It describes the data sources, the sampling technique, and the statistical methods employed. The third part presents the results of the study. It includes a detailed analysis of the data and a discussion of the findings. The final part concludes the report and offers some suggestions for further research.

CHAPTER VI

PRESENT AIR INLET DESIGN FEATURES

Whereas a few short years ago the idea of driving an aircraft with anything except a propeller would have been scoffed at, now dozens of practical jet propelled bombers and fighter planes are available. A survey of the field will reveal a wide variation of entrance duct designs, and air inlet locations. It must be remembered, however, that the majority of these airplanes were designed for subsonic speeds, although several experimental designs for transonic and supersonic flight are also available.

Designs which feature fuselage engine installations are confined to fighter types. The air entrance duct locations vary with the different designs. Examples of the nose inlet ducts are the Republic P-84, the North American P-86, the Republic XP-91, and the McDonnell XP-85. One thing common to all these models is an axial flow turbojet engine.

The P-84 had serious duct trouble in its development. The inlet duct is divided into two rectangular ducts aft of the circular nose inlet. The ducts extend along the side of the fuselage to a Y inlet assembly at the face of the engine. The ducts are fifteen feet long and considerable leakage occurred in the early

CHAPTER II

THE HISTORY OF THE UNITED STATES

The history of the United States is a story of growth and expansion. It begins with the first European settlers in the early 17th century, who established colonies along the Atlantic coast. These colonies were founded for various reasons, including the search for new lands, economic opportunities, and religious freedom. Over time, the colonies grew in number and size, and they began to assert their independence from British rule. The American Revolution, which began in 1775, was a result of the growing tensions between the colonies and the British government. The revolution led to the signing of the Declaration of Independence in 1776, and the establishment of the United States as a new nation. The early years of the United States were marked by westward expansion, as settlers moved into the interior of the continent. This expansion was driven by the desire for land, resources, and new markets. The Louisiana Purchase of 1803 was a major event in this process, as it doubled the size of the United States. The 19th century was a period of rapid growth and change for the United States. The Industrial Revolution brought new technologies and methods of production, which led to a significant increase in the country's economic power. At the same time, the United States was engaged in a series of wars, including the Mexican-American War and the Civil War. The Civil War, which lasted from 1861 to 1865, was a defining moment in the nation's history, as it resolved the issue of slavery and preserved the Union. The late 19th and early 20th centuries were characterized by the rise of the United States as a world power. The country's economic strength and military capabilities grew, and it became a major player in international affairs. The United States played a key role in the Spanish-American War of 1898, which resulted in the acquisition of territories such as Puerto Rico, Guam, and the Philippines. The 20th century has been a period of continued growth and change for the United States. The country has experienced significant technological advances, particularly in the fields of science and industry. At the same time, it has faced a series of challenges, including the Great Depression, World War II, and the Cold War. The United States emerged from World War II as a superpower, and it played a leading role in the formation of the United Nations and the North Atlantic Treaty Organization (NATO). The 1960s and 1970s were a period of social and political upheaval in the United States, as the country grappled with issues such as the Vietnam War, the civil rights movement, and the energy crisis. The 1980s and 1990s were a period of economic growth and technological innovation, as the United States became a global leader in the information technology industry. The 21st century has been a period of continued growth and change for the United States, as the country has faced a series of challenges, including the 9/11 attacks, the global financial crisis, and the rise of China as a major power. The United States remains a leading nation in the world, and its history continues to shape the present and the future.

models. Losses in the F duct were reduced by the use of sealing compound and a decrease in fastener spacing. To clear the pressurized portion of the fuselage the ducts extend down along the side and then rise upward. To eliminate losses due to duct bends, the engine was tipped down four degrees to permit a straight connection with the air inlet ducts. This requires a similar four degree bend aft of the engine at the tail cone splice. Auxiliary air inlets near the compressor inlet for low speed flight were considered, but the complexity outweighed the thrust saving which would have amounted to four per cent gain in static thrust. Present development of an improved model of the F-36 envisages a flush type air inlet instead of the stagnation point inlet

The F-36, present holder of the world's air speed record, differs from the F-34 in that the air entrance duct is not divided but passes directly rearward to the compressor inlet. The cockpit floor is located above the air duct. The nose air inlet features an extended upper lip to furnish adequate air to the engine at high angles of attack. The latest version of the F-36, the XF-33, will feature flush type air inlets.

The XF-91, a new high speed, high altitude interceptor reputed to be capable of supersonic speed, has a divided air inlet duct with a four to five foot sting projecting out of it. It is not known if this sting is to function as an Oswatitch type diffuser (Ref. 7) or not.

The XP-35, the parasite fighter, features an annular type nose air inlet. The air inlet duct leads directly to the face of the compressor of the Westinghouse J-34 axial flow turbojet.

Examples of fighter designs employing wing-fuselage junction air inlets to engines installed in the fuselage are the Chance-Vought XP63 and the P70, the Grumman F9F, the McDonnell XP-38, and the following British designs, the Hawker H. 7/46 and Gloster H. 1/44. Both axial flow and centrifugal flow type engines are represented in these airplanes.

The XP63 has semi-circular shaped air inlets, the semi-circles projecting below the wing. No information seems to be available on this configuration which is unique, but the change in the orientation of the duct entrance on the P70 would indicate that the first installation was not entirely satisfactory. Semi-circular shaped entrance ducts are also used on the P70, but the semi-circle now appears as a scoop extending out of the fuselage. To improve the velocity distribution across the face of the air inlet, a boundary layer suction slot is provided adjacent to the fuselage. Information about the duct problems with these aircraft is not available, but some information on the design principles can be gleaned from Ref. 22 which was written by a member of the Chance Vought engineering staff. In this reference the author recommends a velocity ratio of 0.7 at the

The first of these is the fact that the...
 the second is the fact that the...
 the third is the fact that the...
 the fourth is the fact that the...
 the fifth is the fact that the...
 the sixth is the fact that the...
 the seventh is the fact that the...
 the eighth is the fact that the...
 the ninth is the fact that the...
 the tenth is the fact that the...
 the eleventh is the fact that the...
 the twelfth is the fact that the...
 the thirteenth is the fact that the...
 the fourteenth is the fact that the...
 the fifteenth is the fact that the...
 the sixteenth is the fact that the...
 the seventeenth is the fact that the...
 the eighteenth is the fact that the...
 the nineteenth is the fact that the...
 the twentieth is the fact that the...

maximum speed flight condition with a flow velocity at the compressor inlet of about 200 miles per hour. A good duct six feet long, with a gentle curvature of five to ten degrees gives about a one per cent total pressure loss, equivalent to a 1.7 - 2.0 per cent loss in thrust. An S-shaped duct with two gentle bends having a total curvature of sixty degrees gives a three to four per cent total pressure loss corresponding to a five to eight per cent loss in thrust. The air entrance duct configuration of the P70 and the Gloster W.1/44 are very similar, semi-circular in shape with a boundary layer bleed next to the fuselage. Internally some difference must exist since the P70 has two J-34 engines while the W. 1/44 has a single Rolls-Royce "Vene".

The P9F, the XF-33 and the Hawker W. 7/46 have triangular shaped air entrance ducts with the base of the triangle adjacent to the fuselage. Whether boundary layer suction slots are used at the fuselage is not evident from pictures of the installations. The air inlet of the P9F is normal to the direction of flow. The air inlets of the XF-33 and the W.7/46 have an angularity in plan view. The upper lip of the W.7/46 also extends beyond the lower lip. McDonnell must have solved the problem of lateral flow across the face of the duct which caused velocity distribution problems on a similar configuration in the XP-1. On the P-1 of which the XP-1 was a prototype the orientation of the

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

... ..

face of the duct entrance was changed to be normal to the air flow direction. The P-3F features four auxiliary blower doors opening directly into the plenum chamber for low speed and ground operation of the engine. The ducting of the P.7/46 is unique in that having two air intakes in the wing root, it also has two exhaust outlets in the wing trailing edge at the fuselage. A single engine is located in the fuselage. The Hawker air inlet design must have proven satisfactory because it is retained on the new Hawker P.1052.

Fighters having ^{ing} scoop type air entrance ducts to engine installations in the fuselage are the Lockheed P-30, TP-300 and XP-90, the Northrop XP-89, and the Vickers-Armstrong "Attacker". The air inlet ducts of the P-30 and TP-300 are nostril shaped on either side of the fuselage ahead of the wing root. Ref. 23 gives an explanation of the choice of entrance duct location and reveals some of the problems encountered with this design. It was found that unstable duct flow resulted at low flow ratios due to flow breakdown and boundary layer separation. The flow separation gave a loud duct "rumble" which could be heard for miles. Directional "snaking" of the aircraft could also be traced to this source. During ground operation flow reversal occurred in the ducts, flow coming in the duct on one side and out the duct on the opposite side. Introduction of a boundary layer bleed at the duct entrances cured the

difficulties at a cost of two to three miles per hour in airspeed. The final result was a net run at high speed equal to seventy per cent of the available adiabatic compression ratio. Spring loaded doors behind the pilot supply air to the compressor at low speeds and for ground operation.

The XF-90 was originally reported to have a flush type air inlet duct, but pictures show ducts similar to those employed on the F-30. The XF-90, however, has two axial flow turbojets in the fuselage whereas the F-30 had one centrifugal flow engine. The XF-89 has two engines slung semi-externally from the lower part of the fuselage. Semi-circular air inlet ducts lead directly to the two J-35 engines. It would seem that a uniform flow at the compressor entrance would be difficult with this design. The "Attacker" has air inlet ducts in the shape of circular arcs, less than semi-circles. The inlets project from the fuselage forward of the wing. Boundary layer slots are located adjacent to the fuselage at the duct entrances. The flow through the boundary layer slots exhausts through louvred openings in the fuselage skin aft of the duct entrance. The main air ducts follow aft on both sides of the fuselage and dump into a plenum chamber at the forward face of the engine. An auxiliary air intake on top of the fuselage provides air to the engine for ground operation.

Dividing it into 100 parts, we find that the number of parts is 100. The total number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100.

The total number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100.

The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100.

The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100.

The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100. The number of parts is 100.

Three fighter designs which have engine installations in the wings are the McDonnell F8U-1, and F2U-1 and the Curtiss P-57. The McDonnell models are similar in appearance with similar engine installations and air inlet ducts. The F8U-1 is equipped with two Westinghouse 19XB axial flow jet engines; the F2U-1 is equipped with two J-34 engines. The engines are located in the wing roots and a triangular shaped air inlet is used. It is claimed that this configuration gives constant velocity distribution across the inlet face, and the ram pressure recovery is 99 per cent of that available. The design is said to be free from internal flow separation at any velocity ratio to be expected in normal operation. Due to the fact that the upper and lower portions of the powerplant section act as two thin airfoils, the critical Mach number of the wing root is higher than that of the outer wing panel. To cool the powerplant section and bleed off the boundary layer adjacent to the fuselage, a boundary layer suction slot is provided at the air inlet. The air from the suction slot flows through the necessary compartment and thence into the air stream. A reverse flow through the boundary layer suction slot occurs in ground operation, but no adverse effects are noticed with this flow reversal.

The P-57 is powered by four J-34 engines. The engines are installed in nacelles in the wings, two engines to each nacelle. The engine nacelles are about

There is a large number of cases in which the

cases in the state are not reported, and the

and the number of cases in the state are not

in accordance with the number of cases in the

state, and the number of cases in the state

is not in accordance with the number of cases

in the state. The number of cases in the

state is not in accordance with the number of

cases in the state, and the number of cases

in the state is not in accordance with the

number of cases in the state. The number of

cases in the state is not in accordance with

the number of cases in the state, and the

number of cases in the state is not in

accordance with the number of cases in the

state, and the number of cases in the state

is not in accordance with the number of cases

in the state. The number of cases in the

state is not in accordance with the number of

cases in the state, and the number of cases

in the state is not in accordance with the

number of cases in the state. The number of

cases in the state is not in accordance with

the number of cases in the state, and the

number of cases in the state is not in

accordance with the number of cases in the

state, and the number of cases in the state

ten feet long so that the air entrance duct must necessarily be short. A single rectangular shaped air inlet provides air to the two engines in each nacelle, the flow dividing just aft of the entrance. The air intake ducts are protected to prevent icing or water entering during heavy rain. The extent or nature of this protection was not made known.

The bomber types almost all have engines installed in the wings, or attached to the wings. The air inlets, therefore, are of the stagnation point type. Representative installations are those on the Consolidated XB-46, Boeing XB-47, Martin XB-48 and the Northrop YB-49. The XB-46 has four engines contained in two engine nacelles slung below the wing. One elliptical air inlet provides flow to both engines in the same nacelle. The air inlet duct is divided just aft of the entrance. The XB-47 holds the transcontinental flight record, crossing the U.S. in 3 hours and 46 minutes and averaging 607.2 miles per hour. It has six engines supported by pylons extending down from the wing, two engines mounted on each of the inboard pylons and one engine on each of the outboard pylons. The air inlet ducts are annular, one for each engine. On the inboard pylons where the engines are located adjacent to each other, the segments of the outer cones common to both engines extend further forward than the remainder of the inlet rim to prevent interaction of the individual flows to

The first part of the report is devoted to a general survey of the situation in the country. It is found that the economy is in a state of depression, and that the government is unable to meet its obligations. The report then proceeds to a detailed analysis of the various causes of the economic crisis, and suggests several measures which might be adopted to bring about a recovery. It is pointed out that the most important of these measures is the re-organization of the public services, and that this should be done as a matter of priority. The report also discusses the need for a more efficient system of taxation, and for a more liberal policy towards foreign trade. It concludes by stating that the success of these measures will depend on the co-operation of the government and the people, and that it is essential that the government should be able to carry out its policy without any undue delay.

each engine. The B-47 also has six engines, three on each wing in a common nacelle. The air entrance ducts to each engine are annular in form, and tunnels through the nacelle are provided between adjacent engines to keep the critical Mach number over the wings as high as possible. The YB-49 has four engines located side by side in each wing. The air inlet to the engines is located in the wing leading edge. The air inlet is wide and narrow with internal partitions to divide the flow to each engine.

The Martin P4M-1 is an example of a hybrid installation. Its main motive power is two reciprocating engines with two jet engines for additional power when needed. One reciprocating engine and one jet engine are mounted in a common nacelle projecting below the wing. When the jet engine is in operation air is provided through a scoop which opens forward and down from the nacelle. When the jet engine is not operating the scoop retracts and its bottom provides the lower forward face of the nacelle. Since the top speed of the P4M-1 is not very high, ram recovery is not a serious problem and careful duct design is not critical.

The experimental planes designed to investigate flight at or near the sonic velocity are not unlike the latest fighter designs. The Douglas D553-I designed for high subsonic velocities features a circular nose inlet with the ducting dividing just aft of the inlet.

The first part of the report is devoted to a description of the work done during the period covered by this report. It is divided into three main sections: a general survey of the work done, a description of the work done in the various departments, and a description of the work done in the various sections of the departments.

The second part of the report is devoted to a description of the work done during the period covered by this report. It is divided into three main sections: a general survey of the work done, a description of the work done in the various departments, and a description of the work done in the various sections of the departments.

The third part of the report is devoted to a description of the work done during the period covered by this report. It is divided into three main sections: a general survey of the work done, a description of the work done in the various departments, and a description of the work done in the various sections of the departments.

The split duct rejoins just forward of the J-33 jet engine. The ducting and air inlet are similar to the installation on the F-84.

The Douglas D558-II, a combination rocket and turbojet powered airplane, is designed for supersonic speeds. It features two flush air inlets on either side of the lower, forward fuselage. Few details on these air inlets are available. NACA was responsible for the design. Pictures show nothing projecting beyond the contour of the fuselage.

The Consolidated 7002 research plane, powered by a J-33 engine, has a circular air inlet in the nose of the fuselage. A sting projects forward out of the center of the air inlet. It is reported that this sting is an Oswatitsch type diffuser (Ref. 7). Further details on the air inlet ducting are not available.

The Northrop X-4, designed to investigate the transonic speed range, Mach numbers 0.8 - 1.2, is powered by two Westinghouse 19XB engines installed at the wing-fuselage junction. Scoop type air inlet ducts supply the engine air. The shape of the duct entrances is not unlike that of the F-80.

The Armstrong-Whitworth 52, a British design to test the potentialities of the flying wing, is powered by two Rolls-Royce "Went" engines, located in separate nacelles projecting below the wing. The air inlet duct entrance to each is elliptical with an overhanging upper

The first part of the report deals with the general situation of the country and the progress of the work done during the year.

The second part of the report deals with the work done during the year.

The third part of the report deals with the work done during the year.

The fourth part of the report deals with the work done during the year.

The fifth part of the report deals with the work done during the year.

The sixth part of the report deals with the work done during the year.

The seventh part of the report deals with the work done during the year.

The eighth part of the report deals with the work done during the year.

The ninth part of the report deals with the work done during the year.

The tenth part of the report deals with the work done during the year.

The eleventh part of the report deals with the work done during the year.

The twelfth part of the report deals with the work done during the year.

The thirteenth part of the report deals with the work done during the year.

The fourteenth part of the report deals with the work done during the year.

The fifteenth part of the report deals with the work done during the year.

The sixteenth part of the report deals with the work done during the year.

The seventeenth part of the report deals with the work done during the year.

The eighteenth part of the report deals with the work done during the year.

The nineteenth part of the report deals with the work done during the year.

