

AN
ELEMENTARY; PRACTICAL AND
THEORETICAL
TREATISE ON NAVIGATION:

WITH A
NEW AND EASY PLAN

FOR FINDING
DIFF. LAT., DEP., COURSE, AND DISTANCE BY PROJECTION.

BY M^r F. MAURY,
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SECOND EDITION, REVISED AND CORRECTED.



PHILADELPHIA:
EDWARD C. BIDDLE, NO. 6 SOUTH FIFTH STREET.

1843.

NOTICES
OF FIRST EDITION OF
MAURY'S NAVIGATION.

“U. S. N. S., New York, January 19, 1836.

“Dear Sir,—I have had much pleasure in the perusal of your “New Theoretical and Practical Treatise on Navigation;” the plan and arrangements of which are original; it contains little or nothing superfluous, and every part of it appears to be as clear and intelligible as the nature of the subject will admit. Such a work has long been wanted in our Naval Schools, and on board our vessels of war. I intend to make use of it in the Naval School on this station; and I recommend it to be used by all the professors of Mathematics, and Nautical Science in the Navy of the United States.

Yours respectfully,
EDW. C. WARD.
“Passed Midshipman M. F. Maury. Prof. Math. U. S. Navy.”
U. S. Navy.”

“U. S. Navy Yard, Gosport, March 7, 1836.

“I have examined a Treatise on Navigation written by M. F. Maury of the U. S. Navy; and have no hesitation in recommending it to the students of that science. The explanations are clear, the rules are illustrated by many examples, and the new arrangement of some of the tables exemplify the calculations of the navigator. Mr. Maury is deserving of great credit for the work, and I wish him every success.

P. J. RODRIGUEZ.

“Navy Department, April 9, 1836.

“Sir,—I have to request that you will add the “New Theoretical and Practical Treatise on Navigation,” by M. F. Maury, Passed Midshipman, to the list of books furnished vessels of the navy going to sea.

I am respectfully yours.

(Signed,) M. DICKERSON.”

“COM. JOHN RODGERS,
President of the Board of Navy Commissioners.”

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PREFACE.

THE object of the present volume, is to place in the hands of students, and especially of the Midshipmen of the United States Navy, a Text Book, in which the theory as well as the practice of Navigation, is explained and taught.

It is not pretended that new theories are set forth, or that new principles are established in this work; but it is believed that those which have already been established, are here embodied in such a form, that the means of becoming a theoretical as well as a practical navigator, are placed within the reach of every student.

For this purpose the works of Bonnycastle, Colburn, Hutton, Legendre, Davies, Bowditch, Lardner, Hassler, Kelly, Keith, and La Place, have been consulted.

Care has been taken to introduce only those theorems upon which the problems in Navigation immediately depend, and which it is necessary to understand, in order, satisfactorily to comprehend the principles of Mathematics and Astronomy, involved in the solution of these problems.

The fear of introducing more than is essentially requisite for this purpose, may have led to an error on the other extreme, by causing something to be omitted, which should have been inserted; but if such a fault be detected in the work, while it will be readily admitted on one hand to be a fault, it can scarcely be unjust on the other, to say that the error is on the safe side; especially when they who judge, are reminded, that there is not throughout the whole work, a single principle laid down which does not serve at once as a rule, or as the basis of a rule, or as reference in some succeeding demonstration, position, or explanation either to prove, establish, or elucidate; and moreover, that there are many, (perhaps the greater number,) of those for whose benefit the work is chiefly designed, who, during the whole period of their service at sea, never have the advantage of instruction from a teacher of Navigation; consequently they have to depend upon their own exertions, and the books before them, for their proficiency as Navigators. How necessary is it then, that the work on Navigation for them, should be an elementary one, adapted to the capacity of all, and that it should not embrace the widest range; more particularly so, as there is not yet any regular system of education provided for the Navy.

The idea of such a work as the present, grew out of the author's own experience, and was suggested to him by his own wants while

a student of Navigation ; if it be not sufficient for the supply of similar wants on the part of others, it is hoped that it will, at least, serve to provoke some more capable pen to undertake and complete what is here attempted.

A more elementary work than any hitherto published on Navigation is much required as a school book in the United States. The attention of teachers of Navigation throughout the country is respectfully invited to it.

These pages were written chiefly on board of a man-of-war, in the midst of the various calls of duty, and the thousand interruptions incident to such a place ; the author trusts that this circumstance will ensure him on the part of his brother officers, and those into whose hands his work may fall, the indulgence usually claimed for inexperienced authors.

CONTENTS.

	PAGE		PAGE
ALGEBRA.			
Definitions - - - -	3	The five circular parts - - -	87
Addition - - - -	4	Solutions of the cases - - -	88
Subtraction - - - -	5	Equivalents for sine, cos., etc. -	95
Multiplication - - - -	6	OBLIQUE TRIGONOMETRY - - -	99
Division - - - -	7	The six cases - - - -	99
Equations - - - -	8	Solutions of the cases - - -	100
Proportions - - - -	10		
GEOMETRY. PART I.		NAUTICAL ASTRONOMY.	
Definitions (of rectilineals) -	15	Figure and Motions of the earth	121
Axioms - - - -	18	Day, astronomical, sea, civil, and sidereal - - - -	122
Propositions - - - -	19	Equation of time - - - -	122
GEOMETRY. PART II.		Ecliptic and signs of the zodiac	123
Definitions (of the circle and its parts) - - - -	33	Equinoctial and solstitial points	123
Propositions - - - -	35	Year, solar and sidereal - - -	124
Proportions and ratios - - -	38	Primary planets and nodes - -	124
Axioms and propositions - - -	39	Equator and the poles - - -	125
LOGARITHMS.		Tropics and zones - - - -	126
Nature and use of - - - -	49	Latitude, meridians, and longitude	127
Multiplication and division -	57	Declination, right ascension, and horary angles - - - -	128
Involution and evolution -	57 & 58	Colures, cardinal points and hori- zon - - - -	129
Log. sines, tangs., etc. - - -	58	Zenith, azimuth circles, and prime vertical - - - -	130
PLANE TRIGONOMETRY.		Altitude, refraction, and parallax	131
Cases and problems - - - -	65	VARIATION OF THE COMPASS - - -	132
Examples for practice - - - -	74	Stereographic projection - - -	135
SPHERICS.		Azimuths and amplitudes - - -	137
Definitions - - - -	81	OF THE SUN'S RISING AND SET- TING - - - -	140
RIGHT ANGLED TRIGONOMETRY	85	Time and degrees - - - -	140
The six cases and Napier's rules	85	OF THE PLANETS, MOON, ETC.	142
		Jupiter and its satellites - - -	143
		The moon's motions and phases	143
		The motion of light - - - -	143
		Radius vector - - - -	144

	PAGE		PAGE
OF FINDING THE TIME OF DAY	145	TIDES - - - - -	182
OF LONG. BY CHRONOMETERS	147	Table for time of high water	185
The rate and error of chronometer	148		
NAVIGATION.			
LATITUDE BY MERIDIAN ALTI- TUDES - - - - -	151	Of course, distance, etc. - -	198
LATITUDE BY DOUBLE ALTITUDES	153	Explanation of Plate 1 - -	191
of the sun - - - - -	154	Loxodromic sailing - - - -	195
of two stars - - - - -	158		
of the sun and a star	161	OF TURNING DEP. INTO DIFF.	
LUNARS - - - - -	165	LONG. - - - - -	199
Latitude, time, etc., by lunars	170	MERCATOR'S SAILING - - - -	210
LATITUDE BY THE NORTH STAR	178	SURVEYING - - - - -	213
Tables for finding same - - -	180	Base line - - - - -	213
		Triangulating - - - - -	214
		Reducing soundings to low water	215

ALGEBRA.

B

ALGEBRA.

§ I. ALGEBRA is a method of computation, in which magnitudes, or quantities, are represented by means of the letters of the alphabet. These letters have no positive or fixed value; they only stand for the quantities to be computed.

§ II. In algebra, known quantities are expressed either according to their numerical value, or by the first letters a, b, c , etc., of the alphabet.

§ III. And quantities of unknown value are usually represented by the last letters, x, y, z , etc.

§ IV. In algebraical computations, certain characters, called *signs*, have been introduced, and are used in the place of written words: thus,

+ (*plus*) is the sign of addition.

− (*minus*) is the sign for subtraction.

× or . is the sign for multiplication.

= is the sign of equality.

÷ is the sign for division.

$a + b - c \times d = x + y$, or $\frac{x}{y}$, is read a plus b minus c multiplied by d equals x divided by y .

§ V. $a > b$ signifies that the former quantity (a) is greater than the latter (b).

$a < b$ signifies that the latter quantity (b) is greater than the former (a).

§ VI. ($:$) is to ($:$) as, represents equality of ratio, and denotes proportion: thus $a : b :: c : d$, (read a is to b as c is to d), signifies that the ratio of a to b is equal to the ratio of c to d , and that these four quantities are proportional.

§ VII. \smile represents the difference between any two unknown quantities between which it is placed; thus, $x \smile y$ denotes the difference between x and y .

§ VIII. ∞ signifies that the quantity standing before it, thus, $x \infty$, is infinite in value.

§ IX. The numbers 2, 3, 4, etc., placed after a letter, thus, a^2, a^3, a^4 , denotes the 2d, 3d, 4th, etc., power of the quantity which that letter represents. The second power is the *square*, the 3d the *cube*, the 4th the *biquadrate*:

$$a \times a = a^2,$$

$$a^2 \times a = a^3,$$

$$a^3 \times a = a^4.$$

§ X. The numbers 2, 3, 4, etc., placed as above, are called the *indices* of the quantities to which they are affixed.

§ XI. The quantity which is a constant multiplier in the involu

tion of a power, is called the root of that power: thus, (§ IX.,) a is the cube root of a^3 , and the square root of a^2 .

§ XII. $\sqrt{\quad}$ is called the *radical* sign; and \sqrt{x} , or $\sqrt[3]{x}$, also $x^{\frac{1}{2}}$, denotes that the square root of x is the quantity alluded to; so $\sqrt[3]{y}$, or $y^{\frac{1}{3}}$, denotes the cube root of y : and so on with the other numbers, or with letters thus placed.

The number or letter placed over the radical sign, thus, $\sqrt[4]{\quad}$, $\sqrt[5]{\quad}$, or placed thus, $x^{\frac{1}{4}}$, etc., is called the exponent.

§ XIII. A *surd* is a quantity to which the radical sign ($\sqrt{\quad}$) is prefixed, and whose root cannot be expressed by numbers; thus, $\sqrt{3}$, $\sqrt[3]{5}$, are surds.

§ XIV. A *term* is any quantity that is separated from another by a sign; thus, a , b and x , are terms in the compound quantity $a + b - x$.

§ XV. The number, (5,) or the letter, (c,) that is prefixed to any quantity, (5 a , or $c a$,) is called the *coefficient* of that quantity.

§ XVI. *Like quantities* consist of the same letters as $a b + 4 a b - 2 a b$.

§ XVII. *Unlike quantities* consist of different letters, as $x + 2 y \times a + b$.

§ XVIII. When a quantity has no sign prefixed to it, +, or plus, is understood.

§ XIX. $\sqrt{x^2 + y}$, or $(x^2 + y)^{\frac{1}{2}}$, denotes that these two quantities are as one, and that the square root of their *sum* is alluded to by the radical sign, or the exponent $\frac{1}{2}$. Thus, the square root of $64 + 36$, or $\sqrt{64 + 36}$, is $8 + 36 = 42$, but the square root of $64 + 36$, or $(64 + 36)^{\frac{1}{2}}$, under a *vinculum*, is 10, for $64 + 36 = 100$, and the square root of 100 is 10.

§ XX. Addition is performed by collecting several quantities in a more simple form: $3 a + 10 a + a = 14 a$, (read *fourteen times a*). 1 is understood to be the coefficient of every quantity that has no coefficient prefixed to it.

§ XXI. When the quantities to be cast up have unlike signs, the problem is solved, partly by addition and partly by subtraction. If the *negative* be greater than the *positive* quantities, the negative sign must be retained in the result. The sum of $6 - 10 + 9$, is 5; for 6 and 9 are here positive quantities, and make 15; and $15 - 10 = 5$: and the sum of $6 - 10 - 9$, is -13 ; for $-10 - 9 = -19$; and $-19 + 6$, or $6 - 19 = -13$. Every quantity, which has not a sign prefixed to it, is understood to be positive.

To add together, $4 x - 9 x + x + 3 x - 5 x$. Collecting all the positive quantities into one sum, and all the negative quantities into another, then taking the less from the greater, the remainder, (prefixing the sign of the greater,) is the answer. Thus:

$$\begin{array}{r}
 4 x - 9 x \\
 \quad x - 5 x \\
 3 x \\
 \hline
 8 x - 14 x = -6 x
 \end{array}$$

$$\begin{array}{r}
 -6ay^2 \\
 4ay^2 \\
 9ay^2 \\
 \hline
 \text{Ans. } 7ay^2
 \end{array}
 \qquad
 \begin{array}{r}
 10ba \\
 2ba \\
 -19ba \\
 \hline
 -7ba
 \end{array}
 \qquad
 \begin{array}{r}
 -ac \\
 7ac \\
 -9ac \\
 \hline
 -3ac
 \end{array}$$

§ XXII. If all the terms be not *like* quantities, the positive and the negative of those that are like must each be added up separately; then these two sums must be subtracted, the one from the other, and the remainder thus obtained, connected by its proper sign to the *unlike* quantities, shows the answer. To add together:

$$\begin{array}{r}
 4x + 6a - c^2 + 9y \\
 -10x - 5a + c^2 - 5y \\
 x - a + 4c^2 + 3y \\
 2x + 2a \\
 \hline
 -3x + 2a + 4c^2 + 7y
 \end{array}$$

The positive x 's are, $4x + x + 2x = 7x$; the negative are, $-10x$. The difference is, $(7x - 10x =)$, $-3x$. The positive a 's are, $6a + 2a = 8a$; the negative are, $-5a - a = -6a$. The difference is, $(8a - 6a =)$, $2a$. The positive c^2 's are, $c^2 + 4c^2 = 5c^2$; the negative is, $-c^2$. The difference is, $(5c^2 - c^2 =)$, $4c^2$. The positive y 's are, $9y + 3y = 12y$; and the negative are, $-5y$. The difference is, $(12y - 5y =)$, $7y$.

To add together:

$$\begin{array}{r}
 \sqrt{ab - a^2 + 2xy - 6x + 10a^2 - 9xy - a^2b + y - a} \\
 -\sqrt{6ab + 3a^2 + \sqrt{5ab - x + xy + a^2b - 4xy - 2x} \\
 a - c^2 + 4y - \sqrt{2ab - 2a^2 - 3xy + 4x + 14xy + a^2b} \\
 \sqrt{ab - a^2 + 2xy + 6x - a^2b + a - c^2 + 4y} \\
 -\sqrt{6ab + 10a^2 - 9xy - x - 2a^2b + a + y} \\
 \sqrt{5ab + 3a^2 + xy - 2x + a^2b} \\
 -\sqrt{2ab - 2a^2 - 4xy + 4x} \\
 \qquad \qquad \qquad -3xy \\
 \qquad \qquad \qquad 14xy \\
 \hline
 -\sqrt{4ab + 20a^2 + 2xy + 2x - a^2b + 2a - 2c^2 + 10y}
 \end{array}$$

To add together:

$$\begin{array}{r}
 y + ab + dx^3 - z^3a \\
 y + cb + bx^3 - z^3x \\
 \hline
 2y + (a+c)b + (d+b)x^3 - z^3(a+x)
 \end{array}$$

To add together:

$$\begin{array}{r}
 a + b + c - x \\
 2a - b - 2c - 2x \\
 -a + ab - c - 4x \\
 \hline
 2a + ab - 2c - 7x
 \end{array}$$

§ XXIII. Subtraction is the reverse of addition. The method of performing it consists in changing, or reversing, all the signs of the subtrahend, (i. e., making the positive negative, and the reverse,) and then proceeding as in addition; viz., by adding together like quantities that have like signs; and subtracting from each other like quantities that have unlike signs. The quantity or the quantities that result from this operation is the remainder.

To subtract $a - b$ from $a + b$.

$$\begin{array}{r} \text{Changing the signs of the subtrahend} \quad a + b \\ a - b \\ \hline \text{The remainder} \quad \underline{\underline{= 2b}} \end{array}$$

This will be readily understood by ascribing a numerical value to a and b . Let $a = 6$ and $b = 4$; now subtract $6 - 4$ from $6 + 4$; $6 - 4 = 2$, and $6 + 4 = 10$, and $10 - 2 = 8$ (or twice $4 = 2b$.)

To subtract $a + b$ from $a - b$.

$$\begin{array}{r} a - b \\ a + b \\ \hline - 2b \\ \hline \end{array}$$

To subtract :

$$\begin{array}{r} 2xy + b^2c - 3a \\ xy - b^2c + a \\ \hline \underline{\underline{xy + 2b^2c - 4a}} \end{array}$$

To subtract :

$$\begin{array}{r} 10x - y - ac \\ - 3x - 2y - 4ac \\ \hline \underline{\underline{13x + y + 3ac}} \end{array}$$

§ XXIV. In the multiplication of letters, the product of any two factors is obtained and expressed by prefixing, as coefficients, the several letters contained in the multiplier, to those of the multiplicand. Thus:

$$\begin{array}{r} x + y \\ \text{by } a + b \\ \hline \underline{\underline{ax + ay + bx + by}} \end{array}$$

§ XXV. Multiplication is denoted thus, $a \times b$; or thus, $a \cdot b$; or thus, ab .

† 1. By recollecting that a times b , and b times a , are expressions for the same product, just as 4 times 9, and 9 times 4, express the same number, it will at once be understood how there is no difference in the value of the quantity, whether it be expressed ab , or ba . But when several letters are contained in the same term, as $a \times c \times b$, it is generally expressed by the letters arranged in alphabetical order; thus, abc .

§ XXVI. To multiply $x + y$ by $a - b$. Ans. $ax + ay - bx - by$.

When terms of *unlike* signs are multiplied together, their product is negative, and $(-)$ must be prefixed to it.

§ XXVII. The product of $x + y$ by $x + y$ is $x^2 + 2xy + y^2$, or $xx + xy + xy + yy$. The former, being the shorter method of writing it, is the better. The small figures that are affixed show how many times the letter with which they are connected enters as a factor in the term.

§ XXVIII. The product of $x + y$ by $-x - y$, is $-x^2 - 2xy - y^2$.

§ XXIX. The product of $x + y$ by $x - y$, is $x^2 - y^2$; for xy occurring twice in the product, and with unlike signs, $(+ \text{ and } -)$, cancels itself.

$$\begin{array}{r}
 \text{To multiply } x^2 - y^2 + 3xy \\
 \text{by } \quad \quad \quad x + y \\
 \hline
 x^3 - xy^2 + 3x^2y \\
 \quad \quad \quad x^2y - y^3 + 3xy^2 \\
 \hline
 x^3 + 2xy^2 + 4x^2y - y^3
 \end{array}$$

§ XXX. Unless the quantity be under a vinculum, the index applies only to that letter with which it is in juxta-position. The term xy^2 denotes the product of x and y^2 ; and x^2y denotes the product of the two factors x^2 and y . The term $(xy)^2$, or $\overline{xy^2}$, denotes the square of the product of the two factors x and y . Let $x = 4$ and $y = 3$: $x^2 = 16$ and $y^2 = 9$. The value then of the first term (xy^2) is $4 \times 9 (= 36)$; of the second, (x^2y), it is $16 \times 3 (= 48)$; and of the third, ($\overline{xy^2}$), it is the square of the product, (12), of 3 and 4, ($= 144$).

$$\begin{array}{r}
 \text{To multiply } ax + ab - a^2 \\
 \text{by } \quad \quad \quad a + x + b \\
 \hline
 a^2x + a^2b - a^3 \\
 \quad \quad \quad ax^2 + abx - a^2x \\
 \quad \quad \quad \quad \quad abx + ab^2 - a^2b \\
 \hline
 ax^2 - a^3 + 2abx + ab^2
 \end{array}$$

$$\begin{array}{r}
 \text{To multiply } -5a - 4x \\
 \text{by } \quad \quad \quad 2 - a - x \\
 \hline
 -10a - 8x \\
 \quad \quad \quad 5a^2 + 4ax \\
 \quad \quad \quad \quad \quad 5ax + 4x^2 \\
 \hline
 -10a + 5a^2 - 8x + 9ax + 4x^2
 \end{array}$$

§ XXXI. When the same letter enters into both factors, the product is obtained by adding the indices or exponents of the letter, as $a^3 \times a^2 = a^5$; for $3 + 2$ is 5. And $x \times x$ is x^2 ; 1 is the index and coefficient of every letter which has no other index or coefficient expressed.

§ XXXII. Division is the converse of multiplication.

4 times b divided by 4 gives b . So a times b divided by a gives b .

$$\begin{array}{r}
 4ax \div 2x = 2a \\
 4ax \div 2a = 2x
 \end{array}$$

§ XXXIII. Division being the converse of multiplication, the product of the divisor by the quotient gives the dividend. Thus, $2x \times 2a = 4ax$.

§ XXXIV. When the dividend and divisor are powers, or are roots, of the same quantity, the index, or exponent, of the divisor, minus that of the dividend, is the quotient. Thus, $x^3 \div x^2 = x$; $x^5 \div x^2 = x^3$.

§ XXXV. When all the terms of the dividend have letters that are common to the divisor, the operation of dividing is performed

by striking out from the dividend the letters of the divisor, and dividing the coefficients. Thus,

$$\begin{aligned} 8xy + 2y &= 4x \\ 12axz + 3ax &= 4z \\ 6xy^2z + 2xy &= 3yz. \end{aligned}$$

§ XXXVI. Division is sometimes expressed without being performed, as $x + y + a$, or $\frac{x+y}{a}$.

§ XXXVII. This last quantity is a fraction. Fractions in algebra are multiplied, divided, etc., after the same manner by which such operations are performed in common arithmetic.

§ XXXVIII. Two or more quantities, with the sign (=) of equality between them, constitute an equation; as $x + 10 = 14 + 6$.

§ XXXIX. All the quantities or terms that are on either side of the sign (=) constitute a *member* of the equation; $x + 10$ is the *first*, and $14 + 6$ is the *second*, member of the equation $x + 10 = 14 + 6$. The two members, necessarily, are always equal to each other.

§ XL. In the process of solving, or reducing, an equation, the known quantities, or terms, of the equation, are all collected and arranged with their proper signs, in one member of the equation, and the unknown quantities in the other member, as $x = 14 + 6 - 10$. The value of x in this equation, is therefore equal to 10.

§ XLI. In transposing a term from one member to another, the equality of the two members of the equation is preserved, by *changing the sign* of the term transposed. By transposition, *positive* terms become *negative*, and the reverse; also the sign (\times) of multiplication becomes (\div) the sign of division, and vice versa. Thus, in the equation above $x + 10 = 20$, (or $6 + 14$;) by transposition, $x = 20 - 10$. Also, in the equation $12 \times 4 = 8 \times 6$, by transposing we have $\frac{12}{8} = \frac{6}{4}$; and the equation $a + b = x + y$, by transposition, becomes $a \times y = x \times b$.

To find the value of x in the equation $a + x - c = b + 14$; by transposing a and $-c$, and changing their signs, the value of x is obtained: it stands thus, $x = b + 14 - a + c$.

Ex. $a - x^2 + y = 90 + a - 40$. To find y ; a being in each member, and having the same sign, cancels itself, and may therefore be stricken from the equation; for if transposed, the expression would be $a - a$, which two balance each other. The value of y is obtained then, by transposing $-x^2$, when the equation stands thus, $y = 90 - 40 + x^2$; in its most simple form, thus, $y = 50 + x^2$.

Ex. $8x - 10 = 80 + 2x$. To find x ; transposing and placing the known and unknown quantities on opposite sides, the equation stands, $8x - 2x = 80 + 10$. Subtracting and adding, it becomes $6x = 90$; and $x = 15$, (by division).

Ex. $x + 2 + 10 = 14 + 8$. To find x ; $\frac{x}{2}$ or $\frac{x}{2} = 14 + 8$

—10. The value of the second member of the equation is 12; therefore $\frac{x}{2} = 12$; and by multiplication, $x = 24$.

From the two last examples, this general conclusion may be drawn, viz.:

§ XLII. When a multiplier of either member is transposed, it becomes divisor to the other member; and vice versâ.

Ex. $8x^2 + ax - 10x = 14x + 4x^2 + 16x$. To find x . x is common in every term of each member of the equation. Then, dividing by x , the equation becomes $8x + a - 10 = 14 + 4x + 16$; transposing and placing all the x terms alone in one member, $8x - 4x = 14 + 16 + 10 - a$; subtracting and adding, $4x = 40 - a$; dividing, $x = 10 - \frac{a}{4}$.

Ex. $3bx - 9ab = 3y$. To find x . Transposing, $3bx = 3y + 9ab$; dividing, $x = \frac{3y + 9ab}{3b} = \frac{y}{b} + 3a$. Therefore, $x = \frac{y}{b} + 3a$.

Ex. $\frac{x}{3} + \frac{x}{2} = 10$. To find x . Clearing the equation of fractions; 1st, $x + \frac{3x}{2} = 30$; 2d, $2x + 3x = 60$; adding, $5x = 60$; dividing, $x = 12$.

§ XLIII. Thus an equation is cleared of fractions *by multiplying every term (except the fraction itself) by the denominator*.

Ex. 1. The commander of a man-of-war is desirous of having his ship calked, that he may proceed on his voyage. His own calkers can finish the job of calking in 10 days. But he employs a gang from the shore, that could finish the whole work in 6 days, to assist his. How many days' job are there for both gangs together?

Let x denote the job of work. Then $\frac{x}{10}$ is one day's work for the ship's calkers; $\frac{x}{6}$ is one day's work for the shore gang; and $\frac{x}{10} + \frac{x}{6} = 1$ day's work for both gangs together. Clearing this equation of fractions, $6x + 10x = 60$; and $16x = 60$, or $x = 3\frac{3}{4}$, the number of days.

Ex. 2. A vessel, after an engagement, could muster only 238 able bodied men; on examining her list of sick and wounded, she found her loss in killed to be $\frac{1}{3}$ of her whole crew, and in wounded $\frac{1}{4}$ of the whole crew. What crew had she when she went into action?

Let x denote her crew when the action commenced. Thus, $\frac{x}{5} + \frac{x}{3} + 238 = x$. Clearing the equation of fractions, $3x + 5x + 3570 = 15x$; transposing, $3570 = 7x$, or $510 = x$, the whole crew when the action commenced.

§ XLIV. When the value of more than one unknown quantity is required, the problem, if definite, comprises conditions for as many equations as there are quantities required. In such cases the unknown quantities (x, y, z , etc.) have the same value in all the equations; i. e. x in one equation is equal to x in another of the same set. When the value of x, y , or z , is found, its value is substituted in its stead.

Ex. $x + y = 44$
 $x - 3y = 36$ } To find x and y ; $x = 44 - y$, and $x = 36 + 3y$; thus $44 - y = 36 + 3y$; transposing, $4y = 8$, or $y = 2$; and substituting, $x = 44 - y$, or $x = 42$.

Ex. $x + y + z = 60$
 $x + 4y + 3z = 144$
 $2x + y + 8z = 132$ } To find x, y , and z ; $x = 60 - y - z$; $x = 144 - 4y - 3z$; and $x = 66 - \frac{y}{2} - 4z$. Eliminating x ; $60 - y - z = 144 - 4y - 3z$; and $144 - 4y - 3z = 66 - \frac{y}{2} - 4z$. Transposing, to find the value of y ; $3y = 144 - 60 - 2z$, or $y = 28 - \frac{2z}{3}$; again, $7y = 288 - 132 - 8z + 6z$, or $y = \frac{156 - 2z}{7}$; eliminating y , $28 - \frac{2z}{3} = \frac{156 - 2z}{7}$; clearing the equation, $14z - 588 = 468 - 6z$; transposing, $20z = 120$ or $z = 6$.

For z , in the equation $y = 28 - \frac{2z}{3}$, substituting its value (6), $y = 28 - \frac{12}{3}$, or $y = 24$. And for z and y , in the equation $x = 60 - y - z$, substituting their values (24 and 6), $x = 60 - 24 - 6$, or $x = 30$.

§ XLV. There is another manner of expressing certain equations which do not involve more than 4 terms, and when thus expressed the terms are said to be *proportional*. Thus the proportion $3 : 4 :: 6 : 8$, is but another method of expressing the equation $3 + 4 = 6 + 8$, or $\frac{3}{4} = \frac{6}{8}$. The dots ($:$) being an abbreviation of the sign ($+$) of division; and the dots ($::$) being another form for expressing the sign ($=$) of equality, to show that the *ratio* between the quantities on each side of it is the same.

§ XLVI. Whence it may be inferred as a general rule, that, if the *quotient of two quantities be equal to the quotient of two others*, these four quantities are proportional. And,

† 1. That the ratio between either divisor and its dividend, is equal to the ratio between the other divisor and its dividend.

§ XLVII. By this rule we have $4 : 3 :: 8 : 6$, for $\frac{4}{3} = \frac{8}{6}$. This form of expression for the proportion ($3 : 4 :: 6 : 8$) first quoted, is called "*invertendo*," (from inverting the divisor and dividends,) thus $3 + 4 = 6 + 8$, and *inversely* $4 + 3 = 8 + 6$.

§ XLVIII. By the same rule we also have $3 : 6 :: 4 : 8$. This form of expression for the proportion ($3 : 4 :: 6 : 8$) is called

“*alternando*,” for by taking the terms *alternately* we have $3 \div 6 = 4 \div 8$.

§ XLIX. Whence also another general rule in proportions: that, if four quantities be proportional, they are also proportional when taken *inversely*, or when taken *alternately*.

§ L. $3 \div 4 = 6 \div 8$, by transposition $3 \times 8 = 6 \times 4$; wherefore, also, if the product of two factors be equal to the product of two other factors, those four factors are proportional, as $3 : 6 :: 4 : 8$.

GEOMETRY.

PART I.

GEOMETRY.

DEFINITIONS.

- § 1. *A point* is an atom of space.*
§ 2. *A line* (——) is length without breadth.
§ a. The track of a moving point would be a line.
§ b. The extremities of every line are points.
§ c. A line may be of any length.
§ d. Lines are either straight or curved.
§ 3. *A straight or right line* (——) is the shortest line that can be drawn from one point to another.

§ a. If two lines meet each other they form an angle.



§ 4. *A plane* is an extent, (as the surface of this page), on which the straight line will lie that joins any two points which are in that extent.

§ a. A plane is without thickness, and it may be of any length and breadth.

§ b. The limits of every plane are lines.

§ c. If two planes cross each other, the line of their intersection is a straight line.

§ 5. Two lines diverging from, or meeting in, the same point, form an *angle*.

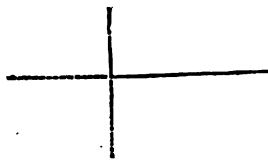


§ a. The point in which the lines join or cross each other, is called the *angular point*.

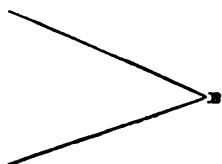
§ b. Angles are either right, acute, or obtuse.

§ 6. When one straight line stands upon another, without inclining to either side, the angle, or angles, which these two lines form, are called *right angles*.

§ a. All right angles are equal, and every one contains 90° (*degrees*). (Vide § 49, § d.)

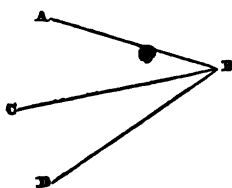


* According to the *atomic* theory of matter, all bodies are composed of indivisible and impenetrable particles, called atoms; an atom then is to matter what a point is to space; hence the idea of an atom of space.



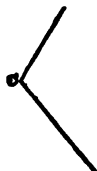
§ *b*. Straight lines that form right angles with each other, are said to be *perpendicular* the one to the other; and those that are perpendicular are at right angles with each other.

§ 7. Every angle which is *less* than a right angle, is an *acute* angle.



§ *a*. Angles are generally particularized by means of letters; as the angle B. But when there are more angles than one at the same angular point, the angle to be particularized is made known by placing the letter at the angular point *between* the letters which stand for the lines that form the angle. As the angle A B C, or C B D.

§ 8. Every angle which is *greater* than a right angle is an *obtuse* angle; as the angle C.



§ *a*. An *oblique* angle may be either acute or obtuse.

§ *b*. Two angles are equal, when they contain the same number of degrees ($^{\circ}$), minutes ($'$), and seconds ($''$), or when the lines which form an angle have the same divergence from each other, which the lines have that form the other angle.

§ *c*. The difference between an oblique angle and a right angle is the *complement* of the oblique angle.



§ 9. *Parallel lines* are lines that have always the same distance between them. They lie in the same direction, and if lengthened, *ad infinitum*, would neither

approach, or recede from, each other.

§ *a*. The distance of two parallel lines from each other is measured by any straight line (*p*) that may be drawn between them, perpendicularly from one to the other.

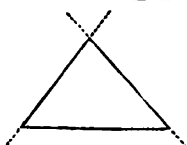
§ 10. A *figure* is any extent bounded by one or more lines, or surfaces.

§ *a*. The space included by a figure is called its *area*.

§ 11. A *superficies* is the surface of a figure.

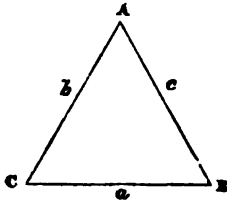
§ *a*. A superficies and a plane coincide, when a straight line, that joins any two points in the superficies, lies on that surface. The superficies of a figure is limited to the extent of the surface of that figure; but its plane is infinite.

§ *b*. When the superficies and the plane of a figure coincide, the former is called a *plane* superficies.



§ 12. A *plane triangle* is a figure that is formed by the intersection of three straight lines, any two of which intersect the other in different points.

§ *a*. The intercepted parts of these lines are called the *sides* of the triangle.



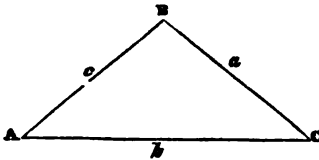
§ b. Every triangle has six parts; viz., three sides, and three angles.

§ c. Triangles, with regard to their sides, are either equilateral, isosceles, or scaline; with regard to their angles, they are either acute, right, or obtuse angled.

§ 13. An equilateral triangle has its sides all equal to each other; viz., b equal to a or c .

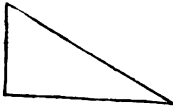
§ 14. An isosceles triangle has two equal sides; as, c and a .

§ a. An isosceles triangle may be either acute, right, or obtuse angled. Its third side (b) is its base.

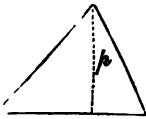


§ 15. A scaline triangle has none of its sides equal.

§ a. A scaline triangle may also be right or oblique angled.



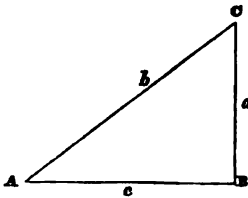
§ 16. An acute angled triangle has each of its angles less than a right angle.



§ a. The vertex of a triangle is the angle that is opposite to the base of the triangle.

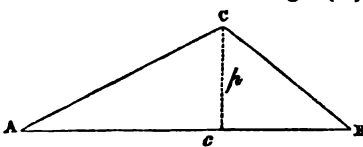
§ b. Any angle may be called the vertical angle, and consequently any side may be made the base.

§ 17. A right angled triangle has an angle (B), that is, a right angle.



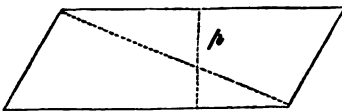
§ a. The side (b) which subtends the right angle, is called the *hypotenuse*; the two other sides (c and a) are called *legs*.

§ 18. An obtuse angled triangle has an angle (C) that is obtuse.



§ a. The altitude of a triangle is the perpendicular distance (p) of the vertical angle (C) (§ 16, § b.) from the base (c). The base must be produced to meet the perpendicular, if the perpendicular fall without the triangle.

§ b. As any side (§ 16, § b.) may be made the base of a triangle, the perpendicular distance of any angle from its opposite side may be called the altitude, or height of the triangle.

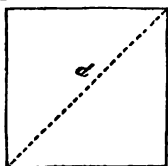


§ 19. A parallelogram is a right lined (§ 3.) quadrilateral figure, the opposite sides of which are equal and parallel.

§ a. The altitude of a parallelogram is the distance (p) (§ 9. § a.) between either pair of its opposite sides. To show the altitude of a parallelogram, either of two

D

opposite sides may be produced until it meets at right angles, a perpendicular from the other side.

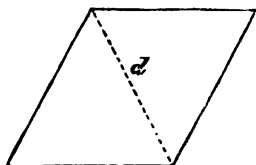


§ b. The measure or *area* of a parallelogram, is the product of its length and breadth, or of its base and altitude.

§ c. Any side of a parallelogram may be made its base.

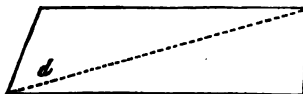
§ 20. A *square* is a parallelogram of which all the sides and angles are respectively equal.

§ a. Every angle of a square is a right angle.



§ 21. A *rhombus* is a parallelogram that has all of its sides equal to each other; but its angles are not right angles.

§ 22. A *trapezoid* is also a four-sided figure, but only two sides of it are parallel, though they are not equal.



§ a. A diagonal is a straight line (*d*) that joins two opposite angles in

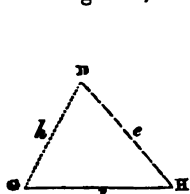
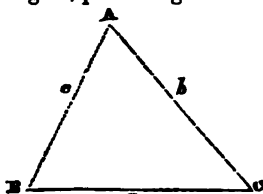
a four-sided figure.

§ b. The space included by a parallelogram is called (§ 10. § a.) its *area*, or *measure*, and is expressed (§ 19. § b.) by the product of its base and altitude.

§ 23. Two figures are *equal* when every *part* in one is equal to the part in the other, which corresponds to it; and two equal figures are always of the same magnitude.

§ a. And two figures are of the same *magnitude* when their areas are equal: a triangle and a parallelogram may be of the same magnitude, but they cannot be equal. A triangle only can be equal to a triangle; a parallelogram to a parallelogram, etc.

§ b. Two figures are *similar* when every *angle* in one is equal to the angle which corresponds to it in another figure. Figures only of the same class are similar, viz.: triangles are similar to triangles, parallelograms to parallelograms, etc.



§ c. *Homologous* sides, or angles, are the sides, or angles, which, in two equal or similar triangles, correspond by their relative positions to each other; thus *c* and *f*

are homologous sides, also *b* and *e*, and *a* and *d*.

§ d. Homologous angles are equal to each other. B and E are homologous angles; so also are A and D, and C and F.

AXIOMS.

§ 24. *Axioms* are self-evident truths, such as:

§ a. Things that are equal to the same, or to equal things, are themselves equal.

§ b. If equals be added to, or subtracted from, or substituted for, multiplied or divided by, the same or equal quantities, the sums or remainders, quotients or products, will be equal.

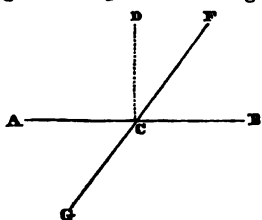
§ c. A part is less than the whole.

§ d. All of the parts are equal to the whole, and the whole to all of its parts.

PROPOSITIONS.

PROPOSITION I.

§ 25. Two straight lines which cross each other, make the two angles that are on the same side of either line, either two right angles, or equal to two right angles.

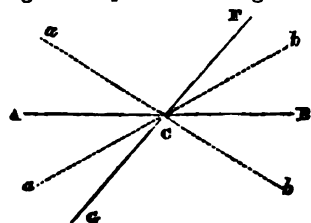


§ a. Let AB and FG be two straight lines that cross each other in C ; the two angles (FCA , FCB) on the same side of either line (AB) are either two right angles, or are equal to two right angles.

§ b. If AB and FG be perpendicular to each other, they cut each other at right angles (§ 6. § b.); and consequently each of the angles FCA and FCB is a right angle. But if AB and FG be not perpendicular to each other, from C , the point of their intersection, draw CD , which shall be perpendicular to (AB) one of them, then will DCA and DCB , the whole angular space from C , on one side of AB , be two right angles (§ 6. § b.); FCA and FCB , together, also comprehend the same angular space; therefore they are equal to $DCA + DCB$ (§ 24. § c.), which are two right angles. In a similar manner, it may be proven, that $BCF + BCG$, or $GCB + GCA$, or $ACG + ACF$, are equal to two right angles.

PROPOSITION II.

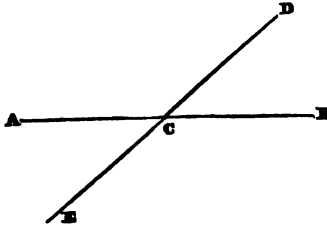
§ 26. All the angles, that any number of straight lines, which cross each other in the same point, make with each other, are together equal to four right angles.



§ a. Since the two angles (§ 25.) FCA , FCB , are equal to two right angles, and also GCB , GCA , equal to two right angles; the four angles FCA , FCB , GCA , GCB , which two straight lines make by crossing each other, are equal to four right angles. If these four angles be divided into any number of other angles, by straight lines ab , ab , crossing in the point C , the

sum of the divisions thus made will be equal (§ 24. § d.) to four right angles.

PROPOSITION III.

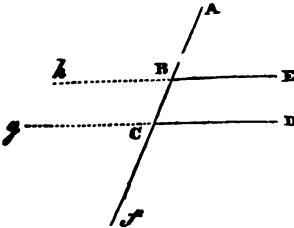


§ 27. When two straight lines A B, D E, cross each other, they make the angles D C B and A C E, or A C D and B C E, that are vertically opposite, equal to each other.

§ a. The angles A C D and D C B, (§ 25.) are together equal to two right angles; by the same proposition A C D + A C E, are also equal to two right angles; wherefore (§ 24. § c.) A C D + D C B = A C D + A C E; and A C D is a term in each member of the equation, and being taken away or cancelled, we have (§ 24. § b.) D C B = A C E.

§ b. It may be demonstrated in a similar manner, that the vertical and opposite angles A C D and B C E, are equal to each other.

PROPOSITION IV.



§ 28. When a straight line (A C) crosses two others (B E and C D) that are parallel, it makes the angles (A B E and A C D), which are on the same side of the two lines, equal to each other.

§ a. If the straight line A C cross the two others perpendicularly, the proposition becomes evident, for the angles formed would be (§ 6. § b.) right angles, and consequently equal.

§ b. But if they cross obliquely, it is obvious that if two lines be parallel to each other, they must have the same divergence from any straight line which crosses them; wherefore (§ 8. § b.) A B E = A C D; for B E and C D have the same divergence from A C.

§ c. In the same manner it may be shown that E B f is equal to D C f.

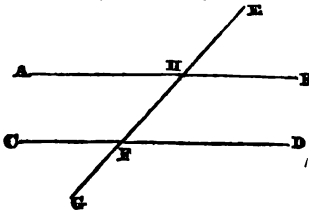
§ d. The angles (A B E, h B f, A C D, g C f, etc.) taken alternately on each side of A f, are called *alternate* angles.

§ e. The angles (A B h, A B E, f C g, and f C D,) on the outside of the two parallel lines are called the *external* or *exterior* angles.

§ f. And the others are called *internal* or *interior* angles.

PROPOSITION V.

§ 29. A right line that crosses two others which are parallel, makes the interior angles (§ 28. § *f.*) ($A H G$ and $D F E$) that are alternate (§ 28. § *d.*) equal to each other.

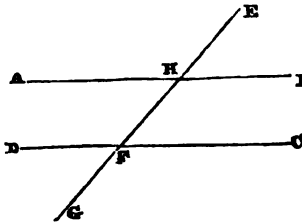


each other.

§ *a.* $A H G$ and $E H B$ are opposite and vertical angles, wherefore (§ 27.) they are equal to each other, and $E H B$ (§ 28.) is equal to $D F E$; therefore (§ 24. § *a.*) $A H G$ is equal to $D F E$.

§ *b.* In the same manner it may be proven that the alternate and interior angles $B H F$ and $C F H$ are equal to

PROPOSITION VI.



§ 30. If a straight line cross two others that are parallel, it makes the sum of the two internal angles ($B H F$ and $H F C$) that are on the same side of it, equal to two right angles; and the alternate (§ 28. § *d.*) angles ($E H B$, $A H F$, $H F C$, and $D F G$) equal to each other.

§ *a.* The angles $B H E$ and $B H F$ (§ 25.) are together equal to two right angles, and (§ 28.) $B H E$ is equal to $H F C$, therefore (§ 24. § *b.*) the internal angles ($B H F$ and $H F C$) that are on the same side of $E G$, are together equal to two right angles.

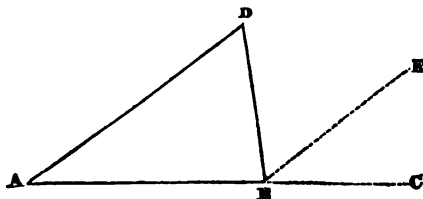
§ *b.* The alternate angle $E H B = A H F$, and $H F C = D F G$, because (§ 27.) they are vertically opposite; and (§ 29.) $A H F = H F C$; wherefore (§ 24. § *a.*) the alternate angles $E H B$, $A H F$, $H F C$, and $D F G$, are equal to each other.

§ *c.* After the same manner of demonstration, it may be proven, that the alternate angles $A H E$, $B H F$, $H F D$, and $C F G$, are equal to each other.

§ *d. Cor.* If a straight line ($E G$) cross two others ($A B$ and $D C$) so as to make the sum of the internal angles (§ *a.*) ($B H F$ and $H F C$) on the same side of it, equal to two right angles; or the alternate angles (§ *b.*) ($E H B$, $A H F$, $H F C$, and $D F G$), equal to each other; or an exterior angle (§ 28.) ($E H B$) equal to its alternate and internal angle ($H F C$), these two straight lines are parallel.

PROPOSITION VII.

§ 31. The exterior angle (D B C) which is formed by producing any side (A B) of a triangle, is equal to the two interior and remote angles (A and D) of the triangle.



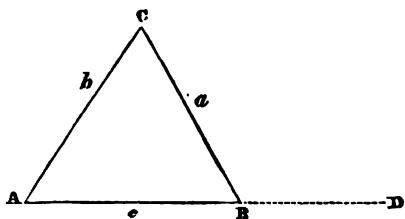
§ a. From B let B E be drawn parallel to A D ; also let A B be produced to C.

§ b. Because A D and B E are parallel (§ a.) and A C crosses them, the angles A and E B C (§ 28.) are equal to each other ; moreover D B, by crossing the same two parallels (D A and B E), makes (§ 29.) the alternate and interior angles (D and D B E) equal to each other ; the exterior angle D B C is made up of D B E and E B C, then substituting the whole for its parts (§ 24. § d.) we have (§ 24. § b.) the exterior angle D B C = A + D, the two interior and remote angles in the triangle A D B.

§ c. If either of the two other sides be produced, the proposition is proven in the same way.

PROPOSITION VIII.

§ 32. The sum of the angles of a triangle is 180° , or two right angles.



§ a. Produce a side (c) of any triangle to D. Then C B A and the exterior angle C B D (§ 25.) are equal to two right angles : and the exterior angle C B D, (§ 31.) is equal to the two remote angles C and A : therefore (§ 24. § b.) C, A,

and C B A are equal to two right angles : and C, A, and C B A are the three angles of the triangle (A C B) proposed.

§ b. *Cor.* If two angles of one triangle be known, the third is also known. It is found by subtracting the sum of the two known angles from 180° .

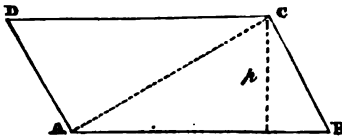
§ c. *Cor.* And the two acute angles of a right angled triangle (§ 17.) are together equal to one right angle.

§ d. Wherefore the acute angles of any right angled triangle are the complements (§ 8. § c.) of each other.

§ e. It is also evident from the above, that if two angles in one triangle be equal to two angles of another, the remaining angles are also equal to each other.

PROPOSITION IX.

§ 33. A diagonal (A C) of a parallelogram divides the parallelogram into two equal (§ 23.) triangles (A C D and A C B).



§ a. The opposite sides of a parallelogram (§ 19.) are parallel and equal to each other; wherefore $D C = A B$, $A D = C B$, and A C is common to the two triangles (A C D and A C B); therefore their sides are equal,

those of the one to those of the other. The angles D C A and C A B are equal to each other (§ 30.), for they are alternate angles (§ 28. § d.) made by A C crossing the two parallels D C and A B. For the same reason the alternate angles D A C and A C B made by A C with the parallels A D and C B, are equal to each other. Wherefore, the two angles (D C A and D A C) in one triangle being equal to two angles (A C B and C A B) in another, the remaining angles (D and B) (§ 32. § e.) are also equal to each other. Therefore, the triangle A C D having its sides and angles respectively equal to the sides and angles of the triangle A C B, is equal (§ 23.) to the latter, and the diagonal (A C) divides the parallelogram D A B C into these two equal triangles.

§ b. Scholium. The area (§ 10. § a.) of a parallelogram (§ 19. § b.) is the product of its base and altitude. The triangle A B C and the parallelogram D A B C have the same base (A B) and altitude (p), and the triangle is proven to be *half* of the parallelogram; Therefore,

§ c. Cor. The area or magnitude of a triangle is the product of its base by *half* its altitude.

§ d. Cor. The triangles into which a diagonal divides a parallelogram are both equal and (§ 23.) of the same magnitude.

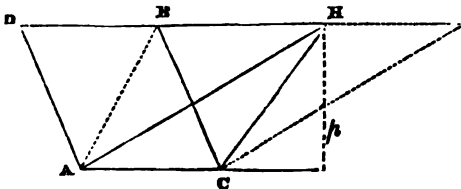
§ e. Scholium. $D A C + B A C$ (§ a.) = $D C A + B C A$, and $D = B$. Therefore,

§ f. Cor. The opposite angles of a parallelogram are equal.

§ g. Cor. If the opposite angles of a quadrilateral figure be equal, figure is a parallelogram.

PROPOSITION X.

§ 34. If a parallelogram (D A C B) and a triangle (A B C) stand upon the same base (A C), and between the same parallels (D B and A C), they have the same altitude (p), and the triangle is equal to *half* the parallelogram.



§ a. If one side (A B) of the triangle be diagonal to the parallelogram, the triangle falls within the parallelogram, and (§ 33.) the proposition is proven.

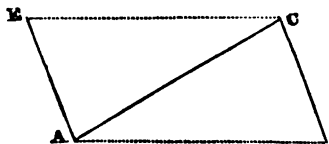
§ b. But if the vertex (H) of the triangle proposed, fall without the parallelogram, as A H C, continue one of the parallels (D B) on, through the vertex H, to E; and upon the base A C construct the parallelogram A H E C, to which the side H C of this triangle is diagonal (§ 22. § a.), therefore A H C (§ 33.) is half of the parallelogram A H E C. The parallelograms A H E C and D A C B (§ 19. § a.) have the same base (A C) and altitude (p), and the area of each (§ 19. § b.) is the product of A C by p ; wherefore (§ 24. § b.) these two parallelograms are of the same magnitude; therefore (§ 24. § a.) the triangle A H C is also equal in *magnitude* to half of either parallelogram, say D B C A; and p (§ 18. § a.) is also the altitude of the triangle A H C.

§ c. *Cor.* If a triangle and a parallelogram have their bases and altitudes equal, the triangle is equal in magnitude to half the parallelogram.

§ d. *Cor.* Triangles which have the same or equal bases and altitudes, are of the same magnitude.

PROPOSITION XI.

§ 35. When two sides (A C and C B) of any triangle (A C B) are equal to two sides (E A and A C) of another (A E C), if the angles (A C B and C A E), which these sides contain, be equal, the two triangles are equal.



§ a. Let one of the equal sides (A C) be made common to the two triangles proposed, by constructing them on opposite sides of it; the figure A E C B, thus formed, will be a quadrilateral.

§ b. By the conditions of the proposition, the angle E A C = A C B, and they are alternate angles, made by A C with the equal lines E A and C B, therefore (§ 30.) E A and C B are parallel; and the opposite straight lines (E C and A B) which join their extremities are also parallel, wherefore (§ 30.) the alternate angles E C A and C A B are equal to each other.

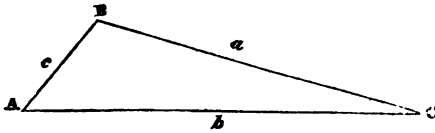
§ c. E and B are the remaining angles of the two triangles, and (§ 32. § e.) they are equal to each other, for (§ b.) E A C + E C A = A C B + C A B, therefore the angles of the two triangles proposed are equal to each other.

§ d. Now, since E A C + B A C = E C A + B C A the whole (§ 24. § d.) E A B is equal to the whole E C B; and (§ c.) E = B; these four are the opposite angles of the quadrilateral A E C B, which therefore (§ 33. § g.) is a parallelogram, and (§ 19.) E C = A B, and (§ 33.) A C divides the parallelogram into the two equal triangles A C B and A E C.

§ e. *Cor.* If the opposite sides of a quadrilateral figure be either parallel or equal, the figure is a parallelogram.

PROPOSITION XII.

§ 36. Either side (b) of any triangle is less than the sum of the two other sides (a & c).

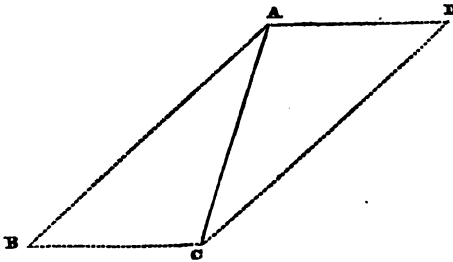


§ a . The straight line b , which joins the two points A and C, is less than the two straight lines c and a which join the same two points,

because the shortest distance between any two points (A and C) (§ 3.) is the straight line (b) which joins them; wherefore b is less than the sum of the two other sides of the triangle, or of any two lines that can join A and C.

PROPOSITION XIII.

§ 37. Any two triangles (C A B and D C A) are equal, if a side (A C), and the two angles (B A C and B C A) adjacent to it, in the one, be respectively equal to a side (C A) and the two angles (A C D and C A D) adjacent to this side in the other.



§ a . Let the equal side (A C) be made common, by constructing the two proposed triangles upon it, so that one of them may be on each side of the common line A C; the figure (B A D C) thus formed is a quadrilateral, and the side A C,

which is common to the two proposed triangles, is a diagonal of it.

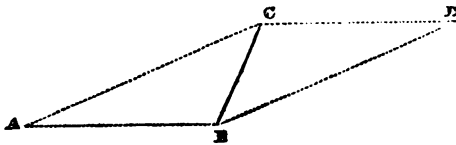
§ b . By the conditions of the proposition, the angles B A C and A C D are equal, and (§ 28. § d .) they are alternate angles, wherefore (§ 30. § d .) the two opposite sides (B A and C D) of the quadrilateral, are parallel. By supposition also, B C A and C A D are equal, and they are likewise alternate angles, wherefore (§ 30. § d .) the other two opposite sides (B C and A D) of the figure, are parallel.

§ c . If the opposite sides of a quadrilateral figure (§ 35. § e .) be parallel, the figure is a parallelogram; therefore B A D C is a parallelogram, and it is divided by the diagonal A C into the two proposed triangles C A B and D C A, which (§ 33.) are therefore equal to each other.

PROPOSITION XIV.

§ 38. Any triangles (B C A and D B C) are equal, if two angles (A & A B C) and an opposite side (C B), in one of the triangles

be respectively equal to two angles ($D \ \& \ B C D$) and the corresponding side ($B C$), of the other triangle.



§ a. Let the equal side ($B C$) be made common to the two triangles, by constructing them so that one will be on each side of $B C$.

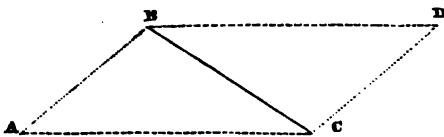
Then $B C$ becomes diagonal to the quadrilateral figure $A C D B$, which is formed by thus constructing the two proposed triangles.

§ b. By supposition, $A = D$, and $A B C = B C D$; wherefore (§ 32. § e.) the remaining angles $A C B$ and $C B D$ are equal to each other, and they are alternate angles, therefore (§ 30. § d.) the two opposite sides, $C A$ and $D B$, of the four sided figure, are parallel; the other two opposite sides, $C D$ and $A B$, are also parallel, the alternate angles $A B C$ and $B C D$ being equal, by the conditions of the proposition. Therefore, the quadrilateral $A C D B$ (§ 35. § e.) is a parallelogram, and is divided by the diagonal $B C$; (§ 33.) into the two equal triangles $B C A$ and $D B C$.

§ c. Cor. Hence it is inferred, that if two angles and a side of one triangle be equal to two angles and a side of another, the two triangles are equal.

PROPOSITION XV.

§ 39. Any two triangles ($B A C$ and $B D C$) are equal, if every side of the former be equal to its corresponding side in the latter: e. g. $A B = D C$; $A C = B D$; and $B C = C B$.



§ a. Let one of the sides ($B C$) be made common to the two triangles proposed, by constructing one of them on each side of

$B C$; the figure ($A B D C$) thus formed is a quadrilateral, and the common side $B C$ is a diagonal of it.

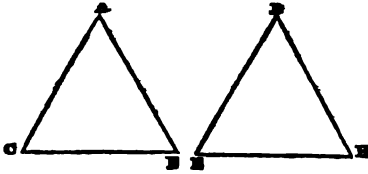
§ b. By the conditions of the proposition $A B$ is equal to $D C$, and $A C$ to $B D$, and they are opposite sides of the quadrilateral figure $A B D C$; and if the opposite sides of a quadrilateral figure be equal (§ 35. § e.), the figure is a parallelogram; therefore $A B D C$ is a parallelogram, and its diagonal $B C$ divides it into the two proposed triangles $B A C$ and $B D C$, which (§ 38.) are therefore equal.

§ c. Scholium. Since the corresponding parts in equal figures (§ 23.) are equal, it follows:—

§ d. Cor. That, if the sides of one triangle be equal to the sides of another triangle, the angles opposite the equal sides are equal.

PROPOSITION XVI.

§ 40. Every equilateral triangle ($A B C$) is also equiangular.



§ a. Let an equilateral triangle (E D H) be drawn, having its sides equal to those of the proposed triangle. The two triangles (§ 39.) are then equal, and the angles A and D which correspond, (§ 39. § d.) are equal to each other.

§ b. By the conditions of the proposition each side of A B C is equal to the same thing, and by construction, equal to either side of E D H; then $AB = EH$; and the two triangles (§ a.) being equal the angles D and C, which are opposite to those equal sides (§ 39. § d.), are equal. Wherefore A and C are each equal to D, and, therefore, (§ 24. § a.) equal to each other. In the same manner B and A may be proven to be equal to each other. Wherefore C and B are each equal to A, and consequently the equilateral triangle A B C is equiangular.

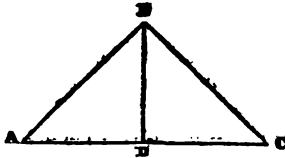
§ c. Cor. Every equiangular triangle is also equilateral.

§ d. Scholium. Since the three angles of any triangle (§ 32.) are together equal to 180° , and the three angles of an equilateral or equiangular triangle, are equal to each other:

§ e. Cor. Every angle in any equilateral or equiangular triangle; contains 60° .

PROPOSITION XVII.

§ 41. The angles (A & C) at the base of an isosceles triangle A B C (§ 14.), are equal to each other.



§ a. Let the base (A C) of the proposed triangle, be divided into two equal parts (A D & D C) by a straight line (B D) drawn from the vertex (B) of the triangle.

§ b. This line (B D) divides the isosceles triangle into the two triangles A B D and D B C; in which every side of the one, is equal to the side which corresponds to it in the other; viz: $AB = CB$ (§ 14.) for they are the legs of the isosceles triangle A B C; $AD = DC$ (§ a.), by construction; and B D is common to both of the triangles; therefore (§ 39.) these two triangles (A B D and D B C) are equal, and the corresponding angles A and C, being opposite to the common side B D, are therefore (§ 39. § d.) equal to each other.

§ c. Scholium. $ABD = CBD$, because (§ 39. § d.) they are opposite to the two equal sides A D and D C; for a similar reason BDA and BDC are also equal to each other, and (§ 25.) these are together equal to two right angles, therefore each of them is a right angle, and the right line B D (§ 6. § b.) is perpendicular to the base (A C) of the isosceles triangle A B C; wherefore:—

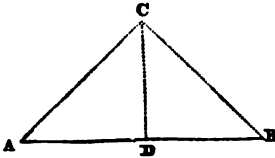
§ d. Cor. A straight line drawn from the vertex, so as to bisect

the base of an isosceles triangle, is perpendicular to the base, and it divides the vertical angle ($A B C$) into two equal parts, and the isosceles into two equal triangles. Also;

§ *e. Cor.* A straight line ($B D$) that is drawn perpendicularly from the vertex, to the base of an isosceles triangle, bisects the vertical angle and the base.

PROPOSITION XVIII.

§ 42. If only two angles (A & B) of a triangle ($A C B$) be equal, the triangle is isosceles.



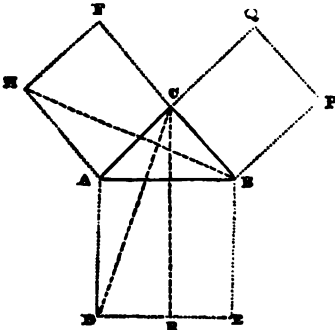
§ *a.* Call the other angle (C) (§ 16. § *b.*) the vertex of the proposed triangle; and from it, let the straight line $C D$ be drawn, so as to bisect the vertical angle (C) and divide the proposed triangle into the two $C A D$ and $C B D$, in which, by construction, the side $C D$ is common, the angles $A C D$ and $B C D$ equal, and (§ 42.) $A = B$; wherefore in these two triangles ($C A D$ & $C B D$), two angles and a side of the one are equal to the homologous angles and side of the other, and therefore (§ 38. § *c.*) these two triangles are equal to each other; consequently (§ 23.) the corresponding sides, $C A$ & $C B$, are equal, and hence, (§ 14.) the triangle $A C B$ is isosceles.

PROPOSITION XIX.

§ 43. In every right angled triangle ($A C B$), the square ($D A B E$) of the hypotenuse (§ 17. § *a.*) is equal in magnitude to the squares ($A C F H$ & $B C Q P$) of the two legs.

§ *a.* Let $D A B E$ represent the square (§ 20.) of the hypotenuse ($A B$), and $A C F H$ & $B C Q P$, the squares of the two legs $A C$ and $B C$; then (§ 43.) $D A B E = A C F H + B C Q P$.

§ *b.* From the right angle ($A C B$) let $C R$ be drawn parallel to the parallels (§ 20. & § 19.) $A D$ & $B E$, join $C D$ and $H B$.



§ *c.* The angles of a square (§ 20. § *a.*) are right angles, and all right angles (§ 6. § *a.*) are equal, therefore $H A C = D A B$; to each of these equals add the angle $B A C$, and the sums $H A B$ and $D A C$ (§ 24. § *b.*) will be equal; also $H A = A C$, because (§ 20.) they are sides of the same square $A F$; and $D A = A B$, because they also are sides of a square $A E$.

§ *d.* Wherefore, in the two triangles $A H B$ and $A D C$, the two sides $H A$ and $A B$ of the one,

are respectively equal to the two sides CA and AD , of the other, and the angles HAB and DAC , contained by these sides, are also equal (§ *c.*), therefore (§ 35.) the two triangles are equal.

§ *e.* The triangle ADC is equal in magnitude (§ 34.) to half of the parallelogram AR , for they stand upon the same base DA , and between the same parallels (§ *b.*) CR and AD . And the triangle AHB is equal in magnitude to half of the parallelogram AF , because they stand upon the same base AH , and between the same parallels HA and FCB .

§ *f.* The parallelograms AF and AR , being each double of either of the equal triangles (§ *d.*) AHB and ADC , are therefore (§ 24. § *b.*) equal to each other in magnitude; but the parallelogram AF (§ *a.*) is the square of the leg AC ; wherefore the square of the leg AC , and the parallelogram AR , are of the same magnitude.

§ *g.* By joining AP and CE , it may be demonstrated in the same manner, that the parallelogram BR , and the square (BPC) of the other leg BC , are of the same magnitude.

§ *h.* The parallelograms AR and BR make up the square ($DA BE$) of the hypotenuse (§ *a.*) AB , therefore (§ 24. § *a.*) the square of the hypotenuse (AB) is equal in magnitude to the sum of the squares of the two legs (AC & CB).

GEOMETRY.

PART II.

§ *e*. When the straight lines which contain an angle, are produced to the circumference of any circle that may be described from the angular point as a centre, that part of the circumference which the two lines intercept, contains the degrees, etc., which express the value of said angle. An angle is said to *stand* upon the part of the circumference that is thus intercepted. Neither the length of the lines which contain the angle, or the distance of it from the circumference by which it is measured, affects its angular value.

§ 50. *The radius* of a circle is a straight line (*e*) that extends from the centre to the circumference of the circle.

§ *a*. All the radii of the same, or equal circles, are themselves equal.

§ 51. *The diameter* of a circle is a straight line (A C) that passes through the centre of the circle, and is terminated at each end by the circumference of the circle.

§ *a*. Either of the two parts (A B C & A H C) into which the diameter divides the circle, is a *semicircle*.

§ *b*. *A segment* of a circle is any part (*g*) cut from the circle by a line (*f*), or a plane, which crosses the circle.

§ 52. *An arc* of a circle is any part of its circumference. That part (A H) of 'the circumference which bounds a segment (*g*) is an arc; and the straight line (*f*) which joins the extremities of an arc, is a *chord*.

§ *a*. *The complement* of an arc, or angle, is the difference between either and 90° ; and the *supplement* is what either wants of being 180° .

§ *b*. The radius and centre of a segment, or of an arc, are the radius and centre of the circle, of which the segment, or the arc, is a part.

§ *c*. Every arc or angle has its sine and co-sine, tangent and co-tangent, secant and co-secant, besides its versed sine and semi-tangent.

§ *d*. The "co" is an abbreviation for *complement*: the co-sine, co-tangent, etc., of an angle or an arc, are the sine, tangent, etc., of the *complement* of that arc or angle.

§ *e*. The sine, tangent, secant, etc., of an arc, are also the sine, tangent, secant, etc., of the supplement of that arc.

§ 53. *A chord* is a straight line (*i*) (§ 52.) that joins the extremities of an arc (B C).

§ *a*. Every arc has its chord.

§ *b*. When a chord passes through the centre of a circle, it becomes a diameter, and the arc it subtends is a semicircle.

§ 54. *A sine* is a straight line (*o*) that extends from one extremity (B) of an arc (B C) perpendicularly to the radius (*a C*) that joins the other extremity.

§ 55. *A versed sine* is that part (*s C*) of the radius which is intercepted between the sine and the extremity of the arc.

§ 56. *A tangent* is a line (*b*) that touches one extremity of an arc (B C), is perpendicular to the radius (*a C*) at that extremity,

and extends to another radius (e) produced through (B) the other extremity of the arc.

§ 57. A *secant* ($a B e$) is the produced radius (e) that intersects the tangent.

§ *a*. The co-sine, co-tangent, and co-secant, of the arc BC , are p , $D t$, and $a t$; and p (§ 19.) is equal to $a s$.

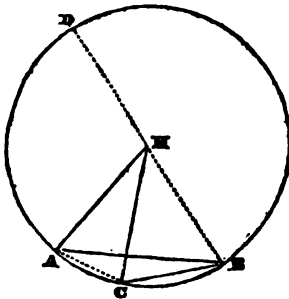
§ *b*. The sine, co-sine, tangent, co-tangent, etc., of an angle, is the sine, co-sine; tangent, co-tangent, etc., of the arc which subtends that angle.

§ *c*. These are sometimes called *trigonometric functions*.

§ 58. A *sector* is a figure (h) contained by two radii ($a B$, $a C$), and the arc ($B O$) between them.

PROPOSITION I.

§ 59. An angle ($A B C$) at the circumference, is equal to half of an angle ($A H C$) at the centre, if they stand upon the same arc ($C A$), of a circle.



§ *a*. Draw the chord AC , and from B let a diameter ($B H D$) be drawn. The radii HA , HC , and HB (§ 50. § *a*.) are equal, and the triangles $A H B$ and $C H B$ (§ 14.) are isosceles. The exterior angle $C H D$ (§ 31.) is equal to the two interior angles ($H B C$ and $H C B$) of the triangle $C H B$; for the same reason the exterior angle ($A H D$) of the triangle $A H B$, is equal to its two interior angles $H A B$ and $H B A$, which are equal to each other, because (§ 41.) they are at the base of the isosceles

triangle $A H B$; therefore $A H D$ is double of either of them, say of $H B A$. For the same reason $H B C$ and $H C B$ are equal to each other, and $C H D$ is double of either, say of $H B C$.

The difference between $C H D$ and $A H D$, is $C H A$, and the difference between their equals, viz., twice $H B C$ and twice $H B A$, is twice $A B C$. Wherefore $C H A$ (§ 24. § *b*.) is equal to twice $A B C$; or, which is the same thing, the angle ($A B C$) at the circumference, is equal to half of the angle $A H C$ at the centre of a circle, and both of them stand upon the same base.

§ *b*. An angle at the centre of a circle, is measured (§ 49. § *e*.) by the arc it stands upon; Wherefore—

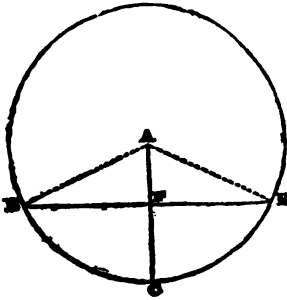
§ *c*. *Cor.* An angle at the circumference of a circle is measured by half the arc which subtends it.

§ *d*. *Cor.* All angles are equal that are at the centre, or all angles are equal that are at the circumference, if they stand upon the same, or equal arcs.

§ *e*. *Cor.* An angle that is at the circumference, and that stands upon a semicircle (§ *c*.), is a right angle.

PROPOSITION II.

§ 60. If the radius (A C) of a circle cut a chord (B H) at right angles, it bisects that chord and its arc (B C H).



§ a. Let the radii, A B and A H, be drawn to join to extremities of the chord (B H). The triangle (B A H) thus formed (§ 50. § a. & § 14.) is isosceles. And the straight line A F C bisects the vertical angle H A B (§ 41. § e.); for by the conditions of the proposition, A C is perpendicular to the chord B H, which is the base of the isosceles triangle B A H. Wherefore (§ 41. § d.) the two triangles B F A and H F A are equal, B H is bisected, and the angles B A C and

H A C are equal to each other, and being equal (§ 59. § d.) they stand upon equal arcs (B C & C H). Therefore the chord (B H), and its arc (B C H), are bisected by the radius A C.

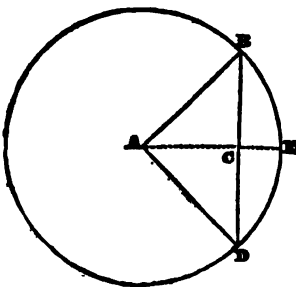
§ b. Cor. If a radius bisect an arc, it also bisects the chord of that arc, and cuts the chord at right angles.

§ c. Cor. If a radius bisect a chord, it also bisects the arc of that chord, and cuts the chord perpendicularly.

§ d. Cor. If a radius bisect a chord, or its arc, it also bisects the angle at the centre, which stands upon that arc.

PROPOSITION III.

§ 61. B C, half the chord (B D) of an arc (B E D), is the sine of C A B, half the angle (D A B) which that arc subtends.

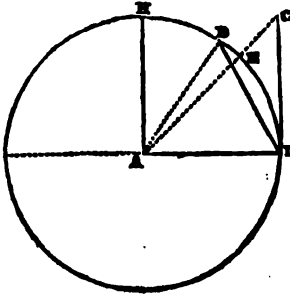


§ a. Let the chord be bisected at C, and through C let the radius A C E be drawn, then this radius (§ 60. § c.) bisects the arc B E D, cuts the chord B D at right angles, and also (§ 60. § d.) bisects the angle (D A B) which this arc subtends. Wherefore, B A C is half of the angle D A B, B C is half the chord of B E D, and it is perpendicular to the radius A C E; therefore (§ 54.) B C, half the chord of B E D, is the sine of C A B, which is half of the angle (D A B) proposed.

PROPOSITION IV.

§ 62. In any circle, radius (A D), the sine (A H) of 90°, the

chord (BD) of 60° , and the tangent (DC) of 45° , are all equal to each other.



§ a. Let A be the centre of the circle, the arc H B E D = 90° , the arc B E D = 60° , and the arc E D = 45° , and join B A and C A. The angles at the centre (A) (§ 49. § c.) are measured by the arcs they stand upon; therefore the angle D A C = 45° , D A B = 60° , and D A H = 90° ; A H then (§ 6. § b.) is perpendicular to A D, and A H (§ 54.) is the sine of the arc H B E D = 90° , it is a radius, and therefore (§ 50. § a.) equal to A D.

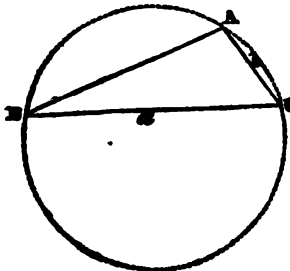
§ b. The radii A B and A D being equal (§ 50. § a.), makes the triangle B A D (§ 14.) isosceles; consequently (§ 41.) the angles A B D and A D B are equal. The angle D A B = 60° (§ 49. § c.) because it stands upon the arc B E D; wherefore (§ 32.) A B D + A D B = 120° , and being equal, the value of each is 60° ; therefore the triangle B A D is equiangular, and (§ 40. § c.) also equilateral; consequently (§ 13.) the chord (B D) of 60° is equal to radius (A D).

§ c. C D is the tangent of E D = 45° , and consequently (§ 56.) is perpendicular to A D; wherefore (§ 6. § b. & § a.) the angle C D A = 90° , and (§ 17.) the triangle A D C is right angled. The angle C A D = 45° (§ 49. § c.), because it stands upon the arc E D, therefore (§ 32. § d.) the angle A C D is also equal to 45° , and is equal to C A D, and (§ 42.) the triangle A D C is isosceles, and (§ 14.) the tangent (D C.) of 45° is equal to radius (A D).

§ d. Therefore the tangent of 45° (§ c.), the chord of 60° (§ b.), and the sine of 90° (§ a) being each equal to radius, are (§ 24. § a.) equal to each other.

PROPOSITION V.

§ 63. In every triangle, the angle (A) that is opposite to the greatest side (a) is the largest, and (B), that which is opposite to the smallest side (b), is the smallest angle of the triangle.



§ a. Describe a circle (A C H B) about the proposed triangles B A C, the circumference of which touches the three angular points (B, A, & C) of the triangle. Each side of the triangle then becomes the chord to the arc, which subtends the angle that is opposite to it.

§ b. The angle A stands upon the arc B H C, which is greater than either of the arcs (B A, A C) upon which the

two other angles (C & B) of the triangle stand. Each of these three angles (§ 59. § c.) is measured by half the arc that subtends it. Therefore A, which stands upon the greatest arc, and subtends the greatest side (a), is the largest angle of the proposed triangle.

§ c. Half the smallest arc (A C) (§ 59. § c.) measures the angle (B) that stands upon it; therefore B (the angle that is opposite to the smallest side) (b) is the smallest angle of the triangle.

DEFINITIONS.

§ 64. The *multiple* of a magnitude is the product of this magnitude and any other factor.

§ a. *Equimultiples* of magnitudes are the product of each of these magnitudes by the same or equal multipliers.

§ b. Thus, 15 and 30 are equimultiples of 3 and 6; for $3 \times 5 = 15$, and $6 \times 5 = 30$. Consequently (§ 24. § b.)—

§ 65. The same or equal multiples of equal magnitudes are equal to each other.

§ 66. *Ratio* is the relation which the value of any magnitude bears to that of another, and it is shown by dividing one magnitude by the other.

§ a. Thus, the ratio of a to b is $a \div b$, and is expressed thus,— $a : b$.

§ b. And if the ratio between two quantities (a & b) be equal to the ratio between two other quantities (c & d), this equality of ratio is expressed (§ XLV. Algebra) by writing the sign ($::$) between the two former and the two latter quantities, thus,— $a : b :: c : d$.

§ 67. *Proportion* consists in the equality of the ratios between magnitudes.

§ a. Thus, the ratio (§ 66.) of 3 to 4 is $\frac{3}{4}$; and the ratio of 6 to 8 is $\frac{6}{8} = \frac{3}{4}$; and these quantities are proportional; *i. e.* $3 : 4 :: 6 : 8$.

§ b. Four quantities are in *direct* proportion, when the 4th is equal to the quotient, which arises from dividing by the 1st quantity, the product of the 2d and 3d. Thus ($3 : 4 :: 6 : 8$), $4 \times 6 = 24$, and $24 \div 3 = 8$. So, also, $a : b :: c : d$, which in Algebra (§ XLV.) is but another form for expressing that $a \div b = c \div d$; and by transposition $a \times d = c \times b$; also, $(c \times b) \div a = d$.

§ c. The first and third (a & c) of four magnitudes that are in *direct* proportion, are called *antecedents*; and the second and fourth (b & d) are called *consequents*.

§ d. Also the first and fourth (a & d) are called *extremes*; and the second and third (b & c) are called *means*.

§ e. It is a rule in proportion, that the quantities for calculation be so arranged that the product of the two extremes be equal to the product of the two means. Thus, $a \times d = b \times c$; and as $a \times d = d \times a$. (§ XXV. †1. Algebra), $d \times a = c \times b$. Wherefore the means may be made extremes, and the extremes means; as, $b : a :: d : c$ (§ XLVIII. Alg.); the antecedents may be made consequents and the consequents antecedents; as, $d : c :: b : a$, without interrupting the harmony of the proportion between the quantities.

§ *f*. Hence if the value of three magnitudes be known, the unknown value of the fourth, which is in the same ratio of proportion, is determinable. It is the quotient that arises (§ *b*.) from dividing the product of the two means by the known extreme. Thus, $3 : 4 :: 6 -$; a 4th quantity, $4 \times 6 = 24$, and $24 \div 3 = 8$, the 4th quantity. Generally speaking, the magnitude whose value is required is expressed last in the order of proportion.

AXIOMS.

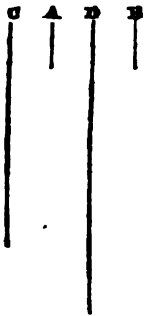
§ 69. Among quantities that are proportional, equals may be substituted for equals.

§ *a*. Magnitudes that are proportional to the same two, or to other magnitudes equal to these, are proportional to each other.

§ *b*. Equal magnitudes have the same ratio to the same magnitudes.

PROPOSITION VI.

§ 70. The same, or equimultiples (C and D), of any two magnitudes (A and B), are to each other as the magnitudes themselves.



§ *a*. Let C be the same multiple, say the 5th, of A, that D is of B; then (§ 64. § *a*.) $A \times 5 = C$, and $B \times 5 = D$; by transposition $C \div A = 5$, and $D \div B = 5$; wherefore (§ 24. § *a*.) $C \div A = D \div B$; then (§ XLVI.) $C : A :: D : B$, and alternately (§ XLVIII.) $C : D :: A : B$. Therefore, the equal multiples are as the magnitudes.

§ *b*. Scholium. The magnitude of a triangle (§ 33. § *c*.) is the product of its base and half of its altitude.

§ *c*. Wherefore the magnitudes of triangles of the same altitude, are equimultiples of their bases. And so of parallelograms of equal altitudes; and therefore,

§ *d*. Cor. Triangles, or parallelograms, that have the same altitude, are, in magnitude to each other as their bases; or those that have equal bases are to each other as their altitudes.

PROPOSITION VII.

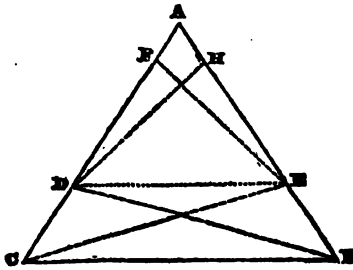
§ 71. When the product of any two quantities (*a* & *b*) equals the product of two others (*c* & *d*), the ratio of the greater multiplicand to the greater multiplier, is equal the ratio of the less multiplicand to the less multiplier; and the four quantities are proportional.

§ *a*. Let $a \times b = c \times d$ be the four quantities proposed, and let *a* be the greater multiplicand, then *d* will be the greater multiplier, *b* the less, and *c* the less multiplicand; and (§ 71.) $a : d :: c : b$.

§ *b*. By the conditions of the proposition $a \times b = c \times d$, and by transposition (§ XLII.) $a \div d = c \div b$; therefore these quantities (§ XLV.) are proportional; *i. e.*, $a : d :: c : b$, and consequently (§ 67. § *a*.) their ratios are the same.

PROPOSITION VIII.

§ 72. If a straight line (D E) be drawn parallel to the base (C B) (§ 16. § b.), and so as to cut the two sides (A C and A B) of any triangle (A B C), the sections (A D, D C, A E, & E B) of these two sides will be proportional; *i. e.*, $A D : D C :: A E : E B$.



§ a. Join D B and C E; and let E F be drawn from the vertex (E) of the two triangles A E D and C E D, perpendicularly upon A C, then (§ 18. § a.) E F is the altitude of each of these two triangles. In the same manner, by drawing D H perpendicular to A B, it is shown that the two triangles A D E and B D E have the same altitude (D H).

§ b. The triangles A E D and C E D, having the same altitude (E F), are to each other (§ 70. § d.) as their bases; *i. e.*, $A E D : C E D :: A D : D C$. And the triangles A D E and B D E are to each other also as their bases; *i. e.*, $A D E : B D E :: A E : E B$.

§ c. The triangle A D E is a magnitude in each set of these proportions; and the triangles C E D and B D E are of the same magnitude (§ 34. § d.), for they stand upon the same base (D E), and between the same parallels (§ 72.) D E and C B.

§ d. Wherefore A D and D C, A E and E B, are proportional to the same or equal magnitudes; they are therefore (§ 69. § a.) proportional to each other; *i. e.*, $A D : D C :: A E : E B$.

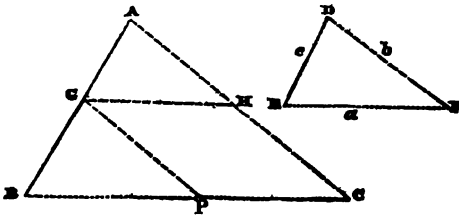
§ e. By drawing a straight line from the vertex B, perpendicularly upon A C, as a base; and another from C as a vertex, perpendicularly upon A B, it may be proven in the same way, that $A C : D C :: A B : E B$. And also that $A C : A D :: A B : A E$. Wherefore,—

§ f. *Cor.* If the two sides of a triangle be crossed by a line that is parallel to the base, these two sides will be proportional to their sections.

PROPOSITION IX.

§ 73. The homologous (§ 23. § c.) sides of similar triangles (A B C & D E F) are proportional to each other, *viz.*, $A B : c :: A C : b :: C B : a$.

§ a. By the conditions of the proposition, the triangles A B C and D E F are similar, wherefore (§ 23. § b.) their corresponding angles are equal, *viz.*, $B = E$, $A = D$, and $C = F$. Upon the two sides A B and A C of the greater triangle, (A B C) let A G be set off, equal to c, and A H = b; let G H be joined, then (§ 35.) the two triangles A G H and D E F are equal to each other; therefore (§ 23.) $G H = a$, the angle A G H = E, etc.



§ b. The angle A G H (§ a.) = E, and B = E, therefore (§ 42, § a.) A G H = B, and (§ 30. § d.) G H is parallel to B C. Consequently (§ 72. § f.) $AB : AG :: AC : AH$; by construction $AG = c$,

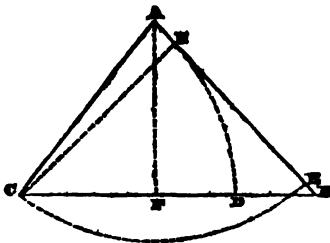
and $AH = b$; then substituting for AG and AH their equals, we have (§ 69.) the proportion $AB : c :: AC : b$.

§ c. Then by drawing from G, GP parallel to AC, the parallelogram G P C H (§ 35. § e.) is formed; and (§ 72. § f.) we have $AB : AG :: CB : CP$. But (§ 19.) $CP = GH$, and (§ a.) $GH = a$; also $AG = c$. Therefore (§ 69.) $AB : c :: CB : a$.

§ d. Cor. Whence it may be inferred, that if a straight line be within a triangle and parallel to its base, the ratio of the base to this line will be equal to the ratio of the sides to their sections.

PROPOSITION X.

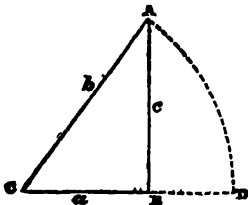
§ 74. In every triangle (ABC) the sides are proportional to the sines of their opposite angles.



§ a. From C and A, as centres, and with AC as the radius, let the arcs AD and CE be described, and draw AF perpendicular upon BC, and CH perpendicular upon AB, then (§ 54.) AF is the sine of the angle ACB, and CH is the sine of the angle CAB.

§ b. Of the two triangles BHC and BAF, the angle at B is common, the right angles AFB and CHB are equal, wherefore (§ 32. § e.) the remaining angles HCB and FAB are equal, and (§ 23. § b.) these two triangles are similar.

§ c. The homologous sides of similar triangles (§ 73.) are proportional; wherefore $AB : CB :: AF : CH$; and AF & CH (§ a.) are the sines of the angles ACB and CAB; therefore $AB : CB :: \text{sine } ACB : \text{sine } CAB$. In the same manner it may be proven that $AC : CB :: \text{sine } ABC : \text{sine } CAB$.



§ d. If the proposed triangle be right angled, and the hypotenuse be made radius, the hypotenuse becomes (§ 62. § a.) the sine of the right angle, and the legs (c and a) the sines of their opposite angles (C & A), whence we have a self-evident truth, viz., $AB : CB :: c : a$; but c and a are the sines of C and A, therefore $AB : CB :: \text{sine } C : \text{sine } A$. Also $AC : AB :: b : c$;

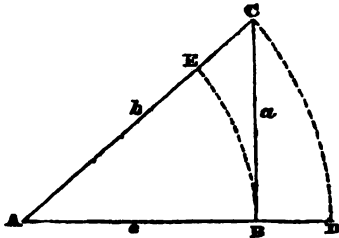
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but b is the sine of B , and c of C , therefore $AC : AB :: \text{sine } B : \text{sine } C$; and (§ 62.) the sine of B is equal to radius. By like reasoning, it is shown that $AC : CB :: \text{sine } B : \text{sine } A$. Wherefore,

§ *e. Cor.* If an hypotenuse be made radius, that hypotenuse is to either leg as radius is to the sine of the angle opposite that leg.

PROPOSITION XI.

§ 75. In every right angled triangle, the sides are proportional to the several *trigonometric functions* (§ 57. § *c.*) of the two acute angles.



§ *a.* Let the hypotenuse (b) of the proposed triangle, be made radius (AC) to an arc $CD = A$. Then (§ 54. & § 57. § *a.*) CB is the sine, and AB the co-sine of A ; likewise AB is the sine, and CB the co-sine of C .

§ *b.* Now (§ XXV. †1.) $b \times a = CB \times AC$; then (§ 71.) $b : AC :: CB : a$; by construction (§ *a.*) AC is radius, and CB is sine A or co-sine C ; therefore $b : \text{radius} :: \text{sine } A \text{ or co-sine } C : a$. Again, $b \times c = AB \times AC$, and AB (§ *a.*) is the co-sine of A , and sine of C ; therefore, $b : \text{radius} :: \text{co-sine } A \text{ or sine } C : c$. And these quantities (§ XLVII.) are also proportional, when taken inversely or alternately.

§ *c.* Let either of the legs (c) be made radius (AB) to another arc $EB = A$. Then CB becomes tangent (§ 56.) to A , and (§ 57. § *b.*) co-tangent to C ; and AC (§ 57.) the sec. of A , and co-sec. of C . And (§ XXV. †1.),

$$1st. AB \times a = CB \times c, \text{ and } (§ 71.) AB : c :: CB : a.$$

$$2d. AB \times b = AC \times c, \quad ,, \quad AB : c :: AC : b.$$

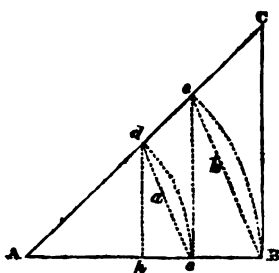
$$3d. AC \times a = CB \times b, \quad ,, \quad AC : b :: CB : a.$$

Now (§ *c.*) AB is radius, CB is tangent A , or co-tangent C , and AC is sec. A , or co-sec. C . Therefore in these three sets of proportions, the first is, radius : $c :: \text{tangent } A$, or co-tangent $C : a$. The second is, radius : $c :: \text{sec. } A$, or co-sec. $C : b$. And the third is, sec. A , or co-sec. $C : b :: \text{tangent } A$, or co-tangent $C : a$. And (§ XLVIII.) these quantities are also proportional, when taken inversely, or alternately.

§ *d.* If BC be made radius, the same method of demonstration will show that radius, the tangent and secant of C , and of its complement, are proportional to the sides (a, b & c) of the proposed triangle.

PROPOSITION XII.

§ 76. The chords (a & b), sines ($d p$ & $e s$), tangents ($e s$ & BC), etc., of equal arcs ($d s$ & $e B$), which have different radii (AB, As), are to each other, as the radius of one of the arcs is to the radius of the other.



§ a. The proposed arcs (*ds* & *eB*) are concentric; *es* is the tangent of *ds*, and *CB* of *eB*; by the definition of a tangent (§ 56.), they are perpendicular to *AB*; they are therefore parallel; and (§ 73. § d.) $se : BC :: \text{radius } As : \text{radius } AB$.

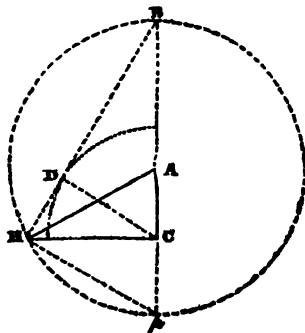
§ b. The sines (*dp* & *es*) of these two arcs, are also parallel, and by the same proposition (§ 73. § d.) $dp : es :: As : AB$.

§ c. The chords *a* and *b*, are also parallel, and, for the reason above, are to each other as, $As : AB$.

§ d. By similar methods of demonstration the secants, co-secants, co-sines, co-tangents, etc., of the two arcs, may be proven to have the same proportion to each other, which the two radii *As* and *AB* have.

PROPOSITION XIII.

§ 77. The sum (*BC*) of two sides (*CA* & *AH*) of any triangle (*ACH*), is to the tangent of half the sum of their adjacent angles (*H* & *C*), as the difference (*Cp*) between the same two sides, is to the tangent of half the difference between the same two angles; or $BC : \text{tangent } \frac{1}{2} (ACH + AHC) :: Cp : \text{tangent } \frac{1}{2} (ACH - AHC)$.



§ a. With the greatest side (*AH*) of the proposed triangle, as radius, describe the circle *BHp*, about the centre *A*. The side *AC* is extended both ways, until it forms the diameter (*Bp*) of the circle. Join *BH*, *Hp*. *DC* is drawn parallel to *Hp*.

§ b. Because $AH = AB$ (§ 50. § a.); *CA* + *AB*, or *CB* is the sum of the two sides *CA* & *AH*. And because $AH = Ap$; *Ap* — *AC*, or *Cp* is the difference between the same two sides.

§ c. The angle *BHp* (§ 59. § e.) is a right angle; then *CD* is perpendicular to *BH*, for it is drawn parallel to *Hp*; therefore (§ 30.) *CDB* is a right angle; and *BD* is tang. of *BCD*.

§ d. The exterior angle *HAB* (§ 31.) is equal to the sum of the adjacent angles (*ACH* & *AHC*); *HpB* (§ 59.) is equal to half of *HAB*, for they stand upon the same arc (*BH*); then (§ 24. § a.)

$HpB = \frac{ACH + AHC}{2}$. Because *DC* and *Hp* (§ a.) are parallel, *BCD* (§ 28.) is equal to *HpB*; therefore *BCD* is equal to

half the sum of the two angles $A C H$ and $A H C$. And in the right angled triangle $B D C$, $C B$ is the sum (§ *b.*) of the two sides $A H$, $A C$ of the proposed triangle $A C H$, and $B D$ (§ *c.*) is the tangent of $B C D$, which is half the sum of $A C H$ and $A H C$.

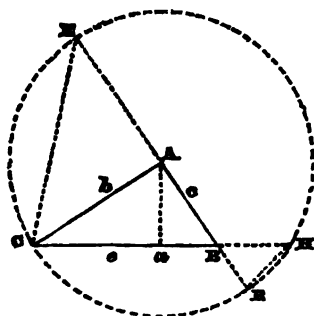
§ *e.* By § 31, the angle $A C H = C p H + C H p$. Because $A H = A p$ (§ 50. § *a.*), the triangle $H A p$ (§ 14.) is isosceles; and (§ 41.) $C p H = A H p$. Then (§ 24. § *a.*) $A C H = A H p + C H p$; from this sum, subtracting $A H C$, the remainder is twice $C H p$, which is the difference between the two angles $A C H$ and $A H C$; then $C H p$ is *half* this difference. And (§ 29.) $C H p = H C D$; therefore $H C D$ is half the difference between the angles $A C H$ and $A H C$. Now making $C D$ radius, $D H$ (§ 56.) becomes tangent of $H C D$.

§ *f.* Now $C p$ being the difference (§ *b.*) between the two sides $A H$ and $A C$; and $D C$ being parallel (§ *a.*) to the side $H p$ of the triangle $H B p$; we have (§ 72.) $B C : B D :: C p : D H$. Or,
 $C A + A H : \text{tangent } \frac{A H C + A C H}{2} :: C A \propto A H : \text{tangent } \frac{A H C \propto A C H}{2}$

§ *g.* Scholium. The half sum (§ *d.*) $B C D$ added to the half difference $H C D$ (§ *e.*) makes the greater angle $A C H$; and the half difference $C H p$ (§ *e.*) subtracted from the half sum $A H p$ (§ *e.*), gives the less angle $A H C$. Wherefore,

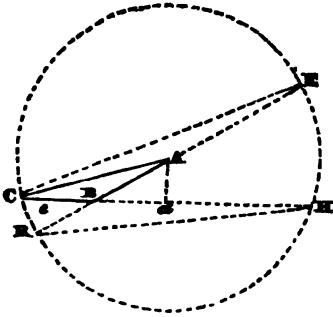
§ *h.* *Cor.* Half the difference and half the sum of any two magnitudes being added to each other, give the greater, and being subtracted from each other, give the less of the two magnitudes.

PROPOSITION XIV.



§ 79. The base (e) of any triangle ($A B C$) is to the difference between the two sides (b & c), as their sum is to twice the distance from the middle of the base to a perpendicular ($A a$) falling upon the base from its opposite angle (A); that is, $e : b \propto c :: b + c$ is to twice the distance of a from the middle of the base.

§ *a.* With a radius equal to the longer side (b) of the proposed triangle, the circle $E C R H$ is described about the angle (A) that is opposite to the base. Then b (§ 50. § *a.*) is equal both to $A E$ and to $A R$; and the difference between the two sides b and c is ($A R - c =$) $B R$; and their sum is ($c + A E =$) $B E$;



§ b. Because the perpendicular A a is drawn from the centre of the circle upon the chord C H (§ 60.), it bisects it. Then the distance of the perpendicular at a from the middle of the base (e), plus, half the base, makes up (C a) half the chord C H. Double this, and we have the whole chord C H, which is made up of twice the distance from a to the middle of the base, and twice the half of the base e. Twice the

half, is equal to the whole base e. Therefore subtracting the base e from the chord C H, the remainder (B H) is twice the distance of the perpendicular at a from the middle of the base.

§ c. The two sides C B, B E of the triangle E B C, are the base (e), and the sum of the two sides (b & c) of the proposed triangle. And the two sides B R, B H of the triangle H B R, are the difference between those sides (b & c), and twice the distance (§ b.) from the perpendicular to the middle of the base (e). These two triangles (E B C & H B R) (§ 23. § b.) are similar; for the vertical angles E B C & H B R (§ 27.) are equal; and H C E = H R E (§ 59. § d.), they stand upon the same arc (H E); and the remaining angles C E R, C H R, (§ 32. § e.) are equal. Therefore (§ 73.) the homologous sides of these two similar triangles are proportional; that is, C B : B R :: B E : B H; or, e : b ∞ c :: b + c : twice the distance of the perpendicular at a from the middle of the base.

§ d. Scholium. Then if the distance of the perpendicular from the middle of the base be added to half the base, the sum will be the greater segment (C a); or, if it be subtracted, the difference will be the smaller segment (B a) (§ 77. § h.).

§ e. The distance of each angle from the perpendicular are the segments of the base.

LOGARITHMS.

LOGARITHMS.

§ 80. The purpose of logarithms is to facilitate arithmetical calculations. The term is derived from two Greek words (*logos* and *arithmos*), and may rightly be called the language of numbers; for by means of logarithms, not only multiplication and division, but also the tedious operations of involving powers, extracting roots, etc., are simplified. They are performed by the simple process of addition and subtraction, multiplication and division.

§ a. Through the intervention of logarithms, angular and linear magnitudes are compared with each other, as quantities of the same denomination are in common arithmetic; and the unknown value of a line, arc, or an angle, may be deduced from the known ratio between other lines and angles.

§ b. Before the invention of Lord Napier had introduced into mathematical calculations the use of logarithms, the solution of trigonometrical problems was referred to synthesis, and obtained by construction. The process of finding the value of unknown quantities in trigonometry was tedious; and the result, owing to the mechanical manner in which the operation was conducted, was subject to partial inaccuracies.

§ c. If the logarithms that correspond to a series of numbers in geometrical progression, be taken out and noted down, they will be found to constitute another series of numbers in arithmetical progression. And if two series of numbers be arranged, one in the order of geometrical progression (the first term of which shall be unity or 1, and the common ratio 10), and the other in the order of arithmetical progression, (the first term of which shall be zero (0), and the common difference 1), these two series will constitute a basis, or the ground work for forming a table of logarithmic numbers, like those most generally used.

§ d. By arranging the two series of numbers, the one in geometrical, the other in arithmetical order of progression, thus,

Geometrical progression.	-	-	-	-	-	Arithmetical progression.*
1	-	-	-	-	-	0
10	-	-	-	-	-	1
100	-	-	-	-	-	2
1000	-	-	-	-	-	3
10000	-	-	-	-	-	4
100000	-	-	-	-	-	5
1000000	-	-	-	-	-	6
10000000	-	-	-	-	-	7
100000000	-	-	-	-	-	8
1000000000	-	-	-	-	-	9
10000000000	-	-	-	-	-	10,

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the relation and connexion between the orders of the two series will appear. The terms in the order of arithmetical progression, are the logarithms of those in the geometrical order: each the logarithm of the term to which it is opposite; i. e., 0 is the logarithm of 1; the logarithm of 10 is 1, of 100 is 2, of 1000 is 3, of 10,000 is 4, and of 100,000 it is 5, etc.

§ e. By observing the different relations which exist between the terms in the two series above, it appears,—

1st. That the logarithm of any whole number has for its index the figure, which expresses the number of digits, *minus one*, that are in the natural number for which the logarithm is required. Thus 1 is the logarithmic index of 10, which has two digits; 2 is the logarithmic index of 100, which has 3 digits; 3 of 1000; 4 of 10,000, etc.

2d. That the logarithm of any number intervening between 1 and 10, must be a fraction less than unity; for the logarithm of 1 is 0, and of 10 it is 1; then the logarithm of any number between 1 and 10 must be less than 1. The logarithm that corresponds to any number between 10 and 100, must be greater than 1 and less than 2, etc.

3d. That the product of any two numbers in the series of geometrical progression, answers to the sum of the two numbers in the arithmetical order, which correspond to them. Thus; 100,000,000 in the geometrical, answers to 8 in the arithmetical order, and 100,000,000 is the product of $1000 \times 100,000$, which two numbers correspond with 3 and 5 in the arithmetical series; and in this series $3 + 5$, or $8 = 100,000,000$ in the geometrical series. Now 3 is the logarithm of 1000, and 5 of 100,000. Hence, therefore, if the logarithms of any quantities whose product is required, be added together, this sum will be the logarithm of the required product.

4th. That the difference (4) between any two numbers (2—6) in the series of the arithmetical order of progression, is the logarithm of the quotient (10,000) which arises from dividing by each other, the two numbers ($1,000,000 \div 100$) that correspond, in the geometrical order, to the two said arithmetical terms (2 and 6). And,

5th. That logarithms of numbers are a series of terms in the order of arithmetical progression, which series corresponds to another series of numbers in the order of geometrical progression.

§ f. The logarithm of 10 is not necessarily 1. Any other number as well as 1 may be assumed as the logarithm of 10. But if any other number were taken as the logarithm of 10, it would establish another base for calculating a table of logarithms, and this change would effect the logarithm of every other number in the same ratio. From this it appears that the value of a logarithm is entirely conventional. But in order to simplify, and facilitate their application to practice, mathematicians have assumed, in the order of geometrical progression, a series of numbers in the ratio of 1, 10, 100, 1000, 10,000, etc.; and as logarithms to these, they have assigned, in arithmetical progression, a series of numbers in the

order of 0, 1, 2, 3, 4, etc., having 1 for the common difference. The latter numbers, taken in the order in which they stand, are called the logarithmic *indices*, or *characteristics*, of the former, taken in the same order. Whence (§ e. 1st) the logarithmic index of every whole number, is made always to express *one less* than the number of digits contained in the whole number. Thus, the characteristic of 100 is 2, as the number of digits or figures in 100, is 3. The number of digits in 1000 is 4, and the logarithmic characteristic of 1000, is 3.

§ g. The logarithmic signs and tangents, co-sines and co-tangents, etc. of degrees, minutes, and seconds, are also of conventional value. They are expressed in parts of the radius of a circle; the value of which radius is assumed to be equal to 10,000,000, etc., with as many ciphers affixed as the compiler intends the *mantissa* shall consist of digits.

§ h. The *mantissa* is the decimal part of a logarithm; or the part which is not the index. The logarithm of 250 is 2 .397940; 2 is the index, and .397940 is the mantissa.

§ 81. The characteristic of a logarithm depends upon the number of digits which are contained in its *geometrical** number; being one less than the number of digits, it is known by counting the figures of the geometrical number, and writing down one less than their number for the index.

§ 82. The mantissæ have been previously calculated and arranged in a tabular form, and in such a manner that the mantissa for any geometric number, (however great or small), may be determined with readiness.

§ 83. The first column of the tables (I.) is marked N. (Numbers.) It contains the geometrical numbers, from 1 to 999. The mantissa of each term in this series, is in a line with its geometrical number, and in the next column which is marked 0. The nine other columns, headed with the cardinal numbers 1, 2, 3, etc., to 9, also contain mantissæ; but these are of geometrical numbers that have *four* digits; the last figure of which, being found at the head of one of these columns, and the three first in the first column (N), show at their angle of meeting, the proper mantissa. Thus, the logarithm of 3681 is 3.565966; 368 being found in the first column, N., the mantissa for 3681 is found in a line with 368, and in the column, at the top and bottom of which, stands 1.

§ 84. To take from the table (I.) the mantissa for any geometrical number less than 1000.

§ a. Find the given number in the first column (N.); its mantissa is opposite to it in the next column (0).

§ b. The mantissa for 9 is .954243; for 14 it is .146128; and for 964 it is .984077.

* The natural numbers, which correspond to, or are represented by, a logarithm, are here called *geometrical* numbers, from their being terms in the geometrical series¹ of progression. Thus 419, of which 2.622214 is the logarithm, is the *geometrical* number of log. 2.622214.

§ c. These mantissæ, with the proper characteristics prefixed, constitute the logarithms of those numbers; thus, logarithm of 9 = 0.954243; of 14 = 1.146128; and of 964 = 2.984077.

§ 85. To take from the tables, the mantissa for any geometrical number that is greater than 1000, but less than 10,000.

§ a. Find, in the first column (N.) of the tables, the three first figures of the proposed number; in a line with them, and in the column over which the fourth figure stands, is the proper mantissa.

§ b. The mantissa (.973590) for 9410 is found in the column marked (0), and opposite to 941 in the first column; and the mantissa (.954918) for 9014, is found in the column marked (4), and opposite to 901 in the first column (N.).

§ c. The geometrical numbers in this case have four digits; 3, then, is the characteristic of their logarithms; which are, 3.973590 = 9410; and 3.954918 = 9014.

§ 86. To take from the tables the mantissa of any geometrical number that has more than *four digits*, or that is greater than 10,000; say of 43568.

§ a. Take out the mantissa for the four first digits (§ 85. § b.), and subtract it from the mantissa next in order. Then say,—If unity (1), prefixed to as many ciphers as there are digits remaining of the proposed geometrical number, give this mantissal difference, what mantissal difference will the remaining digits of the geometrical number, give? This last mantissal difference being added to the mantissa for the four first digits, produces the required mantissa.

§ b. The mantissa for the four first digits (4356) of 43568 is .639088; the mantissal difference between this and the next (.639188) in order, is .000100; one digit (8) of the proposed geometrical number remains; and unity (1) (§ a.) must be prefixed to one cipher (0), which makes (10); then the order and terms of the proportion are, 10 : .000100 :: 8 : .000080. This last term, *plus* the former mantissa, (or .639088 + .000080) = .639168, the mantissa required.

§ c. The geometrical number (43568) in this example has *five* digits; then (4) being prefixed as an index to the mantissa (.639168) makes the logarithm of 43568 = 4.639168.

§ d. The mantissa for the four first digits (7419) of 741946 is .870345; the difference between the mantissa of 7419, and of 7420, is .000059. And the order and terms of the proportion are, 100 : 000059 :: 46 : .000027. This last term being added, and the characteristic (5) being prefixed to the mantissa (.870345), makes the logarithm of 741946 = 5.870372.

§ e. The mantissa for the four first digits (5941) of 594106734 is .773860; the mantissal difference = .000073; the remaining digits (06734) are *five* in number. Prefixing 1 to *five* ciphers, the proportion is 10000 : 000073 :: 06734 : 000004. Prefixing the characteristic (8) to .773860 + 000004, makes the logarithm of 594106734 = 8.773864.

§ f. The mantissa for 124, and the mantissa for 1240000000 are

the same (.093422). But the logarithm of $124 = 2.093422$; and the logarithm of $1240000000 = 9.093422$. Hence,

§ g. The effect of final ciphers in a geometrical number, on its logarithm, is confined to the characteristic of the logarithm, for the logs. (§ f.) of 124 and 1240000000 have the same mantissa.

§ 87. To find the logarithm of a geometrical number that is mixed with a decimal fraction.

§ a. The mantissa is found as it would be, were the proposed number integral; but the characteristic of the logarithm must express one less than the number of digits in the *integral* part of the number proposed. Thus;

Mixed Geometrical Nos.	Their Logarithms.
9414.5 - - -	= 3.973797
941.45 - - -	= 2.973797
94.145 - - -	= 1.973797
9.4145 - - -	= 0.973797

§ 88. As the logarithm of unity, or (1), is 0, it follows that the logarithm of any quantity less than unity, or the logarithm of a fraction, must be less than 0; that is, it is a *negative quantity*. Thus,—

Logarithm of 1 =	0 .000000
Logarithm of 0.1 =	-1 +.000000
Logarithm of 80 =	1 .903090
Logarithm of 0.08 =	-2 +.903090

§ a. But the use of negative and positive quantities (such as the logarithms of integers and of fractions, as just quoted above), in the same operation, has a tendency sometimes to perplex the calculator. It is better, therefore, that all quantities in the same sum should be affected with like signs. This may be effected with the logarithms of fractions by means of a little artifice, by which negative quantities are made to change their signs, or become as positive quantities.

§ b. This artifice consists in borrowing and applying 10, or 20, or 100, etc., to the logarithmic index of the fraction, and restoring the borrowed quantity again during the progress of the calculation. Thus, in the summing up of the logarithms of 80, and of 0.08, instead of adding the mantissæ and subtracting the characteristics of the two logarithms ($1.903090 - 2 + .903090 = 0.806180$), the operation may be performed entirely by addition, if the arithmetical complement of -2 , which is 8, be used as the index; thus, $1.903090 + 8 + .903090 = 10.806180$; rejecting the 10, which was borrowed in the logarithmic index of 0.08, there remains 0.806180.

§ c. Any quantity with the sign (—) prefixed, may be commuted into a positive quantity by substituting for that quantity its *arithmetical* complement. In this way subtraction may be performed by addition, as we have seen (§ b.) in the case of the negative index -2 .

§ d. The *arithmetical complement* of a number, is the difference

between that number, and the first number that ends with a cipher, and is one scale higher in the decimal order of notation. The arithmetical complement of 6, is 4, ($10 - 6 = 4$); of 77, is 23, ($100 - 77 = 23$); of 115, is 885, ($1000 - 115 = 885$), etc.

§ c. If it be required to subtract 6 from 9, the result is the same, whether we say $9 - 6 = 3$, or take the arithmetical complement (4) of 6, add it to 9, ($4 + 9 = 13$), and reject the borrowed (10) from their sum ($13 - 10 = 3$).

§ 89. To find the arithmetical complement of a logarithm.

§ a. Prefix (1) to as many ciphers as there are digits in the proposed logarithm; then from this number subtract the proposed logarithm, and the remainder will be the required arithmetical complement.

§ b. Thus, the arithmetical complement of 1.903090 is 8.096910; for 1000000.

1.903090

8.096910

§ c. The same result may be obtained by beginning at the left, and subtracting from 9, every figure except the last significant one, which must be subtracted from 10.

Thus—

9.9999	(10)0
1.9030	9 0
8.0969	1 0

§ d. If the index be greater than 9, it must be subtracted from 19.

§ 90. To find the logarithm of a decimal fraction.

§ a. The mantissa for the proposed fraction is taken from the table, as for an integral geometrical number of the same significant figures which the fraction has.

§ b. The logarithm for the same figures expressed both integrally and fractionally, differs only in the characteristic; the mantissa is the same in both cases. Therefore we have only to teach how to determine a *positive* characteristic, or the logarithm of a decimal fraction.

§ c. The characteristic is determined by means of the number of ciphers which precede the first significant figure of the decimal, for the number of these subtracted from (9), gives the required characteristic.

Thus, logarithm of the decimal .301 = 9.478567

Logarithm of the decimal .0301 = 8.478567

Logarithm of the decimal .000301 = 6.478567

§ 91. To find the logarithm of a vulgar fraction that is less than unity.

§ a. Take from the tables the mantissa for the numerator, and for the denominator, separately, and as if each were a whole number expressed by the same figures. Then, from the logarithm of the numerator, *plus* 10 to the index, subtracting the logarithm of the denominator, leaves the logarithm of the proposed fraction. Thus,

§ b. To find the logarithm of $\frac{25}{100}$.

$$\begin{aligned} \text{Logarithm of } 25 &= 1.397940 \\ \text{Logarithm of } 100 &= 2.000000 \end{aligned}$$

$$\text{Logarithm of } \frac{25}{100} = \underline{\underline{9.397940}}$$

To find the logarithm of $\frac{3}{8}$.

$$\begin{aligned} \text{Logarithm of } 3 &= 0.477121 \\ \text{Logarithm of } 8 &= 0.903090 \end{aligned}$$

$$\text{Logarithm of } \frac{3}{8} = \underline{\underline{9.574031}}$$

§ 92. To find the logarithm of a mixed number.

§ a. If the number proposed (9.05) consist of a whole and a decimal fraction, take from the tables the mantissa for the mixed number as if it were a whole, and then prefix the index, *which expresses one less than the number of digits in the integral part of the mixed number proposed*. Thus, the index of the logarithm for 9.05 is 0, and for 90.5 it is 1; the mantissa (.956649) is the same for each number; because it is taken out for the figures (905) as though they stood for a whole number.

Then, the logarithm of 9.05 = 0.956649

The logarithm of 90.5 = 1.956649

§ b. But if the proposed mixed number consist partly of a vulgar fraction, let it be reduced to an improper fraction; then find the logarithm of the numerator, and of the denominator, as if they were separately whole numbers; and the remainder of logarithm of the numerator, *minus* logarithm of the denominator, is the required logarithm.

Thus, logarithm $12\frac{2}{3} = 1.102663$; for $12\frac{2}{3}$ reduced to an improper fraction is $\frac{38}{3}$; and

$$\text{Logarithm } 38 = 1.579784$$

$$\text{Logarithm } 3 = 0.477121$$

$$\underline{\underline{1.102663 = 12\frac{2}{3}}}$$

§ c. The index to the logarithm of an improper fraction, is always a *proper* index; for the numerator, being greater than the denominator of such a fraction, the logarithm of the latter can be subtracted from that of the former, without borrowing 10 in the index.

§ 93. To find the geometrical number which corresponds to a logarithm.

§ a. The number of digits in the geometrical number for a logarithm, is known by the characteristic of the logarithm; for 1 added to the *characteristic* tells the number of digits.

§ b. Find, in the table, the mantissa of the proposed logarithm. The figures in the first column (N.) being prefixed to the figure that stands at the top of the column in which the mantissa is found, compose the geometrical number that is required.

§ c. The geometrical number of log. 3.759214 = 5744.

The geometrical number of log. 2.759214 = 574.4.

The geometrical number of log. 1.759214 = 57.44.

The geometrical number of log. 0.759214 = 5.744.

This mantissa is found in the column (4) of the table, and opposite to 574 in the first column (N.).

§ d. Had the index of the logarithm been greater than (3), the number of digits for the geometrical number required, would have been made up by affixing ciphers to the numbers (574 and 4) found above, and opposite to, the mantissa. Thus, the geometrical number for 4.976854 is known (§ a.) to consist of five digits, because of the index (4). The mantissa (.976854) is found opposite to 948 (in the column N.), and under 1; making up with ciphers, the proper number of digits.

The geometrical number for 4.976854 = 94810

The geometrical number for 5.976854 = 948100

The geometrical number for 6.976854 = 9481000

§ e. If the proposed mantissa cannot be found in the tables, take that mantissa in the tables, which, being less, comes nearest to it, and affixing any number of ciphers to the difference between these two mantissæ, divide it by the difference between said tabular mantissa and the one next in order after it; the quotient, being affixed to the numbers opposite to, and at the head of the column of, said least mantissa, comprise the figures of the required geometrical number. The digits for the integral part of the geometrical number are determined by the index of the proposed logarithm (§ a.), and the figures which are to the right of these digits, constitute the fractional part of the geometrical number. Thus,

§ f. Geometrical number for 4.979744 = 95443.

Geometrical number for 2.979744 = 954.43.

Geometrical number for 0.979744 = 95.443.

The proposed mantissa (979744) cannot be found in the tables. The difference between the next less (.979730) and the next greater (979776) found in the tables, is 46; and the difference (14) between the less of these two and the proper mantissa being prefixed to any number of ciphers, (14000 - - -), and divided by the tabular difference (46), gives 3 + to be affixed to the four figures 9544, from which the required digits for the integral part of the geometrical number, are to be separated according to the index of the logarithm proposed.

§ g. If the index of the logarithm proposed be an *improper* characteristic, the geometrical number of the logarithm is a decimal fraction. And the difference between this characteristic and (9), tells how many ciphers must intervene between the decimal point (.) and the first significant figure of the fraction. Thus (the indices being *improper*),

The geometrical number for 7.911424 = 0.008155.

The geometrical number for 9.897627 = 0.79.

The geometrical number for 5.698970 = 0.00005.

§ 94. To perform multiplication by logarithms.

§ a. Add the logarithms of the factors together; the sum of these is the logarithm of the product. Thus,

§ b. To multiply 3 by 4; 20 by 2.5; and .25 by .30.

$\begin{array}{r} \text{Logarithm } 3 = 0.477121 \\ \text{“ } 4 = 0.602060 \\ \hline 1.079181 = 12 \end{array}$	$\begin{array}{r} \text{Logarithm } 20 = 1.301030 \\ \text{“ } 2.5 = 0.397940 \\ \hline 1.698970 = 50 \end{array}$
---	--

$$\begin{array}{r} \text{Logarithm } 0.25 = 9.397940 \\ \text{“ } 0.30 = 9.477121 \\ \hline 8.875061 = 0.075 \end{array}$$

§ 95. To perform division by logarithms.

§ a. Subtract the logarithm of the divisor from the logarithm of the dividend, the remainder will be the logarithm of the quotient.

§ b. To divide 36 by 3; 8941 by 19; 50 by .05; and 82.7 by 70.91.

$\begin{array}{r} \text{Log. } 36 = 1.556302 \\ \text{“ } 3 = 0.477121 \\ \hline 1.079181 = 12. \end{array}$	$\begin{array}{r} \text{Log. } 8941 = 3.951386 \\ \text{“ } 19 = 1.278754 \\ \hline 2.672632 = 470.57 + \end{array}$
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$\begin{array}{r} \text{Log. } 50 = 1.698970 \\ \text{“ } .05 = 8.698970 \\ \hline 3.000000 = 1000 \end{array}$	$\begin{array}{r} \text{Log. } 82.7 = 1.917506 \\ \text{“ } 70.91 = 1.850708 \\ \hline 0.066798 = 1.16 + \end{array}$
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§ 96. To perform involution by logarithms.

§ a. Multiply the logarithm of the proposed geometrical number by the index (§ X.) of the power to be involved; this product will be the logarithm of the required power.

§ b. Raise 8^2 17^3 112^4 516^9 .

$\begin{array}{r} \text{Log. } 8 = 0.903090 \\ \quad \quad \quad 2 \\ \hline 1.806180 = 64 \end{array}$	$\begin{array}{r} \text{Log. } 17 = 1.230449 \\ \quad \quad \quad 3 \\ \hline 3.691347 = 4913 \end{array}$
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$$\begin{array}{r} \text{Log. } 112 = 2.049218 \\ \quad \quad \quad 4 \\ \hline 8.196872 = 157351936 \end{array}$$

$$\text{Log. } 516 = 2.712650$$

9

$$24.413850 = 2593267484132083176308736$$

§ c. If the geometrical number that is proposed to be raised, be a decimal fraction, the difference between the characteristic of the logarithm of the power, and the product of 10 by the index of the power involved, expresses *one* more than the number of ciphers, that must precede the first significant figure of the required power.

§ d. To raise .17³ .05³ .064³.

$$\text{Log. } 0.17 = 9.230449$$

3

$$\text{Log. } 0.05 = 8.698970$$

2

$$27.691347 = 0.00491 +$$

$$17.397940 = 0.0025$$

$$\text{Log. } 0.064 = 8.806180$$

5

$$44.030900 = 0.000001073 +$$

§ 97. Evolution is the converse of involution.

§ a. To perform evolution by logarithms.

§ b. The quotient, obtained by dividing the logarithm of the power proposed, by the exponent (§ XII.) of the root to be extracted, is the logarithm of the root required.

§ c. To evolve the square root of 196, the $\sqrt{}$ of 81, and the $\sqrt[3]{}$ of 128.

$$\text{Log. } 196 = 2.292256 \div 2 = 1.146128 = 14.$$

$$\text{Log. } 81 = 1.908485 \div 3 = 0.636161 + = 4.326 +.$$

$$\text{Log. } 128 = 2.107210 \div 7 = 0.301030 = 2.$$

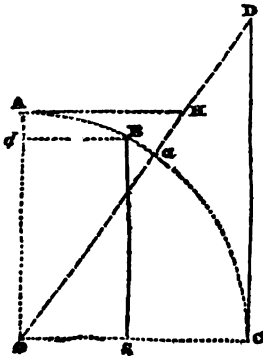
§ d. If the geometrical number whose root is to be evolved, be a decimal fraction, in order to obtain the logarithm of the root required, the exponent, *less one*, of the root to be extracted, must be prefixed to the characteristic of the logarithm of the number proposed; and then the quotient, that arises from dividing this quantity by the exponent of the root to be evolved, will be the logarithm of the power required. Thus, to find the cube root of .27. The logarithmic index of 0.27 is 9; now, to 9, prefixing *one less* (2), than the exponent (3) of the root to be evolved, makes the logarithm of $0.27 = 29.431364 \div 3 = 9.810454 + = 0.646 +$. To find the square root of 0.00776, the logarithmic index of which is (7); prefixing to 7 *one less* (1) than the exponent (2), makes the logarithm of $0.00776 = 17.889862 \div 2 = 8.944931 = 0.088 +$.

§ 98. In the tables (II.) containing logarithms for sines and co-sines,

tangents and co-tangents, the logarithms are calculated from the ratio between the radius and the sine, or the tangent of an arc.

§ a. In these tables, as in all others, the logarithmic value of a sine or a tangent is conventional, as are the logarithms of geometrical numbers.

§ b. In forming these tables, radius is taken as the base, or the ground work for the calculations; and its value is assumed to be 10.000000. The logarithmic value of the sine of 90° , or of the tangent of 45° (§ 62.), shows that this is the value with which radius enters this system. Wherefore, in every calculation, radius = 10.



§ 99. If an arc of 90° , or if a right angle, be divided into any two parts, the sine or the tangent of either part, is the co-sine or co-tangent of the other. Thus, in the quadrant ABC; $AB=30^\circ$, $BC=60^\circ$, $Aa=35^\circ$, and $aC=55^\circ$; PB is the sine of $AB=30^\circ$, and co-sine of $BC=60^\circ$; BS is the sine of 60° (BC), and co-sine of 30° (AB); therefore the co-sine of AB, is BS, which is sine of BC, and the co-sine of BC is Bp, which is sine of AB. In the same manner AH and CD are reciprocally the tangents and co-tangents of Aa and aC. Wherefore the tables, by being calculated as far as 45° , answer for the whole circle, or for two right angles.

§ 100. The logarithmic value of the sec. of an arc, or an angle, is the arithmetical complement of the logarithmic co-sine of the same arc or angle.

§ a. The logarithmic co-sec. is the arithmetical co. of the logarithmic sine, and the logarithmic co-tangent is the arithmetical co. of the logarithmic tangent, and *vice versa* (Vide § 109. § h.).

§ b. Wherefore in logarithmic tables of the trigonometric functions, it is only essential that the logarithms of the sine, co-sine, and tangent, or of the sec., co-sec., and co-tangent, should be given, for the first three are the arithmetical co. of the latter, and *vice versa*; but to facilitate beginners in their calculations, the logarithmic sine, co-sec., co-sine, secant, tangent, and co-tangent, for every degree ($^\circ$) and minute ($'$), are given in the tables (II.), as well as for every hour (H), minute (M), and four seconds (S), of the day.

§ 101. In trigonometrical calculations, when any logarithm is to be subtracted, the proper result may be obtained by adding the arithmetical co. of such logarithm.

§ a. This method of changing subtraction into addition is found very convenient in practice. After a little exercise in it, the arithmetical co. of a logarithm may be read from the logarithm, as readily as the logarithm itself is read from the tables.

§ b. Wherefore in the solution of trigonometrical problems, sub-

traction need never be performed, for (§ 101.) instead of subtracting a logarithm, the same result is obtained by substituting, for this logarithm, its arithmetical co., and adding this arithmetical co. in the calculation; therefore (§ 100. § a.),

When { A logarithmic sine of an arc or an angle is to be subtracted, add its co-sec., and *vice versâ*.
 A logarithmic co-sine of an arc or an angle is to be subtracted, add its sec., and *vice versâ*.
 A logarithmic tangent of an arc or an angle is to be subtracted, add its co-tangent, and *vice versâ*.

§ 102. To find in the tables (II.), the logarithmic value of the sine of an arc or an angle.

§ a. If the proposed arc or angle be an *extreme* one, the number of *degrees* contained in it, is at the top of the page. But if the one proposed be a *mean* arc or angle, the *degrees* contained in it, are to be found at the *bottom* of the page.

§ b. An *extreme* arc or angle is one that contains *less* than 45° , or *more* than 135° . A *mean* arc or angle contains *more* than 45° but *less* than 135° .

§ c. If the proposed arc contain *less* than 45° or 3 H, or having *more* than 90° or 6 H, contain *less* than 135° or 9 H, the odd minutes of it are to be found in the proper minute column at the left of the page. But if it be *greater* than 135° or 9 H, or being *greater* than 45° or 3 H, contain *less* than 90° or 6 H, the odd minutes of it are contained in the minute column, that is at the right hand side of the page.

§ d. The columns marked at the bottom, Cos., Sec., Sin., Co-sec., Co-tang., and Tang., contain the logarithmic co-sine, secant, sine, co-sec., co-tang., and tang., of the degrees, etc., that are at the *bottom* of the page. And those marked Sin., Co-sec., Cos., Sec., Tang., and Co-tang., at the top, contain the logarithmic sine, co-sec., co-sine, secant, tangent, and co-tangent of the degrees, etc., at the *top* of the page.

§ e. To take out of the tables the logarithmic sine of an extreme arc, that is *less* than 45° , say of $34^\circ 40'$. The degrees (34°) of the arc proposed being found at the top of the page, and the minutes ($40'$) in the minute (') column at the left of the page, the logarithm (9.754960) which, in the column of Sin. stands opposite to the minutes ($40'$), is the required logarithm. In the same way the logarithmic co-sine, or tangent, etc., is found in its proper column, and opposite to the given minutes.

Co-sine $21^\circ 14'$ logarithm = 9.969469.

Tangent $19^\circ 56'$ logarithm = 9.559491.

§ f. If the arc ($179^\circ 7'$) proposed be extreme, and *greater* than 135° , the odd minutes ($7'$) must be found in the last minute (') column on the page; the required logarithm (8.187985) is then found opposite, and in the column marked (Sin.) at the top.

§ g. The odd minutes of a mean arc, say $61^\circ 12'$, that is *less* than 90° , are found in the last minute (') column; and those of one, say $114^\circ 59'$, that is *greater* than 90° , are found in the first minute

([']) column of the page; and the character (Sin., Cos., Co-tang.) of the column is taken from the bottom of the page.

Sine $61^{\circ} 12' = 9.942656$.

Co-tangent $114^{\circ} 59' = 9.668343$.

Tangent $114^{\circ} 59' = 10.331657$.

§ *h*. The trigonometric functions of hours, minutes, and seconds, are taken from the tables in the same way.

§ 103. To find the degs. etc. for a log. sine.

§ *a*. The minutes, in the minute ([']) column, which are found opposite to the proposed logarithm, and the degrees, which stand where the column in which the proposed logarithm is found, is marked Sin., are the degrees and minutes required. The same directions answer for taking out the tangent, secant, co-sine, etc., of a logarithm. Thus,

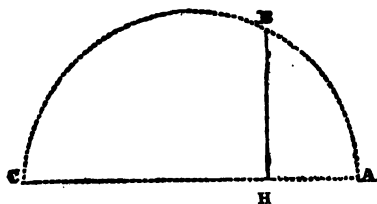
Logarithm 9.627300 sine = $25^{\circ} 5'$ or $154^{\circ} 55'$.

„ 9.956566 cos. = $25^{\circ} 12'$ or $154^{\circ} 48'$.

„ 9.831709 tang. = $34^{\circ} 10'$ or $145^{\circ} 50'$.

„ 9.745494 cos. = $56^{\circ} 11'$ or $123^{\circ} 49'$.

„ 10.377793 tang. = $67^{\circ} 16'$ or $112^{\circ} 44'$.



§ 104. An arc (A B) and its supplement (B C) have the same sine (B H); therefore the same logarithm answers either to the sine of A B or B C. But, for the most part, in calculations, there is some circumstance connected in the operation, which determines

whether an arc or its supplement be required. If not, the case or the solution is called *doubtful*. The same remarks apply to co-sines, secants, tangents, etc.

PLANE TRIGONOMETRY.

PLANE TRIGONOMETRY.

§ 105. Plane trigonometry is that branch of mathematics by which, with certain data, the unknown parts of triangles are determined.

§ a. Plane trigonometry is divided into right, and oblique, angled trigonometry. The solution of right angled triangles pertains to the former; and that of oblique angled triangles to the latter. The methods of solving problems in either, in most cases are similar.

§ 106. Every plane triangle consists of three sides and three angles; which, in a general term, are called *the six parts* of a triangle.

§ a. If the value of any three of these six parts (the *three* angles excepted), be known, the value of every one of the remaining parts is determinable by trigonometrical operations.

§ b. When the angles constitute the only data, the sides cannot be determined (except in *species*); because there may be any number of triangles which are equiangular to each other, and their homologous sides may all be unequal, as the sides of the two triangles under § 73. are.

§ 107. In order to solve a trigonometric problem, the value of three of five parts, viz., two of the angles and the three sides, must be given, and at least *one* of these three parts must be a side.

§ 108. The several combinations of three, which can be formed of five parts, comprise all the cases that are necessary for solving trigonometric problems.

§ a. To one of these every problem in trigonometry resolves itself for solution.

§ b. These several combinations are reduced to *five* cases; viz.,

1st, When two sides and the angle which is opposite to either of them, are given:

2d, When two angles and the side which subtends either of them, are given:

3d, When two sides and the angle which they contain, are given:

4th, When two angles and the side that is between them, are given:

5th, When the three sides are given.

CASE I.

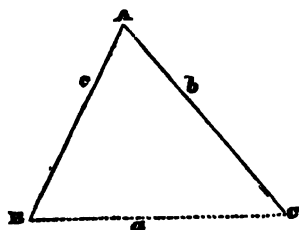
§ 109. Given the sides (c & b) and the angle (B), that is opposite to (b) one of them:

$$c = 450 \text{ yards.}$$

$$b = 600 \text{ yards.}$$

$$B = 74^\circ 49'$$

Required the remaining parts (A , C , & a)?



§ *a*. First, to find the value of C .

By § 74., $b : \text{sine } B :: c : \text{sine } C$;

and substituting for these given parts (b , c , and C), their values, the proportion is, $600 : \text{sine } 74^\circ 49' :: 450 : \text{sine } C$.

$$\text{Log. sine of } 74^\circ 49' = 9.984569$$

$$\text{Logarithm of } 450 = 2.653213$$

$$12.637782$$

$$\text{Logarithm of } 600 = 2.778151$$

$$\text{Log. sine } C = 9.859631 = 46^\circ 22' 15''.$$

§ *b*. The sum of the two angles B and C (§ 32. § *b*.) being subtracted from 180° , gives the remaining angle (A) of the proposed triangle ABC . Thus, $B + C = 121^\circ 11' 15'' - 180^\circ = 58^\circ 48' 45'' = A$.

§ *c*. The logarithmic process (§ *a*.) of finding the value of C , might have been abbreviated, and the operation might have been performed entirely by addition. This abbreviation (§ 101.) consists in using the arithmetical complement of the logarithm of the first term in the order of proportion, in the place of said logarithm. This arithmetical complement, added to the logarithm of the second and third terms, gives the logarithm, (rejecting 10 from the index), of the fourth or required term.

§ *d*. When one or more logarithms are to be subtracted in the process of a calculation, the operation may be simplified (§ 88. § *c*.) by substituting for such logarithms, their arithmetical complements (§ 88. § *e*.), and adding these arithmetical complements in the calculation, and then rejecting the borrowed 10 from the index of the sum thus obtained, the remainder is that which would have resulted by adding together the logarithms which were to be added, and then subtracting from their sum, the logarithms which were to be subtracted.

§ *e*. Hereafter, instead of the logarithm of the first term in the order of proportion being used, its arithmetical complement will be adopted in calculation. This substitution of the arithmetical complement renders the arrangement for calculation uniform; for it changes the process of addition and subtraction, into the simple operation of addition.

§ f. Let it be borne in mind that the *arithmetical complement* (§ 88. § d.) of any numerical expression, is obtained, by subtracting the expression proposed from the number which is made by prefixing unity (1) to as many cyphers, as there are figures in said expression. Thus the arithmetical complement of 89 is 11, for 89—100 = 11. Or, the arithmetical complement is obtained by beginning at the left, and subtracting each figure from 9 (§ 79. § c.), except the last significant figure, which must be subtracted from 10. Thus the arithmetical complement of 9.984569 is 0.015431 (what the former wants of 10.000000), and is obtained thus:

$$\begin{array}{r} 9.99999(10) \\ \text{Logarithm } 9.984569 \\ \hline \text{Ar. co. } 0.015431 \end{array}$$

§ g. And the arithmetical complement of 3.450000 (§ f.) is 6.550000, and is obtained thus:

$$\begin{array}{r} 9.9(10)0000 \\ \text{Logarithm } 3.450000 \\ \hline \text{Ar. co. } 6.550000 \end{array}$$

§ h. When the logarithmic index of any of the *trigonometric functions exceeds 9*, the arithmetical complement of such index is the difference between itself and 19, (§ 89. § d.) and consequently the arithmetical complement is found by subtracting said *index* from 19. Thus the logarithmic tangent of 74° is 10.542504, and its arithmetical complement is 9.457496, which is the co-tang. of 74°.

$$\begin{array}{r} 19.99999(10) \\ 74^\circ \text{ log. tang. } 10.542504 \\ \hline \text{Ar. co. } 9.457496 \end{array}$$

§ i. To find the value of the side *a*; according to § 74, sin. B : *b* :: sin. A : *a*; or, substituting their values, sin. 74° 49' : 600 :: sin. 58° 48' 45'' : *a*.

$$\begin{array}{r} \text{Log. sine } 74^\circ 49' \text{ ar. co.} = 0.015431 = \text{co-sec. B } (\S 100. \S a) \\ \text{Logarithm } 600 \quad \quad \quad = 2.778151 \\ \text{Log. sine } 58^\circ 48' 45'' \quad \quad = 9.932208 \end{array}$$

$$\text{Log. } a = 2.725790 = 531.8 \text{ yards.}$$

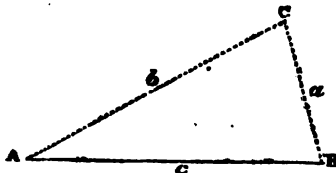
The 10, which was borrowed for the arithmetical complement of the logarithmic sine of 74° 49', being rejected in the sum, gives 2 for the index of the logarithmic value of *a*.

§ j. In the solution of all trigonometric problems by calculation, the *logarithmic* values of the functions employed are always used;

therefore the repetition of the word *log.* before *sine*, *tangent*, etc., will be omitted; and the arithmetical complement of the logarithm of a function or number, is that which is to be understood, and not the arithmetical complement of the number itself.

CASE II.

§ 110. Given two angles (*A* & *C*) and the side (*c*) that subtends one of them.



$$A = 23^{\circ} 56'$$

$$C = 76^{\circ} 4'$$

$$c = 1760 \text{ feet.}$$

To find the other parts (*B*, *a* and *b*),

§ *a.* The process of solution in this case is a repetition of the methods shown § 109. § *b.* & § *i.*; for $A + C$ subtracted from 180° (§ 32. § *b.*) gives $B = 80^{\circ}$; and (§ 74.) $\sin C : c :: \sin A : a :: \sin B : b$.

§ *b.* To find *a.* $\sin. 76^{\circ} 4' : 1760 :: \sin. 23^{\circ} 56' : a$.

$$\text{Sine } 76^{\circ} 4' \text{ ar. co.} = 0.012970 = \text{co-sec. } C. (\S 101. \S b.)$$

$$\text{Log. } 1760 = 3.245513$$

$$\text{Sine } 23^{\circ} 56' = 9.608177$$

$$\text{Log. } a = 2.866660 = 735.6 \text{ feet.}$$

§ *c.* To find *b.* $\sin. 76^{\circ} 4' : 1760 :: \sin. 80^{\circ} : b$.

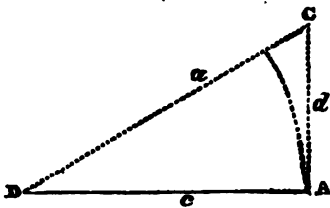
$$\text{Sine } 76^{\circ} 4' \text{ ar. co.} = 0.012970 = \text{co-sec. } C$$

$$\text{Log. } 1760 = 3.245513$$

$$\text{Sine } 80^{\circ} = 9.993352$$

$$\text{Log. } b = 3.251835 = 1785.8 \text{ feet.}$$

§ *d.* If, with similar data, the proposed, be a right angled triangle, the problem may be solved as the one above is, by means of the proportion between the sides and sines of opposite angles; or it may be solved by means of the principles involved (§ 75.) in the proportion between the sides and trigonometric functions of a right angled triangle. Thus, the data being,



$$C = 67^{\circ} 19'$$

$$c = 1760 \text{ feet.}$$

The value of *A* is known by the rectangularity of the proposed triangle (*D A C*). To find the other parts (*D*, *d* & *a*),

§ e. The third angle (D) is *always* known (§ 32. § b.) by subtracting the sum of the two other angles from 180°; $A + C - 180° = D$, or 22° 41'.

§ f. To find the two sides *a* and *d*; making D A radius, the following proportions (§ 75. § c.) are deduced, viz.:

Rad. : *c* :: tang. D : *d*; and Rad. : *c* :: sec. D : *a*.

Radius (*always*, § 98. § b.) = 10.000000

c = 1760 log. = 3.245513

D = 22° 41' tang. = 9.621142

Log. *d* = 2.866655 = 735.6 feet.

Radius = 10.

c = 1760 log. = 3.245513

D = 22° 41' sec. = 0.034963

Log. *a* = 3.280476 = 1907.5 feet.

CASE III.

§ 111. Given two sides (*b* & *a*) and the angle (C) they contain;

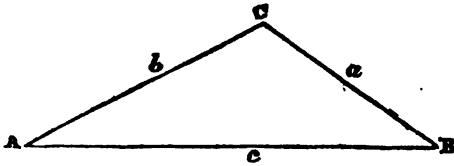
b = 479 fathoms.

a = 419.8 "

C = 119° 41'.

To find the other parts (A, B & *c*),

§ a. The solution of this problem is founded



upon § 77.

§ b. One angle (C) of the proposed triangle being known, the sum of the two other angles (A & B) (§ 32. § b.) is obtained by subtracting the given angle from 180°. Thus, $180° - 119° 41' = 60° 19'$, the sum of A & B.

§ c. To find the values of A and B; according to § 77., $(b + a) :$

$\text{tang. } \frac{A+B}{2} :: (b \oslash a) : \text{tang. } \frac{A \oslash B}{2}$. Therefore, by substitution,

$898.8 : \text{tang. } 30° 9' 30'' :: 59.2 : \text{tang. } \frac{A \oslash B}{2}$.

$(b + a) = 898.8$ log. ar. co. = 7.046337

$(A + B) + 2 = 30° 9' 30''$ tang. = 9.764207

$(b \oslash a) = 59.2$ log. = 1.772322.

Tang. $\frac{A \oslash B}{2} = 8.582866 = 2° 11' 30''$.

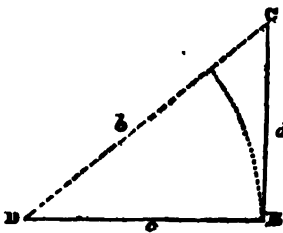
Now half the difference ($2^{\circ} 11' 30''$) between A and B, being added to half their sum ($30^{\circ} 9' 30''$) (§ 78. § h.), gives B the greater angle; and being subtracted from said half sum, gives A the less angle. Thus $30^{\circ} 9' 30'' + 2^{\circ} 11' 30'' = 32^{\circ} 21'$, or B; and $30^{\circ} 9' 30'' - 2^{\circ} 11' 30'' = 27^{\circ} 58'$, or A. A is known to be the less angle (§ 63.), because its subtending side (a) is the less of the sides b & c .

§ d. The angles and two sides being known, the value of the third side (c) is deducible by means of calculations conducted upon the proportion (§ 74.) between the sides and sines of the angles of plane triangles.

$$\begin{aligned} \text{§ e. To find } c. \quad \text{Sin. B} : b :: \text{sin. C} : c. \\ B = 32^{\circ} 21' \text{ sin. ar. co.} &= 0.271573 = \text{co-sec. B} \text{ (§ 100. § a.)} \\ b = 479 \text{ faths. log.} &= 2.680336 \\ C = 119^{\circ} 41' \text{ sin.} &= 9.988908 \text{ (§ 102. § g.)} \end{aligned}$$

$$\text{Log. } c = 2.890817 = 777.7 \text{ faths.}$$

§ f. If the problem comprise a right angle triangle, with similar data, the process of solving it is much more simple. For the two legs and the right angle being the given parts, the calculations for determining the unknown parts, are founded upon the relations of the sides and trigonometric functions of a right angled triangle, as they are shown § 75.



§ g. In the proposed triangle (D B C), right angled at B, the values of the legs, are;

$c = 479$ faths.; and $d = 419.8$ faths.; to find the other parts.

§ h. Making either leg (c) radius, (§ 75. § c.) the terms and order of the proportion for finding the value of D, are, $c : \text{rad.} :: d : \text{tang. D}$. And for finding the hypotenuse (b) they are, $\text{rad.} : c :: \text{sec. D} : b$.

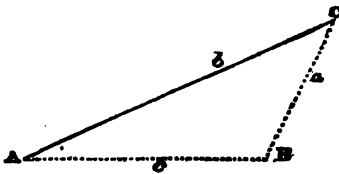
$$\begin{aligned} \text{§ i. To find D.} \\ c = 479. \text{ Log. ar. co.} &= 7.319664 \\ \text{Radius} &= 10. \\ d = 419.8 \text{ log.} &= 2.623042 \end{aligned}$$

$$\text{Tang. D} = 9.942706 = 41^{\circ} 13' 53''$$

$$\begin{aligned} \text{§ j. To find } b. \\ \text{Radius} &= 10. \\ c = 479 \text{ log.} &= 2.680336 \\ D = 41^{\circ} 13' 53'' \text{ sec.} &= 0.123777 \end{aligned}$$

$$\text{Log. } b = 2.804113 = 636.9 \text{ faths.}$$

CASE IV.



§ 112. Given two angles (A & C) and the side (b) between them;
 $A=26^{\circ} 1'$
 $C=38^{\circ} 49'$
 $b=179$ chains,
 To find the values of the other parts (B, c & a) of the proposed triangle. (A B C).

§ a. Two angles being known, the third (B) (§ 32. § b.) is also known; it is $B=115^{\circ} 10'$.

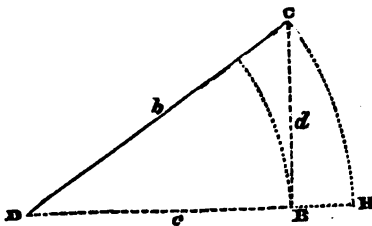
§ b. The remaining unknown parts (a & c) of this triangle, are determined by means of the principles involved in the solution of the problem under Case 2. The process of operation in the solution of this, is precisely similar to that of § 109. § i. under Case 1. In the method of their solution, Cases 1, 2, and 4, are only repetitions of each other. For whenever two angles of a triangle are given, the third is also known (§ 32. § b.); and whenever an angle and its subtending side are two of the known parts, the required parts are determinable through calculations conducted upon the proportion (§ 74.) which exists between the sides and sines of angles in all triangles.

§ c. To find the value of a. $\sin B : b :: \sin A : a$.
 $B=115^{\circ} 10'$, $\sin. ar. co.=0.043316=\text{co-sec. } B$ (§ 101. § b.)
 $b=179$ chains $\log. =2.252853$
 $A=26^{\circ} 1'$, $\sin. =9.642101$

$$\text{Log. } a = 1.938270 = 86.7 \text{ chains.}$$

§ d. To find the value of c. $\sin. B : b :: \sin. C : c$.
 $B = 115^{\circ} 10'$ $\text{co-sec.} = 0.043316$
 $b = 179$ chains $\log. = 2.252853$
 $C = 38^{\circ} 49'$ $\sin. = 9.797150$

$$\text{Log. } c = 2.093319 = 123.9 \text{ chains.}$$



§ e. Transferring the conditions of this problem to one in right angled trigonometry, the use of sines may be retained in the calculation for determining the unknown parts (c & d); for by making the given side (b), radius to an arc (CH), the two legs of the proposed triangle (D B C)

become (§ 75. § a.) sine and co-sine to the acute angles (D & C);

and (§ 75. § b.) $\text{rad.} : b :: \sin. D : d :: \text{co-sine } D : c$. The parts given are $D = 26^\circ 1'$, and $b = 179$ chains.

§ f. To find the values of c and d .

$$\begin{array}{rcl} \text{Radius} & - & = 10. \\ b = 179. & \log. & = 2.252853 \\ D = 26^\circ 1' & \sin. & = 9.642101 \end{array}$$

$$\text{Log. } d = \underline{\underline{1.894954}} = 78.5 \text{ chs.}$$

$$\begin{array}{rcl} & \text{Radius} & = 10. \\ b = 179 & \log. & = 2.252853 \\ D = 26^\circ 1' & \cos. & = 9.953599 \end{array}$$

$$\text{Log. } c = \underline{\underline{2.206452}} = 160.8 \text{ chains.}$$

§ g. The same result may be obtained by making a radius of either leg (c), and introducing different trigonometric functions into calculation, upon the principles shown under § 75. § c. Thus; $\sec. D : b :: \text{radius} : c :: \text{tang. } D : d$.

§ h. To find c and d by this method of calculation :

$$\begin{array}{rcl} D = 26^\circ 1' \text{ sec. (ar. co.)} & = & 9.953599 = \text{cos. } D \text{ (§ 101. § b.)} \\ b = 179 \text{ chains} & \log. & = 2.252853 \\ \text{Radius} & - & = 10. \end{array}$$

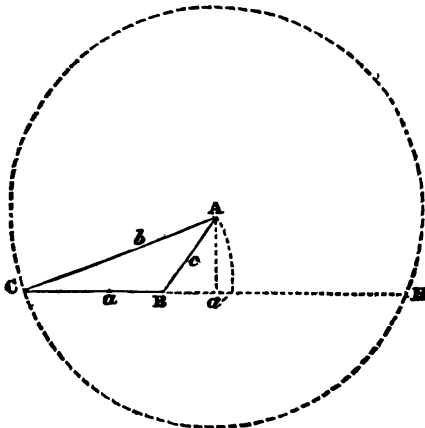
$$\text{Log. } c = \underline{\underline{2.206452}} = 160.8 \text{ chains.}$$

$$\begin{array}{rcl} D = 26^\circ 1' \text{ cos. (§ 101. § b.)} & = & 9.953599 \\ b = 179 \text{ chains} & \log. & = 2.252853 \\ D = 26^\circ 1' & \text{tang.} & = 9.688502 \end{array}$$

$$\text{Log. } d = \underline{\underline{1.894954}} = 78.5 \text{ chains.}$$

§ i. The use of sine and co-sine as functions in plane trigonometrical calculations, being more convenient than that of other functions, the former (§ f.) is generally preferable to the latter method (§ h.) of solving problems.

CASE V.



§ 113. Given the three sides (BC, b , c)
 $BC = 144$ chains.
 $b = 220$ chains.
 $c = 103$ chains.
 To find the angles (C, A & B)

§ *a*. Here is the application to practice of the principles involved in § 79. And in order to determine the value of any one (C) of these angles by calculation, the distance ($a a'$) from the middle (a) of the base (CB), to the perpendicular ($A a'$) upon

it, must be found by means of the proportion, (§ 79.) the base BC : $b \sin c :: b + c : 2 a a'$. Then either of the segments (C a') is found (§ 79. § *d*.) by applying (C a) half the base (CB) to ($a a'$) the distance of the perpendicular at a' from the middle of the base. This segment (C a'), the perpendicular ($A a'$), and the side (b), adjacent to the required angle (C), form a right angled triangle (C $A a'$); of which are known the hypotenuse (b) and a leg (C a').

§ *b*. The value of the required angle (C) is then found according to the principles established under § 75. For by making the hypotenuse (CA) radius, the segment (C a') becomes co-sine to the required angle (C); the value of which may then be determined (§ 75. § *b*) by means of the proportion, $b : \text{radius} :: C a' : \cos. C$.

§ *c*. Knowing the value of any one (C) of the angles, either of the others (A) may then be determined by means of calculations conducted upon the proportion (§ 74.) of the sides of triangles to the sines of their opposite angles. And the remaining angle (B) (§ 32. § *b*.) is determinable by subtraction.

§ *d*. To find the value of the angle C.

1st. Call CB the base, in order to find twice the distance ($a a'$) from the middle of the base, to a perpendicular drawn upon the base, from its opposite angle (A) (§ 79.). Twice the length of this distance ($a a'$) is evolved by the proportion; $CB : b \sin c :: b + c : 2 a a'$.

$$\begin{aligned} CB &= 144, \log. \text{ ar. co.} = 7.841637 \\ b \sin c &= 117, \log. = 2.068186 \\ b + c &= 323, \log. = 2.509203 \end{aligned}$$

$$\text{Log. } 2 a a' = 2.419026 = 282.4$$

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2d. To find the greater segment $C a'$. One half of 262.4 ($2 a a'$) is equal to the distance ($a a'$) of the perpendicular from the middle of the base; and (§ 79. § d.) $a a' + \frac{B C}{2} = C a'$. Therefore, $131.2 + 72 = C a' = 203.2$.

§ e. If twice the distance ($a a'$) of the perpendicular from the middle of the base be *greater* than the base, the perpendicular falls *without* the triangle, as in the case before us. But if it be *less* than the base, the perpendicular falls *within* the triangle.

To find the value of C . According to § b. we have, $b : \text{rad.} :: C a' : \cos. C$.

$$b = 220. \text{ log. ar. co.} = 7.657577$$

$$\text{Radius} = 10.$$

$$C a' = 203.2 \text{ log.} = 2.307924$$

$$\text{Cos. } C = 9.965501 = 22^\circ 32' 11''$$

§ f. To find the value of A (§ c.) we have, $c : \sin. C :: B C : \sin. A$.

$$c = 103. \text{ log. ar. co.} = 7.987163$$

$$C = 22^\circ 32' 11'' \text{ sine} = 9.583504$$

$$B C = 144. \text{ log.} = 2.158363$$

$$\text{Sine } A = 9.729030 = 32^\circ 24' 2''$$

§ g. To find the value of B . According to § 32. § b. $C + A - 180^\circ = B$; therefore $B = 125^\circ 3' 47''$.

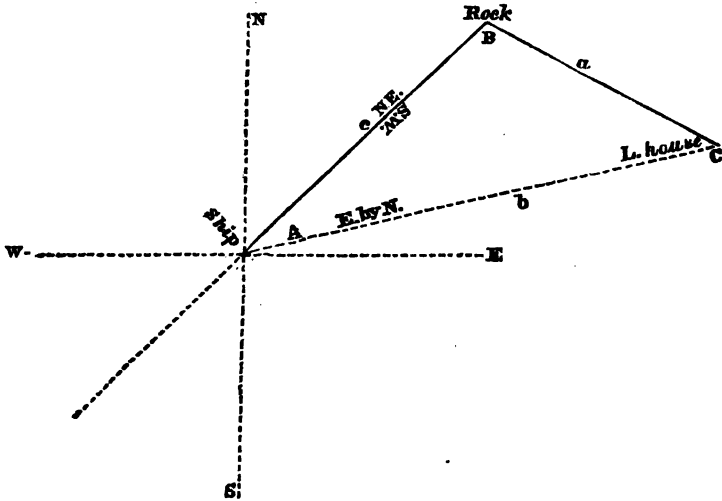
§ h. If, when the perpendicular falls *without* the triangle, the obtuse angle (B) be the first part required, the side (c) adjacent to it becomes hypotenuse to the right angled triangle, of which, the perpendicular to the base and the smaller segment ($B a'$) of the base, are legs, and the supplement ($A B a'$) of the required angle (B) is that which is evolved from the proportion (§ b.), $c : \text{rad.} :: B a' : \cos. A B a'$.

EXAMPLE I.

§ 114. A rock is seven miles from a light-house, and a ship, having the light-house to bear E. by N., is nine miles S. W. of the rock; What is the distance between the ship and the light-house?

Ans. 12.4 miles.

§ a. The solution of this problem is conducted after the methods shown under § a. and § i. (§ 109.) The parts given are the sides a and c , and the angle (A) contained at the ship, between the bearing of the rock and light-house. The value of A is known by converting into degrees, etc., the points contained between the bear-



ing of the rock and light-house, from the ship. The rock bears N. E., and the light-house E. by N. from the ship. Three points intervene between E. by N. and N. E., and each point contains $11^{\circ} 15'$; therefore the angle (A) contained between the lines of these bearings is $11^{\circ} 15' \times 3$, or $33^{\circ} 45'$.

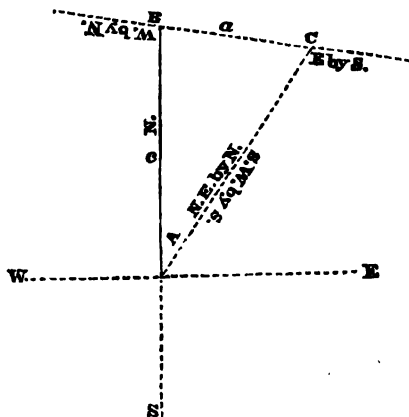
§ b. Unless the problem were embraced in a right angled triangle, the value of C must be found, and B known (§ 32. § b.) before that of b is determined. C is found (§ 109. § b.) from the proportion (§ 74.) which exists between certain parts of every triangle; viz., $a : \sin. A :: c : \sin. C$. Then $C + A - 180^{\circ} = B$; and then, $\sin. C : c :: \sin. B : b$, affords the solution required.

EXAMPLE II.

§ 115. A ship was steering N. and sailing 10 knots per hour; she made a point of land bearing N. E. by N.; two hours afterwards the same point bears E. by S. What is the distance of it from the ship?

Ans. 12. + miles.

§ a. The solution of this problem depends upon the principles which Example 1 involves. The angle (A) between the point of land and the ship's course is three points, or $33^{\circ} 45'$. The angle (C) between the bearing of the ship from the point of land at each station, is six points, or $67^{\circ} 30'$. And the angle (B) between the second bearing of the land and the line upon which the ship sailed,

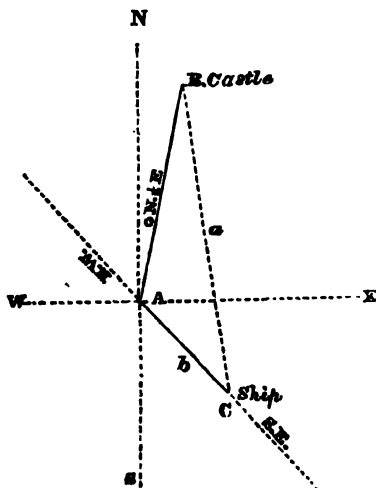


is seven points, or $78^\circ 45'$; or it is $A + C - 180 = 78^\circ 45'$. Then the proportion of $\sin. C : c :: \sin. A : a$, determines the value of the part required.

EXAMPLE III.

§ 116. Several boats, intending to cut a ship out from under the guns of a castle, wish to know how far she is off from the castle, which bears $N. \frac{1}{4} E.$ 917 fathoms from a watch-tower, that is 491 fathoms $N. W.$ from the ship.

Ans. 1285.7 fathoms.



§ a. The solution of this problem involves in it the principles demonstrated § 77, by which either angle (B or C) is found; and then the length of the required side (a) is determined by the ratio between the sides and sines of opposite angles.

§ b. The parts given are, the distances (b & c) of the watch-tower (A) from the ship and castle, and the angle (A) contained at the watch-tower between the lines of bearing from it to the castle and ship. The angle (A) at the watch-

towr contains $11\frac{1}{2}$ points, or $129^\circ 22' 30''$. The sum of the angles B and C is found by subtracting A (§ 32.) from 180° . And half their difference is determined by the proportion (§ 77.), $b+c :$

$$\text{tangent } \frac{B+C}{2} :: b \propto c : \text{tang. } \frac{B \propto C}{2}.$$

§ c. The value of B and of C is then known by § 77. § h.; and the solution completed by evolving the value of a from the proportion,— $\sin. C : c :: \sin. A : a$.

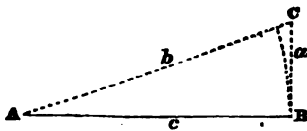
EXAMPLE IV.

§ 117. Wishing to know the height of a Chinese pagoda that stood in a plane, I took the altitude of the sun from an artificial horizon, and at the same time the length of the shadow cast by the pagoda was marked and measured.

The sun's corrected altitude was $21^\circ 10'$.

The length of the shadow 347 feet.

Ans. Height of pagoda 134.3 feet.



§ a. The pagoda is supposed to stand upright. The angle (A) which is formed at the end of the shadow by an imaginary line drawn thence to the top of the pagoda, is $21^\circ 10'$, or whatever be the altitude of the body which

causes the shadow. The solution of this problem may be conducted according to the principles shown § 75. § c.

§ b. The parts given are the length (c) of the shadow, the angles A and B. The latter is known from the primitive condition of the triangle, which is right angled.

§ c. Making the given leg radius, the other leg (a) or height of the pagoda, becomes tangent to the angle (A) of altitude. The value of the required part (a) is evolved by means of the proportion, $\text{rad.} : c :: \text{tang. } A : a$.

EXAMPLE V.

§ 118. A road crosses a mountain, the base of which is nine miles across. The distance from the foot to the top of the mountain, is 4.5 miles on one side, and 5.3 on the other.

What is the angular ascent of the road on each side of the mountain, and how high is the top above the base ?

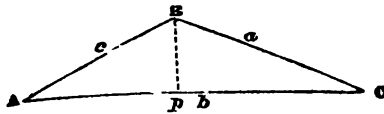
Ans. Angle of ascent on one side = $31^\circ 32' 21''$

Angle of ascent on the other = $26^\circ 32' 25''$

Height of the mountain 1.94 miles.

§ a. This problem involves in the solution of it, the principles

demonstrated § 79. and § 75. The parts given are the three sides (*a*, *b*, *c*).



§ *b*. The operation for finding the ascent of the road, or the angles *A* and *C*, is a repetition of the method shown in Case 5, §113, for finding *C* and *B*. *Bp*, the perpendicular upon the

base (*b*) of the mountain, shows its height; the value of it is determined (§ 75.) after the angles *A* & *C* are determined. $AC : c \cos a :: c + a : 2pb$; and (§ 79. § *d*.) $pb + \frac{AC}{2} = pC$; and (§ 75. § *b*.) $a : \text{rad.} :: pC : \cos. C$; and (§ 74.) $c : \sin. C :: a : \sin. A$; and $\text{rad.} : a :: \sin. C : Bp$.

EXAMPLE VI.

Wishing to ascertain the breadth of a river, I observed that a cocoa-nut tree, which stood at the water's edge on the opposite bank, bore west of me; then after having walked due south 194 yards, the same tree bore N. W.

How wide was the river?

Ans. 194 yards.

EXAMPLE VII.

Wishing to know the height of a mountain in South America, on the morning of the 22d December, 1832, between eight and nine o'clock, I measured with a sextant the altitude of the sun above the top of the mountain; it was $19^{\circ} 40' 15''$. The apparent altitude of the sun, measured at the same time from an artificial horizon, was $41^{\circ} 47' 45''$. Then going from the mountain, I measured 4420 fathoms, and the next day, when the top of the mountain was again in the plane of the sun's azimuth circle, the sun's altitude above the top of the mountain, and from an artificial horizon taken as before, was, from the horizon = $40^{\circ} 21' 30''$, above the mountain = $25^{\circ} 14'$

What is its height?

Ans. 3564.1 fathoms, or 21384 feet 7 inches.

EXAMPLE VIII.

Supposing that a ray of light is not refrangible, that the earth is a perfect sphere, that its diameter is 7924 miles, and that the height of Chimborazo is 21384 feet, How far can the top of this mountain be seen from the surface of the earth?

186 miles for a sea

* The mean diameter of the earth is about 7923.57 miles.

80

SPHERICS.

SPHERICS.

§ 119. Spherical Trigonometry is one of the principal branches upon which the science of navigation is founded. The solution of all problems for finding latitude, longitude, variation, etc., from data obtained by means of observations made upon celestial objects, depends upon the principles of spherical trigonometry.

§ *a*. As the figure of the earth is an approximation to that of a sphere, the whole science of navigation, properly speaking, is based upon the doctrines of the sphere.

§ 120. The figure of a *sphere* may be generated by the revolution of a semicircle about its diameter, as an axis. A perfectly round globe or ball is a sphere.

§ 121. Trigonometrically speaking, all lines upon a sphere are curved lines. These lines are either circles, or arcs of circles. Circles are either *great* or *small*.

§ 122. A *great circle* is concentric with the sphere.

§ *a*. The shortest distance between two points on a plane (§ 3.) is the straight line that joins them; and the shortest distance on a sphere, between two points, is the arc of a great circle, that joins them.

§ *b*. Every great circle has two *poles*.

§ 123. The *poles* of a great circle are two points on the surface of a sphere, that are diametrically opposite to each other, and are equidistant from all points at the circumference of their circle. Consequently each pole is 90° from the circumference of its circle.

§ *a*. The north and south poles are the poles of the equator. The equator is 90° from either pole.

§ 124. The straight line, which, passing through the centre of a great circle, joins its poles, is the *axis* of that circle.

§ 125. All great circles cross each other in points diametrically opposite. Therefore,

§ *a*. Two great circles cannot be parallel; but they divide each other into arcs of 180° each.

§ *b*. The space contained between the intersecting halves of two great circles, is called a *lune*.

§ 126. One great circle is perpendicular to another, when the two cross each other at right angles.

§ *a*. When two great circles cut each other at right angles, the axis of either lies along the plane of the other; and they pass through the poles of each other.

§ 127. A *secondary* is a great circle that crosses another, perpendicularly.

§ *a.* A meridian of longitude is secondary to the equator.

§ 128. Every great circle divides its sphere into two equal parts, as the Equator does the earth.

§ 129. A *small circle* divides the sphere into two unequal parts; as the Tropic of Cancer, or of Capricorn, or as a parallel of latitude, does the earth.

§ *a.* If every point at the circumference of a small circle be equidistant from either pole of a great circle, the small is parallel to the great circle.

§ *b.* The centre of a small circle is in the axis of the great circle to which it is parallel.

§ 130. The radius of a small circle, is the sine of the arc intercepted between its circumference and the pole of the great circle, to which it is parallel.

§ *a.* The radius of a parallel of latitude is the co-sine of its own latitude.

§ 131. All spheric, like all rectilineal, angles, are either acute right, or obtuse; and their values are expressed under the same denominations of degrees ($^{\circ}$), minutes ($'$), and seconds ($''$).

§ 132. Two arcs of great circles, like two straight lines, (§ 25 & § 27.) that cross each other, make the vertically opposite angles equal to each other, the two angles that are on the same side of either, equal to two right angles, and the four angles together equal to four right angles.

§ 133. A spherical angle is at the pole of the circle, upon which it is measured.

§ *a.* And the arc of this circle, which is intercepted between the two arcs forming the angle, is its measure.

§ *b.* The two circles which form an angle are secondaries (§ 127.) to that upon which the angle is measured.

§ *c.* This circle (§ 126. § *a.*) passes through the poles of its secondaries.

§ *d.* The distance between the poles of two great circles that form an angle with each other, measures that angle.

§ 134. Every spherical, like every plane triangle, has three sides and three angles, and any two of the former are greater than the third.

§ 135. The sides of a spherical triangle are arcs of circles. Their values are *always* expressed in degrees ($^{\circ}$), minutes ($'$), and seconds ($''$).

§ 136. Plane triangles are unlimited as to the value of their sides; the sum of the three sides of a spherical triangle is less than 360° . For if two arcs that form an angle be each 180° , they will intersect each other (§ 125.) in another point, that is diametrically opposite to their angular point; then, if a third arc cross these two, it will divide the lune (§ 125. § *b.*) into two triangles, and be a side to each. This third side is less (§ 134.) than the sum of the two other sides of either triangle, and the sum of these four sides, by supposition,

is two semicircles, or equal to 360° ; therefore the sum of the two sides of either triangle plus the third side is *less* than 360° ; and so with any spherical triangle.

§ a. The minimum of the sides of a spherical triangle is without limits.

§ 137. The sum of the angles of a plane triangle is equal to two right angles; the sum of the angles of a spherical triangle, in all cases, is greater than two, but less than six, right angles.

§ a. The exterior angle of a spherical triangle (§ 132.), therefore is not, as in a plane triangle, necessarily equal to the sum of the two remote interior angles of the triangle.

§ b. Most of the other propositions of elementary geometry which show the ratio, relations, or equality between the parts of plane triangles, are likewise applicable to spherical triangles.

§ 138. Two angles, or two legs, of a spherical triangle, are *alike*, or of the *same affection*, when both of them are either acute or obtuse.

§ 139. In spherical, as in plane triangles (§ 63.), the greatest side and angle subtend each other; so also do the mean and least.

§ a. An angle and its opposite side are not always of the same affection.

§ 140. Spherical, besides being, as plane triangles, divided into equilateral, isosceles, and scalene, are either right angled, quadrantal, or oblique.

§ 141. A *right angled spherical triangle* has one right angle.

§ a. The side subtending the right angle is the hypotenuse; but it is not, as in a plane triangle, necessarily the greatest side.

§ b. If the hypotenuse be less than 90° , the legs are of the same affection; and the oblique angles also.

§ c. If the hypotenuse be greater than 90° the legs are unlike, and the oblique angles also.

§ d. A leg of a right angled spherical triangle, and its opposite angle, are always of the same affection.

§ 142. A *quadrantal triangle* has a side that is a quadrant, or 90° .

§ 143. An *oblique spherical triangle* has neither a side, nor an angle of 90° .

§ 144. In plane triangles, the sides, and the sines of their opposite angles, have the same ratio to each other; in spherical triangles, the sines of the opposite sides and angles are proportional.

§ 145. In plane triangles (§ 107.), one side, at least, must be among the three parts that constitute the data necessary for finding the other parts; in spherical triangles any three parts are data sufficient for determining the other parts. Therefore—

§ 146. In spherical trigonometry, the three sides of a triangle can be determined by having the three angles as data; and the reverse.

§ 147. For the purpose of facilitating, by logarithmic calculation, the solution of problems in spherical trigonometry that are included in oblique triangles, spherical trigonometry is here divided into right and oblique angled trigonometry.

§ a. All the problems that come under the several cases, two excepted, of oblique spherical trigonometry, may be solved by reducing them to analogous cases in right angled trigonometry; this is done by means of drawing a perpendicular from an angle upon its subtending side, of the proposed triangle, and from such an angle, that the proposed oblique triangle will be divided into two right angled triangles, one of which shall contain two of the parts given in the problem.

§ 148. Every problem in oblique trigonometry may be solved without the direct intervention of a perpendicular, and of right angled triangles.

§ a. The process of calculation is shortened by solving the problems without conducting the operation upon the principles of right angled triangles. For this reason spherical trigonometry is here divided into right and oblique trigonometry.

§ 149. Problems comprising as data the three angles, or the three sides of an oblique triangle, do not admit of the intervention of right angles for determining the unknown parts; because, in neither case can a perpendicular be so drawn in the proposed triangle, that two of the given parts will fall in either of the right angled triangles, or on either side of the perpendicular.

§ 150. By some, problems that depend upon quadrantal triangles, are included in a separate division of spherical trigonometry, called "quadrantal trigonometry." But knowing three parts, the other three of a quadrantal triangle may be determined by the rules for finding with similar data, like parts that are unknown in a right angled triangle.

§ a. In arranging for calculation the trigonometric functions of the parts in a problem included in a quadrantal triangle, the legs must be called *angles*, and their adjacent angles, *legs*; the *supplement* of the angle that subtends the quadrantal side, must be called the *hypotenuse*, and the quadrantal side, *radius*.

§ 151. The side and angle that are opposite in a quadrantal triangle, are of the same affection.

§ 152. The relations between the parts of a triangle in plane, and the parts of a triangle in spherical, trigonometry, are similar; and the formulæ for the solution of problems in the one, are analogous to the formulæ for the solution of similar problems in the other.

§ a. As much, with regard to the sides, can be determined from the three angles of a plane triangle, as can be determined from the three angles of a spherical triangle. In the former case, the triangle can be determined in *species*; and in the latter, the sides are determined in degrees and minutes of arcs, which arcs, in *absolute* length, may be infinitely great or small. And the number of miles, or of any units of a positive quantity, contained by any one of these arcs, depends upon the relations of other quantities to it, and not at all upon the relations between it and the other parts of its triangle.

§ b. In order then to arrive at absolute values for the sides and angles of a triangle which are submitted for calculation, a third

quantity, that will answer the purpose of a common measure for lines and angles, or arcs, must be brought into consideration.

§ c. And this common measure is the *radius* of a circle. When we say that a side of a spherical triangle is an arc containing a certain number of degrees and minutes, we have no reference to the *absolute* length of this arc, or to the number of inches, or fathoms, or miles, contained in it. It may be an arc whose radius is infinitely great or small. But if the length of its radius in inches, or miles, be known, the *absolute* length of the arc also in the denominations of the same dimensions is determinable. But this belongs to another branch of mathematics, which is not relevant to the purposes for which this treatise is designed.

§ 153. The analogy between the formulæ for the solution of problems of like data and quæsitæ in plane and spherical trigonometry, grows out of the resemblance between the parts of a plane and a spherical triangle.

§ a. Suppose that the sides of a spherical triangle should remain of the same *absolute* length, and that the radius of their sphere be increased *ad infinitum*. The angles at the centre of the sphere, which these sides subtend, and the number of degrees contained in these sides, or arcs, will be decreased until they reach the *ultimatum*, when the surface included by these three sides becomes a plane, the triangle a plane triangle, and a *finite* portion of infinity.

RIGHT ANGLED SPHERICAL TRIGONOMETRY.

§ 154. In the trigonometrical solution of right angled spherical triangles, there are *five parts*, (three sides and two angles,) any one of which may be the unknown and required part of the problem.

§ a. The right angle is ever known from the condition of the triangle. In calculation the right angle is not called a *part*.

§ 155. Any two of the five parts of a right angled spherical triangle being known, the rest are determinable by means of trigonometrical calculations.

§ 156. In right angled spherical trigonometry, there can be six cases of two different parts as data, viz.:

1. The hypotenuse and a leg.
2. The hypotenuse and an angle.
3. The two legs.
4. The two angles.
5. An angle and its opposite leg.
6. A leg and its adjacent angle.

§ 157. Lord Napier has given *two rules*, by which every problem that can occur in any of these several cases, may be solved. But he has not made known the process of reasoning, by which he arrived at the conclusions, whence he deduced these rules; nor have mathematicians been able to follow the steps of this bold reasoner.

§ a The truth of his, called the Catholic Proposition, is sufficiently

established by practice, and by its utility, and may therefore be admitted as an axiom or received truth.

§ 158. In his Analytical Treatise on Plane and Spherical Trigonometry, Dr. Lardner observes, "We have thus established *Napier's rules*, by proving separately all the several cases which they include. There is no independent or general demonstration of these remarkable theorems, nor is it easy to conceive the process of mind by which their illustrious inventor arrived at them. Professor Woodhouse justly observes, that there are not, perhaps in the whole compass of mathematical science, rules which more completely attain that which is the proper object of rules, namely, brevity and facility of computation. He might have added, that few, or perhaps no theorems equally general, make such an immediate and permanent impression on the memory."*

§ 159. The *five* parts of a right angled triangle, are called, in *Napier's rules*, the *circular* parts.

§ a. The circular parts are the two legs, and the *complements* of the hypotenuse and its adjacent angles, instead of these three parts themselves.

§ 160. The right angle (§ 154. § a.) is thrown out of consideration; and the five circular parts join each other.

§ a. The complement of the hypotenuse joins the complement of each of the two angles; each of which angular complements joins its adjacent leg, and the two legs join each other.

§ 161. In every problem two of these parts are given and a third is sought. They are named from their relative position with regard to each other.

