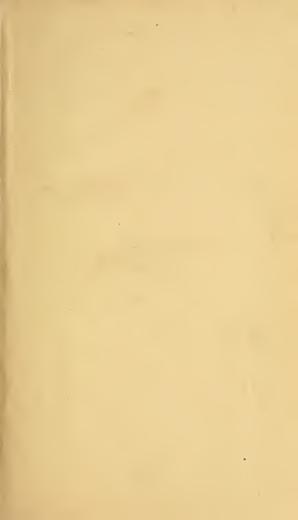


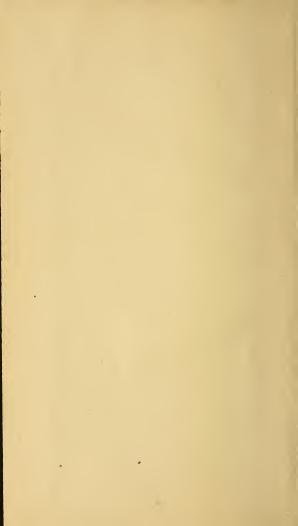


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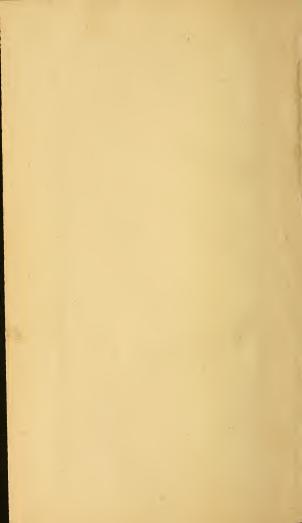
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# MECHANICAL ENGINEER'S POCKET-BOOK.

915

A REFERENCE-BOOK OF RULES, TABLES, DATA,

AND FORMULÆ, FOR THE USE OF

ENGINEERS, MECHANICS,

AND STUDENTS.

MAY 6 11895

BY

# WILLIAM KENT, A.M., M.E.,

Consulting Engineer, Member Amer. Soc'y Mechl. Engrs. and Amer Inst. Mining Engrs.

FIRST THOUSAND.

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## PREFACE.

More than twenty years ago the author began to follow the advice given by Nystrom: "Every engineeer should make his own pocket-book, as he proceeds in study and practice, to suit his particular business." The manuscript pocket-book thus begun, however, soon gave place to more modern means for disposing of the accumulation of engineering facts and figures, viz., the index rerum, the scrapbook, the collection of indexed envelopes, portfolios and boxes, the card catalogue, etc. Four years ago, at the request of the publishers, the labor was begun of selecting from this accumulated mass such matter as pertained to mechanical engineering, and of condensing, digesting, and arranging it in form for publication. In addition to this, a careful examination was made of the transactions of engineering societies, and of the most important recent works on mechanical engineering, in order to fill gaps that might be left in the original collection, and insure that no important facts had been overlooked.

Some ideas have been kept in mind during the preparation of the Pocket-book that will, it is believed, cause it to differ from other works of its class. In the first place it was considered that the field of mechanical engineering was so great, and the literature of the subject so vast, that as little space as possible should be given to subjects which especially belong to civil engineering. While the mechanical engineer must continually deal with problems which belong properly to civil engineering, this latter branch is so well covered by Trautwine's "Civil Engineer's Pocketbook" that any attempt to treat it exhaustively would not only fill no "long-felt want," but would occupy space which should be given to mechanical engineering.

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Another idea prominently kept in view by the author has been that he would not assume the position of an "authority" in giving rules and formulæ for designing, but only that of compiler, giving not only the name of the originator of the rule, where it was known, but also the volume and page from which it was taken, so that its derivation may be traced when desired. When different formulæ for the same problem have been found they have been given in contrast, and in many cases examples have been calculated by each to show the difference between them. In some cases these differences are quite remarkable, as will be seen under Safety-valves and Crank-pins. Occasionally the study of these differences has led to the author's devising a new formula, in which case the derivation of the formula is given.

Much attention has been paid to the abstracting of data of experiments from recent periodical literature, and numerous references to other data are given. In this respect the present work will be found to differ from other Pocketbooks.

The author desires to express his obligation to the many persons who have assisted him in the preparation of the work, to manufacturers who have furnished their catalogues and given permission for the use of their tables, and to many engineers who have contributed original data and tables. The names of these persons are mentioned in their proper places in the text, and in all cases it has been endeavored to give credit to whom credit is due. The thanks of the author are also due to the following gentlemen who have given assistance in revising manuscript or proofs of the sections named: Prof. De Volson Wood, mechanics and turbines; Mr. Frank Richards, compressed air: Mr. Alfred R. Wolff, windmills; Mr. Alex. C. Humphreys, illuminating gas; Mr. Albert E. Mitchell, locomotives; Prof. James E. Denton, refrigerating-machinery: Messrs. Joseph Wetzler and Thomas W. Varley, electrical engineering; and Mr. Walter S. Dix, for valuable contributions on several subjects, and suggestions as WM. KENT. to their treatment.

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# AND ABBREVIATIONS OF PERIODICALS NAMES AND TEXT-BOOKS FREQUENTLY REFERRED TO IN THIS WORK.

Am, Mach. American Machinist. Bull, I. & S. A. Bulletin of the American Iron and Steel Association (Philadelphia).

Burr's Elasticity and Resistance of Materials. Clark, R. T. D. D. K. Clark's Rules, Tables, and Data for Mechanical Engineers.

D. K. Clark's Treatise on the Steam-engine.

Clark, S. E. D. K. Clark's Treatise on the Stea Engg. Engineering (London). Eng. News. Engineering News. Engr. The Engineer (London). Fairbairn's Useful Information for Engineers. Fairbairn's Useful Information for Engineers.

Fantomer's Oscill Information for Engineers, Flynn's Irrigation Canals and Flow of Water, Jour, A. C. I. W. Journal of American Charcoal Iron Workers' Association. Jour, F. J. Journal of the Franklin Institute.

Kapp's Electric Transmission of Energy.

Merriman's Strength of Materials.

Lanza's Applied Mechanics.

Proc. Inst. C. E. Proceedings Institution of Civil Engineers (London),

Proc. Inst. M. E. Proceedings Institution of Mechanical Engineers (London).

Proc. 118t. B. E. Frocecungs Institution of Administration of Admi

Rontgen's Thermodynamics. Seaton's Manual of Marine Engineering.

Seaton's Manual of Marine Engineering.
Hamilton Smith, Jr.'s Hydraulics.
The Stevens Indicator.
Thompson's Dynamo-electric Machinery.
Thurston's Manual of the Steam Engine.
Thurston's Materials of Engineering.
Trans. A. I. E. E. Transactions American Institute of Electrical Engineers.
Trans. A. I. M. E. Transactions American Institute of Mining Engineers.
Trans. A. S. C. E. Transactions American Society of Civil Engineers.
Trans. A. S. M. E. Transactions American Society of Mechanical Engineers
Trantwine's Civil Engineer's Focket Book.
The Locomotive (Hartford, Connecticut).

Unwin's Elements of Machine Design. Weisbach's Mechanics of Engineering.

Wood's Resistance of Materials,

Wood's Thermodynamics.



# MATHEMATICS.

# Arithmetical and Algebraical Signs and Abbreviations.

∠ angle.

```
+ plus (addition).

    positive.

- minus (subtraction).
- negative.
± plus or minus.

∓ minus or plus.
= equals.
× multiplied by.
ab \text{ or } a.b = a \times b.

\Rightarrow \text{ divided by.}
/ divided by.
  or a-b = a/b = a \div b.
  =\frac{2}{10}; .002 = \frac{2}{1000}.
square root.
 v cube root.
 1/4th root.
: is to, :: so is, : to (proportion).
 2: 4: 3: 6, as 2 is to 4 so is 3 to 6.
: ratio; divided by.
 2:4, ratio of 2 to 4=2/4.
 . therefore.
> greater than.
< less than.
g square.
o round.
 degrees, arc or thermometer.
 ' minutes or feet.
 " seconds or inches.
"" accents to distinguish letters, as
       a', a", a".
a1, a2, a3, ab, ac. read a sub 1, a sub b,
      etc.
()[] { --- vincula, denoting
       that the numbers enclosed are
       to be taken together; as,
       (a+b)c = 4+3 \times 5 = 35.
a2, a3, a squared, a cubed.
an, a raised to the nth power,
a^{\frac{2}{3}} = \sqrt[3]{a^2}, a^{\frac{3}{2}} = \sqrt{a^3}.
a^{-1} = \frac{1}{a}, a^{-2} = \frac{1}{a^2}
10^9 = 10 to the 9th power = 1,000,000,-
```

000.

 $\sin a^{-1} = \frac{1}{\sin a}$ 

log. = logarithm.

 $\sin \alpha =$ the  $\sin \alpha$ 

```
L right angle.
                                                 perpendicular to.
                                                sin., sine.
                                                cos., cosine,
                                                tang., or tan., tangent.
                                                sec., secant.
                                                versin., versed sine.
                                                cot., cotangent.
                                                cosec., cosecant.
                                                covers., co-versed sine.
                                                  In Algebra, the first letters of the
                                               alphabet, a, b, c, d, etc., are generally used to denote known quantities,
                                                and the last letters, w, x, y, z, etc.,
                                                unknown quantities.
                                                 Abbreviations and Symbols com-
                                                               monly used.
                                                d, differential (in calculus).
                                                   integral (in calculus).
                                                   , integral between limits a and b.
                                                Δ, delta, difference
                                                Σ, sigma, sign of summation.
                                                π, pi, ratio of circumference of circle
                                                       to diameter = 3.14159.
                                                g, acceleration due to gravity = 32.16
                                                       ft. per sec.
                                                Abbreviations frequently used in
                                                                this Book.
                                                L., l., length in feet and inches.B., b., breadth in feet and inches.
                                                D., d., depth or diameter.
                                                H., h., height, feet and inches.
                                                T., t., thickness or temperature.
                                                V., v., velocity
                                                F., force, or factor of safety.
                                                f., coefficient of friction.
                                                E., coefficient of elasticity.
                                                R., r., radius.
W., w., weight.
                                                H.P., pressure or load.
H.P., horse-power.
I.H.P., indicated horse-power.
B.H.P., brake horse-power.
                                                h. p., high pressure.
                                                i. p., intermediate pressure.
l. p., low pressure.
A. W. G., American Wire Gauge
\sin - \alpha =  the arc whose sine is \alpha.
                                                                       (Brown & Sharpe).
                                                B.W.G., Birmingham Wire Gauge.
log. or hyp. log. = hyperbolic logarithm.
                                              r. p. m., or revs. per min., revolutions
                                                          per minute.
```

# ARITHMETIC.

The user of this book is supposed to have had a training in arithmetic as well as in elementary algebra. Only those rules are given here which are apt to be easily forgotten.

# GREATEST COMMON MEASURE, OR GREATEST COMMON DIVISOR OF TWO NUMBERS.

Rule. Divide the greater number by the less; then divide the divisor by the remainder, and so on, dividing always the last divisor by the last remainder, until there is no remainder, and the last divisor is the greatest common measure required.

# LEAST COMMON MULTIPLE OF TWO OR MORE NUMBERS.

Rule .- Divide the given numbers by any number that will divide the greatest number of them without a remainder, and set the quotients with the undivided numbers in a line beneath,

Divide the second line as before, and so on, until there are no two numbers that can be divided; then the continued product of the divisors and last quotients will give the multiple required.

# FRACTIONS.

To reduce a common fraction to its lowest terms.-Divide

both terms by their greatest common divisor:  $\frac{39}{5} = \frac{3}{4}$ To change an improper fraction to a mixed number.— Divide the numerator by the denominator; the quotient is the whole number,

and the remainder placed over the denominator is the fraction:  $\frac{34}{4} = 9\frac{3}{4}$ .

To change a mixed number to an improper fraction.

Multiply the whole number by the denominator of the fraction, to the product add the numerator; place the sum over the denominator:  $1\frac{1}{4} = \frac{14}{4}$ . To express a whole number in the form of a fraction with a given denominator.—Multiply the whole number by the given denominator and place the product over that denominator;  $13 = \frac{39}{4}$ . To reduce a compound to a simple fraction, also to multiply fractions,—Multiply the numerator stogether for a new numerator and the denominators together for a new denominator:

$$\frac{2}{3}$$
 of  $\frac{4}{3} = \frac{8}{9}$ , also  $\frac{2}{3} \times \frac{4}{3} = \frac{8}{9}$ .

To reduce a complex to a simple fraction.—The numerator and denominator must each first be given the form of a simple fraction; then multiply the numerator of the upper fraction by the denominator of the lower for the new numerator, and the denominator of the upper by the numerator of the lower for the new edenominator.

$$\frac{\frac{2}{3}}{1\frac{1}{3}} = \frac{\frac{2}{3}}{\frac{3}{3}} = \frac{6}{12} = \frac{1}{2}.$$

To divide fractions .- Reduce both to the form of simple fractions, invert the divisor, and proceed as in multiplication:

$$\frac{2}{9} \div 1\frac{1}{3} = \frac{2}{9} \div \frac{4}{3} = \frac{2}{9} \times \frac{3}{4} = \frac{6}{19}$$

Cancellation of fractions.—In compound or multiplied fractions. divide any numerator and any denominator by any number which will divide them both without remainder, striking out the numbers thus divided and setting down the quotients in their stead.

To reduce fractions to a common denominator.—Reduce each fraction to the form of a simple fraction; then multiply each numera-

tor by all the denominators except its own for the new numerators, and all the denominators together for the common denominator;

$$\frac{1}{2}$$
,  $\frac{1}{3}$ ,  $\frac{3}{7} = \frac{21}{42}$ ,  $\frac{14}{42}$ ,  $\frac{18}{42}$ .

To add fractions .- Reduce them to a common denominator, then add the numerators and place their sum over the common denominator:

$$\frac{1}{2} + \frac{1}{3} + \frac{3}{7} = \frac{21 + 14 + 18}{42} = \frac{58}{42} = 1\frac{11}{42}$$

To subtract fractions .- Reduce them to a common denominator. subtract the numerators and place the difference over the common denominator:

$$\frac{1}{2} - \frac{3}{7} = \frac{7 - 6}{14} = \frac{1}{14}.$$

### DECIMALS.

To add decimals. - Set down the figures so that the decimal points are one above the other, then proceed as in simple addition: 18.75 + .012 =18,762,

To subtract decimals .- Set down the figures so that the decimal

points are one above the other, then proceed as in simple subtraction: 18.75 0.012 = 18.738

-.012 = 18.738.
To multiply decimals.—Multiply as in multiplication of whole numbers, then point off as many decimal places as there are in multiplier and multiplicand taken together: 1.5 × 0.02 = .030 = .03.
To divide decimals.—Divide as in whole numbers, and point off in the quotient as many decimal places as those in the dividend exceed those in the divisor. Ciphers must be added to the dividend to make its decimal places at least equal those in the divisor, and as many more as it is desired to have in the quotient: 1.5 + .25 = 6. 0.1 + 0.3 = 0.10000 + 0.3 = 0.3333 +

# Decimal Equivalents of Fractions of One Inch.

			_				
1-64	.015625	17-64	.265625	33-64	.515625	49-64	.765625
1-32	.03125	9-32	.28125	17-32	.53125	25-32	.78125
3-64	.046875	19-64	.296875	35-64	.546875	51-64	.796875
1-16	.0625	5=16	.3125	9-16	.5625	13-16	.8125
5-64	.078125	21- 64	.328125	37-64	.578125	53-64	.828125
3-32	.09375	11-32	.34375	19-32	.59375	27-32	.84375
7-64	.109375	23-64	.359375	39-64	.609375	55-64	.859375
<b>1-</b> 8	.125	3-8	.375	5=8	.625	7-8	.875
9-64	.140625	25-64	.390625	41-64	.640625	57-64	.890625
5-32	.15625	13-32	.40625	21-32	.65625	29-32	.90625
11-64	.171875	27-64	.421875	43-64	.671875	59-64	.921875
<b>3-1</b> 6	.1875	7-16	.4375	11-16	.6875	15-16	.9375
13-64 7-32 15-64 1-4	.208125 .21875 .234375 .25	29-64 15-32 31-64 1-2	.453125 .46875 .484375 .50	45-64 23-32 47-64 3-4	.708125 .71875 .734875 .75	61-64 31-32 63-64 1	.953125 .96875 .984375

To convert a common fraction into a decimal.—Divide the numerator by the denominator, adding to the numerator as many ciphers prefixed by a decimal point as are necessary to give the number of decimal places desired in the result:  $\frac{1}{2} = 1.0000 + 3 = 0.3333 + 1.0000$  From the results of the r

the decimal as a numerator, and place as the denominator 1 with as many ciphers annexed as there are decimal places in the numerator; erase the

Product of Fractions Expressed in Decimals.

					An	.111	11 M	CII	C.							
- 1																1.000
1 6															.8789	.9375
∞ <del> -</del> 1														.7656	.8203	.8750
111													1099	.7109	.7617	.8125
c3 4+								-				.5625	.6094	.6563	.7031	.7500
11											.4727	.5156	.5586	.6016	.6445	.6875
10/00										.3906	.4397	.4688	.5078	.5469	.5859	.6250
1 6									.3164	,3516	.3867	.4219	.4570	.4999	.5273	.5625
⊢(c3								.2500	.2813	.3125	.2438	.3750	.4063	.4375	.4688	.5000
$\frac{7}{16}$							.1914	.2188	.2461	.2734	3008	.3281	.3555	.3828	.4102	.4375
cc co						.1406	.1641	.1875	.2109	.2344	.2578	.2813	.3047	.3281	.3516	.3750
16					7760.	.1172	.1367	.1562	.1758	.1953	.2148	.2344	.2539	.2734	.2930	.3125
H4				.0625	.0781	.0937	.1093	.1350	.1406	.1562	.1719	.1875	.2031	.2187	.2344	.2500
1 6			.0852	0409	.0586	.0703	0880	.0938	.1055	.1172	.1289	.1406	.1523	.1641	.1758	.1875
<b>⊢</b>  ∞		.0156	.0234	.0313	.0391	.0469	.0547	.0625	.0703	.0781	.0859	8860.	9101.	.1094	.1172	.1350
1 6	.0039	8200.	.0117	.0156	.0195	.0234	.0273	.0313	.0352	1680.	.0430	6950.	.0508	.0547	.0586	.0625
1	.0625	.1350	.1875	.2500	.3125	.3750	.4375	.5000	.5635	.6250	6875	.7500	.8125	.8750	.9375	1.000
0	16	r(x)	200	4	102	00 00	12	- c1	100	rojos	14	60 <del> 4</del>	13	F- 30	15	1

decimal point in the numerator, and reduce the fraction thus formed to its lowest terms:

.25 = 
$$\frac{25}{100} = \frac{1}{4}$$
; .3333 =  $\frac{3333}{10000} = \frac{1}{3}$ , nearly.

To reduce a recurring decimal to a common fraction.— Subtract the decimal figures that do not recur from the whole decimal including one set of recurring figures; set down the remainder as the numerator of the fraction, and as many nines as there are recurring figures, followed by as many ciphers as there are non-recurring figures, in the denominator. Thus:

.79054054, the recurring figures being 054.

Japarace

$$\frac{78975}{99900}$$
 = (reduced to its lowest terms)  $\frac{117}{148}$ .

# COMPOUND OR DENOMINATE NUMBERS.

Reduction descending,—To reduce a compound number to a lower denomination. Multiply the number by as many units of the lower denomination as makes one of the higher.

3 yards to inches:  $3 \times 36 = 108$  inches.

.04 square feet to square inches:  $.04 \times 144 = 5.76$  sq. in.

If the given number is in more than one denomination proceed in steps from the highest denomination to the next lower, and so on to the lowest, adding in the units of each denomination as the oper tion proceeds.

3 vds, 1 ft. 7 in, to inches: 
$$3 \times 3 = 9$$
,  $+1 = 10$ ,  $10 \times 12 = 120$ ,  $+7 = 127$  in.

Reduction ascending.—To express a number of a lower denomination in terms of a higher, divide the number by the numb r of units of the lower denomination contained in one of the next higher; the quotient is in the higher denomination, and the remainder, if any, in the lower.

127 inches to higher denomination.

$$127 \div 12 = 10 \text{ feet} + 7 \text{ inches}; \quad 10 \text{ feet} \div 3 = 3 \text{ yards} + 1 \text{ foot.}$$
Ans. 3 yds. 1 ft. 7 in.

To express the result in decimals of the higher denomination, divide the given number by the number of units of the given denomination contained in one of the required denomination, carrying the result to as many places of decimals as may be desired.

127 inches to yards:  $127 \div 36 = 3\frac{19}{12} = 3.5277 + \text{yards}$ .

# RATIO AND PROPORTION.

Ratio is the relation of one number to another, as obtained by dividing one by the other.

Ratio of 2 to 4, or 2 : 
$$4 = 2/4 = 1/2$$
.  
Ratio of 4 to 2, or 4 :  $2 = 2$ .

**Proportion** is the equality of two ratios. Ratio of 2 to 4 equals ratio of 3 to 6, 2/4 = 3/6; expressed thus, 2:4::3:6; read, 2 is to 4 as 3 is to 6. The first and fourth terms are called the extremes or outer terms, the second and third the means or inner terms.

The product of the means equals the product of the extremes;

$$2:4::3:6; 2\times 6=12; 3\times 4=12.$$

Hence, given the first three terms to find the fourth, multiply the second and third terms together and divide by the first.

2:4::3: what number? Ans. 
$$\frac{4 \times 3}{2} = 6$$
.

Algebraic expression of proportion.  $-a:b::c:d; \frac{a}{b} = \frac{c}{d}; ad$ = bc; from which  $a = \frac{bc}{d}; d = \frac{bc}{a}; b = \frac{ad}{c}; c = \frac{ad}{b}.$ 

Mean proportional between two given numbers, 1st and 2d, is such a number that the ratio which the first bears to it equals the ratio which it bears to the second. Thus, 2: 4: 1: 4: 8; 4 is a mean proportional between 2 and 8. To find the mean proportional between two numbers, extract the square root of their product.

Mean proportional of 2 and 
$$8 = \sqrt[4]{2 \times 8} = 4$$
.

Single Rule of Three; or, finding the fourth term of a proportion when three terms are given.—Rule, as above, when the terms are stated in their proper order, multiply the second by the third and divide by the first. The difficulty is to state the terms in their proper order. The term which is of the same kind as the required or fourth term is made the third; the first and second must be like each other in kind and decomination. To direct mine which is to be made second and which first requires a little reasoning. If an inspection of the problem shows that the answer should be greater than the third term, then the greater of the other two given terms should be made the second term—otherwise the first. Thus, 3 men remove 34 cubic feet of rock in a day; how many men will remove in the same time 10 cubic yards? The answer is to be more than three men, therefore make the greater quantity, 10 cubic yards, the second term; but as it is not the same denomination as the other term it must be reduced, = 270 cubic feet. The proportion is then stated:

54: 270:: 3: 
$$x$$
 (the required number);  $x = \frac{3 \times 270}{54} = 15$  men.

The problem is more complicated if we increase the number of given terms. Thus, in the above question, substitute for the words "in the same time" the words "in 3 days." First solve it as above, as if the work were to be done in the same time: then make another proportion, stating it thus: If 15 men do it in the same time, it will take fewer men to do it in 3 days; make 1 day the 2d term and 3 days the first term. 3:1::15 men; 5 men.

to be done in the same time; then make another proportion, stating it thus: If 15 men do it in the same time, it will take fewer men to do it in 3 days; make 1 day the 2d term and 3 days the first term 3:1::15 men:5 men. Compound Proportion, or Double Rule of Three.—By this rule are solved questions like the one just given, in which two or more statings are required by the single rule of three. In it as in the single rule, there is one third term, which is of the same kind and denomination as the fourth or required term, but there may be two or more first and second terms. Set down the third term, take each pair of terms of the same kind separately, and arrange them as first and second by the same reasoning as is adopted in the single rule of three, making the greater of the pair the second if this pair considered alone should require the answer to be greater.

Set down all the first terms one under the other, and likewise all the second terms. Multiply all the first terms together and all the second terms together. Multiply the product of all the second terms by the third term, and divide this product by the product of all the first terms. Example: If 3 men remove 4 cubic yards in one day, working 12 hours a day, how many men working 10 hours a day will remove 20 cubic yards in 3 days?

To abbreviate by cancellation, any one of the first terms may cancel either the third or any of the second terms; thus, 3 in first cancels 3 in third, making it 1, 10 cancels into 20 making the latter 2, which into 42 makes it 2, which into 12 makes it 6, and the figures remaining are only 1: 6:: 1: 6.

# INVOLUTION, OR POWERS OF NUMBERS.

**Involution** is the continued multiplication of a number by itself a given number of times. The number is called the root, or first power, and the products are called powers. The second power is called the square and

the third power the cube. The operation may be indicated without being the third power the cube. The operation may be indicated without being performed by writing a small figure called the index or exponent to the right of and a little above the root; thus,  $3^3 = \text{cube of } 3$ , = 27. To multiply two or more powers of the same number, add their exponents; thus,  $2^2 \times 2^3 = 2^5$ , or  $4 \times 8 = 32 = 2^5$ . To divide two powers of the same number, subtract their exponents; thus,

1  $2^3 \div 2^2 = 2^1 = 2$ ;  $2^2 \div 2^4 = 2^{-2}$  $=\frac{1}{2^2}=\frac{1}{4}$ . The exponent may thus be negative.  $2^3 + 2^3 = 2^0 = 1$ , whence the zero power of any number = 1. The first power of a number is the number itself. The exponent may be fractional, as  $2^{\frac{1}{2}}$ ,  $2^{\frac{2}{3}}$ , which means that the root is to be raised to a power whose exponent is the numerator of the fraction, and the root whose sign is the exponent is to be influenced or the fraction, and the root whose Sign is the denominator is to be extracted (see Evolution). The exponent may be a decimal, as 2<sup>9-3</sup>, 2<sup>9-3</sup>, read, two to the five-tenths power, two to the one and five-tenths power. Those powers are solved by means of Logarithms (which

## First Nine Powers of the First Nine Numbers.

1st Pow'r	2d Pow'r	3d Power.	4th Power.	5th Power.	6th Power.	7th Power.	8th Power.	9th Power.
1	1	1	1	1	1	1	1	1
9	4	8	16	32	64	128	256	512
2 3	9	1 8 27	16 81	243	729	2187	6561	19683
4 5	16	64	256	1024	4096	16384	65536	262144
5	25	125	625	3125	15625	78125	390625	1953125
	-00	242	*200	www.a	10000	200000	4000040	400000000
6	36	216	1296	7776	46656	279936	1679616	10077696
7	49	343	2401	16807	117649	823543	5764801	40353607
8 9	64	512	4096	32768	262144	2097152	16777216	134217728
9	81	729	6581	59049	531441	4782969	43046721	387420489

# The First Forty Powers of 2.

Power.	Value.	A A A		Power,		Power.	Value.	Power.	Value.
0	1	9	512	18	262144	27	134217728	36	68719476736
1	2	10	1024	19	524288	28	268435456	37	137438953472
2	4	11	2048	20	1048576	29	536870912	38	274877906944
3	8	12	4096	21	2097152	30	1073741824	39	549755813888
4	16	13	8192	22	4194304	31	2147483648	40	1099511627776
5	32	14	16384	23	8388608	32	4294967296		
6	64	15	32768	24	16777216	33	8589934592		
7	128	16	65536	25	33554432	34	17179869184		
8	256	17	131072	26	67108864	35	34350738368		

### EVOLUTION.

Evolution is the finding of the root (or extracting the root) of any number the power of which is given.

The sign  $\sqrt{1}$  indicates that the square root is to be extracted:  $\sqrt[3]{4} \sqrt[3]{4}$ , the cube root, 4th root, nth root.

A fractional exponent with 1 for the numerator of the fraction is also used to indicate that the operation of extracting the root is to be performed; thus,  $2^{\frac{1}{3}}$ ,  $2^{\frac{1}{3}} = \sqrt{2}$ ,  $\sqrt[3]{2}$ .

When the power of a number is indicated, the involution not being performed, the extraction of any root of that power may also be indicated by dividing the index of the power by the index of the root, indicating the division by a fraction. Thus, extract the square root of the 6th power of 2:

$$\sqrt{2^6} = 2^{\frac{6}{2}} = 2^{\frac{3}{1}} = 2^3 = 8.$$

The 6th power of 2, as in the table above, is 64;  $\sqrt{64} = 8$ .

Difficult problems in evolution are performed by logarithms, but the square root and the cube root may be extracted directly according to the rules given below. The 4th root is the square root of the square root. The 6th root is the cube root of the square root, or the square root of the cube

root is the cube root of the square root, or the square root of the cube root; the 9th root is the cube root of the cube root; etc.

To Extract the Square Root.—Point off the given number into periods of two places each, beginning with units. If there are decimals, point these off likewise, beginning at the decimal point, and supplying as many ciphers as may be needed. Find the greatest number whose square is less than the first left-hand period, and place it as the first figure in the quotient. Subtract its square from the left-hand period, and to the remainder annex the two figures of the second period for the root of the root of the second period for the root of the a dividend. Double the first figure of the quotient for a partial divisor; find how many times the latter is contained in the dividend exclusive of the right-hand figure, and set the figure representing that number of times as the second figure in the quotient, and annex it to the right of the partial divisor, forming the complete divisor. Multiply this divisor by the second figure in the quotient and subtract the product from the divi-dend. To the remainder bring down the next period and proceed as before, in each case doubling the figures in the rest closed if round to obtain the tine ach case doubling the figures in the root already found to obtain the trial divisor. Should the product of the second figure in the root by the completed divisor be greater than the dividend, erase the second figure both from the quotient and from the divisor, and substitute the next smaller figure, or one small enough to make the product of the second figure by the divisor less than or equal to the dividend.

To extract the square root of a fraction, extract the root of numerator and denominator separately.  $\sqrt{\frac{4}{9}} = \frac{2}{3}$ , or first convert the fraction into a

decimal, 
$$\sqrt{\frac{4}{9}} = \sqrt{.4444 +} = .6666 +$$
.

To Extract the Cube Root .- Point off the number into periods of 3 figures each, beginning at the right hand, or unit's place. Point off decimals in periods of 3 figures from the decimal point. Find the greatest cube that does not exceed the left-hand period; write its root as the first figure in the required root. Subtract the cube from the left-hand period, and to the remainder bring down the next period for a dividend.

Square the first figure of the root; multiply by 300, and divide the product into the dividend for a trial divisor; write the quotient after the first figure

of the root as a trial second figure.

Complete the divisor by adding to 300 times the square of the first figure, 30 times the product of the first by the second figure, and the square of the second figure. Multiply this divisor by the second figure; subtract the product from the remainder. (Should the product be greater than the remainder, the last figure of the root and the complete divisor are too large;

substitute for the last figure the next smaller number, and correct the trial divisor accordingly.)

To the remainder bring down the next period, and proceed as before to find the third figure of the root—that is, square the two figures of the root already found; multiply by 300 for a trial divisor, etc. If at any time the trial divisor is less than the dividend, bring down an-

other period of 3 figures, and place 0 in the root and proceed.

The cube root of a number will contain as many figures as there are periods of 3 in the number.

Shorter Methods of Extracting the Cube Root.—1. From Wentworth's Algebra:

After the first two figures of the root are found the next trial divisor is found by bringing down the sum of the 60 and 4 obtained in completing the preceding divisor, then adding the three lines connected by the brace, and annexing two ciphers. This method shortens the work in long examples, as is seen in the case of the last two trial divisors, saving the labor of squaring 123 and 1234. A further shortening of the work is made by obtaining the last two figures of the root by division, the divisor employed being three times the square of the part of the root already found; thus, after finding the first three figures:

$$3 \times 123^2 = 45387 | 20498963 | 45.1 + \\ 181548 \\ \hline 234416 \\ \underline{226935} \\ \hline 74813$$

The error due to the remainder is not sufficient to change the fifth figure of the root.

By Prof. H. A. Wood (Stevens Indicator, July, 1890);
 I. Having separated the number into periods of three figures each, counting from the right, divide by the square of the nearest root of the first period, or first two periods; the nearest root is the trial root.

II. To the quotient obtained add twice the trial root, and divide by 3. This gives the root, or first approximation.

III. By using the first approximate root as a new trial root, and proceeding as before, a nearer approximation is obtained, which process may be repeated until the root has been extracted, or the approximation carried as far as desired.

EXAMPLE.—Required the cube root of 20. The nearest cube to 20 is 33,

$$3^{2} = 9)\underline{30.0}$$

$$\underline{2.2}$$

$$6$$

$$3)\underline{8.1}$$

$$2.7^{2} = 7.29)\underline{20.000}$$

$$\underline{2.743}$$

$$5.4$$

$$3)\underline{8.143}$$

$$2.714, 1st ap. cube root.$$

 $2.714^2 = 7.365796)20.0000000$ 

2.7152584 5.428 3)8.1432584

2.7144178 2d ap. cube root.

REMARK.—In the example it will be observed that the second term, or first two figures of the root, were obtained by using for trial root the root of the first period. Using, in like manner, these two terms for trial root, we obtained four terms of the root; and these four terms for trial root gave seven figures of the root correct. In that example the last figure should be 7. Should we take these eight figures for trial root we should obtain at least fifteen figures of the root correct.

To Extract a Higher Root than the Cube.—The fourth root is the square root of the square root; the sixth root is the cube root of the square root or the square root of the cube root. Other roots are most conveniently found by the use of logarithms.

### ALLIGATION

shows the value of a mixture of different ingredients when the quantity and value of each is known.

Let the ingredients be a, b, c, d, etc., and their respective values per unit w, x, y, z, etc.

A =the sum of the quantities = a + b + c + d, etc.

P = mean value or price per unit of A.

r = mean value or price per un

AP = aw + bx + cy + dz, etc.  $P = \frac{aw + bx + cy + dz}{A}.$ 

### PERMITATION

shows in how many positions any number of things may be arranged in a row; thus, the letters a,b,c may be arranged in six positions, viz. abc,acb,cad,bca,bac,bca.

Rule.—Multiply together all the numbers used in counting the things; thus, permutations of 1, 2, and  $3 = 1 \times 2 \times 3 = 6$ . In how many positions can 9 things in a row be placed ?

 $1 \times 2 \times 3 \times 4 \times 5 \times 6 \times 7 \times 8 \times 9 = 362880$ 

# COMBINATION

shows how many arrangements of a few things may be made out of a greater number. Rule: Set down that figure which indicates the greater number, and after it a series of figures diminishing by 1, until as many are set down as the number of the few things to be taken in each combination. Then beginning under the last one set down said number of few things; then going backward set down a series diminishing by 1 until arriving under the first of the upper numbers. Multiply together all the upper numbers to form one product, and all the lower one.

How many combinations of 9 things can be made, taking 3 in each combination?

$$\frac{9 \times 8 \times 7}{1 \times 2 \times 3} = \frac{504}{6} = 84.$$

# ARITHMETICAL PROGRESSION.

in a series of numbers, is a progressive increase or decrease in each successive number by the addition or subtraction of the same amount at each step, as 1, 2, 3, 4, 5, etc., or 15, 12, 9, 6, etc. The numbers are called terms, and the equal increase or decrease the difference. Examples in arithmetical progression may be solved by the following formula:

gression may be solved by the following formulæ: Let a = first term, l = last term, d = common difference, n = number of

terms, s = sum of the terms:

$$\begin{split} l &= a + (n-1)d, &= -\frac{1}{2} d \pm \sqrt{2ds + \left(a - \frac{1}{2} d\right)^2}, \\ &= \frac{2s}{n} - a, &= \frac{s}{n} + \frac{(n-1)d}{2}. \\ s &= \frac{1}{2} n[2a + (n-1)d], &= \frac{l+a}{2} + \frac{l^2 - a^2}{2d}, \\ &= (l+a)\frac{n}{2}, &= \frac{1}{2} n[2l - (n-1)d]. \\ &= \frac{1}{2} d \pm \sqrt{\left(l + \frac{1}{2} d\right)^2 - 2ds}, &= \frac{2s}{n} - l. \\ d &= \frac{l-a}{n-1}, &= \frac{2(s-an)}{n(n-1)}, \\ &= \frac{l^2 - a^2}{2s - l - a}, &= \frac{2(nl-s)}{n(n-1)}, \\ n &= \frac{l-a}{d} + 1, &= \frac{2s}{l+a}, &= \frac{2l+d \pm \sqrt{(2l+d)^2 - 8ds}}{2d}. \end{split}$$

# GEOMETRICAL PROGRESSION,

in a series of numbers, is a progressive increase or decrease in each successive number by the same multiplier or divisor at each step, as 1, 2, 4, 8, 16, etc., or 243, 81, 27, 9, etc. The common multiplier is called the ratio. Let a= first term, t= last term, r= ratio or constant multiplier, n= number of terms, m= any term, as r= 15, 24, etc., s= sum of the terms

Let a = nrst term, t = last term, r = ratio or constant multiplier, n = number of terms, m = any term, as 1st, 2d, etc., s = sum of the terms:  $l = ar^{n-1}, \qquad = \frac{a + (r-1)s}{r}, \qquad = \frac{(r-1)sr^{n-1}}{r^n-1},$ 

$$\log l = \log a + (n-1) \log r, \qquad l(s-l)^{n-1} - a(s-a)^{n-1} = 0.$$

 $m = ar^{m-1}. \qquad \log m = \log a + (m-1)\log r.$ 

$$s = \frac{a(r^n-1)}{r-1}, \qquad = \frac{rl-a}{r-1}, \qquad = \frac{r-1}{\sqrt[n]{l}-1}, \qquad = \frac{r-1}{\sqrt[n]{l}-1}, \qquad = \frac{lr^n-l}{r^n-r^{n-1}}.$$

$$\begin{aligned} a &= \frac{l}{r^n - 1}, & = \frac{(r - 1)s}{r^n - 1} \\ r &= \sqrt[n - 1]{\frac{7}{a}}, & = \frac{s - a}{s - 1}, & \log a = \log l - (n - 1)\log r, \\ \log r &= \frac{\log l - \log a}{n - 1}, & \log r &= \frac{\log l - \log a}{n - 1}, \\ n &= \frac{\log l - \log a}{\log r} + 1, & = \frac{\log l - \log a}{\log (s - a) - \log (s - b)} + 1, & = \frac{\log l - \log (lr - (r - 1)s)}{\log r} + 1. \end{aligned}$$

# Population of the United States.

(A problem in geometrical progression.)

Year.	Population.	Increase in 10 Years, per cent.	Annual Increase, per cent.
1860	31,443,321		por come.
1870	39,818,449*	26.63	2.39
1880	50,155,783	25,96	2.33
1890	62,622,250	24.86	2.25
1895	Est. 69,733,000		Est. 2.174
1900	" 77,652,000	Est. 24.0	" 2.174

# Estimated Population in Each Year from 1860 to 1899.

(Based on the above rates of increase, in even thousands.)

		1					
1860	31,443	1870	39,818	1880	50,156	1890	62,622
1861	32,195	1871	40,748	1881	51,281	1891	63,984
1862	32,964	1872	41,699	1882	52,433	1892	65,375
1863	33,752	1873	42,673	1883	53,610	1893	66,797
1864	34,558	1874	43,670	1884	54,813	1894	68,249
1865	35,384	1875	44,690	1885	56,043	1895	69,733
1866	36,229	1876	45,373	1886	57,301	1896	71,249
1867	37.095	1877	46,800	1887	58,588	1897	72,799
1868	37,981	1878	47,893	1888	59,903	1898	74,382
1869	38,889	1879	49,011	1889	61,247	1899	75,999

The above table has been calculated by logarithms, as follows:

$$\log r = \log l - \log a + (n-1), \qquad \log m = \log a + (n-1) \log r$$

$$\text{Pop. } 1870 \dots 39.818449 \log = 7.6000841 \qquad = \log l$$

$$\text{"} 1860 \dots 31.443321 \log = 7.4975288 \qquad = \log a$$

$$a = 11, n - 1 = 10, \text{ diff.} + 10 = 0.0125533 \qquad = \log r,$$

$$\text{add log for } 1860 \qquad - 7.4975288 \qquad = \log a$$

$$\log for \\ 1861 = - 7.50778433 \quad \text{No.} = 32.195 \dots$$

$$\log for \\ 1862 = - 7.5078433 \quad \text{No.} = 32.195 \dots$$

Compound interest is a form of geometrical progression; the ratio being 1 plus the percentage.

<sup>\*</sup> Corrected by addition of 1,260,078, estimated error of the census of 1870, Census Bulletin No. 16, Dec. 12, 1890,

### INTEREST AND DISCOUNT.

Interest is money paid for the use of money for a given time; the fac tors are:

p, the sum loaned, or the principal:

t, the time in years; r, the rate of interest;

i, the amount of interest for the given rate and time: a = p + i = the amount of the principal with interest

at the end of the time.

Formulæ:

$$i$$
 = interest = principal × time × rate per cent =  $i = \frac{ptr}{100}$ ;  $a$  = amount = principal + interest =  $p + \frac{ptr}{100}$ ;

$$r = {\rm rate} = \frac{100i}{pt};$$

$$p = \text{principal} = \frac{100i}{tr} = a - \frac{ptr}{100};$$

$$t = \text{time} = \frac{100i}{pr}$$
.

If the rate is expressed decimally as a per cent,-thus, 6 per cent = .06,the formulæ become

$$i=prt; \ a=p(1+rt); \ r=\frac{i}{pt}; \ t=\frac{i}{pr}; \ p=\frac{i}{tr}=\frac{a}{1+rt}.$$

Rules for finding Interest.—Multiply the principal by the rate per annum divided by 100, and by the time in years and fractions of a year. If the time is given in days, interest =  $\frac{\text{principal} \times \text{rate per annum}}{365 \times 100}$ In happy interest.

In banks interest is sometimes calculated on the basis of 360 days to a

year, or 12 months of 30 days each. Short rules for interest at 6 per cent, when 360 days are taken as 1 year:

Multiply the principal by number of days and divide by 6000, Multiply the principal by number of months and divide by 200.

The interest of 1 dollar for one month is 1/2 cent.

# Interest of 100 Dollars for Different Times and Rates.

Time.	2%	3%	4%	5%	6%	8%	10%
1 year	\$2.00	\$3.00	\$4.00	\$5.00	\$6.00	\$8.00	\$10.00
1 month	.16%	.25	.333	.413	.50	.66%	.831
$1 \text{ day} = \frac{1}{360} \text{ year}$	.00555	.00831	.01111	.01388	.01662	.02222	.02777
$1 \text{ day} = \frac{1}{365} \text{ year}$	.005479	.008219	.010959	.013699	.016438	.0219178	.0273973

Discount is interest deducted for payment of money before it is due. True discount is the difference between the amount of a debt payable at a future date without interest and its present worth. The present worth is that sum which put at interest at the legal rate will amount to the debt when it is due.

To find the present worth of an amount due at future date, divide the amount by the amount of \$1 placed at interest for the given time. The dis-

count equals the amount minus the present worth.

What discount should be allowed on \$103 paid six months before it is due, interest being 6 per cent per annum?

leing 6 per cent per annum?
$$\frac{103}{1+1 \times .06 \times \frac{1}{2}} = $100 \text{ present worth, discount} = 3.00.$$

Bank discount is the amount deducted by a bank as interest on money loaned on promissory notes. It is interest calculated not on the actual sum loaned, but on the gross amount of the note, from which the discount is deducted in advance. It is also calculated on the basis of 360 days in the year, and for 3 (in some banks 4) days more than the time specified in the note. These are called days of grace, and the note is not payable till the last of these days.

What discount will be deducted by a bank in discounting a note for \$103 payable 6 months hence? Six months = 182 days, add 3 days grace = 185 days;  $\frac{103 \times 155}{6000} = $3.176$ .

Compound Interest.—In compound interest the interest is added to the principal at the end of each year, (or shorter period if agreed upon).

the principal at the end of each year, (or shorter period if agreed upon). Let p = the principal, r = the rate expressed decimally, n = no of years, and a the amount:

$$a = \text{amount} = p (1 + r)^n; r = \text{rate} = \sqrt[n]{\frac{a}{p}} - 1,$$

$$p = \text{principal}, = \frac{a}{(1+r)^n}$$
, no of years  $= n$ ,  $= \frac{\log a - \log p}{\log (1+r)}$ .

# Compound Interest Table.

(Value of one dollar at compound interest, compounded yearly, at 3, 4, 5, and 6 per cent, from 1 to 50 years.)

Years.	3%	4%	5%	6%	Years.	3%	4%	5%	6%
1	1.03	1.04	1.05	1.06	16	1.6047	1.8730	2.1829	2,5403
9	1.0609	1.0816	1.1025	1.1236	17	1.6528	1.9479	2.2920	2.6928
2 3	1.0927	1.1249	1.1576	1.1910	18	1.7024	2.0258	2.4066	2.8543
4	1.1255	1.1699	1.2155	1.2625	19	1.7535	2,1068	2 5269	3.0256
5	1.1593	1.2166	1.2763	1.3382	20	1.8061	2,1911	2,6533	3.2071
	1.1000	1.0100	1.2100	1.0000	~0	1.0001	~	2.0000	0.2011
6	1.1941	1.2653	1.3401	1.4185	21	1.8603	2,2787	2.7859	3,3995
7	1.2299	1.3159	1.4071	1.5036	22	1.9161	2.3699	2.9252	3.6035
6 7 8 9	1.2668	1.3686	1.4774	1.5938	23	1.9736	2.4647	3.0715	3.8197
9	1.3048	1.4233	1.5513	1.6895	24	2.0328	2,5633	3,2251	4 0487
10	1.3439	1.4802	1.6289	1.7908	25	2.0937	2.6658	3.3864	4.2919
11	1.3842	1.5394	1.7103	1.8983	30	2,4272	3,2434	4.3219	5 7435
12	1.4258	1.6010	1.7958	2.0122	35	2.8138	3.9460	5,5166	7.6861
13	1.4685	1.6651	1.8856	2.1329	40	3,2620	4.8009	7 0100	10.2858
14	1.5126	1.7317	1.9799	2,2609	45	3.7815	5.8410	8.9850	13.7646
15	1.5580	1.8009	2.0789	2.3965	50	4.3838	7.1064	11.6792	18.4190
							1		

At compound interest at 3 per cent money will double itself in 23½ years, at 4 per cent in 17% years, at 5 per cent in 14.2 years, and at 6 per cent in 11.9 years.

### EQUATION OF PAYMENTS.

By equation of payments we find the equivalent or average time in which one payment should be made to cancel a number of obligations due at different dates; also the number of days upon which to calculate interest or discount upon a gross sum which is composed of several smaller sums payable at different dates.

Rule.—Multiply each item by the time of its maturity in days from a fixed date, taken as a standard, and divide the sum of the products by the sum of the items: the result is the average time in days from the standard date.

A owes B \$100 due in 30 days, \$200 due in 60 days, and \$300 due in 90 days. In how many days may the whole be paid in one sum of \$600?

$$100 \times 30 + 200 \times 60 + 300 \times 90 = 42,000$$
;  $42,000 \div 600 = 70$  days, ans.

A owes B \$100, \$200, and \$300, which amounts are overdue respectively 30, 60, and 90 days. If he now pays the whole amount, \$600, how many days interest should he pay on that sum ? Ans. 70 days,

### PARTIAL PAYMENTS.

To compute interest on notes and bonds when partial payments have been made:

United States Rule. - Find the amount of the principal to the time of the first payment, and, subtracting the payment from it, find the amount of the remainder as a new principal to the time of the next payment,

If the payment is less than the interest, find the amount of the principal to the time when the sum of the payments equals or exceeds the interest due, and subtract the sum of the payments from this amount.

Proceed in this manner till the time of settlement.

Note.—The principles upon which the preceding rule is founded are:
1st. That payments must be applied first to discharge accrued interest, and then the remainder, if any, toward the discharge of the principal.

2d. That only unpaid principal can draw interest.

Mercantile Method.—When partial payments are made on short notes or interest accounts, business men commonly employ the following Find the amount of the whole debt to the time of settlement; also find

the amount of each payment from the time it was made to the time of settlement. Subtract the amount of payments from the amount of the debt; the remainder will be the balance due.

### ANNUITTIES.

An **Annuity** is a fixed sum of money paid yearly, or at other equal times agreed upon. The values of annuities are calculated by the principles of compound interest.

1. Let i denote interest on \$1 for a year, then at the end of a year the

amount will be 1+i. At the end of n years it will be  $(1+i)^n$ .

2. The sum which in n years will amount to 1 is  $\frac{1}{(1+i)^n}$  or  $(1+i)^{-n}$ , or the present value of 1 due in n years.

3. The amount of an annuity of 1 in any number of years n is  $\frac{(1+i)^n-1}{i}$ .

4. The present value of an annuity of 1 for any number of years n is  $1 - (1+i)^{-n}$ 

5. The annuity which 1 will purchase for any number of years n is  $1 - (1+i)^{-n}$ 

6. The annuity which would amount to 1 in n years is  $\frac{i}{(1+i)^n-1}$ .

# Amounts, Present Values, etc., at 5% Interest.

Years	(1)_	(2)	(3)	(4)	(5)	(6)
	$(1+i)^n$	$(1+i)^{-n}$	$\frac{(1+i)^n-1}{}$	$1-(1+i)^{-n}$		i
			. 1	i	$1-(1+i)^{-n}$	$(1+i)^n - 1$
1	1.05	.952381	1.	.952381	1.05	1.
2	1.1025	.907029	2.05	1.859410	.537805	.487805
3 4	1.157625	.863838 .822702	3.1525 4.310125	2.723248 3.545951	.367209 .282012	.317209
5	1.276282	.783526	5.525631	4.329477	.230975	.180975
6	1.340096	.746215	6.801913	5.075692	.197017	.147018
7	1.407100	.710681	8.142008	5.786373	.172820	.122820
8	1.477455	.676839	9.549109	6.463213	.154722	.104722
9	1.551328	.644609 .613913	11.026564 12.577893	7.107822 7.721735	.140690	.090690
10	1.046593	.010910	12.011000	1.121199	.1~5000	.018303

Table I.-Annuity Required to Redeem \$1000 in from 1 to 50 Years.

	9	485.43 314.10 228 60 177.39 143.36	119.13 101.03 87.02 75.87 66.79	59.28 47.58 42.96 38.95	35.44 32.36 29.62 27.18 18.23	12.65 8.97 6.46 4.70 3.44
	578	486.62 315.63 230.29 179.13	130.96 102.86 88.83 77.67 68.57	61.03 54.68 49.28 44.62 40.58	37.04 33.92 31.15 28.68 19.55	13.80 9.97 7.32 5.43 4.06
	73	487.80 317.21 232.01 180.98 147.02	122.82 104.72 90.69 79.50 70.39	62.83 56.45 51.03 46.34 42.27	38.70 35.54 32.75 30.24 20.95	15.05 11.07 8.28 6.36 4.78
	47%	489.00 818.77 233.74 182.79 148.88	124.67 106.60 92.57 81.38 72.25	64.67 58.27 52.89 48.11 44 01	40.42 87.24 84.40 81.87 22.44	16.39 12.27 7.20 5.60
	4	490.20 320.36 235.50 184.63 150.79	126.61 108.53 94.49 83.29 74.15	66.55 60.14 54.67 49.94 45.83	42.30 38.99 36.14 33.58	17.83 10.52 8.96 6.55
st, per cent.	334	490.81 821.13 236.38 185.56 151.73	127.59 109.50 95.46 84.26 75.12	67.51 61.10 55.62 50.88 46.70	43.19 89.90 87.04 84.47 24.84	18.60 14.29 11.17 8.85 7.09
1 6	31/2	491.42 321.94 237.26 186.49 152.67	128.57 110.48 96.44 85.24 76.09	68.48 62.06 56.57 51.82 47.68	44.04 40.82 87.94 85.86	19.37 15.00 11.83 7.63
Rate of Inter	31/4	492.05 822.75 238.14 187.42 153.64	129.54 111.47 97.44 86.34 77.08	69.47 63.05 57.55 52.79 48.64	44.99 41.76 38.87 36.29 26.55	30.19 15.77 10.12 8.25
	60	492.69 823.56 239.02 188.35 154.61	130.51 112.46 98.44 87.34 78.07	70.46 64.03 58.53 53.77	45.95 42.71 39.81 37.33 27.43	21.02 16.54 13.26 10.78 8.87
	53%	498.28 824.35 239.98 189.30 155.58	131.50 113.46 99.45 88.34 79.09	71.47 65.04 59.53 54.77	46.94 43.69 40.78 38.18 28.35	21.90 17.37 14.05 11.52 9.56
	21/2	493.78 325.14 240.84 190.24 156.56	132.49 114.47 100.46 89.35 80.11	72.49 66.05 60.54 55.77 51.60	47.93 44.67 41.76 39.14 29.27	22.78 18.20 14.84 12.27 10.26
	21/4	494.50 325.94 241.74 191.18	133.51 115.48 101.48 90.39 81.14	73.52 67.08 61.56 56.79 52.62	48.91 45.67 42.76 40.14 30.24	23.70 19.09 15.68 13.07 11.02
	21	495.05 826.72 242.63 192.16 158.53	134.52 116.51 102.52 91.83 82.18	74.56 68.12 62.60 57.83 58.65	49.97 46.70 43.78 41.15 31.33	24.65 20.00 16.55 13.91 11.82
Years to run.		0,0041020	7-8-8-9-110 110	12 14 15 15 16 16 17 18 18 18 18 18 18 18 18 18 18 18 18 18	17 18 20 25 25	88 84 4 00 0 25 4 4 00

### TABLES FOR CALCULATING SINKING-FUNDS AND PRESENT VALUES.

Engineers and others connected with municipal work and industrial enterprises often find it necessary to calculate payments to sinking-funds which will provide a sum of money sufficient to pay off a bond issue or other debt will provide a sum of money summers to pay on a bond issue of certain annual charges. The accompanying tables were computed by Mr. John W. Hill, of Cincinnati, Engly 9 News, Jan. 25, 1894.
Table I (opposite page) shows the annual sum at various rates of interest required to (note \$100 in from 2 to 5) years, and Table II shows the present

value at various rates of interest of an annual charge of \$1000 for from 5 to

50 years, at five-year intervals and for 100 years,

Table II.—Capitalization of Annuity of \$1000 for from 5 to 100 Years.

Years.	Rate of Interest, per cent.												
	21/2	51/2	6										
5 10		4,579.60	4.514.92 8,316.45	4,451.68 8 110.74	4,389.91	4,329.45	4,268.09	4,212.40					
15 20	12,381.41 15,589.215	11,937.80 14,877.27	11,517.23 14,212.12	11,118.06 13,590.21	10,739.42 13,007.88	10,379.53 12,462.13	10,037.48 11,950.26	9,712.30 11,469.96					
	18,424.67		16,481.28 18,391.85		, ,	1							
40	23,145.31 25,103.53 26,833.15	23,114.36	20,000.43 21,354.83 22,495.23	19,792.65	18,401.49	17,159.01	16,044.92	15,046.31					
50	28,362.48 36,614.21	25,729.58	23,455.21 27,655.36	21,482.08	19,761.93	18,255.86	16,931.97	15,761.87					

# WEIGHTS AND MEASURES.

# Long Measure.-Measures of Length.

12 inches = 1 foot. 3 feet = 1 yard. 51 vards, or 161 feet = 1 rod, pole, or perch. 40 poles, or 220 yards = 1 furlong. 8 furlongs, or 1760 yards, or 5280 feet = 1 mile. 3 miles = league.

Additional measures of length in occasional use: 1000 mils = 1 inch; 4 inches = 1 hand; 9 inches = 1 span; 21 feet = 1 military pace; 2 yards = 1 fathom.

Old Land Measure. - 7.92 inches = 1 link; 100 links, or 66 feet, or 4 poles = 1 chain; 10 chains = 1 furlong; 8 furlongs = 1 mile; 10 square chains = 1 acre.

### Nautical Measure.

6080.26 feet, or 1.15156 stat-= 1 nautical mile, or knot.\* ute miles = 1 league. 3 nautical miles 60 nautical miles, or 69.168 = 1 degree (at the equator). statute miles = circumference of the earth at the equator. 360 degrees

<sup>\*</sup>The British Admiralty takes the round figure of 6080 ft. which is the length of the "measured mile" used in trials of vessels. The value varies from 6080.26 to 6088.4t. according to different measures of the earth's diameter. There is a difference of opinion among writers as to the use of the word "knot" to mean length or a distance-some holding that it should be

### Square Measure.-Measures of Surface.

144 square inches, or 183.35 circular = 1 square foot. inches 9 square feet = 1 square yard. 301 square vards, or 2721 square feet = 1 square rod, pole, or perch. 40 square poles = 1 rood. 4 roods, or 10 sq. chains, or 160 sq. poles, or 4840 sq. yards, or 43560 = 1 acre. sq. feet. 640 acres = 1 square mile.

An acre equals a square whose side is 208.71 feet.

A circular inch is the area of a circle 1 inch in diameter = 0.7854 square inch.

1 square inch = 1,2732 circular inches.

A circular mil is the area of a circle 1 mil, or .001 inch in diameter. 10002 or 1,000,000 circular mils = 1 circular inch.

1 square inch = 1,273,239 circular mils. The mil, and circular mil are used in electrical calculations involving the diameter and area of wires.

# Solid or Cubic Measure.-Measures of Volume.

1728 cubic inches = 1 cubic foot.

27 cubic feet = 1 cubic yard. 1 cord of wood = a pile,  $4 \times 4 \times 8$  feet = 128 cubic feet. 1 perch of masonry =  $16\frac{1}{2} \times 1\frac{1}{2} \times 1$  foot =  $24\frac{3}{4}$  cubic feet.

# Liquid Measure.

4 gills = 1 pint.

2 pints = 1 quart. = 1 gallon { U. S. 231 cubic inches. Eng. 277.274 cubic inches. 4 quarts

311 gallons = 1 barrel. 42 gallons = 1 tierce. 2 barrels, or 63 gallons = 1 hogshead.

2 darlors, or 2 tierces = 1 puncheon. 2 hogsheads, or 126 gallons = 1 pipe or butt. 2 pipes, or 3 puncheons = 1 tun.

The U. S. gallon contains 231 cubic inches; 7.4805 gallons = 1 cubic foot. A cylinder 7 in, diam. and 6 in. high contains 1 gallon, very nearly, or 230.9 cubic inches. The British Imperial gallon contains 27.274 cubic inches = 1.20032 U. S. gallon.

The Miner's Inch .- (Western U. S. for measuring flow of a stream

of water).

The term Miner's Inch is more or less indefinite, for the reason that Californic water companies do not all use the same head above the centre of the aperture, and the inch varies from 1.36 to 1.73 cubic feet per minute each; but the most common measurement is through an aperture 2 inches high and whatever length is required, and through a plank 11 inches thick. The lower edge of the aperture should be 2 inches above the bottom of the measuring-box, and the plank 5 inches high above the aperture, thus making a 6-inch head above the centre of the stream. Each square inch of this opening represents a miner's inch, which is equal to a flow of 11 cubic feet per minute.

# Apothecaries' Fluid Measure.

= 1 fluid drachm. 60 minims 8 drachms, or 4371 grains, or 1.732 cubic inches = 1 fluid ounce.

# Dry Measure, U. S.

2 pints = 1 quart. 8 quarts = 1 peck. 4 pecks = 1 bushel.

used only to denote a rate of speed. The length between knots on the log line is  $\frac{1}{120}$  of a nautical mile or 50.7 ft. when a half-minute glass is used; so that a speed of 10 knots is equal to 10 nautical miles per hour.

The standard U.S. bushel is the Winchester bushel, which is in evlinder form, 181 inches diameter and 8 inches deep, and contains 2150.42 cubic inches.

A struck bushel contains 2150 42 cubic inches = 1.2445 cu, ft.; 1 cubic foot = 0.80356 struck bushel. A heaped bushel is a cylinder 181 inches diameter and 8 inches deep, with a heaped cone not less than 6 inches high. It is equal to 14 struck bushels.

The British Imperial bushel is based on the Imperial gallon, and contains 8 such gallons, or 2218.192 cubic inches = 1.8837 cubic feet. The English quarter = 8 Imperial bushels.

Capacity of a cylinder in U. S. gallons = square of diameter, in inches X

height in inches X.0034. (Accurate within 1 part in 100,000.)

Capacity of a cylinder in U. S. bushels = square of diameter in inches X height in inches X.0003653.

# Shipping Measure.

Register Ton.—For register tonnage or for measurement of the entire internal capacity of a vessel:

100 cubic feet = 1 register ton.

This number is arbitrarily assumed to facilitate computation, Shipping Ton .- For the measurement of cargo:

> 40 cubic feet =  $\begin{cases} 1 \text{ U. S. shipping ton.} \\ 31.16 \text{ Imp. bushels.} \end{cases}$ 32.143 U. S.  $42 \text{ cubic feet} = \begin{cases} 1 \text{ British shipping ton.} \\ 32.719 \text{ Imp. bushels.} \\ 33.75 \text{ U. S.} \end{cases}$

Carpenter's Rule.—Weight a vessel will carry = length of keel  $\times$  breadth at main beam  $\times$  depth of hold in feet +95 (the cubic feet allowed for a ton). The result will be the tonnage. For a double-decker instead of the depth of the hold take half the breadth of the beam.

# Measures of Weight,-Avoirdupois, or Commercial Weight.

16 drachms, or 437.5 grains = 1 ounce, oz. 16 ounces, or 7000 grains = 1 pound, lb. 28 pounds = 1 quarter, qr.

= 1 hundredweight, cwt. = 112 lbs. 4 quarters 20 hundred weight = 1 ton of 2240 pounds, or long ton.

2000 pounds 2204.6 pounds = 1 net, or short ton. = 1 metric ton. 1 stone = 14 pounds; 1 quintal = 100 pounds.

# Troy Weight.

24 grains = 1 pennyweight, dwt. 20 pennyweights = 1 ounce, oz. = 480 grains. 12 ounces = 1 pound, lb. = 5760 grains.

Troy weight is used for weighing gold and silver. The grain is the same in Avoirdupois, Troy, and Apothecaries' weights. A carat, used in weighing diamonds = 3.168 grains = .205 gramme.

# Apothecaries' Weight.

20 grains = 1 scruple, 9 3 scruples = 1 drachm, 3 = 60 grains. 12 ounces = 1 pound, lb. = 5760 grains.

To determine whether a balance has unequal arms.-After weighing an article and obtaining equilibrium, transpose the article and the weights. If the balance is true, it will remain in equilibrium; if

untrue, the pan suspended from the longer arm will descend. To weigh correctly on an incorrect balance.—First, by substitution. Put the article to be weighed in one pan of the balance and counterpoise it by any convenient heavy articles placed on the other pan. Remove the article to be weighed and substitute for it standard weights until equipoise is again established. The amount of these weights is the

weight of the article.

Second, by transposition. Determine the apparent weight of the article as usual, then its apparent weight after transposing the article and the weights, If the difference is small, add half the difference to the smaller of the apparent weights to obtain the true weight. If the difference is 2 per cent the error of this method is 1 part in 10,000. For larger differences, or to obtain a perfectly accurate result, multiply the two apparent weights together and extract the square root of the product.

### Circular Measure.

60 seconds, " = 1 minute, '. 60 minutes, ' = 1 degree, ° 90 degrees = 1 quadrant. 360 = circumference.

# Time.

60 seconds = 1 minute. 60 minutes = 1 hour.24 hours  $= 1 \, day$ 

7 days = 1 week.

365 days, 5 hours, 48 minutes, 48 seconds = 1 year.

By the Gregorian Calendar every year whose number is divisible by 4 is a leap year, and contains 366 days, the other years containing 365 days, except that the centesimal years are leap years only when the number of the year is divisible by 400.

The comparative values of mean solar and sidereal time are shown by the

following relations according to Bessel:

365,24222 mean solar days = 366,24222 sidereal days, whence 1 mean solar day = 1.00273791 sidereal days: 1 sidereal day = 0 99726957 mean solar day: 24 hours mean solar time = 24h 3m 56s,555 sidereal time; 24 hours sidereal time = 22h 56m 4s.091 mean solar time.

whence 1 mean solar day is 3m 55s.91 longer than a sidereal day, reckoned in mean solar time.

# BOARD AND TIMBER MEASURE.

### Board Measure.

In board measure boards are assumed to be one inch in thickness. obtain the number of feet board measure (B. M.) of a board or stick of square timber, multiply together the length in feet, the breadth in feet, and the thickness in inches.

To compute the measure or surface in square feet,-When all dimensions are in feet, multiply the length by the breadth, and the pro-

duct will give the surface required.

When either of the dimensions are in inches, multiply as above and divide the product by 12.

When all dimensions are in inches, multiply as before and divide product

by 144.

### Timber Measure.

To compute the volume of round timber,—When all dimensions are in feet, multiply the length by one quarter of the product of the mean girth and diameter, and the product will give the measurement in cubic feet. When length is given in feet and girth and diameter in inches, divide the product by 144; when all the dimensions are in inches, divide by

To compute the volume of square timber,—When all dimensions are in feet, multiply together the length, breadth, and depth; the product will be the volume in cubic feet. When one dimension is given in inches, divide by 12; when two dimensions are in inches, divide by 144; when

all three dimensions are in inches, divide by 1728.

# Contents in Feet of Joists, Scantling, and Timber.

Length in Feet.

Size.	12	14	16	18	20	22	24	26	28	30	
	Feet Board Measure.										
$\begin{array}{c} 2 \times 4 \\ 2 \times 6 \\ 2 \times 8 \\ 2 \times 10 \\ 2 \times 12 \end{array}$	8	9	11	12	13	15	16	17	19	20	
	12	14	16	18	20	22	24	26	28	30	
	16	19	21	24	27	29	32	35	37	40	
	20	23	27	30	33	37	40	43	47	50	
	24	28	32	36	40	44	48	52	56	60	
$2 \times 14$ $3 \times 8$ $3 \times 10$ $3 \times 12$ $3 \times 14$	28	33	37	42	47	51	56	61	65	70	
	24	28	32	36	40	44	48	52	56	60	
	30	35	40	45	50	55	60	65	70	75	
	36	42	48	54	60	66	72	78	84	90	
	42	49	56	68	70	77	84	91	98	105	
$\begin{array}{c} 4 \times 4 \\ 4 \times 6 \\ 4 \times 8 \\ 4 \times 10 \\ 4 \times 12 \end{array}$	16	19	21	24	27	29	32	35	37	40	
	24	23	32	36	40	44	48	52	56	60	
	32	37	43	48	53	59	64	69	75	80	
	40	47	53	60	67	73	.80	87	93	100	
	48	56	64	72	80	88	96	104	112	120	
$\begin{array}{c} 4 \times 14 \\ 6 \times 6 \\ 6 \times 8 \\ 6 \times 10 \\ 6 \times 12 \end{array}$	56	65	75	84	93	103	112	121	131	140	
	36	42	48	54	60	66	72	78	84	90	
	48	56	64	72	80	88	96	104	112	120	
	60	70	80	90	100	110	120	130	140	150	
	72	84	96	108	120	132	144	156	168	180	
$\begin{array}{c} 6 \times 14 \\ 8 \times 8 \\ 8 \times 10 \\ 8 \times 12 \\ 8 \times 14 \end{array}$	84	98	112	126	140	154	168	182	196	210	
	64	75	85	96	107	117	128	139	149	160	
	80	93	107	120	133	147	160	173	187	200	
	96	112	128	144	160	176	192	208	224	240	
	112	131	149	168	187	205	224	243	261	280	
$10 \times 10$	100	117	133	150	167	183	200	217	233	250	
$10 \times 12$	120	140	160	180	200	220	240	260	280	300	
$10 \times 14$	140	163	187	210	233	257	280	303	327	350	
$12 \times 12$	144	168	192	216	240	264	288	312	336	360	
$12 \times 14$	168	196	224	252	280	308	336	364	392	420	
14 × 14	196	229	261	294	327	359	392	425	457	490	

# FRENCH OR METRIC MEASURES.

The metric unit of length is the metre = 39.37 inches. The metric unit of weight is the gram = 15.432 grains. The following prefixes are used for subdivisions and multiples; Milli =  $_{10^{10}0}$ , Centi =  $_{10^{10}}$ , Deci =  $_{10}^{10}$ , Deca = 10, Hecto = 100, Kilo = 1000, Myria = 10,000.

# FRENCH AND BRITISH (AND AMERICAN) EQUIVALENT MEASURES.

### Measures of Length.

FRENCH. BRITISH and U. S.

1 metre = 39.37 inches, or 3.28083 feet, or 1.09361 yards. .3048 metre = 1 foot.

1 centimetre = .3937 inch.

2.54 centimetres = 1 inch. 1 milimetre = .03937 inch, or 1/25 inch, nearly.

2.54 millimetres = 1 inch. 1 kilometre = 1093.61 vards, or 0.62137 mile.

# Measures of Surface.

FRENCH. BRITISH. = { 10.764 square feet, 1.196 square yards. 1 square metre 836 square metre = 1 square yard. = 1 square foot. .0929 square metre

1 square centimetre = .155 square inch. 6.452 square centimetres = 1 square inch, 1 square millimetre = .00155 square inch.

645.2 square millimetres = 1 square inch. = 10 764 square feet, 1 centiare = 1 sq. metre = 1076.41

1 are = 1 sq. decametre 1 hectare = 100 ares " = 2.4711 acres. = 107641= .386109 sq. miles = 247.111 sq. kilometre = 38 6109 "

1 sq. myriametre

### Of Volume.

FRENCH. BRITISH and U. S.

 $= \begin{cases} 35.314 \text{ cubic feet,} \\ 1.308 \text{ cubic yards.} \end{cases}$ 1 cubic metre .7645 cubic metre

= 1 cubic yard. = 1 cubic foot. .02832 cubic metre

(61.023 cubic inches, 1 cubic decimetre .0353 cubic foot.

28.32 cubic decimetres = 1 cubic foot. 1 cubic centimetre = .061 cubic inch.

16.387 cubic centimetres = 1 cubic inch. 1 cubic centimetre = 1 millilitre = .061 cubic inch. 1 centilitre = .610

44 44 1 decilitre = 6.102 64 66

l litre = 1 cubic decimetre = 61.023 " = 1.05671 quarts, U. S. 1 hectolitre or decistere = 3.314 cubic feet = 2.8375 bushels, " 1 stere, kilolitre, or cubic metre = 1.308 cubic yards = 28.37 bushels, "

# Of Capacity.

FRENCH. BRITISH and U. S. (61.023 cubic inches,

.03531 cubic foot. 1 litre (= 1 cubic decimetre) = {

.2642 gallon (American), 2.202 pounds of water at 62° F. 28.317 litres = 1 cubic foot.

4.543 litres = 1 gallon (British). 3 785 litres = 1 gallon (American).

# Of Weight.

BRITISH and U. S. FRENCH.

1 gramme = 15.432 grains. .0648 gramme = 1 grain. = 1 ounce avoirdupois.

28.35 gramme 1 kilogramme = 2.2046 pounds. .4536 kilogramme = 1 pound.

1 tonne or metric ton = \( \begin{align\*} .9842 \text{ ton of 2240 pounds,} \\ 19.68 \text{ cwts.,} \end{align\*} 1000 kilogrammes

= \ 2204.6 pounds. = 1 ton of 2240 pounds. 1.016 metric tons 1016 kilogrammes

Mr. O. H. Titmann, in Bulletin No. 9 of the U. S. Coast and Geodetic Survey, discusses the work of various authorities who have compared the yard and the metre, and by referring all the observations to a common standard has succeeded in reconciling the discrepancies within very narrow limit. The following are his results for the number of inches in a metre according to the comparisons of the authorities named:

Hassler. 39.36994 inches. Kater. 39.36990 " 1818. 1835. Baily...... 39.36973 1866. Clarke. 39.36970 1885. 

# METRIC CONVERSION TABLES.

The following tables, with the subjoined memoranda, were published in 1890 by the United States Coast and Geodetic Survey, office of standard weights and measures, T. C. Mendenhall, Superintendent.

# Tables for Converting U. S. Weights and Measures— Customary to Metric.

### LINEAR.

			1	
	Inches to Millimetres.	Feet to Metres.	Yards to Metres.	Miles to Kilo- metres.
1 = 2 = 3 = 4 = 5 =	25.4000	0.304801	0.914402	1,60935
	50.8001	0.609601	1.828804	3,21869
	76.2001	0.914402	2.743205	4,82804
	101.6002	1.219202	3.657607	6,43739
	127.0002	1.524003	4.572009	8,04674
6 =	152.4003	1.828804	5.486411	9.65608
7 =	177.8003	2.133604	6.400813	11.26543
8 =	203.2004	2.438405	7.315215	12.87478
9 =	228.6004	2.743205	8.229616	14.48412

# SQUARE.

	Square Inches to Square Centi- metres.	Square Feet to Square Deci- metres.	Square Yards to Square Metres.	Acres to Hectares.
1 =	6.452	9.290	0.836	0.4047
2 =	12.903	18.581	1.672	0.8094
3 =	19.355	27.871	2.508	1.2141
4 =	25.807	37.161	3.344	1.6187
5 =	32.258	46.452	4.181	2.0234
6 =	38.710	55.742	5.017	2.4281
7 =	45.161	65.032	5.858	2.8328
8 =	51.613	74.323	6.689	3.2375
9 =	58.065	83.613	7.525	8.6422

### CUBIC.

			··	
	Cubic Inches to Cubic Centi- metres.	Cubic Feet to Cubic Metres.	Cubic Yards to Cubic Metres.	Bushels to Hectolitres.
1 = 2 = 3 = 4 = 5 =	16.387	0.02832	0.765	0.35242
	32.774	0.05663	1.529	0.70485
	49.161	0.08495	2.294	1.05727
	65.549	0.11327	3.058	1.40969
	81.936	0.14158	3.823	1.76211
6 =	98.323	0.16990	4.587	2.11454
7 =	114.710	0.19822	5.352	2.46696
8 =	131.097	0.22654	6.116	2.81938
9 =	147.484	0.25485	6.881	3.17181

# CAPACITY.

	Fluid Drachms to Millilitres or Cubic Centi- metres.	Fluid Ounces to Millilitres.	Quarts to Litres.	Gallons to Litres
1 =	3.70	29.57	0.94636	3.78544
2 =	7.39	59.15	1.89272	7.57088
3 =	11.09	88.72	2.83908	11.35632
4 =	14.79	118.30	3.78544	15.14176
5 =	18.48	147.87	4.73180	18.92720
6 = 7 =	22.18	177.44	5.67816	22.71264
	25.88	207.02	6.62452	26.49808
8 =	29.57	236.59	7.57088	30.28352
9 =	33.28	266.16	8.51724	34.06896

# WEIGHT.

	Grains to Milligrammes.	Avoirdupois Ounces to Grammes,	Avoirdupois Pounds to Kilo- grammes.	Troy Ounces to Grammes.
1 = 2 = 3 = 4 = 5 =	64.7989	28.3495	0.45359	31.10348
	129.5978	56.6991	0.90719	62.20696
	194.3968	85.0486	1.36078	93.31044
	259.1957	113.3981	1.81437	124.41392
	323.9946	141.7476	2.26796	155.51740
6 =	388.7985	170.0972	2.72156	186.62089
7 =	453.5924	198.4467	3.17515	217.72487
8 =	518.3914	226.7962	3.62874	248.82785
9 =	583.1903	255.1457	4.08233	279.93133

1 chain = 20.169 metres. 1 square mile = 259 hectares. 1 fathom = 1.829 metres. 1 nautical mile = 1853.27 metres. 1 foot = 0.304801 metre. 1 avoir. pound = 435.594277 gram. 15482,35639 grains = 1 kilogramme.

# Tables for Converting U. S. Weights and Measures— Metric to Customary.

# LINEAR.

	Metres to Inches.	Metres to Feet.	Metres to Yards.	Kilometres to Miles.
1 = 2 = 3 = 4 = 5 =	39.3700	3.28088	1.093611	0.62187
	78.7400	6.56167	2.187222	1.24274
	118.1100	9.84250	3.280833	1.86411
	157.4800	13.12333	4.374444	2.48548
	196.8500	16:40417	5.468056	3.10685
6 =	236.2200	19.68500	6.561667	3.72822
7 =	275.5900	22.96583	7.655278	4.34959
8 =	314.9600	26.24667	8.748889	4.97096
9 =	354,3300	29.52750	9.842500	5.59233

# SQUARE.

	Square Centi- metres to Square Inches.	Square Metres to Square Feet.	Square Metres to Square Yards.	Hectares to Acres.
1 = 2 = 3 = 4 = 5 =	0.1550	10.764	1.196	2.471
	0.3100	21.528	2.392	4.942
	0.4650	32.292	3.588	7.413
	0.6200	43.055	4.784	9.884
	0.7750	53.819	5.980	12.355
6 =	0.9300	64.583	7.176	14.826
7 =	1.0850	75.347	8.372	17.297
8 =	1.2400	86.111	9.568	19.768
9 =	1.3950	96.874	10.764	22.239

# CUBIC.

	Cubic Centimetres to Cubic Inches.	Cubic Decimetres to Cubic Inches.	Cubic Metres to Cubic Feet.	Cubic Metres to Cubic Yards.
1 =	0.0610	61.023	85.314	1.308
2 =	0.1220	122.047	70.629	2.616
3 =	0.1831	183.070	105.943	3.924
4 =	0.2441	244.093	141.258	5:232
5 =	0.3051	305.117	176.572	6.540
6 =	0.3661	366,140	211.887	7.848
7 =	0.4272	427,163	247.201	9.156
8 =	0.4882	488,187	282.516	10.464
9 =	0.5492	549,210	817.830	11.771

# CAPACITY.

	Millilitres or Cubic Centi- litres to Fluid Drachms.	Centilitres to Fluid Ounces.	Litres to Quarts.	Dekalitres to Gallons.	Hektolitres to Bushels.
1 =	0.27	0.388	1.0567	2.6417	2.8375
2 =	0.54	0.676	2.1134	5.2834	5.6750
3 =	0.81	1.014	3.1700	7.9251	8.5125
4 =	1.08	1.352	4.2267	10.5668	11.3500
5 =	1.35	1.691	5.2834	13.2085	14.1875
6 =	1.62	2.029	6.3401	15.8502	17.0250
7 =	1.89	2.368	7.3968	18.4919	19.8625
8 =	2.16	2.706	8.4534	21.1336	22.7000
9 =	2.43	8.043	9.5101	23.7753	25 5875

### WEIGHT.

	Milligrammes to Grains.	Kilogrammes to Grains.	Hectogrammes (100 grammes) to Ounces Av.	Kilogrammes to Pounds Avoirdupois.
1 = 2 = 3 = 4 = 5 =	0.01543	15432,36	3.5274	2.20462
	0.03086	30864,71	7.0548	4.40924
	0.04630	46297,07	10.5822	6.61386
	0.06173	61729,43	14.1096	8.81849
	0.07716	77161,78	17.6370	11.02311
6 =	0.09259	92594.14	21.1644	13.22773
7 =	0.10803	108026.49	24.6918	15.43235
8 =	0.12346	123458.85	28.2192	17.63697
9 =	0.13889	138891.21	31.7466	19.84159

# WEIGHT—(Continued).

	Quintals to	Milliers or Tonnes to	Grammes to Ounces,
	Pounds Av.	Pounds Av.	Troy.
1 = 2 = 3 = 4 = 5 =	220,46	2204.6	0.03215
	440,92	4409.2	0.06430
	661,38	6613.8	0.09645
	881,84	8818.4	0.12860
	1102,30	11023.0	0.16075
6 = 7 = 8 = 9 =	1322.76	13227.6	0.19290
	1543.22	15432.2	0.22505
	1763.68	17636.8	0.25721
	1984.14	19841.4	0.28936

The only authorized material standard of customary length is the Troughton scale belonging to this office, whose length at 59°.62 Fahr. conforms to the British standard. The yard in use in the United States is therefore equal to the British yard.

The only authorized material standard of customary weight is the Troy pound of the mint. It is of brass of unknown density, and therefore not suitable for a standard of mass. It was derived from the British standard Troy pound of 1758 by direct comparison. The British avoirdupois pound

Troy pound of 1758 by direct comparison. The British Avoirdupois pound was also derived from the latter, and contains 7000 grains Troy.

The grain Troy is therefore the same as the grain Avoirdupois, and the pound Avoirdupois in use in the United States is equal to the British pound

Avoirdupois.

The metric system was legalized in the United States in 1866.

By the concurrent action of the principal governments of the world an International Bureau of Weights and Measures has been established near Paris.

The International Standard Metre is derived from the Mètre des Archives, and its length is defined by the distance between two lines at 0° Centigrade, on a platinum-iridium bar deposited at the International Bureau.

The International Standard Kilogramme is a mass of platinum-iridium deposited at the same place, and its weight in vacuo is the same as that of the Kilogramme des Archives.

Copies of these international standards are deposited in the office of standard weights and measures of the U. S. Coast and Geodetic Survey.

The litre is equal to a cubic decimetre of water, and it is measured by the quantity of distilled water which, at its maximum density, will counterpoise the standard kilogramme in a vacuum; the volume of such a quantity of water being, as nearly as has been ascertained, could to a cubic decimetre.

### COMPOUND UNITS.

# Measures of Pressure and Weight.

1 lb. per square inch.	144 lbs. per square foot. 2.0355 ins. of mercury at 32° F. 2.0416 " 62° F. 2.0916 ft, of water at 62° F. 27.71 ins. " " 62° F.
1 atmosphere (14.7 lbs, per sq. in.)	{ 2116.3 lbs. per square foot. 33.947 ft. of water at 62° F. 30 ins. of mercury at 62° F. 29.922 ins. of mercury at 32° F. 760 millimetres of mercury at 32° F.
1 inch of water at 62° F.	= \ \begin{align*} .0361 lb. per square inch. \ 5.196 lbs. \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \
1 inch of water at 32° F.	$= \begin{cases} 5.2021 \text{ lbs. per square foot.} \\ .036125 \text{ lbs. per "inch.} \end{cases}$
1 foot of water at 62° F.	$= \begin{cases} .433 \text{ lb. per square inch.} \\ 62.355 \text{ lbs.} \text{ "" foot.} \\ .883 \text{ in. of mercury at } 62^{\circ} \text{ F.} \end{cases}$
1 inch of margury at 690 F	49 lb. per square inch. 70.56 lbs. "foot.

# Weight of One Cubic Foot of Pure Water.

13.98 ins. "

1 inch of mercury at 62° F.

" 62º F.

1.165 ft. of water at 62° F

At 32° F. (freezing-point)
" 39.1° F. (maximum density)
" 62° F. (standard temperature)
" 212° F. (boiling-point, under 1 atmosphere) 59.76 "
American gallon = 231 cubic ins. of water at 62° F. = 8.3356 lbs.
British " = 277.274 " " " " = 10 lbs.

# Measures of Work, Power, and Duty.

Work.—The sustained exertion of pressure through space.
Unit of work.—One foot-pound, i.e., a pressure of one pound exerted through a space of one foot.

Horse-power.—The rate of work. Unit of horse-power = 32,000 ft.— lbs. per minute, or 550 ft.—ibs. per second = 1,980,000 ft.—ibs. per hour. Heat unit = heat required to raise 1 lb. of water 1° F. (from 38° to 40°).

33000 Horse-power expressed in heat units =  $\frac{69000}{778}$  = 42.416 heat units per minute = .707 heat unit per second = 2545 heat units per hour.

1 lb. of fuel per H. P. per hour=  $\begin{cases} 1,980,000 \text{ ft.-lbs. per lb. of fuel.} \\ 2.545 \text{ heat units} \end{cases}$ 

1.000.000 ft.-lbs, per lb, of fuel = 1.98 lbs, of fuel per H. P. per hour.

**Velocity.**—Feet per second =  $\frac{5280}{2600} = \frac{22}{15} \times \text{miles per hour.}$ 

Gross tons per mile =  $\frac{1760}{2240} = \frac{11}{14}$  lbs. per yard (single rail.)

# French and British Equivalents of Weight and Press-ure per Unit of Area,

FRENCH.	British.						
1 gramme per square millimetre	~=	1.422	lbs.	per	square	inch.	
1 kilogramme per square "	=	1422.32		- 66	-64	**	
1 " centimetre	=	14.223		44	**	44	
1.0335 kilogrammes per square centimetre (1 atmosphere)	,					**	
0.70308 kilogramme per square centimetre	ė =	1 lb. per	squ	ıare	inch.		

# WIRE AND SHEET-METAL GAUGES COMPARED

WIR	E ANI	D SHI	EET-M	ETAI	GAU	GES (	COMPARI	ED.
Number of Gauge.	Birmingham Wire Gauge.	American or Brown and Sharpe Gauge.	Roebling's and Washburn & Moen's Gauge.	S. noon S. noo		British Imperial Standard Wire Gauge. (Legal Standard in Great Britain since March 1, 1884.)		Number of Gauge.
0000000 000000 00000 0000 0000 000 000	.454 .425 .38 .34	inch.  46 40964 3648 32486 28983 28763 28942 2942 2943 11819 116202 114428 11819 11789 00074 00074 005082 0408 03196 02535 0201 0179 01594 01019 01264 01019 01264 01002 00089 00063 00063 00063 00063 00063 00063	inch 49 46 48 393 48 393 263 331 263 324 244 225 207 283 207 283 207 283 207 283 207 283 207 207 207 207 207 207 207 207 207 207	inch,  45 40 40 86 88 88 88 8905 8905 8905 8905 8905 8905	inch500 .600 .464 .432 .44 .732 .834 .834 .832 .936 .932 .912 .192 .116 .104 .116 .104 .092 .08 .072 .064 .032 .032 .032 .032 .038 .0164 .0146 .0146 .01068 .01068	millim. 12.7 11.78 10.97 10.16 1.8 .8.23 17.60 1 6.49 1.5 1.8 1.8 1.8 1.8 1.8 1.8 1.8 1.8 1.8 1.8	inch5 .469 .438 .406 .875 .344 .313 .281 .266 .25 .249 .219 .188 .172 .156 .156 .077 .0625 .0563 .05 .0438 .05 .0438 .0281 .0281 .019 .019 .0194 .0188 .0172 .0196 .0101 .0094 .0086 .0078 .0078	7/0 6/00 4/00 4/00 2/00 1 2 3 4 4 5 6 6 7 8 9 9 10 11 12 13 14 11 15 11 19 12 12 22 23 14 12 25 25 25 25 25 25 25 25 25 25 25 25 25
47 48 49 50					.002 .0016 .0012 .001	.05 .04 .03 .025		48 49 50

# EDISON, OR CIRCULAR MIL GAUGE, FOR ELECTRICAL WIRES.

Gauge Num- ber,	Circular Mils.	Diam- eter in Mils.	Gauge Num- ter.	Circular Mils.	Diam- eter in Mils.	Gauge Num- ber.	Circular Mils.	Diam- eter in Mils.
3	3.000	54.78	70	70,000	264.58	190	190,000	435.89
3 5 8	5,000	70.72	75	75,000	273.87	200	200,000	447.22
8	8,000	89.45	80	80,000	282.85	220	220,000	469.05
12	12,000	109.55	85	85,000	291.55	240	240,000	489.90
15	15,000	122.48	90	90,000	300.00	260	260,000	509.91
20	20,000	141.43	95	95,000	308.23	280	280,000	529.16
25	25,000	158.12	100	100,000	316.23	300	300,000	547.73
30	30,000	173.21	110	110,000	331.67	320	320,000	565.69
35	35,000	187.09	120	120,000	346.42	340	340,000	583.10
40	40,000	200.00	130	130,000	360.56	360	360,000	600.00
		242 44	4.0		004 40	1		
45	45,000	212.14	140	140,000	374.17	1		
50	50,000	223.61	150	150,000	387.30	1		1
55	55,000	234.53	160	160.000	400.00			
60	60,000	244.95	170	170,000	412.32			
65	65,000	254.96	180	180,000	424.27			
	1		1	1	1 1	l l	i	1

# TWIST DRILL AND STEEL WIRE GAUGE.

(Morse Twist Drill and Machine Co.)

No.	Size.	No.	Size.	No.	Size.	No.	Size.
1 2 3 4 5	inch. .2280 .2210 .2130 .2090 .2055	16 17 18 19 20	inch. .1770 .1730 .1695 .1660 .1610	31 32 33 34 35	inch. .1200 .1160 .1130 .1110 .1100	46 47 48 49 50	inch. .0810 .0785 .0760 .0730 .0700
6 7 8 9 10	.2010 .1990 .1960 .1935	22 23 24 25	.1570 .1540 .1520 .1495	37 38 39 40	.1040 .1015 .0995 .0980	52 53 54 55	. 0635 . 0595 . 0550 . 0520
11 12 18 14 15	.1910 .1890 .1850 .1820 .1800	26 27 28 29 80	.1470 .1440 .1405 .1360 .1285	41 42 43 44 45	.0960 .0935 .0890 .0860 .0820	56 57 58 59 60	.0465 .0430 .0420 .0410 .0400

# STEEL MUSIC-WIRE GAUGE.

(Washburn & Moen Mfg Co.)

No.	Size.	No.	Size.	· No.	Size.	No.	Size.
12 13 14 15 16	inch. .0295 .0311 .0325 .0343 .0359	17 18 19 20	inch. .0378 .0395 .0414 .043	21 22 23 24	inch. .0461 .0481 .0506 .0547	25 26 27 28	inch. .0585 .0626 .0663 .0719

### THE EDISON OR CIRCULAR MIL WIRE GAUGE.

(For table of copper wires by this gauge, giving weights, electrical resistances, etc., see Copper Wire.)

Mr. C. J. Field (Stevens Indicator, July, 1887) thus describes the origin of

the Edison gauge:

The Edison company experienced inconvenience and loss by not having a wide enough range nor sufficient number of sizes in the existing gauges. This was felt more particularly in the central-station work in making electrical determinations for the street system. They were compelled make use of two of the existing gauges at least, thereby introducing a complication that was liable to lead to mistakes by the contractors and linemen.

In the incandescent system an even distribution throughout the entire system and a uniform pressure at the point of delivery are obtained by calculating for a given maximum percentage of loss from the potential as delivered from the dynamo. In carrying this out, on account of lack of regular sizes, it was often necessary to use larger sizes than the occasion demanded, and even to assume new sizes for large underground conductors. It was also found that nearly all manufacturers based their calculation for the conductivity of their wire on a variety of units, and that not one used the latest unit as adopted by the British Association and determined from Dr. Matthiessen's experiments; and as this was the unit employed in the manufacture of the Edison lamps, there was a further reason for constructing a new gauge. The engineering department of the Edison company, ing a new gauge. The engineering teptualism of the Law Johnson, which widest range obtainable and a large number of sizes which increase in a regular and uniform manner. The basis of the graduation is the sectional area, and the number of the wire corresponds. A wire of 100,000 circular mils area is No. 100; a wire of one half the size will be No. 50; twice the size No. 200. In the older gauges, as the number increased the size decreased. With

In the order gadges, as the number increased the size decreased. With this gauge, however, the number increases with the wire, and the number multiplied by 1000 will give the circular nils.

The weight per mil-foot, 0,0000502705 pounds, agrees with a specific gravity of 8.889, which is the latest figure given for copper. The ampere capacity which is given was deduced from experiments made in the company's laboratory, and is based on a rise of temperature of 50° F. in the wire. In 1893 Mr. Field writes, concerning gauges in use by electrical engineers:

The B. and S. gauge seems to be in general use for the smaller sizes, up to 100,000 c. m., and in some cases a little larger. From between one and two hundred thousand circular mils upwards, the Edison gauge or its equivalent is practically in use, and there is a general tendency to designate all sizes above this in circular mils, specifying a wire as 200,000, 400,000, 500,-

000, or 1,000,000 c. m.

In the electrical business there is a large use of copper wire and rod and other materials of these large sizes, and in ordering them, speaking of them, specifying, and in every other use, the general method is to simply specify the circular milage. I think it is going to be the only system in the future for the designation of wires, and the attaining of it means practically the adoption of the Edison gauge or the method and basis of this gauge as the correct one for wire sizes.

### THE U. S. STANDARD GAUGE FOR SHEET AND PLATE IRON AND STEEL, 1893.

The Committee on Coinage, Weights, and Measures of the House of Representatives in 1893, in introducing the bill establishing the new sheet and plate gauge, made a report from which we take the following:

The purpose of this bill is to establish an authoritative standard gauge for the measurement of sheet and plate iron.

There is in this country no uniform or standard gauge, and the same numbers in different gauges represent different thicknesses of sheets or plates. This has given rise to much misunderstanding and friction between employers and workmen and mistakes and fraud between dealers and con-

The practice of describing the different thicknesses of sheet and plate iron by gauge numbers has been so long established and become so universal both here and in Great Britain that it is not deemed advisable to change this mode of designation; but these descriptive gauge numbers

# U. S. STANDARD GAUGE FOR SHEET AND PLATE IRON AND STEEL, 1893.

	Number of Gauge.	Approximate Thickness in Fractions of an Inch.	Approximate Thickness in Decimal Parts of an Inch.	Approximate Thickness in Millimeters.	Weight per Square Foot in Ounces Avoirdupois.	Weight per Square Foot in Pounds Avoirdupois.	Weight per Square Foot in Kilograms.	Weight per Square Meter in Kilograms.	Weight per Square Meter in Pounds Avoirdupois.
	000000 000000 00000 0000 0000	1-2 15-32 7-16 13-32 3-8	0.5 0.46875 0.4375 0.40625 0.375	12.7 11.90625 11.1125 10.31875 9.525	320 300 280 260 240	20. 18.75 17.50 16.25	9.072 8.505 7.938 7.371 6.804	97.65 91.55 85.44 79.33 73.24	215.28 201.82 188.37 174.91 161.46
	00.	11-32	0.84875	8.78125	220	13.75	6.237	67.13	148.00
	0	5-16	0.8125	7.9875	200	12.50	5.67	61.03	134.55
	1	9-32	0.28125	7.14875	180	11.25	5.103	54.93	121.09
	2	17-64	0.265625	6.746875	170	10.625	4.819	51.88	114.37
	3	1-4	0.25	6.35	160	10.	4.536	48.82	107.64
	4	15-64	0.234375	5.953125	150	9.375	4.252	45.77	100.91
	5	7-32	0.21875	5.55625	140	8.75	3.969	42.72	94.18
	6	13-64	0.203125	5.159375	130	8.125	3.685	39.67	87.45
	7	3-16	0.1875	4.7625	120	7.5	3.402	36.62	80.72
	8	11-64	0.171875	4.365625	110	6.875	3.118	33.57	74.00
	9	5-32	0.15625	3.96875	100	6.25	2.835	30.52	67.27
	10	9-64	0.140625	3.571875	90	5.625	2.552	27.46	60.55
	11	1-8	0.125	3.175	80	5.	2.268	24.41	53.82
	12	7-64	0.109375	2.778125	70	4.375	1.984	21.36	47.09
	13	3-32	0.09375	2.38125	60	3.75	1.701	18.31	40.36
	14	5-64	0.078125	1.984375	50	3.125	1.417	15.26	33.64
	15	9-128	0.0703125	1.7859375	45	2.8125	1.276	13.73	30.27
	16	1-16	0.0625	1.5875	40	2.5	1.134	12.21	26.91
	17	9-160	0.05625	1.42875	36	2.25	1.021	10.99	24.22
	18	1-20	0.05	1.27	32	2.25	0.9072	9.765	21.53
	19	7-160	0.04375	1.11125	28	1.75	0.7938	8.544	18.84
	20	3-80	0.0375	0.9525	24	1.50	0.6804	7.324	16.15
	21	11-320	0.034375	0.873125	22	1.375	0.6237	6.713	14.80
	22	1-32	0.03125	0.793750	20	1.25	0.567	6.103	13.46
	23	9-320	0.028125	0.714375	18	1.125	0.5103	5.493	12.11
	24	1-40	0.025	0.635	16	1.	0.4536	4.882	10.76
	25	7-320	0.021875	0.555625	14	0.875	0.3969	4.272	9.42
	26	3-160	0.01875	0.47625	12	0.75	0.3402	3.662	8.07
	27	11-640	0.0171875	0.4365625	11	0.6875	0.3119	3.357	7.40
	28	1-64	0.015625	0.396875	10	0.625	0.2835	3.052	6.73
	29 30 31 32 33	9-640 1-80 7-640 13-1280 3-320	$\begin{array}{c} 0.0140625 \\ 0.0125 \\ 0.0109375 \\ 0.01015625 \\ 0.009375 \end{array}$	0.3571875 0.3175 0.2778125 0.25796875 0.238125	9 8 7 6½ 6	0.5625 0.5 0.4375 0.40625 0.375	0,2551 0,2268 0,1984 0,1843 0,1701	2.746 2.441 2.136 1.983 1.831	6.05 5.38 4.71 4.37 4.04
	34	11-1280	0.00859375	0.21828125	51/6	0.34375	0.1559	1.678	3 70
	35	5-640	0.0078125	0.1984375	5	0.3125	0.1417	1.526	3.36
	36	9-1280	0.00703125	0.17859875	41/6	0.28125	0.1276	1.373	3.03
	37	17-2560	0.006640625	0.168671875	41/4	0.265625	0.1205	1.297	2.87
	38	1-160	0.00625	0.15875	4	0.25	0.1134	1.221	2.69
-									

ought to have the same meaning and significance at all times and under all circumstances.

To accomplish this and furnish a legal guide in the collection of government duties, the United States should establish a legal standard gauge. None of the existing gauge-tables or scales exactly meet the requirements of accuracy and convenience, nor rest on a systematic basis; but the one submitted by your committee is believed to fully meet these requirements.

It is based on the fact that a cubic foot of iron weighs 480 pounds. This is the same basis on which the Imperial gauge of Great Britain rests, and also the New Birmingham and Amalgamated Association gauges.

A sheet of iron 1 foot square and 1 inch thick weighs 40 pounds, or 640 ounces, and 1 ounce in weight should be 1/640 inch thick. The scale has been arranged so that each descriptive number represents a certain number of onnees in weight, and an equal number of six hundred and fortieths of an inch in thickness, and the weights, and hence the thicknesses, have been arranged in a regular series of gradations. A micrometer for measuring the thickness of sheets and plates can be constructed to indicate six hundred. dred and fortieths of an inch as easily as one thousandths, and thus the measurement of a sheet of iron will give the thickness in six hundred and fortieths of an inch and in weight in ounces at the same time

It is probable that the adoption of this gauge will gradually lead to the abandonment of the numbers and to the use of the number of ounces in weight per square foot as the descriptive terms of the different thicknesses of sheet and plate iron. It will become as easy to order a 20-ounce sheet as a No. 22, or a 10 ounce as a No. 25; and this will cause a more general and intelligent comprehension of just what is being contracted for, and the opportunity for mistake or fraud growing out of an uncertainty of designation will be removed.

A natural consequence also will be the substitution of such weight designation for the arbitrary methods now in vogue of describing tin and terne plates as IC, IX, IXX, DC, DX, etc.

The law establishing the new gauge enacts as follows:

That for the purpose of securing uniformity, the following is established as the only standard gauge for sheet and plate iron and steel in the United States of America, namely:

And on and after July 1, 1893, the same and no other shall be used in determining duties and taxes levied by the United States of America on

sheet and plate iron and steel. Sec. 2. That the Secretary of the Treasury is authorized and required to prepare suitable standards in accordance herewith.

SEC. 3. That in the practical use and application of the standard gauge hereby established a variation of 21/2 per cent either way may be allowed.

# ALGEBRA.

**Addition.**—Add a and b. Ans. a+b. Add a, b, and -c. Ans. a+b-c. Add 2a and -3a. Ans. -a. Add 2ab, -3ab, -c, -3c. Ans. -ab-4c. **Subtraction.**—Subtract a from b. Ans. b-a. Subtract a from -b. Ans. -b+a.

Subtract b+c from a. Ans. a-b-c. Subtract  $3a^2b-9c$  from  $4a^2b+c$ . Ans.  $a^2b + 10c$ . Rule: Change the signs of the subtrahend and proceed as in addition.

**Multiplication.**—Multiply a by b. Ans. ab. Multiply ab by a+b.

Ans.  $a^2b + ab^2$ . Multiply a + b by a + b. Ans.  $(a + b)(a + b) = a^2 + 2ab + b^2$ . Multiply -a by -b. Ans. ab. Multiply -a by b. Ans. -ab. signs give plus, unlike signs minus,

Powers of numbers. - The product of two or more powers of any

number is the number with an exponent equal to the sum of the powers:  $a^2 \times a^3 = a^5$ ;  $a^2b^2 \times ab = a^3b^3$ ;  $-7ab \times 2ac = -14 a^2bc$ .

To multiply a polynomial by a monomial, multiply each term of the polynomial by the monomial and add the partial products:  $(6a - 3b) \times 3c = 18ac$ - 3bc.

To multiply two polynomials, multiply each term of one factor by each term of the other and add the partial products:  $(5a - 6b) \times (3a - 4b) =$  $15a^2 - 38ab + 24b^2$ 

The square of the sum of two numbers = sum of their squares + twice their product.

The square of the difference of two numbers = the sum of their squares - twice their product.

The product of the sum and difference of two numbers = the difference of their squares:

$$(a+b)^2 = a^2 + 2ab + b^2;$$
  $(a-b)^2 = a - 2ab + b^2;$   $(a+b) \times (a-b) = a^2 - b^2.$ 

The square of half the sums of two quantities is equal to their product plus the square of half their difference:  $\left(\frac{a+b}{2}\right)^2 = ab + \left(\frac{a-b}{2}\right)^2$ .

The square of the sum of two quantities is equal to four times their products, plus the square of their difference:  $(a+b)^2 = 4ab + (a-b)^2$ 

The sum of the squares of two quantities equals twice their product, plus the square of their difference:  $a^2 + b^2 = 2ab + (a - b)^2$ .

The square of a trinomial = the square of each term + twice the product

$$(a+b)^2 = a^2 + 2ab + b^2;$$
  $(a+b)^3 = a^3 + 3a^2b + 3ab^2 + b^3;$   $(a+b)^4 = a^4 + 4a^3b + 6a^2b^2 + 4ab^3 + b^4.$ 

In each case the number of terms is one greater than the exponent of

the power to which the binomial is raised. 2. In the first term the exponent of a is the same as the exponent of the power to which the binomial is raised, and it decreases by 1 in each succeeding term.

3. b appears in the second term with the exponent 1, and its exponent increases by 1 in each succeeding term.

 The coefficient of the first term is 1.
 The coefficient of the second term is the exponent of the power to which the binomial is raised.

6. The coefficient of each succeeding term is found from the next preceding term by multiplying its coefficient by the exponent of a, and dividing the product by a number greater by 1 than the exponent of b. (See Binomial Theorem, below.)

Parentheses. - When a parenthesis is preceded by a plus sign it may be **FARENTHESES.** — when a parenthesis is preceded by a plus sign it may be removed without changing the value of the expression: a+b+(a+b)=2a+2b. When a parenthesis is preceded by a minus sign it may be removed if we change the signs of all the terms within the parenthesis: 1-(a-b-c)=1-a+b+c. When a parenthesis is within a parenthesis remove

the inner one first: 
$$a - \left[b - \left\{c - (d - e)\right\}\right] = a - \left[b - \left\{c - d + e\right\}\right]$$

=a-[b-c+d-e]=a-b+c-d+e. Multiplication sign. X, has the effect of a parenthesis, in that the operation indicated by it must be performed before the operations of addition

or subtraction.  $a+b\times a+b=a+ab+b$ ; while  $(a+b)\times (a+b)=a^2+ab+b^2$ , and  $(a+b)\times a+b=a^2+ab+b$ . **Division.**—The quotient is positive when the dividend and divisor have like signs, and negative when they have unlike signs: abc+b=ac;

 $abc \div - b = -ac$ . To divide a monomial by a monomial, write the dividend over the divisor with a line between them. If the expressions have common factors, remove the common factors:

$$a^{2}bx + aby = \frac{a^{2}bx}{aby} = \frac{ax}{y}; \quad \frac{a^{4}}{a^{3}} = a; \quad \frac{a^{3}}{a^{6}} = \frac{1}{a^{2}} = a^{-2}.$$

To divide a polynomial by a monomial, divide each term of the polynomial

To divide a polynomial by a honomial, divide each term of the polynomial by the monomial; (8db – 12dc) + 4d = 2b – 3c.

To divide a polynomial by a polynomial, arrange both dividend and divisor in the order of the ascending or descending powers of some common letter, and keep this arrangement throughout the operation.

Divide the first term of the dividend by the first term of the divisor, and write the result as the first term of the quotient,

Multiply all the terms of the divisor by the first term of the quotient and subtract the product from the dividend. If there be a remainder, consider it as a new dividend and received as before (22 kg), (a, 1, b)

it as a new dividend and proceed as before:  $(a^2 - b^2) \div (a + b)$ .

$$\begin{array}{c|c}
a^{2} - b^{2} & a + b. \\
a^{2} + ab & a - b. \\
- ab - b^{2}. \\
- ab - b^{2}.
\end{array}$$

The difference of two equal odd powers of any two numbers is divisible

by their difference and also by their sum:

 $(a^3 - b^3) + (a - b) = a^2 + ab + b^2; (a^3 - b^3) + (a + b) = a^2 - ab + b^2.$ 

The difference of two equal even powers of two numbers is divisible by their difference and also by their sum:  $(a^2 - b^2) + (a - b) = a + b$ . The sum of two equal even powers of two numbers is not divisible by either the difference or the sum of the numbers; but when the exponent of each of the two equal powers is composed of an odd and an even factor, the sum of the given power is divisible by the sum of the powers expressed by the even factor. Thus  $x^6 + y^6$  is not divisible by x + y or by x - y, but is divisible by  $x^2 + y^2$ .

Simple equations.—An equation is a statement of equality between

two expressions; as, a+b=c+d. A simple equation, or equation of the first degree, is one which contains only the first power of the unknown quantity. If equal changes be made (by addition, subtraction, multiplication, or division) in both sides of an

(by addition, subtraction, multiplication, or division) in both sides of an equation, the results will be equal. Any term may be changed from one side of an equation to another, provided its sign be changed: a+b=c+d; a=c+d-b. To solve an equation having one unknown quantity, transpose all the terms involving the unknown quantity to one side of the equation, and all the other terms to the other side; combine like terms, and divide both sides by the coefficient of the unknown quantity. Solve 8x - 29 = 26 - 3x. 8x + 3x = 29 + 26; 11x = 55; x = 5, ans.

Simple algebraic problems containing one unknown quantity are solved by making x = the unknown quantity, and stating the conditions of the problem in the form of an algebraic equation, and then solving the equation. What two numbers are those whose sum is 48 and difference 14? Let x= the smaller number, x+14 the greater. x+x+14=48. 2x=34, x=17; x+14=31, ans. Find a number whose treble exceeds 50 as much as its double falls short

of 40. Let x = the number. 3x - 50 = 40 - 2x; 5x = 90; x = 18, ans. Prov-

ing, 54 - 50 = 40 - 36.

Equations containing two unknown quantities.- If one Equations containing two unknown quantities,—If one equation contains two unknown quantities, and y, an indefinite number of pairs of values of x and y may be found that will satisfy the equation, but a second equation be given only one pair of values can be found that will satisfy both equations. Simultaneous equations, or those that may be satisfied by the same values of the unknown quantities, are solved by combining the equations so as to obtain a single equation containing only one unknown quantity. This process is called elimination.

Elimination by addition or subtraction.—Multiply the equation by such numbers as will make the coefficients of one of the unknown quanti-

ties equal in the resulting equation. Add or subtract the resulting equations according as they have unlike or like signs.

Solve 
$$\begin{cases} 2x + 3y = 7. & \text{Multiply by 2: } 4x + 6y = 14 \\ 4x - 5y = 3. & \text{Subtract: } 4x - 5y = 3 \end{cases}$$
  $11y = 11; y = 1.$ 

Substituting value of y in first equation, 2x+3=7; x=2. Elimination by substitution.—From one of the equations obtain the value of one of the unknown quantities in terms of the other. Substitute for this unknown quantity its value in the other equation and reduce the resulting equations.

Solve 
$$\begin{cases} 2x + 3y = 8. & (1). & \text{From (1) we find } x = \frac{8 - 3y}{2}. \\ 3x + 7y = 7. & (2). \end{cases}$$

Substitute this value in (2): 
$$3\left(\frac{8-3y}{2}\right) + 7y = 7$$
; =  $24 - 9y + 14y = 14$ ,

whence y=-2. Substitute this value in (1): 2x-6=8; x=7. Elimination by comparison.—From each equation obtain the value of one of the unknown quantities in terms of the other. Form an equation from these equal values, and reduce this equation.

Solve 
$$\begin{cases} 2x - 9y = 11. & \text{(1). From (1) we find } x = \frac{11 + 9y}{2}. \\ 3x - 4y = 7. & \text{(2). From (2) we find } x = \frac{7 + 4y}{3}. \end{cases}$$

Equating these values of 
$$x$$
,  $\frac{11+9y}{2} = \frac{7+4y}{3}$ ;  $19y = -19$ ;  $y = -1$ .

Substitute this value of y in (1): 2x + 9 = 11; x = 1. If three simultaneous equations are given containing three unknown quantities, one of the unknown quantities must be eliminated between two pairs of the equations; then a second between the two resulting equations.

Quadratic equations.—A quadratic equation contains the square of the unknown quantity, but no higher power. A pure quadratic contains the square only; an affected quadratic both the square and the first power. To solve a pure quadratic, collect the unknown quantities on one side, and the known quantities on the other; divide by the coefficient of the unknown quantity and extract the square root of each side of the resulting

Solve  $3x^2 - 15 = 0$ .  $3x^2 = 15$ ;  $x^2 = 5$ ;  $x = \sqrt{5}$ 

equation.

A root like \$\sqrt{5}\$, which is indicated, but which can be found only approximately, is called a surd.

Solve  $3x^2 + 15 = 0$ .  $3x^2 = -15$ ;  $x^2 = -5$ ;  $x = \sqrt{-5}$ . The square root of -5 cannot be found even approximately, for the square

The square root of -5 cannot be found even approximately, for the square of any number positive or negative is positive; therefore a root which is indicated, but cannot be found even approximately, is called imaginary. To solve an affected quadratic.<math>-1. Convert the equation into the form  $a^2x^2 \pm 2abx = c$ , multiplying or dividing the equation if necessary, so as to make the coefficient of  $x^2$  a square number.

2. Complete the square of the first member of the equation, so as to convert it to the form of  $a^2x^2 \pm 2abx + b^2$ , which is the square of the hinomial vertex of the follows: add to each side of the equation the square of the quotient obtained by dividing the second term by twice the square root of the first term. first term.

3. Extract the square root of each side of the resulting equation. Solve  $3x^2 - 4x = 32$ . To make the coefficient of  $x^2$  a square number, multiply by  $3: 9x^2 - 12x = 96: 12x + (2 \times 3x) = 2: 2^2 = 4$ . Complete the square:  $9x^2 - 12x + 4 = 100$ . Extract the root:  $3x - 2 = \pm$ 

10, whence x = 4 or -2.2/3. The square root of 100 is either +10 or -10.

since the square of -10 as well as  $+10^2 = 100$ .

Problems involving quadratic equations have apparently two solutions, as a quadratic has two roots. Sometimes both will be true solutions, but generally one only will be a solution and the other be inconsistent with the conditions of the problem.

The sum of the squares of two consecutive positive numbers is 481. Find

the numbers.

Let x = one number, x + 1 the other.  $x^2 + (x + 1)^2 = 481$ .  $2x^2 + 2x + 1$ = 481. $x^2 + x = 240$ . Completing the square,  $x^2 + x + 0.25 = 240.25$ . Extracting

the root we obtain  $x + 0.5 = \pm 15.5$ ; x = 15 or -16.

The positive root gives for the numbers 15 and 16. The negative root -

16 is inconsistent with the conditions of the problem. Quadratic equations containing two unknown quantities require different methods for their colution, according to the form of the equations. For these methods reference must be made to works on algebra.

**Theory of exponents.**  $\sqrt[n]{a}$  when n is a positive integer is one of n equal factors of a.  $\sqrt[n]{a^m}$  means a is to be raised to the mth power and the

nth root extracted.  $(\sqrt[n]{a})^m$  means that the nth root of a is to be taken and the result raised to the mth power.

 $\sqrt[n]{a^m} = \left(\sqrt[n]{a}\right)^m = a^m$ . When the exponent is a fraction, the numerator indicates a power, and the denominator a root.  $a^{\frac{6}{2}} = \sqrt{a^6} = a^3$ ;  $a^{\frac{3}{2}} =$ 

 $V a^3 = a^{1.5}$ To extract the root of a quantity raised to an indicated power, divide the exponent by the index of the required root; as,

$$\frac{m}{4\sqrt{a^m}}$$
  $\frac{m}{n}$ ;  $\frac{3}{4\sqrt{a^6}}$   $\frac{6}{a^3}$   $\frac{6}{a^3}$ 

 $\sqrt[n]{a^m} = a^{\frac{m}{n}}; \qquad \sqrt[3]{a^6} = a^{\frac{6}{3}} = a^2.$  Subtracting 1 from the exponent of a is equivalent to dividing by a:

 $a^{2}-1=a^{1}=a; \ a^{1}-1=a^{0}=\frac{a}{a}=1; \ a^{0}-1=a^{-1}=\frac{1}{a}; \ a^{-1}-1=a^{-2}=\frac{1}{a^{2}}$ 

A number with a negative exponent denotes the reciprocal of the number

with the corresponding positive exponent.

A factor under the radical sign whose root can be taken may, by having the root taken, be removed from under the radical sign:

$$\sqrt{a^2b} = \sqrt{a^2} \times \sqrt{b} = a \sqrt{b}$$
.

A factor outside the radical sign may be raised to the corresponding power and placed under it:

$$\sqrt{\frac{a}{b}} = \sqrt{\frac{a\overline{b}}{b^2}} = \sqrt{ab \times \frac{1}{b^2}} = \frac{1}{b} \sqrt{ab}; \qquad \sqrt{\frac{a}{b^2}} = \frac{1}{b} \sqrt{a}$$

Binomial Theorem .- To obtain any power, as the nth, of an expression of the form x + a

$$(a+x)^n = a^n + na^{n-1}x + \frac{n(n-1)a^{n-2}}{1.2}x^2 + \frac{n(n-1)(n-2)a^{n-3}}{1.2.3.}x^2 +$$

The following laws hold for any term in the expansion of  $(a + x)^n$ .

The exponent of x is less by one than the number of terms. The exponent of a is n minus the exponent of x.

The last factor of the numerator is greater by one than the exponent of a. The last factor of the denominator is the same as the exponent of x.

In the rth term the exponent of x will be r-1. The exponent of a will be n-(r-1), or n-r+1. The last factor of the numerator will be n-r+2.

The last factor of the denominator will be = r - 1. Hence the rth term  $= \frac{n(n-1)(n-2) \dots (n-r+2)}{1 \cdot 2 \cdot 3 \dots (r-1)} a^{n-r+1} x^{r-1}$ 

## GEOMETRICAL PROBLEMS.

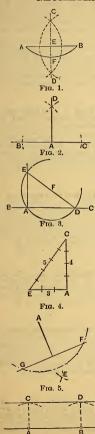


FIG. 6.

- 1. To bisect a straight line, or an arc of a circle (Fig. 1).— From the ends A, B, as centres, describe arcs intersecting at C and D, and draw a line through C and D which will bisect the line at E or the arc at F.
- 2. To draw a perpendicular to a straight line, or a radial line to a circular arc.—Same as in Problem 1. *CD* is perpendicular to the line *AB*, and also radial to the arc.
- 3. To draw a perpendicular to a straight line from a given point in that line (Fig. 2).—With any radius, from the given point A in the line B C, cut the line at B and C. With a longer radius describe arcs from B and C, cutting leach other at D, and draw the perpendicular D A.
- 4. From the end A of a gievn line A D to erect a perpendicular A E (Fig. 3).—From any centre F, above A D, describe a circle passing through the given point A, and cutting the given line at D. Draw D F and produce it to cut the circle at E, and draw the perpendicular A E. the control of the circle at E, and draw the perpendicular A E.

ting the given line at D. Draw D E and produce it to cut the circle at E, and draw the perpendicular A E. Second Method (Fig. 4).—From the given point A set off a distance A E equal to three parts, by any scale; and on the centres A and E, with radii of four and five parts respectively, describe arcs intersecting at C. Draw the perpendicular A C.

Note.—This method is most useful on very large scales, where straight edges are inapplicable. Any multiples of the numbers 3, 4, 5 may be taken with the same effect as 6, 8, 10, or 9, 12, 15.

- 5. To draw a perpendicular to a straight line from any point without it (Fig. 5.)—From the point A, with a sufficient radius cut the given line at F and G, and from these points describe arcs cutting at E. Draw the perpendicular A E.
- 6. To draw a straight line parallel to a given line, at a given distance apart (Fig. 6).— From the centres A, B, in the given line, with the given distance as radius, describe arcs C, D, and draw the parallel lines C D touching the arcs.

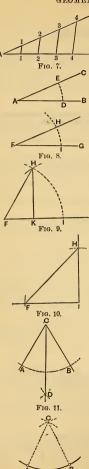


Fig. 12.

7. To divide a straight line into a number of equal parts (Fig. 7).—To divide the line AB into, say, five parts, draw the line AC at an angle from A; set off five equal parts; draw B 5 and draw parallels to from the other points of division in AC. These parallels divide AB as required.

Nors.—By a similar process a line may be divided into a number of unequal parts; setting off divisions on A C, proportional by a scale to the required divisions, and drawing parallel cutting A B. The triangles 411, A22, 433, etc., are similar triangles

- 8. Upon a straight line to draw an angle equal to a given angle (Fig. 8).—Let A be the given angle and FG the line. From the point A with any radius describe the arc D E. From F with the same radius describe IH. Set off the arc I H equal to D E, and draw FH. The angle F is equal to A, as required.
- 9. To draw angles of  $60^{\circ}$  and  $30^{\circ}$  (Fig. 9.—From E, with any radius FL describe an arc IH; and from I, with the same radius, cut the arc at H and draw F Hto form the required angle IF H. Draw the perpendicular H K to the base line to form the angle of  $30^{\circ}$  F H K.
- 10. To draw an angle of  $45^{\circ}$  (Fig. 10).—Set off the distance FI; draw the perpendicular IH equal to IF, and join HF to form the angle at F. The angle at H is also  $45^{\circ}$ .
- 11. To bisect an angle (Fig. 1),—Let  $A \subset B$  be the angle; with C as a centre draw an arc cutting the sides at A, B. From A and B as centres, describe arcs cutting each other at D. Draw C D, dividing the angle into two equal parts.
- 12. Through two given points to describe an arc of a circle with a given radius (Fig. 12).—From the points A and B as centres, with the given radius, describe arcs cutting at C; and from C with the same radius describe an arc A B.



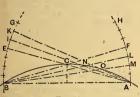
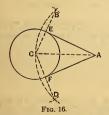


Fig. 14.



Fig. 15.



13. To find the centre of a circle or of an arc of a circle (Fig. 13).—Select three points, A, B, C, in the circumference, well apart; with the same radius describe arcs from these three points, cutting each other, and draw the two lines, D E, F G, through their intersections. The point O, where they cut, is the centre of the circle or arc.

To describe a circle passing through three given points.

—Let A, B, C be the given points, and proceed as in last problem to find the centre O, from which the circle may be described.

14. To describe an arc of a circle passing through three given points when the centre is not available (Fig.14).-From the extreme points A, B, as centres, describe arcs AH, B, G. Through the third point C draw A, E, B, G, cutting the arcs. Divide A, F and B, E into any number of equal parts, and set off a series of equal parts of the same series of equal parts of the arcs beyond the points EF. Draw straight lines, BL, BM, etc., to the divisions in AF, and AL, AK, etc., to the divisions in EG. The successive intersections N, O, etc., of these lines are points in the circle required between the given points A and C. which may be drawn in; similarly the remaining part of the curve B C may be described. (See also Problem 54.)

15. To draw a tangent to a circle from a given point in the circumference (Fig. 15). —Through the given point A, draw the radial line A C, and a perpendicular to it, F G, which is the tangent required.

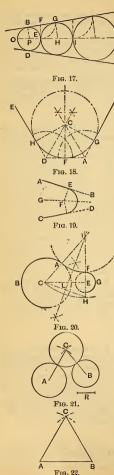
16. To draw tangents to a circle from a point without it (Fig. 16).—From A, with the radius A C, describe an arc B C D, and from C. with a radius equal to the diameter of the circle, cut the arc at B D. Join B C, C D, cutting the circle at EF, and draw A E, A F, the tangents.

Note.—When a tangent is already

drawn, the exact point of contact may be found by drawing a perpendicular

to it from the centre.

17. Between two inclined lines to draw a series of circles touching these lines and touching each other (Fig. 17). Bisect the inclination of the given lines AB, CB, by the line NB. From point P in this line draw the perpendicular BB to the line AB, and



on P describe the circle B D, touching the lines and cutting the centre line at E. From E draw E P perpendicular to the centre line, cutting A B at F, and from F describe an arc E G, cutting A B at G. Draw G H parallel to B P, giving H, the centre of the next circle, to be described with the radius H E, and so on for the next circle IN.

Inversely, the largest circle may be described first, and the smaller ones in succession. This problem is of fre-

quent use in scroll-work.

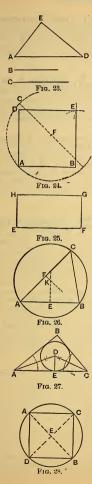
18. Between two inclined lines to draw a circular segment tangent to the lines and passing through a point F on the line-F C which bisects the angle of the lines (Fig. 18). —Through F draw D A at right angles to F C: bisect the angles A and D, as in Problem 11, by lines cutting at C, and from C with radius C F draw the arc H F G required.

19. To draw a circular are that will be tangent to two given lines A B and C D inclined to one another, one tangential point E being given (Fig. 19).—Draw the centre line GF. From E draw EF at right to angles AB; then F is the centre of the circle required.

20. To describe a circular are joining two circles, and touching one of them at a given point (Fig. 20).—To join the circles AB, FG, by an are touching one of them at F, draw the radius EF, and produce it both ways. Set off FH equal to the radius AC of the other circle; join CH and bisect it with the perpendicular LI, cutting EF at I. On the centre I, with radius IF, describe the arc FA as required.

21. To draw a circle with a given radius R that will be tangent to two given circles A and B (Fig. 21).—From center of circle A with radius equal R plus radius of A, and from centre of E with radius equal to R + radius of B, draw two arcs cutting each other in C, which will be the centre of the circle required.

22. To construct an equilateral triangle, the sides being given (Fig. 29.—On the ends of one side, A, B, with A B as radius, describe arcs cutting at C, and draw A C, CB,



23. To construct a triangle of unequal sides (Fig. 23).—On either end of the base A D, with the side B as radius, describe an arc; and with the side C as radius, on the other end of the base as a centre, cut the arc at E. Join A E, D E.

24. To construct a square on a given straight line A B (Fig. 24).—At A erect a perpendicular A C, as in Problem 4. Lay off A Dequal to AB: from D and B as centres with radius equal AB, describe arcs cutting each other in E. Join DE and BE.

25. To construct a rectangle with given base E F and height E H (Fig. 25).—On the base EF draw the perpendiculars EH, F G equal to the height, and join G H.

26. To describe a circle about a triangle (Fig. 26).—
Bisect two sides AB, AC of the triangle at EF, and from these points draw perpendiculars cutting at K. On the centre K, with the radius KA, draw the circle A B C.

27. To inscribe a circle in a triangle (Fig. 27).-Bisect two of the angles A, C, of the triangle by lines cutting at D; from D draw a perpendicular D E to any side, and with DE as radius describe a circle

When the triangle is equilateral, draw a perpendicular from one of the angles to the opposite side, and from the side set off one third of the per-

pendicular.

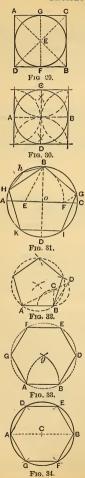
28. To describe a circle about a square, and to inscribe a square in a circle (Fig. 28).—To describe the circle, draw the diagonals AB, CD of the square, cutting at E. On the centre E, with the radius AB, describe the circle.

To inscribe the square.—
Draw the two diameters, AB, CD, at the truly and the square of the squar

right angles, and join the points A, B,

CD, to form the square.

Note.-In the same way a circle may be described about a rectangle.



29. To inscribe a circle in a square (Fig. 29).—To inscribe the circle, draw the diagonals AB, CD of the square, cutting at E; draw the perpendicular E F to one side, and with the radius E F describe the circle.

30. To describe a square about a circle (Fig. 30).—Drawtwo diameters AB, CD at right angles. With the radius of the circle and A, B, C and D as centres, draw the four half circles which cross one another in the corners of the square.

31. To inscribe a pentagon in a circle (Fig. 3).—Draw diameters A C, B D at right angles, cutting at o. Bisect A o at E, and from E, with radius E E, cut the circumference at G, H, and with the same radius step round the circle to I and K; join the points so found to form the pentagon.

32. To construct a pentagon on a given line A B (Fig. 32).—From B evect a perpendicular B C half the length of A B; join A C and prolong it b D, making C D = B C. Then B D is the radius of the circle circumscribing the pentagon. From A and B as centres, with B D as radius, draw arcs cutting each other in O, which is the centre of the circle.

33. To construct a hexagon upon a given straight line (Fig. 33).—From A and B, the ends of the given line, with radius A B, describe arcs cutting at g: from g, with the radius g A, describe a circle; with the same radius set off the arcs A G, G, and B D, D E. Join the points so found to form the hexagon. The side of a hexagon = radius of its circumscribed circle.

34. To inscribe a hexagon in a circle (Fig. 31).—Draw a diamieter A CB. From A and B as centres, with the radius of the circle A C, cut the circumference at D, E, F, G, and draw A D, D E, etc., to form the hexagon. The radius of the circle is equal to the side of the hexagon; therefore the points D, E, etc., may also be found by stepping the radius six times round the circle. The angle between the diameter and the sides of a hexagon and also the exterior angle between a side and an adjacent side prolonged is 60 degrees; therefore a hexagon may conveniently be drawn by the use of a 60-degree triangle.

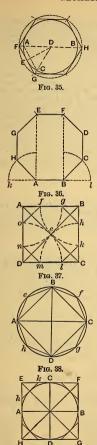


Fig. 39.

35. To describe a hexagon dbaut a circle (Fig. 35).—Draw a diabeter AD but and with the radius AD but and with the radius AD but and with the radius AD but and bisect it with the radius DE; through E draw FG, parallel to AC, cutting the diameter at F, and with the radius D E describe the circumscribing circle F H. Within this circle describe a hexagon by the preceding problem. A more convenient method is by use of a 60-degree triangle. Four of the sides make angles of 60 degrees with the diameter, and the other two are parallel to the diameter.

36. To describe an octagon on a given straight line (Fig. 36).—Produce the given line A B both ways, and draw perpendiculars A E, B F; bisect the external angles A and B by the lines A H, B C, which make equal to A B. Draw C D and H G parallel to A E, and equal to A B; from the centres G, D, with the radius A B, cut the perpendiculars at E, F, and A and A B C C is complete the octagon.

37. To convert a square into an octagon (Fig. 37).—Draw the diagonals of the square cutting at e; from the corners A, B, C, D, with A e as radius, describe arcs cutting the sides at gn, fk, hm, and ol, and join the points so found to form the octagon. Adjacent sides of an octagon make an angle of 135 degrees.

38. To inscribe an octagon in a circle (Fig. 38).—Draw two diameters,  $A \subset B D$  at right angles; bisect the arcs A B, B C, etc., at e f, etc., and join A e, e B, etc., to form the octagon.

39. To describe an octagon about a circle (Fig. 39).—Describe a square about the given circle AB; draw perpendiculars hk, etc., to the diagonals, touching the circle to form the octagon.

40. To describe a polygon of any number of sides upon a given straight line (Fig. 40).—Produce the given line A B, and on A,

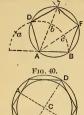


Fig. 41.



Fig. 42.



with the radius A B, describe a semi-circle; divide the semi-circumference into as many equal parts as there are to be sides in the polygon—say, in this example, five sides. Draw lines from A through the divisional points D, b, and c, omitting one point a; and on the centres B, D, with the radius A B, cut A B at E and A C at F. Draw D E, F, F B to complete the polygon.

41. To inscribe a circle within a polygon (Figs. 41, 42).—When the polygon has an even number of sides (Fig. 41), bisect two opposite sides at A and B; draw AB, and bisect it at C by a diagonal DE, and with the radius CA describe the circle.

When the number of sides is odd (Fig. 42), bisect two of the sides at A and B, and draw lines  $A \in B$  D to the opposite angles, intersecting at C; from C, with the radius CA, describe the circle.

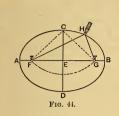
**42. To describe a circle without a polygon** (Figs. 41, 42). —Find the centre *C* as before, and with the radius *C D* describe the circle.

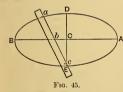
43. To inscribe a polygon of any number of sides within a circle (Fig. 43).—Draw the diameter AB and through the eentre E draw the perpendicular EC, cutting the circle at F. Divide EF into four equal parts, and set off three parts equal to those from F to C. Divide the diameter AB into as many equal parts as the polygon is to have sides; and from C draw CD, through the second point of division, cutting the circle at D. Then AD is equal to one side of the polygon, and by stepping round the circumference with the length AD the polygon may be completed.

TABLE OF POLYGONAL ANGLES.

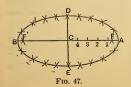
Number			Angle	Number	Angle		
of Sides.			at Centre.	of Sides.	at Centre.		
No. 3 4 5 6 7 8	Degrees. 120 90 72 60 5137 45	No. 9 10 11 12 18 14	Degrees.  40 36 32 <sup>1</sup> / <sub>1</sub> 30 27 <sup>1</sup> / <sub>1</sub> 25 <sup>2</sup> / <sub>7</sub>	No. 15 16 17 18 19 20	Degrees.  24  22½  21 17  20  19  18		

In this table the angle at the centre is found by dividing 360 degrees, the number of degrees in a circle, by the number of sides in the polygon; and by setting off round the centre of the circle a succession of angles by means of the protractor, equal to the angle in the table due to a given number of sides, the radii so drawn will divide the circumference into the same number of parts.









44. To describe an ellipse when the length and breadth are given (Fig. 44). - A B, transverse axis; CD, conjugate axis; FG, foci. The sum of the distances from C to F and G, also the sum of the distances from F and G to any other point in the curve, is equal to the transverse axis. From the centre C, with A E as radius, cut the axis A B at F and G, the foci; fix a couple of pins into the axis at F and G, and loop on a thread or cord upon them equal in length to the axis A B, so as when stretched to reach to the extremity C of the conjugate axis, as shown in dot-lining. Place a pencil inside the cord as at H, and guiding the pencil in this way, keeping the cord equally in tension, carry the pencil round the pins F, G, and so describe the ellipse.

Note.—This method is employed in setting off elliptical garden - plots,

walks, etc.

2d Method (Fig. 45). — Along the straight edge of a slip of stiff paper mark off a distance a c equal to A C. half the transverse axis; and from the same point a distance ab equal to CD, half the conjugate axis. Place the slip so as to bring the point b on the line AB of the transverse axis, and the point c on the line DE; and set off on the drawing the position of the point a. Shifting the slip so that the point b travels on the transverse axis, and the point c on the conjugate axis, any number of points in the curve may be found, through which the curve may be traced.

3d Method (Fig. 46).—The action of the preceding method may be em-bodied so as to afford the means of bounds on as to about the means of describing a large curve continuously by means of a bar m k, with steel points m, l, k, riveted into brass slides adjusted to the length of the semi-axis and fixed with set-screws. A rectangular cross E G, with guiding-axis and Gslots is placed, coinciding with the two axes of the ellipse A C and B H. By sliding the points k, l in the slots, and carrying round the point m, the curve may be continuously described.

A pen or pencil may be fixed at m.
4th Method (Fig. 47).—Bisect the
transverse axis at C and through C transverse axis at C, and through C draw the perpendicular D E, making C D and C E each equal to half the conjugate axis. From D or E, with the radius A C, cut the transverse axis at F, F', for the foci. Divide A C into a number of parts at the points 1, 2, 3, etc. With the radius A I on F and F' as centres, describe arcs, and with the radius B I on the same centres cut these arcs as shown.

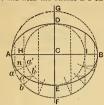


Fig. 48.

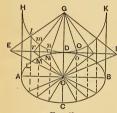


Fig. 49.

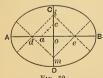


Fig. 50.



Fig. 51.

Repeat the operation for the other divisions of the transverse axis. The series of intersections thus made are points in the curve, through which the

curve may be traced.

5th Method (Fig. 48).—On the two
axes A B, D E as diameters, on centre C, describe circles; from a number of points a, b, etc., in the circumference AFB, draw radii cutting the inner circle at a', b', etc. From a, b, etc., draw perpendiculars to AB; and from a', b', etc., draw parallels to A B, cut-

ting the respective perpendiculars at n, o, etc. The intersections are points in the curve, through which the curve may be traced. 6th Method (Fig. 49). - When the

transverse and conjugate diameters are given, AB, CD, draw the tangent EF parallel to AB. Produce CD, and on the centre G with the radius of half AB, describe a semicircle HDK; from the centre G draw any number of straight lines to the points E, r, etc., in the line E, F, cutting the Let M, the line B, B, enting in the centre of the ellipse draw straight lines to the points B, P, etc., and from the points B, P, etc., and from the points B, P, etc., draw parallels to G. Centring the lines O E, or, etc., at E, M, N, etc. These are points in the circumference of the ellipse, and the curve may be traced through them. Points in the other half of the ellipse are formed by extending the intersecting lines as indicated in the figure.

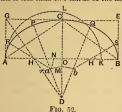
45. To describe an ellipse approximately by means of circular arcs.—First.—With arcs of two radii (Fig. 50).—Find the different control of two radii (Fig. 50). ence of the two axes, and set it off from the centre O to a and c on O A and O C; draw a c, and set off half a c to d; draw d i parallel to a c; set off 0 e equal to 0 d; join e i, and draw the parallels e m, d m. From m, with radius m C, describe an arc through C; and from i describe an arc through D; from d and e describe ares through A and B. The four arcs form the

ellipse approximately.

Note.—This method does not apply satisfactorily when the conjugate axis is less than two thirds of the transverse axis.

2d Method (by Carl G. Barth, Fig. 51).—In Fig. 51 a b is the major and c d the minor axis of the ellipse to be approximated. Lay off be equal to the semi-minor axis c O, and use a e as radius for the arc at each extremity of the minor axis. Bisect e o at f and lay off e g equal to e f, and use g b as radius for the arc at each extremity of the major axis.

The method is not considered applicable for cases in which the minor axis is less than two thirds of the major.



3d Method: With arcs of three radii (Fig. 52).-On the transverse axis A B draw the rectangle B G on the height OC; to the diagonal AC draw the perpendicular GHD; set off OK equal to OC, and describe a semi-circle on AK, and produce OC to L; set off O M equal to C L, and from D describe an arc with radius DM; from A, with radius OL, cut this arc at a. Thus the five centres D, a, b, H, H' are found, from which the arcs are described to form the ellipse.

Note.—This process works well for

nearly all proportions of ellipses. It is employed in striking out vaults and

FIG. 52. stone bridges.

4th Method (by F. R. Honey, Figs. 53 and 54).—Three radii are employed. With the shortest radius describe the two arcs which pass through the vertices of the major axis, with the longest the two arcs which pass through the vertices of the minor axis, and with the third radius the four arcs which connect the former.

A simple method of determining the radii of curvature is illustrated in

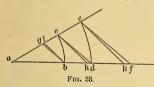
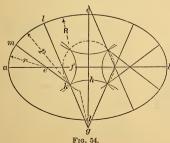


Fig. 53. Draw the straight lines a f and a c, forming any angle at a. With a as a centre, and with radii ab and ac, respectively, equal to the semi-minor and semi-major axes, draw the arcs be and cd. Join ed, and through b and c respectively draw bg and cf parallel to ed, intersecting ac at g, and af at f; af is the radius of curvature at the vertex of the minor axis; and a a the radius of curvature at the

vertex of the major axis.

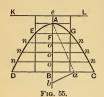
Lay off dh (Fig. 53) equal to one eighth of bd. Join eh, and draw ck and b l parallel to e h. Take a k for the longest radius (=R), a l for the shortest radius (=r), and the arithmetical mean, or one half the sum of the semi-axes for the third radius (= p), and employ these radii for the eight-centred oval as follows:



Let a b and cd (Fig. 54) be the major and minor axes. Lay off ae equal to r, and af equal to p; also lay off cg equal to R, and ch equal to p. With g as a centre and gh as a radius, draw the arc h k with the centre e and radius e f draw the arc f k, intersecting h k at k. Draw the line gk and produce it, making g l equal to R. Draw ke and produce it, making k m equal to p. With the centre g and radius g c (= R) draw the arc cl; with the centre k and radius kl (= p) draw the arc lm, and with the centre e and radius em (=r) draw the arc  $m \alpha$ .

The remainder of the work is symmetrical with

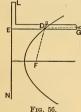
respect to the axes.



' 46. The Parabola. - A parabola (DAC, Fig. 55) is a curve such that every point in the curve is equally distant from the directrix KL and the focus F. The focus lies in the axis A B drawn from the vertex or head of the curve A, so as to divide the figure into two equal parts. The vertex A is equidistant from the directrix and the focus, or A e = A F. Any line the focus, or Ae = AF. Any I parallel to the axis is a diameter. straight line, as EG or DC, drawn across the figure at right angles to the axis is a double ordinate, and either half of it is an ordinate. The ordinate to the axis E F G, drawn through the focus, is called the parameter of the axis. A segment of the axis, reckoned from the vertex, is an abscissa of the axis, and it is an abscissa of the ordinate drawn from the base of the abscissa. Thus, AB is an abscissa of the ordinate BC.

Abscissæ of a parabola are as the squares of their ordinates.

To describe a parabola when an abscissa and its ordinate are given (Fig. 55).—Bisect the given ordinate B C at a, draw Aa, and then a b perpendicular to it, meeting the axis at b. Set off Ae, AF, each equal to Bb; and draw KeL perpendicular to the axis. Then KL is the directrix and F is the focus. Through F and any number of points, o, o, etc., in the axis, draw double ordinates, no, n, etc. and from the centre F, with the radii Fe, o, e, etc., cut the respective ordinates at E, G, n, n, etc. The curve may be traced through these points as shown.



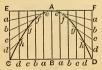


Fig. 57.

2d Method: By means of a square and a cord (Fig. 5b)—Place a straightedge to the directrix E.N, and apply to it a square L.E.G. Fasten to the end G one end of a thread or cord equal in length to the edge E.G, and attach the other end to the focus F; slide the square along the straightedge, holding the cord taut against the edge of the square by a peucil D, by which the curve is described.

 $3d\ Method$ ; When the height and the base are given (Fig. 57).—Let AB be the given axis, and CD a double ordinate or base; to describe a parabola of which the vertex is at A. Through A draw EF parallel to CD and through C and D draw CE and DF parallel to the axis. Divide BC and DF parallel to the axis, Divide BC and DF parallel to the axis, Divide BC and DF into the same number of parts. Through the points a,b,c,d in the base CD on each side of the axis draw perpendiculars, and through a,b,c,d in CE and DF draw lines to the vertex A, cutting the perpendiculars at e,f,g,h. These are points in the parabola, and the curve CAD may be traced as shown, passing through them.

47. The Hyperbola (Fig. 58).—A hyperbola is a plane curve, such that the difference of the distances from any point of it to two fixed points



Fig. 58.



Fig. 59.

is equal to a given distance. The fixed

points are called the foci

To construct a hyperbola.

Let H' and H' be the foci, and H' H' the distance between them. Take a ruler longer than the distance F' F. and fasten one of its extremities at the focus F'. At the other extremity, H. attach a thread of such a length that the length of the ruler shall exceed the length of the thread by a given distance A B. Attach the other extremity of the thread at the focus F

Press a pencil, P, against the ruler, and keep the thread constantly tense, while the ruler is turned around F' as a centre. The point of the pencil will describe one branch of the curve.

2d Method: By points (Fig. 59).— From the focus F' lay off a distance F' N equal to the transverse axis, or distance between the two branches of the curve, and take any other distance,

as F'H, greater than F'N.

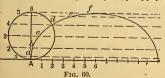
With F' as a centre and F'H as a radius describe the arc of a circle. Then with F as a centre and NH as a radius describe an arc intersecting the arc before described at p and q.

These will be points of the hyperbola, for F'q - Fq is equal to the trans-

verse axis AB.

If, with F as a centre and F' H as a radius, an arc be described, and a second arc be described with F' as a centre and NH as a radius, two points in the other branch of the curve will be determined. Hence, by changing the centres, each pair of radii will determine two points in each branch

The Equilateral Hyperbola. - The transverse axis of a hyperbola is the distance, on a line joining the foci, between the two branches of the curve. The conjugate axis is a line perpendicular to the transverse axis, drawn from its centre, and of such a length that the diagonal of the rectangle of the transverse and conjugate axes is equal to the distance between the foci. The diagonals of this rectangle, indefinitely prolonged, are the asymptotes of the hyperbola, lines which the curve continually approaches, but touches only at an infinite distance. If these asymptotes are perpendicular to each other, the hyperbola is called a rectangular or equilateral hyperbola. It is a property of this hyperbola that if the asymptotes are taken as axes of a rectangular system of coördinates (see Analytical Geometry), the product of the abscissa and ordinate of any point in the curve is equal to the product of the abscissa and ordinate of any other point; or, if p is the ordinate of any point and v its abscissa, and  $p_1$  and  $v_1$  are the ordinate of any point and v its abscissa, and  $p_1$  and  $p_2$  are the ordinate of any point and v its abscissa, and  $p_1$  and  $p_2$  are the ordinate of any point and v its abscissa, and  $p_2$  and  $p_3$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and v its abscissa, and  $p_4$  and  $p_4$  are the ordinate of any point and  $p_4$  and  $p_4$  are the ordinate of any point and  $p_4$  and  $p_4$  are the ordinate of any point and  $p_4$  are the ordina nate and abscissa of any other point,  $pv=p_1v_1$ ; or pv=a constant 48. The Cycloid



(Fig. 60).—If a circle Adbe rolled along a straight line A6, any point of the circumference as A will describe a curve, which is called a cycloid. The circle is called the generating circle, and A the generating point.

To draw a cycloid. -Divide the circumference

of the generating circle into an even number of equal parts, as A 1, 12, etc., and set off these distances on the base. Through the points 1, 2, 3, etc., on the circle draw horizontal lines, and on them set off distances 1a = A1, 2b = A2, 3c = A3, etc. The points A, a, b, c, etc., will be points in the cycloid, through which draw the curve.

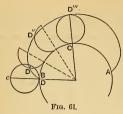


FIG. 62.



Fig. 63.

52. The Spiral.—The spiral is a curve described by a point which moves along a straight line according to any given law, the line at the same time having a uniform angular motion. The line is called the radius vector.



Fig. 64.

(Fig. 64). This curve is commonly used for cams. To describe it draw the radius

vector in several different directions around the centre, with equal angles between them; set off the distances 1, 2, 3, 4, etc., corresponding to the scale

upon which the curve is drawn, as shown in Fig. 64. In the common spiral (Fig. 64) the pitch is uniform; that is, the spires are equidistant. Such a spiral is made by rolling up a belt of uniform thickness,



Fig. 65.

49. The Epicycloid (Fig. 61) is generated by a point D in one circle DC rolling upon the circumference of Deforming upon the entire the container of another circle  $A \subset B$ , instead of on a flat surface or line; the former being the generating circle, and the latter the fundamental circle. The generating circle is shown in four positions, in which the generating point is successively marked D, D', D'', D'''. AD'''Bis the epicycloid.

50. The Hypocycloid (Fig. 62) is generated by a point in the generating circle rolling on the inside of the fundamental circle.

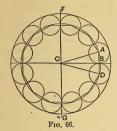
When the generating circle = radius of the other circle, the hypocycloid becomes a straight line.

51. The Tractrix Schiele's anti-friction curve (Fig. 63).—R is the radius of the shaft, C, 1, 2, etc., the axis. From O set off on R a small distance, o a; with radius R and centre a cut the axis at 1, join a 1, and set off a like small distance ab; from b with radius R cut axis at 2, join b 2, and so on, thus finding points o, a, b, c, d, etc., through which the curve is to be drawn.

If the radius vector increases directly as the measuring angle, the spires, or parts described in each revolution, thus gradually increasing their dis-tance from each other, the curve is known as the spiral of Archimedes

To construct a spiral with four centres (Fig. 65) .- Given the pitch of the spiral, construct a square about the centre, with the sum of the four sides equal to the pitch. Prolong the sides in one direction as shown; the corners are the centres for each arc of the external angles, forming a quadrant of a spire.

53. To find the diameter of a circle into which a certain number of rings will fit on its inside (Fig. 66).—For instance, what is the diameter of a circle into which twelve ½-inch rings will fit, as per sketch? Assume that we have found the diameter of the required



circle, and have drawn the rings inside of it. Join the centres of the rings by straight lines, as shown: we then by straight lines, as shown: we then obtain a regular polygon with 12 sides, each side being equal to the diameter of a given ring. We have now to find the diameter of a circle circumscribed about this polygon, and add the diameter of one ring to it; the sum will be the diameter of the circle sum will obtain the rings will fit. Through the centres A and D of two adjacent rings draw the radii CA and CD; since the polygon has twelve sides the angle  $A C D = 30^{\circ}$  and  $A C B = 15^{\circ}$ . One half of the side A D is equal to A B. We now give the following proportion: The sine of the angle ACB

Fig. 66. Is to AB as 1 is to the required radius. From this we get the following rule: Divide AB by the sine of the angle AB by the sine of the angle AB is the sine of the sine radius of the circumscribed circle; add to the corresponding diameter the diameter of one ring; the sum will be the required diameter FG.

diameter of one ring; the sum will be the required diameter F G.

54. To describe an arc of a circle which is too large to
be drawn by a beam compass, by means of points in the
arc, radius being given.—Suppose the radius is 20 feet and it is
desired to obtain five points in an arc whose half chord is 4 feet. Draw a
line equal to the half chord, full size, or on a smaller scale if more convenient, and erect a perpendicular at one end, thus making rectangular
axes of coordinates. Erect perpendiculars at points 1, 2, 3, and 4 feet from
the first perpendicular. Find values of x in the forgula of the circle the first perpendicular. Find values of y in the formula of the circle,  $x^2 + y^2 = R^2$  by substituting for x the values 0, 1, 2, 3, and 4, etc., and for  $R^2$ the square of the radius, or 400. The values will be  $y = \sqrt[4]{R^2 - x^2} = \sqrt[4]{400}$ .  $\sqrt{399}$ ,  $\sqrt{396}$ ,  $\sqrt{391}$ ,  $\sqrt{384}$ ; = 20, 19.975, 19.90, 19.774, 19.596,

Subtract the smallest,

or 19.596, leaving

0.404, 0.379, 0.304, 0.178, feet. Lay off these distances on the five perpendiculars, as ordinates from the

half chord, and the positions of five points on the arc will be found.

Through these the curve may be

drawn. (See also Problem 14.)
55. The Catenary is the curve assumed by a perfectly flexible chord when its ends are fastened at two points, the weight of a unit length

being constant.

The equation of the catenary is  $y = \frac{a}{2} \left( e^{\frac{a}{a}} + e^{-\frac{a}{a}} \right)$ , in which e is the

base of the Naperian system of logarithms.

To plot the catenary.-Let o (Fig. 67) be the origin of coordinates. Assigning to a any value as 3, the equation becomes

$$y = \frac{3}{2} \left( e^{\frac{x}{3}} + e^{-\frac{x}{3}} \right).$$

Fig. 67. To find the lowest point of the curve.

Put 
$$x = 0$$
;  $y = \frac{3}{2} \left( e^0 + e^{-0} \right) = \frac{3}{2} (1 + 1) = 3$ .

Then put 
$$x = 1$$
;  $y = \frac{3}{2} \left( e^{\frac{1}{3}} + e^{-\frac{1}{3}} \right) = \frac{3}{2} (1.396 + 0.717) = 3.17.$ 

Put 
$$x = 2$$
;  $y = \frac{3}{2} \left( e^{\frac{2}{3}} + e^{-\frac{2}{3}} \right) = \frac{3}{2} (1.948 + 0.513) = 3.69$ .

Put x = 3, 4, 5, etc., etc., and find the corresponding values of y. each value of y we obtain two symmetrical points, as for example p and  $p^1$ . In this way, by making a successively equal to 2, 3, 4, 5, 6, 7, and 8, the curves of Fig. 68 were plotted.

In each case the distance from the origin to the lowest point of the curve is equal to a; for putting x = 0, the general equation reduces to y = a.

is equal to a; for putting x=a, the general equation reduces to y=a. For values of a=6, 7, and 8 the catenary closely approaches the parabola. For derivation of the equation of the catenary see Bowser's Analytic Mechanics. For comparison of the catenary with the parabola, see article by F. R. Honey, Amer. Machinist, Feb. 1, 1894.

56. **The Involute** is a name given to the curve which is formed by the end of a string which is unwound from a cylinder and kept taut; confirmed to the confirmed tauthors are confirmed tauthors.

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sequently the string as it is unwound will always lie in the direction of a tangent to the cylinder. To describe the involute of any given circle, Fig. 68, take any point A on its circumby take any point A of its electric ference, draw a diameter AB, and from B draw B b perpendicular to AB. Make B b equal in length to half the circumference of the circle. Divide B b and the semi-circumference into the same number of equal parts, say six. From each point of division 1, 2, 3, etc., on the circumference draw lines to the centre C of the circle. Then draw 1 a perpendicular to C1;

Fig. 68. Since the perpendicular to C2; and so on. Make 1 a equal to  $bb_1$ ; 2 $a_2$  equal to  $bb_3$ ; 3 $a_3$  equal to  $bb_3$ ; 3 $a_3$  equal to  $bb_3$ ; and so on. Join the points A,  $a_1$ ,  $a_2$ ,  $a_3$ , etc., by a curve; this curve will be the required involute.

57. Method of plotting angles without using a protractor.—The radius of a circle whose circumference is 300 is 57.2 (more accurately 57.296). Striking a semicircle with a radius 57.3 by any scale, curately 51,220). Striking a semicircie with a radius 51.5 by any scale, spacers set to 10 by the same scale will divide the arc into 18 spaces of 10<sup>5</sup> each, and intermediates can be measured indirectly at the rate of 1 by scale for each 1<sup>5</sup>, or interpolated by eye according to the degree of accuracy required. The following table shows the chords to the above-mentioned radius, for every 10 degrees from 0° up to 110°. By means of one of these,

Angle.	Chord.	Angle.	Chord.
1°	0.999	60°	57,296
10°	9.988	70°	65,727
20°		80°	73.658
30°		90°	81.029
40°		100°	87.782
50°	48.429	110°	93.869

a 10° point is fixed upon the paper next less than the required angle, and the remainder is laid off at the rate of 1 by scale for each degree.

### GEOMETRICAL PROPOSITIONS.

In a right-angled triangle the square on the hypothenuse is equal to the sum of the squares on the other two sides.

If a triangle is equilateral, it is equiangular, and vice versa.

If a straight line from the vertex of an isosceles triangle bisects the base, it bisects the vertical angle and is perpendicular to the base.

If one side of a triangle is produced, the exterior angle is equal to the sum of the two interior and opposite angles. If two triangles are mutually equiangular, they are similar and their

corresponding sides are proportional.

If the sides of a polygon are produced in the same order, the sum of the

exterior angles equals four right angles. In a quadrilateral, the sum of the interior angles equals four right angles.

In a parallelogram, the opposite sides are equal; the opposite angles are equal; it is bisected by its diagonal; and its diagonals bisect each other

If three points are not in the same straight line, a circle may be passed through them.

If two arcs are intercepted on the same circle, they are proportional to the corresponding angles at the centre.

If two arcs are similar, they are proportional to their radii.

The areas of two circles are proportional to the squares of their radii. If a radius is perpendicular to a chord, it bisects the chord and it bisects the arc subtended by the chord.

A straight line tangent to a circle meets it in only one point, and it is

perpendicular to the radius drawn to that point.

If from a point without a circle tangents are drawn to touch the circle, there are but two; they are equal, and they make equal angles with the chord joining the tangent points.

If two lines are parallel chords or a tangent and parallel chord, they intercept equal arcs of a circle.

If an angle at the circumference of a circle, between two chords, is subtended by the same arc as an angle at the centre, between two radii, the angle at the circumference is equal to half the angle at the centre,

If a triangle is inscribed in a semicircle, it is right-angled.

If an angle is formed by a tangent and chord, it is measured by one half
of the arc intercepted by the chord; that is, it is equal to half the angle at the centre subtended by the chord.

If two chords intersect each other in a circle, the rectangle of the seg-

ments of the one equals the rectangle of the segments of the other.

And if one chord is a diameter and the other perpendicular to it, the rectangle of the segments of the diameter is equal to the square on half the other chord, and the half chord is a mean proportional between the segments of the diameter.

# MENSURATION.

### PLANE SURFACES.

Quadrilateral. - A four-sided figure.

Parallelogram.—A quadrilateral with opposite sides parallel.
Varieties.—Square: four sides equal, all angles right angles. Rectangle: opposite sides equal, all angles right angles. Rhombus: four sides equal, opposite angles equal, angles not right angles. Rhomboid: opposite sides equal, opposite angles equal, angles not right angles.

Trapezium.—A quadrilateral with unequal sides.

Trapezidi.—A quadrilateral with only one pair of opposite sides

paraliel.

Diagonal of a square =  $\sqrt{2 \times \text{side}^2} = 1.4142 \times \text{side}$ .

Diagonal of a rectangle = 1/product of two adjacent sides.

Area of any parallelogram = base x altitude.

Area of rhombus or rhomboid = product of two adjacent sides x sine of angle included between them.

Area of a trapezium = half the product of the diagonal by the sum

of the perpendiculars let fall on it from opposite angles.

Area of a trapezoid = product of half the sum of the two parallel

sides by the perpendicular distance between them.

To find the area of any quadrilateral figure.—Divide the quadrilateral into two triangles; the sum of the areas of the triangles is the

Or, multiply half the product of the two diagonals by the sine of the angle

at their intersection.

To find the area of a quadrilateral inscribed in a circle.

From half the sum of the four sides subtract each side severally; multiply the four remainders together; the square root of the product is the area. Triangle.-A three-sided plane figure.

Varieties.-Right-angled, having one right angle; obtuse-angled, having one obtuse angle; isosceles, having two equal angles and two equal sides;

equilateral, having three equal sides and equal angles.

The sum of the three angles of every triangle = 180°.

The two acute angles of a right-angled triangle are complements of each other. Hypothenuse of a right-angled triangle, the side opposite the right angle,

= 4/sum of the squares of the other two sides.

To find the area of a triangle:

RULE 1. Multiply the base by half the altitude. RULE 2. Multiply half the product of two sides by the sine of the included

angle. RULE 3. From half the sum of the three sides subtract each side severally; multiply together the half sum and the three remainders, and extract the

square root of the product. The area of an equilateral triangle is equal to one fourth the square of one

of its sides multiplied by the square root of 3,  $=\frac{a^2\sqrt{3}}{4}$ , a being the side; or

 $a^2 \times .433013$ .

Hypothenuse and one side of right-angled triangle given, to find other side, Required side = √hyp2 - given side2.

If the two sides are equal, side = hyp  $\div$  1.4142; or hyp  $\times$  .7071. Area of a triangle given, to find base: Base = twice area + perpendicular

height. Area of a triangle given, to find height: Height = twice area + base. Two sides and base given, to find perpendicular height (in a triangle in

which both of the angles at the base are acute). Rule.—As the base is to the sum of the sides, so is the difference of the sides to the difference of the divisions of the base made by drawing the perpendicular. Half this difference being added to or subtracted from half the base will give the two divisions thereof. As each side and its opposite division of the base constitutes a right-angled triangle, the perpendicular is ascertained by the rule perpendicular = Vhyp2 - base2.

Polygon. - A plane figure having three or more sides. Regular or irregular, according as the sides or angles are equal or unequal. Polygons

are named from the number of their sides and angles.

To find the area of an irregular polygon.-Draw diagonals dividing the polygon into triangles, and find the sum of the areas of these triangles.

To find the area of a regular polygon:

RUE.—Multiply the length of a side by the perpendicular distance to the centre; multiply the product by the number of sides, and divide it by 2. Or, multiply half the perimeter by the perpendicular let fall from the centre on one of the sides.

The perpendicular from the centre is equal to half of one of the sides of the polygon multiplied by the cotangent of the angle subtended by the half side.

The angle at the centre = 360° divided by the number of sides.

TABLE OF REGULAR POLYGONS

THE OF THE OFFICE TO SECOND.										
	ono.		cums	s of Cir- cribed rcle.	ibed = 1.	, Ra- msc.	dî	Ad-		
Sides.	Name of Polygon.	Side = 1.	from s = 1.	1.	of Inscribed e, Side = 1.	of Side, Rao of Circumsc, e = 1.	Angle at Centre.	Angle between jacent Sides.		
No. of S	Tame o	Area, S	Perpen, from Centre = 1.	Side =	Radius o	Length dius o Circle	ngle a	ngle b		
Z		< 4	Д.	<i>0</i> 2	<b>H</b>	H		⋖		
3	Triangle	.4330127	2.	.5773	.2887	1.739	1200	60°		
5	Square Pentagon	1. 1.7204774	1.414 1.238	.7071	.5	1.4142 1.1756	90 72	90 108		
6	Hexagon	2 5980762	1.156	1.	.866	1.	60	120		
7	Heptagon	3.6339124	1.11	1.1524	1.0383	.8677	51 26'	128 4-7		
8	Octagon	4.8284271	1.083	1.3066	1.2071	.7653	45	135		
10	Nonagon Decagon	6.1818242 7.6942088	1.064	1.4619 1.618	1.3737	.684	40 36	140 144		
11	Undecagon	9.3656399	1.042	1.7747	1.7028	.5634	32 43'	147 3-11		
12	Dodecagon	11.1961524	1.037	1.9319	1.866	.5176	30	150		
				•	i					

To find the area of a regular polygon, when the length of a side only is given:

RULE—Multiply the square of the side by the multiplier opposite to the name of the polygon in the table.

To find the area of an ir-

regular figure (Fig. 69).-Draw ordinates across its breadth at equal distances apart, the first and the last ordinate each being one half space from the ends of the figure. Find the average breadth by adding together the lengths of these lines included between the boundaries of the figure, and divide by the number of the lines added; multiply this mean breadth by the length. The greater the number Fig. 69.

of lines the nearer the approximation. In a figure of very irregular outline, as an indicator diagram from a high-speed steam-engine, mean lines may be substituted for the actual lines of the figure, being so traced as to intersect the undulations, so that the total area of the spaces cut off may be compensated by that of the extra spaces inclosed.

2d Method: The Trapezoidal Rule. — Divide the figure into any sufficient number of equal parts; add half the sum of the two end ordinates to the sum of all the other ordinates; divide by the number of spaces (that is, one less than the number of ordinates) to obtain the mean ordinate, and

one less than the number of ordinates, we obtain the free multiply this by the length to obtain the area.

3d Method: Surpson's Rules.—Divide the length of the figure into any even number of equal parts, at the common distance D apart, and draw ordinates through the points of division to touch the boundary lines. Add together, the first and last ordinates and call the sum A; add together the even ordinates and call the sum B; add together the odd ordinates, except the first and last, and call the sum C. Then,

area of the figure = 
$$\frac{A+4B+2C}{3} \times D$$
.

4th Method: Durand's Rule .- Add together 4/10 the sum of the first and last ordinates, 1 1/10 the sum of the second and the next to the last (or the penultimates), and the sum of all the intermediate ordinates. Multiply the sum thus gained by the common distance between the ordinates to obtain the area, or divide this sum by the number of spaces to obtain the mean ordinate.

Prof. Durand describes the method of obtaining his rule in Engineering News, Jan. 18, 1894. He claims that it is more accurate than Simpson's rule, and practically as simple as the trapezoidal rule. He thus describes its application for approximate integration of differential equations. Any defi-nite integral may be represented graphically by an area. Thus, let

$$Q = \int u \, dx$$

be an integral in which u is some function of x, either known or admitting of computation or measurement. Any curve plotted with x as abscissa and u as ordinate will then represent the variation of u with x, and the area between such curve and the axis X will represent the integral in question, no matter how simple or complex may be the real nature of the function u,

Substituting in the rule as above given the word "volume" for "area" and the word "section" for "ordinate," it becomes applicable to the determination of volumes from equidistant sections as well as of areas from

equidistant ordinates.

Having approximately obtained an area by the trapezoidal rule, the area by Durand's rule may be found by adding algebraically to the sum of the ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the end ordinates used in the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, half the sum of the trapezoidal rule (that is, nates + sum of the other ordinates) 1/10 of (sum of penultimates - sum of first and last) and multiplying by the common distance between the other ordinates

5th Method.-Draw the figure on cross-section paper. Count the number of squares that are entirely included within the boundary; then estimate of squares that are entirely included within the boundary; then estimate the fractional parts of squares that are cut by the boundary, add together these fractions, and add the sum to the number of whole squares. The result is the area in units of the dimensions of the squares. The finer the

ruling of the cross-section paper the more accurate the result.

6th Method.—Use a planimeter.

7th Method.—With a chemical balance, sensitive to one milligram, draw the figure on paper of uniform thickness and cut it out carefully; weigh the piece cut out, and compare its weight with the weight per square inch of the paper as tested by weighing a piece of rectangular shape.

#### THE CIRCLE.

Circumference = diameter × 3.1416, nearly; more accurately, 3.14159265359. Approximations,  $\frac{22}{7} = 3.143$ ;  $\frac{355}{113} = 3.1415929$ .

The ratio of circum, to diam, is represented by the symbol  $\pi$  (called Pi),

Multiples of π.	Multiples of $\frac{\pi}{4}$ .
$1\pi = 3.14159265359$	$\frac{1}{4}\pi = .7853982$
$2\pi = 6.28318530718$	" × 2 = 1.5707963
$3\pi = 9.42477796077$	" × 3 = 2.3561945
$4\pi = 12.56637061436$	" × 4 = 3.1415927
$5\pi = 15.70796326795$	" × 5 = 3.9269908
$6\pi = 18.84955592154$	" × 6 = 4.7123890
$7\pi = 21.99114857513$	" × 7 = 5.4977871
$8\pi = 25.13274122872$	" × 8 = 6.2831853
$9\pi = 28.27433388231$	" × 9 = 7.0685835

Ratio of diam. to circumference = reciprocal of 
$$\pi = 0.3183099$$
.

Reciprocal of  $\frac{1}{4}\pi = 1.27324$ .

$$\frac{7}{\pi} = 2.22817$$
Multiples of  $\frac{1}{\pi}$ .

$$\frac{8}{\pi} = 2.54648$$

$$\frac{1}{\pi} = .31831$$

$$\frac{9}{\pi} = 2.86479$$

$$\frac{360}{\pi} = 0.0087266$$

$$\frac{1}{\pi} = .63662$$

$$\frac{10}{\pi} = 3.18310$$

$$\frac{3}{\pi} = .95493$$

$$\frac{12}{\pi} = 3.81972$$

$$\frac{4}{\pi} = 1.27324$$

$$\frac{1}{2}\pi = 1.570796$$

$$\frac{5}{\pi} = 1.59155$$

$$\frac{1}{3}\pi = 1.047197$$

$$\frac{1}{6}\pi = 0.523599$$
Log  $\pi = 0.49714987$ 

Diam. in ins. =  $13.5405 \, \text{Varea in sq. ft.}$ Area in sq. ft. =  $(\text{diam. in inches})^2 \times .0054542$ . D = diameter, R = radius, C = circumference,

$$C = \pi D; = 2\pi R; = \frac{4A}{D}; = 2\sqrt{\pi A}; = 3.545\sqrt{A};$$

$$A = D^2 \times .7854; = \frac{CR}{2}; = 4R^2 \times .7854; = \pi R^2; = \frac{1}{4}\pi D^2; = \frac{C^2}{4\pi}; = .07958C^2; = \frac{CD}{4}.$$

$$D = \frac{C}{\pi}; = 0.31831C; = 2\sqrt{\frac{A}{\pi}}; = 1.12838\sqrt{A};$$

$$D = \frac{C}{\pi}; = 0.316310; = \frac{V}{\pi}; = 1.12636 VA;$$

$$R = \frac{C}{2\pi}; = 0.159155C; = \sqrt{\frac{A}{\pi}}; = 0.564189 V\overline{A}.$$

Areas of circles are to each other as the squares of their diameters.

To find the length of an arc of a circle:
RULE 1. As 360 is to the number of degrees in the arc, so is the circumference of the circle to the length of the arc.

RULE 2. Multiply the diameter of the circle by the number of degrees in the arc, and this product by 0.0087266,

# Relations of Arc, Chord, Chord of Half the Arc, Versed Sine, etc.

Let R = radius. D = diameter.Arc = length of arc.Cd =chord of the arc. ch =chord of half the arc.

 $V = \text{versed sine}, \quad D - V = \text{diam. minus ver. sin.}$ 

$$Arc = \frac{8ch - Cd}{3}$$
 (very nearly),  $= \frac{\sqrt{Cd^2 + 4V^2} \times 10V^2}{15Cd^2 + 33V^2} + 2ch$ , nearly.

$$Arc = \frac{2ch \times 10V}{60D - 27V} + 2ch$$
, nearly.

Chord of the arc =  $2\sqrt{ch^2 - V^2}$ ; =  $\sqrt{D^2 - (D - 2V)^2}$ ; = 8ch - 3Arc.

$$=2\sqrt{R^2-(R-V)^2}; = 2\sqrt{(D-V)} \times V.$$

Chord of half the arc,  $ch = \frac{1}{2} \sqrt{Cd^2 + 4V^2}$ ;  $= \sqrt{D \times V}$ ;  $= \frac{3Arc + Cd}{c}$ .

 $=\frac{ch^2}{2}$ ;  $=\frac{\left(\frac{1}{2}Cd\right)^2+V^2}{2}$ ; Diameter

 $=\frac{ch^2}{D}$ ;  $=\frac{1}{2}(D-\sqrt{D^2-Cd^2})$ Versed sine

(or 
$$\frac{1}{2}(D+\sqrt{D^2-Cd^2})$$
, if  $V$  is greater than radius. 
$$=\sqrt{ch^2-\frac{Cd^2}{cd}}.$$

Half the chord of the arc is a mean proportional between the versed sine and diameter minus versed sine:

$$\frac{1}{2}Cd = \sqrt{V \times (D - V)}.$$

Length of a Circular Arc.—Huyghens's Approximation. Let C represent the length of the chord of the arc and c the length of the arc hord of half the arc; the length of the arc

$$L = \frac{8c - C}{3}.$$

Professor Williamson shows that when the arc subtends an angle of 30°, the radius being 100,000 feet (nearly 19 miles), the error by this formula is about two inches, or 1/600000 part of the radius. When the length of the arc is equal to the radius, i.e., when it subtends an angle of 57°.3, the error is less than 1/7880 part of the radius. Therefore, if the radius is 100,000 feet, the error is less than  $\frac{100000}{7680} = 13$  feet. The error increases rapidly with the

jucrease of the angle subtended.

In the measurement of an arc which is described with a short radius the error is so small that it may be neglected. Describing an arc with a radius of 12 inches subtending an angle of 30°, the error is 1/50000 of an inch. For 57°.3 the error is less than 0",0015.

In order to measure an arc when it subtends a large angle, bisect it and measure each half as before—in this case making B = length of the chord of half the arc, and b = length of the chord of one fourth the arc; then

$$L = \frac{16b - 2B}{3}.$$

## Relation of the Circle to its Equal, Inscribed, and Circumscribed Squares.

Diameter of circle  $\times$  .88623 = side of equal square. = 28209 = side of equal square.

Circumference of circle × 1.1284 = perimeter of equal square.

Diameter of circle × .7071 | Circumference of circle × .22508 | Area of circle × .90031 -- diameter = side of inscribed square. Area of circle × Area of circle × = area of circumscribed square. = area of inscribed square. 1.2732 .63662 Side of square × 1.4142 = diam. of circumscribed circle. 4.4428 = circum. .. " 1.1284 = diam, of equal circle. × " " 3.5449 = circum. Perimeter of square × 0.88623

1.2732 Square inches x = circular inches. Sectors and Segments.—To find the area of a sector of a circle. RULE 1. Multiply the arc of the sector by half its radius. RULE 2. As 360 is to the number of degrees in the arc, so is the area of

the circle to the area of the sector.

Rule 3. Multiply the number of degrees in the arc by the square of the

radius and by .008727.

To find the area of a segment of a circle; Find the area of the sector which has the same arc, and also the area of the triangle formed by the chord of the segment and the radii of the sector.

Then take the sum of these areas, if the segment is greater than a semicircle, but take their difference if it is less.

Another Method: Area of segment  $=\frac{R}{2}$  (arc  $-\sin A$ ) in which A is the central angle, R the radius, and arc the length of arc to radius 1.

To find the area of a segment of a circle when its chord and height or

versed sine only are given. First find radius, as follows:

radius = 
$$\frac{1}{2} \left[ \frac{\text{square of half the chord}}{\text{height}} + \text{height} \right]$$
.

2. Find the angle subtended by the arc, as follows: half chord = sine of half the angle. Take the corresponding angle from a table of sines, and double it to get the angle of the arc.

3. Find area of the sector of which the segment is a part;

area of sector = area of circle 
$$\times \frac{\text{degrees of are}}{360}$$

4. Subtract area of triangle under the segment:

Area of triangle = 
$$\frac{\text{chord}}{2}$$
 × (radius - height of segment).

The remainder is the area of the segment.

When the chord, are, and diameter are given, to find the area. From the length of the arc subtract the length of the chord. Multiply the remainder by the radius or one-half diameter; to the product add the chord multiplied by the height, and divide the sum by 2.

Another rule: Multiply the chord by the height and this product by .6834

plus one tenth of the square of the height divided by the radius.

To find the chord: From the diameter subtract the height; multiply the remainder by four times the height and extract the square root,

When the chords of the arc and of half the arc and the versed sine are given: To the chord of the arc add four thirds of the chord of half the arc;

given: To the chord of the are add four thirds of the chord of half the arc; multiply the sum by the versed sine and the product by .4046 (approximate). **Circular Hing.**—To find the area of a ring included between the circumferences of two concentric circles: Take the difference between the area of the two circles; or, subtract the square of the less radius from the square of the greater, and multiply their difference by 3.14159. The area of the greater circle is equal to  $\pi R^2$ ; and the area of the smaller,  $(P^2 - \pi^2)^2$ .