The twentieth part of the report deals with the work done during the year.

The twenty-first part of the report deals with the work done during the year.

The twenty-second part of the report deals with the work done during the year.

The twenty-third part of the report deals with the work done during the year.

The twenty-fourth part of the report deals with the work done during the year.

The twenty-fifth part of the report deals with the work done during the year.

The twenty-sixth part of the report deals with the work done during the year.

The twenty-seventh part of the report deals with the work done during the year.

The twenty-eighth part of the report deals with the work done during the year.

lip. A novel feature of the air inlet ducting is the auxiliary source of air at low speeds. A boundary layer suction slot on the wing near the tip at the fifty per cent chord point supplies air directly to the plenum chamber at low speed flight. This serves a dual purpose. In addition to supplying additional air to the engine, it delays wing tip stall. It would seem that such a system would have great possibility.

This resume of the types and locations of engine air inlet ducts on some representative modern airplanes reveals the variations in design which have been successful in the past. The trend in experimental aircraft is just as varied. The results of flights with the experimental aircraft may show that one type of installation is superior to another, but more than likely it will only show that the final design must still be a compromise.

CHAPTER VII

CONCLUSIONS AND RECOMMENDATIONS

In this report an attempt has been made to investigate analytically the performance of a diffuser for use in a turbo-jet engine at transonic flight speeds. The factors which detract from diffuser performance have been explored, and means to minimize these losses have been discussed. Convenient methods of determining the magnitude of these losses analytically have been suggested, but final corroboration of these methods will depend upon future experimental verification.

It was found that the internal diffuser flow was not affected greatly by the presence of a shock wave ahead of the diffuser entrance. With such a situation, the internal flow in the diffuser was not materially different from that resulting at subsonic flight speeds. The losses encountered across such a shock wave were not found to penalize the diffuser performance greatly at flight mach numbers below 1.5. Of course, the validity of these findings, and the advisability of allowing a detached shock to form ahead of the diffuser entrance are open to question.

It is believed that the key to the advisability of utilizing a shock ahead of the diffuser entrance to assist in ram pressure recovery, lies in the extent of

THE HISTORY OF THE UNITED STATES

The history of the United States is a story of growth and expansion. It begins with the first European settlers in the early 17th century, who established colonies along the Atlantic coast. These colonies grew and developed, and by the mid-18th century, the United States had become a major power in the world. The American Revolution (1775-1783) was a turning point in the nation's history, as it led to the birth of a new, independent nation. The Constitution of 1787 established a federal government, and the United States continued to expand westward. The Civil War (1861-1865) was a major conflict that resulted in the abolition of slavery and the preservation of the Union. The Reconstruction era (1865-1877) followed, as the nation sought to rebuild and reunite. The late 19th and early 20th centuries saw the United States emerge as a global superpower, with the Spanish-American War (1898) and the acquisition of territories like Hawaii and the Philippines. The Progressive Era (1890s-1920s) brought significant social and political reforms. The Great Depression (1930s) and World War II (1941-1945) were major challenges, but the United States emerged as a dominant world power. The Cold War (1947-1991) was a period of tension between the United States and the Soviet Union. The end of the Cold War and the beginning of the 21st century have seen the United States continue to play a leading role in global affairs.

the influence of this shock on the drag of the airplane. It is also believed that the drag of the airplane will be affected by the velocity ratio of the airflow entering the diffuser. The limits of velocity ratio, particularly the lower limit, found suitable for subsonic flight will not necessarily be satisfactory for supersonic flight. Experimental investigation of this problem is warranted. It may be found that the lower limit of allowable velocity ratio is raised so high that it complicates the internal flow of the diffuser.

Other problems which are associated with the detached shock wave, and which should be investigated experimentally are the location of the shock wave ahead of the diffuser entrance, and the persistence of turbulence induced in the flow by the shock wave. The location of the shock wave is of interest primarily in that it might explain the limits of permissible velocity ratios, and might be a measure of the shock induced turbulence entering the diffuser. The persistence of the shock induced turbulence is of interest because it will have great influence on the internal diffuser flow if it persists beyond the throat of the diffuser. This shock induced turbulence if it is transmitted to the boundary layer in the region of positive pressure gradient will limit the rate of pressure recovery, or may cause internal flow separation.

Two dimensional effects at the entrance and exit of the diffuser section are not explained clearly in any of the literature dealing with flow in a diffuser, although hints are given in Refs. 3 and 21 when it is suggested that extra lengths of constant area ducting following the diverging section are necessary for complete pressure recovery. It would be interesting to investigate experimentally the velocity profile across the face of the diffuser at various velocity ratios, for both subsonic and supersonic flows. The velocity profile at the diffuser exit would be of even greater interest, particularly its variation with diffuser length and divergence angle, and the effect of suction slots and induced rotation on the velocity profile. This latter effect, induced flow rotation, is not mentioned in any of the literature on diffuser flow encountered to date. The advantages of a flow with rotation are set forth in Ref. 3. With rotating flow in a diffuser, separation is delayed and more complete pressure recovery is obtained in the diffuser proper. Since the diffuser exhausts to the compressor, a rotating machine, it is reasonable to believe that rotation of flow in the diffuser will be induced by the compressor rotation. The strength of the rotation and the region of flow affected would be useful design information.

Finally, the development of the boundary layer in a diffuser is worthy of investigation. The method of

The second part of the document is

the first part of the document is

the second part of the document is

the third part of the document is

the fourth part of the document is

the fifth part of the document is

the sixth part of the document is

the seventh part of the document is

the eighth part of the document is

the ninth part of the document is

the tenth part of the document is

the eleventh part of the document is

the twelfth part of the document is

the thirteenth part of the document is

the fourteenth part of the document is

the fifteenth part of the document is

the sixteenth part of the document is

the seventeenth part of the document is

the eighteenth part of the document is

the nineteenth part of the document is

the twentieth part of the document is

the twenty-first part of the document is

the twenty-second part of the document is

the twenty-third part of the document is

the twenty-fourth part of the document is

the twenty-fifth part of the document is

the twenty-sixth part of the document is

the twenty-seventh part of the document is

analysis suggested in Ref. 12 is not strictly applicable to flow in a duct, and it also entails considerable computation. An experimental investigation involving variation of rates of pressure recovery and diffuser lengths, with necessary corrections for variation of the Reynolds number, could speed the problem of diffuser analysis and fill a gap in the study of diffuser performance. Past investigations of permissible diffuser divergence angles have neglected the effect of diffuser length, and have been conducted at area ratios much higher than those necessary for a turbo-jet engine air inlet duct.

It is not felt that these suggestions for future investigation exhaust the possibilities for diffuser research. It is believed that they include the more immediately important items, those topics neglected in the past which may influence diffuser performance at transonic speeds. Other subjects, equally interesting, will probably be suggested by discussions in the body of the report. Undoubtedly, ideas on diffuser performance and analysis different from those included in this report will arise, and errors in reasoning may be found, but if this report stimulates thought on diffuser problems, then it has fulfilled its purpose.

THESE RESULTS ARE IN ACCORD WITH THE THEORY OF THE

RELATIONSHIP BETWEEN THE TWO VARIABLES.

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

THE RESULTS OF THE EXPERIMENT ARE AS FOLLOWS:

APPENDIX I

SYMBOLS

- a - speed of sound.
- A - cross-sectional area.
- c_p - specific heat at constant pressure.
- c_v - specific heat at constant volume.
- M - Mach number, V/a .
- n - exponent for a polytropic process, $p v^n =$
constant.
- p - static pressure.
- p^0 - total pressure
- q - dynamic pressure, $\frac{1}{2} \rho V^2$.
- R - gas constant, 1545/molecular weight.
- dS - change in entropy.
- T - static temperature.
- T^0 - total temperature.
- V - velocity.
- γ - ratio of specific heats.
- η_0 - diffuser efficiency.
- $1+n$ - compressibility factor.
- μ - coefficient of viscosity.
- ν - kinematic viscosity, μ/ρ .
- ρ - density.

Where symbols other than the above are used in the text, they are defined where used.

THE UNIVERSITY OF CHICAGO

PHYSICS DEPARTMENT

1 - ...
 2 - ...
 3 - ...
 4 - ...
 5 - ...
 6 - ...
 7 - ...
 8 - ...
 9 - ...
 10 - ...
 11 - ...
 12 - ...
 13 - ...
 14 - ...
 15 - ...
 16 - ...
 17 - ...
 18 - ...
 19 - ...
 20 - ...
 21 - ...
 22 - ...
 23 - ...
 24 - ...
 25 - ...
 26 - ...
 27 - ...
 28 - ...
 29 - ...
 30 - ...
 31 - ...
 32 - ...
 33 - ...
 34 - ...
 35 - ...
 36 - ...
 37 - ...
 38 - ...
 39 - ...
 40 - ...
 41 - ...
 42 - ...
 43 - ...
 44 - ...
 45 - ...
 46 - ...
 47 - ...
 48 - ...
 49 - ...
 50 - ...
 51 - ...
 52 - ...
 53 - ...
 54 - ...
 55 - ...
 56 - ...
 57 - ...
 58 - ...
 59 - ...
 60 - ...
 61 - ...
 62 - ...
 63 - ...
 64 - ...
 65 - ...
 66 - ...
 67 - ...
 68 - ...
 69 - ...
 70 - ...
 71 - ...
 72 - ...
 73 - ...
 74 - ...
 75 - ...
 76 - ...
 77 - ...
 78 - ...
 79 - ...
 80 - ...
 81 - ...
 82 - ...
 83 - ...
 84 - ...
 85 - ...
 86 - ...
 87 - ...
 88 - ...
 89 - ...
 90 - ...
 91 - ...
 92 - ...
 93 - ...
 94 - ...
 95 - ...
 96 - ...
 97 - ...
 98 - ...
 99 - ...
 100 - ...

REFERENCES

1. Hanson, Frederick H., Jr. and Wossman, Ernest A.: Effect of Pressure Recovery on the Performance of a Jet Propelled Airplane. NACA TN No. 1695, September, 1948.
2. Leipmann, H. W., and Puckett, A. S.: Introduction to the Aerodynamics of a Compressible Fluid. Third Printing, 1948. John Wiley and Sons, New York.
3. Patterson, G. W.: Modern Diffuser Design. Aircraft Engineering, Vol. 19, September 1933.
4. Zucrow, W. J.: Principles of Jet Propulsion and Gas Turbines. 1948. John Wiley and Sons, New York.
5. Kenan, J. H., and Kaye, J.: Gas Tables. 1948. John Wiley and Sons, New York.
6. Fantrowitz, A., and Donaldson, C. duP.: Preliminary Investigations of Supersonic Diffusers. NACA ACR L5D20, May 1945.
7. Oswatitsch, K.: Pressure Recovery for Missiles with Reaction Propulsion at High Supersonic Speeds. NACA TN No. 1140, June 1947.
8. Cox, G. W. and Germano, F. J.: Fluid Mechanics. Third printing, 1946. D. van Nostrand and Company, New York.
9. Dryden, H. L.: Some Recent Contributions to the Study of Transition and Turbulent Boundary Layers, NACA TN No. 1163, April 1947.
10. von Doenhoff, A. W.: A Method of Rapidly Estimating the Position of the Laminar Separation Point. NACA TN No. 671, October 1933.
11. von Doenhoff, A. W.: A Preliminary Investigation of Boundary Layer Transition along a Flat Plate with Adverse Pressure Gradient. NACA TN No. 639, 1933.
12. von Doenhoff, A. W., and Tetervin, S.: Determination of General Relations for the Behavior of Turbulent Boundary Layers. NACA TN No. 772, 1943.

CONTENTS

1. Introduction
2. The first part of the work
3. The second part of the work
4. The third part of the work
5. The fourth part of the work
6. The fifth part of the work
7. The sixth part of the work
8. The seventh part of the work
9. The eighth part of the work
10. The ninth part of the work
11. The tenth part of the work
12. The eleventh part of the work
13. The twelfth part of the work

13. Bodge, R. A. and Thompson, W. J.: Fluid Mechanics. 1937. First Edition, McGraw-Hill Book Co., New York.
14. Squire, H. B.: A Note on Boundary Layer Flow. British A.R.C., R. & M. No. 1664.
15. Garner, H. C.: The Development of Turbulent Boundary Layers. British A.R.C., R. & M. No. 2133, June 1944.
16. Squire, H. B., and Young, A. D.: The Calculation of the Profile drag of Airfoils. British A.R.C., R. & M. No. 1838, 1938.
17. Goldstein, S.: Modern Developments in Fluid Dynamics, Vol. I. Oxford, Clarendon Press. 1938.
18. Young, A. D., and Green, G. L.: Tests of High Speed Flow in Diffusers of Rectangular Cross-Section. British A.R.C., R. & M. No. 2201, July 1944.
19. Patterson, G. N.: Corner Losses in Ducts. Aircraft Engineering, Vol. IX, August 1937.
20. Patterson, G. N.: The Design of Aeroplane Ducts. Aircraft Engineering, Vol. XI, July 1939.
21. Peters, H.: Conversion of Energy in Cross-Sectional Divergences under Different Conditions of Inflow, NACA TN No. 737, 1934.
22. Jordan, E. J.: Design of Turbo-jet Installations, Part I. Aero Digest, October 1948.
23. Johnson, C. L.: Development of the Lockheed P-80A Jet Fighter Airplane. Journal of the Aeronautical Sciences, December 1947.

1. The first part of the report, which is the most important, is the one which deals with the general principles of the subject.

2. The second part of the report, which is the most interesting, is the one which deals with the practical application of the principles.

3. The third part of the report, which is the most useful, is the one which deals with the results of the experiments.

4. The fourth part of the report, which is the most valuable, is the one which deals with the conclusions drawn from the experiments.

5. The fifth part of the report, which is the most complete, is the one which deals with the details of the experiments.

6. The sixth part of the report, which is the most thorough, is the one which deals with the methods used in the experiments.

7. The seventh part of the report, which is the most accurate, is the one which deals with the measurements made during the experiments.

8. The eighth part of the report, which is the most precise, is the one which deals with the calculations made from the measurements.

9. The ninth part of the report, which is the most exact, is the one which deals with the comparison of the results with the theoretical predictions.

10. The tenth part of the report, which is the most correct, is the one which deals with the discussion of the results.

11. The eleventh part of the report, which is the most reliable, is the one which deals with the summary of the results.

12. The twelfth part of the report, which is the most trustworthy, is the one which deals with the references.

13. The thirteenth part of the report, which is the most dependable, is the one which deals with the appendix.

14. The fourteenth part of the report, which is the most accurate, is the one which deals with the index.

15. The fifteenth part of the report, which is the most complete, is the one which deals with the bibliography.

16. The sixteenth part of the report, which is the most thorough, is the one which deals with the list of figures.

TABLE I

PHENOMENON CONDITIONS IN THE DIFFUSER

$M_0 = 1.5$

$n = 40,000$ feet

ξ	x/c	D/D_0	A/A_0	p lb/ft ²	$\frac{P}{\rho V^2}$ slugs/ft ³	θ °	V ft/sec	$\frac{q}{\rho V^2}$ ft ²	dq/dx
.409	0	1.08	1.104	1189	1.261x10 ⁻³	550	470	139.5	
.43	.0066	1.065	1.133	1174	1.250	548	494	152.5	
.45	.0137	1.046	1.097	1160	1.240	547	516	165	
.47	.0225	1.03	1.062	1145	1.230	545	538	177.8	
.49	.0349	1.014	1.03	1130	1.218	543	558	189	
.51	.0618	1.0	1.0	1116	1.205	541	581	204	
.49	.1175	1.014	1.03	1130	1.218	543	558	189	-6.10
.47	.1850	1.03	1.062	1145	1.230	545	538	178	-5.54
.45	.2520	1.046	1.097	1160	1.240	547	516	165	-5.00
.43	.319	1.065	1.136	1174	1.250	548	494	153	-4.52
.41	.408	1.086	1.180	1188	1.261	550	472	141	-4.00
.38	.542	1.12	1.255	1207	1.276	553	439	122	-3.53
.35	.700	1.16	1.348	1225	1.290	555	405	106	-3.12
.32	.877	1.205	1.458	1241	1.301	557	371	90	-2.78
.30	1.000	1.24	1.541	1251	1.310	559	349	79	-2.70

Date	Particulars	Debit	Credit	Balance
1920	Jan 1			
	Jan 2			
	Jan 3			
	Jan 4			
	Jan 5			
	Jan 6			
	Jan 7			
	Jan 8			
	Jan 9			
	Jan 10			
	Jan 11			
	Jan 12			
	Jan 13			
	Jan 14			
	Jan 15			
	Jan 16			
	Jan 17			
	Jan 18			
	Jan 19			
	Jan 20			
	Jan 21			
	Jan 22			
	Jan 23			
	Jan 24			
	Jan 25			
	Jan 26			
	Jan 27			
	Jan 28			
	Jan 29			
	Jan 30			
	Jan 31			
	Feb 1			
	Feb 2			
	Feb 3			
	Feb 4			
	Feb 5			
	Feb 6			
	Feb 7			
	Feb 8			
	Feb 9			
	Feb 10			
	Feb 11			
	Feb 12			
	Feb 13			
	Feb 14			
	Feb 15			
	Feb 16			
	Feb 17			
	Feb 18			
	Feb 19			
	Feb 20			
	Feb 21			
	Feb 22			
	Feb 23			
	Feb 24			
	Feb 25			
	Feb 26			
	Feb 27			
	Feb 28			
	Feb 29			
	Feb 30			
	Feb 31			