§ a. One of them is the *middle* part; the two others are *extremes*, either *conjunct* or *disjunct*.

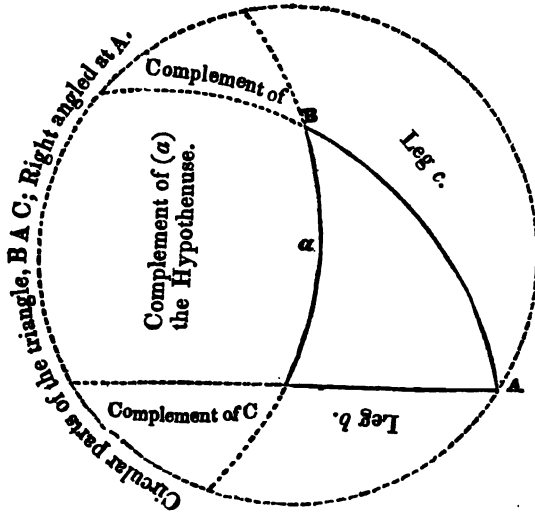
§ 162. If the parts given and the part sought join each other in circular order, the first and last in this order are called *extremes conjunct*; and the part between them connects them together, and is called the *middle* part.

§ a. The triangle A B C, represents a right angled spherical triangle, right angled at A; its hypotenuse is *a*, and *b* & *c* are its two legs. The circular parts are the leg *b*, the complement of C, do. of *a*, do. of B, and the other leg *c*.

§ b. The three parts, *a*, B, *c*, join in circular order. The complement of B is the connecting part between *c* and the complement of *a*. The complement of B is the middle part; *c*, and the complement of *a*, are extremes conjunct.

§ c. Of the parts	Middle part is,	Extremes conjunct are,
B, <i>c</i> , <i>b</i> .	<i>c</i> .	<i>b</i> , and complement of B.
<i>c</i> , <i>b</i> , C.	<i>b</i> .	<i>c</i> , and complement of C.
<i>b</i> , C, <i>a</i> .	Complement of C.	<i>b</i> , and complement of <i>a</i> .
C, <i>a</i> , B.	Complement of <i>a</i> .	Complements of C and B.
<i>a</i> , B, <i>c</i> .	Complement of B.	<i>c</i> , and complement of <i>a</i> .

* See Analytical Treatise on Plain and Spherical Trigonometry, by the Rev. Dionysius Lardner.



§ 163. If the parts given, and the parts sought, be not adjacent to each other in the circular order, that part which stands alone, or is not adjacent to either of the two other parts, is the middle part, and the two others are *extremes disjunct*.

§ a. The three parts, a, c, b , do not join each other in the circular order; the complement of a is not adjacent to either of the two other parts, being separated from them by the complement of the two acute angles, C & B ; it stands alone, and is therefore (§ 163.) the middle part, and the two other parts that do join each other, are the *extremes disjunct*.

§ b. Of the parts	Middle part is,	Extremes disjunct are,
$B, b, C.$	Complement of $B.$	b , and complement of $C.$
$c, C, a.$	$c.$	Complements of C and $a.$
$c, C, B.$	Complement of $C.$	c , and complement of $B.$
$b, a, B.$	$b.$	Complements of B and $a.$
$a, c, b.$	Complement of $a.$	b and $c.$

§ 164. Napier's rules establish an equality of ratio between radius, the *sine* of the middle part, and certain trigonometric functions of the *extremes*. They are,

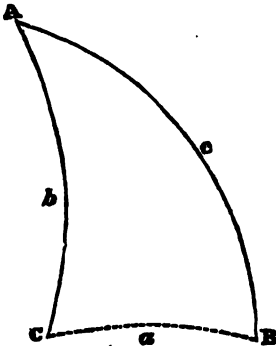
§ 165. The product of radius and sine of the middle part, is equal to the product of the tangents of extremes conjunct. And,

§ 166. The product of the co-sines of extremes disjunct, is equal to the product of radius and sine of the middle part.

§ 167. Every problem in right angled spherical trigonometry can be solved either by the one or the other of these two rules.

§ a. They have been put in the following mnemonic form :

“The *product* of radius and middle part's sine
 Equals *that* of the tangents of parts that combine ;
 Or, *that* of the co-sines of those that disjoin.”



§ 168. If the data and quæsitæ be opposite sides and angles, the problem proposed may be solved by the proportion (§ 144.) between the sines of opposite sides and angles.

§ 169. A B C represents a right angled spherical triangle upon a plane; B is the right angle, and b the hypotenuse.

§ a . The circular parts, commencing with c , and naming them in the order around to the right, in which they join; are c , a , $\cos. C$, $\cos. b$, and $\cos. A$.

CASE I.

§ 170. Given the hypotenuse (b) and a leg (c).

The hypotenuse $b = 74^\circ 40'$.

The leg $c = 60^\circ 14'$.

To find the other parts.

§ a . 1st. To find the other leg (a).

The three parts that, in this case, comprise the data and quæsitum of the problem, are the two legs (c , a), and the hypotenuse (b). The complement of b , (§ 163. § a .) is not adjacent to either of the other parts, (c , a .); therefore (§ 163.) it is the middle part, and c and a are extremes disjunct; and (§ 166.) $\cos. c \times \cos. a = \text{Sin. } b^\circ \times \text{Rad.}$;* then (§ 71.) $\cos. c : \text{Rad.} :: \text{sin. } b^\circ : \cos. a$.

$$c = 60^\circ 14'. \cos. \text{ar. co.} = 0.804108 (= \sec. c.)$$

$$\text{Radius} \qquad \qquad \qquad 10.$$

$$b = 74^\circ 40'. \cos. (= \text{sin. } b^\circ) = 9.423318$$

$$\text{Cos. } a = 9.726426 = 57^\circ 49'.$$

§ c . In looking in the tables for the degrees, etc., which correspond to the logarithmic co-sine, 9.726426, it will be seen that $122^\circ 11'$, the supplement of $57^\circ 49'$, also corresponds to it. Which of the two to take, is known (§ 141. § b .) by the affection of the two legs.

§ d . The sine, tangent, secant, etc., of an arc or angle, (§ 52. § d .) are the co-sine, co-tangent, co-secant, etc., of the complement of that arc, and (§ 104.) the sine, tangent, secant, etc., of the supplement of the same arc. Therefore,

§ e . Cor. The logarithmic value of any trigonometric function

* To obviate the necessity of writing *complement*, the circular parts of the hypotenuse and two angles will be denoted in the rest of the work by writing an ($^\circ$) after the letter which stands for any one of those parts. Thus, a° , C° , B° , stands for the complements of a , C , B .

corresponds to two arcs or angles; viz., an angle and its supplement. Thus, log. sine $9.611576 = 24^\circ 8'$, or $155^\circ 52'$.

§ f. There is generally some circumstance connected with the conditions of the problem, or triangle, under solution, which determines the affection of the required part, and thence the arc required; for every one of the sides and of the angles of a spherical triangle (§ 136. & § 137.), may be either greater or less than a right angle, or 90° .

§ g. To find the value of a . In this case A° is the middle part. It is between, and joins, the two other parts b° and c . Therefore (§ 162.) b° and c are extremes conjunct. And (§ 165.) $\text{rad.} \times \sin. A^\circ = \text{tang. } c \times \text{tang. } b^\circ$. Then (§ 71.), $\text{rad.} : \text{tang. } b^\circ :: \text{tang. } c : \sin. A^\circ$.

Radius		= 10.
$b = 74^\circ 40'$	co-tang.	= 9.438059 (= tang. b° , § 52. § d.)
$c = 60^\circ 14'$	tang.	10.242655

Sin. A° (= co-sin. A. (§ 52. § d.) = 9.680714 = $61^\circ 21' 9''$.

§ h. $61^\circ 21' 9''$, and *not* its supplement, is known (§ 141. § b. & § d.) to be the required value of the angle A.

§ i. If the angle (C) opposite to (c) one of the given sides be required from the data of this case, the ratio (§ 144.) between the sines of opposite sides and angles, will determine the value of it, viz. : $\text{Sin. } b : \text{sin. } B$ (= (§ 62.) rad.) :: $\text{sin. } c : \text{sin. } C$.

§ j. Or the value of C may be determined by means (§ 166.) of the Catholic Proposition; c (§ 163.) is the middle part, and b° and C° are extremes disjunct; and (§ 166.) $\text{cos. } b^\circ \times \text{cos. } C^\circ = \text{sin. } c \times \text{rad.}$; wherefore (§ 71.) $\text{cos. } b^\circ : \text{rad.} :: \text{sin. } c : \text{cos. } C^\circ$; which is the proportion under § i., stated under different denominations, but the same ultimately; for the co-sine b° and $\text{cos. } C^\circ$ (§ 52. § d.) are the same as $\text{sin. } b$ and $\text{sin. } C$.

$b = 74^\circ 40'$	sin. ar. co.	= 0.015741 = co-sec. (§ 101. § b.)
Radius		= 10.
$c = 60^\circ 14'$	sine	= <u>9.938547</u>

Sine C = 9.954288 = $64^\circ 10' 14''$ (§ 141. § d.)

CASE II.

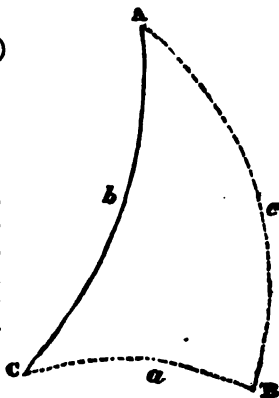
§ 171. Given the hypotenuse (b)
and an angle (C),

$$b = 119^{\circ} 39'$$

$$C = 104^{\circ} 01'$$

To find the other parts.

§ a . 1st. To find the other angle (A).
The two angles (A, C) are adjacent to
the hypotenuse (b), which is therefore
(§ 162.) the middle part, and the two
angles (A, C) are extremes conjunct;
then (§ 170. § g .) $\text{tang. } C^{\circ} : \text{rad.} ::$
 $\text{sin. } b^{\circ} : \text{tang. } A^{\circ}$; and (§ 52. § d .) co-
 $\text{tang. } C : \text{rad.} :: \text{cos. } b : \text{cotang. } A$.



$$C = 104^{\circ} 01' \text{ co-tang. ar. co.} = 0.602691 = \text{tang. } (\S 100. \S a.)$$

$$\text{Radius} = 10.$$

$$b = 119^{\circ} 39' \text{ cos.} = 9.694342$$

$$\text{Co-tang. } A = 10.297033 = 26^{\circ} 46' 36''.$$

§ b . The value of A is known to be less than 90° (§ 141. § c),
because C is greater than a right angle.

§ c . 2d. To find a , which (§ 141. § d .) is also less than a right
angle. The three parts, a, C° , and b° , join in circular order; and
(§ 162. § c .) C° is the middle part, and b° and a are conjunct ex-
tremes. Then (§ 170. § g .) $\text{tang. } b^{\circ} : \text{rad.} :: \text{sin. } C^{\circ} : \text{tang. } a$; and
(§ 52. § d .) $\text{co-tang. } b : \text{rad.} :: \text{cos. } C : \text{tang. } a$.

$$b = 119^{\circ} 39' \text{ co-tang. ar. co.} = 0.244709 = \text{tang. } (\S 101. \S b.)$$

$$\text{Radius} = 10.$$

$$C = 104^{\circ} 01' \text{ cos.} = 9.384182$$

$$\text{Tang. } a = 9.628891 = 23^{\circ} 2' 58''.$$

§ d . 3d. To find c ; c (§ 141. § d .) is greater than a quadrant. The
method for finding the value of c in this case, is similar to that
(§ 170. § j .) of finding C , Case 1.

$$\text{Rad.} : \text{sin. } b :: \text{sin. } C : \text{sin. } c.$$

$$\text{Radius} = 10.$$

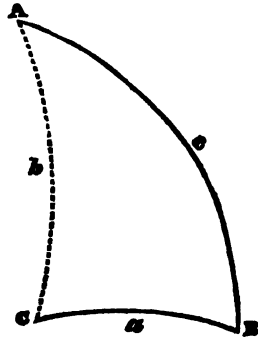
$$b = 119^{\circ} 39' \text{ sin.} = 9.939052$$

$$C = 104^{\circ} 01' \text{ sin.} = 9.986873$$

$$\text{Sin. } c = 9.925925 = 122^{\circ} 31' 18''.$$

CASE III.

§ 172. Given the two legs (a, c),
 $a=31^{\circ} 16'$
 $c=74^{\circ} 14'$



To find the other parts (A, C, b .)

§ *a*. 1st. To find the hypotenuse (b); it is less than a quadrant, because (§ 141. § *b*.) the legs are of the same affection. The three parts, a, b° , and c , do not join each other in the circular order; b° stands alone: then (§ 163. § *a*.) a and c are disjunct extremes, and b° is the middle part; and (§ 170. § *a*. & § XLIX. Alg.) radius :

$$\cos. c :: \cos. a : \sin. b^{\circ} = (\S 52. \S d.) \cos. b.$$

$$\text{Radius} = 10.$$

$$c=74^{\circ} 14' \cos. = 9.434122$$

$$a=31^{\circ} 16' \cos. = 9.931845$$

$$\text{Cos. } b = \frac{9.365967}{9.931845} = 76^{\circ} 34' 12''.$$

§ *b*. 2d. To find an angle (C); it is less (§ 141. § *d*.) than 90° . The three parts C°, a, c , join in circular order; and (§ 162.) C° & c , are conjunct extremes, and a is the middle part: then (§ 165. & § 71.) tang. c : rad. :: sin. a : tang. $C^{\circ} = \text{co-tang. } C$.

$$c=74^{\circ} 14' \text{ tang. ar. co.} = 9.450777 = \text{co-tang. } C$$

$$\text{Radius} = 10.$$

$$a=31^{\circ} 16' \text{ sine} = 9.715186$$

$$\text{Co-tang. } C = \frac{9.165963}{9.715186} = 81^{\circ} 39' 47''.$$

§ *c*. 3d. To find the other angle (A); it is also less than 90° , and it is an extreme conjoined to a by c , which (c) is the middle part; then (§ *b*.) tang. a : rad. :: sin. c : tang. $A^{\circ} = \text{co-tang. } A$.

$$a=31^{\circ} 16' \text{ tang. ar. co.} = 0.216659 = \text{co-tang. } A \text{ (§ 101. § b.)}$$

$$\text{Radius} = 10.$$

$$c=74^{\circ} 14' \text{ sin.} = 9.983345$$

$$\text{Co-tang. } A = \frac{10.200004}{9.983345} = 32^{\circ} 15'.$$

CASE IV.

§ 173. Given the two angles (A, C),

$$A=31^{\circ} 56'$$

$$C=111^{\circ} 11'$$

To find the sides a , b , and c .

§ a. 1st. To find the hypotenuse (b); it is (§ 141. § c.) greater than a quadrant; it connects A° and C° in the circular order, which are conjunct extremes; and (§ 171. § a. § XLIX. Alg.)

$$\text{rad.} : \text{tang. } A^{\circ} :: \text{tang. } C^{\circ} : \text{sin. } b^{\circ}; \text{ or,}$$

$$\text{rad.} : \text{co-tang. } A :: \text{co-tang. } C : \text{cos. } b.$$

$$\text{Radius} = 10$$

$$A=31^{\circ} 56' \text{ co-tang.} = 10.205336$$

$$C=111^{\circ} 11' \text{ co-tang.} = 9.588316$$

$$\text{Cos. } b = 9.793652 = 128^{\circ} 26' 53''.$$

§ b. 2d. To find the leg c ; it and A° are extremes disjunct; and (§ 166. & § 71.)

$$\text{cos. } A^{\circ} : \text{rad.} :: \text{sin. } C^{\circ} : \text{cos. } c; \text{ or,}$$

$$\text{Sin. } A : \text{rad.} :: \text{cos. } C : \text{cos. } c.$$

$$A=31^{\circ} 56' \text{ sin. ar. co.} = 0.276600 = \text{co-sec.} (\S 101. \S b.)$$

$$\text{Radius} = 10.$$

$$C=111^{\circ} 11' \text{ cos.} = 9.557932$$

$$\text{Cos. } c = 9.834532 = 133^{\circ} 5' 32'' (\S 139.)$$

C and c (§ 141. § d.) are of the same affection.

§ c. 3d. To find the other leg a ; it is less than a quadrant, and a disjunct extreme; A° is the middle part, and (§ b.)

$$\text{cos. } C^{\circ} : \text{rad.} :: \text{sin. } A^{\circ} : \text{cos. } a; \text{ or,}$$

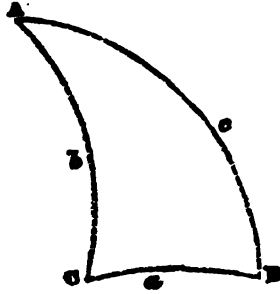
$$\text{Sin. } C : \text{rad.} :: \text{cos. } A : \text{cos. } a.$$

$$C=111^{\circ} 11' \text{ sin. ar. co.} = 0.030384 = \text{co-sec.} (\S 101. \S b.)$$

$$\text{Radius} = 10.$$

$$A=31^{\circ} 56' \text{ cos.} = 9.928736$$

$$\text{Cos. } a = 9.959120 = 24^{\circ} 28' 18''.$$



CASE V.

§ 174. Given an angle (C) and its
opposite leg (c),

$$c = 45^\circ 19'$$

$$C = 54^\circ 49'$$

To find the other parts (*a*, *b*, *A*).

§ *a*. This is called the "doubtful case," because there is nothing in the condition of any problem that falls under this case, which will determine the affection of the part whose value is sought.

§ *b*. 1st. To find the other leg (*a*); it is the middle part, connecting the conjunct extremes, C° and *c*; and (§ 172. § *b*.) $\text{rad.} : \text{tang. } C^\circ :: \text{tang. } c : \sin. a$, or,

$$\text{Rad.} : \text{co-tang. } C :: \text{tang. } c : \sin. a.$$

$$\text{Radius} \quad \quad \quad 10.$$

$$C = 54^\circ 49' \quad \text{co-tang.} = 9.848181$$

$$c = 45^\circ 19' \quad \text{tang.} = 10.004801$$

$$\text{Sin. } a = \frac{9.852982}{10} = 45^\circ 27' 54''.$$

§ *c*. 2d. To find the hypotenuse (*b*); it is a disjoined extreme, and is found (§ 170. § *j*.) $\cos. C^\circ : \text{rad.} :: \sin. c : \cos. b^\circ$; or,

$$\text{Sin. } C : \text{rad.} :: \sin. c : \sin. b.$$

$$C = 54^\circ 49' \quad \text{sin. ar. co.} = 0.087612 = \text{co-sec.} \quad (\S 101. \S b.)$$

$$c = 45^\circ 19' \quad \text{sin.} = 9.851872$$

$$\text{Radius} \quad \quad \quad = 10.$$

$$\text{Sin. } b = \frac{9.939484}{10} = 60^\circ 27' 2''.$$

§ *d*. 3d. To find the other angle (*A*); it is a disjunct extreme; and (§ 173. § *b*.) $\cos. c : \text{rad.} :: \sin. C^\circ : \cos. A^\circ$; or,

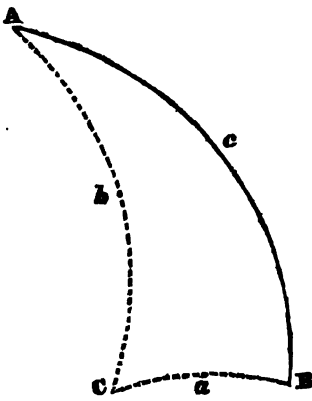
$$\text{Cos. } c : \text{rad.} :: \cos. C : \sin. A.$$

$$c = 45^\circ 19' \quad \text{cos. ar. co.} = 0.152929 = \text{sec.} \quad (\S 101. \S b.)$$

$$\text{Radius} \quad \quad \quad = 10.$$

$$C = 54^\circ 49' \quad \text{cos.} = 9.760569$$

$$\text{Sin. } A = \frac{9.913498}{10} = 55^\circ 1' 30''.$$



CASE VI.

§ 175. Given a leg (c) and its adjacent angle (A),

$$c = 35^\circ 15' 7''$$

$$A = 74^\circ 47'$$

To find the values of the other parts (b , C , a).

§ a . 1st. To find the value of the hypotenuse (b); it is (§ 141. § b . & § d .) less than a quadrant; and the problem is the converse of § g ., Case I, (§ 170.). Tang. c : rad. :: sin. A° : tang. b° ; or,

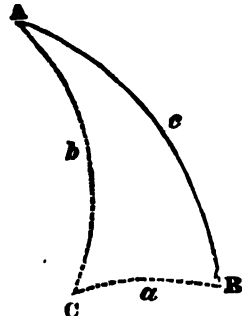
$$\text{Tang. } c : \text{rad.} :: \text{sin. } A : \text{co-tang. } b.$$

$$c = 35^\circ 15' 7'' \text{ tang. ar. co.} = 0.150715 = \text{cot. } (\S 101. \S b.)$$

$$\text{Radius} = 10.$$

$$A = 74^\circ 47' \text{ cos.} = 9.419080$$

$$\text{Co-tang. } b = 9.569795 = 69^\circ 37' 37''.$$



§ b . 2d. To find the value of the angle C . This is the converse of § b ., Case IV. (§ 173.), Radius : cos. A° :: cos. c : sin. C° ; or,

$$\text{Rad.} : \text{sin. } A :: \text{cos. } c : \text{cos. } C.$$

$$\text{Radius} = 10.$$

$$A = 74^\circ 47' \text{ sin.} = 9.984500$$

$$c = 35^\circ 15' 7'' \text{ cos.} = 9.912022$$

$$\text{Cos. } C = 9.896522 = 38^\circ 00' 7''.$$

§ c . 3d. To find the other leg a . The calculation for this is the converse of § c ., Case III., (§ 172.)

$$\text{Tang. } A^\circ : \text{rad.} :: \text{sin. } c : \text{tang. } a; \text{ and } \text{tang. } A^\circ =$$

$$\text{Co-tang. } A = 74^\circ 47' \text{ ar. co.} = 0.565421 = \text{tang. } (\S 101. \S b.)$$

$$\text{Radius} = 10.$$

$$c = 35^\circ 15' 7'' \text{ sin.} = 9.761305$$

$$\text{Tang. } a = 10.326726 = 64^\circ 46' (\S 141. \S d.)$$

§ 176. The rules which have been given for the solution of any problem that can occur in right angled spherical trigonometry, are good in theory; but instances may occur in practice, wherein they will not yield the most accurate result. This apparent defect arises from the trigonometric functions by which certain arcs, or angles, that enter into calculation, are denominated. For instance: If the required part be a very small arc or angle, and the result give its log.

co-sine, the solution is not a good one; because a small error in the log. cos. will produce a much larger one in the arc or angle. This arises from the different manner in which an arc and its sine increase.

§ a. By referring to a logarithmic table, even of six digits in the mantissæ, it will be observed that an arc of 89° 51' may increase 18', or to 90° 9', and that the value of its sine will only vary .000001.

§ b. The same thing is true of the co-sine of the complement of such an arc.

§ c. For these reasons, *the sine of an arc near 90°, or the cos. of one near 1', should not be used in trigonometrical calculation.*

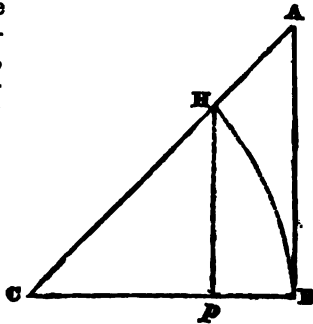
§ 177. The value of sine and co-sine of such arcs may be substituted by their equivalents in other trigonometric functions.

§ 178. The principles from which such equivalents are obtained, are involved in § 75.

§ a. The elements of trigonometry are chiefly contained in the principles of § 43. and § 75.

§ 179. An equivalent for the sine, co-sine, etc., of any angle, may be found by means of the principles developed under § 75.

§ a. Let the proposed angle (C) be made an oblique angle in a right angled triangle (A B C); and from it, with its adjacent side (C B) as radius, describe the arc H B, and draw the sine (H p) of the angle (C) proposed; C p is its co-sine, A B its tangent, and C A its secant.



§ b. Now, instead of naming these sides by letters, denominate them by the trigonometric functions whose offices they fill; thus, calling H p, sin. C; C p, cos. C; A B, tang. C; and so on; we have (§ 75. and § 73.),

$$\text{Sin. } C : \text{cos. } C :: \text{tang. } C : \text{radius}; \text{ or, } \text{sin. } C = \frac{\text{Cos. } C \times \text{tang. } C}{\text{radius.}}$$

$$\text{§ c. } \text{Cos. } C : \text{sin. } C :: \text{rad.} : \text{tang. } C; \text{ or, } \text{cos. } C = \frac{\text{Sin. } C \times \text{rad.}}{\text{tang. } C}$$

§ d. Equivalents for other trigonometric functions may be found after a similar manner; and the same relations exist between the trigonometric functions of plane and spherical triangles. Therefore—

§ 180. The logarithmic sine of any angle is equal to its log. co-sine and tangent, minus radius, or 10. And—

§ 181. The log. cos. of any angle is equal to its log. sine and radius, minus the log. tang. of the same angle.

OBLIQUE SPHERICS.

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OBLIQUE SPHERICS.

§ 182. In every oblique spherical triangle, there are *six parts*, any three of which constitute sufficient data (§ 145.) for determining the value of any of the remaining parts by means of trigonometrical calculation.

§ 183. Every problem in oblique spherical trigonometry is comprised in one of the six following cases; in which the data are,

1st, Two sides and angle opposite to one of them.

2d, Two angles and the side subtending either.

3d, Two angles and the side between them.

4th, Two sides and the angle they include.

5th, The three sides.

6th, The three angles.

§ 184. When any one of the four first cases, comprises the data of the problem, it may be solved by right angled trigonometrical operations; for this purpose the proposed triangle (§ 147. § a.) must be divided into two right angled triangles.

§ a. The perpendicular arc must be so drawn, that *two* of the given parts must be on the *same side* of it, and consequently, in one of the right angled triangles, into which this arc divides the triangle of the problem.

§ 185. The rules in right angled trigonometry, for determining *in species* an unknown side or angle, (i. e. whether it be greater or less than 90°), do not hold good in all cases in oblique trigonometry.

§ 186. The opposite sides and angles of oblique spherical triangles, are not necessarily of the same affection.

§ a. But if the greatest *side* be greater than a quadrant, it and its opposite angle are of the same affection.

§ 187. The converse of § 186. § a. does not hold good; for the sides (§ 136. § a.) of a spherical triangle may be indefinitely small, and the sum of the angles (§ 137.) being greater than two right angles, an obtuse angled spherical triangle may be formed of these indefinitely small sides; in which case an obtuse angle and its subtending side will be unlike.

§ 188. In most cases though, there are circumstances connected either with the condition of the problem, or of the triangle it involves, by which the species of the part required may be determined. Some of these circumstances are mentioned below.

§ 189. If an angle of a triangle be greater than 90° , an arc drawn from it, perpendicular to the subtending side, will fall *within* such triangle.

§ a. If the angles adjacent to the base, be of the same affection, the perpendicular falls upon it, also within the triangle.

§ 190. If all the angles of a triangle be not of the same affection, and a perpendicular arc be drawn from one of the angles which is less than 90° upon the subtending side, it will fall *without* the triangle.

§ 191. An opposite side and angle of a spherical triangle cannot be unlike, unless the sine of this side be greater than the sines of the other sides.

§ *a*. The sine of the angle opposite to such a side is also greater than the sines of the two other angles.

§ *b*. In an isosceles triangle, each side and its opposite angle are alike.

§ 192. If an obtuse side be opposite to an acute angle in any triangle, the two other sides are unlike; and (§ 191.) they and their opposite angles are of the same affection; consequently, the two angles are unlike.

§ *a*. If an obtuse angle subtend an acute side, the other sides and angles are all alike.

§ 193. Whether the perpendicular fall within or without the triangle, the less segment of the base is next to that angle which, of the two adjacent to the base, is the nearer 90° .

§ *a*. When the perpendicular falls within the triangle, the sum of the segments equals the base.

§ *b*. And when it falls without the triangle, the base equals the difference of the segments.

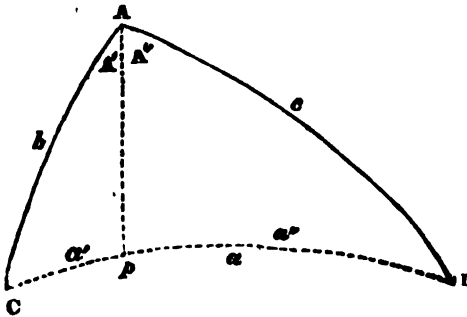
§ 194. If a side and its subtending angle be each less than 90° , a smaller side and its opposite angle, of the same triangle, must be (§ 139.) of the same affection.

§ 195. If the sum of two angles of a triangle be less than 90° , the third angle (§ 137.) is greater than a right angle.

§ 196. By writing co-tang. for the arithmetical complement (§ 101. § *b*.) of the tangent; sec. for the arithmetical complement of cos.; cosec. for the arithmetical complement of sine, etc., greater simplicity and uniformity of calculation will be effected.

§ *a*. The learner will have observed by the reference (§ 101. § *b*.) appended to the arithmetical complement of sines, etc., in some of the calculations in right angled spherical trigonometry, that by taking from the tables the cosec. of an arc, he obtains at once the arithmetical complement of the logarithmic sine of the same arc. So, co-tang. for arithmetical complement of the tangent, etc.

CASE I.



§ 197. Given two sides (*b* & *c*) and an angle (*C*) opposite to one of them,

$$b = 21^\circ 17'$$

$$c = 74^\circ 14'$$

$$C = 69^\circ 10'$$

To find the other parts (*A*, *B* and *a*) by right angular operations.

§ *a*. If the third side (*a*) or its oppo-

site angle (A) be computed, the two other remaining parts are determinable by means of the ratio (§ 144.) between the sines of opposite sides and angles.

§ b. In order that two (*b* & *C*) of the given parts, may be on the same side (§ 184. § a.) of the perpendicular *A p*, it is drawn from *A*, upon its opposite side *a*, so as to divide the triangle of the problem into two right angled triangles *A p C* and *A p B*; the former of which contains two of the given parts (*C* & *b*).

§ c. *C* & *B* are less than 90° (§ 184.); therefore (§ 141. § b.) *C p* & *A p* are each less than 90°; the perpendicular upon the side (*a*) adjacent to *C* & *B* (§ 189. § a.) falls within the triangle; and makes the sum of the segments of the angle *A*, equal to *A*.

§ d. The distance (*C p*) of the given angle (*C*) from the intersecting point (*p*) of the perpendicular and the base, is called auxiliary *a'*.

§ e. To compute the value of the auxiliary arc *a'*.

The method of doing it, is shown under Case II. (§ 171. § c.).

$$\text{Tang. } a' = \frac{\cos. C}{\cot. b} = (\S 196.) \text{ tang. } b \cos. C.$$

$$\begin{aligned} \S f. \quad b &= 21^\circ 17'. & \text{Tang.} &= 9.590562 \\ C &= 69^\circ 10'. & \text{Cos.} &= 9.551024 \end{aligned}$$

$$\text{Tang. auxl. } a' = 9.141586 = 7^\circ 52' 16'' *$$

§ g. The value of *B* is calculated from the ratio (§ 144.) between the sines of sides and of angles. $\text{Sin. } c : \text{sin. } C :: \text{sin. } b : \text{sin. } B$; $\text{sin. } c \text{ ar. co. } (\S 196.) = \text{cosec. } c$.

$$\begin{aligned} \S h. \quad c &= 74^\circ 14' & \text{cosec.} &= 0.016655 \\ C &= 69^\circ 10' & \text{sin.} &= 9.970635 \\ b &= 21^\circ 17' & \text{sin.} &= 9.559883 \end{aligned}$$

$$\text{Sin. } B = 9.547173 = 20^\circ 38' 27''$$

§ i. Now, in the other right angled triangle *A p B*, the value both of *c* and of *B* is known, and the other segment (*p B*) of the base can be determined; for (§ e.) $\text{tang. } B p = \cos. B \text{ tang. } c$.

$$\begin{aligned} \S j. \quad c &= 74^\circ 14' & \text{tang.} &= 0.549223 \\ B &= 20^\circ 38' 27'' & \text{cos.} &= 9.971187 \end{aligned}$$

$$\text{Tang. } B p = 0.520410 = 73^\circ 12' 39''$$

* Rad. (§ 98. § b.), being always equal to 1 or to 10 in logarithmic calculations, is not written down in these formulæ; its value is brought into account by applying it to the log. index of the result, as in the case above. By omitting rad. the formulæ for calculation are rendered more compact and convenient. The proper value will always be given rad. in calculation, by having the log. index of the result to consist only of one figure, as in the case above, where radius is taken into the account by simply writing 9 instead of 19 for the log. index of auxl. *a'*.

§ k. The perpendicular falling within the triangle, makes the *sum* of the segments (§ 193. § a.) equal to the base a ; therefore (§ f. & § j.) $a=81^{\circ} 5' 55''$.

§ l. To find the value of A.

$$\begin{array}{l} \text{Sin. } c : \text{sin. } C :: \text{sin. } a : \text{sin. } A. \\ c = 74^{\circ} 14' \quad \text{cosec.} = 0.016655 \\ C = 69^{\circ} 10' \quad \text{sin.} = 9.970635 \\ a = 81^{\circ} 5' 55'' \quad \text{sin.} = 9.994738 \end{array}$$

$$\text{Sin. } A = 9.982028 = 106^{\circ} 22' 12''; \text{ A is greater}$$

(§ 195.) than 90° .

§ m. The value of A may also be determined by the Catholic Proposition; for (§ 171. § a.) $\cotang. C A p = \frac{\cos. b}{\cot. C} = (\S 196.) \cos. b \text{ tang. } C$. Also $\text{co-tang. } B A p = \cos. c \text{ tang. } B$.

§ n. $B A p + C A p = A$, according as the perpendicular arc A p falls within or without the triangle.

$$\begin{array}{l} \S o. C = 69^{\circ} 10' \quad \text{tang.} = 0.419611 \\ b = 21^{\circ} 17' \quad \text{cos.} = 9.969321 \end{array}$$

$$\text{Co-tang. } C A p = 0.388932 = 22^{\circ} 12' 51''$$

$$\begin{array}{l} B = 20^{\circ} 38' 27'' \quad \text{tang.} = 9.575983 \\ c = 74^{\circ} 14' \quad \text{cos.} = 9.434122 \end{array}$$

$$\text{Co-tang. } B A p = 9.010105 = 84^{\circ} 9' 21''$$

$$B A p + C A p (\S c.) = A \quad 106^{\circ} 22' 12''$$

§ p. The process of solution by such methods of calculation as the above, is circuitous. But cases sometimes occur when they may be used with advantage. And in order that the process, by which the required result is obtained from calculations conducted upon the principles of right angled spherical trigonometry, may be made familiar to the learner, the calculations are carried out.

§ q. By analysis and the use of a little artifice, rules are deduced, and formula constructed, for obtaining the same result from the application of the same principles to calculation, but by less tedious operations. The *auxiliary arcs* and *angles* used in such methods, are derived from the principles of the Catholic Proposition; and the methods themselves are nothing more than right angled spherical calculations, rendered less circuitous in execution by previous combinations, eliminations, and substitutions of the parts that are contained in the two right angled triangles, into which the oblique one of the problem is divided.

§ r. To find the value of A by the help of auxiliaries. Let the angle $B A p$ be called auxiliary A'' ; and let auxiliary A' , be the angle $(C A p)$ which is in the right angled triangle in which two (b, C) , of the given parts of the primitive triangle are contained.

§ s. According to § m. co-tang. $A' = \cos. b \text{ tang. } C$.

§ t. Now, (§ 165. & § XLV. Alg.); $\frac{\text{Tang. } A p}{\text{rad.}}$

$$\frac{\text{Cos. } A'}{\text{cot. } b}; \text{ also } \frac{\text{Tang. } A p}{\text{rad.}} = \frac{\text{Cos. } A''}{\text{cot. } c}; \text{ wherefore } \frac{\text{Cos. } A'}{\text{cot. } c}$$

$$\frac{\text{Cos. } A'}{\text{cot. } b}; \text{ and by transposition, } \text{Cos. } A'' = \frac{\text{Cos. } A' \text{ Cot. } c}{\text{cot. } b}$$

& (§ 101. § b.) $\frac{\text{Cos. } A' \text{ Cot. } c}{\text{cot. } b} = \text{Cos. } A' \text{ Cot. } c \text{ tang. } b$. Therefore,

Cos. auxiliary $A'' = \cos. A' \text{ cot. } c \text{ tang. } b$. Whence the general rule for finding the value of (A) the angle opposite to the unknown side.

§ u. The product (§ s.) of tang. of the given angle, and cos. of the given side that is adjacent to it, is co-tang. of auxiliary A' . And,

§ v. The product of tang. of the same side, and co-tang. of the other given side, multiplied by cos. of auxl. A' (§ t.), is cos. of the other auxiliary A'' . And the sum (§ 193. § a.), or difference (§ 193. § b.), of the two auxiliaries, gives the required angle.

§ w.	$c = 74^\circ 14'$
$b = 21^\circ 17'$	$\text{cot.} = 9.450777$
$\text{cos.} = 9.969321$	$\text{tang.} = 9.590562$
$C = 69^\circ 10'$	$\text{tang.} = 0.419611$

$$\text{Cot. } A' = 9.388932 = 22^\circ 12' 51'' \quad - \quad \text{cos.} = 9.966506$$

$$84^\circ 9' 21'' \quad - \quad \text{Cos. } A'' = 9.007845$$

$$A = 106^\circ 22' 12'' \text{ (§ o.)}$$

§ x. The formula for the calculation (§ w.) is arranged in the most convenient order for operation. The value of auxl. A' is evolved during the process of finding that of the other A'' ; and the log. tang. and cos. of b , are taken out at one opening of the tables; so, also is the value of A' and its cos. System and method in calculation should by no means be neglected. They promote accuracy and facilitate practice. It is therefore the business of every calculator to introduce system in his operations. The habit of arranging the several quantities in the most convenient order for calculation, contributes to accuracy, and makes verification more ready.

§ y. To find the value of a , by the help of auxiliaries. Call the segment $C p$, auxl. a' , and the segment $B p$, auxl. a'' .

§ z. From a train of reasoning analogous to that under § m., it is shown that, tang. auxl. $a' = \text{tang. } b \text{ cos. } C$.

$$\text{§ z a. Also (166. & § XLV. Alg.) } \frac{\text{Rad.}}{\text{cos. } A p} = \frac{\text{Cos. } a'}{\text{cos. } b}; \text{ and}$$

$$\frac{\text{Rad.}}{\text{cos. } A p} = \frac{\text{Cos. } a''}{\text{cos. } c}; \text{ therefore } \frac{\text{Cos. } a''}{\text{cos. } c} = \frac{\text{Cos. } a'}{\text{cos. } b}; \text{ and by transpo-}$$

sition $\cos. a' = \frac{\text{Cos. } a \text{ cos. } c}{\text{cos. } b} = (\S 101. \S b.) \cos. a' \cos. c \text{ sec. } b$;
 then $a' \overset{+}{\infty} a' (\S c. \& \S n.) = a$. Whence the general rule for finding
 the third side.

§ z b. The product of cos. of the given angle and tang. of its adjacent side, is (§ z.) tang. of auxl. a' . And,

§ z c. Sec. of the same side, multiplied by the *product* of cos. of the other side and cos. of auxl. a' (§ z a.), is cos. of the other auxl. a'' .

§ z d. If the two angles adjacent to the base, be each less than 90° , the perpendicular falls within the triangle, and (§ 193. § a.) the *sum* of the auxiliaries is the required part.

§ z e. But if these two angles be unlike, the perpendicular falls without the triangle; and then (§ 193. § b.) the *difference* of the auxiliaries is the required part.

§ z f.
 $b = 21^\circ 17'$ tang. = 0.590562 $c = 74^\circ 14'$ cos. = 0.434123
 $C = 69^\circ 10'$ cos. = 0.551024 - - sec. = 0.030079

Tang. $a' = 0.141586 = 7^\circ 53' 16''$ - cos. = 0.995872

$73^\circ 12' 39''$ - Cos. $a'' = 0.466979$

$a = 81^\circ 5' 55''$ (§ z d.)

§ z g. The value of the third side (a), or of its opposite angle (A), may also be determined by another method; but in this, the value of the other unknown angle (B) is necessary.

§ z h. To determine the third side (a),

Is to the cos. of $\frac{1}{2}$ the difference of the two angles, (B, C);

As to the cos. of $\frac{1}{2}$ their sum;

As tang. of $\frac{1}{2}$ the sum of the two sides (b, c);

Is to tang. of $\frac{1}{2}$ the required side.

§ z i. $\frac{1}{2} (C \infty B) = 24^\circ 15' 46''$ sec. = 0.040162

$\frac{1}{2} (C + B) = 44^\circ 54' 13''$ cos. = 0.850215

$\frac{1}{2} (b + c) = 47^\circ 45' 30''$ tang. = 0.041880

Tang. $\frac{1}{2} a = 0.932257 = 40^\circ 32' 58''$

2

$a = 81^\circ 5' 56''$

§ z j. To find the value of A by a similar method.

Is to the cos. of $\frac{1}{2}$ the difference of the two sides (b, c);

As to the cos. of $\frac{1}{2}$ their sum;

As tang. of $\frac{1}{2}$ the sum of the two angles (A, B);

Is to co-tang. of $\frac{1}{2}$ the angle required.

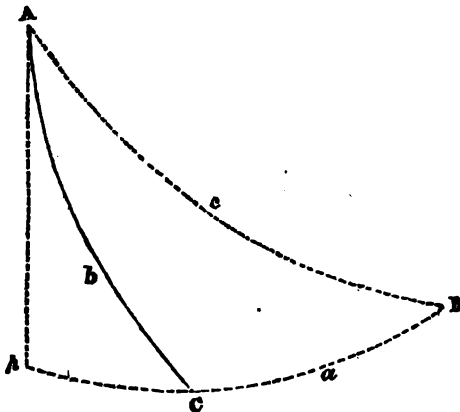
$$\begin{aligned} \S z k. \frac{1}{2} (c \pm b) &= 26^\circ 28' 30'' \text{ sec.} = 0.048114 \\ \frac{1}{2} (c + b) &= 47^\circ 45' 30'' \text{ cos.} = 9.827537 \\ \frac{1}{2} (C + B) &= 44^\circ 54' 13'' \text{ tang.} = 9.998538 \end{aligned}$$

$$\text{Co-tang. } \frac{1}{2} A = 9.874189 = 53^\circ 11' 7''$$

$$\begin{array}{r} 2 \\ \hline A = 106^\circ 22' 14'' \\ \hline \end{array}$$

These two last methods are the most common in practice.

CASE II.



§ 198. Given two angles and the side that subtends one of them,

$$\begin{aligned} B &= 29^\circ 16' \\ C &= 150^\circ 51' 50'' \\ b &= 74^\circ 46' \end{aligned}$$

To find the value of each of the other parts (A, c & a.)

§ a. The value of c (§ 144.) is determinable by a direct calculation; Sin. B : sin. c :: sin. C :

$$\begin{aligned} B = 29^\circ 16' & \quad \text{co-sec.} = 0.810802 \\ b = 74^\circ 46' & \quad \text{sin.} = 9.984466 \\ C = 150^\circ 51' 50'' & \quad \text{sin.} = 9.687427 \end{aligned}$$

$$\text{Sin. } c = 9.982695 = 106^\circ 4' 2''$$

§ b. Suppose the perpendicular (A p) from A, upon the side opposite to A, to fall without the triangle. Then the two known parts in the right angled triangle A p C, are b, and (§ 192.) the supplement of C. The unknown parts of the proposed oblique triangle may be computed by right angled trigonometric operations.

§ c. In the triangle A p C, (§ 197. § e.) tang. C p = cos. C tang. b. Also in the triangle p A B, tang. p B = cos. B tang. c. Then (§ 193. § b.) C p ∝ p B = a.

§ d. The value of A also, may be determined by rules of right angled trigonometry.

§ e. When the perpendicular falls without the triangle, the difference of the two auxiliary angles B A p, and C A p, is the angle A.

P

§ f. But if it falls within the triangle, $B A p + C A p = A$, (§ 197. § n.)

§ g. Co-tang. $p A C = \cos. b \text{ tang. } C$; and co-tang. $B A p = \cos. c \text{ tang. } B$ (§ 197. § m.). Then (§ e.) $A = B A p + C A p$.

§ h. $C = 150^\circ 51' 50''$ $\cos. = 9.941246$ (§ c.)

$b = 74^\circ 46'$ $\text{tang.} = 0.564922$

$$\text{Tang. } C p = \frac{0.506168}{0.564922} = 72^\circ 41' 3''$$

$B = 29^\circ 16'$ $\cos. = 9.940693$

$c = 106^\circ 4' 2''$ $\text{tang.} = 0.540585$

$$\text{Tang. } p B = \frac{0.481278}{0.540585} = 106^\circ 16' 15''$$

$$\text{Now } (\S c.) p B - C p = a = 35^\circ 35' 12''$$

§ i. $C = 150^\circ 51' 50''$ $\text{tang.} = 9.746181$ (§ g.)

$b = 74^\circ 46'$ $\cos. = 9.419544$

$$\text{Co-tang. } p A C = \frac{9.165725}{9.419544} = 81^\circ 40' 4''$$

$c = 106^\circ 4' 2''$ $\cos. = 9.442111$

$B = 29^\circ 16'$ $\text{tang.} = 9.748505$

$$\text{Co-tang. } B A p = \frac{9.190616}{9.748505} = 98^\circ 49' 0''$$

$$\text{Now } (\S e.) B A p - p A C = A = 17^\circ 8' 56''$$

§ j. To determine the third angle (A) by the help of auxiliaries. The angle $p A C$ is auxiliary A' ; and the angle $B A p$ is auxiliary A'' .

§ k. Co-tang. $A' = \cos. b \text{ tang. } C$ (§ g.).

§ l. And (§ 166. and § XLV. Alg.) $\frac{\text{Rad.}}{\cos. A p} = \frac{\text{Sin. } A'}{\cos. C}$; also

$\frac{\text{Rad.}}{\cos. A p} = \frac{\text{Sin. } A''}{\cos. B}$; therefore $\frac{\text{Sin. } A''}{\cos. B} = \frac{\text{Sin. } A'}{\cos. C}$; and by trans-

position, $\text{sin. } A'' = \frac{\text{Sin. } A' \cos. B}{\cos. C} = (\S 101. \S b.) = \text{sin. } A' \cos. B$

sec. C . Whence the general rule for finding the third angle.

§ m. The product of $\cos.$ of the given side, and tang. of its adjacent angle, (§ k.) is co-tang. of auxl. A' . And,

§ n. The product of sec. of the same angle, and sin. of auxl. A' , multiplied by $\cos.$ of the other angle, (§ b.) is sin. of auxl. A'' . And (§ 197. § n.) $A' + A''$ is the required angle.

$$\begin{array}{l} \S o. \\ C=150^{\circ} 51' 50'' \text{ tang.} = 9.746181 \\ b=74^{\circ} 40' \text{ cos.} = 9.419544 \end{array} \qquad \begin{array}{l} B=29^{\circ} 16' \text{ cos.} = 9.940693 \\ \text{sec.} = 0.058754 \end{array}$$

$$\text{Cot. } A' = 9.165725 = 81^{\circ} 40' 4'' \qquad \text{sin.} = 9.995391$$

$$98^{\circ} 49' \qquad \text{Sin. } A'' = 9.994838$$

$$A = 17^{\circ} 8' 56'' (\S e.)$$

$\S p.$ To determine the value of the side (a) opposite to the unknown angle with the help of auxiliaries. Let the segment $p C$ be auxiliary a' ; and the other segment $p B$, be auxiliary a'' ,

$\S q.$ Tang. a' ($\S c.$) = cos. C tang. b .

$\S r.$ And by a process of reasoning similar to that under Case I, ($\S 197. \S z a.$), it is shown that $\text{sin. } a'' = \text{sin. } a' \text{ tang. } C \text{ co-tang. } B$;

for ($\S 165.$) $\frac{\text{Tang. } A p}{\text{rad.}} = \frac{\text{Sin. } a'}{\text{cot. } C}$; also $\frac{\text{Tang. } A p}{\text{rad.}} = \frac{\text{Sin. } A''}{\text{cot. } B}$;

therefore, $\frac{\text{Sin. } a''}{\text{cot. } B} = \frac{\text{Sin. } a'}{\text{cot. } C}$; and by transposition, $\text{sin. } a'' =$

$\frac{\text{Sin. } A' \text{ cot. } B}{\text{cot. } C} = \text{sin. } a' \text{ cot. } B \text{ tang. } C.$ Whence the general rule

for finding the value of the side that subtends the unknown angle.

$\S s.$ The product of tang. the given side, and cos. its adjacent angle ($\S q.$) is tang. of auxl. a' . And,

$\S t.$ Tang. the same angle multiplied by the product of co-tang. the other angle, and sin. the auxl. a' , is sin. the other auxiliary a'' .

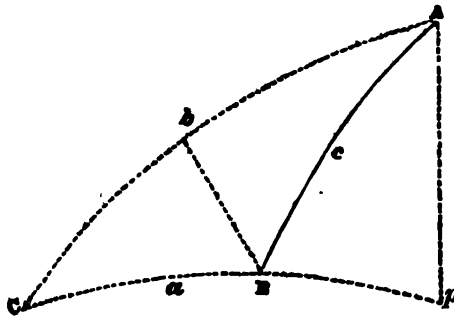
$$\begin{array}{l} \S u. \\ C=150^{\circ} 51' 50'' \text{ cos.} = 9.941246 \\ b=74^{\circ} 46' \text{ tan.} = 0.564922 \end{array} \qquad \begin{array}{l} B=29^{\circ} 16' \text{ cot.} = 0.251495 \\ \text{tang.} = 9.746181 \end{array}$$

$$\text{Tang. } a' = 0.506168 = 72^{\circ} 41' 3'' \qquad \text{sin.} = 9.979857$$

$$108^{\circ} 16' 15'' \text{ Sin. } a'' = 9.977533$$

$$a = 35^{\circ} 35' 12''$$

CASE III.



§ 199. Given two angles, and the side between them,

$$A=19^{\circ} 41'$$

$$B=134^{\circ} 17'$$

$$c=36^{\circ} 19'$$

To find the value of the other parts (a , b , & C .)

§ a . The perpendicular (Ap) being so drawn that the two given parts B , c , may

be on the same side of it, falls without the triangle proposed; and (§ 198. § e .) the auxiliary angle $BAp+A$, equals the auxiliary angle CAp . Also the difference of the auxiliary arcs pB & pC (§ 193. § b .) is the side a .

§ b . If any one of the unknown parts be determined, the two others may be found from the proportion between the sines of opposite sides and angles.

§ c . To determine the value of C by the rules of right angled trigonometry.

§ d . In the right angled triangle BpA , (§ 165. & § 197. § m .) $\text{co-tang. } BAp=\text{cos. } c \text{ tang. } B$. Also, (§ 166.) $\text{sin. } Ap=\text{sin. } B \text{ sin. } c$. And $BAp+A=CAp$.

§ e . Then in the right angled triangle CpA , the parts CAp & Ap are known, and (§ 166.) $\text{cos. } C=\text{sin. } CAp \text{ cos. } Ap$.

$$\text{§ } f. c=36^{\circ} 19' \text{ cos. } =0.906204$$

$$B=134^{\circ} 17' \text{ tang. } =0.010866$$

$$\text{Co-tang. } BAp=0.917079=50^{\circ} 26' 15''$$

$$c \text{ sin. } =0.772503$$

$$B \text{ sin. } =0.854850$$

$$\text{Sin. } Ap=0.627353=25^{\circ} 5' 12''$$

$$BAp+A=CAp=70^{\circ} 7' 15'' \text{ (§ } a.)$$

$$\text{§ } g. CAp=70^{\circ} 7' 15'' \text{ sin. } =0.973318$$

$$Ap=25^{\circ} 5' 12'' \text{ cos. } =0.956969$$

$$\text{Cos. } C=0.930267=31^{\circ} 36' 10''$$

§ h . To find the value of the third angle (C), with the help of auxiliaries. The angle BAp is auxiliary A' . $\text{Co-tang. } A' \text{ (§ } d.) =\text{cos. } c \text{ tang. } B$.

§ i. And (§ 198. § l.) $\frac{\text{Cos. } A p}{\text{rad.}} = \frac{\text{Cos. } B}{\text{Sin. } A'}$; also $\frac{\text{Cos. } A p}{\text{rad.}} = \frac{\text{Cos. } C}{\text{sin. } (A + A')}$; therefore $\frac{\text{Cos. } C}{\text{sin. } (A + A')} = \frac{\text{Cos. } B}{\text{sin. } A'}$; and by transposition, $\text{Cos. } C = \frac{\text{Cos. } B \text{ sin. } (A + A')}{\text{sin. } A'} = \text{cos. } B \text{ sin. } (A + A') \text{ co-sec. } A'$.

§ j. $\text{Cos. } C = \text{cos. } B \text{ co-sec. } A' \text{ sin. } (A + A')$ when $A p$ falls without the triangle. And,

§ k. $\text{Cos. } C = \text{cos. } B \text{ co-sec. } A' \text{ sin. } (A - A')$ when $A p$ falls within it. Whence the rule.

§ l. The product of cos. the given side, and tang. of either angle (§ h.), is co-tang. of auxl. A' . And, (§ i.),

§ m. Cos. of the same angle, multiplied by the product of co-sec. of auxl. A' and sine of the sum (§ j.), or difference (§ k.) of auxl. A' and the other angle, is cos. of the required angle.

§ n.

$c = 36^\circ 19' \text{ cos.} = 9.906204$

$B = 184^\circ 17' \text{ tang.} = 0.010866$

$\text{cos.} = 9.843984$

$\text{Cot. } A' = 9.917070 = 50^\circ 26' 15''$

$\text{cosec.} = 0.112985$

$(A + A') = 70^\circ 7' 15'' \text{ sin.} = 9.978816$

$31^\circ 36' 10'' \text{ Cos. } C = 9.930287$

To find the value of the two sides (a and b) with the help of auxiliaries.

§ o. According to a train of reasoning similar to that shown under Case I, (§ 197. § t.) $\text{cot. } b = \text{cot. } c \text{ cos. } (A + A') \text{ sec. } A'$; for

$\frac{\text{Rad.}}{\text{Cot. } b} = \frac{\text{Cot. } c}{\text{cos. } A'}$; also $\frac{\text{Rad.}}{\text{Cot. } b} = \frac{\text{Cot. } c \text{ cos. } (A + A')}{\text{Cot. } b}$; then

$\frac{\text{Cot. } c}{\text{cos. } (A + A')} = \text{cos. } A'$; and by transposition, $\text{cot. } b =$

$\frac{\text{Cot. } c \text{ cos. } (A + A')}{\text{cos. } A'} = \text{cot. } c \text{ cos. } (A + A') \text{ sec. } A'$.

§ p. By drawing the perpendicular from B upon its opposite side, and calling the angle $A B b$ auxiliary B' , we obtain by a similar process of reasoning. $\text{Cot. } a = \text{cot. } c \text{ cos. } (B + B') \text{ sec. } B'$.

§ q. $\text{Cot. } B' = \text{cos. } c \text{ tang. } A$. Whence the rule for finding the value of either unknown side.

§ r. The product of cos. the given side and tang. of the angle (§ h. & § q.) opposite to the required side, is co-tang. of the required auxiliary which call A' . And (§ o. & § p.),

§ s. The product of cot. the given side and sec. of this auxl. A' ,

multiplied by cos. of the sum, or difference of A' and the angle adjacent to the required side, is co-tang. of the required side.

§ *t.* To find the value of *b* by this rule.

$$B = 134^\circ 17' \text{ tang.} = 0.010866$$

$$c = 36^\circ 19' \text{ cos.} = 9.906204 \quad - \quad - \quad - \quad \text{cot.} = 0.133700$$

$$\text{Cot. } A' = 9.917070 = 50^\circ 26' 15'' \quad - \quad \text{sec.} = 0.195916$$

$$(A + A') = 70^\circ 7' 15'' \text{ cos.} = 9.531528$$

$$54^\circ 0' 27'' \text{ Cot. } b = 9.861144$$

§ *u.* To find the value of *a* by the same rule.

$$A = 19^\circ 41' \text{ tang.} = 9.553548$$

$$c = 36^\circ 19' \text{ cos.} = 9.906204 \quad - \quad - \quad - \quad \text{cot.} = 0.133700$$

$$\text{Cot. } A' = 9.459752 = 73^\circ 55' 15'' \quad - \quad \text{sec.} = 0.557576$$

$$(B - A') = 60^\circ 21' 45'' \text{ cos.} = 9.694175$$

$$22^\circ 22' 32'' \text{ Cot. } a = 0.385451$$

§ *v.* A triangle that has a side or an angle greater than 180° must never be used in the solution of trigonometrical problems.

§ *w.* Therefore in the solution of all cases (§ *u.*) where the sum, or difference of an auxiliary, and an arc or angle, is to be brought into calculation, if the *sum* would exceed 180° , the *difference* is the proper quantity to be used.

§ *x.* The two unknown sides may also be determined by a method of calculation differing from that above, but depending on principles analogous to those under § 77. for plane triangles. This method is the most common in practice.

§ *y.* The sine of $\frac{1}{2}$ the *sum* of the two given angles (A, B);
Is to the sine of $\frac{1}{2}$ their *difference*;
As the tang. of $\frac{1}{2}$ the given side (*c*);
Is to the tang. of $\frac{1}{2}$ the *difference* of the two required sides (*a, b*). And,

§ *z.* Cos. of the *same* $\frac{1}{2}$ *sum*;
Is to the cos. of the *same* $\frac{1}{2}$ *difference*;
As the tang. of $\frac{1}{2}$ the given side;
Is to the tang. of $\frac{1}{2}$ the *sum* of the two required sides (*a, b*.)

$$\begin{aligned} \S z a. \quad \frac{1}{2} (A+B) &= 76^\circ 59' \text{ co-sec.} = 0.011305 \\ \frac{1}{2} (A-B) &= 57^\circ 18' \text{ sin.} = 9.925060 \\ \frac{1}{2} c &= 18^\circ 9' 30'' \text{ tang.} = 9.515844 \end{aligned}$$

$$\text{Tang. } \frac{1}{2} (a \times b) = 9.452209 = 15^\circ 48' 58''$$

$$\begin{aligned} \frac{1}{2} (A+B) \text{ sec.} &= 0.647365 \\ \frac{1}{2} (A-B) \text{ cos.} &= 9.732587 \\ \frac{1}{2} c \text{ - tang.} &= 9.515844 \end{aligned}$$

$$\text{Tang. } \frac{1}{2} (a+b) = 9.895796 = 38^\circ 11' 29''$$

§ z b. The greater side (*b*) is opposite (§ 139.) to the greater angle; and (§ 77. § g.) $38^\circ 11' 29'' + 15^\circ 48' 58'' = 54^\circ 00' 27''$ or *b*; and $a = (38^\circ 11' 29'' - 15^\circ 48' 58'') = 22^\circ 22' 31''$.

§ z c. To determine the value of the third angle (*C*) with the help of an auxiliary arc *a'*.

§ z d. The sine of $\frac{1}{2}$ the sum } of the two given angles
 Is to $\frac{1}{2}$ the sum of the sines } (*A* & *B*);
 As the sine of $\frac{1}{2}$ the given side (*c*);
 Is to the sine of auxl. *a'*. Then,

§ z e. The product of cos. of auxl. *a'* and sine of $\frac{1}{2}$ the sum of the two given angles, is cos. of $\frac{1}{2}$ the third angle (*C*).

$$\begin{aligned} \S z f. \quad B &= 134^\circ 17' \text{ sin.} = 9.854850 \\ A &= 19^\circ 41' \text{ sin.} = 9.527400 \end{aligned}$$

$$2) 19.382250$$

$$9.691125 = \frac{1}{2} \text{ sum of the sines of the two given angles.}$$

$$\begin{aligned} \frac{1}{2} c = 18^\circ 9' 30'' \text{ sin.} &= 9.493659 \\ \frac{1}{2} (A+B) = 76^\circ 59' \text{ co-sec.} &= 0.011305 \quad - \quad \text{sin.} = 9.988695 \end{aligned}$$

$$\text{Sin. auxl. } a' = 9.196089 = 9^\circ 2' 12'' \text{ cos.} = 9.994576$$

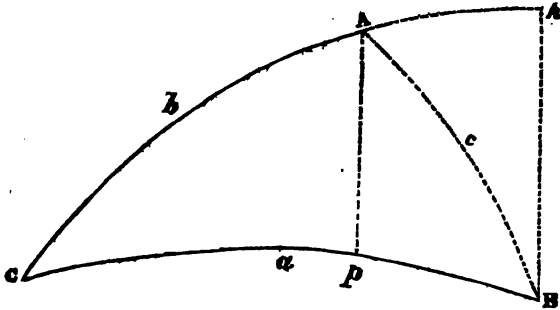
$$15^\circ 48' 5'' \text{ Cos. } \frac{1}{2} C = 9.983271$$

2

$$C = 31^\circ 36' 10''$$

CASE IV.

§ 200. Given two sides and the angle they include,



$$\begin{aligned} a &= 109^\circ 30' \\ b &= 60^\circ 00' \\ C &= 27^\circ 06' \end{aligned}$$

To find the other parts (A, B, c). This is the converse of Case III., for we have to find here what is there given.

§ a. If the perpendicular A p fall within the triangle, the sum of the segments (C p + p B) is equal to a; and the sum of the auxiliary angles, C A p + p A B = A.

§ b. Any one of the unknown parts of the triangle proposed, being found, the two others are determinable from the relations (§ 144.) of sides to their opposite angles.

§ c. To find B, by the Catholic Proposition. By Case II.,

$$(\S 171. \S c.) \text{ tang. } C p = \frac{\text{Cos. } C}{\text{Cot. } b} = (\S 101. \S b.) \text{ cos. } C \text{ tang. } b; \text{ also}$$

(§ 171. § d.) $\sin. A p = \sin. b \sin. C$. Then (§ a.) $a - C p = p B$; and the value of A p, and of B p, in the triangle A p B, being known, that of B (§ 155.) is determinable; $\text{cotang. } B = (\S 172. \S b.) = \frac{\text{Sin. } p B}{\text{Tang. } A p} = \sin. p B \text{ cotang. } A p$.

$$\begin{aligned} \S d. \quad C &= 27^\circ 6' \quad \text{cos.} = 9.949494 \\ b &= 60^\circ 0' \quad \text{tang.} = 0.238561 \end{aligned}$$

$$\text{Tang. } C p = \frac{0.238561 \times 9.949494}{1} = 0.188055 = 57^\circ 2' 4''$$

$$\begin{aligned} C \sin. &= 9.658531 \\ b \sin. &= 9.937531 \end{aligned}$$

$$\text{Sin. } A p = \frac{9.658531}{9.937531} = 9.596062 = 23^\circ 14' 8''$$

$$109^\circ 30' - 57^\circ 2' 4'' (\S a.) = p B = 52^\circ 27' 56''$$

§ e. p B = $52^{\circ} 27' 58''$ Sin. = 9.899267
 A p = $29^{\circ} 14' 8''$ Cotang. = 0.367204

Cotang. B = $10.266471 = 28^{\circ} 25' 54''$

§ f. To find the value of each of the unknown angles (A, B), with the help of an auxiliary arc (a'). A perpendicular drawn from either of the unknown angles (A, B) fulfils the conditions of § a. (§ 184.); suppose the perpendicular drawn from B to the fall without the triangle.

§ g. Let the distance (Cp or Ch) of the given angle from the perpendicular be auxiliary a' . Then whether the perpendicular fall within or without the triangle, the *difference* (§ d.) between the side upon which it falls and the auxl. a' is the other segment of that side.

§ h. First, to find the value of B, the arc Cp being auxl. a' ; tang. a' (§ d.) = $\cos C \text{ tang. } b$.

§ i. According to Case II. (§ 198. § r.) $\frac{\text{Rad.}}{\text{tang. } A p} = \frac{\text{Cot. } C}{\text{Sin. } a'}$
 $\frac{\text{Cot. } B}{\text{Sin. } (a \infty a')}$; and by transposition $\text{Cot. } B = \frac{\text{Cot. } C \text{ Sin. } (a \infty a')}{\text{Sin. } a'}$
 = $\text{cot. } C \text{ sin. } (a \infty a') \text{ cosec. } a'$.

§ j. To find the value of A. In the triangle ChB, Ch is auxl. a' ; and $\text{tang. } a' = \cos. C \text{ tang. } a$.

§ k. Also, $\frac{\text{Rad.}}{\text{Tang. } B h} = \frac{\text{Cot. } C}{\text{Sin. } a'} = \frac{\text{Cot. } A}{\text{Sin. } (b \infty a')}$; and by transposition, $\text{Cot. } A = \frac{\text{Cot. } C \text{ Sin. } (b \infty a')}{\text{Sin. } a'}$ = $\text{cot. } C \text{ sin. } (b \infty a') \text{ cosec. } a'$.

Whence the general rule for finding either angle.

§ l. The product of $\cos.$ of the given angle (§ h. and § j.) and tang. of the side *opposite* to the required angle, is tang. of auxl. a' . And,

§ m. The *sin.* of the *difference* between auxl. a' and the side *adjacent* to the required angle, multiplied by the *product* of the cosec. of auxl. a' and cotang. of the given angle (§ i. and § h.), is cotang. of the required angle.

§ n. $b = 60^{\circ} 0'$ tang. = 0.238561
 $C = 27^{\circ} 6'$ cos. = 9.949494 - - cot. = 0.290963

Tang. auxl. $a' = 0.188055 = 57^{\circ} 2' 4''$ cosec. = 0.076240

$(a' \infty a) = 52^{\circ} 27' 56''$ sin. = 9.899268

$28^{\circ} 25' 54''$ Cot. B = 0.266471

§ o. Or, to find the value of A ;
 $a = 109^\circ 30' \text{ tang} = 0.450851$
 $C = 27^\circ 6' \text{ cos.} = 9.949494$ - - - $\text{cot.} = 0.290963$

 $\text{Tang. } a' = 0.400345 = 111^\circ 41' 32''$ $\text{cosec.} = 0.031898$
 $(a' \omega b) = 51^\circ 41' 32''$ $\text{sin.} = 9.894699$

 $148^\circ 47' 10''$ $\text{Cot. A} = 0.217560$

§ p. The value of the third side (c) can be found with the help of the same auxiliary a'.

§ q. When the perpendicular falls within the triangle, $\frac{\text{Cos. } A p}{\text{Rad.}}$
 (§ 198. § l.) $= \frac{\text{Cos. } b}{\text{Cos. } a'} = \frac{\text{Cos. } c}{\text{Cos. } (a \omega a')}$; by transposition $\text{Cos. } c =$
 $\frac{\text{Cos. } b \text{ Cos. } (a \omega a')}{\text{Cos. } a'} = \text{cos. } b \text{ cos. } (a \omega a') \text{ sec. } a'.$

§ r. And when the perpendicular (Bh) falls without the triangle,
 $\frac{\text{Cos. } B h \text{ Cos. } a}{\text{Rad.}} = \frac{\text{Cos. } c}{\text{Cos. } (b \omega a')}$; by transposition, $\text{cos. } c =$
 $\frac{\text{Cos. } a \text{ Cos. } (b \omega a')}{\text{Cos. } a'} = \text{cos. } a \text{ cos. } (b \omega a') \text{ sec. } a'.$

N. B. $(a \omega a') = p B$, and $(b \omega a') = A h$.

Hence the general rule for finding the third side.

§ s. The product of cos. of the given angle, and tangent of either given side, (§ h. & § j.), is tang. of auxl. a'.

§ t. Then (§ q. & § r.) cos. of the same given side, multiplied by the product of sec. of auxl. a', and cos. of the difference between auxl. a', and the other given side, is cos. of the required side.

§ u. $C = 27^\circ 6' \text{ cos.} = 9.949494$
 $b = 60^\circ 0' \text{ tang.} = 0.238561$ - - - $\text{cos.} = 9.898970$

 $\text{Tang. } a' = 0.188055 = 57^\circ 2' 4''$ $\text{sec.} = 0.264293$
 $(a \omega a') = 52^\circ 27' 56''$ $\text{cos.} = 9.784786$

 $55^\circ 57' 24''$ $\text{Cos. } c = 9.748049$

§ v. Or, taking the tang. and cos. of a ;

$C = 27^\circ 6' \text{ cos.} = 9.949494$
 $a = 102^\circ 30' \text{ tang.} = 0.450851$ - - - $\text{cos.} = 9.523495$

 $\text{Tang. } a' = 0.400345 = 111^\circ 41' 32''$ $\text{sec.} = 0.432244$
 $(b \omega a') = 51^\circ 41' 32''$ $\text{cos.} = 9.792312$

 $55^\circ 57' 24''$ $\text{Cos. } c = 9.748051$

§ w. The difference between the two log. co-sines of c arises from fractions of a second (") , which are in some of the parts operated upon. These fractions may sometimes cause an error of a few seconds (") in the value of the part required.

§ x. There is a method for finding the value of the two angles (A & B) analogous to that under § y. and § z. (§ 199.), for finding two sides. In drawing up formulæ, and selecting methods, for trigonometrical calculations, attention should be paid to what is given, as well as to what is required, in the problem; and that method of solution should be adopted, which equally as correct as others, leads most directly to the result required.

§ y. To find A and B without the help of auxiliaries.

§ z. The cos. of $\frac{1}{2}$ the *sum*, } of the two sides;
 Is to cos. of $\frac{1}{2}$ the *difference*, }
 As co-tang. of $\frac{1}{2}$ the given angle;
 Is to tang. of $\frac{1}{2}$ the *sum* of the required angles.

§ z a. The sine of $\frac{1}{2}$ the *sum*, } of the two sides;
 Is to the sine of $\frac{1}{2}$ the *difference*, }
 As co-tang. of $\frac{1}{2}$ the given angle;
 Is to tang. of $\frac{1}{2}$ the difference of the required angles.

§ z b. $\frac{1}{2}(a+b) = 84^\circ 45' \text{ sec.} = 1.038571$
 $\frac{1}{2}(a-b) = 24^\circ 45' \text{ cos.} = 9.958154$
 $\frac{1}{2} C = 13^\circ 33' \text{ cot.} = 0.617980$

Tang. $\frac{1}{2}$ sum (A & B) = 1.614705 = $88^\circ 36' 32''$

$\frac{1}{2}(a+b)$, co-sec. = 0.001826
 $\frac{1}{2}(a-b)$, sin. = 9.621861
 $\frac{1}{2} C$ cot. = 0.617980

Tang. $\frac{1}{2}$ diff. (A & B) = 0.241667 = $60^\circ 10' 38''$

§ x c. $88^\circ 36' 32'' + 60^\circ 10' 38'' = A = 148^\circ 47' 10''$ } ($\S 77. \S h.$)
 And, $88^\circ 36' 32'' - 60^\circ 10' 38'' = B = 28^\circ 25' 54''$ }

§ z d. The following method of finding the value of the third side (c) with the help of an auxl. a' , is useful and of frequent occurrence in nautical calculations.

§ z e. Half the *product* of the sines of the given sides, and *twice* the sine of half the given angle, *multiplied* by the co-sec. of $\frac{1}{2}$ the *difference* between the two sides, is the tang. of auxl. a' .

§ z f. Then the product of co-sec. of a' and said *half product* of the sines of the *three* said quantities, is the sine of *half* the required side.

§ z g.

$$a = 109^\circ 30' \sin. = 9.974347$$

$$b = 60^\circ 00' \sin. = 9.937531$$

$$\frac{1}{2} C = 13^\circ 33' \sin. \times 2 = 18.739522$$

$$2 \cdot 38.651400$$

$$19.325700$$

$$19.325700$$

$$\frac{1}{2} (a \sin b) = 24^\circ 45' \text{ co-sec.} = 0.378139$$

$$\text{Tang. auxl. } a' = 9.703839 = 26^\circ 49' 22'' \text{ cosec.} = 0.345600$$

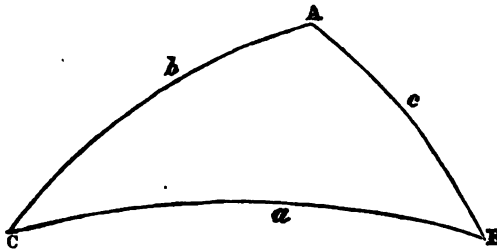
$$27^\circ 58' 42''$$

$$\text{Sin. } \frac{1}{2} c = 9.671300$$

2

$$c = 55^\circ 57' 24''$$

CASE V.



§ 201. Given the three sides

$$a = 66^\circ$$

$$b = 44^\circ$$

$$c = 30^\circ$$

To find the angles.

§ a. Neither in this, nor in the preceding case, can the value of any one of the unknown

parts be determined by the Catholic Proposition; for the proposed triangle cannot be so divided into two right angled triangles, that two of the given parts shall be contained in either of them.

§ b. This, and the case that immediately precedes it, are particularly useful to the navigator. Some of the most important problems, and those which are of most frequent occurrence in navigation, come under one or both of these cases for solution. The problems, for finding azimuths and the time of day at sea, fall under this case. This and the preceding case are both involved in the calculations for finding the *true*, from the *observed*, lunar distance. Both cases are also involved in finding the latitude by "double altitudes." And by Case IV, the lunar tables in the nautical almanac, are calculated.

§ c. In this, as under the other cases, there are several methods for finding the value of the required part. In all cases the methods, which are the best adapted to practical purposes, are given.

§ d. To find one of the angles (A). The *product* of the co-sec. of the sides that contain the required angle, *multiplied* by the *pro-*

duct of the sine of half the sum of the three sides, and sine of that half sum, less the side opposite the required angle, is double the cos. of $\frac{1}{2}$ the required angle.

§ e. Twice the tang. of $\frac{1}{2}$ the required angle, is the product of co-sec. of $\frac{1}{2}$ the sum of the three sides, and co-sec. of said $\frac{1}{2}$ sum, less the side opposite the required angle, multiplied by the product of the sines of the difference between said half sum and each of the sides that contain the required angle.

$$\begin{aligned} \S f. \quad a &= 66^\circ \quad (\S d.) \\ b &= 44^\circ \text{ co-sec.} = 0.158229 \\ c &= 30^\circ \text{ co-sec.} = 0.301030 \end{aligned}$$

$$\underline{\underline{2)140^\circ}}$$

$$\frac{(a+b+c)}{2} = 70^\circ \text{ sin.} = 9.972986$$

$$\frac{(a+b+c-a)}{2} = 4^\circ \text{ sin.} = 8.843585$$

$$\text{Twice cos. } \frac{1}{2} A = 2)19.275830$$

$$\text{Cos. } \frac{1}{2} A = 9.637915 = 64^\circ 15' 5''$$

2

$$A = 128^\circ 30' 10''$$

$$\S g. \quad \frac{(a+b+c)}{2} = 70^\circ \text{ co-sec.} = 0.027014 \quad (\S e.)$$

$$\frac{(a+b+c-a)}{2} = 4^\circ \text{ co-sec.} = 1.156415$$

$$\frac{(a+b+c-b)}{2} = 26^\circ \text{ sin.} = 9.641842$$

$$\frac{(a+b+c-c)}{2} = 40^\circ \text{ sin.} = 9.808068$$

$$\text{Twice tang. } \frac{1}{2} A = 2)20.633339$$

$$\text{Tang. } \frac{1}{2} A = 10.316669 = 64^\circ 15' 5''$$

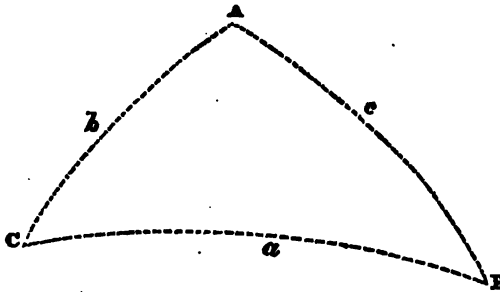
2

$$A = 128^\circ 30' 10''$$

§ h. In all cases § g. is a good solution. But when the required angle (A) is near 180° , (§ 176. § c.) solution § f. will not carry great accuracy into the result. But this seldom occurs in practice, and in most cases either solution may be adopted with success.

§ i. One of the angles being found, the two others (§ 144.) are determinable.

CASE VI.



§ 202. Given the three angles,

$$A = 114^\circ$$

$$B = 39^\circ$$

$$C = 49^\circ$$

To find the value of the sides.

§ a. This problem is but of little practical utility to the navigator, for problems in

which the three angles of a triangle are the data, seldom occur. But there are several methods by which the side required may be found; one of which, being general in its application, is thought sufficient.

§ b. The *product* of *cos.* of the difference between half the sum of the three angles, and each angle adjacent to the required side, *multiplied* by the *product* of *co-sec.* of each of said angles, is twice the *cos* of $\frac{1}{2}$ the required side.

§ c. To find the value of a .

$$\frac{(A+B+C)}{2} - B = 62^\circ \text{ co-sine} = 9.671609$$

$$\frac{(A+B+C)}{2} - C = 52^\circ \text{ co-sine} = 9.789342$$

$$B = 39^\circ \text{ co-sec.} = 0.201128$$

$$C = 49^\circ \text{ co-sec.} = 0.122220$$

$$\text{Twice cos. of } \frac{1}{2} a = 2) 19.784299$$

$$\text{Cos. } \frac{1}{2} a = 9.892149 = 38^\circ 43' 50''$$

$$\frac{2}{a} = 77^\circ 27' 40''$$

§ d. The value of one side being known, that of the others is determinable.

NAUTICAL ASTRONOMY.

NAUTICAL ASTRONOMY.

§ 203. That part of astronomy which treats of the motions and of the positions of the heavenly bodies, is an important branch of navigation. A knowledge of these motions and positions is highly essential to the navigator; for it is by understanding them, that methods have been devised for determining latitude and longitude at sea, by means of observations made upon the heavenly bodies.

§ 204. The figure of the earth is that of an oblate spheroid. It resembles that which would be described by the revolution of a semi-ellipse about its minor axis. It is flattened in at the poles, and elevated towards the equator.

§ 205. To suit the common purposes of navigation, the earth may be considered as a perfect sphere; the sun as the centre of the universe, and the centre of motion in the planetary system; the fixed stars may be considered to be almost stationary, and immeasurably distant from the earth and from each other; from every part of the earth's orbit, they are seen in the same relative positions, with regard to each other.

§ 206. The earth has two rotary motions; one about its axis, which produces day and night; the other in its orbit, and around the sun, which causes the seasons.

§ a. The latter is called the earth's annual, and the former its diurnal, motion.

§ 207. In its annual revolution around the sun, the earth describes the periphery of an ellipse.

§ a. The centre of the sun is in the plane, and at one of the foci of this ellipse, and the centre of the earth moves on its circumference.

§ 208. The axis of the earth is inclined, from a perpendicular to the plane of its orbit, nearly at an angle of $23^{\circ} 28'$.

§ a. If the earth's axis were perpendicular to this plane, there would be no change of seasons, or variation in the length of day and night; and at either pole there would be continual day.

§ b. It is this angle of inclination which causes the *declination* of the sun.

§ c. In a northern winter, the earth is nearer to the sun than it is in summer; but owing to the sun's declination, or the inclination of the earth's axis to the plane of the earth's orbit, the south pole is turned towards the sun during the former season, and the sun's rays striking the northern hemisphere more obliquely than they do in

summer, are in consequence, spread over a greater surface, and are therefore less effective in producing heat.

§ 209. The earth revolves from west to east. It completes one revolution on its axis in a day, and one around the sun in a year.

§ 210. The periphery of the earth's orbit, like the circumference of every re-entering curve, contains 360° .

§ a. The earth completes one revolution in its orbit, in 365d, 5h, 48m, and 48s.

§ b. Therefore, the motion of the earth in its orbit, in one day, is, as 365d, 5h, 48m, 48s is to 360° ; the ratio of which is $59' 8''$.

§ 211. An *astronomical, sea* or *civil*, day, is the time between two consecutive noons, or midnights.

§ 212. A *sidereal* day is the time between two consecutive transits of a star across the same meridian.

§ 213. The intervals of time from the passage of the sun and a star across, until their return to, the same meridian, are unequal. The difference between these intervals, results from the combined effect of the earth's motion about her axis, and in her orbit; for, during the interval between two consecutive transits of a star across the same meridian, the earth advances in its orbit (§ 210. § b.) nearly $59' 8''$; so that the transit meridian has to go $59' 8''$ more than one complete revolution around the axis of the earth, before it returns to the sun.

§ a. Thus, during the time in which the earth is making one complete revolution in its orbit, a star has one transit more than the sun has, across any proposed meridian.

§ b. Sidereal accelerates upon *mean* solar time, 3m, 56s.55 in 24h, or about $9\frac{1}{2}$ s in an hour.

§ 214. The motion of the earth about its axis, is uniform; but the velocity of the earth in its orbit, is irregular. This irregularity is caused by the variation in the mutual action of the centrifugal and centripetal forces upon the earth.

§ a. The sidereal day is consequently of a uniform length; and the solar day varies with the velocity of the earth in its orbit.

§ b. This variation produces *equation of time*.

§ 215. *Apparent time* is the time which is deduced by calculation, from the bearing, or the altitude of the sun.

§ a. The time shown by a dial, is apparent time.

§ 216. *Mean time* is the average of apparent time.

§ a. Watches, etc., are designed to keep mean time.

§ 217. *Equation of time* is the difference between mean and apparent time.

§ 218. If the motion of the earth in its orbit, were uniform, describing equal arcs in equal times, there would always be the same length of time from one transit of the sun to another, across the same meridian; and apparent and mean time would always agree. But from noon to the succeeding noon, there is sometimes more, and sometimes less, than 24 hours.

§ a. Twenty-four hours is the average, or mean of the time, in

which, during one complete revolution of the earth in its orbit, the sun performs every one of its 365 transits across the same meridian.

§ *b*. This is the time which all good time pieces show. The time shown by them and the sun agrees only four times during a year; when this agreement takes place, then there is no equation of time.

§ 219. All astronomical calculations, such as those in the nautical almanacs, etc., are computed for astronomical time.

§ *a*. Of those in the ephemeris, some are for *mean*, and some for *apparent* astronomical time.

§ 220. An astronomical day commences when the centre of the sun is on the meridian (say of Greenwich), and ends, when it returns to the same meridian.

§ *a*. An astronomical day is divided into 24 hours, which are reckoned in succession, from 1 up to 24.

§ 221. A civil day commences at the midnight, that *precedes* the beginning of the astronomical day.

§ *a*. A civil day is divided into two equal portions; the first is A.M.; it ends at noon, when the astronomical day begins: the latter is P.M.; it ends at midnight, when the succeeding day begins. Each division consists of 12 hours.

§ *b*. Consequently, the day civil, is always 12 hours in advance of the day astronomical. Thus, Dec. 11th, 9h 34m 44s A.M. is, according to astronomical time, Dec. 10th, 21h 34m 44s; and 16 hours of civil time, or Dec. 11th, 4h P.M., is Dec. 11th, 4h, according to the astronomical time. Therefore, when the civil time is A.M. 12 hours added to it makes it astronomical time.

§ 222. The *ecliptic* is a great circle, the centre of which is that of the earth, and the plane of which coincides with the plane of the earth's orbit. Therefore these planes cut the axis of the earth at the same angle.

§ 223. The sun is always in the ecliptic.

§ *a*. Considering the earth to be stationary in its orbit, the sun appears to perform an annual revolution, moving around the earth, on the periphery of the ecliptic, and crossing the equator twice during the year.

§ 224. The ecliptic is divided into 12 arcs, of 30° each. These divisions, named and marked, are called the Signs of the Zodiac. They are—

§ *a*. Aries (♈), Taurus (♉), Gemini (♊), Cancer (♋), Leo (♌), Virgo (♍), Libra (♎), Scorpio (♏), Sagittarius (♐), Capricornus (♑), Aquarius (♒), and Pisces (♓).

§ *b*. The first six being north of the equator, are called *northern signs*.

§ *c*. The other six are south of the equator, and are called *southern signs*.

§ 225. The points in which the ecliptic (§ 223. § *a*.) crosses the equator, are called the *equinoctial points*; because, when the sun passes through these points, the days and nights are equal.

§ 226. The sun crosses the equator, and enters the first point of

Aries, about the 21st of March. The sun then passes through **Aries**, **Taurus**, and **Gemini**, towards the north; and about the 21st of June, it reaches its greatest northern declination at the first point of **Cancer**, where it appears to be stationary for a while; it is then said to be in the *summer solstice*.

§ a. The first point of **Cancer**, is a *solstitial point*.

§ b. Returning thence, towards the south, the sun passes through **Cancer**, **Leo**, and **Virgo**, and completing its tour, or the north side of the equator, it arrives, about the 23d of September, at the intersection of the ecliptic with the equator, when the day and night are again equal, and the sun is in the *autumnal equinox*.

§ c. Recrossing the equator then, the sun enters the first point of **Libra**, and continuing on towards the south, it *descends* through **Libra**, and the succeeding signs, and reaches its greatest southern declination, about the 22d of December; then it is at the first point of **Capricorn**, and again appears to stand still.

§ d. The sun is now in its winter solstice; and returning towards the north, it *ascends* through **Capricorn**, **Aquarius**, and **Pisces**, and entering the first point of **Aries**, completes one annual revolution, and goes on to renew the seasons.

§ 227. The time from the sun's passing the first point of **Aries**, until its return to that point again, is about (§ 210. § a.) 365d 5h 48m 48s.

§ a. This is called a *solar*, or a *tropical year*, and it is the year by which the seasons are regulated.

§ b. A solar, differs from a sidereal, year, about 20m 23s.

§ 228. A *sidereal year* is the time from the sun's leaving, until its return to, the same part of the heavens, or to the same fixed star.

§ a. A sidereal, is longer (§ 227. § b.) than a solar, year, on account of the *precession* of the *equinoxes*, which is a motion contrary to that of the sun through the signs.

§ b. While the sun is completing a revolution from left to right through the signs in successive order, they are moving in the contrary direction, or from right to left, and by the time the sun has returned to the first point of **Aries**, for instance, this point will have retrograded a little more than 51"; and, on account of this motion, the sun comes to this point sooner than it would have done, had the first point of **Aries** remained stationary.

§ 229. The *zodiac* is a belt in the heavens that extends 8° on each side of the ecliptic.

§ a. The orbits of all the primary planets are within the zodiac.

§ 230. The *primary planets* are **Mercury**, **Venus**, the **Earth**, **Mars**, **Jupiter**, and **Saturn**.

§ a. There are five other planets, but they cannot be seen with the naked eye. They are called *telescopic planets*.

§ 231. The points in which the orbit of a planet cuts the ecliptic, are called *nodes*.

§ a. That node is called the *ascending node* (Ω), through which

the planet passes, as it crosses the ecliptic, going from the south to the north side of it.

§ *b.* The other point of intersection is called the *descending node* (Ω).

§ 232. The *equator*, or *equinoctial line*, is a great circle, whose plane divides the earth into two equal parts.

§ *a.* These parts are called the northern and southern hemispheres.

§ *b.* The centre of the earth is the centre of the equator, and of all the *great circles used in nautical astronomy*.

§ 233. The *poles* (§ 123.) of the equator, also called the *Poles*, are two points on the earth, that are diametrically opposite to each other; each is 90° from the equator.

§ *a.* The one on the north side of the equator, is the *north pole*; and that on the south side, is the *south pole*.

§ 234. A straight line from one pole to the other, passes through the centre of the earth, and (§ 124.) is called the *axis* of the earth.

§ *a.* Around this axis, the earth performs its diurnal revolutions.

§ 235. From the best measurements, the equatorial appears to be about 26 miles greater than the polar diameter of the earth. And the degrees of latitude increase in length from the equator towards the poles.

§ *a.* The surface of the earth (§ 204.) being flattened in at the poles, and elevated at the equator, its meridional curvature is less near the former than it is near the latter; consequently a degree of latitude near the poles contains more fathoms, feet, etc., than one at or near the equator.

§ 236. Suppose the plane of the equator to be extended to the heavens; it there forms the *celestial equator*, and its poles, are the *poles* of the world.

§ 237. The latitude of places on the earth, is measured from the terrestrial equator; and their longitude is measured on it.

§ *a.* In the heavens, the declination of the bodies are measured from the celestial equator, and their ascension on it.

§ *b.* Declination and ascension are, in the heavens, what latitude and longitude are on the earth.

§ 238. The sun crosses the equator twice in a year.

§ *a.* While the sun is on the north side of the equator, the sun is constantly visible from the north pole, and daylight continues there until after the sun recrosses the equator, when the sun goes below the horizon, and does not rise again, until (§ 226. § *d.*) completing its southern tour, it is approaching the vernal equinox.

§ 239. The year, instead of being divided into seasons at the poles, may, more properly, be divided into day and night; for there is but one day and one night at each pole during the year.

§ *a.* At the north pole, the day commences about the 21st of March, when the sun crosses the equator, and continues until the sun recrosses the equator, which happens about the 23d of September, when night succeeds the day, and day begins at the south pole, and lasts until the sun again returns to the first point of Aries.

§ *b*. Owing to atmospheric refraction, the sun may be seen at either pole for several days previously to its rising above, and after it has gone below, the natural horizon.

§ 240. The morning and evening twilights at either pole, are together about two months and a half long.

§ *a*. When the sun crosses the *crepusculum*, the twilight begins and ends.

§ 241. *Crepusculum* is a small circle parallel to the horizon, and 18° below it.

§ 242. All small circles that are parallel to the horizon, are *almacanters*.

§ *a*. To an observer at the north, or south pole, the horizon and the equator coincide, and the parallels of declination are *almacanters*.

§ *b*. At the north pole, the *crepusculum* coincides with the parallel of the 18th degree of southern declination, which the sun crosses about the 29th of January, (near 51 days before it rises;) and on the 13th of November, (near 50 days after it has gone down).

§ *c*. On account of such long twilights, the winter nights, in high southern or northern latitudes, are rendered less gloomy than they otherwise would be.

§ 243. The earth is divided into five *zones*; two frigid, two temperate, and one torrid.

§ *a*. The torrid zone is the largest; it extends to the parallels of $23^\circ 28'$ north and south latitude; consequently it is $46^\circ 56'$ broad.

§ *b*. The small circles which limit it, pass through the solstitial points, and are called *tropics*, from *trepho*, (Gr.); because, when the sun reaches the parallel of declination for $23^\circ 28'$ (§ 226. § *b*. & § *d*.) it appears to turn its course, and to recede from the pole which it was approaching, and to retrograde towards the direction whence it came.

§ *c*. That parallel which is north of the equator, (§ 226.) is the *tropic* of Cancer.

§ *d*. And that on the south side of the equator, (§ 226. § *c*.), is the *tropic* of Capricorn.

§ *e*. The sun is vertical twice a year, at every place within the tropics.

§ 244. Each of the temperate zones extends over $43^\circ 4'$ of latitude.

§ *a*. That on the north side of the equator, called the north temperate zone, extends from the *tropic* of Cancer to the arctic circle.

§ *b*. And the south temperate zone extends from the *tropic* of Capricorn to the antarctic circle.

§ 245. The *arctic* and *antarctic* are small circles, parallel to the equator, and $23^\circ 28'$ from the poles.

§ *a*. The arctic is about the north, and the antarctic about the south pole.

§ *b*. They are sometimes called the *polar circles*.

§ 246. The *frigid* zones are between the polar circles and the poles.

§ 247. *Latitude* is distance on the earth, measured north or south, from the equator.

§ 248. *Meridians* are great circles, that are secondaries to the equator.

§ a. Therefore (§ 126. § a. & § 127.) they cut it perpendicularly, and intersect each other at the poles.

§ b. The arc of a meridian that is contained between a place and the equator, measures the latitude of that place.

§ c. The meridian of an observer passes through his zenith.

§ 249. *Parallels of latitude* are small circles, parallel to the equator.

§ a. All places upon the same parallel have the same latitude.

§ b. And all places that are on the same meridian, are in the same longitude.

§ 250. *Circles of longitude* are meridians.

§ 251. *Elevation of the pole* is the distance of either pole above the horizon of any observer.

§ a. This distance is measured on the meridian of the observer; it is equal to his latitude.

§ 252. *Longitude* is the distance, expressed in degrees, etc., between two meridians. It is measured on the equator, and east or west from a meridian.

§ a. A meridian from which longitude is measured, is called the *prime meridian*.

§ b. The location of this meridian is optional with topographers. The French reckon the longitude of all other places from the meridian of Paris; the Spaniards from Cadiz. The English use the meridian of the Royal Observatory at Greenwich for their prime meridian: and the Americans generally construct their charts from the meridian of Washington City.

§ c. But as long as most of the charts and the tables of the Nautical Almanac which we use, shall be constructed and calculated to the meridian of the Greenwich observatory, it will be found more expedient to reckon longitude from this, as the prime meridian.

§ 253. It is to be wished that all nations would fix upon one common prime meridian. One might be established from celestial phenomena, by which all that is arbitrary in its locality, might be made to disappear. La Place recommends the adoption of a universal first meridian, and suggests the propriety of selecting for this purpose, that meridian, upon which it was 12 o'clock when the sun entered the point of the vernal equinox in the year (1250), in which the apogee of the earth's orbit coincided with the solstitial point in Cancer. Such a universal meridian would pass about 8 miles west of Cape Mesurada on the Coast of Africa.

§ 254. The longitude of a place is measured on the arc of the equator, which is contained between the meridian of that place, and the prime meridian.

§ a. The angle at either pole, which these two meridians make with each other, is equal to the longitude.

§ b. Consequently the arc of a parallel of latitude (§ 249.), which

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is intercepted between that place and the meridian of any other place, contains, in degrees, the difference of longitude between these two places.

§ c. The difference of latitude between two places, is the arc which is contained on the meridian of either place, between the parallels of latitude of these two places.

§ 255. *Declination* is the distance of a heavenly body from the equatorial plane.

§ a. Declination is north or south, according as the body is north or south of the equator. It is measured in the heavens, as latitude (§ 248. § b.) is on the earth.

§ b. The arc of the circle of declination or of right ascension, that is contained between the equator and the centre of the body, measures its declination.

§ 256. *Circles of right ascension* or of *declination* in the heavens, correspond with meridians of terrestrial longitude.

§ a. They cut the equator at right angles, and intersect each other in the poles of the world.

§ 257. *Parallels of declination* are small circles in the heavens, that are parallel to the equator.

§ a. They correspond with parallels of latitude on the earth.

§ b. The tropics (§ 243. § c. & § d.) are the parallels of the sun's greatest declination.

§ 258. *Polar distance* is the distance of any celestial body from either pole.

§ a. It is the arc of the circle of declination that is contained between the body and either pole.

§ b. The complement of the declination of a heavenly body, expresses its polar distance.

§ 259. The *right ascension* of a body is the arc of the equator, which is between the first point of Aries and the circle of the declination of that body.

§ a. This arc is always counted in the order (§ 224. § a.) of the signs, and its dimensions are expressed in hours, minutes, and seconds.

§ 260. Right ascension in the heavens, is what longitude is on the earth. But the manner of reckoning them is different.

§ a. Longitude is reckoned from the prime meridian as far as 180° both east and west.

§ 261. Right ascension commences to be reckoned from the first point of Aries, and goes entirely around, in the direction in which the sun passes through the signs.

§ 262. The *ascensional difference* of the sun, is the difference between its right and oblique ascension, or between sunrise and 6 o'clock.

§ 263. *Horary angles* are those which meridians, or circles of declination, make with each other at the poles.

§ a. The *6 o'clock hour circle*, is that circle of declination (§ 256. § a.) which cuts the equator and the horizon in the east and west points.

§ *b*. It is secondary to the equator and to the meridian of the observer.

§ *c*. Any circle of declination is an *hour circle*.

§ 264. *Celestial latitude* is distance between the ecliptic and any body in the heavens; it is measured from the ecliptic, and upon a secondary to it.

§ 265. The secondaries of the ecliptic, are circles of celestial longitude.

§ *a*. The arc of the circle of celestial longitude, that lies between the ecliptic, and a body in the heavens, measures in degrees, etc., the latitude of that body.

§ 267. The longitude of heavenly bodies is reckoned on the ecliptic, as right ascension is on the equator (§ 259.).

§ *a*. It commences at the first point of Aries, and is reckoned around in the direction in which the sun passes through the signs.

§ 268. The right ascension and longitude of an object are never the same, except when the body is on the solstitial colure, which cuts both the ecliptic and the equator at right angles, and passes through their poles.

§ 269. The *solstitial colure* is that circle of declination which passes through the solstitial points (§ 226. § *a*. & *c*.).

§ 270. The *equinoctial colure* is the circle of declination, which passes through the equinoctial points (§ 226. § *b*.).

271. The equinoctial and the solstitial points are the four *cardinal* points of the heavens.

§ 272. The four *cardinal* points of the horizon are the east and west, and the north and south points.

§ *a*. The *east* and *west* are the points in which the equator and the horizon intersect each other.

§ *b*. The *north* and *south* are the points in which the meridian of the place cuts the horizon.

§ 273. Every observer has two horizons, one *rational*, the other *sensible*.

§ *a*. The eye is the centre of the latter, and is on the axis of the former.

§ 274. The *sensible horizon* is that circle which terminates the view upon an uninterrupted plane.

§ *a*. It is formed by the apparent meeting of the plane upon which we stand, with the concave expanse above.

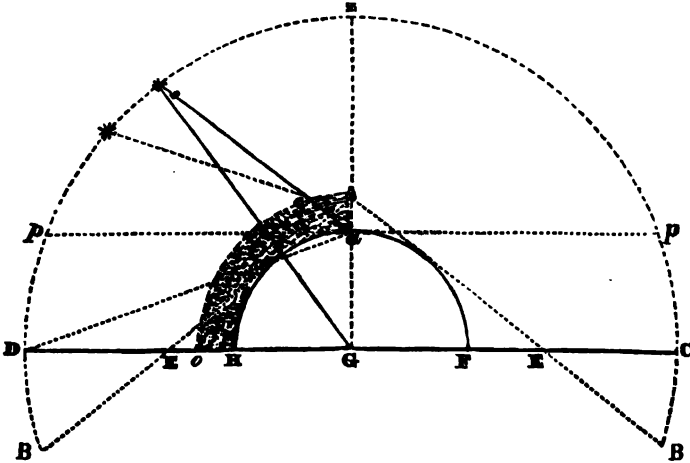
§ *b*. It is a small circle, and is parallel to the rational horizon.

§ *c*. The circle which terminates our view at sea, is the *sensible horizon*.

§ 275. The *rational horizon* is a great circle; its plane passes through the centre of the earth, and its axis through the eye of the observer. Suppose *H a F* to be half of the earth, *D Z C* the concave blue which bounds the vision, and *D H C* the plane of the rational horizon. If an observer were placed at the centre (*G*) of the earth, the angle *D G Z* would show the altitude of an object in the zenith, at *Z*, from the rational horizon. If the observer were placed at the circumference (at *a*) of the earth, *p a p* would be the plane

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of his visible horizon, and the angle $p a Z$ ($= D G Z \text{ } \S 30.$) would show the altitude of a body at Z , from the sensible horizon. But if the observer were placed at A above the surface of the earth, the angle $B A Z$ ($> D G Z$) would show the altitude of Z from his sensible horizon.



§ a. When the eye is elevated above the level of the sea, (as at A ,) the line of vision AB to a point B in the sensible horizon, cuts the plane CD of the rational horizon at an angle, DEB , which angle is called the *dip*. Consequently, when the eye is above the surface of the plane on which we stand, the sensible horizon is *below* the rational horizon.

§ b. The poles of the rational horizon are the zenith and nadir.

§ 276. The *zenith* is the point in the heavens which is directly over head.

§ a. Being a pole of the horizon, the zenith is 90° from the horizon.

§ 277. The *nadir* is the other pole of the horizon; it is in the lower part of the heavens, directly under our feet, and diametrically opposite to the zenith.

§ 278. *Azimuth* circles are secondaries (§ 127.) to the horizon; cutting it perpendicularly, they intersect each other in the zenith and nadir.

§ a. They are also called *vertical* circles.

§ 279. The azimuth circle which cuts the horizon in the east and west points, is called the *prime vertical*.

§ a. The prime vertical of every observer, is secondary to his meridian.

§ 280. The altitude, and zenith distance of a heavenly body, are measured on its azimuth circle.

§ 281. The *zenith distance* of a heavenly body is its distance from the zenith of the observer; thus, Zs (§ 275.) is the zenith distance of the star at s .

§ *a*. It is measured on the arc of the azimuth circle, which lies between the centre of that body and the zenith.

§ *b*. The *zenith distance* is *north* when the body is south of the observer.

§ *c*. And south, when the body is north of the observer.

§ 282. The *altitude* of a heavenly body, is its distance above the horizon.

§ *a*. The arc of the azimuth circle which is contained between the centre of a body and the horizon, measures the altitude of that body; thus, Ds (§ 275.) is the altitude of the star at s .

§ *b*. The complement of the altitude of a body, gives its zenith distance.

§ 283. The altitude which is taken of the sun or moon, with a quadrant or sextant, is the observed *altitude* of one of the edges, called a *limb*.

§ *a*. The apparent altitude of the *centre* is found by applying the corrections, (which are laid down in the Nautical Almanac,) for the semidiameter of the body, to the apparent altitude of its limb.

§ *b*. And the *true*, is obtained from the *apparent* altitude of the centre, by applying to the latter, corrections for the parallax and refraction, which are also known by previous calculations.

§ *c*. The apparent and the true altitude of a body, are always measured on the same azimuth circle.

§ 284. The rays of light coming from the heavenly bodies strike the atmosphere obliquely, and entering from a rarer into a denser medium, are refracted, or *bent downwards*; this causes the body whence they emanate to appear higher up in its azimuth circle than it really is. Suppose $*e$ (§ 275.) be a ray of light from $*$, and Ao to represent the atmosphere; when this ray strikes the atmosphere, it will be refracted so as to reach the eye of the observer at a , in the direction ae , which makes $*$ appear at s , above its true place.

§ *a*. Hence the apparent altitude of the sun or a star is always greater than the true altitude, unless the body be in the zenith.

§ 285. Parallax has a contrary effect; it acts in a direction opposite to that of refraction, and causes a body to appear *lower* down in its azimuth circle than it really is.

§ *a*. But the effects of parallax and refraction, though acting in contrary and opposite directions, seldom counterbalance each other, so as to make an object appear in its true place.

§ 286. The parallax of the moon is always greater than the refraction; and the moon always appears below its true place.

§ *a*. Hence the apparent, is always *less* than the true altitude of the moon.

§ 287. The *horizontal parallax* of a body, is the difference between the *true* and *apparent* place of that body, (supposing there be no refraction), when it is in the horizon.

§ *a*. The horizontal parallax is equal to the angle at the body,

which is subtended by the distance of the observer, from the centre of the earth.

§ *b*. The angle which this distance, or semidiameter, subtends, is greatest when the body is in the plane of the rational horizon; thus, the parallax of a body at *D*, (§ 275.) is the angle $G D a$; and the parallax of the same body, when at *s*, is $G s a$.

§ *c*. As the object rises above the horizon, the angle which this semidiameter subtends, is called *parallax in altitude*; it gradually decreases until the object reaches the zenith, when it vanishes.

§ *d*. The nearer the object is to the earth, the greater will this angle be at the centre. Hence the moon's parallax is greater than the sun's, and this greater than that of the fixed stars.

§ 288. The parallax of a body decreases from the horizon to the zenith, in the proportion of sine of the zenith distance (§ 281.) to radius.

§ 289. Owing to the effects of parallax and refraction upon the heavenly bodies (§ 285. § *a*.), they are never seen in their *true* places, except when in the zenith.

§ *a*. The places in which the heavenly bodies are seen, are called their *apparent places*.

§ 290. The *true place* of a heavenly body, is that place in which it would appear, if seen from the centre of the earth.

§ 291. The *azimuth* of a celestial body is the angle which is contained at the zenith, between the meridian of the place, and an arc of the azimuth circle, which passes through the centre of that body.

§ *a*. In north latitudes, the angle on the *north* side, and in south latitudes, the angle on the *south* side, of the arc of this azimuth circle, is called the azimuth.

§ *b*. Before a body crosses the meridian of the observer, its azimuth is east, and west afterwards.

§ *c*. Thus, in north latitude, an azimuth is said to be *north*, so many degrees east, if the body be east of the meridian; or *N*, so many degrees west, if it have passed the meridian.

§ *d*. And in south latitude, the azimuth is reckoned in the same manner from the south point, to the east or west.

§ 292. The *amplitude* of a celestial object, is the arc of the horizon that lies between the east or west point, and the centre of that object when it is rising or setting.

VARIATION OF THE COMPASS.

§ 293. The variation of the needle, is determined by means of azimuths, or amplitudes.

§ 294. The needle does not always point to the north and south poles. At some places it points to the east, and at others to the west, of the true north and south points.

§ *a*. Even at the same place, the polarity of the needle does not remain constant.

§ *b*. As to the direction in which the needle points, it is subject to certain periodical changes, which do not follow any known laws.

At some places, after having pointed, for several years, to the eastward of the true north, it has gradually pointed nearer to the north point, until its position lay due north and south; then crossing the direction of the meridian, the needle has continued to turn more and more to the westward of the true north, until it has attained the maximum of its deviation for that place, when, after having remained stationary for a time, it commenced its return towards its former position.

§ 295. *Variation* of the compass is the deviation of the needle, from pointing to the north and south poles.

§ 296. The points to which the needle tends, are called the *magnetic* north and south points.

§ 297. When the northern point of the needle, or the N point on the compass card, points to the eastward, or to the *right*, of the true north, the variation is *easterly*.

§ *a*. And *westerly* when the same point points to the *left*, or to the westward of the true north.

§ 298. The true direction of the magnetic north point, is found by applying the variation, when it is easterly, to the *right* of the true north; and to the *left* of the *true* north, when the variation is westerly.

§ *a*. Thus, when the variation is one point easterly, the north point of the needle, or the N point on the compass card, points N. by E. And it points N.N. W. when the variation is two points westerly.

§ *b*. Wherefore, knowing the magnetic bearing of any object, its true bearing may be determined, by applying the variation, when easterly, to the *right* of its compass bearing; and to the *left*, when the variation is westerly.

§ *c*. The true bearing of an object, that bears east per compass, is E. by S. if the variation be one point easterly; but E. by N. if the variation be one point westerly.

§ 299. The cause of variation, as well as of the attraction of the needle, towards the poles, is unknown.

§ 300. The needle is subject to the influence of another power equally mysterious in its nature; it is called *local attraction*.

§ *a*. This attraction operates on ship-board, and with different effects in different latitudes, as well as in the different directions in which the vessel may be heading,

§ *b*. Its effects upon the needle become obvious by taking the bearing of a fixed point on shore, then swinging the ship entirely around, and observing at several different points of her heading, the bearing of said fixed point.

§ *c*. The effect of local attraction upon the compass, is not often taken into consideration by navigators, although on board of vessels in some latitudes, (as in the English channel), it is said to cause the needle to deviate several degrees. The loss of fleets has been ascribed to the neglect of this attraction, on the part of navigators.

§ *d*. In conducting surveys particular attention should be paid to the effect of local attraction upon the needle.

§ 301. A *magnetic* meridian is a great circle that passes through the magnetic north and south points, and through the zenith of the observer.

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§ *a*. The needle always lies in the direction of this meridian.

§ *b*. Magnetic meridians cross each other in the magnetic poles.

§ 302. The *magnetic* equator is a secondary to all magnetic meridians.

§ 303. The *magnetic* prime vertical is a secondary to the magnetic meridian of the observer.

§ *a*. It passes through the zenith and the magnetic east and west points of the horizon.

§ 304. The *magnetic* azimuth of a celestial body, is an angle at the zenith, that is contained between the magnetic meridian of the observer and the zenith distance of the object, when its bearing is taken.

§ *a*. The magnetic azimuth should always be reckoned from the nearest pole, around towards the east, when the object is on the east side of the meridian of the observer; and to the west, after the object has crossed the meridian.

§ *b*. The advantage of reckoning the magnetic azimuth in this way, consists in having the true and magnetic azimuth always of the same name; i. e. either both east, or both west.

§ 305. The *magnetic* amplitude of a celestial body, is that arc of the horizon, which lies between the centre of the body, when the body is in the horizon, and the magnetic east or west point, according as the body is rising or setting.

§ 306. Upon the magnetic equator, the needle assumes a horizontal position.

§ *a*. To the north or south of this equator, it points *downwards*, inclining towards the nearest magnetic pole.

§ 307. The angle of this inclination of the needle, below the plane of the horizon, is called the *dip* of the needle.

§ *a*. The maximum of the dip is at the magnetic poles, and the minimum at the equator.

§ *b*. The ratio of the increment in dip, from the equator, towards the poles, has never been satisfactorily established.

§ 308. The variation of the compass is found by ascertaining the true and magnetic azimuths, or amplitudes, of any celestial object at the same moment.

§ *a*. The difference between them is the variation.

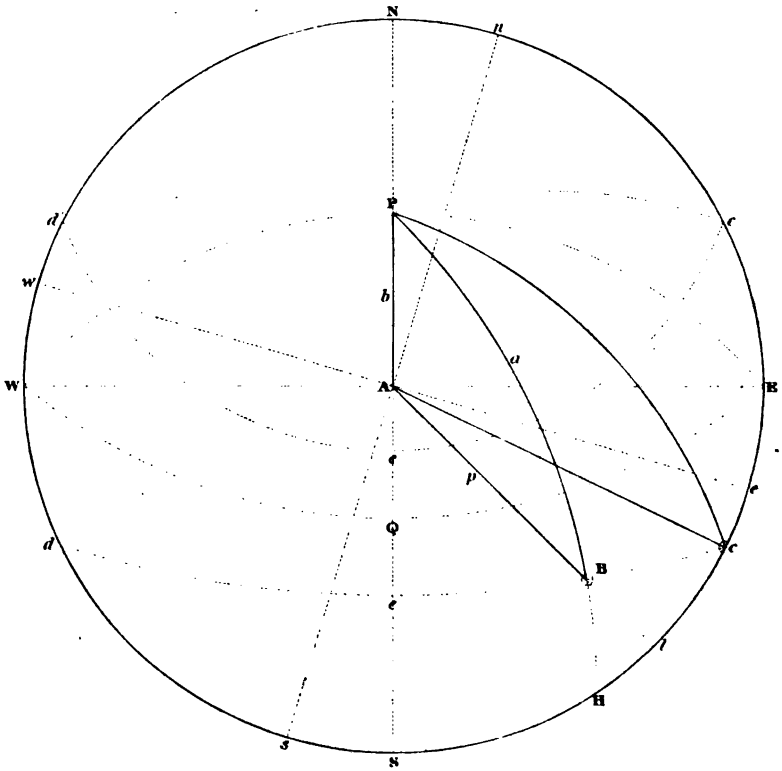
§ 309. The magnetic azimuth, or amplitude of a celestial object, is found by taking its bearing with an azimuth compass.

§ 310. The true azimuth or amplitude of a celestial object is determined by trigonometrical calculations.

§ *a*. The usual data for this operation, are the co-latitude of the observer, and the zenith, and polar, distances of the object.

§ 311. In North Latitude; the variation is easterly, if the magnetic, be less than the true, azimuth, when the object is on the east side of the meridian; or the variation is easterly, if the magnetic be the greater azimuth, when the object is west of the meridian.

§ *a*. And in South Latitude; the variation is easterly, when the magnetic is the greater azimuth in the former, and the less in the latter case.



§ 312. In each case, *mutatis mutandis*, the variation is westerly.

§ 313. *Stereographic projection* is the most useful, and being the most natural, is the most simple mode of representing a sphere, or circles of a sphere, upon a plane.

§ 314. In stereographic projection the eye is supposed to be at some point on the surface of the sphere, and to see one half of the sphere.

§ a. The circle which terminates the vision is called, in projection, the *primitive circle*.

§ b. The eye is the centre of this circle, and is the *projecting point*.

§ 315. The diagrams for the purposes of nautical astronomy, in this treatise, are projected upon the plane of the horizon.

§ 317. This Fig. is a stereographic projection upon the } Plate 2.
plane of the horizon, in lat. 40° north.

§ a. A, the projecting point, represents the centre of the horizon W N E S, as well as the zenith and the eye of the observer; P, the pole of the observer; P N (§ 251.) the elevation of the pole; W Q E (§ 232.) the equator; A Q (§ 248. § b.) the latitude of the observer; and A P the complement of his latitude; W A E (§ 279.) his prime vertical; N P S (§ 248. § c.) his meridian; A B I (§ 278.) the azimuth circle of the body whose altitude is taken; B I and A B (§ 280.) its altitude and zenith distance; *d e c* (§ 257.) the parallel of its declination; P B (§ 258. § a.) its polar distance, and P B H (§ 256. § a.) is an arc of its circle of declination; A P B (§ 263.) is the horary angle at which the body is; B A P (§ 291.) is its azimuth; N, E, S, and W, (§ 272.) are the cardinal points of the horizon; and W P E (§ 263. § a.) is the six o'clock hour circle.

§ b. It is easily conceived how it is, that, of all circles which cut the primitive circle of a projection, only that part of their circumference which is above the primitive, can be seen from the projecting point; and that 180° of every arc of these circles, that are great circles, is above (§ 125. § a.) the horizon or plane of projection.

§ c. And consequently that all of these arcs will appear in the projection to be more straightened out, or of less curvature than the primitive circle; and this curvature will be in proportion inverse to the obliquity with which their planes cut the plane of the primitive.

§ d. The less obliquely these planes cut the plane of the horizon, the more obliquely the observer at A looks upon them, and consequently the less their arcs appear to be curved, until, looking upon the edge of the planes of those which pass through his zenith, they appear as straight lines.

§ 318. In these projections, every great circle (N P S, W A E,) which passes through the zenith, is represented as a straight line.

§ a. And the length of every line (A N, A I, etc.) included between the projecting point (A) and the circumference of the primitive, measures 90° , and is considered as the quadrant of a circle.

§ 319. All of those circles which cut the plane of the primitive obliquely, and whose arcs (W Q E, P B, etc.) appear in the pro-

jection, to be of less curvature than the primitive, are called *oblique circles*.

Plate 2. { § 320. And those circles, whose arcs (N P S, W A E,) pass through the zenith (§ 318.) are called *right circles*.

§ a. With the horizon as the primitive circle; the meridian, (§ 248. § c.), prime vertical, (§ 279. § a.), and azimuth circles (§ 278.), pass through the zenith, and appear upon the plane of projection (§ 318.) as right circles.

§ 321. In lat. 40 N., the sun's declination being 20° S.; its magnetic azimuth was N. 119° 25' E. in the morning, when its true altitude was 16° 48' 25''; required the sun's true azimuth, and the variation of the compass.

§ 322. W N E S, (§ 316. § a.) represents the horizon of the observer; A, the centre of it, his zenith, and the place at which he stood to take the observation; *n A s*, the magnetic (§ 301.) meridian; and (§ 308. § a.) N A *n* is the variation.

§ a. The co-lat. (A P), the zenith, and the polar distance, (A B, P B) (§ 317. § a.), are the sides of the triangle A P B, and (§ 321.) are the given parts; and the azimuth P A B, is the required part; the value of it is determined according to Case V, (§ 201. § d.)

§ b. In the formulæ for calculation,

P D, stands for polar distance.

Z D, " zenith distance.

Co-lat. " complement of the latitude of the place of observation.

§ c. The complements of what is given (§ 321.) constitute the data of the proposed triangle.

§ d. $b = 50^\circ$ - = Co-lat.

$p = 73^\circ 11' 35'' = Z D$

$a = 110^\circ$ - = P D

To find the azimuth P A B, (§ 201. § f.)

§ e. a , or P D = 110°

p , or Z D = $73^\circ 11' 35''$ co-sec. = 0.018959

b , or Co-lat. = 50° - co-sec. = 0.115746

Sum 2) $233^\circ 11' 35''$

$\frac{1}{2}$ Sum = $116^\circ 35' 47''$ sin. = 9.951426

$\frac{1}{2}$ Sum \propto P D = $6^\circ 35' 47''$ sin. = 9.060224

2) 19.146355

Cos. $\frac{1}{2}$ P A B = $9.573177 = 68^\circ 1' 18''$

2

P A B (the true azimuth, § 291. § c.) = N $136^\circ 2' 32''$ E

B A *n* (the magnetic do. (§ 304. § a.)) = N $119^\circ 25'$ E

N A *n* = Variation (§ 311.) = $16^\circ 37' 32''$ E.

§f. The difference between the true and magnetic azimuths (§ 308. § a.) (N A B—n A B=N A n) is the variation. } Plate 2.

§g. The true, being greater than the magnetic azimuth, the variation (§ 311.) is easterly.

§ 323. Bearing in mind, that the co-sec. sine, etc., of an arc (§ 99.), is the sec., cos., etc., of the complement of that arc, the process by which the subjoined formula is deduced from (§ 322. § e.) the one above, becomes manifest.

§ a. Calculation by this formula operates more directly upon the data, and is, perhaps, preferable in practice on account of its greater readiness.

§ b. P.D.=110°

Alt. = 16° 48' 25'' sec. = 0.018959

Lat. = 40° sec. = 0.115746

2)166° 48' 25''

$\frac{1}{2}$ Sum = 83° 24' 12'' cos. = 9.060242

($\frac{1}{2}$ S. ∞ P.D.) = 26° 35' 48'' cos. = 9.951425

2)19.146372

Cos. $\frac{1}{2}$ tr. azim. = 9.573186 = 68° 1' 15''

2

Tr. azimuth = N 136° 2' 30'' E.

§ c. This difference of 2'' in the result of the two methods, arises from the fraction of a second in $\frac{1}{2}$ sum; which, in either case, is not taken into computation.

§ d. Whence (§ 323.) the rule for calculating an azimuth. Take the difference between the P.D., and $\frac{1}{2}$ sum of the lat. alt. and P.D.; then the product of the cos. of this $\frac{1}{2}$ sum and of this difference, multiplied by the product of the sec. of the lat. and of the alt., is double the cos. of $\frac{1}{2}$ of the true azimuth.

AMPLITUDES.

§ 324. When the magnetic, and true amplitudes of a body, are both north, or both south, the difference between them is the variation.

§ a. But when one of the amplitudes is north and the other south, they are of different names; and their sum is the variation.

§ 325. If the amplitudes be of the same name (§ 324.), and the true be the less northern, or the greater southern amplitude, the variation is easterly when the object is rising; and,

§ a. The variation is also easterly, when the object is setting, and the true is north and the greater, or south and the less, of the two amplitudes.

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§ 326. If "*magnetic*" be read for "*true*" in the conditions above, the variation becomes westerly.

§ 327. If the amplitudes be of different names (§ 324. § a.), and the *true* be the northern amplitude, when the object is rising, or the southern amplitude when the object is setting, the variation is westerly.

§ a. The converse of these conditions makes the variation easterly.

§ 328. The true amplitude and declination of a body, are always of the same name.

§ a. Therefore it is known by inspecting the declination, whether the true amplitude be north or south.

§ 329. Every object in the heavens, always rises and sets to the north, or to the south of the east and west points, according as its declination is north or south;

§ a. The equator (§ 272. § a.) cuts the horizon in the east and west points; and a parallel of north or south declination, being (§ 257.) parallel to the equator, must therefore cut the horizon, (if at all), to the north or south of the east or west points.

§ 330. A body (say the sun), rises and sets in the points, in which the parallel of its declination cuts the horizon.

Plate 2. { § a. Thus the sun's declination being 20° S., it rises and sets in the points (*c* & *d*) in which the parallel (*d e c*) of that declination cuts the horizon.

§ 331. To an observer who is on the equator, the sun's declination at the time of its rising or setting, is its amplitude; for,

§ a. The equator is then the prime vertical, and that arc of the horizon which (§ 292.) measures the amplitude, coincides with the arc of the circle of right ascension, which (§ 255. § b.) measures the declination.

§ 332. The sun rises in the east, and sets in the west, point, only twice in the year.

§ a. This happens at the moments in which the sun enters the first point of Aries, and the first point of Libra, for (§ 226. and § 226. § c.) the sun is then crossing the equator.

§ 333. To an observer at either pole, the horizon and equator coincide, and the sun does not set, while it is on that side of the equator, which is next to the observer. And,

§ 334. If the observer approach any point of the equator, that point will rise *above*, and the one diametrically opposite, will sink *below*, the horizon as many degrees as the observer advances from the pole. And,

§ a. The observer will not see the sun go below the horizon, until his distance from the pole is greater than the sun's declination.

§ 335. When the latitude and the sun's declination are of the same name, the sun is not seen to set as long as its declination is greater than the co-latitude.

§ 336. To find the sun's true amplitude, and thence the variation.

§ 337. At sun-rise in lat. 40° N., the sun's declination being 20° S., its magnetic amplitude was E. $9^{\circ} 53' 32''$ South; required the true amplitude, and the variation.

§ 338. The place of the sun at the time of its rising (§ 330. § a.) is at the point (*c*) in which the parallel of its declination intersects the horizon; *w A e* (§ 303.) is the magnetic prime vertical; } Plate 2.
the arc *E c* (§ 292.) is the true, and *e c* (§ 305.) the mag- }
netic, amplitude of the sun; and *P A c* is the triangle of the proposed problem, of which the sides are given, and *P A c* is the part required. The triangle (§ 142.) is quadrantal, of which the quadrantal side is *A c*, the zenith distance.

§ a. Now (§ 150. § a.), calling the quadrantal side (*A c*) radius, and the legs (*P A*, *P c*) angles, and the angle *P A c* a leg, the problem is an example under Case IV. (§ 173. § b.).

$$\text{§ b. } P A \text{ or co-lat.} = 50^\circ \text{ cosec.} = 0.115746$$

$$P c \text{ or Z. D.} = 110^\circ \text{ cos.} = 9.534052$$

$$\text{Cos. } P A c = 9.649798 = 116^\circ 31' 4''$$

§ c. Now (§ 133. § a.) the arc *N E c* is the measure of the angle *P A c*; and the arc *E c* (§ 52. § a.) is the complement of *N E c*, and (§ 292.) the sun's true amplitude.

$$\text{§ d. } E c, \text{ the sun's true amplitude} = E 26^\circ 31' 4'' S$$

$$e c, \text{ the sun's magnetic do.} = E 9^\circ 53' 32'' S$$

$$\text{The variation} = 16^\circ 37' 32'' E \text{ (§ 324.)}$$

§ e. The amplitudes are both south, and the true is the greater; wherefore (§ 325.) the variation is easterly.

§ 339. By recurring to § 323. it is evident that the process of calculation (§ 338. § b.) for determining the amplitude, may be simplified, and rendered more convenient in practice, by a similar artifice.

$$\text{§ a. Lat.} = 40^\circ \text{ sec.} = 0.115746$$

$$\text{Dec.} = 20^\circ \text{ sin.} = 9.534052$$

$$\text{Sin. ampl.} = 9.649798 = 26^\circ 31' 4''$$

$$\text{Magnetic ampl.} = 9^\circ 53' 32''$$

$$\text{Variation} = 16^\circ 37' 32'' E$$

§ b. Whence the general rule in practice, for finding an amplitude.

The sine of the amplitude is the *product* of sec. of the lat. and sine of the dec. See Table VII.

SUNRISE.

§ 340. When the latitude of an observer, and the sun's declination, are either both north, or both south, the sun always rises before, and sets after, six o'clock.

§ 341. When the latitude and declination are of different names, the sun rises after, and sets before, six o'clock.

§ 342. When the sun rises in the east, or sets in the west, point of the horizon, the sun is (§ 272. § a.) on the equator, and (§ 263. Plate 2. § a.) in its six o'clock hour circle (W P E); and therefore rises and sets at six o'clock.

§ 343. The time of sunrise subtracted from 12 o'clock, gives the time of sunset, when the points in which the sun rises and sets, are equidistant from the point at which it crossed the meridian.

§ a. This happens when the declination at sunrise, and at sunset, is the same.

§ 344. When the sun (§ 342.) rises and sets at six o'clock, it is also in the first point of Aries, or of Libra;

§ a. As the sun's declination increases, its right ascension (§ 259.) becomes greater, and the first point of Aries farther from the east point of the horizon, when the sun is rising; and,

§ b. The interval between sunrise and 6 o'clock, also increases.

TIME.

§ 345. The time between sunrise and 12 o'clock, in any latitude, may be determined by knowing the sun's declination.

§ a. This operation consists in finding the value of the horary angle A P c, which the circle (P c) of declination, in which the sun rises, makes (§ 263.) with the meridian (N P S) of the place.

§ 346. The value of this angle, (A P c), like that of every other, is expressed in degrees; but may be converted into time, in the proportion of 360° to 24h, which (§ 218. § a.) is the mean time in which the earth performs a diurnal revolution.

§ a. $\frac{360^\circ}{24} = 15^\circ$; therefore the sun describes an horary angle of 15° in 1h; $\frac{1h}{15} = \frac{60m}{15} = 4m$; wherefore the sun describes an horary angle of 1° in 4m, of $15'$ in 1m, and of $15''$ in 1s.

§ b. Whence the rule for converting longitude, degrees, etc., into time, and the reverse.

§ 347. Divide the degrees by 15, for hours, the product of 4 and the remainder, is minutes, (m); the quotient of the minutes (') by 15 is also minutes, (m); and the product of 4 and the remainder to this quotient, is seconds (s); also the quotient of the seconds (") by 15 is seconds (s) of time.

§ 348. The product of hours by 15, and the quotient of the minutes (m) by 4, are degrees; the product of the remainder of the minutes (m) by 15, and the quotient of the seconds (s) by 4, are minutes ('); and the product of the remaining seconds (s) by 15, is seconds (").

§ a. The two first and two last columns of Tables II., show (with the hours at the bottom or top,) the value in time of the degrees and minutes which stand nearest to them.

§ b. And these columns may be used for finding the logarithmic value of hours, minutes, and seconds, as well as for converting de-

degrees, etc., into hours, etc., and vice versa. Therefore in the solution of problems, in which a given or required part consists of hours, etc., these need not be commuted in the process of solution, into degrees, etc.; but may be operated with in calculations, under the denomination of *time*, and thus save the trouble of substituting their value in degrees, etc.

§ c. Substituting hours, etc., for degrees, etc., the logarithmic value of a horary angle may be taken from Tables II., according to the directions given under § 102. for degrees, etc. Thus, to take from the tables the log. of $4h, 20m, 40s$; $4h$ is found at the right hand *bottom* corner of the tables; $20m$ is found in the right hand (*m*) column; and above $20m, 40s$ is found in the (*s*) column on the same side; opposite to $40s$, and in the column which has the required precept at the *bottom*, is the required log.; thus, log. sine $4h 20m 40s = 9.957863$.

§ d. The time corresponding to any log. is taken from the tables according to the directions under § 103. given for taking out the degrees, etc., for a log. sine, etc. Thus, the value in time of log. sin. $9.618004 = 1h 38m 4s$. The log. 9.618004 is found in the column marked (sin.) at the *top*. In the left hand column (*s*) of the page, and opposite to 9.618004 , is $4s$; above $4s$ in the (*m*) column is $38m$, and at the top of the page on the same side is $1h$.

§ e. The small columns marked (diff.) show the difference which $1s.$ or $15''$ make in the log. sine, etc. of an arc or angle.

§ f. To convert $33^\circ 10'$ into hours, etc.; in juxtaposition with 33° is $2h$; and in the left hand columns, $10'$ is opposite to $40s$; and above $40s$, is $12m$; then $33^\circ 10' = 2h 12m 40s$.

§ g. To convert $5h 20m 28s$ into degrees, etc.; $5h$ is found at the bottom, and $20m 28s$ in the right hand columns. In juxtaposition with $5h$ is 80° , and above $20m$, but opposite to $28s$, stands $7'$ in the (*'*) column; then $5h 20m 28s = 80^\circ 7'$.

§ 349. To find the time of sunrise in lat. $40^\circ N.$, the declination being 20° south.

§ a. The triangle of the problem proposed, is the quadrantal triangle $A P c$ with the same data, and a similar } Plate 2.
process, which were used (§ 338. § b.) for finding the amplitude;

$$\S b. P c, \text{ or } P. D. = 110^\circ \cot. = 9.561066$$

$$P A, \text{ or } \text{Co-lat.} = 50^\circ \cot. = 9.923813$$

$$\text{Cos. } A P c \text{ (§ 348. § d.)} = 9.484879 = 4h 48m 52s.$$

§ c. $4h 48m 52s \propto 12h$ (§ 341.) $= 7h 11m 8s$, the apparent time of day at sunrise.

§ d. If the declination were $20^\circ N.$, $4h 48m 52s$ (§ 340.) would be the apparent time of day at sunrise, and $7h 11m 8s$ at sunset,

§ e. The angle $c P E$, (§ 263. § b.) is the complement of the horary angle $A P c$.

§ f. And being the difference between sunrise and 6 o'clock, (§ 262.) it is the ascensional difference.

§ 350. To find the ascensional difference, we have only to take

Plate 2. $\left\{ \begin{array}{l} \text{the sine, where cos. was taken above, in the operation} \\ (\S 349. \S b.) \text{ for finding the time between sunrise and noon.} \end{array} \right.$

§ a. P. Dist. = 110° co-tang. = 9.561066
 Co-lat. = 50° co-tang. = 9.923813

$$\text{Sin. } c P E = 9.484879 = 1h 11m 8s.$$

§ b. 1h 11m 8s (§ 349. § c.) is the complement of 4h 48m 52s, and (§ 349. § f.) is the ascensional difference.

§ 351. By using the trigonometric functions of the complements, the calculation (§ 350. § a.) is rendered more convenient for practice.

§ a. Dec. 20° tang. = 9.561066
 Lat. 40° tang. = 9.923813

$$\text{Sin. } c P E = 9.484879 = 1h 11m 8s.$$

Whence the rule for finding ascensional diff.

§ b. The *product* of the tang. of the lat. and dec., is the sine of the ascensional difference.

§ 352. When the latitude and declination are of the *same* name, the ascensional difference *subtracted* from 6 o'clock, gives the apparent time of day at sunrise; and,

§ 353. *Added* to 6 o'clock, when they are of *different* names, it gives the apparent time of sunrise.

§ a. Hence Table VIII. also shows the apparent time at *sunrise*, when the lat. and dec. are of the *same* name; and the apparent time of *sunset* when the lat. and dec. are of *different* names; for (§ 343.) the time at sunrise subtracted from 12h shows nearly the time at sunset. In the Table, the time from sunrise to 12 o'clock is supposed to be always equal to the time from noon till sunset.

§ 354. The length of the days and nights may be determined by means of the problem (§ 351.); for doubling the time from sunrise till noon, gives the time that the sun remains above the horizon; and,

§ a. Subtracting this time from 24, gives the length of the night, or the time that the sun is below the horizon.

THE PLANETS, MOON, ETC.

§ 355. A satellite is a body that revolves around a planet, as the centre of one of its motions, and also revolves with that planet around the sun.

§ a. The moon is the earth's satellite.

§ 356. Mercury and Venus, (§ 230.) are called *inferior* planets, because their orbits are between the earth's and the sun.

§ 357. Mars, Jupiter, Saturn, Herschel, etc., (§ 230. § a.) are *superior* planets.

§ a. Their orbits are further than the earth's is, from the sun.

§ 358. Jupiter has four satellites, which, revolving with different radii around its centre, accompany it in its revolutions around the sun.

§ a. As they revolve in their orbits from west to east, they pass behind Jupiter; and as they pass in front of it, they cross its disc. From the frequency of these passages, (called eclipses,) and the celerity of the motion of the satellites, their eclipses with Jupiter furnish excellent opportunities for ascertaining longitude, when the observer is on shore. The satellites cannot be seen with the naked eye, and are of no use for ascertaining longitude at sea, because telescopes for observing their immersions and emersions, cannot be used on ship-board on account of the motion of the vessel.

§ b. When Jupiter is nearly in conjunction with the sun, the satellites cannot be seen at all.

§ 359. The moon moves from west to east in its orbit, around the earth.

§ a. The average, or mean time in which the moon performs one revolution in its orbit, is $27d\ 7h\ 43m\ 5s$; this is called a *periodical month*.

§ b. The moon performs, in nearly the same time, one revolution on its axis, by which means the same side of the moon is always presented towards the earth.

§ 360. At the same time every day, the moon is seen about $13^{\circ}\ 10'\ 30''$ further to the east than it was the day preceding.

§ a. This gives the moon an hourly motion with regard to the sun, or fixed stars, of about $32'\ 56''$; and makes the lunar, about $49m$ longer than the solar day.

§ 361. When the moon presents a round, illuminated disc towards the earth, the latter is between the sun and the moon.

§ a. The moon is then about the point in its orbit at which it attains its greatest distance from the sun; and is said to be in *opposition* with the sun.

§ 362. At new moon, the moon is nearest to the sun, being between it and the earth.

§ a. The moon is then in *conjunction* with the sun.

§ b. The interval between two consecutive new or full moons is about $29d\ 12\frac{1}{2}h$.

§ c. This interval of time is called a *synodical month*, to distinguish it from a *periodical month* (§ 359. § a.).

§ d. The difference between the *periodical* and *synodical* months is caused by the motion of the earth in its orbit around the sun; for by the time the moon returns in its orbit to the same place in the heavens, and is again in the position with regard to the fixed stars, which it had occupied $27d\ 7h\ 43m\ 5s$ (§ 359. § a.) before, the earth will have advanced in its own orbit, and the moon will have to continue on in its orbit, about $2d$ and $5h$, before it overtakes the earth, and occupies the position, with regard to the earth and the sun, and presents the same appearance, which it did when the two months commenced together.

§ 363. The light of the moon is reflected from the sun.

§ *a*. And the different appearances of the moon's figure, called *phases*, are caused by the enlightened part of the moon being turned more or less towards the earth.

§ 364. When the moon, passing between the earth and the sun, crosses the straight line which joins their centres, the whole of its unenlightened side is turned towards the earth; then it eclipses the sun, and is seen, like an opaque circular plane, passing over the disc of the sun.

§ 365. If the plane of the moon's orbit coincided with the plane of the ecliptic, the sun would be eclipsed at every new moon.

§ *a*. But as these planes are inclined at an angle of several degrees towards each other, the new moon passes sometimes below, and sometimes above, the line of vision from the earth to the sun.

§ 366. At full moon, when the earth intercepts the line of vision from the sun to the moon, the latter passes into the shadow of the earth caused by the sun, and is eclipsed.

§ *a*. The moon is not eclipsed at every opposition, on account (§ 365. § *a*.) of the inclination of the plane of its orbit to that of the ecliptic.

§ 367. *Syzygies* are the points in which the moon is, (§ 361. § *a*. & § 362. § *a*.), at opposition and conjunction. Consequently, the moon is in syzygy at every new or full moon.

§ 368. An eclipse of the sun or moon takes place only when the moon is in syzygy, and at, or near, one of its nodes (§ 231.).

§ 369. When the moon is half way between the syzygies, it appears as a semicircular plane, with the round part turned towards the sun.

§ *a*. Only half of the enlightened surface of the moon being seen from the earth, produces the appearance of a *half moon*.

§ *b*. In this position, the moon's angular distance from the sun is about 90°, and the moon is said to be in quadrature.

§ 370. A quadrature is marked (\square), opposition (δ), and conjunction (δ).

§ *a*. There are two quadratures; one between new and full moon, the other between full and new moon.

§ 371. *Disc* is the face of the sun, of a planet, or of a satellite.

§ 372. *Digit* is the twelfth part of the breadth of a disc.

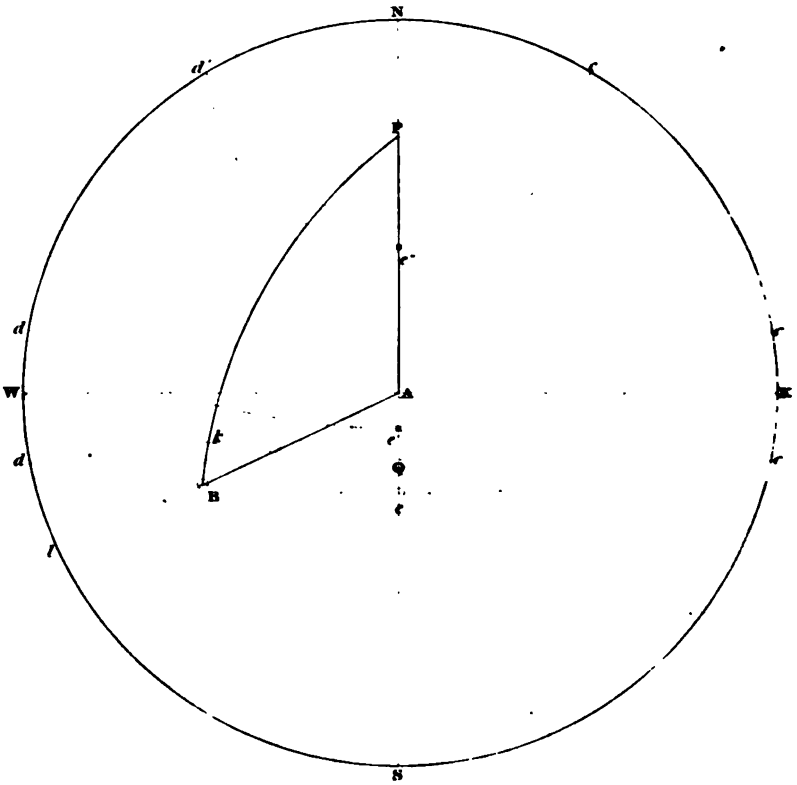
§ 373. *Apogee* is that point in the orbit of a body which is furthest from the earth.

§ 374. *Perigee* is that point in which, when a body is, it is nearest to the earth.

§ 375. *Aphelion* and *perihelion* are positions of a body with regard to the sun, similar to those of apogee and perigee with regard to the earth.

§ 376. The motion of light is progressive.

§ *a*. During the time which a ray of light requires to come from the sun to the earth, the latter advances in its orbit nearly 21''; this



causes the sun to be seen about that much always in the rear of its actual position in longitude.

§ 377. The sun's *aberration*, is the difference between the sun's longitude, at the time of the emanation of a ray of light from it, and its longitude, at the time when this ray reaches the earth.

§ a. The amount of aberration must always be added to the sun's *apparent* longitude, in order to obtain the *true* longitude of the sun.

§ b. The longitude of the sun, given in the ephemeris, is *apparent*.

§ 378. *Radius vector* is a line supposed to join the centres of a planet and the sun.

§ a. The logarithm of "the radius vector of the earth" is the logarithmic value of the earth's radius vector; the semi-axis major of the earth's orbit being taken as the base, or unity, in the logarithmic scale.

TIME OF DAY.

§ 379. In the triangle P A B, are comprised the elements necessary to the operation of finding, by trigonometrical calculation, the apparent time of day. } Plate 3.

§ a. B P A, (§ 263.), is an horary angle, and if any three parts of the triangle in which it is, be given, the value of B P A is at once determinable.

§ 381. The primitive data, in the problem for finding the time of day by an observation, are usually the latitude of the observer, and the altitude and declination of the body under observation.

§ a. The complements of which form the triangle (B A P) of the problem.

§ 382. By inspecting the triangle of the problem proposed, it appears evident, that the horary angle (A P B) expresses the interval of time that elapses between the taking of the observation, and the transit of the body, (say the sun), across the meridian of the observer.

§ a. The time thus deduced is *apparent* time.

§ 383. If the observation be made in the forenoon, the value of the horary angle must be subtracted from 12h, in order to find the apparent time of day.

§ a. But if the time be P. M. the value of the horary angle expresses the apparent time of day when the altitude was measured.

§ 384. This problem, coming under Case V., (§ 201.), may be solved by either of the methods of solution there shown.

§ a. But as it is a rule, in the application of theory to practice, (and one too, which is highly important in navigation,) to combine facility of design with readiness of execution, a solution of the problem after the formula, § f. (§ 201.), will be given, in order to show thereby a process of solution less circuitous; by which process the problem under consideration may be solved.

§ 385. In lat. 20° N.; the observed altitude of the sun's lower

limb, was $29^{\circ} 29' 50''$; and its declination was $10^{\circ} 20'$ south. To

Plate 3. { find the time of day, the observation being made P. M.

§ a. First to find the true altitude of the sun's centre.
 § b. Obs. alt. Sun's L. L. = $29^{\circ} 29' 50''$
 Sun's semi-diam. = $15' 47''$

Sun's app. alt. = $29^{\circ} 45' 37''$ (§ 283. § a.)
 Refraction (§ 284.) = $1' 37''$ (Table IX.)
 Dip = $4'$ (§ 275. § a.)
 Sun's true alt. = $29^{\circ} 40'$ (§ 283. § b.)

§ c. To find the time of day.

B A, or Z, Dist. = $60^{\circ} 20'$
 P A, or Co-lat. = $70^{\circ} 00'$ co-sec. = 0.027014 (§ 201. § f.)
 P B, or P. Dist. = $100^{\circ} 20'$ co-sec. = 0.007102

2) $230^{\circ} 40'$

$\frac{1}{2}$ sum = $115^{\circ} 20'$ sin. = 0.956089
 ($\frac{1}{2}$ sum ∞ Z. Dist.) = $55^{\circ} 00'$ sin. = 0.913364

2) 19.903569

Cos. $\frac{1}{2}$ A P B = 0.951784 = $1^h 46^m \frac{1}{2}s$

2

Horary angle A P B = $3^h 32^m 1s$

This time (§ 383. § a.) is P. M.

§ 386. The data of the problem may be operated upon, more directly, by using the lat. and alt., instead of their complements.

§ a. Alt. = $29^{\circ} 40'$
 Lat. = $20^{\circ} 00'$ sec. = 0.027014
 P. D. = $100^{\circ} 20'$ co-sec. = 0.007102

2) $150^{\circ} 00'$

$\frac{1}{2}$ sum = $75^{\circ} 00'$ cos. = 0.412996
 ($\frac{1}{2}$ sum ∞ Alt.) = $45^{\circ} 20'$ sin. = 0.851997

2) 19.299109

Sin. $\frac{1}{2}$ A P B = 0.649554 = $1^h 46^m \frac{1}{2}s$

2

Horary angle A P B = $3^h 32^m 1s$

§ 387. Whence the general rule for practice.

Take the difference between the true alt., and half the sum of the lat., P. dist., and alt.; then the *product* of the sine of this difference, and cos. of said half sum, *multiplied* by the *product* of sec. of lat., and co-sec. of P. dist., is the sine of half the horary angle.

§ 388. The time thus found being apparent time, may be converted into mean time (§ 217.), by applying to it the equation of time, according to the precept given with the equation of time in the Nautical Almanac.

§ a. App. time (§ 385. § c.) 3h 32m 1s P. M.
Equation of time — 13m 50s

Mean time = 3h 18m 11s

§ 389. By comparing the mean time thus found, with the time shown by a chronometer, or other time-piece, when the altitude was measured, the error of the time-piece is obtained.

§ a. If this time-piece be regulated for a prime meridian, which is the case with chronometers; the difference between the true chronometrical, and the mean, time found by observation, expresses in *time* the difference in longitude between said prime meridian and the place of observation.

§ b. This difference of time being converted (§ 348. § g.) into degrees (°), minutes (′), etc., expresses the longitude of the observer.

LONGITUDE BY CHRONOMETER.

§ 390. The whole doctrine of determining longitude, consists in knowing the time of day at any two places at the same instant.

§ a. This is what is determined by every practicable method of finding longitude; whether it be by means of rockets, eclipses, occultations, lunar observations, or chronometers.

§ 391. The time of day at the prime meridian when an eclipse, occultation, or distance, occurs, is set down in the ephemeris; and the time of day at any other place when the same eclipse, etc., occurs, is known, either by well-regulated time-pieces, or by observations.

§ a. And the difference between these times, (§ 389. § b.), gives the longitude of the observer.

§ b. The longitude is west, when the *prime meridian* (Greenwich, § 252. § c.) time is in advance of the time of day at the observer.

§ c. But if the observer's time of day be in advance of the Greenwich time, his longitude is east; for it is evident that the sun must cross his meridian, before it does that of Greenwich, and consequently, that Greenwich must be to the westward.

§ 392. Chronometers are generally regulated so as to show the mean time of day at Greenwich.

§ a. But they are subject to variations from change of tempera-

ture, etc., and from other causes, and cannot be regulated so as to show at all times, the true time of day at Greenwich, or at any other prime meridian.

§ 393. The difference between the time shown by the face of a chronometer, and the mean time of day at Greenwich, is called "the error of chronometer."

§ *a.* The daily variation of this error is "the rate of chronometer."

§ 394. The rate of chronometer is found by noting the difference between mean time, and the time shown by the face of the chronometer, and after several days, noting again the difference between the mean and the chronometer time.

§ *a.* The difference between these two *differences*, (called "comparisons"), shows the time which the chronometer has gained, or lost, from the first to the last comparison.

§ *b.* And the quotient of this gain or loss, by the number of days that elapsed between the two comparisons, is the daily gain or loss, or rate, of the chronometer.

§ 395. The error (§ 393.) being applied to the chronometer time, with the precept of *plus* or *minus*, according as the chronometer be slow or fast, of Greenwich time, gives the mean time of day at Greenwich.

§ *a.* And the *rate* of the chronometer being applied to the chronometer's error yesterday, with the precept +, or —, according as the *rate* is *increasing* or *decreasing*, gives the chronometer's error for to-day.

§ 396. Before the chronometer is rated, the mean time of day at Greenwich for rating it, is found by turning the longitude of the observer, (§ 347.) into time; and,

§ *a.* Adding this time to the observer's mean time of day, if he be in west long.

§ *b.* And subtracting it from his mean time of day, if he be in east longitude.

§ 397. Ten or twelve days previous to the sailing of the vessel, will generally serve for keeping her chronometer under comparison, in order to find its error, and ascertain its rate.

§ *a.* But after sailing, the rate should be compared, (and corrected if necessary), as often as opportunities for making comparisons occur.

§ 398. To find the error and ascertain the rate of a chronometer, the observer being in lat. $40^{\circ} 42' N.$ and long. $74^{\circ} 00' W.$

§ *a.* Aug. 4th, A. M., 1834.

Chro. 12h 58m. App. alt. Sun's L. L. $30^{\circ} 17' 20''$
Sun's semi-diam. = $15' 47''$

App. alt. Sun's centr. = $30^{\circ} 33' 7''$
Refraction - = $1' 37''$

Sun's Tr. alt. = $30^{\circ} 31' 30''$

§ b.

Sun's tr. alt. = $30^{\circ} 31' 30''$ (§ 387.)
 Lat. = $40^{\circ} 42' 00''$ sec. = 0.120254
 Sun's P. dist. = $72^{\circ} 40' 30''$ co-sec. = 0.020164

$$\underline{2)143^{\circ} 54' 00''}$$

$\frac{1}{2}$ sum = $71^{\circ} 57' 00''$ cos. = 9.491147
 (Alt. $\infty \frac{1}{2}$ sum) = $41^{\circ} 25' 30''$ sin. = 9.820621

$$\underline{2)19.452186}$$

Sin. $\frac{1}{2}$ Horary angle = $9.726093 = 2h 8m 37s +$

2

Horary angle = $12h 00m 00s$ (§ 383.)
 $4h 17m 14s$ - $= 4h 17m 14s$

Equation $7h 42m 46s$ App. time
 $+ 5m 47s$ (§ 388.)

Chron. $7h 48m 33s$ Mean time, A. M.
 $12h 58m 00s$ (§ 398. § a.)

$5h 9m 27s$ 1st comparison, (§ 394.)

§ c. Aug. 15, A. M. Chron. $12h 34m 25s$.
 App. alt. Sun's L. L. $24^{\circ} 2' 10''$
 Sun's semi-diam. $15' 49''$

App. alt. Sun's centr. $24^{\circ} 17' 59''$
 Refraction - $2' 9''$ (Table IX.)

§ d. Sun's tr. alt. $24^{\circ} 15' 50''$
 Lat. - $40^{\circ} 42' 0''$ sec. = 0.120254
 Sun's P. dist. $75^{\circ} 51' 10''$ cosec. = 0.013376

$$\underline{2)140^{\circ} 49' 00''}$$

$\frac{1}{2}$ Sum - $70^{\circ} 24' 30''$ cos. = 9.525452
 ($\frac{1}{2}$ sum ∞ Alt.) $46^{\circ} 8' 40''$ sin. = 9.857989

$$\underline{2)19.517071}$$

Sin. $\frac{1}{2}$ Horary angle = $9.758535 = 2h 19m 58\frac{1}{2}s$

2

Horary angle = $4h 39m 57s$

	12h 0m 0s	
Horary angle	4h 39m 57s	
	<hr style="width: 50%; margin-left: auto; margin-right: 0;"/>	
Equation	7h 20m 3s	App. time
	+ 4m 15s	
	<hr style="width: 50%; margin-left: auto; margin-right: 0;"/>	
	7h 24m 18s	Mean time, A. M.
Chro.	12h 34m 25s	
	<hr style="width: 50%; margin-left: auto; margin-right: 0;"/>	
	5h 10m 7s	2d comparison.

§ e. 2d Compr. 5h 10m 7s
 1st do. 5h 9m 27s (§ 394. § a.)

Chro. gains 40s in 11 days.

§ f. $40s \div 11 = 3\frac{7}{11}s$ (§ 394. § b.) the daily gain, or rate.

§ g. Long. of the observer $74^\circ W.$ = 4h 58m
 Time of (§ d.) last. obs. - = 7h 24m 18s

(§ 396. § a.) Greenwich time do. = 12h 20m 18s
 Chro. (§ c.) - - = 12h 34m 25s

Error (§ 393.) of chro. Aug. 15th, = 14m 7s (fast.)

§ h. To find long. by chronometer;

Time per watch 3h P. M. = 15h 0m 0s
 do. chron. - = 11h 15m 22s

Diff. = 3h 44m 38s Chr. slow.

Time of obs. per W. 15h 2m 30s
 Chro. slow of W. 3h 44m 38s

Chro. time of obs. = 11h 17m 52s

Formula for calculation.

Sun's Alt. $31^{\circ} 18'$ (corrected)
 Lat. $36^{\circ} 19'$ sec. = 0.093796
 P. D. $104^{\circ} 9'$ co-sec. = 0.013381

Sum = 2) $171^{\circ} 46'$

$\frac{1}{2}$ sum = $85^{\circ} 53'$ cos. = 8.856049
 Rem'r. = $54^{\circ} 35'$ sin. = 9.911136 (Alt. $\infty \frac{1}{2}$ Sum.)

2) 18.874362

Sin. $\frac{1}{2}$ App. time = 9.437181 = $1h 3m 31\frac{1}{2}s$

2

App. time of obs. = $2h 7m 3s$ P. M.
 Equation - + $4m 16s$

Mean time of obs. $2h 11m 19s$ P. M.

Time of obs. per chro. $11h 17m 52s$
 Chro. slow of Gr. time $1h 3m 8s$

Greenwich time $12h 21m 0s$
 Time of obs. - $14h 11m 19s$

Long. in time (§ 391. § c.) $1h 50m 19s = 27^{\circ} 34' 45''$ E.

§ 399. By inspecting the triangle (P B A) of the problem for finding the apparent time of day, it becomes evident, that if, of the lat., time of day, dec., alt., and azimuth, of the sun, or any other body, any three be known, the two others are determinable. } Plate 3.

§ a. The azimuth gives the angle P A B; and the apparent time of day gives the angle A P B; the altitude (B I) determines the zenith distance A B; the latitude A Q, determines P A, the co-lat., and the declination k B, determines the polar distance P B.

LATITUDE BY MERIDIAN ALTITUDES.

§ 400. The most common method of determining latitude at sea, is by means of an altitude of a celestial body, measured when the body is on the meridian.

§ a. Then the circle of the body's declination, coincides with the meridian (N A S) of the observer.

§ 401. Suppose the body be a star; the zenith distance (A e') (§ 282. § b.) expresses the number of degrees, etc., from (A) the zenith to the star.

§ a. And the declination Q e' (§ 255. § b.) gives in the same measure, the distance of the body from the equator.

Plate 3. $\left\{ \begin{array}{l} \S b. \text{ Wherefore the difference between the declination} \\ \text{(Q } e') \text{ and the zenith distance (A } e') \text{ gives A Q the latitude.} \end{array} \right.$

$\S 402.$ The sun being south of the observer, and its declination $10^{\circ} 20'$ south, its meridian altitude (corrected) was $59^{\circ} 40'$.

To find the latitude of the observer,

$\S a.$ The sun's altitude ($\S 282. \S a.$) is $e S$; $90^{\circ} - e S = A e$ ($\S 282. \S b.$) the zenith distance.

$\S b.$ The observer being at A, north of the sun, makes ($\S 281. \S b.$) the zenith dist., A e , north.

$\S c.$ The dec. Q e , being taken from the zenith dist. A e , leaves A Q, the required latitude.

$\S d.$ Sun's Z. D. ($\S a.$) = $30^{\circ} 20' N.$ ($\S b.$)

Sun's dec. = $10^{\circ} 20' S.$

Lat. = $20^{\circ} 00' N.$

$\S 403.$ Suppose the object to bear south, but its dec. to be $9^{\circ} 3' N.$ and its meridian alt. $79^{\circ} 3'$.

To find the latitude,

$\S a.$ The stars alt. is $e' S$; A $S - e' S = A e'$ the *'s zenith dist.

$\S b.$ The dec. Q e' being added to $e' A$ the zenith dist., makes A Q, which is the latitude.

$\S c.$ *'s Z. D. = $10^{\circ} 57' N.$

*'s dec. = $9^{\circ} 3' N.$

Lat. = $20^{\circ} 00' N.$

$\S 404.$ Suppose the star to be north of the observer, its declination $60^{\circ} 5' N.$, and its meridian alt. = $49^{\circ} 55'$.

To find the lat. of the observer,

$\S a.$ N e'' is the *'s alt. The zenith dist. ($\S 281. \S c.$) is south; N A — N $e'' = A e''$, the *'s zenith dist.

$\S b.$ The dec. Q $e'' - A e''$ (the zenith dist.), gives A Q, the lat.

$\S c.$ *'s dec. = $60^{\circ} 5' N.$

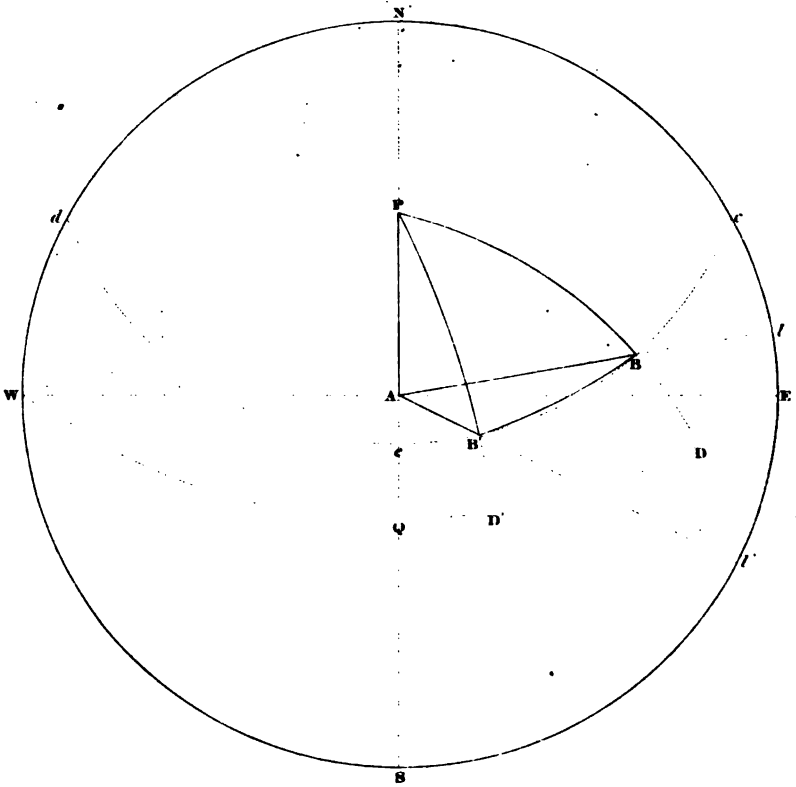
*'s Z. D. = $40^{\circ} 5' S.$

Lat. = $20^{\circ} 0' N.$

$\S 405.$ Wherefore, when the dec., and the meridian zenith dist. are both north, or both south, their *sum* is the latitude.

$\S 406.$ And, when one is north, and the other south, their *difference* is the latitude.

$\S 407.$ When the body is in the zenith, there is no zenith dist., and the dec. is the lat.



LATITUDE BY DOUBLE ALTITUDES.

§ 408. The sun, (and every other celestial object), is frequently obscured by clouds, so that a meridian alt. cannot be measured.

§ a. Under such circumstances, data sufficient for determining the lat. may be obtained by taking at two different hours of the day the sun's alt., and noting the time that elapses between the two observations.

§ 409. The time, expressed in degrees, or hours, etc. (§ 348. § b.) constitutes, with the zenith and polar distances, the required data.

§ 410. This method of finding the lat. is called "by *Double Altitudes*."

§ a. The process of calculation is tedious, but the result will give the latitude as correctly as it can be obtained through any other process of observation and calculation.

§ 412. For determining the lat. by "double altitudes," }
 B D represents the declination, and B l the alt. of the sun, } Plate 4.
 at the first observation; and B' D', and B' l' the dec. and alt., at the second observation.

§ a. A P B is the sun's horary angle at the first, and A P B', its horary angle at the second, observation.

§ b. The difference (B' P B) between these two angles, is the angular value of the time that elapses between the observations.

§ c. B B' is the arc of the great circle, which passes through the points, in which the centre of the sun was at each observation.

§ d. The other circles, arcs and angles, of the Fig., are explained under § 317. (§ a.).

§ 413. The problem of "double altitudes" involves three triangles (B' P B, A B B', & A P B') in the process of solution.

§ a. The side B' B is common to the first and second triangles; P B' to the first and third; and A B' to the second and third.

§ 414. The parts that are given in the first triangle (B' P B), are the two sides, P B and P B' (§ 412.), which are the P. dist. (§ 256.) at the first, and the second observation; and (§ 412. § b.) their contained angle B' P B = Elapsed Time.

§ a. And the parts required are, the third side B' B, and the angle P B' B.

§ 415. The value of P B' B and B' B being determined by calculation, the parts that are then known in the second triangle A B B', are B A and B' A (§ 412.); which are the zenith dist. (§ 281.) of the sun at the first and the second observation; and the common side B' B.

§ a. The part here required, is the angle A B' B.

§ 416. The difference between the angles A B' B, and P B' B (§ 414. § a.) gives the value of the angle A B' P, in the third triangle A P B'.

§ 417. Then in the third triangle, the two sides A B', P B' and their contained angle A B' P, are the given parts; and P A is the part required, and the co-lat.

§ 418. In north latitude, at 7 A. M. by a watch.

Sun's true alt. $24^{\circ} 58' 12''$

Sun's dec. $22^{\circ} 25' 00''$ N.

Plate 4. $\left\{ \begin{array}{l} \text{§ a. And at the } 10^h 15^m \text{ by the same watch,} \\ \text{Sun's true alt. } 62^{\circ} 49' 20'' \\ \text{Sun's dec. } 22^{\circ} 24' 00'' \text{ N.} \end{array} \right.$

§ b. The elapsed time is $3^h 15^m$.

§ 419. P B (1st P. D.) = $67^{\circ} 35'$

P B' (2d P. D.) = $67^{\circ} 36'$

A B (1st Z. D.) = $65^{\circ} 1' 48''$

A B' (2d Z. D.) = $27^{\circ} 10' 40''$

B' P B (E. time) = $3^h 15^m$. (§ 409.)

§ 420. To find the side B' B and angle P B' B (§ 414. § a.) in the first triangle B' P B.

§ a. 1st. To find the value of B' B (§ 200. § s. & § t.).

B' P B (E. T.) = $3^h 15^m$ cos. = 9.819113 (§ 348. § c.)

P B' (2d P. D.) = $67^{\circ} 36'$ tang. = 0.384923

Tang. aux. $a = 0.204036 = 57^{\circ} 59' 23''$

P B = $67^{\circ} 35'$

(a_{∞} P B) = $9^{\circ} 35' 37''$

P B' (2d P. D.) = $67^{\circ} 36'$ cos. = 9.581005

Auxl. $a = 57^{\circ} 59' 23''$ sec. = 0.275666

(a_{∞} 1st P. D.) = $9^{\circ} 35' 37''$ cos. = 9.993884

Cos. B' B = 9.850555 = $44^{\circ} 51' 30''$

§ b. To find the value of P B' B (§ 144.).

B' B = $44^{\circ} 51' 30''$ co-sec. = 0.151591

B' P B (E. T.) = $3^h 15^m$ sin. = 9.876125

P B (1st P. D.) = $67^{\circ} 35'$ sin. = 9.965876

Sin P B' B = 9.993592 = $80^{\circ} 10' 53''$

§ c. In the second triangle, to find the value of the an- } Plate 4.
gle A B' B (§ 201. § d.).

A B (1st Z. D.) = 65° 1' 48''
A B' (2d Z. D.) = 27° 10' 40'' co-sec. = 0.340319
B' B (§ a.) = 44° 51' 30'' co-sec. = 0.151591

2) 137° 3' 58''

½ Sum = 68° 31' 59'' sin. = 9.968776
(½ S. ∞ 1st Z. D.) = 3° 30' 11'' sin. = 8.786053

2) 19.246739

Cos. $\frac{A B' B}{2}$ = 9.623369 = 65° 9' 29''

2

A B' B = 130° 18' 58''

P B' B (§ b.) = 80° 10' 53''

A B' P = 50° 8' 5''

§ d. In the third triangle, to find the value of the third side A P ;
or to find the latitude (§ 200. § s. & § t.)

A B' P = 50° 8' 5'' cos. = 9.806848

P B (2d P. D.) = 67° 36' tang. = 0.884923

Tang. auxl. a = 0.191771 = 57° 15' 29''

A B' = 27° 10' 40''

(∞ A B') = 30° 4' 49''

P B' (2d P. D.) = 67° 36' cos. = 9.581005

Auxl. a = 57° 15' 29'' sec. = 0.266918

(∞ 2d Z. D.) = 30° 4' 49'' cos. = 9.937178

Cos. A P = 9.785101 sin. = lat. 37° 33' 59'' N

§ 421. In the example last quoted, the two observations are taken at the same place ; but in practice, this cannot always be done, especially at sea, when the vessel is changing her place during the time that elapses between the taking of the observations.

§ a. Therefore the 1st altitude must be corrected, in order to know what it would have been, had it been taken at the same time per watch, but at the place where the 2d obs. was made.

§ 422. When the first observation is being made, note the bearing of the sun and the course of the ship ; and after the second observation has been taken, find in a traverse table (Table IV.), the

course and distance from the place where the first, to that where the second, observation was taken.

§ a. The angle, which this distance makes with the bearing of the sun, being used in the traverse table, as a course, the correction which is to be applied to the first alt., is found under this course, and opposite to said distance, and in the column marked "*d. lat.*"

§ 423. If this angle be less than 90° , the correction thus found is additive.

§ 424. If it be greater than 90° , its supplement is the course; and,

§ a. The correction is subtractive.

§ 425. If the ship sail on the line of the sun's bearing, the distance sailed in miles, is the correction in minutes (') of a degree.

§ a. It is additive when the ship sails towards the sun; and,

§ b. Subtractive when she sails from the sun.

§ 426. The corrections are found as geographical miles, but are to be applied to the altitude as minutes (') of a degree.

§ 427. When the angle between the bearing of the sun, and the course which the ship makes, is 90° , there is no correction.

§ 428. The corrections thus obtained and applied, do not show *exactly* what the 1st altitude would have been at the place of the second observation; but the approximation is sufficiently close to answer the purposes of common navigation.

§ 429. The time that elapses between the taking of the observations, should not be less than 30*m*, or more than 6*h*, if avoidable, especially if the observer be at sea.

§ a. If the body under observation do not change much in declination during the "elapsed time," the *mean* of its declination at the two observations may be used as the body's declination at each observation.

§ b. This "*mean*" declination is found by taking out the declination for half of the "elapsed time," *plus* the time of the first observation.

Plate 4. } § c. When the *mean* declination is used, $PB = PB'$; and the first triangle $B'PB$ (§ 140.) is isosceles.

§ 430. The latitude at the time and place of the first observation, may be found, if required, by making APB the third triangle, and using the angles PBB' , ABB' and ABP , instead of $PB'B$, $AB'B$ and $AB'P$ (§ 420. § b. & § c.).

§ a. But generally, in navigation, the latitude of the time present, is most desirable to be known; and usually, when the problem is solved, the vessel is nearer to the place of the second, than she is to the place of the first observation.

§ b. A formula for practice in finding the latitude at sea by "double altitudes;" the mean declination being used. Under the example § 418.

Sun's mean dec. = $22^\circ 24' 30''$, P. D. = $67^\circ 35' 30''$

Sun's 1st alt. = $24^\circ 58' 12''$, 1st Z. D. = $65^\circ 1' 48''$

Sun's 2d alt. = $62^\circ 49' 20''$, 2d Z. D. = $27^\circ 10' 40''$

E. time - 3*h* 15*m*

§ c. The first triangle (§ 429. § c.) is isosceles; wherefore (§ 200. § z a., § z c. & § z f.)

P. D. = 87° 35' 30" sin. = 9.965903 sec. = 0.418842
 (½ E. time) = 1h 37m 30s sin. = 9.615642 cot. = 0.343812

Arc $\frac{B'B}{2}$ = 22° 25' 46" Sin. = 9.581545
 2 1st Ang. 80° 12' 2" Tang. = 0.762654

Arc B'B = 44° 51' 32" co-sec. = 0.151587 (§ 420. § c.)

2d Z. D. = 27° 10' 40" co-sec. = 0.340319

1st " = 65° 1' 48"

2) 137° 4' 0"

½ S. = 68° 32' 0" sin. = 9.968777

(½ S. as Z. D.) 3° 30' 12" sin. = 8.786087

2) 19.248770

Cos. ½ 2d Angle = 9.623385 = 65° 9' 25"

2

2d Angle = 130° 18' 50"

1st " = 80° 12' 2"

3d " = 50° 6' 48"

½ (3d Angle) = 25° 3' 24" sin. × 2 = 19.253736 (§ 200. § z f.)

P. D. = 87° 35' 30" sin. = 9.965903

2d Z. D. = 27° 10' 40" sin. = 9.659681

2) 38.879320

(P. D. = 2d Z. D.) = 40° 24' 50" 19.439660

$\frac{P. D. \times 2d Z. D.}{2}$ = 20° 12' 25" co-sec. = 0.461662

Tang. a = 9.901322 = 38° 32' 46"

a. co-sec. = 0.205412

Sin. ½ co-lat. = 9.645072 = 26° 12' 32"

2

Lat. = 37° 34' 56" or co-lat. = 52° 25' 4"

§ d. The result by this method differs 57" from the truth. Like every other trigonometrical calculation, in which true data are not

operated upon, it brings an error into the result; but the result is an approximation, which oscillates about the truth, and within limits that depend upon the correctness of the assumed data.

§ *c.* Some navigators solve the problem of "double altitudes" by the method proposed by a Mr. Douwes; but the correctness of the result by his method, depends upon repeated calculations, or the proximity of a *supposed*, to the correct, latitude.*

§ 431. Latitude by "double altitudes" may also be determined by taking, at the same instant, the altitudes of any two bodies, whose right ascension and declination are given.

§ 432. The method of solving this problem consists in a process of operation, precisely similar to that (§ 420.) for finding the latitude by means of two altitudes of the same body, taken at different times.

Plate 4. { § 433. The difference in right ascension of the two bodies gives an angle, which corresponds to the angular value (B' P B) of the "elapsed time," between the two observations.

§ 434. When the difference in right ascension of the two bodies, exceeds 180° or $12h$, the greater right ascension, subtracted from the less *plus* $24h$, gives the angle corresponding to B' P B.

§ 435. In this method of finding latitude, the altitude of the moon, unless the Greenwich time be known, cannot be used with certainty of success. For the moon's variation in declination and right ascension, is so rapid, that unless the Greenwich time of day, when the observations are made, be known, the proper value of the angle corresponding to B' P B, cannot be obtained.

§ 436. The stars afford the greatest facilities for the application of this problem to practice.

§ *a.* Their variation in declination and right ascension, being for the most part, not very rapid; consequently when the horizon is well defined, the data requisite to the solution of the problem, can be obtained by means of the stars, with sufficient accuracy.

§ 437. In north lat. June 2, 1834, Jupiter being east, and Mars west, of the meridian; their altitudes were taken at the same instant;

J.'s alt.	71°	49'	To find the latitude.
" dec.	18°	0' 40" N	
" rt. asn.	3h	27m 36s	
M.'s "	1h	9m 20s	
" dec.	5°	54' 20" N	
" alt.	70°	29' 12"	

Plate 5. { § *a.* Difference in right ascension is $2h\ 18m\ 16s$.
 { § 438. B I and B D are Jupiter's altitude and declina-

* Mr. Douwes' method is both supported and questioned by high authority. Bowditch has adopted it in his PRACTICAL NAVIGATOR. And there is a paper from M. Delambre, showing that the result by this method is not always an approximation, but that, in some cases, if repetitions be made, the result will recede from the true latitude.

tion; and $B' P'$, and $B' D'$ are Mars' alt. and dec.; and $B' P B$ } Plate 5.
 is the angular value of their difference in right ascension. }

§ 440. $B P B'$ is the first triangle in the problem, that is brought under calculation; $B' B$ and $B' B P$, are the required parts.

§ a. $B' A B$ is the second triangle, and $A B B'$ is the part in it, that is required;

§ b. $A B B' \propto B' B P = A B P$.

§ c. $A P B$ is the third triangle, and $A P$ is the part required to complete the problem.

§ 441. $P B$ (J.'s P. D.) = $71^\circ 59' 20''$

$P B'$ (M.'s P. D.) = $84^\circ 5' 40''$

$B' P B$ (diff. R. A.) = $2h 18m 16s$

$A B$ (J.'s Z. D.) = $18^\circ 11' 0''$

$A B'$ (M.'s Z. D.) = $19^\circ 30' 48''$

§ a. To find the value of $B' B$ (§ 200. § s. & § t.)

$B' P B$ (diff. R. A.) $2h 18m 16s$ cos. = 0.915646

$P B$ (J.'s P. D.) = $71^\circ 59' 20''$ tang. = 0.487937

Tang. auxl. $a = 0.403583 = 68^\circ 27' 15''$

M.'s P. D. = $84^\circ 5' 40''$

M.'s P. D. $\propto a = 15^\circ 38' 25''$

$P B$ (J.'s P. D.) = $71^\circ 59' 20''$ cos. = 0.9490243

Auxl. $a = 68^\circ 27' 15''$ sec. = 0.435044

($a \propto P B'$) (M.'s P. D.) = $15^\circ 38' 25''$ cos. = 0.983614

Cos. $B' B = 0.908901 = 35^\circ 49' 42''$

§ b. To find the value of the angle $P B B'$ (§ 420. § b.)