Their difference, or the area of the ring, is  $\pi(R^2-r^2)$ . The Ellipse. - Area of an ellipse = product of its semi-axes x 3.14159 = product of its axes x .785398.

The Ellipse,—Circumference (approximate) = 3.1416  $\sqrt{\frac{D^2 + \overline{d^2}}{2}}$ , D and d

being the two axes. Trautwine gives the following as more accurate: When the longer axis D is not more than five times the length of the shorter axis, d,

Circumference = 3.1416 
$$\sqrt{\frac{D^2 + d^2}{2} - \frac{(D-d)^2}{8.8}}$$
.

When D is more than 5d, the divisor 8.8 is to be replaced by the following divisors .

$$\frac{D}{d}$$
 = 6, 7, 8, 9, 10, 12, 14, 16, 18, 20, 30, 40, 50.

Divisor = 9, 9.2, 9.3, 9.35, 9.4, 9.5, 9.6, 9.68, 9.75, 9.8, 9.92, 9.98,

Reuleaux gives: Circumference = 
$$\pi (a + b) \left(1 + \frac{n^2}{4} + \frac{n^4}{64} + \frac{n^6}{256} + \ldots\right)$$
, in

which  $n = \frac{a-b}{a+b}$ , a and b being the semi-axes.

Area of a segment of an ellipse the base of which is parallel to one of the axes of the ellipse. Divide the height of the segment by the axis of which it is part, and find the area of a circular segment, in a table of circular segments, of which the height is equal to the quotient; multiply the area thus found by the product of the two axes of the ellipse. Cycloid.—A curve generated by the rolling of a circle on a plane.

Length of a cycloidal curve =  $4 \times$  diameter of the generating circle. Length of the base = circumference of the generating circle. Area of a cycloid = 3 x area of generating circle.

Helix (Screw).—A line generated by the progressive rotation of a point around an axis and equidistant from its centre.

Length of a helix.—To the square of the circumference described by the generating-point add the square of the distance advanced in one revolution, and take the square root of their sum multiplied by the number of revolutions of the generating point. Or,

$$\sqrt{(c^2+h^2)n} = \text{length}, n \text{ being number of revolutions.}$$

Spirals.—Lines generated by the progressive rotation of a point around a fixed axis, with a constantly increasing distance from the axis.

A plane spiral is when the point rotates in one plane.

A conical spiral is when the point rotates around an axis at a progressing distance from its centre, and advancing in the direction of the axis, as around

Length of a plane spiral line.-When the distance between the coils is uniform.

RULE .- Add together the greater and less diameters; divide their sum by multiply the quotient by 3.1416, and again by the number of revolutions.
 Or, take the mean of the length of the greater and less circumferences and multiply it by the number of revolutions.
 Or,

length = 
$$\pi n \frac{d+d'}{2}$$
,  $d$  and  $d'$  being the inner and outer diameters.

Length of a conical spiral line.—Add together the greater and less diameters; divide their sum by 2 and multiply the quotient by 3.1416. To the square of the product of this circumference and the number of revolutions of the spiral add the square of the height of its axis and take the square root of the sum.

Or, length = 
$$\sqrt{\left(\pi n \frac{d+d'}{2}\right)^2 + h^2}$$
.

# SOLID BODIES.

The Prism.-To find the surface of a right prism: Multiply the perimeter of the base by the altitude for the convex surface. To this add the areas of the two ends when the entire surface is required.

Volume of a prism = area of its base  $\times$  its altitude.

The pyramid.—Convex surface of a regular pyramid = perimeter of its base × half the slant height. To this add area of the base if the whole surface is required.

Volume of a pyramid = area of base × one third of the altitude.

To find the surface of a frustum of a regular pyramid; Multiply half the slant height by the sum of the perimeters of the two bases for the convex To this add the areas of the two bases when the entire surface is surface. required.

To find the volume of a frustum of a pyramid: Add together the areas of

the two bases and a mean proportional between them, and multiply the sum by one third of the altitude. (Mean proportional between two numbers

= square root of their product.)

Wedge. - A wedge is a solid bounded by five planes, viz.: a rectangular base, two trapezoids, or two rectangles, meeting in an edge, and two tri-angular ends. The altitude is the perpendicular drawn from any point in the edge to the plane of the base.

To find the volume of a wedge: Add the length of the edge to twice the length of the base, and multiply the sum by one sixth of the product of the

height of the wedge and the breadth of the base.

**Rectangular prismoid.**—A rectangular prismoid is a solid bounded by six planes, of which the two bases are rectangles, having their corresponding sides parallel, and the four upright sides of the solids are trape-

To find the volume of a rectangular prismoid: Add together the areas of the two bases and four times the area of a parallel section equally distant

from the bases, and multiply the sum by one sixth of the altitude.

Cylinder.-Convex surface of a cylinder = perimeter of base × altitude. To this add the areas of the two ends when the entire surface is required.

Volume of a cylinder = area of base  $\times$  altitude.  $Cone_{\bullet}$ -Convex surface of a cone = circumference of base  $\times$  half the slant

side. To this add the area of the base when the entire surface is required.

Volume of a cone = area of base  $\times \frac{1}{2}$  altitude.

To find the surface of a frustum of a cone: Multiply half the side by the sum of the circumferences of the two bases for the convex surface; to this add the areas of the two bases when the entire surface is required

To find the volume of a frustum of a cone: Add together the areas of the two bases and a mean proportional between them, and multiply the sum

by one third of the altitude.

**Sphere.**—To find the surface of a sphere; Multiply the diameter by the circumference of a great circle; or, multiply the square of the diameter by 3,14159,

Surface of sphere  $= 4 \times$  area of its great circle.

= convex surface of its circumscribing cylinder.

Surfaces of spheres are to each other as the squares of their diameters. To find the volume of a sphere: Multiply the surface by one third of the radius; or, multiply the cube of the diameter by 1/6\*; that is, by 0.5336. Value of \*\*\frac{1}{2}\* to 10 decimal places = .5235981756.

The volume of a sphere = 2/3 the volume of its circumscribing cylinder. Volumes of spheres are to each other as the cubes of their diameters.

Spherical triangle. - To find the area of a spherical triangle: Compute the surface of the quadrantal triangle, or one eighth of the surface of the sphere. From the sum of the three angles subtract two right angles; divide the remainder by 90, and multiply the quotient by the area of the quadrantal triangle.

Spherical polygon. - To find the area of a spherical polygon: Compute the surface of the quadrantal triangle. From the sum of all the angles subtract the product of two right angles by the number of sides less two; divide the remainder by 90 and multiply the quotient by the area of the quadrantal triangle.

The prismoid.—The prismoid is a solid having parallel end areas, and may be composed of any combination of prisms, cylinders, wedges, pyramids, or cones or frustums of the same, whose bases and apices lie in the

end areas.

Inasmuch as cylinders and cones are but special forms of prisms and pyramids, and warped surface solids may be divided into elementary forms of them, and since frustums may also be subdivided into the elementary forms, it is sufficient to say that all prismoids may be decomposed into prisms, wedges, and pyramids. If a formula can be found which is equally applicable to all of these forms, then it will apply to any combination of them. Such a formula is called

#### The Prismoidal Formula.

Let A = area of the base of a prism, wedge, or pyramid;  $A_1, A_2, A_m =$  the two end and the middle areas of a prismoid, or of any of its elementary solids:

h =altitude of the prismoid or elementary solid; V =its volume;

$$V = \frac{h}{6}(A_1 + 4A_m - A_2).$$

For a prism  $A_1$ ,  $A_m$  and  $A_2$  are equal,  $A_3$ ;  $V = \frac{h}{c} \times 6A = hA$ .

For a wedge with parallel ends,  $A_2 = 0$ ,  $A_m = \frac{1}{2}A_1$ ;  $V = \frac{h}{6}(A_1 + 2A_1) = \frac{hA}{2}$ .

For a cone or pyramid, 
$$A_2 = 0$$
,  $A_m = \frac{1}{4}A_1$ ;  $V = \frac{h}{6}(A_1 + A_1) = \frac{hA}{3}$ .

The prismoidal formula is a rigid formula for all prismoids. The only approximation involved in its use is in the assumption that the given solid may be generated by a right line moving over the boundaries of the end areas.

The area of the middle section is never the mean of the two end areas if the prismoid contains any pyramids or cones among its elementary forms. When the three sections are similar in form the dimensions of the middle area are always the means of the corresponding end dimensions. This fact often enables the dimensions, and hence the area of the middle section, to be computed from the end areas.

Polyedrons.—A polyedron is a solid bounded by plane polygons. A

regular polyedron is one whose sides are all equal regular polygons.

To find the surface of a regular polyedron.—Multiply the area of one of the faces by the number of faces; or, multiply the square of one of the edges by the surface of a similar solid whose edge is unity.

#### A TABLE OF THE REGULAR POLYEDRONS WHOSE EDGES ARE UNITY.

Names.	No. of Faces.	Surface.	Volume.
Tetraedron	4	1.7320508	0.1178513
Hexaedron	6	6.0000000	1.0000000
Octaedron	8	3.4641016	0.4714045
Dodecaedron	12	20.6457288	7.6631189
Icosaedron,	20	8.6602540	2.1816950

To find the volume of a regular polyedron. - Multiply the surface by one third of the perpendicular let fall from the centre on one of the faces; or, multiply the cube of one of the edges by the solidity of a

similar polyedron whose edge is unity.

Solid of revolution.—The volume of any solid of revolution is equal to the product of the area of its generating surface by the length of the path of the centre of gravity of that surface.

The convex surface of any solid of revolution is equal to the product of the perimeter of its generating surface by the length of path of its centre

Cylindrical ring.—Let d = outer diameter; d' = inner diameter;  $\frac{1}{2}(d-d')=$  thickness = t;  $\frac{1}{4}\pi$   $t^2=$  sectional area;  $\frac{1}{2}(d+d')=$  mean diameter = M;  $\pi t$  = circumference of section;  $\pi M$  = mean circumference of

ring; surface =  $\pi t \times \pi M$ ; =  $\frac{1}{4}\pi^2 (d^2 - d'^2)$ ; = 9.86965 t M; = 2.46741  $(d^2 - d'^2)$ ;

volume = 
$$\frac{1}{4}\pi t^2 M \pi$$
; = 2.46741 $t^2 M$ .

Spherical zone. - Surface of a spherical zone or segment of a sphere = its altitude x the circumference of a great circle of the sphere. A great

circle is one whose plane passes through the centre of the sphere.

For the sum of the squares of the radii of the ends add one third of the square of the height; multiply the sum

by the height and by 1.5708.

Spherical segment.-Volume of a spherical segment with one base.-

Multiply half the height of the segment by the area of the base, and the cube of the height by .5236 and add the two products. Or, from three times the diameter of the sphere subtract twice the height of the segment; multiply the difference by the square of the height and by 5236. Or, to three times the square of the radius of the base of the segment add the square of its height, and multiply the sum by the height and by .5236.

Spheroid or ellipsoid. - When the revolution of the spheroid is about the transverse diameter it is prolate, and when about the conjugate it is

Convex surface of a segment of a spheroid.—Square the diameters of the spheroid, and take the square root of half their sum; then, as the diameter from which the segment is cut is to this root so is the height of the segment to the proportionate height of the segment to the mean diameter. Multiply the product of the other diameter and 3,1416 by the proportionate

Convex surface of a frustum or zone of a spheroid.—Proceed as by previous rule for the surface of a segment, and obtain the proportionate height of the frustum. Multiply the product of the diameter parallel to the base of the frustum and 3,1416 by the proportionate height of the frustum.

Volume of a spheroid is equal to the product of the square of the revolving axis by the fixed axis and by .5236. The volume of a spheroid is two thirds

of that of the circumscribing cylinder,

Volume of a segment of a spheroid.—1. When the base is parallel to the revolving axis, multiply the difference between three times the fixed axis and twice the height of the segment, by the square of the height and by 5236. Multiply the product by the square of the revolving axis, and divide by the square of the fixed axis.

When the base is perpendicular to the revolving axis, multiply the difference between three times the revolving axis and twice the height of the segment by the square of the height and by .5236. Multiply the product by the length of the fixed axis, and divide by the length of the

revolving axis.

Volume of the middle frustum of a spheroid.—1. When the ends are circular, or parallel to the revolving axis: To twice the square of the middle diameter add the square of the diameter of one end; multiply the sum by the length of the frustum and by .2618

 When the ends are elliptical, or perpendicular to the revolving axis:
 To twice the product of the transverse and conjugate diameters of the middle section add the product of the transverse and conjugate diameters of one end; multiply the sum by the length of the frustum and by .2618

Spindles. - Figures generated by the revolution of a plane area, when the curve is revolved about a chord perpendicular to its axis, or about its double ordinate. They are designated by the name of the arc or curve from which they are generated, as Chrudar, Elliptic, Parabolic, etc., etc.

Convex surface of a circular spindle, zone, or segment of it -Rule: Multiply the length by the radius of the revolving are; multiply this are by the central distance, or distance between the centre of the spindle and centre of the revolving are; subtract this product from the former, double the remainder, and multiply it by 3,1416

Volume of a circular spindle.-Multiply the central distance by half the area of the revolving segment; subtract the product from one third of the

cube of half the length, and multiply the remainder by 12 5664.

Volume of frustum or zone of a circular spindle.—From the square of half the length of the whole spindle take one third of the square of half the length of the frustum, and multiply the remainder by the said half length of the frustum; multiply the central distance by the revolving area which generates the frustum; subtract this product from the former, and multiply the remainder by 6.2832.

Volume of a segment of a circular spindle.—Subtract the length of the segment from the half length of the spindle; double the remainder and ascertain the volume of a middle frustum of this length; subtract the

result from the volume of the whole spindle and halve the remainder, Volume of a cycloidal spindle = five eighths of the volume of the circumscribing cylinder.—Multiply the product of the square of twice the diameter of the generating circle and 3.927 by its circumference, and divide this pro-

duct by 8. Parabolic conoid. - Volume of a parabolic conoid (generated by the revolution of a parabola on its axis). - Multiply the area of the base by half the height,

Or multiply the square of the diameter of the base by the height and by 3927

Volume of a frustum of a parabolic conoid.—Multiply half the sum of

the areas of the two ends by the height.

Volume of a parabolic spindle (generated by the revolution of a parabola on its base).—Multiply the square of the middle diameter by the length and by .4189.

The volume of a parabolic spindle is to that of a cylinder of the same

height and diameter as 8 to 15.

Volume of the middle frustum of a parabolic spindle.—Add together 8 times the square of the maximum diameter, 3 times the square of the end diameter, and 4 times the product of the diameters. Multiply the sum by the length of the frustum and by .05236.

This rule is applicable for calculating the content of casks of parabolic

Casks.—To find the volume of a cask of any form.—Add together 39 times the square of the bung diameter, 25 times the square of the head diameter, and 26 times the product of the diameters. Multiply the sum by the length, and divide by 31,773 for the content in Imperial gallons, or by 26,470 for U. S. gallons.

This rule was framed by Dr. Hutton, on the supposition that the middle third of the length of the cask was a frustum of a parabolic spindle, and

each outer third was a frustum of a cone.

To find the ullage of a cask, the quantity of liquor in it when it is not full.

1. For a lying cask: Divide the number of wet or dry inches by the bung diameter in inches. If the quotient is less than 5, deduct from it one fourth part of what it wants of 5. If it exceeds .5, add to it one fourth part of the excess above 5. Multiply the remainder or the sum by the whole content of the cask. The product is the quantity of liquor in the cask, in gallons, when the dividend is wet inches; or the empty space, if dry inches.

2. For a standing cask: Divide the number of wet or dry inches by the length of the cask. If the quotient exceeds .5, add to it one tenth of its excess above .5; if less than .5, subtract from it one tenth of what it wants of .5. Multiply the sum or the remainder by the whole content of the cask. The product is the quantity of liquor in the cask, when the dividend is wet

inches; or the empty space, if dry inches.

Volume of cask (approximate) U. S. gallons = square of mean diam.

× length in inches × .0034. Mean diam. = half the sum of the bung and

head diams.

Volume of an irregular solid.—Suppose it divided into parts, resembling prisms or other bodies measurable by preceding rules. Find the content of each part; the sum of the contents is the cubic contents of the solid.

The content of a small part is found nearly by multiplying half the sum of the areas of each end by the perpendicular distance between them.

The contents of small irregular solids may sometimes be found by immersing them under water in a prismatic or cylindrical vessel, and observing the amount by which the level of the water descends when the solid is

withdrawn. The sectional area of the vessel being multiplied by the descent of the level gives the cubic contents. Or, weigh the solid in air and in water; the difference is the weight of water it displaces. Divide the weight in pounds by 62.4 to obtain volume in

water it displaces. Divide the weight in points by 0.3 to obtain the cubic feet, or multiply it by 27.7 to obtain the volume in cubic inches. When the solid is very large and a great degree of accuracy is not requisite, measure its length, breadth, and depth in several (ifferent places, and take the mean of the measurement for each dimension, and

multiply the three means together.

When the surface of the solid is very extensive it is better to divide it into triangles, to find the area of each triangle, and to multiply it by the mean depth of the triangle for the contents of each triangular portion; the contents of the triangular sections are to be added together.

The mean depth of a triangular section is obtained by measuring the depth at each angle, adding together the three measurements, and taking

one third of the sum.

## PLANE TRIGONOMETRY.

### Trigonometrical Functions.

Every triangle has six parts—three angles and three sides. When any three of these parts are given, provided one of them is a side, the other parts may be determined. By the solution of a triangle is meant the determination of the unknown parts of a triangle when certain parts are given. The complement of an angle or arc is what remains after subtracting the

angle or arc from 90°.

In general, if we represent any arc by A, its complement is  $90^{\circ} - A$ . Hence the complement of an arc that exceeds  $90^{\circ}$  is negative. Since the two acute angles of a right angled triangle are together equal to a right angle, each of them is the complement of the other.

The supplement of an angle or are is what remains after subtracting the angle or are from 180°. If A is an arc its supplement is  $180^{\circ} - A$ . The supplement of an arc that exceeds 180° is negative.

The sum of the three angles of a triangle is equal to 180°. Either angle is the supplement of the other two. In a right-angled triangle, the right angle

the suppenient of the other two. In a right-angled triangle, the right angle being equal to 90°, each of the acute angles is the complement of the other. In all right-angled triangles having the same acute angle, the sides have to each other the same ratio. These ratios have received special names, as follows:

If A is one of the acute angles, a the opposite side, b the adjacent side, and c the hypothenuse.

The sine of the angle A is the quotient of the opposite side divided by the hypothenuse. Sin.  $A = \frac{a}{a}$ 

The tangent of the angle A is the quotient of the opposite side divided by the adjacent side. Tang.  $A = \frac{a}{b}$ 

The secant of the angle A is the quotient of the hypothenuse divided by the adjacent side. Sec.  $A = \frac{1}{2}$ 

The cosine, cotangent, and cosecant of an angle are respectively the sine, taugent, and secant of the complement of that angle. The

terms sine, cosine, etc., are called trigonometrical functions.

In a circle whose radius is unity. the sine of an arc, or of the angle at the centre measured by that arc, is the perpendicular let fall from one extremity of the arc upon the diam-ter passing through the other catremity.

The tangent of an arc is the line which touches the circle at one extremity of the arc, and is limited by the diameter (produced) passing through the other extremity.

• The secant of an arc is that part of the produced diameter which is intercepted between the centre and the tangent.

The versed sine of an arc is that part of the diameter intercepted between the extremity of the arc and the foot of the sine.

In a circle whose radius is not unity, the trigonometric functions of an are will be equal to the lines here defined, divided by the radius of the circle. If ICA (Fig. 70) is a nagle in the first quadrant, and CF = radius, The sine of the angle  $=\frac{FG}{Rad}$ .  $Cos = \frac{CG}{Rad} = \frac{KF}{Rad}$ .

Tang. =  $\frac{IA}{\text{Rad}}$ . Secant =  $\frac{CI}{\text{Rad}}$ . Cot. =  $\frac{DL}{\text{Rad}}$ .

Cosec. =  $\frac{CL}{\text{Rad}}$ . Versin, =  $\frac{GA}{\text{Rad}}$ .

sin arc FA.

If radius is 1, then Rad. in the denominator is omitted, and sine = FG, etc.

The sine of an arc = half the chord of twice the

The sine of the supplement of the arc is the same M as that of the arc itself. Sine of arc BDF = FG =



Fig. 70.

The tangent of the supplement is equal to the tangent of the arc, but with a contrary sign. Tang. B D F = B M. The secant of the supplement is equal to the secant of the arc, but with a

The secant of the supplement is equal to the secant or the arc, but with a contrary sign. Sec. B D F = C M.

Signs of the functions in the four quadrants,—If we divide a circle into four quadrants by a vertical and a horizontal diameter, the upper right-hand quadrant is called the first, the upper left the second, the lower left the third, and the lower right the fourth. The signs of the functions in the four quadrants are as follows:

First quad, Second quad, Third quad, Fourth quad,

The values of the functions are as follows for the angles specified:

Angle	0	30	° 45	60	90	120	135	° 150	180	270	5 360
Sine	0	1/2	$\frac{1}{\sqrt{2}}$	$\frac{\sqrt{3}}{2}$	1	$\frac{\sqrt{3}}{2}$	$\frac{1}{\sqrt{2}}$	1 2	0	1	0
Cosine	1	$\frac{\sqrt[4]{3}}{2}$	$\frac{1}{\sqrt{2}}$	$\frac{1}{2}$	0	$-\frac{1}{2}$	$-\frac{1}{\sqrt{2}}$	$-\frac{\sqrt{3}}{2}$	-1	0	1
Tangent	0	$\frac{1}{\sqrt{3}}$	1	1/3		<b>-</b> √3	-1	$-\frac{1}{\sqrt{3}}$	0	8	0
Cotangent	œ	7.3	1	$\frac{1}{\sqrt{3}}$	0	$-\frac{1}{\sqrt{3}}$	- 1	- 1/3	oc	0	œ
Secant	1	$\frac{2}{\sqrt{3}}$	√2	2	œ	- 2	- V 2	$-\frac{2}{\sqrt{3}}$	-1	œ	1
Cosecant	œ		1√2	$\frac{2}{\sqrt{3}}$	1	$\frac{2}{\sqrt{3}}$	1/2	2	co.	-1	œ
Versed sine	0	$\frac{2-\sqrt{3}}{2}$	$\frac{\sqrt{2}-1}{\sqrt{2}}$	$\frac{1}{2}$	1	3 2	$\frac{\sqrt{2}+1}{\sqrt{2}}$	$\frac{2+\sqrt{8}}{2}$	2	1	2
											1

#### TRIGONOMETRICAL FORMULÆ.

The following relations are deduced from the properties of similar triangles (Radius = 1):

$$\cos A : \sin A :: 1 : \tan A, \text{ whence } \tan A = \frac{\sin A}{\cos A};$$

$$\sin A : \cos A :: 1 : \cot A, \quad \cot A = \frac{\cos A}{\sin A};$$

$$\cos A :: 1 \quad :: 1 : \sec A, \quad \sec A = \frac{1}{\cos A};$$

$$\sin A :: 1 \quad :: 1 : \csc A, \quad \csc A = \frac{1}{\sin A};$$

$$\tan A :: 1 \quad :: 1 : \cot A \quad \cot A = \frac{1}{\cot A};$$

The sum of the square of the sine of an arc and the square of its cosine equals unitv. Sin<sup>2</sup>  $A + \cos^2 A = 1$ . Formulæ for the functions of the sum and difference of

two angles:

Let the two angles be denoted by A and B, their sum A + B = C, and their difference A - B by D.

$$\cos A + B = \cos A \cos B - \sin A \sin B; \dots (2)$$
  
$$\sin (A - B) = \sin A \cos B - \cos A \sin B; \dots (3)$$

$$\cos(A - B) = \cos A \cos B + \sin A \sin B. \qquad (4)$$

From these four formulæ by addition and subtraction we obtain

$$\sin (A + B) + \sin (A - B) = 2 \sin A \cos B;$$
 . . . . . (5)

$$\sin (A + B) - \sin (A - B) = 2\cos A \sin B;$$
 . . . . . (6)

$$\cos (A + B) + \cos (A - B) = 2 \cos A \cos B; \dots (7)$$

$$\cos(A - B) - \cos(A + B) = 2\sin A \sin B$$
. . . . . (8)

If we put A+B=C, and A-B=D, then  $A=\frac{1}{2}(C+D)$  and  $B=\frac{1}{2}(C-D)$ , and we have

$$\sin C + \sin D = 2 \sin \frac{1}{2}(C + D) \cos \frac{1}{2}(C - D);$$
 (9)

$$\sin C - \sin D = 2 \cos \frac{1}{6}(C+D) \sin \frac{1}{6}(C-D); \dots (10)$$

$$\cos C + \cos D = 2\cos\frac{1}{2}(C+D)\cos\frac{1}{2}(C-D);$$
 . . . (11)

$$\cos D - \cos C = 2 \sin \frac{1}{5} (C + D) \sin \frac{1}{5} (C - D).$$
 (12)

Equation (9) may be enunciated thus: The sum of the sines of any two angles is equal to twice the sine of half the sum of the angles multiplied by the cosine of half their difference. These formulæ enable us to transform

a sum or difference into a product.

The sum of the sines of two angles is to their difference as the tangent of half the sum of those angles is to the tangent of half their difference.

$$\frac{\sin A + \sin B}{\sin A - \sin B} = \frac{2 \sin \frac{1}{2}(A + B)\cos \frac{1}{2}(A - B)}{2 \cos \frac{1}{2}(A + B)\sin \frac{1}{2}(A - B)} = \frac{\tan \frac{1}{2}(A + B)}{\tan \frac{1}{2}(A - B)}.$$
 (13)

The sum of the cosines of two angles is to their difference as the cotangent of half the sum of those angles is to the tangent of half their difference.

$$\frac{\cos A + \cos B}{\cos B - \cos A} = \frac{2 \cos \frac{1}{2}(A+B) \cos \frac{1}{2}(A-B)}{2 \sin \frac{1}{2}(A+B) \sin \frac{1}{2}(A-B)} = \frac{\cot \frac{1}{2}(A+B)}{\tan \frac{1}{2}(A-B)}.$$
 (14)

The sine of the sum of two angles is to the sine of their difference as the sum of the tangents of those angles is to the difference of the tangents.

$$\frac{\sin (A+B)}{\cos A \cos B} = \tan A + \tan B; \qquad \tan (A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}; \qquad \tan (A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}; \qquad \tan (A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B + \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B + \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B + 1}{\cot B - \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B + 1}{\cot B - \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B + 1}{\cot B - \cot A}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A \cot B - 1}{\cot B - \cot B}; \qquad \cot (A+B) = \frac{\cot A - \tan B}{\cot A - \tan B}; \qquad \cot (A+B) = \frac{\cot A - \tan B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot B}{\cot A - \cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot A - \cot A}{\cot A}; \qquad \cot (A+B) = \frac{\cot$$

#### Solution of Plane Right-angled Triangles.

Let A and B be the two acute angles and C the right angle, and a, b, and c the sides opposite these angles, respectively, then we have

1. 
$$\sin A = \cos B = \frac{a}{c}$$
; 3.  $\tan A = \cot B = \frac{a}{b}$ ;  
2.  $\cos A = \sin B = \frac{b}{c}$ ; 4.  $\cot A = \tan B = \frac{b}{a}$ .

1. In any plane right-angled triangle the sine of either of the acute angles is equal to the quotient of the opposite leg divided by the hypothenuse.

2. The cosine of either of the acute angles is equal to the quotient of the adjacent leg divided by the hypothenuse.

3. The tangent of either of the acute angles is equal to the quotient of the opposite leg divided by the adjacent leg.

4. The cotangent of either of the acute angles is equal to the quotient of

the adjacent leg divided by the opposite leg. 5. The square of the hypothenuse equals the sum of the squares of the other two sides.

# Solution of Oblique-angled Triangles.

The following propositions are proved in works on plane trigonometry. In

any plane triangle—

Theorem 1. The sines of the angles are proportional to the opposite sides.

Theorem 2. The sum of any two sides is to their difference as the tangent of half the sum of the opposite angles is to the tangent of half their difference.

Theorem 3. If from any angle of a triangle a perpendicular be drawn to the opposite side or base, the whole base will be to the sum of the other two sides as the difference of those two sides is to the difference of the segments of the base.

CASE I. Given two angles and a side, to find the third angle and the other two sides. 1. The third angle = 180° - sum of the two angles. 2. The sides may be found by the following proportion:

The sine of the angle opposite the given side is to the sine of the angle opposite the required side as the given side is to the required side.

Case II. Given two sides and an angle opposite one of them, to find the

third side and the remaining angles.

The side opposite the given angle is to the side opposite the required angle

as the sine of the given angle is to the sine of the required angle.

The third angle is found by subtracting the sum of the other two from 180°, and the third side is found as in Case I.

Case III. Given two sides and the included angle, to find the third side and

the remaining angles.

The sum of the required angles is found by subtracting the given angle from 180°. The difference of the required angles is then found by Theorem II. Half the difference added to half the sum gives the greater angle, and half the difference subtracted from half the sum gives the less angle. The third side is then found by Theorem I.

Another method

Given the sides c, b, and the included angle A, to find the remaining side aand the remaining angles B and C.

From either of the unknown angles, as B, draw a perpendicular B e to the opposite side. Then

$$Ae = c \cos A$$
,  $Be = c \sin A$ ,  $eC = b - Ae$ ,  $Be \div eC = \tan C$ .

Or, in other words, solve Be, Ae and Be Cas right-angled triangles.

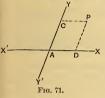
CASE IV. Given the three sides, to find the angles.

Let fall a perpendicular upon the longest side from the opposite angle, dividing the given triangle into two right-angled triangles. The two segments of the base may be found by Theorem III. There will then be given the hypothenuse and one side of a right-angled triangle, to find the angles.

For areas of triangles, see Mensuration.

### ANALYTICAL GEOMETRY.

Analytical geometry is that branch of Mathematics which has for its object the determination of the forms and magnitudes of geometrical magnitudes by means of analysis.



Ordinates and abscissas.—In analytical geometry two intersecting lines YY', XX' are used as coordinate axes, XX' being the axis of abscissas or axis of X, and YY' the axis of ordinates or axis of Y. A, the intersection, is called the origin of coördinates. The distance of any point P from the axis of Y measured parallel to the axis of the axis of Y measures parallel to the axis of X is called the abscissa of the point, as AD or CP, Fig. 71. Its distance from the axis of X, measured parallel to the axis of Y, is called the ordinate, as AC or PD. The abscissa and ordinate taken together are called the coordinates of the point P. The angle of intersection to avoid the coordinate and the coordinates of the point P. The angle of intersection to avoid the coordinate and the coordinates of the point P. tion is usually taken as a right angle, in which case the axes of X and Y are called rectangu-

The abscissa of a point is designated by the letter x and the ordinate by y.

The equations of a point are the equations which express the distances of

the point from the axis. Thus x = a, y = b are the equations of the point P. **Equations referred to rectangular coördinates.**—The equation of a line expresses the relation which exists between the coördinates of

that of a line expresses are constant of the line. Equation of a straight line,  $y = ax \pm b$ , in which a is the tangent of the angle the line makes with the axis of X, and b the distance above A in which the line cuts the axis of Y. Every equation of the first degree between two variables is the equation of

a straight line, as Ay + Bx + C = 0, which can be reduced to the form y = $ax \pm b$ .

Equation of the distance between two points:

$$D = \sqrt{(x'' - x')^2 + (y'' - y')^2},$$

in which x'y', x"y" are the coordinates of the two points. Equation of a line passing through a given point:

$$y - y' = a(x - x'),$$

in which x'y' are the coördinates of the given point, a, the tangent of the angle the line makes with the axis of x, being undetermined, since any num-

ber of lines may be drawn through a given point.

Equation of a line passing through two given points:

$$y-y'=\frac{y^{\prime\prime}-y^{\prime}}{x^{\prime\prime}-x^{\prime}}(x-x^{\prime}).$$

Equation of a line parallel to a given line and through a given point:

$$y - y' = a(x - x').$$

Equation of an angle V included between two given lines:

tang 
$$V = \frac{a' - a}{1 + a'a}$$
,

in which a and a' are the tangents of the angles the lines make with the axis of abscissas,

If the lines are at right angles to each other tang  $V = \infty$ , and

$$1 + a'a = 0.$$

Equation of an intersection of two lines, whose equations are

$$y = ax + b$$
, and  $y = a'x + b'$ ,  $x = -\frac{b - b'}{a - a'}$ , and  $y = \frac{ab' - a'b}{a - a'}$ .

axis:

Equation of a perpendicular from a given point to a given line:

$$y - y' = -\frac{1}{a}(x - x').$$

Equation of the length of the perpendicular P:

$$P = \frac{y' - ax' - b}{\sqrt{1 \times a^2}}.$$

The circle.-Equation of a circle, the origin of coordinates being at the centre, and radius = R:

$$x^2 + y^2 = R^2$$

If the origin is at the left extremity of the diameter, on the axis of X:

$$y^2 = 2Rx - x^2.$$

If the origin is at any point, and the coördinates of the centre are x'y':

$$(x-x')^2 + (y-y')^2 = R^2$$

Equation of a tangent to a circle, the coordinates of the point of tangency being x"y" and the origin at the centre,

$$yy'' + xx'' = R^2.$$

The ellipse. - Equation of an ellipse, referred to rectangular coordinates with axis at the centre:

$$A^2y^2 + B^2x^2 = A^2B^2,$$

in which A is half the transverse axis and B half the conjugate axis. Equation of the ellipse when the origin is at the vertex of the transverse

 $y^2 = \frac{B_{-}^2}{42}(2Ax - x^2).$ 

The eccentricity of an ellipse is the distance from the centre to either focus, divided by the semi-transverse axis, or

$$e = \frac{\sqrt{A^2 - B^2}}{A}.$$

The parameter of an ellipse is the double ordinate passing through the focus. It is a third proportional to the transverse axis and its conjugate, or

$$2A:2B::2B:$$
 parameter; or parameter =  $\frac{2B^2}{4}$ .

Any ordinate of a circle circumscribing an ellipse is to the corresponding ordinate of the ellipse as the semi-transverse axis to the semi-conjugate. Any ordinate of a circle inscribed in an ellipse is to the corresponding ordinate of the ellipse as the semi-conjugate axis to the semi-transverse. Equation of the tangent to an ellipse, origin of axes at the centre:

$$A^2yy^{\prime\prime} + B^2xx^{\prime\prime} = A^2B^2,$$

y''x'' being the coördinates of the point of tangency. Equation of the normal, passing through the point of tangency, and perpendicular to the tangent:

$$y - y'' xx \frac{A^2 y''}{B^2 x''} (x - x'').$$

The normal bisects the angle of the two lines drawn from the point of tangency to the foci. The lines drawn from the foci make equal angles with the tangent.

**The parabola.**—Equation of the parabola referred to rectangular coördinates, the origin being at the vertex of its axis.  $y^2 = 2px$ , in which 2p is the parameter or double ordinate through the focus.

The parameter is a third proportional to any abscissa and its corresponding ordinate, or

Equation of the tangent:

$$yy^{\prime\prime}=p(x+x^{\prime\prime}),$$

y''x'' being coördinates of the point of tangency.

Equation of the normal:

$$y-y^{\prime\prime}\,xx-rac{y^{\prime\prime}}{p}(x-x^{\prime\prime}).$$

The sub-normal, or projection of the normal on the axis, is constant, and equal to half the parameter.

The tangent at any point makes equal angles with the axis and with the line drawn from the point of tangency to the focus.

The hyperbola. - Equation of the hyperbola referred to rectangular coordinates, origin at the centre;

$$A^2y^2 - B^2x^2 = -A^2B^2,$$

in which A is the semi-transverse axis and B the semi-conjugate axis. Equation when the origin is at the vertex of the transverse axis:

$$y^2 = \frac{B^2}{A^2} (2A \ xx \ x^2).$$

Conjugate and equilateral hyperbolas.-If on the conjugate axis, as a transverse, and a focal distance equal to  $\sqrt{A^2 + B^2}$ , we construct the two branches of a hyperbola, the two hyperbolas thus constructed are called conjugate hyperbolas. If the transverse and conjugate axes are equal, the hyperbolas are called equilateral, in which case  $y^2 - x^2 = -A^2$  when A is the transverse axis, and  $x^2 - y^2 = -B^2$  when B is the transverse axis, and  $x^2 - y^2 = -B^2$  when B is the transverse axis, and  $x^2 - y^2 = B^2$  when B is the transverse axis, and  $x^2 - y^2 = B^2$  when B is the transverse axis, and  $x^2 - y^2 = B^2$  when B is the transverse axis, and  $x^2 - y^2 = B^2$  when B is the transverse axis, and  $x^2 - y^2 = B^2$  when B is the transverse axis, and B i verse axis.

The parameter of the transverse axis is a third proportional to the trans-

verse axis and its conjugate.

The tangent to a hyperbola bisects the angle of the two lines drawn from the point of tangency to the foci.

The asymptotes of a hyperbola are the diagonals of the rectangle described on the axes, indefinitely produced in both directions. In an equilateral hyperbola the asymptotes make equal angles with the

transverse axis, and are at right angles to each other.

The asymptotes continually approach the hyperbola, and become tangent to it at an infinite distance from the centre.

Conic sections.—Every equation of the second degree between two

variables will represent either a circle, an ellipse, a parabola or a hyperbola. These curves are those which are obtained by intersecting the surface of a cone by planes, and for this reason they are called conic sections.

Logarithmic curve.—A logarithmic curve is one in which one of the coordinates of any point is the logarithm of the other.

The coordinate axis to which the lines denoting the logarithms are parallel is called the axis of logarithms, and the other the axis of numbers. If y is the axis of logarithms and x the axis of numbers, the equation of the curve is  $y = \log x$ .

If the base of a system of logarithms is a, we have  $a^y = x$ , in which y is the

logarithm of x.

Each system of logarithms will give a different logarithmic curve. If y =0, x = 1. Hence every logarithmic curve will intersect the axis of numbers at a distance from the origin equal to 1.

#### DIFFERENTIAL CALCULUS.

The differential of a variable quantity is the difference between any two of its consecutive values; hence it is indefinitely small. It is expressed by writing d before the quantity, as dx, which is read differential of x.

The term  $\frac{dy}{dx}$  is called the differential coefficient of y regarded as a function of x.

The differential of a function is equal to its differential coefficient multiplied by the differential of the independent variable; thus,  $\frac{dy}{dx}dx=dy$ .

The *limit* of a variable quantity is that value to which it continually approaches, so as at last to differ from it by less than any assignable quantity.

tity.

The differential coefficient is the limit of the ratio of the increment of the independent variable to the increment of the function.

ndependent variable to the increment of the function.

The differential of a constant quantity is equal to 0.

The differential of a product of a constant by a variable is equal to the constant multiplied by the differential of the variable.

If 
$$u = Av$$
,  $du = Adv$ .

In any curve whose equation is y=f(x), the differential coefficient  $\frac{dy}{dx}=\tan a$ ; hence, the rate of increase of the function, or the ascension of the curve at any point, is equal to the tangent of the angle which the tangent line makes with the angle of abscissas.

All the operations of the Differential Calculus comprise but two objects:

1. To find the rate of change in a function when it passes from one state

of value to another, consecutive with it.

2. To find the actual change in the function: The rate of change is the

differential coefficient, and the actual change the function.

Differentials of algebraic functions.—The differential of the sum or difference of any number of functions, dependent on the same variable, is equal to the sum or difference of their differentials taken separately:

If 
$$u = y + z - w$$
,  $du = dy + dz - dw$ .

The differential of a product of two functions dependent on the same variable is equal to the sum of the products of each by the differential of the other:

$$d(uv) = vdu + udv.$$
  $\frac{d(uv)}{uv} = \frac{du}{u} + \frac{dv}{v}.$ 

The differential of the product of any number of functions is equal to the sum of the products which arise by multiplying the differential of each function by the product of all the others:

$$d(uts) = tsdu + usdt + utds.$$

The differential of a fraction equals the denominator into the differential of the numerator minus the numerator into the differential of the denominator, divided by the square of the denominator:

$$dt = d\left(\frac{u}{v}\right) = \frac{vdu - udv}{v^2}.$$

If the denominator is constant, dv = 0, and  $dt = \frac{vdu}{v^2} = \frac{du}{v}$ .

If the numerator is constant, du = 0, and  $dt xx - \frac{udv}{v^2}$ 

The differential of the square root of a quantity is equal to the differential of the quantity divided by twice the square root of the quantity:

If 
$$v = u^{\frac{1}{2}}$$
, or  $v = \sqrt{u}$ ,  $dv = \frac{du}{2\sqrt{u}}$ ;  $= \frac{1}{2}u^{-\frac{1}{2}}du$ .

The differential of any power of a function is equal to the exponent multiplied by the function raised to a power less one, multiplied by the differential of the function,  $d(u^n) = nu^{n-1}du$ .

Formulas for differentiating algebraic functions.

1. 
$$d(a) = 0$$
.  
2.  $d(ax) = adx$ .  
3.  $d(x + y) = dx + dy$ .  
4.  $d(x - y) = dx - dy$ .  
5.  $d(xy) = xdy + ydx$ .  
6.  $d(\frac{x}{y}) = \frac{ydx - xdy}{y^2}$ .  
7.  $d(x^m) = mx^{m-1}dx$ .  
8.  $d(\sqrt{x}) = \frac{dx}{2\sqrt{x}}$ .  
9.  $d(x^{-\frac{r}{s}}) = -\frac{r}{s}x^{-\frac{r}{s}} - 1$ .

To find the differential of the form  $u=(a+bx^n)^m$ . Multiply the exponent of the parenthesis into the exponent of the variable within the parenthesis, into the coefficient of the variable, into the binomial raised to a power less i, lift the variable within the parenthesis raised to a power less i, into the differential of the variable.

$$du = d(a + bx^n)^m = mnb(a + bx^n)^{m-1}x^{n-1}dx.$$

To find the rate of change for a given value of the variable: Find the differential coefficient, and substitute the value of the variable in the second member of the equation.

Example.—If w is the side of a cube and u its volume,  $u = x^3$ ,  $\frac{du}{dx} = 3x^2$ .

Hence the rate of change in the volume is three times the square of the edge. If the edge is denoted by 1, the rate of change is 3.

Application. The coefficient of expansion by heat of the volume of a body is three times the linear coefficient of expansion. Thus if the side of a cube expands. 901 inch. its volume expands. 903 cubic inch. 1.003 = 1.003003001.

A partial differential coefficient is the differential coefficient of a function of two or more variables under the supposition that only one of

them has changed its value.

A partial differential is the differential of a function of two or more variables under the supposition that only one of them has changed its value. The total differential of a function of any number of variables is equal to the sum of the partial differentials.

If 
$$u=f(xy)$$
, the partial differentials are  $\frac{du}{dx}dx$ ,  $\frac{du}{dy}dy$ .  
If  $u=x^2+y^2-z$ ,  $du=\frac{du}{dx}dx+\frac{du}{dy}dy+\frac{du}{dz}dz$ ;  $=2xdx+3y^2dy-dz$ .

Integrals.—An integral is a functional expression derived from a differential. Integration is the operation of finding the primitive function the differential function. It is indicated by the sign  $f_i$  which is read "the integral of." Thus  $\int 2xdx = x^2$ ; read, the integral of 2xdx equals  $x^2$ . To integrate an expression of the form  $mx^{m-1}dx$  or  $x^mdx$ , add 1 to the exponent of the variable, and divide by the new exponent and by the differential of the variable:  $\int 3x^2dx = x^3$ . (Applicable in all cases except when m=-1. For  $\int x^{-1} dx$  see formula 2 page 78.)

The integral of the product of a constant by the differential of a variable is equal to the constant multiplied by the integral of the differential:

$$\int ax^m dx = a \int x^m dx = a \frac{1}{m+1} x^{m+1}.$$

The integral of the algebraic sum of any number of differentials is equal to the algebraic sum of their integrals:

$$du = 2ax^{2}dx - bydy - z^{2}dz; \quad fdu = \frac{2}{3}ax^{3} - \frac{b}{2}y^{2} - \frac{z^{3}}{3}.$$

Since the differential of a constant is 0, a constant connected with a variable by the sign + or - disappears in the differentiation; thus  $d(a+x^m)$  =  $dx^m = mx^{m-1}dx$ . Hence in integrating a differential expression we must annex to the integral obtained a constant represented by C to compensate for the term which may have been lost in differentiation. Thus if we have dy=adx; fdy=afdx. Integrating,

$$y = \alpha x \pm C$$
.

The constant C, which is added to the first integral, must have such a value as to render the functional equation true for every possible value that may be attributed to the variable. Hence, after having found the first integral equation and added the constant C, if we then make the variable equal to zero, the value which the function assumes will be the true value of C.

An indefinite integral is the first integral obtained before the value of the

constant C is determined. A particular integral is the integral after the value of C has been found. A definite integral is the integral corresponding to a given value of the

variable. Integration between limits.—Having found the indefinite inte-

gral and the particular integral, the next step is to find the definite integral, and then the definite integral between given limits of the variable. The integral of a function, taken between two limits, indicated by given values of x, is equal to the difference of the definite integrals corresponding to those limits. The expression

$$\int_{x'}^{x''} dy = a \int dx$$

is read: Integral of the differential of y, taken between the limits x' and x''; the least limit, or the limit corresponding to the subtractive integral, being placed below. Integrate  $du = 9x^2dx$  between the limits x = 1 and x = 3, u being equal to

81 when x = 0,  $fdu = f9x^2dx = 3x^3 + C$ ; C = 81 when x = 0, then

$$\int_{x=1}^{x=3} du = 3(3)^3 + 81, \text{ minus } 3(1)^3 + 81 = 78.$$

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# Integration of particular forms.

To integrate a differential of the form  $du = (a + bx^n)^m x^{n-1} dx$ 

1. If there is a constant factor, place it without the sign of the integral, and omit the power of the variable without the parenthesis and the differential;

2. Augment the exponent of the parenthesis by 1, and then divide this quantity, with the exponent so increased, by the exponent of the parenthesis, into the exponent of the variable within the parenthesis, into the coefficient of the variable. Whence

$$\int du = \frac{(a + bx^n)^{m+1}}{(m+1)nb} = C.$$

The differential of an arc is the hypothenuse of a right-angle triangle of which the base is dx and the perpendicular dy.

If z is an arc, 
$$dz = \sqrt{dx^2 + dy^2}$$
  $z = \int \sqrt{dx^2 + dy^2}$ .

Quadrature of a plane figure.

The differential of the area of a plane surface is equal to the ordinate into the differential of the abscissa.

$$ds = udx$$
.

To apply the principle enunciated in the last equation, in finding the area of any particular plane surface: Find the value of y in terms of x, from the equation of the bounding line:

substitute this value in the differential equation, and then integrate between the required limits of x.

Area of the parabola. -Find the area of any portion of the common parabola whose equation is

$$y^2 = 2px$$
; whence  $y = \sqrt{2px}$ .

Substituting this value of u in the differential equation ds = udx gives

$$\int ds = \int \sqrt{2px} dx = \sqrt{2p} \int x^{\frac{1}{2}} dx = \frac{2\sqrt{2p}}{3} x^{\frac{3}{2}} + C;$$
or,  $s = \frac{2\sqrt{2px}}{3} \times x = \frac{2}{3} xy + C.$ 

If we estimate the area from the principal vertex, x = 0, y = 0, and C = 0: and denoting the particular integral by s',  $s' = \frac{2}{5}xy$ .

That is, the area of any portion of the parabola, estimated from the vertex, is equal to % of the rectangle of the abscissa and ordinate of the extreme point. The curve is therefore quadrable.

Quadrature of surfaces of revolution. — The differential of a surface of revolution is equal to the circumference of a circle perpendicular to the axis into the differential of the arc of the meridian curve.

$$ds = 2\pi y \sqrt{dx^2 + dy^2};$$

in which y is the radius of a circle of the bounding surface in a plane perpendicular to the axis of revolution, and x is the abscissa, or distance of the plane from the origin of coördinate axes.

Therefore, to find the volume of any surface of revolution:

Find the value of y and dy from the equation of the meridian curve in terms of x and dx, then substitute these values in the differential equation. and integrate between the proper limits of x.

By application of this rule we may find: The curved surface of a cylinder equals the product of the circumference

of the base into the altitude.

The convex surface of a cone equals the product of the circumference of the base into half the slant height.

The surface of a sphere is equal to the area of four great circles, or equal to the curved surface of the circumscribing cylinder,

Cubature of volumes of revolution.—A volume of revolution is a volume generated by the revolution of a plane figure about a fixed line called the axis.

If we denote the volume by V,  $dV = \pi y^2 dx$ . The area of a circle described by any ordinate y is  $\pi y^2$ ; hence the differential of a volume of revolution is equal to the area of a circle perpendicular to the axis into the differential of the axis.

The differential of a volume generated by the revolution of a plane figure about the axis of Y is  $\pi x^2 dy$ .

To find the value of Y for any given volume of revolution:

Find the value of  $y^2$  in terms of x from the equation of the meridian curve, substitute this value in the differential equation, and then integrate between the required limits of x. By application of this rule we may find:

The volume of a cylinder is equal to the area of the base multiplied by the

altitude. The volume of a cone is equal to the area of the base into one third the

altitude. The volume of a prolate spheroid and of an oblate spheroid (formed by

the revolution of an ellipse around its transverse and its conjugate axis respectively) are each equal to two thirds of the circumscribing cylinder. If the axes are equal, the spheroid becomes a sphere and its volume =

 $\frac{8}{3}\pi R^2 \times D = \frac{1}{6}\pi D^3$ ; R being radius and D diameter.

The volume of a paraboloid is equal to half the cylinder having the same base and altitude.

The volume of a pyramid equals the area of the base multiplied by one third the altitude Second, third, etc., differentials.—The differential coefficient being a function of the independent variable, it may be differentiated, and

we thus obtain the second differential coefficient:  $d\left(\frac{du}{dx}\right) = \frac{d^2u}{dx}.$ Dividing by dx, we have for the second differential coefficient  $\frac{d^2u}{dx^2}$ , which is read: second differential of u divided by the square of the differential of x (or dx squared).

The third differential coefficient  $\frac{d^3u}{dx^3}$  is read: third differential of u divided

by dx cubed The differentials of the different orders are obtained by multiplying the differential coefficients by the corresponding powers of dx; thus  $\frac{d^3u}{dx^3} dx^3 =$ 

third differential of u. Sign of the first differential coefficient.—If we have a curve whose equation is y = fx, referred to rectangular coördinates, the curve will recede from the axis of X when  $\frac{dy}{dx}$  is positive, and approach the axis when it is negative, when the curve lies within the first angle of the coördinate axes. For all angles and every relation of y and x the curve will recede from the axis of X when the ordinate and first differential coefficient have the same sign, and approach it when they have different signs. If the tangent of the curve becomes parallel to the axis of X at any point  $\frac{dy}{dx} = 0$ . If the tangent becomes perpendicular to the axis of X at any point  $\frac{dy}{dx} = \infty$ .

Sign of the second differential coefficient.—The second dif-ferential coefficient has the same sign as the ordinate when the curve is terement coefficient has are saint sign as the contrary sign when it is coronave. **Maclaurin's Theorem.**—For developing into a series any function of a single variable as  $A + Bx + Cx^2 + Dx^3 + Ex^3$ , etc., in which A, B,

C, etc., are independent of x:  $u = (u)_{x=0} + \left(\frac{du}{dx}\right)_{x=0} x + \frac{1}{1 \cdot 2} \left(\frac{d^2u}{dx^2}\right)_{x=0} x^2 + \frac{1}{1 \cdot 2 \cdot 3} \left(\frac{d^3u}{dx^3}\right)_{x=0} x^3 + \text{etc.}$ 

In applying the formula, omit the expressions x = 0, although the coefficients are always found under this hypothesis.

EXAMPLES:

$$\begin{split} (a+x)^m &= a^m + ma^{m-1}x + \frac{m}{1}\frac{(m-1)}{2}a^{m-2}x^2 \\ &\qquad \qquad + \frac{m}{1}\frac{(m-1)}{2}\frac{(m-2)}{3}a^{m-3}x^3 + \text{etc.} \end{split}$$

$$\frac{1}{a+x} = \frac{1}{a} - \frac{x}{a^2} + \frac{x^3}{a^3} - \frac{x^3}{a^4} + \dots + \frac{x^n}{a^{n+1}}$$
, etc.

Taylor's Theorem. - For developing into a series any function of the sum or difference of two independent variables, as  $u' = f(x \pm y)$ :

$$u' = u + \frac{du}{dx}y + \frac{d^2u}{dx^2}\frac{y^2}{1 \cdot 2} + \frac{d^3u}{dx^3}\frac{y^3}{1 \cdot 2 \cdot 3} + \text{etc.},$$

in which u is what u' becomes when  $y=0, \frac{du}{dx}$  is what  $\frac{du'}{dx}$  becomes when

Maxima and minima. -To find the maximum or minimum value of a function of a single variable:

1. Find the first differential coefficient of the function, place it equal to 0,

and determine the roots of the equation.

2. Find the second differential coefficient, and substitute each real root; in succession, for the variable in the second member of the equation. Each root which gives a negative result will correspond to a maximum value of the function, and each which gives a positive result will correspond to a minimum value.

Example.—To find the value of x which will render the function y a maximum or minimum in the equation of the circle,  $y^2 + x^2 = R^2$ ;

$$\frac{dy}{dx} = -\frac{x}{y}$$
; making  $-\frac{x}{y} = 0$  gives  $x = 0$ ,

The second differential coefficient is:  $\frac{d^2y}{dx} = -\frac{x^2 + y^2}{x^3}$ .

When x = 0, y = R; hence  $\frac{d^2y}{dx^2} = -\frac{1}{R}$ , which being negative, y is a maximum for R positive.

In applying the rule to practical examples we first find an expression for the function which is to be made a maximum or minimum.

2. If in such expression a constant quantity is found as a factor, it may be omitted in the operation; for the product will be a maximum or a mini-

to committee in the operation; for the product will be a maximum or a minimum.

3. Any value of the independent variable which renders a function a maximum or a minimum will render any power or root of that function a maximum or minimum; hence we may square both members of an equation to free it of radicals before differentiating.

By these rules we may find: The maximum rectangle which can be inscribed in a triangle is one whose altitude is half the altitude of the triangle.

The altitude of the maximum cylinder which can be inscribed in a cone is one third the altitude of the cone.

The surface of a cylindrical vessel of a given volume, open at the top, is a minimum when the altitude equals half the diameter.

The altitude of a cylinder inscribed in a sphere when its convex surface is a maximum is  $r\sqrt{2}$ . r = radius.

The altitude of a cylinder inscribed in a sphere when the volume is a maximum is

#### Differential of an exponential function.

then 
$$du = da^x = a^x k dx$$
, . . . . . . . . . . . (2)

in which k is a constant dependent on a.

The relation between 
$$a$$
 and  $k$  is  $a^{\frac{1}{k}} = e$ ; whence  $a = e^k$ , . . . . . (3)

in which  $e=2.7182818\ldots$  the base of the Naperian system of logarithms. **Logarithms.**—The logarithms in the Naperian system are denoted by t, Nap. log or hyperbolic log, hyp. log, or  $\log_{\theta}$ ; and in the common system always by  $\log$ .

The common logarithm of  $e_1 = \log 2.7182818 \dots = .4342945 \dots$ , is called the modulus of the common system, and is denoted by M. Hence, if we have the Naperian logar thm of a number we can find the common logarithm of the same number by multiplying by the modulus. Reciprocally, Nap.  $\log = \text{com}$ ,  $\log \times 2$  3025851.

If in equation (4) we make a = 10, we have

$$1 = k \log e$$
, or  $\frac{1}{k} = \log e = M$ .

That is, the modulus of the common system is equal to 1, divided by the Naperian logarithm of the common base.

From equation (2) we have

$$\frac{du}{u} = \frac{da^x}{a^x} = kdx.$$

If we make a = 10, the base of the common system,  $x = \log u$ , and

$$d(\log u) = dx = \frac{du}{u} \times \frac{1}{k} = \frac{du}{u} \times M.$$

That is, the differential of a common logarithm of a quantity is equal to the differential of the quantity divided by the quantity, into the modulus. If we make a=e, the base of the Naperian system, x becomes the Naperian

10.

rian logarithm of u, and k becomes 1 (see equation (3)); hence M = 1, and

$$d(\text{Nap. log } u) = dx = \frac{du}{a^x}; = \frac{du}{u}.$$

That is, the differential of a Naperian logarithm of a quantity is equal to the differential of the quantity divided by the quantity; and in the Naperian system the modulus is 1.

Since k is the Naperian logarithm of a,  $du = a^x l a dx$ . That is, the

differential of a function of the form  $a^x$  is equal to the function, into the Naperian logarithm of the base a, into the differential of the exponent. If we have a differential in a fractional form, in which the numerator is the differential of the denominator, the integral is the Naperian logarithm of the denominator. Integrals of fractional differentials of other forms are

Differential forms which have known integrals; exponential functions, (l = Nap. log.)

1. 
$$\int a^{x} l a dx = a^{x} + C;$$
2. 
$$\int \frac{dx}{x} = \int dx x^{-1} = lx + C;$$
3. 
$$\int (xy^{x^{-1}}dy + y^{x} l y \times dx) = y^{x} + C;$$
4. 
$$\int \frac{dx}{\sqrt{x^{2} \pm a^{2}}} = l(x + \sqrt{x^{2} \pm a^{2}}) + C;$$
5. 
$$\int \frac{dx}{\sqrt{x^{2} \pm 2ax}} = l(x \pm a + \sqrt{x^{2} \pm 2ax}) + C;$$
6. 
$$\int \frac{2adx}{a^{2} - x^{2}} = l(\frac{a + x}{a - x}) + C;$$
7. 
$$\int \frac{2adx}{x^{2} - a^{2}} = l(\frac{x - a}{x + a}) + C;$$
8. 
$$\int \frac{2adx}{x\sqrt{a^{2} + x^{2}}} = l(\frac{\sqrt{a^{2} + x^{2} - a}}{\sqrt{a^{2} + x^{2} + a}}) + C;$$
9. 
$$\int \frac{2adx}{x\sqrt{a^{2} - x^{2}}} = l(\frac{a - \sqrt{a^{2} - x^{2}}}{a + \sqrt{a^{2} - x^{2}}}) + C;$$
10. 
$$\int \frac{x^{-2}dx}{\sqrt{a^{2} - x^{2}}} = -l(\frac{1 + \sqrt{1 + a^{2}x^{2}}}{a + \sqrt{1 + a^{2}x^{2}}}) + C.$$

Circular functions.-Let z denote an arc in the first quadrant, y its sine, x its cosine, v its versed sine, and t its tangent; and the following notation be employed to designate an arc by any one of its functions, viz.,

$$\sin^{-1} y$$
 denotes an arc of which  $y$  is the sine  $\cos^{-1} x$  " " "  $x$  is the cosine,  $\tan^{-1} t$  " " "  $t$  is the tangent

(read "arc whose sine is u," etc.),—we have the following differential forms which have known integrals (r = radius);

$$\int \cos z \, dz = \sin z + C;$$

$$\int -\sin z \, dz = \cos z + C;$$

$$\int \frac{dy}{\sqrt{1 - y^2}} = \sin^{-1} y + C;$$

$$\int \frac{-dx}{\sqrt{1 - x^2}} = \cos^{-1} x + C;$$

$$\int \frac{dv}{\sqrt{2v - v^2}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int \frac{dv}{\sqrt{2v - v^2}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int \frac{dv}{\sqrt{2v - v^2}} = \operatorname{ver-sin}^{-1} v + C;$$

$$\int \frac{dv}{\sqrt{2v - v^2}} = \sin^{-1} v + C;$$

$$\int \frac{dv}{\sqrt{v^2 - u^2}} = \sin^{-1} v + C;$$

$$\int \frac{du}{\sqrt{v^2 - u^2}} = \sin^{-1} u + C;$$

$$\int \frac{-du}{\sqrt{v^2 - u^2}} = \cos^{-1} \frac{u}{a} + C;$$

$$\int \frac{dv}{\sqrt{v^2 - u^2}} = \cos^{-1} \frac{u}{a} + C;$$

$$\int \frac{du}{\sqrt{v^2 - u^2}} = \cos^{-1} \frac{u}{a} + C;$$

$$\int \frac{du}{\sqrt{v^2 - u^2}} = \cos^{-1} \frac{u}{a} + C;$$

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$$\int \frac{du}{\sqrt{v^2 - u^2}} = \cos^{-1} \frac{u}{a} + C;$$

**The cycloid.**—If a circle be rolled along a straight line, any point of the circumference, as P, will describe a curve which is called a cycloid. The circle is called the generating circle, and P the generating point.

The transcendental equation of the cycloid is

$$x = \text{ver-sin}^{-1} y - \sqrt{2ry - y^2},$$

and the differential equation is  $dx = \frac{ydx}{\sqrt{2xy - y^2}}$ 

The area of the cycloid is equal to three times the area of the generating circle.

The surface described by the arc of a cycloid when revolved about its base is equal to 64 thirds of the generating circle.

The volume of the solid generated by revolving a cycloid about its base is

equal to five eighths of the circumscribing cylinder.

Integral calculus.—In the integral calculus we have to return from the differential to the function from which it was derived. A number of differential expressions are given above, each of which has a known integral corresponding to it, and which being different ated, will produce the

given differential.

In all classes of functions any differential expression may be integrated. In all classes of functions any differential expression may be integrated. when it is reduced to one of the known forms; and the operations of the integral calculus consist mainly in making such transformations of given differential expressions as shall reduce them to equivalent ones whose integrals are known.

For methods of making these transformations reference must be made to the text-books on differential and integral calculus.

# RECIPROCALS OF NUMBERS.

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3	.00309597	8 9	.00257732	3	.00220751	18 19	.00193050	3 4	.00171527
5	.00307692	390	.00256410	5 6	.00219780	520	.00192308	5	.00170940
6	.00306748	1	.00255754	6	.00219298	1	.00191939	6	.00170648
7 8	.00305510	2 3	.00255102	8	.00218818	2 3	.00191571	8	.00170358
9	.00303951	4	.00253807	9	.00217865	4	,00190840	9	.00169779
330	.00303030	5	.00253165	460	.00217391	5	.00190476	590	.00169491
1	.00302115	6 7 8	.00252525	1 2	.00216920	7	.00190114	1 2	.00169205
3	.00300300	8	.00251256	a s	.90215983	8	.00189394	3	.00168634
4	.00299401	9	.00250627	4	.00215517	9	.00189036	4	.00168350
5 6	.00298507	400	.00250000	5	.00215054	530	.00188679	5 6	.00168067
7	.00296736	2	.00249377	7	.00214392	2	.00187970	7	.00167504
8	.00295858	3	.00248139	8	.00213675	3	.00187617	8	.00167224
9	.00294985	5 6 7 8	.00247525	470	.00213220	4	.00187266	9	.00166945
340	.00294118	6	.00246914	470	.00212766	5 6 7	.00186916	600	.00166667
1 2 3	.00292398	7	.00245700	2 3	.00211864	7	.00186220	2	.00166113
	.00291545	8	.00245098	3	.00211416	8 9	.00185874	3	.00165837
4 5	.00290698	410		5	.00210970	540	.00185528	3 5	.00165563
6	.00289017	11	.00243309	6	.00210084	1	.00184843	6	.00165016
7 8	.00288184	12	.00242718	7	.00209644	3	.00184502	7	.00164745
9	.00287356	13 14		8 9	.00209205		.00184162 .00183823	8 9	.00164474
350	.00285714	15		480	.00208333	5 6 7	.00183486	610	
1	.00284900	16	.00240385	1	.00207900	6	.00183150	11	.00163666
3	.00284091	17 18	.00239808	3	.00207469	8	.00182815 .00182482	12 13	.90163399
4	.00282486	19	.00238663	4	.00206612	9	.00182149	14	.00162866
5	.00281690	420		5	.00206186	550		15	.00162602
6	.00280899	1	.00237530	6	.00205761	1 1	.00181488	16	
7 8	.90279330	3	.00236407	8	.00204918	2 3	.00180832	18	
9	.00278551	4	.00235849	9		4	.00180505	19	
360 1	.00277778	5 6 7	.00235294	490	.00204082	4 5 6 7 8	.00180180	620	.00161290
2	.00276243	7	.00234142			7	.00179533		
3	.00275482	8	.00233645	3	.00202840			3	.00160514
4 5	.00274725	430	.00233100	5	.00202429	560		3 5	.00160256
6	.00273224	1	.00232019	6		1	.00178253	6	.00159744
7	.00272480	3	.00231481	7	.00201207	3	.00178253 .00177936 .00177620	7	.00159490
8	.00271739			8			.00177620	8 9	
370	.00271003	5	.00230415	500		5	.00177305 00176991	630	
1	.00269542	5 6 7	.00229358	1	.00199601	6	.00176678	1	.00158479
2	.00268817	8	.00228833	3	.00199203	4 5 6 7 8	.00176367	3	.00158228
4	.00268096	9	.00228310	4	.00198413	9	.00175747	4	.00157729
5	.00266667	440	.00227273	5	.00198020	570	.00175439	5	.00157480
6	.00265957	1	.00226757	6	.00197628	1	.00175131	6	.00157233
8	.00265252	2	.00226244	6 7 8	.00197239	3	.00174825	8 9	.00156986
9	.00263852	4	.00225225			4	.00174216		
380	.00263158	5	.00224719	1 510	.00196078	11 5	.00173913	640	.00156250

No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-
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641	.00156006	706	.00141643	771	.00129702	836	.00119617	901	.00110988
2 3	.00155763	7	.00141443	2 3	.00129534	7	.00119474	2	.00110865
4	.00155521	8	.00141243	4	.00129366	. 8	.00119332	3 4	.00110742
5	.00155039	710	.00140845	5	.00129032	840	.00119048	5	.00110497
5 6 7 8	.00154799	11 12	.00140647	6	.00128866	1	.00118906	6	.00110375
8	.00154339	13	.00140419	7 8	.00128535	2 3	.00118624	8	.00110234
9	.00154083	14	.00140056	9	.00128370	4	.00118483	9	.00110011
650 1	.00153846	15 16	.00139860	780	.00128205	5 6	.00118343	910	.00109890
2	.00153374	17	.00139470	2	.00127877	7	.00118064	12	.00109649
2 3	.00153140	18	.00139276	3	.00127714	8	.00117924	13	.00109529
4 5	.00152905	19 720	.00139082	5	.00127551 .00127388	850	.00117786	14 15	.00109409
6	.00152439	1	.00138696	6	.00127226	1	.00117509	16	.00109170
7	.00152207	2	.00138501	7	.00127065	2	.00117371	17	.00109051
8	.00151975	3 4	.00138313	8 9	.00126904	3 4	00117233	18 19	.00108932
660	.00151745		.00137931	790	.00126582	5	.00116959	920	.00108696
1	.00151286	5 6 7	.00137741	1	.00126422	6	.00116822	1	.00108578
2 3	.00151057	8	.00137552	2 3	.00126263	8	.00116686	2 3	.00108460
4	.00150602	9	.00137174	4	.00125945	9	.00116414	4	.00108225
5	.00150376	730	.00136986	5	.00125786	860		5	.00108108
6 7	.00150150	1 9	.00136799	6	.00125628	1 2	.00116144	6	.00107991
6 7 8	.00149701	2 3	.00136426	8		l ~	.00115875	8	.00107759
9	.00149477	4	.00136240	9	.00125156	4	.00115741	9	.00107643
670 1	.00149254	5	.00136054	800	.00125000	5	.00115607	930	.00107527
2	.00148809	8	.00135685	2	.00124688	7	.00115340	2	.00107296
3	.00148588			3	.00124533	8		3	
3 4 5 6	.00148368	740			.00124378	870		4	.60107066
6	.00147929	1	.00134953		.00124069	1	.00114811	6	.00106838
7	.00147710	2	.00134771	7	.00123916	3	.00114679	7	.00106724
8		4	.00134589	8	.00123762	4	.00114547	8	.00106610
680	.00147059	l ē	.00134228	810	.00123457	5	.00114286	940	.00106383
1		7	.00134048		.00123305	6	.00114155		.00106270
2	.00146628	8	.00133690			8	.00114025	92.63	.00106157
4	.00146199	1 9	.00133511	14	.00122850	9	.00113766	4	.00105932
5	.00145985	750			.00122699	880			
7	.00145776	1 2	.00132979	17	.00122399			7 8	.00105708
8	.00145349	8	.00132802	18	.00122249	3		8	.00105485
690	00145137 00144927	4	.00132626			4 5 6 7 8	.00113122	950	.00105374
1	.00144718	1 6	.00132275	1	.00121803	6	.00112867	1	.00105152
2	.00144509	7 8	.00132100	1 2		7	.00112740	1 2	.00105042
8	.00144300		.00131926	4	.00121507	8 9	.00112613	3	
4 5 6 7 8	.00143885	760	.00131579	5	.00121212	890	.00112360	5	.00104712
6	.00143678	1 1	.00131406	6	.90121065	1	.00112233	67	
2	.00143472	3	.00131234	8	.00120919	3	.00112108	8	.00104493
9	.00143061	4	.00130890	9	.00120627	4	.00111857	9	.00104275
700	.00142857	5	.00130719	830	.00120482	5	.00111732	960	.00104167
1 2	.00142653	6	.00130548	1 2	.00120337	6	.00111607	1 2	.00104058
2 3 4 5	.00142247	8	.00130208	1 3	.00120048	8	.00111359	3	.00103842
4	.00142045	770	.00130039	4 5	.00119904	900	.00111235	4 5	.00103734
51	.00141844	1 770	.00129870	9	.001197601	900	.001111111	5	.00103627

No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-	No.	Recipro-
	cal.		cal.		cal.		cal.		cal.
000	00109590	1001	.000969932	1000	.000912409	1101	.000861326	1000	000012001
966	.00103520	1031	.0009689932	1096	.000912409	1161	,000860585	1226	.000815661
8	.00103306	3	.000968054	8	.000910747	a s	.000859845	8	.000814332
9	.00103199	4	.000967118	9	.000909918	4	.000859106	9	.000813670
970	.00103093	5 6	.000966184	1100	.000909091	5 6	000858369 000857633	1230	.000813008
1 2	.00102881	7	.000964320	2	.000907441	7	.000856898	2	.000811688
ã	.00102775	8	.000963391	3	.000906618	8	.000856164	3	.000811030
4	.00102669	9	.000962464	4	.000905797	9	.000855432	4	.000810373
5 6	.00102564	1040	.000961538	5 6	.000904977	1170	.000854701	5 6	.000809717
7	.00102354	2	.000959693	7	.000903342	2	.000853242	7	.000808407
8	.00102250	8	.000958774	8	.000902527	3	.000852515	8	.000807754
9	.00102145	4	.000957854	9	.000901713	4	.000851789	1040	.000807102
980 1	.00102041	5	.000956023	1110	000900901	5 6	1.000850340	1240 1	.000806452
2	.00101833	7	.000955110	12	.000899281	7	.000849618	2	.000805153
3	.00101729	8	.000954198	13	.000898473	8	.000848896	3	.000804505
4	.00101626	9	.000953289	14	.000897666	1100	.000848176	'4	.000803858
5 6	.00101523	1050	.000952381	15 16		1180	.000847457	5	.000803213
7	.00101317	2	,000950570	17	.000895255	2	.000846024	7	.000801925
8	.00101215	3	.000949668	18		3	.000845308	8	.000801282
9	.00101112	4	.000948767	19		4	.000844595	9	.000800640
990	.00101010	5 6	.000947867	1120	.000892061	5 6	.000843882	1250	.000800000
2	.00100806	7	.000946074	2		7	.000842460	2	.000798722
3	.00100705	8	.000945180	3	.000890472	8	.000841751	3	.000798085
4	.00100604	9	.000944287	4		9	.000841043	4	.000797448
5	.00100502	1060	.000943396	5		1190	.000840336	5 6	000796813
7	.00100301	2		7		2		7	000795545
8	.00100200	3	.000940734	8	.000886525	3	.000838222	8	.000794913
4000	.00100100	4		9		4		9	.000794281
1000	.00100000	6		11130	.000884956	5		1260	.000793651
2		7		2		7	.000835422	2	.000792393
ê	.000997009	8	.000936330	3	.000882612	8	.000834724	3	.000791766
4		9		4		9		4	.000791139
5		1070	.000934579			1200	.600833333	5	.000790514
		2		7		2		7	.000789266
8		3	.000931966	8	.000878735	3	.000831255	8	.000788643
1010		4		9		4		9	.000788022
1010	.000990099	6		1140	.000877193	5 6		1270	.000787402
12		1 7	.000928505	2	.000875657	7	.000828500	2	.000786163
18	.000987167	8	.000927644	8	.000874891	8	.000827815	3	.000785546
14		1000		.4		1010			
15 16		1080		5		1210	.000826446		
17	.000983284	2	.000924214	7	.000871840	12			.000783085
18	.000982318	3	.000923361	8	.000871080	13	.000824402	8	.000782478
19		4	.000922509	9		14	.000823723	1000	
1020	.000980392	5		11150	.000869565	15 16		1280	.000781250
2	.000978474	7	.000919963	2	.000868056	17	.000821693	2	.000780031
8	.000977517	8	.000919118	3	.000867303	18	000821018	3	.000779423
4	.000976562	1000		4		19		4	
5 6	.000975610	1090	.000917431	5 6		1220	.000819672	5	.000778210
7	.000973710	2		7	.000864304	2		7	.000777001
. 8	.000972763	3	.000914913	. 8	.000863558	3	.000817661	8	000776397
1000	.000971817	5	.000914077	1160	.000862813	4 5		1000	
1030	1.000970874	G 11	1.000915242	111100	4.000003069	0	1.000816326	11290	1.000775194

		1 1		1		1		1	1
No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.
1291	.000774593	1356	.000737463	1421	.000703730	1486	.000672948	1551	.000644745
2	.000773994	7	000736920	2	.000703235	7	.000672495	2	.000644330
3	.000773395	8	.000736377	3	.000702741	8	.000672043	3	.000643915
4	.000772797 .000772201	9	.000735835	4	.900702247	9	.000671592	4	.000643501
5	.000772201	1360	.000735294	5	.000701754	1490	.000671141	5	.000643087
6	.000771605	1	.000734754	6	.000701262	1	.000670691	6	.000642673
7 8	.000771010	2 3	.000734214	8	.000700771	2 3	.000670241	8	.000642261
9	.000769823	4	.000733138	9	.000699790	4	.000669344	9	.000641437
1300	.000769231	5	.000732601	1430	.000699301	5	.000668896	1560	.000641026
1	.000768639	6	.000732064	1	.000698812	6	.000668449	1	.000640615
2	.000768049	7	.000731529	2	.000698324	7	.000668003	2	.000640205
3	.000767459	8	.000730994	3	.000697837	8	.000667557	3	.000639795
4	.000766871	9	.000730460	4	.000697350	1500	.000667111	4	.000639386
5	.000765697	1370	.000729395	5	.000696864	1500	.00066667	5 6	.000638570
7	.000765111	2	.000728863	7	.000695894	2	.000665779	7	.000638162
8	.000764526	3	.000728332	8	.000695410	3	.000655336	8	.000637755
9	.000763942	4	.000727802	9	.000694927	4	.000664894	9	.000637349
1310	.000763359	5	.000727273	1440	.000694444	5	.000664452	1570	.000636943
11	.000762776	6	.000726744	1	.000693962	6	.000664011	1 1	.000636537
12	.000762195	8	.000726216	2	.000693481	7	.000663570	2 3	.000636132
13 14	.000761615	9	.000725689	3 4	.000693001		.000663130	4	.000635324
15	.000760456	1380	.000724638		.000692041	1510	.000662252	5	.000634921
16	.000759878	1	.000724113		.000691563	11	.000661813	6	.000634518
17	.000759801	2	.000723589	7	.000691085		.000661376	7	.000634115
18	.000758725	3	.000723066	8	.000690608	13	.000660939	8	.000633714
19	.000758150	4	.000722543	9	.000690131	14	.000660502	9	.000633312
1320	.000757576	5	.000722022	1450	.000689655		.000660066	1580	.000632911
1 2	.000757002	6	.000721501	1 2	.000689180	16 17	.000659631	1 2	.000632511
3	.000755858	8	.000720980 .000720461	3	.000688231		.000658761	3	.000632111
4	.000755287	9	.000719942	4	.000687758	19	.000658328	4	.000631313
5	.000754717	1390	.000719424	5	.000687285		.000657895	5	.000630915
6	.000754148	1	.000718907	6	.000686813		.000657462	6	.000630517
7	.000753579	2	000718391	7	.000686341	2	.000657030	7	.000630120
8	.000753012	3	.000717875	8	.000685871		.000656598	8 9	.000629723
1330	.000752445	4	.000717360	9 1460	.000685401	5	.000656168	1590	.000629327
1	.000751315	6	.000716332	1400	.000684463	6	.000655308	1000	.000628536
2	.000750750	7	.000715820	2	.000683994	7	.000654879	2	.000628141
3	.000750187	8	.000715308	3	.000683527	8	.000654450	3	.000627746
4	.000749625	9	.000714796	4	.000683060	9	.000654022	4	.000627353
5	.000749064	1400	.000714286	5	.000682594	1530	.000653595	5	.000626959
6	.000748503	2	.000713776	6	.000682128	1	.000653168	6	.000626566
7 8	.000747943	3	.000713267 .000712758	8	.000681663	2 3	.000652742	8	.000625782
9	.000746826	4	.000712251	9	.000680735	4	.000651890	9	.000625391
1340	.000746269	5	.000711744	1470	.000680272	5	.00065146€	1600	.000625000
1	.000745712	6	.000711238	1	.000679810	6	.000651042	2	.000624219
2	.000745156	7	.000710732	2	.000679348	7	.000650618	4	.000623441
3	.009744602	8	.000710227		.000678887	8	.000650195	6	.000622665
4	.000744048	9	.000709723	4	.000678426	1540	.000649773	1610	.000621890
5	.000743494	1410 11	.000709220	5	.000677966	1540 1	.000649351	1610 2	.000621118
7	.000742390	12	.000708717	7	.000677048	2	.000648508	4	.000619578
8	.000741840	13	.000707714	8	.000676590	3	.000648088	6	.000618812
9	.000741290	14	.000707214	9	.000676132	4	.000647668	8	.000618047
1350	.000740741	15	.000706714	1480	000675676	5	.000647249	1620	.000617284
1	.000740192	16	.000706215	1	.000675219	6	.000646830	2	.000616528
2 3	000739645	17	.000705716	2 3	.000674764	8	.000646412	6	.000615763
4	.000739098	18	.000705219	4	.000674309	9	.000645995	8	.000615006

No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.	No.	Recipro- cal.
						_			
1632	.000612745	1706		1780	.000561798	1854	.000539374	1928	.000518672
4	.000611995	8	.000585480	2	.000561167	6	.000538793	1930	.000518135
6	.000611247	1710	.000584795	4	.000560538	8	.000538213	2	.000517599
8	.000610500	12	.000584112	6	.000559910	1860	.000537634	4	.000517063
1640	.000609756	14	.000583430	8	.000559284	5	.000537057	6	.000516528
2	.000609013	16	.000582750	17 90		4	.000536480	8	.000515996
4	.000608272	18	.000582072	2	.000558035	6	.000535905	1940	.000515464
6	.000607533	1720	.000581395	4	.000557413	8	.000535332	2	.000514933
- 8	.000606796	2	.000580720	6	.000556793	1870	.000534759	4	.000514403
1650		4	.000580046	8	.000556174	2	.000534188	6	.000513874
2	.000605327	6	.000579374	18 00	.000555556	4	.000533618	8	.000513347
4	.000604595	8	.000578704	2	.000554939	6	.000533049	1950	.000512820
6	7000603865	1730	.000578035	4	.000554324	8	.000532481	2	.000512295
8	.000603136	2	.000577367	6	.000553710	1880		4	.000511770
1660	.000602410	4	.000576701	8	.000553097	2	.000531350	6	.000511247
2	.000601685	6	.000576037	18 10	.000552486	4	.000530785	8	.000510725
4	.000600962	8	.000575374	12	.000551876	6	.000530222	1960	
6	.000600240	1740	.000574713	14	.000551268	8	.000529661	2	.000509684
8	.000599520	2	.000574053	16	.000550661	1890	.000529100	4	.000509165
1670	.000598802	4	.000573394	18	.000550055	2	.000528541	6	.000508647
2	.000598086	6	.000572737	1820	.000549451	4	.000527983	8	.000508130
4	.000597371	8	.000572082	2	.000548848	6	.000527426	1970	.000507614
6	.000596658	1750	.000571429	4	.000548246	8	.000526870	2	.000507099
8	.000595947	2	.000570776	6	.000547645	1900		4	.600506585
1680	.000595238	4	.000570125	8	.000547046	2	.000525762	6	.000506073
2	.000594530	6	.000569476	1830	.000546448	4	.000525210	8	.000505561
4	.000593824	8	.000568828	2	.000545851	6	.000524659	1980	.000505051
6	.000593120	1760	.000568182	4	.000545256	8	.000524109	2	.000504541
8	.000592417	2	.000567537	6	.000544662	19 10	.000523560	4	.000504032
1690	.000591716	4	.000566893	8	.000544069	12	.000523012	6	.000503524
2	.000591017	6	.000566251	18 40	.000543478	14	.000522466	8	.000503018
4	.000590319	8	.000565611	2	.000542888	16	.000521920	1990	.000502513
6	.000589622	1770	.000564972	4	.000542299	18	.000521376	2	.000502008
8	.000588928	2	.000564334	6	.000541711	1920	.000520833	4	.000501504
1700	.000588235	4	.000563698	8	.000541125	2	.000520291	6	.000501002
2	.000587544	6	.000563063	1850	.000540540	4	.000519750	8	.000500501
4	.000586854	8	.000562430	5	.000539957	1 6	.000519211	2000	000500000

Use of reciprocals. - Reciprocals may be conveniently used to facilitate computations in long division. Instead of dividing as usual, multiply the dividend by the reciprocal of the divisor. The method is especially useful when many different dividends are required to be divided by the same divisor. In this case find the reciprocal of the divisor, and make a small table of its multiples up to 9 times, and use this as a multiplicationtable instead of actually performing the multiplication in each case.

Example. -9871 and several other numbers are to be divided by 1638. The reciprocal of 1638 is .000610500.

Multiples of the reciprocal:

> 8. .0048840

> 9. .0054945

1. .0006105 .0012210 .0018315 4. .0024420 .0030525 .0036630 .0042735

.0061050 10.

The table of multiples is made by continuous addition of 6105. The tenth line is written to check the accuracy of the addition, but it is not afterwards used.

Operation: Dividend 9871 Take from table 1..... .0006105 0.042735

00.48840 9..... 005.4945

Quotient..... 6.0262455 Correct quotient by direct division...... 6.0262515 The result will generally be correct to as many figures as there are significant figures in the reciprocal, less one, and the error of the next figure will in general not exceed one. In the above example the reciprocal has six significant figures, 610500, and the result is correct to five places of figures.

# SQUARES, CUBES, SQUARE ROOTS AND CUBE ROOTS OF NUMBERS FROM .1 TO 1600.

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root,
.1 .15 .2 .25	.01 .0225 .04 .0625 .09	.001 .0034 .008 .0156 027	.3162 .3873 .4472 .500 .5477	.4642 .5313 .5848 .6300 .6694	3.1 .2 .3 .4 .5	9.61 10.24 10.89 11.56 12.25	29.791 32.768 35.937 39.304 42.875	1.761 1.789 1.817 1.844 1.871	1.458 1.474 1.489 1.504 1.518
.35 .4 .45 .5	.1225 .16 .2025 .25 .3025	.0429 .064 .0911 .125 .1664	.5916 .6325 .6708 .7071 .7416	.7047 .7368 .7663 .7937 .8193	.6 .7 .8 .9 4.	12.96 13.69 14.44 15.21 16.	46.656 50.653 54.872 59.319 64.	1.897 1.924 1.949 1.975 2.	1.533 1.547 1.560 1.574 1.5874
.6 .65 .7 .75	.36 .4225 .49 .5625 .64	.216 .2746 .343 .4219 .512	.7746 .8062 .8367 .8660 .8944	.8434 .8662 .8879 .9086 .9283	.1 .2 .3 .4 .5	16.81 17.64 18.49 19.36 20.25	79.507	2.025 2.049 2.074 2.098 2.121	1.601 1.613 1.626 1.639 1.651
.85 .9 .95 1. 1.05	.7225 .81 .9025 1. 1.1025	.6141 .729 .8574 1.	.9219 .9487 .9747 1. 1.025	.9473 .9655 .9830 1. 1.016	.6 .7 .8 .9 5.	21.16 22.09 23.04 24.01 25.	97.336 103.823 110.592 117.649 125.	2.145 2.168 2.191 2.214 2.2361	1.663 1.675 1.687 1.698 1.7100
1.1 1.15 1.2 1.25 1.3	1.21 1.3225 1.44 1.5625 1.69	1.331 1.521 1.728 1.953 2.197	1.049 1.072 1.095 1.118 1.140	1.032 1.048 1.063 1.077 1.091	.1 .2 .3 .4 .5	26.01 27.04 28.09 29.16 30.25	132.651 140.608 148.877 157.464 166.375	2.258 2.280 2.302 2.324 2.345	1.721 1.732 1.744 1.754 1.765
1.85 1.4 1.45 1.5 1.55	1.8225 1.96 2.1025 2.25 2.4025	2.460 2.744 3.049 3.375 3.724	1.162 1.183 1.204 1.2247 1.245	1.105 1.119 1.132 1.1447 1.157	.6 .7 .8 .9 6.	31.36 32.49 33.64 34.81 36.	175.616 185.193 195.112 205.379 216.	2.366 2.387 2.408 2.429 2.4495	1.776 1.786 1.797 1.807 1.8171
1.65 1.65 1.7 1.75 1.8	2.56 2.7225 2.89 3.0625 3.24	4.096 4.493 4.913 5.359 5.832	1.265 1.285 1.304 1.323 1.342	1.170 1.182 1.193 1.205 1.216	.1 .2 .3 .4 .5	37.21 38.44 39.69 40.96 42.25	226.981 238.328 250.047 262.144 274.625	2.470 2.490 2.510 2.530 2.550	1.827 1.837 1.847 1.857 1.866
1.85 1.9 1.95 2.	3.4225 3.61 3.8025 4. 4.41	6.332 6.859 7.415 8. 9.261	1.360 1.378 1.396 1.4142 1.449	1.228 1.239 1.249 1.2599 1.281	.6 .7 .8 .9 7.	43.56 44.89 46.24 47.61 49.	287.496 300.763 314.432 328.509 343.	2.569 2.588 2.608 2.627 2.6458	1.876 1.885 1.895 1.904 1.9129
.2 .3 .4 .5 .6	4.84 5.29 5.76 6.25 6.76	10.648 12.167 13.824 15.625 17.576	1.483 1.517 1.549 1.581 1.612	1.301 1.320 1.339 1.357 1.375	.1 .2 .3 .4 .5	50.41 51.84 53.29 54.76 56.25	357.911 373.248 389.017 405.224 421.875	2.665 2.683 2.702 2.720 2.739	1.922 1.931 1.940 1.949 1.957
.7 .8 .9 <b>3</b> .	7.29 7.84 8.41 9.	19.683 21.952 24.389 27.	1.643 1.673 1.703 1.7321	1.392 1.409 1.426 1.4422	.6 .7 .8 .9	57.76 59.29 60.84 62.41	438.976 456.533 474.552 493.039	2.757 2.775 2.793 2.811	1.966 1.975 1.983 1.992

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
8.	64.	512.	2.8284	2.	45	2025	91125	6.7082	3.5569
.1	65.61	531.441	2.846	2.008	46	2116	97336	6.7823	3.5830
.2	67.24	551.368	2.864	2.017	47	2209	103823	6.8557	3.6088
.3	68.89	571.787	2.881	2.025	48	2304	110592	6.9282	3.6342
.4	70.56	592.704	2.898	2.033	49	2401	117649	7.	3.6593
.5 .6 .7 .8	72.25 73.96 75.69 77.44 79.21	614.125 636.056 658.503 681.472 704.969	$2.950 \\ 2.966$	2.041 2.049 2.057 2.065 2.072	50 51 52 58 54	2500 2601 2704 2809 2916	125000 132651 140608 148877 157464	7.0711 7.1414 7.2111 7.2801 7.3485	3.6840 3.7084 3.7325 3.7563 3.7798
9. .1 .2 .3 .4	81. 82.81 84.64 86.49 88.36	729. 753.571 778.688 804.357 830.584	3.017 3.033 3.050 3.066	2.0801 2.088 2.095 2.103 2.110	55 56 57 58 59	3025 3136 3249 3364 3481	166375 175616 185193 195112 205379	7.4162 7.4833 7.5498 7.6158 7.6811	3.8030 3.8259 3.8485 3.8709 3.8930
.5 .6 .7 .8	90.25 92.16 94.09 96.04 98.01	857.375 884.736 912.673 941.192 970.299	3.082 3.098 3.114 3.130 3.146	2.118 2.125 2.133 2.140 2.147	60 61 62 63 64	3600 3721 3844 3969 4096	216000 226981 238328 250047 262144	7.7460 7.8102 7.8740 7.9373 8.	3.9149 3.9365 3.9579 3.9791 4.
10	100	1000	3.1623	2.1544	65	4225	274625	8.0623	4.0207
11	121	1331	3.3166	2.2240	66	4356	287496	8.1240	4.0412
12	144	1728	3.4641	2.2894	67	4489	300763	8.1854	4.0615
13	169	2197	3.6056	2.3513	68	4624	314432	8.2462	4.0817
14	196	2744	3.7417	2.4101	69	4761	328509	8.3066	4.1016
15	225	3375	3.8730	2.4662	70	4900	343000	8.3666	4.1213
16	256	4096	4.	2.5198	71	5041	357911	8.4261	4.1408
17	289	4913	4.1231	2.5713	72	5184	373248	8.4853	4.1602
18	324	5832	4.2426	2.6207	73	5329	389017	8.5440	4.1793
19	361	6859	4.3589	2.6684	74	5476	405224	8.6023	4.1983
20	400	8000	4.4721	2.7144	75	5625	421875	8.6603	4.2172
21	441	9261	4.5826	2.7589	76	5776	438976	8.7178	4.2358
22	484	10648	4.6904	2.8020	77	5929	456533	8.7750	4.2543
23	529	12167	4.7958	2.8439	78	6084	474552	8.8318	4.2727
24	576	13824	4.8990	2.8845	79	6241	493039	8.8882	4.2908
25	625	15625	5.	2.9240	80	6400	512000	8.9443	4.3089
26	676	17576	5.0990	2.9625	81	6561	531441	9.	4.3267
27	729	19683	5.1962	3.	82	6724	551368	9.0554	4.3145
28	784	21952	5.2915	3.0366	83	6889	571787	9.1104	4.8621
29	841	24389	5.3852	3.0723	84	7056	592704	9.1652	4.3795
30	900	27000	5.4772	3.1072	85	7925	614125	9.2195	4.3968
31	961	29791	5.5678	3.1414	86	7396	636056	9.2736	4.4140
32	1024	32768	5.6569	3.1748	87	7569	658503	9.3276	4.4310
33	1089	35937	5.7446	3.2075	88	7744	681472	9.3808	4.4480
34	1156	39304	5.8310	3.2396	89	7921	704969	9.4340	4.4647
35	1225	42875	5.9161	3.2711	90	8100	729000	9.4868	4.4814
36	1296	46656	6.	3.3019	91	8281	753571	9.5394	4.4979
37	1369	50653	6.0828	3.3322	92	8464	778688	9.5917	4.5144
38	1444	54872	6.1644	3.3620	93	8649	804357	9.6437	4.5807
39	1521	59319	6.2450	3.3912	94	8836	830584	9.6954	4.5468
40	1600	64000	6.3246	3 4200	95	9025	857375	9 7468	4.6104
41	1681	68921	6.4031	3.4482	96	9216	884736	9.7980	
42	1764	74088	6.4807	3.4760	97	9409	912673	9.8489	
43	1849	79507	6.5574	3.5034	98	9604	941192	9.8995	
44	1936	85184	6.6332	3.5303	99	9801	970299	9.9499	

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	. Cube,	Sq. Root.	Cube Root,
100	10000	1000000	10.	1 6416	155	24025	9709975	12,4499	5:3717
100	10201	1030301	10.0199	4 6500	156	24336	3723875 3796416	19 4000	5.3832
101	10404	1061208	10.0199	4.6416 4.6570 4.6723	157	24649	3869893	12.4900 12.5300	5.3947
102 103	10404	1092727	10.0993	4.6875	158	24964	3944312	12.5698	5.4061
103	10816	1124864	10.1980	4.7027	159	25281	4019679	12.6095	
104	10010	1124004	10.1900	4.1021	100	20201	4019079	12.0000	5.4175
105	11025	1157625	10.2470	4.7177	160	25600	4096000	12.6491	5.4288
106	112 6	1191016	10.2956	4.7326	161	25921	4173281	12.6886	5.4401
107	11449	1225043	10.3441	4.7475	162	26244	4251528	12.7279	5 4514
108	11664	1259712	10.3923	4.7622	163	26569	4330747	12.7671	5.4626
109	11881	1295029	10.4403	4,7769	164	26896	4410944	12.8062	5.4737
110	12100	1331000	10.4881	4.7914	165	27225	4492125	12.8452	5.4848
111	12321	1367631	10.5357	4.8059	166	27556	4574296	12.8841	5.4959
112	12544	1404928	10.5830	4.8203		27889	4657463	12.9228	5.5069
113	12769	1442897	10.6301	4.8346		28224	4741632	12.9615	5.5178
114	12996	1481544	10.6771	4.8488	169	28561	4826809	13.0000	5.5288
115	13225	1520875	10.7238	4,8629	170	28900	4913000	13.0384	5.5397
116	13456	1560896	10.7703	4.8770	171	29241	5000211	13.0767	5.5505
117	13689	1601613	10.8167	4.8910 4.9049	172	29584	5088448	13.1149	5.5613
118	13924	1643032	10.8628	4:9049	173	29929	5177717	13.1529	5.5721
119	14161	1685159	10.9087	4.9187	174	30276	5268024	13,1909	5.5828
120	14400	1728000	10.9545	4.9324	175	30625	5359375	13,2288	5.5934
121	14641	1771561	11.0000	4.9461	176	30976	5451776	13.2665	5.6041
122	14884	1815848	11.0454	4.9597	177	31329	5545233	13.3041	5.6147
122 123	15129	1860867	11.0905	4.9732	178	31684	5639752	13.3417	5.6252
124	15376	1906624	11.1355	4.9866	179	32041	5735339	13.3791	5.6357
125	15625	1953125	11.1803	5.0000	180	32400	5832000	13.4164	5.6462
126	15876	2000376	11.2250	5.0133	181	32761	5929741	13.4536	5.6567
127	16129	2018383	11.2694	5.0265	182	33124	6028568	13.4907	5.6671
128	16384	2097152	11.3137	5.0397	183	33489	6128487	13.5277	5.6774
129	16641	2146689	11.3578	5.0528	184	33856	6229504	13.5647	5.6877
130	16900	2197000	11.4018	5.0658		34225	6331625	13.6015	5.6980
131	17161	2248091	11.4455	5.0788	186	34596	6434856	13.6382	5.7083
132	17424	2299968	11.4891	5.0916 5.1045	187	34969	6539203	13.6748	5.7185
133	17689	2352637	11.5326	5.1045	188	35344	6644672	13.6748 13.7113	5.7287
134	17956	2406104	11.5758	5.1172	189	35721	6751269	13.7477	5.7388
135	18225	2460375	11.6190	5.1299	190	36100	6859000	13.7840	5.7489
136	18496	2515456	11.6619	5.1426		36481	6967871	13.8203	5.7590
137	18769	2571353	11.7047	5.1551	192	36864	7077888	13.8564	5.7690
138	19044	2628072	11.7473	5.1676		37249	7189057	13.8924	5 7790
139	19321	2685619	11.7898	5.1801	194	37636	7301384	13.9284	5.7890
140	19600	2744000	11.8322	5.1925	195	38025	7414875	13.9642	5.7989
141	19881	2803221	11.8743	5.2048		38416	7529536	14.0000	5.8088
142	20164	2863288	11.9164	5.2171 5.2293	197	38809	7645373	14.0357	5.8186
143	20449	2924207	11.9583	5.2293	198	39204	7762392	14.0712	5.8285
144	20736	2985984	12.0000	5.2415	199	39601	7880599	14.1067	5.8383
145	21025	3048625	12.0416	5.2536	200	40000	8000000	14.1421	5.8480
146	21316	3112136	12.0830	5.2656	201	40401	8120601	14.1774	5.8578
147	21609	3176523	12.1244	5.2776	202	40804	8242408	14.2127	5.8675
148	21904	3241792	12.1655	5.2896	203	41209	8365127	14.2478 14.2829	5.8771
149	22201	3307949	12.2066	5.3015	204	41616	8489664	14.2829	5.8868
150	22500	3375000	12.2474 12.2882	5.8133	205	42025	8615125	14.3178	5.8964
151	22801	-3442951	12.2882	5.1251	206	42436	8741816	14.3527	5.9059
152	23104	3511803	12.3288	5.3368	207	42849	8869743	14.3875	5.9155
153	23409	3581577	12.3693	5.3485	208	43264	8998912	14.4222	5.9250
154	23716	3652264	112 4097	5.3601	200	43681	9129329	14.4568	5.9345

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square,	Cube,	Sq. Root.	Cube Root.
210	44100	9261000	14.4914	5.9439	265	70225	18609625	16.2788	6.4232
211	44521	9393931	14.5258	5.9533	266	70756	18821096	16.3095	6.4312
212 213	44944 45369	9528128 9663597	14.5602 14.5945	5.9627 5.9721	267 268	71289 71824	19034163 19248832	16.3401 16.3707	6.4393
214	45796	9800344	14.6287	5.9814	269	72361	19465109	16.4012	6.4553
215	46225	9938375	14.6629	5 9907	270	72900	19683000	16 4317	6.4633
216 217	46656	10077696 10218313	14.6969 14.7309	6.0000	271 272	73441 73984	19902511 20123648	16.4621 16.4924	6.4713 6.4792
218	47524	10360232	14.7648	6.0185	273	74529	20346417	16,5227	6.4872
219	47961	10503459	14.7986	6 0277	274	75076	20570824	16.5529	6.4951
220	48400	10648000	14.8324	6:0368	275.	75625	20796875	16.5831	6.5030
221 222	48841 49284	10793861 10941048	14.8661 14.8997	6.0459	276 277	76176 76729	21024576 21253933	16.6132 16.6433	6.5108 6.5187
223	49729	11089567	14.9332	6.0641	278	77284	21484952	16.6733	6.5265
224	50176	11239424	14.9666	6.0732	279	77841	21717639	16.7033	6.5343
225	50625	11390625	15.0000	6.0822	280	78400	21952000	16.7332	6.5421
226 227	51076 51529	11543176 11697083	15.0333 15.0665	6.0912	281 282	78961 79524	22188041 22425768	16.7631 16.7929	6.5499
228	51984	11852352	15.0997	6.1091	283	80089	22665187	16.8226	6.5654
229	52441	12008989	15.1327	6.1180	284	80656	22906304	16.8523	6.5731
230	52900	12167000	15.1658	6.1269	285	81225	23149125	16.8819	6.5808
231 232	53361 53824	12326391 12487168	15.1987 15.2315	6.1358 6.1446	286 287	81796 82369	23393656 23639903	16.9115 16.9411	6.5885 6.5962
233	54289	12649337	15.2643	6.1534	288	82944	23887872	16.9706	6.6039
234	54756	12812904	15.2971	6.1622	289	83521	24137569	17.0000	6.6115
235	55225	12977875	15.3297	6.1710	290	84100	24389000	17.0294	6.6191
236 237	56169	13144256 13312053	15.3623 15.3948	6.1797 6.1885	291 292	84681 85:264	24642171 24897088	17.0587 17.0880	6.6267
238	56644	13481272	15.4272	6.1972	293	85849	25153757	17.1172	6,6419
239	57121	13651919	15.4596	6.2058	294	86436	25412184	17.1464	6.6494
240	57600	13824000	15.4919	6.2145	295	87025	2567:375	17.1756	6.6569
241 242	58081 58564	13997521	15.5242	6.2231 6.2317	296 297	87616 88209	25934336	17.2047	6.6644
243	59049	14172488 14348907	15.5563 15.5885	6.2403	298	88804	26198073 26463592	17.1756 17.2047 17.2337 17.2627	6.6719
244	59536	14526784	15.6205	6.2488	299	89401	26730899	17.2916	6.6869
245	60025	14706125	15.6525	6.2573	300	90000	27000000	17.3205	6.6943
246	60516	14886936	15.6844	6.2658	301	90601	27270901	17.3494	6.7018
247 248	61009 61504	15069223 15252992	15.7162 15.7480	6.2743	303 303	91204 91809	27543608 27818127	17.3781 17.4069	6.7092 6.7166
249	62001	15438249	15.7797	6.2912	304	92416	28094464	17 4356	6.7240
250	62500	15625000	15.8114	6.2996	305	93025	28372625	17.4642	6.7313
251	63001	15813251	15.8430	6.3080	306	93636	28652616	17.4642 17.4929 17.5214	6.7387 6.7460
252 253	63504 64009	16003008 16194277	15.8745 15.9060	6.3164 6.3247	307 308	94249 94864	28934443 - 29218112	17.5214 17.5499	6.7460 $6.7533$
254	64516	16387064	15.9374	6.3330	309	95481	29503629	17.5784	6.7606
255	65025	16581375	15.9687	6.3413	310	96100	29791000	17.6068	6.7679
256 257	65536 66049	16777216 16974593	16.0000 16.0312	6.3496	311 312	96721 97344	30080231 30371328	17.6352 17.6635	6.7752
258	66564	17173512	16.0624	6.3661	313	97969	30664297	17.6918	6.7897
259	67081	17373979	16.0935	6.3743	314	98596	30959144	17.7200	6.7969
260	67600	17576000	16.1245	6 3825	815	99225	31255875	17.7482	6.8041
261 262	68121 68644	17779581 17984728	16.1555 16.1864	6.3907	316 317	99856 100489	31554496	17.7482 17.7764 17.8045	6.8113
263	69169	18191447	16.2173	6.4070	318	101124	31855013 32157432	17.8045	6.8185 6.8256
264	69696	18399744	16.2481			101761	33461759	17.8606	6.8328

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
320	102400	32768000	17.8885	6.8399	375	140625	52734375	19.3649	7.2112
321	103041	33076161	17.9165	6.8470	376	141376	53157376	19.3907	7.2177
322	103684	33386248	17.9444	6.8541	377	142129	53582633	19.4165	7.2240
323	104329	33698267	17.9722	6.8612	378	142884	54010152	19.4422	7.2304
324	104976	34012224	18.0000	6.8683	379	143641	54439939	19.4679	7.2368
825	105625	34328125	18.0278	6.8753	380	144400	54872000	19.4936	7.2432
326	106276	34645976	18.0555	6.8824	381 382	145161 145924	55306341	19.5192 19.5448	7.2495
327 328	106929 107584	34965783 35287552	18.0831 18.1108	6.8964	383	146689	55742968 56181887	16.5704	7.2558 7.2622
329	108241	35611289	18.1384	6.9034	384	147456	56623104	19.5959	7.2685
S30	108900	35937000	18.1659	6.9104	385	148225	57066625	19.6214	7.2748
331	109561	36264691	18.1934	6.9174	386	148996	57512456	19.6469	7.2811
332	110224	36594368	18.2209	6.9244	387	149769	57960603	19.6723	7.2874
333 334	110889 111556	36926037 37259704	18.2483 18.2757	6.9313 6.9382	388 389	150544 151321	58411072 58863869	19.6977 19.7231	7.2936 7.2999
385	112225	37595375	18.3030	6.9451	390	152100	59319000	19.7484	7.3061
386	112896	37933056	18.3303	6.9521	391	152881	59776471	19.7737	7.3124
337	113569	38272753	18.3576	6.9589	392	153664	60236288	19.7990	7.3186
338	114244	38614472	18.3848	6.9658	393	154449	60698457	19.8242	7.3186 7.3248
339	114921	38958219	18.4120	6.9727	394	155236	61162984	19.8494	7.3310
340	115600	39304000	18.4391	6.9795	395	156025	61629875	19.8746	7.3372
341	116281	39651821	18.4662	6.9864		156816	62099136	19.8997	7.3434
342 343	116964 117649	40001688 40353607	18.4932 18.5203	6 9932		157609 158404	62570773 63044792	19.9249 19.9499	7.3496
344	118336	40707584	18.5472		399	159201	63521199	19.9750	7.3619
345	119025	41063625	18.5742	7.0136	400	160000	64000000	20 0000	7.3681
346	119716	41421736	18.6011	7.0203	401	160801	64481201	20 0250	7.3742
347	120409	41781923	18.6279	7.0271	402	161604	64964808	20.0499	7.3803 7.3864
348	121104	42144192	18.6548	7.0338	403	162409	65450827	20 0749	7.3864
349	121801	42508549	18.6815	7.0406	404	163216	65939264	20.0998	7.3925
350	122500	42875000	18.7083	7.0473	405	164025	66430125	20.1246	7.3986
351	123201	43243551	18.7350	7.0540	406	164836	66923416	20.1494	7.4047
352 353	123904	43614208	18.7617 18.7883	7.0607 7.0674	407	165649	67419143	20.1742	7.4108
354	124609 125316	43986977 44361864	18.8149	7.0740		166464 167281	67917312 68417929	20.1990 20.2237	7.4169 7.4229
355	126025	44738875	18.8414	7.0807	410	168100	68921000	20.2485	7.4290
3 6	126736	45118016	18.8680	7.0873		168921	69426531	20.2731	7.4350
357	127449	45499293	18.8944	7.0940	412	169744	69934528	20.2978	7 4410
358 359	128164 128881	45882712 46268279	18 9209 18 9473	$7.1006 \\ 7.1072$	413 414	170569 171396	70444997 70957944	20.3224 20.3470	7.4470 7.4530
360	129600	46656000	18.9737	7.1188	415	172225	71473375	20.3715	7.4590
361 362	130321 131044	47045881 47437928	19.0000 19.0263	7.1188 7.1204 7.1269	416 417	173056 173889	71991296 72511713	20.3961	7.4650
363	131769	47832147	17.0526	7.1335	418	174724	73034632	20.4206 20.4450	7.4710 7.4770
364	132496	48228544	19.0788	7.1400	419	175561		20.4695	7.4829
365	133225	48627125	19.1050	7.1466	420	176400	74088000	20,4939	7.4889
366	133956	49027896	19.1311	7.1531	421	177241	74618461	20.5183	7.4948
367	134689	49430863	19.1572	7.1596	422	178084	75151448	20.5426	7.5007
368 369	135424 136161	49886032 50243409	19.1833 19.2094	7.1661 7.1726	423 424	178929 179776	75686967 76225024	20.5670 20.5913	7.5067 7.5126
370	136900	50653000	19.2354	7 1701	105	180625			
371	137641	51064811	19.2554	7 1855	426	181476	76765625 77308776	20.6155 20.6398	7.5185
872	188384	51478848	19.2873	7 1990	427	182329	77854483	20.6640	$7.5244 \\ 7.5302$
873 874	139129	51895117	19.3132 19.3391	7.1855 7.1920 7.1984 7.2048	428	183184 184041	78402752	20 6882 20.7123	7.5361

	·								
No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
430	184900	79507000	20.7364	7.5478	485	235225	114084125	22.0227	7.8568
431	185761	80062991	20.7605	7.5537	486	236196	114791256	22.0454	7.8622
432	186624	80621568	20.7846	7.5595	487	237169	115501303	22.0681	7.8676
433 434	187489 188356	S1182737 81746504	20,8087 20,8327	7.5654 7.5712	488 489	238144 239121	116214272 116930169	22.0907 22.1133	7.8730 7.8784
435	189225	82312875	20.8567	7.5770	490	240100	117649000	22.1359	7.8837
436 437	190096 190969	82881856 83453453	20.8806 20.9045	7.5828 7.5886	491 492	241081 242064	118370771 119095488	22.1585 22.1811	7.8891
438	191844	84027672	20.9284	7.5944	492	243049	119823157	22.2036	7.8998
439	192721	84604519	20.9523	7.6001	494	244036	120553784	22.2261	7.9051
440	193600	85184000	20.9762	7.6059	495	245025	121287375	22.2486	7.9105
441 442	194481 195364	85766121 86350888	21.0000 21.0238	7.6117 7.6174	496 497	246016 247009	122023936 122763473	22.2711 22.2935	7.9158
443	196249	86938307	21.0476	7.6232	498	248004	123505992	22.3159	7.9211 7.9264
444	197136	87528384	21.0713	7.6289	499	249001	124251499	22 3383	7.9317
445	198025	88121125	21.0950	7.6346	500	250000	125000000	22.3607	7.9370
446 447	198916 199809	88716536 89314623	21.1187 21.1424	7.6460	501 502	251001 252004	125751501 126506008	22.3830 22.4054	7.9423 $7.9476$
448	200704	89915392	21.1660	7.6403 7.6460 7.6517	503	253009	127263527	22.4277	7.9528
449	201601	90518849	21.1896	7.6574	504	254016	128024064	22.4499	7.9581
450	202500	91125000	21.2132	7.6631	505	255025	128787625	22,4722	7.9634
451 452	203401 204304	91733851 92345408	21.2368 21.2603	7.6688 7.6744	506 507	256036 257049	129554216 130323843	22.4944 22.5167	7.9686
453	205209	92959677	21.2838	7.6800	508	258064	131096512	22.5389	7.9791
454	206116	93576664	21.3073	7.6857	509	259081	131872229	22.5610	7.9843
455	207025	94196375	21.3307	7.6914	510	260100	132651000	22.5832	7.9896 7.9948
456 457	207936 208849	94818816 95443993	21.3542 21.3776	7.6970 7.7026	511 512	261121 262144	133432831 134217728	22.6053 22.6274	8.0000
458	209764	96071912	21 4009	7.7002	513	263169	135005697	22.6495	8.0052
459	210681	96702579	21,4243	7.7138	514	264196	135796744	22.6716	8.0104
460	211600	97336000	21.4476	7.7194	515	265225	136590875	22.6936	8.0156
461 462	212521 213444	97972181 98611128	21.4709 21.4942	7.7250 7.7306		266256 267289	137388096 138188413	22.7156 22.7376	8.0208 8.0260
463	214369	99252847	21.5174	7.7362		268324	138991832	22.7596	8.0311
464	215296	99897344	21.5407	7.7418	519	269361	139798359	22.7816	8.0363
465	216225	100544625	21.5639	7.7473	520	270400	140608000	22.8035	8.0415
466 467	217156 218089	101194696 101847563	21.5870 21.6102	7.7529 7.7584	521 522	271441 272484	141420761 142236648	22.8254 22.8478	8.0466
468	219024	102503232	21.6333	7.7639 7.7695	523	273529	143055667	22.8692	
469	219961	103161709	21.6564	7.7695	524	274576	143877824	22.8910	8.0620
470	220900	103823000	21.6795 21.7025	7.7750	525	275625	144703125	22.9129	
471	221841	104487111	21.7025	7.7750 7.7805 8.7860	526	276676	145531576	22.9347	8.0723
472 473	222784 223729	105154048 105823817	21.7256 21.7486	7.7915	528	277729 278784	146363183 147197952	22.9565 22.9783	
474	224676	106496424	21.7715	7.7970	529	279841	148035889	23.0000	8.0876
475	225625	107171875	21.7945	7.8025	530	280900	148877000	23.0217	
476 477	226576 227529	107850176 108531333	21.8174	7.8079 7.8134	531 532	281961 283024	149721291 150568768	23.0434 23.0651	
478	228484	109215352	21.8632	7.8188	533	284089	151419437	23.0868	8.1079
479	229441	109902239	21.8861	7.8243	534	285156	152273304	23.1084	
480	230400	110592000	21.9089	7.8297	535	286225	153130375	23.1301	8.1180
481 482	231361 232324	111284641 111980168	21.9317	7.8352	536	287296 288369	153990656 154854153	23.1517 23.1733	8.1231 8.1281
483	233289	112678587	21.9773	7.8406 7.8460 7.8514	538	289444	155720872	23.1948	
484	234256	113379904	22.0000	7.8514	539	290521	156590819	23.2164	8.1382

No.	Square.	Cube.	Sq. Root,	Cube Root.	No.	Square.	Cube.	Sq. Root,	Cube Root.
F 40	001600	150101000	09 0970	P 1499	595	354025	010044000	04 9000	0.4100
540 541	291600 292681	157464000 158340421	23.2379 23.2594	8.1433 8.1483	596	355216	210644875 211708736	24.3926 24.4131	8.4108 8.4155
542	293764	159220088	23.2809	8.1533	597	356409	212776173	24.4336	8.4202
543	294849	160103007	23.3024	8.1583	598	357604	213847192	24.4540	8.4249
544	295936	160989184	23.3238	8.1633	599	358801	214921799	24.4745	8.4296
545	297025	161878625	23.3452	8.1683	600	360000	216000000	24.4949	8 4343
546	298116	162771336	23.3666	8.1733	601	361201	217081801	24.5153	8.4390
547	299209 300304	163667323	23.3880 23.4094	8.1783	602 603	362404 363609	218167208	24.5357	8.4437
548 549	301401	164566592 165469149	23.4307	8.1833 8.1882	604	364816	219256227 220348864	24.5561 24.5764	8.4484 8.4530
550	302500	166375000	23.4521	8.1932	605	366025	221445125	24.5967	8,4577
551	305601	167284151	23.4734	8.1982	606	367236	222545016	24.6171	8.4623
552	304704	168196608	23.4947	8.2031	607	368449	223648543	24.6374	8.4670
553	305809	169112377	23.5160	8,2081	608	369664	224755712	24.6577	8.4716
554	306916	170031464	23.5372	8.2130	609	370881	225866529	24.6779	8.4763
555	308025	170953875	23.5584	8.2180	610	372100	226981000	24 6982	8.4809
556	309136	171879616	23.5797	8.2229	611	373321	228099131	24.7184	8.4856
557	310249	172808693	23.6008	8.2278 8.2327	612	374544	229220928	24 7386	8.4902
558 559	311364 312481	173741112 174676879	23.6220 23.6432	8.2377	613 614	375769 376996	230346397 231475544	24.7588 24.7790	8.4948 8.4994
560	313600	175616000	23.6643	8.2426	615	378225	232608375	24.7992	8.5040
561	314721	176558481	23.6854	8.2475	616	379456	233744896	24.8193	8.5086
562	315844	177504328	23.7065	8.2524	617	380689	234885113	24.8395	8.5132
563	316969	178453547	23.7276	8.2573	618	381924	236029032	24.8596	8.5178
564	318096	179406144	23.7487	8.2621	619	383161	237176659	24.8797	8.5224
565	319225	180362125	23.7697	8.2670	620	384400	238328000	24.8998	8.5270
566	320356	181321496	23.7908	8.2719	621	385641	239483061	24.9199	8.5316
567 568	321489 322624	182284263 183250432	23.8118 23.8328	8.2768 8.2816	622 623	386884 388129	240641848 241804367	24.9399 24.9600	8.5362 8.5408
569	323761	184220009	23.8537	8.2865	624	389376	242970624	24.9800	8.5453
570	324900	185193000	23.8747	8.2913	625	390625	244140625	25,0000	8.5499
571	326041	186169411	23.8956	8.2962	626	391876	245314376	25.0200	8.5544
572	327184	187149248	23.9165	8.3010	627	393129	246491883	25.0400	8.5590
573	328329	188132517	23.9374	8.3059	628	394384	247673152	25.0599	8.5635
574	329476	189119224	23,9583	8.3107	629	395641	248858189	25.0799	8.5681
575 .	330625	190109375	23.9792	8.3155	630	396900	250047000	25.0998	8.5726
576	331776	191102976	24.0000	8.3203	631	398161	251239591	25.1197	8.5772
577 578	332929 334084	192100033 193100552	24.0208 24.0416	8.3251 8.3300	632 633	399424 400689	252435968 258636137	25,1396 25,1595	8.5817
579	335241	194104539	24.0624	8.3348		401956	254840104	25.1794	8.5862 8.5907
580	336400	195112000	24.0832	8.3396	635	403225	256047875	25,1992	8.5952
581	337561	196122941	24.1039	8.3443	636	404496	257259456	25.2190	8.5997
582	338724	197137368	24.1247	8.3491	637	405769	258474853	25.2389	8.6043
583	339889	198155287	24.1454	8.3539	638	407044	259694072	25.2587	8.6088
584	341056	199176704	24.1661	8.3587	639	408321	260917119	25.2784	8.6132
585	342225	200201625	24.1868	8.3634	640	409600	262144000	25.2982	8.6177
586	343396	201230056	24.2074 24.2281	8.3682	641	410881	263374721	25.3180	8.6222
587 588	344569 345744	202262003 203297472	24.2281	8.3777	642 643	412164 413449	264609288 265847707	25.3377 25.3574	8.6267
589	346921	204336469	24.2693	8.3825	644	414736	267089984	25.3772	8.6312 8.6357
590	348100	205379000	24.2899	8.3872	645	416025	268336125	25.3969	8.6401
591	349281	206425071	24 3105	8.3919	646	417316	269586136	25.4165	8 6446
592	350464	207474688	24.3311	8.3967	647	418609	270840023	25.4362	8.6490
593	351649	208527857	24.3516	8.4014	648	419904	272097792	25.4558	8.6585
594	352836	209584584	24.3721	8.4061	# 049	421201	273359449	25.4755	8.6579

No.	Square.	Cube.	Sq. Root.	Cube Root,	No.	Square.	Cube.	Sq. Root.	Cube Root.
650	422500	274625000	25,4951	8.6624	705	497025	350402625	26.5518	8.9001
651	423801	275894451	25.5147	8.6668	706	498436	351895816	26.5707	8.9043
652	425104	277167808	25.5343	8.6713	707	499849	353393243	26.5895	8.9085
653	426409	278445077	25.5539	8.6757	708	501264	354894912	26.6083	8,9127
654	427716	279726264	25.5734	8.6801	709	502681	356400829	26.6271	8.9169
655	429025	281011375	25.5930	8.6845		504100	357911000	26.6458	8.9211
656	430336	282300416	25.6125	8.6890	711	505521	359425431	26.6646	8.9253
657	431649	283593393	25.6320	8.6934	712	506944	360944128	26.6833	8.9295
658 659	432964 434281	284890312 286191179	25.6515 25.6710	8 6978 8.7022		508369 509796	362467097 363994344	26,7021 26,7208	8.9337 8.9378
059	404201	200191179	25.0710	0.1022	114	309790	909994944	20.1200	0.0010
660	435600	287496000	25,6905	8.7066	715	511225	365525875	26.7395	8.9420
661	436921	288804781	25.7099	8.7110	716	512656	367061696	26.7582	8.9462
662	438244	290117528	25 7294	8.7154	717	514089	368601813	26.7769	8.9503
663	439569	291434247	25.7488	8.7198	718	515524	370146232	26.7955	8.9545
664	440896	292754944	25.7682	8.7241	719	516961	371694959	26.8142	8.9587
665	442225	294079625	25.7876	8.7285	720	518400	373248000	26.8328	8.9628
666	443556	295408296	25.8070	8.7329	721	519841	374805361	26.8514	8.9670
667	444889	296740963	25.8263	8.7373	722	521284	376367048	26.8701	8.9711
668	446224	298077632	25.8457	8.7416		522729	377933067	26.8887	8.9752
669	447561	299418309	25.8650	8.7460	724	524176	379503424	26,9072	8.9794
670	448900	300763000	25.8844	8.7503	725	525625	381078125	26.9258	8.9835
671	450241	302111711	25.9037	8.7547	726	527076	382657176	26.9444	8.9876
672 673	451584	303464448	25.9230		727	528529	384240583	26.9629	8.9918
673	452929	304821217	25.9422		728	529984	385828352	26.9815	8.9959
674	454276	306182024	25.9615	8.7677	729	531441	387420489	27.0000	9.0000
675	455625	307546875	25.9808	8.7721	730	532900	389017000	27 0185	9 0041
676	456976	308915776	26.0000		731	534361	390617891	27.0370	9.0082
677	458329	310288733	26.0192		732	535824	392223168	27.0555	9.0123
678	459684	311665752	26.0384	8.7850	733	537289	393832837	27.0740	9.0164
679	461041	313046839	26.0576		734	538756	395446904	27.0924	9.0205
680	462400	314432000	26.0768		735	540225	397065375	27.1109 27.1293 27.1477 27.1662	9.0246
681	463761	315821241	26.0960		736	541696	398688256	27.1293	9.0287
682	465124	317214568	26.1151	8.8023	737	543169	400315553	27.1477	9.0328
683 684	466489 467856	318611987 320013504	26.1343 26.1534			544644 546121	401947272 403583419	27.1846	9.0369
	1		10.				1		
685	469225 470596	321419125 322828856	26.1725 26.1916		740	547600	405224000	27,2029	9.0450 9.0491
686 687	471969	324242703	26.2107		741 742	549801 550564	406869021 408518488	27.2213 27.2397	9.0491
688	473344	325660672	26.2298	8.8280	743	552049	410172407	27.2580	9.0572
689	474721	327082769	26,2488	8.8323	744	553536	411830784	27.2764	9.0613
690	476100	328509000	26.2679	8.8366	745	555025	413493625	27.2947 27.3130	9.0654
691	477481	329939371	26.2869	8.8408	746	556516	415160936	27.3130	9.0694
692	478864	331373888	26.3059		747	558009	416832723	27.3313	9.0735
693	480249	332812557	26.3249			559504	418508992	27.3496	9.0775
694	481636	334255384	26,3439			561001	420189749	27.3679	ł
695	483025	335702375	26.3629		750	562500	421875000	27.3861	9.0856
696 697	484416 485809	337153536 338608873	26.3818 26.4008		751 752	564001 565504	423564751 425259008	27.4044	9.0896 9.0937
698	487204	340068392	26.4008	8 8708	753	567009	426957777	27 4408	9.0937
699	488601	341532099	26.4386	8.8706 8.8748	754	568516	428661064	27.4226 27.4408 27.4591	9.1017
700	490000	343000000	26.4575	1	755	570025	430368875	27.4773	
701	491401	344472101	26.4764			571536	432081216	27.4955	9.1098
702	492804	345948408	26.4953			573049	433798093	27.5136	9.1138
703	494209	347428927	26.5141	8.8917	758	574564	435519512	27.5318	9.1178
704	495616	348013664	26.5330	8.8959	759	576081	437245479	27.5500	9.1218

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
760	577600	438976000	27.5681	9.1258	815	664225	541343375	28.5482	9.3408
761	579121	440711081	27.5862	9.1298	816	665856	543338496	28.5657	9.3447
762	580644	442450728	27.6043	9.1338	817	667489	545338513	28.5832	9.3485
763 764	582169 583696	441194947 445943744	27.6225	9.1378 9.1418	818 819	669124	547343432 549353259	28,6007	9.3523 9.3561
				0.1410					
765	585225	447697125	27.6586	9.1458	820	672400	551368000	28.6356	9.3599
766 767	586756 588289	449455096 451217663	27 6048	9.1498 9.1537	821 822	674041 675684	558387661 555412248	28.6531	9.3637 9.3675
768	589824	452984832	27.7128	9.1577	823	677329	557441767		9.3713
769	591361	454756609	27.7308	9.1617	824	678976	559476224	28.7054	9.3751
770	592900	456533000	27 7489	9.1657	825	680625	561515625	28 7228	9.3789
771	594441	456533000 458314011	27.7669	9.1696	S26	682276	563559976	28.7402	9.8827
772	595984	460099648	27.7849	9.1736	827	683929	565609283	28.7576	9.3865
771 772 773 774	597529 599076	461889917 463684824	27.8029	9.1775 9.1815	828 829	685584 687241	567663552 569722789	28.7750	9.3902 9.3940
775	600625	465484375		9.1855	830	688900	571787000		9.3978
776	602176 603729	467288576 469097433	27 8747	9.1894 9.1933	831 832	690561 692224	573856191 575930368		9.4016 9.4053
777 778	605284	470910952	27.8927	9.1978	S83	693889	578009537	28.8617	9.4091
779	606841	472729139	27.9106	9.2012	834	695556	580093704	28.8791	9.4129
780	608400	474552000	27 9285	9.2052	835	697225	582182875	28.8964	9.4166
781	609961	476379541	27.9464	9.2091	836	698896	584277056	28.9137	9.4204
782	611524	478211768	27.9643	9.2130	837	700569	586876258		9.4241
783 784	613089 614656	480048687 481890304		9.2170 9.2209	838 839	702244 703921	588480472 590589719	28.9482	9.4279 9.4316
									3.4010
785	616225	483736625		9.2248	840	705600	592704000		9.4354
786 787	617796 619369	485587656 487443403		9.2287 9.2326	841 842	707281 708964	594823321 596947688	29.0000 29.0172	9.4391 9.4429
788	620944	489303872		9.2365	843	710649	599077107	29.0345	9.4466
789	622521	491169069	28.0891	9.2404	844	712336	601211584	29.0517	9.4503
790	624100	493039000	28.1069	9.2443	845	714025	603351125	29.0689	9,4541
791	625681	494913671	28.1247	9.2482	846	715716	605495736	29.0861	9.4578
792	627264	496793088	28.1425	9.2521	847	717409	607645423	29.1033	9.4615
793 794	628849 630436	498677257 500566184	28.1603 $28.1780$	9.2560 9.2599	848 849	719104 720801	609800192 611960049	29.1204	9.4652 9.4690
795 796	632025 633616	502459875	28.1957 28.2135	9.2638 9.2677	850	722500 724201	614125000		9.4727
797	635209	504358336 506261573	28.2312	9.2716	851 852	725904	616295051 618470208	29.1719	9.4764 9.4801
798	636804	508169592	28,2489	9.2754	853	727609	620650477	29.2062	9.4838
799	638401	510082399	28.2666	9.2793	854	729316	622835864	29.2233	9.4875
800	640000	512000000	28.2843	9.2832	855	731025	625026375	29.2404	9.4912
801	641601	513922401	28.3019	9.2870	856	732736	627222016	29.2575	9.4949
802 803	643204 644809	515849608 517781627	28.3196	9.2909 9.2948	857 858	734449 736164	629422793 631628712	29.2746	9 4986
804	646416	519718464	28.3549	9.2986	859	737881		29.2916 29.3087	9 5023 9.5060
805 806	648025 649636	521660125 523606616		9.3025 9.3063	860 861	739600 741321		29.3258 29.3428	9.5097 9.5134
807	651249	525557943	28.4077	9.3102	862	743044	640503928	29.3598	9.5171
808	652864	527514112		9.3140	863	744769	642735647		9.5207
809	654481	529475129	28.4429	9.3179	864	746496	644972544	29.3939	9.5244
810	656100	531441000		9.3217	865	748225	647214625		9.5281
811	657721 659344	533411731 535387328	28.4781	9.3255 9.3294	866 867	749956 751689	649461896	29.4279	9.5317
812 813	660969	585887828 587367797	28 5139	9.3332	868	753424	651714368 653972032	29.4449	9.5354 9.5391
814	662596	539353144	28.5307	9.3370	869		656234909	29.4788	9.5427
					-				

No.   Square   Cube   Roct										
871         758841         660776311 99.5127         9.5501         926         857470         79.022776 30.4902         9.7470         9.7507         926         857470         79.022776 30.4902         9.7470         9.7505         926         855470         79.7505         928         861184         79.7505         9.7575         875         762626         665287624 99.5635         9.5161         929         863018         71765069         9.7610         929         864900         804357000         30.4631         9.7616         875         765625         669921875 29.5831         9.5637         9.7179         938         864900         804357000         30.4959         9.7610         8577781         932         864900         804357000         30.4959         9.7610         8577781         932         86801         86561529         9.7811         9.7579         938         870489         8812166237         30.5400         9.7715         888         877614         85778781         99.6816         9.5855         935         870498         870498         88072856         8305303         30.5101         9.7785         883         870498         88176749         88367899         89.6810         9.887696         88006289         9.7879         9.887799         8800 </th <th>No.</th> <th>Square.</th> <th>Cube.</th> <th></th> <th></th> <th>No.</th> <th>Square.</th> <th>Cube,</th> <th>Sq. Root.</th> <th></th>	No.	Square.	Cube.			No.	Square.	Cube,	Sq. Root.	
871         758841         660776311 99.5127         9.5501         926         857470         79.022776 30.4902         9.7470         9.7507         926         857470         79.022776 30.4902         9.7470         9.7505         926         855470         79.7505         928         861184         79.7505         9.7575         875         762626         665287624 99.5635         9.5161         929         863018         71765069         9.7610         929         864900         804357000         30.4631         9.7616         875         765625         669921875 29.5831         9.5637         9.7179         938         864900         804357000         30.4959         9.7610         8577781         932         864900         804357000         30.4959         9.7610         8577781         932         86801         86561529         9.7811         9.7579         938         870489         8812166237         30.5400         9.7715         888         877614         85778781         99.6816         9.5855         935         870498         870498         88072856         8305303         30.5101         9.7785         883         870498         88176749         88367899         89.6810         9.887696         88006289         9.7879         9.887799         8800 </td <td>870</td> <td>756900</td> <td>658503000</td> <td>29 4958</td> <td>9 5464</td> <td>925</td> <td>855625</td> <td>791453125</td> <td>30.4138</td> <td>9.7435</td>	870	756900	658503000	29 4958	9 5464	925	855625	791453125	30.4138	9.7435
873 769219 665388617 29.5646 9.5571 928 861184 709178752 30.4631 9.7510 876 765625 667027624 29.5635 9.5610 929 863041 801765089 30.4705 9.7575 875 765625 667027624 29.5637 3.5653 931 806701 806054491 30.5123 9.7610 876 76726 672221376 93.5653 931 806701 806054491 30.5123 9.7610 876 776844 676580132 9.6311 9.5756 938 870489 812166237 30.5450 9.7718 932 868024 80557568 30.5287 9.7680 877 870844 676580132 9.6311 9.5756 938 870489 812166237 30.5450 9.7718 932 868024 80557588 30.5450 9.7718 932 868024 80557588 30.5287 9.7680 877 870844 8708249 9.6470 9.7729 934 872355 814780349 30.5101 9.7730 889 774400 861478000 29.6468 9.5828 80.5585 9.6885 9.6885 9.5885	871		660776311	29.5127	9.5501	926	857476	794022776	30.4302	9.7470
874 768876 667627624 19.5663 9.5610 929 863041 801765089 30.4795 9.7575 876 768736 669921875 29.5804 9.5647 93.808060 804857000 30.4959 9.7610 876 768736 672821876 29.5814 9.5756 938 876198 809557568 30.4957 9.7681 879 772641 679151439 29.6479 9.5792 934 872356 814780504 30.5614 9.7715 889 772641 679151439 29.6479 9.5792 934 872356 814780504 30.5614 9.7715 881 777440 881628968 29.6845 9.5855 936 876096 80028565 30.5947 9.7858 881 776161 883797814 19.6816 9.5835 936 876096 80028565 30.5947 9.7858 881 778161 883797814 19.6816 9.5835 936 876096 80028565 30.5947 9.7858 881 781456 600807104 29.7821 9.5073 938 81721 822656663 30.6105 9.7858 884 781456 600807104 29.7821 9.5073 938 81721 827080019 30.6431 9.7898 885 785496 605506456 29.7658 9.6046 941 885481 83237612 30.6757 9.7993 886 78496 605506456 29.7658 9.6046 941 885481 83237621 30.6757 9.7993 887 78759 970321 700227072 99.7993 9.1615 948 89136 848 78196 605506456 29.7658 9.6046 941 885481 83237621 30.6757 9.7993 887 7988 878544 700227072 99.7993 9.1615 948 89136 848 78196 605506456 29.7658 9.6046 941 885481 83237621 30.6757 9.7993 887 7988 878544 9700227072 99.7993 9.1615 948 89136 848 8878544 700227072 99.7993 9.1615 948 89136 848 8878544 700227072 99.7993 9.1615 948 89136 848 8878544 700227072 99.7993 9.1615 948 89136 848 8878544 88591 90.8081 70744971 99.8891 707497289 89.8614 9.6286 946 8046 8046 8046 8046 8046 8046 8046 80	872		663054848	29.5296		927		796597983	30.4467	9.7505
875         765625         660921875         29.5804         9.5647         930         864900         804357000         30.4959         9.7610           876         767376         672221376         99.583         931         869701         800354491         30.5123         9.7610           877         77611         67154329         39.39         86971         932         86824         89557588         30.529         9.7815           880         77400         681472000         29.6493         9.7529         38.73255         81740304         30.5400         9.7715           880         774100         681472000         29.6648         9.5825         935         874225         81740337         30.5778         9.7785           881         776161         68377811         29.6189         9.6010         34         871995         88056863         30.5103         9.7819           881         78106         690807101         29.7821         9.9737         938         879241         855.9863         30.0103         9.7873         938         879241         855.9863         30.0103         9.7873         938         879241         87925062         9.6010         9.6010         9.6010         9.6010			665338617	29.5466				799178752	30.4631	9 7540
876         767376         67222[376] 92,5973         9,5083         931         89071         800354491         9,513         9,7645         893         870781         932         880824         9,857558         9,328         88024         9,857558         9,328         88024         9,857558         9,33         870489         812166237         30,3400         9,7715         9,33         870489         812166237         30,3400         9,7715           880         777400         681472000         29,6493         9,5792         934         870489         8170639         30,3410         9,7785           881         777616         683787841         29,6815         9,5301         937         87969         88365863         30,1513         9,7819         9,8791         937         8798         8796963         30,1513         9,7831         9,7737         938         87944         855,93672         30,028         9,7859         9,8773         938         87944         855,93672         631,51125         9,7839         9,6010         940         883600         883600         8800         9,801         9,478         9,801         9,478         9,801         9,478         9,801         9,478         9,801         9,478         9,8										
877 769129		765625	669921875	29.5804	9.5647			804357000	30.4959	
578         770891         6768836152 99.6311         9.5756         938         870489         812166237 30.5450         9.7150           890         77401         679151439         99.6479         9.5759         934         872356         814780504         30.5614         9.7750           890         77400         681472000         29.6481         9.5828         935         874225         81709345         30.5778         9.7783           881         776161         683797841 29.6816         9.5836         936         876006         820053563 30.6914         9.7783           883         77669         68465387 29.7153         9.5973         938         879444         85293672 30.6368         9.7893           885         784966         60950704 29.7321         9.5973         939         881212         28736079 30.6368         9.7893           887         784966         60950446 29.7658         9.6010         940         883600         89054940         30.5777         9.7933           887         78496         60950446 29.7658         9.6046         941         885481         883327621         30.7677         9.7939           8887         78496         79626049         98.88949         88356180						991				9.7680
879         772641         679151429 (2) 6.648         9.5792         934         872356         814780504 (3) 0.5614 (9) 7.7785         93.774400         861 776161         683797811 (2) 6.616         9.5865         936         876006         800205356 (3) 0.5911 (9) 7.785         93.77850         82.777994         686128968 (2) 6.685 (9) 5.9501 (9) 937         877860         820205356 (3) 0.5911 (9) 7.785         93.778796         822569633 (0) 6105 (9) 7.788         93.787960         822569633 (0) 6105 (9) 7.788         93.8787196         822569633 (0) 6105 (9) 7.788         93.878712 (9) 822566633 (0) 6105 (9) 7.788         93.878712 (9) 822566633 (0) 6105 (9) 7.788         93.881721 (8) 82736019 (9) 6.016 (9) 7.788         83.87874 (8) 82736019 (9) 6.016 (9) 7.783         93.881721 (8) 82736019 (9) 6.016 (9) 7.784         83.87874 (9) 7.785         83.87854 (1) 70022707 (29) 7.793 (9) 7.618 (9) 7.785         93.8817 (1) 8.874 (1) 8.873	878							812166237	30.5450	
881 776161 683797841 19.6816 9.5855 936 876006 820025856 30.5941 9.7819 882 777969 68456587 92.7153 9.5931 937 87969 8256653 30.6105 9.7854 883 770689 68456587 19.7153 9.5937 938 879844 825293672 30.6268 9.7859 609807104 92.7321 9.5973 939 881721 827393019 30.6368 9.7859 884 781456 609807104 92.7321 9.5973 939 881721 827393019 30.6368 9.7859 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7529 9.7693 9.6010 946 883600 830558400 30.5534 9.7932 97.7932 92.7933 9.6115 941 885481 833237621 30.7675 9.7932 8885 783247 700227072 93.7993 9.6118 943 889249 838561807 30.7083 9.8023 889 790321 702595309 92.8610 9.1615 944 89133 88123834 90.7249 9.8081 7938481 707347971 19.8496 9.6226 946 891916 846590536 9.7571 9.8167 709732288 99.8661 9.6226 947 896809 898501 8749723 71.50849 9.8989 80821 714510891 29.8998 9.8344 949 90061 854673849 30.8025 9.8220 849 199236 714510891 29.8998 9.8344 949 90061 85467349 30.8025 9.8220 898 806104 724150732 29.9666 9.6477 95. 90060 856737500 30.8221 9.8305 898 806104 724150732 29.9666 9.6477 95. 90060 8565283177 30.8507 9.8468 899 808201 726572609 29.9833 9.613 954 91016 88256064 30.8859 9.8340 90.831 9.8340 90.831500 728200000 30.0000 9.6549 955 912025 87088875 30.9031 9.8477 901 811801 73343701 30.0167 9.6855 956 913936 87372816 30.9132 9.8511 90.9138 91.804401 80.855664 30.8859 9.8340 90.9138 91.80404 724150732 29.9666 9.6477 955 900803 88532177 30.9109 9.8347 9618 900803 9.85404 73845330 9.0333 9.6466 9519 900803 885664 30.8859 9.8340 90080			679151439	29.6479	9.5792	934	872356	814780504	30.5614	
881 776161 683797841 19.6816 9.5855 936 876006 820025856 30.5941 9.7819 882 777969 68456587 92.7153 9.5931 937 87969 8256653 30.6105 9.7854 883 770689 68456587 19.7153 9.5937 938 879844 825293672 30.6268 9.7859 609807104 92.7321 9.5973 939 881721 827393019 30.6368 9.7859 884 781456 609807104 92.7321 9.5973 939 881721 827393019 30.6368 9.7859 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7321 9.5973 939 881721 827393019 30.6431 9.7924 885 781966 609807104 92.7529 9.7693 9.6010 946 883600 830558400 30.5534 9.7932 97.7932 92.7933 9.6115 941 885481 833237621 30.7675 9.7932 8885 783247 700227072 93.7993 9.6118 943 889249 838561807 30.7083 9.8023 889 790321 702595309 92.8610 9.1615 944 89133 88123834 90.7249 9.8081 7938481 707347971 19.8496 9.6226 946 891916 846590536 9.7571 9.8167 709732288 99.8661 9.6226 947 896809 898501 8749723 71.50849 9.8989 80821 714510891 29.8998 9.8344 949 90061 854673849 30.8025 9.8220 849 199236 714510891 29.8998 9.8344 949 90061 85467349 30.8025 9.8220 898 806104 724150732 29.9666 9.6477 95. 90060 856737500 30.8221 9.8305 898 806104 724150732 29.9666 9.6477 95. 90060 8565283177 30.8507 9.8468 899 808201 726572609 29.9833 9.613 954 91016 88256064 30.8859 9.8340 90.831 9.8340 90.831500 728200000 30.0000 9.6549 955 912025 87088875 30.9031 9.8477 901 811801 73343701 30.0167 9.6855 956 913936 87372816 30.9132 9.8511 90.9138 91.804401 80.855664 30.8859 9.8340 90.9138 91.80404 724150732 29.9666 9.6477 955 900803 88532177 30.9109 9.8347 9618 900803 9.85404 73845330 9.0333 9.6466 9519 900803 885664 30.8859 9.8340 90080	880	774400	681472000	29.6648	9.5828	935	874225	817400375	30.5778	9.7785
8881         779689         688465387; 19.7153         9.5937         938         879444         85293872; 30.6268         9.7889         9.7973         938         871456         609807104         99.773         938         87121         8273836019         30.6318         9.7873         938         87121         8273836019         30.6318         9.7933           885         784966         605506456         29.7693         9.6010         940         883600         83058400         30.6594         9.7939           887         784760         607861103         29.7933         9.6118         8418         85481         83237621         30.7677         9.7938           887         784760         6072702         99.7939         9.6115         944         891130         84123384         30.7349         9.8021           890         793210         704969000         29.8329         9.6190         945         893025         843908625         30.7409         9.8132           891         79381         79.9221         9.80347971         9.8263         9.46         891016         8659033         9.74199         9.8132           891         79321         719323136         9.82634         9.8950090         9.8518123<	881		683797841	29.6816	9.5865	936		820025856	30.5941	
884         781456         60007104 [9.7321]         9.5073         930         SS1721         82738019         30.4431         9.7924           885         783966         6093154125 [9.7489]         9.6010         940         883600         80550403         0.6584 [9.758]         9.6016         941         885000         80550403         0.6584 [9.759]         9.6082         942         887364         83237621 [3.07577]         9.793         9.6115         943         885181         838327621 [3.07577]         9.8002         9.8028         885949         88561807 [3.0768]         9.8007         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029         9.8028         9.8025         848891136         841232384 [30.7246]         9.8027         9.8025         9.8025         848891136         841232384 [30.7246]         9.807         9.807         9.8025         9.8025         9.8025         84890650         9.80749 [9.813]         9.8025         9.8025         9.8025         9.8025         9.8025         9.8025         9.8025         9.8027         9.8027         9.8029         9.8029         9.8029         9.8029         9.8029         9.8029			686128968	29.6985						
885         783225         693154125         29.7489         9.6010         940         883600         83058400         30.6594         9.7359           886         784966         695506456         29.7688         9.6046         941         885481         83227621         30.6757         9.7993           887         784760         607861103         29.7993         9.6118         941         885481         83237621         30.7675         9.7993           888         785541         700227072         29.7993         9.6118         9418         881949         88561807         30.7083         9.8023           890         793210         704969000         29.8329         9.6190         945         899225         843908625         30.7409         9.8132           891         79381         79.9881         9.6292         947         896000         79.8173         9.8173           892         79.9881         9.6292         947         896000         896718123         30.7734         9.8210           891         79323         79.8183         9.6292         947         896000         89671823         9.7744         9.8214           893         801025         716017375         29										
886         784996         69550446 99, 7668         9, 6046         941         885481         833237621 30, 6757         9, 7908           887         784769         697861403 29, 7825         9, 6082         948         887864         835868883 0, 6990         9, 8028           888         785541         700227072 99, 7993         9, 6115         944         891138         841323843 0, 7246         9, 8067           800         793100         704869000         29, 8329         9, 6190         945         89025         843908625         30, 7409         9, 8132           891         793881         70747971 29, 8891         9, 6202         947         89600         96805         96805         96805         96805         96805         96805         96807         9, 8270           803         797449         712121957 29, 8881         9, 6282         947         89600         96805         96805         968078123 30, 7734         9, 8210           805         801025         716917375         29, 9166         9, 6370         950         90500         857375000         30, 8221         9, 830           807         804004         724150732 29, 9666         9, 6442         952         906004         885614083 30, 8334	004		090001104	29.1921	9.0910	959	001121	021990019	00.0401	9.1944
887 78547 70022707 297.093 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	885		693154125	29.7489						
888         788541         700227072 p9.7993         9.6118         943         889249         888561807 30.7083         9.7083         9.8067           890         7093210         704969000         29.8329         9.6190         945         890255         843908625         30.7409         9.8132           891         793881         707447971 29.8496         9.6226         946         894916         86590536         30.7571         9.8132           893         79749         712121957 29.8831         9.6282         947         89680         9.88261         868080         89187183         30.7349         9.8210           894         199236         71451084129,8989         9.8334         949         900601         58670349         9.8270           895         801025         716017375         29.9166         9.6370         950         902500         857375000         30.8231         9.830           897         804004         724150732         29.9669         9.6442         952         906034         882810483         30.833         9.8347           900         810000         729000000         30 0000         9.6549         955         910225         87088875         30.933         9.6660			695506456	29.7658	9.6046					
889         790321         702503309         29.8161         9.6154         944         891130         841232384         30.7346         9.807           800         792100         704969000         29.8329         9.6190         945         89025         84309685         30.7460         9.8132           891         793881         707347971         29.896         9.6226         947         806500         84300685         30.7734         9.8071           891         793881         792864         9.6226         947         806500         86500536         30.7571         9.8171           894         799236         71510984         9.9816         9.6226         947         806500         86718123         30.7734         9.8201           895         801025         716917375         9.9166         9.6370         9.50         902500           896         802516         713231362         9.9333         9.6406         951         904401         860853513         30.8323         9.8334           897         804609         724734973         39.9060         9.6477         935         904901         86085313         30.8323         9.831           898         804301         733750	888		700227072	29 7993	9 6118					
891         7938S1         707347971         9.8167         9.8262         946         881916         86350936         9.7571         9.8167           892         795664         70973288         98.664         9.8262         947         88698         94871813         9.7734         9.8210           893         79749         712121957         9.8818         9.6834         949         900601         851671292         90.7836         9.8236           895         800025         716917375         9.9166         9.6370         950         902500         857375000         90.8221         9.833           898         808216         71323136         39.9333         9.6406         951         904401         86085351         30.8383         9.8336           898         8080404         724150792         29.9666         9.6472         95         90803         868504183         30.8707         9.8448           900         810000         728000000         30.0000         9.6549         955         912025         87088875         30.9031         9.817           901         811801         731432701         30.0669         9.6620         95         912025         87088875         30.9031         <					9.6154					
891         7938S1         707347971         9.8167         9.8262         946         881916         86350936         9.7571         9.8167           892         795664         70973288         98.664         9.8262         947         88698         94871813         9.7734         9.8210           893         79749         712121957         9.8818         9.6834         949         900601         851671292         90.7836         9.8236           895         800025         716917375         9.9166         9.6370         950         902500         857375000         90.8221         9.833           898         808216         71323136         39.9333         9.6406         951         904401         86085351         30.8383         9.8336           898         8080404         724150792         29.9666         9.6472         95         90803         868504183         30.8707         9.8448           900         810000         728000000         30.0000         9.6549         955         912025         87088875         30.9031         9.817           901         811801         731432701         30.0669         9.6620         95         912025         87088875         30.9031         <	890	792100	704969000	29 8329	9 6190	945	893025	843908695	30 7409	9.8182
803         737419         71211937 19.8831         9.698         948         895701         851971892 30.7836         9.8236         9.8270           895         801025         716917375         99.9166         9.6370         950         902500         85737500         30.8221         9.8236           895         802816         71323136 29.9333         9.6406         951         904401         86085351         30.8383         9.8336           898         806404         724150732 29.9666         9.6472         953         908209         865523177         30.8707         9.8448           900         810000         728000000         30.000         9.6549         955         912025         87088875         30.9031         9.8477           901         811801         731432701         30.0167         9.6856         956         913836         87372816         30.9132         9.8517           903         815409         73614327         30.0609         9.6620         958         917584         8792179123         9.9516         9.8540           905         820353         743677416         30.0693         9.6620         959         9596         935214         958739681         31.0000         98.648 <td>891</td> <td></td> <td>707347971</td> <td>29.8496</td> <td>9.6226</td> <td></td> <td></td> <td>846590536</td> <td>30.7571</td> <td></td>	891		707347971	29.8496	9.6226			846590536	30.7571	
894         799236         714510981 29.8998         9.6334         949         900601         854670349         30.8058         9.8270           896         802816         716917375         39.9166         9.6370         950         902500         85787500         30.8221         9.8305           897         804600         721734273         39.9500         9.6442         952         906304         862801408         30.8539         9.8339           899         80404         724157029         39.9669         9.6477         953         90890         862801408         30.8549         9.8478           899         80402         725000000         30.000         9.6549         9.55         910116         868250664         30.8869         9.8443           900         810000         729000000         30.000         9.55         91025         870983875         80.9031         9.8477           901         813604         733576080         30.0600         9.655         955         913836         8732722816         30.9031         9.847           901         817216         738763264         30.0600         9.665         588         9174974         87279179         9.8648           905			709732288	29.8664	9.6262			849278123	30.7734	9.8201
895         801025         716917375         29.9166         9.6370         950         902500         85737500         30.8321         9.8305           896         802816         719323136         29.9333         9.6406         9.51         904401         86085351         30.8383         9.8334           898         8080404         724150732         29.9666         9.6472         953         908030         86523177         30.8707         9.8448           900         810000         728000000         30.0000         9.6549         955         912025         87083875         30.9031         9.8177           901         811801         731432701         30.0167         9.6856         9.5602         955         912025         87083875         30.9031         9.8177           903         815409         73631327         30.0600         9.6650         958         917764         87921791230,9516         9.8540           905         810025         743217683         30.0632         9.6620         956         915818         8764764733         30.934         9.8546           905         810225         743217663         30.0682         9.6692         959         910818         81747073         9.		797449	712121957	29.8831			898704	851971892	30.7896	9.8236
896         8902816         719323136 29.9333         9.6406         951         904401         860085351 30.8383         9.8339         9.8349           898         808404         724150732 39.9666         9.6477         953         908309         86523177 30.8707         9.8478           900         810000         728000000         30         9000         9.6539         9.8539         9.613         954         9101         865233177 30.8707         9.8408           900         810000         729000000         30         9000         9.6549         955         912025         87088875         30.9031         9.8417           901         811801         73183701 30.0467         9.6560         956         918336         873728216 30.9192         9.8514           903         815409         736814327 30.0500         9.6660         958         917764         879217912 30.9516         9.8546           905         820836         743677416 30.0669         9.6092         299         919681         817470470 30.9677         9.60         92600         825501           908         8224104         748613312 30.1330         9.6834         963         927369         8893056347 31.0322         9.8517           910	004	199250	114010904	29.6996	9.0554	949	900001	004070549	30.8038	9.6210
807         804609         721731273 39.9.500         9.6442         952         906304         862801408 30.8545         9.8574         9.8578           899         80610         724150762 29.9666         9.6477         953         908309         86532177 30.8707         9.8408           900         810000         726672699 29.9833         9.6513         954         910116         868250664         30.8869         9.8543           900         810000         729000000         30.0000         9.6549         955         919225         870898875         99.901         9.8574           902         813004         738763264         30.0609         6.665         959         919681         876467433         30.9354         9.8564           903         815109         741216253         30.0832         9.6727         960         21600         84174070         30.9677         9.8614           905         810025         741216625         30.0832         9.6727         960         201600         84174070         30.9677         9.8614           905         810025         741216633         30.1449         9.6796         96229521         8503681         31.0601         9.8714           908         82								857375000	30.8221	
898         809404         724150792 29.9666         9.6477         935         908209         865523177 30.8707         9.8408           900         810000         7289000000         30 0000         9.6549         955         912025         870983875         30.9031         9.8417           901         811801         73133701830.0333         9.6630         957         912025         870983875         30.9031         9.8171           903         815409         738576384         30.0630         9.6630         958         917764         87921791290.9516         9.8546           905         819025         741217625         30.0682         9.6692         959         919681         887704707         30.967         9.8614           905         820386         743677416         30.0689         9.6763         961         923521         887503681         31.0000         9.8648           905         824464         748613312         30.1389         9.6875         961         923521         8875036347         31.0322         9.8719           910         825100         753371000         30.1682         9.6695         962         9259         9594448         8937171283         31.0322         9.8719										9.8339
899         808201         726572699         29.9833         9 6513         954         910116         868250664         30.8869         9.8443           900         810000         729000000         30.0000         9.6549         955         910285         87008875         30.9031         9.8431           902         813004         738763264         30.0633         9.6630         957         91549         876467493         30.9341         9.8546           903         815106         738763264         30.0606         6665         959         919681         881974070         30.9677         9.8546           905         819025         741217625         30.0832         9.6727         960         291600         84736000         30.8939         9.8614           905         819025         741217625         30.0832         9.6727         960         291600         84736000         30.8939         9.8614           905         823610         741217625         30.0832         9.6727         960         291600         8473600330         30.8939         9.8614           907         828161         74121633         30.1449         9.6739         962         225444         890271128         31.0161 </td <td></td>										
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904 817216 738763284 30.0666 9.6692 959 919681 881974079 30.9677 9.8614 905 819025 741217625 30.0832 9.6727 960 921600 84378000 30.9899 9.8636 907 829616 74367436 30.0698 9.7678 961 925321 887503681 31.0000 9.8683 907 829619 746124361 30.1144 9.6799 962 925444 890277128 31.0161 9.8717 908 824464 748613312 30.1330 9.6834 963 927368 98906347131.0392 9.8751 909 826281 751089429 30.1496 9.6870 964 929296 805841344 31.0483 9.8785 910 828100 753571000 30.1662 9.6805 965 931225 898632125 31.0644 9.8819 911 829921 756055031 30.1889 9.6814 966 391325 898632125 31.0644 9.8819 912 831744 758550528 30.1993 9.6876 967 935089 904231063 31.0966 9.8884 963 9678 9678 9678 9678 9678 9678 9678 9678								876467493	30.9354	9.8546
905         819025         741217625         30.0832         9.6727         960         921600         884736000         30.9839         9.8648           906         280836         743677416         30.0968         9.6763         961         923521         887593681         31.0000         9.8648           907         824164         74612913         30.1164         9.679         962         925444         88971218         31.0110         9.8779         962         925444         89871218         31.0110         9.8787         964         925364         8980517128         31.0322         9.8781         9.8786         9893056347         31.0322         9.8781         9.8786         9893056347         31.0322         9.8781         9.8786         9893056347         31.0322         9.8781         9.8819         9.8819         9.8819         9.8819         9.891         9.8929         898631245         31.0644         9.8819         9.8819         9.891         9.8956         931225         898632125         31.0644         9.8819         9.8914         8936         935699         901238603         31.0644         9.8819         9.8914         89369         935699         99123803         31.1127         9.8922         9868         937021								881074070	30.9516	
907 82461 7468331 30,1164 9.6799 962 92544 809271823 31.0161 9.8717 9698 82464 74861831 23,01380 9.6834 968 927968 89305634731.0329 9.8751 909 826281 751089429 30.1969 9.6870 964 92929 88581344 31.0483 9.8785 911 82921 756058031 30.1682 9.6941 966 933156 901428063 31.0644 9.8819 912 831744 75850528 30.1993 9.6976 967 935089 904231063 31.0645 9.8854 912 831744 75850528 30.1993 9.6976 967 935089 904231063 31.0966 9.8888 918 835396 761048497 30.2159 9.7012 968 937024 907039233 31.127 9.8922 918 84561 76105829 30.2659 9.1718 971 94541 9454861 31.1669 9.9024 918 84561 7776151559 30.3150 9.7224 974 94676 924010424 31.2090 9.9026 918 844540 7776651559 30.3459 9.7259 978 980622 926859375 31.2850 9.9126						8				
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909 826281 751089429 30.1496 9.6870 964 929296 89581344 31.1488 9.8785 911 82921 756058031 30.1682 9.6904 966 93125 896832125 31.0644 9.8819 912 831744 758550528 30.1993 9.6976 967 935089 90423063 31.0966 9.8884 913 835596 761048497 30.2159 9.7012 968 937024 90703923 31.1279 7.8922 916 835396 763551944 30.2324 9.7047 969 938961 90985320 31.1288 9.8956 914 835396 763551944 30.2324 9.7047 969 938961 90985320 31.1288 9.8956 915 837225 768660875 30.2490 9.7082 970 940900 912673000 31.1448 9.8990 918 84424 773620632 30.2859 9.718 971 94241 915489613 31.6969 9.9024 918 84274 773620632 30.2985 9.7188 972 944784 91839048 31.1769 9.9082 919 84451 773651555 30.3150 9.7224 974 948676 92410424 31.2090 9.9024 919 844501 776151555 30.3150 9.7224 974 948676 92410424 31.2090 9.9126			748613312	30.1134	9.6834			893056347	31.0322	9.8751
911         829921         756058031 30.1828         9.6941         966         933156         901428006 31.0805         9.8854           912         83174         75885058 30.1993         9.6076         967         955089         9943106 31.0966         9.8858           913         833569         761048497 30.2159         9.7012         968         937024         907039323 31.1127         9.8922           915         837225         766060875 30.2490         9.7082         970         940900         912673000         31.1448         9.8990           916         839056         768573296 30.2855         9.7118         971         942841         915498011 31.1609         9.9058           918         843724         7778920632 30.2855         9.71185         973         946729         931167317 31.1923         9.9052           920         846400         778688000 30.3150         9.7224         974         94676         946710343 31.2000         9.9126           920         844640         778688000 30.3815         9.7259         975         90022         928589378 31.3230         9.1016			751089429	30.1496				895841344	31.0483	9.8785
911         829921         756058031 30.1828         9.6941         966         933156         901428006 31.0805         9.8854           912         83174         75885058 30.1993         9.6076         967         955089         9943106 31.0966         9.8858           913         833569         761048497 30.2159         9.7012         968         937024         907039323 31.1127         9.8922           915         837225         766060875 30.2490         9.7082         970         940900         912673000         31.1448         9.8990           916         839056         768573296 30.2855         9.7118         971         942841         915498011 31.1609         9.9058           918         843724         7778920632 30.2855         9.71185         973         946729         931167317 31.1923         9.9052           920         846400         778688000 30.3150         9.7224         974         94676         946710343 31.2000         9.9126           920         844640         778688000 30.3815         9.7259         975         90022         928589378 31.3230         9.1016	910	828100	753571000	30 1669	9 6905	965	931225	898632125	31.0644	9 8819
912         831744         75850528         30.1993         9.6076         967         935069         90423106331         1.9966         9.8888           913         835596         761048497         30.2159         9.7012         968         937024         96703923         31.1127         9.8922           914         835396         763551944         30.2324         9.7047         969         938961         90853309         31.1288         9.8956           915         837225         766660875         30.2409         9.7082         970         90000         912673000         31.1448         9.8990           917         84089         771095213         30.2890         9.7158         972         944784         91830048         31.1769         9.9082           918         84274         773650639         30.2855         9.7188         973         946729         921673173         31.1299         9.9082           92         844640         77651559         30.3150         9.7259         975         96023         928559375         31.2250         9.916           920         844400         77688000         30.3315         9.7259         975         96023         928559375         31.2250	911	829921	756058031	30.1828	9.6941	966	933156	901428696	31.0805	9.8854
914 835396 763551944 30,2324 9.7047 969 938961 999853209 31.1288 9.8956 915 837225 766660875 30,2490 9.7082 970 940900 912673000 31.1448 9.8990 916 839056 768875296 90,2655 9.7118 971 92841 91498611 31.1609 9.9024 917 840889 71098213 30,3880 9.7153 972 944784 918330048 31.1769 9.9082 918 84561 7766151559 30,3150 9.7224 974 948676 924010424 31.2090 9.9126 920 846400 778688000 30,3315 9.7259 975 980825 996859375 31.2250 9.910								904231063	31.0966	9.8888
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916         \$39056         768575296         \$0.2655         9.7118         971         942841         915498511         31.1609         9.9024           917         \$40889         771095213         30.2820         9.7153         972         944784         91833048         31.1769         9.9058           918         \$4274         773620632         30.2855         9.7188         93         946720         921167317         31.1929         9.9092           919         844561         776151559         30.3150         9.7224         974         948676         924010424         31.2090         9.9126           920         8446400         778688000         80.3315         9.7259         975         950625         996859375         31.2920         9.9160           94         448940         778687678         924010416         31.2000         9.9160										
917 840889 771095213 30.2859 9.7153 972 944784 918330048 31.1769 9.9058 918 842724 773680639 30.2885 9.7158 973 946729 91167317 31.1799 9.9058 919 844561 776151559 30.3150 9.7224 974 948676 92401042 31.2090 9.9126 920 846400 778688000 30.3315 9.7259 975 950625 926859375 31.2250 9.9160					9.7082			912673000	31.1448	
918 842724 773620632 30.2985 9.7188 973 946729 921167317 31.1929 9.9092 919 844561 776151559 30.3150 9.7224 974 948676 924010434 31.2090 9.9126 920 944040 778688000 80.3159 9.7259 975 95655 9687317 31.2250 9.9160 920 944040 778688000 80.3159 9.7259 975 95655 9687317 31.2250 9.9160 920 944040 9440 9440 9440 9440 9440 94			771005919	30.2655	9.7118	971		915498611	31 1760	
919 844561 776151559 30.3150 9.7224 974 948676 924010424 31.2090 9.9126 920 84690 778688000 30.3315 9.7259 975 950625 926859875 81.2250 9.9160	918		773620632	30.2985		973	946729			
041 949944 794990064 90 9490 0 7904 076 070776 090714166 91 9410 0 0104		844561	776151559	30.3150	9.7224	974	948676	924010424	31.2090	
041 949944 794990064 90 9490 0 7904 076 070776 090714166 91 9410 0 0104	920	846400	778688000	30 3315	9 7259	975	950625	926859375	31.2250	9.9160
$\begin{array}{llllllllllllllllllllllllllllllllllll$	921	848241	781229961	30,3480	0 2004	000	952576	929714176	31.2410	9.9194
923 851929 786380467130.3809 9.7364 978 956484 935141352[31,2730 9.9261 924 853776 788889024]30.3974 9.7400 979 958441 938313739]31,2890 9.9295	922	850084	783777448	30.3645	9.7329	977	954529	932574833	31.2570	
941 000110 1000000024100.00141 9.1400 9 919 000441 1 000013[59/5], 2090 9.9290		851929	786330467	30.3809	9.7364	978		935441352	31.2730	
	941	000110	1000090241	00.09741	3.74001	919	900441 1	990919199	51.20901	0.0400

No.	Square.	Cube.	Sq. Root.	Cube, Root,	No.	Square,	Cube.	Sq. Root.	Cube Root,
980	960400	941192000	31.3050	9.9329	1035	1071225	1108717875	32 1714	10 1158
981	962361	944076141	31.3209	9.9363	1036	1073296	1111934656	32.1870	10.1186
982 983	964324 966289	946966168 949862087	31.3369	9.9396 9.9430	1037 1038	1075369	1115157653 1118386872	32.2025	10.1218 10.1251
984	968256	952763904	31.3688	9.9464	1039		1121622319		
985	970225	955671625	31.3847	9.9497	1040	1081600	1124864000 1128111921	32.2490	10.1316
986 987	972196 974169		31.4006	9.9531 9.9565	1041 1042	1083681	1128111921 1131366088	32.2645	10.1348
988	976144	964430272	31.4325	9.9598	1043	1087849	1134626507	32,2955	10.1413
989	978121	967361669	31.4484	9.9632	1044	1089936	1137893184	32.3110	10.1446
990	980100	970299000	31.4643	9.9666	1045		1141166125		
991 992	982081 984064	973242271 976191488			1046		1144445336 1147730823		
993	986049	979146657	31.5119	9.9766	1048	1098304	1151022592	32.3728	10.1575
994	988036	982107784	31.5278	9.9800	1049	1100401	1154320649	32.3883	10.1607
995	990025	985074875	31.5436	9.9833	1050		1157625000		
996 997	992016 994009	988047936 991026973		9.9866	1051 1052	1104601	1160935651 1164252608	32.4191	10.1672 $10.1704$
998	996004	994011992	31.5911	9 9933	1053	1108809	1167575877	32.4500	10.1736
999	998001	997002999	31.6070	9.9967	1054	1110916	1170905464	32.4654	10.1769
1000		1000000000			1055		1174241375		
1001 1002		1003003001 1006012008			1056 1057		1177583616 1180932193		
1003	1006009	1009027027	31.6702	10.0100	1058	1119364	1184287112	32.5269	10.1897
1004	1008016	1012048064	31.6860	10.0133	1059	1121481	1187648379	32.5423	10.1929
1005	1010025	1015075125	31.7017	10.0166	1060		1191016000		
1006 1007	1012036	1018108216 1021147343	31.7333	10.0200	1061 1062	1125721	1194389981 1197770328	32.5883	10.1993
1008	1016064	1021147343 1024192512	31.7490	10.0266	1063	1129969	1197770328 1201157047	32.6036	10.2057
1009		1027243729			1064		1204550144		
1010	1020100	1030301000 1033364331	31.7805	10.0332	1065	1134225	1207949625	32.6343	10.2121
1011 1012	1022121	1033364331	31.7962	10.0365	1066 1067	1136356	1211355496 1214767763	32.6497 32.6650	10.2153
1013	1026169	1039509197	31.8277	10.0431	1068	1140624	1218186432	32.6803	10.2217
1014	1028196	1042590744	31.8434	10.0465	1069	1142761	1221611509	32.6956	10.2249
1015	1030225	1045678375	31.8591	10.0498	1070	1144900	1225043000	32.7109	10.2281
1016 1017		1048772096 1051871913			1071 1072	1147041	1228480911 1231925248	82.7261 82.7414	10.2313
1018	1036324	1054977832	31.9061	10.0596	1073	1151329	1235376017	32.7567	10.2376
1019	1038361	1058089859	31.9218	10.0629	1074	1153476	1238833224	32.7719	10.2408
1020	1040400	1061208000	31.9374	10.0662	1075	1155625	1242296875	32.7872	
1021 1022	1042441 1044484	1064332261 1067462648	31.9531	10.0695 10.0728	1076 1077	1157776	1245766976 1249243533	32.8024	10.2472 10.2503
1023	1046529	1070599167	31.9844	10.0761	1078	1162084	1252726552	32,8329	10.2535
1024	1048576	1073741824	32.0000	10.0794	1079	1164241	1256216039	32.8481	10.2567
1025	1050625	1076890625	32.0156	10.0826	1080	1166400	1259712000	32.8634	10.2599
$\frac{1026}{1027}$		1080045576 1083206683			1081 1082	1168561	1263214441 1266723368	32.8786	10.2630
1028	1056784	1086373952	32.0624	10.0925	1083	1172889	1270238787	32.9090	10.2693
1029	1058841	1089547389	32.0780	10.0957	1084	1175056	1273760704	32.9242	10.2725
1030		1092727000			1085	1177225	1277289125	32.9393	10.2757
1031 1032		1095912791 1099104768			1086 1087	1179396 1181569	1280824056 1284365503	32.9545 32.9697	$10.2788 \\ 10.2820$
1033	1067089	1102302937	32.1403	10.1088	1088	1183744	1287913472	32.9848	10.2851
1034	1069156	1105507304	32.1559	10.1121	1089	1185921	1291467969	33.0000	10.2883

No.	Square.	Cube.	Sq. Root,	Cube Root,	No.	Square.	Cube.	Sq. Root.	Cube Root,			
1090 1091	1188100 1190281	1295029000 1298596571	33.0151 33.0303	10.2914 10.2946	1145 1146		1501123625 1505060136					
1092 1093 1094	1192464 1194649 1196836	1298596571 1302170688 1305751357 1309338584	33.0454 33.0606 33.0757	10.2977 10.3009 10.3040	1147 1148 1149	1315609	1509003523 1512953792	33.8674 $33.8821$	10.4678 10.4708			
1095 1096	1199025	1312932375 1316532736	<b>33.0908</b>	10.3071	1150 1151	1322500	1520875000 1524845951	33.9116	10.4769			
1097 1098 1099	1203409 1205604	1320139673 1323753192 1327373299	33.1210 33.1361	10.3134 10.3165	1152 1153 1154	1327104 1329409		33.9411 38.9559	10.4830 10.4860			
1100 1101	1210000	1331000000 1334683301	33.1662	10.3228	1155 1156	1334025	1540798875 1544804416	33,9853	10.4921			
1102 1103 1104	1214404 1216609	1338273208 1341919727 1345572864	33.1964 33.2114	10.3290 10.3322	1157 1158 1159	1338649 1340964	1548816898 1552836312 1556862679	$34.0147 \\ 34.0294$	10.4981 10.5011			
1105 1106	1223236	1349232625 1352899016	33.2566	10.3415	1161	1347921	1560896000 1564936281	34.0735	10.5102			
1107 1108 1109	1227664	1356572043 1360251712 1363938029	33.2866	10.3478	1162 1163 1164	1352569	1568983528 1573037747 1577098944	34.1028	10.5162			
1110 1111	1234321	1367631000 1371330631	33.3317	10.3571	1165 1166	1359556	1581167125 1585242296	34.1467	10.5253			
1112 1113 1114	1238769	1375036928 1378749897 1382469544	33,3617	10.3633	1167 1168 1169	1364224 1366561	1589324463 1593413632 1597509809	34.1760	10.5313			
1115 1116 1117	1243225 1245456 1247689	1386195875 1389928896 1393568613 1397415032 1401168159	33,3916 33,4066 33,4215	10 3695 10.3726 10 3757	1170 1171 1172	1368900 1371241 1373584	1601613000 1605723211 1609840448	34.2199	10.5403			
1118 1119	1249924 1252161	1897415032 1401168159	33.4365 33.4515	10.3788 10.3819	1173 1174	1375929	1613964717 1618096024	34.2491	10.5463			
1120 1121 1122	1256641	1404928000 1408694561 1412467848	33.4813	10.3881	1176	1382976	1622234375 1626379776 1630532233	34.2929	10.5553			
1123 1124	1261129	1416247867 1420034624	33.5112	10.3943	1178	1387684	1634691752 1638858339	34,3220	10.5612			
1125 1126 1127	1262826	1423828125 1427628376 1431435383	33 5559	10 4035	1181	1394761 1397124	1643032000 1647212741 1651400568	34.3657 34.3802	10.5702 10.5732			
1128 1129		1431435383 1435249152 1439069689				1399489	1655595487 1659797504	34.3948	10 5762			
1130 1131 1132	1279161	1442897000 1446731091 1450571968	33.6303	10.4189	1186	1406596	1664006625 1668222856 1672446203	34.4384	10.5851			
1133 1134	1285956	1450571968 1454419637 1458274104	33.6749	10.4281	1189	1411344 1413721	1676676672 1680914269	34.4674 34.4819	10.5910 10.5940			
1135 1136 1137	1290496 1292769	1462135375 1466003456 1469878353	33.7046 33.7174	10.4342 10.4373	1190 1191 1192	1418481 1420864	1685159000 1689410871 1693669888	34.5109 34.5254	10,6000 10,6029			
1138 1139	1297321	1478760072 1477648619	33.7491	10.4434	1193 1194	1425636	1697936057 1702209384	34.5543	10.6088			
1140 1141 1142	1299600 1301881 1304164	1481544000 1485446221 1489355288	33.7639 33.7787 33.7935	10.4464 10.4495 10.4525	1195 1196 1197	1430416	1706489875 1710777536 1715072373	34.5832 34.5977	10.6148 10.6177			
1143 1144	1306449 1308736	1489355288 1493271207 1497193984	33.8083 33.8231	10.4556 10.4586	1198 1199	1435204 1437601	1719374392 1723683599	34.6121	10.6207			

-									
No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
1200 1201 1202 1203	1442401 1444804 1447209	1728000000 1732323601 1736654408 1740992427	34.6554 $34.6699$ $34.6843$	10.6295 10.6325 10.6354	1256 1257 1258	1577536 1580049 1582564	1976656375 1981385216 1986121593 1990865512	35.4401 35.4542 35.4683	10.7894 10.7922 10.7951
1204 1205 1206 1207	1450005	1745337664 1749690125 1754049816 1758416743 1762790912	04 5191	10 6419	1260 1261 1262	1587600 1590121 1592644	1995616979 2000376000 2005142581 2009916728	35.4965 35.5106 35.5246	10.8008 10.8037 10.8065
1208 1209 1210 1211 1212	1464100 1466521	1762790912 1767172329 1771561000 1775956931 1780360128	34.7851 34.7994	10.6560 10.6590	1263 1264 1265 1266 1267	1597696 1600225 1602756	2014698447 2019487744 2024284625 2029089096 2033901163	35,5528 35,5668 35,5809	10.8151 10.8179
1213 1214 1215 1216	1471369 1478796 1476225	1784770597 1789188344 1798613375 1798045696	34.8281 34.8425 34.8569	10.6648 10.6678 10.6707 10.6736	1268 1269 1270 1271	1607824 1610361 1612900	2038720832 2048548109 2048383000 2053225511	35,6090 35,6230 35,6371	10.8236 10.8265 10.8293
1217 1218 1219 1220	1481089 1483524 1485961 1488400	1802485313 1806932232 1811386459 1815848000	34.8855 34.8999 34.9142 34.9285	10.6765 10.6795 10.6824 10.6858	1272 1278 1274 1275	1617984 1620529 1623076 1625625	2058075648 2062933417 2067798824 2072671875	35.6651 35.6791 35.6931 35.7071	10.8350 10.8378 10.8407 10.8435
1221 1222 1223 1224	1493284 1495729 1498176	1820316861 1824793048 1829276567 1833767424	34.9571 34.9714 34.9857	10.6911 10.6940 10.6970	1277 1278 1279	1630729 1633284 1635841	2077552576 2082440933 2087336952 2092240639	85.7851 85.7491 85.7681	10.8492 10.8520 10.8548
1225 1226 1227 1228 1229	1503076 1505529 1507984	1838265625 1842771176 1847284083 1851804352 1856331989	35.0143 35.0286 35.0428	10.7028 10.7057 10.7086		1640961 1643524 1646089	2097152000 2102071041 2106997768 2111932187 2116874304	35.7911 35.8050 35.8190	10.8605 10.8633 10.8661
1230 1231 1232 1233 1234	1515861 1517824 1520289	1860867000 1865409391 1869959168 1874516337 1879080904	35.0856 35.0999 35.1141	10.7173 10.7202 10.7231	1285 1286 1287 1288 1289	1653796 1656369 1658944	2121824125 2126781656 2131746903 2136719872 2141700569	35.8608 35.8748 35.8887	10.8746 10.8774 10.8802
1235 1236 1237 1238 1239	1527696 1530169 1532644	1883652875 1888232256 1892819053 1897413272 1902014919	35.1568 35.1710 35.1852	10.7318 10.7347 10.7376	1290 1291 1292 1293 1294	1666681 1669264 1671849	2146689000 2151685171 2156689088 2161700757 2166720184	35.9305 35.9444 35.9583	10.8887 10.8915 10.8943
1240 1241 1242 1243	1540081 1542564 1545049	1906624000 1911240521 1915864488 1920495907	35.2278 35.2420 35.2562	10.7463 10.7491 10.7520	1295 1296 1297 1298	1677025 1679616 1682209 1684804	2171747375 2176782336 2181825073 2186875592	35.9861 36.0000 36.0139 36.0278	10.8999 10.9027 10.9055 10.9083
1244 1245 1246 1247 1248	1550025 1552516 1555009	1925134784 1929781125 1934434936 1939096223 1943764992	35.2846 35.2987 35.3129	10.7578 10.7607 10.7635	1300 1301 1302 1303	1690000 1692601 1695204	2191933899 2197000000 2202073901 2207155608 2212245127	36.0555 36.0694 36.0832	10.9139 10.9167 10.9195
1249 1250 1251 1252	1560001 1562500 1565001 1567504	1948441249 1953125000 1957816251 1962515008	35.3412 35.3553 35.3695 35.3886	10.7693 10.7722 10.7750 10.7779	1304 1305 1306 1307	1700416 1703025 1705636	2217342464 2222447625 2227560616 2232681443	36.1109 36.1248 36.1386	10.9251 10.9279 10.9307
1258 1254	1570009	1967221277 1971935064	35.3977	10 7808	1308	1710864	2237810112 2242946629	36.1663	10.9363

No.	Square.	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
1310	1016100	2248091000	26 1020	10 0418	1365	1969005	05/19900105	26 0450	11 0000
1311		2253243231		10.9416		1865956	2543302125 2548895896	36 9594	11.0939
1312	1721344	2258403328	36,2215	10.9474	1367	1868689	2554497863	36,9730	11.0983
1313	1723969	2263571297	36.2353	10.9502		1871424	2560108032	36.9865	11.1010
1314	1726596	2268747144	36.2491	10.9530	1369	1874161	2565726409.	37.0000	11.1037
1315		2273930875					2571353000		
1316		2279122496				1879641	2576987811	37.0270	11.1091
1317 1318	1734489	2284322013 2289529432	36 2012	10.9613	1372 1373	1885190	2582630848 2588282117	37.0400	11.1118
1319	1739761	2294744759	36.3180	10.9668	1374	1887876	2593941624	37.0675	11.1172
1320	1742400	2299968000	36.3318	10.9696	1375	1890625	2599609375	37.0810	11.1199
1321	1745041	2305199161	36.3456	10.9724	1376	1893376	2605285376	37 0945	11,1226
1322 1323	1747684	2310438248 2315685267	36.3593	10.9752	1377 1378	1896129	2610969638 2616662152	37.1080	11.1258
1323	1752976	2320940224	36.3868	10.9807	1379	1901641	2622362939		
1325	1755695	2326203125	36 4005	10 9834	1380	1904400	2628072000	37 1484	11 1334
1326	1758276	2331473976	36,4143	10.9862	1381	1907161	2633789341	37.1618	11,1361
1327	1760929	2336752783	36.4280	10.9890	1382	1909924	2639514968	37.1753	11.1387
1328		2342039552		10.9917	1383	1912689	2645248887 2650991104	37.1887	11.1414
1329	1766241	2347334289	36.4555	10.9945	1384				
1330		2352637000			1385	1918225	2656741625 2662500456	37.2156	11.1468
1331	1771561	2357947691	36,4829	11.0000	1386	1920996	2662500456	37.2290	11.1495
1332 1333	1774224	2363266368 2368593037		11.0028	1387 1388	1096544	2668267603 2674043072	27 2550	11.1522
1334		2373927704					2679826869		
1335	1790005	2379270375	26 5277	11 0110	1390	1039100	2685619000	97 9997	11 1609
1336		2384621056			1391		2691419471		
1337		2389979753			1392	1937664	2697228288	37 3095	11 1655
1338	1790244	2395346472	36.5787	11 0193	1393	1940449	2703045457 2708870984	37.3229	11.1682
1339	1792921	2400721219	36.5923	11.0220	1394	1943236	2708870984	37.3363	11.1709
1340		2406104000			1395	1946025	2714704875	37.3497	11.1736
1341		2411494821				1948816	2720547136	37.3631	11.1762
1342		2416893688				1951609	2726397773	37.3765	11.1789
1343 1344		2422300607 2427715584					2732256792 2738124199		
1345	1800005	2433138625	36 6749	11 0384	1400		2744000000		
1346	1811716	2438569736	26 6879	11 0412	1401	1962801	2749884901	37 4999	11 1896
1347	1814409	2444008923 2449456192	36.7015	11.0439	1402	1965604	2755776808	37.4433	11.1922
1348	1817104	2449456192	36.7151	11.0466	1403	1968409	2755776808 2761677827 2767587264	37.4566	11.1949
1349	1819801	2454911549	36.7287	11.0494	1404	1971216	2767587264	37.4700	11.1975
1350		2460375000				1974025	2773505125	37.4833	11.2002
1351	1825201	2465846551	36.7560	11.0548	1406	1976836	2779431416	37.4967	11.2028
1352		2471326208 2476813977				1979649	2785366143 2791309312	37 5022	11.2055
1353 1854		2482309864					2797260929		
1355	1836025	2487813875	36.8103	11.0657	1410	1988100	2803221000	37.5500	11.2135
1356	1838736	2493326016	36.8239	11.0684	1411	1990921	2809189521	137 5633	11 2161
1357	1841449	2498846293	36.8375	11.0712	1412	1993744	2815166528	37.5766	11.2188
1358	1844164	2504374712	36.8511	11.0739	1413	1996569	2815166528 2821151997 2827145944	37.5899	11.2214
1359	1846881	2509911279	36.8646	11.0766	1414	1999396	2827145944	37.6032	11.2240
1360	1849600	2515456000	36.8782	11.0793	1415	2002225	2833148375	37,6165	11.2267
1361	1852321	2521008881	36.8917	11.0820	1416	2005056	2839159296	37.6298	11 2293
1362 1363	1850044	2526569928	36.9053	11.0847	1417	2007889	2845178713 2851206632	37 6569	11.2320
1364	1860196	2532139147 2537716544	36 9324	11 0909	1410	2010724	2857243059		
1.304	1000+90		00.0004	11.0002	1419	2010001	~0010400000	0600.10	11.2010

No.	Square	Cube.	Sq. Root.	Cube Root.	No.	Square.	Cube.	Sq. Root.	Cube Root.
1420	2016400	2863288000	37.6829	11.2399	1475		3209046875		
1421	2019241	2869341461	37.6962	11.2425	1476	2178576	3215578176	38.4187	11.3858
1422	2022084	2875403448	37.7094	11.2452	1477	2181529	3222118333	38.4318	11.3883
1423 1424	2024929	2875403448 2881473967 2887553024	37.7359	11.2478	1478 1479	2184484	3228667352 3235225239	38.4578	11.3935
1425	2030625	2893640625 2899736776 2905841483 2911954752 2918076589	37.7492	11.2531	1480	2190400	3241792000 3248367641	38.4708	11.3960
1426 1427	2035470	2899730770	37.7024	11 2588	1481 1482	2196394	3254952168	38 4968	11 4012
428	2039184	2911954752	37.7889	11.2610	1483	2199289	3261545587	38.5097	11.4037
1429	2042041	2918076589	37.8021	11.2636	1484	2202256	3268147904	38.5227	11.4063
430	2044900	2924207000	87.8153	11.2662	1485		3274759125		
[431]	2047761	2930345991 2936493568	37.8286	11.2689	1486 1487		3281379256 3288008303		
1483		2942649737			1488		3294646272		
1434		2948814504			1489	2217121	3301293169	38.5876	11.4191
1435	2059225	2954987875	37.8814	11.2793			3307949000		
$\frac{1436}{1437}$	2062096	2961169856 2967360458	37.8946	11 2820	1491 1492	2223081	3314613771 3321287488	38.6135	11.4242
1438	2067844	2973559672 2979767519	37.9210	11.2872	1493	2229049	3327970157 3634661784	38.6394	11.4293
1439	2070721	2979767519	37.9342	11.2898	1494	2232036	3634661784	38.6523	11.4319
1440	2073600	2985984000 2992209121	37.9473	11.2924	1495	2235025	3341362375	38.6652	11.4344
1441 1442	2076481	2992209121	37.9605	11.2950	$\frac{1496}{1497}$	2238016	8348071936 3354790473	38.6782	11.4370
1443	2082249	2998442888 3004685307	37.9868	11 3003	1497		3361517992		
1444	2085136	3010936384	38.0000	11.3029	1499		3368254499		
1445	2088025	3017196125	38.0132	11.3055	1500		3375000000		
1446 1447	2090916	3023464536 3029741623	38.0263	11.3081	1501		3381754501		
448	2095609	3036027392	38.0526	11 3133	1502 1503	22590004	3388518008 3395290527	38 7685	11.4548
1449	2099601	3042321849	38.0657	11.3159	1504	2262016	3402072064	38.7814	11.4578
1450	2102500	3048625000	38.0789	11.3185	1505	2265025	3408862625	38.7943	11.4598
1451	2105401	3054936851 3061257408	38.0920	11.3211	1506	2268036	3415662216 3422470843 3429288512	38.8072	11.4624
452 453	2108304	3061257408 3067586677	38.1051	11.3237	1507 1508	2271049	3422470843	38.8201	11.4649
454	2114116	3073924664	38.1314	11.3289	1509	2277081	3436115229	38.8458	11.4700
455		3080271375			1510		3442951000		
456	2119936	3086626816	38.1576	11.3341	1511		3449795831		
457 458	2122849	3092990993 3099363912	38 1838	11 3393	1512 1513		3456649728 3463512697		
459		3105745579			1514		3470384744		
460		3112136000			1515	2295225	3477265875	38.9230	11,4852
1461		3118535181			1516	2298256	3484156096	38.9358	11.4877
463 463	2137444	3124943128 3131359847	38.2361	11.3496	1517 1518		3491055413 3597963832		11.4902
464	2143296	3137785344	38.2623	11.3548	1519		3504881359		
465	2146225	3144219625	38.2753	11.8574	1520	2310400	3511808000	38.9872	11.4978
$1466 \\ 1467$		3150662696 3157114563			1521 1522		3518743761 3525688648		
468		3163575232			1523		3532642667		
469	2157961	3170044709	38.3275	11.3677	1524		3539605824		
470		3176523000			1525	2325625	3546578125	39.0512	11.5104
1471		3183010111			1526		3553559576		
1472	2100784	3189506048 3196010817	38 3707	11.5700	1527	2331729	3560550183 3567549952	20 0206	11 5170
1473									

No.	Square.	Cube.	Sq. Root,	Cube Root.	No.	Square.	Cube.	Sq. Root,	Cube Root.
-	-								
1530	2340900	3581577000	39.1152	11.5230	1565	2449225	3833037125	39.5601	11.6102
1531	2343961	3588604291	39.1280	11.5255	1566		3840389496		
1532 1533	2347024	3595640768 3602686437	39.1408	11.5280	1567 1568		3847751263 3855123432		
1534		3609741304			1569		3862503009		
1535		3616805375			1570		3869893000		
1536 1537		3623878656 3630961153			1571 1572	9471184	3877292411 3884701248	39.0308	11 6274
1538		3638052872			1573		3892119517		
1539	2368521	3645153819	39.2301	11.5455	1574	2477476	3899547224	39.6737	11.6324
1540	9351600	3652264000	30 9498	11 5190	1575	9480695	3906984375	20 6869	11 6318
1541		3659383421			1576		3914430976		
1542	2377764	3666512088	39.2683	11.5530	1577		3921887033		
1543		3673650007			1578		3929352552		
1544	2585950	3680797184	39.2938	11.5580	1579	2493241	3936827539	39.7300	11.0444
1545	2387025	3687953625	39.3065	11.5605	1580		3944312000		
1546		3695119336			1581		3651805941		
1547 1548		3702294323 3709478592			1582		3959309368 3966822287		
1549		3716672149			1583 1584		3974344704		
1550		3723875000			1585		3981876625		
1551 1552		3731087151 3738308608			1586 1587		3989418056 3996969003		
1553		3745539377			1588		4004529472		
1554		3752779464			1589	2524921	4012099469	39.8623	11.6692
1555	0410005	3760028875	90 (99)	11 5054	1590	0500100	4019679000	90 0740	11 0010
1556		3767287616			1591		4019679000		
1557	2424249	3774555693	39.4588	11.5903	1592	2534464	4034866688	39.8999	11.6765
1558	2427364	3781833112	39.4715	11.5928	1593		4042474857		
1559	2430481	3789119879	39.4842	11.5953	1594	2540836	4050092584	39.9249	11.0814
1560		3796416000	39 4968	11.5978	1595	2544025	4057719875	39,9375	11.7839
1561	2436721	3803721481	39.5095	11.6003	1596	2547216	4065356736	39.9500	11.6863
1562 1563		3811036328 3818360547			1597 1598		4073003173 4080659192		
1564		3825694144			1598		4080659192		
1	1	3010301111	30.0114	12.5011					
	1	1	1	l	1600	2560000	4096000000	140.0000	11.6961

# SQUARES AND CUBES OF DECIMALS.

No. Square. Cube	No. Square.	Cube. No.	Square.	Cube.
.1 .01 .001	.01 .0001	.000 001 .001		.000 000 001
.3 .09 .027 .4 .16 .064 .5 .25 .125	.03 .0009 .04 .0016 .05 .0025	.000 027 .003 .000 064 .004 .000 125 .005	.00 00 09 .00 00 16	.000 000 027 .000 000 064 .000 000 125
.6 .36 .216 .7 .49 .343	.06 .0036 .07 .0049	.000 216 .006 .000 343 .007	.00 00 36	.000 000 216 .000 000 343
.8 .64 .512 .9 .81 .729 1.0 1.00 1.000 1.2 1.44 1.728	.08 .0064 .09 .0081 .10 .0100	.000 512 .008 .000 729 .009 .001 000 .010	.00 00 81	.000 000 512 .000 000 729 .000 001 000

Note that the square has twice as many decimal places, and the cube three times as many decimal places, as the root.