$\sum D^2 = 114$ $\sum C^2 = 114$ $\sum BC = 114$
 (Total sum of squares) (Total sum of squares) (Total sum of squares)

TABLE II
 COMPUTATION TO DETERMINE SEPARATION
 OF THE TURBULENT BOUNDARY LAYER

$M_0 = 1.5$

$h = 40,000 \text{ ft.}$

$c/q_0 = .1575$

x/c	R_0	e/c	H	q/q_0	$\frac{c}{q_0} \frac{dq}{dx}$	$\frac{\tau_0}{2q}$
.0613	260	$.0501 \times 10^{-3}$	1.286	1	0	3.14×10^{-3}
.070	394	$.0759 \times 10^{-3}$	1.286	.99	-1.025	2.81×10^{-3}
.09	685	.1347	1.289	.963	-.995	2.43
.20	2090	.4267	1.305	.850	-.850	1.48
.30	3210	.6852	1.323	.765	-.735	1.71
.40	4320	.9657	1.343	.690	-.637	1.60
.50	5490	1.275	1.365	.630	-.575	1.53
.60	6850	1.623	1.390	.572	-.530	1.46
.65	7350	1.823	1.405	.545	-.512	1.44
.73	8810	2.271	1.431	.505	-.485	1.39
.80	9910	2.630	1.459	.475	-.465	1.36
.85	10720	2.920	1.478	.45	-.450	1.35
.90	11630	3.242	1.510	.429	-.436	1.34
.94	12400	3.527	1.536	.411	-.426	1.31
.97	13060	3.760	1.559	.400	-.420	1.30
1.00	13750	4.010	1.568	.389	-.415	1.29

TABLE III

RELATIONSHIP BETWEEN THE PERCENTAGE OF
 THE TOTAL POPULATION IN THE
 VARIOUS CATEGORIES OF THE

Year	Total population		Male		Female	
	No.	%	No.	%	No.	%
1950	1,000,000	100	500,000	50	500,000	50
1951	1,010,000	101	505,000	50	505,000	50
1952	1,020,000	102	510,000	50	510,000	50
1953	1,030,000	103	515,000	50	515,000	50
1954	1,040,000	104	520,000	50	520,000	50
1955	1,050,000	105	525,000	50	525,000	50
1956	1,060,000	106	530,000	50	530,000	50
1957	1,070,000	107	535,000	50	535,000	50
1958	1,080,000	108	540,000	50	540,000	50
1959	1,090,000	109	545,000	50	545,000	50
1960	1,100,000	110	550,000	50	550,000	50
1961	1,110,000	111	555,000	50	555,000	50
1962	1,120,000	112	560,000	50	560,000	50
1963	1,130,000	113	565,000	50	565,000	50
1964	1,140,000	114	570,000	50	570,000	50
1965	1,150,000	115	575,000	50	575,000	50
1966	1,160,000	116	580,000	50	580,000	50
1967	1,170,000	117	585,000	50	585,000	50
1968	1,180,000	118	590,000	50	590,000	50
1969	1,190,000	119	595,000	50	595,000	50
1970	1,200,000	120	600,000	50	600,000	50

TABLE II (Continued)

$\frac{n+2}{2}$	$\frac{q}{q} \frac{dq}{dx}$	$\frac{dq}{dx}$	$\Delta q/c$	$-\frac{q}{q} \frac{dq}{dx} \frac{2q}{r_0}$	$\frac{2.035}{x}$ ($n-1.286$)
0		3.14×10^{-3}	$.0258 \times 10^{-3}$	0	0
-	$.129 \times 10^{-3}$	2.94	.0588	.028	0
-	.229	2.66	.292	.0572	.0057
-	.705	2.535	.2585	.2270	.0386
-	1.095	2.805	.2805	.3850	.0754
	1.490	3.070	.3090	.5560	.1160
	1.955	3.485	.3485	.760	.1610
	2.55	4.01	.200	1.03	.211
	2.91	4.35	.348	1.19	.242
	3.74	5.13	.359	1.57	.295
	4.45	5.81	.290	1.89	.352
	5.09	6.44	.322	2.16	.401
	5.80	7.14	.285	2.46	.456
	6.46	7.77	.233	2.79	.509
	7.03	8.33	.250	3.04	.555

TABLE II (Continued)

$\bullet 4.68(H-2.975)$	$\bullet \frac{dH}{dx}$	$\bullet \frac{dH}{dx}$	ΔH	$\Delta x/c$
$.38 \times 10^{-3}$	0	0	0	.0082
$.38 \times 10^{-3}$	$.0107 \times 10^{-3}$.140	.0023	.02
.38	.0196	.145	.0160	.11
.405	.0763	.179	.0179	.10
.440	.1363	.199	.0199	.10
.480	.2110	.219	.0219	.10
.530	.317	.249	.0249	.10
.600	.491	.303	.0152	.05
.630	.598	.328	.0263	.08
.700	.892	.393	.0275	.07
.805	1.238	.480	.0249	.05
.900	1.585	.543	.0272	.05
1.050	2.10	.646	.0253	.04
1.20	2.74	.778	.0233	.03
1.35	3.36	.892	.0263	.03

Δ	Δ	$\frac{\Delta}{\Delta}$	$\frac{\Delta}{\Delta}$	(1954-1954)
100.	100.	100.	100.	100.
11.	110.	110.	110.	110.
12.	120.	120.	120.	120.
13.	130.	130.	130.	130.
14.	140.	140.	140.	140.
15.	150.	150.	150.	150.
16.	160.	160.	160.	160.
17.	170.	170.	170.	170.
18.	180.	180.	180.	180.
19.	190.	190.	190.	190.
20.	200.	200.	200.	200.
21.	210.	210.	210.	210.
22.	220.	220.	220.	220.
23.	230.	230.	230.	230.
24.	240.	240.	240.	240.
25.	250.	250.	250.	250.
26.	260.	260.	260.	260.
27.	270.	270.	270.	270.
28.	280.	280.	280.	280.
29.	290.	290.	290.	290.
30.	300.	300.	300.	300.

TABLE III

COMPUTATION TABLE FOR FRICTION FACTORS IN DIFFUSER

$Mo = 15$

$h = 40,000 \text{ ft.}$

LAMINAR INLET ZONE

$$\frac{\tau_0}{q} = 0.730 \sqrt{\frac{1}{Rx}}$$

$c = 2.67 \text{ ft.}$

$\nu \approx 2.96 \times 10^{-4} \text{ ft.}^2/\text{sec.}$

x/c	x ft.	$\frac{p}{1b/ft^2}$	$\frac{q}{1b/ft^2}$	D ft.	v ft./sec	$1/Rx$	$\sqrt{1/Rx}$	τ_0/q	$4 \frac{\tau_0}{q} \frac{D}{p}$
0	0	1139	139.5	1.590	470	∞	∞	∞	∞
.0066	.0175	1174	152.5	1.575	494	$\cdot 342 \times 10^{-4}$.00585	.00426	3.73×10^{-3}
.0137	.0366	1160	165	1.546	516	$\cdot 1565 \times 10^{-4}$.00396	.00239	2.81×10^{-3}
.0225	.0599	1145	177.8	1.522	538	$\cdot 092 \times 10^{-4}$.00304	.00222	2.40×10^{-3}
.0349	.093	1130	189	1.50	558	$\cdot 0571 \times 10^{-4}$.00239	.00174	2.08×10^{-3}
.0618	.165	1116	204	1.48	581	$\cdot 0303 \times 10^{-4}$.00174	.00127	1.66×10^{-3}

TURBULENT BOUNDARY LAYER ZONE

x/c	$\frac{q}{1b/ft^2}$	$\frac{p}{1b/ft^2}$	c/D	$\frac{q}{p} \frac{D}{D}$	$\tau_0/2q$	$4 \frac{\tau_0}{q} \frac{D}{p}$
.0618	204	1116	1.805	2.64	3.14×10^{-3}	8.30×10^{-3}
.1175	189	1130	1.78	2.305	2.19×10^{-3}	5.22×10^{-3}
.1850	177.8	1145	1.75	2.175	1.92×10^{-3}	4.10×10^{-3}
.2520	165	1160	1.725	1.96	1.77×10^{-3}	3.47×10^{-3}
.319	152.5	1174	1.695	1.76	1.69×10^{-3}	2.975×10^{-3}
.408	140.8	1188	1.665	1.58	1.60×10^{-3}	2.53×10^{-3}
.542	122.5	1207	1.61	1.308	1.51×10^{-3}	1.975×10^{-3}
.700	105.9	1225	1.555	1.076	1.415×10^{-3}	1.52×10^{-3}
.877	90.0	1241	1.498	.867	1.31×10^{-3}	1.162×10^{-3}
1.000	79.2	1251	1.455	.736	1.21×10^{-3}	$.950 \times 10^{-3}$

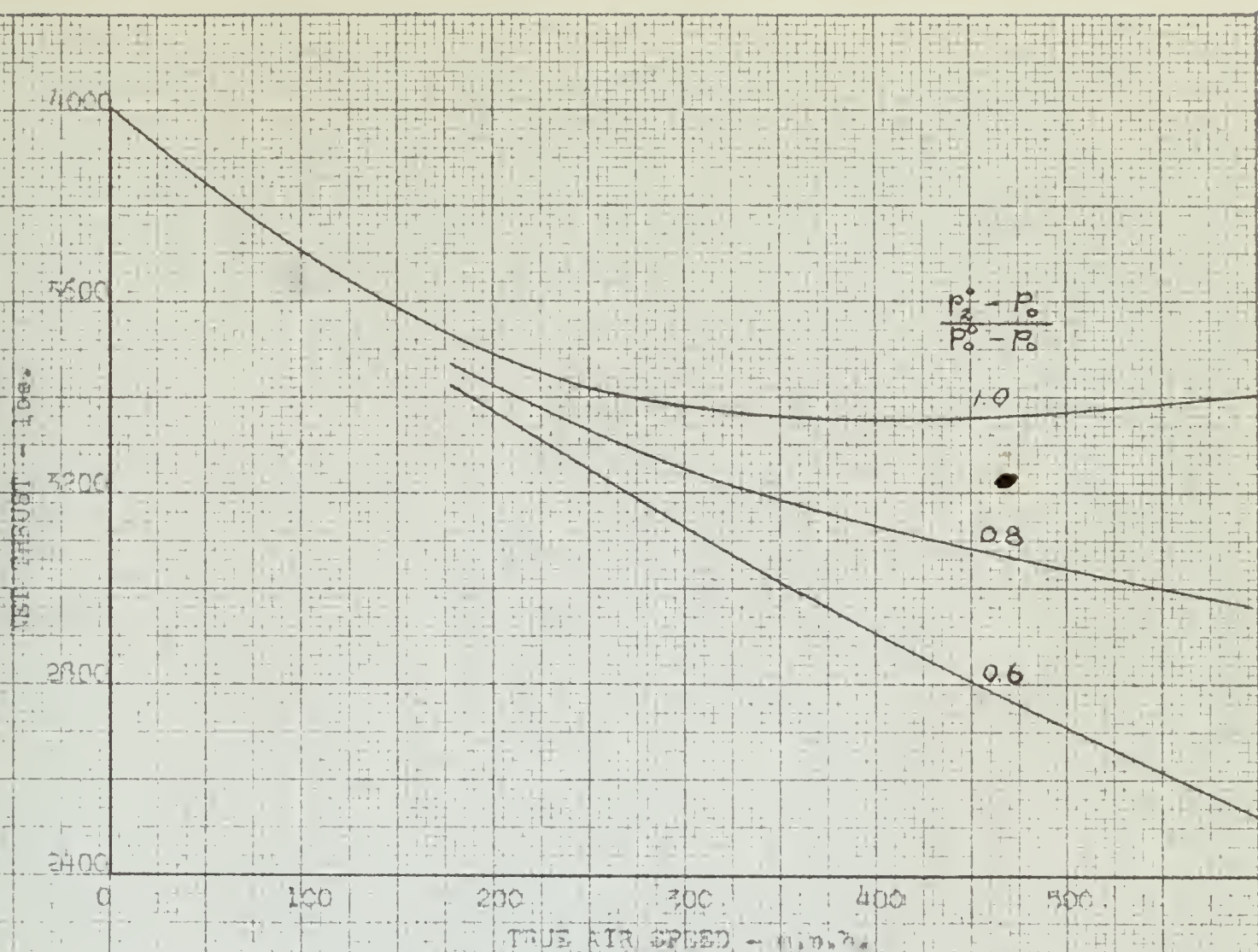


FIG. 1 - EFFECT OF RAM RECOVERY RATIO ON THE MAXIMUM AVAILABLE NET THRUST OF A TURBOJET ENGINE AT SEA LEVEL.