$B B'$ $30^\circ 49' 42''$ co-sec. = 0.232578

$B P B'$ (diff. R. A.) = $7h 18m 16s$ sin. = 0.9753862

$P B'$ (M.'s P. D.) = $84^\circ 5' 40''$ sin. = 0.997689

Sin. $P B B' = 0.984129 = 105^\circ 23' 52''$

Plate 5. | § c. To find the value of A B B' (§ 201. § f.)

$$\begin{aligned} \text{A B' (M.'s Z.D.)} &= 19^\circ 30' 48'' \\ \text{A B (J.'s Z. D.)} &= 18^\circ 11' 00'' \text{ cosec.} = 0.505764 \\ \text{B' B} &= 35^\circ 49' 42'' \text{ " } = 0.232578 \end{aligned}$$

$$\underline{2)73^\circ 31' 30''}$$

$$\begin{aligned} \frac{1}{2} \text{ Sum} &= 36^\circ 45' 45'' \text{ sin.} = 9.777063 \\ (\frac{1}{2} \text{ S } \omega \text{ A B', M.'s Z.D.}) &= 17^\circ 14' 57'' \text{ " } = 9.472066 \end{aligned}$$

$$\underline{2)19.987471}$$

$$\text{Cos. } \frac{\text{A B B'}}{2} = 9.993735 = 9^\circ 42' 30''$$

2

$$\text{A B B'} = 19^\circ 25' 00''$$

$$\text{P B B'} = 106^\circ 23' 52''$$

$$\text{A B P} = 85^\circ 58' 52''$$

§ d. To find the value of A P or co-lat. (§ 200. § u.)

$$\text{A B P} = 85^\circ 58' 52'' \text{ cos.} = 8.845627$$

$$\text{P B} = 71^\circ 59' 20'' \text{ tang.} = 0.487937$$

$$\text{Tang. Auxl. } a = 9.333564 = 12^\circ 9' 52''$$

$$\text{A B (J.'s Z. D.)} = 18^\circ 11' 06''$$

$$\underline{(\alpha \omega \text{ J.'s Z. D.}) = 6^\circ 01' 8''}$$

$$\text{P B (J.'s P. D.)} = 71^\circ 59' 20'' \text{ cos.} = 9.490243$$

$$\text{Auxl. } a = 12^\circ 9' 52'' \text{ sec.} = 0.009864$$

$$\underline{(\alpha \omega \text{ A B, J.'s Z.D.}) = 6^\circ 1' 8'' \text{ cos.} = 9.997599}$$

$$\text{Cos. A P (co-lat.)} = 9.497706 \text{ S.} = \text{lat. } 18^\circ 30' 4'' \text{ N.}$$

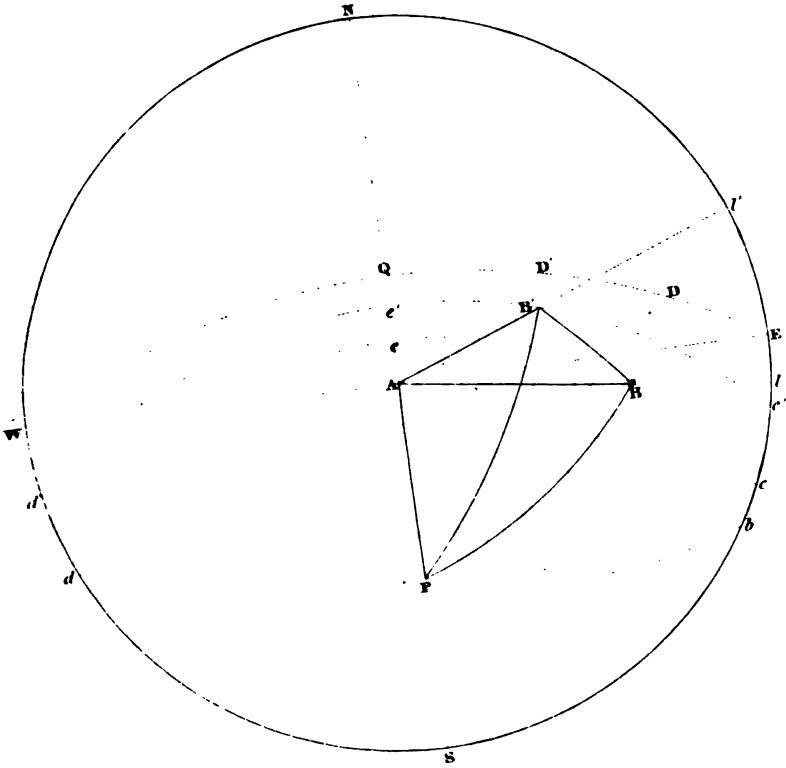
§ 442. The data for determining latitude by "double altitudes" may be obtained also by taking the altitude of two objects, each at a different time of the day.

§ a. This method may sometimes be found useful in cloudy weather, when the two objects cannot be seen at the same time, and when it is highly important to know the latitude.

§ 443. When the first object (say a star) is seen, let its altitude be taken, and the time, per watch, when the observation is made, noted down.

§ a. The bearing of the star at the same time, must also be observed, in order that the angle may be known, which is contained between this bearing, and the rhumb line, upon which the ship sails until the second observation may be made.

§ b. This angle, and the distance sailed during the interval that elapses between the taking of the two observations, are to be used



in finding the correction (§ 422. § a.) which must be applied to the first altitude, to make it what it would have been, had it been taken at the place where the second observation was taken.

§ 444. The right ascension and declination of this star must be taken out of the Nautical Almanac, also for the time at which its altitude was measured.

§ 445. When the second object (say the sun) is seen, its altitude also must be taken, and the time of its being done noted down, in order to know the time which has elapsed since the first observation.

§ 446. The right ascension and declination of the sun, when its altitude is measured, must also be found, in order to obtain the difference in right ascension of the two bodies when their altitudes were taken.

§ u. This difference is an angle formed at the pole, by the intersection of the circle of right ascension, in which the star was, when its altitude was taken, with the circle of right ascension which passed through the centre of the sun, when the alt. of it was measured.

§ 447. This angle corresponds to $B'PB$; and with the } Plate 5,
portion of *apparent time* that elapses from the taking of }
the first, till the taking of the last, observation, it constitutes the
angle which is contained between the P. distances of the two bodies;
and with the polar and zenith distances of these bodies, it also constitutes the required data of the problem.

§ 448. The sum or difference of the *difference* of the two bodies in right ascension, and the portion of *mean time* from one observation to the other, give the required contained angle.

§ a. If the sun be the second object, the *apparent* instead of the *mean* time, from one observation to the other, must be taken.

§ 449. The sum of said two quantities is the value of this angle, when the first object is to the eastward of the second.

§ 450. But when the second is the more eastwardly object, the difference of the two in right ascension, *minus* the *elapsed* time, gives the value of the required polar angle.

§ 451. If, when the second is the eastern object, the elapsed time exceed the difference in right ascension of the two bodies, the second will have crossed the hour circle (§ 263. § c.) which coincides with the circle of declination, in which the first object was, when its altitude was measured.

§ 452. The excess of the elapsed time above this difference } Plate 6.
ence in ascension, is the value of the required polar angle }
($B'PB$).

§ 453. B represents the place of Venus (the first object), when its altitude was taken.

§ a. Venus was then the morning star, and consequently to the westward of the sun, (which is the second object).

§ b. Venus' altitude was taken in the morning, when the sun was below the horizon.

§ c. Pb is an arc of the circle of right ascension in which the sun was, when Venus' altitude was taken.

Plate 6. } § *d.* $B' P b$, is the angular value of the difference in right ascension of the sun and Venus, when the altitude (B) of the latter was taken; it is about $2h\ 36m\ 54s$.

§ 454. The sun's altitude, $B' l'$, was taken $4h\ 29m\ 45s$ after Venus' was measured.

§ 455. The sun had then crossed over the hour circle $P B$ (§ 263. § *c.*) in which Venus was, when its altitude was taken.

§ *a.* The sun was at B' , to the westward of this circle, when its altitude was taken.

§ 456. $B' P b$, is the horary angle, in *apparent* time, which the sun described during the interval between the taking of the altitudes.

§ *a.* Consequently the difference ($B P b$) of the sun and Venus in right ascension, when their altitudes were measured, subtracted from ($B' P b$) the angular value of the *apparent* time between the observations, gives the value of the angle $B' P B$.

§ 457. If the portion of time that elapses, between the observations, be given in mean time, it may be converted into apparent time, by applying to it the fraction which during the elapsed time, the second object's equation of time gains or loses, on mean time.

§ 458. In surveying expeditions the elapsed time should be corrected and changed into *apparent* time, in order to determine the latitude with exactness.

§ 459. But upon the open sea, this nicety in operation may be omitted, for it only advances, by a very small fraction, the accuracy of the result.

§ 460. If the altitude of the more easterly object, be taken last, and the elapsed time be equal to their difference in right ascension, the same hour circle (§ 263. § *c.*) will pass through each object when its altitude is taken; and the process of deducing the latitude will be confined to the simple operation of finding an angle with the three sides of a triangle as data; and thence in deducing, from the two sides and their contained angle, as data in a second triangle, its third side, which is the co-lat.

§ *a.* The three sides of the former of these two triangles, would be the zenith dist. of each body, and the difference between their polar distances.

§ 461. Feb. 25, 1832. Venus being the morning star, and the observer being in south latitude when he made his observations.

§ *a.* Venus' Alt. $24^{\circ}\ 50'$ (*True.*)
 " Dec. $20^{\circ}\ 5'$ S.
 " Rt. Ascen. $19h\ 59m$
 " bearing $E. \frac{1}{4} S.$ (§ 443. § *a.*)

Time per watch $3h\ 16m\ 19s$

§ *b.* The ship then sailed N. E. $\frac{1}{4} N.$ 18 miles, when the sun was seen, and its altitude taken.

Sun's Alt. $43^{\circ}\ 44'$ (*Correct.* § 385. § *b.*)
 Sun's Dec. $9^{\circ}\ 16'$ S.
 Sun's Rt. A. $22h\ 30m\ 59s$
 Time per watch $7h\ 46m\ 8s$

§ 462. The angle between the bearing of Venus (§ 461. § a.), and the ship's course, is five points, which (§ 422. § a.) with the distance sailed, (18 miles), gives 10' (§ 426.) in the column (*d. lat.*) of the traverse tables; which 10' (§ 423.) being added to Venus' altitude, makes it 25°, (what it was at the time of its being taken, but at the place where the sun's alt. was observed.)

§ 463. The watch kept *mean* time. The elapsed time (§ 457.) must therefore be corrected, in order to obtain the portion of *apparent* time, that elapsed from the first, until the second observation was taken.

§ a. During this interval there were 2s less of apparent, than of mean time, which being subtracted from the mean time elapsed, gives the elapsed apparent time.

§ 464. This correction is obtained from the ephemeris. It is the quantity which the equation of time gains or loses from the first to the second observation; and it must be applied accordingly.

§ 465. The triangulation, through which the process } Plate 6.
of finding the latitude by means of the data in this pro- }
blem is conducted, is represented in the triangles B' P B, A B' B and }
A B' P. }

$$\begin{aligned} \text{§ 466. } AB (\text{star's Z. D.}) &= 65^\circ 0' \\ PB (\text{star's P. D.}) &= 69^\circ 55' \\ AB' (\text{sun's Z. D.}) &= 46^\circ 16' \\ PB' (\text{sun's P. D.}) &= 80^\circ 44' \\ \text{Elapsed mean time} &= 4h 29m 49s \\ \text{Correction (§ 463. § a.)} & \quad \quad \quad 2s \end{aligned}$$

$$\begin{aligned} \text{Elapsed app. time} & \quad \quad \quad = 4h 29m 47s \\ \text{Diff. in R. A. of sun and star} &= 2h 31m 59s \end{aligned}$$

$$B' P B = 1h 57m 48s \quad (\text{§ 456. § a.})$$

To find the latitude.

§ a. In the triangle B' B P, to find the value of B' B. (§ 200. § n.)

$$\begin{aligned} B' P B = 1h 57m 48s \quad \cos. &= 9.939911 \\ P B' (\text{Sun's P.D.}) = 80^\circ 44' \quad \text{tang.} &= 0.787389 \end{aligned}$$

$$\text{Tang. auxl. } a = 0.727300 = 79^\circ 23' 15''$$

$$PB = 69^\circ 55' 0''$$

$$(a \oslash \text{star's P. D.}) = 9^\circ 28' 15''$$

$$\begin{aligned} PB' (\text{sun's P. D.}) = 80^\circ 44' \quad \cos. &= 9.206906 \\ \text{Auxl. } a = 79^\circ 23' 15'' \quad \text{sec.} &= 0.734791 \\ (a \oslash PB) \quad \quad \quad = 9^\circ 28' 15'' \quad \cos. &= 9.994040 \end{aligned}$$

$$\text{Cos. } B' B = 9.935737 = 30^\circ 24' 21''$$

Plate 6. $\left\{ \begin{array}{l} \S b. \text{ To find the value of } P B' B. \\ B' B = 30^\circ 24' 24'' \text{ co-sec.} = 0.295734 \\ B' P B = 1^h 57^m 48^s \text{ sin.} = 9.691668 \\ P B (\text{star's P. D.}) = 69^\circ 55' 0'' \text{ sin.} = 9.972755 \end{array} \right.$

$$\text{Sine } P B' B = 9.960157 = 65^\circ 49' 50''$$

$\S c.$ To find $A B' B$ ($\S 201. \S f.$)
 $A B$ (star's Z. D.) = 65°
 $A B'$ (sun's Z. D.) = $46^\circ 16'$ co-sec. = 0.141123
 $B' B = 30^\circ 24' 24''$ co-sec. = 0.295734

$$2) 141^\circ 40' 24''$$

$\frac{1}{2}$ sum = $70^\circ 50' 12''$ sin. = 9.975241
 $(\frac{1}{2} S. \omega \text{ star's Z. D.}) = 5^\circ 50' 12''$ sin. = 9.007291

$$2) 19.419389$$

$$\text{Cos. } \frac{A B' B}{2} = 9.709694 = 59^\circ 10' 10''$$

2

$$A B' B = 118^\circ 20' 20''$$

$$P B' B = 65^\circ 49' 50''$$

$$A B' P = 52^\circ 30' 30''$$

$\S d.$ To find $A P$, the co-lat.

$A B' P = 52^\circ 30' 30''$ cos. = 9.784365
 $P B' (\text{Sun's P. D.}) = 80^\circ 44'$ tang. = 0.787389

$$\text{Tang. auxl. } a = 0.571754 = 74^\circ 59' 37''$$

$$A B' = 46^\circ 16' 0''$$

$$(a \omega A B') = 28^\circ 43' 37''$$

$P B' (\text{sun's P. D.}) = 80^\circ 44'$ cos. = 9.206906
 Auxl. $a = 74^\circ 59' 37''$ sec. = 0.586823
 $(a \omega \text{ sun's Z. D.}) = 28^\circ 43' 37''$ cos. = 9.942959

$$\text{Sin. Complement } A P, \text{ or lat.} = 9.736688 = 33^\circ 2' 59'' \text{ South.}^*$$

* This differs $1''$ from the truth.

LUNARS.

§ 467. The problem of finding the *true* distance between the sun, or a star, and the moon, for the purpose of thence determining the longitude, is one of great importance in navigation.

§ 468. The necessity for the circuitry of calculation in finding the longitude by lunar observations, arises from the circumstance that the two observed bodies are not seen (§ 289.) in their true places.

§ *a.* They always appear, each in its proper azimuth circle, but higher up, or lower down in it (§ 283. § *c.*), than its true place,

§ *b.* And consequently (§ 283.) they appear either nearer to, or farther from, each other, than they really are, which makes the difference between the true, and apparent lunar distance.

§ 469. Only two triangles are involved in the process of finding, by trigonometrical calculation, the *true* from the *observed* lunar distance.

§ *a.* Of the first triangle, the three sides are given; and the angle required is that which is contained at the zenith, between the zenith distance of the moon, and of the other body.

§ *b.* Of the second triangle, this angle and its adjacent sides, are the given parts; and the third side, or true lunar distance, is the part required.

§ *c.* The three sides of the first triangle are the apparent lunar, and the app. zenith distances of the two bodies.

§ *d.* And the three sides of the second triangle, are the *true* lunar and zenith distances.

§ 470. The *lunar*, or the *true lunar distance* of the sun, or a star, is an arc of a great circle, contained between the centres of either of those objects, and the moon.

§ 471. The distance between the perfect limb (§ 283.), or the round edge, of the moon and the near limb of the sun, is the distance usually measured with a sextant.

§ 472. The *apparent* is obtained from the observed distance, by applying, with proper signs, the corrections for the error of the sextant, for the semidiameters of the two bodies, and for the augmentation of the moon's semidiameter.

§ *a.* The sun and moon's semidiameter is given in the ephemeris; the sun's for every 24*h*, and the moon's for every noon and midnight.

§ *b.* The correction for augmentation is found in Table X.

§ 473. *Augmentation* of the moon's semidiameter, is the difference between the visual angle of the moon's semidiameter at the centre, and its visual angle at the circumference, of the earth.

§ 474. The difference between these two angles, is proportional to the ratio between the length of the semidiameter of the earth, and its distance from the moon.

§ 475. On account of its great distance from the earth, the sun's semidiameter has no augmentation.

§ *a.* As the earth's semidiameter measures more in proportion to

the moon's geocentric distance, than to that distance of the sun, or of any other heavenly body, the difference of the moon's semidiameter, when seen from the circumference and from the centre of the earth, is greater than that of any other body, when seen from the same positions.

§ 476. The semidiameter of the moon when it is in the horizon, appears under nearly the same visual angle (barring refraction) that it does from the centre of the earth.

§ 477. The moon appears larger when it is in the horizon, than it does when in the zenith. This though is an optical delusion, for the moon actually subtends the largest visual angle when in the zenith; as it is then nearer to the observer than it is when in the horizon, by a little more than the semidiameter of the earth.

Plate 7. } § 478. $B' A B$ represents a diagram of the lunar problem.
 $b' b$ is the apparent, (§ 472.), and $B' B$ the true (§ 470.) lunar distance.

§ 479. The three apparent distances, ($b' b$, $b' A$, $A b$), are the given parts (§ 469. § α .) of the first triangle $b' A b$, and the angle $b' A b$ is the part required in it.

§ 480. The angle $b' A b$ is common to the second triangle $B' A B$, of which the true zenith distances $A B$, and $A B'$ are the given, and the true lunar distance $B' B$ is the required part.

§ 481. The apparent Z. D. of the sun, or of a star, (§ 284. § α .) being less, and the app. Z. D. of the moon (§ 286. § α .) being greater, than the true Z. D.; it appears from the diagram, that, when the moon's is the greater of the two Z. D., the true is always less than the apparent lunar distance.

§ α . And when the moon's is the less Z. D., the true is sometimes greater, and sometimes less, than the app. distance.

§ b . The true is the less, when the lunar distance exceeds 90° .

§ c . And it is generally the greater, when the distance is less than a quadrant, and the ratio of cos. moon's Z. D. to cos. sun or star's Z. D., is greater than the ratio of rad. to cos. of the lunar distance.

§ 482. The reason why the difference between the app. and the true L. dist., appears to be governed by the moon more than by the other body, is, that the moon being nearer to the earth, has the greater parallax, and is generally seen further from its true place in the heavens, than any other body, from which lunar distances are measured, appears from its true place.

§ 483. In N. lat., Aug. 27th, 1834.

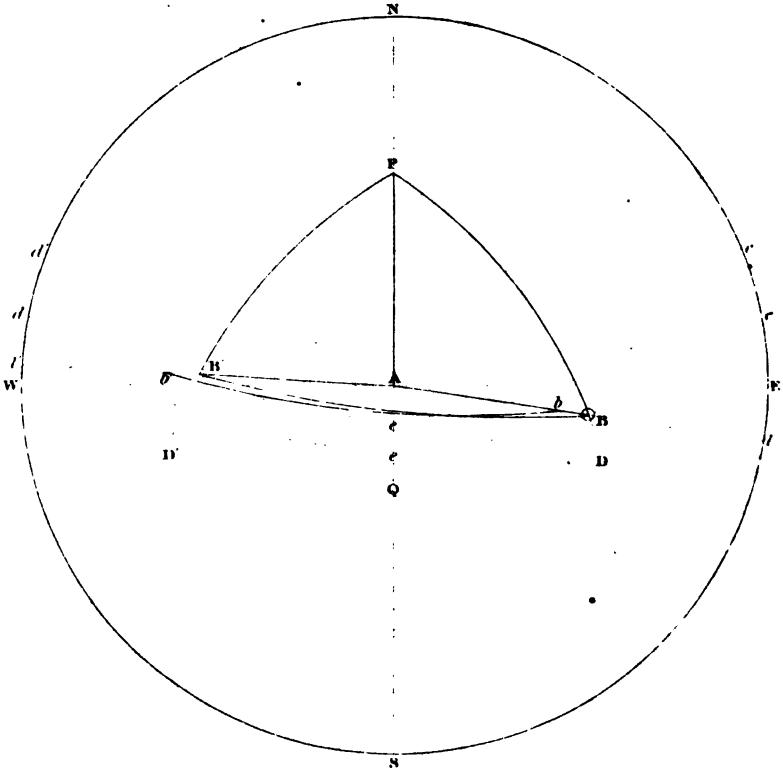
Obs. Dist. sun and moon = $89^\circ 51' 40''$

Obs. Alt. sun - = $34^\circ 4' 50''$

Obs. Alt. moon's upper limb = $54^\circ 27' 50''$

§ α . Obs. dist. sun & moon	=	$89^\circ 51' 40''$	
Sun's semidiameter	-	$15' 51''$	
Moon's " "	-	$15' 1''$	
Moon's augmentation	-	$13''$	(§ 472. § b .)
Error of sextant	-	$+ 6''$	

App. lunar dist. = $90^\circ 22' 51''$



§ <i>b</i> . Sun's obs. alt.	-	34° 4' 50"	
Sun's semidiameter	-	15' 51"	
*Dip (§ 275. § <i>a</i> .)	-	— 3' 21"	
<hr/>			
Sun's app. alt.	-	34° 17' 20"	
§ <i>c</i> . Refraction for sun's alt.	—	1' 20"	(Table IX.)
Sun's plx. in alt.		8"	(Table XI.)
<hr/>			
Sun's true alt.	-	34° 16' 8"	
<hr/>			
§ <i>d</i> . Obs. alt. moon's U. L.	54° 27' 50"		
Moon's semidiameter	-	—15' 1"	
Moon's augmentation	-	—13"	(Table X.)
Dip (§ 275. § <i>a</i> .)	-	— 3' 21"	
<hr/>			
§ <i>e</i> . Moon's app. alt.	54° 9' 15"	cos. = 9.767605	(§ 288.)
Moon's hor. plx. (§ 287.)	55' 7"	sin. = 8.204991	
<hr/>			
Moon's plx. in alt. (§ 287. § <i>c</i> .)	=	32' 16"	sin. = 7.972596
<hr/>			
§ <i>f</i> . Refraction for moon's alt.	=	—43"	
<hr/>			
Correction for moon's app. alt.	=	31' 33"†	
<hr/>			
§ <i>g</i> . To find the value of <i>b' A b</i> (§ 201. § <i>f</i> .) in the first } Plate 7. triangle.			
<i>b' b</i> (app. lunar dist.)	=	90° 22' 51"	
<i>b' A</i> (moon's app. Z. D.)	=	35° 50' 45"	co-sec. = 0.232394
<i>A b</i> (sun's app. Z. D.)	=	55° 42' 40"	co-sec. = 0.082911
<hr/>			
	2)	181° 56' 16"	
<hr/>			
$\frac{1}{2}$ sum	-	90° 58' 8"	sin. = 9.999938
($\frac{1}{4}$ S. ∞ app. lunar dist.)	=	0° 35' 17"	sin. = 8.011288
<hr/>			
	2)	18.326531	
<hr/>			
Cos. 81° 37' 34"	(=	$\frac{b' A b}{2}$)	9.163265
<hr/>			
<i>b' A b</i>	=	163° 15' 8"	
<hr/>			

* The *dip*, when the eye is 9 feet above the water, is about 3'; and 4', when the height of the eye is 17 feet. On board ship 4' is generally allowed for *dip*.

† When the nicest accuracy is required, corrections may be applied for the difference in the effects of refraction on the upper and the lower limb of the sun and moon; for the moon's parallax in different latitudes, supposing the equatorial to be greater than the polar diameter; and also a correction for the actual barometrical, and thermometrical state of the atmosphere; but at sea, greater errors are unavoidable, hence these corrections are of minor importance.

$$\begin{array}{r}
 \S h. \text{ To find } B' B (\S 200. \S v.) \text{ the tr. lunar dist. } (\S 480.) \\
 b' A b = 163^\circ 15' 8'' \quad \cos. = 9.981176 \\
 A B (\text{Sun's tr. Z. D.}) = 55^\circ 43' 52'' \quad \text{tang.} = 0.166625 \\
 \hline
 \text{Tang. auxl. } a = 0.147801 = 125^\circ 26' \\
 \hline
 \text{Moon's tr. Z. D.} = 35^\circ 19' 12'' \\
 \hline
 90^\circ 6' 48'' \\
 \hline
 A B (\text{Sun's tr. Z. D.}) = 55^\circ 43' 52'' \quad \cos. = 9.750567 \\
 \text{Auxl. } a = 125^\circ 26' \quad \text{sec.} = 0.236755 \\
 (\text{Moon's tr. Z. D.}) = 90^\circ 6' 48'' \quad \cos. = 7.296235 \\
 \hline
 \text{Tr. lunar dist.} = 89^\circ 53' 24'' \quad \text{Cos. } B' B = 7.283557 \\
 \hline
 \end{array}$$

§ 484. By referring to the Nautical Almanac, page xvli., of the ephemeris for Aug. 1834, it will be observed, that it was near noon of the 27th at the Greenwich observatory, when the moon was $89^\circ 53' 24''$ from the sun.

§ a. If the latitude of the place at which the observation (§ 483.) was made, be known, the time of day at that place, and when the observation was taken, may be found according to the rule § 387.

§ b. And the difference (§ 391. § a.) between the time of day thus found, and the time in the ephemeris, which corresponds to the calculated lunar distance, is the longitude in time.

§ 485. Distances for determining longitude are always measured from the moon, because the change of the moon's position in the heavens is more obvious than that of any other heavenly body that is visible to the naked eye.

§ 486. The moon (§ 360.) has a daily motion of about $13^\circ 10'$ in the heavens; owing to which the moon rises, culminates, and sets, later and later every day, until, having passed through all its phases, it crosses the circle of the sun's altitude, gets to the eastward of the sun, and presents the appearance of a new moon.

§ 487. At a mean, an error of $2' 12''$ in the lunar distance, will produce an error of 1° in the longitude.

§ 488. The moon changes its distance from those bodies, which lie directly in its path, more rapidly than it does from those towards or from which it moves more obliquely.

§ a. Therefore the stars from which the change of the lunar distance for the time being is the most obvious, should be preferred in taking lunar observations; for the more rapidly the distance changes, the less will the longitude be affected by a small error in the observation.

§ 489. In the Nautical Almanac; pages xliii. to xviii., of the ephemeris for each month, contain at intervals of three hours, the distance of the moon from the sun, from four of the planets, and eight of the principal fixed stars.

§ a. The small column, marked P. L. contains the proportional

correct itself by its own counteracting effects in distances measured to the east and west of the moon.

§ 492. Latitude by "double altitudes" may also be determined by means of the data in the lunar problem.

Plate 7. { 493. By inspecting the lunar diagram, it is seen that the arcs (P B, P B') of the circles of declination of the sun and moon, join the extremities of the true lunar distance (B' B), forming thereby the triangle B' P B, of which the three sides are known.

§ a. Then the value of the angles P B B', and A B B' being found, their difference gives the value of A B P, which, with B A, and B P in the triangle P A B, constitutes data requisite for determining A P, the co-latitude.

§ 494. The lunar problem is one of the most useful and most beautiful problems in navigation; for besides his longitude and latitude, the navigator may deduce, from the principles involved in it, data for the solution of almost any problem in nautical astronomy.

§ 495. The three parts A P, P A B, A P B, in the fourth triangle, are determinable from the data obtained by a lunar observation.

§ a. A P is the co-lat. of the place of observation.

§ b. A P B is the horary angle, which (§ 382. § a.) shows the app. time of day at the place of observation when the latter was made. And,

§ c. The difference between this time converted into *mean* time, and the Greenwich time in the N. A. that corresponds to the lunar dist., expresses, in time, the longitude of the place of observation.

§ d. P A B is the sun's true azimuth at the time and place of observation; the difference between it, and the sun's magnetic azimuth, (§ 308. § a.) is the variation of the compass.

§ 496. By increasing the triangulation, and extending the operations, other *quæsitæ* may be added to the problem; and the length of the day and night; the time of the sun and moon's rising and setting; the hour of the moon's passing the meridian; the hour when each object bears east or west; the duration of twilight; and the amplitudes of the two objects on the day, and at the place of observation, may all be determined by means of the parts involved in the common lunar problem.

§ 497. Therefore when, on account of unknown drifts, and of gales during several days in succession of thick or cloudy weather, a ship has lost her reckoning, it may be successfully restored by a single lunar observation.

§ a. If the variation of the compass be required also at the same time in addition to the lat., time of day, and longitude, the calculation, after being conducted into the fourth triangle B A P, should be conducted by a process different from that for evolving the value of A P, the co-lat., alone.

§ b. In the latter case, the value of A P would be determined by the rule § s. and § t., under Case IV. (§ 200.)

§ c. And in the former case, the proportion between the sines of opposite sides and angles, would evolve it; for, when the three un-

Plate 7. $\left\{ \begin{array}{l} \text{known parts of this triangle (B A P) are required, the} \\ \text{most direct method of arriving at the required results,} \end{array} \right.$ consists in applying the rules § z. and § z a., Case IV., (§ 200.) to calculation, in order to determine first the value of the horary and azimuth angles (A P B, & P A B.)

§ d. In trigonometrical operations, that method of calculation should ever be adopted, which, being less elaborate, arrives more directly at the required result.

§ 498. When the latitude, etc., is required by means of a lunar observation, the operation of correcting altitudes and of finding the true lunar distance, is conducted as it is under § 483. ; and then the value of A B B' is found, before the operation passes from the second triangle B' A B.

§ a. The true lunar distance B' B being determined, the Greenwich time corresponding thereto, is found (§ 489. § d.) in the lunar tables of the Ephemeris; and then the declination and the right ascension of the sun and moon, at this time, are found in the appropriate tables of the Nautical Almanac.

§ 499. The declination of the two bodies thus found, gives (§ 258. § b.) the sides B' P and B P.

§ a. And the difference of their right ascensions (§ 433.), expresses in time the value of the angle B' P B.

§ b. The angle P B B' is the only part in this triangle, which is required, and it may be found without the trouble of taking from the Ephemeris, the right ascension of the two bodies.

§ 500. The true lunar distance (§ 483.) $89^{\circ} 53' 24''$ of the problem occurred (§ 484.) at Greenwich, August 27, 1834, near mean noon, when the sun's declination (page ii. of the Monthly Ephemeris) was $10^{\circ} 10' 2''$ N.; and the moon's (page v. to xii. do.) was $19^{\circ} 12' 39''$ N. Their difference in right ascension then was $6h 13m 52s$.

§ a. And the sun's magnetic azimuth (§ 304. § a.) at the time of observation, was N. $109^{\circ} 4' 30''$ East.

§ 501. The apparent and true zenith distances are found, and the calculation for determining the true lunar distance (B' B) is conducted precisely in the same manner, as it is (§ 483.) when the true distance is the only object of the problem.

§ 502. In the second triangle B' A B, to find the value of A B B'.

B' B (Tr. lunar D.)	= $89^{\circ} 53' 24''$ cosec. = 0.000001
B' A B	= $163^{\circ} 15' 8''$ sin. = 9.459632
B' A (Moon's Z. D.)	= $35^{\circ} 19' 12''$ sin. = 9.762035

Sin. A B B' = 9.221668 = $9^{\circ} 35' 24''$

Plate 7. $\left\{ \begin{array}{l} \S a. \text{ In the third triangle } B' P B, \text{ to find the value of} \\ P B B'. \end{array} \right.$
 $B' B$ (Tr. L. D.) = $89^{\circ} 53' 24''$ cosec. = 0.000001
 $B' P B$ (Diff. R. A.) = $6h 13m 52s$ sin. = 9.999205
 $B' P$ (Moon's P.D.) = $70^{\circ} 47' 21''$ sin. = 9.975116

$$\text{Sin. } P B B' = 9.974322 = 70^{\circ} 29' 27''$$

$$A B B' = 9^{\circ} 35' 24''^{\wedge}$$

$$A B P = 60^{\circ} 54' 3''$$

$\S b.$ To find, in the fourth triangle, the sun's azimuth $P A B$, and the horary angle $A P B$ ($\S 200.$ $\S z b.$)

$$\frac{AB+BP}{2} = 67^{\circ} 46' 55'' \quad \text{sec.} = 0.422357 \quad \text{cosec.} = 0.033505$$

$$\frac{AB \oslash BP}{2} = 12^{\circ} 3' 3'' \quad \text{cos.} = 9.990322 \quad \text{sin.} = 9.319687$$

$$\frac{ABP}{2} = 30^{\circ} 27' 1'' \quad \text{cot.} = 0.230713 \quad \text{cot.} = 0.230713$$

$$\text{Tang. } \frac{PAB+APB}{2} = 77^{\circ} 11' 38'' = 0.643392$$

$$\text{Tang. } \frac{PAB \oslash APB}{2} = 20^{\circ} 59' 17'' \quad - \quad - \quad - \quad = 9.583905$$

$$A P B \text{ (H. Ang.)} = 56^{\circ} 12' 21'' \text{ (}\S 77. \S h.)$$

$$P A B \text{ (Azm.)} = N. 98^{\circ} 10' 55'' \text{ E.}$$

$\S c.$ APB (H. Ang.) = $56^{\circ} 12' 21'' = 3h 44m 49s = (\S 348. \S g.)$
 $8h 15m 11s$ A.M.

$1m 25s$ = Equation of time, (Naut. Al., p. ii. Mon. Eph.)

$8h 16m 36s$ A.M. = Mean time of day at the place of observation.

$\S d.$ To find $A P$, the co-lat.

$$A P B \text{ (Hry. Ang.)} = 56^{\circ} 12' 21'' \quad \text{cosec.} = 0.080377$$

$$A B \text{ (Sun's Z. D.)} = 55^{\circ} 43' 52'' \quad \text{sin.} = 9.917192$$

$$A B P = 60^{\circ} 54' 3'' \quad \text{sin.} = 9.941402$$

$$\text{Cos. } 29^{\circ} 40' 8'' \text{ N. Lat.} = \text{Sin. } A P \text{ (co-lat.)} = 9.938971$$

$\S e.$ Sun's Mag. Azm. ($\S 500. \S a.$) N. $109^{\circ} 4' 30''$ E.

Sun's Azm. ($\S b.$) N. $98^{\circ} 10' 55''$ E.

$$\text{Variation (}\S 312.) = 10^{\circ} 53' 35'' \text{ Westerly.}$$

§f. Time at Greenwich (§ 484.)
 when the obs. was made, 12h 00m 17s P.M. } Plate 7.
 Time (§ c.) at the place of observation, 8h 16m 36s A.M.

Long. of the obsr. (§ 391. § b.) W. 3h 43m 41s = 55° 55' 15''

§ 503. If the latitude and time of day, without the variation, be required from a lunar observation, the process of calculation may be varied from that above for finding the azimuth, time, and latitude; and may be made more direct.

§ a. But in either case, the order and method of calculation are the same, in the process of arriving at the value of A B P in the fourth triangle.

§ 504. The true lunar distance (B' B) must always be determined, before the correct P. distances, (P B, P B') and the difference (B' P B) in right ascension (§ 498. § a.) of the two bodies, can be known.

§ a. These parts must always be taken from the Ephemeris, and for the time in it, which corresponds to the true lunar distance.

§ 505. Having found, in the second triangle, the required angle A B B'; then having taken (§ 498. § a.) from the Ephemeris, the proper P. D., etc., and calculated (§ 502. § a.) the value of the angle (P B B') required in the third triangle; the value of A B P is obtained, and the lat. and time of day may thence be deduced by the following formula.

§ 506. Formula of calculation for finding the latitude and time of day by a lunar observation.

To find the lat. (§ 200. § n.)

	Contd. Angle (A B P) cos. = *.*****	
Sun's Z. D. (A B) cos. = *.*****		tang. = *.*****
 		<hr/>
Auxl. a sec. = *.*****		Tang. auxl. a = *.*****
(a ∝ Sun's P. D.) cos. = *.*****		<hr/>
Cos. co-lat. (A P) = *.*****		

To find the time of day, (§ 144.)

Co-lat. (A P)	co-sec. = *.*****	
Contd. Angle (A B P)	sin. = *.*****	
Sun's Z. D. (A B)	sin. = *.*****	
 		<hr/>
Sin. Horary Angle (A P B)	= *.*****	

§ 507. If the second and third triangles fall on opposite sides of the lunar distance B' B, then the sum of the angles (A B B' & P B B') of the second and third triangles, gives the value of the required angle (P B A) of the fourth triangle. } Plate 8.

§ 508. When the polar distance of each body is greater than the co-latitude of the observer, then the second and third triangles fall upon the same side of the lunar distance B' B, } Plate 7.

Plate 7. } and the difference between the angles (A B B', P B B') is
 } the value of the angle (A B P) sought in the fourth triangle.

§ 509. It may always be known, whether the sum or difference of the angles of the second and third triangle, will give the angle required to be known in the fourth triangle, by observing the inclination of the plane in which the sextant is held to bring the sun and moon in contact.

§ a. If the sextant be inclined to the plane of the horizon, towards the pole of the observer, then his co-lat. is greater than the P. dist. of either body, and the second and third triangles fall upon different sides of the lunar distance, and the sum of the two angles is the required angle of the fourth triangle.

§ 510. May 16, (P. M.), 1834.

Obs. dist. sun & moon 97° 16' 28''

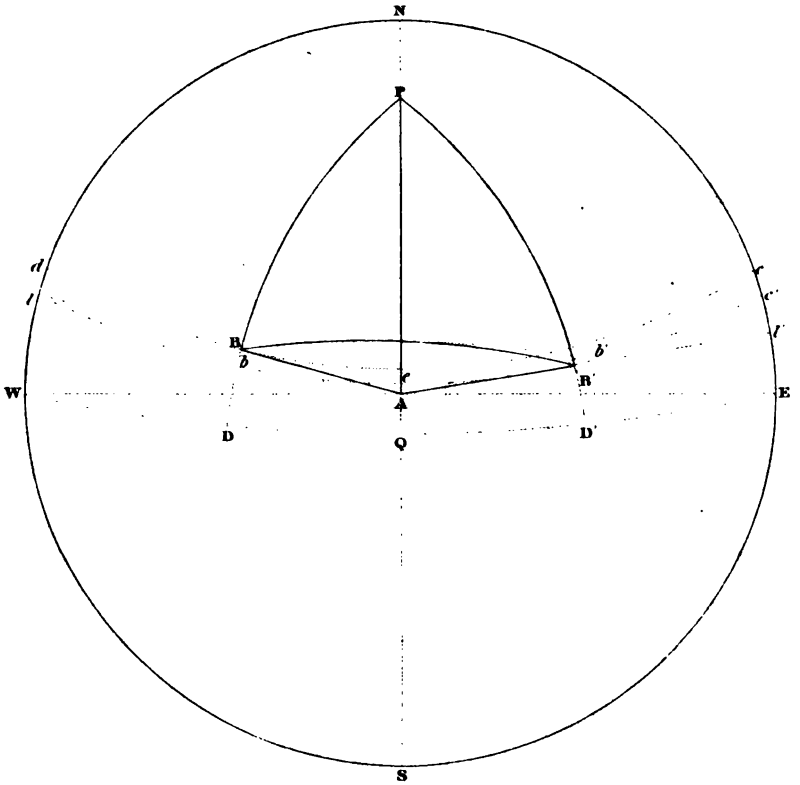
Obs. alt. sun's L. L. = 41° 3' 59''

Obs. alt. moon's U. L. = 37° 58' 24''

Required the latitude and longitude of the place of observation ?

§ a. To apply the preliminary corrections.

1st. Obs. lunar dist.	97° 16' 28''	
Sun's semidiam.	- 15' 50''	(N. A., p. ii., M. E.)
Moon's " "	- 16' 6''	(" iii. ")
Moon's augmentation	- 10''	
App. lunar dist.	= 97° 48' 34''	
2d. Obs. alt. sun's L. L.	41° 3' 59''	
Sun's semidiameter	- 15' 50''	
Sun's app. alt.	41° 19' 49''	App. Z. D. 48° 40' 11''
3d. Sun's refraction	- 1' 11''	
Sun's plx. in alt.	- 7''	
Sun's true alt.	41° 18' 45''	Z. D. 48° 41' 15''
4th. Obs. alt. moon's U. L.	37° 58' 24''	
Moon's semidiameter	- 16' 6''	
Moon's augmentation	- 10''	
Moon's app. alt.	37° 42' 8''	cos. = 9.898286
Moon's hor. plx.	-	59' 4'' sin. = 8.235047
Moon's plx. in alt.	46' 44''	Sine = 8.133333
Moon's refraction	- 1' 14''	
Moon's true alt.	38° 27' 38''	Z. D. 51° 32' 22''



§ *b*. To find the tr. lunar dist.

1st. To find *b A b'* in the first triangle, (§ 201. § *f*.) } Plate 8.
b b' (Ap. lunar dist.) = 97° 48' 34"
A b (sun's ap. Z. D.) = 48° 40' 11" co-sec. = 0.124410
A b' (moon's ap. Z. D.) = 52° 17' 52" co-sec. = 0.101714

2) 198° 46' 37"

$\frac{1}{2}$ sum = 99° 23' 18" sin. = 9.994144
 $(\frac{1}{2} S. \omega b b')$ = 1° 34' 44" sin. = 8.440173

2) 18.660441

Cos. $\frac{b A b'}{2}$ = 77° 38' 55" = 9.330220

2

2d. To find *B B'* }
 (§ 200. § *u*.) } *b A b'* = 155° 17' 50" cos. = 9.958319
A B = 48° 41' 15" cos. = 9.819653 - - - tang. = 0.056056

Auxl. *a* - sec. = 0.157822 Tang. *a* 134° 3' 7" = 0.014375

51° 32' 22" (M.'s Z. D.)

(*a* ∞ M.'s Z. D.) cos. = 9.114977 - 82° 30' 45" (*A B' a*)

Cos. *B B'* = 9.092452 = 97° 6' 25" (Tr. l'r dist.)

When this distance (97° 6' 25") occurred, it was 9 P. M. at Greenwich of the given day (N. A. p. xv., Monthly Ephemeris.)

§ *c*. To take (§ 498. § *a*.) the other requisite data from the ephemeris.

Moon's dec. 14° 59' 6" N. P. D. 75° 0' 54" (N. A., p. viii. M. E.)

Sun's dec. 19° 8' 28" N. P. D. 70° 51' 32" (" ii. ")

Moon's Rt. A. 10h 25m 15s - (" viii. ")

Sun's " 3h 52m 25s - (" ii. ")

Polar angle = 6h 52m 50s = *B P B'*.

§ *d*. To find the required angle *B' B A* of the second triangle.

B B' (lunar dist.) = 97° 6' 25" cosec. = 0.003350

B A B' - 155° 17' 50" sine = 9.621084

A B' (moon's Z. D.) = 51° 32' 22" sine = 9.893782

Sin. *B' B A* = 9.518216 = 19° 15' 18"

Plata 8. } § e. To find the required angle B' B P of the third
 } triangle
 B B' (lunar dist.) = 97° 6' 25" co-sec. = 0.003350
 B' P B (pl'r. angl.) = 6h 52m 50" sin. = 9.988356
 P B' (moon's P. D.) = 75° 0' 54" sin. = 9.984975

§ f. 4th triangle B A P; } Sin. B' B P = 71° 23' 30" = 9.976681
 to find the co-lat. } B' B A = 19° 15' 18" (§ 506.)

P B A = 90° 38' 48" cos. = 8.052549
 A B = 48° 41' 15" cos. = 9.819653 - tang. = 0.056056

Auxl. a - sec. = 0.000036 Tang. a 179° 15' 51" = 8.108605
 70° 51' 32" (S.'s P. D.)

(a ∞ sun's P. D.) cos. = 9.499325 108° 24' 19" (A B ∞ a)

Cos. A P, or sin. lat. = 9.319014 = 12° 1' 55" N. sec. = 0.009647

To find the Hr. } P B A = 90° 38' 49" sin. = 9.999973
 angle A P B. } A B (sun's Z. D.) = 48° 41' 15" sin. = 9.875710

Sin. A P B 3h 20m 41s = 9.885330

Equation = 3m 56s

Mean time = 3h 16m 45s P. M.

Gr. time (§ b.) = 9h P. M.

W. Long. (§ 391. § b.) 5h 43m 15s = 85° 48' 45"

§ 511. Examples under § 483. and § 510. are drawn out in the solution, in order to familiarize the problem to the student. But such a process of calculation as is there shown, is not desirable in practice; especially that part of it which has been made to come under Case IV., (§ 200. § n.) on account of the perplexity in determining whether the value of the auxl. *a* be greater or less than 90°.

§ a. Therefore, in practice, those methods of calculation are generally preferred, which give the trigonometric function of *half* the value of the required part; such as § a. (§ 386.), for *half* the value of a required arc or angle should never exceed 90°.

§ 512. The learner has now become familiar with the triangulation, which is brought under calculation in the process of finding longitude, etc., from a lunar observation; he will therefore readily comprehend the manner by which such an operation is simplified, and reduced to the following methods and formulæ for practice.

§ 513. The process of correcting the obs. distance and altitudes is fully shown under § 483. and § 510. This part of the operation

is the same in every method for calculating the true from an obs. lunar distance.

§ 514. An improved method for finding the true from an observed lunar dist.*

§ a. Aug. 27th, 1834.

App. dist. sun & moon = $88^{\circ} 26' 52''$

Sun's app. alt. - $47^{\circ} 52' 12''$
 Sun's refraction - $53''$
 Sun's pl'x. in alt. $7''$

Sun's tr. alt. - $47^{\circ} 51' 26''$

Moon's app. alt. - $40^{\circ} 52' 58''$ cos. = 9.878550
 Moon's hor. pl'x. - $55' 0''$ sin. = 8.204070

Moon's pl'x. in alt. - $41' 35''$ sine = 8.082620

Moon's refraction - $1' 7''$

Moon's true alt. = $41^{\circ} 33' 26''$

§ b. App. lunar D. $88^{\circ} 26' 52''$
 Sun's app. alt. - $47^{\circ} 52' 12''$ sec. = 0.178397
 Moon's " - $40^{\circ} 52' 58''$ sec. = 0.121449

$2) 177^{\circ} 12' 2''$

$\frac{1}{2}$ sum = $88^{\circ} 36' 1''$ cos. = 8.367876
 ($\frac{1}{2}$ S. ∞ app. lunar D.) = $0^{\circ} 9' 9''$ cos. = 9.999998

Sun's tr. alt. - $47^{\circ} 51' 26''$ cos. = 9.826710
 Moon's " - $41^{\circ} 33' 26''$ cos. = 9.874073

$2) 38.383503$

Sun's + Mon's alt. $2) 89^{\circ} 24' 52''$
 19.191751

$\frac{\text{Sun's} + \text{Moon's Alt.}}{2} = 44^{\circ} 42' 26''$ cos. = 9.851693†

Sin. auxl. $a = 9.340058 = 12^{\circ} 38' 20''$

Auxl. a cos. = 9.989847†

Sin. $\frac{\text{Tr. lunar dist.} - 9.841040}{2} = 43^{\circ} 54' 25''$

$\frac{2}{2}$

True lunar dist. = $87^{\circ} 48' 50''$

* Vide KELLY'S SPHERICS, p. 195.

§ c. (N. A., p. xvii., M. E.) 3h P. M.

Sun's lunar dist. $88^{\circ} 29' 8''$ P. L. = 3277

True lunar dist. = $87^{\circ} 48' 50''$

$40^{\circ} 18''$ P. L. = 6500 3h P. M.

3223 = 1h 25m 42s

Greenwich time = 4h 25m 42s P. M.

LATITUDE BY THE NORTH STAR.

§ 515. In northern latitudes, the latitude may be found at any time of the night, by an altitude of the north star.

§ 516. If the north star were situated in the pole of the world, its altitude would always show the elevation of the north pole; and (§ 251. § a.) consequently to the observer, his latitude.

§ 517. But as this star revolves in a very small circle around the pole, the elevation of the pole may always be determined by applying to the star's altitude at any time, the corrections opposite to that time in the subjoined tables (A & B).

§ 518. The corrections in Table A, and those after (*'s alt. +) in the hour columns of Table B, are *always* to be added to the star's alt. They are expressed in seconds (").

§ 519. And the other corrections in Table B, must be applied to the star's altitude, according to the precept, which is at the head of the hour column in which the *sidereal* time is found.

§ 520. To find the lat. by an alt. of the north star; the altitude being corrected for dip, refraction, etc.

§ a Subtract 1' from the star's alt.

§ b. For the supposed time of night when the observation is made, take the corresponding sidereal time; the correction found in Table B and opposite to this time, being applied, according to the precept (§ 519.) at the head of its column, to the star's alt., gives the approximate latitude.

§ c. And the corrections under the hour in Table B, and opposite the hour, but under the "approximate latitude," in Table A, being added to the approximate latitude, give the lat. of the observer.

§ 521. May 4, 1834, long. 85° W. the altitude of the north star, at 7h P. M., was $35^{\circ} 29' 43''$. To find the lat.

§ a. Supposed time - - 7h 0m 0s P. M.

Longitude in time - - 5h 40m 0s

Time at Greenwich - - 12h 40m 0s (§ 396. § a.)

Sidereal time, May 4 - - 2h 47m 34s (N. A., p. ii., M. E.)

Supposed time - - 7h

Acceleration of S. T. for 12h 40m 2m 5s (§ 213. § b.)

Sidereal time of obs. - - = 9h 49m 39s

$\S b.$	Star's alt. $35^{\circ} 29' 43''$	
	1'	($\S 520. \S a.$)
	<u>$35^{\circ} 28' 43''$</u>	
Oppos. $9h 49m 39s$ (Table B) correction +	$1^{\circ} 3' 38''$	
	<u>Apprx. lat. $36^{\circ} 32' 21''$</u>	
Under $9h$, *'s alt. + (Table B)	-	66''
Oppos. $9h 49m 39s$ and under 40° (Table A)	-	<u>32''</u>
	Latitude $36^{\circ} 33' 59''$ N.	

$\S 522.$ Jan. 14, 1834. Long. 45° East $9h$ P. M.; the altitude of the north star was $41^{\circ} 11'$. To find the lat.

$\S a.$ Supposed time	-	$9h$
Longitude in time	-	$3h$
	<u>Time at Greenwich</u>	$6h$ ($\S 396. \S b.$)
Sidereal time, Jan. 14	-	$19h 33m 53s$ (N. A., p. ii., M.E.)
Supposed time of obs.	-	$9h$
Acceleration of S. T. for $6h$	-	<u>$59s$</u> ($\S 213. \S b.$)
Sidereal time of obs.	-	$28h 34m 52s - 24h = 4h 34m 52s$
$\S b.$ Star's altitude	-	$41^{\circ} 11'$

		1'
	<u>$41^{\circ} 10'$</u>	
Opposit. $4h 34m 52s$ (Table B)	Cor.	<u>$-56' 15''$</u>
Apprx. lat.	-	$40^{\circ} 13' 45''$
Under $4h$, *'s alt. + (Table B)	Cor.	$56''$
Oppos. $4h 34m 52s$, and under 41° (Table A)	-	<u>$41''$</u>
	Latitude $40^{\circ} 15' 22''$ N.	

$\S 523.$ Aug. 8, 1834, longitude 150° East. The alt. of the north star at 4 A. M. was $49^{\circ} 33'$. To find the latitude.

$\S a.$ Supposed time $4h$ A. M.	-	$= 16h$
Longitude in time	-	$= 10h$
	<u>Time at Greenwich</u>	$= 6h$
Sidereal time, Aug. 8	-	$9h 6m 3s$
Supposed time of obs.	-	$16h$
Acceleration of S. time for $6h$	-	<u>$59s$</u>
Sidereal time of observation	-	<u>$25h 7m 2s = 1h 7m 2s.$</u>

§ b. Star's altitude	-	-	-	-	51° 34'
					1'
					51° 33'
Oppos. 1h 7m 2s (Table B)		Cor.			-1° 41' 54''
					50° 1' 6''
Approx. latitude					50° 1' 6''
Under 1h, *'s alt.+(Table B)		Cor.			58''
Oppos. 1h and under 50° (T. A)		"			0''
					Latitude 50° 2' 4''

§ 524. An error of several degrees in the longitude, and of several minutes in the time of taking the star's altitude, brings only a small error into the latitude, therefore the ship's time, and longitude by dead reckoning, may always be used for finding the latitude at sea by the polar star.

*Tables for finding the Latitude by the alt. of the North Star.**

TABLE A.

Sidereal Time.	APPROXIMATE LATITUDE.							Sidereal Time.
	15°	30°	40°	50°	60°	65°	70°	
h m	"	"	"	"	"	"	"	h m
0.	1	3	4	6	9	12	15	12
30	0	1	1	2	2	3	4	30
1.	0	0	0	0	0	0	0	13.
30	0	1	1	2	2	3	3	30
2.	1	3	4	6	9	11	14	14.
30	3	7	9	13	13	24	31	30
3.	5	11	16	23	34	42	53	15.
30	7	17	24	34	50	62	79	30
4.	10	22	32	46	67	83	106	16.
30	13	28	41	58	85	109	134	30
5.	15	34	49	70	101	128	160	17.
30	18	38	56	79	115	145	182	30
6.	19	42	61	87	126	159	199	18.
30	20	44	65	91	133	168	210	30
7.	21	45	64	93	135	170	214	19.
30	21	44	64	91	133	168	211	30
8.	20	42	60	87	127	159	200	20.
30	18	38	50	79	116	146	183	30
9.	15	44	43	70	102	129	161	21.
30	13	28	32	59	86	109	136	30
10.	10	23	29	47	69	84	109	22.
30	8	17	27	35	50	62	80	30
11.	5	11	17	23	34	42	54	23.
30	3	7	10	13	20	25	32	30
12.	1''	3''	4''	6''	9''	12''	15''	24.
Sidereal Time.	15°	30°	40°	50°	60°	65°	70°	Sidereal Time.

* Vide N. A. for 1834, p. 483.

TABLE B.

Sidereal Time.			Corrections.	Sidereal Time.			Corrections.
H	M	H		H	M	H	
1	0	12	1° 31' 19"	6	0	18	0° 24' 43"
	10		32 12		10		20 44
	20		33 1		20		16 41
	30		33 39		30		12 36
	40		34 7		40		8 31
	50		34 24		50		4 24
1	0	13	1° 34' 30"	7	0	19	0° 01' 6"
	10		34 25		10	7	3 51
	20		34 10		20		7 58
	30		33 44		30		12 4
	40		33 7		40		16 8
	50		32 19		50		20 11
2	0	14	1° 31' 21"	20	0	8	0° 24' 12"
	10		29 13		10		28 9
	20		29 54		20		32 4
	30		27 25		30		35 55
	40		25 46		40		39 41
	50		23 57		50		43 23
3	0	15	1° 21' 59"	21	0	9	0° 47' 1"
	10		19 51		10		50 33
	20		17 34		20		53 59
	30		15 8		30		57 19
	40		12 34		40	1°	0 32
	50		9 52		50		3 38
4	0	16	1° 7' 1"	22	0	10	1° 6' 38"
	10		4 3		10		9 29
	20		0 57		20		12 13
	30	0°	57 45		30		14 48
	40		54 26		40		17 15
	50		51 0		50		19 33
5	0	17	0° 47' 29"	23	0	11	1° 21' 42"
	10		43 53		10		23 42
	20		40 11		20		25 32
	30		36 25		30		27 12
	40		32 35		40		28 42
	50		28 41		50		30 3
6	0	18	1° 24' 43"	24	0	12	1° 31' 12"
H	M	H	Corrections.	H	M	H	Corrections.

TIDES.

§ 525. The flux and reflux of the waters, known under the name of **TIDES**, are caused by the attractive forces of the sun and moon exerted upon the ocean.

§ 526. The moon being nearer to the earth than the sun is, has a greater effect than the sun upon the tides.

§ a. The action of the moon upon the tides, is about three times greater than that of the sun.

§ 527. When the attractive forces of the sun and moon act in conjunction, they produce the highest tides.

§ a. When this is the case, the moon (§ 367.) is in syzygy.

§ b. And the tides caused about this time are called *spring* tides.

§ 528. The tides have the least rise and fall, when the attractive forces act perpendicularly to each other.

§ a. And this is the case, when the moon (§ 369. § b.) is in quadrature. Then the tides are called *neap* tides.

§ 529. That portion of the ocean which is immediately under, and nearest to, the sun or moon, is more attracted by either than the centre of the earth is. This portion then, has a tendency to approach the attracting body, and rises up, until its tendency is counteracted by the attraction of gravitation towards the centre of the earth.

§ a. About twelve hours afterwards, this portion of the ocean, owing to the earth's diurnal motion (§ 206. § a.), is at the furthest point from the sun or moon; and the waters about it, owing to their tendency to restore the equilibrium, which is disturbed by the effects of the attraction of the sun or moon on the opposite side of the earth, rise up and make high tide again.

§ b. Hence, during the time in which the moon is performing one revolution around the earth (§ 362. § d.), the tide rises twice, and falls twice, at the same place.

§ 530. The attractive forces of the sun and moon upon equal portions of the surface of the sea, being (§ 526. § a.) about 3 to 1 in favour of the latter; if the solar tide at any place be 2 feet and the lunar 6, and the moon be in syzygy, the two tides will happen at the same time, and (§ 527. § b.) make a spring tide of 8 feet.

§ a. Then, as the lunar (§ 360. § a.) is longer than a solar day, the following solar will happen earlier than the succeeding lunar tide, by the difference between half a solar and half a lunar day.

§ b. Thus, the lunar tide continues to retard upon the solar tide, until the moon quadrates; when the high lunar and low solar tides coincide in time, and (§ 528. § a.) we have a neap tide of four feet rise.

§ c. After this, the lunar still continues to retard upon the solar tide, until the moon arrives in the other syzygy; when the two high tides again happen at the same time, and bring about other spring tides.

§ *d.* At this second spring tide, the moon has completed half of a revolution in its orbit, and has lost one tide upon the sun; therefore, while the moon is completing one entire revolution through its phases, there are two more solar, than lunar, tides.

§ 531. The attraction of the moon being more partial, and its effect upon small portions of the earth's surface being more obvious than that of the sun, the combined tides are governed more by the moon than by the sun.

§ 532. The effects of the moon's attraction upon the earth, tend (§ 529.) to create high tide, both in that part of the ocean immediately under, and nearest to, the moon, and in that part diametrically opposite; and were not the motion of the waters resisted and obstructed, there would be high tide at the moment when the moon crosses either the superior or the inferior meridian.

§ *a.* But, at some places, the passage of the moon across the meridian, precedes, by several hours, the time of high water.

§ *b.* This retardation of the tides might be explained, by attributing the retarding power to the effects of the resistance, which the shores, unequal depths of ocean, etc., offer to the mass of moving waters, were it not, that the waters do not rise up into spring tides, when the moon is in syzygy, and when the attractive forces of the sun and moon are combined in their action upon the waters; but the highest tides in every synodical month (§ 362. § *c.*), is generally about the third tide after the passage of the moon through either syzygy.

§ *c.* And the least neap tide, is generally the third tide after the moon quadrates.

§ 533. Observations show, that the tides require a little longer time to ebb, than they do to flow.

§ *a.* This difference observable at sea, becomes more obvious in rivers of strong currents.

§ 534. Upon the smaller seas, and sheets of water, such as the Lakes, the Mediterranean, etc., the effect of the lunar and solar attractions, are partially counteracted by the circumscribed limits to their action; and hence but little, or no tide is produced there.

§ 335. There are a variety of causes, (and some of a local nature), which, acting together, tend, some to retard at one place, and others to hasten at another place, the hour of high tide on the full and change days of the moon; so that, there are no general rules for determining beyond certain limits of approximation, the time of high or low water at any place.

§ 536. The greatest interval between two consecutive tides, generally happens about a day and a half after the moon has quadrated; when the tides, (§ 532. § *c.*) being at the minimum of their rise and fall, are the weakest.

§ *a.* And the least retardation of one tide after another, is the 2d upon the 3d, or the 3d upon the 4th tide, after the moon's latest passage through a syzygy; the tides, having then (§ 532. § *b.*) the greatest rise and fall, are strongest.

§ 537. On an average, the tides rise and fall once, in about 12 $\frac{1}{2}$ 48m.

· § a. Consequently every tide retards, at a mean, about 24m, upon the one which it succeeds; and each tide happens about 48m later than it did the day before.

§ 538. Were there not so wide a difference in the tides, between the minimum and maximum of their retardation, the hour of high or low water, at any place and on any day, might be found by adding to the time of high water on full or change days, the product of 48m, and the number of days from the latest full or new moon, to the day proposed.

§ a. About the time of neap tides, there is sometimes a difference of more than an hour and three quarters in the time of high water, on two successive days.

§ b. And a similar difference about the time of spring tides, is frequently less than half an hour.

§ 539. The annexed table (C) shows the retardation of the *mean* tides, upon the hour of high tide on full and change days, for every day between the full and change of the moon.

§ a. Therefore, to find the time of mean high water on any day, we have only to look in the Nautical Almanac (page xii. M. Ephemeris), for the day of the latest new, or full moon, in order to find its age (in days) since the last change in syzygy; the time, in the annexed table (C), found opposite to this age, and added to the time of high water at the place proposed, on full and change days, gives the time of mean high tide for the day when it is so required.

§ b. The hour of high tide at any port, on full and change days, is called the *establishment* of the port.^a

§ c. And the *establishment of the port* for any one place is always the same; for on every full and change day throughout the year, high tides are considered to take place there at the same hour of the day.

§ 540. A table for finding the time of high or low water, at any place, the establishment of the port (§ 539. § b.) being known.

TABLE C.

From \bullet to \circ		Days.	From \circ to \bullet	
Corrections.			Corrections.	
H	M		H	M
	21	$\frac{1}{2}$		20
	41	1		41
1	0	$1\frac{1}{2}$	1	5
1	19	2	1	28
1	38	$2\frac{1}{2}$	1	47
1	58	3	2	6
2	18	$3\frac{1}{2}$	2	26
2	38	4	2	46
2	58	$4\frac{1}{2}$	3	5
3	19	5	3	24
3	40	$5\frac{1}{2}$	3	45
4	3	6	4	6
4	26	$6\frac{1}{2}$	4	28
4	51	7	4	50
5	15	$7\frac{1}{2}$	5	15
5	41	8	5	44
6	14	$8\frac{1}{2}$	6	14
6	53	9	6	48
7	30	$9\frac{1}{2}$	7	28
8	5	10	8	10
8	38	$10\frac{1}{2}$	8	47
9	7	11	9	20
9	29	$11\frac{1}{2}$	9	48
9	51	12	10	14
10	18	$12\frac{1}{2}$	10	35
10	48	13	10	35
11	10	$13\frac{1}{2}$	11	16
11	30	14	11	38
11	51	$14\frac{1}{2}$	11	59
12	12	15	12	20

§ a. To find the time of high water at Charleston, Aug. 29, 1834. The establishment of the port being 7h 5m.

§ b. The last change in syzygy (§ 367.) was full moon, Aug. 18th, 20h (N. A., p. 12, M. E.); consequently the moon's age is 10 days.

§ c. Opposite to 10d, and in the column, from \circ to \bullet , is 8h 10m, which, added to the establishment of the port, gives 15h 25m, the hour of high water on the day proposed.

§ d. To find the time of high water at Portland, Feb. 14, 1834; the establishment of the port being 10h 45m

§ e. The last change in syzygy was new moon February 3; consequently the age of the moon is six days.

§ f. Opposite to 6d, and in the column, from \bullet to \circ , is 4h 3m, which, added to 10h 45m, gives 14h 48m, the time of high water.

§ 541. This method does not show the precise hour of high water; but it approximates the true time of high water, within limits which will serve on all ordinary occasions.

§ a. The time of low water may be found by adding 6h 15m to the time of high water on the day proposed.

* The arguments \bullet to \circ , mean from *New* to *Full* moon; and \circ to \bullet , from *Full* to *New* moon.

NAVIGATION.

NAVIGATION.

§ 542. The geographical situation of places, is designated by their distances, north or south, from the equator; and by their distance, east or west, from a prime meridian (§ 252. § c.).

§ a. These distances (§ 248. § b. & § 252.) are known by the name of Latitude and Longitude of the places.

§ 543. It has been shown in Nautical Astronomy, how the latitude and longitude of places may be determined by means of observations made upon the sun, moon, or stars; but in practice these means are not always at hand.

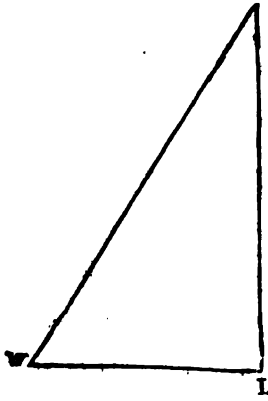
§ a. It remains then to be shown, how the geographical position of places may be determined, by knowing in certain respects, their relative situation with regard to each other.

§ 544. Washington city is to the southward and westward of Baltimore. The difference of latitude between them (§ 254. § c.) is the meridional arc, which is contained between Baltimore and the parallel of the latitude of Washington.

§ a. And the arc of this parallel which is between Washington and the meridian of Baltimore, (§ 254. § b.), is the difference in longitude between the two places.

§ b. These two arcs are perpendicular to each other; for the meridian of Baltimore (§ 248. § a.) cuts the equator at right angles, and the parallel of Washington (§ 249.) is parallel to the equator.

§ c. Now, if a line (W B) be drawn direct from Washington to Baltimore, it will connect their difference of longitude (W L) and of latitude (B L), and form a right angled triangle (W L B), of which the hypotenuse (W B) is the distance, and the legs, the difference of latitude and of longitude, between Washington and Baltimore.



§ d. The two acute angles (W & B) show the bearings of each place from the other. The angle W is the course from Washington to Baltimore, and the angle B is the course from Baltimore to Washington.

§ e. Hence if, of the Dist., Diff. Lat., Diff. Long., and Course, between two places, any two be given, the others are determinable.

§ 545. Now, the section of a loxodromic curve, which a ship traces while she is sailing upon a given course, is the hypotenuse of a right angled triangle, and corresponds to *W B*.

§ *a*. Then if the course and distance, which a ship sails in any given time, be known, we have the hypotenuse and an acute angle of a right angled triangle, given; and the other parts are determinable.

§ *b*. Therefore, knowing the latitude and longitude of the place from which a ship takes her departure, and knowing the course and distance which she sails from that place, in a specified time, we may determine by right angled trigonometrical calculations, the latitude and longitude of the ship, at the end of that time.

§ 546. The sides of all such triangles are curved lines; for the earth (§ 204.) is a spheroid, therefore all triangles upon its surface are spherical triangles, and are properly subject to the rules of spherical trigonometry, for investigation.

§ *a*. But the laborious operations of obtaining results from these triangles, when brought under calculation, as spherical triangles, would be inconvenient in practice; and they are not necessary in the ordinary purposes of navigation.

§ *b*. Therefore all such triangles are considered in navigation as right angled plane triangles, and are brought under calculation according to the rules of plane trigonometry.

§ 547. A degree ($^{\circ}$) of all great circles, such as the equator, meridians of longitude, etc., whose radii and the earth's semidiameter are the same, consists of 60 *nautical miles*, or of about $69\frac{1}{2}$ statute miles; so that, calling the number of minutes ($'$), miles, which is contained in an arc of one of these great circles, we have the value of this arc considered as a straight line.

§ *a*. Wherefore, knowing the distance and the difference of latitude between any two places, the difference of longitude between them, may be determined also in *nautical miles*, by right angled, plane trigonometrical calculations founded upon § 75.

§ *b*. The difference of longitude thus found, is called departure.

§ 548. *Departure* is the difference in longitude between any two places, expressed in *miles*.

§ *a*. And the departure in any latitude, may be converted into its corresponding minutes ($'$) of longitude by means of the principles established under § 76.

§ 549. It is evident, that, if in mathematical calculations, curved lines be treated as right lines, there must be an error in the result; and this error increases with the number of degrees contained in such curved lines.

§ 550. The result then, obtained by calculating the sides of a spherical triangle, as though they were the straight lines of a plane triangle, is only an approximation; and the smaller the sides, the closer is the approximation.

§ *a*. This method therefore is particularly applicable in small distances, and short runs; it is used for working up "dead reckoning", and for calculating the distance, the difference of latitude and

of longitude, and the course, from one place to another; any two of which four quantities being known, (§ 544. § e.), the others are determinable.

§ 551. The diagram shows by a mere inspection, the } Plate 1.
solution of every problem which can occur in right angled }
plane trigonometry, provided the hypotenuse of the triangle involved, do not exceed 300 miles, or 300 units of any measure.

§ a. This diagram may answer the purpose of Tables IV. & V.; and it also shows the principles upon which they are constructed; for the number in the Dist. column of these tables, is the length of the hypotenuse of a right angled triangle, whose acute angles contain, one the number of degrees at the top, and the other those at the bottom of the page, and the value of whose legs is set down opposite to that of the hypotenuse, and in the columns marked Dep. and D. Lat.

§ 552. This diagram, then, shows the solution of every case, or problem in loxodromic sailing; for it shows the dimensions of the triangle involved in every problem, provided the distance or hypotenuse do not exceed 300 miles.

§ a. If it exceed 300 miles, the solution may be obtained by dividing the given side or sides, by 2 or 3, or by any other divisor, which will reduce the triangle of the problem within the limits of the diagram; then the value of the side or sides, obtained, by using said quotient in the diagram, being multiplied by the same divisor (§ 70.), gives the value of the required side or sides.

§ 553. The angle B A D is 45° .

§ a. The acute angles of a right angled triangle (§ 32. § d.) being complementary to each other, the less must always be located at A.

§ b. And the leg adjacent to it, must be called the *base*, and be a part of A D.

§ c. And the leg opposite to it, must be called the *perpendicular*.

§ d. All the straight lines standing upon A D, are alluded to as *perpendiculars*.

§ e. B C is the greatest *perpendicular* in the diagram. Equal portions of it are transferred by means of the parallels *b d*, to the graduated arc B D, for admeasurement.

§ f. The graduated arc B D is thus made to answer the purpose of a graduated *perpendicular*, for the arc contains the same divisions which the *perpendicular* B C would have shown, had it been graduated to the scale of A B and A D.

§ g. The height of every *perpendicular* is therefore shown on that portion of the graduated arc, which is between the *base* (§ b.) and that parallel, under which the *perpendicular* stands. Thus the height of the *perpendicular* *b C*, transferred by the parallel *b d*, to the graduated arc, is $D d = 11.3$.

§ 554. The arcs in the diagram show the angular value of any course, provided it be not more than 4 Points, or 45° .

§ a. If the course be greater than this, they show the angular value of its complement.

§ b. The arcs, 3, 4, 5, etc., also show the length of the *base* and

Plate 1. } hypotenuse of the triangle proposed; while the scale on
 the graduated arc (§ 553. § g.) shows the value of the *perpendicular* ($b c$) in the several triangles.

§ c. The section of any arc, which is contained between the *base*, and the lines $A e$, shows the angular value of the courses which are marked upon these lines; and the angular value of the complements (§ 553. § a.) of the courses, marked *under* these lines.

§ d. The marks on the arcs show the value of these arcs in degrees.

§ e. The even numbers (2° , 4° , 6° , etc.) of degrees are marked on the concave side of the arcs; and the odd numbers (1° , 3° , 5° , etc.) are marked on the convex side.

§ f. The degrees (46° , 47° , 48° , etc.) that stand on the outside of the graduated arc, are the complements of those (42° , 43° , 44° , etc.) on the inside of the arc.

§ g. The entire length of every arc (§ 553.) is 45° .

§ 555. The dotted lines, $A e'$, represent quarters of Points; the broken lines $A e$, represent halves of Points; and the continuous lines $A e$ whole Points.

§ a. The distance on a given course is shown on the lines $A e$, at the end of which lines that course is found; then the portion of that line ($A e$) which is contained between A , and the arc 3, 4, etc., which is marked with the distance proposed, is hypotenuse to the triangle required.

§ b. Thus 24 miles on a $2\frac{1}{4}$ Point course, is the distance $A b$ on the broken line $A e$, at the end of which $2\frac{1}{4}$ is marked; and $A C b$ is the right angled triangle, of which the course and the distance proposed constitute an angle and the hypotenuse.

§ c. The two legs of this triangle are the *base* $A C$, and the *perpendicular* $b C$ which stands under the parallel $b d$.

§ d. The graduated scale on $A D$ shows the value of $A C=21.1$, the *D. lat.*; and the portion ($D d$) of the scale on the graduated arc, between the *base* and the parallel $b d$ (§ 553. § g.), shows the height of the *perpendicular* $b C=11.3$, the *Dep.*

§ 556. Now as the distance which a ship may sail upon any loxodromic course, is considered (§ 546. § b.) as the hypotenuse of a right angled plane triangle, if the distance sailed upon such course can be found in the diagram, the departure and difference of latitude, which correspond to that course and distance, may be found by means of the graduated *base* and arc, $A D$ and $B D$.

§ a. Or, if any two of these quantities; viz., Course, Dist., Dep., and Diff. Lat., be known, the other two are determinable by means of the diagram.

§ 557. A ship sails N. W. $\frac{1}{4}$ N. 19 miles, What departure and difference of latitude does she make?

§ a. The given course is found upon the dotted line $A e'$, and that portion ($A b$) of this line, which is between A and the 19th arc, is the hypotenuse of the triangle ($A c b$) involved.

§ b. The *perpendicular* ($b c$) intersects the *base* at 14.1, which is the difference of latitude.

§ c. And the parallel, from the top of the *perpendicular*, } intersects the graduated arc at 12.7, which is the departure. } Plate 1.

§ 558. A ship sails N. W. by N. and makes 12.7 miles of departure, What distance and diff. lat. does she make ?

§ a. The parallel from 12.7 on the graduated arc, intersects the N. W. by N. line, in the point, (nearly), where the 23d arc crosses it; then nearly 23 (22.9) miles in the distance sailed.

§ b. And the *perpendicular* from this point of intersection, falls upon the *base*, and shows the difference of latitude required, to be 19.1 miles.

§ 559. A ship sails N. by W. $\frac{1}{2}$ W. and makes 19.8 miles diff. lat., What departure and distance does she make ?

§ a. The *perpendicular* at 19.8 on the *base*, being traced up, is found to intersect the N. by W. $\frac{1}{2}$ W. line on the 21st arc; then 21 miles is the distance sailed.

§ b. And the parallel from this point of intersection, being traced to the graduated arc, shows the height of the perpendicular 7 miles, which is the departure required.

§ 560. A ship, after sailing 18 miles, finds that she has made 16.2 miles diff. lat., What course did she sail, and what departure has she made ?

§ a. The *perpendicular* from 16.2 on the *base*, intersects the 18th arc on the dotted line marked $2\frac{1}{2}$ Points, which is the course required.

§ b. And the parallel from this point of intersection, shows, on the graduated arc, the height of the perpendicular to be 7.8 miles, which is the departure required.

§ 561. A ship sails 28 miles, and finds that she has made 15.6 miles departure, What course and diff. lat. has she made ?

§ a. The parallel from 15.6 on the graduated arc, cuts the 28th arc, on the line marked 3 Points, which is the course sailed.

§ b. And the *perpendicular* from this point of intersection, falls upon the *base* at 23.3 miles, which is the diff. lat. required.

§ 562. The departure between two places is 8.7 miles, and the diff. lat. between them is 28.6 miles, What is the course, and the distance from one place to the other ?

§ a. The *perpendicular* from 28.6 on the *base*, intersects the 30th arc on the broken line, $1\frac{1}{2}$, which shows the required course and distance to be $1\frac{1}{2}$ Points, and 30 miles.

§ 563. If the distance sailed be not more than a mile, or if the hypotenuse of the triangle proposed, be not greater than 3, the divisions on the scales must be decimated; then the figures 1, 2, 3, 4, 5, etc., stand for $\frac{1}{10}$, $\frac{2}{10}$, $\frac{3}{10}$, $\frac{4}{10}$, $\frac{5}{10}$, etc., and the subdivisions stand for 100ths.

§ a. Wherefore, when the distance is not more than 3 miles, the distance from A, to the 10th arc, is 1 mile; to the 20th, 2 miles; and to the 30th, 3 miles; and all the numbers in the diagram stand for 10ths.

§ 564. What departure and difference of the lat. would a ship make by sailing 2 miles N. W. $\frac{1}{2}$ N. ?

Plate 1. } § a. The parallel and *perpendicular* which would pass through the point in which the 20th arc intersects the N. W. $\frac{1}{4}$ N. line, measured by the eye, would cut the graduated arc and base in 12.7 and 15.4.

§ b. And using only one decimal place (§ 563.), the nearest would be 1.5 diff. lat. and 1.3 departure; but the exact is 1.54 and 1.27 diff. lat. and dep.

§ 565. When the lines in the diagram do not pass through the point required by the conditions of the triangle involved, the imaginary lines required, may be traced by the eye with all the precision which is necessary; and after a little practice, with the utmost accuracy and facility.

§ a. Thus, the distance of one place from another, is N. by W. $27\frac{1}{2}$ miles; the triangle involved in this problem, being filled up by the eye, the imaginary parallel and *perpendicular*, cut the graduated arc and *base* in 5.3 and 27; which shows the departure between the two places to be 5.3 miles, and the diff. lat. 27 miles.

§ 566. If the distance sailed on a single course exceed 30 miles, or the hypotenuse of the triangle involved, be greater than 30, all the numbers in the diagram must be increased tenfold.

§ a. Then the arcs must be reckoned as being 10 miles a part; the numbers 1, 2, 3, 4, 5, etc., will stand for 10, 20, 30, 40, 50, etc.; and the distance between these numbers being divided, every one in 10 equal parts, every one of these subdivisions must be counted as 1 mile.

§ 567. A ship sails N. W. 240 miles; what departure and diff. lat. does she make?

§ a. The parallel and *perpendicular* from the intersection of the 24th arc (now counted (§ 566) 240), with the N. W. line, cuts the graduated arc and *base* (§ 41.) at equal distances, and the departure and diff. lat. (§ 14.) are the same.

§ b. Departure = 169.5. diff. lat. = 169.5. This is $\frac{2}{5}$ of a mile less than the result by logarithmic calculation. This difference is owing to the smallness of the scale upon which the diagram is projected, and not to any defect in the principles involved in the projection of the diagram.

§ 568. In the examples quoted above, the courses are *on* the lines, and the diff. lat., except (§ 567.) when the course consists of 4 Points, is always greater than the departure.

§ 569. The courses and figures *under* the lines, (§ 554. § e.) are the complements of those *on* the line above them; and when the course is found *under* the line, the departure is the longest leg of the triangle involved, and must be read off upon the *base* A D; and the diff. lat. is taken from the graduated arc B D.

§ a. A ship sails E. $\frac{1}{4}$ N. 28 miles. What departure and diff. lat. does she make?

§ b. The parallel and *perpendicular* which pass through the point where the 28th arc cuts the dotted line, *under* which the given course is marked, meet the graduated arc and base in 1.3 and 27.9+.

§ c. Then (§ 569.) the departure = 27.9. and the diff. lat. = 1.3.

§ 570. The four cardinal points of the horizon (§ 272.) } Plate 1.
 divide it into four quadrants, each containing 8 Points.

§ a. Wherefore a Point = $11^{\circ} 15'$, the quotient of 90° by 8.

§ 571. The Points, when expressed by numbers, begin at the north and south, and are reckoned in numerical order, to the east and west points.

§ a. Hence, it is easy to conceive that a vessel that sails N. 3 Points W., or N. W. by N., would make more *northing* than *westing*, and that her diff. lat. would be greater than her departure.

§ b. And conversely, that if a vessel sail on any course between 4 and 8 Points, e. g., N. 5 Points W., or N. W. by W., she would make more *westing* than *northing*, and that consequently her departure would be greater than her diff. lat.

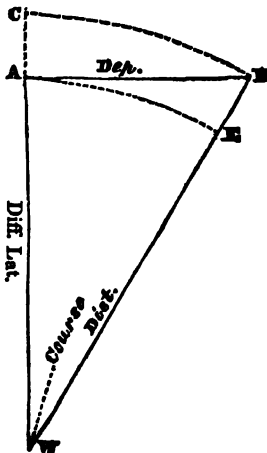
§ 572. From what has already been advanced in explanation of the diagram, it appears that the triangle involved in the trigonometrical solution of any problem in *loxodromic* sailing, is a right angled plane triangle.

§ a. *Loxodromic* sailing,* is so called from the sort of curve which the track of a ship forms, when she is sailing upon any course not exactly due east or west, north or south.

§ b. *Loxodromic* curves are spirals, which continually approach the poles, but can never reach them.

§ c. And any course, not due east or west, north or south, is called a *loxodromic* course.†

§ 573. A number of formulæ, varied in the trigonometric functions to be used, may be drawn up for the solutions of the several cases in *loxodromic* sailing.



§ a. The terms in these formulæ depend upon the side of the triangle, whether it be the distance, the departure, or diff. lat., which is made radius.

§ 574. Baltimore is 35 miles N. N. E. $\frac{1}{4}$ E. from Washington. The formula for finding by calculation the departure and diff. lat. between the two places, depends upon the trigonometrical construction which is given to the triangle involved.

§ a. If the hypotenuse be made radius, to an arc B C, the dep. becomes (§ 54.) sine to the course, and the diff. lat. its co-sine.

§ b. Then, (§ 75.), rad. : dist. :: sin. of course : dep. :: cos. course : diff. lat.

* The subdivisions of the *sailings*, viz., Plane, Traverse, Parallel, and Middle Latitude Sailing, are not here preserved. These distinctions are by no means necessary for the purpose of facilitating the navigator's calculations; they have therefore been generalized under the term of *loxodromic sailing*.

† E. by N. is a *loxodromic* course. Suppose a vessel could sail E. by N.

§ c. Hence (§ 74.) are deduced the following formulæ; the three first being the given terms, and the fourth, the unknown and required term, of the proportion.

§ d. Sin. course : dep. : : rad. : dist. (§ 75. § b.).

§ e. Dist. : rad. : : dep. : sin. course.

§ f. Cos. course : diff. lat. : : rad. : dist.

§ g. Dist. : rad. : : diff. lat. : : cos. course.

§ h. Cos. course : diff. lat. : : sin. course : dep.

§ i. Dist. = 35. log. = - - - 1.544068
Course = 2½ pts. (§ 571.) sin. (Table D) = 9.711049

Log. dep. = 1.255117 = 18 miles.

§ j. Dist. 35. log. = - - - 1.544068
Course, 2½ pts. cos. = - - - 9.933350

Log. diff. lat. = 1.477418 = 30 miles.

§ 575. If the triangle be constructed upon the diff. lat. as radius of the arc A E, then the dist. becomes (§ 57.) secant, and the dep. (§ 56.) tangent, to the course.

§ a. And (§ 75.) sec. course : dist. : : rad. : diff. lat. : : tang. course : dep.

§ b. Wherefore, the diff. lat. being taken as radius, the following formulæ are derived either (§ 75. § c.) immediately from the construction of the triangle, or (§ 67. § e.) from the relation of the terms, as they are expressed in the proportion § a.

§ c. Diff. lat. : rad. : : dist. : sec. course.

§ d. Rad. : diff. lat. : : sec. course : dist.

§ e. Diff. lat. : rad. : : dep. : tang. course.

§ f. Tang. course : dep. : : rad. : diff. lat.

§ g. Tang. course : dep. : : sec. course : dist.

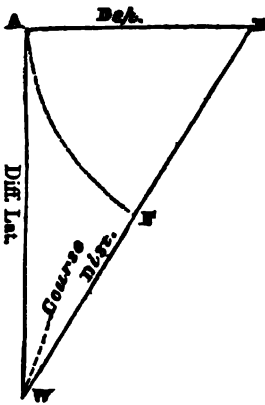
§ h. Course 2½ pts. cos. = 9.933350 (§ 101. § b.)
Dist. 35 miles, log. = 1.544068

Log. diff. lat. = 1.477418 = 30 miles.

§ i. Course 2½ pts. cos. = 9.933350
Dist. 35 miles, log. = 1.544068
Course 2½ pts. tang. = 9.777700

Log. dep. = 1.255118 = 18 miles.

without any obstruction, or without ever deviating from that course; the N. pole would then be always *one Point* forward of her beam. It is difficult to imagine how a vessel could ever arrive at such a point.



§ 576. Or if the triangle be constructed upon the dep., as radius of the arc A F, the dist. becomes secant, and the diff. lat. the tangent, of B, the complement (§ 32. § d.) of the course.

§ a. Wherefore (§ 75. § c.) co-sec. course : dist. :: rad. : dep. :: co-tang. course : diff. lat.

§ b. Other formulæ of proportion, similar to those under § 575., might be drawn out here, but these for the most part would be a repetition of those, as the expression 4×6 is a repetition of the form 6×4 of multiplication. Indeed several sets of the proportions under § 574. & § 575., are similar repetitions of each other.

§ c. Course $2\frac{1}{2}$ pts. $\sin.$ = 9.711049 (§ 101. § b.)
 Dist. 35 miles, $\log.$ = 1.544068

$$\text{Log. dep.} = 1.255117 = 18 \text{ miles.}$$

§ d. Course $2\frac{1}{2}$ pts. $\sin.$ = 9.711049
 Dist. 35 miles, $\log.$ = 1.544068
 Course $2\frac{1}{2}$ pts. co-tang. = 0.222300

$$\text{Log. diff. lat.} = 1.477417 = 30 \text{ miles.}$$

§ 577. The principles of the above trigonometrical construction are also developed in the solution of problems } Plate 1.
 by the diagram.

§ a. Thus, to find the course and dist. which correspond to 12 miles diff. lat., and 5 miles dep.

§ b. The perpendicular which cuts the base in 12, is tangent to the 12th arc, and A 12 is its radius.

§ c. The parallel from 5, on the graduated arc, cuts this perpendicular on the 13th arc, at its intersection with the 2 Point line, and A 13 is secant to the course (2 Points) and the dist. required.

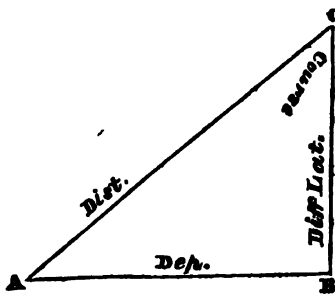
§ d. If the dist. A 13, on the 2 Point line be called radius of the 13th arc, then the portion of the perpendicular, between the point of this intersection, is sine of the course, and A 12 on the base, is its co-sine.

§ 578. Table of log. sines, etc., of the Points of the Compass.

TABLE D.

Points.	Sine.	Co-sec.	Co-sin.	Sec.	Tang.	Co-Tang.	
$\frac{1}{4}$	8.690795	1.309205	9.999477	0.000523	8.691319	1.308681	$7\frac{1}{4}$
$\frac{1}{2}$.991302	.008698	.997904	.002096	.993398	.006602	$7\frac{1}{2}$
$\frac{3}{4}$	9.166520	0.833480	.995274	.004726	9.171246	0.828754	$7\frac{3}{4}$
1	.290236	.709764	.991574	.008426	.298662	.701338	7
$1\frac{1}{4}$.385572	.614428	.986787	.013213	.398784	.601216	$6\frac{3}{4}$
$1\frac{1}{2}$.462824	.537176	.980885	.019115	.481939	.518061	$6\frac{1}{2}$
$1\frac{3}{4}$.527488	.472512	.973840	.026160	.553647	.446353	$6\frac{1}{4}$
2	.589840	.417160	.965615	.034385	.617224	.382776	6
$2\frac{1}{4}$.630992	.369008	.956163	.043837	.674829	.325171	$5\frac{3}{4}$
$2\frac{1}{2}$.673387	.326613	.945430	.054570	.727957	.272043	$5\frac{1}{2}$
$2\frac{3}{4}$.711049	.288951	.933350	.066650	.777700	.222300	$5\frac{1}{4}$
3	.744739	.255261	.919846	.080154	.824893	.175107	5
$3\frac{1}{4}$.775037	.224963	.904828	.095172	.870199	.129801	$4\frac{3}{4}$
$3\frac{1}{2}$.802359	.197641	.888185	.111815	.914173	.085827	$4\frac{1}{2}$
$3\frac{3}{4}$.827083	.172917	.869790	.130210	.957294	.042706	$4\frac{1}{4}$
4	.849485	.150515	.849485	.150515	0.000000	0.000000	4
	Co-sine.	Sec.	Sine.	Co-sec.	Co-tang.	Tang.	Points.

§ 579. In every case, except when the dep. and diff. lat. constitute the two given parts, the solution of the problem proposed, may be obtained by means of the proportion (§ 74.) between the sides of a triangle and sines of their opposite angles.



§ a. In the triangle A B C (§ 74.) right angled at B, (§ 74.) dist. : sin. B=90° :: dep. : sin. course; but the sine of 90 (§ 62.) is radius, wherefore we have again the formula § e., (§ 574.), viz., dist. : rad. :: dep.

: sin. course, and a repetition of others under § 574.

§ 580. Some one of the following formulæ (rejecting or borrowing 10 for rad., (§ 197. § f.), in the index of the second member of the equation), may be used in every case where two of the four quantities, dist., course, dep. and diff. lat., are given.

§ a. Dep. (§ 574. § b.)=dist. × sin. course.

§ b. Dep. (§ 575. § e.)=diff. lat. × tang. course.

§ c. Diff. lat. (§ 574. § j.)=dist. × cos. course.

§ d. Diff. lat. (§ 575. § f.)= $\frac{\text{Dep.}}{\text{tang. course}}$ (§ 101. § b.)=dep. × cot.

course.

§ e. Dist. (§ 575. § d.) = diff. lat. \times sec. course.

§ f. Dist. (§ 576. § a.) = dep. \times co-sec. course.

§ g. Sin. course (§ 574. § e.) = $\frac{\text{Dep.}}{\text{dist.}}$

§ h. Cos. course (§ 574. § g.) = $\frac{\text{Diff. lat.}}{\text{dist.}}$

§ i. Tang. course (§ 575. § e.) = $\frac{\text{Dep.}}{\text{diff. lat.}}$

§ j. These formulæ will always be found convenient in practice.

OF TURNING DEPARTURE INTO DIFF. LONG.

§ 581. If the difference of longitude between two places (§ 548.) be expressed in miles, it is called departure.

§ a. A minute of longitude is no where, except at the equator, equal to a mile of departure; for the distance between any two meridians of longitude (§ 248. § a.) is greatest at the equator, and the least about the poles.

§ b. Therefore the dep. between any two meridians is greater at the equator than in any latitude.

§ c. Furthermore, as all meridians (§ 248. § a.) intersect at the poles, the dep. between any two becomes less and less, as you approach the poles, where there can be no dep.; whereas the difference of longitude, between these meridians in any latitude, (§ 254. § a.) is the same, being expressed by the same number of degrees ($^{\circ}$), minutes ($'$), etc.

§ 582. Suppose two places to be situated in the same latitude, the arc of this parallel of latitude, contained between them, (§ 254. § b.) is their difference in longitude.

§ a. And parallels of latitude (§ 249.) are small circles.

§ b. Suppose also an arc of a great circle (§ 122.) to be drawn from one of these places to the other, this arc (§ 122. § a.) would be the shortest distance between the two places, and the minutes ($'$) contained in it, would show (§ 547.) the departure between them.*

§ 583. These two arcs are contained between the same two points, and (§ 76.) the arcs are to each other, as the radius of the great circle is to the radius of the small circle.

§ a. The rad. of such a great circle, as well as of the equator, etc., (§ 122.) is semidiameter to the earth.

§ b. And the radius of the small circle, or the parallel, (§ 130. § a.) is the cos. of its latitude.

§ 584. Then, calling the semidiameter of the earth, unity, or rad., we have (§ 76.) for any latitude, diff. long. : dep. : : rad. : cos. lat.

§ a. Also cos. lat. : dep. : : rad. : diff. long.

§ b. And rad. : diff. long. : : cos. lat. : dep.

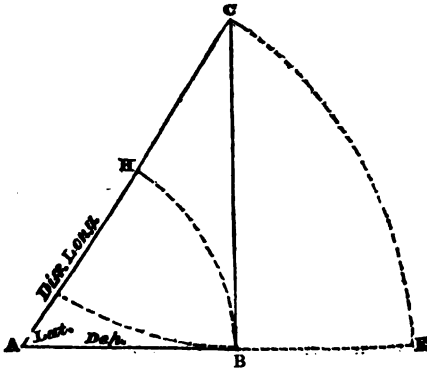
* Hence it appears that the *course* between two places, is never the shortest distance between them, unless they be either upon the equator, or upon the same meridian.

§ c. Wherefore, if any two of these three quantities, (rad. is always known), be given, the other and remaining one is determinable.

§ 585. The terms of these proportions represent quantities, comprised in the elements of a right angled plane triangle.

§ a. Wherefore, if the figure which furnishes such proportions, be considered a plane triangle; it will be right angled, the latitude will be one of its acute angles; the diff. long., the hypotenuse; and the dep. will be one of the legs of such triangle.

§ b. The result obtained from calculations conducted upon such principles, (§ 549.) must be only an approximation.



§ 586. Suppose a ship sailed E. $15\frac{1}{2}$ miles on the parallel of $56^{\circ} 15'$ south latitude, her departure would be $15\frac{1}{2}$ miles, the distance sailed.

§ a. And in the right angled triangle ABC, the angle $A = 56^{\circ} 15'$, the lat.; the leg $AB = 15\frac{1}{2}$, the dep.; and the hypotenuse (§ 585. § a.) is the diff. long.

§ b. Now, if the diff. long. be made radius, of the arc CE; CB becomes its sine, and AB its co-sine, whence (§ 75.) arise the proportions, under § 584.

§ c. Rad. : diff. long. : : cos. lat. : dep.

§ d. Diff. long. : rad. : : dep. : cos. lat.

§ e. Cos. lat. : dep. : : rad. : diff. long.

§ f. To find the corresponding diff. long. by calculation (§ e.).

Lat. $56^{\circ} 15'$ sec. = 0.255261 (§ 101. § b.)

Dep. 15.5 log. = 1.190332

Log. diff. long. = 1.445593 = 27.9 minutes (')

§ 587. If the dep. (AB) be made radius, to the arc BH, then the diff. long. becomes secant to the lat., and we have (§ 75. § c.)

§ a. Rad. : dep. : : sec. lat. : diff. long.

§ b. Sec. lat. : diff. long. : : rad. : dep.

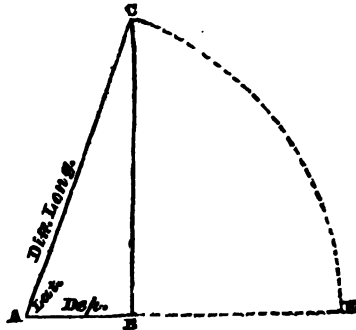
§ c. Dep. : rad. : : diff. long. : sec. lat.

§ 588. Now, if the other leg (CB) be made radius, the dep. becomes co-tang. (§ 57. § b.), and the diff. long. the co-sec., of the latitude, whence (§ 75.) arise the following sets of proportions.

§ a. Co-tang. lat. : dep. : : co-sec. lat. : diff. long.

§ b. Co-sec. lat. : diff. long. : co-tang. lat. : dep.

§ 589. To find the number of miles, or the dep., which correspond to 1° or 60' on the parallel of 67° 30'.



§ a. The diff. long. being made radius, we have, (§ 586. § c.),
 Rad. : diff. long. :: cos. lat. : dep.

$$\begin{aligned} \text{Diff. long. } 60 \text{ log.} &= 1.778151 \\ \text{Lat. } 67^\circ 30' \text{ cos.} &= 9.582840 \end{aligned}$$

$$\text{Log. dep.} = \underline{\underline{1.360991}} = 22.9$$

§ 590. C (§ 32. § d.) is the complement of A, and is equal to 22° 30'. C B is the cos. of C, and shows the number of miles contained in 1° of long. on the parallel of lat. 22° 30'.

$$\begin{aligned} \text{§ a. Diff. long. } 60 \text{ log.} &= 1.778151 \text{ (§ 589. § a.)} \\ \text{Lat. } 22^\circ 30' \text{ cos.} &= 9.965615 \end{aligned}$$

$$\text{Log. dep.} = \underline{\underline{1.743766}} = 55.4 \text{ miles,}$$

which is equal to 1° of long. in lat. 22° 30'.

§ b. Now (§ 75. § b.) $CB : \cos. C :: AB : \cos. A$. AB shows the number of miles equal to 1° of long. in lat. 67° 30', and CB shows the number of miles, that make 1° of long. in lat. 22° 30', the complement of 67° 30'.

§ c. Wherefore, in any lat., the miles in a degree of long. are to the cos. of that lat., as the miles contained by a deg. of long. in any other lat., are to the cos. of this lat. And alternately.

§ 591. As a right angled plane triangle (§ 585,) is in- } Plate 1.
 volved in the solution of the several problems under § 586. }
 § 587. § 588., etc.; the solution of every one of such problems may be obtained by means of the diagram.

§ a. The diff. long. (§ 585. § a.) is the hypotenuse; and the leg adjacent to the angle which in degrees (°), is equal to the latitude in which the dep. or diff. long. is made, is the dep.

§ 592. Of dep., diff. long. and lat., either is determined on the diagram, by means of the two others, in the same manner, that any

D D

Plate 1. } one of the three quantities, viz., diff. lat., dist. and course,
 } is determined (§ 556. § a.) by means of any two of these.

§ 593. When the latitude in which the diff. long. or dep. is made, is less than 45° , the degrees of lat. are to be found on the *inside* of the graduated arc; and the dep. on the *base*.

§ a. But when the latitude is *greater* than 45° , the degrees of it are to be found on the *outside*, and the dep. on, the graduated *arc*.

§ b. Thus, 26' of long. is equal to 24.5 miles, in lat. 19° ; and in lat. 71° , it is equal to 8.4 miles.

§ c. The *perpendicular* from the mark for the 19° th on the 26th arc, cuts the *base* at 24.5, which shows the dep. for 26' of long. in lat. 19° .

§ d. The parallel from 71° on the 26th arc, cuts the graduated arc at 8.4, which is the dep. (§ 593. § a.) for 26' of long. in lat. 71° .

§ 594. A ship in lat. 27° , makes 20.5 miles dep. To find the diff. long.

§ a. The diff. lat. is found on the *inside* (§ 593.) of the graduated arc, and the dep. on the *base*.

§ b. The *perpendicular* from 20.5 on the *base*, intersects 27° on the 23d arc, then 23' is the required diff. long.

§ 595. A ship in lat. 60° , makes 12 miles dep. To find the diff. long.

§ a. The degrees of the lat. (§ 593. § a.) are found on the *outside*, and the dep. on the graduated arc.

§ b. The parallel from 12, intersects 60° on the 24th arc; 24' is the diff. long.

§ 596. The diff. long. between two places in lat. 33° is 27'. To find the dist. between them.

§ a. The lat. is found on the *inside* (§ 593.) of the graduated arc, and the dep. on the *base*.

§ b. The *perpendicular* from 33° on the 27th arc, falls upon the *base* at 22.6, the dist. in miles between the two places.

§ 597. The diff. long. between two places in lat. 54° , is 24'. To find the dist. between them.

§ a. The degrees of lat. are on the *outside*, and the dist. (§ 593. § a.) is to be found on the graduated arc.

§ b. The parallel from 54° on the 24th arc, cuts the graduated arc at 14.1, the dist. required.

§ 598. The dep. between two places on the same parallel, is 18.4 miles, and the diff. long. is 20'. To find their lat.

§ a. The *perpendicular* from 18.4 cuts the 20th arc at 23° , the lat. required.

§ b. The dep. being found on the *base*, the degrees (§ 593. § a.) are taken from the *inside* of the arc.

§ c. But if the dep. were found on the graduated arc, then the degrees on the *outside* of the arc, would show the lat.

§ 599. The diff. long. being 20', and the dep. between two places in the same latitude being 6.8 miles; to find their lat.

§ *c.* The parallel from 7.8, cuts the 20th arc at 67° , { Plate 1.
which (§ 598. § *c.*) is the lat.

§ *b.* When the minutes ($'$) of long. exceed $30'$, every division on the several graduated scales, (§ 566.) must be counted as a mile, or as a minute ($'$).

§ *c.* And when the minutes ($'$) of long. do not exceed $3'$, the divisions on the graduated scales (§ 563.) must be decimated.

§ 600. Of the diff. long., dep. and lat., either one may be found, the others being given, by means of Table V.

§ *a.* The degrees at the top of the table, are those which are *inside* of the arc; and those at the bottom of the table, and on the *outside* of the arc, are the same.

§ *b.* The numbers in the column marked (dist.) stand for minutes ($'$) of longitude; they show the value of the hypothenuse of a triangle, whose legs are equal to the quantities in the next two columns; and whose acute angles contain, one the degrees at the *top*, and the other those at the *bottom* of the page.

§ *c.* When the lat. is found at the top of the page, the miles which are equal to any number of minutes of longitude, are opposite to them in the column marked, at the top, (d. lat.)

§ *d.* Thus, in lat. 41° , $60'$ of long. = 45.3 miles.

§ *e.* If the degrees of lat. be found at the bottom of the page, then the miles which are equal to any number of minutes ($'$) of long., are found opposite to them in the column marked (d. lat.), at the bottom.

§ *f.* Thus, in lat. 71° , $60'$ of long. = 19.5 miles.

§ 601. When a ship sails due east, or west, she sails either upon a parallel of lat., or upon the equator, and the whole distance sailed is dep.; which may be converted into diff. long. by the formula § *f.* (§ 566.), or by means of the diagram (Plate I.), or Table V.; either of the two latter means is most convenient in practice.

§ 602. When a ship sails due North or South, she sails upon the arc of a meridian, and the whole distance sailed is diff. lat.

§ 603. It is frequently the case, that a ship sails during the day, on more courses than one, making a zig-zag track.

§ *a.* In such cases, it would be a very tedious operation, after finding the diff. lat. and dep. for every course and distance, to convert the dep. for every such course and dist. into diff. long. by a separate operation.

§ *b.* Such circuitry is avoided by taking the whole amount of dep., and converting it into diff. long. by a single inspection of the diagram, or of Table V.

§ 604. Suppose a ship sails from lat. 64° N., 216 miles N.E. by N.; she makes 120 miles of dep. and 179.6, say 180 or 3° diff. lat.

§ *a.* Now this dep., or the diff. long. is not all made upon the parallel of 64° , $'5^{\circ}$, $'6^{\circ}$, or $'7^{\circ}$; or upon any one of the intermediate parallels, but upon all of them together.

§ *b.* And in order to convert, by a single operation, this dep. into long., and to find the diff. long. which the ship has made by sailing this course and distance, the whole dep. is supposed to be

made upon that parallel ($65^{\circ} 30'$) which is midway between the lat. left (64°), and that (67°) arrived at.

§ c. This lat. ($65^{\circ} 30'$) is called the *middle latitude*; it is *half the diff. lat. added to lat. left*; or to that arrived at, if the latter be the less lat.

§ 605. If the number of miles in a degree of long. on the different parallels, as you approach the poles, decreased, as the miles from the equator to those parallels increase, this method would show the true diff. long.

§ a. But the number of miles in a degree of long. at different parallels, is (§ 590. § c.) as the cosines of the lat. of such parallels.

§ b. Wherefore, the result given by this method is only an approximate one.

§ c. But in working up "dead reckoning," "days' works," etc., this method is generally used; it is used in all cases, except in the computation of great distances.

§ 606. On ship-board at the expiration of every hour, sometimes of every two hours, the course and distance sailed during that time are marked opposite each other, on the *log slate*.

§ a. And at the end of every sea day, or at every noon, the courses and distances sailed in the last 24 hours, are "taken off," for the purpose of "working up;" and the whole distance sailed on every separate course is set down, opposite to that course, in a *traverse table*.

Plate 1. } § b. The diff. lat. and the dep. for every course and dist., are taken, either from the diagram, or from Table IV., and set down opposite to their proper course and dist. in the "traverse table."

§ c. The dep. and diff. lat. for every course and dist., are then added up; the sums show the whole dep. and diff. lat.

§ d. And by means of the whole dep. and diff. lat., the course and dist. "made good," are found on the diagram (§ 577. § a.), or are taken from Table IV. or V.

§ e. The "middle lat." (604. § c.) is then found; and by means of it and the dep., the diff. long. is found (§ 594.) on the diagram, or in Table V.

Fig. A.

Course.	Dist.	Diff. Lat.		Depart.	
		N.	S.	E.	W.
N. by E.	20	19.6	--	3.9	--
S. W.	12	--	8.5	--	8.5

§ 607. Fig. A is the formula of a "traverse table."

§ a. The diff. lat. is written in the column marked N. or S. according as the course has *nothing*, or *southing* in it. Thus, the diff. lat. for 20 miles N. by E. is put in the N. column, and the diff. lat. for 12 miles S. W. is written in the S. column.

§ b. The dep. must be placed in the column E. or W., according as the course has *easting*, or *westing* in

it. Thus the dep. for the dist. 20 N. by E., is written in the E. column, and the dep. for the dist. 12, S.W. is written in the W. column.

§ 608. The dep. and diff. lat. for any dist. less than 300 miles, and for any course, are found in Table IV., in a manner similar to that by which they are found on the diagram.

§ a. If the course be less than 4 Points, it is to be found at the top of the page, and the diff. lat. must be taken from the column marked at the top (d. lat.), and over which the course is found.

§ b. Thus, to take from Table IV. the dep. and diff. lat. for 120 miles S. $\frac{1}{2}$ E.; find S. $\frac{1}{2}$ E. at the top of the page, and 120 in the dist. column; then in the two columns, at the head of which S. $\frac{1}{2}$ E. is found, and opposite to 120, are the diff. lat. 119.4, and the dep. 11.8.

§ c. But if the course be more than 4 Points, it is to be found at the bottom of the page, and the precept at the foot of the column must be the guide for taking out dep. and diff. lat.

§ d. Thus to take from Table IV. the dep. and diff. lat. for 30 miles E.N.E.; find E.N.E. at the bottom of the page, and 30 in the dist. column, then in the two columns, at the foot of which E.N.E. is found, are 27.7 (dep.) and 11.5 (diff. lat.) opposite to 30.

§ e. If the dist. exceed 300 miles, some aliquot part of it is taken as the 2d, 3d, etc., and the dep. and diff. lat. opposite to this quotient being increased by 2, 3, etc., as much as the dist. was reduced, give the required dep. and diff. lat. Thus to find the dep. and diff. lat. for 400 miles N.N.W.; take 200, the half of it; then, under N.N.W. and opposite 200, stands 184.8 in the d. lat. column, and 76.5 in the dep. do.; each of which being multiplied by 2, gives the required diff. lat. 369.6 or $6^{\circ} 9' 36''$, and the dep. 153 miles.

§ f. Table V. is used in the same way for finding dep., diff. lat., etc., when the course is given in degrees. Thus the dep. for 18 miles N. 30° E. is 9 miles; and the diff. lat. for 40 miles S. 74° E. is 11 miles.

TRAVERSE TABLE.

Compass Courses.	Courses Corrected.	Dist.	Diff. Lat.		Dep.		
			N.	S.	E.	W.	
N.N.E.	N.E. by N.	14	11.6	—	7.8	—	
S.S.E.	S. by E.	18	—	17.7	3.5	—	
South	S. by W.	40	—	39.2	—	7.8	
S.½E.	S.½W.	19	—	18.9	—	1.9	
N.W.½N.	N.N.W.½W.	9	7.9	—	—	4.3	
N. by W.	North	6	6	—	—	—	
W. by S.	West	3	—	—	—	3	
East	E. by S.	2	—	.4	2	—	
N.E.	N.E. by E.	60	33.3	—	49.9	—	
S.W. by S.	S.W.	16	—	11.3	—	11.3	
W.½S.	W.½N.	7	.3	—	—	7.	
W.½N.	W. by N.½N.	4	1	—	—	3.9	
Lat. sailed from			41° 13' N.	60.1	87.5	63.2	39.1
Diff. Lat.			—	—	66.1	89.1	—
Lat. in			40° 45' 36" N.	—	—	—	—
Mid. Lat. (§ 604. § c.)			41°	—	27.4	24.1	—
Long. sailed from			70° 15' W.	—	—	—	—
Diff. Long.			32' E.	—	—	—	—
Long. in			69° 43' W.	Variation 1 Point E.			—

§ 609. The courses in the 1st column of the "traverse table" are the courses sailed per compass.

§ a. Those in the 2d column are those corrected (§ 298. § b.) for variation, which is 1 Point E.

§ b. The diff. lat. and dep. in their columns, answer to the dist. and *corrected courses* to which they are opposite.

§ d. The diff. lat. 27' 4 S. and the dep. 24.1 E. show that the ship, by sailing the several courses and distances in the table, went to the Southward and Eastward.

§ d. The dep. 24.1 and diff. lat. 27.4 are found opposite 36 (Table V.) and *under* 42°, which shows the course and dist. "made good," (§ 606. § d.) to be S. 42° E., 36 miles.

§ e. Under 41° (Table V.) 24.1 in the d. lat. column, stands opposite to 32 in the dist. column; the diff. long. then is 32' East.

§ 610. The manner in which "dead reckoning," "days' works," etc., are worked up, and kept at sea, whether by means of the Tables IV. and V., or the diagram, may be learned from the subjoined formulæ. } Plate 1.

§ a. Aug. 28, lat. and long., 62° N. and 47° W.

§ b. Variation W. 1½ Pt., which (§ 298. § b.) is to be allowed towards the left.

Aug. 24.

Compass Courses.	Courses Corrected.	Dist.	Diff. Lat.		Dep.	
			N.	S.	E.	W.
S. E.	S. E. by E. ¼ E.	16		7.5	14.1	
E. ½ N.	E. N. E.	12	4.6		11.1	
E. by N.	N. E. by E. ¼ E.	14	6.6		12.3	
N. E.	N. N. E. ¼ E.	20	17.6		9.4	
N. N. E.	N. ¼ E.	18	17.9		1.8	
N. by E. ¼ E.	North	66	66			
North.	N. by W. ¼ W.	40	38.3			11.6
S. W.	S. S. W. ¼ W.	26		23.9		13.3
Yesterday's lat. (§ a.) 62° N.			151.	30.4	48.7	23.9
Diff. lat. - - - 2° 0' 36" N.			30.4		23.9	
Lat. in - - - 64° 0' 36" N.						
Mid. lat. - - - 63° 0'						
Yesterday's long. 47° 0' W.			120.6		24.8	
Diff. long. - - - 55' E.						
Long. in - - - 46° 5' W.						
Course and dist. "made good" N. 12° E. 123 miles.						

§ c. Above 63°, the mid. lat. (Table V.) 24.8* in the d. lat. column, stands opposite to 55 in the dist. column; the diff. long. then is 55' E.

§ d. And the dep. 24.8 and diff. lat. 120.6 are found opposite to each other under 12°, (Table V.), and opposite to 123, which shows the course and distance made good.

* In this and all similar cases, the tabular number which is nearest to the given number is always used, when the given number cannot be found. Thus, in the present example, the given number 24.8 cannot be found in the d. lat. column over 63°; 25 is the tabular number nearest to 24.8; and 55' is opposite 25.

AUG. 25.

Compass Courses.	Courses Corrected.	Dist.	Diff. Lat.		Dep.	
			N.	S.	E.	W.
East	E. $\frac{1}{2}$ S.	30		4.4	29.7	
E.S.E.	S.E. by E. $\frac{1}{2}$ E.	18		9.3	15.4	
S. $\frac{1}{2}$ E.	South	16		10		
S.S.W.	S.S.W. $\frac{1}{2}$ W.	19		16.3		9.8
S.W. by S.	S.W. $\frac{1}{2}$ S.	25		18.5		16.8
W.S.W.	W. by S. $\frac{1}{2}$ S.	22		5.3		21.3
W. $\frac{1}{2}$ S.	West	17				17
West	W. $\frac{1}{2}$ N.	30	4.4			29.7
W.N.W.	N. W. by W. $\frac{1}{2}$ W.	29	14.9			24.9
Yesterday's lat. $64^{\circ} 0' 36''$ N.			19.3	69.8	45.1	119.5
Diff. lat. - $50' 30''$ S.				19.3		45.1
Lat. in - $63^{\circ} 10' 6''$				50.5		74.4
Mid. lat. - 64°						
Yesterday's long. $46^{\circ} 5' W.$						
Diff. long. - $2^{\circ} 50' W.$						
Long. in - $49^{\circ} 55' W.$						
			Variation $\frac{1}{2}$ Point E.			
Course and dist. sailed S. $56^{\circ} W.$ 90 miles.						

§ f. To find the bearing and dist. of a place in Lat. $63^{\circ} 20' N.$, and long. $49^{\circ} 10' W.$

§ g.

Lat. of place	$63^{\circ} 20'$
Lat. in	$63^{\circ} 10'$
Diff. lat.	<u>10 miles.</u>
Long. of place	49.10
Long. in	48 49
Diff. long.	<u>$=21'$</u>

§ h. 21 being found in the dist. column (Table V.) over 63° the lat., shows opposite to it 9.5 in the d. lat. column; 9.5 then is the dep. between the ship and the place.

§ i. The diff. lat. 10, and dep. 9.5 are found together under 43° (Table V.) and opposite 14; the course and dist. then from the ship to the place, is N. $43^{\circ} W.$ 14 miles.

§ j. April 9, lat. 39° 50' N., long. 70° 10' W.; bound to New York.

APRIL 10.

Compass Courses.	Courses Corrected.	Dist.	Diff. Lat.	Dep.
			N.	W.
W.N.W.	W. by N. $\frac{1}{4}$ N.	30	8.7	28.7
W. by N. $\frac{1}{4}$ N.	W. by N. $\frac{1}{4}$ N.	25	6.1	24.3
W. by N. $\frac{1}{2}$ N.	W. by N.	18	3.5	17.7
W. by N.	W. $\frac{1}{4}$ N.	29	2.8	28.9
W. by N. $\frac{1}{4}$ N.	W. $\frac{1}{2}$ N.	26	3.8	25.7
W. $\frac{1}{2}$ N.	W. $\frac{1}{4}$ N.	9	.4	9
W. $\frac{1}{4}$ N.	West	5	.0	5
Yesterday's lat. 39° 50' N.			25.3	139.3
Diff. lat. - 25' 18" N.				
Lat. in - 40° 15' 18"				
Mid. lat. 40°				
Yesterday's long. 70° 10' W.			Variation $\frac{1}{2}$ Point W.	
Diff. long. - 3° 2' W.				
Long. in - 73° 12' W.				
Course and dist. sailed N. 80° W. 143 miles.				

§ k. To find the bearing and dist. of Sandy Hook Light House.

S. L. House, lat. 40° 28' N.

Lat. ship - 40° 15' N.

Diff. long. 13'

Long. S. L. House, 74° 1' W.

Long. ship - 73° 12' W.

Diff. long. 49'

49' of long. in lat. 40° is equal to 37.5 miles. (Table V.)

§ l. 13 and 37.5 are found together over 71° (Table V.), and opposite 40. The dist. then of the Light House from the ship, is N. 71° W. 40 miles.

MERCATOR'S SAILING.

§ 611. Dep. : rad. : : diff. long. : sec. lat. (§ 587. § c.). Upon the principles involved in this proportion, the charts, called Mercator's, are constructed.

§ a. In these charts, the meridians of longitude, after they cross the equator, instead of approaching each other, till they reach the parallel of any latitude, in the ratio (§ 486. § b.) of rad. to the cos. of that lat., are drawn parallel to each other.

§ b. And the parallels of lat., say at 1° a part, instead of being at equal distances from each other, are drawn in the ratio of rad. to the sec. of their latitude. By which means, places on a sphere, are represented on a plane with their proper relative positions.

§ 612. In this manner of representing portions of the surface of a sphere upon planes, the parallels of latitude are lengthened out, and the meridians of longitude are expanded.

§ a. So that, if the 1st degree of lat., from the equator, be divided on the chart into 60 equal parts, every degree as they succeed each other in numerical order will contain a greater number of these parts, than the 1st, or than that which precedes it; thus, the 61st of lat. contains 126 of these parts, and the 31st, 70 of the same parts.

§ 613. These parts are called *meridional parts*.

§ a. Table VI. shows the number of meridional parts from the equator to any degree and minute within the parallel of the 84th of lat.

§ b. The number of meridional parts between any two parallels, is called the *meridional diff. lat.* of those parallels.

§ c. Thus, the mer. diff. lat. between $13^\circ 10'$ and $18^\circ 10'$, is 312.

The mer. parts of $18^\circ 10' = 1109$	}	Table VI.
do. $13^\circ 10' = 797$		

Mer. diff. lat. = 312

§ 614. Now, if any section of the earth's surface be represented on a plane projected according to Mercator's plan, the *true* (nearly), instead (§ 550.) of the *approximate*, distance, etc., between any two places, may be determined by *plane* trigonometrical operations.

§ a. To do this, the Mer. diff. lat., as well as the actual diff. lat. between places, must be used.

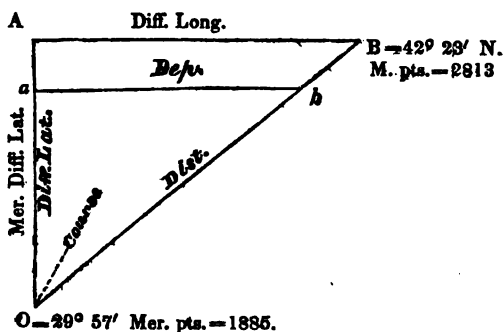
§ 615. Mercator's sailing is useful to the navigator, chiefly in enabling him to find, by plane trigonometrical calculations, the number of miles between places that are at a great distance from each other.

§ a. The several cases in loxodromic sailing, may also be accurately solved, according to the principles of Mercator's sailing; but the Mer. diff. lat. must be used, as well as the actual diff. lat.

§ b. Methods of applying the principles of Mercator's sailing to the solution of cases in loxodromic sailing, will be shown; but the

application of them to practice, will be left for the amusement of the learner.

§ 616. A B O represents the relative position of Boston and New Orleans in lat. and long., according to the principles of Mercator's sailing.



§ a. And the triangle $a b O$ shows the bearing, dist., etc., according to loxodromic sailing.

§ b. The meridional lat. of Boston is 2813, and that of New Orleans, is 1885 (Table VI.); and the difference between these (§ 613. § b.) is (O A) the Mer. diff. lat.; and A B is the diff. long.; A O B is the course from New Orleans to Boston.

§ c. According to the loxodromic plan of constructing the triangle, $a O$ is the actual diff. lat. between the two places, and $a b$ is the dep.

§ d. Whether the problem proposed be solved according to the loxodromic or Mercator plan, the actual diff. lat. between the two places is the same.

§ e. But the dep. and dist. determined by the former method (§ 550.) are not the true dep. and dist. between the two places.

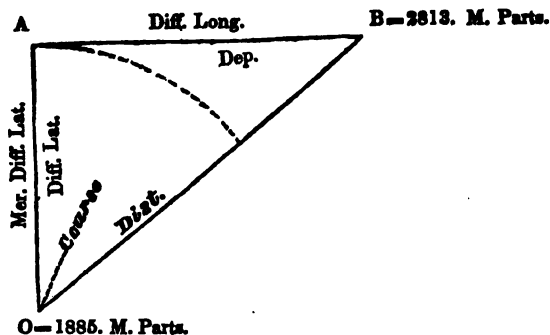
§ 617. As the angles $a b O$ and A B O (§ 616. § d.) are equal, $a b$ (§ 30. § d.) is parallel to A B; whence (§ 73. § d.) arise the relation between the sides of a triangle in loxodromic sailing when compared with the sides of a similar triangle in Mercator's sailing.

§ a. Diff. lat. : dep. : : Mer. diff. lat. : diff. long.; also inversely and alternately.

§ b. The relations between the other parts of the two triangles may be established according to the principles derived from § 72. & § 73. The learner may arrange them.

§ 618. If the Mer. diff. of lat. (O A) between New Orleans and Boston be made radius, several sets of proportions (§ 75.) will appear among the different parts of the triangle involved.

MERCATOR'S SAILING.



§ a. But the most useful proportion (and in fact almost the only one which occurs in practice), in Mercator's sailing, is that by which the *true* course and dist. between any two places are evolved. I shall give the terms of this proportion, and leave the others to be arranged by the learner.

§ 619. The Mer. diff. lat. (§ 618:) being radius ; Mer. diff. lat. : rad. :: diff. long. : tang. course.

§ a. The diff. long. thus used, must in all cases be converted into minutes, which must be used in the log. Table of Numbers, as miles.

§ b. To find the course from New Orleans to Boston.

Boston	lat.	42° 23'	M. pts.	=2813
N. Orleans	"	29° 57'	"	1885
		12° 26'	"	
		60	"	928 = Mer. diff. lat.

Diff. lat. = 746 miles.

N. Orleans,	long.	90° 9' W.
Boston	"	71° 4' W.
		19° 5'
		60

Diff. long. = 1145 minutes (').

Now, (§ 619.) 928 : rad. :: 1145 : tang. course.

928	log. (Ar. co.)	=7.032452
1145	log. (§ b.)	=3.058806

Tang. course = 0.091258 N. 50° 58' 34" E.

§ c. Then calling O A, the actual diff. lat., A B becomes dep., and retaining O A, as rad., we have (§ 574. § d.) rad. : diff. lat. :: sec. course : dist.

Diff. lat. 746 miles log.=2.872739
 Course N. 50° 58' 34" E. sec.=0.200906

Log. dist.=3.073645=1184.8 miles.

§ d. Problems in Mercator's sailing may also be solved either by Tables IV. & V., or by the diagram (Plate 1). Thus the mer. diff. lat., and the diff. long., being used on the diagram, or in the tables as diff. lat. and dep., show the course. Then with this course the dist. is found opposite to the actual diff. lat.

§ e. Philadelphia lat.	39° 57' N.	M. parts	2610
Washington city lat.	38° 53' N.	"	2536
	1° 4'	M. diff. lat.=	83
	60		60

Diff. lat.=64 miles.

Washington long.	77° 2' W.
Philadelphia "	75° 9' W.

1° 53'
60

Diff. long.=113 minutes (').

113 in the dep. column stands opposite to 83 in the d. lat. column; (Table V.) 54° is at the bottom of the page. The course then from Philadelphia to Washington is S. 54° W. On the same page 64 in the d. lat. column stands opposite to 109 miles, which is the dist. between the two places.

SURVEYING.

§ 620. In conducting the survey of a coast, harbour, etc., the first object should be to ascertain the geographical position of some point connected with the survey, and the next to establish a *base line*.

§ 621. The most advantageous location for the base line, must be determined by the surveyor himself; and in this, he should be governed by circumstances, such as the nature of the ground about the place to be surveyed, and the place itself.

§ a. A level piece of ground should be selected for the base line, and the line should terminate at points, whence some of the prominent points, headlands, etc., of the place (say a harbour) under survey can be seen.

§ 622. The length of the base line must be ascertained by actual measurement, and the direction in which it lies must be established by observations, and noted down.

§ a. Then, knowing the length of the base line, it serves as a

given side of a triangle, either for determining the length of other lines, or for finding the distance between either end of it, and any point visible from each end of the base.

§ *b*. For if the bearing of such point be taken from each end of the base, a triangle may be formed, in which the angles and the base are known, wherefore (§ 106. § *a*.) the two sides are determinable.

Plate 9. { § 623. The figure in the annexed plate is the *profile* of a harbour, that is being surveyed. A B is the base line, A C B, A D B, etc., are triangles constructed upon it; the angles at A, B, C, D, etc., are measured with a sextant or a theodolite, and the length of the lines B D, B C, A C, etc., is determined by trigonometrical calculation. The principal triangles used, are represented by the broken lines A X, A D, etc.

§ *a*. So that triangles may be constructed from one line to another, until sufficient data are obtained for determining, by trigonometrical calculation, the position of every point of the survey.

§ *b*. The line (X Y) of verification is determined, as to its length, both by trigonometrical calculation, and by measurement, in order to establish the accuracy of the survey.

§ 624. The position of the prominent points C, D, E, F, etc., is determined to a greater degree of nicety in this way, than it can be by taking cross bearings, etc., and the intersection of lines.

§ 625. After the *triangulation* of the survey is completed, and the points C, D, E, F, etc., are laid down upon the chart to the requisite scale; the intermediate spaces, G L, L H, etc., of the shore, may be filled up by the eye. A little practice will enable one to sketch these intermediate spaces with all necessary accuracy.

§ *a*. The position though, of every prominent point, such as light houses, rocks, hills, castles, etc., should be established by actual calculation.

§ *b*. In taking the angles, all the angles of every triangle should be measured whenever it can be done. This affords one means of detecting errors during the work of triangulating; for if the sum (§ 32.) of the three angles of a triangle be not 180° according to the measurement, an error is known to exist.

§ *c*. Also the sum of all the angles around the same point (§ 26.) should be 360° ; and, the sum of all the angles which lie within any measured angle, should be equal (§ 24. § *d*.) to the whole angle.

§ 626. After the work of triangulation is completed, or when it is temporarily suspended, the trigonometrical calculations for the part already triangulated, may be made.

§ 627. The soundings of the harbour should be accurately taken, and correctly laid down upon the chart.

§ *b*. The most practicable way of doing this, is to take a row boat, which will pull equal distances in equal times; establish the position of the point from which she sets out, and let her pull directly for a given point, sounding and noting the soundings at every interval of one, two, three, or more, minutes, as she goes along. When

she arrives at the end of this line, establish the position of this end also, draw the line on the chart, divide it into as many equal parts as there were soundings taken, and write along the line every one at its proper point.

§ *b*. The surest way of making a straight course in the boat, is to bring two points on shore in the same line of bearing, and then pull for them, keeping them in that line. For instance; a boat at *a*, would pull in a straight line to *E*, if she kept a tree, or a steeple, or any object at *b*, in a line with *E*; then the soundings taken would all be on the line *a E*; and the position at *a* being determined; taking the angles *B a E* & *E B a*, the length of *a E* may be known, and the soundings laid down.

§ 628. The soundings should be given for low water; wherefore the time of the tide when the soundings are being taken, should be noted, in order to correct them for low water.

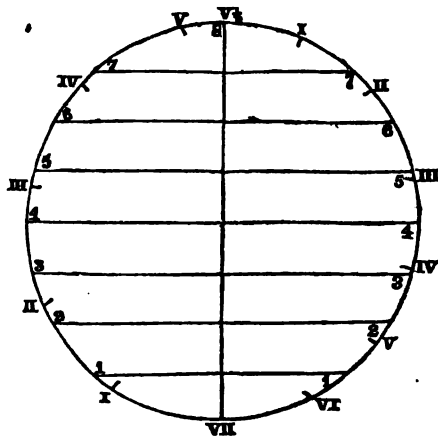
§ *a*. The corrections to be applied may be obtained, either according to the rate of the rise and fall of the tide, as established by previous observation, or by means of a figure (§ *e*.), thus;

§ *b*. Say that the rise and fall of the tide is 8 feet, and that the flood tide lasts $5\frac{1}{2}$ hours, and the ebb, 7.

§ *c*. Let the diameter of a circle be divided into 8 equal parts, by the chords 1, 2, 3, etc. Also let one semicircumference of this circle be divided into $V\frac{1}{2}$ equal parts or hours, to represent the time of flooding; and let the other semicircumference be divided into VII. equal arcs to represent the hours during ebb.

§ *d*. The point in which each of these chords cuts the circle, shows the correction in feet which is to be applied, when the tide is that number of hours, flood or ebb. Thus, when the tide is $III\frac{1}{2}$ flood, the correction to be applied is $4\frac{1}{2}$ feet; and when the tide is III. hours ebb, the correction is 5 feet.*

§ *e*.



* These corrections are always subtractive.

§ 629. The sort of bottom should also be noted down, i. e. mud, rock, sand, etc.

§ 630. The position, extent, etc., of all the hidden dangers, such as rocks, reefs, shoals, banks, and of every other object of importance to the navigator, should be ascertained and laid down.

§ 631. Surveys of harbours are frequently taken by measuring first, a base line, then drawing this line upon the paper at the proportional length to the scale upon which the chart is to be constructed, and then establishing the position of the principal points in the survey, by the intersection of the lines of their bearing from different points.

§ a. But the difficulty of measuring with accuracy the proper angles upon paper, makes this method of taking a survey more liable to inaccuracies, than the triangulating plan.

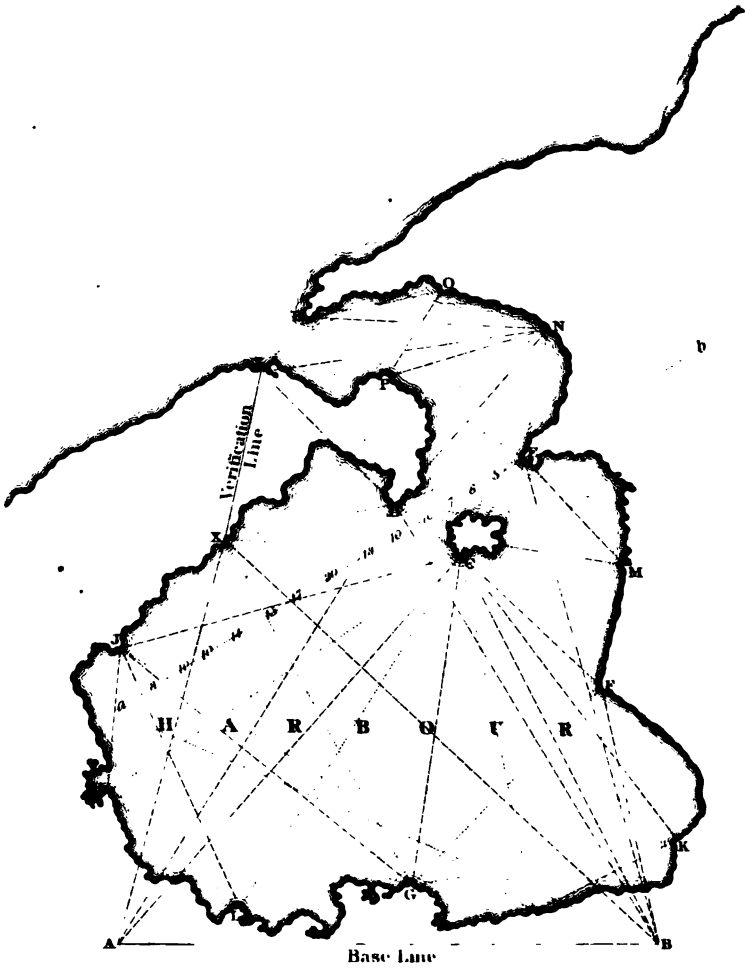


TABLE I.

LOGARITHMS OF NUMBERS

1

TABLE I.

LOGARITHMS OF NUMBERS.

N.	Log.	N.	Log.	N.	Log.	N.	Log.
1	0.000000	25	1.397940	50	1.698970	75	1.875061
2	0.301030	26	1.414973	51	1.707570	76	1.880814
3	0.477121	27	1.431363	52	1.716003	77	1.886491
4	0.602060	28	1.447158	53	1.724976	78	1.892044
		29	1.462398	54	1.732393	79	1.897627
5	0.698970						
6	0.778151	30	1.477121	55	1.740363	80	1.903090
7	0.845098	31	1.491362	56	1.748188	81	1.908484
8	0.903090	32	1.505150	57	1.755875	82	1.913814
9	0.954242	33	1.518514	58	1.763493	83	1.9191078
		34	1.531479	59	1.770852	84	1.924379
10	1.000000						
11	1.041393	35	1.544068	60	1.778151	85	1.929619
12	1.079181	36	1.553092	61	1.785330	86	1.934799
13	1.113743	37	1.558202	62	1.792392	87	1.939919
14	1.146128	38	1.570784	63	1.799340	88	1.944833
		39	1.581064	64	1.806180	89	1.949639
15	1.176091						
16	1.204120	40	1.609060	65	1.812913	90	1.954343
17	1.230449	41	1.613784	66	1.819544	91	1.959041
18	1.255272	42	1.623949	67	1.826075	92	1.963738
19	1.278734	43	1.633469	68	1.832509	93	1.968433
		44	1.643453	69	1.838849	94	1.973128
20	1.301030						
21	1.322219	45	1.653212	70	1.845098	95	1.977724
22	1.342483	46	1.662758	71	1.851258	96	1.982371
23	1.361789	47	1.672098	72	1.857332	97	1.986979
24	1.380211	48	1.681241	73	1.863323	98	1.991526
		49	1.690196	74	1.869232	99	1.996035

TABLE I.—LOG. OF NOS.

N.	0	1	2	3	4	5	6	7	8	9	
100	00	0000	0434	0868	1301	1734	2166	2598	3030	3460	3891
01		4321	4751	5181	5609	6038	6466	6894	7321	7748	8174
02		8600	9026	9451	9876						
	01					0300	0724	1147	1570	1993	2415
03		2837	3259	3680	4100	4521	4940	5360	5779	6197	6616
04		7033	7451	7868	8284	8700	9116	9532	9947		
	02									0061	0776
105		1189	1603	2016	2428	2841	3253	3664	4075	4486	4896
(6		5306	5715	6124	6533	6942	7350	7757	8164	8571	8978
07		9384	9789								
	03		0185	0600	1004	1409	1812	2216	2619	3021	3421
08		3424	3826	4228	4628	5028	5430	5830	6230	6629	7028
09		7427	7825	8223	8620	9017	9414	9811			
	04							0207	0602	0996	
110		1393	1787	2182	2576	2969	3362	3755	4148	4540	4932
11		5323	5714	6105	6495	6885	7275	7664	8053	8442	8830
12		9218	9606								
	05			0380	0766	1152	1538	1924	2309	2694	3079
13		3078	3463	3846	4230	4613	4996	5378	5761	6142	6524
14		6905	7286	7666	8046	8426	8806	9185	9563	9942	
	06										0030
115		0698	1075	1453	1829	2206	2582	2958	3333	3709	4083
16		4458	4832	5206	5580	5953	6326	6699	7071	7443	7815
17		8186	8557	8928	9298						
	07					0036	0407	0777	1145	1514	1882
18		1893	2250	2617	2985	3352	3718	4085	4451	4816	5182
19		5547	5912	6276	6640	7004	7368	7731	8094	8457	8819
	08	9181	9543	9905							
				0266	0636	0967	1347	1707	2067	2426	2786
21		2775	3144	3503	3861	4219	4576	4934	5291	5647	6004
22		6370	6716	7071	7427	7781	8136	8491	8845	9198	9552
23		9905									
	09	0252	0611	0963	1315	1667	2018	2370	2720	3071	3421
24		3422	3772	4122	4471	4820	5169	5518	5867	6215	6562
	10	6910	7257	7604	7951	8297	8644	8990	9335	9681	
26		0370	0715	1059	1403	1747	2091	2434	2777	3119	3462
27		3804	4146	4487	4828	5169	5510	5851	6191	6531	6871
28		7210	7549	7888	8227	8565	8903	9241	9578	9916	
	11	0520	0896	1263	1628	1994	2370	2605	2940	3275	3609
29											3609
130		3043	4277	4611	4944	5278	5610	5943	6276	6608	6940
31		7271	7603	7934	8265	8595	8926	9256	9586	9915	
	12										0245
32		0574	0903	1232	1560	1888	2216	2543	2871	3198	3525
33		3852	4178	4504	4830	5156	5481	5807	6131	6456	6781
34		7105	7429	7753	8076	8399	8722	9045	9368	9690	
	13										0012
135		0334	0655	0977	1298	1619	1939	2260	2580	2900	3219
36		3539	3858	4177	4496	4814	5133	5451	5769	6086	6403
37		6721	7037	7354	7671	7987	8303	8618	8934	9249	9564
38		9879									
	14	0194	0509	0823	1136	1450	1763	2077	2390	2702	3012
39		3015	3327	3638	3951	4263	4574	4885	5196	5507	5818
140		6128	6438	6748	7058	7367	7676	7985	8294	8603	8911
41		9219	9527	9835							
	15			0142	0449	0756	1063	1370	1676	1982	2288
42		2928	3234	3540	3846	4151	4456	4761	5066	5371	5676
43		5336	5640	5943	6246	6549	6852	7154	7457	7759	8061
44		8302	8604	8905	9206	9507					
	16						0168	0469	0769	1068	
145		1368	1667	1967	2266	2564	2863	3161	3460	3757	4055
46		4353	4650	4947	5244	5541	5838	6134	6430	6726	7022
47		7317	7613	7908	8203	8498	8792	9086	9381	9674	9968
48	17	0268	0555	0842	1121	1404	1786	2019	2311	2603	2895
N.	0	1	2	3	4	5	6	7	8	9	

TABLE I.—LOG. OF NOS.

N.	0	1	2	3	4	5	6	7	8	9
140	17 3186	3478	3769	4060	4351	4641	4932	5222	5512	5802
150	6091	6381	6670	6959	7248	7536	7825	8113	8401	8689
51	8977	9265	9552	9839						
52	1844	2139	2435	2730	0126	0413	0699	0986	1272	1558
53	4681	4975	5265	5552	5825	6108	6391	6674	6956	7239
54	7521	7803	8084	8366	8647	8928	9210	9490	9771	0051
155	0339	0612	0892	1172	1451	1730	2010	2289	2568	2846
56	3125	3403	3681	3959	4232	4514	4792	5069	5346	5622
57	5000	6178	6452	6727	7005	7281	7556	7832	8107	8382
58	8657	8932	9206	9481	9755					
59	1397	1670	1943	2216	2488	0029	0303	0577	0851	1124
160	4190	4391	4662	4934	5204	5475	5746	6016	6286	6556
61	6926	7036	7365	7634	7904	8173	8441	8710	8979	9247
62	9515	9783								
63	2188	2454	2720	2986	3252	3518	3783	4049	4314	4579
64	4844	5109	5373	5638	5902	6166	6430	6694	6957	7221
165	7484	7747	8010	8273	8536	8798	9060	9323	9585	9846
66	0108	0370	0631	0892	1153	1414	1675	1936	2196	2456
67	2717	2978	3236	3496	3755	4015	4274	4533	4792	5051
68	5309	5578	5826	6084	6342	6600	6858	7115	7372	7630
69	7867	8144	8400	8657	8913	9170	9426	9682	9938	0193
170	0449	0704	0960	1215	1470	1724	1979	2233	2488	2742
71	2396	3250	3504	3757	4011	4264	4517	4770	5023	5275
72	5523	5781	6033	6285	6537	6789	7041	7292	7544	7795
73	8046	8297	8548	8799	9049	9300	9550	9800	0050	0300
74	0549	0799	1048	1297	1547	1795	2044	2293	2541	2790
175	3038	3286	3534	3782	4030	4277	4525	4772	5019	5266
76	5513	5753	6006	6252	6499	6745	6991	7236	7482	7728
77	7973	8219	8464	8709	8954	9198	9443	9687	9932	0178
78	0420	0664	0908	1151	1395	1638	1882	2125	2368	2610
79	2853	3096	3338	3580	3822	4064	4305	4548	4790	5031
180	5273	5514	5755	5996	6237	6477	6718	6959	7198	7437
81	7679	7919	8158	8398	8637	8877	9116	9355	9594	9833
82	0071	0310	0548	0787	1025	1263	1501	1738	1976	2214
83	2451	2688	2926	3162	3399	3636	3873	4110	4346	4582
84	4818	5054	5290	5525	5761	5996	6232	6467	6702	6937
185	7172	7406	7641	7875	8110	8344	8578	8812	9046	9279
86	9513	9746	9980							
87	1942	2074	2205	2337	2470	2601	2733	2864	2996	3127
88	4158	4389	4620	4850	5081	5311	5542	5772	6002	6232
89	6462	6692	6921	7151	7380	7609	7838	8067	8296	8525
190	8754	8982	9210	9439	9667	9895				
91	1073	1261	1448	1715	1942	2169	0123	0351	0578	0806
92	3301	3527	3753	3979	4205	4431	4656	4882	5107	5332
93	5557	5782	6007	6232	6457	6681	6905	7130	7354	7578
94	7802	8025	8249	8473	8696	8920	9143	9366	9589	9812
195	0075	0257	0420	0702	0925	1147	1369	1591	1813	2034
96	2256	2478	2699	2920	3142	3363	3584	3804	4025	4246
97	4466	4687	4907	5127	5347	5567	5787	6007	6226	6446
98	6675	6894	7104	7321	7542	7761	7979	8198	8416	8635
99	8853	9071	9289	9507	9725	9943				
200	1070	1247	1444	1681	1896	2114	2331	2547	2764	2980
01	3196	3412	3628	3844	4060	4275	4490	4706	4921	5136
N.	0	1	2	3	4	5	6	7	8	9

TABLE I.—LOG. OF Nos.

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202	30	5351	5506	5781	5906	6211	6425	6639	6854	7068	7282
03		74J6	7710	7994	8137	8351	8564	8778	8991	9204	9417
04		9630	9843								
	31			0056	0268	0481	0693	0906	1118	1330	1542
205		1754	1966	2177	2389	2600	2812	3023	3234	3445	3656
06		3867	4078	4289	4499	4710	4920	5130	5340	5551	5761
07		5770	6180	6390	6599	6801	7018	7237	7457	7676	7894
08		8063	8272	8481	8689	8898	9106	9314	9523	9730	9938
09	32	0146	0354	0562	0769	0977	1184	1391	1598	1806	2013
210		2219	2426	2633	2839	3046	3252	3458	3665	3871	4077
11		4283	4488	4694	4900	5105	5310	5516	5721	5926	6131
12		6336	6541	6745	6950	7154	7359	7563	7767	7972	8176
13		8390	8593	8797	8991	9194	9398	9601	9805		
	33									0008	0211
14		0414	0617	0819	1022	1225	1427	1630	1832	2034	2236
215		2439	2640	2842	3044	3246	3447	3649	3850	4051	4253
16		4454	4655	4856	5056	5257	5458	5657	5859	6059	6259
17		6460	6660	6860	7060	7260	7453	7659	7858	8058	8257
18		8457	8656	8855	9054	9253	9451	9650	9849		
	34									0047	0246
19		0444	0642	0841	1039	1237	1435	1633	1830	2028	2225
220		2423	2620	2817	3014	3212	3409	3606	3802	3999	4196
21		4392	4589	4785	4981	5178	5374	5570	5766	5962	6157
22		6353	6549	6744	6939	7135	7330	7525	7720	7915	8110
23		8305	8500	8694	8889	9083	9277	9472	9666	9860	
	35										0054
24		0248	0443	0638	0832	1027	1216	1410	1603	1796	1989
225		2182	2376	2568	2761	2954	3147	3339	3532	3724	3916
26		4108	4301	4493	4685	4876	5068	5260	5452	5643	5835
27		6026	6217	6408	6599	6791	6981	7173	7363	7554	7744
28		7935	8125	8316	8506	8696	8886	9076	9266	9456	9646
29		9636									
	36		0025	0215	0404	0593	0783	0973	1161	1350	1539
230		1738	1917	2105	2294	2483	2671	2859	3048	3236	3424
31		3612	3800	3988	4176	4363	4551	4739	4926	5113	5301
32		5488	5675	5862	6049	6236	6423	6610	6796	6983	7170
33		7356	7542	7729	7915	8101	8287	8473	8659	8845	9030
34		9216	9401	9587	9772	9958					
	37						0143	0338	0513	0688	0863
235		1058	1233	1437	1622	1807	1991	2175	2360	2544	2729
36		2112	2286	2460	2634	2807	2981	3154	3328	3501	3675
37		4748	4922	5115	5288	5461	5634	5807	5980	6152	6324
38		6577	6759	6942	7124	7306	7488	7670	7852	8034	8216
39		8398	8580	8761	8943	9124	9306	9487	9668	9849	0030
	38										
240		0211	0392	0573	0754	0935	1115	1296	1476	1656	1837
41		2017	2197	2377	2557	2737	2917	3097	3277	3456	3636
42		3815	3995	4174	4353	4533	4712	4891	5070	5249	5428
43		5104	5283	5462	5641	5820	6000	6179	6358	6537	6716
44		7390	7568	7746	7923	8101	8279	8457	8634	8811	8989
245		9166	9343	9521	9698	9875					
	39						0052	0228	0405	0582	0759
46		0235	1112	1289	1464	1641	1817	1993	2169	2345	2521
47		2697	2873	3048	3224	3400	3575	3751	3926	4101	4277
48		4452	4627	4802	4977	5152	5326	5501	5676	5850	6025
49		6199	6374	6548	6723	6896	7071	7245	7419	7592	7766
250		7940	8114	8287	8461	8634	8808	8981	9154	9327	9501
51		9674	9847								
	40			0090	0192	0265	0338	0411	0483	0556	0628
52		1400	1573	1745	1917	2089	2261	2433	2605	2777	2949
53		3121	3292	3464	3635	3807	3978	4149	4321	4492	4663
54		4834	5005	5176	5346	5517	5688	5858	6029	6199	6370
255		6540	6711	6881	7051	7221	7391	7561	7731	7901	8070
N.	0	1	2	3	4	5	6	7	8	9	

TABLE I.—LOG. OF NOS.

N.	0	1	2	3	4	5	6	7	8	9
256	40 8940	8410	8579	8749	8918	9087	9257	9426	9595	9764
57	9933									
58	41 1690	0102	0271	0440	0608	0777	0946	1114	1283	1451
59	3300	1788	1956	2124	2293	2461	2628	2796	2964	3132
260	4973	5140	5307	5474	5641	5808	5974	6141	6308	6474
61	0640	6607	6773	7139	7306	7472	7638	7804	7970	8135
62	8301	8467	8633	8798	8964	9129	9295	9460	9625	9791
63	9956									
64	42 1604	0121	0286	0451	0616	0781	0945	1110	1275	1439
265	3946	3410	3573	3737	3901	4064	4228	4392	4555	4718
66	4922	5045	5208	5371	5534	5697	5860	6023	6186	6349
67	6511	6674	6837	6999	7161	7324	7486	7648	7811	7973
68	8135	8297	8459	8621	8783	8944	9106	9268	9429	9591
69	9752	9914								
270	1364	1525	1685	1846	2007	2167	2328	2488	2649	2809
71	2269	2430	2590	2750	2910	3070	3230	3390	3549	3709
72	4569	4728	4888	5048	5207	5367	5526	5685	5844	6004
73	6163	6322	6481	6640	6799	6957	7116	7275	7433	7592
74	7751	7909	8067	8226	8384	8542	8701	8859	9017	9175
275	8333	9491	9648	9806	9964					
76	0909	1066	1224	1381	1538	1695	1852	2009	2166	2323
77	2470	2627	2783	2940	3097	3253	3410	3567	3723	3880
78	4045	4201	4357	4513	4669	4825	4981	5137	5292	5449
79	5604	5760	5915	6071	6226	6382	6537	6693	6848	7003
280	7158	7313	7468	7623	7778	7933	8088	8242	8397	8552
81	8706	8861	9015	9170	9324	9478	9633	9787	9941	
82	0949	0403	0557	0711	0865	1018	1172	1326	1479	1633
83	1786	1940	2093	2247	2400	2553	2706	2859	3012	3165
84	3328	3471	3624	3777	3930	4082	4235	4387	4540	4692
285	4845	4997	5150	5302	5454	5606	5758	5910	6062	6214
86	6366	6518	6670	6821	6973	7125	7276	7428	7579	7731
87	7892	8043	8194	8346	8497	8648	8799	8950	9101	9252
88	9392	9543	9694	9845	9995					
89	0896	1048	1198	1348	1499	1649	1799	1949	2098	2248
290	2396	2548	2697	2847	2997	3146	3296	3445	3594	3744
91	3623	4042	4191	4341	4490	4639	4787	4936	5085	5234
92	5383	5532	5680	5829	5977	6126	6274	6423	6571	6719
93	6968	7016	7164	7312	7460	7608	7756	7904	8052	8200
94	8347	8495	8643	8790	8938	9085	9233	9380	9528	9675
295	9822	9969								
96	1292	1436	0116	0263	0411	0557	0704	0851	0998	1145
97	2756	2903	1525	1732	1878	2025	2171	2317	2464	2610
98	4916	4369	3049	3195	3341	3487	3633	3779	3925	4070
99	5671	5816	4508	4653	4799	4944	5090	5235	5381	5526
300	7191	7266	5962	6107	6252	6397	6542	6687	6832	6977
01	8267	7866	7411	7555	7700	7845	7989	8133	8278	8422
02	0007	8711	8855	8999	9143	9287	9431	9575	9719	9863
03	1443	0151	0295	0438	0582	0725	0869	1012	1156	1300
04	2874	1586	1729	1872	2016	2159	2302	2445	2588	2731
305	4300	3016	3159	3302	3445	3587	3730	3873	4015	4157
06	5721	4442	4585	4727	4869	5011	5153	5295	5438	5579
07	7139	5853	6003	6147	6289	6431	6572	6714	6855	6997
08	8551	7260	7421	7563	7704	7845	7986	8128	8269	8410
09	9458	8092	8253	8374	8514	8655	8796	8937	9077	9218
310	1292	0990	0940	0380	0580	0661	0801	0941	1081	1222
N.	0	1	2	3	4	5	6	7	8	9

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311	49	2760	2900	3040	3179	3319	3458	3597	3737	3876	4015
12		4155	4294	4433	4572	4711	4850	4989	5128	5267	5406
13		5544	5683	5822	5960	6099	6237	6376	6515	6653	6791
14		6930	7068	7206	7344	7482	7621	7759	7897	8035	8173
315		8311	8448	8586	8724	8862	8999	9137	9275	9412	9550
16		9687	9825	9962							
	50			0090	0236	0374	0511	0648	0785	0922	
17		1059	1196	1333	1470	1607	1744	1881	2017	2154	2291
18		2427	2564	2700	2837	2973	3109	3246	3382	3518	3654
19		3791	3927	4063	4199	4335	4471	4607	4743	4878	5014
320		5150	5286	5421	5557	5692	5828	5964	6099	6234	6370
21		6505	6640	6776	6911	7046	7181	7316	7451	7586	7721
22		7856	7991	8126	8260	8395	8530	8664	8799	8934	9068
23		9203	9337	9471	9606	9740					
24	51	0545	0679	0813	0947	1081	1215	1349	1482	1616	1750
325		1863	2017	2150	2284	2418	2551	2684	2818	2951	3084
26		3218	3351	3484	3617	3750	3883	4016	4149	4282	4415
27		4548	4681	4813	4946	5079	5211	5344	5476	5608	5741
28		5874	6006	6138	6271	6403	6535	6668	6800	6932	7064
29		7196	7328	7460	7592	7724	7855	7987	8119	8251	8382
330		8514	8646	8777	8909	9040	9172	9303	9434	9566	9697
31		9828	9959								
	52		0090	0231	0372	0513	0653	0794	0935	1076	1217
32		1138	1280	1420	1561	1702	1842	1983	2123	2264	2405
33		2444	2575	2705	2835	2966	3096	3226	3356	3486	3616
34		3747	3877	4006	4136	4266	4396	4526	4656	4785	4915
335		5045	5174	5304	5434	5563	5693	5822	5951	6081	6210
36		6339	6469	6598	6727	6856	6985	7114	7243	7372	7501
37		7630	7759	7888	8017	8145	8274	8402	8531	8660	8788
38		8917	9045	9174	9302	9430	9559	9687	9815	9943	
39	53	0300	0338	0456	0584	0712	0840	0968	1096	1223	1351
340		1479	1607	1734	1862	1990	2117	2245	2372	2500	2627
41		2754	2882	3009	3136	3263	3391	3518	3645	3772	3899
42		4026	4153	4280	4407	4534	4661	4787	4914	5041	5168
43		5394	5491	5547	5674	5800	5927	6053	6180	6306	6432
44		6558	6685	6811	6937	7063	7189	7315	7441	7567	7693
345		7819	7945	8071	8197	8322	8448	8574	8699	8825	8951
46		9076	9202	9327	9453	9578	9703	9829	9954		
47	54	0330	0455	0580	0705	0830	0955	1080	1205	1330	1454
48		1579	1704	1829	1953	2078	2203	2327	2452	2577	2701
49		2825	2950	3074	3199	3323	3447	3571	3696	3820	3944
350		4068	4192	4316	4440	4564	4688	4812	4936	5060	5183
51		5307	5431	5555	5678	5802	5925	6049	6172	6296	6419
52		6543	6666	6789	6913	7036	7159	7282	7405	7528	7651
53		7775	7898	8021	8144	8266	8389	8512	8635	8758	8881
54		9003	9126	9249	9371	9494	9616	9739	9861	9984	
	55										0106
355		0298	0351	0473	0595	0717	0840	0962	1084	1206	1328
56		1450	1579	1694	1816	1938	2060	2182	2303	2425	2547
57		2668	2790	2919	3033	3155	3276	3398	3519	3640	3762
58		3883	4004	4126	4247	4368	4489	4610	4731	4852	4974
59		5094	5215	5336	5457	5578	5699	5820	5940	6061	6182
360		6302	6423	6544	6664	6785	6905	7026	7146	7267	7387
61		7507	7628	7748	7868	7988	8108	8228	8348	8468	8588
62		8709	8829	8948	9068	9188	9308	9428	9548	9667	9787
63		9907									
	56		0026	0146	0265	0385	0504	0624	0743	0863	0982
64		1101	1221	1340	1459	1578	1697	1817	1936	2055	2174
365		2293	2412	2531	2650	2769	2887	3006	3125	3244	3363
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TABLE I.—LOG. OF NOS.

N.	0	1	2	3	4	5	6	7	8	9	
366	56	3481	3600	3718	3837	3956	4074	4192	4311	4429	4548
67		4668	4784	4903	5021	5139	5257	5376	5494	5612	5730
68		5848	5966	6084	6202	6320	6438	6555	6673	6791	6909
69		7036	7154	7272	7390	7507	7624	7742	7859	7977	8094
370		8209	8310	8436	8554	8671	8788	8905	9023	9140	9257
71		9374	9491	9608	9725	9842	9959				
	57							0076	0193	0309	0426
72		0543	0660	0776	0893	1010	1126	1243	1359	1476	1592
73		1709	1825	1942	2058	2174	2291	2407	2523	2639	2756
74		2873	2988	3104	3220	3336	3452	3568	3684	3800	3915
375		4031	4147	4263	4379	4494	4610	4726	4841	4957	5072
76		5188	5303	5419	5534	5650	5765	5880	5996	6111	6226
77		6341	6456	6572	6687	6802	6917	7032	7147	7262	7377
78		7492	7607	7722	7838	7953	8068	8183	8298	8413	8528
79		8639	8754	8868	8983	9097	9212	9326	9441	9555	9669
380		9784	9898								
	58			0019	0136	0240	0355	0469	0583	0697	0811
81		0925	1039	1153	1267	1381	1495	1608	1722	1836	1950
82		2063	2177	2291	2404	2518	2631	2745	2859	2972	3085
83		3199	3312	3426	3539	3652	3765	3879	3992	4105	4218
84		4331	4444	4557	4670	4783	4896	5009	5122	5235	5348
385		5461	5574	5686	5799	5912	6024	6137	6250	6362	6475
86		6597	6700	6812	6925	7037	7150	7262	7374	7487	7599
87		7711	7823	7935	8047	8160	8272	8384	8496	8608	8720
88		8833	8944	9055	9167	9279	9391	9503	9615	9726	9838
89		9950									
	59		0061	0173	0284	0396	0508	0619	0730	0842	0953
390		1065	1176	1287	1399	1510	1621	1732	1843	1955	2066
91		2177	2288	2399	2510	2621	2732	2843	2954	3064	3175
92		3286	3397	3508	3618	3729	3840	3950	4061	4172	4282
93		4393	4503	4614	4724	4834	4945	5055	5165	5275	5385
94		5496	5606	5717	5827	5937	6047	6157	6267	6377	6487
395		6597	6707	6817	6927	7037	7146	7256	7366	7476	7586
96		7695	7805	7914	8024	8134	8243	8353	8462	8572	8681
97		8791	8900	9009	9119	9228	9337	9446	9556	9665	9774
98		9883	9992								
	60		0101	0210	0319	0428	0537	0646	0755	0864	0974
99		0973	1082	1191	1300	1408	1517	1625	1734	1843	1951
400		2060	2169	2277	2386	2494	2602	2711	2819	2928	3036
01		3144	3253	3361	3469	3577	3686	3794	3902	4010	4118
02		4226	4334	4442	4550	4658	4766	4874	4982	5090	5197
03		5305	5413	5520	5628	5736	5843	5951	6059	6166	6274
04		6361	6469	6576	6684	6791	6899	7006	7113	7221	7328
405		7455	7562	7670	7777	7884	7991	8098	8205	8312	8419
06		8586	8693	8740	8847	8954	9060	9167	9274	9381	9488
07		9594	9701	9808	9914						
	61					0021	0129	0234	0341	0447	0554
08		0660	0767	0873	0979	1086	1192	1308	1405	1511	1617
09		1723	1830	1936	2042	2148	2254	2360	2466	2572	2678
410		2784	2890	2996	3102	3207	3313	3419	3525	3630	3736
11		3843	3948	4053	4159	4264	4370	4475	4581	4686	4791
12		4897	5003	5108	5213	5319	5424	5529	5635	5740	5845
13		5950	6055	6160	6265	6370	6476	6581	6686	6791	6896
14		7000	7105	7210	7315	7420	7525	7630	7734	7839	7943
415		8048	8153	8257	8362	8467	8571	8676	8780	8884	8989
16		9093	9198	9302	9406	9511	9615	9719	9823	9928	
	62										0032
17		0136	0240	0344	0448	0552	0657	0760	0864	0968	1072
18		1176	1280	1384	1488	1592	1695	1799	1903	2007	2110
19		2214	2318	2421	2525	2628	2732	2836	2939	3042	3146
420		3249	3353	3456	3559	3663	3766	3869	3973	4076	4179
21		4282	4385	4488	4591	4695	4798	4901	5004	5107	5210
22		5313	5415	5518	5621	5724	5827	5930	6033	6135	6238
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422	62 6340	6443	6546	6648	6751	6853	6956	7059	7161	7263
94	7368	7468	7571	7673	7775	7878	7980	8082	8184	8287
425	8389	8491	8593	8695	8797	8899	9002	9104	9206	9308
96	9410	9512	9613	9715	9817	9919				
	63						0081	0183	0284	0386
97	0408	0530	0631	0733	0835	0936	1038	1139	1241	1342
98	1444	1545	1647	1748	1849	1951	2052	2153	2255	2356
99	2457	2559	2660	2761	2862	2963	3064	3165	3266	3367
430	3469	3569	3670	3771	3872	3973	4074	4175	4276	4377
31	4477	4578	4679	4780	4880	4981	5081	5182	5283	5383
32	5484	5584	5685	5785	5886	5986	6086	6187	6287	6388
33	6488	6588	6688	6789	6889	6989	7089	7189	7290	7390
34	7490	7590	7690	7790	7890	7990	8090	8190	8290	8390
435	8490	8590	8690	8790	8890	8990	9090	9190	9290	9390
36	9487	9586	9686	9785	9885	9984				
	64						0084	0183	0283	0388
37	0481	0581	0680	0780	0879	0978	1077	1176	1276	1375
38	1474	1573	1672	1771	1871	1970	2069	2168	2267	2366
39	2465	2563	2662	2761	2860	2959	3058	3157	3255	3354
440	3453	3551	3650	3749	3847	3946	4044	4143	4242	4340
41	4439	4537	4636	4734	4832	4931	5029	5127	5226	5324
42	5425	5523	5621	5719	5817	5915	6013	6111	6209	6308
43	6404	6502	6600	6698	6796	6894	6992	7089	7187	7285
44	7383	7481	7579	7676	7774	7872	7969	8067	8165	8262
445	8360	8458	8555	8653	8750	8848	8945	9043	9140	9237
46	9335	9432	9530	9627	9724	9822	9919			
	65							0016	0113	0210
47	0307	0405	0502	0599	0696	0793	0890	0987	1084	1181
48	1278	1375	1472	1569	1666	1762	1859	1956	2053	2150
49	2246	2343	2440	2536	2633	2730	2826	2923	3019	3116
480	3219	3300	3406	3502	3598	3695	3791	3888	3984	4080
51	4177	4273	4369	4465	4562	4658	4754	4850	4946	5042
52	5136	5232	5331	5427	5523	5619	5715	5811	5906	6002
53	6096	6194	6290	6386	6482	6577	6673	6769	6865	6960
54	7056	7152	7247	7343	7438	7534	7629	7725	7821	7916
455	8011	8107	8202	8298	8393	8489	8584	8679	8774	8870
56	8965	9060	9155	9250	9346	9441	9536	9631	9726	9821
57	9916									
	66							0086	0181	0276
58	0386	0480	0575	0670	0765	0860	0955	1050	1145	1240
59	1333	1427	1521	1615	1709	1803	1897	1991	2085	2179
460	2272	2365	2458	2551	2644	2737	2830	2923	3016	3109
61	3081	3173	3265	3357	3449	3541	3633	3725	3816	3908
62	4019	4110	4201	4292	4383	4474	4565	4656	4747	4838
63	5001	5091	5181	5271	5361	5451	5541	5631	5721	5811
64	6001	6091	6181	6271	6361	6451	6541	6631	6721	6811
465	7453	7546	7640	7733	7826	7920	8013	8106	8200	8293
66	8386	8479	8572	8665	8758	8851	8945	9038	9131	9224
67	9317	9410	9503	9596	9689	9782	9875	9967		
	67								0066	0153
68	0246	0339	0431	0524	0617	0710	0802	0895	0988	1080
69	1173	1265	1358	1451	1543	1636	1728	1821	1913	2005
470	2008	2100	2193	2285	2377	2469	2561	2653	2744	2837
71	3081	3173	3265	3357	3449	3541	3633	3725	3816	3908
72	3942	4034	4126	4218	4310	4402	4494	4586	4677	4769
73	4811	4903	5045	5137	5228	5320	5411	5503	5595	5687
74	5778	5870	5962	6053	6145	6236	6328	6419	6511	6602
475	6604	6705	6806	6908	7009	7110	7211	7312	7413	7514
76	7607	7708	7809	7911	8012	8113	8214	8315	8416	8517
77	8518	8619	8720	8821	8922	9023	9124	9225	9326	9427
78	9428	9529	9630	9731	9832	9933				
	68							0063	0154	0245
79	0336	0428	0517	0607	0698	0789	0879	0970	1060	1151
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TABLE I.—LOG. OF NOS.

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80	1941	1399	1459	1513	1603	1693	1794	1874	1965	2065
81	2145	2235	2295	2416	2506	2596	2696	2777	2867	2957
82	3047	3137	3237	3317	3407	3497	3597	3677	3767	3857
83	3947	4037	4137	4217	4307	4396	4486	4576	4666	4756
84	4845	4935	5035	5115	5205	5294	5383	5473	5563	5653
85	5748	5831	5921	6010	6100	6189	6279	6368	6458	6547
86	6636	6726	6815	6904	6994	7083	7173	7261	7351	7440
87	7390	7481	7570	7659	7748	7837	7926	8015	8104	8193
88	8490	8580	8669	8758	8847	8936	9025	9114	9203	9292
89	9300	9388	9476	9565	9654	9743	9831	9920		
	60								0019	0107
90	0196	0285	0373	0462	0551	0639	0728	0816	0905	0993
91	1082	1170	1258	1347	1435	1524	1612	1700	1789	1877
92	1965	2053	2142	2230	2318	2406	2494	2583	2671	2759
93	2847	2935	3023	3111	3199	3287	3375	3463	3551	3639
94	3737	3825	3913	3991	4078	4166	4254	4342	4430	4517
95	4605	4693	4781	4868	4956	5044	5131	5219	5307	5394
96	5482	5569	5657	5744	5832	5919	6007	6094	6182	6269
97	6356	6444	6531	6619	6706	6793	6880	6968	7055	7143
98	7319	7407	7494	7581	7668	7755	7843	7930	8018	8105
99	8101	8188	8275	8362	8449	8536	8623	8710	8797	8883
500	8970	9057	9144	9231	9317	9404	9491	9578	9664	9751
01	9838	9924								
02	0704	0790	0877	0963	1050	1136	1222	1309	1395	1482
03	1568	1654	1741	1827	1913	2000	2086	2172	2258	2344
04	2420	2517	2603	2689	2775	2861	2947	3033	3119	3205
05	3261	3377	3463	3549	3635	3721	3807	3893	3979	4065
06	4151	4236	4322	4408	4494	4579	4665	4751	4837	4922
07	5008	5094	5179	5265	5351	5436	5522	5607	5693	5778
08	5864	5949	6035	6120	6206	6291	6376	6462	6547	6632
09	6718	6803	6888	6974	7059	7144	7229	7315	7400	7485
510	7570	7655	7741	7826	7911	7996	8081	8166	8251	8336
11	8491	8576	8661	8746	8831	8916	9001	9086	9171	9256
12	9270	9355	9440	9524	9609	9694	9779	9863	9948	
13	71	0117	0202	0287	0371	0456	0540	0625	0710	0794
14	0863	1048	1133	1217	1301	1385	1470	1554	1638	1723
515	1807	1891	1976	2060	2144	2229	2313	2397	2481	2566
16	2650	2734	2818	2902	2986	3070	3154	3238	3322	3407
17	3491	3575	3659	3743	3827	3910	3994	4078	4162	4246
18	4390	4474	4558	4642	4726	4809	4893	4976	5060	5144
19	5167	5251	5335	5418	5502	5586	5669	5753	5836	5920
520	6003	6087	6170	6254	6337	6421	6504	6588	6671	6754
21	6838	6921	7004	7088	7171	7254	7338	7421	7504	7587
22	7670	7754	7837	7920	8003	8086	8169	8252	8335	8418
23	8509	8592	8675	8758	8841	8924	9007	9090	9173	9256
24	9331	9414	9497	9580	9663	9746	9829	9911	9994	
	72									0077
25	0159	0242	0325	0407	0490	0573	0655	0738	0821	0903
26	0986	1068	1151	1233	1316	1398	1481	1563	1646	1729
27	1811	1893	1975	2058	2140	2222	2304	2387	2469	2552
28	2634	2716	2798	2881	2963	3045	3127	3209	3291	3374
29	3456	3538	3620	3702	3784	3866	3948	4030	4112	4194
300	4276	4358	4440	4522	4603	4685	4767	4849	4931	5013
31	5004	5086	5168	5249	5330	5412	5493	5575	5656	5738
32	5819	5901	5982	6063	6144	6225	6306	6387	6468	6549
33	6737	6818	6899	6979	7060	7141	7221	7302	7383	7464
34	7341	7422	7502	7583	7663	7744	7824	7905	7985	8066
525	8354	8435	8515	8596	8676	8757	8837	8918	9000	9084
35	9165	9245	9325	9405	9485	9565	9645	9725	9805	9885
37	9974									
	73	0065	0136	0217	0298	0379	0459	0540	0621	0701
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TABLE I.—LOG. OF NOS.

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538	73 07:2	0883	0444	1024	1105	1186	1266	1347	1428	1508
39	15:9	1609	1750	1830	1911	1991	2072	2153	2233	1.313
540	2384	2474	2555	2635	2715	2796	2876	2956	3037	3117
41	3197	3278	3358	3438	3518	3598	3679	3759	3839	3919
42	3999	4079	4160	4240	4320	4400	4480	4560	4640	4720
43	4800	48:0	4900	5040	5120	5200	5280	5360	5440	5520
44	5599	5679	5758	5838	5918	5998	6078	6157	6237	6317
545	6397	6476	6556	6636	6715	6795	6874	6954	7034	7113
46	7193	7272	7352	7431	7511	7590	7670	7749	7829	7908
47	79:7	80:7	8146	8225	8305	8384	8463	8543	8622	8701
48	8781	8860	8939	9018	9097	9177	9256	9335	9414	9493
49	9573	9651	9731	9810	9889	9968				
	74						0047	0126	0205	0284
550	0363	0442	0521	0600	0678	0757	0836	0915	0994	1073
51	1153	1230	1309	1388	1467	1546	1624	1703	1782	1860
52	1930	2018	2096	2175	2254	2332	2411	2490	2568	2647
53	2725	2804	2882	2961	3039	3118	3196	3274	3353	3431
54	3510	3588	3667	3745	3823	3902	3980	4058	4137	4215
555	4293	4371	4450	4528	4606	4684	4763	4841	4919	4997
56	5075	5153	5231	5309	5387	5465	5543	5621	5699	5777
57	5855	5933	6011	6089	6167	6245	6323	6401	6479	6557
58	6634	6712	6790	6868	6945	7023	7101	7179	7257	7334
59	7413	7490	7567	7645	7723	7800	7878	7955	8033	8111
500	8198	8276	8354	8431	8508	8586	8663	8741	8818	8895
61	8963	9040	9118	9195	9272	9350	9427	9504	9581	9658
62	9736	9814	9891	9968						
	75				0045	0122	0200	0277	0354	0431
63	0508	0585	0663	0740	0817	0894	0971	1048	1125	1202
64	1279	1356	1433	1510	1587	1664	1741	1818	1895	1972
565	2048	2125	2202	2279	2356	2433	2509	2586	2663	2740
66	2816	2893	2970	3047	3123	3200	3277	3353	3430	3507
67	3583	3660	3736	3813	3889	3966	4042	4119	4195	4272
68	4348	4425	4501	4578	4654	4731	4807	4883	4960	5036
69	5112	5189	5265	5341	5417	5494	5570	5646	5722	5798
570	5875	5951	6027	6103	6180	6256	6332	6408	6484	6560
71	6636	6712	6788	6864	6940	7016	7092	7168	7244	7320
72	7396	7472	7548	7624	7700	7776	7851	7927	8003	8079
73	8155	8230	8306	8382	8458	8533	8609	8685	8761	8836
74	8912	8988	9063	9139	9214	9290	9366	9441	9517	9592
575	9668	9743	9819	9894	9970					
	76					0045	0121	0196	0272	0347
76	0422	0498	0573	0649	0724	0799	0875	0950	1025	1100
77	1176	1251	1326	1402	1477	1552	1627	1702	1777	1852
78	1928	2003	2078	2153	2228	2303	2378	2453	2528	2603
79	2679	2754	2829	2903	2979	3053	3128	3203	3278	3353
580	3428	3503	3578	3653	3727	3802	3877	3952	4027	4101
81	4176	4251	4326	4400	4475	4550	4624	4699	4774	4848
82	4893	4968	5042	5117	5191	5266	5340	5415	5489	5563
83	5609	5743	5817	5892	5966	6041	6115	6190	6264	6338
84	6413	6487	6561	6636	6710	6785	6859	6933	7007	7081
585	7156	7230	7304	7378	7453	7527	7601	7675	7749	7823
86	7898	7972	8046	8120	8194	8268	8342	8416	8490	8564
87	86:36	8712	8786	8860	8934	9008	9082	9156	9230	9304
88	9377	9451	9525	9599	9673	9747	9820	9894	9968	
	77									
89	0115	0189	0263	0336	0410	0484	0558	0631	0705	0778
590	0852	0926	0999	1073	1146	1220	1293	1367	1441	1514
91	1587	1661	1734	1808	1881	1955	2028	2102	2175	2248
92	2292	2365	2438	2511	2584	2657	2730	2803	2876	2949
93	3055	3128	3201	3274	3347	3420	3493	3566	3639	3712
94	3786	3859	3932	4005	4078	4151	4224	4297	4370	4443
595	4517	4590	4663	4736	4809	4882	4955	5028	5100	5173
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N.	0	1	2	3	4	5	6	7	8	9
506	77 5946	5319	5392	5465	5538	5610	5683	5756	5829	5902
97	5974	6047	6120	6192	6265	6338	6411	6483	6556	6629
98	6701	6774	6846	6919	6992	7064	7137	7209	7282	7354
99	7487	7499	7572	7644	7717	7789	7862	7934	8007	8079
600	8151	8224	8296	8368	8441	8513	8585	8658	8730	8802
01	8775	8847	8919	9001	9103	9206	9308	9390	9452	9524
02	9597	9669	9741	9813	9885	9957				
03	78 0317	0389	0461	0533	0605	0677	0749	0821	0893	0965
04	1037	1109	1181	1253	1325	1396	1468	1540	1612	1684
605	1755	1827	1899	1971	2043	2114	2186	2258	2329	2401
06	2473	2544	2616	2688	2759	2831	2902	2974	3046	3117
07	3189	3260	3332	3403	3475	3546	3618	3689	3761	3832
08	3904	3975	4046	4118	4189	4261	4332	4403	4475	4546
09	4617	4689	4760	4831	4902	4974	5045	5116	5187	5259
610	5330	5401	5472	5543	5615	5686	5757	5828	5899	5970
11	6041	6112	6183	6254	6325	6396	6468	6538	6609	6680
12	6751	6822	6893	6964	7035	7106	7177	7248	7319	7390
13	7461	7531	7602	7673	7744	7815	7885	7956	8027	8098
14	8168	8239	8310	8381	8451	8522	8593	8663	8734	8805
615	8875	8946	9016	9087	9158	9228	9299	9369	9440	9510
16	9581	9651	9722	9792	9863	9933				
17	79 0285	0356	0426	0496	0567	0637	0707	0778	0848	0918
18	0988	1059	1129	1199	1270	1340	1410	1480	1550	1620
19	1691	1761	1831	1901	1971	2041	2111	2182	2252	2322
620	2372	2442	2512	2582	2652	2722	2792	2862	2932	3002
21	3092	3162	3231	3301	3371	3441	3511	3581	3651	3721
22	3770	3840	3910	4000	4070	4130	4200	4270	4340	4418
23	4488	4558	4627	4697	4767	4837	4906	4976	5045	5115
24	5185	5254	5324	5393	5463	5532	5602	5672	5741	5810
625	5890	5959	6019	6088	6158	6227	6297	6366	6436	6505
26	6574	6644	6713	6782	6852	6921	6990	7060	7129	7198
27	7287	7357	7426	7495	7564	7634	7703	7772	7841	7910
28	7960	8029	8098	8167	8236	8305	8374	8443	8512	8581
29	8651	8720	8789	8858	8927	8996	9065	9134	9203	9272
630	9341	9410	9479	9547	9616	9685	9754	9823	9892	9960
31	0022	0091	0160	0228	0297	0365	0434	0503	0571	0640
32	0717	0786	0855	0923	0992	1061	1129	1198	1266	1335
33	1404	1472	1541	1609	1678	1747	1815	1884	1952	2021
34	2089	2158	2226	2295	2363	2432	2500	2569	2637	2705
635	2774	2842	2911	2979	3047	3116	3184	3252	3321	3389
36	3457	3525	3594	3662	3730	3798	3867	3935	4003	4071
37	4139	4207	4276	4344	4412	4480	4548	4616	4684	4753
38	4821	4889	4957	5025	5093	5161	5229	5297	5365	5433
39	5501	5569	5637	5705	5773	5841	5909	5976	6044	6112
640	6180	6248	6316	6384	6451	6519	6587	6655	6722	6790
41	6858	6926	6994	7061	7129	7197	7264	7332	7400	7467
42	7535	7603	7670	7738	7806	7873	7941	8008	8076	8143
43	8211	8279	8346	8414	8481	8549	8616	8684	8751	8818
44	8896	8963	9031	9098	9165	9232	9299	9366	9433	9499
645	9500	9567	9634	9701	9768	9835	9902			
46	0233	0300	0367	0434	0501	0568	0635	0703	0770	0837
47	0904	0971	1039	1106	1173	1240	1307	1374	1441	1508
48	1575	1642	1709	1776	1843	1910	1977	2044	2111	2178
49	2245	2312	2379	2445	2512	2579	2646	2713	2780	2847
650	2913	2980	3047	3114	3180	3247	3314	3381	3448	3514
51	3581	3648	3714	3781	3848	3914	3981	4048	4114	4181
52	4248	4314	4381	4447	4514	4580	4647	4714	4780	4847
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TABLE I.—LOG. OF NOS.