# FIFTH ROOTS AND FIFTH POWERS. (Abridged from Transmine.)

	(Abridged from Trautwine.)												
No. or Root.	Power.	No. or Root.	Power.	No. or Root.	Power.	No. or Root.	Power.	No. or Root.	Power.	1			
.10 .15	.000010	3.7	693.440	9.8	90393	21.8	4923597	40	102400000				
.15	.000075	3.8	792.352 902.242	9.9	95099	22.0	5153632	41	115856201				
.20 .25 .30	.000320	3.9	902.242 1024.00	10.0	100000 110408	$\frac{22.2}{22.4}$	5392186	42 43	130691232				
.20	.002430	4.1	1158.56	$\frac{10}{10.4}$	121665	22.6	5639493 5895793	44	147008443 164916224				
.35	.005252	4.2	1306.91	10.6	133823	22.8	6161827	45	184528125				
.35 .40	.005252 .010240	4.2	1470.08	10.8	146933	23.0	6436343	46	205962976				
* .451	.018453	4.4	1649.16	11.0	161051	28.2	6721093	47	229345007	۱			
.50 .55	.031250	4.6	1845,28 2059,63	$\frac{11.2}{11.4}$	176284 192541	$23.4 \\ 23.6$	7015834 7320825	48 49	254803968 282475249				
.60	.077760	4.7	2293.45	11.6	210(31	23.8	7636332	50	312500000				
. 65	.116029	4.8	2293.45 2548.04	11.8	228776	24.0	7960624	51	345025251	ı			
.70 .75	.168070 .237305	4.9	2824.75	12.0	248832	24.2	8299976	52	380204032	ı			
.75	.237805	5.0 5.1	3125.00	12.2 12.4	270271	$24.4 \\ 24.6$	8648666	53 54	418195493 459165024	ı			
.80 .85	.327680 .443705	5.1	3450.25 3802.04	12.6	293163 317580	24.8	9008978 9381200	55	503984375	ı			
. 901	.590490	5.2 5.3	4181.95	12.8	343597	25.0	9765625	56	503284375 550731776	ı			
.95 1.00	.773781	5.4	4591.65	$\frac{13.0}{13.2}$	371293 400746	25.2	10162550	57	601692057	ı			
1.00	1.00000	5.5	5032.84	13.2	400746	25.4	10572278	58	656356768	ı			
1.05 1.10	1.27628 1.61051	5.6 5.7	5507.82 6016.92	13.4 13.6	432040 465259	$25.6 \\ 25.8$	10995116 11431377	59 60	714924299 777600000	п			
1.15	2.01135	5.8	6563.57	13.8	500490	26.0	11881376	61	844596301	ı			
1 201	2.48832	5.9	7149.24	14.0	537824	26.2	12345437	62	916132832	ı			
1.25 1.30	2.48832 3.05176	5.9 6.0	7776.00 8445.96	14.2	577353	26.4	12823886	63	992436543	ı			
1.30	3.71293 4.48403	6.1	8445.96	14.4	619174 663383	$\frac{26.6}{26.8}$	13317055 13825281	64	1073741824	1			
1.35	5.37824	6.2	9161.33 9924.37	14 6 14.8	710082	27.0	14348907	65 66	1160290625 1252332576				
1.45	6.40973	6 4	10737	15.0	759375	27 2	14888280	67	1350125107	ı			
1.40 1.45 1.50	7.59375	6.5	11603	15.2 15.4	811368	27.4 27.6 27.8	15443752	68	1453933568				
1.55	8.94661	6.6	12523	15.4	866171	27.6	16015681	69	1564031349	ı			
1.60 1.65	10.4858 12.2298	6.7	13501 14539	15.6	923896 984658	27.8	16604430 17210368	70	1680700000 1804229351				
1 70	14.1986	6.9	15640	15.8 16.0	1048576	28.0 28.2	17833868	71 72	1934917632				
1.75 1.80	16.3141	7.0 7.1 7.2 7.3	16807 18042	16.2 16.4	1115771 1186367	28 4	18475309 19135075	78 74 75	2073071593	ı			
1.80	16.3141 18.8957	7.1	18042	16.4	1186367	28.6 28.8	19135075	74	2219006624				
1.85 1.90	21.6700 24.7610	7.2	19349 20731	16.6 16.8	1260493 1338278	$\frac{28.8}{29.0}$	19813557 20511149	75	2373046875 2535525376	1			
1.95	28.1951	7.4	22190	17.0	1419857	29.0	21228253	76 77 78 79	2706784157	ľ			
2.00	32.0000	7.5 7.6	23730	17.2	1505366	29.4	21965275	78	2887174368 3077056399	1			
2.05	32.0000 36.2051	7.6	25355	17.4	1594947	29.6	22722628	79	3077056399	1			
2.10 2.15	40.8410	7.7 7.8	27068	17.6 17.8	1688742	29 8 30.0	23500728	80 81	3276800000	4			
2.10	45.9401 51.5368	7.9	28872	18.0	1786899 1889568	30.5	24300000 26393634	82	3486784401 3707398432	II.			
2.20 2.25 2.30	51.5368 57.6650	8.0	30771 32768	18.2	1996903	$\frac{30.5}{31.0}$	28629151	83	3939040648	ı			
2.30	64.3634	8.1	34868	18.4	2109061	31.5	31013642	84	4182119424	l			
2.35 2.40	71.6703	8.2 8.3	37074	18.6 18.8	2226203	32.0	33554432	85	4437053125	1			
9.45	79.6262	8.4	39390 41821	19.0	2348493 2476099	32.5 33.0	36259082 39135393	86 87	4704270176 4984209207	9			
$\frac{2.45}{2.50}$	97.6562	8.5	41821 44371	19.2	2609193	33.5	42191410	88	5277319168				
$\frac{2.55}{2.60}$	88.2735 97.6562 107.820	8.6	47043	19.4	2747949	34.0	45435424	89	5584059449	10			
2.60	118.814	8.7	49842	19.6	2892547	34.5	48875980	90	5904900000	5			
2.70 2.80 2.90	143.489	8.8 8.9	52773	19.8 20.0	3043168 3200000	35.0	52521875 56382167	91 92	6240321451 6590815232	50			
2.90	172.104 205.111	9.0	55841 59049	20.0	3363232	$\frac{35.5}{36.0}$	60466176	93	6956883693	200			
3.00	243.000	9.1	62403	20.4	3533059	36.5 37.0	64783487	94	7339040224	200			
3.10	286.292	9.2	65908	20.6	3709677	37.0	69343957	95	7737809375	200			
3.00 3.10 3.20 3.30	335.544	9.3	69569 73390	$\frac{20.8}{21.0}$	3893289 4084101	37.5 38.0	74157715 79235168	96 97	8153726976 8587340257	0			
3.40	391.354 454.354	9.4	77378	21.2	4282322	38.5	84587005	98	9039207968	1			
3.50	525.219	9.6	81537	21.4	4488166	39.0	90224199	99	9509900499	1			
3.60	604.662	9.7	85873	21.6	4701850	39.5	96158012			i			

#### CIRCUMFERENCES AND AREAS OF CIRCLES.

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
1	3.1416	0.7854	65	204.20	3318.31	129	405.27	13069.81
2	6.2832	3.1416	66	207.34	3421.19	130	408.41	13273.23
3	9.4248	7.0686	67	210.49	3525.65	131	411.55	13478.22
4 5 6 7	12.5664	12.5664	68	213.63	3631.68	132	414.69	13684 78
5	15.7080	19.635	69	216.77	3739.28	133	417.83	13892.91
6	18.850 21.991	28.274 38.485	70 71	219.91 223.05	3848.45 3959.19	134 135	420.97 424.12	14102.61 14313.88
8	25.133	50.266	72	226.19	4071.50	136	427.26	14526,72
9	28.274	63,617	73	229.34	4185,39	137	430.40	14741.14
10	31.416	78,540	74	232.48	4300.84	138	433.54	14957.12
11	34.558	95.033	75	235.62	4417.86	139	436.68	15174.68
12	37.699	113.10	76	238.76	4536.46	140	439.82	15393.80
13	40.841	132.73	77	241.90	4656.63	141	442.96	15614.50
14 15	43.982 47.124	153.94 176.71	78 79	245.04 248.19	4778.36 4901.67	142 143	446.11	15836.77 16060.61
16	50.265	201,06	80	251.33	5026.55	144	452.39	16286.02
17	53.407	226,98	81	254.47	5153.00	145	455.53	16513.00
18	56.549	254,47	82	257.61	5281.02	146	458.67	16741.55
19	59.690	283.53	83	260.75	5410.61	147	461.81	16971.67
20	62.832	314.16	84	263.89	5541.77	148	464.96	17203.36
21	65.973	346.36	85	267.04	5674 50	149	468.10	17436.62
22 23	69.115 72.257	380.13 415.48	86 87	270.18 273.32	5808.80 5944.68	150 151	471.24 474.38	17671.46 17907 86
24	75.398	452,39	88	276.46	6082.12	152	477.52	18145.84
25	78.540	490.87	89.	279.60	6221.14	153	480.66	18385,39
26	81.681	530,93	90	282,74	6361.73	154	483.81	18626.50
27	84.823	572.56	91	285.88	6503.88	155	486.95	18869.19
28	87.965	615.75	92	289.03	6647.61	156	490.09	19113.45
29	91.106	660.52	93	292.17	6792.91	157	493.23	19359.28
30	94.248	706.86	94 95	295.31 298.45	6939.78 7088.22	158 159	496.37	19606.68
31 32	100.53	754.77 804.25	96	301.59	7238.23	160	499.51 502.65	19855.65 20106.19
33	103.67	855.30	97	304.73	7389.81	161	505.80	20358.31
34	106.81	907.92	98	307.88	7542.96	162	508.94	20611.99
35	109.96	962.11	99	311.02	7697.69	163	512.08	20867.24
36	113.10	1017.88	100	314.16	7853.98	164	515.22	21124.07
37	116.24	1075.21	101	317.30	8011.85	165	518.36	21382.46
38 39	119.38 122.52	1134.11 1194.59	102	320.44	8171.28 8332.29	166 167	521.50 524.65	21642.43 21903.97
40	125.66	1256.64	104	326.73	8494.87	168	527.79	22167 08
41	128.81	1320.25	105	329 87	8659.01	169	530.93	22431.76
42	131.95	1385.44	106	333.01	8824.73	170	534.07	22698.01
43	135.09	1452.20	107	336.15	8992.02	171	537.21	22965.83
44	138.23	1520.53	108	339.29	9160.88	172	540.35	23235.22
45	141.37	1590.43	109	342.43	9331.32	173	543.50	23506.18
46 47	144.51 147.65	1661.90 1734.94	110 111	345.58 348.72	9503.32 9676.89	174 175	546.64 549.78	23778.71 24052.82
48	150.80	1809.56	112	351.86	9852.03	176	552.92	24328.49
49	153 94	1885.74	113	355.00	10028.75	177	556.06	24605.74
50	157.08	1963.50	114	358.14	10207.03	178	559.20	24884.56
51	160.22	2042.82	115	361.28	10386 89	179	562.35	25164.94
52	163.36	2123.72	116	364.42	10568.32	180	565.49	25446 90
53 54	166.50 169.65	2206.18 2290.22	117 118	367.57 370.71	10751.32 10935.88	181 182	568.63	25730.43 26015.53
55	172.79	2375.83	119	373.85	11122.02	183	571.77	26302.20
56	175.93	2463.01	120	376.99	11309.73	184	578.05	26590.44
57	179.07	2551.76	121	380.13	11499.01	185	581.19	26880.25
58	182.21	2642.08	122	383.27	11689.87	186	584.34	27171.63
59	185.35	2733.97	123	386.42	11882.29	187	587.48	27464.59
60	188.50	2827.43	124	389.56	12076.28	188	590.62	27759.11
61	191.64 194.78	2922.47 3019.07	125 126	392.70 395.84	12271.85 12468.98	189 <b>190</b>	593.76 596.90	28055.21
63	197.92	3117.25	127	398.98	12667.69	191	600.04	28352.87 28652.11
64	201.06	3216.99	128	402.12	12867.96	192	603.19	28952.92
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)iam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
193	606.33	29255.30	260	816.81	53092.92	327	1027.30	83981.84
194	609.47	29559.25	261	819.96	58502.11	328	1030.44	84496.28
195	612.61	29864.77	262	823.10	53912.87	329	1033.58	85012.28
196	615.75	30171.86	268	826.24	54325.21	330	1036.73	85529.80
197	618.89	30480.52	264	829.38	54739.11	331	1039.87	86049.03
198	622.04	30790.75	265	832.52	55154.59	332	1043.01	86569.7
199	625.18 628.32	31102.55	266	835.66	55571.63	333	1046.15	87092.0
200	628.32	31415.93	267	888.81 841.95 845.09	55990.25	334	1049.29	87615.8
201		31730.87	268	841.95	56410.44	335	1052.43	88141.3
202	634.60 637.74 640.88	32047.39	269	845.09	56832.20	336	1055.58 1058.72	88668.3
203	051.74	32865.47 32685.13	270	848.23 851.37	57255.53	337 338	1061.86	89196.8 89127.0
204 205	644.03	33006.36	271 272	854.51	57680.43 58106.90	339	1065.00	90258.7
206	647.17	33329.16	273	857.65	58534.94	340	1068.14	90792.0
207	650.31	33653.53	274	860.80	58964.55	341	1071.28	91326.8
208	653.45	33979.47	275	863.94	59395.74	342	1074.42	91863.3
209	656.59	34306.98	276	867.08	59828.49	343	1077.57	92401.3
210	659.73	34636.06	277	870.22	60262.82	344	1080.71	92940.8
211	662.88	34966.71	278	873.36	60698.71	345	1083.85	93482.0
212	666.02	35298.94	279	876.50	61136.18	346	1086.99	94024.7
211 212 213	669.16	35632.73	280	879.65	61575.22	347	1090.13	94569.0
214	672.30	35968.09	281	882.79	62015.82	348	1093.27	95114.8
215	675.44	36305.03	282	885.93	62458.00	349	1096.42	95662.2
216	675.44 678.58 681.73 684.87	36643.54	283	889.07	62901.75 63347.07	350	1099.56	96211.2 96761.8
217	681.73	36983.61	284	892.21 895.35 898.50	63347.07	351	1102.70 1105.84	96761.8
218	684.87	37325.26	285	890.30	63793.97	352	1100.84	97313.9
219	688.01	37668.48 38013.27	286	001.64	64242.43 64692.46	353 354	1108.98 1112.12	97867.6 98422.9
220	691.15 694.29	38359.63	287 288	901.64 904.78	65144.07	355	1115.27	98979.8
222	697.43	38707.56	289	907.92	65597.24	356	1118.41	99538.2
223	700.58	39057.07	290	911.06	66051.99	357	1121.55	100098.2
224	703.72	39408.14	291	914 20	66508.30	358	1124.69	100659.7
225	706.86	39760.78	292	914.20 917.35	669€6.19	359	1127.83	101222.9
226	710.00	40115.00	298	920.49	67425.65	360	1130.97	101787.6
227	713.14	40470.78	294	923.63	67886.68	361	1134.11	102353.8
228	716.28	40828.14	295	926.77	68349.28	365	1137.26	102921.7
229	719.42	41187.07	296	929.91	68813.45	363	1140.40	103491.1
230	722,57	41547.56	297	933.05	69279.19	364	1143.54	104062.1
231	725.71	41909.63	298	936.19	69746.50	365	1146.68	104634.6
232	728.85	42273.27	299	939.34	70215.38	366	1149.82	105208.8
233	731.99	42638.48	300	942.48	70685.83	367	1152.96	105784.4
234	735.13 738.27	43005.26	301	940.62	71157.86	368	1156.11	106361.7
235 236	730.27	43373.61 43743.54	302 303	945.62 948.76 951.90	71681.45 72106.62	369 370	1159.25 1162.39	106940.6
237	744.56	44115.03	304	955.04	72583.36	371	1165.53	107521.0 108102.9
238	747 70	44488.09	305	958.19	73061.66	372	1168.67	108686.5
239	741.42 744.56 747.70 750.84	44862.73	306	961.33	73541.54	373	1171.81	109271.6
240	753.98	45238.93	307	964.47	74022,99	374	1174 96	109858.3
241	757.12	45616.71	308	967.61	74506.01	375	1178.10	110446.6
242	757.12 760.27	45996.06	309	970.75	74990.60	376	1181.24	111036.4
243	763.41	46376.98	310	973.89	75476.76	377	1184.38	111627.8
244	766.55	46759.47	311	977.04	75964.50	378	1187.52	112220.8
245	769.69	47143.52	312	980.18	76453.80	379	1190.66	112815.3
246	772.83	47529.16	313	983.32	76944.67	380	1193.81	113411.4
247	775.97	47916.36	314	986.46	77437.12	381	1196.95	114009.1
248	779.11	48305.13	815	989.60	77931.18	382	1200.09	114608.4
$\frac{249}{250}$	782.26 785.40	48695.47 49087.39	316 317	992.74 995.88	78426.72 78923.88	383 384	1203.23 1206.37	115209.2 115811.6
200	788 54	49087.39	318	999.08	78923.88	904	1206.37	116415.6
251 252	701.68	40875 99	319	1009 17	79922.90	295 386	1212.65	1170913.0
253	791.00	50079 55	320	1002.17 1005.31	80424.77	387	1215.80	117021.1 117628.3
254	788.54 791.68 794.82 797.96	49875.92 50272.55 50670.75	321	11008 45	80928.21	388	1218.94	118236.9
255	801 11	51070.52	322	1011.59	81433 22	389	1222.08	118847.2
256	804.25	51471.85	323	1014.73	81939.80	390	1225.22	119459.0
257	801.11 804.25 807.39	51874.76	324	1011.59 1014.73 1017.88	82447.96	391	1228.36	120072.4
258	810.53	52279.24	325	1021.02	82957.68	392	1231.50	120687.4
259	813.67	52685.29	326	1024.16	83468.98	393	1234.65	121303.9

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
394	1237.79	121922.07	461	1448.27	166913.60	528	1658.76	218956.44
395	1240.93	122541.75	462	1451.42	167638 53	529	1661.90	219786.61
396	1244.07	123163.00	463	1454.56	168365.02	530	1665.04	220618.34
397	1247.21	123785.82	464	1457.70	169093.08	531	1668.19	221451.65
398 399	1250.35 1253.50	124410.21 125036.17	465 466	1460.84 1463.98	169822.72 170553.92	533 533	1671.33 1674.47	222286.58 223122.98
400	1256.64	125663.71	467	1467.12	171286.70	534	1677.61	223961.00
401	1259.78	126292.81	468	1470.27	172021.05	535	1680.75	224800.59
402	1262.92	126923.48	469	1473 41	172756.97	536	1683.89	225641.75
403	1266.06	127555.78	470	1476.55	173494.45	537	1687.04	226484.48
404	1269.20 1272.35	128189.55 128824.93	471	1479.69 1482.83	174233.51 174974:14	538 539	1690.18 1693.32	227328.79 228174.66
405 406	1275.49	129461.89	472 473	1485.97	175716.35	540	1696.46	229022.10
407	1278.63	130100.42	474	1489.11	176460 12	541	1699.60	229871.12
408	1281.77	130740.52	475	1492.26	177205.46	542	1702.74	230721.71
409	1284.91	131382.19	476	1495.40	177952.37	543	1705.88	231573.86
410	1288.05 1291.19	132025.43 132670.24	477 478	1498.54 1501.68	178700.86 179450.91	544 545	1709.03 1712.17	232427.59 233282.89
411	1294.34	133316.63	479	1504.82	180202.54	546	1715.31	234139.76
413	1297.48	133964.58	480	1507.96	180955.74	547	1718.45	234998.20
414	1300.62	134614.10	481	1511.11	181710.50	548	1721.59	235858.21
415	1303.76	135265.20	482	1514.25	182466.84	549	1724.73	286719.79
416 417	1306.90 1310.04	135917.86 136572.10	483 484	1517.39 1520.53	183224.75 183984.23	550 551	1727.88 1731.02	237582.94 238447.67
418	1313.19	137227.91	485	1523.67	184745 28	552	1734 16	289313.96
419	1316.33	137885.29	486	1526,81	184745.28 185507.90 186272.10	553	1734.16 1737.30	240181.83
420	1319.47	138544.24	487	1529.96	186272.10	554	1740.44	241051.26
421	1322.61	139204.76	488	1533.10	187037.86	555	1743.58	241922.27
422 423	1325.75 1328.89	139866.85 140530.51	489 <b>490</b>	1536.24 1539.38	187805.19 188574.10	556 557	1746.73 1749.87	242794.85 243668.99
424	1332 04	141195.74	491	1542.52	189344.57	558	1753.01	244544.71
425	1335.18	141862.54	492	1545.66	190116.62	559	1756.15	245422 00
426	1338.32	142530.92	493	1548.81	190890.24	560	1759.29	246300.86
427 428	1341.46	143200.86	494	1551.95	191665,43 192442,18	561	1762.43	247181.30
428	1344.60	143872.38 144545.46	495 496	1555 09 1558.23	193442.16	562 563	1765.58 1768.72	248063.30 248946.87
430	1347.74 1350.88	145220.12	497	1561.37	194000.41	564	1771.86	249832.01
431	1354.03	145896.35	498	1564.51	194781.89	565	1775.00	250718.73
432	1357.17 1360.31	146574 15	499	1567.65 1570.80	195564.93	566	1778.14	251607.01
433 434	1363.45	147258.52 147984.46	500 501	1573.94	196349.54 197135.72	567 568	1781.28 1784.42	252496.87 253388.30
435	1366.59	148616.97	502	1577.08	197923.48	569	1787.57	254281.29
436	1369.73	149301.05	503	1580.22	198712.80	570	1790.71	255175:86
437	1372.88	149986.70	504	1583.36	199503.70	571	1793.85	256072.00
438 439	1376.02 1379.16	150673.93 151362.72	505 506	1586 50 1589.65	200296.17 201090.20	572 573	1796.99 1800.13	256969.71 257868.99
440	1382.30	152053.08	507	1592.79	201080.20	574	1803.27	258769.85
441	1385.44	152745.02	508	1595.93	202682.99	575	1806.42	259672.27
442	1388.58	153438 53	509	1599.07	203481.74	576	1809.56	260576.26
443 444	1391.73 1394.87	154133.60 154830.25	510	1602.21 1605.35	204282,06 205083,95	577	1812.70 1815 84	261481.83 262388.96
445	1398.01	155528.47	511 512	1608.50	205887.42	578 579	1818.98	263297.67
446	1401 15	156228.26	513	1611.64	206692.45	580	1822.12	264207.94
447	1404.29 1407.43	156929.62	514	1614.78 1617.92	207499.05	581	1825.27	265119.79
448	1407.43	157632.55	515	1617,92	208307.23	582	1828.41	266033.21
449 <b>450</b>	1410.58 1413.72	158337.06 159043.13	516 517	1621.06 1624.20	209116.97 209928.29	583 584	1831.55 1834.69	266948.20 267864.76
451	1416.86	159750.77	518	1627.34	210741.18	585	1837.83	268782,89
452	1420.00	160459.99	519	1630.49	211555.63	586	1840.97	269702.59
453	1423.14	161170.77	520	1633.63	212371.66	587	1844.11	270623.86
454	1426.28	161883.13	521	1636.77	213189,26 214008,43	588 589	1847.26 1850.40	271546.70
455 456	1429.42 1432.57	162597.05 163312.55	522 523	1639.91 1643.05	214008.45	590	1853.54	272471.12 273397.10
457	1435.71	164029.62	524	1646.19	215651.49	591	1856.68	274324.66
458	1438.85	164748.26	525	1649.34	216475.37	592	1859.82	275253.78
459	1441.99	165468.47	526	1652.48	217300.82	593	1862.96	276184.48
460	1445.13	166190.25	527	1655.62	218127.85	594	1866.11	277116.75

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
595	1869.25	278050.58	663	2082.88	345236.69	731	2296.50	419686.15
596	.1872.39	278985.99	664	2086.02	346278.91	732	2299.65	420835.19
597	1875.58	279922.97	665	2089.16	347322.70	733	2302.79	421985.79
598	1878.67 1881.81	280861.52 281801 65	666	2092.30 2095.44	348368.07	734	2305.93	423137.93 424291.73
599 <b>600</b>	1884.96	282743.34	667 668	2095.44	349415.00 350463.51	735 736	2309.07 2312.21	425447.0
601	1888.10	283686.60	669	2098.58 2101.73 2104.87	351513.59	737	2315.35	426603.94
602	1891 94	284631 44	670	2104 87	352565.24	738	2318.50	427762.40
603	1891.24 1894.38	284631.44 285577.84	671	2108.01	353618.45	739	2321.64	428922.48
604	1897.52	286525.82	672	2111.15	354673 24	740	2324.78	430084.08
605	1900.66	287475.36	678	2111.15 2114.29	355729.60	741	2327.92	431247.21
606	1903.81	288426.48	674	2117.43	356787.54	742	2331.06	432411.93
607	1906.95	289379.17	675	2120.58	357847.04	743	2334.20	433578,27
608	1910.09	290333.43	676	2123.72	358908.11	744	2337.34	434746.16
609	1913.23	291289.26	677	2126.86	359970.75	745	2340.49	435915.6
610	1916.37	292246.66	678	2130.00	361034.97	746	2343.63	437086.6
611	1919 51	293205.63	679	2133.14	362100.75	747	2346.77	438259.24
612	1922.65	294166.17	680	2136.28	363168.11	748	2349.91	439433.41
613 614	1925.80 1928.94	295128.28 296091.97	681 682	2139.42 2142.57	364237.04 365307.54	749 750	2353.05 2356.19	440609 16
615	1932.08	297057.22	683	2142.57	366379.60	751	2359.34	441760.4
616	1935.22	298024.05	684	2148.85	367453.24	752	2362.48	444145.8
617	1938.36	298992.44	685	2151.99	368528.45	753	2365.62	445327.8
618	1941.50	299962.41	686	2155.13	369605.23	754	2368.76	446511.4
619	1944.65	300933.95	687	2158.27	370683.59	755	2371.90	447696.5
620	1947.79 1950.93	301907.05	688	9161 49	371763.51	756	2375.04	448883.3
621	1950.93	302881.73 303857.98	689	2164.56 2167.70 2170.84	372845.00	757	2378.19	450071.68
622	1954.07	303857.98	690	2167.70	373928.07	758	2381.33	451261.5
623	1957.21	304835.80	691	2170.84	375012.70	759	2384.47	452452.90
624	1960.35	305815.20	692	2173.98	376098.91	760	2387.61 2390.75	453645.9
625	1963.50	306796.16	693	2177.12 2180.27	377186.68	761	2890.75	454840.5
626	1966.64	307778.69	694	2180.27	378276.03	762	2893.89 2397.04	456036.73
627 628	1969.78 1972.92	308762.79	695	2183.41	379366.95	763	8400 19	457234.40 458433.73
629	1976.06	309748.47 310735.71	696 697	2186.55 2189.69	380459.44 381553.50	764 765	2400.18 2403.32	459634.6
630	1979.20	311724.53	698	2192.83	382649.13	766	2406.46	460837.08
631	1982.35	312714.92	699	2195.97	383746.33	767	2409.60	462041.10
632	1985.49	313706.88	700	2199.11	384845.10	768	2412.74	463246.69
633	1988.63	314700.40	701	2202.26	385945.44	769	2415.88	464453.8
634	1991.77	315695.50	702	2205,40	387047.36	770	2419.03	465662.57
635	1994.91	316692.17	703	2208.54	388150.84	771	2422.17	466872.83
636	1998.05	317690.42	704	2211.68	389255.90	772	2425.31	468084.74
637	2001.19	318690.23	705	2214.82	390362.52	778	2428.45	469298.18
638	2004.34	319691.61	706	2217.96	391470.72	774	2431.59	470513.19
639	2007.48	320694.56	707	2221.11	392580.49	775	2434.73	471729.77
640 641	2010.62 2013.76	321699.09 322705.18	708 709	2224 .25 2227 .39	393691.82 394804.73	776	2437.88	472947.9:
642	2016.76	323712.85	710	2230.53	394804.73	777	2441.02 2444.16	474167.65 475388.94
643	2020.04	324722.09	711	2233.67	397035 26	778 779	2447.30	476611.81
644	2023.19	325732.89	712	2236.81	398152.89	780	2450.44	477836.24
645	2026.33	326745.27	713	2239.96	399272.08	781	2453.58	479062.25
646	2029.47	327759.22	714	2243.10	400392.84	782	2456.73	480289.88
647	2032.61	328774.74	715	2246.24	401515.18	783	2459.87	481518.97
648	2035.75	329791.83	716	2249.38	402639.08	784	2463.01	482749.69
649	2038,89	330810.49	717	2252.52	403764.56	785	2466.15	483981.98
650	2042.04	331830.72	718	2255.66	404891.60	786	2469.29	485215.84
651	2045.18	332852.53	719	2258.81	406020.22	787	2472.48 2475.58	486451.28
652	2048.32	333875.90	720	2261.95	407150.41	788	2475.58	487688.28
653	2051.46	334900.85	721	2265.09	408282.17	789	2478.72	488926.85
654	2054.60	335927.36	722	2268.23	409415.50	790	2481.86	490166.99
655	2057.74 2060.88	336955.45	723	2271.37	410550.40	791	2485.00	491408.71
656	2060.88	337985.10	724	2274.51	411686.87	792 793	2488.14 2491.28	492651.99 493896.85
657 658	2064.03	339016.33 340049.13	725 726	2277.65 2280.80	412824.91 418964.52	794	2491.26	495090.00
659	2067.17 2070.31	341083.50	727	2283.94	415105.71	795	2497.57	496391.27
660	2073.45	342119.44	728	2287.08	416243.46	796	2500.71	497640.84
661	2076.59	343156.95	729	2290.22	417392.79	797	2503.85	498891.98

	CIRC	UMPERE	HOE	AND	AREAS	Or C	INCLES	5. 101
Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
799	2510.13	501398.97	867	2723.76	590375.16	935	2937.39	686614.71
800	2513.27	502654.82	868	2726.90	591787.83	936	2940.53	688084.19
801	2516.42	503912.25	869	2730.04	593102.06	937	2943.67	689555.24
802	2519.56 2522.70	505171.24	870	2733.19 2736.33	594467.87 595835.25	93S 939	2946 81 2949.96	691027.86
803 804	2525.84	506431.80 507693.94	871 872	2739.47	597204.20	940	2953.10	692502.05 693977.82
805	2528.98	508957.64	873	2742.61	598574.72	941	2956.24	695455,15
806	2532.12	510222.92	874	2745.75	599946.81	942	2959.38	696934.06
807	2535.27	511489.77	875	2748.89	601320.47	943	2962.52	698414.53
808	2538.41	512758.19	876	2752.04	602695.70	944	2965.66	699896.58
809	2541.55	514028.18	877	2755.18	604072.50	945	2968.81	701380.19
810	2544.69	515299.74	878	2758.32	605450.88	946	2971.95	702865.38
811 812	2547.88 2550.97	516572.87 517847.57	879 880	2761.46 2764.60	606830.82 608212.34	947 948	2975.09 2978.23	704352.14 705840.47
813	2554.11	519123.84	881	2767.74	609595.42	949	2981.37	707330.37
814	2557.26	520401.68	882	2770.88	610980.08	950	2984.51	708821.84
815	2560.40	521681.10	883	2774.03	612366.31	951	2987.65	710314.88
816	2563.54	522962.08	884	2777.17	613754.11	952	2990.80	711809.50
817	2566.68	524244.63	885	2780.31	615143,48	953	2993.94	713305.68
818	2569.82	525528.76	886	2783.45	616534.42	954	2997.08	714803.43
819	2572.96	526814.46	887	2786.59	617926.93	955	3000.22	716302.76
820	2576.11	528101.73 529390.56	888 889	2789.73 2792.88	619321.01 620716.66	956 957	3003.36 3006.50	717803.66
821 822	2579.25 2582.39	530680.97	890	2796.02	622113.89	958	3009.65	719306.12 720810.16
823	2585.53	531972.95	891	2799.16	623512.68	959	3012.79	722315.77
824	2588.67	533266.50	892	2802.30	624913.04	960	3012.79 3015.93	723822.95
825	2591.81	534561.62	893	2805,44	626314.98	961	3019.07	725331.70
826	2594.96	535858.32	894	2808.58 2811.73	627718.49 629123.56	962	3022.21	726842.02
827	2598.10	537156.58	895	2811.73	629123.56	963	3025.35	728353.91
828	2601.24	538456 41	896	2814.87	630530.21	964	3028.50	
829	2604.38	539757.82	897	2818.01	631938.43	965	3031.64	731382.40
830	2607.52 2610.66	541060.79 542365.34	898 899	2821.15 2824.29	633348,22 634759.58	966 967	3034.78 3037.92	732899.01
831 832	2613.81	543671.46	900	2827.43	636172.51	968	3041.06	734417.18 735936.93
833	2616.95	544979.15	901	2830.58	637587.01	969	3044.20	
834	2620.09	546288.40	902	2833.72	639003.09	970	3047.34	738981.13
835	2623.23	547599.23	903	2836.86	640420.73	971	3050.49	740505.59
836	2626.37	548911.63	904	2840.00	641839.95	972	3053.63	742031.62
837	2629.51	550225.61	905	2843.14	643260.73	973	3056.77	743559.22
838	2632.65	551541.15	906	2846.28	644683.09	974	3059.91	745088.39
839	2635.80	552858.26	907 908	2849.42 2852.57	646107.01 647532.51	975 976	3063.05	746619.13
840 841	2638.94 2642.08	554176.94 555497.20	909	2855.71	648959.58	977	3066.19 3069.34	~40605 90
842	2645.22	556819.02	910	2858.85	650388.22	978	3009.34	749685.32 751220.78
843	2648 36	558142.42	911	2861.99	651818.43	979	3075.62	752757.80
811	2651.50	558142.42 559467.39	912	2865.13	653250.21	980	3078.76	754296.40
845	2654.65	560793.92	913	2868.27	654683.56	981	3072.48 3075.62 3078.76 3081.90	755836.56
846	2657.79 2660.93	562122.03	914	2871.42	656118.48	982	3085.04	757378.30
847	2660.93	563451.71	915	2871.42 2874.56 2877.70	657554.98	983	3088.19	
848	2664.07 2667.21	564782.96 566115.78	916 917	2880.84	658993.04 660432.68	984 985	3091.33 3094.47	760466.48
849 850	2670.35	567450.17	918	2883.98	661873.88	986	3097.61	762012.93 763560.95
851	2673.50	568786.14	919	2887.12	663316 66	987	3100.75	765110.54
852	2676.64	570128.67	920	2890.27	664761.01	988	3103.89	766661.70
853	2679.78	571462.77	921	2893.41	666206.92	989	3107.04	768214.44
854	2682.92	572803.45	922	2896.55	667654.41	990	3110.18	769768.74
855	2686.06	574145.69	923	2899.69	669103.47	991	3113.32	771324.61
856	2689.20	575489.51	924 925	2903.83	670554.10	992	3116.46	772882.06
857 858	2692.34 2695.49	576834.90 578181.85	925	2905.97 2909.11	672006.30 673460.08	993 994	3119.60 3122.74	774441.07 776001.66
859	2698.63	579530.38	927	2912.26	674915.42	995	3125.88	777563.82
860	2701 77	580880.48	928	2915.40	676372.33	996	3129.03	779127.54
861	2701.77 2704.91	582232.15	929	2918.54	677830.82	997	3132.17	780692.84
862	1 2708 05	583585.39	930	2921.68	679290.87	998	3135.31	782259.71
863	2711.19 2714.34	584940.20	931	2924.82	680752.50	999	3138.45	783828.15
864	2714.34	586296.59	932	2927.96	682215.69	1000	3141.59	785398.16
865	2717.48 2720 62	587654.54	933	2931.11	683680.46			
866	1 2720 62	589014.07	934	2934.25	685146.80	1		1

# CIRCUMFERENCES AND AREAS OF CIRCLES Advancing by Eighths,

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
1/64	.04909	.00019	2 3/8 7/16 1/5 9/16	7.4613	4.4301	6 1/8	19.242	29.465
1/64 1/32	.09818	.00077	7/16	7.6576	4.6664	1/4	19.635	30.680
3/61	.14726	.00173	1/2	7.8540	4.9087	3/8	20.028	31.919
1/16	.19635	.00307	9/16	8.0503	5.1572	1/2	20.420	33,188
3/32	.29452	.00690	9/8	8.2467	5.4119	5/8	20.813	34.47
1/16 3/32 1/8	.39270	.01227	11/16	8.4430	5.6727	6 1/8	21 206	35.78
0/52	.49087	.01917	19/10	8.6394 8.8357	5.9396 6.2126	7. 1/8	21.598 21.991	37,123 38,485
3/16 7/32	.68722	.03758	76	9.0321	6.4918		22.384	39.87
1,00	.00122	.00100	34 13/16 78 15/16	9.2284	6.7771	1%	22.776	41.28
1/4	.78540	.04909	,			1/8 1/4 3/8 1/5 3/4 7/8	23.169	42.718
9/32	.88357	.06213	3.	9.4248	7 0686	1/8	23.562	42.718 44.179
5/16	.98175	.07670	1/16	9.6211	7.3662	5/8	23.955	45.664
11/32	1.0799	.09281	1/8	9.8175	7.6699	3/4	24.347	47.178
5/16 11/32 3/6 13/32	1.1781 1.2763	.11045	3/16	10.014 10.210	7.9798 8.2958	s. <sup>1/8</sup>	24.740 25.133	48.707 50.265
7/16	1.3744	.15033	5/16	10.407	8.6179		25.525	51.849
15/32	1.4726	.17257	3/6	10.603	8.9462	1/1	25.918	53.456
10,00	1.1140		7/16	10.799	9.2806 9.6211	3%	26.311	55.088
1/2	1 5708	.19635	5/16 3/8 7/16 1/2 9/16	10.996	9.6211	1/8 1/4 3/8 1/2 5/8 1/8	26.704	56.74
17/32	1.6690	.22166	9/16	11.192	9.9678	5/8	27.096	58.426
9/16	1.7671	.24850	5/8 11/16 3/4	11.388	10.321	34	27.489	60.13:
19/32	1.8653	.27688	11/16	11.585 11.781	10.680 11.045	9. 1/8	27.882 28.274	61.862
91/30	1.9635 2.0617	.33824	12/16	11.751	11.416		28.667	63.617
9/16 19/32 5/8 21/32 11/16 23/32	2.1598	.37122	13/16 7/8 15/16	12.174	11.793	1/8 1/4 3/8 1/8 1/8 3/4 8	29.060	67.201
23/32	2.2580	.40574	15/16	12.370	12.177	3%	29.452	69.029
			4.	12.566	12.566	1/2	29.845	70.882
3/4 25/32 13/16	2.3562	.44179	1/16	12.763	12.962	5%	30.238	72.760
25/32	2.4544	.47937	3/16 1/4 5/16 3/8	12.959	13.364	3/4	30.631	74.662
13/16	2.5525	.51849	3/16	13.155 13.352	13.772	10.78	31.023	76.589
27/32	2.6507 2.7489	.55914 .60132	5/16	13.548	14.186 14.607		31.416 31.809	78.540 80.516
7/8 29/32	2 8471	.64504	36	13.744	15.033	1/8 1/4 3/8 1/2 8/4 8/4 8/4 8/4 8/4 8/4 8/4 8/4 8/4 8/4	32.201	82.516
15/16	2.9452	.69029		13.941	15.466	3%	32.594	84.541
15/16 31/32	3.0434	.73708	9/16 5/8	14.137	15.904	1/2	32.987	86.590
			9/16	14.334	16.349	5/8	33.379	88.664
1/10	3.1416	.7854	11/10	14.530 14.726	16.800	34	33.772 34.165	90.768
1/16 1/8 3/16	3.3379 3.5343	.8866	11/16 3/4 13/16	14.720	17.257 17.728	11 1/8	34.558	92.886
3/16	3.7306	1.1075	13/16	15.119	18.190	1/6	34.950	97.20
1/4	3.9270	1.2272	7/8	15.315	18.665	1/4	35.343	99.402
5/16	4.1233	1.3530	10/10	15 512	19.147	3/8	35.343 35.736	101.62
3/8 7/16	4.3197	1.4849	5	15.708	19.635	1/2	36.128	103.87
7/16	4.5160	1.6280	1/16 1/8	15.904	20.129	38	36.521	106.14
9/16	4.7124 4.9087	1.7671	3/16	16.101 16.297	20.629 21.135	94 74	36.914 37.306	108.43 110.75
5/8	5.1051	2.0739	1/1	16.493	21.648	94 78 11. 18 144 18 18 18 18 18 18 18 18 18 18 18 18 18	37.699	113.10
11/16	5.3014	2.2365	5/16 5/16 3/8 7/16	16.690	22.166	12 1/8 1/4 8/22/8	38.092	115.47
3/4	5.4978	2.4053	3/8	16.886	22,691	1/4	38.485	117.86
13/16	5.6941	2.5802	7/16	17.082	23.221	3/8	38.877	120.28
7/8 15/16	5.8905	2.7612	9/16 5/8	17.279	23.758	1/2	39.270	122.72
15/16	6.0868	2.9483	9/16	17.475	24.301	%8	39.663	125.19
)	6.2832	3.1416	11/16	17.671 17.868	24.850 25.406	24	40.055 40.448	127.68 130.19
1/16	6.4795	3.3410	11/16 34 13-16	18.064	25.967	113.	40.448	132.73
1/8	6.6759	3.5466	13-16	18.261	26.535	1/8	41.233	135.30
3/16	6.8722	3.7583	7/8 15-16	18.457 18.653	27.109 27.688	1/4	41.626	137.89
1/4	7.0686	3.9761	15-16	18.653	27.688	1/8 1/4 3/8	42.019	140.50
5/16	7.2649	4.2000	6.	18.850	28.274	1/2	42.412	143.14

1

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
13 5%	42.804	145.80	21 %	68.722	375.83	30 1/8 1/4 3/8 1/3/8 1/8 3/4/8 31/8	94.640	712.76
3/4	43.197	148.49		69.115 69.508	380.13	1/4	95.053	718.69
14.78	43.590	151.20 153.94	1/8	69.508	384.46 388.82	18	95.426	724 64 730.62
14.	43.982 44.375	156.70	3/8	70.293	393.20	52	95.819 96.211	736.62
1/4	44.768	159.48	1%	70.686	397.61	3%	96.604	742.64
3/8	45.160	162.30	1/2 5/8 3/4 2/8	71.079	402.04	7/8	96.997	748.69
1/2	45.553	165.13	34	71.471	406.49		97.389	754.77
9/8 3/	45.946 46.338	167.99 170.87	23. 18	71.864 72.257	410.97	1/8/4/8/27/8/44/8	97.782 98.175	760.87 766.99
72	46,731	173.78		72.649	420.00	3%	98.567	773.14
15.	47.124	176.71	1/2/4/20/21/20/4/20 2/4/20/21/20/4/20	73.042	424.56	1/2	98.960	779.31
1/8	47.517	179.67	3/8	73.435	429.13	28	99.353	785.51
34	47.909 48.302	182.65 185.66	23	73.827 74.220	433.74 438.36	23	99.746 100.138	791.73 797.98
18	48.695	188.69	3/4	74.613	443.01	32. 8	100.138	804.25
5%	49.087	191,75	猛	75.006	447.69		100.924	810.54
3/4	49.480	194.83	24.	75 398	452.39	1/8/4/8/27/8/4/8	101 216	816.86
7/8	49.873	197.93	1/8	75.791 76.184 76.576	457.11 461.86	3/8	101.709 102.102 102.494 102.887	823.21
16.	50.265 50.658	201.06	3/4	76.184	466.64	52	102,102	829.58 835.97
1/4	51.051	207.39	1/8	76.969	471.44	3/4	102.887	842.39
3%	51.444	204.22 207.39 210.60	1/2 5/8 3/4 7/8	77.362	476.26	3/8	103.280	848.83
1/2	51.836	213.82	3/4	77.362 77.754	481.11	33.	103.673	855.30
28	52.229	217.08	25.78	78.147	485.98	1/0/44/20/20/20/24/20/20/20/20/20/20/20/20/20/20/20/20/20/	104.065	861.79
24	52.622 53.014	220.35 223.65	20.	78.540 78.933	490.87 495.79	82	104.458 104.851	868.31 874.85
17.28	53.407	226.98	1/8 1/4	79.325	500.74	128	105.243	881.41
1/8	53.800	230.33	3/8	79.718	505.71	5%	105.636	888.00
1/4	54.192	233.71	1/2	80.111	510.71	3/4	106.029	894.62
3/8	54.585 54.978	237.10	1/2 5/8	80.503	515.72	34. 18	106.421	901.26
5%	55.371	240.53 243.98	3/4 7/8	80.896 81.289	520.77 525.84		106.814 107.207	907.92 914.61
3/4	55.763	247.45	26.	81.681	530.93	1/8 1/3/8 1/	107.600	921.32
. <sup>3</sup> /8	56.156	250.95	1/8	82.074	536.05	3/8	107.992 108.385	928.06
18.	56.549	254.47	14 38 15 58 4	82.467	541.19 546.35	1/2	108.385	934.82
1/8	56.941	258.02 261.59	28	82 860 83,252	551 55	2/8	108.778 109.170	941.61 948.42
36	57.334 57.727	265.18	56 56	83.645	551.55 556.76	74	109.563	955.25
1%	58.119	268.80	\$%	84.038	562.00	35.	109.956	962.11
5/8	58.512	272.45	1/8	84.430	567.27	1/8	110.348	969.00
3/4	58.905 59.298	276.12 279.81	27.	84.823	572.56 577.87	14	110.741 111.134	975.91 982.84
19.	59.690	283.53	1/8 1/4	85.216 85.608	583.21	1/8	111.527	989.80
1/8	60.083	287.27	3/2	86.001	588.57	5%	111.919	996.78
14	60.476	291.04	3/8 1/2 5/8	86.394	593.96	1/8 1/4 3/8 1/3/8 3/4 8/8	112.312	1003.8
3/8	60.868	294.83	5/8	86.786	599.37	7/8	112.705	1010.8
52	61.261 61.654	298.65 302.49	78 34 78	87.179 87.572	604.81 610.27	36.	113.097 113.490	1017.9 1025.0
3/4	62.046	306.35	28.	87.965	615.75	1/8	113.883	1032.1
78	62.439	310.24	1/8	88.357	621.26	1/4 3/8 1/3 5/8 3/4 2/8	114.275	1039.2
20.	62.832	314.16	1/4	88.750	626 80	1/2	114.668	1046.3
1/8	63.225 63.617	318.10	8/8	89.143	632.36	28	115.061	1053.5
32	64.010	322.06 326.05	52	89.535 89.928	637.94 643.55	34	115.454 115.846	1060.7 1068.0
1/2	64 403	330.06	14 86 14 58 14 58	90.321	649.18	37. 8	116.239	1075.2
5%	64.795 65.188	334.10 338.16	7/8.	90.321 90.713	654.84		116 600	1082.5
3/4	65.188	338.16	29.	91.106	660.52	1/8 1/4 3/8 1/2 5/8 3/4 3/8	117.024 117.417 117.810 118.202	1089.8
21.78	65.581 65.973	342.25 346.36	1/8	91.499	666.23	3/8	117.417	1097.1
1/6	66.366	350.50	34	91.892 92.284	671.96 677.71	5%	118 202	1111.8
14	66.759	354.66	1/3	92.677	683.49	3/4	118.596	1119.2
8/8	67.152	358.84	5%	93.070	689.30	3/8	118.988	1126.7
1/3	67.544	363.05	3/4	93.462	695.13	38.	119.381	1134.1
2/8	67.937 68.330	367.28 371.54	1/8	93.855	700.98	1/8 1/4	119.773 120.166	1141.6

Diam.	Circum.	Area.	Diam.	Circum.	Area.	Diam.	Circum.	Area.
383%	120.559	1156.6	465%	146.477	1707.4	54 7/8	172,395	2365.0
1/2	120 951	1164.2	3/4 7/8	146.869 147.262	1716.5	55.	172.788 173.180	2375.8
3/8	121.344	1164.2 1171.7 1179.3	47.78	147,262	1725.7 1734.9	1/8	173.180 173.573	2386.6 2397.5
1/2 5/8 3/4 2/8	121.344 121.787 122.129	1186.9	1/	147.655 148.048	1744.2	1/8 1/4 3/8	178.966	2408.3
39.	122.522	1194.6	1/8 1/4	148.440	1758.5	1/9	174.358	2419.2
1/8 1/4	122.915	1202.3 1210.0	98	148.833	1762.7 1772.1	3/4	174.751	2430.1
74 8%	123.308 123.700	1217.7	1/2 5/6	149.226 149.618	1781.4	74	175.144 175.536	2441.1 2452.0
1/2	124.093	1225,4	7% 5% 3/4 7/8	150.011	1790.8	90.	175.929	2463.0
3/8 1/2 5/8 3/4 7/8	124.486	1233.2 1241.0	18	150.404	1800.1	1/8 1/4 3/8	176.322	2474.0
7/6	124.878 125.271	1248.8	48.	150.796 151.189	1809.6 1819.0	3/4 3/6	176.715 177.107	2485.0 2496.1
40.	125.664	1256.6	14	151.582	1828.5	1/2	177.500 177.893	2507.2
1/8	126.056	1264.5 1272.4	3/8	151.975	1837.9 1847.5	1/2 5/8 8/4 7/8	177.893 178.285	2518.3
34	126.449 126.842	1280.3	52	152.367 152.760	1847.5	74	178.285	2529.4 2540.6
1/2	127.235	1288.2	1/8 1/4 8/8 1/2 5/8 3/4	153.153	1866.5	57.	179.071	2551.8
1/8 1/4 3/8 1/2 5/8 3/4 7/8	127.627	1296.2	1/8	153.545	1876.1	1/8 • 1/4 8/8 1/2 5/8	179.463	2563.0
%4 7%	128.020 128.413	1304.2 1312.2	49.	153.938 154.331	1885.7 1895.4	74 82	179.856 180.249	2574.2 2585.4
	128.805	1320.3	1/4	154.723	1905.0	1/6	180.642	2596.7
11. 1/8 1/4 3/8 1/2 5/8	129.198	1328.3	1/8 1/4 3/8 1/6	155.116	1914.7	5%	181.034	2608.0
1/4 8/2	129.591 129.983	1336.4 1344.5	1/2 5/2	155.509 155.902	1924.4 1934.2	92 78	181.427 181.820	2619.4 2630.7
1%	120 276	1352.7	78 3/4	156.294	1943.9	58.	182.212	2642.1
5%	130.769 131.161 131.554	1360.8	5/8 5/8 3/4 7/8	156 687	1953.7		182.605	2653.5
3/4	131.161	1369.0 1377.2	50.	157.080	1963.5 1973.3	34	182.998 183.390	2664.9 2676.4
42.	131.947	1385.4	78 1/4	157.472 157.865	1983.2	1/8	183.783	2687.8
	132.340	1393.7	3/8	158.258	1993.1	1/8 1/4 3/8 1/2 5/8	184.176	2699.3
1/8 1/4 3/8 1/8 1/8 3/4 8 1/8	132.732	1402.0	1/8 1/4 3/8 1/2 5/8 3/4	158.650	2003.0 2012.9	3/4	184.569 184.961	2710.9 2722.4
28	133.125 133.518	1410.3 1418.6	3/8	159.043 159.436	2012.9	59.	185,354	2734.0
5%	133.910	1427.0	3/8	159.829	2032.8	1/8 1/4	185.747	2745.6
3/4	134.303	1435.4	51.	160.221	2042.8	1/4	186.139	2757.2
43. 8	134.696 135.088	1443.8 1452.2	1/8 1/4	160.614 161.007	2052.8 2062.9	3/8 1/3	186.532 186.925	2768.8 2780.5
	135.481	1460.7	3/8 1/8	161,399	2073.0	1/2 5/8 3/4 7/8	187.317 187.710 188.103	2792.2
1/8 1/4 8/8 1/2 5/8	135.874	1469.1	1/2	161,399 161,792	2083.1	3/4	187.710	2803.9
% 1/4	136,267 136,659	1477.6 1486.2	1/2 5/8 3/4 2/8	162.185 162.577	2093.2 2103.3	60. 8	188.103	2815.7 2827.4
5/8	137.052	1494.7	7/4	162.970	2113.5	1/8	188.888	2839.2
3/4 7/8	137.445	1503.3	5%.	163.363	2123.7	1/8 1/4	189.281	2851.0
44.78	137.837 138.230	1511.9 1520.5	1/8 1/4	163.756 164.148	2133.9 2144.2	3/8 1/6	189.674 190.066	2862.9 2874.8
14 1/8 1/4 8/8 1/2 5/8	138.623	1529.2	3/8 1/2	164.541	2154.5	1/2 5/8 3/4 7/8	190.459	2886.6
1/4	139.015	1537.9		164.934	2164.8	3/4	190.852	2898.6
3/8 1/6	139.408 139.801	1546.6 1555.3	5%	165.326 165.719	2175.1 2185.4	61. 8	191.244 191.637	2910.5 2922.5
5/8	140.194	1564.0	3/4 7/8	166.112	2195.8		192.030	2934.5
3/4 7/8	140.586	1572.8 1581.6	53.	166.504	2206.2	1/8 1/4 8/8	192.423	2946.5
45.	140.979	1581.6	1/8 1/4	166.897 167 290	2216.6 2227.0	% 1/6	192.815 193.208	2958.5 2970.6
	141.372 141.764	1599.3	3/8	167,290 167.683	2227.0 2237.5	1/2 5/8	193.601	2982.7
1/8 1/4 3/8 1/9 5/8 3/4	142.157	1608.2	1/4	168.075	2248.0	3/4	193.998	2994.8
5/8 1/4	142.550 142.942	1617.0 1626.0	5% 3%	168.468 168.861	2258.5 2269.1	$62.$ $\frac{1}{8}$	194.386 194.779	3006 9 3019.1
5%	143.335	1634.9	3% 3%	169.253	2279.6	1/8	195.171	3031.3
34	143.728	1643.9	54.	169.646	2290.2	1/4	195.564	3043.5
46.	144.121 144.513	1652.9 1661.9	1/8	170.039 170.431	2300.8 2311.5	3/8 1/6	195.957 196.350	3055.7 3068.0
	144.906	1670.9	3/4 3/8	170.824	2322.1	5%	196.742	3080.3
1/8 1/4 3/8	145.299	1680.0		171.217	2332.8	3/4	197.135	3092.6
3/8 1/4	145.691 146.084	1689.1 1698.2	5% 3%	171.609	2343.5	63 78	197.528 197.920	3104.9
1/2	140.084	1098.2	9/4	1475.002	2004.0	• 00-	191.920	2.1116

	CIRCU:	MFERE	ENCES	AND A	REAS	OF CI	RCLES.	111
Diam.	Circum.	Area.	Diam.	Circum,	Area.	Diam.	Circum.	Area.
63 1/8	198.313 198.706	3129.6	71 %	224.231	4001.1	795%	250.149	4979.5
1/4 3/8	198.706	3142.0	1/2 5/8	224.624	4015.2	34	250 542	4995.2
%8 1/2	199.098 199.491	3154.5 3166.9	% 3/2	225.017 225.409	4029.2 4043.3	80. 8	250.935	5010.9 5026.5
1/3 5/8 8/4	199.884	3179.4	78	225.802	4057.4	1/8	251.327 251.720 252.113 252.506 252.898	5042.3
34	200.277	3191.9	72.	226.195	4071.5	1/1	252.113	5058.0
1/2	200.669	3204.4 3217.0	1/8 1/4	226.587	4085.7	3%	252.506	5073.8
04.	201.062 201.455	3229.6	14 38	226.980	4099.8 4114.0	52	252.898 253.291	5089.6 5105.4
1/8 1/4 3/8 1/2 5/8	201.847	3242.2	1/6	227.373 227.765 228.158	4128 2	5/8 3/4	253.684	5121 2
3/8	201.847 202.240 202.633	3254.8	79 5/8 3/4 7/8	228.158	4142 5	1/8	254.076	5137.1
29	202.633	3267.5	34	228,551	4156.8 4171.1 4185.4	81.	254.469	5153.0
9/8	203.025 203.418	3280.1 3292.8	73. 8	228.944 229.336	4171.1	1/8	254.862 255.254	5168.9 5184.9
3/4	203.811	3305.6	1/8	229.729	4199.7	1/4 3/8	255.647	5200.8
60.	204.204	3305.6 3318.3	1/4	230 122	4914 1	16	256,040	5216.8
1/8	204.596	3331.1 3343.9	3/8	230.514	4228.5	1/2 5/8 3/4 7/8	256.433	5232.8
32	204.989	3343.9 3356.7	52	230,907	4242.9	34	256.825	5248.9 5264.9
1/8 1/4 1/8 1/8 1/8 1/8 1/8	205.382 205.774 206.167	3369.6	3/8 1/2 5/8 3/4 7/8	230,514 230,907 231,300 231,692	4228.5 4242.9 4257.4 4271.8	82.	257.218 257.611 258.003	5281.0
5%	206.167	3382.4	7/8	232 085	4280.3	1/8	258.003	5297.1 5313.3
34	206.560	3395.3	74.	282.478 282.871 283.263	4300.81	1/4	258.396 258.789 259.181	5313.3
66.	206.952	3408.2 3421.2	1/8	282.871	4315.4 4329.9	9/8	258.789	5329.4 5345.6
	207 738	3434.2	1/4 3/8	233.656	4344.5	1/2 5/8	259.101	5361.8
1/4	208.131	3447.2 3460.2	1/2 5/8 3/4	234.019	4359.2	9/4	259.967	5378.1
3/8	208.523	3460.2	- 5%	234.441	4373.8	7/8	260.359	5394.3
52	208.916	3473.2 3486.3	78	284.884 285.227	4388.5	83.	260.752	5410.6
3/4	206.952 207.345 207.738 208.131 208.523 208.916 209.309 209.701	3499.4	75.	235.619	4403.1 4417.9	1/8 1/4	261.145 261.538	5426.9 5443.3
1/8 1/4 8/8 1/2 5/8 1/8	210.094	3512.5	1/8	236.012	4432.6	3/6	261.930	5459.6
67.	210.487	3525 7	-/4	236.405	4447.4 4462.2	1/9 5/8	262.323	5476.0
18	210.879	3538.8 3552.0	3/8	236.798	4462.2	%	262.716	5492.4
1/8 1/4 3/8	211.272 211.665	3565.2	1/2 5/8 3/4 7/8	236.798 237.190 237.583 237.976	4477.0 4491.8	3/4	263.108 263.501	5508.8 5525.3
1/2	212.058	3578.5	3%	237.976	4506.7	84.	263.894	5541.8
1/2 5/8 3/4 3/8	212.450	3591.7	7/8	200.000	4521.5	1/8 1/4 3/8	264.286	5558.3
34	212.843 213.236	3605.0 3618.3	76.	238.761 239.154	4536.5 4551.4	34	264.679	5574.8
68.	213.628	3631.7	1/8 1/4	239.546	4566.4	1/8	265.072 265.465	5591.4 5607.9
	214.021	3645.0	3/8 1/8	239.939	4581.3	1/3/ 5/8/ 3/4/	265.857	5624.5
1/8 1/4 3/8	214.414	3658.4	1/2 5/8 3/4	240.332	4596.3	34	266.250	5641.2
3/8	214.806 215.199	3671.8 3685.3	%	240,725 241,117	4611.4 4626.4	/8	266.643	5657.8
1/2 5/8 3/4 2/8	215.592	3698.7	% %	241.510	4641.5	85.	267.035 267.428	5674.5 5691.2
3/4	215.984	3712.2	77.	241.903	4656.6	1/8 1/4 8/8	267.821	5707.9
69.78	216.377	3725.7	1/8 1/4	242.295	4671.8	3/8	268.213	5724.7
	216.770	3739.3 3752.8	74 3/8	242.688 243.081	4686.9 4702.1	122	268.606 268.999	5741.5 5758.3
1/8 1/4	217.163 217.555 217.948 218.341	3766.4	1%	243.473	4717.3		269,392	5775.1
1/4 3/8 1/2 5/8	217.948	3780.0	1/2/8 5/8 3/4	243.866	4732.5	38	269.784	5791.9
1/2	218.341	3793.7	3/4	244.259	4747.8	180. 1	270.177	5808.8
3/8	218.73 <b>2</b> 219.126	3807.3 3821.0	78.	244.652	4763.1 4778.4	1/8 1/4 8/8	270.570	5825.7
3% 3%	219.519	3834.7	1/6	245.044 245.437	4793.7	3/4	270.962 271.355	5842.6 5859.6
70.	219.911	3848.5	1/4	245.830	4809.0	1%	271.748	5876.5
1/8	220.304	3862.2	1/4 8/8	246.222	4824.4	1/3 5/8 8/4	272.140	5893.5
34	220.697 221.090	3876.0 3889.8	52	246.615 247.008	4839 8 4855.2	34	272.533 272.926	5910.6
1/2	221.482	3903.6	3/4	247.400	4870.7	87.	273,319	5927.6 5944.7
5/8 3/4	221.875	3917.5	/8	247.400 247.793	4886.2	1/8 1/4	273.711	5961.8
3/4 7/8	222.268	3931.4	79.	248.186	4901.7	1/4	274.104	5978.9
71.78	222.660 223.053	3945.3 3959.2	1/8	248.579	4917.2	3/8	274.497	5996.0
1/6	223.446	3973.1	3%	248.971 249.364	4932.7 4948.3	1/2 5/8 3/4	274.889 275.282	6013.2 6030.4
1/8 1/4	223.838	3987.1	1%	249.757	4963.9	34	275.675	6047.6

Diam.	Circum.	Area.	Diam.	Circum,	Area.	Diam.	Circum.	Area.
87 7/8	276.067	6064.9	92.	289.027	6647.6	961/8	301.986	7257.1
88.	276.460	6082.1	1/8	289,419	6665.7	1/4	302.378	7276.0
1/8	276.853	6099.4	1/4	289.812	6683.8	3%	302.771	7294.9
1/8 1/4 1/8 1/8 1/8 1/8	277,246	6116.7	14 3/8 1/2/8 3/4 5/8	290,205	6701.9	% 12 5/8 34 78	303.164	7313.8
3/8	277.638	6134.1	1/2	290.597	6720.1	5%	303.556	7332.8
1/2	278.031	6151.4	5/8	290.990	6738.2	3/4	303.949	7351.8
5/8	278.424	6168.8	3/4	291.383	6756.4	7/8	304.342	7370.8
3/4	278.816	6186.2	7/8	291.775	6774.7	97.	304.734	7389.8
7/8	279.209	6203.7	93.	292.168	6792.9	1/8	305.127	7408.9
89.	279,602	6221.1	1/8	292.561	6811.2	1/8 1/4	305.520	7428.0
1/8 1/4	279.994	6238.6	1/8/44/8/1/3/8/4/8	292.954	6829.5	3/8	305.913	7447.1
1/4	280.387	6256.1	3/8	293.346	6847.8	1/2	306.305	7466.2
3/8	280.780	6273.7	1/2	293.739	6866.1	8/8/2/8/4/8 5/4/8/4/8	306.698	7485.3
1/2	281.173	6291.2	5/8	294.132	6884.5	3/4	307.091	7504.5
%	281.565	6.08.8	34	294.524	6902.9	₹⁄8	307.483	7523.7
3/8 1/2 5/8 3/4 7/8	281.958	6326.4	. 7/8	294.917	6921.3	98.	307.876	7543.0
7/8	282.351	6344.1	94.	295.310	6939.8	1/8 1/4	308.269	7562.2
90.	282.743	6361.7	101438138948	295.702	6958.2	1/4	308.661	7581.5
1/8	283.136	6379.4	1/4	296.095	6976.7	3/8 1/2 5/8 3/4 2/8	309.054	7600.8
24	283.529	6397.1	3/8	296.488	6995.3	1∕2	309.447	7620.1
%	283.921	6414.9	1/2	296.881	7013.8	%	309.840	7639.5
22	284.314	6432.6	%	297.273	7032.4	9/4	310.232	7658.9
%	284.707	6450.4	24	297.666	7051.0	3/8	310.625	7678.3
1/8/4/8/4/8/4/8/4/8/4/8/4/8/4/8/4/8/4/8/	285,100	6468.2	1/8	298.059	7069.6	99.	311.018	7697.7
. 1/8	285.492	6486.0	95.	298.451	7088.2	1/8	311.410	7717.1
91.	285.885	6503.9	<del>1</del> /8	298.844	7106.9	24	311.803	7736.6
1/8	286.278	6521.8	1/4	299.237	7125.6	%	312.196	7756.1
24	286.670	6539.7	3/8	299.629	7144.3	22	312.588	7775.6
28	287.063	6557.6	23	300.022	7163.0	%	312.981	7795.2
1/8/4/8/24/8	287.456	6575.5	1814881888148	300.415	7181.8	3/4 7/8	313.374	7814.8
28	287.848	6593.5	24	300.807	7200.6	100/8	313.767	7834.4
24	288.241	6611.5	00 18	301.200	7219.4	100.	314.159	7854.0
1/8	288.634	6629.6	96.	301.593	7238.2			

# DECIMALS OF A FOOT EQUIVALENT TO INCHES AND FRACTIONS OF AN INCH.

Inches.	0	1/8	1/4	3/8	1/2	5/8	3/4	7/8	
0	0	.01042	.02083	.03125	.04166	.05208	.06250	.07292	
2 3	.0833	.0937	.1042	.1146	.1250	.1354	.1459	.1563	
3 4 5	.2500 .3333 .4167	.2604 .3437 .4271	.2708 .3542 .4375	.2813 .3646 .4479	.2917 .3750 .4588	.3021 .3854 .4688	.3125 .3958 .4792	.3229 .4063 .4896	
6 7	.5000	.5104	.5208	.5313	.5417	.5521	.5625	.5729	
8 9 10	.7500	.6771 .7604	.6875 .7708	.6979 .7813	.7083 .7917	.7188 .8021	.7292 .8125	.7396 .8229	
10 11	.8333	.8437 .9271	.8542 .9375	.8646 .9479	.8750 .9583	.8854 .9688	.8958 .9792	.9063 .9896	

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# LENGTHS OF CIRCULAR ARCS. (Degrees being given. Radius of Circle = 1.)

In

Formula.—Length of arc =  $\frac{3.1415927}{180}$  × radius × number of degrees.

RULE.—Multiply the factor in table for any given number of degrees by the radius.

EXAMPLE.—Given a curve of a radius of 55 feet and an angle of 78° 20′.
What is the length of same in feet.

		I	Degrees.			М	inutes.
1	.0174533	61	1.0646508	121	2.1118484	1	.0002909
1 2 3 4 5 6 7 8	.0349066	62 63	1.0821041	122	2.1293017 2.1467550	2 3 4 5 6 7 8	.0005818
3	.0523599	63	1.0995574	123	2.1467550 2.1642083	3	.0008727
4	.0698132 .0872665	64 65	1.1170107 1.1344640	124 125	2.1816616	4 6	.0011636 .0014544
6	.1047198	66	1.1519173	125	2,1991149	6	.0014544
7	1221730	67	1 1693706	127	9 9165689	7	.0020362
8	.1221730 .1396263	68	1.1693706 1.1868239	128	2.2340214	8	.0023271
9	.1570796	69	1.2042772	129	2.2514747	9	.0026180
10	.1745329	70	1.2217305	130	2,2689280	10	.0029089
11 12 13	.1919862 .2094395	71	1.2391838	131 132	2,2863813 2,3038346	11 12	.0031998
12	,2268928	72 73 74 75	1.2566371	133	2.3212879	13	.0037815
14	.2443461	74	1.2740904 1.2915436	134	2.3387412	14	.0040724
14 15	.2617994	75	1.3089969	135	2.3561945	15	.0043633
16	.2792527	76	1.3264502	136	2.3736478	16	.0046542
17	.2967060	76 77 78 79	1.3439035	137	2.3911011	17	.0049451
18	.3141593	78	1.3613568	138	2.4085544	18	.0052360
19	.3316126 .3490659	79 80	1.3788101 1.3962634	139 140	2.4260077 2.4434610	19	,0055269 ,0058178
20 21	.3665191	81	1.4137167	141	2.4609142	20 21 22	.0061087
22	,3839724	82	1.4311700	142	2,4783675	22	.0063995
23	,4014257	83	1.4486233	143	2.4958208	23 24 25 26	.0066904
24	.4188790	84	1.4660766	144	2.5132741	24	.0069813
25	. 4363323	85	1.4835299	145	2.5307274	25	.0072722
26	.4537856 .4712389	86 87	1.5009832	146 147	2.5481807 2.5656340	26	.0075631 .0078540
22 23 24 25 26 27 28 29 30	,4886922	88	1.5184364 1.5358897	148	2.5830873	27 28	.0078540
29	.5061455	89	1.5533430	149	2.6005406	29	.0084358
30	,5235988	90	1.5707963	150	2.6179939	30	.0087266
31	.5410521	91	1.5882496	151	2.6354472	31	.0090175
32	.5585054	92	1.6057029	152	2.6529005 2.6703538	32	.0093084
33 34	.5759587	93 94	1.6231562	153	2.6703538	33 34	.0095993
35	.5934119 .6108652	95	1.6406095 1.6580628	154 155	2.6878070 2.7052603	35	.0098902
36	.6283185	96	1.6755161	156	2.7227136	26	.0104720
36 37 38	.6457718	97	1.6929694	157	2.7401669	37 38	.0107629
38	.6632251	98	1.7104227	158	2 7576202	38	.0110538
39	.6806784	99	1.7278760 1.7453293	159	2.7750735 2.7925268	39	
40	.6981317	100	1.7453293	160	2.7925268	40	.0116355
41 42	.7155850 .7330383	101 102	1.7627825 1.7802358	161 162	2.8099801 2.8274334	41 42	.0119264
43	.7504916	103	1.7976891	163	2.8448867	43	.0125082
44	.7679449	104	1.8151424	164	2.8623400	44	.0127991
45	.7853982	105	1.8325957	165	2.8623400 2.8797933	45	.0130900
46	.8028515	106	1.8500490	166	2.8972466 2.9146999	46	.0133809
47	.8203047	107	1.8675023	167	2.9146999	47	.0136717
48 49	.8377580 .8552113	108 109	1.8849556 1.9024089	168 169	2.9321531 2.9496064	48 49	.0139626 .0142535
50	.8726646	110	1.9198622	170	2.9670597	50	.0142555
51	. 8901179	111	1.9373155	171	2.9845130	51	.0148353
52	.9075712	112	1 9547688	172	3.0019663	52	.0151262
52 53 54	.9250245	113	1.9722221	173 174	3.0194196 3.0368729	53	.0154171 .0157080
54	.9424778	114	1.9896753	174	3.0368729	54	.0157080
55 56	.9599311	115 116	2.0071286 2.0245819	175 176	3.0543262 3.0717795	55 56	.0159989
57	.9773844 .9948377	117	2 0420352	176	3.0717795	56 57	.0162897
58	1 0122910	113	2.0594885	178	3.1066861	58	.0168715
59	1.0297443	119	2.0769418	179	3.1241394	59	.0171624 .0174533
60	1.0471976	120	2.0943951	180	3.1415927	60	.0174533

#### LENGTHS OF CIRCULAR ARCS.

#### (Diameter = 1. Given the Chord and Height of the Arc.)

RULE FOR USE OF THE TABLE .- Divide the height by the chord. Find in the

RULE FOR USE OF THE TABLE.—Divide the height by the chord. Find in the column of heights the number equal to this quotient. Take out the corresponding number from the column of lengths. Multiply this last number by the length of the given chord; the product will be length of the arc. If the arc is greater than a semicircle, first find the diameter from the formula, Diam.—(square of half chord + rise) + rise; the formula is true whether the arc exceeds a semicircle or not. Then find the circumference. From the diameter subtract the given height of arc, the remainder will be height of the smaller arc of the circle; find its length according to the rule, and subtract it from the circumference.

Hgts.	Lgths.	Hgts.	Lgths.	Hgts.	Lgths.	Hgts.	Lgths.	Hgts.	Lgths.
.001	1.00002	.15	1.05896 1.06051	.238	1.14480 1.14714	.326	1.26288 1.26588	.414	1.40788 1.41145
.005	1.00007 1.00027	.154	1.06209	.242	1.14951	.33	1.26892	.418	1.41143
.01 .015	1.00021	.156	1.06368	.244	1.15189	.332	1.27196	.42	1.41861
.015	1.00107	.158	1.06530	.246	1.15428	,334	1.27502	.422	1.42221
.02	1.00167	.16	1.06693	.248	1.15670	.336	1.27502 1.27810	.424	1.42583
.03	1.00240	.162	1.06858	.25	1.15912	.338	1.28118	.426	1.42945
.03 .035	1.00327	.164	1.07025	.252	1.16156	.34	1.28428	.428	1.43309
.04 .045	1.00426	.166	1.07194 1.07365	.254	1.16402	.342	1.28739	.43	1.43673
.045	1.00539	.168	1.07365	.256	1.16650	.344	1.29052	. 432	1.44039
.05 .055	1.00665	.17	1.07537	.258	1.16899	.346	1.29366	.434	1.44405
.055	1.00805	.172	1.07711	.26	1.17150	.348	1.29681	.436	1.44773
.06	1.00957	.174	1.07888	.262	1.17403 1.17657	.35	1.29997	. 438	1.45142
.065	1.01123	.176	1.08066	.264	1.17912	.352	1.30315	.44	1.45512
.07	1.01302	.178	1.08246	.266	1.18169	.356	1.30634 1.30954	.442	1.45883
610.	1.01493	.18	1.00420	.268 .27	1.18429	.358	1 21276	.446	1.46628
.08	1.01916	.184	1.08611 1.08797	.272	1.18689	.36	1.31276 1.31599	.448	1.47002
.000	1.02146	.186	1.08984	.274	1.18951	.362	1.31923	.45	1.47377
.09	1.02389	.188	1.09174	976	1.19214	.364	1.32249	.452	1.47753
10	1.02646	.19	1.09365	.278	1.19479	,366	1.32577	.454	1.48131
.10 .102	1.02752	.19	1.09557	.278 .28 .282 .284 .286 .286	1.19746	.368	1.32905	.456	1.48509
.104	1.02860	.194	1.09752	.282	1.20014	.37	1.33234	.458	1.48889
.106	1.02970	.196	1.09949	.284	1.20284	.372	1.33564	.46	1.49269
.108	1.03082	.198	1.10147 1.10347	.286	1.20555	.374	1.33896 1.34229	.462	1.49651
.11	1.03196	.20	1.10347	.288	1.20827	.376	1.34229	.464	1.50033
.112	1.03312	.202	1.10548 1.10752	1 .29	1.21102 1.21377	.378	1.34563	.466	1.50416
.114	1.03430	.204	1.10752	.292 .294	1.21377	.38	1.34899	.468	1.50800
.116	1.03551	.206	1.10908	.294	1.21654 1.21933	.382	1.35237 1.35575	.47	1.51185 1.51571
.118	1.03572	.208	1.11100	.298	1.22213	.386	1.35914	.472 .474	1.51958
100	1.03923	212	1 11584	.30	1.22495	.388	1.36254	.476	1.52346
194	1.04051	.214	1 11706	.302	1.22778	.39	1.36596	.478	1.52736
.104 .106 .108 .11 .112 .114 .116 .118 .12 .122 .124 .126 .128 .13	1.04181	.216	1.10752 1.10958 1.11165 1.11374 1.11584 1.11796 1.12011 1.12225 1.12464	.304	1.23063	.392	1,36939	.48	1.53126
128	1.04313	.218	1.12225	.306	1.23349	.394	1.37283	.482	1.53518
.13	1.04447	.22	1.12444	.308	1,23636	.396	1.37628	.484	1.53910
.132	1.04584	.222	1.12664	.31	1.23926	.398	1.37974	.486	1.54302
.134	1.04722	.224	1.12885	.31	1.24216	.40	1 1 38322	.488	1.54696
.136	1.04862	.226	1.13108	.314	1.24507	.402	1.38671 1.39021	. 49	1.55091
.132 .134 .136 .138	1.05003	.228	1.12444 1.12664 1.12885 1.13108 1.13381 1.13557 1.13785	.316	1.24801	.404	1.39021	.492	1.55487
.14 .142	1.05147	.23	1.13557	.318	1.25095	.406	1.39372	.494	1.55854
.142	1.05293	.232	1.13785	.32	1.25391	.408	1.39724	.496	1.56282
.144	1.05441	.234	1.14010	. 322	1.25689	.41	1.40077	.498	1.56681
.146	1.05591	. 236	1.14247	.324	1.25988	.412	1.40432	.5	1.57080
.148	1.05743	1				1	1		1

#### AREAS OF THE SEGMENTS OF A CIRCLE.

# (Diameter = 1; Rise or Versed Sine in parts of Diameter being given.)

RULE FOR USE OF THE TABLE,—Divide the rise or height of the segment by the diameter to obtain the versed sine. Multiply the area in the table corresponding to this versed sine by the square of the diameter. If the segment exceeds a semicircle its area is area of circle—area of segment whose rise is (diam. of circle—rise of given segment). Given chord and rise, to find diameter. Diam. = (square of half chord + rise) + rise. The half chord is a mean proportional between the two parts into which the chord divides the diameter which is nepreclaimer to:

into w	nto which the chord divides the diameter which is perpendicular to it.											
Versed Sine.	Area.	Versed Sine.	Area.	Versed Sine.	Area,	Versed Sine.	Area.	Versed Sine.	Area,			
.001	.00004	.054	.01646	.107	.04514	.16	.08111	.213	.12235			
.002	.00012	.055	.01691	.108	.04576	.161	.08185	.214	.12317			
.003	.00022	.056	.01737	.109	.04638	.162	.08258	.215	.12399			
.004	.00034	.057	.01783	.11	.04701	.163	.08332	.216	.12481			
.005	.00047	.058	.01830	.111	.04763	.164	.08406	.217	.12563			
.006	.00062	.059	.01877	.112	.04826	.165	.08480	.218	.12646			
.007	.00078	.06	.01924	.113	.04889	.166	.08554	.219	.12729			
.008	.00095	.061	.01972	.114	.04953	.167	.08629	.22	.12811			
.009	.00113	.062	.02020	.115	.05016	.168	.08704	.221	.12894			
.01	.00133	.063	.02068	.116	.05080	.169	.08779	.222	.12977			
.011	.00153	.064	.02117	.117	.05145	.17	.08854	.223	.13060			
.012	.00175	.065	.02166	.118	.05209 .05274	.171	.08929	.224	.13144			
		.067	.02265	.12	.05338			.226				
.014	.0022	.068	.02315	121	.05404	.173	.09080	.227	.13311			
.016	.00244	.069	.02366	.122	.05469	.175	.09231	.228	.13478			
.017	.00294	.07	.02417	.123	.05535	.176	.09307	.229	.13562			
.018	.0032	.071	.02468	.124	.05600	.177	.09384	.23	.13646			
.019	.00347	.072	.02520	.125	.05666	.178	.09460	.231	.13731			
.02	.00375	.073	.02571	.126	.05733	.179	.09537	.232	.13815			
.021	.00403	.074	.02624	,127	.05799	.18	.09613	.233	.13900			
.022	.00432	.075	.02676	.128	.05866	.181	.09690	,234	.13984			
.023	.00462	.076	.02729	.129	.05933	.182	.09767	.235	.14069			
.024	.00492	.077	.02782	.13	.06000	.183	.09845	.236	.14154			
.025	.00523	.078	.02836	.131	.06067	.184	.09922	.237	. 14239			
.026	.00555	.079	.02889	.132	.06135	.185	.10000	.238	.14324			
.027	.00587	.08	.02943	.138	.06203	. 186	.10077	.239	.14409			
.028	.00619	.081	.02998	.134	.06271	.187	. 10155	.24	.14494			
.029	.00653	.082	.03053	.135	.06339	.188	.10233	.241	.14580			
.03	.00687	.083	.03108	.136	.06407	.189	.10312	.242	.14666			
.031	.00721	.084	.03163	.137	.06476	.19	.10390	.243	.14751			
.032	.00756	.085	.03219	.138	.06545	.191	.10469	.244	.14837			
.033	.00791	.086	.03275	.139	.06614	.192	.10547	.245	.14923			
.034	.00827	.087	.03331	.14	.06683	.193	.10626	.246	.15009			
.035 .036	.00864	.088	.03387	.141	.06753	.194	.10705	.247	.15095			
.037	.00901	.009	.03501	.143	.06892	.196	.10784	.248	.15182			
.038	.00956	.091	.03559	.144	.06963	.197	.10943	.25	.15355			
.039	.01015	.092	.03616	.145	.07033	.198	.11023	.251	.15441			
.04	.01054	.093	.03674	.146	.07103	.199	.11102	.252	.15528			
.041	.01093	.094	.03732	.147	.07174	2	.11182	.253	.15615			
.042	.01133	.095	.03791	.148	.07245	.201	.11262	.254	.15702			
.043	.01173	.096	.03850	.149	.07316	.202	.11343	.255	.15789			
.044	.01214	.097	.03909	.15	.07387	.203	.11423	.256	.15876			
.045	.01255	.098	.03968	.151	.07459	.204	.11504	.257	.15964			
.046	.01297	.099	.04028	.152	.07531	.205	.11584	.258	.16051			
.047	.01339	.1	.04087	.158	.07603	.206	.11665	.259	.16139			
.048	.01382	.101	.04148	.154	.07675	.207	.11746	.26	.16226			
.049	.01425	.102	.04208	.155	.07747	.208	.11827	.261	.16314			
.05	.01468	.103	.04269	.156	.07819	.209	.11908	.262	.16402			
.051	.01512	.104	.04330	.157	.07892	.21	.11990	.263	.16490			
.052	.01556	.105	.04391	.158	.07965	.211	.12071	.264	.16578			
.053	.01601	.106	.04452	.159	.08038	.212	.12153	.265	.16666			

Versed	Area.	Versed	Area.	Versed	Area.	Versed	Area.	Versed	Area.
Sine.	Area	Sine.	211044	Sine.	Zircii	Sine.	Zireii,	Sine.	221 CM
	.16755	,313	.21015	.36	.25455	.407	.30024	.454	.34676
.266	.16843	.314	.21108	.361	.25551	.408	.30122	.455	.34776
.268	.16932	.315	.21201	.362	.25647	.409	.30220	.456	.34876
.269	.17020	.316	.21294	.363	.25743	.41	.30319	457	.34975
.27	.17109	.317	.21387	.364	.25839	.411	.30417	.458	.35075
.271	.17198	.318	.21480	.365	.25936	412	.30516	,459	.35175
.272	.17287	,319	.21573	.366	,26032	.413	.30614	.46	.35274
.278	.17376	.32	.21667	.367	.26128	.414	.30712	.461	.25374
.274	.17465	.321	.21760	.368	.26225	.415	.30811	.462	.35474
.275	.17554	.322	.21853	.369	.26321	.416	.30910	.463	.35573
.276	.17644	.323	.21947	.37	.26418	,417	.31008	.464	.35673
.277	.17733	.324	.22040	.371	.26514	.418	.31107	.465	.35773
.278	.17823	325	.22134	.372	.26611	.419	.31205	.466	.35873
.279	.17912	.326	.22228	. 73	.26708	.42	.31304	.467	.35972
.28	.18002	.327	.22322	.374	.26805	.421	.31403	.468	.36072
.281	.18092	.328	.22415	.375	.26901	.422	.31502	.469	.36172
.282	.18182	.329	.22509	.376	.26998	.423	.31600	.47	.36272
.283	.18272	.83	.22603	,377	.27095	,424	.31699	.471	.36372
.284	.18362	.331	.22697	.378	.27192	.425	.31798	.472	.36471
.285	.18452	.332	.22792	.379	.27289	.426	.31897	.473	.36571
.286	.18542	.333	.22886	.38	.27386	.427	.31996	.474	.36671
.287	.18633	.334	.22980	.381	.27483	.428	.32095	.475	.36771
.288	.18723	.385	.23074	.382	.27580	.429	.32194	.476	.36871
.289	.18814	.336	.23169	.383	.27678	.43	.32293	.477	.36971
.29	.18905	.337	.23263	.384	.27775	.431	.32392	.478	.37071
.291	.18996	.338	23358	.385	.27872	.432	.32491	.479	.37171
.292	.19086	.339	.23453	.386	.27969	.433	.32590	.48	.37270
.293	.19177	.34	.28547	.387	.28067	.434	.32689	.481	.37370
.294	.19268	.341	.23642	.388	.28164	.435	.32788	.482	.37470
.295	.19360	.342	.23737	.389	.28262	.436	.32887	.483	.37570
.296	.19451	.843	.23832	.39	.28359	.437	.32987	.484	.37670
.297	.19542	.344	.23927	.391	.28457	.438	.33086	.485	.37770
.298	.19634	.345	.24022	.392	.28554	.439	.33185	.486	.37870
.299	.19725	.346	.24117 .24212	.393	.28652 .28750	.44	.33284	.488	.37970
.301	.19908	.348	.24307	.395	.28848	.442	33483	.489	.38170
.302	.20000	.349	.24403	.396	.28945	.443	.33582	.409	.38270
.303	.20092	.35	.24498	.397	.29043	.444	.33682	.491	.38370
.304	.20184	.351	.24593	.398	.29141	.445	.33781	.492	.38470
.305	.20276	352	.24689	.399	.29239	.446	.33880	.493	.38570
.306	.20368	.353	,24784	.4	.29337	.447	.33980	.494	.38670
.307	.20460	.354	.24880	.401	.29435	.448	.34079	.495	.38770
.308	.20553	.355	,24976	.402	.29533	,449	.34179	.496	.38870
.309	.20645	.356	.25071	403	.29631	.45	.34278	497	.38970
.31	.20738	.357	.25167	.404	.29729	.451	.34378	.498	.39070
.311	.20830	.358	.25263	.405	.29827	.452	.34477	.499	.39170
.312	.20923	.359	.25359	.406	.29926	.453	.34577	.5	.39270
			-			-			

For rules for finding the area of a segment see Mensuration, page 59.

SPHERES.

(Some errors of 1 in the last figure only. From TRAUTWINE.)

Diam. Sur- Solid- dity. Diam. Sur- face. Sur- face.	Solid- ity.
1-32 .00307 .00002 3 14 33.183 17.974 9 78 306.36	504.21
1-16 .01227 .00013 5-16 34.472 19.031 10314.16	523.60
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	543.48
1/6     .04909     .00102     7-16     37.122     21.268     1/2     330.06       5-32     .07670     .00200     1/2     38.484     22.449     3/8     338.16	563.86 584.74
5-32 .07670 .00200 ½ 38.484 22.449 38 338.16 3 3-16 .11045 .00345 9-16 39.872 23.674 ½ 346.36	606.13
7-32 .15033 .00548	628.04
1/4     .19635     .00818     11-16     42.719     26.254     34     363.05       9-32     .24851     .01165     34     44.179     27.611     76     371.54	650.46
9-82 .24851 .01165 34 44.179 27.611 78 371.54 5-16 .30680 .01598 13-16 45.664 29.016 11. 380.13	673.42
11-32 .37123 .02127 76 47.173 30.466 16 388.83	696.91 720.95
	745.51
13-32   .51848   .03511   4.   50.265   33.510   36   406.49	770.64
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	796.33
15-32	822.58 849.40
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	876.79
56   1,2272   ,12783   56   67,201   51,801   12,   452,39	904.78
11-16 1.4849 .17014 34 70.883 56.116 14 471.44	962.52
11-18 1.4849 1.17014 54 70.883 56.116 14 471.44 34 1.7671 2.2089 78 74.663 60.668 15 490.87 1 13-16 2.0739 2.28081 5. 78.540 65.450 34 510.71 1	022.7 085.3
76 2.4053 .35077	150.3
76     2.4053     .35077     16     82,516     70.482     13.     530.93     1       15-16     2.7611     .43143     14     86.591     75.767     14     551.55     1	218.0
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	288.3
1-16 3.5466 .62804 1/2 95.033 87.113 3/4 593.95 1 1/4 3.9761 .74551 5/6 99.401 93.189 14. 615.75 1	361.2
14   3.9761   .74551   58   99.401   93.189   14.   615.75   1   3-16   4.4301   .87681   34   103.87   99.541   14   637.95   1	436.8 515.1
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	596.3
5-16   5.4119   1.1839   6.   113.10   113.10   34   683.49   1	680.3
36 5.9396 1.3611 36 117.87 120.31 15. 706.85 1 7-16 6.4919 1.5558 4 122.72 127.83 4 730.63 1	767.2
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	857.0 949.8
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	045.7
% 8.2957   2.2468   % 137.89   152.25   16.   804.25   2	144.7
11-16 8.9461 2.5161 34 143.14 161.03 14 829.57 2 34 9.6211 2.8062 78 148.49 170.14 14 855.29 2 13-16 10.321 3.1177 7. 153.94 179.59 34 881.43 2	246.8
34     9.6211     2.8062     78     148.49     170.14     14     32     855.29     2       13-16     10.321     3.1177     7.     153.94     179.59     34     881.42     2	352.1 460.6
76 11.044 3.4514 16 159.49 189.39 17. 4 861.42 2	572.4
76   11.044   3.4514   16   159.49   189.39   17.   907.98   2   15-16   11.793   3.8083   14   165.13   199.53   14   934.83   2   12.566   4.1888   36   170.87   210.03   16   962.12   2	2687.6
15-16 11.799   3.8083   14 165.13   199.53   14 934.83   2	806.2
1-16   13.364   4.5939   13   176.71   220.89   34   989.80   2   16.71   18.   18.   19.	928.2 3053.6
74 11.044 3.4514 14 159.49 189.39 17. 907.93 2 15-16 11.793 3.8083 14 165.13 195.33 14 934.83 2 2. 12.566 4.1888 36 170.87 210.03 14 98.88 2 1-16 13.364 4.5939 1.4 176.71 220.89 34 98.89 2 3-16 15.033 5.4809 34 188.69 243.73 18. 1017.9 3 3-16 15.033 5.4809 34 188.69 243.73 14 1046.4 3 14 15.904 5.9641 76 194.83 257.2 34 1054.6 3	8182.6
3-16 15 033 5 4809 34 188.69 248.73 14 1046.4 8 14 15 904 5 9641 76 194.83 255.72 14 1075.2 3 5-16 16 800 6 4751 8. 201.06 298.08 34 1104.5 3	315.3
5-16   16 800   6 4751   8	3451.5
36 17.721   7.0144   46   207.39   280.85   19.   1134.1   3	3591.4 3735.0
16 19.635 8.1813 36 220.36 307.58 16 1194.6 3	3882.5
7-16 18.666 7.5829 14 213.82 291.01 14 1164.2 8 14 19.635 8.1813 34 220.35 307.58 14 1164.6 3 9-16 20.629 8.8103 24 226.38 321.56 34 1225.4 4	1033.7
98 21.648   9.4708   98 233.71   335.95   20.   1256.7   4	1188.8
9-16 20, 629 8, 8103 46, 226, 98 821, 56 34 1225, 4 4 9 12 12 12 12 12 12 12 12 12 12 12 12 12	1347.8
13-16' 24 850   11 649   9   (254 47   381 70   34   1352 7   4	1510.9 1677.9
76 25.967 12.443 16 261.59 397.83 21. 1385.5 4	849.1
74 25.067 12.448 14.261.59 397.83 21. 4 1385.5 1 15-16 27.109 13.272 14.268.81 414.41 14.1 14.148.6 3. 28.274 14.137 36.270.12 431.44 26 1452.2 5	024.3
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	5203.7 5387.4
1-10 29.405 15.059	5575.3
	5767.6

### SPHERES-(Continued.)

To the same of the	Sur-	Solid-	D'	Sur-	Solid-	D'	Sur-	Solid-
Diam.	face.	ity.	Diam.	face.	ity.	Diam.	face.	ity.
22 1/2	1590.4	5964.1	40 1/2	5153.1	34783	70 1/2	15615	183471
3/4	1626.0	6165.2	41.	5281.1 5410.7	36087	71.	15837	187402
23.	1661.9 1698.2	6370.6 6580.6	42.	5410.7 5541.9	37423 38792	72. 1/2	16061 16286	191389 195433
14	1735 0	6795.2	1/6	5674.5	40194	1/6	16513	199532
34	1772.1 1809.6	7014.3 7238.2	43.	5808.8 5944.7	41630	73.	16742 16972	203689
24.	1809.6 1847.5	7238.2 7466.7	44. 1/2	5944.7 6082.1	43099 44602	74. 1/2	16972 17204	207903 212175
1/4	1885.8	7700.1	1/2	6221.2	46141	14.	17437	216505
1/4 1/2 3/4	1924.4	7938.3 8181.3	45.	6361.7 6503.9	47713	75.	17672 17908	220894
25.	1963.5 2002.9	8181.3 8429.2	46. 1/2	6503.9 6647.6	49821 50965	76. 1/2	17908 18146	225341 229848
14 14 14 94	2042.8	8682.0	1/2	6792.9	52645	10.	18386	234414
34	2083 0	8939.9	47.	6939 9	54362	77.	18626	239041
26.	2123.7 2164.7	9202.8 9470.8	48.	7088.3 7238.3	56115 57906	78. 1/2	18869 19114	243728 248475
1/6	2206.2	9744.0	16.	7389.9	59734	15.	19360	253284
1/4 1/2 3/4	2248.0	10022	49.	7543.1 7697.7	61601	79.	19607	258155
26.	2290.2 2332.8	10306	72	7697.7	63506	1/2	19856	263088
14 14 14 34	2332.8	10595 10889	50.	7854.0 8011.8	65450 67433	80.	20106 20358	268083 273141
3%	2419 2	11189	51.	8171.2	69456	81.	20612	278263
28.	2463.0 2507.2	11494	1/2	8332.3	71519	1/2	20867	283447
14 12 34	2507.2	11805 12121	52. 1/2	8494.8 8658.9	73622 75767	82.	21124 21382	288696 294010
3/4	2596 7	12443	53.	8894 8	77952	83. 72	21642	299388
29.	2642.1 2687.8	12770	1/9	8992.0	80178	1/2	21904	304831
14	2687.8 2734.0	13103 13442	54.	9160.8	82448 84760	84.	22167 22432	310340 315915
14 12 34	2780.5	13787	55. 1/2	9331.2 9503.2	87114	85. 1/2	22698	321556
30.	2827.4 2874.8	14137	1/6	9676.8 9852.0	89511	1/6	22966	327264
1/4 1/2 3/4	2874.8	14494	56.	9852.0 10029	91953	86.	23235	333039
3/4	2922.5 2970.6	14856 15224	57. 1/2	10207	94438 96967	87. 1/2	23506 23779	338882 344792
31.	3019.1	15599	1/6	10387	99541	1/6	24053	350771
1/4 1/3 3/4	3068.0	15979	58.	10568	102161	88.	24328	356819
37	3117.3 3166.9	16366 16758	59.	10751 10936	104826 107536	89. 1/2	24606 24885	362935 369122
32.	3217.0 3267.4 3318.3	17157	1/6	11122 11310	110294	1/6	25165	375378
1/4 1/2 3/4	3267.4	17563	60.	11310	113098	90.	25447	381704
7/2 3/	3318.3	17974 18392	61.	11499 11690	115949 118847	91. 1/2	25730 26016	388102 394570
33.	3421.2	18817	1/2	11882	121794	1/6	26302	401109
14 173 374	3473.3	19248	62.	12076 12272	124789	92.	26590	407721
32	3525.7 3578.5	19685 20129	63. 1/2	12272 12469	127832 130925	93. 1/2	26880 27172	414405 421161
54.	3631.7	20580	1/9	12668	134067	1/6	27464	427991
14 1/2	3685.3	21037	64.	12868 13070	137259	94.	27759 28055	434894
35.	3739.3 3848.5	21501 22449	65, 1/2	13070	140501 143794	95. 1/2	28055 28353	441871 448920
35.	3959.2	23425	1/2	13273 13478	147138	95.	28652	448920
36.	4071.5 4185.5	24429	66.	13685	150533	96.	28953	463248
37. 1/2	4185.5	25461 26522	67. 1/2	13893	153980 157480	97. 1/2	29255 29559	470524 477874
31.	4417.9	27612	1/2	14103 14314	161032	1/3	29865	485302
38.	4536.5	28731	68.	14527 14741 14957	164637	98.	30172	499808
39. 1/2	4656.7 4778.4	29880	69. 1/2	14741	168295	99. 1/2	30481 30791	500388
39.	4901.7	31059 32270	1/2	15175	172007 175774	99.	31103	508047 515785
40.	5026.5	33510	70.	15394	179595	100.	31416	523598
	1	1						

## CONTENTS IN CUBIC FEET AND U. S. GALLONS OF PIPES AND CYLINDERS OF VARIOUS DIAMETERS AND ONE FOOT IN LENGTH.

1 gallon = 231 cubic inches. 1 cubic foot = 7,4805 gallons.

	0	•						
ü	For 1 F Leng		ui.	For 1 F Leng		ui.	For 1 F Leng	
Diameter in Inches.	Cubic Ft. also Area in Sq. Ft.	U. S. Gals., 281 Cu. In.	Diameter in Inches.	Cubic Ft, also Area in Sq. Ft.	U. S. Gals., 231 Cu. In.	Diameter in Inches.	Cubic Ft. also Area in Sq. Ft.	U. S. Gals., 231 Cu. In.
5-16 3/8 7-16 1/2	.0003 .0005 .0008 .001 ,0014	.0025 .004 .0057 .0078 .0102	634 7 714 714 734	.2485 .2673 .2867 .3068 .3276	1.859 1.999 2.145 2.295 2.45	19 191/2 20 201/2 21	1.969 2.074 2.182 2.292 2.405	14.73 15.51 16.32 17.15 17.99
9-16 5/8 11-16 3/4 13-16	.0017 .0021 .0026 .0031 .0036	.0129 .0159 .0193 .0230 .0269	8 814 815 834 9	.3491 .3712 .3941 .4176 .4418	2.611 2.777 2.948 3.125 3.305	21½ 22 22½ 22½ 23 23½	2,521 2,640 2,761 2,885 3,012	18.86 19.75 20.66 21.58 22.53
78	.0042	.0312	914	.4667	3.491	24	3.142	23.50
15-16	.0048	.0359	912	.4922	3.682	25	3.409	25.50
1	.0055	.0408	934	.5185	3.879	26	3.687	27.58
114	.0085	.0638	10	.5454	4.08	27	3.976	29.74
11/2	.0123	.0918	1014	.5730	4.286	28	4.276	31.99
13/4	.0167	.1249	101/6	.6013	4.498	29	4.587	34.31
2	.0218	.1632	103/4	.6303	4.715	30	4.909	36.72
21/4	.0276	.2066	11	.66	4.937	31	5.241	39.21
21/2	.0341	.2550	111/4	.6903	5.164	32	5.585	41.78
23/4	.0412	.3085	111/6	.7213	5.396	33	5.940	44,43
3	.0491	.3672	113/4	.7530	5.633	34	6.305	47.16
31/4	.0576	.4309	12	.7854	5.875	35	6.681	49.98
51/2	.0668	.4998	121/2	.8522	6.375	36	7.069	52.88
33/4	.0767	.5738	13	.9218	6.895	37	7.467	55.86
4	.0878	.6528	131/2	.994	7,436	38	7.876	58.92
41/4	.0985	.7369	14	1.069	7.997	39	8.296	62.06
41/6	.1134	.8263	14½	1 147	8.578	40	8.727	65.28
43/4	.1231	.9206	15	1.227	9.180	41	9.168	68.58
5	.1364	1.020	15½	1.310	9.801	42	9.621	71.97
51/4	.1503	1.125	16	1.396	10.44	43	10.085	75.44
51/2	.1650	1.234	16½	1.485	11.11	44	10.559	78.99
53/4	.1803	1.349	17	1.576	11.79	45	11.045	82.62
6	.1963	1.469	17½	1.670	12.49	46	11.541	86.33
61/4	.2131	1.594	18	1.768	13.22	47	12.048	90.13
61/2	.2304	1.724	18½	1.867	13.96	48	12.566	94.00

To find the capacity of pipes greater than the largest given in the table, look in the table for a pipe of one half the given size, and multiply its capacity by 4; or one of one third its size, and multiply its capacity by 9, etc.

To find the weight of water in any of the given sizes multiply the capacity in cubic feet by 624 or the gallons by 834, or, if a closer approximation is required, by the weight of a cubic foot of water at the actual temperature in the pipe.

#### CYLINDRICAL VESSELS, TANKS, CISTERNS, ETC. Diameter in Fect and Inches, Area in Square Fect, and U. S. Gallons Capacity for One Foot in Depth.

1 gallon = 231 cubic inches =  $\frac{1 \text{ cubic foot}}{2 \text{ ASOL}}$  = 0.13368 cubic feet.

7.4805 = 0.15506 cubic feet.											
Diam.	Area.	Gals.	Diam.	Area.	Gals.	Diam.	Area.	Gals.			
Ft. In.	Sq. ft.	1 foot	Ft. In.	Sq. ft.	1 foot	Ft, In,	Sq. ft.	1 foot			
	.785	depth.		25,22	depth. 188.66	19	_	depth. 2120.9			
1 1 1 1 2 1 3 1 4 1 5 1 6 1 7	.922	5.87 6.89	5 8 9 10 5 11 6 3 6 6 6 9 7 7 7 8 8 8 8 6 9 9 9 9 9 9 9 9 9 9	25.22	194.25	19 3	283,53 291.04	2177.1			
1 2	1.069	8.00	5 10	26.73	199.92	19 6	298.65	2234.0			
1 1 1 2 1 3 1 4 1 5 1 6 1 7 1 8	1,227	9.18	5 11	27.49	205.67	19 9	306.35	2291.7			
1 4	1.396	10.44	6	28.27	211.51	20	314.16	2350.1			
1 5	1.576 1.767	11.79 13.22	6 3 6	30.68	229.50 248,23	20 3 20 6	322.06 330.06	2409.2			
1 7	1.969	14.73	6 9	33,18 35,78	267.69	20 6	338.16	2469.1 2529.6			
i 8	2.182	16.32	7	38.48	287.88		346.36	2591.0			
1 9	2.405	17.99	7 3	41.28	308.81	21 21 3	354.66	2653.0			
1 10	2.640	19.75	7 6 7 9	44.18	330.49	21 6	363.05	2715.8			
1 11	2.885	21.58	7 9	47.17 50.27	352.88 376.01	21 9 22	371.54	2779.3			
2 1	3.142 3.409	23.50 25,50	8 9	53,46	399.88	22 3	380.13 388.82	2843,6 2908,6			
2 2	3,687	27.58	8 3 8 6	56.75	424.48	22 3 22 6 22 9	397.61	2974.3			
2 2 2 3 2 4	3.976	29.74	8 9	60.13	449.82	22 6 22 9	406.49	3040.8			
2 4	4.276	31.99	9	63.62	475.89	1 23	415.48	3108.0			
2 5 2 6 2 7 2 8	4.587	34.31	9 3 9 6	67.20 70.88	502.70	23 3 23 6	424.56	3175.9			
2 6	4.909	36.72 39,21	9 6	70.88	530 24 558,51	28 6 23 9	433.74	3244.6			
9 8	5.241 5.585	41.78	10	78.54	587.52	24	443.01 452.39	3314.0 3384.1			
2 9	5,940	44.43	10 3	82.52	617.26	24 3	461.86	3455.0			
2 9 2 10	6.305	47.16	10 6	86.59	647.74	24 6	471.44	3526.6			
2 11	6.681	49.98	10 9	90.76	678.95	24 9	481.11	3598.9			
3 1	7.069	52.88	11	95.03	710.90	25	490.87	3672.0			
1 10 1 11 2 1 2 2 2 3 2 2 4 5 2 2 6 7 8 2 8 9 2 10 3 1 1 3 2 3 3 4 4 3 3 5 6 6 7 3 7 8 9 8 3 10 3 3 11 4	7.467 7.876	55.86 58.92	11 3 11 6	99.40	743.58 776.99	25 25 3 25 6	500.74 510.71	3745.8 3820.3			
3 3	8.296	62.06	11 9	108.43	811.14	25 9	520.77	3895.6			
3 4	8.727	65.28 68.58	12	113.10 117.86	846.03	26 26 3	530.93	3971.6			
3 5	9.168	68.58	12 3	117.86	881.65	26 3 26 6	541.19	4048.4			
3 6	9.621	71.97 75,44	12 6 12 9 13	122.72 127.68	918.00 955.09	26 6 26 9	551.55 562,00	4125,9 4204.1			
3 8	10.065	78,99	12 9	132.73	992.91	27 9	572.56	4283.0			
3 9	11.045	82.62	13 3	137.89	1031.5	27 3	583.21	4362.7			
3 10	11.541	86.33	13 6	143.14	1070.8	27 3 27 6 27 9	593.96	4443.1			
3 11	12.048	90.13	13 9	148.49	1110.8	27 9	604.81	4524.3			
4 1	12,566 13.095	94.00 97.96	14 14 3	153.94 159.48	1151.5 1193.0	28	615.75 626.80	4606,2 4688.8			
4 1 4 2 4 3	13.635	102.00	14 6	165.13	1235.3	28 3 28 6	637.94	4772.1			
4 1 4 2 4 8 4 4 4 5 4 6 4 7 4 8	14.186	106.12	14 9	170.87	1278.2	28 9	649.18	4856.2			
4 4 4 5 4 6	14.748	110.32	15	176.71	1321.9	29	660.52	4941.0			
4 5	15.321	114.61	15 3	182 65	1366.4	29 3 29 6	671.96	5026.6			
4 6	15,90 16.50	118.97 123.42	15 6 15 9	188.69 194.83	1411.5 1457.4	29 6 29 9	683.49 695.13	5112.9 5199.9			
4 8	17.10	127.95	16	201.06	1504.1	30	706.86	5287.7			
4 9	17.72	132.56	16 3	207.39	1551.4	30 3	718.69	5376.2			
4 10	17.72 18.35	132.56 137.25	16 6	213 82	1599.5	30 6	730.62	5465.4			
4 11	18.99	142.02	16 9	220.35	1648.4	30 9	742.64	5555.4			
5 1	19.63 20.29	146.88 151.82	17 17 3	226.98 233.71	1697.9	31 31 3	754.77	5646.1			
5 2	20.29	156.83	17 6	240.53	1748.2 1799.3	31 3 31 6 31 9	766.99 779.31	5737.5 5829.7			
5 3	21.65	161 93	17 9	247.45	1851.1	31 9	791.73	5922,6			
5 4	22.34	167.12	18	254.47	1903.6	32	791.73 804.25	6016.2			
5 1 2 5 5 5 5 5 5 5 7	23.04	172.38	18 3	261.59	1956.8	32 3	816.86	6110.6			
5 6 7	23.76	177.72	18 6	268.80	2010.8	32 6 32 9	829.58	6205.7			
9 7	24.48	183.15	18 9	276.12	2065.5	32 9	842.39	6301.5			

#### GALLONS AND CUBIC FEET.

### United States Gallons in a given Number of Cubic Feet.

1 cubic foot = 7.480519 U. S. gallons; 1 gallon = 231 cu. in. = .13368056 cu. ft.

Cubic Ft.	Gallons.	Cubic Ft.	Gallons.	Cubic Ft.	Gallons.
0.1	0.75	50	374.0	8,000	59,844.2
0 2	1.50	60	448.8	9,000	67,324.7
0.3	2.24	70	523.6	10,000	74,805.2
0.4	2,99	80	598.4	20,000	149,610.4
0.5	3.74	90	673.2	30,000	224,415.6
0.6	4.49	100	748.0	40,000	299,220.8
0.7	5.24	200	1,496.1	50,000	374,025.9
0.8	5.98	300	2,244.2	60,000	448,831.1
0.9	6.73	400	2,992.2	70,000	523,636.3
1	7.48	500	3,740.3	80,000	598,441.5
	14.96	600	4,488.3	90,000	673,246.7
2	22.44	700	5,236.4	100,000	748,051.9
3	29.92	800	5,984.4	200,000	1,496,103.8
4	37.40	900	6,732.5	300,000	2,244,155.7
5	44.88	1,000	7,480.5	400,000	2,992,207.6
· 7 8 9	52.36 59.84	2,000 3,000	14,961.0 22,441.6	500,000 600,000	3,740,259.5 4,488,311.4
9	67.32	4,000	29,922.1	700,000	5,236,363.3
10	74.80	5,000	37,402.6	800,000	5,984,415.2
20	149.6	6,000	44,883.1	900,000	6,732,467.1
30 40	224.4 299.2	7,000	52,363.6	1,000,000	7,480,519.0

### Cubic Feet in a given Number of Gallons.

Gallons.	Cubic Ft.	Gallons.	Cubic Ft.	Gallons.	Cubic Ft.
1 2 3 4 5	.134 .267 .401 .535 .668	1,000 2,000 3,000 4,000 5,000	133,681 267,361 401,042 534,722 668,403	1,000,000 2,000,000 3,000,000 4,000,000 5,000,000	133,680.6 267,361.1 - 401,041.7 534,722.2 668,402.8
6 7 8 9	.802 .936 1.069 1.203 1.337	6,000 7,000 8,000 9,000 10,000	802.083 935.764 1,069.444 1,203,125 1,386.806	6,000,000 7,000,000 8,000,000 9,000,000 10,000,000	802,083.3 935,763.9 1,069,444.4 1,203,125.0 1,336,805.6

#### NUMBER OF SQUARE FEET IN PLATES 3 TO 32 FEET LONG, AND 1 INCH WIDE.

For other widths, multiply by the width in inches. 1 sq. in. = .00694 sq. ft.

1.01.011	CI WIG	ciis, maior	,	, WICIOI	i in inches			300g 3q. 1c.
Ft. and	Ins.	Square	Ft. and	Ins.	Square	Ft. and	Ins.	Square
Īn.	Long.	Feet.	Ins.	Long.	Feet.	Ins.	Long.	Feet.
Long.	20.00		Long.		2 0001	Long.	and and	
3. 0 1 2 3 4 5 6 7 8	36 37	.25 .2569	7.10	94 95	.6528 .6597	12. 8 9	159 153	1.056 1.063
2	38	.2639	8. 0	96	.6667	10	154	1.069
$\tilde{3}$	39	.2708	1	97	.6736	11	155	1.076
4	40	.2708 .2778	2 3 4	98	.6806	13. 0	155 156	1.083
5	41	.2847	3	99	.6875	1	157	1.09
6	42	.2917	4	100	.6944	1 2 3	158 159	1.097
8	43 44	.3056	5 6	101 102	.7014 .7083		160	1.104
9	45	.3125	7	103	.7153	5	161	1.104 1.114 1.118
10	46	.3194	8	104	7222	6	161 162	1.125
4. 0	47	.3264	9	105	.7292	4 5 6 7 8	163	1.132
4. 0	48 49	. 3333	10	106 107	.7361	9	164	1.139
9	50	.3472	9, 0	108	.7431 .75	10	165 166	1.146
ã	51	.3542	1	108 109	.7569	11	167	1.159
4	52	.3611	2	110	.7639	14.0	168	1.158 1.159 1.167
5	53	.3681	3	111	.7708 .7778	1	168 169 170	1.174 1.181
2 3 4 5 6 7 8	54 55	.375 .3819	2 3 4 5 6 7 8	112 113	.7778	2 3	170	1.181 1.188
é	56	.3889	6	114	.7917	4	172	1.100
9-	57	.3958	7	115	.7986	5	173	1.201
10	57 58	.4028	8	116	.8056	5 6 7 8 9	173 174	1.201 1.208
5. 0	59	.4097	9	117	.8125	7	175	1.215
5. 0	60 61	.4167 .4236	10	118 119	.8194 .8264	8	176 177	1.222 1.229
2	62	.4306	10. 0	120	.8333	10	178	1.236
1 2 3 4	63	.4375	1	121	.8403	11	170	1.243
4	64	.4444	2 3	122 123	.8472	15. 0 1	180 181 182 183	1.25 1.257
5. 6 7 8 9	65	.4514	3	123 124	.8542	1	181	1.257
7	66 67	.4583 .4653	4 5 6 7 8	124	.8611 .8681	2 3	182	1.264
8	68	.4722	6	126	.875	4	184	1.278
9	69	.4792	7	127	.8819	4 5 6 7 8	185	1.285
10	70 71 72	.4861	8	128	.8889	6	186	1.292
6. 0	71	.4931	9 10	129 130	.8958	7	187 188	1.299
0. 0	73	.5 .5069	11	131	.9028 .9097	9	189	1.306 1.313
2	74	.5139	11. 0	131 132	.9167	10	189 190	1.319
8	75 76	.5208	1 2	133	. 9236	11	191	1.326
4	76	.5278	2	134 135	.9306	16. 0 1	192	1.333
6. 0 1 2 3 4 5 6 7 8	78	.5347 .5417	3 4 5 6 7	100	.9375	1 9	193 194	1.34
7	78 79	.5486	5	137 138 139	.9514	2 3	195	1.354
8	80	. 5556	6	138	.9583	4	196	1 361
	81	.5625	7	139	.9653	5	197	1.368
10 11	82 83	.5694 .5764	8 9	140 141	.9722 .9792	5 6 7	198 199	1.375 1.382
7 0	84	.5834	10	141	.9861	8	200	1.389
1	84 85 86 87	.5903	11	143 .	.9931	8 9	201	1.396
2	86	.5972	12.0	144	1.000	10	202	1.403
3	87	.6042	1	145	1.007 1.014	17. 0	203	1.41
5	88 89	.6111 .6181	2 3	146 147	1.014	17.0	204 205	1.417 1.424
6	90	.625	4	148	1.028	2	206	1.434
7	91	.6319	5	149	1.035	2 3 4	207	1.438
2 3 4 5 6 7 8	92	.6389	4 5 6 7	150	1.042	4	208	1.444
9	93	.6458	7	151	1.049	5	209	1.451

## SQUARE FEET IN PLATES-(Continued.)

Ft. and Ins. Long.	Ins. Long.	Square Feet.	Ft. and Ins. Long.	Ins. Long.	Square Feet.	Ft. and Ins. Long.	Ins. Long.	Square Feet.
Ins.	210 311 312 213 214 4215 216 217 218 220 221 222 224 225 226 227 227 238 231 232 234 241 242 245 246 257 247 248 244 245 256 257 256 257 256	1.458 1.465 1.472 1.486 1.472 1.486 1.507 1.514 1.521 1.528 1.542 1.556 1.556 1.556 1.570 1.514 1.611 1.622 1.633 1.603 1.705 1.705 1.728 1.729 1.736 1.737 1.757 1.757 1.7757 1.7757 1.7757 1.7755	Ins. Long.  22. 5 6 7 8 9 10 11 23. 0 11 24. 0 11 24. 0 11 25. 0 10 11 25. 0 10 11 26. 0	Long.  269 270 271 272 273 273 274 275 276 277 278 277 278 280 281 281 281 281 281 281 281 281 281 281	Feet.  1.868 1.875 1.889 1.890 1.91 1.91 1.91 1.924 1.931 1.94 1.931 1.94 1.931 1.94 1.931 1.955 1.952 2.001 2.001 2.001 2.001 2.001 2.001 2.002 2.003 2.003 2.003 2.003 2.003 2.003 2.003 2.004 2.014 2.181 2.182 2.183 2.183 2.183 2.183 2.183 2.184 2.188	Ins. Long.  27. 4  5 6 6  7 8 9 10 11 28. 0  11 29. 0  10 11 29. 0  10 11 30. 0  11 31. 0  11 31. 0	Long.  328 329 331 331 332 333 333 334 335 338 339 331 341 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 341 345 345 346 347 347 347 347 347 347 347 347 347 347	Feet.  2.278 2.287 2.299 2.299 2.299 2.306 2.313 2.347 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.354 2.355 2.364 2.365
66 77 88 99 100 111 22.0 1 2 3 4		1.792 1.799 1.806 1.813 1.819 1.826 1.833 1.84 1.847 1.854 1.861	4 5 6 7 8 9 10 11 27.0 1 12		2.201 2.208 2.215 2.222 2.229 2.236 2.243 2.25 2.257 2.264 2.271	3 4 5 6 7 8 9 10 11 32.0 1		

# CAPACITIES OF RECTANGULAR TANKS IN U. S. GALLONS, FOR EACH FOOT IN DEPTH.

1 cubic foot = 7.4805 U.S. gallons.

_					L	ength (	of Tanl	ζ.			
	idth of										1
	ink.	feet.	ft. in. 2 6	feet. ft		et. ft. 4	in. fee		6 feet.	ft. in.	feet.
ft. 2 2 3 3 4	in. 6	29.92	46.75	56.10 67.32 7	5.45 7 8.54 8 1.64 10	4.80 8- 9.77 100 4.73 11	4.16 93 0.99 112 7.82 130	.81 82.5 .51 102.8 .21 123.4 .91 144.0 .61 164.5	86 112.2 13 134.6 00 157.0	1 121.56 5 145.87 9 170.18	183.27
4 5 5 6 6	6 6 6						187	.31 185.1 .01 205.1 226.5	71 224.4 28 246.8 269.3	1 243.11 6 267.43 0 291.74	261.82 288.00
7											366.54
=											
w	idth				L	ength o	of Tanl	ζ.			
	of ank.	ft. in.	feet.	ft. in. 8 6	feet.	ft. in. 9 6	feet.	ft. in. 10 6	feet.	ft. in. 11 6	feet. 12
ft. 2 2 3 3 4	in. 6 6	112.21 140.26 168.31 196.36 224.41	119.69 149.61 179.58 209.45 239.37	127.17 158.96 190.75 222.54 254.34	134.65 168.31 202.97 235.63 269.30	142 13 177,66 213,19 248,73 284,26	187.01 224.41 261.82		164.57 205.71 246.86 288.00 329.14	172.05 215.06 258.07 301.09 344.10	179 53 224.41 269.30 314.18 359.06
4 5 6 6	6 6 6	252.47 280.52 308.57 336.62 364.67	269,30 299,22 329,14 359,06 388,98	317.92 349.71	336.62 370.28 403.94	319.79 355,32 390.85 426.39 461.92	374.08 411.43 448.83	392.72 432.00 471.27	370.28 411.43 452.57 493.71 534.85	387.11 430.13 473.14 516.15 559.16	403.94 448.83 493.71 538.59 583,47
7 8 8 9	6	392.72 420.78	418.91 448.88 478.75	445 09 476.88 508.67 540.46	504.93 538.59	497,45 532,98 568,51 604,05 639,58	561 04 598,44 635.84	589.08 628.36 667 63	575.99 617.14 658.28 699.42 740.56	602.18 645.19 688.20 731.21 774.23	628 36 673.24 718.12 763.00 807.89
9 10 10 11 11	6 6 6					675.11	710.65 748.05		781.71 822.86 864.00 905.14	817.24 860.26 903.26 946.27 989,29	852.77 897.66 942.56 987.43 1032,3
12											1077.2

## NUMBER OF BARRELS (31 1-2 GALLONS) IN CISTERNS AND TANKS.

1 Barrel = 31½ gallons =  $\frac{31.5 \times 231}{1728}$  = 4.21094 cubic feet. Reciprocal = .237477.

Depth				I	iamete	er in F	eet.			
Feet.	5	6	7	8	9	10	11	12	13	14
1 5 6 7 8	4.663 23.3 28.0 32.6 37.3	33.6 40.3 47.0	9.139 45.7 54.8 64.0 73.1	11.937 59.7 71.6 83.6 95.5	75.5 90.6 105.8	18.652 93.3 111.9 130.6 149.2	22,569 112,8 135,4 158,0 180,6	26.859 134.3 161.2 188.0 214.9	31.529 157.6 189.1 220.7 252.2	36.557 182.8 219 3 255.9 292.5
9 10 11 12 13	42.0 46.6 51.3 56.0 60.6	60.4 67.1 73.9 80.6	82.3 91.4	107.4 119.4 131.3 143.2 155.2	136.0 151.1 166.2 181.3	167.9 186.5 205.2 223.8 242.5	203.1 225.7 248 3 270.8 293.4	241.7 268.6 295.4 322.3 349.2	283.7 315.2 346.7 378.3 409.8	329.0 365.6 402.1 438.7 475.2
14 15 16 17 18	65.3 69.9 74.6 79.3	94.0   1 100.7   1 107.4   1 114.1   1	27.9 37.1 46.2 55.4	167.1 179.1 191.0 202.9 214.9	211.5 226.6 241.7 256.8	261.1 289.8 298.4 317.1 335.7	316.0 338.5 361.1 383.7 406.2	376.0 402.9 429.7 456.6 483.5	441.3 472.8 504.4 535.9 567.4	511.8 548.4 584.9 621.5 658.0
19 20	88.6 93 3		73.6 82.8	226.8 238.7	287.1 302.2	354.4 373.0	428.8 451.4	510.3 537.2	598.9 630.4	694.6 731.1
Depth				I	Diamete	er in F	eet.			
feet.	15	16		17	18	19	20	)	21	22
1 5 6 7 8	41.96 209.8 251.8 293.8 335.7	238. 286.	$   \begin{array}{c cccc}     7 & 2 \\     5 & 3 \\     2 & 3   \end{array} $	3.903 69.5 23.4 77.3 31.2	60.431 302.2 362 6 423.0 483.4	67.8 336. 404. 471. 538.	7 373 0 445 3 525	3.0 4 7.6 49 2.2 5	32.253 11.3 93.5 75.8 58.0	90.273 451.4 541.6 631.9 722.2
9 10 11 12 13	377.7 419.7 461.6 503.6 545.6	477. 525. 573.	$\begin{bmatrix} 5 & 5 \\ 2 & 5 \\ 0 & 6 \end{bmatrix}$	85 1 39.0 92.9 46.8 00.7	543.9 604.3 664.7 725.2 785.6	606 673 740 808 875	3 746 7 826 0 895	5.1 8: 0.7 9: 5.3 9:	40.3 22.5 04.8 87.0 69.3	812.5 902.7 993.0 1083.3 1173.5
14 15 16 17 18	587.5 629.5 671.5 713.4 755.4	716. 764.	$\begin{bmatrix} 2 & 8 \\ 0 & 8 \\ 7 & 9 \end{bmatrix}$	54.6 08.5 62.4 16.4 70.3	846.0 906.5 966.9 1027.3 1087.8	942. 1010. 1077. 1144. 1212.	0   1119 3   1198 6   1268	0.1   123 3.7   133 3.3   133	33.8 16.0 98.3	1263.8 1354.1 1444.4 1534.5 1624.9
19										

#### NUMBER OF BARRELS (31 1-2 GALLONS) IN CISTERNS AND TANKS .- Continued.

Depth		Diameter in Feet.									
in Feet.	23	24	25	26	27	28	29	30			
1	98.666	107.432	116.571	126.083	135.968	146.226	157.858	167.868			
5	493.3	537.2	582.9	630.4	679.8	731.1	784.3	839.3			
6	592.0	644.6	699.4	756.5	815.8	877.4	941.1	1007.2			
7	690.7	752.0	816.0	882.6	951.8	1023.6	1098.0	1175.0			
8	789.3	859.5	932.6	1008.7	1087.7	1169.8	1254.9	1342.9			
9	888.0	966.9	1049.1	1134.7	1223.7	1316.0	1411.7	1510.8			
10	986.7	1074.3	1165.7	1260.8	1359.7	1462.2	1568.6	1678.6			
11	1085.3	1181.8	1282.3	1386.9	1495.6	1608.5	1725.4	1846.5			
12	1184.0	1289.2	1398.8	1513.0	1631.6	1754.7	1882.3	2014.4			
13	1282.7	1396.6	1515.4	1639.1	1767.6	1900.9	2039.2	2182.2			
14	1381.3	1504 0	1632.0	1765.2	1903.6	2047.2	2196.0	2350.1			
15	1480.0	1611.5	1748.6	1891.2	2039.5	2193.4	2352.9	2517.9			
16	1578.7	1718.9	1865.1	2017.3	2175.5	2339.6	2509.7	2685.8			
17	1677.3	1826.3	1981.7	2143.4	2311.5	2485.8	2666.6	2853.7			
18	1776.0	1933.8	2098.3	2269.5	2447.4	2632.0	2823.4	3021.5			
19	1874.7	2041.2	2214.8	2395.6	2583.4	2778.3	2980.3	3189.4			
20	1973.3	2148.6	2321.4	2521.7	2719.4	2924.5	3137.2	3357.3			

#### LOGARITHMS.

Logarithms (abbreviation log).—The log of a number is the exponent of the power to which it is necessary to raise a fixed number to produce the given number. The fixed number is called the base. Thus if the base is 10, the log of 1000 is 3, for  $10^2 = 1000$ . There are two systems of logs in general use, the common, in which the base is 10, and the Naperian, or hyperbolic, in which the base is 2/18281828. The Naperian base is commonly de-

noted by e, as in the equation  $e^y = x$ , in which y is the Nan. log of x. In any system of logs, the log of 1 is 0; the log of the base, taken in that system, is 1. In any system the base of which is greater than 1, the logs of all numbers greater than 1 are positive and the logs of all numbers less than

1 are negative.

The modulus of any system is equal to the reciprocal of the Naperian log of the base of that system. The modulus of the Naperian system is 1, that

of the observed mat system. The modulus of the Naperian system is 1, that of the common system is .4342945.

The log of a number in any system equals the modulus of that system × the Naperian log of the number.

The hyperbolic or Naperian log of any number equals the common log

Every log consists of two parts, an entire part called the *characteristic*, or index, and the decimal part, or *mantissa*. The mantissa only is given in the usual tables of common logs, with the decimal point omitted. The characteristic is found by a simple rule, viz., it is one less than the number of figures to the left of the decimal point in the number whose log is to be found. Thus the characteristic of numbers from 1 to 9.99 + is 0, from 10 to 99.99 + is 1, from 100 to 999 + is 3, from .1 to .99 + is -1, from .01 to .999 + is -2, etc. Thus

> log of 2000 is 3.30103; log of .2 is - 1.30103; 200 " 2.30103; 20 " 1.30103; .02 " - 2.30103; .002 " - 3.30103; .. .. 2 " 0.30103; 44 44 .0002 " - 4,30103

The minus sign is frequently written above the characteristic thus:  $\log_{100} .002 = 3.30103$ . The characteristic only is negative, the decimal part, or mantissa, being always positive.

When a log consists of a negative index and a positive mantissa, it is usual to write the negative sign over the index, or else to add 10 to the index, and to indicate the subtraction of 10 from the resulting logarithm.

Thus  $\log .2 = T.30103$ , and this may be written 9.30103 - 10. In tables of logarithmic sines, etc., the -10 is generally omitted, as being understood.

Rules for use of the table of Logarithms.—To find the log of any whole number.—For 1 to 100 inclusive the log is given complete in the small table on page 129.

For 100 to 999 inclusive the decimal part of the log is given opposite the

For 100 to 999 inclusive the decimal part of the log is given opposite the given number in the column headed 0 in the table (including the two figures to the left, making six figures). Prefix the characteristic, or index, 2. For 1000 to 9999 inclusive: The last four figures of the log are found opposite the first three figures of the given number and in the vertical column headed with the fourth figure of the given number; prefix the two figures under column 0, and the index, which is 3. For numbers over 10,000 having five or more digits: Find the decimal part of the log for the first four digits as above, multiply the difference figure in the last column by the remaining digit or digits, and divide by 10 if there be only one digit more, by 100 if there be two more, and so on; add the quotient to the log of the first four digits and prefix the index, which is 4 if there are five digits, 5 if there are six digits, and so on. The table of proportional parts may be used, as shown below.

To find the log of a decimal fraction or of a whole number and a decimal. First find the log of the quantity as if there were no decimal point, then prefix the index according to rule; the index is one less than the number of figures to the left of the decimal point.

Required log of 3.141593.

To find the number corresponding to a given log.—Find in the table the log nearest to the decimal part of the given log and take the first four digits of the required number from the column N and the top or foot of the column containing the log which is the next less than the given log. To find the 5th and 6th digits subtract the log in the table from the given log, multiply the difference by 100, and divide by the figure in the lift column converts that low, we want to except the table from the given log. Diff. column opposite the log; annex the quotient to the four digits already found, and place the decimal point according to the rule; the number of figures to the left of the decimal point is one greater than the index.

> Find number corresponding to the log ...... 0.497150 Next lowest log in table corresponds to 3141..... .497068 Diff. = 82

Tabular diff. = 138;  $82 \div 138 = .59 +$ 

The index being 0, the number is therefore 3.14159 +.

To multiply two numbers by the use of logarithms.—Add together the logs of the two numbers, and find the number whose log is the sum.

To divide two numbers.—Subtract the log of the less from the

log of the greater, and find the number whose log is the difference.

To raise a number to any given power,—Multiply the log of the number by the exponent of the power, and find the number whose log is the product.

To find any root of a given number.—Divide the log of the number by the index of the root. The quotient is the log of the root. To find the reciprocal of a number.—Subtract the decimal

part of the log of the number from 0, add 1 to the index and change the sign of the index. The result is the log of the reciprocal.

Required the reciprocal of 3.141593.

.. 0.4971498 Log of 3,141593, as found above...... Subtract decimal part from 0 gives..... 0.5028502 Add 1 to the index, and changing sign of the index gives .. T.5028502

which is the log of 0.31831.

To find the fourth term of a proportion by logarithms.

—Add the logarithms of the second and third terms, and from their sum subtract the logarithm of the first term.

When one logarithm is to be subtracted from another, it may be more convenient to convert the subtraction into an addition, which may be done by first subtracting the given logarithm from 10, adding the difference to the

other logarithm, and afterwards rejecting the 10.

The difference between a given logarithm and 10 is called its arithmetical

complement, or cologarithm.

To subtract one logarithm from another is the same as to add its complement and then reject 10 from the result. For a-b=10-b+a-10

To work a proportion, then, by logarithms, add the complement of the logarithm of the first term to the logarithms of the second and third terms.

The characteristic must afterwards be diminished by 10.

Example in logarithms with a negative index.-Solve by 526 \2.45 , which means divide 526 by 1011 and raise the quotient logarithms 1011

to the 2.45 power.

In multiplying -1.7 by 5, we say:  $5 \times 7 = 35$ , 3 to carry;  $5 \times -1 = -5$  less +3 carried =-2. In adding -2+8+3+1 carried from previous column, we say: 1+3+8=12, minus 2=10, set down 0 and carry 1; 1+4-2=3.

#### LOGARITHMS OF NUMBERS FROM 1 TO 100.

N.	Log.	N.	Log.	N.	Log.	N.	Log.	N.	Log.
1	0.000000	21	1.322219	41	1.612784	61	1.785330	81	1.908485
2	0.301030	22	1.342423	42	1.623249	62	1.792392	82	1.913814
3	0.477121	23	1.361728	43	1.633468	63	1.799341	83	1.919078
4	0.602060	24	1.380211	44	1.643453	64	1.806180	84	1.924279
5	0.698970	25	1.397940	45	1.653213	65	1.812913	85	1.929419
6	0.778151	26	1.414973	46	1.662758	66	1.819544	86	1.934498
7	0.845098	27	1.431364	47	1.672098	67	1.826075	87	1.939519
8	0.903090	28	1.447158	48	1.681241	68	1.832509	88	1.944483
9	0.954243	29	1.462398	49	1.690196	69	1.838849	89	1.949390
10	1.000000	30	1.477121	50	1.698970	70	1.845098	90	1.954243
11	1.041393	31	1.491362	51	1.707570	71	1.851258	91	1.959041
12	1.079181	32	1.505150	52	1.716003	72	1.857332	92	1.963788
13	1.113943	33	1.518514	53	1.724276	73	1.863323	93	1.968483
14	1.146128	34	1.531479	54	1.732394	74	1.869232	94	1.973128
15	1.176091	35	1.544068	55	1.740363	75	1.875061	95	1.977724
16	1.204120	36	1.556303	56	1.748188	76	1.880814	96	1.982271
17	1.230449	37	1.568202	57	1.755875	77	1.886491	97	1.986772
18	1.255273	38	1.579784	58	1.763428	78	1.892095	98	1.991226
19	1.278754	39	1.591065	59	1.770852	79	1.897627	99	1.995635
20	1.301030	40	1.602060	60	1.778151	80	1.903090	100	2.000000

No.	100 L. 00	0.]							[N	To. 109	L. 040
N.	6	1	2	8	4	5	6	7	8	9	Diff
100	000000 4321 8600	0434 4751 9026	0868 5181 9451	1301 5609 9876	1734 6038	2166 6466	2598 6894	3029 7821	3461 7748	3891 8174	435 426
3 4	012837 7033	3259 7451	3680 7868	4100 8284	0300 4521 8700	0724 4940 9116	1147 5360 9532	1570 5779 9947	1993 6197 0361	2415 6616 0775	420 420 410
5 6 7	021189 5306 9384	1603 5715 9789	2016 6125	2428 6533	2841 6942	3252 7350	3664 7757	4075 8164	4486 8571	4896 8978	419 408
8	033424 7426 04	3826 7825	0195 4227 8223	0600 4628 8620	1004 5029 9017	1408 5430 9414	1812 5830 9811	2216 6230 0207	2619 6629 0602	3021 7028 0998	40- 40- 39-

#### PROPORTIONAL PARTS.

Diff.	1	2	3	4	5	6	.7	8	9
434	43.4	86.8	130.2	173.6	217.0	260.4	303.8	347.2	390.6
433	43.3	86.6	129.9	173.2	216.5	259.8	303.1	346.4	389.7
432	43.2	86.4	129.6	172.8	216.0	259.2	302.4	345.6	388.8
431	43.1	86.2	129.3	172.4	215.5	258.6	301.7	344.8	387.9
430	43.0	86.0	129.0	172.0	215.0	258.0	301.0	344.0	387.0
429	42.9	85.8	128.7	171.6 171.2	214.5	257.4	300.3	343.2	386.1
428	42.8	85.6	128.4	171.2	214.0	256.8	299.6	342.4	385.2
427	42.7	85.4	128.1	170.8	213.5	256.2	298.9	341.6	384.3
426	42.6	85.2	127.8	170.4	213.0	255.6	298.2	340.8	383.4
425	42.5	85.0	127.5	170.0	212.5	255.0	297.5	340.0	382.5
424	42.4	84.8	127.2	169.6	212.0	254.4	296.8	339.2	381.6
423	42.3	84.6	126.9	169.2	211.5	253.8	296.1	338.4	380.7
422	42.2	84.4	126.6	168.8	211.0	253.2	295.4	337.6	379.8
421	42.1	84.2	126.3	168.4	210.5	252.6	294.7	336.8	378.9 378.0
420	42.0	84.0	126.0	168.0	210.0	252.0	294.0	336.0	378.0
419	41.9	83.8	125.7	167.6	209.5	251.4	293.3	335.2	377.1
418	41.8	83.6	125.4	167.2	209.0	250.8	292.6	334.4 333.6	376.2 375.3
417	41.7	83.4	125.1	166.8	208.5	250.2	291.9	333.6	375.3
416	41.6	83.2	124.8	166.4	208.0	249.6	291.2	332.8	374.4
415	41.5	83.0	124.5	166.0	207.5	249.0	290.5	332.0	373.5
414	41.4	82.8	124.2	165.6	207.0	248.4	289.8	331.2	372.6
413	41.8	82.6	123.9	165.2	206.5	247.8	289.1	330.4	371.7
412	41.2	82.4	123.6	164.8	206.0	247.2	288.4	329.6	370.8
411	41.1	82.2	123.3	164.4	205.5	246.6	287.7	328.8	369.9
410	41.0	82.0	123.0	164.0	205.0	246.0	287.0	328.0	369.0
409	40.9	81.8	122.7	163.6	204.5	245.4	286.3	327.2	368.1
408	40.8	81.6	122.4 122.1	163.2	204.0	244.8	285.6	326.4	367.2
407	40.7	81.4	122.1	162.8	203.5	244.2	284.9	325.6	366.3
406	40.6	81.2	121.8	162.4	203.0	243 6	284.2	324.8	365.4
405	40.5	81.0	121.5	162.0	202.5	243.0	283.5	324.0	364.5
404	40.4	80.8	121.2	161.6	202.0	242.4	282.8	323.2	363.6
403	40.3	80.6	120.9	161.2	201.5	241.8	282.1	322.4	362.7
402	40.2	80.4	120.6	160.8	201.0	241 2	281.4	321.6	361.8
401	40.1	80.2	120.3	160.4	200.5	240.6	280.7	320.8	360.9
400	40.0	80.0	120.0	160.0	200.0	240.0	280.0 279.3	320.0	360.0
399	39.9	79.8	119.7	159.6	199.5	239.4	279.3	319.2	359.1
398	39.8	79.6	119.4	159.2	199.0	238.8	278.6 277.9	318.4	358.2
397	39.7	79.4	119.1	158.8	198.5	238.2	277.9	317.6	357.3
396	39.6	79.2	118.8	158.4		237.6	277.2	316.8	356.4
395	39.5	79.0	118.5	158.0	197.5	237.0	276.5	316 0	355.5

No.	110	L.	041.7	

[No. 119 L. 078.

Ņ.	0	1	2	3	4	5	6	7	8	9	Diff.
110 1 2	041393 5323 9218	1787 5714 9606	2182 6105 9998	2576 6495	2969 6885	3362 7275	3755 7664	4148 8053	4540 8442	4932 8830	393 390
3 4	053078 6905	3463 7286	3846 7666	0380 4230 8046	0766 4613 8426	1153 4996 8805	1538 5378 9185	1924 5760 9563	2309 6142 9942	2694 6524	386 383
5 6 7	060698 4458 8186	1075 4832 8557	1452 5206 8928	1829 5580 9298	2206 5953 9668	2582 6326	2958 6699	3333 7071	3709 7443	0320 4083 7815	379 376 373
8 9	071882 5547	2250 5912	2617 6276	2985 6640	3352 7004	0038 3718 7368	0407 4085 7731	0776 4451 8094	1145 4816 8457	1514 5182 8819	370 366 363
	001,	0012	0.010	0010	1001	1000	1101	0034	Oioi	0015	000

8 9	071882 5547	2250 5912	2617 6276	2985 6640	3352 7004	0038 3718 7368	0407 4085 7731	0776 4451 8094	1145 4816 8457	1514 5182 8819	370 366 363
				Pro	OPORTIC	NAL PAI	RTS.		1		
Diff	. 1	2		3	4	5	6		7	8	9
395 394 393 391 390 389 388 387 386 385 381 380 377 376 373 373 373	39.5 39.4 39.3 39.2 39.1 39.0 38.9 38.8 38.7 38.6 38.5 38.4 38.3 38.1 38.0 37.9 37.6 37.4 37.3 37.4	79.0 78.8 78.4 78.2 78.0 77.4 77.0 76.8 76.6 76.4 75.6 75.6 75.4 75.0 74.8	111 111 111 111 111 111 111 111 111 11	8.5 7.8 7.6 7.7 6.7 6.7 6.6 6.7 6.6 6.1 6.1 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5.5 5	158.0 157.6 157.2 156.8 156.6 155.6 155.5 154.8 154.0 158.6 155.2 154.8 154.0 158.6 159.8 152.4 152.0 151.6 151.6 151.6 151.6 151.6 151.6 151.6 151.6 151.6 151.6 151.8	197.5 197.0 196.5 196.0 195.5 195.0 194.5 193.5 192.5 192.0 191.5 190.0 189.5 189.0 188.5 187.0 187.5	2377 2366 2355 2344 2343 2332 2313 2310 2299 2292 2272 2272 2272 2272 2272 227	.4 .8 .2 .6 .0 .4 .8 .2 .6 .0 .4 .8 .2 .6 .0 .4 .8 .2 .6 .0 .4 .8 .8 .8 .8 .8 .8 .8 .8 .8 .8 .8 .8 .8	276.5 275.8 275.1 274.4 273.0 273.0 271.6 270.9 270.2 269.5 268.8 268.8 268.1 266.0 26	316.0 315.2 314.4 313.8 312.0 311.2 310.4 309.8 308.0 307.2 306.4 305.6 304.8 304.0 303.2 301.6 302.4 301.6 300.8	355.5 354.6 353.7 352.8 351.9 351.0 350.1 349.2 348.3 347.4 346.5 345.8 344.7 348.8 342.0 341.1 349.2 349.2 349.2 349.3 347.4 346.5 347.4 346.5 347.4 347.5 348.8 349.2 349.3 34
371 370 369 368 367 366 565	37.1 37.0 36.9 36.8 36.7 36.6	74.2 74.0 78.8 78.6 78.4 78.2 78.2		11.3 11.0 10.7 10.4 10.1 09.8 09.5	148.4 148.0 147.6 147.2 146.8 146.4 146.0	185.5 185.0 184.5 184.0 183.5 183.0 182.5	222 221 221 220 220 219 219	.6 .0 .4 .8 .2	259.7 259.0 258.3 257.6 256.9 256.2 255.7	296.8 296.0 295.2 294.4 293.6 292.8 292.0	333.9 333.0 332.1 331.2 330.3 329.4 328.5
364 363 362 361 360 359 358 357 356	36.3 36.2 36.1 36.0 35.9 35.8 35.8	72.8 72.6 72.4 72.5 72.0 71.8 71.6 71.4	10 10 10 10 10 10 10 10 10 10 10 10 10 1	09.2 08.9 08.6 08.3 08.0 07.7 07.4 07.1 06.8	145.6 145.2 144.8 144.4 144.0 143.6 143.2 142.8 142.4	182.0 181.5 181.0 180.5 180.0 179.5 179.0 178.5 178.0	218 217 217 216 216 216 214 214 214 213	.8 .2 .6 .0 .4 .8	254.8 254.1 253.4 252.7 252.0 251.3 250.6 249.9 249.2	291.2 290.4 289.6 288.8 288.0 287.2 286.4 285.6 284.8	327.6 326.7 325.8 324.9 323.1 322.2 321.3 320.4

Diff. 1

329 32.9 32.8 65.8

328

327  $\frac{32.7}{32.6}$ 65.4

326

325 32.5 65.0

324

323

322 32.2 64.4

32.4

32.3

No.	120 L. 0	79.]							[N	o. 134	L. 130.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
120	079181	9543	9904	0266	0626	0987	1347	1707	2067	2426	360
1 2	082785 6360	3144 6716	3503 7071	3861 7426	4219 7781	4576 8136	4984 8490	5291 8845	5647 9198	6004 9552	357 355
3 4	9905 093422	0258 3772	0611 4122	0963 4471	1315 4820	1667 5169	2018 5518	2370 5866	2721 6215	3071 6562	352 349
5 6	100371	7257 0715	7604 1059	7951	8298 1747	2091	8990 2434	9885	9681	0026 3462	346 343
7 8	3804 7210	4146 7549	4487 7888	4828 8227	5169 8565	5510 8903	5851 9241	6191 9579	6531 9916	0253	341 338
9	110590	0926	1263	1599	1934	2270	2605	2940	3275	3609	335
130	3943 7271	4277 7603	4611 7934	4944 8265	5278 8595	5611 8926	5943 9256	6276 9586	6608 9915	6940	333
2 3	120574 3852	0903 4178	1231 4504	1560 4830	1888 5156	2216 5481	2544 5806	2871 6131	3198 6456	0245 3525 6781	330 328 325
4	7105 13	7429	7753	8076	8399	8722	9045	9368	9690	0012	323

#### Proportional Parts.

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CONTROL CONTRO

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65.6

65.2

64.8

64.6

3

355	35.5	71.0	106.5	142.0	177.5	213.0	248.5	284.0	319.5
354	35.4	70.8	106.2	141.6	177.0	212.4	247.8	283.2	318.6
353	35.3	70.6	105.9	141.2	176.5	211.8	247.1	282.4	317.7
352	35.2	70.4	105.6	140.8	176.0	211.2	246.4	281.6	316.8
351	35.1	70.2	105.3	140.4	175.5	210.6	245.7	280.8	315.9
350	35.0	70.0	105.0	140.0	175.0	210.0	245.0	280.0	315.0
349	34.9	69.8	104.7	139.6	174.5	209.4	244.3	279.2	314.1
348	34.8	69.6	104.4	139.2	174.0	208.8	243.6	278.4	313.2
347	34.7	69.4	104.1	138.8	173.5	208.2	242.9	277.6	312.3
346	34.6	69.2	103.8	138.4	173.0	207.6	242.2	276.8	311.4
345	34.5	69.0	103.5	138.0	172.5	207.0	241.5	276.0	310.5
344	34.4	68.8	103.2	137.6	172.0	206.4	240.8	275.2	309.6
343	34.3	68.6	102.9	137.2	171.5	205.8	240.1	274.4	308.7
342	34.2	68.4	102.6	136.8	171.0	205.2	239.4	273.6	307.8
341	34.1	68.2	102.3	136.4	170.5	204.6	238.7	272.8	306.9
340	34.0	68.0	102.0	- 136.0	170.0	204.0	238.0	272.0	306.0
339	33.9	67.8	101.7	135.6	169.5	203.4	237.3	271.2	305.1
338	33.8	67.6	101.4	135.2	169.0	202.8	236.6	270.4	304.2
337	33.7	67.4	101.1	134.8	168.5	202.2	235.9	269.6	303.3
336	33.6	67.2	100.8	134.4	168.0	201.6	235.2	268.8	302.4
335	33.5	67.0	100.5	134.0	167.5	201.0	234.5	268.0	301.5
334	33.4	66.8	100.2	133.6	167.0	200.4	233.8	267.2	300.6
333	33.3	66.6	99.9	133.2	166.5	199.8	233.1	266.4	299.7
332	33.2	66.4	99.6	132.8	166.0	199.2	232.4	265.6	298.8
331	33.1	66.2	99.3	132.4	165.5	198.6	231.7	264.8	297.9
330	33.0	66.0	99.0	132.0	165.0	198.0	231.0	264.0	297.0
000	00.0	00.0	00.0	100.0	100.0	100.0	201.0	~UI.U	201.0

131.6

131.2

130.8

130.4

130.0

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129.2

128.8

98.7

 $98.4 \\ 98.1$ 

97.8

97.5

97.2

96.9

96.6

164.5 164.0

163.5

163.0

162.5

162.0

161.5

161.0

197.4 196.8

196.2

195.6

195.0

194.4

193.8

193.2

230.3 229.6 228.9

228.2

227.5

226.8

226.1

225.4

264.0 263.2 297.0

262.4 261.6

260.8 293.4

260.0 292.5

259.2 291.6

258.4

257.6 289.8

296.1 295.2 294.3

290.7

							01 1						
No.	135 L. 1	30.]									[	No. 149	L. 175.
N.	0	1		2	3	4	5	6		7	8	9	Diff.
135	130334 3539	0655 3858	0	977 1177	129 449		1939 5133	2260 5451	2	580 769	290 608	0 3219 6 6403	321 318
6 7 8	6721 9879	7037	7	354	767		8303	8618		984	924		316
9	143015	0194 3327	1 6	)508 3639	082 395		1450 4574	1763 4885		076 196	2389 550		314 311
140 1	6128 9219	6438 9527	1	6748 9835	705		7676	7985		294	860	1	* 309
	152288	2594	_	2900	014 320		0756 3815	1063 4120		370 124	167 472		307 305
2 3 4	5336 8362	5640 8664	1 5	943 965	624 926	6   6549	6852 9868	7154	7	457	775		303
5	161368	1667	-	967	226	6 2564	2863	0168 3161	3	469 460	076 375	8 4055	301 299
6	4353 7317	4650 7613		1947 1908	524 820		5838 8792	6134 9086		430 380	672 967	$ \begin{array}{c c} 6 & 7022 \\ 4 & 9968 \end{array} $	297 295
8 9	170262	0555	9	848	114		1726	2019	2	311	260		293
9	3186	3478	100	3769	406	0 4351	4641	4932	97	222	551	2   5802	291
					Pı	ROPORTI	ONAL PA	RTS.					
Diff	. 1	2		;	3	4	5	6			7	8	9
321 320	32.1 32.0	64.2 64.0		96 96	.3	128.4 128.0	160.5 160.0	192 192	.6	22	24.7 24.0	256.8 256.0	288.9
319 318	31.9	63.8		95 95	.7	127.6 127.2	159.5 159.0	191 190	.4	25	23.3	255.2 254.4	287.1 286.2
317 316	31.7 31.6	63.4 63.2		95 94	.1	$126.8 \\ 126.4$	158.5 158.0	190 189	.2	22	21.9	253.6 252.8	285.3 284.4
315 314	31.5	63.0		94	.5	126.0 125.6	157.5 157.0	189 188	.4	25	20.5 19.8	252.0 251.2	283.5 282.6
313 312	31.3 31.2	62.6 62.4		93 93	.9 .6	125.2 124.8	156.5 156.0	187 187	.8	2:	$19.1 \\ 18.4$	250.4 249.6	281.7 280.8
311 310	31.1 31.0	62.2 62.0		93 93	.0	124.4 124.0	155.5 155.0	186	0.6	2	17.7	248.8 248.0	279.9 279.0
309 308	30.9	61.8		92 92	.4	123.6 123.2	154.5 154.0	185 184	.8	2	16.3 15.6	247.2 246.4	278.1 277.2
307 306	30.7 30.6 30.5	61.4 61.2 61.0		92 91	.8	122.8 122.4	153.5 153.0 152.5	184 188 188	1.6	2:	14.2	245.6 244.8	
305 304 303	30.4 30.3	60.8		91 91 90	.2	122.0 121.6 121.2	152.0 151.5	182	.4	2	13.5 12.8 12.1	244.0 243.2 242.4	273.6 272.7 271.8
302	30.2	60.4		90	.6	120.8	151.0	181	.2	2:	11.4	241.6	
301 300 299	30.1 30.0 29.9	60.2 60.0 59.8		90 90 89	.0	120.4 120.0 119.6	150.5 150.0 149.5	180 180 179	0.0	2:	10.7 $10.0$ $09.3$	240.8 240.0 239.2	270.9 270.0 269.1
299 298 297	29.9 29.8 29.7	59.6 59.4		89	.4	119.0 119.2 118.8	149.0 148.5	178 178	3.8	20	08.6 07.9	239.2 238.4 237.6	268.2 267.3
296 295	29.6 29.5	59.2 59.0	,	88	.8	118.4 118.0	148.0 147.5	177	.6	20	07.2	236.8 236.0	266.4 265.5
294 293	29.4 29.3	58.8	3	88	.2	117.6 117.2	147.0 146.5	176	5.4	20	05.8	235.2 234.4	264.6 263.7
292 291	29.2 29.1	58.4 58.2	Į	87	.6	116.8 116.4	146.0 145.5	175	5.2	2	04.4	232.8	262.8 261.9
290 289	29.0	58.0	)	87	.0	116.0 115.6	145.0 144.5	174	1.0	20	03.0	232.0	261.0 260.1
288 287	28.8 28.7	57.6 57.4 57.2	L	86	.4	115.2 114.8	144.0 143.5	179 179 179	2.8	20	01.6	230.4 229.6	259.2 258.3
286	28.6	57.2	2		.8	114.4	143.0	177	.6	2	00.2	228.8	257.4

N.	0	1	2	3	4	5	6	7	8	9	Diff.
150	176091	6381	6670	6959 9839	7248	7536	7825	8113	8401	8689	289
2 3	8977 181844 4691	9264 2129 4975	9552 2415 5259	2700 5542	0126 2985 5825	0413 3270 6108	0699 3555 6391	0986 3839 6674	1272 4123 6956	1558 4407 7239	287 285 283
4 5	7521	7803	0892	8366 1171	8647	8928 1730	9209	9490 2289	9771	0051 2846	281 279
678	3125 5900 8657	3403 6176 8932	3681 6453 9206	3959 6729 9481	4287 7005 9755	4514 7281	4792 7556	5069 7832	5346 8107	5623 8382	278 276
9	201397	1670	1943	2216	2488	0029 2761	0303 3033	0577 3305	0850 3577	1124 3848	274 272
160 1 2	4120 6826 9515	4391 7096 9783	4663 7365	4934 7634	5204 7904	5475 8173	5746 8441	6016 8710	6286 8979	6556 9247	271 269
3 4 5	212188 4844 7484	2454 5109 7747	0051 2720 5373 8010	0319 2986 5638 8273	0586 3252 5902 8536	0853 3518 6166 8798	1121 3783 6430 9060	1388 4049 6694 9323	1654 4314 6957 9585	1921 4579 7221 9846	267 266 264 262
6 7 8 9	220108 2716 5309 7887	0370 2976 5568	0631 3236 5826	0892 3496 6084	1153 3755 6342	1414 4015 6600	1675 4274 6858 9426	1936 4533 7115 9682	2196 4792 7372 9938	2456 5051 7630	261 259 258
9	23	8144	8400	8657	8913	9170	9426	9082	9998	0193	256
				Pro	PORTIC	NAL PA	RTS.				
Diff	f. 1	2	É	3	4	5	6		7	8	9
285 284 283 282 281 280 279 278 277 276	28.4 28.3 28.2 28.1 28.0 27.9 27.8 27.7	57.0 56.8 56.6 56.4 56.2 56.0 55.8 55.6 55.4 55.2	85 85 84 84 84 84 83 83 83	.2 .9 .6 .3 .0 .7 .4	114.0 113.6 113.2 112.8 112.4 112.0 111.6 111.2 110.8 110.4	142.5 142.0 141.5 141.0 140.5 140.0 139.5 139.0 138.5 138.0	171 170 169 169 168 168 167 166 166	.4 1 .8 1 .2 1 .6 1 .0 1 .4 1 .8 1 .2 1	99.5 98.8 98.1 97.4 96.7 96.0 95.3 94.6 93.9 93.2	228.0 227.2 226.4 225.6 224.8 224.0 223.2 222.4 221.6 220.8	256. 255. 254. 253. 252. 252. 251. 250. 249. 248.
275 274 273 272 271 270 269 268 267 266	27.4 27.3 27.2 27.1 27.0 26.9 26.8 26.7	55.0 54.8 54.6 54.4 54.2 54.0 53.8 53.6 53.4 53.2	81 81 81 81 80 80 80	.9 .6 .3 .0 .7	110.0 109.6 109.2 108.8 108.4 108.0 107.6 107.2 106.8 106.4	137.5 137.0 136.5 136.0 135.5 135.0 134.5 134.0 133.5 133.0	165 164 163 163 162 162 161 160 160 159	.4   1 .8   1 .2   1 .6   1 .0   1 .4   1 .8   1 .2   1	92.5 91.8 91.1 90.4 89.7 89.0 88.3 87.6 86.9 86.2	220.0 219.2 218.4 217.6 216.8 216.0 215.2 214.4 213.6 212.8	247. 246. 245. 244. 243. 243. 242. 241. 240. 239.
265 264 263 262 261 260 259 258 257 256	26.4 26.3 26.2 26.1 26.0 25.9 25.8 25.8	53.0 52.8 52.6 52.4 52.2 52.0 51.8 51.6 51.4	79 78 78 78 78 77	.5 .9 .6 .3 .0 .7 .4	106.0 105.6 105.2 104.8 104.4 104.0 103.6 103.2 102.8	132.5 132.0 131.5 131.0 130.5 130.0 129.5 129.0 128.5	159 158 157 157 156 156 155 154 154	.4 1 .8 1 .2 1 .6 1 .0 1 .4 1 .8 1	85.5 84.8 84.1 83.4 82.7 82.0 81.3 80.6 79.9 79.2	212.0 211.2 210.4 209.6 208.8 208.0 207.2 206.4 205.6 204.8	238. 237. 236. 235. 234. 234. 233. 232. 231.