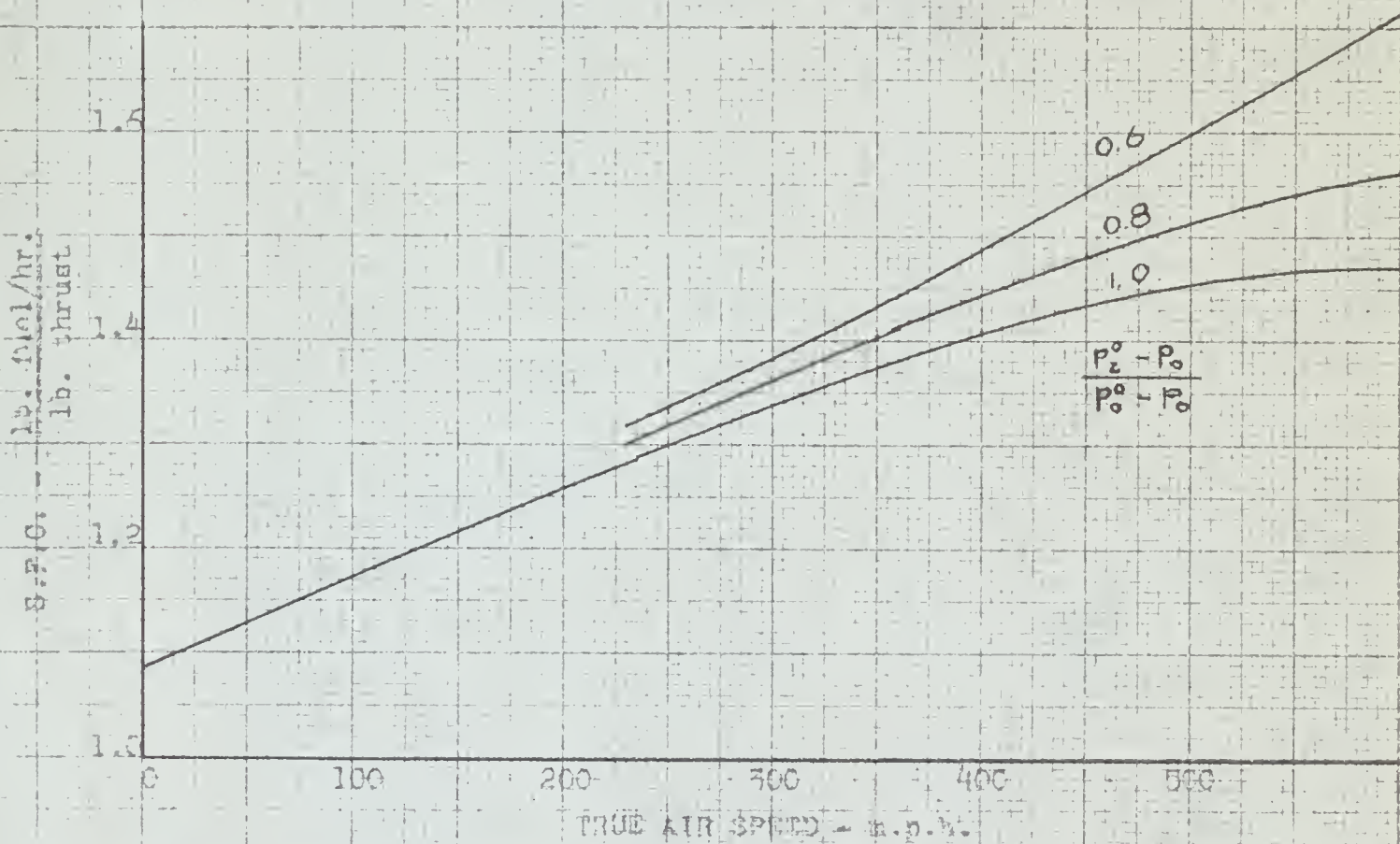
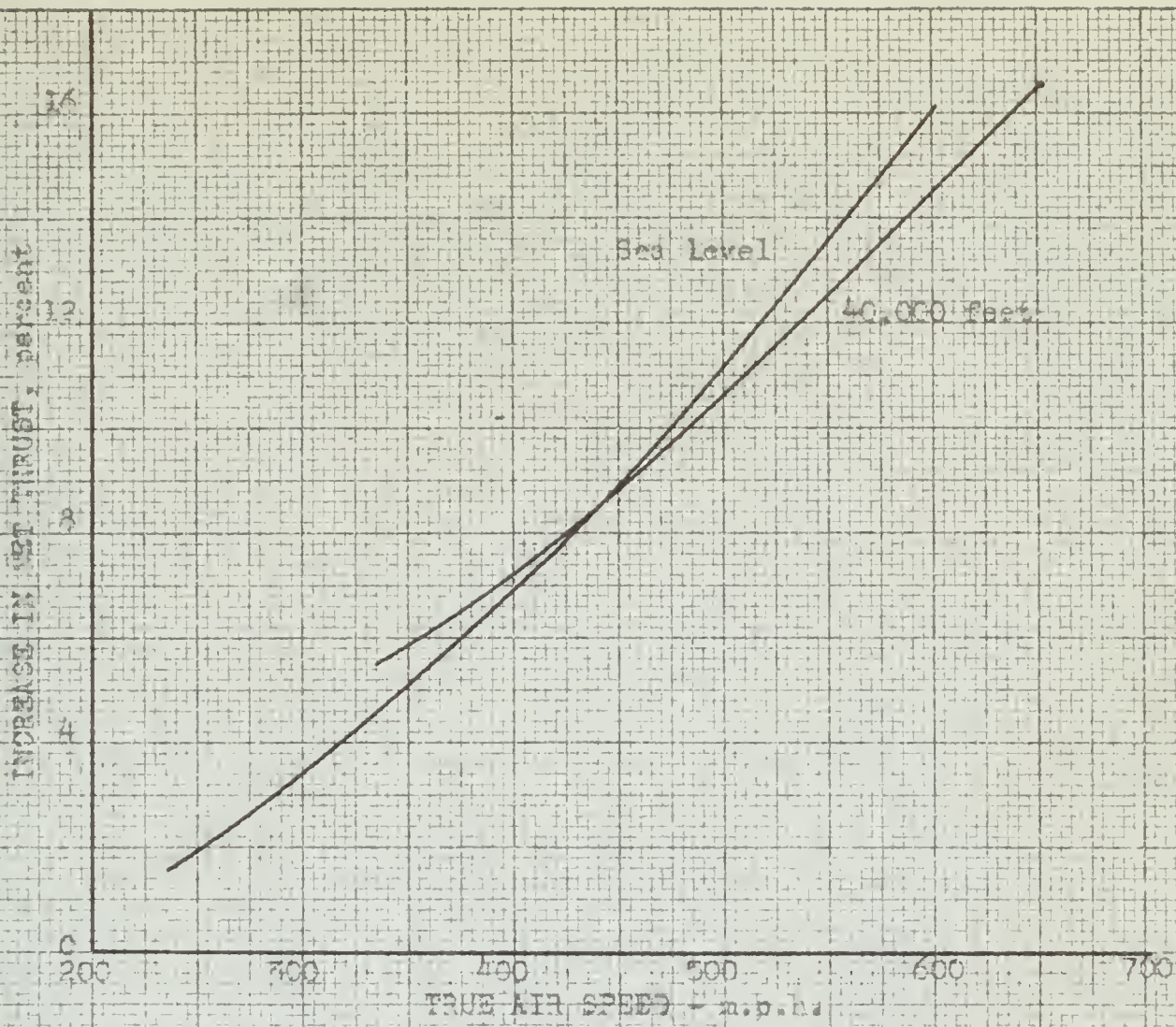
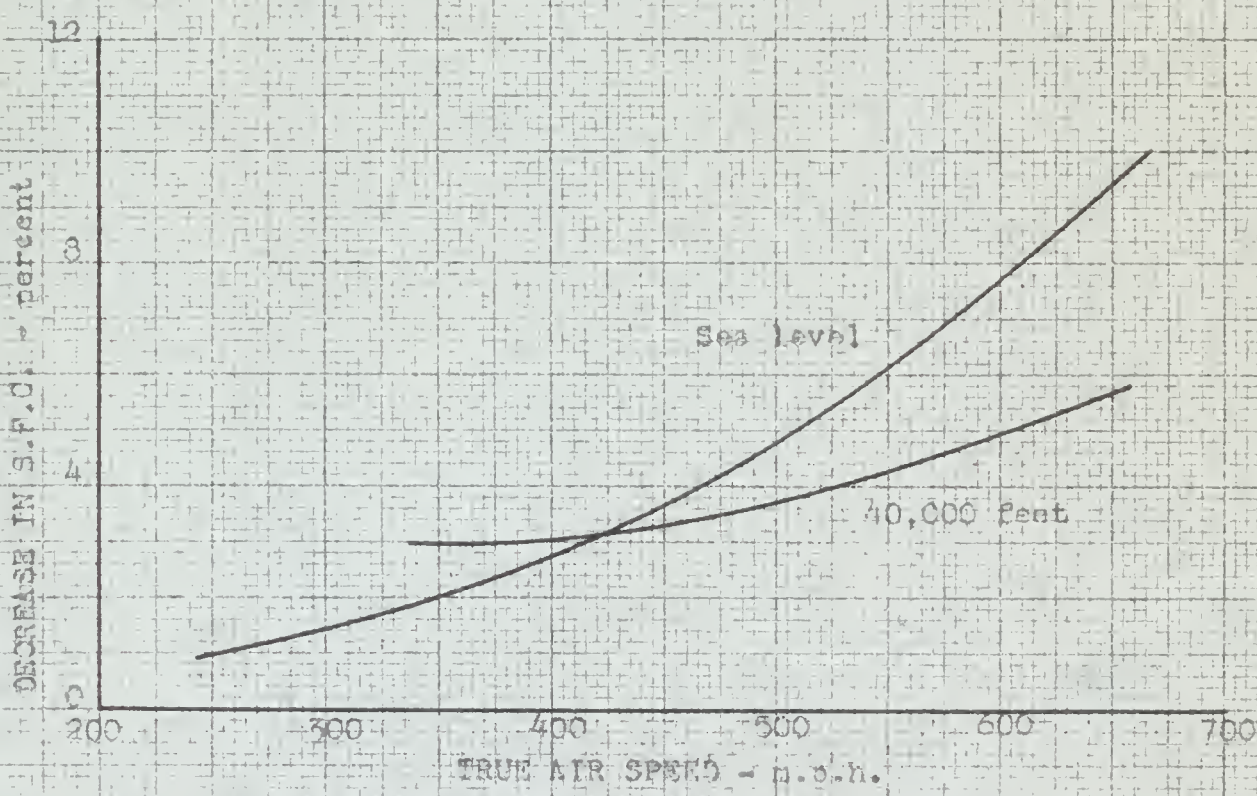


FIG. 2 - EFFECT OF RAM RECOVERY RATIO ON SPECIFIC FUEL CONSUMPTION AT MAXIMUM AVAILABLE NET THRUST OF A TURBOJET ENGINE AT SEA LEVEL.





(a) INCREASE IN NET THRUST.



(b) DECREASE IN SPECIFIC FUEL CONSUMPTION.

FIG. 5 - CHANGE IN NET THRUST AND SPECIFIC FUEL CONSUMPTION FOR AN INCREASE IN RAY RECOVERY RATIO FROM 0.70 TO 0.79. (NACA TN 1695)

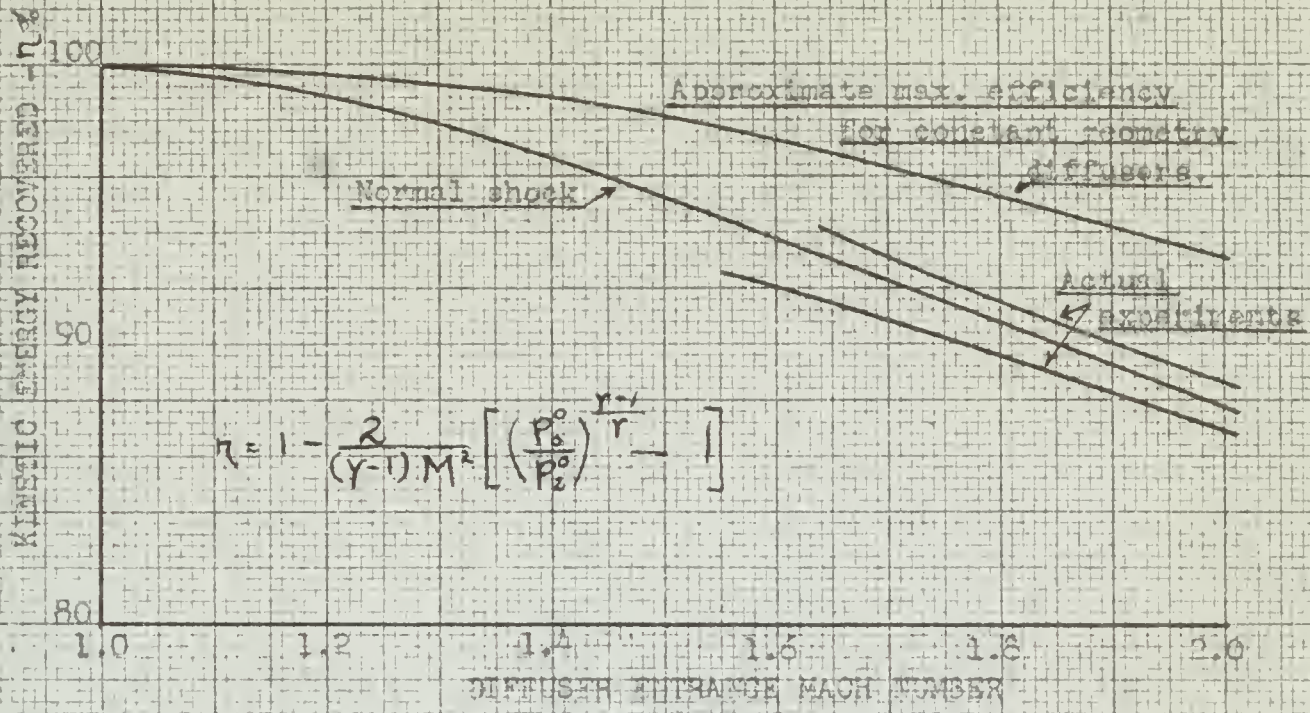


FIG. 4 - COMPARISON OF TEST RESULTS WITH THEORETICAL EXPECTATIONS FOR DIFFUSERS WITH INTERNAL SHOCK.

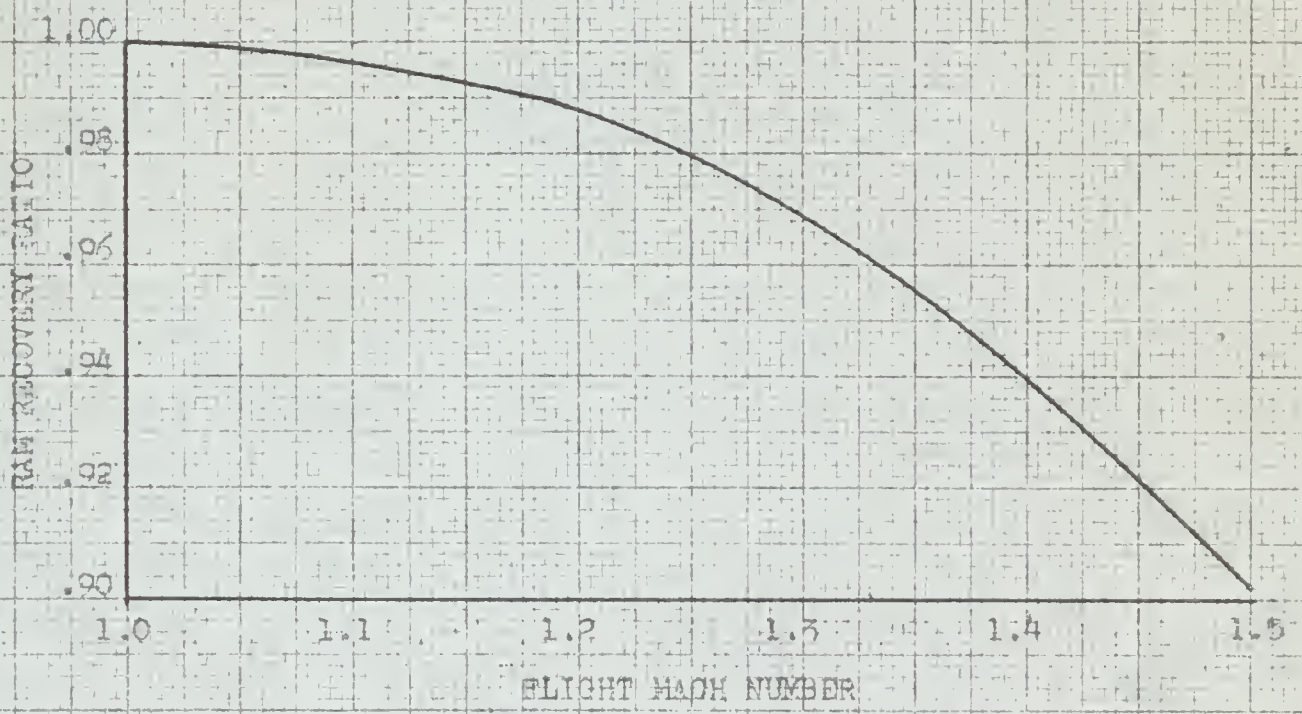


FIG. 5 - RAM RECOVERY RATIO ACROSS A NORMAL SHOCK.

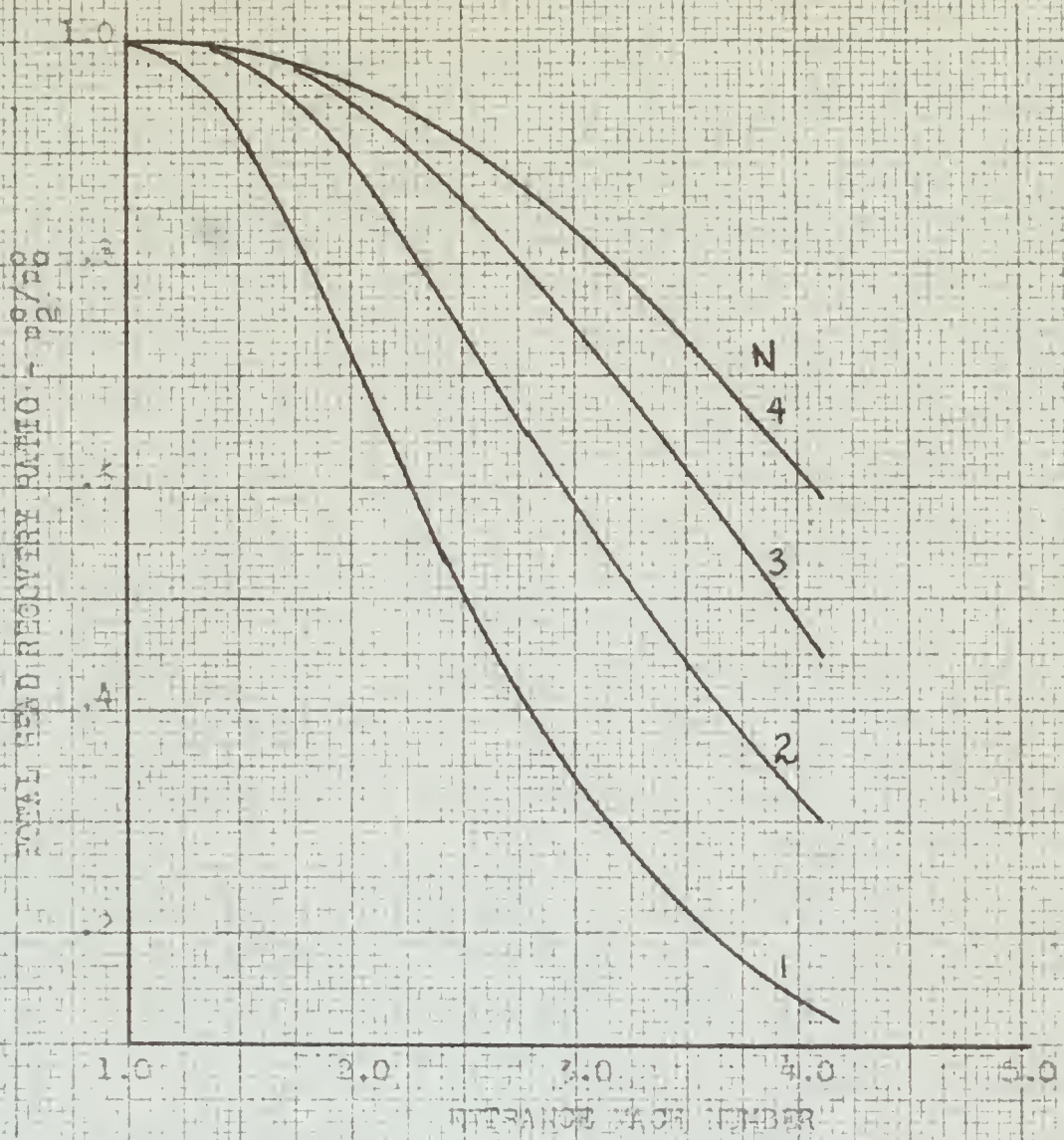


FIG. 6 - THEORETICAL PRESSURE RECOVERY RATIO AFTER "N" COMPRESSION SHOCKS. (NACA TM 1140)

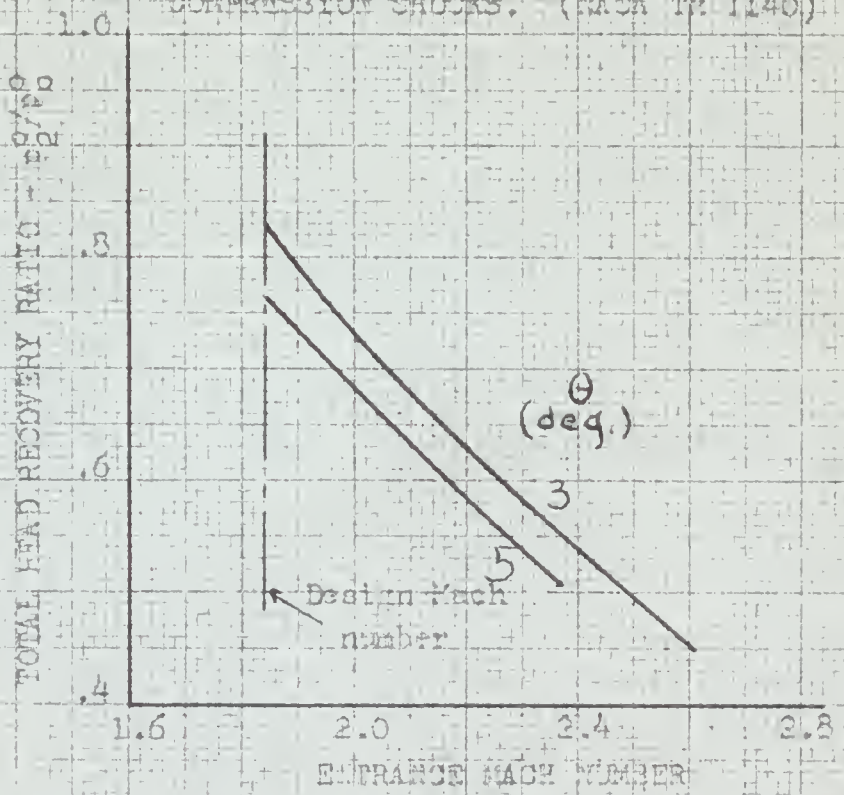


FIG. 7 - EFFECT OF EXIT CONE ANGLE ON THE PERFORMANCE OF TWO SUPERSONIC DIFFUSERS WITH EQUAL CONTRACTION RATIOS AND ENTRANCE CONE ANGLES.