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633	81 4913	4960	5046	5113	5179	5246	5312	5378	5445	5511
54	5578	5644	5711	5777	5843	5910	5976	6043	6109	6175
655	6241	6308	6374	6440	6506	6573	6639	6705	6771	6838
56	6904	6970	7036	7102	7169	7235	7301	7367	7433	7499
57	7565	7632	7698	7764	7830	7896	7962	8028	8094	8160
58	8226	8292	8358	8424	8490	8556	8622	8688	8754	8820
59	8885	8951	9017	9083	9149	9215	9281	9346	9412	9478
660	9544	9610	9676	9741	9807	9873	9939	0004	0070	0136
61	0202	0267	0333	0399	0464	0530	0596	0661	0727	0792
62	0858	0924	0989	1055	1120	1186	1251	1317	1383	1448
63	1513	1579	1645	1710	1776	1841	1906	1972	2037	2103
64	2168	2234	2299	2364	2430	2495	2560	2626	2691	2756
665	2822	2887	2952	3018	3083	3148	3213	3279	3344	3409
66	3474	3539	3605	3670	3735	3800	3865	3931	3996	4061
67	4126	4191	4256	4321	4386	4451	4516	4581	4646	4711
68	4777	4841	4907	4972	5036	5101	5166	5231	5296	5361
69	5426	5491	5556	5621	5686	5751	5815	5880	5945	6010
670	6075	6140	6204	6269	6334	6399	6464	6528	6593	6658
71	6723	6787	6852	6917	6981	7046	7111	7175	7240	7305
72	7369	7434	7499	7563	7628	7692	7757	7821	7886	7950
73	8015	8080	8144	8209	8273	8338	8402	8467	8531	8596
74	8660	8724	8789	8853	8918	8982	9046	9111	9175	9239
675	9304	9368	9432	9497	9561	9625	9690	9754	9818	9882
76	9947	0011	0075	0139	0204	0268	0332	0396	0460	0524
77	0589	0653	0717	0781	0845	0909	0973	1037	1101	1165
78	1230	1294	1358	1422	1486	1550	1614	1678	1742	1806
79	1870	1934	1998	2062	2126	2190	2253	2317	2381	2445
680	2509	2573	2637	2701	2764	2828	2892	2956	3020	3083
81	3147	3211	3275	3338	3402	3466	3530	3593	3657	3721
82	3784	3848	3912	3975	4039	4103	4166	4230	4293	4357
83	4421	4484	4548	4611	4675	4738	4802	4865	4929	4992
84	5056	5120	5183	5246	5310	5373	5437	5500	5564	5627
685	5691	5754	5817	5881	5944	6007	6071	6134	6198	6261
86	6324	6387	6451	6514	6577	6641	6704	6767	6830	6894
87	6957	7020	7083	7146	7210	7273	7336	7399	7462	7525
88	7588	7652	7715	7778	7841	7904	7967	8030	8093	8156
89	8219	8282	8345	8408	8471	8534	8597	8660	8723	8786
690	8849	8912	8975	9038	9101	9164	9227	9290	9353	9415
91	9478	0541	0604	0667	0730	0793	0855	0918	0981	1043
92	0106	0169	0232	0294	0357	0420	0483	0545	0608	0671
93	0733	0796	0859	0921	0984	1047	1109	1172	1234	1297
94	1360	1423	1485	1547	1610	1672	1735	1797	1860	1922
695	1985	2047	2110	2173	2235	2297	2360	2423	2484	2547
96	2609	2672	2734	2796	2859	2921	2983	3046	3108	3170
97	3233	3295	3357	3420	3482	3544	3607	3669	3731	3793
98	3855	3918	3980	4042	4104	4166	4228	4291	4353	4415
99	4477	4539	4601	4663	4725	4787	4850	4912	4974	5036
700	5098	5160	5222	5284	5346	5408	5470	5532	5594	5656
01	5718	5780	5842	5904	5966	6028	6090	6151	6213	6275
02	6337	6399	6461	6523	6585	6646	6708	6770	6832	6894
03	6955	7017	7079	7141	7202	7264	7326	7388	7449	7511
04	7573	7634	7696	7758	7819	7881	7943	8004	8066	8128
705	8189	8251	8313	8374	8436	8497	8559	8620	8682	8743
06	8805	8866	8928	8989	9051	9112	9174	9235	9296	9358
07	9419	9481	9542	9604	9665	9726	9788	9849	9911	9972
08	0033	0095	0156	0217	0279	0340	0401	0462	0524	0585
09	0646	0707	0769	0830	0891	0952	1014	1075	1136	1197
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710	85	1938	1319	1361	1449	1503	1564	1685	1686	1747	1809
11		1870	1931	1988	2053	2114	2175	2236	2297	2358	2419
12		9480	2541	9602	9663	9724	9785	9846	9907	9968	3029
13		3090	3150	3211	3272	3333	3394	3455	3516	3577	3637
14		3688	3759	3820	3881	3941	4002	4063	4124	4185	4245
715		4306	4367	4428	4489	4549	4610	4670	4731	4792	4852
16		4913	4974	5034	5095	5156	5216	5277	5337	5398	5459
17		5519	5580	5640	5701	5761	5822	5882	5943	6004	6064
18		6194	6185	6245	6306	6366	6427	6487	6548	6608	6668
19		6729	6789	6850	6910	6970	7031	7091	7151	7212	7272
720		7332	7393	7453	7513	7574	7634	7694	7755	7815	7875
21		7935	7996	8056	8116	8176	8236	8297	8357	8417	8477
22		8537	8597	8658	8718	8778	8838	8898	8958	9018	9078
23		9138	9198	9258	9318	9378	9439	9499	9559	9619	9679
24		9739	9799	9858	9918	9978					
	86					0038	0098	0158	0218	0278	
725		0338	0398	0458	0518	0578	0637	0697	0757	0817	0877
26		0937	0996	1056	1116	1176	1236	1295	1355	1415	1475
27		1534	1594	1654	1714	1773	1833	1893	1952	2012	2072
28		2131	2191	2251	2310	2370	2430	2489	2549	2608	2668
29		2737	2797	2847	2906	2966	3025	3085	3144	3204	3263
730		3323	3382	3442	3501	3561	3620	3680	3739	3798	3858
31		3917	3977	4036	4096	4155	4214	4274	4333	4392	4452
32		4511	4570	4630	4689	4748	4808	4867	4926	4986	5045
33		5104	5163	5222	5282	5341	5400	5459	5519	5578	5637
34		5696	5755	5814	5874	5933	5992	6051	6110	6169	6228
735		6287	6346	6406	6465	6524	6583	6642	6701	6760	6819
36		6878	6937	6996	7055	7114	7173	7232	7291	7350	7409
37		7498	7557	7615	7674	7733	7792	7851	7910	7969	7988
38		8056	8115	8174	8233	8292	8351	8409	8468	8527	8586
39		8644	8703	8762	8821	8879	8938	8997	9056	9114	9173
740		9232	9290	9349	9408	9466	9525	9584	9642	9701	9760
41		9818	9877	9935	9994						
	87				0053	0111	0170	0228	0287	0345	
42		0404	0462	0521	0580	0638	0696	0755	0813	0872	0930
43		0989	1047	1106	1164	1223	1281	1339	1398	1456	1515
44		1573	1631	1690	1748	1806	1865	1923	1981	2040	2098
745		2156	2215	2273	2331	2389	2448	2506	2564	2622	2681
46		2739	2797	2855	2913	2971	3029	3088	3146	3204	3262
47		3321	3379	3437	3495	3553	3611	3669	3727	3786	3844
48		3903	3960	4018	4076	4134	4192	4250	4308	4366	4424
49		4482	4540	4598	4656	4714	4772	4830	4888	4945	5003
750		5061	5119	5177	5235	5293	5351	5409	5466	5524	5582
51		5640	5698	5756	5813	5871	5929	5987	6045	6102	6160
52		6218	6276	6333	6391	6449	6507	6564	6622	6680	6737
53		6825	6883	6940	6998	7056	7114	7171	7229	7286	7344
54		7371	7429	7487	7544	7602	7659	7717	7774	7832	7889
755		7947	8004	8062	8119	8177	8234	8292	8349	8407	8464
56		8522	8579	8637	8694	8752	8809	8866	8924	8981	9038
57		9096	9153	9211	9268	9325	9383	9440	9497	9555	9612
58		9669	9726	9784	9841	9898	9956				
	88							0013	0070	0127	0185
59		0242	0299	0356	0413	0471	0528	0585	0642	0699	0756
760		0814	0871	0928	0985	1042	1099	1156	1213	1270	1328
61		1385	1442	1499	1556	1613	1670	1727	1784	1841	1898
62		1955	2012	2069	2126	2183	2240	2297	2354	2411	2468
63		2525	2582	2638	2695	2752	2809	2866	2923	2980	3037
64		3093	3150	3207	3264	3321	3378	3434	3491	3548	3605
765		3661	3718	3775	3832	3889	3945	4002	4059	4115	4172
66		4239	4296	4342	4399	4456	4512	4569	4626	4682	4739
67		4795	4852	4909	4965	5022	5078	5135	5191	5248	5305
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768	88	5361	5418	5474	5531	5587	5644	5700	5757	5813	5870
69		5396	5453	6039	6096	6152	6209	6265	6322	6378	6434
770		6491	6547	6604	6660	6716	6773	6829	6885	6942	6998
71		7054	7111	7167	7223	7280	7336	7392	7449	7505	7561
72		7617	7674	7730	7786	7842	7899	7955	8011	8067	8123
73		8180	8236	8292	8348	8404	8460	8517	8573	8629	8685
74		8741	8797	8853	8909	8965	9021	9077	9134	9190	9246
775		9302	9358	9414	9470	9526	9582	9638	9694	9750	9806
76		9869	9918	9974							
	89			0030	0085	0142	0197	0253	0309	0365	
77		0421	0477	0533	0589	0645	0700	0756	0812	0868	0924
78		0980	1035	1091	1147	1203	1259	1314	1370	1426	1482
79		1538	1593	1649	1705	1760	1816	1872	1927	1983	2039
780		2035	2150	2206	2262	2317	2373	2429	2484	2540	2595
81		2651	2707	2762	2818	2873	2929	2985	3040	3096	3151
82		3207	3262	3318	3373	3429	3484	3540	3595	3651	3706
83		3762	3817	3873	3928	3984	4039	4094	4150	4205	4261
84		4316	4372	4427	4483	4538	4593	4648	4704	4759	4814
785		4870	4925	4980	5036	5091	5146	5202	5257	5312	5367
86		5423	5478	5533	5588	5644	5699	5754	5809	5864	5919
87		5975	6030	6085	6140	6195	6251	6306	6361	6416	6471
88		6526	6581	6636	6692	6747	6802	6857	6912	6967	7022
89		7076	7132	7187	7242	7297	7352	7407	7462	7517	7572
790		7627	7682	7737	7792	7847	7902	7957	8012	8067	8122
91		8176	8231	8286	8341	8396	8451	8506	8561	8616	8671
92		8725	8780	8835	8890	8945	8999	9054	9109	9164	9219
93		9273	9328	9383	9438	9492	9547	9602	9657	9712	9767
94		9821	9875	9930	9985						
	90			0039	0094	0149	0204	0259	0314	0369	0424
795		0377	0432	0487	0542	0597	0652	0707	0762	0817	0872
96		0913	0968	1023	1077	1132	1187	1242	1297	1352	1407
97		1452	1507	1562	1617	1672	1727	1782	1837	1892	1947
98		2003	2057	2112	2167	2222	2277	2332	2387	2442	2497
99		2547	2601	2655	2710	2765	2820	2875	2930	2985	3040
800		3030	3144	3199	3253	3307	3361	3416	3470	3524	3578
01		3632	3687	3741	3795	3849	3903	3957	4011	4065	4119
02		4174	4228	4282	4337	4391	4445	4499	4553	4607	4661
03		4716	4770	4824	4878	4932	4986	5040	5094	5148	5202
04		5256	5310	5364	5418	5472	5526	5580	5634	5688	5742
805		5796	5850	5904	5958	6012	6066	6120	6173	6227	6281
06		6335	6389	6443	6497	6550	6604	6658	6712	6766	6820
07		6873	6927	6981	7035	7089	7143	7196	7250	7304	7358
08		7411	7465	7519	7573	7626	7680	7734	7787	7841	7895
09		7949	8002	8056	8110	8163	8217	8271	8324	8378	8431
810		8485	8539	8592	8646	8699	8753	8807	8860	8914	8967
11		9021	9074	9128	9181	9235	9289	9342	9396	9449	9503
12		9556	9609	9663	9717	9770	9823	9877	9930	9984	
	91										0037
13		0020	0144	0197	0251	0304	0358	0411	0464	0518	0571
14		0624	0678	0731	0784	0838	0891	0944	0998	1051	1104
815		1158	1211	1264	1317	1371	1424	1477	1530	1584	1637
16		1690	1743	1797	1850	1903	1956	2009	2063	2116	2169
17		2222	2275	2328	2381	2435	2488	2541	2594	2647	2700
18		2753	2806	2860	2913	2966	3019	3072	3125	3178	3231
19		3284	3337	3390	3443	3496	3549	3602	3655	3708	3761
820		3814	3867	3920	3973	4026	4079	4132	4184	4237	4290
21		4343	4396	4449	4502	4555	4608	4660	4713	4766	4819
22		4872	4925	4978	5030	5083	5136	5189	5242	5294	5347
23		5400	5453	5505	5558	5611	5664	5717	5769	5822	5875
24		5927	5980	6033	6085	6138	6191	6243	6296	6349	6401
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TABLE I.—LOG. OF NOS.

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825	91	6454	6507	6559	6619	6665	6717	6770	6822	6875	6927
26		6960	7033	7025	7136	7190	7243	7295	7348	7400	7453
27		7506	7558	7611	7663	7716	7768	7821	7873	7925	7978
28		8030	8083	8135	8188	8240	8293	8345	8397	8450	8502
29		8555	8607	8659	8713	8764	8816	8869	8921	8973	9026
830		9078	9130	9183	9235	9287	9340	9392	9444	9497	9549
31		9601	9653	9706	9758	9810	9862	9914	9967		
	92									0019	0071
32		0123	0176	0228	0280	0332	0384	0436	0489	0541	0593
33		0645	0697	0749	0801	0853	0906	0958	1010	1062	1114
34		1166	1218	1270	1322	1374	1426	1478	1530	1582	1634
835		1687	1739	1790	1842	1894	1946	1998	2050	2102	2154
36		2206	2258	2310	2362	2414	2466	2518	2570	2622	2674
37		2725	2777	2829	2881	2933	2985	3037	3089	3141	3193
38		3244	3296	3348	3400	3451	3503	3555	3607	3658	3710
39		3762	3814	3866	3917	3969	4021	4072	4124	4176	4228
840		4279	4331	4383	4434	4486	4538	4589	4641	4693	4744
41		4796	4848	4899	4951	5003	5054	5106	5157	5209	5261
42		5319	5364	5415	5467	5518	5570	5621	5673	5725	5776
43		5828	5879	5931	5982	6034	6085	6137	6188	6240	6291
44		6342	6394	6445	6497	6548	6600	6651	6703	6754	6805
845		6857	6908	6960	7011	7062	7114	7165	7216	7268	7319
46		7370	7422	7473	7524	7576	7627	7678	7730	7781	7832
47		7883	7935	7986	8037	8089	8140	8191	8242	8293	8345
48		8396	8447	8498	8550	8601	8652	8703	8754	8805	8857
49		8908	8959	9010	9061	9112	9163	9214	9266	9317	9368
850		9419	9470	9521	9572	9623	9674	9725	9776	9827	9879
51		9930	9981								
	93										
52		0040	0091	0142	0193	0244	0295	0346	0397	0448	0499
53		0549	0600	0651	0702	0753	0804	0855	0906	0957	1008
54		1058	1109	1160	1211	1262	1313	1364	1415	1466	1517
855		1568	1619	1670	1721	1772	1823	1874	1925	1976	2027
56		2078	2129	2180	2231	2282	2333	2384	2435	2486	2537
57		2588	2639	2690	2741	2792	2843	2894	2945	2996	3047
58		3098	3149	3200	3251	3302	3353	3404	3455	3506	3557
59		3608	3659	3710	3761	3812	3863	3914	3965	4016	4067
860		4118	4169	4220	4271	4322	4373	4424	4475	4526	4577
61		4628	4679	4730	4781	4832	4883	4934	4985	5036	5087
62		5138	5189	5240	5291	5342	5393	5444	5495	5546	5597
63		5648	5699	5750	5801	5852	5903	5954	6005	6056	6107
64		6158	6209	6260	6311	6362	6413	6464	6515	6566	6617
865		6668	6719	6770	6821	6872	6923	6974	7025	7076	7127
66		7178	7229	7280	7331	7382	7433	7484	7535	7586	7637
67		7688	7739	7790	7841	7892	7943	7994	8045	8096	8147
68		8198	8249	8300	8351	8402	8453	8504	8555	8606	8657
69		8708	8759	8810	8861	8912	8963	9014	9065	9116	9167
870		9218	9269	9320	9371	9422	9473	9524	9575	9626	9677
71	94	0018	0069	0120	0171	0222	0273	0324	0375	0426	0477
72		0528	0579	0630	0681	0732	0783	0834	0885	0936	0987
73		1038	1089	1140	1191	1242	1293	1344	1395	1446	1497
74		1548	1599	1650	1701	1752	1803	1854	1905	1956	2007
875		2058	2109	2160	2211	2262	2313	2364	2415	2466	2517
76		2568	2619	2670	2721	2772	2823	2874	2925	2976	3027
77		3078	3129	3180	3231	3282	3333	3384	3435	3486	3537
78		3588	3639	3690	3741	3792	3843	3894	3945	3996	4047
79		4098	4149	4200	4251	4302	4353	4404	4455	4506	4557
880		4608	4659	4710	4761	4812	4863	4914	4965	5016	5067
81		4978	5029	5080	5131	5182	5233	5284	5335	5386	5437
82		5488	5539	5590	5641	5692	5743	5794	5845	5896	5947
83		5998	6049	6100	6151	6202	6253	6304	6355	6406	6457
N.	0	1	2	3	4	5	6	7	8	9	

TABLE I.—LOG. OF NOS.

N.	0	1	2	3	4	5	6	7	8	9
884	94 6432	6501	6551	6600	6649	6698	6747	6796	6845	6894
885	6943	6992	7041	7091	7140	7189	7238	7287	7336	7385
886	7434	7483	7532	7581	7630	7679	7728	7777	7826	7875
887	7974	7973	8022	8071	8119	8168	8217	8266	8315	8364
888	8413	8462	8511	8560	8609	8657	8706	8755	8804	8853
889	8902	8951	8999	9048	9097	9146	9195	9244	9293	9341
890	9390	9439	9488	9536	9585	9634	9683	9732	9780	9829
91	9878	9926	9975							
92	95	0065	0114	0162	0211	0260	0309	0357	0406	0455
93	0652	0700	0749	0797	0846	0895	0944	0993	1042	1091
94	1337	1386	1435	1483	1532	1580	1629	1677	1726	1775
895	1823	1872	1920	1969	2017	2066	2114	2163	2211	2260
96	2308	2356	2405	2453	2502	2550	2599	2647	2696	2744
97	2792	2841	2889	2938	2986	3034	3083	3131	3180	3228
98	3276	3325	3373	3421	3470	3518	3567	3615	3663	3711
99	3760	3808	3856	3905	3953	4001	4049	4098	4146	4194
900	4242	4291	4339	4387	4436	4484	4532	4580	4629	4677
01	4725	4773	4821	4869	4918	4966	5014	5062	5110	5158
02	5207	5255	5303	5351	5399	5447	5495	5543	5591	5640
03	5688	5736	5784	5832	5880	5928	5976	6024	6072	6120
04	6168	6216	6264	6312	6361	6409	6457	6505	6553	6601
905	6649	6697	6745	6793	6841	6889	6937	6985	7033	7081
06	7128	7176	7224	7272	7320	7368	7416	7464	7512	7560
07	7607	7655	7703	7751	7799	7847	7895	7943	7991	8039
08	8086	8134	8182	8230	8278	8326	8374	8422	8470	8518
09	8564	8612	8660	8707	8755	8803	8851	8899	8947	8994
910	9041	9089	9137	9185	9233	9281	9329	9377	9425	9473
11	9518	9566	9614	9661	9709	9757	9804	9852	9900	9947
12	9995									
13	96	0042	0090	0138	0185	0233	0280	0328	0376	0423
14	0471	0518	0566	0614	0661	0709	0756	0804	0851	0899
15	0946	0994	1041	1089	1136	1184	1231	1279	1326	1374
915	1421	1469	1516	1563	1611	1658	1706	1753	1801	1848
16	1896	1943	1990	2038	2085	2132	2180	2227	2275	2322
17	2369	2417	2464	2511	2559	2606	2653	2701	2748	2795
18	2843	2890	2937	2985	3032	3079	3126	3174	3221	3268
19	3316	3363	3410	3457	3505	3552	3599	3646	3693	3741
920	3788	3835	3882	3929	3977	4024	4071	4118	4165	4213
21	4280	4327	4374	4421	4468	4515	4562	4609	4656	4703
22	4731	4778	4825	4872	4919	4966	5013	5061	5108	5155
23	5202	5249	5296	5343	5390	5437	5484	5531	5578	5625
24	5672	5719	5766	5813	5860	5907	5954	6001	6048	6095
925	6142	6189	6236	6283	6329	6376	6423	6470	6517	6564
26	6611	6658	6705	6752	6799	6845	6892	6939	6986	7033
27	7070	7117	7163	7210	7257	7304	7351	7398	7445	7492
28	7548	7595	7642	7688	7735	7782	7829	7875	7922	7969
29	8016	8063	8109	8156	8203	8249	8296	8343	8390	8436
930	8483	8530	8576	8623	8670	8716	8763	8810	8856	8903
31	8950	8996	9043	9090	9136	9183	9230	9276	9323	9369
32	9416	9462	9509	9556	9602	9649	9695	9742	9789	9835
33	9882	9928	9975							
34	97	0347	0393	0440	0486	0533	0579	0626	0672	0719
935	0812	0858	0905	0951	0997	1044	1090	1137	1183	1229
36	1276	1322	1369	1415	1461	1508	1554	1601	1647	1693
37	1740	1786	1832	1879	1925	1971	2018	2064	2110	2157
38	2203	2249	2295	2342	2388	2434	2481	2527	2573	2619
39	2666	2712	2758	2804	2851	2897	2943	2989	3035	3082
940	3128	3174	3220	3266	3312	3359	3405	3451	3497	3544
N.	0	1	2	3	4	5	6	7	8	9

N.	0	1	2	3	4	5	6	7	8	9	
941	97	3590	3636	3689	3738	3774	3800	3866	3913	3959	4005
42		4051	4097	4143	4189	4235	4281	4327	4374	4420	4466
43		4519	4558	4604	4650	4696	4742	4788	4834	4880	4926
44		4979	5018	5064	5110	5156	5202	5248	5294	5340	5386
945		5438	5478	5524	5570	5616	5662	5707	5753	5799	5845
45		5891	5937	5983	6029	6075	6121	6167	6213	6259	6304
46		6350	6396	6442	6488	6533	6579	6625	6671	6717	6763
47		6808	6854	6900	6946	6992	7037	7083	7129	7175	7220
49		7266	7312	7358	7404	7449	7495	7541	7586	7632	7678
950		7724	7769	7815	7861	7906	7952	7998	8043	8089	8135
51		8180	8226	8272	8317	8363	8409	8454	8500	8546	8591
52		8637	8683	8728	8774	8819	8865	8911	8956	9002	9047
53		9093	9139	9184	9230	9275	9321	9366	9412	9457	9503
54		9548	9594	9639	9685	9730	9776	9821	9867	9912	9958
955	98	0003	0049	0094	0140	0185	0231	0276	0322	0367	0413
56		0458	0504	0549	0594	0640	0685	0730	0776	0821	0867
57		0912	0957	1003	1048	1093	1139	1184	1229	1275	1320
58		1366	1411	1456	1501	1547	1592	1637	1683	1728	1773
59		1819	1864	1909	1954	2000	2045	2090	2135	2181	2226
960		2271	2317	2362	2407	2452	2497	2543	2588	2633	2678
61		2723	2769	2814	2859	2904	2949	2995	3040	3085	3130
62		3175	3220	3265	3311	3356	3401	3446	3491	3536	3581
63		3626	3671	3716	3762	3807	3852	3897	3942	3987	4032
64		4077	4122	4167	4212	4257	4302	4347	4392	4437	4482
965		4527	4572	4617	4662	4707	4752	4797	4842	4887	4932
66		4977	5022	5067	5112	5157	5202	5247	5292	5337	5382
67		5426	5471	5516	5561	5606	5651	5696	5741	5786	5831
68		5875	5920	5965	6010	6055	6100	6145	6190	6235	6280
69		6324	6369	6414	6459	6503	6548	6593	6638	6683	6728
970		6772	6817	6861	6906	6951	6996	7040	7085	7130	7175
71		7219	7264	7309	7353	7398	7443	7488	7532	7577	7622
72		7666	7711	7756	7800	7845	7890	7934	7979	8024	8068
73		8112	8157	8201	8246	8291	8335	8380	8424	8469	8513
74		8559	8603	8648	8692	8737	8781	8826	8870	8915	8959
975		9005	9049	9094	9138	9182	9227	9271	9315	9360	9404
76		9450	9494	9539	9583	9628	9672	9717	9761	9805	9850
77		9895	9939	9984							
980	99	0039	0083	0128	0172	0217	0261	0305	0349	0393	0437
78		0783	0827	0871	0916	0960	1004	1049	1093	1137	1181
985		1226	1270	1314	1358	1402	1446	1490	1534	1578	1622
81		1666	1710	1754	1798	1842	1886	1930	1974	2018	2062
82		2105	2149	2193	2237	2281	2325	2369	2413	2457	2501
83		2544	2588	2632	2676	2720	2764	2808	2852	2896	2940
84		2984	3028	3072	3116	3160	3204	3248	3292	3336	3380
985		3424	3468	3512	3556	3600	3644	3688	3732	3776	3820
86		3877	3921	3965	4009	4053	4097	4141	4185	4229	4273
87		4317	4361	4405	4449	4493	4537	4581	4625	4669	4713
88		4757	4801	4845	4889	4933	4977	5021	5065	5109	5153
89		5198	5242	5286	5330	5373	5417	5461	5505	5549	5593
990		5635	5679	5723	5767	5811	5854	5898	5942	5986	6030
91		6074	6118	6161	6205	6249	6293	6337	6380	6424	6468
93		6512	6555	6599	6643	6687	6731	6774	6818	6862	6906
94		6949	6993	7037	7080	7124	7168	7211	7255	7299	7343
94		7386	7430	7474	7517	7561	7605	7649	7692	7736	7779
995		7823	7867	7910	7954	7998	8041	8085	8128	8172	8216
96		8259	8303	8347	8390	8434	8477	8521	8564	8608	8652
97		8696	8739	8783	8826	8870	8913	8957	9000	9043	9087
98		9121	9164	9208	9251	9295	9338	9382	9425	9469	9512
99		9555	9599	9642	9686	9729	9773	9816	9860	9903	9947
1000	00	0000	0043	0087	0130	0174	0217	0261	0304	0347	0391
N.	0	1	2	3	4	5	6	7	8	9	

TABLE II.

LOGARITHMS OF SINES, COSEC'S, TANGENTS, &c.

0° 00'		1° — 15'							179° 11'				
Hours.	Deg.	L. Sin.	Diff. for 5"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 5"	L. Cot.	Deg.	Hours.		
0	1	0	15	5.861666	100343	4.136334	0.000000	0.000000	5.861666	100343	4.136334	45	59
	2	0	30	5.163696	999657	3.837304	0.000000	0.000000	5.163696	999657	3.837304	30	58
	3	0	45	.336767	58997	.661813	0.000000	0.000000	.336767	58997	.661813	15	57
	4	1		.463736	41646	.536274	0.000000	0.000000	.463736	41646	.536274	30	56
	5	15		.560636	32303	.439364	0.000000	0.000000	.560636	32303	.439364	45	55
	6	30		.639817	26394	.360183	0.000000	0.000000	.639817	26394	.360183	30	54
	7	45		.706764	22316	.293236	0.000000	0.000000	.706764	22316	.293236	15	53
	8	9		.764756	19331	.235244	0.000000	0.000000	.764756	19331	.235244	30	52
	9	15		.813906	17051	.184091	0.000000	0.000000	.813906	17051	.184091	45	51
	10	30		.861666	15232	.136334	0.000000	0.000000	.861666	15232	.136334	30	50
	11	45		.903059	13796	.096941	0.000000	0.000000	.903059	13796	.096941	15	49
	12	3		.940647	12596	.059353	0.000000	0.000000	.940647	12596	.059353	57	47
	13	15		.975609	11587	.024391	0.000000	0.000000	.975609	11587	.024391	45	46
	14	30		7.007764	9989	2.992236	0.000000	0.000000	7.007764	9989	2.992236	30	46
	15	45		.037757	9343	.962243	0.000000	0.000000	.037757	9343	.962243	15	45
	16	4		.065796	8776	.934214	0.000000	0.000000	.065796	8776	.934214	56	44
	17	15		.092115	8275	.907885	0.000000	0.000000	.092115	8275	.907885	45	43
	18	30		.116929	7827	.883071	0.000000	0.000000	.116929	7827	.883071	30	42
	19	45		.140430	7423	.859570	0.000000	0.000000	.140430	7423	.859570	15	41
	20	5		.162606	7063	.837304	0.000000	0.000000	.162606	7063	.837304	55	40
	21	15		.183685	6735	.816115	0.000000	0.000000	.183685	6735	.816115	45	39
	22	30		.203609	6435	.795911	0.000000	0.000000	.203609	6435	.795911	30	38
	23	45		.222304	6161	.776606	0.000000	0.000000	.222304	6161	.776606	15	37
	24	6		.241877	5910	.758123	0.000000	0.000000	.241877	5910	.758123	54	36
	25	15		.259906	5678	.740394	0.000000	0.000000	.259906	5678	.740394	45	35
	26	30		.276639	5464	.723361	0.000000	0.000000	.276639	5464	.723361	30	34
	27	45		.292030	5265	.706970	0.000000	0.000000	.292030	5265	.706970	15	33
	28	7		.306224	5080	.691176	0.000000	0.000000	.306224	5080	.691176	53	32
	29	15		.320264	4908	.675936	0.000000	0.000000	.320264	4908	.675936	45	31
	30	30		.336767	4747	.661213	0.000000	0.000000	.336767	4747	.661213	30	30
	31	45		.353029	4596	.646979	0.000000	0.000000	.353029	4596	.646979	15	29
	32	8		.366816	4455	.633184	0.000000	0.000000	.366816	4455	.633184	58	28
	33	15		.380180	4322	.619890	0.000000	0.000000	.380180	4322	.619890	45	27
	34	30		.393145	4196	.606855	0.000000	0.000000	.393145	4196	.606855	30	26
	35	45		.405734	4078	.594266	0.000000	0.000000	.405734	4078	.594266	15	25
	36	9		.417968	3966	.582039	0.000000	0.000000	.417968	3966	.582039	51	24
	37	15		.429867	3861	.570133	0.000000	0.000000	.429867	3861	.570133	45	23
	38	30		.441449	3760	.558551	0.000000	0.000000	.441449	3760	.558551	30	22
	39	45		.452730	3665	.547270	0.000000	0.000000	.452730	3665	.547270	15	21
	40	10		.463725	3575	.536275	0.000000	0.000000	.463725	3575	.536275	50	20
	41	15		.474449	3489	.525581	0.000000	0.000000	.474449	3489	.525581	45	19
	42	30		.484915	3406	.515086	0.000000	0.000000	.484915	3406	.515086	30	18
	43	45		.495134	3328	.504866	0.000000	0.000000	.495134	3328	.504866	15	17
	44	11		.505118	3253	.494890	0.000000	0.000000	.505118	3253	.494890	49	16
	45	15		.514878	3182	.485122	0.000000	0.000000	.514878	3182	.485122	45	15
	46	30		.524423	3113	.475577	0.000000	0.000000	.524423	3113	.475577	30	14
	47	45		.533703	3048	.466237	0.000000	0.000000	.533703	3048	.466237	15	13
	48	19		.542806	2985	.457094	0.000000	0.000000	.542806	2985	.457094	48	12
	49	15		.551861	2925	.448139	0.000000	0.000000	.551861	2925	.448139	45	11
	50	30		.560835	2867	.439365	0.000000	0.000000	.560835	2867	.439365	30	10
	51	45		.569725	2811	.430765	0.000000	0.000000	.569725	2811	.430765	15	9
	52	12		.577668	2758	.422339	0.000000	0.000000	.577668	2758	.422339	47	8
	53	15		.585641	2706	.414099	0.000000	0.000000	.585641	2706	.414099	45	7
	54	30		.594039	2656	.405941	0.000000	0.000000	.594039	2656	.405941	30	6
	55	45		.602028	2608	.397972	0.000000	0.000000	.602028	2608	.397972	15	5
	56	14		.609653	2562	.390147	0.000000	0.000000	.609653	2562	.390147	46	4
	57	15		.617540	2518	.382460	0.000000	0.000000	.617540	2518	.382460	45	3
	58	30		.625093	2476	.374907	0.000000	0.000000	.625093	2476	.374907	30	2
	59	45		.632517	2433	.367423	0.000000	0.000000	.632517	2433	.367423	15	1
	60	15		7.838616	2390	2.300184	0.999996	0.000004	7.838616	2390	2.300184	45	59

0° — 00°

1° — 4' 10 — 4"

80° — 00°

TABLE II.—LOG. SINES, TANG'S, &C.

0° 00'		1° - 15' 1" - 15'							179°		180°	
Hours.	Deg.	L. Sin.	Diff. for 5"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 5"	L. Cot.	Deg.	Hours.	
1	0	15	7.030816	2398	8.360184	9.999996	0.000004	7.030820	2398	8.360180	45	58
	1	15	.646995	2394	.353005	.96	.04	.646999	2394	.353001	45	59
	2	30	.654056	2394	.345944	.96	.04	.654061	2394	.345939	30	57
	3	45	.661005	2390	.338895	.96	.04	.661010	2390	.338890	15	57
	4	16	.667845	2244	.331855	.95	.05	.667849	2244	.331851	44	56
	5	15	.674578	2210	.325422	.95	.05	.674583	2210	.325417	45	55
	6	30	.681908	2177	.318792	.95	.05	.681913	2177	.318787	30	54
	7	45	.687739	2177	.312861	.95	.05	.687744	2177	.312856	15	53
	8	17	.694173	2145	.305827	.95	.05	.694178	2145	.305823	43	52
	9	15	.700513	2113	.299487	.95	.05	.700519	2113	.299481	45	51
	10	30	.706768	2082	.292836	.94	.06	.706773	2082	.292830	30	50
	11	45	.712922	2054	.287078	.94	.06	.712928	2054	.287072	15	49
	12	18	.718997	2025	.281003	.94	.06	.718993	2025	.281007	42	47
	13	15	.724867	1997	.275013	.94	.06	.724873	1997	.275007	45	47
	14	30	.730696	1943	.269104	.94	.06	.730702	1943	.269096	30	46
	15	45	.736725	1917	.263275	.94	.06	.736732	1917	.263268	15	45
	16	19	.742477	1892	.257522	.93	.07	.742484	1892	.257516	41	44
	17	15	.748155	1868	.251845	.93	.07	.748161	1868	.251839	45	43
	18	30	.753758	1844	.246242	.93	.07	.753765	1844	.246235	30	42
	19	45	.759291	1821	.240709	.93	.07	.759298	1821	.240702	15	41
	20	30	.764754	1798	.235246	.93	.07	.764761	1798	.235239	40	40
	21	15	.770149	1776	.229851	.93	.07	.770156	1776	.229844	45	39
	22	30	.775477	1755	.224523	.92	.08	.775485	1755	.224515	30	38
	23	45	.780742	1734	.219258	.92	.08	.780750	1734	.219250	15	37
	24	31	.785943	1713	.214057	.92	.08	.785951	1713	.214049	30	36
	25	15	.791082	1693	.208918	.92	.08	.791090	1693	.208910	45	35
	26	30	.796162	1674	.203836	.92	.08	.796170	1674	.203830	30	34
	27	45	.801183	1654	.198817	.92	.08	.801191	1654	.198809	15	33
	28	28	.806146	1636	.193864	.91	.09	.806155	1636	.193845	30	32
	29	15	.811053	1618	.188977	.91	.09	.811062	1618	.188958	45	31
	30	30	.815906	1599	.184094	.91	.09	.815915	1599	.184085	30	30
	31	45	.820704	1582	.179296	.91	.09	.820714	1582	.179286	15	29
	32	23	.825451	1565	.174549	.90	.10	.825460	1565	.174540	37	28
	33	15	.830146	1548	.169854	.90	.10	.830156	1548	.169844	45	27
	34	30	.834791	1532	.165209	.90	.10	.834801	1532	.165199	30	26
	35	45	.839386	1516	.160614	.89	.11	.839397	1516	.160603	15	25
	36	34	.843934	1500	.156066	.89	.11	.843944	1500	.156056	36	24
	37	15	.848434	1485	.151566	.89	.11	.848445	1485	.151555	45	23
	38	30	.852889	1470	.147111	.89	.11	.852890	1470	.147100	30	22
	39	45	.857298	1455	.142702	.89	.11	.857300	1455	.142691	15	21
	40	25	.861662	1441	.138338	.89	.11	.861674	1441	.138326	35	20
	41	15	.865984	1426	.134016	.89	.11	.865995	1426	.134005	45	19
	42	30	.870262	1412	.129736	.88	.12	.870274	1412	.129726	30	18
	43	45	.874490	1412	.125501	.88	.12	.874511	1412	.125489	15	17
	44	26	.878685	1365	.121305	.88	.12	.878706	1365	.121292	34	16
	45	15	.882851	1379	.117149	.87	.13	.882864	1379	.117136	45	15
	46	30	.886988	1359	.113032	.87	.13	.886991	1359	.113019	30	14
	47	45	.891046	1346	.108954	.87	.13	.891059	1346	.108941	15	13
	48	27	.895028	1334	.104915	.87	.13	.895039	1334	.104901	33	12
	49	15	.898936	1322	.100912	.87	.13	.898949	1322	.100898	45	11
	50	30	.902854	1310	.096946	.86	.14	.902868	1310	.096932	30	10
	51	45	.906684	1298	.093016	.86	.14	.906698	1298	.093002	15	9
	52	26	.910479	1287	.089121	.86	.14	.910494	1287	.089106	32	8
	53	15	.914740	1275	.085260	.86	.14	.914754	1275	.085246	45	7
	54	30	.918366	1264	.081434	.85	.15	.918381	1264	.081419	30	6
	55	45	.922355	1253	.077641	.85	.15	.922374	1253	.077626	15	5
	56	30	.926119	1242	.073881	.85	.15	.926134	1242	.073866	31	4
	57	15	.929647	1232	.070153	.85	.15	.929663	1232	.070137	45	3
	58	30	.933543	1222	.066457	.84	.16	.933559	1222	.066441	30	2
	59	45	.937306	1211	.062792	.84	.16	.937324	1211	.062776	15	1
1	00	30	7.940842	1911	8.059158	9.999994	0.000006	7.940852	1911	8.059142	30	58

0° - 90°

1° - 15' 1" - 15'

89° - 5'

TABLE II.—LOG. SINES, TANG'S, &c.

0°		1° - 15' 1° - 15' 1° - 15°										179°		11°	
Hours.	Deg.	L. Sin.	Diff. for 5'	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 5'	L. Cot.	Deg.	Hours.				
0	30	7.940842	1201	9.0515-	9.9999-4	0.000016	7.940858	1202	9.057142	30	57				
1	15	.944445	1191	.055554	.84	.16	.944463	1191	.055537	45	59				
2	30	.948020	1182	.051380	.83	.17	.948037	1182	.051363	30	58				
3	15	.951505	1172	.048435	.83	.17	.951523	1172	.048417	15	57				
4	31	.955082	1163	.044918	.82	.18	.955100	1163	.044900	29	56				
5	15	.958570	1154	.041430	.82	.18	.958588	1154	.041412	45	55				
6	30	.962031	1144	.037969	.82	.18	.962049	1144	.037951	30	54				
7	45	.965464	1135	.034536	.81	.19	.965482	1136	.034518	15	53				
8	32	.968870	1127	.031130	.81	.19	.968889	1127	.031111	28	52				
9	15	.972250	1118	.027750	.81	.19	.972269	1118	.027731	45	51				
10	30	.975603	1109	.024397	.81	.19	.975622	1110	.024378	30	50				
11	45	.978931	1101	.021069	.80	.20	.978951	1101	.021049	15	49				
12	33	.982233	1093	.017767	.80	.20	.982253	1093	.017747	27	48				
13	15	.985511	1084	.014489	.80	.20	.985531	1085	.014469	45	47				
14	30	.988764	1076	.011236	.79	.21	.988785	1076	.011215	30	46				
15	45	.991993	1068	.008007	.79	.21	.992014	1068	.007986	15	45				
16	34	.995198	1060	.004802	.79	.21	.995219	1061	.004781	26	44				
17	15	.998379	1051	.001621	.78	.22	.998401	1053	.001529	45	43				
18	30	8.001538	1045	1.998462	.78	.22	8.001550	1045	1.998440	30	42				
19	45	.004674	1038	.995326	.78	.22	.004686	1038	.995304	15	41				
20	35	.007787	1030	.992213	.78	.22	.007809	1031	.992191	35	40				
21	15	.010878	1023	.989122	.77	.23	.010901	1023	.989099	45	39				
22	30	.013947	1016	.986053	.77	.23	.013970	1016	.986030	30	38				
23	45	.016994	1009	.983006	.77	.23	.017018	1009	.982982	15	37				
24	36	.020021	1002	.979979	.76	.24	.020045	1002	.979955	34	36				
25	15	.023026	995	.976974	.76	.24	.023050	995	.976950	45	35				
26	30	.026011	988	.973989	.76	.24	.026035	988	.973965	30	34				
27	45	.028975	982	.971025	.75	.25	.029000	982	.971000	15	33				
28	17	.031920	975	.968080	.75	.25	.031945	975	.968055	23	32				
29	30	.034844	968	.965158	.75	.25	.034869	969	.965131	45	31				
30	45	.037749	962	.962251	.74	.26	.037775	962	.962229	30	30				
31	30	.040634	956	.959336	.74	.26	.040660	956	.959320	15	29				
32	15	.043501	949	.956449	.74	.26	.043527	950	.956473	22	28				
33	30	.046349	943	.953551	.73	.27	.046376	943	.953524	45	27				
34	45	.049178	937	.950622	.73	.27	.049205	937	.950735	30	26				
35	30	.051989	931	.948011	.72	.28	.052016	931	.947984	15	25				
36	15	.054781	925	.945219	.72	.28	.054803	925	.945111	21	24				
37	30	.057556	919	.942444	.72	.28	.057584	919	.943416	45	23				
38	45	.060314	913	.939686	.71	.29	.060342	914	.939658	30	22				
39	30	.063054	907	.936946	.71	.29	.063083	908	.936917	15	21				
40	15	.065776	902	.934224	.71	.29	.065806	902	.934194	20	20				
41	30	.068482	896	.931518	.70	.30	.068512	896	.931488	45	19				
42	45	.071171	891	.928829	.70	.30	.071201	891	.928797	30	18				
43	30	.073844	885	.926153	.70	.30	.073874	886	.926126	15	17				
44	15	.076500	880	.923500	.69	.31	.076531	880	.923469	19	16				
45	30	.079140	875	.920860	.69	.31	.079171	875	.920829	45	15				
46	45	.081764	869	.918236	.68	.32	.081795	870	.918205	30	14				
47	30	.084372	864	.915628	.68	.32	.084404	864	.915596	15	13				
48	15	.086965	859	.913035	.68	.32	.086997	859	.913003	18	12				
49	30	.089542	854	.910458	.67	.33	.089575	854	.910425	45	11				
50	45	.092104	849	.907896	.67	.33	.092137	849	.907863	30	10				
51	30	.094651	844	.905334	.66	.34	.094685	844	.905315	15	9				
52	15	.097183	839	.902817	.66	.34	.097217	839	.902837	17	8				
53	30	.099701	834	.900279	.65	.34	.099735	835	.900265	45	7				
54	45	.102204	829	.897796	.65	.35	.102239	830	.897761	30	6				
55	30	.104693	825	.895307	.65	.35	.104728	825	.895272	15	5				
56	15	.107167	820	.892833	.64	.36	.107203	820	.892797	16	4				
57	30	.109627	816	.890375	.64	.36	.109663	816	.890337	45	3				
58	45	.112074	811	.887926	.64	.36	.112110	811	.887870	30	2				
59	30	.114507	806	.885493	.63	.37	.114544	806	.885459	15	1				
60	15	8.116926	801	1.883074	9.999933	0.000037	8.116963	801	1.883037	15	57				

6° - 90

1° - 4° 10° - 48°

89°

54

D

TABLE II.—LOG. SINES, TANG'S, &C.

0°		1° - 15' 1" - 15' 1" - 15°						179°		180°	
Deg.	L. Sin.	Diff. for 5'	L. Cosec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 5'	L. Cot.	Deg.	Hours.	
45	8.116926	802	1.883074	9.999963	0.000037	8.116963	802	1.883037	15	56 60	
15	.119332	798	.890668	.62	.38	.119370	798	.890630	45	59	
30	.121725	793	.878275	.62	.38	.121763	793	.878237	30	58	
45	.124104	789	.875896	.62	.38	.124143	789	.875857	15	57	
46	.126471	785	.873529	.61	.39	.126510	785	.873490	14	56	
15	.128825	780	.871175	.61	.39	.128864	781	.871136	45	55	
30	.131166	776	.868834	.60	.40	.131206	776	.868794	30	54	
45	.133494	772	.866506	.60	.40	.133534	772	.866466	15	53	
47	.135810	768	.864190	.59	.41	.135851	768	.864149	13	52	
15	.138114	764	.861886	.59	.41	.138155	764	.861845	45	51	
30	.140405	760	.859594	.59	.41	.140447	760	.859553	30	50	
45	.142685	756	.857315	.58	.42	.142727	756	.857273	15	49	
18	.144953	752	.855047	.57	.43	.144996	752	.855004	12	48	
15	.147209	748	.852791	.57	.43	.147252	748	.852748	45	47	
30	.149453	744	.850547	.56	.44	.149497	744	.850503	30	46	
45	.151686	741	.848314	.56	.44	.151730	741	.848270	15	45	
19	.153908	737	.846092	.56	.44	.153952	737	.846048	11	44	
15	.156118	733	.843882	.55	.45	.156162	733	.843838	45	43	
30	.158316	729	.841684	.55	.45	.158361	729	.841639	30	42	
45	.160504	726	.839496	.54	.46	.160550	726	.839450	15	41	
50	.162681	722	.837319	.54	.46	.162727	722	.837273	10	40	
15	.164847	719	.835153	.54	.46	.164893	719	.835107	45	39	
30	.167002	715	.832998	.53	.47	.167048	715	.832952	30	38	
45	.169146	711	.830854	.52	.48	.169194	711	.830806	15	37	
51	.171280	708	.828720	.52	.48	.171332	708	.828672	9	36	
15	.173404	705	.826596	.52	.48	.173452	705	.826548	45	35	
30	.175517	701	.824483	.51	.49	.175566	701	.824434	30	34	
45	.177620	698	.822380	.51	.49	.177669	698	.822331	15	33	
52	.179713	694	.820287	.50	.50	.179763	694	.820237	8	32	
15	.181796	691	.818204	.50	.50	.181846	691	.818154	45	31	
30	.183868	688	.816132	.49	.51	.183919	688	.816081	30	30	
45	.185931	684	.814069	.48	.52	.185982	684	.814017	15	29	
53	.187984	682	.812016	.48	.52	.188036	682	.811964	7	28	
15	.190028	678	.809972	.48	.52	.190081	678	.809919	45	27	
30	.192062	675	.807938	.47	.53	.192115	675	.807885	30	26	
45	.194087	672	.805913	.47	.53	.194140	672	.805860	15	25	
14	.196102	669	.803898	.46	.54	.196156	669	.803844	6	24	
15	.198108	665	.801892	.46	.54	.198162	666	.801838	45	23	
30	.200104	663	.799896	.45	.55	.200159	663	.799841	30	22	
45	.202092	659	.797908	.45	.55	.202147	660	.797853	15	21	
15	.204070	657	.795930	.44	.56	.204126	657	.795874	5	20	
15	.206040	653	.793960	.44	.56	.206096	654	.793904	45	19	
30	.208000	651	.792000	.43	.57	.208057	651	.791943	30	18	
45	.209952	648	.790048	.43	.57	.210009	648	.789991	15	17	
16	.211895	645	.788105	.42	.58	.211953	645	.788047	4	16	
15	.213829	642	.786171	.42	.58	.213887	642	.786113	45	15	
30	.215755	639	.784245	.41	.59	.215814	639	.784186	30	14	
45	.217672	636	.782328	.41	.59	.217731	637	.782269	15	13	
17	.219581	634	.780419	.40	.60	.219641	634	.780359	3	12	
15	.221482	631	.778518	.40	.60	.221542	631	.778458	45	11	
30	.223374	628	.776626	.39	.61	.223435	628	.776565	30	10	
45	.225258	625	.774742	.39	.61	.225319	625	.774681	15	9	
18	.227133	625	.772867	.38	.62	.227195	625	.772805	2	8	
15	.229001	623	.770999	.37	.63	.229064	623	.770926	45	7	
30	.230861	620	.769139	.37	.63	.230924	620	.769076	30	6	
45	.232713	617	.767287	.37	.63	.232776	617	.767224	15	5	
19	.234557	615	.765443	.36	.64	.234621	615	.765379	1	4	
15	.236393	612	.763607	.35	.65	.236459	612	.763542	45	3	
30	.238221	609	.761779	.35	.65	.238290	609	.761714	30	2	
45	.240042	607	.759958	.34	.66	.240116	607	.759892	15	1	
20	8.241855	604	1.758145	9.999933	0.000067	8.241922	605	1.758075	0	56 1 0	

- 90°

1° = 4' 1" = 4"

89° 5'

0 10

1' - 15' 1" - 15' 1" - 15'

1780 11'

Hours	Deg.	L. Sin.	Diff for 15" or 1'	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours
4	0	8.241855	1802	1.758145	9.999933	0.000067	8.241922	1802	1.758078	60	55
	1	245459	1787	.754541	.33	.67	245526	1787	.754474	59	58
	2	249303	1772	.750667	.32	.68	249401	1772	.750699	58	56
	3	252578	1758	.746222	.30	.70	252648	1758	.747352	57	54
	4	256004	1744	.742006	.29	.71	256165	1744	.743835	56	52
	5	259582	1730	.740418	.28	.72	259654	1730	.740346	55	50
	6	263042	1716	.736958	.27	.73	263115	1716	.736855	54	48
	7	266475	1703	.733525	.26	.74	266549	1703	.733451	53	46
	8	269881	1689	.730119	.25	.75	269956	1689	.730044	52	44
	9	273260	1677	.726740	.24	.76	273337	1677	.726663	51	42
	10	276614	1663	.723386	.23	.77	276691	1664	.723309	50	40
	11	279941	1651	.720059	.22	.79	280020	1651	.720080	49	38
	12	283243	1639	.716757	.20	.80	283323	1639	.716677	48	36
	13	286521	1626	.713479	.19	.81	286602	1627	.713392	47	34
	14	289773	1614	.710227	.17	.83	289856	1615	.710144	46	32
	15	293002	1602	.706998	.16	.84	293086	1603	.706914	45	30
	16	296207	1590	.703793	.15	.85	296292	1591	.703708	44	28
	17	299388	1579	.700612	.14	.86	299474	1580	.700520	43	26
	18	302546	1567	.697454	.13	.87	302633	1568	.697377	42	24
	19	305681	1556	.694319	.11	.89	305770	1557	.694230	41	22
	20	308794	1545	.691206	.10	.90	308884	1546	.691116	40	20
	21	311885	1534	.688115	.09	.91	311976	1535	.688024	39	18
	22	314954	1523	.685046	.08	.93	315046	1524	.684954	38	16
	23	318001	1513	.681999	.07	.94	318095	1514	.681905	37	14
	24	321027	1502	.678973	.05	.95	321122	1503	.678878	36	12
	25	324032	1492	.675968	.03	.97	324129	1492	.675871	35	10
	26	327016	1482	.672984	.02	.98	327114	1483	.672866	34	8
	27	329981	1472	.670019	.01	.99	330080	1473	.669920	33	6
	28	332924	1462	.667076	.999899	.000101	333025	1463	.666975	32	4
	29	335848	1452	.664152	.98	.02	335950	1453	.664050	31	2
	30	338753	1442	.661247	.97	.03	338856	1443	.661144	45	0
5	0	341639	1433	.658362	.95	.05	341743	1434	.658257	30	58
	1	344504	1424	.655496	.94	.06	344610	1425	.655390	44	56
	2	347352	1414	.652648	.93	.07	347459	1415	.652541	30	54
	3	350181	1405	.649819	.91	.09	350290	1406	.649710	43	52
	4	352991	1396	.647009	.90	.10	353101	1397	.646899	30	50
	5	355783	1387	.644217	.88	.12	355885	1388	.644105	42	48
	6	358558	1378	.641442	.87	.13	358671	1379	.641329	40	46
	7	361315	1370	.638685	.85	.15	361430	1371	.638570	41	44
	8	364055	1361	.635945	.84	.16	364171	1362	.635829	40	42
	9	366777	1352	.633223	.82	.18	366895	1353	.633105	40	40
	10	369482	1344	.630518	.81	.19	369601	1345	.630389	39	38
	11	372171	1336	.627829	.79	.21	372292	1337	.627678	39	36
	12	374843	1328	.625157	.77	.22	374965	1329	.625035	30	34
	13	377499	1319	.622501	.78	.23	377622	1320	.622378	38	32
	14	380138	1312	.619862	.75	.25	380263	1313	.619737	30	30
	15	382762	1304	.617238	.73	.27	382889	1305	.617111	37	28
	16	385370	1296	.614630	.72	.29	385498	1297	.614502	30	26
	17	387962	1288	.612038	.70	.30	388092	1289	.611906	36	24
	18	390530	1281	.609461	.69	.31	390670	1282	.609330	30	22
	19	393101	1273	.606899	.67	.33	393234	1274	.606766	35	20
	20	395648	1265	.604352	.66	.34	395782	1266	.604218	30	18
	21	398179	1258	.601821	.64	.36	398315	1259	.601685	34	16
	22	400696	1251	.599304	.62	.38	400834	1252	.599166	30	14
	23	403199	1244	.596801	.61	.39	403338	1245	.596662	33	12
	24	405687	1237	.594313	.59	.41	405828	1238	.594172	30	10
	25	408162	1230	.591838	.58	.42	408304	1231	.591696	32	8
	26	410621	1223	.589379	.56	.44	410765	1224	.589235	30	6
	27	413068	1216	.586932	.55	.45	413213	1217	.586787	31	4
	28	415500	1209	.584500	.53	.47	415647	1210	.584353	30	2
	29	417919	1202	.582081	.999985	.000015	418068	1203	.581932	30	0

6A 910

1' - 4' 10 - 4"

880 5A

TABLE II.—LOG. SINES, TANG'S, &c.

10		1' = 15" 1" = 15' 1" = 150						1780		11'	
Deg.	L. Sin.	Diff. for 15" or 1'	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours.	
90	8.417919	1203	1.582081	9.999851	0.000149	8.418066	1904	1.581922	50	53	
30	.420325	1194	.579675	.58	.50	.420475	1197	.579325	30	55	
11	.422717	1189	.577283	.46	.52	.422869	1190	.577131	29	56	
30	.425006	1183	.574904	.44	.54	.425250	1184	.574750	28	54	
12	.427462	1176	.572532	.46	.56	.427618	1177	.572322	28	52	
30	.429816	1170	.570184	.43	.57	.429973	1171	.570027	30	50	
13	.432158	1164	.567844	.41	.59	.432315	1165	.567653	27	46	
30	.434484	1158	.565516	.39	.61	.434645	1159	.565355	30	42	
14	.436800	1151	.563200	.38	.62	.436962	1152	.563038	36	44	
30	.439103	1145	.560897	.36	.64	.439267	1146	.560733	30	42	
15	.441394	1140	.558606	.34	.66	.441560	1141	.558440	35	40	
30	.443674	1133	.556326	.31	.67	.443841	1134	.556152	20	36	
16	.445941	1127	.554059	.29	.69	.446110	1128	.553882	0	34	
30	.448196	1122	.551804	.27	.71	.448367	1123	.551633	30	34	
17	.450440	1116	.549560	.26	.73	.450613	1117	.549387	33	32	
30	.452672	1110	.547328	.25	.75	.452847	1111	.547153	30	30	
18	.454893	1105	.545107	.23	.77	.455070	1106	.544930	22	26	
30	.457103	1099	.542897	.22	.78	.457281	1100	.542711	30	22	
19	.459301	1094	.540699	.20	.80	.459481	1095	.540511	21	24	
30	.461489	1088	.538511	.18	.82	.461671	1089	.538322	30	22	
20	.463665	1082	.536335	.16	.84	.463849	1083	.536151	30	20	
30	.465830	1077	.534170	.14	.86	.466016	1078	.533984	18	16	
1	.467985	1072	.532015	.13	.87	.468172	1073	.531822	19	18	
30	.470129	1067	.529871	.11	.89	.470318	1068	.529654	30	14	
2	.472263	1062	.527737	.09	.91	.472454	1063	.527522	18	12	
30	.474386	1056	.525614	.07	.93	.474579	1057	.525421	30	10	
3	.476496	1051	.523502	.05	.95	.476693	1052	.523307	17	8	
30	.478601	1046	.521394	.03	.97	.478798	1047	.521192	30	6	
4	.480693	1041	.519307	.01	.99	.480892	1042	.519102	16	4	
30	.482775	1036	.517225	999798	0.000201	.482976	1037	.517024	30	2	
5	.484848	1031	.515152	.97	.63	.485051	1032	.514949	15	0	
30	.486910	1026	.513090	.85	.65	.487115	1027	.512883	30	54	
6	.488963	1021	.511037	.83	.67	.489170	1022	.510830	14	56	
30	.491008	1017	.508994	.82	.68	.491214	1018	.508786	30	54	
17	.493040	1012	.506960	.80	.70	.493250	1013	.506750	13	52	
30	.495064	1007	.504936	.88	.12	.495272	1008	.504724	30	50	
18	.497079	1003	.502921	.86	.14	.497283	1004	.502707	12	48	
30	.499084	998	.500916	.84	.16	.499290	999	.500700	30	46	
19	.501080	993	.498920	.82	.18	.501292	994	.498702	11	44	
30	.503067	989	.496933	.80	.20	.503287	990	.496713	30	42	
20	.505045	984	.494955	.78	.22	.505287	985	.494733	10	40	
30	.507014	980	.492980	.76	.24	.507282	981	.492752	30	38	
11	.508974	975	.491022	.74	.26	.509280	976	.490800	9	36	
30	.510925	971	.489075	.72	.28	.511273	972	.488847	30	34	
12	.512867	967	.487133	.69	.31	.513268	968	.486902	8	32	
30	.514801	962	.485199	.67	.33	.515264	963	.484966	30	30	
13	.516726	958	.483274	.65	.35	.517261	959	.483033	7	28	
30	.518643	954	.481357	.63	.37	.519260	955	.481101	30	26	
14	.520551	950	.479449	.61	.39	.521260	951	.479170	6	24	
30	.522451	946	.477549	.59	.41	.523262	947	.477238	30	22	
15	.524343	941	.475657	.57	.43	.525266	943	.475314	5	20	
30	.526228	938	.473774	.55	.45	.527271	939	.473390	30	18	
16	.528109	933	.471898	.53	.47	.529278	934	.471465	4	16	
30	.529982	929	.470031	.51	.49	.531286	930	.469542	30	14	
17	.531848	925	.468172	.48	.52	.533296	926	.467620	3	12	
30	.533707	922	.466321	.46	.54	.535303	923	.465707	30	10	
18	.535552	918	.464477	.44	.56	.537317	919	.463802	2	8	
30	.537395	913	.462641	.42	.58	.539336	914	.461904	30	6	
19	.539226	910	.460814	.40	.60	.541357	911	.460012	1	4	
30	.541047	906	.458993	.38	.62	.543384	907	.458123	30	2	
20	8.542861		1.457181	9.999735	0.000265	8.543084		1.456916	0	59	

TABLE II.—LOG. SINES, TANG'S, &c.

6° 30'

1° - 15' 1° - 15' 1° - 15°

177°

Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.
8	0 0	8.542810	902	1.457181	0.999735	0.000265	8.543084	003	1.456916	60
	2 0	.544624	890	.453376	.31	67	.544801	900	.455109	59
	4 1	.546422	893	.453578	.21	69	.546691	896	.453300	59
	6 0	.548212	891	.451788	.29	71	.548483	892	.451517	30
	8 2	.549995	887	.450005	.27	73	.550268	889	.449732	58
	10 3	.551770	884	.448230	.24	76	.552046	885	.447954	30
	12 3	.553539	880	.446461	.22	78	.553817	881	.446183	57
	14 3	.555300	877	.444700	.20	80	.555580	878	.444420	30
	16 4	.557054	873	.442946	.18	82	.557336	874	.442664	56
	18 4	.558800	870	.441200	.15	85	.559085	871	.440915	30
	20 5	.560541	866	.439459	.13	87	.560828	867	.439172	55
	22 2	.562273	863	.437727	.10	99	.562563	864	.437437	30
	24 6	.563999	860	.436001	.08	92	.564291	861	.435709	54
	26 6	.565719	856	.434281	.06	94	.566013	857	.433987	30
	28 7	.567431	853	.432560	.04	96	.567727	854	.432273	53
	30 30	.569137	849	.430833	.01	99	.569436	850	.430564	30
	32 8	.570836	846	.429164	0.999501	.000301	.571137	847	.428863	52
	34 3	.572528	843	.427472	.96	04	.572832	844	.427168	30
	36 9	.574214	839	.425786	.94	06	.574520	840	.425480	51
	38 30	.575893	836	.424107	.92	08	.576201	838	.423799	30
	40 10	.577566	833	.422434	.89	11	.577877	834	.422123	50
	42 30	.579232	830	.420768	.87	13	.579545	831	.420455	30
	44 11	.580892	827	.419108	.84	16	.581208	828	.418792	49
	46 46	.582546	823	.417454	.82	18	.582864	825	.417130	30
	48 12	.584193	820	.415807	.80	20	.584513	822	.415487	48
	50 30	.585834	817	.414160	.77	23	.586157	819	.413843	30
	52 13	.587469	814	.412531	.75	25	.587794	816	.412206	47
	54 3	.589098	811	.410902	.72	28	.589426	812	.410574	30
	56 14	.590721	808	.409279	.70	30	.591051	809	.408949	46
	58 30	.592338	805	.407662	.68	32	.592670	806	.407330	30
9	0 15	.593948	802	.406052	.65	35	.594283	803	.405717	45
	2 30	.595553	799	.404447	.63	37	.595890	801	.404110	30
	4 16	.597152	796	.402848	.60	40	.597492	797	.402508	44
	6 30	.598745	793	.401255	.58	42	.599089	795	.400913	30
	8 17	.600332	790	.399668	.55	45	.600677	792	.399323	43
	10 30	.601913	788	.398087	.52	48	.602261	789	.397739	30
	12 18	.603489	785	.396511	.50	50	.603839	786	.396161	42
	14 30	.605058	782	.394942	.47	53	.605411	783	.394589	30
	16 19	.606623	779	.393377	.45	55	.606978	780	.393023	41
	18 30	.608181	776	.391810	.42	58	.608539	777	.391461	30
	20 20	.609734	774	.390260	.40	60	.610094	775	.389906	40
	22 2	.611281	771	.388719	.37	63	.611644	772	.388356	30
	24 21	.612824	768	.387176	.35	65	.613189	769	.386811	39
	26 30	.614360	765	.385640	.32	68	.614728	767	.385272	30
	28 22	.615891	763	.384109	.29	71	.616262	764	.383738	38
	30 30	.617417	760	.382583	.27	73	.617790	761	.382210	30
	32 23	.618937	757	.381063	.24	76	.619313	758	.380687	37
	34 30	.620452	755	.379548	.22	78	.620830	756	.379170	30
	36 24	.621962	752	.378038	.19	81	.622343	753	.377657	36
	38 30	.623466	749	.376534	.16	84	.623850	751	.376150	30
	40 25	.624965	747	.375035	.13	87	.625352	748	.374645	35
	42 30	.626459	744	.373541	.11	89	.626848	746	.373152	30
	44 20	.627948	742	.372052	.08	92	.628340	743	.371660	34
	46 30	.629432	739	.370568	.05	95	.629827	740	.370173	30
	48 27	.630911	737	.369080	.03	97	.631308	738	.368692	33
	50 30	.632385	734	.367615	.00	0.000400	.632785	735	.367215	30
	52 28	.633854	732	.366146	0.999508	.02	.634256	733	.365744	32
	54 30	.635318	729	.364682	.95	05	.635723	731	.364277	30
	56 29	.636776	727	.363224	.92	08	.637184	729	.362816	31
	58 30	.638230	725	.361770	.89	11	.638641	726	.361359	30
9	00 30	8.639680	723	1.360320	0.999587	0.000413	8.640093	720	1.359907	30

6° 30'

1° - 4' 1° - 4'

87°

1° — 15' 1° — 15' 1° — 15° 177° 11°

Hours.		Deg.		L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.		Hours.	
m	s	'	"									'	"	m	s
10	0	30		8.639680		1.360320	9.999587	0.000413	8.640093		1.359907	30		49	0
	2	30		.641124	722	.358876	.84	16	.641540	723	.358460	30			36
	4	31		.642563	717	.357437	.81	19	.642982	719	.357018	29			54
	6	30		.643998	715	.356002	.78	22	.644420	716	.355580	29			54
	8	32		.645428	713	.354572	.75	25	.645853	714	.354147	28			52
	10	30		.646853	710	.353147	.72	28	.647281	711	.352719	30			50
	12	33		.648274	708	.351726	.70	30	.648704	709	.351296	27			48
	14	34		.649690	706	.350310	.67	33	.650123	707	.349877	27			46
	16	34		.651102	703	.348898	.64	36	.651538	704	.349462	26			44
	18	30		.652508	701	.347492	.61	39	.652947	702	.349053	30			42
	20	35		.653911	698	.346089	.59	41	.654352	700	.348648	25			40
	22	36		.655308	697	.344692	.55	45	.655753	698	.348247	24			38
	24	36		.656702	694	.343298	.53	47	.657149	696	.347851	24			36
	26	36		.658091	692	.341909	.50	50	.658541	693	.347459	23			34
	28	37		.659475	690	.340525	.47	53	.659928	691	.347072	23			32
	30	30		.660855	687	.339145	.44	56	.661311	689	.346689	30			30
	32	38		.662230	685	.337770	.41	59	.662699	687	.346311	22			28
	34	34		.663601	685	.336399	.38	62	.664003	685	.345937	30			26
	36	39		.664969	684	.335031	.35	64	.665433	683	.345567	21			24
	38	30		.666331	681	.333669	.32	68	.666799	680	.345201	30			22
	40	40		.667689	677	.332311	.29	71	.668160	678	.344840	20			20
	42	30		.669043	675	.330957	.26	74	.669517	676	.344483	30			18
	44	41		.670393	673	.329607	.23	77	.670870	674	.344130	19			16
	46	44		.671739	673	.328261	.21	79	.672218	672	.343782	30			14
	48	42		.673081	671	.326919	.18	82	.673563	670	.343437	18			12
	50	30		.674418	666	.325582	.15	85	.674903	668	.343097	30			10
	52	43		.675751	664	.324249	.12	88	.676239	666	.342761	17			8
	54	34		.677080	664	.322920	.09	91	.677571	666	.342429	6			6
	56	44		.678405	662	.321595	.06	94	.678899	664	.342101	16			4
	58	30		.679727	661	.320273	.03	97	.680224	662	.341776	30			2
11	0	45		.681044	656	.318956	.00	100	.681544	658	.341456	15		49	0
	2	30		.682356	656	.317644	.999496	.04	.682860	658	.341140	30			58
	4	46		.683665	654	.316335	.93	.07	.684172	656	.340828	14			56
	6	30		.684971	653	.315029	.91	.09	.685489	652	.340520	30			54
	8	47		.686272	648	.313728	.88	.12	.686804	650	.340216	13			52
	10	30		.687569	647	.312431	.84	.16	.688125	648	.340015	30			50
	12	48		.688862	645	.311138	.81	.19	.689431	646	.340019	12			48
	14	34		.690152	643	.309848	.78	.22	.690728	644	.340026	30			46
	16	49		.691438	641	.308562	.75	.25	.692023	642	.340037	11			44
	18	30		.692720	639	.307280	.72	.28	.693318	640	.340052	30			42
	20	50		.693998	637	.306002	.69	.31	.694620	639	.340071	10			40
	22	36		.695273	635	.304727	.66	.34	.695907	637	.340093	30			38
	24	51		.696543	633	.303457	.62	.38	.697081	635	.340119	9			36
	26	30		.697810	631	.302190	.59	.41	.698251	633	.340149	30			34
	28	52		.699073	630	.300927	.56	.44	.699417	631	.340183	8			32
	30	30		.700333	628	.299667	.53	.47	.700580	629	.340220	30			30
	32	53		.701589	626	.298411	.50	.50	.701739	628	.340261	7			28
	34	34		.702841	624	.297159	.47	.53	.702894	626	.340306	30			26
	36	54		.704090	622	.295910	.44	.56	.704046	624	.340354	6			24
	38	30		.705335	621	.294665	.40	.60	.705205	622	.340405	30			22
	40	55		.706577	619	.293423	.37	.63	.707140	620	.340460	5			20
	42	30		.707815	617	.292185	.34	.66	.708381	619	.340519	30			18
	44	56		.709049	615	.290951	.31	.69	.709618	617	.340582	4			16
	46	30		.710280	614	.289720	.27	.73	.710853	615	.340647	30			14
	48	57		.711507	612	.288493	.24	.76	.712083	614	.340717	3			12
	50	30		.712732	610	.287268	.21	.79	.713311	612	.340789	30			10
	52	58		.713952	608	.286048	.18	.82	.714534	610	.340866	2			8
	54	30		.715169	607	.284831	.14	.86	.715755	609	.340946	30			6
	56	59		.716383	607	.283617	.11	.89	.716972	609	.341028	1			4
	58	30		.717593	605	.282407	.08	.92	.718185	607	.341115	30			2
	60	30		.718800	603	.281200	.04	.96	.719396	605	.341206	0		48	0
Hours.	m	s	'	L. Sin.	Diff. for 15' or 1"	L. Sec.	L. Sin.	L. Cossec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	'	"	m	s

TABLE II.—LOG. SINES, TANG'S, &c.

0° 30'		1° - 15' 1" - 15' 1" - 15°					176° 11'				
Hours.	Deg.	L. Sin.	Diff. for 15" or 1'	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours.
12	0 0	8.718800	602	1.281200	9.999404	0.000506	8.719396	603	1.280604	60	47 00
	30	730004	600	279096	01	99	729003	601	279307	59	58
	4 1	731204	598	278796	999398	000602	728106	600	278194	59	50
	6 30	732401	597	277599	94	06	723007	598	276993	58	54
	8 2	733545	595	276405	91	09	724204	596	275796	58	52
	10 30	734785	593	275215	88	12	725397	595	274603	30	50
	12 3	735978	592	274028	84	16	726588	593	273412	57	48
	14 14	737158	592	272844	81	19	727775	592	272225	30	46
	16 4	738337	590	271663	78	22	728959	592	271041	56	30
	18 30	739514	588	270486	74	26	730140	590	269860	30	44
	20 5	740688	587	269312	71	29	731317	588	268683	55	40
	22 30	741859	585	268141	67	33	732498	587	267508	30	38
	24 6	743027	584	266973	64	36	733663	585	266337	54	36
	26 30	744192	582	265808	61	39	734831	584	265169	30	34
	28 7	745353	581	264647	57	43	735996	582	264004	53	32
	30 30	746512	579	263488	54	46	737158	581	262842	30	30
	32 8	747667	577	262333	50	50	738317	579	261683	32	30
	34 34	748820	575	261180	47	53	739473	577	260527	30	28
	36 9	749969	573	260031	43	57	740626	575	259374	51	34
	38 30	751115	572	258885	40	60	741775	573	258225	30	22
	40 10	752259	570	257741	37	63	742922	572	257078	50	20
	42 30	753399	568	256601	33	67	744066	570	255934	30	18
	44 11	754536	567	255464	29	71	745207	568	254793	49	16
	46 46	755670	566	254330	26	74	746344	567	253656	30	14
	48 12	756801	564	253199	22	78	747479	566	252521	48	12
	50 30	757930	562	252070	19	81	748611	564	251389	30	10
	52 13	759055	561	250945	15	85	749740	563	250260	47	8
	54 54	760178	559	249822	12	88	750866	561	249134	30	6
	56 14	761297	558	248703	08	92	751989	560	248011	46	4
	58 30	762414	557	247586	04	96	753110	558	246890	30	2
13	0 15	763528	555	246472	01	99	754227	557	245773	45	47 0
	2 16	764639	554	245361	999297	000703	755342	556	244658	30	58
	4 6	765747	552	244253	94	06	756453	554	243547	44	30
	6 30	766852	551	243148	90	10	757562	553	242438	30	54
	8 17	767955	549	242045	87	13	758668	551	241332	43	52
	10 30	769054	548	240946	83	17	759771	550	240229	30	50
	12 18	770151	547	239849	79	21	760872	549	239128	42	48
	14 14	771245	546	238755	75	25	761970	547	238030	30	46
	16 19	772337	544	237663	72	28	763065	546	236935	41	44
	18 30	773425	543	236575	68	32	764157	544	235843	30	42
	20 30	774511	541	235489	65	35	765246	543	234754	40	40
	22 30	775594	540	234406	61	39	766333	542	233667	30	38
	24 21	776675	539	233325	57	43	767418	541	232582	39	36
	26 30	777753	538	232247	54	46	768499	539	231501	30	34
	28 22	778828	537	231172	50	50	769578	538	230422	38	32
	30 30	779900	535	230100	46	54	770654	536	229346	30	30
	32 23	770970	533	229030	43	57	771727	535	228273	37	28
	34 34	772037	532	227963	39	61	772798	534	227202	30	26
	36 24	773101	531	226899	35	65	773866	533	226134	36	24
	38 30	774163	530	225837	31	69	774932	531	225068	30	22
	40 25	775223	528	224777	28	72	775995	530	224005	35	20
	42 19	776279	527	223721	24	77	777056	529	222944	30	18
	44 9	777334	526	222668	20	80	778114	527	221886	34	16
	46 46	778385	524	221615	16	84	779169	526	220831	30	14
	48 27	779434	523	220566	12	88	780222	525	219776	33	12
	50 30	780480	522	219520	08	92	781272	524	218729	30	10
	52 28	781525	520	218475	05	95	782320	522	217690	32	8
	54 54	782566	519	217434	01	99	783365	521	216653	30	6
	56 29	783605	518	216395	999197	000803	784408	520	215619	31	4
	58 30	784641	517	215359	93	07	785448	519	214582	30	2
	13 60 30	8.785675	517	1.214225	9.999189	0.000811	8.786486	519	1.213514	30	46 0

6° 30'

1° - 4' 10" - 4°

86° 5'

TABLE II.—LOG. SINES, TANG'S, &C.

30

1° - 15' 1° - 15' 1° - 15'

170° 11°

Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours
30	8.785675	516	1.214325	9.999189	0.000811	8.786486	518	1.213514	30	45
30	.786707	514	.213203	.85	15	.787522	516	.212478	30	46
31	.787736	513	.212264	.82	18	.788554	515	.211446	29	50
30	.788763	512	.211327	.78	22	.789585	514	.210415	30	54
32	.789787	511	.210393	.74	26	.790613	513	.209387	28	52
30	.790809	509	.209461	.70	30	.791639	512	.208361	30	58
33	.791828	508	.208532	.66	34	.792662	510	.207338	27	30
30	.792845	507	.207605	.62	38	.793683	509	.206317	30	46
34	.793859	506	.206680	.58	42	.794701	508	.205299	26	30
30	.794872	505	.205758	.54	46	.795718	507	.204282	30	42
35	.795881	504	.204841	.50	50	.796731	506	.203269	25	40
30	.796889	502	.203928	.46	54	.797743	504	.202257	30	46
36	.797894	501	.203016	.42	58	.798752	503	.201248	24	30
30	.798897	500	.202103	.38	62	.799759	502	.200241	30	34
37	.799897	499	.201193	.34	66	.800762	501	.199237	23	28
30	.800896	498	.199104	.30	70	.801766	500	.198234	30	30
38	.801891	497	.198109	.26	74	.802765	499	.197235	22	28
30	.802885	497	.197115	.22	78	.803763	497	.196237	30	28
39	.803876	495	.196124	.18	82	.804758	496	.195242	21	24
30	.804865	493	.195135	.14	86	.805751	495	.194249	30	28
40	.805852	492	.194148	.10	90	.806742	494	.193258	20	30
30	.806837	491	.193163	.06	94	.807731	493	.192269	30	18
41	.807819	490	.192181	.02	98	.808717	492	.191283	19	16
30	.808799	489	.191201	.999098	-0.000902	.809701	491	.190299	30	14
42	.809777	488	.190223	.94	05	.810683	490	.189317	18	12
30	.810753	487	.189247	.90	10	.811663	489	.188337	30	10
43	.811727	485	.188273	.86	14	.812641	487	.187359	17	08
30	.812708	484	.187302	.82	18	.813616	486	.186384	30	06
44	.813687	483	.186333	.78	22	.814589	486	.185411	16	04
30	.814664	482	.185366	.73	27	.815561	484	.184439	30	02
45	.815638	481	.184402	.69	31	.816529	483	.183471	15	00
30	.816614	480	.183433	.65	35	.817496	482	.182504	30	58
46	.817592	479	.182478	.61	39	.818461	481	.181539	14	56
30	.818569	478	.181529	.57	43	.819423	480	.180577	30	54
47	.819543	477	.180584	.52	48	.820384	479	.179616	13	52
30	.820519	476	.179640	.48	52	.821342	478	.178658	30	50
48	.821492	475	.178695	.44	56	.822298	477	.177702	12	48
30	.822463	474	.177757	.40	60	.823253	476	.176747	30	46
49	.823431	473	.176809	.36	64	.824205	475	.175795	11	44
30	.824396	472	.175864	.31	69	.825155	474	.174845	30	42
50	.825359	471	.174922	.27	73	.826103	473	.173897	10	40
30	.826319	470	.173982	.23	77	.827049	471	.172951	30	38
51	.827276	469	.173043	.19	81	.827992	471	.172008	9	36
30	.828230	467	.172105	.15	85	.828934	470	.171066	30	34
52	.829181	467	.171168	.10	90	.829874	469	.170126	8	32
30	.830129	466	.170232	.06	94	.830812	468	.169188	30	30
53	.831075	464	.169297	.02	98	.831748	467	.168252	7	28
30	.832018	464	.168362	.998997	-0.001003	.832682	466	.167318	30	26
54	.832957	463	.167428	.93	07	.833614	465	.166386	6	24
30	.833892	462	.166495	.89	11	.834543	464	.165457	30	22
55	.834823	460	.165564	.85	15	.835471	463	.164529	5	20
30	.835757	460	.164633	.80	20	.836397	462	.163603	30	18
56	.836687	459	.163703	.76	24	.837321	461	.162679	4	16
30	.837615	457	.162775	.72	28	.838243	461	.161757	30	14
57	.838540	457	.161849	.67	33	.839163	460	.160837	3	12
30	.839464	456	.160925	.63	37	.840081	459	.159919	30	10
58	.840386	455	.160004	.58	42	.841008	458	.159002	2	8
30	.841306	455	.159084	.54	46	.841932	457	.158088	30	6
59	.842224	454	.158165	.50	50	.842854	456	.157176	1	4
30	.843140	453	.157248	.45	55	.843773	455	.156265	30	2
60	8.843585	452	1.156415	9.998941	0.001059	8.844644	454	1.155356	0	0

93°

1° - 4' 1° - 4'

86° 5'

TABLE II.—LOG. SINES, TANG'S, &C.

0°		4°		1° - 15' 1" - 15' 1" - 15°				175°		11°			
Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.		Hours.	
										'	''		'
16	0	8.843585	451	1.150415	9.998941	0.001059	8.844.44	453	1.153356	60		43	60
	2	.844487	450	.155513	36	64	.845551	452	.154449	30			58
	4	.845387	449	.154613	32	68	.846455	451	.153545	59			56
	6	.846286	448	.153714	27	73	.847353	450	.152641	58			54
	8	.847183	447	.152817	23	77	.848260	449	.151740	58			52
	10	.848078	446	.151922	19	81	.849159	449	.150841	30			50
	12	.848971	445	.151023	14	86	.850057	447	.149943	57			48
	14	.849862	444	.150138	10	90	.850952	447	.149048	30			46
	16	.850751	444	.149249	05	95	.851846	447	.148154	53			44
	18	.851639	443	.148361	01	99	.852738	446	.147262	30			42
	20	.852524	442	.147476	998969	0.001104	.853626	444	.146372	55			40
	22	.853409	441	.146591	92	03	.854517	444	.145483	30			38
	24	.854290	440	.145710	87	13	.855403	443	.144597	54			36
	26	.855171	440	.144832	83	17	.856288	442	.143712	30			34
	28	.856049	439	.143951	78	22	.857171	441	.142829	53			32
	30	.856926	437	.143074	73	27	.858053	439	.141947	30			30
	32	.857801	436	.142199	69	31	.858932	439	.141062	52			28
	34	.858674	436	.141328	64	36	.859810	438	.140180	30			26
	36	.859546	434	.140454	60	40	.860686	437	.139314	51			24
	38	.860415	434	.139585	55	45	.861560	436	.138440	30			22
	40	.861283	433	.138717	50	50	.862433	435	.137567	50			20
	42	.862150	432	.137850	46	54	.863304	434	.136696	30			18
	44	.863014	431	.136986	41	59	.864173	433	.135827	49			16
	46	.863877	430	.136123	37	63	.865040	433	.134960	30			14
	48	.864738	429	.135262	32	68	.865906	432	.134094	48			12
	50	.865597	429	.134403	27	73	.866770	431	.133230	30			10
	52	.866455	428	.133545	23	77	.867632	430	.132368	47			8
	54	.867310	427	.132690	18	82	.868492	429	.131508	30			6
	56	.868165	426	.131835	14	86	.869351	428	.130649	46			4
	58	.869017	425	.130983	09	91	.870208	428	.129792	30			2
17	0	.869868	424	.130132	04	96	.871064	427	.128936	45		43	0
	2	.870717	424	.129283	998799	0.001301	.871918	425	.128082	30			58
	4	.871565	423	.128435	95	05	.872770	425	.127227	44			56
	6	.872411	422	.127589	90	10	.873621	424	.126379	30			54
	8	.873255	421	.126745	85	15	.874470	423	.125530	43			52
	10	.874097	420	.125903	80	20	.875317	422	.124683	30			50
	12	.874938	419	.125062	76	24	.876162	422	.123833	42			48
	14	.875777	419	.124223	71	29	.877006	421	.122994	30			46
	16	.876615	418	.123385	66	34	.877849	420	.122151	11			44
	18	.877451	417	.122549	61	39	.878690	419	.121310	30			42
	20	.878286	416	.121714	57	43	.879529	418	.120471	40			40
	22	.879118	415	.120882	52	48	.880366	418	.119634	30			38
	24	.879949	415	.120051	47	53	.881202	417	.118798	39			36
	26	.880779	414	.119221	42	58	.882037	417	.117963	30			34
	28	.881607	413	.118393	37	63	.882870	416	.117130	38			32
	30	.882433	413	.117567	32	68	.883701	414	.116299	30			30
	32	.883258	411	.116742	28	72	.884530	414	.115470	37			28
	34	.884081	411	.115919	23	77	.885358	414	.114642	30			26
	36	.884903	411	.115097	18	82	.886185	413	.113815	36			24
	38	.885723	409	.114277	13	87	.887010	412	.112990	30			22
	40	.886542	408	.113458	09	91	.887833	411	.112167	35			20
	42	.887359	407	.112641	04	96	.888655	410	.111345	30			18
	44	.888174	407	.111826	998698	0.001302	.889476	409	.110524	34			16
	46	.888988	406	.111012	94	05	.890294	409	.109706	30			14
	48	.889801	405	.110199	89	11	.891112	408	.108888	33			12
	50	.890612	404	.109388	84	16	.891922	407	.108072	30			10
	52	.891421	404	.108579	79	21	.892727	407	.107258	32			8
	54	.892229	403	.107771	74	26	.893535	405	.106445	30			6
	56	.893035	402	.106965	69	31	.894336	405	.105634	31			4
	58	.893840	401	.106160	64	36	.895137	404	.104824	30			2
	60	.894643	401	.105357	998659	0.001341	.895931	404	.104017	30		43	0

6° 91°

1° - 4' 10° - 4°

85° 5°

E

0°		40		1° = 15' 1" = 15' 1" = 15°					175°		11°	
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
" "	" "	" "	" "	" "	" "	" "	" "	" "	" "	" "	" "	
18	0	8.894643	401	1.103357	9.998658	0.001341	8.89584	403	1.104016	30	41	
	2	88.5445	400	.104535	.54	.46	896761	402	.103899	30	42	
	4	88.2445	3.9	.103755	.49	.51	897586	402	.103404	29	43	
	6	87.9744	398	.102450	.44	.56	898400	401	.101600	30	44	
	8	87.7842	398	.102158	.39	.61	899203	400	.100797	28	45	
	10	87.6638	397	.101362	.34	.66	900004	399	.999996	30	46	
	12	87.60432	396	.100568	.29	.71	900803	398	.999197	27	47	
	14	87.60225	396	.999775	.24	.76	901601	398	.998399	30	48	
	16	87.60117	365	.998983	.19	.81	902398	397	.997602	26	49	
	18	87.60187	344	.998193	.14	.86	903193	397	.996807	30	50	
	20	87.62596	393	.997404	.09	.91	903987	396	.996013	25	51	
	22	87.6383	393	.996617	.04	.96	904779	395	.995221	30	52	
	24	87.64169	392	.995831	.998599	.001401	905570	394	.994430	24	53	
	26	87.64453	391	.995047	.94	.06	906359	394	.993641	30	54	
	28	87.64736	390	.994264	.89	.11	907147	393	.992853	23	55	
	30	87.6517	390	.993483	.83	.17	907934	392	.992066	30	56	
	32	87.65497	389	.992703	.78	.22	908719	392	.991281	22	57	
	34	87.65776	388	.991924	.73	.27	909503	391	.990497	30	58	
	36	87.65853	388	.991147	.68	.32	910288	390	.989715	21	59	
	38	87.65929	387	.990371	.63	.37	911066	390	.988934	30	60	
	40	87.66104	386	.989596	.58	.42	911846	389	.988154	30	61	
	42	87.66177	386	.988823	.53	.47	912624	388	.987376	30	62	
	44	87.66199	385	.988051	.48	.52	913401	388	.986599	19	63	
	46	87.66179	384	.987281	.42	.58	914177	387	.985823	30	64	
	48	87.66148	384	.986512	.37	.63	914951	386	.985049	18	65	
	50	87.66105	383	.985744	.32	.68	915724	385	.984276	30	66	
	52	87.66052	382	.984978	.27	.73	916495	385	.983505	17	67	
	54	87.66000	382	.984214	.21	.79	917265	385	.982735	30	68	
	56	87.65950	382	.983450	.16	.84	918034	384	.981966	16	69	
	58	87.65902	381	.982688	.11	.89	918801	383	.981199	30	70	
	60	87.65858	380	.981927	.06	.94	919567	382	.980433	15	71	
19	0	87.65813	380	.981167	.01	.99	920332	382	.979668	30	72	
	2	87.65769	379	.980409	.998495	.001505	921096	382	.978904	14	73	
	4	87.65726	378	.979652	.00	.10	921858	381	.978142	30	74	
	6	87.65683	377	.978896	.85	.15	922619	380	.977381	13	75	
	8	87.65640	377	.978142	.80	.20	923378	379	.976622	30	76	
	10	87.65600	376	.977380	.74	.26	924136	378	.975864	12	77	
	12	87.65562	376	.976638	.69	.31	924893	378	.975107	30	78	
	14	87.65526	375	.975898	.63	.37	925649	377	.974351	11	79	
	16	87.65492	374	.975159	.58	.42	926403	376	.973597	30	80	
	18	87.65460	374	.974421	.53	.47	927156	376	.972844	10	81	
	20	87.65429	373	.973685	.47	.53	927908	375	.972092	30	82	
	22	87.65400	372	.972950	.42	.58	928658	375	.971342	9	83	
	24	87.65372	372	.972216	.37	.63	929407	374	.970593	30	84	
	26	87.65346	371	.971483	.32	.68	930155	373	.969845	8	85	
	28	87.65322	370	.970752	.26	.74	930902	372	.969098	7	86	
	30	87.65300	369	.970022	.21	.79	931647	372	.968353	30	87	
	32	87.65280	369	.969294	.15	.85	932391	371	.967609	30	88	
	34	87.65262	368	.968568	.10	.90	933134	371	.966866	6	89	
	36	87.65246	367	.967844	.04	.96	933876	370	.966124	30	90	
	38	87.65232	367	.967122	.998399	.001601	934618	369	.965384	5	91	
	40	87.65220	367	.966402	.94	.00	935355	369	.964645	30	92	
	42	87.65210	366	.965683	.88	.06	936093	368	.963907	4	93	
	44	87.65202	365	.964965	.83	.12	936829	368	.963171	30	94	
	46	87.65196	365	.964248	.77	.17	937565	368	.962435	2	95	
	48	87.65192	364	.963532	.72	.23	938299	367	.961701	30	96	
	50	87.65190	363	.962818	.66	.29	939032	366	.960968	2	97	
	52	87.65189	363	.962105	.61	.34	939764	366	.960236	30	98	
	54	87.65190	362	.961393	.55	.40	940495	365	.959505	1	99	
	56	87.65192	362	.960682	.50	.45	941224	365	.958776	30	100	
	58	87.65195	361	.959972	.45	.50	941952	364	.958048	0	101	
	60	87.65200	361	.959264	.40	.55	942679	364	.957322	30	102	
19	0	8.940296		1.039704	9.998344	0.001656	8.941532		1.058048	0	103	

91 1° - 1' 10" = 4" 53° 34

0° 50'		1° — 15' 1" — 15' 1" — 15°						174°		11°		
Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cosec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.	
20	0 0	8.940296	361	1.030704	9.998344	0.001656	8.941932	363	1.058048	60	39	60
	2	.941014	360	.038982	.39	61	.942679	362	.057321	30		58
	4	.941738	359	.058292	.33	67	.943405	363	.056505	39		56
	6	.942457	358	.057543	.28	72	.944139	362	.055871	30		54
	8	.943174	358	.056826	.22	78	.944882	361	.055148	58		52
			358					361				
	10	.943891	357	.056100	.17	83	.945574	360	.054426	30		50
	12	.944606	357	.055394	.11	89	.946295	360	.053705	57		48
	14	.945329	357	.054680	.05	95	.947015	360	.052985	30		46
	16	.946031	357	.053998	.00	0.017000	.947734	359	.052266	56		44
	18	.946745	355	.053253	.998294	.06	.948451	358	.051549	30		42
			355					358				
	20	.947456	355	.052544	.88	12	.949168	357	.050832	55		40
	22	.948166	354	.051834	.83	17	.949883	357	.050117	30		38
	24	.948874	353	.051127	.77	23	.950597	356	.049403	54		36
	26	.949581	353	.050419	.72	28	.951309	356	.048691	30		34
	28	.950287	352	.049713	.66	34	.952021	355	.047979	53		32
			352					355				
	30	.950992	352	.049008	.60	40	.952732	354	.047268	30		30
	32	.951696	351	.048304	.55	45	.953441	354	.046559	52		28
	34	.952398	351	.047602	.49	51	.954149	354	.045851	30		26
	36	.953100	350	.046900	.43	57	.954857	353	.045143	51		24
	38	.953809	349	.046200	.38	62	.955562	352	.044438	30		22
			349					352				
	40	.954499	349	.045501	.32	68	.956267	352	.043733	50		20
	42	.955197	348	.044803	.26	74	.956971	351	.043029	30		18
	44	.955894	348	.044106	.20	80	.957674	350	.042326	49		16
	46	.956590	347	.043410	.15	85	.958375	350	.041625	30		14
	48	.957284	347	.042716	.09	91	.959075	350	.040925	48		12
			347					350				
	50	.957978	346	.042022	.03	97	.959775	349	.040225	30		10
	52	.958670	346	.041330	.998197	.001803	.960473	348	.039527	47		8
	54	.959362	345	.040638	.92	08	.961170	348	.038830	30		6
	56	.960052	344	.039948	.86	14	.961866	347	.038134	46		4
	58	.960741	344	.039259	.80	20	.962561	347	.037439	30		2
			344					347				
21	0 15	.961429	343	.038571	.74	26	.963255	346	.036745	45	39	0
	2	.962118	343	.037884	.69	31	.963947	346	.036053	30		58
	4	.962802	342	.037198	.63	37	.964639	345	.035361	44		56
	6	.963486	342	.036514	.57	43	.965329	345	.034671	30		54
	8	.964170	341	.035830	.51	49	.966019	344	.033981	43		52
			341					344				
	10	.964852	341	.035148	.45	55	.966707	344	.033293	30		50
	12	.965534	340	.034466	.39	61	.967395	343	.032605	42		48
	14	.966214	340	.033786	.33	67	.968083	342	.031919	30		46
	16	.966893	339	.033107	.27	73	.968766	342	.031234	41		44
	18	.967572	338	.032428	.22	78	.969450	341	.030550	40		42
			338					341				
	20	.968245	338	.031751	.16	84	.970133	341	.029867	40		40
	22	.968925	337	.031075	.10	90	.970815	340	.029185	30		38
	24	.969600	337	.030400	.04	96	.971496	340	.028504	39		36
	26	.970274	337	.029726	.998098	.001902	.972176	340	.027824	30		34
	28	.970947	336	.029053	.92	08	.972855	339	.027145	38		32
			336					339				
	30	.971619	336	.028381	.86	14	.973533	338	.026467	30		30
	32	.972289	335	.027711	.80	20	.974209	338	.025791	37		28
	34	.972953	335	.027041	.74	26	.974885	337	.025115	30		26
	36	.973628	334	.026372	.68	32	.975560	337	.024440	36		24
	38	.974306	333	.025704	.62	38	.976234	336	.023766	30		22
			333					336				
	40	.974982	333	.025038	.56	44	.976906	335	.023094	35		20
	42	.975658	332	.024372	.50	50	.977578	335	.022422	30		18
	44	.976332	332	.023707	.44	56	.978248	335	.021752	34		16
	46	.976995	331	.023044	.38	62	.978918	334	.021082	30		14
	48	.977659	330	.022381	.32	68	.979587	333	.020413	33		12
			330					333				
	50	.978320	330	.021720	.26	74	.980254	332	.019740	30		10
	52	.978981	329	.021059	.20	80	.980921	332	.019079	32		8
	54	.979640	329	.020400	.14	86	.981586	332	.018414	30		6
	56	.980299	328	.019741	.08	92	.982251	331	.017749	31		4
	58	.980956	328	.019084	.02	98	.982914	331	.017086	30		2
	21	8 981573	328	1.018427	9.997996	0.002004	8.983577	331	1.016423	30	38	0
Hours.	Deg.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Sin.	L. Cosec.	L. Cot.	Diff. for 15'' or 1'	L. Tang.	Deg.	Hours.	

TABLE II.—LOG. SINES, TANG'S, &c.

Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.		Hours.	
									1	2	m	s
30	8.981373	327	1.018427	9.997936	0.002004	8.983577	331	1.016423	30	37	00	00
	.982245	327	.017772	.99	10	.984238	330	.015762			50	00
	.982823	327	.017117	.84	16	.984899	330	.015101	23	30	56	50
	.983537	32	.016463	.78	22	.985559	329	.014441	30	30	54	54
	.984189	325	.015811	.72	28	.986217	329	.013783	28	30	52	52
30	.984840	325	.015160	.65	35	.986875	329	.013125	30	30	50	50
	.985491	325	.014509	.59	41	.987532	327	.012468	27	30	48	48
	.986140	324	.013860	.53	47	.988187	327	.011813	30	30	46	46
	.986789	324	.013211	.47	53	.988842	327	.011158	28	30	44	44
30	.987437	323	.012563	.41	59	.989496	326	.010504	25	30	42	42
	.988084	323	.011916	.35	65	.990149	326	.009851	23	30	40	40
	.988729	322	.011271	.28	72	.990801	325	.009199	30	30	38	38
	.989374	321	.010626	.22	78	.991452	325	.008546	34	30	36	36
30	.990017	321	.009983	.16	84	.992101	324	.007899	30	30	34	34
	.990660	321	.009340	.10	90	.992750	324	.007250	23	30	32	32
	.991302	320	.008698	.04	96	.993398	323	.006602	30	30	30	30
30	.991943	320	.008057	.997898	.002102	.994045	323	.005955	22	30	28	28
	.992583	319	.007417	.91	03	.994692	322	.005308		30	26	26
	.993222	319	.006778	.85	15	.995337	322	.004663	31	30	24	24
30	.993860	318	.006140	.79	21	.995981	321	.004019	30	30	22	22
	.994497	318	.005503	.73	27	.996624	321	.003376	30	30	20	20
	.995133	317	.004867	.66	34	.997267	320	.002733	30	30	18	18
	.995768	317	.004232	.60	40	.997908	320	.002092	19	30	16	16
30	.996402	317	.003598	.53	47	.998549	320	.001451	30	30	14	14
	.997035	316	.002965	.47	53	.999188	319	.000812	18	30	12	12
	.997668	316	.002332	.41	59	.999827	319	.000173	30	30	10	10
	.998300	315	.001700	.35	65	.999465	318	.009535	17	30	8	8
	.998930	315	.001070	.28	72	.999102	318	.998898	30	30	6	6
	.999550	314	.000440	.22	78	.998738	317	.998262	16	30	4	4
30	9.000188	314	0.999812	.16	84	.998372	317	.997625	30	30	2	2
	.000816	313	.999154	.09	91	.998007	316	.996993	15	30	0	0
	.001443	313	.998537	.03	97	.997640	316	.996360		30	58	58
30	.002069	312	.997931	.997797	.002303	.997272	316	.995725	14	30	56	56
	.002694	312	.997306	.90	10	.996904	315	.995096		30	54	54
30	.003318	311	.996682	.84	16	.996534	315	.994463	13	30	52	52
	.003941	311	.996059	.77	23	.996164	314	.993836	30	30	50	50
	.004563	311	.995437	.71	29	.995792	314	.993202	12	30	48	48
30	.005185	310	.994815	.65	35	.995420	313	.992568	30	30	46	46
	.005805	310	.994193	.58	42	.995047	313	.991933	11	30	44	44
30	.006425	309	.993575	.52	48	.994673	313	.991297	30	30	42	42
	.007044	309	.992956	.45	55	.994299	312	.990701	10	30	40	40
	.007662	308	.992332	.39	61	.993923	311	.990077	30	30	38	38
30	.008278	308	.991712	.32	68	.993546	311	.989454	9	30	36	36
	.008895	307	.991105	.26	74	.993169	311	.988831	30	30	34	34
30	.009510	307	.990490	.20	80	.992790	310	.988210	8	30	32	32
	.010124	306	.989876	.13	87	.992411	310	.987589	7	30	30	30
	.010737	306	.989263	.06	94	.992031	309	.986969	7	30	28	28
30	.011350	305	.988650	.00	.002300	.991650	309	.986350	30	30	26	26
	.011961	305	.988039	.997603	.00	.991268	308	.985732	6	30	24	24
	.012572	305	.987428	.87	13	.990885	308	.985115	30	30	22	22
	.013182	305	.986818	.80	20	.990502	308	.984498	5	30	20	20
	.013792	304	.986208	.74	26	.990118	307	.983882	30	30	18	18
	.014400	304	.985600	.67	33	.989733	307	.983267	4	30	16	16
30	.015007	303	.984993	.61	39	.989346	306	.982654	30	30	14	14
	.015613	303	.984387	.54	46	.988959	306	.982041	3	30	12	12
	.016219	302	.983781	.47	53	.988572	305	.981428	30	30	10	10
	.016824	302	.983176	.41	59	.988183	305	.980817	2	30	8	8
30	.017428	301	.982572	.34	66	.987794	304	.980206	30	30	6	6
	.018031	301	.981969	.28	72	.987403	304	.979597	1	30	4	4
	.018633	301	.981367	.21	79	.987012	304	.978988	0	30	2	2
30	9.019234	301	0.980766	.9997614	.0002386	9.021620	304	0.978380	0	30	0	0

TABLE II.—LOG. SINES, TANG'S, &c.

0° 0'

1° - 15' 1° - 15' 1° - 15°

173° 11'

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.	
m	s											m	s
24	0	0.01924	300	9.98076	9.99701	3	0.00238	9.02162	303	0.97830	60	35	00
	1	0.02035	294	9.97595	9.99133	3	23.09	2534	302	7166	50		50
	2	16.32	2.88	8308	7588	3	2412	4044	302	5456	58		52
	3	2.25	2.88	7175	7574	3	2426	5251	301	4749	57		48
	4	4010	2.97	5984	7561	3	2439	6455	300	3545	56		44
	5	5203	296	4707	7548	3	2452	7655	299	2345	55		40
	6	63.06	295	3614	7534	3	2466	8852	298	1148	54		36
	7	75.07	294	2433	7521	3	2479	0.30046	296	969654	53		32
	8	87.44	293	1255	7507	3	2493	1237	297	8763	52		28
	9	99.18	293	0082	7493	3	2507	2425	296	7575	51		24
	10	0.31089	292	9.98911	7480	3	2520	3609	295	6391	50		20
	11	2.257	2.91	7743	7466	3	2534	4791	294	5209	49		16
	12	34.21	2.90	6579	7452	3	2548	5969	294	4031	48		12
	13	45.83	2.89	5417	7437	3	2561	7144	293	2859	47		8
	14	57.41	2.89	4259	7425	3	2575	8316	292	1684	46		4
	15	6.896	2.88	3104	7411	3	2589	9485	291	515	45	35	0
	16	80.48	2.87	1952	7397	3	2603	0.40631	291	95340	44		50
	17	91.97	2.86	80.83	7383	3	2617	1814	291	8186	43		52
	18	0.40342	2.86	9.95658	7369	3	2631	2973	290	7027	42		48
	19	14.85	2.85	8515	7355	3	2645	4130	289	5870	41		44
	20	26.25	2.84	7375	7341	3	2659	5284	288	4716	40		40
	21	37.62	2.83	6238	7327	3	2673	6435	288	35.5	39		36
	22	48.95	2.83	5105	7313	3	2687	7582	287	2412	38		32
	23	60.26	2.82	3974	7299	3	2701	8727	286	1273	37		28
	24	71.54	2.81	2846	7285	3	2715	9869	285	1131	36		24
	25	82.79	2.80	1721	7271	3	2729	0.51008	284	94892	35		20
	26	94.01	2.79	6.959	7257	4	2743	2144	284	8340	34		16
	27	0.50519	2.79	9.94981	7242	4	2758	3277	283	7230	33		12
	28	16.35	2.78	8365	7228	3	2772	4407	282	6123	32		8
	29	27.49	2.77	7251	7214	4	2786	5535	281	5003	31		4
	30	38.59	2.77	6141	7199	3	2801	6660	280	3340	30	34	0
	31	49.60	2.76	5034	7185	3	2815	7781	280	2219	29		56
	32	60.71	2.75	3929	7171	4	2829	8900	279	1100	28		52
	33	71.72	2.75	2828	7156	4	2844	0.60016	278	93984	27		48
	34	82.71	2.74	1729	7141	3	2859	1130	277	8270	26		44
	35	93.67	2.73	6833	7127	4	2873	2240	277	7160	25		40
	36	0.50460	2.73	9.93540	7112	3	2888	3348	276	6052	24		36
	37	15.51	2.72	8449	7098	4	2902	4453	276	5547	23		32
	38	26.38	2.71	7361	7083	4	2917	5556	275	4444	22		28
	39	37.23	2.71	6277	7068	3	2932	6655	274	3345	21		24
	40	48.05	2.70	5194	7054	4	2946	7752	273	2248	20		20
	41	58.85	2.69	4115	7039	4	2961	8846	273	1154	19		16
	42	69.62	2.68	3038	7024	4	2976	9938	272	1002	18		12
	43	80.36	2.68	1964	7009	4	2991	0.71027	271	89273	17		8
	44	91.07	2.67	8803	6994	4	3006	2113	271	7887	16		4
	45	0.70176	2.66	9.92924	6979	4	3021	3197	270	6803	15	33	0
	46	12.42	2.66	8758	6964	4	3036	4278	269	5722	14		56
	47	23.05	2.65	7695	6949	4	3051	5356	269	4644	13		52
	48	33.66	2.64	6634	6934	4	3066	6432	268	3568	12		48
	49	44.24	2.64	5576	6919	4	3081	7505	268	2495	11		44
	50	54.80	2.63	4520	6904	4	3096	8576	267	1424	10		40
	51	65.33	2.62	3467	6889	4	3111	9644	266	336	9		36
	52	75.83	2.62	2417	6873	4	3127	0.80710	265	919290	8		32
	53	86.31	2.61	1369	6858	4	3142	1773	265	8227	7		28
	54	96.76	2.61	334	6843	4	3157	2833	264	7167	6		24
	55	0.80719	2.60	9.91921	6828	4	3172	3891	264	6109	5		20
	56	17.59	2.59	8241	6812	4	3188	4947	263	5053	4		16
	57	27.97	2.59	7303	6797	4	3203	6000	262	4000	3		12
	58	38.32	2.58	6368	6782	4	3218	7050	262	2950	2		8
	59	48.64	2.58	5436	6766	4	3234	8098	261	1902	1		4
	60	9.08595	2.58	9.914105	9.996751	4	0.003249	9.089144	261	0.910856	0	32	0

6° 93° 1° = 4' 15° = 4" 83° 5'

TABLE II.—LOG. SINES, TANG'S, &C.

70		1° - 15' 1° - 15' 1° - 15°				175°		11°			
Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot	Deg	Hours
0	0.003345	257	0.914105	0.997751	4	0.003249	0.089144	261	0.910356	60	31 1/2
1	6.222	253	3078	8735	4	2935	0.090187	240	90313	59	5 1/2
2	7.447	253	9053	6719	4	2921	1228	251	8772	58	3 1/2
3	8970	255	1030	6704	4	2936	2246	253	7734	57	4 1/2
4	9030	254	0010	6688	4	3312	3302	258	6688	56	44
5	0.91008	254	908992	6673	4	3327	4335	258	5665	55	46
6	2034	253	7976	6657	4	3343	5367	257	4633	54	3 1/2
7	3037	252	6963	6641	4	3359	6396	256	3604	53	2 1/2
8	4047	252	5953	6625	4	3375	7422	253	2576	52	2 1/2
9	5058	251	4944	6610	4	3390	8446	253	1554	51	2 1/2
10	6092	251	3938	6594	4	2406	9468	255	0532	50	2 1/2
11	7035	250	2935	6578	4	3422	1.0487	254	894513	49	1 1/2
12	8036	250	1934	6562	4	3438	1504	254	8496	48	1 1/2
13	9085	249	0935	6546	4	3454	2519	253	7481	47	4
14	1.0002	248	893828	6530	4	3470	3532	252	6468	46	4
15	1056	248	8944	6514	4	3486	4542	253	5458	45	3 1/2
16	2042	247	7352	6498	4	3502	5550	251	4450	44	5 1/2
17	3037	247	6363	6481	4	3519	6556	251	3444	43	5 1/2
18	4025	246	5375	6468	4	3534	7559	251	2441	42	5 1/2
19	5010	245	4390	6449	4	3551	8561	250	1431	41	44
20	5992	245	4008	6432	4	3567	9559	249	0441	40	40
21	6973	244	3027	6417	4	3583	1.0556	249	89444	39	3 1/2
22	7951	244	2049	6400	4	3600	1551	248	8443	38	2 1/2
23	8927	243	1073	6384	4	3616	2543	248	7457	37	2 1/2
24	9901	243	0099	6368	4	3632	3533	247	6467	36	24
25	1.10872	242	899128	6351	4	3649	4521	246	5479	35	20
26	1842	242	8159	6335	4	3665	5507	246	4473	34	16
27	2890	241	7191	6318	4	3682	6491	245	3507	33	12 1/2
28	3774	241	6226	6302	4	3698	7472	245	2528	32	8 1/2
29	4737	240	5263	6285	4	3715	8452	244	1548	31	4
30	5698	239	4302	6269	4	3731	9429	244	0571	30	0
31	6656	239	3344	6252	4	3748	1.0404	243	873929	29	5 1/2
32	7612	239	2388	6235	4	3765	1377	243	8223	28	5 1/2
33	8567	238	1433	6219	4	3781	2248	242	7652	27	4 1/2
34	9519	237	0481	6202	4	3798	3217	242	6683	26	4 1/2
35	1.0469	237	879531	6185	4	3815	4184	241	5716	25	40
36	1417	236	8583	6169	4	3832	5149	240	4751	24	3 1/2
37	2369	236	7638	6151	4	3849	6111	240	3783	23	3 1/2
38	3306	235	6694	6134	4	3866	7172	239	2828	22	2 1/2
39	4248	235	5752	6118	4	3882	8130	239	1870	21	24
40	5187	234	4813	6100	4	3900	9087	238	0913	20	20
41	6125	234	3875	6084	4	3916	1.0041	238	8625	19	16
42	7030	233	2940	6066	4	3934	0994	237	8006	18	12 1/2
43	7993	233	2007	6049	4	3951	1944	237	8051	17	8 1/2
44	8925	232	1075	6032	4	3968	2893	236	7107	16	4
45	9854	232	0146	6015	4	3985	3839	236	6161	15	29 0
46	1.0771	231	862919	5998	4	4002	4783	236	5217	14	5 1/2
47	1703	231	8214	5980	4	4020	5725	236	4274	13	5 1/2
48	2430	230	7370	5963	4	4037	6667	235	3333	12	4 1/2
49	3551	230	6449	5946	4	4054	7603	234	2335	11	44
50	4470	229	5530	5928	4	4072	8549	233	1458	10	40
51	5387	229	4613	5911	4	4089	9476	233	0524	9	3 1/2
52	6303	228	3697	5894	4	4106	1.0409	233	8935	8	2 1/2
53	7216	228	2784	5876	4	4124	1340	233	8060	7	2 1/2
54	8128	227	1872	5859	4	4141	2269	232	7231	6	24
55	9037	227	0963	5841	4	4159	3199	231	6804	5	20
56	9945	226	0055	5824	4	4176	4121	231	5879	4	16 1/2
57	1.0850	226	880150	5806	4	4194	5044	230	4956	3	12 1/2
58	1754	225	8246	5788	4	4212	5966	230	4011	2	8 1/2
59	2459	225	7344	5771	4	4237	6885	229	3112	1	4 1/2
60	9.143555	225	8986445	9.995733	4	0.003247	9.147862	229	0.9921	0	0

97°

1° - 15' - 10°

82°

8°

TABLE II.—LOG. SINES, TANG'S, &c.

0° 80		1° - 15' 1° - 15' 1° - 15°							1710 1		
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cos.ec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.
32	0	0.143555	224	0.856445	0.995733	4	0.004247	0.147702	229	0.85218	60
	4	4453	224	5547	5735	4	428.5	8718	228	1322	59
	8	5340	223	4651	5717	4	4283	9032	228	0368	58
	12	6243	223	3757	5699	4	4301	150544	227	049450	57
	16	7136	222	2864	5682	4	4318	1454	227	8546	56
	20	8036	222	1974	5663	4	4337	2263	226	7637	55
	24	8915	222	1085	5646	4	4354	3269	226	6731	54
	28	9802	221	0198	5628	4	4372	4174	226	5826	53
	32	1.0688	221	849314	5609	4	4391	5077	225	4923	52
	36	1569	220	8431	5591	4	4409	5978	225	4022	51
	40	2451	220	7549	5574	4	4426	6877	224	3123	50
	44	3330	219	6670	5555	4	4445	7775	224	2225	49
	48	4206	219	5792	5537	4	4463	8671	223	1321	48
	52	5084	218	4916	5519	4	4481	9555	223	0435	47
	56	5957	218	4043	5500	4	4500	160457	222	839543	46
33	0	6829	218	3171	5482	4	4518	1347	222	8653	45
	4	7700	217	2300	5464	4	4536	2236	222	7764	44
	8	8569	217	1431	5446	4	4554	3123	221	6873	43
	12	9435	216	0565	5427	4	4573	4008	221	5992	42
	16	1.0301	216	839899	5409	4	4591	4892	220	5108	41
	20	1164	215	8836	5390	4	4610	5774	220	4226	40
	24	2121	215	7974	5372	5	4628	6654	219	3340	39
	28	2985	214	7115	5353	4	4647	7532	219	2468	38
	32	3843	214	6257	5334	5	4666	8409	219	1591	37
	36	4690	213	5400	5316	5	4684	9284	218	0716	36
	40	5544	213	4546	5297	4	4703	170157	218	899843	35
	44	6307	213	3693	5278	5	4722	1029	217	8071	34
	48	7159	212	2841	5260	5	4740	1899	217	8101	33
	52	8008	212	1992	5241	5	4757	2767	217	7273	32
	56	8856	211	1144	5222	5	4772	3634	216	6366	31
34	0	9702	211	0298	5203	5	4797	4499	216	5501	30
	4	1.0546	211	899454	5184	5	4811	5369	215	4638	29
	8	1389	210	8611	5165	5	4835	6224	215	3776	28
	12	2230	210	7770	5146	5	4854	7084	215	2910	27
	16	3070	209	6930	5127	5	4873	7943	214	2057	26
	20	3908	209	6092	5108	5	4892	8800	214	1200	25
	24	4744	208	5256	5089	5	4911	9655	213	0345	24
	28	5578	208	4422	5070	5	4930	180508	213	819492	23
	32	6411	208	3590	5051	5	4949	1300	213	8440	22
	36	7243	207	2757	5032	5	4968	2211	212	7789	21
	40	8072	207	1928	5013	5	4987	3059	212	6941	20
	44	8900	207	1100	4993	5	5007	3907	211	6093	19
	48	9727	206	0273	4974	5	5026	4757	211	5247	18
	52	1.0551	206	819449	4954	5	5046	5597	210	4403	17
	56	1374	205	8620	4935	5	5065	6430	210	3561	16
35	0	2196	205	7804	4916	5	5084	7280	210	2720	15
	4	3016	204	6984	4896	5	5104	8120	209	1880	14
	8	3834	204	6166	4877	5	5123	8957	209	1043	13
	12	4648	204	5349	4857	5	5143	9794	209	0202	12
	16	5467	203	4533	4836	5	5162	190029	208	803371	11
	20	6290	203	3720	4818	5	5182	1462	208	8538	10
	24	7092	203	2908	4798	5	5202	2274	207	7706	9
	28	7903	202	2097	4779	5	5221	3124	207	6876	8
	32	8712	202	1288	4759	5	5241	3953	207	6047	7
	36	9519	201	0481	4739	5	5261	4780	206	5220	6
	40	1.0325	201	809675	4719	5	5281	5606	206	4394	5
	44	1130	200	8870	4700	5	5300	6430	206	3570	4
	48	1933	200	8067	4680	5	5320	7253	205	2747	3
	52	2734	200	7266	4660	5	5340	8074	205	1926	2
	56	3534	199	6466	4640	5	5360	8894	204	1105	1
	60	0.194332	199	0.805668	0.994620	5	0.005320	0.197712	204	0.800884	0

0° 90

1° - 4' 1° - 4'

810 1

TABLE II.—LOG. SINES, TANG'S, &c.

90		1° - 15' 1° - 15' 1° - 15°				170°		11°			
deg.	L. Sin.	Diff. for 15' or 1'	L. Cossec.	L. Cos.	Diff. for 15' or 1'	L. Sec.	L. Tang.	Diff. for 15' or 1'	L. Cot.	Deg.	Hours.
0	9.194338		0.805869	0.994620		0.005380	9.193719		0.800228	00	23 0'
1	5139	199	4871	4800	5	5400	900524	204	79471	59	5
2	5925	198	4075	4580	5	5420	1345	203	8555	58	5
3	6719	198	3281	4500	5	5440	2157	203	7641	57	4
4	7511	198	2489	4540	5	5460	2971	203	7022	56	4
5	8302	197	1698	4519	5	5481	3783	202	6217	55	4
6	9091	197	9099	4499	5	5501	4592	202	5408	54	3
7	9879	197	0121	4479	5	5521	5400	202	4600	53	3
8	906866	196	79334	4459	5	5541	6207	201	3793	52	2
9	1451	196	8549	4438	5	5562	7013	201	2987	51	2
10	2235	195	7765	4418	5	5582	7817	200	2183	50	2
11	3017	195	6983	4398	5	5602	8619	200	1381	49	1
12	3797	195	6203	4377	5	5623	9420	200	0580	48	1
13	4577	194	5423	4357	5	5643	91920	199	78970	47	1
14	5354	194	4646	4336	5	5664	1018	199	8022	46	4
15	6131	194	3869	4316	5	5684	1815	199	7185	45	23 0'
16	6906	193	3094	4295	5	5705	2611	198	6328	44	5
17	7679	193	2321	4274	5	5726	3405	198	5455	43	2
18	8452	192	1548	4254	5	5746	4198	198	4562	42	4
19	9222	192	0778	4233	5	5767	4989	197	3611	41	4
20	9991	192	0009	4213	5	5788	5779	197	2691	40	4
21	910760	191	789240	4192	5	5808	6568	197	1728	39	3
22	1528	191	8474	4170	5	5830	7356	196	9644	38	2
23	2302	191	7708	4150	5	5850	8142	196	8552	37	2
24	3055	191	6945	4129	5	5871	8926	196	1074	36	2
25	3818	190	6189	4108	5	5892	9710	195	0290	35	1
26	4579	190	5421	4087	5	5913	90492	195	77250	34	1
27	5338	190	4662	4066	5	5934	1872	195	8723	33	1
28	6097	189	3903	4045	5	5955	2652	194	7948	32	1
29	6854	189	3146	4024	5	5976	3430	194	7170	31	4
30	7609	189	2391	4003	5	5997	4206	194	6394	30	23 0'
31	8364	188	1636	3982	5	6018	4328	193	5618	29	5
32	9118	188	0884	3960	5	6040	5158	193	4844	28	5
33	9868	188	0132	3939	5	6061	5929	193	4071	27	4
34	90618	187	77932	3918	5	6082	6700	193	3300	26	4
35	1367	187	8633	3896	5	6104	7471	192	2529	25	4
36	2115	186	7885	3875	5	6125	8240	192	1760	24	3
37	2861	186	7130	3854	5	6146	9007	192	0993	23	2
38	3606	186	6384	3832	5	6168	9774	191	0226	22	2
39	4350	185	5650	3811	5	6189	90530	191	78961	21	2
40	5092	185	4908	3789	5	6211	1303	190	8697	20	2
41	5833	185	4167	3768	5	6232	2065	190	7935	19	16
42	6572	185	3428	3746	5	6254	2826	190	7174	18	12
43	7311	184	2689	3725	5	6275	3586	190	6414	17	8
44	8048	184	1952	3703	5	6297	4345	189	5655	16	4
45	8784	184	1216	3681	5	6319	5103	189	4907	15	21 0'
46	9519	183	0481	3660	5	6340	5859	189	4141	14	26
47	90252	183	789748	3638	5	6362	6614	188	3386	13	52
48	0984	182	9016	3616	5	6384	7368	189	2639	12	4
49	1714	182	8286	3594	5	6406	8120	188	1880	11	44
50	2444	182	7556	3572	5	6428	8872	187	1129	10	40
51	3172	182	6828	3550	5	6450	9623	187	0378	9	36
52	3899	181	6101	3528	5	6472	940371	187	78989	8	32
53	4625	181	5375	3506	6	6494	1119	186	8891	7	28
54	5349	181	4651	3484	5	6516	1865	186	8135	6	24
55	6072	180	3928	3462	5	6538	2610	186	7390	5	20
56	6794	180	3206	3440	5	6560	3354	186	6646	4	16
57	7515	180	2485	3418	5	6582	4077	185	5903	3	12
58	8235	180	1765	3396	5	6604	4839	185	5161	2	8
59	8953	179	1047	3374	5	6626	5579	185	4421	1	4
60	9.939670	179	0.780330	9.993351	6	0.006649	9.944319		0.783681	0	20 0'
deg.	L. Cos.	Diff. for 15' or 1'	L. Sec.	L. Sin.	Diff. for 15' or 1'	L. Cossec.	L. Cot.	Diff. for 15' or 1'	L. Tang.	Deg.	Hours.

90°

1° - 4' 10 - 4°

60°

8°

TABLE II.—LOG. SINES, TANG'S, &c.

0° 100		1° — 15' 1° — 15' 1° — 15°						160° 11°				
Hours.	Deg.	L. Sin.	Diff. for 15' or 1'	L. Cossec.	L. Cos.	Diff. for 15' or 1'	L. Sec.	L. Tang.	Diff. for 15' or 1'	L. Cot.	Deg.	Hours.
40	0	0.239670	179	0.760330	0.993351	6	0.006649	0.246319	184	0.753681	60	19 00
	4	.240386	179	.759614	.993329	6	.6671	.7057	184	.753943	59	56
	8	.1101	179	.8830	.3307	5	.6693	.7794	184	.2206	59	52
	12	.2	178	.8186	.3284	6	.6716	.8530	183	.1470	57	48
	16	.2586	178	.7474	.3262	5	.6738	.9264	183	.0736	56	44
	20	.3328	177	.6769	.3240	6	.6760	.9998	183	.0002	55	40
	24	.3947	177	.6053	.3217	6	.6783	.30730	183	.72270	54	36
	28	.4656	177	.5344	.3195	5	.6805	.1461	182	.8539	53	32
	32	.5363	177	.4637	.3172	6	.6828	.2191	182	.780	52	28
	36	.6069	176	.3931	.3149	5	.6851	.2920	182	.7080	51	24
	40	.6775	176	.3225	.3127	6	.6873	.3648	181	.6352	50	20
	44	.7472	176	.2522	.3104	6	.6896	.4374	181	.5626	49	16
	48	.8161	175	.1819	.3081	5	.6919	.5100	181	.4900	48	12
	52	.8853	175	.1117	.3059	5	.6941	.5824	181	.4176	47	8
	56	.9533	175	.0417	.3036	6	.6964	.6547	180	.3453	46	4
41	0	.254932	174	.749718	.3013	6	.6987	.7269	180	.2731	45	19 00
	4	.0730	174	.9020	.2990	6	.7010	.7990	180	.2010	44	56
	8	.1677	174	.8323	.2967	6	.7033	.8710	180	.1290	43	52
	12	.2373	173	.7627	.2944	6	.7056	.9439	179	.0571	42	48
	16	.3077	173	.6933	.2921	6	.7079	.30646	179	.739654	41	44
	20	.3761	173	.6239	.2898	6	.7102	.0863	179	.9137	40	40
	24	.4453	173	.5547	.2875	6	.7125	.1578	178	.8492	39	36
	28	.5144	173	.4856	.2852	6	.7148	.2292	178	.7798	38	32
	32	.5834	173	.4166	.2829	6	.7171	.3005	178	.6995	37	28
	36	.6523	172	.3477	.2806	6	.7194	.3717	178	.6283	36	24
	40	.7211	172	.2789	.2783	6	.7217	.4428	177	.5572	35	20
	44	.7898	171	.2102	.2760	6	.7240	.5138	177	.4862	34	16
	48	.8583	171	.1417	.2736	6	.7264	.5847	177	.4153	33	12
	52	.9268	171	.0739	.2713	6	.7287	.6555	176	.3445	32	8
	56	.9951	170	.0049	.2690	6	.7310	.7261	176	.2739	31	4
42	0	.266033	170	.739267	.2666	6	.7334	.7967	176	.2033	30	18 00
	4	.1314	170	.8686	.2643	6	.7357	.8671	176	.1329	29	56
	8	.1994	170	.8006	.2619	6	.7381	.9375	175	.6635	28	52
	12	.2673	169	.7327	.2596	6	.7404	.370077	175	.72923	27	48
	16	.3351	169	.6649	.2572	6	.7428	.0779	175	.6521	26	44
	20	.4027	169	.5973	.2548	6	.7452	.1479	175	.5821	25	40
	24	.4703	168	.5277	.2525	6	.7475	.2178	174	.7822	24	36
	28	.5377	168	.4573	.2501	6	.7499	.2875	174	.7124	23	32
	32	.6051	168	.3849	.2477	6	.7522	.3573	174	.6427	22	28
	36	.6723	168	.3277	.2454	6	.7546	.4269	174	.5731	21	24
	40	.7394	168	.2601	.2430	6	.7570	.4964	174	.5036	20	20
	44	.8035	167	.1935	.2406	6	.7594	.5653	173	.4341	19	16
	48	.8731	167	.1271	.2382	6	.7618	.6352	173	.3648	18	12
	52	.9402	167	.0578	.2359	6	.7641	.7043	173	.2957	17	8
	56	.370039	166	.783331	.2335	6	.7665	.7734	172	.2266	16	4
43	0	.0735	166	.9265	.2311	6	.7689	.8424	172	.1576	15	17 00
	4	.1400	166	.8600	.2287	6	.7713	.9113	172	.0857	14	56
	8	.2064	165	.7936	.2263	6	.7737	.9801	172	.0109	13	52
	12	.2728	165	.7274	.2239	6	.7762	.380488	171	.719512	12	48
	16	.3388	165	.6619	.2211	6	.7786	.1174	171	.6326	11	44
	20	.4042	165	.5951	.2190	6	.7810	.1859	171	.5411	10	40
	24	.4709	165	.5272	.2166	6	.7834	.2542	171	.4554	9	36
	28	.5367	164	.4633	.2143	6	.7858	.3225	170	.3775	8	32
	32	.6025	164	.3975	.2118	6	.7882	.3907	170	.3003	7	28
	36	.6681	164	.3319	.2093	6	.7907	.4588	170	.2212	6	24
	40	.7337	163	.2673	.2069	6	.7931	.5268	170	.1472	5	20
	44	.7991	163	.2027	.2044	6	.7956	.5947	169	.0753	4	16
	48	.8645	163	.1355	.2020	6	.7980	.6625	169	.0033	3	12
	52	.9297	163	.0707	.1996	6	.8004	.7301	169	.2699	2	8
	56	.9948	163	.0052	.1971	6	.8029	.7977	169	.2023	1	4
43	00	.280539	162	.0719401	.9991947	6	0.009053	0.288652	169	0.711348	0	16 00

110°			1° — 15' 1" — 15' 1" — 15°						160°			12		
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.		
44	0	0.260399	163	0.719401	0.991947	6	0.008053	0.368659	166	0.711349	60	15	00	
	4	1948	163	8732	1982	6	8078	8386	166	6674	59		58	
	8	1897	163	8163	1898	6	8192	9990	166	0061	58		58	
	12	9544	163	7456	1873	6	8107	300671	166	709320	57		46	
	16	3191	161	6869	1848	6	8151	1342	166	8658	56		44	
	20	3636	161	6164	1823	6	8177	9012	167	7967	55		40	
	24	4480	161	5360	1798	6	8202	9682	167	7318	54		36	
	28	5194	161	4576	1774	6	8226	3350	167	6650	53		32	
	32	5766	160	3824	1749	6	8251	4017	167	5963	52		28	
	36	6404	160	3082	1724	6	8276	4684	167	5316	51		24	
	40	7048	160	2362	1699	6	8301	5349	166	4651	50		20	
	44	7687	160	1674	1674	6	8326	6013	166	3987	49		16	
	48	8328	159	1014	1649	6	8351	6677	166	3323	48		12	
	52	8964	159	1386	1624	6	8376	7340	165	2660	47		8	
	56	9600	159	0480	1599	6	8401	8001	165	1999	46		4	
45	0	0.290236	159	0.709764	0.991947	6	0.008053	0.368659	165	0.711349	45	15	00	
	4	0671	158	9129	1549	6	8451	8382	164	6678	44		56	
	8	1504	158	8496	1524	6	8476	9080	164	6089	43		52	
	12	2137	158	7863	1499	6	8501	300638	164	5502	42		48	
	16	2768	158	7232	1473	6	8527	1296	164	4905	41		44	
	20	3399	157	6601	1448	6	8552	1951	164	4309	40		40	
	24	4029	157	5971	1422	6	8578	2607	163	3723	39		36	
	28	4658	157	5342	1397	6	8603	3261	163	3137	38		32	
	32	5286	157	4714	1372	6	8628	3914	163	2551	37		28	
	36	5913	156	4087	1346	6	8654	4567	163	1965	36		24	
	40	6539	156	3461	1321	6	8679	5218	163	1379	35		20	
	44	7164	156	2836	1295	6	8705	5869	162	793	34		16	
	48	7788	156	2212	1269	6	8731	6519	162	3481	33		12	
	52	8412	155	1588	1244	6	8756	7168	162	2928	32		8	
	56	9034	155	0966	1218	6	8782	7816	162	2374	31		4	
46	0	0.320076	155	0.0345	1193	6	0.008053	0.368659	162	0.711349	30	15	00	
	4	31	155	699734	1167	6	8833	9199	161	6691	29		56	
	8	0685	155	9105	1141	6	8859	9754	161	6094	28		52	
	12	1514	154	8486	1115	6	8885	310399	161	5507	27		48	
	16	2132	154	7868	1090	6	8910	1042	161	4920	26		44	
	20	2749	154	7251	1064	6	8936	1685	160	4333	25		40	
	24	3365	153	6635	1038	6	8962	2327	160	3747	24		36	
	28	3979	153	6021	1012	6	8988	2967	160	3161	23		32	
	32	4593	153	5407	986	6	9014	3607	160	2575	22		28	
	36	5207	153	4792	960	6	9040	4247	159	1989	21		24	
	40	5819	152	4178	934	6	9066	4885	159	1403	20		20	
	44	6430	152	3570	908	6	9092	5522	159	817	19		16	
	48	7041	152	2959	882	7	9118	6159	159	3641	18		12	
	52	7650	152	2350	855	7	9145	6795	159	2925	17		8	
	56	8259	152	1741	829	6	9171	7430	158	2270	16		4	
47	0	0.349915	152	0.0133	0863	6	0.008053	0.368659	158	0.711349	15	15	00	
	4	0474	151	6986	0777	7	9223	8097	158	1263	14		56	
	8	1090	151	699990	0750	6	9250	9280	158	0670	13		52	
	12	1685	151	9315	0724	7	9276	9661	158	0089	12		48	
	16	2269	151	8711	6997	6	9303	300698	157	9502	11		44	
	20	2850	150	8107	6671	7	9329	1289	157	8776	10		40	
	24	3425	150	7505	6344	6	9356	1651	157	8149	9		36	
	28	3997	150	6903	6018	6	9383	2479	157	7521	8		32	
	32	4568	150	6302	5692	7	9409	3166	157	6894	7		28	
	36	5138	150	5702	5365	7	9435	3733	156	6267	6		24	
	40	5705	149	5104	5038	6	9462	4352	156	5642	5		20	
	44	5268	149	4505	4712	6	9488	4983	156	5017	4		16	
	48	4828	149	3906	4485	7	9515	5607	156	4393	3		12	
	52	4385	149	3311	4258	7	9542	6231	155	3769	2		8	
	56	3934	149	2716	4031	7	9569	6853	155	3147	1		4	
47	00	0.317879	149	0.682121	0.990404	7	0.008053	0.368659	155	0.711349	0	15	00	

TABLE II. ← LOG. SINES, TANG'S, &C.

0°		120°		1° - 15'		1° - 15'		1° - 15'		167°		11°	
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosec.	L. Cot.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
18	0 0	9.217929	148	0.002121	9.999884	6	0.000386	9.337475	153	0.673325	60	11 00	
	4 1	8473	148	1527	0378	7	0622	8093	153	1905	59		
	8 2	9066	148	0934	0351	7	0649	8715	153	2235	58		
	12 3	9658	148	0349	0324	7	0676	9334	153	0666	57	48	
	16 4	300250	147	97750	0297	7	0703	9953	154	0047	56	44	
	20 5	0840	147	9160	0270	7	0730	30570	154	669430	55	40	
	24 6	1430	147	8570	0243	7	0757	1187	154	8813	54	36	
	28 7	2019	147	7981	0216	7	0784	1803	154	8197	53	32	
	32 8	2606	147	7394	0189	7	0812	2418	154	7582	52	28	
	36 9	3194	146	6806	0161	7	0839	3033	153	6967	51	24	
	40 10	3780	146	6220	0134	7	0866	3646	153	6354	50	20	
	44 11	4366	146	5634	0107	7	0893	4259	153	5741	49	16	
	48 12	4950	146	5050	0079	7	0921	4871	153	5139	48	12	
	52 13	5534	146	4466	0052	7	0949	5482	153	4518	47	8	
	56 14	6118	145	3882	0025	7	0975	6093	153	3907	46	4	
19	0 15	6700	145	3300	999977	7	010003	6703	152	2297	45	11 0	
	4 16	7281	145	2719	9970	7	0020	7311	152	9069	44	56	
	8 17	7862	145	2138	9942	7	0058	7920	152	9006	43	52	
	12 18	8443	144	1558	9915	7	0063	8527	152	1473	42	48	
	16 19	9023	144	998	9887	7	0113	9133	151	0867	41	44	
	20 20	9599	144	0401	9860	7	0140	9739	151	0261	40	40	
	24 21	30176	144	60984	9832	7	0168	304344	151	65866	39	36	
	28 22	0753	144	9947	9804	7	0196	0949	151	9051	38	32	
	32 23	1329	144	8671	9777	7	0223	1552	151	8448	37	28	
	36 24	1904	143	8096	9749	7	0251	2155	151	7845	36	24	
	40 25	2478	143	7522	9721	7	0279	2757	150	7243	35	20	
	44 26	3051	143	6949	9693	7	0307	3358	150	6642	34	16	
	48 27	3624	143	6376	9666	7	0334	3958	150	6042	33	12	
	52 28	4195	143	5805	9637	7	0363	4558	150	5442	32	8	
	56 29	4767	142	5233	9610	7	0390	5157	150	4843	31	4	
50	0 30	5337	142	4663	9582	7	0418	5755	149	4245	30	10 0	
	4 31	5906	142	4094	9553	7	0447	6353	149	3647	29	56	
	8 32	6473	142	3525	9525	7	0475	6950	149	3050	28	52	
	12 33	7043	142	2957	9497	7	0503	7546	149	2454	27	48	
	16 34	7610	141	2390	9469	7	0531	8141	148	1859	26	44	
	20 35	8176	141	1824	9441	7	0559	8735	148	1265	25	40	
	24 36	8742	141	1258	9413	7	0587	9329	148	0671	24	36	
	28 37	9307	141	693	9385	7	0615	9922	148	0078	23	32	
	32 38	9870	141	0130	9356	7	0644	350514	148	649480	22	28	
	36 39	30434	140	659566	9328	7	0672	1108	148	6864	21	24	
	40 40	0696	140	9004	9299	7	0701	1697	147	6263	20	20	
	44 41	1268	140	8443	9271	7	0729	2287	147	5663	19	16	
	48 42	9119	140	7881	9243	7	0757	2876	147	5063	18	12	
	52 43	9679	140	7321	9214	7	0786	3465	147	4463	17	8	
	56 44	3239	139	6761	9186	7	0814	4053	147	3867	16	4	
51	0 45	3797	139	6203	9157	7	0843	4640	147	3268	15	9 0	
	4 46	4355	139	5645	9128	7	0872	5227	146	2673	14	56	
	8 47	4913	139	5087	9100	7	0900	5813	146	2078	13	52	
	12 48	5469	139	4531	9071	7	0929	6398	146	1482	12	48	
	16 49	6024	139	3976	9042	7	0958	6982	146	908	11	44	
	20 50	6580	138	3420	9014	7	0986	7566	146	2434	10	40	
	24 51	7134	138	2866	8985	7	1015	8149	145	1851	9	36	
	28 52	7687	138	2313	8956	7	1044	8731	145	1269	8	32	
	32 53	8240	138	1760	8927	7	1073	9313	145	687	7	28	
	36 54	8792	138	1206	8898	7	1102	9894	145	0106	6	24	
	40 55	9343	137	6517	8869	7	1131	360174	145	63926	5	20	
	44 56	9893	137	0107	8840	7	1160	1053	145	6047	4	16	
	48 57	30443	137	448557	8811	7	1189	1632	144	5688	3	12	
	52 58	0992	137	9006	8782	7	1218	2210	144	4329	2	8	
	56 59	1540	137	8490	8753	7	1247	2787	144	3473	1	4	
51	0 60	9.350088	137	0.007912	9.992088	7	0.011376	9.362364	144	0.636636	0	8 0	

0° 13°			1° = 15' 1" = 15' 1" = 15°						166° 11°			
Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
52	0	9.352068	137	0.647912	9.988794	7	0.011976	9.363364	144	0.636636	66	7
	4	9635	136	7365	8693	7	1305	3040	144	6080	39	56
	8	3181	136	6819	8663	7	1335	4516	143	5484	56	52
	12	3726	136	6274	8636	7	1364	5000	143	4910	57	47
	16	4271	136	5739	8607	7	1393	5664	143	4336	58	44
	20	4815	136	5185	8578	7	1422	6237	143	3763	55	40
	24	5358	136	4642	8548	7	1452	6810	143	3190	54	36
	28	5901	135	4099	8519	7	1481	7382	143	2618	53	32
	32	6449	135	3558	8489	7	1511	7953	143	2047	52	27
	36	6984	135	3016	8460	7	1540	8524	142	1476	51	24
	40	7524	135	2476	8430	7	1570	9094	142	9060	50	20
	44	8064	135	1936	8401	7	1599	9663	142	8237	49	16
	48	8603	135	1397	8371	7	1629	370233	142	680769	48	12
	52	9141	134	8599	8342	7	1658	0799	142	5901	47	8
	56	9679	134	3231	8312	7	1688	1367	141	5033	46	4
53	0	360215	134	639785	8282	7	1718	1933	141	8067	45	7
	4	0751	134	5249	8252	7	1748	2499	141	7501	44	3
	8	1387	134	4113	8222	7	1778	3065	141	6935	43	32
	12	1822	133	3178	8193	7	1807	3629	141	6371	42	28
	16	2250	133	2244	8163	7	1837	4193	141	5807	41	24
	20	2680	133	1311	8133	7	1867	4756	141	5244	40	20
	24	3122	133	6576	8103	7	1897	5319	140	4681	39	16
	28	3564	133	6046	8073	7	1927	5881	140	4119	38	12
	32	3993	133	5515	8043	7	1957	6442	140	3558	37	8
	36	4423	132	4984	8013	7	1987	7003	140	2997	36	4
	40	4854	132	4454	7983	7	2017	7563	140	2437	35	39
	44	5285	132	3925	7953	8	2047	8123	140	1878	34	16
	48	5716	132	3397	7922	7	2078	8681	139	1319	33	12
	52	6147	132	2869	7892	7	2108	9239	139	0761	32	8
	56	6578	131	2341	7862	7	2138	9797	139	0203	31	4
54	0	8185	131	1815	7832	8	2168	360254	139	619646	30	0
	4	8711	131	1289	7801	7	2199	0010	139	9090	29	56
	8	9236	131	0764	7771	7	2229	1465	139	8535	28	52
	12	9761	131	0239	7740	8	2259	2921	138	7979	27	48
	16	370885	131	639715	7710	8	2290	2575	138	7425	26	44
	20	0608	130	9192	7679	7	2321	3129	138	6871	25	40
	24	1330	130	8670	7649	8	2351	3681	138	6319	24	36
	28	1852	130	8148	7618	8	2382	4234	138	5766	23	32
	32	2374	130	7626	7588	7	2412	4786	138	5214	22	28
	36	2894	130	7106	7557	8	2443	5337	138	4663	21	24
	40	3414	130	6586	7526	8	2474	5888	137	4112	20	20
	44	3933	130	6067	7495	8	2505	6438	137	3562	19	16
	48	4452	129	5548	7465	8	2535	6987	137	3013	18	12
	52	4970	129	5030	7434	8	2566	7536	137	2464	17	8
	56	5487	129	4513	7403	8	2597	8084	137	1916	16	4
55	0	6003	129	3997	7372	8	2628	8631	137	1369	15	0
	4	6519	129	3481	7341	8	2659	9176	137	8229	14	56
	8	7035	129	2965	7310	8	2690	9725	136	2875	13	52
	12	7549	128	2451	7279	8	2721	390270	136	609730	12	48
	16	8063	128	1937	7248	8	2752	0615	136	9185	11	44
	20	8577	128	1423	7217	8	2783	1260	136	8240	10	40
	24	9090	128	0911	7186	8	2814	1803	136	7297	9	36
	28	9602	128	0396	7155	8	2845	2447	135	6353	8	32
	32	53	128	619887	7124	8	2876	3099	135	5409	7	28
	36	0684	127	5576	7093	8	2907	3651	135	4466	6	24
	40	1134	127	4960	7061	8	2939	4203	135	3527	5	20
	44	1644	127	4346	7030	8	2970	4754	135	2586	4	16
	48	2152	127	3732	6998	8	3002	5304	135	1646	3	12
	52	2661	127	3119	6967	8	3033	5854	135	701	2	8
	56	3168	127	2505	6935	8	3065	6403	134	3767	1	4
55	0	9.393075	127	0.616325	9.996904	8	0.013096	9.396771	144	0.603889	66	0

TABLE II.—LOG. SINES, TANG'S, &c.

140		1' - 15' 1" - 15' 1" - 15"						165° - 11'				
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
56	0	9.383675	127	0.616325	9.986004	8	0.013096	9.396771	134	0.603229	60	3
	1	418.2	126	5818	6873	8	3127	7309	134	2939	59	56
	2	484.7	126	5313	6841	8	3159	7846	134	2154	58	52
	3	519.2	126	4808	6809	8	3191	8383	134	1617	57	48
	4	569.7	126	4303	6778	8	3223	8919	134	1081	56	44
	5	620.1	126	3799	6746	8	3254	9453	134	6545	55	40
	6	670.4	126	3296	6714	8	3286	9990	133	6010	54	36
	7	720.7	125	2793	6683	8	3317	10524	133	59476	53	32
	8	770.9	125	2291	6651	8	3349	1058	133	8942	52	28
	9	821.0	125	1790	6619	8	3381	1501	133	8409	51	24
	10	871.1	125	1289	6587	8	3413	2124	133	7876	50	20
	11	921.1	125	789	6555	8	3445	2656	133	7344	49	16
	12	971.0	125	290	6523	8	3477	3187	133	6813	48	12
	13	390309	125	60791	6491	8	3509	3718	133	6282	47	8
	14	0708	124	9292	6459	8	3541	4249	132	5751	46	4
57	0	15	1203	124	8794	8	3573	4779	132	5221	45	3
	1	1703	124	8297	8305	8	3605	5308	132	4692	44	56
	2	1909	124	7801	7833	8	3637	5836	132	4164	43	52
	3	2119	124	7305	7363	8	3669	6364	132	3636	42	48
	4	2331	123	6809	6899	8	3701	6892	132	3108	41	44
	5	2545	123	6315	6386	8	3734	7419	131	2581	40	40
	6	2761	123	5821	6324	8	3766	7945	131	2055	39	36
	7	2978	123	5327	6262	8	3798	8471	131	1529	38	32
	8	3196	123	4833	6199	8	3831	8997	131	1003	37	28
	9	3415	123	4339	6137	8	3863	9521	131	6479	36	24
	10	3635	123	3845	6075	8	3895	10045	131	59955	35	20
	11	3856	123	3351	6012	8	3928	10569	131	9431	34	16
	12	4077	123	2857	5949	8	3961	1092	131	8008	33	12
	13	4299	122	2363	5887	8	3993	1615	130	6585	32	8
	14	4521	122	1869	5824	8	4026	2137	130	5163	31	4
58	0	30	8606	122	1400	8	4058	2658	130	3742	30	0
	1	31	9088	122	9912	8	4091	3179	130	6639	29	56
	2	32	9575	122	6025	8	4124	3699	130	6301	28	52
	3	400692	122	599036	5943	8	4157	4219	130	5781	27	48
	4	0549	121	9451	5811	8	4189	4738	130	5262	26	44
	5	1035	121	8965	5778	8	4222	5257	129	4743	25	40
	6	1520	121	8480	5745	8	4255	5775	129	4225	24	36
	7	2005	121	7995	5712	8	4288	6292	129	3707	23	32
	8	2489	121	7511	5679	8	4321	6810	129	3190	22	28
	9	2972	121	7028	5646	8	4354	7329	129	2674	21	24
	10	3455	121	6545	5613	8	4387	7842	129	2158	20	20
	11	3938	120	6062	5580	8	4420	8358	129	1642	19	16
	12	4420	120	5580	5547	8	4453	8873	128	1127	18	12
	13	4901	120	5099	5514	8	4486	9387	128	6613	17	8
	14	5381	120	4619	5480	8	4520	9901	128	6099	16	4
59	0	45	5862	120	4138	8	4553	10415	128	579585	15	1
	1	46	6341	120	3659	8	4586	0927	128	9073	14	56
	2	47	6820	120	3180	8	4620	1440	128	8560	13	52
	3	48	7299	119	2701	8	4653	1952	128	8048	12	48
	4	7777	119	2223	5314	8	4686	2463	128	7537	11	44
	5	8254	119	1746	5280	8	4720	2974	127	7026	10	40
	6	8731	119	1269	5247	8	4753	3484	127	6516	9	36
	7	9207	119	793	5213	8	4787	3994	127	6006	8	32
	8	9682	119	318	5180	8	4820	4503	127	5496	7	28
	9	10157	119	58943	5146	8	4854	5011	127	4989	6	24
	10	0632	118	9368	5113	8	4887	5519	127	4481	5	20
	11	1106	118	8844	5079	8	4921	6027	127	3973	4	16
	12	1579	118	8321	5045	8	4955	6534	127	3466	3	12
	13	2052	118	7798	5011	8	4989	7041	126	2959	2	8
	14	2525	118	7275	4978	8	5022	7547	126	2453	1	4
59	0	30	9.412906	0.587004	9.984944	8	0.015036	9.428652	126	0.571948	0	0

140

1' - 15' 1" - 15' 1" - 15"

165° - 11'

TABLE II.—LOG. SINES, TANG'S, &c.

1° 10°

1° - 15' 1° - 15'

163° 10°

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.		
m	s											m	s	
4	0	0	9.440338	110	0.550662	9.982842	9	0.017158	9.457496	110	0.542504	60	53	60
	4	1	0778	110	9922	2405	9	7195	7973	110	2027	59		56
	8	2	1218	110	8782	2769	9	7231	8449	110	1551	58		52
	12	3	1658	110	8342	2733	9	7207	8925	110	1075	57		48
	16	4	2096	110	7904	2696	9	7304	9400	110	0900	56		44
		5	2535	109	7465	2660	9	7349	9875	110	0125	55		40
	24	6	2973	109	7027	2624	9	7376	10349	110	53051	54		36
	28	7	3410	109	6590	2587	9	7413	10823	110	9177	53		32
	32	8	3847	109	6153	2550	9	7450	11297	110	8709	52		28
	36	9	4284	109	5716	2514	9	7486	11770	110	8230	51		24
	40	10	4720	109	5280	2477	9	7523	12243	110	7757	50		20
	44	11	5155	109	4845	2441	9	7559	12714	110	7286	49		16
	48	12	5540	109	4410	2404	9	7596	13186	110	6814	48		12
	52	13	6025	108	3975	2367	9	7633	13658	110	6342	47		8
	56	14	6459	108	3541	2331	9	7669	14128	110	5872	46		4
5	0	15	6893	108	3107	2294	9	7706	14599	117	5401	45	55	0
	4	16	7326	108	2674	2257	9	7743	15069	117	4931	44		56
	8	17	7759	108	2241	2220	9	7780	15539	117	4461	43		52
	12	18	8191	108	1809	2183	9	7817	16009	117	3992	42		48
	16	19	8623	108	1377	2146	9	7854	16477	117	3523	41		44
	20	20	9054	108	946	2109	9	7891	16945	117	3055	40		40
	24	21	9485	107	515	2072	9	7928	17413	117	2587	39		36
	28	22	9915	107	085	2035	9	7965	17880	117	2120	38		32
	32	23	10345	107	54955	1998	9	8002	18347	117	1653	37		28
	36	24	0775	107	9225	1961	9	8039	18814	116	1186	36		24
	40	25	1204	107	8796	1924	9	8076	19280	116	0720	35		20
	44	26	1632	107	8368	1889	9	8114	19746	116	0254	34		16
	48	27	2060	107	7940	1849	9	8151	20211	116	52978	33		12
	52	28	2488	107	7512	1812	9	8188	20676	116	9324	32		8
	56	29	2915	107	7085	1774	9	8225	11141	116	8859	31		4
6	0	30	3342	106	6658	1737	9	8263	11605	116	8395	30	54	0
	4	31	3768	106	6232	1699	9	8301	2009	116	7929	29		56
	8	32	4194	106	5806	1662	9	8338	2532	116	7462	28		52
	12	33	4619	106	5381	1624	9	8376	2995	115	7005	27		48
	16	34	5044	106	4956	1587	9	8413	3457	115	6543	26		44
	20	35	5469	106	4531	1550	9	8450	3919	115	6081	25		40
	24	36	5893	106	4107	1512	9	8488	4381	115	5619	24		36
	28	37	6316	106	3684	1474	9	8526	4842	115	5158	23		32
	32	38	6739	106	3261	1436	9	8564	5303	115	4697	22		28
	36	39	7162	105	2838	1399	9	8601	5763	115	4237	21		24
	40	40	7584	105	2416	1361	9	8639	6223	115	3777	20		20
	44	41	8006	105	1994	1323	9	8677	6683	115	3317	19		16
	48	42	8427	105	1573	1285	9	8715	7142	115	2858	18		12
	52	43	8848	105	1152	1247	9	8753	7601	114	2399	17		8
	56	44	9268	105	0732	1209	9	8791	8059	114	1941	16		4
7	0	45	9688	105	0312	1171	9	8829	8517	114	1483	15	53	0
	4	46	10108	105	53862	1133	9	8867	8975	114	1025	14		56
	8	47	0527	105	9473	1095	9	8905	9432	114	0568	13		52
	12	48	0946	104	9054	1057	9	8943	9889	114	0111	12		48
	16	49	1364	104	8636	1019	9	8981	10345	114	519655	11		44
	20	50	1782	104	8218	0981	9	9019	10801	114	0199	10		40
	24	51	2199	104	7801	0942	10	9058	11257	114	8743	9		36
	28	52	2616	104	7384	0904	9	9096	11712	114	8288	8		32
	32	53	3032	104	6968	0866	10	9134	12166	114	7834	7		28
	36	54	3448	104	6552	0827	9	9173	12621	114	7379	6		24
	40	55	3864	104	6136	0789	9	9211	13075	113	6925	5		20
	44	55	4279	104	5721	0751	10	9249	13529	113	6471	4		16
	48	57	4694	103	5306	0712	9	9288	13982	113	6018	3		12
	52	58	5108	103	4892	0674	10	9326	14434	113	5566	2		8
	56	59	5522	103	4478	0635	10	9365	14887	113	5113	1		4
7	0	60	9.165935	103	0.534065	9.980596	10	0.019404	9.485339	113	0.514661	0	52	0

7° 100°

1° - 4' 10° - 4°

73° 4°

TABLE II.—LOG. SINES, TANG'S, &c.

1°		17°		1° - 15' 1° - 15' 1° - 15°		163°		16°				
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosoc.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
8	0	9.465935	103	0.534065	9.980536	9	0.019404	9.465339	113	0.514061	69	51 00
	1	6348	103	3652	0558	10	0442	5701	113	4804	69	50
	2	6761	103	3239	0519	10	0481	6942	113	3750	69	52
	3	7173	103	2827	0480	9	0520	6843	113	3307	69	54
	4	7585	103	2415	0442	10	0559	7143	113	2857	69	56
	5	7990	103	2004	0403	10	0607	7503	113	2407	69	58
	6	8407	102	1593	0364	10	0636	8043	112	1957	69	59
	7	8817	102	1183	0325	10	0675	8493	112	1508	69	59
	8	9227	102	0773	0286	10	0714	8941	112	1059	69	59
	9	9637	102	0363	0247	10	0753	9390	112	0610	69	59
	10	470046	102	520054	0208	10	0792	9838	112	0162	69	59
	11	0455	102	9545	0169	10	0831	490236	112	509714	69	59
	12	0863	102	9137	0130	10	0870	0733	112	9667	69	59
	13	1271	102	8729	0091	10	0909	1180	112	9200	69	59
	14	1679	102	8321	0053	10	0948	1627	111	8773	69	59
9	0	9065	102	7915	0012	10	0988	2073	111	7927	45	51 00
	1	9492	102	7508	979973	10	020097	2519	111	7481	45	50
	2	9909	101	7101	9034	10	0066	2965	111	7035	45	50
	3	3304	101	6696	9694	10	0108	3410	111	6590	45	50
	4	3719	101	6290	9655	10	0145	3855	111	6145	45	50
	5	4115	101	5885	9616	10	0184	4300	111	5701	45	50
	6	4519	101	5481	9578	10	0221	4743	111	5257	45	50
	7	4923	101	5077	9537	10	0263	5186	111	4814	45	50
	8	5327	101	4673	9497	10	0303	5630	111	4370	45	50
	9	5731	101	4269	9458	10	0342	6073	110	3927	45	50
	10	6133	101	3867	9418	10	0382	6515	110	3483	45	50
	11	6536	100	3464	9379	10	0421	6957	110	3043	45	50
	12	6939	100	3062	9339	10	0461	7399	110	2601	45	50
	13	7340	100	2660	9299	10	0501	7841	110	2159	45	50
	14	7741	100	2259	9259	10	0541	8282	110	1718	45	50
10	0	8142	100	1858	9220	10	0580	8723	110	1278	30	49 00
	1	8542	100	1458	9180	10	0620	9163	110	0838	30	49
	2	8943	100	1058	9140	10	0660	9603	110	0398	30	49
	3	9343	100	658	9100	10	0700	500042	110	49028	27	49
	4	9741	100	0259	9060	10	0740	0481	110	9519	27	49
	5	490140	100	519000	9020	10	0780	0920	110	9080	25	49
	6	0639	99	9461	9180	10	0820	1354	109	8641	25	49
	7	0937	99	9063	9140	10	0860	1797	109	8203	25	49
	8	1334	99	8666	9099	10	0901	2235	109	7765	25	49
	9	1731	99	8269	9059	10	0941	2672	109	7328	25	49
	10	2128	99	7872	9019	10	0981	3109	109	6891	25	49
	11	2525	99	7475	8979	10	1021	3546	109	6454	25	49
	12	2921	99	7079	8939	10	1061	3982	109	6017	25	49
	13	3316	99	6684	8898	10	1102	4418	109	5582	25	49
	14	3712	99	6288	8858	10	1142	4854	109	5146	25	49
11	0	4107	98	5893	8818	10	1182	5289	109	4711	15	49 00
	1	4501	98	5499	8777	10	1223	5724	107	4276	14	49
	2	4895	98	5105	8736	10	1264	6159	108	3841	13	49
	3	5289	98	4711	8695	10	1304	6597	108	3407	12	49
	4	5682	98	4318	8655	10	1345	7027	108	2973	11	49
	5	6075	98	3925	8615	10	1385	7460	108	2540	10	49
	6	6467	98	3533	8574	10	1426	7893	108	2107	9	49
	7	6859	98	3141	8533	10	1467	8326	108	1674	8	49
	8	7251	98	2749	8493	10	1507	8758	108	1242	7	49
	9	7643	98	2357	8452	10	1548	9191	108	809	6	49
	10	8033	98	1967	8411	10	1589	9623	108	378	5	49
	11	8424	97	1578	8370	10	1630	510654	108	469046	4	49
	12	8814	97	1189	8329	10	1671	0485	108	9515	3	49
	13	9204	97	0799	8288	10	1712	6016	108	5044	2	49
	14	9593	97	0407	8247	10	1753	1346	107	2854	1	49
	15	9982	97	0017	8206	10	0091794	9.511776	107	0.468284	0	49 00

TABLE II.—LOG. SINES, TANG'S, & C

1° 18'			1° — 15' 1" — 15'						161° 10'				
Hours.	Deg.	L. Sin.	Diff. for 15" or 1'	L. Cossec.	L. Cos.	Diff. for 15" or 1'	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours.	
12	0	9.489069	97	0.510018	0.978906	10	0.021794	9.511776	107	0.488294	60	47	60
	1	490371	97	509639	8165	10	1835	9206	107	7794	59		59
	2	0739	97	9241	8124	10	1876	9265	107	7365	58		58
	3	1147	97	8853	8083	10	1917	9304	107	6936	57		57
	4	1535	97	8465	8043	10	1958	9343	107	6507	56		56
	5	1923	97	8078	8001	10	1999	9381	107	6079	55		55
	6	2308	97	7692	7959	10	2041	9420	107	5651	54		54
	7	2685	96	7305	7918	10	2082	9457	107	5223	53		53
	8	3061	96	6919	7877	10	2123	9494	107	4796	52		52
	9	3436	96	6534	7835	10	2165	9531	107	4369	51		51
	10	3811	96	6149	7794	10	2206	9567	107	3943	50		50
	11	4186	96	5764	7753	10	2248	9604	106	3516	49		49
	12	4561	96	5379	7711	10	2289	9640	106	3090	48		48
	13	4936	96	4994	7669	10	2331	9675	106	2665	47		47
	14	5311	96	4612	7628	10	2372	9710	106	2240	46		46
13	0	5779	96	4228	7586	10	2414	9746	106	1814	45	47	0
	1	6154	96	3846	7544	10	2456	9781	106	1390	44		56
	2	6527	95	3463	7503	10	2497	9816	106	966	43		55
	3	6899	95	3081	7461	10	2539	9851	106	542	42		48
	4	7271	95	2699	7419	10	2581	9886	106	118	41		44
	5	7643	95	2318	7377	10	2623	9921	106	479	40		40
	6	8015	95	1937	7335	10	2665	9956	106	972	39		36
	7	8387	95	1556	7293	10	2707	10000	105	884	38		38
	8	8759	95	1175	7252	10	2748	10044	105	847	37		38
	9	9131	95	0795	7210	11	2790	10088	105	805	36		28
	10	9503	95	0416	7167	10	2833	10132	105	758	35		30
	11	9875	95	0037	7125	10	2875	10176	105	712	34		16
	12	10247	95	49658	7083	10	2917	10220	105	671	33		12
	13	10619	94	9979	7041	10	2959	10264	105	630	32		8
	14	10991	94	9991	6999	10	3001	10308	105	590	31		4
14	0	1477	94	8523	6957	11	3043	10352	105	548	30	46	0
	1	1854	94	8146	6914	11	3086	10396	105	506	29		56
	2	2231	94	7769	6872	10	3128	10440	105	464	28		52
	3	2608	94	7392	6830	10	3170	10484	105	422	27		48
	4	2984	94	7016	6787	10	3213	10528	104	380	26		44
	5	3361	94	6640	6745	11	3255	10572	104	338	25		40
	6	3737	94	6265	6702	11	3298	10616	104	297	24		36
	7	4111	94	5890	6660	10	3340	10660	104	256	23		32
	8	4485	94	5515	6617	11	3383	10704	104	215	22		28
	9	4860	93	5140	6575	11	3425	10748	104	175	21		24
	10	5234	93	4766	6532	11	3468	10792	104	136	20		20
	11	5608	93	4392	6489	11	3511	10836	104	97	19		16
	12	5981	93	4019	6446	10	3554	10880	104	65	18		12
	13	6354	93	3646	6404	10	3596	10924	104	30	17		8
	14	6727	93	3273	6361	11	3639	10968	104	4	16		4
15	0	7099	93	2901	6319	11	3682	11012	104	92	15	45	0
	1	7471	93	2529	6275	11	3725	11056	104	84	14		56
	2	7843	93	2157	6232	11	3768	11100	103	86	13		52
	3	8214	93	1786	6189	11	3811	11144	103	87	12		48
	4	8585	93	1415	6146	11	3854	11188	103	88	11		44
	5	8956	92	1044	6103	11	3897	11232	103	89	10		40
	6	9327	92	0674	6060	11	3940	11276	103	90	9		36
	7	9698	92	0304	6017	11	3983	11320	103	91	8		32
	8	10069	92	48925	5974	11	4026	11364	103	92	7		28
	9	10439	92	9566	5930	11	4070	11408	103	93	6		24
	10	10809	92	9197	5887	11	4113	11452	103	94	5		20
	11	11179	92	8828	5844	11	4156	11496	103	95	4		16
	12	11549	92	8460	5801	11	4199	11540	103	96	3		12
	13	11919	92	8092	5757	11	4243	11584	103	97	2		8
	14	12289	92	7725	5714	11	4286	11628	103	98	1		4
15	0	12659	92	0.487339	0.973970		0.024330	9.530979		0.483028	0	44	0

1° 18'

1° — 15' 1" — 15'

161° 10'

TABLE II.—LOG. SINES, TANG'S, &c.