No.	170 L. 23	0.]							[N	o. 189	L. 278.
N.	0	1	2	3	4	5	6	7	8	9	Diff.
170 1 2 3	230449 2996 5528 8046	0704 3250 5781 8297	0960 3504 6033 8548	1215 3757 6285 8799	1470 4011 6537 9049	1724 4264 6789 9299	1979 4517 7041 9550	2234 4770 7292 9800	2488 5023 7544	2742 5276 7795	255 253 252
4 5 6	240549 3038 5513	0799 3286 5759	1048 3534 6006	1297 3782 6252	1546 4030 6499	1795 4277 6745	2044 4525 6991	2293 4772 7237	0050 2541 5019 7482	0800 2790 5266 7728	250 249 248 246
7 8 9	7978 250420 2853	8219 0664 3096	8464 0908 3338	8709 1151 3580	1395 3822	9198 1638 4064	9443 1881 4306	9687 2125 4548	9932 2368 4790	0176 2610 5081	245 243 242
180	5273 7679	5514 7918	5755 8158	5996 8398	6237 8637	6477 8877	6718 9116	6958 9355	7198 9594	7439 9833	241 239
2 3 4 5 6	260071 2451 4818 7172 9513	0310 2688 5054 7406 9746	0548 2925 5290 7641 9980	0787 3162 5525 7875	1025 3399 5761 8110	1263 3636 5996 8344	1501 3873 6232 8578	1739 4109 6467 8812	1976 4346 6702 9046	2214 4582 6937 9279	238 237 235 234
7 8 9	271842 4158 6462	2074 4389 6692	2306 4620 6921	0213 2538 4850 7151	0446 2770 5081 7380	0679 3001 5311 7609	0912 3233 5542 7838	1144 3464 5772 8067	1377 3696 6002 8296	1609 3927 6232 8525	233 232 230 229
8	4158	4389	4620	2538 4850	2770 5081	3001 5311	3233 5542	3464 5772	3696 6002	3927 6232	62.62

### PROPORTIONAL PARTS.

Diff.	1	2	3	4	5	6	7	8	9
255	25.5	51.0	76.5	102.0	127.5	153.0	175.5	204.0	229.5
254	25.4	50.8	76.2	101.6	127.0	152.4	177.8	203.2	228.6
253	25.3 25.2	50.6 50.4	75.9 75.6	101.2 100.8	126.5 126.0	151.8 151.2	177.1 176.4	201.6	227.7 226.8
252	25.1	50.4	75.8	100.8	125.5	150.6	175.7	200.8	225.9
251	25 0	50.2	75.0	100.4	125.0	150.0	175.0	200.8	225.0
250 249	24.9	49.8	74.7	99.6	124.5	149.4	174.3	199.2	224.1
249	24.9	49.6	74.4	99.0	124.0	148.8	173.6	198.4	223.2
247	24.0	49.4	74.1	98.8	123.5	148.2	172.9	197.6	222.3
246	24.6	49.2	73.8	98.4	123.0	147.6	172.2	196.8	221.4
245	24.5	49.0	73.5	98.0	122.5	147.0	171.5	196.0	220.5
244	24.4	48.8	73.2	97.6	122.0	146.4	170.8	195.2	219.6
243	24.3	48.6	72.9	97.2	121.5	145.8	170.1	194.4	218.7
242	24.2	48.4	72.6	96.8	121.0	145.2	169.4	193.6	217.8
241	24.1	48.2	72.3	96.4	120.5	144.6	168.7	192.8	216.9
240	24.0	48.0	72.0	96.0	120.0	144.0	168.0	192.0	216.0
239	23.9	47.8	71.7	95.6	119.5	143.4	167.3	191.2	215.1
238	23.8	47.6	71.4	95.2	119.0	142.8	166.6	190.4	214.2
237	23.7	47.4	71.1 70.8	94.8 94.4	118.5	142.2	165.9	189.6	213.3 212.4
236	23.6 23.5	47.2	70.8	94.4	118.0 117.5	141.6 141.0	165.2 164.5	188.8 188.0	211.5
235	25.5	47.0							
234	23.4	46.8	70.2	93.6	117.0	140.4	163.8	187.2	210.6
233 232	23.3	46.6	69.9	93.2	116.5	139.8	163.1	186.4	209.7
232	23.2	46.4	69.6	92.8	116.0	139.2	162.4	185.6	208.8
231	23.1	46.2	69.3	92.4	115.5	138.6	161.7	184.8	207.9
230	23.0	46.0	69.0	92.0	115.0	138.0	161.0	184.0	207.0
229	22.9	45.8	68.7	91.6	114.5	137.4	160.3	183.2	206.1
228	22.8	45.6	68.4	91.2	114.0	136.8	159.6	182.4	205.2
227	22.7	45.4	68.1	90.8	113.5	136.2	158.9	181.6	204.3
226	22.6	45.2	67.8	90.4	113.0	135.6	158 2	180.8	203.4

		LOG.	ARI	THMS	OF N	UMB.	ero.			
190 L. 27	(8.]						(	[N	To. 214	L. 332
0	1	2	3	4	5	6	7	8	9	Diff.
278754	8982	9211	943	9 9667	9895				; 	
281033	1261	1488			2169	2396	2622	2849	3075	228 227
5557	5782	6007	623	2 6456	6681	6905	7130	7354	7578	226 225 223
				_						222
2256	2478	2699	292	0 2141	3363	3584	3804	4025	4246	221 220
6665 8853	6884 9071	7104 9289	732	3 7542	7761 9943	7979	8198	8416	8635	219
			-			0161	0378	0595	0813	218
3196	3412	3628	384	4 4059	4275	4491	4706	4921	5136	216 215
7496	7710	7924			8564	8778	8991	9204	9417	213
		0056 2177			0693 2812	0906 3023	1118	1330 3445	1542 3656	212 211
3867	4078	4289	449	9 4710	4920	5130	5340	5551	5760	210 209
8063	8272	8481			9106	9314	9522	9730	9938	208
320146	0354	0562			1184	1391	1598	1805	2012	207
4282	4488	4694	489	9 5105	5310	5516	5721	5926	6131	206 205 204
8380	8583	8787			9398	9601	9805		-	203
330414	0617	0819	102	2 1225	1427	1630	1832	2034	2236	202
				Proport	TONAL ]	Parts.				
. 1	2	3	3	4	5	6		7	8	9
22.5	45.0	67	.5	90.0	112.5		.0 1	57.5	180.0	202.5
22.3	44.6	66	.9	89.2	111.5	133	.8 1	56.1	179.2	201.6 200.7 199.8
22.1	44.2	66	.3	88.4	110.5	132	.6 15	54.7	176.8	198.9 198.9 198.0
21.9	43.8 43.6	65	.7	87.6 87.2	109.5 109.0	131.	.4 1	53.3	175.2 174.4	197.1
21.7	43.4	65	.1	86.8	108.5	130	.2 1	51.9	173.6	195.8 194.4
21.5	43.0	64	.5	86.0	107.5	129	.0 1	50.5	172.0	193.5
21.3	42.6	63	.9	85.2	106.5	127	8 14	49.1	170.4	192.6 191.7 190.8
21.1	42.2 42.0	63	.3	84.4 84.0	105.5 105.0	126.	.6 14	17.7	168.8 168.0	189.5
	278754 281033 3301 5557 7802 290035 4406 8853 301030 3196 9630 311754 4962 6336 8301 320146 2219 22.5 22.4 22.2 22.2 22.2 22.2 22.2 22.2	278754 8982 281033 1361 3301 3527 5557 5587 5587 7802 8026 290035 0257 4466 4687 6665 6865 9971 301030 1947 3196 3412 5351 5566 7496 770 6180 8903 8943 311754 1966 3867 4078 5970 6180 8903 827 320146 0354 2219 426 4282 438 6336 6541 8380 8583 330414 0617	190 L. 278.]   0	190 L. 278.]	190 L. 278.    0	190 L. 278.]	190 L. 278.	190 L. 278.]	190 L. 278.	190 L. 278.

41.4 41.2

211 210 21.0 42.0

209 20.9 41.8

208

207

206

205 20.5 44.0

204 20.4 40.8

203 20.3 40.6

202 20.2 40.4

20.8 20.7 20.6 41.6 63.0

62.7

62.4

62.1

61.8

€1.5

61.2

60.9

60.6

83.6

83.2

82.8

82.4

82.0

81.6

81.2 0.8

104.5

104.0

103.5

103.0 102.5 102.0

101.5

101.0

126.6 126.0

125.4

124.8

124.2

123.6

123.0

122.4 121.8

121.2

148.4 147.7 147.0

146.3

145.6

144.9

144.2

143.5

142.8

142.1

141.4

168.0 189.0

167.2 188.1 187.2 Ks 186.8 Kg

166 4

165.6

164.8

164.0

163.2

162.4

161.6

186.8 185.4 18 184.5 18 182.7 181.8

No. 215 L. 332.] [No. 239 L. 380.													
N.	0	1	2	8	4	5	6	7	8	9	Diff.		
215 6 7	332438 4454 6460	2640 4655 6660	2842 4856 6860	3044 5057 7060	3246 5257 7260	3447 5458 7459	3649 5658 7659	8850 5859 7858	4051 6059 8058	4258 6260 8257	202 201 200		
8 9 220	8456 340444 2423	8656 0642 2620	8855 0841 2817	9054 1039 3014	9253 1237 3212	9451 1435 3409	9650 1632 3606	9849 1830 3802	0047 2028 3999		199 198 197		
1 2 3	4392 6353 8305	4589 6549 8500	4785 6744 8694	4981 6989 8889	5178 7135 9083	5374 7330 9278	5570 7525 9472	5766 7720 9666	5962 7915 9860	6157 8110 - 0054	196 195 194		
4 5 6 7 8	350248 2183 4108 6026 7935	0442 2375 4301 6217 8125	0636 2568 4493 6408 8316	0829 2761 4685 6599 8506	1023 2954 4876 6790 8696	1216 3147 5068 6981 8886	1410 3839 5260 7172 9076	1603 3582 5452 7868 9266	1796 3724 5643 7554 9456		193 193 192 191 190		
230	9835 361728	0025 1917 3800	0215 2105 3988	0404 2294 4176	0593	0783 2671 4551	0972 2859 4739	1161 3048 4926	1350	1589 3424	189 188		
3 4	3612 5488 7856 9216	5675 7542 9401	5862 7729 9587	6049 7915 9772	6236	6423 8287 0143	6610 8473 0328	6796 8659 0513	5113 6983 8845 0698	7169 9030	188 187 186 185		
5 6 7 8 9	371068 2912 4748 6577	1253 3096 4932 6759	1437 3280 5115 6942	1622 3464 5298 7124	3647 5481 7306	1991 3831 5664 7488	2175 4015 5846 7670	2360 4198 6029 7852	2544 4382 6212 8034	2728 4565 6894 8216	184 184 183 182		
9	8398 <b>3</b> 8	8580	8761	8943	9124	9306	9487	9668	9849	0030	181		
	1 -	1		PR	OPORTIC	ONAL PA	ARTS.				1		
Diff	_	2		_	4	5	6	0 1	7	8	9 181.8		
202 201 200 199	20.2 20.1 20.0 19.9	40.4 40.2 40.0 39.8	60 60 59	.8	80.8 80.4 80.0 79.6	101.0 100.5 100.0 99.5	121 120 120 119	.6 1 .0 1	41.4   40.7   40.0   39.3	161.6 160.8 160.0 159.2	180.9 180.0 179.1		

Diff.	1	2	3	4	5	6	7	8	9
1									
202	20.2	40.4	60.6	80.8	101.0	121.2	141.4	161.6	181.8
201	20.1	40.2	60.3	80.4	100.5	120.6	140.7	160.8	180.9
200	20.0	40.0	60.0	80.0	100.0	120.0	140.0	160.0	180.0
199	19.9	39.8	59.7	79.6	99.5	119.4	139.3	159.2	179.1
198	19.8	39.6	59.4	79.2	99.0	118.8	138.6	158.4	178.2
197	19.7	39.4	59.1	78.8	98.5	118.2	137.9	157.6	177.3
196	19.6	39.2	58.8	78.4	98.0	117.6	137.2	156.8	176.4
195	19.5	39.0	58.5	78.0	97.5	117.0	136.5	156.0	175.5
194	19.4	38.8	58.2	77.6	97.0	116.4	135.8	155.2	174.6
193	19.3	38.6	57.9	77.2	96.5	115.8	135.1	154.4	173.7
192	19.2	38.4	57.6	76.8	96.0	115.2	134.4	153.6	172.8
191	19.1	38.2	57.3	76.4	95.5	114.6	133.7	152.8	171.9
190	19.0	38.0	57.0	76.0	95.0	114.0	133.0	152.0	171.0
189	18.9	37.8	56.7	75.6	94.5	113.4	132.3	151.2	170.1
188 187	18.8	37.6	56.4	75.2	94.0	112.8	131.6	150.4	169.2
187	18.7	37 4	56.1	74.8	93.5	112.2	130.9	149.6	168.3
186	18.6	37.2	55.8	74.4	93.0	111.6	130.2	148.8	167.4
185	18.5	37.0	55.5	74.0	92.5	111.0	129.5	148.0	166.5
184	18.4	36.8	55.2	73.6	92.0	110.4	128.8	147.2	165.6
183	18.3	36.6	54.9	73.2	91.5	109.8	128.1	146.4	164.7
182	18.2	36.4	54.6	72.8	91.0	109.2	127.4	145.6	163.8
181	18.1	36.2	54.3	72.4	90.5	108.6	126.7	144.8	162.9
180	18.0	36.0	54.0	72.0	90.0	108.0	126.0	144.0	162.0
179	17.9	35.8	53.7	71.6	89.5	107.4	125.3	143.2	161.1

No.	240 L. 38	0.]						1	[N	0. 269 ]	L. 431
N.	0	1	2	3	4	5	6	7	8	9	Diff.
240 1 2 3 4 5	380211 2017 3815 5606 7390 9166	0892 2197 3995 5785 7568 9343	0578 2377 4174 5964 7746 9520	0754 2557 4353 6142 7924 9698	0934 2737 4533 6321 8101 9875	1115 2917 4712 6499 8279	1296 3097 4891 6677 8456	1476 3277 5070 6856 8634	1656 3456 5249 7034 8811	1837 3636 5428 7212 8989	181 180 179 178 178
6 7 8 9 250	390935 2697 4452 6199 7940 9674	1112 2873 4627 6374 8114 9847	1288 3048 4802 6548 8287	1464 3224 4977 6722 8461	1641 3400 5152 6896 8634	0051 1817 3575 5326 7071 8808	0228 1993 3751 5501 7245 8981	0405 2169 3926 5676 7419 9154	0582 2345 4101 5850 7592 9328	0759 2521 4277 6025 7766 9501	177 176 176 175 174 173
2 3 4 5 6 7	401401 3121 4834 6540 8240 9933	1573 3292 5005 6710 8410	0020 1745 3464 5176 6881 8579	0192 1917 3635 5346 7051 8749	0365 2089 .3807 5517 7221 8918	0538 2261 3978 5688 7391 9087	0711 2488 4149 5858 7561 9257	0883 2605 4320 6029 7731 9426	1056 2777 4492 6199 7901 9595	1228 2949 4663 6370 8070 9764	173 172 171 171 170 169
8 9	411620 3300	0102 1788 3467	0271 1956 3635	0440 2124 3803	0609 2293 3970	0777 2461 4137	0946 2629 4305	1114 2796 4472	1283 2964 4639	1451 3132 4806	169 168 167
260 1 2 3	4973 6641 8301 9956	5140 6807 8467	5307 6973 8633	5474 7139 8798	5641 7306 8964	5808 7472 9129	5974 7638 9295	6141 7804 9460	6308 7970 9625	6474 8135 9791	167 166 165
4 5 6 7 8 9	421604 8246 4882 6511 8135 9752	0121 1768 3410 5045 6674 8297 9914	0286 1933 3574 5208 6836 8459	0451 2097 3737 5371 6999 8621	0616 2261 3901 5534 7161 8783	0781 2426 4065 5697 7324 8944	0945 2590 4228 5860 7486 9106	1110 2754 4392 6023 7648 9268	1275 2918 4555 6186 7811 9429	1439 3082 4718 6349 7978 9591	165 164 164 163 162 162
-	43	<u> </u>	0075	0236	0398	0559	0720	0881	1042	1203	161

### PROPORTIONAL PARTS.

1									
Diff.	1	8	3	4	5	6	7	8	9
178	17.8	35.6	53.4	71.2	89.0	106.8	124.6	142.4	160.2
177	17.7	85.4	53.1	70.8	88.5	106.2	123.9	141.6	159.3
176	17.6	35.2	52.8	70.4	88.0	105.6	123.2	140.8	158.4
175	17.5	35.0	52.5	70.0	87.5	105.0	122.5	140.0	157.5
174	17.4	34.8	52.2	69.6	87.0	104.4	121.8	139.2	156.6
173	17.3	34.6	51.9	69.2 68.8	86.5	103.8	121.1	138.4	155.7
172 171	17.2 17.1	34.4 34.2	51.6 51.3	68.4	86.0 85.5	103.2 102.6	120.4	137.6	154.8
170	17.0	34.2	51.0	68.0	85.0	102.0	119.7 119.0	136.8 136.0	153.9
1	1								153.0
169	16.9	33.8	50.7	67.6	84.5	101.4	118.3	135.2	152.1
168	16.8	33.6	50.4	67.2	84.0	100.8	117.6	134.4	151.2
167	16.7	33.4	50.1	66.8	83.5	100.2	116.9	133.6	150.3
166	16.6	33.2	49.8	66.4	83.0	99.6	116.2	132.8	149.4
165	16.5	83.0	49.5	66.0	82.5	99.0	115.5	132.0	148.5
164	16.4	32.8	49.2	65.6 65.2	82.0	98.4	114.8	131.2	147.6
163 162	16.3 16.2	32.6 32.4	48.9 48.5	64.8	81.5 81.0	97.8 97.2	114.1 113.4	130.4	146.7
181	16.2	32.2	48.3	64.4	80.5	96.6	112.7	129.6 128.8	145.8
101	10.1	02.2	40.0	04.4	00.0	90.01	112.7	125.8	144.9

No. 5	No. 270 L, 431.] • [No. 299 L, 476.												
N.	0	1	2	3	4	5	6	7	8	9	Diff.		
270 1 2 3 4 5	431364 2969 4569 6163 7751 9833	1525 3130 4729 6322 7909 9491	1685 3290 4888 6481 8067 9648	1846 3450 5048 6640 8226 9806	2007 3610 5207 6799 8384 9964	2167 3770 5367 6957 8542	2328 3930 5526 7116 8701	2488 4090 5685 7275 8859	2649 4249 5844 7433 9017	2809 4409 6004 7592 9175	161 160 159 159 158		
6 7 8 9	440909 2480 4045 5604	1066 2637 4201 5760	1224 2798 4357 5915	1381 2950 4513 6071	1538 3106 4669 6226	0122 1695 3263 4825 6382	0279 1852 3419 4981 6537	0437 2009 3576 5137 6692	0594 2166 3732 5293 6848	0752 2323 3889 5449 7003	158 157 157 156 155		
280 1 2 3 4 5 6 7 8	7158 8706 450249 1786 3318 4845	7313 8861 0403 1940 3471 4997	7468 9015 0557 2093 3624 5150	7623 9170 0711 2247 3777 5302	7778 9324 0865 2400 3930 5454 6973	7983 9478 1018 2553 4082 5606	8088 9633 1172 2706 4235 5758	8242 9787 1326 2859 4387 5910	8397 9941 1479 3012 4540 6062	0095 1633 3165 4692 6214 7781	155 154 154 158 158 158 152		
9 290	6366 7882 9392 460898 2398	6518 8033 9543 1048 2548	6670 8184 9694 1198 2697	6821 8336 9845 1348 2847	8487 9995 1499 2997	7125 8638 0146 1649 3146	5758 7276 8789 0296 1799 3296	7428 8940 0447 1948 8445	7579 9091 0597 2098 3594	9242 0748 2248 3744	152 151 151 150 150		
1 2 3 4 5	3893 5383 6868 8347 9822 471292	4042 5532 7016 8495 9969 1438	4191 5680 7164 8643 0116 1585	4340 5829 7312 8790 0263 1732	4490 5977 7460 8938 0410 1878	4639 6126 7608 9085 0557 2025	4788 6274 7756 9233 0704 2171	4936 6423 7904 9380 0851 2318	5085 6571 8052 9527 0998 2464	5234 6719 8200 9675 1145 2610	149 149 148 148 147 147		
6 7 8 9	2756 4216 5671	2903 4362 5816	3049 4508 5962	3195 465 <b>3</b> 6107	3341 4799 6252	3487 4944 6397	2171 3633 5090 6542	3779 5235 6687	3925 5381 6832	4071 5526 6976	146 146 145		
Diff	. 1	2	8		4	5	6		7	8	9		
161 160 159 158 157 156 155 154 153 152 151	16.1 16.0 15.9 15.8 15.7 15.6 15.5 15.4 15.3 15.2 15.1	32.2 32.0 31.8 31.6 31.4 31.2 31.0 30.8 30.6 30.4 30.2	48 48 47 47 47 46 46 46 45 45 45	.5 .9 .6 .3	64.4 64.0 63.6 63.2 62.8 62.4 62.0 61.6 61.2 60.8 60.4	80.5 80.0 79.5 79.0 78.5 78.0 77.5 77.0 76.5 76.0 75.5	96.6 96.0 95.4 94.8 94.8 93.6 93.6 91.8 91.8 90.6	1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	12.7 12.0 11.3 10.6 19.9 19.2 198.5 17.8 106.4 105.7	128.8 128.0 127.2 126.4 125.6 124.8 124.0 123.2 122.4 121.6 120.8	144.9 144.0 143.1 142.2 141.3 140.4 189.5 138.6 137.7 136.8 135.9		
150 149 148 147 146 145 144 143 142 141 140	15.0 14.9 14.8 14.7 14.6 14.5 14.4 14.3 14.2 14.1 14.0	30.0 29.8 29.6 29.4 29.2 29.0 28.8 28.6 28.4 28.2 28.0	45 44 44 43 43 43 42 42 42 42 42	.7 .4 .1 .8 .5 .2 .9 .6 .3	60.0 59.6 59.2 58.8 58.4 58.0 57.6 57.2 56.8 56.4 56.0	75.0 74.5 74.0 73.5 73.0 72.5 72.0 71.5 71.0 70.5 70.0	90.0 89.4 88.8 87.6 87.6 86.4 85.8 85.8 84.6 84.6	1 10 3 10 2 10 3 10 10 10 4 10 8 10	05.0 04.3 03.6 02.9 02.2 01.5 00.8 00.1 99.4 98.7	120.0 119.2 118.4 117.6 116.8 116.0 115.2 114.4 113.6 112.8 112.0	135.0 134.1 133.2 132.3 131.4 130.5 129.6 128.7 127.8 126.9 126.0		

No.	300 L. 47	7.]							[]	No. 339 1	531.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
300	477121 8566	7266 8711	7411 8855	7555 8999	7700 9143	7844 9287	7989 9431	8133 9575	8278 9719	8422 9863	145 144
2 3 4 5 6 7	480007 1443 2874 4300 5721	0151 1586 3016 4442 5863	0294 1729 3159 4585 6005	0438 1872 3302 4727 6147	0582 2016 3445 4869 6289	0725 2159 3587 5011 6430	0869 2302 3730 5153 6572	1012 2445 3872 5295 6714	1156 2588 4015 5437 6855	3 2731 5 4157 5579 6 6997	144 143 148 142 142
8 9	7138 8551 9958	7280 8692	7421 8833	7563 8974	7704 9114	7845 9255	7986 9396	8127 9537	8269 9677	9818	141 141
212		0099	0239	0380	0520	0661	0801	0941	1081		140
310 1 2 3 4 5 6	491362 2760 4155 5544 6930 8311 9687	1502 2900 4294 5683 7068 8448 9824	1642 3040 4433 5822 7206 8586 9962	1782 3179 4572 5960 7344 8724	1922 3319 4711 6099 7483 8862	2062 3458 4850 6238 7621 8999	2201 3597 4989 6376 7759 9137	2341 3737 5128 6515 7897 9275	248: 3876 526: 665: 803: 941:	3 4015 7 5406 8 6791 5 8173	140 139 139 139 138 138
7 8 9	501059 2427 3791	1196 2564 3927	1333 2700 4063	0099 1470 2837 4199	0236 1607 2973 4335	0374 1744 3109 4471	0511 1880 3246 4607	0648 2017 3382 4743	078 215 3518 4878	4   2291 8   3655	137 137 136 136
320 1 2 3	5150 6505 7856 9203	5286 6640 7991 9337	5421 6776 8126 9471	5557 6911 8260 9606	5693 7046 8395 9740	5828 7181 8530 9874	5964 7316 8664	6099 7451 8799	623 758 893	6 7721 4 9068	136 135 135
4 5 6 7 8 9	510545 1883 3218 4548 5874 7196	0679 2017 3351 4681 6006 7328	0813 2151 3484 4813 6139 7460	0947 2284 3617 4946 6271 7592	1081 2418 3750 5079 6403 7724	1215 2551 3883 5211 6535 7855	0009 1349 2684 4016 5344 6668 7987	0143 1482 2818 4149 5476 6800 8119	027 161 295 428 560 693 825	6   1750 1   3084 2   4415 9   5741 2   7064	134 134 138 138 138 138 138
330	8514 9828	8646 9959	8777	8909	9040	9171	9303	9434	956	6 9697	131
2 3 4 5 6 7 8	521138 2444 3746 5045 6339 7630 8917	1269 2575 3876 5174 6469 7759 9045	0090 1400 2705 4006 5304 6598 7888 9174	0221 1530 2835 4136 5434 6727 8016 9302	0353 1661 2966 4266 5563 6856 8145 9430	0484 1792 3096 4396 5693 6985 8274 9559	0615 1922 3226 4526 5822 7114 8402 9687	0745 2053 3856 4656 5951 7243 8531 9815	087 218 348 478 608 737 866 994	3 2314 3616 5 4915 6210 7501 8788	131 130 130 130 129 129 129
9	530200	0328	0456	0584	0712	0840	0968	1096	122	- 0072 3 1351	128 128
				PRO	PORTIC	NAL PA	RTS.				
Diff	f. 1	2		3	4	5	6		7	8	9
139 138	13.9 13.8	27.8 27.6		.7	55.6 55.2	69.5 69.0	83. 82.	4 9	7.3 6. <b>6</b>	111.2 110.4	125 124

Diff.	1	2	3	4	5	6	7	8	9
139	13.9	27.8	41.7	55.6	69.5	83.4	97.3	111.2	125.
138	13.8	27.6	41.4	55.2	69.0	82.8	96.6	110.4	124.
137	13.7	27.4	41.1	54.8	68.5	82.2	95.9	109.6	123.
136	13.6	27.2	40.8	54.4	68.0	81.6	95.2	108.8	122.
135	13.5	27.0	40.5	54.0	67.5	81.0	94.5	108.0	121
134	13.4	26.8	40.2	53.6	67.0	80.4	93.8	107.2	120.
133	13.3	26.6	39.9	53.2	66.5	79.8	93.1	106.4	119.
132	13.2	26.4	39.6	52.8	66.0	79.2	92.4	105.6	118.
131	13.1	26.2	89.3	52.4	65.5	78.6	91.7	104.8	117.
130	13.0	26.0	39.0	52.0	65.0	78.0	91.0	104.0	117.
129	12.9	25.8	38.7	51.6	64.5	77.4	90.3	103.2	116.
128	12.8	25.6	38.4	51.2	64.0	76.8	89.6	102.4	115.
127	12 7	25.4	38.1	50.8	63.5	76.2	88.9	101.6	114.

No.	340 L. 53	1.]							[N	o. 379	L. 579.
N.	0	1	2	8	4	5	6	7	8	9	Diff.
340 1 2 3 4 5 6	581479 2754 4026 5294 6558 7819 9076	1607 2882 4153 5421 6685 7945 9202	1734 3009 4280 5547 6811 8071 9327	1862 3136 4407 5674 6937 8197 9452	1990 3264 4534 5800 7063 8322 9578	2117 3891 4661 5927 7189 8448 9708	2245 3518 4787 6053 7315 8574 9829	2372 3645 4914 6180 7441 8699 9954	2500 3772 5041 6306 7567 8825	2627 3899 5167 6432 7693 8951	128 127 127 126 126 126
7 8 9	540329 1579 2825	0455 1704 2950	0580 1829 3074	0705 1953 3199	0830 2078 3323	0955 2208 3447	1080 2327 3571	1205 2452 3696	0079 1330 2576 3820	0204 1454 2701 3944	125 125 125 124
350 1 2 3 4	4068 5307 6543 7775 9003	4192 5481 6666 7898 9126	4316 5555 6789 8021 9249	4440 5678 6913 8144 9371	4564 5802 7036 8267 9494	4688 5925 7159 8389 9616	4812 6049 7282 8512 9789	4936 6172 7405 8635 9861	5060 6296 7529 8758 9984	5183 6419 7652 8881	124 124 123 123
5 6 7 8 9	550228 1450 2668 3883 5094	0351 1572 2790 4004 5215	0473 1694 2911 4126 5336	0595 1816 3033 4247 5457	0717 1938 3155 4368 5578	0840 2060 3276 4489 5699	0962 2181 3398 4610 5820	1084 2303 3519 4731 5940	1206 2425 3640 4852 6061	0106 1328 2547 3762 4973 6182	123 122 122 121 121 121 121
360 1 2 3	6303 7507 8709 9907	6423 7627 8829	6544 7748 8948	6664 7868 9068	6785 7988 9188	6905 8108 9308	7026 8228 9428	7146 8349 9548	7267 8469 9667	7387 8589 9787	120 120 120 120
4 5 6 7 8 9	561101 2293 3481 4666 5848 7026	0026 1221 2412 3600 4784 5966 7144	0146 1340 2531 3718 4903 6084 7262	0265 1459 2650 3837 5021 6202 7379	0385 1578 2769 3955 5139 6320 7497	0504 1698 2887 4074 5257 6437 7614	0624 1817 3006 4192 5376 6555 7732	0743 1936 3125 4311 5494 6673 7849	0868 2055 3244 4429 5612 6791 7967	0982 2174 3362 4548 5730 6909 8084	119 119 119 119 118 118 118
370	8202 9374	8319 9491	8436 9608	8554 9725	8671 9842	8788 9959	8905	9023 0193	0309	0426	117
2 3 4 5 6 7 8 9	570543 1709 2872 4031 5188 6341 7492 8639	0660 1825 2988 4147 5303 6457 7607 8754	0776 1942 3104 4263 5419 6572 7722 8868	0893 2058 3220 4379 5534 6687 7836 8983	1010 2174 3336 4494 5650 6802 7951 9097	1126 2291 3452 4610 5765 6917 8066 9212	1243 2407 3568 4726 5880 7032 8181 9326	1359 2523 3684 4841 5996 7147 8295 9441	1476 2639 3800 4957 6111 7262 8410 9555	1592 2755 3915 5072 6226 7377 8525 9669	117 116 116 116 115 115 115 114
	1	1	-	Pro	PORTIC	ONAL PA	ARTS.			'	
Diff	f. 1	2	;	3	4	5	6		7	8	9
128 127 126 125 124 123 122 121 120 119	12.1	25.6 25.4 25.2 25.0 24.8 24.6 24.4 24.2 24.0 23.8	38 37 37 37 36 36 36 36	.8 .5 .9 .6	51.2 50.8 50.4 50.0 49.6 49.2 48.8 48.4 48.0 47.6	64.0 63.5 63.0 62.5 62.0 61.5 61.0 60.5 60.0 59.5	76. 76. 75. 75. 74. 73. 73. 72. 72. 71.	2   8 6   8 0   8 4   8 8   8 8   8 8   8 8   8	9.6 8.9 8.2 7.5 8.8 8.1 6.4 1.7	102.4 101.6 100.8 100.0 99.2 98.4 97.6 96.8 96.0 95.2	115.2 114.3 113.4 112.5 111.6 110.7 109.8 108.9 108.0 107.1

	No. 380. L. 579.] [No. 414 L. 617.]													
N.	0	1	2	3	4	5	6	7	8	9	Diff.			
380	579784	9898	0012	0126	0241	0355	0469	0583	0697	0811	114			
1	580925	1039	1153	1267	1381	1495	1608	1722 2858	1836	1950				
2	2063	2177	2291	2404	2518	2631	2745	2858	2972	3085				
3	3199	3312	3426	3539	3652	3765	3879	3992 5122	4105 5235	4218	440			
4	4331	4444	4557 5686	4670 5799	4783 5912	4896 6024	5009 6137	6250	6362	5348 6475	113			
9	5461 6587	5574 6700	6812	6925	7037	7149	7262	7374	7486	7599				
0	7711	7823	7935	8047	8160	8272	8384	8496	8608	8720	112			
8	8832	8944	9056	9167	9279	9391	9503	9615	9726	9838	112			
5 6 7 8 9	9950	0011	5000	0101	5210	0001								
		0061	0173	0284	0396	0507	0619	0730	0842	0953.				
390	591065	1176	1287	1399	1510	1621	1732	1843	1955	2066				
1	2177	2288	2399	2510	2621	1621 2732	2843	2954	3064	3175	111			
2	3286	3397	3508	3618	3729	3840	3950	4061	4171	4282				
3	4393	4503	4614	4724	4834	4945	5055	5165	5276	5386				
4	5496	5606	5717	5827	5937	6047	6157	6267	6377	6487	110			
5	6597	6707	6817	6927	7037	7146	7256	7366	7476	7586	110			
6	7695	7805	7914	8024	8134	8243	8353	8462	8572	8681				
2 3 4 5 6 7 8	8791	8900	9009	9119	9228	9337	9446	9556	9665	9774	1			
8	9883	9992	0101	0210	0319	0428	0537	0646	0755	0864	109			
9	600973	1082	0101 1191	1299	1408	1517	1625	1734	1843	1951	1			
400	2060	2169	2277	2386	2494	2603	2711	2819	2928	3036				
1	3144	3253	3361	3469	3577	3686	3794	3902	4010	4118	108			
2	4226	4334	4442	4550	4658	4766	4874 5951	4982 6059	5089	5197				
3	5305 6381	5413 6489	5521 6596	5628 6704	5736 6811	5844 6919	7026	7133	6166 7241	6274 7348				
4 5	7455	7562	7669	7777	7884	7991	8098	8205	8312	8419				
6	8526	8633	8740	8847	8954	9061	9167	9274	9381	9488	107			
1 2 3 4 5 6	9594	9701	9808	9914	0001	0001	0101	0.012	0001	0100				
	0001	0101	0000		0021	0128	0234	0341	0447	0554				
8 9	610660	0767	0873	0979	1086	1192	1298	1405	1511	1617				
9	1723	1829	1936	2042	2148	2254	2360	2466	2572	2678	106			
410	2784	2890	2996	3102	3207	3313	3419	-3525	3630	3736	100			
1	3842	3947	4053	4159	4264	4370	4475	4581	4686	4792				
2	4897	5003	5108	5213	5319	5424	5529	5634	5740	5845				
3	5950	6055	6160	6265	6370	6476	6581 7629	6686	6790	6895	105			
4	7000	7105	7210	7315	7420	7525	7629	7734	7839	7943				

### PROPORTIONAL PARTS.

Diff.	1	2	3	4	5	6	7	8	9
118	11.8	23.6	35.4	47.2	59.0	70.8	82.6	94.4	106.2
117	11.7	23.4	35.1	46.8	58.5	70.2	81.9	93.6	105.3
116	11.6	23.2	34.8	46.4	58.0	69.6	81.2	92.8	104.4
115	11.5	23.0	34.5	46.0	57.5	69.0	80.5	92.0	103.5
114	11.4	22.8	34.2	45.6	57.0	68.4	79.8	91.2	102.6
113	11.3	22.6	33.9	45.2	56.5	67.8	79.1	90.4	101.7
112	11.2	22.4	88.6	44.8	56.0	67.2	78.4	89.6	100.8
111	11.1	22.2	33.3	44.4	55.5	66.6	77.7	88.8	99.9
110	11.0	22.0	33.0	44.0	55.0	66.0	77.0	88.0	99.0
109	10.9	21.8	32.7	43.6	54.5	65.4	76.3	87.2	98.1
108	10.8	21.6	32.4	43.2	54.0	64.8	75.6	86.4	97.2
107	10.7	21.4	32.1	42.8	53.5	64.2	74.9	85.6	96.3
106	10.6	21.2	31.8	42.4	53.0	63.6	74.2	84.8	95.4
105	10.5	21.0	31.5	42.0	52.5	63.0	73.5	84.0	94.5
105	10.5	21.0	31.5	42.0	52.5	63.0	73.5	84.0	94.5
104	10.4	20.8	31.2	41.6	52.0	62.4	72.8	83.2	93.6

No.	No. 415 L. 618.] [No. 459 L. 662]  N. 0 1 2 3 4 5 6 7 8 9 Diff.													
N.	0	1	2	3	4	5	6	7	8	9	Diff.			
415	618048 9093	8153 9198	8257 9302	8362 9406	8466 9511	8571 9615	8676 9719	8780 9824	8884 9928	8989	105			
7 8 9	620136 1176 2214	0240 1280 2318	0344 1384 2421	0448 1488 2525	0552 1592 2628	0656 1695 2732	0760 1799 2835	0864 1903 2939	0968 2007 3042	0032 1072 2110 3146	104			
420 1 2 3 4 5 6	3249 4282 5312 6340 7366	3353 4385 5415 6443 7468	3456 4488 5518 6546 7571	3559 4591 5621 6648 7673	3663 4695 5724 6751 7775 8797	3766 4798 5827 6853 7878	3869 4901 5929 6956 7980	3973 5004 6032 7058 8082	4076 5107 6135 7161 8185	4179 5210 6238 7263 8287	103			
5 6	8389 9410	8491 9512	8593 9613	8695 9715	8797 9817	7878 8900 9919	9002	9104	9206	9308	102			
7 8 9	630428 1444 2457	0530 1545 2559	0631 1647 2660	0733 1748 2761	0835 1849 2862	0936 1951 2963	0021 1038 2052 3064	0123 1139 2153 3165	0224 1241 2255 3266	0326 1342 2356 3367				
430 1 2 3 4	3468 4477 5484 6488 7490	3569 4578 5584 6588 7590	3670 4679 5685 6688 7690	3771 4779 5785 6789 7790	3872 4880 5886 6889 7890	3973 4981 5986 6989 7990	4074 5081 6087 7089 8090	4175 5182 6187 7189 8190	4276 5283 6287 7290 8290	4376 5383 6388 7390 8389	101			
5 6	8489 9486	8589 9586	8689 9686	7790 8789 9785	8888 9885	8988 9984	9088	9188	9287	9387	100			
7 8 9	640481 1474 2465	0581 1573 2563	0680 1672 2662	0779 1771 2761	0879 1871 2860	0978 1970 2959	1077 2069 3058	0183 1177 2168 3156	0283 1276 2267 3255	0382 1375 2366 3354	99			
440 1 2 3 4 5 6	3453 4439 5422 6404 7383 8360 9335	3551 4537 5521 6502 7481 8458 9432	3650 4636 5619 6600 7579 8555 9530	3749 4734 5717 6698 7676 8653 9627	3847 4832 5815 6796 7774 8750 9724	3946 4931 5913 6894 7872 8848 9821	4044 5029 6011 6992 7969 8945 9919	4143 5127 6110 7089 8067 9043	4242 5226 6208 7187 8165 9140	4340 5324 6306 7285 8262 9237	98			
7 8 9	650308 1278 2246	0405 1375 2343	0502 1472 2440	0599 1569 2536	0696 1666 2633	0793 1762 2730	0890 1859 2826	0016 0987 1956 2923	0113 1084 2053 3019	0210 1181 2150 3116	97			
450 1 2 3 4 5 6	3213 4177 5138 6098 7056 8011 8965	3309 4273 5235 6194 7152 8107 9060	3405 4369 5331 6290 7247 8202 9155	3502 4465 5427 6386 7343 8298 9250	3598 4562 5523 6482 7438 8393 9346	3695 4658 5619 6577 7534 8488 9441	3791 4754 5715 6673 7629 8584 9536	3888 4850 5810 6769 7725 8679 9631	3984 4946 5906 6864 7820 8774 9726	4080 5042 6002 6960 7916 8870 9821	96			
8 9	9916 660865 1813	0011 0960 1907	0106 1055 2002	0201 1150 2096	0296 1245 2191	0391 1339 2286	0486 1434 2380	0581 1529 2475	0676 1623 2569	0771 1718 2663	95			
-				1	PORTIO		1	1						
Diff	_	2		3	4	5	6		7	.8	9			
105 104 108 102 101 100 99	10.5 10.4 10.3 10.2 10.1 10.0 9.9	21.0 20.8 20.6 20.4 20.2 20.0 19.8	31 30 30 30 30 29	.6	42.0 41.6 41.2 40.8 40.4 40.0 39.6	52.5 52.0 51.5 51.0 50.5 50.0 49.5	63.6 62.4 61.8 61.8 60.6 60.6 59.4	70	3.5 2.8 2.1 1.4 0.7 0.0 0.3	84.0 83.2 82.4 81.6 80.8 80.0 79.2	94.5 93.6 92.7 91.8 90.9 90.0 89.1			

No.	460 L. 6	62.]								[	No. 499	L. 698
N	0	1	2	8	4		5	6	7	8	9	Diff
460	662758	2852	2947	3041	3135	5	3230	3324	3418	3512	3607	
1	3701	3795	3889	3983	4078	3	4172	4266	4360	4454	4548	
2	4642	4736 5675	4830	4924	5018	3	4172 5112	4266 5206	5299	5393	5487	94
1 2 3 4 5 6 7	5581	5675	5769	5862	5956	3	6050	6143	6237	6331	6424	94
4	6518	6612	6705	6799 7733	6892	3	6986	7079	7173	7266	7360	
9	7453	7546	7640	7733	7826 8759	3	7920	8013	8106	7266 8199	8293	
6	8386	8479	8572	8665	8759	)	8852	8945	9038	9131	9224	
4	9317	9410	9503	9596	9689	)	9782	9875	9967		_	
8	670246	0000	0.404	0001	-	-11		-	-	- 0060	0153 1080	98
9	1173	0339 1265	0431	0524	0617		0710	0802	0895	0988	1080	
-	1		1358	1451	1543	Ш	1636	1728	1821	1913	2005	
470	2098	2190	2283	2375	2467	· 11	2560	2652	2744	9836	9000	
1	3021	3113	3205	3297	3390		3482	2652 3574	3666	2836 3758	2929 3850 4769	
2	3942	4034	4126	4218	4310	T	4402	4494	4586	4677	4760	92
3	4861	4953	5045	5137	5228	Ш	5320	5412	5503	4677 5595	5687	32
4	5778 6694	5870 6785	5962	6053	6145	Ш	5320 6236	6328 7242	6419	6511	6602	
5	6694	6785	6876	6968 7881	7059	H	7151	7242	7333	7424	7516	
1 2 3 4 5 6 7	7607	7698	5962 6876 7789	7881	7972	11	8063	8154	8245	8336	7516 8427	
8	8518	8609	8700	8791	8882	H	8973	9064	9155	9246	9337	91
8	9428	9519	9610	9700	9791	H	9882	9973				-
9	680336	0426	0517	0607	0698	-  -	0789	0879	0063	0154 1060	0245 1151	
480	1241	1332	1422	1513		Ш			1		1	
1	2145	1332 2235	2326	2416	1603 2506	Ш	1693	1784 2686	1874	1964	2055	1
2	3047	3137	3227	3317	3407	П	2596	2686	2777	2867	2957	
2 3 4 5 6 7 8 9	3047 3947	4037	4127	4217	4307	Н	3497 4396	3587	3677	3767	3857	90
4	4845	4935	5025	5114	5204	Î	5294	4486 5383	4576	4666	4756	i
5	5742	5831	5921	6010	6100		6189	6279	5473 6368	5563 6458	5652	1
6	6636 7529	6726	6815	6904	6994	7	7083	7172	7261	7351	6547	
7	7529	7618	7707	7796	.7886		7975	8064	8153	8242	7440 8331	
8	8420	8509	8598	8687	8776	11	8865	8953	9042	9131	9220	89
9	9309	9398	9486	9575	9664	H	9753	9841	9930	9191	3220	
100	202100					-  -				0019	0107	
190	690196	0285	0373 1258 2142	0462	$0550 \\ 1435$	1	0639	0728	0816	0905	.0993	
1 2 3 4 5 6 7 8 9	1081 1965	1170 2053	1258	1347	1435		1524	1612	1700 2583	1789	1877 2759	
2	2847	2003	2142	2230	2318 3199	il.	2406	2494	2583	2671	2759	
4	3727	3815	3023 3903	3111	3199	11 -	3287	3375	3463	3551	3639	88
7	4605	4609	4731	3991	4078	11 -	4166	4254	4342	4430	4517	
6	5482	4693 5569	5657	4868	4956	11 :	5044	5131	5219	5307	5394	
7	6356	6444	6531	5744 6618	4956 5832 6706	113	5919	6007	6094	6182	6269	
8	7229	7317	7404	7491	7578		6793	6880	6968	7055	7142	
9	8100	8188	8275	8362	8449		7665 8535	7752 8622	7839 8709	7926 8796	8014 8883	87
!				Prop	ORTIO	NA	L PA		1		0000	_
Diff.	111		I .	1	. 1	_			1	1		
III.	1	2	3		4		5	6	7		8	9

5 6 7 8 9	3727 4605 5482 6356 7229 8100	3815 4693 5569 6444 7317 8188	4731   5657   6531   7404   78275   8	$     \begin{array}{c cccc}       4868 & 4 \\       5744 & 5 \\       6618 & 6 \\       7491 & 7      \end{array} $	1078 1956 1832 1706 1578 1449	4166 5044 5919 6793 7665 8535	4254 5131 6007 6880 7752 8622	4342 5219 6094 6968 7839 8709	4430 5307 6182 7055 7926 8796	4517 5394 6269 7142 8014 8883	87
98 97 96 95 94 93 92 91 90 89 88 87 86	9.8 9.7 9.6 9.5 9.4 9.3 9.2 9.1 9.0 8.9 8.8 8.7 8.6	19.6 19.4 19.2 19.0 18.8 18.6 18.4 18.2 18.0 17.8 17.6 17.4	29.4 29.1 28.8 28.5 28.2 27.9 27.6 27.3 27.0 26.7 26.1 25.8	39 38 38 37 36 36 36 35 34.8 34.4	844000000000000000000000000000000000000	5 49.0 48.5 48.0 47.0 46.5 46.0 45.5 44.0 43.5 44.0	58.8 58.2 57.6 57.0 56.4 55.8 55.2 54.0 53.4 52.2 51.6	68. 67. 66. 65. 65. 63. 63. 63. 63. 60. 60.	6 9 9 2 5 8 1 1 4 4 7 7 7 7 9 8 8 9 9 9 9 9 9 9 9 9 9 9 9 9	8 78.4 77.6 76.8 76.0 75.2 73.6 72.8 72.0 71.2 70.4 79.6 38.8	88.2 87.3 86.4 85.5 84.6 83.7 82.8 81.9 81.0 79.2 78.3 77.4

No. 500 L. 698.] [No. 544 L. 736.]													
N.	0	1	2	8	4	5	6	7	8	9	Diff.		
500	698970 9838	9057 9924	9144	9231	9317	9404	9491	9578	9664	9751			
23456789	700704 1568 2431 3291 4151 5008 5864 6718	0790 1654 2517 3377 4236 5094 5949 6803	0011 0877 1741 2603 3463 4322 5179 6035 6888	0098 0963 1827 2689 3549 4408 5265 6120 6974	0184 1050 1913 2775 3635 4494 5350 6266 7059	0271 1136 1999 2861 3721 4579 5436 6291 7144	0358 1222 2086 2947 3807 4665 5522 6376 7229	0444 1309 2172 3033 3893 4751 5607 6462 7315	0531 1395 2258 3119 3979 4837 5693 6547 7400	0617 1482 2344 3205 4065 4922 5778 6632 7485	86		
510 1 2	7570 8421 9270	7655 8506 9355	7740 8591 9440	7826 8676 9524	7911 8761 9609	7996 8846 9694	8081 8931 9779	8166 9015 9863	8251 9100 9948	8336 9185	85		
3 4 5 6 7 8 9	710117 0963 1807 2650 3491 4330 5167 6003	0202 1048 1892 2734 3575 4414 5251 6087	0287 1132 1976 2818 3659 4497 5335 6170	0371 1217 2060 2902 3742 4581 5418 6254	0456 1301 2144 2986 3826 4665 5502 6337	0540 1385 2229 3070 3910 4749 5586 6421	0625 1470 2313 3154 3994 4833 5669 6504	0710 1554 2397 3238 4078 4916 5753 6588	0794 1639 2481 3323 4162 5000 5836 6671	0033 0879 1723 2566 3407 4246 5084 5920 6754	84		
1 2 3 4	6838 7671 8502 9331	6921 7754 8585 9414	7004 7837 8668 9497	7088 7920 8751 9580	7171 8003 8834 9663	7254 8086 8917 9745	7338 8169 9000 9828	7421 8253 9083 9911	7504 8336 9165 9994	7587 8419 9248	83		
5 6 7 8 9	720159 0986 1811 2634 3456	0242 1068 1893 2716 3538	0325 1151 1975 2798 3620	0407 1233 2058 2881 3702	0490 1316 2140 2963 3784	0573 1398 2222 3045 3866	0655 1481 2305 3127 3948	0738 1563 2387 3209 4030	0821 1646 2469 3291 4112	0077 0903 1728 2552 3374 4194	82		
530 1 2 3 4 5 6 7	4276 5095 5912 6727 7541 8354 9165 9974	4358 5176 5993 6809 7623 8435 9246	4440 5258 6075 6890 7704 8516 9327	4522 5340 6156 6972 7785 8597 9408	4604 5422 6238 7053 7866 8678 9489	4685 5503 6320 7134 7948 8759 9570	4767 5585 6401 7216 8029 8841 9651	4849 5667 6483 7297 8110 8922 9732	4931 5748 6564 7379 8191 9003 9813	5013 5830 6646 7460 8273 9084 9893	81		
8 9 540 1 2	730782 1589 2394 3197 3999	0055 0863 1669 2474 3278 4079	0136 0944 1750 2555 3358 4160	0217 1024 1830 2635 3438 4240	0298 1105 1911 2715 3518 4320	0378 1186 1991 2796 3598 4400	0459 1266 2072 2876 3679 4480	0540 1347 2152 2956 3759 4560	0621 1428 2233 3037 3839 4640	0702 1508 2313 3117 3919 4720	00		
2 3 4	4800 5599	4880 5679	4960 5759	5040 5838	5120 5918	5200 5998	5279 6078	5359 6157	5439 6237	5519 6317	80		
				Pro	PORTIC	NAL PA	ARTS.						
Diff	. 1	2	8		4	5	6		7	8	9		
87 86 85 84	8.7 8.6 8.5 8.4	17.4 17.2 17.0 16.8	26 25 25 25 25	.8	34.8 34.4 34.0 33.6	43.5 43.0 42.5 42.0	51.6 6 51.0 5		).9 ).2 ).5 3.8	69.6 68.8 68.0 67.2	78.3 77.4 76.5 75.6		

N.	0	1	2	8	4	5	6	7	8	9	Diff.
545	736397	6476	6556	6635	6715	6795	6874	6954	7034	7113	
6	7193	7272	7352	7431	7511	7590	7670	7749	7829	7908	
7	7987	8067	8146	8225	8305	8384	8463	8543	8622	8701	
8	8781	8860	8939	9018	9097	9177	9256	9335	9414	9493	
9	9572	9651	9731	9810	9889	9968					
							0047	0126	0205	0284	79
550	740363	0442	0521	0600	0678	0757	0836	0915	0994	1073	
1	1152	1230	1309	1388	1467	1546	1624	1703	0994 1782	1860	
2	1939	2018	1309 2096	1388 2175	1467 2254	2332	2411	2489	2568	2647	
3	2725	2804	2882	2961	2020	3118	3196	3275	3353	3431	
3 4	3510	3588	3667	3745	3823 4606 5387	3902	3980	4058	4136	4215	
5	4293	4371	4449	4528 5309	4606	4684	4762	4840	4919	4997	1
6	5075	5153	5231	5309	5387	5465	5543	5621	5699	5777	78
7	5855	5933	6011	6089	6167	6245	6323	6401	6479	6556	
8	6634	6712	6790	6868	6945	7023	7101 7878	7179	7256	7334	
9	7412	7489	7567	7645	7722	7800		7955	8033	8110	
560	8188	8266	8343	8421	8498	8576	8653	8731	8808	8885	
1	8963	9040	9118	9195	9272	9350	9427	9504	9582	9659	
2	9736	9814	9891	9968							
					0045	0123	0200	0277	0354	0431	
3	750508	0586	0663	0740	0817 1587	0894	0971 1741	1048	1125 1895	1202	
4	1279	1356	1433	1510 2279	1587	1664	1741	1818	1895	1972	7
5 6 7 8	2048	2125	2202	2279	2356	2433	2509	2586	2663	2740	
6	2816 3583	2893	2970	3047	3123 3889	3200	3277	3353	3430	3506 4272	
7	4348	3660 4425	3736 4501	3813 4578	4654	3966 4730	4042 4807	4119 4883	4195 4960	5036	
ိ	5112	5189	5265	5341	5417	5494	5570	5646	5722	5799	
	1										
570	5875	5951	6027	6103	6180	6256	6332	6408	6484	6560	-
1	6636	6712	6788	6864	6940	7016 7775	1092	7168	7244	7320	70
2	7396 8155	7472 8230	7548	7624 8382	7700 8458	0770	7092 7851 8609	7927 8685	8003	8079	1
4	8100	8988	8306 9063	9139	9214	8533 9290	9366	9441	8761 9517	8836 9592	
5	9668	9743	9819	9894	9970	9290	9300	3441	9517	9392	
9	3000	9749	9019	9094	9910	0045	0121	0196	0272	0347	
6	760422	0498	0573	0649	0724	0799	0121 0875 1627 2378	0950	1025	1101	
6	1176	1251	1326	1402	1477	1552	1627	1702	1025 1778	1853	
8	1928	2003	2078	2153	2228	2303	2378	2453	2529	2604	77
9	2679	2754	2829	2904	2978	3053	3128	3203	3278	3353	1 70
580	3428	3503	3578	3653	3727	3802	3877	3952	4027	4101	
1	4176	4251	4326	4400	4475	4550	4694	4699	4774	4848	
	4923	4998	5072	5147	5221	4550 5296	4624 5370	4699 5445	5520	5594	
3 4	5669	5743	5072 5818	5892	5221 5966	6041	6115	6190	6264	6338	
4	6413	6487	6562	6636	6710	6785	6859	6933	7007	7082	

Diff.	1	2	3	4	5	6	7	8	9
83	8.3	16.6	24.9	33.2 32.8	41.5 41.0	49.8 49.2	58.1 57.4	66.4 65.6	74.7 73.8
82 81	8.2 8.1 8.0	16.4 16.2 16.0	24.6 24.3 24.0	32.4 32.0	40.5 40.0	48.6 48.0	56.7 56.0	64.8 64.0	72.9
79	7.9 7.8 7.7	15.8 15.6	23.7 23.4	31.6 31.2	39.5 39.0	47.4 46.8	55.3 54.6	63.2 62.4	72.0 71.1 70.2
83 82 81 80 79 78 77 76	7.7	15.4 15.2	23.1	30.8	38.5 38.0	46.2 45.6	53.9 53.2	61.6	69.3
75 74	7.5 7.4	15.0 14.8	22.5	30.0 29.6	37.5 37.0	45.0 44.4	52.5 51.8	60.0 59.2	67.5

No. 585 L. 767.]         [No. 629 L. 799.]           N.         0         1         2         3         4         5         6         7         8         9         Diff.													
N.	0	1	2	3	4	5	6	7	8	9	Diff.		
585 6 7 8	767156 7898 8638 9377	7230 7972 8712 9451	7304 8046 8786 9525	7379 8120 8860 9599	7453 8194 8934 9673	7527 8268 9008 9746	7601 8342 9082 9820	7675 8416 9156 9894	7749 8490 9230 9968	7823 8564 9303	74		
9	770115	0189	0263	0336	0410	0484	0557	0631	0705	0042 0778			
590 1 2 3 4 5 6 7 8	0852 1587 2322 3055 3786 4517 5246 5974 6701 7427	0926 1661 2395 3128 3860 4590 5319 6047 6774 7499	0999 1734 2468 3201 3933 4663 5392 6120 6846 7572	1073 1808 2542 3274 4006 4736 5465 6193 6919 7644	1146 1881 2615 3348 4079 4809 5538 6265 6992 7717	1220 1955 2688 3421 4152 4882 5610 6338 7064 7789	1293 2028 2762 3494 4225 4955 5683 6411 7137 7862	1367 2102 2835 3567 4298 5028 5756 6483 7209 7934	1440 2175 2908 3640 4371 5100 5829 6556 7282 8006	1514 2248 2981 3713 4444 5173 5902 6629 7354 8079	73		
600 1 2	8151 8874 9596	8224 8947 9669	8296 9019 9741	8368 9091 9813	8441 9163 9885	8513 9236 9957	8585 9308	8658 9380	8730 9452	8802 9524			
3 4 5 6 7 8 9	780317 1037 1755 2473 3189 3904 4617	0389 1109 1827 2544 3260 3975 4689	0461 1181 1899 2616 3332 4046 4760	0533 1253 1971 2688 3403 4118 4831	0605 1324 2042 2759 3475 4189 4902	0677 1396 2114 2831 3546 4261 4974	0029 0749 1468 2186 2902 3618 4332 5045	0101 0821 1540 2258 2974 3689 4403 5116	0173 0893 1612 2329 3046 3761 4475 5187	9245 0965 1684 2401 3117 3832 4546 5259	72		
610 1 2 3 4 5	5330 6041 6751 7460 8168 8875 9581	5401 6112 6822 7531 8239 8946 9651	5472 6183 6893 7602 8310 9016 9722	5543 6254 6964 7673 8381 9087 9792	5615 6325 7035 7744 8451 9157 9863	5686 6396 7106 7815 8522 9228 9933	5757 6467 7177 7885 8593 9299	5828 6538 7248 7956 8663 9369	5899 6609 7319 8027 8734 9440	5970 6680 7390 8098 8804 9510	71		
7 8 9	790285 0988 1691	0356 1059 1761	0426 1129 1831	0496 1199 1901	0567 1269 1971	0637 1340 2041	0004 0707 1410 2111	0074 0778 1480 2181	0144 0848 1550 2252	0215 0918 1620 2322			
620 1 2 3 4 5 6 7 8	2392 3092 3790 4488 5185 5880 6574 7268 7960 8651	2462 3162 3860 4558 5254 5949 6644 7337 8029 8720	2532 3231 3930 4627 5324 6019 6713 7406 8098 8789	2602 3301 4000 4697 5393 6088 6782 7475 8167 8858	2672 3371 4070 4767 5463 6158 6852 7545 8236	2742 3441 4139 4836 5532 6227 6921 7614 8305	2812 3511 4209 4906 5602 6297 6990 7683 8374 9065	2882 3581 4279 4976 5672 6366 7060 7752 8443	2952 3651 4349 5045 5741 6436 7129 7821 8513	3022 3721 4418 5115 5811 6505 7198 7890 8582	70		
9	8001	8720	9199		8927	8996 NAL PA		9134	9203	9272	69		
Diff	2. 1	2	8	3	4	5	6		7	8	9		
75 74 73 72 71 70 69	7.5 7.4 7.3 7.2 7.1 7.0 6.9	15.0 14.8 14.6 14.4 14.2 14.0 13.8	1 27	.9	30.0 29.6 29.2 28.8 28.4 28.0 27.6	37.5 37.0 36.5 36.0 35.5 35.0 34.5	45.0 44.4 43.8 43.8 42.0 42.0 41.4	5 49	2.5 1.8 1.1 0.4 0.7 0.0 8.3	60.0 59.2 58.4 57.6 56.8 56.0 55.2	67.5 66.6 65.7 64.8 63.9 63.0 62.1		

No. 630 L. 799.] [No. 674 L. 829.]												
N.	0	1	2	3	4	5	6	7	8	9	Diff.	
630	799341	9409	9478	9547	9616	9685	9754	9823	9892	9961	4	
1	800029	0098	0167	0236	0305 0992 1678	0373	0442 1129	0511	0580	0648		
3	0717	0786 1472	0854	0923 1609	0992	1061 1747	1129	1198	0580 1266 1952 2637 3321 4008 4685 5365	1335		
4	1404	2158	1541 9996	2295	2363	9429	1815	1884 2568	1952	2021		
5	2089 2774	2842	2226 2910	2979	3047	2432 3116 3798	2500 3184	3252	3321	3389		
6	3457	3525 4208	3594	3662	3047 3730	3798	3867	3935	4008	4071		
7	4139	4208	4276	4344	4412	4480	4548	4616	4685	4753	1 00	
5 6 7 8 9	4821 5501	4889 5569	4957 5637	5025 5705	5093 5773	5161 5841	5229 5908	5297 5976	6044	2 2021 2705 3389 4071 4753 5 4433 6 6112	68	
640	806180	6248	6316	6384	6451	6519	6587	6655		6790		
1	6858	6926	6994	7061	7129 7806 8481	7197	7264	7332	6728 7400	6790 7467 8143 8818 9492		
2 3	7535	7603	7670	7738	7806	7873	7941	8008	1 8076	8143		
3	8211	8279	8346	8414	8481	8549	8616	8684	8751 9425	8818		
4 5	8211 8886 9560	8953 9627	9021 9694	9088 9762	9156 9829	9223 9896	9290 9964	9358	9420			
								0031 0703 1374	0098 0770 1441	0165		
6 7 8	810233	0300	0367	0434	0501 1173 1843	0569	0636	0703	0770	0837	an	
7	0904	0971 1642	1039	1106	1173	1240	1307	1374 2044	1441	1508	67	
9	1575 2245	2312	1039 1709 2379	1106 1776 2445	2512	1910 2579	1977 2646	2713	2111 2780	0165 0837 1508 2178 2847		
	0019	2980	3047	3114	3181	3247	3314	3381	3448	3514		
650 1	3581 4248 4913 5578 6241 6904	3648	3714	3781	3848	3914	2081	4048	4114	3514 4181 4847		
2	4248	4314 4980	3714 4381	3781 4447	3848 4514	4581	4647 5312 5976	4714 5378	4114 4780	4847		
2 3 4 5 6 7 8 9	4913	4980	5046	5113 5777 6440	5179 5843 6506	5246	5312	5378	5445 6109 6777 7435 8094 8754	5511		
4	5578	5644	5711	5777	5843	5910	5976	6042	6109	6175		
6	6904	6308 6970	6374 7036	7102	7169	7925	6639	6705	7435	7499		
7	7565	7631	7036 7698	7102 7764	7830	6573 7235 7896	7962	7367 8028	8094	8160		
8	7565 8226	7631 8292	8358	8424	7169 7830 8490	8556	7301 7962 8622	8688	8754	6838 7499 1 8160 1 8820 2 9478	66	
	8885	8951	9017	9083	9149	9215	9281	9346	9412	9478	00	
660	9544	9610	9676	9741	9807	9873	9939	0004	0070	0136		
1	820201 0858 1514	0267	0333 0989	0399	0464	0530	0595	0661 1317 1972	0727 1382	0 0136 0792 1448		
2	0858	0924	0989	1055	1120	1186 1841	1251	1317	1382	1448		
3	1514	1579	1645 2299	1710	1775	1841	1906	1972	2037	2103		
5	2168 2822 3474	0924 1579 2233 2887	2952	1055 1710 2364 3018	3083	2495	1251 1906 2560 3213	2626 3279 3930	2037 2691 3344 3996	2103 2756 3409		
6.	3474	3539	3605		3735	3800	3865	3930	3996	4061		
7	4126 4776	4191	4256 4906	4321 4971	1120 1775 2430 3083 3785 4386	3148 3800 4451	4516	4581 5231	4646 5296	4061 4711 5361	65	
2 3 4 5 6 7 8 9	4776	4841	4906	4971	9030	5101	5166	5231	5296	5   5361	00	
	5426	5491	5556	5621	5686	5751	5815	5880	5945			
670	6075 6723 7369	6140	6204	6269 6917 7563	6334 6981 7628 8273	6399	6464	6528 7175 7821 8467	6598	6658 7305 7951 8595		
2	7260	6787 7434	6852 7499	7563	7698	7692	7111 7757	7891	7886	7951		
1 2 3 4	8015	8080	8144	8209	8273	7046 7692 8338	8402	8467	8531	8595		
4	8660	8724	8789	8853	8918	8982	9046	9111	7240 7886 8531 9175	9239		
				Dec	DODETO	nal Pa	pme		1	1		
				PRO	PORTIO	NAL PA	K178.				1	
Diff	. 1	2	8	3	4	5	6		7	8	9	
68	6.8	13.6	20	.4	27.2	34.0	40.8	3 47	7.6	54.4 58.6 52.8 52.0 51.2	61.2	
68 67 66	6.8	12.4	20	.1	27.2 26.8	33.5 33.0	40.5	2 46	39 1	53.6	60.3	
66 65 <b>64</b>	6.6 6.5 6.4	13.2 13.0 12.8	19 19 19	· 0	26.4 26.0 25.6	32.5	39.6	40	5.5	59.0	59 4 58.5	

No. 675 L. 829.] [No. 719 L. 857.											
N.	0	1	2	2	4	5	6	7	8	9	Diff.
675	829304 9947	9368	9432	949	7 9561	9625	9690	9754	9818	9882	
7 8 9	830589 1230 1870	0011 0653 1294 1934	0075 0717 1358 1998	013 078 142 206	2   1486	0268 0909 1550 2189	0332 0973 1614 2253	0396 1037 1678 2317	0460 1102 1742 2381	0525 1166 1806 2445	64
680 1 2 3 4 5 6 7 8	2509 3147 3784 4421 5056 5691 6324 6957 7588 8219	2573 3211 3848 4484 5120 5754 6387 7020 7652 8282	2637 3275 3912 4548 5183 5817 6451 7083 7715 8345	270 333 397 461 524 588 651 714 777 840	8 3402 4039 1 4675 7 5310 5944 6577 7210 7841 8471	2828 3466 4103 4739 5373 6007 6641 7273 7904 8534	2892 3530 4166 4802 5437 6071 6704 7336 7967 8597	2956 3593 4230 4866 5500 6134 6767 7399 8030 8660	3020 3657 4294 4929 5564 6197 6830 7462 8093 8723	3083 3721 4357 4993 5627 6261 6894 7525 8156 8786	63
690 1	8849 9478	8912 9541	8975 9604	903		9164 9792	9227 9855	9289 9918	9352 9981	9415	
2 3 4 5 6 7 8 9	840106 0733 1359 1985 2609 3233 3855 4477	0169 0796 1422 2047 2672 3295 3918 4539	0232 0859 1485 2110- 2734 3357 3980 4601	029- 092: 154' 217: 279: 342: 404: 466-	1 0984 7 1610 2 2235 6 2859 0 3482 2 4104	0420 1046 1672 2297 2921 8544 4166 4788	0482 1109 1735 2360 2983 3606 4229 4850	0545 1172 1797 2422 3046 3669 4291 4912	0608 1234 1860 2484 3108 3731 4353 4974	0043 0671 1297 1922 2547 3170 3793 4415 5036	
700 1 2 3 4 5 6 7	5098 5718 6337 6955 7573 8189 8805 9419	5160 5780 6399 7017 7634 8251 8866 9481	5222 5842 6461 7079 7696 8312 8928 9542	528- 590- 652: 7141 7758 837- 8989 960-	4 5966 3 6585 1 7202 8 7819 4 8435 9 9051	5408 6028 6646 7264 7881 8497 9112 9726	5470 6090 6708 7326 7943 8559 9174 9788	5532 6151 6770 7388 8004 8620 9235 9849	5594 6213 6832 7449 8066 8682 9297 9911	5656 6275 6894 7511 8128 8743 9358 9972	62
8	850033 0646	0095 0707	0156 0769	0217 0830	0279	0340 0952	0401 1014	0462 1075	0524 1136	0585 1197	
710 1 2 3 4 5 6 7 8 9	1258 1870 2480 3090 3698 4306 4913 5519 6124 6729	1320 1931 2541 3150 3759 4367 4974 5580 6185 6789	1381 1992 2602 3211 3820 4428 5034 5640 6245 6850	144% 2058 2668 327% 3881 4488 5098 5701 6306 6910	3   2724 2   3333 3   3941 3   4549 5   5156 5   5761 6   6366	1564 2175 2785 3394 4002 4610 5216 5822 6427 7081	1625 2236 2846 3455 4063 4670 5277 5882 6487 7091	1686 2297 2907 8516 4124 4731 5387 5943 6548 7152	1747 2358 2968 3577 4185 4792 5398 6003 6608 7212	1809 2419 3029 3637 4245 4852 5459 6064 6668 7272	61
				PR	OPORTIC	NAL PA	RTS.				
Diff	Diff. 1 2 3		3	4	5	6		7	8	9	
65 64 63 62 61 60	6.5 6.4 6.3 6.2 6.1 6.0	13.0 12.8 12.6 12.4 12.2 12.0	19 19 18 18 18 18 18	.5 .2 .9 .6 .3	26.0 25.6 25.2 24.8 24.4 24.0	32.5 32.0 31.5 31.0 30.5 20.0	39.0 38.4 37.8 37.2 36.6 36.0	44 44 43 42	.7	52.0 51.2 50.4 49.6 48.8 48.0	58.5 57.6 56.7 55.8 54.9 54.0

No. 720 L. 857.1

[No. 764 L. 883.

N.	0	1	2	8	4	5	6	7	8	9	Diff.
720 1 2 3 4	857332 7935 8537 9138 9739	7393 7995 8597 9198 9799	7453 8056 8657 9258 9859	7513 8116 8718 9318 9918	7574 8176 8778 9379 9978	7634 8236 8838 9439	7694 8297 8898 9499	7755 8357 8958 9559	7815 8417 9018 9619	7875 8477 9078 9679	60
5 6 7 8 9	860338 0937 1534 2131 2728	0398 0996 1594 2191 2787	0458 1056 1654 2251 2847	0518 1116 1714 2310 2906	0578 1176 1773 2370 2966	0038 0637 1236 1833 2430 3025	0098 0697 1295 1893 2489 3085	0158 0757 1355 1952 2549 3144	0218 0817 1415 2012 2608 3204	0278 0877 1475 2072 2668 3263	
730 1 2 3 4 5 6 7 8	3323 3917 4511 5104 5696 6287 6878 7467 8056 8644	3382 3977 4570 5163 5755 6346 6937 7526 8115 8703	3442 4036 4630 5222 5814 6405 6996 7585 8174 8762	3501 4096 4689 5282 5874 6465 7055 7644 8233 8821	3561 4155 4748 5341 5933 6524 7114 7703 8292 8879	3620 4214 4808 5400 5992 6583 7173 7762 8350 8938	3680 4274 4867 5459 6051 6642 7232 7821 8409 8997	3739 4333 4926 5519 6110 6701 7291 7880 8468 9056	3799 4392 4985 5578 6169 6760 7350 7939 8527 9114	3858 4452 5045 5637 6228 6819 7409 7998 8586 9173	59
740 1	9232 9818	9290 9877	9349 9935	9408 9994	9466	9525	9584	9642	9701	9760	
2 3 4 5 6 7 8 9	870404 0989 1573 2156 2739 3321 3902 4482	0462 1047 1631 2215 2797 3379 3960 4540	0521 1106 1690 2273 2855 3437 4018 4598	0579 1164 1748 2331 2913 3495 4076 4656	0053 0638 1223 1806 2389 2972 3553 4134 4714	0111 0696 1281 1865 2448 3030 3611 4192 4772	0170 0755 1339 1923 2506 3088 3669 4250 4830	0228 0813 1398 1981 2564 3146 3727 4308 4888	0287 0872 1456 2040 2622 3204 3785 4366 4945	0345 0930 1515 2008 2681 3262 3844 4424 5003	58
750 1 2 3 4 5 6 7	5061 5640 6218 6795 7371 7947 8522 9096 9669	5119 5698 6276 6853 7429 8004 8579 9153 9726	5177 5756 6333 6910 7487 8062 8637 9211 9784	5235 5813 6391 6968 7544 8119 8694 9268 9841	5293 5871 6449 7026 7602 8177 8752 9325 9898	5351 5929 6507 7083 7659 8234 8809 9383 9956	5409 5987 6564 7141 7717 8292 8866 9440	5466 6045 6622 7199 7774 8349 8924 9497	5524 6102 6680 7256 7832 8407 8981 9555	5582 6160 6737 7314 7889 8464 9039 9612	
9	880242	0299	0356	0413	0471	0528	0013 0585	$0070 \\ 0642$	0127 0699	0185 0756	
760 1 2 3 4	0814 1385 1955 2525 3093	0871 1442 2012 2581 3150	0928 1499 2069 2638 3207	0985 1556 2126 2695 3264	1042 1613 2183 2752 3321	1099 1670 2240 2809 3377	1156 1727 2297 2866 3434	1218 1784 2354 2923 3491	1271 1841 2411 2980 3548	1328 1898 2468 3037 3605	57
Proportional Parts.											
Diff	. 1	2	8		4	5	6		7	8	9
59 58 57 56	5.9 5.8 5.7 5.6	11.8 11.6 11.4 11.2	17. 17. 17. 16.	.7 .4 .1	23.6 23.2 22.8 22.4	29.5 29.0 28.5 28.0	35.4 34.8 34.2 33.6	40	.3	47.2 46.4 45.6 44.8	58. 52. 51. 50.

Diff	9	8	7	6	5	4	3	2	1	0	N.
	4172	4115	4059	4002	3945	3888	3832	3775	3718	883661 4229 4795 5361	765
	4739	4682	4625	4569	4512	4455	4399	4342	4285	4229	6
	5305	5248 5813	5192 5757	5135 5700	5078	5022	4965 5531	4909 5474	4852 5418	4795	8
	5870 6434	6378	6321	6265	4512 5078 5644 6209	4455 5022 5587 6152	6096	6039	5983	5926	9
	6998	6942	6885	6829	6772	6716	6660	6604	6547	6491	770
r	7561	7505	7449	7392	7336 7898 8460 9021	6716 7280 7842 8404	7223 7786	7167 7730 8292 8853	7111 7674	7054	1
	8123	8067	8011	7955	7898	7842	7786	7730	7674	7617	2
	8685 9246	8067 8629 9190	8573 9134	7955 8516 9077	8460	8404	8348	8292	8236 8797	7617 8179 8741	3 4
50	9806	9190 9750	9694	9638	9582	8965 9526	8909 9470	9414	9358	0202	4
J1								9974	9918	9302 9862	5
	0365	0309 0868	0253 0812 1370	0197 0756 1314	0141 0700 1259	0086 0645 1203	$0030 \\ 0589 \\ 1147$				
	0924 1482	1426	1200	1914	1950	1909	0589	0533 1091	1025	890421 0980	7 8
	2039	1983	1928	1872	1816	1760	1705	1649	0477 1035 1593	1537	9
									9150		780
	3151	3096	3040	2985	2929	2873	2818	2762	2707	2651	1
	2595 3151 3706	2540 3096 3651 4205 4759 5312 5864	2484 3040 3595 4150 4704 5257 5809	2429 2985 3540	2373 2929 3484 4039 4593 5146 5699 6251 6802 7352	2317 2873 3429 3984 4538 5091 5644	2262 2818 3373	2206 2762 3318 3873 4427 4980 5533 6085 6636	2150 2707 3262 3817 4371	2095 2651 3207 3762 4316 4870 5423 5975 6526 7077	23456789
	4261	4205	4150	4094 4648	4039	3984	3928 4482 5036 5588	3873	3817	3762	3
	4814	4759	4704	4648	4593	4538	4482	4427	4371	4316	4
	5367 5920	5864	5800	5201 5754	5600	5614	5588	5533	4925 5478	5/10	8
	6471	6416	6361	6306-	6251	6195	6140	6085	6030	5975	7
	7022 7572	6967	6912	6306- 6857	6802	6195 6747	6692	6636	6030 6581	6526	8
5		7517	7462	7407		7297	7242	7187	7132		9
"	8122 8670 9218 9766	8067 8615 9164	8012 8561 9109 9656	7957 8506 9054	7902 8451 8999	7847 8396	7792 8341 8890 9437	7787	7682 8231 8780	7627 8176 8725 9273	790
	8670	8615	8561	8506	8451	8396	8341	8286	8231	8176	1
	9210	9711	9109	9602	9547	8944 9492	0437	8286 8835 9383	0308	0972	2
							9985	9930	9328 9875	9821	1 2 3 4
	0312 0859 1404	0258 0804 1349	0203 0749 1295 1840 2384 2927	0149 0695 1240 1785 2329 2873	0094 0640 1186 1731 2275 2818	0039 0586 1131 1676	0504	0.000		0000000	
	1404	1240	1005	1040	1106	0586	1022	1000	0422	900367 0913	5
	1948	1894	1840	1785	1731	1676	1622	0476 1022 1567	1513	1458	7
	2492	1894 2438	2384	2329	2275	2221 2764	2166	2112	2057	2003 2547	5 6 7 8 9
	3036	2981	2927	2873	2818	2764	0531 1077 1622 2166 2710	2655	0422 0968 1513 2057 2601	2547	9
	3578	3524	3470	3416 3958	3361 3904	3307	3253	3199	3144	3090	800
	4120 4661	4066	4012	3958	3904	3849 4391	3795	3741	3687	3633 4174	1
	4661	4607	4558 5094	4499	4445	4391	4337	4283	4229	4174	2
5	5749	5688	5634	5040 5580	5526	5479	5418	5364	5310	5956	4
	6281	6227	6173	6119	6066	6012	3253 3795 4337 4878 5418 5958	3741 4283 4824 5364 5904	5850	5796	5
	6820	6766	6712	6658	6604	4982 5472 6012 6551		0443	3144 3687 4229 4770 5310 5850 6389	6335	6
	7358	7304	7250	7196	7143	7089 7626	7035 7573	6981	6927	6874	7
	5202 5742 6281 6820 7358 7895 8431	5148 5688 6227 6766 7304 7841 8378	5634 6173 6712 7250 7787 8324	7196 7734 8270	4986 5526 6066 6604 7143 7680 8217	7626 8163	7573 8110	7519 8056	7465 8002	4716 5256 5796 6335 6874 7411 7949	1 2 3 4 5 6 7 8 9

Diff.	1	2	3	4	5	6	7	8	9
57	5.7	11.4	17.1	22.8	28.5	34.2	39.9	45.6	51.3
56	5.6	11.2	16.8	22.4	28.0	33.6	39.2	44.8	50.4
55	5.5	11.0	16.5	22.0	27.5	33.0	38.5	44.0	49.5
54	5.4	10.8	16.2	21.6	27.0	32.4	37.8	43.2	48.6

N.	0	1	2	3	4	5	` 6	7	8	9	Dif
10	908485	8539	8592	8646	8699	8753	8807	8860	8914	8967	
1 2	9021 9556	9074 9610	9128 9663	9181 9716	9235 9770	9289 9823	9342 9877	9396 9930	9449 9984	9503	
3	910091	0144	0197	0251	0304	0358	0411	0464	0518	0037 0571	
4	0624	0678	0731	0251 0784	0838	0891	0944	0998	1051	1104	
5678	1158	1211 1743	1264 1797	1317 1850	1371	1424	1477 2009	1530	1584	1687	
7	1690 2222	2275	2328	2381	1903 2435	1956 2488	2009 2541	2063 2594	2116 2647	2169 2700	
8	2753	2806	2859	2913	2966	3019	3072	3125	3178	3231	
9	3284	3337	3390	3443	3496	3549	3602	3655	3708	3761	5
20	3814	3867	3920	3973	4026	4079 4608	4132	4184 4713	4237	4290	
1	4343	4396	4449	4502	4555 5083	4608	4660	4713	4766	4819	
2345678	4872 5400	4925 5453	4977 5505	5030 5558	5611	5136 5664	5189 5716	5241 5769	5294 5822	5347 5875	
4	5927	5980	6033	6085	6138	6191	6243	6296	6349	6401	
5	6454 6980	6507	6559 7085	6612	6664	6717 7243	6770 7295	6296 (822 7348	6875	6927	
6	6980	7033	7085	7138	7190	7243	7295	7348	7400	7453	
7	7506 8030	7558	7611 8135	7663	7716	7768	7820	7873	7925	7978	
9	8555	8083 8607	8659	8188 8712	8240 8764	8293 8816	8345 8869	8397 8921	8450 8973	8502 9026	
30	9078	9130	9183	9235	9287	9340	9392	9444	9496	9549	
1	9601	9653	9706	9758	9810	9862	9914	9967	0010	0054	
2	920123	0176	0228	0280	0332	0384	0436	0489	0019 0541	0071 0593	
3	0645	0697	0749	0801	0853	0906	0958 1478 1998 2518	1010	1062	1114	1
4 5 6 7	1166 1686	1218 1738	1270	1322 1842	1374	1426	1478	1530	1582	1634	
5	1686	1738	1790	1842	1894	1946	1998	2050	2102	2154	
0	2206 2725	2258 2777	2310 2829	2362 2881	2414 2933	2466 2985	3037	2570 3089	2622 3140	2674 3192	
8	3244	3296	3348	3399	3451	3503	3555	3607	8658	3710	
8	3244 3762	3814	3865	3917	3969	4021	3555 4072	4124	3658 4176	4228	
340	4279 4796	4331	4383	4434	4486	4538	4589	4641	4693 5209 5725	4744	
1	4796	4848 5364	4899 5415	4951 5467	5003 5518	5054 5570	5106 5621	5157 5673	5209	5261 5776	
3	5828	5879	5931	5982	6034	6085	6137	6188	6240	6291	i
4	5312 5828 6342	5879 6394	6445	6497	6548	6085 6600	6651	6702	6754 7268	6291 6805	1
4 5 6 7	6857 7370	6908	6959	7011	7062	7114	7165 7678	6702 7216	7268	7319	1
6	7370	7422	7473	7524	7576	7627	7678	7730	7781	7832	1
6	7883	7935 8447	7986 8498	8037 8549	8088 8601	8140 8652	8191	8242 8754	8293 8805	8345 8857	
8	8396 8908	8959	9010	9061	9112	9163	8708 9215	9266	9317	9368	
350	9419	9470	9521	9572	9623	9674	9725	9776	9827	9879	,
1	9930	9981	0000		0404	0405	0000	0000	0000	0000	•
2	930440	0491	0032 0542	0083	0134	0185 0694	0236 0745	0287 0796	0338 0847	0389 0898	
ã	0949	1000	1051	0592 1102	0643 1153	1204	1254	1305	1356	1407	
4	1458	1509	1560	1610	1661	1712	1254 1763	1305 1814	1356 1865	1915	

Diff.	1	2	3	4	5	6	7	8	9
58	5.8	10.6	15.9	21.2	26.5	31.8	37.1	42.4	47.7
52	5.2	10.4	15.6	20.8	26.0	31.2	36.4	41.6	46.8
51	5.1	10.2	15.8	20.4	25.5	30.6	35.7	40.8	45.9
50	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0

\$55 981966	N.	0	1	2	3	4	6	6	3	8	9	Diff
7 2981 3091 3082 3133 3183 3234 3285 3335 3386 3437 9 3893 344 4094 4495 4495 4496 4497 4397 3481 3892 3943 404 4094 4495 4495 4496 4496 4497 4497 4498 4596 4497 4498 4596 4497 4498 4596 4497 4498 4596 4497 4498 4598 4597 4448 4596 4497 4498 4598 4597 4498 4598 4597 4498 4598 4598 4598 4598 4598 4598 4598		001000	90177	9000	0110	0160	9990	9071	9999	9970	0409	-
7 2981 3091 3082 3133 3183 3234 3285 3335 3386 3437 9 3893 344 4094 4495 4495 4496 4497 4397 3481 3892 3943 404 4094 4495 4495 4496 4496 4497 4497 4498 4596 4497 4498 4596 4497 4498 4596 4497 4498 4596 4497 4498 4598 4597 4448 4596 4497 4498 4598 4597 4498 4598 4597 4498 4598 4598 4598 4598 4598 4598 4598		981900	2017	2000	2110	9677	2220	9779	9990	0970	2020	
9 3993 4044 4094 4145 4195 4246 4296 4347 4397 4448  1 5003 5054 5104 5104 5154 5205 5255 5906 5356 5406 5457  2 5507 5538 5668 5658 5709 5759 5809 5860 5510 5600  3 6011 6061 6111 6162 6212 6262 6313 6363 6413 6463  4 6514 6544 6614 6665 6715 6765 6815 6855 6916 6066  6 7518 7588 7618 7688 7718 7769 7810 7869 7919 7969  5 7 7016 7066 7116 7167 7217 72267 7317 7367 7418 7468  7 8019 8069 8119 8169 8219 8269 8320 8370 8420 8470  8 8520 8570 8620 8670 8720 8720 8820 8870 8820 8870  9 9020 9070 9120 9170 9220 9270 9320 9909 9419 9469  3 1014 004 1114 1163 1213 1203 1313 1326 1492 8968  1 940018 0088 0118 0168 6218 0267 0317 0367 0417 0467  2 0516 0566 0616 0666 0716 0765 0815 0865 0015 0664  4 1511 1561 1611 1606 1710 1700 1809 1859 1909 1958  6 2504 2534 2603 2653 2702 2752 2801 2851 2901 2950  8 3195 3544 3503 3643 3692 3742 3791 3841 3890 3039  8 3195 3544 3503 3643 3692 3742 3791 3841 3890 3039  9 3089 4088 4088 4137 4186 4236 4238 4238 4338 8891 8869  9 3089 4088 4088 4137 4186 4236 4238 4238 4338 8891 8869  1 4976 5025 574 5124 5173 5227 2256 2851 2901 2950  8 3195 3544 3503 3643 3692 3742 3791 3841 3890 3039  8 3195 3544 3503 3643 3692 3742 3791 3841 3890 3039  8 4483 4532 4581 4631 4680 4729 4779 4828 4877 4927  2 5690 5518 5067 5650 6108 6157 7607 778 777 7800 5051 5065 5065 5065 5065 5065 5065 50	0	2414	2024	2000	2122	2182	2024	2005	2225	2286		
9 3993 4044 4094 4145 4195 4246 4296 4347 4397 4448  1 5003 5054 5104 5154 5205 5255 5906 5356 5406 5457  2 5507 5538 5668 5658 5709 5759 5809 5869 5610 5600  3 6011 6061 6111 6162 6212 6232 6313 6343 6413 6463  4 6514 6544 6614 6655 6715 6735 6815 6855 6016 6366  5 7016 7066 7116 7167 7217 7297 7317 7367 7418 7468  5 7 7016 7066 7116 7167 7217 7297 7317 7367 7418 7468  7 8019 8069 8119 8169 8219 8269 8230 8370 8420 8470  9 9020 9070 9120 9170 9220 9270 9320 9369 9419 9469  8 8520 8570 8620 8670 8780 8770 8820 8770 8820 8770  9 9020 9070 9120 9170 9220 9270 9320 9369 9419 9469  3 1014 004 1114 1163 1213 1263 1313 1323 1493 1412 1462 1414 1618 1213 1263 1313 132 1424 1412 1412 1416 1416 1416 1416 141	é	3487	3538	3589	3639	3690	3740	3791	3841	3892	3943	
1 5003 5054 5104 5104 5154 5205 5255 5306 5365 5406 5457 5360 360 5658 5709 5759 5580 5809 5800 5610 5960 360 3601 6111 6162 6212 6222 6232 6313 6303 6413 6463 6463 6461 6654 6614 6655 6715 6765 6815 6805 6016 6066 6716 7066 716 716 7167 7217 7267 7317 7307 7418 7468 758 7618 7688 7618 7688 7618 7689 7819 7809 7919 7969 9809 8019 819 8169 8219 8280 8230 8370 8220 8470 7418 7768 8762 87718 7760 7819 7809 9020 9070 9120 9170 9220 9270 9320 9309 9419 9469 9470 9200 9070 9120 9170 9220 9270 9320 9309 9419 9469 9470 9509 9619 9669 9719 9769 9619 9869 918 9868 918 9869 918 9868 918 9868 918 9868 918 9868 918 9869 918 9868 918 9869 918 9868 918 9869 918 9868 918 918 918 918 918 918 918 918 918 91	9	3993	4044	4094	4145	4195	4246	4296		4397		ļ
1 5003 5054 5104 5104 5154 5205 5255 5306 5365 5406 5457 5360 360 5658 5709 5759 5580 5809 5800 5610 5960 360 3601 6111 6162 6212 6222 6232 6313 6303 6413 6463 6463 6461 6654 6614 6655 6715 6765 6815 6805 6016 6066 6716 7066 716 716 7167 7217 7267 7317 7307 7418 7468 758 7618 7688 7618 7688 7618 7689 7819 7809 7919 7969 9809 8019 819 8169 8219 8280 8230 8370 8220 8470 7418 7768 8762 87718 7760 7819 7809 9020 9070 9120 9170 9220 9270 9320 9309 9419 9469 9470 9200 9070 9120 9170 9220 9270 9320 9309 9419 9469 9470 9509 9619 9669 9719 9769 9619 9869 918 9868 918 9869 918 9868 918 9868 918 9868 918 9868 918 9869 918 9868 918 9869 918 9868 918 9869 918 9868 918 918 918 918 918 918 918 918 918 91	360	4498	4549	4599	4650	4700	4751	4801	4852	4902	4953	
3 6011 6001 6011 6111 6162 6212 6232 6313 6303 6413 6463 55 7016 7066 7116 7167 7217 7297 7317 7367 7418 7468 55 7016 7066 7116 7167 7217 7297 7317 7367 7418 7468 75 8019 8069 8119 8169 8219 8260 8230 8320 8370 8420 8470 8420 970 9020 9070 9120 9170 9220 9270 9320 9369 9419 9469 9479 9699 9020 9070 9120 9170 9220 9270 9320 9369 9419 9469 9479 9569 9619 9669 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 9769 9619 9869 9719 971	1	5003	5054	5104	5154	5905	5255	5306	5356	5406	5457	
3 6011 6001 6111 6162 6212 6202 6313 6363 6413 6463 6463 655 6765 6765 6765 6765 6016 6006 6 6 7516 7066 716 716 7167 7217 7297 7317 7367 7418 7468 7 7867 7418 7568 7618 7688 7718 7769 7819 7809 7819 7809 7819 7809 7819 7809 7819 7809 7819 7809 7819 7809 8119 8169 8219 8203 8203 8270 820 8270 820 8470 820 870 870 870 870 870 870 870 870 870 87		5507	5558	KENQ	5658	5709	5759	5809	5860	5910	5960	
5 7016 7068 7116 7167 7217 7217 7817 7817 7807 7418 7488 7688 7718 7568 7618 7688 7718 7768 7718 7768 7819 7809 7919 7909 7819 7809 8119 8169 8119 8169 8219 82808 8230 8270 8230 8270 8220 8470 8420 8420 8420 8420 8420 8420 8420 842	3	6011	6061	6111	6162	6212	6262	6313	6363	6413	6463	
5 7016 7068 7116 7167 7217 7217 7317 7307 7418 7488 7488 7688 7718 7688 7718 7768 7718 7768 7317 7307 7418 7488 7688 7718 8768 7718 7768 7519 7509 7509 8019 8099 8119 8169 8219 82808 8230 8270 8230 8270 8280 828	4	6514	6564	6614	6665	6715	6765	6815	6865	6916	6966	
	5	7016	7066	7116	7167	7217	7267	7317	7367	7418	7468	
	6	7518	7568	7618	7668	7718	7769	7819	7869	7919	7969	5
	7	8019	8069	8119	8169	8219	8269	8320	8370	8420	8470	ľ
	8		8570	8620	8670	8720	8770	8820	8870			
1 940018 0068 0118 0168 0218 0267 0317 0367 0417 0467 2 0516 0566 0616 0666 0716 0765 0815 0865 0915 0964 4 1318 1004 1114 1163 1213 1263 1313 1362 1412 1462 4 1511 1561 1611 1600 1710 1760 1809 1859 1909 1958 5 2008 2058 2107 2157 2207 1256 2306 2355 2405 2455 6 2504 2554 2603 2653 2702 2752 2801 2851 2901 2950 8 3195 3514 3593 3483 3487 2397 3316 3396 3445 8 3495 3494 3495 3495 3495 3495 3495 3495				9120						1		
8         3900         3049         3099         3643         3692         3742         3371         3810         3890         3433         3939         3433         3692         3742         3371         3811         3890         3339         3433         3890         3339         3433         3890         3339         3939         4088         4088         4481         4814         4861         4826         4287         4335         4384         4433           1         4076         5025         5074         5124         5173         5522         5272         5321         5570         5419         5471         5212         5499         5618         5567         5616         5665         5715         5764         5812         5570         5419         5612         5680         6690         6690         6690         6690         6690         6690         6690         6690         6697         6776         4512         5643         6907         6545         6894         6908         6747         6766         6645         6894         6908         6747         6766         6445         6894         6892         8973         7887         7788         7777         7896 <td>370</td> <td>9519</td> <td>9569</td> <td>9619</td> <td>9669</td> <td>9719</td> <td></td> <td>9819</td> <td>9869</td> <td>9918</td> <td>9968</td> <td></td>	370	9519	9569	9619	9669	9719		9819	9869	9918	9968	
8 3495 3544 3893 3483 3692 3742 3397 3340 3399 3899 4038 4088 4088 4088 4088 4088 4088 4088	1	940018	0068	0118	0168	0218	0267	0317	0367	0417	0467	
8         3900         3049         3099         3643         3692         3742         3371         3810         3890         3433         3939         3433         3692         3742         3371         3811         3890         3339         3433         3890         3339         3433         3890         3339         3939         4088         4088         4481         4814         4861         4826         4287         4335         4384         4433           1         4076         5025         5074         5124         5173         5522         5272         5321         5570         5419         5471         5212         5499         5618         5567         5616         5665         5715         5764         5812         5570         5419         5612         5680         6690         6690         6690         6690         6690         6690         6690         6690         6697         6776         4512         5643         6907         6545         6894         6908         6747         6766         6645         6894         6908         6747         6766         6445         6894         6892         8973         7887         7788         7777         7896 <td>2</td> <td>0516</td> <td>0566</td> <td>0616</td> <td>0666</td> <td>0716</td> <td>0765</td> <td>0815</td> <td>0865</td> <td>0915</td> <td>0964</td> <td></td>	2	0516	0566	0616	0666	0716	0765	0815	0865	0915	0964	
8 3495 3544 3893 3483 3692 3742 3397 3340 3399 3899 4038 4088 4088 4088 4088 4088 4088 4088	3	1014	1064	1114	1163	1213	1263	1313	1362	1412	1462	1
8         3900         3049         3099         3643         3692         3742         3371         3810         3890         3433         3939         3433         3692         3742         3371         3811         3890         3339         3433         3890         3339         3433         3890         3339         3939         4088         4088         4481         4814         4861         4826         4287         4335         4384         4433           1         4076         5025         5074         5124         5173         5522         5272         5321         5570         5419         5471         5212         5499         5618         5567         5616         5665         5715         5764         5812         5570         5419         5612         5680         6690         6690         6690         6690         6690         6690         6690         6690         6697         6776         4512         5643         6907         6545         6894         6908         6747         6766         6645         6894         6908         6747         6766         6445         6894         6892         8973         7887         7788         7777         7896 <td>4</td> <td>1511</td> <td>1561</td> <td>1611</td> <td>1660</td> <td>1710</td> <td>1760</td> <td>1809</td> <td>1859</td> <td>1909</td> <td>1958</td> <td></td>	4	1511	1561	1611	1660	1710	1760	1809	1859	1909	1958	
8         3900         3049         3099         3643         3692         3742         3371         3810         3890         3433         3939         3433         3692         3742         3371         3811         3890         3339         3433         3890         3339         3433         3890         3339         3939         4088         4088         4481         4814         4861         4826         4287         4335         4384         4433           1         4076         5025         5074         5124         5173         5522         5272         5321         5570         5419         5471         5212         5499         5618         5567         5616         5665         5715         5764         5812         5570         5419         5612         5680         6690         6690         6690         6690         6690         6690         6690         6690         6697         6776         4512         5643         6907         6545         6894         6908         6747         6766         6645         6894         6908         6747         6766         6445         6894         6892         8973         7887         7788         7777         7896 <td>5</td> <td>2008</td> <td>2058</td> <td>2107</td> <td>2157</td> <td>2207</td> <td>2256</td> <td>2306</td> <td>2355</td> <td>2405</td> <td>2455</td> <td></td>	5	2008	2058	2107	2157	2207	2256	2306	2355	2405	2455	
8         3900         3049         3099         3643         3692         3742         3371         3810         3890         3433         3939         3433         3692         3742         3371         3811         3890         3339         3433         3890         3339         3433         3890         3339         3939         4088         4088         4481         4814         4861         4826         4287         4335         4384         4433           1         4076         5025         5074         5124         5173         5522         5272         5321         5570         5419         5471         5212         5499         5618         5567         5616         5665         5715         5764         5812         5570         5419         5612         5680         6690         6690         6690         6690         6690         6690         6690         6690         6697         6776         4512         5643         6907         6545         6894         6908         6747         6766         6645         6894         6908         6747         6766         6445         6894         6892         8973         7887         7788         7777         7896 <td>6</td> <td>2504</td> <td>2554</td> <td>2603</td> <td>2653</td> <td>2702</td> <td>2752</td> <td>2801</td> <td>2851</td> <td>2901</td> <td>2950</td> <td></td>	6	2504	2554	2603	2653	2702	2752	2801	2851	2901	2950	
\$\begin{array}{cccccccccccccccccccccccccccccccccccc	7	3000	3049	3099	3148	3198	3247	3297	3346	3396	3445	
\$\begin{array}{cccccccccccccccccccccccccccccccccccc	8	3495	4028	4000	3643	3692	3742	4995	3841	3890	3939	
3 5961 0010 9099 6108 6137 6207 6236 6305 6354 6493   5 6943 6992 7041 7090 7139 7189 7238 7287 7336 7385   6 7434 7483 7532 7581 7630 7679 7728 7777 7826 7575 4   7 7924 7973 8022 8070 8119 8168 8217 8266 8315 8364   8 8413 8402 8511 8560 8608 8657 8706 8755 8804 8853   9 8902 8951 8999 9048 9097 9146 9195 9244 9292 9341   9578 9926 9975   1 9578 9926 9975   2 95065 0414 0462 0511 0560 0608 0657 0706 0754 0803   3 0851 0900 0949 0997 1046 1005 1143 1192 1240 1289   4 1388 1386 1485 1483 1532 1580 1629 1677 1726 1775   5 1823 1872 1920 1969 2017 2066 2114 2163 2211 2260   6 2308 2356 2405 2453 2502 2550 2599 2647 2669 3274   7 2792 2841 2859 2488 2966 3034 3083 3181 3180 3225   8 2826 3225 2355 2450 3636 3613 3180 3225   8 2826 3225 3235 3421 3470 3518 3568 3615 3636 3611 1	-											
3 5961 0010 9099 6108 6137 6207 6236 6305 6354 6493   5 6943 6992 7041 7090 7139 7189 7238 7287 7336 7385   6 7434 7483 7532 7581 7630 7679 7728 7777 7826 7575 4   7 7924 7973 8022 8070 8119 8168 8217 8266 8315 8364   8 8413 8402 8511 8560 8608 8657 8706 8755 8804 8853   9 8902 8951 8999 9048 9097 9146 9195 9244 9292 9341   9578 9926 9975   1 9578 9926 9975   2 95065 0414 0462 0511 0560 0608 0657 0706 0754 0803   3 0851 0900 0949 0997 1046 1005 1143 1192 1240 1289   4 1388 1386 1485 1483 1532 1580 1629 1677 1726 1775   5 1823 1872 1920 1969 2017 2066 2114 2163 2211 2260   6 2308 2356 2405 2453 2502 2550 2599 2647 2669 3274   7 2792 2841 2859 2488 2966 3034 3083 3181 3180 3225   8 2826 3225 2355 2450 3636 3613 3180 3225   8 2826 3225 3235 3421 3470 3518 3568 3615 3636 3611 1	380	4486	#00Z	E074	4001	4000	#129 #000	5070	#904 #901	4077	4927 E410	
3 5961 0010 9099 6108 6137 6207 6236 6305 6354 6493   5 6943 6992 7041 7090 7139 7189 7238 7287 7336 7385   6 7434 7483 7532 7581 7630 7679 7728 7777 7826 7575 4   7 7924 7973 8022 8070 8119 8168 8217 8266 8315 8364   8 8413 8402 8511 8560 8608 8657 8706 8755 8804 8853   9 8902 8951 8999 9048 9097 9146 9195 9244 9292 9341   9578 9926 9975   1 9578 9926 9975   2 95065 0414 0462 0511 0560 0608 0657 0706 0754 0803   3 0851 0900 0949 0997 1046 1005 1143 1192 1240 1289   4 1388 1386 1485 1483 1532 1580 1629 1677 1726 1775   5 1823 1872 1920 1969 2017 2066 2114 2163 2211 2260   6 2308 2356 2405 2453 2502 2550 2599 2647 2669 3274   7 2792 2841 2859 2488 2966 3034 3083 3181 3180 3225   8 2826 3225 2355 2450 3636 3613 3180 3225   8 2826 3225 3235 3421 3470 3518 3568 3615 3636 3611 1	4	4970	5519	5587	50124	2119	5715	5764	5019	5000	5019	
1	2	5061	6010	6050	6108	6157	6907	6956	6305	6254	6403	
1	4	6452	6501	6551	6600	6649	6698	6747	6796	6845	6894	
90	5	6943	6992	7041	7090	7139	7189	7238	7287	7336	7385	١.
1	6	7434	7483	7532	7581	7630	7679	7728	7777	7826	7875	4
90	7	7924	7973	8022	8070	8119	8168	8217	8266	8315	8364	
1	8	8413			8560		8657	8706	8755	8804		
1 9878 9926 9975	9	8902	8951	8999	9048	9097	9146	9195	9244	9292	9341	
2 950865 0414 0462 0511 0506 0608 0657 0706 0754 0803 3 0851 0900 0949 0997 1046 1005 143 1192 1240 1289 4 1338 1386 1435 1438 1532 1580 1639 1677 1726 1775 5 1823 1872 1920 1969 2017 2066 2114 2163 2211 2260 6 2308 2356 2405 2453 2502 2550 2599 2647 2696 2744 2898 2868 2876 3034 3083 3181 3180 3225 3878 3225 3325 3420 3318 3383 3381 3181 3180 3225 3236 3245 3247 3325 3325 3325 3325 3421 3470 3518 3566 3615 3663 3111	90	9390		9488	9536	9585	9634	9683	9731	9780	9829	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	1	9878	9926	9975	0094	0073	0121	0170	0219	0967	0316	
4 1338 1386 1495 1493 1532 1580 1639 1677 1726 1775 5 1883 1572 1920 1699 3017 2066 2114 2163 2211 2260 6 2308 2356 2405 2453 2502 2550 2599 2647 2696 2744 7 2792 2841 2859 2398 2396 3034 3083 3181 3180 3225 8 3276 3225 3373 4221 3470 3518 368 3613 5711	2	950365	0414	0462	0511	0560	0608	0657	0706	0754	0803	
4 1338 1386 1495 1493 1532 1580 1639 1677 1726 1775 5 1883 1572 1920 1699 2017 2066 2114 2163 2211 2260 6 2208 2356 2405 2453 2502 2550 2599 2647 2696 2744 7 2792 2841 2859 2385 2396 3034 3083 3181 3180 3225 8 326 325 325 3470 3518 3566 3615 3663 3711	3	0851	0900	0949	0997	1046	1095	1143	1192	1940	1289	
5 1883 1872 1920 1969 2017 2066 2114 2163 2211 2260 6 2838 2356 2465 2453 2502 2550 2599 2647 2696 2744 7 2792 2841 2859 2485 2986 3034 3083 3181 3180 3225 3873 3421 3470 3518 3566 3615 3663 3711	4	1338	1386	1435	1483	1532	1580	1629	1677	1726	1775	
6 2308 2356 2405 2453 2502 2550 2599 2647 2696 2744 7 2792 2841 2889 2938 2986 3034 3083 3131 3180 3228 8 3276 3325 3373 3421 3470 3518 3566 3615 3663 3711	5	1823	1872	1920 i	1969	2017	2066	2114	2163	2211	2260	
7 2792 2841 2889 2938 2986 3034 3083 3131 3180 3228 8 3276 3325 3373 3421 3470 3518 3566 3615 3663 3711	6	2308	2356	2405	2453	2502	2550	2599	2647	2696	2744	
8   3276   3325   3373   3421   3470   3518   3566   3615   3663   3711	7	2792 1	2841	2889	2938	2986	3034	3083	3131	3180	3228	
9 3760 3808 3856 3905 3953 4001 4049 4098 4146 4194	8	3276	3325	3373		3470	3518	3566 4049	3615 4098	3663 4146	3711	

Diff.	1	2	3	4	5	6	7	8	9
51	5.1	10.2	15.3	20.4	25.5	30.6	35.7	40.8	45.9
50	5.0	10.0	15.0	20.0	25.0	30.0	35.0	40.0	45.0
49	4.9	9.8	14.7	19.6	24.5	29.4	34.3	39.2	44.1
48	4.8	9.6	14.4	19.2	24.0	28.8	33.6	38.4	43.2

L. 97	o. 944	[N							4.]	900 L. 95	No !
Diff	9	8	7	6	5	4	3	2	1	0	N.
	4677	4628	4580	4532	4484	4435	4387	4339	A901	954243	900
	5158	5110	5062	5014	4966	4918	4869	4821	4291 4773	4725	1
	5640	5592	5543	5495	5447	5399	5351	5303	5255	5207	2
	6120	6072	6024	5976	5928	5880	5832	5784	5736	5688	3
	6601	6553	6505	6457	6409	6361	6313	6265	6216	6168	4
4	7080	7032	6984	6936	6888	6840	6793	6745	6697	6649	5
	7559	7512	7464	7416	7368	7320	7272	7224	7176	7128	4 5 6 7 8 9
	8038	7990	7942	7894	7847 8325	7799	7751 8229	7703	7655	7607	7
	8516	8468	8421	8373	8325	8277	8229	8181	8134	8086	8
	8994	8946	8898	8850	8803	8755	.8707	8659	8612	8564	9
	9471	9423	9375	9328	9280	9232	9185	9137	9089	9041	910
	9947	9900	9852	9804	9757	9709	9661	9614	9566	9518	1
	0423	0376	0328	0280	0233	0185	0138	0090	0042	9995	2
	0899	0851	0804	0756	0709	0661	0613	0566	0518	960471	3
	1374	1326	0804 1279	1231	1184	1136	1089	1041	0994	0946	4
	1848	1801	1753	1706	1658	1611	1563	1516	1469	1421	4 5 6 7 8 9
	2322	2275	2227	2180	2132	2085	2038	1990	1943	1895	6
	2795	2748	2701	2653	2606	2559	2511	2464	2417	2369	7
	3268	3221	3174	3126	3079	3032	2985	2937	2890	2848	- 8
	3741	3221 3693	3646	3599	3552	3504	3457	2937 3410	3363	2848 3316	9
	4212	4165	4118	4071	4024	3977	3929	3882	3835	3788	920
	4684	4637	4590	4542	4495	4448	4401	4254	4307	4260	1
	5155	5108	5061	5013	4966	4919	4872	4825	4778	4731	2
	5625 6095	5578	5531 6001	5484	5437	5390	5343	4825 5296 5766	5249 5719	5202 5672	2 3 4 5 6
4	6095	6048	6001	5954	5907	5860	5813	5766	5719	5672	4
	6564	6517	6470	6423	6376	6329	6283	6236	6189	6142	5
	7033	6986	6939	6892	6845	6799	6752	6705	6658	6611	6
	7501	7454	7408	7361	7314	7267	7220 7688	7173	7127	7080	7 8 9
	7969	7922	7875	7829	7782	7735	7688	7642	7595	7548	8
	8436	8390	8343	8296	8249	8203	8156	8109	8062	8016	
	8903	8856	8810	8763	8716	8670	8623	8576	8530	8483	930
	9369	9323	9276	9229	9183	9136	9090	9043	8996	8950	1
	9835	9789	9742	9695	9649	9602	9556	9509 9975	9463 9928	9416 9882	2
	0300	0254	0207	0161	0114	0068	0021	9915	9920	900%	o o
	0765	0719	0672	0626	0579	0533	0486	0440	0393	970347	4
	1229	1183	0672 1137	1090	0579 1044	0997	$0486 \\ 0951$	0904	0858	0812	5
	0765 1229 1693	1647	1601	1554	1508 1971	1461	1415	1369	1322	0812 1276	6
	2157	2110	2064	2018	1971	1925	1879	1832	1786	1740	7
	2619	2573	2527	2481	2434	2388	2342	2295	2249	2203	5 6 7 8 9
	3082	3035	2989	2943	2897	2851	2804	2758	2712	2666	9
	3543	3497	3451	3405	3359	3313	3266	3220	3174	3128	940
	4005	3959	3913 4374	3866	3820	3774	3728	3682	3636	3590	
	4466	4420	4374	4327	4281	4235	4189	4143	4097	4051	2
	4926	4880	4834	4788	4742	4696	4650	4604	4558	4512	1 2 3 4
4	5386	5340	5294	5248	5202	5156	5110	5064	5018	4972	4

Diff,	1	2	3	4	5	6	7	8	9
47	4.7	9.4	14.1	18.8	28.5	28.2	32.9	37.6	42.3
46	4.6	9.2	13.8	18.4	28.0	27.6	32.2	36.8	41.4

N.	0	1	2	3	4	5	6	7	8	9	Diff.
945	975432	5478	5524	5570	5616	5662	5707	5753	5799	5845	
6	5891 6350	5937	5983	6029	6075 6533	6121 6579	6167 6625 7083 7541	6212 6671	6258 6717	6304 6763	
7	6350	6396	6442	6488	6533	6579	6625	6671	6717	6763	
8	6808 7266	6854 7312	6900 7358	6946 7403	6992 7449	7037 7495	7088	7129 7586	7175 7632	7220 7678	
	4										
950	7724 8181	7769 8226	7815 8272	7861	7906	7952	7998	8043	8089	8135	
1	8637	8683	8212	8817	8868	8409	8454	8500 8956	8546	8591 9047	
2 3	9093	9138	8728 9184	8317 8774 9230	9275	9321	8911 9366	9412	9002 9457	9503	
4	9548	9594	9639	9685	8363 8819 9275 9730	8865 9321 9776	9821	9867	9912	9958	
E	980003	0049	0094	0140	0185		0000	0200	0367	0412	
5 6 7 8 9	0458	0503	0549	0594	0640	0231 0685 1139	0730	0322 0776 1229	0821	0867	
7	0912	0957	0549 1003	0594 1048	0640 1093	1139	1184	1229	1275	1320	
8	1366	1411	1456	1501	1547	1592	1637	1683	1728	1773	
9	1819	1864	1909	1501 1954	1547 2000	1592 2045	0276 0730 1184 1637 2090	1683 2135	1728 2181	1773 2226	
960	2271 2723 3175	2316 2769 3220 3671	2362 2814 3265 3716	2407 2859 3310	2452	2497 2949	2543 2994	2588 3040	2633 3085 3536	2678 3130 3581	
	2723	2769	2814	2859	2904	2949	2994	3040	3085	3130	
2	3175	3220	3265	3310	3356	3401 3852	3446	3491	3536	3581	
3	3626 4077	3671	3716	3762 4212 4662	3807	3852	3897	3942	3987 4437	4032 4482	
4	4527	4122 4572	4167 4617	4212	4257	4502	4347 4797	4392 4842	4437	4482	45
123456789	4077	5000	5067	5119	2452 2904 3356 3807 4257 4707 5157 5606 6055	4302 4752 5202 5651	5947	5909	4887 5337 5786	4932 5382 5830	
7	4977 5426	5022 5471	5516	5112 5561 6010	5606	5651	5247 5696	5292 5741	5786	5830	
8	5875	5920	5965	6010	6055	6100	6144	6189	6234	6279	
9	6324	6369	6413	6458	6503	6548	6593	6637	6682	6727	
970	6772	6817	6861 7309 7756	6906 7353 7800	6951 7398 7845 8291 8737 9183	6996 7443	7040 7488 7934 8381 8826 9272	7085 7532 7979 8425 8871	7130	7175	
1	7219 7666 8113	7264 7711	7309	7353	7398	7443	7488	7532	7577 8024 8470	7622 8068	
2	7666	8157	7756	7800	7845	7890	7934	7979	. 8024	8008	
4	0113 9550	8604	8202 8648	8247 8693	8291	7890 8336 8782 9227	99991	9971	8916	8514 8960	
5	8559 9005	9049	9094	9138	9183	9227	9272	9316	9361	9405	
2 3 4 5 6 7	9450	9494	9539	9583	9628	9672	9717	9761	9806	9850	
7	9895	9939	9983								
_	000000	0000	0.100	0028	0072	0117	0161 0605	0206 0650	0250	0294	
8	990339 0783	0383 0827	0428 0871	0472 0916	0516 0960	0561 1004	1049	1093	0694 1137	0738 1182	
980	1226 1669	1270 1713	1315 1758	1359	1403	1448_	1492 1935 2377	1536	1580	1625 2067	
1	2111	2156	9900	2014	9999	1980	9977	9491	2023 2465	2509	
ã	2554	2598	2200 2642	1802 2244 2686	1846 2288 2730 3172 3613	1890 2333 2774 3216	2819	1979 2421 2863	2907	2951	
4	2995	3039	3083	3127	3172	3216	3260	3304	3348	3392 3833 4273 4713	
5	3436 3877	3039 3480	3524	3127 3568	3613	3657	3260 3701	3745	3348 3789	3833	
6	3877	3921	3965	4009	4058	4097	4141	4185	4229	4273	
7	4317	4361	4405	4449	4493	4097 4537 4977	4141 4581 5021	4625 5065	4669	4713	44
2 3 4 5 6 7 8 9	4757	4801 5240	4845	4889	4933	4977	5021	5065	5108 5547	5152	
9	5196	0240	5284	5328	5372	5416	5460	5504	5547	5591	

Diff.	1	2	3	4	5	6	7	8	9
46	4.6	9.2	13.8	18.4	23.0	27.6	32.2	36.8	41.4
45	4.5	9.0	13.5	18.0	22.5	27.0	31.5	36.0	40.5
44	4.4	8.8	13.2	17.6	22.0	26.4	30.8	35.2	39.6
48	4.8	8.6	12.9	17.2	21.5	25.8	30.1	34.4	38.7

No. 990 L. 995.]

[No. 999 L. 999.

N.	0	1	2	8	4	5	6	7	8	9	Diff.
990	995635	5679	5723	5767	5811	5854	5898	5942	5986	6030	44
1	6074	6117	6161	6205	6249	6293	6337	6380	6424	6468	
2	6512	6555	6599	6643	6687	6731	6774	6818	6862	6906	
3	6949	6993	7037	7080	7124	7168	7212	7255	7299	7343	
4	7386	7430	7474	7517	7561	7605	7648	7692	7736	7779	
5	7823	7867	7910	7954	7998	8041	8085	8129	8172	8216	
6	8259	8303	8347	8390	8434	8477	8521	8564	8608	8652	
7	8695	8739	8782	8826	8869	8913	8956	9000	9043	9087	
8 9	9131 9565	9174 9609	9218 9652	9261 9696	9305 9739	9348 9783	9392 9826	9435 9870	9479 9913	9522 9957	43

### HYPERBOLIC LOGARITHMS.

		NA K I	PERD	OLLIC	LUGA	ILLE.	mms.		
No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
1.01	.0099	1.45	.3716	1.89	.6366	2.33	.8458	2.77	1.0188
1.02	.0198	1.46	.3784	1.90	.6419	2.34	.8502	2.78	1.0225
1.03	.0296	1.47	.3853	1.91	.6471	2.35	.8544	2.79	1.0260 1.0296
1.05	.0488	1.49	.3988	1.93	.6575	2.37	.8629	2.81	1.0230
1.06	.0583	1.50	.4055	1.94	.6627	2.38	.8671	2.82	1.0367
1.07	.0677	1.51	.4121	1.95	.6678	2,39	.8713	2.83	1.0403
1.08	.0770	1.52	.4187	1.96	.6729	2.40	.8755	2.84	1.0438
1.09	.0862	1.53	.4253	1.97	.6780	2.41	.8796	2.85	1.0473
1.10	.0953	1.54	.4318	1.98	.6831	2.42 2.43	.8838 .8879	2.86	1.0508
1.11	.1133	1.56	.4447	2.00	.6931	2.44	.8920	2.88	1.0578
1.13	.1222	1.57	.4511	2.01	.6981	2.45	.8961	2.89	1.0613
1.14	.1310	1.58	.4574	2.02	.7031	2.46	.9002	2.90	1.0647
1.15	.1398	1.59	.4637	2.03	.7080	2.47	.9042	2.91	1.0682
1.16	.1484	1.60	.4700	2.04	.7129	2.48	.9083	2.92	1.0716
1.17	.1570	1.61	.4762	2.05	.7178	2.49 2.50	.9123	2.93	1.0750
1.18 1.19	.1740	1.63	.4886	2.07	.7275	2.51	.9203	2.95	1.0813
1.20	.1823	1.64	.4947	2.08	.7324	2,52	.9243	2.96	1.0852
1.20 1.21 1.22 1.23	.1906	1.65	.5008	2.09	.7372	2.53	.9282	2.97	1.0886
1.22	.1988	1.66	.5068	2.10	.7419	2.54	.9322	2.98	1.0919
1.23	.2070	1.67	.5128	2.11	.7467	2.55	.9361	2.99	1.0953
1.24 1.25 1.26 1.27 1.28 1.29 1.30	.2151	1.68	.5188	2.12	.7514 .7561	2.56 2.57	.9400	3.00	1.0986
1 26	.2311	1.70	.5306	2.14	.7608	2.58	.9478	3.02	1.1019
1.27	.2390	1.71	.5365	2.15	.7655	2.59	.9517	3.03	1.1086
1.28	.2469	1.72	.5423	2.13	.7701	2.60	.9555	3.04	1.1119
1.29	.2546	1.73	.5481	2.17	.7747	2.61	.9594	3.05	1.1151
1.30	.2624	1.74	.5539	2.18	.7793	2.62	.9632	3.06	1.1184
1.31 1.32	.2776	1.75	.5596	2.19	.7839 .7885	2.63	.9670 .9708	3.07	1.1217
1.33	.2852	1.77	.5710	2.21	.7930	2.65	.9746	3.09	1.1249
1.34	.2927	1.78	.5766	2.22	.7975	2.66	.9783	3.10	1.1314
1.35	.3001	1.79	.5822	2.23	.8020	2.67	.9821	3.11	1.1346
1.36	.3075	1.80	.5878	2.24	.8065	2.68	.9858	3.12	1.1378
1.37 1.38	.3148	1.81	.5933	2.25	.8109	2.69	9895	3.13	1.1410
1.38	.3221	1.83	.5988	2.26 2.27	.8154 .8198	2.70	.9933	3.14	1.1442
1.40	.3365	1.84	.6098	2.28	.8242	2.72	1.0006	3 16	1.1506
1.41	.3436	1.85	.6152	2.29	.8286	2.73	1.0043	3.17	1.1537
1.42	.3507	1.86	.6206	2.30	.8329	2.74	1.0080	3.18	1.1569
1.43	.3577	1.87	.6259	2.31	.8372	2.75	1.0116	3.19	1.1600
1.44	.3646	1.88	.6313	2.32	.8416	2.76	1.0152	3.20	1.1632
		1					' <u>'</u>	-	

No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
3 91	1.1663	3.87	1.3533	4.53	1.5107	5.19	1.6467	5.85	1 7664
$\frac{3.21}{3.22}$	1.1694	3.88	1.3558	4.54	1.5129	5.20	1.6487	5.86	1.7664 1.7681
3.23	1.1725	3.89	1.3584	4.55	1.5151	5.21	1.6506	5.87	1.7699 1.7716 1.7733
$\frac{3.24}{3.25}$	1.1756 1.1787	3.90	1.3610 1.3635	4.56	1.5173 1.5195	5.22 5.23	1.6525	5.88	1.7710
3.26	1.1817	3.92	1.3661	4.58	1.5217	5.24	1.6563	5.90	1.7750
3.27	1.1848	3.93	1.3686	4.59	1.5239 1.5261	5.25 5.26	1.6582	5.91	1.7766 1.7783
3.28 3.29	1.1878 1.1909	3.94	1.3712	4.61	1.5282	5.27	1.6601	5.92 5.93	1.7800
3.30	1.1939	3.96	1.3762	4.62	1.5304	5.28	1.6639	5.94	1.7817
3.31	1.1969 1.1999	3.97	1.3788	4.63	1.5326 1.5347	5.29 5.30	1.6658	5.95 5.96	1.7834
3.33	1.2030	3.99	1.3838	4.65	1.5369	5.31	1 6696	5.97	1.7867
3.34	1.2060	4.00	1.3863	4.66	1.5390	5.32	1.6715 1.6734 1.6752	5.98	1 2004
3.35	1.2090	4.01	1.3888	4.68	1.5412 1.5433	5.33	1.6734	5.99	1.7901 1.7918 1.7984 1.7951 1.7967
3.37	1.2119 1.2149	4.03	1.3938	4.69	1.5454	5.35	1.6771	6.01	1.7934
3.38	1.2179	4.04	1.3962	4.70	1.5476	5.36	1.6771 1.6790	6.02	1.7951
3.39	1.2208 1.2238	4.05	1.3987	4.71	1.5497 1.5518	5.37	1.6808 1.6827	6.03	1.7967
3.41	1.2267	4.07	1.4036	4.73	1.5539	5.39	1.6845	6.05	1.8001
3.42	1.2296	4.08	1.4061	4.74	1.5560	5.40	1.6864	6.06	1.8017
$\frac{3.43}{3.44}$	1.2326 1.2355	4.09	1.4085	4.75	1.5581 1.5602	5.41 5.42	1.6882	6.07	1.8034 1.8050
3.45	1.2384	4.11	1.4134	4.77	1.5623	5.43	1.6919	6.08	1.8066
3.46	1.2413	4.12	1.4159	4.78	1.5644	5.44	1.6938	6.10	1.8083
3.47	1.2442	4.13	1.4183	4.79	1.5665	5.45	1.6956	6.11	1.8099
$\frac{3.48}{3.49}$	$1.2470 \\ 1.2499$	4.14	1.4207	4.80	1.5686	5.46	1.6974 1.6993	6.12	1.8116 1.8132
3.50	1.2528	4.16	1.4255	4.82	1.5707 1.5728	5.48	1.7011	6.14	1.8148
3.51	1.2556	4.17	1.4279	4.83	1 5748	5.49	1.7011 1.7029 1.7047 1.7066	6.15	1.8165
3.52 3.53	1.2585 1.2613	4.18	1.4327	4.85	1.5769 1.5790	5.50	1.7047	6.16	1.8181
3.54	1.2641	4.20	1.4351	4.86	1.5810	5.52	1.7084	6.18	1.8213
3.55	1.2669	4.21 4.22	1.4375 1.4398	4.87	1.5831	5.53	1.7102	6.19	1.8229
$\frac{3.56}{3.57}$	1.2698 1.2726	4.23	1.4422	4.89	1.5851 1.5872	5.54	1.7138	6.20	1.8245 1.8262
3.58	1.2754	4.24	1.4446	4.90	1.5892	5.56	1.7156	6.22	1.8278
3.59	1.2782 1.2809	4.25	1.4469 1.4493	4.91	1.5913 1.5933	5.57	1.7174	6.23	1.8294
3.61	1.2837	4.27	1.4516	4.93	1.5953	5.59	1.7210	6.25	1.8326
3.62	1.2865	4.28	1.4540	4.94	1.5974	5.60	1.7228 1.7246	6.26	1.8342
3.63 3.64	1.2892 1.2920	4.29	1.4563	4.95	1.5994 1.6014	5.61 5.62	1.7246	6.27	1.8358 1.8374
3.65	1.2947 1.2975 1.3002	4.31	1.4609	4.97	1.6034	5.63	1.7281	6.29	1.8390
3.66	1.2975	4.32	1.4633	4.98	1.6054	5.64	1.7281 1.7299 1.7317	6.30	1.8405
3.67 3.68	1.3002 1.3029	4.33	1.4656 1.4679	4.99 5.00	1.6074 1.6094	5.65	1.7317	6.31	1.8421
3.69	1.3056	4.34 4.35 4.36	1.4702	5.01	1.6114	5.67	1.7352	6.33	1.8453
3.70	1.3083	4.36	1.4725	5.02	1.6134	5.68	1.7370	6.34	1.8469
3.71	1.3110 1.3137	4.37	1.4748	5.03	1.6154 1.6174	5.69 5.70	1.7387	6.35	1.8485 1.8500
3.72 3.73	1.3164	4.39	1.4793	5.05	1.6194	5.71	1.7422	6.37	1.8516
3.74	1.3191	4.40	1.4816	5.06	1.6214	5.72	1.7440	6.38	1.8532
$\frac{3.75}{3.76}$	1.3218 1.3244	4.41	1.4839 1.4861	5.07	1.6233 1.6253	5.73	1.7457	6.39	1.8547
3.77	1.3271	4.43	1.4884	5.09	1.6273	5.75	1.7492	6.41	1 8579
3.78	1.3297	4.44	1.4907	5.10	1.6292	5.76	1.7509	6.42	1.8594
$\frac{3.79}{3.80}$	1.3324 1.3350	4.45	1.4929 1.4951	5.11 5.12	1.6312 1.6332	5.77	1.7527 1.7544	6.43	1.8610 1.8625
3.81	1.3376	4.47	1.4974	5.13	1.6351	5.79	1 7561	6.45	1.8641
3.82	1.3403	4.48	1.4996	5.14	1.6371	5.80	1.7579	6.46	1.8656
3.83 3.84	1.3429 1.3455	4.49	1.5019 1.5041	5.15	1.6390 1.6409	5.81 5.82	1.7596	6.47	1.8672 1.8687
3.85	1.3481	4.51	1.5063	5.17	1.6429	5.83	1.7579 1.7596 1.7618 1.7630	6.49	1.8703
3.86	1.3507	4.52	1.5085	5.18	1.6448	5.84	1.7647	6.50	1.8718

No.	Log.	No.	Log.	No.	Log.	No.	Log.	No.	Log.
6.51	1.8733	7.15	1.9671	7.79	2.0528	8,66	2.1587	9.94	2,2966
6.52	1.8749	7.16	1.9685	7.80	2.0541	8.68	2.1610	9.96	2.2986
6.53	1.8764	7 17	1.9699	7.81	2.0554	8.70	2.1633	9.98	2.3006
6.54	1.8779	7.18	1.9713	7.82 7.83	2.0567	8.72	2.1656	10.00	2.3026
6.55	1.8795 1.8810	7.18 7.19 7.20	1.9727 1.9741	7.84	2.0580 2.0592	8.74 8.76	2.1679 2.1702	10.25 10.50	2.3279 2.3513
6.57	1.8825	7.21	1.9754	7.85	2.0605	8.78	2.1725	10.75	2.3749
6.58	1.8840	7.22	1.9769	7.86	2.0618	8.80	2.1748	11.00	2.3979
6.59	1.8856	7.23 7.24	1.9782	7.87	2.0631 2.0643	8.82	2.1770 2.1793	11.25 11.50	2.4201 2.4430
6.60	1.8871 1.8886	7.25	1.9810	7.89	2.0656	8.86	2.1815	11.75	2.4636
6.62	1.8901	7.26	1.9824	7.90	2.0669	8.88	2.1838	12.00	2.4849
6.63	1.8916	7.27	1.9838	7.91	2.0681	8.90	2.1861	12.25	2.5052
6.64	1.8931 1.8946	7.28	1.9851 1.9865	7.92	2.0694 2.0707	8.92 8.94	2.1883 2.1905	12.50 12.75	2.5262 2.5455
6.66	1.8961	7.30	1.9879	7.94	2.0719	8.96	2.1928	13.00	2.5649
6.67	1.8976	7.31	1.9892	7.95	2.0732	8.98	2.1950	13.25	2.5840
6.68	1.8991	7.32	1.9906	7.96	2.0744	9.00	2.1972	13.50	2.6027
6.69	1.9006 1.9021	7.33	1.9920 1.9933	7.97	2.0757 2.0769	9.02 9.04	2.1994 2.2017	13.75	2.6211 2.6391
6.70 6.71 6.72	1.9036	7.35	1.9947	7.99	2.0782	9.06	2.2039	14.25	2.6567
6.72	1.9051	7.36	1.9961	8.00	2.0794	9.08	2.2061	14.50	2.6740
6.73	1.9066	7.37	1.9974	8.01	2.0807	9 10	2.2083	14.75	2.6913
6.74	1.9081	7.38	1.9988 2.0001	8.02	2.0819 2.0832	9.12	2.2105 2.2127	15.00 15.50	2.7081
6.76	1.9110	7.40	2.0015	8.04	2.0844	9.16	2.2148	16.00	2.7726
6.77	1.9125	7.41	2.0028	8.05	2.0857	9.18	2.2170	16.50	2.8034
6.78 6.79	1.9140	7.42	2.0041	8.06	2.0869	9.20	2.2192	17.00	2.8332
6.80	1.9155 1.9169	7.43	2.0055 2.0069	8.07	2.0882 2.0894	9.22 9.24	2.2214 2.2235	17.50 18.00	2.8621 2.8904
6.81	1.9184	7.45	2.0082	8.09	2.0906	9.26	2.2257	18.50	2.9173
6.82	1.9199	7.46	2.0096	8.10	2.0919	9.28	2,2279	19.00	2.9444
6.83	1.9213	7.47	2.0108	8.11	2.0931	9.30	2.2300	19.50	2.9703
6.84	1.9228 1.9242	7.48	2.0122 2.0136	8.13	2.0943 2.0956	9.32	2.2322 2.2343	20.00 21	2.9957 3.0445
6.86	1.9257	7.50	2.0149	8.14	2.0968	9.36	2.2364	22	3.0910
6.87	1.9272	7.51	2.0162	8.15	2.0980	9.38	2.2386	23	3.1355
6.88	1.9286	7.52 7.53	2.0176 2.0189	8.16	2.0992 2.1005	9.40	2.2407 2.2428	24 25	3.1781 3.2189
6.90	1.9301	7.54	2.0202	8.18	2.1003	9.44	2.2450	26	3.2581
6.91	1.9330	7.55	2.0215	8.19	2.1029	9.46	2.2471	27	3.2958
6.92	1.9344	7.56	2.0229	8.20	2.1041	9.48	2.2492	28	3.3322
6.93	1.9359 1.9373	7.57 7.58	2.0242 2.0255	8.22 8.24	2.1066 2.1090	9.50 9.52	2.2513 2.2534	29 30	3.3673 3.4012
8.95	1.9387	7.59	2.0268	8.26	2.1114	9.54	2.2555	31	3.4340
6.96	1.9402	7.60	2.0281	8.28	2.1138	9.56	2.2576	32	3.4657
6.97	1.9416	7.61	2.0295 2.0308	8.30	2.1168	9.58	2.2597 2.2618	33	3.4965
6.98	1.9430	7.63	2.0321	8.34	2.1211	9.60	2.2638	34 35	3.5263 3.5553
7.00	1.9459	7.64	2.0334	8.36	2.1235	9.64	2.2659	36	3.5835
7.01	1.9473	7.65	2.0347	8.38	2.1258	9.66	2.2680	37	3.6109
$7.02 \\ 7.03$	1.9488	7.66	2.0360 2.0373	8.40	2.1282	9.68	2.2701 2.2721	38 39	3.6376
7.04	1.9516	7.68	2.0386	8.44	2.1330	9.72	2.2742	40	3.6636 3.6889
7.05	1.9530	7.69	2.0399	8.46	2.1353	9.72 9.74	2.2762	41	3.7136
7.06	1.9544	7.70	2.0412	8.48	2.1377	9.76	2.2783	42	3.7377
7.07	1.9559 1.9578	7.71 7.72	2.0425 2.0438	8.50	2.1401 2.1424	9.78	2.2803 2.2824	43 44	3.7612 3.7842
7.09	1.9587	7.73	2.0451	8.54	2.1448	9.82	2.2844	45	3.8067
7.10	1.9601	7.74	2.0464	8.56	2.1471	9.84	2.2865	46	3.8286
7 11	1.9615 1.9629	7.75	2.0477 2.0490	8.58	2.1494 2.1518	9.86 9.88	2.2885 2.2905	47 48	3.8501
7.12 7.13 7.14	1.9643	7.76	2.0503	8.62	2.1541	9.90	2.2905	48	3.8712 3.8918
7.14	1.9657	7.77	2.0516	8.64	2.1564	9.92	2.2946	50	3.9120

# NATURAL TRIGONOMETRICAL FUNCTIONS.

•	м.	Sine,	Co-Vers.	Cosec,	Tang.	Cotan.	Secant.	Ver. Sin.	Cosine,		
0	0	.00000	1,0000	Infinite		Infinite	1.0000		1.0000	90	0
-	15	.00436		229.18	.00436	229.18	1.0000	.00001	.99999	-	45
	30	.00873	.99127	114.59	.00873	114.59	1.0000	.00004	.99996		30
	45	.01309	.98691	76.397	.01309	76.390	1.0001	.00009	.99991		15
1	0	.01745	.98255	57.299	.01745	57.290	1.0001	.00015	.99985	89	0
	15	.02181	.97819	45.840	.02182	45.829	1.0002	.00024	.99976		45
	30	.02618	.97382	38.202	.02618	38.188	1.0003	.00034	.99966		30
	45	.03054	.96946	32.746	.03055	32.730	1.0005	.00047	.99953		15
2	0	.03490	.96510	28.654	.03492	28.636	1.0006	.00061	.99939	88	0
	15	.03926	.96074	25.471	.03929	25.452	1.0008	.00077	.99923		45
1	30	.04362	.95638	22.926	.04366	22.904	1.0009	.00095	.99905		30
	45	.04798	.95202	20.843	.04803	20.819	1.0011	.00115	.99885		15
3	0	.05234	.94766	19.107	.05241	19.081	1.0014	.00137	.99863	87	0
	15	.05669	.94331	17.639	.05678	17.611	1.0016	.00161	.99839		45
	30	.06105	.93895	16.380	.06116	16.350	1.0019	.00187	.99813		30
	45	.06540	,93460	15.290	.06554	15.257	1.0021	.00214	.99786		15
4	0	.06976	.93024	14.336	.06993	14.301	1.0024	.00244	.99756	86	0
	15	.07411	.92589	13.494	.07431	13.457	1.0028	.00275	.99725		45
	30	.07846	.92154	12.745	.07870	12.706	1.0031	.00308	.99692		30
	45	.08281	.91719	12.076	.08309	12.035	1.0034	.00343	.99656		15
5	0	.08716	.91284	11.474	.08749	11.430	1.0038	.00381	.99619	85	0
	15	.09150	.90850	10.929	.09189	10.883	1.0042	,00420	.99580	-	45
	30	.09585	.90415	10.433	.09629	10.385	1.0046	.00460	.99540		30
	45	.10019	.89981	9.9812		9.9310	1.0051	,00503	.99497		15
6	0	.10453	.89547		.10510	9.5144	1.0055	.00548	.99452	84	0
	15	.10453 .10887	.89113	9.1855	.10952	9.1309	1.0660	.00594	.99406	0.	45
	30	.11320	.88680	8.8337	.11393	8.7769	1.0065	.00643	.99357		30
	45	.11754	.88246	8.5079	.11836	8.4490	1.0070	.00693	.99307		15
7	1 0	.12187	.87813	8.2055		8.1443	1.0075	.00745	.99255	83	0
•	15	.12620	87380	7.9240	.12722	7.8606	1.0081	.00800		00	45
	30	.13053	.86947	7.6613			1.0086	.00856			30
	45	.13485	.86515		.13609		1.0092	.00918			15
8	0	.13917	.86083	7 1853	.14054	7.1154	1.0098	.00978	.99027	82	0
G	15	.14349	.85651	6.9690			1.0105	.01035		02	45
	30	.14781					1.0111	.01098			30
	45	.15212			15391	6.4971	1.0118	.01164			15
9	0	.15643	.84357	6.3924				.01231	.98769	81	0
ð	15	16074	.83926		.16286				.98700	91	45
	30	.16505						.01371	.98629		30
	45	16935			1718		1.0147	.01444			15
10	0				1763					80	0
10	15	.17365 .17794	.82206	5 6100	1808	5.5301	1.0162	.01519	.98481	00	45
	30	.18224				5.3955	1.0170				30
	45			5.3612							15
11	1 40	18652			19438						15
11					1989						45
	15 30	19509		5.1258	2034	5.0278	1.0196	.01921			30
		1993									
10	45	2036			2080		1.0214	.02093		=0	15
12	0	2079			.2125						45
	15	.21218	.7878	4.7130			1.023	.02277	.97728		
	30	.2164		4.0202	2216	9 4.5107	1.024	.02370			30
10	45	.22070		4.531			1.0258	.02466		- mm	15
13	0	.2249									0
	15	.2292									45
	30	.2334		4.283	2400	8 4.165	1.028				30
	45	.2376									15
14		.2419	2 .7580								0
	15	.2461	5 .7538	5  4.062							45
	30	.2503									30
	45	.2546								5	15
15	0	.2588	2 .7411	8   3.863	7 .2679	5 3.732	1.035	.0340	.96593	75	0
		a	Y7. C1		10.	m.	0	G. W	C**-	0	1
	1	Cosine	Ver, Sir	. Secant.	Cotan	. Tang.	Cosec.	Co - Vers	. Sine.	1 °	M.
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From 75° to 90° read from bottom of table upwards.

۰	м.	Sine.	Co-Vers.	Cosec.	Tang.	Cotan.	Secant.	Ver. Sin.	Cosine.		
15	0	.25882	.74118	3.8637	.26795	3.7320	1.0353	.03407	.96693	75	0
19	15	.26303	.73697	3.8018		3.6680	1.0365	.03521	.96479	40	45
	30	,26724	.73276	3.7420	.27732	3.6059	1.0377	.03637	.96363		30
	45	.27144	.72856		.28203	3.5457	1.0390	.03754	.96246		15
16	0	.27564	.72436	3.6280	.28674	3.4874	1.0403	.03874	.96126	74	0
	15	.27983	.72017	3.5736	.29147	3.4308	1.0416	.03995	.96005		45
	30	.28402	.71598	3.5209	.29621	3.3759	1.0429	.04118	.95882		30
	45	.28820	.71180	3.4699	.30096	3.3226	1.0443	.04243	.95757		15
17	0	.29237	.70763	3.4203	.30573	3.2709	1.0457	.04370	.95630	73	0
	15	.29654	.70346	3.3722		3.2205	1.0471	.04498	.95502		45
	30	.30070	.69929	3.3255	.31530	3.1716	1.0485	.04628	.95372		30
	45	.30486	.69514	3.2801	.32010	3.1240	1.0500	.04760	.95240		15
18	0	.30902	.69098	3.2361	.32492	3.0777	1.0515	.04894	.95106	72	0
	15	.31316	.68684	3.1932	.32975	3.0326	1.0530	.05030	.94970		45
	30	.31730	.68270	3.1515	.33459	2.9887	1.0545	.05168	.94832		30
40	45	.32144	.67856	3.1110	.33945	2.9459	1.0560	.05307	.94693	P. 1	15
19	0 15	.32557	.67443 .67031	3.0715 3.0331	.34433	2.9042 2.8636	1.0576 1.0592	.05448	.94552 .94409	71	0 45
	30	.33381	.66619	2.9957	.35412	2.8239	1.0608	05091	.94264		30
	45	.33792	.66208	2.9593	.35904	2.7852	1.0625	.05736 .05882	.94118		15
20	0	.34202	65798	2.9238	.36397	2.7475	1.0642	.06031	.93969	70	0
20	15	.34612	65388	2.8892		2.7106	1.0659	.06181	.93819	••	45
	30	.35021	.64979	2.8554	.37388	2.6746	1.0676	.06333	.93667		30
	45	.35429	.64571	2.8225	.37887	2.6395	1.0694	.06486	.93514		15
21	Õ	.35837	.64163	2.7904	-38386	2.6051	1.0711	.06642	.93358	69	0
	15	.36244	.63756	2.7591	.38888	2.5715	1.0729	.06799	.93201		45
	30	.36650	.63350	2.7285	.39391	2.5386	1.0748	.06958	.93042		30
	45	.37056	.62944		.39896	2.5065	1.0766	.07119	.92881		15
22	0	.37461	.62539	2.6695	.40403	2.4751	1.0785	.07282	.92718	68	0
	15	.37865	.62135	2.6410		2.4443	1.0804	.07446	.92554		45
	30	.38268	.61732	2.6131	.41421	2.4142	1.0824	.07612	.92388		30
	45	.38671	.61329	2.5859	.41933	2.3847	1.0844	.07780	.92220	0.5	15
23	0	.39073	.60927	2.5598	.42447	2.3559	1.0864	.07950	.92050	67	0
	15 30	.39474	.60526		.42963	2.3276 2.2998	1.0884	.08121	.91879		45 30
	45	.40275	.60125	2.5078 2.4829	.44001	2 2727	1.0904	.08469	.91706 .91531		15
24	0	.40674	.59326	2.4586		2.2460	1.0946	.08645	.91355	66	10
44	15	.41072	.58928	2.4348	.45047	2.2199	1.0968	.08824	.91176	00	45
	30	.41469	.58531	2.4114	.45573	2.1943	1.0989	.09004	.90996		30
	45	41866	.58134	2.3886	.46101	2.1692	1.1011	.09186	.90814		15
25	0	.42262	.57738	2.3662		2.1445	1.1034	.09369	.90631	65	0
	15	.42657	.57343	2.3443		2.1203	1.1056	.09554	.90446		45
	30	.43051	.56949	2.3228	.47697	2.0965	1.1079	.09741	.90259		30
	45	.43445	.56555	2.3018	. 48234	2.0732	1.1102	.09930	.90070		15
26	0	.43837	.56163	2.2812	.48773	2.0503	1.1126	.10121	.89879	64	0
	15	.44229	.55771	2.2610	.49314	2.0278	1.1150	.10313	.89687		45
	30	.44620	.55380	2.2412	49858	2.0057	1.1174	.10507	.89493		30
27	45	.45010	.54990 .54601	2.2217 2.2027	.50404	1.9840 1.9626	1.1198	.10702	.89298 .89101	63	15 0
24	15	.45399 .45787	.54213	2.1840	.51503	1.9416	1.1223 1.1248	.11098	.88902	00	45
	30	.46175	.53825	2.1657	.52057	1.9210	1.1274	.11299	.88701		30
	45	.46561	.53439	2.1477	.52612	1.9007	1.1300	.11501	.88499		15
28	0	.46947	.53053	2.1300	.53171	1.8807	1.1326	.11705	.88295	62	0
	15	.47332	.52668	2.1127	.53732	1.8611	1.1352	.11911	.88089	التنا	45
	30	.47716	.52284	2.0957	.54295	1.8418	1.1379	.12118	.87882		30
	45	.48099	.51901	2.0790	.54862	1.8228	1.1406	.12327	.87673		15
29	0	.48481	.51519	2.0627	.55431	1.8040	1.1433	12538	.87462	61	0
	15	. 48862	.51138	2.0466	.56003	1.7856 1.7675	1.1461	.12750	.87250		45
	30	.49242	.50758	2.0308	.56577	1.7675	1.1490	.12964	.87036		30
	45	.49622	.50378	2.0152	.57155	1.7496	1.1518	.13180	.86820	0.0	15
30	0	.50000	.50000	2.0000	.57735	1.7320	1.1547	.13397	.86603	60	0
								G 71	01	۰	
		Cosine.	Ver. Sin.	Secant.	Cotan.	Tang.	Cosec.	Co-Vers.	Sine.	0	M.
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•	м.	Sine.	Co-Vers.	Cosec.	Tang.	Cotan,	Secant,	Ver. Sin.	Cosine,		
30	0	.50000	.50000	2.0000	.57735	1.7320	1.1547	.13397	.86603	60	0
	15	.50377	.49623	1.9850	.58318	1.7147	1.1576	.13616	.86384		45
	30	.50754	.49246	1.9703	.58904	1.6977	1.1606	.13837	.86163		30
31	45	.51129 .51504	.48871 .48496	1.9558 1.9416	.59494 .60086	1.6808 1.6643	1.1636 1.1666	.14059	.85941 .85717	59	15 0
91	15	.51877	.48123	1.9276	.60681	1.6479	1.1697	.14509	.85491	99	45
	30	.52250	.47750	1.9139	.61280	1.6319	1.1728	.14736	.85264		30
	45	.52621	.47379	1.9004	.61882	1.6160	1.1760	.14965	.85035		15
32	0	.52992	.47008	1.8871	.62487	1.6003	1.1792	.15195	.84805	58	0
	15	.53361	.46639	1.8740	.63095	1.5849	1.1824	.15427	.84573		45
	30	.53730	.46270	1.8612	.63707	1.5697	1.1857	.15661	.84339		30
	45	.54097	.45903	1.8485	.64322	1.5547	1.1890	.15896	.84104	- N	15
33	0	.54464	.45536	1.8361	.64941	1.5399	1 1924	.16133	.83867	57	45
	15 30	.54829 .55194	.45171	1.8238 1.8118	.65563 .66188	1.5253 1.5108	1.1958 1.1992	.16371	.83629 .83389		30
	45	55557	.44443	1.7999	.66818	1.4966	1.2027	.16853	.83147		15
34	0	.55919	.44081	1.7883	.67451	1.4826	1.2062	.17096	.82904	56	0
~~	15	.56280	.43720	1.7768	.68087	1.4687	1.2098	.17341	.82659		45
	30	.56641	.43359	1.7655	.68728	1.4550	1.2134	.17587	.82413		30
	45	.57000	.43000	1.7544	.69372	1.4415	1.2171	.17835	.82165		15
35	0	.57358	.42642	1.7434	.70021	1.4281	1.2208	.18085	.81915	55	0
	15	.57715	.42285	1.7327	.70673	1.4150	1.2245 1.2283	.18336	.81664		45 30
	30 45	.58070 .58425	.41930 .41575	1.7220	.71329 .71990	1.4019 1.3891	1.2322	.18588	.81412 .81157		15
36	0	.58779	.41221	1.7013	.72654	1.3764	1.2361	19098	.80902	54	0
90	15	.59131	.40869	1.6912	.73323	1.3638	1.2400	.19356	.80644	01	45
	30	.59482	.40518	1.6812	.73996	1.3514	1.2440		.80386		30
	45	.59832	.40168	1.6713	.74673	1.3392	1.2480		.80125		15
37	0	.60181	.39819	1.6616	.75355	1.3270	1.2521	.20136	.79864	53	0
	15	.60529	.39471	1.6521	.76042	1.3151	1.2563	.20400	.79600	1	45
	30	.60876	.39124	1.6427	.76733	1.3032	1.2605	.20665	.79335		30
38	45	.61222 .61566	.38778 .38434	1.6334 1.6243	.77428 .78129	1.2915 1.2799	1.2647 1.2690	.20931	.79069	52	15 0
99	15	.61909	.38091	1.0345	.78834	1.2685	1.2734		.78532	92	45
	30	.62251	.37749	1.6064	.79548	1.2572	1.2778		.78261		30
	45	.62592	.37408	1.5976	.80258	1.2460	1.2822		77988		15
39	0	.62932	.37068	1.5890	.80978	1,2349	1.2868	. 22285	.77715 .77439 .77162	51	0
	15	.63271	.36729	1.5805	.81703	1.2239	1.2913		.77439		45
	30	.63608	.36392	1.5721	.82434	1.2131 1.2024	1.2960		.77162		30
10	45	.63944	.36056	1.5639	.83169	1.2024	1.3007	.23116		50	15
40	0 15	.64279	.35721 .35388	1.5557 1.5477	.83910 .84656	1.1918 1.1812	1.3054 1.3102		.76604 .76323	90	0 45
	30	.64945	.35055	1.5398	.85408	1.1708	1.3151	.23959			30
	45	.65276	.34724	1.5320	.86165	1.1606	1.3200		.75756		15
41	0	.65606	.34394	1 5242	.86929	1.1504	1.3250	.24529	.75471	49	0
	15	.65935	.34065	1.5166	.87698	1.1403	1.3301	.24816	.75184		45
	30	.66262	.33738	1 5092	.88472	1.1303	1.3352		.74896		30
10	45	.66588	.33412	1.5018	.89253	1.1204	1.3404	. 25394	.74606	48	15
42	15	66913	.33087	1.4945	.90040	1.1106	1.3456		.74314	43	0
	15 30	.67237 .67559	.32763	1.4873 1.4802	.90834	1.1009 1 0913	1.3509 1.3563		.74022		45 30
	45	.67880	.32120	1.4732	.92439	1.0818	1.3618	.26568	.73432		15
43	0	.68200	.31800	1.4663	93251	1.0724	1.3673	.26865	.73135	47	0
	15	.68518	.31482	1.4595	.94071	1.0630	1.3729	.27163	.72837		45
	30	.68835	.31165	1.4527	.94896	1.0538	1.3786	.27463	.72537		30
	45	.69151	.30849	1.4461	.95729	1.0446	1.3843	.27764	.72236	10	15
44	0	.69466	.30534	1.4396	.96569	1.0355	1.3902	.28066	.71934	46	0
	15 30	.69779	.30221	1.4331	.97416	1.0265	1.3961	.28370	.71630		45
	45	.70091 .70401	.29909	1.4267 1.4204	0.98270 $0.99131$	1.0176	1.4020 1.4081	.28675	.71325 .71019		30 15
45	1 40	.70711	.29289	1.4204		1.0000	1.4081	.29289	.70711	45	19
TO.	-			1.7140		1.0000	1.7140				-
		Cosine	Ver. Sin.	Secant.	Cotan.	Tang.	Cosec.	Co-Vers.	Sine,	0	M.
0		Journe.		Scound.	Journa.	Tung.	00000		, J	1	-
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From 45° to 60° read from bottom of table upwards.

# LOGARITHMIC SINES, ETC.

Deg.	Sine.	Cosec.	Versin.	Tangent.	Cotan.	Covers.	Secant.	Cosine.	Deg.
0	In Neg	Infinite.	In.Neg.	In.Neg.	Infinite.	10.00000	10,00000	10.00000	90
1	8.24186	11.75814	6.18271	8.24192	11.75808		10.00007	9.99993	89
2 3	8.54282	11.45718	6.78474	8.54308	11.45692	9.98457	10.00026	9.99974	88
3		11.28120	7.13687		11.28060		10.00060	9.99940	
4	8.84358	11.15642	7.38667	8.84464	11.15536	9.96860	10.00106	9.99894	86
5	8.94030	11.05970	7,58039	8.94195	11.05805	9.96040	10.00166	9.99834	85
6	9.01923	10.98077	7.73863 7.87238	9.02162	10.97838	9.95205	10.00239	9.99761	84
7 8	9.08589	10.91411	7.87238	9.08914	10.91086	9.94356	10.00325	9.99675	83
8	9.14356	10.85644	7.98820		10.85220	9.93492	10.00425	9.99575	82
9	9.19433	10.80567	8.09032	9.19971	10.80029	9.92612	10.00538	9.99462	81
10	9.23967	10.76033	8.18162	9.24632	10.75368	9,91717	10.00665	9,99335	80
11		10.71940	8.26418	9.28865	10.71135	9.90805	10.00805	9.99195	79
12		10.68212	8.33950		10.67253	9.89877	10.00960	9.99040	78
13		10.64791	8.40875		10.63664		10.01128	9.98872	77
14	9.38368	10.61632	8.47282	9.39677	10.60323	9.87971	10.01310	9.98690	76
15	9,41300	10.58700	8.53243	9,42805	10.57195	9.86992	10.01506	9.98494	75
16		10.55966	8,58814	9.45750	10.54250	9.85996	10.01716	9.98284	74
17		10.53406	8.64043		10.51466		10.01940	9.98060	
18		10.51002	8.68969		10.48822	9.83947	10.02179	9.97821	72
19	9.51264	10.48736	8.73625	9.53697	10.46303	9.82894	10.02433	9.97567	71
20	9 53405	10.46595	8.78037	9 56107	10.43893	9 81821	10.02701	9.97299	70
21		10.44567	8.82230		10.41582	9.80729	10.02985	9.97015	69
22	9.57358	10.42642	8.86223	9.60641	10.39359	9.79615	10.03283	9.96717	68
23		10.40812	8,90034		10.37215		10.03597	9.96403	
24	9.60931	10.39069	8.93679	9.64858	10.35142	9.77325	10.03927	9.96073	66
25	9 62595	10.37405	8.97170	9 66867	10.33133	9.7614€	10.04272	9.95728	65
25 26		10.35816	9.00521		10.31182	9.74945	10.04634	9.95366	64
27	9.65705	10.34295	9.03740	9.70717	10.29283	9.73720	10.05012	9.94988	63
28 29		10.32839	9.06838		10.27433	9.72471	10.05407	9.94593	62
29	9.68557	10.31443	9.09823	9.74375	10.25625	9.71197	10.05818	9.94182	61
30	9 69892	10.30103	9,12702	9 76144	10.23856	9.69897	10.06247	9.93753	60
31		10.28816	9.15483		10.22123	9.68571	10.06693	9.93307	59
32	9.72421	10.27579	9.18171	9.79579	10.20421	9.67217	10.07158	9.92842	58
33	9.73611	10.26389	9.20771				10.07641	9.92359	57
34	9.74756	10.25244	9.23290	9.82899	10,17101	9.64425	10.08143	9.91857	56
35	0 75850	10.24141	9.25731	0 84593	10.15477	9.62984	10.08664	9,91336	55
36		10.23078	9.28099		10.13874		10.00004	9.90796	54
37		10.22054	9,30398		10.12289		10.09765	9.90235	53
38	9.78934	10.21066	9.32631	9.89281	10.10719	9.58471	10.10347	9.89653	52
39	9.79887	10.20113	9.34802	9.90837	10.09163		10.10950	9.89050	51
40	0 80800	10.19193	9,36913	9.92381	10.07619	9.55293	10.11575	9.88425	50
41	9.81694	10.18396	9.38968		10.06084		10.11273	9.87778	49
42		10.17449	9.40969		10.04556		10.12893	9.87107	48
43	9.83378	10.16622	9.42918	9.96966	10.03034	9.50243	10.13587	9.86413	47
44	9.84177	10.15823	9.44818	9.98484	10.01516	9.48479	10.14307	9.85693	46
45	9.84949	10.15052	9.46671	10.00000	10.00000	9.46671	10.15052	9.84949	45
	Conte	Connect	Comon	Coton		W-mate.	Coming	Cinn	
	·Cosine.	Secant.	Covers.	Cotan,	Tangent.	Versin.	Cosec.	Sine.	
-									_

From 45° to 90° read from bottom of table upwards.

#### MATERIALS.

# THE CHEMICAL ELEMENTS.

#### The Common Elements (42).

Chemical Symbol.	Name.	Atomic Weight,	Chemical Symbol.	Name.	Atomic Weight.	Chemical Symbol.	Name,	Atomic Weight.
Al Sb As Ba Bi B Br Cd Ca C Cl Cr Co Cu	Aluminum Antimony Arsenic Barium Bismuth Boron Bromine Cadmium Carbon Chlorine Chromium Cobalt Copper	27.1 120. 75. 137. 208. 10.9 79.8 111.8 40. 12. 35.4 52.3 59. 63.2	F Au H I Ir Fe Pb Li Mg Mn Hg Ni N O	Fluorine Gold Hydrogen Iodine Iridium Iron Lead Lithium Magnesium Manganese Mercury Nickel Nitrogen Oxygen	19. 196.2 1. 126.6 193. 56. 206.4 7.01 24. 55. 199.8 58.3 14. 15.96	Pd PP Pt K Si Ag Na Sr Sr Sn Ti W Va Zn	Palladium Phosphorus Platinum Potassium Silicon Silver Sodium Strontium Sulphur Tin Titanium Tungsten Vanadium Zinc	106. 30.96 195. 39.03 28.4 107.7 23. 87.4 32. 118. 50. 184. 51.2 65.

The atomic weights of many of the elements vary in the decimal place as given by different authorities.

#### The Rare Elements (27).

Beryllium, Be. Cæsium, Cs. Cerium, Ce. Didymium, D. Erbium, E. Gallium, Ga. Germanium, Ge.

Glucinum, G. Indium, In. Lanthanum, La. Molybdenum, Mo. Niobium, Nb. Osmium, Os. Rhodium, R.

Rubidium, Rb. Ruthenium, Ru. Samarium, Sm. Scandium, Sc. Selenium, Se. Tantalum, Ta. Tellurium, Te.

Thallium, Tl. Thorium, Th. Uranium, U. Ytterbium, Yr. Yttrium, Y. Zirconium, Zr.

#### SPECIFIC GRAVITY.

The specific gravity of a substance is its weight as compared with the weight of an equal bulk of pure water.

To find the specific gravity of a substance. W = weight of body in air; w = weight of body submerged in water.

Specific gravity = 
$$\frac{W}{W-w}$$

If the substance be lighter than the water, sink it by means of a heavier substance, and deduct the weight of the heavier substance.

Specific-gravity determinations are usually referred to the standard of the weight of water at 62° F, 62.355 lbs, per cubic foot. Some experimenters have used 60° F. as the standard, and others 32° and 39.1° F. There is no general agreement.

Given sp. gr. referred to water at 39.1° F., to reduce it to the standard of 62° F. multiply it by 1.00112.

Given sp. gr. referred to water at 62° F., to find weight per cubic foot multiply by 62.355. Given weight per cubic foot, to find sp. gr. multiply by 0.016037. Given sp. gr., to find weight per cubic inch multiply by 0.30085.

## Weight and Specific Gravity of Metals.

	Specific Gravity. Range accord- ing to several Authorities.	Specific Grav- ity. Approx. Mean Value, used in Calculation of Weight.	Weight per Cubic Foot, lbs.	Weight per Cubic Inch, lbs.
AluminumAntimonyBismuth	2.56 to 2.71 6.66 to 6.86 9.74 to 9.90	2.67 6.76 9.82	166.5 421.6 612.4	.0963 .2439 .3454
Brass: Copper $+$ Zinc $\begin{cases} 80 & 20 \\ 70 & 30 \\ 60 & 40 \\ 50 & 50 \end{cases}$	7.8 to 8.6	$\begin{cases} 8.60 \\ 8.40 \\ 8.36 \\ 8.20 \end{cases}$	536.3 523.8 521.3 511.4	.3103 .3031 .3017 .2959
Bronze { Copper, 95 to 80 { Tin, 5 to 20 }	8.52 to 8.96	8.853	552.	.3195
Cadmium	8.6 to 8.7 1.58	8.65	539.	.3121
Chromium	5.0 8.5 to 8.6	40.000	1000.0	0040
Gold, pure Copper Iridium	19.245 to 19.361 8.69 to 8.92 22.38 to 23.	19.258 8.853	1200.9 552. 1396.	.6949 .3195 .8076
Iron, Cast	6.85 to 7.48 7.4 to 7.9	7.218 7.70	450. 480.	.2604 .2779
Lead. Manganese	11.07 to 11.44 7. to 8.	11.38 8.	709.7 499.	.4106
Magnesium		1.75 13.62 13.58	109. 849.3 846.8	.0641 .4915 .4900
Nickel	13.37 to 13.38 8.279 to 8.93	13.38 8.8	834.4 548.7	.4828
Platinum	20.33 to 22.07 0.865	21.5	1347.0	.7758
Silver	10.474 to 10.511 0.97 7.69* to 7.932†	10.505 7.854	655.1 489.6	.3791
TinTitanium	7.291 to 7.409 5.3	7.350	458.3	.2652
TungstenZinc	17. to 17.6 6.86 to 7.20	7.00	436.5	.2526

<sup>\*</sup> Hard and burned.

Yerry pure and soft. The sp. gr. decreases as the carbon is increased. In the first column of figures the lowest are usually those of cast metals, which are more or less porous; the highest are of metals finely rolled or drawn into wire.

# Specific Gravity of Liquids at 60° F.

Acid, Muriatic	1.200	Oil, Olive	.92
" Nitrie	1.217	" Palm	.97
" Sulphuric	1.849	" Petroleum	.78 to .88
Alcohol, pure95 per cent	.794	" Rape	.92
" 95 per cent	.816	" Turpentine	.87
50 " "	.934	" Whale	.92
Ammonia, 27.9 per cent	.891	Tar	1.
Bromine	2.97	Vinegar	1.08
Carbon disulphide	1.26	Water	1.
Ether, Sulphuric	.72	" sea	1.026 to 1.03
Oil, Linseed	.94		

# Compression of the following Fluids under a Pressure of 15 lbs. per Square Inch.

Water	.00004663	Ether	.00006158
Alcohol			

#### The Hydrometer.

The hydrometer is an instrument for determining the density of liquids. It is usually made of glass, and consists of three parts: (1) the upper part, a graduated stem or fine tube of uniform diameter; (2) a bulb, or enlargement of the tube, containing air; and (3) a small bulb at the bottom, containing shot or mercury which causes the instrument to float in a vertice position. The graduations are figures representing either specific gravities, or the numbers of an arbitrary scale, as in Beaumé's, Twaddell's, Beck's, and other bydrometers.

There is a tendency to discard all hydrometers with arbitrary scales and to use only those which read in terms of the specific gravity directly.

## Beaume's Hydrometer and Specific Gravities Compared.

_				T			Y	
e s	Liquids	Liquids	8 -9	Liquids	Liquids	S. co	Liquids	Liquids
3 6	Heavier	Lighter	ğΕ	Heavier	Lighter	ğΞ	Heavier	Lighter
5, 3	than	than	203	than	than	26.53	than	than
Degrees Beaumé.	Water,	Water,	Degree Beaum	Water,	Water,	e e	Water,	Water,
BL	sp. gr.	sp. gr.	HM	sp. gr.	sp. gr.	Degrees Beaumé.	sp. gr.	sp. gr.
0	1.000		19	1.143	.942	38	1.333	.839
1	1.007		20	1.152	.936	39	1.345	.834
2	1.013		21	1.160	.930	40	1.357	.830
3	1.020		22	1.169	.924	41	1.369	.825
5	1.027		23	1.178	.918	42	1.382	.820
5	1.034		24	1.188	.913	44	1.407	.811
6	1.041		25	1.197	.907	46	1.434	.802
7	1.048		26	1.206	.901	48	1.462	.794
8	1.056		27	1.216	.896	50	1.490	.785
9	1.063		28	1.226	.890	52	1.520	.777
10	1.070	1.000	29	1.236	.885	54	1.551	.768
11	1.078	.993	30	1.246	.880	56	1.583	.760
12	1.086	.986	31	1.256	.874	58	1.617	.753
13	1.094	.980	32	1.267	.869	60	1.652	.745
14	1.101	.973	33	1.277	.864	65	1.747	
15	1.109	.967	34	1.288	.859	70	1.854	
16	1.118	.960	35	1.299	.854	75	1.974	
17	1.126	.954	36	1.310	.849	76	2.000	
18	1.134	.948	37	1.322	.844			
-								

# Specific Gravity and Weight of Wood.

Specine Gravity and Weight of Wood.									
	Specific Grav	ity.	Weight per Cubic Foot, lbs.		Specific Gra	vity.	Weight per Cubic Foot, lbs.		
Apple	0.56 to 0.80 .73 to .79 .60 to .84 .31 to .40 .62 to .85 .56 to .74 .91 to 1.33 .49 to .75 .61 to .72	1.12 .68 .76 .72 .35 .73 .65 1.12 .62 .66 .56 .24 .53	47 45 22 46 41 70 39 41 35 15	Hornbeam Juniper Larch Lignum vitæ Linden Locust Mahogany. Mulberry Oak, Live " Red Pine, White	.76 .56 .55 to 1.33 .604 .728 .56 to 1.06 .57 to .79 .56 to .90 .96 to 1.26 .69 to .86 .73 to .75 .85 to .55	Avge. .76 .56 .56 1.00 .81 .68 .73 1.11 .77 .74	47 35 35 62 37 46 51 42 46 69 48 46		
Dogwood Ebony Fir Gum Hackmatack Hemlock Hickory Holly	1.13 to 1.33 1.55 to .78 .48 to .70 .84 to 1.00 .59 .36 to .41 .69 to .94	1.23 .61 .59 .92 .59 .38 .77	76 38 37 57 37 24 48	rine, White. "Yellow. Poplar. Spruce. Sycamore. Teak. Walnut Willow.	.35 to .55 .46 to .76 .38 to .58 .40 to .50 .59 to .62 .66 to .98 .50 to .67 .49 to .59	.45 .61 .48 .45 .60 .82 .58	38 30 28 37 51		

#### Weight and Specific Gravity of Stones, Brick, Cement, etc.

·	Pounds per Cubic Foot.	Specific Gravity.
Asphaltum	87	1.39
Brick, Soft	100 -	1.6
" Common	112	1.79
" Hard	125	2.0
" Pressed	135	2.16
" Fire	140 to 150	2.24 to 2.4
Brickwork in mortar	100	1.6
" cement	112	1.79
Cement, Rosendale, loose	60	.96
" Portland, "	78	1.25
Clay	120 to 150	1.92 to 2.4
Concrete	120 to 140	1.92 to 2.24
Earth, loose	72 to 80	1.15 to 1.28
" rammed	90 to 110	1.44 to 1.76
Emery	250	4.
Hass	156 to 172	2.5 to 2.75
" flint	180 to 196	2.88 to 3.14
Gneiss ( Granite (	160 to 170	2.56 to 2.72
Frante (		
Gravel	100 to 120	1.6 to 1.92
Gypsum	130 to 150	2.08 to 2.4
Hornblende	200 to 220 50 to 55	3.2 to 3.52 .8 to .88
Lime, quick, in bulk	170 to 200	2.72 to 3.2
Limestone	150	2.4
Magnesia, Carbonate	160 to 180	2.56 to 2.88
Marble	140 to 160	2.24 to 2.56
" dressed	140 to 180	2.24 to 2.88
Mortar	90 to 100	1.44 to 1.6
Pitch	72	1.15
Plaster of Paris	74 to 80	1.18 to 1.28
Quartz	165	2.64
Sand.	90 to 110	1.44 to 1.76
Sandstone	140 to 150	2.24 to 2.4
Slate	170 to 180	2.72 to 2.88
Stone, various	135 to 200	2.16 to 3.4
Trap	170 to 200	2.72 to 3.4
Tile	110 to 120	1.76 to 1.92
Soapstone	166 to 175	2.65 to 2.8

#### PROPERTIES OF THE USEFUL METALS.

Aluminum, Al.—Atomic weight 27.1. Specific gravity 2.6 to 2.7. The lightest of all the useful metals except magnesium. A soft, ductile, malleable metal, of a white color, approaching silver, but with a bluish cast. Very non-corrosive. Tenacity about one third that of wrought-iron. Formerly a rare metal, but since 1890 its production and use have greatly increased on account of the discovery of cheap processes for reducing it from the ore. Melts at about 1160° F. For further description see Aluminum, under Strength of Materials.

Antimony (Stibium), Sb.—At. wt. 120. Sp. gr. 6.7 to 6.8. A brittle metal of a bluish-white color and highly crystalline or laminated structure. Melts at 842° F. Heated in the open air it burns with a bluish-white flame. Its chief use is for the manufacture of certain alloys, as type-metal (antimony 1, lead 4), britannia (antimony 1, tin 9), and various anti-friction metals (see Alloys). Cubical expansion by heat from 32° to 212° F., 0.0070. Specific heat .050.

Bismuth, Bi.—At. wt. 208. Bismuth is of a peculiar light reddish color, highly crystalline, and so brittle that it can readily be pulverized. It melts at 510° F., and boils at about 200° F. Sp. gr. 9,823 at 54° F., and 10.055 just above the melting-point. Specific heat about .0301 at ordinary

temperatures. Coefficient of cubical expansion from 32° to 212°, 0.0040. Conductivity for heat about 1/56 and for electricity only about 1/80 of that of ductivity for neat about 1/30 and for electricity only about 1/30 of that of silver. Its tensile strength is about 6400 lbs, per square inch. Bismuth ex-pands in cooling, and Tribe has shown that this expansion does not take place until after solidification. Bismuth is the most diamagnetic element known, a sphere of it being repelled by a magnet; and on account of its marked thermo-electric properties it is much used in laboratories in the construction of delicate thermopiles.