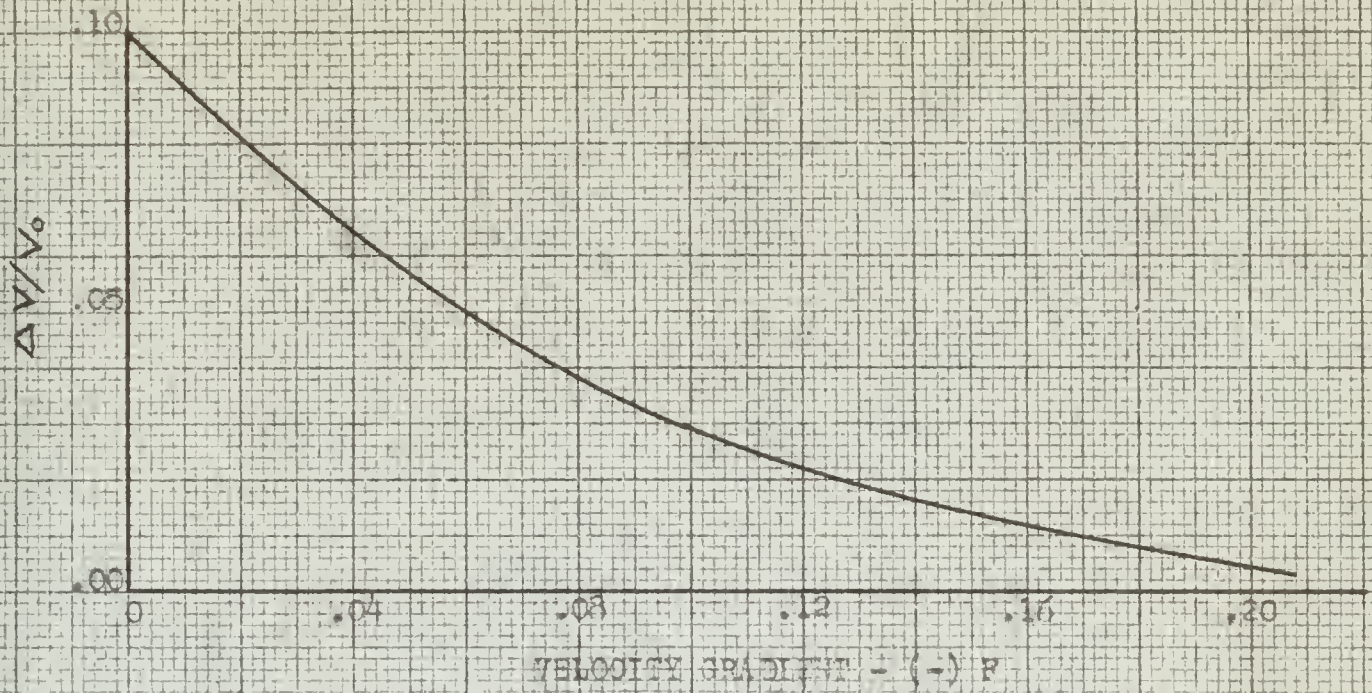


FIG. 8 - VELOCITY DECREMENT OBTAINABLE BEFORE LAMINAR SEPARATION OCCURS. (NACA TN 671)

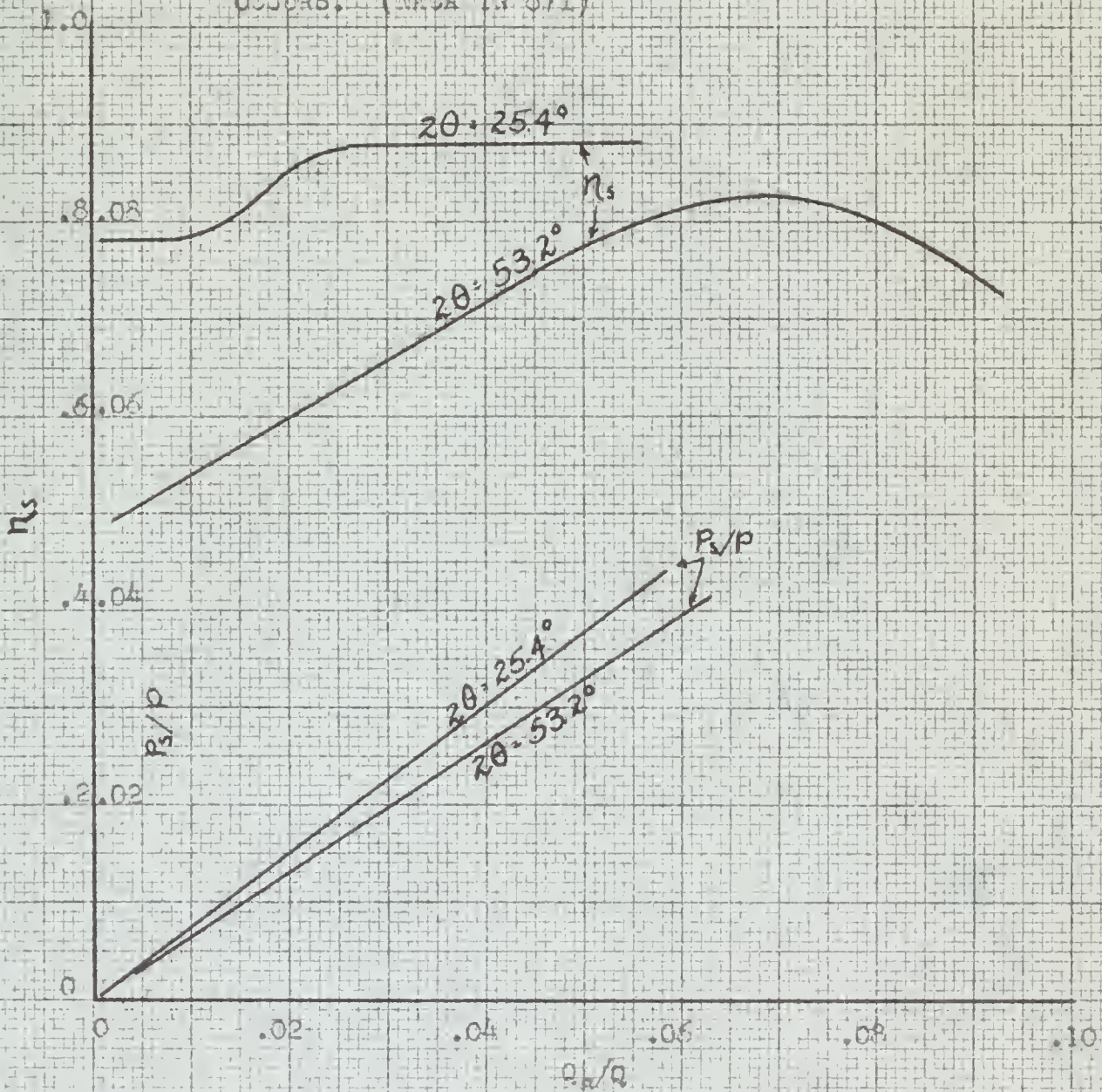
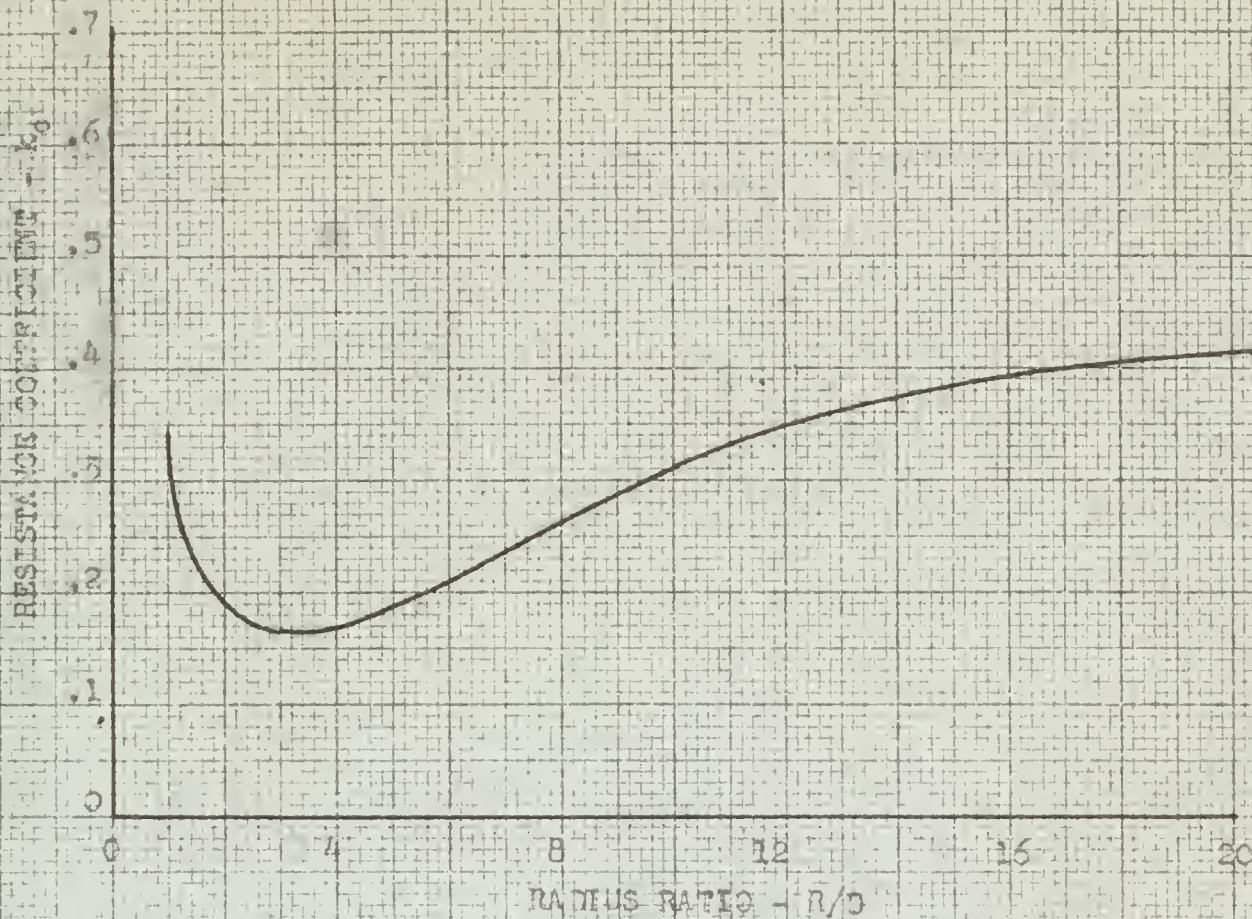
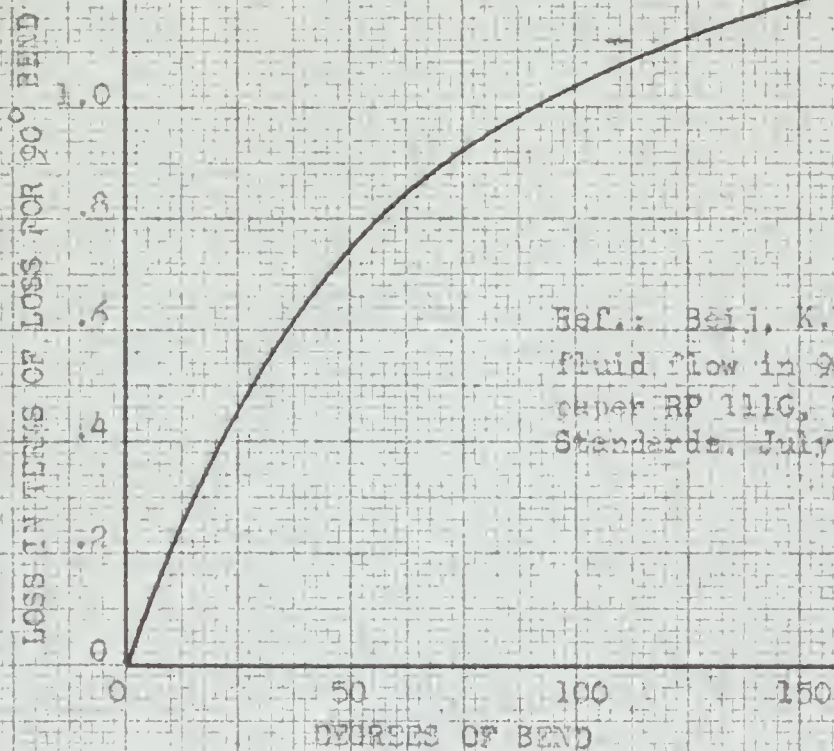


FIG. 9 - IMPROVEMENT OF DISPENSER EFFICIENCY WITH SUCTION.



(a) RESISTANCE COEFFICIENT IN A 90 DEG. BEND.



Ref.: Bell, K.H.: Pressure losses for fluid flow in 90° pipe bends, Research paper RP 1116, National Bureau of Standards, July 1958.

(b) CORRECTION FOR DEGREE OF BEND.

FIG. 10 - EFFECT OF RADIUS RATIO AND DEFLECTION ANGLE ON TRIMING LOSSES IN DUCTS.