180°		1° — 15' 1° — 15' 1° — 15'				160°		10°			
Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
0	9.513648	99	0.487358	9.973670	11	0.024330	9.536972	102	0.463098	60	43 00
1	3009	91	6991	5627	11	4373	7322	102	9618	59	58
2	3375	91	6625	5533	11	4417	7792	102	2908	58	52
3	3741	91	6259	5539	11	4461	8262	102	1798	57	46
4	4107	91	5893	5496	11	4504	8611	102	1269	56	44
5	4473	91	5528	5452	11	4548	9090	102	0980	55	40
6	4837	91	5163	5408	11	4592	9429	102	0571	54	36
7	5203	91	4798	5365	11	4635	9637	102	0163	53	32
8	5566	91	4434	5321	11	4679	540945	102	459755	52	28
9	5930	91	4070	5277	11	4723	0653	102	9347	51	24
10	6294	91	3706	5233	11	4767	1061	102	8939	50	20
11	6657	91	3343	5189	11	4811	1468	102	8532	49	16
12	7020	91	2980	5145	11	4855	1875	102	8125	48	12
13	7383	91	2618	5101	11	4899	2281	102	7719	47	8
14	7745	90	2255	5057	11	4943	2688	101	7312	46	4
15	8107	90	1893	5013	11	4987	3094	101	6906	45	43 0
16	8468	90	1532	4969	11	5031	3490	101	6501	44	56
17	8830	90	1170	4925	11	5075	3905	101	6095	43	52
18	9190	90	0810	4880	11	5119	4310	101	5690	42	48
19	9551	90	0449	4836	11	5164	4715	101	5285	41	44
20	9911	90	0089	4792	11	5208	5119	101	4881	40	40
21	590271	90	479799	4747	11	5253	5524	101	4478	39	36
22	0631	90	0380	4703	11	5297	5928	101	4073	38	32
23	0990	90	0010	4659	11	5341	6331	101	3669	37	28
24	1349	90	0651	4614	11	5386	6735	101	3265	36	24
25	1708	89	8992	4570	11	5430	7138	101	2862	35	20
26	2066	89	7934	4525	11	5475	7541	100	2459	34	16
27	2424	89	7576	4481	11	5519	7943	100	2057	33	12
28	2781	89	7219	4436	11	5564	8345	100	1655	32	8
29	3138	89	6862	4391	11	5609	8747	100	1253	31	4
30	3495	89	6505	4346	11	5654	9149	100	0851	30	43 0
31	3852	89	6148	4302	11	5698	9550	100	0450	29	39
32	4208	89	5792	4257	11	5743	9951	100	0049	28	35
33	4564	89	5436	4213	11	5788	580322	100	440449	27	48
34	4919	89	5081	4167	11	5833	0722	100	9948	26	44
35	5275	89	4725	4123	11	5878	1123	100	8947	25	40
36	5630	89	4370	4077	11	5923	1523	100	8447	24	36
37	5984	89	4016	4032	11	5968	1922	100	8048	23	32
38	6339	88	3661	3987	11	6013	2321	100	7648	22	28
39	6693	88	3307	3942	11	6058	2721	100	7249	21	24
40	7046	88	2954	3897	11	6103	3149	100	6851	20	20
41	7400	88	2600	3852	11	6148	3548	99	6452	19	16
42	7753	88	2247	3807	11	6193	3946	99	6054	18	12
43	8105	88	1895	3761	11	6238	4344	99	5656	17	8
44	8458	88	1542	3716	11	6284	4742	99	5258	16	4
45	8810	88	1190	3671	11	6329	5139	99	4861	15	43 0
46	9161	88	0839	3625	11	6375	5536	99	4464	14	38
47	9513	88	0487	3580	11	6420	5933	99	4067	13	34
48	9864	88	0136	3535	11	6465	6329	99	3671	12	41
49	530215	88	469785	3489	11	6511	6726	99	3274	11	44
50	0685	87	9435	3444	11	6556	7121	99	2879	10	40
51	0915	87	9065	3398	11	6602	7517	99	2483	9	36
52	1265	87	8735	3353	11	6648	7913	99	2087	8	32
53	1615	87	8365	3307	11	6693	8308	99	1692	7	28
54	1964	87	8006	3261	11	6739	8703	99	1297	6	24
55	2313	87	7656	3215	11	6785	9097	99	8903	5	20
56	2661	87	7309	3169	11	6831	9492	98	8508	4	16
57	3009	87	6961	3124	11	6878	9885	98	8115	3	12
58	3357	87	6613	3078	11	6924	560979	98	439731	2	8
59	3705	87	6265	3032	11	6969	0673	98	9287	1	4
60	9.534022	87	0.463946	9.973922	11	0.027014	9.561626	98	0.438224	0	40 0

100°

1° — 4° 10° — 4°

90°

4°

14 200		P = 15' 1" - 15' 12" P = 150										150° 10'	
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosc.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
00	0	9.534072	87	0.465048	9.972986	11	0.027014	9.561066	98	0.438934	60	00	
4	1	4309	87	5601	2940	11	7060	1459	98	8541	59	36	
8	2	4745	87	5255	2894	11	7106	1851	98	8149	58	52	
12	3	5092	87	4908	2848	11	7152	2244	98	7756	57	48	
16	4	5438	86	4562	2802	12	7198	2636	98	7364	56	44	
20	5	5783	86	4217	2755	11	7245	3028	98	6972	55	40	
24	6	6128	86	3872	2709	11	7291	3419	98	6.581	54	36	
28	7	6474	86	3526	2663	11	7337	3811	98	6.180	53	32	
32	8	6819	86	3181	2617	11	7383	4202	98	5.798	52	28	
36	9	7163	86	2837	2570	11	7430	4593	97	5407	51	24	
40	10	7507	86	2493	2524	11	7476	4983	97	5017	50	20	
44	11	7851	86	2149	2478	11	7522	5373	97	4627	49	16	
48	12	8194	86	1806	2431	12	7569	5763	97	4237	48	12	
52	13	8538	86	1462	2385	11	7615	6153	97	3847	47	8	
56	14	8880	86	1120	2338	12	7662	6542	97	3457	46	4	
00	15	9223	85	777	2291	11	7709	6932	97	3068	45	39	
4	16	9565	85	0435	2245	12	7755	7320	97	2680	44	56	
8	17	9907	85	0093	2198	12	7802	7709	97	2291	43	52	
12	18	540319	85	459731	2151	11	7849	8098	97	1902	42	48	
16	19	0390	85	9410	2105	12	7895	8485	97	1515	41	44	
20	20	0921	85	9069	2058	12	7942	8873	97	1127	40	40	
24	21	1472	85	8728	2011	12	7988	9261	97	0739	39	36	
28	22	1673	85	8387	1964	12	8035	9649	97	0351	38	32	
32	23	1953	85	8047	1917	12	8082	570036	97	420964	37	28	
36	24	2292	85	7708	1870	12	8130	0429	97	9578	36	24	
40	25	2632	85	7368	1823	12	8177	0809	96	9191	35	20	
44	26	2971	85	7029	1776	12	8224	1195	96	8805	34	16	
48	27	3310	85	6690	1729	12	8271	1581	96	8419	33	12	
52	28	3649	85	6351	1682	12	8318	1967	96	8033	32	8	
56	29	3987	84	6013	1635	12	8365	2352	96	7648	31	4	
00	30	4325	84	5675	1587	12	8413	2738	96	7262	30	38	
4	31	4663	84	5337	1540	12	8460	3123	96	6877	29	56	
8	32	5000	84	5000	1493	12	8507	3507	96	6493	28	52	
12	33	5338	84	4662	1446	12	8554	3892	96	6108	27	48	
16	34	5674	84	4326	1398	12	8602	4276	96	5724	26	44	
20	35	6011	84	3989	1351	12	8649	4660	96	5340	25	40	
24	36	6347	84	3653	1303	12	8697	5044	96	4956	24	36	
28	37	6683	84	3317	1256	12	8744	5427	96	4573	23	32	
32	38	7019	84	2981	1209	12	8791	5810	96	4190	22	28	
36	39	7354	84	2646	1161	12	8838	6193	96	3807	21	24	
40	40	7689	84	2311	1113	12	8887	6576	96	3424	20	20	
44	41	8024	84	1976	1066	12	8934	6958	96	3042	19	16	
48	42	8359	84	1641	1018	12	8982	7341	95	2659	18	12	
52	43	8693	83	1307	970	12	9030	7723	95	2277	17	8	
56	44	9028	83	0974	922	12	9078	8104	95	1896	16	4	
00	45	9360	83	0640	874	12	9126	8486	95	1514	15	37	
4	46	9694	83	0306	827	12	9173	8867	95	1133	14	56	
8	47	530927	83	440972	779	12	9221	9248	95	0752	13	52	
12	48	0357	83	0641	731	12	9269	9629	95	0372	12	48	
16	49	0692	83	0308	683	12	9317	580000	95	419991	11	44	
20	50	1024	83	8976	635	12	9365	0389	95	9611	10	40	
24	51	1356	83	8644	587	12	9413	0769	95	9231	9	36	
28	52	1687	83	8313	538	12	9462	1149	95	8851	8	32	
32	53	2018	83	7982	490	12	9510	1529	95	8472	7	28	
36	54	2349	83	7651	442	12	9558	1907	95	8093	6	24	
40	55	2680	83	7320	394	12	9606	2286	95	7714	5	20	
44	56	3010	83	6990	345	12	9655	2665	95	7335	4	16	
48	57	3341	82	6659	297	12	9703	3044	94	6956	3	12	
52	58	3671	82	6329	249	12	9751	3422	94	6578	2	8	
56	59	4000	82	6000	200	12	9800	3800	94	6200	1	4	
00	60	9.534322	82	0.443671	9.970152	12	0.029848	9.564177	94	0.418223	0	36	

Hours	Deg.	L. Sin.	Diff. for 15" or 1'	L. Cossec.	L. Cos.	Diff. for 15" or 1'	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours	
m	s											m	s
24	0	0	82	0.445671	0.970152	12	0.029848	9.584177	94	0.415823	60	35	00
	4	1	82	.5342	.0103	12	.9897	.4555	94	.5445	59		56
	8	2	82	.5013	.0055	12	.9945	.4932	94	.5608	58		52
	12	3	82	.4685	.0006	12	.9994	.5309	94	.4691	57		48
	16	4	82	.4357	.969957	12	.030043	.5686	94	.4314	56		44
	20	5	82	.4029	.9909	12	.0091	.6062	94	.3938	55		40
	24	6	82	.3701	.9860	12	.0140	.6439	94	.3561	54		36
	28	7	82	.3374	.9811	12	.0189	.6815	94	.3185	53		32
	32	8	82	.3047	.9763	12	.0237	.7190	94	.2810	52		28
	36	9	81	.2720	.9714	12	.0286	.7566	94	.2434	51		24
	40	10	81	.2394	.9665	12	.0335	.7941	94	.2059	50		20
	44	11	81	.2068	.9616	12	.0384	.8316	94	.1684	49		16
	48	12	81	.1742	.9567	12	.0433	.8691	94	.1309	48		12
	52	13	81	.1416	.9518	12	.0482	.9066	93	.0934	47		8
	56	14	81	.1091	.9469	12	.0531	.9440	93	.0560	46		4
25	0	15	81	.0766	.9420	12	.0580	.9814	93	.0186	45	35	0
	4	16	81	.0442	.9370	12	.0630	.500188	93	.40812	44		56
	8	17	81	.0117	.9321	12	.0679	.5382	93	.9438	43		52
	12	18	81	.560207	.439703	12	.0728	.5762	93	.9065	42		48
	16	19	81	.531	.9409	12	.0777	.6138	93	.8692	41		44
	20	20	81	.0854	.9146	12	.0827	.6514	93	.8319	40		40
	24	21	81	.1178	.8822	12	.0876	.6891	93	.7946	39		36
	28	22	81	.1501	.8499	12	.0925	.7266	93	.7574	38		32
	32	23	81	.1824	.8176	12	.0975	.7642	93	.7201	37		28
	36	24	80	.2146	.7854	12	.1024	.8017	93	.6828	36		24
	40	25	80	.2468	.7532	12	.1074	.8392	93	.6453	35		20
	44	26	80	.2790	.7210	12	.1124	.8767	93	.6078	34		16
	48	27	80	.3112	.6888	12	.1173	.9142	93	.5703	33		12
	52	28	80	.3433	.6567	12	.1223	.9517	93	.5328	32		8
	56	29	80	.3755	.6245	12	.1272	.9892	93	.4953	31		4
26	0	30	80	.4075	.5925	12	.1322	.5397	93	.4603	30	34	0
	4	31	80	.4396	.5604	12	.1372	.5768	92	.4232	29		56
	8	32	80	.4716	.5284	12	.1422	.6139	92	.3862	28		52
	12	33	80	.5036	.4964	12	.1472	.6508	92	.3492	27		48
	16	34	80	.5356	.4644	12	.1522	.6878	92	.3122	26		44
	20	35	80	.5676	.4324	12	.1571	.7247	92	.2753	25		40
	24	36	80	.5995	.4005	12	.1621	.7616	92	.2384	24		36
	28	37	80	.6314	.3686	12	.1671	.7985	92	.2015	23		32
	32	38	80	.6632	.3368	13	.1722	.8354	92	.1646	22		28
	36	39	80	.6951	.3049	12	.1772	.8723	92	.1277	21		24
	40	40	79	.7269	.2731	12	.1822	.9091	92	.0909	20		20
	44	41	79	.7587	.2413	12	.1872	.9459	92	.0541	19		16
	48	42	79	.7905	.2095	12	.1922	.9827	92	.0173	18		12
	52	43	79	.8222	.1778	12	.1972	.600194	92	.39806	17		8
	56	44	79	.8539	.1461	12	.2023	.5362	92	.9438	16		4
27	0	45	79	.8856	.1144	12	.2073	.0929	92	.9071	15	33	0
	4	46	79	.9172	.0828	13	.2124	.1296	92	.8704	14		56
	8	47	79	.9488	.0512	12	.2174	.1662	92	.8338	13		52
	12	48	79	.9804	.0196	13	.2225	.2029	92	.7971	12		48
	16	49	79	.570120	.429880	13	.2275	.2395	91	.7605	11		44
	20	50	79	.0435	.9565	12	.2326	.2761	91	.7239	10		40
	24	51	79	.0751	.9249	12	.2376	.3127	91	.6873	9		36
	28	52	79	.1066	.8934	13	.2427	.3493	91	.6507	8		32
	32	53	79	.1380	.8620	13	.2478	.3858	91	.6142	7		28
	36	54	79	.1694	.8306	12	.2529	.4223	91	.5777	6		24
	40	55	78	.2009	.7991	13	.2579	.4588	91	.5412	5		20
	44	56	78	.2323	.7677	13	.2630	.4953	91	.5047	4		16
	48	57	78	.2636	.7364	13	.2681	.5317	91	.4683	3		12
	52	58	78	.2950	.7050	13	.2732	.5682	91	.4318	2		8
	56	59	78	.3263	.6737	13	.2783	.6046	91	.3954	1		4
27	60	60	78	.9573576	0.426424	13	0.032834	9.606410	91	0.393590	0	32	0

TABLE II.—LOG. SINES, TANG'S, &C.

1°		22°	1° = 15' 1" = 15' 1" = 15°				187°	10°					
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosc.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
28	0	0.5737376	78	0.428424	9.967166	13	0.032834	9.604410	91	0.393590	60	31	60
	1	3 488	78	6112	7115	13	2885	6773	91	3227	59		56
	2	4200	76	5809	7084	13	2936	7136	91	2864	58		52
	3	4512	76	5488	7012	13	2988	7500	91	2500	57		48
	4	4824	78	5176	6961	13	3039	7863	91	2137	56		44
	5	5135	78	4865	6910	13	3090	8225	91	1775	55		40
	6	5447	78	4553	6859	13	3141	8588	90	1412	54		36
	7	5758	78	4242	6808	13	3192	8950	90	1050	53		32
	8	6038	78	3932	6756	13	3244	9312	90	688	52		28
	9	6379	77	3621	6705	13	3295	9674	90	326	51		24
	10	6689	77	3311	6653	13	3347	610039	90	389964	50		20
	11	6999	77	3001	6602	13	3398	0397	90	9603	49		16
	12	7309	77	2691	6550	13	3450	0759	90	9241	48		12
	13	7618	77	2382	6499	13	3501	1119	90	8881	47		8
	14	7927	77	2073	6447	13	3553	1480	90	8520	46		4
29	0	8236	77	1764	6395	13	3605	1841	90	8159	45	31	0
	1	8545	77	1455	6344	13	3656	2201	90	7799	44		56
	2	8854	77	1146	6292	13	3708	2562	90	7438	43		52
	3	9162	77	838	6240	13	3760	2922	90	7078	42		48
	4	9469	77	531	6188	13	3812	3281	90	6719	41		44
	5	9777	77	223	6136	13	3864	3641	90	6359	40		40
	6	580085	77	19915	6085	13	3915	4000	90	6000	39		36
	7	0392	77	9068	6033	13	3967	4359	90	5641	38		32
	8	0999	76	9301	5981	13	4019	4718	90	5282	37		28
	9	1005	76	8995	5928	13	4072	5077	89	4923	36		24
	10	1311	76	8689	5876	13	4124	5435	90	4565	35		20
	11	1618	76	8382	5824	13	4176	5794	90	4206	34		16
	12	1924	76	8076	5772	13	4228	6152	89	3848	33		12
	13	2229	76	7771	5720	13	4280	6509	89	3491	32		8
	14	2535	76	7465	5668	13	4332	6867	89	3133	31		4
30	0	2840	76	7160	5616	13	4384	7224	89	2776	30	30	0
	1	3145	76	6855	5563	13	4437	7582	89	2418	29		56
	2	3449	76	6551	5511	13	4489	7938	89	2060	28		52
	3	3753	76	6247	5458	13	4542	8295	89	1705	27		48
	4	4058	76	5942	5406	13	4594	8652	89	1346	26		44
	5	4361	76	5639	5353	13	4647	9008	89	992	25		40
	6	4665	76	5335	5301	13	4699	9364	89	636	24		36
	7	4969	76	5031	5248	13	4752	9721	89	279	23		32
	8	5272	76	4728	5196	13	4804	620076	89	37924	22		28
	9	5575	75	4425	5143	13	4857	0432	89	956	21		24
	10	5877	75	4123	5090	13	4910	0787	89	9213	20		20
	11	6179	75	3821	5037	13	4963	1142	89	8858	19		16
	12	6481	75	3519	4984	13	5016	1497	89	8503	18		12
	13	6783	75	3217	4931	13	5069	1852	89	8148	17		8
	14	7085	75	2915	4878	13	5122	2207	88	7793	16		4
31	0	7387	75	2613	4825	13	5174	2561	88	7439	15	29	0
	1	7688	75	2312	4773	13	5227	2915	88	7085	14		56
	2	7989	75	2011	4720	13	5280	3269	88	6731	13		52
	3	8290	75	1711	4666	13	5334	3623	88	6377	12		48
	4	8591	75	1411	4613	13	5387	3976	88	6024	11		44
	5	8890	75	1110	4560	13	5440	4330	88	5670	10		40
	6	9190	75	810	4507	13	5493	4683	88	5317	9		36
	7	9490	75	510	4454	13	5546	5035	88	4965	8		32
	8	9790	75	211	4401	13	5599	5388	88	4612	7		28
	9	590088	75	40912	4347	13	5653	5741	88	4259	6		24
	10	0987	75	9613	4294	13	5706	6093	88	3907	5		20
	11	0685	74	9314	4240	13	5760	6446	88	3554	4		16
	12	0384	74	9019	4187	13	5813	6797	88	3203	3		12
	13	1242	74	8718	4133	13	5867	7149	88	2851	2		8
	14	1599	74	8420	4080	13	5920	7500	88	2500	1		4
31	60	9.591878	74	0.401122	9.961026	13	0.035774	9.627852	88	0.372148	0	28	0

7° 112°

1° = 15' 1" = 15°

67° 24

TABLE II.—LOG. SINES, TANG'S, &C

1° 33°		1° - 15' 1" - 15' 1" - 15°						156° 10°				
Hours.	Deg.	L. Sin	Diff. for 15'' or 1'	L. Cosc.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
32	0 0	9.591878		0.408122	9.964096	13	0.035974	9.627852	86	0.272148	60	27 0
	4 1	. 2175	74	. 7825	. 3972	13	. 6028	. 8903	86	. 1797	59	56
	8 2	. 9473	74	. 7527	. 3919	13	. 6081	. 8554	86	. 1446	58	52
	12 3	. 2770	74	. 7230	. 3865	13	. 6135	. 8905	86	. 1065	57	48
	16 4	. 3066	74	. 6934	. 3811	13	. 6189	. 9255	86	. 0745	56	44
	20 5	. 3363	74	. 6637	. 3757	13	. 6243	. 9606	87	. 0394	55	40
	24 6	. 3659	74	. 6341	. 3703	13	. 6297	. 9956	87	. 0044	54	36
	28 7	. 3956	74	. 6044	. 3650	13	. 6350	. 620306	87	. 369694	53	32
	32 8	. 4251	74	. 5749	. 3596	13	. 6404	. 0655	87	. 9345	52	28
	36 9	. 4547	74	. 5453	. 3542	13	. 6458	. 1005	87	. 8995	51	24
	40 10	. 4842	74	. 5158	. 3488	14	. 6512	. 1354	87	. 8646	50	20
	44 11	. 5137	74	. 4863	. 3433	14	. 6567	. 1704	87	. 8296	49	16
	48 12	. 5432	74	. 4568	. 3379	14	. 6621	. 2053	87	. 7947	48	12
	52 13	. 5727	74	. 4273	. 3325	14	. 6675	. 2402	87	. 7598	47	8
	56 14	. 6021	73	. 3978	. 3271	13	. 6729	. 2750	87	. 7250	46	4
33	0 15	. 6315	73	. 3683	. 3217	14	. 6783	. 3098	87	. 6902	45	27 0
	4 16	. 6609	73	. 3391	. 3162	14	. 6838	. 3447	87	. 6553	44	56
	8 17	. 6903	73	. 3097	. 3108	14	. 6892	. 3795	87	. 6205	43	52
	12 18	. 7197	73	. 2803	. 3054	14	. 6946	. 4143	87	. 5857	42	48
	16 19	. 7490	73	. 2510	. 3000	14	. 7000	. 4490	87	. 5510	41	44
	20 20	. 7783	73	. 2217	. 2945	14	. 7055	. 4838	87	. 5162	40	40
	24 21	. 8075	73	. 1925	. 2890	14	. 7110	. 5185	87	. 4815	39	36
	28 22	. 8368	73	. 1632	. 2836	14	. 7164	. 5532	87	. 4468	38	32
	32 23	. 8660	73	. 1340	. 2781	14	. 7219	. 5879	87	. 4121	37	28
	36 24	. 8952	73	. 1048	. 2726	14	. 7274	. 6226	87	. 3774	36	24
	40 25	. 9244	73	. 0756	. 2672	14	. 7328	. 6572	87	. 3428	35	20
	44 26	. 9536	73	. 0464	. 2617	14	. 7383	. 6919	86	. 3081	34	16
	48 27	. 9827	73	. 0173	. 2562	14	. 7438	. 7265	86	. 2735	33	12
	52 28	. 601118	73	. 399689	. 2507	14	. 7493	. 7611	86	. 2389	32	8
	56 29	. 0409	73	. 9591	. 2453	14	. 7547	. 7956	86	. 2044	31	4
34	0 30	. 0700	72	. 9300	. 2398	14	. 7602	. 8302	86	. 1698	30	26 0
	4 31	. 0990	72	. 9010	. 2343	14	. 7657	. 8647	86	. 1353	29	56
	8 32	. 1280	72	. 8720	. 2288	14	. 7712	. 8992	86	. 1008	28	52
	12 33	. 1570	72	. 8430	. 2233	14	. 7767	. 9337	86	. 0663	27	48
	16 34	. 1860	72	. 8140	. 2178	14	. 7822	. 9682	86	. 0318	26	44
	20 35	. 2150	72	. 7850	. 2123	14	. 7877	. 640027	86	. 359973	25	40
	24 36	. 2439	72	. 7561	. 2067	14	. 7933	. 0373	86	. 9698	24	36
	28 37	. 2728	72	. 7272	. 2012	14	. 7988	. 0718	86	. 9354	23	32
	32 38	. 3017	72	. 6983	. 1957	14	. 8043	. 1060	86	. 8940	22	28
	36 39	. 3305	72	. 6695	. 1902	14	. 8098	. 1403	86	. 8527	21	24
	40 40	. 3593	72	. 6407	. 1846	14	. 8154	. 1747	86	. 8123	20	20
	44 41	. 3882	72	. 6118	. 1791	14	. 8209	. 2091	86	. 7709	19	16
	48 42	. 4170	72	. 5830	. 1736	14	. 8264	. 2434	86	. 7296	18	12
	52 43	. 4457	72	. 5543	. 1680	14	. 8320	. 2777	86	. 6883	17	8
	56 44	. 4745	72	. 5255	. 1625	14	. 8375	. 3120	86	. 6469	16	4
35	0 45	. 5032	72	. 4968	. 1569	14	. 8431	. 3463	86	. 6057	15	25 0
	4 46	. 5319	72	. 4681	. 1513	14	. 8487	. 3806	85	. 5644	14	56
	8 47	. 5606	72	. 4394	. 1458	14	. 8542	. 4148	85	. 5232	13	52
	12 48	. 5892	72	. 4108	. 1402	14	. 8598	. 4490	85	. 4820	12	48
	16 49	. 6179	71	. 3821	. 1347	14	. 8653	. 4832	85	. 4408	11	44
	20 50	. 6465	71	. 3535	. 1291	14	. 8709	. 5174	85	. 4000	10	40
	24 51	. 6751	71	. 3249	. 1235	14	. 8765	. 5516	85	. 3594	9	36
	28 52	. 7036	71	. 2964	. 1179	14	. 8821	. 5857	85	. 3188	8	32
	32 53	. 7322	71	. 2678	. 1123	14	. 8877	. 6199	85	. 2781	7	28
	36 54	. 7607	71	. 2393	. 1067	14	. 8933	. 6540	85	. 2374	6	24
	40 55	. 7892	71	. 2108	. 1011	14	. 8989	. 6881	85	. 1968	5	20
	44 56	. 8177	71	. 1823	. 9555	14	. 9045	. 7222	85	. 1562	4	16
	48 57	. 8461	71	. 1539	. 8929	14	. 9101	. 7562	85	. 1156	3	12
	52 58	. 8745	71	. 1255	. 8303	14	. 9158	. 7903	85	. 0750	2	8
	56 59	. 9029	71	. 0971	. 7678	14	. 9214	. 8243	85	. 0344	1	4
35	60 60	9.609313		0.399837	9.960730	14	0.039270	9.648583	85	0.351417	0	24 0
Hours.	Deg.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Sin.	Diff. for 15'' or 1'	L. Cosc.	L. Cot.	Diff. for 15'' or 1'	L. Tang.	Deg.	Hours.

1° 25'			1° - 15'			1° - 15°			154°			10°		
Hours.	Deg.	L. Sin.	Diff. for 15' or 1'	L. Cossec.	L. Cos.	Diff. for 15' or 1'	L. Sec.	L. Tang.	Diff. for 15' or 1'	L. Cot.	Deg.	Hours.		
40	0	9.625948	64	0.374052	9.957276	15	0.042724	9.668679	82	0.33332	60	19		
	4	6219	68	37'1	7217	15	2783	9002	82	0944	59	50		
	8	6490	67	3510	7158	15	2842	9332	82	0616	58	52		
	12	6760	67	3240	7099	15	2901	9661	82	0338	57	54		
	16	7030	67	2970	7040	15	2960	9990	82	0010	56	44		
	20	7300	67	2700	6980	15	3020	670320	82	339670	55	40		
	24	7570	67	2430	6921	15	3079	0649	82	9351	54	36		
	28	7840	67	2160	6863	15	3137	0977	82	9023	53	32		
	32	8109	67	1991	6803	15	3197	1306	82	8694	52	28		
	36	8378	67	1822	6744	15	3256	1634	82	8366	51	24		
	40	8647	67	1353	6684	15	3316	1963	82	8037	50	20		
	44	8916	67	1084	6625	15	3372	2291	82	7707	49	16		
	48	9185	67	815	6566	15	3434	2619	82	7371	48	12		
	52	9453	67	547	6506	15	3494	2947	82	7033	47	8		
	56	9721	67	279	6447	15	3553	3274	82	6736	46	4		
41	0	9989	67	0011	6387	15	3613	3602	82	6398	45	19		
	4	030957	67	369743	6328	15	3672	3929	82	6071	44	15		
	8	0524	67	9476	6268	15	3732	4256	82	5744	43	11		
	12	0792	67	9908	6208	15	3792	4584	82	5417	42	7		
	16	1059	67	8941	6148	15	3852	4911	82	5089	41	4		
	20	1326	67	8674	6089	15	3911	5237	82	4763	40	0		
	24	1583	67	8407	6029	15	3971	5564	82	4437	39	56		
	28	1859	67	8144	3089	15	4031	5890	81	4110	38	52		
	32	2126	66	7874	5006	15	4091	6217	81	3783	37	48		
	36	2392	66	7606	5849	15	4151	6543	81	3457	36	44		
	40	2658	66	7342	5789	15	4211	6869	81	3131	35	40		
	44	2923	66	7077	5729	15	4271	7194	81	2804	34	36		
	48	3189	66	6811	5669	15	4331	7520	81	2479	33	32		
	52	3454	66	6546	5609	15	4391	7845	81	2153	32	28		
	56	3719	66	6281	5548	15	4452	8171	81	1827	31	4		
42	0	3984	66	6016	5488	15	4512	8496	81	1504	30	18		
	4	4249	66	5751	5428	15	4572	8821	81	1179	29	14		
	8	4514	66	5486	5368	15	4632	9146	81	0854	28	10		
	12	4778	66	5222	5307	15	4693	9471	81	0529	27	6		
	16	5042	66	4958	5247	15	4753	9795	81	0203	26	4		
	20	5306	66	4694	5186	15	4814	680130	81	319990	25	0		
	24	5570	66	4430	5126	15	4874	0444	81	9556	24	56		
	28	5833	66	4167	5065	15	4935	0768	81	9232	23	52		
	32	6097	66	3903	5005	15	4995	1092	81	8908	22	48		
	36	6360	66	3640	4944	15	5056	1416	81	8584	21	44		
	40	6623	66	3377	4883	15	5117	1740	81	8260	20	40		
	44	6886	66	3114	4823	15	5177	2063	81	7937	19	36		
	48	7149	66	2852	4762	15	5238	2386	81	7614	18	32		
	52	7411	66	2590	4701	15	5299	2710	81	7290	17	28		
	56	7673	65	2327	4640	15	5360	3033	81	6967	16	4		
43	0	7935	65	2065	4579	15	5421	3356	81	6644	15	17		
	4	8197	65	1803	4519	15	5482	3679	80	6321	14	13		
	8	8459	65	1542	4457	15	5543	4001	80	5999	13	9		
	12	8720	65	1280	4396	15	5604	4324	80	5678	12	5		
	16	8981	65	1019	4335	15	5665	4646	80	5354	11	4		
	20	9242	65	0758	4274	15	5726	4968	80	5032	10	0		
	24	9503	65	0497	4213	15	5787	5290	80	4710	9	56		
	28	9764	65	0236	4152	15	5848	5612	80	4388	8	52		
	32	640921	65	389776	4091	15	5910	5934	80	4066	7	48		
	36	0234	65	9716	4029	15	5971	6255	80	3743	6	44		
	40	0545	65	9455	3968	15	6032	6577	80	3423	5	40		
	44	0804	65	9196	3905	15	6094	6898	80	3102	4	36		
	48	1034	65	8936	3845	15	6155	7219	80	2781	3	32		
	52	1263	65	8677	3783	15	6217	7540	80	2460	2	28		
	56	1503	65	8417	3722	15	6278	7861	80	2139	1	24		
43	00	9.641849	65	0.338158	9.953660	15	0.046340	9.668182	80	0.311818	0	16		

TABLE II.—LOG. SINES, TANG'S, &c.

1° 29'		1° - 15' 1" - 15'						153°		10°				
Hours	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cosec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	deg.	Hours		
44	0	0.031412	65	0.333153	9.933360	15	0.016340	0.081182	80	0.311316	60	15	30	
	4	2101	65	7593	3510	15	6101	8502	80	1478	53		53	
	8	2140	65	7040	3537	15	6433	8623	81	1177	58		48	
	12	2114	65	7332	3475	15	6525	9143	80	805	57		45	
	16	2276	64	7124	3413	15	6567	9463	80	6537	56		44	
	20	5	3135	64	6865	3352	15	6642	9783	80	5217	55		40
	24	6	3134	64	6607	320	15	6710	9910	80	3067	54		35
	28	7	3151	64	6349	3228	15	6772	0423	80	9577	51		32
	32	8	300	64	6092	3106	15	6834	0742	80	925	52		28
	36	9	4166	64	5834	3101	15	6896	1062	80	8936	51		24
45	40	10	4421	64	5577	3042	15	6958	1381	80	8619	50		20
	44	11	4483	64	5320	2980	15	7020	1709	80	8300	49		16
	48	12	4437	64	5063	2915	15	7082	2011	80	7981	48		12
	52	13	5173	64	4807	2855	15	7145	2312	80	7662	47		8
	56	14	5450	64	4550	2793	15	7207	2657	79	7343	46		4
	0	15	5707	64	4294	2731	15	7269	2975	79	7025	45	15	0
	4	16	5462	64	4037	2669	15	7331	3293	79	6707	44		53
	8	17	6218	64	3782	2607	16	7394	3612	79	6386	43		52
	12	18	6474	64	3525	2544	15	7456	3930	79	6070	42		48
	16	19	6732	64	3271	2481	16	7519	4248	79	5752	41		44
46	20	20	6985	64	3015	2419	16	7581	4566	79	5434	40		40
	24	21	7231	64	2758	2357	15	7644	4883	79	5117	39		36
	28	22	7475	64	2503	2295	16	7706	5201	79	4771	38		32
	32	23	7719	64	2251	2231	16	7769	5518	79	4422	37		28
	36	24	8034	63	1996	2168	15	7832	5836	79	4104	36		24
	40	25	8338	63	1742	2105	16	7895	6153	79	3847	35		20
	44	26	8512	63	1483	2043	16	7957	6470	79	3530	34		16
	48	27	8746	63	1234	1980	16	8020	6786	79	3213	33		12
	52	28	9020	63	0980	1917	16	8083	7101	79	2907	32		8
	56	29	9274	63	0723	1854	16	8146	7420	79	2590	31		4
47	0	30	9527	63	0473	1791	16	8209	7736	79	2264	30	14	0
	4	31	9781	63	0219	1728	16	8272	8053	79	1947	29		53
	8	32	630374	63	343066	1865	16	8335	8379	79	1631	27		52
	12	33	0247	63	9713	1802	16	8398	8685	79	1315	27		48
	16	34	0540	63	9460	1739	16	8461	9001	79	099	26		44
	20	35	0792	63	9219	1476	16	8524	9316	79	0584	25		40
	24	36	1044	63	8975	1412	16	8587	9632	79	0184	24		36
	28	37	1317	63	8733	1349	16	8651	9948	79	0052	23		32
	32	38	1519	63	8491	1285	16	8714	701233	79	99737	22		28
	36	39	1803	63	8250	1222	16	8778	0578	79	9422	21		24
48	40	40	2152	63	7998	1159	16	8841	0893	79	9107	20		20
	44	41	2391	63	7733	1096	16	8904	1204	79	8792	19		16
	48	42	2533	63	7465	1032	16	8968	1521	78	8477	18		12
	52	43	2801	63	7114	0969	16	9031	1837	78	8163	17		8
	56	44	3057	63	6843	0905	16	9095	2152	78	7844	16		4
	0	45	3317	62	6573	0841	16	9159	2466	78	7524	15	13	0
	4	46	3532	62	6342	0778	16	9223	2780	78	7221	14		53
	8	47	3791	62	6111	0714	16	9287	3095	78	6905	13		52
	12	48	4053	62	5881	0650	16	9350	3401	78	6511	12		48
	16	49	4330	62	5691	0586	16	9414	3721	78	6277	11		44
49	20	57	4552	62	5442	0522	16	9478	4036	78	5961	10		40
	24	51	4792	62	5192	0458	16	9542	4350	78	5651	9		36
	28	52	5117	62	4943	0394	16	9606	4663	78	5347	8		32
	32	53	5477	62	4723	0330	16	9670	4977	78	5037	7		28
	36	54	5831	62	4444	0266	16	9734	5290	78	4710	6		24
	40	55	5991	62	4195	0202	16	9798	5607	78	4397	5		20
	44	56	6051	62	3945	0138	16	9862	5911	78	4084	4		16
	48	57	6113	62	3795	0074	16	9926	6223	78	3772	3		12
	52	58	6511	62	3447	0010	16	9990	6511	78	345	2		8
	56	59	6717	62	3191	9945	16	00545	6841	78	314	1		4
0	60	0.537017	62	0.242351	9.913881	16	0.050111	0.707166	78	0.392331	0	12	0	

116°

1° - 4' 10" - 4"

63° 4'

1°		27°		1° - 15'		1° - 15'		1° - 15'		182°		1°	
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cos.	L. Sec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
48	0	9.657947	62	0.34253	9.943881	0.050119	9.707160	0.292554	60	11	60	0	0
	1	7245	62	2705	9817	16	0153	7478	78		2522	59	36
	2	7542	62	2454	9752	16	0248	7749	78		2210	58	52
	3	7790	62	2210	9688	16	0312	8102	78		1845	57	48
	4	8337	62	1903	9623	16	0377	8444	78		1580	56	44
	5	8284	62	1716	9558	16	0442	8726	78		1374	55	40
	6	8111	62	1464	9444	16	0503	9037	78		0463	54	36
	7	8778	62	1222	9423	16	0571	9349	78		0651	53	32
	8	9125	61	0753	9345	16	0635	9609	78		0349	52	28
	9	9271	61	0729	9300	16	0700	9971	78		0029	51	24
	10	9517	61	0483	9235	16	0765	710282	78	389718	50	20	20
	11	9763	61	0237	9170	16	0830	0533	78		9407	49	16
	12	639099	61	33991	9103	16	0835	0404	78		9086	48	12
	13	0255	61	9745	9040	16	0900	1213	78		8785	47	8
	14	0300	61	9500	8975	16	1025	1543	78		8479	46	4
49	0	15	61	0746	9254	16	1030	1836	77		8104	45	11
	1	0611	61	0391	8945	16	1155	2146	77		7854	44	56
	2	1326	61	8764	8780	16	1220	2456	77		7544	43	52
	3	1491	61	8519	8715	16	1245	2766	77		7234	42	48
	4	1726	61	8274	8650	16	1350	3076	77		6924	41	44
	5	1970	61	8030	8584	16	1416	3386	77		6614	40	40
	6	2215	61	7785	8519	16	1481	3696	77		6304	39	36
	7	2459	61	7541	8454	16	1546	4005	77		5995	38	32
	8	2703	61	7297	8388	16	1612	4315	77		5685	37	28
	9	2947	61	7053	8323	16	1677	4624	77		5376	36	24
	10	3190	61	6810	8257	16	1743	4933	77		5067	35	20
	11	3431	61	6566	8192	16	1808	5242	77		4758	34	16
	12	3677	61	6321	8126	16	1874	5551	77		4449	33	12
	13	3920	61	6080	8060	16	1940	5860	77		4140	32	8
	14	4163	61	5837	7995	16	2005	6168	77		3832	31	4
50	0	30	60	5574	7929	16	2071	6477	77		3523	30	10
	1	4648	60	5332	7863	16	2137	6785	77		3215	29	56
	2	4940	60	5110	7797	16	2203	7093	77		2907	28	52
	3	5179	60	4847	7732	16	2268	7401	77		2599	27	48
	4	5375	60	4625	7666	16	2334	7709	77		2291	26	44
	5	5617	60	4430	7600	16	2400	8017	77		1983	25	40
	6	5859	60	4141	7534	16	2466	8325	77		1675	24	36
	7	6100	60	3900	7467	17	2533	8633	77		1367	23	32
	8	6341	60	3659	7401	16	2599	8940	77		1060	22	28
	9	6583	60	3417	7335	16	2665	9248	77		0752	21	24
	10	6824	60	3176	7269	16	2731	9555	77		0445	20	20
	11	7065	60	2935	7203	17	2797	9862	77		0138	19	16
	12	7305	60	2705	7136	17	2864	720169	77	327831	18	12	12
	13	7546	60	2454	7070	17	2930	0476	77		0524	17	8
	14	7786	59	2214	7003	17	2997	0783	77		0217	16	4
51	0	45	60	1974	6937	17	3073	1089	77		8911	15	0
	1	8217	60	1733	6871	17	3129	1396	77		8604	14	56
	2	8509	60	1494	6804	17	3196	1702	77		8298	13	52
	3	8749	60	1253	6738	17	3262	2008	77		7992	12	48
	4	8986	60	1014	6671	17	3329	2315	77		7685	11	44
	5	9225	60	0775	6604	16	3396	2621	76		7379	10	40
	6	9464	60	0536	6537	16	3463	2927	76		7073	9	36
	7	9703	60	0297	6471	17	3529	3232	76		6768	8	32
	8	9942	60	0058	6404	17	3596	3538	76		6462	7	28
	9	670181	59	339819	6337	17	3663	3844	76		6156	6	24
	10	0419	59	9581	6270	17	3730	4149	76		5851	5	20
	11	0657	59	9343	6203	17	3797	4454	76		5546	4	16
	12	0896	59	9104	6136	17	3864	4760	76		5240	3	12
	13	1134	59	8866	6069	17	3931	5065	76		4935	2	8
	14	1372	59	8628	6002	17	3998	5370	76		4630	1	4
51	60	9.671609	59	0.328301	9.945935	0.054065	9.725074	0.274326	0	8	0	0	0

TABLE II.—LOG. SINES, TANG'S, &c.

1° 29°			1° - 15' 1" - 15' 1" - 15°						151° 10°			
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Ho.
52	0	0.6710	59	0.328311	0.945935	17	0.054065	9.725674	76	0.274328	60	7
	1	1847	59	8153	5848	17	4132	5779	76	4021	59	
	2	2084	59	7916	5500	17	4900	6294	76	3711	58	
	3	2281	59	7679	5233	17	4267	6589	76	3412	57	
	4	2558	59	7442	5066	17	4334	6892	76	3106	56	
	5	2795	59	7205	5398	17	4402	7197	76	2803	55	
	6	3032	59	6968	5531	17	4469	7501	76	2496	54	
	7	3299	59	6731	5464	17	4536	7805	76	2195	53	
	8	3585	59	6495	5396	17	4604	8109	76	1891	52	
	9	3741	59	6259	5322	17	4671	84.9	76	1568	51	
	10	3977	59	6023	5261	17	4739	8716	76	1284	50	
	11	4213	59	5787	5193	17	4807	9020	76	9860	49	
	12	4449	59	5551	5126	17	4874	9323	76	6877	48	
	13	4684	59	5316	5058	17	4942	9626	76	3874	47	
	14	4919	59	5081	4990	17	5010	9929	76	0071	46	
53	0	5155	59	4845	4922	17	5078	730233	76	266767	45	7
	1	5390	59	4609	4854	17	5146	0536	76	9464	44	
	2	5624	59	4376	4786	17	5214	0838	76	9162	43	
	3	5859	59	4141	4718	17	5282	1141	76	8859	42	
	4	6094	58	3906	4650	17	5350	1444	75	8556	41	
	5	6328	58	3672	4582	17	5418	1746	75	8254	40	
	6	6562	58	3438	4514	17	5486	2048	75	7952	39	
	7	6796	58	3204	4446	17	5554	2350	75	7650	38	
	8	7030	58	2970	4377	17	5623	2653	75	7347	37	
	9	7264	58	2736	4309	17	5691	2955	75	7045	36	
	10	7498	58	2502	4241	17	5759	3257	75	6743	35	
	11	7731	58	2268	4173	17	5827	3559	75	6442	34	
	12	7964	58	2034	4104	17	5896	3860	75	6140	33	
	13	8197	58	1803	4036	17	5964	4161	75	5837	32	
	14	8430	58	1570	3967	17	6033	4463	75	5537	31	
54	0	8663	58	1337	3899	17	6101	4764	75	5236	30	6
	1	8896	58	1104	3830	17	6170	5066	75	4934	29	
	2	9129	58	872	3761	17	6239	5367	75	4633	28	
	3	9362	58	640	3692	17	6308	5668	75	4332	27	
	4	9595	58	408	3624	17	6376	5968	75	4032	26	
	5	9828	58	176	3555	17	6445	6269	75	3731	25	
	6	10061	58	319444	3486	17	6514	6570	75	3430	24	
	7	10294	58	8712	3417	17	6583	6871	75	3127	23	
	8	10527	58	9481	3348	17	6652	7171	75	2827	22	
	9	10760	58	9250	3279	17	6721	7471	75	2529	21	
	10	10993	58	9018	3210	17	6790	7772	75	2229	20	
	11	11226	58	8787	3141	17	6859	8072	75	1928	19	
	12	11459	58	8555	3072	17	6928	8371	75	1627	18	
	13	11692	58	8324	3003	17	6997	8671	75	1327	17	
	14	11925	57	8093	2934	17	7066	8971	75	1027	16	
55	0	12158	57	7862	2865	17	7136	9271	75	0729	15	8
	1	12391	57	7631	2795	17	7205	9570	75	0430	14	
	2	12624	57	7403	2725	17	7274	9870	75	0130	13	
	3	12857	57	7175	2656	17	7344	740169	75	259031	12	
	4	13090	57	6945	2587	17	7413	0468	75	9532	11	
	5	13323	57	6716	2517	17	7483	0767	75	9233	10	
	6	13556	57	6486	2447	17	7552	1066	75	8934	9	
	7	13789	57	6257	2377	17	7622	1365	75	8635	8	
	8	14022	57	6028	2307	17	7692	1664	75	8337	7	
	9	14255	57	5799	2237	17	7761	1962	75	8038	6	
	10	14488	57	5570	2167	17	7831	2261	75	7739	5	
	11	14721	57	5342	2097	17	7901	2559	75	7441	4	
	12	14954	57	5113	2027	17	7971	2858	74	7142	3	
	13	15187	57	4885	1957	17	8041	3156	74	6844	2	
	14	15420	57	4657	1887	17	8111	3454	74	6547	1	
55	15	9.685571	57	0.314422	9.941819	17	0.058181	9.743752	74	0.256242	0	4

118°

1° - 4' 10" - 4"

81° 4'

TABLE II.—LOG. SINES, TANG'S, &C.

29°		1° - 15' 1" - 15' 1" - 15°				150° - 10°					
PR.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
0	9.665571		0.31442	9.941819		0.038181	9.74375		0.25024	10	3 00
1	57:9	57	4201	1749	17	8251	4056	74	5050	59	58
2	027	57	3973	1679	17	8221	4344	74	5152	58	57
3	0254	57	3746	1609	17	8201	4645	74	5255	57	47
4	64e2	57	3518	1539	17	8181	4945	74	5357	56	44
5	6709	57	3291	1469	17	8161	5240	74	5470	55	40
6	6936	57	3064	1398	18	8142	5535	74	5482	54	36
7	7163	57	2837	1328	17	8122	5835	74	5495	53	32
8	730	57	2610	1258	17	8102	6132	74	5508	52	28
9	760	57	2384	1187	17	8083	6422	74	5521	51	24
10	7843	56	2157	1117	17	8063	6720	74	5534	50	20
11	8089	56	1931	1046	18	8054	7022	74	5547	49	16
12	825	56	1705	976	17	8044	7321	74	5560	48	12
13	8521	56	1479	905	18	8035	7618	74	5574	47	8
14	8747	56	1253	834	18	8026	7913	74	5587	46	4
15	8922	56	1028	763	17	8017	8209	74	5599	45	3 0
16	9118	56	802	693	17	8007	8505	74	5612	44	3 0
17	9293	56	577	622	18	7998	8801	74	5625	43	3 0
18	9447	56	352	551	18	7988	9097	74	5638	42	3 0
19	9673	56	127	480	18	7979	9393	74	5651	41	44
20	600000	56	300002	0409	18	7970	9689	74	5664	40	40
21	0323	56	9677	0338	18	7960	9985	74	5677	39	36
22	0547	56	9452	0267	18	7951	75021	74	5690	38	32
23	0772	56	9227	0196	18	7942	0576	74	5703	37	28
24	0357	56	9003	0125	18	7933	0872	74	5716	36	24
25	1221	56	8777	0054	18	7924	1167	74	5729	35	20
26	1444	56	8556	93982	18	7915	1462	74	5742	34	16
27	1648	56	8332	8911	18	7906	1757	74	5755	33	12
28	182	56	8108	8420	18	7897	2052	74	5768	32	8
29	2115	56	7885	7768	18	7888	2347	74	5781	31	4
30	233	56	7661	6987	18	7879	2642	74	5794	30	0
31	252	56	7438	6225	18	7870	2937	74	5807	29	56
32	275	56	7215	5454	18	7861	3231	74	5820	28	52
33	3009	56	6992	4682	18	7852	3526	73	5833	27	48
34	3231	56	6769	3911	18	7843	3820	73	5846	26	44
35	3454	55	6546	3139	18	7834	4115	73	5859	25	40
36	376	55	6324	2367	18	7825	4409	73	5872	24	36
37	3898	55	6102	1595	18	7816	4703	73	5885	23	32
38	4120	55	5880	9123	18	7807	4997	73	5898	22	28
39	4342	55	5658	8351	18	7798	5291	73	5911	21	24
40	4564	55	5436	7579	18	7789	5584	73	5924	20	20
41	4786	55	5214	6808	18	7780	5878	73	5937	19	16
42	5008	55	4992	6036	18	7771	6172	73	5950	18	12
43	5229	55	4771	5264	18	7762	6465	73	5963	17	8
44	5450	55	4550	4491	18	7753	6759	73	5976	16	4
45	5671	55	4328	3719	18	7744	7052	73	5989	15	1 0
46	5892	55	4106	2947	18	7735	7345	73	5999	14	5 0
47	6113	55	3884	2175	18	7726	7638	73	6010	13	52
48	6334	55	3662	1403	18	7717	7931	73	6021	12	48
49	6554	55	3440	630	18	7708	8224	73	6031	11	44
50	6775	55	3218	958	18	7700	8517	73	6042	10	40
51	6995	55	3005	815	18	7691	8810	73	6052	9	36
52	7215	55	2792	613	18	7682	9102	73	6063	8	32
53	7435	55	2579	409	18	7673	9395	73	6074	7	28
54	7654	55	2366	206	18	7664	9687	73	6085	6	24
55	7874	55	2153	78.5	18	7655	9979	73	6096	5	20
56	8094	55	1940	762	18	7646	76122	73	6107	4	16
57	8313	55	1727	740	18	7637	057	73	6118	3	12
58	8532	55	1514	718	18	7628	090	73	6129	2	8
59	8751	55	1301	696	18	7619	123	73	6140	1	4
60	8970	55	1088	674	18	7610	156	73	6151	0	0
			0.301030	9.937571		0.062466	9.761437		0.239910		
	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cot.	Diff. for 15' or 1"	L. Tang.	Deg.	Hou s

TABLE II.—LOG. SINES, TANG'S, &c.

90° — 30°

1° — 15' 1" — 15' 1" — 15°

149° 90

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cosec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
0	0	9.69376	55	0.301030	9.937531	18	0.062469	9.761438	73	0.238561	60	0
	1	918	55	0811	7458	18	2542	1731	73	8219	59	56
	2	9407	55	0593	7385	18	2615	2029	73	7778	58	52
	3	962	54	0374	7312	18	2688	2314	73	7186	57	48
	4	9844	54	0156	7238	18	2762	2606	73	6594	56	44
	5	70069	54	99938	7165	18	2835	2897	73	6003	55	40
	6	028	54	9730	7092	18	2908	3188	73	5412	54	36
	7	048	54	9502	7018	18	2981	3479	73	4821	53	32
	8	0711	54	9284	6946	18	3054	3770	73	4230	52	28
	9	0335	54	9067	6872	18	3128	4061	73	3639	51	24
	10	1151	54	8849	6799	18	3201	4352	73	3048	50	20
	11	138	54	8632	6725	18	3275	4643	73	2457	49	16
	12	1545	54	8415	6652	18	3348	4933	73	1866	48	12
	13	1802	54	8198	6578	18	3422	5224	73	1275	47	8
	14	2018	54	7981	6505	18	3495	5514	73	684	46	4
1	0	2236	54	7764	6431	18	3568	5805	72	4195	45	0
	1	2452	54	7548	6357	18	3643	60.5	72	3605	44	56
	2	2689	54	7331	6284	18	3716	6385	72	3015	43	52
	3	2925	54	7115	6210	18	3790	6675	72	2425	42	48
	4	3161	54	6899	6136	18	3864	6965	72	1835	41	44
	5	3407	54	6683	6062	18	3938	7255	72	1245	40	40
	6	3653	54	6467	5988	18	4012	7545	72	655	39	36
	7	3900	54	6251	5914	18	4086	7834	72	216	38	32
	8	4148	54	6036	5840	18	4160	8124	72	187	37	28
	9	4400	54	5820	5766	18	4234	8414	72	158	36	24
	10	4655	54	5605	5692	18	4308	8703	72	129	35	20
	11	4913	54	5390	5618	18	4382	8992	72	100	34	16
	12	5173	54	5175	5543	18	4457	9282	72	71	33	12
	13	5435	54	4960	5469	18	4531	9571	72	42	32	8
	14	5700	54	4746	5395	19	4605	9859	72	14	31	4
2	0	5409	53	4531	5320	18	4680	770149	72	29851	30	0
	1	5783	53	4317	5246	18	4754	0437	72	953	29	56
	2	588	53	4102	5172	18	4828	0726	72	9774	28	52
	3	6112	53	3888	5097	19	4903	1015	72	8965	27	48
	4	632	53	3674	5023	19	4977	1303	72	8097	26	44
	5	6540	53	3460	4948	19	5052	1592	72	7209	25	40
	6	6753	53	3247	4873	19	5127	1880	72	6320	24	36
	7	6967	53	3033	4798	19	5202	2169	72	5431	23	32
	8	7180	53	2820	4723	19	5277	2457	72	4542	22	28
	9	7393	53	2607	4648	19	5352	2745	72	3653	21	24
	10	7606	53	2394	4573	19	5427	3033	72	2764	20	20
	11	7818	53	2181	4498	19	5502	3321	72	1875	19	16
	12	8032	53	1968	4424	19	5578	3608	72	986	18	12
	13	8245	53	1755	4349	19	5653	3896	72	6104	17	8
	14	8458	53	1542	4274	19	5728	4184	72	5311	16	4
3	0	8670	53	1330	4199	19	5801	4471	72	5526	15	0
	1	8882	53	1118	4123	19	5877	4759	72	4731	14	56
	2	9094	53	906	4048	19	5952	5046	72	3936	13	52
	3	9301	53	694	3973	19	6027	5333	72	3141	12	48
	4	9518	53	482	3898	19	6102	5620	72	2346	11	44
	5	9730	53	270	3822	19	6178	5906	72	1551	10	40
	6	9942	53	58	3747	19	6253	6195	72	756	9	36
	7	710153	53	38847	3671	19	6328	6482	72	358	8	32
	8	074	53	9636	3596	19	6404	6768	72	279	7	28
	9	0575	53	9425	3520	19	6480	7055	72	200	6	24
	10	0788	53	9214	3444	19	6556	7342	72	121	5	20
	11	0997	53	9003	3368	19	6631	7628	71	42	4	16
	12	1208	53	8792	3293	19	6707	7915	71	23	3	12
	13	1418	53	8582	3217	19	6783	8201	71	14	2	8
	14	1629	53	8371	3141	19	6859	8488	71	5	1	4
3	0	971839	52	0288161	9933065		0.060935	9.778774		0.291297	0	56

90° — 180°

1° — 4' 10 — 4°

80° 90

31°		1° - 15' 1" - 15'						149°				
Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
4	0	0	9.711839	53	0.988161	0.933665	19	0.066035	9.776774	71	0.221226	10
	4	1	3050	52	7.50	2540	19	7010	9000	71	0.0000	50
	8	2	2200	52	7740	2914	19	7086	9340	71	0.054	52
	12	3	2470	52	7530	2838	19	7162	9652	71	0.060	58
	16	4	2679	52	7321	2761	19	7239	9912	71	0.062	56
	20	5	2889	52	7111	2685	19	7315	780204	71	0.19796	55
	24	6	3098	52	6902	2609	19	7391	0489	71	0.511	54
	28	7	3308	52	6692	2533	19	7467	0775	71	0.225	53
	32	8	3517	52	6483	2457	19	7543	1064	71	0.40	52
	36	9	3726	52	6274	2380	19	7620	1346	71	0.554	51
	40	10	3935	52	6065	2304	19	7696	1631	71	0.266	50
	44	11	4144	52	5856	2228	19	7772	1916	71	0.064	49
	48	12	4352	52	5648	2151	19	7849	2201	71	0.779	48
	52	13	4561	52	5439	2075	19	7925	2484	71	0.514	47
	56	14	4769	52	5231	1998	19	8002	2771	71	0.226	46
5	0	15	4977	52	5023	1921	19	8079	3056	71	0.644	45
	4	16	5186	52	4814	1845	19	8155	3341	71	0.659	44
	8	17	5394	52	4606	1768	19	8232	3626	71	0.374	43
	12	18	5601	52	4399	1691	19	8309	3910	71	0.000	42
	16	19	5809	52	4191	1614	19	8386	4195	71	0.505	41
	20	20	6017	52	3983	1538	19	8463	4479	71	0.521	40
	24	21	6224	52	3776	1460	19	8540	4764	71	0.226	39
	28	22	6432	52	3568	1384	19	8616	5048	71	0.502	38
	32	23	6639	52	3361	1307	19	8693	5332	71	0.466	37
	36	24	6846	52	3154	1230	19	8770	5616	71	0.224	36
	40	25	7053	52	2948	1152	19	8848	5900	71	0.400	35
	44	26	7259	52	2741	1075	19	8925	6184	71	0.316	34
	48	27	7466	52	2534	0998	19	9002	6468	71	0.532	33
	52	28	7673	52	2327	0921	19	9079	6752	71	0.246	32
	56	29	7879	51	2121	0843	19	9157	7036	71	0.264	31
6	0	30	8085	51	1915	0766	19	9234	7319	71	0.2681	30
	4	31	8291	51	1709	0688	19	9312	7603	71	0.237	29
	8	32	8497	51	1503	0611	19	9389	7886	71	0.214	28
	12	33	8703	51	1297	0533	19	9467	8170	71	0.1830	27
	16	34	8909	51	1091	0456	19	9544	8453	71	0.1547	26
	20	35	9114	51	886	0378	19	9622	8736	71	0.1264	25
	24	36	9319	51	681	0300	19	9700	9019	71	0.0961	24
	28	37	9525	51	0475	09. 3	19	9777	9302	71	0.0692	23
	32	38	9730	51	0370	0145	19	9855	9585	71	0.0415	22
	36	39	9935	51	0065	0067	19	9933	9868	71	0.0132	21
	40	40	790140	51	279860	929689	19	070011	790151	71	0.20949	20
	44	41	0345	51	9655	9911	19	0089	0434	71	0.856	19
	48	42	0549	51	9451	8233	19	0167	0718	71	0.284	18
	52	43	0754	51	9246	6755	19	0245	0999	71	0.001	17
	56	44	0958	51	9043	5677	19	0323	1281	71	0.719	16
7	0	45	1102	51	8838	4599	19	0401	1563	70	0.847	15
	4	46	1366	51	8634	3521	20	0479	1846	70	0.154	14
	8	47	1570	51	8430	2443	19	0556	2129	70	0.772	13
	12	48	1774	51	8226	1365	19	0633	2410	70	0.750	12
	16	49	1978	51	8022	2286	20	0714	2692	70	0.730	11
	20	50	2181	51	7819	1207	19	0792	2974	70	0.708	10
	24	51	2385	51	7615	9123	20	0871	3256	70	0.744	9
	28	52	2588	51	7412	8045	19	0950	3538	70	0.682	8
	32	53	2791	51	7209	6967	20	1029	3819	70	0.181	7
	36	54	2994	51	7006	5889	19	1107	4101	70	0.589	6
	40	55	3197	51	6803	4814	20	1186	4383	70	0.517	5
	44	56	3400	51	6600	3736	20	1264	4664	70	0.536	4
	48	57	3603	50	6397	2657	20	1343	4946	70	0.554	3
	52	58	3805	50	6195	1578	20	1422	5227	70	0.4773	2
	56	59	4007	50	5993	4899	20	1501	5508	70	0.4492	1
7	00	60	9.734210	50	0.275790	0.928421	20	0.071579	9.795779	70	0.204211	0
m	o			Diff. for 15'' or 1'		Diff. for 15'' or 1'		Diff. for 15'' or 1'		Diff. for 15'' or 1'		Hours.
Hours.	Deg.	L. Cos.		L. Sec.	L. Sin.		L. Cossec.	L. Cot.		L. Tang.	Deg.	Hours.

TABLE II.—LOG. SINES, TANG'S, &c.

90° 30'

1° - 15' 1" - 15' 1" - 150

147° 0'

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cos. c.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
8	0	9.724210	50	0.275730	9.924211	30	0.071579	9.795789	70	0.203211	6.0	51 0
	1	4412	50	55.98	8342	30	1658	6070	70	3380	5.0	51 5
	2	4614	50	53.96	8263	30	1737	6351	70	3643	5.0	52 5
	3	4816	50	51.94	8184	30	1816	6632	70	3908	5.0	53 5
	4	5017	50	49.93	8104	30	1896	6913	70	4187	5.0	54 5
	5	5219	50	47.91	8025	30	1975	7194	70	4466	5.0	55 5
	6	5420	50	45.90	7946	30	2054	7474	70	4746	5.0	56 5
	7	5622	50	43.88	7867	30	2133	7755	70	5025	5.0	57 5
	8	5823	50	41.87	7787	30	2213	8036	70	5305	5.0	58 5
	9	6024	50	39.86	7708	30	2292	8316	70	5584	5.0	59 5
	10	6225	50	37.85	7629	30	2371	8596	70	5864	5.0	60 5
	11	6426	50	35.84	7549	30	2451	8877	70	6143	5.0	61 5
	12	6627	50	33.83	7469	30	2531	9157	70	6423	5.0	62 5
	13	6827	50	31.82	7389	30	2610	9437	70	6703	5.0	63 5
	14	7027	50	29.81	7310	30	2690	9717	70	6983	5.0	64 5
	15	7228	50	27.80	7231	30	2769	9997	70	7263	5.0	65 5
	16	7428	50	25.79	7151	30	2849	800277	70	7543	5.0	66 5
	17	7629	50	23.78	7071	30	2929	0557	70	7823	5.0	67 5
	18	7829	50	21.77	6991	30	3009	0837	70	8103	5.0	68 5
	19	8029	50	19.76	6911	30	3089	1116	70	8383	5.0	69 5
	20	8229	50	17.75	6831	30	3169	1396	70	8663	5.0	70 5
	21	8429	50	15.74	6751	30	3248	1675	70	8943	5.0	71 5
	22	8629	50	13.73	6671	30	3329	1955	70	9223	5.0	72 5
	23	8829	50	11.72	6591	30	3409	2234	70	9503	5.0	73 5
	24	9029	50	9.71	6511	30	3489	2513	70	9783	5.0	74 5
	25	9229	50	7.70	6431	30	3569	2792	70	10063	5.0	75 5
	26	9429	50	5.69	6351	30	3649	3071	70	10343	5.0	76 5
	27	9629	50	3.68	6271	30	3729	3351	70	10623	5.0	77 5
	28	9829	50	1.67	6191	30	3809	3630	70	10903	5.0	78 5
	29	730018	49	309982	6110	30	3889	3908	70	11183	5.0	79 5
	30	0216	49	9784	6029	30	3971	4187	70	5813	30	50 0
	1	0415	49	9585	5949	30	4051	4466	70	5534	29	50 5
	2	0613	49	9387	5868	30	4132	4745	70	5255	28	51 5
	3	0811	49	9189	5788	30	4212	5023	70	4977	27	52 5
	4	1009	49	8991	5707	30	4293	5302	70	4698	26	53 5
	5	1208	49	8794	5626	30	4374	5580	70	4420	25	54 5
	6	1406	49	8596	5545	30	4455	5859	69	4141	24	55 5
	7	1604	49	8398	5465	30	4535	6137	69	3863	23	56 5
	8	1802	49	8201	5384	30	4616	6415	69	3585	22	57 5
	9	1999	49	8004	5303	30	4697	6693	69	3307	21	58 5
	10	2197	49	7807	5222	30	4778	6971	69	3029	20	59 5
	11	2394	49	7610	5141	30	4859	7249	69	2751	19	60 5
	12	2592	49	7413	5060	30	4940	7527	69	2473	18	61 5
	13	2789	49	7216	4979	30	5021	7805	69	2195	17	62 5
	14	2987	49	7020	4897	30	5103	8083	69	1917	16	63 5
	15	3177	49	6823	4816	30	5184	8351	69	1639	15	64 5
	16	3373	49	6627	4735	30	5265	8633	69	1361	14	65 5
	17	3570	49	6431	4653	30	5347	8916	69	1083	13	66 5
	18	3767	49	6235	4572	30	5428	9193	69	805	12	67 5
	19	3961	49	6039	4490	30	5510	9471	69	527	11	68 5
	20	4157	49	5843	4409	30	5591	9748	69	250	10	69 5
	21	4353	49	5647	4328	30	5672	810923	69	180	9	70 5
	22	4549	49	5451	4246	30	5754	0703	69	90	8	71 5
	23	4744	49	5255	4164	30	5835	0590	69	0	7	72 5
	24	4939	49	5059	4082	30	5916	0857	69	0	6	73 5
	25	5135	49	4863	4001	30	5997	1134	69	0	5	74 5
	26	5330	49	4667	3919	30	6078	1410	69	0	4	75 5
	27	5526	49	4471	3837	30	6159	1687	69	0	3	76 5
	28	5721	49	4275	3755	30	6240	1964	69	0	2	77 5
	29	5917	49	4079	3673	30	6321	2241	69	0	1	78 5
	30	9.734103	49	0.265897	9.924103	30	0.076409	9.812518	69	0.187432	0	49 0

90° 12'

1° - 4' 10" - 4"

57° 3'

2° 33°

1° = 15' 1" = 15' 1" = 15°

146°

Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
12	0	9.73610	48	0.26381	9.993591	90	0.07640	9.81251	64	0.18742	16	42
	4	6303	48	2897	350	90	6491	271.4	64	729	31	
	8	6494	48	3502	3427	90	6573	3071	60	692	26	
	12	6692	48	3906	3345	90	6655	3347	60	645	27	
	16	6891	48	3114	3263	90	6737	3623	60	6377	26	
	20	7080	48	2920	3181	91	6819	3899	60	6101	25	
	24	7274	48	2736	3099	90	6902	4176	60	5824	24	
	28	7468	48	2562	3011	91	6984	4452	60	5548	23	
	32	7661	48	2397	2933	90	7067	4729	60	5272	22	
	36	7855	48	2145	2851	91	7149	5004	60	4996	21	
	40	8048	48	1952	2768	90	7232	5280	60	4720	20	
	44	8241	48	1759	2686	91	7314	5555	60	4445	19	
	48	8434	48	1566	2603	90	7397	5831	60	4169	18	
	52	8627	48	1373	2520	91	7480	6107	60	3893	17	
	56	8820	48	1180	2436	91	7562	6382	60	3618	16	
13	0	9012	48	0787	2355	91	7645	6658	60	3342	15	47
	4	9101	48	0744	2272	91	7727	6934	60	3064	14	
	8	9194	48	0602	2189	91	7811	7207	60	2787	13	
	12	9270	48	0410	2106	91	7894	7484	60	2511	12	
	16	9353	48	0217	2023	91	7977	7760	60	2234	11	
	20	9475	48	0025	1940	91	8060	8035	60	1958	10	
	24	9617	48	29833	1857	91	8143	8310	60	1681	9	
	28	9735	48	0641	1774	91	8226	8585	60	1405	8	
	32	9822	48	0449	1691	91	8309	8860	60	1129	7	
	36	9942	48	0258	1607	91	8393	9135	60	853	6	
	40	95	48	9066	1524	91	8476	9410	60	576	5	
	44	1125	48	875	1441	91	8559	9684	60	301	4	
	48	97	48	8694	1357	91	8643	9957	60	24	3	
	52	150	48	8492	1274	91	8726	10234	60	17	2	
	56	1086	48	8302	1190	91	8810	10508	60	9	1	
14	0	1800	48	8110	1107	91	8893	10783	60	921	0	46
	4	9070	48	730	1023	91	8977	1057	60	846	0	
	8	9271	48	7729	933	91	9061	1338	60	866	0	
	12	9472	47	7538	856	91	9144	1106	60	8347	0	
	16	9652	47	7348	777	91	9228	1880	60	8190	0	
	20	9842	47	7158	698	91	9312	2154	60	7947	0	
	24	3033	47	6967	619	91	9396	2429	60	7571	0	
	28	3923	47	6777	540	91	9480	2703	60	72	0	
	32	3413	47	6587	461	91	9564	2977	60	702	0	
	36	3802	47	6398	382	91	9648	3250	60	6750	0	
	40	3792	47	6208	303	91	9732	3524	60	6477	0	
	44	3369	47	6018	224	91	9816	3798	60	6202	0	
	48	471	47	5829	145	91	9901	4072	60	5927	0	
	52	4361	47	5639	66	91	9985	4346	60	5651	0	
	56	4550	47	5450	91931	91	10069	4619	60	5374	0	
15	0	4739	47	5261	9846	91	0154	4893	60	5107	15	45
	4	4928	47	5072	9762	91	0238	5166	60	4834	14	
	8	5117	47	4883	9678	91	0323	5439	60	4561	13	
	12	5306	47	4694	9593	91	0407	5713	60	4287	12	
	16	5494	47	4506	9508	91	0492	5988	60	4014	11	
	20	5683	47	4317	9424	91	0576	6257	60	3741	10	
	24	5871	47	4127	9339	91	0661	6532	60	3467	9	
	28	6059	47	3941	9254	91	0746	6805	60	3193	8	
	32	6248	47	3752	9170	91	0830	7078	60	2919	7	
	36	6436	47	3564	9085	91	0915	7351	60	2644	6	
	40	6624	47	3376	9000	91	1000	7624	60	2370	5	
	44	6812	47	3187	8915	91	1085	7897	60	2107	4	
	48	6999	47	3001	8830	91	1170	8169	60	1831	3	
	52	7187	47	2814	8745	91	1255	8442	60	1557	2	
	56	7374	47	2628	8659	91	1341	8715	60	1282	1	
15	60	9747532	47	0.292138	9.918574	91	0.081436	9.829889	60	0.177012	0	45

133°

1° = 4' 10" = 4"

86°

TABLE II.—LOG. SINES, TANG'S, &c.

34°		1° - 15' 1° - 15' 1° - 15°						145°					
Hours.	Deg.	L. Sin.	Diff. for 15' or 1°	L. Cossec.	L. Cos.	Diff. for 15' or 1°	L. Sec.	L. Tang.	Diff. for 15' or 1°	L. Cot.	Deg.	Hours.	
16	0	9.747539	47	0.332438	9.918574	21	0.061426	9.922988	68	0.171012	60	42	00
	1	7749	47	8251	8489	21	1511	9260	68	0740	59		50
	2	7936	47	9034	8404	21	1530	9532	68	0468	58		52
	3	8123	47	1877	8318	21	1629	9805	68	0195	57		48
	4	8310	47	1600	8233	21	1767	930077	68	16923	56		44
	5	8497	46	1503	8148	21	1852	0349	68	9651	55		40
	6	8683	46	1317	8063	21	1938	0621	68	9379	54		36
	7	8870	46	1130	7977	21	2023	0893	68	9107	53		32
	8	9056	46	0944	7891	21	2109	1165	68	8835	52		28
	9	9243	46	0758	7805	21	2195	1437	68	8563	51		24
	10	9429	46	0571	7720	21	2280	1709	68	8291	50		20
	11	9615	46	0385	7634	21	2366	1981	68	8019	49		16
	12	9801	46	0199	7548	21	2452	2253	68	7747	48		12
	13	9987	46	0013	7462	21	2538	2525	68	7475	47		8
	14	750172	46	949282	7376	21	2624	2796	68	7204	46		4
17	0	0358	46	9649	7290	21	2710	3068	68	6932	45	43	0
	1	0543	46	9457	7204	21	2796	3339	68	6661	44		56
	2	0729	46	9271	7118	21	2882	3611	68	6389	43		52
	3	0914	46	9086	7032	21	2968	3882	68	6118	42		48
	4	1099	46	8901	6945	21	3055	4154	68	5846	41		44
	5	1284	46	8716	6859	21	3141	4425	68	5575	40		40
	6	1469	46	8531	6773	21	3227	4696	68	5304	39		36
	7	1654	46	8346	6687	21	3313	4967	68	5033	38		32
	8	1838	46	8161	6601	21	3400	5238	68	4762	37		28
	9	2023	46	7977	6514	21	3486	5509	68	4491	36		24
	10	2209	46	7793	6427	21	3573	5780	68	4220	35		20
	11	2394	46	7608	6341	21	3659	6051	68	3949	34		16
	12	2576	46	7424	6254	21	3746	6322	68	3678	33		12
	13	2760	46	7240	6167	21	3833	6593	68	3407	32		8
	14	2944	46	7056	6080	21	3920	6864	68	3136	31		4
18	0	3128	46	6872	5994	21	4006	7134	68	2866	30	43	0
	1	3313	46	6688	5907	21	4093	7405	68	2595	29		56
	2	3495	46	6505	5820	21	4180	7675	68	2325	28		52
	3	3679	46	6321	5733	21	4267	7946	68	2054	27		48
	4	3862	46	6138	5646	21	4354	8216	67	1784	26		44
	5	4046	46	5954	5559	21	4441	8487	67	1513	25		40
	6	4229	46	5771	5472	21	4528	8757	67	1243	24		36
	7	4412	46	5588	5385	21	4615	9027	67	0973	23		32
	8	4595	46	5405	5297	21	4703	9298	67	0702	22		28
	9	4778	46	5222	5210	21	4790	9568	67	0432	21		24
	10	4961	46	5039	5123	21	4877	9838	67	0162	20		20
	11	5143	46	4857	5035	21	4965	94010	67	15962	19		16
	12	5326	45	4674	4948	21	5052	0378	67	9622	18		12
	13	5509	45	4492	4860	21	5140	0348	67	9352	17		8
	14	5690	45	4310	4773	21	5227	0917	67	9083	16		4
19	0	5872	45	4128	4685	21	5315	1187	67	8813	15	41	0
	1	6054	45	3946	4597	21	5403	1457	67	8543	14		56
	2	6236	45	3764	4510	21	5490	1728	67	8274	13		52
	3	6418	45	3582	4423	21	5578	1998	67	8004	12		48
	4	6600	45	3400	4334	21	5666	2268	67	7734	11		44
	5	6781	45	3219	4246	21	5754	2535	67	7465	10		40
	6	6963	45	3037	4159	21	5843	2805	67	7195	9		36
	7	7144	45	2856	4070	21	5930	3074	67	6924	8		32
	8	7325	45	2675	3982	21	6018	3343	67	6657	7		28
	9	7507	45	2493	3894	21	6106	3613	67	6387	6		24
	10	7688	45	2312	3805	21	6194	3882	67	6118	5		20
	11	7869	45	2131	3718	21	6282	4151	67	5848	4		16
	12	8050	45	1950	3630	21	6370	4420	67	5579	3		12
	13	8230	45	1770	3541	21	6458	4689	67	5311	2		8
	14	8411	45	1589	3453	21	6547	4958	67	5042	1		4
19	0	9.753511	45	0.24140	9.913314	21	0.086636	9.945227	67	0.154773	0	40	0

34°

1° - 15' 1° - 15' 1° - 15°

145°

Hours.		Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
m	s	'										'	m	s
20	0	0	9.75851		0.24140	9.943304	22	0.086636	9.845227		0.154773	60	39	00
	4	1	8772	45	1.28	3270	22	6724	5490	67	450	59		56
	8	2	8952	45	1048	3188	22	6812	5764	67	4730	58		52
	12	3	9131	45	8668	3090	22	6901	6033	67	3967	57		48
	16	4	9319	45	8688	3010	22	6990	6302	67	3698	56		44
	20	5	9492	45	659	2921	22	7079	6571	67	3429	55		40
	24	6	9672	45	6428	2833	22	7167	6839	67	3161	54		36
	28	7	9852	45	6148	2744	22	7255	7108	67	2892	53		32
	32	8	760011	45	33969	2655	22	7343	7376	67	2624	52		28
	36	9	9241	45	9789	2566	22	7434	7645	67	2355	51		24
	40	10	9390	45	9610	2477	22	7523	7913	67	2087	50		20
	44	11	9539	45	9431	2388	22	7612	8181	67	1819	49		16
	48	12	9748	45	9252	2299	22	7701	8449	67	1551	48		12
	52	13	9827	45	9073	2210	22	7790	8717	67	1283	47		8
	56	14	1106	45	8894	2121	22	7879	8985	67	1015	46		4
21	0	15	1285	45	8715	2031	22	7969	9254	67	0747	45	39	00
	4	16	1464	45	8536	1942	22	8058	9522	67	0479	44		56
	8	17	1643	44	8357	1853	22	8147	9790	67	0210	43		52
	12	18	1821	44	8179	1763	22	8237	85058	67	14942	42		48
	16	19	1999	44	8001	1674	22	8326	9325	67	9675	41		44
	20	20	2177	44	7823	1584	22	8416	9593	67	9407	40		40
	24	21	2356	44	7644	1495	22	8505	9861	67	9139	39		36
	28	22	2534	44	7466	1405	22	8595	1129	67	8871	38		32
	32	23	2712	44	7288	1316	22	8684	1396	67	8604	37		28
	36	24	2890	44	7111	1226	22	8774	1664	67	8336	36		24
	40	25	3067	44	6933	1136	22	8864	1931	67	8069	35		20
	44	26	3245	44	6755	1046	22	8954	2199	67	7801	34		16
	48	27	3422	44	6578	956	22	9044	2466	67	7534	33		12
	52	28	3600	44	6400	866	22	9134	2734	67	7266	32		8
	56	29	3777	44	6223	776	22	9224	3001	67	6999	31		4
22	0	30	3954	44	6046	686	22	9314	3268	67	6732	30	38	00
	4	31	4131	44	5869	596	22	9404	3535	67	6465	29		56
	8	32	4308	44	5692	506	22	9494	3802	67	6198	28		52
	12	33	4485	44	5515	416	22	9584	4069	67	5931	27		48
	16	34	4662	44	5338	326	22	9674	4337	67	5663	26		44
	20	35	4839	44	5162	235	22	9765	4603	67	5397	25		40
	24	36	5015	44	4985	145	22	9855	4870	67	5130	24		36
	28	37	5191	44	4809	54	22	9946	5137	67	4863	23		32
	32	38	5367	44	4633	90	22	000037	5404	67	4596	22		28
	36	39	5544	44	4456	9873	23	0137	5671	67	4329	21		24
	40	40	5720	44	4280	9792	22	0218	5938	67	4062	20		20
	44	41	5896	44	4104	9692	22	0308	6204	67	3796	19		16
	48	42	6072	44	3928	9601	22	0399	6471	67	3529	18		12
	52	43	6247	44	3751	9500	22	0490	6737	67	3262	17		8
	56	44	6423	44	3577	9419	22	0581	7004	67	2996	16		4
23	0	45	6598	44	3402	9328	22	0672	7270	66	2730	15	37	00
	4	46	6774	44	3226	9237	22	0763	7537	66	2463	14		56
	8	47	6949	44	3051	9146	22	0854	7804	66	2197	13		52
	12	48	7124	44	2876	9055	22	0945	8071	66	1931	12		48
	16	49	7300	44	2700	8964	22	1036	8338	66	1664	11		44
	20	50	7475	44	2525	8873	22	1127	8602	66	1398	10		40
	24	51	7651	44	2351	8781	22	1218	8869	66	1132	9		36
	28	52	7824	44	2177	8690	22	1310	9134	66	866	8		32
	32	53	7999	44	2001	8599	22	1401	9400	66	600	7		28
	36	54	8173	44	1827	8507	22	1493	9666	66	334	6		24
	40	55	8348	44	1652	8415	22	1584	9932	66	68	5		20
	44	56	8522	43	1477	8323	22	1675	860124	66	1309	4		16
	48	57	8697	43	1301	8231	22	1767	9154	66	953	3		12
	52	58	8871	43	1124	8141	22	1859	9707	66	687	2		8
	56	59	9045	43	945	8049	22	1951	9960	66	421	1		4
24	00	60	9 76 9211		0 23 0721	9 90 7458		0 09 2012	9 85 1261		0 13 8733	0	35	00

TABLE II.—LOG. SINES, TANG'S, &c.

24 36°

1° - 15' 1" - 15' 1" - 15°

143° 0'

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cosc.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.		
24	0	0	9 70 219	43	0.320781	0.907138	23	0.093042	0.861261	66	0.13 739	0	30	60
	4	1	930.3	43	0.607	786.0	23	21.4	1527	66	8473	59		53
	8	2	956.6	43	0.434	7774	23	2.26	1792	66	8302	53		52
	12	3	9740	43	02.0	7622	23	2 1 8	2052	66	7942	57		43
	16	4	9913	43	0067	7500	23	2410	2323	66	7677	56		44
	20	5	.770087	43	.229913	7408	23	2502	2589	66	7411	55		40
	24	6	0260	43	9740	7406	23	2594	2554	66	7141	54		36
	28	7	0433	43	9567	7314	23	2686	3119	66	6821	53		32
	32	8	0606	43	9394	7221	23	2779	3385	66	6615	52		28
	36	9	0779	43	9221	7129	23	2871	3650	66	6350	51		24
	40	10	0952	43	9048	7037	23	2963	3915	66	6085	50		20
	44	11	1125	43	8875	6945	23	3055	4180	66	5820	49		16
	48	12	1297	43	8703	6852	23	3148	4445	66	5555	48		12
	52	13	1470	43	8530	6760	23	3240	4710	66	5290	47		8
	56	14	1643	43	8357	6667	23	3333	4975	66	5025	46		4
25	0	15	1815	43	8185	6575	23	3425	5240	66	4760	45	35	0
	4	16	1987	43	8013	6482	23	3517	5505	66	4495	44		56
	8	17	2159	43	7841	6389	23	3611	5770	66	4230	43		52
	12	18	2331	43	7669	6296	23	3704	6035	66	3965	42		48
	16	19	2503	43	7497	6203	23	3797	6300	66	3700	41		44
	20	20	2675	43	7325	6111	23	3889	6564	66	3435	40		40
	24	21	2847	43	7153	6018	23	3982	6829	66	3170	39		36
	28	22	3019	43	6981	5925	23	4075	7094	66	2905	38		32
	32	23	3190	43	6810	5832	23	4168	7359	66	2640	37		28
	36	24	3362	43	6638	5739	23	4261	7623	66	2375	36		24
	40	25	3534	43	6467	5646	23	4354	7887	66	2110	35		20
	44	26	3704	43	6296	5552	23	4447	8152	66	1845	34		16
	48	27	3875	43	6125	5459	23	4541	8416	66	1580	33		12
	52	28	4046	43	5954	5366	23	4634	8680	66	1315	32		8
	56	29	4217	43	5783	5272	23	4727	8945	66	1050	31		4
26	0	30	4388	43	5612	5179	23	4821	9209	66	0785	30	34	0
	4	31	4559	43	5442	5085	23	4915	9473	66	0520	29		56
	8	32	4729	43	5271	4992	23	5008	9737	66	0255	28		52
	12	33	4899	43	5101	4899	23	5102	870001	66	.12999	27		48
	16	34	5070	42	4930	4805	23	5195	0265	66	9735	26		44
	20	35	5240	42	4760	4711	23	5288	0529	66	9471	25		40
	24	36	5410	42	4590	4617	23	5383	0793	66	9207	24		36
	28	37	5580	42	4420	4523	23	5477	1057	66	8943	23		32
	32	38	5750	42	4250	4429	23	5571	1321	66	8679	22		28
	36	39	5920	42	4080	4335	23	5665	1585	66	8415	21		24
	40	40	6090	42	3910	4241	23	5759	1849	66	8151	20		20
	44	41	6259	42	3741	4147	23	5853	2112	66	7888	19		16
	48	42	6429	42	3571	4053	23	5947	2376	66	7624	18		12
	52	43	6598	42	3402	3959	23	6041	2639	66	7361	17		8
	56	44	6767	42	3233	3864	23	6136	2903	66	7097	16		4
27	0	45	6937	42	3063	3770	23	6230	3167	66	6833	15	33	0
	4	46	7106	42	2894	3675	23	6324	3430	66	6570	14		56
	8	47	7275	42	2725	3581	23	6419	3694	66	6306	13		52
	12	48	7444	42	2556	3487	23	6513	3957	66	6043	12		48
	16	49	7613	42	2387	3392	23	6608	4221	66	5779	11		44
	20	50	7782	42	2218	3298	24	6702	4484	66	5516	10		40
	24	51	7950	42	2050	3203	24	6797	4747	66	5253	9		36
	28	52	8119	42	1881	3107	24	6891	5010	66	4990	8		32
	32	53	8287	42	1713	3014	24	6986	5273	66	4727	7		28
	36	54	8455	42	1545	2919	24	7081	5536	66	4464	6		24
	40	55	8624	42	1376	2824	24	7176	5800	66	4200	5		20
	44	56	8792	42	1208	2729	24	7271	6063	66	3937	4		16
	48	57	8960	42	1040	2634	24	7366	6326	66	3673	3		12
	52	58	9128	42	872	2539	24	7461	6589	66	3411	2		8
	56	59	9295	42	705	2444	24	7556	6851	66	3149	1		4
27	0	0	9 779463	42	0.220537	0.902349	24	0.097651	0.877114	66	0.122286	0	32	0

84 136°

1° - 4' 10" - 4"

53° 3'

TABLE II.—LOG. SINES, TANG'S, &c.

28°		37°		1° - 15' 1° - 15' 1° - 15°		142°		9°					
Hours.	Deg.	L. Sin.	Diff. for 15' or 1°	L. Cossec.	L. Cos.	Diff. for 15' or 1°	L. Sec.	L. Tang.	Diff. for 15' or 1°	L. Cot.	Deg.	Hours.	
28	0 0	9.77463	42	0.92037	9.902349	94	0.09751	9.877114	66	0.12288	10	31	10
	4 1	9630	42	0370	2.53	94	7747	7377	66	2.2	10		56
	8 2	9708	42	0202	2158	94	7842	7640	66	230.0	10		58
	12 3	9666	42	0034	2063	94	7937	7503	66	20.7	10		57
	16 4	780133	42	91867	1967	94	8033	8160	66	1834	10		56
	20 5	0300	42	9700	1872	94	8128	8428	66	1572	10		56
	24 6	0467	42	9533	1776	94	8224	8691	66	130.	10		54
	28 7	0634	42	9366	1681	94	8319	8953	66	1047	10		53
	32 8	0801	42	9199	1585	94	8415	9210	66	0784	10		52
	36 9	0368	42	9032	1490	94	8510	9478	66	0522	10		51
	40 10	1135	42	8865	1394	94	8606	9741	65	0256	10		50
	44 11	1301	42	8699	1298	94	8702	980003	65	11997	10		49
	48 12	1467	42	8533	1.02	94	8798	02.5	66	9735	10		48
	52 13	1634	42	8366	1108	94	8894	0522	65	9472	10		47
	56 14	1800	41	8200	1010	94	8990	0750	65	9210	10		46
29	0 15	1966	41	8034	0914	94	9086	1052	65	8945	10	31	0
	4 16	2132	41	7868	0818	94	9182	1314	65	8680	10		56
	8 17	2298	41	7702	0722	94	9278	1576	65	8424	10		52
	12 14	2464	41	7536	0626	94	9374	1838	65	8162	10		48
	16 19	2630	41	7370	05.9	94	9471	2101	65	7900	10		44
	20 20	2796	41	7204	0433	94	9567	2363	65	7637	10		40
	24 21	2962	41	7038	0337	94	9663	2625	65	7375	10		36
	28 22	3127	41	6873	0240	94	9750	2887	65	7113	10		32
	32 23	3292	41	6708	0144	94	9846	3148	65	6852	10		28
	36 24	3457	41	6543	0047	94	9943	3410	65	65.0	10		24
	40 25	3623	41	6377	899051	94	10040	3672	65	6328	10		20
	44 26	3788	41	6212	8954	94	0146	3934	65	6066	10		16
	48 27	3953	41	6047	8917	94	0243	4196	65	5804	10		12
	52 28	4118	41	5882	8881	94	0339	4457	65	5543	10		8
	56 29	4283	41	5717	8844	94	0436	4719	65	5281	10		4
30	0 30	4447	41	5553	8807	94	0533	4980	65	5020	10	30	0
	4 31	4612	41	5388	8770	94	0630	5242	65	4758	10		56
	8 32	4776	41	5224	8733	94	0727	5503	65	4497	10		52
	12 33	4941	41	5059	8697	94	0824	5765	65	4235	10		48
	16 34	5105	41	4895	8660	94	0921	6026	65	3974	10		44
	20 35	5269	41	4731	8624	94	1019	6288	65	3712	10		40
	24 36	5433	41	4567	8588	94	1116	6549	65	3451	10		36
	28 37	5597	41	4403	8552	94	1213	6810	65	3190	10		32
	32 38	5761	41	4239	8516	94	1311	7072	65	2928	10		28
	36 39	5925	41	4075	8480	94	1408	7333	65	2667	10		24
	40 40	6089	41	3911	8445	94	1505	7594	65	2406	10		20
	44 41	6252	41	3748	8409	94	1603	7855	65	2145	10		16
	48 42	6416	41	3584	8374	94	1701	8117	65	1883	10		12
	52 43	6579	41	3421	8339	94	1799	8378	65	1622	10		8
	56 44	6743	41	3257	8304	94	1896	8639	65	1361	10		4
31	0 45	6906	41	3094	8269	94	1994	8900	65	1100	15	29	0
	4 46	7069	41	2931	8234	94	2092	9161	65	0839	14		56
	8 47	7232	41	2768	8199	94	2190	9422	65	0578	13		52
	12 48	7394	41	2606	8164	95	2288	9682	65	0318	11		48
	16 49	7557	41	2443	8129	94	2386	9943	65	0057	11		44
	20 50	7720	41	2280	8094	94	2484	990304	65	109796	10		40
	24 51	7883	41	2117	8059	95	2582	0465	65	9535	9		36
	28 52	8045	41	1955	8024	95	2680	0725	65	9275	8		32
	32 53	8208	40	1792	7989	95	2778	0986	65	9014	7		28
	36 54	8370	40	1630	7954	95	2877	1247	65	8753	6		24
	40 55	8532	40	1468	7919	94	2975	1507	65	8493	5		20
	44 56	8694	40	1306	8886	95	3074	1768	65	8232	4		16
	48 57	8857	40	1143	8851	95	3172	2029	65	7971	3		12
	52 58	9019	40	0982	8816	95	3271	2290	65	7711	2		8
	56 59	9180	40	0820	8781	95	3369	2551	65	7451	1		4
31	00 60	9342	40	0658	8746	95	0.103468	9.892810	65	0.107190	0	28	0

28° 120°

1° - 15' - 15°

9° 30°

TABLE II.—LOG. SINES, TANG'S, &c.

32° 30'		1° — 15' 1" — 15' 1" — 15°										141° 0'	
Hours.	Deg.	L. Sin.	Diff. for 15" or 1'	L. Cosec.	L. Cos.	Diff. for 15" or 1'	L. Sec.	L. Tang.	Diff. for 15" or 1'	L. Cot.	Deg.	Hours.	
32	0	0.789312	40	0.210658	0.909532	25	0.103466	0.892810	65	0.107190	60	27	60
	1	9533	40	0147	6433	25	3597	3070	65	6930	59		56
	2	9665	40	0335	6334	25	3366	3331	65	6669	58		52
	3	9827	40	0173	6236	25	3764	3531	65	6409	57		48
	4	9988	40	0012	6137	25	3803	3851	65	6149	56		44
	5	.790147	40	.203851	6038	25	3962	4111	65	5889	55		40
	6	0310	40	9890	5939	25	4061	4371	65	5629	54		36
	7	0472	40	9528	5840	25	4160	4639	65	5368	53		32
	8	0633	40	9347	5741	25	4259	4892	65	5108	52		28
	9	0793	40	9207	5642	25	4357	5152	65	4848	51		24
	10	0954	40	9046	5542	25	4458	5412	65	4588	50		20
	11	1115	40	8885	5443	25	4557	5672	65	4328	49		16
	12	1275	40	8725	5343	25	4657	5932	65	4068	48		12
	13	1436	40	8564	5244	25	4756	6192	65	3808	47		8
	14	1596	40	8404	5144	25	4856	6452	65	3548	46		4
33	0	1757	40	8243	5045	25	4955	6712	65	3288	45	27	0
	1	1917	40	8083	4945	25	5055	6972	65	3028	44		56
	2	2077	40	7923	4846	25	5154	7231	65	2769	43		52
	3	2237	40	7763	4746	25	5254	7491	65	2509	42		48
	4	2397	40	7603	4646	25	5354	7751	65	2249	41		44
	5	2557	40	7443	4546	25	5454	8011	65	1989	40		40
	6	2716	40	7284	4446	25	5554	8270	65	1730	39		36
	7	2876	40	7124	4346	25	5654	8530	65	1470	38		32
	8	3035	40	6965	4246	25	5754	8789	65	1211	37		28
	9	3195	40	6805	4146	25	5854	9049	65	0951	36		24
	10	3354	40	6646	4046	25	5954	9308	65	0692	35		20
	11	3514	40	6486	3946	25	6054	9568	65	0432	34		16
	12	3673	40	6327	3846	25	6154	9827	65	0173	33		12
	13	3832	40	6168	3745	25	6255	10087	65	0913	32		8
	14	3991	40	6009	3645	25	6355	10346	65	0654	31		4
34	0	4150	40	5850	3544	25	6456	10605	65	0395	30	26	0
	1	4309	40	5692	3444	25	6556	10864	65	0136	29		56
	2	4467	40	5533	3343	25	6657	11124	65	0877	28		52
	3	4626	40	5374	3243	25	6757	11383	65	0617	27		48
	4	4784	40	5216	3142	25	6858	11642	65	0358	26		44
	5	4942	39	5058	3041	25	6959	11901	65	0099	25		40
	6	5101	39	4899	2940	25	7060	12161	65	0840	24		36
	7	5259	39	4741	2839	25	7161	12420	65	0581	23		32
	8	5417	39	4583	2738	25	7262	12679	65	0322	22		28
	9	5575	39	4425	2637	25	7363	12938	65	0062	21		24
	10	5733	39	4267	2536	25	7464	13197	65	0803	20		20
	11	5891	39	4109	2435	25	7565	13456	65	0544	19		16
	12	6049	39	3951	2334	25	7666	13715	65	0285	18		12
	13	6206	39	3794	2233	25	7767	13973	65	0027	17		8
	14	6364	39	3636	2132	25	7868	14232	65	0768	16		4
35	0	6521	39	3479	2030	25	7970	14491	65	5509	15	25	0
	1	6679	39	3321	1929	25	8071	14750	65	5250	14		56
	2	6836	39	3164	1827	25	8173	15009	65	4991	13		52
	3	6993	39	3007	1726	25	8274	15267	65	4733	12		48
	4	7150	39	2850	1624	25	8376	15526	65	4474	11		44
	5	7307	39	2693	1523	25	8477	15784	64	4216	10		40
	6	7464	39	2536	1421	25	8579	16043	65	3957	9		36
	7	7621	39	2377	1319	25	8681	16302	65	3698	8		32
	8	7777	39	2220	1217	25	8783	16560	65	3440	7		28
	9	7934	39	2066	1115	25	8885	16819	65	3181	6		24
	10	8090	39	1910	1013	25	8987	17077	65	2923	5		20
	11	8247	39	1753	0911	25	9089	17336	65	2664	4		16
	12	8403	39	1597	0809	25	9191	17594	65	2407	3		12
	13	8559	39	1440	0707	25	9293	17853	65	2147	2		8
	14	8716	39	1284	0605	25	9395	18111	64	1889	1		4
	15	8872	39	1129	0503	25	9497	18369	65	1631	0	24	0

TABLE II.—LOG. SINES, TANG'S, &c.

30°		1° = 15' 1" = 15' 1" = 15°						140°		90°		
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
36	0	9.798872	38	0.20112	9.890503	26	0.109497	9.903369	65	0.091031	60	23
	4	9029	39	0.72	0400	25	9600	8628	64	1772	59	5
	8	9184	39	0816	0238	26	9702	8686	64	1114	58	5
	12	9333	39	0661	0195	25	9805	9144	64	0252	57	4
	16	9495	39	0505	0093	26	9907	9402	64	0390	56	4
	20	9651	39	0349	99991	25	110009	9660	64	0340	55	4
	24	9806	39	0194	9888	25	0112	9918	64	0082	54	3
	28	9962	39	0039	9785	26	0215	910177	64	99921	53	3
	32	900117	39	199683	9682	26	0318	0435	64	9565	52	2
	36	0272	39	9728	9579	26	0421	0693	64	9207	51	2
	40	0427	39	9573	9476	26	0524	0951	64	9049	50	2
	44	0582	39	9418	9373	26	0627	1309	64	8791	49	1
	48	0737	39	9263	9270	26	0730	1467	64	8533	48	1
	52	0892	39	9108	9167	26	0833	1725	64	8272	47	1
	56	1047	39	8953	9064	26	0936	1983	64	8017	46	1
37	0	1201	39	8799	8961	26	1030	2240	64	7760	45	23
	4	1356	39	8644	8858	26	1142	2498	64	7502	44	5
	8	1511	39	8489	8755	26	1245	2756	64	7244	43	5
	12	1665	39	8335	8651	26	1349	3014	64	6986	42	4
	16	1819	39	8181	8548	26	1452	3271	64	6729	41	4
	20	1973	39	8027	8444	26	1556	3529	64	6471	40	4
	24	2128	39	7872	8341	26	1659	3787	64	6213	39	3
	28	2282	39	7718	8237	26	1763	4045	64	5955	38	2
	32	2436	39	7564	8134	26	1866	4302	64	5697	37	2
	36	2590	39	7410	8030	26	1970	4560	64	5440	36	2
	40	2743	39	7257	7926	26	2074	4817	64	5183	35	2
	44	2897	39	7103	7822	26	2178	5075	64	4925	34	1
	48	3050	39	6950	7718	26	2282	5332	64	4667	33	1
	52	3204	39	6796	7614	26	2386	5590	64	4410	32	1
	56	3357	39	6643	7510	26	2490	5847	64	4153	31	1
38	0	3511	38	6489	7406	26	2594	6105	64	3905	30	23
	4	3664	38	6336	7302	26	2698	6362	64	3632	29	5
	8	3817	38	6183	7198	26	2802	6619	64	3361	28	5
	12	3970	38	6030	7093	26	2907	6877	64	3123	27	4
	16	4123	38	5877	6989	26	3011	7134	64	2866	26	4
	20	4276	38	5724	6885	26	3115	7391	64	2607	25	4
	24	4428	38	5572	6780	26	3220	7648	64	2352	24	3
	28	4581	38	5419	6676	26	3324	7905	64	2095	23	3
	32	4734	38	5266	6571	26	3429	8163	64	1837	22	2
	36	4886	38	5114	6466	26	3534	8420	64	1580	21	2
	40	5039	38	4961	6362	26	3638	8677	64	1323	20	2
	44	5191	38	4809	6257	26	3743	8934	64	1066	19	1
	48	5343	38	4657	6152	26	3848	9191	64	809	18	1
	52	5495	38	4505	6047	26	3953	9448	64	552	17	1
	56	5647	38	4353	5942	26	4058	9705	64	295	16	1
39	0	5799	38	4201	5837	26	4163	9962	64	0039	15	21
	4	5951	38	4049	5732	26	4268	920219	64	079781	14	5
	8	6103	39	3897	5627	26	4373	0476	64	9324	13	5
	12	6254	39	3746	5521	26	4479	0733	64	9867	12	4
	16	6406	39	3594	5416	26	4584	0990	64	9010	11	4
	20	6558	39	3442	5311	26	4689	1247	64	8753	10	4
	24	6707	39	3291	5206	26	4794	1503	64	8497	9	3
	28	6860	39	3140	5100	26	4900	1760	64	8240	8	2
	32	53	39	2988	4994	26	5006	9017	64	7983	7	2
	36	54	39	2837	4889	26	5111	2974	64	7726	6	2
	40	55	39	2686	4783	26	5217	2531	64	7469	5	2
	44	56	39	2535	4678	26	5322	2787	64	7213	4	1
	48	57	39	2384	4572	26	5428	3044	64	6957	3	1
	52	58	39	2234	4466	26	5534	3300	64	6700	2	1
	54	59	39	2083	4360	26	5640	3557	64	6443	1	1
	56	60	39	1932	4254	26	5746	3814	64	6186	0	20
Hours.	Deg.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Sin.	Diff. for 15' or 1"	L. Cossec.	L. Cot.	Diff. for 15' or 1"	L. Tang.	Deg.	Hours.

1300

1° = 4' 10" = 4"

500

TABLE II.—LOG. SINES, TANG'S, &c.

20 40°

F = 15' 1" = 15' 1" = 15°

130° 0'

Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cosec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
40	0	0.8030.8	37	0.191332	0.684954	96	0.115748	9.923814	64	0.076186	60	19
	4	8218	37	1762	4148	96	5552	4070	64	5930	5	0
	8	8369	37	1631	4042	93	5154	4327	64	5673	5	2
	12	8519	37	1481	3936	93	4664	4583	64	5417	5	4
	16	8669	37	1331	3829	93	4171	4840	64	4160	5	6
	20	8819	37	1181	3723	96	3677	5096	64	3904	5	8
	24	8969	37	1031	3617	97	3183	5352	64	3648	5	10
	28	9119	37	881	3510	97	2690	5609	64	3391	5	12
	32	9269	37	731	3404	97	2196	5865	64	3135	5	14
	36	9419	37	581	3297	97	1703	6122	64	2878	5	16
	40	9569	37	431	3191	97	1209	6378	64	2622	5	18
	44	9718	37	281	3084	97	716	6634	64	2365	5	20
	48	9868	37	131	2978	97	202	6890	64	2108	5	22
	52	10017	37	181	2871	97	712	7146	64	1852	5	24
	56	10167	37	933	2764	97	7326	7403	64	1597	5	26
41	0	0316	37	9684	2657	97	7343	765	64	2341	45	19
	4	0463	37	9535	2550	97	7450	7915	64	2085	44	0
	8	0614	37	9386	2443	97	7557	8171	64	1829	43	5
	12	0763	37	9237	2336	97	7664	8427	64	1573	42	10
	16	0912	37	9088	2229	97	7771	8683	64	1317	41	15
	20	1061	37	8939	2121	97	7879	8940	64	1060	40	20
	24	1210	37	8790	2014	97	7986	9196	64	804	39	25
	28	1358	37	8641	1907	97	8093	9451	64	548	38	30
	32	1507	37	8492	1800	97	8201	9708	64	292	37	35
	36	1656	37	8344	1692	97	8308	9964	64	36	36	40
	40	1804	37	8195	1584	97	8416	10220	64	110	35	45
	44	1952	37	8046	1477	97	8523	10475	64	8525	34	50
	48	2100	37	7897	1370	97	8631	10731	64	5969	33	55
	52	2248	37	7748	1262	97	8739	10987	64	3413	32	60
	56	2396	37	7600	1155	97	8847	11243	64	8757	31	65
42	0	2544	37	7451	1047	97	8955	11499	64	6201	30	18
	4	2692	37	7302	939	97	9063	11755	64	3645	29	23
	8	2840	37	7153	832	97	9170	12011	64	1089	28	28
	12	2988	37	7004	724	97	9278	12267	64	734	27	33
	16	3135	37	6855	617	97	9387	12522	64	478	26	38
	20	3283	37	6706	509	97	9495	12778	64	222	25	43
	24	3430	37	6557	402	97	9603	13033	64	66	24	48
	28	3578	37	6408	294	97	9711	13289	64	6711	23	53
	32	3725	37	6259	187	97	9820	13545	64	4155	22	58
	36	3873	37	6110	79	97	9928	13800	64	1599	21	63
	40	4019	37	5961	71	97	10037	14056	64	5044	20	68
	44	4166	37	5812	62	97	10145	14311	64	2488	19	73
	48	4313	37	5663	53	97	10254	14567	64	5133	18	78
	52	4460	37	5514	44	97	10363	14823	64	5177	17	83
	56	4607	37	5365	35	97	10471	15078	64	4923	16	88
43	0	4753	37	5216	26	97	10580	15333	64	4667	15	17
	4	4900	37	5067	17	97	10689	15589	64	4411	14	22
	8	5048	37	4918	8	97	10798	15844	64	4156	13	27
	12	5195	37	4769	0	97	10907	16100	64	3900	12	32
	16	5343	37	4620	-9	97	11016	16355	64	3645	11	37
	20	5490	37	4471	-18	97	11125	16610	64	3390	10	42
	24	5638	36	4322	-27	97	11234	16866	64	3134	9	47
	28	5785	36	4173	-36	97	11343	17121	64	2879	8	52
	32	5932	36	4024	-45	97	11452	17377	64	2623	7	57
	36	6079	36	3875	-54	97	11561	17632	64	2368	6	62
	40	6215	36	3726	-63	97	11670	17887	64	2113	5	67
	44	6361	36	3577	-72	97	11779	18142	64	1858	4	72
	48	6507	36	3428	-81	97	11888	18397	64	1602	3	77
	52	6653	36	3279	-90	97	11997	18653	64	1347	2	82
	56	6799	36	3130	-99	97	12106	18908	64	1092	1	87
43	0	6844	36	3081	-108	97	12215	19163	64	837	0	92
	4	6990	36	2932	-117	97	12324	19418	64	582	0	97

81 130°

1' = 4' 10" = 4"

40° 3'

131°

1° - 15' 1° - 15' 1° - 15'

132°

Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cos. ec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.
131	0	9.816943	36	0.183057	9.877780	27	0.122230	9.928163	64	0.066057	132	0
	1	7038	36	2912	7670	27	2330	9418	64	0523		15
	2	7233	36	2767	7560	27	2440	9673	64	0327		30
	3	7378	36	2622	7450	27	2550	9928	64	0072		45
	4	7534	36	2476	7340	27	2660	940184	64	059216		0
	5	7699	36	2331	7230	27	2770	0439	64	9561		15
	6	7813	36	2187	7120	27	2880	0683	64	9207		30
	7	7958	36	2042	7010	27	2990	0048	64	9052		45
	8	8103	36	1897	6899	28	3101	1904	64	8796		0
	9	8247	36	1753	6789	28	3211	1458	64	8549		15
	10	8392	36	1608	6678	28	3322	1714	64	8304		30
	11	8536	36	1464	6568	28	3432	1968	64	8062		45
	12	8681	36	1319	6458	28	3542	2223	64	7822		0
	13	8825	36	1175	6347	28	3653	2478	64	7584		15
	14	8969	36	1031	6236	28	3764	2733	64	7347		30
	15	9113	36	887	6125	28	3875	3088	64	7112		45
	16	9257	36	743	6014	28	3986	3243	64	6877		0
	17	9401	36	599	5904	28	4096	3497	64	6642		15
	18	9545	36	455	5793	28	4207	3752	64	6408		30
	19	9689	36	311	5682	28	4318	4007	64	6173		45
	20	9833	36	167	5571	28	4429	4262	64	5938		0
	21	9976	36	2	5459	28	4541	4517	64	5703		15
	22	820120	36	179880	5348	28	4652	4772	64	5468		30
	23	0263	36	9737	5237	28	4763	5027	64	5233		45
	24	0406	36	9594	5125	28	4875	5281	64	5000		0
	25	0550	36	8450	5014	28	4986	5536	64	4765		15
	26	0693	36	9307	4903	28	5097	5790	64	4530		30
	27	0836	36	9164	4791	28	5209	6045	64	4295		45
	28	0979	36	9021	4680	28	5320	6299	64	4060		0
	29	1122	36	8878	4568	28	5432	6554	64	3825		15
	30	1265	36	8735	4456	28	5544	6809	64	3590		30
	1	1407	36	8593	4344	28	5656	7063	64	3355		45
	2	1550	36	8450	4232	28	5768	7317	64	3120		0
	3	1693	36	8307	4121	28	5879	7572	64	2885		15
	4	1835	36	8165	4009	28	5991	7826	64	2650		30
	5	1978	35	8023	3897	28	6103	8081	64	2415		45
	6	2120	35	7880	3784	28	6216	8336	64	2180		0
	7	2262	35	7738	3672	28	6328	8590	64	1945		15
	8	2404	35	7596	3560	28	6440	8844	64	1710		30
	9	2546	35	7454	3447	28	6553	9099	64	1475		45
	10	2688	35	7312	3335	28	6665	9353	64	1240		0
	11	2830	35	7170	3223	28	6777	9607	63	1005		15
	12	2972	35	7028	3110	28	6890	9862	63	770		30
	13	3114	35	6886	2998	28	7002	950116	63	04204		45
	14	3256	35	6744	2885	28	7115	0371	63	0221		0
	15	3397	35	6603	2772	28	7228	0625	63	0375		15
	16	3538	35	6462	2659	28	7341	0879	63	0121		30
	17	3680	35	6320	2547	28	7453	1133	63	067		45
	18	3821	35	6179	2434	28	7566	1387	63	0613		0
	19	3963	35	6037	2321	28	7679	1642	63	0358		15
	20	4104	35	5896	2208	28	7792	1896	63	0104		30
	21	4245	35	5755	2095	28	7905	2150	63	759		45
	22	4386	35	5614	1981	28	8019	2405	63	7545		0
	23	4527	35	5473	1868	28	8132	2659	63	7341		15
	24	4668	35	5332	1755	28	8245	2913	63	7087		30
	25	4808	35	5192	1641	28	8359	3167	63	6833		45
	26	4949	35	5051	1528	28	8472	3421	63	6579		0
	27	5090	35	4910	1415	28	8585	3675	63	6325		15
	28	5230	35	4770	1301	28	8699	3929	63	6071		30
	29	5370	35	4630	1187	28	8813	4183	63	5817		45
	30	9.825511	35	0.174489	9.871074	28	0.128926	9.954437	63	0.065553	132	0

131°

1° - 4' 10' - 4"

132°

TABLE II.—LOG. SINES, TANG'S, &c.

130°		1° - 15' 1" - 15' 1" - 15°						137°		9°			
Hours.	Deg.	L. Sin.	Diff. for 15' or 1"	L. Cos.ec.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Tang.	Diff. for 15' or 1"	L. Cot.	Deg.	Hours.	
8	0	9.825511	35	0.174489	9.871074	28	0.128926	9.954437	63	0.045563	60	11	00
	1	3651	35	4349	0860	28	9040	4691	63	5309	59		56
	2	3791	35	4289	0846	28	9154	4945	63	5053	58		52
	3	3931	35	4069	0732	28	9268	5199	63	4801	57		48
	4	4072	35	3928	0618	28	9382	5454	63	4546	56		44
	5	6211	35	3789	0504	28	9496	5707	63	4293	55		40
	6	6351	35	3649	0390	28	9610	5961	63	4039	54		36
	7	6491	35	3509	0276	28	9724	6215	63	3785	53		32
	8	6630	35	3370	0161	28	9839	6469	63	3531	52		28
	9	6770	35	3230	0047	28	9953	6723	63	3277	51		24
	10	6910	35	3090	869933	29	130067	6977	63	3023	50		20
	11	7049	35	2951	9818	28	0182	7231	63	2769	49		16
	12	7189	35	2811	9704	28	0296	7485	63	2515	48		12
	13	7328	35	2672	9589	29	0411	7739	63	2261	47		8
	14	7467	35	2532	9474	28	0526	7993	63	2007	46		4
10	0	7606	35	2394	9360	29	0640	8246	63	1754	45	11	0
	1	7745	35	2255	9245	29	0755	8500	63	1500	44		56
	2	7884	35	2116	9130	29	0870	8754	63	1246	43		52
	3	8023	35	1977	9015	29	0985	9008	63	0992	42		48
	4	8162	35	1838	8900	29	1100	9262	63	0738	41		44
	5	8301	35	1699	8785	29	1215	9516	63	0484	40		40
	6	8439	35	1561	8670	29	1330	9769	63	0231	39		36
	7	8578	35	1422	8555	29	1445	060023	63	039077	38		32
	8	8716	35	1284	8439	29	1561	0277	63	0723	37		28
	9	8855	34	1145	8324	29	1676	0531	63	0469	36		24
	10	8993	34	1007	8209	29	1791	0784	63	0216	35		20
	11	9131	34	0869	8093	29	1907	1038	63	0062	34		16
	12	9269	34	0731	7978	29	2022	1291	63	0709	33		12
	13	9407	34	0593	7862	29	2138	1545	63	0455	32		8
	14	9546	34	0454	7747	29	2253	1799	63	0201	31		4
50	0	9683	34	0317	7631	29	2369	2054	63	0794	30	10	0
	1	9821	34	0179	7515	29	2485	2306	63	0709	29		56
	2	9959	34	0041	7399	29	2601	2559	63	0740	28		52
	3	830096	34	169904	7283	29	2717	2813	63	0787	27		48
	4	0234	34	9766	7167	29	2833	3067	63	0933	26		44
	5	0372	34	9628	7051	29	2949	3321	63	0679	25		40
	6	0509	34	9491	6935	29	3065	3574	63	0426	24		36
	7	0646	34	9354	6819	29	3181	3827	63	0173	23		32
	8	0784	34	9216	6703	29	3297	4081	63	0919	22		28
	9	0921	34	9079	6586	29	3414	4335	63	0665	21		24
	10	1058	34	8942	6470	29	3530	4588	63	0412	20		20
	11	1195	34	8805	6353	29	3647	4842	63	0158	19		16
	12	1332	34	8668	6237	29	3763	5095	63	0905	18		12
	13	1469	34	8531	6120	29	3880	5349	63	0651	17		8
	14	1606	34	8394	6004	29	3996	5602	63	0398	16		4
51	0	1742	34	8258	5887	29	4113	5855	63	0145	15	9	0
	1	1879	34	8121	5770	29	4230	6109	63	0389	14		56
	2	2015	34	7985	5653	29	4347	6362	63	0363	13		52
	3	2152	34	7848	5536	29	4464	6616	63	0338	12		48
	4	2288	34	7712	5419	29	4581	6869	63	0313	11		44
	5	2425	34	7575	5302	29	4698	7123	63	0287	10		40
	6	2561	34	7439	5185	29	4815	7376	63	0262	9		36
	7	2697	34	7303	5068	29	4932	7629	63	0237	8		32
	8	2833	34	7167	4950	29	5050	7883	63	0212	7		28
	9	2969	34	7031	4833	29	5167	8136	63	0186	6		24
	10	3105	34	6895	4716	29	5284	8389	63	0161	5		20
	11	3241	34	6759	4598	29	5402	8643	63	0135	4		16
	12	3377	34	6623	4481	29	5519	8896	63	0110	3		12
	13	3513	34	6488	4363	29	5637	9149	63	0085	2		8
	14	3648	34	6352	4245	29	5755	9403	63	0059	1		4
	15	3783	34	6217	4127	29	5873	9656	63	0034	0	8	0
51	0	9.833723		0.160217	9.864127		0.135873	9.969655		0.030344			
Hours.	Deg.	L. Cos.	Diff. for 15' or 1"	L. Sec.	L. Sin.	Diff. for 15' or 1"	L. Cos.ec.	L. Cot.	Diff. for 15' or 1"	L. Tang.	Deg.	Hours.	

Hours.	Deg.	L. Sin.	Diff. for 15'' or 1'	L. Cossec.	L. Cos.	Diff. for 15'' or 1'	L. Sec.	L. Tang.	Diff. for 15'' or 1'	L. Cot.	Deg.	Hours.
52	0 0	9.833783		0.166217	9.864127		0.133573	9.969656		0.030344	60	7
	4 1	3919	34	6081	4010	29	5090	9909	63	0091	59	
	8 2	4054	34	5946	3892	29	6108	970162	63	028638	58	
	12 3	4190	34	5810	3774	29	6220	0416	63	9584	57	
	16 4	4325	34	5675	3656	29	6344	0069	63	9331	56	
	20 5	4460	34	5540	3538	30	6462	0022	63	9078	55	
	24 6	4595	34	5405	3419	30	6581	1177	63	8824	54	
	28 7	4730	34	5270	3301	29	6699	1429	63	8571	53	
	32 8	4865	34	5135	3183	29	6817	1682	63	8318	52	
	36 9	4999	34	5001	3064	29	6936	1935	63	8065	51	
	40 10	5134	34	4866	2946	30	7054	2188	63	7812	50	
	44 11	5269	34	4731	2828	30	7172	2441	63	7559	49	
	48 12	5403	34	4597	2709	30	7291	2694	63	7306	48	
	52 13	5538	34	4462	2590	30	7410	2948	63	7052	47	
	56 14	5672	34	4328	2471	30	7529	3201	63	6799	46	
53	0 15	5807	33	4193	2353	30	7647	3454	63	6546	45	7
	4 16	5941	33	4059	2234	30	7766	3707	63	6293	44	
	8 17	6075	33	3925	2115	30	7885	3960	63	6040	43	
	12 18	6209	33	3791	1996	30	8004	4213	63	5787	42	
	16 19	6343	33	3657	1877	30	8123	4466	63	5534	41	
	20 20	6477	33	3523	1758	30	8242	4719	63	5281	40	
	24 21	6611	33	3389	1638	30	8362	4973	63	5027	39	
	28 22	6745	33	3255	1519	30	8481	5226	63	4774	38	
	32 23	6879	33	3121	1400	30	8600	5479	63	4521	37	
	36 24	7012	33	2988	1280	30	8720	5732	63	4268	36	
	40 25	7146	33	2854	1161	30	8839	5985	63	4015	35	
	44 26	7279	33	2721	1041	30	8959	6238	63	3762	34	
	48 27	7413	33	2587	922	30	9078	6491	63	3509	33	
	52 28	7546	33	2454	802	30	9198	6744	63	3256	32	
	56 29	7679	33	2321	682	30	9318	6997	63	3003	31	
54	0 30	7812	33	2188	562	30	9438	7250	63	2750	30	6
	4 31	7945	33	2055	442	30	9558	7503	63	2497	29	
	8 32	8078	33	1922	322	30	9678	7756	63	2244	28	
	12 33	8211	33	1789	202	30	9798	8009	63	1991	27	
	16 34	8344	33	1656	82	30	9918	8262	63	1738	26	
	20 35	8477	33	1523	85962	30	140038	8515	63	1485	25	
	24 36	8610	33	1390	9842	30	0158	8768	63	1232	24	
	28 37	8742	33	1258	9721	30	0279	9021	63	0979	23	
	32 38	8875	33	1125	9601	30	0399	9274	63	0726	22	
	36 39	9007	33	0993	9480	30	0520	9527	63	0473	21	
	40 40	9140	33	0860	9360	30	0640	9780	63	0220	20	
	44 41	9272	33	0728	9239	30	0761	98033	63	01967	19	
	48 42	9404	33	0596	9118	30	0882	0286	63	9714	18	
	52 43	9537	33	0464	8998	30	1002	0538	63	9462	17	
	56 44	9668	33	0332	8877	30	1123	0791	63	9209	16	
55	0 45	9800	33	0200	8756	30	1244	1044	63	8956	15	5
	4 46	9932	33	0068	8635	30	1365	1297	63	8703	14	
	8 47	840064	31	859936	8514	30	1486	1550	63	8450	13	
	12 48	0196	31	9804	8393	30	1607	1803	63	8197	12	
	16 49	0328	33	9672	8272	30	1728	2056	63	7944	11	
	20 50	0459	33	9541	8150	30	1850	2309	63	7691	10	
	24 51	0591	33	9409	8029	30	1971	2562	63	7438	9	
	28 52	0722	33	9278	7908	30	2092	2814	63	7186	8	
	32 53	0853	33	9147	7786	30	2214	3067	63	6933	7	
	36 54	0985	33	9015	7665	30	2335	3320	63	6680	6	
	40 55	1116	33	8884	7543	30	2457	3573	63	6427	5	
	44 56	1247	33	8753	7421	30	2579	3826	63	6174	4	
	48 57	1379	33	8621	7300	30	2700	4079	63	5921	3	
	52 58	1510	33	8490	7178	30	2822	4332	63	5668	2	
	56 59	1640	33	8360	7056	30	2944	4584	63	5415	1	
55	0 60	9.841771		0.158229	9.856934		0.143066	9.984837		0.015163	0	4

TABLE III.

PROPORTIONAL LOGARITHMS.

TABLE III.—PROPORTIONAL LOGARITHMS.

"	0° 0'	0° 1'	0° 2'	0° 3'	0° 4'	0° 5'	0° 6'	0° 7'	0° 8'	"
0		2.2553	1.9542	1.7782	1.6332	1.5583	1.4771	1.4102	1.3522	0
1	4.0334	.3481	.9506	.7757	.6514	.5549	.4759	.4091	.3513	1
2	8.7394	.2410	.9471	.7734	.6496	.5534	.4747	.4081	.3504	2
3	.5863	.2341	.9435	.7710	.6478	.5520	.4735	.4071	.3493	3
4	.4214	.2272	.9400	.7686	.6460	.5506	.4723	.4061	.3486	4
5	.2345	.2205	.9365	.7663	.6443	.5491	.4711	.4050	.3477	5
6	.5533	.2139	.9331	.7639	.6425	.5477	.4699	.4040	.3468	6
7	.1883	.2073	.9296	.7616	.6407	.5463	.4688	.4030	.3459	7
8	.1303	.2009	.9262	.7593	.6390	.5449	.4676	.4020	.3450	8
9	.0792	.1946	.9228	.7570	.6372	.5435	.4664	.4010	.3441	9
10	.0334	.1883	.9195	.7547	.6355	.5421	.4652	.4000	.3432	10
11	2.9920	.1822	.9162	.7524	.6338	.5407	.4640	.3989	.3423	11
12	.9542	.1761	.9128	.7501	.6320	.5393	.4628	.3979	.3415	12
13	.9195	.1701	.9096	.7479	.6303	.5379	.4617	.3969	.3406	13
14	.8873	.1642	.9063	.7456	.6286	.5365	.4606	.3959	.3397	14
15	.8573	.1584	.9031	.7434	.6269	.5351	.4594	.3949	.3388	15
16	.8293	.1526	.8999	.7412	.6252	.5337	.4582	.3939	.3379	16
17	.8030	.1469	.8967	.7390	.6235	.5324	.4571	.3929	.3371	17
18	.7782	.1413	.8935	.7368	.6218	.5310	.4559	.3919	.3362	18
19	.7547	.1358	.8904	.7346	.6201	.5296	.4548	.3910	.3353	19
20	.7324	.1303	.8873	.7324	.6185	.5283	.4536	.3900	.3345	20
21	.7112	.1249	.8842	.7302	.6168	.5269	.4525	.3890	.3336	21
22	.6910	.1196	.8811	.7281	.6151	.5256	.4514	.3880	.3327	22
23	.6717	.1143	.8781	.7259	.6135	.5242	.4502	.3870	.3319	23
24	.6532	.1091	.8751	.7238	.6118	.5228	.4491	.3860	.3310	24
25	.6355	.1040	.8721	.7217	.6102	.5215	.4480	.3851	.3302	25
26	.6185	.0989	.8691	.7196	.6085	.5202	.4468	.3841	.3293	26
27	.6021	.0939	.8661	.7175	.6069	.5189	.4457	.3831	.3284	27
28	.5863	.0889	.8632	.7154	.6053	.5174	.4446	.3821	.3276	28
29	.5710	.0840	.8602	.7133	.6037	.5162	.4435	.3812	.3267	29
30	.5563	.0792	.8573	.7112	.6021	.5149	.4424	.3802	.3259	30
31	.5421	.0744	.8544	.7091	.6005	.5136	.4412	.3792	.3250	31
32	.5283	.0696	.8516	.7071	.5989	.5123	.4401	.3782	.3242	32
33	.5149	.0649	.8487	.7050	.5973	.5110	.4390	.3773	.3233	33
34	.5019	.0603	.8459	.7030	.5957	.5097	.4379	.3764	.3225	34
35	.4894	.0557	.8431	.7010	.5941	.5084	.4368	.3754	.3216	35
36	.4771	.0512	.8403	.6990	.5925	.5071	.4357	.3745	.3208	36
37	.4652	.0467	.8375	.6970	.5909	.5058	.4346	.3735	.3199	37
38	.4536	.0423	.8348	.6950	.5894	.5045	.4335	.3726	.3191	38
39	.4424	.0378	.8320	.6930	.5878	.5032	.4325	.3716	.3183	39
40	.4314	.0334	.8293	.6910	.5863	.5019	.4314	.3707	.3174	40
41	.4206	.0291	.8266	.6890	.5847	.5006	.4303	.3697	.3166	41
42	.4102	.0248	.8239	.6871	.5832	.4994	.4292	.3688	.3158	42
43	.4000	.0206	.8212	.6851	.5816	.4981	.4281	.3678	.3149	43
44	.3900	.0164	.8186	.6832	.5801	.4968	.4270	.3669	.3141	44
45	.3802	.0122	.8159	.6812	.5786	.4956	.4260	.3660	.3133	45
46	.3707	.0081	.8133	.6793	.5771	.4943	.4249	.3650	.3124	46
47	.3613	.0040	.8107	.6774	.5755	.4931	.4238	.3641	.3116	47
48	.3522	.0000	.8081	.6755	.5740	.4918	.4228	.3632	.3108	48
49	.3432	1.9860	.8055	.6736	.5725	.4906	.4217	.3623	.3100	49
50	.3345	.9920	.8030	.6717	.5710	.4894	.4206	.3613	.3091	50
51	.3259	.9881	.8004	.6698	.5695	.4881	.4196	.3604	.3083	51
52	.3174	.9842	.7979	.6679	.5680	.4868	.4185	.3595	.3075	52
53	.3091	.9803	.7954	.6661	.5666	.4856	.4175	.3586	.3067	53
54	.3010	.9765	.7929	.6642	.5651	.4844	.4164	.3576	.3059	54
55	.2931	.9727	.7904	.6624	.5636	.4832	.4154	.3567	.3051	55
56	.2852	.9690	.7879	.6605	.5621	.4820	.4143	.3558	.3043	56
57	.2775	.9652	.7855	.6587	.5607	.4808	.4133	.3549	.3034	57
58	.2700	.9615	.7830	.6568	.5592	.4795	.4122	.3540	.3026	58
59	2.2626	1.9579	.7806	.6550	.5578	.4783	.4112	.3531	.3018	59

TABLE III.—PROPORTIONAL LOGARITHMS.

"	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	"
"	00 9'	00 10'	00 11'	00 12'	00 13'	00 14'	00 15'	00 16'	00 17'	"	"
0	1.3010	1.3053	1.3139	1.1761	1.1413	1.1091	1.0792	1.0512	1.0249	0	0
1	.02	.45	.32	.55	.08	.86	.87	.07	.44	1	1
2	.9934	.38	.96	.49	.02	.81	.82	.02	.40	2	2
3	.86	.31	.19	.43	.1297	.76	.77	.0498	.35	3	3
4	.78	.24	.13	.37	.91	.71	.73	.93	.31	4	4
5	.70	.17	.06	.31	.86	.66	.68	.89	.27	5	5
6	.62	.10	.9090	.25	.80	.61	.63	.84	.23	6	6
7	.54	.02	.93	.19	.74	.55	.58	.60	.19	7	7
8	.46	.9495	.86	.13	.69	.50	.53	.75	.14	8	8
9	.30	.88	.80	.07	.63	.45	.49	.71	.10	9	9
10	.31	.81	.73	.01	.58	.40	.44	.67	.06	10	10
11	.23	.74	.67	.1695	.52	.35	.39	.62	.02	11	11
12	.15	.67	.61	.89	.47	.30	.34	.56	.0197	12	12
13	.07	.60	.54	.83	.42	.25	.30	.53	.93	13	13
14	.9899	.53	.48	.77	.36	.20	.25	.49	.86	14	14
15	.91	.45	.41	.71	.31	.15	.20	.44	.85	15	15
16	.82	.38	.35	.65	.25	.09	.15	.40	.81	16	16
17	.76	.31	.28	.60	.20	.04	.11	.35	.76	17	17
18	.68	.24	.22	.54	.14	.0999	.06	.31	.72	18	18
19	.60	.17	.16	.48	.09	.94	.01	.26	.68	19	19
20	.52	.10	.09	.42	.03	.89	.0696	.22	.64	20	20
21	.45	.03	.03	.36	.1296	.84	.92	.18	.60	21	21
22	.37	.9396	.1996	.30	.92	.79	.87	.13	.56	22	22
23	.29	.89	.90	.24	.87	.74	.82	.09	.51	23	23
24	.21	.82	.84	.19	.82	.68	.78	.04	.47	24	24
25	.14	.75	.77	.13	.76	.64	.73	.00	.43	25	25
26	.06	.68	.71	.07	.71	.59	.68	.0398	.39	26	26
27	.9796	.62	.65	.01	.66	.54	.63	.91	.35	27	27
28	.91	.55	.58	.1595	.60	.49	.59	.87	.31	28	28
29	.83	.48	.52	.89	.55	.44	.54	.82	.26	29	29
30	.75	.41	.46	.84	.49	.39	.49	.78	.22	30	30
31	.68	.34	.39	.78	.44	.34	.45	.74	.18	31	31
32	.60	.27	.33	.72	.39	.29	.40	.69	.14	32	32
33	.53	.20	.27	.66	.33	.24	.35	.65	.10	33	33
34	.45	.13	.21	.61	.28	.19	.31	.60	.06	34	34
35	.38	.07	.14	.55	.23	.14	.26	.56	.03	35	35
36	.30	.00	.08	.49	.17	.09	.21	.52	.0036	36	36
37	.22	.9293	.02	.43	.12	.04	.17	.47	.93	37	37
38	.15	.86	.1696	.38	.07	.0899	.12	.43	.89	38	38
39	.07	.79	.80	.32	.01	.94	.06	.39	.85	39	39
40	.00	.72	.83	.26	.1196	.89	.03	.34	.81	40	40
41	.9692	.66	.77	.20	.91	.84	.9398	.30	.77	41	41
42	.85	.59	.71	.15	.86	.80	.94	.26	.73	42	42
43	.78	.52	.65	.09	.80	.75	.89	.21	.69	43	43
44	.70	.45	.59	.03	.75	.70	.85	.17	.65	44	44
45	.63	.39	.52	.1496	.70	.65	.80	.13	.61	45	45
46	.55	.32	.46	.92	.64	.60	.75	.08	.57	46	46
47	.48	.25	.40	.86	.59	.55	.71	.04	.53	47	47
48	.40	.18	.34	.81	.54	.50	.66	.00	.49	48	48
49	.33	.12	.28	.75	.49	.45	.62	.0295	.44	49	49
50	.26	.05	.22	.69	.43	.40	.57	.91	.40	50	50
51	.18	.9198	.16	.64	.38	.35	.52	.87	.36	51	51
52	.11	.99	.09	.58	.33	.31	.46	.82	.32	52	52
53	.04	.85	.03	.52	.28	.26	.43	.78	.28	53	53
54	.9596	.78	.1797	.47	.23	.21	.39	.74	.24	54	54
55	.89	.72	.91	.41	.17	.16	.34	.70	.20	55	55
56	.82	.65	.85	.36	.12	.11	.30	.65	.16	56	56
57	.74	.59	.79	.30	.07	.06	.25	.61	.12	57	57
58	.67	.52	.73	.24	.02	.01	.21	.57	.08	58	58
59	.60	.45	.67	.19	.1097	.0797	.16	.52	.04	59	59
"	00 9'	00 10'	00 11'	00 12'	00 13'	00 14'	00 15'	00 16'	00 17'	"	"
"	h =	h =	h =	h =	h =	h =	h =	h =	h =	"	"

"	00 18'	00 19'	00 20'	00 21'	00 22'	00 23'	00 24'	00 25'	00 26'	00 27'	00 28'	00 29'	"
"	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	"
0	10000	9765	9542	9331	9128	8935	8751	8573	8408	8250	8091	7939	0
1	9906	61	39	27	25	32	48	70	90	36	79	28	1
2	92	58	35	24	22	29	45	68	83	97	34	76	2
3	88	54	32	20	19	26	42	65	81	95	31	73	3
4	84	50	28	17	15	23	39	62	78	92	28	71	4
5	80	46	24	13	12	20	36	59	80	96	26	68	5
6	76	42	21	10	09	17	33	56	86	93	23	66	6
7	72	39	17	06	06	13	30	53	84	90	20	63	7
8	68	35	14	03	02	10	27	50	81	87	18	61	8
9	64	31	10	00	00	07	24	47	78	84	15	58	9
10	60	27	06	9706	96	04	21	44	75	82	12	55	10
11	56	23	03	93	92	01	18	42	72	80	10	53	11
12	52	20	00	89	89	00	15	39	70	77	07	50	12
13	48	16	96	86	86	95	12	36	67	04	48	48	13
14	44	12	92	83	83	92	09	33	64	02	45	45	14
15	40	08	88	79	79	88	06	30	61	5199	43	41	15
16	36	05	85	76	76	85	03	27	59	96	40	39	16
17	32	01	81	72	72	82	00	24	56	94	37	37	17
18	28	98	78	69	70	79	98	22	53	91	35	34	18
19	24	93	74	66	66	76	94	19	50	88	32	32	19
20	20	90	71	63	63	73	91	16	48	86	30	29	20
21	16	86	67	59	60	70	88	13	45	83	27	27	21
22	12	82	64	55	57	67	85	10	42	81	25	24	22
23	08	78	60	52	53	64	82	07	39	78	22	22	23
24	05	75	56	49	50	61	79	04	37	75	20	20	24
25	01	71	53	45	47	57	76	02	34	73	17	17	25
26	98	67	49	42	44	54	73	9499	31	70	14	14	26
27	93	64	46	39	41	51	70	96	28	67	12	12	27
28	89	60	43	35	37	48	67	93	26	65	09	09	28
29	85	56	39	32	34	45	64	90	23	62	07	07	29
30	81	52	35	28	31	42	61	87	20	59	04	04	30
31	77	49	32	25	28	39	58	84	18	57	02	02	31
32	73	45	28	22	24	36	55	82	15	54	7999	50	32
33	69	41	25	18	21	33	52	79	12	52	97	47	33
34	65	38	21	15	18	30	49	76	09	49	94	45	34
35	61	34	18	12	15	27	46	73	07	46	92	42	35
36	58	30	14	08	12	24	43	70	04	44	89	40	36
37	54	26	11	05	08	21	40	67	01	41	87	37	37
38	50	23	07	01	05	17	37	65	9898	38	84	35	38
39	46	19	04	9198	02	14	35	62	96	36	81	32	39
40	42	15	00	8899	11	32	59	59	93	33	79	30	40
41	38	12	9397	91	96	08	29	56	90	31	76	28	41
42	34	08	93	88	92	05	26	53	88	28	74	25	42
43	30	04	90	85	89	02	23	51	85	25	71	23	43
44	27	01	86	81	86	9799	20	48	82	23	69	20	44
45	23	9897	83	78	23	96	17	45	79	20	66	18	45
46	19	93	79	75	20	93	14	42	77	17	64	15	46
47	15	90	76	71	17	90	11	39	74	15	61	13	47
48	11	86	72	68	14	87	08	37	71	13	59	10	48
49	07	82	68	65	10	84	05	34	69	10	56	08	49
50	03	79	65	62	07	81	02	31	66	07	54	06	50
51	00	75	62	58	04	78	9899	28	63	04	51	03	51
52	9796	71	59	55	01	75	97	25	61	02	49	01	52
53	92	68	55	52	98	72	94	22	58	9999	46	9798	53
54	88	64	51	48	94	69	91	20	55	97	44	96	54
55	84	61	48	45	91	66	88	17	53	94	41	94	55
56	80	57	44	42	88	63	85	14	50	91	39	91	56
57	77	53	41	38	85	60	82	11	47	89	36	89	57
58	73	50	37	35	82	57	79	09	44	86	34	86	58
59	69	46	34	32	80	54	76	06	42	84	31	84	59
"	00 18'	00 19'	00 20'	00 21'	00 22'	00 23'	00 24'	00 25'	00 26'	00 27'	00 28'	00 29'	"
"	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	"

TABLE III.—PROPORTIONAL LOGARITHMS.

"	00 30'	00 31'	00 32'	00 33'	00 34'	00 35'	00 36'	00 37'	00 38'	00 39'	00 40'	00 41'	"
0	7793	7639	7501	7368	7238	7112	6990	6871	6755	6642	6532	6425	0
1	79	37	7499	65	36	10	96	69	53	40	30	23	1
2	77	34	97	63	34	08	86	67	51	38	29	21	2
3	74	32	94	61	32	06	84	65	49	37	27	20	3
4	73	30	92	59	29	04	82	63	47	35	25	18	4
5	69	27	90	57	27	02	80	61	45	33	23	16	5
6	67	25	88	54	25	00	78	59	43	31	21	14	6
7	65	23	85	52	23	7098	76	57	42	29	19	13	7
8	63	20	83	50	21	96	74	55	40	27	18	11	8
9	60	18	81	48	19	93	72	53	38	25	16	09	9
10	57	16	79	46	17	91	70	51	36	24	14	07	10
11	55	13	76	44	15	89	68	49	34	22	13	05	11
12	53	11	74	41	13	87	66	47	32	20	10	04	12
13	50	09	72	39	10	85	64	45	30	18	09	02	13
14	48	07	70	37	08	83	62	43	28	16	07	00	14
15	45	04	67	35	06	81	60	42	26	14	05	6398	15
16	43	02	65	33	04	79	58	40	25	12	03	97	16
17	41	00	63	30	02	77	56	38	23	11	01	95	17
18	38	7597	61	28	00	75	54	36	21	09	00	93	18
19	36	95	58	26	7196	73	52	34	19	07	6496	91	19
20	34	93	56	24	66	71	50	32	17	05	66	90	20
21	31	90	54	22	63	69	48	30	15	03	64	88	21
22	29	88	52	20	60	67	46	28	13	01	62	86	22
23	26	86	50	17	58	65	44	26	11	00	61	84	23
24	24	83	47	15	57	63	42	24	09	6598	59	83	24
25	22	81	45	13	55	61	40	22	08	66	57	81	25
26	19	79	43	11	53	59	38	20	06	64	55	79	26
27	17	77	41	09	51	57	36	18	04	62	54	77	27
28	14	74	38	07	49	55	34	16	02	60	52	75	28
29	12	72	36	04	47	53	32	14	00	58	50	74	29
30	10	70	34	02	45	50	30	12	6698	57	48	72	30
31	07	67	32	00	43	48	28	11	66	55	46	71	31
32	05	65	29	7398	40	46	26	09	64	53	45	69	32
33	03	63	27	96	38	44	24	07	62	51	43	67	33
34	00	60	25	94	36	42	22	05	61	49	41	65	34
35	7698	58	23	91	34	40	20	03	59	48	39	64	35
36	96	56	21	89	32	38	18	01	57	46	37	62	36
37	93	54	18	87	30	36	16	6799	55	44	35	60	37
38	91	51	16	85	28	34	14	97	53	42	34	58	38
39	88	49	14	83	26	32	12	95	51	40	32	57	39
40	86	47	12	81	24	30	10	93	49	38	30	55	40
41	84	44	09	79	22	28	08	91	47	36	28	53	41
42	81	42	07	76	20	26	06	89	45	34	26	51	42
43	79	40	05	74	17	24	04	87	43	32	24	49	43
44	77	38	03	72	15	22	02	85	41	30	22	47	44
45	74	35	01	70	13	20	00	84	39	28	20	45	45
46	72	33	7398	68	11	18	6898	82	37	26	18	44	46
47	70	31	96	66	09	16	96	80	35	24	16	42	47
48	67	28	94	64	07	14	94	78	33	22	14	41	48
49	65	26	92	61	05	12	92	76	31	20	12	39	49
50	63	24	90	59	03	10	90	74	29	18	10	38	50
51	60	22	87	57	01	08	88	72	27	16	08	36	51
52	58	20	85	55	99	06	86	70	25	14	06	34	52
53	55	17	83	53	97	04	84	68	23	12	04	32	53
54	53	15	81	51	94	02	83	66	21	10	02	31	54
55	51	13	79	49	92	00	81	64	19	08	00	29	55
56	48	10	76	46	90	6998	79	63	17	06	34	27	56
57	46	08	74	44	88	06	77	61	15	04	32	25	57
58	44	06	72	42	86	04	75	59	13	02	30	23	58
59	41	03	70	40	84	02	73	57	11	00	28	21	59
"	00 30'	00 31'	00 32'	00 33'	00 34'	00 35'	00 36'	00 37'	00 38'	00 39'	00 40'	00 41'	"

TABLE III.—PROPORTIONAL LOGARITHMS.

"	0° 42'	0° 43'	0° 44'	0° 45'	0° 46'	0° 47'	0° 48'	0° 49'	0° 50'	0° 51'	0° 52'	0° 53'	"
0	6320	6318	6118	6021	5925	5832	5740	5651	5563	5477	5393	5310	0
1	19	17	17	17	19	24	30	39	49	62	76	91	09
2	17	15	15	15	17	22	29	37	48	60	74	90	07
3	15	13	13	13	16	20	27	36	46	59	73	89	06
4	13	11	11	12	14	19	26	34	45	57	71	87	05
5	12	10	10	13	17	24	33	43	56	70	86	03	5
6	10	08	08	11	16	23	31	41	54	69	84	02	6
7	08	06	07	09	14	21	30	40	53	67	83	00	7
8	06	05	05	06	13	19	28	39	51	66	82	58	8
9	05	03	03	06	11	18	27	37	50	64	80	96	9
10	03	01	02	05	09	16	25	36	49	63	79	96	10
11	01	00	00	03	08	15	24	35	47	61	77	95	11
12	00	00	6099	01	06	13	22	33	46	60	76	94	12
13	6098	96	97	00	05	12	21	32	44	59	75	93	13
14	96	95	95	5096	03	10	19	30	43	57	73	91	14
15	94	93	94	97	02	09	18	29	41	56	72	90	15
16	93	91	92	95	00	07	16	27	40	54	70	88	16
17	91	90	90	93	5898	06	15	26	38	53	69	87	17
18	89	88	89	92	97	04	13	24	37	52	68	85	18
19	88	86	87	90	95	03	12	23	36	50	66	84	19
20	86	85	85	89	94	01	10	21	34	49	65	83	20
21	84	83	84	87	92	00	09	20	33	47	64	81	21
22	82	81	82	85	91	5798	07	18	31	46	62	80	22
23	81	79	81	84	89	96	06	17	30	45	61	79	23
24	79	78	79	82	88	95	04	15	28	43	59	77	24
25	78	76	77	81	86	93	03	14	27	42	58	76	25
26	76	74	76	79	84	92	01	13	26	40	57	75	26
27	74	73	74	77	83	90	00	11	24	39	55	73	27
28	72	71	72	76	81	89	5698	10	23	37	54	72	28
29	71	69	71	74	80	87	97	08	21	36	53	71	29
30	69	68	69	73	78	86	95	07	20	35	51	69	30
31	67	66	67	71	77	84	94	05	18	33	50	68	31
32	65	65	66	69	75	83	92	04	17	32	48	66	32
33	64	63	64	68	74	81	91	02	16	30	47	65	33
34	63	61	63	66	72	80	89	01	14	29	46	64	34
35	60	60	61	65	70	78	86	5599	13	28	44	62	35
36	59	58	59	63	69	77	86	98	11	26	43	61	36
37	57	56	58	61	67	75	85	96	10	25	41	60	37
38	55	55	56	60	66	74	83	95	08	23	40	58	38
39	54	53	55	58	64	72	82	94	07	22	39	57	39
40	52	51	53	57	63	71	80	92	06	21	37	56	40
41	50	50	51	55	61	69	79	91	04	19	36	54	41
42	48	48	50	54	60	68	77	89	03	18	35	53	42
43	47	46	48	52	58	66	76	88	01	16	33	52	43
44	45	45	46	50	56	65	74	86	00	15	32	50	44
45	43	43	45	49	55	63	73	85	5498	14	31	49	45
46	42	41	43	47	53	61	71	83	97	12	29	48	46
47	40	40	42	46	52	60	70	82	96	11	28	46	47
48	38	38	40	44	50	58	68	80	94	09	26	45	48
49	37	36	38	42	49	57	67	79	93	08	25	44	49
50	35	35	37	41	47	55	66	78	91	07	24	42	50
51	33	33	35	39	46	54	64	76	90	05	22	41	51
52	32	31	33	38	44	52	63	75	88	04	21	40	52
53	30	30	32	36	43	51	61	73	87	02	20	38	53
54	28	28	30	35	41	49	60	72	86	01	18	37	54
55	26	26	29	33	39	48	58	70	84	00	17	35	55
56	25	25	27	31	38	46	57	69	83	5398	15	34	56
57	23	23	25	30	36	45	55	67	81	97	14	33	57
58	21	21	24	28	35	43	54	66	80	95	13	31	58
59	20	20	22	27	33	42	53	64	78	94	11	30	59

"	00 30'	00 31'	00 32'	00 33'	00 34'	00 35'	00 36'	00 37'	00 38'	00 39'	00 40'	00 41'	"
0	7788	7639	7501	7368	7238	7112	6990	6871	6755	6642	6532	6425	0
1	79	37	7499	65	36	10	86	69	53	40	30	23	1
2	77	34	97	63	34	06	86	67	51	38	29	21	2
3	74	32	94	61	32	06	84	65	49	37	27	20	3
4	72	30	92	59	29	04	82	63	47	35	25	18	4
5	69	27	90	57	27	02	80	61	45	33	23	16	5
6	67	25	88	54	25	00	78	59	43	31	21	14	6
7	65	23	85	52	23	7098	76	57	42	29	19	13	7
8	62	20	83	50	21	96	74	55	40	27	18	11	8
9	60	18	81	48	19	93	72	53	38	25	16	09	9
10	57	16	79	46	17	91	70	51	36	24	14	07	10
11	55	13	76	44	15	89	68	49	34	22	12	06	11
12	53	11	74	41	12	87	66	47	32	20	10	04	12
13	50	09	72	39	10	85	64	45	30	18	09	02	13
14	48	07	70	37	08	83	62	43	28	16	07	00	14
15	45	04	67	35	06	81	60	42	26	14	05	6308	15
16	43	02	65	33	04	79	58	40	25	12	03	97	16
17	41	00	63	30	02	77	56	38	23	11	01	95	17
18	38	7597	61	28	00	75	54	36	21	09	00	93	18
19	36	95	58	26	7198	73	52	34	19	07	6498	91	19
20	34	93	56	24	96	71	50	32	17	05	96	96	20
21	31	90	54	22	93	69	48	30	15	03	94	88	21
22	29	88	52	20	91	67	46	28	13	01	92	86	22
23	26	86	50	17	89	65	44	26	11	00	91	84	23
24	24	83	47	15	87	63	43	24	09	6598	89	83	24
25	22	81	45	13	85	61	40	22	08	96	87	81	25
26	19	79	43	11	83	59	38	20	06	94	85	79	26
27	17	77	41	09	81	57	36	18	04	92	84	77	27
28	14	74	38	07	79	55	34	16	02	90	82	76	28
29	12	72	36	04	77	53	32	14	00	89	80	74	29
30	10	70	34	02	75	50	30	12	6698	87	78	72	30
31	07	67	32	00	72	48	28	11	96	85	76	71	31
32	05	65	29	7398	70	46	26	09	94	83	75	69	32
33	03	63	27	96	68	44	24	07	92	81	73	67	33
34	00	60	25	94	66	42	22	05	91	79	71	65	34
35	7698	58	23	91	64	40	20	03	89	78	69	64	35
36	96	56	21	89	62	38	18	01	87	76	67	62	36
37	93	54	18	87	60	36	16	6798	85	74	66	60	37
38	91	51	16	85	58	34	14	97	83	72	64	58	38
39	88	49	14	83	56	32	12	95	81	70	62	57	39
40	86	47	12	81	54	30	10	93	79	68	60	55	40
41	84	44	00	79	52	28	08	91	77	67	59	53	41
42	81	42	07	76	49	26	06	89	76	65	57	51	42
43	79	40	05	74	47	24	04	87	74	63	55	50	43
44	77	38	03	72	45	22	02	85	72	61	53	48	44
45	74	35	01	70	43	20	00	84	70	59	51	46	45
46	72	33	7398	68	41	18	6898	82	68	58	50	44	46
47	70	31	96	66	39	16	96	80	66	56	48	43	47
48	67	28	94	64	37	14	94	78	64	54	46	41	48
49	65	26	92	61	35	12	92	76	63	52	44	39	49
50	63	24	90	59	33	10	90	74	61	50	43	38	50
51	60	22	87	57	31	08	88	72	59	48	41	36	51
52	58	19	85	55	29	06	86	70	57	47	39	34	52
53	55	17	83	53	27	04	84	68	55	45	37	32	53
54	53	15	81	51	24	02	82	66	53	43	35	31	54
55	51	13	79	49	22	00	81	64	51	41	34	29	55
56	48	10	76	46	20	6998	79	63	50	39	32	27	56
57	46	08	74	44	18	96	77	61	48	38	30	25	57
58	44	06	72	42	16	94	75	59	46	36	28	24	58
59	41	03	70	40	14	92	73	57	44	34	27	22	59
"	00 30'	00 31'	00 32'	00 33'	00 34'	00 35'	00 36'	00 37'	00 38'	00 39'	00 40'	00 41'	"

"	00 42'	00 43'	00 44'	00 45'	00 46'	00 47'	00 48'	00 49'	00 50'	00 51'	00 52'	00 53'	"
0	6320	6318	6118	6021	5925	5832	5740	5651	5563	5477	5393	5310	0
1	17	16	17	19	24	30	39	49	62	76	91	07	1
2	15	15	15	17	22	29	37	48	60	74	90	07	2
3	13	13	13	16	20	27	36	46	59	73	89	06	3
4			12	14	19	26	34	45	57	71	87	03	4
5	19	10	10	13	17	24	33	43	56	70	86	03	5
6	10	08	08	11	16	23	31	42	54	69	84	02	6
7	08	06	07	09	14	21	30	40	53	67	83	00	7
8	06	05	05	08	13	19	28	39	51	66	82	5899	8
9	05	03	03	06	11	18	27	37	50	64	80	96	9
10	03	01	02	05	09	16	25	36	49	63	79	96	10
11	01	00	00	03	08	15	24	35	47	61	77	95	11
12	00	0198	6099	01	06	13	22	33	46	60	76	94	12
13	6398	96	97	00	05	12	21	32	44	59	75	92	13
14	96	95	95	5926	03	10	19	30	43	57	73	91	14
15	94	93	94	97	02	09	18	29	41	56	72	90	15
16	93	91	92	95	00	07	16	27	40	54	70	88	16
17	91	90	90	93	5898	06	15	26	38	53	69	87	17
18	89	88	89	92	97	04	13	24	37	52	68	85	18
19	88	86	87	90	95	03	12	23	36	50	66	84	19
20	86	85	85	89	94	01	10	21	34	49	65	83	20
21	84	83	84	87	92	00	09	20	33	47	64	81	21
22	82	81	82	85	91	5798	07	18	31	46	62	80	22
23	81	79	81	84	89	96	06	17	30	45	61	79	23
24	79	78	79	82	88	95	04	15	28	43	59	77	24
25	78	76	77	81	86	93	03	14	27	42	58	76	25
26	76	74	76	79	84	92	01	13	26	40	57	75	26
27	74	73	74	77	83	90	00	11	24	39	55	73	27
28	72	71	72	76	81	89	5698	10	23	37	54	72	28
29	71	69	71	74	80	87	97	08	21	36	53	71	29
30	69	68	69	73	78	86	95	07	20	35	51	69	30
31	67	66	67	71	77	84	94	05	18	33	50	68	31
32	65	65	66	69	75	83	92	04	17	32	48	66	32
33	64	63	64	68	74	81	91	02	16	30	47	65	33
34	62	61	63	66	72	80	89	01	14	29	46	64	34
35	60	60	61	65	70	78	86	5599	13	28	44	62	35
36	59	58	59	63	69	77	86	98	11	26	43	61	36
37	57	56	58	61	67	75	85	96	10	25	41	60	37
38	55	55	56	60	66	74	83	95	08	23	40	58	38
39	54	53	55	58	64	72	81	94	07	22	39	57	39
40	52	51	53	57	63	71	80	92	06	21	37	56	40
41	50	50	51	55	61	69	79	91	04	19	36	54	41
42	48	48	50	54	60	68	77	89	03	18	35	53	42
43	47	46	48	52	58	66	76	88	01	16	33	52	43
44	45	45	46	50	56	65	74	86	00	15	32	50	44
45	43	43	45	49	55	63	73	85	5498	14	31	49	45
46	42	41	43	47	53	61	71	83	97	12	30	48	46
47	40	40	42	46	52	60	70	82	96	11	28	46	47
48	38	38	40	44	50	58	68	80	94	09	26	45	48
49	37	36	38	42	49	57	67	79	93	08	25	44	49
50	35	35	37	41	47	55	66	78	91	07	24	42	50
51	33	33	35	39	46	54	64	76	90	05	23	41	51
52	32	31	33	38	44	52	63	75	88	04	21	40	52
53	30	30	32	36	43	51	61	73	87	02	20	38	53
54	28	28	30	35	41	49	60	72	86	01	18	37	54
55	26	26	29	33	39	48	58	70	84	00	17	35	55
56	25	25	27	31	38	46	57	69	83	5398	15	34	56
57	23	23	25	30	36	45	55	67	81	97	14	33	57
58	21	21	24	28	35	43	54	66	80	95	13	31	58
59	20	20	22	27	33	42	52	64	78	94	11	30	59

TABLE III.—PROPORTIONAL LOGARITHMS.

"	00 54'	00 55'	00 56'	00 57'	00 58'	00 59'	10 0'	10 1'	10 2'	10 3'	10 4'	10 5'	"
0	5239	5149	5071	4924	4818	4744	4771	4669	4638	4559	4491	4424	0
1	27	48	70	93	17	43	70	98	97	58	90	22	1
2	26	46	68	91	16	42	69	67	26	57	89	21	2
3	25	45	67	90	15	41	68	96	25	56	88	20	3
4	23	44	66	89	13	39	66	95	24	55	86	19	4
5	22	43	64	88	12	38	65	93	23	54	85	18	5
6	21	41	63	86	11	37	64	92	22	52	84	17	6
7	19	40	62	85	10	36	63	91	21	51	83	16	7
8	18	39	61	84	08	34	62	90	19	50	82	15	8
9	17	37	59	83	07	33	60	89	18	49	81	14	9
10	15	36	58	81	06	32	59	88	17	48	80	13	10
11	14	35	57	80	05	31	58	86	16	47	79	11	11
12	13	33	55	79	03	30	57	85	15	46	77	10	12
13	11	32	54	77	02	28	56	84	14	44	76	09	13
14	10	31	53	76	01	27	54	83	13	43	75	08	14
15	00	29	51	75	00	26	53	82	11	42	74	07	15
16	07	28	50	74	4999	25	52	80	10	41	73	06	16
17	06	27	49	73	97	23	51	79	09	40	72	05	17
18	05	25	48	71	96	22	50	78	08	39	71	04	18
19	03	24	46	70	95	21	48	77	07	38	69	03	19
20	02	23	45	69	94	20	47	76	06	36	68	01	20
21	01	22	44	67	92	19	46	75	04	35	67	00	21
22	5199	20	43	66	91	17	45	73	03	34	66	4399	22
23	98	19	41	65	90	16	44	72	02	33	65	98	23
24	97	18	40	64	89	15	43	71	01	32	64	97	24
25	96	16	39	62	87	14	41	70	00	31	63	96	25
26	94	15	37	61	86	12	40	69	4599	30	62	95	26
27	93	14	36	60	85	11	39	68	97	28	60	94	27
28	91	12	35	59	84	10	38	66	96	27	59	93	28
29	90	11	34	57	82	09	36	65	95	26	58	91	29
30	89	10	32	56	81	07	35	64	94	25	57	90	30
31	87	08	31	55	80	06	34	63	93	24	56	89	31
32	86	07	30	54	79	05	33	62	92	23	55	88	32
33	85	06	28	53	77	04	32	60	90	22	54	87	33
34	83	05	27	51	76	03	30	59	89	20	53	86	34
35	82	03	26	50	75	01	29	58	88	19	52	85	35
36	81	02	25	49	74	00	28	57	87	18	50	84	36
37	79	01	24	47	73	4799	27	56	86	17	49	83	37
38	78	5099	23	46	71	98	26	55	85	16	48	81	38
39	77	98	21	45	70	97	24	53	84	15	47	80	39
40	75	97	19	43	69	95	23	52	83	14	46	79	40
41	74	95	18	42	68	94	22	51	81	12	45	78	41
42	73	94	17	41	66	93	21	50	80	11	44	77	42
43	72	93	16	40	65	92	20	49	79	10	43	76	43
44	70	92	14	38	64	91	18	48	78	09	41	75	44
45	69	90	13	37	63	89	17	46	77	08	40	74	45
46	68	89	12	36	61	88	16	45	75	07	39	73	46
47	66	88	11	35	60	87	15	44	74	06	38	72	47
48	65	86	09	33	59	86	14	43	73	05	37	70	48
49	64	85	08	32	58	85	12	42	72	03	36	69	49
50	62	84	07	31	56	83	11	40	71	02	35	68	50
51	61	82	05	30	55	82	10	39	70	01	34	67	51
52	60	81	04	29	54	81	09	38	69	00	33	66	52
53	58	80	03	27	53	80	08	37	67	4599	31	65	53
54	57	79	02	26	52	78	06	36	66	98	30	64	54
55	56	77	00	25	50	77	05	35	65	97	29	63	55
56	54	76	4099	23	49	76	04	33	64	95	28	62	56
57	53	75	98	22	48	75	03	32	63	94	27	61	57
58	52	73	97	21	47	74	02	31	62	93	26	59	58
59	50	72	96	20	45	73	01	30	60	92	25	58	59
"	00 54'	00 55'	00 56'	00 57'	00 58'	00 59'	10 0'	10 1'	10 2'	10 3'	10 4'	10 5'	"

°	′	″	‴	‵	‶	‷	‸	‹	›	※	‼	‽	‾	‿	°
10 6'	10 7'	10 8'	10 9'	10 10'	10 11'	10 12'	10 13'	10 14'	10 15'	10 16'	10 17'	10 18'	10 19'	10 20'	10 21'
0	4357	4302	4238	4164	4108	4040	3979	3919	3860	3802	3745	3688			0
1	56	91	37	63	01	39	78	18	59	01	44	87			1
2	55	90	36	62	00	38	77	18	58	00	43	86			2
3	54	89	34	61	4009	37	76	17	57	3299	42	85			3
4	53	88	33	60	98	36	75	16	56	98	41	84			4
5	52	86	32	59	97	35	74	15	55	97	40	83			5
6	51	85	31	58	96	34	73	14	55	96	39	82			6
7	50	84	30	57	95	33	72	13	54	95	38	81			7
8	49	83	29	56	93	32	71	12	53	94	37	80			8
9	47	82	18	55	92	31	70	11	52	93	36	79			9
10	46	81	17	54	91	30	69	10	51	92	35	78			10
11	45	80	16	53	90	29	68	09	50	91	34	77			11
12	44	79	15	52	89	28	67	08	49	90	33	77			12
13	43	78	14	51	88	27	66	07	48	89	32	76			13
14	43	77	13	50	87	26	65	06	47	88	31	75			14
15	41	76	12	48	86	25	64	05	46	86	30	74			15
16	40	75	11	47	85	24	63	04	45	87	29	73			16
17	39	74	10	46	84	23	62	03	44	86	28	72			17
18	38	73	09	45	83	22	61	02	43	85	27	71			18
19	36	71	07	44	82	21	60	01	42	84	27	70			19
20	35	70	06	43	81	20	59	00	41	83	26	69			20
21	34	69	05	42	80	19	58	3899	40	82	25	68			21
22	33	68	04	41	79	18	57	98	39	81	24	67			22
23	32	67	03	40	78	17	56	97	38	80	23	66			23
24	31	66	03	39	77	16	55	96	37	79	22	65			24
25	30	65	01	38	76	15	54	95	36	78	21	64			25
26	29	64	00	37	75	14	53	94	35	77	20	63			26
27	28	63	4199	36	74	13	52	93	34	76	19	62			27
28	27	62	98	35	73	12	51	92	33	75	18	61			28
29	26	61	97	34	72	11	50	91	32	74	17	61			29
30	25	60	96	33	71	10	49	90	31	73	16	60			30
31	23	59	95	32	70	09	48	89	30	72	15	59			31
32	22	58	94	31	69	08	47	88	29	71	14	58			32
33	21	58	93	30	68	07	46	87	28	70	13	57			33
34	20	55	92	29	67	06	45	86	27	69	12	56			34
35	19	54	91	28	66	05	44	85	26	68	11	55			35
36	18	53	89	27	65	04	43	84	25	67	10	54			36
37	17	52	88	26	64	03	42	83	24	66	09	53			37
38	16	51	87	25	63	02	41	82	23	65	08	52			38
39	15	50	86	23	62	01	40	81	22	64	07	51			39
40	14	49	85	22	61	00	39	80	21	63	07	50			40
41	13	48	84	21	60	3999	38	79	21	62	06	49			41
42	11	47	83	20	59	98	37	78	20	61	05	48			42
43	10	46	82	19	58	97	36	77	19	60	04	47			43
44	09	45	81	18	57	96	35	76	18	59	03	47			44
45	08	44	80	17	55	94	34	75	17	58	02	46			45
46	07	43	79	16	54	93	33	74	16	57	01	45			46
47	06	41	78	15	53	92	32	73	15	57	00	44			47
48	05	40	77	14	52	91	31	72	14	56	3899	43			48
49	04	39	76	13	51	90	30	71	13	55	98	42			49
50	03	38	75	12	50	89	29	70	12	54	97	41			50
51	02	37	74	11	49	88	28	69	11	53	96	40			51
52	01	36	73	10	48	87	27	68	10	52	95	39			52
53	00	35	72	09	47	86	26	67	09	51	94	38			53
54	4399	34	71	08	46	85	25	66	08	50	93	37			54
55	08	33	69	07	45	84	24	65	07	49	92	36			55
56	06	32	68	06	44	83	23	64	06	48	91	35			56
57	05	31	67	05	43	82	22	63	05	47	91	35			57
58	04	30	66	04	42	81	21	62	04	46	90	34			58
59	03	29	65	03	41	80	20	61	03	46	89	33			59

TABLE III.—PROPORTIONAL LOGARITHMS.

"	10 18'	10 19'	10 20'	10 21'	10 22'	10 23'	10 24'	10 25'	10 26'	10 27'	10 28'	10 29'	"
0	3632	3378	3523	3468	3415	3362	3310	3259	3208	3158	3108	3059	0
1	31	76	21	67	14	61	09	58	07	57	07	58	1
2	30	75	20	66	13	60	08	57	06	56	06	57	2
3	29	74	19	65	12	59	07	56	05	55	05	56	3
4	28	73	18	64	11	58	06	55	04	54	05	56	4
5	27	72	17	63	10	58	06	54	04	53	04	55	5
6	26	71	16	63	09	57	05	53	03	53	03	54	6
7	25	70	15	62	08	56	04	53	02	52	02	53	7
8	24	69	15	61	08	55	03	53	01	51	01	52	8
9	23	68	14	60	07	54	02	51	00	50	01	52	9
10	23	67	13	59	06	53	01	50	3190	49	00	51	10
11	22	66	12	58	05	52	00	49	98	48	3090	50	11
12	21	65	11	57	04	51	00	48	98	48	98	49	12
13	20	65	10	56	03	51	00	48	97	47	97	48	13
14	19	64	09	55	02	50	98	47	96	46	96	47	14
15	18	63	08	54	01	49	97	46	95	45	96	47	15
16	17	62	07	54	00	48	96	45	94	44	95	46	16
17	16	61	06	53	00	47	95	44	93	43	94	45	17
18	15	60	06	52	3399	46	94	43	93	43	93	44	18
19	14	59	05	51	98	45	94	42	92	42	92	43	19
20	13	58	04	50	97	45	93	42	91	41	91	43	20
21	12	57	03	49	96	44	92	41	90	40	91	42	21
22	11	56	02	48	95	43	91	40	89	39	90	41	22
23	10	55	01	47	94	42	90	39	88	38	89	40	23
24	10	55	00	46	93	41	89	38	88	38	88	39	24
25	09	54	3490	46	93	40	88	37	87	37	87	38	25
26	08	53	98	45	92	39	88	36	86	36	87	38	26
27	07	52	97	44	91	38	87	36	85	35	86	37	27
28	06	51	97	43	90	38	86	35	84	34	85	36	28
29	05	50	96	42	89	37	85	34	83	33	84	35	29
30	04	49	95	41	88	36	84	33	83	33	83	34	30
31	03	48	94	40	87	35	83	32	82	32	82	34	31
32	02	47	93	39	86	34	82	31	81	31	82	33	32
33	01	46	92	38	85	33	82	31	80	30	81	32	33
34	00	45	91	38	85	32	81	30	79	29	80	31	34
35	3599	45	90	37	84	32	80	29	78	29	79	30	35
36	98	44	89	36	83	31	79	28	78	28	78	30	36
37	98	43	88	35	82	30	78	27	77	27	78	29	37
38	97	42	88	34	81	29	77	26	76	26	77	28	38
39	96	41	87	33	80	28	76	25	75	25	76	27	39
40	95	40	86	32	79	27	75	25	74	24	75	26	40
41	94	39	85	31	79	26	75	24	73	24	74	26	41
42	93	38	84	31	78	25	74	23	73	23	73	25	42
43	92	37	83	30	77	25	73	22	72	22	73	24	43
44	91	36	82	29	76	24	73	21	71	21	72	23	44
45	90	35	81	28	75	23	71	20	70	20	71	22	45
46	89	35	80	27	74	22	70	20	69	19	70	22	46
47	88	34	80	26	73	21	70	19	68	19	69	21	47
48	87	33	79	25	72	20	69	18	68	18	69	20	48
49	87	32	78	24	72	19	68	17	67	17	68	19	49
50	86	31	77	23	71	19	67	16	66	16	67	18	50
51	85	30	76	22	70	18	66	15	65	15	66	18	51
52	84	29	75	22	69	17	65	14	64	14	65	17	52
53	83	28	74	21	68	16	65	14	63	14	65	16	53
54	82	27	73	20	67	15	64	13	63	13	64	15	54
55	81	26	72	19	66	14	63	12	62	12	63	14	55
56	80	25	71	18	65	13	62	11	61	11	62	14	56
57	79	25	71	17	65	13	61	10	60	10	61	13	57
58	78	24	70	16	64	12	60	09	59	10	60	12	58
59	77	23	69	15	63	11	59	08	58	09	59	11	59
"	10 18'	10 19'	10 20'	10 21'	10 22'	10 23'	10 24'	10 25'	10 26'	10 27'	10 28'	10 29'	"

TABLE III.—PROPORTIONAL LOGARITHMS.

"	a m	a m	a m	a m	a m	a m	a m	a m	a m	a m	a m	a m	a m	a m	"
"	10 30'	10 31'	10 32'	10 33'	10 34'	10 35'	10 36'	10 37'	10 38'	10 39'	10 40'	10 41'	"	"	
0	3010	2968	2915	2868	2821	2775	2730	2685	2640	2596	2553	2510	0	0	
1	09	62	14	67	21	75	29	84	40	96	52	09	1	1	
2	03	61	13	66	20	74	29	84	39	95	51	08	2	2	
3	06	60	12	66	19	73	28	83	38	94	51	07	3	3	
4	07	59	12	65	18	72	27	82	38	93	50	07	4	4	
5	06	58	11	64	18	72	26	81	37	93	49	06	5	5	
6	05	58	10	63	17	71	25	81	36	92	48	05	6	6	
7	05	57	09	62	16	70	25	80	35	91	48	04	7	7	
8	04	56	09	62	15	69	24	79	35	91	47	04	8	8	
9	03	55	08	61	15	69	23	78	34	90	46	03	9	9	
10	02	54	07	60	14	68	22	78	33	89	45	02	10	10	
11	01	54	06	59	13	67	22	77	32	88	45	02	11	11	
12	01	53	05	59	12	66	21	76	32	88	44	01	12	12	
13	00	52	05	58	11	66	20	75	31	87	43	00	13	13	
14	2999	51	04	57	11	65	19	75	30	86	43	2499	14	14	
15	96	50	03	56	10	64	19	74	29	85	42	99	15	15	
16	97	50	02	55	09	63	18	73	29	85	41	98	16	16	
17	97	49	01	55	08	63	17	72	28	84	40	97	17	17	
18	96	48	01	54	08	62	16	72	27	83	40	97	18	18	
19	95	47	00	53	07	61	16	71	26	83	39	96	19	19	
20	94	46	2899	52	06	60	15	70	26	82	38	95	20	20	
21	93	46	98	52	05	60	14	69	25	81	38	94	21	21	
22	93	45	98	51	05	59	13	69	24	80	37	94	22	22	
23	92	44	97	50	04	58	13	68	24	80	36	93	23	23	
24	91	43	96	49	03	57	12	67	23	79	35	92	24	24	
25	90	42	95	48	02	56	11	66	22	78	35	92	25	25	
26	89	42	94	48	01	56	10	66	21	77	34	91	26	26	
27	89	41	94	47	01	55	10	65	21	77	33	90	27	27	
28	88	40	93	46	00	54	09	64	20	76	33	89	28	28	
29	87	39	92	45	2999	53	08	63	19	75	32	88	29	29	
30	86	39	91	45	98	53	07	63	18	74	31	88	30	30	
31	85	38	91	44	98	52	07	62	18	74	30	87	31	31	
32	85	37	90	43	97	51	06	61	17	73	30	87	32	32	
33	84	36	89	42	96	50	05	60	16	72	29	86	33	33	
34	83	35	88	42	95	50	04	60	15	72	28	85	34	34	
35	82	35	87	41	95	49	04	59	15	71	27	85	35	35	
36	81	34	87	40	94	48	03	58	14	70	27	84	36	36	
37	81	33	86	39	93	47	02	57	13	69	26	83	37	37	
38	80	32	85	38	92	47	01	57	12	68	25	82	38	38	
39	79	31	84	38	92	46	01	56	11	68	25	82	39	39	
40	78	31	83	37	91	45	00	55	11	67	24	81	40	40	
41	77	30	83	36	90	44	2899	55	10	66	23	80	41	41	
42	77	29	82	35	89	44	98	54	10	66	22	80	42	42	
43	76	28	81	35	88	43	98	53	09	65	22	79	43	43	
44	75	27	80	34	88	42	97	52	08	64	21	78	44	44	
45	74	27	80	33	87	41	96	52	07	64	20	77	45	45	
46	73	26	79	32	86	41	95	51	07	63	20	77	46	46	
47	73	25	78	31	85	40	95	50	06	62	19	76	47	47	
48	72	24	77	31	85	39	94	49	05	61	18	75	48	48	
49	71	24	76	30	84	38	93	49	04	61	17	75	49	49	
50	70	23	76	29	83	38	92	48	04	60	17	74	50	50	
51	69	22	75	28	82	37	92	47	03	59	16	73	51	51	
52	69	21	74	28	82	36	91	46	02	58	15	72	52	52	
53	68	20	73	27	81	35	90	46	01	58	15	72	53	53	
54	67	20	73	26	80	35	89	45	01	57	14	71	54	54	
55	66	19	72	25	79	34	89	44	00	56	13	70	55	55	
56	65	18	71	25	79	33	88	43	2899	56	12	70	56	56	
57	65	17	70	24	78	32	87	43	99	55	11	69	57	57	
58	64	16	69	23	77	32	87	42	98	54	11	68	58	58	
59	63	16	69	22	76	31	86	41	97	53	10	67	59	59	
"	10 30'	10 31'	10 32'	10 33'	10 34'	10 35'	10 36'	10 37'	10 38'	10 39'	10 40'	10 41'	"	"	

"	h = 10 42'	h = 10 43'	h = 10 44'	h = 10 45'	h = 10 46'	h = 10 47'	h = 10 48'	h = 10 49'	h = 10 50'	h = 10 51'	h = 10 52'	h = 10 53'	"
0	24 07	24 24	24 39	24 41	24 300	24 59	24 18	24 78	24 30	24 99	24 61	24 22	0
1	66	24	82	40	22 39	58	18	78	33	99	60	21	1
2	65	23	81	33	98	58	17	77	37	98	59	21	2
3	65	22	80	39	98	57	16	76	37	98	59	20	3
4	64	22	80	38	97	56	16	76	36	97	58	19	4
5	63	21	79	37	96	56	15	75	36	96	57	19	5
6	62	20	78	37	96	55	14	74	35	96	57	18	6
7	62	19	78	36	95	54	14	74	34	95	56	17	7
8	61	19	77	35	94	53	13	73	34	94	55	17	8
9	60	18	76	35	94	53	12	72	33	94	55	16	9
10	60	17	75	34	93	52	12	72	32	93	54	16	10
11	59	17	75	33	92	51	11	71	32	92	53	15	11
12	58	16	74	33	91	51	10	70	31	92	53	14	12
13	58	15	73	32	91	50	10	70	30	91	52	14	13
14	57	15	73	31	90	49	09	69	30	90	52	13	14
15	56	14	72	31	89	49	08	69	29	90	51	12	15
16	55	13	71	30	89	48	08	68	28	89	50	12	16
17	55	12	71	29	88	47	07	67	28	88	50	11	17
18	54	12	70	28	87	47	06	67	27	88	49	10	18
19	53	11	69	28	87	46	06	66	26	87	48	10	19
20	53	10	68	27	86	45	05	65	26	86	48	09	20
21	52	10	68	26	85	45	04	65	25	86	47	09	21
22	51	09	67	26	85	44	04	64	24	85	46	08	22
23	50	08	66	25	84	43	03	63	24	85	46	07	23
24	50	08	66	24	83	43	02	63	23	84	45	07	24
25	49	07	65	24	83	42	02	62	22	83	44	06	25
26	48	06	64	23	82	41	01	61	22	83	44	05	26
27	48	05	64	22	81	41	00	61	21	82	43	05	27
28	47	05	63	22	81	40	00	60	20	81	42	04	28
29	46	04	62	21	80	39	2199	59	20	81	42	03	29
30	45	03	62	20	79	38	98	59	19	80	41	03	30
31	45	03	61	20	79	38	98	58	18	79	41	02	31
32	44	02	60	19	78	37	97	57	17	79	40	01	32
33	43	01	59	18	77	37	96	57	17	78	39	01	33
34	43	01	59	17	77	36	96	56	16	77	39	00	34
35	42	00	58	17	76	35	95	55	16	77	38	00	35
36	41	2399	57	16	75	35	94	55	15	76	37	10 39	36
37	41	98	57	15	74	34	94	54	15	75	37	98	37
38	40	98	56	15	74	33	93	53	14	75	36	98	38
39	39	97	55	14	73	33	92	53	13	74	35	97	39
40	39	96	55	13	72	32	92	52	13	73	35	96	40
41	38	96	54	13	72	31	91	51	12	73	34	96	41
42	37	95	53	12	71	31	90	51	11	72	33	95	42
43	36	94	53	11	70	30	90	50	11	72	33	94	43
44	36	94	52	11	70	29	89	49	10	71	32	94	44
45	35	93	51	10	69	29	88	49	09	70	29	93	45
46	34	92	50	09	68	28	88	48	09	70	31	93	46
47	33	91	50	09	68	27	87	47	08	69	30	92	47
48	33	91	49	08	67	27	86	47	07	68	30	91	48
49	32	90	48	07	66	26	86	46	07	68	29	91	49
50	31	89	48	07	66	25	85	45	06	67	28	90	50
51	31	89	47	06	65	25	84	45	05	66	28	89	51
52	30	88	46	05	64	24	84	44	05	66	27	88	52
53	29	87	46	04	64	23	83	43	04	65	26	87	53
54	29	87	45	04	63	23	82	43	03	64	26	87	54
55	28	86	44	03	62	22	82	42	03	64	25	87	55
56	27	85	44	02	62	21	81	41	02	63	25	86	56
57	26	84	43	02	61	20	80	41	01	62	24	86	57
58	26	84	42	01	60	20	80	40	01	62	23	85	58
59	25	83	42	00	60	19	79	39	00	61	23	84	59
"	h = 10 42'	h = 10 43'	h = 10 44'	h = 10 45'	h = 10 46'	h = 10 47'	h = 10 48'	h = 10 49'	h = 10 50'	h = 10 51'	h = 10 52'	h = 10 53'	"

TABLE III.—PROPORTIONAL LOGARITHMS.