In the arts bismuth is used chiefly in the preparation of alloys.

Cadmium, Cd.—At. wt. 112. Sp. gr. 8.6 to 8.7. A bluish-white metal, lustrous, with a fibrous fracture. Melts below 500° F. and volatilizes at about 680° F. It is used as an ingredient in some fusible alloys with lead,

about 680° F. It is used as an ingredient in some fusible alloys with lead, tin, and bismuth. Cubical expansion from 32° to 212° F., 0,0094.

Copper, Cu.—At. wt. 63.2. Sp. gr. 8.81 to 8.95. Fuses at about 1930°
F. Distinguished from all other metals by its reddish color. Very duetile and malleable, and its tenacity is next to iron. Tensile strength 20,000 to 30,000 lbs, per square inch. Heat conductivity 73.6% of that of silver, and superior to that of other metals. Electric conductivity equal to that of gold and silver. Expansion by heat from 32° to 212° F., 0,0051 of its volume. Specific heat .093. (See Copper under Strength of Materials; also Alloys.)

Gold (Aurum), Au.—At. wt. 197. Sp. gr., when pure and pressed in a die. 19.34. Melts at about 1915° F. The most malleable and ductile of all metals. One conce Troy may be beaten so as to cover 16° or the fourtage.

metals. One ounce Troy may be beaten so as to cover 160 sq. ft. of surface, The average thickness of gold-leaf is 1/282000 of an inch, or 100 sq. ft. per ounce. One grain may be drawn into a wire 500 ft. in length. The ductility is destroyed by the presence of 1/2000 part of lead, bismuth, or antimony, Gold is hardened by the addition of silver or of copper. In U. S. gold coin there are 90 parts gold and 10 parts of alloy, which is chiefly copper with a By jewelers the fineness of gold is expressed in carats, pure little silver. gold being 24 carats, three fourths fine 18 carats, etc.

Tridium.—Iridium is one of the rarer metals. It has a white lustre, resembling that of steel; its hardness is about equal to that of the ruby; in the cold it is quite brittle, but at a white heat it is somewhat malleable. It is one of the heaviest of metals, having a specific gravity of 22.38. When heated in the air to a red heat the metal is very slowly oxidized. It is insolved. uble in all single acids, but is very slightly soluble in aqua regia after being heated in the state of fine powder for many hours. In a massive state, how-

ever, aqua regia does not attack it.

Iridium is extremely infusible. With the heat of the oxyhydrogen or electric furnaces, a globule of very small size may be melted. Mr. John Holland found that by heating the ore in a Hessian crucible to a white heat Holland found that by heating the ore in a Hessian crucible to a white heat and adding to it phosphorus, and continuing the heating for a few minutes, he could obtain a perfect fusion of the metal, which could be poured out and cast into almost any desired shape. This material was about as hard as the natural grains of iridium, and contained, according to two determinations, 7:52% and 7:74% of phosphorus. By heating the metal in a bed of lime the phosphorus could be completely removed. In this operation the metal is first heated in an ordinary furnace at a white heat, and finally, after no more phosphorus makes its appearance. It is removed and placed in an effect of the furnace with a lime crucible, and where heated uttil the last traces of phosphorus are removed; the metal which then remains will resist as much heat without fusion as the native metal.

For uses of indium, methods of manufacturing it, etc., see paper by W. D. Dudley on the "Iridium Industry." Trans. A. I. M. E. 1881, Tron (Ferrum), Fe.—At. wt. 56. Sp. gr.: Cast, 6.85 to 7.48; Wrought, 7.4 to 7.9. Pure iron is extremely infusible, its melting point being above 3000° F., but its fusibility increases with the addition of carbon, cast iron fusing about \$500° F. Conductivity for heat 11.9, and for electricity 12 to 14.8, silver being 100. Expansion in bulk by heat: cast iron .0033, and wrought iron .0035, from 32° to 212° F. Specific heat: cast iron .1298, wrought iron .1138, steel .1165. Cast iron exposed to continued heat becomes permanently expanded 1½ to .3 per cent of its length. Grate-bars should therefore be allowed about 4 per cent play. (For other properties see Iron and Steel under Strength of Materials.)

Lead (Plumbum), Pb .- At. wt. 206.4. Sp. gr. 11.07 to 11.44 by different authorities. Melts at about 625° F., softens and becomes pasty at about 617° F. If broken by a sudden blow when just below the melting-point it is quite brittle and the fracture appears crystalline. Lead is very malleable and ductile, but its tenacity is such that it can be drawn into wire with great difficulty. Tensile strength, 1600 to 2400 lbs. per square inch. Its elasticity is very low, and the metal flows under very slight strain. Lead dissolves to some extent in pure water, but water containing carbonates or sulphates forms over it a film of insoluble salt which prevents further action. (For

alloys of lead see Alloys.)

Magnesium, Mg.—At. wt. 24. Sp. gr. 1.69 to 1.75. Silver-white, brilliant, malleable, and ductile. It is one of the lightest of metals, weighing only about two thirds as much as aluminum. In the form of filings, wire, or thin ribbons it is highly combustible, burning with a light of dazzling brilliancy, useful for signal-lights and for flash-lights for photographers. It is nearly non-corrosive, a thin film of carbonate of magnesia forming on exposure to damp air, which protects it from further corrosion. It may be alloyed with aluminum, 5 per cent Mg added to Al giving about as much increase of strength and hardness as 10 per cent of copper. Cubical expansion by heat 0.0083, from 32 vo 212 F. Melts at 120°F. Specific heat 25. Manganese, Mn.—At. wt. 55. Sp. gr. 7 to 8. The pure metal is not used in the arts, but alloys of manganese and iror, called spiegeleisen when

containing below 25 per cent of manganese, and ferro-manganese when containing from 25 to 90 per cent, are used in the manufacture of steel. Metallic manganese oxidizes rapidly in the air, and its function in steel manufacture is to remove the oxygen from the bath of steel whether it exists as oxide of

iron or as occluded gas,

Mercury (Hydrargyrum), Hg.-At. wt. 199.8. A silver-white metal, liquid at temperatures above—39° F., and boils at 680° F. Unchangeable as liquid at temperatures above—30° F., and boils at 680° F. Unchangeable as gold, silver, and platinum in the atmosphere at ordinary temperatures, but oxidizes to the red oxide when near its boiling-point. Sp. gr.: when liquid 3.58 to 13.59, when frozen 14.4 to 14.5. Easily tarnished by sulphur fumes, also by dust, from which it may be freed by straining through a cloth. No metal except iron or platinum should be allowed to touch mercury. The smallest portions of tin, lead, zinc, and even copper to a less extent, cause it to tarnish and lose its perfect liquidity. Coefficient of cubical expansion from 32° to 212° F. (182; per deg. .00010].

Nickel, Ni.—At. wt. 58.3. Sp. gr. 8.27 to 8.93. A silvery-white metal with a strong lustre, not tarnishing on exposure to the air. Ductile, hard, and as tenacious as iron. It is attracted to the magnet and may be made magnetic like iron. Nickel is very difficult of fusion making at shout.

magnetic like iron. Nickel is very difficult of fusion, melting at about 3000° F. Chiefly used in alloys with copper, as german-silver, nickel-silver, etc., and recently in the manufacture of steel to increase its hardness and strength, also for nickel-plating. Cubical expansion from 32° to 212° F., 0.0038. Specific heat .109.

Plathum, Pt.—At. wt. 195. A whitish steel-gray metal, malleable, and refined it is as soft as copper. Sp. gr. 21.15. It is fusible only by the oxydrogen blowpipe or in strong electric currents. When combined with iridium it forms an alloy of great hardness, which has been used for gunvents and for standard weights and measures. The most important uses of platinum in the arts are for vessels for chemical laboratories and manufactories, and for the connecting wires in incandescent electric lamps. Cubical expansion from 32° to 212° F., 0.0027, less than that of any other metal ex-

cept the rare metals, and almost the same as glass.

Silver (Argentum), Ag. At. wt. 107.7. Sp. gr. 10.1 to 11.1, according to condition and purity. It is the whitest of the metals, very malleable and ductile, and in hardness intermediate between gold and copper. Melts at about 1750° F. Specific heat .056. Cubical expansion from 32° to 212° F., 0.0058. As a conductor of electricity it is equal to copper. As a conductor

of heat it is superior to all other metals.

Tin (Stannum) Sn.—At. wt. 118. Sp. gr. 7.293. White, lustrous, soft, maileable, of little strength, tenacity about 5500 lbs, per square inch. Fuse at 442° F. Not sensibly volatile when melted at ordinary heats. Heat conat 449° F. Not sensibly volatile when melted at ordinary heats. Heat conductivity 14.5, electric conductivity 12.4; silver being 100 in each case. Expansion of volume by heat 0069 from 32° to 212° F. Specific heat 055, Its chief uses are for coating of sheet-iron (called tin plate) and for making

alloys with copper and other metals.

Zine, Zn.-At. wt. 65. Sp. gr. 7.14. Melts at 780° F. Volatilizes and burns in the air when melted, with bluish-white fumes of zine oxide. It is ductile and malleable, but to a much less extent than copper, and its tenacity, about 5000 to 6000 lbs. per square inch, is about one tenth that of wrought iron. It is practically non-corrosive in the atmosphere, a thin film of carbonate of zinc forming upon it. Cubical expansion between 32° and 212° F.,

0.0088. Specific heat .096. Electric conductivity 29, heat conductivity 36, silver being 100. Its principal uses are for coating iron surfaces, called "galvanizing," and for making brass and other alloys.

#### Table Showing the Order of

Malleability.	Ductility.	Tenacity.	Infusibility					
Gold	Platinum	Iron	Platinum					
Silver	Silver	Copper	Iron					
Aluminum	Iron	Aluminum	Copper					
Copper	Copper	Platinum	Gold					
Tin	Gold	Silver	Silver					
Lead	Aluminum	Zine	Aluminum					
Zinc	Zinc	Gold	Zine					
Platinum	Tin	Tin	Lead					
Tron	Lead	Lead	Tin					

# FORMULÆ AND TABLE FOR CALCULATING THE WEIGHT OF RODS, BARS, PLATES, TUBES, AND SPHERES OF DIFFERENT MATERIALS.

Notation: b = breadth, t = thickness, s = side of square, d = external

diameter,  $d_1$  = internal diameter, all in inches.

Sectional areas: of square bars =  $s^2$ ; of flat bars = bt; of round rods =  $.7854d^2$ ; of tubes =  $.7854(d^2 - d_1^2) = 3.1416(dt - t^2)$ . Volume of 1 foot in length: of square bars =  $12s^2$ ; of flat bars = 12bt; of

round bars =  $9.4248d^2$ ; of tubes =  $9.4248(d^2 - d_1^2) = 37.6992(dt - t^2)$ , in cubic

Weight per foot length = volume × weight per cubic inch of the material. Weight of a sphere = diam. 3 × .5236 × weight per cubic inch.

Material.	Specific Gravity.	Weight per cubic foot, lbs.	Weight of Plates 1 inch thick per per sq. ft., lbs.	Weight of Square Bars per foot length, lbs.	Weight of Flat Bars per foot length, lbs.	Weight per cubic inch, lbs.	Relative Weights. Wrought Iron = 1.	Weight of Round Rod per foot length, lbs.	Weight of Spheres or Balls, lbs.
Cast iron Wrought Iron. Steel. Copper & Bronze \(\) (copper & Bronze \(\) (5 Copper. \(\) (35 Zine. Lead. Aluminum Glass. Pine Wood, dry	7.854 8.855	480. 489.6 552.	46. 43.6 59.1 13.9 13.6	31,382 3.482 3.83382 3.68382 4.9382 1.1682 1.1382	31/6bt 31/3bt 3.4bt 3.883bt 3.683bt 4.93bt 1.16bt 1.13bt 0.21bt	.2779 .2833 .3195 .3029 .4106	1.02 1.15 1.09 1.48 0.347 0.34	$2.454d^2$ $2.618d^2$ $2.670d^2$ $3.011d^2$ $2.854d^2$ $3.870d^2$ $0.908d^2$ $0.164d^2$	.1455d³ .1484d³ .1673d³ .1586d³ .2150d³ .0504d³ .0495d³

**For tubes** use the coefficient of  $d^2$  in ninth column, as for rods, and multiply it into  $(d^2 - d_1^2)$ ; or take four times this coefficient and multiply it into  $(dt - t^2)$ .

For hollow spheres use the coefficient of d3 in the last column and multiply it into  $(d^3 - d_1^3)$ .

# MEASURES AND WEIGHTS OF VARIOUS MATERIALS (APPROXIMATE).

Brickwork.-Brickwork is estimated by the thousand, and for various thicknesses of wall runs as follows:

81/4-in. wall, or 1 brick in thickness, 14 bricks per superficial foot. 1234 " 17 " " 1½ " " 2 " 21 66 66 66 66 28 44 44 44 " 21/9 " 66 44 44 35

An ordinary brick measures about  $814 \times 4 \times 2$  inches, which is equal to 66 cubic inches, or 26.2 bricks to a cubic foot. The average weight is 416 lbs.

Fuel.—A bushel of bituminous coal weighs 76 pounds and contains 2688 cubic inches = 1,554 cubic feet. 29.47 bushels = 1 gross ton.

A bushel of coke weighs 40 lbs. (35 to 42 lbs.). One acre of bituminous coal contains 1600 tons of 2240 lbs. per foot of thickness of coal worked. 15 to 25 per cent must be deducted for waste in

min	ing.										
44.8	cubic	feet	bituminous	coal w	hen b	roken (	down.	 =1	ton.	2240	lbs.
42.3	66	6.6	anthracite	4.6	44	"	44	 = 1	ton.	2240	lbs.
123	"		of charcoal					 = 1	ton.	2240	lbs.
70.9	44	66	" coke					 = 1	ton.	2240	lbs.
1 eu	bic fo	ot of	anthracite	coal				 =	= 50 t	o 55	lbs.
1			bituminous	"				 =	= 45 f	0 55	lbs.
1		' Cu	imberland c	oal					=	53 lb	
1	66 6	· Čε	nnel coal						=	50.3	lbs.
î		' ch	arcoal (hard	(boow					'=	18.5	lbs.
-	4 4	6	th (mino	1						10.11	

#### Ores, Earths, etc.

13	cubic	feet	t of	ordinary gold or silver ore, in mine = 1	ton =	2000 lbs
20	**	44	"	broken quartz = 1	ton =	2000 lbs
18	feet o	of gr	ave	d in bank		= 1 ton
27	cubic	feet	t of	gravel when dry		= 1 ton
25	66			sand		= 1 ton
18	44	6.6	66	earth in bank		= 1 ton
27		4.6	64	" when dry		= 1  ton
17	4.6	66	66	clay		= 1 ton
				7 11 1 70 11 1 1 10 11 1 11 11		

30 lbs. Salt.—A struck bushel of salt, coarse, Syracuse, N. Y. = 56 lbs.; Turk's Island = 76 to 80 lbs.

# Weight of Earth Filling.

to ordine or murely a strange
(From Howe's "Retaining Walls,")
Average weight in
lbs. per cubic foot.
Earth, common loam, loose
" " shaken 82 to 92
" " rammed moderately 90 to 100
Fravel 90 to 106
Sand 90 to 106
Soft flowing mud
Sand, perfectly wet

#### COMMERCIAL SIZES OF IRON BARS. Flats.

A Tables														
Width.	Thickness.	Width.	Thickness.	Width.	Thickness.									
34 28 1 114 114 134 134 155 154	16 to 56 1/8 to 34 1/8 to 15/16 1/8 to 11/6 1/8 to 11/6 1/8 to 11/8 1/8 to 11/4 1/8 to 11/4 1/8 to 11/2 8/16 to 11/2	17/8 2 21/4 23/8 21/5 25/8 23/4 3 31/6	15 to 11/2 18 to 13/4 14 to 13/4 14 to 13/4 3/16 to 13/4 14 to 11/8 14 to 11/8 14 to 2 14 to 2	4 41/2 5 51/2 61/2 7 71/2	14 to 2 14 to 2									

Rounds: 1/4 to 13/4 inches, advancing by 16ths, and 13/4 to 5 inches by 8ths.

Squares: 5/16 to 11/4 inches, advancing by 16ths, and 11/4 to 3 inches by 8ths

gauge, 31/4 to 5 inches.

# WEIGHTS OF SQUARE AND ROUND BARS OF WROUGHT IRON IN POUNDS PER LINEAL FOOT.

Iron weighing 480 lbs, per cubic foot. For steel add 2 per cent.

1.								
Thickness or Diameter in Inches.	Veight of Square Bar One Foot Long.	Veight of Round Bar One Foot Long.	Phickness or Diameter in Inches.	Veight of Square Bar One Foot Long.	1 2 . 1	Thickness or Diameter in Inches.	Veight of Square Bar One Foot Long.	Veight of Round Bar One Foot Long.
hickness Diameter in Inches.	Weight of Square Boone Foot Long.	Veight of Round Ba Oue Foot Long.	hickness Diameter in Inches,	Veight of Square B One Foot Long.	Veight of Round Bar One Foot Long.	hickness Diameter in Inches.	Veight of Square Ba One Foot Long.	Weight of Round Ba One Foot Long.
P S S	0.00	Weight of Round B One Fool Long.	1 S 2 3	Weight of Square B One Foot Long.	00	8 5 5	Weight of Square B One Foo Long.	0,70
2 2 2	Har K	# 55 E 75	l a e e	# # # K	[상 편집답	a a o	17 5 F 16	# 5E %
* 5 5	Veight Square One F Long.	Veight Round One F Long.	1 4 2 2	Veight Squar One F Long.	Weight Round One F Long.	본분들	Veight Squar One F Long.	Weight Round One F Long.
5.5	12 P E O	20 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	1 5 5 7	- F G E G	12000	1.2.2.	1 5 5 5 C	2000
현면표	200H	NE WOU	Tab'#	200H	REWO'L	40°E	P WO H	E HOH
H	12	-		P .	-	H	>	
0			11/16	24.08	18.91	3/8 7/16	96.30	75.64
1/18	.013	.010	11/10	25.21	19.80	7/180	98.55	77.40
1/10	.010	.010	3/4 13/16	26.37	20.71	1/10	100.00	
78	.052	.041	13/10			72	100.8 103.1	79.19
1/16 1/8 3/16	.117	.092	1 %	27.55	21.64	9/16	103.1	81.00
1/4 5/16	.117	.164	7/8 15/16	28.76	22.59	9/16 5/8 11/16	105.5 107.8	82.83
5716	.326	.256	3	30.00	23.56	11/16	107.8	84.69
34	.469	.368	1/16	31.26	24.55	3/	110.2	86.56
78/10	.638	.501	1/10	32.55	25.57	19/10	110.6	88.45
7/16	.000	.501	3/16	00.00	00.07	19/10	112.6 115.1	00.40
9/16	.883	.654	8/16	23.87	26.60	34 13/16 7/8	115.1	90.36
9/16	1.055	.828	1/4	35.21	27.65	15/16	117.5	92.29
5/6	1.055 1.302	1.023	5/16	36.58	28.73	6	120.0	94.25
11/16	1.576	1.237	3/6	37.97	29.82		125.1	98.22
3/	1.875	1.473	7/16	39.39	30.94	1/8 1/4 3/8 1/2 5/8 3/4 7/8	130.2	102.3
3/4 13/16	0.001	1.728	1/10	40.83	32.07	34	195.5	106.4
13/16	2.201		/2	40.03		28	135.5	
7/8 15/16	2.552	2.004	9/16	42.30	33.23	1/2	140.8	110.6
15/16	2.930	2.301	5/2	43.80	34.40	5/2	146.3	114.9
1	3.333	2.618	11/16	45.33	35.60	3/4	151.9	119.3
1/16	3.763	2.955	3/	46.88	36.82	62	157.6	123.7
1/10	4.219	3.313	13/16	48.45	38.05	7 78	163.3	128.3
1/8 3/16	4.219	0.013	13/10				105.5	
3/16	4.701	3.692	15/16	50.05	39.31	1 1/8	169.2	132.9
1/4 5/16	5.208	4.091	15/16	51.68	40.59	1 34	175.2	137.6
5/16	5.742	4.510	4	53.33	41.89	3/2	181.3	142.4
3/8 7/16	6.302	4.950	1/16	55.01	43.21	1/8 1/4 3/8 1/2 5/8 3/4 8 7/8	187.5	147.3
7/18	6.888	5.410	12	56.72	44.55	62	193.8	152.2
1/10	7.500	5.890	3/16	58.45	45.91	78	200.2	157.2
9/16	1.000	0.090	3/10		40.01	24	200.2	100.4
9/10	8.138	6.392	1 4	60.21	47.29	_ 1/8	206.7	162.4
%	8.802	6.913	5/16	61.99	48.69	8	213.3	167.6
5/8 11/16	9.492	7.455	3/8	63.80	50.11	1/4	226.9	167.6 178.2
3/4	10.21	8.018	7/16	65.64	51.55	1,7	240.8	189.2
13/16	10.95	8.601	16	67.50	53.01	1/4 1/3 3/4	255.2	200.4
74	11.72	9.204	9/16	69.39	54.50	9 74	270.0	212.1
7/8 15/16	10.12						005 0	224.0
15/16	12.51 13.33	9.828	5/8 11/16	71.30	56.00	1 74	285.2 300.8	
2	13.33	10.47	11/16	73.24	57.52	14 1/3 3/4	300.8	236.3
1/16	14.18	11.14	3/4	75.21	59.07	3/4	316.9	248.9
1/8 3/16	15.05	11.82	13/16	77.20	60.63	10	333.3	261.8
3/16	15.95	12.53		79.22	62.22		350.2	275.1
1/	16 88	13.25	15/16	81 96	63.82	1/4 1/2 3/4	367.5	288.6
5/16	16.88 17.83	14.00	5 13/10	81.26 83.33	65.45	1 32	385.2	302.5
5/16	17.00		9 4 40	00.00		1 74	1.000.2	302.0
%	18.80	14.77	1/16	85.43	67.10	11	403.3	316.8
7/16	19.80	15.55	3/16	87.55	68.76	1/4	421.9	331.3
1,6	20.83	16.36	3/16	89.70	70.45	1/6	440.8	346.2
9/16	21.89	17.19	1/1	91.88	72.16	3%	460.2	361.4
54	22.97	18.04	5/16	94.08	73.89	12	480.	377.
78	No.31	10.04	3/10	04.00	10.05	122	200.	011.
	1	1	11	1		1		

# WEIGHTS OF FLAT ROLLED IRON IN POUNDS PER LINEAL FOOT. Widths from 1 In. to 12 In.

on weighing 480 lbs. ner cubic foot. For steel add 2 ner cent.

	434".	066	1.98	2.97	3.96	4.95	5.94	6.93	7.92	8.91	9.30	68.0	1.88	2.86	3.85	4.84	5.83	6.83	7.81	8.80	9.79	0.78	1.77	2.76	3.75	4.74	5.73	6.72	7.71	8.70	69.6	30.68	10.1
	41/2". 4																															80.06	
	414".																															27.45	
	4".	833	1.67	2.50	3.33	4.17	5.00	5.83	6.67	7.50	8.83	9.17	10.00	10.83	11.67	13.50	13,33	14.17	15.00	15.83	16.67	17.50	18.33	19.17	30.00	20.83	21.67	22.50	33.33	24.17	35.00	25.83	
	334".	781	1.56	2.34	3.13	3.91	4.69	5.47	6.25	7.03	7.81	8.59	9.38	10.16	10.94	11.72	12.50	13.28	14.06	14.84	15.63	16.41	17.19	17.97	18.75	19.53	20.31	21.09	21.88	22.66	23.44	24.22	WO.00
r cent.	31/2".	729	1.46	5.19	3.95	3.65	4.38	5.10	5.83	92.9	7.39	8.03	8.75	9.48	10.21	10.94	11.67	12.40	13.13	13.85	14.58	15.31	16.04	16.77	17.50	18.23	18.96	19.69	20.45	21.15	21.88	22.60 93.83	20.00
ed 2 pp	314".	1.	_	_			_	_	_					_			_			_	_		_	_	_	_	_	_		=		20.99	
For steel add 2 per cent.	3,,'	l.a	_	-	-	_			-	-	_	-	-	-	-	-	-	_	-	-	-	-	-			-	_	-	-	-	-	19.38	•
02	234".	1	_	_		-		-	-	-	-	-	-	_	-	-		_	_				-	-	-	-		_	-		_	17.76	٠,
weighing 480 lbs. per cubic foot. Width	21/2".	-	_	_	_	-			-	_		_	-	-		-	-			_	_	_	_	_	-	_	_	_		-	-	16:15	-
lbs. per	24".   2	<u></u>			_	_	-				-	-	-	-	-	-	-	-	-	-	-	-	-	-	-	-		-	-	_	-	14.53	-
ng 480	-	1	_	-		_	-	-	-			-	-		-		-			_	-					_	-	-					
reighin	2″.	4	80	1.2	1.6	20.00	.5 .5	30.00	80°	ee 	4.1	4.5	5.0	5.4	20.00	6.3	9.6	2.0	7.5	2.9	80	œ	9.1	9.5	10.0	10.45	10.8	11.2	11.6	12.0	12.5	12.92	
Iron v	134".	.365	.729	1.09	1.46	1.83	2.19	2.55	35 35 35	3.58	30.00	4.01	4.38	4.74	5.10	5.47	5.83	6.20	6.56	6.93	7.39	2.66	8.03	8.33	8.75	9.11	9.48	9.84	10.21	10.57	10.94	11.30	
	11/2".	.313	.625	.938	1.25	1.56	.88	2.19	5.50	. S.		8.44	3.75	4.06	4.38	4.69	2.00	5.31	5.63	5.94	6.25	6.56	88.9	7.19	7.50	7.81	8.13	8.44	8.75	9.08	200	10.00	-
	11/4".	. 260	.521	781	1.04	1.30	1.56	1.82	3°.08	2.34	5.60	2.76	3.13	8.39	3.65	3.91	4.17	4.43	4.69	4.95	5.21	5.47	5.73	5.99	6.25	6.51	6.77	7.03	7.29	7.55	7.81	8.33	
	1".	.208	.417	.635	.833	1.04	1.25	1.46	1.67	1.88	5.08	87.53	2.50	2.71	20.00	3.13	20.00	8.54	30	3.96	4.17	4.97	4.58	4.79	2.00	5.21	5.45	5.63	5.83	6.04	6.20	6.46	-
Thick-	Inches.	1-16	77	3-16	77	5-i6	3%	7-16	700	9-16	88	11-16	%	13-16	28	15-16	-	1 1-16	1 1/8	1 3-16	1 22	1 5-16	1 3/8	1 7-16	72	1 9-16	1 %	1 11-16	7	1 13-16		1 15-16	The owner ow

	12″.	### 1
	11".	8888745988888888888888888888888888888888
	10′′.	87.488408761886887488887488888 87.488408761886687488889718877
	9′′.	######################################
	81,87.	7.18.6.7.8.30.14.61.17.17.18.8.8.8.8.8.8.8.8.9.4.17.17.17.18.8.8.8.8.8.8.8.8.8.8.8.8.8.8
	8′′.	856888888888888988988888888888888888888
	77%".	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	7	488888664627868888888886649 48888866468788888886688866
Widths.	634".	
	61/6".	1044600000324277888888844 8184624888888888888888888888888888888888
	614".	1.95.5.5.2.0.11.8.4.7.5.5.2.0.9.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8
	6′′.	1988.89.85.85.11.88.83.75.88.88.89.89.89.89.89.89.89.89.89.89.89.
	53,4".	1989467896118446776988888888888888888888888888888888
	51%".	1.05.04.05.06.01.05.04.05.05.05.05.05.05.05.05.05.05.05.05.05.
	5,4".	001888486558 00181416576 01888888888888888888888888888888888888
	5".	1984-6-6-7-8-6-6-115-14-6-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-8-
Thick-	Inches.,	1.26.26.26.26.25.25.25.25.25.25.25.25.25.25.25.25.25.

Other sizes. Weight of other sizes can easily be obtained from the above table by means of Thus, for example,

# WEIGHT OF IRON AND STEEL SHEETS. Weights per Square Foot.

(For weights by new U. S. Standard Gauge, see page 31.)

Thickne	ss by Birm	ingham	Gauge.	Thickne	ss by Ame Sharpe's	erican (Bro ) Gauge.	own and
No. of Gauge.	Thick- ness in Inches.	Iron.	Steel.	No. of Gauge.	Thick- ness in Inches.	Iron.	Steel.
0000	.454	18.16	18.52	0000	.46	18.40	18.77
000	.425	17.00	17.34	000	.4096	16.38	16.71
00	.38	15.20	15.30	00	.3648	14.59	14.88
0	.34	13.60	13.87	0	.3249	13.00	13.26
1	.3	12.00	12.24	1	.2893	11.57	11.80
2	.284	11.36	11.59	2	.2576	10.30	10.51
3	.259	10.36	10.57	3	.2294	9.18	9.36
4	.238	9.52	9.71	4	.2043	8.17	8.34
5	.22	8.80	8.98	5	.1819	7.28	7.42
6 7 8 9	.203 .18 .165 .148 .134	8.12 7.20 6.60 5.92 5.36	8.28 7.34 6.73 6.04 5.47	6 7 8 9 10	.1620 .1443 .1285 .1144 .1019	6.48 5.77 5.14 4.58 4.08	6.61 5.89 5.24 4.67 4.16
11	.12	4.80	4.90	11	.0907	3.63	3.70
12	.109	4.36	4.45	12	.0808	3.23	3.30
13	.095	3.80	3.88	13	.0720	2.88	2.94
14	.083	3.32	3.39	14	.0641	2.56	2.62
15	.072	2.88	2.94	15	.0571	2.28	2.33
16	.065	2,60	2.65	16	.0508	2.03	2.07
17	.058	2,32	2.37	17	.0453	1.81	1.85
18	.049	1,96	2.00	18	.0403	1.61	1.64
19	.042	1,68	1.71	19	.0359	1.44	1.46
20	.035	1,40	1.43	20	.0320	1.28	1.31
21	.032	1.28	1.31	21	.0285	1.14	1.16
22	.028	1.12	1.14	22	.0253	1.01	1.03
23	.025	1.00	1.02	23	.0226	.904	.922
24	.022	.88	.898	24	.0201	.804	.820
25	.02	.80	.816	25	.0179	.716	.730
26	.018	.72	.784	26	.0159	.636	.649
27	.016	.64	.653	27	.0142	.568	.579
28	.014	.56	.571	28	.0126	.504	.514
29	.013	.52	.530	29	.6113	.452	.461
30	.012	.48	.490	30	.0100	.400	.408
31	.01	.40	.408	31	.0089	.356	.363
32	.009	.36	.367	32	.0080	.320	.326
33	.008	.32	.326	33	.0071	.284	.290
34	.007	.28	.286	34	.0063	.252	.257
35	.005	.20	.204	35	.0056	.224	.228

	Iron.	Steel,
Specific gravity	7.7	7.854
Weight per cubic foot	480.	489.6
" " inch	.2778	.2833

As there are many gauges in use differing from each other, and even the thicknesses of a certain specified gauge, as the Birmingham, are not assumed the same by all manufacturers, orders for sheets and wires should always state the weight per square foot, or the thickness in thousandths of an inch.

		_	00.0	33	6.67	00.0	3.33	6.67	00.0	3.33	6.67	00.0	3.33	6.67	00.0	3.33	6.67	0.00	3.33	6.67	0.0	6.7	00.	0.0	2.9	000	2.0	-0	00	2	65	0.0	2-1	e C	
		9	100	33	5 4	38 50	30	13 56	35 60	37 63	30	33 7	2 2	88	80	80	35 8	88	6 09	33 9	75 10	100	=======================================	<u> </u>	<u> </u>	100	146	155	186	16	172	3 180.0	186	200	
		15-16	37.5	40.6	43.7	46.8	50.0	53.1	56.5	59.	62.5	65.6	68.7	71.8	75.0	 18:	81.5	8.5	87.50	8	88	100.0	106.8	112.5	38.5	3	101.0	200	150	156.8	162.5	168.8	175.0	181.8	
		2%	0.0	7.92	88.	3.75	9.67	9.59	2.50	5.41	3.33	1.25	4.17	60.7	0.00	2.91	5.83	3.75	1.67	1.59	200	3.33	9.15	0.0	202	- 1	0.000	00	20	000	į.	ıc	00	0,0	
			188	20	32	33	33	35 45	55	25 25	2	38	9 89	900	20	<u>2</u> 2	<u> </u>	<u>~</u>	-56 -57 -58	φ 32	00	37.	80	00.0		2	2 0	7 0	120	147	151	3 157	16	122	
os.		13-16	33	32	37.5	40.6	43.5	46.0	48.	51.	54	56.8	59.	62.5	65.0	67.	20	23	33.	200	25	86.6	38	97.	202	8	000	107	120	135	140.8	146.3	151	157.1	
IN POUNDS.		3%	8	200	8	22	8	20	8	20	8	20	8	.50	8	50	8	.50	8	90	8	8	8	8	3.	0.0		, -		. 0	0	0.	0	145.0	
Po		- e		_								_			_		_			_		_		_			-		-						. 1
IN		11-16	7.50	62.	80.	88.	3.67	3.96	1.25	3.54	83	3.13	.43	7.7	90.9	. 53	.58	88.	-12	3.46	.75	33	6	25	3 8	29	, o	0.		9	es:	8.8	80.	182.0	
d's		11	<u>'-</u>						_	_					_	_	_			_								_			_				. 1
INEAL FOOT, For Steel add 2		8%	5.00	7.08	9.17	1.25	3.33	5.43	7.50	9.58	1.67	3.75	5.83	7.92	0.00	80.8	4.17	6.25	8.33	0.45	5.50	6.67	82	200	9.17	20.00	3.5	53		. C.	00	2.5	6.7	130.8	
reel teel		_	1																																4
LINEAL For St	Inches.	9-16	22.50	38.	36.25	8.13	80.00	31.88	33.75	35.67	37.50	39.38	11.25	13,13	15.00	88.91	8.75	90.63	25.50	88.78	96.25	00.00	55 15	20.	5.55	3:	0.0	8. 9. S.	38	5.5	77.50	1.3	0.0	108.8	
E S	Inc	-	1_		_						-		-						_		-		-			-		_			-				
E I	ui ss	7%	20.00	21.67	23.85	25.00	26.67	28.38	30.00	31.67	33.35	35.00	36.67	38.35	40.00	41.67	43.35	45.00	46.67	48.35	20.00	53.35	56.67	90.08	80.00	0000	5 5 8 8 8	76.5	2	88	86.67	90.00	98.38	00.67	
E S	Phickness		_	_			_	_	_	_	_	_	_	_	_						_				_	_					_	_			1
N, l	Thi	7-16	17.5	18.9	20.4	21.8	23.3	24.7	36.2	27.7%	29.1	30.6	35.0	33.5	35.0	36.4	37.9	39.3	40.8	3,0	43.7	46.6	49.5	52.5	4.00	000	2.5	67.0	0.0	25.9	75.8	7.8.7	81.6	87.58	
RO Cu			<u> </u>	33.	98	10	2	53	9	20		22	9	10	2	55	9	<u></u>	 8	25.	9:		9:	29	25	2 9	22	25	2 2		_	9	0		
480 lbs. per Cubic Foot.		8%	15.	16.	17.	18	20.	2	55	33	25.	56.	25	g	30.0	31.	35	33	35.	8	55	40.	2	45	4	33	5 10	3 2	9	62	65.	67.	200	35.50	١
NTI bs.		9	000	72	58	83	67	2	75	62	88	 88	- 8	96	8	- 50	80	13	12	55	53	 83	3	00.	 5 0	- 10	3 2	- 6	38	80	17	33	 ;;	50.00	-
PL.		5-16	12.	13.	14.	15.	16.	17.	18.	19.	8	23	85 85	23	35	56.	27.	æ	65	င္တ	25	89		, o		÷ 9		4	2	55	54	56.	58	38	١
OF ]		14	8	.83	.67	20	88.	.17	8	88.	- 67	03.	88	.17	8.	88.	.67	20	80	.17	3	.67	33.5	3.5	200	95	3.5	8	88	.67	.33	8	.67	50.00	
		/-	101	9	=	15	13	14	15	15	16	17	18	20	ಽ	8	25	33	8	77	3	8	38 8	200	2 2 2	900	3 8	88	4	4	43	45	46	500	-
(Based		3-16	.50	3.13	. F	.38	8.	.63	33	8	.50	3.13	.3	.38	8.	39.	.55	88.	22	22	92	3	33	3 5	9.5	3 6	35	3 15	8	52	.50	20.	8	37.50	ı
BIG		e.p	-	<u></u>	w	-	=	=	Ξ	=		==	==	7	12	=	=	<u>≃</u>	_	=	~	್ಷ-	25.5	. Š	% ö	इंट	. S	. %	, Sc	8	ěš	86	55 6	20 ES	
A		1/8	5.00	5.45	5.83	6.25	6.67	7.08	7.50	7.92	8.33	8.75	9.17	9.58	0.0	0.45	0.83	1.25	1.67	80.8	00.20	33	4.17	30.0	60.0	30.0	3 8	6 17	00.0	0.83	1.67	2.50	20.00	25.00	
			_			_			_		_	_	_			_	_	_	_		_		_				_				_				
		1-16	2.50	2.71	20.00	3.13	89	8.54	80	36.8	4.17	4.38	4.58	4.79	2.00	5.2	5.45	5.63	33	6.0	6.25	9.9	500	200	-0	3 %		6	00.0	10.49	10.88	11.35	11.67	12.50	
	- u			_		_	_	_	_	_				-			_	_	_	_		_	_	_		_	_	_	-					_	
	Width	Inches.	12	13	14	15	16	17	18	19	ನ	53	83	ĸ	24	32	92	22	33	33	88	3	400	000	86	9	44	46	48	20	52	20.0	00	88	-

## WEIGHTS OF STEEL BLOOMS.

Soft steel. 1 cubic inch = 0.284 lb. 1 cubic foot = 490.75 lbs.

			Lengths.										
Si	zes.	1''	6"	12"	18**	24"	30"	36"	42"	48"	54"	60"	66"
12" 11	× 4" × 6 × 5 × 4	13.68 18.75 15.62 12.50	82 113 94 75	164 225 188 150	245 338 281 225	327 450 375 300	409 563 469 375	491 675 562 450	573 788 656 525	654 900 750 600	736 1013 843 675	818 1125 937 750	900 1238 1031 825
10	× 7 × 6 × 5 × 4 × 3	19.88 17.04 14.20 11.36 8.52	120 102 85 68 51	239 204 170 136 102	358 307 256 205 153	477 409 341 273 204	596 511 426 341 255	715 613 511 409 306	835 716 596 477 358	955 818 682 546 409	1074 920 767 614 460	1193 1022 852 682 511	1312 1125 937 750 562
9	× 7 × 6 × 5 × 4	17.89 15.34 12.78 10.22	107 92 77 61	215 184 153 123	322 276 230 184	430 368 307 245	537 460 383 307	644 552 460 368	751 644 537 429	859 736 614 490	966 828 690 552	1073 920 767 613	1181 1012 844 674
8	× 8 × 7 × 6 × 5 × 4	18.18 15.9 13.63 11.36 9.09	109 95 82 68 55	218 191 164 136 109	327 286 245 205 164	436 382 327 273 218	545 477 409 341 278	655 572 491 409 327	764 668 573 477 382	878 763 654 546 436	982 859 736 614 491	1091 954 818 682 545	1200 1049 900 750 600
7	× 7 × 6 × 5 × 4 × 3	13.92 11.93 9.94 7.95 5.96	83 72 60 48 36	167 143 119 96 72	251 215 179 143 107	334 286 238 191 143	418 358 298 239 179	501 430 358 286 214	585 501 417 334 250	668 573 477 382 286	752 644 536 429 322	835 716 596 477 358	919 788 656 525 393
61 <u>/2</u> 6	× 6½ × 4 × 6 × 5 × 4 × 3	12. 7.38 10.22 8.52 6.82 5.11	72 44 61 51 41 81	144 89 123 102 82 61	216 133 184 153 123 92	288 177 245 204 164 123	360 221 307 255 204 153	432 266 368 307 245 184	504 310 429 358 286 214	576 354 490 409 327 245	648 399 551 460 368 276	720 443 613 511 409 307	792 487 674 562 450 337
5½ 5	× 5½ × 4 × 5 × 4	8.59 6.25 7.10 5.68	52 37 43 34	103 75 85 68	155 112 128 102	206 150 170 136	258 188 213 170	309 225 256 205	361 262 298 239	412 300 341 273	464 337 383 307	515 375 426 341	567 412 469 375
4½ 4	× 4½ × 4 × 4 × 8½ × 3	5.75 5.11 4.54 3.97 3.40	35 31 27 24 20	69 61 55 48 41	104 92 82 72 61	138 123 109 96 82	173 153 136 119 102	207 184 164 143 122	242 215 191 167 143	276 246 218 181 163	311 276 246 215 184	345 307 272 238 204	380 338 300 262 224
3½ 3	× 3½ × 3 × 3	3.48 2.98 2.56	21 18 15	42 36 31	63 54 46	84 72 61	104 89 77	125 107 92	146 125 108	167 143 123	188 161 138	209 179 154	230 197 169

## SIZES AND WEIGHTS OF STRUCTURAL SHAPES.

# Minimum and Maximum Weights and Dimensions of Carnegie I-Beams.

STEEL BEAMS.

Section Index.	epth of eam, in inches,	Weigh Foot,		Flange	Width.	Web Th	ickness.	Increase of Web and Flanges for each lb, in-		
Index.	Depth Beam, inche	Min.	Max.	Min.	Max.	Min.	Max.	crease of weight.		
B 1	24	80.00	100.00	6.95	7,20	.50	.75	.0123		
B 2	20	80.00	100.00	7 00	7.30	.60	.90	.015		
B 3	20	64.00	75.00	6.25	6.41	.50	.66	.015		
B 4	15	80.00	100.00	6.41	6.79	.77	1.16	.020		
B 5	15	60.00	75.00	6.04	6.34	.54	.84	.020		
B 6	15	50.00	59.00	5.75	5.93	.45	.63	.020		
*B 7	15	41.00	49.00	5.50	5.66	.40	.56	.020		
B 8	12	40.00	56.70	5.50	5.91	.39	.80	.025		
*B 9	12	32.00	39.00	5.25	5.42	.35	.52	.025		
B10	10	33.00	40.00	5.00	5.21	.37	.58	.029		
B11	10	25.50	32.00	4.75	4.94	.32	.51	.029		
B12	9	27.00	33.00	4.75	4.95	.31	.51	.033		
B13	9	21.00	26.00	4.50	4.66	.27	.43	.033		
B14	8	22.00	27.00	4.50	4.68	.27	.45	.037		
B15	8	18.00	21.70	4.25	4.39	.25	.39	.037		
B16	7	20.00	22.00	4.25	4.33	.27	.35	.042		
B17	7	15.50	19.00	4.00	4.15	.23	.38	.042		
B18	6	16.00	20.00	3.63	3.83	.26	.46	.049		
B19	6	13.00	15.00	3.50	3.60	.23	.34	.049		
B20	5	13.00	16.00	3.13	3.31	.26	.44	.059		
B21	9 9 8 8 7 6 6 5 5 4 4	10.00	12.00	3.00	3.12	.22	.33	.059		
B22	4	10.00	13.00	2.75	2.97	.24	.46	.074		
B23	4	7.50	9.00	2.63	2.74	.20	.31	.074		
B24	4	6.00	8.00	2.18	2.33	.18	.33	.074		
					1					

Iron. Stéel. Given weight in pounds per foot, to find sectional area, \*\* 334 (\*\* 0.3 Given sectional area, to find weight in lbs. per foot \*\* 335 (\*\* 1bs. per yard \*\* 10 (\*\* 1bs. per yard \*\* 1bs. per yard \*\* 10 (\*\* 1bs. per yard \*\* 1bs. per yard \*\* 10 (\*\* 1bs. per yard \*\* 1bs. per yard \*\* 10 (\*\* 1bs. per yard \*\* 1bs. 3.4 .2941 3.4 Given sectional area, to find weight in lbs. per foot 10.2

# Maximum and Minimum Weights and Dimensions of Carnegie Deck Beams.

STEEL.

Section Index.	Depth of Beam, inches.	Weight per Foot, lbs.		Flange	Width.	W	eb ness.	Increase of Web and Flanges per lb. in-	
index.		Min.	Max.	Min.	Max.	Min.	Max.	crease of weight.	
B100	10	27.23	35.70	5.25	5.50	.38	.63	.029	
B101	9	26.52	30.60	4.94	5.07	.44	.57	.032	
B102	8	20.15	24.48	5.00	5.16	.31	.47	.037	
B103	7	18.10	23.46	4.87	5.10	.31	.54	.042	
B105	6	15.30	18.36	4.38	4.53	.28	.43	.049	

# Weights and Dimensions of Carnegie Steel Channels.

Sec- tion Index	Depth of Chan-		ht per in lbs.	Flange	Width.	Thick	eb mess.	Increase of Web and Flanges for each	
	nel, in inches.	Min.	Max.	Min.	Max.	Min.	Max.	lb. in- crease of weight.	
C1 C2 C3 C4 C5 C6 C7 C8 C9	15 12 10 9 8 7 6 5	32.00 20.00 15.25 12.75 10.00 8.50 7.00 6.00 5.00	51 00 30.25 23.75 20.50 17.25 14.50 12.00 10.25 8.25	3.40 2.90 2.66 2.44 2.20 2.00 1.89 1.78 1.67	3.78 3.15 2.91 2.69 2.47 2.25 2.14 2.03 1.91	.40 .30 .26 .24 .20 .20 .19 .18 .17	.78 .55 .51 .49 .47 .45 .44 .43	.020 .025 .029 .033 .037 .042 .049 .059	

# Weights and Dimensions of Carnegie Z-Bars.

Section	Thickness		Size.	Weight,		
Index.	of Metal.	Flange.	Web.	Flange.	Iron.	Steel.
Z 1 Z 2 Z 3	3% 7–16 14 9–16 5% 11–16 34 13–16	3 ½ 3 9-16 3 58 3 ½ 3 9-16 3 58 3 ½ 3 9-16 3 58 3 ½ 3 9-16 3 58	6 1-16 6 ½8 6 1-16 6 ½8 6 1-16 6 ½8	3 1/2 3 9-16 3 5/6 3 1/2 3 9-16 3 5/8 3 9-16 3 5/8	15.3 18.0 20.6 22.3 24.9 27.5 28.8 31.3 33.9	15.6 18.3 21.0 22.7 25.4 28.0 29.3 32.0 34.6
Z, 4 Z, 5 Z, 6	5-16 3/6 7-16 1/2 9-16 5/8 11-16 3/4 13-16	3 5-16 3 36 3 14 3 5-16 3 36 3 14 3 5-16 3 36	5 1-16 5 1/8 5 1-16 5 1/8 5 1-16 5 1-16 5 1/8	3 14 3 5-16 3 36 3 14 3 5-16 3 36 3 14 3 5-16 3 36	11.3 13.7 16.0 17.5 19.8 22.1 23.2 25.5 27.8	11.6 13.9 16.4 17.8 20.2 22.6 23.7 26.0 28.3
Z.7  Z.8  Z.9	5-16 3/8 7-16 1/2 9-16 9-16 11-16 3/4	3 1-16 3 ½ 3 3-16 3 1-16 3 ½ 3 3-16 3 1-16 3 ½ 3 3-16	4 1-16 4 ½8 4 1-16 4 ½8 4 1-16 4 ½8 4 1-16 4 ½8	3 1-16 3 ½ 3 3-16 3 1-16 3 ½ 3 3-16 3 1-16 3 ½ 3 3-16	8.0 10.1 12.2 13.5 15.5 17.6 18.5 20.5 22.5	8.2 10.3 12.4 13.8 15.8 17.9 18.9 20.9 22.9
Z <sub>1</sub> 10 Z <sub>1</sub> 11 Z <sub>1</sub> 12	5-16 38 7-16 12 9-16	2 11-16 2 34 2 11-16 2 34 2 11-16 2 34	3 1-16 3 1-16 3 1-16 3 1-16	2 11-16 2 34 2 11-16 2 34 2 11-16 2 34	6.6 8.3 9.5 11.2 12.3 13.9	6.7 8.4 9.7 11.4 12.5 14.2

#### Pencoyd Steel Angles.

#### EVEN LEGS.

Sec-	ize		Approximate Weight in Pounds per Foot for Various Thicknesses in Inches.									ious		
No. of stion.	in ches.	1/8 .125	3-16 .1875	1/4 .25	5-16 .3125	3/8 .375	7–16 .4375	½ .50	9-16 .5625	5/8 .625	11–16 .6875	34 .75	7/8 .875	1 1 1 1 1 1 1 1 1 1 1 1
120 6 121 5 122 4 123 31 2 124 3 124 3 125 28 4 126 21 2 127 21 4 128 2 129 129 11 11 11 11 11 11 11 11 11 11 11 11 11	×3 ×23/4 ×21/2 ×21/4 ×2 ×13/4 ×11/4 ×11/4		2.14 1.80 1.53	4.9 4.5 4.1 3.6 3.3 2.9 2.4 2.04 1.53		14.8 12.2 9.8 8.6 7.1 6.7 6.1 5.4 4.9 4.4 3.6	14.3 11.3 10.0 8.3 7.8 7.1	16.4 13.0 11.4 9.4	18.5 14.6 12.8 10.5	20.7 $16.1$ $14.2$	22.8 17.7	25.0	34.2 29.2	39.3 33.4

#### UNEVEN LEGS.

Size in		Approximate Weight in Pounds per Foot for Various Thicknesses in Inches.											
in Inches.	1/8 .125	3-16 .1875	1/4 .25	5-16 .3125	3/8 .375	7-16 .4375	.50	9–16 .5625	5/8 .625	11–16 .6875	3/4 .75	7/8 .875	1 1 1 .00
154 7 × 33½ 152 6½ × 4 151 6 × 34½ 151 6 × 35½ 141 5 × 35½ 141 5 × 35½ 142 5 × 31½ 143 5 × 33 144 41 × 33 146 14 × 33 147 134 × 33 147 134 × 32 159 314 × 2½ 159		2.7 2.24 1.94	4.9 4.5 4.5 4.1 3.6 3.03 2.7	8.7 8.2 7.7 7.1 6.6 5.6 5.6 5.6 5.6 5.3	12.9 12.2 11.5 11.0 11.0 10.3 9.7 9.2 9.2 8.6 7.9 7.1 6.7 6.7 6.1 5.4 4.6	14.4 13.6 12.8 12.8 12.0 11.2 10.6 10.0 9.2 8.3 7.8 7.1 6.3	15.6 14.6 14.6 13.6 12.8 12.1 12.1 11.4 10.5 9.4 8.9 8.2	19.3 18.6 17.6 16.4 16.4 15.2 14.3 13.6 12.8 11.8	18.2 18.2 16.8 15.8 15.0 15.0 14.2	23.6 22.8 21.7 20.0 18.5 17.3 16.5 16.5	25.7 24.9 23.8 21.8 20.1 18.9	30.0 29.1 27.8	32.5 34.3 33.3 31.9

#### Pencoyd Tees.

#### EVEN TEES.

#### UNEVEN TEES.

Chart	Size	Weigl Fo	ht per ot.	Chart	Size	Weigh	nt per ot.
Number.	Inches.	Iron.	Steel.	Number.	Inches.	Iron.	Steel.
70 71 72 82 83 84 74 75 76 77 77 78 80 81 85	4 × 4 31/4 31/4 31/4 31/4 31/4 31/4 31/4 × 1	12.40 10.17 8.38 6.43 7.53 4.83 6.50 5.73 3.90 3.47 2.37 2.00 1.03 10.98	12.65 10.37 8.50 6.56 7.68 4.93 5.85 3.98 4.01 3.54 2.41 2.04 4.153 1.05 11.19	107 106 93 92 90 109 91 94 95 96 97 98 110 111 117 99 104 100 108 101 112 102 103 116 113 114 115 118 119	5 × 4 5 × 39-16 5 × 29-16 5 × 29-16 5 × 29-16 4 × 31-2 4 × 31-2 4 × 31-2 4 × 31-2 4 × 31-2 4 × 31-2 4 × 31-2 3 × 21-2 3 × 21-2 2 × 1 1-16 2 × 1 1-16 1 3 × 11-16 1 3 × 11-16	2.33 2.03 3.47 1.87 1.37	15.00 16.46 11.25 10.44 15.18 13.50 14.21 8.81 8.53 6.56 9.55 8.09 5.98 7.00 5.10 3.81 7.28 6.66 6.3.09 2.24 2.96 2.11 2.88 2.07 3.11 2.88 2.07 3.11 2.88 2.07 3.07 3.07 3.07 3.07 3.07 3.07 3.07 3

#### Pencoyd Car-Builders' Channels, Iron.

									,		
on Number.	h in Inches.	inum Flange idth in Inches.	num Web ickness in thes.	imum Weight er Foot in ounds.	Appr F	oxima l'oot fo W	te Wei r Each /eb, in	Thick	ness o	s per f	used Thickness iches for Each itional Pound Foot.
Section	Depth	Minim	Minin Thi Inel	Mini Po Po	5–16	3/8	7–16	1/2	9–16	5/8	Increa in In Add
55 54	13	37/8	3/8 9-32	29.5		29.5	32.2	34.9	37.6	40.3	.023
54 33½ 33	12 101/6	( 534	9-32 7-16	22.4 23.6	23.6	26.1	28.6 23.6	31.1 25.8	33.6		.025
33	101/6	1 21%	5-16	17.6	17.6	19.8					.029

#### Pencoyd Car-Builders' Channels, Steel.

### SIZES AND WEIGHTS OF ROOFING MATERIALS.

Corrugated Iron (Phoenix Iron Co.).

-	BLAC	K IRON.	GALVANIZED IRON.			
Thickness in Inches.  0.065 0.049 0.035	Weight in Lbs. per Sq. Ft., Flat.	Weight in Lbs. per Sq. Ft. on Roof. Flat.	Weight in Lbs. per Sq. Ft., on Roof. Corrugated 3.37 2.54	Weight in Lbs. per Sq. Ft., Flat.	Weight in Lbs. per Sq. Ft. on Roof. Flat.  3.50 2.76 2.03	Weight in Lbs. per Sq. Ft., on Roof. Corrugated
0.028 0.022 0.018	1.12 0.88 0.72	1.31 1.03 0.84	1.45 1.14 0.93	1.31 1.06 0.94	1.53 1.24 1.09	1.71 1.37 1.21

The above table is calculated for the ordinary size of sheet, which is from 2 to 21/2 feet wide, and from 6 to 8 feet long, allowing 4 inches lap in length and 21/2 inches in width of sheet.

The galvanizing of sheet iron adds about one-third of a pound to its weight

per square foot.

In corrugated iron made by the Keystone Bridge Co., the corrugations are In corrugated from made by the Keystone Bridge Co., the corrugations are 2.437 long, measured on the straight line; they require a length of iron of 2.7357 to make one corrugation, and the depth of corrugation is 21-327. One corrugation is allowed for lap in the width of the sheet and 67 in the length, for the usual pitch of roof of two to one. Sheets can be corrugated of any length not exceeding ten feet. The most advantageous width is 30%, which (allowing ½7 for irregularities) will make eleven corrugations = 30°, or, making allowance for laps, will cover 24¼7 of the surface of the

By actual trial it was found that corrugated iron No. 20, spanning 6 feet, will begin to give a permanent deflection for a load of 30 lbs. per square foot, and that it will collapse with a load of 60 lbs. per square foot. The distance between centres of purlins should therefore not exceed 6 feet, and, preferably, be less than this.

#### Terra-Cotta.

Porous terra-cotta roofing 3" thick weighs 16 lbs, per square foot and 2" thick, 12 lbs. per square foot. Ceiling made of the same material 2" thick weighs 11 lbs. per square foot.

#### Tiles.

Flat tiles  $6\frac{1}{4}$ "  $\times$   $10\frac{1}{2}$ "  $\times$   $5\frac{1}{6}$ " weigh from 1480 to 1850 lbs. per square of roof, the lap being one-half the length of the tile.

Tiles with grooves and fillets weigh from 740 to 925 lbs. per square of roof. Pan-tiles 14½" × 10½" laid 10" to the weather, weigh 850 lbs. per square.

#### Tin.

The usual sizes for roofing tin are  $14'' \times 20''$  and  $20'' \times 28''$ . Without allowance for lap or waste, tin roofing weighs from 50 to 62 lbs, per square. Tin on the roof weighs from 62 to 75 lbs, per square. Roofing plates or terne plates (steel plates coated with an alloy of tin and lead) are made only in IC and IX thicknesses (27 and 29 Birmingham gauge). "Coke" and "charcoal" tin plates, old names used when iron made with coke and charcoal was used for the tinned plate, are still used in the trade, although steel plates have been substituted for iron; a coke plate now commonly meaning one made of Bessemer steel, and a charcoal plate one of open-hearth steel. The thickness of the tin coating on the plates varies with different "brands."

For valuable information on Tin Roofing, see circulars of Merchant & Co.,

Philadelphia,

TIN PLATES. (TINNED SHEET STEEL.)
Standard Stock Sizes, with Number of Sheets and Net
Weight per Box.

10	B. W. Gauge.	Thickness.	Size.	Sheets.	Net Weight lbs.	B. W. Gauge,	Thickness.	Size.	Sheets.	Net Weight lbs.
26	29	IC	10 × 14	225		- 29	IC	10 × 20	225	
26   IXX   10 × 14   225   160   26   IXX   10 × 20   225   229   229   IX   12 × 12   225   130   229   IC   IX   11 × 22   225   235   260   IXX   12 × 12   225   138   27   IX   11 × 22   225   235   260   IXX   12 × 12   225   138   27   IX   11 × 22   225   235   235   236   IXX   14 × 20   112   138   229   IC   12 × 24   112   110   112   113   114   114   114   115							ÎX			195
27	26			225		26	IXX		225	
29 IC 14 × 20 112 108 29 IC 12 × 24 112 110 27 IX 14 × 20 112 108 29 IC 12 × 24 112 110 26 IXX 14 × 20 112 160 26 IXX 12 × 24 112 165 25 IXXX 14 × 20 112 180 29 IC 13 × 26 112 182 29 IC 20 20 × 28 112 216 26 IXX 13 × 26 112 182 29 IC 20 × 28 112 216 26 IXX 13 × 26 112 182 29 IXXX 20 × 28 112 270 29 IC 14 × 22 112 120 26 IXX 20 × 28 112 270 29 IC 14 × 22 112 120 26 IXX 20 × 28 112 320 27 IX 14 × 22 112 120 27 IX 20 × 28 12 320 27 IX 14 × 22 112 120 28 IXXX 20 × 28 56 180 26 IXX 14 × 22 112 120 29 IC 13 × 13 × 13 225 162 26 IXX 14 × 22 112 174 20 IC 13 × 13 × 13 225 162 26 IXX 14 × 24 112 130 27 IX 13 × 13 225 162 26 IXX 14 × 24 112 161 27 IX 13 × 13 225 162 26 IXX 14 × 24 112 161 27 IX 14 × 14 12 12 12 25 25 26 IXX 14 × 24 112 161 27 IX 15 × 15 × 15 × 25 × 17 IX 14 × 28 112 155 29 IC 15 × 15 × 15 × 25 × 27 IX 14 × 28 112 155 20 IC 15 × 15 × 15 × 25 × 27 IX 14 × 28 112 155 29 IC 16 × 16 × 16 × 25 × 27 IX 14 × 28 112 155 29 IC 16 × 16 × 16 × 25 × 27 IX 14 × 28 112 120 20 IC 16 × 15 × 15 × 25 × 27 IX 14 × 28 112 155 20 IC 16 × 16 × 25 × 25 × 27 IX 14 × 28 112 120 20 IC 16 × 16 × 25 × 25 × 26 × 27 IX 14 × 28 112 120 20 IC 16 × 16 × 25 × 25 × 26 × 27 IX 14 × 28 112 120 20 IC 16 × 16 × 25 × 25 × 26 × 27 IX 14 × 28 112 120 20 IC 16 × 16 × 25 × 25 × 26 × 27 IX 14 × 28 112 120 20 IC 16 × 16 × 25 × 25 × 26 × 27 IX 14 × 28 112 120 20 IC 15 × 16 × 25 × 25 × 26 × 27 IX 14 × 38 112 120 20 IC 16 × 16 × 16 × 25 × 26 × 27 IX 14 × 38 112 120 21 IX 16 × 16 × 16 × 25 × 26 × 27 IX 14 × 38 112 120 22 IX X 16 × 16 × 16 × 25 × 26 × 27 IX 14 × 36 56 58 20 23 IX X 16 × 16 × 16 × 25 × 26 × 27 IX 14 × 36 56 58 20 246 IX X 17 × 17 × 25 × 300 × 30 IX IX 14 × 36 56 58 20 25 IX X 16 × 16 × 16 × 16 × 10 × 112 100 27 IX 18 × 18 × 18 112 158 27 IX 16 × 10 × 112 100 29 IC 20 × 20 I12 120 0 0 0 0 II2 120 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0 0	29					29			225	190
27				225	138	27	IX		225	235
26   IXX										
26						27				
25		IXX				26				
29	25	IXXX	14 × 20	112		29	IC			
26 IXX 20 × 28 112 270 29 IC 14 × 22 112 148 25 IXXX 20 × 28 66 180 26 IXX 14 × 22 112 174 244 11XXXX 20 × 28 66 180 26 IXX 14 × 22 112 174 29 IC 13 × 13 × 13 × 25 132 97 IX 14 × 24 112 130 29 IC 14 × 14 × 12 112 170 29 IC 14 × 14 × 12 15 155 27 IX 14 × 24 112 170 29 IC 15 × 15 × 25 160 26 IXX 14 × 24 112 180 29 IC 15 × 15 × 25 160 26 IXX 14 × 24 112 180 29 IC 15 × 15 × 25 160 20 10 IXX 14 × 24 I12 190 29 IC 14 × 25 193 26 IXX 14 × 28 I12 155 27 IX 14 × 25 193 26 IXX 14 × 28 I12 178 29 IC 15 × 15 × 25 178 27 IX 14 × 31 I12 210 210 210 210 210 210 210 210 210 2			14 × 20				IX			
26   IXX   20 × 28   112   320   27   IX   14 × 22   112   148   2414   IXXXX   20 × 28   56   180   26   IXX   14 × 22   112   174						26				
XXX						29				
29   IC						26	IXX			174
29						29				
26	29	IC		225		27	IX			161
29 IC	27									
26 IXX						29				
29	29					27				
29	21			995		20				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$				225	178	27	IX			
26						26				
27   IX	26					27	IX	14×56	56	
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						26	IXX			
29	27			225		27	1X			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	26					20				
26	27					97				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	26									
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	29	IC	18×18	112	138	29	IC.		112	120
29   IC   20 × 20   112   160   29   IC   16 × 20   112   127     27   IX   20 × 20   112   195   27   IX   16 × 20   112   124     26   IXX   20 × 20   112   195   27   IX   16 × 20   112   124     29   IC   22 × 22   112   190   29   IC   16 × 22   112   138     27   IX   22 × 22   112   235   27   IX   16 × 22   112   138     26   IXX   22 × 22   112   235   27   IX   16 × 22   112   138     27   IX   24 × 24   112   220     27   IX   24 × 24   112   230     26   IXX   22 × 22   112   276     26   IXX   24 × 24   112   330     27   IX   24 × 24   112   330     28   DC   124 × 17   100   94   23   DXXX   15 × 21   100   244     28   DC   124 × 17   100   143   28   DC   17 × 25   50   94     29   DXXXX   124 × 17   100   143   28   DC   17 × 25   50   142     20   DXXXX   124 × 17   100   143   28   DC   17 × 25   50   142     29   DXXXX   124 × 17   100   164   25   DX   17 × 25   50   122     29   DXXXX   124 × 17   100   164   25   DX   DX × 17 × 55   50   122     20   DXXXX   124 × 17   100   185   24   DXX × 17 × 25   50   143     28   DC   15 × 21   100   130   23   DXXX   17 × 25   50   164     20   DXXX   17 × 25   100   130   23   DXXX   17 × 55   50   164     20   DXXX   17 × 100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   164     20   DXXX   17 × 55   100   130   23   DXXX   17 × 55   100   100   100   100   100   100   100   100   100   100   100   100   100   100   100   100   100   1										
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$						26				
26						29				
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	26					96				
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	29					29				
29   IC   24 x 24   112   230		1X	22 × 22			27	IX			170
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$						26	IXX	16 × 22	112	200
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	29									
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		IX								
Tolkhoess   Size   Sheets   Weight   Gauge   Tolkhoess   Size   Sheets   Weight   Gauge   Tolkhoess   Size   Sheets   Weight   Sheets   Sheets   Weight   Sheets   Sheets   Sheets   Sheets	20	IAA	1 24 X 24	1 112			1	1	1	
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	B. W. Gauge.	Thickness.	Size.	Sheets,	Weight	B. W. Gauge.	Thickness.	Size.	Sheets.	Weight
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	28	DC	121/6 × 17	100		23	DXXX	15 × 21	100	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	25	DX	1216 × 17	100		22	DXXXX	15 × 21	100	275
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$			1216 × 17			28				
28 DC   15×21   100   130   23   DXXX   17×25   50   164	23		$ 12\frac{1}{2} \times 17 $				DX			
25 DC 15 x 21 100 150 25 DAAA 17 x 25 50 104	22		121/2 × 17				DXX			
95 (DY   15 v 21   100   180   99   DXXXX   17 v 95   50   185	28 25	DX	15 × 21	100	180	22	DXXXX	17 × 25	50	185
24 DXX   15×21   100   213   24   DXXXX   11×20   30   100						~~	DILILIA	11. ^ ~0	00	200

Slate.

Number and superficial area of slate required for one square of roof.

(1 square = 100 square feet.)

Dimensions in Inches,	Number per Square.	Superficial Area in Sq. Ft.	Dimensions in Inches.	Number per Square.	Superficial Area in Sq. Ft.
6×12	533	267	12×18	160	240
7 × 12	457	-	10×20	169	235
8 x 12	400		11×20	154	400
9 × 12	855		12×20	141	
7×14	374	254	14×20	121	
8×14	327	201	16×20	137	
9×14	291		12×22	126	231
10×14	261		14 × 22	108	- 201
8×16	277	246	12×24	114	228
9×16	246		14×24	98	440
			16 × 24		
10×16	221			86	00#
9×18	213	240	14×26	89	225
10 × 18	192		16×26	78	

As slate is usually laid, the number of square feet of roof covered by one slate can be obtained from the following formula:

 $\frac{\text{width} \times (\text{length} - 3 \text{ inches})}{288} = \text{the number of square feet of roof covered.}$ 

Weight of slate of various lengths and thicknesses required for one square of roof:

Length	Weight in Pounds per Square for the Thickness.												
Inches.	1/8"	3-16"	1/4"	3/8′′	1/9"	5/8′′	34''	1''					
12 14 16 18 20 22 24 26	483 460 445 434 425 418 412 407	724 688 667 650 637 626 617 610	967 920 890 869 851 836 825 815	1450 1379 1336 1303 1276 1254 1238 1222	1936 1842 1784 1740 1704 1675 1653 1631	2419 2301 2229 2174 2129 2093 2066 2039	2902 2760 2670 2607 2553 2508 2478 2445	3872 3683 3567 3480 3408 3350 3306 3263					

The weights given above are based on the number of slate required for one square of roof, taking the weight of a cubic foot of slate at 175 pounds.

#### Pine Shingles.

Number and weight of pine shingles required to cover one square of roof:

Number of Inches Exposed to Weather.	Number of Shingles per Square of Roof.	Weight in Pounds of Shingle on One-square of Roofs.	Remarks.
4	900	216	The number of shingles per square is for common gable-roofs. For hiproofs add five per cent. to these figures. The weights per square are based on the number per square.
41/6	800	192	
5	720	173	
51/2	655	157	
6	600	144	

#### Skylight Glass.

The weights of various sizes and thicknesses of fluted or rough plate-glass required for one square of roof.

Dimensions in Inches.	Thickness in	Area	Weight in Lbs. per
	Inches.	in Square Feet.	Square of Roof.
$\begin{array}{c} 12 \times 48 \\ 15 \times 60 \\ 20 \times 100 \\ 94 \times 156 \end{array}$	3–16	3.997	250
	14	6.246	350
	38	13.880	500
	12	101.768	700

In the above table no allowance is made for lap.

If ordinary window-glass is used, single thick glass (about 1-16") will weigh about 82 lbs, per square, and double thick glass (about  $\frac{1}{2}$ ") will weigh about 164 lbs, per square, no allowance being made for lap. A box of ordinary window-glass contains as nearly 50 square feet as the size of the panes will admit of. Panes of any size are made to order by the manufacturers, but a great variety of sizes are usually kept in stock, ranging from  $6\times 8$  inches to  $36\times 60$  inches.

#### APPROXIMATE WEIGHTS OF VARIOUS ROOF-COVERINGS.

per

For preliminary estimates the weights of various roof coverings may be taken as tabulated below:

Name.	Weight in Lbs.
rame.	Square of Ro
Cast-iron plates (%" thick)	1500
Copper.	. 80- 125
Felt and asphalt	100
Felt and gravel	. 800-1000
Iron, corrugated	. 100- 375
Iron, galvanized, flat	. 100- 350
Sheathing, pine, 1" thick yellow, northern southern.	300
" " " " couthern	. 400
Spruce, 1" thick	. 200
Sheathing, chestnut or maple, 1" thick	400
ash, hickory, or oak, 1" thick	500
Sheet iron (1-16" thick)	300
Sheet iron (1–16" thick)	500
Shingles, pine	200
Slates (¼" thick)	900
Skylights (glass 3-16" to ½" thick)	. 250- 700
Sheet lead.	. 500- 800
Thatch	. 650
Tin	. 70- 125
Tilos flot	. 1500-2000
Tiles, flat	. 700-2000
" (grooves and fillets)	. 100-1000
" pan	
" with mortar	. 100-3000
Zinc	. 100- 200

## WEIGHT OF CAST-IRON PIPES OR COLUMNS.

## In Lbs. per Lineal Foot.

Cast iron = 450 lbs. per cubic foot.

Bore.	Thick. of Metal.	Weight per Foot.	Bore.	Thick. of Metal.	Weight per Foot.	Bore.	Thick. of Metal.	Weight per Foot.
						_	_	
Ins.	Ins.	Lbs.	Ins.	Ins.	Lbs.	Ins.	Ins.	Lbs.
3	3/8 1/8	12.4 17.2	10	3/4	79.2	22	34 7/8	167.5
	29	17.2	101/2	22	54.0		<b>%</b> 8	196.5
01.4	%	22.2		28	68 2 82.8	23	24	174.9
31/2	9/8	14.3		94	82.8		1/8	205.1
	29	19.6	11	29	56.5	0.4	1	235.6
	%	25.3		28	71.3	24	24	182.2
4	2/8	16.1		24	86.5 58.9		1/8	213.7
	22	22.1	111/2	23	74.4	05	1 0/	245.4
41.7	28	28.4 17.9		38	90.2	25	24	189.6 222.3
41/2	%	24.5	12	94	61.3		1/8	255.3
	22	31.5	12	23	77.5	26	19/	197.0
5	38	19.8		28	93.9	20	24	230.9
о	18	27.0	121/2	74	63.8		1/8	265.1
	72	34.4	12/2	63	80.5	27	3/	203.1
51/2	78	21.6		78	97.6	~1	74	239.4
372	18	29.4	13	12	66.3		1/8	274.9
	72	37.6	10	52	83.6	28	3/	211.7
6	28	23.5		28	101.2	200	3/4 3/8	248.1
U	18	21.8	14	12	71.2		1/8	284.7
	22	31.8 40.7	14	52	89.7	29	3/	219.1
61/2	28	25.3		38	108.6	40	33	256.6
0/2	18	34.4	15	54	95.9		1/8	294.5
	52	43.7	10	3%	116.0	30	7/8	265.2
7	82	27.1		72	136.4	00	1/8	304.3
•	78 14	36.8	16	58	102.0		11/6	343.7
	72	46.8	10	3%	123.3	31	178	273.8
71/2	8%	29.0		7%	145.0	0.	1 28	314.2
172	78	39.3	17	56	108.2		116	354.8
	52	49.9	11	3%	130.7	32	7/8	282.4
8	36	30.8		72	153.6	0.0	1 28	324.0
0	12	41.7	18	6%	114.3			365.8
	5%	52.9	10	3%	138.1	33	1½ 7/8	291.0
81/2	1%	44.2		4%	162.1		1/8	333.8
0/2	52	56.0	19	5%	120.4		116	376.9
	3%	68 1	10	3%	145.4	34	1½ %	299.6
9	12	46.6		7%	170.7		1′°	343.7
	5%	59.1	20	5%	126.6		11/6	388.0
	3%	71.8		3/4	152.8	35	7%	308.1
91/2	1/6	49.1		7/8	179.3		1′°	353.4
-72	5%	62.1	21	5%	132.7		î½	399.0
	3%	75.5		3/4	160.1	36	1%	316.6
10	1/3	51.5		7/8	187.9		1	363.1
	5%	65.2	22	5%	138.8		11/8	410.0
	, 0			. 0				

The weight of the two flanges may be reckoned = weight of one foot.

#### WEIGHTS OF CAST-IRON PIPE TO LAY 12 FEET LENGTH.

#### Weights are Gross Weights, including Hub.

(Calculated by F. H. Lewis.)

Thic	kness.				Insid	le Dia	meter.			
Inches.	Equiv. Decimals.	4''	6"	8"	10"	12"	14"	16"	18"	20"
38 13-32 7-16 15-32 1/2 17-32 9-16 19-32 54 11-16 34 13-16 78 15-16 1 114 138	.875 .40625 .4375 .4687 .5 .58125 .5625 .625 .625 .6875 .75 .8125 .875 .9875 .9875 1.125 1.25 1.375	209 228 247 266 286 306 327	304 331 358 386 414 442 470 498	400 435 470 505 541 577 613 649 686	581 624 668 712 756 801 845 935 1026	692 744 795 846 899 951 1003 1110 1216 1324 1432	804 863 922 983 1043 1103 1163 1285 1408 1531 1656 1783 1909	1050 1118 1186 1254 1322 1460 1598 1738 1879 2021 2163	1177 1253 1329 1405 1485 1635 1789 1945 2101 2259 2418 2738 3062	1640 1810 1980 2152 2324 2498 2672 3024 3380
Thic	kness.		:		Insid	e Diar	neter.			
Inches.	Equiv. Decimals.	22"	24"	27''	30"	33''	36′′	42"	48"	60′′
56 11-16 34 13-16 78 15-16 1 114 136 114 138 114 138 115 158 134 2 2 214 214 234	.625 .6875 .75 .8125 .875 .9875 1 1 125 1 .25 1 .5 1 .5 1 .5 1 .5 1 .875 2 .25 2 .75	1799 1985 2171 2359 2547 2787 2927 3310 3698	2160 2362 2565 2769 2975 3180 3598 4016 4439	2422 2648 2875 3103 3332 3562 4027 4492 4964 5439	2984 3186 3437 3690 3942 4456 4970 5491 6012 6539	3221 3496 3771 4048 4325 4886 5447 6015 6584 7159 7737	3507 3806 4105 4406 4708 5316 5924 6540 7158 7782 8405	4426 4773 5122 5472 6176 6880 7591 8303 9022 9742 10468 11197	5442 5839 6236 7034 7833 8640 9447 10260 11076 11898 12725 14385	9742 10740 11738 12744 13750 14763 15776 17821 19880 21956

## CAST-IRON PIPE FITTINGS. Approximate Weight.

Addyston Pipe and Steel Co., Cincinnati, Ohio.

Size in Inches.	Weight in Lbs.	Size in Inches.	Weight in Lbs.	Size in Inches,	Weight in Lbs.	Size in Inches.	Weight in Lbs.
CROS	SES.	TEE	is.	SLEE	VES.	REDUC	CERS.
2	40	8×3	220	6	65	10×4	128
3 3×2	104 90	10 10×8	390 330	8 10	86 140	12×10 12×8	278 254
3×2	150	10 × 6	312	12	176	12×6	250
4×3	114	10×4	292	14	208	12×4	250
4×2	110	10 × 3	290	16	340	14 × 12	475
6 6×4	200 150	12 12×10	565 510	20 24	500 710	14×10 14×8	430 340
6×3	150	12×10	492	30	965	14×6	285
8	325	12×6	484	36	1500	16×12	475
8×6	265	12×4	460			16 × 10	435
8×4	265 225	14 × 12 14 × 10	650 650	90° ELI	BOWS.	20 × 16 20 × 14	690 575
8×3 10	510	14×10	575	2	14	20 × 19	540
10×8	415	14×6	545	2 3 4 6	34	20 × 8	300
10×6	388	14×4	525	4	48	$24 \times 20$	745
10×4	338 350	14×3 16	490 790	8	110 145	30 × 24 30 × 18	1305 1385
10 × 3 12	700	16 × 14	850	10	225	36 × 30	1730
12×10	650	16×12	825	12	370	307.00	1100
12×8	615	16×10	890	14	450	ANGLE	REDUC-
12×6	540	16×8	755	16	525	ERS FO	
12×4 12×3	525 495	16×6 16×4	630 655	20 24	900 1400	6×4	95
14×10	750	20 4	1375	~*	1400	6×3	80
14×8	635	20 × 16	1115	1% or 45°	BENDS.		
14×6	570	20 × 12	1025		4.4	S PII	PES.
16 16×14	1025 1070	20 × 10 20 × 8	1090 900	3 -	30 65	· 1	90
16 × 12	1025	20×6	875	6 .	85	6	- 190
16 × 10	1010	20 × 4	845	8	160		
16×8	825	21 × 10	1465	10	190	PLU	GS.
16×6 16×4	700 650	24 24×12	1875 1425	12 16	290 510	- 9	9
20	1790	24×8	1375	20	740	3	2 5
20 × 12	1370	24×6	1375	24	1425	4	l 8
20 × 10	1225	30	3025	30	2000	6	12
20 × 8 20 × 6	1000 1000	30 × 24 30 × 20	2640 2200			8 10	26 46
20×4	1000	30 × 12	2035	1-16 or BEN	22½°	12	66
24	2190	'30×10	2050			14	70
24 × 20	2020	30 × 6	1825	6 .	150	16	100
24×6 30×20	1340 2635	36 36 × 30	5140 4200	8	155 165	20	150 185
30 × 12	2250	36 × 12	4050	12	260	24 30	370
30 × 8	1995	45° BR.		16	500		
TER	ES.	PIPI	ES.	24 30	1280 1735	CAF	s.
2 3	28	3	• 90			3	15
3 3×2	76	6×6×4	145	REDUC	CERS.	6	25
3×2 4	76 100	8 8×6	300 - 290	3×2	35	8	60 75
4×3	90	24	2765	4×3	42	10	100
4×2	87	$24 \times 24 \times 20$	2145	4×2	40	12	120
6 6×4	150 130	30 36	4170 10300	6×4 6×3	95 80		
6×3	125			8×6	126		OXES.
6×2	120	SLEE		8 × 4	116	4	235
8	266	2 3	10 20	8×3	116	8	355 760
8×6 8×4	252 222	4	44	10×8 10×6	212 150	20	1420
	1 222						

#### WEIGHTS OF CAST-IRON WATER- AND GAS-PIPE.

(Addyston Pipe and Steel Co., Cincinnati, Ohio.)

in nes.	Stand	lard Wate	r-Pipe.	in nes.	Standard Gas-Pipe.					
Size in Inches.	Per Foot.	Thick- ness.	Per Length.	Size	Per Foot.	Thick- ness.	Per Length.			
2 3	7 15	5-16 3/8	63 180	2 3	6 121/2	1/4 5-16	48 150			
2 3 4 6 8 10	17 22 33 42	3/8 1/2 1/2 1/2 1/2 1/2 9-16	204 264 396 504	4 6 8	17 30 40	3/8 7–16 7–16	204 360 480			
10 12 14	60 75 117	9-16	720 900 1400	10 12 14	50 70 84	7-16 1/2 9-16	600 840 1000			
16 18	125 167 200	3/4 5/4 7/8 15–16	1500 2000 2400	16 18 20	100 134 150	9–16 11–16 11–16	1200 1600 1800			
20 24 30 36	250 350 475	1 1½ 1¾ 1¾	3000 4200 5700	24 30 36	184 250 350	3/4 3/4 7/8 1/8	2200 3000 4200			
42 48 60	600 775 1330	13/8 11/2 2	7200 9300 15960	42 48 60	383 542 900	7% 11% 13%	4600 6500 10800			

#### THICKNESS OF CAST-IRON PIPES.

P. H. Baermann, in a paper read before the Engineers' Club of Phila-delphia in 1882, gave twenty different formulas for determining the thick-ness of cast-iron water-pipes under pressure. The formulas are of three classes:

1. Depending upon the diameter only.

2. Those depending upon the diameter and head, and which add a con-

3. Those depending upon the diameter and head, contain an additive or subtractive term depending upon the diameter, and add a constant.

The more modern formulas are of the third class, and are as follows:

$$\begin{array}{llll} t = .00008hd + .01d + .36 & Shedd, & No. 1. \\ t = .00008hd + .0133d + .296 & Warren Foundry, No. 3. \\ t = .000058hd + .0152d + .312 & Francis, & No. 3. \\ t = .000048hd + .013d + .32 & Dupuit, & No. 4. \\ t = .00004hd + .1 \sqrt{d} + .15 & Box, & No. 5. \\ t = .000135hd + 4 & -0.011d & Whitman, & No. 6. \\ t = .00006(h + .20d) + .333 - .0033d & Fanning, & No. 7. \\ t = .00015hd + .25 - .0052d & Meggs, & No. 8. \\ \end{array}$$

In which t = thickness in inches, h = head in feet,  $d \Rightarrow$  diameter in inches.

Rankine, "Civil Engineering," p. 721, says: "Cast-iron pipes should be made of a soft and tough quality of iron. Great attention should be made to moulding them correctly, so that the thickness may be exactly uniform all round. Each pipe should be tested for air-bubbles and flaws by ringing it with a hammer, and for strength by exposing it to double the intended greatest working pressure." The rule for computing the thickness of a pipe

to resist a given working pressure is  $t = \frac{rp}{f}$ , where r is the radius in inches,

p the pressure in pounds per square inch, and f the tenacity of the iron per square inch. When f = 18000, and a factor of safety of 5 is used, the above expressed in terms of d and h becomes

$$t = \frac{.5d \cdot .433h}{3600} = \frac{dh}{16628} = .00006dh.$$

"There are limitations, however, arising from difficulties in casting, and by the strain produced by shocks, which cause the thickness to be made greater than that given by the above formula."

#### Thickness of Metal and Weight per Length for Different Sizes of Cast-iron Pipes under Various Heads of Water.

(Warren Foundry and Machine Co.)

1,000													
	Ft. I	0 Iead.	1( Ft. H		Ft. H		20 Ft. H		25 Ft. I	io Iead.	300 Ft. Head.		
Size.	ress	Weight per Length.	ress tal.	tht ngth.	ness tal.	Weight per Length.	ral.	tht ngth.	ness etal.	tht ngth.	ness tal.	tht agth.	
	Thickness of Metal.	Weight r Lengt	Thickness of Metal.	Weight per Length	Thickness of Metal.	Weight	Thickness of Metal.	Weight per Length	Thickness of Metal.	Weight per Length	Thickness of Metal.	Weight per Length	
	T o	pe	F o	be	To	be	To	be	F "	be	100	pe	
											_		
3	.344 .361 .378	144 197	.353 .373	149 204	.362	153	.371	157 218	.380	161 226	.390	166 235	
4 5 6 8	378	254	.393	265	.408	211 275	.423	286	.438	298	.453	309	
6	.393	315	.411	330	. 429	345	.447	361	.465	377	.483	393	
8	.422	445	.450	475	.474 .519	502	498	529	.522	557	.546	584	
10	.459	600	.489	641	.519	682	.549	723	.579	766	.609	808	
12	.491	768	.527	826	.563	885	.599	944	.635	1004	.671 .734	1064	
14	.524	952	.566	1031	.608	1111	.650	1191	.692 .748	1272	734	1352 1673	
10	.557	1152 1370	.604	1253 1500	.652 .697	1360 1630	.700 .751	1468 1761	.740	1568 1894	.796 .859	2026	
90	.622	1603	.682	1763	.742	1924	.802	2086	.805 .862	2248	.922	2412	
24	.687	2120	.759	2349	.831	2580	.903	2811	.975	3045	1.047	3279	
30	.785	3020	.875	3376	.965	3735	1.055	4095	1.145	4458	1.235	4822	
10 12 14 16 18 20 24 30 36 42 48	.882	4070	.990	4581	1.098		1.206	5613	1.314	6133	1.422	6656	
42	.980	5265	1.106	5958	1.232	6657	1.358	7360	1.484	8070	1.610	8804	
48	1.078	6616	1.222	7521	1.366	8431	1.510	9340	1.654	10269	1.798	11195	

All pipe cast vertically in dry sand; the 3 to 12 inch in lengths of 12 feet, all larger sizes in lengths of 12 feet 4 inches.

# Safe Pressures and Equivalent Heads of Water for Castiron Pipe of Different Sizes and Thicknesses.

(Calculated by F. H. Lewis, from Fanning's Formula.)

		Size of Pipe.											
	4"	6"	8"	10"	12"	14"	16′′	18"	20"				
Thick- ness.	Pressure in Pounds. Head in	Pressure in Pounds. Head in Feet.	Pressure in Pounds. Head in Feet,	Pressure in Pounds. Head in Feet.	Pressure in Pounds. Head in Feet,								
7-16 1-2 9-16 5-8	112 25 224 51 336 77	6 124 250 4 199 458	74 171 130 300	44 101 89 205	24 55 62 143 99 228	42 97 74 170							
11-16 3-4 13-16		. 274 631	186 429	132 304 177 408 224 516	137 316 174 401 212 488	106 244 138 316 170 392	56 129 84 194 112 258 140 323	41 95 66 152 91 210 116 267	51 118 74 170 96 221				
7-8 15-16 1 1 1-8					249 574	202 465 234 538 266 612	168 387 196 452 224 516	141 325 166 382 191 440 216 497	119 274 141 325				
1 1-4	:::. .::	: :::: ::::							256 589				

#### Safe Pressures, etc., for Cast-iron Pipe.-(Continued.)

		Size of Pipe.																
mı tələ	22	"	24"		27"		30′′		33"		36"		42"		48"		60"	
Thick- ness.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.	Pressure in Pounds.	Head in Feet.
11-16 3-4 13-16 7-8 15-16 1 1-8 1 1-8 1 1-4 1 3-8 1 1-2 1 3-8 1 1-2 2 1-8 2 1-8 2 1-8 2 1-2 2 3-4	40 60 80 101 121 142 182 224	92 138 184 233 279 327 419 516	30 49 68 86 105 124 161 199 237	69 113 157 198 242 286 371 458 546	19 36 52 69 85 102 135 169 202 236	64 83 120 159 196 235 311 389 465 544	24 39 54 69 84 114 144 174 204 234	55 90 124 159 194 263 332 401 470 538	42 55 69 96 124 151 178 205 233	97 127 159 221 286 348 410 472 537	32 44 57 82 107 132 157 182 207	74 101 131 189 247 304 362 419 477	38 59 81 103 124 145 167 188 210	88 136 187 237 286 334 385 433 484	99 118 136 155	55 99 143 187 228 272 313 357 401 445 488	34 49 64 79 94 109 124	78 113 147 182 217 251 286 320 355 424 482

Note.—The absolute safe static pressure which may be put upon pipe is given by the formula  $P=\frac{2T}{D}\times\frac{8}{5}$ , in which formula P is the pressure per square inch; T, the thickness of the shell; S, the ultimate strength per square inch of the metal in tension; and D, the inside diameter of the pipe. In the tables S is taken as 18000 pounds per square inch, with a working strain of one fifth this amount or 3600 pounds per square inch. The formula for the absolute safe static pressure then is:  $P=\frac{7300T}{D}$ .

It is, however, usual to allow for "water-ram" by increasing the thickness enough to provide for 100 pounds additional static pressure, and, to insure sufficient metal for good casting and for wear and tear, a further increase equal to .333  $\left(1-\frac{D}{100}\right)$ .

The expression for the thickness then becomes:

$$T = \frac{(P+100)D}{7200} + .333 \left(1 - \frac{D}{100}\right),$$

and for safe working pressure

$$P = \frac{7200}{D} \left( T - .333 \left( 1 - \frac{D}{100} \right) \right) - 100.$$

The additional section provided as above represents an increased value under static pressure for the different sizes of pipe as follows (see table in margin). So that to test the pipes up to one fifth of the ultimate strength of the material, the pressures in the marginal table should be added to the pressure-values given in the table above.

Size of Pipe.	Lbs.
4" 6 8 10 12 14 16 18 20 22 24 27 30 33 36 42 48 60	676 476 346 316 276 248 226 209 196 185 176 165 156 149 143 183 126 116

#### SHEET-IRON HYDRAULIC PIPE.

(Pelton Water-Wheel Co.)

Weight per foot, with safe head for various sizes of double-riveted pipe.

Diameter of Pipe.		je eg	afe Head in Feet the Pipe will stand.	Veight of Pipe per Lineal Ft.	Diameter of Pipe.		Thickness of Iron by Wire Gauge.	afe Head in Feet the Pipe will stand.	تب
ĭ		Thickness of Iron by Wire Gauge	Safe Head in Feet th Pipe wil stand.	Weight of Pipe per Lineal F	ĭ		Thickness of Iron by Wire Gauge	Safe Head in Feet th Pipe will stand.	Weight of Pipe per Lineal Ft
<u>e</u> .	Area of Pipe.	8 6 e	- de e	ಕ್ಕಾ	<u>9</u> .	Area of Pipe.	age	E e e	고수급
e e	o oi	1 7 TO	in Fee Pipe Stand	4 e e	lamet Pipe.	l g	550 550 550	afe He in Fee Pipe stand.	d e e
2,5	8.i.	e	ta Hille	2011	55	l g	0 4 e	tarie	90.5-1
Fig.	50	[∄ ⊙ ;=	S TE	PHG.	Fig.	1 2 4	id o'ii	S P :: B	15 mm
А	4	1 8	00	=	А	< 4	H 8	ďΩ	=
in.	ea in	B.W.G.	feet.	lbs.	in	sq. in. 254 254 254 254 254 254 314	B.W.G.	foot	lbs.
2	$\frac{\text{sq. in.}}{7}$	18	400	9	18	954	16	165	101/
9	10	10	200	01/	10	204	10	100	161/2 201/2
4	120	10	500	274	10	201	14	202	201/2
4	12	16	400 350 525 325 500 675	2 21/4 3 31/4 41/4 5	18	254	12	385	214
5	20	18	325	31/2	18	254	11	424	30
5	20	16	500	41/4	18	254	10	505	34
5	20	14	675	5	20	314	16	148	18
6	28	18	296	41/4	20		14	227	221/6
6	28	16	487	53/4	20	314	12	346	30 ~
6	28	14	743	41/4 53/4 71/5	20	314 314 314 380	14 12 11 10 16 14 12 11 10 16	380	3214
7	38	18	254	517	20	314	10	456	3612
÷	38	16	419	632	22	380	16	125	20
7	38	14	640	812		380	14	906	9/3/
é	50	16	967	712	99	980	10	216	2017 2714 30 34 18 221/2 30 321/2 361/2 20 243/4 323/4
0	12 12 20 20 20 28 28 28 38 38 50 50 63 63 63 78 78 78 95	B.W. G. 18 16 14 18 16 14 18 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 14 12 16 16 17 17 18 18 18 18 18 18 18 18 18 18 18 18 18	296 487 743 459 640 267 560 854 327 409 761 295 450 687 754 900 687 826 687 820 246	91%	90	380 380 380 380 452 452	14 12 11 10	feet. 165 252 385 424 505 148 227 346 380 456 135 206 415 316 3415 188 290 406 175 267 267 273 273 273 273 273 273 273 273 273 27	2527
0	50	14	300	972	22	900	11	347	559/4
0	90	12	604	10	32	300	10	415	40
9	63	16	327	13 S1/2	24	452	14	188	271/4
9	63	14	499	10%	24	452	12	290	351/2
9	63	12	.61	141/4	24	452	14 12 11	318	39
10	78	16	295	91/4	24	452	10	379	431/2
10	78	14	450	1134	24	453	8	466	53
10	78	12	687	153/4	26	530	14	175	291/4
10	78	11	754	1716	53	530	12	267	3812
10	78	10	900	191/4	26	530	11	294	42
11	95	16 14 12 11 10 16	269	93/4	26	452 452 530 530 530 530 530 615 615 615	10	352	47
11	95	14	412	18 17 <sup>1</sup> / <sub>4</sub> 183/ <sub>4</sub> 21 11 <sup>1</sup> / <sub>4</sub>	26	520	- 8	432	571/
11	95	12	326	171/4	28	615	14	162	3117
11	95	11	687	1834	28	615	12	247	4114
11	95	10	820	21	28	615	11	273	45
12	113	16	246	1114	28	615	10	397	5014
12	113	14	377	14	28	G15	8	400	6117
12	113	12	571	1814	80	206	19	931	44
12	112	14 12 11	630	1816 1934 2234	20	706	11	954	48
12	112	10	753	9987	30	706	10	204	54
12	120	10 16	228	19	20	706	10	975	65
13	199	14	348	15	20	706	, .	010	74
3 4 4 4 5 5 5 6 6 6 6 6 7 7 7 7 8 8 8 8 9 9 9 10 10 10 11 11 11 11 11 12 12 12 12 12 12 13 13 13 13 14 14 14 14	95 95 95 113 113 113 113 113 132 132 132 132 153 153 153 176 176 176 176 176 176	12	377 574 630 753 228 348 530 583 696 211 324	12 15 20 22 24 13 16 21 23 25 26 133 4 17 23 24 24 24 24 24 24 24 24 24 24 24 24 24	n. 18 18 18 18 18 18 18 18 18 18 18 18 18	1017	10 8 14 12 11 10 8 14 12 11 10 8 11 10 8 7 10 8 7		58
13	139	12 11	583	99	36	1017	10		677
13	132	10	696	2414	26	1017	8		78
14	159	10 16 14	911	19	26	1017	5		90
14	159	14	224	16	40	1017	10		00
14	159	10	404	011/	40	1050	10		00
14	150	12 11 10 16	549	0217	40	1200	0		90
14	150	11	040	20/2	40	1200	6		100
14	105	10	040	20	40	1206	0		108
10	170	. 10	197	1394	40	1256	4		120
15	170	14 12 11	802	17	42	1385	10		141/2
15	176	12	460	28	42	1385	8		91
15	176	. 11	507	241/2	42	1385	7		102
15	176	10 16	606	28	42	1385	4 10 8 7 6 4		114
16	201	16	185	141/6	42	1385	4		133
16	201	14	283	171/4	42	1385	1/4		137
14 14 14 15 15 15 15 15 16 16 16	201	12 11	432	141/4 171/4 241/4 261/4	42	615 615 706 706 706 706 706 1017 1017 1256 1256 1256 1256 1256 1385 1385 1385 1385 1385	3		145
16	201 201 201	11	494 543 648 197 302 460 507 606 185 283 432 474 567	261/2	40 40 40 42 42 42 42 42 42 42 42 42 42 42 42	1385	5-16 3/8		2834 4414 5835 5844 4414 6614 486 657 788 7186 97 910 114 1133 1137 1133 1137 1138 1137 1138 1137 1138 1137 1138 1138
16	201	10	567	291/2	42	1385	3/8		216

#### STANDARD PIPE FLANGES.

Adopted July 18, 1894, at a conference of committees of the American Society of Mechanical Engineers, and the Master Steam and Hot Water Fitters' Association, with representatives of leading manufacturers and users

of pipe.

The list is divided into two groups; for medium and high pressures, the first ranging up to 75 lbs. per square inch, and the second up to 200 lbs.

nrst	ranging		67 01	Ibs	, per squa			and	tne	seco	nd u	p to	20	O IP	s.
Pipe size, inches.	Pipe Thickness, P+100 $333$ $\left(1-\frac{d}{100}\right)$	Thickness, nearest Fraction, inches.	Stress on Pipe per square inch @ 200 lbs.	Radius of Fillet, inches.	Flange Diameters, inches.		Flange Thickness, inches.	Width Flange Face,	inches.	Rolt Circle Dismeter	inches.	Number of Bolts.	Bolt Diameter, inches.	Bolt Length, inches.	Stress on each Bolt, per square inch, at Bottom of Thread @ 200 lbs.
2 21/5 3 31/2 4 41/2 5 6 7 8 9 10 12 14 15 16 18 20 22 24 28 30 36 42 48	.409 .429 .448 .466 .496 .498 .525 .563 .60 .678 .713 .904 .904 .946 1.02 1.09 1.09 1.38 1.48 1.48 1.48 1.47 1.38	75757582222555515315755511111111111111111111111	460 550 690 900 1060 11280 1310 1600 1600 1780 1920 2040 2100 2100 21100	18181818181818181818181818181818181814	66777; 8529999991111124421145151515151515151515151515151	11.4 17.8 11.6 11.4 13.4 13.4 13.4	5 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	334 378 4 414 414 414 414 414 414 414 414 414	2 2144 4 5 6 6 5 5 3 4 4 1 4 1 4 1 6 6 6 5 5 5 5 5 6 6 6 6 6 6 6 6 6 6 6	29\4 33\4 35\4 42 48\4 48\4 48\4	4344 56 61424 7734 8142 958 81434 11834 11	4 4 4 4 4 4 8 8 8 8 8 8 8 8 8 8 8 8 8 8	566666343434343434568	2 2 2 2 3 4 4 4 4 4 4 4 5 5 5 5 5 6 6 6 7 7 7 7 7 7 7 7 7 7 7 7	825 1050 1330 21530 2100 1430 1630 2360 4190 3610 2970 4280 4210 4540 4320 4490 4320 5030 5030 55790 5790 6090

48 | 2.17 | 214 | 2130| 14 | 15714 | 5914 | 2 | 234 | 434 | 534 | 5434 | 56 | 44114 | 1734 | 6090 |

Notes.—Sizes up to 24 inches are designed for 200 lbs. or less.

Sizes from 24 to 48 inches are divided into two scales, one for 200 lbs., the other for less.

The sizes of bolts given are for high pressure. For medium pressures the threat 14-inch less for pipes 2 to 20 inches diameter inclusive, and 14 inch less for larger sizes, except 48-inch pipe, for which the size of bolt is 1%

When two lines of figures occur under one heading, the single columns up to 24 inches are for both medium and high pressures. Beginning with 24 inches, the left-hand columns are for medium and the right-hand lines are for high pressures.

The sudden increase in diameters at 16 inches is due to the possible insertion of wrought-iron pipe, making with a nearly constant width of gasket a greater diameter desirable.

When wrought-iron pipe is used, if thinner flanges than those given are sufficient, it is proposed that bosses be used to bring the nuts up to the standard lengths. This avoids the use of a reinforcement around the pipe. Figures in the third, fourth, fifth, and last columns refer only to pipe for

200 lbs. pressure.

In drilling valve flanges a vertical line parallel to the spindles should be midway between two holes on the upper side of the flanges.

#### DIMENSIONS OF PIPE FLANGES AND CAST-IRON PIPES.

(J. E. Codman, Engineers' Club of Philadelphia, 1889.)

	, , , , , , , , , , , , , , , , , , , ,										
Diameter of Pipe.	Diamater of Flange.	Diameter of Bolt Circle.	Diameter of Bolt	Number of Bolts.	Thickness of Tlange.	Thick of H	pec.	Weight per foot without Flange.	Weight of Flange and Bolts.		
2 3 4 5 6 8 10 12 14 16 18 20 22 24 26 28 30 32 44 44 46 48	614 715 9 9 9 9 1034 1034 1134 20 22 24 27 283 44 27 283 43 45 47 49 47 49 47 49 47 49 5534 5554 5554	434 578 7 8 914 1138 11534 18 20 2214 2414 2614 2414 2614 314 44 46 4814 44 46 4814 55	**************************************	4 4 6 8 8 10 12 14 16 16 18 20 24 24 24 28 30 32 32 34 34 36 38 40	556 576 11-16 54 13-16 26 15-16 1 1-16 11-3-16 1	13-32 7-16 7-16 15-32 1½-16 19-32 21-32 21-32 21-32 27-32 78 31-32 11-16 31-32 11-16 31-32 11-16 115-32 13-16 114-16 114-16 111-32 13-16	373 .396 .420 .443 .466 .511 .557 .603 .649 .695 .741 .787 .833 .879 .925 .971 1.017 1.017 1.201 1.293 1.389 1.389 1.385	6.96 11.16 15.84 21.00 26.64 21.00 26.64 39.36 54.00 70.56 89.04 109.44 1131.76 156.00 158.16 210.24 272.16 373.40 24.24 24.21 26.21 272.16 373.40 24.24 273.16 373.40 24.20 259.36 259.	4.41 5.93 7.66 9.63 11.82 16.91 23.00 30.13 38.34 47.70 58.23 70.00 83.05 97.42 113.18 130.85 149.00 144.26 239.27 266.00 294.49 324.78 356.94		

D = Diameter of pipe. All dimensions in inches,

FORMULE.—Thickness of flange = 0.033D + 0.56.

Thickness of pipe = 0.023D + 0.327.

Weight of pipe per foot =  $0.34D^2 + 3D$ .

Weight of flange =  $0.01D^3 + 0.1D^2 + 3D$ .

Weight of flange =  $0.01D^3 + 0.1D^2 + D + 2$ .

Diameter of flange =  $0.01D^3 + 0.1D^2 + D + 2$ .

Diameter of bolt-circle = 0.02D + 2.566.

Diameter of bolt = 0.011D + 0.73.

Number of bolts = 0.78D + 2.56.

#### PIPE FLANGES FOR HIGH STEAM-PRESSURE. (Chapman Valve Mfg. Co.)

Size of Pipe.	Diameter of Flange.	Number of Bolts.	Diameter of Bolts.	Diameter of Bolt Circle.	Length of Pipe-Thread.
Inches. 21/6 3 31/2 4 41/2 5 6 6 7 8 9 10 12 14 15	Inches. 71/2 9 9 10 10/6 11 13 14 15 16 17/4 20 23	Inches. 6 6 7 8 8 9 10 12 12 13 15 18	Inches. 5/8 3/4 3/4 3/4 3/4 3/4 7/8 7/8 7/8	Inches, 576 656 714 726 816 816 1056 1176 13 14 1514 2014	Inches.  11/4  13/4  1 7-16  1 9-16  1 11-16  1 13-16  1 15-16  2  21/6  21/4  21/6  25/6  21/6  21/6

#### STANDARD SIZES, ETC., OF WROUGHT-IRON PIPE. For Water, Gas, or Steam.

(Briggs Standard.)

Dian	Diameter of Tube.			nal nm-	mal um-	of per t. of e Sur-	of toof toof de ce.	nal a.	nal a.
Nomi- nal Inside.	Actual Inside.	Actual Out- side.	Thickness of Metal.	Internal Circum- ference.	External Circum- ference,	Length Pipe p Sq. Ft. Inside face.	Length o Pipe pe Sq. Ft. Outside Surface	Internal Area.	External Area.
Ins.	Ins.	Ins.	Ins.	Ins.	Ins.	Feet.	Feet.	Ins.	Ins.
1/8	.270	.405	.068	.848	1.272	14.15	9.44	.0572	.129
1/8 1/4 3/8 1/2 3/4	.364	.540	.088	1.144	1.696	10.50	7.075	.1041	.229
3/8	.494	.675	.091	1.552	2.121	7.67	5.657	.1916	. 358
1/2	.623	.840	.109	1.957	2.652	6.13	4.502	.3048	.554
3/4	.824	1.050	.113	2.589	3.299	4.635	3.637	. 5333	.866
1	1.048	1.315	.134	3.292	4.134	3.679	2.903	.8627	1.357
11/4 11/2 2	1.380	1.660	.140	4.335	5.215	2.768	2.301	1.496	2.164
11/6	1.610	1.900	.145	5.061	5.969	2.371	2.01	2.038	2.835
2, 2	2.067	2.375	.154	6.494	7.461	1.848	1.611	3.355	4.430
21/6	2.468	2.875	.204	7.754	9.032	1.547	1.328	4.783	6.491
3 ~	3.067	3.500	.217	9.636	10.996	1.245	1.091	7.388	9.621
31/6	3.548	4.000	.226	11.146	12.566	1.077	.955	9.887	12.566
21/2 3 31/2 4	4.026	4.500	.237	12.648	14.137	.949	.849	12,730	15,904
41/6	4.508	5.000	.246	14.153	15.708	.848	.765	15.939	19.635
5 ~	5.045	5.563	. 259	15.849	17.475	.757		19.990	24,299
6	6.065	6.625	.280	19.054	20 813	.63	.577	28.889	34.471
41/2 5 6 7 8	7.023	7.695	.301	22.063	23,954	.544	.505	38.737	45.663
8	7.982	8.625	.322	25.076	27.096	.478	.444		58.426
*9	9.000	9.688	.344	28.277	30.433	.425	.394	63.633	73.715
10	10.019	10.750	.366	31.475	33.772		.355		90.762

\* By the action of the Manufacturers of Wrought-iron Pipe and Boiler Tubes, at a meeting held in New York, May 9, 1889, a change in size of actual outside diameter of 9-inch pipe was adopted, making the latter 9.625 instead of 9.688 inches, as given in the table of Briggs' standard pipe diameters. For discussion of the Briggs Standard of Wrought-iron Pipe Dimensions, see Report of the Committee of the A. S. M. E. in "Standard Pipe and Pipe Threads," 1886. Trans., Vol. VIII. p. 29. The figures in the next to the last column are derived from the formula

$$D - (0.05D + 1.9) \times \frac{1}{n}$$

in which D =outside diameter of the tubes, and n the number of threads to the inch. The figures in the last column are derived from the formula  $0.8\frac{1}{n} \times 2 + d$ , or  $1.6\frac{1}{n} + d$ , in which d is the diameter at the bottom of the

thread at the end of the pipe.

Having the taper, length of full-threaded portion, and the sizes at bottom Having the taper, length of full-threaded portion, and the sizes at bottom and top of thread at the end of the pipe, as given in the table, taps and dies can be made to secure these points correctly, the length of the imperfect threaded portions on the pipe, and the length the tap is run into the fittings beyond the point at which the size is as given, or, in other words, beyond the end of the pipe, having no effect upon the standard. The angle of the thread is 60°, and it is slightly rounded off at top and bottom, so that, instead of its depth being equal to its pitch, as is the case with a full V-thread, it is

4/5 the pitch, or equal to  $0.8\frac{1}{n}$ , n being the number of threads per inch.

#### Sizes, etc., of Wrought-iron Pipe-(Continued.)

	8	Sizes, et	c.		Screwed Ends.							
Nominal Inside Diameter.	Length of Pipe Con- taining One Cubic Foot.	Weight per Foot of Length.	Contents in U. S. Gallons per Foot.	Weight of Water per Foot of Length.	Number of Threads per Inch.	Length of Perfect Screw.	Diameter of Bottom of Thread at End of Pipe.	Diameter of Top of Thread at End of Pipe.				
Inch. 148 144 344 1144 1142 2142 3 4 4 4 4 5 6 6 7 8 9	Feet. 2500 . 1385	Lbs243 .422 .561 .845 .1.126 .1.126 .2.258 .2.694 .3.667 .7.547 .9.055 .12.492 .14.564 .18.767 .28.448 .410 .28.348 .407	.0006 .0026 .0057 .0102 .0230 .0408 .0638 .0918 .1632 .2550 .3673 .4998 .8263 1.020 1.469 1.999 2.611	Lbs005 .021 .047 .085 .190 .349 .527 .760 .1.756 .851 .8.500 .12.312 .312 .312 .312 .312 .312 .312 .	No. 27 18 18 14 14 111,22 111,23 111,23 8 8 8 8 8 8 8	Inch	Inches	Inches393 .522 .656 .815 .1.025 .1.283 .1.627 .1.866 .2.339 .2.82 .3.441 .3.938 .4.435 .4.932 .5.491 .6.546 .7.54 .8.534 .9.59				
10	1.80	40.641	4.081	34.000	8	1.68	10.445	10.645				

Taper of conical tube ends, 1 in 32 to axis of tube = 34 inch to the foot total taper.

1 inch and below are butt-welded, and proved to 300 pounds per square inch

hydraulic pressure.
14 inch and above are lap-welded, and proved to 500 pounds per square inch hydraulic pressure.

# SIZES ABOVE 10 INCHES. (Morris, Tasker & Co., Limited.)

Nominal Size.	Actual Inside Diameter.	Actual Outside Diameter.	Thickness.	Internal Cir- cumference.	External Cir- cumference.	Internal Area.	External Area.	Length of Pipe per sq. ft. of Inside Surface.	Length of Pipe per sq. ft. of Outside Surface.	Length of Pipe containing 1 cubic foot.	Weight per foot of Length.
in. 11 12 13 14 15 16 17 18 19 20	in. 11.224 12.180 13.136 14.092 15.048 16.004 16.960 17.916 18.872 19.828	in. 12 13 14 15 16 17 18 19 20 21	in. .388 .41 .432 .454 .476 .498 .520 .542 .564 .586	in. 35.26 38.26 41.27 44.27 47.27 50.28 53.28 56.28 59.29 62.29	47.12 50.27 53.41 56.55 59.69 62.83	98.94 116.54 134.58 155.97 177.87 201.16 225.91	176.72 201.06 226.98 254.47 283.53 314.16	.313 .290 .271 .254 .238 .225	ft. .318 .293 .273 .254 .238 .225 .212 .201 .191 .183		lbs. 47.73 54.66 61.94 70.01 78.27 87.12 96.38 106.07 116.21 126.76

#### WROUGHT-IRON WELDED TUBES, EXTRA STRONG. Standard Dimensions.

Nominal Diameter.	Actual Out- side Diameter.	Thickness, Extra Strong.	Thickness, Double Extra Strong.	Actual Inside Diameter, Extra Strong.	Actual Inside Diameter, Double Extra Strong.
Inches, 1/6 1/4 3/4 3/4 1/2 2 21/6 3 3/4 4	Inches. 0.405 0.54 0.675 0.84 1.05 1.315 1.66 1.9 2.375 2.875 3.5 4.0 4.5	Inches. 0.100 0.123 0.127 0.149 0.157 0.182 0.194 0.293 0.221 0.280 0.304 0.324 0.324	0.298 0.314 0.364 0.388 0.406 0.442 0.560 0.608 0.642 0.682	Inches, 0.205 0.294 0.421 0.542 0.736 0.951 1.272 1.494 1.933 2.315 2.892 3.358 3.818	0.244 0.422 0.587 0.884 1.088 1.491 1.755 2.284 2.716 3.136

#### STANDARD SIZES, ETC., OF LAP-WELDED CHAR-COAL-IRON BOILER-TUBES.

(Morris, Tasker & Co., Limited),

External Diameter.	Internal Diam- eter.	Standard Thick- ness.	Internal Cir- cumference.	External Circumference.	Internal Area.		£xter Are		Length of Tube per Sq. Ft. of InsideSurface.	Length of Tube per Sq. Ft. of Outside Sur- face.	Length of Tube per Sq. Ft. of Mean Surface.	Weight per Lineal Foot.
Ins. 1 1-4 1 1-2 1 3-4 2 1-2 2 3-4 3 1-4 4 1-2 5 6 7 8 9 10 11 12 13 14	Ins 856 1.106 1.334 1.560 1.804 2.054 2.283 2.533 2.783 3.012 3.262 3.512 3.741 4.720 6.657 7.636 6.657 7.636 6.011.542 12.524 13.504	Ins	Ins. 2.689 3.474 4.191 5.667 6.484 7.172 7.957 8.743 9.462 10.248 11.033 11.753 13.818 17.904 22.051 30.074 33.175 36.26	Ins. 3.142 3.927 4.712 5.498 6.283 7.069 7.854 8.639 9.425 10.210 10.995 11.781 12.566 14.137 15.708 18.849 21.991 25.132 28.274	Sq. In.	Sq.Ft .004 .0067 .0097 .0133 .0177 .0230 .0284 .035 .0495 .058 .0673 .0763 .0981 .1215 .1771 .2417 .318 .4048 .4098 .6075 .7205 .8554	Sq. In., 785, 1,227, 1,767, 1,767, 1,767, 2,405, 3,142, 3,142, 4,909, 5,940, 7,069, 8,296, 9,621, 11,045, 12,566, 15,904, 19,635, 28,274, 38,274, 36,265, 63,617, 78,540, 95,033, 113,097, 132,732,153,938	.0055 .0085 .0123 .0167 .0216 .0341 .0412 .0491 .0576 .0668 .0767 .0872 .1104 .1364 .1963 .2673 .3490 .4418 .6601 .7854 .6601	Ft. 4.460 3.455 2.863 8.1455 2.8648 2.118 1.850 1.673 1.508 1.373 1.268 1.171 1.088 1.023 .901 .574 .500 .444 .399 .361 .330 .305 .305 .282	Ft. 3.819 3.056 1.998 1.528 1.999 1.273 1.1091 1.091 1.095 .849 .637 .478 .424 .382 .347 .348 .293 .272	Ft. 4.139 3.255 2.705 2.705 2.705 2.015 2.015 1.774 1.600 1.323 1.221 1.131 1.053 .875 .786 .653 .589 .434 .391 .354 .391 .354 .297	Lbs., .708 .9 1. 25 1. 665 1. 981 2. 238 2. 755 3. 045 3. 3.33 3. 958 4. 273 2.4 590 5. 32 6.01 7. 226 6.01 2. 435 15. 109 18. 002 22. 19 25. 489 28. 516 32. 208 336, 271 366, 271 366, 271 366, 271 366, 271 366, 271 376 276 376 276 376 276 376 276 376 276 376 376 276 376 376 376 376 376 376 376 376 376 3
15 16 17 18 19 20 21	13.504 14.482 15.458 16.432 17.416 18.400 19.360 20.320	.248 .259 .271 .284 .292 .3 .32 .34	45.496 48.562 51.662 54.714 57.805 60.821	43.982 47.124 50.265 53.407 56.548 59.690 62.832 65.973	164.718 187.667 212.227 238.224 265.903 294.373	1.1438 1.3032 1.4738 1.6543 1.8465 2.0443	153 938 176,715 201,062 226,980 254,469 283,529 314,159 346,361	1.2272 1.188 1.5762 1.7671 1.969 2.1817	.263 .247 .232 .219 .207 .197	.272 .254 .238 .224 .212 .200 .190 .181	.277 .258 .242 .228 .215 .203 .193 .184	50.271 40.612 45.199 49.902 54.816 59.479 66.765 73.404

In estimating the effective steam-heating or boiler surface of tubes, the surface in contact with air or gases of combustion (whether internal or external to the tubes) is to

contact with air or gases of community (received the control of th

To find the square feet of surface, S, in a tube of a given length, L, in feet, and diameter, d, in inches, multiply the length in feet by the diameter in inches and by .2618. Or,  $S = \frac{3.1416dL}{L} = .2618dL$ . For the diameters in the

inches and by .2618. Or,  $S=\frac{6478000}{12}=.2618dL$ . For the diameters in the table below, multiply the length in feet by the figures given opposite the diameter.

Inches, Diameter.	Square Feet per Foot Length.	Inches, Diameter.	Square Feet per Foot Length.	Inches, Diameter.	Square Feet per Foot Length.
14 14 32 34 1 114 114 114 134 2	.0654 .1809 .1963 .2618 .3272 .3927 .4581 .5236	21/4 21/2 23/4 3 31/4 31/2 33/4 4	.5890 .6545 .7199 .7854 .8508 .9163 .9817 1.0472	5 6 7 8 9 10 11 12	1.3090 1.5708 1.8326 2.0944 2.3562 2.6180 2.8798 3.1416

#### RIVETED IRON PIPE.

(Abendroth & Root Mfg. Co.)

Sheets punched and rolled, ready for riveting, are packed in convenient form for shipment. The following table shows the iron and rivets required for punched and formed sheets.

required Feet Pu	Square Fe I to make nched and when put t	100 Lineal Formed	nate N rts 1 In- require 0 Line Punch Form	required Feet Pu	Square Fe I to make nched and then put t	100 Lineal Formed	mate No. ets 1 Inch required 00 Lineal Punched Formed
Diam- eter in Inches.	Width of Lap in Inches.	Square Feet.	Approxin of Rive apart for 10 Feet and Sheets.	Diam- eter in Inches.	Width of Lap in Inches.	Square Feet.	Approxi of Riv apart for 16 Feet and Sheets
3 4 5 6 7 8 9 10 11 12 13	1 1 11/2 11/2 11/2 11/2 11/2 11/2 11/2	90 116 150 178 206 234 258 289 314 343 369	1,600 1,700 1,800 1,900 2,000 2,200 2,300 2,400 2,500 2,600 2,700	14 15 16 18 20 22 24 26 28 30 36	11/2 11/2 11/2 11/2 11/2 11/2 11/2 11/2	397 423 452 506 562 617 670 725 779 836 998	2,800 2,900 3,000 3,200 3,500 3,700 3,900 4,100 4,400 4,600 5,200

## WEIGHT OF ONE SQUARE FOOT OF SHEET-IRON FOR RIVETED PIPE.

#### Thickness by the Birmingham Wire-Gauge.

No. of Gauge.	Thick- ness in Decimals of an Inch.	Weight in lbs , Black.	Weight in lbs., Galvan- ized.	No. of Gauge.	Thick- ness in Decimals of an Inch.	Weight in lbs., Black.	Weight in lbs., Galvan- ized.
26	.018	.72	.94	18	.049	1.97	2.19
24	.022	.88	1.13	16	.065	2.61	2.82
22	.028	1.12	1.38	14	.083	3.33	3.52
20	.035	1.40	1.69	12	.109	4.37	4.50

#### SPIRAL RIVETED PIPE.

(Abendroth & Root Mfg, Co.)

Thickness,  B. W. G. Inches.		Diameter, Inches.		ate Weigl er foot in gth.		Approximate Bursting Pressure in lbs. per sq. in.					
26 24 22	.018 .022 .028	3 to 6 3 to 12 3 to 14	lbs.= '' =½ of d	liam. in ji	ns.						
22 20 18 16	.035	3 to 24 3 to 24		" "		2700 1 3600		iam.	in ins.		
16 14	.065 .083	6 to 24 8 to 24	" =.8 " =1.1	" "		4800 6400	"÷	"	66		

The above are black pipes. Galvanized weighs from 10 to 30 per cent heavier. Double Galvanized Spiral Riveted Flanged Pressure Pipe, tested to 150 bts, hydraulic pressure.

Inside diameters, inches Thickness, B. W. G Nominal weight per foot, lbs	3	4	5	6	7	8,	9	10	11	12	13	14	115	16	18	20
Thickness, B. W. G	20	20	20	18	18	18	18	16	16	16	16	14	14	14	14	14
Nominal weight per foot, lbs	21/4	3	4	5	6	7	8	11	12	14	15	20	22	24	59	34

## DIMENSIONS OF SPIRAL PIPE FITTINGS. Dimensions in Inches.

Inside Diameter.	Outside Diameter Flanges.	Number Bolt Holes.	Diameter Bolt Holes.	Diameter Circles on which Bolt Holes are Drilled.	Sizes of Bolts.
ins.  3 4 5 6 7 8 9 10 11 12 13 14 15 16 18 20	6 7 8 8 76 10 11 13 14 15 16 16 17 17 76 19 21 3 14 25 16 23 14 25 16	4 8 8 8 8 8 8 12 12 12 12 12 12 12 12 12	1272 278 28 28 28 28 28 28 28 28 28 28 28 28 28	434 5 15-16 6 15-16 776 9 10 1114 1234 1234 1336 1444 1544 1644 17 7-16 1944 2144 2214 2214 2216	7-16 × 13444 1-16 × 13444 1-16 × 13444 1-16 × 13444 1-16 × 13444 1-16 × 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2

#### SEAMLESS BRASS TUBE. IRON-PIPE SIZES.

(Randolph & Clowes),

(For actual dimensions see tables of Wrought-iron Pipe.)

Nominal Size.	Weight per Foot, lbs.	Nom- inal Size.	Weight per Foot, lbs.	Nom- inal Size.	Weight per Foot, lbs.	inal	Weight per Foot, lbs.
1/8 1/4 3/6 1/2	.266 .461 .617 .925	34 1 11/4 11/4	1.228 1.837 2.468 3.045	2 2½ 3 3½ 3½	4. 6.323 8.266 9.878	4 5 6 7 8	11.719 15.935 20.690 26.286 29.881

#### SEAMLESS DRAWN BRASS-TUBING.

(Randolph & Clowes, Waterbury, Conn.)

Outside diameter 3-16 to 734 inches. Thickness of walls 8 to 25 Stubbs' Gauge, length 12 feet. The following are the standard sizes:

#### SEAMLESS DRAWN BRASS-TUBING.

Outside Diam- eter.	Length Feet.	Stubbs' or Old Gauge.	Outside Diam- eter.	Length Feet.	Stubbs' or Old Gauge.	Ontside Diam- eter.	Length Feet.	Stubbs' or Old Gauge.
5-16 38 15-25 54 13-16 78 15-16 114 114	12 12 12 12 12 12 12 12 12 12 12 12 12	20 19 19 18 18 17 17 17 17 16 16	13/6 11/6 15/8 13/4 1 13-16 17/8 1 15-16 2 21/8 21/4 23/6 21/2	19 12 12 12 12 12 12 12 12 12 12 12	14 14 18 18 18 12 12 12 12 12 12 12	25/3/4 23/4 31/5 4 51/4/3/4 55/3/4	12 12 12 12 12 12 10 to 12 10 to 12 10 to 12 10 to 12 10 to 12 10 to 12	11 11 11 11

#### COILED PIPES.

(National Pipe-bending Co., New Haven, Conn.)

#### COILS OF STEEL OR IRON PIPE; WELDED LENGTHS.

		Butt	-wel	ded I	Pipe		La wel Pi	ded
Size of pipeInches Least outside diameter of coil contain-	′ -	3/8	1/2	3/4	1	11/4	11/2	2
ing 25 feet of pipe and less Inches Least outside diameter of coils over 25 feet and not over 200 feet Inches		21/2 7	3½ 7½	4 8½	9	11	12	18 18

#### COILS OF SEAMLESS DRAWN BRASS AND COPPER TUBING.

Size of tube, outside diameterIns. Least outside diam- eter of coilsIns. 1	3/8 1/2 11/2 2		34 1 3	1½ 1¾ 6 7	1½ 1¾ 8 10	2 2 14	4 23% 23½ 16 18
---	-------------------	--	--------	--------------	---------------	--------	--------------------

Welded solid drawn-steel tubes, imported by P. S. Justice & Co., Philadelphia, are made in sizes from  $\frac{1}{2}$  to  $\frac{4}{2}$  inches external diameter, varying by  $\frac{1}{2}$ ths, and with thickness of walls from 1-16 to 11-16 inches. The maximum length is 15 feet,

#### WEIGHT OF BRASS, COPPER, AND ZING TUBING. Per Foot.

Thickness by Brown & Sharne's Gauge

Brass,	Brass, No. 17.		No. 20.	Copper, Lightning-rod Tube, No. 23.		
Inch.  14 5-16 36 7-16 12 9-11 56 34 76	Lbs. .107 .157 .185 .234 .266 .318 .393 .377 .462	Inch.  1/8 3-16 1/4 5-16 3/8 7-16 1/4 9-16	Lbs. .032 .039 .063 .106 .126 .158 .189 .208 .220	Inch.  1/2 9-16 9/8 11-16 3/4  Zinc,	Lbs. .162 .176 .186 .211 .229	
11/6 11/4 11/6 13/4 2 21/6 3	.675 .740 .915 .980 1.90 1.506 2.188	178 114 114 11%	.284 .378 .500 .580	1/6 5/8 3/4 7/6 1 11/4 11/2	.161 .185 .234 .272 .311 .380 .452	

#### LEAD PIPE IN LENGTHS OF 10 FEET.

In.	3-8 Thick.		5-16 7	5-16 Thick.		1/4 Thick.		Thick.
2½ 3 3½ 4 4 4½ 5	lb. 17 20 22 25 31	0	1b. 14 16 18 21	oz. 0 0 0 0 0	lb. 11 12 15 16 18 20	OZ. 0 0 0 0 0 0 0	lb. 8 9 9 12 14	oz. 0 0 8 8 8

#### LEAD WASTE-PIPE.

1½ in., 2 lbs. per foot. 2 " 3 and 4 lbs. per foot. " 31/2 and 5 lbs. per foot.

31/2 in., 4 lbs. per foot. Foot. 4 " 5, 6, and 8 lbs. 5 in. 8, 10, and 12 lbs.

#### LEAD AND TIN TUBING.

1/2 inch.

1/4 inch.

#### SHEET LEAD.

Weight per square foot, 21/2, 3, 31/2, 4, 41/2, 5, 6, 8, 9, 10 lbs. and upwards. Other weights rolled to order.

#### BLOCK-TIN PIPE.

3% in , 4½, 6½, and 8 oz. per foot. ½ " 6, 7½, and 10 oz. " 58 " 8 and 10 oz. " ¾ " 10 and 12 oz. "

1 in., 15, and 18 oz. per foot. 1¼ " 1¼ and 1½ lbs. " 1½ " 2 and 2½ lbs. " 2 " 2½ and 3 lbs. "

#### LEAD AND TIN-LINED LEAD PIPE.

(Tatham & Bros., New York.)

		(Tuthum 6		DI, 21011	I OI II.)		
Calibre.	Letter.	Weight per Foot and Rod.	Thickness in 1-100th In.	Calibre.	Letter,	Weight per Foot and Rod.	Thickness in 1-100th In.
% in	E D C B A AAA AAA AAA AAAA AAAA	7 lbs. per rod 10 oz. per foot 12 " " 1 lb. " 114 " " 1 lb. " 1 lb. " 1 lb. " 1 lb. per rod 3 lb. per rod 3 lb. per rod 1 lb. " 1 lc " " 1	6 8 12 16 19 27 7 9 11 13 16 19 23 25 8 9 13 16 20 22 25	1 in. " " " " " " " " " " " " " " " " " " "	E D C B A AAA AAA E D C B B A AAAA C B B A AAAA AAA C B B A AAAA AAA	11/4 lbs. per foot 22 " " " " " " " " " " " " " " " " " "	10 11 11 14 17 21 24 30 10 12 14 16 19 25 12 14 17 19 23 27
34 in.	E D C B A AA AAA	114 " per foot 114 " " 134 " " 214 " " 3 " " 316 " " 434 " "	8 10 12 16 20 23 30	2 .in.	C B A AA AAA	434 6 7 9 1134	15 18 22 27

## WEIGHT OF LEAD PIPE WHICH SHOULD BE USED FOR A GIVEN HEAD OF WATER.

(Tatham & Bros., New York,)

Head or Number	Pressure		Calibre and Weight per Foot.								
of Feet Fall.	sq. inch.	Letter.	¾ inch.	⅓ inch.	% inch.	34 inch.	1 inch.	1¼ in.			
30 ft.	15 lbs.	D	10 oz.	3/4 lb.	1 lb.	1½ lbs.	2 lbs.	21/6 lbs.			
50 ft. 75 ft.	25 lbs. 38 lbs.	D C B A	12 oz. 1 lb.	1 lb. 1½ lbs.	11/2 lbs.	134 lbs.	2½ lbs. 3¼ lbs.	3 lbs.			
100 ft. 150 ft.	50 lbs. 75 lbs.	AA	1¼ lbs. 1½ lbs.	2 lbs.	234 lbs.	31/2 lbs.	43/4 lbs.	6 lbs.			
200 ft.	100 lbs.	AAA	134 lbs.	3 lbs.	31/2 lbs.	43/4 lbs.	6 lbs.	6¾ lbs.			

To find the thickness of lead pipe required when the head of water is given. (Chadwick Lead Works).

Rule.—Multiply the head in feet by size of pipe wanted, expressed decimally, and divide by 750; the quotient will give thickness required, in one-hundredths of an inch.

EXAMPLE.—Required thickness of half-inch pipe for a head of 25 feet.

# WEIGHT OF COPPER AND BRASS WIRE AND PLATES.

Brown & Sharpe's Gauge.

1	i ei		9098818868080041014	
	Plates p Foot.	Brass.	1.25% 1.25% 1.26%	
	Weight of Plates per Square Foot.	Copper.	11.59 11.59 11.15 19.17 19.17 19.17 19.18	
	Wire per al Feet.	Brass.	1 bs. 2.217 1.1588 1.1588 1.1588 1.1588 1.1588 1.1588 1.157 1.157 1.157 1.157 1.157 1.157 1.158	
	Weight of Wire per 1,000 Lineal Feet.	Copper.	11.54 11.54 11.55	
acturers.)	Size of	,	Inch.   Construction   Constructio	
(From tables of leading manufacturers.	No. of	- Samp	202 202 202 202 202 202 202 202 202 202	
les of lead	Plates per Foot.	Brass.	日本にたおおになるためのの4.48888488411111 888288888458888888888848411111	
(From tab	Weight of Plates per Square Foot.	Copper.	12875421100000044000000011 .%2787611689422232331111	
	Wire per	Brass.	128-528-83878-1-4-1-4-1-4-4-4-4-4-4-4-4-4-4-4-4-4-4-	
	Weight of Wire per 1000 Lineal Feet.	Copper.	2.4.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2.2	
	Size of	Each No.	Inch.   4000	

#### WEIGHT OF ROUND BOLT COPPER.

#### Per Foot.

Inches.	Pounds.	Inches.	Pounds.	Inches.	Pounds.
3/8 1/2 5/8/4 7/8	.425 .756 1.18 1.70 2.31	1 11/6 11/4 13/6 11/2	3.02 3.83 4.72 5.72 6.81	15/8 13/4 17/8	7.99 9.27 10.64 12.10

#### WEIGHT OF SHEET AND BAR BRASS.

-							
Thick- ness. Inches.	Sheets per sq. ft.	Square Bars 1 ft. long.	Round Bars 1 ft. long.	Thick- ness. Inches.	Sheets per sq. ft.	Square Bars 1 ft, long.	Round Bars 1 ft. long.
1-16 1/8 3-16	lbs. 2.7 5.41	lbs. .015 .055	lbs. .011 .045	1 1-16 11/8 1 3-16	lbs. 45.95 48.69	lbs. 4.08 4.55	lbs 3.20 3.57
3-16 14 5-16 3/8 7-16	8.12 10.76 13.48 16.25	.125 .225 .350 .51	.1 .175 .275 .395 .54	1 3-16 11/4 1 5-16 13/8 1 7-16	51.4 54.18 56.85 59.55 62.25	5.08 5.65 6.22 6.81 7.45	3.97 4.41 4.86 5.35 5.85
7-16 5/8 9-16 5/8 11-16	21.65 24.3 27.12 29.77	.905 1.15 1.4 1.72	.54 .71 .9 1.1 1.35	1 % 10 11% 1 9-16 15% 1 11-16	65 67.75 70.85	8.13 8.83 9.55 10.27	6.37 6.92 7.48 8.05
13-16 13-16 7/8 15-16	32.46 35.18 37.85 40.55	2.05 2.4 2.75 3.15	1.66 1.85 2.15 2.48	134 1 13-16 176 1 15-16	75.86 78.55 81.25 84	11 11.82 12.68 13.5	8.65 9.29 9.95 10.58
1	43.29	3.65	2.85	2	86.75	14.35	11.25

## COMPOSITION OF VARIOUS GRADES OF ROLLED BRASS, ETC.

Trade Name.	Copper	Zine.	Tin.	Lead.	Nickel.
Common high brass	61.5	38.5			
Yellow metal	60	40			
Cartridge brass	66¾ 80	33½ 20			
Low brass	80				
Clock brass	60	40		11/6	
Drill rod	60	40		11/2 to 2	
Spring brass	66%	331/3	11/2		
18 per cent German silver	611/2	201/2			18

The above table was furnished by the superintendent of a mill in Connecticut in 1894. He says: While each mill has its own proportions for various mixtures, depending upon the purposes for which the product is intended, the figures given are about the average standard. Thus, between cartridge brass with 33½ per cent zinc and common high brass with 38½ per cent zinc, there are any number of different mixtures known generally as "high brass," or specifically as "spinning brass," drawing brass," etc., wherein the amount of zinc is dependent upon the amount of scrap used in the mixture, the degree of working to which the metal is to be subjected, etc.

#### AMERICAN STANDARD SIZES OF BROD-SHOT

28.418.83	THE ROLLING	THE PARTY	AP 28 A	CAP IS A RELATION		WATER OF	- COLLO I	•
	Diameter.	No. of Shot to the oz.			No. of Shot to the oz.		Diam- eter.	No. of Shot to the oz.
Fine Dust. Dust. No. 12. " 11. " 10. " 10. " 9.	3-100" 4-100 5-100 6-100 Trap Shot 7-100" Trap Shot 8-100"	4565 2326 1346 1056 848	" 6 " 5 " 4	Trap Shot 9-100" Trap Shot 10-100" 11-100 12-100 13-100 14-100	399	No. 2 " 1 " B " BB " BBB " T " TT " F " FF	15-100" 16-100 17-100 18-100 19-100 20-100 21-100 22-100 23-100	86 71 59 50 42 36 31 27 24

#### COMPRESSED BUCK-SHOT.

	Diameter.	No. of Balls to the lb.		Diameter.	No. of Balls to the lb.
No. 3		232	No. 00 000 Balls		115 98 85 50

#### SCREW-THREADS, SELLERS OR U. S. STANDARD.

In 1864 a committee of the Franklin Institute recommended the adoption of the system of screw-threads and bolts which was devised by Mr. William Sellers, of Philadelphia. This same system was subsequently adopted as the standard by both the Army and Navy Departments of the United States, and by the Master Mechanics' and Master Car Builders' Associations, so that it may now be regarded, and in fact is called, the United States Standard.

The rule given by Mr. Sellers for proportioning the thread is as follows: Divide the pitch, or, what is the same thing, the side of the thread, into eight equal parts; take off one part from the top and fill in one part in the bottom of the thread; then the flat top and bottom will equal one eighth of the pitch, the wearing surface will be three quarters of the pitch, and the diameter of screw at bottom of the thread will be expressed by the formula

1.299

diameter of bolt  $-\frac{1}{100}$  no. threads per inch

For a sharp V thread with angle of 60° the formula is

diameter of bolt  $-\frac{1.100}{\text{no. of threads per inch}}$ 

The angle of the thread in the Sellers system is 60°. In the Whitworth or English system it is 55°, and the point and root of the thread are rounded.

#### Screw-Threads, United States Standard.

Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.
5-16 3/8 7-16 1/2 9-16 5/8 11-16	20 18 16 14 13 12 11	34 13-16 78 15-16 1 1 1-16 1½	10 10 9 9 8 7	11/4 1 5-16 13/8 11/2 15/8 13/4 17/8	7 6 6 6 5 5 5 5	1 15-16 2 21/4 2 5-16 23/6 21/2 23/4	5 41/2 41/2 41/2 4 4 4 4	2 13–16 3 31/4 3 5–16 31/2 33/4 4	31/2 31/2 31/2 31/4 31/4 31/4 3

#### Screw-Threads, Whitworth (English) Standard.

Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.	Diam.	Pitch.
5-16 3/8 7-16 1/2 9-16	20 18 16 14 12 12	5/8 11-16 3/4 13-16 7/8 15-16	11 11 10 10 9 9	1 11/8 11/4 13/8 11/6 15/8	8 7 6 6 5	134 17/8 2 21/4 21/3 23/4	5 41/2 41/2 4 4 31/2	3 31/4 31/2 33/4 4	31/4 31/4 31/4 3 3

#### U. S. OR SELLERS SYSTEM OF SCREW-THREADS.

Ins.   Ins.	В	BOLT	S AN	D TH	REAL	s.	HE	x, NUT	S AND	HEA	DS.	÷.
$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	Diam. of Bolt.	Threads per Inch.	Diam. of Root of Thread.	Width of Flat.	Area of Bolt Body in Sq. Inches.	Area at Root of Thread in Sq. Inches.	Short Diam., Rough.	Short Diam., Finish.	Long Diam., Rough.	Thickness, Rough:	Thickness, Finish.	Long Diam. Sq Nuts Rough.
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Ins.		Ins.	Ins.			Ins.	Ins.	Ins.	Ins.	Ins.	Ins.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	14 16 38 16 16 17 18 18 17 18 18 18 18 18 18 18 18 18 18 18 18 18	13 12 11 10 9 8 7 7 6 6 5 5 5 4 4 4 4 3 1,2 3 4 4 3 1,2 4 4 3 3 4 4 4 3 4 4 4 4 4 4 4 4 4 4 4	.240 .294 .400 .454 .450 .620 .731 .065 .940 .1 .065 .1 .160 .1 .284 .1 .389 .1 .161 .1 .12 .2 .176 .2 .426 .2 .2 .2 .2 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3	.0074 .0078 .0079 .0089 .0096 .0104 .0113 .0125 .0138 .0208 .0277 .0250 .0277 .0312 .0357 .0312 .0357 .0313 .0413 .0413 .0456	0777 .110 .150 .196 .249 .3070 .442 .601 .7855 .1 .455 .2 .761 .3 .142 .4 .909 .4 .909 .1 .227 .7 .059 .8 .299 .1 .1 .455 .1 .	0455 0686 11626 11	19-32 11-16 25-32 76 31-32 11-16 117-16 117-16 117-16 117-16 123-16 23-16 234 458 5534 458 5534 6612 886	7-16 17-32 96 23-32 13-16 29-32 1 13-16 134 13-16 134 23-5-16 22 11-16 22 3-16 3 13-16 4 9-16 4 9-16 4 9-16 6 7-16 6 7-16 6 7-16 6 7-16 6 7-16 7 9-16 7 15-16 8 5-16	37-64 11-16 51-64 9-10 1 17-32 1 17-32 2 1-32 1 17-32 2 5-16 3 13-32 3 3-16 3 13-32 3 3-16 6 7-64 6 7-64 6 7-7 7 31-32 8 17-32 8 17-32 8 17-32 9 9-32 9 9-32	19-16 19-16 11-18-18-18-18-18-18-18-18-18-18-18-18-1	3-16 14 5-16 3-16 11-16 15-16 15-16 15-16 1 15-16 1 15-16 1 15-16 2 15-16 3 15-16 3 15-16 3 15-16 3 15-16 3 15-16 4 15-16 4 15-16 4 15-16 4 15-16 5 3-16 5 3-16 5 3-16 5 5-16	1 23-64 11/49-61 2 1-32 2 19-64 2 9-16 2 9-16 3 3-32 3 23-64 35/4 3 57-61 4 5-32 4 27-64 4 5-32 4 27-64 5 31-64 6 17-32 7 1-16 7 39-64 9 3-16 9 3/4 10/4 9 3-16 10 49-64 11 23-64

#### LIMIT GAUGES FOR IRON FOR SCREW THREADS.

In adopting the Sellers, or Franklin Institute, or United States Standard, as it is variously called, a difficulty arose from the fact that it is the habit from manufacturers to make iron over-size, and as there are no over-size

screws in the Sellers system, if iron is too large it is necessary to cut it away screws in the Seiters system, it iron is too large it is necessary to cut it away with the dies. So great is this difficulty, that the practice of making taps and dies over-size has become very general. If the Sellers system is adopted it is essential that iron should be obtained of the correct size, or very nearly so. Of course no high degree of precision is possible in rolling iron, and when exact sizes were demanded, the question arose how much allowable variation; there should be from the true size. It was proposed to make limit to some the second of t gauges for inspecting iron with two openings, one larger and the other smaller than the standard size, and then specify that the iron should enter the large end and not enter the small one. The following table of dimensions for the limit-gauges was recommended by the Master Car-Builders' sistion and adopted by letter hallot in 1883

Associa	tion and a	dopted by	letter bar	100 111 100	J.		
Size of Iron.	Size of Large End of Gauge.	Size of Small End of Gauge.	Differ- ence.	Size of Iron.	Size of Large End of Gauge.	Size of Small End of Gauge.	Differ- ence.
1/4 in. 5-16 3/8 7-16 1/2 9-16	0.2550 0.3180 0.3810 0.4440 0.5070 0.5700	0.2450 0.3070 0.3690 0.4310 0.4930 0.5550	0.010 0.011 .0.012 9.013 0.014 0.015	5% in. 34 78 1 11% 114	0.6330 0.7585 0.8840 1.0095 1.1350 1.2605	0.6170 0.7415 0.8660 0.9905 1.1150 1.2395	0.016 0.017 0.018 0.019 0.020 0.021

Caliper gauges with the above dimensions, and standard reference gauges for testing them are made by the Pratt & Whitney Co.

## THE MAXIMUM VARIATION IN SIZE OF ROUGH IRON FOR U. S. STANDARD BOLTS.

Am. Mach., May 12, 1892.

By the adoption of the Sellers or U. S. Standard thread taps and dies keep their size much longer in use when flatted in accordance with this system than when sharp, though it has been found advisable in practice in most cases to make the taps of somewhat larger outside diameter than the nominal size, thus carrying the threads further towards the V-shape and giving corresponding clearance to the tops of the threads when in the nuts or

tapped holes.

Makers of taps and dies often have calls for taps and dies, U. S. Standard,

"for rough iron," An examination of rough iron will show that much of it is rolled out of

round to an amount exceeding the limit of variation in size allowed.

In view of this it may be desirable to know what the extreme variation in iron may be, consistent with the maintenance of U.S. Standard threads, i.e., threads which are standard when measured upon the angles, the only place where it seems advisable to have them fit closely. Mr. Chas. A. Bauer, the general manager of the Warder, Bushnell & Glessner Co., at Springfield, Ohio, in 1884 adopted a plan which may be stated as follows: All bolts, whether cut from rough or finished stock, are standard size at the bottom and at the sides or angles of the threads, the variation for fit of the nut and allowance for wear of taps being made in the machine taps. Nuts are punched with holes of such size as to give 85 per cent of a full thread, experience showing that the metal of wrought nuts will then crowd into the threads of the taps sufficiently to give practically a full thread, while if punched smaller some of the metal will be cut out by the tap at the bottom of the threads, which is of course undesirable. Machine taps are made enough larger than the nominal to bring the tops of the threads up sharp, plus the amount allowed for fit and wear of taps. This allows the iron to be enough above the nominal diameter to bring the threads up full (sharp) at top, while if it is small the only effect is to give a flat at top of threads; neither condition affecting the actual size of the thread at the point at which it is intended to bear. Limit gauges are furnished to the mills, by which the iron is rolled, the maximum size being shown in the third column of the table. The minimum diameter is not given, the tendency in rolling being nearly always to exceed the nominal diameter.

In making the taps the threaded portion is turned to the size given in the eighth column of the table, which gives 6 to 7 thousandths of an inch allowance for fit and wear of tap. Just above the threaded portion of the tap a place is turned to the size given in the ninth column, these sizes being the same as those of the regular U. S. Standard bott, at the bottom of the thread, plus the amount allowed for fit and wear of tap;  $\sigma$ ,  $\sigma$ , in other words, d'=U. S. Standard d+(D'-D). In flushing the threads of the tap a tool 72, are furnished for this sizing. In flushing the threads of the tap a tool



Fig. 72.

is used which has a removable cutter finished accurately to gauge by grinding, this tool being correct U. S. Standard as to angle, and flat at the point. It is fed in and the threads chased until the flat point just touches the portion of the tap which has been turned to size d'. Care having been taken with the form of the tool, with its grinding on the top face (a fixture being provided for this to insure its being ground properly), and also with the setting of the tool properly in the lathe, the result is that the threads of the tap are correctly sized without further attention

ting of the tool properly in the lathe, the result is that the threads of the tap are correctly sized without further attention.

It is evident that one of the points of advantage of the Sellers system is sacrificed, i.e., instead of the taps being flatted at the top of the threads they are sharp, and are consequently not so durable as they otherwise would be; but practically this disadvantage is not found to be serious, and is far overbalanced by the greater ease of getting iron within the prescribed limits; while any rough bolt when reduced in size at the top of the threads, by filing or otherwise, will fit a hole tapped with the U. S. Standard hand taps, thus affording proof that the two kinds of bolts or screws made for the two different kinds of work are practically interchangeable. By this system \( \frac{1}{2} \) '' iron can be .005'' smaller or .0809'' larger than nominal—a total variation of .0158'', while 1½'' iron can be .0105'' smaller or .0809'' larger than nominal—a total variation of .0144''—and within these limits it is found practicable to procure the iron.

#### STANDARD SIZES OF SCREW-THREADS FOR BOLTS AND TAPS. (Chas. A. Bauer.)

1	2	3	4	5	6	7	8	9	10
A	$\overline{n}$	D	d	h	f	D'-D	D'	d'	H
5-16 3%	20 18 16	Inches. .2608 .3245 .3885	Inches. .1855 .2403 .2938	Inches. .0379 .0421 .0474	Inches. .0062 .0070 .0078	Inches. .006 .006	Inches. .2668 .3305 .3945	Inches. .1915 .2463 .2998	Inches. .2024 .2589 .3139
3/8 7-16 5/8 9-16 3/4 7/8	14 13 12 11	.4530 .5166 .5805 .6447	.3447 .4000 .4543 .5069	.0541 .0582 .0631 .0689	.0089 .0096 .0104 .0114	.006 .006 .007	.4590 .5226 .5875 .6517	.3507 .4060 .4613 .5139	.3670 .4236 .4802 .5346
1 11/8 11/4	10 9 8 7	.7717 .8991 1.0271 1.1559 1.2809	.6201 .7307 .8376 .9394 1.0644	.0758 .0842 .0947 .1083 .1083	.0125 .0139 .0156 .0179 .0179	.007 .007 .007 .007	.7787 .9061 1.0341 1.1629 1.2879	.6271 .7377 .8446 .9464 1.0714	.6499 .7630 .8731 .9789 1.1039

A = nominal diameter of bolt.

D = actual diameter of bolt.

d =diameter of bolt at bottom of thread.

n =number of threads per inch.

f =flat of bottom of thread,

h = depth of thread.

D' and d' = diameters of tap. H = hole in nut before tapping.

$$D = A + \frac{.2165}{n},$$

$$d = A - \frac{1.29904}{n},$$

$$h = \frac{.7577}{n} = \frac{D - d}{2},$$

$$f = \frac{.125}{n},$$

$$H = D' - \frac{1.288}{n} = D' - .85(2h.)$$

#### STANDARD SET-SCREWS AND CAP-SCREWS.

American, Hartford, and Worcester Machine-Screw Companies. (Compiled by W. S. Dix.)

Diameter of Screw Threads per Inch Size of Tap Drill*	(A) 1/8 40 No. 43	(B) 3-16 24 No. 30	(C) 14 20 No. 5	(D) 5-16 18 17-64	(E) 3/8 16 21-64	(F) 7-16 14 3/8	(G) 12 12 27-64
Diameter of Screw Threads per Inch Size of Tap Drill*	(H) 9-16 12 31-64	(I) 5% 11 17-32	(J) 34 10 21-32	(K) 7/8 9 49-64	(L) 1 8 7/8	(M) 1½ 7 63-64	(N) 1½ 7 1½

	Set Scre	ws.	Hex. I	Head Ca	p-screws.	Sq. Head Cap-screws.			
S ort Diam of Head	Long Diam. of Head	Lengths (under Head).	Short Diam. of Head.	of	Lengths (under Head).	Short Diam. of Head.	Long Diam. of Head.	Lengths (under Head).	
(C) ½4 (D) 5-16 (E) 3% (F) 7-16 (G) ½6 (H) 9-16 (I) 5% (J) 3½ (K) 7% (L) 1 (M) 1½ (N) 1½	.53 .62 .71 .80 .89 1.06 1.24 1.42 1.60	34 to 3 34 to 334 34 to 334 34 to 433 34 to 44 34 to 44 34 to 44 31 to 434 114 to 5 134 to 5 134 to 5	7-16 1/2 9-16 5/8 3/4 13-16 7/6 1 11/8 11/4 13/8 11/2	.51 .58 .65 .72 .87 .94 1.01 1.15 1.30 1.45 1.59 1.73	34 to 3 34 to 334 34 to 334 34 to 434 1 to 444 1 to 444 114 to 434 114 to 5 134 to 5 2 to 5 2 to 5	9-16 5/8 11-16	.53 .62 .71 .80 .89 .98 1.06 1.24 1.60 1.77 1.95 2.13	34 to 3 34 to 314 34 to 315 34 to 334 34 to 44 34 to 44 1 to 44 114 to 434 115 to 5 2 to 5 214 to 5	

Round and F Cap-s	Filister Head screws.	Flat Head	Cap-screws.	Button-head Cap- screws.		
Diam. of Head.	Lengths (under Head).	Diam. of Head.	Lengths (including Head).	Diam. of Head.	Lengths (under Head).	
(A) 3-16 (B) 14 (C) 38 (D) 7-16 (E) 9-16 (F) 54 (G) 34 (H) 13-16 (H) 13-16 (J) 1 (K) 114	34 to 2½ 34 to 234 34 to 3 34 to 3 34 to 3 34 to 3 34 to 3 34 to 4 1 to 44 114 to 434 114 to 434 134 to 5	144 386 15-32 566 34 13-16 78 1 118 138	34 to 134 34 to 24 34 to 24 34 to 234 34 to 3 1 to 3 114 to 3 115 to 3 1 to 3 1 to 3 1 to 3 1 to 3 1 to 3 1 to 3	7-82 (.225) 5-16 7-16 9-16 9-16 56 13-16 15-16 1 11/4	34 to 134 34 to 2 34 to 214 34 to 214 34 to 234 4 to 3 114 to 3 115 to 3 134 to 3	

\* For cast iron.

Threads are U. S. Standard. Cap-screws are threaded 34 length up to and including 1" diam.  $\times$  4" long, and  $\frac{1}{2}$  length above. Lengths increase by  $\frac{1}{4}$ " each regular size between the limits given. Lengths of heads, except flat and button, equal diam. of screws. The angle of the cone of the flat-head screw is 76°, the sides making angles of 52° with the top.

#### STANDARD MACHINE SCREWS.

(Am. Screw Co.'s Catalogue, 1883, 1892.)

No.	Threads per	Diam. of	OI Flat	Diam, of Round	Diam. of Filister	Lengths.		
140.	Inch.	Body.	Head.	Head.	Head.	From	То	
2	56	.0842	.1631	.1544	.1332	3–16	1/2	
3	48	.0973	.1894	.1786	.1545	3-16	5/8	
2 3 4 5 6 7 8 9	32, 36, 40	.1105	.2158	.2028	.1747	3-16	1/2 5/8 3/4 7/8	
5	32, 36, 40	.1236	.2421	.2270	.1985	3-16	7/8	
6	30, 32	.1368	.2684	.2512	.2175	3-16	1	
7	30, 32	.1500	.2947	.2754	.2392	1/4	11/8	
8	30, 32	.1631	.3210	.2936	.2610	24	11/4	
9	24, 30, 32	.1763	.3474	.3238	.2805	14	13%	
10	24, 30, 32	.1894	.3737	.3480	.3035	24	11/2	
12	20, 24	.2158	.4263	.3922	.3445	8	19/4	
14	20, 24	.2421	.4790	.4364	.3885	%	2017	
16	16, 18, 20	.2684	.5316	.4866	.4300	18	274	
18	16, 18	.2947	.5842	.5248	.4710	72	272	
20 22	16, 18	.3474	.6368 .6894	.5690 .6106	.5200	1/2	294	
24	16, 18 14, 16	.3737	.7420	.6522	,6005	72	9	
26		.4000	.7420	.6938	.6425	3/2	3	
28	14, 16 14, 16	.4263	.7946	.7354	.6920		3 3 3	
30		.4520	.8473	.7770	.7240	1/8	9	
50	14, 16	.4550	0419	.1110	.1240	1		

Lengths vary by 16ths from 3-16 to  $\frac{1}{2}$ , by Sths from  $\frac{1}{2}$  to  $\frac{1}{2}$ , by 4ths from  $\frac{1}{2}$  to 3.

## SIZES AND WEIGHTS OF SQUARE AND HEXAGONAL NUTS.

United States Standard Sizes, Chamfered and trimmed, Punched to suit U. S. Standard Taps.

Bolt.	,		Hole.	a. Sq.	Diam. Nuts.	_	are.	Hexa	
Diam. of I	Width.	Thickness.	Diam. of I	Long Diam. Nuts.	Long Di Hex. Nu	No. in 100 lbs.	Wt. each in lbs.	No. in 100 lbs.	Wt. each in lbs.
146 5-16 8-8-6 7-16 1-19-16 1-19-18-18-18-18-18-18-18-18-18-18-18-18-18-	19-32 11-16 25-32 76 31-32 1 1-16 14 1 7-16 2 2 3-16 2 34 2 15-16 33/6 31/6 31/6 31/6 31/6 31/6 31/6 31	5/8 3/4 7/8 1 11/6 11/4	19-64	11-16 1 13-16 1 148 1148 1148 1149 124 134 134 134 2 1-16 2 5-16 2 13-16 348 338 338 447 47-16 4 15-16 6 6 6 6	9-16 11-16 13-16 7/8 11/8 11/4 11 7-16 1 11-16 17/8 2 1-16 2 5-16 2 5-16 2/2 2/3/4 2 15-16 3/8 3 3-16 3/8 4 1-16 4 1/5-16 5 5-16	7270 4700 4700 2350 1630 1120 890 640 280 280 170 58 44 34 34 34 32 32 19 12 9	.0138 .0231 .0426 .0613 .0893 .1124 .156 .263 .357 .588 .769 1.04 1.72 2.27 2.294 3.33 4.25 5.26 8.33 1.111 13.64	7615 5200 3000 2000 1430 1100 740 450 309 216 148 55 68 40 37 29 21 15 11 85/2	.0131 .0192 .0338 .050 .070 .091 .135 .222 .468 .676 .901 1.18 1.47 1.79 2.50 2.70 3.45 4.76 6.67 9.09 11.76

#### WEIGHTS OF 100 BOLTS WITH SQUARE HEADS AND NUTS.

(Hoopes & Townsend's List.)

Length un- der Head				Dian	neter o	f Bolts.			
to Point.	¼ in.	5-16 in.	3% in.	7–16 in.	1⁄2 in.	5% in.	3/4 in.	% in.	1 in.
11/	lbs. 4.00	lbs.	lbs.	lbs. 15.20	lbs. 22,50	lbs. 39.50	lbs. 63.00	lbs.	lbs.
11/2 13/4 2	4.35	7.50	11.25		23.82	41.62	66.00		
274	4.75	8.00	12.00		25.15	43.75	69.00	109.00	163
21/4	5.15	8.50	12.75	18.50	26.47	45.88	72.00	113.25	169
21%	5.50	9.00	13.50	19.60	27.80	48.00	75.00	117.50	174
23%	5.75	9.50	14.25	20.70	29.12	50.12	78.00	121.75	180
21/4 21/2 23/4 3	6.25	10.00	15.00	21.80	30.45	52.25	81.00	126.00	185
. 81/2	7.00	11.00	16.50	24.00	33.10	56.50	87.00	134.25	196
4	7.75	12.00	18.00	26.20	35.75	60.75	93.10	142.50	207
41/2	8.50	13.00	19.50		38.40	65.00	99.05	151.00	218
5	9.25	14.00	21.00	30.60	41.05	69.25	105.20	159.55	229
51/2	10.00	15.00	22.50	32,80	43.70		111.25	168.00	240
6 ~	10.75	16.00	24.00	35.00	46.35	77.75	117.30	176.60	251
61/2			25.50	37.20	49.00	82.00	123.35	185.00	262
7.7		, .	27.00	39.40	51.65	86.25	129.40	193.65	273
71/2 8 9			28.50	41.60	54.30	90.50	135.00	202.00	284
8			30.00	43.80	59.60	94.75	141.50	210.70	295
10		••••		46.00	64.90	103.25	153.60	227.75	317
10 11			• • • • • •	48.20	$70.20 \\ 75.50$	111.75 120.25	165.70 177.80	224.80 261.85	339
12				52.60	80.80	128.75	189.90	278.90	360 382
13				32.00	86.10	137.25	202.00	295.95	404
14					91.40	145.75	214.10	313.00	426
15		•••••			96.70	154.25	226.20	330.05	448
16					102.00	162.75	238.30	347.10	470
17					107.30	171.00	250.40	364.15	492
18					112.60	179.50	262.60	381.20	514
19					117.90	188.00	274.70	398.25	536
20					123.20	206.50	286.80	415.30	558
Per inch additional.	}1.37	2.13	3.07	4.18	5.45	8.52	12.27	16.70	21.82

TRACK BOLTS.

#### With United States Standard Hexagon Nuts.

Rails used.	Bolts.	Nuts.	No. in Keg, 200 lbs.	Kegs per Mile.
45 to 85 lbs	34 × 41/4 34 × 4 34 × 33/4 34 × 31/6 34 × 31/4 34 × 31/4	114 114 114 114 114 114 114	230 240 254 260 266 283	6.3 6. 5.7 5.5 5.4 5.1
30 to 40 lbs	5/8 × 31/2 5/8 × 3 5/8 × 23/4 5/8 × 21/2	1 1-16 1 1-16 1 1-16 1 1-16	375 410 435 465	4. 3.7 3.8 3.1
20 to 30 lbs	14×3 14×214 14×214 14×2	7/8 7/8 7/8 7/8 7/8	715 760 800 820	2. 2. 2. 2.

# WEIGHTS OF NUTS AND BOLT-HEADS, IN POUNDS. For Calculating the Weight of Longer Bolts.

Diameter of Bolt, in Inches.		1/4	3/8	1/2	5%	3/4	7/8
Weight of hexagon nut and head. Weight of square nut and head	::::::	.017 .021	.057 .069	.128 .164	.267 .320	.43 .55	.73 .88
Diameter of Bolt, in Inches.	1	11/4	11/2	13/4	2	21/2	3
Weight of hexagon nut and head. Weight of square nut and head	1.10 1.31	2.14 2.56	3.78 4.42	5.6 7.0	8.75 10.5	17 21	28.8 36.4

#### NUMBER OF RIVETS IN 100 POUNDS.

Lengths.	3% in.	7-16 in.	1½ in.	9-16 in.	5% in.	11-16 in.	3/4 in.	7% in.
3/4	1965	1419	1092	944	665			
7/8	1848	1335	1027	846	597			
1	1692	1222	940	763	538	450		
11/8	1512	1092	840	726	512	415		
11/4	1437	1036	797	691	487	389	356	228
13/8	1368	988	760	653	460	370	329	211
11/2	1300	949	730	624	440	357	280	180
15%	1260	924	711	596	420	340	271	174
13/4	1200	900	693	553	390	325	262	169
17/8	1156	840	648	532	375	312	257	165
2	1100	789	608	511	360	297	243	156
21/8	1031	744	573	502	354	289	237	152
21/4	999	721	555	491	347	280	232	149
21/2	945	682	525	475	335	260	220	141
23/4	900	650	500	443	312	242	208	133
3	828	598	460	411	290	224	197	127
31/4	779	562	433	379	267	212	180	115
31/2	743	536	413	352	248	201	169	108
33/4	715	513	395	341	241	192	160	102
4				326	230	184	158	99
41/4				312	220	177	150	96
41/2				298	210	171	146	94
43/4				284	200	166	138	89
5				270	190	161	135	87
51/4				256	180	156	130	84
51/2				244	172	151	124	80
53/4				233	164	145	120	77
6				223	157	140	115	74
61/4				213	150	138	111	71
61/2				207	146	134	107	69
68/4				203	143	129	104	67
7				198	140	125	100	64

#### TURNBUCKLES.

Turnbuckles with right and left threads are made of standard sizes. B =



Fig. 73.

diameter of bolt, O=6 inches in all sizes of turnbuckle. H= length of tapped heads =  $1\frac{1}{2}B$ . L= length = 6 inches + 3 B.

#### SIZES OF WASHERS.

Diameter in inches.	Size of Hole; in inches.	Thickness, Birmingham Wire-gauge.	Bolt in inches.	No. in 100 lbs.
5/6 3/4 11/6 11/6 11/6 11/6 11/6 13/4 22/6 23/4 3	5-16  36 7-16 9-16 9-16 11-16 13-16 31-32 114 114 119 119	No. 16 " 16 " 14 " 11 " 11 " 11 " 11 " 10 " 8 " 8 " 7	5-16 36 29-16 56 34 78 114 136	29,300 18,000 7,600 3,300 2,180 2,350 1,680 1,140 580 470 360 360

#### TRACK SPIKES.

Rails used.	Spikes.	Number in Keg, 200 lbs.	Kegs per Mile, Ties 24 in. between Centres.
45 to 85 40 " 52 35 " 40 24 " 35 24 " 30 18 " 24 16 " 20 14 " 16 8 " 12 8 " 10	$\begin{array}{c} 5\frac{1}{2} \times 9 - 16 \\ 5 \times 9 - 16 \\ 5 \times 9 - 16 \\ 5 \times \frac{1}{2} \times \frac{1}{2} \\ 4\frac{1}{2} \times 7 - 16 \\ 4 \times 7 - 16 \\ 3\frac{1}{2} \times \frac{3}{2} \\ 3 \times \frac{3}{2} \\ 2\frac{1}{2} \times \frac{3}{2} \times \frac{1}{2} \\ 2\frac{1}{2} \times 5 - 16 \end{array}$	380 400 490 550 725 820 1250 1350 1550 2260	30 27 22 20 15 13 9 8 7

#### STREET RAILWAY SPIKES.

Spikes.	Number in Keg, 200 lbs.	Kegs per Mile, Ties 24 in. between Centres.
5½ × 9-16	400	30
5 × ½	575	19
4½ × 7-16	800	13

# BOAT SPIKES. Number in Keg of 200 lbs.

Length.	1/4	5–16	3/8	1/2
4 inch. 5 " 6 " 7 " 8 " 9 " 10 "	2375 2050 1825	1230 1175 990 880	940 800 650 600 525 475	450 375 335 300 275

# WROUGHT SPIKES. Number of Nails in Keg of 150 Pounds.

Size.	1/4 in.	5-16 in.	3% in.	7–16 in.	½ in.
3 inches	2250 1890 1650 1464 1380 1292 1161	1208 1135 1064 930 868 662 635 573	742 570 482 455 424 391	445 384 300 270 249 236	

#### WIRE SPIKES.

Size.	Approx. Size Ap. No. in 1 lb.	Size.	Approx. Size Ap. No. of Wire Nails. in 1 lb.
10d Spike 16d " 20d " 30d " 40d " 50d "	4 " " 5 26 41/2 " " 4 20 5 " " 8 15	60d Spike 6½ in 7 8 9	6 in. No. 1 10 61½ ""1 9 7 ""0 7 8 ""00 7 9 ""00 44½

# LENGTH AND NUMBER OF CUT NAILS TO THE POUND.

Size.	Length.	Common.	Clinch.	Fence.	Finishing.	Fine.	Barrel.	Casing.	Brads.	Tobacco.	Cut Spikes.
6d	34 in. 18 114 114 114 114 12 214 22 23 34 34 34 22 23 44 44 44 44 44 44 54	800 480 288 200 168 124 88 70 58 44 23 18	95 74 62 53 46 42 38 33 20	84 64 48 36 30 24 20 16	1100 720 523 410 268 188 146 130 102 76 62 54	1000 760 368	800 500 876 224 180	398 224 128 110 91 71 54 40 33	126 98 75 65 55 40 27	130 96 82 68	28 22 141/4 121/2
40d 50d 60d	5	14 10 8						27			91/2 8 6

SIZES, LENGTH, AND NUMBER TO THE POUND OF STANDARD STEEL WIRE NAILS.

(John A. Roebling's Sons Co.)

		Sizes	20 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	tp' inches.	° ren	220 121 21 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
	Spikes,	91iW	0.0000000000000000000000000000000000000
	.3:	ijaiJ	2100 1780 1500
	,000	вооТ	4788 121 4788 128 138 138 138 138 138 138 138 138 138 13
	gle.	aidS	88.4 3.70 88.4 3.70 88.4 3.70
	ed Roofing.	Bark	44 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
	ug.	Slati	251
	Oval Car 1.	Heavy.	201 202 202 203 203 203 203 203 203 203 203
	Barbed Oval Head Car Nail.	Light. I	45488888748888277
	ring Brads.	Floo	139 99 99 90 90 90 90 90 90 90 90 90 90 90
	ng, and rooth and rbed Box,	Casi Sn Ba	281 282 281 281 281 281 281 281 281 281
	.egr	Ват	1500 1000 1000 8890 890 890 890 890
		Fine	1556 1140 760
	oth and ed Finishing.	Smo	880 980 976 977 977 977 977 977 977 977 977 977
	,96,	Еепс	200 200 200 200 200 200 200 200 200 200
	Length, inches, Common Vails and Brads, Barbed Common.		710 138 138 138 138 138 138 138 138 138 138
			876 876 876 876 877 877 877 878 878 878
			2000 2000 2000 2000 2000 2000 2000 200
			7% - 1572574 - 2572 - 2584 - 4° 19° 0
	*2	səziS	24 fine

3% lbs. of 4d Common, or 2% lbs. of 3d Common, will lay 1000 shingles. 34 lbs. of 3d Fine will put on 1000 laths—4 nails to the lath.

# APPROXIMATE NUMBER OF WIRE NAILS PER POUND.

	12	anly, v by wind dedd dedd dedd dedd dedd dedd dedd d
	=	1 bo
	10	were ither to th
	6	10 88 10 10 88 10 10 10 10 10 10 10 10 10 10 10 10 10
	∞	5 446 4 834 834 834 834 834 834 834 834 834 8
	7	25 6 7 6 8 7 7 6 8 7 111 9 111 11 9 118 118 118 118 118 125 125 125 125 125 125 125 125 125 125
	9	8 8 8 111 111 111 111 111 111 111 111 1
	10	12   10   9   8   7   6   5   445   4   394
	47%	1 10 10 10 10 10 10 10 10 10 10 10 10 10
	4	se api reserved to the true true true true true true true tru
	37.8	These and the number of the nu
es.	က	4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
inche	2,62	### ### ### ### ### ### #### #########
Length, inches.	CS	828884225282222222222222222222222222222
Leng	13%	88 88 88 88 88 88 88 88 88 88 88 88 88
	11/2	28 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
	17,	88 88 88 88 88 88 88 88 88 88 88 88 88
	-	577 657 657 667 667 670 670 670 670 670 670 670 67
	%	100 120 120 120 120 120 120 120 120 120
	2%	169 197 197 197 238 197 239 231 1136 1140 249 254 3310 4267 67 47 47 47 47 47 47 47 47 47 47 47 47 47
	7%	2211 247 247 258 258 258 258 258 258 258 258 258 258
	8%	668 887 1893 1893 2836 8048 8048 1155 10000 111850
	74	2840 8354 4571 15000 17777 22856
Wire Gange	B. W. G.	80-100400100511331757730899

# SIZE, WEIGHT, LENGTH, AND STRENGTH OF IRON WIRE.

(Trenton Iron Co.)

No. by Wire Gauge.	Diam, in Deci- mals of One	Area of Section in Decimals of	Feet to the Pound.	Weight of One Mile in pounds.	Tensile Str proximate) Iron Wire	rength (Ap- of Charcoal in Pounds.
dauge.	Inch.	One Inch.		in pounds.	Bright.	Annealed.
00000	.450	.15904	1.863	2833,248	12598	9449
0000	.400	.12566	2.358	2238.878	9955	7466
000	.360	.10179	2.911	1813.574	8124	6091
00	.330	.08553	3.465	1523.861	6880	5160
0	.305	.07306	4.057	1301.678	5926	4445
1	.285	.06379	4.645	1136.678	5226	3920
2	.265	.05515	5.374	982 555	4570	3425
3	.245	.04714	6.286	839.942	3948	2960
4	.225	.03976	7.454 8.976	708.365	3374	2530
0 1 2 3 4 5 6 7 8 9	.205 .190	.03301	10.453	588.139 505.084	2839 2476	2130 1860
0	.175	.02405	12.322	428.472	2136	1600
8	.160	.02011	14.736	358.3008	1813	1360
9	.145	.01651	17.950	294.1488	1507	1130
10	.130	.01327	22.333	236.4384	1233	925
11	.1175	.01084	27.340	193.1424	1010	758
12	.105	.00866	34.219	154.2816	810	607
13	.0925	.00672	44 092	119.7504	631	473
14	.080	.00503	58.916	89.6016	474	356
15	.070	.00385	76.984	68.5872	372	280
16 17 18	.061	.00292	101.488	52.0080	292	220
17	.0525	.00216	137.174	38.4912	222	165
18	.045	.00159	186.335	28.3378	169	127
19 20	.035	.0012566	235.084 308.079	22.3872 17.1389	137 107	103
21	.033	.0009021	392.772	13.4429	107	00
99	.028	.0006157	481.234	10.9718	. ಹಿರಡ	e é
23	.025	.0004909	603.863	8.7437	100 H . 83	more,
22 23 24	.0225	.0003976	745.710	7.0805	1, 1, 5 m e	8
25	.020	.0003142	943.396	5.5968	15° of 50°	22% 8
26	.018	.0002545	1164.689	4.5334	gengie	1 to 10 .
25 26 27 28 29 30 31 32	.017	.0002270	1305.670	4.0439	nt est	E = 2 E S = 3
28	.016	.0002011	1476.869	3.5819	ut re ger	10 a 20 a
29	.015	.0001767	1676.989	3.1485	1 1 1 2 2 2	S T S
30	.014	.0001539	1925.321	2.7424 2.3649	a Pos o	5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
31	.013	.0001327	2232.653 2620.607	2.0148	8847.	te sel
33	.012	.0000950	3119.092	1.6928	0.02 C + E	g e prest
34	.010	.0000330	3773.584	1.3992	Te was	ha, ibici
35	.0095	.00007088	4182.508	1.2624	string.	uc on E
35 36	.009	.00006362	4182.508 4657.728	1.1336	ir de	0 6488
37	.0085	,00005675	5222.035	1.0111	re alese	al al
38	.008	.00005027	5896.147	.89549	od cop o	# 65E
37 38 39	.0075	.00004418	6724.291	.78672	The above figures on tensile strength are based upon tests made with good charvoal-iron wire from Trenton blooms. Good, refined from its about 13g less,	sweats transcast then is about 10 Mild Bessemer steel is about 10 Ordinary curcible steel is about 25 Special crucible steel is from 25 pecial crucible steel is from 20 to 120 Man that of charcoal-iron wire.
40	.007	.00003848	7698,253	.68587	545	- 4

### GALVANIZED IRON WIRE FOR TELEGRAPH AND TELEPHONE LINES.

(Trenton Iron Co.)