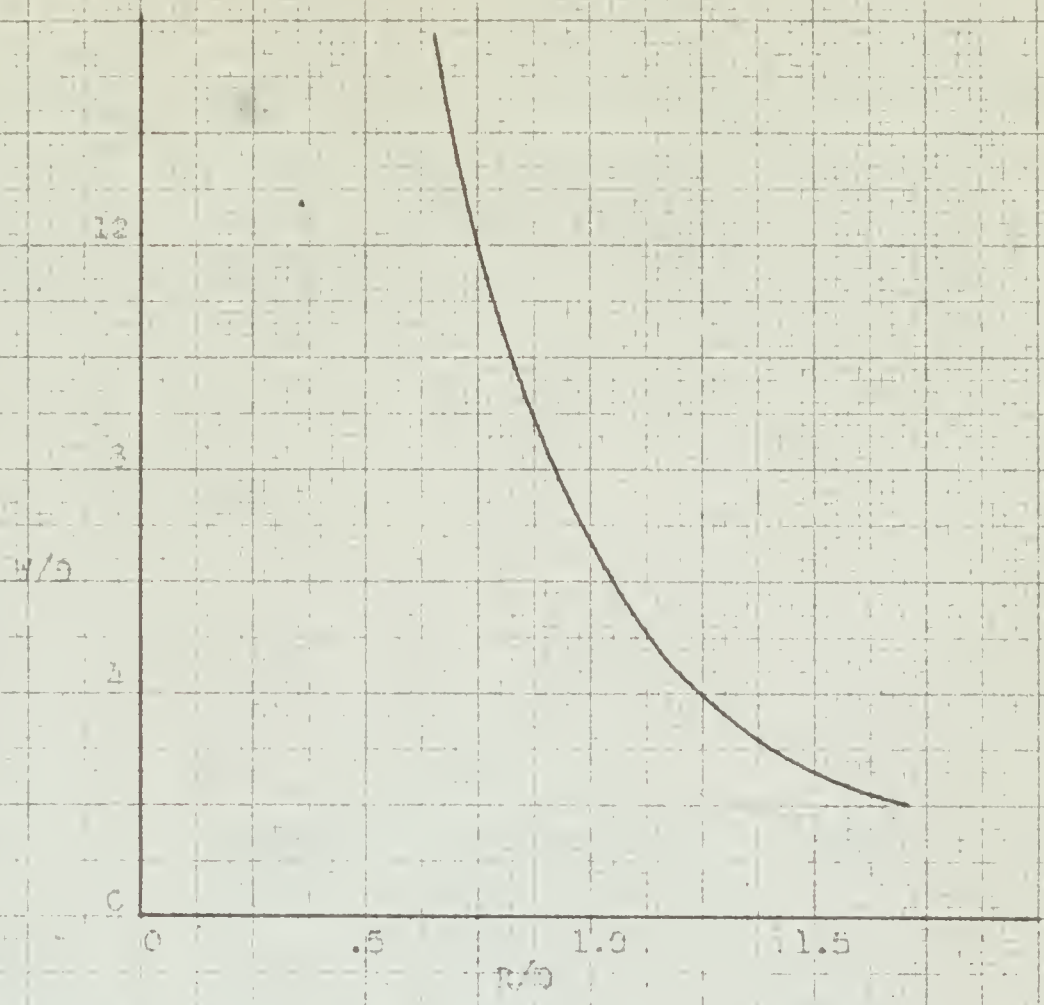


FIG. 11 -- ASPECT RATIO VERSUS RADIUS RATIO TO MAINTAIN A RESISTANCE COEFFICIENT OF 0.15

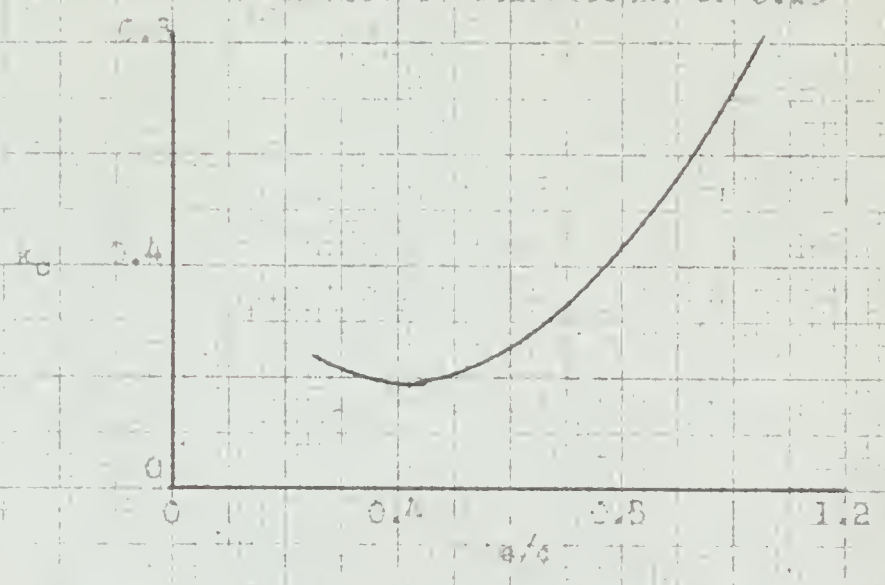
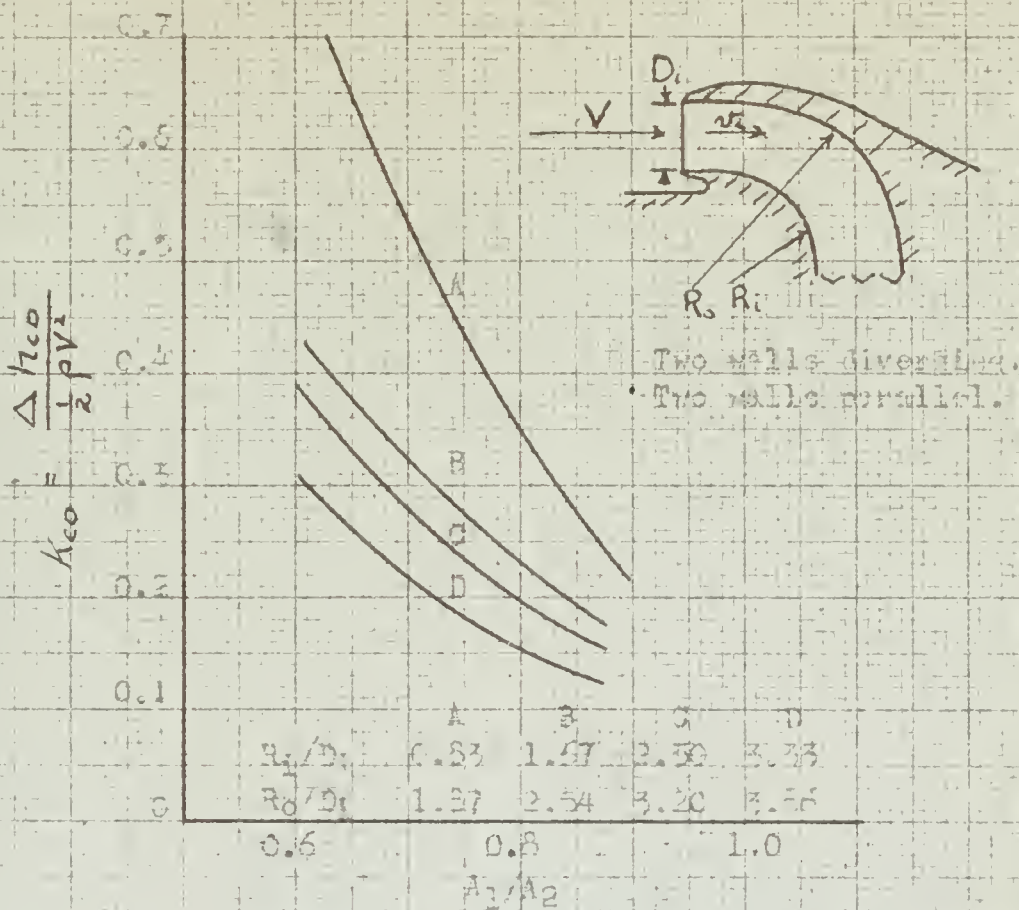
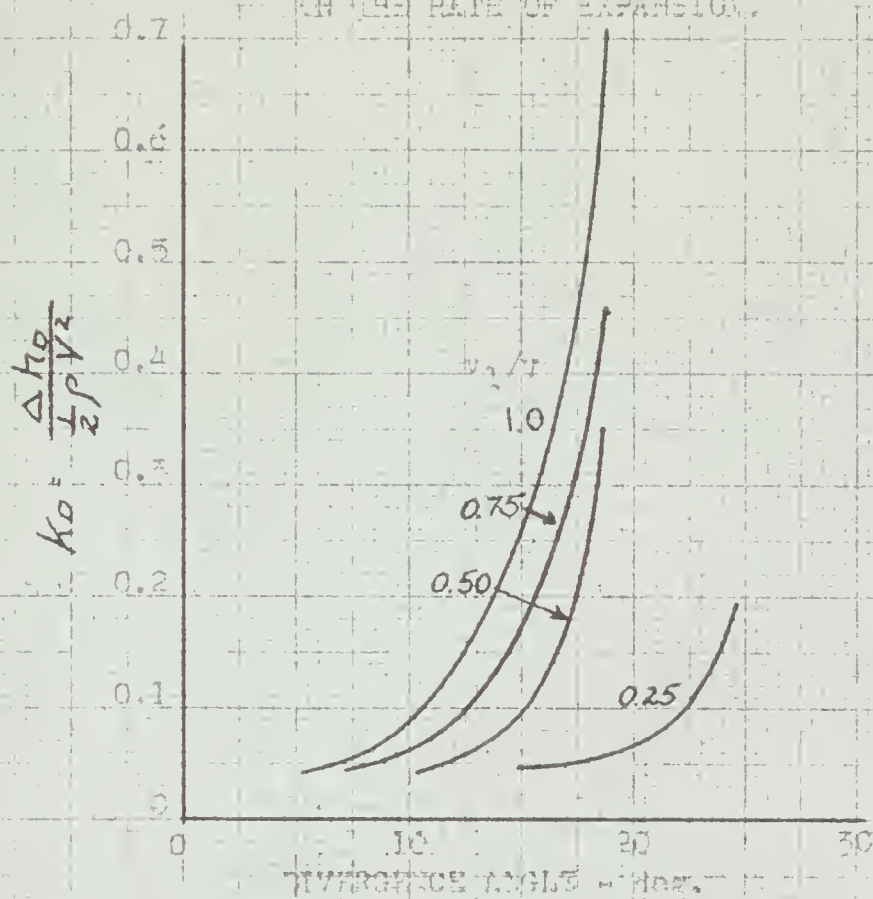


FIG. 12 -- EFFECT OF GAP/CHORD RATIO ON RESISTANCE COEFFICIENT.



(a) DEPENDENCE OF THE LOSS IN A CURVED ENTRANCE ON THE RATE OF EXPANSION.



(b) VARIATION OF THE LOSS IN A STRAIGHT EXPANDING ENTRY WITH INTERNAL AND EXTERNAL EXPANSION.

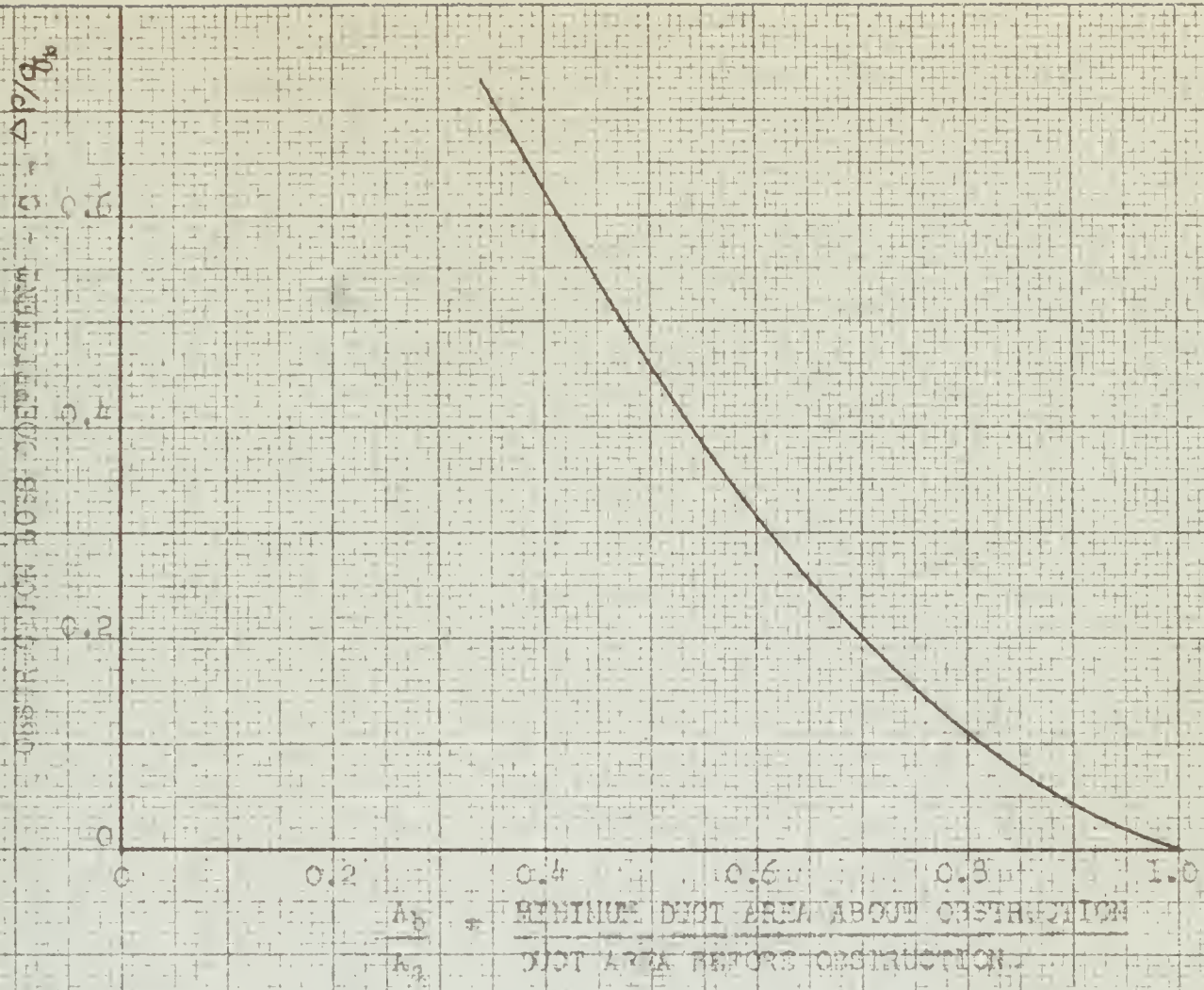


FIG. 14 - OBSTRUCTION LOSS COEFFICIENT IN A DUCT.

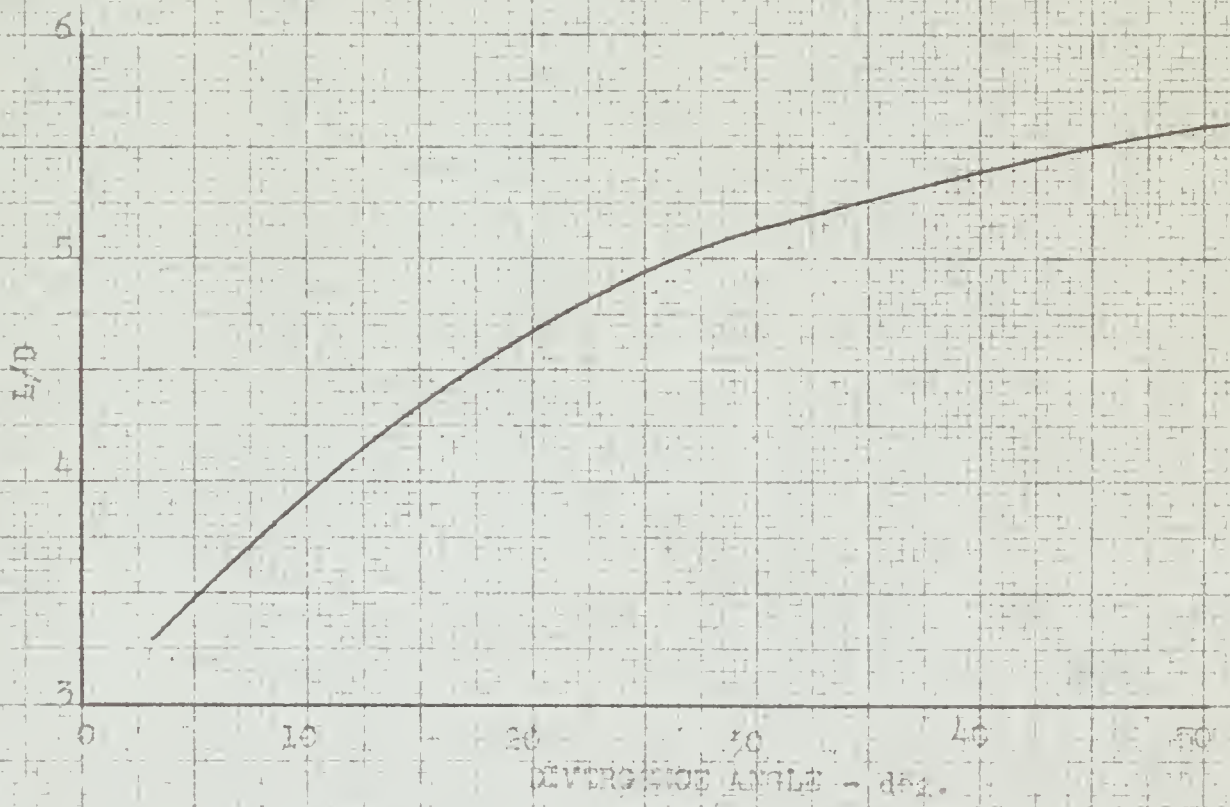


FIG. 15 - LENGTH OF CONSTANT AREA DUCT FOLLOWING A DIFFUSER NECESSARY FOR COMPLETE PRESSURE RECOVERY.