"	h = 10 54'	h = 10 55'	h = 10 56'	h = 10 57'	h = 10 58'	h = 10 59'	h = 20 0'	h = 20 1'	h = 20 2'	h = 20 3'	h = 20 4'	"
0	1984	1946	1908	1871	1834	1797	1761	1725	1689	1654	1619	0
1	63	45	08	70	33	97	60	24	89	53	18	1
2	62	44	07	70	33	96	60	24	88	52	17	2
3	62	44	06	69	32	95	59	23	87	52	17	3
4	61	43	06	68	31	95	59	22	87	51	16	4
5	81	43	05	68	31	94	58	22	86	51	16	5
6	80	42	04	67	30	94	57	21	86	50	15	6
7	79	41	04	67	30	93	57	21	85	50	14	7
8	79	41	03	66	29	92	56	20	84	49	14	8
9	78	40	03	65	28	92	55	19	84	48	13	9
10	77	39	02	65	28	91	55	19	83	48	13	10
11	77	39	01	64	27	91	54	18	83	47	12	11
12	76	38	01	63	27	90	54	18	82	47	12	12
13	75	38	00	63	26	89	53	17	81	46	11	13
14	75	37	1899	62	25	89	52	17	81	45	10	14
15	74	36	99	62	25	88	52	16	80	45	10	15
16	74	36	98	61	24	88	51	15	80	44	09	16
17	73	35	98	60	23	87	51	15	79	44	09	17
18	72	34	97	60	23	86	50	14	78	43	08	18
19	72	34	96	59	22	86	49	14	78	43	07	19
20	71	33	96	59	22	85	49	13	77	42	07	20
21	70	33	95	58	21	85	48	12	77	41	06	21
22	70	32	94	57	20	84	48	12	76	41	06	22
23	69	31	94	57	20	83	47	11	76	40	05	23
24	68	31	93	56	19	83	46	11	75	40	05	24
25	68	30	93	55	19	82	46	10	74	39	04	25
26	67	29	92	55	18	81	45	09	74	38	03	26
27	67	29	91	54	17	81	45	09	73	38	03	27
28	66	28	91	54	17	80	44	08	73	37	02	28
29	65	28	90	53	16	80	43	08	72	37	02	29
30	65	27	89	52	16	79	43	07	71	36	01	30
31	64	26	89	52	15	78	42	06	71	35	00	31
32	63	26	88	51	14	78	42	06	70	35	00	32
33	63	25	88	50	14	77	41	05	70	34	1599	33
34	62	24	87	50	13	77	40	05	69	34	99	34
35	62	24	86	49	12	76	40	04	68	33	98	35
36	61	23	86	49	12	75	39	03	68	33	98	36
37	60	23	85	48	11	75	39	03	67	32	97	37
38	60	22	84	47	11	74	38	02	67	31	96	38
39	59	21	84	47	10	74	37	02	66	31	96	39
40	58	21	83	46	09	73	37	01	65	30	95	40
41	58	20	83	46	09	72	36	00	65	30	95	41
42	57	19	82	45	08	72	36	00	64	29	94	42
43	56	19	81	44	08	71	35	1699	64	28	93	43
44	56	18	81	44	07	71	34	99	63	28	93	44
45	55	18	80	43	06	70	34	98	63	27	92	45
46	55	17	80	43	06	69	33	97	62	27	92	46
47	54	16	79	42	05	69	33	97	61	26	91	47
48	53	16	78	41	05	68	32	96	61	26	91	48
49	53	15	78	41	04	68	31	96	60	25	90	49
50	52	14	77	40	03	67	31	95	60	24	89	50
51	51	14	76	39	03	66	30	94	59	24	89	51
52	51	13	76	39	02	66	30	94	58	23	88	52
53	50	13	75	38	02	65	29	93	58	23	88	53
54	50	12	75	38	01	65	28	93	57	22	87	54
55	49	11	74	37	00	64	28	92	57	21	87	55
56	49	11	73	36	00	63	27	92	56	21	86	56
57	48	10	73	36	1799	63	27	91	55	20	85	57
58	47	09	72	35	98	62	26	90	55	20	85	58
59	46	09	71	35	98	62	25	90	54	19	84	59
"	10 54'	10 55'	10 56'	10 57'	10 58'	10 59'	20 0'	20 1'	20 2'	20 3'	20 4'	"
.	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	h =	.

TABLE III.—PROPORTIONAL LOGARITHMS.

°	15		16		17		18		19		20		21		°
	30'	30'	30'	30'	30'	30'	30'	30'	30'	30'	30'	30'	30'		
0	1564	1549	1515	1481	1447	1413	1380	1347	1314	1282	1249			0	
1	83	48	14	80	46	13	79	46	14	81	49			1	
2	82	48	14	79	46	12	78	46	13	81	48			2	
3	82	47	13	79	45	12	78	45	13	80	48			3	
4	81	47	12	78	45	11	78	45	12	80	47			4	
5	81	46	12	78	44	11	77	44	11	79	47			5	
6	80	46	11	77	43	10	77	44	11	78	46			6	
7	80	45	11	77	43	09	76	43	10	78	46			7	
8	79	44	10	76	42	09	76	43	10	77	45			8	
9	78	44	10	76	42	08	75	42	09	77	45			9	
10	78	43	09	75	41	08	74	42	09	76	44			10	
11	77	43	08	74	41	07	74	41	08	76	43			11	
12	77	42	08	74	40	07	73	41	08	75	43			12	
13	76	42	07	73	40	06	73	40	07	75	42			13	
14	76	41	07	73	39	06	72	39	07	74	42			14	
15	75	40	06	72	38	05	72	39	06	74	41			15	
16	74	40	06	72	38	04	71	38	06	73	41			16	
17	74	39	05	71	37	04	71	38	05	73	40			17	
18	73	39	04	70	37	03	70	37	04	72	40			18	
19	73	38	04	70	36	03	70	37	04	71	39			19	
20	72	38	03	69	36	02	69	36	03	71	39			20	
21	71	37	03	69	35	02	68	35	03	70	38			21	
22	71	36	02	68	35	01	68	35	02	70	38			22	
23	70	36	02	68	34	01	67	34	02	69	37			23	
24	70	35	01	67	33	00	67	34	01	69	37			24	
25	69	35	00	67	33	1309	66	33	01	68	36			25	
26	69	34	00	66	32	99	66	33	00	68	35			26	
27	68	34	1409	65	32	98	65	32	00	67	35			27	
28	67	33	99	65	31	98	65	32	1209	67	34			28	
29	67	32	98	64	31	97	64	31	98	66	34			29	
30	66	32	98	64	30	97	63	31	98	66	33			30	
31	66	31	97	63	29	96	63	30	97	65	33			31	
32	65	31	96	63	29	96	62	29	97	64	32			32	
33	65	30	96	62	28	95	62	29	96	64	32			33	
34	64	30	95	61	28	94	61	28	96	63	31			34	
35	63	29	95	61	27	94	61	28	95	63	31			35	
36	63	28	94	60	27	93	60	27	95	62	30			36	
37	62	28	94	60	26	93	60	27	94	62	30			37	
38	62	27	93	59	26	92	59	26	94	61	29			38	
39	61	27	93	59	25	92	59	26	93	61	29			39	
40	61	26	92	58	24	91	58	25	92	60	28			40	
41	60	26	91	58	24	91	57	25	92	60	27			41	
42	59	25	91	57	23	90	57	24	91	59	27			42	
43	59	24	90	56	23	89	56	23	91	59	26			43	
44	58	24	90	56	22	89	56	23	90	58	26			44	
45	58	23	89	55	22	88	55	22	90	57	25			45	
46	57	23	89	55	21	88	55	22	89	57	25			46	
47	57	22	88	54	21	87	54	21	89	56	24			47	
48	56	22	87	54	20	87	54	21	88	56	24			48	
49	55	21	87	53	19	86	53	20	88	55	23			49	
50	55	20	86	52	19	86	52	20	87	55	23			50	
51	54	20	86	52	18	85	52	19	87	54	22			51	
52	54	19	85	51	18	84	51	19	86	54	22			52	
53	53	19	85	51	17	84	51	18	85	53	21			53	
54	52	18	84	50	17	83	50	17	85	53	21			54	
55	52	18	83	50	16	83	50	17	84	52	20			55	
56	51	17	83	49	16	82	49	16	84	52	19			56	
57	51	16	82	49	15	82	49	16	83	51	19			57	
58	50	16	82	48	14	81	48	15	83	50	18			58	
59	50	15	81	47	14	81	48	15	82	50	18			59	

TABLE III.—PROPORTIONAL LOGARITHMS.

°	' 16'		' 17'		' 18'		' 19'		' 20'		' 21'		' 22'		' 23'		' 24'		' 25'		' 26'		°
	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	h	m	
0	19	17	11	81	11	54	11	47	11	40	11	33	11	26	11	19	11	12	11	05	11	00	0
1	17	85	83	53	82	46	81	39	80	32	80	25	79	18	78	11	77	04	76	00	75	00	1
2	16	84	82	52	81	45	80	38	79	31	78	24	77	17	76	10	75	03	74	00	73	00	2
3	15	84	81	52	80	45	79	38	78	31	77	24	76	17	75	10	74	03	73	00	72	00	3
4	16	83	80	52	79	45	78	38	77	31	76	24	75	17	74	10	73	03	72	00	71	00	4
5	15	83	80	51	80	46	79	39	78	32	77	25	76	18	75	11	74	04	73	00	72	00	5
6	14	82	80	51	79	46	78	39	77	32	76	25	75	18	74	11	73	04	72	00	71	00	6
7	14	82	80	50	79	46	78	39	77	32	76	25	75	18	74	11	73	04	72	00	71	00	7
8	13	81	80	50	78	46	77	39	76	32	75	25	74	18	73	11	72	04	71	00	70	00	8
9	13	81	80	49	78	47	77	39	76	32	75	25	74	18	73	11	72	04	71	00	70	00	9
10	12	80	80	49	77	47	76	39	75	32	74	25	73	18	72	11	71	04	70	00	69	00	10
11	11	80	80	48	77	48	76	40	75	33	74	26	73	19	72	12	71	05	70	00	69	00	11
12	11	79	80	48	76	48	75	40	74	33	73	26	72	19	71	12	70	05	69	00	68	00	12
13	10	79	80	47	76	49	75	40	74	33	73	26	72	19	71	12	70	05	69	00	68	00	13
14	10	78	80	47	75	49	74	40	73	33	72	26	71	19	70	12	69	05	68	00	67	00	14
15	09	78	80	46	75	50	74	41	73	33	72	27	71	20	70	13	69	06	68	00	67	00	15
16	09	77	80	46	74	50	73	41	72	33	71	27	70	20	69	13	68	06	67	00	66	00	16
17	08	77	80	45	74	51	73	41	72	33	71	27	70	20	69	13	68	06	67	00	66	00	17
18	08	76	80	45	73	51	72	41	71	33	70	27	69	20	68	13	67	06	66	00	65	00	18
19	07	75	80	44	73	52	72	41	71	33	70	27	69	20	68	13	67	06	66	00	65	00	19
20	07	75	80	43	73	52	72	41	71	33	70	27	69	20	68	13	67	06	66	00	65	00	20
21	06	74	80	43	72	52	71	41	70	33	69	27	68	20	67	13	66	06	65	00	64	00	21
22	06	74	80	42	72	53	71	41	70	33	69	27	68	20	67	13	66	06	65	00	64	00	22
23	05	73	80	42	71	53	70	41	69	33	68	27	67	20	66	13	65	06	64	00	63	00	23
24	05	73	80	41	71	54	70	41	69	33	68	27	67	20	66	13	65	06	64	00	63	00	24
25	04	72	80	41	70	54	69	41	68	33	67	27	66	20	65	13	64	06	63	00	62	00	25
26	04	72	80	40	70	55	69	41	68	33	67	27	66	20	65	13	64	06	63	00	62	00	26
27	03	71	80	40	69	55	68	41	67	33	66	27	65	20	64	13	63	06	62	00	61	00	27
28	02	71	80	39	69	56	68	41	67	33	66	27	65	20	64	13	63	06	62	00	61	00	28
29	02	70	80	39	68	56	67	41	66	33	65	27	64	20	63	13	62	06	61	00	60	00	29
30	01	70	80	38	67	56	66	41	65	33	64	27	63	20	62	13	61	06	60	00	59	00	30
31	01	69	80	38	66	57	65	41	64	33	63	27	62	20	61	13	60	06	59	00	58	00	31
32	00	69	80	37	66	57	64	41	63	33	62	27	61	20	60	13	59	06	58	00	57	00	32
33	00	68	80	37	65	57	63	41	62	33	61	27	60	20	59	13	58	06	57	00	56	00	33
34	11	68	80	36	65	58	62	41	61	33	60	27	59	20	58	13	57	06	56	00	55	00	34
35	00	67	80	36	64	58	61	41	60	33	59	27	58	20	57	13	56	06	55	00	54	00	35
36	00	67	80	35	64	59	60	41	59	33	58	27	57	20	56	13	55	06	54	00	53	00	36
37	99	66	80	35	63	59	59	41	58	33	57	27	56	20	55	13	54	06	53	00	52	00	37
38	97	65	80	34	63	59	58	41	57	33	56	27	55	20	54	13	53	06	52	00	51	00	38
39	97	65	80	34	62	59	57	41	56	33	55	27	54	20	53	13	52	06	51	00	50	00	39
40	96	64	80	33	62	59	56	41	55	33	54	27	53	20	52	13	51	06	50	00	49	00	40
41	96	64	80	32	61	59	56	41	54	33	53	27	52	20	51	13	50	06	49	00	48	00	41
42	95	63	80	32	61	59	55	41	53	33	52	27	51	20	50	13	49	06	48	00	47	00	42
43	95	63	80	31	60	59	55	41	52	33	51	27	50	20	49	13	48	06	47	00	46	00	43
44	94	62	80	31	60	58	54	41	51	33	50	27	49	20	48	13	47	06	46	00	45	00	44
45	93	62	80	30	60	58	53	41	50	33	49	27	48	20	47	13	46	06	45	00	44	00	45
46	93	61	80	30	59	58	53	41	49	33	48	27	47	20	46	13	45	06	44	00	43	00	46
47	92	61	80	29	58	58	52	41	48	33	47	27	46	20	45	13	44	06	43	00	42	00	47
48	92	60	80	29	58	57	52	41	47	33	46	27	45	20	44	13	43	06	42	00	41	00	48
49	91	60	80	28	57	57	51	41	46	33	45	27	44	20	43	13	42	06	41	00	40	00	49
50	91	59	80	28	57	56	51	41	45	33	44	27	43	20	42	13	41	06	40	00	39	00	50
51	90	59	80	27	56	56	50	41	44	33	43	27	42	20	41	13	40	06	39	00	38	00	51
52	90	58	80	27	56	55	50	41	43	33	42	27	41	20	40	13	39	06	38	00	37	00	52
53	89	58	80	26	55	55	49	41	42	33	41	27	40	20	39	13	38	06	37	00	36	00	53
54	89	57	80	26	55	54	49	41	41	33	40	27	39	20	38	13	37	06	36	00	35	00	54
55	88	57	80	25	54	54	48	41	40	33	39	27	38	20	37	13	36	06	35	00	34	00	55
56	88	56	80	25	54	53	48	41	39	33	38	27	37	20	36	13	35	06	34	00	33	00	56
57	87	56	80	24	53	53	47	41	38	33	37	27	36	20	35	13	34	06	33	00	32	00	57
58	87	55	80	24	53	52	47	41	37	33	36	27	35	20	34	13	33	06	32	00	31	00	58
59	86	54	80	23	52	52	46	41	36	33	35	27	34	20	33	13	32	06	31	00	30	00	59

TABLE III.—PROPORTIONAL LOGARITHMS.

°	' 27'		' 28'		' 29'		' 30'		' 31'		' 32'		' 33'		' 34'		' 35'		' 36'		' 37'		°
	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	A	B	
0	0820	0850	0881	0792	0703	0734	0706	0678	0649	0621	0594	0	0	0	0	0	0	0	0	0	0	0	0
1	79	50	90	91	62	34	05	77	49	21	93	1	1	1	1	1	1	1	1	1	1	1	1
2	79	49	90	91	62	33	05	77	48	21	93	2	2	2	2	2	2	2	2	2	2	2	2
3	78	49	19	90	62	33	04	76	48	20	92	3	3	3	3	3	3	3	3	3	3	3	3
4	78	48	19	90	61	32	04	76	48	20	92	4	4	4	4	4	4	4	4	4	4	4	4
5	77	48	18	89	61	32	03	75	47	19	91	5	5	5	5	5	5	5	5	5	5	5	5
6	77	47	18	89	60	31	03	75	47	19	91	6	6	6	6	6	6	6	6	6	6	6	6
7	76	47	17	88	60	31	03	74	46	18	91	7	7	7	7	7	7	7	7	7	7	7	7
8	76	46	17	88	59	30	02	74	46	18	90	8	8	8	8	8	8	8	8	8	8	8	8
9	75	46	16	87	59	30	02	73	45	17	90	9	9	9	9	9	9	9	9	9	9	9	9
10	75	45	16	87	58	30	01	73	45	17	89	10	10	10	10	10	10	10	10	10	10	10	10
11	74	45	16	87	58	29	01	72	44	16	89	11	11	11	11	11	11	11	11	11	11	11	11
12	74	44	15	86	57	29	00	72	44	16	88	12	12	12	12	12	12	12	12	12	12	12	12
13	73	44	15	86	57	28	00	71	43	15	88	13	13	13	13	13	13	13	13	13	13	13	13
14	73	43	14	85	56	28	00	71	43	15	87	14	14	14	14	14	14	14	14	14	14	14	14
15	72	43	14	85	56	27	99	70	42	15	87	15	15	15	15	15	15	15	15	15	15	15	15
16	72	42	13	84	55	27	98	70	42	14	86	16	16	16	16	16	16	16	16	16	16	16	16
17	71	42	13	84	55	26	98	70	41	14	86	17	17	17	17	17	17	17	17	17	17	17	17
18	71	41	12	83	54	26	97	69	41	13	85	18	18	18	18	18	18	18	18	18	18	18	18
19	70	41	12	83	54	25	97	69	41	13	85	19	19	19	19	19	19	19	19	19	19	19	19
20	70	40	11	82	53	25	96	68	40	12	85	20	20	20	20	20	20	20	20	20	20	20	20
21	69	40	11	82	53	24	96	68	40	12	84	21	21	21	21	21	21	21	21	21	21	21	21
22	69	39	10	81	52	24	95	67	39	11	84	22	22	22	22	22	22	22	22	22	22	22	22
23	68	39	10	81	52	23	95	67	39	11	83	23	23	23	23	23	23	23	23	23	23	23	23
24	68	38	09	80	51	23	94	66	38	10	83	24	24	24	24	24	24	24	24	24	24	24	24
25	67	38	09	80	51	22	94	66	38	10	82	25	25	25	25	25	25	25	25	25	25	25	25
26	67	37	08	79	51	22	94	65	37	09	82	26	26	26	26	26	26	26	26	26	26	26	26
27	66	37	08	79	50	21	93	65	37	09	81	27	27	27	27	27	27	27	27	27	27	27	27
28	66	36	07	78	50	21	93	64	36	09	81	28	28	28	28	28	28	28	28	28	28	28	28
29	65	36	07	78	49	21	92	64	36	08	80	29	29	29	29	29	29	29	29	29	29	29	29
30	65	35	06	77	49	20	92	63	35	08	80	30	30	30	30	30	30	30	30	30	30	30	30
31	64	35	06	77	48	20	91	63	35	07	79	31	31	31	31	31	31	31	31	31	31	31	31
32	64	34	05	76	48	19	91	63	34	07	79	32	32	32	32	32	32	32	32	32	32	32	32
33	63	34	05	76	47	19	90	62	34	06	79	33	33	33	33	33	33	33	33	33	33	33	33
34	63	34	04	75	47	18	90	62	34	06	78	34	34	34	34	34	34	34	34	34	34	34	34
35	62	33	04	75	46	18	89	61	33	05	78	35	35	35	35	35	35	35	35	35	35	35	35
36	62	33	03	74	46	17	89	61	33	05	77	36	36	36	36	36	36	36	36	36	36	36	36
37	61	32	03	74	45	17	88	60	32	04	77	37	37	37	37	37	37	37	37	37	37	37	37
38	61	32	02	74	45	16	88	60	32	04	76	38	38	38	38	38	38	38	38	38	38	38	38
39	60	31	02	73	44	16	87	59	31	03	76	39	39	39	39	39	39	39	39	39	39	39	39
40	60	31	01	73	44	15	87	59	31	03	75	40	40	40	40	40	40	40	40	40	40	40	40
41	59	30	01	72	43	15	86	58	30	02	75	41	41	41	41	41	41	41	41	41	41	41	41
42	59	30	01	72	43	14	86	58	30	02	74	42	42	42	42	42	42	42	42	42	42	42	42
43	58	29	00	71	42	14	86	57	29	02	74	43	43	43	43	43	43	43	43	43	43	43	43
44	58	29	00	71	42	13	85	57	29	01	73	44	44	44	44	44	44	44	44	44	44	44	44
45	57	28	0799	70	41	13	85	56	28	01	73	45	45	45	45	45	45	45	45	45	45	45	45
46	57	28	99	70	41	12	84	56	28	00	73	46	46	46	46	46	46	46	46	46	46	46	46
47	56	27	98	69	40	12	84	55	28	00	72	47	47	47	47	47	47	47	47	47	47	47	47
48	56	27	98	69	40	11	83	55	27	0599	72	48	48	48	48	48	48	48	48	48	48	48	48
49	55	26	97	68	40	11	83	55	27	99	71	49	49	49	49	49	49	49	49	49	49	49	49
50	55	25	97	68	39	11	82	54	26	98	71	50	50	50	50	50	50	50	50	50	50	50	50
51	55	25	96	67	39	10	82	54	26	98	70	51	51	51	51	51	51	51	51	51	51	51	51
52	54	25	96	67	38	10	81	53	25	97	70	52	52	52	52	52	52	52	52	52	52	52	52
53	54	24	95	66	38	09	81	53	25	97	69	53	53	53	53	53	53	53	53	53	53	53	53
54	53	24	95	66	37	09	80	52	24	96	69	54	54	54	54	54	54	54	54	54	54	54	54
55	53	23	94	65	37	08	80	52	24	96	68	55	55	55	55	55	55	55	55	55	55	55	55
56	52	23	94	65	36	08	79	51	23	96	68	56	56	56	56	56	56	56	56	56	56	56	56
57	52	22	93	64	36	07	79	51	23	95	68	57	57	57	57	57	57	57	57	57	57	57	57
58	51	22	93	64	35	07	78	50	22	95	67	58	58	58	58	58	58	58	58	58	58	58	58
59	51	21	92	63	35	06	78	50	22	94	67	59	59	59	59	59	59	59	59	59	59	59	59
°	' 27'	' 28'	' 29'	' 30'	' 31'	' 32'	' 33'	' 34'	' 35'	' 36'	' 37'	°											

TABLE III.—PROPORTIONAL LOGARITHMS.

°	h m		h m		h m		h m		h m		h m		h m		°
	30'	30'	40'	41'	49'	43'	44'	45'	46'	47'	48'	47'	48'		
0	0566	0530	0512	0494	0458	0431	0404	0378	0352	0326	0300			0	
1	66	36	11	84	57	30	04	77	51	25	99			1	
2	65	36	11	84	57	30	03	77	51	25	99			2	
3	65	37	10	83	56	30	03	77	50	24	98			3	
4	64	37	10	83	56	29	03	76	50	24	98			4	
5	64	36	09	82	55	29	02	76	49	23	97			5	
6	63	36	09	82	55	28	02	75	49	23	97			6	
7	63	36	08	81	54	28	01	75	49	23	97			7	
8	62	35	08	81	54	27	01	74	48	22	96			8	
9	62	35	07	80	54	27	00	74	48	22	96			9	
10	62	34	07	80	53	26	00	74	47	21	95			10	
11	61	34	07	80	53	26	0399	73	47	21	95			11	
12	61	33	06	79	52	26	90	73	46	20	94			12	
13	60	33	06	79	52	25	99	72	46	20	94			13	
14	60	32	05	78	51	25	98	72	46	19	94			14	
15	59	32	05	78	51	24	98	71	45	19	93			15	
16	59	31	04	77	50	24	97	71	45	19	93			16	
17	58	31	04	77	50	23	97	70	44	18	92			17	
18	58	31	03	76	50	23	96	70	44	18	92			18	
19	57	30	03	76	49	22	96	70	43	17	91			19	
20	57	30	02	75	49	22	95	69	43	17	91			20	
21	57	29	02	75	48	22	95	69	42	16	91			21	
22	56	29	02	75	48	21	95	68	42	16	90			22	
23	56	28	01	74	47	21	94	68	42	16	90			23	
24	55	28	01	74	47	21	94	67	41	15	89			24	
25	55	27	00	73	46	20	93	67	41	15	89			25	
26	54	27	00	73	46	19	93	66	40	14	88			26	
27	54	26	0099	72	46	19	92	66	40	14	88			27	
28	53	26	99	72	45	18	92	66	39	13	88			28	
29	53	26	98	71	45	18	92	65	39	13	87			29	
30	52	25	98	71	44	18	91	65	39	13	87			30	
31	52	25	98	71	44	17	91	64	38	12	86			31	
32	52	24	97	70	43	17	90	64	38	12	86			32	
33	51	24	97	70	43	16	90	63	37	11	85			33	
34	51	23	96	69	42	16	89	63	37	11	85			34	
35	50	23	96	69	42	15	89	63	36	10	85			35	
36	50	22	95	68	42	15	88	62	36	10	84			36	
37	49	22	95	68	41	14	88	62	36	10	84			37	
38	49	21	94	67	41	14	88	61	35	09	83			38	
39	48	21	94	67	40	14	87	61	35	09	83			39	
40	48	21	93	67	40	13	87	60	34	08	82			40	
41	47	20	93	66	39	13	86	60	34	08	82			41	
42	47	20	93	66	39	12	86	59	33	07	82			42	
43	46	19	92	65	38	12	85	59	33	07	81			43	
44	46	19	92	65	38	11	85	59	33	07	81			44	
45	46	18	91	64	38	11	84	58	32	06	80			45	
46	45	18	91	64	37	10	84	58	32	06	80			46	
47	45	17	90	63	37	10	84	57	31	05	79			47	
48	44	17	90	63	36	10	83	57	31	05	79			48	
49	44	17	89	62	36	09	83	56	30	04	79			49	
50	43	16	89	62	35	09	82	56	30	04	78			50	
51	43	16	89	62	35	08	82	56	29	04	78			51	
52	42	15	88	61	34	08	81	55	29	03	77			52	
53	42	15	88	61	34	07	81	55	29	03	77			53	
54	41	14	87	60	34	07	81	54	28	02	76			54	
55	41	14	87	60	33	06	80	54	28	02	76			55	
56	41	13	86	59	33	06	80	53	27	01	76			56	
57	40	13	86	59	32	06	79	53	27	01	75			57	
58	40	12	85	58	32	05	79	52	26	00	75			58	
59	39	12	85	58	31	05	78	52	26	00	74			59	

TABLE III.—PROPORTIONAL LOGARITHMS.

"	h = 30 49'	h = 30 50'	h = 30 51'	h = 30 52'	h = 30 53'	h = 30 54'	h = 30 55'	h = 30 56'	h = 30 57'	h = 30 58'	h = 30 59'	"
0	0274	0248	0223	0197	0173	0147	0122	0098	0073	0049	0024	0
1	73	48	23	97	73	47	22	97	73	48	24	1
2	73	47	23	97	71	46	22	97	73	48	23	2
3	73	47	21	96	71	46	21	96	73	47	23	3
4	72	47	21	96	71	46	21	96	71	47	23	4
5	72	46	21	95	70	45	20	96	71	46	22	5
6	71	46	20	95	70	45	20	95	71	46	22	6
7	71	45	20	94	69	44	19	95	70	45	21	7
8	70	45	19	94	69	44	19	94	70	45	21	8
9	70	44	19	94	69	43	19	94	69	45	21	9
10	70	44	19	93	68	43	18	93	69	44	20	10
11	69	44	18	93	68	43	18	93	68	44	20	11
12	69	43	18	92	67	42	17	93	68	44	19	12
13	68	43	17	92	67	42	17	92	68	43	19	13
14	68	42	17	92	66	41	17	92	67	43	19	14
15	67	42	16	91	66	41	16	91	67	42	18	15
16	67	41	16	91	66	41	16	91	66	42	18	16
17	67	41	16	90	65	40	15	91	66	42	17	17
18	66	41	15	90	65	40	15	90	66	41	17	18
19	66	40	15	89	64	39	14	90	65	41	17	19
20	65	40	14	89	64	39	14	89	65	40	16	20
21	65	39	14	89	63	38	14	89	64	40	16	21
22	64	39	13	88	63	38	13	89	64	40	15	22
23	64	38	13	88	63	38	13	88	64	39	15	23
24	64	38	13	87	62	37	12	88	63	39	15	24
25	63	38	12	87	62	37	12	87	63	38	14	25
26	63	37	12	87	61	36	12	87	62	38	14	26
27	62	37	11	86	61	36	11	87	62	38	13	27
28	62	36	11	86	61	36	11	86	62	37	13	28
29	61	36	11	85	60	35	10	86	61	37	12	29
30	61	35	10	85	60	35	10	85	61	36	12	30
31	61	35	10	84	59	34	10	85	60	36	12	31
32	60	35	09	84	59	34	09	84	60	36	11	32
33	60	34	09	84	58	34	09	84	60	35	11	33
34	60	34	08	83	58	33	08	84	59	35	10	34
35	59	33	08	83	58	33	08	83	59	34	10	35
36	59	33	08	82	57	32	07	83	58	34	10	36
37	58	33	07	82	57	32	07	82	58	34	09	37
38	58	32	07	81	56	31	07	82	57	33	09	38
39	57	32	06	81	56	31	06	82	57	33	08	39
40	57	31	06	81	56	31	06	81	57	32	08	40
41	56	31	05	80	55	30	05	81	56	32	08	41
42	56	30	05	80	55	30	05	80	56	31	07	42
43	55	30	05	79	54	29	05	80	55	31	07	43
44	55	30	04	79	54	29	04	80	55	31	06	44
45	55	29	04	79	53	29	04	79	55	30	06	45
46	54	29	03	78	53	28	03	79	54	30	06	46
47	54	28	03	78	53	28	03	78	54	29	05	47
48	53	28	02	77	52	27	03	78	53	29	05	48
49	53	27	02	77	52	27	02	77	53	29	04	49
50	52	27	02	76	51	26	02	77	53	28	04	50
51	52	27	01	76	51	26	01	77	52	28	04	51
52	52	26	01	76	51	26	01	76	52	27	03	52
53	51	26	00	75	50	25	00	76	51	27	03	53
54	51	25	00	75	50	25	00	75	51	27	02	54
55	50	25	00	74	49	24	00	75	50	26	02	55
56	50	24	00	74	49	24	00	75	50	26	02	56
57	50	24	99	74	48	24	99	74	50	25	01	57
58	49	24	98	73	48	23	98	74	49	25	01	58
59	49	23	98	73	48	23	98	73	49	25	00	59

TABLE IV.

**COURSES, DISTANCE, DEPARTURE, AND
DIFFERENCE OF LATITUDE.**

Distance.	C. † Pt.		C. † Pt.		C. † Pt.		C. † Pt.		C. † Pt.		C. † Pt.		C. † Pt.		C. † Pt.	
	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.	N. † E.	S. † W.
	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
1	1	0	1	.1	1	0.1	1	0	1	0.2	1	0	1	0	1	0
2	2	0.1	2	0.2	2	0.3	2	0.4	2	0.5	2	0.6	2	0.7	2	0.8
3	3	0.1	3	0.3	3	0.4	3	0.5	3	0.6	3	0.7	3	0.8	3	0.9
4	4	0.2	4	0.4	4	0.6	4	0.8	4	1.0	4	1.2	4	1.4	4	1.6
5	5	0.2	5	0.5	5	0.7	5	0.9	5	1.1	5	1.3	5	1.5	5	1.7
6	6	0.3	6	0.6	6	0.9	6	1.2	6	1.5	6	1.8	6	2.1	6	2.4
7	7	0.3	7	0.7	7	0.9	7	1.1	7	1.4	7	1.7	7	2.0	7	2.3
8	8	0.4	8	0.8	8	1.2	8	1.5	8	1.8	8	2.1	8	2.4	8	2.7
9	9	0.4	9	0.9	9	1.3	9	1.6	9	1.9	9	2.2	9	2.5	9	2.8
10	10	0.5	10	1	10	1.5	10	2	10	2.5	10	3	10	3.5	10	4
11	11	0.5	10.9	1.1	10.9	1.6	10.8	2.1	10.7	2.7	10.5	3.2	10.4	3.7	10.2	4.2
12	12	0.6	11.9	1.2	11.9	1.8	11.8	2.3	11.6	2.9	11.5	3.5	11.3	4	11.1	4.6
13	13	0.6	12.9	1.3	12.9	1.9	12.8	2.5	12.6	3.2	12.4	3.8	12.2	4.4	12	5
14	14	0.7	13.9	1.4	13.8	2.1	13.7	2.7	13.6	3.4	13.4	4.1	13.2	4.7	12.9	5.4
15	15	0.7	14.9	1.5	14.8	2.2	14.7	2.9	14.6	3.6	14.4	4.4	14.1	5.1	13.9	5.7
16	16	0.8	15.9	1.6	15.8	2.3	15.7	3.1	15.5	3.9	15.3	4.6	15.1	5.4	14.9	6.1
17	17	0.8	16.9	1.7	16.8	2.5	16.7	3.3	16.5	4.1	16.3	4.9	16.1	5.7	15.9	6.5
18	18	0.9	17.9	1.8	17.8	2.6	17.7	3.5	17.5	4.4	17.3	5.2	17.1	6.1	16.9	6.9
19	19	0.9	18.9	1.9	18.8	2.8	18.6	3.7	18.4	4.6	18.2	5.5	17.9	6.4	17.7	7.1
20	20	1	19.9	2	19.8	2.9	19.6	3.9	19.4	4.9	19.1	5.8	18.8	6.7	18.5	7.7
21	21	1	20.9	2.1	20.8	3.1	20.6	4.1	20.4	5.1	20.1	6.1	19.8	7.1	19.4	8
22	22	1.1	21.9	2.2	21.8	3.3	21.6	4.3	21.3	5.3	21.1	6.4	20.7	7.4	20.3	8.4
23	23	1.1	22.9	2.3	22.8	3.4	22.6	4.5	22.3	5.5	22	6.6	21.7	7.7	21.3	8.4
24	24	1.2	23.9	2.4	23.7	3.5	23.5	4.7	23.3	5.8	23	7	22.6	8.1	22.2	9.2
25	25	1.2	24.9	2.5	24.7	3.7	24.5	4.9	24.3	6.1	23.9	7.3	23.5	8.4	23.1	9.6
26	26	1.3	25.9	2.6	25.7	3.8	25.5	5.1	25.2	6.3	24.9	7.5	24.5	8.8	24.1	9.9
27	27	1.3	26.9	2.7	26.7	4	26.5	5.3	26.2	6.6	25.8	7.9	25.4	9.1	24.9	10.1
28	28	1.4	27.9	2.8	27.7	4.1	27.5	5.5	27.2	6.8	26.8	8.1	26.4	9.4	25.9	10.7
29	29	1.4	28.9	2.8	28.7	4.3	28.4	5.7	28.1	7	27.8	8.4	27.3	9.6	26.9	11.1
30	30	1.5	29.9	2.9	29.7	4.4	29.4	5.9	29.1	7.3	28.7	8.7	28.2	10.1	27.7	11.5
31	31	1.5	30.8	3	30.7	4.5	30.4	6	30.1	7.5	29.7	9	29.2	10.4	28.6	11.9
32	32	1.6	31.8	3.1	31.7	4.7	31.4	6.2	31.1	7.8	30.6	9.3	30.1	10.8	29.5	12.2
33	33	1.6	32.8	3.2	32.6	4.8	32.4	6.4	32	8	31.6	9.6	31.1	11.1	30.5	12.6
34	34	1.7	33.8	3.3	33.6	5	33.3	6.6	33	8.3	32.5	9.9	32	11.5	31.4	13
35	35	1.7	34.8	3.4	34.6	5.1	34.3	6.8	34	8.5	33.5	10.2	33	11.8	32.3	13.4
36	36	1.8	35.8	3.5	35.6	5.3	35.3	7	34.9	8.7	34.4	10.5	33.9	12.1	33.3	13.8
37	37	1.8	36.8	3.6	36.6	5.4	36.3	7.2	35.9	9	35.4	10.7	34.8	12.5	34.2	14.2
38	38	1.9	37.8	3.7	37.6	5.6	37.3	7.4	36.9	9.2	36.4	11	35.6	12.9	35.1	14.5
39	39	1.9	38.8	3.8	38.6	5.7	38.3	7.6	37.8	9.5	37.3	11.3	36.7	13.1	36	14.9
40	40	2	39.8	3.9	39.6	5.9	39.2	7.8	38.8	9.7	38.3	11.6	37.7	13.5	37	15.3
41	41	2	40.8	4	40.6	6	40.2	8	39.8	10	39.2	11.9	38.6	13.9	37.9	15.7
42	41.9	2.1	41.8	4.1	41.5	6.2	41.2	8.2	40.7	10.2	40.2	12.3	39.5	14.1	38.8	16.1
43	42.9	2.1	42.8	4.2	42.5	6.3	42.2	8.4	41.7	10.4	41.1	12.5	40.5	14.5	39.7	16.5
44	43.9	2.2	43.8	4.3	43.5	6.5	43.2	8.6	42.7	10.7	42.1	12.8	41.4	14.9	40.7	16.9
45	44.9	2.2	44.8	4.4	44.5	6.6	44.1	8.8	43.7	10.9	43.1	13.1	42.4	15.2	41.6	17.3
46	45.9	2.3	45.8	4.5	45.5	6.7	45.1	9	44.6	11.2	44	13.4	43.3	15.5	42.4	17.6
47	46.9	2.3	46.8	4.6	46.5	6.9	46.1	9.2	45.0	11.4	44.4	13.6	44.2	15.8	43.3	18
48	47.9	2.4	47.8	4.7	47.5	7	47.1	9.4	46.0	11.7	45.3	13.9	45.1	16.1	44.2	18.4
49	48.9	2.4	48.8	4.8	48.5	7.2	48.1	9.6	47.0	11.9	46.2	14.2	46.0	16.4	45.1	18.8
50	49.9	2.5	49.8	4.9	49.5	7.3	49	9.8	48.0	12.1	47.1	14.5	47.0	16.8	46.0	19.1
	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.	W. † N.	W. † S.
	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 7 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.	C. 6 † Pts.

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.		Distance.				
N. N. E. † E.	S. S. E. † E.	S. S. W. † W.	N. N. W. † W.	N. N. E. † E.	S. S. E. † E.	S. S. W. † W.	N. N. W. † W.	N. E. by N.	S. E. by S.	S. W. by S.	N. W. by N.	N. E. † N.	S. E. † S.	S. W. † S.	N. W. † N.		N. E.	S. E.	S. W.	N. W.
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	
0.0	0.0	0.9	0.5	0.9	0.5	0.8	0.6	0.8	0.6	0.8	0.6	0.8	0.6	0.7	0.7					1
1.6	0.4	1.8	0.9	1.7	1.1	1.7	1.1	1.6	1.2	1.5	1.3	1.5	1.3	1.5	1.3					2
3.2	0.9	3.6	1.4	3.4	1.5	3.4	1.5	3.2	1.6	3.1	1.9	3.2	1.9	3.1	1.9					3
4.6	1.3	5.0	1.9	4.4	2.4	4.3	2.6	4.2	2.6	4.0	2.6	3.9	2.9	3.7	2.9					4
5.9	1.7	6.3	2.4	5.7	3.3	5.6	3.3	5.4	3.3	5.2	3.6	5.1	3.6	4.9	3.6					5
7.2	2.1	7.6	2.8	7.0	3.8	6.9	4.1	6.7	4.1	6.4	4.8	6.3	4.8	6.1	4.8					6
8.5	2.5	8.9	3.3	8.3	4.7	8.2	4.6	7.9	5.4	7.7	5.4	7.5	5.4	7.3	5.4					7
9.8	2.9	10.2	3.8	9.6	5.1	9.5	5.1	9.2	5.6	9.0	5.6	8.8	5.6	8.6	5.6					8
11.1	3.3	11.5	4.3	10.9	5.7	10.8	5.7	10.5	6.1	10.3	6.1	10.1	6.1	9.9	6.1					9
12.4	3.7	12.8	4.8	12.2	6.2	12.1	6.2	11.8	6.6	11.6	6.6	11.4	6.6	11.2	6.6					10
13.7	4.1	14.1	5.3	13.5	6.7	13.4	6.7	13.0	7.1	12.8	7.1	12.6	7.1	12.4	7.1					11
15.0	4.5	15.4	5.8	14.8	7.2	14.7	7.2	14.3	7.5	14.1	7.5	13.9	7.5	13.7	7.5					12
16.3	4.9	16.7	6.3	16.1	7.7	16.0	7.7	15.6	8.0	15.4	8.0	15.2	8.0	15.0	8.0					13
17.6	5.3	18.0	6.8	17.4	8.2	17.3	8.2	16.9	8.3	16.7	8.3	16.5	8.3	16.3	8.3					14
18.9	5.7	19.3	7.3	18.7	8.7	18.6	8.7	18.2	8.8	18.0	8.8	17.8	8.8	17.6	8.8					15
20.2	6.1	20.6	7.8	20.0	9.2	19.9	9.2	19.5	9.3	19.3	9.3	19.1	9.3	18.9	9.3					16
21.5	6.5	21.9	8.3	21.3	9.7	21.2	9.7	20.8	9.8	20.6	9.8	20.4	9.8	20.2	9.8					17
22.8	6.9	23.2	8.8	22.6	10.2	22.5	10.2	22.1	10.3	21.9	10.3	21.7	10.3	21.5	10.3					18
24.1	7.3	24.5	9.3	23.9	10.7	23.8	10.7	23.4	10.8	23.2	10.8	23.0	10.8	22.8	10.8					19
25.4	7.7	25.8	9.8	25.2	11.2	25.1	11.2	24.7	11.3	24.5	11.3	24.3	11.3	24.1	11.3					20
26.7	8.1	27.1	10.3	26.5	11.7	26.4	11.7	26.0	11.8	25.8	11.8	25.6	11.8	25.4	11.8					21
28.0	8.5	28.4	10.8	27.8	12.2	27.7	12.2	27.3	12.3	27.1	12.3	26.9	12.3	26.7	12.3					22
29.3	8.9	29.7	11.3	29.1	12.7	29.0	12.7	28.6	12.8	28.4	12.8	28.2	12.8	28.0	12.8					23
30.6	9.3	31.0	11.8	30.4	13.2	30.3	13.2	29.9	12.9	29.7	12.9	29.5	12.9	29.3	12.9					24
31.9	9.7	32.3	12.3	31.7	13.7	31.6	13.7	31.2	13.8	31.0	13.8	30.8	13.8	30.6	13.8					25
33.2	10.1	33.6	12.8	33.0	14.2	32.9	14.2	32.5	14.3	32.3	14.3	32.1	14.3	31.9	14.3					26
34.5	10.5	34.9	13.3	34.3	14.7	34.2	14.7	33.8	14.4	33.6	14.4	33.4	14.4	33.2	14.4					27
35.8	10.9	36.2	13.8	35.6	15.2	35.5	15.2	35.1	14.5	34.9	14.5	34.7	14.5	34.5	14.5					28
37.1	11.3	37.5	14.3	36.9	15.7	36.8	15.7	36.4	14.6	36.2	14.6	36.0	14.6	35.8	14.6					29
38.4	11.7	38.8	14.8	38.2	16.2	38.1	16.2	37.7	14.7	37.5	14.7	37.3	14.7	37.1	14.7					30
39.7	12.1	40.1	15.3	39.5	16.7	39.4	16.7	39.0	14.8	38.8	14.8	38.6	14.8	38.4	14.8					31
41.0	12.5	41.4	15.8	40.8	17.2	40.7	17.2	40.3	14.9	40.1	14.9	39.9	14.9	39.7	14.9					32
42.3	12.9	42.7	16.3	42.1	17.7	42.0	17.7	41.6	15.0	41.4	15.0	41.2	15.0	41.0	15.0					33
43.6	13.3	44.0	16.8	43.4	18.2	43.3	18.2	42.9	15.1	42.7	15.1	42.5	15.1	42.3	15.1					34
44.9	13.7	45.3	17.3	44.7	18.7	44.6	18.7	44.2	15.2	44.0	15.2	43.8	15.2	43.6	15.2					35
46.2	14.1	46.6	17.8	46.0	19.2	45.9	19.2	45.5	15.3	45.3	15.3	45.1	15.3	44.9	15.3					36
47.5	14.5	47.9	18.3	47.3	19.7	47.2	19.7	46.8	15.4	46.6	15.4	46.4	15.4	46.2	15.4					37
48.8	14.9	49.2	18.8	48.6	20.2	48.5	20.2	48.1	15.5	47.9	15.5	47.7	15.5	47.5	15.5					38
50.1	15.3	50.5	19.3	49.9	20.7	49.8	20.7	49.4	15.6	49.2	15.6	49.0	15.6	48.8	15.6					39
51.4	15.7	51.8	19.8	51.2	21.2	51.1	21.2	50.7	15.7	50.5	15.7	50.3	15.7	50.1	15.7					40
52.7	16.1	53.1	20.3	52.5	21.7	52.4	21.7	52.0	15.8	51.8	15.8	51.6	15.8	51.4	15.8					41
54.0	16.5	54.4	20.8	53.8	22.2	53.7	22.2	53.3	15.9	53.1	15.9	52.9	15.9	52.7	15.9					42
55.3	16.9	55.7	21.3	55.1	22.7	55.0	22.7	54.6	16.0	54.4	16.0	54.2	16.0	54.0	16.0					43
56.6	17.3	57.0	21.8	56.4	23.2	56.3	23.2	55.9	16.1	55.7	16.1	55.5	16.1	55.3	16.1					44
57.9	17.7	58.3	22.3	57.7	23.7	57.6	23.7	57.2	16.2	57.0	16.2	56.8	16.2	56.6	16.2					45
59.2	18.1	59.6	22.8	59.0	24.2	58.9	24.2	58.5	16.3	58.3	16.3	58.1	16.3	57.9	16.3					46
60.5	18.5	60.9	23.3	60.3	24.7	60.2	24.7	59.8	16.4	59.6	16.4	59.4	16.4	59.2	16.4					47
61.8	18.9	62.2	23.8	61.6	25.2	61.5	25.2	61.1	16.5	60.9	16.5	60.7	16.5	60.5	16.5					48
63.1	19.3	63.5	24.3	62.9	25.7	62.8	25.7	62.4	16.6	62.2	16.6	62.0	16.6	61.8	16.6					49
64.4	19.7	64.8	24.8	64.2	26.2	64.1	26.2	63.7	16.7	63.5	16.7	63.3	16.7	63.1	16.7					50
65.7	20.1	66.1	25.3	65.5	26.7	65.4	26.7	65.0	16.8	64.8	16.8	64.6	16.8	64.4	16.8					51
67.0	20.5	67.4	25.8	66.8	27.2	66.7	27.2	66.3	16.9	66.1	16.9	65.9	16.9	65.7	16.9					52
68.3	20.9	68.7	26.3	68.1	27.7	68.0	27.7	67.6	17.0	67.4	17.0	67.2	17.0	67.0	17.0					53
69.6	21.3	70.0	26.8	69.4	28.2	69.3	28.2	69.0	17.1	68.8	17.1	68.6	17.1	68.4	17.1					54
70.9	21.7	71.3	27.3	70.7	28.7	70.6	28.7	70.2	17.2	70.0	17.2	69.8	17.2	69.6	17.2					55
72.2	22.1	72.6	27.8	72.0	29.2	71.9	29.2	71.5	17.3	71.3	17.3	71.1	17.3	70.9	17.3					56
73.5	22.5	73.9	28.3	73.3	29.7	73.2	29.7	72.8	17.4	72.6	17.4	72.4	17.4	72.2	17.4					57
74.8	22.9	75.2	28.8	74.6	30.2	74.5	30.2	74.1	17.5	73.9	17.5	73.7	17.5	73.5	17.5					58
76.1	23.3	76.5	29.3	75.9	30.7	75.8	30.7	75.4	17.6	75.2	17.6	75.0	17.6	74.8	17.6					59
77.4	23.7	77.8	29.8	77.2	31.2	77.1	31.2	76.7	17.7	76.5	17.7	76.3	17.7	76.1	17.7					60
78.7	24.1	79.1	30.3	78.5	31.7	78.4	31.7	78.0	17.8	77.8	17.8	77.6	17.8	77.4	17.8					61
80.0	24.5	80.4	30.8	79.8	32.2	79.7	32.2	79.3	17.9	79.1	17.9	78.9	17.9	78.7	17.9					62
81.3	24.9	81.7	31.3	81.1	32.7	81.0	32.7	80.6	18.0	80.4	18.0	80.2	18.0	80.0	18.0					63
82.6	25.3	83.0	31.8	82.4	33.2	82.3	33.2	81.9	18.1	81.7	18.1	81.5	18.1	81.3	18.1					64
83.9	25.7	84.3	32.3	83.7	33.7	83.6	33.7	83.2	18.2	83.0	18.2	82.8	18.2	82.6	18.2					65
85.2	26.1	85.6	32.8	85.0	34.2	84.9	34.2	84.5	18.3	84.3	18.3	84.1	18.3	83.9	18.3					66
86.5	26.5	86.9	33.3	86.3	34.7	86.2	34.7	85.8	18.4	85.6	18.4	85.4	18.4	85.2	18.4					67
87.8	26.9	88.2	33.8	87.6	35.2	87.5	35.2	87.1	18.5	86.9	18.5	86.7	18.5	86.5	18.5					68
89.1	27.3	89.5	34.3	88.9	35.7	88.8	35.7	88.4	18.6	88.2	18.6	88.0	18.6	87.8	18.6					69
90.4	27.7	90.8																		

Distance.	C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 2 Pts.	
	C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 2 Pts.	
	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.
51	50.9	9.9	50.8	8.8	50.4	7.5	50.	9.9	49.5	12.4	48.8	14.8	48.	17.2
52	51.9	9.5	51.7	8.4	51.4	7.6	51.	10.1	50.4	12.6	49.8	15.1	49.	17.5
53	52.9	9.2	52.7	8.1	52.4	7.8	52.	10.3	51.4	12.9	50.7	15.4	49.	17.9
54	53.9	8.9	53.7	7.8	53.4	7.9	53.	10.5	52.4	13.1	51.7	15.7	50.6	18.2
55	54.9	8.7	54.7	7.4	54.4	8.1	53.9	10.7	53.4	13.4	52.6	16.	51.6	18.5
56	55.9	8.7	55.7	7.5	55.4	8.2	54.9	10.9	54.3	13.6	53.6	16.3	52.7	18.9
57	56.9	8.6	56.7	7.6	56.4	8.4	55.9	11.1	55.3	13.8	54.5	16.5	53.7	19.2
58	57.9	8.6	57.7	7.7	57.4	8.5	56.9	11.3	56.3	14.1	55.5	16.8	54.6	19.5
59	58.9	8.5	58.7	7.8	58.4	8.7	57.9	11.5	57.3	14.3	56.5	17.1	55.6	19.8
60	59.9	8.5	59.7	7.9	59.4	8.8	58.9	11.7	58.2	14.6	57.4	17.4	56.6	20.1
61	60.9	8.4	60.7	8.	60.3	9.	59.8	11.9	59.2	14.8	58.4	17.7	57.4	20.6
62	61.9	8.4	61.7	8.1	61.3	9.1	60.8	12.1	60.2	15.1	59.3	18.	58.4	20.9
63	62.9	8.3	62.7	8.2	62.3	9.2	61.8	12.3	61.1	15.3	60.3	18.3	59.3	21.2
64	63.9	8.3	63.7	8.3	63.3	9.4	62.8	12.5	62.1	15.6	61.2	18.6	60.3	21.6
65	64.9	8.2	64.7	8.4	64.3	9.5	63.8	12.7	63.1	15.8	62.1	18.9	61.2	21.9
66	65.9	8.2	65.7	8.5	65.3	9.7	64.7	12.9	64.	16.	63.2	19.2	62.1	22.2
67	66.9	8.2	66.7	8.6	66.3	9.8	65.7	13.1	65.	16.3	64.1	19.4	63.1	22.6
68	67.9	8.1	67.7	8.7	67.3	10.	66.7	13.3	66.	16.5	65.1	19.7	64.	22.9
69	68.9	8.1	68.7	8.8	68.3	10.1	67.7	13.5	66.9	16.8	66.	20.	65.	23.2
70	69.9	8.1	69.7	8.9	69.3	10.3	68.7	13.7	67.9	17.	67.	20.3	66.	23.6
71	70.9	8.1	70.7	9.	70.3	10.4	69.6	13.9	68.9	17.3	67.9	20.6	66.8	23.9
72	71.9	8.0	71.7	9.1	71.3	10.6	70.6	14.	69.8	17.5	68.9	20.9	67.8	24.3
73	72.9	8.0	72.7	9.2	72.3	10.7	71.6	14.2	70.8	17.7	68.9	21.2	68.7	24.6
74	73.9	8.0	73.7	9.3	73.3	10.9	72.6	14.4	71.8	18.	70.8	21.5	69.7	24.9
75	74.9	8.0	74.7	9.4	73.9	11.	73.6	14.6	72.8	18.2	71.8	21.8	70.6	25.3
76	75.9	8.0	75.7	9.5	75.3	11.2	74.5	14.8	73.7	18.5	72.7	22.1	71.6	25.6
77	76.9	8.0	76.7	9.6	76.3	11.3	75.5	15.	74.7	18.7	73.7	22.4	72.5	25.9
78	77.9	8.0	77.7	9.7	77.3	11.4	76.5	15.2	75.7	19.	74.6	22.6	73.4	26.3
79	78.9	8.0	78.7	9.8	77.9	11.6	77.5	15.4	76.6	19.2	75.6	22.9	74.4	26.6
80	79.9	8.0	79.7	9.9	79.1	11.7	78.5	15.6	77.6	19.4	76.6	23.2	75.3	27.
81	80.9	8.0	80.6	10.	80.1	11.9	79.4	15.8	78.6	19.7	77.5	23.5	76.3	27.3
82	81.9	8.0	81.6	10.1	81.1	12.	80.4	16.	79.5	19.9	78.5	23.8	77.2	27.6
83	82.9	8.0	82.6	10.2	82.1	12.2	81.4	16.2	80.5	20.2	79.4	24.1	78.1	27.9
84	83.9	8.0	83.6	10.3	83.1	12.3	82.4	16.4	81.5	20.4	80.4	24.4	79.1	28.2
85	84.9	8.0	84.6	10.4	84.1	12.5	83.4	16.6	82.5	20.7	81.3	24.7	80.	28.6
86	85.9	8.0	85.6	10.5	85.1	12.6	84.3	16.8	83.4	20.9	82.3	25.	81.	29.
87	86.9	8.0	86.6	10.6	86.1	12.8	85.3	17.	84.4	21.1	83.3	25.3	82.	29.3
88	87.9	8.0	87.6	10.7	87.	12.9	86.3	17.2	85.4	21.4	84.3	25.5	83.	29.6
89	88.9	8.0	88.6	10.8	88.	13.1	87.3	17.4	86.4	21.6	85.3	25.8	84.	29.9
90	89.9	8.0	89.6	10.9	89.	13.2	88.3	17.6	87.3	21.9	86.1	26.1	85.	30.2
91	90.9	8.0	90.6	11.	90.	13.4	89.3	17.8	88.3	22.1	87.1	26.4	86.	30.6
92	91.9	8.0	91.6	11.1	91.	13.5	90.2	17.9	89.2	22.4	88.	26.7	87.	31.
93	92.9	8.0	92.6	11.2	92.	13.6	91.2	18.1	90.2	22.6	89.	27.	88.	31.4
94	93.9	8.0	93.5	11.3	93.	13.8	92.2	18.3	91.2	22.8	90.	27.3	89.	31.7
95	94.9	8.0	94.5	11.4	94.	13.9	93.2	18.5	92.2	23.1	90.9	27.6	90.	32.
96	95.9	8.0	95.5	11.5	95.	14.1	94.2	18.7	93.1	23.3	91.9	27.9	91.	32.3
97	96.9	8.0	96.5	11.6	96.	14.2	95.1	18.9	94.1	23.6	92.8	28.2	92.	32.6
98	97.9	8.0	97.5	11.7	97.	14.4	96.1	19.1	95.1	23.8	93.8	28.4	93.	32.9
99	98.9	8.0	98.5	11.8	98.	14.5	97.1	19.3	96.	24.1	94.7	28.7	94.	33.2
100	99.9	8.0	99.5	11.9	99.	14.7	98.1	19.5	97.	24.3	95.7	29.	95.	33.5

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.		Distance.					
N. N. E. † E.	S. S. E. † E.	S. E. W. † W.	N. N. W. † W.	N. N. E. † E.	S. S. E. † E.	S. E. W. † W.	N. N. W. † W.	N. N. E. † N.	S. E. † S.	S. W. † S.	N. W. † N.	N. E. † N.	S. E. † S.	S. W. † S.	N. W. † N.		N. E. † E.	S. E. † E.	S. W. † W.	N. W. † W.	
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
46.1	21.6	45.	24.	43.7	26.9	42.4	29.3	41.1	30.4	39.4	32.4	37.8	34.9	36.1	36.1	51					
47.0	22.7	45.9	24.5	44.4	28.2	43.2	30.7	41.8	31.	40.2	33.	38.5	34.9	36.8	36.8	52					
47.8	23.7	46.7	25.	45.1	29.1	44.1	31.4	42.6	31.6	41.	33.6	39.3	35.6	37.5	37.5	53					
48.6	24.1	47.6	25.5	45.8	30.5	44.9	32.	43.4	32.9	41.7	34.3	40.2	36.3	38.2	38.2	54					
49.7	25.5	48.5	26.9	47.	31.8	45.7	33.6	44.2	33.8	42.5	34.9	40.8	36.9	38.9	38.9	55					
50.6	26.9	49.4	28.4	48.	33.1	46.6	34.1	45.	33.4	43.3	35.5	41.5	37.6	39.6	39.6	56					
51.5	28.4	50.3	29.9	48.9	34.5	47.4	34.7	45.8	34.	44.1	36.2	42.2	38.3	40.3	40.3	57					
52.4	29.8	51.3	31.4	49.8	35.9	48.3	35.2	46.6	34.6	44.8	36.9	43.1	39.1	41.	41.	58					
53.3	31.2	52.3	32.9	50.7	37.3	49.2	35.8	47.4	35.1	45.6	37.4	43.7	39.6	41.7	41.7	59					
54.2	32.7	53.2	34.3	51.5	38.8	50.1	36.3	48.2	35.7	46.4	38.1	44.5	40.3	42.4	42.4	60					
55.1	34.1	54.1	35.8	52.4	40.2	51.1	41.4	49.	36.3	47.2	38.7	45.2	41.	43.1	43.1	61					
56.	35.5	55.1	37.3	53.3	41.7	52.1	42.4	49.8	36.9	47.9	39.3	45.9	41.6	43.8	43.8	62					
57.9	36.9	56.1	38.8	54.2	43.1	53.1	43.4	50.6	37.5	48.7	40.	46.7	42.3	44.5	44.5	63					
58.8	37.4	57.1	40.3	55.1	44.5	54.1	44.4	51.4	38.1	49.5	40.6	47.4	43.	45.3	45.3	64					
59.7	38.9	58.1	41.8	56.1	45.9	55.1	45.4	52.3	38.7	50.2	41.2	48.2	43.7	46.	46.	65					
60.6	40.3	59.1	43.3	57.1	47.3	56.1	46.4	53.	39.3	51.	41.9	48.9	44.3	46.7	46.7	66					
61.5	41.8	60.1	44.8	58.1	48.8	57.1	47.3	53.8	39.9	51.8	42.5	49.6	45.	47.4	47.4	67					
62.4	43.3	61.1	46.3	59.1	50.3	58.1	48.3	54.6	40.5	52.6	43.1	50.4	45.7	48.1	48.1	68					
63.3	44.8	62.1	47.8	60.1	51.8	59.1	49.3	55.4	41.1	53.4	43.8	51.1	46.3	48.8	48.8	69					
64.2	46.3	63.1	49.3	61.1	53.3	60.1	50.3	56.2	41.7	54.1	44.4	51.9	47.	49.5	49.5	70					
65.1	47.8	64.1	50.8	62.1	54.8	61.1	51.3	57.	42.3	54.9	45.	52.6	47.7	50.2	50.2	71					
66.1	49.3	65.1	52.3	63.1	56.3	62.1	52.3	57.8	42.9	55.7	45.7	53.3	48.4	50.9	50.9	72					
67.1	50.8	66.1	53.8	64.1	57.8	63.1	53.3	58.6	43.5	56.4	46.3	54.1	49.4	51.6	51.6	73					
68.1	52.3	67.1	55.3	65.1	59.3	64.1	54.3	59.4	44.1	57.2	46.9	54.8	49.7	52.3	52.3	74					
69.1	53.8	68.1	56.8	66.1	60.8	65.1	55.3	60.2	44.7	58.	47.5	55.6	50.4	53.	53.	75					
70.1	55.3	69.1	58.3	67.1	62.3	66.1	56.3	61.	45.3	58.7	48.2	56.3	51.	53.7	53.7	76					
71.1	56.8	70.1	59.8	68.1	63.8	67.1	57.3	61.8	45.9	59.5	48.8	57.1	51.7	54.4	54.4	77					
72.1	58.3	71.1	61.3	69.1	65.3	68.1	58.3	62.6	46.5	60.3	49.5	57.8	52.4	55.2	55.2	78					
73.1	59.8	72.1	62.8	70.1	66.8	69.1	59.3	63.4	47.1	61.1	50.1	58.5	53.1	55.9	55.9	79					
74.1	61.3	73.1	64.3	71.1	68.3	70.1	60.3	64.3	47.7	61.8	50.8	59.3	53.7	56.6	56.6	80					
75.1	62.8	74.1	65.8	72.1	69.8	71.1	61.3	65.1	48.3	62.6	51.4	60.	54.4	57.3	57.3	81					
76.1	64.3	75.1	67.3	73.1	71.3	72.1	62.3	65.9	48.8	63.4	52.	60.8	55.1	58.	58.	82					
77.1	65.8	76.1	68.8	74.1	72.8	73.1	63.3	66.7	49.4	64.2	52.7	61.5	55.7	58.7	58.7	83					
78.1	67.3	77.1	70.3	75.1	74.3	74.1	64.3	67.5	50.	64.9	53.3	62.2	56.4	59.4	59.4	84					
79.1	68.8	78.1	71.8	76.1	75.8	75.1	65.3	68.3	50.6	65.7	53.9	63.	57.1	60.1	60.1	85					
80.1	70.3	79.1	73.3	77.1	77.3	76.1	66.3	69.1	51.2	66.5	54.6	63.7	57.8	60.8	60.8	86					
81.1	71.8	80.1	74.8	78.1	78.8	77.1	67.3	70.1	51.8	67.3	55.2	64.5	58.4	61.5	61.5	87					
82.1	73.3	81.1	76.3	79.1	80.3	78.1	68.3	70.7	52.4	68.	55.8	65.2	59.1	62.2	62.2	88					
83.1	74.8	82.1	77.8	80.1	81.8	79.1	69.3	71.5	53.	68.8	56.5	65.9	59.8	62.9	62.9	89					
84.1	76.3	83.1	79.3	81.1	83.3	80.1	70.3	72.3	53.6	69.6	57.1	66.7	60.4	63.6	63.6	90					
85.1	77.8	84.1	80.8	82.1	84.8	81.1	71.3	73.1	54.2	70.3	57.7	67.4	61.1	64.3	64.3	91					
86.1	79.3	85.1	82.3	83.1	86.3	82.1	72.3	73.9	54.8	71.1	58.4	68.2	61.8	65.1	65.1	92					
87.1	80.8	86.1	83.8	84.1	87.8	83.1	73.3	74.7	55.4	71.9	59.	68.9	62.5	65.8	65.8	93					
88.1	82.3	87.1	85.3	85.1	89.3	84.1	74.3	75.5	56.	72.7	59.6	69.6	63.1	66.5	66.5	94					
89.1	83.8	88.1	86.8	86.1	90.8	85.1	75.3	76.3	56.6	73.4	60.3	70.4	63.8	67.2	67.2	95					
90.1	85.3	89.1	88.3	87.1	92.3	86.1	76.3	77.1	57.2	74.2	60.9	71.1	64.5	67.9	67.9	96					
91.1	86.8	90.1	89.8	88.1	93.8	87.1	77.3	77.9	57.8	75.	61.5	71.9	65.1	68.6	68.6	97					
92.1	88.3	91.1	91.3	89.1	95.3	88.1	78.3	78.7	58.4	75.8	62.2	72.6	65.8	69.3	69.3	98					
93.1	89.8	92.1	92.8	90.1	96.8	89.1	79.3	79.5	59.	76.5	62.8	73.4	66.5	70.	70.	99					
94.1	91.3	93.1	94.3	91.1	98.3	90.1	80.3	80.3	59.6	77.3	63.4	74.1	67.2	70.7	70.7	100					
dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
N. W. by W. † W.	S. E. by E. † E.	S. W. by W. † W.	N. E. by E. † E.	N. W. by W. † W.	S. E. by E. † E.	S. W. by W. † W.	N. E. by E. † E.	N. W. by W. † W.	S. E. by E. † E.	S. W. by W. † W.	N. E. by E. † E.	N. W. by W. † W.	S. E. by E. † E.	S. W. by W. † W.	N. E. by E. † E.	N. W. by W. † W.	S. E. by E. † E.	S. W. by W. † W.	N. E. by E. † E.	N. W. by W. † W.	
C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 3 Pts.	C. 3 Pts.	C. 3½ Pts.	C. 3½ Pts.	C. 3½ Pts.	C. 3½ Pts.	C. 3½ Pts.	C. 3½ Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	

C. 1 Pt.		C. 2 Pt.		C. 3 Pt.		C. 4 Pt.		C. 5 Pt.		C. 6 Pt.		C. 7 Pt.		C. 8 Pt.	
S. by E.	S. by W.	N. by E.	N. by W.	S. by E.	S. by W.	N. by E.	N. by W.	S. by E.	S. by W.	N. by E.	N. by W.	S. by E.	S. by W.	N. by E.	N. by W.
lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
10 5	100.5	9 9	99.9	14 8	99.1	19 7	98.9	24 5	98.7	29 3	98.5	34	98.3	38 7	98.1
10 10	101.5	10	100.9	15	100	19 9	98.9	24 8	98.6	29 6	98.4	34 4	98.2	39	98
10 15	102.5	10 1	101.9	15 1	101	20 1	98.9	25	98.6	29 9	98.4	34 7	98.2	39 4	98
10 20	103.5	10 2	102.9	15 3	102	20 3	100.9	25 3	98.5	30 2	98.3	35	98.1	39 8	98
10 25	104.5	10 3	103.9	15 4	103	20 5	101.9	25 5	100.5	30 5	98.3	35 4	98.1	40 2	98
10 30	105.5	10 4	104.9	15 6	104	20 7	102.8	25 8	101.4	30 8	98.3	35 7	97.9	40 6	98
10 35	106.5	10 5	105.9	15 7	104.9	20 9	103.8	26	102.4	31 1	101.7	36	98.0	41	98
10 40	107.5	10 6	106.9	15 8	105.9	21 1	104.8	26 3	103.4	31 4	101.7	36 4	98.0	41 5	98
10 45	108.5	10 7	107.9	15 9	106.9	21 3	105.7	26 5	104.3	31 7	102.6	36 7	98.0	41 9	98
10 50	109.5	10 8	108.9	16 1	107.9	21 5	106.7	26 7	105.3	31 9	103.6	37 1	101.6	42 3	98
10 55	110.5	10 9	109.8	16 3	108.9	21 7	107.7	27	106.2	32 2	104.5	37 4	102.6	42 6	98
10 60	111.5	11	110.8	16 4	109.8	21 9	108.6	27 2	107.2	32 5	105.5	37 7	103.5	42 9	98
10 65	112.5	11 1	111.8	16 6	110.8	22	109.6	27 5	108.1	32 8	106.4	38 1	104.4	43 2	98
10 70	113.5	11 2	112.8	16 7	111.8	22 2	110.6	27 7	109.1	33	107.3	38 4	105.3	43 5	98
10 75	114.4	11 3	113.8	16 9	112.8	22 4	111.6	27 9	110	33 4	108.3	38 7	106.2	43 8	98
10 80	115.4	11 4	114.7	17	113.8	22 6	112.5	28 2	111	33 7	109.2	39 1	107.2	44 1	98
10 85	116.4	11 5	115.7	17 2	114.8	22 8	113.5	28 4	112	34	110.2	39 4	108.1	44 4	98
10 90	117.4	11 6	116.7	17 3	115.7	23	114.5	28 7	112.9	34 3	111.1	39 8	109	44 7	98
10 95	118.4	11 7	117.7	17 5	116.7	23 2	115.4	28 9	113.9	34 5	112	40 1	109.9	45 1	98
10 100	119.4	11 8	118.7	17 6	117.7	23 4	116.4	29 2	114.8	34 8	113	40 4	110.9	45 4	98
10 5 50	120.4	11 9	119.7	17 8	118.7	23 6	117.4	29 4	115.8	35 1	113.9	40 8	111.8	45 7	98
10 5 55	121.4	12	120.7	17 9	119.7	23 8	118.3	29 6	116.7	35 4	114.9	41 1	112.7	46 1	98
10 6 00	122.4	12 1	121.7	18	120.6	24	119.3	29 9	117.7	35 7	115.8	41 4	113.6	46 4	98
10 6 05	123.4	12 2	122.7	18 2	121.6	24 2	120.3	30 1	118.7	36	116.8	41 8	114.6	46 7	98
10 6 10	124.4	12 3	123.6	18 3	122.6	24 4	121.3	30 4	119.6	36 3	117.7	42 1	115.5	47 1	98
10 6 15	125.4	12 4	124.6	18 5	123.6	24 6	122.3	30 6	120.6	36 6	118.6	42 4	116.4	47 4	98
10 6 20	126.4	12 4	125.6	18 6	124.6	24 8	123.3	30 9	121.5	36 9	119.6	42 8	117.3	47 8	98
10 6 25	127.4	12 5	126.6	18 8	125.5	25	124.3	31 1	122.5	37 2	120.5	43 1	118.3	48 1	98
10 6 30	128.4	12 6	127.6	18 9	126.5	25 2	125.3	31 3	123.4	37 4	121.5	43 5	119.3	48 4	98
10 6 35	129.4	12 7	128.6	19 1	127.5	25 4	126.3	31 6	124.4	37 7	122.4	43 8	120.3	48 7	98
10 6 40	130.4	12 8	129.6	19 2	128.5	25 6	127.3	31 8	125.4	38	123.3	44 1	121.3	49 1	98
10 6 45	131.4	12 9	130.6	19 4	129.5	25 8	128.3	32 1	126.3	38 3	124.3	44 5	122.3	49 4	98
10 6 50	132.4	13	131.6	19 5	130.4	25 9	129.3	32 3	127.3	38 6	125.3	44 8	123.3	49 7	98
10 6 55	133.4	13 1	132.5	19 7	131.4	26 1	130.3	32 6	128.2	38 9	126.3	45 1	124.3	50 1	98
10 7 00	134.3	13 2	133.5	19 8	132.4	26 3	131	32 8	129.2	39 2	127.3	45 5	125.3	50 4	98
10 7 05	135.3	13 3	134.5	20	133.4	26 5	131.9	33	130.1	39 5	128.3	45 8	126.3	50 7	98
10 7 10	136.3	13 4	135.5	20 1	134.4	26 7	132.9	33 3	131.1	39 8	129.3	46 2	127.3	51 1	98
10 7 15	137.3	13 5	136.5	20 2	135.3	26 9	133.9	33 5	132.1	40 1	130.3	46 5	128.3	51 4	98
10 7 20	138.3	13 6	137.5	20 3	136.3	27 1	134.8	33 8	133	40 4	131.3	46 8	129.3	51 7	98
10 7 25	139.3	13 7	138.5	20 5	137.3	27 3	135.8	34	134	40 6	132.3	47 2	130.3	52 1	98
10 7 30	140.3	13 8	139.5	20 7	138.3	27 5	136.8	34 3	134.9	40 9	133.3	47 5	131.3	52 4	98
10 7 35	141.3	13 9	140.5	20 8	139.3	27 7	137.7	34 5	135.9	41 2	134.3	47 8	132.3	52 7	98
10 7 40	142.3	14	141.5	21	140.3	27 9	138.7	34 7	136.8	41 5	135.3	48 2	133.3	53 1	98
10 7 45	143.3	14 1	142.4	21 1	141.3	28 1	139.7	35	137.8	41 8	136.3	48 5	134.3	53 4	98
10 7 50	144.3	14 2	143.4	21 3	142.3	28 3	140.7	35 2	138.8	42 1	137.3	48 8	135.3	53 7	98
10 7 55	145.3	14 3	144.4	21 4	143.3	28 5	141.6	35 5	139.7	42 4	138.3	49 1	136.3	54 1	98
10 8 00	146.3	14 4	145.4	21 6	144.3	28 7	142.6	35 7	140.7	42 7	139.3	49 4	137.3	54 4	98
10 8 05	147.3	14 5	146.4	21 7	145.3	28 9	143.6	35 9	141.6	43	140.3	49 7	138.3	54 7	98
10 8 10	148.3	14 6	147.4	21 9	146.3	29 1	144.6	36 1	142.6	43 3	141.3	50 1	139.3	55 1	98
10 8 15	149.3	14 7	148.4	21 9	147.3	29 3	145.6	36 3	143.6	43 6	142.3	50 4	140.3	55 4	98
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.	W. by E.	E. by W.
7 1 Pt.	C. 7 1 Pt.	C. 7 2 Pt.	C. 7 3 Pt.	C. 7 4 Pt.	C. 7 5 Pt.	C. 7 6 Pt.	C. 7 7 Pt.	C. 7 8 Pt.	C. 7 9 Pt.	C. 7 10 Pt.	C. 7 11 Pt.	C. 7 12 Pt.	C. 7 13 Pt.	C. 7 14 Pt.	C. 7 15 Pt.

6 Distance 101 to 150 miles. TABLE IV.

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.																	
N. N. E. † E.	S. S. E. † E.	N. N. W. † W.	S. S. W. † W.	N. N. E. † E.	S. S. E. † E.	N. N. W. † W.	S. S. W. † W.	N. E. by N.	S. E. by S.	N. E. by S.	S. W. by S.	N. E. † N.	S. E. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.				
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.		
91.3	43.9	89.1	47.6	86.6	51.9	84	56.1	81.1	60.9	78.1	64.1	74.8	67.8																
92.9	43.6	90	48.1	87.5	52.4	84.8	56.7	81.9	60.8	78.8	64.7	75.6	68.5																
93.1	44	90.8	48.6	88.3	53	85.6	57.3	82.7	61.4	79.6	65.3	76.3	69.2																
94	44.5	91.7	49	89.2	53.5	86.5	57.8	83.5	62	80.4	66	77.1	69.8																
94.9	44.9	92.6	49.5	90.1	54	87.3	58.3	84.3	62.5	81.3	66.6	77.8	70.5																
95.8	45.3	93.5	50	90.9	54.5	88.1	58.9	85.1	63.1	82.0	67.2	78.5	71.2																
96.7	45.7	94.4	50.4	91.8	55	89	59.4	85.9	63.7	82.7	67.9	79.3	71.9																
97.6	46.2	95.3	50.9	92.7	55.5	89.8	60	86.7	64.3	83.5	68.5	80	72.5																
98.5	46.6	96.1	51.4	93.5	56	90.6	60.6	87.5	64.9	84.3	69.1	80.8	73.2																
99.4	47	97	51.9	94.4	56.6	91.5	61.1	88.4	65.5	85	69.7	81.5	73.9																
100.3	47.5	97.9	52.3	95.2	57.1	92.3	61.7	89.3	66.1	85.8	70.4	82.2	74.5																
101.2	47.9	98.8	52.8	96.1	57.6	93.1	62.2	90.2	66.7	86.6	71.1	83.1	75.2																
102.9	48.3	99.7	53.3	96.9	58.1	94	62.8	91.0	67.3	87.4	71.7	84.1	75.9																
103.1	48.7	100.5	53.7	97.8	58.6	94.8	63.3	91.6	67.9	88.1	72.3	84.5	76.6																
104	49.2	101.4	54.2	98.6	59.1	95.6	63.9	92.4	68.3	88.9	73	85.2	77.2																
104.9	49.6	102.3	54.7	99.5	59.6	96.5	64.4	93.3	68.9	89.7	73.6	86	77.9																
105.8	50	103.2	55.2	100.4	60.2	97.3	65	94	69.7	90.4	74.2	86.7	78.6																
106.7	50.5	104.1	55.6	101.2	60.7	98.1	65.5	94.8	70.3	91.2	74.9	87.4	79.2																
107.6	50.9	104.9	56.1	102.1	61.2	98.9	66.1	95.6	70.9	92	75.5	88.2	79.9																
108.5	51.3	105.8	56.6	102.9	61.7	99.8	66.7	96.4	71.5	92.8	76.1	89.0	80.6																
100.4	51.7	106.7	57	103.8	62.2	100.6	67.2	97.2	72.1	93.5	76.8	90.4	81.3																
110.3	52.2	107.6	57.5	104.6	62.7	101.4	67.8	98	72.7	94.3	77.4	91.4	81.9																
111.2	52.6	108.5	58	105.5	63.2	102.3	68.3	98.8	73.3	95.1	78	91.1	82.6																
112	53	109.4	58.5	106.4	63.7	103.1	68.9	99.6	73.9	95.9	78.7	91.9	83.3																
113	53.4	110.3	58.9	107.2	64.3	103.9	69.4	100.4	74.5	96.6	79.3	92.6	83.9																
113.9	53.9	111.1	59.4	108.1	64.8	104.8	70	101.2	75.1	97.4	79.9	93.4	84.6																
114.8	54.3	112	59.9	108.9	65.3	105.6	70.5	102	75.7	98.2	80.6	94.1	85.3																
115.7	54.7	112.9	60.3	109.8	65.8	106.4	71.1	102.8	76.2	98.9	81.2	94.8	86																
116.6	55.2	113.8	60.8	110.6	66.3	107.3	71.7	103.6	76.9	99.6	81.9	95.6	86.6																
117.5	55.6	114.6	61.3	111.5	66.8	108.1	72.2	104.4	77.4	100.5	82.5	96.3	87.3																
118.4	56	115.5	61.8	112.4	67.3	108.9	72.8	105.2	78	101.3	83.1	97.1	88																
119.3	56.4	116.4	62.2	113.2	67.9	109.8	73.3	106	78.6	102	83.7	97.8	88.6																
120.2	56.9	117.3	62.7	114.1	68.4	110.6	73.9	106.8	79.2	102.8	84.4	98.5	89.3																
121.1	57.3	118.2	63.2	114.9	68.9	111.4	74.4	107.6	79.8	103.6	85	99.3	90																
122	57.7	119.1	63.6	115.8	69.4	112.2	75	108.4	80.4	104.4	85.6	100	90.7																
122.9	58.1	119.9	64.1	116.7	69.9	113.1	75.5	109.2	81	105.1	86.3	100.8	91.3																
123.8	58.6	120.8	64.6	117.5	70.4	113.9	76.1	110	81.6	105.9	86.9	101.5	92																
124.8	59	121.7	65.1	118.4	71	114.7	76.7	110.8	82.2	106.7	87.5	102.3	92.7																
125.7	59.4	122.6	65.5	119.2	71.5	115.6	77.2	111.6	82.8	107.4	88.2	103	93.3																
126.6	59.9	123.5	66	120.1	72	116.4	77.8	112.4	83.4	108.2	88.8	103.7	94																
127.5	60.3	124.4	66.5	120.9	72.5	117.2	78.3	113.3	84	109	89.4	104.5	94.7																
128.4	60.7	125.2	66.9	121.8	73	118.1	78.9	114.1	84.6	109.8	90.1	105.2	95.4																
129.3	61.1	126.1	67.4	122.7	73.5	118.9	79.4	114.9	85.2	110.5	90.7	106	96																
130.2	61.6	127	67.9	123.5	74	119.7	80	115.7	85.8	111.3	91.4	106.7	96.7																
131.1	62	127.9	68.4	124.4	74.5	120.6	80.5	116.5	86.4	112.1	92.1	107.4	97.4																
132	62.4	128.8	68.8	125.2	75.1	121.4	81.1	117.3	87	112.9	92.6	108.2	98																
132.9	62.9	129.6	69.3	126.1	75.6	122.2	81.7	118.1	87.6	113.6	93.3	108.9	92.7																
133.8	63.3	130.5	69.8	126.9	76.1	123.1	82.2	118.9	88.2	114.4	93.9	109.7	93.4																
134.7	63.7	131.4	70.3	127.8	76.6	123.9	82.8	119.7	88.8	115.2	94.5	110.4	100.1																
135.6	64.1	132.3	70.7	128.7	77.1	124.7	83.3	120.5	89.4	116	95.2	111.1	100.7																
dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.	N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.	N. W. by W.	S. W. by W.	N. E. by E.	S. E. by E.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.	N. E. † N.	S. E. † S.	N. W. † W.	S. W. † S.
C. 5½ Pts.	C. 5½ Pts.	C. 5½ Pts.	C. 5 Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.

Distance.	C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 2 Pts.	
	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.	N. by E.	S. by W.
	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
151	150.8	7.4	150.3	14.8	149.4	22.2	148.1	29.5	146.5	36.7	144.5	43.6	142.2	50.9
152	151.8	7.5	151.3	14.9	150.4	22.3	149.1	29.7	147.4	36.9	145.5	44.1	143.2	51.2
153	152.8	7.5	152.3	15.0	151.3	22.4	150.1	29.8	148.4	37.2	146.4	44.4	144.1	51.5
154	153.8	7.6	153.3	15.1	152.3	22.5	151.1	30.0	149.4	37.4	147.4	44.7	145.0	51.8
155	154.8	7.6	154.3	15.2	153.3	22.6	152.1	30.2	150.4	37.7	148.4	45.0	146.0	52.1
156	155.8	7.7	155.3	15.3	154.3	22.7	153.1	30.4	151.3	37.9	149.3	45.3	147.0	52.4
157	156.8	7.7	156.3	15.4	155.3	22.8	154.1	30.6	152.3	38.1	150.2	45.6	148.0	52.7
158	157.8	7.8	157.3	15.5	156.3	22.9	155.1	30.8	153.3	38.4	151.2	45.9	149.0	53.0
159	158.8	7.8	158.3	15.6	157.3	23.0	156.1	31.1	154.3	38.6	152.2	46.2	150.0	53.3
160	159.8	7.9	159.3	15.7	158.3	23.1	157.1	31.2	155.3	38.9	153.2	46.5	151.0	53.6
161	160.8	7.9	160.3	15.8	159.3	23.2	157.9	31.4	156.2	39.1	154.1	46.7	151.8	53.9
162	161.8	7.9	161.3	15.9	160.3	23.3	158.9	31.6	157.1	39.4	155.1	47.0	152.8	54.2
163	162.8	8.0	162.3	16.0	161.3	23.4	159.1	31.8	158.1	39.6	156.1	47.3	153.8	54.5
164	163.8	8.1	163.3	16.1	162.3	23.5	160.8	32.0	159.1	39.9	157.0	47.6	154.8	54.8
165	164.8	8.1	164.3	16.2	163.3	23.6	161.8	32.2	160.1	40.1	157.9	47.9	155.8	55.1
166	165.8	8.1	165.3	16.3	164.3	23.7	162.8	32.4	161.0	40.3	158.9	48.2	156.8	55.4
167	166.8	8.2	166.3	16.4	165.3	23.8	163.8	32.6	162.0	40.6	159.8	48.5	157.8	55.7
168	167.8	8.3	167.3	16.5	166.3	23.9	164.8	32.8	163.0	40.8	160.8	48.8	158.8	56.0
169	168.8	8.3	168.3	16.6	167.3	24.0	165.8	33.0	164.0	41.1	161.7	49.1	159.8	56.3
170	169.8	8.3	169.3	16.7	168.3	24.1	166.7	33.2	164.9	41.3	162.7	49.3	160.7	56.6
171	170.8	8.4	170.3	16.8	169.3	24.2	167.7	33.4	165.9	41.5	163.6	49.6	161.7	56.9
172	171.8	8.4	171.3	16.9	170.3	24.3	168.7	33.6	166.8	41.8	164.6	49.9	162.7	57.2
173	172.8	8.5	172.3	17.0	171.3	24.4	169.7	33.8	167.8	42.0	165.6	50.2	163.7	57.5
174	173.8	8.5	173.3	17.1	172.3	24.5	170.7	33.9	168.8	42.3	166.5	50.5	164.8	57.8
175	174.8	8.6	174.3	17.2	173.3	24.6	171.6	34.1	169.8	42.5	167.5	50.8	165.8	58.1
176	175.8	8.6	175.3	17.3	174.3	24.7	172.6	34.3	170.7	42.8	168.4	51.1	166.7	58.4
177	176.8	8.7	176.3	17.4	175.3	24.8	173.6	34.5	171.7	43.0	169.4	51.4	167.7	58.7
178	177.8	8.7	177.3	17.4	176.3	24.9	174.6	34.7	172.7	43.3	170.3	51.7	168.7	59.0
179	178.8	8.8	178.3	17.5	177.3	25.0	175.6	34.9	173.6	43.5	171.3	52.0	169.7	59.3
180	179.8	8.8	179.3	17.6	178.3	25.1	176.5	35.1	174.6	43.7	172.2	52.3	170.7	59.6
181	180.8	8.9	180.3	17.7	179.3	25.2	177.5	35.3	175.5	44.0	173.2	52.5	171.7	59.9
182	181.8	8.9	181.3	17.8	180.3	25.3	178.5	35.5	176.5	44.2	174.2	52.8	172.7	60.2
183	182.8	9.0	182.3	17.9	181.3	25.4	179.5	35.7	177.5	44.5	175.1	53.1	173.7	60.5
184	183.8	9.0	183.3	18.0	182.3	25.5	180.5	35.9	178.5	44.7	176.1	53.4	174.7	60.8
185	184.8	9.1	184.3	18.1	183.3	25.6	181.4	36.1	179.5	45.0	177.1	53.7	175.7	61.1
186	185.8	9.1	185.3	18.2	184.3	25.7	182.4	36.3	180.4	45.3	178.0	54.0	176.7	61.4
187	186.8	9.2	186.3	18.3	185.3	25.8	183.4	36.5	181.4	45.5	179.0	54.3	177.7	61.7
188	187.8	9.2	187.3	18.4	186.3	25.9	184.4	36.7	182.4	45.7	180.0	54.6	178.7	62.0
189	188.8	9.3	188.3	18.5	187.3	26.0	185.4	36.9	183.3	45.9	181.0	54.9	179.7	62.3
190	189.8	9.3	189.3	18.6	188.3	26.1	186.3	37.1	184.3	46.2	182.0	55.2	180.7	62.6
191	190.8	9.4	190.3	18.7	189.3	26.2	187.3	37.3	185.3	46.4	183.0	55.4	181.7	62.9
192	191.8	9.4	191.3	18.8	190.3	26.3	188.3	37.5	186.3	46.7	184.0	55.7	182.7	63.2
193	192.8	9.5	192.3	18.9	191.3	26.4	189.3	37.7	187.3	46.9	185.0	56.0	183.7	63.5
194	193.8	9.5	193.3	19.0	192.3	26.5	190.3	37.9	188.3	47.1	186.0	56.3	184.7	63.8
195	194.8	9.6	194.3	19.1	193.3	26.6	191.3	38.1	189.3	47.4	187.0	56.6	185.7	64.1
196	195.8	9.6	195.3	19.2	194.3	26.7	192.3	38.3	190.3	47.6	188.0	56.9	186.7	64.4
197	196.8	9.7	196.3	19.3	195.3	26.8	193.3	38.4	191.3	47.9	189.0	57.2	187.7	64.7
198	197.8	9.7	197.3	19.4	196.3	26.9	194.3	38.6	192.3	48.1	190.0	57.5	188.7	65.0
199	198.8	9.8	198.3	19.5	197.3	27.0	195.3	38.8	193.3	48.4	191.0	57.8	189.7	65.3
200	199.8	9.8	199.3	19.6	198.3	27.1	196.3	39.0	194.3	48.6	192.0	58.1	190.7	65.6

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.		Distance.	
N. N. E. † E.	S. S. E. † E.	N. N. E. † E.	S. S. E. † E.	N. N. E. † E.	S. S. E. † E.	N. N. E. by N.	S. S. E. by S.	N. E. † N.	S. E. † S.	N. E. † N.	S. E. † S.	N. E. † N.	S. E. † S.		N. E. † N.
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
136.5	64.6	133.9	71.9	139.5	77.6	135.6	83.9	131.3	90.	116.7	95.8	111.9	101.4	106.8	151
137.4	65.	134.1	71.7	130.4	78.1	136.4	84.4	132.1	90.5	117.5	96.4	112.6	102.1	107.5	152
133.3	65.4	134.9	73.1	131.9	78.7	137.2	85.	132.9	91.1	118.3	97.1	113.4	102.7	104.2	153
139.2	65.8	135.8	73.6	132.1	79.9	138.	85.5	133.7	91.7	119.	97.7	114.1	103.4	104.9	154
140.1	66.3	136.7	73.1	132.9	79.7	138.9	86.1	134.5	92.3	119.8	98.3	114.8	104.1	106.6	155
141.	66.7	137.6	73.5	133.8	80.9	139.7	86.7	135.3	92.9	120.6	99.	115.6	104.8	110.3	156
141.9	67.1	138.5	74.5	134.7	80.7	139.5	87.9	136.1	93.5	121.4	99.6	116.3	105.4	111.	157
145.9	67.6	139.3	74.5	135.5	81.9	139.4	87.8	136.9	94.1	122.1	100.2	117.1	106.1	111.7	158
143.7	68.	140.2	75.	136.4	81.7	139.2	88.3	137.7	94.7	122.9	100.9	117.8	106.8	112.4	159
144.6	68.4	141.1	75.4	137.2	82.3	139.	88.9	138.5	95.3	123.7	101.5	118.6	107.4	113.1	160
145.5	68.8	142.	75.9	138.1	82.8	139.9	89.4	139.3	95.9	124.5	102.1	119.3	108.1	113.8	161
146.4	69.3	142.9	76.4	139.	83.3	140.7	90.	140.1	96.5	125.3	102.8	120.	108.8	114.6	162
147.4	69.7	143.8	76.8	139.8	83.8	141.5	90.5	140.9	97.1	126.1	103.4	120.8	109.5	115.3	163
148.3	70.1	144.6	77.3	140.7	84.3	142.4	91.1	141.7	97.7	126.9	104.	121.5	110.1	116.	164
149.2	70.5	145.5	77.8	141.5	84.8	143.2	91.7	142.5	98.3	127.5	104.7	122.3	110.8	116.7	165
150.1	71.	146.4	78.3	142.4	85.3	144.	92.9	143.3	98.9	128.3	105.3	123.	111.5	117.4	166
151.	71.4	147.3	78.7	143.2	85.9	144.9	92.8	144.1	99.5	129.1	105.9	123.7	112.2	118.1	167
151.9	71.8	148.2	79.2	144.	86.4	145.7	93.3	144.9	100.1	129.9	106.6	124.5	112.9	118.8	168
152.8	72.3	149.	79.7	144.9	86.9	146.6	93.9	145.7	100.7	130.6	107.2	125.2	113.5	119.5	169
153.7	72.7	149.9	80.1	145.8	87.4	147.4	94.4	146.5	101.3	131.4	107.8	126.	114.2	120.2	170
154.6	73.1	150.8	80.6	146.7	87.9	148.2	95.	147.3	101.9	132.2	108.5	126.7	114.8	120.9	171
155.5	73.5	151.7	81.1	147.5	88.4	149.	95.5	148.1	102.5	133.	109.1	127.4	115.5	121.6	172
156.4	74.	152.6	81.6	148.4	88.9	149.8	96.1	148.9	103.1	133.7	109.8	128.1	116.2	122.3	173
157.3	74.4	153.5	82.	149.2	89.5	150.7	96.7	149.8	103.7	134.5	110.4	128.9	116.9	123.	174
158.2	74.8	154.3	82.5	150.1	90.	151.5	97.2	150.6	104.2	135.3	111.	129.7	117.5	123.7	175
159.1	75.3	155.2	83.	151.	90.5	152.4	97.8	151.4	104.8	136.	111.7	130.4	118.2	124.5	176
160.	75.7	156.1	83.4	151.8	91.	153.2	98.3	152.2	105.4	136.8	112.3	131.1	118.9	125.2	177
160.9	76.1	157.	83.9	152.7	91.5	154.	98.9	153.	106.	137.6	112.9	131.9	119.5	125.9	178
161.8	76.5	157.9	84.4	153.5	92.	154.8	99.4	153.8	106.6	138.4	113.6	132.6	120.2	126.6	179
162.7	77.	158.7	84.9	154.4	92.5	155.7	100.	154.6	107.2	139.1	114.2	133.4	120.9	127.3	180
163.6	77.4	159.6	85.3	155.2	93.1	156.5	100.5	155.4	107.8	139.9	114.8	134.1	121.6	128.	181
164.5	77.8	160.5	85.8	156.1	93.6	157.3	101.1	156.2	108.4	140.7	115.5	134.9	122.3	128.7	182
165.4	78.2	161.4	86.3	157.	94.1	158.2	101.7	157.	109.	141.5	116.1	135.6	122.9	129.4	183
166.3	78.7	162.3	86.7	157.8	94.6	159.1	102.2	157.8	109.6	142.3	116.7	136.3	123.6	130.1	184
167.2	79.1	163.2	87.2	158.7	95.1	160.	102.8	158.6	110.2	143.	117.4	137.1	124.2	130.8	185
168.1	79.5	164.	87.7	159.5	95.6	160.9	103.3	159.4	110.8	143.8	118.	137.8	124.9	131.5	186
169.	80.	164.9	88.2	160.4	96.1	161.8	103.9	160.2	111.4	144.6	118.6	138.6	125.6	132.2	187
169.9	80.4	165.8	88.6	161.3	96.7	162.7	104.4	161.	112.	145.3	119.3	139.3	126.3	132.9	188
170.9	80.8	166.7	89.1	162.1	97.2	163.6	105.1	161.8	112.6	146.1	119.9	140.	127.	133.6	189
171.8	81.2	167.6	89.6	163.	97.7	164.5	105.5	162.6	113.2	146.9	120.5	140.8	127.6	134.4	190
172.7	81.7	168.4	90.	163.8	98.2	165.4	106.1	163.4	113.8	147.6	121.2	141.5	128.3	135.1	191
173.6	82.1	169.3	90.5	164.7	98.7	166.3	106.7	164.2	114.4	148.4	121.8	142.3	129.	135.8	192
174.5	82.5	170.2	91.	165.5	99.2	167.2	107.2	165.	115.	149.2	122.4	143.	129.6	136.5	193
175.4	82.9	171.1	91.5	166.4	99.7	168.1	107.8	165.8	115.6	150.	123.1	143.7	130.3	137.2	194
176.3	83.4	172.	91.9	167.3	100.3	169.	108.3	166.6	116.2	150.7	123.7	144.5	131.	137.9	195
177.2	83.8	172.9	92.4	168.1	100.8	169.8	108.9	167.4	116.8	151.5	124.3	145.	131.6	138.6	196
178.1	84.2	173.7	92.9	168.9	101.3	170.7	109.4	168.2	117.4	152.3	124.9	145.9	132.3	139.3	197
179.	84.7	174.6	93.3	169.8	101.8	171.6	110.	169.	117.9	153.1	125.6	146.7	133.	140.	198
179.9	85.1	175.5	93.8	170.7	102.3	172.5	110.5	170.8	118.5	153.9	126.2	147.4	133.6	140.7	199
180.8	85.5	176.4	94.3	171.5	102.8	173.4	111.1	171.6	119.1	154.6	126.9	148.2	134.3	141.4	200
dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.	N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.	N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.	N. W. by W. † W.	S. W. by W. † W.	N. E. by E. † E.	S. E. by E. † E.
C. 5½ Pts.	C. 5½ Pts.	C. 5½ Pts.	C. 5½ Pts.	C. 5 Pts.	C. 5 Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4 Pts.	C. 4 Pts.		

Distance.	C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 2 Pts.			
	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 1 Pt.	C. 2 Pts.		
	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	d. lat. dep.	N. by E. S. by E. S. by W. N. by W.	
901	900.8	9.9	900.	19.7	198.8	99.5	197.1	39.9	195.	48.8	199.3	58.9	199.3	67.7	195.7	76.9
902	901.8	9.9	901.	19.8	199.8	99.6	198.1	39.4	195.9	49.1	199.3	59.0	199.3	68.1	196.7	77.9
903	902.8	10.	902.	19.9	200.8	99.7	199.1	39.6	196.9	49.3	199.3	59.1	199.3	69.4	197.7	78.9
904	903.8	10.	903.	20.	201.8	99.8	200.1	39.6	197.9	49.6	199.3	59.2	199.3	70.7	198.7	79.9
905	904.8	10.1	904.	20.1	202.8	99.9	201.1	40.	198.9	49.8	199.3	59.3	199.3	71.9	199.7	80.9
906	905.8	10.1	905.	20.2	203.8	99.9	202.	40.2	199.8	50.1	197.1	59.8	194.	62.4	199.3	81.9
907	906.8	10.2	906.	20.3	204.8	99.9	203.	40.4	200.8	50.3	196.1	60.1	194.9	63.7	199.3	82.9
908	907.7	10.2	907.	20.4	205.7	99.9	204.	40.6	201.8	50.5	199.	60.4	195.8	65.0	199.3	83.9
909	908.7	10.3	908.	20.5	206.7	99.7	205.	40.8	202.7	50.8	200.	60.7	196.7	70.4	199.3	84.9
910	909.7	10.3	909.	20.6	207.7	99.7	206.	41.	203.7	51.	201.	61.	197.8	71.7	194.	85.9
911	910.7	10.4	910.	20.7	208.7	99.7	206.9	41.2	204.7	51.3	201.9	61.3	198.7	71.1	194.9	86.7
912	911.7	10.4	911.	20.8	209.7	99.7	207.9	41.4	205.6	51.5	202.9	61.5	199.6	71.4	195.9	87.1
913	912.7	10.5	912.	20.9	210.7	99.7	208.9	41.6	206.6	51.8	203.8	61.8	200.5	71.8	196.8	87.5
914	913.7	10.5	913.	21.	211.7	99.7	209.9	41.7	207.6	52.	204.8	62.1	201.5	72.1	197.7	87.9
915	914.7	10.5	914.	21.1	212.7	99.7	210.9	41.9	208.6	52.2	205.7	62.4	202.4	72.4	198.6	88.1
916	915.7	10.6	915.	21.2	213.7	99.7	211.8	42.1	209.5	52.5	206.7	62.7	203.4	72.8	199.6	88.1
917	916.7	10.6	916.	21.3	214.7	99.7	212.8	42.3	210.5	52.7	207.7	63.	204.3	73.1	200.5	88.1
918	917.7	10.7	917.	21.4	215.6	99.7	213.8	42.5	211.5	53.	208.6	63.3	205.3	73.4	201.4	88.1
919	918.7	10.7	918.9	21.5	216.6	99.7	214.8	42.7	212.4	53.2	209.6	63.6	206.2	73.8	202.3	88.1
920	919.7	10.8	919.9	21.6	217.6	99.7	215.8	42.9	213.4	53.5	210.5	63.9	207.1	74.1	203.2	88.1
921	920.7	10.8	919.9	21.7	218.6	99.7	216.8	43.1	214.4	53.7	211.5	64.2	208.1	74.5	204.2	88.1
922	921.7	10.8	920.9	21.8	219.6	99.6	217.7	43.3	215.3	53.9	212.4	64.4	209.	74.8	205.1	88.1
923	922.7	10.9	921.9	21.9	220.6	99.6	218.7	43.5	216.3	54.2	213.4	64.7	210.	75.1	206.	88.1
924	923.7	11.	922.9	22.	221.6	99.6	219.7	43.7	217.3	54.4	214.3	65.	210.9	75.5	206.9	88.1
925	924.7	11.	923.9	22.1	222.6	99.6	220.7	43.9	218.3	54.7	215.3	65.3	211.8	75.8	207.9	88.1
926	925.7	11.1	924.9	22.2	223.6	99.6	221.7	44.1	219.3	54.9	216.3	65.6	212.8	76.1	208.9	88.1
927	926.7	11.2	925.9	22.3	224.5	99.6	222.6	44.3	220.3	55.2	217.2	65.9	213.7	76.5	209.7	88.1
928	927.7	11.2	926.9	22.3	225.5	99.6	223.6	44.5	221.2	55.4	218.2	66.2	214.7	76.8	210.6	88.1
929	928.7	11.2	927.9	22.4	226.5	99.6	224.6	44.7	222.1	55.6	219.1	66.5	215.6	77.1	211.6	88.1
930	929.7	11.3	928.9	22.5	227.5	99.6	225.6	44.9	223.1	55.8	220.1	66.8	216.6	77.5	212.5	88.1
931	930.7	11.3	929.9	22.6	228.5	99.6	226.6	45.1	224.1	56.1	221.1	67.1	217.5	77.8	213.4	88.1
932	931.7	11.4	930.9	22.7	229.5	99.6	227.5	45.3	225.	56.4	222.	67.3	218.4	78.2	214.3	88.1
933	932.7	11.4	931.9	22.8	230.5	99.6	228.5	45.5	226.	56.6	223.	67.6	219.4	78.5	215.2	88.1
934	933.7	11.5	932.9	22.9	231.5	99.6	229.5	45.7	227.	56.9	224.	67.9	220.3	78.8	216.2	88.1
935	934.7	11.5	933.9	23.	232.5	99.6	230.5	45.8	228.	57.1	225.9	68.2	221.3	79.2	217.1	88.1
936	935.7	11.6	934.9	23.1	233.4	99.6	231.5	46.	229.	57.3	226.8	68.5	222.2	79.5	218.	88.1
937	936.7	11.6	935.9	23.2	234.4	99.6	232.4	46.2	230.	57.6	227.8	68.8	223.1	79.8	219.	88.1
938	937.7	11.7	936.9	23.3	235.4	99.6	233.4	46.4	231.	57.8	228.7	69.1	224.1	80.2	220.	88.1
939	938.7	11.7	937.9	23.4	236.4	99.6	234.4	46.6	232.	58.1	229.7	69.4	225.	80.5	221.	88.1
940	939.7	11.8	938.9	23.5	237.4	99.6	235.4	46.8	233.	58.3	230.7	69.7	226.	80.8	222.	88.1
941	940.7	11.8	939.9	23.6	238.4	99.6	236.4	47.	233.8	58.6	231.6	70.	227.	81.2	223.	88.1
942	941.7	11.9	940.9	23.7	239.4	99.6	237.4	47.2	234.7	58.8	232.5	70.2	228.	81.5	224.	88.1
943	942.7	11.9	941.9	23.8	240.4	99.6	238.4	47.4	235.7	59.	233.5	70.5	229.	81.9	225.	88.1
944	943.7	12.	942.9	23.9	241.4	99.6	239.4	47.6	236.7	59.2	234.5	70.8	230.	82.2	226.	88.1
945	944.7	12.	943.9	24.	242.4	99.6	240.4	47.8	237.7	59.5	235.5	71.1	231.	82.5	227.	88.1
946	945.7	12.1	944.9	24.1	243.3	99.6	241.3	48.	238.6	59.8	236.4	71.4	232.	82.8	228.	88.1
947	946.7	12.1	945.9	24.2	244.3	99.6	242.3	48.2	239.5	60.	237.4	71.7	233.	83.1	229.	88.1
948	947.7	12.2	946.9	24.3	245.3	99.6	243.3	48.4	240.4	60.2	238.3	72.	234.	83.4	230.	88.1
949	948.7	12.2	947.9	24.4	246.3	99.6	244.3	48.6	241.3	60.5	239.2	72.3	235.	83.7	231.	88.1
950	949.7	12.3	948.9	24.5	247.3	99.6	245.3	48.8	242.2	60.7	240.1	72.6	236.	84.	232.	88.1

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.		Distance.	
N. E. by E.	S. E. by E.	N. N. W. by W.	S. S. W. by W.	N. N. E. by E.	S. S. E. by E.	N. N. W. by W.	S. S. W. by W.	N. E. by N.	S. E. by S.	N. W. by N.	S. W. by S.	N. E. by N.	S. E. by S.	N. W. by N.	S. W. by S.		
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
181.7	85.9	177.3	94.8	173.4	103.3	167.1	111.7	161.4	119.7	155.4	197.5	148.9	135.	142.1	901		
182.6	88.4	178.1	95.2	173.3	103.8	168.	112.9	162.4	120.3	156.1	198.1	149.7	135.7	142.8	902		
183.5	90.8	179.	95.7	174.1	104.4	168.8	112.8	163.1	120.9	156.9	198.8	150.4	136.3	143.5	903		
184.4	92.2	179.9	96.2	175.	104.9	169.6	113.3	163.9	121.5	157.7	199.4	151.2	137.	144.2	904		
185.3	93.7	180.8	96.8	175.6	105.4	170.5	113.9	164.7	122.1	158.5	130.1	151.9	137.7	145.	905		
186.2	95.1	181.7	97.1	176.7	105.9	171.3	114.4	165.5	122.7	159.2	130.7	152.6	138.3	145.7	906		
187.1	96.5	182.6	97.7	177.5	106.4	172.1	115.	166.3	123.3	160.	131.3	153.4	139.	146.4	907		
188.	98.3	183.4	98.1	178.4	106.9	172.9	115.5	167.1	123.9	160.8	132.	154.1	139.7	147.1	908		
188.9	99.4	184.3	98.5	179.3	107.4	173.8	116.1	167.9	124.5	161.6	132.6	154.9	140.4	147.8	909		
189.8	100.8	185.2	99.	180.1	108.	174.6	116.7	168.7	125.1	162.3	133.2	155.6	141.	148.5	910		
190.7	102.2	186.1	99.5	181.	108.5	175.4	117.2	169.5	125.7	163.1	133.9	156.3	141.7	149.2	911		
191.6	103.6	187.	99.9	181.8	109.	176.3	117.8	170.3	126.3	163.9	134.5	157.1	142.4	149.9	912		
192.5	105.1	187.8	100.4	182.7	109.5	177.1	118.3	171.1	126.9	164.7	135.1	157.8	143.	150.6	913		
193.5	106.5	188.7	100.9	183.6	110.	177.9	118.9	171.9	127.5	165.4	135.8	158.6	143.7	151.3	914		
194.4	107.9	189.6	101.4	184.4	110.5	178.8	119.4	172.7	128.1	166.3	136.4	159.3	144.4	152.	915		
195.3	109.4	190.5	101.8	185.3	111.	179.6	120.	173.5	128.7	167.	137.	160.	145.1	152.7	916		
196.2	110.8	191.4	102.3	186.1	111.6	180.4	120.5	174.3	129.3	167.7	137.7	160.8	145.7	153.4	917		
197.1	112.3	192.3	102.8	187.	112.1	181.3	121.	175.1	129.9	168.5	138.3	161.5	146.4	154.1	918		
198.	113.8	193.1	103.3	187.8	112.6	182.1	121.7	175.9	130.5	169.3	138.9	162.3	147.1	154.9	919		
198.9	115.3	194.	103.7	188.7	113.1	182.9	122.2	176.7	131.1	170.1	139.6	163.	147.7	155.6	920		
199.8	116.8	194.9	104.2	189.6	113.6	183.8	122.8	177.5	131.6	170.8	140.2	163.8	148.4	156.3	921		
200.7	118.3	195.8	104.7	190.4	114.1	184.6	123.3	178.3	132.2	171.6	140.8	164.5	149.1	157.	922		
201.6	119.8	196.7	105.1	191.3	114.6	185.4	123.9	179.1	132.8	172.4	141.5	165.2	149.8	157.7	923		
202.5	121.3	197.6	105.6	192.1	115.2	186.2	124.4	179.9	133.4	173.2	142.1	166.	150.4	158.4	924		
203.4	122.8	198.4	106.1	193.	115.7	187.1	125.	180.7	134.	173.9	142.7	166.7	151.1	159.1	925		
204.3	124.3	199.3	106.5	193.8	116.2	187.9	125.5	181.5	134.6	174.7	143.4	167.5	151.8	159.8	926		
205.2	125.8	200.2	107.	194.7	116.7	188.7	126.1	182.3	135.2	175.5	144.	168.2	152.4	160.5	927		
206.1	127.3	201.1	107.5	195.6	117.2	189.6	126.7	183.1	135.8	176.2	144.6	169.9	153.1	161.2	928		
207.	128.8	202.	107.9	196.4	117.7	190.4	127.2	183.9	136.4	177.	145.3	170.7	153.8	161.9	929		
207.9	130.3	202.8	108.4	197.3	118.2	191.2	127.8	184.7	137.	177.8	145.9	170.4	154.5	162.6	930		
208.8	131.8	203.7	108.9	198.1	118.8	192.1	128.3	185.5	137.6	178.6	146.5	171.2	155.1	163.3	931		
209.7	133.3	204.6	109.4	199.	119.3	192.9	128.9	186.3	138.2	179.3	147.2	171.9	155.8	164.	932		
210.6	134.8	205.5	109.8	199.9	119.8	193.7	129.4	187.1	138.8	180.1	147.8	172.6	156.5	164.8	933		
211.5	136.3	206.4	110.3	200.7	120.3	194.6	130.	188.	139.4	180.9	148.4	173.4	157.1	165.5	934		
212.4	137.8	207.3	110.8	201.6	120.8	195.4	130.5	188.8	140.	181.7	149.1	174.1	157.8	166.2	935		
213.3	139.3	208.1	111.3	202.4	121.3	196.2	131.1	189.6	140.6	182.4	149.7	174.9	158.5	166.9	936		
214.2	140.8	209.	111.7	203.3	121.8	197.1	131.7	190.4	141.2	183.2	150.4	175.6	159.2	167.6	937		
215.1	142.3	209.9	112.2	204.1	122.3	197.9	132.2	191.2	141.8	184.	151.	176.3	159.8	168.3	938		
216.1	143.8	210.8	112.7	205.	122.8	198.7	132.8	192.	142.4	184.7	151.6	177.1	160.5	169.	939		
217.	145.3	211.7	113.1	205.9	123.4	199.6	133.3	192.8	143.	185.5	152.3	177.8	161.2	169.7	940		
217.9	146.8	212.5	113.6	206.7	123.9	200.4	133.9	193.6	143.6	186.3	152.9	178.6	161.8	170.4	941		
218.8	148.3	213.4	114.1	207.6	124.4	201.2	134.4	194.4	144.2	187.1	153.5	179.3	162.5	171.1	942		
219.7	149.8	214.3	114.5	208.4	124.9	202.	135.	195.2	144.8	187.8	154.2	180.1	163.2	171.8	943		
220.6	151.3	215.2	115.	209.3	125.4	202.9	135.5	196.	145.4	188.6	154.8	180.8	163.9	172.5	944		
221.5	152.8	216.1	115.5	210.1	126.	203.7	136.1	196.8	145.9	189.4	155.4	181.5	164.5	173.2	945		
222.4	154.3	217.	116.	211.	126.5	204.5	136.7	197.6	146.5	190.2	156.1	182.3	165.2	173.9	946		
223.3	155.8	217.8	116.4	211.9	127.	205.4	137.2	198.4	147.1	190.9	156.7	183.	165.9	174.7	947		
224.2	157.3	218.7	116.9	212.7	127.5	206.2	137.8	199.2	147.7	191.7	157.3	183.8	166.5	175.4	948		
225.1	158.8	219.6	117.4	213.6	128.	207.	138.3	200.	148.3	192.5	158.	184.5	167.2	176.1	949		
226.	160.3	220.5	117.8	214.4	128.5	207.9	138.9	200.8	148.9	193.3	158.6	185.2	167.9	176.8	950		
dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.	N. W. by W.
C. 5½ Pts.	C. 5½ Pts.	C. 5½ Pts.	C. 5½ Pts.	C. 5 Pts.	C. 5 Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4½ Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.	C. 4 Pts.

Distance.	C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 Pt.		C. 1 1/2 Pt.		C. 1 1/2 Pt.		C. 1 1/2 Pt.		C. 2 Pts.	
	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.	N. by E.	S. by E.
	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
251	250.7	12.3	249.8	24.6	248.3	36.8	246.9	49.	243.5	61.	240.9	72.9	236.3	84.6	231.9	96.1
252	251.7	12.4	250.8	24.7	249.3	37.	247.9	49.9	244.4	61.9	241.1	73.2	237.3	84.9	232.9	96.4
253	252.7	12.4	251.8	24.8	250.3	37.1	248.1	49.4	245.4	61.9	242.1	73.4	238.2	85.2	233.7	96.6
254	253.7	12.5	252.8	24.9	251.3	37.3	249.1	49.6	246.4	61.7	243.1	73.7	239.2	85.6	234.7	97.0
255	254.7	12.5	253.8	25.	252.3	37.4	250.1	49.7	247.4	62.	244.1	74.	240.1	85.9	235.6	97.3
256	255.7	12.6	254.8	25.1	253.3	37.6	251.1	49.9	248.3	62.2	245.	74.3	241.	86.2	236.5	97.6
257	256.7	12.6	255.8	25.2	254.3	37.7	252.1	50.1	249.3	62.5	246.	74.6	242.	86.6	237.4	97.9
258	257.7	12.7	256.8	25.3	255.3	37.9	253.1	50.3	250.3	62.7	247.	74.9	243.	86.9	238.3	98.2
259	258.7	12.7	257.8	25.4	256.3	38.	254.	50.5	251.3	62.9	248.	75.2	244.	87.3	239.2	98.5
260	259.7	12.8	258.7	25.5	257.3	38.1	255.	50.7	252.3	63.2	249.	75.5	245.	87.6	240.1	98.8
261	260.7	12.8	259.7	25.6	258.3	38.3	256.	50.9	253.3	63.4	249.8	75.8	245.7	87.9	241.1	99.
262	261.7	12.9	260.7	25.7	259.3	38.4	257.	51.1	254.1	63.7	250.7	76.1	246.7	88.3	242.1	99.3
263	262.7	12.9	261.7	25.8	260.3	38.6	257.9	51.3	255.1	63.9	251.7	76.3	247.6	88.6	243.	99.6
264	263.7	13.	262.7	25.9	261.1	38.7	258.9	51.5	256.1	64.1	252.6	76.6	248.6	88.9	243.9	99.9
265	264.7	13.	263.7	26.	262.1	38.9	259.9	51.7	257.	64.4	253.6	76.9	249.5	89.3	244.8	100.1
266	265.7	13.1	264.7	26.1	263.1	39.	260.9	51.9	258.	64.6	254.5	77.2	250.5	89.6	245.8	100.4
267	266.7	13.1	265.7	26.2	264.1	39.3	261.9	52.1	259.	64.9	255.5	77.5	251.4	89.9	246.7	100.7
268	267.7	13.2	266.7	26.3	265.1	39.5	262.9	52.3	260.	65.1	256.5	77.8	252.3	90.3	247.6	101.
269	268.7	13.2	267.7	26.4	266.1	39.5	263.8	52.5	260.9	65.4	257.4	78.1	253.3	90.6	248.5	101.3
270	269.7	13.2	268.7	26.5	267.1	39.6	264.8	52.7	261.9	65.7	258.4	78.4	254.2	91.	249.4	101.6
271	270.7	13.3	269.7	26.6	268.1	39.8	265.8	52.9	262.8	65.8	259.3	78.7	255.2	91.3	250.4	101.7
272	271.7	13.3	270.7	26.7	269.1	39.9	266.8	53.1	263.8	66.1	260.3	79.	256.1	91.6	251.3	101.9
273	272.7	13.4	271.7	26.8	270.	40.1	267.8	53.3	264.8	66.3	261.2	79.2	257.	92.	252.2	102.
274	273.7	13.4	272.7	26.9	271.	40.2	268.7	53.5	265.8	66.6	262.2	79.5	258.	92.3	253.1	102.1
275	274.7	13.5	273.7	27.	272.	40.4	269.7	53.6	266.7	66.8	263.2	79.8	259.9	92.6	254.1	102.3
276	275.7	13.5	274.7	27.1	273.	40.5	270.7	53.8	267.7	67.1	264.1	80.1	260.9	93.	255.	102.5
277	276.7	13.6	275.7	27.2	274.	40.6	271.7	54.	268.7	67.3	265.1	80.4	261.8	93.3	256.	102.7
278	277.7	13.6	276.7	27.3	275.	40.8	272.7	54.2	269.6	67.5	266.	80.7	262.7	93.7	257.	102.9
279	278.7	13.7	277.7	27.4	276.	40.9	273.6	54.4	270.6	67.8	267.	81.	263.7	94.	257.8	103.
280	279.7	13.7	278.7	27.4	277.	41.1	274.6	54.6	271.6	68.	267.9	81.3	263.6	94.3	258.7	103.1
281	280.7	13.8	279.6	27.5	278.	41.2	275.6	54.8	272.5	68.3	268.9	81.6	264.6	94.7	259.6	103.3
282	281.7	13.8	280.6	27.6	278.9	41.4	276.6	55.	273.5	68.5	269.9	81.9	265.5	95.	260.5	103.5
283	282.7	13.9	281.6	27.7	279.9	41.5	277.6	55.2	274.5	68.8	270.8	82.2	266.5	95.3	261.5	103.7
284	283.7	13.9	282.6	27.8	280.9	41.7	278.6	55.4	275.5	69.1	271.8	82.4	267.4	95.7	262.4	103.9
285	284.7	14.	283.6	27.9	281.9	41.8	279.5	55.6	276.4	69.2	272.7	82.7	268.3	96.	263.3	104.
286	285.7	14.	284.6	28.	282.9	42.	280.5	55.8	277.4	69.5	273.7	83.	269.3	96.4	264.2	104.1
287	286.7	14.1	285.6	28.1	283.9	42.1	281.5	56.	278.4	69.7	274.6	83.3	270.2	96.7	265.1	104.3
288	287.7	14.1	286.6	28.2	284.9	42.3	282.5	56.2	279.3	70.	275.6	83.6	271.2	97.	266.	104.5
289	288.7	14.2	287.6	28.3	285.9	42.4	283.4	56.4	280.3	70.2	276.6	83.9	272.1	97.4	267.	104.7
290	289.7	14.2	288.6	28.4	286.9	42.6	284.4	56.6	281.3	70.5	277.5	84.2	273.	97.7	267.9	104.9
291	290.6	14.3	289.6	28.5	287.9	42.7	285.4	56.8	282.2	70.7	278.5	84.5	274.	98.	268.8	105.
292	291.6	14.3	290.6	28.6	288.8	42.8	286.4	57.	283.2	71.	279.4	84.8	275.	98.4	269.8	105.1
293	292.6	14.4	291.6	28.7	289.8	43.	287.4	57.2	284.2	71.2	280.4	85.1	276.9	98.7	270.7	105.3
294	293.6	14.4	292.6	28.8	290.8	43.1	288.4	57.4	285.2	71.4	281.3	85.3	277.8	99.	271.6	105.5
295	294.6	14.5	293.6	28.9	291.8	43.3	289.3	57.6	286.1	71.7	282.3	85.6	277.8	99.4	272.5	105.7
296	295.6	14.5	294.6	29.	292.8	43.4	290.3	57.7	287.1	71.9	283.3	85.9	278.7	99.7	273.5	105.9
297	296.6	14.6	295.6	29.1	293.8	43.6	291.3	57.9	288.1	72.2	284.2	86.2	279.6	100.1	274.4	106.1
298	297.6	14.6	296.6	29.2	294.8	43.7	292.3	58.1	289.	72.4	285.2	86.5	280.6	100.4	275.3	106.3
299	298.6	14.7	297.6	29.3	295.8	43.9	293.3	58.3	290.	72.7	286.1	86.8	281.5	100.7	276.2	106.5
300	299.6	14.7	298.6	29.4	296.8	44.	294.3	58.5	291.	72.9	287.1	87.1	282.5	101.1	277.2	106.7
Distance.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	W. 1/2 N.	E. 1/2 S.	
	W. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	W. 1/2 S.	E. 1/2 N.	
	W. 1/2 S.	W. 1/2 N														

C. 2½ Pts.		C. 2½ Pts.		C. 2½ Pts.		C. 3 Pts.		C. 3½ Pts.		C. 3½ Pts.		C. 4 Pts.		Distance.	
N. N. E. † E.	S. S. E. † E.	N. N. E. † E.	S. S. E. † E.	N. N. E. † E.	S. S. E. † E.	N. E. by N.	S. E. by S.	N. E. † S.	S. E. † S.	N. E. † N.	S. E. † S.	N. E. † S.	S. E. † S.		
d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.
298.9	107.3	291.4	118.3	215.3	189.	908.7	139.4	901.6	149.5	194.	199.9	198.	198.6	177.5	251
297.9	107.7	292.9	118.9	216.1	189.6	906.5	140.	902.4	152.1	194.8	199.9	197.7	199.9	178.2	252
298.7	108.2	293.1	119.3	217.	190.	910.4	140.5	903.9	155.7	195.8	199.9	197.5	199.9	178.9	253
299.6	108.6	294.	119.7	217.9	190.6	911.9	141.1	904.	151.9	196.9	199.9	198.2	199.9	179.6	254
299.5	109.	294.9	120.3	218.7	191.1	912.	141.7	904.8	151.9	197.1	199.9	198.9	199.9	180.3	255
321.4	109.5	295.8	190.7	219.6	191.6	912.9	142.9	905.6	152.5	197.9	199.9	199.7	199.9	181.	256
322.3	109.9	296.7	191.1	220.4	192.1	913.7	142.8	906.4	153.1	198.7	199.9	199.4	199.9	181.7	257
323.2	110.3	297.5	191.6	221.3	192.6	914.5	143.3	907.2	153.7	199.4	199.9	199.1	199.9	182.4	258
324.1	110.7	298.4	192.1	222.2	193.1	915.4	143.9	908.	154.3	200.2	199.9	199.8	199.9	183.1	259
325.	111.2	299.3	192.6	223.	193.7	916.2	144.4	908.8	154.9	201.	199.9	199.6	199.9	183.8	260
326.9	111.6	299.2	193.	223.9	194.9	917.	145.	909.6	155.5	201.8	199.9	199.3	199.9	184.6	261
328.8	112.	291.1	192.3	224.7	194.7	917.8	145.5	910.4	156.	202.5	199.9	199.4	199.9	185.3	262
327.7	112.4	291.9	194.	225.6	195.9	918.7	146.1	911.2	156.7	203.3	199.9	199.1	199.9	186.	263
328.6	112.9	292.8	194.4	226.4	195.7	919.5	146.7	912.	157.3	204.1	199.9	198.6	199.9	186.7	264
329.6	113.3	293.7	194.9	227.3	196.9	920.3	147.9	912.8	157.9	204.8	199.9	198.3	199.9	187.4	265
340.5	113.7	294.6	195.4	228.2	196.8	921.2	147.8	913.7	158.5	205.6	199.9	197.1	199.9	188.1	266
341.4	114.	295.5	195.9	229.	197.3	922.	148.3	914.5	159.1	206.4	199.9	197.8	199.9	188.8	267
342.3	114.6	296.4	196.3	229.9	197.8	922.8	148.9	915.3	159.6	207.2	199.9	198.6	199.9	189.5	268
343.2	115.	297.3	196.8	230.7	198.3	923.7	149.4	916.1	160.9	207.9	199.9	199.3	199.9	190.2	269
344.1	115.4	298.2	197.3	231.6	198.8	924.5	150.	916.9	160.8	208.7	199.9	199.1	199.9	190.9	270
345.	115.9	299.	197.7	232.4	199.3	925.3	150.5	917.7	161.4	209.5	199.9	199.8	199.9	191.6	271
345.9	116.2	299.9	198.2	233.3	199.8	926.2	151.1	918.5	162.	210.3	199.9	199.5	199.9	192.3	272
346.8	116.7	300.8	198.7	234.2	140.4	927.	151.7	919.3	162.6	211.1	199.9	199.2	199.9	193.	273
347.7	117.2	301.6	199.2	235.	140.9	927.8	152.2	920.1	163.9	211.8	199.9	198.9	199.9	193.7	274
348.6	117.6	302.5	199.6	235.8	141.4	928.7	152.8	920.9	163.8	212.6	199.9	198.6	199.9	194.5	275
349.5	118.	303.4	130.1	236.7	141.9	929.5	153.3	921.7	164.4	213.4	199.9	198.4	199.9	195.2	276
349.4	118.4	304.3	130.6	237.6	142.4	930.3	153.9	922.5	165.	214.1	199.9	198.1	199.9	195.9	277
350.3	118.9	305.2	131.	238.4	142.9	931.1	154.4	923.3	165.6	214.9	199.9	197.8	199.9	196.6	278
352.2	119.3	306.1	131.5	239.3	143.4	932.	155.	924.1	166.2	215.7	199.9	197.5	199.9	197.3	279
353.1	119.7	307.	132.	240.2	143.9	932.8	155.5	924.9	166.8	216.4	199.9	197.2	199.9	198.	280
354.	120.	307.9	132.5	241.	144.5	933.6	156.1	925.7	167.4	217.2	199.9	196.9	199.9	198.7	281
354.9	120.6	308.8	133.	241.9	145.	934.5	156.7	926.5	168.	218.	199.9	196.6	199.9	199.4	282
355.8	121.	309.6	133.4	242.7	145.5	935.3	157.3	927.3	168.6	218.8	199.9	196.3	199.9	200.1	283
356.7	121.4	310.5	133.9	243.6	146.	936.1	157.8	928.1	169.2	219.5	199.9	196.	199.9	200.8	284
357.6	121.9	311.3	134.3	244.5	146.5	937.	158.3	928.9	169.8	220.3	199.9	195.7	199.9	201.5	285
358.5	122.3	312.2	134.8	245.3	147.	937.8	158.9	929.7	170.4	221.1	199.9	195.4	199.9	202.2	286
359.4	122.7	313.1	135.3	246.2	147.5	938.6	159.4	930.5	171.	221.9	199.9	195.1	199.9	202.9	287
360.3	123.1	314.	135.8	247.	148.1	939.5	160.	931.3	171.6	222.7	199.9	194.8	199.9	203.6	288
361.2	123.5	314.9	136.3	247.9	148.6	940.3	160.5	932.1	172.2	223.4	199.9	194.5	199.9	204.3	289
362.1	124.	315.8	136.8	248.7	149.1	941.1	161.1	932.9	172.8	224.2	199.9	194.2	199.9	205.1	290
363.1	124.4	316.6	137.3	249.6	149.6	942.	161.7	933.7	173.3	224.9	199.9	193.9	199.9	205.8	291
364.	124.8	317.5	137.8	250.5	150.1	942.8	162.2	934.5	173.9	225.7	199.9	193.6	199.9	206.5	292
364.9	125.3	318.4	138.3	251.4	150.6	943.6	162.8	935.3	174.5	226.5	199.9	193.3	199.9	207.2	293
365.8	125.7	319.3	138.8	252.2	151.1	944.5	163.3	936.1	175.1	227.3	199.9	193.	199.9	207.9	294
366.7	126.1	320.2	139.3	253.	151.7	945.3	163.9	936.9	175.7	228.	199.9	192.7	199.9	208.6	295
367.6	126.6	321.1	139.8	253.9	152.2	946.1	164.4	937.7	176.3	228.8	199.9	192.4	199.9	209.3	296
368.5	127.	322.	140.3	254.7	152.7	946.9	165.	938.5	176.9	229.6	199.9	192.1	199.9	210.	297
369.4	127.4	322.9	140.8	255.6	153.2	947.8	165.5	939.4	177.5	230.4	199.9	191.8	199.9	210.7	298
370.3	127.9	323.7	141.3	256.5	153.7	948.6	166.	940.2	178.1	231.1	199.9	191.5	199.9	211.4	299
371.2	128.3	324.6	141.8	257.3	154.2	949.4	166.7	941.	178.7	231.9	199.9	191.2	199.9	212.1	300
dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.	dep.	d. lat.
N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.	N. W. by W. † W.	S. W. by W. † W.
C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.	C. 2½ Pts.

TABLE V.

**DISTANCE, DIFFERENCE OF LATITUDE,
AND DEPARTURE.**

Course 10.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.	61	61.	1.1	121	121.	2.1	181	181.	3.1	241	241.	4.1
2	2.	0.	62	62.	1.1	2	122.	2.1	2	182.	3.2	3	242.	4.2
3	3.	0.1	63	63.	1.1	3	123.	2.1	3	183.	3.3	3	243.	4.2
4	4.	0.1	64	64.	1.1	4	124.	2.2	4	184.	3.4	4	244.	4.3
5	5.	0.1	65	65.	1.1	5	125.	2.2	5	185.	3.4	5	245.	4.3
6	6.	0.1	66	66.	1.2	6	126.	2.3	6	186.	3.5	6	246.	4.3
7	7.	0.1	67	67.	1.2	7	127.	2.3	7	187.	3.5	7	247.	4.3
8	8.	0.1	68	68.	1.2	8	128.	2.3	8	188.	3.5	8	248.	4.3
9	9.	0.2	69	69.	1.2	9	129.	2.3	9	189.	3.5	9	249.	4.3
10	10.	0.2	70	70.	1.2	120	120.	2.3	190	190.	3.5	250	250.	4.4
11	11.	0.2	71	71.	1.2	1	131.	2.3	1	191.	3.5	1	251.	4.4
12	12.	0.2	72	72.	1.2	2	132.	2.3	2	192.	3.5	2	252.	4.4
13	13.	0.2	73	73.	1.3	3	133.	2.3	3	193.	3.5	3	253.	4.4
14	14.	0.2	74	74.	1.3	4	134.	2.4	4	194.	3.4	4	254.	4.4
15	15.	0.3	75	75.	1.3	5	135.	2.4	5	195.	3.4	5	255.	4.5
16	16.	0.3	76	76.	1.3	6	136.	2.4	6	196.	3.4	6	256.	4.5
17	17.	0.3	77	77.	1.3	7	137.	2.4	7	197.	3.4	7	257.	4.5
18	18.	0.3	78	78.	1.4	8	138.	2.4	8	198.	3.5	8	258.	4.5
19	19.	0.3	79	79.	1.4	9	139.	2.4	9	199.	3.5	9	259.	4.5
20	20.	0.3	80	80.	1.4	140	140.	2.4	200	200.	3.5	260	260.	4.5
21	21.	0.4	81	81.	1.4	1	141.	2.5	1	201.	3.5	1	261.	4.6
22	22.	0.4	82	82.	1.4	2	142.	2.5	2	202.	3.5	2	262.	4.6
23	23.	0.4	83	83.	1.4	3	143.	2.5	3	203.	3.5	3	263.	4.6
24	24.	0.4	84	84.	1.5	4	144.	2.5	4	204.	3.6	4	264.	4.6
25	25.	0.4	85	85.	1.5	5	145.	2.5	5	205.	3.6	5	265.	4.6
26	26.	0.5	86	86.	1.5	6	146.	2.5	6	206.	3.6	6	266.	4.6
27	27.	0.5	87	87.	1.5	7	147.	2.6	7	207.	3.6	7	267.	4.7
28	28.	0.5	88	88.	1.5	8	148.	2.6	8	208.	3.6	8	268.	4.7
29	29.	0.5	89	89.	1.6	9	149.	2.6	9	209.	3.6	9	269.	4.7
30	30.	0.5	90	90.	1.6	150	150.	2.6	210	210.	3.7	270	270.	4.7
31	31.	0.5	91	91.	1.6	1	151.	2.6	1	211.	3.7	1	271.	4.7
32	32.	0.6	92	92.	1.6	2	152.	2.7	2	212.	3.7	2	272.	4.7
33	33.	0.6	93	93.	1.6	3	153.	2.7	3	213.	3.7	3	273.	4.8
34	34.	0.6	94	94.	1.6	4	154.	2.7	4	214.	3.7	4	274.	4.8
35	35.	0.6	95	95.	1.7	5	155.	2.7	5	215.	3.8	5	275.	4.8
36	36.	0.6	96	96.	1.7	6	156.	2.7	6	216.	3.8	6	276.	4.8
37	37.	0.6	97	97.	1.7	7	157.	2.7	7	217.	3.8	7	277.	4.8
38	38.	0.7	98	98.	1.7	8	158.	2.8	8	218.	3.8	8	278.	4.9
39	39.	0.7	99	99.	1.7	9	159.	2.8	9	219.	3.8	9	279.	4.9
40	40.	0.7	100	100.	1.7	160	160.	2.8	220	220.	3.8	280	280.	4.9
41	41.	0.7	1	101.	1.8	1	161.	2.8	1	221.	3.9	1	281.	4.9
42	42.	0.7	2	102.	1.8	2	162.	2.8	2	222.	3.9	2	282.	4.9
43	43.	0.8	3	103.	1.8	3	163.	2.8	3	223.	3.9	3	283.	4.9
44	44.	0.8	4	104.	1.8	4	164.	2.9	4	224.	3.9	4	284.	5
45	45.	0.8	5	105.	1.8	5	165.	2.9	5	225.	3.9	5	285.	5
46	46.	0.8	6	106.	1.8	6	166.	2.9	6	226.	3.9	6	286.	5
47	47.	0.8	7	107.	1.9	7	167.	2.9	7	227.	4.	7	287.	5
48	48.	0.8	8	108.	1.9	8	168.	2.9	8	228.	4.	8	288.	5
49	49.	0.9	9	109.	1.9	9	169.	2.9	9	229.	4.	9	289.	5
50	50.	0.9	110	110.	1.9	170	170.	3.	230	230.	4.	290	290.	5.1
51	51.	0.9	1	111.	1.9	1	171.	3.	1	231.	4.	1	291.	5.1
52	52.	0.9	2	112.	2.	2	172.	3.	2	232.	4.	2	292.	5.1
53	53.	0.9	3	113.	2.	3	173.	3.	3	233.	4.1	3	293.	5.1
54	54.	0.9	4	114.	2.	4	174.	3.	4	234.	4.1	4	294.	5.1
55	55.	1.	5	115.	2.	5	175.	3.1	5	235.	4.1	5	295.	5.1
56	56.	1.	6	116.	2.	6	176.	3.1	6	236.	4.1	6	296.	5.2
57	57.	1.	7	117.	2.	7	177.	3.1	7	237.	4.1	7	297.	5.2
58	58.	1.	8	118.	2.1	8	178.	3.1	8	238.	4.2	8	298.	5.2
59	59.	1.	9	119.	2.1	9	179.	3.1	9	239.	4.2	9	299.	5.2
60	60.	1.	120	120.	2.1	180	180.	3.1	240	240.	4.2	300	300.	5.2
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 80°.

Course 90°.

Distance, Diff Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.	61	61.	2.1	181	180.9	4.8	181	180.9	6.3	281	280.9	8.4
2	2.	0.1	62	62.	2.2	2	181.9	4.3	2	181.9	6.4	3	281.9	8.4
3	3.	0.1	63	63.	2.3	3	182.9	4.3	3	182.9	6.4	3	282.9	8.5
4	4.	0.1	64	64.	2.4	4	183.0	4.3	4	183.9	6.4	4	283.9	8.5
5	5.	0.2	65	65.	2.3	5	184.9	4.4	5	184.9	6.5	5	284.9	8.6
6	6.	0.9	66	66.	2.3	6	185.9	4.4	6	185.9	6.5	6	285.9	8.6
7	7.	0.2	67	67.	2.3	7	186.9	4.4	7	186.9	6.5	7	286.9	8.6
8	8.	0.3	68	68.	2.4	8	187.9	4.5	8	187.9	6.6	8	287.9	8.7
9	9.	0.3	69	69.	2.4	9	188.9	4.5	9	188.9	6.6	9	288.9	8.7
10	10.	0.3	70	70.	2.4	180	189.9	4.5	180	189.9	6.6	280	289.9	8.7
11	11.	0.4	71	71.	2.5	1	190.9	4.6	1	190.9	6.7	1	290.9	8.8
12	12.	0.4	72	72.	2.5	2	191.9	4.6	2	191.9	6.7	2	291.9	8.8
13	13.	0.5	73	73.	2.5	3	192.9	4.6	3	192.9	6.7	3	292.9	8.8
14	14.	0.5	74	74.	2.6	4	193.9	4.7	4	193.9	6.8	4	293.9	8.9
15	15.	0.5	75	75.	2.6	5	194.9	4.7	5	194.9	6.8	5	294.9	8.9
16	16.	0.6	76	76.	2.7	6	195.9	4.7	6	195.9	6.8	6	295.9	8.9
17	17.	0.6	77	77.	2.7	7	196.9	4.8	7	196.9	6.9	7	296.9	9.
18	18.	0.6	78	78.	2.7	8	197.9	4.8	8	197.9	6.9	8	297.9	9.
19	19.	0.7	79	79.	2.8	9	198.9	4.9	9	198.9	6.9	9	298.9	9.
20	20.	0.7	80	80.	2.8	140	199.9	4.9	200	199.9	7.	280	299.9	9.1
21	21.	0.7	81	81.	2.8	1	200.9	4.9	1	200.9	7.	1	200.9	9.1
22	22.	0.8	82	82.	2.9	2	201.9	5.	2	201.9	7.	2	201.9	9.1
23	23.	0.8	83	83.	2.9	3	202.9	5.	3	202.9	7.1	3	202.9	9.2
24	24.	0.8	84	84.	2.9	4	203.9	5.	4	203.9	7.1	4	203.9	9.2
25	25.	0.9	85	85.	3.	5	204.9	5.1	5	204.9	7.2	5	204.9	9.2
26	26.	0.9	86	86.	3.	6	205.9	5.1	6	205.9	7.2	6	205.9	9.3
27	27.	0.9	87	87.	3.	7	206.9	5.1	7	206.9	7.2	7	206.9	9.3
28	28.	1.	88	88.	3.1	8	207.9	5.2	8	207.9	7.3	8	207.9	9.4
29	29.	1.	89	89.	3.1	9	208.9	5.2	9	208.9	7.3	9	208.9	9.4
30	30.	1.	90	90.	3.1	150	209.9	5.2	210	209.9	7.3	270	209.9	9.4
31	31.	1.1	91	91.	3.2	1	210.9	5.3	1	210.9	7.4	1	270.9	9.5
32	32.	1.1	92	92.	3.2	2	211.9	5.3	2	211.9	7.4	2	271.9	9.5
33	33.	1.2	93	93.	3.2	3	212.9	5.3	3	212.9	7.4	3	272.9	9.5
34	34.	1.3	94	94.	3.3	4	213.9	5.4	4	213.9	7.5	4	273.9	9.6
35	35.	1.3	95	95.	3.3	5	214.9	5.4	5	214.9	7.5	5	274.9	9.6
36	36.	1.3	96	96.	3.4	6	215.9	5.4	6	215.9	7.5	6	275.9	9.6
37	37.	1.3	97	97.	3.4	7	216.9	5.5	7	216.9	7.6	7	276.9	9.7
38	38.	1.3	98	98.	3.4	8	217.9	5.5	8	217.9	7.6	8	277.9	9.7
39	39.	1.4	99	99.	3.5	9	218.9	5.5	9	218.9	7.6	9	278.9	9.7
40	40.	1.4	100	100.	3.5	160	219.9	5.6	220	219.9	7.7	280	279.9	9.8
41	41.	1.4	1	100.9	3.5	1	220.9	5.6	1	220.9	7.7	1	280.9	9.8
42	42.	1.5	2	101.9	3.6	2	221.9	5.7	2	221.9	7.7	2	281.9	9.8
43	43.	1.5	3	102.9	3.6	3	222.9	5.7	3	222.9	7.8	3	282.9	9.9
44	44.	1.5	4	103.9	3.6	4	223.9	5.7	4	223.9	7.8	4	283.9	9.9
45	45.	1.6	5	104.9	3.7	5	224.9	5.8	5	224.9	7.9	5	284.9	9.9
46	46.	1.6	6	105.9	3.7	6	225.9	5.8	6	225.9	7.9	6	285.9	10.
47	47.	1.6	7	106.9	3.7	7	226.9	5.8	7	226.9	7.9	7	286.9	10.
48	48.	1.7	8	107.9	3.8	8	227.9	5.9	8	227.9	8.	8	287.9	10.1
49	49.	1.7	9	108.9	3.8	9	228.9	5.9	9	228.9	8.	9	288.9	10.1
50	50.	1.7	110	109.9	3.8	170	229.9	5.9	230	229.9	8.	290	289.9	10.1
51	51.	1.8	1	110.9	3.9	1	230.9	6.	1	230.9	8.1	1	290.9	10.2
52	52.	1.8	2	111.9	3.9	2	231.9	6.	2	231.9	8.1	2	291.9	10.2
53	53.	1.8	3	112.9	3.9	3	232.9	6.	3	232.9	8.1	3	292.9	10.2
54	54.	1.9	4	113.9	4.	4	233.9	6.1	4	233.9	8.2	4	293.9	10.3
55	55.	1.9	5	114.9	4.	5	234.9	6.1	5	234.9	8.2	5	294.9	10.3
56	56.	2.	6	115.9	4.	6	235.9	6.1	6	235.9	8.2	6	295.9	10.3
57	57.	2.	7	116.9	4.1	7	236.9	6.2	7	236.9	8.3	7	296.9	10.4
58	58.	2.	8	117.9	4.1	8	237.9	6.2	8	237.9	8.3	8	297.9	10.4
59	59.	2.1	9	118.9	4.2	9	238.9	6.2	9	238.9	8.3	9	298.9	10.4
60	60.	2.1	190	119.9	4.2	180	239.9	6.3	240	239.9	8.4	300	299.9	10.5
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff Latitude.

Course 90°

Course 30°.

Distance, Diff. Latitude and Departure

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.9	3.9	121	120.8	6.3	181	180.8	9.5	241	240.7	12.6
2	2.	0.1	62	61.9	3.9	2	121.8	6.4	2	181.8	9.5	2	241.7	12.7
3	3.	0.2	63	62.9	3.3	3	122.8	6.4	3	182.7	9.6	3	242.7	12.7
4	4.	0.2	64	63.9	3.3	4	123.8	6.5	4	183.7	9.6	4	243.7	12.8
5	5.	0.3	65	64.9	3.4	5	124.8	6.5	5	184.7	9.7	5	244.7	12.8
6	6.	0.3	66	65.9	3.5	6	125.8	6.6	6	185.7	9.7	6	245.7	12.9
7	7.	0.4	67	66.9	3.5	7	126.8	6.6	7	186.7	9.8	7	246.7	12.9
8	8.	0.4	68	67.9	3.6	8	127.8	6.7	8	187.7	9.8	8	247.7	13.
9	9.	0.5	69	68.9	3.6	9	128.8	6.8	9	188.7	9.9	9	248.7	13.
10	10.	0.5	70	69.9	3.7	130	129.8	6.8	190	189.7	9.9	250	249.7	13.1
11	11.	0.6	71	70.9	3.7	1	130.8	6.9	1	190.7	10	1	250.7	13.1
12	12.	0.6	72	71.9	3.8	2	131.8	6.9	2	191.7	10.	2	251.7	13.2
13	13.	0.7	73	72.9	3.8	3	132.8	7.	3	192.7	10.1	3	252.7	13.2
14	14.	0.7	74	73.9	3.9	4	133.8	7.	4	193.7	10.2	4	253.7	13.3
15	15.	0.8	75	74.9	3.9	5	134.8	7.1	5	194.7	10.2	5	254.7	13.3
16	16.	0.8	76	75.9	4.	6	135.8	7.1	6	195.7	10.3	6	255.6	13.4
17	17.	0.9	77	76.9	4.	7	136.8	7.2	7	196.7	10.3	7	256.6	13.5
18	18.	0.9	78	77.9	4.1	8	137.8	7.2	8	197.7	10.4	8	257.6	13.5
19	19.	1.	79	78.9	4.1	9	138.8	7.3	9	198.7	10.4	9	258.6	13.6
20	20.	1.	80	79.9	4.2	140	139.8	7.3	200	199.7	10.5	260	259.6	13.6
21	21.	1.1	81	80.9	4.2	1	140.8	7.4	1	200.7	10.5	1	260.6	13.7
22	22.	1.2	82	81.9	4.3	2	141.8	7.4	2	201.7	10.6	2	261.6	13.7
23	23.	1.2	83	82.9	4.3	3	142.8	7.5	3	202.7	10.6	3	262.6	13.8
24	24.	1.3	84	83.9	4.4	4	143.8	7.5	4	203.7	10.7	4	263.6	13.8
25	25.	1.3	85	84.9	4.4	5	144.8	7.6	5	204.7	10.7	5	264.6	13.9
26	26.	1.4	86	85.9	4.5	6	145.8	7.6	6	205.7	10.8	6	265.6	13.9
27	27.	1.4	87	86.9	4.6	7	146.8	7.7	7	206.7	10.8	7	266.6	14.
28	28.	1.5	88	87.9	4.6	8	147.8	7.7	8	207.7	10.9	8	267.6	14.
29	29.	1.5	89	88.9	4.7	9	148.8	7.8	9	208.7	10.9	9	268.6	14.1
30	30.	1.6	90	89.9	4.7	150	149.8	7.9	210	209.7	11.	270	269.6	14.1
31	31.	1.6	91	90.9	4.8	1	150.8	7.9	1	210.7	11.	1	270.6	14.2
32	32.	1.7	92	91.9	4.8	2	151.8	8.	2	211.7	11.1	2	271.6	14.2
33	33.	1.7	93	92.9	4.9	3	152.8	8.	3	212.7	11.1	3	272.6	14.3
34	34.	1.8	94	93.9	4.9	4	153.8	8.1	4	213.7	11.2	4	273.6	14.3
35	35.	1.8	95	94.9	5.	5	154.8	8.1	5	214.7	11.3	5	274.6	14.4
36	36.	1.9	96	95.9	5.	6	155.8	8.2	6	215.7	11.3	6	275.6	14.4
37	36.9	1.9	97	96.9	5.1	7	156.8	8.2	7	216.7	11.4	7	276.6	14.5
38	37.9	2.	98	97.9	5.1	8	157.8	8.3	8	217.7	11.4	8	277.6	14.5
39	38.9	2.	99	98.9	5.2	9	158.8	8.3	9	218.7	11.5	9	278.6	14.6
40	39.9	2.1	100	99.9	5.2	160	159.8	8.4	220	219.7	11.5	280	279.6	14.7
41	40.9	2.1	1	100.9	5.3	1	160.8	8.4	1	220.7	11.6	1	280.6	14.7
42	41.9	2.2	2	101.9	5.3	2	161.8	8.5	2	221.7	11.6	2	281.6	14.8
43	42.9	2.3	3	102.9	5.4	3	162.8	8.5	3	222.7	11.7	3	282.6	14.8
44	43.9	2.3	4	103.9	5.4	4	163.8	8.6	4	223.7	11.7	4	283.6	14.9
45	44.9	2.4	5	104.9	5.5	5	164.8	8.6	5	224.7	11.8	5	284.6	14.9
46	45.9	2.4	6	105.9	5.5	6	165.8	8.7	6	225.7	11.9	6	285.6	15.
47	46.9	2.5	7	106.9	5.6	7	166.8	8.7	7	226.7	11.9	7	286.6	15.
48	47.9	2.5	8	107.9	5.7	8	167.8	8.8	8	227.7	11.9	8	287.6	15.1
49	48.9	2.6	9	108.9	5.7	9	168.8	8.8	9	228.7	12.	9	288.6	15.1
50	49.9	2.6	110	109.8	5.8	170	169.8	8.9	230	229.7	12.	290	289.6	15.2
51	50.9	2.7	1	110.8	5.8	1	170.8	8.9	1	230.7	12.1	1	290.6	15.2
52	51.9	2.7	2	111.8	5.9	2	171.8	9.	2	231.7	12.1	2	291.6	15.3
53	52.9	2.8	3	112.8	5.9	3	172.8	9.1	3	232.7	12.2	3	292.6	15.3
54	53.9	2.8	4	113.8	6.	4	173.8	9.1	4	233.7	12.2	4	293.6	15.4
55	54.9	2.9	5	114.8	6.	5	174.8	9.2	5	234.7	12.3	5	294.6	15.4
56	55.9	2.9	6	115.8	6.1	6	175.8	9.2	6	235.7	12.4	6	295.6	15.5
57	56.9	3.	7	116.8	6.1	7	176.8	9.3	7	236.7	12.4	7	296.6	15.5
58	57.9	3.	8	117.8	6.2	8	177.8	9.3	8	237.7	12.5	8	297.6	15.6
59	58.9	3.1	9	118.8	6.2	9	178.8	9.4	9	238.7	12.5	9	298.6	15.6
60	59.9	3.1	190	119.8	6.3	180	179.8	9.4	240	239.7	12.6	300	299.6	15.7
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 37°.

Course 40.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.9	4.3	121	120.7	8.4	181	180.6	12.6	241	240.4	16.6
2	2.	0.1	62	61.8	4.3	2	131.7	8.5	2	181.6	12.7	2	241.4	16.9
3	3.	0.2	63	62.8	4.4	3	132.7	8.6	3	182.6	12.8	3	242.4	17.
4	4.	0.3	64	63.8	4.5	4	133.7	8.6	4	183.6	12.8	4	243.4	17.
5	5.	0.3	65	64.8	4.5	5	134.7	8.7	5	184.5	12.9	5	244.4	17.1
6	6.	0.4	66	65.8	4.6	6	135.7	8.8	6	185.5	13.	6	245.4	17.2
7	7.	0.5	67	66.8	4.7	7	136.7	8.9	7	186.5	13.	7	246.4	17.2
8	8.	0.6	68	67.8	4.7	8	137.7	8.9	8	187.5	13.1	8	247.4	17.3
9	9.	0.6	69	68.8	4.8	9	138.7	9.	9	188.5	13.2	9	248.4	17.4
10	10.	0.7	70	69.8	4.9	130	139.7	9.1	190	189.5	13.3	250	249.4	17.4
11	11.	0.8	71	70.8	5.	1	130.7	9.1	1	190.5	13.3	1	250.4	17.5
12	12.	0.8	72	71.8	5.	2	131.7	9.2	2	191.5	13.4	2	251.4	17.6
13	13.	0.9	73	72.8	5.1	3	132.7	9.3	3	192.5	13.5	3	252.4	17.6
14	14.	1.	74	73.8	5.2	4	133.7	9.3	4	193.5	13.5	4	253.4	17.7
15	15.	1.	75	74.8	5.2	5	134.7	9.4	5	194.5	13.6	5	254.4	17.8
16	16.	1.1	76	75.8	5.3	6	135.7	9.5	6	195.5	13.7	6	255.4	17.9
17	17.	1.2	77	76.8	5.4	7	136.7	9.6	7	196.5	13.7	7	256.4	17.9
18	18.	1.3	78	77.8	5.4	8	137.7	9.6	8	197.5	13.8	8	257.4	18.
19	19.	1.3	79	78.8	5.5	9	138.7	9.7	9	198.5	13.9	9	258.4	18.1
20	20.	1.4	80	79.8	5.6	140	139.7	9.8	200	199.5	14.	260	259.4	18.1
21	20.9	1.5	81	80.8	5.7	1	140.7	9.8	1	200.5	14.	1	260.4	18.2
22	21.0	1.5	82	81.8	5.7	2	141.7	9.9	2	201.5	14.1	2	261.4	18.3
23	20.9	1.6	83	82.8	5.8	3	142.7	10.	3	202.5	14.2	3	262.4	18.3
24	20.9	1.7	84	83.8	5.9	4	143.6	10.	4	203.5	14.2	4	263.4	18.4
25	20.9	1.7	85	84.8	5.9	5	144.6	10.1	5	204.5	14.3	5	264.4	18.5
26	20.9	1.8	86	85.8	6.	6	145.6	10.2	6	205.5	14.4	6	265.4	18.6
27	20.9	1.9	87	86.8	6.1	7	146.6	10.3	7	206.5	14.4	7	266.4	18.7
28	20.9	2.	88	87.8	6.1	8	147.6	10.3	8	207.5	14.5	8	267.4	18.7
29	20.9	2.	89	88.8	6.2	9	148.6	10.4	9	208.5	14.6	9	268.4	18.8
30	20.9	2.1	90	89.8	6.3	150	149.6	10.5	210	209.5	14.6	270	269.4	18.8
31	20.9	2.2	91	90.8	6.3	1	150.6	10.5	1	210.5	14.7	1	270.4	18.9
32	21.0	2.2	92	91.8	6.4	2	151.6	10.6	2	211.5	14.8	2	271.4	19.
33	20.9	2.3	93	92.8	6.5	3	152.6	10.7	3	212.5	14.9	3	272.4	19.
34	20.9	2.4	94	93.8	6.6	4	153.6	10.7	4	213.5	14.9	4	273.4	19.1
35	20.9	2.4	95	94.8	6.6	5	154.6	10.8	5	214.5	15.	5	274.4	19.2
36	20.9	2.5	96	95.8	6.7	6	155.6	10.9	6	215.5	15.1	6	275.4	19.3
37	20.9	2.6	97	96.8	6.8	7	156.6	11.	7	216.5	15.1	7	276.4	19.3
38	20.9	2.7	98	97.8	6.8	8	157.6	11.	8	217.5	15.2	8	277.4	19.4
39	20.9	2.7	99	98.8	6.9	9	158.6	11.1	9	218.5	15.3	9	278.4	19.5
40	20.9	2.8	100	99.8	7.	160	159.6	11.2	220	219.5	15.3	280	279.4	19.5
41	40.9	2.9	1	100.8	7.	1	160.6	11.3	1	220.5	15.4	1	280.4	19.6
42	41.0	2.9	2	101.8	7.1	2	161.6	11.3	2	221.5	15.5	2	281.4	19.7
43	40.9	3.	3	102.7	7.2	3	162.6	11.4	3	222.5	15.6	3	282.4	19.7
44	40.9	3.1	4	103.7	7.3	4	163.6	11.4	4	223.5	15.6	4	283.4	19.8
45	40.9	3.1	5	104.7	7.3	5	164.6	11.5	5	224.5	15.7	5	284.4	19.9
46	40.9	3.2	6	105.7	7.4	6	165.6	11.6	6	225.4	15.8	6	285.4	20.
47	40.9	3.3	7	106.7	7.5	7	166.6	11.6	7	226.4	15.8	7	286.4	20.
48	40.9	3.3	8	107.7	7.5	8	167.6	11.7	8	227.4	15.9	8	287.4	20.1
49	40.9	3.4	9	108.7	7.6	9	168.6	11.8	9	228.4	16.	9	288.4	20.2
50	40.9	3.5	110	109.7	7.7	170	169.6	11.9	230	229.4	16.	290	289.4	20.2
51	50.9	3.6	1	110.7	7.7	1	170.6	11.9	1	230.4	16.1	1	290.4	20.3
52	51.0	3.6	2	111.7	7.8	2	171.6	12.	2	231.4	16.2	2	291.4	20.4
53	50.9	3.7	3	112.7	7.9	3	172.6	12.1	3	232.4	16.3	3	292.4	20.4
54	50.9	3.8	4	113.7	8.	4	173.6	12.1	4	233.4	16.3	4	293.4	20.5
55	50.9	3.8	5	114.7	8.	5	174.6	12.2	5	234.4	16.4	5	294.4	20.6
56	50.9	3.9	6	115.7	8.1	6	175.6	12.3	6	235.4	16.5	6	295.4	20.6
57	50.9	4.	7	116.7	8.2	7	176.6	12.3	7	236.4	16.5	7	296.4	20.7
58	50.9	4.	8	117.7	8.2	8	177.6	12.4	8	237.4	16.6	8	297.4	20.8
59	50.9	4.1	9	118.7	8.3	9	178.6	12.5	9	238.4	16.7	9	298.4	20.9
60	50.9	4.2	190	119.7	8.4	180	179.6	12.6	240	239.4	16.7	300	299.4	20.9
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude

Course 60°.

Course 50.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.8	5.3	121	120.5	10.5	181	180.3	15.8	241	240.1	21.
2	2.	0.2	62	61.8	5.4	2	121.5	10.6	2	181.3	15.9	2	241.1	21.1
3	3.	0.3	63	62.8	5.5	3	122.5	10.7	3	182.3	15.9	3	242.1	21.2
4	4.	0.3	64	63.8	5.6	4	123.5	10.8	4	183.3	16.	4	243.1	21.3
5	5.	0.4	65	64.8	5.7	5	124.5	10.9	5	184.3	16.1	5	244.1	21.4
6	6.	0.5	66	65.7	5.8	6	125.5	11.	6	185.3	16.2	6	245.1	21.4
7	7.	0.6	67	66.7	5.8	7	126.5	11.1	7	186.3	16.3	7	246.1	21.5
8	8.	0.7	68	67.7	5.9	8	127.5	11.2	8	187.3	16.4	8	247.1	21.6
9	9.	0.8	69	68.7	6.	9	128.5	11.3	9	188.3	16.5	9	248.1	21.7
10	10.	0.9	70	69.7	6.1	130	129.5	11.3	190	189.3	16.6	250	249.	21.8
11	11.	1.	71	70.7	6.2	1	130.5	11.4	1	190.3	16.6	1	250.	21.9
12	12.	1.	72	71.7	6.3	2	131.5	11.5	2	191.3	16.7	2	251.	22.
13	13.	1.1	73	72.7	6.4	3	132.5	11.6	3	192.3	16.8	3	252.	22.1
14	13.9	1.2	74	73.7	6.4	4	133.5	11.7	4	193.3	16.9	4	253.	22.1
15	14.9	1.3	75	74.7	6.5	5	134.5	11.8	5	194.3	17.	5	254.	22.2
16	15.9	1.4	76	75.7	6.6	6	135.5	11.9	6	195.3	17.1	6	255.	22.3
17	16.9	1.5	77	76.7	6.7	7	136.5	11.9	7	196.3	17.2	7	256.	22.4
18	17.9	1.6	78	77.7	6.8	8	137.5	12.	8	197.3	17.3	8	257.	22.5
19	18.9	1.7	79	78.7	6.9	9	138.5	12.1	9	198.3	17.3	9	258.	22.6
20	19.9	1.7	80	79.7	7.	140	139.5	12.2	200	199.9	17.4	260	259.	22.7
21	20.9	1.8	81	80.7	7.1	1	140.5	12.3	1	200.9	17.5	1	260.	22.8
22	21.9	1.9	82	81.7	7.1	2	141.5	12.4	2	201.9	17.6	2	261.	22.8
23	22.9	2.	83	82.7	7.2	3	142.5	12.5	3	202.9	17.7	3	262.	22.9
24	23.9	2.1	84	83.7	7.3	4	143.5	12.6	4	203.9	17.8	4	263.	23.
25	24.9	2.2	85	84.7	7.4	5	144.5	12.6	5	204.9	17.9	5	264.	23.1
26	25.9	2.3	86	85.7	7.5	6	145.5	12.7	6	205.9	18.	6	265.	23.2
27	26.9	2.4	87	86.7	7.6	7	146.5	12.8	7	206.9	18.	7	266.	23.3
28	27.9	2.4	88	87.7	7.7	8	147.5	12.9	8	207.9	18.1	8	267.	23.4
29	28.9	2.5	89	88.7	7.8	9	148.5	13.	9	208.9	18.2	9	268.	23.4
30	29.9	2.6	90	89.7	7.8	150	149.5	13.1	210	209.9	18.3	270	269.	23.5
31	30.9	2.7	91	90.7	7.9	1	150.5	13.2	1	210.9	18.4	1	270.	23.6
32	31.9	2.8	92	91.6	8.	2	151.5	13.2	2	211.9	18.5	2	271.	23.7
33	32.9	2.9	93	92.6	8.1	3	152.5	13.3	3	212.9	18.6	3	272.	23.8
34	33.9	3.	94	93.6	8.2	4	153.5	13.4	4	213.9	18.7	4	273.	23.9
35	34.9	3.1	95	94.6	8.3	5	154.5	13.5	5	214.9	18.7	5	274.	24.
36	35.9	3.1	96	95.6	8.4	6	155.5	13.6	6	215.9	18.8	6	274.9	24.1
37	36.9	3.2	97	96.6	8.5	7	156.5	13.7	7	216.9	18.9	7	275.9	24.1
38	37.9	3.3	98	97.6	8.5	8	157.5	13.8	8	217.9	19.	8	276.9	24.2
39	38.9	3.4	99	98.6	8.6	9	158.5	13.9	9	218.9	19.1	9	277.9	24.3
40	39.8	3.5	100	99.6	8.7	160	159.5	13.9	220	219.9	19.2	280	278.9	24.4
41	40.8	3.6	1	100.6	8.8	1	160.4	14.	1	220.9	19.3	1	279.9	24.5
42	41.8	3.7	2	101.6	8.9	2	161.4	14.1	2	221.9	19.3	2	280.9	24.6
43	42.8	3.7	3	102.6	9.	3	162.4	14.2	3	222.9	19.4	3	281.9	24.7
44	43.8	3.8	4	103.6	9.1	4	163.4	14.3	4	223.1	19.5	4	282.9	24.8
45	44.8	3.9	5	104.6	9.2	5	164.4	14.4	5	224.1	19.6	5	283.9	24.9
46	45.8	4.	6	105.6	9.2	6	165.4	14.5	6	225.1	19.7	6	284.9	24.9
47	46.8	4.1	7	106.6	9.3	7	166.4	14.6	7	226.1	19.8	7	285.9	25.
48	47.8	4.2	8	107.6	9.4	8	167.4	14.6	8	227.1	19.9	8	286.9	25.1
49	48.8	4.3	9	108.6	9.5	9	168.4	14.7	9	228.1	20.	9	287.9	25.2
50	49.8	4.4	110	109.6	9.6	170	169.4	14.8	230	229.1	20.	290	288.9	25.3
51	50.8	4.4	1	110.6	9.7	1	170.3	14.9	1	230.1	20.1	1	289.9	25.4
52	51.8	4.5	2	111.6	9.8	2	171.3	15.	2	231.1	20.2	2	290.9	25.4
53	52.8	4.6	3	112.6	9.8	3	172.3	15.1	3	232.1	20.3	3	291.9	25.5
54	53.8	4.7	4	113.6	9.9	4	173.3	15.2	4	233.1	20.4	4	292.9	25.6
55	54.8	4.8	5	114.6	10.	5	174.3	15.3	5	234.1	20.5	5	293.9	25.7
56	55.8	4.9	6	115.6	10.1	6	175.3	15.3	6	235.1	20.6	6	294.9	25.8
57	56.8	5.	7	116.6	10.2	7	176.3	15.4	7	236.1	20.7	7	295.9	25.9
58	57.8	5.1	8	117.6	10.3	8	177.3	15.5	8	237.1	20.7	8	296.9	26.
59	58.8	5.1	9	118.5	10.4	9	178.3	15.6	9	238.1	20.8	9	297.9	26.1
60	59.8	5.2	190	119.5	10.5	180	179.3	15.7	240	239.1	20.9	300	298.9	26.1
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 65.

Course 60.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.7	6.4	121	120.3	12.6	181	180.	18.9	241	240.7	24.2
2	2.	0.2	62	61.7	6.5	2	121.3	12.8	2	181.	19.	3	240.7	24.3
3	3.	0.3	63	62.7	6.6	3	122.3	13.	3	182.	19.1	4	241.7	24.4
4	4.	0.4	64	63.6	6.7	4	123.3	13.1	4	183.	19.2	5	242.7	24.5
5	5.	0.5	65	64.6	6.8	5	124.3	13.2	5	184.	19.3	6	243.7	24.6
6	6.	0.6	66	65.6	6.9	6	125.3	13.3	6	185.	19.4	7	244.7	24.7
7	7.	0.7	67	66.6	7.	7	126.3	13.4	7	186.	19.5	8	245.6	24.8
8	8.	0.8	68	67.6	7.1	8	127.3	13.5	8	187.	19.7	9	246.6	24.9
9	9.	0.9	69	68.6	7.2	9	128.3	13.5	9	188.	19.8		247.6	25.
10	9.9	1.	70	69.6	7.3	130	129.3	13.6	190	189.	19.9	250	248.6	25.1
11	10.9	1.1	71	70.6	7.4	1	130.3	13.7	1	190.	20.	1	249.6	25.2
12	11.9	1.3	72	71.6	7.5	2	131.3	13.8	2	190.9	20.1	2	250.6	25.3
13	12.9	1.4	73	72.6	7.6	3	132.3	13.9	3	191.9	20.2	3	251.6	25.4
14	13.9	1.5	74	73.6	7.7	4	133.3	14.	4	192.9	20.3	4	252.6	25.5
15	14.9	1.6	75	74.6	7.8	5	134.3	14.1	5	193.9	20.4	5	253.6	25.6
16	15.9	1.7	76	75.6	7.9	6	135.3	14.2	6	194.9	20.5	6	254.6	25.7
17	16.9	1.8	77	76.6	8.	7	136.3	14.3	7	195.9	20.6	7	255.6	25.8
18	17.9	1.9	78	77.6	8.2	8	137.3	14.4	8	196.9	20.7	8	256.6	25.9
19	18.9	2.	79	78.6	8.3	9	138.3	14.5	9	197.9	20.8	9	257.6	26.
20	19.9	2.1	80	79.6	8.4	140	139.3	14.6	200	198.9	20.9	260	258.6	26.2
21	20.9	2.2	81	80.6	8.5	1	140.3	14.7	1	199.9	21.	1	259.6	26.3
22	21.9	2.3	82	81.6	8.6	2	141.3	14.8	2	200.9	21.1	2	260.6	26.4
23	22.9	2.4	83	82.5	8.7	3	142.3	14.9	3	201.9	21.2	3	261.6	26.5
24	23.9	2.5	84	83.5	8.8	4	143.3	15.1	4	202.9	21.3	4	262.6	26.6
25	24.9	2.6	85	84.5	8.9	5	144.3	15.2	5	203.9	21.4	5	263.6	26.7
26	25.9	2.7	86	85.5	9.	6	145.3	15.3	6	204.9	21.5	6	264.6	26.8
27	26.9	2.8	87	86.5	9.1	7	146.3	15.4	7	205.9	21.6	7	265.6	26.9
28	27.9	2.9	88	87.5	9.2	8	147.3	15.5	8	206.9	21.7	8	266.6	27.
29	28.6	3.	89	88.5	9.3	9	148.3	15.6	9	207.9	21.8	9	267.6	27.1
30	29.8	3.1	90	89.5	9.4	150	149.3	15.7	210	208.8	22.	270	268.5	27.2
31	30.8	3.2	91	90.5	9.5	1	150.3	15.8	1	209.8	22.1	1	269.5	27.3
32	31.8	3.3	92	91.5	9.6	2	151.2	15.9	2	210.8	22.2	2	270.5	27.4
33	32.8	3.4	93	92.5	9.7	3	152.2	16.	3	211.8	22.3	3	271.5	27.5
34	33.8	3.6	94	93.5	9.8	4	153.2	16.1	4	212.8	22.4	4	272.5	27.6
35	34.8	3.7	95	94.5	9.9	5	154.2	16.2	5	213.8	22.5	5	273.5	27.7
36	35.8	3.8	96	95.5	10.	6	155.1	16.3	6	214.8	22.6	6	274.5	27.8
37	36.8	3.9	97	96.5	10.1	7	156.1	16.4	7	215.8	22.7	7	275.5	27.9
38	37.8	4.	98	97.5	10.2	8	157.1	16.5	8	216.8	22.8	8	276.5	28.
39	38.8	4.1	99	98.5	10.3	9	158.1	16.6	9	217.8	22.9	9	277.5	28.1
40	39.8	4.3	100	99.5	10.5	160	159.1	16.7	220	218.8	23.	280	278.5	28.2
41	40.8	4.4	1	100.4	10.6	1	160.1	16.8	1	219.8	23.1	1	279.5	28.3
42	41.8	4.4	2	101.4	10.7	2	161.1	16.9	2	220.8	23.2	2	280.5	28.4
43	42.8	4.5	3	102.4	10.8	3	162.1	17.	3	221.8	23.3	3	281.5	28.5
44	43.8	4.6	4	103.4	10.9	4	163.1	17.1	4	222.8	23.4	4	282.4	28.6
45	44.8	4.7	5	104.4	11.	5	164.1	17.2	5	223.8	23.5	5	283.4	28.7
46	45.7	4.8	6	105.4	11.1	6	165.1	17.4	6	224.8	23.6	6	284.4	28.8
47	46.7	4.9	7	106.4	11.2	7	166.1	17.5	7	225.8	23.7	7	285.4	28.9
48	47.7	5.	8	107.4	11.3	8	167.1	17.6	8	226.8	23.8	8	286.4	29.
49	48.7	5.1	9	108.4	11.4	9	168.1	17.7	9	227.7	23.9	9	287.4	29.1
50	49.7	5.3	110	109.4	11.5	170	169.1	17.8	230	228.7	24.	290	288.4	29.2
51	50.7	5.3	1	110.4	11.6	1	170.1	17.9	1	229.7	24.1	1	289.4	29.3
52	51.7	5.4	2	111.4	11.7	2	171.1	18.	2	230.7	24.2	2	290.4	29.4
53	52.7	5.5	3	112.4	11.8	3	172.1	18.1	3	231.7	24.3	3	291.4	29.5
54	53.7	5.6	4	113.4	11.9	4	173.	18.2	4	232.7	24.4	4	292.4	29.6
55	54.7	5.7	5	114.4	12.	5	174.	18.3	5	233.7	24.5	5	293.4	29.7
56	55.7	5.9	6	115.4	12.1	6	175.	18.4	6	234.7	24.6	6	294.4	29.8
57	56.7	6.	7	116.4	12.2	7	176.	18.5	7	235.7	24.7	7	295.4	29.9
58	57.7	6.1	8	117.4	12.3	8	177.	18.6	8	236.7	24.8	8	296.4	30.
59	58.7	6.2	9	118.3	12.4	9	178.	18.7	9	237.7	25.	9	297.4	30.1
60	59.7	6.3	190	119.3	12.5	180	179.	18.8	240	238.7	25.1	300	298.4	31.4

Distance, Departure and Diff. Latitude.

Course 840.