WEIGHT PER MILE-OHM .- This term is to be understood as distinguishing the resistance of material only, and means the weight of such material required per mile to give the resistance of one ohm. To ascertain the mileage resistance of any wire, divide the "weight per mile-ohm" by the weight of the wire per mile. Thus in a grade of Extra Best Best, of which the weight reason is about the weight of the wire per mile. per mile-ohm is 5000, the mileage resistance of No. 6 (weight per mile 525) bs.) would be about 9½ olums; and No. 14 steel wire, 6500 lbs. weight per mile-ohm (95 lbs. weight per mile), would show about 69 ohms.

### Sizes of Wire used in Telegraph and Telephone Lines.

No. 4. Has not been much used until recently; is now used on important lines where the multiplex systems are applied.
No. 5. Little used in the United States.
No. 6. Used for important circuits between cities.
No. 8. Medium size for circuits of 400 miles or less.

No. 9. For similar locations to No. 8, but on somewhat shorter circuits: until lately was the size most largely used in this country. Nos. 10, 11. For shorter circuits, railway telegraphs, private lines, police

and fire-alarm lines, etc.

No. 12. For telephone lines, police and fire-alarm lines, etc.

Nos. 13, 14. For telephone lines and short private lines: steel wire is used most generally in these sizes.

The coating of telegraph wire with zinc as a protection against oxidation

The coating of chegraph whe will zinc as a processor against standing in now generally admitted to be the most efficacious method.

The grades of line wire are generally known to the trade as "Extra Best Best" (E. B. B.), "Best Best "(B. B.), and "Steel."

"Extra Best Best "is made of the very best iron, as nearly pure as any

commercial iron, soft, tough, uniform, and of very high conductivity, its weight per mile-ohm being about 5000 lbs.

The "Best Best" is of iron, showing in mechanical tests almost as good results as the E. B. B., but not quite as soft, and being somewhat lower in

conductivity; weight per mile-ohm about 5700 lbs.

The Trenton "Steel" wire is well suited for telephone or short telegraph

lines, and the weight per mile-ohm is about 6500 lbs.

The following are (approximately) the weights per mile of various sizes of galvanized telegraph wire, drawn by Trenton Iron Co.'s gauge:

8. No. 6. 7. 9, 10, 11, 13. 4. 14. 720, 610, 525, 450, 375, 310, 200, 160, 125, 250,

### TESTS OF TELEGRAPH WIRE.

The following data are taken from a table given by Mr. Prescott relating to tests of E. B. B. galvanized wire furnished the Western Union Telegraph Co.:

Size	Diam. Parts of		ght.	Length. Feet	Resist Temp. 75	.8° Fahr.	Ratio of Breaking Weight to
Wire.	One Inch.		Pounds per mile.	per pound.	Feet per ohm.	Ohms per mile.	Weight
4 5	,238	1043.2	886.6	6.00	958	5.51	
5	.220	891.3	673.0	7.85	727	7.26	!
6	. 203	758.9	572.2	9.20	618	8.54	3.05
7	.180	596.7	449.9	11.70	578	10.86	3.40
8 9	.165	501.4	378.1	14.00	409	12.92	3.07
9	.148	403.4	304.2	17.4	328	16.10	3.38
10	.134	330.7	249.4	21.2	269	19.60	3.37
11	.120	265.2	200.0	26.4	216	24.42	2.97
12	.109	218.8	165.0	32.0	179	29.60	3.43
14	.083	126.9	95.7	55.2	104	51.00	3.05
	1	1	1		1		

Joints in Telegraph Wires,—The fewer the joints in a line the better. All joints should be carefully made and well soldered over, for a bad joint may cause as much resistance to the electric current as several miles of wire.

HABLE OF DIMENSIONS, WEIGHT, AND RESISTANCE OF COPPER WIRE

	Gongo	Number.	용 용 용 용 용 용 용 용 용 용 용 용 용 용 용 용 용 용 용
WIRE.	Resistance.	Ohms per Foot.	00000000000000000000000000000000000000
OF COPPER	Resis	Ohms per Lb.	99 F18811 94 F1881 95
TANCE	gth.	Feet per Ohm.	119966. 15 111986. 15 111988. 1 111988. 1 111988. 1 11198. 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1
44	Length	Feet per Lb.	1.0007 1.00007 1.00007 1.00007 1.00007 1.00007 1.00007 1.00007 1.00007 1
(Birmingham	cht.	Lbs. per Ohm.	19366.73 19366.73 1936.94 1
DIMENSIONS, V	Weight	Lbs. per Foot.	6.02905 2.0200
	Sectional Area	= diam².	1
TABLE OF	Diameter,		44444444444444444444444444444444444444
	Gauge	Number.	888.0000000000000000000000000000000000

TARLE OF EIMENSIONS, WEIGHT, AND RESISTANCE OF PIRE COPPER

E. S. G.	Gauge Number,	6	010	0 00	100	12	18	96	35	250	39	25	22	816	39	8 5	38	5,5	25	8 2	8	92	100	110	120	130	041	001	961	071	9	006	066	076	096	086	300	350	340	360
Legal Ohms at Fahr.	Ohms per Ft.	009407600	00000000	.001311780	.000874578	000699663	0000000000	000419807	000349840	000000863	.000569400	000933997	00000014	108061000	000174931	000161465	00010140037	000130938	000131193	.000123480	.000116622	.000110477	096701000	017€60000.	.000084460	.000080730	.00000000	18880000°	000000000	000025000	000002000	0000052478	0000047707	000043733	000040368	000037484	.000034986	.000032799	.000030870	.000029155
Resistance. J	Ohms per Lb.	3850405	1386225	.0651602	.0240743	.0154178	0086664	.0055470	0038592	0098301	.0021671	0012190	0013868	.0011467	00006315	000089057	000000	00061635	.00054172	00047990	.00042807	.00038415	.00034673	.00028656	.00024070	.00020514	069/1000	00000000000000000000000000000000000000	1001000	10201000	T0101000	2998000	000002163	00000019	00002199	00004499	.00003852	.00003386	66620000	00000675
ength.	Feet per Ohm.	985 0	476.5	762.3	1143.4	1429.2	1905.7	2382.0	9859.9	3334.9	3811.0	4987.7	4763.8	5240.5	5716.5	6109.0	6669.4	7146.0	7622.3	808.4	8574.7	9021.6	9527.6	10480.6	11433.6	12386.0	1,000,0	15049.0	16107 4	17149 9	18109.1	19055.4	90961.1	0 9886	24779.1	8 222	28583.1	30488.3	32393.8	34298.7
Length.	Feet per Lb.	110.087	66.054	41.288	27.527	22,022	16.516	13.213	11.011	9.4381	8.2589	7.3407	69099	0900.9	5.5059	5 0890	4.7192	4.4044	4.1292	3.8865	3.6706	3,4773	3.3035	3.0031	2.7528	2.5411	2.0030	0.00.0	1 0489	1 8353	1.7387	1.6517	1.5016	1.3765	1.2706	1.1798	1.1012	1.0323	9716	7716.
gr. 8.889.	Lbs. per Ohm.	2.597	7.214	18.464	41.538	64.902	115.372	180.278	259,729	353,340	461.440	584.098	721.026	872.547	1038,258	1918.586	1413.264	1622, 457	1845.952	2083,759	2336 405	2603.046	2884.082	3489.958	4158.433	4874.226	6404 670	7363 049	8985 595	9344 686	10411 941	11536.681	13959.567	16612,114	19496.997	22612,233	25957.464	29533.696	33340.181	37376.652
Weight, Sp.	Lbs. per Foot.	.009084	.015139	.024220	.036328	045410	.060548	.075682	.090817	.105955	.121082	.136227	.151357	10991	181625	196772	106112	227043	.242176	.257303	.272434	.287587	.302709	.332991	.363267	126585.	154061	866787	669719	544884	.575140	.605427	.665975	726498	787058	847605	.908140	.968672	1.029214	1.089738
Diameter in	Mil = .001 in.	54.78	70.72	89.45	109.55	122.48	141.43	158.12	173.21	187.09	200.00	212,14	223.61	234.53	244.95	254.96	264.58	273.87	282 85	291.55	300.00	308.23	316 23	331.67	346.42	260.56	007.00	00.007	419.39	424.27	435.89	447.22	469.05	489.90	509.91	529.16	547.73	565.69	583.10	600.00
Maximum Amperes.	*(CNF) 2	19.5	18:3	26.0	35.2	41.6	91.19	01.9	20.0	78.6	86.8	6.46	102.7	110.3	117.7	125.0	135.1	139.1	146.0	152.8	159.5	1991	172.6	185.4	198.0	210.2	0000	9.45.6	957.0	8883	979.4	\$30.4	312.0	333.0	353.5	373.7	393.6	413.1	432.3	451.3
Circular	anns,	3000	2000	8000	12000	15000	20000	52000	30000	35000	₹0000	45000	20000	25000	00009	65000	20000	75000	80000	85000	00006	92000	100000	110000	120000	130000	150000	160000	170000	180000	190000	200000	220000	240000	260000	580000	300000	820000	340000	360000
E. S. G.	Number.	000	ıco	*	13	15	50	22	30	:8:	40	45	20	22	09	65	20	75	80	85	06	92	100	911	027	995	150	160	170	180	190	200	220	240	980	980	300	350	340	360

# DIMENSIONS, WEIGHT, AND RESISTANCE OF COPPER WIRE.

	Gange	Number.		
	Resistance,-Ohms.	Per Lb.	0.002111 0.002111 0.002112 0.002102 0.0	
	Resistan	Per Foot.	0.000,615.90 0.000,615.90 0.000,773.13 0.000	
	LengthFeet.	Per Ohm.	1893-17-7 1893-17-7	
n & Sharpe's Gauge.	Length	Per Lb.	1 - 66129 1 - 166129 2 - 167724 2 - 167	
n &	Weight.	Lbs. per Ohm.	1819.99 98 825.80 825.8	
)	Wei	Lbs. per Foot,	6.000.00.00.00.00.00.00.00.00.00.00.00.0	
DIMENSIONS,	Sect. Area	Mils.	101000 101000 101000 101000	
	Diameter	Inch.	6.66 4.66 4.66 4.66 4.66 4.66 4.66 4.66	
	Gauge	Number.	養養性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性性	

### HARD-DRAWN COPPER TELEGRAPH WIRE.

(J. A. Roebling's Sons Co.)

Furnished in half-mile coils, either hare or insulated.

Size, B. & S. Gauge.	Resistance in Ohms per Mile.	Breaking Strength.	Weight per Mile.	Approximate Size of E. B. B. Iron Wire equal to Copper.
9 10 11 12 13 14 15	4.30 5.40 6.90 8.29 10.90 13.70 17.40 22.10	625 525 420 330 270 213 170 130	209 166 131 104 83 66 52 41	Iron-wire Gauge

In handling this wire the greatest care should be observed to avoid kinks, bends, scratches, or cuts. Joints should be made only with McIntire Con-

On account of its conductivity being about five times that of Ex. B. B. Iron Wire, and its breaking strength over three times its weight per mile, copper may be used of which the section is smaller and the weight less than an equivalent iron wire, allowing a greater number of wires to be strung on the poles.

Besides this advantage, the reduction of section materially decreases the electrostatic capacity, while its non-magnetic character lessens the self-induction of the line, both of which features tend to increase the possible speed of signalling in telegraphing, and to give greater clearness of enunciation over telephone lines, especially those of great length.

### INSULATED COPPER WIRES. Weight per 1000 feet.

B. & S. Gauge.	Weather- proof Line Wire.	Under- writers' Line Wire.	B. & S. Gauge.	Weather- proof Line Wire.	Under- writers' Line Wire.	B. & S. Gauge.	Weather- proof Line Wire.	Under- writers' Line Wire.
0000 000 00 0 0 1 2 3 4	671. 537. 426. 342. 274. 220. 178. 141.	701. 565. 447. 364. 294. 241. 185.	5 6 7 8 9 10 11 12	115. 93. 77. 64. 53. 44. 37.	121. 99. 80. 67. 54. 45. 37.	13 14 15 16 17 18 19 20	26. 20.5 17. 14. 12. 10.75 9. 7.5	26.5 22. 20. 15. 13. 11.

### LEAD-ENCASED ANTI-INDUCTION TELEPHONE AND TELEGRAPH CABLES.

	Cables, Lead Encased.	For Me	TALLIC CIRCUIT.	For Telegraph Circuits.			
No. of Wires.  4 7 10 50 100	Size Wire B. & S. Gauge. 18 18 18 18 18	No. of Pairs.  5 15 25 50 75	Size Wire B. & S. Gauge.	No. of Wires.  3 4 7 10 20 50 100	Size Wire B. & S. Gauge. 14 14 14 14 14 14 14		

### FLEXIBLE CABLES.

Area Circ, Mils.	No. of Wires.	Size Wire B. & S. Gauge.	Approximate Size of Equivalent Solid Wire.	Area Circ. Mils.	No. of Wires.	Size Wire B. & S. Gauge.	Diameter of Equivalent Solid Wire, Mils.
15699.6 24963.0 39693.9 63116.9	49 49 49 49	25 23 21 19	8 B. & S. 6 " 4 " 2 "	272410.6 433154.4 688727.2 868476.7 1095135.3 210964.6 420127.2 657656.8 835827.2 1062198.9	133 133 133 133 133 103 103 129 127 128 129	17 15 13 12 11 17 15 13 12	522. 658. 830. 932. 1046. 459. 649. 811. 914. 1035.

### WEATHERPROOF AERIAL CABLES.

No. of Con- ductors.	Weight per Conductor per 1000 feet.	No, of Conductors.	Weight per Conductor per 1000 feet.	No. of Conductors.	Weight per Conductor per 1000 feet.
1 2 3 4 5 6 7	10.75 lbs. 18.00 " 13.00 " 10.75 " 10.00 " 9.50 " 9.25 "	8 9 10 11 12 13 14	9.25 lbs. 9.25 " 9.25 " 9.25 " 9.25 " 9.25 " 9.25 "	15 16 17 18 19 20	9.25 lbs. 9.25 " 9.25 " 9.25 " 9.25 " 9.25 "

### LEAD-ENCASED ELECTRIC-LIGHT CABLES.

Single Wires. (J. A. Roebling's Sons Co.)

		0. 11. 1000011	·g & 2000 CO.		
Size, B. & S. Gauge.	Diameter of Solid Cop- per Wire, Mils.	Area. Circular Mils.	Nearest Approximate Birming- ham Wire- gauge No.	Approxi- mate Weight per Foot of Cable. Oz.	Approxi- mate Diameter of Cable. Mils.
20 19 18 17 16 15 14 13 12 11 10 9 8	31.96 35.39 40.30 45.25 50.82 57.07 64.08 71.96 80.80 90.74 101.89 114.23 128.49 144.28	1021. 1252. 1624. 2048. 2583. 3257. 4107. 5178. 6530. 8234. 10381. 13094. 16509. 20816.	21 20 19 18 18 17 16 15 14 131/4 121/2 111/2 9	1.63 1.70 1.75 1.84 2.00 3.20 3.38 3.56 5.00 5.23 5.68 5.95 6.35 6.90	170 175 180 185 245 250 255 265 310 320 335 345 360 375

As tested by the Bell Telephone Co. of Philadelphia, the insulation may be stated at 2000 megohms per mile, with an electrostatic capacity of .14 microfarad.

### GALVANIZED STEEL-WIRE STRAND.

### For Smokestack Guys, Signal Strand, etc.

(J. A. Roebling's Sons Co.)

This strand is composed of 7 wires, twisted together into a single strand.

7 Wires.	Diameter.	Weight per 100 Feet.	Estimated Breaking Strength.	7 Wires.	Diameter.	Weight per 100 Feet.	Estimated Breaking Strength.
No. 8 9 10 11 12 13 14	in, 15–32 7–16 3/8 5–16 9-32 17–64	lbs. 52 42 36 29 21 16 12	lbs. 8,320 6,720 5,720 4,640 3,360 2,560 1,920	No. 15 16 17 18 19 20 21	in, 14 7-32 3-16 11-64 9-64 1/6 3-32	lbs. 10 8 6 4 3-10 3 3-10 2 4-10	1bs. 1,600 1,280 960 688 528 384 320

For special purposes these strands can be made of 50 to 100 per cent greater tensile strength. When used to run over sheaves or pulleys the use of soft-iron stock is advisable.

### FLEXIBLE STEEL-WIRE CABLES FOR VESSELS.

(Trenton Iron Co., 1886.)

With numerous disadvantages, the system of working ships' anchors with chain cables is still in vogue. A heavy chain cable contributes to the holding-power of the anchor, and the facility of increasing that resistance by paying out the cable is prized as an advantage. The requisite holding-power is obtained, however, by the combined action of a comparatively light anchor and a correspondingly great mass of chain of little service in proportion to lis weight or to the weight of the anchor. If the weight and size of the anchor were increased so as to give the greatest holding-power required, and it were attached by means of a light wire cable, the combined weight of the cable and anchor would be much less than the total weight of the chain and anchor, and the facility of handling would be much greater. English shipbuilders have taken the initiative in this direction, and many of the largest and most serviceable vessels afloat are fitted with steel-wire cables. They have given complete satisfaction.

cables. They have given complete satisfaction.

The Trenton Iron Co.'s cables are made of crucible cast-steel wire, and guaranteed to fulfil Lloyd's requirements. They are composed of 72 wires subdivided into six strands of twelve wires each. In order to obtain great flexibility, hempen centres are introduced in the strands as well as in the completed cable.

### FLEXIBLE STEEL-WIRE HAWSERS.

These hawsers are extensively used. They are made with six strands of twelve whree such, hemp centres being inserted in the individual strands swell as in the completed rope. The material employed is crucible cast steel, galvanized, and gnaranteed to fulfil Lloyd's requirements. They are only one third the weight of hempen hawsers; and are sufficiently pliable to work round any bitts to which hempen rope of equivalent strength can be applied.

only any ones of which temper rope of edutations strength can be applied to the hold of the strength of the st

# SPECIFICATIONS FOR GALVANIZED IRON WIRE. Issued by the British Postal Telegraph Authorities.

Weig	ht pe	r Mile.	Mile. Diameter.			Tests for Strength and Ductility.				ıd	Mile ird hr.		
red Standard.	Alle	owed.	d Standard.	Allo	wed.	Breaking Weight.	No. of Twists in 6 in.	king Weight not less than-	No. of Twists in 6 in.	Breaking Weight not less than-	No. of Twists in 6 in.	Resistance per Mi of the Standard Size at 60° Fahr.	t, being Standard
Required	Minimum.	Maximum.	Required	Minimum.	Maximum.	Minimum.	Minimum.	For Breaking less t	Minimum.	For Break	Minimum.	Maximum.	Constant, Weight
lbs. 800	lbs.	lbs. 833	mils.	mils.	mils.	lbs.	15	lbs.	14	lbs.	**	ohms.	- 400
600 450	571 424	629 477	242 209 181	237 204 176	247 214 186	2480 1860 1390		2550 1910 1425	14 16 18	2620 1960 1460	13 15 17	6.75 9.00 12.00	5400 5400 5400
400 200	377 190	424 218	171 121	166 118	176 125	1240 620	21 30	1270 638	20 28	1300 655	19 26	13.50 27.00	5400 5400

### STRENGTH OF PIANO-WIRE.

The average strength of English piano-wire is given as follows by Webster, Horsfals & Lean:

Numbers	Equivalents		Numbers	Equivalents	Ultimate.
in Music-	in Fractions		in Music-	in Fractions	Tensile
wire	of Inches in		wire	of inches in	Strength in
Gauge.	Diameters.		Gauge.	Diameters.	Pounds.
12 13 14 15 16 17	.029 .031 .033 .035 .037 .039	225 250 285 305 840 860	18 19 20 21 22	.041 .048 .045 .047 .052	395 425 500 540 650

These strengths range from 300,000 to 340,000 lbs. per sq. in. The composition of this wire is as follows: Carbon, 0.570; silicon, 0.090; sulphur, 0.011; phosphorus, 0.018; manganese, 0.425.

### "PLOUGH"-STEEL WIRE.

The term "plough," given in England to steel wire of high quality, was derived from the fact that such wire is used for the construction of ropes used for ploughing purposes. It is to be hoped that the term will not be used in this country, as it tends to confusion of terms. Plough-steel is known here in some steel-works as the quality of plate steel used for the mould-boards of ploughs, for which a very ordinary grade is good enough.

mould-boards of ploughs, for which a very ordinary grade is good enough.

Experiments by Dr. Percy on the English plough-steel (so-called) gave the
following results: Specific gravity, 7.814; carbon, 0.828 per cent; manganese, 0.587 per cent; silicon, 0.143 per cent; sulphur, 0.009 per cent; phosphorus, nil; copper, 0.630 per cent. No traces of chromium, titanium, or
tungsten were found. The breaking strains of the wire were as follows:

The elongation was only from 0.75 to 1.1 per cent.

### WIRES OF DIFFERENT METALS AND ALLOYS.

(J. Bucknall Smith's Treatise on Wire.)

Brass Wire is commonly composed of an alloy of 13/4 to 2 parts of copper to 1 part of zinc. The tensile strength ranges from 20 to 40 tons per square inch, increasing with the percentage of zinc in the alloy.

German or Nickel Silver, an alloy of copper, zinc, and nickel, is practically brass whitened by the addition of nickel. It has been drawn into

wire as fine as .002" diam.

Platinum wire may be drawn into the finest sizes. On account of its high price its use is practically confined to special scientific instruments and electrical appliances in which resistances to high temperature, oxygen, and acids are essential. It expands less than other metals when heated, which property permits its being sealed in glass without fear of cracking. It is therefore used in incandescent electric lamps.

**Phosphor-bronze Wir**o contains from 2 to 6 per cent of tin and from  $\frac{1}{40}$  to  $\frac{1}{40}$  per cent of phosphorus. The presence of phosphorus is detrimental to electric conductivity.

66 Delta-metal " wire is made from an alloy of copper, iron, and zinc. Its strength ranges from 45 to 62 tons per square inch. It is used for some kinds of wire rope, also for wire-gauze. It is not subject to deposits of ver-digris. It has great toughness, even when its tensile strength is over 60 tons per square inch. Aluminum Wire. - Specific gravity .268. Tensile strength only

about 10 tons per square inch. It has been drawn as fine as 11,400 yards to the ounce, or .042 grains per yard.

Aluminum Bronze, 90 copper, 10 aluminum, has high strength and ductility: is inoxidizable, sonorous. Its electric conductivity is 12.6 per cent

of that of pure copper.

Silicon Bronze, patented in 1882 by L. Weller of Paris, is made as follows: Fluosilicate of potash, pounded glass, chloride of sodium and calcium, carbonate of soda and line, are heated in a plumbago crudble, and after the reaction takes place the contents are thrown into the molten bronze to be treated. Silicon-bronze wire has a conductivity of from 40 to 98 per cent of that of copper wire and four times more than that of iron. while its tensile strength is nearly that of steel, or 28 to 55 tons per square inch of section. The conductivity decreases as the tensile strength increases. Wire whose conductivity equals 95 per cent of that of pure copper gives a tensile strength of 28 tons per square inch, but when its conductivity is 34 per cent of pure copper, its strength is 50 tons per square inch. It is being largely used for telegraph wires. It has great resistance to oxidation.

Ordinary Drawn and Annealed Copper Wire has a strength of from 15 to 20 tons per square inch.

### SPECIFICATIONS FOR HARD-DRAWN COPPER WIRE.

The British Post Office authorities require that hard-drawn copper wire supplied to them shall be of the lengths, sizes, weights, strengths, and conductivities as set forth in the annexed table.

Weig	Weight per Statute Mile.			Approximate Equiva- lent Diameter.			No. of Inches.	Resist- Mile of en hard) nr.	Veight ece (or ire.
Required Standard.	Minimum.	Maximum	Standard.	Minimum.	Maximum.	Weigl Weigl nimum sts in 3		gee E	mun mach
1bs, 100 150 200 400	lbs. 97½ 146¼ 195 390	lbs. 102½ 153¾ 205 410	mils. 79 97 112 158	mils. 78 951/9 1101/2 1551/2	mils. 80 98 1131/4 1601/4	lbs. 330 490 650 1300	30 25 20 10	ohms. 9.10 6.05 4.53 2.27	10s. 50 50 50 50

### WIRE ROPES.

List adopted by manufacturers in 1892. See pamphlets of Trenton Iron Co., John A. Roebling's Sons Co., and other makers.

### Pliable Hoisting Rope,

With 6 strands of 19 wires each.

Trade Number.	Diameter.	Circumference ir inches.	Weight per foot i pounds. Rope with Hemp Cen- tre.	Breaking Strain, tons of 2000 lbs.	Proper Working Load in tons of 2000 lbs.	Circumference of new Manila Rope of equal Strength.	Min. Size of Drun or Sheave in feet
1 2 3 4 5 5 5 5 6 7 8 9 10 10 14 10 10 4 10 10 10 10 10 10 10 10 10 10 10 10 10	214 2 134 158 114 118 114 118 114 118 176 114 118 176 176 176 176 176 176 176 176 176 176	634 6 51/2 5 434 43/8 4 31/2 23/4 21/4 2 15/6 11/4 13/8	8.00 6.30 5.25 4.10 3.65 3.00 2.50 2.00 1.58 1.20 0.88 0.60 0.44 0.35 0.29	74 65 54 44 39 33 27 20 16 11.50 8.64 5.13 4.27 3.48 3.00 2.50	15 13 11 9 8 614 552 4 3 214 134 134 142 36	14 13 12 11 10 914 819 719 616 514 334 334 319 3 3 3 2 3 4	13 12 10 81/2 71/2 7 61/4 4 4 4 4 4 23/4 21/4 2 11/6
			CAST	STEEL.			
1 2 3 4 5 5 5 6 7 8 9 10 10 10	21/4 2 13/4 15/8 11/8 11/4 11/8 1 1/8 11/4 11/8 1 1/8	63/4 6 51/2 5 43/4 43/8 4 31/8 23/4 21/4 2	8.00 6.30 5.25 4.10 3.65 3.00 2.50 2.50 1.58 1.20 0.88 0.66	155 125 106 86 77 63 52 42 33 25 18	31 25 21 17 15 12 10 8 6 5 31 21 22	15 14 13 12 11 914 814 7 534	81/2 8 71/4 61/4 53/4 51/2 4 4 31/2 31/2 21/4

### Cable-Traction Ropes.

41/2

0.35

0.29

0.26

9-16

7-16 138

 $10\frac{1}{6}$   $10\frac{3}{4}$ 

10a

107/8

According to English practice, cable-traction ropes, of about 3½ in, incircumference, are commonly constructed with six strands of seven or fitteen wires, the lays in the strands varying from, say, 3 in, to 3½ in, and the lays in the ropes from, say, 7½ in, to 9 in. In the United States, however, strands of nineteen wires are generally preferred as being more flexible; but, on the other hand, the smaller external wires wear out more rapidly. The Market street Street Railway Company, San Francisco, has used ropes 1¼ in, in diameter, composed of six strands of nineteen steel wires, weighing 2½ lbs, per foot, the longest continuous length being 24,125 ft. The Chicago City Railroad Company has employed cables of identical construction, the longest length being 27,700 ft. On the New York and Brooklyn Bridge cablerailway steel ropes of 11,500 ft, long, containing 114 wires, have been used.

### Transmission and Standing Rope.

With 6 strands of 7 wires each.

TRON.

Trade Number.	Diameter.	Circumference.	Weight per foot in pounds of Rope with Hemp Cen- tre.	Breaking Strain in tons of 2000 lbs	Proper Working Load in tons of 2000 lbs.	Circumference of new Manila Rope of equal Strength.	Min. Size of Drum or Sheave in feet.
11 12 13 14 15 16 17 18 19 20 21 22 23 24 25	11/4 13/8 11/4 11/8 1 1/8 11-16 9-16 1/2 7-16 3/8 5-16 9-32	45/8 41/4 33/4 33/8 35/8 25/8 25/8 21/8 11/8 11/4 11/8	8.37 2.77 2.28 1.89 1.50 1.12 0.88 0.70 0.57 0.41 0.31 0.23 0.19 0.16	36 30 25 20 16 12.3 8.8 7.6 5.8 4.1 2.83 2.13 1.65 1.38	9 714 614 4 3 214 2 115 115	10 9 81/5 71/2 61/4 61/4 41/2 41/2 41/2 21/4 21/4 21/4	13 12 1034 9142 8142 634 6 5144 4 234 214 214

### CAST STEEL.

15   1 16   7 17   3 18   1 19   5 20   21   1 22	454 414 44 334 45 334 46 335 46 25 6 25 6 25 6 15 6 15 6 114 6 114	3.37 2.77 2.28 1.82 1.50 1.12 0.88 0.70 0.41 0.23 0.19 0.16 0.12	62 52 44 36 30 22 17 14 11 8 6 41 3	13 10 9 71/2 6 41/5 33/2 3 21/4 13/4 11/4 11/4 11/4	13 12 11 10 9 8 7 6 51/4 43/4 43/4 23/4 23/4	81/2 8 71/4 61/4 53/4 5 4 4 31/2 21/4 21/4 11/2

### Plough-Steel Rope.

Wire ropes of very high tensile strength, which are ordinarily called "Plough-steel Ropes," are made of a high grade of crucible steel, which, when put in the form of wire, will bear a strain of from 100 to 150 tons per

when put in the form of wire, win bear a strain of from low to 150 tons per square inch.

Where it is necessary to use very long or very heavy ropes, a reduction of the dead weight of ropes becomes a matter of serious consideration.

It is advisable to reduce all bends to a minimum, and to use somewhat larger drums or sheaves than are suitable for an ordinary crucible rope having a strength of 60 to 80 tons per square inch. Before using Plough-steel Ropes it is best to have advice on the subject of adaptability.

### Plough-Steel Rope.

With 6 strands of 19 wires each.

Trade Number. Diameter inches.	weight per foot in pounds.	Breaking Strain in tons of 2000 lbs.	Proper Work- ing Load.	Min. Size of Drum or Sheave in feet.
1 234 2 2 3 134 4 156 5 136 6 134 7 136 6 114 7 136 10 10 10 10 10 10 10 10 10 10 10 10 10	8.00 6.30 5.25 4.10 3.65 3.00 2.50 2.00 1.58 1.20 0.88 0.60 0.44	240 189 157 123 110 90 75 60 47 37 27 18 13 10	46 37 25 22 22 18 15 12 9 7 5 31/2 2	9 81.59 6 51.54 41.44 33.44 33.44 33.44 33.42 32.22

With 7 Wires to the Strand.

15 1 16 7/8 17 34 18 11-16 19 5/8 20 9-16 21 1/7-16 22 7-16	1.50 1.12 0.88 0.70 0.57 0.41 0.31 0.23 0.19	45 33 25 21 16 12 9 5 4	9 6145 415 4 334 2 1145 344	51/2 5 4 31/2 3 23/4 21/2 2 11/2
--	--	---	--	--

### Galvanized Iron Wire Rope.

For Ships' Rigging and Guys for Derricks.

### CHARCOAL ROPE.

Circum- ference in inches.	Weight per Fath- om in pounds.	Cir. of new Manila Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds	Circum- ference in inches	Weight per Fathom in pounds.	Cir. of new Manila Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds
51/4 51/4 54/4 41/4 4 4 31/4 31/4 31/4 32/4	2616 2412 23 21 19 1616 1414 1234 1034 916 8 634	11 1015 10 915 9 816 8 715 615 634	43 40 35 33 30 26 23 20 16 14 12 10	214 214 2 134 114 114 115 1 78 34 58	51/2 41/2 31/2 21/2 2 13/4 11/4 7/8 3/4 12/2 3/4	5 43/4 41/2 33/4 21/2 21/2 11/4 11/4 11/4	9 8 7 5 21/2 21/4 2 1 3/4 5/8

### Galvanized Cast-steel Yacht Rigging.

Circum- ference in inches.	Weight per Fath- om in pounds.	Cir. of new Manilla Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds	Circum- ference in inches	Weight per Fathom in pounds.	Cir. of new Manilla Rope of equal Strength.	Break- ing Strain in tons of 2000 pounds
4 31/2 3 23/4 21/2 21/4	141/4 103/4 8 63/4 51/2 41/2	13 11 91/2 81/2 8	66 43 32 27 22 18	2 134 116 138 114 1	31/2 21/2 2 17/8 13/4 7/8	61/2 51/4 48/4 41/4 33/4 3	14 10 8 61/2 51/2 31/2

### Steel Hawsers.

For Mooring, Sea, and Lake Towing.

Circumfer- ence.	Breaking Strength.	Size of Manilla Haw- ser of equal Strength.	Circumfer- ence.	Breaking Strength.	Size of Manilla Haw- ser of equal Strength.
Inches. 21/6 23/4 3	Tons. 15 18 22	Inches. 61/2 7 81/2	Inches. 31/2 4	Tons. 29 35	Inches. 9 10

# Steel Flat Ropes. (J. A. Roebling's Sons Co.)

Steel-wire Flat Ropes are composed of a number of strands, alternately twisted to the right and left, laid alongside of each other, and sewed together with soft iron wires. These ropes are used at times in place of round ropes in the shafts of mines. They wind upon themselves on a narrow winding-drum, which takes up less room than one necessary for a round rope. The soft-iron sewing-wires wear out sooner than the steel strands, and then it becomes necessary to sew the rope with new liron wires.

Width and Thickness in inches.	Weight per foot in pounds.	Strength in pounds.	Width and Thickness in inches.	Weight per foot in pounds.	Strength in pounds.
36 × 2 36 × 21/2 36 × 3 36 × 31/2 36 × 4 36 × 41/2 36 × 51/2	1.19 1.86 2.00 2.50 2.86 3.12 3.40 3.90	85,700 55,800 60,000 75,000 85,800 93,600 100,000 110,000	14 × 3 14 × 314 14 × 4 14 × 414 14 × 5 14 × 5 14 × 6 14 × 7	2.38 2.97 3.30 4.00 4.27 4.82 5.10 5.90	71,400 89,000 99,000 120,000 128,000 144,600 153,000 177,000

For safe working load allow from one fifth to one seventh of the breaking stress.

### "Lang Lay" Rope.

In wire rope, as ordinarily made, the component strands are laid up into rope in a direction opposite to that in which the wires are laid into strands; that is, if the wires in the strands are laid from right to left, the strands are laid into rope from left to right. In the "Lang Lay," sometimes known as "Universal Lay," the wires are laid into strands and the strands into rope in the same direction; that is, if the wire is laid in the strands from right to left, the strands are also laid into rope from right to left. Its use has been found desirable under certain conditions and for certain purposes, mostly for haulage plants, inclined planes, and street railway cables, although it has also been used for vertical hoists in mines, etc. Its advantages are that

### GALVANIZED STEEL CABLES.

For Suspension Bridges, (Roebling's.)

			•						
Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot.	Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot.	Diameter in inches.	Ultimate Strength in tons of 2000 pounds.	Weight per foot.	
25/8 21/4 23/8	220 200 180	13 11.3 10	21/4 2 17/8	155 110 100	8.64 6.5 5.8	134 156 1½	95 75 65	5.6 4 35 3.7	

### COMPARATIVE STRENGTHS OF FLEXIBLE GAL-VANIZED STEEL-WIRE HAWSERS,

### With Chain Cable, Tarred Russian Hemp, and White Manila Ropes. (Trenton Iron Co.)

Transa Ropes, (Tenton from Co.)												
Patent Flexible Steel-wire Hawsers and Cables.			Chain Cable.				Tarred Rus- sian Hemp Rope.			IV:	White Manilla Ropes.	
	Weight per Fathom. Guaranteed Breaking Strain.	Diameter of Barrel or Sheave round which it may be worked.	Size.	Weight per Fathom.	Proof Strain.	Breaking Strain.	Size.	Weight per Fathom.	Breaking Strain.	Size.	Weight per Fathom.	Breaking Strain.
2 21/4 21/6 23/4 31/4 31/4 41/6 11	5   39 31/2   64 8   74 3   88 7   102 1   116 7   130	6 71/2 9 101/2 131/2 15 161/2 18 191/2 24 27 30 33 36 39 42 45 48	9-16 10-16 11-16 12-16 13-16 15-16 1 1/4 1 17-32 156 1 17-32 156 2 1-16 2 3-16 2 5-16	54 68 112 143 166 204 231 256	761% 861%	6 714 915 1234 1316 17 8-10 23 7-10 23 7-10 3416 6616 7714 6616 7714 107 1-10 12016 13434	23/4 31/2 4 5 53/4 61/2 71/2 81/2 9 10 11 12 13 15 17 19 21 23 24 25	3 31/6 8 10 13 16 19 23 28 33 39 56 67 84 106 123 134 146	11/5 21/5 81/4 5 7 9 11/5 14 61/6 20 24/5 29 34 50 60 72 89 106 115 125	21/2 3 31/4 4 5 53/4 61/4 7 71/6 9 10 11 123/4 131/2 15	11/4 13/4 2 3 41/6 6 7 83/4 101/2 13 141/2 122 291/4 42	2 234 314 5 734 1016 1214 15 18 2234 25 3116 3816 62 7316

it is somewhat more flexible than rope of the same diameter and composed of the same number of wires laid up in the ordinary manner; and (especially) that owing to the fact that the wires are laid more axially in the rope, longer surfaces of the wire are exposed to wear, and the endurance of the rope is thereby increased. (Trenton Iron Co.)

### Notes on the Use of Wire Rope.

(J. A. Roebling's Sons Co.)

Two kinds of wire rope are manufactured. The most pliable variety contains nineteen wires in the strand, and is generally used for hoisting and running rope. The ropes with twelve wires and seven wires in the strand are stiffer, and are better adapted for standing rope, guys, and rigging. Orders should state the use of the rope, and advice will be given. Ropes are

made up to three inches in diameter, upon application. For safe working load, allow one fifth to one seventh of the ultimate strength, according to speed, so as to get good wear from the rope. When substituting wire rope for hemp rope, it is good economy to allow for the former the same weight per foot which experience has approved for the

Wire rope is as pliable as new hemp rope of the same strength; the former will therefore run over the same-sized sheaves and pulleys as the latter. But the greater the diameter of the sheaves, pulleys, or drums, the longer wire rope will last. The minimum size of drum is given in the table.

Experience has demonstrated that the wear increases with the speed. It

is, therefore, better to increase the load than the speed.

Wire rope is manufactured either with a wire or a hemp centre. The latter is more pliable than the former, and will wear better where there is short bending. Orders should specify what kind of centre is wanted.

Wire rope must not be coiled or uncoiled like hemp rope. When mounted on a reel, the latter should be mounted on a spindle or flat turn-table to pay off the rope. When forwarded in a small coil, without reel, roll it over the ground like a wheel, and run off the rope in that way. All untwisting or kinking must be avoided.

To preserve wire rope, apply raw linseed-oil with a piece of sheepskin, wool inside; or mix the oil with equal parts of Spanish brown or lamp-black. To preserve wire rope under water or under ground, take mineral or vegetable tar, and add one bushel of fresh-slacked lime to one barrel of tar,

which will neutralize the acid. Boil it well, and saturate the rope with the To give the mixture body, add some sawdust

In no case should galvanized rope be used for running rope. One day's use scrapes off the coating of zinc, and rusting proceeds with twice the

rapidity.

The grooves of cast-iron pulleys and sheaves should be filled with well-seasoned blocks of hard wood, set on end, to be renewed when worn out. This end-wood will save wear and increase adhesion. The smaller pulleys or rollers which support the ropes on inclined planes should be constructed on the same plan. When large sheaves run with very great velocity, the on the same plan. When large sheaves the wall very shear plan. When large sheaves the distribution of power between is done in the case of sheaves used in the transmission of power between distant points by means of rope, which frequently runs at the rate of 4000 feet per minute.

Steel ropes are taking the place of iron ropes, where it is a special object

to combine lightness with strength.

But in substituting a steel rope for an iron running rope, the object in view should be to gain an increased wear from the rope rather than to reduce the size.

Locked Wire Rope.

Fig. 74 shows what is known as the Patent Locked Wire Rope, made by the Trenton Iron Co. It is claimed to wear two to three times as long as an



Fig. 74.

ordinary wire rope of equal diameter and of like material. Sizes made are from 1/2 to 11/2 inches diameter.

# CRANE CHAINS.

(Pencovd Iron Works.)

	"	Crane.							
Size of Chain, inches.	Pitch Approximate- ly, inches	Weight per Foot in pounds, approximately.	Outside Width, inches.	Proof Test, pounds.	Average Breakage Strain, pounds.	Ordinary Safe Load, General Use, pounds.	Proof Test, pounds.	Average Breaking Strain, pounds.	Ordinary Safe Load, General Use, pounds.
7-16 1 19-16 1 5-8 1 11-16 1 12-16 2 7-8 2 15-16 2 1 1-16 2 1 1-16 2 1 1-16 2 1 1-16 2 1 1-16 3 1 1-16 3	25-82 27-32 31-32 5-32 15-32 15-32 27-32 31-32 7-32 15-32 15-32 15-32 7-32 7-32 7-32 7-32 7-32 7-32 7-32 7	76 1 7-10 2 214 3 2-10 44,6 5 57,6 6 7-10 8 9 10 7-10 11 2-10 12,4 13 7-10 16 18 4-10 18 4-10 19 7-10 21 7-10	7/8 1 1-16 11/4 11/8 1 11-16 17/8 2 1-16 21/4 2 11-16 27/4 2 11-16 31/4 3 5-16 33/4 43/5 49/8 49/8 49/8 49/8 49/8 49/8 49/8 49/8	1932 2898 4186 5796 7728 266 11914 14490 17388 20286 22484 24584 29568 3364 46200 50512 55748 60368 66528	3864 5796 8372 11592 15456 19320 23888 28980 34776 40572 44968 51744 59126 66538 8776 92400 101024 111496 120736 133055	1288 1932 2790 3864 5182 6440 7942 9660 11592 13524 14989 17248 19712 22176 25050 27925 30800 38674 40245 44352	1680 2520 3640 5040 6720 8400 10360 15120 17640 20520 26880 30240 34160 45920 50680 54880 60480	3360 5040 7280 10080 13440 16800 20720 25200 30240 35280 40880 47040 53760 68320 76160 84000 91840 101360 109760	1120 1680 2427 3360 4480 5600 6907 8400 10780 117680 17920 20160 22773 25387 28000 30613 33787 36587 40320

The distance from centre of one link to centre of next is equal to the inside length of link, but in practice 1/32 inch is allowed for weld. This is approximate, and where exactness is required, chain should be made so.

FOR CHAIN SHEAVES.—The diameter, if possible, should be not less than twenty times the diameter of chain used.

Example. - For 1-inch chain use 20-inch sheaves.

### WEIGHTS OF LOGS, LUMBER, ETC.

The state of the s		
Weight of Green Logs to Scale 1,000 Feet, Board Mea	sur	e.
Yellow pine (Southern)		
Norway pine (Michigan)		
White pine (Michigan) off of stump. 6,000 to 7,000 to 8,000 to 7,000 to 8,000 to 7,000 to 8,000 to 8,0	900 °	
white pine (menigan) out of water 7,000 to 8,0		
White pine (Pennsylvania), bark off 5,000 to 6,0	900 '	14
Hemlock (Pennsylvania), bark off 6,000 to 7,0	000 °	
Francisco of water are required to store 1 000 000 feet of loge		

Weight of 1,000 Feet of Lumber, Board Measure. Yellow or Norway pine . . . . . . Dry, 3,000 lbs. Green, 5,000 lbs. White pine.... 2,500 " 4,000 "

# Weight of 1 Cord of Seasoned Wood, 128 Cubic Feet per Cord.

Hickory or sugar maple	 4.500 11	bs
White oak		
Beech, red oak or black oak		
Poplar, chestnut or elm		
ropiar, chestilut of eth	 2,000	
Pine (white or Norway)	 2,000	
Hamlook bank day	9 900 (	

### SIZES OF FIRE-BRICK.

	9-inch straight 9 × 4½ × 2½ inches.
	Soap 9 × 216 × 216 "
/ Jamb	Checker 9×3 ×3 "
/	2-inch
9×4½×2½	Split 9×41/3×11/4 "
V 1/2 ~ ~/2	
	No. 1 key
1	wide.
/ Key	118 bricks to circle 12 feet inside diam.
	No. 2 key
9 x 21/2× (41/2·21/4)	inches wide. 63 bricks to circle 6 ft. inside diam.
V87472	No. 3 key
	inches wide.
	38 bricks to circle 3 ft. inside diam.
( ) , , , , ,	No. 4 key 9 × 2½ thick × 4½ to 2½
Wedge ,	inches wide,
(0×416: (01: 116)	25 bricks to circle 11/2 ft. inside diam.
9×4½× (2½:1½)	No. 1 wedge (or bullhead). 9×41/2 wide × 21/2 to 2 in.
	thick, tapering lengthwise.
_	98 bricks to circle 5 ft. inside diam.
/ Arch	No. 2 wedge $9 \times 4\frac{1}{2} \times 2\frac{1}{2}$ to $1\frac{1}{2}$ in. thick.
	60 bricks to circle 21/2 ft. inside diam.
9×4½×(2½·1½)	No. 1 arch 9×4½×2½ to 2 in. thick
V/	tapering breadthwise. 72 bricks to circle 4 ft, inside diam,
-	No. 2 arch 9 × 4½ × 2½ to 1½.
	42 bricks to circle 2 ft. inside diam.
No. 1 Skew	No. 1 skew 9 to 7 × 41/2 to 21/2.
(	Bevel on one end.
	No. 2 skew 9 × 21/6 × 41/6 to 21/6.
(9:7)×4½×2½/	Equal bevel on both edges.
	No. 3 skew $9 \times 2\frac{1}{2} \times 4\frac{1}{2}$ to $1\frac{1}{2}$ .  Taper on one edge.
	Taper on one edge.
No.2 Skew	24 inch circle
No.2 BREW	Edges curved, 9 bricks line a 24-inch circle.
	36-inch circle
9×2½×(4½·2½)	48-inch circle
V	17 bricks line a 48-inch circle.
	13½-inch straight 13½×2½×6.
	13½-inch key No. 1 13½ × 2½ × 6 to 5 inch.
No.3 Skew	90 bricks turn a 12-ft, circle.
1210.0 020	13½-inch key No. 213½×2½×6 to 4¾ inch. 52 bricks turn a 6-ft. circle.
/0×2½×(4½:1½)	52 bricks turn a 6-ft. circle,
V /2 - ( - /2 - /2 )	Bridge wall, No. 1
	Bridge wall, No. 213×6½×3.
36 in. Circle	Mill tile
834	Stock-hole tiles
多 6%	18-inch block
3 072	Flat back arch 9 × 6 × 3½ to 2½.
	22-inch radius, 56 bricks to circle.
	Locomotive tile32 × 10 × 3.
	34 × 10 × 3.
Cupola	34 × 8 × 3.
	36× 8×3.
	40×10×3.
	Tiles, slabs, and blocks, various sizes 12 to 30 inches

long, 8 to 30 inches wide, 2 to 6 inches thick. Cupola brick, 4 and 6 inches high, 4 and 6 inches radial width, to line shells

Cuplon orices, a fact orients figure 1.23 to 66 in diameter.
A 9-inch straight brick weighs 7 lbs, and contains 100 cubic inches. (=120 lbs, per cubic foot. Specific gravity 1.93.)
One cubic foot of wall requires 17 9-inch bricks, one cubic yard requires 460. Where keys, wedges, and other "shapes" are used, add 10 per cent in estimating the number required.

100.760

100,450

One ton of fire-clay should be sufficient to lay 3000 ordinary bricks. To secure the best results, fire-bricks should be laid in the same clay from which they are manufactured. It should be used as a thin paste, and not as mortar. The thinner the joint the better the furnace wall. In ordering bricks the service for which they are required should be stated.

### NUMBER OF FIRE-BRICK REQUIRED FOR VARIOUS CIRCLES.

i e		KEY BRICKS.					ARCH BRICKS.			WEDGE BRICKS.			
Diam.	No. 4.	No. 3.	No. 2.	No. 1.	Total.	No. 2.	No. 1.	9,,	Total.	No. 2.	No. 1.	9,,	Total.
ft. in 1 6 2 0 3 6 3 0 4 6 5 0 6 6 0 6 6 0 7 6 8 0 9 6 10 0 11 6 12 0 11 6	25 17 9	13 25 38 32 25 19 13 6	10 21 32 42 53 63 58 58 47 42 37 31 16 11	9 19 29 38 47 57 66 85 94 104 113 113	25 30 34 38 42 46 51 55 63 67 71 76 80 92 97 101 105 113 117	42 31 21 10	18 36 54 72 72 72 72 72 72 72 72 72 72 72 72 72	8 15 23 30 38 45 53 60 68 75 83 90 98 105 113 121	42 49 57 64 72 80 87 95 102 110 117 125 132 140 147 155 162 170 177 185 193	60 48 36 24 12	20 40 59 98 98 98 98 98 98 98 98 98 98 98 98	8 15 23 30 38 46 53 61 68 87 76 83 91 98 106	60 68 76 83 91 98 103 121 128 136 144 151 159 166 174 189 196 204

For larger circles than 12 feet use 113 No. 1 Key, and as many 9-inch brick as may be needed in addition.

AN	ALYSES	OF MT.	SAVAGE	FIRE-CLA	W.
(1)	(2)			(3)	(4)
1871	1877.			1878.	1885.
Mass, Institute of Technology	Report of Clays of New Jers Prof. G. H.	f		Second Geological Survey of Pennsylvania.	(2 samples) Dr. Otto Wuth.
50.457	56.80	Silica		. 44.395	56.15
35.904	30.08	Alumina.		. 33.558	33.295
	1.15	Titanic ac	id	. 1.530	
1.504	1.12	Peroxide :	iron :	. 1.080	0.59
0.133		Lime		. trace	0.17
0.018					0.115
trace	0.80	Potash (al	kalies)	. 0.247	
12.744	10.50	Water and	l inorg. matter	r. 14.575	9.68

100:493

100,000

### MAGNESTA BRICKS.

"Foreign Abstracts" of the Institution of Civil Engineers, 1893, gives a paper by C. Bischof on the production of magnesia bricks. The material most in favor at present is the magnesite of Styria, which, although less pure considered as a source of magnesia than the Greek, has the property of fritting at a high temperature without melting. The composition of the two substances, in the natural and burnt states, is as follows:

Magnesite.	Styrian.	Greek.
Carbonate of magnesia	90.0 to 96.0%	94.46%
" " lime		4.49 FeO 0.08
Silica		0.52
Manganous oxide	0,5	Water 0.54
Burnt Magnesite.		
Magnesia	77.6	82.46-95.36
Lime		0.83 - 10.92
Alumina and ferric oxide	13.0	0.56 - 3.54
Silica	1.2	0.73 7.98

At a red heat magnesium carbonate is decomposed into carbonic acid and caustic magnesia, which resembles lime in becoming hydrated and recarbonated when exposed to the air, and possesses a certain plasticity, so that it can be moulded when subjected to a heavy pressure. By long-continued it can be moulded when subjected to a heavy pressure. By long-continued or stronger heating the material becomes dead-burnt, giving a form of magnesia of high density, sp. gr. 3.8, as compared with 3.0 in the plastic form, which is unatterable in the air but devoid of plasticity. A mixture of two volumes of dead-burnt with one of plastic magnesia can be moulded into bricks which contract but little in firing. Other binding materials that have been used are: clay up to 10 or 15 per cent; gas-tar, perfectly freed from water, soda, silica, vinegar as a solution of magnesium acetate which is readily decomposed by heat, and carbolates of alkalies or lime. Among magnesium compounds a weak solution of magnesium chloride may also be used. For setting the bricks lightly burnt, caustic magnesia, with a small proportion of silica to reuder it less refractory, is recommended. The strength of the bricks may be increased by adding iron, either as oxide or silicate. If a porous product is required, sawdust or starch may be added to the mixture. When dead-burnt magnesia is used alone, soda is said to be the best binding material.

the best binding material.

See also papers by A. E. Hunt, Trans. A. I. M. E., xvi, 720, and by T. Egleston, Trans. A. I. M. E., xiv, 458.

Asbestos.—J. T. Donald, Eng. and M. Jour., June 27, 1891.

### ANALYSIS.

		Canadian.			
	Italian.	Broughton.	Templeton.		
Silica		40.57%	40.52%		
Magnesia	. 43.37	41.50	42.05		
Ferrous oxide	87	2.81	1.97		
Alumina	. 2.27	.90	2.10		
Water	. 13.72	13.55	13.46		
	100.53	99.33	100.10		

Chemical analysis throws light upon an important point in connection with asbestos, i.e., the cause of the harshness of the fibre of some varieties, Asbestos is principally a hydrous silicate of magnesia, i.e., silicate of magnesia combined with water. When harsh fibre is analyzed it is found to contain less water than the soft fibre. In fibre of very fine quality from Black Lake analysis showed 14.38% of water, while a harsh-fibred sample gave only 11.70%. If soft fibre be heated to a temperature that will drive off a portion of the combined water, there results a substance so brittle that it may be crumbled between thumb and finger. There is evidently some connection between the consistency of the fibre and the amount of water in its composition,

### STRENGTH OF MATERIALS.

Stress and Strain.-There is much confusion among writers on strength of materials as to the definition of these terms. An external force applied to a body, so as to pull it apart, is resisted by an internal force, or resistance, and the action of these forces causes a displacement of the molecules, or deformation. By some writers the external force is called a stress, and the internal force a strain; others call the external force a strain, and the internal force a stress: this confusion of terms is not of importance, as the words stress and strain are quite commonly used synonymously, but the use of the word strain to mean molecular displacement, deformation, or distortion, as is the custom of some, is a corruption of the language. See Engineering News, June 23, 1892. Definitions by leading authorities are given

Stress.-A stress is a force which acts in the interior of a body, and resists the external forces which tend to change its shape. A deformation is the amount of change of shape of a body caused by the stress. The word strain is often used as synonymous with stress and sometimes it is also used to designate the deformation. (Merriman.)

The force by which the molecules of a body resist a strain at any point is

called the stress at that point.

The summation of the displacements of the molecules of a body for a given point is called the distortion or strain at the point considered. (Burr). Stresses are the forces which are applied to bodies to bring into action their elastic and cohesive properties. These forces cause alterations of the forms of the bodies upon which they act. Strain is a name given to the kind of alteration produced by the stresses. The distinction between stress

and strain is not always observed, one being used for the other. (Wood.)

Stresses are of different kinds, viz.: tensile, compressive, transverse, torsional, and shearing stresses.

A tensile stress, or pull, is a force tending to elongate a piece. A compressive stress, or push, is a force tending to shorten it. A transverse stress tends to bend it. A torsional stress tends to twist it. A shearing stress tends to force one part of it to slide over the adjacent part.

Tensile, compressive, and shearing stresses are called simple stresses. Transverse stress is compounded of tensile and compressive stresses, and

torsional of tensile and shearing stresses

To these five varieties of stresses might be added tearing stress, which is either tensile or shearing, but in which the resistance of different portions of the material are brought into play in detail, or one after the other, instead of simultaneously, as in the simple stresses, Effects of Stresses.—The following general laws for cases of simple

tension or compression have been established by experiment. (Merriman): 1. When a small stress is applied to a body, a small deformation is produced, and on the removal of the stress the body springs back to its original form. For small stresses, then, materials may be regarded as perfectly

elastic.

2. Under small stresses the deformations are approximately proportional to the forces or stresses which produce them, and also approximately pro-

portional to the length of the bar or body

3. When the stress is great enough a deformation is produced which is partly permanent, that is, the body does not spring back entirely to its original form on removal of the stress. This permanent part is termed a set. In such cases the deformations are not proportional.

4. When the stress is greater still the deformation rapidly increases and

5. A sudden stress, or shock, is more injurious than a steady stress or than a stress gradually applied.

Elastic Limit. The elastic limit is defined as that point at which the deformations cease to be proportional to the stresses, or, the point at which the rate of stretch (or other deformation) begins to increase. It is also defined as the point at which the first permanent set becomes visible. last definition is not considered as good as the first, as it is found that with some materials a set occurs with any load, no matter how small, and that with others a set which might be called permanent vanishes with lapse of time, and as it is impossible to get the point of first set without removing the whole load after each increase of load, which is frequently inconvenient. The elastic limit, defined, however, as the point at which the extensions begin to increase at a higher ratio than the applied stresses, usually corresponds

very nearly with the point of first measurable permanent set.

Yield-point.—The term yield-point has recently been introduced into the literature of the strength of materials. It is defined as that point at which the rate of stretch suddenly increases rapidly. The difference between the elastic limit, strictly defined as the point at which the rate of stretch begins to increase, and the yield-point, at which the rate increases suddenly, may in some cases be considerable. This difference, however, will not be discovered in short test-pieces unless the readings of elongations are

made by an exceedingly fine instrument, as a micrometer reading to  $\frac{1}{10000}$ 

of an inch. In using a coarser instrument, such as calipers reading to 1/100 of an inch, the elastic limit and the yield-point will appear to be simultaneous. Unfortunately for precision of language, the term yield-point was not introduced until long after the term elastic limit had been almost universally adopted to signify the same physical fact which is now defined by the term yield-point, that is, not the point at which the first change in rate observable only by a microscope, occurs, but that later point (more or less observable only by a microscope, occurs, but that later point (more or less indefinite as to its precise position) at which the increase is great enough to be seen by the naked eye. A most convenient method of determining the point at which a sudden increase of rate of stretch occurs in short specimens, when a testing-machine in which the pulling is done by screws used, is to note the weight on the beam at the instant that the beam "drops." During the earlier portion of the test, as the extension is steadily increased by the uniform but slow rotation of the series, the police is moved steadily along the beam to keep it in equipoise; suddenly a point is reached at which the beam drops, and will not rise until the elongation has been considerably increased by the further rotation of the screws, the advancing of the poise meanwhile being suspended. This point corresponds practically to the point meanwhite being suspended. This point corresponds practically to the point at which the rate of elongation suddenly increases, and to the point at which an appreciable permanent set is first found. It is also the point which has hitherto been called in practice and in text-books the elastic limit, and it will probably continue to be so called, although the use of the newer term "yield-point" for it, and the restriction of the term elastic limit to mean the earlier point at which the rate of stretch begins to increase, as determined by the property in the property in the property in the property is the property of the property in the property is the property of the property in the property is the property of the property in the property is the property of the property in the property is the property of the property in the property is the property of the property in the property is the property of the property in the property of the property is the property of t

able only by micrometric measurements, is more precise and scientific.

In tables of strength of materials hereafter given, the term elastic limit is used in its customary meaning, the point at which the rate of stress has begun to increase, as observable by ordinary instruments or by the drop of the beam. With this definition it is practically synonymous with yield-

point. Coefficient (or Modulus) of Elasticity. - This is a term expressing the relation between the amount of extension or compression of a mate-

rial and the load producing that extension or compression.

It may be defined as the load per unit of section divided by the extension per unit of length; or the reciprocal of the fraction expressing the elongation per inch of length, divided by the pounds per square inch of section producing that elongation.

Let P be the applied load, k the sectional area of the piece, l the length of the part extended,  $\lambda$  the amount of the extension, and E the coefficient of elasticity. Then

 $\frac{P}{L}$  = the load on a unit of section;  $\frac{\lambda}{\tau}$  = the elongation of a unit of length.

$$E = \frac{P}{k} \div \frac{\lambda}{l} = \frac{Pl}{k\lambda}.$$

The coefficient of elasticity is sometimes defined as the figure expressing the load which would be necessary to elongate a piece of one square inch section to double its original length, provided the piece would not break, and the ratio of extension to the force producing it remained constant. This definition follows from the formula above given, thus: If k =one square lnch, l and k each =one inch, then E = P.

Within the elastic limit, when the deformations are proportional to the

stresses, the coefficient of elasticity is constant, but beyond the elastic limit

it decreases rapidly

In cast iron there is generally no apparent limit of elasticity, the deformations increasing at a faster rate than the stresses, and a permanent set being produced by small loads. The coefficient of elasticity therefore is not constant during any portion of a test, but grows smaller as the load increases. The same is true in the case of timber. In wrought iron and steel, however, there is a well-defined elastic limit, and the coefficient of elasticity within that limit is nearly constant

Resilience, or Work of Resistance of a Material,-Within the elastic limit, the resistance increasing uniformly from zero stress to the stress at the elastic limit, the work done by a load applied gradually is equal to one half the product of the final stress by the extension or other deformation. Beyond the elastic limit, the extensions increasing more rapidly than the loads, and the strain diagram approximating a parabolic form, the work is approximately equal to two thirds the product of the maximum stress by the extension.

The amount of work required to break a bar, measured usually in inchpounds, is called its resilience; the work required to strain it to the elastic

limit is called its elastic resilience.

Under a load applied suddenly the momentary elastic distortion is equal to twice that caused by the same load applied gradually.

When a solid material is exposed to percussive stress, as when a weight falls upon a beam transversely, the work of resistance is measured by the product of the weight into the total fall.

Filevation of Ultimate Resistance and Elastic Limit,—It was first observed by Prof. R. H. Thurston, and Commander L. A. Beards-lee, U. S. N., independently, in 1873, that if wrought iron be subjected to a stress beyond its elastic limit, but not beyond its ultimate resistance, and then allowed to "rest" for a definite interval of time, a considerable increase of elastic limit and ultimate resistance may be experienced. In other words, the application of stress and subsequent "rest" increases the resistance of wrought iron.

This "rest" may be an entire release from stress or a simple holding the

test-piece at a given intensity of stress.

Commander Beardslee prepared twelve specimens and subjected them to an intensity of stress equal to the ultimate resistance of the material, with-out breaking the specimens. These were then allowed to rest, entirely free from stress, from 24 to 30 hours, after which period they were again stressed until broken. The gain in ultimate resistance by the rest was found to vary from 4.4 to 17 per cent.

This elevation of elastic and ultimate resistance appears to be peculiar to

iron and steel: it has not been found in other metals.

Relation of the Elastic Limit to Endurance under Repeated Stresses (condensed from Engineering, August 7, 1891).— When engineers first began to test materials, it was soon recognized that if a specimen was loaded beyond a certain point it did not recover its original dimensions on removing the load, but took a permanent set; this point was called the elastic limit. Since below this point a bar appeared to recover completely its original form and dimensions on removing the load, it appeared obvious that it had not been injured by the load, and hence the working load might be deduced from the elastic limit by using a small factor of safety.

Experience showed, however, that in many cases a bar would not carry safely a stress anywhere near the elastic limit of the material as determined by these experiments, and the whole theory of any connection between the elastic limit of a bar and its working load became almost discredited, and engineers employed the ultimate strength only in deducing the safe working load to which their structures might be subjected. Still, as experience accumulated it was observed that a higher factor of safety was required for a live

load than for a dead one.

In 1871 Wöhler published the results of a number of experiments on bars of iron and steel subjected to live loads. In these experiments the stresses were put on and removed from the specimens without impact, but it was, nevertheless, found that the breaking stress of the materials was in every case much below the statical breaking load. Thus, a bar of Krupp's axle steel having a tenacity of 49 tons per square inch broke with a stress of 28.6 tons per square inch, when the load was completely removed and replaced without impact 170,000 times. These experiments were made on a large number of different brands of iron and steel, and the results were concordant in showing that a bar would break with an alternating stress of only, say, one third the statical breaking strength of the material, if the repetitions of stress were sufficiently numerous. At the same time, however, it appeared from the generaltrend of the experiments that a bar would stand an indefinite number of alternations of stress, provided the stress was kept below the limit.

Prof. Bauschinger defines the elastic limit as the point at which stress ceases to be sensibly proportional to strain, the latter being measured with

a mirror apparatus reading to  $\frac{1}{5000}$ th of a millimetre, or about  $\frac{1}{100000}$  in.

This limit is always below the yield-point, and may on occasion be zero. On loading a bar above the yield-point, this point rises with the stress, and the rise continues for weeks, months, and possibly for years if the bar is left at rest under its load. On the other hand, when a bar is loaded beyond its true elastic limit, but below its yield-point, this limit rises, but reaches a maximum as the yield-point, is approached, and then falls rapidly, reaching even to zero. On leaving the bar at rest under a stress exceeding that of its primitive breaking-down point the elastic limit begins to rise again, and may, if left a sufficient time, rise to a point much exceeding its previous value.

This property of the elastic limit of changing with the history of a bar has done more to discredit it than anything else, nevertheless it now seems as if it, owing to this very property, were once more to take its former place in the estimation of engineers, and this time with fixity of tenure. It had long been known that the limit of elasticity might be raised, as we have said, to almost any point within the breaking load of a bar. Thus, in some experiments by Professor Styfe, the elastic limit of a puddled-steel bar was raised 16,000 lbs. by subjecting the bar to a load exceeding its primitive elastic limit.

A bar has two limits of elasticity, one for tension and one for compression. Bauschinger loaded a number of bars in tension until stress ceased to be sensibly proportional to strain. The load was then removed and the bar tested in compression until the elastic limit in this direction had been exceeded. This process raises the elastic limit in compression, as would be found on testing the bar in compression a second time. In place of this, however, it was now again tested in tension, when it was found that the artificial raising of the limit in compression had lowered that in tension below its previous value. By repeating the process of alternately testing in tension and compression, the two limits took up points at equal distances from the line of no load, both in tension and compression. These limits Bauschinger calls natural elastic limits of the bar, which for wrought from correspond to a stress of about 8½ tons per square inch, but this is practically the limiting load to which a bar of the same material can be strained alternately in tension and compression, without breaking when the loading is repeated sufficiently often, as determined by Wöhler's method.

As received from the rolls the elastic limit of the bar in tension is above the natural elastic limit of the bar as defined by Bauschinger, having been artificially raised by the deformations to which it has been subjected in the process of manufacture. Hence, when subjected to alternating stresses, the limit in tension is immediately lowered, while that in compression is raised until they both correspond to equal loads. Hence, in Wöhler's experiments, in which the bars broke at loads nominally below the elastic limits of the material, there is every reason for concluding that the loads were really greater than true elastic limits of the material. This is confirmed by tests on the connecting-rods of engines, which of course work under alternating stresses of equal intensity. Careful experiments on old rods show that the elastic limit in compression is the same as that in tension, and that both are far below the tension elastic limit of the material as

received from the rolls.

The common opinion that straining a metal beyond its elastic limit injures it appears to be untrue. It is not the mere straining of a metal beyond one elastic limit that injures it, but the straining, many times repeated, beyond its two elastic limits. Sir Benjamin Baker has shown that in bending a shell plate for a boiler the metal is of necessity strained beyond its elastic limit, so that stresses of as much as 7 tons to 15 tons per square inch may obtain it as it comes from the rolls, and unless the plate is annealed, these stresses will still exist after it has been built into the boiler. In such a case, however, when exposed to the additional stress due to the pressure inside

the boiler, the overstrained portions of the plate will relieve themselves by stretching and taking a permanent set, so that probably after a year's working very little difference could be detected in the stresses in a plate built into the boiler as it came from the bending rolls, and in one which had been annealed, before riveting into place, and the first, in spite of its having been strained beyond its elastic limits, and not subsequently annealed, would be as strong as the other.

### Resistance of Metals to Repeated Shocks.

More than twelve years were spent by Wöhler at the instance of the Prussian Government in experimenting upon the resistance of iron and steel to repeated stresses. The results of his experiments are expressed in what is known as Wöhler's law, which is given in the following words in Dubois's translation of Wevrauch:

"Rupture may be caused not only by a steady load which exceeds the carrying strength, but also by repeated applications of stresses, none of which are equal to the carrying strength. The differences of these stresses are measures of the disturbance of continuity, in so far as by their increase the minimum stress which is still necessary for rupture diminishes."

A practical illustration of the meaning of the first portion of this law may be given thus: If 50,000 pounds once applied will just break a bar of iron or steel, a stress very much less than 50,000 pounds will break it if repeated

sufficiently often.

This is fully confirmed by the experiments of Fairbairn and Spangenberg, as well as those of Wöhler; and, as is remarked by Weyrauch, it may be considered as a long-known result of common experience. It partially accounts for what Mr. Holley has called the "intrinsically ridiculous factor of safety of six."

Another "long-known result of experience" is the fact that rupture may

Another "long-known result of experience" is the fact that rupture may be caused by a succession of shocks or impacts, none of which alone would be sufficient to cause it. Iron axles, the piston-rods of steam hammers, and other pieces of metal subject to continuously repeated shocks, invariably break after a certain length of service. They have a "life" which is lim-

ited.

Sereal years ago Fairbairn wrote: "We know that in some cases wrought iron subjected to continuous vibration assumes a crystalline structure, and that the cohesive powers are much deteriorated, but we are ignorant of the causes of this change." We are still ignorant, not only of the causes of this change, but of the conditions under which it takes place. Who knows whether wrought from subjected to very slight continuous vibration will endure forever? or whether to insure final rupture each of the continuous small shocks must amount at least to a certain percentage of single heavy shock (both measured in foot pounds), which would cause rupture with one application? Wöhler found in testing iron by repeated stresses (not impacts) that in one case 400,000 applications of a stress of 500 centurers to the square inch caused rupture, while a similar bar remained sound after 48,000,000 applications of a stress of 500 centurers to the square inch (1 centure = 110.2 lbs.).

Who knows whether or not a similar law holds true in regard to repeated shocks? Suppose that a bar of iron would break under a single impact of 1000 foot-pounds, how many times would it be likely to bear the repetition of 100 foot-pounds, or would it be safe to allow it to remain for fifty years subjected to a continual succession of blows of even 10 foot-pounds each? Mr. William Metcalf published in the Metalturgical Review, Dec. 1877, the results of some tests of the life of steel of different percentages of carbon

Mr. William Metcalf published in the Metallurgical Review, Dec. 1877, the under impact. Some tests of the life of steel of different percentages of carbon under impact. Some small steel pitmans were made, the specifications for which required that the unloaded machine should run 4½ hours at the rate of 1300 revolutions per minute before breaking.

The steel was all of uniform quality, except as to carbon. Here are the

results: The

.30 C. ran 1 h. 21 m. Heated and bent before breaking.

.49 C. " 1 h. 28 m., " " " " " .43 C. " 4 h. 57 m. Broke without heating.

.65 C. "3 h. 50 m. Broke at weld where imperfect.

.80 C. " 5 h. 40 m. .84 C. " 18 h.

.87 C. Broke in weld near the end.

.96 C. Ran 4.55 m., and the machine broke down.

Some other experiments by Mr. Metcalf confirmed his conclusion, viz.,

that high-carbon steel was better adapted to resist repeated shocks and vibrations than low-carbon steel.

These results, however, would scarcely be sufficient to induce any engineer to use .84 carbon steel in a car-axle or a bridge-rod. Further experi-

ments are needed to confirm or overthrow them.

(See description of proposed apparatus for such an investigation in the author's paper in Trans. A. I. M. E., vol. viii, p. 76, from which the above extract is taken.)

### Stresses Produced by Suddenly Applied Forces and Shocks.

(Mansfield Merriman, R. R. & Eng. Jour., Dec. 1889.)

Let P be the weight which is dropped from a height h upon the end of a bar, and let y be the maximum elongation which is produced. The work performed by the falling weight, then, is

W = P(h + y),

and this must equal the internal work of the resisting molecular stresses. The stress in the bar, which is at first 0, increases up to a certain limit Q, which is greater than P; and if the elastic limit be not exceeded the elongation increases uniformly with the stress, so that the internal work is equal to the mean stress 1/2Q multiplied by the total elongation y, or

$$W = 1/2 Qy$$
.

Whence, neglecting the work that may be dissipated in heat,

1/2Qu = Ph + Pu

If e be the elongation due to the static load P, within the elastic limit  $y = \frac{Q}{D} e$ ; whence

$$Q = P\left(1 + \sqrt{1 + 2\frac{h}{e}}\right), \quad \dots \quad (1)$$

which gives the momentary maximum stress. Substituting this value of Q. there results

 $y = e\left(1 + \sqrt{1 + 2\frac{h}{a}}\right),$ 

which is the value of the momentary maximum elongation. A shock results when the force P, before its action on the bar, is moving with velocity, as is the case when a weight P falls from a height h. The above formulas show that this height h may be small if e is a small quantum. tity, and yet very great stresses and deformations be produced. For instance, let h=4e, then Q=4P and y=4e; also let h=12e, then Q=6P and y=6e. Or take a wrought iron bar 1 in. square and 5 ft. long; under a steady load of 5000 lbs. this will be compressed about 0.0012 in., supposing that no lateral flexure occurs; but if a weight of 5000 lbs, drops upon its end from the small height of 0.0048 in, there will be produced the stress of 20,000 lbs.

A suddenly applied force is one which acts with the uniform intensity P upon the end of the bar, but which has no velocity before acting upon it. This corresponds to the case of h=0 in the above formulas, and gives Q=2P and y=2e for the maximum stress and maximum deformation. Probably the action of a rapidly-moving train upon a bridge produces stresses of this character.

Increasing the Tensile Strength of Iron Bars by Twisting them. -Ernest L. Ransome of San Francisco has obtained an English Patent, No. 16221 of 1888, for an "improvement in strengthening and testing wrought metal and steel rods or bars, consisting in twisting the same in a con state. . . . Any defect in the lamination of the metal which would otherwise be concealed is revealed by twisting, and imperfections are shown at once. The treatment may be applied to bolts, suspension-rods or bars subjected to tensile strength of any description." Results of tests of this process were reported by Lieutenant F. P. Gilmore, U. S. N., in a paper read before the Technical Society of the Pacific Coast, published in the Transactions of the Society for the month of December, 1888.

Tests were also made in 1889 in the University of California. The experiments include trials with thirty-nine bars, twenty-nine of which were variously twisted, from three-eighths of one turn to six turns per foot. test-pieces were cut from one and the same bar, and accurately measured and numbered. From each lot two pieces without twist were tested for tensile strength and ductility. One group of each set was twisted until the pieces broke, as a guide for the amount of twist to be given those to be tested for tensile strain.

The following is the result of one set of Lieut. Gilmore's tests, on iron bars 8 in. long, 719 in. diameter.

No. of Bars.	Conditions,	Twists in Turns.	Twists per ft.	Tensile Strength.	Tensile per sq. in,	Gain per cent.
2 2 2 2 2 1	Not twisted. Twisted cold. """	0 1/2 1 2 21/2	0 3/4 11/2 3 33/4	22,000 23,900 25,800 26,300 26,400	54,180 59,020 63,500 64,750 65,000	9 17 19 20

### TENSILE STRENGTH.

The following data are usually obtained in testing by tension in a testingmachine a sample of a material of construction:

The load and the amount of extension at the elastic limit. The maximum load applied before rupture.

The elongation of the piece, measured between gauge-marks placed a stated distance apart before the test; and the reduction of area at the

point of fracture.

The load at the elastic limit and the maximum load are recorded in pounds per square inch of the original area. The elongation is recorded as a percentage of the stated length between the gauge-marks, and the reduction area as a percentage of the original area. The coefficient of elasticity is calculated from the ratio the extension within the elastic limit per inch of length bears to the load per square inch producing that extension.

On account of the difficulty of making accurate measurements of the fractured area of a test-piece, and of the fact that elongation is more valuable than reduction of area as a measure of ductility and of resilience or work of resistance before rupture, modern experimenters are abandoning the custom of reporting reduction of area. The "strength per square inch of fractured section" formerly frequently used in reporting tests is now almost entirely abandoned. The data now calculated from the results of a tensile test for commercial purposes are: 1. Tensile strength in pounds per square inch of original area. 2. Elongation per cent of a stated length between gauge-marks, usually 8 inches. 3. Elastic limit in pounds per square inch of original area.

The short or grooved test specimen gives with most metals, especially with wrought iron and steel, an apparent tensile strength much higher than the real strength. This form of test-piece is now almost entirely aban-

The following results of the tests of six specimens from the same 11/4" steel bar illustrate the apparent elevation of elastic limit and the changes in other properties due to change in length of stems which were turned down in each specimen to .798" diameter. (Jas. E. Howard, Eng. Congress 1893, Section G.)

Description of Stem.	Elastic Limit,	Tensile Strength,	Contraction of	
	Lbs. per Sq. In.	Lbs. per Sq. In.	Area, per cent.	
1.00" long	64,900	94,400	49.0	
	65,320	97,800	43.4	
	68,000	102,420	39.6	
Semicircular groove, .4" radius	75,000	116,380	81.6	
V-shaped groove	86,000, about	134,960	23.0	
	90,000, about	117,000	Indeterminate.	

Tests plate made by the author in 1879 of straight and grooved test-pieces of boiler-plate steel cut from the same gave the following results:

5 straight pieces, 56,605 to 59,012 lbs. T. S. Aver. 57,566 lbs. 4 grooved "64,341 to 67,400" "65,452" Excess of the short or grooved specimen, 21 per cent, or 12.114 lbs.

Measurement of Elongation.—In order to be able to compare records of elongation, it is necessary not only to have a uniform length of section between gauge-marks (say 8 inches), but to adopt a uniform method of measuring the elongation to compensate for the difference between the apparent elongation when the piece breaks near one of the gauge-marks, and when it breaks midway between them. The following method is recommended (Traus. A. S. M. E., vol. xi., p. 622);

Mark on the specimen divisions of 1/2 inch each. After fracture measure

from the point of fracture the length of 8 of the marked spaces on each fractured portion (or 7 + on one side and 8 + on the other if the fracture is not at one of the marks). The sum of these measurements, less 8 inches, is the elongation of 8 inches of the original length. If the fracture is so near one end of the specimen that 7+spaces are not left on the shorter portion, then take the measurement of as many spaces (with the fractional part next to the fracture) as are left, and for the spaces lacking add the measurement of as many corresponding spaces of the longer portion as are necessary to make the 7+ spaces.

Shapes of Specimens for Tensile Tests.—The shapes shown in Fig. 74 were recommended by the author in 1882 when he was connected

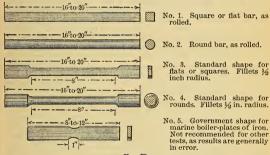


Fig. 75.

with the Pittsburgh Testing Laboratory. They are now in most general use, the earlier forms, with 5 inches or less in length between shoulders. being almost entirely abandoned.

Precautions Required in making Tensile Tests .- The testing-machine itself should be tested, to determine whether its weighing apparatus is accurate, and whether it is so made and adjusted that in the test of a properly made specimen the line of strain of the testing-machine

is absolutely in line with the axis of the specimen.

The specimen should be so shaped that it will not give an incorrect record of strength.

It should be of uniform minimum section for not less than five inches of

its length. Regard must be had to the time occupied in making tests of certain mate-Wrought iron and soft steel can be made to show a higher than their actual apparent strength by keeping them under strain for a great length

of time. In testing soft alloys, copper, tin, zinc, and the like, which flow under constant strain their highest apparent strength is obtained by testing them rapidly. In recording tests of such materials the length of time occupied in the test should be stated.

For very accurate measurements of elongation, corresponding to increments of load during the tests, the electric contact micrometer, described in Trans. A. S. M. E., vol. vi., p. 479, will be found convenient. When readings of elongation are then taken during the test, a strain diagram may be plotted from the reading, which is useful in comparing the qualities of different specimeus. Such strain diagrams are made automatically by the new Olsen testing-machine, described in Jour. Frank. Inst. 1891.

The coefficient of elasticity should be deduced from measurement observed between fixed increments of load per unit section, say between 2000 and 12,000 pounds per square inch or between 1000 and 11,000 pounds instead

of between 0 and 10,000 pounds.

### COMPRESSIVE STRENGTH.

What is meant by the term "compressive strength" has not yet been settled by the authorities, and there exists more confusion in regard to this term than in regard to any other used by writers on strength of materials. The reason of this may be easily explained. The effect of a compressive stress upon a material varies with the nature of the material, and with the shape and size of the specimen tested. While the effect of a tensile stress is to produce rupture or separation of particles in the direction of the line of strain, the effect of a compressive stress on a piece of material may be either to cause it to fly into splinters, to separate into two or more wedge-shaped pieces and fly apart, to bulge, buckle, or bend, or to flatten out and utterly resist rupture or separation of particles. A piece of speculum metal under compressive stress will exhibit no change of appearance until rupture takes place, and then it will fly to pieces as suddenly as if blown apart by gunpowder. A piece of cast iron or of stone will generally split into wedge-shaped fragments. A piece of wrought iron will buckle or bend. A piece of wood or zine may bulge, but its action will depend upon its shape and size. A piece of lead will flatten out and resist compression till the last degree; that is, the more it is compressed the greater becomes its resistance.

Air and other gaseous bodies are compressible to any extent as long as they retain the gaseous condition. Water not confined in a vessel is compressed by its own weight to the thickness of a mere film, while when con-

fined in a vessel it is almost incompressible.

It is probable, although it has not been determined experimentally, that solid bodies when confined are at least as incompressible as water. When they are not confined, the effect of a compressive stress is not only to shorten them, but also to increase their lateral dimensions or bulge them.

Lateral strains are therefore induced by compressive stresses.

The weight per square inch of original section required to produce any given amount or percentage of shortening of any material is not a constant quantity, but varies with both the length and the sectional area, with the shape of this sectional area, and with the relation of the area to the length. The "compressive strength" of a material, if this term be supposed to mean the weight in pounds per square inch necessary to cause rupture, may vary with every size and shape of specimen experimented upon. Still more difficult would it be to state what is the "compressive strength" of a material which does not rupture at all, but flattens out. Suppose we are testing a cylinder of a soft metal like lead, two inches in length and one inch in diameter, a certain weight will shorten it one per cent, another weight ten per cent, another fifty per cent, but no weight that we can place upon it will rupture it, for it will flatten out to a thin sheet. What, then, is its compressive strength? Again, a similar cylinder of soft wrought iron would probably compress a few per cent, bulging evenly all around; it would then comence to bend, but at first the bend would be imperceptible to the eye and too small to be measured. Soon this bend would be great enough to be noticed, and finally the piece might be bent nearly double, or otherwise distorted. What is the "compressive strength" of this piece of iron? Is it weight per square inch which compresses the piece one per cent or five per cent, that which causes the first bending (impossible to be discovered), or that which causes a perceptible bend?

As showing the confusion concerning the definitions of compressive strength, the following statements from different authorities on the strength

of wrought iron are of interest.

Wood's Resistance of Materials states, "comparatively few experiments have been made to determine how much wrought iron will sustain at the point of crushing. Hodgkinson gives 65,000, Rondulet 70,800, Weisbach 72,000, Rondulet 70,800, Rondulet

Rankine 30,000 to 40,000. It is generally assumed that wrought iron will resist about two thirds as much crushing as to tension, but the experiments fail

to give a very definite ratio."

Mr. Whipple, in his treatise on bridge-building, states that a bar of good wrought iron will sustain a tensile strain of about 60,000 pounds per square inch, and a compressive strain, in pieces of a length not exceeding twice the least diameter, of about 90,000 pounds.

The following values, said to be deduced from the experiments of Major Wade, Hodgkinson, and Capt. Meigs, are given by Haswell:

65,200 " English 40,000 "

Stoney states that the strength of short pillars of any given material, all having the same diameter, does not vary much, provided the length of the piece is not less than one and does not exceed four or five diameters, and that the weight which will just crush a short prism whose base equals one square nuch, and whose height is not less than 1 to 1½ and does not exceed 4 or 5 diameters, is called the crushing strength of the material. It would be wall if experimentary would all expect more some study destrict. be well if experimenters would all agree upon some such definition of the term "crushing strength," and hisist that all experiments which are made for the purpose of testing the relative values of different materials in compression be made on specimens of exactly the same shape and size. An arbitrary size and shape should be assumed and agreed upon for this purpose. The size mentioned by Stoney is definite as regards area of section, viz., one square inch, but is indefinite as regards length, viz., from some to five diameters. In some metals a specimen five diameters long would bend, and give a much lower apparent strength than a specimen having a length of one diameter. The words "will just crush" are also indefinite for ductile materials, in which the resistance increases without limit if the piece tested does not bend. In such cases the weight which causes a certain percentage of compression, as five, ten, or fifty per cent, should be assumed as the crushing strength.

For future experiments on crushing strength three things are desirable: First, an arbitrary standard shape and size of test specimen for comparison of all materials. Secondly, a standard limit of compression for ductile materials, which shall be considered equivalent to fracture in brittle materials. Thirdly, an accurate knowledge of the relation of the crushing strength of a specimen of standard shape and size to the crushing strength of specimens of all other shapes and sizes. The latter can only be secured by a very extensive and accurate series of experiments uppon all kinds of materials, and on specimens of a great number of different shapes

and sizes

The author proposes, as a standard shape and size, for a compressive test specimen for all metals, a cylinder one inch in length, and one half square inch in sectional area, or 0.798 inch diameter; and for the limit of compressions. sion equivalent to fracture, ten per cent of the original length. The term "compressive strength," or "compressive strength of standard specimen," would then mean the weight per square inch required to fracture by con-pressive stress a cylinder one inch long and 0.798 inch diameter, or to reduce its length to 0.9 inch if fracture does not take place before that reducreduce its length to 3.5 men in tracture toos not take place critical too in length is reached. If such a standard, or any standard size whatever, had been used by the earlier authorities on the strength of materials, we never would have had such discrepancies in their statements in regard to

the compressive strength of wrought iron as those given above.

The reasons why this particular size is recommended are: that the sectional area, one-half square inch, is as large as can be taken in the ordinary testing-machines of 100,000 pounds capacity, to include all the ordinary metals ing-machines of 100,000 pounds capacity, to include all the ordinary metals of construction, cast and wrought iron, and the softer steels; and that the length, one inch, is convenient for calculation of percentage of compression. If the length were made two inches, many materials would bend in testing, and give incorrect results. Even in cast iron Hodgkinson found as the mean of several experiments on various grades, tested in specimens ¾ inch in height, a compressive strength per square inch of 91,730 pounds, while the mean of the same number of specimens of the same irons tested in pieces 1½ inches in height was only §8,800 pounds. The best size and shape of standard specimen should, however, he settled upon only after consultation and agreement among several authorities. agreement among several authorities.

The Committee on Standard Tests of the American Society of Mechanical

Engineers say (vol. xi., p. 624):

Although compression tests have heretofore been made on diminutive sample pieces, it is highly desirable that tests be also made on long pieces from 10 to 20 diameters in length, corresponding more nearly with actual practice, in order that elastic strain and change of shape may be determined by using proper measuring apparatus.

The elastic limit, modulus or coefficient of elasticity, maximum and ultimate resistances, should be determined, as well as the increase of section at mathematical control of the control of t

various points, viz., at bearing surfaces and at crippling point,

The use of long compression-test pieces is recommended, because the investigation of short cubes or cylinders has led to no direct application of the constants obtained by their use in computation of actual structures, which have always been and are now designed according to empirical formulæ obtained from a few tests of long columns."

## COLUMNS, PILLARS, OR STRUTS.

### Hodgkinson's Formula for Columns.

 $P = \text{crushing weight in pounds}; d = \text{exterior diameter in inches}; d_1 = \text{in-}$ terior diameter in inches: L = length in feet.

Both ends rounded, the Both ends flat, the length of the column length of the column Kind of Column... exceeding 15 times exceeding 30 times its diameter. its diameter.  $P = 33,380 \frac{d^{3\cdot76}}{}$  $P = 98,920 \frac{d^{3*55}}{L^{1*7}}$ Solid cylindrical col-) umns of cast iron....  $P = 99,320 \frac{t^{3\cdot55} - d_1^{3\cdot55}}{}$  $P = 29,120 \frac{d^{3\cdot76} - d^{3\cdot76}}{}$ Hollow cylindrical col- ) umns of cast iron.... Solid evlindrical col-) umns of wrought iron. Solid square pillar of ) Dantzie oak (dry)... Solid square pillar of red deal (dry)....

The above formulæ apply only in cases in which the length is so great that the column breaks by bending and not by simple crushing. If the column be shorter than that given in the table, and more than four or five times its diameter, the strength is found by the following formula:

$$W = \frac{PCK}{P + \frac{3}{4}CK},$$

in which P = the value given by the preceding formulæ, K = the transverse section of the column in square inches, C = the ultimate compressive resistance of the material, and W = the crushing strength of the column.

Hodgkinson's experiments were made upon comparatively short columns, the greatest length of cast-iron columns being 60½ inches, of wrought iron 90% inches, or wrought iron 90% i

The following are some of his conclusions:

1. In all long pillars of the same dimensions, when the force is applied in the direction of the axis, the strength of one which has flat ends is about three times as great as one with rounded ends.

2. The strength of a pillar with one end rounded and the other flat is an arithmetical mean between the two given in the preceding case of the same

dimensions.

3. The strength of a pillar having both ends firmly fixed is the same as one of half the length with both ends rounded.

4. The strength of a pillar is not increased more than one seventh by enlarging it at the middle.

Gordon's formulæ deduced from Hodgkinson's experiments are more generally used than Hodgkinson's own. They are:

**rdon's form ulæ** deduced from Hodgkinson's expally used than Hodgkinson's own. They are:

Columns with both ends fixed or flat, 
$$P = \frac{fS}{1 + a_{72}^{12}}$$

Columns with one end flat, the other end round, 
$$P = \frac{fS}{1 + 1.8a\frac{l^2}{r^2}}$$

Columns with both ends round, or hinged, 
$$P = \frac{fS}{1 + 4a_{-2}^{2}}$$

S = area of cross-section in inches:

S= area of cross-section III menes, P= ultimate resistance of column, in pounds; f= crushing strength of the material in lbs. per square inch; r= least radius of gyration, in inches,  $r^2=\frac{\text{Moment of inertia}}{\text{area of section}}$ ;

l = length of column in inches:

a = a coefficient depending upon the material:

f and a are usually taken as constants; they are really empirical variables, dependent upon the dimensions and character of the column as well as upon the material. (Burr.)

For solid wrought-iron columns, values commonly taken are: f = 36,000 to

40,000; 
$$a = \frac{1}{36,000}$$
 to  $\frac{1}{40,000}$ .

For solid cast-iron columns, 
$$f = 80,000$$
,  $a = \frac{1}{6400}$ 

For hollow cast-iron columns, fixed ends,  $p = \frac{80,000}{1 + 800 \frac{12}{32}}$ , l = length and

d = diameter in the same unit, and p = strength in lbs. per square inch. Sir Benjamin Baker gives,

For mild steel, 
$$f = 67,000$$
 lbs.,  $a = \frac{1}{22,400}$ .  
For strong steel,  $f = 114,000$  lbs.,  $a = \frac{1}{14,400}$ 

Mr. Burr considers these only loose approximations for the ultimate resistances.

### MOMENT OF INERTIA AND RADIUS OF GYRATION.

The moment of inertia of a section is the sum of the products of each elementary area of the section into the square of its distance from an assumed axis of rotation, as the neutral axis.

The radius of gyration of the section equals the square root of the quotient of the moment of inertia divided by the area of the section. If

 $\hat{R}$  = radius of gyration, I = moment of inertia and A = area,

$$R = \sqrt{\frac{I}{A}}$$
.  $\frac{I}{A} = R^2$ .

The moments of inertia of various sections are as follows;

The hollness of hierards of various sections are as follows, d= diameter, or outside diameter;  $d_1=$  inside diameter; b= breadth; b= depth;  $b_1$ ,  $b_1$ , inside breadth and diameter; Solid regular  $I=I/12(bh^3-b_1h_1^2)$ ; Solid square  $I=I/12(bh^3-b_1h_1^2)$ ; Hollow square  $I=I/12(bh^2-b_1^4)$ ; Solid eylinder  $I=I/64\pi d^4+(blow)$  Hollow cylinder  $I=I/64\pi d^4-d_1^4$ ).

Moments of Inertia and Radius of Gyration for Various Sections, and their Use in the Formulas for Strength of Girders and Columns.—The strength of sections to resit strains, either as girders or as columns, depends not only on the area but also on the form of the section, and the property of the section which forms the basis of the constants used in the formulas for strength of girders and columns to express the effect of the form, is its moment of inertia about its neutral axis. Thus the moment of resistance of any section to transverse bending is its moment of inertia divided by the distance from the neutral axis to the fibres farthest removed from that axis; or

Moment of inertia Moment of resistance =  $\frac{\text{Moment of inertia}}{\text{Distance of extreme fibre from axis}}$ .  $M = \frac{I}{v}$ 

Moment of Inertia of Compound Shapes. (Pencoyd Iron Works).—The moment of inertia of any section about any axis is equal to the I about a parallel axis passing through its centre of gravity + (the area of the section X the square of the distance between the axes).

By this rule, the moments of inertia or radii of gyration of any single sec-

tions being known, corresponding values may be obtained for any combination of these sections.

Radius of Gyration of Compound Shapes.—In the case of a pair of any shape without a web the value of R can always be found without considering the moment of inertia.

The radius of gyration for any section around an axis parallel to another axis passing through its centre of gravity is found as follows:

Let r = radius of gyration around axis through centre of gravity; R =radius of gyration around another axis parallel to above; d = distance between axes:

 $R = \sqrt{d^2 + r^2}.$ 

When r is small, R may be taken as equal to d without material error. **Graphical Method for Finding Radius of Gyration.**—Benj. F. La Rue, Eng. News, Feb. 2, 1893, gives a short graphical method for finding the radius of gyration of hollow, cylindrical, and rectangular columns, as follows:

For cylindrical columns:

Lay off to a scale of 4 (or 40) a right-angled triangle, in which the base equals the outer diameter, and the altitude equals the inner diameter of the column, or vice versa. The hypothenuse, measured to a scale of unity (or 10), will be the radius of gyration sought.
This depends upon the formula

$$G = \sqrt{\frac{\text{Mom. of Inertia}}{\text{Area}}} = \frac{\sqrt{D^2 + d^2}}{4},$$

in which A =area and D =diameter of outer circle,  $\alpha =$ area and d =diameter of outer circle. meter of inner circle, and G = radius of gyration.  $\sqrt{D^2 + d^2}$  is the expression for the hypothenuse of a right-angled triangle, in which D and d are the base and altitude.

The sectional area of a hollow round column is  $.7854(D^2-d^2)$ . By constructing a right-angled triangle in which D equals the hypothenuse and d equals the altitude, the base will equal  $\sqrt{D^2-d^2}$ . Calling the value of this expression for the base B, the area will equal .7854 $B^2$ .

Value of G for square columns: Lay off as before, but using a scale of 10, a right-angled triangle of which the base equals D or the side of the outer square, and the altitude equals d, the side of the inner square. With a scale of 3 measure the hypothenuse, which will be, approximately, the radius of gyration.

This process for square columns gives an excess of slightly more than 4%. By deducting 4% from the result, a close approximation will be obtained.

A very close result is also obtained by measuring the hypothenuse with the same scale by which the base and altitude were laid off, and multiplying by the decimal 0.29; more exactly, the decimal is 0.28867.

The formula is

$$G = \sqrt{\frac{\text{Mom. of inertia}}{\text{Area}}} = \frac{1}{4\sqrt{12}} \sqrt{D^2 + d^2}, = 0.28867 \sqrt{D^2 + d^2}$$

This may also be applied to any rectangular column by using the lesser diameters of an unsupported column, and the greater diameters if the column is supported in the direction of its least dimensions.

ELEMENTS OF USUAL SECTIONS.

Moments refer to horizontal axis through centre of gravity. This table is intended for convenient application where extreme accuracy is not important. Some of the terms are only approximate; those marked \*are correct. Values for radius of gyration in flanged beams apply to standard minimum sections only.  $A = \operatorname{are}$  are of section;  $b = \operatorname{breadth}$ ;  $b = \operatorname{breadth}$ ;

Shape of Section.		Moment of Inertia.	Moment of Resistance.	Square of Least Radius of Gyration.	Least Radius of Gyration.	
( ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~ ~	Solid Rect- angle.	bh³ *	bh2 *	(Least side)2*	Least side *	
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	Hollow Rectangle.	$\frac{bh^3-b_1h_1^3}{12}$ *	$\frac{bh^3 - b_1h_1^{3*}}{6h}$	$\frac{h^2 + h_1^2}{12} *$	$\frac{h+h^1}{4.89}$	
	Solid Circle.	AD2 *	<u>AD</u> *	<u>D</u> <sup>2</sup> * <u>16</u>	<u>D</u> *	
	Hollow Circle.  A, area of large section; a, area of small section.	$\frac{AD^2 - ad^2}{16}$	$\frac{AD^2 - ad^2}{8D}$	$\frac{D^2 + d^2}{16}$ *	$\frac{D+d}{5.64}$	
	Solid Triangle.	bh³ 36	bh² 24	The least of of the two: $\frac{h^2}{18}$ or $\frac{b^2}{24}$	The least of the two; $\frac{h}{4.24}$ or $\frac{b}{4.9}$	
-b-+	Even Angle.	$\frac{Ah^2}{10.2}$	$rac{Ah}{7.2}$	b <sup>2</sup> 25	b 5	
To have	Uneven Angle.	Ah <sup>2</sup> 9.5	$\frac{Ah}{6.5}$	$\frac{(hb)^2}{13(h^2+b^2)}$	$\frac{hb}{2.6(h+b)}$	
	Even Cross.	$\frac{Ah^2}{19}$	$\frac{Ah}{9.5}$	$\frac{h^2}{22.5}$	h 4.74	
	Even Tee.	<u>Ah²</u> 11.1	$\frac{Ah}{8}$	$\frac{b^2}{22.5}$	b 4.74	
	I Beam.	$\frac{Ah^2}{6.66}$	$\frac{Ah}{3.2}$	$\frac{b^2}{21}$	<u>b</u> 4.58	
3	Channel.	Ah <sup>2</sup> 7.34	$\frac{Ah}{3.67}$	$\frac{b^2}{12.5}$	<u>b</u> 3.54	
	Deck Beam.	$\frac{Ah^2}{6.9}  \cdot$	$\frac{Ah}{4}$	$\frac{b^2}{36.5}$	<u>b</u> <u>6</u>	

Distance of base from centre of gravity, solid triangle,  $\frac{h}{3}$ ; even angle,  $\frac{h}{3.3}$ ; uneven angle,  $\frac{h}{3.5}$ ; even tee,  $\frac{h}{3.3}$ ; deck beam,  $\frac{h}{2.3}$ ; all other shapes given in the table,  $\frac{h}{2}$  or  $\frac{D}{2}$ .

### Solid Cast-iron Columns.

Hurst gives the following table, based on Hodgkinson's formula (tons of 2240 lbs.).

The figures are the safe load or to of the breaking weight in tons, for solid columns, ends flat and fixed.

r in		Length of Column in Feet.							
Diam. Inche	6.	8.	10.	12.	14.	16.	18.	20.	25.
1½ 1¾	.82	.50	.34	.25	.19	.15	.13	.11	.07
-2 -	2.31 3.52 5.15	2.16 3.16		1.08	.55 .83 1.22	.67	.36 .54 .80	.30 .46 .66	.20 .31 .56
21/4 21/5 23/4 3	7.26 9.93	4.45 6.09	3.05 4.17	2.23 3.06	1.72 2.35	1.37	1.12 1.53	1.28	.64
31/2 4 41/6	17.29 27.96 42.73	10.60 17.15 26.20	17.93	13.15	4.10 6.62 10.12	3.26 5.28 8.07	2.67 4.32 6.60	2.23 3.61 5.52	1.53 2.47 3.78
4½ 5 5½ 6	62.44 88.00 120.4	38.29 53.97 73.82	26.20 36.93 50.51	19.22 27.09 37.05	14.79 20.84 28.51	11.79 16.61 22.72	9.65 13.60 18.60	8.06 11.37 15.55	5.52 7.78 10.64
6½ 7	160.6 209.7 268.8	98.47 128.6 164.8	67.38 87.98 112.8	49.43	38.03 49.66 63.66	30.31 39.57 50.73	24.81 32.30 41.53	20.74 27.08 34.72	14.19 18.53 -23.76
7½ 8 - 8½	339.1 421.8	207.9 258.6	142.3 177.0	104.4 129.8	80.31	64.00 -79.61	52.39 65.16	43.80 54.48	29.97 37.28
91/2	629.5 757.2	317.7 386.0 464.3	217.4 264.2 317.7	159.5 193.8 233.1	122.7 149.1 179.3	97.80 118.8 142.9	80.05 97.25 117.0	66.92 81.70 97.79	45.80 55.64 66.92
10½ 11 11½		553.5 654.4 767.9	378.7 447.8 525.5	277.8 328.5 385.4	213.8 252.7 296.6	170.3 201.4 236.4	139.4 164.9 193.5	116.6 137.8 161.7	79.77 94.31 110.7
12		895.1	612.5	449.3	845.7	275.5	225.5	188.5	129.0

The correction for short columns should be applied where the length is less than 30 diameters.

Strength in tons of short columns = 
$$\frac{SC}{10S + \frac{3}{4}C}$$
,

S being the strength for long columns given in the above table, and C=49times the sectional area of the metal in inches.

Hollow Columns.—The strength nearly equals the difference between that of two solid columns the diameters of which are equal to the external and internal diameters of the hollow one,

### Ultimate Strength of Hollow, Cylindrical Wrought and Cast-iron Columns, when fixed at the ends.

(Pottsville Iron and Steel Co.)

Computed by Gordon's formula, 
$$p = \frac{f}{1 + C \left(\frac{l}{\bar{d}}\right)^{\frac{\alpha}{2}}}$$
.

p =Ultimate strength in lbs. per square inch:

p = 0 Trimate strength of solumn, both in same units; h = 0 Diameter of column, both in same units;  $f = \begin{cases} 40,000 \text{ lbs. for east-iron;} \\ 80,000 \text{ lbs. for east-iron;} \end{cases}$ 

C = 1/3000 for wrought-iron, and 1/800 for cast-iron.

For east-iron, 
$$p = \frac{80000}{1 + \frac{1}{800} \left(\frac{l}{h}\right)^2}$$
For wrought-iron, 
$$p = \frac{40000}{1 + \frac{1}{3000} \left(\frac{l}{h}\right)^2}$$

### HOLLOW CYLINDRICAL COLUMNS.

Ratio of Length to	Maximum L	oad per sq. in.	Safe Load pe	er square inch.
Diameter. $\frac{l}{h}$	Cast Iron.	Wrought Iron.	Cast Iron, Factor of 6.	Wrought Iron, Factor of 4.
8 102 144 118 222 268 280 284 286 286 286 286 286 286 286 286 286 286	74075 77110 64256 64256 60606 60606 56938 53938 53938 49415 49510 43904 43704	39164 38710 38168 37548 38554 38559 35294 34452 33612 30768 29682 29873 27002 28873 27002 28168 2416 2416 2118 2118 2118 2118 2118 2118 2118 21	12346 11851 11299 10709 10101 9480 8889 8897 7721 7725 6734 6274 5848 5453 5097 4753 4444 4160 3898 3898 3498 2877 28710 28710	9791 9877 9542 9386 9213 9055 8820 8860 8380 8161 7925 7455 7215 6930 6750 6527 6077 6077 5863 5654 5259 5071 4889 4771
.60	14544	18180	2424	4545

### Ultimate Strength of Wrought-iron Columns.

p = ultimate strength per square inch; l = length of column in inches;

t = length of column in inches;r = least radius of gyration in inches.

For square end-bearings,

$$p = \frac{40000}{1 + \frac{1}{40000} \left(\frac{l}{r}\right)^2}$$

For one pin and one square bearing,  $p = \frac{400}{1}$ 

$$p = \frac{40000}{1 + \frac{1}{20000} \left(\frac{l}{r}\right)^2}.$$

For two pin-bearings,

$$0 = \frac{40000}{1 + \frac{1}{20000} \left(\frac{l}{r}\right)^2}$$

For safe working load on these columns use a factor of 4 when used in buildings, or when subjected to dead load only; but when used in bridges the factor should be 5.

### WROUGHT-IRON COLUMNS.

$\frac{l}{r}$	Ultimat per	e Strength square in	in lbs.	$\frac{l}{r}$	Safe Strength in lbs. per square inch—Factor of 5.			
$\overline{r}$	Square Ends.	Pin and Square End.	Pin Ends.	$\overline{r}$	Square Ends.	Pin and Square End.	Pin Ends.	
10 15 20 25 30 35 40 45 50 65 70 75 80 85 90 90 100	39944 39776 39364 39384 39318 38460 38460 37186 36667 36182 35634 35076 34882 35076 34882 3593 34882 3593 34882 3593 34882 3593 34882 3593 3593 3593 3593 3593 3593 3593 359	39866 39702 39472 39182 38583 38583 38583 36928 36938 35714	39800 39554 39214 38788 38278 37036 36332 35525 34744 32128 33024 32128 32128 30282 2470 25786	10 15 20 25 30 35 40 45 50 55 60 65 70 75 80 85 90 100	7989 7955 7921 7877 7821 7762 7692 7694 7529 7387 7386 7127 7015 6896 6777 6658 66587 66400 6271	7973 7940 7894 7896 7767 7886 7395 7494 7386 7267 7386 7267 7386 6896 6877 6736 6996 6877 6736 6990 6500 6000 5850	7960 7911 7843 7758 7656 7587 7407 7264 7105 6949 6780 6605 6426 6244 6058 5877 5694 5512 5333 7457	

Maximum Permissible Stresses in columns used in buildings. (Building Ordinances of City of Chicago, 1893.)

Maximum permissible loads:

For cast-iron round columns :

$$S = \frac{10000a}{1 + \frac{l^2}{1000a^2}}.$$

 $S = \frac{10000a}{1 + \frac{l^2}{600d^2}}.$  l = length of column in inches; d = diameter of column in inches; a = area of column in square inches;a = area of column in square inches.

For cast-iron rectangular columns;

$$S = \frac{10000a}{1 + \frac{l^2}{10000a}}$$

l and a as before:

d = least horizontal dimension of column.

For riveted or other forms of wrought-iron columns:

$$S = \frac{12000a}{1 + \frac{l^2}{36000r^2}}, \quad l = \text{and } a \text{ as before;} \\ r = \text{least radius of gyration in inches.}$$

For riveted or other steel columns, if less than 60r in length:

$$S = 17,000 - \frac{60l}{r}$$
.  $l$  and  $r$  as before.

If more than 60r in length:

S = 13,500a, a as before.

For wooden posts:

$$S = \frac{ac}{1 + \frac{l^2}{250d^2}}.$$

$$a = \text{area of post in square inches;}$$

$$d = \text{least side of rectangular post in inches;}$$

$$l = \text{length of post in inches;}$$

$$l = \text{length of rwhite or Norway pine;}$$

$$c = \frac{800 \text{ for white or Norway pine;}}{800 \text{ for long-leaf yellow pine.}}$$

### SAFF LOAD OF HOLLOW CYLINDRICAL CAST-IRON COLUMNS. (New Jersey Steel Iron Co.)

(One fifth the breaking weight.)

The following tables give the safe load in tons of 2,000 lbs., for columns having capitals and bases accurately turned to a true plane, and having a perfectly fair bearing on these surfaces. In the case of columns having turned ends, but set only with the degree of care usual in ordinary building, only one half of these loads should be taken; and for columns not turned at all, or having rounded ends, one third of these amounts should be taken for the safe load. Columns having one end accurately turned to a true plane and the other rounded, may be loaded to two thirds the amount given in the tables.

### Safe Load, in Tons of 2000 lbs, for Cast-iron Columns with Turned Conitals and Ruses

With I tilled capitals and Dases.											
Outside Diameter, 3 inches.	Outside Diameter, 3 inches.	Outside Diameter, 4 inches.	Outside Diameter, 4 inches.								
Thickness in inches.		Thickness in inches.	Thickness in inches.								
7 12.8 15.9 17.2 8 10.9 13.0 14.0 9 8.9 10.7 11.4 10 7.5 8.9 9.6 11 6.4 7.6 8.1	17 3.0 3.6 3.9 18 2.8 3.3 3.5 19 2.5 3.0 3.2 20 2.3 2.7 2.9 21 2.1 2.5 2.7	724.932.938.341.7821.728.433.035.8919.024.828.731.01017.422.024.926.3	1   1/4   1   1/4   1/4   1/7   7.0   8.9   10.1   10.7   18   6.4   8.1   9.1   9.7   19   5.8   7.4   8.3   8.8   20   5.3   6.8   7.6   8.1   21   4.9   6.2   7.0   7.5								
12 5.4 6.6 7.0 13 4.8 5.7 6.1 14 4.2 5.0 5.4 15 3.7 4.5 4.8 16 3.4 4.0 4.3	22 1.9 2.3 2.5 23 1.8 2.1 2.3 24 1.7 2.0 2.1 25 1.6 1.9 2.0	12 12.7 16.2 18.2 19.3 13 11.1 14.1 15.9 16.8 14 9.8 12.4 14.0 14.9	22 4.6 5.8 6.5 6.9 23 4.2 5.3 6.0 6.4 24 3.9 5.0 5.6 5.9								

in ft.	Outsig	side Diameter, 5 inches. Outside Diameter, 6 inches.					ter,	Outside Diameter, 7 inches.			
Length in	Thickn	ess in i	nches.	Thi	ekness	in in	Thickness in inches.				
Ler	1/2 3/4	1	11/4	3/4	1	11/4	11/2	3/4	1	11/4	11/2
9 10 11 12 13 14	39.5 53. 35.1 47. 31.3 42. 28.0 37. 25 2 33. 22.7 30. 21.0 27. 18.5 24.	6 57.3 3 50.7 7 45.1 8 40.3 5 36.2 6 32.2 3 28.3	73.3 64.4 56.8 50.4 44.9 40.3 35.2 31.0	77.3 69.7 62.8 56.9 51.6 46.9 42.9 39.3	95.5 85.7 77.1 69.6 63.0 57.2 52.1 47.6	110.3 98.7 88.5 79.6 71.9 65.2 59.3 54.1	122.1 108.8 97.3 87.4 78.7 71.2 64.6 58.9	102.4 93.6 85.6 78.4 71.8 66.0 60.7 56.0	97.5 89.2 81.7 75.1 69.2	87.0 80.0	153.5 139.3 126.6 115.3 105.3 96.5 88.6
16 17 18 19	16.5 21. 14.8 19. 13.3 17. 12.1 15. 11.0 14. 10.1 13. 9.3 12. 8.6 11. 8.0 10. 7.4 9. 6.9 9.	4 22.6 5 20.4 9 18.5 5 16.9 3 15.4 2 14.2 3 13.1 5 12.2 7 11.3	27.6 24.7 22.8 20.2 18.4 16.9 15.5 14.4 13.3 12.4 11.5	36.8 33.0 29.8 27.0 24.6 22.6 20.8 19.2 17.8 16.6 15.4	43.9 39.4 35.5 32.2 29.4 26.9 24.8 22.9 21.2 19.7 18.4	49.0 44.0 39.7 36.0 32.8 30.1 27.7 25.6 23.7 22.1 20.6	52.6 47.2 42.5 38.6 35.2 32.3 29.7 27.4 25.4 23.7 22.1	51.8 48.1 44.6 42.0 38.3 35.1 32.3 29.8 27.7 25.7 24.0	63.9 59.2 54.9 50.9 46.4 42.5 39.1 36.2 33.5 31.2 29.1	73.8 68.2 63.2 57.8 52.7 48.3 44.5 41.1 38.1 35.4 33.1	81.6 75.4 69.8 63.0 57.4 52.6 48.4 44.7 41.5 38.6 36.0

### Safe Load, in Tons of 2000 lbs. for Cast-iron Columns with Turned Capitals and Bases.

in ft.	Out	side I 8 inc	Diame ches.	ter,	Outside Diameter. 9 inches.				Outside Diameter, 10 inches.				
Thickness in inches.					Thi	ckness	in inc	hes.	Thic	kness	in incl	ies.	
Ler	3/4	1	11/4	11/2	3/4	1	11/4	11/2	3/4	1	11/4	11/2	
7 8				219.5 201.6	154.8 144.7	197.7 184.5	236.6	271.4 252.0	181.6 171.1	233.4 219.5	280.9 263.8	324.2	
9 10	109.8 101.5	138.5 127.8	163.6 150.7	$185.2 \\ 170.2$	135.0 126.0	171.8 160.0	204.7 190.3	233.9 217.0	160.9 151.2	206.2 193.4	247.3 231.6	284.5 266.0	
11 12 13		109.2	128.2	156.7 144.3 133.2	117.5 109.6 102.4	149.0 138.8 129.4	177.0 164.5 153.2	201.4 187.0 173.9	142.0 133.4 125.3	181.4 170.1 159.6	216.9 203.1 190.3	248.7 232.6 217.7	
14 15	75.0 69.8		109.8	123.2 114.2	95.7	120.8	142.8 133.3	161.9 150.9	117.8 110.8	149.8 140.7	178.4 167.5	203.8	
16 17	65.0 60.7	81.1	94.7 88.3	106.1 98.7	83.9 78.7 73.9	105.7 99.0 92.9	124.6 116.7 109.4	140.9 131.8 123.5	98.3	132.4 124.6	157.3	179.3 168.5	
18 19 20	56.8 53.2 51.1		82.4 77.1 72.1	92.1 86.1 79.5	69.6 65.5	87.4 82.3	102.7	115.9 108.9	92.7 87.5 82.7	117.4 110.8 104.6	139.3 131.3 124.0	158.5 149.3 140.8	
21 22	47.0 43.5	57.7 53.3	66.4 61.3	73.2 67.6	61.8 58.4	75.5 73.2	91.0 85.9	102.6 96.7	78.3 74.2	99.0 93.7	117.2 110.9	$133.0 \\ 125.8$	
23 24 25	40.3 37.5 35.0	46.0	56.8 52.9 49.3	62.7 58.3 54.4	55.9 52.0 48.5	69.3 64.4 60.1	80.4 74.8 69.8	89.5 83.3 77.7	70.4 66.9 64.9	88.9 84.3 81.0	105.1 99.7 94.2	119.1 112.9 106.3	

in ft.	Out		Diame ches.	ter,	Outside Diameter, 12 inches.				Outside Diameter, 13 inches.					
Thickness in inches.					Thi	ckness	in inc	hes.	Thickness in inches.					
Lei	. 1	11/4	11/2	.2	1	11/4	11/2	.2	1	11/4	11/2	2		
	255.1	308.1		442.2	290.9	370.8 352.8	431.7 410.2	540.9 512.8	341.5 327.0	414.4 396.3	485.7 464.1	612.7 583.9		
10 11	$227.8 \\ 214.9$	$274.2 \\ 258.4$	316.7 298.1	366.3	$262.7 \\ 249.2$	335.0 317.7 301.0	389.1 368.6 348.8	485.0 458.3 432.9	298.0 284.0	378.4 360.6 343.4	442.5 421.3 400.6	555.5 527.8 501.1		
13	191.2	229.4	264.0	343.9 322.8 303.3	236.3 223.9 212.3	285.1 270.0 255.6	330.0 312.2 295.3	408.6 385.7 364.1	270.5 257.5 245.0	326.7 310.8 295.5	380.8 361.8 343.7	475.3 450.7 427.4		
15 16	170.3 160.9	203.9 $192.4$	234.1 $220.7$	$285.1 \\ 268.3$	201.2 190.8	242.1 229.4	279.4 264.5	343.9 325.0	233.2 222.0	281.1 267.3	$326.5 \\ 310.3$	405.4 384.6		
19	143.9 136.2	171.7 $162.5$	196.7 185.9	252.7 238.3 225.0	171.9 163.3	217.5 206.3 195.8	250.6 237.5 225.3	307.4 290.9 275.6	211.3 201.3 191.8	254.4 242.1 230.6	295.0 280.5 267.0	365.1 346.7 329.5		
21	122.4	145.9	166.7	212.6 201.2 190.6		186.0 176.9 168.3	213.9 203.2 193.3	261.3 247.9 235.5	182.8 174.4 166.5	219.7 209.5 199.9	254.2 242.2 230.9	313.3 298.2 284.0		
23 24	110.5 105.2	131.5 125.1	150.1 142.7	180.7 171.6 163.1	134.0 127.8	$160.3 \\ 152.8$	184.0 175.3 167.1	224.0 213.2 203.1	159.0 152.0	190.8 182.3	220.4 210.4	270.7 258.3 246.6		
20	100.2	1119.1	1 601	1,601	100.0	140.0	1107.1	1.00.1	140.4	1114.0	1201.0	1240.0		

Safe Load of Cast-iron Columns-(Continued).

in ft.	Out		Diame	eter,	Outside Diameter, 15 inches.				Outside Diameter, 16 inches.				
	Thick	ness	in in	ches.	Thic	kness	in inc	hes.	Thickness in inches.				
Length	1	11/4	11/2	2	1	11/4	11/2	2	1	11/4	11/2	2	
99 100 111 122 133 144 155 166 177 188 199 20 21 222 238 24	368.1 348.5 333.8 319.4 305.4 291.8 278.8 266.2 254.3 242.9 232.0 202.7 1194.0 185.7 177.9	442.8 424.4 406.3 388.5 371.1 354.3 354.3 322.7 308.0 294.0 280.6 268.0 256.1 244.7 234.0 224.0 2214.4	518.0 496.3 474.6 453.4 482.6 412.7 393.6 875.3 357.9 341.4 325.6 310.8 296.7 283.5 270.9 259.1 248.0	627.0 598.5 570.7 543.6 517.7 493.0 446.9 425.7 105.5 386.5 368.6 351.8 335.9 306.8	275.1 263.6 252.5 242.0 232.0 222.5 213.4	506.1 487.9 469.5 451.0 433.0 397.6 380.7 364.5 348.9 334.0 319.7 306.2 293.3 281.0 269.3 258.3 247.8	594.0 572.2 550.1 528.2 556.3 485.0 464.5 444.4 425.2 446.5 389.1 372.2 356.2 341.0 326.5 312.8 299.8 287.5 275.9	756.7 727.7 698.4 669.3 640.9 612.8 585.9 559.7 534.9 510.9 488.1 445.9 426.3 407.8 390.8 373.7 358.1	449.8 435.3 420.5 405.6 056.6 376.0 361.6 333.9 320.7 308.0 295.8 284.1 272.9 262.1 251.9 242.2 232.9	551.1 532.8 514.4 496.0 477.4 459.3 441.2 423.8 406.9 390.6 374.9 359.9 345.4 331.6 331.6 305.9 298.9 298.5 271.6	648.0 626.3 604.1 581.8 559.8 559.8 538.0 516.7 495.9 475.9 475.9 476.6 438.0 420.1 403.0 386.8 371.2 356.4 342.3 328.8	828.6 799.8 770.4 740.9 711.7 683.4 655.1 628.0 601.8 576.6 552.5 529.4 4507.3 486.3 447.2 429.1 411.9	

### ECCENTRIC LOADING OF COLUMNS.

In a given rectangular cross-section, such as a masonry joint under pressure, the stress will be distributed uniformly over the section only when the resultant passes through the centre of the section; any deviation from such a central position will bring a maximum unit pressure to one edge and a minimum to the other; when the distance of the resultant from one edge is one third of the entire width of the joint, the pressure at the nearer edge is twice the mean pressure, while that at the farther edge is zero, and that when the resultant approaches still nearer to the edge the pressure at the farther edge becomes less than zero; in fact becomes a tension, if the material (nortar, etc., there is capable of resisting tension. Or, if, as usual in masonry joints, the material is practically incapable of resisting tension, the pressure at the nearer edge, when the resultant approaches it nearer than one third of the width, increases very rapidly and dangerously, becoming theoretically infinite when the resultant reaches the edge.

With a given position of the resultant relatively to one edge of the joint or section, a similar redistribution of the pressures throughout the section may be brought about by simply adding to or diminishing the width of the section.

Let P = the total pressure on any section of a bar of uniform thickness. w = the width of that section = the area of the section, when thickness -1

 $p = \frac{P}{m}$  = the mean unit pressure on the section.

M = the maximum unit pressure on the section.

m = the minimum unit pressure on the section. d = the eccentricity of the resultant = its distance from the centre of the section.

Then 
$$M = p \left(1 + \frac{6d}{w}\right)$$
 and  $m = p \left(1 - \frac{6d}{w}\right)$ .

When  $d = \frac{1}{6} w$  then M = 2p and m = 0.

When d is greater than 1/6w, the resultant in that case being less than one third of the width from one edge, p becomes negative. (J. C. Trautwine, Jr., Engineering News, Nov. 23, 1893.)

### BUILT COLUMNS.

From experiments by T. D. Lovett, discussed by Burr, the values of f and a in several cases are deterrained, giving empirical forms of Gordon's formula as follows: p= pounds crushing strength per square inch of section, l= length of column in inches, r= radius of gyration in inches.

### Flat Ends.

$$p = \frac{\frac{\text{Keystone}}{\text{Columns.}}}{1 + \frac{1}{18,300} \frac{l^2}{r^2}} (1) = \frac{\frac{39,000}{1 + \frac{1}{35,000}}}{1 + \frac{1}{35,000} \frac{l^2}{r^2}} (4) = \frac{\frac{42,000}{1 + \frac{1}{50,000}}}{1 + \frac{l^2}{50,000} \frac{l^2}{r^2}} (6) = \frac{\frac{36,000}{46,000}}{1 + \frac{l^2}{46,000} \frac{l^2}{r^2}} (9)$$

Flat Ends. Swelled.

$$p = \frac{36,000}{1 + \frac{1}{118,300}} \frac{l^2}{r^2}$$
(2)

### Pin Ends.

$$p = \frac{39,000}{1 + \frac{1}{17,000} \frac{l^2}{r^2}} (5) \quad \frac{42,000}{1 + \frac{1}{22,700} \frac{l^2}{r^2}} (7) \quad \frac{36,000}{1 + \frac{1}{21,500} \frac{l^2}{r^2}} (10)$$

### Pin Ends, Swelled.

$$p = \frac{36,000}{1 + \frac{1}{15,000}} \frac{l^2}{r^2}$$
(3)

### Round Ends.

$$p = \frac{42,000}{1 + \frac{1}{12,500}} \frac{2}{r^2} (8) \frac{36,000}{1 + \frac{1}{11,500}} \frac{1}{r^2} (11)$$

With great variations of stress a factor of safety of as high as 6 or 8 may be used, or it may be as low as 3 or 4, if the condition of stress is uniform or essentially so.

Burr gives the following general principles which govern the resistance of built columns

The material should be disposed as far as possible from the neutral axis of the cross-section, thereby increasing r:

There should be no initial internal stress; The individual portions of the column should be mutually supporting; The individual portions of the column should be so firmly secured to each

the moving portions of the continuis should be so firmly secured to each other that no relative motion can take place, in order that the column may fail as a whole, thus maintaining the original value of r. Stoney says: "When the length of a rectangular wrought-iron tubular column does not exceed 30 times its least breadth, it fails by the bulging or buckling of a short portion of the plates, not by the flexure of the pillar as a

whole."

In Trans. A. S. C. E., Oct. 1880, are given the following formulæ for the ultimate resistance of wrought-iron columns designed by C. Shaler Smith:

### Flat Ends.

### One Pin End.

$$p = \frac{38,500}{1 + \frac{1}{3000} \frac{l^2}{d^2}} (13) \frac{40,000}{1 + \frac{1}{2250} \frac{l^2}{d^2}} (16) \frac{36,500}{1 + \frac{1}{2250} \frac{l^2}{d^2}} (19) \frac{36,500}{1 + \frac{1}{1500} \frac{l^2}{d^2}} (22)$$

### Two Pin Ends.

$$p = \frac{37,500}{1 + \frac{1}{1900}} \frac{l^2}{d^2} (14) \quad \frac{36,600}{1 + \frac{1}{1500}} \frac{l^2}{d^2} (17) \quad \frac{36,500}{1 + \frac{1}{1750}} \frac{l^2}{d^2} (20) \quad \frac{36,500}{1 + \frac{1}{1200}} \frac{l^2}{d^2} (23)$$

The "common" column consists of two channels, opposite, with flanges

outward, with a plate on one side and a lattice on the other.

The formula for "square" columns may be used without much error for the common-chord section composed of two channel-bars and plates, with the axis of the pin passing through the centre of gravity of the crosssection. (Burr).

Compression members composed of two channels connected by zigzag bracing may be treated by formulæ 4 and 5, using f = 36,000 instead of

Experiments on full-sized Pheenix columns in 1873 showed a close agreement of the results with formulæ 6-8. Experiments on full-sized Pheenix columns on the Watertown testing-machine in 1881 showed considerable discrepancies when the value of l + r became comparatively small. The following modified form of Gordon's formula gave tolerable results through the whole range of experiments:

Phoenix columns, flat end, 
$$p = \frac{40,000\left(1 + \frac{2r}{l}\right)}{1 + 50,000 \quad r^2}$$
. (24)

Plotting results of three series of experiments on Phœnix columns, a more simple formula than Gordon's is reached as follows:

Phœnix columns, flat ends,  $p = 39,640 - 46\frac{l}{r}$ , when  $l \div r$  is from 30 to 140;

$$p = 64,700 - 4600 \sqrt{\frac{l}{r}}$$
 when  $l + r$  is less than 30.

### Dimensions of Phoenix Columns.

(Phœnix Iron Co.)

The dimensions are subject to slight variations, which are unavoidable in rolling iron shapes.

The weights of columns given are those of the 4, 6, or 8 segments of which they are composed. The rivet-heads add from 2 to 5 per cent to the weights given. Rivets are spaced 3, 4, or 6 inches apart from centre to centre, and somewhat more closely at the ends than towards the centre of the column.

G columns have 8 segments, E columns 6 segments, C,  $B^2$ ,  $B^1$ , and A have 4 segments. Least radius of gyration =  $D \times .3636$ .

One Se	gment.	Diame	ters in i	oches.	On	e Colum	ın.	Cafa
Thickness in inches.	Weight in lbs. per yard.	d inside.	D Outside.	D <sup>1</sup> Over Flanges.	Area of Cross- section, sq. inches	Weight per ft. in pounds.	Least Radius of Gyration, in inches.	Safe Load in net tons for 16-feet Lengths.
3-16 14 5-16 3/8	9½ 12 14½ 17	A 35% {	4 41/8 41/4 48/8	6 1-16 6 3-16 6 5-16 6 7-16	3.8 4.8 5.8 6.8	12.6 16.0 19.3 22.6	1.45 1.50 1.55 1.59	17.72 22.65 27.66 32.58
3/6 3/6 7-16 1/6 9-16 5/8	16 19½ 23 26½ 30 33½ 37	B <sup>1</sup> 4 <sup>13</sup> / <sub>16</sub> {	5 5-16 5 7-16 5 9-16 5 11-16 5 13-16 5 15-16 6 1-16	8 1-16 8½ 8½ 8¼ 8¾ 838 8 7-16 8½ 858	6.4 7.8 9.2 10.6 12.0 13.4 14.8	21.3 26.0 30.6 35.3 40.0 44.6 49.3	1.92 1.96 2.02 2.07 2.11 2.16 2.20	32.00 39.15 46.45 53.72 61.08 68.48 70.88
5-16 36 7-16 12 9-16 56	1816 2216 2616 3016 3416 3816 4216	$egin{array}{c} B_2 \ 5 \frac{15}{16} \end{array} \ \left\{ \begin{array}{c} \end{array} \right.$	6 7-16 6 9-16 6 11-16 6 13-16 6 15-16 7 1-16 7 3-16	91/8 91/4 9 5-16 93/8 91/2 95/8 9 11-16	7.4 9.0 10.6 12.2 13.8 15.4 17.0	24.6 30.0 35.3 40.6 46.0 51.3 56.6	2.34 2.39 2.43 2.48 2.52 2.57 2.61	45.72 55.77 65.82 75.95 86.08 96.30 106.49
14 5-16 36 7-16 14 9-16 56 11-16 34 13-16 78 114 114	251/2 31 36 41 46 51 56 62 68 73 78 89 99 109	C 736	7 11-16 7 13-16 7 15-16 8 1-16 8 3-16 8 5-16 8 7-16 8 9-16 8 11-16 8 13-16 9 3-16 9 11-16	11 9-16 1156 11 11-16 1134 11 13-16 1176 12 1-16 12 3-16 12 5-16 12 7-16 12 9-16 1234 12 15-16	10.2 12.4 14.4 16.4 18.4 20.4 22.4 34.8 27.2 29.2 31.2 35.6 39.6 43.6	34. 41.3 48.0 54.6 61.3 68. 74.6 82.6 90.6 97.3 104. 118.6 132. 145.3	2.80 2.85 2.90 2.94 2.98 3.03 3.08 3.12 3.16 3.21 3.26 3.34 3.43 3.52	64.41 78.45 91.28 104.09 116.94 129.87 142.83 158.34 173.86 186.93 200.02 228.72 228.72 255.02
34 5-16 36 7-16 19 9-16 56 11-16 34 13-16 76 114	28 321/2 37 42 47 52 57 62 68 73 78 88 98 108	E	111/6 115/6 113/4 117/8 12 121/8	15 7-16 15 9-16 15 11-16 15 13-16 15 13-16 16 1-16 16 3-16 16 5-16 16 7-16 1658 1634 17 17 3-16	16.8 19.5 22.2 25.2 28.2 31.2 34.2 37.2 40.8 43.8 46.8 52.8 55.8 64.8	56. 65. 74. 84. 94. 104. 114. 124. 136. 146. 156. 176. 196. 216.	4.18 4.23 4.28 4.32 4.36 4.40 4.45 4.50 4.55 4.60 4.64 4.73 4.82 4.91	109.88 127.64 145.48 165.21 184.98 205.33 224.64 244.53 268.37 288.30 308.16 348.15 388.15 428.26
5-16 3% 7-16 1/2 9-16 5%	31 36 41 46 51 56	G 14%	15 15 <sup>1</sup> /8	19½ 19¼ 19¼ 1988 19 7-16 19½ 1958	24.8 28.8 32.8 36.8 40.8 44.8	82.6 96. 109.3 122.6 136. 149.3	5.45 5.50 5.55 5.59 5.63 5.68	164.87 191.54 218.25 244.95 271.69 298.45

One Se	egment.	Diame	eters in	inches.	Oı	n.	Safe	
Thickness in inches.	Weight in lbs. per yard.	d inside.	D Outside.	Di Over Flanges.	Area of Cross- Section, sq. inches.	Weight per ft. in pounds.	Least Radius of Gyration, in inches.	Load in net tons for 16-feet Lengths,
11-16 34 13-16 7/8 1 11/8 11/4 13/8	61 66 71 76 86 96 106 116	.G 143%	1534 1578 16 1616 1636 1636 1658 1676 1718	1934 1978 20 2016 2036 2036 2034 2034 21	48.8 52.8 56.8 60.8 68.8 76.8 84.8 92.8	162.6 176. 189.3 202.6 229.3 256. 282.6 309.3	5.72 5.77 5.82 5.87 5.95 6.04 6.14 6.23	325.21 352.02 378.85 405.70 464.38 513.17 567.06 620.98

Working Formulæ for Wrought-iron and Steel Struts of various Forms. -Burr gives the following practical formulæ, which

he believes to possess advantages over	r Gordon's:			
Kind of Strut,	p = Ultimate Strength, lbs. per sq. in, of Section.	$p_1$ = Working Strength = 1/5 Ultimate, lbs. per sq. in. of Section.		
Flat and fixed end iron angles and tees	$344000-140 \frac{l}{r}$ (1)	$8800 - 28 \frac{l}{r}$ (2)		
Hinged-end iron angles and tees	$.46000 - 175 \frac{l}{r}$ (3)	$9200 - 35 \frac{l}{r}$ (4)		
Flat-end iron channels and I beams	.40000—110 $\frac{l}{r}$ (5)	$8000 - 22 \frac{l}{r}$ (6)		
Flat-end mild-steel angles	$.52000 - 180 \frac{l}{r}$ (7)	$10400 - 36 \frac{l}{r}$ (8)		
Flat-end high-steel angles				
Pin-end solid wrought iron columns	$.32000 - 80 \frac{l}{r} \bigg _{(11)}$	$6400-16\frac{l}{r}$ (12)		
	/			
Equations (1) to (4) are to be used o	only between $\frac{l}{r} = 4$			
" (5) and (6) " " " " " " " " " " " " " " " " " " "	" " = 21 " " = 41	0 " " = 200 0 " " = 200 0 " " = 200		
(11) and (12) " " " "	or $\frac{l}{d} = 0$	$0  \text{``}  = 200$ $0  \text{and}  \frac{l}{d} = 65$		

Steel columns, properly made, of steel ranging in specimens from 65,000 to 73,000 lbs. per square inch should give a resistance 25 to 33 per cent in excess of that of wrought-iron columns with the same value of  $l+\tau$ , provided that ratio does not exceed 140.

The unsupported width of a plate in a compression member should not exceed 30 thines its thickness.

In built columns the transverse distance between centre lines of rivets securing plates to angles or channels, etc., should not exceed 35 times the plate thickness. If this width is exceeded, longitudinal buckling of the plate takes place, and the column ceases to fail as a whole, but yields in detail.

The same tests show that the thickness of the leg of an angle to which latticing is riveted should not be less than 1/9 of the length of that leg or side if the column is purely and wholly a compression member. The above limit may be passed somewhat in stiff ties and compression members designed to carry transverse loads.

The panel points of latticing should not be separated by a greater distance than 60 times the thickness of the angle-leg to which the latticing is riveted.

if the column is wholly a compression member.

The rivet pitch should never exceed 16 times the thickness of the thinnest metal pierced by the rivet, and if the plates are very thick it should never nearly equal that value.

Merriman's Rational Formula for Columns (Eng. News, July 19, 1894).

 $C = \frac{B}{1 - \frac{nB}{\pi^2 E} \frac{l^2}{r^2}}.$ 

$$B = \frac{C}{1 + \frac{nC}{\pi^2 E} \frac{l^2}{r^2}}.$$
 (2)

B = unit-load on the column = total load P + area of cross-section A; C = maximum compressive unit-stress on the concave side of the column; l = length of the column; r = least radius of gyration of the cross-section; E = coefficient of elasticity of the material; n = 1 for both ends round; n = 4/9 for one end round and one fixed;  $n = \frac{1}{4}$  for both ends fixed. This formula is for use with strains within the elastic limit only: it does not hold good when the strain C exceeds the elastic limit. Prof. Merriman takes the mean value of E for timber = 1,500,000, for cast

iron = 15,000,000, for wrought-iron = 25,000,000, and for steel = 30,000,000,

putes the following tables from formula (1):

### I .- Wrought-iron Columns with Round Ends.

Unit-		Maximum Compressive Unit-stress C.											
load.		M	aximum	Compre	ssive Un	it-stress	C.						
$\frac{P}{A}$ or B.	1 00	1 40	1 _ 60	1 _ 00	l _ 100	l 100	1 _ 140	1 _ 100					
$\overline{A}$ or $B$ .	$\frac{1}{r} = 20$	$\frac{1}{r} = 40$	r = 00	$\frac{-}{r}$	$\frac{1}{r}$	r - 120	r - 140	$\frac{1}{r}$ - 100					
5,000	5.040	5.170	5,390	5,730	6,250	6,980	8,220	10.250					
6,000	6,055	6,240	6,560	7,090	7,890	9,090	11,330	15,560					
7,000	7,080	7,330	7,780	8,530	9,720	11,610	15,510	24,720					
8,000	8,100	8,430	9,040	10,060	11,660	14,640	21,460						
9,000	9,130	9,550	10,340	11,690	14,060	18,380							
10,000	10,160	10,680	11,680	13,440	16,670	23,090							
11,000	11.200	11,750	13,070	15,310	19,640								
12,000	12,240	13,000	14,500	17,320	23,080								
13,000	13,280	14,180	15,990	19,480									

### II .- Wrought-iron Columns with Fixed Ends.

Unit- load.	'	Maximum Compressive Unit-stress $\it C$ .											
$\frac{P}{A}$ or $B$ .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$					
6,000	6,010	6,060	6,130	6,240	6,380	6,570	6,800	7,090					
7,000	7,020	7,080	7,180	7,330	7,530	7,780	8,110	8,530					
8,000	8,025	8,100	8,240	8,430	8,700	9,040	9,490	10,060					
9,000	9,030	9,130	9,300	9,550	9,890	10,340	10,930	11,690					
10,000	10,040	10,160	10,370	10,710	11,110	11,680	12,440	13,440					
11,000	11,050	11,200	11,450	11,830	12,360	13,070	14,020	15,310					
12,000	12,060	12,240	12,540	13,000	13,640	14,510	15,690	17,320					
13,000	13,070	13,280	13,640	14,210	14,940	15,990	17,440	19,480					
14,000	14,080	14,320	14,740	15,380	16,280	17,530	19,290	21,820					

### III .- Steel Columns with Round Ends.

Unit- load.		Ma	aximum	Compre	ssive Un	it-stress	C.,	
$\frac{P}{A}$ or $B$ .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$
6,000 7,000 8,000 9,000 10,000 11,000 12,000 13,000 14,000	6,050 7,070 8,090 9,110 10,130 11,160 12,200 13,330 14,250	6,200 7,270 8,380 9,450 10,560 11,690 12,820 13,970 15,130	6,470 7,650 8,770 10,090 11,360 12,670 14,020 15,400 16,830	6,880 8,230 9,650 11,140 12,710 14,370 16,130 18,000 19,960	7,500 9,130 10,870 12,850 15,000 17,370 20,000 22,940 26,250	8,430 10,540 12,990 15.850 19,230 23,300 28,300	9,870 12,900 16,760 20,930 28,850	12,300 17,400 24,590

### IV .- Steel Columns with Fixed Ends.

		Secon	COLUM			Ott Mark		
Unit- load.		М	aximum	Compre	ssive Un	it-stress	C.	
$\frac{P}{A}$ or $B$ .	$\frac{l}{r} = 20$	$\frac{l}{r} = 40$	$\frac{l}{r} = 60$	$\frac{l}{r} = 80$	$\frac{l}{r} = 100$	$\frac{l}{r} = 120$	$\frac{l}{r} = 140$	$\frac{l}{r} = 160$
7,000 8,000 9,000 10,000 11,000 12,000 13,000 14,000	7,020 8,020 9,030 10,030 11,040 12,050 13,060 14,070 15,080	7,070 8,090 9,110 10,130 11,160 12,200 13,230 14,250 15,310	7,150 8,200 9,250 10,310 11,380 12,450 13,530 14,610 15,710	7,270 8,380 9,450 10,560 11,690 12,820 13,970 15,130 16,310	7,430 8,570 9,730 10,910 12,110 13,330 14,580 15,850 17,140	7,650 8,770 10,090 11,360 12,670 14,020 15,400 16,830 18,290	7,900 9,200 10,550 11,810 13,410 14,930 16,500 18,150 19,870	8,230 9,650 11,140 12,710 14,370 16,130 17,990 19,960 22,060

The design of the cross-section of a column to carry a given load with maximum unit-stress C may be made by assuming dimensions, and then

computing C by formula (1). If the agreement between the specified and computed values is not sufficiently close, new dimensions must be chosen, and the computation be repeated. By the use of the above tables the work will be shortened.

The formula (1) may be put in another form which in some cases will abbreviate the numerical work. For B substitute its value  $P \rightarrow A$ , and for  $Ar^2$  write I, the least moment of inertia of the cross-section; then

$$I - \frac{P}{C}r^2 = \frac{nPl^2}{\pi^2 E}, \qquad (3)$$

in which I and r2 are to be determined.

In which I and  $I^*$  are to be determined. For example, let it be required to find the size of a square oak column with fixed ends when loaded with 24,000 lbs, and 16 ft. long, so that the maximum compressive stress C shall be 1000 lbs. per square inch. Here  $I=24,000,\ C=1000,\ n=\frac{1}{4},\ \pi^2=10,\ E=1,500,000,\ l=16\times12,\ \text{and}$  (3) becomes

$$I - 24r^2 = 14.75$$
.

Now let x be the side of the square; then

$$I = \frac{x^4}{12}$$
 and  $r^2 = \frac{x^2}{12}$ ,

so that the equation reduces to  $x^4 - 24x^2 = 177$ , from which  $x^2$  is found to be 29.92 sq. in., and the side x = 5.47 in. Thus the unit-load B is about 802 lbs. per square inch.

### WORKING STRAINS ALLOWED IN BRIDGE MEMBERS.

Theodore Cooper gives the following in his Bridge Specifications: Compression members shall be so proportioned that the maximum load shall in no case cause a greater strain than that determined by the following formula :

g formula ; 
$$P = \frac{8000}{1 + \frac{l^2}{40,000r^2}}$$
for square-end compression members ;

$$P = \frac{8000}{1 + \frac{l^2}{30,000r^2}}$$
for compression members with one pin and one square end;

$$P = \frac{8000}{1.1 + \frac{l^2}{l^2}}$$
 for compression members with pin-bearings;

(These values may be increased in bridges over 150 ft, span. See Cooper's Specifications.)

P = the allowed compression per square inch of cross-section:

l =the length of compression member, in inches;

r= the least radius of gyration of the section in inches. No compression member, however, shall have a length exceeding 45 times

its least width. The Phœnix Bridge Company give the following:

The greatest working stresses in wrought-iron compression members of spans 150 feet in length and under shall be the following:

80

Upper chords shall be proportioned by the flat-end formula.

A mean between flat-end and pin-end results shall be used for one pin end and one flat end.

Lateral and transverse struts shall be designed by taking working stresses equal to one and four tenths those given by the preceding formulæ.

### Working Stresses allowed in Bridge Tension Members.

(Theodore Cooper's Specifications.)

All parts of the structure shall be so proportioned that the maximum loads shall in uo case cause a greater tension than the following (except in spans exceeding 150 feet):

Pou	nds per
· s	q. in.
On lateral bracing	15,000
On solid rolled beams, used as cross floor-beams and stringers.	9,000
On bottom chords and main diagonals (forged eve-bars)	10,000
On bottom chords and main diagonals (plates or shapes), net	
section	8,000
On counter rods and long verticals (forged eye-bars)	8,000
On counter and long verticals (plates or shapes), net section	6,500
On bottom flange of riveted cross-girders, net section	8,000
On bottom flange of riveted longitudinal plate girders over	-,
20 ft. long, net section	8,000
On bottom flange of riveted longitudinal plate girders under	0,000
20 ft. long, net section	7,000
On floor-beam hangers, and other similar members liable to	*,000
sudden loading (bar iron with forged ends)	6,000
On floor beam hangers, and other similar members liable to	0,000
sudden loading (plates or shapes), net section	5,000
squaen loading (places of snapes), her section	5,000
No	1 11 1

Members subject to alternate strains of tension and compression shall be proportioned to resist each kind of strain. Both of the strains shall, however, be considered as increased by an amount equal to 8/10 of the least of the two strains, for determining the sectional area by the above allowed strains.

The Phoenix Bridge Company specify: The greatest working stresses in all wrought-iron tensile members of railway spans 150 feet in length and under shall be as follows:

	Pounds per
	sq. in.
In counter web members	
In long verticals	
In main-web and lower-chord members (eye-bars)	10,000
In suspension loops	7.000
In suspension loops	7,000
In suspension plates (net section)	7,000
In tension members of lateral and transverse bracing	
In counter rods and long verticals of lattice girders (net se	
tiou)	
In lower chords and main tension members of lattice girds	rs
(net section)	8,000
In bottom flange of plate girders (net section)	
In bottom flange of rolled beams	8.000
In angle-iron lateral ties (net section)	19,000
In angio-iron tacciar cros (nec section)	12,000

In spans over 150 feet in length, the greatest working tensile stresses per square inch of wrought iron, lower-chord and end main-web eye-bars, shall ba

$$8000 \left(1 + 0.9 \times \frac{\text{min. total stress}}{\text{max. total stress}}\right)$$

whenever this quantity exceeds 10,000.

### Working Stresses for Steel.

The greatest allowed working stresses for steel tension members, for spans of 200 feet in length and less, shall be as follows:

Po	ounds pe
	sq. in.
In counter web members	
In long verticals	10,000
In all main-web and lower-chord eye-bars	13,200
In plate hangers (net section)	9,000
In tension members of lateral and transverse bracing	
In steel-angle lateral ties (net section)	15,000

For spans over 200 feet in length the greatest allowed working stresses per square inch, in lower-chord and end main-web eye-bars, shall be taken at

$$10,\!000 \Big(1 \!+\! \frac{\mathrm{min.\ total\ stress}}{\mathrm{max.\ total\ stress}}\Big)$$

whenever this quantity exceeds 13,200.

The greatest allowable stress in the main-web eye-bars nearest the centre of such spans shall be taken at 13,200 pounds per square inch; and those for the intermediate eye-bars shall be found by direct interpolation between

the preceding values.

The greatest allowable working stresses in steel plate and lattice girders

and rolled heams shall be taken as follows:

	Pounds per
	sq. in.
Upper flange of plate girders (gross section)	10,000
Lower flange of plate girders (net section)	10,000
In counters and long verticals of lattice girders (net section	1) 9,000
In lower chords and main diagonals of lattice girders (	net
section)	10,000
In bottom flanges of rolled beams	10,000
In top flanges of rolled beams	10,000
	,
DESIGNATE OF HOLLOW CVILINDED	S TO

### RESISTANCE OF HOLLOW CYLINDERS TO COLLAPSE,

Fairbairn's empirical formula (Phil. Trans. 1858) is

$$p = 9,675,600 \frac{t^{2\cdot 19}}{ld}, \dots \dots \dots \dots$$

where p = pressure in lbs. per square inch, t = thickness of cylinder, d = diameter, and l = length, all in inches; or,

$$p = 806,600 \frac{t^{2\cdot 19}}{Ld}$$
, if L is in feet. . . . . . (2)

He recommends the simpler formula

as sufficiently accurate for practical purposes, for tubes of considerable diameter and length.

The diameters of Fairbairn's experimental tubes were 4", 6", 8", 10", and 12", and their lengths, between the cast-iron ends, ranged between 19 inches and 60 inches.

His formula (3) has been generally accepted as the basis of rules for ascertaining the strength of boiler-flues. In some cases, however, limits are fixed to its application by a supplementary formula.

Lloyd's Register contains the following formula for the strength of circular

boiler-flues, viz.,

The English Board of Trade prescribes the following formula for circular flues, when the longitudinal joints are welded, or made with riveted buttstraps, viz.,

$$P = \frac{90,000t^2}{(L+1)d}.$$
 (6)

For lap-joints and for inferior workmanship the numerical factor may be reduced as low as 60,000,

The rules of Lloyd's Register, as well as those of the Board of Trade, prescribe further, that in no case the value of P must exceed the amount given by the following equation, viz.,

In formulæ (4), (5), (6) P is the highest working pressure in pounds per square inch, t and d are the thickness and diameter in inches, L is the length of the flue in feet measured between the strengthening rings, in case it is fitted with such. Formula (4) is the same as formula (3), with a factor of safety of 9. In formula (5) the length L is increased by 1; the influence which this addition has on the value of P is, of course, greater for short tubes than for long ones.

Nystrom has deduced from Fairbairn's experiments the following formula for the collapsing strength of flues :

$$p = \frac{4Tt^2}{d\sqrt[4]{L}}, \quad \dots \qquad \dots \qquad \dots$$
 (7)

where p,t, and d have the same meaning as in formula (1), L is the length in feet, and T is the tensile strength of the metal in pounds per square inch. If we assign to T the value 50.000, and express the length of the flue in inches, equation (7) assumes the following form, viz.,

$$p = 692,800 \frac{t^2}{d\sqrt{l}}$$
 . . . . . . . . . . . (8)

Nystrom considers a factor of safety of 4 sufficient in applying his formula. (See ' A New Treatise on Steam Engineering," by J. W. Nystrom, p. 100.) Formula (1), (4), and (8) have the common defect that they make the

collapsing pressure decrease indefinitely with increase of length, and vice versa. M. Love has deduced from Fairbairn's experiments an equation of a different form, which, reduced to English measures, is as follows, viz.,

$$p = 5,358,150 \frac{t^2}{id} + 41,906 \frac{t^2}{d} + 1323 \frac{t}{d}, \dots$$
 (9)

where the notation is the same as in formula (1).

D. K. Clark, in his "Manual of Rules," etc., p. 696, gives the dimensions of D. K. Clark, in fis "manual or Rules," etc., p. 696, gives the dimensions of six flues, selected from the reports of the Manchester Steam-Users Association, 1862-69, which collapsed while in actual use in boilers. These flues varied from 24 to 60 inches in diameter, and from 3-16 to 3/2 inch in thickness. They consisted of rings of plates riveted together, with one or two longitudial seams, but all of them unfortified by intermediate flanges or strengthening rings. At the collapsing pressures the flues experienced compressions ranging from 1.53 to 2.17 tons, or a mean compression of 1.82 tons per square inch of the section. From these data Clark deduced the following formula "for the section. From these data Clark deduced the following formula "for the section." viz.,

where p is the collapsing pressure in pounds per square inch, and d and t are the diameter and thickness expressed in inches. C. R. Roelker, in Van Nostrand's Magazine, March, 1881, discussing the above and other formule, shows that experimental data are as yet insufficient to determine the value of any of the formule. He says that Nystrom's formula, (8), gives a closer agreement of the calculated with the actual collapsing pressures in experiments on these of every description than any of the other formulæ.

### Collapsing Pressure of Plain Iron Tubes or Flues.

(Clark, S. E., vol. i, p. 643.)

The resistance to collapse of plain-riveted flues is directly as the square of the thickness of the plate, and inversely as the square of the diameter. The support of the two ends of the flue does not practically extend over a length of tube greater than twice or three times the diameter. The collapsing pressure of long tubes is therefore practically independent of the length.

Instances of collapsed flues of Cornish and Lancashire boilers collated by Clark, showed that the resistance to collapse of flues of \$\frac{3}{2}\$ finch plates, 18 to 48 feet long, and 30 to 50 inches diameter, varied as the 1.75 power of the diameter. Thus,

For collapsing pressures of plain iron flue-tubes of Cornish and Lanca-shire steam-boilers, Clark gives:

$$P = \frac{200,000t^2}{d^{1.75}}$$
.

P = collapsing pressure, in pounds per square inch;

t = thickness of the plates of the furnace tube, in inches.

d = internal diameter of the furnace tube, in inches.

For short lengths the longitudinal tensile resistance may be effective in augmenting the resistance to collapse. Flues efficiently fortified by flangejoints or hoops at intervals of 3 feet may be enabled to resist from 50 lbs. to 60 lbs. or 70 lbs. pressure per square inch more than plain tubes, accord-

io 60 lbs. or 70 lbs. pressure per square inch more than plain tubes, according to the thickness of the plates.

Strength of Small Tubes.—The collapsing resistance of solid-drawn tubes of small diameter, and from 134 inch to .109 inch in thickness, has been tested experimentally by Messrs. J. Russell & Sons. The results for wrought-iron tubes varied from 14.33 to 20.07 tons per square-inch section of the metal, averaging 18.20 tons, as against 17.57 to 24.28 tons, averaging 22.40 tons, for the bursting pressure.

(For strength of Segmental Crowns of Furnaces and Cylinders see Clark, S. E., vol. i, pp. 649-651 and pp. 627, 628.)

Formula for Corrugated Furnaces (Eng'g, July 24, 1891, p. 102).—As the result of a series of experiments on the resistance to collapse of Fox's corrugated furnaces, the Board of Trade and Lloyd's Registry altered their formulae for these furnaces in 1891 as follows:
Board of Trade formula is altered from

Board of Trade formula is altered from

$$\frac{12,500 \times T}{D} = WP \text{ to } \frac{14,000 \times T}{D} = WP.$$

T =thickness in inches; D =mean diameter of furnace;

WP = working pressure in pounds per square inch. Lloyd's formula is altered from

$$\frac{1000 \times (T^2)}{D} = WP \text{ to } \frac{1234 \times (T^2)}{D} = WP.$$

T = thickness in sixteenths of an inch:

D =greatest diameter of furnace;

WP = working pressure in pounds per square inch.

### TRANSVERSE STRENGTH.

In transverse tests the strength of bars of rectangular section is found to vary directly as the breadth of the specimen tested, as the square of its depth, and inversely as its length. The deflection under any load varies as the cube of the length, and inversely as the breadth and as the cube of the depth. Represented algebraically, if S =the strength and D the deflection, l the length, b the breadth, and d the depth.

S varies as 
$$\frac{bd^2}{l}$$
 and D varies as  $\frac{l^3}{bd^3}$ .

For the purpose of reducing the strength of pieces of various sizes to a common standard, the term modulus of rupture (represented by R) is used. Its value is obtained by experiment on a bar of rectangular section supported at the ends and loaded in the middle and substituting numerical values in the following formula:

$$R = \frac{3}{2} \frac{Pl}{bd^2},$$

in which P = the breaking load in pounds, l = the length in inches, b the breadth, and d the depth,

The modulus of rupture is sometimes defined as the strain at the instant of rupture upon a unit of the section which is most remote from the neutral axis on the side which first ruptures. This definition, however, is based upon a theory which is yet in dispute among authorities, and it is better to define it as a numerical value, or experimental constant, found by the ap-

plication of the formula above given. From the above formula, making l 12 inches, and b and d each 1 inch, it follows that the modulus of rupture is 18 times the load required to break a bar one inch square, supported at two points one foot apart, the load being

applied in the middle,

Coefficient of transverse strength =  $\frac{\text{span in feet} \times \text{load at middle in lbs.}}{\text{breadth in inches} \times (\text{depth in inches})^2}$ .

=  $\frac{1}{18}$ th of the modulus of rupture.

### Fundamental Formulæ for Flexure of Beams (Merriman), Resisting shear = vertical shear;

Resisting moment = bending moment;

Sum of tensile stresses = sum of compressive stresses;

Resisting shear = algebraic sum of all the vertical components of the in-

ternal stresses at any section of the beam.

If A be the area of the section and  $S_s$  the shearing unit stress, then resist-

ing shear =  $AS_8$ ; and if the vertical shear = V, then  $V = AS_8$ .

The vertical shear is the algebraic sum of all the external vertical forces

on one side of the section considered. It is equal to the reaction of one support, considered as a force acting upward, minus the sum of all the vertical

downward forces acting between the support and the section.

The resisting moment = algebraic sum of all the moments of the internal horizontal stresses at any section with reference to a point in that section, =  $\frac{SI}{c}$ , in which S = the horizontal unit stress, tensile or compressive

as the case may be, upon the fibre most remote from the neutral axis, c =the shortest distance from that fibre to said axis, and I = the moment of

inertia of the cross-section with reference to that axis.

The bending moment M is the algebraic sum of the moment of the external forces on one side of the section with reference to a point in that section = moment of the reaction of one support minus sum of moments of loads between the support and the section considered.

$$M = \frac{SI}{c}$$

The bending moment is a compound quantity = product of a force by the distance of its point of application from the section considered, the distance being measured on a line drawn from the section perpendicular to the

direction of the action of the force.

Concerning the above formula, Prof. Merriman, Eng. News, July 21, 1894, says: The formula just quoted is true when the unit stress S on the part of the beam farthest from the neutral axis is within the elastic limit of the material. It is not true when this limit is exceeded, because then the neutral axis does not pass through the centre of gravity of the cross-section, and because also the different longitudinal stresses are not proportional to their distances from that axis, these two requirements being involved in the deduction of the formula. But in all cases of design the permissible unitstresses should not exceed the elastic limit, and hence the formula applies rationally, without regarding the ultimate strength of the material or any of the circumstances regarding rupture. Indeed so great reliance is placed upon this formula that the practice of testing beams by rupture has been almost entirely abandoned, and the allowable unit-stresses are mainly derived from tensile and compressive tests.

# GENERAL FORMULE FOR TRANSVERSE STRENGTH OF BEAMS OF UNIFORM CROSS-SECTION.

Formulæ for Transverse Strength of Beams.-Referring to table on preceding page,

P = load at middle W= total load, distributed uniformly;

l = length, b = breadth, d = depth, in inches:

E = modulus of elasticity:

R = modulus of rupture, or stress per square inch of extreme fibre:

I = moment of inertia;

c = distance between neutral axis and extreme fibre.

For breaking load of circular section, replace  $bd^2$  by  $0.59d^3$ . For good wrought iron the value of R is about 80,000, for steel about 120,000. the percentage of carbon apparently having no influence. (Thurston, Iron and Steel, p. 491).

For east iron the value of R varies greatly according to quality. Thurston

found 45,740 and 67,980 in No. 2 and No. 4 cast iron, respectively.

For beams fixed at both ends and loaded in the middle, Barlow, by experiment, found the maximum moment of stress = 1/6/P instead of ½P, the result given by theory. Prof. Wood (Resist. Matls. p. 155) says of this case: The phenomena are of too complex a character to admit of a through and exact analysis, and it is probably safer to accept the results of Mr. Barlow in practice than to depend upon theoretical results.

### APPROXIMATE GREATEST SAFE LOADS IN LBS. ON STEEL BEAMS. (Pencoyd Iron Works.)

Based on fibre strains of 16.800 lbs, for steel, (For iron the loads should be one sixth less, corresponding to a fibre strain of 14,000 lbs, per square inch). L =length in feet between supports; a = interior area in square

A =sectional area of beam in square

inches: d = interior depth in inches.

inches; D = depth of beam in inches.

w = working load in net tons.

Shape of	Greatest Safe	Load in Pounds	Deflection in Inches.						
Section.	Load in Middle.	Load Distributed.	Load in Middle.	Load Distributed.					
Solid Rect- angle.	940AD L	1880AD L	$\frac{wL^3}{32AD^2}$	$\frac{wL^3}{52AD^2}$					
Hollow Rect- angle.	$\frac{940(AD-ad)}{L}$	1880(AD-ad) L	$\frac{wL^3}{32(AD^2-ad^2)}$	$\frac{wL^3}{52(AD^2-ad^2)}$					
Solid Cylin- der.	$\frac{700AD}{L}$	1400AD	$\frac{wL^3}{24AD^2}$	$\frac{wL^3}{38AD^2}$					
Hollow Cylinder.	700(AD-ad) L	$\frac{1400(AD-ad)}{L}$	$\frac{wL^3}{24(AD^2-ad^2)}$	$\frac{wL^{3}}{38(AD^{2}-ad^{2})}$					
Even-legged Angle or Tee.	$\frac{930AD}{L}$	1860AD L	$\frac{wL^3}{32AD^2}$	$rac{wL^3}{52AD^2}$					
Channel or Z bar.	$\frac{1600AD}{L}$	$\frac{3200AD}{L}$	$\frac{wL^3}{58AD^2}$	$\frac{wL^3}{85AD^2}$					
Deck Beam.	1450AD L	2900AD L	$\frac{wL^3}{50AD^2}$	$\frac{wL^3}{80AD^2}$					
I Beam.	1780AD L	$\frac{3560AD}{L}$	$\frac{wL^3}{58AD^2}$	$\frac{wL^{3}}{93AD^{2}}$					
I	II	III	IV	v					

The above formulæ for the strength and stiffness of rolled beams of various sections are intended for convenient application in cases where strict accuracy is not required.

The rules for rectangular and circular sections are correct, while those for the flanged sections are approximate, and limited in their application to the standard shapes as given in the Pencoyd tables. When the section of any beam is increased above the standard minimum dimensions, the flanges remaining unaltered, and the web alone being thickened, the tendency will be for the load as found by the rules to be in excess of the actual; but within the limits that it is possible to vary any section in the rolling, the rules will apply without any serious inaccuracy.

The calculated safe loads will be approximately one half of loads that

would injure the elasticity of the materials.

The rules for deflection apply to any load below the elastic limit, or less than double the greatest safe load by the rules.
If the beams are long without lateral support, reduce the loads for the

ratios of width to span as follows: Duonoution of Coloulated T

	Lengt	h of B	eam.		Greatest Sa		
20	times	flange	width.	Whole	calculated	load.	
30	"	"	**	9-10	**	44	
40	44	44	44	8-10	4.6	64	
50	64	66	66	7-10	66	66	
60		4.4	44	6-10	66	**	
70	44	66	64	5_10	44	66	

These rules apply to beams supported at each end. For beams supported otherwise, alter the coefficients of the table as described below, referring to the respective columns indicated by number.

### Changes of Coefficients for Special Forms of Beams.

Kind of Beam.	Coefficient for Safe Load.	Coefficient for Deflection.
Fixed at one end, loaded at the other.	One fourth of the coeffi- cient, col. II.	One sixteenth of the coefficient of col. IV.
Fixed at one end, load evenly distributed.	One fourth of the coeffi- cient of col. III.	Five forty-eighths of the coefficient of col. V.
Both ends rigidly fixed, or a continuous beam, with a load in middle.	Twice the coefficient of col. II.	Four times the coeffi- cient of col. IV.
Both ends rigidly fixed, or a continuous beam, with load evenly dis- tributed.	One and one-half times the coefficient of col. III.	Five times the coefficient of col. V.

### ELASTIC RESILIENCE.

In a rectangular beam tested by transverse stress, supported at the ends and loaded in the middle,

$$P = \frac{2}{3} \frac{Rbd^2}{l};$$
  
$$\Delta = \frac{1}{4} \frac{Pl^3}{Ebd^3};$$

in which, if P is the load in pounds at the elastic limit, R = the modulus of transverse strength, or the strain on the extreme fibre, at the elastic limit, E = modulus of elasticity,  $\Delta = \text{deflection}$ , l, b, and d = length, breadth, and depth in inches. Substituting for P in (2) its value in (1), we have

$$\Delta = \frac{1}{6} \, \frac{Rl^2}{Ed}.$$

The elastic resilience = half the product of the load and deflection =  $\frac{1}{2}P\Delta$ , and the elastic resilience per cubic inch

$$=\frac{1}{2}\frac{P\Delta}{lbd}$$

Substituting the values of P and  $\Delta$ , this reduces to elastic resilience per cubic inch =  $\frac{1}{18}\frac{R^2}{E}$ , which is independent of the dimensions; and therefore

the elastic resilience per cubic inch for transverse strain may be used as a modulus expressing one valuable quality of a material.

Similarly for tension:

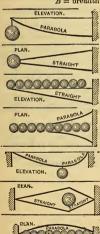
Let P = tensile stress in pounds per square inch at the elastic limit;

e= elongation per unit of length at the elastic limit; E= modulus of elasticity = P+e; whence e=P+E.

Then elastic resilience per cubic inch =  $\frac{1}{2}Pe = \frac{1}{2}\frac{P^2}{E}$ .

### BEAMS OF UNIFORM STRENGTH THROUGHOUT THEIR LENGTH.

The section is supposed in all cases to be rectangular throughout. The beams shown in plan are of uniform depth throughout. Those shown in elevation are of uniform breadth throughout. B = b readth of beam. D = d enth of beam.



ELEVATION.

Fixed at one end, loaded at the other; curve parabola, vertex at loaded end; BD<sup>2</sup> proportional to distance from loaded end. The beam may be reversed, so that the upper edge is parabolic, or both edges may be parabolic.

Fixed at one end, loaded at the other; triangle, apex at loaded end;  $BD^2$  proportional to the distance from the loaded end.

Fixed at one end; load distributed; triangle, apex at unsupported end;  $BD^2$  proportional to square of distance from unsupported end.

Fixed at one end; load distributed; curves two parabolas, vertices touching each other at unsupported end;  $BD^2$  proportional to distance from unsupported end.

Supported at both ends; load at any one point; two parabolas, vertices at the points of support, bases at point loaded; \$B^p proportional to distance from nearest point of support. The upper edge or both edges may also be parabolic.

Supported at both ends; load at any one point; two triangles, apices at points of support, bases at point loaded;  $BD^2$  proportional to distance from the nearest point of support.

Supported at both ends; load distributed; curves two parabolas, vertices at the middle of the beam; bases centre line of beam;  $BD^2$  proportional to product of distances from points of support.

Supported at both ends; load distributed; curve semi-ellipse;  $BD^2$  proportional to the product of the distances from the points of support.

### PROPERTIES OF ROLLED STRUCTURAL SHAPES. Explanation of Tables of the Properties of Carnegie I Beams, Channels, and Z Bars.

The tables of I beams are calculated for the minimum weight to which each pattern can be rolled. The tables of channels are calculated for the minimum and maximum weights of the various shapes, while the properties

of Z bars are given for thicknesses differing by 1/16 inch. Columns 11 and 13, in the tables for I beams and channels, give coefficients Columns 11 and 15, in the tables for 10 beams and channels, give coemicients by the help of which the safe uniformly-distributed load may readily be determined. To do this, divide the coefficient given by the span or distance between supports in feet. If the weight of the section is intermediate between the minimum and maximum weights given, add to the coefficient for the minimum weight the value given in columns 12 or 14 (for one pound increase of weight), multiplied by the number of pounds the section is

heavier than the minimum. If a section is to be selected (as will usually be the case) intended to carry a certain load, for a length of span already determined on, ascertain the coefficient which this load and span will require, and refer to the table for a section having a coefficient of this value. The coefficient is obtained by multiplying the load, in pounds uniformly distributed, by the span

length in feet. In case the load is not uniformly distributed, but is concentrated at the middle of the span, multiply the load by 2 and then consider it as uniformly distributed. The deflection will be 8/10 of the deflection for the latter load.

For other cases of loading obtain the bending moment in foot-pounds; this

multiplied by 8 will give the coefficient required.

If the loads are quiescent, the coefficients for a fibre strain of 16,000 lbs. If the loads are quiescent, the coefficients for a fibre strain of 16,000 lbs, per square inch for steel and 12,000 lbs, for iron may be used; but, if moving loads are to be provided for, the coefficients for 12,500 and 10,000 lbs, respectively, should be taken. Inasmuch as the effects of impact may be very considerable (the strains produced in an unyielding, inelastic material by a load suddenly applied being double those produced by the same load in a quiescent state), it will sometimes be advisable to use still smaller fibre strains than those given in the tables. In such cases the coefficients can readily be determined by proportion. Thus, for a fiber strain the strains that the second control of the strains of the strains that the second control of the strains of the strains that the second control of the strains o 10.000 lbs. fibre strain, from the table, multiplied by 8/10.

The moments of resistance given in column 9 are used to determine the fibre strain per square inch in a beam, or other shape, subjected to bending or transverse strains, by dividing the same into the bending moment

expressed in inch-pounds,
For Carnegie Z bars, complete tables of moments of inertia, moments of resistance, radii of gyration, and values of the coefficients (O) are given for thicknesses varying by 1/16 inch. These coefficients may be applied, as explained above, for cases where the Z bars are subjected to transverse loading, as, for example, in the case of roof-purlins.

For more complete and detailed information concerning structural shapes. consult the pocket-books and circulars issued by the manufacturers.

## Spacing of Carnegie I Beams for Uniform Load of 100 lbs. per square foot.

Proper Distance in Feet, Centre to Centre of Beams.

1101.	ERTIES	OF I	COLL	ı Eı L	ומ	. 11		TUI	LAL	1 3	HA.	PER	5.
l ii	77% Ibs.	8.7. 6.4.	3.9	3.1	જાં જાં	1.9	1.6		1.0		:	: :	to 100.
4	10 1bs.	16.5 11.4 8.4	5.1	4.1	4.0	2.4	2.1		4.00	H.	1.0	1	s to
H	10 1bs.	2.45	6.5	5.3	4.8	8.1	65	လွ်င		Η.			square foot bears
2,,	13 1bs.	26.8 18.6 13.7	8.3	6.7	5.5	4.0	3.4	60.0	00.00	÷.		1.4	foot
H	13 lbs.	33.4 28.2 17.0	13.0 10.3	8.4	6.9	4.9	4.3	တ်တ	000	CS.	cs.	1.7	nare
6,4	16 lbs.	28.3 28.3 7.8 8.8	15.9 12.6	10.2	7.1	6.0	5.5	यं र		σś	os o	5. CS	ber so
7" I.	15½ 1bs.	28.2 2.0	18.4 14.5	11.8	00		6.0	70.∠	4.00	က်	000	3.03	ad pe
ž-	20 1bs.	60.6 42.1 30.9	18.7	15.1	12.5	9.0	2-	6,10	10.4	ず	90.0	3.1	he given load pe
H	18 1bs.	61.6 42.8 31.4	24.1 19.0	15.4	12.7 10.7	9.1	6.	6.6	10.4 00.00	4	00.0	0 cs	give
, 8	lbs.	76.6 53.2 39.1	29.9 23.7	19.2	15.8	11.3	9.8		9.0		8.4	20.4	the
-9d 9c -quS	Distand tween ports in	2002	တ. ဇာ	10	#2	13	14	10 2	222	19	50	2 SS	e ratio the
	lbs.	13.9 11.8 10.2	8.7	6.9	5.5	5.0	4.5	4.1	0,00,00 0,10,00	3.0	2.3	0.60	2 2
12" I. 10" I. 9" I. 9" I. 9" I. 9" I. 9" I. 9" II. 9" III. 9" II. 9" III	27 lbs.	18.2	11.7	9.1	7.3	9.9	5.9	4.4	944	3.9		0000	ο . Σ
10" I.	251/s 10s.	18.8 15.6 13.5	11.7	9.1	67.3	9.9	6.0		44		3.6	4.00	ج   غ
10′	33 Ibs.	23.9 20.4 17.6	15.3	11.9	9.6	8.6	2.8	5- C	0.0	5.1	7.	4-0	ر پارچ
12" I.	32 lbs.	23.4 20.3	17.6	13.7	12.2	6.6	8.9		0.00		4.0	0.7.	divide
13″	40 1bs.	34.7 29.6 25.5	22.2	17.8	15.4	12.5	11.3		0000			6.0	د   <u>د</u>
	41 lbs.	41.9 35.7 30.8	28.8	80.0	18.6	15.1	13.7	12.5	10.5	8.9	00 1	-03	9   5
i.	50 lbs.	52.3 44.6 38.4	23.5 29.4	26.1	23.3	18.8	17.1	15.6	13.1	11.11		0.0	
15″	60 lbs.	63.6 54.2 46.7	40.7 35.8	31.7	28.3 25.4	22.9	8.0%	18.9	15.9	13.6	12.6	10.9	100.2
	80 lbs.		50.0	38.7	34.5	28.0	25.3	23.1	19.4	16.5	15.8	5.65	haj
ij	64 lbs.	84.9 62.4	54.3	42.8	37.7	30.6	27.7	25.3	23.5	18.1		0.45	٠.
20" I.	80 1bs.	107.3 91.5 78.8	68.7	53.5	47.7	38.6	35.0		26.8			18.4	30 V
-dng	Distand tween ports in	55.54	15	17	81	50	21	818	8 24 58	98	200	888	- la

Thus for a load of 150 lbs. per square foot divide by 1.5. Maximium flore strain, 16,000 lbs. per square inch.
Only figures above the cross lines should be used for plastered ceilings, so that the deflection will not cause cracking of the plaster.