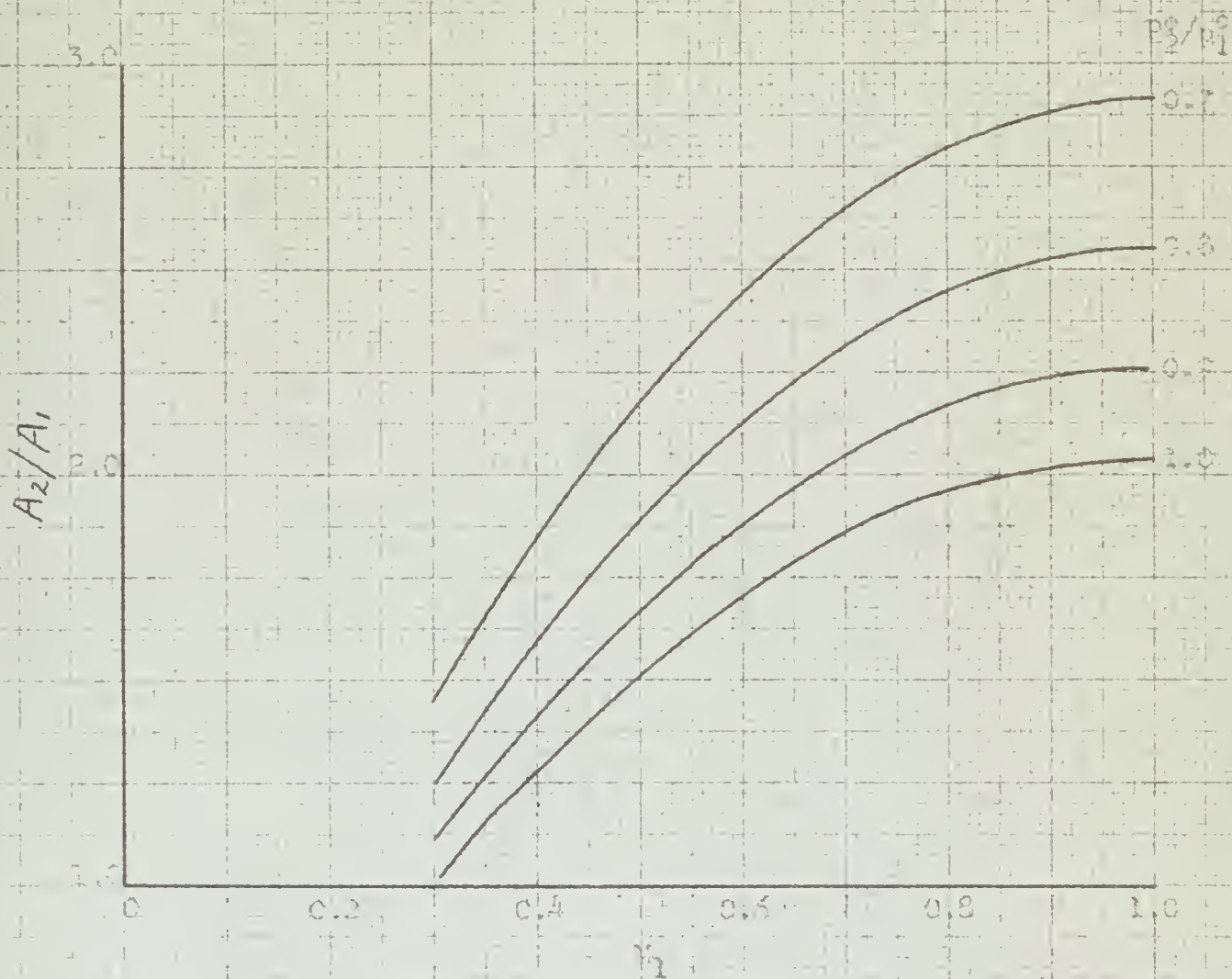


FIG. 16 - VARIATION OF AREA RATIO WITH DIFFUSER ENTRANCE MACH NUMBER TO GIVE A DIFFUSER EXIT MACH NUMBER OF 0.3.

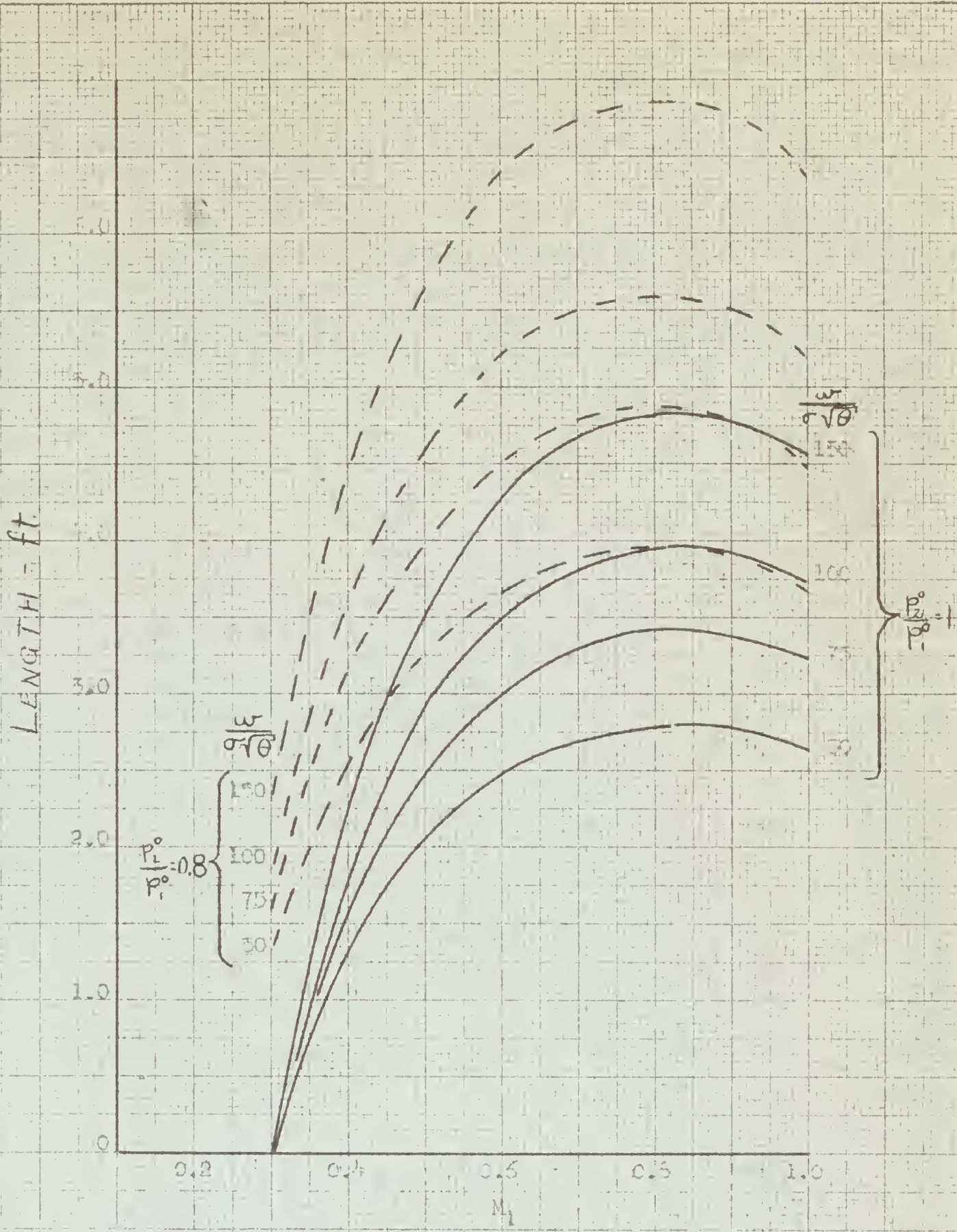


FIG. 17 - LENGTH OF CONICAL TAPER REQUIRED FOR VARIOUS MACH NUMBERS. EXIT MACH. NO. 0.5. DIVERGENCE ANGLE - 6° .

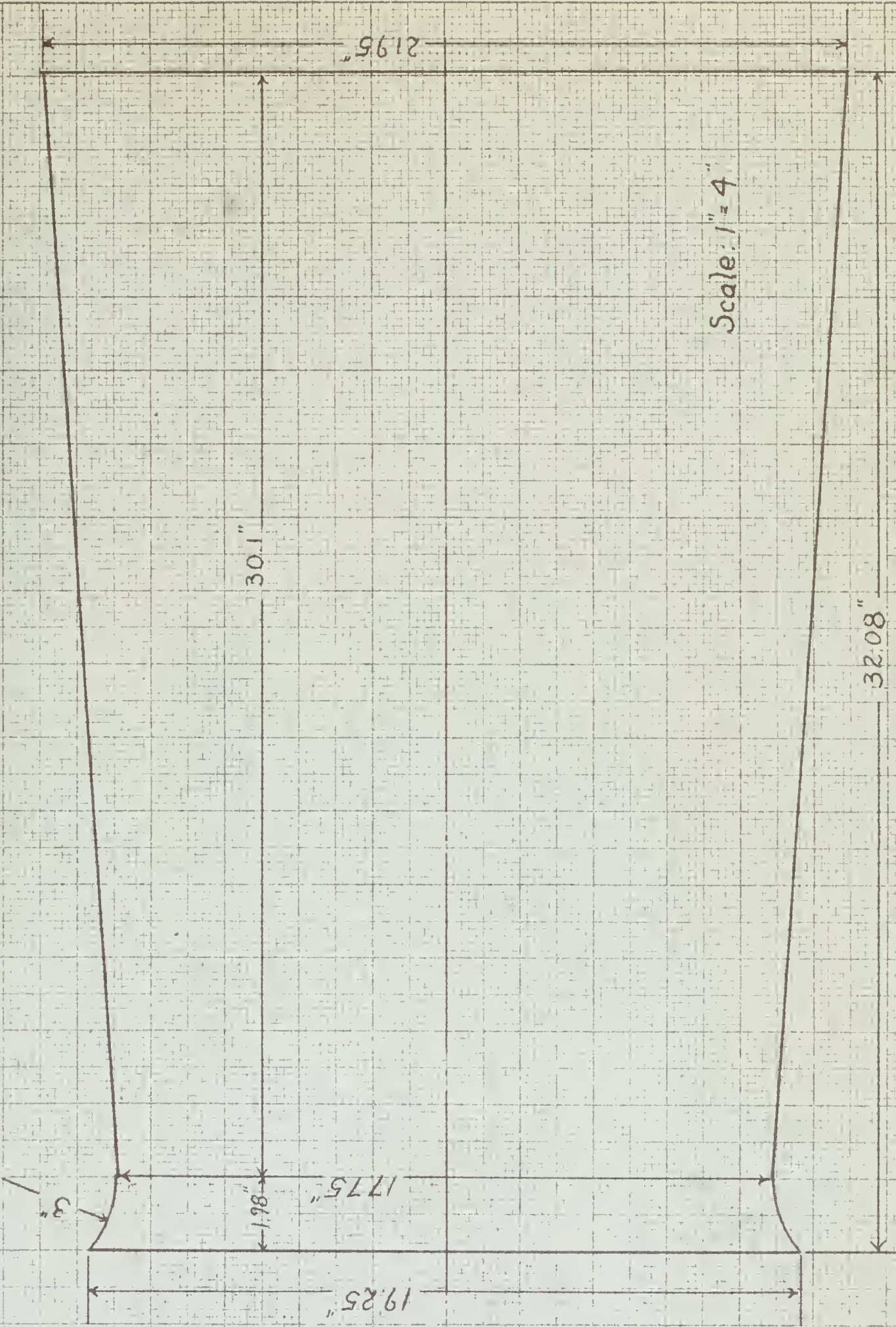
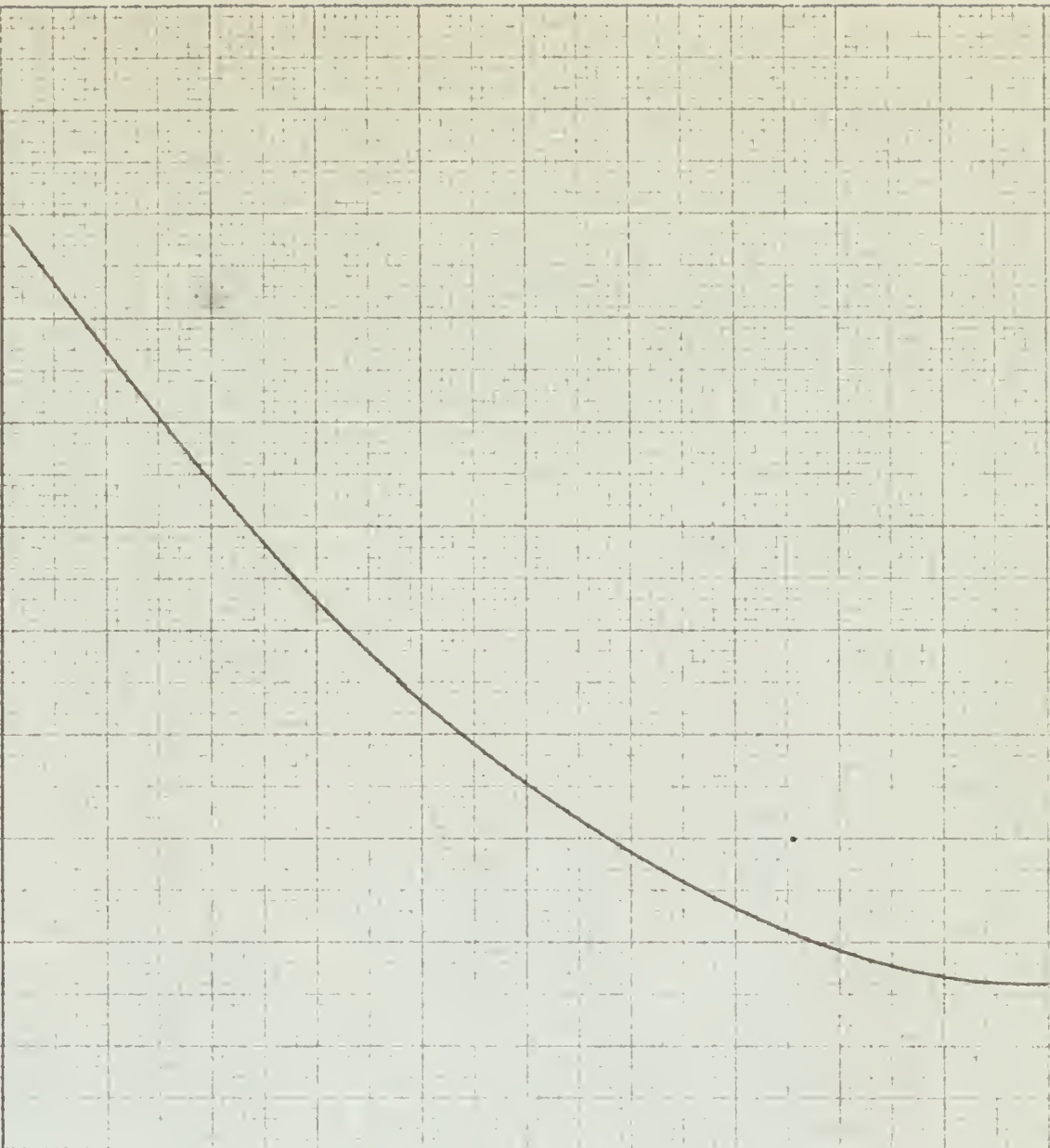


FIG. 18 - DIFFUSER FOR ILLUSTRATIVE PROBLEM

PRESSURE - lb/sq. ft.

1100

1100



(a) STATIC PRESSURE DISTRIBUTION AT DIFFUSER ENTRANCE.
ALTITUDE = 40,000 FT. FLIGHT MACH NUMBER = 1.5



(b) SHAPE OF DIFFUSER ENTRANCE LIP. Scale: 1" = 0.5"

FIG. 10.