Course 70.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.5	7.4	181	180.1	14.7	181	179.7	24.1	241	239.2	29.4
2	2.	0.2	62	61.5	7.6	2	181.1	14.9	2	180.6	23.3	3	240.2	29.5
3	3.	0.4	63	62.5	7.7	3	182.1	15.	3	181.6	22.4	3	241.2	29.6
4	4.	0.5	64	63.5	7.8	4	183.1	15.1	4	182.6	22.4	4	242.2	29.7
5	5.	0.6	65	64.5	7.9	5	184.1	15.2	5	183.6	22.5	5	243.2	29.9
6	6.	0.7	66	65.5	8.	6	185.1	15.4	6	184.6	22.7	6	244.2	30.
7	6.9	0.9	67	66.5	8.2	7	186.1	15.5	7	185.6	22.8	7	245.2	30.1
8	7.9	1.	68	67.5	8.3	8	187.	15.6	8	186.6	22.9	8	246.2	30.2
9	8.9	1.1	69	68.5	8.4	9	188.	15.7	9	187.6	23.	9	247.1	30.3
10	9.9	1.2	70	69.5	8.5	130	189.	15.8	190	188.6	23.2	250	248.1	30.5
11	10.9	1.3	71	70.5	8.7	1	130.	16.	1	189.6	23.3	1	249.1	30.6
12	11.9	1.5	72	71.5	8.8	2	131.	16.1	2	190.6	23.4	2	250.1	30.7
13	12.9	1.6	73	72.5	8.9	3	132.	16.2	3	191.6	23.5	3	251.1	30.8
14	13.9	1.7	74	73.4	9.	4	133.	16.3	4	192.6	23.6	4	252.1	31.
15	14.9	1.8	75	74.4	9.1	5	134.	16.5	5	193.5	23.8	5	253.1	31.1
16	15.9	1.9	76	75.4	9.3	6	135.	16.6	6	194.5	23.9	6	254.1	31.2
17	16.9	2.1	77	76.4	9.4	7	136.	16.7	7	195.5	24.	7	255.1	31.3
18	17.9	2.2	78	77.4	9.5	8	137.	16.8	8	196.5	24.1	8	256.1	31.4
19	18.9	2.3	79	78.4	9.6	9	138.	16.9	9	197.5	24.3	9	257.1	31.6
20	19.9	2.4	80	79.4	9.7	140	139.	17.1	200	198.5	24.4	260	258.1	31.7
21	20.9	2.6	81	80.4	9.9	1	139.9	17.2	1	199.5	24.5	1	259.1	31.8
22	21.8	2.7	82	81.4	10.	2	140.9	17.3	2	200.5	24.6	2	260.	31.9
23	22.8	2.8	83	82.4	10.1	3	141.9	17.4	3	201.5	24.7	3	261.	32.1
24	23.8	2.9	84	83.4	10.2	4	142.9	17.5	4	202.5	24.9	4	262.	32.2
25	24.8	3.	85	84.4	10.4	5	143.9	17.7	5	203.5	25.	5	263.	32.3
26	25.8	3.2	86	85.4	10.5	6	144.9	17.8	6	204.5	25.1	6	264.	32.4
27	26.8	3.3	87	86.4	10.6	7	145.9	17.9	7	205.5	25.2	7	265.	32.5
28	27.8	3.4	88	87.3	10.7	8	146.9	18.	8	206.4	25.3	8	266.	32.7
29	28.8	3.5	89	88.3	10.8	9	147.9	18.2	9	207.4	25.5	9	267.	32.8
30	29.8	3.7	90	89.3	11.	150	148.9	18.3	210	208.4	25.6	270	268.	32.9
31	30.8	3.8	91	90.3	11.1	1	148.9	18.4	1	209.4	25.7	1	269.	33.
32	31.8	3.9	92	91.3	11.2	2	150.9	18.5	2	210.4	25.8	2	270.	33.1
33	32.8	4.	93	92.3	11.3	3	151.9	18.6	3	211.4	26.	3	271.	33.2
34	33.8	4.1	94	93.3	11.5	4	152.9	18.8	4	212.4	26.1	4	272.	33.3
35	34.7	4.3	95	94.3	11.6	5	153.8	18.9	5	213.4	26.2	5	273.	33.5
36	35.7	4.4	96	95.3	11.7	6	154.8	19.	6	214.4	26.3	6	273.9	33.6
37	36.7	4.5	97	96.3	11.8	7	155.8	19.1	7	215.4	26.4	7	274.9	33.8
38	37.7	4.6	98	97.3	11.9	8	156.8	19.3	8	216.4	26.6	8	275.9	33.9
39	38.7	4.8	99	98.3	12.1	9	157.8	19.4	9	217.4	26.7	9	276.9	34.
40	39.7	4.9	100	99.3	12.2	160	158.8	19.5	220	218.4	26.8	280	277.9	34.1
41	40.7	5.	1	100.2	12.3	1	159.8	19.6	1	219.4	26.9	1	278.9	34.2
42	41.7	5.1	2	101.9	12.4	2	160.8	19.7	2	220.3	27.1	2	279.9	34.3
43	42.7	5.2	3	102.9	12.6	3	161.8	19.9	3	221.3	27.2	3	280.9	34.5
44	43.7	5.4	4	103.2	12.7	4	162.8	20.	4	222.3	27.3	4	281.9	34.6
45	44.7	5.5	5	104.2	12.8	5	163.8	20.1	5	223.3	27.4	5	282.9	34.7
46	45.7	5.6	6	105.2	12.9	6	164.8	20.2	6	224.3	27.5	6	283.9	34.9
47	46.7	5.7	7	106.2	13.	7	165.8	20.4	7	225.3	27.7	7	284.9	35.
48	47.6	5.8	8	107.2	13.2	8	166.7	20.5	8	226.3	27.8	8	285.9	35.1
49	48.6	6.	9	108.2	13.3	9	167.7	20.6	9	227.3	27.9	9	286.8	35.3
50	49.6	6.1	116	109.2	13.4	170	168.7	20.7	230	228.3	28.	290	287.8	35.3
51	50.6	6.2	1	110.2	13.5	1	169.7	20.8	1	229.3	28.2	1	288.8	35.5
52	51.6	6.3	2	111.2	13.6	2	170.7	21.	2	230.3	28.3	2	289.8	35.6
53	52.6	6.5	3	112.2	13.8	3	171.7	21.1	3	231.3	28.4	3	290.8	35.7
54	53.6	6.6	4	113.2	13.9	4	172.7	21.2	4	232.3	28.5	4	291.8	35.8
55	54.6	6.7	5	114.1	14.	5	173.7	21.3	5	233.2	28.6	5	292.8	36.
56	55.6	6.8	6	115.1	14.1	6	174.7	21.4	6	234.2	28.8	6	293.8	36.1
57	56.6	6.9	7	116.1	14.3	7	175.7	21.6	7	235.2	28.9	7	294.8	36.2
58	57.6	7.1	8	117.1	14.4	8	176.7	21.7	8	236.2	29.	8	295.8	36.3
59	58.6	7.2	9	118.1	14.5	9	177.7	21.8	9	237.2	29.1	9	296.8	36.4
60	59.6	7.3	120	119.1	14.6	180	178.7	21.9	240	238.2	29.2	300	297.8	36.6

Distance, Departure and Diff. Latitude.

Course 80.

Course 80°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.1	61	60.4	8.5	121	119.8	16.8	181	179.2	25.2	241	237.7	33.5
2	2.	0.3	62	61.4	8.6	2	120.8	17.	2	180.2	25.3	2	236.7	33.7
3	3.	0.4	63	62.4	8.8	3	121.8	17.1	3	181.2	25.5	3	240.6	33.8
4	4.	0.6	64	63.4	8.9	4	122.8	17.3	4	182.2	25.6	4	241.6	34.
5	5.	0.7	65	64.4	9.	5	123.8	17.4	5	183.2	25.7	5	242.6	34.1
6	5.9	0.8	66	65.4	9.2	6	124.8	17.5	6	184.2	25.9	6	243.6	34.2
7	6.9	1.	67	66.3	9.3	7	125.8	17.7	7	185.2	26.	7	244.6	34.4
8	7.9	1.1	68	67.3	9.5	8	126.8	17.8	8	186.2	26.2	8	245.6	34.5
9	8.9	1.3	69	68.3	9.6	9	127.7	18.	9	187.2	26.3	9	246.6	34.7
10	9.9	1.4	70	69.3	9.7	130	128.7	18.1	100	188.2	26.4	250	247.6	34.8
11	10.9	1.5	71	70.3	9.9	1	129.7	18.2	1	189.1	26.6	1	248.6	34.9
12	11.9	1.7	72	71.3	10.	2	130.7	18.4	2	190.1	26.7	2	249.5	35.1
13	12.9	1.8	73	72.3	10.3	3	131.7	18.5	3	191.1	26.9	3	250.5	35.2
14	13.9	1.9	74	73.3	10.3	4	132.7	18.6	4	192.1	27.	4	251.5	35.3
15	14.9	2.1	75	74.3	10.4	5	133.7	18.8	5	193.1	27.1	5	252.5	35.5
16	15.8	2.2	76	75.3	10.6	6	134.7	18.9	6	194.1	27.3	6	253.5	35.6
17	16.8	2.4	77	76.3	10.7	7	135.7	19.1	7	195.1	27.4	7	254.5	35.8
18	17.8	2.5	78	77.2	10.9	8	136.7	19.2	8	196.1	27.6	8	255.5	35.9
19	18.8	2.6	79	78.2	11.	9	137.7	19.3	9	197.1	27.7	9	256.5	36.
20	19.8	2.8	80	79.2	11.1	140	138.6	19.5	200	198.1	27.8	300	257.5	36.2
21	20.8	2.9	81	80.2	11.3	1	139.6	19.6	1	199.	28.	1	258.5	36.3
22	21.8	3.1	82	81.2	11.4	2	140.6	19.8	2	200.	28.1	2	259.5	36.5
23	22.8	3.2	83	82.2	11.6	3	141.6	19.9	3	201.	28.3	3	260.4	36.6
24	23.8	3.3	84	83.2	11.7	4	142.6	20.	4	202.	28.4	4	261.4	36.7
25	24.7	3.5	85	84.2	11.8	5	143.6	20.2	5	203.	28.5	5	262.4	36.9
26	25.7	3.6	86	85.2	12.	6	144.6	20.3	6	204.	28.7	6	263.4	37.
27	26.7	3.8	87	86.2	12.1	7	145.6	20.5	7	205.	28.8	7	264.4	37.2
28	27.7	3.9	88	87.1	12.2	8	146.6	20.6	8	206.	28.9	8	265.4	37.3
29	28.7	4.	89	88.1	12.4	9	147.5	20.7	9	207.	29.1	9	266.4	37.4
30	29.7	4.3	90	89.1	12.5	150	148.5	20.9	210	208.	29.2	310	267.4	37.6
31	30.7	4.3	91	90.1	12.7	1	149.5	21.	1	208.9	29.4	1	268.4	37.7
32	31.7	4.5	92	91.1	12.8	2	150.5	21.2	2	209.9	29.5	2	269.4	37.9
33	32.7	4.6	93	92.1	12.9	3	151.5	21.3	3	210.9	29.6	3	270.3	38.
34	33.7	4.7	94	93.1	13.1	4	152.5	21.4	4	211.9	29.8	4	271.3	38.1
35	34.6	4.9	95	94.1	13.2	5	153.5	21.6	5	212.9	29.9	5	272.3	38.3
36	35.6	5.	96	95.1	13.4	6	154.5	21.7	6	213.9	30.1	6	273.3	38.4
37	36.6	5.1	97	96.1	13.5	7	155.5	21.9	7	214.9	30.3	7	274.3	38.6
38	37.6	5.3	98	97.	13.6	8	156.5	22.	8	215.9	30.3	8	275.3	38.7
39	38.6	5.4	99	98.	13.8	9	157.5	22.1	9	216.8	30.5	9	276.3	38.8
40	39.6	5.6	100	99.	13.9	160	158.4	22.2	220	217.9	30.6	320	277.3	39.
41	40.6	5.7	1	100.	14.1	1	159.4	22.4	1	218.8	30.8	1	278.3	39.1
42	41.6	5.8	2	101.	14.2	2	160.4	22.5	2	219.8	30.9	2	279.3	39.2
43	42.6	6.	3	102.	14.3	3	161.4	22.7	3	220.8	31.	3	280.3	39.4
44	43.6	6.1	4	103.	14.5	4	162.4	22.8	4	221.8	31.2	4	281.3	39.5
45	44.6	6.3	5	104.	14.6	5	163.4	23.	5	222.8	31.3	5	282.3	39.6
46	45.5	6.4	6	105.	14.8	6	164.4	23.1	6	223.8	31.5	6	283.2	39.8
47	46.5	6.5	7	106.	14.9	7	165.4	23.2	7	224.8	31.6	7	284.2	39.9
48	47.5	6.7	8	106.9	15.	8	166.4	23.4	8	225.8	31.7	8	285.2	40.1
49	48.5	6.8	9	107.9	15.2	9	167.4	23.5	9	226.8	31.9	9	286.2	40.2
50	49.5	7.	110	108.9	15.3	170	168.3	23.7	230	227.8	32.	330	287.2	40.4
51	50.5	7.1	1	109.9	15.4	1	169.3	23.8	1	228.8	32.1	1	288.2	40.5
52	51.5	7.2	2	110.9	15.6	2	170.3	23.9	2	229.7	32.3	2	289.2	40.6
53	52.5	7.4	3	111.9	15.7	3	171.3	24.1	3	230.7	32.4	3	290.1	40.8
54	53.5	7.5	4	112.9	15.9	4	172.3	24.2	4	231.7	32.6	4	291.1	40.9
55	54.5	7.7	5	113.9	16.	5	173.3	24.4	5	232.7	32.7	5	292.1	41.1
56	55.5	7.8	6	114.9	16.1	6	174.3	24.5	6	233.7	32.8	6	293.1	41.2
57	56.4	7.9	7	115.9	16.3	7	175.3	24.6	7	234.7	33.	7	294.1	41.3
58	57.4	8.1	8	116.9	16.4	8	176.3	24.8	8	235.7	33.1	8	295.1	41.5
59	58.4	8.2	9	117.8	16.6	9	177.3	24.9	9	236.7	33.3	9	296.1	41.6
60	59.4	8.4	190	118.8	16.7	180	178.9	25.1	240	237.7	33.4	300	297.1	41.8

Distance, Departure and Diff. Latitude.

Course 80°.

Course 90.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.2	61	60.2	9.5	129	119.5	18.9	181	178.8	28.3	241	238.	37.7
2	2.	0.3	62	61.9	9.7	2	120.5	19.1	2	179.8	28.5	2	239.	37.9
3	3.	0.5	63	63.9	9.9	3	121.5	19.2	3	180.7	28.6	3	240.	38.
4	4.	0.6	64	63.9	10.	4	122.5	19.4	4	181.7	28.8	4	241.	38.2
5	4.9	0.8	65	64.2	10.2	5	123.5	19.6	5	182.7	28.9	5	242.	38.3
6	5.9	0.9	66	65.2	10.3	6	124.4	19.7	6	183.7	29.1	6	243.	38.5
7	6.9	1.1	67	66.3	10.5	7	125.4	19.9	7	184.7	29.3	7	244.	38.6
8	7.9	1.3	68	67.3	10.6	8	126.4	20.	8	185.7	29.4	8	244.9	38.8
9	8.9	1.4	69	68.3	10.8	9	127.4	20.2	9	186.7	29.6	9	245.9	39.
10	9.9	1.6	70	69.1	11.	130	128.4	20.3	190	187.7	29.7	250	246.9	39.1
11	10.9	1.7	71	70.1	11.1	1	129.4	20.5	1	188.6	29.9	1	247.9	39.3
12	11.9	1.9	72	71.1	11.3	2	130.4	20.6	2	189.6	30.	2	248.9	39.4
13	12.8	2.	73	72.1	11.4	3	131.4	20.8	3	190.6	30.2	3	249.9	39.6
14	13.8	2.2	74	73.1	11.6	4	132.4	21.	4	191.6	30.3	4	250.9	39.7
15	14.8	2.3	75	74.1	11.7	5	133.3	21.1	5	192.6	30.5	5	251.9	39.9
16	15.8	2.5	76	75.1	11.9	6	134.3	21.3	6	193.6	30.7	6	252.8	40.
17	16.8	2.7	77	76.1	12.	7	135.3	21.4	7	194.6	30.8	7	253.8	40.2
18	17.8	2.8	78	77.	12.2	8	136.3	21.6	8	195.6	31.	8	254.8	40.4
19	18.8	3.	79	78.	12.4	9	137.3	21.7	9	196.5	31.1	9	255.8	40.5
20	19.7	3.1	80	79.	12.5	140	138.3	21.9	200	197.5	31.3	260	256.8	40.7
21	20.7	3.3	81	80.	12.7	1	139.3	22.1	1	198.5	31.4	1	257.8	40.8
22	21.7	3.4	82	81.	12.8	2	140.3	22.2	2	199.5	31.6	2	258.8	41.
23	22.7	3.6	83	82.	13.	3	141.3	22.4	3	200.5	31.8	3	259.8	41.1
24	23.7	3.8	84	83.	13.1	4	142.2	22.5	4	201.5	31.9	4	260.7	41.3
25	24.7	3.9	85	84.	13.3	5	143.2	22.7	5	202.5	32.1	5	261.7	41.5
26	25.7	4.1	86	84.9	13.5	6	144.2	22.8	6	203.5	32.2	6	262.7	41.6
27	26.7	4.2	87	85.9	13.6	7	145.2	23.	7	204.5	32.4	7	263.7	41.8
28	27.6	4.4	88	86.9	13.8	8	146.2	23.2	8	205.4	32.5	8	264.7	41.9
29	28.6	4.5	89	87.9	13.9	9	147.2	23.3	9	206.4	32.7	9	265.7	42.1
30	29.6	4.7	90	88.9	14.1	150	148.2	23.5	210	207.4	32.9	270	266.7	42.2
31	30.6	4.8	91	89.9	14.2	1	149.1	23.6	1	208.4	33.	1	267.7	42.4
32	31.6	5.	92	90.9	14.4	2	150.1	23.8	2	209.4	33.2	2	268.7	42.6
33	32.6	5.2	93	91.9	14.5	3	151.1	23.9	3	210.4	33.3	3	269.6	42.7
34	33.6	5.3	94	92.8	14.7	4	152.1	24.1	4	211.4	33.5	4	270.6	42.8
35	34.6	5.5	95	93.8	14.9	5	153.1	24.2	5	212.4	33.6	5	271.6	43.
36	35.5	5.6	96	94.8	15.	6	154.1	24.4	6	213.3	33.8	6	272.6	43.2
37	36.5	5.8	97	95.8	15.2	7	155.1	24.6	7	214.3	33.9	7	273.6	43.3
38	37.5	5.9	98	96.8	15.3	8	156.1	24.7	8	215.3	34.1	8	274.6	43.5
39	38.5	6.1	99	97.8	15.5	9	157.	24.9	9	216.3	34.3	9	275.6	43.6
40	39.5	6.3	100	98.8	15.6	160	158.	25.	220	217.3	34.4	280	276.6	43.8
41	40.5	6.4	1	99.8	15.8	1	159.	25.2	1	218.3	34.6	1	277.5	44.
42	41.5	6.6	2	100.7	16.	2	160.	25.3	2	219.3	34.7	2	278.5	44.1
43	42.5	6.7	3	101.7	16.1	3	161.	25.5	3	220.3	34.9	3	279.5	44.3
44	43.5	6.9	4	102.7	16.3	4	162.	25.7	4	221.2	35.	4	280.5	44.4
45	44.4	7.	5	103.7	16.4	5	163.	25.8	5	222.2	35.2	5	281.5	44.6
46	45.4	7.2	6	104.7	16.6	6	164.	26.	6	223.2	35.4	6	282.5	44.7
47	46.4	7.4	7	105.7	16.7	7	164.9	26.1	7	224.2	35.5	7	283.5	44.9
48	47.4	7.5	8	106.7	16.9	8	165.9	26.3	8	225.2	35.7	8	284.5	45.1
49	48.4	7.7	9	107.7	17.1	9	166.9	26.4	9	226.2	35.8	9	285.4	45.2
50	49.4	7.8	110	108.6	17.2	170	167.9	26.6	230	227.2	36.	290	286.4	45.4
51	50.4	8.	1	109.6	17.4	1	168.9	26.8	1	228.2	36.1	1	287.4	45.5
52	51.4	8.1	2	110.6	17.5	2	169.9	26.9	2	229.1	36.3	2	288.4	45.7
53	52.3	8.3	3	111.6	17.7	3	170.9	27.1	3	230.1	36.4	3	289.4	45.8
54	53.3	8.4	4	112.6	17.8	4	171.9	27.2	4	231.1	36.6	4	290.4	46.
55	54.3	8.6	5	113.6	18.	5	172.8	27.4	5	232.1	36.8	5	291.4	46.1
56	55.3	8.8	6	114.6	18.1	6	173.8	27.5	6	233.1	36.9	6	292.4	46.3
57	56.3	8.9	7	115.6	18.3	7	174.8	27.7	7	234.1	37.1	7	293.3	46.5
58	57.3	9.1	8	116.5	18.5	8	175.8	27.8	8	235.1	37.2	8	294.3	46.6
59	58.3	9.2	9	117.5	18.6	9	176.8	28.	9	236.1	37.4	9	295.3	46.8
60	59.3	9.4	120	118.5	18.8	180	177.8	28.2	240	237.	37.5	300	296.3	46.9

Distance Departure and Diff. Latitude.

Course 810.

Course 100°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.2	61	60.1	10.6	121	119.2	21.	181	178.3	31.4	241	237.3	41.8
2	2.	0.3	62	61.1	10.8	2	120.1	21.2	2	179.2	31.6	2	238.3	42.
3	3.	0.5	63	62.	10.9	3	121.1	21.4	3	180.9	31.8	3	239.3	42.9
4	3.9	0.7	64	63.	11.1	4	122.1	21.5	4	181.2	32.	4	240.3	42.4
5	4.9	0.9	65	64.	11.3	5	123.1	21.7	5	182.2	32.1	5	241.3	42.5
6	5.9	1.	66	65.	11.5	6	124.1	21.9	6	183.2	32.3	6	242.3	42.7
7	6.9	1.2	67	66.	11.6	7	125.1	22.1	7	184.2	32.5	7	243.2	42.9
8	7.9	1.4	68	67.	11.8	8	126.1	22.2	8	185.1	32.6	8	244.2	43.1
9	8.9	1.6	69	68.	12.	9	127.	22.4	9	186.1	32.8	9	245.2	43.3
10	9.8	1.7	70	68.9	12.2	130	128.	22.6	190	187.1	33.	250	246.2	43.4
11	10.8	1.9	71	69.9	12.3	1	129.	22.7	1	188.1	33.2	1	247.2	43.6
12	11.8	2.1	72	70.9	12.5	2	130.	22.9	2	189.1	33.3	2	248.2	43.8
13	12.8	2.3	73	71.9	12.7	3	131.	23.1	3	190.1	33.5	3	249.2	43.9
14	13.8	2.4	74	72.9	12.8	4	132.	23.3	4	191.1	33.7	4	250.1	44.1
15	14.8	2.6	75	73.9	13.	5	132.9	23.4	5	192.	33.9	5	251.1	44.3
16	15.7	2.8	76	74.8	13.9	6	133.9	23.6	6	193.	34.	6	252.1	44.5
17	16.7	3.	77	75.8	13.4	7	134.9	23.8	7	194.	34.9	7	253.1	44.6
18	17.7	3.1	78	76.8	13.5	8	135.9	24.	8	195.	34.4	8	254.1	44.8
19	18.7	3.3	79	77.8	13.7	9	136.9	24.1	9	196.	34.6	9	255.1	45.
20	19.7	3.5	80	78.8	13.9	140	137.9	24.3	200	197.	34.7	260	256.1	45.1
21	20.7	3.6	81	79.8	14.1	1	138.9	24.5	1	197.9	34.9	1	257.	45.3
22	21.7	3.8	82	80.8	14.2	2	139.8	24.7	2	198.9	35.1	2	258.	45.5
23	22.6	4.	83	81.7	14.4	3	140.8	24.8	3	199.9	35.3	3	259.	45.7
24	23.6	4.2	84	82.7	14.6	4	141.8	25.	4	200.9	35.4	4	260.	45.8
25	24.6	4.3	85	83.7	14.8	5	142.8	25.2	5	201.9	35.6	5	261.	46.
26	25.6	4.5	86	84.7	14.9	6	143.8	25.4	6	202.9	35.8	6	262.	46.2
27	26.6	4.7	87	85.7	15.1	7	144.8	25.5	7	203.9	35.9	7	262.9	46.4
28	27.6	4.9	88	86.7	15.3	8	145.8	25.7	8	204.8	36.1	8	263.9	46.5
29	28.5	5.	89	87.6	15.5	9	146.7	25.9	9	205.8	36.3	9	264.9	46.7
30	29.5	5.2	90	88.6	15.6	150	147.7	26.	210	206.8	36.5	270	265.9	46.9
31	30.5	5.4	91	89.6	15.8	1	148.7	26.2	1	207.8	36.6	1	266.9	47.1
32	31.5	5.6	92	90.6	16.	2	149.7	26.4	2	208.8	36.8	2	267.9	47.2
33	32.5	5.7	93	91.6	16.1	3	150.7	26.6	3	209.8	37.	3	268.9	47.4
34	33.5	5.9	94	92.6	16.3	4	151.7	26.7	4	210.7	37.2	4	269.8	47.6
35	34.5	6.1	95	93.6	16.5	5	152.6	26.9	5	211.7	37.3	5	270.8	47.8
36	35.4	6.3	96	94.5	16.7	6	153.6	27.1	6	212.7	37.5	6	271.8	47.9
37	36.4	6.4	97	95.5	16.8	7	154.6	27.3	7	213.7	37.7	7	272.8	48.1
38	37.4	6.6	98	96.5	17.	8	155.6	27.4	8	214.7	37.9	8	273.8	48.3
39	38.4	6.8	99	97.5	17.2	9	156.6	27.6	9	215.7	38.	9	274.8	48.4
40	39.4	6.9	100	98.5	17.4	160	157.6	27.8	220	216.7	38.2	280	275.7	48.6
41	40.4	7.1	1	99.5	17.5	1	158.6	28.	1	217.6	38.4	1	276.7	48.8
42	41.4	7.3	2	100.5	17.7	2	159.5	28.1	2	218.6	38.5	2	277.7	49.
43	42.3	7.5	3	101.4	17.9	3	160.5	28.3	3	219.6	38.7	3	278.7	49.1
44	43.3	7.6	4	102.4	18.1	4	161.5	28.5	4	220.6	38.9	4	279.7	49.3
45	44.3	7.8	5	103.4	18.2	5	162.5	28.7	5	221.6	39.1	5	280.7	49.5
46	45.3	8.	6	104.4	18.4	6	163.5	28.8	6	222.6	39.2	6	281.7	49.7
47	46.3	8.2	7	105.4	18.6	7	164.5	29.	7	223.6	39.4	7	282.6	49.8
48	47.3	8.3	8	106.4	18.8	8	165.4	29.2	8	224.5	39.6	8	283.6	50.
49	48.3	8.5	9	107.3	18.9	9	166.4	29.3	9	225.5	39.8	9	284.6	50.2
50	49.2	8.7	110	108.3	19.1	170	167.4	29.5	230	226.5	39.9	290	285.6	50.4
51	50.2	8.9	1	109.3	19.3	1	168.4	29.7	1	227.5	40.1	1	286.6	50.5
52	51.2	9.	2	110.3	19.4	2	169.4	29.9	2	228.5	40.3	2	287.6	50.7
53	52.2	9.2	3	111.3	19.6	3	170.4	30.	3	229.5	40.5	3	288.5	50.9
54	53.2	9.4	4	112.3	19.8	4	171.4	30.2	4	230.4	40.6	4	289.5	51.1
55	54.2	9.6	5	113.3	20.	5	172.3	30.4	5	231.4	40.8	5	290.5	51.2
56	55.1	9.7	6	114.2	20.1	6	173.3	30.6	6	232.4	41.	6	291.5	51.4
57	56.1	9.9	7	115.2	20.3	7	174.3	30.7	7	233.4	41.2	7	292.5	51.6
58	57.1	10.1	8	116.2	20.5	8	175.3	30.9	8	234.4	41.3	8	293.5	51.7
59	58.1	10.2	9	117.2	20.7	9	176.3	31.1	9	235.4	41.5	9	294.5	51.9
60	59.1	10.4	120	118.2	20.8	180	177.3	31.3	240	236.4	41.7	300	295.4	52.1
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 80°.

Course 110.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.2	61	59.9	11.6	121	118.6	23.1	181	177.7	34.5	241	236.6	46.9
2	2.	0.4	62	60.9	11.8	2	119.6	23.3	2	178.7	34.7	3	237.6	46.9
3	2.9	0.6	63	61.8	12.	3	120.7	23.5	3	179.6	34.9	4	238.5	46.4
4	3.9	0.8	64	62.8	12.2	4	121.7	23.7	4	180.6	35.1	4	239.5	46.6
5	4.9	1.	65	63.8	12.4	5	122.7	23.9	5	181.6	35.3	5	240.5	46.7
6	5.9	1.1	66	64.8	12.6	6	123.7	24.	6	182.6	35.5	6	241.5	46.9
7	6.9	1.3	67	65.8	12.8	7	124.7	24.2	7	183.6	35.7	7	242.5	47.1
8	7.9	1.5	68	66.8	13.	8	125.6	24.4	8	184.5	35.9	8	243.4	47.3
9	8.8	1.7	69	67.7	13.2	9	126.6	24.6	9	185.5	36.1	9	244.4	47.5
10	9.8	1.9	70	68.7	13.4	130	127.6	24.8	100	186.5	36.3	250	245.4	47.7
11	10.8	2.1	71	69.7	13.5	1	128.6	25.	1	187.5	36.4	1	246.4	47.9
12	11.8	2.3	72	70.7	13.7	2	129.6	25.2	2	188.5	36.6	2	247.4	48.1
13	12.8	2.5	73	71.7	13.9	3	130.6	25.4	3	189.5	36.8	3	248.4	48.3
14	13.7	2.7	74	72.6	14.1	4	131.5	25.6	4	190.4	37.	4	249.3	48.5
15	14.7	2.9	75	73.6	14.3	5	132.5	25.8	5	191.4	37.2	5	250.3	48.7
16	15.7	3.1	76	74.6	14.5	6	133.5	26.	6	192.4	37.4	6	251.3	48.8
17	16.7	3.3	77	75.6	14.7	7	134.5	26.1	7	193.4	37.6	7	252.3	49.
18	17.7	3.4	78	76.6	14.9	8	135.5	26.3	8	194.4	37.8	8	253.3	49.3
19	18.7	3.6	79	77.5	15.1	9	136.4	26.5	9	195.3	38.	9	254.3	49.4
20	19.6	3.8	80	78.5	15.3	140	137.4	26.7	200	196.3	38.2	260	255.3	49.6
21	20.6	4.	81	79.5	15.5	1	138.4	26.9	1	197.3	38.4	1	256.3	49.8
22	21.6	4.2	82	80.5	15.6	2	139.4	27.1	2	198.3	38.6	2	257.3	50.
23	22.6	4.4	83	81.5	15.8	3	140.4	27.3	3	199.3	38.7	3	258.3	50.2
24	23.6	4.6	84	82.5	16.	4	141.4	27.5	4	200.3	38.9	4	259.1	50.4
25	24.5	4.8	85	83.4	16.2	5	142.3	27.7	5	201.2	39.1	5	260.1	50.6
26	25.5	5.	86	84.4	16.4	6	143.3	27.9	6	202.2	39.3	6	261.1	50.8
27	26.5	5.2	87	85.4	16.6	7	144.3	28.	7	203.2	39.5	7	262.1	50.9
28	27.5	5.3	88	86.4	16.8	8	145.3	28.2	8	204.2	39.7	8	263.1	51.1
29	28.5	5.5	89	87.4	17.	9	146.3	28.4	9	205.2	39.9	9	264.1	51.3
30	29.4	5.7	90	88.3	17.2	150	147.2	28.6	210	206.1	40.1	270	265.	51.5
31	30.4	5.9	91	89.3	17.4	1	148.2	28.8	1	207.1	40.3	1	266.	51.7
32	31.4	6.1	92	90.3	17.6	2	149.2	29.	2	208.1	40.5	2	267.	51.9
33	32.4	6.3	93	91.3	17.7	3	150.2	29.2	3	209.1	40.6	3	268.	52.1
34	33.4	6.5	94	92.3	17.9	4	151.2	29.4	4	210.1	40.8	4	269.	52.3
35	34.4	6.7	95	93.3	18.1	5	152.2	29.6	5	211.	41.	5	270.9	52.5
36	35.3	6.9	96	94.2	18.3	6	153.1	29.8	6	212.	41.2	6	271.9	52.7
37	36.3	7.1	97	95.2	18.5	7	154.1	30.	7	213.	41.4	7	272.9	52.9
38	37.3	7.3	98	96.2	18.7	8	155.1	30.1	8	214.	41.6	8	273.9	53.
39	38.3	7.4	99	97.2	18.9	9	156.1	30.3	9	215.	41.8	9	273.9	53.2
40	39.3	7.6	100	98.2	19.1	160	157.1	30.5	220	216.	42.	280	274.9	53.4
41	40.2	7.8	1	99.1	19.3	1	158.	30.7	1	216.9	42.2	1	275.8	53.6
42	41.2	8.	2	100.1	19.5	2	159.	30.9	2	217.9	42.4	2	276.8	53.8
43	42.2	8.2	3	101.1	19.7	3	160.	31.1	3	218.9	42.6	3	277.8	54.
44	43.2	8.4	4	102.1	19.8	4	161.	31.3	4	219.9	42.7	4	278.8	54.2
45	44.2	8.6	5	103.1	20.	5	162.	31.5	5	220.9	42.9	5	279.8	54.4
46	45.2	8.8	6	104.1	20.2	6	163.	31.7	6	221.8	43.1	6	280.7	54.6
47	46.1	9.	7	105.	20.4	7	163.9	31.9	7	222.8	43.3	7	281.7	54.8
48	47.1	9.2	8	106.	20.6	8	164.9	32.1	8	223.8	43.5	8	282.7	55.
49	48.1	9.3	9	107.	20.8	9	165.9	32.3	9	224.8	43.7	9	283.7	55.1
50	49.1	9.5	110	108.	21.	170	166.9	32.4	230	225.8	43.9	290	284.7	55.3
51	50.1	9.7	1	109.	21.2	1	167.9	32.6	1	226.8	44.1	1	285.7	55.5
52	51.	9.9	2	109.9	21.4	2	168.8	32.8	2	227.7	44.3	2	286.6	55.7
53	52.	10.1	3	110.9	21.6	3	169.8	33.	3	228.7	44.5	3	287.6	55.9
54	53.	10.3	4	111.9	21.8	4	170.8	33.2	4	229.7	44.6	4	288.6	56.1
55	54.	10.5	5	112.9	21.9	5	171.8	33.4	5	230.7	44.8	5	289.6	56.3
56	55.	10.7	6	113.9	22.1	6	172.8	33.6	6	231.7	45.	6	290.6	56.5
57	56.	10.9	7	114.9	22.3	7	173.7	33.8	7	232.6	45.2	7	291.5	56.7
58	56.9	11.1	8	115.8	22.5	8	174.7	34.	8	233.6	45.4	8	292.5	56.9
59	57.9	11.3	9	116.8	22.7	9	175.7	34.2	9	234.6	45.6	9	293.5	57.1
60	58.9	11.4	190	117.8	22.9	180	176.7	34.3	240	235.6	45.8	300	294.5	57.2
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 70°.

Course 120.

Distance, DiE Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.9	61	59.7	12.7	181	118.4	25.2	181	177.	37.6	241	235.7	50.1
2	2.	0.4	62	60.6	12.9	2	119.3	25.4	2	178.	37.8	2	236.7	50.3
3	2.9	0.6	63	61.6	13.1	3	120.3	25.6	3	179.	38.	3	237.7	50.5
4	3.9	0.8	64	62.6	13.3	4	121.3	25.8	4	180.	38.2	4	238.7	50.7
5	4.9	1.	65	63.6	13.5	5	122.3	26.	5	181.	38.5	5	239.6	50.9
6	5.9	1.2	66	64.6	13.7	6	123.3	26.2	6	181.9	38.7	6	240.6	51.1
7	6.8	1.5	67	65.5	13.9	7	124.3	26.4	7	182.9	38.9	7	241.6	51.4
8	7.8	1.7	68	66.5	14.1	8	125.3	26.6	8	183.9	39.1	8	242.6	51.6
9	8.8	1.9	69	67.5	14.3	9	126.2	26.8	9	184.9	39.3	9	243.6	51.8
10	9.8	2.1	70	68.5	14.6	130	127.9	27.	190	185.8	39.5	250	244.5	52.
11	10.8	2.3	71	69.4	14.8	1	128.1	27.2	1	186.8	39.7	1	245.5	52.2
12	11.7	2.5	72	70.4	15.	2	129.1	27.4	2	187.8	39.9	2	246.5	52.4
13	12.7	2.7	73	71.4	15.3	3	130.1	27.7	3	188.8	40.1	3	247.5	52.6
14	13.7	2.9	74	72.4	15.4	4	131.1	27.9	4	189.8	40.3	4	248.4	52.8
15	14.7	3.1	75	73.4	15.6	5	132.	28.1	5	190.7	40.5	5	249.4	53.
16	15.6	3.3	76	74.3	15.8	6	133.	28.3	6	191.7	40.8	6	250.4	53.2
17	16.6	3.5	77	75.3	16.	7	134.	28.5	7	192.7	41.	7	251.4	53.4
18	17.6	3.7	78	76.3	16.2	8	135.	28.7	8	193.7	41.2	8	252.4	53.6
19	18.6	4.	79	77.3	16.4	9	136.	28.9	9	194.7	41.4	9	253.3	53.8
20	19.6	4.2	80	78.3	16.6	140	136.9	29.1	200	195.6	41.6	260	254.3	54.1
21	20.5	4.4	81	79.2	16.8	1	137.9	29.3	1	196.6	41.8	1	255.3	54.3
22	21.5	4.6	82	80.2	17.	2	138.9	29.5	2	197.6	42.	2	256.3	54.5
23	22.5	4.8	83	81.2	17.3	3	139.9	29.7	3	198.6	42.2	3	257.3	54.7
24	23.5	5.	84	82.2	17.5	4	140.9	29.9	4	199.5	42.4	4	258.3	54.9
25	24.4	5.2	85	83.1	17.7	5	141.8	30.1	5	200.5	42.6	5	259.3	55.1
26	25.4	5.4	86	84.1	17.9	6	142.8	30.4	6	201.5	42.8	6	260.3	55.3
27	26.4	5.6	87	85.1	18.1	7	143.8	30.6	7	202.5	43.	7	261.3	55.5
28	27.4	5.8	88	86.1	18.3	8	144.8	30.8	8	203.5	43.2	8	262.1	55.7
29	28.4	6.	89	87.1	18.5	9	145.7	31.	9	204.4	43.5	9	263.1	55.9
30	29.3	6.2	90	88.	18.7	150	146.7	31.2	210	205.4	43.7	270	264.1	56.1
31	30.3	6.4	91	89.	18.9	1	147.7	31.4	1	206.4	43.9	1	265.1	56.3
32	31.3	6.7	92	90.	19.1	2	148.7	31.6	2	207.4	44.1	2	266.1	56.6
33	32.3	6.9	93	91.	19.3	3	149.7	31.8	3	208.3	44.3	3	267.	56.8
34	33.3	7.1	94	91.9	19.5	4	150.6	32.	4	209.3	44.5	4	268.	57.
35	34.3	7.3	95	92.9	19.8	5	151.6	32.2	5	210.3	44.7	5	269.	57.2
36	35.3	7.5	96	93.9	20.	6	152.6	32.4	6	211.3	44.9	6	270.	57.4
37	36.3	7.7	97	94.9	20.2	7	153.6	32.6	7	212.3	45.1	7	270.9	57.6
38	37.3	7.9	98	95.9	20.4	8	154.5	32.9	8	213.2	45.3	8	271.9	57.8
39	38.1	8.1	99	96.8	20.6	9	155.5	33.1	9	214.2	45.5	9	272.9	58.
40	39.1	8.3	100	97.8	20.8	160	156.5	33.3	220	215.2	45.7	280	273.9	58.2
41	40.1	8.5	1	98.8	21.	1	157.5	33.5	1	216.2	45.9	1	274.9	58.4
42	41.1	8.7	2	99.8	21.2	2	158.5	33.7	2	217.1	46.2	2	275.8	58.6
43	42.1	8.9	3	100.7	21.4	3	159.4	33.9	3	218.1	46.4	3	276.8	58.8
44	43.	9.1	4	101.7	21.6	4	160.4	34.1	4	219.1	46.6	4	277.8	59.
45	44.	9.4	5	102.7	21.8	5	161.4	34.3	5	220.1	46.8	5	278.8	59.3
46	45.	9.6	6	103.7	22.	6	162.4	34.5	6	221.1	47.	6	279.8	59.5
47	46.	9.8	7	104.7	22.2	7	163.4	34.7	7	222.	47.2	7	280.7	59.7
48	47.	10.	8	105.7	22.5	8	164.3	34.9	8	223.	47.4	8	281.7	59.9
49	47.9	10.2	9	106.6	22.7	9	165.3	35.1	9	224.	47.6	9	282.7	60.1
50	48.9	10.4	110	107.6	22.9	170	166.3	35.3	230	225.	47.8	290	283.7	60.3
51	49.9	10.6	1	108.6	23.1	1	167.3	35.6	1	226.	48.	1	284.6	60.5
52	50.9	10.8	2	109.6	23.3	2	168.2	35.8	2	226.9	48.2	2	285.6	60.7
53	51.8	11.	3	110.5	23.5	3	169.2	36.	3	227.9	48.4	3	286.6	60.9
54	52.8	11.2	4	111.5	23.7	4	170.2	36.2	4	228.9	48.7	4	287.6	61.1
55	53.8	11.4	5	112.5	23.9	5	171.2	36.4	5	229.9	48.9	5	288.6	61.3
56	54.8	11.6	6	113.5	24.1	6	172.2	36.6	6	230.8	49.1	6	289.5	61.5
57	55.8	11.9	7	114.4	24.3	7	173.1	36.8	7	231.8	49.3	7	290.5	61.7
58	56.7	12.1	8	115.4	24.5	8	174.1	37.	8	232.8	49.5	8	291.5	62.
59	57.7	12.3	9	116.4	24.7	9	175.1	37.2	9	233.8	49.7	9	292.5	62.2
60	58.7	12.5	130	117.4	24.9	180	176.1	37.4	240	234.8	49.9	300	293.4	62.4
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and DiE Latitude.

Course 120.

Course 130.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.2	61	30.4	13.7	121	117.9	27.2	181	176.4	40.7	241	234.8	54.3
2	1.9	0.4	62	30.4	13.9	2	118.9	27.4	2	177.3	40.9	2	235.8	54.4
3	2.9	0.7	63	31.4	14.2	3	119.8	27.7	3	178.3	41.2	3	236.8	54.7
4	3.9	0.9	64	32.4	14.4	4	120.8	27.9	4	179.3	41.4	4	237.7	54.9
5	4.9	1.1	65	33.3	14.6	5	121.8	28.1	5	180.3	41.6	5	238.7	55.1
6	5.8	1.3	66	34.3	14.8	6	122.8	28.3	6	181.2	41.8	6	239.7	55.3
7	6.8	1.6	67	35.3	15.1	7	123.7	28.6	7	182.2	42.1	7	240.7	55.6
8	7.8	1.8	68	36.3	15.3	8	124.7	28.8	8	183.2	42.3	8	241.6	55.8
9	8.8	2.	69	37.2	15.5	9	125.7	29.	9	184.2	42.5	9	242.6	56.
10	9.7	2.2	70	38.2	15.7	130	190.7	29.2	100	185.1	42.7	250	243.6	56.2
11	10.7	2.5	71	39.2	16.	1	157.6	29.5	1	186.1	43.	1	244.6	56.5
12	11.7	2.7	72	70.2	16.2	2	158.6	29.7	2	187.1	43.2	2	245.5	56.7
13	12.7	3.0	73	71.1	16.4	3	159.6	29.9	3	188.1	43.4	3	246.5	56.9
14	13.6	3.1	74	72.1	16.6	4	130.6	30.1	4	189.	43.6	4	247.5	57.1
15	14.6	3.4	75	73.1	16.9	5	131.5	30.4	5	190.	43.9	5	248.5	57.4
16	15.6	3.6	76	74.1	17.1	6	132.5	30.6	6	191.	44.1	6	249.4	57.6
17	16.6	3.8	77	75.	17.3	7	133.5	30.8	7	192.	44.3	7	250.4	57.8
18	17.5	4.	78	76.	17.5	8	134.5	31.	8	193.	44.5	8	251.4	58.
19	18.5	4.3	79	77.	17.8	9	135.4	31.3	9	193.9	44.8	9	252.4	58.3
20.	19.5	4.5	80	77.9	18.	140	136.4	31.5	200	194.9	45.	260	253.3	58.6
21	20.5	4.7	81	78.9	18.2	1	137.4	31.7	1	195.8	45.2	1	254.3	58.7
22	21.4	4.9	82	79.9	18.4	2	138.4	31.9	2	196.8	45.4	2	255.3	58.9
23	22.4	5.2	83	80.9	18.7	3	139.3	32.2	3	197.8	45.7	3	256.3	59.2
24	23.4	5.4	84	81.8	18.9	4	140.3	32.4	4	198.8	45.9	4	257.3	59.4
25	24.4	5.6	85	82.8	19.1	5	141.3	32.6	5	199.7	46.1	5	258.2	59.6
26	25.3	5.8	86	83.8	19.3	6	142.3	32.8	6	200.7	46.3	6	259.2	59.8
27	26.3	6.1	87	84.8	19.6	7	143.2	33.1	7	201.7	46.6	7	260.2	60.1
28	27.3	6.3	88	85.7	19.8	8	144.2	33.3	8	202.7	46.8	8	261.1	60.3
29	28.3	6.5	89	86.7	20.	9	145.2	33.5	9	203.6	47.	9	262.1	60.5
30	29.2	6.7	90	87.7	20.2	150	146.2	33.7	210	204.6	47.2	270	263.1	60.7
31	30.2	7.	91	88.7	20.5	1	147.1	34.	1	205.6	47.5	1	264.1	61.
32	31.2	7.2	92	89.6	20.7	2	148.1	34.2	2	206.6	47.7	2	265.	61.2
33	32.1	7.4	93	90.6	20.9	3	149.1	34.4	3	207.5	47.9	3	266.	61.4
34	33.1	7.6	94	91.6	21.1	4	150.1	34.6	4	208.5	48.1	4	267.	61.6
35	34.1	7.9	95	92.6	21.4	5	151.	34.9	5	209.5	48.4	5	268.	61.9
36	35.1	8.1	96	93.5	21.6	6	152.	35.1	6	210.5	48.6	6	268.9	62.1
37	36.1	8.3	97	94.5	21.8	7	153.	35.3	7	211.4	48.8	7	269.9	62.3
38	37.	8.5	98	95.5	22.	8	154.	35.5	8	212.4	49.	8	270.9	62.5
39	38.	8.8	99	96.5	22.3	9	154.9	35.8	9	213.4	49.3	9	271.8	62.8
40	39.	9.	100	97.4	22.5	160	155.9	36.	220	214.4	49.5	280	272.8	63.
41	39.9	9.2	1	98.4	22.7	1	156.9	36.2	1	215.3	49.7	1	273.8	63.2
42	40.9	9.4	2	99.4	22.9	2	157.8	36.4	2	216.3	49.9	2	274.8	63.4
43	41.9	9.7	3	100.4	23.2	3	158.8	36.7	3	217.3	50.2	3	275.7	63.7
44	42.9	9.9	4	101.3	23.4	4	159.8	36.9	4	218.3	50.4	4	276.7	63.9
45	43.8	10.1	5	102.3	23.6	5	160.8	37.1	5	219.2	50.6	5	277.7	64.1
46	44.8	10.3	6	103.3	23.8	6	161.7	37.3	6	220.2	50.8	6	278.7	64.3
47	45.8	10.6	7	104.3	24.1	7	162.7	37.6	7	221.2	51.1	7	279.6	64.6
48	46.8	10.8	8	105.2	24.3	8	163.7	37.8	8	222.2	51.3	8	280.6	64.8
49	47.7	11.	9	106.2	24.5	9	164.7	38.	9	223.1	51.5	9	281.6	65.
50	48.7	11.2	110	107.2	24.7	170	165.6	38.2	230	224.1	51.7	290	282.6	65.2
51	49.7	11.5	1	108.2	25.	1	166.6	38.5	1	225.1	52.	1	283.5	65.5
52	50.7	11.7	2	109.2	25.2	2	167.6	38.7	2	226.1	52.2	2	284.5	65.7
53	51.6	11.9	3	110.1	25.4	3	168.6	38.9	3	227.	52.4	3	285.5	65.9
54	52.6	12.1	4	111.1	25.6	4	169.5	39.1	4	228.	52.6	4	286.4	66.1
55	53.6	12.4	5	112.1	25.9	5	170.5	39.4	5	229.	52.9	5	287.4	66.4
56	54.6	12.6	6	113.	26.1	6	171.5	39.6	6	230.	53.1	6	288.4	66.6
57	55.5	12.8	7	114.	26.3	7	172.5	39.8	7	230.9	53.3	7	289.4	66.8
58	56.5	13.	8	115.	26.5	8	173.4	40.	8	231.9	53.5	8	290.4	67.
59	57.5	13.3	9	116.	26.8	9	174.4	40.3	9	232.9	53.8	9	291.3	67.3
60	58.5	13.5	120	116.9	27.	180	175.4	40.5	240	233.8	54.	300	292.3	67.5
dist.	dep.	d.lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 77°.

Course 140.

Distance, DIF. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1		0.2	61	59.2	14.8	181	117.4	29.3	181	175.6	43.8	241	233.8	58.3
2	1.9	0.5	62	60.3	15.	2	118.4	29.5	2	176.6	44.	2	234.8	58.5
3	2.9	0.7	63	61.1	15.2	3	119.3	29.8	3	177.6	44.3	3	235.8	58.8
4	3.9	1.	64	62.1	15.5	4	120.3	30.	4	178.5	44.5	4	236.8	59.
5	4.9	1.3	65	63.1	15.7	5	121.3	30.2	5	179.5	44.8	5	237.7	59.3
6	5.8	1.5	66	64.	16.	6	122.3	30.5	6	180.5	45.	6	238.7	59.5
7	6.8	1.7	67	65.	16.2	7	123.3	30.7	7	181.4	45.2	7	239.7	59.8
8	7.8	1.9	68	66.	16.5	8	124.3	31.	8	182.4	45.5	8	240.6	60.
9	8.7	2.2	69	67.	16.7	9	125.2	31.2	9	183.4	45.7	9	241.6	60.2
10		2.4	70	67.9	16.9	180	126.1	31.4	180	184.4	46.	250	242.6	60.5
11	9.7	2.7	71	68.9	17.2	1	127.1	31.7	1	185.3	46.2	1	243.5	60.7
12	11.6	2.9	72	69.9	17.4	2	128.1	31.9	2	186.3	46.4	2	244.5	61.
13	12.6	3.1	73	70.8	17.7	3	129.	32.2	3	187.3	46.7	3	245.5	61.2
14	13.6	3.4	74	71.8	17.9	4	130.	32.4	4	188.2	46.9	4	246.5	61.4
15	14.6	3.6	75	72.8	18.1	5	131.	32.7	5	189.2	47.2	5	247.4	61.7
16	15.5	3.9	76	73.7	18.4	6	132.	32.9	6	190.3	47.4	6	248.4	61.9
17	16.5	4.1	77	74.7	18.6	7	132.9	33.1	7	191.1	47.7	7	249.4	62.2
18	17.5	4.4	78	75.7	18.9	8	133.9	33.4	8	192.1	47.9	8	250.3	62.4
19	18.4	4.6	79	76.7	19.1	9	134.9	33.6	9	193.1	48.1	9	251.3	62.7
20		4.8	80	77.8	19.4	140	135.8	33.9	200	194.1	48.4	260	252.3	62.9
21	20.4	5.1	81	78.6	19.6	1	136.8	34.1	1	195.	48.6	1	253.2	63.1
22	21.3	5.3	82	79.6	19.8	2	137.8	34.4	2	196.	48.9	2	254.2	63.4
23	22.3	5.6	83	80.5	20.1	3	138.8	34.6	3	197.	49.1	3	255.2	63.6
24	23.3	5.8	84	81.5	20.3	4	139.7	34.8	4	197.9	49.4	4	256.2	63.9
25	24.3	6.	85	82.5	20.6	5	140.7	35.1	5	198.9	49.6	5	257.1	64.1
26	25.3	6.3	86	83.4	20.8	6	141.7	35.3	6	199.9	49.8	6	258.1	64.4
27	26.2	6.5	87	84.4	21.	7	142.6	35.6	7	200.9	50.1	7	259.1	64.6
28	27.2	6.8	88	85.4	21.3	8	143.6	35.8	8	201.8	50.3	8	260.	64.8
29	28.1	7.	89	86.4	21.5	9	144.6	36.	9	202.8	50.6	9	261.	65.1
30		7.3	90	87.3	21.8	150	145.5	36.3	210	203.8	50.8	270	262.	65.3
31	30.1	7.5	91	88.3	22.	1	146.5	36.5	1	204.7	51.	1	263.	65.6
32	31.	7.7	92	89.3	22.3	2	147.5	36.8	2	205.7	51.3	2	263.9	65.8
33	32.	8.	93	90.2	22.5	3	148.5	37.	3	206.7	51.5	3	264.9	66.
34	33.	8.2	94	91.2	22.7	4	149.4	37.3	4	207.6	51.8	4	265.9	66.3
35	34.	8.5	95	92.2	23.	5	150.4	37.5	5	208.6	52.	5	266.8	66.5
36	34.9	8.7	96	93.1	23.2	6	151.4	37.7	6	209.6	52.3	6	267.8	66.8
37	35.9	9.	97	94.1	23.5	7	152.3	38.	7	210.6	52.5	7	268.8	67.
38	36.9	9.2	98	95.1	23.7	8	153.3	38.2	8	211.5	52.7	8	269.7	67.3
39	37.8	9.4	99	96.1	24.	9	154.3	38.5	9	212.5	53.	9	270.7	67.5
40		9.7	100	97.	24.2	160	155.2	38.7	280	213.5	53.2	280	271.7	67.7
41	39.8	9.9	1	98.	24.4	1	156.2	38.9	1	214.4	53.5	1	272.7	68.
42	40.8	10.2	2	99.	24.7	2	157.2	39.2	2	215.4	53.7	2	273.6	68.2
43	41.7	10.4	3	100.9	24.9	3	158.2	39.4	3	216.4	53.9	3	274.6	68.5
44	42.7	10.6	4	100.9	25.2	4	159.1	39.7	4	217.3	54.2	4	275.6	68.7
45	43.7	10.9	5	101.9	25.4	5	160.1	39.9	5	218.3	54.4	5	276.5	68.9
46	44.6	11.1	6	102.9	25.6	6	161.1	40.2	6	219.3	54.7	6	277.5	69.2
47	45.6	11.4	7	103.8	25.9	7	162.	40.4	7	220.3	54.9	7	278.5	69.4
48	46.6	11.6	8	104.8	26.1	8	163.	40.6	8	221.2	55.2	8	279.4	69.7
49	47.5	11.9	9	105.8	26.4	9	164.	40.9	9	222.2	55.4	9	280.4	69.9
50		12.1	110	106.7	26.6	170	165.	41.1	230	223.2	55.6	290	281.4	70.2
51	49.5	12.3	1	107.7	26.9	1	165.9	41.4	1	224.1	55.9	1	282.4	70.4
52	50.5	12.6	2	108.7	27.1	2	166.9	41.6	2	225.1	56.1	2	283.3	70.6
53	51.4	12.8	3	109.6	27.3	3	167.9	41.9	3	226.1	56.4	3	284.3	70.9
54	52.4	13.1	4	110.6	27.6	4	168.8	42.1	4	227.	56.6	4	285.3	71.1
55	53.4	13.3	5	111.6	27.8	5	169.8	42.3	5	228.	56.9	5	286.2	71.4
56	54.3	13.5	6	112.6	28.1	6	170.8	42.6	6	229.	57.1	6	287.2	71.6
57	55.3	13.8	7	113.5	28.3	7	171.7	42.8	7	230.	57.3	7	288.2	71.9
58	56.3	14.	8	114.5	28.5	8	172.7	43.1	8	230.9	57.6	8	289.1	72.1
59	57.2	14.3	9	115.5	28.8	9	173.7	43.3	9	231.9	57.8	9	290.1	72.3
60	58.2	14.5	120	116.4	29.	180	174.7	43.5	240	232.9	58.1	300	291.1	72.6
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and DIF. Latitude.

Course 70°.

Course 150.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.3	61	58.9	15.8	120	116.9	31.3	181	174.8	46.8	241	232.8	62.4
2	1.9	0.5	62	59.9	16.	2	117.8	31.6	2	175.8	47.1	3	233.8	62.6
3	2.9	0.8	63	60.9	16.3	3	118.8	31.8	3	176.8	47.4	3	234.7	62.9
4	3.9	1.	64	61.8	16.6	4	119.8	32.1	4	177.7	47.6	4	235.7	63.2
5	4.8	1.3	65	62.8	16.8	5	120.7	32.4	5	178.7	47.9	5	236.7	63.4
6	5.8	1.6	66	63.8	17.1	6	121.7	32.6	6	179.7	48.1	6	237.6	63.7
7	6.8	1.8	67	64.7	17.3	7	122.7	32.9	7	180.6	48.4	7	238.6	63.9
8	7.7	2.1	68	65.7	17.6	8	123.6	33.1	8	181.6	48.7	8	239.5	64.2
9	8.7	2.3	69	66.6	17.9	9	124.6	33.4	9	182.6	48.9	9	240.5	64.4
10	9.7	2.6	70	67.6	18.1	130	125.6	33.6	190	183.5	49.3	250	241.5	64.7
11	10.6	2.8	71	68.6	18.4	1	126.5	33.9	1	184.5	49.4	1	242.4	65.
12	11.6	3.1	72	69.5	18.6	2	127.5	34.2	2	185.5	49.7	2	243.4	65.2
13	12.6	3.4	73	70.5	18.9	3	128.5	34.4	3	186.4	50.	3	244.4	65.5
14	13.5	3.6	74	71.5	19.2	4	129.4	34.7	4	187.4	50.3	4	245.3	65.7
15	14.5	3.9	75	72.4	19.4	5	130.4	34.9	5	188.4	50.5	5	246.3	66.
16	15.5	4.1	76	73.4	19.7	6	131.4	35.2	6	189.3	50.7	6	247.3	66.3
17	16.4	4.4	77	74.4	19.9	7	132.3	35.5	7	190.3	51.	7	248.2	66.5
18	17.4	4.7	78	75.3	20.2	8	133.3	35.7	8	191.3	51.2	8	249.2	66.8
19	18.4	4.9	79	76.3	20.4	9	134.3	36.	9	192.2	51.5	9	250.2	67.
20	19.3	5.3	80	77.3	20.7	140	135.2	36.2	200	193.2	51.8	300	251.1	67.3
21	20.3	5.4	81	78.2	21.	1	136.2	36.5	1	194.2	52.	1	252.1	67.6
22	21.3	5.7	82	79.2	21.2	2	137.2	36.8	2	195.1	52.3	2	253.1	67.8
23	22.2	6.	83	80.2	21.5	3	138.1	37.	3	196.1	52.5	3	254.	68.1
24	23.2	6.2	84	81.1	21.7	4	139.1	37.3	4	197.	52.8	4	255.	68.3
25	24.1	6.5	85	82.1	22.	5	140.1	37.5	5	198.	53.1	5	256.	68.6
26	25.1	6.7	86	83.1	22.3	6	141.	37.8	6	199.	53.3	6	257.	68.8
27	26.1	7.	87	84.	22.5	7	142.	38.	7	199.9	53.6	7	258.	69.1
28	27.	7.3	88	85.	22.8	8	143.	38.3	8	200.9	53.8	8	259.	69.4
29	28.	7.5	89	86.	23.	9	143.9	38.6	9	201.9	54.1	9	260.	69.6
30	29.	7.8	90	86.9	23.3	150	144.9	38.8	210	202.8	54.4	370	260.8	69.9
31	29.9	8.	91	87.9	23.6	1	145.9	39.1	1	203.8	54.6	1	261.8	70.1
32	30.9	8.3	92	88.9	23.8	2	146.8	39.3	2	204.8	54.9	2	262.7	70.4
33	31.9	8.5	93	89.8	24.1	3	147.8	39.6	3	205.7	55.1	3	263.7	70.7
34	32.8	8.8	94	90.8	24.3	4	148.8	39.9	4	206.7	55.4	4	264.7	70.9
35	33.8	9.1	95	91.8	24.6	5	149.7	40.1	5	207.7	55.6	5	265.6	71.2
36	34.8	9.3	96	92.7	24.8	6	150.7	40.4	6	208.6	55.9	6	266.6	71.4
37	35.7	9.6	97	93.7	25.1	7	151.7	40.6	7	209.6	56.2	7	267.6	71.7
38	36.7	9.8	98	94.7	25.4	8	152.6	40.9	8	210.6	56.4	8	268.5	72.
39	37.7	10.1	99	95.6	25.6	9	153.6	41.3	9	211.5	56.7	9	269.5	72.2
40	38.6	10.4	100	96.6	25.9	160	154.5	41.4	220	212.5	56.9	380	270.5	72.5
41	39.6	10.6	1	97.5	26.1	1	155.5	41.7	1	213.5	57.2	1	271.4	72.7
42	40.6	10.9	2	98.5	26.4	2	156.5	41.9	2	214.4	57.5	2	272.4	73.
43	41.5	11.1	3	99.5	26.7	3	157.4	42.2	3	215.4	57.7	3	273.4	73.2
44	42.5	11.4	4	100.5	26.9	4	158.4	42.4	4	216.4	58.	4	274.3	73.5
45	43.5	11.6	5	101.4	27.2	5	159.4	42.7	5	217.3	58.2	5	275.3	73.8
46	44.4	11.9	6	102.4	27.4	6	160.3	43.	6	218.3	58.5	6	276.3	74.
47	45.4	12.2	7	103.4	27.7	7	161.3	43.2	7	219.3	58.8	7	277.2	74.3
48	46.4	12.4	8	104.3	28.	8	162.3	43.5	8	220.3	59.	8	278.2	74.5
49	47.3	12.7	9	105.3	28.2	9	163.3	43.7	9	221.3	59.3	9	279.2	74.8
50	48.3	12.9	110	106.3	28.5	170	164.3	44.	230	222.3	59.5	390	280.1	75.1
51	49.3	13.2	1	107.2	28.7	1	165.2	44.3	1	223.1	59.8	1	281.1	75.2
52	50.3	13.5	2	108.2	29.	2	166.1	44.5	2	224.1	60.	2	282.1	75.6
53	51.2	13.7	3	109.1	29.2	3	167.1	44.8	3	225.1	60.3	3	283.	75.8
54	52.2	14.	14	110.1	29.5	4	168.1	45.	4	226.	60.6	4	284.	76.1
55	53.1	14.2	15	111.1	29.8	5	169.	45.3	5	227.	60.8	5	284.9	76.4
56	54.1	14.5	16	112.	30.	6	170.	45.6	6	228.	61.1	6	285.9	76.6
57	55.1	14.8	17	113.	30.3	7	171.	45.8	7	228.9	61.3	7	286.9	76.9
58	56.	15.	18	114.	30.5	8	171.9	46.1	8	229.9	61.6	8	287.8	77.1
59	57.	15.3	19	114.9	30.8	9	172.9	46.3	9	230.9	61.9	9	288.8	77.4
60	58.	15.5	190	115.9	31.1	180	173.9	46.6	240	231.8	62.1	300	289.8	77.6

Distance, Departure and Diff. Latitude

Course 750.

Course 100

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.3	61	58.6	16.8	121	116.3	33.4	181	174.	49.9	241	231.7	66.4
2	1.9	0.6	62	59.6	17.1	2	117.3	33.6	2	174.9	50.2	2	232.6	66.7
3	2.9	0.8	63	60.6	17.4	3	118.2	33.9	3	175.9	50.4	3	233.6	67.
4	3.8	1.1	64	61.5	17.6	4	119.2	34.2	4	176.9	50.7	4	234.5	67.3
5	4.8	1.4	65	62.5	17.9	5	120.2	34.5	5	177.8	51.	5	235.5	67.5
6	5.8	1.7	66	63.4	18.2	6	121.1	34.7	6	178.8	51.3	6	236.5	67.8
7	6.7	1.9	67	64.4	18.5	7	122.1	35.	7	179.8	51.5	7	237.4	68.1
8	7.7	2.2	68	65.4	18.7	8	123.	35.3	8	180.7	51.8	8	238.4	68.4
9	8.7	2.5	69	66.3	19.	9	124.	35.6	9	181.7	52.1	9	239.4	68.6
10	9.6	2.8	70	67.3	19.3	130	125.	35.8	190	182.6	52.4	250	240.3	68.9
11	10.6	3.	71	68.2	19.6	1	125.9	36.1	1	183.6	52.6	1	241.3	69.2
12	11.5	3.3	72	69.2	19.8	2	126.9	36.4	2	184.6	52.9	2	242.2	69.5
13	12.5	3.6	73	70.2	20.1	3	127.8	36.7	3	185.5	53.2	3	243.2	69.7
14	13.5	3.9	74	71.1	20.4	4	128.8	36.9	4	186.5	53.5	4	244.2	70.
15	14.4	4.1	75	72.1	20.7	5	129.8	37.2	5	187.4	53.7	5	245.1	70.3
16	15.4	4.4	76	73.1	20.9	6	130.7	37.5	6	188.4	54.	6	246.1	70.6
17	16.3	4.7	77	74.	21.2	7	131.7	37.8	7	189.4	54.3	7	247.	70.8
18	17.3	5.	78	75.	21.5	8	132.7	38.	8	190.3	54.6	8	248.	71.1
19	18.3	5.2	79	75.9	21.8	9	133.6	38.3	9	191.3	54.9	9	249.	71.4
20	19.9	5.5	80	76.9	22.1	140	134.6	38.6	200	192.3	55.1	300	249.9	71.7
21	20.2	5.8	81	77.9	22.3	1	135.5	38.9	1	193.2	55.4	1	250.9	71.9
22	21.1	6.1	82	78.8	22.6	2	136.5	39.1	2	194.2	55.7	2	251.9	72.2
23	22.1	6.3	83	79.8	22.9	3	137.5	39.4	3	195.1	56.	3	252.8	72.5
24	23.1	6.6	84	80.7	23.2	4	138.4	39.7	4	196.1	56.2	4	253.8	72.8
25	24.	6.9	85	81.7	23.4	5	139.4	40.	5	197.1	56.5	5	254.7	73.
26	25.	7.2	86	82.7	23.7	6	140.3	40.2	6	198.	56.8	6	255.7	73.3
27	26.	7.4	87	83.6	24.	7	141.3	40.5	7	199.	57.1	7	256.7	73.6
28	26.9	7.7	88	84.6	24.3	8	142.3	40.8	8	199.9	57.3	8	257.6	73.9
29	27.9	8.	89	85.6	24.5	9	143.2	41.1	9	200.9	57.6	9	258.6	74.1
30	28.8	8.3	90	86.5	24.8	150	144.2	41.3	210	201.9	57.9	310	259.5	74.4
31	29.8	8.5	91	87.5	25.1	1	145.2	41.6	1	202.8	58.2	1	260.5	74.7
32	30.8	8.8	92	88.4	25.4	2	146.1	41.9	2	203.8	58.4	2	261.5	75.
33	31.7	9.1	93	89.4	25.6	3	147.1	42.2	3	204.7	58.7	3	262.4	75.2
34	32.7	9.4	94	90.4	25.9	4	148.	42.4	4	205.7	59.	4	263.4	75.5
35	33.6	9.6	95	91.3	26.2	5	149.	42.7	5	206.7	59.3	5	264.3	75.8
36	34.6	9.9	96	92.3	26.5	6	150.	43.	6	207.6	59.5	6	265.3	76.1
37	35.6	10.2	97	93.2	26.7	7	150.9	43.3	7	208.6	59.8	7	266.3	76.4
38	36.5	10.5	98	94.2	27.	8	151.9	43.6	8	209.6	60.1	8	267.3	76.6
39	37.5	10.7	99	95.2	27.3	9	152.8	43.8	9	210.5	60.4	9	268.2	76.9
40	38.5	11.	100	96.1	27.6	160	153.8	44.1	260	211.5	60.6	360	269.2	77.2
41	39.4	11.3	1	97.1	27.8	1	154.8	44.4	1	212.4	60.9	1	270.1	77.5
42	40.4	11.6	2	98.	28.1	2	155.7	44.7	2	213.4	61.2	2	271.1	77.7
43	41.3	11.9	3	99.	28.4	3	156.7	44.9	3	214.4	61.5	3	272.	78.
44	42.3	12.1	4	100.	28.7	4	157.6	45.2	4	215.3	61.7	4	273.	78.3
45	43.3	12.4	5	100.9	29.0	5	158.6	45.5	5	216.3	62.	5	274.	78.6
46	44.2	12.7	6	101.9	29.2	6	159.6	45.8	6	217.2	62.3	6	274.9	78.8
47	45.2	13.	7	102.9	29.5	7	160.5	46.	7	218.2	62.6	7	275.9	79.1
48	46.1	13.2	8	103.8	29.8	8	161.5	46.3	8	219.2	62.8	8	276.8	79.4
49	47.1	13.5	9	104.8	30.	9	162.5	46.6	9	220.1	63.1	9	277.8	79.7
50	48.1	13.8	110	105.7	30.3	170	163.4	46.9	280	221.1	63.4	380	278.8	79.9
51	49.	14.1	1	106.7	30.6	1	164.4	47.1	1	222.1	63.7	1	279.7	80.2
52	50.	14.3	2	107.7	30.9	2	165.3	47.4	2	223.	63.9	2	280.7	80.5
53	50.9	14.6	3	108.6	31.1	3	166.3	47.7	3	224.	64.2	3	281.6	80.8
54	51.9	14.9	4	109.6	31.4	4	167.3	48.	4	224.9	64.5	4	282.6	81.
55	52.9	15.2	5	110.5	31.7	5	168.2	48.3	5	225.9	64.8	5	283.6	81.3
56	53.8	15.4	6	111.5	32.	6	169.2	48.5	6	226.9	65.1	6	284.5	81.6
57	54.8	15.7	7	112.5	32.2	7	170.1	48.8	7	227.8	65.3	7	285.5	81.9
58	55.8	16.	8	113.4	32.5	8	171.1	49.1	8	228.8	65.6	8	286.5	82.1
59	56.7	16.3	9	114.4	32.8	9	172.1	49.3	9	229.7	65.9	9	287.4	82.4
60	57.7	16.5	190	115.4	33.1	180	173.	49.6	240	230.7	66.2	300	288.4	82.7
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 74°.

Course 170.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.3	61	58.3	17.8	121	115.7	35.4	181	173.1	52.9	241	230.5	70.5
2	1.9	0.6	62	59.3	18.1	2	116.7	35.7	2	174.	53.2	2	231.4	70.8
3	2.9	0.9	63	60.2	18.4	3	117.6	36.	3	175.	53.5	3	232.4	71.1
4	3.8	1.2	64	61.2	18.7	4	118.6	36.3	4	176.	53.8	4	233.3	71.3
5	4.8	1.5	65	62.2	19.	5	119.5	36.5	5	176.9	54.1	5	234.3	71.6
6	5.7	1.8	66	63.1	19.3	6	120.5	36.8	6	177.9	54.4	6	235.3	71.9
7	6.7	2.	67	64.1	19.6	7	121.5	37.1	7	178.8	54.7	7	236.2	72.2
8	7.7	2.3	68	65.	19.9	8	122.4	37.4	8	179.8	55.	8	237.2	72.5
9	8.6	2.6	69	66.	20.2	9	123.4	37.7	9	180.7	55.3	9	238.1	72.8
10	9.6	2.9	70	66.9	20.5	130	124.3	38.	190	181.7	55.6	250	239.1	73.1
11	10.5	3.2	71	67.9	20.8	1	125.3	38.3	1	182.7	55.8	1	240.	73.4
12	11.5	3.5	72	68.9	21.1	2	126.2	38.6	2	183.6	56.1	2	241.	73.7
13	12.4	3.8	73	69.8	21.3	3	127.2	38.9	3	184.6	56.4	3	241.9	74.
14	13.4	4.1	74	70.8	21.6	4	128.1	39.2	4	185.5	56.7	4	242.9	74.3
15	14.3	4.4	75	71.7	21.9	5	129.1	39.5	5	186.5	57.	5	243.9	74.6
16	15.3	4.7	76	72.7	22.2	6	130.1	39.8	6	187.4	57.3	6	244.8	74.8
17	16.3	5.	77	73.6	22.5	7	131.	40.1	7	188.4	57.6	7	245.8	75.1
18	17.2	5.3	78	74.6	22.8	8	132.	40.3	8	189.3	57.9	8	246.7	75.4
19	18.2	5.6	79	75.5	23.1	9	132.9	40.6	9	190.3	58.2	9	247.7	75.7
20	19.1	5.8	80	76.5	23.4	140	133.9	40.9	200	191.3	58.5	260	248.6	76.
21	20.1	6.1	81	77.5	23.7	1	134.8	41.2	1	192.2	58.8	1	249.6	76.3
22	21.	6.4	82	78.4	24.	2	135.8	41.5	2	193.2	59.1	2	250.6	76.6
23	22.	6.7	83	79.4	24.3	3	136.8	41.8	3	194.1	59.4	3	251.5	76.9
24	23.	7.	84	80.3	24.6	4	137.7	42.1	4	195.1	59.6	4	252.5	77.2
25	24.	7.3	85	81.3	24.9	5	138.7	42.4	5	196.	59.9	5	253.4	77.5
26	24.9	7.6	86	82.2	25.1	6	139.6	42.7	6	197.	60.2	6	254.4	77.8
27	25.8	7.9	87	83.2	25.4	7	140.6	43.	7	198.	60.5	7	255.3	78.1
28	26.8	8.2	88	84.2	25.7	8	141.5	43.3	8	198.9	60.8	8	256.3	78.4
29	27.7	8.5	89	85.1	26.	9	142.5	43.6	9	199.9	61.1	9	257.2	78.6
30	28.7	8.8	90	86.1	26.3	150	143.4	43.9	210	200.8	61.4	270	258.2	78.9
31	29.6	9.1	91	87.	26.6	1	144.4	44.1	1	201.8	61.7	1	259.2	79.2
32	30.6	9.4	92	88.	26.9	2	145.4	44.4	2	202.7	62.	2	260.1	79.5
33	31.6	9.6	93	88.9	27.2	3	146.3	44.7	3	203.7	62.3	3	261.1	79.8
34	32.5	9.9	94	89.9	27.5	4	147.3	45.	4	204.6	62.6	4	262.	80.1
35	33.5	10.2	95	90.8	27.8	5	148.2	45.3	5	205.6	62.9	5	263.	80.4
36	34.4	10.5	96	91.8	28.1	6	149.2	45.6	6	206.6	63.2	6	263.9	80.7
37	35.4	10.8	97	92.8	28.4	7	150.1	45.9	7	207.5	63.4	7	264.9	81.
38	36.3	11.1	98	93.7	28.7	8	151.1	46.2	8	208.5	63.7	8	265.9	81.3
39	37.3	11.4	99	94.7	29.	9	152.1	46.5	9	209.4	64.	9	266.8	81.6
40	38.3	11.7	100	95.6	29.2	160	153.	46.8	220	210.4	64.3	280	267.8	81.9
41	39.2	12.	1	96.6	29.5	1	154.	47.1	1	211.3	64.6	1	268.7	82.2
42	40.2	12.3	2	97.5	29.8	2	154.9	47.4	2	212.3	64.9	2	269.7	82.4
43	41.1	12.6	3	98.5	30.1	3	155.9	47.7	3	213.3	65.2	3	270.6	82.7
44	42.1	12.9	4	99.5	30.4	4	156.8	47.9	4	214.2	65.5	4	271.6	83.
45	43.	13.2	5	100.4	30.7	5	157.8	48.2	5	215.2	65.8	5	272.5	83.3
46	44.	13.4	6	101.4	31.	6	158.7	48.5	6	216.1	66.1	6	273.5	83.6
47	44.9	13.7	7	102.3	31.3	7	159.7	48.8	7	217.1	66.4	7	274.5	83.9
48	45.9	14.	8	103.3	31.6	8	160.7	49.1	8	218.	66.7	8	275.4	84.2
49	46.9	14.3	9	104.2	31.9	9	161.6	49.4	9	219.	67.	9	276.4	84.5
50	47.8	14.6	110	105.2	32.2	170	162.6	49.7	230	220.	67.2	290	277.3	84.8
51	48.8	14.9	1	106.1	32.5	1	163.5	50.	1	220.9	67.5	1	278.3	85.1
52	49.7	15.2	2	107.1	32.7	2	164.5	50.3	2	221.9	67.8	2	279.2	85.4
53	50.7	15.5	3	108.1	33.	3	165.4	50.6	3	222.8	68.1	3	280.2	85.7
54	51.6	15.8	4	109.	33.3	4	166.4	50.9	4	223.8	68.4	4	281.2	86.
55	52.6	16.1	5	110.	33.6	5	167.4	51.2	5	224.7	68.7	5	282.1	86.2
56	53.6	16.4	6	110.9	33.9	6	168.3	51.5	6	225.7	69.	6	283.1	86.5
57	54.5	16.7	7	111.9	34.2	7	169.3	51.7	7	226.6	69.3	7	284.	86.8
58	55.5	17.	8	112.8	34.5	8	170.2	52.	8	227.6	69.6	8	285.	87.1
59	56.4	17.2	9	113.8	34.8	9	171.2	52.3	9	228.6	69.9	9	285.9	87.4
60	57.4	17.5	190	114.8	35.1	180	172.1	52.6	240	229.5	70.2	300	286.9	87.7

Distance, Departure and Diff. Latitude.

Course 73°.

Course 180.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	1.	0.3	61	58.	18.9	131	115.1	37.4	181	172.1	55.9	241	200.2	74.5
2	1.9	0.6	62	59.	19.2	9	116.	37.7	2	173.1	56.2	2	200.9	74.8
3	2.9	0.9	63	59.9	19.5	3	117.	38.	3	174.	56.6	3	201.1	75.1
4	3.8	1.2	64	60.9	19.8	4	117.9	38.3	4	175.	56.9	4	202.1	75.4
5	4.8	1.5	65	61.8	20.1	5	118.9	38.6	5	175.9	57.2	5	203.	75.7
6	5.7	1.9	66	62.8	20.4	6	119.8	38.9	6	176.9	57.5	6	204.	76.
7	6.7	2.2	67	63.7	20.7	7	120.8	39.2	7	177.8	57.8	7	204.9	76.3
8	7.6	2.5	68	64.7	21.	8	121.7	39.6	8	178.8	58.1	8	205.9	76.6
9	8.6	2.8	69	65.6	21.3	9	122.7	39.9	9	179.7	58.4	9	206.8	76.9
10	9.5	3.1	70	66.6	21.6	130	123.6	40.2	190	180.7	58.7	250	237.8	77.3
11	10.5	3.4	71	67.5	21.9	1	124.6	40.5	1	181.7	59.	1	238.7	77.6
12	11.4	3.7	72	68.5	22.2	2	125.5	40.8	2	182.6	59.3	2	239.7	77.9
13	12.4	4.	73	69.4	22.5	3	126.5	41.1	3	183.6	59.6	3	240.6	78.2
14	13.3	4.3	74	70.4	22.9	4	127.4	41.4	4	184.5	59.9	4	241.6	78.5
15	14.3	4.6	75	71.3	23.2	5	128.4	41.7	5	185.5	60.3	5	242.5	78.8
16	15.3	4.9	76	72.3	23.5	6	129.3	42.	6	186.4	60.6	6	243.5	79.1
17	16.3	5.3	77	73.2	23.8	7	130.3	42.3	7	187.4	60.9	7	244.4	79.4
18	17.1	5.6	78	74.2	24.1	8	131.2	42.6	8	188.3	61.2	8	245.4	79.7
19	18.1	5.9	79	75.1	24.4	9	132.2	43.	9	189.3	61.5	9	246.3	80.
20	19.	6.2	80	76.1	24.7	140	133.1	43.3	200	190.2	61.8	260	247.3	80.3
21	20.	6.5	81	77.	25.	1	134.1	43.6	1	191.2	62.1	1	248.2	80.7
22	20.9	6.8	82	78.	25.3	2	135.1	43.9	2	192.1	62.4	2	249.2	81.
23	21.9	7.1	83	78.9	25.6	3	136.	44.2	3	193.1	62.7	3	250.1	81.3
24	22.8	7.4	84	79.9	26.	4	137.	44.5	4	194.	63.	4	251.1	81.6
25	23.8	7.7	85	80.8	26.3	5	137.9	44.8	5	195.	63.3	5	252.	81.9
26	24.7	8.	86	81.8	26.6	6	138.9	45.1	6	195.9	63.7	6	253.	82.2
27	25.7	8.3	87	82.7	26.9	7	139.8	45.4	7	196.9	64.	7	253.9	82.5
28	26.6	8.7	88	83.7	27.3	8	140.8	45.7	8	197.8	64.3	8	254.9	82.8
29	27.6	9.	89	84.6	27.5	9	141.7	46.	9	198.8	64.6	9	255.8	83.1
30	28.5	9.3	90	85.6	27.8	150	142.7	46.4	210	199.7	64.9	270	256.8	83.4
31	29.5	9.6	91	86.5	28.1	1	143.6	46.7	1	200.7	65.2	1	257.7	83.7
32	30.4	9.9	92	87.5	28.4	2	144.6	47.	2	201.6	65.5	2	258.7	84.1
33	31.4	10.2	93	88.4	28.7	3	145.5	47.3	3	202.6	65.8	3	259.6	84.4
34	32.3	10.5	94	89.4	29.	4	146.5	47.6	4	203.5	66.1	4	260.6	84.7
35	33.3	10.8	95	90.4	29.4	5	147.4	47.9	5	204.5	66.4	5	261.5	85.
36	34.3	11.1	96	91.3	29.7	6	148.4	48.2	6	205.4	66.7	6	262.5	85.3
37	35.3	11.4	97	92.3	30.	7	149.3	48.5	7	206.4	67.1	7	263.4	85.6
38	36.1	11.7	98	93.2	30.3	8	150.3	48.9	8	207.3	67.4	8	264.4	85.9
39	37.1	12.1	99	94.2	30.6	9	151.2	49.1	9	208.3	67.7	9	265.3	86.2
40	38.	12.4	100	95.1	30.9	160	152.2	49.4	220	209.2	68.	280	266.3	86.5
41	39.	12.7	1	96.1	31.2	1	153.1	49.8	1	210.2	68.3	1	267.2	86.8
42	39.9	13.	2	97.	31.5	2	154.1	50.1	2	211.1	68.6	2	268.2	87.1
43	40.9	13.3	3	98.	31.8	3	155.	50.4	3	212.1	68.9	3	269.1	87.5
44	41.8	13.6	4	99.9	32.1	4	156.	50.7	4	213.	69.2	4	270.1	87.8
45	42.8	13.9	5	99.9	32.4	5	156.9	51.	5	214.	69.5	5	271.1	88.1
46	43.7	14.2	6	100.8	32.8	6	157.9	51.3	6	214.9	69.8	6	272.	88.4
47	44.7	14.5	7	101.8	33.1	7	158.8	51.6	7	215.9	70.1	7	273.	88.7
48	45.7	14.8	8	102.7	33.4	8	159.8	51.9	8	216.8	70.5	8	273.9	89.
49	46.6	15.1	9	103.7	33.7	9	160.7	52.2	9	217.8	70.8	9	274.9	89.3
50	47.6	15.5	110	104.6	34.	170	161.7	52.5	230	218.7	71.1	290	275.8	89.6
51	48.5	15.8	1	105.6	34.3	1	162.6	52.8	1	219.7	71.4	1	276.8	89.9
52	49.5	16.1	2	106.5	34.6	2	163.6	53.2	2	220.6	71.7	2	277.7	90.2
53	50.4	16.4	3	107.5	34.9	3	164.5	53.5	3	221.6	72.	3	278.7	90.5
54	51.4	16.7	4	108.4	35.2	4	165.5	53.8	4	222.5	72.3	4	279.6	90.9
55	52.3	17.	5	109.4	35.5	5	166.4	54.1	5	223.5	72.6	5	280.6	91.2
56	53.3	17.3	6	110.3	35.8	6	167.4	54.4	6	224.4	72.9	6	281.5	91.5
57	54.3	17.6	7	111.3	36.2	7	168.3	54.7	7	225.4	73.2	7	282.5	91.8
58	55.3	17.9	8	112.2	36.5	8	169.3	55.	8	226.4	73.5	8	283.4	92.1
59	56.1	18.2	9	113.2	36.8	9	170.3	55.3	9	227.3	73.9	9	284.4	92.4
60	57.1	18.5	190	114.1	37.1	180	171.3	55.6	240	228.3	74.2	300	285.3	92.7
dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.

Distance, Departure and Diff. Latitude.

Course 720.

TABLE V.

Course 19°.

Distance, Diff. Latitude and Departure.

dist.	l. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.3	61	57.7	19.9	121	114.4	39.4	181	171.1	58.9	241	237.9	78.5
2	1.9	0.7	62	58.6	20.2	3	115.4	39.7	2	172.1	59.3	2	238.8	78.8
3	2.8	1.1	63	59.6	20.5	3	116.3	40.	3	173.	59.6	3	239.8	79.1
4	3.8	1.3	64	60.5	20.8	4	117.3	40.4	4	174.	59.9	4	240.7	79.4
5	4.7	1.6	65	61.5	21.2	5	118.2	40.7	5	174.9	60.2	5	241.7	79.8
6	5.7	2.	66	62.4	21.5	6	119.1	41.	6	175.9	60.6	6	242.6	80.1
7	6.6	2.3	67	63.3	21.8	7	120.1	41.3	7	176.8	60.9	7	243.5	80.4
8	7.6	2.6	68	64.3	22.1	8	121.	41.7	8	177.8	61.2	8	244.5	80.7
9	8.5	2.9	69	65.2	22.5	9	122.	42.	9	178.7	61.5	9	245.4	81.1
10	9.5	3.3	70	66.2	22.8	130	122.9	42.3	190	179.6	61.9	250	246.4	81.4
11	10.4	3.6	71	67.1	23.1	1	123.9	42.6	1	180.6	62.2	1	247.3	81.7
12	11.3	3.9	72	68.1	23.4	2	124.8	43.	2	181.5	62.5	2	248.2	82.
13	12.3	4.3	73	69.	23.8	3	125.8	43.3	3	182.5	62.8	3	249.2	82.4
14	13.2	4.6	74	70.	24.1	4	126.7	43.6	4	183.4	63.2	4	250.2	82.7
15	14.2	4.9	75	70.9	24.4	5	127.6	44.	5	184.4	63.5	5	251.1	83.
16	15.1	5.2	76	71.9	24.7	6	128.6	44.3	6	185.3	63.8	6	252.1	83.3
17	16.1	5.5	77	72.8	25.1	7	129.5	44.6	7	186.3	64.1	7	253.	83.7
18	17.	5.9	78	73.8	25.4	8	130.5	44.9	8	187.2	64.5	8	253.9	84.
19	18.	6.2	79	74.7	25.7	9	131.4	45.3	9	188.2	64.8	9	244.9	84.3
20	18.9	6.5	80	75.6	26.	140	132.4	45.6	200	189.1	65.1	260	245.8	84.6
21	19.9	6.8	81	76.6	26.4	1	133.3	45.9	1	190.	65.4	1	246.8	85.
22	20.8	7.2	82	77.5	26.7	2	134.3	46.2	2	191.	65.8	2	247.7	85.3
23	21.7	7.5	83	78.5	27.	3	135.2	46.6	3	191.9	66.1	3	248.7	85.6
24	22.7	7.8	84	79.4	27.3	4	136.2	46.9	4	192.9	66.4	4	249.6	86.
25	23.6	8.1	85	80.4	27.7	5	137.1	47.3	5	193.8	66.7	5	250.6	86.3
26	24.6	8.5	86	81.3	28.	6	138.	47.5	6	194.8	67.1	6	251.5	86.6
27	25.5	8.9	87	82.3	28.3	7	139.	47.9	7	195.7	67.4	7	252.5	86.9
28	26.5	9.1	88	83.2	28.7	8	139.9	48.2	8	196.7	67.7	8	253.4	87.3
29	27.4	9.4	89	84.2	29.	9	140.9	48.5	9	197.6	68.	9	254.3	87.6
30	28.4	9.8	90	85.1	29.3	150	141.8	48.8	210	198.6	68.4	270	255.3	87.9
31	29.3	10.1	91	86.	29.6	1	142.8	49.2	1	199.5	68.7	1	256.2	88.2
32	30.3	10.4	92	87.	30.	2	143.7	49.5	2	200.4	69.	2	257.2	88.6
33	31.2	10.7	93	87.9	30.3	3	144.7	49.8	3	201.4	69.3	3	258.1	88.9
34	32.1	11.1	94	88.9	30.6	4	145.6	50.1	4	202.3	69.7	4	259.1	89.2
35	33.1	11.4	95	89.8	30.9	5	146.6	50.5	5	203.3	70.	5	260.	89.5
36	34.	11.7	96	90.8	31.3	6	147.5	50.8	6	204.2	70.3	6	261.	89.9
37	35.	12.	97	91.7	31.6	7	148.4	51.1	7	205.2	70.6	7	261.9	90.2
38	35.9	12.4	98	92.7	31.9	8	149.4	51.4	8	206.1	71.	8	262.9	90.5
39	36.9	12.7	99	93.6	32.2	9	150.3	51.8	9	207.1	71.3	9	263.8	90.8
40	37.8	13.	100	94.6	32.6	160	151.3	52.1	220	208.	71.6	280	264.7	91.2
41	38.8	13.3	1	95.5	32.9	1	152.2	52.4	1	209.	72.	1	265.7	91.5
42	39.7	13.7	2	96.4	33.2	2	153.2	52.7	2	209.9	72.3	2	266.6	91.8
43	40.7	14.	3	97.4	33.5	3	154.1	53.1	3	210.9	72.6	3	267.6	92.1
44	41.6	14.3	4	98.3	33.9	4	155.1	53.4	4	211.8	72.9	4	268.5	92.5
45	42.5	14.7	5	99.3	34.2	5	156.	53.7	5	212.7	73.3	5	269.5	92.8
46	43.5	15.	6	100.2	34.5	6	157.	54.	6	213.7	73.6	6	270.4	93.1
47	44.4	15.3	7	101.2	34.8	7	157.9	54.4	7	214.6	73.9	7	271.4	93.4
48	45.4	15.6	8	102.1	35.2	8	158.8	54.7	8	215.6	74.2	8	272.3	93.8
49	46.3	16.	9	103.1	35.5	9	159.8	55.	9	216.5	74.6	9	273.3	94.1
50	47.3	16.3	110	104.	35.8	170	160.7	55.3	230	217.5	74.9	290	274.3	94.4
51	48.2	16.6	1	105.	36.1	1	161.7	55.7	1	218.4	75.2	1	275.1	94.7
52	49.2	16.9	2	105.9	36.5	2	162.6	56.	2	219.4	75.5	2	276.1	95.1
53	50.1	17.3	3	106.8	36.8	3	163.6	56.3	3	220.3	75.9	3	277.	95.4
54	51.1	17.6	4	107.8	37.1	4	164.5	56.6	4	221.3	76.2	4	278.	95.7
55	52.	17.9	5	108.7	37.4	5	165.5	57.	5	222.2	76.5	5	278.9	96.
56	52.9	18.2	6	109.7	37.8	6	166.4	57.3	6	223.1	76.8	6	279.9	96.4
57	53.9	18.6	7	110.6	38.1	7	167.4	57.6	7	224.1	77.2	7	280.8	96.7
58	54.8	18.9	8	111.6	38.4	8	168.3	58.	8	225.	77.5	8	281.8	97.
59	55.8	19.2	9	112.5	38.7	9	169.2	58.3	9	226.	77.8	9	282.7	97.3
60	55.7	19.5	190	113.5	39.1	180	170.2	58.6	240	226.9	78.1	300	283.7	97.7

Distance, Departure and Diff. Latitude.

Course 71°.

R

Course 90°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.3	61	57.3	20.9	121	113.7	41.4	181	170.1	61.9	241	226.5	82.4
2	1.9	0.7	62	58.3	21.2	2	114.6	41.7	2	171.	62.2	3	227.4	82.8
3	2.8	1.1	63	59.2	21.5	3	115.6	42.1	3	172.	62.6	4	228.3	83.1
4	3.8	1.4	64	60.1	21.9	4	116.5	42.4	4	172.9	62.9	5	229.2	83.5
5	4.7	1.7	65	61.1	22.2	5	117.5	42.8	5	173.8	63.3	6	230.2	83.9
6	5.6	2.1	66	62.	22.6	6	118.4	43.1	6	174.8	63.6	7	231.2	84.1
7	6.6	2.4	67	63.	22.9	7	119.3	43.4	7	175.7	64.	8	232.1	84.8
8	7.5	2.7	68	63.9	23.3	8	120.3	43.8	8	176.7	64.3	9	233.	84.8
9	8.5	3.1	69	64.8	23.6	9	121.2	44.1	9	177.6	64.6		234.	85.2
10	9.4	3.4	70	65.8	23.9	130	122.2	44.5	190	173.5	65.	250	234.9	85.5
11	10.3	3.8	71	66.7	24.3	1	123.1	44.8	1	179.5	65.3	1	235.9	85.8
12	11.3	4.1	72	67.7	24.6	2	124.	45.1	2	180.4	65.7	2	236.8	86.2
13	12.2	4.4	73	68.6	25.	3	125.	45.5	3	181.4	66.	3	237.7	86.5
14	13.2	4.8	74	69.5	25.3	4	125.9	45.8	4	182.3	66.4	4	238.7	86.9
15	14.1	5.1	75	70.5	25.7	5	126.9	46.2	5	183.2	66.7	5	239.6	87.2
16	15.	5.5	76	71.4	26.	6	127.8	46.5	6	184.2	67.	6	240.6	87.6
17	16.	5.8	77	72.4	26.3	7	128.7	46.9	7	185.1	67.4	7	241.5	87.9
18	16.9	6.2	78	73.3	26.7	8	129.7	47.2	8	186.1	67.7	8	242.4	88.2
19	17.9	6.5	79	74.3	27.	9	130.6	47.5	9	187.	68.1	9	243.4	88.6
20	18.8	6.8	80	75.2	27.4	140	131.6	47.9	200	187.9	68.4	260	244.3	88.9
21	19.7	7.2	81	76.1	27.7	1	132.5	48.2	1	188.9	68.7	1	245.3	89.2
22	20.7	7.5	82	77.1	28.	2	133.4	48.6	2	189.8	69.1	2	246.2	89.6
23	21.6	7.9	83	78.	28.4	3	134.4	48.9	3	190.8	69.4	3	247.1	89.9
24	22.6	8.2	84	78.9	28.7	4	135.3	49.3	4	191.7	69.8	4	248.1	90.2
25	23.5	8.6	85	79.9	29.1	5	136.3	49.6	5	192.6	70.1	5	249.	90.6
26	24.4	8.9	86	80.8	29.4	6	137.2	49.9	6	193.6	70.5	6	250.	91.
27	25.4	9.2	87	81.8	29.8	7	138.1	50.3	7	194.5	70.8	7	250.9	91.3
28	26.3	9.6	88	82.7	30.1	8	139.1	50.6	8	195.5	71.1	8	251.8	91.7
29	27.3	9.9	89	83.6	30.4	9	140.	51.	9	196.4	71.5	9	252.8	92.
30	28.2	10.3	90	84.6	30.8	150	141.	51.3	210	197.3	71.8	270	253.7	92.3
31	29.1	10.6	91	85.5	31.1	1	141.9	51.6	1	198.3	72.2	1	254.7	92.7
32	30.1	10.9	92	86.5	31.5	2	142.8	52.	2	199.2	72.5	2	255.6	93.
33	31.	11.3	93	87.4	31.8	3	143.8	52.3	3	200.2	72.9	3	256.5	93.4
34	31.9	11.6	94	88.3	32.1	4	144.7	52.7	4	201.1	73.2	4	257.5	93.7
35	32.9	12.	95	89.3	32.5	5	145.7	53.	5	202.	73.5	5	258.4	94.1
36	33.8	12.3	96	90.2	32.8	6	146.6	53.4	6	203.	73.8	6	259.4	94.4
37	34.8	12.7	97	91.2	33.2	7	147.5	53.7	7	203.9	74.2	7	260.3	94.7
38	35.7	13.	98	92.1	33.5	8	148.5	54.	8	204.9	74.6	8	261.2	95.1
39	36.6	13.3	99	93.	33.9	9	149.4	54.4	9	205.8	74.9	9	262.2	95.4
40	37.6	13.7	100	94.	34.2	160	150.4	54.7	220	206.7	75.3	280	263.1	95.8
41	38.5	14.	1	94.9	34.5	1	151.3	55.1	1	207.7	75.6	1	264.1	96.1
42	39.5	14.4	2	95.8	34.9	2	152.2	55.4	2	208.6	75.9	2	265.	96.4
43	40.4	14.7	3	96.8	35.2	3	153.2	55.7	3	209.6	76.3	3	265.9	96.8
44	41.3	15.	4	97.7	35.6	4	154.1	56.1	4	210.5	76.6	4	266.9	97.1
45	42.3	15.4	5	98.7	35.9	5	155.	56.4	5	211.4	77.	5	267.8	97.5
46	43.3	15.7	6	99.6	36.3	6	156.	56.8	6	212.4	77.3	6	268.8	97.8
47	44.3	16.1	7	100.5	36.6	7	156.9	57.1	7	213.3	77.6	7	269.7	98.2
48	45.1	16.4	8	101.5	36.9	8	157.9	57.5	8	214.3	78.	8	270.6	98.5
49	46.	16.8	9	102.4	37.3	9	158.8	57.8	9	215.3	78.3	9	271.6	98.8
50	47.	17.1	110	103.4	37.6	170	159.7	58.1	230	216.1	78.7	290	272.5	99.2
51	47.9	17.4	1	104.3	38.	1	160.7	58.5	1	217.1	79.	1	273.5	99.5
52	48.9	17.8	2	105.3	38.3	2	161.6	58.8	2	218.	79.3	2	274.4	99.9
53	49.8	18.1	3	106.3	38.6	3	162.6	59.2	3	218.9	79.7	3	275.3	100.2
54	50.7	18.5	4	107.1	39.	4	163.5	59.5	4	219.9	80.	4	276.3	100.6
55	51.7	18.8	5	108.1	39.3	5	164.4	59.9	5	220.8	80.4	5	277.2	100.9
56	52.6	19.2	6	109.	39.7	6	165.4	60.2	6	221.8	80.7	6	278.1	101.2
57	53.6	19.5	7	109.9	40.	7	166.3	60.5	7	222.7	81.1	7	279.1	101.6
58	54.5	19.8	8	110.9	40.4	8	167.3	60.9	8	223.6	81.4	8	280.	101.9
59	55.4	20.2	9	111.8	40.7	9	168.3	61.2	9	224.6	81.7	9	281.	102.3
60	56.4	20.5	190	112.8	41.	190	169.1	61.6	240	225.5	82.1	300	281.9	102.6
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 70°.

Course 210°.

Distance, Dist. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	56.9	21.9	121	112.	42.4	181	169.	64.9	241	225.	86.4
2	1.9	0.7	62	57.9	22.2	2	112.9	42.7	2	169.9	65.2	2	225.9	86.7
3	2.8	1.1	63	58.8	22.6	3	114.8	44.1	3	170.8	65.6	3	226.9	87.1
4	3.7	1.4	64	59.7	22.9	4	115.8	44.4	4	171.8	65.9	4	227.8	87.4
5	4.7	1.8	65	60.7	22.3	5	116.7	44.8	5	172.7	66.3	5	228.7	87.8
6	5.6	2.2	66	61.6	22.7	6	117.6	45.2	6	173.6	66.7	6	229.7	88.2
7	6.5	2.5	67	62.5	24.	7	118.6	45.5	7	174.6	67.	7	230.6	88.5
8	7.5	2.9	68	63.5	24.4	8	119.5	45.9	8	175.5	67.4	8	231.5	88.9
9	8.4	3.2	69	64.4	24.7	9	120.4	46.2	9	176.4	67.7	9	232.5	89.2
10	9.3	3.6	70	65.4	25.1	120	121.4	46.6	190	177.4	68.1	250	233.4	89.6
11	10.3	3.9	71	66.3	25.4	1	122.3	46.9	1	178.3	68.4	1	234.3	90.
12	11.2	4.3	72	67.2	25.8	2	123.2	47.3	2	179.2	68.8	2	235.2	90.3
13	12.1	4.7	73	68.2	26.2	3	124.2	47.7	3	180.2	69.2	3	236.2	90.7
14	13.1	5.	74	69.1	26.5	4	125.1	48.	4	181.1	69.5	4	237.1	91.
15	14.	5.4	75	70.	26.9	5	126.	48.4	5	182.	69.9	5	238.1	91.4
16	14.9	5.7	76	71.	27.2	6	127.	48.7	6	183.	70.2	6	239.	91.7
17	15.9	6.1	77	71.9	27.6	7	127.9	49.1	7	183.9	70.6	7	239.9	92.1
18	16.8	6.5	78	72.8	28.	8	128.8	49.5	8	184.8	71.	8	240.9	92.5
19	17.7	6.8	79	72.8	28.3	9	129.8	49.8	9	185.8	71.3	9	241.8	92.8
20	18.7	7.2	80	74.7	28.7	140	130.7	50.2	200	186.7	71.7	260	242.7	93.2
21	19.6	7.5	81	75.6	29.	1	131.6	50.5	1	187.6	72.	1	243.7	93.5
22	20.5	7.9	82	76.6	29.4	2	132.6	50.9	2	188.6	72.4	2	244.6	93.9
23	21.5	8.2	83	77.5	29.7	3	133.5	51.2	3	189.5	72.7	3	245.5	94.3
24	22.4	8.6	84	78.4	30.1	4	134.4	51.6	4	190.5	73.1	4	246.5	94.6
25	23.3	9.	85	79.4	30.5	5	135.4	52.	5	191.4	73.5	5	247.4	95.
26	24.3	9.3	86	80.3	30.8	6	136.3	52.3	6	192.3	73.8	6	248.3	95.3
27	25.2	9.7	87	81.2	31.2	7	137.2	52.7	7	193.2	74.2	7	249.2	95.7
28	26.1	10.	88	82.2	31.5	8	138.2	53.	8	194.2	74.5	8	250.2	96.
29	27.1	10.4	89	83.1	31.9	9	139.1	53.4	9	195.1	74.9	9	251.1	96.4
30	28.	10.8	90	84.	32.3	150	140.	53.8	210	196.1	75.3	270	252.1	96.8
31	28.9	11.1	91	85.	32.6	1	141.	54.1	1	197.	75.6	1	253.	97.1
32	29.9	11.5	92	85.9	33.	2	141.9	54.5	2	197.9	76.	2	253.9	97.5
33	30.8	11.8	93	86.8	33.3	3	142.8	54.8	3	198.8	76.3	3	254.8	97.8
34	31.7	12.2	94	87.8	33.7	4	143.8	55.2	4	199.8	76.7	4	255.8	98.2
35	32.7	12.5	95	88.7	34.	5	144.7	55.5	5	200.7	77.	5	256.7	98.6
36	33.6	12.9	96	89.6	34.4	6	145.6	55.9	6	201.7	77.4	6	257.7	98.9
37	34.5	13.3	97	90.6	34.8	7	146.6	56.3	7	202.6	77.8	7	258.6	99.3
38	35.5	13.6	98	91.5	35.1	8	147.5	56.6	8	203.5	78.1	8	259.5	99.6
39	36.4	14.	99	92.4	35.5	9	148.4	57.	9	204.5	78.5	9	260.5	100.
40	37.3	14.3	100	93.4	35.8	160	149.4	57.3	220	205.4	78.8	280	261.4	100.2
41	38.3	14.7	1	94.3	36.2	1	150.3	57.7	1	206.3	79.2	1	262.3	100.7
42	39.3	15.1	2	95.2	36.6	2	151.2	58.1	2	207.2	79.6	2	263.2	101.1
43	40.1	15.4	3	96.2	36.9	3	152.2	58.4	3	208.2	79.9	3	264.2	101.4
44	41.1	15.8	4	97.1	37.3	4	153.1	58.8	4	209.1	80.3	4	265.1	101.8
45	42.	16.1	5	98.	37.6	5	154.	59.1	5	210.1	80.6	5	266.1	102.1
46	42.9	16.5	6	99.	38.	6	155.	59.5	6	211.	81.	6	267.	102.5
47	43.9	16.8	7	99.9	38.3	7	155.9	59.8	7	211.9	81.3	7	267.9	102.9
48	44.8	17.2	8	100.8	38.7	8	156.8	60.2	8	212.8	81.7	8	268.9	103.2
49	45.7	17.6	9	101.8	39.1	9	157.8	60.6	9	213.8	82.1	9	269.8	103.6
50	46.7	17.9	110	102.7	39.4	170	158.7	60.9	230	214.7	82.4	290	270.7	103.9
51	47.6	18.3	1	103.6	39.8	1	159.6	61.3	1	215.7	82.8	1	271.7	104.3
52	48.5	18.6	2	104.6	40.1	2	160.6	61.6	2	216.6	83.1	2	272.6	104.6
53	49.5	19.	3	105.5	40.5	3	161.5	62.	3	217.5	83.5	3	273.5	105.
54	50.4	19.4	4	106.4	40.9	4	162.4	62.4	4	218.5	83.9	4	274.5	105.4
55	51.3	19.7	5	107.4	41.2	5	163.4	62.7	5	219.4	84.2	5	275.4	105.7
56	52.3	20.1	6	108.3	41.6	6	164.3	63.1	6	220.3	84.6	6	276.3	106.1
57	53.2	20.4	7	109.2	41.9	7	165.2	63.4	7	221.3	84.9	7	277.2	106.4
58	54.1	20.8	8	110.2	42.3	8	166.2	63.8	8	222.2	85.3	8	278.1	106.8
59	55.1	21.1	9	111.1	42.6	9	167.1	64.1	9	223.1	85.6	9	279.1	107.2
60	56.	21.5	190	112.	43.	180	168.	64.5	240	224.1	86.	300	280.1	107.5

Distance, Departure and Dist. Latitude.

Course 60°

Course 88°.

Distance, Dist. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	56.6	22.9	121	112.2	45.3	181	167.8	67.8	241	222.5	90.3
2	1.9	0.7	62	57.5	23.2	2	113.1	45.7	3	168.7	68.2	2	224.4	90.7
3	2.8	1.1	63	58.4	23.6	3	114.	46.1	3	169.7	68.6	3	225.3	91.
4	3.7	1.5	64	59.3	24.	4	115.	46.5	4	170.6	69.0	4	226.2	91.4
5	4.6	1.9	65	60.3	24.3	5	115.9	46.8	5	171.5	69.3	5	227.2	91.8
6	5.6	2.2	66	61.2	24.7	6	116.8	47.2	6	172.5	69.7	6	228.1	92.2
7	6.5	2.6	67	62.1	25.1	7	117.8	47.6	7	173.4	70.1	7	229.	92.5
8	7.4	3.	68	63.	25.5	8	118.7	47.9	8	174.3	70.4	8	230.9	92.9
9	8.3	3.4	69	64.	25.8	9	119.6	48.3	9	175.2	70.8	9	230.9	92.3
10	9.3	3.7	70	64.9	26.2	130	120.5	48.7	190	176.2	71.2	250	231.8	92.7
11	10.2	4.1	71	65.8	26.6	1	121.5	49.1	1	177.1	71.5	1	232.7	94.
12	11.1	4.5	72	66.8	27.	2	122.4	49.4	2	178.	71.9	2	233.7	94.4
13	12.1	4.9	73	67.7	27.3	3	123.3	49.8	3	178.9	72.3	3	234.6	94.8
14	13.	5.2	74	68.6	27.7	4	124.2	50.2	4	179.9	72.7	4	235.5	95.2
15	13.9	5.6	75	69.5	28.1	5	125.2	50.6	5	180.8	73.	5	236.4	95.5
16	14.8	6.	76	70.5	28.5	6	126.1	50.9	6	181.7	73.4	6	237.4	95.9
17	15.8	6.4	77	71.4	28.9	7	127.	51.3	7	182.7	73.8	7	238.3	96.3
18	16.7	6.7	78	72.3	29.3	8	128.	51.7	8	183.6	74.2	8	239.3	96.6
19	17.6	7.1	79	73.2	29.6	9	128.9	52.1	9	184.5	74.5	9	240.1	97.
20	18.5	7.5	80	74.1	30.	140	129.8	52.4	200	185.4	74.9	300	241.1	97.4
21	19.5	7.9	81	75.1	30.3	1	130.7	52.8	1	186.4	75.3	1	242.	97.8
22	20.4	8.2	82	76.	30.7	2	131.7	53.2	2	187.3	75.7	2	242.9	98.1
23	21.3	8.6	83	77.	31.1	3	132.6	53.6	3	188.2	76.	3	243.8	98.5
24	22.3	9.	84	77.9	31.5	4	133.5	53.9	4	189.1	76.4	4	244.8	98.9
25	23.2	9.4	85	78.8	31.8	5	134.4	54.3	5	190.1	76.8	5	245.7	99.3
26	24.1	9.7	86	79.7	32.2	6	135.4	54.7	6	191.	77.2	6	246.6	99.6
27	25.	10.1	87	80.7	32.6	7	136.3	55.1	7	191.9	77.5	7	247.6	100.
28	25.9	10.5	88	81.6	33.	8	137.2	55.4	8	192.9	77.9	8	248.5	100.4
29	26.8	10.9	89	82.5	33.3	9	138.2	55.8	9	193.8	78.3	9	249.4	100.8
30	27.8	11.2	90	83.4	33.7	150	139.1	56.2	210	194.7	78.7	370	250.3	101.1
31	28.7	11.6	91	84.4	34.1	1	140.	56.6	1	195.6	79.	1	251.3	101.5
32	29.7	12.	92	85.3	34.5	2	140.9	56.9	2	196.6	79.4	2	252.2	101.9
33	30.6	12.4	93	86.2	34.8	3	141.9	57.3	3	197.5	79.8	3	253.1	102.3
34	31.5	12.7	94	87.1	35.2	4	142.8	57.7	4	198.4	80.2	4	254.	102.6
35	32.5	13.1	95	88.1	35.6	5	143.7	58.1	5	199.3	80.5	5	255.	103.
36	33.4	13.5	96	89.	36.	6	144.6	58.4	6	200.3	80.9	6	255.9	103.4
37	34.3	13.9	97	89.9	36.3	7	145.6	58.8	7	201.2	81.3	7	256.8	103.8
38	35.2	14.2	98	90.8	36.7	8	146.5	59.2	8	202.1	81.7	8	257.8	104.1
39	36.2	14.6	99	91.8	37.1	9	147.4	59.6	9	203.1	82.	9	258.7	104.5
40	37.1	15.	100	92.7	37.5	160	148.3	59.9	320	204.	82.4	380	259.6	104.9
41	38.	15.4	1	93.6	37.8	1	149.3	60.3	1	204.9	82.8	1	260.5	105.3
42	38.9	15.7	2	94.6	38.2	2	150.2	60.7	2	205.8	83.2	2	261.5	105.6
43	39.9	16.1	3	95.5	38.6	3	151.1	61.1	3	206.8	83.5	3	262.4	106.
44	40.8	16.5	4	96.4	39.	4	152.1	61.4	4	207.7	83.9	4	263.3	106.4
45	41.7	16.9	5	97.4	39.3	5	153.	61.8	5	208.6	84.3	5	264.2	106.8
46	42.7	17.2	6	98.3	39.7	6	153.9	62.2	6	209.5	84.7	6	265.2	107.1
47	43.6	17.6	7	99.2	40.1	7	154.8	62.6	7	210.5	85.	7	266.1	107.5
48	44.5	18.	8	100.1	40.5	8	155.8	62.9	8	211.4	85.4	8	267.	107.9
49	45.4	18.4	9	101.1	40.8	9	156.7	63.3	9	212.3	85.8	9	268.	108.3
50	46.4	18.7	110	102.	41.2	170	157.6	63.7	330	213.2	86.2	390	269.9	108.6
51	47.3	19.1	1	102.9	41.6	1	158.5	64.1	1	214.2	86.5	1	269.8	109.
52	48.2	19.5	2	103.8	42.	2	159.5	64.4	2	215.1	86.9	2	270.7	109.4
53	49.1	19.9	3	104.8	42.3	3	160.4	64.8	3	216.	87.3	3	271.7	109.8
54	50.1	20.2	4	105.7	42.7	4	161.3	65.2	4	217.	87.7	4	272.6	110.1
55	51.	20.6	5	106.6	43.1	5	162.3	65.6	5	217.9	88.	5	273.5	110.5
56	51.9	21.	6	107.6	43.5	6	163.2	65.9	6	218.8	88.4	6	274.4	110.9
57	52.8	21.4	7	108.5	43.8	7	164.1	66.3	7	219.7	88.8	7	275.4	111.3
58	53.8	21.7	8	109.4	44.2	8	165.	66.7	8	220.7	89.2	8	276.3	111.6
59	54.7	22.1	9	110.3	44.6	9	166.	67.1	9	221.6	89.5	9	277.3	112.
60	55.6	22.5	120	111.3	45.	180	166.9	67.4	240	222.5	89.9	300	278.2	112.4
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Dist. Latitude.

Course 60°.

Course 83°

Distance, Dis. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	56.9	23.8	129	111.4	47.3	161	166.6	70.7	241	231.8	94.9
2	1.8	0.8	62	57.1	24.9	3	112.3	47.7	2	167.5	71.1	2	232.8	94.6
3	2.8	1.2	63	58.	26.3	3	113.2	48.1	3	168.5	71.5	3	233.7	94.6
4	3.7	1.6	64	58.9	25.	4	114.1	48.5	4	169.4	71.9	4	234.6	95.3
5	4.6	2.	65	59.8	25.4	5	115.1	48.8	5	170.3	72.3	5	235.5	95.7
6	5.5	2.3	66	60.8	25.8	6	116.	49.2	6	171.2	72.7	6	236.4	96.1
7	6.4	2.7	67	61.7	26.2	7	116.9	49.6	7	172.1	73.1	7	237.4	96.5
8	7.4	3.1	68	62.6	26.6	8	117.8	50.	8	173.1	73.5	8	238.3	96.9
9	8.3	3.5	69	63.5	27.	9	118.7	50.4	9	174.	73.8	9	239.3	97.3
10	9.2	3.9	70	64.4	27.4	130	119.7	50.8	190	174.9	74.2	250	239.1	97.7
11	10.1	4.3	71	65.4	27.7	1	120.6	51.2	1	175.8	74.6	1	241.	98.1
12	11.	4.7	72	66.3	28.1	2	121.5	51.6	2	176.7	75.	2	242.	98.5
13	12.	5.1	73	67.2	28.5	3	122.4	52.	3	177.7	75.4	3	243.	98.9
14	12.9	5.5	74	68.1	28.9	4	123.3	52.4	4	178.6	75.8	4	243.8	99.2
15	13.8	5.9	75	69.	29.3	5	124.2	52.7	5	179.5	76.2	5	244.7	99.6
16	14.7	6.3	76	70.	29.7	6	125.2	53.1	6	180.4	76.6	6	245.6	100.
17	15.6	6.6	77	70.9	30.1	7	126.1	53.5	7	181.3	77.	7	246.6	100.4
18	16.6	7.	78	71.8	30.5	8	127.	53.9	8	182.3	77.4	8	247.5	100.8
19	17.5	7.4	79	72.7	30.9	9	128.	54.3	9	183.2	77.8	9	248.4	101.2
20	18.4	7.8	80	73.6	31.3	140	128.9	54.7	200	184.1	78.1	260	248.3	101.6
21	19.3	8.2	81	74.6	31.6	1	129.8	55.1	1	185.	78.5	1	249.3	102.
22	20.3	8.6	82	75.5	32.	2	130.7	55.5	2	185.9	78.9	2	249.2	102.4
23	21.2	9.	83	76.4	32.4	3	131.6	55.9	3	186.9	79.3	3	249.1	102.8
24	22.1	9.4	84	77.3	32.8	4	132.6	56.3	4	187.8	79.7	4	249.	103.2
25	23.	9.8	85	78.2	33.2	5	133.5	56.7	5	188.7	80.1	5	248.9	103.5
26	23.9	10.2	86	79.2	33.6	6	134.4	57.	6	189.6	80.5	6	248.9	103.9
27	24.9	10.5	87	80.1	34.	7	135.3	57.4	7	190.5	80.9	7	248.8	104.3
28	25.8	10.9	88	81.	34.4	8	136.2	57.8	8	191.5	81.3	8	248.7	104.7
29	26.7	11.3	89	81.9	34.8	9	137.2	58.2	9	192.4	81.7	9	248.6	105.1
30	27.6	11.7	90	82.8	35.2	150	138.1	58.6	210	193.3	82.1	270	248.5	105.5
31	28.5	12.1	91	83.8	35.6	1	139.	59.	1	194.3	82.4	1	249.5	105.9
32	29.5	12.5	92	84.7	35.9	2	139.9	59.4	2	195.1	82.8	2	249.4	106.3
33	30.4	12.9	93	85.6	36.3	3	140.8	59.8	3	196.1	83.2	3	249.3	106.7
34	31.3	13.3	94	86.5	36.7	4	141.8	60.2	4	197.	83.6	4	249.2	107.1
35	32.2	13.7	95	87.4	37.1	5	142.7	60.6	5	197.9	84.	5	249.1	107.5
36	33.1	14.1	96	88.4	37.5	6	143.6	61.	6	198.8	84.4	6	249.1	107.9
37	34.1	14.5	97	89.3	37.9	7	144.5	61.3	7	199.7	84.8	7	249.	108.3
38	35.	14.8	98	90.2	38.3	8	145.4	61.7	8	200.7	85.2	8	248.9	108.6
39	35.9	15.2	99	91.1	38.7	9	146.4	62.1	9	201.6	85.6	9	248.8	109.
40	36.8	15.6	100	92.1	39.1	160	147.3	62.5	220	202.5	86.	280	248.7	109.4
41	37.7	16.	1	93.	39.5	1	148.3	62.9	1	203.4	86.4	1	248.7	109.8
42	38.7	16.4	2	93.9	39.9	2	149.1	63.3	2	204.4	86.7	2	248.6	110.2
43	39.6	16.8	3	94.8	40.2	3	150.	63.7	3	205.3	87.1	3	248.5	110.6
44	40.5	17.2	4	95.7	40.6	4	151.	64.1	4	206.3	87.6	4	248.4	111.
45	41.4	17.6	5	96.7	41.	5	151.9	64.5	5	207.2	87.9	5	248.3	111.4
46	42.3	18.	6	97.6	41.4	6	152.8	64.9	6	208.	88.3	6	248.3	111.7
47	43.3	18.4	7	98.5	41.8	7	153.7	65.3	7	209.	88.7	7	248.2	112.1
48	44.2	18.8	8	99.4	42.2	8	154.6	65.6	8	209.9	89.1	8	248.1	112.5
49	45.1	19.1	9	100.3	42.6	9	155.6	66.	9	210.8	89.5	9	248.	112.9
50	46.	19.5	110	101.3	43.	170	156.5	66.4	230	211.7	89.9	290	248.9	113.3
51	46.9	19.8	1	102.2	43.4	1	157.4	66.8	1	212.6	90.3	1	248.9	113.7
52	47.9	20.3	2	103.1	43.8	2	158.3	67.2	2	213.6	90.6	2	248.8	114.1
53	48.8	20.7	3	104.	44.2	3	159.2	67.6	3	214.5	91.	3	248.7	114.5
54	49.7	21.1	4	104.9	44.5	4	160.9	68.	4	215.4	91.4	4	248.6	114.9
55	50.6	21.5	5	105.9	44.9	5	161.1	68.4	5	216.3	91.8	5	248.5	115.3
56	51.5	21.9	6	106.8	45.3	6	162.	68.8	6	217.2	92.2	6	248.5	115.7
57	52.5	22.3	7	107.7	45.7	7	162.9	69.2	7	218.2	92.6	7	248.4	116.
58	53.4	22.7	8	108.6	46.1	8	163.8	69.6	8	219.1	93.	8	248.3	116.4
59	54.3	23.1	9	109.5	46.5	9	164.8	69.9	9	220.	93.4	9	248.2	116.8
60	55.2	23.4	190	110.5	46.9	180	165.7	70.3	240	220.9	93.8	300	248.1	117.2
dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.

Distance, Departure and Dis. Latitude.

Course 67°.

Course 84°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	55.7	94.8	181	110.5	49.9	181	165.4	73.6	241	220.9	98
2	1.8	0.8	62	56.6	95.9	2	111.5	49.6	2	166.3	74	2	221.1	98.4
3	2.7	1.2	63	57.6	96.6	3	112.4	50.	3	167.3	74.4	3	222.	98.8
4	3.7	1.6	64	58.5	96.	4	113.3	50.4	4	168.1	74.8	4	222.9	99.2
5	4.6	2.	65	59.4	96.4	5	114.2	50.8	5	169.	75.2	5	223.8	99.7
6	5.5	2.4	66	60.3	96.8	6	115.1	51.2	6	169.9	75.7	6	224.7	100.1
7	6.4	2.8	67	61.2	97.3	7	116.	51.7	7	170.8	76.1	7	225.6	100.5
8	7.3	3.3	68	62.1	97.7	8	116.9	52.1	8	171.7	76.5	8	226.6	100.9
9	8.2	3.7	69	63.	98.1	9	117.8	52.5	9	172.7	76.9	9	227.5	101.3
10	9.1	4.1	70	63.9	98.5	130	118.8	52.9	190	173.6	77.3	280	228.4	101.7
11	10.	4.5	71	64.9	98.9	1	119.7	53.3	1	174.5	77.7	1	229.3	102.1
12	11.	4.9	72	65.8	99.2	2	120.6	53.7	2	175.4	78.1	2	230.3	102.5
13	11.9	5.3	73	66.7	99.7	3	121.5	54.1	3	176.3	78.5	3	231.1	102.9
14	12.8	5.7	74	67.6	30.1	4	122.4	54.5	4	177.2	78.9	4	232.	103.3
15	13.7	6.1	75	68.5	30.5	5	123.3	54.9	5	178.1	79.3	5	233.	103.7
16	14.6	6.5	76	69.4	30.9	6	124.2	55.3	6	179.1	79.7	6	234.9	104.1
17	15.5	6.9	77	70.3	31.3	7	125.2	55.7	7	180.	80.1	7	234.8	104.5
18	16.4	7.3	78	71.3	31.7	8	126.1	56.1	8	180.9	80.5	8	235.7	104.9
19	17.4	7.7	79	72.2	32.1	9	127.	56.5	9	181.8	80.9	9	236.6	105.3
20	18.3	8.1	80	73.1	32.5	140	127.9	56.9	200	182.7	81.3	260	237.5	105.7
21	19.2	8.5	81	74.	32.9	1	128.8	57.3	1	183.6	81.8	1	238.4	106.1
22	20.1	8.9	82	74.9	33.4	2	129.7	57.8	2	184.5	82.2	2	239.3	106.5
23	21.	9.4	83	75.8	33.8	3	130.6	58.2	3	185.4	82.6	3	240.3	107.
24	21.9	9.8	84	76.7	34.2	4	131.6	58.6	4	186.4	83.	4	241.2	107.4
25	22.8	10.2	85	77.7	34.6	5	132.5	59.	5	187.3	83.4	5	242.1	107.8
26	23.8	10.6	86	78.6	35.	6	133.4	59.4	6	188.3	83.8	6	243.	108.2
27	24.7	11.	87	79.5	35.4	7	134.3	59.8	7	189.1	84.2	7	243.9	108.6
28	25.6	11.4	88	80.4	35.8	8	135.2	60.2	8	190.	84.6	8	244.8	109.
29	26.5	11.8	89	81.3	36.2	9	136.1	60.6	9	190.9	85.	9	245.7	109.4
30	27.4	12.2	90	82.2	36.6	150	137.	61.	210	191.8	85.4	270	246.7	109.8
31	28.3	12.6	91	83.1	37.	1	137.9	61.4	1	192.8	85.8	1	247.6	110.2
32	29.2	13.	92	84.	37.4	2	138.9	61.8	2	193.7	86.2	2	248.5	110.6
33	30.1	13.4	93	85.	37.8	3	139.8	62.2	3	194.6	86.6	3	249.4	111.
34	31.1	13.8	94	85.9	38.2	4	140.7	62.6	4	195.5	87.	4	250.3	111.4
35	32.	14.2	95	86.8	38.6	5	141.6	63.	5	196.4	87.4	5	251.2	111.8
36	32.9	14.6	96	87.7	39.	6	142.5	63.5	6	197.3	87.9	6	252.1	112.2
37	33.8	15.	97	88.6	39.5	7	143.4	63.9	7	198.2	88.3	7	253.1	112.7
38	34.7	15.5	98	89.5	39.9	8	144.3	64.3	8	199.2	88.7	8	254.	113.1
39	35.6	15.9	99	90.4	40.2	9	145.3	64.7	9	200.1	89.1	9	254.9	113.5
40	36.5	16.3	100	91.4	40.7	160	146.2	65.1	220	201.	89.5	280	255.8	113.9
41	37.5	16.7	1	92.3	41.1	1	147.1	65.5	1	201.9	89.9	1	256.7	114.2
42	38.4	17.1	2	93.2	41.5	2	148.	65.9	2	202.8	90.3	2	257.6	114.7
43	39.3	17.5	3	94.1	41.9	3	148.9	66.3	3	203.7	90.7	3	258.5	115.1
44	40.2	17.9	4	95.1	42.3	4	149.8	66.7	4	204.6	91.1	4	259.4	115.5
45	41.1	18.3	5	96.0	42.7	5	150.7	67.1	5	205.5	91.5	5	260.4	115.9
46	42.	18.7	6	96.8	43.1	6	151.6	67.5	6	206.5	91.9	6	261.3	116.3
47	42.9	19.1	7	97.7	43.5	7	152.6	67.9	7	207.4	92.3	7	262.2	116.7
48	43.9	19.5	8	98.7	43.9	8	153.5	68.3	8	208.3	92.7	8	263.1	117.1
49	44.8	19.9	9	99.6	44.3	9	154.4	68.7	9	209.2	93.1	9	264.	117.5
50	45.7	20.3	110	100.5	44.7	170	155.3	69.1	230	210.1	93.5	290	264.9	118.
51	46.6	20.7	1	101.4	45.1	1	156.2	69.6	1	211.	94.	1	265.8	118.4
52	47.5	21.2	2	102.3	45.6	2	157.1	70.	2	211.9	94.4	2	266.8	118.8
53	48.4	21.6	3	103.2	46.	3	158.	70.4	3	212.9	94.8	3	267.7	119.2
54	49.3	22.	4	104.1	46.4	4	159.	70.8	4	213.8	95.2	4	268.6	119.6
55	50.2	22.4	5	105.1	46.8	5	159.9	71.2	5	214.7	95.6	5	269.5	120.
56	51.2	22.8	6	106.	47.2	6	160.8	71.6	6	215.6	96.	6	270.4	120.4
57	52.1	23.2	7	106.9	47.6	7	161.7	72.	7	216.5	96.4	7	271.3	120.8
58	53.	23.6	8	107.8	48.	8	162.6	72.4	8	217.4	96.8	8	272.2	121.2
59	53.9	24.	9	108.7	48.4	9	163.5	72.8	9	218.3	97.2	9	273.2	121.6
60	54.8	24.4	190	109.6	48.8	180	164.4	73.2	240	219.3	97.6	300	274.1	122.
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 86°.

Course 85°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	55.3	28.8	121	100.7	51.1	181	164.	76.5	241	218.4	101.9
2	1.8	0.8	62	55.3	29.3	2	110.6	51.6	2	164.9	76.9	2	219.3	102.3
3	2.7	1.3	63	57.1	29.6	3	111.5	52.	3	165.9	77.3	3	220.2	102.7
4	3.6	1.7	64	58.	27.	4	112.4	52.4	4	166.8	77.8	4	221.1	103.1
5	4.5	2.1	65	58.9	27.5	5	113.3	52.8	5	167.7	78.2	5	222.	103.5
6	5.4	2.5	66	59.8	27.9	6	114.2	53.2	6	168.6	78.6	6	223.	104.
7	6.3	3.	67	60.7	28.3	7	115.1	53.7	7	169.5	79.	7	223.9	104.4
8	7.3	3.4	68	61.6	28.7	8	116.	54.1	8	170.4	79.5	8	224.8	104.8
9	8.2	3.8	69	62.5	29.2	9	116.9	54.5	9	171.3	79.9	9	225.7	105.2
10	9.1	4.2	70	63.4	29.6	130	117.8	54.9	190	172.2	80.3	250	226.6	105.7
11	10.	4.6	71	64.3	30.	1	118.7	55.4	1	173.1	80.7	1	227.5	106.1
12	10.9	5.1	72	65.3	30.4	2	119.6	55.8	2	174.	81.1	2	228.4	106.5
13	11.8	5.5	73	66.2	30.9	3	120.5	56.2	3	174.9	81.6	3	229.3	106.9
14	12.7	5.9	74	67.1	31.3	4	121.4	56.6	4	175.8	82.	4	230.2	107.3
15	13.6	6.3	75	68.	31.7	5	122.4	57.1	5	176.7	82.4	5	231.1	107.8
16	14.5	6.8	76	68.9	32.1	6	123.3	57.5	6	177.6	82.8	6	232.	108.2
17	15.4	7.2	77	69.8	32.5	7	124.2	57.9	7	178.5	83.3	7	232.9	108.6
18	16.3	7.6	78	70.7	33.	8	125.1	58.3	8	179.4	83.7	8	233.8	109.
19	17.2	8.	79	71.6	33.4	9	126.	58.7	9	180.4	84.1	9	234.7	109.5
20	18.1	8.5	80	72.5	33.8	140	126.9	59.2	200	181.3	84.5	260	235.6	109.9
21	19.	8.9	81	73.4	34.2	1	127.8	59.6	1	182.2	84.9	1	236.5	110.3
22	19.9	9.3	82	74.3	34.7	2	128.7	60.	2	183.1	85.4	2	237.4	110.7
23	20.8	9.7	83	75.2	35.1	3	129.6	60.4	3	184.	85.8	3	238.4	111.1
24	21.8	10.1	84	76.1	35.5	4	130.5	60.9	4	184.9	86.2	4	239.3	111.6
25	22.7	10.6	85	77.	35.9	5	131.4	61.3	5	185.8	86.6	5	240.2	112.
26	23.6	11.	86	77.9	36.3	6	132.3	61.7	6	186.7	87.1	6	241.1	112.4
27	24.5	11.4	87	78.8	36.8	7	133.2	62.1	7	187.6	87.5	7	242.	112.8
28	25.4	11.8	88	79.8	37.2	8	134.1	62.5	8	188.5	87.9	8	242.9	113.3
29	26.3	12.3	89	80.7	37.6	9	135.	63.	9	189.4	88.3	9	243.8	113.7
30	27.2	12.7	90	81.6	38.	150	135.9	63.4	210	190.3	88.7	270	244.7	114.1
31	28.1	13.1	91	82.5	38.5	1	136.9	63.8	1	191.2	89.2	1	245.6	114.5
32	29.	13.5	92	83.4	38.9	2	137.8	64.2	2	192.1	89.6	2	246.5	115.
33	29.9	13.9	93	84.3	39.3	3	138.7	64.7	3	193.	90.	3	247.4	115.4
34	30.8	14.4	94	85.2	39.7	4	139.6	65.1	4	193.9	90.4	4	248.3	115.8
35	31.7	14.8	95	86.1	40.1	5	140.5	65.5	5	194.9	90.9	5	249.2	116.2
36	32.6	15.2	96	87.	40.6	6	141.4	65.9	6	195.8	91.3	6	250.1	116.6
37	33.5	15.6	97	87.9	41.	7	142.3	66.4	7	196.7	91.7	7	251.	117.1
38	34.4	16.1	98	88.8	41.4	8	143.2	66.8	8	197.6	92.1	8	252.	117.5
39	35.3	16.5	99	89.7	41.8	9	144.1	67.2	9	198.5	92.6	9	252.9	117.9
40	36.3	16.9	100	90.6	42.3	160	145.	67.6	220	199.4	93.	280	253.8	118.3
41	37.2	17.3	1	91.5	42.7	1	145.9	68.	1	200.3	93.4	1	254.7	118.8
42	38.1	17.7	2	92.4	43.1	2	146.8	68.5	2	201.2	93.8	2	255.6	119.2
43	39.	18.2	3	93.3	43.5	3	147.7	68.9	3	202.1	94.2	3	256.5	119.6
44	39.9	18.6	4	94.3	44.	4	148.6	69.3	4	203.	94.7	4	257.4	120.
45	40.8	19.	5	95.2	44.4	5	149.5	69.7	5	203.9	95.1	5	258.3	120.4
46	41.7	19.4	6	96.1	44.8	6	150.4	70.2	6	204.8	95.6	6	259.2	120.9
47	42.6	19.9	7	97.	45.2	7	151.4	70.6	7	205.7	95.9	7	260.1	121.3
48	43.5	20.3	8	97.9	45.6	8	152.3	71.	8	206.6	96.4	8	261.	121.7
49	44.4	20.7	9	98.8	46.1	9	153.2	71.4	9	207.5	96.8	9	261.9	122.1
50	45.3	21.1	110	99.7	46.5	170	154.1	71.8	230	208.5	97.2	290	262.8	122.6
51	46.2	21.6	1	100.6	46.9	1	155.	72.3	1	209.4	97.6	1	263.7	123.
52	47.1	22.	2	101.5	47.3	2	155.9	72.7	2	210.3	98.	2	264.6	123.4
53	48.	22.4	3	102.4	47.8	3	156.8	73.1	3	211.2	98.5	3	265.5	123.8
54	48.9	22.8	4	103.3	48.2	4	157.7	73.5	4	212.1	98.9	4	266.4	124.2
55	49.8	23.2	5	104.2	48.6	5	158.6	74.	5	213.	99.3	5	267.4	124.7
56	50.8	23.7	6	105.1	49.	6	159.5	74.4	6	213.9	99.7	6	268.3	125.1
57	51.7	24.1	7	106.	49.4	7	160.4	74.8	7	214.8	100.2	7	269.2	125.5
58	52.6	24.5	8	106.9	49.9	8	161.3	75.2	8	215.7	100.6	8	270.1	125.9
59	53.5	24.9	9	107.9	50.3	9	162.2	75.6	9	216.6	101.	9	271.	126.4
60	54.4	25.4	190	108.8	50.7	180	163.1	76.1	240	217.5	101.4	300	271.9	126.8
dist.	dep.	d.lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 65°.

Course 360.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.4	61	54.8	26.7	131	106.8	53.	181	169.7	79.3	241	216.6	105.6
2	1.8	0.9	62	55.7	27.2	2	109.7	53.5	2	163.6	79.8	3	217.5	106.1
3	2.7	1.3	63	56.6	27.6	3	110.6	53.9	3	164.5	80.2	3	218.4	106.5
4	3.6	1.8	64	57.5	28.1	4	111.5	54.4	4	165.4	80.7	4	219.3	107.
5	4.5	2.2	65	58.4	28.5	5	112.3	54.8	5	166.3	81.1	5	220.9	107.4
6	5.4	2.6	66	59.3	28.9	6	113.2	55.2	6	167.2	81.5	6	221.1	107.8
7	6.3	3.1	67	60.2	29.4	7	114.1	55.7	7	168.1	82.	7	222	108.3
8	7.2	3.5	68	61.1	29.8	8	115.	56.1	8	169.	82.4	8	222.9	108.7
9	8.1	3.9	69	62.	30.2	9	115.9	56.5	9	169.9	82.9	9	223.8	109.2
10	9.	4.4	70	62.9	30.7	120	116.8	57.	190	170.8	83.3	250	224.7	109.6
11	9.9	4.8	71	63.9	31.1	1	117.7	57.4	1	171.7	83.7	1	225.6	110.
12	10.8	5.3	72	64.7	31.6	2	118.6	57.9	2	172.6	84.2	2	226.5	110.5
13	11.7	5.7	73	65.6	32.	3	119.5	58.3	3	173.5	84.6	3	227.4	110.9
14	12.6	6.1	74	66.5	32.4	4	120.4	58.7	4	174.4	85.	4	228.3	111.3
15	13.5	6.6	75	67.4	32.9	5	121.3	59.2	5	175.3	85.5	5	229.2	111.8
16	14.4	7.	76	68.3	33.3	6	122.2	59.6	6	176.2	85.9	6	230.1	112.2
17	15.3	7.5	77	69.2	33.8	7	123.1	60.1	7	177.1	86.4	7	231.	112.7
18	16.2	7.9	78	70.1	34.2	8	124.	60.5	8	178.	86.8	8	231.9	113.1
19	17.1	8.3	79	71.	34.6	9	124.9	60.9	9	178.9	87.2	9	232.8	113.5
20	18.	8.8	80	71.9	35.1	140	125.8	61.4	200	179.8	87.7	260	233.7	114.
21	18.9	9.2	81	72.8	35.5	1	126.7	61.8	1	180.7	88.1	1	234.6	114.4
22	19.8	9.6	82	73.7	35.9	2	127.6	62.2	2	181.6	88.6	2	235.5	114.9
23	20.7	10.1	83	74.6	36.4	3	128.5	62.7	3	182.5	89.	3	236.4	115.3
24	21.6	10.5	84	75.5	36.8	4	129.4	63.1	4	183.4	89.4	4	237.3	115.7
25	22.5	11.	85	76.4	37.3	5	130.3	63.6	5	184.3	89.9	5	238.2	116.2
26	23.4	11.4	86	77.3	37.7	6	131.2	64.	6	185.2	90.3	6	239.1	116.6
27	24.3	11.8	87	78.2	38.1	7	132.1	64.4	7	186.1	90.7	7	240.	117.
28	25.2	12.2	88	79.1	38.6	8	133.	64.9	8	187.0	91.2	8	240.9	117.5
29	26.1	12.7	89	80.	39.	9	133.9	65.3	9	187.8	91.6	9	241.8	117.9
30	27.	13.2	90	80.9	39.5	150	134.8	65.8	210	188.7	92.1	270	242.7	118.4
31	27.9	13.6	91	81.8	39.9	1	135.7	66.2	1	189.6	92.5	1	243.6	118.8
32	28.8	14.	92	82.7	40.3	2	136.6	66.6	2	190.5	92.9	2	244.5	119.2
33	29.7	14.5	93	83.6	40.8	3	137.5	67.1	3	191.4	93.4	3	245.4	119.7
34	30.6	14.9	94	84.5	41.2	4	138.4	67.5	4	192.3	93.8	4	246.3	120.1
35	31.5	15.3	95	85.4	41.6	5	139.3	67.9	5	193.2	94.2	5	247.2	120.6
36	32.4	15.8	96	86.3	42.1	6	140.2	68.4	6	194.1	94.7	6	248.1	121.
37	33.3	16.2	97	87.2	42.5	7	141.1	68.8	7	195.	95.1	7	249.	121.4
38	34.2	16.7	98	88.1	43.	8	142.	69.3	8	195.9	95.6	8	249.9	121.9
39	35.1	17.1	99	89.	43.4	9	142.9	69.7	9	196.8	96.	9	250.8	122.3
40	36.	17.5	100	89.9	43.8	160	143.8	70.1	220	197.7	96.4	280	251.7	122.7
41	36.9	18.	1	90.8	44.3	1	144.7	70.6	1	198.6	96.9	1	252.6	123.2
42	37.7	18.4	2	91.7	44.7	2	145.6	71.	2	199.5	97.3	2	253.5	123.6
43	38.6	18.8	3	92.6	45.2	3	146.5	71.5	3	200.4	97.8	3	254.4	124.1
44	39.5	19.3	4	93.5	45.6	4	147.4	71.9	4	201.3	98.2	4	255.3	124.5
45	40.4	19.7	5	94.4	46.	5	148.3	72.3	5	202.2	98.6	5	256.2	124.9
46	41.3	20.2	6	95.3	46.5	6	149.2	72.8	6	203.1	99.1	6	257.1	125.4
47	42.2	20.6	7	96.2	46.9	7	150.1	73.2	7	204.	99.5	7	258.	125.8
48	43.1	21.	8	97.1	47.3	8	151.	73.6	8	204.9	99.9	8	258.9	126.3
49	44.	21.5	9	98.	47.8	9	151.9	74.1	9	205.8	100.4	9	259.8	126.7
50	44.9	21.9	110	98.9	48.2	170	152.8	74.5	230	206.7	100.8	290	260.7	127.1
51	45.8	22.4	1	99.8	48.7	1	153.7	75.	1	207.6	101.3	1	261.5	127.6
52	46.7	22.8	2	100.7	49.1	2	154.6	75.4	2	208.5	101.7	2	262.4	128.
53	47.6	23.2	3	101.6	49.5	3	155.5	75.8	3	209.4	102.1	3	263.3	128.4
54	48.5	23.7	4	102.5	50.	4	156.4	76.3	4	210.3	102.6	4	264.2	128.9
55	49.4	24.1	5	103.4	50.4	5	157.3	76.7	5	211.2	103.	5	265.1	129.3
56	50.3	24.5	6	104.3	50.9	6	158.2	77.2	6	212.1	103.5	6	266.	129.8
57	51.2	25.	7	105.2	51.3	7	159.1	77.6	7	213.	103.9	7	266.9	130.2
58	52.1	25.4	8	106.1	51.7	8	160.	78.	8	213.9	104.3	8	267.8	130.6
59	53.	25.9	9	107.	52.2	9	160.9	78.5	9	214.8	104.8	9	268.7	131.1
60	53.9	26.3	190	107.9	52.6	180	161.8	78.9	240	215.7	105.2	300	269.6	131.5
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 64°.

TABLE V.

137

Course 37°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.5	61	54.4	37.7	121	107.8	54.9	181	161.3	82.9	241	314.7	109.4
2	1.8	0.9	62	53.9	38.1	2	108.7	55.4	2	162.9	82.6	2	315.6	109.9
3	2.7	1.4	63	56.1	38.6	3	109.6	55.8	3	163.1	83.1	3	316.5	110.3
4	3.6	1.8	64	57.	39.1	4	110.5	56.3	4	163.9	83.5	4	317.4	110.8
5	4.5	2.3	65	57.9	39.5	5	111.4	56.7	5	164.8	84.	5	318.3	111.9
6	5.3	2.7	66	58.8	39.	6	112.3	57.2	6	165.7	84.6	6	319.2	111.7
7	6.2	3.2	67	59.7	39.4	7	113.2	57.7	7	166.6	84.9	7	320.1	112.1
8	7.1	3.6	68	60.6	39.9	8	114.	58.1	8	167.5	85.4	8	321.	112.6
9	8.	4.1	69	61.5	31.3	9	114.9	58.6	9	168.4	85.8	9	321.9	113.
10	8.9	4.5	70	62.4	31.8	130	115.8	59.	190	169.3	86.3	250	322.8	113.5
11	9.8	5.	71	63.3	32.2	1	116.7	59.5	1	170.9	86.7	1	323.6	114.
12	10.7	5.4	72	64.2	32.7	2	117.6	59.9	2	171.1	87.2	2	324.5	114.4
13	11.6	5.9	73	65.	33.1	3	118.5	60.4	3	172.	87.6	3	325.4	114.9
14	12.5	6.4	74	65.9	33.6	4	119.4	60.8	4	172.9	88.1	4	326.3	115.3
15	13.4	6.8	75	66.8	34.	5	120.3	61.3	5	173.7	88.5	5	327.2	115.8
16	14.3	7.3	76	67.7	34.5	6	121.2	61.7	6	174.6	89.	6	328.1	116.9
17	15.1	7.7	77	68.6	35.	7	122.1	62.2	7	175.5	89.4	7	329.	117.1
18	16.	8.2	78	69.5	35.4	8	123.	62.7	8	176.4	89.8	8	329.9	117.7
19	16.9	8.6	79	70.4	35.9	9	123.8	63.1	9	177.3	90.2	9	330.8	117.6
20	17.8	9.1	80	71.3	36.3	140	124.7	63.6	200	178.2	90.8	260	331.7	118.
21	18.7	9.5	81	72.2	36.8	1	125.6	64.	1	179.1	91.3	1	332.6	118.5
22	19.6	10.	82	73.1	37.2	2	126.5	64.5	2	180.	91.7	2	333.4	119.
23	20.5	10.4	83	74.	37.7	3	127.4	64.9	3	180.9	92.2	3	334.3	119.4
24	21.4	10.9	84	74.8	38.1	4	128.3	65.4	4	181.8	92.6	4	335.2	119.9
25	22.3	11.3	85	75.7	38.6	5	129.2	65.8	5	182.7	93.1	5	336.1	120.3
26	23.2	11.8	86	76.6	39.	6	130.1	66.3	6	183.5	93.5	6	337.	120.8
27	24.1	12.3	87	77.5	39.5	7	131.	66.7	7	184.4	94.	7	337.9	121.2
28	24.9	12.7	88	78.4	40.	8	131.9	67.2	8	185.3	94.4	8	338.8	121.7
29	25.8	13.2	89	79.3	40.4	9	132.8	67.6	9	186.2	94.9	9	339.7	122.1
30	26.7	13.6	90	80.2	40.9	150	133.7	68.1	210	187.1	95.3	270	340.6	122.6
31	27.6	14.1	91	81.1	41.3	1	134.5	68.6	1	188.	95.8	1	341.5	123.
32	28.5	14.5	92	82.	41.8	2	135.4	69.	2	188.9	96.2	2	342.4	123.5
33	29.4	15.	93	82.9	42.3	3	136.3	69.5	3	189.8	96.7	3	343.3	123.9
34	30.3	15.4	94	83.8	42.7	4	137.2	69.9	4	190.7	97.2	4	344.1	124.4
35	31.2	15.9	95	84.6	43.1	5	138.1	70.4	5	191.6	97.6	5	345.	124.8
36	32.1	16.3	96	85.5	43.6	6	139.	70.8	6	192.5	98.1	6	345.9	125.3
37	33.	16.8	97	86.4	44.	7	139.9	71.3	7	193.3	98.5	7	346.8	125.8
38	33.9	17.3	98	87.3	44.5	8	140.8	71.7	8	194.2	99.	8	347.7	126.2
39	34.7	17.7	99	88.2	44.9	9	141.7	72.2	9	195.1	99.4	9	348.6	126.9
40	35.6	18.2	100	89.1	45.4	160	142.6	72.6	220	196.	99.9	280	349.5	127.1
41	36.5	18.6	1	90.	45.9	1	143.5	73.1	1	196.9	100.3	1	350.4	127.6
42	37.4	19.1	2	90.9	46.3	2	144.3	73.5	2	197.8	100.8	2	351.3	128.
43	38.3	19.5	3	91.8	46.8	3	145.2	74.	3	198.7	101.2	3	352.2	128.5
44	39.2	20.	4	92.7	47.2	4	146.1	74.5	4	199.6	101.7	4	353.	129.9
45	40.1	20.4	5	93.6	47.7	5	147.	74.9	5	200.5	102.1	5	353.9	129.4
46	41.	20.9	6	94.4	48.1	6	147.9	75.4	6	201.4	102.6	6	354.8	129.8
47	41.9	21.3	7	95.3	48.6	7	148.8	75.8	7	202.3	103.1	7	355.7	130.3
48	42.8	21.8	8	96.2	49.	8	149.7	76.3	8	203.1	103.5	8	356.6	130.7
49	43.7	22.2	9	97.1	49.5	9	150.6	76.7	9	204.	104.	9	357.5	131.2
50	44.6	22.7	110	98.	49.9	170	151.5	77.2	230	204.9	104.4	290	358.4	131.7
51	45.4	23.2	1	98.9	50.4	1	152.4	77.6	1	205.8	104.9	1	359.3	132.1
52	46.3	23.6	2	99.8	50.8	2	153.3	78.1	2	206.7	105.3	2	360.2	132.6
53	47.2	24.1	3	100.7	51.3	3	154.1	78.5	3	207.6	105.8	3	361.1	133.
54	48.1	24.5	4	101.6	51.8	4	155.	79.	4	208.5	106.2	4	362.	133.5
55	49.	25.	5	102.5	52.2	5	155.9	79.4	5	209.4	106.7	5	362.8	133.9
56	49.9	25.4	6	103.4	52.7	6	156.8	79.9	6	210.3	107.1	6	363.7	134.4
57	50.8	25.9	7	104.3	53.1	7	157.7	80.4	7	211.2	107.6	7	364.6	134.8
58	51.7	26.3	8	105.1	53.6	8	158.6	80.8	8	212.1	108.	8	365.5	135.3
59	52.6	26.8	9	106.	54.	9	159.5	81.3	9	213.	108.5	9	366.4	135.7
60	53.5	27.2	120	106.9	54.5	180	160.4	81.7	240	213.8	109.	300	367.3	136.3
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 63°.

8

Course 30°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.5	61	52.9	32.6	121	106.8	56.8	181	159.8	85.	241	212.8	112.1
2	1.8	0.9	62	54.7	33.1	2	107.7	57.3	2	160.7	85.4	2	213.7	112.6
3	2.6	1.4	63	55.8	33.6	3	108.6	57.7	3	161.6	85.9	3	214.6	113.1
4	3.5	1.9	64	56.5	34.	4	109.5	58.2	4	162.5	86.4	4	215.4	113.6
5	4.4	2.3	65	57.4	34.5	5	110.4	58.7	5	163.3	86.9	5	216.3	114.
6	5.3	2.8	66	58.3	35.	6	111.3	59.2	6	164.2	87.3	6	217.3	114.5
7	6.2	3.3	67	59.2	35.5	7	112.1	59.6	7	165.1	87.8	7	218.1	115.
8	7.1	3.8	68	60.	35.9	8	113.	60.1	8	166.	88.3	8	219.	115.4
9	7.9	4.3	69	60.9	36.4	9	113.9	60.6	9	166.9	88.7	9	219.9	115.9
10	8.8	4.7	70	61.8	36.9	120	114.8	61.	190	167.8	89.2	250	220.7	117.0
11	9.7	5.2	71	62.7	37.3	1	115.7	61.5	1	168.6	89.7	1	221.6	117.5
12	10.6	5.6	72	63.6	37.8	2	116.5	62.	2	169.5	90.1	2	222.5	118.0
13	11.5	6.1	73	64.5	38.3	3	117.4	62.4	3	170.4	90.6	3	223.4	118.5
14	12.4	6.6	74	65.3	38.7	4	118.3	62.9	4	171.3	91.1	4	224.3	119.0
15	13.3	7.	75	66.2	39.2	5	119.2	63.4	5	172.2	91.5	5	225.2	119.7
16	14.1	7.5	76	67.1	39.7	6	120.1	63.8	6	173.1	92.	6	226.	120.2
17	15.	8.	77	68.	40.1	7	121.	64.3	7	174.0	92.5	7	226.9	120.7
18	15.9	8.5	78	68.9	40.6	8	121.8	64.8	8	174.8	93.	8	227.8	121.1
19	16.8	8.9	79	69.8	41.1	9	122.7	65.3	9	175.7	93.4	9	228.7	121.6
20	17.7	9.4	80	70.6	41.5	140	123.6	65.7	200	176.6	93.9	260	229.6	122.1
21	18.5	9.9	81	71.5	42.	1	124.5	66.2	1	177.5	94.4	1	230.4	122.6
22	19.4	10.3	82	72.4	42.5	2	125.4	66.7	2	178.4	94.8	2	231.3	123.
23	20.3	10.8	83	73.3	43.	3	126.3	67.1	3	179.2	95.3	3	232.2	123.5
24	21.2	11.3	84	74.2	43.4	4	127.1	67.6	4	180.1	95.8	4	233.1	124.0
25	22.1	11.7	85	75.1	43.9	5	128.	68.1	5	181.	96.2	5	234.	124.4
26	23.	12.2	86	75.9	44.4	6	128.9	68.5	6	181.9	96.7	6	234.9	124.9
27	23.8	12.7	87	76.8	44.8	7	129.8	69.	7	182.8	97.2	7	235.7	125.3
28	24.7	13.1	88	77.7	45.3	8	130.7	69.5	8	183.7	97.7	8	236.6	125.8
29	25.6	13.6	89	78.6	45.8	9	131.6	70.	9	184.5	98.1	9	237.5	126.3
30	26.5	14.1	90	79.5	46.3	150	132.4	70.4	210	185.4	98.6	270	238.4	126.8
31	27.4	14.6	91	80.3	46.7	1	133.3	70.9	1	186.3	99.1	1	239.3	127.3
32	28.3	15.	92	81.2	47.2	2	134.2	71.4	2	187.2	99.5	2	240.2	127.7
33	29.1	15.5	93	82.1	47.7	3	135.1	71.8	3	188.1	100.	3	241.	128.2
34	30.	16.	94	83.	48.1	4	136.	72.3	4	189.	100.5	4	241.9	128.6
35	30.9	16.4	95	83.9	48.6	5	136.9	72.8	5	189.8	100.9	5	242.8	129.1
36	31.8	16.9	96	84.8	49.1	6	137.7	73.2	6	190.7	101.4	6	243.7	129.6
37	32.7	17.4	97	85.6	49.5	7	138.6	73.7	7	191.6	101.9	7	244.6	130.
38	33.6	17.8	98	86.5	49.9	8	139.5	74.2	8	192.5	102.3	8	245.5	130.5
39	34.4	18.3	99	87.4	50.4	9	140.4	74.6	9	193.4	102.8	9	246.3	131.
40	35.3	18.8	100	88.3	50.9	160	141.3	75.1	220	194.2	103.3	280	247.2	131.5
41	36.2	19.3	1	89.2	51.4	1	142.2	75.6	1	195.1	103.8	1	248.1	132.0
42	37.1	19.7	2	90.1	51.9	2	143.	76.1	2	196.	104.3	2	249.	132.4
43	38.	20.2	3	90.9	52.4	3	143.9	76.5	3	196.9	104.7	3	249.9	132.9
44	38.8	20.7	4	91.8	52.8	4	144.8	77.	4	197.8	105.2	4	250.8	133.3
45	39.7	21.1	5	92.7	53.3	5	145.7	77.5	5	198.7	105.6	5	251.6	133.8
46	40.6	21.6	6	93.6	53.8	6	146.6	77.9	6	199.5	106.1	6	252.5	134.2
47	41.5	22.1	7	94.5	54.3	7	147.5	78.4	7	200.4	106.6	7	253.4	134.7
48	42.4	22.5	8	95.4	54.8	8	148.3	78.9	8	201.3	107.	8	254.3	135.2
49	43.3	23.	9	96.2	55.3	9	149.2	79.3	9	202.2	107.5	9	255.2	135.7
50	44.1	23.5	110	97.1	55.8	170	150.1	79.8	230	203.1	108.	290	256.1	136.1
51	45.	24.0	1	98.	56.3	1	151.	80.3	1	204.	108.4	1	256.9	136.6
52	45.9	24.4	2	98.9	56.8	2	151.9	80.7	2	204.8	108.9	2	257.8	137.1
53	46.8	24.9	3	99.8	57.3	3	152.7	81.2	3	205.7	109.3	3	258.7	137.6
54	47.7	25.4	4	100.7	57.8	4	153.6	81.7	4	206.6	109.8	4	259.6	138.
55	48.6	25.8	5	101.5	58.3	5	154.5	82.2	5	207.5	110.3	5	260.5	138.5
56	49.4	26.3	6	102.4	58.8	6	155.4	82.6	6	208.4	110.8	6	261.4	139.
57	50.3	26.8	7	103.3	59.3	7	156.3	83.1	7	209.3	111.3	7	262.3	139.4
58	51.2	27.3	8	104.2	59.8	8	157.2	83.6	8	210.1	111.7	8	263.1	139.9
59	52.1	27.7	9	105.1	60.3	9	158.	84.	9	211.	112.2	9	264.	140.4
60	53.	28.2	120	106.	60.8	180	158.9	84.5	240	211.9	112.7	300	264.9	140.8

Distance, Departure and Diff. Latitude.

Course 60°.

Course 30°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.5	61	53.4	29.6	121	105.8	58.7	181	158.3	87.6	241	210.8	118.8
2	1.7	1.	62	54.9	30.1	2	106.7	59.1	2	159.9	88.9	2	211.7	117.3
3	2.6	1.5	63	55.1	30.5	3	107.6	59.6	3	160.1	89.7	3	212.5	117.8
4	3.5	1.9	64	58.	31.	4	108.5	60.1	4	160.9	89.9	4	213.4	118.3
5	4.4	2.4	65	58.9	31.5	5	109.3	60.6	5	161.8	89.7	5	214.3	118.8
6	5.3	2.9	66	57.7	32.	6	110.2	61.1	6	162.7	90.3	6	215.3	119.3
7	6.1	3.4	67	56.6	32.5	7	111.1	61.6	7	163.6	90.7	7	216.	119.7
8	7.	3.9	68	59.5	33.	8	112.	62.1	8	164.4	91.1	8	216.9	120.2
9	7.9	4.4	69	60.3	33.5	9	112.8	62.5	9	165.3	91.6	9	217.8	120.7
10	8.7	4.8	70	61.2	33.9	130	113.7	63.	190	166.2	92.1	250	218.7	121.2
11	9.6	5.3	71	62.1	34.4	1	114.6	63.5	1	167.1	92.6	1	219.5	121.7
12	10.5	5.8	72	63.	34.9	2	115.4	64.	2	167.9	93.1	2	220.4	122.2
13	11.4	6.3	73	63.8	35.4	3	116.3	64.5	3	168.8	93.6	3	221.3	122.7
14	12.2	6.8	74	64.7	35.9	4	117.2	65.	4	169.7	94.1	4	222.2	123.2
15	13.1	7.3	75	65.6	36.4	5	118.1	65.4	5	170.6	94.5	5	223.	123.6
16	14.	7.8	76	66.5	36.8	6	118.9	65.9	6	171.4	95.	6	223.9	124.1
17	14.9	8.2	77	67.3	37.3	7	119.8	66.4	7	172.3	95.5	7	224.8	124.6
18	15.7	8.7	78	68.2	37.8	8	120.7	66.9	8	173.2	96.	8	225.7	125.1
19	16.6	9.2	79	69.1	38.3	9	121.6	67.4	9	174.	96.5	9	226.5	125.6
20	17.5	9.7	80	70.	38.8	140	122.4	67.9	200	174.9	97.	300	227.4	126.1
21	18.4	10.2	81	70.8	39.3	1	123.3	68.4	1	175.8	97.4	1	228.3	126.6
22	19.2	10.7	82	71.7	39.8	2	124.2	68.8	2	176.7	97.9	2	229.2	127.1
23	20.1	11.2	83	72.6	40.2	3	125.1	69.3	3	177.5	98.4	3	230.	127.6
24	21.	11.6	84	73.5	40.7	4	125.9	69.8	4	178.4	98.9	4	230.9	128.1
25	21.9	12.1	85	74.3	41.2	5	126.8	70.3	5	179.3	99.4	5	231.8	128.6
26	22.7	12.6	86	75.2	41.7	6	127.7	70.8	6	180.2	99.9	6	232.6	129.1
27	23.6	13.1	87	76.1	42.2	7	128.6	71.3	7	181.	100.4	7	233.5	129.6
28	24.5	13.6	88	77.	42.7	8	129.4	71.8	8	181.9	100.8	8	234.4	130.1
29	25.4	14.1	89	77.8	43.1	9	130.3	72.3	9	182.8	101.3	9	235.3	130.6
30	26.3	14.5	90	78.7	43.6	150	131.2	72.7	210	183.7	101.8	270	236.1	131.0
31	27.1	15.	91	79.6	44.1	1	132.1	73.2	1	184.5	102.3	1	237.	131.4
32	28.	15.5	92	80.5	44.6	2	133.0	73.7	2	185.4	102.8	2	237.9	131.9
33	28.9	16.	93	81.3	45.1	3	133.8	74.2	3	186.3	103.3	3	238.8	132.4
34	29.7	16.5	94	82.2	45.6	4	134.7	74.7	4	187.3	103.7	4	239.6	132.8
35	30.6	17.	95	83.1	46.1	5	135.6	75.1	5	188.	104.2	5	240.5	133.3
36	31.5	17.5	96	84.	46.5	6	136.4	75.6	6	188.9	104.7	6	241.4	133.8
37	32.4	17.9	97	84.8	47.	7	137.3	76.1	7	189.8	105.2	7	242.3	134.3
38	33.2	18.4	98	85.7	47.5	8	138.2	76.6	8	190.7	105.7	8	243.1	134.8
39	34.1	18.9	99	86.6	48.	9	139.1	77.1	9	191.5	106.2	9	244.	135.3
40	35.	19.4	100	87.5	48.5	160	139.9	77.6	260	192.4	106.7	260	244.9	135.7
41	35.9	19.9	1	88.3	49.	1	140.8	78.1	1	193.3	107.1	1	245.8	136.2
42	36.7	20.4	2	89.2	49.5	2	141.7	78.5	2	194.3	107.6	2	246.6	136.7
43	37.6	20.8	3	90.1	49.9	3	142.6	79.	3	195.	108.1	3	247.5	137.2
44	38.5	21.3	4	91.	50.4	4	143.4	79.5	4	195.9	108.6	4	248.4	137.7
45	39.4	21.8	5	91.8	50.9	5	144.3	80.	5	196.8	109.1	5	249.3	138.2
46	40.2	22.3	6	92.7	51.4	6	145.2	80.5	6	197.7	109.6	6	250.1	138.7
47	41.1	22.8	7	93.6	51.9	7	146.1	81.	7	198.5	110.1	7	251.	139.1
48	42.	23.3	8	94.5	52.4	8	146.9	81.4	8	199.4	110.5	8	251.9	139.6
49	42.9	23.8	9	95.3	52.8	9	147.8	81.9	9	200.3	111.	9	252.8	140.1
50	43.7	24.2	110	96.2	53.3	170	148.7	82.4	230	201.2	111.5	290	253.6	140.6
51	44.6	24.7	1	97.1	53.8	1	149.6	82.9	1	202.	112.	1	254.5	141.1
52	45.5	25.2	2	98.	54.3	2	150.4	83.4	2	202.9	112.5	2	255.4	141.6
53	46.4	25.7	3	98.8	54.8	3	151.3	83.9	3	203.8	113.	3	256.3	142.
54	47.3	26.2	4	99.7	55.3	4	152.2	84.4	4	204.7	113.4	4	257.1	142.5
55	48.1	26.7	5	100.6	55.8	5	153.1	84.8	5	205.5	113.9	5	258.	143.
56	48.9	27.1	6	101.5	56.2	6	153.9	85.3	6	206.4	114.4	6	258.9	143.5
57	49.7	27.6	7	102.3	56.7	7	154.8	85.8	7	207.3	114.9	7	259.8	144.
58	50.7	28.1	8	103.2	57.2	8	155.7	86.3	8	208.2	115.4	8	260.6	144.5
59	51.6	28.6	9	104.1	57.7	9	156.6	86.8	9	209.	115.9	9	261.5	145.
60	52.5	29.1	190	105.	58.2	180	157.4	87.3	240	209.9	116.4	300	262.4	145.4
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 61°.

Course 30°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.5	61	53.8	30.5	121	104.8	60.5	181	156.8	90.5	241	208.7	120.5
2	1.7	1.1	62	53.7	31.	2	105.7	61.	2	157.6	91.	2	209.6	121.
3	2.6	1.5	63	54.6	31.5	3	106.5	61.5	3	158.5	91.5	3	210.4	121.5
4	3.5	2.	64	55.4	32.	4	107.4	62.	4	159.3	92.	4	211.3	122.
5	4.3	2.5	65	56.3	32.5	5	108.3	62.5	5	160.2	92.5	5	212.2	122.5
6	5.2	3.	66	57.2	33.	6	109.1	63.	6	161.1	93.	6	213.	123.
7	6.1	3.5	67	58.	33.5	7	110.	63.5	7	161.9	93.5	7	213.9	123.5
8	6.9	4.	68	58.9	34.	8	110.9	64.	8	162.8	94.	8	214.8	124.
9	7.8	4.5	69	59.8	34.5	9	111.7	64.5	9	163.7	94.5	9	215.6	124.5
10	8.7	5.	70	60.6	35.	130	112.6	65.	190	164.5	95.	250	216.5	125.
11	9.5	5.5	71	61.5	35.5	1	113.4	65.5	1	165.4	95.5	1	217.4	125.5
12	10.4	6.	72	62.4	36.	2	114.3	66.	2	166.3	96.	2	218.3	126.
13	11.3	6.5	73	63.3	36.5	3	115.2	66.5	3	167.1	96.5	3	219.1	126.5
14	12.1	7.	74	64.1	37.	4	116.	67.	4	168.	97.	4	220.	127.
15	13.	7.5	75	65.	37.5	5	116.9	67.5	5	168.9	97.5	5	220.8	127.5
16	13.9	8.	76	65.8	38.	6	117.8	68.	6	169.7	98.	6	221.7	128.
17	14.7	8.5	77	66.7	38.5	7	118.6	68.5	7	170.6	98.5	7	222.6	128.5
18	15.6	9.	78	67.5	39.	8	119.5	69.	8	171.5	99.	8	223.4	129.
19	16.5	9.5	79	68.4	39.5	9	120.4	69.5	9	172.3	99.5	9	224.3	129.5
20	17.3	10.	80	69.3	40.	140	121.2	70.	200	173.2	100.	260	225.2	130.
21	18.2	10.5	81	70.1	40.5	1	122.1	70.5	1	174.1	100.5	1	226.	130.5
22	19.1	11.	82	71.	41.	2	123.	71.	2	174.9	101.	2	226.9	131.
23	19.9	11.5	83	71.9	41.5	3	123.8	71.5	3	175.8	101.5	3	227.8	131.5
24	20.8	12.	84	72.7	42.	4	124.7	72.	4	176.7	102.	4	228.6	132.
25	21.7	12.5	85	73.6	42.5	5	125.6	72.5	5	177.5	102.5	5	229.5	132.5
26	22.5	13.	86	74.5	43.	6	126.4	73.	6	178.4	103.	6	230.4	133.
27	23.4	13.5	87	75.3	43.5	7	127.3	73.5	7	179.3	103.5	7	231.3	133.5
28	24.2	14.	88	76.2	44.	8	128.2	74.	8	180.1	104.	8	232.1	134.
29	25.1	14.5	89	77.1	44.5	9	129.	74.5	9	181.	104.5	9	233.	134.5
30	26.	15.	90	77.9	45.	150	129.9	75.	210	181.9	105.	270	233.8	135.
31	26.8	15.5	91	78.8	45.5	1	130.8	75.5	1	182.7	105.5	1	234.7	135.5
32	27.7	16.	92	79.7	46.	2	131.6	76.	2	183.6	106.	2	235.6	136.
33	28.6	16.5	93	80.5	46.5	3	132.5	76.5	3	184.5	106.5	3	236.4	136.5
34	29.4	17.	94	81.4	47.	4	133.4	77.	4	185.3	107.	4	237.3	137.
35	30.3	17.5	95	82.3	47.5	5	134.2	77.5	5	186.2	107.5	5	238.2	137.5
36	31.2	18.	96	83.1	48.	6	135.1	78.	6	187.1	108.	6	239.	138.
37	32.	18.5	97	84.	48.5	7	136	78.5	7	187.9	108.5	7	239.9	138.5
38	32.9	19.	98	84.9	49.	8	136.8	79.	8	188.8	109.	8	240.8	139.
39	33.8	19.5	99	85.7	49.5	9	137.7	79.5	9	189.7	109.5	9	241.6	139.5
40	34.6	20.	100	86.6	50.	160	138.6	80.	220	190.5	110.	280	242.5	140.
41	35.5	20.5	1	87.5	50.5	1	139.4	80.5	1	191.4	110.5	1	243.4	140.5
42	36.4	21.	2	88.3	51.	2	140.3	81.	2	192.3	111.	2	244.2	141.
43	37.3	21.5	3	89.2	51.5	3	141.2	81.5	3	193.1	111.5	3	245.1	141.5
44	38.1	22.	4	90.1	52.	4	142.	82.	4	194.	112.	4	246.	142.
45	39.	22.5	5	90.9	52.5	5	142.9	82.5	5	194.9	112.5	5	246.8	142.5
46	39.8	23.	6	91.8	53.	6	143.8	83.	6	195.7	113.	6	247.7	143.
47	40.7	23.5	7	92.7	53.5	7	144.6	83.5	7	196.6	113.5	7	248.5	143.5
48	41.6	24.	8	93.5	54.	8	145.5	84.	8	197.5	114.	8	249.4	144.
49	42.4	24.5	9	94.4	54.5	9	146.4	84.5	9	198.3	114.5	9	250.3	144.5
50	43.3	25.	110	95.3	55.	170	147.2	85.	230	199.2	115.	290	251.1	145.
51	44.2	25.5	1	96.1	55.5	1	148.1	85.5	1	200.1	115.5	1	252.	145.5
52	45.	26.	2	97.	56.	2	149.	86.	2	200.9	116.	2	252.9	146.
53	45.9	26.5	3	97.9	56.5	3	149.8	86.5	3	201.8	116.5	3	253.7	146.5
54	46.8	27.	4	98.7	57.	4	150.7	87.	4	202.6	117.	4	254.6	147.
55	47.6	27.5	5	99.6	57.5	5	151.6	87.5	5	203.5	117.5	5	255.5	147.5
56	48.5	28.	6	100.5	58.	6	152.4	88.	6	204.4	118.	6	256.3	148.
57	49.4	28.5	7	101.3	58.5	7	153.3	88.5	7	205.3	118.5	7	257.2	148.5
58	50.3	29.	8	102.2	59.	8	154.2	89.	8	206.1	119.	8	258.1	149.
59	51.1	29.5	9	103.1	59.5	9	155.	89.5	9	207.	119.5	9	259.0	149.5
60	52.	30.	190	103.9	60.	180	155.9	90.	240	207.8	120.	300	259.8	150.
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 60°.