## Properties of Carnegie I Beams-Steel.

16	Radius of Gy- ration, Neut. Axisasbefore.	3.7	1.34	1.30	1.35	1.32	38	1.30	1.04	07.0	1.07	0.95	1.01	0.91	0.97	20.0	0.00	0.72	99.0	0.65	0.58	0.45
15	Mom. of Inertia Neutral Axis, coincident with Cent Line with O	I'	41.6 6.5 6.0	27.3	45.3	80.4	14.0	16.8	10.3	7.39	9.10	5.56	6.62	4.35	0.03	4.00	9.03	1.99	1.29	1.22	0.75	0.36
14	Add to Coeff. for every lb. Increase in Wt. of Beam		10000 8300		0019	6100	2010	4900	00,7	4100	3600		3300	0000	2800	0010	2012	2000		1600		
13	Ooefficient of Strength for Fibre Strain 12,500 lbs. per sq. inch. Used for Bridges.	,,	1430100	955000	873:200	715800	471300	390700	208800	206100	204900	156100	149700	120800	118800	79500	65300	55400	41300	35500	24600	19000
13	Add to Coeff. for every lb, Increase in Wt. of Beam,		10450		2800	2800	000	6300	2000	2000	4600		4300	0000	2000	3100	0010	2600		2100		
#	Coefficient of Strength for Fibre Strain of 16,000 lbs. per sq. inch. Used for Used for	O	1830500 1545600	1222400	1117700	916300	603200	200100	395200	263800	262200	199900	191600	154000	151400	101800	83500	67000	25300	41200	31400	24400
20	Radius of Gy- ration, Neutral ratios as before.		3.5	28.	5.82	5.04	20.00	4.90	38.8	90.9	8.72	8.70	80.	80.80	5.0	20.00	2.5	203	2.02	1.62	1.63	1.61
6	Monient of Resistance, Neutral Axis as before,	R	171.6	114.6	104.8	85.9	56.6	46.9	87.0	24.7	9.4.6	18.7	18.0	14.4	25.5	0.77	38.	6.28	4.96	3.86	20.32	2.30
œ	Moment of Inertia, Meu- tral Axis Per- pendicular to Webat Centre.	I	2059.3	1146.0	785.9	644.0	424.1	281.3	65.5	193.7	110.6	84.3	71.9	57.8	49.7	960	88	15.7	12.4	i-	0.0	4.0
ţ-	Increase of Thickness of Web for each lb, Increase of Weight,	inch.	.0123		.020	000	2000	.025	000	.000	.033		.037	070	. 042	049	OEO.	.059		.074		. 10 . 2. 10 .
9	Width of Flange.	ij	2.00	6.25	6.41	6.04 7.77	5.50	5.50	33.	4.75	4.75	4.50	4.50	3.5	65.5	2.63	35.50	3.13	3.00	2.75	2.63	
70	Thickness of Web.		3,8		•									•	•	•				•		. 10
4	Area of Section,	sq. in.	25 85 10 10	18.8	23.5	17.6	12.0	11.7	4.5	7.5	6.7	6.2	6.5	0.0	0.0	2.4	8	8.8	8.0	6.2	03.0	1.0
00	Weight per foot.		38			_	_			70		_	-	_	10	5			_		50.	5
c≀	Depth of Beam.		2,00	20,	15"	15//	15,	12/	15	10,01	9/	6	200	200	112	6,1	1/9	2,,'	2′′	4"	4	31
-	Section Index.		m m	B3	B 4	n n n	m P	B	600	BII	B12	B18	B14	Sign	PIG	B18	B19	B20	B21	.B22	B53	100

PROPERTIES OF CARNEGIE CHANNELS—STEE

15	Distance of Centre of Gravity from Outside of Web.	5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.5.	
14	Add to Coefficient for every lo, In- crease in Weight of Channel.	6100 4900 4100 3600 3800 2800 2900 1600	
13	Coefficient of Strength for Fibre Strain of 12,500 lbs. per square inch, used for Bridges	433400 315290 153800 163800 108400 108400 108400 81000 57100 57100 58600 83000 80	
12	Add to Coefficient for every lb. In- crease in Weight of Channel.	7800 6300 5200 4600 4300 3100 2600	1
11	Ooefficient of Strength for Briting of Torength for Fibre Strain of 16,000 last per gangre inch, used sull strength of the Buildings.	274700 404700 404700 273600 273600 273600 1188700 1188700 1188700 1188700 1188700 1188700 1188700 1188700 1188700 1188700	00000
10	Radius of Gyration, Redius Axis as before,	777446000000000000000000000000000000000	1
6	Moment of Resist- ance, Veutral Axis as before.	######################################	
œ	Moment of Inertis, Neutral Axis Per- Pendicular to Web at Centre,	0.48.87 0.47.88.88.88.88.88.88.88.88.88.88.88.88.88	Poot
<b>L</b> *	increase of Thick- ness of Web for each lb. Increase of Weight.	.020. .025. .029. .033. .049. .049. .049	coon in foot
9	r G Width of Flange.	85-51-99-98-98-98-98-98-98-98-98-98-98-98-98-	ad . 1 -
10	г. с. Тріскпеза of Web.	\$645685584454564545555555555555555555555	listribut
4	Å Area of Section.	псоотите 4 от от 4 от от от 4 от	formly
00	Neight per foot.	28.88.88.88.89.81.04.88.81.1.05.88.70.00.00.00.00.00.00.00.00.00.00.00.00.	Safe load in the uniformly distributed.
61	Depth of Channel.	######################################	e load in
-	Section Index.	DODDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDDD	L = Saf

PROPERTIES OF CARNEGIE CHANNELS—STEEL. 273

### PROPERTIES OF CARNEGIE Z BARS, IRON OR STREET.

	16	For Flore Strain of 12,000 lbs. per square inco. Axis Perpendicular to many Web at Centre.		67500 88800 88800 82400 102500 112300 112300 112300 112300 11100 61100 61000 61000 61000 75800 75800
	15	Coefficient	For Fibre Strain of 16,000 lbs. per square inch, Axis Perpendicular to Web at Centre.	90000 1104800 1138700 138700 156400 156400 1749800 174900 174900 18900 110800 110800
	14	ution.	Least Radius, Neu- tral Axis Diagonal.	88.88.88.88.88.88.88.88.88.88.88.88.88.
	13	of Gyration.	Meutral Axis through Centre of Gravity Coin- cident with Web.	+6447284428878878888888888888888888888888
	15	Radii	Meutral Axis through Centre of Gravity Per- pendicular to Web	88888888888888888888888888888888888888
	11	nts of ance.	Neutral Axis through Centre of Gravity Coin- cident with Web.	6.5282444400000000000000000000000000000000
STEEL.	10	Moments of Resistance.	Neutral Axis through Centre of Gravity Per- pendicular to Web.	4.8.9.11.11.14.14.16.16.16.17.17.17.17.17.17.17.17.17.17.17.17.17.
RON OR STEEL	6	nts of tia.	Meutral Axis through Centre of Gravity Coin- cident with Web.	0.03.54.55.55.00.00.00.00.00.00.00.00.00.00.00.
IR	œ	Moments of Inertia.	Neutral Axis through Centre of Gravity Per- pendicular to Web.	8.84.48.84.48.85.00.00.42.88.8 8.84.88.64.68.85.00.00.42.88.8
	2		g Area of Section,	4.00.00-00.00-4.4.00.00-6- 8.80-6.80-6-00-8-4.4.00.00-6-
	9	Weight per foot, Steel.		######################################
	70	non.	S Weight per foot,	######################################
	4	.la	È. Дріскпезз оц Мер	27.7.3.16 27.7.3.11.16 27.7.3.16 27.7.3.16 27.7.3.16 27.7.3.16 27.7.3.16 27.7.3.16
	00		F Width of Flange.	60 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
	e1		Ë. Depth of Web.	6 1-16 6
	1		Section Index.	11110000000000000000000000000000000000

		11 - 1 - 1	
91	of Strength.	For Fibre Strain of 12,000 lbs. per square inch, Axis Perpendic- ular to Web at Centre.	91500 83100 837400 837400 88600 444000 65200 653100 115400 115400 828800 82800 82800 82800 82800 82800 82800 82900 82000 8000 8000 8000 8000 8000 8000 8000 8000 8000 8000 8000 8000 8000 8
15	Coefficient of $\frac{1}{C}$	For Fibre Strain of 16,000 lbs, per square inch, Axis Perpendic- ular to Web at Centre.	132000 41700 41700 41700 41700 51500 64500 64500 77400 20500 20500 20500 31800 31800 31800 31800 31800
14	Gyration.	Least Radius, Neutral Axis Diagonal.	00000000000000000000000000000000000000
13	go	Neutral Axis through Centre of Gravity Coincident with Web,	4454484848488
12	Radii	Neutral Axis through Centre of Gravity Perpendicular to Web.	211111111111111111111111111111111111111
==	Moments of Resistance.	Neutral Axis through Centre of Gravity Coincident with Web.	4.11.03.30.00.00.4.1.1.1.1.1.1.0.34.20.20.20.4.1.1.1.1.1.1.1.0.34.20.20.1.4.20.20.20.20.20.20.20.20.20.20.20.20.20.
10	Mome Resis	Neutral Axis through Centre of Gravity Perpendicular to Web,	11883.4.4.7.0.0.0.7.1.9.9.9.8.8.4.4.1.2.8.8.2.1.9.9.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8.8
6	nts of	Mentral Axis through Centre of Gravity Coincident with Web.	44 88.34 75.60 88.34 75.60 88.82 88.84 86.88 86 86 86 86 86 86 86 86 86 86 86 86 8
œ	Moments c Inertia.	Neutral Axis through Centre of Gravity Perpendicular to Web.	8.00 c c 115151543 8 8 8 4 4 6 8 8 8 4 4 1155 8 4 3 8 8 4 4 6 8 8 8 8 8 8 8 8 8 8 8 8 8 8 8
L.		g Area of Section.	8.33.83.83.83.83.83.83.83.83.83.83.83.83
9	le.	Weight per foot, Stee	88.80 8.85.77 8.85.77 8.60.00 8.60.00 8.60.00 7.40.00 7.40.00 7.40.00 7.40.00
	.iron, Iron. 당 Weight per foot, Iron.		2.001827578088000013181 8.001937778088000013181 8.0019377400000000000000000000000000000000000
10		ionI toot neg tdvieW =	2002222228880002132
4		F. Thickness of Metal.	
			89.8 90.1
4		F. Thickness of Metal.	2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1

### TRENTON IRON BEAMS AND CHANNELS.

OX--- T----- C4--1 --- 4 T--- O

	(New Jersey Steel and Iron Co.)								
Height in inches.	Least Weight per Yard, in pounds.	Width of Flange, in inches.	Thickness of Web, in inches.	Coefficient in lbs. for Transverse Strength,	Height in inches.	Least Weight per Yard, in pounds.	Width of Flange, in inches.	Thickness of Web, in inches.	Coefficient in lbs. for Transverse Strength.
I Beams.						(	Chann	els.	
20 20 15.4 15.3-16 15.4 12.5-14 12.5-14 12.5-14 10.5 10.5 10.5 10.5 10.5 10.5 10.5 10.5	272 200 200 150 125 170 125 120 96 135 105 90 65 55 120 90 50	6534 6535 55161 6536 6536 6536 6536 6536 653	11-16 1½.6 1½.42 .6.47 .39 .32 .32 .35 .57 .57 .38 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3 .3	1,320,000 990,000 748,000 551,000 375,000 377,000 375,000 360,000 250,000 250,000 167,000 168,000 172,000 172,000 172,000 172,000 172,000	15 15 12 12 10 10 9 9 8 8 7 7 6 6 6 6 5 4 3	190 120 140 70 60 48 870 50 45 33 36 25 45 33 22 45 19 16 16 25	434 4 4 3 234 214 214 214 214 214 176 114 114 ck Be	34 14 12 11-16 38 5-16 7-16 33 .26 .20 14 .20 .40 .28 .18 .20 .20 .20 .20 .20	625,000 401,000 381,000 200,100 134,750 102,000 146,000 62,000 63,950 65,800 62,000 39,500 58,300 45,700 33,680 15,700 10,500
5 5 4	40 40 30 37	3 23/4 3	5-16 14 5-16 14 5-16 14 3-16	62,600 49,100 38,700 36,800	8 7	65 55	4½ 4½	3/8 5-16	91,800 63,500
4 4	30	23/4 3 23/4 2	3-16	30,100 18,000					

### Trenton Beams and Channels.

To find which beam, supported at both ends, will be required to support

with safety a given uniformly distributed load:

Multiply the load in pounds by the span in feet, and take the beam whose "Coefficient for Strength" is nearest to and exceeds the number so found.

The weight of the beam itself should be included in the load.

The weight of the beam itself should be included in the load. The deflection in inches, for such distributed load, will be found by dividing the square of the span taken in feet, by 70 times the depth of the beam, taken in inches, for iron beams, and by \$25 times the depth for steel. Example.—Which beam will be required to support a uniformly distributed load of 12 tons (= 24,000 bts.) on a span of 15 feet? 2,000  $\times$  15 = 360,000, which is less than the coefficient of the 12½-inch 125-b. iron beam. The weight of the beam itself would be 625 bls., which, added to the load and multiplied by the span, would still give a product less than the coefficient; thus,

 $24,625 \times 15 = 369,375$ .

The deflection will be

$$\frac{15 \times 15}{70 \times 12\frac{1}{4}} = 0.26 \text{ inch.}$$

The safe distributed load for each beam can be found by dividing the coefficient by the span in feet, and subtracting the weight of the beam.

When the load is concentrated entirely at the centre of the span, one half The beans must be secured against yielding sideways, or the safe loads will be much less.

For beams used with plastered ceilings, the deflection allowed should not exceed 1/30 inch per foot of span, to avoid cracking of the plaster.

### TRENTON ANGLE-BARS.

Size of Bar.	App	Approximate Weight, in pounds per yard, for each thickness in inches.							
6 × 6 41,6 × 41,6 4 × 4 31,6 × 31,6 3 × 8 234 × 234 21,6 × 21,6 21,4 × 21,4 2 × 2 13,4 × 13,4 11,6 × 11,6 11,7 × 17,6 3,4 × 34,6 3,4 × 34,6 3,4 × 34,6 3,6 × 31,6 3,6 × 31,6 3,7 × 31	7/16 37.5 38.6 24.8 14.4 15/16 16.2 14.9 10.6 7/32 8.3 3/16 5.27 1/4 2.97 2.34 2.03 1.72	125 57.5 716 33.1 28.7 5/16 17.7 38 19.2 5/16 14.7 9/32 11.9 14 7/32 6.09 5/32 3.66 2.88 2.48 2.09	9/16 64.3 47.5 37.5 32.5 21.1 18/32 20.7 11/32 16.0 5/16 13.1 10.4 14 8.13 8.13 8.13 10.4 14 4 34 4 34 4 34 2.9 34 2.9 34 2.1 2.1 2.1 34 34 34 34 34 34 34 34 34 34 34 34 34	5% 71.1 52.3 9/16 41.8 36.2 7/16 24.4 7/16 22.2 7/16 22.2 3% 11/32 14.3 5/16 11.5 9/32 9 05 7.64 7.732 4.99 3.91	11/16 77.8 57.2 58 46.1 39.8 27.5 15/32 23.6 18/32 18.6 5/16 9.96 5/16 9.96 14 5.63 4.38	34.4 84.4 61.9 11/16 50.5 43.4 9/16 30.6 25.0 7/16 20.0 18/32 16.8 13.6 11/.2 10.8 9.13	13/16 91.0 	978 97.3 11/16 36.5 9/16 27.7 1/2 22.5	Thinnest Bar 36,900 lbs. 18,000 " 12,184 ",9,200 " 4,611 " 4,710 " 8,156 " 2,530 " 1,752 " 1,150 " 882 " 393 " 246 " 186 " 133 "
74 ^ 74	1	2.00							100

### Uneven Legs.

6 ×4		7/16 41.8 47	9/16 53.1	5% 58.6	11/16 64.0	3/4 69.4	( 30,680, 6" way ) 14,750, 4" "
5 × 3½ 4½ × 3	$ \begin{array}{c} 3/8 \\ 30.5 \\ 26.7 \end{array} $			49.2 43.0	53.7 46.8	58.1 50.6	\$ 18,353, 5" " 9,651, 3½" " 14,580, 4½" "
4 ×3	5/16 20.9	36 7/1	6 1/6	9/16 36.2	5% 39.8	11/16 43.4	7,020, 3" " 9,850, 4" " 5,871, 3" "
31/6 × 3	15.6 19.3	23.0 26	5 30.0	33.4	36.7	40 0	6,180, 31/2" " 4,710, 3" "
31/2 × 21/2	14.4 17.7	21.1 24	4 27.5	30.6	33.6	36.5	\$ 6,037, 314" " \$ 3,296, 214" " \$ 5,515, 314" "
31/2×11/2	11.9 5/16	11/32 3/8	13/32	7/16	25.0	9/16	1,148, 11/3" " 4,490, 3" "
3 ×21/2 3 ×2	13.116.2 $7/32$ $10.4$	1/4 9/8	2 5/16	22.2 3/8 17.3	25.0 7/16 20.0	27.7 $1/2$ $22.5$	3,233, 21/2" " 3,833, 3" " 1,850, 2" "

### TRENTON THE BARS.

	TREENTON	LEE BARS.	
Designation of Bar.	Approximate Weig yard, for each th	Coefficient for Transverse Strength.	
Table, Leg.  4" × 4" 3½" × 3½" 3" × 3½" 2½" × 2½" 2½" × 2½" 1½" × 1½" 1½" × 1½" 5" × 2½" 3" × 2½"	7-16" 28 7 lbs. 34" 21.1 " 5-16" 14.7 " 5-16" 13 09 " 14" 9.4 " 14" 6.68 " 7-32" 4.87 " 5-82" 2.80 " 5-16" 14.6 lbs.	15" 37.5 lbs. 15" 32.5 " 15" 32.5 " 15" 27.5 " 36" 17.3 " 5-16" 11.5 " 14" 55.5 " 14" 35.0 " 15" 33.0 " 16" 35.0 "	Thinnest Bar, 15,800 lbs, 10,550 " 6,680 " 3,880 " 1,970 " 1,933 " 596 " 268 " 6,344 " 2,540 "
2½" × 3" 2" × 3" 2" × 1½" 2½" × 1½" 2½" × 1" 1½" × 1"	36" 19.2 " 36" 17.3 " 9-32" 9.1 " 14" 7.4 " 14" 6.5 " 14" 5.6 "		6,404 " 6,173 " 1,355 " 604 " 457 " 421 "

### SIZE OF BEAMS, AND THEIR DISTANCE APART, Suitable for Floors having Loads per square foot from 100 lbs. to 300 lbs. (New Jersey Steel and Iron Co.)

- <u>-</u> -	Load sq. 100	per ft. lbs.	Load sq. 150	per ft. lbs.	sq	d per . ft. 0 lbs.	Load 1 sq. f 250 ll	per t.	Load sq. f	t.
Clear Span in feet.	Size and Weight per yard.	Distance from Centre to Cen- tre.	Size and Weight per yard.	Distance from Centre to Cen- tre,	Size and Weight per yard.	Distance from Centre to Cen-	Size and Weight per yard.	Dist. from Cen- tre to Centre.	Size and Weight per yard.	Dist, from Cen- tre to Centre,
8 { 10 } 12 {	in. lb. 4 30 5 30 5 40 6 40 6 50	feet 4.6 5.9 3.8 4.8 4.2 5.2	in. lb. 4 30 5 30 6 40 6 50 7 55	feet 3.1 4.0 4.1 5.0 3.4 4.6	6 6 7 8	3.0 4.8 40 3.0 50 3.7 55 3.4 4.5	in. lb. 6 40 6 50 6 50 7 55 8 65 9 70 9 70	3.9 4.7 3.0 4.0 3.6 4.5	in. lb. 6 40 5 50 7 55 8 65 8 65 9 70 9 85	feet 3.2 3.9 3.3 4.4 3.0 3.8 3.8
14 }	7 55 8 65 8 65 9 70 9 70	5.0 6.7 5.0 6.3 4.9	6 50 6 50 7 55 7 55 8 65 8 65 9 70 9 85	3.3 4.5 3.3 4.2 3.9	9 8	70 4.1 35 3.7 90 4.7	9 70 10½ 90 10½ 90 10½ 105 10½ 105	3.8	9 80 101/2 90 101/2 105 121/4 125 101/2 135	3.6 4.8 3.6
18 20	9 85 10½ 90	5.9 6.0	101/2 90 101/2 105 121/4 125	4.9 4.5 6.0	12 9 101/6 10 121/4 19	06 4.6 05 3.4 25 4.5	121/4 125 121/4 125 121/4 170	4.5 3.6 4.9	$12\frac{1}{4}$ $125$ $12\frac{1}{4}$ $125$ 15 $150$	3.7 3.0 4.4
22 }	10½ 90 10½ 105 12 96 12¼ 125	4.9 5.6 5.0 6.1	12 96 12½ 125 12¼ 125 12 125 15 125	4.1 5.0	1214 15 15 15 1214 15 15 15	5 4.5 5 3.0 60 4.5	1214 125 15 125 1214 170 15 150	3.6 3.3 3.6	15 200	3.3 3.6 3.0 4.1
26 { 28 {	1214 125 15 125	5.1	15 425 15 150 15 150 15 200	5.1 4.3 5.9	15 15 15 20 15 20 20 20	00 5.2 00 4.4 00 6.0	15 150 15 200 15 200 20 200	4.2 3.5 4.8	15 200 20 200 20 200 20 272	3.5 4.7 3.9 5.3
30 {	15 150	5.6	15 150 15 200		15 20 20 20		20 200 20 272	4.1 5.5	200	3.4 4.6

### FLOORING MATERIAL.

For fire-proof flooring, the space between the floor-beams may be spanned with brick arches, or with hollow brick made especially for the purpose, the

with offick arches, of with notion of the made especially for the purpose, the latter being much lighter than ordinary brick.

Arches 4 inches deep of solid brick weigh about 70 lbs, per square foot, including the concrete levelling material, and substantial floors are thus made up to 6 feet span of arch, or much greater span if the skew backs at made up to 6 feet span of arcin, or much greater span if the skew backs at the springing of the arch are made deeper, the rise of the arch being preferably not less than 1/10 of the span. Hollow brick for floors are usually in depth about ½ of the span, and are used up to, and even exceeding, spans of 10 feet. The weight of the latter material will vary from 20 lbs. per square foot for 3-foot spans up to 80 lbs. per square foot for spans of 10 feet. Full particulars of this construction are given by the manufacturers. For supporting brick floors the beams should be securely tied with rods to resist

the lateral pressure.

In the following cases the loads, in addition to the weight of the floor

itself, may be assumed as:

For street bridges for general public traffi	.c 80 l	bs. per sq	1. ft.
For floors of dwellings	40 1		
For churches, theatres, and ball-rooms	80	lbs. "	
For hay-lofts	80	bs. "	
For storage of grain			66
For warehouses and general merchandise	250	bs. "	44
For factories			66
For snow thirty inches deep			46
For maximum pressure of wind	50	lbs "	44
For brick walls			1 ft.
For masonry walls			"
Roofs, allowing thirty pounds per square fo	ot for wind a	nd snow:	
For corrugated iron laid directly on the p	urlins 37 l	bs, per so	ft.
For corrugated iron laid directly on the p For corrugated iron laid on boards	40	hs "	1.66

For slate nailed to laths..... 43 lbs. For slate nailed on boards..... 46 lbs.

If plastered below the rafters, the weight will be about ten pounds per square foot additional.

### TIE-RODS FOR BEAMS SUPPORTING BRICK ARCHES.

The horizontal thrust of brick arches is as follows:

$$\frac{1.5WS^2}{R} = \text{pressure in pounds. per lineal foot of arch:}$$

W = load in pounds. per square foot; S = span of arch in feet;

R = rise in inches.

Place the tie-rods as low through the webs of the beams as possible and spaced so that the pressure of arches as obtained above will not produce a greater stress than 15,000 lbs. per square inch of the least section of the bolt.

### TORSIONAL STRENGTH.

Let a horizontal shaft of diameter = d be fixed at one end, and at the other or free end, at a distance = l from the fixed end, let there be fixed a horizontal lever arm with a weight = P acting at a distance = a from the axis of the shaft so as to twist it; then Pa = moment of the applied force.

Resisting moment = twisting moment =  $\frac{SJ}{c}$ , in which S = unit shearingresistance, J = polar moment of inertia of the section with respect to the axis, and c = distance of the most remote fibre from the axis, in a crosssection. For a circle with diameter d,

$$J = \frac{\pi d^4}{32}; \qquad c = \frac{1}{2}d;$$

$$Pa = \frac{SJ}{c} = \frac{\pi d^3S}{16} = \frac{d^3}{5.1} = .1963d^3S; \quad d = \sqrt[3]{\frac{5.1Pa}{S}}.$$

For hollow shafts of external diameter d and internal diameter  $d_1$ .

$$Pa = .1963 \frac{d^4 - d_1^4}{d}S;$$
  $d = \sqrt[3]{\frac{5.1Pa}{\left(1 - \frac{d_1^4}{d^4}\right)S}}.$ 

For a square whose side = d,

$$J = \frac{d^4}{6};$$
  $c = d\sqrt{\frac{1}{2}};$   $\frac{SJ}{c} = Pa = \frac{d^3S}{4.2426} = 0.236d^3S.$ 

For a rectangle whose sides are b and d.

$$J = \frac{bd^3}{12} + \frac{b^3d}{12}; \qquad c = \frac{1}{2} \sqrt{b^2 + d^2}; \qquad \frac{SJ}{c} = Pa = \frac{(bd^3 + b^3d)S}{6 \sqrt{b^2 + d^2}}.$$

The above formulæ are based on the supposition that the shearing resistance at any point of the cross-section is proportional to its distance from the axis; but this is true only within the elastic limit. In materials capable of flow, while the particles near the axis are strained within the elastic limit those at some distance within the circumference may be strained nearly to the ultimate resistance, so that the total resistance is something greater than that calculated by the formulæ. (See Thurston, "Matls of Eng." Part II. p. 527.) Saint Venant finds for square shafts Pa = 0.281678 (Rankine, "Mach. and Millwork." p. 504). For working strength, however, the formulæ may be used, with S taken at the safe working unit resistance.

mulæ may be used, with S taken at the safe working unit resistance. The ultimate torsional shearing resistance S is about the same as the direct shearing resistance, and may be taken at 20,000 to 25,000 lbs. per square inch for cast iron, 45,000 lbs. for wrought iron, and 50,000 to 150,000 lbs. for steel, according to its carbon and temper. Large factors of safety should be taken, especially when the direction of stress is reversed, as in reversing engines, and when the torsional stress is combined with other stresses, as is usual in shafting. (See "Shafting.")

\*\*Elastic Resistance to Torsion.\*\*—Let l = length of bar being twisted, d = diameter, P = force applied at the extremity of a lever arm of length = a, P are twisting moment, G = torsional modulus of elasticity,  $\theta$  = angle through which the free end of the shaft is twisted, measured in any of sodius -1.

arc of radius = 1.

For a cylindrical shaft

$$Pa = \frac{\pi \theta G d^4}{32l}; \qquad \theta = \frac{32Pal}{\pi d^4 G}; \qquad G = \frac{32Pal}{\theta \pi d^4}; \qquad \frac{32}{\pi} = 10.186.$$

If  $\alpha$  = angle of torsion in degrees,

$$\theta = \frac{a\pi}{180};$$
  $a = \frac{180\theta}{\pi} = \frac{180 \times 32 Pal}{\pi^2 d^4 G} = \frac{583.6 Pal}{d^4 G}.$ 

The value of G is given by different authorities as from  $\frac{1}{2}$  to  $\frac{2}{5}$  of E, the modulus of elasticity for tension.

### COMBINED STRESSES.

(From Merriman's "Strength of Materials.")

Combined Tension and Flexure.—Let A = the area of a bar subjected to both tension and flexure, P = tensile stress applied at the ends, P+A= unit tensile stress, S= unit stress at the fibre on the tensile side most P+A= unit fensile stress, S= unit stress at the more on the tensile such more remote from the neutral axis, due to discure alone, then maximum tensile unit stress = (P+A)+S. A beam to resist combined tension and flexure should be designed so that (P+A)+S shall not exceed the proper allowable working unit stress.

Combined Compression and Flexure.—If  $P \div A =$  unit stress due to compression alone, and S = unit compressive stress at fibre most remote from neutral axis, due to flexure alone, then maximum compressive unit stress

$$=\frac{P}{4}+S.$$

Combined Tension (or Compression) and Shear,-If ap-

plied tension (or compression) unit stress = p, applied shearing unit stress = v, then from the combined action of the two forces

Max. 
$$S = \pm \sqrt{v^2 + \frac{1}{4}p^2}$$
, Maximum shearing unit stress;

Max.  $t = \frac{1}{2}p + \sqrt{v^2 + \frac{1}{2}p^2}$ . Maximum tensile (or compressive) unit stress.

Combined Flexure and Torsion.—If S = greatest unit stress due to flexure alone, and  $S_s$  = greatest torsional shearing unit stress due to torsion alone, then for the combined stresses

Max. tension or compression unit stress  $t = \frac{1}{2}S + \sqrt{Ss^2 + \frac{1}{4}S^2}$ ;

Max, shear 
$$s = \pm \sqrt{Ss^2 + \frac{1}{4}S^2}$$
.

Formula for diameter of a round shaft subjected to transverse load while transmitting a given horse-power (see also Shafts of Engines):

$$d^3 = \frac{16M}{\pi t} + \frac{16}{t} \sqrt{\frac{M^2}{\pi^2} + \frac{402,500,000H^2}{n^2}},$$

where  $M=\max$  maximum bending moment of the transverse forces in poundinches, H= horse-power transmitted, n= No. of revs. per minute, and t= the safe allowable tensile or compressive working strength of the material. Combined Compression and Torsion.—For a vertical round shaft carrying a load and also transmitting a given horse-power, the result-

ant maximum compressive unit stress

$$t = \frac{4P}{\pi d^2} + \sqrt{321,000^2 \frac{H^2}{\pi^2 d^6} + \frac{16P^2}{\pi^2 d^4}},$$

in which P is the load. From this the diameter d may be found when t and

the other data are given.

Stress due to Temperature.—Let l= length of a bar, A= its sectional area, c= coefficient of linear expansion for one degree, t= rise or fall in temperature in degrees, E= modulus of elasticity,  $\lambda$  the change of length due to the rise or fall t; if the bar is free to expand or contract,  $\lambda=$ 

If the bar is held so as to prevent its expansion or contraction the stress produced by the change of temperature = S = Act E. The following are average values of the coefficients of linear expansion for a change in temperature. ature of one degree Fahrenheit:

For brick and stone....a = 0.0000050,

The stress due to temperature should be added to or subtracted from the

The stress due to deinperature should be added to or shotracted from the stress caused by other external forces according as it acts to increase or to relieve the existing stress. What stress will be caused in a steel bar 1 inch square in area by a change of temperature of  $100^\circ$  F,  $S=ActE=l\times.0000065\times100\times30.000.000=19,500 lbs. Suppose the bar is under tension of <math>19,500$  lbs. between rigid abutments before the change in temperature takes place, a cooling of 100° F, will double the tension, and a heating of 100° will reduce the tension to zero.

### STRENGTH OF FLAT PLATES.

For a circular plate supported at the edge, uniformly loaded, according to Grashof,

$$f = \frac{5}{6} \frac{r^2}{t^2} p;$$
  $t = \sqrt{\frac{5r^2p}{6f}};$   $p = \frac{6ft^2}{5r^2}.$ 

For a circular plate fixed at the edge, uniformly loaded,

$$f = \frac{2}{3} \, \frac{r^2}{t^2} \, p; \qquad t = \sqrt{\frac{2}{3} \, \frac{r^2 p}{f}}; \qquad p = \frac{3 f t^2}{2 r^2};$$

in which f denotes the working stress; r, the radius in inches; t, the thick ness in inches; and p, the pressure in pounds per square inch.

For mathematical discussion, see Lanza, "Applied Mechanics," p. 900, etc. Lanza gives the following table, using a factor of safety of 8, with tensile strength of cast iron 20,000, of wrought iron 40,000, and of steel 80,000;

Supported.	Fixed.
Cast iron $t = .0182570r \sqrt{p}$	$t = .0163300r \sqrt{p}$
Wrought iron $t = .0117850r \sqrt{p}$	$t = .0105410r \sqrt{p}$
Steel $t = .0091287r \sqrt{p}$	$t = .0081649r \sqrt{p}$

For a circulate plate supported at the edge, and loaded with a concentrated load P applied at a circumference the radius of which is r<sub>0</sub>:

$$f = \left(\frac{4}{3}\log\frac{r}{r_0} + 1\right) \frac{P}{\pi t^2} = c\frac{P}{\pi t^2};$$
for 
$$\frac{r}{r_0} = 10 \quad 20 \quad 30 \quad 40 \quad 50;$$

$$c = 4.07 \quad 5.00 \quad 5.53 \quad 5.92 \quad 6.22;$$

$$t = \sqrt{\frac{cP}{\pi f}}; \qquad P = \frac{\pi t^2 f}{c}.$$

The above formulæ are deduced from theoretical considerations, and give thicknesses much greater than are generally used in steam-engine cylinder heads. (See empirical formulæ under Dimensions of Parts of Engines.) The theoretical formulæ seem to be based on incorrect or incomplete hypoth-

sees, but they err in the direction of safety.

The Strength of Unstayed Flat Surfaces.—Robert Wilson (Eng'g, Sept. 24, 1877) draws attention to the apparent discrepancy between the results of theoretical investigations and of actual experiments on the strength of unstayed flat surfaces of boiler-plate, such as the unstayed flat

strength of unsayed hat surfaces of noner-place, such as the unstayed hat crowns of domes and of vertical boilers.

Rankine's "Civil Engineering" gives the following rules for the strength of a circular plate supported all round the edge, prefaced by the remark that "the formula is founded on a theory which is only approximately true; but which nevertheless may be considered to involve no error of practical importance:"

$$M = \frac{Wb}{6\pi} = \frac{Pb^3}{24}.$$

Here

M =greatest bending moment ;

 $W = \text{total load uniformly distributed} = \frac{Pb^2\pi}{\epsilon}$ ;

b = diameter of plate in inches;

P =bursting pressure in pounds per square inch.

Calling t the thickness in inches, for a plate supported round the edges,

$$M = \frac{1}{6} 42,000bt^2;$$
  $\therefore \frac{Pb^2}{24} = 7000t^2.$ 

For a plate fixed round the edges, 
$$\frac{2}{3}\frac{Pb^2}{24}=7000t^2; \text{ whence } P=\frac{t^2\times 63{,}000}{r^2},$$

where r = radius of the plate.

Dr. Grashof gives a formula from which we have the following rule:

$$P = \frac{t^2 \times 72,000}{r^2}$$
.

This formula of Grashof's has been adopted by Professor Unwin in his "Elements of Machine Design." These formule by Rankine and Grashof may be regarded as being practically the same.

On trying to make the rules given by these authorities agree with the results of his experience of the strength of unstayed flat ends of cylindrical boilers and domes that had given way after long use, Mr. Wilson was led to believe that the above rules give the breaking strength much lower than it actually is. He describes a number of experiments made by Mr. Nichols of Kirkstall, which gave results varying widely from each other, as the method of supporting the edges of the plate was varied, and also varying widely from the calculated bursting pressures, the actual results being in all cases very much the higher.

Some conclusions drawn from these results are:

1. Although the bursting pressure has been found to be so high, boilermakers must be warned against attaching any importance to this, since the plates deflected almost as soon as any pressure was put upon them and sprang back again on the pressure being taken off. This springing of the plate in the course of time inevitably results in grooving or channelling, which, especially when aided by the action of the corrosive acids in the water or steam, will in time reduce the thickness of the plate, and bring about the destruction of an unstaved surface at a very low pressure.

2. Since flat plates commence to deflect at very low pressures, they should never be used without stays; but it is better to dish the plates when they are

not stayed by flues, tubes, etc.

3. Against the commonly accepted opinion that the limit of elasticity should never be reached in testing a boiler or other structure, these experiments show that an exception should be made in the case of an unstayed flat end-plate of a boiler, which will be safer when it has assumed a permanent set that will prevent its becoming grooved by the continual variation of pressure in working. The hydraulic pressure in this case simply does what should have been done before the plate was fixed, that is, dishes it.

4. These experiments appear to show that the mode of attaching by flange or by an inside or outside angle-iron exerts an important influence on the

manner in which the plate is strained by the pressure.

When the plate is secured to an angle-iron, the stretching under pressure is, to a certain extent, concentrated at the line of rivet-holes, and the plate partakes rather of a beam supported than fixed round the edge. Instead of the strength increasing as the square of the thickness, when the plate is attached by an angle-fron, it is probable that the strength does not increase even directly as the thickness, since the plate gives way simply by stretching at the rivet-holes, and the thicker the plate, the less uniformly is the strain borne by the different layers of which the plate may be considered to be made up. When the plate is flanged, the flange becomes compressed by the pressure against the body of the plate, and near the rim, as shown by the contrary flexure, the inside of the plate is stretched more than the outside, and it may be by a kind of shearing action that the plate gives way along the line where the crushing and stretching meet.

5. These tests appear to show that the rules deduced from the theoretical investigations of Lamé, Rankine, and Grashof are not confirmed by experi-

ment, and are therefore not trustworthy.

Unbraced Wrought-iron Heads of Boilers, etc. (The Locomotive, Feb. 1890).—Few experiments have been made on the strength of flat heads, and our knowledge of them comes largely from theory. Experiments have been made on small plates 1-16 of an inch thick, yet the data so obtained cannot be considered satisfactory when we consider the far thicker heads that are used in practice, although the results agreed well with Ran-kine's formula. Mr. Nichols has made experiments on larger heads, and from them he has deduced the following rule: "To find the proper thickness for a flat unstayed head, multiply the area of the head by the pressure per square inch that it is to bear safely, and multiply this by the desired factor of safety (say 8); theu divide the product by ten times the tensile strength of the material used for the head." His rule for finding the bursting pressure when the dimensions of the head are given is: "Multiply the thickness of the end-plate in inches by ten times the tensile strength of the material used, and divide the product by the area of the head in inches."

In Mr. Nichols's experiments the average tensile strength of the iron used for the heads was 44,800 pounds. The results he obtained are given below, with the calculated pressure, by his rule, for comparison.

1. An unstayed flat boiler-head is 34½ inches in diameter and 9-16 inch thick. What is its bursting pressure? The area of a circle 34½ inches in diameter is 935 square inches; then 9-16 × 44,800 × 10 = 252,000, and 252,000 ÷ 935 = 279 pounds, the calculated bursting pressure. The head actually burst at 280 pounds.

2. Head 34/2 inches in diameter and 36 inch thick. The area = 935 square inches; then,  $36\times44.800\times10=168.000$ , and 168.000+935=180 pounds, calculated bursting pressure. This head actually burst at 200 pounds.

3. Head 26¼ inches in diameter, and 3½ inch thick. The area 541 square inches. Then,  $35\times14,800\times10=108,000$ , and 108,000+541=311 pounds. This head burst at 370 pounds.

4. Head 28½ inches in diameter and 3½ inch thick. The area = 638 square inches; then,  $\frac{3}{2} \times 44,800 \times 10 = 168,000$ , and  $\frac{168,000 + 638}{263} = 263$ pounds. The actual bursting pressure was 300 pounds.

In the third experiment, the amount the plate bulged under different pressures was as follows:

120 170 140 5/8 3/4

The pressure was now reduced to zero, "and the end sprang back 3-16 inch, leaving it with a permanent set of 9-16 inch. The pressure of 200 lbs. was again applied on 36 separate occasions during an interval of five days, the bulging and permanent set being noted on each occasion, but without any appreciable difference from that noted above.

The experiments described were confined to plates not widely different in their dimensions, so that Mr. Nichols's rule cannot be relied upon for heads

that depart much from the proportions given in the examples.

Thickness of Flat Cast-iron Plates to resist Bursting
Pressures.—In Church's Life of Ericsson is found the following letter: "My dear Sir: The proper thickness of a square cast-iron plate will be obtained by following: Multiply the side in feet (or decimals of a foot) by 1/4 of the pressure in pounds and divide by 850 times the side in inches; the

quotient is the square of the thickness in inches. "Example.-A plate 5 feet or 60 inches square, with a pressure of 30 lbs.

per square inch.

"Thickness = 
$$\frac{5 \times \frac{14}{4} \times 3600 \times 30}{850 \times 60} = 2.64$$
.  $\sqrt{2.64} = 1.62$  inches.

"For a circular plate, multiply 11-14 of the diameter in feet by ½ of the pressure on the plate in pounds. Divide by 850 times 11-14 of the diameter in inches. [Extract the square root.]
"Example.—Plate 5 feet diameter, pressure 30 lbs. per square inch.

"Example.—Frace 5 test diameter, pressure 30 los. per square inch.

"Area 2827 
$$\times \frac{30}{4} = \frac{84,810}{4} = 21,202$$
; diam.  $60 \times \frac{11}{14} = 47.1$ ;  $5 \times \frac{11}{14} = 3.92$ .

 $3.92 \times 21,202 = 83,811$ 
 $8.50 \times 4.71 = 41,035 = 2.02$ .  $\sqrt{2.02} = 1.42$  inch.

"A great mathematician would cover half a dozen sheets with figures to solve this problem."

Strength of Stayed Surfaces .- A flat plate of thickness t is supported uniformly by stays whose distance from centre to centre is a, uniform load p lbs. per square inch. Each stay supports  $pa^2$  lbs. The greatest stress on the plate is

 $f = \frac{2}{0} \frac{a^2}{t^2} p$ . (Unwin).

### SPHERICAL SHELLS AND DOMED BOILER-HEADS.

To find the Thickness of a Spherical Shell to resist a given Pressure, Let d = diameter in inches, and p the internal pressure per square inch. The total pressure which tends to produce rupture around the great circle will be  $\frac{1}{4}\pi d^3p$ . Let S = safe tensile stress per square inch, and t the thickness of metal in inches; then the resistance to the pressure will be  $\frac{1}{2}\pi d^3p$ . Let  $\frac{1}{2}\pi d^3p$ . Le

$$\frac{1}{4}\pi d^2p = \pi dtS$$
. Whence  $t = \frac{pd}{4S}$ .

The same rule is used for finding the thickness of a hemispherical head

to a cylinder, as of a cylindrical boiler.

Thickness of a Domed Head of a boiler.—If S = safe tensilestress per square inch, d = diameter of the shell in inches, and t = thicknessof the shell, t = pd + 2S; but the thickness of a hemispherical head of the same diameter is t=pd+4S. Hence if we make the *radius* of curvature of a domed head equal to the diameter of the boiler, we shall have t= $rac{2pd}{4S}=rac{pd}{2S},$  or the thickness of such a domed head will be equal to the thick-

ness of the shell.

Stresses in Steel Plating due to Water-pressure, as in plating of vessels and bulkheads (Engineering, May 22, 1891, page 629). Mr. J. A. Yates has made calculations of the stresses to which steel plates

Mr. J. A. Yates has made calculations of the stresses to which steel plates are subjected by external water-pressure, and arrives at the following conclusions:

Assume 2a inches to be the distance between the frames or other rigid supports, and let d represent the depth in feet, below the surface of the water, of the plate under consideration, t = thickness of plate in inches, D the deflection from a straight line under pressure in inches, and P = stress per square inch of section.

For outer bottom and ballast-tank plating,  $a=420\frac{t}{d^3}$ , D should not be greater than .05  $\frac{2a}{12}$ , and  $\frac{P}{2}$  not greater than 2 to 3 tons; while for bulkheads, etc.,  $a=2352\frac{t}{d^3}$ . D should not be greater than .1 $\frac{2a}{12}$ , and  $\frac{P}{2}$  not greater than 7 tons. To illustrate the application of these formulæ the following cases have been taken:

For	Outer Bo	ttom, etc.	For Bulkheads, etc.				
Thick- ness of Plating.	Depth below Water.	Spacing of Frames should not exceed	Thick- ness of Plating	Depth of Water.	Maximum Spacing of Rigid Stiffeners.		
in.	ft. 20 10 18 9 10 5	in. About 21	in.	ft. 20 20 10 20 10 10	ft. in. 9 10 7 4 14 8 4 10 9 8 4 10		

It would appear that the course which should be followed in stiffening bulkheads is to fit substantially rigid stiffening frames at comparatively wide intervals, and only work such light angles between as are necessary for making a fair job of the bulkhead.

# THICK HOLLOW CYLINDERS UNDER TENSION.

Burr, "Elasticity and Resistance of Materials," p. 36, gives

$$t = r \left\{ \left( \frac{h+p}{h-p} \right)^{\frac{1}{2}} - 1 \right\} \cdot \begin{array}{l} t = \text{thickness}; \ r = \text{interior radius}; \\ h = \max \text{maximum allowable hoop tension at the} \\ \text{interior of the cylinder}; \\ p = \text{intensity of interior pressure}. \end{array}$$

Merriman gives

s =unit stress at inner edge of the annulus; r =interior radius; t =thickness;

The total interior pressure which tends to rupture the cylinder is 2rl-p. If p be the unit pressure, then  $p=\frac{st}{r+t}$ , from which one of the quantities  $s,\,p,\,r,\,$  or t can be found when the other three are given.

$$s = \frac{p(r+t)}{t}; \qquad r = \frac{(s-p)t}{p}; \qquad t = \frac{rp}{s-p}.$$

In eq. (1), if t be neglected in comparison with r, it reduces to 2slt, which is the same as the formula for thin cylinders. If t=r, it becomes slt, or only half the resistance of the thin cylinder.

only han the resistance of the finit cyninder.

The formulæ given by Burr and by Merriman are quite different, as will be seen by the following example: Let maximum unit stress at the inner edge of the annulus = 8000 lbs. per square inch, radius of cylinder = 4 inches, interior pressure = 4000 lbs. per square inch. Required the thickness.

By Burr, 
$$t = 4\left\{ \left( \frac{8000 + 4000}{8000 - 4000} \right)^{\frac{1}{2}} - 1 \right\} = 4 \left( \sqrt[4]{3} - 1 \right) = 2.928 \text{ inches.}$$

By Merriman, 
$$t = \frac{4 \times 4000}{8000 - 4000} = 4$$
 inches.

Limit to Useful Thickness of Hollow Cylinders (Eng'g, Jan. 4, 1884).—Professor Barlow lays down the law of the resisting powers

of thick cylinders as follows:
"In a homogeneous cylinder, if the metal is incompressible, the tension on every concentric layer, caused by an internal pressure, varies inversely as the square of its distance from the centre."

Suppose a twelve-inch gun to have walls 15 inches thick.

$$\frac{\text{Pressure on exterior}}{\text{Pressure on interior}} = \frac{6^2}{21^2} = 1:12.25.$$

So that if the stress on the interior is 121/4 tons per square inch, the stress

on the exterior is only 1 ton. Let s = the stress on the inner layer, and  $s_1$  that at a distance x from the axis; r = internal radius, R = external radius.

$$s_1: s:: r^2: x^2$$
, or  $s_1 = s \frac{r^2}{r^2}$ .

The whole stress on a section 1 inch long, extending from the interior to the exterior surface, is  $S = sr \times \frac{R - r}{R}$ .

In a 12-inch gun, let s = 40 tons, r = 6 in., R = 21 in.

$$s = 40 \times 6 \times \frac{21 - 6}{21} = 172$$
 tons.

Suppose now we go on adding metal to the gun outside: then R will become so large compared with r, that R-r will approach the value R, so that the fraction  $\frac{R-r}{R}$  becomes nearly unity.

Hence for an infinitely thick cylinder the useful strength could never exceed Sr (in this case 240 tons).

Barlow's formula agrees with the one given by Merriman.

Another statement of the gun problem is as follows: Using the formula

$$p = \frac{st}{r+t},$$

 $s = 40 \text{ tons}, t = 15 \text{ in.}, r = 6 \text{ in.}, p = \frac{40 \times 15}{21} = 28 \text{ tons per sq. in.}, 28 \text{ $\frac{1}{2}$} \times$ radius = 172 tons, the pressure to be resisted by a section 1 inch long of the thickness of the gun on one side. Suppose thickness were doubled, making t=30 in.:  $p=\frac{40\times30}{36}=33\%$  tons, or an increase of only 16 per cent.

For short cast-iron cylinders, such as are used in hydraulic presses, it is doubtful if the above formulæ hold true, since the strength of the cylindrical portion is reinforced by the end. In that case the bursting strength would be higher than that calculated by the formula. A rule used in practice for such presses is to make the thickness = 1/10 of the inner circumference, for pressures of 3000 to 4000 lbs. per square inch. The latter pressure would bring a stress upon the inner layer of 10,330 lbs, per square inch, as calculated by the formula; which would necessitate the use of the best charcoal-iron to make the press reasonably safe.

#### THIN CYLINDERS UNDER TENSION.

Let p = safe working pressure in lbs. per sq. in.:

d = diameter in inches; T = tensile strength of the material, lbs. per sq. in.;

t =thickness in inches;

f = factor of safety; c = ratio of strength of riveted joint to strength of solid plate.

$$fpd=2Ttc; \ \ p=\frac{2Ttc}{df}; \ \ t=\frac{fpd}{2\,Tc}.$$

If T = 50000, f = 5, and c = 0.7; then

$$p = \frac{14000t}{d}$$
;  $t = \frac{dp}{14000}$ .

The above represents the strength resisting rupture along a longitudinal seam. For resistance to rupture in a circumferential seam, due to pressure

seam. For resistance to rupture in  $\frac{\partial r}{\partial t} = \frac{T t \pi dc}{f}$ ; on the ends of the cylinder, we have  $\frac{p \pi d^2}{4} = \frac{T t \pi dc}{f}$ ;

whence 
$$p = \frac{4Ttc}{df}$$
.

Or the strength to resist rupture around a circumference is twice as great as that to resist rupture longitudinally; hence boilers are commonly single-riveted in the circumferential seams and double-riveted in the longitudinal seams

#### HOLLOW COPPER BALLS.

Hollow copper balls are used as floats in boilers or tanks, to control feed

Hollow copper balls are used as noats in bollers or tanks, to control feed and discharge valves, and regulate the water-level.

They are spun up in halves from sheet copper, and a rib is formed on one half. Into this rib the other half fits, and the two are then soldered or brazed together. In order to facilitate the brazing, a hole is left on one side of the ball, to allow air to pass freely in or out; and this hole is made use of afterwards to secure the float to its stem. The original thickness of the metal may be anything up to about 1-16 of an inch, if the spinning is done on a hand lathe, though thicker metal may be used when special machinery is provided for forming it. In the process of spinning, the metal is thinned is provided for forming it. In the process of spinning, the metal is thinned down in places by stretching; but the thinnest place is neither at the equator of the ball (i.e., along the rib) nor at the poles. The thinnest points lie along two circles, passing around the ball parallel to the rib, one on each side of it, from a third to a balf of the way to the poles. Along these lines the thickness may be 10, 15, or 20 per cent less than elsewhere, the reduction depending somewhat on the skill of the workman.

The Locomotive for October, 1891, gives two empirical rules for determining the chickness of a copper ball which is to work under an external

pressure, as follows:

1. Thickness = diameter in inches × pressure in pounds per sq in. 16,000

2, Thickness = diameter × √pressure

These rules give the same result for a pressure of 166 lbs. only. Example: Required the thickness of a 5-inch copper ball to sustain

166 Pressures of ..... 100 150 250 lbs. per sq. in. Answer by second rule .0285 .0403 .0494 .0518 .0570 .0637

#### HOLDING-POWER OF NAILS, SPIKES, AND SCREWS.

(A. W. Wright, Western Society of Engineers, 1881.)

 Spikes.—Spikes driven into dry cedar (cut 18 monus).

 Size of spikes.
  $5 \times 14$  in, sq.  $6 \times 14$   $6 \times 16$   $5 \times 36$  

 Size of spikes.
 44 in, 5 in, 5 in, 5 in, 41 in, 10 100 1159 923 2129 1556 766 1120 766

A. M. Wellington found the force required to draw spikes 9/16 × 9/16 in., driven 41/4 inches into seasoned oak, to be 4281 lbs.; same spikes, etc., in un-

seasoned oak, 6523 lbs.
"Professor W. R. Johnson found that a plain spike 3% inch square driven 3% inches into seasoned Jersey yellow pine or unseasoned chestnut required about 2000 lbs. force to extract it; from seasoned white oak about 4000 and from well-seasoned locust 6000 lbs."

Experiments in Germany, by Funk, give from 2465 to 3940 lbs. (mean of Experiments in Germany, by Funk, give from 2465 to 3940 lbs. (mean of many experiments about 3000 lbs.) as the force necessary to extract a plain ½-inch square iron spike 6 inches long, wedge-pointed for one inch and driven 4½ inches into white or yellow pine. When driven 5 inches the force required was about 1/10 part greater. Similar spikes 9/16 inches square, 7 inches long, driven 6 inches deep, required from 3700 to 6745 lbs. to extract them from pine; the mean of the results being 4873 lbs. In all cases about twice as much force was required to extract them from oak. The spikes were all driven across the grain of the wood. When driven with the grain, spikes or nails do not hold with more than half as much force.

Boards of ask or pine nailed together by from 4 to 16 tengany common out.

Boards of oak or pine nailed together by from 4 to 16 tenpenny common cut nails and then pulled apart in a direction lengthwise of the boards, and across the nails, tending to break the latter in two by a shearing action, averaged about 300 to 400 lbs. per nail to separate them, as the result of

many trials. Resistance of Drift-bolts in Timber.—Tests made by Rust and

Coolidge.	, in 1878.												
tet Teet	1 in. square	iron	drove	20	in	in	white	nina	15/16	in	holo	Pound	
2d "	1 in, round	11011	uiove		**		Willite	pine,	13/16			16,80	
3d "	1 in. square	66	44		44		66	66	15/16			14,60	
4th "	1 in. round	66	64		44		46	66	13/16			13,20	no
5th "	1 in. round	46	44	34	44	66	Norw'v	nine	.13/16	i-in.	66	18,7:	20
6th "	1 in, square	66	4.6	30	66	66	"	2.6	15/16	in.	66	19,20	00
7th "	1 in. square		66	18	66	66	66	66	15/16	3-in.		15,60	
8th "	1 in. round	44	4.6	22	"	46	6.6	6.6	13/16	-in.		14,40	

Note.—In test No. 6 drift-bolts were not driven properly, holes not being in line, and a piece of timber split out in driving.

Force required to draw Screws out of Norway Pine. 1/4" diam. drive screw 4 in. in wood. Power required, average 2424 lbs. 4 threads per in. 5 in. in wood. 2743 66 44 44 66 2730 44 1465 66. 2026 46 66 1/2 inch R.R. spike...

Force required to draw Wood Screws out of Dry Wood. Tests made by Mr. Bevan. The screws were about two inches in length, .22 diameter at the exterior of the threads, .15 diameter at the bottom, the depth of the worm or thread being .035 and the number of threads in one depin of the worm of thread being so and the number of threads in one inch equal 12. They were passed through pieces of wood balf an inch in thickness and drawn out by the weights stated: Beech, 400 lbs.; and, 700 lbs.; blbs.; dea, 760 lbs.; and, 700 lbs.; and, 760 lbs.; and, 760 lbs.; and, 760 lbs.; and, 760 lbs.; and 760 lbs.; and, 760 lbs.; and,

Kind of Wood.	Size Screw.	Size Hole bored.	Length in Tie.	Max. Resist. lbs.	No. Tests.
Seasoned white oak	5% in.	7/16 ''.	41/2 in.	8037	3
	9/16 "	7/16 "	3′~ ''	6480	1
	5% "	3/6 "	41/2 "	8780	2
Yellow-pine stick	5% "	18 "	4 " "	3800	2
White cedar, unseasoned	58	12 "	4 "	3405	2

In figuring area for lag-screws, the surface of a cylinder whose diameter is equal to that of the screw was taken. The length of the screw part in each case was 4 inches.—Engineering News, 1891.

Cut versus Wire Nalls.—Experiments were made at the Watertown

Arsenal in 1893 on the comparative direct tensile adhesion, in pine and spruce, of cut and wire nails. The results are stated by Prof. W. H. Burr as follows:

There were 58 series of tests, ten pairs of nails (a cut and a wire nail in each) being used, making a total of 1150 nails drawn. The tests were made in spruce wood in most instances, but some extra ones were made in white pine, with 'box nails'. The nails were of all sizes, varying from 1½ inches to 6 inches in length. In every case the cut nails showed the superior holding strength by a large percentage. In spruce, in nine different sizes of nails, both standard and light weight, the ratio of tenacity of cut to wire nail was about 3 to 2, or, as he terms it, "a superiority of 47,455 of the former. With the "finishing" nails the ratio was roughly 3.5 to 2; superiority 72%. With box nails (1½ to 4 inches long) the ratio was roughly 3 to 2; superiority 75%. The mean superiority in spruce wood was 61%. In white pine, cut nails, driven with taper along the grain, showed a superiority of 100%, and with taper across the grain of 135%. Also when the nails were driven in the end of the stick, i.e., along the grain, the superiority of cut nails was 100%, or the ratio of cut to wire was 2 to 1. The total of the results showed the ratio of tenacity to be about 3,2 to 2 for the harder wood, and about 2 to 1 for the softer, and for the whole taken together the ratio was 3,5 to 2. We are led to conclude that under these circumstances the cut nail is superior to the wire nail in direct tensle holding-nower by 72,74%.

#### Nail-holding Power of Various Woods.

(Watertown Experiments.)

Kind of	Wood,	Size of Nail.	Holding-power per square inch of Surface in Wood, lbs.						
			Wire	Nail,	Cut Nail.	Mean.			
White pine		8d , 9 " , 20 " 50 "	- 16	87	450 455 477 347 363 340	405			
Yellow pine.		8 " 10 " 50 " 60 "	- 31	18 {	695 755 596 604	662			
White oak	{	8 '' 20 '' 60 ''	94	40 {	1340 1292 1018	1216			
Chestnut	{	50 '' 60 ''			664 702	683			
Laurel		9 " }	- 68	51 {	1179 1221	1200			

## Nail-holding Power of Various Woods.

(F W Clay's Evneriments Fug'a Name In 11 1804)

(F. W. Clay & Experiments. En				
Wood.	T	enacity o	f 6d nai	ils——
	Plain,	Barbed,	Blued.	Mean.
White pine:	106	94	135	-111
Yellow pine	190	130	270	196
Basswood	78	132	219	143
White oak	226	300	555	360
Hemlock (	141	201 .	319	990

Tests made at the University of Illinois gave the resistance of a 1-in, round rod in a 15/16-inch hole perpendicular to the grain, as 6000 lbs. per lin, ft. in pine and 15,000 lbs. in oak, Experiments made at the East River Bridge gave resistances of 12,000 and 15,000 lbs. per lin, ft. for a 1-in, round rod in holes 15/16-in, and 14/16-in, diameter, respectively, in Georgia pine.

# Holding-power of Bolts in White Pine,

(Eng'a News, September 26, 1891.)

	Round.	Square.
	Lbs.	Lbs.
Average of all plain 1-in, bolts	8224	8200
Average of all plain bolts, % to 11/4 in	7805	8110
Average of all bolts	8383	8598

Round drift-bolts should be driven in holes 13/16 of their diameter, and square drift-bolts in holes whose diameter is 14/16 of the side of the square.

#### STRENGTH OF WROUGHT IRON BOLTS.

(Computed by A. F. Nagle.)

	w.	g .		Stress u	pon Bolt	upon I		
Diameter of Bolt, Inches.  Number of Threads.	Diameter of Bottom of Thread, Inches.	Area at Bottom of Thread, Square Inches.	g 3000 lbs. per sq. inch.	eg 4000 lbs. per sq. inch.	g 5000 lbs. per sq. inch.	g 7000 lbs. per sq. inch.	g 10000 lbs. per sq. inch.	Probable graking Froad.
1 1	.38 .44 .49 .60 .71 .81 .91 1.04 1.12 1.25 1.35 1.45 1.57 1.66 1.92 2.12 2.37 2.57 3.04	.12 .15 .19 .28 .39 .52 .65 .84 1.03 1.23 1.44 1.65 2.18 2.88 3.55 4.43 5.20 7.25 9.62	350 450 560 750 1180 1950 2520 3000 3680 4300 5840 6540 6540 10640 11290 11580 11760 28860	460 600 750 1130 1570 2070 2600 3360 4910 5740 6600 7800 11530 14200 20770 29070 29070	580 750 930 1410 1970 2600 3250 4200 6140 7180 9800 14400 117730 26000 36260 36260 48100	810 1050 1310 1980 2760 3630 4560 5900 7000 10000 11560 20180 24830 36360 50760 67350	1160 1500 1870 2830 3940 5180 6510 8410 10000 12280 14360 21800 21800 52800 52000 72500	5800 7500 9000 14000 19000 25000 30000 39000 46000 56000 65000 74000 85000 125000 125000 130000 213000 213000 2390000

When it is known what load is to be put upon a bolt, and the judgment of the engineer has determined what stress is safe to put upon the iron, look down in the proper column of said stress until the required load is found. The area at the bottom of the thread will give the equivalent area of a flat bar to that of the bolt.

Effect of Initial Strain in Bolts,—Suppose that bolts are used to connect two parts of a machine and that they are screwed up tightly before the effective load comes on the connected parts. Let  $P_1 =$  the initial tension on a both due to screwing up, and  $P_2 =$  the load afterwards added. The greatest load may vary but little from  $P_1$  or  $P_2$ , according as the former or the latter is greater, or it may approach the value  $P_1 + P_2$ , depending upon the relative rigidity of the bolts and of the parts connected. Where rigid flanges are bolted together, metal to metal, it is probable that the extension of the bolts with any additional tension relieves the initial tension, and that the total tension is  $P_1$  or  $P_2$ , but in cases where elastic packing, as india rubber, is interposed, the extension of the bolts may very little affect the initial tension, and the total strain may be nearly  $P_1 + P_2$ . Since the latter assumption is more unfavorable to the resistance of the bolt, this contingency should usually be provided for. (See Unwin, "Elements of Machine Design "for demonstration.)

#### STAND-PIPES AND THEIR DESIGN.

(Freeman C. Coffin, New England Water Works Assoc., Eng. News, March (6, 1893.) See also papers by A. H. Howland, Eng. Club of Phill. 1887; B. F. Stephens, Amer. Water Works Assoc., Eng. News, Oct. 6 and 13, 1888; W. Kiersted, Rensealer Soc. of Civil Eng., Eng. News, Oct. 6 and 13, 1888; W. 1894, and W. D. Pence, Eng. News, April and May, 1894.

The question of diameter is almost entirely independent of that of height, The efficient capacity must be measured by the length from the high-water

The question of diameter is almost entirely independent of that of height. The efficient capacity must be measured by the length from the high-water line to a point below which it is undesirable to draw the water on account of loss of pressure for fire-supply, whether that point is the actual bottom of the stand-pipe or above it. This allowable fluctuation ought not to exceed 50 ft., in most cases. This makes the diameter dependent upon two condi-

tions, the first of which is the amount of the consumption during the ordimany interval between the stopping and starting of the pumps. This should never draw the water below a point that will give a good fire stream and leave a margin for still further draught for fires. The second condition is the maximum number of fire streams and their size which it is considered necessary to provide for, and the maximum length of time which they are liable to have to run before the pumps can be relied upon to reinforce

Another reason for making the diameter large is to provide for stability

against wind-pressure when empty.

The following table gives the height of stand-pipes beyond which they are not safe against wind-pressures of 40 and 50 lbs. per square foot. The area of surface taken is the height multiplied by one half the diameter.

#### Heights of Stand-pipe that will Resist Wind-pressure by its Weight alone, when Empty.

Diameter,	Wind, 40 lbs.	Wind, 50 lt
feet.	per sq. ft.	per sq. ft.
20	45	35
25	70	55
30	150	80
35		160

To have the above degree of stability the stand-pipes must be designed

with the outside angle-iron at the bottom connection.

Any form of anchorage that depends upon connections with the side Any form of actionage and depends upon confections with the sad-plates near the bottom is unsafe. By suitable guys the wind-pressure is re-sisted by tension in the guys, and the stand-plpe is relieved from wind strains that tend to overthrow it. The guys should be attached to a band of angle or other shaped iron that completely encircles the tank, and rests upon some sort of bracket or projection, and not be riveted to the tank. They should be anchored at a distance from the base equal to the height of the point at which they are attached, if possible.

The best plan is to build the stand-pipe of such diameter that it will resist

the wind by its own stability.

#### Thickness of the Side Plates.

The pressure on the sides is outward, and due alone to the weight of the The pressure on the saces is outward, and due alone to the weight of the water, or pressure per square inch, and increases in direct ratio to the height, and also to the diameter. The strain upon a section I inch in height at any point is the total strain at that point divided by two—for each side is supposed to bear the strain equally. The total pressure at any point is equal to the diameter in inches, multiplied by the pressure per square inch, due to the height at that point. It may be expressed as follows:

H = height in feet, and f = factor of safety;

d = diameter in inches;

p =pressure in lbs. per square inch; .434 = p for 1 ft. in height;

s = tensile strength of material per square inch; T = thickness of plate.

Then the total strain on each side per vertical inch

$$=\frac{.434Hd}{2}=\frac{pd}{2}; \qquad T=\frac{.434Hdf}{2s}=\frac{pdf}{2s}.$$

Mr. Coffin takes f = 5, not counting reduction of strength of joint, equivalent to an actual factor of safety of 3 if the strength of the riveted joint is taken as 60 per cent of that of the plate.

The amount of the wind strain per square inch of metal at any joint can be found by the following formula, in which

H = height of stand-pipe in feet above joint;

T =thickness of plate in inches;

p = wind-pressure per square foot:
 W = wind-pressure per foot in height above joint;

W = Dp where D is the diameter in feet; m =average leverage or movement about neutral axis

or central points in the circumference; or,  $m = \text{sine of } 45^{\circ}$ , or .707 times the radius in feet.

Then the strain per square inch of plate

$$= \frac{(Hw)\frac{H}{2}}{\text{circ, in ft, } \times mT}.$$

Mr. Coffin gives a number of diagrams useful in the design of stand-pipes, together with a number of instances of failures, with discussion of their

probable causes. Mr. Kiersted's paper contains the following: Among the most prominent strains a stand-pipe has to bear are: that due to the static pressure of the water, that due to the overturning effect of the wind on an empty standpipe, and that due to the collapsing effect, on the upper rings, of violent wind storms.

For the thickness of metal to withstand safely the static pressure of

water, let

t =thickness of the plate iron in inches;

H = height of stand-pipe in feet;D = diameter of stand-pipe in feet.

Then, assuming a tensile strength of 48,000 lbs, per square inch, a factor of safety of 4, and efficiency of double-riveted lap-joint equalling 0.6 of the strength of the solid plate,

$$t = .00036H \times D;$$
  $H = \frac{10,000t}{3.6D};$ 

which will give safe heights for thicknesses up to 5% to 34 of an inch. The same formula may also apply for greater heights and thicknesses within practical limits, if the joint efficiency be increased by triple riveting. The conditions for the severest overturning wind strains exist when the

stand-pipe is empty.

Formula for wind-pressure of 50 pounds per square foot, when

d = diameter of stand-pipe in inches;

x = any unknown height of stand-pipe:  $x = \sqrt{80\pi dt} = 15.85 \sqrt{dt}$ 

The following table is calculated by these formulæ. The stand-pipe is intended to be self-sustaining; that is, without guys or stiffeners.

### Heights of Stand-pipes for Various Diameters and Thicknesses of Plates.

	Zaromiosses of Zames.												
Thickness of		Diameters in Feet.											
Plate in Frac- tions of an Inch.	5	6	7	8	9	10	12	14	15	16	18	20	25
3-16	50 55	55	60	65	55 65	50 60	35 50						
4-16	60 70	65 75	70 80	75 85	75 90	70 85	55 70	50 60	45 55	40 50	35 45	35 40	25 35
6-16 7-16	75 80	80 90	90 95	95 100	100 110	100 115	85 100	75 85	70 80	65 75	55 65	50 60	40
8-16 9-16	85	95	100	110 115	115 125	120 130	115 130	100 110		85 95	75 85	70 80	55 60
10-16 11-16				:::.	130	135 145	145 155	120 135	115 125	105 120	95 105	95	65 75
12-16						150	165	145 160	135 150 160	130 140 150	115 125 135	105 110 120	80 90 95
14–16 15–16 16–16										160	145 155	130 140	105 110

Heights to nearest 5 feet. Rings are to build 5 feet vertically.

Failures of Stand-pipes have been numerous in recent years. list showing 23 important failures inside of nine years is given in a paper by Prof. W. D. Pence, Eng'g News, April 5, 12, 19 and 20, May 3, 10 and 24, and June 7, 1894. His discussion of the probable causes of the failures is most valuable.

Kenneth Allen, Engineers Club of Philadelphia, 1886, gives the following

Kenneth Allen, Engineers (2000 of Finladelphia, 1880, gives the following rules for thickness of plates for stand pipes. Assume: Wrought iron plate T. S. 48,000 pounds in direction of fibre, and T. S. 45,000 pounds across the fibre. Strength of single riveted joint 4 that of the plate, and of double riveted joint, 7 that of the plate; wind pressure = 50 pounds per square foot; safety factor = 3.

Let h = total height in feet; r = outer radius in feet; r' = inner radius

in feet; p = pressure per square inch; t = thickness in inches; d = outer diameter in feet.

Then for pipe filled and longitudinal seams double riveted

$$t = \frac{pr \times 12}{48,000 \times .7 \times \frac{1}{3}} = \frac{hd}{4301};$$

and for pipe empty and lateral seams, single riveted, we have by equating

$$50\times 2r\;\Big(\frac{h}{2}\Big)^2=144\times 6000\;(r^4-r'^4)\;\frac{.7854}{r}, \text{whence}\;\;r^4-r'^4=\frac{h^2\;r^2}{27144}.$$

# Table showing required Thickness of Bottom Plate.

Height in	Diameter.									
Feet.	5 feet. 10 feet.		15 feet.	20 feet.	25 feet.	30 feet.				
50 60 70 80 90 100 • 125 150 175 200	" + 7-64* +11-64* + 7-32 +19-64 + 38 +29-64	16 * 9-64* 11-64* 3-16 7-32 15-64 11-16 123-64 111-16 129-32	77 11-64* 7-32 14 9-32 5-16 23-64 7-16 17-32 39-64 45-64	15-64 9-32 21-64 34 27-64 15-32 37-64 45-64 13-16	19-64 23-64 13-32 15-32 17-32 37-64 47-64 78 1 1-32 1 11-64	23-64 27-64 31-64 9-16 58 45-64 7/8 1 3-64 1 7-32 1 25-64				

\* The minimum thickness should = 3-16".

N.B.—Dimensions marked † determined by wind-pressure.

Water Tower at Yonkers, N. Y.—This tower, with a pipe 12? feet hand 20 feet diameter, is described in Engineering News, May 18, 1892. The thickness of the lower rings is 11-16 of an inch., based on a tensile strength of 60,000 lbs. per square then of metal, allowing 5% for the strength of the fiveted joints, using a factor of safety of 3% and adding a constant of % inch. The plates diminish in thickness by 1-16 inch to the last four

plates at the top, which are 1/4 inch thick.

plates at the top, which are 44 inch thick.

The contract for steel requires an elastic limit of at least 33,000 lbs, per square inch; an ultimate tensile strength of from 56,000 to 66,000 lbs, per square inch; an elongation in 8 inches of at least 20%, and a reduction of area of at least 45%. The inspection of the work was made by the Pittsburgh Testing Laboratory. According to their report the actual conditions developed were as follows: Flastic limit from 34,020 to 39,420; the tensile strength from 58,320 to 65,390; the elongation in 8 inches from 234,00 to 32%; reduction in area from 52.72 to 71.32%; 17 plates out of 141 were rejected in the inspection. the inspection.

#### WROUGHT-IRON AND STEEL WATER-PIPES.

Riveted Steel Water-pipes (Engineering News, Oct. 11, 1890, and Ang. 1, 1891).—The use of riveted wrought-iron pipe has been common in the Padfile States for many years, the largest being a 44-inch conduit in connection with the works of the Spring Valley Water Co., which supplies San Francisco. The use of wrought iron and steel pipe has been necessary in the West, owing to the extremely high pressures to be withstood and the difficulties of transportation. As an example: In commection with

the water supply of Virginia City and Gold Hill, Nev., there was laid in 1872 an 1116-inch riveted wrought-iron pipe, a part of which is under a head

of 1720 feet.

In the East, the most important example of the use of riveted steel water pipe is that of the East Jersey Water Co., which supplies the city of Newark. The contract provided for a maximum high service supply of 25,000,000 gallons daily. In this case 21 mues of 48-inch pipe was laid, some of it under 340 feet head. The plates from which the pipe is made are about 13 feet long by 7 feet wide, open-hearth steel. Four plates are used to make one section of pipe about 27 feet long. The pipe is riveted longitudinally with a double row, and at the end joints with a single row of rivets of varying diameter, corresponding to the thickness of the steel plates. Before being rolled into the trench, two of the 27-feet lengths are riveted together, thus diminishing still further the number of joints to be made in the trench and the extra excavation to give room for jointing. All changes in their and the extra line are made by 10° curves and all changes in line by 2½, 5, 7½ and 10° curves. To lay on curved lines a standard bevel was used, and the different curves are secured by varying the number of beveled joints used on a certain length of pipe.

The thickness of the plates varies with the pressure, but only three thicknesses are used, 14, 5-16, and 34 inches, the pipe made of these thicknesses having a weight of 160, 185, and 225 lbs. per foot, respectively. At the works

all the pipe was tested to pressure 134 times that to which it is to be sub-jected when in place.

Mannesmann Tubes for High Pressures.—At the Mannesmann Works at Komotau, Hungary, more than 600 tons or 25 miles of 3-inch and 4-inch tubes averaging 14 inch in thickness have been successfully tested to a pressure of 2000 lbs. per square inch. These tubes were intended for a high-pressure water-main in a Chilian nitrate district.

This great tensile strength is probably due to the fact that, in addition to being much more worked than most metal, the fibres of the metal run spirally, as has been proved by microscopic examination. While cast-iron tubes will hardly stand more than 200 lbs, per square inch, and welded tubes are not safe above 1000 lbs. per square inch, the Mannesmann tube easily withstands 2000 lbs. per square inch. The length up to which they can be readily made is shown by the fact that a coil of 3-inch tube 70 feet long was made recently.

For description of the process of making Mannesmann tubes see Trans.

A. I. M. E. vol. xix., 384.

#### STRENGTH OF VARIOUS MATERIALS. EXTRACTS FROM KIRKALDY'S TESTS.

The recent publication, in a book by W. G. Kirkaldy, of the results of many thousand tests made during a quarter of a century by his father, David Kirkaldy, has made an important contribution to our knowledge concerning the range of variation in strength of numerous materials. A condensed abstract of these results was published in the American Machinist, May 11 and 18, 1893, from which the following still further condensed extracts are

taken:

The figures for tensile and compressive strength, or, as Kirkaldy calls them, pulling and thrusting stress, are given in pounds per square inch of original section, and for bending strength in pounds of actual stress or pounds per  $BD^2$  (breadth  $\times$  square of depth) for length of 36 inches between supports. The contraction of area is given as a percentage of the original area, and the extension as a percentage in a length of 10 inches, except when otherwise stated. The abbreviations T. S., E. L., Contr., and Ext. are used for the sake of brevity, to represent tensile strength, elastic limit, and percentages of contraction of area, and elongation, respectively

Cast Iron.-44 tests: T. S. 15,468 to 28,740 pounds; 17 of these were unsound, the strength ranging from 15,468 to 24,357 pounds. Average of all,

23,805 pounds.

23,005 pounds. Thrusting stress, specimens 2 inches long, 1.34 to 1.5 in, diameter; 43 tests, all sound, 94,352 to 131,912; one, unsound, 93,759; average of all, 113,825, Bending stress, bars about 1 in, wide by 2 in deep, cast on edge. Ultimate stress 2876 to 3854; stress per  $BP^2 = 725$  to 892; average, 830. Average modulus of rupture, R, e stress per  $BP^2$  Length, = 29,520. Ultimate deflection, .29 to 40 in.; average .34 inch. Other tests of cast iron, 460 tests, 16 lots from various sources, gave re-

sults with total range as follows: Pulling stress, 12,688 to 33,616 pounds; thrusting stress, 66,363 to 175,950 pounds; bending stress, per  $BD^2$ , 505 to 1128 pounds; modulus of rupture, R, 18,180 to 40,608. Ultimate deflection, .21 to .45 inch.

The specimen which was the highest in thrusting stress was also the highest in bending, and showed the greatest deflection, but its tensile strength was only 26,502,

The specimen with the highest tensile strength had a thrusting stress of 143,939, and a bending strength, per  $BD^2$ , of 979 pounds with 0.41 deflection. The specimen lowest in T. S. was also lowest in thrusting and bending, but gave .38 deflection. The specimen which gave .21 deflection had T. S., 19,188; thrusting, 104.281; and bending, 561.

Iron Castings.-69 tests; tensile strength, 10,416 to 31,652; thrusting

ron Castings.—69 tests; tensile strength, 10,416 to 31,652; thrusting stress, utlimate per square inch, 53.502 to 132,031.

Channel Irons.—Tests of 18 pieces cut from channel irons. T. S. 40,693 to 53,141 pounds per square inch; contr. of area from 3,9 to 32,5 %. Ext. in 10 in, from 2.1 to 22.5 %. The fractures ranged all the way from 10.6 fbrons to 10.9 % crystalline. The highest T. S., 53,141, with 8.1 % contr. and 5.3 % ext., was 10.9 % crystalline; the lowest T. S., 40,693, with 3.9 contr. and 2.1 % ext., was 75 % crystalline. The librous irons showed from 12,2 to 22.5 % ext., 17,3 to 32.5 contr. and T. S. from 43,426 to 49,615. The fibrous irons showed from the control of the contro irons are therefore of medium tensile strength and high ductility. T crystalline irons are of variable T. S., highest to lowest, and low ductility.

crystalline irons are of variable T. S., highest to lowest, and low ductility.

Lowmoor Iron Bars.—Three rolled bars 2½ inches diameter; tensile tests: elastic, 23,200 to 42,00; ultimate, 50,875 to 51,905; contraction, 41.4 to 42.5; extension, 29.2 to 24.3. Three hammered bars, 4½ inches diameter, elastic 25,100 to 24,200; ultimate, 46,810 to 49,223; contraction, 20.7 to 46.5; extension, 10.8 to 31.6. Fractures of all, 100 per cent fibrous. In the hammered bars the lowest T. S. was accompanied by lowest ductility.

Iron Bars, Various. -Of a lot of 80 bars of various sizes, some rolled and some hammered (the above Lowmoor bars included) the lowest T. S. ckeept one) 40,808 pounds per square inch, was shown by the Swedish "hoop L" bar 3¼ inches diameter, rolled. Its elastic limit was 19,150 pounds; contraction 68.7% and extension 37.7% in 10 inches. It was also the most ductile of all the bars tested, and was 100% florous. The highest pounds; contraction 68.7% and extension 37.7% in 10 inches. It was also the most ductile of all the bars tested, and was 100 % florous. The highest T. S., 60,789 pounds, with elastic limit, 39,400; contr., 36.6; and ext., 24.3%, was shown by a "Farnley" 2-inch bar, rolled. It was also 100 % florous. The lowest ductility 2.6 % contr., and 4.1% ext., was shown by a 3%-inch hammered bar, without brand. It also had the lowest T. S., 40,278 pounds, but rather high elastic limit, 25,700 pounds, Its fracture was 95 % crystalline. Thus of the two bars showing the lowest T. S., one was the most ductility. It is a shown that the short of the short ductility is ductile in the whole sense of 80 bars ductiled in the whole sense of 80 bars in the Swedish bors. But the Earlyle's lower showed a combination of lacts, as in the

Swedish bars, but the Farnley bars showed a combination of high ductility

and high tensile strength

Locomotive Forgings, Iron. -17 tests: average, E. L., 30,420; T. S., 50.521; contr., 36.5; ext. in 10 inches, 23.8.

Broken Anchor Forgings, Iron.-4 tests: average, E. L., 23,825; T. S , 40,083; contr., 3.0; ext. in 10 inches, 3.8.

T. S., 40,083; contr., 3.0; ext. in 10 inches, 3.8.

Kirkaldy places these two irons in contrast to show the difference between good and bad work. The broken anchor material, he says, is of a most treacherous character, and a disgrace to any manufacturer.

Iron Plate Girder.—Tensile tests of pieces cut from a riveted iron girder after twenty years' service in a railway bridge. Top plate, average of 3 tests, E. L., 25,000; T. S., 49,806; contr., 16 1; ext. in 10 inches, 7.8.

Bottom plate, average of 3 tests, E. L., 31,200; T. S., 44,288; contr., 13.3; ext. in 10 inches, 6.3. Web-plate, average of 3 tests, E. L., 25,000; T. S., 45,902; contr., 15 9; ext. in 10 inches, 8.9. Fractures all fibrous. The results of 30 systs from different parts of the girder prove that the iron has undergone ests from different parts of the girder prove-that the iron has undergone to change during twenty years of use.

**Steel Plates.**—Six plates 100 inches long, 2 inches wide, thickness various 3, 36 to .97 inch T. S., 55,485 to 60,805; E. L., 29,600 to 33,300; contr., 52,9 to 59,55 to 18.57.

Steel Bridge Links. -40 links from Hammersmith Bridge, 1886.

				in.	Frac	Fracture.	
Average of all	67,294 60,753 75,936 64,044 63,745 65,980 63,980	38,294 36,030 44,166 32,441 38,118 36,792 39,017	34.5% 30.1 31.2 34.7 52.8 40.8 6.0	14.11% 15.51 12.49 13.43 15.46 17.78 6.62	30% 15 30 100 35 0	0 0 0 65 100 Granular	

The ratio of elastic to ultimate strength ranged from 50.6 to 65.2 per cent; average, 56.9 per cent.

extension in lengths of 100 inches. At 10,000 lbs. per sq. in., .018 to .024; mean, .020 inch; at 20.000 lbs. per sq. in. .049 to .063; mean, .055 inch; at 30,000 lbs. per sq. in., .083 to .100; mean, .090; set at 30,000 pounds per sq. in., 0 to .002; mean, 0.

The mean extension between 10,000 to 30,000 bs, per sq. in. increased regularly at the rate of .007 inch for each 2000 lbs, per sq. in. increment of strain. This corresponds to a modulus of elasticity of 28,57,1,429. The least increase of extension for an increase of load of 20,000 lbs, per sq. in., .005 inch, corresponds to a modulus of elasticity of 30,769,231, and the greatest, .076 inch, to a modulus of 28,315,789.

Steel Rails.—Bending tests, 5 feet between supports, 11 tests of flange rails 72 pounds per yard, 4.63 inches high.

Hardest Softest	Pounds, 34,200 32,000	Ultimate stress. Pounds. 60,960 56,740 59,209	Deflection at 50,000 Pounds. 3.24 ins. 3.76 " 3.53 "	Ultimate Deflection 8 ins. 8 "
Mean	32,763	59,209	3.53 "	8 "

All uncracked at 8 inches deflection.

Pulling tests of pieces cut from same rails. Mean results.

Top of rails		Ultimate Pounds. per sq. in. 83,110	Contraction of area of frac- ture. 19.9%	Extension in 10 ins. 13.5%
Botton of rails	40,900	77,820	30.9%	22.8%

Steel Tires .- Tensile tests of specimens cut from steel tires.

#### Krupp Steel .- 262 Tests.

771 1	E. L.	T. S.	Contr.	5 inches.
Highest	69,250 52,869	119,079 104.112	31.9 29.5	18.1 19.7
Lowest	41,700	90,523	45.5	23.7

#### Vickers, Sons & Co.-70 Tests.

Highest	E. L. 58.600	T. S. 120,789	Contr.	Ext. in 5 inches. 8.4
Mean	51,066	101,264	17.6	12.4
Lowest	43,700	87,697	24.7	16.0

Note the correspondence between Krupp's and Vickers' steels as to tensite strength and elastic limit, and their great difference in contraction and elongation. The fractures of the Krupp steel averaged 22 per cent silky, 78 per cent granular; of the Vicker steel, 7 per cent silky, 93 per cent granular.

Ext. in

5 inches.

18 4

# Steel Axles.-Tensile tests of specimens cut from steel axles.

PATENT SHAFT AND AXLE TREE CO .- 157 Tests.

Highest Mean Lowest	E. L. 49,800 36,267 31,800	T. S. 99,009 72,099 61,382	Contr. 21.1 33.0 34.8	5 inches. 16.0 23.6 25.3
	VICKERS	Sons & Co	125 Tests.	Ext. in
	E. L.	T. S.	Contr.	5 inches.
Highest	42,600	83,701	18.9	13.2
Mean	37,618	70,572	41.6	27.5
Lowest	30,250	56,388	49.0	37.2

The average fracture of Patent Shaft and Axle Tree Co. steel was 33 per cent silky, 67 per cent granular.

The average fracture of Vickers' steel was 88 per cent silky, 12 per cent granular.

Tensile tests of specimens cut from locomotive crank axles. Vickers'. -- 82 Tests, 1879.

E. L.	T. S.	Contr.
Er. Lr.	1, 5.	Contr.
26 700	68 057	28.3

Mean	24.146	57,922	32.9	24.0
Lowest	21,700	50,195	52.7	36.2
	Vick	ers'78 Tests	. 1884.	
			,	Ext, in
	E. L.	T. S.	Contr.	5 inches.
Highest	27,600	64,873	27.0	20.8
Mean	23,573	56,207	32.7	25.9
Lowest	17,600	47,695	35.0	27.2
	FRIED.	Krupp43 Te	sts, 1889.	
				Ext. in
	E. L.	T. S.	Contr.	5 inches.
Highest	31.650	66.868	48.6	35.6
Mean	29,491	61,774	47.7	32.3
Lowest	21,950	55,172	55.8	35.6

Steel Propeller Shafts.—Tensile tests of pieces cut from two shafts, mean of four tests each. Hollow shaft, Whitworth T. S. 61,290; E. L., 90,575; contr., 52.8; ext. in 10 inches, 28 6. Solid Shaft, Vickers', T. S., 46,870; E. L. 29,425; contr., 44.4; ext. in 10 inches, 30.7.
Thrusting tests, Whitworth, ultimate, 56,201; clastic, 29,300; set at 30,000 lbs., 0.18 per cent; set at 40,000 lbs., 2.04 per cent; set at 50,000 lbs., 3.82 per

Thrusting tests, Vickers', ultimate, 44,602; elastic, 22,250; set at 30,000 lbs., 2.39 per cent; set at 40,000 lbs., 4.69 per cent.
Shearing strength of the Whitworth shaft, mean of four tests, was 40,654

Highest ....

Shearing strength of the whitworth shart, mean of four tests, was accounted by person of the Whitworth steel, 7:867; of the Vickers, 7:856.

Spring Steel, —Untempered, 6 tests, average, E. L., 67,916; T. S., 115,683; contr., 37.8; ext. in 10 inches, 16.6. Spring steel untempered, 15 tests, average, E. L. 87,85; T. S., 69,496; contr., 19.1; ext. in 10 inches, 29.8.

These two lots were shipped for the same purpose, viz., railway carriage test provides.

leaf springs. Steel Castings.—44 tests, E. L., 31,816 to 35,567; T. S., 54,928 to 63,840; contr., 1.67 to 15.8; ext., 1.45 to 15.1. Note the great variation in ductility.

The steel of the highest strength was also the most ductile.

# Riveted Joints, Pulling Tests of Riveted Steel Plates, Triple Riveted Lap Joints, Machine Riveted, Holes Drilled.

Plates, width and thickn ss, inches :  $13.00 \times .51$  $12.25 \times 1.01$  $13.50 \times .25$  $11.75 \times .78$  $14.00 \times .77$ Plates, gross sectional area square inches: 3.375 6.63 9,165 10.780 Stress, total, pounds: 332,640 423,180 528,000 455,210

42.227

52.6 to 82.1%

42.696

Stress per square inch of gross area, joint: 59.058 50.172 46.173

Stress per square inch of plates, solid:

	300 64,050	62,280	68,045
Ratio of strength of joint	to solid plate:	00 kg	02.00
83.46 76 Ratio net area of plate to		68.55	62.06
73.4 65	.5 62.7 .	64.7	72.9
Where fractured:	. 0	04.1	12.0
plate at plat	e at plate at	plate at	rivets
holes. hol	es. holes.		sheared.
Rivets, diameter, area an	d number:		
.45, .159, 24 .64, .	321, 21 .95, .708,	12 1.08, .916, 12	.95, .708, 12
Rivets, total area:	m14 0 100	40.000	0.400
		10.992	8,496
Strength of Welds	.—Tensile tests to	determine ratio o	f strength of
weld to solid bar.		m	
	IRON TIE BARS.—28		
Strength of solid bars va-	ried from	43,201	to 57,065 lbs.
Strenth of welded bars va	ried from	17,816	to 44,586 lbs.
Ratio of weld to solid vari			37.0 to 79.1%
	IRON PLATES7 T	ests.	
Strength of solid plate fro	om	44,851	to 47,481 lbs.
Strength of solid plate from Strength of welded plate	from	26,449	to 38,931 lbs.
Ratio of weld to solid			57.7 to 83.9%
	CHAIN LINKS216	Tests.	
Strength of solid bar from Strength of welded bar fr	n	49,122	to 57,875 lbs.
Strength of welded bar fr	ommo	39,575	to 48,824 lbs.
Ratio of weld to solid			72.1 to 95.4%
Iron Bars	-Hand and Electric	Machine Welded.	
32 tests, solid iron, averag	ge		
17 " electri welded, a	verage	46,8	336 ratio 89.1%
19 " hand "		46,8	89.3%
STEEL STEEL	BARS AND PLATES	s.—14 Tests.	1 000 4 - 04 500
Strength of solid		5	4,226 to 64,580
Strength of weld			8,553 to 46,019

The ratio of weld to solid in all the tests ranging from 37.0 to 95.4 is proof of the great variation of workmanship in welding.

Cast Copper.—4 tests, average, E. L., 5900; T. S., 24,781; ccutr., 24.5;

Ratio weld to solid .....

ext., 21.8.

Copper Plates.—As rolled, 22 tests, 26 to .75 in. thick; E. L., 9766 to 18,650; T. S., 30,93 to 34,281; contr., 31.1 to 57.6; ext., 39.9 to 52.2. The variation in elastic limit is due to difference in the heat at which the plates were finished. Annealing reduces the T. S. only about 1000 pounds, but the E. L. from 3000 to 7000 pounds.

Another series, .38 to .52 thick; 148 tests, T. S., 29,099 to 31,924; contr., 28.7 to 56.7; ext. in 10 inches, 28.1 to 41.8. Note the uniformity in tensile strength.

Strength.

Drawn Copper,—74 tests (0.88 to 1.08 inch diameter); T. S., 31,634 to 40.557; contr., 37.5 to 64.1; ext. in 10 inches, 5.8 to 48.2.

Bronze from a Propeller Blade.—Means of two tests each from centre and edge. Central portion (sp. gr. 8.320), E. L., 7550; T. S., 26,312; contr., 25.4; ext. in 10 inches, 32.8. Edge portion (sp. gr. 8550). E. L., 8950; T. S., 35,960; contr., 37.8; ext. in 10 inches, 47.9.

Cast German Silver.—10 tests: E. L., 12,400 to 29,100; T. S., 23,714 to 46,540; contr., 3.2 to 21.5; ext. in 10 inches, 0.6 to 10.2.

Thin Sheet Metal.-Tensile Strength. 
 German silver, 2 lots
 75,816 to 87,129

 Bronze, 4 lots.
 73,880 to 92,085

 Brass, 2 lots
 44,989 to 85,188

 Copper, 9 lots.
 30,470 to 48,450

 Iron, 13 lots, lengthway
 44,381 to 99,484

 Iron, 18 lots, crossway
 39,838 to 57,330

 Step 6 lots
 49,958 to 76,725
 

#### Wire \_Tensile Strength

TO I CON TO	
German silver, 5 lots	81,735 to 92,224
Bronze, 1 lot	
Brass, as drawn, 4 lots	
Copper, as drawn, 3 lots	
Copper annealed, 3 lots	34,936 to 45,210
Copper (another lot), 4 lots	35,052 to 62,190
Copper (extension 36.4 to 0.6%).	
Iron, 8 lots	59,246 to 97,908
Iron (extension 15.1 to 0.7%).	
Steel, 8 lots	03.272 to 318.823

The Steel of 318,823 T.S. was .047 inch diam., and had an extension of only 0.3 per cent; that of 103,372 T.S. was .107 inch diam. and had an extension of 2.2 per cent. One lot of .044 inch diam. had 367,114 T.S., and 5.2 per cent extension.

Wire Ropes. Selected Tests Showing Range of Variation.

	Circumference, inches.	per m.	Stra	inds.	of hes.		o q
Description.	umfere inches.	eight pe Fathom.	of ds.	ž.	Diameter of Wires, inches,	Hemp Core.	Ultimate Strength lbs.
	ing	Weight Fathor	No. of Strands.	No. of Wires.	am		Stre
	Sirc	1	St	ZP	ΩŅ		D 32
			_				
Galvanized	7.70	53.00	6	19	.1563	Main	339,780
Ungalvanized	7.00	53.10	7	19	.1495	Main and Strands	314,860
Ungalvanized	6.38	42.50	7	19	.1347	Wire Core	295,920
Galvanized	7.10	37.57	6	30	.1004	Main and Strands	272,750
Ungalvanized	6.18	40.46	7	19	.1302	Wire Core	268,470
Ungalvanized	6.19	40.33	7	19	.1316	Wire Core	221,820
Galvanized	4.92	20.86	6	30	.0728	Main and Strands	190,890
Galvanized	5.36	18.94	6	12	.1104	Main and Strands	136,550
Galvanized	4.82	21.50	6	7	.1693	Main	129,710
Ungalvanized	3.65	12.21	6	19	.0755	Main	110,180
Ungalvanized	3.50	12.65	7	7	.122	Wire Core	101,440
Ungalvanized	3.82	14.12	6	7	.135	Main	98,670
Galvanized	4.11	11.35	6	12	.080	Main and Strands	75,110
Galvanized	3.31	7.27	6	12	.068	Main and Strands	55,095
Ungalvanized	3.02	8.62	6	7	.105	Main	49,555
Ungalvanized	2.68	6.26	6	6	.0963	Main and Strands	41,205
Galvanized	2.87	5.43	6	12.	.0560	Main and Strands	38,555
Galvanized	2.46	3.85		12	.0472	Main and Strands	28,075
Ungalvanized	1.75	2.80	6	7	.0619	Main Main	24,552
Galvanized	2.04	2.72	6	12	.0378	Main and Strands Main	20,415
батуашией	1.76	1.85	0	12	.0305	nan	14,634
			)		1		•

Hemp Ropes, Untarred.—15 tests of ropes from 1.53 to 6.90 inches circumference, weighing 0.42 to 7.77 pounds per fathom, showed an ultimate strength of from 1670 to 33,805 pounds, the strength per fathom weight varying from 2872 to 5534 pounds.

Hemp Ropes, Tarred.—15 tests of ropes from 1.44 to 7.12 inches circumference, weighing from 0.38 to 10.39 pounds per fathom, showed an ultimate strength of from 1046 to 31.549 pounds, the strength per fathom weight varying from 1767 to 5149 pounds.

Cotton Ropes.—5 ropes, 2.48 to 6.51 inches circumference, 1.08 to 8.17 pounds per fathom. Strength 3089 to 23,258 pounds, or 2474 to 3346 pounds per fathom weight.

per fathom weight.

Manila Ropes.—35 tests: 1.19 to 8.90 inches circumference, 0.20 to 11.40 pounds per fathom. Strength 1280 to 65,550 pounds, or 3003 to 7394 pounds per fathom weight.

Derting,	
No. of	Tensile strength
lots.	per square inch.
11 Leather, single, ordinary tanned	
4 Leather, single, Helvetia	5631 to 5944
7 Leather, double, ordinary tanned	2160 to 3572
8 Leather, double Helvetia	4078 to 5412
6 Cotton, solid woven	
14 Cotton, folded, stitched	4570 to 7750
1 Flax, solid, woven	9946
1 Flax, folded, stitched	6389
6 Hair, solid, woven	3852 to 5159
2 Rubber, solid, woven	4271 to 4343

Canvas. -35 lots: Strength, lengthwise, 113 to 408 pounds per inch; crossways, 191 to 468 pounds per inch. The grades are numbered 1 to 6, but the weights are not given. The

strengths vary considerably, even in the same number.

Marbles.-Crushing strength of various marbles. 38 tests, 8 kinds.

Marbles.—Crushing strength of various marbles. 38 tests, 8 kinds. Specimens were 6-inch cubes, or columns 4 to 6 inches diameter, and 6 and 12 inches high. Range 7542 to 13,720 pounds per square inch. Granite.—Crushing strength, 17 tests; square columns 4 × 4 and 6 × 4, 4 to 24 inches high, 3 kinds. Crushing strength ranges 10,026 to 13,271 pounds per square inch. (Very uniform.)

Stones.—(Probably sandstone, local names only given.) 11 kinds, 42 tests, 6 × 6, columns 12, 18 and 24 inches high. Crushing strength ranges from 2165 to 12,122. The strength of the column 24 inches long is generally

from 10 to 20 per cent less than that of the 6-inch cube.

Stones.-(Probably sandstone) tested for London & Northwestern Railway. 16 lots, 3 to 6 tests in a lot. Mean results of each lot ranged from 3785 to 11,956 pounds. The variation is chiefly due to the stones being from different lots. The different specimens in each lot gave results which generally agreed within 30 per cent.

Bricks.—Crushing strength, 8 lots; 6 tests in each lot; mean results ranged from 1835 to 9209 pounds per square inch. The maximum variation in the specimens of one lot was over 100 per cent of the lowest. In the most

uniform lot the variation was less than 20 per cent.

Wood.-Transverse and Thrusting Tests.

	Tests.	Sizes abt, in square.	Span, inches.	Ultimate Stress.	$\frac{S = LW}{4BD^2}.$	Thrust- ing Stress per sq. in.		
Pitch pine	10	11½ to 12½	144	45,856 to 80,520	1096 to 1403	3586 to 5438		
Dantzic fir	12	12 to 13	144	37,948 to 54,152 32,856	657 to 790 1505	2478 to 3423 2473		
English oak	3	4½ × 12	120	to 39,084	to 1779	to 4437		
American white oak	5	4½ × 12	120	23,624 to 26,952	1190 to 1372	2656 to 3899		

| Definition of the content of the c English ash, 1 test.....

Portland Cement.—(Austrian.) Cross-sections of specimens 2 × 21/2 inches for pulling tests only; cubes, 3 x 3 inches for thrusting tests; weight,

98.8 pounds per imperial bushel; residue, 0.7 per cent with sieve 2500 meshes per square inch: 38.8 per cent by volume of water required for mixing; time of setting, 7 days; 10 tests to each lot. The mean results in lbs. per sq. in.

were as 10	nows;				
	Cement	Cement	1 Cement.	1 Cement.	1 Cement.
	alone,	alone,	2 Sand.	3 Sand.	4 Sand,
Age.	Pulling.	Thrusting.	Thrusting.	Thrusting.	Thrusting.
10 days	376	2910	893	407	228
20 days	420	3342	1023	494	275
30 days	451	3724	1172	594	338

Portland Cement. - Various samples pulling tests, 2 × 2½ inches cross-section, all aged 10 days, 180 tests; ranges 87 to 643 pounds per square inch.

#### TENSILE STRENGTH OF WIRE.

(From J. Bucknall Smith's Trea	tise on Wire.)	
	Tons per sq.	Pounds per
	in, sectional	sq. in. sec-
	area.	tional area.
Black or annealed iron wire	. 25	56,000
Bright hard drawn	. 35	78,400
Bessemer, steel wire	. 40	89,600
Mild Siemens-Martin steel wire	. 60	134,000
High carbon ditto (or "improved")	. 80	179,200
Crucible cast-steel "improved" wire	. 100	224,000
"Improved" cast-steel" plough"		268,800
Special qualities of tempered and improved cast	t-	

#### MISCELLANEOUS TESTS OF MATERIALS. Reports of Work of the Watertown Testing-machine in 1883.

TESTS OF RIVETED JOINTS, IRON AND STEEL PLATES.

	Thickness Plate.	Diameter, Rivets, inches.	Diameter, Punched Holes, inches.	Width Plate Tested, inches.	No. Rivets.	Pitch Rivets, inches.	Tensile Strength Joint in Net Sec- tion of Plate per square inch, pounds.	Tensile Strength Plate per square inch, pounds.	Efficiency of Joint, Per Cent.
*********	\$\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\\	11-16 11-16 34 34 11-16 11-16 34 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16 11-16	34/ 34/ 13-16/ 13-16/ 34/ 34/ 14-16/ 11-16/ 11-16/ 13-16/	10/4 10/2 10 10 10 10 10 10 10 10/4 10/4 10/4 10/	6655555544446655555544444	134 134 22 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	39,300 41,000 35,650 35,150 46,360 46,400 44,250 42,370 41,920 60,830 49,840 66,770 66,710 66,710 62,156 66,710 62,560 54,650	47,180 47,180 44,615 44,615 47,180 47,180 44,615 44,635 44,635 44,635 46,590 53,380 57,215 57,215 57,215 57,215 57,215 57,215 57,215 57,215 57,215 57,215 51,545	47.0 + 44.0 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 44.6 + 45
	*Iron. † Steel. † Lap-joint. § Butt-joint.								

<sup>\*</sup> Iron. † Steel.

<sup>§</sup> Butt-joint.

The efficiency of the joints is found by dividing the maximum tensile stress on the gross sectional area of plate by the tensile strength of the material.

#### COMPRESSION TESTS OF 3 × 3 INCH WROUGHT-IRON BARS.

	Tested with Two	Tested with One Flat and One Pin			
Length, inches.	Ultimate Com- pressive Strength pounds per square inch.	Tested with Two Flat Ends, Ulti- mate Compressive Strength, pounds per square inch.	End, Ultimate Compressive Strength, pounds per square inch.		
30	§ 28,260 § 31,990				
60	26,310 26,640				
90		\$ 26,780 25,580	\$ 25,120 \$ 25,190		
120	\$ 20,660 20,200	23,350 23,010 22,450	22,450 21,870		
150	§ 16,520 § 17,840				
180					
Tested with two ends. Length o 120 inches.	f bars 4 % inch	-	17,740		

#### TENSILE TEST OF SIX STEEL EYE-BARS.

22,210

(21/2

#### COMPARED WITH SMALL TEST INGOTS.

The steel was made by the Cambria Iron Company, and the sye-bar heads made by Keystone Bridge Company by upsetting and hammering. All the bars were made from one ingot. Two test pieces,  $\frac{4}{3}$ -inch round, rolled from a test-ingot, gave elastic limit 48,040 and 42,210 pounds; tensile strength, 73,150 and 69,470 pounds, and elongation in 8 inches, 22.4 and 25.6 per cent. respectively. The ingot from which the eye-bars were made was 14 inches square, rolled to billet,  $7 \times 6$  inches. The eye-bars were field to  $6162 \times 1$  inch. Chemical tests gave carbon .27 to .30; manganese, .64 to .73; phosphorus, .074 to  $.080 \times 1$ 

Gauged Length, inches.	Elastic limit, lbs. per sq. in.	Tensile strength per sq. in., lbs.	Elongation per cent, in Gauged Length.
160	37,480	67,800	15.8
160	36,650	64,000	6.96
160		71,560	8.6
200	37,600	68,720	12.3
200	35,810	65,850	12.0
200	33,230	64,410	16.4
200	37.640	68,290	13.9

The average tensile strength of the  $\frac{3}{4}$ -inch test pieces was 71.310 lbs., that of the eye-bars 67.320 lbs., a decrease of 5.7%. The average elastic limit of the test pieces was 45.150 lbs., that of the eye-bars 36.402 lbs., a decrease of 19.4%. The elastic limit of the test pieces was 63.3% of the ultimate strength, that of the eye-bars 42.3% of the ultimate strength,

# COMPRESSION OF WROUGHT-IRON COLUMNS, LATTICED BOX AND SOLID WEB.

#### ALL TESTED WITH PIN ENDS.

Columns made of	Length, feet.	Sectional Area, square inch.	Total Weight of Column, pounds.	Ultimate Strength, per square inch, pounds.
6 inch channel, solid web	10.0 15.0	9.831 9.977	432 592	30,220 21,050
6 " " " "	20.0	9.762	755	16,220
8 " " "		16.281		90 540
8 " " " "	20.0		1,230	22,540
0	26.8	16.141	1,645	17,570
8-inch channels, with 5-16-in. continuous	26.8	40 417	1 040	ar 000
plates	26.8	19.417	1,940	25,290
5-16-inch continuous plates and angles. Width of plates, 12 in., 1 in. and 7.35 in.	26.8	16.168	1,765	28,020
7-16-inch continuous plates and angles.	20.0	00.054	2040	05 450
Plates 12 in. wide.	26.8	20.954	2,242	25,770
8-inch channels, latticed	13.3	7.628	679	33,910
8 " " " " " " " " " " " " " " " " " " "	20.0	7.621	924	34,120
0	26.8	7.673	1,255	29,870
8-inch channels, latticed, swelled sides	13.4	7.624	684	33,530
	20.0	7.517	921	33,390
· · · · · · · · · · · · · · · · · · ·	26.8	7.702	1,280	30,770
10 " "	16.8	11.944	1,470	33,740
10 " "	25.0	12.175	1,926	32,440
10-inch channels, latticed, swelled sides.	16.7	12.366	1,549	31,130
	25.0	11,932	1,962	32,740
* 10-inch channels, latticed one side; con-		-		
tinuous plate one side	25.0	17.622	1,848	26,190
† 10 inch channels, latticed one side; con-			1	
tinuous plate one side	25.0	17.721	1,827	17,270

<sup>\*</sup>Pins in centre of gravity of channel bars and continuous plate, 1.63 inches from centre line of channel bars.

† Pins placed in centre of gravity of channel bars.

#### EFFECT OF COLD-DRAWING ON STEEL.

Three tensile bars and two compression bars, cut from the same bar of

k	not-rolled steel, from the Norway Steel and I	ron Comp	any:	
		Tensile trength pe q. in., lbs.	er tie	nga. on. cent.
1	. Piece of the original hot-rolled bar, length 66 inches, diameter 2.03 inches. Gauged			
9	length 30 inches	55,400	2	3.9
	pass), .094 inch. Gauged length 20 inches. Diameter reduced in compression dies (one	70,420		2.7
ď	pass), .222 inch. Gauged length 20 inches.	81,890		0.075
	S	Compress. Stress, lbs. per sq. in.		Com- press. set, in.
4	. Compression test of cold-drawn bar (same as No. 3). Length 4 inches, diameter			
5	1,808 inches	75,000	.0562	.0395

Pieces 4 and 5 both had diameters increased in the middle to 1.821 inches, and at the ends to 1.813 inches.

#### TESTS OF AMERICAN WOODS. (See also page 309.)

In all cases a large number of tests were made of each wood. Minimum and maximum results only are given. All of the test specimens had a sectional area of 1.575 × 1.575 inches. The transverse test specimens were 39.37 inches between supports, and the compressive test specimens were 12.60 inches long. Modulus of rupture calculated from formula  $R = \frac{3}{2} \frac{P}{\log d^2}$ ;  $P = \log d$  in pounds at the middle,  $l = \log t$  in inches,  $b = \operatorname{breadth}_{l} d = \operatorname{depth}_{l}$ ;

Name of Wood,		rse Tests. lus of ture.	Compression Parallel to Grain, pounds per square inch.		
	Min.	Max.	Min,	Max.	
Cucumber tree (Magnolia acuminata) Yellow poplar white wood (Lirioden-	7,440	12,050	4,560	7,410	
dron tulipifera)	6,560	11,756	4,150	5,790	
cana)	6,720	11,530	3,810	6,480	
charinum	9,680	20,130	7,460	9,940	
Red maple (Acer rubrum)	8,610	13,450	6,010	7,500	
Locust (Robinia pseudacacia)	12,200	21,730	8,330	11,940	
Wild cherry (Prunus serotina)	8,310	16,800	5,830	9,120	
Sweet gum (Liquidambar styraciflua)	7,470	11,130	5,630	7,620	
Dogwood (Cornus florida),	10,190	14,560	6,250	9,400	
Sour gum, Pepperidge (Nyssa sylvatica).	9,830	14,300	6,240	7,480	
Persimmon (Diospyros Virginiana)	18,500	10,290	6,650	8,080	
White ash (Fraxunis Americana)	5,950	15,800	4,520	8,830	
Sassafras (Sassafras officinale)	5,180	10,150	4,050	5,970	
Slippery elm (Ulmus fulva)	10,220	13,952	6,980	8,790	
White elm (Ulmus Americana)	8,250	15,070	4,960	8,040	
Sycamore; Buttonwood (Platanus occi- dentalis)	6,720	11,360	4,960	7,340	
Butternut; white walnut (Juglans ci-	4 8000	44 840	× 400	0.040	
nerea)	4,700	11,740	5,480	6,810	
Black walnut (Juglans nigra)	8,400	16,320	6,940	8,850	
Shellbark hickory (Carya alba)	14,870	20,710	7,650	10,280	
Pignut (Carya porcina)	11,560	19,430	7,460	8,470	
White oak (Quercus alba)	7,010	18,360	5,810	9,070	
Red oak (Quercus rubra)	9,760	18,370	4,960	8,970	
Black oak (Quercus tinctoria)	7,900	18,420	4,540	8,550	
Chestnut (Castanea vulgaris)	5,950	12,870	3,680	6,650	
Beech (Fagus ferruginea)	13,850	18,840	5,770	7,840	
Canoe-birch, paper-birch (Betula papy-	** ***	477.040	* ***	0.800	
racea)	11,710	17,610	5,770	8,590	
Cottonwood (Populus monilifera)	8,390	13,430	3,790	6,510	
White cedar (Thuja occidentalis)	6,310	9,530	2,660	5,810	
Red cedar (Juniperus Virginiana)	5,640	15,100	4,400	7,040	
Cypress (Saxodium Distichum)	9,530	10,030	5,060	7,140	
White pine (Pinus strobus)	5,610	11,530	3,750	5,600	
Spruce pine ( <i>Pinus glabra</i> )Long-leaved pine, Southern pine ( <i>Pinus</i>	3,780	10,980	2,580	4,680	
palustris)	9,220	21,060	4,010	10,600	
White spruce (Picea alba)	9,900	11,650	4,150	5,300	
Hemlock (Tsuga Canadensis)	7,590	14,680	4,500	7,420	
Red fir, yellow fir (Pseudotsuga Doug-	0.000	44.000			
_ lasii)	8,220	17,920	4,880	9,800	
Tamarack (Larix Americana)	10,080	16,770	6,810	10,700	

#### SHEARING STRENGTH OF IRON AND STEEL.

H. V. Loss in American Engineer and Railroad Journal, March and April, 1893, describes an extensive series of experiments on the shearing of iron and steel bars in shearing machines. Some of his results are:

CHAINS.

Depth of penetration at point of maximum resistance for soft steel bars is independent of the width, but varies with the thickness. If d= depth of penetration and t= thickness, d=.3t for a flat knife, d=.25 t for a  $4^\circ$  bevel knife, and  $d = .16 \sqrt{t^3}$  for an 8° bevel knife. The ultimate pressure per inch of width in flat steel bars is approximately 50,000 lbs.  $\times t$ . The energy conof within in flat steel bars is approximately 90,000 lbs.  $\times$  t. The energy consumed in foot pounds per inch width of steel bars is, approximately: 1" thick, 1300 ft.-lbs.;  $11/t^2$ , 2500;  $13/t^2$ , 3700;  $17/t^2$ , 4500; the energy increasing at a slower rate than the thickness. Iron angles require more energy than steel angles of the same size; steel breaks while iron has to be cut off. For hot-rolled steel the resistance per square inch for rectangular sections varies from 4400 lbs. to 20,500 lbs., depending parily upon it hardness and partly upon the size of its cross-area, which latter element indirectly but greatly indicates the temperature, as the smaller dimensions require a considerably longer time to reduce them down to size, which time again means loss of heat.

It is not probable that the resistance in practice can be brought very much below the lowest figures here given-viz., 4400 lbs. per square inchas a decrease of 1000 lbs. will henceforth mean a considerable increase in

cross-section and temperature.

#### HOLDING-POWER OF BOILER-TUBES EXPANDED INTO TUBE-SHEETS.

Experiments by Chief Engineer W. H. Shock, U. S. N., on brass tubes, 3½ inches diameter, expanded into plates ¾-inch thick, gave results ranging from 5850 to 46,000 lbs. Out of 48 tests 5 gave figures under 10,000 lbs., 12 between 10,000 and 20,000 lbs., 18 between 20,000 and 30,000 lbs., 10 between

30,000 and 40,000 lbs., and 3 over 40,000 lbs.

Experiments by Yarrow & Co., on steel tubes, 2 to 214 inches diameter, gave results similarly varying, ranging from 7900 to 41,715 lbs., the majority ranging from 20,000 to 30,000 lbs. In 15 experiments on 4 and 5 lnch tube the strain ranged from 20,720 to 68,040 lbs. Beading the tube does not necessarily give increased resistance, as some of the lower figures were obtained with beaded tubes. (See paper on Rules Governing the Construction of Steam Boilers, Trans. Engineering Congress, Section 6, Chicago, 1893.)

CHAINS. Weight per Foot, Proof Test and Breaking Weight. (Pennsylvania Railroad Specifications.)

Nominal		Specifications.					
Diameter of Wire, inches.	Description.	Weight per foot, lbs.	Proof Test, lbs.	Breaking Weight, lbs.			
5/32 3/16	Lock-chain	0.20					
5/16	Crossing-gate chain	0.70	1500	3000			
5/16	Sprocket-wheel chain	1.10	3000	5500			
3/8	Brake-chain	1.50	3500	7000			
3/8 7/16	Crane-chain	1.50	4000	7500			
7/16	Drop-bottom branch chain.	1.90	5000	9500			
7/16	Crane-chain	1.90	5500	10,000			
1/2	Drop-bottom main chain	2.50	7000	12,500			
2/3	Crane-chain	2.50	7500	13,000			
2/8	Baicty	4.00	11,000	20,000			
%	Crane	4.00	11,000	20,000			
3/4	Log	5.50	16,000	29,000			
24	Crane "	5.50	16,000	29,000			
3/8		7.40	22,000	40,000			
1		9.50	30,000	55,000			
11/8		12.00	40,000	66,000			
11/4	" "	15.00	50,000	82,000			
11/2		21.00	70,000	116,000			

Elongation of all sizes, 10 per cent. All chain must stand the prescribed proof test without deformation.

British Admiralty Proving Tests of Chain Cables.-Studlinks. Minimum size in inches and 16ths. Proving test in tons of 2240 lbs.

Min. Size:  $\frac{1}{16}$   $\frac{1}{16}$ 18 19 110 111 112 113 114 115 2 21 Min. Size: 4018 4318 4718 515 552 592 635 6711 72 7611 815 9120 Test, tons:

Wrought-iron Chain Cables .- The strength of a chain link is less than twice that of a straight bar of a sectional area equal to that of one side of the link. A weld exists at one end and a bend at the other, each requiring at least one heat, which produces a decrease in the strength. The report of the committee of the U. S. Testing Board, on tests of wrought-iron and chain cables contains the following conclusions. That beyond doubt, when made of American bar iron, with cast-iron studs, the studded link is inferior in strength to the unstudded one.

"That when proper care is exercised in the selection of material, a variation of 5 to 17 per cent of the strongest may be expected in the resistance of cables. Without this care, the variation may rise to 25 per cent.

"That with proper material and construction the ultimate resistance of the chain may be expected to vary from 155 to 170 per cent of that of the bar used in making the links, and show an average of about 163 per cent.

"That the proof test of a chain cable should be about 50 per cent of the ultimate resistance of the weakest link."

The decrease of the resistance of the studded below the unstudded cable is probably due to the fact that in the former the sides of the link do not remain parallel to each other up to failure, as they do in the latter. The result is an increase of stress in the studded link over the unstudded in the proportion of unity, to the secant of half the inclination of the sides of the former to each other.

From a great number of tests of bars and unfinished cables, the committee considered that the average ultimate resistance, and proof tests of chain cables made of the bars, whose diameters are given, should be such as are shown in the accompanying table.

ULTIMATE RESISTANCE AND PROOF TESTS OF CHAIN CABLES.

Diam. of Bar.	Average resist. = 163% of Bar.	Proof Test.	Diam. of Bar.	Average resist. = 163% of Bar.	Proof Test.
Inches. 1 1/16 1 1/16 1 1/16 1 1/4 1 3/16 1 1/4 1 5/16 1 3/8 1 7/16 1 1/2	Pounds. 71,172 79,544 88,445 97,731 107,440 117,577 128,129 139,103 150,485	Pounds. 33,840 37,820 42,033 46,468 51,084 55,903 60,920 66,138 71,550	Inches. 1 9/16 15/8 1 11/16 13/4 1 13/16 17/6 1 15/16 2	162,283 174,475 187,075 200,074 213,475	Pounds. 77,159 82,956 88,947 95,128 101,499 108,058 114,806 121,737

#### STRENGTH OF GLASS.

(Fairbairn's "Useful Information for Engineers, " Second Series.) Best Common Extra White Flint Glass, Green Glass, Crown Glass, Mean specific gravity ..... 3.078 2.450 2.528

Mean tensile strength, lbs. per sq. in., bars.. 2,413 2,896 2,546 thin plates. 4,800 do. 4,200 6,000 Mean crush'g strength, lbs. p. sq. in., cyl'drs. 27,582 39,876 31,003 cubes. 13,130 20,206 21,867

The bars in tensile tests were about ½ inch diameter. The crushing tests were made on cylinders about ¾ inch diameter and from 1 to 2 inches high, and on cubes approximately 1 inch on a side. The mean transverse strength of glass, as calculated by Fairbairn from a mean tensile strength of 2560 lbs. and a mean compressive strength of 30,150 lbs. per sq. in., is, for a bar supported at the ends and loaded in the middle,

in which w = breaking weight in lbs., b = breadth, d = depth, and l = length, in inches. Actual tests will probably show wide variations in both directions from the mean calculated strength.

# STRENGTH OF COPPER AT HIGH TEMPERATURES.

The British Admiralty conducted some experiments at Portsmouth Dockyard in 1877, on the effect of increase of temperature on the tensile strength of copper and various bronzes. The copper experimented upon was in rods .72-in, diameter, having a tensile strength of about 25 tons per square inch.

The following	z table snows	some or	the results:
---------------	---------------	---------	--------------

Temperature	Tensile Strength	Temperature	Tensile Strength
Fahr.	in lbs. per sq. in.	Fahr.	in lbs. per sq. in.
Atmospheric. 100° 200° 300°	23,115 23,366 22,110 21,607	Atmospheric, 400° 500°	21,105 19,597

Up to a temperature of 400° F, the loss of strength was only about 10 per cent, and at 500° F, the loss was 16 per cent. The temperature of steam at 200 lbs. pressure is 382° F, so that according to these experiments the loss of strength at this point would not be a serious matter. Above a temperature of 500° the strength is seriously affected.

#### STRENGTH OF TIMBER.

Strength of Long-leaf Pine (Yellow Pine, Pinus Palustris) from Alabama (Bulletin No. 8, Forestry Div., Dept. of Agriculture, 1893. Tests by Prof. J. B. Johnson.)

The following is a condensed table of the range of results of mechanical tests of over 2000 specimens, from 26 trees from four different sites in Alabama: reduced to 15 per cent moisture:

	But	t I	ogs.	Midd	lle	Logs.	Toj	рL	ogs.	Av'g of all Butt Logs.
Specific gravity	0.449	to	1.039	0.575	to	0.859	0.484	to	0.907	0.767
Transverse strength, $\frac{3}{2} \frac{WL}{bh^2}$	4,762	to	16,200	7,640	to	17,128	4,268	to	15,554	12,614
do do, at elast, limit Mod, of elast., thous, lbs.	4,930	to	13,110	5,540	to	11,790	2,558	to	11,950	9,460
Relative elast, resilience.	1,119	ю	0,111	1,150	ιο	2,962	04%	to	2,097	1,926
inch-pounds per cub. in.		to	4.69	1.34	to	4.21	a. 09	to	4.65	2.98
Crushing endwise, str. per sq. inlbs	4,781	to	9,850	5,030	to	9,300	4,587	to	9,100	7,452
Crushing across grain, strength per sq. in., lbs.	675	to	2.094	656	to	1,445	584	to	1.766	1,598
Tensile strength per sq.in.	8,600	to	31,890	6,330	to	29,500	4,170	to	23,280	17,359
Shearing strength (with grain), mean per sq. in.		to	1,299	539	to	1,230	484	to	1156	866

Some of the deductions from the tests were as follows:

1. With the exception of tensile strength a reduction of moisture is accompanied by an increase in strength, stiffness, and toughness.

 Variation in strength goes generally hand in hand with specific gravity.
 In the first 20 or 30 feet in height the values remain constant; then occurs a decrease of strength which amounts at 70 feet to 20 to 40 per cent of that of the butt-log.

4. In shearing parallel with the grain and crushing across and parallel with the grain, practically no difference was found.

 Large beams appear 10 to 20 per cent weaker than small pieces.
 Compression tests endwise seem to furnish the best average statement of the value of wood, and if one test only can be made, this is the safest, as was also recognized by Bauschinger,

7. Bled timber is in no respect inferior to unbled timber.

The figures for crushing across the grain represent the load required to cause a compression of 15 per cent. The relative elastic resilience, in inch-pounds per cubic inch of the material, is obtained by measuring the area of the plotted-strain diagram of the transverse test from the origin to the point in the curve at which the rate of deflection is 50 per cent greater than the rate in the earlier part of the test where the diagram is a straight line. This point is arbitrarily chosen since there is no definite "elastic limit" in timber as there is in iron. The "strength at the elastic limit" is the strength taken at this same point. Timber is not perfectly elastic for any load if left on any great length of time.

The long-leaf pine is found in all the Southern coast states from North Carolina to Texas. Prof. Johnson says it is probably the strongest timber in large sizes to be had in the United States. In small selected specimens, other species, as oak and hickory, may exceed it in strength and toughness. The other Southern yellow pines, viz., the Cuban, short-leaf and the loblolly pines are inferior to the long-leaf about in the ratios of their specific gravities; the long-leaf being the heaviest of all the pines. It averages (kiln-dried) 48 pounds per cubic foot, the Cuban 47, the short-leaf

40, and the loblolly 34 pounds.

Strength of Spruce Timber.—The modulus of rupture of spruce is given as follows by different authors: Hatfield, 9900 lbs. per square inch; Rankine, 1,100; Laslett, 9045; Trautwine, 8100; Rodman, 6168. Trautwine advises for use to deduct one-third in the case of knotty and poor timber.

Prof. Lanza, in 25 tests of large spruce beams, found a modulus of rupture from 2995 to 5666 lbs.; the average being 4613 lbs. These were average beams, ordered from dealers of good repute. Two beams of selected stock, seasoned four years, gave 7562 and 8748 lbs. The modulus of elasticity ranged from 897,000 to 1,588,000, averaging 1,294,000.

Time tests show much smaller values for both modulus of rupture and modulus of elasticity. A beam tested to 5800 lbs. in a screw machine was left over night, and the resistance was found next morning to have dropped

to about 3000, and it broke at 3500.

Prof. Lanza remarks that while it was necessary to use larger factors of safety, when the moduli of rupture were determined from tests with smaller pieces, it will be sufficient for most timber constructions, except in factories, to use a factor of four. For breaking strains of beams, he states that it is better engineering to determine as the safe load of a timber beam the load that will not deflect it more than a certain fraction of its span, say about 1,300 to 1/400 of its length.

# Properties of Timber.

(N. J. Steel & Iron Co.'s Book.)

Description,	Weight per cubic foot, in lbs.	Tensile Strength per sq. inch, in lbs.	Crushing Strength per sq. inch, in lbs.	Relative Strength for Cross Breaking. White Pine = 100.	
Ash	43 to 55.8	11,000 to 17,297	4,400 to 9,363	130 to 180	458 to 700
Beech	43 to 53.4	11,500 to 18,000	5,800 to 9,363	100 to 144	
Cedar	50 to 56.8	10,300 to 11,400	5,600 to 6,000		
Cherry				130	
Chestnut	33	10,500	5,350 to 5,600	96 to 123	
Elm	34 to 36.7	13,400 to 13,489	6.831 to 10.331	96	
Hemlock			5.700	88 to 95	
Hickory		12.800 to 18.000	8,925	150 to 210	
Locust	44	20,500 to 24,800	9.113 to 11.700		
Maple		10,500 to 10,584		122 to 220	367 to 647
Oak, White				130 to 177	752 to 966
Oak, Live		10,200 to 10,000		155 to 189	100 10 000
Pine, White	30	10.000 to 12.000			
Pine, Yellow	00 0 +0 99				286 to 415
		10,000 to 19,500			
Spruce				86 to 110	253 to 374
Walnut, Black.	42	9,286 to 16,000	7,500		

The above table should be taken with caution. The range of variation in the species is apt to be much greater than the figures indicate. See Johnson's

the species is apt to be mucin greater than the lightes indicate, see Johnsons tests on long-leaf pine, and Lanza's on spruce, above. The weight of yellow pine in the table is much less than that given by Johnson. (W. K.)

Compressive Strengths of American Woods, when slowly and carefully seasoned.—Approximate averages, deduced from many experiments made with the U. S. Government testing machine at Watertown, Mass., by Mr. S. P. Sharpless, for the Census of 1880. Seasoned woods resist crushing much better than green ones; in many cases, twice as well. Different specimens of the same wood vary greatly. The strengths may readily vary as much as one-third part more or less from the average.

	End- wise,* lbs. per sq. in.	Side- wise,† lbs. per sq. in.			End- wise,* lbs. per sq. in.	lbs.	se,†
		.01	.1			.01	.1
Ash, red and white	6800	1300	3000	Maple:			
Aspen	4400	800	1400	sugar and black	8000		4300
Beech	7000	1100	1900	white and red	6800	1300	2900
Birch	8000	1300	2600	Oak:			į
Buckeye	4400	600	1400	white, post (or			
Butternut	5400	700	1600	iron), swamp			
Buttonwood				white, red, and	****		
(sycamore)		1300	2600	black	7000		4000
Cedar, red	6000	700	1000	scrub and basket.	6000		4200
Cedar, white (arbor-	4400		000	chestnut and live	7500		4500
vitæ)	4400	500	900	pin	6500	1300	3000
Catalpa (Ind. bean)	5000	700	1300	Pine:	F 100		1000
Cherry, wild	8000	1700	2600	white		₹600	
Chestnut	5300	900	1600 2600	red or Norway	6300	600	1400
Coffee-tree, Ky	5200	1300		pitch and Jersey	F000	4000	2000
Cypress, bald	6000	500	1200	scrub	5000		2000
Elm, Am. or white	6800 7700	1300	2600 2600	Georgia	8500		2600
" red		1300	1100	Poplar	5000		1100
Hemlock	5300 8000	2000	4000	Sassafras	5000 5700		2100
Hickory	10000		13000	Spruce, black			1300
Lignum-vitæ	5000	1600 500	900	white	4500	000	1200
Linden, American. Locust:	5000	900	900	Sycamore (button-	6000	1200	2600
black and yellow.	9800	1900	4400	wood	0000	1900	2000
honey	7000	1600	2600	black	8000	1200	2600
	9000	1700	5300	white (butternut).	5400		1600
Mahogany Maple:	5000	1,00	3300	Willow	4400		1400
broad-leafed, Ore,	5300	1400	2600	** ***********************************	4400	100	1400
broad-leared, Ore.	3300	1300	2000				

# Expansion of Timber Due to the Absorption of Water.

(De Volson Wood, A. S. M. E., vol. x.)

Pieces  $36 \times 5$  in., of pine, oak, and chestnut, were dried thoroughly, and then immersed in water for 37 days. The mean per cent of elongation and lateral expansion were:

	Pine.	Oak,	Chestnut.
Elongation, per cent	0.065	0.085	0.165
Lateral expansion per cent	2.6	3.5	3 65

Expansion of Wood by Heat. - Trautwine gives for the expansion of white pine for 1 degree Fahr. 1 part in 440,530, or for 180 degrees 1 part in 2447, or about one-third of the expansion of iron.

<sup>\*</sup> Specimens 1.57 ins. square  $\times$  12.6 ins. long. † Specimens 1.57 ins. square  $\times$  6.3 ins. long. Pressure applied at mid-length by a punch covering one-fourth of the length. The first column gives the loads producing an indentation of .0 inch, the second those producing an indentation of .1 inch. (See also page 306).

#### Shearing Strength of American Woods, adapted for Pins or Treenails.

J. C. Trautwine (Jour. Franklin Inst.). (Shearing across the grain.)

Ash	Hickory per sq. in. 6045
Beech 5223	" 7285
Birch	Maple
Cedar (white)	Oak (live) 8480
Cedar (Central American) 3410 Cherry 2945	Pine (white)
Chestnut         1536           Dogwood         6510	Pine (Southern yellow) 5735 Pine (very resinous yellow) 5053
Ebony 7750	Poplar 4418
Gum	Spruce 3255 Walnut (black) 4728
Locust	Walnut (common) 2830

# THE STRENGTH OF BRICK, STONE, ETC.

A great advance has recently been made in the manufacture of brick, in the direction of increasing their strength. Chas. P. Chase, in Engineering News, says: "Taking the tests as given in standard engineering books eight News, says: I aking the tests as given in standard engineering books eight or ten years ago, we find in Trantwine the strength of brick given as 500 to 4200 lbs. per sq. in. Now, taking recent tests in experiments made at Watertown Arsenal, the strength ran from 5000 to 22,000 lbs. per sq. in. In the tests on Illinois paving brick, by Prof. I. O. Baker, we find an average strength in hard paving brick of over 5000 lbs. per square inch. The average crushing strength of ten varieties of paving-brick much used in the West, I find to be 7150 lbs. to the square inch."

A recent test of brick made by the dry-clay process at Watertown Arsenal, according to Paving, showed an average compressive strength of 3972 lbs. according to Paving, snowed an average compressive strength of 5042 tops, per sq. in. In one instance it reached 4973 lbs, per sq. in. A test was made at the same place on a "fancy pressed brick." The first crack developed at a pressure of 305,000 lbs., and the brick crushed at 304,300 lbs., or 11,130 lbs. per sq. in. This indicates almost as great compressive strength as granite paving-blocks, which is from 12,000 to 20,000 lbs. per sq. in.

The following notes on bricks are from Trautwine's Engineer's Pocket-Strength of Brick.—40 to 300 tons per sq. ft., 622 to 4668 lbs, per sq. in. A soft brick will crush under 450 to 600 lbs. per sq. in., or 30 to 40 tons psquare foot, but a first-rate master brick representation 200 to 400 tons

per sq. ft. (3112 to 6224 lbs. per sq. in.).

Weight of Bricks.—Per cubic foot, best pressed brick, 150 lbs.; good

pressed brick, 131 lbs.; common hard brick, 125 lbs.; good common brick,

118 lbs.; soft inferior brick, 100 lbs. Absorption of Water.—A brick will in a few minutes absorb 1/2 to 3/4 lb. of water, the last being 1/7 of the weight of a hand-moulded one, or 1/3

Tests of Bricks, full size, on flat side. (Tests made at Watertown Arsenal in 1883.)—The bricks were tested between flat steel buttresses. Compressed surfaces (the largest surface) ground approximately flat. The bricks were all about 2 to 2.1 inches thick, 7.5 to 8.1 inches long, and 3.5 to 3.76 inches wide. Crushing strength per square inch: One lot ranged from 11,066 to 16,734 lbs; a second, 12,936 to 2,2351; a third, 10,390 to 12,709. Other tests gave results from 5990 to 10,250 lbs, per sq. in.
Crushing Strength of Masonry Materials. (From Howe's "Retaining-Walls.")

t	ous per sq. ft	tons per sq. ft.
Brick, best pressed	40 to 300	Limestones and marbles, 250 to 1000
Chalk		Sandstone 150 to 550
Granite	300 to 1200	Soapstone 400 to 800

Strength of Granite. - The crushing strength of granite is commonly rated at 12,000 to 15,000 lbs. per sq. in. when tested in two-inch cubes, and only the hardest and toughest of the commonly used varieties reach a strength above 20,000 lbs. Samples of granite from a quarry on the Connecticut River, tested at the Watertown Arsenal, have shown a strength of 35,965 lbs. per sq. in. (Engineering News, Jan. 12, 1893).

Strength of Avondale, Pa., Limestone—(Engineering News, Feb. 9, 1893).—Crushing strength of 2-in. cubes: light stone 12,112, gray stone

18,040, lbs, per sq. in.

Transverse test of lintels, tool-dressed, 42 in. between knife-edge bearings, load with knife-edge brought upon the middle between bearings. Gray stone, section 6 in. wide × 10 in. high, broke under a load of 20,950 lbs.

Modulus of rupture. 2,200
Light stone, section 8½ in. wide × 10 in. high, broke under. 14,720
Modulus of rupture. 1,170
Absorption.—Gray stone. 551 of 1%
Light stone. 552 of 1%

#### Transverse Strength of Flagging.

(N. J. Steel & Iron Co.'s Book.)

#### EXPERIMENTS MADE BY R. G. HATFIELD AND OTHERS.

b = width of the stone in inches; d = its thickness in inches; l = distance between bearings in inches.

The breaking loads in tons of 2000 lbs., for a weight placed at the centre of the space, will be as follows:

	$bd^2$	$\frac{bd^2}{l} \times$
	$\frac{1}{l}$ ×	TX
Bluestone flagging	.744	Dorchester freestone
Quincy granite	.624	Aubigny freestone
Little Falls freestone	.576	Caen freestone
Belleville, N. J., freestone		Glass
Granite (another quarry)	.432	Slate
Connecticut freestone	.312	

Thus a block of Quincy granite 80 inches wide and 6 inches thick, resting on beams 36 inches in the clear, would be broken by a load resting midway between the beams =  $\frac{80 \times 36}{36} \times .624 = 49.92$  tons.

# STRENGTH OF LIME AND CEMENT MORTAR.

(Engineering, October 2, 1891.)

Tests made at the University of Illinois on the effects of adding cement to line mortar. In all the tests a good quality of ordinary fat line was used, slaked for two days in an earthenware jar, adding two parts by weight of water to one of line, the loss by evaporation being made up by fresh additions of water. The cements used were a German Portland, Black Diamond (Louisville), and Rosendale. As regards fineness of grinding, 85 per cent of the Portland passed through a No. 100 sieve, as did 72 per cent of the Rosendale. A fairly sharp sand, thoroughly washed and dried, passing through a No. 18 sieve and caught on a No. 30, was used. The mortar in all cases consisted of two volumes of sand to one of line paste. The following results were obtained on adding various percentages of cement to the mortar:

Tensile Strength, pounds per square inch.

A	ge	Days.	7 Days.	Days.	Days.	Days.	Days.	84 Days.
	Rosendale Portland Rosendale Portland Rosendale Portland	4 5 5 7 8 10 27	8 81/2 81/2 11 16 12 39	10 91/2 14 13 18 161/2	13 12 20 18½ 22 21½ 48	18 17 25 21 25 22 25 221/2	21 17 24 221/2 28 24 59	26 18 26 23 27 36 57
60 " "	Rosendale	9 45	13 58	38 ~ 20 55	43 16 68	22 67	221/2	23 78
80 " " 80 " " 100 " "	Rosendale Rosendale Portland	12 87 18 90	18½ 91 23 120	22½ 103 26 146	27 124 31 152	29 94 34 181	31½ 210 46 205	33 145 48 202

# MODULI OF ELASTICITY OF VARIOUS MATERIALS.

The modulus of elasticity determined from a tensile test of a bar of any material is the quotient obtained by dividing the tensile stress in pounds per square men as any point of the test by the elongation per inch of length produced by that stress; or if P= pounds of stress applied, K= the sectional area, l= length of the portion of the bar in which the measurement is made, and  $\lambda=$  the elongation in that length, the modulus of elasticity  $E=\frac{P}{K}+\frac{\lambda}{l}=\frac{Pl}{K\lambda}$ . The modulus is generally measured within the elongation limit  $K=\frac{Pl}{k}$ . square inch at any point of the test by the elongation per inch of length

elastic limit only, in materials that have a well-defined elastic limit, such as

iron and steel, and when not otherwise stated the modulus is understood to be the modulus within the elastic limit. Within this limit, for such materials the modulus within the enaste limit. Within think, for such materials the modulus is practically constant for any given bar, the elongation being directly proportional to the stress. In other materials, such as east iron, which have no well-defined elastic limit, the elongations from the beginning of a test increase in a greater ratio than the stresses, and the modulus is therefore at its maximum near the beginning of the test, and continually decreases. The moduli of elasticity of various materials have already been given above in treating of these materials, but the following table gives some additional values selected from different sources : 9,170,000 Brass, cast.....

14,230,000 wire..... 15,000,000 to 18,000,000. Copper..... 1,000,000 Tin, cast..... 4,600,000 12,000,000 to 27,000,000 (?) Iron, cast..... Iron, wrought..... 22,000,000 to 29,000,000 26,000,000 to 32,000,000 25,000,000 14,500,000 Slate, ..... Glass 8,000,000 Ash.... 1,600,000 1,300,000 Birch.... 1,250,000 to 1,500,000 2,191,000 Fir..... 869,000 to Oak ..... 974,000 to 2,283,000 Teak.. .... 2,414,000

Walnut.... 306,000 Pine, long-leaf (butt-logs)... 1,119,000 to 3,117,000 Avge. 1,926,000 The maximum figures given by many writers for iron and steel, viz.,

The maximum incures given by many white the maximum incures given by many 40,000,000 and 42,000,000, are undoubtedly erroneous.

Prof. J. B. Johnson, in his report on Long-leaf Pine, 1893, says: "The modulus of elasticity is the most constant and reliable property of all engineering materials. The wide range of value of the modulus of elasticity of the various metals found in public records must be explained by erro-

neous methods of testing."

In a tensile test of cast iron by the author (Van Nostrand's Science Series, No. 41, page 45), in which the ultimate strength was 23,285 lbs, per sq. in. No. 41, page 45), in which the ultimate strength was 23,285 lbs, per sq. in, the measurements of elongation were mad; 0,0001 inch, and the modulus of elasticity was found to decrease from the beginning of the test, as follows: At 1000 lbs, per sq. in, 25,000,000; at 2000 lbs, 16,666,000; at 4000 lbs, 15,384,000; at 6000 lbs, 13,636,000; at 8000 lbs, 12,500,000; at 12,000 lbs, 10,000,000; at 20,000 lbs, 10,100,000; at 20,000 lbs, 10,100,000; at 23,000 lbs, 11,250,000; The modulus of elasticity of steel (within the elastic limit) is remarkably constant, notwithstanding great variations in chemical analysis, temper, etc. It rarely is found below 28,000,000 or above 31,000,000. It is generally taken at 30,000,000 in engineering calculations.

A factor of safety is the ratio in which the load that is just sufficient to overcome instantly the strength of a piece of material is greater than the greatest safe ordinary working load. (Rankine.)
Rankine gives the following "examples of the values of those factors

which occur in machines ":

De	ad Load.	Live Load, Greatest.	Live Load, Mean.
Iron and steel		6	from 6 to 40
Timber	4 to 5	8 to 10	
Masonry.,	4	8	****

The great factor of safety, 40, is for shafts in millwork which transmit

very variable efforts.

Unwin gives the following "factors of safety which have been adopted in certain cases for different materials." They "include an allowance for ordinary contingencies."

	ead oad.	In Temporary		In Structures subj. to Shocks.
Wrought iron and steel.	3	4	4 to 5	10
Cast iron	3	4	5	10
Timber		4	10	
Brickwork			6	
Masonry	20		20 to 30	

Unwin says says that "these numbers fairly represent practice based on

experience in many actual cases, but they are not very trustworthy.

Prof. Wood in his "Resistance of Materials" says: "In regard to the margin that should be left for safety, much depends upon the character of the loading. If the load is simply a dead weight, the margin may be comparatively small; but if the structure is to be subjected to percussive forces or shocks, the margin should be comparatively large on account of the indeterminate effect produced by the force. In machines which are subjected to a constant jar while in use, it is very difficult to determine the proper margin which is consistent with economy and safety. Indeed, in such cases, economy as well as safety generally consists in making them excessively strong, as a single breakage may cost much more than the extra material necessary to fully insure safety."

For discussion of the resistance of materials to repeated stresses and

For discussion of the resistance of manerials to repeated schools, shocks, see pages 238 to 240.

Instead of using factors of safety it is becoming customary in designing to fix a certain number of pounds per square inch as the maximum stress which will be allowed on a piece. Thus, in designing a boiler, instead of naming a factor of safety of 6 for the plates and 10 for the stay-botts, the ultimate tensile strength of the steel being from 50,000 to 60,000 lbs. per sq. in., an allowable working stress of 10,000 lbs, per sq. in, on the plates and 6000 lbs, per sq. in, on the stay-bolts may be specified instead. So also in Merriman's formula for columns (see page 260) the dimensions of a column are calculated after assuming a maximum allowable compressive stress per square inch on the concave side of the column.

The factors for masonry under dead load as given by Rankine and by Unwin,

viz., 4 and 20, show a remarkable difference, which may possibly be explained as follows: If the actual crushing strength of a pier of masonry is known from direct experiment, then a factor of safety of 4 is sufficient for a pier of the same size and quality under a steady load; but if the crushing strength is merely assumed from figures given by the authorities (such as the crushing strength of pressed brick, quoted above from Howe's Retaining Walls, 40 to 300 tons per square foot, average 170 tons), then a factor of safety of 20 may be none too great. In this case the factor of safety is really a "factor

of ignorance."

The selection of the proper factor of safety or the proper maximum unit stress for any given case is a matter to be largely determined by the judgment of the engineer and by experience. No definite rules can be given. The customary or advisable factors in many particular cases will be found where these cases are considered throughout this book. In general the following circumstances are to be taken into account in the selection of a factor :

1. When the ultimate strength of the material is known within narrow limits, as in the case of structural steel when tests of samples have been made, when the load is entirely a steady one of a known amount, and there is no reason to fear the deterioration of the metal by corrosion, the lowest factor that should be adopted is 3.

2. When the circumstances of 1 are modified by a portion of the load being

variable, as in floors of warehouses, the factor should be not less than 4.

3. When the whole load, or nearly the whole, is apt to be alternately put

on and taken off, as in suspension rods of floors of bridges, the factor should be 5 or 6.

4. When the stresses are reversed in direction from tension to compression, as in some bridge diagonals and parts of machines, the factor should be not less than 6.

5. When the piece is subjected to repeated shocks, the factor should be not less than 10. 6. When the piece is subject to deterioration from corrosion the section

should be sufficiently increased to allow for a definite amount of corrosion before the piece be so far weakened by it as to require removal. 7. When the strength of the material, or the amount of the load, or both

are uncertain, the factor should be increased by an allowance sufficient to

cover the amount of the uncertainty. 8. When the strains are of a complex character and of uncertain amount, such as those in the crank-shaft of a reversing engine, a very high factor is necessary, possibly even as high as 40, the figure given by Rankine for shafts in millwork.

# THE MECHANICAL PROPERTIES OF CORK.

Cork possesses qualities which distinguish it from all other solid or liquid bodies, namely, its power of altering its volume in a very marked degree in consequence of change of pressure. It consists, practically, of an aggregation of minute air-vessels, having thin, water-light, and very strong walls, and hence, if compressed, the resistance to compression rises in a manner more like the resistance of gases than the resistance of an elastic solid such as a spring. In a spring the pressure increases in proportion to the distance to which the spring is compressed, but with gases the pressure intance to which the spring is compressed, out with gases the pressure increases in a much more rapid manner; that is, inversely as the volume which the gas is made to occupy. But from the permeability of cork to air, it is evident that, if subjected to pressure in one direction only, it will gradually part with its octoladed air by effusion, that is, by its passage through the porous walls of the cells in which it is contained. The gaseous part of each constitutes 63% of its bulk. Its elasticity has not only a very considerating, but it is very presistent. Thus in the better kind of corks used in bottling the corks expand the instant they escape from the bottles. This expansion may amount to an increase of volume of 75%, even after the corks have been kept in a state of compression in the bottles for ten years. If the cork be steeped in hot water, the volume continues to increase till it attains nearly three times that which it occupied in the neck of the bottle.

When cork is subjected to pressure a certain amount of permanent deformation or "permanent set" takes place very quickly. This property is common to all solid elastic substances when strained beyond their elastic limits, but with cork the limits are comparatively low. Besides the permanent set, there is a certain amount of sluggish elasticity-that is, cork on being released from pressure springs back a certain amount at once, but

the complete recovery takes an appreciable time.

Cork which had been compressed and released in water many thousand times had not changed its molecular structure in the least, and had continued perfectly serviceable. Cork which has been kept under a pressure of three atmospheres for many weeks appears to have shrunk to from 80% to 85% of its original volume.—Van Nostrand's Eng'g Mag. 1886, xxxv. 307.

#### TESTS OF VULCANIZED INDIA-RUBBER.

Lieutenant L. Vladomiroff, a Russian naval officer, has recently carried out a series of tests at the St. Petersburg Technical Institute with a view to establishing rules for estimating the quality of vulcanized india-rubber. The following, in brief, are the conclusions arrived at, recourse being had to physical properties, since chemical analysis did not give any reliable result: 1. India-rubber should not give the least sign of superficial cracking when bent to an angle of 180 degrees after five hours of exposure in a closed air-bath to a temperature of 125° C. The test-pieces should be 2.4 inches thick. 2. Rubber that does not contain more than half its weight of metallic oxides should stretch to five times its length without breaking. 3. Rubber free from all foreign matter, except the sulphur used in vulcanizing it, should stretch to at least seven times its length without rupture. 4. extension measured immediately after rupture should not exceed 12% of the original length, with given dimensions. 5. Suppleness may be determined by measuring the percentage of ash formed in incineration. This may form the basis for deciding between different grades of rubber for certain purposes. 6. Vulcanized rubber should not harden under cold. These rules have been adopted for the Russian navy.—Iron Age, June 15, 1893.

# XYLOLITH, OR WOODSTONE

is a material invented in 1883, but only lately introduced to the trade by Otto Serrig & Co., of Pottschappel, near Dresden. It is made of magnesia

cement, or calcined magnesite, mixed with sawdust and saturated with a solution of chloride of calcium. This pasty mass is spread out into sheets and submitted to a pressure of about 1000 lbs. to the square inch, and then simply dried in the air. Specific gravity 1.535. The fractured surface shows a uniform close grain of a yellow color. It has a tensional resistance when dry of 100 lbs. per square inch, and when wet about 66 lbs. When immersed in water for 12 hours it takes up 2.1% of its weight, and 3.8% when immersed 216 hours.

When treated for several days with hydrochloric acid it loses 2,3% in weight, and shows no loss of weight under boiling in water, brine, soda-lye, and solution of sulphates of iron, of copper, and of ammonium. In hardness the material stands between feldspar and quartz, and as a non-conductor of

heat it ranks between asbestos and cork,

It stands fire well, and at a red heat it is rendered brittle and crumbles at the edges, but retains its general form and cohesion. This xylolith is supplied in sheets from 14 in. to 11/4 in. thick, and up to one metre square. It is extensively used in Germany for floors in railway stations, hospitals, etc., and for decks of vessels. It can be sawed, bored, and shaped with ordinary woodworking tools. Putty in the joints and a good coat of paint make it entirely water-proof. It is sold in Germany for flooring at about 7 cents per square foot, and the cost of laying adds about 4 cents more. - Eng'g News, July 28, 1892, and July 27, 1893.

#### ALUMINUM—ITS PROPERTIES AND USES. (By Alfred E. Hunt, Pres't of the Pittsburgh Reduction Co.)

The specific gravity of pure aluminum in a cast state is 2.58; in rolled bars of large section it is 2.6; in very thin sheets subjected to high compression under chilled rolls, it is as nuch as 2.7. Taking the weight of a given bulk of cast aluminum as 1, wrought iron is 2.90 times heavier; structural steel, 2.95 times; copper, 3.60; ordinary high brass, 3.45, Most wood suitable for use in structures has about one third the weight of aluminum. which weighs 0.092 lb, to the cubic inch.

Pure aluminum is practically not acted upon by boiling water or steam. Carbonic oxide or hydrogen sulphide does not act upon it at any temperature under 600° F. It is not acted upon by most organic secretions.

Hydrochloric acid is the best solvent for aluminum, and strong solutions of caustic alkalies readily dissolve it. Ammonia has a slight solvent action, and concentrated sulphuric acid dissolves aluminum upon heating, with evolution of sulphurous acid gas. Dilute sulphuric acid acts but slowly on the metal, though the presence of any chlorides in the solution allow rapid decomposition. Nitric acid, either concentrated or dilute, has very little action upon the metal, and sulphur has no action unless the metal is at a red heat. Sea-water has very little effect on aluminum. Strips of the metal placed on the sides of a wooden ship corroded less than 1/1000 inch after six months' exposure to sea-water, corroding less than copper sheets similarly placed.

In malleability pure aluminum is only exceeded by gold and silver. ductility it stands seventh in the series, being exceeded by gold, silver, plathnum, iron, very soft steel, and copper. Sheets of aluminum have been rolled down to a thickness of 0.0005 inch, and beaten into leaf nearly as rolled down to a thickness of vocation and a transport of between thin as gold leaf. The metal is most malleable at a temperature of between 400° and 600° F., and at this temperature it can be drawn down between rolls with nearly as much draught upon it as with heated steel. It has also been drawn down into the very finest wire. By the Mannesmann process

aluminum tubes have been made in Germany.

Aluminum stands very high in the series as an electro-positive metal, and contact with other metals should be avoided, as it would establish a galvanic

couple.

The electrical conductivity of aluminum is only surpassed by pure copper, silver, and gold. With silver taken at 100 the electrical conductivity of aluminum is 54.20; that of gold on the same scale is 78; zinc is 29.90; iron is only 16, and platinum 10.60. Pure aluminum has no polarity, and the

only lo, and pathom 10.00. The authorities as possible metal in the market is absolutely non-magnetic.
Sound castings can be made of aluminum in either dry or "green" sand moulds, or in metal "chills." It must not be heated much beyond its melting-point, and must be poured with care, owing to the ready absorption of occluded gases and air. The shrinkage in cooling is 17/64 inch per foot, or a little more than ordinary brass. It should be melted in plumbago crucibles, and the metal becomes molten at a temperature of 1120° F. according to Professor Roberts-Austen, or at 1300° F. according to Richards.

The coefficient of linear expansion, as tested on \(^3\xi\_1\) inch round aluminum rods, is 0.0002295 per degree centigrade between the freezing and boiling point of water. The mean specific heat of aluminum is higher than that of any other metal, excepting only magnesium and the alkali metals. From zero to the melting-point it is 0.2185; water being taken as 1, and the latent heat of fusion at 28.5 heat units. The coefficient of thermal conductivity of unannealed aluminum is 37.96; of annealed aluminum, 38.7. As a conductor of heat aluminum ranks fourth, being exceeded only by silver, copper, and gold.

Aluminum, under tension, and section for section, is about as strong as cast iron. The tensile strength of aluminum is increased by cold rolling or cold forging, and there are alloys which add considerably to the tensile strength without increasing the specific gravity to over 3 or 3.25.

The strength of commercial aluminum is given in the following table as

the result of many tests:

	Elastic Limit	Ultimate Strength	Percentage
	per sq. in. in	per sq. in, in	of Reduct'n
Form.	Tension,	Tension,	of Area in
	lbs.	lbs.	Tension.
Castings	6,500	15,000	15
Sheet	12,000	24,000	35
Wire	16,000-30,000	30,000-65,000	60
Bars		28,000	40

The elastic limit per square inch under compression in cylinders, with length twice the diameter, is 3500. The ultimate strength per square inch under compression in cylinders of same form is 12,000. The modulus of elasticity of cast aluminum is about 11,000,000. It is rather an open metal in its texture, and for cylinders to stand pressure an increase in thickness must be given to allow for this porosity. Its maximum shearing stress in castings is about 12,000, and in forgings about 16,000, or about that of pure copper.

Pure aluminum is too soft and lacking in tensile strength and rigidity for many purposes. Valuable alloys are now being made which seem to give great promise for the future. They are alloys containing from 2% of % of % of copper, manganese, iron, and nickel. As nickel is one of the principal constituents, these alloys have the trade name of "Nickel-aluminum." Plates and bars of this nickel alloy have a tensile strength of from 40,000 to

Plates and bars of this nickel alloy have a tensile strength of from 40,000 to Plates and bars of this nickel alloy have a tensile strength of from 40,000 to 900 pounds per square inch, an elastic init of 55% to 60% of the ultimate tensile strength, an elongation of 20% it is inline, and a reduction of area of 25%.

This metal is especially capable of withstanding the punishment and distortion to which structural material is ordinarily subjected. Nickel-aluminum alloys have as much resilience and spring as the very hardest of hard-drawn brass.

Their specific gravity is about 2,80 to 2,85, where pure aluminum has a

specific gravity of 2.72

In castings, more of the hardening elements are necessary in order to give the maximum stiffness and rigidity, together with the strength and ductility of the metal; the favorite alloy material being zinc, iron, manganese, and copper. Tin added to the alloy reduces the shrinkage, and alloys of aluminum and tin can be made which have less shrinkage than cast iron.

The tensile strength of hardened aluminum-alloy castings is from 20,000

to 25,000 pounds per square inch.

Alloys of aluminum and copper form two series, both valuable. The first is aluminum-bronze, containing from 5¢ to 11½\$¢ of aluminum; and the second is copper-hardened aluminum, containing from 2¢ to 15¢ of copper. Aluminum-bronze is a very dense, fine-grained, and strong alloy, having good ductility as compared with tensile strength. The 10½ bronze in forged bars will give 100,000 lbs. tensile strength per square inch, with 60,000 lbs. elastic limit per square inch, and 10½ elongation in 8 inches. The 5½ to 7½½ bronze has a specific gravity of 8 to 8.30, as compared with 7.50 for the 10½ to 11½\$bronze, a tensile strength of 70,000 to 80,000 lbs., an elastic limit of 40,000 lbs. per square inch, and an elongation of 30½ in 8 inches.

Aluminum is used by steel manufacturers to prevent the retention of the

Aluminum is used by steel manufacturiers to prevent the retention of the occluded gases in the steel, and thereby produce a solid inpot. The proportions of the dose range from ½ lb, to several pounds of aluminum per ton of steel. Aluminum is also used in giving extra fluidity to steel used in castings, making them sharper and sounder. Added to cast iron, aluminum causes the iron to be softer, free from shrinkage, and lessens the tendency to "chilli."

With the exception of lead and mercury, aluminum unites with all metals,

ALLOYS. 319

though it unites with antimony with great difficulty. A small percentage of silver whitens and hardens the metal, and gives it added strength; and this alloy is especially applicable to the manufacture of fine instruments and apparatus. The following alloys have been found recently to be useful in the arts: Nickel-alluminum, composed of 39 parts alceled to 8 of aluminum, rosine, made of 40 parts nickel, 10 parts sliver, 39 parts aluminum, and parts tin, for jewellers were parts the silver, 39 parts aluminum, and parts tin, for jewellers were parts copier. This plantinum, and parts tin, for jewellers were parts copier. The parts are parts copier. The parts are parts and the parts are parts of 1889, has a specific gravity of 2.9 to 30, and can be east in very solid shapes, as it has very little shrinkage.

From analysis the blowing composition is deduced. Administration, 57.43, tm., 12.945; silicon, 1.325; iron, none.

The metal cas be readily cherically welded, but soldering is still not satterned to the profession of the profess

as copper bits do.

# ALLOYS.

# ALLOYS OF COPPER AND TIN.

(Extract from Report of U. S. Test Board.\*)

2	Mean Composition by		ongth, in.	it, i. in.	n 5	e Test, of	1" sq. long,	ij	Те	rsion sts.
Number.	Ana	lysis.	le Strei per sq.	Lim	tion, ent i	erse	ion, g in,	ng gth,	mum Mom- ftlbs.	of in,
nN _	Cop- per.	Tin.	Tensile Strength lbs. per sq. in.	Elastic Limit, lbs. per sq. in.	Elongation, per cent in 5 inches.	Transverse Modulus o Rupture,	Deflection, 1 Bar 22 in. 1 inches.	Crushing Strength, Ibs. per sq. 3	Maximum Tor. Mom- ent, ftlbs.	Angle of Torsion, degrees.
1	100.		27,800	14,000	6.47	29,848	bent.	42,000	143	153
1a	100.	1.90	12,760	11,000	0.47	21,251	2.31	39,000	65	40
2 2	97.89 96.06		24,580 32,000	10,000 16,000	13.33 14.29	33,232	bent.	34,000 42,048	150 157	317 247
1a 2 3 4 5 6 7 8 9	94.11	5.43	02,000	10,000	14.20	38,659	Dent.	42,040	191	241
5	92.11	7.80	28,540	19,000	5.53	43,731		42,000	160	126
6	90.27	9.58	26,860	15,750	3.66	49,400	66	38,000		114
7	88.41	11.59				60,403	44			
8	87.15	12.73	29,430	20,000	3.33	34,531	4.00	53,000	182	100
10	82.70 80.95	17.34 18.84	32,980		0.04	67,930 56,715	0.63	*** OOO	190	
11	77.56		96,900		0.04	29,926	0.49	78,000	190	16
12	76.63	23.24	22,010	22,010	ő.	32,210	0.19	114,000	122	3.4
13	72.89	26.85			0.	9,512	0.05			0.1
14	69.84	29.88	5,585	5,585	0.	12,076	0.06	147,000	18	1.5
15	68.58	31.26			0.	9,152	0.04			
16	67.87	32.10			0.	9,477	0.05			
17 18	65.34 56.70	34.47 43.17	2,201 1,455	2,201	0.	4,776	0.02	84,700	16	1
19	44.52	55.28	3,010	1,455	0. 0.	2,126 4,776	0.02	92 000		
20	34.22	65.80	3,371	3 371	0.	5,384	0.03	35,800 19,600	23 17	1 2
21	23.35	76.29	6,775	3,010 3,371 6,775	ő.	12,408	0.27	10,000	1.	
22	15.08	84.62				9,063	0.86	6,500	23	25
23	11.49	88.47	6,380	3,500	4.10	10,706	5.85	10,100	23	62
24	8.57	91.39	6,450	3,500	6.87	5,305	bent.	9,800	23	132
25	3.72	96.31	4,780	2,750	12.32	6,925	44	9,800	23	220
26	0.	100.	3,505		35.51	3,740		6,400	12	557

\*The tests of the alloys of copper and tin and of copper and zinc, the results of which are published in the Report of the U.S. Board appointed to test Iron, Steel, and other Metals, Vols. I and II, 1879 and 1881, were made by the author under direction of Prof. R. H. Thurston, chairman of the Committee on Alloys. See preface to the report of the Committee, in Vol. I.

Nos. 1a and 2 were full of blow-holes.

Tests Nos. 1 and 1a show the variation in cast copper due to varying conditions of casting. In the crushing tests Nos. 12 to 20, inclusive, crushed and broke under the strain, but all the others bulged and flattened out. In these cases the crushing strength is taken to be that which caused a decrease of 10% in the length. The test-pieces were 2 in. long and 5% in. diameter. The torsional tests were made in Thurston's torsion-machine, on pieces 5% in. diameter and 1 in. long between heads.

Specific Gravity of the Copper-tin Alloys.—The specific gravity of copper, as found in these tests, is 8.574 (tested in turnings from the ingot, and reduced to 39.1° F.). The alloy of maximum sp. gr. 8,956 contained 62.42 copper, 37.48 tin, and all the alloys containing less than 37% tin varied irregularly in sp. gr. between 8.65 and 8.93, the density depending not on the composition, but on the porosity of the casting. It is probable that the actual sp. gr. of all these alloys containing less than 37% tin is about 8.95, and any smaller figure indicates porosity in the specimen.

From 37% to 100% tin, the sp. gr. decreases regularly from the maximum of

8.956 to that of pure tin, 7.293.

# Note on the Strength of the Copper-tin Alloys.

The bars containing from 2% to 24% tin, inclusive, have considerable strength, and all the rest are practically worthless for purposes in which strength is required. The dividing line between the strong and brittle alloys is precisely that at which the color changes from golden yellow to silver-white, viz., at a composition containing between 24% and 30% of tin.

It appears that the tensile and compressive strengths of these alloys are in no way related to each other, that the torsional strength is closely proportional to the tensile strength, and that the transverse strength may depend in some degree upon the compressive strength, but it is much more nearly related to the tensile strength. The modulus of rupture, as obtained by the transverse tests, is, in general, a figure between those of tensile and compressive strengths per square inch, but there are a few exceptions in

which it is larger than either.

The strengths of the alloys at the copper end of the series increase rapidly The strengths of the alloys at the copper end of the series increase rapidly with the addition of tin till about 4% of tin is reached. The transverse strength continues regularly to increase to the maximum, till the alloy containing about 17½ of tin is reached, while the tensile and torsional strengths also increase, but irregularly, to the same point. This irregularity is probably due to porosity of the metal, and might possibly be removed by any means which would make the castings more compact. The maximum is reached at the alloy containing 82.70 copper, 17.34 tin, the transverse strength, however, being very much greater at this point than the tensile or torsional strength. From the point of maximum strength the figures drop rapidly to the alloys containing about 27.56 of tin, and then more slowly drop rapidly to the alloys containing about 27.5% of tin, and then more slowly to 37.5%, at which point the minimum (or nearly the minimum) strength, by all three methods of test, is reached. The alloys of minimum strength are found from 37.5% tin to 52.5% tin. The absolute minimum is probably about 45% of tin.

From 52.5% of tin to about 77.5% tin there is a rather slow and irregular increase in strength. From 77.5% in to the end of the series, or all tin, the strengths slowly and somewhat irregularly decrease.

The results of these tests do not seem to corroborate the theory given by

some writers, that peculiar properties are possessed by the alloys which are compounded of simple multiples of their atomic weights or chemical equivalents, and that these properties are lost as the compositions vary more or less from this definite constitution. It does appear that a certain percentage composition gives a maximum strength and another certain percentage a minimum, but neither of these compositions is represented by simple multiples of the atomic weights.

There appears to be a regular law of decrease from the maximum to the minimum strength which does not seem to have any relation to the atomic

proportions, but only to the percentage compositions.

Hardness.—The pieces containing less than 24% of tin were turned in the lathe without difficulty, a gradually increasing hardness being noticed, the last named giving a very short chip, and requiring frequent sharpening

With the most brittle alloys it was found impossible to turn the test-pieces in the lathe to a smooth surface. No. 13 to No. 17 (26.85 to 34.47 tin) could not be cut with a tool at all. Chips would fly off in advance of the tool and

beneath it, leaving a rough surface; or the tool would sometimes, apparently, crush off portions of the metal, grinding it to powder. Beyond 40% tin the hardness decreased so that the bars could be easily turned.

ALLOYS OF COPPER AND ZINC. (U. S. Test Board).

		Com-	Tensile	Elastic Limit % of	on %	Trans- verse	n 1" 22"	Crush-	Te	ional sts.
No.	Ana	ysis.	Strength, lbs. per	Break- ing	Elongation % in 5 inches.	Test Modu- lus of	0 - 9	ing Str'gth per sq.	Tors. nent lbs.	e of sion,
	Cop- per.	Zinc.	sq. in.	Load, lbs. per sq. in.	Elol	Rup- ture.	Deflecti sq. bal long, i	in., lbs.	Max. Tors Moment ftlbs.	Angle of Torsion, deg.
_		~		i			-			
1	97.83	1.88							130	357
2 3	82.93	16.98	32,600	26.1	26.7	23,197	Bent		155	329
3	81.91	17.99 22.45		30.6	31.4	21,193			166	345
4 5 6 7 8	77.39 76.65	23.08		20.0 24.6	35.5 35.8		44	42,000	169 165	311 267
6	73.20	26.47		23.7	38.5	25,894		42,000	168	293
7	71.20	28.54		29.5	29.2	24,468	66		164	269
8	69.74	30.06		28.7	20.7	26,930	66		143	202
9	66.27	33.50		25.1	37.7	28,459	64		176	257
10	63.44	36.36	48,300	32.8	31.7	43,216	44		202	230
11	60.94	38.65		40.1	20.7	38,968	- 44	75,000	194	202
12	58.49	41.10		54.4	10.1	63,004	**		227	93
13	55.15	44.44		44.0	15.3	42,463	"	78,000	209	109
14	54.86	44.78	46,400	53.9	8.0	47,955			223	72
15	49.66			54.5	5.0	33,467	1.26	117,400	172	38
16 17	48.99 47.56	50.82 52.28	26,050 24,150	100. 100.	0.8		0.61	121,000	176 155	16
18	43,36	56.22		100.		48,471 17,691	0.10	121,000	88	13
19	41.30	58.12	3,727	100.	••••	7,761	0.04		18	20
20	32.94	66.23	1,774	100.	••••	8,296	0.04		29	ĩ
21	29.20	70.17	6,414	100.		16,579	0.04		40	13 2 2 1 2 1 3
22	20.81	77.63		100.	0.2	22,972	0.13	52,152	65	ĩ
23	12.12	86.67	12,413	100.	0.4		0.31		82	3
24	4.35	94.59	18,065	100.	0.5	26,162	0.46		81	22
25	Cast	Zine.	5.400	75.	0.7	7,539	0.12	22,000	37	142

Variation in Strength of Gun-bronze, and Means of Improving the Strength.—The figures obtained for alloys of from 78% to 12.7% tin, viz., from 26.860 to 29.480 pounds, are much less than are usually given as the strength of gun-metal. Bronze guns are usually cast upder the pressure of a head of metal, which tends to increase the strength under the pressure of a head of metal, which tends to increase the strength and density. The strength of the upper part of a gun casting, or sinking head, is not greater than that of the small bars which have been tested in these experiments. The following is an extract from the report of Major Wade concerning the strength and density of gun-bronze (1850):—Extreme variation of six samples from different parts of the same gun (a 32-pounder howitzer): Specific gravity, 8.487 to 8.855; tenacity, 26,428 to 52,192. Extreme variation of all the samples tested: Specific gravity, 8.308 to 8.850; tenacity, 23,108 to 54,531. Extreme variation of all the samples from the gun heads: Specific gravity, 8.308 to 8.765; tenacity, 25,205 to 53,484.

Major Wade says: The general results on the quality of bronze as it is found in guns are mostly of a negative character. They expose defects in

found in guns are mostly of a negative character. They expose defects in density and strength, develop the heterogeneous texture of the metal in different parts of the same gun, and show the irregularity and uncertainty of quality which attend the casting of all guns, although made from similar

materials, treated in like manner.

Navy ordnance bronze containing 9 parts copper and 1 part tin, tested at Washington, D. C., in 1875-6, showed a variation in tensile strength from 28,800 to 51,400 lbs. per square inch, in elongation from 3% to 58%, and in specific gravity from 8.39 to 8.88.

That a great improvement may be made in the density and tenacity of gun-bronze by compression has been shown by the experiments of Mr. S. B. Dean in Boston, Mass., in 1869, and by those of General Uchatius in Austria in 1873. The former increased the density of the metal next the bore of the gun from 8.321 to 8.875, and the tenacity from 27,238 to 41,471 pounds per

 $7\hat{3}$ 55

49 50

55

55 10 35

0.5 44.5

40

45

square inch. The latter, by a similar process, obtained the following figures for tenacity:

	Victions, per-	Poun	ds per sq. in.
Bronze with	10% tin		72.053
	8% tin		
Dronze with	6% tin		11,000

## ALLOYS OF COPPER, TIN, AND ZINC. (Report of U. S. Test Board, Vol. II, 1881.)

Tensile Elongation Analysis, Transverse Strength per per cent in Original Mixture. Strength. 5 inches. No. square inch. in Report. Modulus Deflec-Cu. Sn. Zn. tion, B. B. A. A. Rupture ins. 41,334 2.34 qa 5 2 63 23,660 30,740 9 68 5 88.14 1.86 10 31,986 3 67 32,000 33,000 17.6 19.5 28,840 70 71 2.85 85 5 44,457 28,560 6 80 5.28 85 36,000 10 5 62,470 2.56 35,680 2.51 89 2.5 62,405 2.83 34,500 1.29 2.79 85 12.5 32,800 69,960 36,000 88 82.5 12.5 5 1.61 34,000 .86 .92 69,045 42,618 67,117 54,476 .68 2.5 1.09 82.5 33,600 33,800 32,300 31,950 30,760 36,000 32,500 34,960 39,300 67 80 37,560 32,830 11.6 5 3.88 3,59 80 10 2.45 1.57 1.67 32,350 1.19 .55 .44 69 80 15 5 35,500 36,000 38,140 86 63,849 61,705 1.00 .72 2.50 1.00 77.5 12.5 77.5 .59 87 12.5 71 63 75 20 55,355 2.91 3.19 85 75 7.5 17.5 62,607 1.39 33,700 1.56 1.33 .73 64 75 10 58,345 35,320 34,000 1.13 1.25 10 .31 28,000 .59 65 75 51,109 35,440 .54 21 .43 66 75 20 5 40,235 23,140 27,660 51,839 72.5 7.5 20 2.86 32,700 34,800 3.73 3.78 53,230 57,349 84 72.5 10 17.5 .74 30,000 30,000 .48 .49 1.37 2.06 .99 59 70 25 38,000 32,940 48,836 36,520 37,924 15,126 .36 .84 7.5 22.5 32,400 .40 38,000 .18 .31 60 70 10 20 33,140 26,300 .20 27,800 .25 61 70 15 15 33,440 .08 70 17,000 34,720 34,000 12,900 20 10 7.27 67.5 58,343 81 2.5 30 2.91 45,850 74 55,976 67.5 5 27.5 .49 34,460 1.06 .43 .32 67.5 7.5 25 46 875 29,500 26 30,000 .36 80 65 2.5 32.5 56 949 2.36 41,350 38,300 3.26 3.02 .56 .61 65 5 30 51.369 37,140 25,720 36,000 1.21 .15 .19 56 65 27,075 .14 22,500 65 13,591 .07 6.820 7.231 11,932 .05 58 65 20 3,765 2,665 69,255 69,508 46,076 24,699 18,248 79 2.5 2.34 44,400 2.15 2.19 62.5 35 45,000 78 2.5 37.5 1.46 57,400 52,900 4.87 3.02 .28 41,160 21,780 18,020 66,500 38,330 21,240 12,400 67,600 .39 5 35 .40 53 .13 60 30 .15 54 60 25 .09 39.48 95,623 12 58.222.30 1.99 3.133 58.75 8.75 35,752 .18 32.5 Broke before t est; ver y brittle 2,752 72,308 4 57.5 21 25 21.25 02 1.300

The transverse tests were made in bars 1 in. square, 22 in. between sup-The tensile tests were made on bars 0,798 in. diam, turned from the two halves of the transverse-test bar, one half being marked A and the other B,

3.05

38,174

28,258

20,814

.22

.14

68.900

27,400

25,460

23,000

68,900

30,500

18,500

31,300

9.43

.46

.29

.66

2.88

.43

.10

.45

Ancient Bronzes. -The usual composition of ancient bronze was the same as that of modern gun-metal-90 copper, 10 tin; but the proportion of tin varies from 5% to 15%, and in some cases lead has been found. Some an-

cient Egyptian tools contained 88 copper, 12 tin.