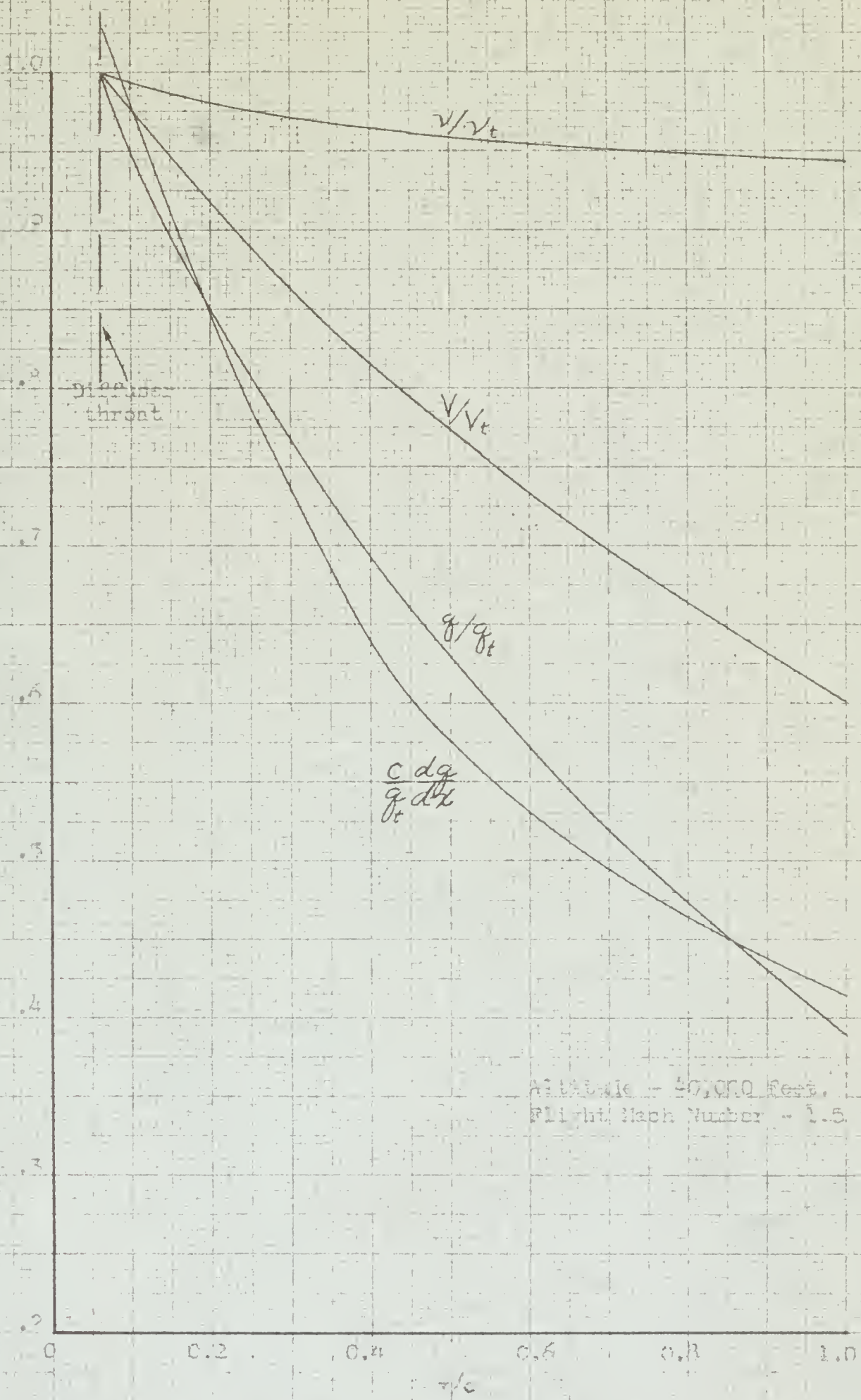
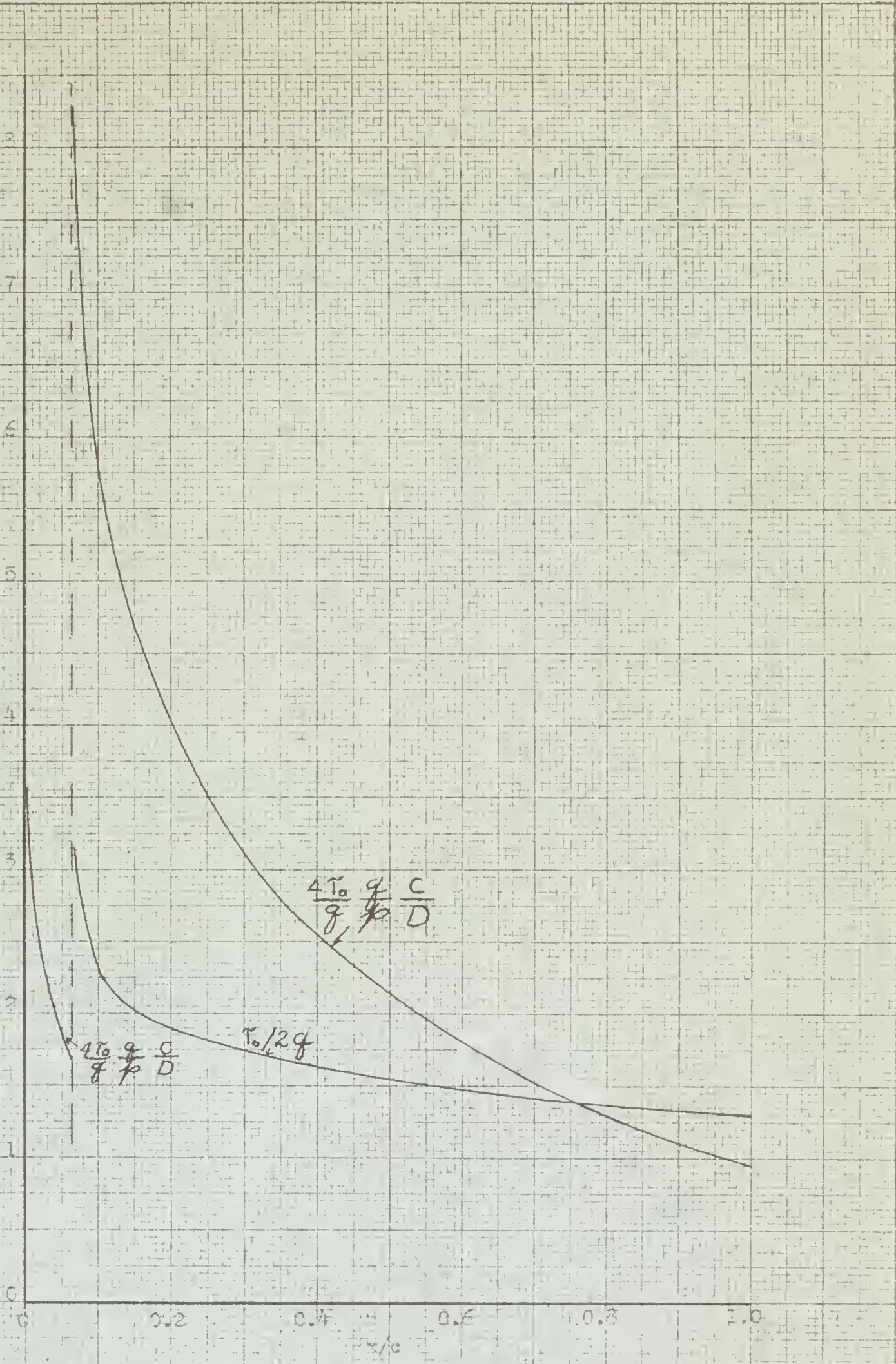


FIG. 20 - INTERNAL CONDITIONS IN THE DIFFUSER.

$\tau_0/2g \times 10^3$, $\frac{4\tau_0}{g} \frac{q}{\rho} \frac{c}{D}$



$\frac{4\tau_0}{g} \frac{q}{\rho} \frac{c}{D}$

$\tau_0/2g$

$\frac{4\tau_0}{g} \frac{q}{\rho} \frac{c}{D}$

FIG. 21 - FRICTION EFFECTS IN THE DISK.

PRESSURE LOSS IN CONSTANT AREA DUCT
 $\Delta p - \text{lb./sq. ft.}$

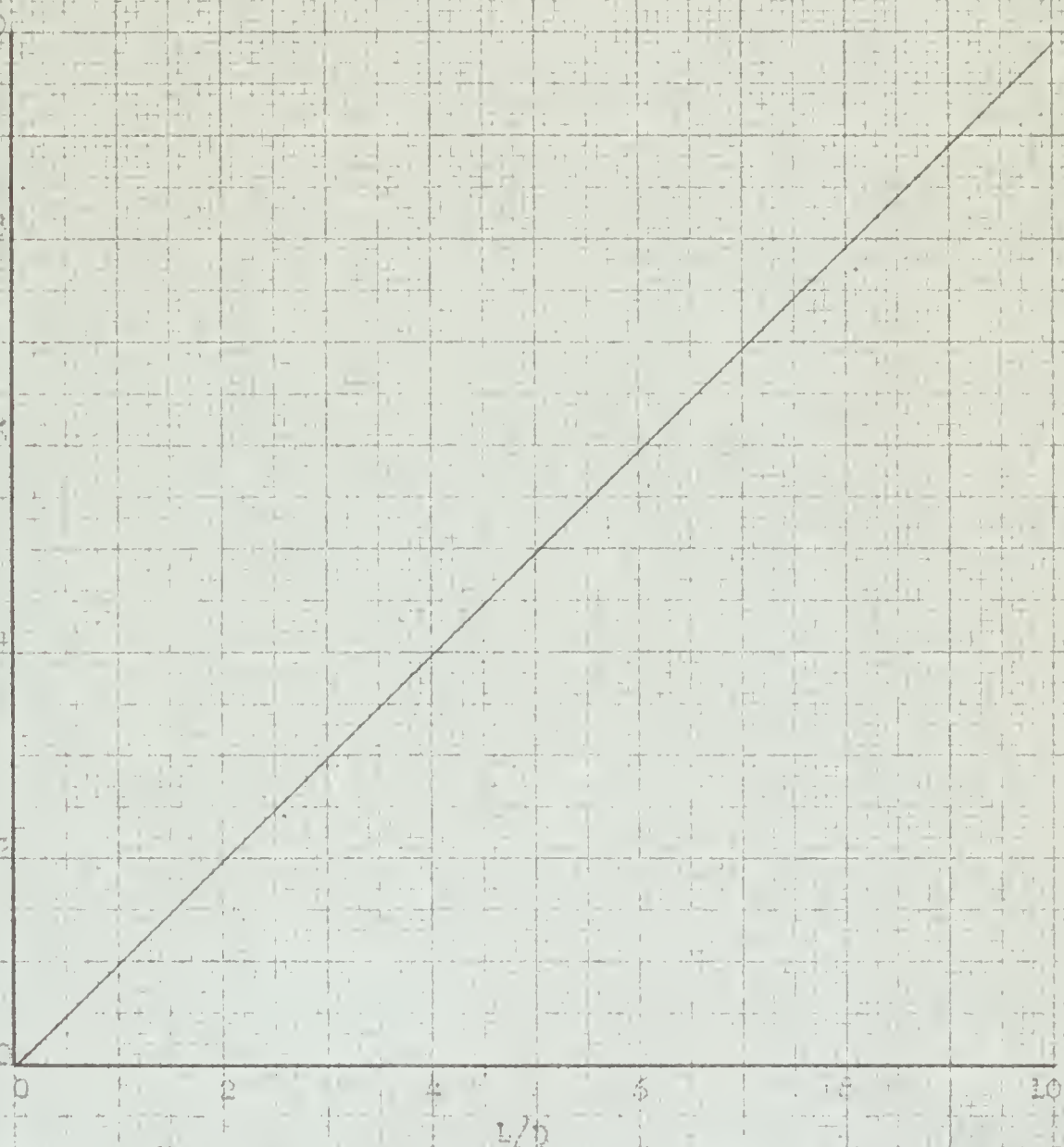


FIG. 22 - VARIATION OF PRESSURE LOSS IN THE CONSTANT AREA DUCT FROM DIFFUSER EXIT TO COMPRESSOR ENTRANCE WITH INCREASED LENGTH.

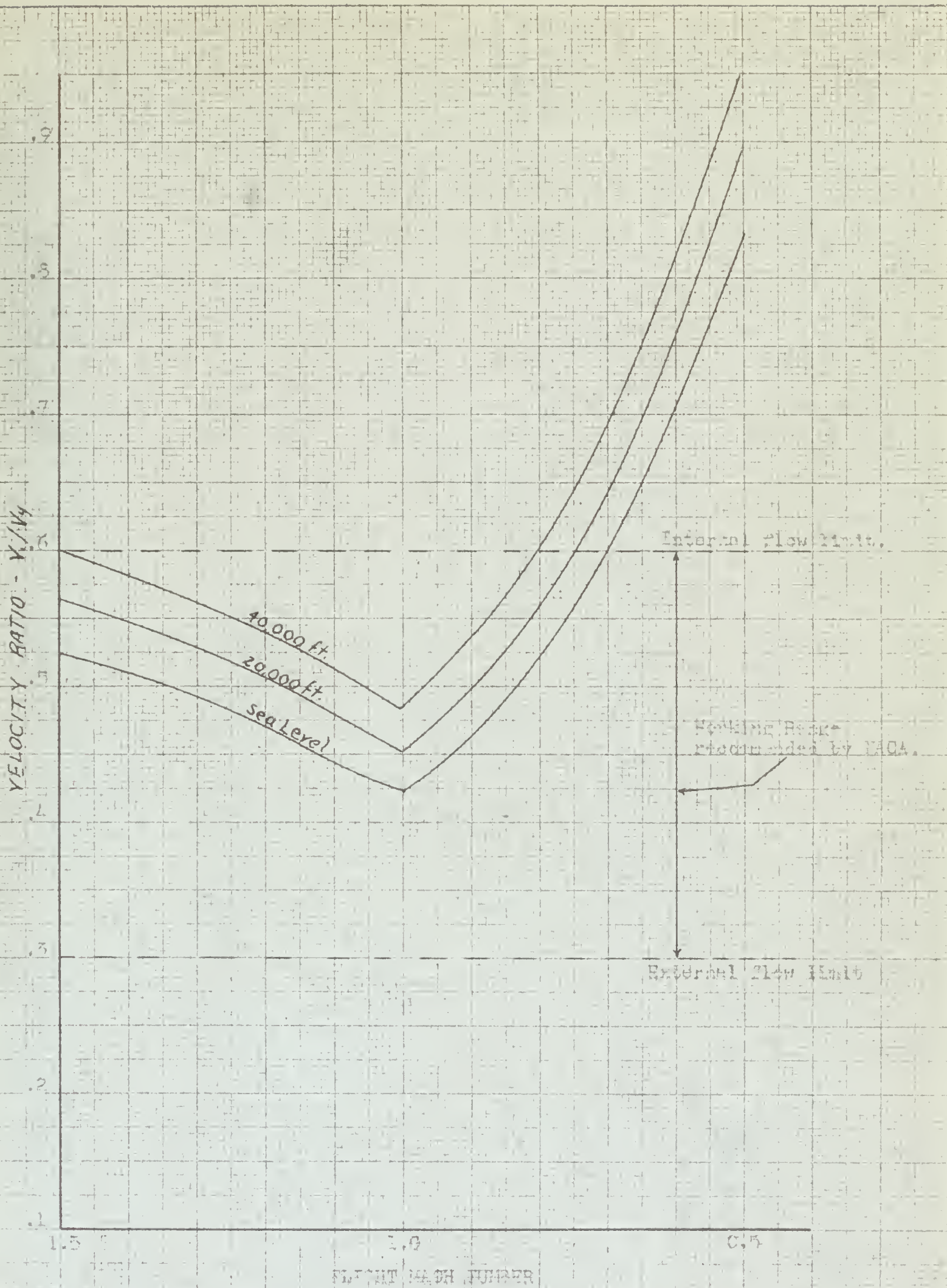


FIG. 22 - VARIATION OF VELOCITY RATIO WITH FLIGHT MACH NUMBER.

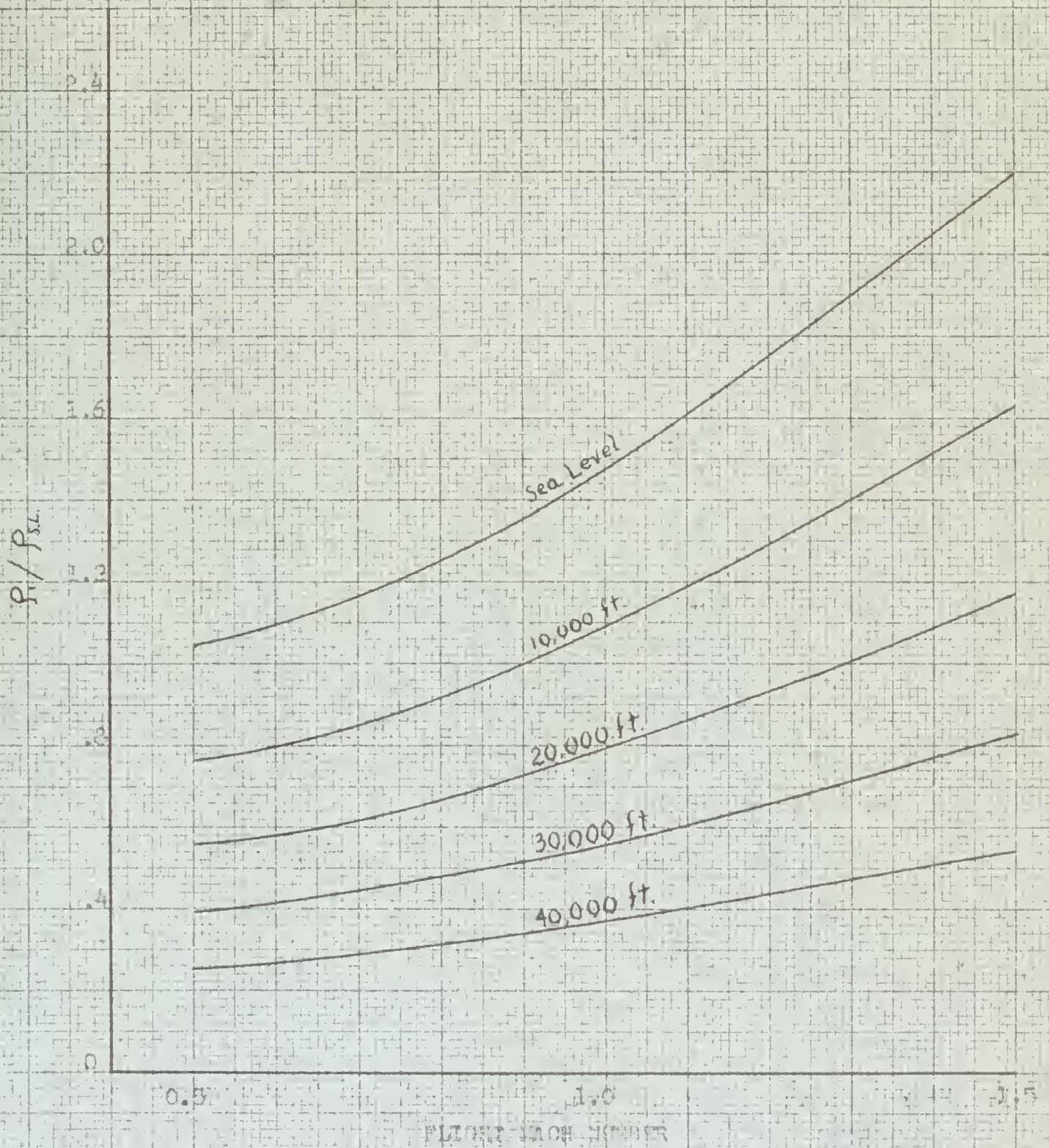


FIG. 24 - VARIATION OF AIR FLOW DENSITY WITH SPEED AND ALTITUDE.

Thesis 11465
C78 Coyle

Air inlets for turbo-
jet engines through the
transonic speed range.

Thesis 11465
C78 Coyle

Air inlets for turbo-
jet engines through the
transonic speed range.

thesC78

Air inlets for turbojet engines through



3 2768 002 09035 9

DUDLEY KNOX LIBRARY