Course 31°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.9	0.5	61	52.3	31.4	121	103.7	62.3	181	153.1	93.3	241	206.6	124.1
2	1.7	1.	62	53.1	31.9	2	104.6	62.8	2	156.	93.7	2	207.4	124.6
3	2.6	1.5	63	54.	32.4	3	105.4	63.3	3	156.9	94.3	3	208.3	125.3
4	3.4	2.1	64	54.9	33.	4	106.3	63.9	4	157.7	94.8	4	209.1	125.7
5	4.3	2.6	65	55.7	33.5	5	107.1	64.4	5	158.6	95.3	5	210.	126.2
6	5.1	3.1	66	56.6	34.	6	108.	64.9	6	159.4	95.8	6	210.9	126.7
7	6.	3.6	67	57.4	34.5	7	108.9	65.4	7	160.3	96.3	7	211.7	127.2
8	6.9	4.1	68	58.3	35.	8	109.7	65.9	8	161.1	96.8	8	212.6	127.7
9	7.7	4.6	69	59.1	35.5	9	110.6	66.4	9	162.	97.3	9	213.4	128.2
10	8.6	5.2	70	60.	36.1	130	111.4	67.	190	162.9	97.9	250	214.3	128.8
11	9.4	5.7	71	60.9	36.6	1	112.3	67.5	1	163.7	98.4	1	215.1	129.3
12	10.3	6.2	72	61.7	37.1	2	113.1	68.	2	164.6	98.9	2	216.	129.8
13	11.1	6.7	73	62.6	37.6	3	114.	68.5	3	165.4	99.4	3	216.9	130.3
14	12.	7.2	74	63.4	38.1	4	114.9	69.	4	166.3	99.9	4	217.7	130.8
15	12.9	7.7	75	64.3	38.6	5	115.7	69.5	5	167.1	100.4	5	218.6	131.3
16	13.7	8.2	76	65.1	39.1	6	116.6	70.	6	168.	100.9	6	219.4	131.8
17	14.6	8.8	77	66.	39.7	7	117.4	70.6	7	168.9	101.5	7	220.3	132.4
18	15.4	9.3	78	66.9	40.2	8	118.3	71.1	8	169.7	102.	8	221.1	132.9
19	16.3	9.8	79	67.7	40.7	9	119.1	71.6	9	170.6	102.5	9	222.	133.4
20	17.1	10.3	80	68.6	41.2	140	120.	72.1	200	171.4	103.	260	222.9	133.9
21	18.	10.8	81	69.4	41.7	1	120.9	72.6	1	172.3	103.5	1	223.7	134.4
22	18.9	11.3	82	70.3	42.2	2	121.7	73.1	2	173.1	104.	2	224.6	134.9
23	19.7	11.8	83	71.1	42.7	3	122.6	73.7	3	174.	104.6	3	225.4	135.5
24	20.6	12.4	84	72.	43.3	4	123.4	74.2	4	174.9	105.1	4	226.3	136.
25	21.4	12.9	85	72.9	43.8	5	124.3	74.7	5	175.7	105.6	5	227.1	136.5
26	22.3	13.4	86	73.7	44.3	6	125.1	75.2	6	176.6	106.1	6	228.	137.
27	23.1	13.9	87	74.6	44.8	7	126.	75.7	7	177.4	106.6	7	228.9	137.5
28	24.	14.4	88	75.4	45.3	8	126.9	76.2	8	178.3	107.1	8	229.7	138.
29	24.9	14.9	89	76.3	45.8	9	127.7	76.7	9	179.1	107.6	9	230.6	138.5
30	25.7	15.5	90	77.1	46.4	150	128.6	77.3	210	180.	108.2	270	231.4	139.1
31	26.6	16.	91	78.	46.9	1	129.4	77.8	1	180.9	108.7	1	232.3	139.6
32	27.4	16.5	92	78.9	47.4	2	130.3	78.3	2	181.7	109.2	2	233.1	140.1
33	28.3	17.	93	79.7	47.9	3	131.1	78.8	3	182.6	109.7	3	234.	140.6
34	29.1	17.5	94	80.6	48.4	4	132.	79.3	4	183.4	110.2	4	234.9	141.1
35	30.	18.	95	81.4	48.9	5	132.9	79.8	5	184.3	110.7	5	235.7	141.6
36	30.9	18.5	96	82.3	49.4	6	133.7	80.3	6	185.1	111.2	6	236.6	142.2
37	31.7	19.1	97	83.1	50.	7	134.6	80.9	7	186.	111.8	7	237.4	142.7
38	32.6	19.6	98	84.	50.5	8	135.4	81.4	8	186.9	112.3	8	238.3	143.2
39	33.4	20.1	99	84.9	51.	9	136.3	81.9	9	187.7	112.8	9	239.1	143.7
40	34.3	20.6	100	85.7	51.5	160	137.1	82.4	220	188.6	113.3	280	240.	144.2
41	35.1	21.1	1	86.6	52.	1	138.	82.9	1	189.4	113.8	1	240.9	144.7
42	36.	21.6	2	87.4	52.5	2	138.9	83.4	2	190.3	114.3	2	241.7	145.2
43	36.9	22.1	3	88.3	53.	3	139.7	84.	3	191.1	114.9	3	242.6	145.8
44	37.7	22.7	4	89.1	53.6	4	140.6	84.5	4	192.	115.4	4	243.4	146.3
45	38.6	23.2	5	90.	54.1	5	141.4	85.	5	192.9	115.9	5	244.3	146.8
46	39.4	23.7	6	90.9	54.6	6	142.3	85.5	6	193.7	116.4	6	245.1	147.3
47	40.3	24.2	7	91.7	55.1	7	143.1	86.	7	194.6	116.9	7	246.	147.8
48	41.1	24.7	8	92.6	55.6	8	144.	86.5	8	195.4	117.4	8	246.9	148.3
49	42.	25.2	9	93.4	56.1	9	144.9	87.	9	196.3	117.9	9	247.7	148.8
50	42.9	25.8	110	94.3	56.7	170	145.7	87.6	230	197.1	118.5	290	248.6	149.4
51	43.7	26.3	1	95.1	57.2	1	146.6	88.1	1	198.	119.	1	249.4	149.9
52	44.6	26.8	2	96.	57.7	2	147.4	88.6	2	198.9	119.5	2	250.3	150.4
53	45.4	27.3	3	96.9	58.2	3	148.3	89.1	3	199.7	120.	3	251.2	150.9
54	46.3	27.8	4	97.7	58.7	4	149.1	89.6	4	200.6	120.5	4	252.	151.4
55	47.1	28.3	5	98.6	59.2	5	150.	90.1	5	201.4	121.	5	252.9	151.9
56	48.	28.8	6	99.4	59.7	6	150.9	90.6	6	202.3	121.5	6	253.7	152.5
57	48.9	29.4	7	100.3	60.3	7	151.7	91.2	7	203.1	122.1	7	254.6	153.
58	49.7	29.9	8	101.1	60.8	8	152.6	91.7	8	204.	122.6	8	255.4	153.5
59	50.6	30.4	9	102.	61.3	9	153.4	92.2	9	204.9	123.1	9	256.3	154.
60	51.4	30.9	120	102.9	61.8	180	154.3	92.7	240	205.7	123.6	300	257.1	154.5
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 59°.

Course 33°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.5	61	51.7	32.3	121	102.6	64.1	181	153.5	95.9	261	304.4	127.7
2	1.7	1.1	62	52.6	32.9	2	103.5	64.7	2	154.3	96.4	2	305.3	128.3
3	2.5	1.6	63	53.4	33.4	3	104.3	65.2	3	155.2	97.	3	306.1	128.9
4	3.4	2.1	64	54.3	33.9	4	105.2	65.7	4	156.	97.5	4	306.9	129.5
5	4.2	2.6	65	55.1	34.4	5	106.	66.2	5	156.9	98.	5	307.8	130.1
6	5.1	3.2	66	56.	35.	6	106.9	66.8	6	157.7	98.6	6	308.6	130.7
7	5.9	3.7	67	56.8	35.5	7	107.7	67.3	7	158.6	99.1	7	309.5	131.3
8	6.8	4.3	68	57.7	36.	8	108.6	67.8	8	159.4	99.6	8	310.3	131.9
9	7.6	4.8	69	58.5	36.6	9	109.4	68.4	9	160.3	100.2	9	311.2	132.5
10	8.5	5.3	70	59.4	37.1	130	110.3	68.9	190	161.1	100.7	250	312.	132.5
11	9.3	5.8	71	60.3	37.6	1	111.1	69.4	1	162.	101.3	1	312.9	133.
12	10.2	6.4	72	61.1	38.2	2	111.9	69.9	2	162.8	101.7	2	313.7	133.5
13	11.	6.9	73	61.9	38.7	3	112.8	70.5	3	163.7	102.3	3	314.6	134.1
14	11.9	7.4	74	62.8	39.2	4	113.6	71.	4	164.5	102.8	4	315.4	134.6
15	12.7	7.9	75	63.6	39.7	5	114.5	71.5	5	165.4	103.3	5	316.3	135.1
16	13.6	8.5	76	64.5	40.3	6	115.3	72.1	6	166.3	103.9	6	317.1	135.7
17	14.4	9.	77	65.3	40.8	7	116.2	72.6	7	167.1	104.4	7	317.9	136.2
18	15.3	9.5	78	66.1	41.3	8	117.	73.1	8	167.9	104.9	8	318.8	136.7
19	16.1	10.1	79	67.	41.9	9	117.9	73.7	9	168.8	105.5	9	319.6	137.3
20	17.	10.6	80	67.8	42.4	140	118.7	74.2	200	169.6	106.	260	320.5	137.8
21	17.8	11.1	81	68.7	42.9	1	119.6	74.7	1	170.5	106.5	1	321.3	138.3
22	18.7	11.7	82	69.5	43.5	2	120.4	75.2	2	171.3	107.	2	322.1	138.8
23	19.5	12.2	83	70.4	44.	3	121.3	75.8	3	172.2	107.6	3	323.	139.4
24	20.4	12.7	84	71.2	44.5	4	122.1	76.3	4	173.	108.1	4	323.9	139.9
25	21.3	13.2	85	72.1	45.	5	123.	76.8	5	173.8	108.6	5	324.7	140.4
26	22.	13.8	86	72.9	45.6	6	123.8	77.4	6	174.7	109.2	6	325.6	141.
27	22.9	14.3	87	73.8	46.1	7	124.7	77.9	7	175.5	109.7	7	326.4	141.5
28	23.7	14.8	88	74.6	46.6	8	125.5	78.4	8	176.4	110.3	8	327.3	142.
29	24.6	15.4	89	75.5	47.2	9	126.4	79.	9	177.3	110.9	9	328.1	142.5
30	25.4	15.9	90	76.3	47.7	150	127.2	79.5	210	178.1	111.3	270	329.	143.1
31	26.3	16.4	91	77.2	48.3	1	128.1	80.	1	178.9	111.8	1	329.8	143.6
32	27.1	17.	92	78.	48.8	2	128.9	80.5	2	179.8	112.3	2	330.7	144.1
33	28.	17.5	93	78.9	49.3	3	129.8	81.1	3	180.6	112.9	3	331.5	144.7
34	28.8	18.	94	79.7	49.8	4	130.6	81.6	4	181.5	113.4	4	332.4	145.2
35	29.7	18.5	95	80.6	50.3	5	131.4	82.1	5	182.3	113.9	5	333.2	145.7
36	30.5	19.1	96	81.4	50.9	6	132.3	82.7	6	183.2	114.5	6	334.1	146.3
37	31.4	19.6	97	82.3	51.4	7	133.1	83.2	7	184.	115.	7	334.9	146.8
38	32.2	20.1	98	83.1	51.9	8	134.	83.7	8	184.9	115.5	8	335.8	147.3
39	33.1	20.7	99	84.	52.5	9	134.8	84.3	9	185.7	116.1	9	336.6	147.8
40	33.9	21.2	100	84.8	53.	160	135.7	84.8	220	186.6	116.6	280	337.5	148.4
41	34.8	21.7	1	85.7	53.5	1	136.5	85.3	1	187.4	117.1	1	338.3	148.9
42	35.6	22.3	2	86.5	54.1	2	137.4	85.8	2	188.3	117.6	2	339.1	149.4
43	36.5	22.8	3	87.3	54.6	3	138.3	86.4	3	189.1	118.2	3	340.	150.
44	37.3	23.3	4	88.2	55.1	4	139.1	86.9	4	190.	118.7	4	340.8	150.5
45	38.2	23.8	5	89.	55.6	5	139.9	87.4	5	190.8	119.2	5	341.7	151.
46	39.	24.4	6	89.9	56.2	6	140.8	88.	6	191.7	119.8	6	342.5	151.6
47	39.9	24.9	7	90.7	56.7	7	141.6	88.5	7	192.5	120.3	7	343.4	152.1
48	40.7	25.4	8	91.6	57.2	8	142.5	89.	8	193.4	120.8	8	344.3	152.6
49	41.6	26.	9	92.4	57.8	9	143.3	89.6	9	194.2	121.4	9	345.1	153.1
50	42.4	26.5	110	93.3	58.3	170	144.2	90.1	230	195.1	121.9	290	345.9	153.7
51	43.3	27.	1	94.1	58.8	1	145.	90.6	1	195.9	122.4	1	346.8	154.2
52	44.1	27.6	2	95.	59.4	2	145.9	91.1	2	196.7	122.9	2	347.6	154.7
53	44.9	28.1	3	95.8	59.9	3	146.7	91.7	3	197.6	123.5	3	348.5	155.2
54	45.8	28.6	4	96.7	60.4	4	147.6	92.2	4	198.4	124.	4	349.3	155.8
55	46.6	29.1	5	97.5	60.9	5	148.4	92.7	5	199.3	124.5	5	350.2	156.3
56	47.5	29.7	6	98.4	61.5	6	149.3	93.3	6	200.1	125.1	6	351.	156.9
57	48.3	30.2	7	99.2	62.	7	150.1	93.8	7	201.	125.6	7	351.9	157.4
58	49.2	30.8	8	100.1	62.5	8	151.	94.3	8	201.8	126.1	8	352.7	157.9
59	50.	31.3	9	100.9	63.1	9	151.8	94.9	9	202.7	126.7	9	353.6	158.4
60	50.9	31.8	190	101.8	63.6	180	152.6	95.4	240	203.5	127.2	300	354.4	159

Distance, Departure and Diff. Latitude

Course 58°.

Course 33°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.5	61	51.9	33.9	121	101.5	65.9	191	151.8	98.8	241	202.1	131.3
2	1.7	1.1	62	52.	33.8	2	102.3	66.4	2	152.6	99.1	2	203.	131.8
3	2.5	1.6	63	52.8	34.3	3	103.2	67.	3	153.5	99.7	3	203.8	132.3
4	3.4	2.2	64	53.7	34.9	4	104.	67.5	4	154.3	100.9	4	204.6	132.9
5	4.2	2.7	65	54.5	35.4	5	104.8	68.1	5	155.9	100.8	5	205.5	133.4
6	5.	3.3	66	55.4	35.9	6	105.7	68.6	6	156.	101.3	6	206.3	134.
7	5.9	3.8	67	56.2	36.5	7	106.5	69.2	7	156.8	101.8	7	207.4	134.5
8	6.7	4.4	68	57.	37.	8	107.3	69.7	8	157.7	102.4	8	208.	135.1
9	7.5	4.9	69	57.9	37.6	9	108.2	70.3	9	158.5	102.9	9	208.8	135.6
10	8.4	5.4	70	58.7	38.1	130	109.	70.8	190	159.3	103.5	250	209.7	136.2
11	9.2	6.	71	59.5	38.7	1	109.9	71.3	1	160.9	104.	1	210.5	136.7
12	10.1	6.5	72	60.4	39.2	2	110.7	71.9	2	161.	104.6	2	211.3	137.2
13	10.9	7.1	73	61.2	39.8	3	111.5	72.4	3	161.9	105.1	3	212.4	137.6
14	11.7	7.6	74	62.1	40.3	4	112.4	73.	4	162.7	105.7	4	213.	138.3
15	12.6	8.2	75	62.9	40.8	5	113.2	73.5	5	163.5	106.9	5	213.9	138.9
16	13.4	8.7	76	63.7	41.4	6	114.1	74.1	6	164.4	106.7	6	214.7	139.4
17	14.3	9.3	77	64.6	41.9	7	114.9	74.6	7	165.3	107.3	7	215.5	140.
18	15.1	9.8	78	65.4	42.5	8	115.7	75.2	8	166.1	107.8	8	216.4	140.5
19	15.9	10.3	79	66.3	43.	9	116.6	75.7	9	166.9	108.4	9	217.2	141.1
20	16.8	10.9	80	67.1	43.6	140	117.4	76.2	200	167.7	108.9	260	218.1	141.6
21	17.6	11.4	81	67.9	44.1	1	118.3	76.8	1	168.6	109.5	1	218.9	142.2
22	18.5	12.	82	68.8	44.7	2	119.1	77.3	2	169.4	110.	2	219.7	142.7
23	19.3	12.5	83	69.6	45.2	3	119.9	77.9	3	170.3	110.6	3	220.6	143.2
24	20.1	13.1	84	70.4	45.7	4	120.8	78.4	4	171.1	111.1	4	221.4	143.8
25	21.	13.6	85	71.3	46.3	5	121.6	79.	5	171.9	111.7	5	222.2	144.3
26	21.8	14.2	86	72.1	46.8	6	122.4	79.5	6	172.8	112.2	6	223.1	144.9
27	22.6	14.7	87	73.	47.4	7	123.3	80.1	7	173.6	112.7	7	223.9	145.4
28	23.5	15.2	88	73.8	47.9	8	124.1	80.6	8	174.4	113.3	8	224.8	146.
29	24.3	15.8	89	74.6	48.5	9	125.	81.2	9	175.3	113.8	9	225.6	146.5
30	25.2	16.3	90	75.5	49.	150	125.8	81.7	210	176.1	114.4	270	226.4	147.1
31	26.	16.9	91	76.3	49.6	1	126.6	82.2	1	177.	114.9	1	227.3	147.6
32	26.8	17.4	92	77.2	50.1	2	127.5	82.8	2	177.8	115.5	2	228.1	148.1
33	27.7	18.	93	78.	50.7	3	128.3	83.3	3	178.6	116.	3	229.	148.7
34	28.5	18.5	94	78.8	51.2	4	129.2	83.9	4	179.5	116.6	4	229.8	149.2
35	29.4	19.1	95	79.7	51.7	5	130.	84.4	5	180.3	117.1	5	230.6	149.8
36	30.2	19.6	96	80.5	52.3	6	130.8	85.	6	181.3	117.6	6	231.5	150.3
37	31.	20.2	97	81.4	52.8	7	131.7	85.5	7	182.	118.2	7	232.3	150.9
38	31.9	20.7	98	82.2	53.4	8	132.5	86.1	8	182.8	118.7	8	233.2	151.4
39	32.7	21.3	99	83.	53.9	9	133.3	86.6	9	183.7	119.3	9	234.	152.
40	33.5	21.8	100	83.9	54.5	160	134.2	87.1	220	184.5	119.8	280	234.8	152.5
41	34.4	22.3	1	84.7	55.	1	135.	87.7	1	185.3	120.4	1	235.7	153.
42	35.2	22.9	2	85.5	55.6	2	135.9	88.2	2	186.2	120.9	2	236.5	153.6
43	36.1	23.4	3	86.4	56.1	3	136.7	88.8	3	187.	121.5	3	237.3	154.1
44	36.9	24.	4	87.2	56.6	4	137.5	89.3	4	187.9	122.	4	238.2	154.7
45	37.7	24.5	5	88.1	57.2	5	138.4	89.9	5	188.7	122.5	5	239.	155.2
46	38.6	25.1	6	88.9	57.7	6	139.3	90.4	6	189.5	123.1	6	239.9	155.8
47	39.4	25.6	7	89.7	58.3	7	140.1	91.	7	190.4	123.6	7	240.7	156.3
48	40.3	26.1	8	90.6	58.8	8	140.9	91.5	8	191.2	124.2	8	241.5	156.9
49	41.1	26.7	9	91.4	59.4	9	141.7	92.	9	192.1	124.7	9	242.4	157.4
50	41.9	27.2	110	92.3	59.9	170	142.6	92.6	230	192.9	125.3	290	243.2	157.9
51	42.8	27.8	1	93.1	60.5	1	143.4	93.1	1	193.7	125.8	1	244.1	158.5
52	43.6	28.3	2	93.9	61.	2	144.3	93.7	2	194.6	126.4	2	244.9	159.
53	44.4	28.9	3	94.8	61.5	3	145.1	94.2	3	195.4	126.9	3	245.7	159.6
54	45.3	29.4	4	95.6	62.1	4	145.9	94.8	4	196.2	127.4	4	246.6	160.1
55	46.1	30.	5	96.4	62.6	5	146.8	95.3	5	197.1	128.	5	247.4	160.7
56	47.	30.5	6	97.3	63.2	6	147.6	95.9	6	197.9	128.5	6	248.2	161.2
57	47.8	31.	7	98.1	63.7	7	148.4	96.4	7	198.8	129.1	7	249.1	161.8
58	48.6	31.6	8	99.	64.3	8	149.3	96.9	8	199.6	129.6	8	249.9	162.3
59	49.5	32.1	9	99.8	64.8	9	150.1	97.5	9	200.4	130.2	9	250.8	162.8
60	50.3	32.7	190	100.6	65.4	180	151.	98.	240	201.3	130.7	300	251.6	163.4
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 57°.

Course 34°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	50.6	34.1	181	100.3	67.7	181	150.1	101.9	241	199.8	134.6
2	1.7	1.1	62	51.4	34.7	2	101.1	68.2	2	150.9	101.8	2	200.6	135.3
3	2.5	1.7	63	52.2	35.2	3	102.	68.8	3	151.7	102.3	3	201.5	135.9
4	3.3	2.2	64	53.1	35.8	4	102.8	69.3	4	152.5	102.9	4	202.3	136.4
5	4.1	2.8	65	53.9	36.3	5	103.6	69.9	5	153.4	103.5	5	203.1	137.
6	5.	3.4	66	54.7	36.9	6	104.5	70.5	6	154.3	104.	6	203.9	137.6
7	5.8	3.9	67	55.5	37.5	7	105.3	71.	7	155.	104.6	7	204.8	138.1
8	6.6	4.5	68	56.4	38.	8	106.1	71.6	8	155.9	105.1	8	205.6	138.7
9	7.5	5.	69	57.3	38.6	9	106.9	72.1	9	156.7	105.7	9	206.4	139.3
10	8.3	5.6	70	58.	39.1	130	107.8	72.7	190	157.5	106.2	250	207.3	139.8
11	9.1	6.2	71	58.9	39.7	1	108.6	73.3	1	158.3	106.8	1	208.1	140.4
12	9.9	6.7	72	59.7	40.3	2	109.4	73.8	2	159.2	107.4	2	208.9	140.9
13	10.8	7.3	73	60.5	40.8	3	110.3	74.4	3	160.	107.9	3	209.7	141.5
14	11.6	7.8	74	61.3	41.4	4	111.1	74.9	4	160.8	108.5	4	210.6	142.
15	12.4	8.4	75	62.2	41.9	5	111.9	75.5	5	161.7	109.	5	211.4	142.6
16	13.3	8.9	76	63.	42.5	6	112.7	76.1	6	162.5	109.6	6	212.3	143.2
17	14.1	9.5	77	63.8	43.1	7	113.6	76.6	7	163.3	110.2	7	213.1	143.7
18	14.9	10.1	78	64.7	43.6	8	114.4	77.3	8	164.1	110.7	8	213.9	144.3
19	15.8	10.6	79	65.5	44.2	9	115.2	77.7	9	165.	111.3	9	214.7	144.8
20	16.6	11.2	80	66.3	44.7	140	116.1	78.3	200	165.8	111.8	260	215.5	145.4
21	17.4	11.7	81	67.2	45.3	1	116.9	78.8	1	166.6	112.4	1	216.4	145.9
22	18.2	12.3	82	68.	45.9	2	117.7	79.4	2	167.5	113.	2	217.2	146.5
23	19.1	12.9	83	68.8	46.4	3	118.6	80.	3	168.3	113.5	3	218.	147.1
24	19.9	13.4	84	69.6	47.	4	119.4	80.5	4	169.1	114.1	4	218.9	147.6
25	20.7	14.	85	70.5	47.5	5	120.2	81.1	5	170.	114.6	5	219.7	148.2
26	21.6	14.5	86	71.3	48.1	6	121.	81.6	6	170.8	115.2	6	220.5	148.7
27	22.4	15.1	87	72.1	48.6	7	121.9	82.2	7	171.6	115.8	7	221.4	149.3
28	23.2	15.7	88	73.	49.2	8	122.7	82.8	8	172.4	116.3	8	222.2	149.9
29	24.	16.2	89	73.8	49.8	9	123.5	83.3	9	173.3	116.9	9	223.	150.4
30	24.9	16.8	90	74.6	50.3	150	124.4	83.9	210	174.1	117.4	270	223.8	151.
31	25.7	17.3	91	75.4	50.9	1	125.2	84.4	1	174.9	118.	1	224.7	151.5
32	26.5	17.9	92	76.3	51.4	2	126.	85.	2	175.8	118.5	2	225.5	152.1
33	27.4	18.5	93	77.1	52.	3	126.8	85.6	3	176.6	119.1	3	226.3	152.7
34	28.2	19.	94	77.9	52.6	4	127.7	86.1	4	177.4	119.7	4	227.2	153.2
35	29.	19.6	95	78.8	53.1	5	128.5	86.7	5	178.2	120.2	5	228.	153.8
36	29.8	20.1	96	79.6	53.7	6	129.3	87.2	6	179.	120.8	6	228.8	154.3
37	30.7	20.7	97	80.4	54.2	7	130.2	87.8	7	179.9	121.3	7	229.6	154.9
38	31.5	21.2	98	81.2	54.8	8	131.	88.4	8	180.7	121.9	8	230.5	155.5
39	32.3	21.8	99	82.1	55.4	9	131.8	88.9	9	181.6	122.5	9	231.3	156.
40	33.2	22.4	100	82.9	55.9	160	132.6	89.5	220	182.4	123.	280	232.1	156.6
41	34.	22.9	1	83.7	56.5	1	133.5	90.	1	183.3	123.6	1	233.	157.1
42	34.8	23.5	2	84.6	57.	2	134.3	90.6	2	184.	124.1	2	233.8	157.7
43	35.6	24.	3	85.4	57.6	3	135.1	91.1	3	184.9	124.7	3	234.6	158.3
44	36.5	24.6	4	86.3	58.2	4	136.	91.7	4	185.7	125.3	4	235.4	158.8
45	37.3	25.2	5	87.	58.7	5	136.8	92.3	5	186.5	125.8	5	236.3	159.4
46	38.1	25.7	6	87.9	59.3	6	137.6	92.8	6	187.4	126.4	6	237.1	159.9
47	39.	26.3	7	88.7	59.8	7	138.4	93.4	7	188.2	126.9	7	237.9	160.5
48	39.8	26.8	8	89.5	60.4	8	139.3	93.9	8	189.	127.5	8	238.6	161.
49	40.6	27.4	9	90.4	61.	9	140.1	94.5	9	189.8	128.1	9	239.6	161.6
50	41.5	28.	110	91.3	61.5	170	140.9	95.1	230	190.7	128.6	290	240.4	162.2
51	42.3	28.5	1	92.	62.1	1	141.8	95.6	1	191.5	129.2	1	241.2	162.7
52	43.1	29.1	2	92.9	62.6	2	142.6	96.2	2	192.3	129.7	2	242.1	163.3
53	43.9	29.6	3	93.7	63.2	3	143.4	96.7	3	193.2	130.3	3	242.9	163.8
54	44.8	30.2	4	94.5	63.7	4	144.3	97.3	4	194.	130.9	4	243.7	164.4
55	45.6	30.8	5	95.3	64.3	5	145.1	97.9	5	194.8	131.4	5	244.6	165.
56	46.4	31.3	6	96.2	64.9	6	145.9	98.4	6	195.7	132.	6	245.4	165.5
57	47.3	31.9	7	97.	65.4	7	146.7	99.	7	196.5	132.5	7	246.2	166.1
58	48.1	32.4	8	97.8	66.	8	147.6	99.5	8	197.3	133.1	8	247.1	166.6
59	48.9	33.	9	98.7	66.5	9	148.4	100.1	9	198.1	133.6	9	247.9	167.2
60	49.7	33.6	130	99.5	67.1	180	149.2	100.7	240	199.	134.2	300	248.7	167.8

Distance, Departure and Diff. Latitude.

Course 56°.

Course 35°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	50.	35.	121	99.1	69.4	181	148.3	103.8	241	197.4	138.9
2	1.6	1.1	62	50.8	35.6	2	99.9	70.	2	149.1	104.4	2	198.2	139.8
3	2.5	1.7	63	51.6	36.1	3	100.8	70.5	3	149.9	105.	3	199.1	140.4
4	3.3	2.3	64	52.4	36.7	4	101.6	71.1	4	150.7	105.5	4	199.9	140.
5	4.1	2.9	65	53.2	37.3	5	102.4	71.7	5	151.5	106.1	5	200.7	140.5
6	4.9	3.4	66	54.1	37.9	6	103.2	72.3	6	152.4	106.7	6	201.5	141.1
7	5.7	4.	67	54.9	38.4	7	104.	72.9	7	153.2	107.3	7	202.3	141.7
8	6.6	4.6	68	55.7	39.	8	104.9	73.4	8	154.	107.8	8	203.1	142.2
9	7.4	5.2	69	56.5	39.6	9	105.7	74.	9	154.8	108.4	9	204.	142.8
10	8.2	5.7	70	57.3	40.2	130	106.5	74.6	190	155.6	109.	250	204.8	143.4
11	9.	6.3	71	58.2	40.7	1	107.3	75.1	1	156.5	109.6	1	205.6	144.
12	9.8	6.9	72	59.	41.3	2	108.1	75.7	2	157.3	110.1	2	206.4	144.5
13	10.6	7.5	73	59.8	41.9	3	108.9	76.3	3	158.1	110.7	3	207.2	145.1
14	11.5	8.	74	60.6	42.4	4	109.8	76.9	4	158.9	111.3	4	208.1	145.7
15	12.3	8.6	75	61.4	43.	5	110.6	77.4	5	159.7	111.8	5	208.9	146.3
16	13.1	9.2	76	62.3	43.6	6	111.4	78.	6	160.6	112.4	6	209.7	146.8
17	13.9	9.8	77	63.1	44.2	7	112.2	78.6	7	161.4	113.	7	210.5	147.4
18	14.7	10.3	78	63.9	44.7	8	113.	79.2	8	162.2	113.6	8	211.3	148.
19	15.6	10.9	79	64.7	45.3	9	113.9	79.7	9	163.	114.1	9	212.2	148.6
20	16.4	11.5	80	65.5	45.9	140	114.7	80.3	200	163.8	114.7	260	213.	149.1
21	17.2	12.	81	66.4	46.5	1	115.5	80.9	1	164.6	115.3	1	213.8	149.7
22	18.	12.6	82	67.2	47.	2	116.3	81.4	2	165.5	115.9	2	214.6	150.3
23	18.8	13.2	83	68.	47.6	3	117.1	82.	3	166.3	116.4	3	215.4	150.9
24	19.7	13.8	84	68.8	48.2	4	118.	82.6	4	167.1	117.	4	216.3	151.4
25	20.5	14.3	85	69.6	48.8	5	118.8	83.2	5	167.9	117.6	5	217.1	152.
26	21.3	14.9	86	70.4	49.3	6	119.6	83.7	6	168.7	118.2	6	217.9	152.6
27	22.1	15.5	87	71.3	49.9	7	120.4	84.3	7	169.6	118.7	7	218.7	153.1
28	22.9	16.1	88	72.1	50.5	8	121.2	84.9	8	170.4	119.3	8	219.5	153.7
29	23.8	16.6	89	72.9	51.	9	122.1	85.5	9	171.2	119.9	9	220.4	154.3
30	24.6	17.2	90	73.7	51.6	150	122.9	86.	210	172.	120.5	270	221.2	154.9
31	25.4	17.8	91	74.5	52.2	1	123.7	86.6	1	172.8	121.	1	222.	155.4
32	26.2	18.4	92	75.4	52.8	2	124.5	87.2	2	173.7	121.6	2	222.8	156.
33	27.	18.9	93	76.2	53.3	3	125.3	87.8	3	174.5	122.2	3	223.6	156.6
34	27.9	19.5	94	77.	53.9	4	126.1	88.3	4	175.3	122.7	4	224.4	157.2
35	28.7	20.1	95	77.8	54.5	5	127.	88.9	5	176.1	123.3	5	225.3	157.7
36	29.5	20.6	96	78.6	55.1	6	127.8	89.5	6	176.9	123.9	6	226.1	158.3
37	30.3	21.2	97	79.5	55.6	7	128.6	90.1	7	177.8	124.5	7	226.9	158.9
38	31.1	21.8	98	80.3	56.2	8	129.4	90.6	8	178.6	125.	8	227.7	159.5
39	31.9	22.4	99	81.1	56.8	9	130.2	91.2	9	179.4	125.6	9	228.5	160.
40	32.8	22.9	100	81.9	57.4	160	131.1	91.8	220	180.3	126.2	280	229.4	160.6
41	33.6	23.5	1	82.7	57.9	1	131.9	92.3	1	181.	126.8	1	230.2	161.2
42	34.4	24.1	2	83.6	58.5	2	132.7	92.9	2	181.9	127.3	2	231.	161.7
43	35.2	24.7	3	84.4	59.1	3	133.5	93.5	3	182.7	127.9	3	231.8	162.3
44	36.	25.2	4	85.2	59.7	4	134.3	94.1	4	183.5	128.5	4	232.6	162.9
45	36.9	25.8	5	86.	60.2	5	135.9	94.6	5	184.3	129.1	5	233.5	163.5
46	37.7	26.4	6	86.8	60.8	6	136.	95.2	6	185.1	129.6	6	234.3	164.
47	38.5	27.	7	87.6	61.4	7	136.8	95.8	7	185.9	130.2	7	235.1	164.5
48	39.3	27.5	8	88.5	61.9	8	137.6	96.4	8	186.8	130.8	8	235.9	165.2
49	40.1	28.1	9	89.3	62.5	9	138.4	96.9	9	187.6	131.3	9	236.7	165.8
50	41.	28.7	110	90.1	63.1	170	139.3	97.5	230	188.4	131.9	290	237.5	166.3
51	41.8	29.3	1	90.9	63.7	1	140.1	98.1	1	189.2	132.5	1	238.4	166.9
52	42.6	29.8	2	91.7	64.2	2	140.9	98.7	2	190.	133.1	2	239.3	167.5
53	43.4	30.4	3	92.6	64.8	3	141.7	99.2	3	190.9	133.6	3	240.	168.1
54	44.2	31.	4	93.4	65.4	4	142.5	99.8	4	191.7	134.2	4	240.8	168.6
55	45.1	31.5	5	94.2	66.	5	143.4	100.4	5	192.5	134.8	5	241.6	169.2
56	45.9	32.1	6	95.	66.5	6	144.9	100.9	6	193.3	135.4	6	242.5	169.8
57	46.7	32.7	7	95.8	67.1	7	145.	101.5	7	194.1	135.9	7	243.3	170.4
58	47.5	33.3	8	96.7	67.7	8	145.8	102.1	8	195.	136.5	8	244.1	170.9
59	48.3	33.8	9	97.5	68.2	9	146.6	102.7	9	195.8	137.1	9	244.9	171.5
60	49.1	34.4	120	98.3	68.8	180	147.4	103.2	240	196.6	137.7	300	245.7	172.1
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 55°.

T

Course 36°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	49.4	35.9	181	97.9	71.1	181	146.4	106.4	241	195.	141.7
2	1.6	1.2	62	50.2	36.4	2	98.7	71.7	2	147.2	107.	2	195.8	142.2
3	2.4	1.8	63	51.	37.	3	99.5	72.3	3	148.1	107.6	3	196.6	142.8
4	3.2	2.4	64	51.8	37.6	4	100.3	72.9	4	148.9	108.2	4	197.4	143.4
5	4.	2.9	65	52.6	38.2	5	101.1	73.5	5	149.7	108.7	5	198.2	144.
6	4.9	3.5	66	53.4	38.8	6	101.9	74.1	6	150.5	109.3	6	199.	144.6
7	5.7	4.1	67	54.2	39.4	7	102.7	74.6	7	151.3	109.9	7	199.8	145.2
8	6.5	4.7	68	55.	40.	8	103.6	75.2	8	152.1	110.5	8	200.6	145.8
9	7.3	5.3	69	55.8	40.6	9	104.4	75.8	9	152.9	111.1	9	201.4	146.4
10	8.1	5.9	70	56.6	41.1	130	105.2	76.4	190	153.7	111.7	250	202.2	146.9
11	8.9	6.5	71	57.4	41.7	1	106.	77.	1	154.5	112.3	1	203.1	147.5
12	9.7	7.1	72	58.2	42.3	2	106.8	77.6	2	155.3	112.9	2	203.9	148.1
13	10.5	7.6	73	59.1	42.9	3	107.5	78.2	3	156.1	113.4	3	204.7	148.7
14	11.3	8.2	74	59.9	43.5	4	108.4	78.8	4	156.9	114.	4	205.5	149.3
15	12.1	8.8	75	60.7	44.1	5	109.2	79.4	5	157.8	114.6	5	206.3	149.9
16	12.9	9.4	76	61.5	44.7	6	110.	79.9	6	158.6	115.2	6	207.1	150.5
17	13.8	10.	77	62.3	45.3	7	110.8	80.5	7	159.4	115.8	7	207.9	151.1
18	14.6	10.6	78	63.1	45.8	8	111.6	81.1	8	160.2	116.4	8	208.7	151.6
19	15.4	11.2	79	63.9	46.4	9	112.5	81.7	9	161.	117.	9	209.5	152.2
20	16.2	11.8	80	64.7	47.	140	113.3	82.3	200	161.8	117.6	260	210.3	152.8
21	17.	12.3	81	65.5	47.6	1	114.1	82.9	1	162.6	118.1	1	211.2	153.4
22	17.8	12.9	82	66.3	48.2	2	114.9	83.5	2	163.4	118.7	2	212.	154.
23	18.6	13.5	83	67.1	48.8	3	115.7	84.1	3	164.2	119.3	3	212.8	154.6
24	19.4	14.1	84	68.	49.4	4	116.5	84.6	4	165.	119.9	4	213.6	155.2
25	20.2	14.7	85	68.8	50.	5	117.3	85.2	5	165.8	120.5	5	214.4	155.8
26	21.	15.3	86	69.6	50.5	6	118.1	85.8	6	166.7	121.1	6	215.2	156.4
27	21.8	15.9	87	70.4	51.1	7	118.9	86.4	7	167.5	121.7	7	216.	156.9
28	22.7	16.5	88	71.2	51.7	8	119.7	87.	8	168.3	122.3	8	216.8	157.5
29	23.5	17.	89	72.	52.3	9	120.5	87.6	9	169.1	122.8	9	217.6	158.1
30	24.3	17.6	90	72.8	52.9	150	121.4	88.2	210	169.9	123.4	270	218.4	158.7
31	25.1	18.2	91	73.6	53.5	1	122.2	88.8	1	170.7	124.	1	219.2	159.3
32	25.9	18.8	92	74.4	54.1	2	123.	89.3	2	171.5	124.6	2	220.1	159.9
33	26.7	19.4	93	75.2	54.7	3	123.8	89.9	3	172.3	125.2	3	220.9	160.5
34	27.5	20.	94	76.	55.3	4	124.6	90.5	4	173.1	125.8	4	221.7	161.1
35	28.3	20.6	95	76.8	55.8	5	125.4	91.1	5	173.9	126.4	5	222.5	161.6
36	29.1	21.2	96	77.7	56.4	6	126.2	91.7	6	174.7	127.	6	223.3	162.2
37	29.9	21.7	97	78.5	57.	7	127.	92.3	7	175.6	127.5	7	224.1	162.8
38	30.7	22.3	98	79.3	57.6	8	127.8	92.9	8	176.4	128.1	8	224.9	163.4
39	31.6	22.9	99	80.1	58.2	9	128.6	93.5	9	177.2	128.7	9	225.7	164.
40	32.4	23.5	100	80.9	58.8	160	129.4	94.	220	178.	129.3	280	226.5	164.6
41	33.2	24.1	1	81.7	59.4	1	130.3	94.6	1	178.8	129.9	1	227.3	165.2
42	34.	24.7	2	82.5	60.	2	131.1	95.2	2	179.6	130.5	2	228.1	165.8
43	34.8	25.3	3	83.3	60.5	3	131.9	95.8	3	180.4	131.1	3	229.	166.3
44	35.6	25.9	4	84.1	61.1	4	132.7	96.4	4	181.2	131.7	4	229.8	166.9
45	36.4	26.5	5	84.9	61.7	5	133.5	97.	5	182.	132.3	5	230.6	167.5
46	37.2	27.	6	85.8	62.3	6	134.3	97.6	6	182.8	132.8	6	231.4	168.1
47	38.	27.6	7	86.6	62.9	7	135.1	98.2	7	183.6	133.4	7	232.2	168.7
48	38.8	28.2	8	87.4	63.5	8	135.9	98.7	8	184.5	134.	8	233.	169.3
49	39.6	28.8	9	88.2	64.1	9	136.7	99.3	9	185.3	134.6	9	233.8	169.9
50	40.5	29.4	110	89.	64.7	170	137.5	99.9	230	186.1	135.2	290	234.6	170.5
51	41.3	30.	1	89.8	65.2	1	138.3	100.5	1	186.9	135.8	1	235.4	171.
52	42.1	30.6	2	90.6	65.8	2	139.2	101.1	2	187.7	136.4	2	236.2	171.6
53	42.9	31.2	3	91.4	66.4	3	140.	101.7	3	188.5	137.	3	237.	172.2
54	43.7	31.7	4	92.2	67.	4	140.8	102.3	4	189.3	137.5	4	237.9	172.8
55	44.5	32.3	5	93.	67.6	5	141.6	102.9	5	190.1	138.1	5	238.7	173.4
56	45.3	32.9	6	93.8	68.2	6	142.4	103.5	6	190.9	138.7	6	239.5	174.
57	46.1	33.5	7	94.7	68.8	7	143.2	104.	7	191.7	139.3	7	240.3	174.6
58	46.9	34.1	8	95.5	69.4	8	144.	104.6	8	192.5	139.9	8	241.1	175.2
59	47.7	34.7	9	96.3	69.9	9	144.8	105.2	9	193.4	140.5	9	241.9	175.7
60	48.5	35.3	190	97.1	70.5	180	145.6	105.8	240	194.2	141.1	300	242.7	176.3
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 54°.

Course 37°.

Distance, Dist. Latitude and Departure

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	48.7	36.7	121	96.6	72.8	181	144.6	108.9	241	192.5	145.
2	1.6	1.2	63	49.5	37.3	2	97.4	73.4	2	145.4	109.5	2	193.3	145.6
3	2.4	1.8	63	50.3	37.9	3	98.2	74.	3	146.2	110.1	3	194.1	146.2
4	3.2	2.4	64	51.1	38.5	4	99.	74.6	4	146.9	110.7	4	194.9	146.8
5	4.	3.	65	51.9	39.1	5	99.8	75.2	5	147.7	111.3	5	195.7	147.4
6	4.8	3.6	66	52.7	39.7	6	100.6	75.8	6	148.5	111.9	6	196.5	148.
7	5.6	4.2	67	53.5	40.3	7	101.4	76.4	7	149.3	112.5	7	197.3	148.6
8	6.4	4.8	68	54.3	40.9	8	102.2	77.	8	150.1	113.1	8	198.1	149.3
9	7.2	5.4	69	55.1	41.5	9	103.	77.6	9	150.9	113.7	9	198.9	149.9
10	8.	6.	70	55.9	42.1	130	103.8	78.2	190	151.7	114.3	250	199.7	150.5
11	8.8	6.6	71	56.7	42.7	1	104.6	78.8	1	152.5	114.9	1	200.5	151.1
12	9.6	7.2	72	57.5	43.3	2	105.4	79.4	2	153.3	115.5	2	201.3	151.7
13	10.4	7.8	73	58.3	43.9	3	106.2	80.	3	154.1	116.1	3	202.1	152.3
14	11.2	8.4	74	59.1	44.5	4	107.	80.6	4	154.9	116.7	4	202.9	152.9
15	12.	9.	75	59.9	45.1	5	107.8	81.2	5	155.7	117.3	5	203.7	153.5
16	12.8	9.6	76	60.7	45.7	6	108.6	81.8	6	156.5	117.9	6	204.5	154.1
17	13.6	10.2	77	61.5	46.3	7	109.4	82.4	7	157.3	118.5	7	205.3	154.7
18	14.4	10.8	78	62.3	46.9	8	110.2	83.1	8	158.1	119.1	8	206.	155.3
19	15.2	11.4	79	63.1	47.5	9	111.	83.7	9	158.9	119.7	9	206.8	155.9
20	16.	12.	80	63.9	48.1	140	111.8	84.3	200	159.7	120.4	260	207.6	156.5
21	16.8	12.6	81	64.7	48.7	1	112.6	84.9	1	160.5	121.	1	208.4	157.1
22	17.6	13.2	82	65.5	49.3	2	113.4	85.5	2	161.3	121.6	2	209.2	157.7
23	18.4	13.8	83	66.3	49.9	3	114.2	86.1	3	162.1	122.2	3	210.	158.3
24	19.2	14.4	84	67.1	50.6	4	115.	86.7	4	162.9	122.8	4	210.8	158.9
25	20.	15.	85	67.9	51.2	5	115.8	87.3	5	163.7	123.4	5	211.6	159.5
26	20.8	15.6	86	68.7	51.8	6	116.6	87.9	6	164.5	124.	6	212.4	160.1
27	21.6	16.2	87	69.5	52.4	7	117.4	88.5	7	165.3	124.6	7	213.2	160.7
28	22.4	16.9	88	70.3	53.	8	118.2	89.1	8	166.1	125.2	8	214.	161.3
29	23.2	17.5	89	71.1	53.6	9	119.	89.7	9	166.9	125.8	9	214.8	161.9
30	24.	18.1	90	71.9	54.2	150	119.8	90.3	210	167.7	126.4	270	215.6	162.5
31	24.8	18.7	91	72.7	54.8	1	120.6	90.9	1	168.5	127.	1	216.4	163.1
32	25.6	19.3	92	73.5	55.4	2	121.4	91.5	2	169.3	127.6	2	217.2	163.7
33	26.4	19.9	93	74.3	56.	3	122.2	92.1	3	170.1	128.2	3	218.	164.3
34	27.2	20.5	94	75.1	56.6	4	123.	92.7	4	170.9	128.8	4	218.8	164.9
35	28.	21.1	95	75.9	57.2	5	123.8	93.3	5	171.7	129.4	5	219.6	165.5
36	28.8	21.7	96	76.7	57.8	6	124.6	93.9	6	172.5	130.	6	220.4	166.1
37	29.6	22.3	97	77.5	58.4	7	125.4	94.5	7	173.3	130.6	7	221.2	166.7
38	30.3	22.9	98	78.3	59.	8	126.2	95.1	8	174.1	131.2	8	222.	167.3
39	31.1	23.5	99	79.1	59.6	9	127.	95.7	9	174.9	131.8	9	222.8	167.9
40	31.9	24.1	100	79.9	60.2	160	127.8	96.3	220	175.7	132.4	280	223.6	168.5
41	32.7	24.7	1	80.7	60.8	1	128.6	96.9	1	176.5	133.	1	224.4	169.1
42	33.5	25.3	2	81.5	61.4	2	129.4	97.5	2	177.3	133.6	2	225.2	169.7
43	34.3	25.9	3	82.3	62.	3	130.2	98.1	3	178.1	134.2	3	226.	170.3
44	35.1	26.5	4	83.1	62.6	4	131.	98.7	4	178.9	134.8	4	226.8	170.9
45	35.9	27.1	5	83.9	63.2	5	131.8	99.3	5	179.7	135.4	5	227.6	171.5
46	36.7	27.7	6	84.7	63.8	6	132.6	99.9	6	180.5	136.	6	228.4	172.1
47	37.5	28.3	7	85.5	64.4	7	133.4	100.5	7	181.3	136.6	7	229.2	172.7
48	38.3	28.9	8	86.3	65.	8	134.2	101.1	8	182.1	137.2	8	230.	173.3
49	39.1	29.5	9	87.1	65.6	9	135.	101.7	9	182.9	137.8	9	230.8	173.9
50	39.9	30.1	110	87.8	66.2	170	135.8	102.3	230	183.7	138.4	290	231.6	174.5
51	40.7	30.7	1	88.6	66.8	1	136.6	102.9	1	184.5	139.	1	232.4	175.1
52	41.5	31.3	2	89.4	67.4	2	137.4	103.5	2	185.3	139.6	2	233.2	175.7
53	42.3	31.9	3	90.2	68.	3	138.2	104.1	3	186.1	140.2	3	234.	176.3
54	43.1	32.5	4	91.	68.6	4	139.	104.7	4	186.9	140.8	4	234.8	176.9
55	43.9	33.1	5	91.8	69.2	5	139.8	105.3	5	187.7	141.4	5	235.6	177.5
56	44.7	33.7	6	92.6	69.8	6	140.6	105.9	6	188.5	142.	6	236.4	178.1
57	45.5	34.3	7	93.4	70.4	7	141.4	106.5	7	189.3	142.6	7	237.2	178.7
58	46.3	34.9	8	94.2	71.	8	142.2	107.1	8	190.1	143.2	8	238.	179.3
59	47.1	35.5	9	95.	71.6	9	143.	107.7	9	190.9	143.8	9	238.8	179.9
60	47.9	36.1	190	95.8	72.2	190	143.8	108.3	240	191.7	144.4	300	239.6	180.5
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Dist. Latitude.

Course 53°.

Course 30°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	48.1	37.6	121	95.3	74.5	181	142.6	111.4	241	189.9	148.4
2	1.6	1.2	62	48.9	38.2	2	96.1	75.1	2	143.4	112.1	3	190.7	149.
3	2.4	1.8	63	49.6	38.8	3	96.9	75.7	3	144.2	112.7	4	191.5	149.6
4	3.2	2.5	64	50.4	39.4	4	97.7	76.3	4	145.	113.3	5	192.3	150.2
5	3.9	3.1	65	51.2	40.	5	98.5	77.	5	145.8	113.9	6	193.1	150.8
6	4.7	3.7	66	52.	40.6	6	99.3	77.6	6	146.6	114.6	7	193.9	151.5
7	5.5	4.3	67	52.8	41.2	7	100.1	78.2	7	147.4	115.1	8	194.6	152.1
8	6.3	4.9	68	53.6	41.9	8	100.9	78.8	8	148.1	115.7	9	195.4	152.7
9	7.1	5.5	69	54.4	42.5	9	101.7	79.4	9	148.9	116.4	10	196.2	153.3
10	7.9	6.2	70	55.2	43.1	130	102.4	80.	190	149.7	117.	290	197.	153.9
11	8.7	6.8	71	55.9	43.7	1	103.2	80.7	1	150.5	117.6	1	197.8	154.5
12	9.5	7.4	72	56.7	44.3	2	104.	81.2	2	151.3	118.2	2	198.6	155.1
13	10.2	8.	73	57.5	44.9	3	104.8	81.9	3	152.1	118.8	3	199.4	155.8
14	11.	8.6	74	58.3	45.6	4	105.6	82.5	4	152.9	119.4	4	200.2	156.4
15	11.8	9.2	75	59.1	46.2	5	106.4	83.1	5	153.7	120.1	5	200.9	157.
16	12.6	9.9	76	59.9	46.8	6	107.2	83.7	6	154.5	120.7	6	201.7	157.6
17	13.4	10.5	77	60.7	47.4	7	108.	84.3	7	155.2	121.3	7	202.5	158.2
18	14.2	11.1	78	61.5	48.	8	108.7	85.	8	156.	121.9	8	203.3	158.8
19	15.	11.7	79	62.3	48.6	9	109.5	85.6	9	156.8	122.5	9	204.1	159.5
20	15.8	12.3	80	63.	49.2	140	110.3	86.3	200	157.6	123.1	300	204.9	160.1
21	16.5	12.9	81	63.8	49.9	1	111.1	86.9	1	158.4	123.7	1	205.7	160.7
22	17.3	13.5	82	64.6	50.5	2	111.9	87.4	2	159.2	124.3	2	206.5	161.3
23	18.1	14.2	83	65.4	51.1	3	112.7	88.	3	160.	125.	3	207.3	161.9
24	18.9	14.8	84	66.2	51.7	4	113.5	88.7	4	160.8	125.6	4	208.	162.5
25	19.7	15.4	85	67.	52.3	5	114.3	89.3	5	161.5	126.2	5	208.8	163.1
26	20.5	16.	86	67.8	52.9	6	115.	89.9	6	162.3	126.8	6	209.6	163.7
27	21.3	16.6	87	68.6	53.6	7	115.8	90.5	7	163.1	127.4	7	210.4	164.4
28	22.1	17.2	88	69.3	54.2	8	116.6	91.1	8	163.9	128.	8	211.2	165.
29	22.9	17.9	89	70.1	54.8	9	117.4	91.7	9	164.7	128.7	9	212.	165.6
30	23.6	18.5	90	70.9	55.4	150	118.2	92.3	210	165.5	129.3	310	212.8	166.2
31	24.4	19.1	91	71.7	56.	1	119.	93.	1	166.3	129.9	1	213.6	166.8
32	25.2	19.7	92	72.5	56.6	2	119.8	93.6	2	167.1	130.5	2	214.3	167.5
33	26.	20.3	93	73.3	57.3	3	120.6	94.3	3	167.9	131.1	3	215.1	168.1
34	26.8	20.9	94	74.1	57.9	4	121.4	94.9	4	168.6	131.8	4	215.9	168.7
35	27.6	21.5	95	74.9	58.5	5	122.1	95.4	5	169.4	132.4	5	216.7	169.3
36	28.4	22.2	96	75.6	59.1	6	122.9	96.	6	170.2	133.	6	217.5	169.9
37	29.2	22.8	97	76.4	59.7	7	123.7	96.7	7	171.	133.6	7	218.3	170.5
38	29.9	23.4	98	77.2	60.3	8	124.5	97.3	8	171.8	134.2	8	219.1	171.1
39	30.7	24.	99	78.	61.	9	125.3	97.9	9	172.6	134.8	9	219.9	171.8
40	31.5	24.6	100	78.8	61.6	160	126.1	98.5	260	173.4	135.4	360	220.6	172.4
41	32.3	25.2	1	79.6	62.2	1	126.9	99.1	1	174.2	136.1	1	221.4	173.
42	33.1	25.9	2	80.4	62.8	2	127.7	99.7	2	174.9	136.7	2	222.2	173.6
43	33.9	26.5	3	81.3	63.4	3	128.4	100.4	3	175.7	137.3	3	223.	174.2
44	34.7	27.1	4	82.	64.	4	129.2	101.	4	176.5	137.9	4	223.8	174.8
45	35.5	27.7	5	82.7	64.6	5	130.	101.6	5	177.3	138.5	5	224.6	175.4
46	36.3	28.3	6	83.5	65.3	6	130.8	102.2	6	178.1	139.1	6	225.4	176.1
47	37.	28.9	7	84.3	65.9	7	131.6	102.8	7	178.9	139.7	7	226.2	176.7
48	37.8	29.6	8	85.1	66.5	8	132.4	103.4	8	179.7	140.4	8	227.	177.3
49	38.6	30.2	9	85.9	67.1	9	133.2	104.	9	180.5	141.	9	227.7	177.9
50	39.4	30.8	110	86.7	67.7	170	134.	104.7	230	181.3	141.8	300	228.5	178.5
51	40.2	31.4	1	87.5	68.3	1	134.7	105.3	1	182.	142.5	1	229.3	179.1
52	41.	32.	2	88.3	69.	2	135.5	105.9	2	182.8	143.1	2	230.1	179.7
53	41.8	32.6	3	89.	69.6	3	136.3	106.5	3	183.6	143.7	3	230.9	180.4
54	42.6	33.2	4	89.8	70.2	4	137.1	107.1	4	184.4	144.1	4	231.7	181.
55	43.3	33.9	5	90.6	70.8	5	137.9	107.7	5	185.2	144.7	5	232.5	181.6
56	44.1	34.5	6	91.4	71.4	6	138.7	108.4	6	186.	145.3	6	233.3	182.2
57	44.9	35.1	7	92.2	72.	7	139.5	109.	7	186.8	145.9	7	234.	182.9
58	45.7	35.7	8	93.	72.6	8	140.3	109.6	8	187.5	146.5	8	234.8	183.5
59	46.5	36.3	9	93.8	73.3	9	141.1	110.2	9	188.3	147.1	9	235.6	184.1
60	47.3	36.9	130	94.6	73.9	180	141.8	110.8	240	189.1	147.8	300	236.4	184.7
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 50°.

Course 39°

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	47.4	38.4	131	94.	76.1	181	140.7	113.9	241	187.3	151.7
2	1.6	1.3	62	48.2	39.	2	94.8	76.8	2	141.4	114.5	3	188.1	152.3
3	2.3	1.9	63	49.	39.6	3	95.6	77.4	3	142.9	115.3	3	188.8	152.9
4	3.1	2.5	64	49.7	40.3	4	96.4	78.	4	143.	115.8	4	189.6	153.6
5	3.9	3.1	65	50.5	40.9	5	97.1	78.7	5	143.8	116.4	5	190.4	154.2
6	4.7	3.8	66	51.3	41.5	6	97.9	79.3	6	144.5	117.1	6	191.2	154.8
7	5.4	4.4	67	52.1	42.2	7	98.7	79.9	7	145.3	117.7	7	192.	155.4
8	6.2	5.	68	52.8	42.8	8	99.5	80.6	8	146.1	118.3	8	192.7	156.1
9	7.	5.7	69	53.6	43.4	9	100.3	81.2	9	146.9	118.9	9	193.5	156.7
10	7.8	6.3	70	54.4	44.1	130	101.	81.8	190	147.7	119.6	250	194.3	157.3
11	8.5	6.9	71	55.2	44.7	1	101.8	82.4	1	148.4	120.2	1	195.1	158.
12	9.3	7.6	72	56.	45.3	2	102.6	83.1	2	149.2	120.8	2	195.8	158.6
13	10.1	8.2	73	56.7	45.9	3	103.4	83.7	3	150.	121.5	3	196.6	159.2
14	10.9	8.8	74	57.5	46.6	4	104.1	84.3	4	150.8	122.1	4	197.4	159.8
15	11.7	9.4	75	58.3	47.2	5	104.9	85.	5	151.5	122.7	5	198.2	160.5
16	12.4	10.1	76	59.1	47.8	6	105.7	85.6	6	152.3	123.3	6	199.0	161.1
17	13.2	10.7	77	59.8	48.5	7	106.5	86.2	7	153.1	124.	7	199.7	161.7
18	14.	11.3	78	60.6	49.1	8	107.3	86.8	8	153.9	124.6	8	200.5	162.4
19	14.8	12.	79	61.4	49.7	9	108.	87.5	9	154.7	125.2	9	201.3	163.
20	15.5	12.6	80	62.2	50.3	140	108.8	88.1	200	155.4	125.9	260	202.1	163.6
21	16.3	13.2	81	62.9	51.	1	109.6	88.7	1	156.2	126.5	1	202.8	164.3
22	17.1	13.8	82	63.7	51.6	2	110.4	89.4	2	157.	127.1	2	203.6	164.9
23	17.9	14.5	83	64.5	52.2	3	111.1	90.	3	157.8	127.8	3	204.4	165.5
24	18.7	15.1	84	65.3	52.9	4	111.9	90.6	4	158.5	128.4	4	205.2	166.1
25	19.4	15.7	85	66.1	53.5	5	112.7	91.3	5	159.3	129.	5	206.0	166.8
26	20.2	16.4	86	66.8	54.1	6	113.5	91.9	6	160.1	129.6	6	206.7	167.4
27	21.	17.	87	67.6	54.8	7	114.3	92.5	7	160.9	130.3	7	207.5	168.
28	21.8	17.6	88	68.4	55.4	8	115.	93.1	8	161.6	130.9	8	208.3	168.7
29	22.6	18.3	89	69.2	56.	9	115.8	93.8	9	162.4	131.5	9	209.1	169.3
30	23.3	18.9	90	69.9	56.6	150	116.6	94.4	210	163.2	132.2	270	209.8	169.9
31	24.1	19.5	91	70.7	57.3	1	117.3	95.	1	164.	132.8	1	210.6	170.5
32	24.9	20.1	92	71.5	57.9	2	118.1	95.7	2	164.8	133.4	2	211.4	171.1
33	25.6	20.8	93	72.3	58.5	3	118.9	96.3	3	165.5	134.	3	212.2	171.8
34	26.4	21.4	94	73.1	59.2	4	119.7	96.9	4	166.3	134.7	4	213.0	172.4
35	27.3	22.	95	73.8	59.8	5	120.5	97.5	5	167.1	135.3	5	213.7	173.1
36	28.	22.7	96	74.6	60.4	6	121.3	98.2	6	167.9	135.9	6	214.5	173.7
37	28.8	23.3	97	75.4	61.	7	122.	98.8	7	168.6	136.6	7	215.3	174.3
38	29.5	23.9	98	76.2	61.7	8	122.8	99.4	8	169.4	137.2	8	216.	175.
39	30.3	24.5	99	76.9	62.3	9	123.6	100.1	9	170.2	137.8	9	216.8	175.6
40	31.1	25.2	100	77.7	62.9	160	124.3	100.7	220	171.	138.5	280	217.6	176.3
41	31.9	25.8	1	78.5	63.6	1	125.1	101.3	1	171.7	139.1	1	218.4	176.8
42	32.6	26.4	2	79.3	64.2	2	125.9	101.9	2	172.5	139.7	2	219.2	177.5
43	33.4	27.1	3	80.	64.8	3	126.7	102.6	3	173.3	140.3	3	219.9	178.1
44	34.2	27.7	4	80.8	65.4	4	127.5	103.2	4	174.1	141.	4	220.7	178.7
45	35.	28.3	5	81.6	66.1	5	128.3	103.8	5	174.9	141.6	5	221.5	179.4
46	35.7	28.9	6	82.4	66.7	6	129.	104.5	6	175.6	142.2	6	222.3	180.
47	36.5	29.6	7	83.2	67.3	7	129.8	105.1	7	176.4	142.9	7	223.	180.6
48	37.3	30.2	8	83.9	68.	8	130.6	105.7	8	177.2	143.5	8	223.8	181.2
49	38.1	30.8	9	84.7	68.6	9	131.3	106.4	9	178.	144.1	9	224.6	181.9
50	38.9	31.5	110	85.5	69.2	170	132.1	107.	230	178.7	144.7	290	225.4	182.5
51	39.6	32.1	1	86.3	69.9	1	132.9	107.6	1	179.5	145.4	1	226.1	183.1
52	40.4	32.7	2	87.	70.5	2	133.7	108.2	2	180.3	146.	2	226.9	183.8
53	41.2	33.4	3	87.8	71.1	3	134.4	108.9	3	181.1	146.6	3	227.7	184.4
54	42.	34.	4	88.6	71.7	4	135.2	109.5	4	181.9	147.3	4	228.5	185.
55	42.7	34.6	5	89.4	72.4	5	136.	110.1	5	182.6	147.9	5	229.3	185.6
56	43.5	35.2	6	90.1	73.	6	136.8	110.8	6	183.4	148.5	6	230.	186.3
57	44.3	35.9	7	90.9	73.6	7	137.6	111.4	7	184.2	149.1	7	230.8	186.9
58	45.1	36.5	8	91.7	74.3	8	138.3	112.	8	185.	149.8	8	231.6	187.5
59	45.9	37.1	9	92.5	74.9	9	139.1	112.6	9	185.7	150.4	9	232.4	188.2
60	46.6	37.8	190	93.3	75.5	190	139.9	113.3	240	186.5	151.	300	233.1	188.8
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 51°.

Course 40°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.6	61	46.7	39.9	181	92.7	77.8	181	138.7	116.3	241	184.6	154.9
2	1.5	1.3	62	47.5	39.9	2	93.5	78.4	2	139.4	117.	2	185.4	155.6
3	2.3	1.9	63	48.3	40.5	3	94.9	79.1	3	140.3	117.6	3	186.1	156.2
4	3.1	2.6	64	49.	41.1	4	95.	79.7	4	141.	118.3	4	186.9	156.8
5	3.8	3.2	65	49.8	41.8	5	95.8	80.3	5	141.7	118.9	5	187.7	157.5
6	4.6	3.9	66	50.6	42.4	6	96.5	81.	6	142.5	119.6	6	188.4	158.1
7	5.4	4.5	67	51.3	43.1	7	97.3	81.6	7	143.3	120.2	7	189.2	158.8
8	6.1	5.1	68	52.1	43.7	8	98.1	82.3	8	144.	120.8	8	190.	159.4
9	6.9	5.8	69	52.9	44.4	9	98.8	82.9	9	144.8	121.5	9	190.7	160.1
10	7.7	6.4	70	53.6	45.	130	99.6	83.6	100	145.5	122.1	250	191.5	160.7
11	8.4	7.1	71	54.4	45.6	1	100.4	84.3	1	146.3	122.8	1	192.3	161.3
12	9.2	7.7	72	55.2	46.3	2	101.1	84.8	2	147.1	123.4	2	193.	162.
13	10.	8.4	73	55.9	46.9	3	101.9	85.5	3	147.8	124.1	3	193.8	162.6
14	10.7	9.	74	56.7	47.6	4	102.6	86.1	4	148.6	124.7	4	194.6	163.3
15	11.5	9.6	75	57.5	48.2	5	103.4	86.8	5	149.4	125.3	5	195.3	163.9
16	12.3	10.3	76	58.3	48.9	6	104.2	87.4	6	150.1	126.	6	196.1	164.6
17	13.	10.9	77	59.	49.5	7	104.9	88.1	7	150.9	126.6	7	196.9	165.2
18	13.8	11.6	78	59.8	50.1	8	105.7	88.7	8	151.7	127.3	8	197.6	165.8
19	14.6	12.2	79	60.5	50.8	9	106.5	89.3	9	152.4	127.9	9	198.4	166.5
20	15.3	12.9	80	61.3	51.4	140	107.2	90.	200	153.2	128.6	260	199.2	167.1
21	16.1	13.5	81	62.	52.1	1	108.	90.6	1	154.	129.2	1	199.9	167.8
22	16.9	14.1	82	62.8	52.7	2	108.8	91.3	2	154.7	129.8	2	200.7	168.4
23	17.6	14.6	83	63.6	53.4	3	109.5	91.9	3	155.5	130.5	3	201.5	169.1
24	18.4	15.4	84	64.3	54.	4	110.3	92.6	4	156.3	131.1	4	202.3	169.7
25	19.2	16.1	85	65.1	54.6	5	111.1	93.2	5	157.	131.8	5	203.	170.3
26	19.9	16.7	86	65.9	55.3	6	111.8	93.8	6	157.8	132.4	6	203.8	171.
27	20.7	17.4	87	66.6	55.9	7	112.6	94.5	7	158.6	133.1	7	204.5	171.6
28	21.4	18.	88	67.4	56.6	8	113.4	95.1	8	159.3	133.7	8	205.3	172.3
29	22.2	18.6	89	68.2	57.3	9	114.1	95.8	9	160.1	134.3	9	206.1	172.9
30	23.	19.3	90	68.9	57.9	150	114.9	96.4	210	160.9	135.	270	206.8	173.6
31	23.7	19.9	91	69.7	58.5	1	115.7	97.1	1	161.6	135.6	1	207.6	174.2
32	24.5	20.6	92	70.5	59.1	2	116.4	97.7	2	162.4	136.3	2	208.4	174.8
33	25.3	21.2	93	71.3	59.8	3	117.2	98.3	3	163.3	136.9	3	209.1	175.5
34	26.	21.9	94	72.	60.4	4	118.	99.	4	163.9	137.6	4	209.9	176.1
35	26.8	22.5	95	72.8	61.1	5	118.7	99.6	5	164.7	138.2	5	210.7	176.8
36	27.6	23.1	96	73.5	61.7	6	119.5	100.3	6	165.5	138.8	6	211.4	177.4
37	28.3	23.8	97	74.3	62.4	7	120.3	100.9	7	166.3	139.5	7	212.2	178.1
38	29.1	24.4	98	75.1	63.	8	121.	101.6	8	167.	140.1	8	213.	178.7
39	29.9	25.1	99	75.8	63.6	9	121.8	102.2	9	167.8	140.8	9	213.7	179.3
40	30.6	25.7	100	76.6	64.3	160	122.6	102.8	220	168.5	141.4	280	214.5	180.
41	31.4	26.4	1	77.4	64.9	1	123.3	103.5	1	169.3	142.1	1	215.3	180.6
42	32.2	27.	2	78.1	65.6	2	124.1	104.1	2	170.1	142.7	2	216.	181.3
43	32.9	27.6	3	78.9	66.3	3	124.9	104.8	3	170.8	143.3	3	216.8	181.9
44	33.7	28.3	4	79.7	66.8	4	125.6	105.4	4	171.6	144.	4	217.6	182.6
45	34.5	28.9	5	80.4	67.5	5	126.4	106.1	5	172.4	144.6	5	218.3	183.2
46	35.2	29.6	6	81.2	68.1	6	127.2	106.7	6	173.1	145.3	6	219.1	183.8
47	36.	30.3	7	82.	68.8	7	127.9	107.3	7	173.9	145.9	7	219.9	184.5
48	36.8	30.9	8	82.7	69.4	8	128.7	108.	8	174.7	146.6	8	220.6	185.1
49	37.5	31.5	9	83.5	70.1	9	129.5	108.6	9	175.4	147.2	9	221.4	185.8
50	38.3	32.1	110	84.3	70.7	170	130.2	109.3	230	176.2	147.8	290	222.2	186.4
51	39.1	32.8	1	85.	71.3	1	131.	109.9	1	177.	148.5	1	223.0	187.1
52	39.8	33.4	2	85.8	72.	2	131.8	110.6	2	177.7	149.1	2	223.7	187.7
53	40.6	34.1	3	86.6	72.6	3	132.5	111.2	3	178.5	149.8	3	224.5	188.3
54	41.4	34.7	4	87.3	73.3	4	133.3	111.8	4	179.3	150.4	4	225.2	189.
55	42.1	35.4	5	88.1	73.9	5	134.1	112.5	5	180.	151.1	5	226.	189.6
56	42.9	36.	6	88.9	74.6	6	134.8	113.1	6	180.8	151.7	6	226.7	190.3
57	43.7	36.6	7	89.6	75.2	7	135.6	113.8	7	181.6	152.3	7	227.5	190.9
58	44.4	37.3	8	90.4	75.8	8	136.4	114.4	8	182.3	153.	8	228.3	191.6
59	45.2	37.9	9	91.2	76.5	9	137.1	115.1	9	183.1	153.6	9	229.	192.3
60	46.	38.6	130	91.9	77.1	180	137.9	115.7	240	183.9	154.2	300	229.8	192.9
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 50°.

TABLE V.

Course 41°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.8	0.7	61	46.	40.	121	91.3	79.4	181	136.6	118.7	241	181.9	158.1
2	1.5	1.3	62	46.8	40.7	2	92.1	80.	2	137.4	119.4	2	182.6	158.8
3	2.3	2.	63	47.5	41.3	3	92.8	80.7	3	138.1	120.1	3	183.4	159.4
4	3.	2.6	64	48.3	42.	4	93.6	81.4	4	138.9	120.7	4	184.1	160.1
5	3.8	3.3	65	49.1	42.6	5	94.3	82.	5	139.6	121.4	5	184.9	160.7
6	4.5	3.9	66	49.8	43.3	6	95.1	82.7	6	140.4	122.	6	185.7	161.4
7	5.3	4.6	67	50.6	44.	7	95.8	83.3	7	141.1	122.7	7	186.4	162.
8	6.	5.2	68	51.3	44.6	8	96.6	84.	8	141.9	123.3	8	187.2	162.7
9	6.8	5.9	69	52.1	45.3	9	97.4	84.6	9	142.6	124.	9	187.9	163.4
10	7.5	6.6	70	52.8	45.9	130	98.1	85.3	100	143.4	124.7	250	188.7	164.
11	8.3	7.2	71	53.6	46.6	1	98.9	85.9	1	144.1	125.3	1	189.4	164.7
12	9.1	7.9	72	54.3	47.2	2	99.6	86.6	2	144.9	126.	2	190.2	165.3
13	9.8	8.5	73	55.1	47.9	3	100.4	87.3	3	145.7	126.6	3	190.9	166.
14	10.6	9.2	74	55.8	48.5	4	101.1	87.9	4	146.4	127.3	4	191.7	166.6
15	11.3	9.8	75	56.6	49.2	5	101.9	88.6	5	147.2	127.9	5	192.5	167.3
16	12.1	10.5	76	57.4	49.9	6	102.6	89.2	6	147.9	128.6	6	193.3	168.
17	12.8	11.2	77	58.1	50.5	7	103.4	89.9	7	148.7	129.2	7	194.	168.6
18	13.6	11.8	78	58.9	51.2	8	104.1	90.5	8	149.4	129.9	8	194.7	169.3
19	14.3	12.5	79	59.6	51.8	9	104.9	91.2	9	150.2	130.6	9	195.5	169.9
20	15.1	13.1	80	60.4	52.5	140	105.7	91.8	200	150.9	131.2	260	196.3	170.6
21	15.8	13.8	81	61.1	53.1	1	106.4	92.5	1	151.7	131.9	1	197.	171.3
22	16.6	14.4	82	61.9	53.8	2	107.2	93.2	2	152.5	132.5	2	197.7	171.9
23	17.4	15.1	83	62.6	54.5	3	107.9	93.8	3	153.3	133.2	3	198.5	172.5
24	18.1	15.7	84	63.4	55.1	4	108.7	94.5	4	154.	133.8	4	199.2	173.2
25	18.9	16.4	85	64.2	55.8	5	109.4	95.1	5	154.7	134.5	5	200.	173.9
26	19.6	17.1	86	64.9	56.4	6	110.2	95.8	6	155.5	135.1	6	200.8	174.5
27	20.4	17.7	87	65.7	57.1	7	110.9	96.4	7	156.3	135.8	7	201.5	175.2
28	21.1	18.4	88	66.4	57.7	8	111.7	97.1	8	157.	136.5	8	202.3	175.8
29	21.9	19.	89	67.2	58.4	9	112.5	97.8	9	157.7	137.1	9	203.	176.5
30	22.6	19.7	90	67.9	59.	150	113.2	98.4	210	158.5	137.8	270	203.8	177.1
31	23.4	20.3	91	68.7	59.7	1	114.	99.1	1	159.2	138.4	1	204.5	177.6
32	24.2	21.	92	69.4	60.4	2	114.7	99.7	2	160.	139.1	2	205.3	178.4
33	24.9	21.6	93	70.2	61.	3	115.5	100.4	3	160.8	139.7	3	206.	179.1
34	25.7	22.3	94	70.9	61.7	4	116.2	101.	4	161.5	140.4	4	206.8	179.8
35	26.4	23.	95	71.7	62.3	5	117.	101.7	5	162.3	141.1	5	207.5	180.4
36	27.2	23.6	96	72.5	63.	6	117.7	102.3	6	163.	141.7	6	208.3	181.1
37	27.9	24.3	97	73.2	63.6	7	118.5	103.	7	163.8	142.4	7	209.1	181.7
38	28.7	24.9	98	74.	64.3	8	119.3	103.7	8	164.5	143.	8	209.8	182.4
39	29.4	25.6	99	74.7	64.9	9	120.	104.3	9	165.3	143.7	9	210.6	183.
40	30.2	26.3	100	75.5	65.6	160	120.8	105.	220	166.	144.3	280	211.3	183.7
41	30.9	26.9	1	76.2	66.3	1	121.5	105.6	1	166.8	145.	1	212.1	184.4
42	31.7	27.6	2	77.	66.9	2	122.3	106.3	2	167.5	145.6	2	212.8	185.
43	32.5	28.2	3	77.7	67.6	3	123.	106.9	3	168.3	146.3	3	213.6	185.7
44	33.2	28.9	4	78.5	68.2	4	123.8	107.6	4	169.1	147.	4	214.3	186.3
45	34.	29.5	5	79.2	68.9	5	124.5	108.2	5	169.8	147.6	5	215.1	187.
46	34.7	30.2	6	80.	69.5	6	125.3	108.9	6	170.6	148.3	6	215.8	187.6
47	35.5	30.8	7	80.8	70.2	7	126.	109.6	7	171.3	148.9	7	216.6	188.3
48	36.2	31.5	8	81.5	70.9	8	126.8	110.2	8	172.1	149.6	8	217.4	188.9
49	37.	32.1	9	82.3	71.5	9	127.5	110.9	9	172.8	150.3	9	218.1	189.6
50	37.7	32.8	110	83.	72.2	170	128.3	111.5	230	173.6	150.9	290	218.9	190.3
51	38.5	33.5	1	83.8	72.8	1	129.1	112.2	1	174.3	151.5	1	219.6	190.9
52	39.2	34.1	2	84.5	73.5	2	129.8	112.8	2	175.1	152.2	2	220.4	191.6
53	40.	34.8	3	85.3	74.1	3	130.6	113.5	3	175.8	152.9	3	221.1	192.2
54	40.8	35.4	4	86.	74.8	4	131.3	114.2	4	176.6	153.5	4	221.9	192.9
55	41.5	36.1	5	86.8	75.4	5	132.1	114.8	5	177.4	154.2	5	222.6	193.5
56	42.3	36.7	6	87.5	76.1	6	132.8	115.5	6	178.1	154.8	6	223.4	194.2
57	43.	37.4	7	88.3	76.8	7	133.6	116.1	7	178.9	155.5	7	224.1	194.8
58	43.8	38.1	8	89.1	77.4	8	134.3	116.8	8	179.6	156.1	8	224.9	195.5
59	44.5	38.7	9	89.8	78.1	9	135.1	117.4	9	180.4	156.8	9	225.7	196.2
60	45.3	39.4	120	90.6	78.7	180	135.8	118.1	240	181.1	157.5	300	226.4	196.8
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 40°.

COURSE 49°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.7	0.7	61	45.3	40.8	121	80.9	81.	181	134.5	121.1	241	179.1	161.3
2	1.5	1.3	62	46.1	41.5	2	90.7	81.6	3	125.3	121.8	9	179.2	161.9
3	2.3	2.	63	46.8	42.2	3	91.4	82.3	3	126.	122.5	3	180.6	162.6
4	3.	2.7	64	47.6	42.8	4	92.1	83.	4	126.7	123.1	4	181.3	163.3
5	3.7	3.3	65	48.3	43.5	5	92.9	83.6	5	127.5	123.8	5	182.1	163.9
6	4.5	4.	66	49.	44.2	6	93.6	84.3	6	128.3	124.5	6	182.8	164.6
7	5.3	4.7	67	49.5	44.8	7	94.4	85.	7	129.	125.1	7	183.6	165.3
8	5.9	5.4	68	50.5	45.5	8	95.1	85.6	8	129.7	125.8	8	184.3	165.9
9	6.7	6.	69	51.3	46.2	9	95.9	86.3	9	130.5	126.5	9	185.	166.6
10	7.4	6.7	70	52.	46.8	130	96.6	87.	190	141.3	127.1	250	185.8	167.3
11	8.2	7.4	71	52.8	47.5	1	97.4	87.7	1	141.9	127.8	1	186.5	168.
12	8.9	8.	72	53.5	48.2	2	98.1	88.3	2	142.7	128.5	2	187.3	168.6
13	9.7	8.7	73	54.2	48.8	3	98.8	89.	3	143.4	129.1	3	188.	169.3
14	10.4	9.4	74	55.	49.5	4	99.6	89.7	4	144.2	129.8	4	188.8	170.
15	11.1	10.	75	55.7	50.2	5	100.3	90.3	5	144.9	130.5	5	189.5	170.6
16	11.9	10.7	76	56.5	50.9	6	101.1	91.	6	145.7	131.1	6	190.2	171.3
17	12.6	11.4	77	57.2	51.5	7	101.8	91.7	7	146.4	131.8	7	191.	172.
18	13.4	12.	78	58.	52.2	8	102.6	92.3	8	147.1	132.5	8	191.7	172.6
19	14.1	12.7	79	58.7	52.9	9	103.3	93.	9	147.9	133.2	9	192.5	173.3
20	14.9	13.4	80	59.5	53.5	140	104.	93.7	200	148.6	133.8	260	193.2	174.
21	15.6	14.1	81	60.2	54.2	1	104.8	94.3	1	149.4	134.5	1	194.	174.6
22	16.3	14.7	82	60.9	54.9	2	105.5	95.	2	150.1	135.2	2	194.7	175.3
23	17.1	15.4	83	61.7	55.5	3	106.3	95.7	3	150.9	135.8	3	195.4	176.
24	17.8	16.1	84	62.4	56.2	4	107.	96.4	4	151.6	136.5	4	196.2	176.7
25	18.6	16.7	85	63.2	56.9	5	107.8	97.	5	152.3	137.2	5	196.9	177.3
26	19.3	17.4	86	63.9	57.5	6	108.5	97.7	6	153.1	137.8	6	197.7	178.
27	20.1	18.1	87	64.7	58.2	7	109.2	98.4	7	153.8	138.5	7	198.4	178.7
28	20.8	18.7	88	65.4	58.9	8	110.	99.	8	154.6	139.2	8	199.2	179.3
29	21.6	19.4	89	66.1	59.6	9	110.7	99.7	9	155.3	139.8	9	199.9	180.
30	22.3	20.1	90	66.9	60.2	150	111.5	100.4	210	156.1	140.5	270	200.6	180.7
31	23.	20.7	91	67.6	60.9	1	112.2	101.	1	156.8	141.2	1	201.4	181.3
32	23.8	21.4	92	68.4	61.6	2	113.	101.7	2	157.5	141.9	2	202.1	182.
33	24.5	22.1	93	69.1	62.2	3	113.7	102.4	3	158.3	142.5	3	202.9	182.7
34	25.3	22.8	94	69.9	62.9	4	114.4	103.	4	159.	143.2	4	203.6	183.3
35	26.	23.4	95	70.6	63.6	5	115.2	103.7	5	159.8	143.9	5	204.4	184.
36	26.8	24.1	96	71.2	64.2	6	115.9	104.4	6	160.5	144.6	6	205.1	184.7
37	27.5	24.8	97	71.9	64.9	7	116.7	105.1	7	161.3	145.2	7	205.9	185.3
38	28.2	25.4	98	72.6	65.6	8	117.4	105.7	8	162.	145.9	8	206.6	186.
39	29.	26.1	99	73.6	66.2	9	118.2	106.4	9	162.7	146.5	9	207.3	186.7
40	29.7	26.8	100	74.3	66.9	160	118.9	107.1	220	163.5	147.3	280	208.1	187.4
41	30.5	27.4	1	75.1	67.6	1	119.6	107.7	1	164.2	147.9	1	208.8	188.
42	31.2	28.1	2	75.8	68.3	2	120.4	108.4	2	165.	148.5	2	209.6	188.7
43	32.	28.8	3	76.5	68.9	3	121.1	109.1	3	165.7	149.2	3	210.3	189.4
44	32.7	29.4	4	77.3	69.6	4	121.9	109.7	4	166.5	149.9	4	211.1	190.
45	33.4	30.1	5	78.	70.3	5	122.6	110.4	5	167.2	150.6	5	211.8	190.7
46	34.2	30.8	6	78.8	70.9	6	123.4	111.1	6	168.	151.2	6	212.5	191.4
47	34.9	31.4	7	79.5	71.6	7	124.1	111.7	7	168.7	151.9	7	213.3	192.
48	35.7	32.1	8	80.3	72.2	8	124.8	112.4	8	169.4	152.6	8	214.	192.7
49	36.4	32.8	9	81.	72.9	9	125.6	113.1	9	170.2	153.2	9	214.8	193.4
50	37.2	33.5	110	81.7	73.6	170	126.3	113.8	230	170.9	153.9	290	215.5	194.
51	37.9	34.1	1	82.5	74.3	1	127.1	114.4	1	171.7	154.6	1	216.3	194.7
52	38.6	34.8	2	83.2	74.9	2	127.8	115.1	2	172.4	155.2	2	217.	195.4
53	39.4	35.5	3	84.	75.6	3	128.6	115.8	3	173.2	155.9	3	217.7	196.1
54	40.1	36.1	4	84.7	76.3	4	129.3	116.4	4	173.9	156.6	4	218.5	196.7
55	40.9	36.8	5	85.5	77.	5	130.1	117.1	5	174.6	157.2	5	219.2	197.4
56	41.6	37.5	6	86.2	77.6	6	130.8	117.8	6	175.4	157.9	6	220.	198.1
57	42.4	38.1	7	86.9	78.3	7	131.5	118.4	7	176.1	158.6	7	220.7	198.7
58	43.1	38.8	8	87.7	79.	8	132.3	119.1	8	176.9	159.3	8	221.5	199.4
59	43.8	39.5	9	88.4	79.6	9	133.	119.8	9	177.6	159.9	9	222.2	200.1
60	44.6	40.1	120	89.2	80.3	180	133.8	120.4	240	178.4	160.6	300	222.9	200.7

Distance, Departure and Diff. Latitude.

COURSE 49°.

Course 43°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.7	0.7	61	44.6	41.6	131	88.5	84.5	161	132.4	123.4	241	176.3	164.4
2	1.5	1.4	63	45.3	42.3	2	89.3	83.9	3	133.1	124.1	2	177.	165.
3	2.2	2.	65	46.1	43.	3	90.	83.9	3	133.8	124.8	3	177.7	165.7
4	2.9	2.7	67	46.8	43.6	4	90.7	84.6	4	134.5	125.5	4	178.5	166.4
5	3.7	3.4	69	47.5	44.3	5	91.4	85.3	5	135.2	126.2	5	179.2	167.1
6	4.4	4.1	71	48.3	45.	6	92.2	85.9	6	136.	126.9	6	179.9	167.8
7	5.1	4.8	73	49.	45.7	7	92.9	86.6	7	136.8	127.5	7	180.6	168.5
8	5.9	5.5	75	49.7	46.4	8	93.6	87.3	8	137.5	128.2	8	181.4	169.2
9	6.6	6.1	77	50.5	47.1	9	94.3	88.	9	138.2	128.9	9	182.1	169.9
10	7.3	6.8	79	51.2	47.7	130	95.1	88.7	190	139.	129.6	280	182.8	170.5
11	8.	7.5	71	51.9	48.4	1	95.8	89.3	1	139.7	130.3	1	183.6	171.2
12	8.8	8.2	73	52.7	49.1	2	96.5	90.	2	140.4	130.9	2	184.3	171.9
13	9.5	8.9	75	53.4	49.8	3	97.3	90.7	3	141.1	131.6	3	185.	172.5
14	10.2	9.5	77	54.1	50.5	4	98.	91.4	4	141.9	132.3	4	185.8	173.2
15	11.	10.2	79	54.9	51.1	5	98.7	92.1	5	142.6	133.	5	186.5	173.9
16	11.7	10.9	77	55.6	51.8	6	99.5	92.8	6	143.3	133.7	6	187.3	174.6
17	12.4	11.6	75	56.3	52.5	7	100.2	93.4	7	144.1	134.4	7	188.	175.3
18	13.2	12.3	73	57.	53.2	8	100.9	94.1	8	144.8	135.	8	188.7	176.
19	13.9	13.	71	57.8	53.9	9	101.7	94.8	9	145.5	135.7	9	189.4	176.6
20	14.6	13.6	80	58.5	54.6	140	102.4	95.5	200	146.3	136.4	300	190.2	177.3
21	15.4	14.3	81	59.2	55.2	1	103.1	96.2	1	147.	137.1	1	190.9	178.
22	16.1	15	83	60.	55.9	2	103.9	96.8	2	147.7	137.8	2	191.6	178.7
23	16.8	15.7	83	60.7	56.6	3	104.6	97.5	3	148.5	138.4	3	192.3	179.4
24	17.6	16.4	84	61.4	57.3	4	105.3	98.2	4	149.2	139.1	4	193.1	180.
25	18.3	17.	85	62.2	58.	5	106.	98.9	5	149.9	139.8	5	193.8	180.7
26	19.	17.7	86	62.9	58.7	6	106.8	99.6	6	150.7	140.5	6	194.5	181.4
27	19.7	18.4	87	63.6	59.3	7	107.5	100.3	7	151.4	141.2	7	195.3	182.1
28	20.5	19.1	88	64.4	60.	8	108.2	100.9	8	152.1	141.9	8	196.	182.8
29	21.2	19.8	89	65.1	60.7	9	109.	101.6	9	152.9	142.5	9	196.7	183.5
30	21.9	20.5	90	65.8	61.4	150	109.7	102.3	210	153.6	143.2	370	197.5	184.1
31	22.7	21.1	91	66.6	62.1	1	110.4	103.	1	154.3	143.9	1	198.2	184.8
32	23.4	21.8	92	67.3	62.7	2	111.2	103.7	2	155.	144.6	2	198.9	185.5
33	24.1	22.5	93	68.	63.4	3	111.9	104.3	3	155.8	145.3	3	199.7	186.2
34	24.9	23.2	94	68.7	64.1	4	112.6	105.	4	156.5	146.0	4	200.4	186.9
35	25.6	23.9	95	69.5	64.8	5	113.4	105.7	5	157.2	146.6	5	201.1	187.5
36	26.3	24.6	96	70.2	65.5	6	114.1	106.4	6	158.	147.3	6	201.9	188.2
37	27.1	25.2	97	70.9	66.2	7	114.8	107.1	7	158.7	148.	7	202.6	188.9
38	27.8	25.9	98	71.7	66.8	8	115.6	107.8	8	159.4	148.7	8	203.3	189.6
39	28.5	26.6	99	72.4	67.5	9	116.3	108.4	9	160.1	149.4	9	204.	190.3
40	29.3	27.3	100	73.1	68.2	160	117.	109.1	260	160.9	150.	360	204.8	191.
41	30.	28.	1	73.9	68.9	1	117.7	109.8	1	161.6	150.7	1	205.5	191.6
42	30.7	28.6	2	74.6	69.6	2	118.5	110.5	2	162.4	151.4	2	206.2	192.3
43	31.4	29.3	3	75.3	70.3	3	119.2	111.2	3	163.1	152.1	3	207.	193.
44	32.2	30.	4	76.1	70.9	4	119.9	111.8	4	163.8	152.8	4	207.7	193.7
45	32.9	30.7	5	76.8	71.6	5	120.7	112.5	5	164.6	153.4	5	208.4	194.4
46	33.6	31.4	6	77.5	72.3	6	121.4	113.2	6	165.3	154.1	6	209.2	195.1
47	34.4	32.1	7	78.3	73.	7	122.1	113.9	7	166.	154.8	7	209.9	195.7
48	35.1	32.7	8	79.	73.7	8	122.9	114.6	8	166.7	155.5	8	210.6	196.4
49	35.8	33.4	9	79.7	74.3	9	123.6	115.3	9	167.5	156.2	9	211.4	197.1
50	36.6	34.1	110	80.4	75.	170	124.3	115.9	270	168.2	156.9	390	212.1	197.8
51	37.3	34.8	1	81.2	75.7	1	125.1	116.6	1	168.9	157.5	1	212.8	198.4
52	38.	35.5	2	81.9	76.4	2	125.8	117.3	2	169.7	158.2	2	213.6	199.1
53	38.8	36.1	3	82.6	77.1	3	126.5	118.	3	170.4	158.9	3	214.3	199.8
54	39.5	36.8	4	83.4	77.7	4	127.3	118.7	4	171.1	159.6	4	215.	200.5
55	40.2	37.5	5	84.1	78.4	5	128.	119.3	5	171.9	160.3	5	215.7	201.2
56	41.	38.2	6	84.8	79.1	6	128.7	120.	6	172.6	161.	6	216.5	201.9
57	41.7	38.9	7	85.6	79.8	7	129.4	120.7	7	173.3	161.6	7	217.3	202.6
58	42.4	39.6	8	86.3	80.5	8	130.2	121.4	8	174.1	162.3	8	217.9	203.3
59	43.1	40.2	9	87.	81.2	9	130.9	122.1	9	174.8	163.	9	218.7	203.9
60	43.9	40.9	120	87.8	81.8	180	131.6	122.8	240	175.5	163.7	300	219.4	204.6
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude

Course 47°.

U

Course 44°.

Distance, Diff. Latitude and Departure.

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.7	0.7	61	43.0	42.4	121	87.	84.1	181	130.2	125.7	241	173.4	167.4
2	1.4	1.4	62	44.6	43.1	2	27.8	84.7	2	130.9	126.4	2	174.1	168.1
3	2.2	2.1	63	45.3	43.8	3	86.5	85.4	3	131.6	127.1	3	174.8	168.8
4	2.9	2.8	64	46.	44.5	4	89.2	86.1	4	132.4	127.8	4	175.5	169.5
5	3.6	3.5	65	46.8	45.2	5	89.9	86.8	5	133.1	128.5	5	176.2	170.2
6	4.3	4.2	66	47.5	45.8	6	90.6	87.5	6	133.8	129.2	6	177.	170.9
7	5.	4.9	67	48.2	46.5	7	91.4	88.2	7	134.5	129.9	7	177.7	171.6
8	5.8	5.6	68	48.9	47.2	8	92.1	88.9	8	135.2	130.6	8	178.4	172.3
9	6.5	6.3	69	49.6	47.9	9	92.8	89.6	9	136.	131.3	9	179.1	173.
10	7.2	6.9	70	50.4	48.6	130	93.5	90.3	190	136.7	132.	250	179.8	173.7
11	7.9	7.6	71	51.1	49.3	1	94.2	91.	1	137.4	132.7	1	180.6	174.4
12	8.6	8.3	72	51.8	50.	2	95.	91.7	2	138.1	133.4	2	181.3	175.1
13	9.4	9.	73	52.5	50.7	3	95.7	92.4	3	138.8	134.1	3	182.	175.8
14	10.1	9.7	74	53.2	51.4	4	96.4	93.1	4	139.6	134.8	4	182.7	176.5
15	10.8	10.4	75	54.	52.1	5	97.1	93.8	5	140.3	135.5	5	183.4	177.1
16	11.5	11.1	76	54.7	52.8	6	97.8	94.5	6	141.	136.2	6	184.1	177.8
17	12.2	11.8	77	55.4	53.5	7	98.5	95.2	7	141.7	136.9	7	184.8	178.5
18	12.9	12.5	78	56.1	54.2	8	99.2	95.9	8	142.4	137.5	8	185.6	179.2
19	13.7	13.3	79	56.8	54.9	9	100.	96.6	9	143.1	138.2	9	186.3	179.9
20	14.4	13.9	80	57.5	55.6	140	100.7	97.3	200	143.9	138.9	260	187.	180.6
21	15.1	14.6	81	58.3	56.3	1	101.4	97.9	1	144.6	139.6	1	187.7	181.3
22	15.8	15.3	82	59.	57.	2	102.1	98.6	2	145.3	140.3	2	188.5	182.
23	16.5	16.	83	59.7	57.7	3	102.9	99.3	3	146.	141.	3	189.3	182.7
24	17.3	16.7	84	60.4	58.4	4	103.6	100.	4	146.7	141.7	4	189.9	183.4
25	18.	17.4	85	61.1	59.	5	104.3	100.7	5	147.5	142.4	5	190.6	184.1
26	18.7	18.1	86	61.9	59.7	6	105.	101.4	6	148.2	143.1	6	191.3	184.8
27	19.4	18.8	87	62.6	60.4	7	105.7	102.1	7	148.9	143.8	7	192.1	185.5
28	20.1	19.5	88	63.3	61.1	8	106.5	102.8	8	149.6	144.5	8	192.8	186.2
29	20.9	20.1	89	64.	61.8	9	107.2	103.5	9	150.3	145.2	9	193.5	186.9
30	21.6	20.8	90	64.7	62.5	150	107.9	104.2	210	151.1	145.9	270	194.2	187.6
31	22.3	21.5	91	65.5	63.2	1	108.6	104.9	1	151.8	146.6	1	194.9	188.3
32	23.	22.2	92	66.2	63.9	2	109.3	105.6	2	152.5	147.3	2	195.7	189.0
33	23.7	22.9	93	66.9	64.6	3	110.1	106.3	3	153.2	148.	3	196.4	189.6
34	24.5	23.6	94	67.6	65.3	4	110.8	107.	4	153.9	148.7	4	197.1	190.3
35	25.2	24.3	95	68.3	66.	5	111.5	107.7	5	154.7	149.4	5	197.8	191.
36	25.9	25.	96	69.1	66.7	6	112.2	108.4	6	155.4	150.	6	198.5	191.7
37	26.6	25.7	97	69.8	67.4	7	112.9	109.1	7	156.1	150.7	7	199.3	192.4
38	27.3	26.4	98	70.5	68.1	8	113.7	109.8	8	156.8	151.4	8	200.	193.1
39	28.1	27.1	99	71.2	68.8	9	114.4	110.5	9	157.5	152.1	9	200.7	193.8
40	28.8	27.3	100	71.9	69.5	160	115.1	111.1	220	158.3	152.8	280	201.4	194.5
41	29.5	28.5	1	72.7	70.2	1	115.8	111.8	1	159.	153.5	1	202.1	195.2
42	30.2	29.2	2	73.4	70.9	2	116.5	112.5	2	159.7	154.2	2	202.9	195.9
43	30.9	29.9	3	74.1	71.5	3	117.3	113.2	3	160.4	154.9	3	203.6	196.6
44	31.7	30.6	4	74.8	72.2	4	118.	113.9	4	161.1	155.6	4	204.3	197.3
45	32.4	31.3	5	75.5	72.9	5	118.7	114.6	5	161.9	156.3	5	205.	198
46	33.1	32.	6	76.3	73.6	6	119.4	115.3	6	162.6	157.	6	205.7	198.7
47	33.8	32.6	7	77.	74.3	7	120.1	116.	7	163.3	157.7	7	206.5	199.4
48	34.5	33.3	8	77.7	75.	8	120.8	116.7	8	164.	158.4	8	207.3	200.1
49	35.2	34.	9	78.4	75.7	9	121.6	117.4	9	164.7	159.1	9	207.9	200.8
50	36.	34.7	110	79.1	76.4	170	122.3	118.1	230	165.4	159.8	290	208.6	201.5
51	36.7	35.4	1	79.8	77.1	1	123.	118.8	1	166.2	160.5	1	209.3	202.1
52	37.4	36.1	2	80.6	77.8	2	123.7	119.5	2	166.9	161.2	2	210.	202.8
53	38.1	36.8	3	81.3	78.5	3	124.4	120.2	3	167.6	161.9	3	210.8	203.5
54	38.8	37.5	4	82.	79.2	4	125.2	120.9	4	168.3	162.6	4	211.5	204.2
55	39.6	38.3	5	82.7	79.9	5	125.9	121.6	5	169.	163.3	5	212.2	204.9
56	40.3	38.9	6	83.4	80.6	6	126.6	122.3	6	169.8	163.9	6	212.9	205.6
57	41.	39.6	7	84.2	81.3	7	127.3	123.	7	170.5	164.6	7	213.6	206.3
58	41.7	40.3	8	84.9	82.	8	128.	123.6	8	171.2	165.3	8	214.4	207.
59	42.4	41.	9	85.6	82.7	9	128.8	124.3	9	171.9	166.	9	215.1	207.7
60	43.2	41.7	190	86.3	83.4	180	129.5	125.	240	172.6	166.7	300	215.8	208.4
dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.	dist.	dep.	d.lat.

Distance, Departure and Diff. Latitude.

Course 46°.

Course 45°.

Distance, Diff. Latitude and Departure

dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.	dist.	d. lat.	dep.
1	0.7	0.7	61	43.1	43.1	131	85.6	85.6	181	138.	138.	231	170.4	170.4
2	1.4	1.4	62	43.8	43.8	3	86.3	86.3	2	138.7	138.7	2	171.1	171.1
3	2.1	2.1	63	44.5	44.5	4	87.	87.	3	139.4	139.4	3	171.8	171.8
4	2.8	2.8	64	45.3	45.3	5	87.7	87.7	4	139.1	139.1	4	172.5	172.5
5	3.5	3.5	65	46.	46.	6	88.4	88.4	5	139.8	139.8	5	173.2	173.2
6	4.2	4.2	66	46.7	46.7	7	89.1	89.1	6	131.5	131.5	6	173.9	173.9
7	4.9	4.9	67	47.4	47.4	8	89.8	89.8	7	132.2	132.2	7	174.7	174.7
8	5.7	5.7	68	48.1	48.1	9	90.5	90.5	8	132.9	132.9	8	175.4	175.4
9	6.4	6.4	69	48.8	48.8	10	91.2	91.2	9	133.6	133.6	9	176.1	176.1
10	7.1	7.1	70	49.5	49.5	130	91.9	91.9	190	134.4	134.4	230	176.8	176.8
11	7.8	7.8	71	50.2	50.2	1	92.6	92.6	1	135.1	135.1	1	177.5	177.5
12	8.5	8.5	72	50.9	50.9	2	93.3	93.3	2	135.8	135.8	2	178.2	178.2
13	9.2	9.2	73	51.6	51.6	3	94.	94.	3	136.5	136.5	3	178.9	178.9
14	9.9	9.9	74	52.3	52.3	4	94.8	94.8	4	137.2	137.2	4	179.6	179.6
15	10.6	10.6	75	53.	53.	5	95.5	95.5	5	137.9	137.9	5	180.3	180.3
16	11.3	11.3	76	53.7	53.7	6	96.2	96.2	6	138.6	138.6	6	181.	181.
17	12.	12.	77	54.4	54.4	7	96.9	96.9	7	139.3	139.3	7	181.7	181.7
18	12.7	12.7	78	55.2	55.2	8	97.6	97.6	8	140.	140.	8	182.4	182.4
19	13.4	13.4	79	55.9	55.9	9	98.3	98.3	9	140.7	140.7	9	183.1	183.1
20	14.1	14.1	80	56.6	56.6	140	99.	99.	200	141.4	141.4	260	183.8	183.8
21	14.8	14.8	81	57.3	57.3	1	99.7	99.7	1	142.1	142.1	1	184.6	184.6
22	15.6	15.6	82	58.	58.	2	100.4	100.4	2	142.8	142.8	2	185.3	185.3
23	16.3	16.3	83	58.7	58.7	3	101.1	101.1	3	143.5	143.5	3	186.	186.
24	17.	17.	84	59.4	59.4	4	101.8	101.8	4	144.2	144.2	4	186.7	186.7
25	17.7	17.7	85	60.1	60.1	5	102.5	102.5	5	145.	145.	5	187.4	187.4
26	18.4	18.4	86	60.8	60.8	6	103.2	103.2	6	145.7	145.7	6	188.1	188.1
27	19.1	19.1	87	61.5	61.5	7	103.9	103.9	7	146.4	146.4	7	188.8	188.8
28	19.8	19.8	88	62.2	62.2	8	104.7	104.7	8	147.1	147.1	8	189.5	189.5
29	20.5	20.5	89	62.9	62.9	9	105.4	105.4	9	147.8	147.8	9	190.2	190.2
30	21.2	21.2	90	63.6	63.6	150	106.1	106.1	210	148.5	148.5	270	190.9	190.9
31	21.9	21.9	91	64.3	64.3	1	106.8	106.8	1	149.2	149.2	1	191.6	191.6
32	22.6	22.6	92	65.1	65.1	2	107.5	107.5	2	149.9	149.9	2	192.3	192.3
33	23.3	23.3	93	65.8	65.8	3	108.2	108.2	3	150.6	150.6	3	193.	193.
34	24.	24.	94	66.5	66.5	4	108.9	108.9	4	151.3	151.3	4	193.7	193.7
35	24.7	24.7	95	67.2	67.2	5	109.6	109.6	5	152.	152.	5	194.5	194.5
36	25.5	25.5	96	67.9	67.9	6	110.3	110.3	6	152.7	152.7	6	195.2	195.2
37	26.2	26.2	97	68.6	68.6	7	111.	111.	7	153.4	153.4	7	195.9	195.9
38	26.9	26.9	98	69.3	69.3	8	111.7	111.7	8	154.1	154.1	8	196.6	196.6
39	27.6	27.6	99	70.	70.	9	112.4	112.4	9	154.9	154.9	9	197.3	197.3
40	28.3	28.3	100	70.7	70.7	160	113.1	113.1	260	155.6	155.6	320	198.	198.
41	29.	29.	1	71.4	71.4	1	113.8	113.8	1	156.3	156.3	1	198.7	198.7
42	29.7	29.7	2	72.1	72.1	2	114.6	114.6	2	157.	157.	2	199.4	199.4
43	30.4	30.4	3	72.8	72.8	3	115.3	115.3	3	157.7	157.7	3	200.1	200.1
44	31.1	31.1	4	73.5	73.5	4	116.	116.	4	158.4	158.4	4	200.8	200.8
45	31.8	31.8	5	74.2	74.2	5	116.7	116.7	5	159.1	159.1	5	201.5	201.5
46	32.5	32.5	6	75.	75.	6	117.4	117.4	6	159.8	159.8	6	202.2	202.2
47	33.2	33.2	7	75.7	75.7	7	118.1	118.1	7	160.5	160.5	7	202.9	202.9
48	33.9	33.9	8	76.4	76.4	8	118.8	118.8	8	161.2	161.2	8	203.6	203.6
49	34.6	34.6	9	77.1	77.1	9	119.5	119.5	9	161.9	161.9	9	204.4	204.4
50	35.4	35.4	110	77.8	77.8	170	120.2	120.2	230	162.6	162.6	290	205.1	205.1
51	36.1	36.1	1	78.5	78.5	1	120.9	120.9	1	163.3	163.3	1	205.8	205.8
52	36.8	36.8	2	79.2	79.2	2	121.6	121.6	2	164.	164.	2	206.5	206.5
53	37.5	37.5	3	79.9	79.9	3	122.3	122.3	3	164.8	164.8	3	207.2	207.2
54	38.2	38.2	4	80.6	80.6	4	123.	123.	4	165.5	165.5	4	207.9	207.9
55	38.9	38.9	5	81.3	81.3	5	123.7	123.7	5	166.2	166.2	5	208.6	208.6
56	39.6	39.6	6	82.	82.	6	124.5	124.5	6	166.9	166.9	6	209.3	209.3
57	40.3	40.3	7	82.7	82.7	7	125.2	125.2	7	167.6	167.6	7	210.	210.
58	41.	41.	8	83.4	83.4	8	125.9	125.9	8	168.3	168.3	8	210.7	210.7
59	41.7	41.7	9	84.1	84.1	9	126.6	126.6	9	169.	169.	9	211.4	211.4
60	42.4	42.4	120	84.8	84.8	180	127.3	127.3	240	169.7	169.7	300	212.1	212.1
dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.	dist.	dep.	d. lat.

Distance, Departure and Diff. Latitude.

Course 45°.

TABLE VI.

MERIDIONAL PARTS.

Meridional Parts.

'	00	10	20	30	40	50	60	70	80	90	100	110	120	130	140	'
0	0	00	180	180	240	300	361	421	482	543	603	664	725	787	848	0
1	1	61	91	81	41	01	62	22	83	43	04	65	26	86	46	1
2	2	62	92	82	42	02	63	23	84	44	05	66	27	87	47	2
3	3	63	93	83	43	03	64	24	85	45	06	67	28	88	48	3
4	4	64	94	84	44	04	65	25	86	46	07	68	29	89	49	4
5	5	65	95	85	45	05	66	26	87	47	08	69	30	90	50	5
6	6	66	96	86	46	06	67	27	88	48	09	70	31	91	51	6
7	7	67	97	87	47	07	68	28	89	49	10	71	32	92	52	7
8	8	68	98	88	48	08	69	29	90	50	11	72	33	93	53	8
9	9	69	99	89	49	09	70	30	91	51	12	73	34	94	54	9
10	10	70	30	90	50	10	71	31	92	52	13	74	35	95	55	10
11	11	71	31	91	51	11	72	32	93	53	14	75	36	96	56	11
12	12	72	32	92	52	12	73	33	94	54	15	76	37	97	57	12
13	13	73	33	93	53	13	74	34	95	55	16	77	38	98	58	13
14	14	74	34	94	54	14	75	35	96	56	17	78	39	99	59	14
15	15	75	35	95	55	15	76	36	97	57	18	79	40	01	60	15
16	16	76	36	96	56	16	77	37	98	58	19	80	41	02	61	16
17	17	77	37	97	57	17	78	38	99	59	20	81	42	03	62	17
18	18	78	38	98	58	18	79	39	00	60	21	82	43	04	63	18
19	19	79	39	99	59	19	80	40	01	61	22	83	44	05	64	19
20	20	80	40	00	60	20	81	41	02	62	23	84	45	06	65	20
21	21	81	41	01	61	21	82	42	03	63	24	85	46	07	66	21
22	22	82	42	02	62	22	83	43	04	64	25	86	47	08	67	22
23	23	83	43	03	63	23	84	44	05	65	26	87	48	09	68	23
24	24	84	44	04	64	24	85	45	06	66	27	88	49	10	69	24
25	25	85	45	05	65	25	86	46	07	67	28	89	50	11	70	25
26	26	86	46	06	66	26	87	47	08	68	29	90	51	12	71	26
27	27	87	47	07	67	27	88	48	09	69	30	91	52	13	72	27
28	28	88	48	08	68	28	89	49	10	70	31	92	53	14	73	28
29	29	89	49	09	69	29	90	50	11	71	32	93	54	15	74	29
30	30	90	50	10	70	30	91	51	12	72	33	94	55	16	75	30
31	31	91	51	11	71	31	92	52	13	73	34	95	56	17	76	31
32	32	92	52	12	72	32	93	53	14	74	35	96	57	18	77	32
33	33	93	53	13	73	33	94	54	15	75	36	97	58	19	78	33
34	34	94	54	14	74	34	95	55	16	76	37	98	59	20	79	34
35	35	95	55	15	75	35	96	56	17	77	38	99	60	21	80	35
36	36	96	56	16	76	36	97	57	18	78	39	00	61	22	81	36
37	37	97	57	17	77	37	98	58	19	79	40	01	62	23	82	37
38	38	98	58	18	78	38	99	59	20	80	41	02	63	24	83	38
39	39	99	59	19	79	39	00	60	21	81	42	03	64	25	84	39
40	40	100	60	20	80	40	01	61	22	82	43	04	65	26	85	40
41	41	01	61	21	81	41	02	62	23	83	44	05	66	27	86	41
42	42	02	62	22	82	42	03	63	24	84	45	06	67	28	87	42
43	43	03	63	23	83	43	04	64	25	85	46	07	68	29	88	43
44	44	04	64	24	84	44	05	65	26	86	47	08	69	30	89	44
45	45	05	65	25	85	45	06	66	27	87	48	09	70	31	90	45
46	46	06	66	26	86	46	07	67	28	88	49	10	71	32	91	46
47	47	07	67	27	87	47	08	68	29	89	50	11	72	33	92	47
48	48	08	68	28	88	48	09	69	30	90	51	12	73	34	93	48
49	49	09	69	29	89	49	10	70	31	91	52	13	74	35	94	49
50	50	10	70	30	90	50	11	71	32	92	53	14	75	36	95	50
51	51	11	71	31	91	51	12	72	33	93	54	15	76	37	96	51
52	52	12	72	32	92	52	13	73	34	94	55	16	77	38	97	52
53	53	13	73	33	93	53	14	74	35	95	56	17	78	39	98	53
54	54	14	74	34	94	54	15	75	36	96	57	18	79	40	99	54
55	55	15	75	35	95	55	16	76	37	97	58	19	80	41	00	55
56	56	16	76	36	96	56	17	77	38	98	59	20	81	42	01	56
57	57	17	77	37	97	57	18	78	39	99	60	21	82	43	02	57
58	58	18	78	38	98	58	19	79	40	01	61	22	83	44	03	58
59	59	19	79	39	99	59	20	80	41	02	62	23	84	45	04	59
60	60	100	80	40	00	60	20	80	40	01	61	21	83	44	05	60
61	61	01	61	21	81	41	01	61	21	81	41	01	61	21	81	61
62	62	02	62	22	82	42	02	62	22	82	42	02	62	22	82	62
63	63	03	63	23	83	43	03	63	23	83	43	03	63	23	83	63
64	64	04	64	24	84	44	04	64	24	84	44	04	64	24	84	64
65	65	05	65	25	85	45	05	65	25	85	45	05	65	25	85	65
66	66	06	66	26	86	46	06	66	26	86	46	06	66	26	86	66
67	67	07	67	27	87	47	07	67	27	87	47	07	67	27	87	67
68	68	08	68	28	88	48	08	68	28	88	48	08	68	28	88	68
69	69	09	69	29	89	49	09	69	29	89	49	09	69	29	89	69
70	70	10	70	30	90	50	10	70	30	90	50	10	70	30	90	70
71	71	11	71	31	91	51	11	71	31	91	51	11	71	31	91	71
72	72	12	72	32	92	52	12	72	32	92	52	12	72	32	92	72
73	73	13	73	33	93	53	13	73	33	93	53	13	73	33	93	73
74	74	14	74	34	94	54	14	74	34	94	54	14	74	34	94	74
75	75	15	75	35	95	55	15	75	35	95	55	15	75	35	95	75
76	76	16	76	36	96	56	16	76	36	96	56	16	76	36	96	76
77	77	17	77	37	97	57	17	77	37	97	57	17	77	37	97	77
78	78	18	78	38	98	58	18	78	38	98	58	18	78	38	98	78
79	79	19	79	39	99	59	19	79	39	99	59	19	79	39	99	79
80	80	20	80	40	00	60	20	80	40	00	60	20	80	40	00	80
81	81	21	81	41	01	61	21	81	41	01	61	21	81	41	01	81
82	82	22	82	42	02	62	22	82	42	02	62	22	82	42	02	82
83	83	23	83	43	03	63	23	83	43	03	63	23	83	43	03	83
84	84	24	84	44	04	64	24	84	44	04	64	24	84	44	04	84
85	85	25	85	45	05	65	25	85	45	05	65	25	85	45	05	85
86	86	26	86	46	06	66	26	86	46	06	66	26	86	46	06	86
87	87	27	87	47	07	67	27	87	47	07	67	27	87	47	07	87
88	88	28	88	48	08	68	28	88	48	08	68	28	88	48	08	88
89	89	29	89	49	09	69	29	89	49	09	69	29	89	49	09	89
90	90	30	90	50	10	70	30	90	50	10	70	30	90	50	10	90
91	91	31	91	51	11	71	31	91	51	11	71	31	91	51	11	91
92	92	32	92	52	12	72	32	92	52	12	72	32	92	52	12	92
93	93	33	93	53	13	73	33	93	53	13	73	33	93	53	13	93
94	94	34	94	54	14	74	34	94	54	14	74	34	94	54	14	94
95	95	35	95	55	15	75	35	95	55	15	75	35	95	55	15	95
96	96	36	96	56	16	76	36	96	56	16	76	36	96	56	16	96
97	97	37	97	57	17	77	37	97								

Meridional Parts.

'	15°	16°	17°	18°	19°	20°	21°	22°	23°	24°	25°	26°	27°	28°	'
0	910	973	1035	1098	1161	1225	1289	1354	1419	1484	1550	1616	1684	1751	0
1	11	74	36	90	63	30	90	55	20	85	51	18	85	52	1
2	12	75	37	91	64	31	91	56	21	86	52	19	86	53	2
3	14	76	38	91	65	32	92	57	22	87	53	20	87	54	3
4	15	77	39	92	66	33	93	58	23	88	54	21	88	55	4
5	16	78	41	93	67	34	94	59	24	90	55	22	89	57	5
6	17	79	42	95	68	35	96	60	25	91	57	23	90	58	6
7	18	80	43	96	69	36	97	61	26	92	58	24	91	59	7
8	19	81	44	97	70	37	98	62	27	93	59	25	92	60	8
9	20	82	45	98	71	38	99	63	28	94	60	26	93	61	9
10	21	83	46	99	72	39	1000	64	30	95	61	26	94	62	10
11	22	84	47	10	73	37	01	66	31	96	62	27	95	64	11
12	23	85	48	11	74	38	02	67	32	97	63	28	96	65	12
13	24	86	49	12	75	39	03	68	33	98	64	31	97	65	13
14	25	87	50	13	76	40	04	69	34	99	65	32	98	67	14
15	26	88	51	14	77	41	05	70	35	1500	67	33	1700	68	15
16	27	89	52	15	78	42	06	71	36	02	68	34	01	68	16
17	28	90	53	16	79	43	07	72	37	03	69	35	02	69	17
18	29	91	54	17	81	44	08	73	38	04	70	37	04	70	18
19	30	93	55	18	82	45	10	74	39	05	71	38	05	71	19
20	31	94	56	19	83	46	11	75	40	06	72	39	06	74	20
21	32	95	57	20	84	48	12	76	41	07	73	40	07	75	21
22	33	96	58	21	85	49	13	77	43	08	74	41	08	76	22
23	34	97	59	22	86	50	14	78	44	09	75	42	09	77	23
24	35	98	60	23	87	51	15	80	45	10	77	43	11	78	24
25	36	99	61	25	88	52	16	81	46	11	78	44	12	80	25
26	37	1000	62	26	89	53	17	82	47	12	79	45	13	81	26
27	38	01	64	27	90	54	18	83	48	14	80	47	14	82	27
28	39	02	65	28	91	55	19	84	49	15	81	48	15	83	28
29	41	03	66	29	92	56	20	85	50	16	82	49	16	84	29
30	42	04	67	30	93	57	21	86	51	17	83	50	17	85	30
31	43	05	68	31	94	58	22	87	52	18	84	51	18	86	31
32	44	06	69	32	95	59	24	88	53	19	85	52	19	87	32
33	45	07	70	33	96	60	25	89	54	20	87	53	21	88	33
34	46	08	71	34	96	61	26	90	56	21	88	54	22	89	34
35	47	09	72	35	99	62	27	92	57	22	89	55	23	91	35
36	48	10	73	36	1000	64	28	93	58	24	90	57	24	92	36
37	49	11	74	37	01	65	29	94	59	25	91	58	25	93	37
38	50	12	75	38	02	66	30	95	60	26	92	59	26	94	38
39	51	13	76	39	03	67	31	96	61	27	93	60	27	95	39
40	52	14	77	40	04	68	32	97	62	28	94	61	28	97	40
41	53	15	78	41	05	69	33	98	63	29	95	62	29	98	41
42	54	16	79	42	06	70	34	99	64	30	96	63	31	99	42
43	55	18	80	44	07	71	35	1400	65	31	98	64	32	1000	43
44	56	19	81	45	08	72	36	01	67	32	99	65	33	01	44
45	57	20	82	46	09	73	38	02	68	33	1600	67	34	02	45
46	58	21	84	47	10	74	39	03	69	35	01	68	35	03	46
47	59	22	85	48	11	75	40	05	70	36	02	69	36	04	47
48	60	23	86	49	12	76	41	06	71	37	03	70	37	05	48
49	61	24	87	50	13	77	42	07	72	38	04	71	38	06	49
50	62	25	88	51	15	78	43	08	73	39	05	72	39	07	50
51	63	26	89	52	16	80	44	09	74	40	06	73	40	08	51
52	64	27	90	53	17	81	45	10	75	41	07	74	41	09	52
53	65	28	91	54	18	82	46	11	76	42	08	75	42	10	53
54	66	29	92	55	19	83	47	12	77	43	10	77	44	11	54
55	68	30	93	56	20	84	48	13	78	44	11	78	45	14	55
56	69	31	94	57	21	85	49	14	80	46	12	79	47	15	56
57	70	32	95	58	22	86	50	15	81	47	13	80	48	16	57
58	71	33	96	59	23	87	51	16	82	48	14	81	49	17	58
59	72	1034	1097	1160	1224	1288	1353	1418	1483	1549	1615	1682	1750	1818	59
'	15°	16°	17°	18°	19°	20°	21°	22°	23°	24°	25°	26°	27°	28°	'

Meridional Parts.

	29°	30°	31°	32°	33°	34°	35°	36°	37°	38°	39°	40°	41°	42°	
0	1819	1888	1958	2028	2100	2171	2244	2318	2393	2468	2545	2623	2702	2782	0
1	21	90	59	30	01	73	46	19	94	70	46	24	03	83	1
2	29	91	60	31	02	74	47	20	95	71	48	25	04	84	2
3	23	92	62	32	03	75	48	22	96	72	49	27	06	86	3
4	24	93	63	33	04	76	49	23	98	73	50	28	07	87	4
5	25	94	64	34	06	78	50	24	99	75	51	29	08	88	5
6	26	95	65	35	07	79	52	25	2490	76	53	31	10	90	6
7	27	96	66	37	08	80	53	27	01	77	54	32	11	91	7
8	29	98	67	38	09	81	54	28	03	78	55	33	12	92	8
9	30	99	69	39	10	82	55	29	04	80	57	34	14	94	9
10	31	1000	70	40	11	84	57	30	05	81	58	36	15	95	10
11	32	01	71	41	13	85	58	32	06	82	59	37	16	97	11
12	33	02	72	43	14	86	59	33	08	84	60	38	18	98	12
13	34	03	73	44	15	87	60	34	09	85	62	40	19	99	13
14	35	05	74	45	16	88	61	35	10	86	63	41	20	201	14
15	37	06	76	46	17	90	63	37	11	87	64	42	22	02	15
16	38	07	77	47	19	91	64	38	13	89	66	44	23	03	16
17	39	08	78	48	20	92	65	39	14	90	67	45	24	05	17
18	40	09	79	50	21	93	66	40	15	91	68	46	26	06	18
19	41	10	80	51	22	94	68	42	16	92	69	48	27	07	19
20	42	11	81	52	23	96	69	43	18	94	71	49	28	09	20
21	43	13	83	53	25	97	70	44	19	95	72	50	29	10	21
22	45	14	84	54	26	98	71	45	20	96	73	51	31	11	22
23	46	15	85	56	27	2900	72	46	22	98	75	53	32	13	23
24	47	16	86	57	28	01	74	48	23	99	76	54	33	14	24
25	48	17	87	58	29	02	75	49	24	2500	77	55	35	15	25
26	49	19	88	59	31	03	76	50	25	01	78	57	36	17	26
27	50	20	90	60	32	04	77	51	27	03	80	58	37	18	27
28	52	21	91	61	33	05	79	53	28	04	81	59	39	20	28
29	53	22	92	63	34	07	80	54	29	05	82	61	40	21	29
30	54	23	93	64	35	08	81	55	30	06	84	62	42	22	30
31	55	25	94	65	37	09	82	56	32	08	85	63	43	24	31
32	56	26	95	66	38	10	83	57	33	09	86	65	44	25	32
33	57	27	97	67	39	11	85	59	34	10	88	66	46	26	33
34	58	28	98	69	40	13	86	60	35	12	89	67	47	28	34
35	60	29	99	70	41	14	87	61	37	13	90	69	48	29	35
36	61	31	2000	71	43	15	88	63	38	14	91	70	50	30	36
37	62	32	01	72	44	16	90	64	39	15	92	71	51	32	37
38	63	33	02	73	45	17	91	65	40	17	94	73	52	33	38
39	64	34	04	75	46	19	92	66	42	18	95	74	54	34	39
40	65	35	05	76	47	20	93	68	43	19	97	75	55	36	40
41	66	36	06	77	49	21	95	69	44	21	98	76	56	37	41
42	68	37	07	78	50	22	96	70	45	22	99	78	58	39	42
43	69	38	08	79	51	24	97	71	47	23	2001	79	59	40	43
44	70	39	10	80	52	25	98	73	48	24	02	80	60	41	44
45	71	41	11	82	53	26	99	74	49	26	03	82	62	43	45
46	72	42	12	83	55	27	201	75	51	27	04	83	63	44	46
47	73	43	13	84	56	28	02	76	52	28	06	84	64	45	47
48	75	44	14	85	57	30	03	78	53	30	07	86	66	47	48
49	76	45	15	86	58	31	04	79	54	31	08	87	67	48	49
50	77	46	17	88	59	32	06	80	56	32	10	88	68	49	50
51	78	48	18	89	61	33	07	81	57	33	11	90	70	51	51
52	79	49	19	90	62	35	08	83	58	35	12	91	71	52	52
53	80	50	20	91	63	36	09	84	59	36	14	92	72	54	53
54	81	51	21	92	64	37	11	85	61	37	15	94	74	55	54
55	83	52	22	94	65	38	12	86	62	38	16	95	75	56	55
56	84	53	24	95	67	39	13	88	63	40	17	96	76	58	56
57	85	55	25	96	68	41	14	89	64	41	19	98	78	59	57
58	86	56	26	97	69	42	16	90	66	42	20	99	79	60	58
59	1867	1957	2027	2098	2170	2243	2317	2391	2467	2544	2621	2700	2780	2862	59
	29°	30°	31°	32°	33°	34°	35°	36°	37°	38°	39°	40°	41°	42°	

Meridional Parts.

	43°	44°	45°	46°	47°	48°	49°	50°	51°	52°	53°	54°	55°	56°	
0	2803	2946	3030	3116	3203	3292	3382	3474	3569	3665	3764	3865	3968	4074	0
1	64	47	31	17	04	93	84	76	70	67	65	66	70	76	1
2	66	49	33	19	06	95	85	78	72	68	67	68	71	77	2
3	67	50	34	20	07	96	87	79	74	70	69	70	73	79	3
4	69	51	36	21	07	98	88	81	75	72	70	71	75	81	4
5	70	53	37	23	10	99	90	82	77	73	72	73	77	83	5
6	71	54	38	24	12	3301	91	84	78	75	74	75	78	85	6
7	73	56	40	26	13	02	93	85	80	77	75	77	80	88	7
8	74	57	41	27	14	03	94	87	82	78	77	78	82	90	8
9	75	58	43	29	16	05	96	88	83	80	79	80	84	92	9
10	77	60	44	30	17	06	97	90	85	81	80	82	85	94	10
11	78	61	46	31	19	08	98	92	86	83	82	83	87	96	11
12	80	63	47	33	20	09	3400	93	88	85	84	85	89	98	12
13	81	64	48	34	22	11	02	95	90	86	85	87	91	97	13
14	82	65	50	35	23	12	03	96	91	88	87	89	92	99	14
15	84	67	51	36	25	14	05	98	93	90	89	90	94	101	15
16	85	68	53	37	26	16	07	99	94	91	90	92	96	103	16
17	86	70	54	40	28	17	08	3501	96	93	92	94	98	104	17
18	88	71	55	42	29	19	10	03	98	95	94	95	99	106	18
19	89	72	57	43	31	20	11	04	99	96	95	97	101	108	19
20	91	74	58	44	32	22	13	06	3601	98	97	99	103	110	20
21	92	75	60	46	34	23	14	07	02	99	99	3901	105	112	21
22	93	76	61	47	35	25	16	09	04	3701	3900	02	106	113	22
23	95	78	63	49	37	26	17	10	06	03	02	04	107	115	23
24	96	79	64	50	38	28	19	12	07	04	04	06	108	117	24
25	97	81	65	52	40	29	20	14	09	06	06	07	109	119	25
26	99	82	67	53	41	31	22	15	10	08	07	09	110	121	26
27	3900	83	68	55	42	32	23	17	12	09	09	11	111	122	27
28	02	85	70	56	44	34	25	18	14	11	11	13	112	124	28
29	03	86	71	57	45	35	27	20	15	13	12	14	113	126	29
30	04	88	73	59	47	37	28	21	17	14	14	16	114	128	30
31	06	89	74	60	48	38	30	23	18	16	16	18	115	130	31
32	07	91	75	62	50	40	31	25	20	17	17	19	116	132	32
33	08	92	77	63	51	41	33	26	22	19	19	21	117	134	33
34	10	93	78	65	53	43	34	28	23	21	21	23	118	136	34
35	11	95	80	66	54	44	36	29	25	22	22	25	119	138	35
36	13	96	81	68	56	46	37	31	26	24	24	26	120	140	36
37	14	98	83	69	57	47	38	32	28	26	26	28	121	142	37
38	15	99	84	71	59	49	40	34	30	27	27	30	122	144	38
39	17	3000	85	72	60	50	41	36	31	29	29	32	123	146	39
40	18	02	87	73	62	52	43	37	33	31	31	33	124	148	40
41	19	03	88	75	63	53	45	39	34	32	32	35	125	150	41
42	21	05	90	76	65	55	47	40	36	34	34	37	126	152	42
43	22	06	91	78	66	56	48	42	38	36	36	38	127	154	43
44	24	07	93	79	68	58	50	43	39	37	37	38	128	156	44
45	25	09	94	81	69	59	51	45	41	39	39	42	129	158	45
46	26	10	95	82	71	61	53	47	43	41	41	44	130	160	46
47	28	12	97	84	72	62	54	48	44	42	43	45	131	162	47
48	29	13	98	85	74	64	56	50	46	44	44	47	132	164	48
49	31	14	3100	87	75	65	57	51	47	46	46	48	133	166	49
50	32	16	01	88	77	67	59	53	49	47	48	51	134	168	50
51	33	17	03	90	78	68	60	55	51	49	49	52	135	170	51
52	35	19	04	91	80	70	62	56	53	50	51	54	136	172	52
53	36	20	05	92	81	71	64	58	54	52	53	56	137	174	53
54	37	21	07	94	83	73	65	59	55	54	54	58	138	176	54
55	39	23	08	95	84	74	67	61	57	55	56	59	139	178	55
56	40	24	10	97	86	76	68	62	59	57	58	61	140	180	56
57	42	26	11	98	87	77	70	64	60	59	60	63	141	182	57
58	43	27	13	3200	89	79	71	66	62	60	61	64	142	184	58
59	3944	3029	3114	01	3290	3381	3473	3567	3664	3762	3863	3966	4072	4181	59
	43°	44°	45°	46°	47°	48°	49°	50°	51°	52°	53°	54°	55°	56°	

Meridional Parts.

	57°	58°	59°	60°	61°	62°	63°	64°	65°	66°	67°	68°	69°	70°	
0	4183	4294	4405	4527	4649	4775	4905	5039	5179	5324	5474	5631	5795	5966	0
1	84	96	11	29	51	77	07	42	81	26	77	33	97	69	1
2	86	98	13	31	53	79	09	44	84	29	79	36	5800	72	2
3	86	4300	15	33	55	81	12	46	86	31	82	39	03	75	3
4	90	02	17	35	57	84	14	48	88	33	84	42	06	78	4
5	92	04	19	37	60	86	16	51	91	36	87	44	09	81	5
6	94	06	21	39	62	88	18	53	93	38	89	47	11	84	6
7	96	08	23	41	64	90	20	55	96	41	92	50	14	86	7
8	97	09	25	43	66	92	23	58	98	43	95	52	17	89	8
9	99	11	27	45	68	94	25	60	5200	46	97	55	20	92	9
10	4201	13	29	47	70	96	27	62	03	48	5500	58	23	95	10
11	03	15	31	49	72	98	29	65	05	51	02	60	25	98	11
12	05	17	33	51	74	4801	31	67	07	53	05	63	28	6001	12
13	07	18	34	53	76	03	34	69	10	56	07	66	31	04	13
14	08	20	36	55	78	05	36	71	12	58	10	68	34	07	14
15	10	22	38	57	80	07	38	74	14	61	13	71	37	10	15
16	12	24	40	59	83	09	40	76	17	63	15	74	39	13	16
17	14	26	42	62	84	11	43	78	19	66	18	76	42	16	17
18	16	28	44	64	87	14	45	81	22	68	20	79	45	19	18
19	18	30	46	66	89	16	47	83	24	71	23	82	48	22	19
20	20	32	48	68	91	18	49	85	26	73	26	85	51	25	20
21	21	34	50	70	93	20	51	88	29	76	28	87	54	28	21
22	23	36	52	72	95	22	54	90	31	78	31	90	56	31	22
23	25	38	54	74	97	24	56	92	34	80	33	93	59	34	23
24	27	40	56	76	99	26	58	95	36	83	36	95	62	37	24
25	29	42	58	78	4701	29	60	97	38	85	39	98	65	40	25
26	31	44	60	80	03	31	63	99	41	88	41	5701	68	43	26
27	32	45	62	82	05	33	65	5102	43	90	44	04	71	46	27
28	34	47	64	84	07	35	67	04	46	93	46	06	74	49	28
29	36	49	66	86	10	37	69	06	48	95	49	09	76	52	29
30	38	51	68	88	12	39	72	08	50	98	52	12	79	55	30
31	40	53	70	90	14	42	74	11	33	5401	54	15	82	58	31
32	42	55	72	92	16	44	76	13	35	03	57	17	85	61	32
33	44	57	74	94	18	46	78	15	38	06	59	20	88	64	33
34	46	59	76	96	20	48	81	18	60	08	62	23	91	67	34
35	47	61	78	98	22	50	83	20	63	11	65	25	94	70	35
36	49	63	80	4600	24	52	85	22	65	13	67	28	96	73	36
37	51	65	82	02	26	55	87	25	67	16	70	31	99	76	37
38	53	67	84	04	28	57	90	27	70	18	73	34	5902	79	38
39	55	69	86	06	31	59	92	29	73	21	75	36	05	82	39
40	57	70	88	08	33	61	94	32	75	23	78	39	08	85	40
41	59	72	90	10	35	63	96	34	77	25	80	42	11	88	41
42	60	74	92	12	37	65	98	36	80	28	83	45	14	91	42
43	62	76	94	14	39	67	5001	39	82	31	86	47	17	94	43
44	64	78	95	16	41	70	03	41	84	33	88	50	19	97	44
45	66	80	97	18	43	72	05	43	87	36	91	53	22	6100	45
46	68	82	99	20	45	74	06	46	89	38	94	56	25	03	46
47	70	84	4501	23	47	76	10	48	92	41	96	58	28	06	47
48	72	86	03	25	50	79	13	51	94	43	99	61	31	09	48
49	74	88	05	27	52	81	14	53	97	46	5003	64	34	12	49
50	75	90	07	29	54	83	17	55	99	48	04	67	37	15	50
51	78	92	09	31	56	85	19	57	5301	51	07	70	40	18	51
52	80	94	11	33	58	87	21	60	04	54	10	72	43	21	52
53	82	96	13	35	60	90	23	62	06	56	12	75	46	24	53
54	84	98	15	37	62	92	25	65	09	59	15	78	48	27	54
55	85	99	17	39	64	94	28	67	11	61	17	81	51	30	55
56	87	4401	19	41	66	96	30	69	14	64	20	83	54	33	56
57	89	03	21	43	68	98	33	72	16	66	23	86	57	36	57
58	91	05	23	45	71	4901	35	74	19	69	25	89	60	40	58
59	4202	07	4525	4647	4773	03	5037	5176	5321	5471	5626	5792	5963	6143	59
	57°	58°	59°	60°	61°	62°	63°	64°	65°	66°	67°	68°	69°	70°	

Meridional Parts.

	71°	72°	73°	74°	75°	76°	77°	78°	79°	80°	81°	82°	83°	84°	
0	6146	6335	6534	6748	6970	7210	7467	7745	8046	8375	8739	9145	9606	10127	0
1	49	38	36	49	74	14	73	49	51	81	45	53	14	147	1
2	52	41	41	53	78	18	76	54	56	87	52	60	22	152	2
3	55	45	45	57	82	22	81	59	61	93	58	67	31	165	3
4	58	48	48	60	86	27	85	64	67	98	65	74	39	176	4
5	61	51	52	64	90	31	90	68	72	104	71	82	47	185	5
6	64	54	55	68	94	35	94	73	77	110	76	88	55	195	6
7	67	56	58	71	97	39	98	78	83	116	81	94	64	205	7
8	70	61	62	75	101	43	103	83	88	122	86	100	72	215	8
9	73	64	65	79	105	47	107	88	93	129	91	105	81	224	9
10	77	67	69	82	109	52	112	93	99	137	96	111	90	234	10
11	80	71	72	86	113	56	116	98	104	145	101	117	97	244	11
12	83	74	76	90	117	60	121	103	109	153	105	123	104	254	12
13	86	77	79	93	121	64	125	108	115	161	109	127	111	264	13
14	89	80	83	97	125	68	130	113	120	170	113	131	118	274	14
15	92	84	86	101	129	73	135	117	125	179	117	135	125	284	15
16	95	87	90	104	133	77	140	122	131	188	121	140	132	294	16
17	98	90	93	108	137	81	144	127	136	197	125	144	140	304	17
18	101	94	97	112	141	85	148	132	141	206	129	148	147	314	18
19	105	97	100	115	145	89	153	137	147	215	133	152	155	324	19
20	108	101	103	119	149	94	157	142	152	224	137	156	163	334	20
21	111	103	107	123	153	98	162	147	158	233	141	161	171	344	21
22	114	107	110	126	157	102	166	152	163	242	145	165	179	354	22
23	117	110	114	130	161	106	171	157	168	251	149	170	187	364	23
24	120	113	117	134	165	111	176	162	174	260	153	174	195	374	24
25	123	117	121	138	169	115	180	167	179	269	157	178	203	384	25
26	126	120	124	141	173	119	185	172	185	278	161	182	211	394	26
27	129	123	128	145	177	123	189	177	190	287	165	186	219	404	27
28	132	127	131	149	181	127	194	182	196	296	169	190	227	414	28
29	135	130	135	153	185	131	198	187	201	305	173	194	235	424	29
30	138	133	138	157	189	135	203	192	207	314	177	198	243	434	30
31	141	137	142	161	193	139	207	197	212	323	181	202	251	444	31
32	144	140	145	165	197	143	211	202	218	332	185	206	259	454	32
33	147	143	148	169	201	147	215	207	223	341	189	210	267	464	33
34	150	147	152	173	205	151	219	212	229	350	193	214	275	474	34
35	153	150	155	177	209	155	223	217	234	359	197	218	283	484	35
36	156	153	158	181	213	159	227	222	240	368	201	222	291	494	36
37	159	157	162	185	217	163	231	227	245	377	205	226	300	504	37
38	162	160	165	189	221	167	235	232	251	386	209	230	308	514	38
39	165	163	168	193	225	171	239	237	256	395	213	234	316	524	39
40	168	167	172	197	229	175	243	242	261	404	217	238	324	534	40
41	171	170	175	201	233	179	247	247	267	413	221	242	332	544	41
42	174	173	178	205	237	183	251	252	272	422	225	246	340	554	42
43	177	177	182	209	241	187	255	257	278	431	229	250	348	564	43
44	180	180	185	213	245	191	259	262	283	440	233	254	356	574	44
45	183	183	188	217	249	195	263	267	289	449	237	258	364	584	45
46	186	187	192	221	253	199	267	272	294	458	241	262	372	594	46
47	189	190	195	225	257	203	271	277	299	467	245	266	380	604	47
48	192	194	199	229	261	207	275	282	305	476	249	270	388	614	48
49	195	197	202	233	265	211	279	287	310	485	253	274	396	624	49
50	198	200	205	237	269	215	283	292	316	494	257	278	404	634	50
51	201	203	208	241	273	219	287	297	321	503	261	282	412	644	51
52	204	206	211	245	277	223	291	302	327	512	265	286	420	654	52
53	207	209	214	249	281	227	295	307	332	521	269	290	428	664	53
54	210	212	217	253	285	231	299	312	338	530	273	294	436	674	54
55	213	215	220	257	289	235	303	317	343	539	277	298	444	684	55
56	216	218	223	261	293	239	307	322	349	548	281	302	452	694	56
57	219	221	226	265	297	243	311	327	354	557	285	306	460	704	57
58	222	224	229	269	301	247	315	332	360	566	289	310	468	714	58
59	225	227	232	273	305	251	319	337	366	575	293	314	476	724	59
60	228	230	235	277	309	255	323	342	371	584	297	318	484	734	60
61	231	233	238	281	313	259	327	347	377	593	301	322	492	744	61
62	234	236	241	285	317	263	331	352	382	602	305	326	500	754	62
63	237	239	244	289	321	267	335	357	388	611	309	330	508	764	63
64	240	242	247	293	325	271	339	362	393	620	313	334	516	774	64
65	243	245	250	297	329	275	343	367	399	629	317	338	524	784	65
66	246	248	253	301	333	279	347	372	404	638	321	342	532	794	66
67	249	251	256	305	337	283	351	377	410	647	325	346	540	804	67
68	252	254	259	309	341	287	355	382	415	656	329	350	548	814	68
69	255	257	262	313	345	291	359	387	421	665	333	354	556	824	69
70	258	260	265	317	349	295	363	392	426	674	337	358	564	834	70
71	261	263	268	321	353	299	367	397	432	683	341	362	572	844	71
72	264	266	271	325	357	303	371	402	437	692	345	366	580	854	72
73	267	269	274	329	361	307	375	407	443	701	349	370	588	864	73
74	270	272	277	333	365	311	379	412	448	710	353	374	596	874	74
75	273	275	280	337	369	315	383	417	454	719	357	378	604	884	75
76	276	278	283	341	373	319	387	422	459	728	361	382	612	894	76
77	279	281	286	345	377	323	391	427	465	737	365	386	620	904	77
78	282	284	289	349	381	327	395	432	470	746	369	390	628	914	78
79	285	287	292	353	385	331	399	437	476	755	373	394	636	924	79
80	288	290	295	357	389	335	403	442	481	764	377	398	644	934	80
81	291	293	298	361	393	339	407	447	487	773	381	402	652	944	81
82	294	296	301	365	397	343	411	452	492	782	385	406	660	954	82
83	297	299	304	369	401	347	415	457	498	791	389	410	668	964	83
84	300	302	307	373	405	351	419	462	503	800	393	414	676	974	84
85	303	305	310	377	409	355	423	467	509	809	397	418	684	984	85
86	306	308	313	381	413	359	427	472	514	818	401	422	692	994	86
87	309	311	316	385	417	363	431	477	520	827	405	426	700	1004	87
88	312	314	319	389	421	367	435	482	525	836	409	430	708	1014	88
89	315	317	322	393	425	371	439	487	531	845	413	434	716	1024	89
90	318	320	325	397	429	375	443	492	536	854	417	438	724	1034	90
91	321	323	328	401	433	379	447	497	542	863	421	442	732	1044	91
92	324	326	331	405	437	383	451	502	547	872	425	446	740	1054	92
93	327	329	334	409	441</										

TABLE VII.

AMPLITUDES

Amplitudes.

Declination of the Sun.													
lat.	0°	1°	2°	3°	4°	5°	6°	7°	8°	9°	10°	11°	12°
0°	0'	10'	20'	30'	40'	50'	00'	10'	20'	30'	40'	50'	00'
1	0	0	0	0	0	0	0	0	0	0	0	0	0
2	0	0	0	0	0	0	0	0	0	0	0	0	0
3	0	0	0	0	0	0	0	1	1	1	1	1	1
4	0	0	0	0	0	1	1	1	1	1	1	1	1
5	0	0	0	0	1	1	1	1	2	2	2	2	2
6	0	0	0	1	1	1	2	2	2	3	3	3	3
7	0	0	1	1	1	2	2	3	3	4	4	4	4
8	0	1	1	1	2	2	3	4	4	5	5	5	5
9	0	1	1	2	2	3	4	5	5	6	6	6	6
10	0	1	2	3	4	5	6	7	7	8	8	9	9
11	0	1	2	3	4	5	6	7	8	9	10	10	11
12	0	1	3	4	5	6	7	8	9	11	12	12	13
13	0	2	3	5	6	7	8	10	11	13	14	14	16
14	0	2	4	6	7	8	9	11	13	15	17	17	19
15	0	2	4	6	8	9	11	13	15	17	19	21	21
16	0	3	5	7	10	12	14	15	17	19	22	24	24
17	0	3	5	8	11	14	17	19	22	25	28	30	31
18	0	3	6	9	12	15	19	22	25	29	32	34	35
19	0	3	7	10	14	17	21	24	28	31	35	37	38
20	0	4	8	12	15	19	23	27	31	35	40	43	45
21	0	4	9	13	17	21	26	30	34	39	43	48	50
22	0	5	9	14	19	24	28	33	38	43	48	53	55
23	0	5	10	16	21	26	31	36	42	47	52	58	60
24	0	6	11	17	23	28	34	40	46	52	57	63	65
25	0	6	12	19	25	31	37	44	50	56	62	68	70
26	0	7	14	20	27	34	41	48	54	61	67	73	75
27	0	7	15	22	29	37	44	52	59	66	72	78	80
28	0	8	16	24	32	40	48	56	64	71	78	84	86
29	0	8	17	26	34	43	52	60	68	75	82	88	90
30	0	9	19	27	37	47	56	65	73	81	89	96	98
31	0	10	20	30	40	50	60	70	80	90	99	107	110
32	0	11	22	32	43	54	65	76	86	96	105	114	118
33	0	12	23	35	46	58	70	81	92	103	113	122	126
34	0	12	25	37	50	62	74	85	96	107	117	126	130
35	0	13	27	40	53	66	78	90	101	112	122	131	135
36	0	14	28	43	57	70	83	95	107	118	128	137	141
37	0	15	30	45	61	75	88	100	112	123	133	142	146
38	0	16	32	48	65	80	94	107	119	130	140	149	153
39	0	17	34	52	70	85	100	114	127	138	148	157	161
40	0	18	37	55	75	90	105	120	134	146	156	165	169
41	0	20	39	59	80	96	111	126	141	153	163	172	176
42	0	21	42	64	86	102	118	133	148	160	170	179	183
43	0	22	44	68	92	109	125	141	156	168	178	187	191
44	0	23	47	73	98	116	133	151	166	178	188	197	201
45	0	25	50	78	104	124	141	159	174	186	196	205	209
46	0	26	53	83	111	133	151	170	185	197	207	216	220
47	0	28	56	89	119	142	161	181	196	208	218	227	231
48	0	30	59	95	127	153	172	192	207	219	229	238	242
49	0	31	63	101	136	165	184	204	219	231	241	250	254
50	0	33	67	108	146	178	200	221	236	248	258	267	271
51	0	35	71	115	157	192	212	233	248	260	270	279	283
52	0	37	75	123	168	206	225	246	261	273	283	292	296
53	0	40	79	132	180	221	240	261	276	288	298	307	311
54	0	42	84	141	193	236	255	276	291	303	313	322	326
55	0	45	89	151	207	252	271	292	307	319	329	338	342
56	0	47	95	161	222	268	287	308	323	335	345	354	358
57	0	50	100	172	238	285	305	326	340	352	362	371	375
58	0	53	107	184	255	304	324	345	359	371	381	390	394
59	0	57	114	200	274	324	344	360	374	386	396	405	409
60	0	60	122	220	296	346	366	381	395	407	417	426	430
lat.	0°	1°	2°	3°	4°	5°	6°	7°	8°	9°	10°	11°	12°

Declination of the Sun.

Amplitudes.

Declination of the Sun.

lat.	19°	13°	14°	15°	16°	17°	18°	19°	20°	21°	22°	23°	lat.
0°	0'	0'	0'	0'	0'	0'	0'	0'	0'	0'	0'	0'	0'
1	0	0	0	0	0	0	0	0	0	0	0	0	1
2	0	0	0	0	0	0	0	0	0	0	0	0	2
3	1	1	1	1	1	1	1	1	1	1	1	1	3
4	2	2	2	2	2	2	2	2	2	2	2	2	4
5	3	3	3	3	3	3	3	3	3	3	3	3	5
6	4	4	4	4	4	4	4	4	4	4	4	4	6
7	5	5	5	5	5	5	5	5	5	5	5	5	7
8	6	6	6	6	6	6	6	6	6	6	6	6	8
9	7	7	7	7	7	7	7	7	7	7	7	7	9
10	10	10	10	10	10	10	10	10	10	10	10	10	10
11	11	11	11	11	11	11	11	11	11	11	11	11	11
12	12	12	12	12	12	12	12	12	12	12	12	12	12
13	13	13	13	13	13	13	13	13	13	13	13	13	13
14	14	14	14	14	14	14	14	14	14	14	14	14	14
15	15	15	15	15	15	15	15	15	15	15	15	15	15
16	16	16	16	16	16	16	16	16	16	16	16	16	16
17	17	17	17	17	17	17	17	17	17	17	17	17	17
18	18	18	18	18	18	18	18	18	18	18	18	18	18
19	19	19	19	19	19	19	19	19	19	19	19	19	19
20	20	20	20	20	20	20	20	20	20	20	20	20	20
21	21	21	21	21	21	21	21	21	21	21	21	21	21
22	22	22	22	22	22	22	22	22	22	22	22	22	22
23	23	23	23	23	23	23	23	23	23	23	23	23	23
24	24	24	24	24	24	24	24	24	24	24	24	24	24
25	25	25	25	25	25	25	25	25	25	25	25	25	25
26	26	26	26	26	26	26	26	26	26	26	26	26	26
27	27	27	27	27	27	27	27	27	27	27	27	27	27
28	28	28	28	28	28	28	28	28	28	28	28	28	28
29	29	29	29	29	29	29	29	29	29	29	29	29	29
30	30	30	30	30	30	30	30	30	30	30	30	30	30
31	31	31	31	31	31	31	31	31	31	31	31	31	31
32	32	32	32	32	32	32	32	32	32	32	32	32	32
33	33	33	33	33	33	33	33	33	33	33	33	33	33
34	34	34	34	34	34	34	34	34	34	34	34	34	34
35	35	35	35	35	35	35	35	35	35	35	35	35	35
36	36	36	36	36	36	36	36	36	36	36	36	36	36
37	37	37	37	37	37	37	37	37	37	37	37	37	37
38	38	38	38	38	38	38	38	38	38	38	38	38	38
39	39	39	39	39	39	39	39	39	39	39	39	39	39
40	40	40	40	40	40	40	40	40	40	40	40	40	40
41	41	41	41	41	41	41	41	41	41	41	41	41	41
42	42	42	42	42	42	42	42	42	42	42	42	42	42
43	43	43	43	43	43	43	43	43	43	43	43	43	43
44	44	44	44	44	44	44	44	44	44	44	44	44	44
45	45	45	45	45	45	45	45	45	45	45	45	45	45
46	46	46	46	46	46	46	46	46	46	46	46	46	46
47	47	47	47	47	47	47	47	47	47	47	47	47	47
48	48	48	48	48	48	48	48	48	48	48	48	48	48
49	49	49	49	49	49	49	49	49	49	49	49	49	49
50	50	50	50	50	50	50	50	50	50	50	50	50	50
51	51	51	51	51	51	51	51	51	51	51	51	51	51
52	52	52	52	52	52	52	52	52	52	52	52	52	52
53	53	53	53	53	53	53	53	53	53	53	53	53	53
54	54	54	54	54	54	54	54	54	54	54	54	54	54
55	55	55	55	55	55	55	55	55	55	55	55	55	55
56	56	56	56	56	56	56	56	56	56	56	56	56	56
57	57	57	57	57	57	57	57	57	57	57	57	57	57
58	58	58	58	58	58	58	58	58	58	58	58	58	58
59	59	59	59	59	59	59	59	59	59	59	59	59	59
60	60	60	60	60	60	60	60	60	60	60	60	60	60
lat.	19°	13°	14°	15°	16°	17°	18°	19°	20°	21°	22°	23°	lat.

Declination of the Sun.

TABLE VIII.

TIME OF THE SUN'S RISING AND SETTING.

Y

Time of the Sun's rising and setting.

App. time at sunrise when the lat. and dec. are of different names. ^a sunset the same name.															
Declination of the Sun.															
lat.	0°	10	20	30	40	50	60	70	80	90	100	110	120	lat.	
00	00	00	00	00	00	00	00	00	00	00	00	00	00	00	
1	6	0	0	0	0	0	0	0	1	1	1	1	1	1	
2	6	0	0	0	0	0	0	1	1	1	1	1	1	1	
3	6	0	0	0	1	1	1	1	1	1	1	1	1	1	
4	6	0	0	1	1	1	1	1	1	1	1	1	1	1	
5	6	0	0	1	1	1	1	1	1	1	1	1	1	1	
6	6	0	0	1	1	1	1	1	1	1	1	1	1	1	
7	6	0	0	1	1	1	1	1	1	1	1	1	1	1	
8	6	0	0	1	1	1	1	1	1	1	1	1	1	1	
9	6	0	1	1	1	1	1	1	1	1	1	1	1	1	
10	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
11	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
12	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
13	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
14	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
15	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
16	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
17	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
18	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
19	6	1	1	1	1	1	1	1	1	1	1	1	1	1	
20	6	1	3	3	4	4	5	5	6	6	7	7	8	8	
21	6	2	3	3	4	5	5	6	6	7	7	8	8	9	
22	6	2	3	4	4	5	6	6	7	7	8	8	9	9	
23	6	2	3	4	5	5	6	6	7	7	8	8	9	9	
24	6	2	3	4	5	6	6	7	7	8	8	9	9	9	
25	6	2	3	4	5	6	7	7	8	8	9	9	9	9	
26	6	2	3	4	5	6	7	8	8	9	9	9	9	9	
27	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
28	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
29	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
30	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
31	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
32	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
33	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
34	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
35	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
36	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
37	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
38	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
39	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
40	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
41	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
42	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
43	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
44	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
45	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
46	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
47	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
48	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
49	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
50	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
51	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
52	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
53	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
54	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
55	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
56	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
57	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
58	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
59	6	2	3	4	5	6	7	8	9	9	9	9	9	9	
60	6	2	3	4	5	6	7	8	9	9	9	9	9	9	

^a 12°—App. time at sunrise, gives the time of setting.

TABLE IX.

TABLE IX.

Atmospherical Refractions. { Barom. 30 in. { Fa. Therm. 50°					
App. Alt.	Refraction.	Diff. for 10° Therm.	App. Alt.	Refraction.	Diff. for 20° Therm.
10°	5' 20''	07''	50°	1' 49''	09''
11	4 51	6	51	47	9
12	28	5	52	45	9
13	8	5	53	44	9
14	3 50	5	54	42	9
15	34	4	55	41	9
16	20	4	56	39	9
17	9	4	57	38	9
18	2 58	4	58	36	1
19	48	3	59	35	1
20	39	3	60	34	1
21	31	3	61	32	1
22	23	3	62	31	1
23	17	3	63	30	1
24	10	3	64	28	1
25	4	3	65	27	1
26	1 59	2	66	26	1
27	54	2	67	25	1
28	49	2	68	24	1
29	45	2	69	22	1
30	41	2	70	21	1
31	37	2	71	20	1
32	33	2	72	19	1
33	30	2	73	18	1
34	26	2	74	17	1
35	23	2	75	16	1
36	20	2	76	14	1
37	17	2	77	13	1
38	14	1	78	12	1
39	12	1	79	11	1
40	9	1	80	10	0
41	7	1	81	9	
42	5	1	82	8	
43	2	1	83	7	
44	0	1	84	6	
45	0 58	1	85	5	
46	56	1	86	4	
47	54	1	87	3	
48	52	1	88	2	
49	51	1	89	1	
50	49	0	90	0	

* When the Therm. is below 50° the correction in these columns is additive to the refraction.

TABLE X.

Augmentation of the moon's semi-diam't'r.	
Altitude.	Augment.
10°	3''
15	4
20	5
25	7
30	8
35	9
40	10
45	11
50	12
55	13
60	14
70	15
90	16

TABLE XI.

Sun's Alt.	P'l'x in alt.
15°	9''
35	8
45	7
55	6
65	5
76	4
75	3
80	2
85	1

MAURY'S NAVIGATION.

AN ELEMENTARY, PRACTICAL, AND THEORETICAL TREATISE ON NAVIGATION: WITH A NEW AND EASY PLAN FOR FINDING DIFF. LAT., DEP., COURSE, AND DISTANCE BY PROJECTION. BY M. F. MAURY, LIEUT., U. S. NAVY.

OPINIONS OF NAVIGATORS AND PROFESSORS.

Boston, April 21st, 1835.

A work of the kind you are preparing for the press, containing the demonstrations of the formulas of Nautical Astronomy, would be very useful to those who have a taste for the subject, and would like to examine the demonstrations of the rules.

Respectfully,

Your obedient servant,
N. BOWDITCH.

PHILADELPHIA, 14th April, 1835.

DEAR SIR:

I have examined, with as much care as the nature of my engagements has permitted, the book intended for the instruction of the younger officers of the navy, which you have left with me. My opinion is, that such a work will be valuable to them, and will meet with favour among them; supplying, as it does, the mathematical principles involved in the studies of their profession in a sufficiently condensed form.

Coming from one of their own profession, especially, I should anticipate that the work would be received among them, even without the injunction of the authorities, who would, however, I think, find it to the interest of the service to sanction it.

Allow me to say, that I consider the work fully to sustain the high character for scientific acquirement, which I have always heard attributed to its author.

Respectfully yours,

A. D. BACHE, Prof., &c.

The undersigned are of opinion that the work of Lieutenant M. F. Maury, on Navigation, is eminently useful as a school book for nautical students. It illustrates with clearness and simplicity, the principles on which the calculations in navigation are founded.

We felt the want of just such a book in aid of our early studies, and cheerfully recommend it to all who desire to inform themselves in this branch of education, with a view to the nautical profession.

FRANCIS H. GREGORY, Capt.
ROBERT F. STOCKTON, Capt.
FREDERICK ENGLE, Com.
G. A. MAGRUDER, Com.

MY DEAR SIR:

I have great pleasure in stating my belief that it is of the utmost importance that the midshipmen of the navy should have some established work, containing within itself all the information on mathematics and navigation, including nautical astronomy, which they are required to know in order to pass an examination for promo-

mentary, and embrace arithmetic, algebra, geometry, and plane and spherical trigonometry, so far, and so far only, as might be necessary to the construction of all the rules and formulæ requisite to solve the various problems in navigation and surveying. When I was preparing for examination, I felt an earnest desire to possess this information, and to ascend step by step to a complete understanding of the whole subject, so as to have the means of reaching all the processes of which I availed myself by my own resources, without taking any thing on trust. After my promotion I devoted my whole time and attention, for a considerable period, in attaining this object; and feeling how much my own course had been impeded by the want of books containing the required knowledge, I carefully preserved all that I had recourse to for the purpose; such as La Croix, Bezout, Légendre, Lassalle, Borda, and Callet, and determined at my earliest leisure to compile from them a treatise, narrowed down to what was indispensable, so as to spare others, ambitious of more complete information on this branch of professional knowledge than is usual, the great difficulty I had experienced in knowing where to apply for information. The appearance of your work, so exactly supplying what was needed, and, from your infinitely higher mathematical attainments, executed in so superior a manner, to what it would have been had the task been left to me, took from me all motive and desire to go on with the undertaking. After having exerted such commendable exertion, ingenuity, and judgment in accomplishing your task, I trust you may, at least, have the satisfaction of seeing your work generally used by the midshipmen, if not as a manual of practical navigation, which Bowditch's admirable work so effectually supplies, at least as an elementary treatise for the instruction of the young officers of the navy, the more acceptable and encouraging for having been supplied by one, who was, at the time, of their number.

Believe me, very truly,

And respectfully yours,

ALEX. SLIDELL MACKENZIE,
Commander, U. S. Navy.

TARRANTS, 14th November, 1843.

I should not hesitate to commend Maury's Navigation for the use of the midshipmen of our navy. To those of them who are advanced in the elements of the science, it supplies the *practical* information necessary to make them good navigators; others, who have commenced with

of the principles are both ample, easy, and well arranged.

The work, I know, originated in the wants of the students of navigation on board ships, and I confidently believe that it will supply those wants.

L. M. POWELL,
Commander, U. S. Navy.

U. S. NAVY YARD, GOSFORD, }
8th January, 1839. }

SIR:

I am much pleased with your "Treatise on Navigation." The mathematical investigations it affords of the principles of the science, particularly of nautical astronomy, place it upon different grounds from the treatises upon the subject in common use, and adapt it much better to the purpose of instruction. I am desirous of introducing it, as far as may be practicable, among my own classes; and recommend it to all the younger officers in our naval service, who desire to become acquainted with the theory, as well as the practice of the mathematical part of their profession. Its designation as one of the books to be used in their examination, would, I think, conduce to elevate the standard of mathematical attainments among them.

With great regard,
Your obedient servant.

JOHN H. C. COFFIN.
Prof. of Mathematics, U. S. Navy.

WASHINGTON, 20th Dec., 1842.

DEAR SIR:

I have been much interested in a hasty examination of your work upon *Navigation*, more particularly with that part of it, which relates to "Spherical Trigonometry," and "Nautical Astronomy," two branches of navigation that have been too superficially treated in the most popular works upon the subject, to answer the increasing general information of the practical navigators of the present day.

During the last forty years, but little improvement of this kind has been introduced into the standard works upon navigation, and as a general remark, it may be safely asserted that they are behind the wants of those who use them.

Ever anxious for the general diffusion of such important knowledge in our profession, I trust you will be encouraged to introduce the work into the navy as a *Text-Book*. I remain, respectfully, etc.,

JAMES GLYNN,
Commander, U. S. Navy.
Lt. M. F. MAURY, U. S. N.

U. S. SHIP DALE, 23d Oct., 1843.

I feel great pleasure in recommending Maury's *Navigation* as a work of real usefulness and importance to the young officers of our navy.

It embodies whatever can be of utility to the navigator, in a concise and perspicuous manner; and its explanations and references calculated to excite, in youthful and inquisitive minds, a desire for the higher attainments. Having used

the work myself, I know its value, and, therefore, hope it will become the authorized book of study for the midshipmen of our navy.

THOS. A. DORNIN,
Commander, U. S. Navy.

FLAG SHIP PENNSYLVANIA, }
November 4th, 1843. }

MY DEAR SIR:

I have, with great pleasure and care, examined your book on *Navigation*, and do decidedly recommend and prefer it to any other in use. The mathematical principles condensed in such a form, is a sufficient recommendation to every student of navigation, and I recommend it to all mathematicians and young officers belonging to, and at schools attached to the navy, and should think that the Hon. Secretary of the Navy would so order it.

I have the pleasure to remain, with regard,
Your obedient servant,
E. P. KENNEDY,
Lt. M. F. MAURY, U. S. N. P. C., Norfolk.

U. S. SHIP PENNSYLVANIA, }
Nov. 3d, 1843. }

SIR:

I have been much gratified in the perusal of your *Treatise on Navigation*; and think it well adapted for use as a school book, and one best calculated, of any that I have seen, to induce a love for the prosecution of the study of navigation as a science, and not merely as an art.

I am, very respectfully,
Your obedient servant,
A. G. PENDLETON,
Prof. of Mathematics, U. S. Navy.
Lt. M. F. MAURY, U. S. N.

U. S. SHIP OHIO, BOSTON, }
Nov. 14th, 1843. }

SIR:

I have examined, with a good deal of attention, your *Treatise on Navigation*, and find it embraces all the elements necessary to constitute a scientific navigator. It would, I believe, be found a valuable auxiliary in our naval schools.

The work of Dr. Bowditch, although eminently useful as a *practical* one, fails almost entirely in the development of the principles from which its rules are derived.

It seems, therefore, desirable, that some work explaining more fully the *theory* of navigation should be put into the hands of our midshipmen, in order that they may become, as we all desire, *scientific*, as well as *practical* navigators.

Hoping that the pleasure of furnishing such a work for the younger officers of the service may be yours,

I remain, very respectfully,
Your obedient servant,
JOS. T. HUSTON,
Prof. of Mathematics, U. S. Navy.
Lt. M. F. MAURY, U. S. N.

U. S. SHIP BOSTON, BOSTON, }
Nov. 15th, 1843. }

DEAR SIR:

I am much pleased to learn, through the

Army and Navy Chronicle, that a new edition of your valuable Navigator is soon to be published.

I cannot doubt the success of a large second edition, and I am confident that it will add to your reputation, and secure for your book the celebrity which it deserves. Its merit is recognised in the navy, and I would recommend it in all schools of navigation, particularly on account of the manner in which many difficult and obscure points are made easy and plain.

Respectfully, etc.,

G. J. PENDERGRAST.

Commander U. S. Navy.

Lt. M. F. MAURY, U. S. Navy.

WILMINGTON, Del. Nov. 5th, 1843.

I consider Maury's Treatise on Navigation, the very work that has long been wanting in our schools, and I hope it will eventually be used in all of them (particularly the naval ones) instead of Bowditch's Practical Navigator; for I think it far superior as a book of instruction.

J. SHUBRICK,

Commander, U. S. N.

NORFOLK, Nov. 7th, 1843.

I think Maury's Navigation is admirably adapted for the instruction of the young officers of the Navy. All the problems are deduced from theorems, in such a manner as to give the young seaman a correct idea of the theory as well as the practice of navigation. The methods are simple and accurate, and the tables well and carefully constructed. The work contains all that the student of navigation can require; and were it made the authorized text book of the Navy, the standard of mathematical attainments among midshipmen, would be greatly elevated.

R. B. CUNNINGHAM.

Commander, U. S. Navy.

NOVEMBER 8th, 1843.

I possess a copy of Maury's Navigation, and consider it a valuable text-book for all nautical students, whether in the United States Naval Service, or in the commercial marine.

The author, Lieutenant M. F. Maury, U. S. Navy, is a man of science, and has produced this work under the advantage of knowing from experience what the nautical student and practical navigator require.

S. P. LEE,

Lt. U. S. Navy.

U. S. NAVAL HOSPITAL, }
New York, Nov. 10th, 1843. }

SIR:

Your volume seems to me well calculated to achieve the object for which it seems designed: namely, to demonstrate the formulas of Nautical Astronomy, and explain the principles upon which the art of navigation is founded. A better book for schools of navigation, than yours, I am persuaded does not exist in our language. But

after the expression of favourable opinions of it, by such men as Bowditch, Alexander Dallas Bache, P. J. Rodriguez, Edward C. Ward, and John H. C. Coffin, all eminently qualified to judge of such a work, few can doubt its worth or set any value upon the opinion of,

Very respectfully,

Your obedient servant.

W. S. W. RUSCHENBERGER,

Surgeon, U. S. N.

Lieut. M. F. MAURY, U. S. Navy.

U. S. SHIP CUMBERLAND, }
Boston, Nov. 14th, 1843. }

DEAR SIR:

From the cursory examination I have given your treatise on navigation, I, for one, am proud that so useful and valuable a work has been furnished by one of our own corps.

With the improvements you propose to add in the new edition you are preparing, I doubt not it will possess advantages over other works of the kind, and be found a valuable auxiliary in our naval schools.

Very truly yours,

JOSEPH SMITH,

Captain U. S. Navy.

Lieut. M. F. MAURY, U. S. Navy.

WASHINGTON CITY, Nov. 23d, 1843.

DEAR MAURY,

I take this occasion to express to you the pleasure I feel, in noticing the announcement of a new edition of your treatise on navigation. Its subject matter being strictly professional, has called for the close scan of many of your brother officers, myself of the number. Its worthiness to become the text book of our young naval officers, may, with propriety, be judged of by those who are called on to exhibit a certificate of having been closely examined on, and found to possess a thorough knowledge of the subject treated of in your book alluded to.

Without an exception, all of our brother officers, and they are many whom I have heard descant freely on the merits of your work on navigation, pronounced it to be the best text book on that subject extant. In a full concurrence with that opinion,

I am with much esteem,

Respectfully yours truly,

WM. W. HUNTER,

Lieut. U. S. Navy.

Lieut. M. F. MAURY, U. S. Navy.

U. S. BRIG PERRY, }
Norfolk, Va., Nov. 24th, 1843. }

DEAR SIR:

I am pleased to learn you are preparing an improved edition of your Navigation, more especially with the view of instructing the midshipmen in the theory of navigation. To carry the student beyond the mechanical solution of nautical problems, into a comprehension of those principles of Mathematics and Astronomy, upon which these problems are based, seems to be wanting in most treatises on Navigation.

Even Dr. Bowditch's invaluable epitome, that has laid every American, who has to trace his way on the great deep, under a lasting debt of gratitude, is wholly practical in its method. But the value of a Class Book proposing to teach the young officer the theory of one branch of his profession, which imbues his mind with some tincture of science, and raises him above the blind worker of mechanical problems, need not be enlarged upon; though it cannot be better appreciated than by those in the profession, who were deprived of the many advantages now offered to our midshipmen, and who were compelled to prepare for their examination with a Practical Navigator for their sole instructor, and a camp-stool between two guns, for their study room.

Uniformity in instruction too is a matter of great importance, and not doubting that the superior authority, who alone can prescribe the book to be taught, will fully appreciate the honorable contribution afforded by your work, to the character and benefit of the Navy, and that it will be made the standard at the examination of midshipmen,

I remain, my dear sir,
Very sincerely, &c.
S. F. DUFOUR,
Commander, U. S. N.

Lieut. M. F. MAURY, U. S. Navy.

ST. AUGUSTINE, FL. FLORIDA,
Nov. 27th, 1843. }

My opinion can contribute nothing to the established reputation of your valuable work. I can only say, that when I first looked through it, I considered it as thoroughly supplying the great desideratum of a midshipman's study of navigation, and remarked to those who were present, "How unfortunate were we, in not having such a book when we were students of navigation." My opinion has been confirmed by that of other and more competent judges, and I believe that throughout the entire service, there has not been a disparaging voice raised against it. I regard it as being to Bowditch what Bowditch was to Hamilton Moore.

Respectfully, &c.
WM. F. LYNCH,
Lieut. U. S. Navy.

Lieut. M. F. MAURY.

YALE COLLEGE, CONN.
October 26th, 1843. }

This valuable work on Navigation, theoretical and practical, it seems to me desirable to have placed in the hands of every naval officer, who may have occasion to navigate a ship or to explain the principles of Nautical Astronomy. These are well brought out, and illustrated with examples of their application, which render the treatise clear and intelligible, and adapt it well to the purposes of a text book for learners. This book as a guide in the rationale principles of navigation, and Bowditch's companion in the practical computa-

tions, the young officers of our Navy may be well prepared for the important and responsible duties of navigators. Having formerly used the work at sea, while engaged as an instructor in the naval service of the U. S., I cordially give it this recommendation.

JAMES NOONEY, Jr.
Tutor in Nat. Philosophy,
Late Prof. of Math. U. S. N.

SURVEYING SCHR. GALLATIN, }
Philadelphia, Dec. 13th, 1843. }

DEAR SIR:

I have learnt with pleasure that a second edition of your work on Navigation will shortly be published.

I have always considered this book, from its general arrangement, and the kinds of solution employed, as decidedly the best work for students extant.

Believe me, truly yours,
(Signed) GEO. S. BLAKE,
Lt. M. F. MAURY, U. S. N. Washington.

Opinion of Capt. M'INTOSH, U. S. N. }
New York, Dec. 12th, 1843. }

It affords me great pleasure to state, that I consider your work on Navigation, as one of the very best now extant, and most cheerfully recommend it as most suitable for a school book for midshipmen.

Lieut. MAURY.

Opinion of Capt. PERCIVAL, U. S. N. }
U. S. SHIP CONSTITUTION, }
Gosport, Dec. 14th, 1843. }

In compliance with your request, I have perused Maury's "New Theoretical, and Practical Treatise on Navigation," and have found it, as far as I am able to judge, a convenient reference, in illustrating the principles of Nautical Astronomy. Its explanations of the principles of Spherical Trigonometry, and its application of them to the solutions of the various astronomical problems, so essential in navigation, render it a book, in my opinion, not only useful as a supplement to our first (Bowditch's) standard work on the subject; but valuable in itself: an acquisition to the nautical student, who, if he is desirous of acquiring a correct, and practical knowledge of his profession, may be largely aided by the study thereof.

Lt. M. F. MAURY, U. S. N.

Opinion of Capt. FORREST, U. S. N. }
WASHINGTON, Dec. 18th, 1843. }

I take much pleasure in recommending your "New Theoretical and Practical Treatise on Navigation." The explanations and illustrations are rendered clear and comprehensive, and I believe it to be just such a production as we require for the instruction of the young officers of our Navy, as well as others desirous of obtaining a well grounded and accurate knowledge of the science.

Lt. M. F. MAURY, U. S. N.

*Opinion of the U. S. Naval Lyceum, }
Brooklyn, New York. }
BROOKLYN, Dec. 20th, 1843.*

The undersigned, a committee to which was referred Lieut. Maury's "Treatise on Navigation," report that they have carefully examined the same, and are of opinion that it is a work well adapted for the instruction of the young officers of the Navy, as all the problems and formulæ that are necessary in their profession, are there brought together in a condensed form, and so clearly, and concisely demonstrated, that the student may easily inform himself of the theory and principles on which his practice is founded; and the accompanying tables are so constructed as to facilitate his calculations; all of which are systematically arranged, with a simplicity that has heretofore been generally wanting in works on Navigation. They would therefore recommend the same to be adopted for the use of the Naval schools.

Signed,
J. H. STRINGHAM,
WM. D. NEWMAN,
ALEX. C. GIBSON.

The following opinions have already appeared in print, but as they have in all probability escaped the notice of many to whom these pages will be presented, they are again inserted here.

"U. S. N. S., New York, January 19, 1836.

"Dear Sir,—I have had much pleasure in the perusal of your "New Theoretical and Practical Treatise on Navigation;" the plan and arrangements of which are original; it contains little or nothing superfluous, and every part of it appears to be as clear and intelligible as the nature of the subject will admit. Such a work has long been wanted in our Naval Schools, and on board our vessels of war. I intend to make use of it in the Naval School on this station; and I recommend it to be used by all the professors of Mathematics and Nautical Science, in the Navy of the United States.

"Yours Respectfully,

"EDW. C. WARD,

"Prof. Math. U. S. Navy."

"Passed Midshipman M. F. Maury,

"U. S. Navy."

"U. S. Navy Yard, Gosport, March 7, 1836.

"I have examined a Treatise on Navigation written by M. F. Maury of the U. S. Navy; and have no hesitation in recommending it to the students of that science. The explanations are clear, the rules are illustrated by many examples, and the new arrangement of some of the tables simplify the calculations of the navigator. Mr. Maury is deserving of great credit for the work, and I wish him every success.

P. J. RODRIGUEZ.