Strength of the Copper-zine Alloys.—The alloys containing less than 15% of zinc by original mixture were generally defective. The bars were full of blow-holes, and the metal showed, signs of oxidation. To insure good castings it appears that copper-zinc alloys should contain more than 15% of zinc.

From No. 2 to No. 8 inclusive, 16.98 to 30.06% zinc the bars show a remarkable similarity in all their properties. They have all nearly the same strength and ductility, the latter decreasing slightly as zinc increases, and are nearly allies in color and appearance. Between Nos. 8 and 10, 30.06 and 30.36% zinc, the strength by all methods of test rapidly increases. Between No. 10 and No. 15, 36.36 and 50.14% zinc, there is another group, distinguished by high strength and diminished ductility. The alloy of maximum tensile, transverse and torsional strength contains about 41% of zinc.

The alloys containing less than 55% of zinc are all yellow metals. Beyond 55% the color changes to white, and the alloy becomes weak and brittle. Between 70% and pure zinc the color is bluish gray, the brittleness decreases and the strength increases, but not to such a degree as to make them useful

for constructive purposes.

Difference between Composition by Mixture and by Analysis.—There is in every case a smaller percentage of zinc in the average analysis than in the original mixture, and a larger percentage of copper. The loss of zinc is variable, but in general averages from 1 to 2%.

Liquation or Separation of the Metals.—In several of the

bars a considerable amount of liquation took place, analysis showing a difference in composition of the two ends of the bar. In such cases the difference in composition of the two class of the bar, in start cases inchange in composition was gradual from one end of the bar to the other, the upper end in general containing the higher percentage of copper. A notable instance was bar No. 13, in the above table, turnings from the upper end containing 40,36% of zinc, and from the lower end 48.52%.

Specific Gravity.—The specific gravity follows a definite law, varying with the composition, and decreasing with the addition of zinc. From the plotted curve of specific gravities the following mean values are taken:

0 10 20 30 40 50 60 70 80 90 100. Per cent zinc ..... Specific gravity...... 8.80 8.72 8.60 8.40 8.36 8.20 8.00 7.72 7.40 7.20 7.14.

Graphic Representation of the Law of Variation of Strength of Copper-Tin-Zinc Alloys. - In an equilateral triangle the sum of the perpendicular distances from any point within it to the three sides is equal to the altitude. Such a triangle can therefore be used to show graphically the percentage composition of any compound of three parts, such as a triple alloy. Let one side represent 0 copper, a second 0 tin, and the third 0 zinc, the vertex opposite each of these sides representing 100 of each element respectively. On points in a triangle of wood representing different alloys tested, wires were erected of lengths proportional to the tensile strengths, and the triangle then built up with plaster to the height of the wires. The surface thus formed has a characteristic topography representing the variations of strength with variations of composition. The cut shows the surface thus made. The vertical section to the left represents the law of tensile strength of the copper-tin alloys, to the ferr represents the law of feising strength in the copper-till alloys, the one to the right that of the sizuic alloys, and the one at the rear that of the copper-zinc alloys. The high point represents the strongest possible alloys of the three metals. Its composition is copper 55, inc 43, tin 2, and its strength about 70,000 lbs. The high ridge from this point to the point of maximum height of the section on the left is the line of the strongest alloys,

represented by the formula zinc + (3 × tin) = 55. All alloys lying to the rear of the ridge, containing more copper and less tin or zinc are alloys of greater ductility than those on the line of maximum strength, and are the valuable commercial alloys; those in front on the declivity toward the central valley are brittle, and those in the valley are both brittle and weak. Passing from the valley toward the section at the right the alloys lose their brittleness and become soft, the maximum softness being at tin = 100, but they remain weak, as is shown by the low elevation of the surface. This model was planned and constructed by Prof. Thurston in 1877. (See Trans. A. S. C. E. 1881, Report of the U. S. Board appointed to

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test Iron, Steel, etc., vol. ii., Washington, 1881, and Thurston's Materials of Engineering, vol. iii.)
The best alloy obtained in Thurston's research for the U. S. Testing Board has the composition, Copper 55, Tin 0.5, Zinc 44.5. The tensile strength in a cast bar was 68,300 lbs, per sq. in, two specimens giving the same result; the elongation was 47 to 51 per cent in 51nthes. Thurston's formula for copperitorize alloys of maximum strength (Trans. A. S. C. E., 1881) is z + 34 = 55,

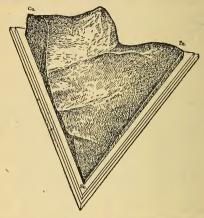


Fig. 77.

in which z is the percentage of zinc and t that of tin. Alloys proportioned according to this formula should have a strength of about 40,000 lbs. per sq. in +500z. The formula fails with alloys containing less than 1 per cent of tin.

The following would be the percentage composition of a number of alloys made according to this formula, and their corresponding tensile strength in castings:

Tin.	Zinc.	Copper.	Tensile Strength, Ibs. per sq. in.	Tin.	Zinc.	Copper.	Tensile Strength, lbs. per sq. in.
1	52	47	66,000	8	31	61	55,500
3	49	49	64,500	9	28	63	54,000
3	46	51	63,000	10	25	65	52,500
4	43	53	61,500	12	19	69	49,500
5	40	55	60,000	14	13	73	46,500
6	37	57	58,500	16	7	77	43,500
7	34	59	57,000	18	1	81	40,500

These alloys, while possessing maximum tensile strength, would in general be too hard for easy working by machine tools. Another series made on the formula z+4 t=50 would have greater ductility, together with considerable strength, as follows, the strength being calculated as before, tensile strength in lbs. per sq. in. =40,000+500z.

Tin.	Zine.	Copper.	Tensile Strength, lbs. per sq. in.	Tin.	Zine.	Copper,	Tensile Strength, Ibs. per sq. in.
1	46	53	63,000	7	22	71	51,000
2	42	56	61,000	8	18	74	49,000
3	38	59	59,000	9	14	77	47,000
4	34	62	57,000	10	10	80	45,000
5	30	65	55,000	11	6	83 .	43,000
6	26	68	53,000	12	2	86	41,000

## Composition of Alloys in Every-day Use in Brass Foundries. (American Machinist.)

	Cop- per.	Zine.	Tin.	Lead.	
	lbs.	lbs.	lbs.	lbs.	
Admiralty metal	87	5	8 .		For parts of engines on board
Bell metal	16		4		naval vessels. Bells for ships and factories.
Brass (yellow)	16	8	4	1/	For plumbers, ship and house
brass (yenow)	10			1/2	brass work.
Bush metal	64	8	4	4	For bearing bushesfor shafting.
Gun metal	32	1	3		For pumps and other hydraulic
					purposes.
Steam metal	20	1	11/2	. 1	Castings subjected to steam
			- ~		pressure.
Hard gun metal	16		21/2		For heavy bearings.
Muntz metal	60	40			Metal from which bolts and nuts
					are forged, valve spindles, etc.
Phosphor bronze	92		8 ph	os, tin	For valves, pumps and general
			10 44		_work.
" "	90		10 ''		For cog and worm wheels,
		1			bushes, axle bearings, slide valves, etc.
Brazing metal	16	3			Flanges for copper pipes.
" solder	50	50			Solder for the above flanges.
Boldet		, 50	,	,	postaci soi one accore nanges.

Gurley's Bronze.—16 parts copper, 1 tin, 1 zinc, ½ lead, used by W. & L. E. Gurley of Troy for the framework of their engineer's transits. Tensile strength 41,114 lbs. per sq. i.n., elongation 27% in 1 inch, sp. gr. 8.696. (W. J. Keep, Trans. A. I. M. E. 1890.)

## Useful Alloys of Copper, Tin, and Zinc.

			(Selected from r	umerou	s sourc	es.)	
				Copper.	Tin.	Zine.	
τ	r. s. 1	Vavy	Dept. journal boxes \ _	16	1		parts.
	and	l gui	de-gibs	82.8	13.8		per cent.
			ze	58.22	2.30	39.48	
N	aval l	oras	8	62	1	37	"
C	ompo	sitio	n, U. S. Navy	88	10	2	" "
10	roce b	agri	ngs (J. Rose)	5 64	8	1	parts.
-	11 a55 L	rear i	ngs (0. Hose)	87.7	11.0		per cent.
G			• • • • • • • • • • • • • • • • • • • •	92.5	5	2.5	- 46 44
		٠.		91	7	2	
				87,75	9.75	2.5	
		٠.	• • • • • • • • • • • • • • • • • • • •	85	5	10	" "
	66	٠.		83	2	15	
n	lough	huar	of for orgina	(13	2		parts.
			s for engines	76.5	11.8	11.7	per cent.
E	Bronze	for	rod-boxes (Lafond)	82	16	2	slightly malleable.
	**	64	pieces subject to shock	83	15	1.50	0.50 lead.
F	Red bra	ass	parts	20	1	1	1 "
	•• •	٠.	per cent	87	4.4	4.3	4.3 "
E			pump casings (Lafond)	88	10	2	
	**	**	eccentric straps. "	84	14	2	
	44		shrill whistles	80	18		2.0 antimony.
	44	"	low-toned whistles	81	17		2.0 ''

Art brox	aza di	ıll red fracture		Copper.	Tin.	Zine,
				89.5	2.1	5.6 2.8 lead.
D	mze				≈.1	5.0 2.0 lead,
				89	8	5
44	44			89	21/6	81/6
66	44			86	14	- / 2
66	66			851/4	123/4	
46	66			80	18	õ
44		• • • • • • • • • • • • • • • • • • • •		79	18	01/ 1/11
- 66	66		• • • • • •		18	21/2 1/2 lead.
	•••			74	91/9	91/2 7 lead.
English	brass	of A.D. 1504		64	3	291% 31% lead.

## Copper-Nickel Alloys, German Silver.

		copper-mener A	moys, u	CHARGERY 13	II VOI .	
			Copper.	Nickel.	Tin.	Zine.
German	silve	r	51.6	25.8	22.6	
44	64		50.2	14.8	3.1	31.9
44	46		51.1	13.8	3.2	31.9
66	66		52 to 55	18 to 25		20 to 30
Nickel	6.6		75 to 66	25 to 33		

A refined copper-nickel alloy containing 50% copper and 49% nickel, with very small amounts of iron, silicon and carbon, is produced direct from Bessemer matte in the Sudbury (Canada) Nickel Works. German silver manufacturers purchase a ready-made alloy, which melts at a low heat and requires simple addition of zinc, instead of buying the nickel and copper separately. This alloy, "50-50" as it is called, is almost indistinguishable from pure nickel. Its cost is less than nickel, its melting point much lower, it can be cast solid in any form desired, and furnishes a casting which works easily in the lathe or planer, yielding a silvery white surface unchanged by air or moisture. For bullet casings now used in various British and continental rifles, a special alloy of 80% copper and 20% nickel is made.

## Special Alloys. (Engineer, March 24, 1893.)

JAPANESE ALLOYS for art work :

	Copper.	Silver.	Gold.	Lead.	Zinc.	Iron.
Shaku-do Shibu-ichi	94.50 67.31	1.55 32.07	3.73 traces.	0.11 .52	trace.	trace.

Gilbert's Alloy for cera-perduta process, for casting in plaster-of-paris ' Copper 91.4 Tin 5.7 Lead 2.9 Very fusible.

### COPPER-ZINC-IRON ALLOYS.

(F. L. Garrison, Jour. Frank, Inst., June and July, 1891.)

Delta Metal.—This alloy, which was formerly known as sterro-metal, is composed of about 60 copper, from 34 to 44 zinc, 2 to 4 fron, and 1 to 2 tin. The peculiarity of all these alloys is the content of iron, which appears to have the property of increasing their strength to an unusual degree. In making delta metal the iron is previously alloyed with zinc in known and definite proportions. When ordinary wrought-iron is introduced into molten zinc, the latter readily dissolves or absorbs the former, and will take it up to the extent of about 5% or more. By adding the zinc-iron alloy thus obtained to the requisite amount of copper, it is possible to introduce any definite quantity of iron up to 5% into the copper alloy. Garrison gives the following as the range of composition of copper-zinc-iron, and copper-zinc-tin-iron alloys:

I.	II.
Per cent.	Per cent.
Iron 0.1 to 5	Iron 0.1 to 5
Copper 50 to 65	Tin 0.1 to 10
Zinc	Zinc 1.8 to 45
	Copper 98 to 40

The advantages claimed for delta metal are great strength and toughness, the produces sound castings of close grain. It can be rolled and forged hot and can stand a certain amount of drawing and hammering when cold. It takes a high polish, and when exposed to the atmosphere tarnishes less than brass.

When cast in sand delta metal has a tensile strength of about 45,000 pounds per square inch, and about 10% elongation; when rolled, tensile strength of 60,000 to 75,000 pounds per square inch, elongation from 9% to 17% on bars 1.128 inch in diameter and 1 inch area.

Wallace gives the ultimate tensile strength 33,600 to 51,520 pounds per

square inch, with from 10% to 20% elongation.

Delta metal can be forged, stamped and rolled hot. It must be forged at a dark cherry-red heat, and care taken to avoid striking when at a black

According to Lloyd's Proving House tests, made at Cardiff, December 20. 1887, a half-inch delta metal-rolled bar gave a tensile strength of 88,400

pounds per square inch, with an elongation of 30% in three inches.

Tobin Bronze.—This alloy is practically a sterro or delta metal with the addition of a small amount of lead, which tends to render copper softer and more ductile.

The following analyses of Tobin bronze were made by Dr. Chas. B. Dudley:

	Pig Metal,	Test Bar (Rolle
	per cent.	per cent.
Copper	59.00	61.20
Zinc	38.40	37.14
Tin	2.16	0.90
Iron	0.11	0.18
Lead		0.35

Dr. Dudley writes, "We tested the test bars and found 78,500 tensile strength with 15% elongation in two inches, and 401/6% in eight inches. This high tensile strength can only be obtained when the metal is manipulated. Such high results could hardly be expected with cast metal."

The original Tobin bronze in 1875, as described by Thurston, Trans. A. S. C. E 1881, had, composition of copper 58.22, tin 2.30, zinc 39.48. As east it had a tenacity of 66,000 lbs, per sq. in., and as rolled 79,000 lbs.; cold

rolled it gave 104,000 lbs.

A circular of Ansonia Brass & Copper Co. gives the following:—The tensile strength of six Tobin bronze one-inch round rolled rods, turned down to a diameter of \$\frac{5}{2}\$ of an inch, tested by Fairbanks, averaged 79,600 ibs. per sq. in., and the elastic limit obtained on three specimens averaged 54,257 lbs. per sq. in.

At a cherry-red heat Tobin bronze can be forged and stamped as readily as steel. Bolts and nuts can be forged from it, either by hand or by machinery, with a marked degree of economy. Its great tensile strength, and resistance to the corrosive action of sea-water, render it a most suitable metal for condenser plates, steam-launch shafting, ship sheathing and fastenings, nails, hull plates for steam yachts, torpedo and life boats, and ship deck fittings.

The Navy Department has specified its use for certain purposes in the machinery of the new cruisers. Its specific gravity is 8.071. The weight of a cubic inch is .291 lb.

#### PHOSPHOR-BRONZE AND OTHER SPECIAL BRONZES.

Phosphor-bronze.—In the year 1868, Montefiore & Kunzel of Liège, Belgium, found by adding small proportions of phosphorus or "phosphoret of tin or copper" to copper that the oxides of that metal, nearly always present as an impurity, more or less, were deoxidized and the copper much improved in strength and ductility, the grain of the fracture became finer,

the color brighter, and a greater fluidity was attained. Three samples of phosphor-bronze tested by Kirkaldy gave: Elastic limit, lbs. per sq. in ... 23,800 24,700 Tensile strength, lbs. per sq. in ... 52,625 46,100 16,100 44,448 Elongation, per cent..... 8.40 1.50

The strength of phosphor-bronze varies like that of ordinary bronze according to the percentages of copper, tin, zinc, lead, etc., in the alloy.

Deoxidized Bronze.—This alloy resembles phosphor bronze some-

what in composition and also delta metal, in containing zinc and iron. The following analysis gives its average composition:

Copper	82 67 1	Iron	0.10
Tin		Silver	0.07
Zinc	3.23	Phosphorus	0.005
Lead ,	2.14	•	
** ** * * * * * * * * * * * * * * * * *			100,615

## Comparison of Copper, Silicon-brouze, and Phosphorbronze Wires.

(Engineering, Nov. 23, 1883.)

	Description of Wire.	Tensile S square	trength per e inch in	Relative Conductivity.				
	•	Tons.	Lbs.					
Silico	copper	18.27 48.25	39,827 41,696 108,080 102,390	100 per cent. 96 " 34 " 26 "				

#### ALUMINUM ALLOYS.

(Aluminum Bronze, Cowles Electric Smelting and Al. Co.'s circular.) The standard A No. 2 grade of aluminum bronze, containing 10% of aluminum and 90% of copper, has many remarkable characteristics which dis-

tinguish it from all other metals.

The tenacity of castings of A No. 2 grade metal varies between 75,000 and 90,000 lbs, to the square inch, with from 4% to 14% elongation.

Increasing the proportion of aluminum in bronze beyond 110 produces a brittle alloy; therefore nothing higher than the A No. 1, which contains 11%, is made.

The B, C, D, and E grades, containing 7½%, 5%, 2½%, and 1½% of aluminum, respectively, decrease in tenacity in the order named, that of the former being about 65,000 pounds, while the latter is 25,000 pounds. While there is also a proportionate decrease in transverse and torsional strengths, elastic limit, and resistance to compression as the percentage of aluminum is lowered and that of copper raised, the ductility on the other hand increases in the same proportion. The specific gravity of the A No. 1 grade is 7.56.

Bell Bros., Newcastle, gave the specific gravity of the aluminum bronzes

as below:

3%	aluminum															8.69	)
4%	**															8.6	2
5%	66															8.30	36
10%	4.6							ı			_					7.68	3

Casting.—The melting point of aluminum bronze varies slightly with the amount of aluminum contained, the higher grades melting at a somewhat lower temperature than the lower grades. The A No. 1 grades melt

at about 1700° F., a little higher than ordinary bronze or brass.

Aluminum bronze shrinks more than ordinary brass. As the metal solidifies rapidly it is necessary to pour it quickly and to make the feeders amply large, so that there will be no "freezing" in them before the casting is properly fed. Baked-sand moulds are preferable to green sand, except for small castings, and when fine skin colors are desired in the castings. (See paper by Thos, D. West, Trans. A. S. M. E. 1886, vol. viii.)
All grades of aluminum bronze can be rolled, swedged, spun, or drawn cold except A I and A 2. They can all be worked at a bright red heat.

In rolling, swedging, or spinning cold, it should be annealed very often, and at a brighter red heat than is used for annealing brass.

Brazing.—Aluminum bronze will braze as well as any other metal, using one quarter brass solder (zinc 500, copper 500 (and three quarters

borax, or, better, three quarters cryolite.

Soldering.—To solder aluminum bronze with ordinary soft (pewter) solder: Cleanse well the parts to be joined free from grease and dirt. Then place the parts to be soldered in a strong solution of sulphate of copper and place in the bath a rod of soft iron touching the parts to be joined. After a while a coppery-like surface will be seen on the metal. Remove from bath, rinse quite clean, and brighten the surfaces. These surfaces can then be the metal beginning the control of the control o be tinned by using a fluid consisting of zinc dissolved in hydrochloric acid, in the ordinary way, with common soft solder.

Mierzinski recommends ordinary hard solder, and says that Hulot uses an alloy of the usual half-and-half lead-tin solder, with 12.5%, 25% or 50% of

zinc amalgam.

## Tests of Aluminum Bronzes.

(By John H. J. Dagger, in a paper read before the British Association, 1889.)

Per cent	Tensile	Strength.	Elonga-	a	
of Aluminum.	Tons per square inch.	Pounds per square inch.	tion, per cent.	Specific Gravity.	
11	40 to 45	89,600 to 100,800	8	7.23	
10	33 '' 40 25 '' 30	73,920 " 89,600	14	7.69 8.00	
7½ 5-5½	15 " 18	56,000 " 67,200 33,600 " 40,320	40 40	8.37	
21/2	13 " 15	29,120 " 33,600	50	8.69	
11/4	11 " 13	24,640 " 29,120	55		

Both physical and chemical tests made of samples cut from various sec-

Both physical and chemical tests made of samples cut from various sections of 245, 55, 75, 6. 710% aluminized copper castings tend to prove that the aluminum unites itself with each particle of copper with uniform proportion in each case, so that we have a product that is free from liquation and highly homogeneous. (R. C. Cole, Iron. Age, Jan, 16, 1890.)

Aluminum-Brass (E. H. Cowles, Trans. A. I. M. E., vol. xviii.)—Cowles aluminum-brass is made by fusing together equal weights of A I aluminum-bronze, copper, and zinc. The copper and bronze are first thoroughly melted and mixed, and the zinc is finally added. The material is left in the furnace until small test-bars are taken from it and broken. When these bars show a tensile strength of 80,000 pounds or over, with 2 or 3 per cent ductility, the metal is ready to be poured. Tests of this brass, on small bars, have at times shown as high as 100,000 pounds tensile strength.

The screw of the United States gunboat Petrel is cast from this brass, mixed with a trifle less zinc in order to increase its ductility.

Tests of Aluminum-Brass. (Cowles E. S. & Al. Co.)

er Tensile Elastic Elonga-
Area. Strength, Limit, lbs. per sq. in. Limit, bs. per sq. in. Remarks.
.1698 41,225 17,668 41½ 25 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5
1698 28,327 2½ 3,000 2,0
1.1661 72,246 21/2 21/3 A P P P P P P P P P P P P P P P P P P
.1698 78,327 21/2

The first brass on the above list is an extremely tough metal with low elastic limit, made purposely so as to "upset" easily. The other, which is called Aluminum-brass No 2, is very hard.

We have not in this country or in England any official standard by which to judge of the physical characteristics of cast metals. There are two conto judge of the physical characteristics of cast metals. There are two conditions that are absolutely necessary to be known before we can make a fair comparison of different materials: namely, whether the casting was made in dry or green sand or in a chill, and whether it was attached to a larger casting or cast by itself. It has also been found that chill-castings give higher results thus sand-castings, and that bars cast by themselves purposely for testing almost invariably run higher than test-bars attached to castings. It is also a fact that bars cut out from castings are generally we can take the condition of the condition

fact of all alloys. They are exceedingly subject to variation in density and in grain, caused by differences in method of molding and casting, temperature of pouring, size and shape of casting, depth of "sinking head," etc.

## Aluminum Hardened by Addition of Copper Rolled Sheets .04 Inch Thick. (The Engineer, Jan 2, 1891.)

Al. Per cent.	Cu. Per cent.	Sp. Gr. Calculated.	Sp. Gr. Determined.	Tensile Strength in pounds per square inch.
100 98	2	2.78	2.67 2.71	26,535 43,563
96	4	2.90	2.77	44,130
94 92	8	$\frac{3.02}{3.14}$	2.82 2.85	54,778 50,374

## Tests of Aluminum Allovs.

(Engineer Harris, H. S. N., Trans, A. I. M. E., vol. xviii)

(magine or alternation of or alternation and a								
Composition.					Tensile	Elastic	Elonga-	Reduc-
Cop- per.	Alumi- num.	Silicon.	Zine.	Iron.	Strength, per sq. in. lbs.		tion, per ct.	Area, per et.
91.50% 88.50 91.50 90.00 63.00 63.00 91.50 93.00 88.50 92.00	6.50% 9.33 6.50 9.00 3.33 3.33 6.50 6.50 9.33 6.50	1.75% 1.66 1.75 1.00 0.33 0.33 1.75 0.50 1.66 0.50	33.33% 33.33	0.25% 0.50 0.25 0.25	60,700 66,000 67,600 72,830 82,200 70,400 59,100 53,000 69,930 46,530	18,000 27,000 24,000 33,000 60,000 55,000 19,000 19,000 33,000 17,000	23.2 3.8 13. 2.40 2.33 0.4 15.1 6.2 1.33 7.8	30.7 7.8 21.62 5.78 9.88 4.33 23.59 15.5 3.30 19.19

For comparison with the above 6 tests of "Navy Yard Bronze," Cu 88, Sn 10, Zn 2, are given in which the T. S. ranges from 18,000 to 24,590, E. L. from 10,000 to 13,000, El. 2,5 to 5,8, Red. 4.7 to 10,89.

## Alloys of Aluminum, Silicon and Iron.

M. and E. Bernard have succeeded in obtaining through electrolysis, by treating directly and without previous purification, the aluminum earths (red and white bauxites) the following:

Alloys such as ferro-aluminum, ferro-silicon-aluminum and silicon-aluminum, where the proportion of silicon may exceed 10% which are employed in the metallurgy of iron for refining steel and cast-iron.

Also silicon-aluminum, where the proportion of silicon does not exceed 10% which may be employed in mechanical constructions in a rolled or hammered condition, in place of steel, on account of their great resistance, especially where the lightness of the piece in construction constitutes one of the main conditions of success.

The following analyses are given:

Types.

1. Alloys applied to the metallurgy of iron, the refining of steel and cast iron:

Iron.

Aluminum.

Silicon. Manganese.

No. 1	70%	25%	5%	0%
No. 2	70	20	10	0
No. 3	70	15	15	0
No. 4	70	10	20	0
No. 5	70	10	10	10
No. 6	70	trace	20	10
2. Mechanical alloys:				
Types.		Aluminum.	Silico	n. Iron.
No. 1		92%	6.759	1.25%
No. 2		90	9.25	0.75
No. 3		90	10.00	trace.

Up to this time it has been thought that silicon was rather injurious when alloyed with aluminum. From numerous experiences it has been demonstrated that it gives to aluminum some remarkable properties of resistance; the best results were with alloys where the proportion of iron was very low, and the proportion of silicon in the neighborhood of 10%. Above that proportion the alloy becomes crystalline and can no longer be employed. The density of the alloys of silicon is approximately the same as that of alumi-

num.—La Metallurgie, 1892.

Tungsten and Aluminum.—Mr. Leinhardt Mannesmann says that the addition of a little tungsten to pure aluminum or its alloys communicates a remarkable resistance to the action of cold and hot water, salt water and other re-agents. When the proportion of tungsten is sufficient the alloys offer great resistance to tensile strains.

Aluminum and Tiu.—M. Bourbouze has compounded an alloy of aluminum and tin, by fusing together 100 parts of the former with 10 parts of the latter. This alloy is paler than aluminum, and has a specific gravity of 2.85. The alloy is not as easily attacked by several reagents as aluminum is, and it can also be worked more readily. Another advantage is that it can be soldered as easily as bronze, without further preliminary prepara-

Aluminum-Antimony Alloys, -Dr. C. R. Alder Wright describes some aluminum-antimony alloys in a communication read before the Society of Chemical Industry. The results of his researches do not disclose the existence of a commercially useful alloy of these two metals, and have greater scientific than practical interest. A remarkable point is that the alloy with the chemical composition Al Sb has a higher melting point than either aluminum or antimony alone, and that when aluminum is added to pure antimony the melting-point goes up from that of antimony (450° C.) to a certain temperature rather above that of silver (1000° C.).

#### ALLOYS OF MANGANESE AND COPPER.

Various Manganese Alloys. -E. H. Cowles, in Trans. A. I. M. E., vol. xviii, p. 495, states that as the result of numerous experiments on mixtures of the several metals, copper, zinc, tin, lead, aluminum, iron, and manganese, and the metalloid silicon, and experiments upon the same in ascertaining tensile strength, ductility, color, etc., the most important determinations appear to be about as follows:

1. That pure metallic manganese exerts a bleaching effect upon copper more radical in its action even than nickel. In other words, it was found that 181/4% of manganese present in copper produces as white a color in the resulting alloy as 25% of nickel would do, this being the amount of each

required to remove the last trace of red.

2. That upwards of 20% or 25% of manganese may be added to copper without reducing its ductility, although doubling its tensile strength and chang-

ing its color.

3. That manganese, copper, and zinc when melted together and poured into moulds behave very much like the most "yeasty" German silver, producing an ingot which is a mass of blow-holes, and which swells up above the mould before cooling.

4. That the alloy of manganese and copper by itself is very easily

oxidized.

5. That the addition of 1.25% of aluminum to a manganese-copper alloy converts it from one of the most refractory of metals in the casting process

into a metal of superior casting qualities, and the non-corrodibility of which is in many instances greater than that of either German or nickel silver. A "silver-bronze" alloy especially designed for rods, sheets, and wire has the following composition: Manganese, 18; aluminum, 1.20; silicon, 0.5; zinc, 13; and copper, 67:55. It has a tensile strength of about 57,000 pounds on small bars, and 20% elongation. It has been rolled into thin plate and drawn into wire .008 inch in diameter. A test of the electrical conductivity of this wire (of size No. 32) shows its resistance to be 41,44 times that of pure copper. This is far lower conductivity than that of German silver.

Manganese Bronze, (F. L. Garrison, Jour. F. I., 1891.)—This alloy has been used extensively for casting propeller-blades. Tests of some made by B. H. Cramp & Co., of Philadelphia, gave an average elastic limit of 30,000 pounds per square inch, tensile strength of about 60,000 pounds per square inch. with an elongation of 8% to 10% in sand castings. When rolled, the elastic limit is about 80,000 pounds per square inch, tensile strength

95,000 to 106,000 pounds per square inch, with an elongation of 12% to 15%.

Compression tests made at United States Navy Department from the
metal in the pouring-gate of propeller-hub of U. S. Maine gave in two tests
a crushing stress of 126,450 and 135,750 lbs. per sq. in. The specimens were 1 inch high by  $0.7 \times 0.7$  inch in cross-section = 0.49 square inch. Both specimens gave way by shearing, on a plane making an angle of nearly 45° with the direction of stress.

A test on a specimen  $1 \times 1 \times 1$  inch was made from a piece of the same pouring-gate. Under stress of 150,000 pounds it was flattened to 0.72 lnch high by about  $11/4 \times 1/4$  inches, but without rupture or any sign of distress.

ngn by about 14 × 14 inches, but without rupture or any sign of distress. One of the great objections to the use of manganese bronze, or in fact any alloy except iron or steel, for the propellers of iron ships is on account of the galvanic action set up between the propeller and the stern-posts. This difficulty has in great measure been overcome by putting strips of

This difficulty has in great measure over overtone by putting scrips of rolled time around the propeller apertures in the stern-frames.

The following analysis of Parsons' manganese bronze No. 2 was made from a chip from the propeller of Mr. W. K. vanderbilt's yacht Alva.

CopperZinc	88.644
Tin	8.700
IronLead	0.295
Phosphorus	trace
	99.923

It will be observed there is no manganese present and the amount of zinc is very small.

E. H. Cowles, Trans. A. I. M. E., vol. xviii, says: Manganese bronze, so called, is in reality a manganese brass, for zinc instead of tin is the chief element added to the copper. Mr. P. M. Parsons, the proprietor of this brand of metal, has claimed for it a tensile strength of from 24 to 28 tons on small bars when cast in sand. Mr. W. C. Wallace states that brass-founders of high repute in England will not admit that manganese bronze has more than from 12 to 17 tons tensile strength. Mr. Horace See found tensile strength of 45,000 pounds, and from % to 12½% elongation.

## GERMAN-SILVER AND OTHER NICKEL ALLOYS.

	Copper.	Nickel.	Zinc.	
Chinese packfong	. 40.4	31.6	6.5	parts.
" tutenag	. 8	3	6.5	46
German silver	. 2	1	1	**
" (cheaper)	. 8	2	3.5	44
" (closely resembles sil		3	3.5	44

For analyses of some German-silvers see page 326.

German Silver.—The composition of German silver is a very uncertain thing and depends largely on the honesty of the manufacturer and the price the purchaser is willing to pay. It is composed of copper, zinc, and nickel in varying proportions. The best varieties contain from 18% to 25% of nickel and from 20% to 30% of zinc, the remainder being copper. The more expensive nickel silver contains from 25% to 33% of nickel and from 75% to 66% of copper. The nickel is used as a whitening element; it also strengthens the alloy and renders it harder and more non-corrodible than the brass made without it, of copper and zinc. Of all troublesome alloys to handle in the foundry or rolling mill, German silver is the worst. It is unmanageable and refractory at every step in its transition from the crude elements into rods, sheets, or wire. (E. H. Cowles, Trans. A. I. M. E., vol. xviii, p. 494.)

#### ALLOYS OF BISMUTH.

By adding a small amount of bismuth to lead that metal may be hardened and toughened. An alloy consisting of three parts of lead and two of bismuth has ten times the hardness and twenty times the tenacity of lead. The alloys of bismuth with both in and lead are extremely fusible, and take fine impressions of casts and moulds. An alloy of one part bismuth, two parts in, and one part lead is used by pewter-workers as a soft solder, and by soap-makers for moulds. An alloy of five parts bismuth, two parts in, and three parts lead melts at 199° F, and is somewhat used for stereotyping, and for metallic writing-pencils. Thorpe gives the following proportions for the better-known fusible metals:

Name of Alloy.	Bismuth.	Lead.	Tin.	Cad- mium		Melting- point.
Newton's. Rose's D'Arcet's D'Arcet's with mercury. Wood's. Lipowitz's. Guthrie's "Entectic"	50 50 50 50 50 50 50	81.25 28.10 25.00 25.00 25.00 26.90 20.55	24.10 25.00 25.00 12.50 12.78	12.50 10.40	250.0	202° F. 203° " 201° " 113° " 149° " 149° " "Very low."

The action of heat upon some of these alloys is remarkable. Thus, Lipo-The action of neat upon some of these alloys is remarkable. Thus, Lipowitz's alloy, which solidifies at 149° Fah., contracts very rapidly at first, as it cools from this point. As the cooling goes on the contraction becomes slower and slower, until the temperature falls to 101.3° Fah. From this point the alloy expands as it cools, until the temperature falls to about 77° Fah., after which it again contracts, so that at 32° F. a bar of the alloy has the same length as at 115° F.

Alloys of bismuth have been used for making fusible plugs for boilers, but it is found that they are altered by the continued action of heat, so that one cannot rely upon them to melt at the proper temperature. Pure Banca tin

is used by the U. S. Government for fusible plugs.

## FUSIBLE ALLOYS. (From various sources.)

Sir Isaac Newton's, bismuth 5, lead 3, tin 2, melts at	2120	F.
Rose's, bismuth 2, lead 1, tin 1, melts at	200	66
Wood's, cadmium 1, bismuth 4, lead 2, tin 1, melts at	165	66
Guthrie's, cadmium 13.29, bismuth 47.38, lead 19.36, tin 19.97, melts at.	160	"
Lead 3, tin 5, bismuth 8, melts at	208	66
Lead 1, tin 3, bismuth 5, melts at	212	66
Lead 1, tin 4, bismuth 5, melts at	240	"
Tin 1, bismuth 1, melts at	286	66
Lead 2, tin 3, melts at	334	66
Tin 2, bismuth 1, melts at	336	66
Lead 1, tin 2, melts at	360	66
Tin 8, bismuth 1, melts at	392	66
Lead 2, tin 1, melts at	475	46
Lead 1, tin 1, melts at	466	66
Lead 1, tin 3, melts at	334	66
Tin 3, bismuth 1, melts at	392	66
Lead 1, bismuth 1, melts at		
Lead 1, Tin 1, bismuth 4, melts at	201	66
Lead 5, tin 3, bismuth 8, melts at	202	66
Tin 3, bismuth 5, melts at	202	66

#### BEARING-METAL ALLOYS.

(C. B. Dudley, Jour. F. I., Feb. and March, 1892.)

Alloys are used as bearings in place of wrought iron, cast iron, or steel. partly because wear and friction are believed to be more rapid when two metals of the same kind work together, partly because the soft metals are more easily worked and got into proper shape, and partly because it is desirable to use a soft metal which will take the wear rather than a hard metal, which will wear the journal more rapidly.

A good bearing-metal must have five characteristics: (1) It must be strong

enough to carry the load without distortion. Pressures on car-journals are frequently as high as 350 to 400 lbs. per square inch.

(2) A good bearing-metal should not heat readily. The old copper-tin bearing, made of seven parts copper to one part tin, is more apt to heat than some other allows. In general, research seems to show that the harder the bearing-metal, the more likely it is to heat.

(3) Good bearing-metal should work well in the foundry. Oxidation while melting causes spongy castings. It can be prevented by a liberal use of powdered charcoal while melting. The addition of 1½ to 2% of zinc or a small amount of phosphorus greatly aids in the production of sound castings. This is a principal element of value in phosphor-bronze,

(4) Good bearing-metals should show small friction. It is true that friction is almost wholly a question of the lubricant used; but the metal of the bearing has certainly some influence.

(5) Other things being equal, the best bearing-metal is that which wears

slowest.

The principal constituents of bearing-metal alloys are copper, tin, lead, zinc, antimony, iron, and aluminum. The following table gives the constituents of most of the prominent bearing-metals as analyzed at the Pennsylvania Railroad laboratory at Altoona.

## Analyses of Bearing-metal Alloys.

Metal.	Cop- per.	Tin.	Lead.	Zine.	Anti- mony.	Iron.
Camelia metal. Anti-friction metal. White metal. Car-brass lining. Salgee anti-friction Graphite bearing-metal Antimonial lead. Carbon bronze. Cornish bronze. Cornish bronze. Delta metal. *Magnolia metal. American anti-friction metal. Tobin bronze. Graney bronze. Damascus bronze. Manganese bronze. Manganese bronze. Ajax metal. Anti-friction metal. Harrington bronze. Car-box metal. Hard lead	70.20 1.60 4.01 75.47 77.83 92.39 trace 59.00 75.80 76.41 90.52 81.24	4.25 98.13 trace 9 91 14.38 9.72 9.60 2.37 2.16 9.20 10.60 9.58 10.98	87.92 84.87 1.15 67.73 80.69 14.57 12.40 83.55 78.44 0.31 15.06 12.52  7.27 88.32  84.33 94.40	85.57 trace trace 0.98 38.40 42.67 trace	12.08 15.10 16.73 18.83 16.45 19.60	0.55 trace
Ex. B. metal	76.80	8.00				

Other constituents:

(1) No graphite.

(5) No manganese.(6) Phosphorus or arsenic, 0.37. (2) Possible trace of carbon.

(3) Trace of phosphorus. (7) Phosphorus, 0.94. (4) Possible trace of bismuth. (8) Phosphorus, 0.20.

\* Dr. H. C. Torrey says this analysis is erroneous and that Magnolia

metal always contains tin. As an example of the influence of minute changes in an alloy, the Harrington bronze, which consists of a minute proportion of iron in a copperzinc alloy, showed after rolling a tensile strength of 75,000 lbs. and 20% elongation in 2 inches.

In experimenting on this subject on the Pennsylvania Railroad, a certain

number of the bearings were made of a standard bearing-metal, and the same number were made of the metal to be tested. These bearings were placed on opposite ends of the same axle, one side of the car having the standard bearings, the other the experimental. Before going into service the bearings were carefully weighed, and after a sufficient time they were again weighed.

again weighed. The standard bearing-metal used is the "S bearing-metal" of the Phosphor-bronze Smelting Co. It contains about 79,70% copper, 9.50% lead. 10% tin, and 0.80% phosphorus. A large number of experiments have shown that the loss of weight of a bearing of this metal is 1 lb. to each 18,000 to 25,000 miles travelled. Besides the measurement of wear, observations were made on the frequency of "hot boxes" with the different metals.

The results of the tests for wear, so far as given, are condensed into the

following table:

Metal.	Composition.					
netar.	Copper.	Tin.	Lead.	Phos.	Arsenic.	of Wear.
Standard	79.70	10.00	9.50	0.80		100
Copper-tin	87.50	12.50				148
Copper-tin, second	d experimen	ıt, same m	retal			. 153
Copper-tin, third			tal <b></b>			
Arsenic-bronze		10.00			0.80	142
Arsenic-bronze	79.20	10.00	7.00		0.80	115
Arsenic-bronze	79.70	10.00	9.50		0.80	101
"K" bronze	77.00	10.50	12.50			92
"K" bronze, seco	nd experim	ent, same	metal			92.7
Alloy "B"	77.00	8.00	15.60			86.5

The old copper-tin alloy of 7 to 1 has repeatedly proved its inferiority to the phosphor-bronze metal. Many more of the copper-tin bearings heated than of the phosphor-bronze. The showing of these tests was so satisfactory that phosphor-bronze was adopted as the standard bearing-metal of

the Pennsylvania R.R., and was used for a long time.

The experiments, however, were continued. It was found that arsenic practically takes the place of phosphorus in a copper-tin alloy, and three fests were made with arsenic-bronzes as noted above. As the proportion tests were made with arsenic-bronzes as noted above. As the proportion to lead is increased to correspond with the standard, the durability increases as well. In view of these results the "K" bronze was tried, in which neither phosphorus nor arsenic were used, and in which the lead was increased above the proportion in the standard phosphor-bronze. The result was that the metal wore 7.30% slower than the phosphor-bronze. No trouble from heating was experienced with the "K" bronze more than with the standard.

Dr. Dudley continues:

At about this time we began to find evidences that wear of bearing-metal alloys varied in accordance with the following law: "That alloy which has the greatest power of distortion without rupture (resilience), will best resist wear." It was now attempted to design an alloy in accordance with this law, taking first the proportions of copper and tin, 916 parts copper to 1 of tin was settled on by experiment as the standard, although some evidence since that time tends to show that 12 or possibly 15 parts copper to 1 of tin might have been better. The influence of lead on this copper-tin alloy seems to be much the same as a still further diminution of tin. However, the tendency of the metal to yield under pressure increases as the amount of tin is diminished, and the amount of the lead increased, so a limit is set to the use of lead. A certain amount of tin is also necessary to keep the lead alloyed with the copper.

Bearings were cost of the metal noted in the table as alloy "B," and it wore 13.5 slower than the standard phosphor-bronze. This metal is now the standard bearing, metal of the Pensylvania Railroad, being slightly changed in composition to allow the use of phosphor-bronze scrap. The formula adopted is: Copper, 103 lbs.; phosphor-bronze, 60 lbs.; tin, 93 lbs.; toruma adopted is: Copper, 105 lost, plosphor-bronze, of lost, tin, 382 lost, lead, 2534 lbs. By using ordinary care in the foundry, keeping the metal well covered with charcoal during the melting, no trouble is found in casting good bearings with this metal. The copper and the phosphor-bronze can be put in the pot before putting it in the melting-hole. The tin and lead should be added after the pot is taken from the fire.

It is not known whether the use of a little zinc, or possibly some other

combination, might not give still better results. For the present, however, this alloy is considered to fulfil the various conditions required for good bearing-metal better than any other alloy. The phosphor-brouze had an ultimate tensile strength of 30,000 bts., with 65 elongation, whereas the alloy "B" had 24,000 lbs. tensile strength and 11% elongation.

(For other bearing-metals, see Alloys containing antimony, on next page.

## ALLOYS CONTAINING ANTIMONY.

VARIOUS ANALYSES OF BABBITT METAL AND OTHER ALLOYS CONTAINING ANTIMONY.

T	in.	Copper	Antimony.	Zinc.	Lead.	Bismuth.
	0	1	5 parts			
Harder Babbitt   9	9.3 6	1.8	8.9 per ct. 8 parts			
Britannia 8	$\frac{8.9}{5.7}$	3.7 1.0	7.4 per ct. 10.1	2.9		
" 8	$\frac{1.9}{1.0}$		16.2 16.	1.9		
" 2	0.5	10	25.5 62.	6.		
Plate pewter 8	$\frac{5}{9.3}$	1.8	13. 7.1			1.8
White metal 8	5 '	5	10.	Bearings	on Ger. lo	comotives.

\* It is mixed as follows: Twelve parts of copper are first melted and then 36 parts of tin are added; 24 parts of antimony are put in, and then 36 parts of tin, the temperature being lowered as soon as the copper is melted in order not to oxidize the tin and antimony, the surface of the bath being protected from contact with the air. The alloy thus made is subsequently remetted in the proportion of 50 parts of alloy to 100 tin. (Joshua Rose,)

White-metal Alloys.—The following alloys are used as lining metals by the Eastern Railroad of France (1890):

Number.	Lead.	Antimony.	Tin.	Copper.
1	65	25	0	10
2		11.12	83.33	5.55
3	70	20	10	0
4	80	8	12	0

No. 1 is used for lining cross-head slides, rod-brasses and axle-bearings; No. 2 for lining axle-bearings and connecting-rod brasses of heavy engines; No. 3 for lining eccentric straps and for bronze slide-valves; and No. 4 for

metallic rod-packing.

Some of the best-known white-metal alloys are the following (Circular of Hoveler & Dieckhaus, London, 1898):

		Tin.	Antimony.	Lead.	Copper.	Zinc.	
1.	Parsons'	86	1	2	- 2	27	
	Richards'	70	15	101/2	41/2	0	
3.	Babbitt's	55	18	231/2	31/2	0	
4.	Fentons'	16	0	0, ~	5	79	
5.	French Navy	71/2	0	7	7	871/2	
6.	German Navy	85	71/2	0	71/2	0	

"There are engineers who object to white metal containing lead or zinc. This is, however, a prejudice quite unfounded, inasmuch as lead and zinc often have properties of great use in white alloys."

It is a further fact that an "easy liquid" alloy must not contain more

than 18% of antimony, which is an invaluable ingredient of white metal for improving its hardness; but in no case must it exceed that margin, as this would reduce the plasticity of the compound and make it brittle.

Hardest alloy of tin and lead: 6 tin, 4 lead. Hardest of all tin alloys (?): 74

tin, 18 antimony, 8 copper.

Alloy for thin open-work, ornamental castings: Lead 2, antimony 1. White metal for patterns: Lead 10, bismuth 6, antimony 2, common brass 8, tin 10. Pype-metal is made of various proportions of lead and antimouy, from

17% to 20% antimony according to the hardness desired.

Babbitt Metals. (C. R. Tompkins, Mechanical News, Jan. 1891.) The practice of lining journal-boxes with a metal that is sufficiently fusi-

ble to be melted in a common ladle is not always so much for the purpose of securing anti-friction properties as for the convenience and cheapness of forming a perfect bearing in line with the shaft without the necessity of boring them. Boxes that are bored, no matter how accurate, require great care in fitting and attaching them to the frame or other parts of a machine.

It is not good practice, however, to use the shaft for the purpose of easing the bearings, especially if the shaft be steel, for the reason that the better bear is apt to spring it; the better plan is to use a mandrel of the same size or a trift; larger for this purpose. For slow-running journals, where the load is moderate, almost any metal that may be conveniently melted and will run free will answer the purpose. For wearing properties, with a moderate speed, there is probably nothing superior to pure zine, but when not combined with some other metal it shrinks so nuch in cooling that it cannot be held firmly in the recess, and soon works loose; and it lacks those anti-friction properties which are necessary in order to stand high speed.

For line-shafting, and all work where the speed is not over 300 or 400 r. p., an alloy of 8 parts zinc and 2 parts block-tin will not only wear longer than any composition of this class, but will successfully resist the force of a heavy load. The tin counteracts the shrinkage, so that the metal, if not overheated, will firmly adhere to the box until it is worn out. But this mixture does not possess sufficient anti-friction properties to warrant its use

in fast-running journals.

Among all the soft metals in use there are none that possess greater autifriction properties than pure lead; but lead alone is impracticable, for it is so soft that it cannot be retained in the recess. But when by any process lead can be sufficiently hardened to be retained in the boxes without materially injuring its anti-friction properties, there is no metal that will wear longer in light fast-running journals. With most of the best and most popular anti-friction metals in use and sold under the name of the Babbitt metal,

the basis is lead.

Lead and antimony have the property of combining with each other in all proportions without impairing the anti-friction properties of either. The antimony hardens the lead, and when mixed in the proportion of 80 parts lead by weight with 20 parts antimony, no other known composition of metals possesses greater anti-friction or wearing properties, or will stand a higher speed without heat or abrasion. It runs free in its melted state, has no shrinkage, and is better adapted to light high-speeded machinery than any other known metal. Care, however, should be manifested in using it, and it should never be heated beyond a temperature that will scorch a dry pine stick.

Many different compositions are sold under the name of Babbitt metal. Some are good, but more are worthless; while but very little genuine Babbitt metal is sold that is made strictly according to the original formula. Most of the metals sold under that name are the refuse of type-foundries and other smelting-works, melted and cast into fancy ingots with special brands,

and sold under the name of Babbitt metal.

It is difficult at the present time to determine the exact formulas used by the original Babbitt, the inventor of the recessed box, as a number of different formulas are given for that composition. Tin, copper, and antimony were the ingredients, and from the best sources of information the original proportions were as follows:

Another writer gives:

0 parts tin	=	89.3%	83.3%	
2 parts copper			8.3%	
A parts antimony	_	7 10	8 94	

The copper was first melted, and the antimony added first and then about ten or fifteen pounds of tin, the whole kept at a dull-red heat and constantly stirred until the metals were thoroughly incorporated, after which the balance of the tin was added, and after being thoroughly stirred again it was then cast into ingots. When the copper is thoroughly melted, and before the antimony is added, a handful of powdered charcoal should be thrown into the crucible to form a flux, in order to exclude the air and prevent the antimony from vaporizing; otherwise much of it will escape in the form of a vapor and consequently be wasted. This metal, when carefully prepared, is probably one of the best metals in use for lining boxes that are subjected to a heavy weight and wear; but for light fast-running journals the copper renders it more susceptible to friction, and it is more liable to heat than the metal composed of lead and antimony in the proportions just given.

#### SOLDERS.

Common solders, equal parts tin and lead; fine solder, 2 tin to 1 lead; cheap solder, 2 lead, 1 tin.

Fusing-point of tin-lead alloys:

	id 25 558° F.	Tin 11/2 to lead 1 334° 1
	' 10541	" 2" " 1340
	5511	" 3 " " 1 356
"1""		" 4 " " 1365
"1""	2441	" 5 " " 1378
"1""	1370	" 6 " " 1,381

Common pewter contains 4 lead to 1 tin.

Gold solder: 14 parts gold, 6 silver, 4 copper. Gold solder for 14-carat gold: 25 parts gold, 25 silver, 12½ brass, 1 zinc. Silver solder: Yellow brass 70 parts, zinc 7, tin 11½. Another: Silver 145

parts, brass (3 copper, 1 zinc) 73, zinc 4.
German-silver solder: Copper 38, zinc 54, nickel 8.

Novel's solders for aluminum:

Tir	1 100 pa	rts,	lead 5;	melts at	536° to 572° F.
	100		zinc 5:	**	536 to 612
44	1000		copper 10 to 15:	**	662 to 842
44	1000		-i-l-al 10 4- 15.		000 4- 040

Novel's solder for aluminum bronze: Tin 900 parts, copper 100, bismuth 2 to 3. It is claimed that this solder is also suitable for joining aluminum to copper, brass, zinc, iron, or nickel.

## ROPES AND CABLES.

## STRENGTH OF ROPES.

(A. S. Newell & Co., Birkenhead, Klein's Translation of Weisbach, vol. iii. part 1, sec. 2.)

Hemp.		Iro	n.	Steel.			
Girth.	Weight per Fathom.	Girth,	Weight per Fathom.	Girth.	Weight per Fathom.	Tensile Strength.	
Inches.	Pounds.	Inches,	Pounds.	Inches.	Pounds.	Gross tons.	
		11/2	11/2	1	1	2 3	
334	4	15%	2	41.0	41/	4 5 6 7 8 9	
41/3	5	124	21/2	11/2	11/2	6	
	1	200	31/2	15%	2 2½	7	
51/2	7	21/8	4	15% 134	21/2	8	
6	9	23/4	4½ 5	17/8	3	10	
61/2	10	25/8 25/8	5½ 6	2	31/2	11 12	
7	12	27/8	61/2	2 21/6 21/4	41/2	13 14 15	
71/2	14	31/8	71/2 8 81/2	23/8	5	16 17	
8	16	33/8	99 10	21/2	5½ 6	18	
81/2	18	35/8 93/	11 12	2½ 25% 234	61/2	20 22 24 26 28	
9½ 10 11	22 26 30	37/8	18 14	31/4	8	26	
11	30	41/1	15	33/8	9	30	
	"	43%	16			30 32 36	
. 19	94	41/2	18	31/2	10	36	

Flat Ropes.

Hemp.		Iron.		Steel.		
Girth.	Weight per Fathom.	Girth.	Weight. per Fathom.	Girth.	Weight per Fathom.	Tensile Strength.
Inches. 4 × 11/8 5 × 11/4 5 15/5 × 11/6 6 × 11/6 6 × 11/6 6 × 11/6 6 × 11/6 8 1/4 × 21/8 8 1/2 × 21/4 9 1/2 × 21/4 10 × 21/5 10 × 21/5	Pounds. 20 24 26 28 30 36 40 45 50 55 60	Inches. 214 × 14 215 × 15 234 × 56 234 × 56 314 × 56 334 × 11/16 4 × 11/16 4 × 14/4 × 34 4 × 34 4 × 34	Pounds.  11 13 15 16 18 20 22 25 25 28 32 34	Inches.  2 × ½ 2½ 4 × ½ 2½ 4 × ½ 2½ 5 × ½ 2½ 5 × ½ 3½ 8 × 3½ 3½ 8 × 3½ 3½ 8 × 3½	Pounds.  10 11 12 13 15 16 18 20	Gross tons. 20 23 27 28 32 36 40 45 50 60

# Working Load, Diameter, and Weight of Ropes and Chains. (Klein's Weisbach, vol. iii, part 1, sec. 2, p. 561.)

Hemp ropes: d= diam. of rope. Wire rope: d= diam. of wire, n= number of wires, G= weight per running foot, k= permissible load in pounds per square inch of section, P= permissible load on rope or chain. Oval chains: d= diam of fron used; inside dimensions of oval 1.5d and 2.6d. Each link is a piece of chain 2.6d long,  $G_0=$  weight of a single link = 2.10 $d^2$  lbs.; G= weight per running foot = 9.73 $d^2$  lbs.

	Hempen	Wire Rope.		
	Dry and Untarred.	Wet or Tarred.		
k (lbs.) =	1420	1160	17000 _	
d (ins.) =	0.03 \sqrt{P}	0.033 VP	$0.0087\sqrt{\frac{P}{n}}$	
P (lbs.) = $G$ (lbs.) =	$\begin{array}{c} 1120d^2 = 2855G \\ 1.28d^2 = 0.00035P \end{array}$	$\begin{array}{c} 916d^2 = 1975G \\ 1.54d^2 = 0.0005P \end{array}$	$\begin{array}{c} 13350nd^2 = 4590G \\ 2.91nd^2 = 0.000218P \end{array}$	

	Open-link Chain,	Stud-link Chain.
$\begin{array}{l} k \text{ (lbs.)} = \\ d \text{ (ins.)} = \\ P \text{ (lbs.)} = \\ G \text{ (lbs.)} = \end{array}$	$\begin{array}{c} 8500 \\ 0.0087 \ \sqrt[4]{P} \\ 13350 d^2 = 1360 G \\ 9.73 d^2 = 0.000737 P \end{array}$	$\begin{array}{c} 11400 \\ 0.0076 \sqrt{P} \\ 17800d^2 = 1660G \\ 10.65d^2 = 0.0006P \end{array}$

Stud Chains 4/3 times as strong as open-link variety. [This is contrary to the statements of Capt. Beardslee, U. S. N., in the report of the U. S. Test Board. He holds that the open link is stronger than the studded link. See p. 308 ante].

# STRENGTH AND WEIGHT OF WIRE ROPE, HEMPEN ROPE, AND CHAIN CABLES. (Klein's Weisbach.)

Breaking Load in tons of 2240 lbs.	Kind of Cable.	Girth of Wire Rope and of Hemp Rope Diameter of Iron of Chain, inches.	
1 Ton	Wire Rope	1.0	0.125
	Hemp Rope	2.0	0.177
	Chain	14	0.500
8 Tons	Wire Rope   Hemp Rope   Chain	2.0° 5.0 1/2 2.5°	0.438 0.978 2.667
12 Tons	Wire Rope	2.5	0.753
	Hemp Rope	7.0	2.036
	Chain	11/16	4.502
16 Tons	Wire Rope	2.0	1.136
	Hemp Rope	8.0	2.365
	Chain	13/16	6.169
20 Tons	Wire Rope	3.5	1.546
	Hemp Rope	9.0	3.925
	Chain	29/32	7.674
24 Tons	Wire Rope	4.0	2.043
	Hemp Rope	10.0	4.166
	Chain	31/32	8.836
30 Tons	Wire Rope	4.5	2.725
	Hemp Rope	11.0	5.000
	Chain	1.1/16	10.335
36 Tons	Wire Rope Hemp Rope	5.0 12.5	3.723 5.940 13.01
44 Tons	Wire Rope Hemp Rope	1.3/16 5.5 14.0	4.50 6.94
54 Tons	Chain	1.5/16	16.00
	Wire Rope	6.0	5.67
	Hemp Rope	5.0	7.92
	Chain	1.7/16	19.16

Length sufficient to provide the maximum working stress:

Hempen rope, dry and untarred	2855	feet.
" wet or tarred	1975	46
Wire rope	4590	"
Open-link chain	1360	6.6

means the tensions in the fibres caused by the rope's own weight can be considerably diminished.

Rope for Hoisting or Transmission. Manila Rope (C. W. Hunt Company, New York.)—Rope used for hoisting or for transmission of power is subjected to a very severe test. Ordinary rope chafes and grinds to powder in the centre, while the exterior may look as though

it was little worn.

In bending a rope over a sheave, the strands and the yarns of these strands slide a small distance upon each other, causing friction, and wear the rope

slide a small distance upon each other, causing friction, and wear the rope internally.

The "Stevedore" rope used by the C. W. Hunt Co. is made by lubricating

The "Stevenore" rope used by the C. W. Hunt Co. is made by indicating the fibres with plumbago, mixed with sufficient tallow to hold it in position. This lubricates the yarns of the rope, and prevents internal chafing and wear. After running a short time the exterior of the rope gets compressed and coated with the lubricant.

In manufacturing rope, the fibres are first spun into a yarn, this yarn being twisted in a direction called "right hand." From 20 to 80 of these yarns, depending on the size of the rope, are then put together and twisted in the opposite direction, or "left hand," into a straad. Three of these

strands, for a 3-strand, or four for a 4-strand rope, are then twisted together, the twist being again in the "right hand" direction. When the strand is twisted, it untwists each of the threads, and when the three strands are twisted together into rope, it untwists he strands, but again twists up the threads. It is this opposite twist that keeps the rope in twists up the threads. It is this opposite twist that keeps the rope in twist proper form. When a weight is hung on the end of a rope, the tendency is for the rope to untwist, and become longer. In untwisting the rope, it would twist the threads up, and the weight will prevolve until the strain of would wrise the intensity by an unit weight win recover until the Strain of the threads being twisted tighter. In making a rope it is impossible to make these strains exactly balance each other. It is this fact that makes it necessary to take out the "turns" in a new rope, that is, untwist it when it is put at work. The proper twist that should be put in the threads has been ascertained approximately by experience.

The amount of work that the rope will do varies greatly. It depends not only on the quality of the fibre and the method of laying up the rope, but also on the kind of weather when the rope is used, the blocks or sheaves over which it is run, and the strain in proportion to the strain put upon the rope. The principal wear comes in practice from defective or badly set

sheaves, from excess of load and exposure to storms,

The loads put upon the rope should not exceed those given in the tables, for the most economical wear. The indications of excessive load will be the twist coming out of the rope, or one of the strands slipping out of its proper twist coming out of the rope, or one of the strands slipping out of its proper position. A certain amount of twist comes out in using it the first day or two, but after that the rope should remain substantially the same. If it does not, the load is too great for the durability of the rope. If the rope wears on the outside, and is good on the inside, it shows that it has been chaffed in running over the pulleys or sheaves. If the blocks are very small, it will increase the sliding of the strands and threads, and result in a more rapid internal wear. Rope made for hoisting and for rope transmission is usually made with four strands, as experience has shown this to be the most serviceable.

The strength and weight of "stevedore" rope is estimated as follows:

Breaking strength in pounds = 720 (circumference in inches)2; Weight in pounds per foot = .032 (circumference in inches)2.

#### The Technical Words relating to Cordage most frequently heard are:

YARN. -Fibres twisted together.

THREAD.—Two or more small yarns twisted together.
STRING.—The same as a thread but a little larger yarns, STRAND .- Two or more large yarns twisted together.

CORD. - Several threads twisted together.

Rope.—Several strands twisted together. HAWSER .- A rope of three strands.

SHROUD-LAID. - A rope of four strands.

Cable -Three hawsers twisted together. Yarns are laid up left-handed into strands.

STRANDS are laid up right-handed into rope.

HAWSERS are laid up left-handed into a cable. A rope is:

LAID by twisting strands together in making the rope.

SPLICED by joining to another rope by interweaving the strands.
WHIPPED.—By winding a string around the end to prevent untwisting.
SERVED.—When covered by winding a yarn continuously and tightly around it

Parceled.—By wrapping with canvas.

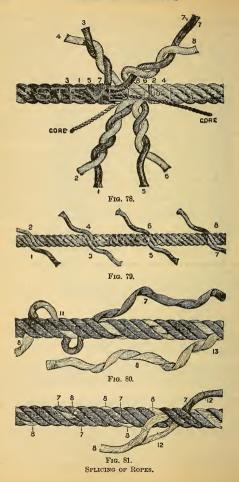
SEIZED .- When two parts are bound together by a yarn, thread or string. PAYED.—When painted, tarred or greased to resist wet.

HAUL.-To pull on a rope. TAUT .- Drawn tight or strained.

Splicing of Ropes. - The splice in a transmission rope is not only the weakest part of the rope but is the first part to fail when the rope is worn out. If the rope is larger at the splice, the projecting part will wear on the pulleys and the rope fall from the cutting off of the strands. The following directions are given for splicing a 4-strand rope.

The engravings show each successive operation in splicing a 134 inch

manila rope. Each engraving was made from a full-size specimen.



Tie a piece of twine, 9 and 10, around the rope to be spliced, about 6 feet from each end. Then unlay the strands of each end back to the twine. But the ropes together and twist each corresponding pair of strands

loosely, to keep them from being tangled, as shown in Fig. 78.

The twine 10 is now cut, and the strand 8 unlaid and strand 7 carefully laid

in its place for a distance of four and a half feet from the junction. The strand 6 is next unlaid about one and a half feet and strand 5 laid in

its place. The ends of the cores are now cut off so they just meet.

Unlay strand 1 four and a half feet, laying strand 2 in its place.

Unlay strand 3 one and a half feet, laying in strand 4.

Cut all the strands off to a length of about twenty inches, for convenience in manipulation.

The rope now assumes the form shown in Fig. 79 with the meeting points

of the strands three feet apart.

Each pair of strands is successively subjected to the following operation: From the point of meeting of the strands 8 and 7, unlay each one three turns; split both the strand 8 and the strand 8 in halves as far back as they are now unlaid and "whip" the end of each half strand with a small piece of twine.

The half of the strand 7 is now laid in three turns and the half of 8 also laid in three turns. The half strands now meet and are tied in a simple

knot, 11, Fig. 80, making the rope at this point its original size

The rope is now opened with a mariin spike and the half strand of worked around the half strand of 8 by passing the end of the half strand 7 worked around the had sainton or passing drawn taut and again worked around this half strand until it reaches the half strand is that was not laid in. This half strand 13 is now split, and the half strand 7 drawn through the opening thus made, and then tucked under the two adjacent strands, as shown in Fig. 81. The other half of the strand 8 is now wound around the other half of the strand 8 is now wound around the other half strand 7 in the same manner. After each pair of strands habeen treated in this manner, the ends are cut off at 12, leaving them about four inches long. After a few days' wear they will draw into the body of the rope or wear off, so that the locality of the splice can scarcely be detected.

Coal Hoisting. (C. W. Hunt Co.).—The amount of coal that can be hoisted with a rope varies greatly. Under the ordinary conditions of use a rope hoists from 5000 to 8000 tons. Where the circumstances are more a rope hoists from 5000 to 8000 tons. Where the circumstances are more favorable, the amounts run up frequently to 12,000 or 15,000 tons, occasionally to 20,000 and in one case 32,400 tons to a single fall.

When a hoisting rope is first put in use, it is likely from the strain put upon it to twist up when the block is loosened from the tub. This occurs in the first day or two only. The rope should then be taken down and the "turns" taken out of the rope. When put up again the rope should give no further trouble until worn out.

It is necessary that the rope should be much larger than is needed to bear

the strain from the load.

Practical experience for many years has substantially settled the most economical size of rope to be used which is given in the table below.

Hoisting ropes are not spliced, as it is difficult to make a splice that will not pull out while running over the sheaves, and the increased wear to be

obtained in this way is very small.

Coal is usually hoisted with what is commonly called a "double whip;" that is, with a running block that is attached to the tub which reduces the strain on the rope to approximately one half the weight of the load hoisted. The following table gives the usual sizes of hoisting rope and the proper working strain:

## Stevedore Hoisting-rope.

## C W Hunt Co

C. W. Hall Co.					
Circumference of the rope in ins.	Proper Working Strain on the Rope in lbs.	Nominal size of Coal tubs. Double whip.	Approximate Weight of a Coil, in lbs.		
3 3½ 4 4 4½ 5	350 500 650 800 1000	1/6 to 1/5 tons. 1/5 " 1/4 " 1/4 " 1/2 " 1/4 " 1/3 " 1/4 " 1/4 " 1/4 " 1/4 " 1/4 " 1/4 " 1/4 " 1/4 "	360 480 650 830 960		

Hoisting rope is ordered by circumference, transmission rope by diameter.

## Weight and Strength of Manila Cordage.

Dodge Manufacturing Co.

Second   S	Douge Manufacturing Co.									
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Size, Diameter in inches.	of oms in 1	Ø ≱ S	Feet in a pound.	Size. Diameter in inches.	of ms in 1	B, ≷ B	Feet in a pound.		
2/4 1 112 21,000 1 0/8	1	12 18 24 30 37 46 65 80 98 120 142 170 200 230 271	780 1,000 1,280 1,562 2,250 3,062 4,000 5,000 6,250 7,500	25 20 17 8 13 9 3 7 6 6	13/6 11/5 1 9/16 15/8 13/4 2 21/8	390 435 480 581 678 797	18,062 20,250 22,500 25,000 30,250 36,000 42,250 49,000 56,250 64,000 72,250 81,000	1 6 1 5 1 3 1 102/3		

T. Spencer Miller (Eng'a News, Dec. 6, 1890) gives the following table of breaking strength of manila rope, which he considers more reliable than the strength computed by Mr. Hunt's formula, Breaking strength = 720 × (circumference in inches)<sup>2</sup>. Mr. Miller's formula is: Breaking weight lbs. = circumference2 x a coefficient which varies from 900 for 1/2" to 700 for 2" diameter rope, as shown in the table,

Diam.	Circum- ference. in.	Ultimate Strength. lbs.	Coeffi- cient.	Diam. in.	Circum- ference.	Ultimate Strength. lbs.	Coeffi- cient.
1/2 5/8 5/4 7/8 1 11/8	11½ 2 21¼ 23¼ 33¼ 31½	2,000 3,250 4,000 6,000 7,000 9,350	900 845 820 790 780 765	11/4 13/8 11/2 15/8 17/8	33/4 41/4 41/2 5 51/2 6	10,000 13,000 15,000 18,200 21,750 25,000	760 745 735 725 712 700

For rope-driving Mr. Hunt recommends that the working strain should not exceed 1/20 of the ultimate breaking strain. For further data on ropes see "Rope-driving."

Knots .- A great number of knots have been devised of which a few only are illustrated, but those selected are the most frequently used. In the cuts, Fig. 82, they are shown open, or before being drawn taut, in order to show the position of the parts. The names usually given to them are:

- A. Bight of a rope. Simple or Overhand knot.
- В. Figure 8 knot.
- C. D. Double knot.
- Boat knot.
- E. F. Bowline, first step.
- G. Bowline, second step. H. Bowline completed.
- I.
- Square or reef knot.
- Ĵ. Sheet bend or weaver's knot.
- K. Sheet bend with a toggle. L. Carrick bend.
- M.
- Stevedore knot completed. Stevedore knot commenced.
- Slip knot.

- P. Flemish loop.
- Chain knot with toggle.
- Half-hitch.
- Timber-hitch.
- Clove hitch.
- Rolling-hitch.
- Timber-hitch and half-hitch.
- W. Blackwall-hitch.
- X. Fisherman's bend.
- Ÿ. Round turn and half-hitch.
- Z. Wall knot commenced.
- A A. B B. " completed.
- Wall knot crown commenced.
- CC. completed.

345 KNOTS.

The principle of a knot is that no two parts, which would move in the same direction if the rope were to slip, should lay along side of and touching each other.

The bowline is one of the most useful knots, it will not slip, and after being strained is easily untied. Commence by making a bight in the rope, then put the end through the bight and under the standing part as shown in

their put the end thought the vight and under the standing part as  $a_{ij}$  and  $a_{ij}$  then pass the end again through the bight, and haul tight. The square or reef knot must not be mistaken for the "granny" knot that slips under a strain. Knots H, K and M are easily untied after being under strain. The knot M is useful when the rope passes through an eye and is held by the knot, as it will not slip and is easily untied after being strained.

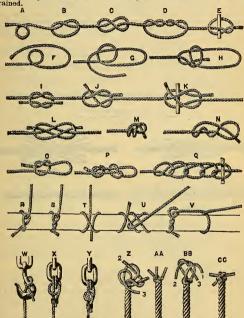


FIG. 82,-KNOTS.

The timber hitch S looks as though it would give way, but it will not; the greater the strain the tighter it will hold. The wall knot looks complicated, but is easily made by proceeding as follows: Form a bight with strand 1 and pass the strand 2 around the end of it, and the strand 3 round the end and pass the strain Z at Z and Z are Z and Z and Z and Z and Z and Z are Z. Haul the ends taut when the appearance is as shown in AA. The end of the strand 1 mow laid over the centre of the knot, strand Z laid over 1 and 3 over Z, when the end of 3 is passed through the bight of 1 as shown in BB. Haul all the strands taut as shown in CC.

To Splice a Wire Rope.—The tools required will be a small marline spike, nipping cutters, and either clamps or a small hemp-rope sling with which to wrap around and untwist the rope. If a bench-vise is accessible it will be found convenient.

In splicing rope, a certain length is used up in making the splice. An allowance of not less than 16 feet for ½ inch rope, and proportionately longer for larger sizes, must be added to the length of an endless rope in

ordering.

ordering. Having measured, carefully, the length the rope should be after splicing, and marked the points M and M', Fig. 83, unlay the strands from each of E and E and E' to M and M' and cut off the centre at M and M', and then:

(1). Interlock the six unlaid strands of each end alternately and draw them together so that the points M and M' meet, as in Fig. 84.

(2). Unlay a strand from one end, and following the unlay closely, lay into

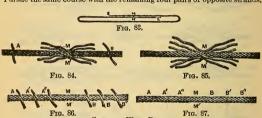
the seam or groove it opens, the strand opposite it belonging to the other end of the rope, until within a length equal to three or four times the length of one lay of the rope, and cut the other strand to about the same length from the point of meeting as at A, Fig. 85.

(3). Unlay the adjacent strand in the opposite direction, and following the

unlay closely, lay in its place the corresponding opposite strand, cutting the ends as described before at B, Fig. 85.

There are now four strands laid in place terminating at A and B, with the eight remaining at MM, as in Fig. 85. It will be well after laying each pair of strands to tie them temporarily at

the points A and B. Pursue the same course with the remaining four pairs of opposite strands,



SPLICING WIRE ROPE. stopping each pair about eight or ten turns of the rope short of the preced-

ing pair, and cutting the ends as before.
We now have all the strands laid in their proper places with their respective ends passing each other, as in Fig. 86.

All methods of rope-splicing are identical to this point; their variety consists in the method of tucking the ends. The one given below is the one

most generally practiced.

Clamp the rope either in a vise at a point to the left of A, Fig. 86, and by a hand-clamp applied near A, open up the rope by untwisting sufficiently to cut the core at A, and seizing it with the nippers, let an assistant draw it out slowly, you following it closely, crowding the strand in its place until it is all laid in. Cut the core where the strand ends, and push the end back into its place. Remove the clamps and let the rope close together around it. Draw out the core in the opposite direction and lay the other strand in the centre of the rope, in the same manner. Repeat the operation at the five remaining points, and hammer the rope lightly at the points where the ends pass each other at A, A, B, B, etc., with small wooden mallets, and the splice is complete, as shown in Fig. 87.

If a clamp and vise are not obtainable, two rope slings and short wooden

levers may be used to untwist and open up the rope.

A rope spliced as above will be nearly as strong as the original rope and smooth everywhere. After running a few days, the splice, if well made, cannot be found except by close examination.

The above instructions have been adopted by the leading rope manufacturers of America.

## SPRINGS

**Definitions.**—A spiral spring is one which is wound around a fixed point or centre, and continually receding from it like a watch spring. A helical spring is one which is wound around an arbor, and at the same time nenear spring is one which is would around all around; and as the same time advancing like the thread of a screw. An elliptical or laminated spring is made of flat bars, plates, or "leaves," of regularly varying lengths, super-posed one upon the other.

Laminated Steel Springs.—Clark (Rules, Tables and Data) gives the following from his work on Railway Machinery, 1855:

$$\Delta = \frac{1.66L^3}{bt^3n};$$
  $s = \frac{bt^2n}{11.3L};$   $n = \frac{1.66L^5}{\Delta bt^2};$ 

 $\Delta$  = elasticity, or deflection, in sixteenths of an inch per ton of load, s = working strength, or load, in tons (2240 lbs.),

L = span, when loaded, in inches,

b = breadth of plates, in inches, taken as uniform, t = thickness of plates, in sixteenths of an inch,

n = number of plates

Note.-The span and the elasticity are those due to the spring when

North.—The span and the ended of a track of the replaced weighted.

2 When extra thick back and short plates are used, they must be replaced by an equivalent number of plates of the ruling thickness, prior to the employment of the first two formula. This is found by multiplying the number of extra thick plates by the cube of their thickness, and dividing by the cube of the ruling thickness. Conversely, the number of plates of the ruling thickness, conversely, the number of plates of the ruling thickness, conversely, the found to the same calculation. by a given number of extra thick plates, are found by the same calculation.

3. It is assumed that the plates are similarly and regularly formed, and that they are of uniform breadth, and but slightly taper at the ends. Reuleaux's Constructor gives for semi-elliptic springs:

$$P = \frac{Snbh^2}{6l} \quad \text{ and } \quad f = \frac{6Pl^3}{Enbh^3};$$
  $S = \max$ , direct fibre-strain in plate;  $b = \text{width of plates};$ 

n = number of plates in spring;

l = one half length of spring;
 P = load on one end of spring;

h = thickness of plates; f = deflection of end of spring; E = modulus of direct elasticity.

The above formula for deflection can be relied upon where all the plates of the spring are regularly shortened; but in semi-elliptic springs, as used, there are generally several plates extending the full length of the spring, and the proportion of these long plates to the whole number is usually about 5.5P/3 (1998).

one fourth. In such cases  $f = \frac{3.3F1^2}{Enbh^3}$ . (G. R. Henderson, Trans. A. S. M. E., vol. xvi.)

In order to compare the formulæ of Reuleaux and Clark we may make the following substitutions in the latter: s in tons = P in lbs. + 1120;  $\triangle s$  = 16t; then

$$\Delta s = 16f = \frac{1.66 \times 8l^3 \times P}{4096 \times 1120 \times nbh^3}, \text{ whence } f = \frac{Pl^3}{5,527,133},$$

which corresponds with Reuleaux's formula for deflection if in the latter we take E = 33.162.800.

Also 
$$s = \frac{P}{1120} = \frac{256nbh^2}{11.3 \times 2l}$$
, whence  $P = \frac{12.687nbh^2}{l}$ ,

which corresponds with Reuleaux's formula for working load when S in the

latter is taken at 76,120. The value of E is usually taken at 30,000,000 and S at 80,000, in which case Reuleaux's formulæ become

$$P = \frac{13,333nbh^2}{l} \quad \text{ and } \quad f = \frac{Pl^3}{5,000,000nbh^3}.$$

Helical Steel Springs .- Clark quotes the following from the report on Safety Valves (Trans. Inst. Engrs. and Shipbuilders in Scotland, 1874-5):

$$E = \frac{d^3 \times w}{D^4 \times C}.$$

E = compression or extension of one coil in inches.

d = diameter from centre to centre of steel bar constituting the spring, in inches,

w =weight applied, in pounds,

D = diameter, or side of the square, of the steel bar, in sixteenths of an

C = a constant, which may be taken as 22 for round steel and 30 for square steel.

Note. - The deflection E for one coil is to be multiplied by the number of

free coils, to obtain the total deflection for a given spring.

The relation between the safe load, size of steel, and diameter of coil, may be taken for practical purposes as follows:

$$D = \sqrt[3]{\frac{vd}{3}}, \text{ for round steel;}$$

$$D = \sqrt[3]{\frac{vd}{4}}, \text{ for square steel.}$$

Rankine's Machinery and Millwork, p. 390, gives the following:

$$\begin{split} \frac{W}{v} &= \frac{cd^4}{64nr^2}; \qquad W_1 = \frac{.196fd^3}{r}; \qquad v_1 = \frac{12.566nfr^2}{cd}; \\ &\frac{W_1}{2} = \text{greatest safe sudden load}. \end{split}$$

In which d is the diameter of wire in inches; c a co-efficient of transverse elasticity of wire, say 10,500,000 to 12,000,000 for charcoal iron wire and steel; radius to centre of wire in coil; n effective number of coils; f greatest safe shearing stress, say 30,000; W any load not exceeding greatest safe load; v corresponding extension or compression; W, greatest safe load; and v<sub>1</sub> greatest safe steady extension or compression.

greatest safe steady extension or compression. If the wire is square, of the dimensions  $d \times d$ , the load for a given deflection is greater than for a round wire of the diameter d in the ratio of 2.81 to 1.96 or of 1.43 to 1, or of 10 to 7, nearly. Wilson Hartnell (Proc. Inst. M. E., 1882, p. 426), says: The size of a spiral spring may be calculated from the formula on page 304 of "Rankine's Userlul Rules and Tables"; but the experience with Salter's springs has shown that the safe limit of stress is more than twice as great as there given, namely 60.000 to 70,000 lbs, per square inch of section with  $\frac{6}{2}$  inch wire, and about 50,000 with  $\frac{1}{2}$  inch wire. Hence the work that can be done by springs of wire is four or five times as great as Rankine allows. For  $\frac{3}{2}$  inch wire and under,

Maximum load in lbs. = 
$$\frac{12,000 \times (\text{diam. of wire})^3}{\text{Mean radius of springs}}$$
;

180,000 × (diam.)4 Weight in lbs. to deflect spring 1 in. =  $\frac{1}{\text{Number of coils} \times (\text{rad.})^3}$ 

The work in foot-pounds that can be stored up in a spiral spring would lift it above 50 ft.

In a few rough experiments made with Salter's springs the coefficient of rigidity was noticed to be 12,600,000 to 13,700,000 with 14 inch wire; 11,000,000 for 11/32 inch; and 10,600,000 to 10,900,000 for 36 inch wire.

Helical Springs.—J. Begtrup, in the American Machinist of Aug. 18, 1892, gives formulas for the deflection and carrying capacity of helical springs of round and square steel, as follow:

$$\begin{aligned} W &= .3927 \frac{Sd^3}{D-d^3} \\ F &= 8 \frac{P(D-d)^3}{Ed^4}, \end{aligned} \quad \begin{cases} \text{for round steel.} \\ W &= .471 \frac{Sd^3}{D-d^3} \\ F &= 4.712 \frac{P(D-d)^3}{Ed^4}, \end{cases}$$

W = carrying capacity in pounds,

S = greatest tensile stress per square inch of material,

d = diameter of steel, D = outside diameter of coil,

F =deflection of one coil, E =torsional modulus of elasticity,

P = load in pounds.

From these formulas the following table has been calculated by Mr. Begtrup. A spring being made of an elastic material, and of such shape as to allow a great amount of deflection, with the same extent as a rigid body, and a factor of safety very much less than for rigid constructions may be used.

#### HOW TO USE THE TABLE.

When designing a spring for continuous work, as a car spring, use a greater factor of safety than in the table; for intermittent working, as in

greater factor of safety than in the table; for intermittent working, as in a steam-engine governor or safety valve, use figures given in table; for square steel multiply line W by 1.2 and line F by .59.

Example 1.—How much will a spring of 3g. round steel and 3" outside diameter carry with safety? In the line headed D we find 3, and right underneath 473, which is the weight it will carry with safety. How many coils must this spring have so as to deflect 3" with a load of 400 pounds? Assuming a modulus of elasticity of 12 millions we find in the centre line headed F the figure .060; this is deflection of one coil for a load of 100 pounds; therefore .601 x 4 = .244" is deflection of one coil for 40 pounds load, and 3 + .244 = 123g is the number of coils wanted. This spring will therefore be 43" long when closed, counting working coils only, and stretch to 73".

+ .34 = 12/2 is the number of coils wanted. This spring will therefore be 43" long when closed, counting working coils only, and stretch to 73" Example 2.—A spring 33" outside diameter of 7/16" steel is wound close; how much can it be extended without exceeding the limit of safety? We find maximum safe load for this spring to be 702 pounds, and deflection one coil for 100 pounds load .0405 inches; therefore 7.02 \times .0405 = .284" is the greatest admissible opening between coils. We may thus, without knowing the load, ascertain whether a spring is overloaded or not.

#### Carrying Capacity and Deflection of Helical Springs of Round Steel.

d = diameter of steel. D = outside diameter of coil. W = safe working load in pounds—tensile stress not exceeding 60,000 pounds per square inch. F = deflection by a load of 100 pounds of one coil, and a modulus of elasticity of 10, 12 and 14 millions respectively. The ultimate carrying capacity will be about twice the safe load.

= .065" No. 16.	T	.25	.50	.75	1.00	1.25	1 10	1.75	0.00		t	
53.0	$D_{\cdot}$						1.50		2.00		1	1
5	$\bar{W}$	35	15	9	7	5	4.5	3.8	3.3		1	
	(	.0276	.3588	1.433	3.562	7 250	12.88	20.85	31.57			
115	$ F\rangle$										1	
2	14.3	.0236	.3075	1.228			11.04	17.87				
.0	1 /	.0197	.2562	1.023	2.544	5.178	9.200	14.89	22.55		1	
	`										1	
_	-		~~	. 00	4 05	4 50	4 60	0.00	2.05	0.00		
2	D	.50	.75	1.00	1.25	1.50	1.75	2.00	2.25	2.50		
≈ <del>-</del> :	· W	107	65	46	36	29	25	22	19	17		
.120″	- 1	.0206	.0937	.2556	.5412	.9856		2.492		5.056		
$d \equiv No$	$ F\rangle$											
11,5	F'	.0176	.0804	.2191	.4639	.8448	1.392	2.136		4.334		
77	1 1	.0147	.0670	.182	.3866	.7040	1.160	1.780	2.589	3.612		
	_ `											
	70	ME	1 00	* 05		4 000	0.00	0.05	0.50	0 80	0.00	
.180″	D	75	1.00	1.25	1.50	1.75	2.00	2.25	2.50	2.75		
œ ::	W	241	167	128	104	88	75	66	59	53	49	
Π.	- (	.0137	.0408	0907	.1703	.2866	.4466	.6571			1.660	
No. 1	- 1											
11 23	$F\langle$	.0118	.0350	.0778	1460	.2457	.3828	.5632	, 7928	1.077	1.423	
q		.0098	,0292	.0648	.1217	.2048	.3190	.4693	. 6607	.8975	1.186	
_											***	
	-	4 05	4 50	4 02	0.00	0.05	0.50	0.00	0.00	0.05	0.00	
5	D	1.25	1.50	1.75	2.00	2.25	2.50	2.75	3.00	3.25		
14"	W	368	294	245	210	184	164	147	134	123	113	
-1	-	.0199	.0389	.0672	.1067	.1593	.2270	.3109	.4139	.5375		
d II	$ F\rangle$	.0171	.0333	.0576	.0914	.1365						
~	15							.2665		.4607		
3		.0142	.0278	.0480	.0762	.1137	.1610	.2221	.2957	.3839	.4883	

# Carrying Capacity and Deflection of Helical Springs of Round Steel.—(Continued).

//91	$\frac{D}{W}$	1.50 605	1.75 500	2.00 426	2.25 371	2.50 329	2.75 295	3.00 267	3.25 245	3,50 226	3.75 209	4.00 195
d = 5/16''	1 (	.0136	.0242	.0392	.0593	.0854	.1187	.1583	.2066	.2640	.3312	.4089
11	$F_i^{j}$	.0117	.0207	.0336	.0508	.0732	.1012	.1357	.1771	.2263	.2839	.3505
-0												
3.00	$\frac{D}{W}$	2.00 765	2.25 663	2.50 589	2.75 523	3.00 473	$\frac{3.25}{433}$	$\frac{3.50}{398}$	3.75 368	4.00 343	4.25 321	4.50 301
1,8%	1	.0169	.0259	.0377	.0528	.0711	.0935	.1200	.1513	.1874	.2290	.2761
q = p	F	.0145	.0222	.0323	.0452	.0610	.0801	.1029	.1297	.1606	.1963	.2367
		.0120	.0185	.0269	.0376	.0508	.0668	.0858	.1081	.1338	. 1685	.1972
7/16"	$\frac{D}{W}$	2.00	2.25	2.50	2.75	3.00	3.25	3.50	3.75	4.00	4.50	5.00
7.	W	1263 .0081	1089 .0126	957 .0186	853 .0262	770 .0357	$702 \\ .0472$	.0617	596 .0772	544 .0960	486 .1423	.2016
11	$ F\langle $	.0069	.0108	.0160	.0225	.0306	.0405	.0529	.0661	.0823	.1220	.1728
q	(	.0058	.0090	.0133	.0187	.0255	.0337	.0441	.0551	.0686	.1017	.1440
>	D	2.00	2.25	2.50	2.75	3.00	3 25	3.50	3.75	4.00	4.50	5.00
12%	W	1963	1683 .0067	1472	1309 .0141	1178 .0194	1071 .0259	982 .0336	906 .0427	841 .0534	736 .0796	654
11	$F^{\downarrow}$	.0042	.0057	.0099	.0121	.0167	.0222	.0288	.0366	.0354	.0683	.0972
q	1	.0030	.0048	.0071	.0101	.0139	.0185	.0240	.0305	.0381	.0569	.0810
-	$\overline{D}$	2.50	2.75	3.00	3.25	3.50	3.75	4.00	4.25	4.50	5.00	5.50
= 9/16"	W	2163	1916	1720	1560	1427	1315	1220	1137	1065	945	849
6	$F^{\{}$	.0056	.0081	.0112	.0151	.0197	.0252	.0316 .0271	.0390	.0474	0.0679 $0.0582$	.0935
d =	1	.0040	.0058	.0080	.0108	.0141	.0180	.0225	.0278	.0339	.0485	.0668
	$\overline{D}$	2.50	2.75	3.00	3.25	3.50	3.75	4.00	4.25	4.50	5.00	5.50
2811	W	3068	2707	2422	2191	2001	1841	1704	1587	1484	1315	1180
II	$ _F \langle$	.0034	.0049	.0068	.0092	.0121	.0155 .0133	.0196	.0243		.0427 $.0366$	.0591
q:	F	.0029	.0042	.0058	.0066	.0086	.0111	.0140	.0173	.0212	.0305	.0422
	-	3:00	3.25	0.50	3.75	4.00	4.25	4.50	4.75	5.00		6.00
	$\frac{D}{W}$	3311	2988	3.50 2723	2500	2311	2151	2009	1885	1776	5.50 1591	1441
d = 11/16''	$F^{\int}$	.0043	.0058	.0077	.0100	.0127	.0157	.0193	.0233	.0279	.0388	.0522
=======================================	F'	.0037	.0050	.0066	.0086	.0108	.0135	.0165	.0200	.0239	.0333	.0447
	-											
34"	$\frac{D}{W}$	3.00	3.25 3976	3.50 3615	3.75 3313	4.00 3058	4.25 2840	4.50 2651	4.75 2485	5.00 2339	5.50 2093	6.00 1893
93,	1 /	.0028	.0038	.0051	.0066	.0084	.0105	.0129	.0157	.0189	.0264	.0356
q =	F	.0024	0033	.0044	.0057	.0072	.0090	.0111	.0135	.0162	.0226	.0305
	(	.0020	.0027	.0036	.0047	.0060	.0075	.0093	.0113	.0135	.0188	.0254
	D	3.50	3.75	4.00	4.25	4.50	4.75	5.00	5.25	5.50	6.00	6.50
1,8%	W	6013	5490 .0027	5051 .0035	4676	.0055	4073	3826 .0081	3607 .0097	3413	3080 .0156	2806
- 11	$ F\rangle$	.0018	.0024	.0030	.0038	.0047	.0058	.0070	.0083	.0098	.0134	.0177
q	1	.0015	.0020	.0025	.0032	.0039	.0048	.0058	.0069	.0082	.0112	.0148
_	$\frac{D}{W}$	3.50	3.75	4.00	4.25	4.50	4.75	5.00	5.25	5.50	6.00	6.50
1,	W	9425	8568 .0016	7854 .0021	7250 .0026	6732	6283	5890 .0049	5544	5236	4712	4284
11	$ F\rangle$	.0012	.0014	.0021	.0023	.0028	.0035	.0043	.0059	.0061	.0083	.0111
p	1	.0008	.0011	.0015	.0019	.0023	.0029	.0035	.0043	.0051	.0069	.0092
	-											

The formulæ for deflection or compression given by Clark, Hartnell, and Begtrup, although very different in form, show a substantial agreement when reduced to the same form. Let d= diameter of wire in inches,  $D_1=$  mean diameter of coil, n the number of coils, w the applied weight in pounds, and C a coefficient, then

Compression or extension of one coil =  $\frac{w\bar{D}_1^3}{Cd^4}$ ;

Weight in pounds to cause comp. or ext. of 1 in. =  $\frac{Cd^4}{nD.3}$ 

The coefficient C reduced from Hartnell's formula is  $8\times180,000=1,440,000$ ; according to Clark,  $16^4\times22=1,441,792$ , and according to Begtrup (using 12,000,000 for the torsional modulus of elasticity) = 12.000,000.  $6\times8=1,500,000$ .

Rankine's formula for greatest safe extension,  $v_1 = \frac{12,566nfr^2}{cd}$  may take

the form  $v_1 = \frac{.7854nD_1^2}{100d}$  if we use 30,000 and 12,000,000 as the values for f

and c respectively. The several formulæ for safe load given above may be thus compared, letting d= diameter of wire, and  $D_1=$  mean diameter of coil, Rankine,  $W=\frac{196 f^2}{f^2}$ ; Clark,  $W=\frac{3(d\times 16)^3}{D_1}$ ; Begtrup,  $W=\frac{3997 K 2l^3}{D_1}$ ; Hartnell,  $W=\frac{12000 d^3}{r}$ . Substituting for f the value 30,000 given by Rankine, and for

S, 60,000 as given by Begtrup, we have W=11,760  $\frac{d^3}{D_1}$  Rankine; 12,388  $\frac{d^3}{D_1}$  Clark; 23,562  $\frac{d^3}{D_2}$  Begtrup; 24,000  $\frac{d^3}{D}$  Hartnell.

Taking from the Pennsylvania Ralicoad specifications the capacity when closed of the following springs, in which d= diameter of wire, D diameter outside of coil,  $D_1=D-d$ , c capacity, H height when free, and h height when closed, all in inches.

No. 
$$T.$$
  $d=\frac{1}{4}$   $D=\frac{1}{3}$   $D_1=\frac{1}{4}$   $c=\frac{400}{1,900}$   $H=\frac{9}{6}$   $h=\frac{6}{5}$   $S.$   $\frac{1}{2}$   $\frac{1}{2}$   $\frac{9}{1,900}$   $0.7$   $\frac{41}{5}$   $0.7$   $0.1$ 

and substituting the values of c in the formula c=W=x  $\frac{d^3}{D_1}$  we find x, the coefficient of  $\frac{d^3}{D_1}$  to be respectively 32,000; 38,000; 32,400; 24,888; 34,560; 42,140, average 34,000. 42,140, average 34,000.

Taking 12,000 as the coefficient of  $\frac{d^2}{D_1}$  according to Rankine and Clark for safe load, and 24,000 as the coefficient according to Begtrup and Hartnell, we have for the safe load on these springs, as we take one or the other coefficient,

5,400 lbs.

J. W. Cloud (Trans. A. S. M. E., v. 173) gives the following:

$$P = \frac{S\pi d^3}{16R}$$
 and  $f = \frac{32PR^2l}{G\pi d^4}$ ;

P = load on spring;

Je boad on spring;
 S = maximum shearing fibre-strain in bar;
 d = diameter of steel of which spring is made;
 R = radius of centre of coil;
 l = length of bar before coil;
 G = modulus of shearing elasticity;

f = deflection of spring under load.

Mr. Cloud takes S = 80,000 and G = 12,600,000.

The stress in a helical spring is almost wholly one of torsion. For method of deriving the formulæ for springs from torsional formula see Mr. Cloud's paper, above quoted.

## ELLIPTICAL SPRINGS, SIZES, AND PROOF TESTS.

Pennsylvania Railroad Specifications, 1889.

	tw'n in.	r all,	shes.	of s.	Tests.	
Class.	Length be centres,	Width over inches.	Bands, inches.	Width of Plates, inches.	To stand ins. High,	With Load of lbs.
A, Triple	40	113/4	3 ×3/8	3	2 " "	5500 A. p. t.*
C, Quadruple	40	151/2	3 ×3/8	3		6650 8000 A. p. t.*
D, Triple	36	1134	3 ×3/8	3	14 " "	6000 8000
E, Single	40	sin.	3 ×3/8	3×11/32	and top of leaf.	When free 2350
F, Triple	36	1134	3 ×3/8	3×11/32	21/2 between bands.	11,800
G, Double	32	71/2	3 × 3/8	3	\\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\	When free 8000
H, Double	36	91/2	3 × 3/8	4	31/2 " "	5400 6000
K, {Double, } 6 plates }	22	105%	3½×3/8	4½×11/32	13/16 " "	13,800
L, Double, 7 plates	22	105/8	3½×3/8	4½×11/32		15,600
M, Quadruple	40	151/2	3 ×3/8	3	$\begin{cases} 4 & " & " \\ 3 & " & " \\ 2 & " & " \end{cases}$	8000 10,000 A. p. t.*

\* A. p. t., auxiliary plates touching,

### PHOSPHOR-BRONZE SPRINGS.

PHOSPHOR-BRONZE SPRINGS.
Wilfred Lewis (Engineers' Club, Philadelphia, 1887) made some tests with phosphor-bronze wire, .12 in. diameter, coiled in the form of a spiral spring, 1½ in. diameter from centre to centre, making 52 coils.
This spring was loaded gradually up to a tension of 30 lbs., but as the load was removed it became evident that a permanent set had taken place. Such a spring of steel, according to the practice of the P. R. R., might be used for 40 lbs. A weight of 21 lbs. was then suspended so as to allow a small amount of vibration, and the length measured from day to day. In 30 hours the spring lengthened from 20% inches to 21½ inches, and in 200 hours to 21¼ inches. It was concluded that 21 lbs. was too great for durability, and that probably 10 lbs. was as much as could be depended upon with safety.
For a given load the extension of the bronze spring was just double the extension of a similar steel spring, that is, for the same extension the steel spring is twice as strong.

spring is twice as strong.

# SPRINGS TO RESIST TORSIONAL FORCE. (Reuleaux's Constructor.)

P =force applied at end of radius or lever-arm R;  $\vartheta =$ angular motion at end of radius R; S = permissible maximum stress, = 4/5 of permissible stress in flexure; E = modulus of elasticity in tension; G = torsional modulus, = 2/5 E; I = developed length of spiral, or length of bar; d = diameter of wire; b = breadth of flat bar; h = thickness.

HELICAL SPRINGS FOR CARS AND LOCOMOTIVES. Arranged in Order of Strength. (Condensed from Specifications of Penna. R. R. Co., 1888 and 1891.)

	-	Capacity,	partly closed.	lbs. at height.	at 3½ in.		170 at 6	at 634		.200 at 6	at 53%	3,600 at 6	at 7		4,000 at 71/2	at 4		5,000 at 774	6,000 at 4 15/16		6,800 at 71/2		at 7		7,000 at 71/4	7.000 at 5 7/16		at 4/3	at 598	ar 5%3	21,000 at 5 27/32	18,500 at 6,5/16
	-	_		lbs. a	110		_	_	_	_		3,600	4,500 at		4,000	6,000 at 4		6,000	0000,9		6,800	:	7.000 at 7	:	2,000	2.000	000 07	13,000	13,500 at 598	10,100	21,000	18,500
		Compositor	Capacit	lbs.	130	240	270	400	200	1.900	2,100	6,000	7,500	8,100	10,000	10,000		11,000	13,000		14,000	16,000	16,000		19,000	19.000	00000	38,000	28,000	42,000	42,000	42,000
,		ght.	Closed.	inches.	တ	13%	20.	9	85%	۵,′۵	41/2	,,,,,	9	œ	23/2	33%	0/-	9	41/8		9	33%	23%	*	9	41%	2/10	828	458	8%	over places	23%
Coning	mide	Height	Free.	inches.	53/4	27%	000	6	277	, , , ,	2	· ∞	878	101%	, 6	51%	6/-	5	634		6	43/8	00		00	9	ì	278	8/18	8/0 /40	511/16 778	77%
		Diam, Out-	side of Coil.	inches.		23/4	1	11%	117	`co	53%	* · 9	2/2	22	œ	~ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	(8%)	20 9	386	800	3516	478		0 0 0	35%	- 450 - 470 - 470 - 470	(8%)	O t	0 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	01/00		5 5/16
obcomorano		Weight.	Normal. Minimum	lbs.	2//32		7/16	1 8/16	9/16	41%	105%	16	18	213%	321/2	16		3278	20		481/2	916	49		34	251%	2110	3472	200	3	7.1	59
ode mon		_	-	lbs.	74	7%	7%	11/4	2%	43%		161%	181/2	55	831/2	161%	2	367%	2034	1	51	8/26	201%		35	7,96	00.1	200%	40%	0172	<u></u>	5/09 J
Tooling of		Length after	Tapering.	inches.						823%	2696	952%	92,	1063/	108	600%	(8,00	1061/3	05%8	10614	10612	4114	9738	6317	163%	6438	0000	8/20	2882	8/02	. 24	67.7%
Ban	Dat.	Longth	Lengtin.	inches.	57.73	25/4	6	942/8	451%	781/2	881%	Z	82	1001/2	977%	523%	000	25	0 0	96	266	359%	2000	2517	727	.56%	24.74	0 92	513%	2000	401%	61
		Diamoton	Diameter.	inches.	9/64	74	11/64	74	77	7.	377	15/16	-		114	1	88.	01/61	178	1 3/16	18/16	11/8	138	871	4%	74%	4 hours 15 /10	4 0ars 15/16	4 "11/16	(4 " 18/18	4 " 19/32	4 "11/16
1	E.s.	R.	.q		7	闰	23	Ħ	A	202	М	ы	ئ	А	н	×	**	4	0	(	3	Ö	ı	1	×	Y	2	2 =	>	. ;	<b>3</b>	M

## RIVETED JOINTS.

# Fairbairn's Experiments. (From Report of Committee on Riveted Joints, Proc. Inst. M. E., April, 1881.)

The earliest published experiments on riveted joints are contained in the memoir by Sir W. Fairbairn in the Transactions of the Royal Society. Making certain empirical allowances, he adopted the following ratios as expressing the relative strength of riveted joints:

	100
Double-riveted joint	70
Single-riveted joint	56

These well-known ratios are quoted in most treatises on riveting, and are still sometimes referred to as having a considerable authority. It is singular, however, that Sir W. Fairbairn does not appear to have been aware that the proportion of metal punched out in the line of fracture ought to be different in properly designed double and single riveted joints. These celebrated ratios would therefore appear to rest on a very unsatisfactory analysis of

ratios would therefore appear to rest on a very unsatisfactory analysis of the experiments on which they were based.

Loss of Strength in Punched Plates.—A report by Mr. W. Parker and Mr. John, made in 1878 to Lloyd's Committee, on the effect of punching and drilling, showed that thin steel plates lost comparatively little from punching, but that in thick plates the loss was very considerable. The following table gives the results for plates punched and not annealed

or reamed:

Thickness of	Material of	Loss of Tenacity,
Plates.	Plates.	per cent.
1/4	Steel	8
3/8		18
1/2	44	26
3/4	"	33
3/4	Iron	18 to 23

The effect of increasing the size of the hole in the die-block is shown in the following table:

Total Taper of Hole in Plate, inches.	Material of Plates.	Loss of Tenacity due to Punching, per cent.
1-16	Steel	17.8
1/8	**	12.3
17	66 (	Hole regreed) 94 5

The plates were from 0.675 to 0.712 inch thick. When 7% in punched holes were reamed out to 1½ in diameter, the loss of tenacity disappeared, and the plates carried as high a stress as drilled plates. Annealing also restores to punched plates their original tenacity.

## Strength of Perforated Plates.

(P. D. Bennett, Eng'g, Feb. 12, 1886, p. 155.)

Tests were made to determine the relative effect produced upon tensile strength of a flat bar of iron or steel: 1. By a 34-inch hole drilled to the required size; 2, by a hole punched 1/2 inch smaller and then drilled to the size of the first hole; and, 3, by a hole punched in the bar to the size of the drilled bar. The relative results in strength per square inch of original area were as follows:

	1.	2.	3.	4.
	Iron.	Iron.	Steel.	Steel.
Unperforated bar		1.000	1.000	1.000
Perforated by drilling	1.029	1.012	1.068	1.103
" punching and drilling,	1.030	1.008	1.059	1.110
" nunching only	0.795	0.894	0.935	0.997

In tests 2 and 4 the holes were filled with rivets driven by hydraulic pressure. The increase of strength per square inch caused by drilling is a phenomenon of similar nature to that of the increased strength of a grooved bar over that of a straight bar of sectional area equal to the smallest section of the grooved bar, Mr. Bennett's tests on an iron bar 0.84 in, diameter, 10 in.

long, and a similar bar turned to 0.84 in, diameter at one point only, showed that the relative strength of the latter to the former was 1.323 to 1.000.

## Riveted Joints.—Drilling versus Punching of Holes.

The Report of the Research Committee of the Institution of Mechanical Engineers, on Riveted Joints (1881), and records of investigations by Prof. A. B. W. Kennedy (1881, 1882, and 1885), summarize the existing information regarding the comparative effects of punching and drilling upon iron and steel plates. From an examination of the voluminous tables given in Professor Unwin's Report, the results of the greatest number of the experiments made on iron and steel plates lead to the general conclusion that, while thin plates, even of steel, do not suffer very much from punching, yet in those of ½-inch thickness and upwards the loss of tenacity due to punching ranges from 10% to 23% in iron plates, and from 11% to 38% in the case of ing ranges from 10% to 23% in fron plates, and from 11% to 33% in the case of mild steel. In drilled plates there is no appreciable loss of strength. It is possible to remove the bad effects of punching by subsequent reaming or annealing; but the speed at which work is turned out in these days is not favorable to multiplied operations, and such additional treatment is seldom practised. The introduction of a practicable method of drilling the plating of ships and other structures, after it has been bent and shaped, is a matter of great importance. If even a portion of the deterioration of tenacity can be prevented, a much stronger structure results from the same material and the same scantling. This has been fully recognized in the modern English practice (1887) of the construction of steam-boilers with steel plates; punching in such cases being almost entirely abolished, and all rivet-holes being drilled after the plates have been bent to the desired form.

## Comparative Efficiency of Riveting done by Different Methods.

The Reports of Professors Unwin and Kennedy to the Institution of Mechanical Engineers (Proc. 1881, 1882, and 1885) tend to establish the four following points:

1. That the shearing resistance of rivets is not highest in joints riveted by means of the greatest pressure;

2. That the ultimate strength of joints is not affected to an appreciable

2. That the ultimate strength of joints is not acceed to an appreciation extent by the mode of riveting; and, therefore,
3. That very great pressure upon the rivets in riveting is not the indispensable requirement that it has been sometimes v-posed to be;
4. That the most serious defect of hand-riveted as compared with machine-riveted work consists in the fact that in hand-riveted joints visible slip commences at a comparatively small load, thus giving such joints a low value as regards tightness, and possibly also rendering them liable to failure under sudden strains after slip has once commenced.

The following figures of mean results, taken from Prof. Kennedy's tables (Proceedings 1885, pp. 218-225), give a comparative view of hand and hydraulic riveting, as regards their ultimate strengths in joints, and the periods

at which in both cases visible slip commenced.

Total Brea	king Load.	Load at which Visible Slip began.						
Hand-riveting.	Hydraulic Rivet- ing.	Hand-riveting.	Hydraulic Rivet- ing.					
Tons. 86.01	Tons. 85.75	Tons. 21.7	Tons. 47.5					
82.16	77.00 82.70 78.58	25.0	35.0 53.7 54.0					
149.2	145.5 140.2	31.7	49.7					
193.6	183.1 183.7	25.0	46.7 56.0					

In these figures hand-riveting appears to be rather better than hydraulic riveting, as far as regards ultimate strength of joint; but is very much in-ferior to hydraulic work, in view of the small proportion of load borne by it before visible slip commenced.

#### Some of the Conclusions of the Committee of Research on Riveted Joints.

(Proc. Inst. M. E., Apl. 1885.)
The conclusions all refer to joints made in soft steel plate with steel rivets, the holes all drilled, and the plates in their natural state (unannealed). In every case the rivet or shearing area has been assumed to be that of the holes, not the nominal (or real) area of the rivets themselves. Also, the strength of the metal in the joint has been compared with that of stript cut from the same plates, and not merely with nominally similar material. The metal between the rivet-holes has a considerably greater tensile resistance per square inch than the unperforated metal. This excess tenacity

amounted to more than 20%, both in %-inch and %-inch plates, when the pitch of the rivet was about 1.9 diameters. In other cases %-inch plate gave an excess of 15% at fracture with a pitch of 2 diameters, of 10% with a pitch of 3.6 diameters, and of 6.6%, with a pitch of 3.9 diameters; and 34-inch plate gave 7.8% excess with a pitch of 2.8 diameters.

In single-riveted joints it may be taken that about 22 tons per square inch is the shearing resistance of rivet steel, when the pressure on the rivets does not exceed about 40 tons per square inch. In double-riveted joints, with rivets of about 34 inch diameter, most of the experiments gave about 24 tons per square inch as the shearing resistance, but the joints in one series went

at 22 tons.

The ratio of shearing resistance to tenacity is not constant, but diminishes

very markedly and not very irregularly as the tenacity increases.

The size of the rivet heads and ends plays a most important part in the strength of the joints—at any rate in the case of single-riveted joints. An increase of about one third in the weight of the rivets (all this increase, of course, going to the heads and ends) was found to add about 816% to the resistance of the joint, the plates remaining unbroken at the full shearing resistance of 22 tons per square inch, instead of tearing at a shearing stress of only a little over 20 tons. The additional strength is probably due to the prevention of the distortion of the plates by the great tensile stress in the rivets.

The intensity of bearing pressure on the rivet exercises, with joints proportioned in the ordinary way, a very important influence on their strength. So long as it does not exceed 40 tons per square inch (measured on the projected area of the rivets), it does not seem to affect their strength; but pressures of 50 to 55 tons per square inch seem to cause the rivets to shear in most cases at stresses varying from 16 to 18 tons per square inch. For ordinary joints, which are to be made equally strong in plate and in rivets, the bearing pressure should therefore probably not exceed 42 or 43 tons per square inch. For double-riveted butt-joints perhaps, as will be noted later, a higher pressure may be allowed, as the shearing stress may probably not be more than 16 or 18 tons per square inch when the plate tears.

A margin (or net distance from outside of holes to edge of plate) equal to the diameter of the drilled hole has been found sufficient in all cases hitherto tried.

To attain the maximum strength of a joint, the breadth of lap must be such as to prevent it from breaking zigzag. It has been found that the net metal measured zigzag should be from 30% to 35% in excess of that measured straight across, in order to insure a straight fracture. This corresponds to a diagonal pitch of 2/3 p + d/3, if p be the straight pitch and d the diameter of the rivet-hole.

Visible slip or "give" occurs always in a riveted joint at a point very much below its breaking load, and by no means proportional to that load. A collation of the results obtained in measuring the slip indicates that it depends upon the number and size of the rivets in the joint, rather than upon anything else; and that it is tolerably constant for a given size of rivet in a given type of joint. The loads per rivet at which a joint will commence to slip visibly are approximately as follows:

Diameter of Rivet.	Type of Joint.	Riveting,	Slipping Load per Rivet.
34 inch	Single-riveted	Hand	2.5 tons
34 "	Double-riveted	Hand	3.0 to 3.5 tons
34 "	Double-riveted	Machine	7 tons
1 inch	Single-riveted	Hand	3.2 tons
1 "	Double-riveted	Hand	4.3 tons
1 "	Double-riveted	Machine	8 to 10 tons

To find the probable load at which a joint of any breadth will commence to slip, multiply the number of rivets in the given breadth by the proper figure taken from the last column of the table above. It will be understood that the above figures are not given as exact; but they represent very well

the results of the experiments.

The experiments point to simple rules for the proportioning of joints of maximum strength. Assuming that a bearing pressure of 43 tons per square inch may be allowed on the rivet, and that the excess tenacity of the plate is 10% of its original strength, the following table gives the values of the ratios of diameter d of hole to thickness t of plate (d + h), and of pitch p to diameter. eter of hole  $(p \div d)$  in joints of maximum strength in \%-inch plate.

## For Single-riveted Plates.

Original Tenacity of Plate.		Shearing Resistance of Rivets.		Ratio.	Ratio.	Ratio.
Tons per sq. in.	Lbs. per sq. in.	Tons per sq. in.	Lbs. per sq. in.	$d \div t$	$p \div a$	Rivet Area
30 28	67,200 62,720	22 22	49,200 49,200	2.48	2.30 2.40	0.667 0.785
30 28	67,200 62,720	24 24	53,760 53,760	2.28	2.27	0.713 0.690

This table shows that the diameter of the hole (not the diameter of the rivet) should be 21/4 times the thickness of the plate, and the pitch of the rivets 23/4 times the diameter of the hole. Also, it makes the mean plate area 71% of the rivet area.

If a smaller rivet be used than that here specified, the joint will not be of uniform, and therefore not of maximum, strength; but with any other size of rivet the best result will be got by use of the pitch obtained from the

simple formula

$$p=a\,\frac{d^2}{t}+d,$$

where, as before, d is the diameter of the hole.

The value of the constant a in this equation is as follows:

For 30-ton plate and 22-ton rivets, 
$$a=0.524$$
 ... 0.558 ... 0.558 ... 0.558 ... 0.570 ... 24 ... 0.570 ... 0.570 ... 28 ... 24 ... 0.606

Or, in the mean, the pitch  $p=0.56 \frac{d^2}{t}+d$ .

It should be noticed that with too small rivets this gives pitches often con-

is siderably smaller in proportion than 2% times the diameter.

For double-riveted lap-joints a similar calculation to that given above, but with a somewhat smaller allowance for excess tenacity, on account of the large distance between the rivet-holes, shows that for joints of maximum strength the ratio of diameter to thickness should remain precisely as in single-riveted joints; while the ratio of pitch to diameter of both should be 3.6 for 30-ton plates and 22 or 24 ton rivets, and 3.8¢ for 28-ton plates with the same (ivets.

Here, still more than in the former case, it is likely that the prescribed

size of rivet may often be inconveniently large. In this case the diameter of rivet should be taken as large as possible; and the strongest joint for a given thickness of plate and diameter of hole can then be obtained by using the pitch given by the equation

 $p = a \frac{d^2}{t} + d,$ 

where the values of the constant  $\alpha$  for different strengths of plates and rivets may be taken as follows:

## Table of Proportions of Double-riveted Lap-joints.

in which 
$$p = a \frac{d^2}{t} + d$$
.

Thickness of Plate.	Original tenacity of Plate, Tons per sq. in.	Shearing Resist- ance of Rivets. Tons per sq. in.	Value of Constant.
	* 30	24	1.15
3% inch	28	24	1.22
3% "	30	22	1.05
3% "	28	22	1.12
34 "	30	24	1.17
34 "	28	24	1.25
34 "	30	22	1.07
3/4 "	28	22	1.14

Practically, having assumed the rivet diameter as large as possible, we can fix the pitch as follows, for any thickness of plate from \( \frac{1}{2} \) to \( \frac{1}{2} \) inch:

For 30-ton plate and 24-ton rivets 
$$\left. \right\} \; p = 1.16 \; \frac{d^2}{t} + d;$$
" 30 " " 22 " "  $p = 1.06 \; \frac{d^2}{t} + d;$ 
" 28 " " 24 " "  $p = 1.24 \; \frac{d^2}{t} + d;$ 

In double-riveted butt-joints it is impossible to develop the full shearing resistance of the joint without getting excessive bearing pressure, because the shearing area is doubled without increasing the area on which the pressure acts. Considering only the plate resistance and the bearing pressure, and taking this latter as 45 tons per square inch, the best pitch would be about 4 times the diameter of the hole. We may probably say with some certainty that a pressure of from 45 to 50 tons per square inch on the rivets will cause shearing to take place at from 16 to 18 tons per square inch. Working out the equations as before, but allowing excess strength of only 5% on account of the large pitch, we find that the proportions of doubleriveted butt-joints of maximum strength, under given conditions, are those of the following table:

#### Double-riveted Butt-joints.

Original Ten- acity of Plate, Tons per sq. in.	Shearing Resistance of Rivets, Tons per sq. in.	Bearing Pressure, Tons per sq. in.	Ratio $\frac{d}{t}$	$\begin{array}{c} \text{Ratio} \\ \frac{p}{d} \end{array}$
30	16	45	1.80	3.85
28	16	45	1.80	4.06
30	18	48	1.70	4.03
28	18	48	1.70	4.27
30	16	50	2.00	4.20
28	16	50	2.00	4.42

Practically, therefore, it may be said that we get a double-riveted butt-joint of maximum strength by making the diameter of hole about 1.8 times the thickness of the plate, and making the pitch 4.1 times the diameter of the hole.

The proportions just given belong to joints of maximum strength. But in a boiler the one part of the joint, the plate, is much more affected by time than the other part, the rivets. It is therefore not unreasonable to estimate the percentage by which the plates might be weakened by corrosion, etc., before the boiler would be umit for use at its proper steam-pressure, and to add correspondingly to the plate area. Probably the best thing to do in this case is to proportion the joint, not for the actual thickness of plate, but for a nominal thickness less than the actual by the assumed p-rcentage. In this case the joint will be approximately one of uniform strength by the time it has reached its final workable condition; up to which time the joint as a whole will not really have been weakened, the corrosion only gradually bringing the strength of the plates down to that of rivets.

#### Efficiencies of Joints.

The average results of experiments by the committee gave: For doubleriveted lap-joints in %-inch plates, efficiencies ranging from 67.1% to 81.2%. For double-riveted butt-joints (in double shear) 61.4% to 71.3%. These low results were probably due to the use of very soft steel in the rivets. For singleriveted lap-joints of various dimensions the efficiencies varied from 54,8% to 60.8%.

The experiments showed that the shearing resistance of steel did not in-The experiments showed that the shearing resistance of steel fit into in-crease nearly so fast as its tensile resistance. With very soft steel, for instance, of only 26 tons tenacity, the shearing resistance was about 30% of the tensile resistance, whereas with very hard steel of 52 tons tenacity the shearing resistance was only somewhere about 65% of the tensile resistance.

### Proportions of Pitch and Overlap of Plates to Diameter of Rivet-Hole and Thickness of Plate.

(Prof. A. B. W. Kennedy, Proc. Inst. M. E., April, 1885.)

t =thickness of plate; d =diameter of rivet (actual) in parallel hole;

p = pitch of rivets, centre to centre;
s = space between lines of rivets;

l = overlap of plate.

The pitch is as wide as is allowable without imparing the tightness of the joint under steam.

For single-riveted lap-joints in the circular seams of boilers which have double-riveted longitudinal lap-joints.

$$\begin{array}{l} d=t\times 2.25; \\ p=d\times 2.25=t\times 5 \ (\mathrm{nearly}); \\ l=t\times 6. \end{array}$$

For double-riveted lap-joints:

d = 2.25t; p = 8t; s = 4.5t: I = 10.5t

Sin	Single-riveted Joints.				Double-riveted Joints.					
t	d	p	ı	t	d	. p	s	ı		
3-16 14 5-16 3/8 7-16 1/2 9-16	7-16 9-16 11-16 13-16 1 11/6 11/4	15-16 11/4 1 9-16 17/8 2 3-16 21/2 2 13-16	11/6 11/2 17/8 21/4 25/8 3 33/8	3-16 14 5-16 36 7-16 12 9-16	7-16 9-16 11-16 13-16 1 11/8 11/4	1½ 2 2½ 3 3½ 4 4½	7/8 1 3–16 11/4 13/4 2 21/4 21/2	2 23/4 33/8 4 45/8 51/4 57/8		

With these proportions and good workmanship there need be no fear of

leakage of steam through the fiveted joint.

The net diagonal area, or area of plate, along a zigzag line of fracture should not be less than 30% in excess of the net area straight across the joint, and 35% is better.
Mr. Theodore Cooper (R. R. Gazette, Aug. 22, 1890) referring to Prof. Ken-

nedy's statement quoted above, gives as a sufficiently approximate rule for the proper pictor between the rows in staggered riveting, one half of the pitch of the rivets in a row plus one quarter the diameter of a rivet-hole.

# Apparent Excess in Strength of Perforated over Unperforated Plates. (Proc. Inst. M. E., October, 1888.)

The metal between the rivet-holes has a considerably greater tensile resistance per square inch than the unperforated metal. This excess tenacity amounted to more than 20%, both in %-inch and 34-inch plates, when the pitch of the rivets was about 1.9 diameters. In other cases % inch plate gave an excess of 15% at fracture with a pitch of 2 diameters, of 10% with a pitch of 3.6 diameters, and of 6.6% with a pitch of 3.9 diameters; and ¾ inch plate gave 7.8% excess with a pitch of 2.8 diameters. (1) The "excess strength due to perforation" is increased by anything which tends to make the stress in the plate uniform, and to diminish the

which tends to make the stress in the plate uniform, and to diminish the effect of the narrow strip of metal at the edge of the specimen. (2) It is diminished by increase in the ratio of p/d, of pitch to diameter of hole, so that in this respect it becomes less as the efficiency of the joint

increases

Kind of Joint. Thickness of

Plate.

(3) It is diminished by any increase in hardness of the plate.

(4) For a given ratio p/d, of pitch to diameter of hole, it is also apparently diminished as the thickness of the plate is increased. The ratio of pitch to thickness of plate does not seem to affect this matter directly, at least within the limits of the experiments.

# Test of Double-riveted Lap and Butt Joints.

(Proc. Inst. M. E., October, 1888.)

Steel plates of 25 to 26 tons per square inch T. S., steel rivets of 24.6 tons shearing-strength per square inch.

Diameter of Ratio of Pitch

Rivet-holes, to Diameter.

Comparative

Efficiency of

Joint.

Lap	9/8"	0.87	5.62	75.2
Butt	3/6	0.7	3,93	76.5
Lap	34	1.1	2.82	68.0
"	$\frac{3}{4}$	1.6	3.41	73.6
Butt	37	1.1	4.00	72.4
44	$\frac{37}{4}$	1.6	3.94	76.1
Lap	1 *	1.3	2.42	63.0
	1	1.75	3.00	70.2
Butt	1	1.3	3.92	76.1
Some Rules wl	hich have	been Pro	posed for th	e Diameter
of the Ri	vet in Sin:	gle Shear	. (Iron, June 1	8, 1880.)
Browne	d = 2	t (with doub	ble covers 11/4t)	(1)
Fairbairn	$d = 3$	2t for plates	less than % in.	(2)
44	$d = 1$	16t for plate	es greater than 3/	ś in. (3)
Lemaitre	$d = 1$	1.5t + 0.16	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	ś in. (3) (4)

Antoine.  $d = 1.1 \sqrt{t}$ Pohlig. d = 2t for boiler riveting d = 3t for extra strong riveting Redtenbacher d = 1.5t to 2t(7) (8)

Unwin......  $d = \frac{34}{4}t + \frac{5}{16}$  to  $\frac{7}{8}t + \frac{3}{8}$ " .....  $d = 1.2 \sqrt{t}$ (10)The following table contains some data of the sizes of rivets used in practice, and the corresponding sizes given by some of these rules.

Diameter of Rivets for Different Thicknesses of Plates.

APACCIAL V	Jeek	OK A		00 IU.		THU CA		1110000	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,	100003
				Dia	met	er of Ri	vets, in i	nches.		
Thick- ness of plate. Inches.	Lloyd's Rules.	Liverpool Rules.	English Dock-yards.	French Veritas.	Browne Eq. (1).	Fairbairn (2) and (3).	Lemaitre (4).	Antoine (5).	Unwin (10).	Wilson,
5/16 5/8 7/16 1/2	5/8 5/8 5/8 3/4	5/8 5/8 3/4 13/16	1/2 5/8 3/4 3/4	5/8 5/8	5/8 3/4 7/8 1	5/8 3/4 21/32 3/4	5/8 23/32 13/16 15/16	5/8 11/16 3/4 3/4	11/16 3/4 13/16 7/8	5/8 11/16 3/4 3/4
9/16 5/8 11/16 3/4	3/4 3/4 7/8 7/8	13/16 7/8 7/8 15/16	7/8 7/8 7/8 1	3/4 13/16 7/8	11/3 11/4	27/32 15/16 1 1/32 1½	1 1½ 1 3/16 1¼	13/16 7/8 15/16 15/16	7/8 15/16 1 1 1/16	7/8 7/8 7/8 1
13/16 7/8 15/16 1	7/8 1 1 1	1 11/6 1 3/16 11/4	1 1½ 1½ 1½ 1½	1 1 1/16		1 7/32	13/8	1 1 1 1/16 11/8	1 3/32 11/8 1 3/16 11/4	1 1 1½ 1½ 1½

Strength of Double-riveted Seams, Calculated.—W. B. Ruggles, Jr., in Poner for June, 1890, gives tables of relative strength of rivets and parts of sheet between rivets in double-riveted seams, compared with strength of shell, based on the assumption that the shearing strength of rivets and the tensile strength of steel are equal. The following figures show the sizes in his tables which show the nearest approximation to equality of strength of rivets and parts of plates between the rivets, together with the percentage of each relative to the strength of the solid plate.

rickness of Pitch of Rivet inche	of Rivet- Plate.		Thickness of Plate, inches.	Pitch of Rivets, inches.		Percentage of Strength of Plate.		
Thicks plate, and the street	s. inches.	Rivets.	Plate.	Thic Plat	inches.	inches.	Rivets.	Plate.
14 21/4 21/4 11/4 21/4 31/4 31/4 31/4 31/4 31/4 31/4 31/4 3	9/16 5/8 11/16 9/16 5/6 11/16 34 5/8 11/16 34 13/16 78 11/16	.739 .795 .785 .819 .748 .761 .780 .727 .755 .754 .762 .777 .714	.765 .775 .800 .810 .735 .762 .780 .793 .722 .738 .760 .776 .788 .711	7/16 7/16 7/16 7/16 7/16 7/16 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2 1/2	234 314 3158 416 2142 278 3144 416 258 3144 4178 3344 4174	34 13/16 76 15/16 34 13/16 78 15/16 1 13/16 78 15/16 1 1 1/16	.734 .758 .758 .765 .707 .721 .740 .736 .761 .701 .714 .727 .745 .742	.728 .740 .759 .773 .700 .718 .731 .750 .758 .690 .708 .722 .733 .750

H. De B. Parsons  $(R.\ R.\ \&\ Eng,\ Journal,\ 1890)$  holds that it is an error to assume that the shearing strength of the rivet is equal to the tensile strength. Also, referring to the apparent excess in strength of perforated over unperforated plates, he claims that on account of the difficulty in properly matching the holes, and of the stress caused by forcing, as is too often the case in practice, this additional strength cannot be trusted much more than

that of friction.

Adopting the sizes of iron rivets as generally used in American practice for steel plates from  $\frac{1}{4}$  to 1 inch thick: the tensile strength of the plates as 60,000 lbs.; the shearing strength of the rivets as 40,000 for single-shear and 35,500 for double-shear, Mr. Parsons calculates the following table of pitches, so that the strength of the rivets against shearing will be approximately equal to that of the plate to tear between rivet-holes. The diameter of the rivets has in all cases been taken at 1/16 in, larger than the nominal size, as the rivet is assumed to fill the hole under the power riveter.

#### Riveted Joints.

LAP OR BUTT WITH SINGLE WELT-STEEL PLATES AND IRON RIVETS.

Thickness	Diameter	Pi	tch.	Efficiency.		
of Plates.	of Rivets.	Single.	Double.	Single.	Double.	
in.	in. 1/2 3/4 7/8 1 1 1 1/8	in. 1 3/16 1 11/16 17/6 1 11/16 17/6 1 13/4 2 3/16	in. 176 2 11/16 234 2 7/16 25/8 2 7/16 25/8	55.7% 52.7 49.0 43.6 42.0 38.6 38.1	70.0% 68.6 65.9 60.4 59.5 55.4 54.9	

Calculated Efficiencies – Steel Plates and Steel Rivets,— The differences between the calculated efficiencies given in the two tables above are notable. Those given by Mr. Ruggles are probably too high, since he assumes the shearing strength of the rivets equal to the tensile strength of the plates. Those given by Mr. Parsons are probably lower than will be obtained in practice, since the figure he adopts for shearing strength is rather low, and he makes no allowance for excess of strength of the perforated over the unperforated plate. The following table has been calculated by the author on the assumptions that the excess strength of the perforated plate is 10%, and that the shearing strength of the rivets per square inch is four fifths of the tensile strength of the plate. If t = thickness of plate, d = diameter of rivet-hole, p = pitch, and T = tensile strength per square inch, then for single-riveted plates

$$(p-d)t \times 1.10T = \frac{\pi}{4}d^2 \times \frac{4}{5}T$$
, whence  $p=.571\frac{d^2}{t}+d$ . For double-riveted plates,  $p=1.142\frac{d^2}{t}+d$ .

The coefficients 571 and 1.142 agree closely with the averages of those given in the report of the committee of the Institution of Mechanical Engineers, quoted on pages 357 and 358, ante.

	T.I	Pit	ch.	Effici	ency.		Ø Diam		ch.	Efficiency.	
Thickness.	Diam, of Rivet- hole.	Single Riveting.	Double Riveting.	Single Riveting.	Double Riveting.	Thickness.	Diam. of Rivet- hole.	Single Riveting.	Double Riveting.	Single Riveting.	Double Riveting.
in.	in.	in.	in.	%	×	in.	in,	in.	in.	%	%
3/16	7/16	1.020	1.603	57.1	72.7	1/2	3/4 7/8	1.392	2.035	46.1	63.1
1/4	1/2 1/2 9/16	1.261	2.023 1.642	$60.5 \\ 53.3$	75.3 69.6		1 1	$\frac{1.749}{2.142}$	2.624 $3.284$	50.0 53.3	66.6
	9/16	1.285	2.008	56.2	72.0	64	11/8 3/4 7/8	2.570	4.016	56.2	72.0 60.3
5/16	9/16 5/8	1.137	1.712 2.053	50.5 53.3	67.1 69.5	9/16	24	1 321 1.652	1.892 2.429	43.2 47.0	64.0
	11/16	1.551	2.415	55.7	71.5	66	1 1	2.015	3.030	50.4	67.0
3/8	5/8	1.218	1.810	48.7	65.5	66	11/6 11/4 3/4 5/8	2.410	3.694	53.3	69.5
6.6	94 7/2	1.607 2.041	2.463 3.206	53.3 57.1	69.5 72.7		11/4	2.836 1.264	4.422 1.778	55.9 40.7	57.8
7/16	5%	1.136	1.647	45.0	62.0	<u>%</u>	72	1.575	2.274	44.4	61.5
66	5/8/4/8/5/8/4/8	1.484	2.218	49.5	66.2	"	1	1.914	2.827	47.7	64.6
**	1 1/8	1.869 2.305	$2.864 \\ 3.610$	53.2 56.6	69.4 72.3	16	1½ 1¼	2.281 2.678	$\frac{3.438}{4.105}$	50.7 53.3	$67.3 \\ 69.5$
	1	~.505	0.010	50.0	12.5		174	2.010	4.100	00.0	

#### Riveting Pressure Required for Bridge and Boiler Work.

(Wilfred Lewis, Engineers' Club of Philadelphia, Nov., 1893.)

A number of \$6,4 inch rivets were subjected to pressures between 10,000 and 60,000 lbs. At 10,000 lbs, the rivet swelled and filled the hole without forming a head. At 20,000 lbs, the head was formed and the plates were slightly pinched. At 30,000 lbs, the rivet was well set, At 40,000 lbs, the metal in the plate surrounding the rivet began to stretch, and the stretching became the plate surrounding the rivet began to stretch, and the stretching became set. From these experiments the conclusion might be drawn than 60,000 lbs. From these experiments the conclusion might be drawn than 60,000 lbs. From the section. Inout riveting was about 300,000 bs. see agong 10 for a pressure exceeding 60,000 lbs., but now pressures as high as 150,000 lbs, are not uncommon, and even 300,000 lbs. have been contemplated as desirable.

# Apparent Shearing Resistance of Rivet Iron and Steel.

(Proc. Inst. M. E., 1879, Engineering, Feb. 20, 1880.)

The true shearing resistance of the rivets cannot be ascertained from experiments on riveted joints (1), because the uniform distribution of the load to all the rivets cannot be insured; (2) because of the friction of the plates, which has the effect of increasing the apparent resistance to shearing in an element uncertain in amount. Probably in the case of single-riveted joints the shearing resistance is not much affected by the friction;

Ultimate Shearing Stress
Tons per so in Lbs per so in

Iron,	single shea	r (12 bars)	24.15	54.096	Clarke.
	double she	ar (8 bars)	22.10	49.504	Clarke.
"	64	**	22,62	50.669	Barnaby.
44	44	**	22,30	49.952	Rankine.
66	3/4-in, rivet	s	23.05 to 25.57	51.632 to 57.277 ]	
6.6	%-in, rivet	S	24.32 to 27.94	54.477 to 62.362	- Rilev.
44		e		56.000	
44			19.01	42.582	Greig and Evth.
Steel			17 to 26	38,080 to 58,240	Parker.
Land	ore steel. 3	i-in, rivets	31.67 to 33.69	70.941 to 75.466	
66	· · · · · · · · · · · · · · · · · · ·	6-in. rivets	30.45 to 35.73	68.208 to 80.035	Riley.
6.6		nean value			
Brow					Greig and Eyth

Fairbairn's experiments show that a rivet is 6½% weaker in a drilled than in a punched hole. By rounding the edge of the rivet-hole the apparent shearing resistance is increased 1½%. Mr. Maynard found the rivets 4½ weaker in drilled holes than in punched holes. But these results were obtained with riveted joints, and not by direct experiments on shearing. There is a good deal of difficulty in determining the true diameter of a punched hole, and it is doubtful whether in these experiments the diameter was very accurately ascertained. Messrs. Greig and Eyth's experiments also indicate a greater resistance of the rivets in punched holes than in drilled holes.

If, as appears above, the apparent shearing resistance is less for double than for single shear, it is probably due to unequal distribution of the stress on the two rivet sections.

The shearing resistance of a bar, when sheared in circumstances which prevent friction, is usually less than the tenacity of the bar. The following results show the decrease:

	Tenacity of Bar.	Shearing Resistance.	Ratio.
Harkort, iron	26.4	16.5	0.62
Lavalley, iron	25.4	20.2	0.79
Greig and Eyth, iron	22.2	19.0	0.85
steel	28.8	22.1	0.77

In Wöhler's researches (in 1870) the shearing strength of iron was found to be four-fifths of the tenacity. Later researches of Bauschinger confirm this result generally, but they show that for iron the ratio of the shearing resistance and tenacity depends on the direction of the stress relatively to the direction of rolling. The above ratio is valid only if the shear is in a plane perpendicular to the direction of rolling, and if the tension is applied parallel to the direction of rolling. The shearing resistance in a plane parallel to the direction, and again differs according as the plane of shear is perpendicular or parallel to the breadth of the bar. In the former case the resistance is 18 to 20% greater than in a plane perpendicular to the fibres, or is equal to the tenacity. In the latter case it is only half as great as in a plane perpendicular to the fibres.

#### TRON AND STEEL.

CLASSIFICATION OF IRON AND STEEL. (W. Kent, Railroad & Engineering Journal, April, 1887.)

-					
Generic Term.			IRON.		
How Obtained.	Or ob	CAST, Or obtained from a fluid mass.	d mass.	WROUGHT, Or welded from a pasty mass.	a pasty mass.
ag <sub>0</sub>	Distinguishing Non-malleable.	Mall	Malleable,	Will Not Harden.	Will Harden.
	CAST IRON.	IRON.	CAST STEEL.	(7) Wrought Iron.	(84) WROUGHT STEEL.
	(1) Ordinary castings.	(2) Maleable (3) Crucible, cast iron, obtained from No. 1 by annealing in oxides. (6) Mittis.*	(3) Crucible, (4) Bessemer, and (5) Open-hearth steels. (6) Mitis.*	a. Obtained by direct Obtained by direct Catalan, Chenot, and German, Shear, bils other process from the control of the contro	a. Obtained by direct obtained by direct voess from ores, as or indirect process as atalan. Ofteno, and ferman, shear, bils. Obtained by indirect process from each or as a finery-learth on, as finery-learth in individual priors.

CLASSIFICATION OF IRON AND \* No. 6. Mitis is the name given to a new product (having the same general properties and produced by the same processes as soft cast steels) made by adding an alloy of aluminum to melted wrought iron or soft steel before pouring.

+ No. 8. Wrought steel is almost an obsolete product, having been replaced in commerce by cast steel.

Sub-varieties of Nos. 3, 4, and 5, soft, mild, medium, and hard steels, according to percentage of carbon, the divisions between them not being well defined. Cast iron usually contains over 3% of carbon; cast steel anywhere from 0.06% to 1.50%, according to the purpose for which it is used; wrought iron from 0.0% to 0.10%. The quality of hardening and tempering which formerly distinguished steel from wrought iron is now no longer the dividing line between them, since soft steels are now produced which, by the ordinary blacksmith's tests, will not harden. All products of the crucible, Bessemer, and open-hearth processes are now commercially known as steel.

#### CAST IRON.

Grading of Pig Iron.—Pig iron is commonly graded according to its fracture, the number of grades varying in different districts. In Eastern Pennsylvania the principal grades recognized are known as No. 1 and 2 foundry, gray forge or No. 3, mottled or No. 4, and white or No. 5. Intermediate grades are sometimes made, as No. 2 X between No. 1 and No. 2, and special names are given to irons more highly silicized than No. 1, as No. 1 X silver, gray and soft. Charcoal foundry nig iron is graded by successions. and special mannes are given to from more linging sincized than No. 1, as, silver-gray, and soft. Charocal foundry pig from is graded by numbers I to 5, but the quality is very different from the corresponding numbers in anthracite and coke pig. Southern coke pig iron is graded into ten bers in antifractic and coke pig. Southern coke pig iron is graded into ten or more grades. Grading by fracture is a fairly satisfactory method of grading irons made from uniform ore mixtures and fuel, but is unreliable as a means of determining quality of irons produced in different sections or from different ores. Grading by chemical analysis, in the latter case, is the only satisfactory method. The following analyses of the five standard grades of northern foundry and mill pig irons are given by J. M. Hartman (2011). The following analyses of the five standard grades of northern foundry and mill pig irons are given by J. M. Hartman (2011). (Bull. I. & S. A., Feb., 1892):

	No. 1.	No. 2.	No. 3.	No. 4.	No. 4 B.	No. 5.
Iron	92.37	92.31	94,66	94.48	94.08	94.68
Graphitic carbon	3.52	2.99	2.50	2.02	2.02	
Combined carbon	.13	.37	1.52	1.98	1.43	3.83
Silicon	2.44	2.52	.72	.56	.92	.41
Phosphorus	1.25	1.08	.26	.19	.04	.04
Sulphur	.02	.02	trace	.08	.04	.02
Manganese	.28	.72	.34	.67	2.02	.98

#### CHARACTERISTICS OF THESE IRONS.

No. 1. Gray.—A large, dark, open-grain iron, softest of all the numbers and used exclusively in the foundry. Tensile strength low. Elastic limit low. Fracture rough. Turns soft and tough.

No. 2. Gray.—A mixed large and small dark grain, harder than No. 1 iron, and used exclusively in the foundry. Tensile strength and elastic limit higher than No. 1. Fracture less rough than No. 1. Turns harder, less tough, and more brittle than No. 1.

tough, and more brittle than No. 1.

No. 3. Gray.—Small, gray, close grain, harder than No. 2 iron, used either in the rolling-mill or foundry. Tensile strength and elastic limit higher than No. 2. Turns hard, less tough, and more brittle than No. 2.

No. 4. Mottled.—White background, dotted closely with small black spots of graphitic earbon; little or no grain. Used exclusively in the rolling-mill. Tensile strength and elastic limit lower than No. 3. Turns with difficulty; less tough and more brittle than No. 3. The manganese in the B pig iron replaces part of the combined carbon, making the iron harder and closing the grain, notwithstanding the lower combined carbon.

No. 5. White.—Smooth, white fracture, no grain, used exclusively in the rolling mill. Tensile strength and elastic limit much lower than No. 4. Too

hard to turn and more brittle than No. 4.

hard to turn and more brittle than No. 4.

Southern pig irons are graded as follows, beginning with the highest in silicon: Nos. 1 and 2 silvery, Nos. 1 and 2 soft, all containing over 3% of silicon; Nos. 1, 2, and 3 foundry, respectively about 2 75%, 25% and 2% silicon; No. 1 mill, or "foundry forge;" No. 2 mill, or gray forge; mottled; white-Good charcoal chilling iron for car wheels contains, as a rule, 0.56 to 0.55 silicon; 0.08 to 0.90 manganese, 0.05 to 0.75 phosphorus. The following is an analysis of a remarkably strong car wheel: Si, 0.734; Mn, 0.438; P. 0.428, S. 0.085 graphitic C, 1.247; Copper, 0.029. The chill was very hard—14 in. deep at root of flange, ½ in. deep on tread. A good ordnance iron analyzed: Si, 0.30; Graphitic C, 2.20; Combined C, 1.76; P, 0.44; Mn, 3 55 (?). Its specific gravity was 7.22 and tenacity 31,734 lbs. per so, in per sq. in

Influence of Silicon, Phosphorus, Sulphur, and Man-ganese upon Cast Iron.—W. J. Keep, of Detroit, in several papers (Trans. A. I. M. E., 1889 to 1893), discusses the influence of various chemical elements on the quality of cast iron. From these the following notes have

been condensed:

SILICON.—Pig iron contains all the carbon that it could absorb during its reduction in the blast-furnace. Carbon exists in cast iron in two distinct forms. In chemical union, as "combined" carbon, it cannot be discerned. except as it may increase the whiteness of the fracture, in so-called white iron. Carbon mechanically mixed with the iron as graphite is visible, varying in color from gray to black, while the fracture of the iron ranges from a light to a very dark gray.

Silicon will expel carbon, if the iron, when melted, contains all the car-

bon that it can hold and a portion of silicon be added.

Prof. Turner concludes from his tests that the amount of silicon producing the maximum strength is about 1.80%. But this is only true when a white base is used. If an iron is used as a base which will produce a sound casting to begin with, each addition of silicon will decrease strength. Silicon itself is a weakening agent. Variations in the percentage of silicon added to a pig iron will not insure a given strength or physical structure, but these results will depend upon the physical properties of the original iron.

After enough silicon has been added to cause solid castings, any further addition and consequent increase of graphite weakens the easting. The softness and strength given to castings by a suitable addition of silicon is, by a further increase of silicon, changed to stiffness, brittleness, and

weakness.

As strength decreases from increase of graphite and decrease of combined carbon, deflection increases; or, in other words, bending is increased by When no more graphite can form and silicon still increases, deflection diminishes, showing that high silicon not only weakens iron, but makes it stiff. This stiffness is not the same strength-stiffness which is

caused by some at ino time same strength-sames. Since the same strength-sames. In pig irons which received their silicon while in the blast-furnace the graphite more easily separates, and the shrimtage is less than in any mixture. As silicon increases, shrinkage also increases. Silicon of itself increases shrinkage, though by reason of its action upon the carbon in ordinary practice it is truly said that silicon "takes the shrinkage out of cast-iron." The slower a casting crystallizes the greater will be the The slower a casting crystallizes, the greater will be the quantity

of graphite formed within it.

Silicon of itself, however small the quantity present, hardens cast-iron; but the decrease of hardness from the change of the combined carbon to graphite, caused by the silicon, is so much more rapid than the hardening produced by the increase of silicon, that the total effect is to decrease hardness, until the silicon reaches from 3 to 5%.

As practical foundry-work does not call for more than 3% of silicon, the

ordinary use of silicon does reduce the hardness of castings; but this is produced through its influence on the carbon, and not its direct influence on the

iron. When the change from combined to graphite carbon has ceased to dimin-

ish hardness, say at from 2/ to 5% of silicon, the hardening by the silicon

itself becomes more and more apparent as the silicon increases.

Similar the silicon increases are almost exactly proportional. When silicon varies, and other elements do not vary materially, castings with low shrinkage are soft; as shrinkage increases, the castings grow hard in almost, if not exactly, the same proportion. For ordinary foundry-practice the scale of shrinkage may be made also the scale of hardness, provided variations in sulphur, and phosphorus especially, are not present to complicate the re-

The term "chilling" irons is generally applied to such as, cooled slowly, would be gray, but cooled suddenly, become white either to a depth sufficient for practical utilization (e.g., in car-wheels) or so far as to be detrimental. Many irons chill more or less in contact with the cold surface of the mould in which they are cast, especially if they are thin. Sometimes this is a valuable quality, but for general foundry purposes it is desirable to have all parts of a casting an even gray.

Silicon exerts a powerful influence upon this property of irons, partially or entirely removing their capacity of chilling.

When silicon is mixed with irons previously low in silicon the fluidity is increased. It is not the percentage of silicon, but the state of the carbon and the

action of silicon through other elements, which causes the iron to be fluid. Silicon irons have always had the reputation of imparting fluidity to other irons. This comes, no doubt, from the fact that up to 3% or 4% they increase

the quantity of graphite in the resulting casting.

From the statement of Prof. Turner, that the maximum strength occurs with just such a percentage of silicon, and his statement that a founder can, with silicon, produce just the quality of iron that he may need, and from his naming the composition of what he calls a typical foundry-iron, some

founders have inferred that if they knew the percentages of silicon in their irons and in their ferro-silicon, they need only mix so as to get 2% of silicon in order to obtain, always and with certainty, the maximum strength. The solution of the problem is not so simple. Each of the irons which the founder uses will have peculiar tendencies, given them in the blast-furnace, which will exert their influence in the most unexpected ways. However, a which will exert their influence in the most unexpected ways. However, a white iron which will invariably give porous and brittle castings can be made solid and strong by the addition of slicon; a further addition of slicon will turn the iron gray; and as the grayness increases the iron will grow weaker. Excessive silicon will again lighten the grain and cause a hard and brittle as well as a very weak iron. The only softening and shrinkage-lessening influence of silicon is exerted during the time when graphite is being evolution. produced, and silicon of itself is not a softener or a lessener of shrinkage; but through its influence on carbon, and only during a certain stage, does it produce these effects.

Phosphorus.-While phosphorus of itself, in whatever quantity present, weakens cast-iron, yet in quantities less than 1.5% its influence is not sufficiently great to overbalance other beneficial effects, which are exerted before the percentage reaches 1%. Probably no element of itself weakens cast iron as much as phosphorus, especially when present in large quantities.

Shrinkage is decreased when phosphorus is increased. All high-phosphorus pig irons have low shrinkage. Phosphorus does not ordinarily harden cast iron, probably for the reason that it does not increase combined carbon.

The fluidity of the metal is slightly increased by phosphorus, but not to

any such great extent as has been ascribed to it.

The property of remaining long in the fluid state must not be confounded with fluidity, for it is not the measure of its ability to make sharp castings, or to run into the very thin parts of a mould. Generally speaking, the statement is justified that, to some extent, phosphorus prolongs the fluidity of the iron while it is filling the mould.

The old Scotch irons contained about 1% of phosphorus. The foundry-irons which are most sought for for small and thin castings in the Eastern States

contain, as a general thing, over 1% of phosphorus. Certain irons which contain from 4% to 7% silicon have been so much used on account of their ability to soften other irons that they have come to be known as "softeners" and as lesseners of shrinkage. These irons are valuable as carriers of silicon; but the irons which are sold most as softeners and shrinkage-lesseners are those containing from 1% to 2% of phosphorus. We must therefore ascribe the reputation of some of them largely to the phosphorus and not wholly to the silicon which they contains

From 1/5% to 1% of phosphorus will do all that can be done in a beneficial way, and all above that amount weakens the iron, without corresponding benefit. It is not necessary to search for phosphorus-irons. Most irons contain more than is needed, and the care should be to keep it within limits. Sulphur.—Only a small percentage of sulphur can be made to remain in carbonized iron, and it is difficult to introduce sulphur into gray cast iron

or into any carbonized iron, although gray cast iron often takes from the fuel as much more sulphur as the iron originally contained. Percentages of sulphur that could be retained by gray cast iron cannot materially injure the iron except through an increase of shrinkage. The higher the carbon, or the higher the silicon, the smaller will be the influence exerted by sulphur.

The influence of sulphur on all cast iron is to drive out carbon and silicon and to increase chill, to increase shrinkage, and, as a general thing, to decrease strength; but if in practice sulphur will not enter such iron, we shall not have any cause to fear this tendency. In every-day work, however, it is found at times that from which was gray when put into the cupol comes out white, with increased shrinkage and chill, and often with decreased strength. This is caused by decreased silicon, and can be remedied by an increase of silicon.

Mr. Keep's opinion concerning the influence of sulphur, quoted above, is

disagreed with by J. B. Nau (Iron Age, March 29, 1894). He says:
"Sulphur, in whatever shape it may be present, has a deleterious influence on the iron. It has the tendency to render the iron white by the influence it exercises on the combination between carbon and iron. Pig iron containing a certain percentage of it becomes porous and full of holes, and castings made from sulphurous iron are of inferior quality. This happens especially when the element is present in notable quantities. With foundry-iron containing as high as 0.1% of sulphur, castings of greater strength may be ob-

tained than when no sulphur is present. Thus, in some tests on this element quoted by R. Akerman, it is stated that in the foundry-iron from Finspong. used in the manufacture of cannons, a percentage of 0.1% to 0.14% of sulphur in the iron increased its strength to a considerable extent. The percentage of sulphur found originally in the iron put in the cupola is liable to be further increased by part of the sulphur that is invariably found in the coke nurther increased by part of the sulphur that is invariantly found in the coke used. It is seldom that a coke with a small percentage of sulphur is found, whereas coke containing 1% of it and over is very common. With such a fuel in the cuploi, if no special precautions are resorted to, the percentage of sulphur in the metal will in most cases be increased."

That the sulphur contents of pig iron may be increased by the sulphur contained in the coke used, is shown by some experiments in the cupola, reported by Mr. Nau. Seven consecutive heats were made.

The sulphur content of the coke was 1%, and 11.7% of fuel was added to the

charge.

Before melting, the silicon ranged from 0.320 to 0.830 in the seven heats; after melting, it was from 0.110 to 0.534, the loss in melting being from .100 to .375. The sulphur before melting was from .076 to .090, and after melting from .132 to .174, a gain from .044 to .098.

From the results the following conclusions were drawn:

1. In all the charges, without exception, sulphur increased in the pig iron after its passage through the cupola. In some cases this increase more than doubled the original amount of sulphur found in the pig iron.

2. The increase of the sulphur contents in the iron follows the elimination of a greater amount of silicon from that same iron. A larger amount of limestone added to these charges would have produced a more basic cinder. and undoubtedly less sulphur would have been incorporated in the iron.

3. This coke contained 1% of sulphur, and if all its sulphur had passed into the iron there would have been an average increase of 0.12 of sulphur for the seven charges, while the real increase in the pig iron amounted to only This shows that two thirds of the sulphur of the coke was taken up by the iron in its passage through the cupola.

MANGANESE.—Manganese is a nearly white metal, having about the same appearance when fractured as white cast iron. Its specific gravity is about 8, while that of white cast iron, reasonably free from impurities, is but a little above 7.5. As produced commercially, it is combined with iron,

and with small percentages of silicon, phosphorus, and sulphur.

It is generally produced in the blast-furnace. If the manganese is under

40%, with the remainder mostly iron, and silicon not over 0.50%, the alloy is called spiegeleisen, and the fracture will show flat reflecting surfaces, from which it takes its name.

With manganese above 50%, the iron alloy is called ferro-manganese.

As manganese increases beyond 50%, the mass cracks in cooling, and when

it approaches 98% the mass crumbles or falls in small pieces. Manganese combines with iron in almost any proportion, but if an iron containing manganese is remelted, more or less of the manganese will escape by volatilization, and by oxidation with other elements present in the iron. If sulphur be present, some of the manganese will be likely to unite with it and escape, thus reducing the amount of both elements in the casting.

Cast iron, when free from manganese, cannot hold more than 4.50% of carbon, and 3.50% is as much as is generally present; but as manganese increases, carbon also increases, until we often find it in spiegel as high as 5%, and in ferro-manganese as high as 6%. This effect on capacity to hold carbon is peculiar to manganese.

Manganese renders cast iron less plastic and more brittle.

Manganese increases the shrinkage of cast iron. An increase of 1% raised the shrinkage 2%. Judging from some test records, manganese does not influence chill at all; but other tests show that with a given percentage silicon the carbon may be a little more inclined to remain in the combined form, and therefore the chill may be a little deeper. Hence, to cause the chill to be the same, it would seem that the percentage of silicon should be a little higher with manganese than without it,

An increase of 1% of manganese increased the hardness 40%. If a hard chill is required, manganese gives it by adding hardness to the whole casting. J. B. Nau (Iron Age, March 29, 1894), discussing the influence of manga-

nese on cast iron, says:

Manganese favors the combination between carbon and iron, Its influence, when present in sufficiently large quantities, is even great enough not only to keep the carbon which would be naturally found in pig iron combined, but it increases the capacity of iron to retain larger amounts of car-

bon and to retain it all in the combined state.

Manganese iron is often used for foundry purposes when some chill and hardness of surface is required in the casting. For the rolls of steel-rail mills we always put into the mixture a large amount of manganiferous iron, and the rolls so obtained always presented the desired hardness of surface and in general a mottled structure on the outside. The inside, which always cooled much slower, was gray iron. One of the standard mixtures that invariably gave good results was the following:

50% of foundry iron with 1.3% silicon and 1.5% manganese; 35% of foundry iron with 1% silicon and 1.5% manganese; 15% steel (rail ends) with about 0.35% to 0.40% carbon.

The roll resulting from this mixture contained about 1% of silicon and 1% of manganese.

Another mixture, which differed but little from the preceding, was as follows:

45% foundry iron with about 1.3% silicon and 1.5% manganese; 30% foundry iron with about 1% silicon and 1.5% manganese:

10% white or mottled iron with about 0.5% to 0.6% Si, and 1.2% Mn.

15% Bessemer steel-rail ends with about 0.35% to 0.40% C. and 0.6% to 1% Mn. The pig iron used in the preceding mixtures contained also invariably from 1.5% to 1.8% of phosphorus, so that the rolls obtained therefrom carried about 1.3% to 1.4% of that element. The last mixture used produced rolls containing on the average 0.8% to 1% of silicon and 1% of manganese. Whenever we tried to make those rolls from a mixture containing but 0.2% to 0.3% manganese our rolls were invariably of inferior quality, grayer, and con-sequently softer. Manganese iron cannot be used indiscriminately for foundry purposes. When greater softness is required in the castings man-ganese has to be avoided, but when hardness to a certain extent has to be

obtained manganese iron can be used with advantage.

Manganese decreases the magnetism of the iron. This characteristic increases with the percentage of manganese that enters into the composition of the iron. The iron loses all its magnetism when manganese raches 25% of its composition. This peculiarity has been made use of by French metallurgists to draw a clear line between spiegel and ferro-manganese. When the pig contains less than 25% of manganese it is classified as spiegel. and when it contains more than 25 it% is classified as ferro-manganese. For this reason manganese iron has to be avoided in castings of dynamo fields and other pieces belonging to electric machinery, where magnetic conduc-

tibility is one of the first considerations.

Irregular Distribution of Silicon in Pig Iron.-J. W. Thomas (Iron Age, Nov. 12, 1891) finds in analyzing samples taken from every Thomas (100 Age, 100 L) (23) must be analyzing samples scan from the trop other bed of a cast of pig fron that the silicon varies considerably, the iron coming first from the furnace having generally the highest percentage. In one series of tests the silicon decreased from 2.040 to 1.713 from the first bed to the eleventh. In another case the third bed had 1.260 Si., the seventh 1.718, and the eleventh 1.101. He also finds that the silicon varies in each pig, being higher at the point than at the butt. Some of his figures are: point of pig 2.338 81, butt of same 2.157; point of pig 1.34, butt of same 1.767.

Some Tests of Cast Iron. (G. Lanza, Trans. A. S. M. E., x., 187.)-The chemical analyses were as follows:

Gun Iron, Common Iron, per cent. per cent. | per

with the skin on being very nearly one inch square, and those tested with the skin removed being cast nearly one and one quarter inches square, and

afterwards planed down to one inch square.

				Tensile Strength.	Elastic Limit.	of Elas-
Unplaned common.	20,200 to 23,000	T. S. A	v. =	22,066	6,500	13,194,233
Planed common	20,300 to 20,800	,	' =	20,520	5,833	11,943,953
Unplaned gun			_	28,175	11,000	16,130,300
Planed gun	29,500 to 31,000	, " '	' =	= 30,500	8,500	15,932,880

The elastic limit is not clearly defined in cast iron, the elongations increasing faster than the increase of the loads from the beginning of the test. The modulus of elasticity is therefore variable, decreasing as the loads increase. For example, the following results of a test of common cast iron, reported by Prof. Lanza:

Lbs. per sq.	in. Elongation in 13.4 inches.	Sets, in.	Modulus of Elasticity.
1000	.0004		18,217,400
2000	.0013		16,777,700
3000	.0024		14,085,400
4000	.0036		13,101,200
5000	.0048		12,809,200
6000	.0061	.0000	12,319,300
8000	.0088	,0001	11,600,800
10000	.0119	.0001	10,930,500
12000	.0162	.0007	9,714,200

#### CHEMISTRY OF FOUNDRY IRONS.

(C. A. Meissner, Columbia College Q'ly, 1890; Iron Age, 1890.)

Silicon is a very important element in foundry irons. Its tendency when not above ½% is to cause the carbon to separate out as graphite, giving the casting the desired benefits of graphite iron. Between ½% and 3½% silicon is best adapted for iron carrying a fair proportion of low silicon scrap and close iron, for ordinarily no mixture should run below 1½% silicon to get good castings.

From 3% to 5% silicon, as occurs in silvery iron, will carry heavy amounts of scrap. Castings are liable to be brittle, however, if not handled carefully as regards proportion of scrap used.

From 1½ % to 2% silicon is best adapted for machine work; will give strong

clean castings if not much scrap is used with it.

Below 1% silicon seems suited for drills and castings that have to stand great variations in temperature.

Silicon has the effect of making castings fluid, strong, and open-grained; also sound, by its tendency to separate the graphite from the total carbon, and consequent slight expansion of the iron on cooling, causing it to fill out thoroughly. Phosphorus, when high, has a tendency to make iron fluid, retain its heat longer, thereby helping to fill out all small spaces in casting. It makes iron brittle, however, when above ½% in castings. It is excellent when high to use in a mixture of low-phosphorus irons, up to 1½% giving good results, but, as said before, the casting should be below ½%. It has a strong tendency when above 1% in pig to make the iron less graphitic, preventing the separation of graphite.

Sulphur in open iron seldom bothers the founder, as it is seldom present to any extent. The conditions causing open iron in the furnace cause low sulphur. A little manganese is an excellent antidote against sulphur in the furnace. Irons above 1% manganese seldom have any sulphur of any consequence.

Graphite is the all-important factor in foundry irons; unless this is present in sufficient amount in the casting, the latter will be liable to be poor. Graphite causes iron to slightly expand on cooling, makes it soft, tough and fuld. (The statement as to expansion on cooling is denied by W. J. Keep.)

Relation of the Appearance of Fracture to the Chemical Composition.—S. H. Chauvenet says, when run from the blast-furnace] the lower bed is almost always close-grain, but shows practically the same analysis as the large grain in the rest of the cast. If the iron runs rapidly, the lower bed may have as large grain as any in the cast. If the iron runs rapidly for, say, six beds and some obstruction in the tap-hole causes the seventh bed to fill up slowly and sluggishly, this bed may be close-grain, although the eighth bed, if the obstruction is removed, will be open-grain. Neither the graphitic carbon nor the silicon seems to have any influence on the fracture in these cases, since by analysis the graphite and silicon is the same in each. The question naturally arises whether it would not be better to be guided by the analysis than by the fracture. The fracture is a guide, but it is not an infallible guide. Should not the open-and the close-grain iron from the same cast be numbered under the same grade when they have the same analysis?

Mr. Meissner had many analyses made for the comparison of fracture

with analysis, and unless the condition of furnace, whether the iron ran fast or slow, and from what part of pig bed the sample is taken, are known, the fracture is often very misleading. Take the following analyses:

	Α.	В.	C.	D.	E.	F.
Silicon Sulphur Graphitic car Comb. carbon	0.008 3.010	4.818 0.008 2.757	4.270 0.007 2.680	3.328 0.033 2.243	3.869 0.006 3.070 0.108	3.861 0.006 3.100 0.096

A. Very close-grain iron, dark color, by fracture, gray forge.

B. Open-grain, dark color, by fracture, No. 1. C. Very close-grain, by fracture, gray forge. D. Medium-grain, by fracture, No. 2, but much brighter and more open

D. Medium-grain, by fracture, No. 2, but much origiter and more open than A. C, or F.

E. Very large, open-grain, dark color, by fracture, No. 1.

F. Very close-grain, by fracture, gray forge.

By comparing analyses A and B. or E and F, it appears that the close-grain iron is in each case the highest in graphitic carbon. Comparing A and E, the graphite is about the same, but the close-grain is highest in silicon.

## Analyses of Foundry Irons. (C. A. Meissner.) SCOTCH IRONS.

Name.	Grade.	Silicon.	Phos- phorus.	Manga- nese.	Sul- phur.	Graph- ite.	Comb.
Summerlee	1 1	2.70 2.47 3.44	0.545 0.760 1.000	1.80 2.51 1.70	0.01 0.015 0.015	3.09	0.25
Eglinton	2 1 1	2.70 2.15 2.59	0.810 0.618 0.840	2.90 2.80 1.70	0.02 0.025 0.010	2.00 3.76 3.75	0.80 0.21 3.75
Carnbroe Glengarnock Glengarnock said	1 1	1.70 3.03	1.100 1.200	1.83 2.85	0.008	3.50	0.40
to carry 3/2 scrap	2	4,00	0.900	3.41	0.010	1.78	0.90

#### AMERICAN SCOTCH TRONS.

No. Sample	Silicon.	Phos phorus.	Manganese	Sulphur.	No. Grade.	
1 2 3 4 5a 5b 6a 6b 7	6.00 1.67 2.40 1.28 3.50 2.90 3.44 3.35 3.68	0.430 1.920 1.000 0.690 0.613 0.733 1.000 1.300 0.503	1.00 1.90 1.70 1.40 2.51 1.40 1.70 1.50 2.96	0.015 0.012	1 2 2 2 1 1 1	casting

Description of Samples.—No. 1. Well known Ohio Scotch iron, almost silvery, but carries two-thirds scrap; made from part black-band ore. Very successful brand The high silicon gives it its scrap-carrying capacity. No. 2. Brier Hill Scotch castings, made at scale works; castings demand-

ing more fluidity than strength.

No. 3. Formerly a famous Ohio Scotch brand, not now in the market Made mainly from black-band ore.

No. 4. A good Ohio Scotch, very soft and fluid; made from black-band ore-mixture.

Nos. 5a and 5b. Brier Hill Scotch iron and casting; made for stove purposes; 350 lbs. of iron used to 150 lbs. scrap gave very soft fluid iron; worked well.

No. 6a. Shows comparison between Summerlee (Scotch) (6a) and Brier Hill Scotch (6b). Drillings came from a Cleveland foundry, which found both irons closely alike in physical and working quality.

No. 7. One of the best southern brands, very hard to compete with, owing to its general qualities and great regularity of grade and general working.

#### MACHINE TRONS.

Sample No.	Silicon.	Phos- phorus.	Manga- nese.	Sulphur.	Graphite.	Comb. Carbon.	Grade No.
8	2.80	0.492	0.61	0.015			1
9	1.30	0.262	0.70	0.030			3
10a	2.66	0.770	1.20	0.020	2.51		3 2
106	3.63	0.411	1.25	0.014	3.05		1
11	2.10	0.415	0.60	0.050			2
12	1.37	0.294	1.51	0.080	2.31	0.78	2 2 2
13	3.10	0.124	trace	0.021			2
14	2.12	0.610	0.80				
15	1.70	0.632	1.60				
16a	1.45	0.470	1.25	0.009			2
16b	1.40	0.316	1.37	0.008			
17	3.26	0.426	0.25				1
18	0.80	0.164	0.90	0.015			1

DESCRIPTION OF SAMPLES. - No. 8. A famous Southern brand noted for fine machine castings.

No. 9. Also a Southern brand, a very good machine iron. Nos. 10a and 10b. Formerly one of the best known Ohio brands. Does not shrink; is very fluid and strong. Foundries having used this have reported very favorably on it.

No. 11. Iron from Brier Hill Co., made to imitate No. 3; was stronger than No. 3; did not pull castings; was fluid and soft.

No. 12. Copy of a very strong English machine iron.

No. 13. A Pennsylvania iron, very tough and soft. This is partially Bessemer iron, which accounts for strength, while high silicon makes it soft.

No. 14. Castings made from Brier Hill Co.'s machine brand for scale works,

very satisfactory, strong, soft and fluid. No. 15. Castings made from Brier Hill Co.'s one half machine brand, one

half Scotch brand, for scale works, castings desired to be of fair strength, but very fluid and soft.

No. 16a. Brier Hill machine brand made to compete with No. 3. No. 16b. Castings (clothes-hooks) from same, said to have worked badly,

castings being white and irregular. Analysis proved that some other iron too high in manganese had been used, and probably not well mixed. No. 17. A Pennsylvania iron, no shrinkage, excellent machine iron, soft

and strong.

#### No. 18. A very good quality Northern charcoal iron.

### "Standard Grades" of the Brier Hill Iron and Coal Company.

Brier Hill Scotch Iron,-Standard Analysis, Grade Nos. 1 and 2. Silicon .... 2.00 to 3.00 Phosphorus 0.50 to 0.75 Manganese 2.00 to 2.50

Used successfully for scales, mowing-machines, agricultural implements, novelty hardware, sounding-boards, stoves, and heavy work requiring no special strength.

Brier Hill Silvery	y Iron.—Standard	Analysis,	Grade No. 1.
Silicon			3.50 to 5.50
			. 1.00 to 1.50
Managanaga			0 00 +0 0 05

Used successfully for hollow-ware, car-wheels, etc., stoves, bumpers, and similar work, with heavy amounts of scrap in all cases. Should be mainly used where fluidity and no great strength is required, especially for heavy work. When used with scrap or close pig low in phosphorus, castings of considerable strength and great fluidity can be made

disiderable strength and great haidity can be made	
Fairly Heavy Machine Iron.—Standard Analysis,	Grade No. 1.
Silicon	
Phosphorus	0.50 to 0.60
Manganese	.20 to 1.40

The best iron for machinery, wagon-boxes, agricultural implements, pump-works, hardware specialties, lathes, stoves, etc., where no large amounts of scrap are to be carried, and where strength, combined with great fluidity and softness, are desired. Should not have much scrap with it.

Regular Machine	Iron.—Standard	Analysis,	Grade	Nos. 1	and 2	
Silicon				1.50 to	2.00	
Phosphorus		· · · · · · · · · · · · · · ·		0.30 to	0.50	
Manganese		• • • • • • • • • • • •		0.80 to	1 00	

Used for hardware, lawn-mowers, mower and reaper works, oil-well machinery, drills, fine machinery, stoves, etc. Excellent for all small fine castings requiring fair fluidity, softness, and mainly strength. Cannot be well used alone for large castings, but gives good results on same when used with above mentioned heavy machine grade; also when used with the Scotch in right proportion. Will carry but little scrap, and should be used alone for good strong castings.

For Axles and			Grade No. 2.
Silicon	 	1.50	
Phosphorus	 	0.200	and less.

This gave excellent results.

A good neutral iron for guns,	etc., will run about as follows:
Silicon	
	0.25
	0.20

It should be open No. 1 iron.

This gives a very tough, elastic metal. More sulphur would make tough but decrease elasticity.

For fine castings demanding elegance of design but no strength, phosphorus to 3.0% is good. Can also stand 1.5% to 2.0% marganese. For work of a hard, abrasive character manganese can run 2.0% in casting.

Analyses of Castings.

Sample No.	Silicon.	Phos- phorus.	Manganese	Sulphur.	Graphite.	Comb. Carbon.	
31 32 33	2.50 0.85 1.53	1.400 0.351 0.327	2.20 0.92 1.08	0.030 0.040	3,10	0.58	
$\frac{34a}{34b}$	1.84 2.20 2.50	0.577 0.742 1.208	1.04 1.10 1.16				
34c 35a 35b	2.80 3.10	0.418 1.280	0.54 1.14				
$\begin{array}{c} 35c \\ 35d \\ 35e \end{array}$	3.30 2.88 4.50	0.879 0.408 0.660	0.80 1.10 0.78				
36 37a 87b	3.43 2.68 1.90	1.439 0.900 0.980	0.90 1.30 1.20	0.025			

No. 31. Sewing-machine casting, said to be very fluid and good casting. This is an odd analysis. I should say it would have been too hard and brittle, yet no complaint was made.

No. 32. Very good machine casting, strong, soft, no shrinkage. No. 33. Drillings from an annealer-box that stood the heat very well.

No. 34a. Drillings from door-hinge, very strong and soft. No. 34b. Drillings from clothes-hooks, tough and soft, stood severe ham-

mering. No. 34c. Drillings from window-blind hinge, broke off suddenly at light Too high phosphorus. strain.

No. 35a. Casting for heavy ladle support, very strong. Nos 35b and 35c. Broke after short usage. Phosphorus too high. Carbumpers

No. 35d. Elbow for steam heater, very tough and strong.

No. 36. Cog-wheels, very good, shows absolutely no shrinkage. No. 37. Heater top network, requiring fluidity but no strength.

No. 37a. Gray part of above. No. 37b. White, honeycombed part of above. Probably bad mixing and got chilled suddenly.

# STRENGTH OF CAST IRON.

Rankine gives the following figures:

Various qualities, T. S..... 13,400 to 29,000, average 16,500 145,000, Compressive strength..... 82,000 to 112,000 Modulus of elasticity ...... 14,000,000 to 22,900,000, 17,000,000

Specific Gravity and Strength. (Major Wade, 1856.) Third-class guns; Sp. Gr. 7.087, T. S. 20,148. Another lot; least Sp. Gr. 7.163. T. S. 22,402.

Second-class guns: Sp. Gr. 7.154, T. S. 24,767. Another lot: mean Sp. Gr.

7.302, T. S. 27,232.

First class guns: Sp. Gr. 7.204, T. S. 28,805. Another lot: greatest Sp. Gr. 7.402, T. S. 31,027.

Nos. 3 and 4 charcoal pig iron from Chapinville, Conn., showed a tensile strength per square inch of from 34,761 lbs. to 41,882 lbs. Charcoal pig iron

strength per square inch of from 34,701 los. to 41,882 los. Charcoal pig from 18helby, Ala. (tests made in August, 1891), showed a strength of 34,800 los. for No. 3: No. 4, 39,675 lbs.; No. 5, 46,450 lbs.; and a mixture of equal parts of Nos. 2, 4, and 5, 41,470 los. (Bull. I. & S. A.)

Variation of Density and Tenacity of Gun-irons.—An increase of density invariably follows the rapid cooling of cast iron, and as a general rule the tenacity is increased by the same means. The tenacity generally increases quite uniformly with the density, until the latter ascends to some given point; after which an increased density is accompanied by a diminished tenacity.

The turning-point of density at which the best qualities of gun-iron attain their maximum tenacity appears to be about 7.30. At this point of density, or near it, whether in proof-bars or gun-heads, the tenacity is greatest.

As the density of iron is increased its liquidity when melted is diminished.

This causes it to congeal quickly, and to form cavities in the interior of the casting. (Pamphlet of Builders' Iron Foundry, 1893.)

Specifications for Cast Iron for the World's Fair Build-

ings, 1892.-Except where chilled iron is specified, all castings shall be of tough gray iron, free from injurious cold-shuts or blow-holes, true to pattern, and of a workmanlike finish. Sample pieces 1 in. square, cast from the same heat of metal in sand moulds, shall be capable of sustaining on a clear span of 4 feet 6 inches a central load of 500 lbs, when tested in the rough bar

Specifications for Tests of Cast Iron in 12" B. L. Mortars, (Pamphlet of Builders Iron Foundry, 1893.)-Charcoal Gun Iron.-The tensile strength of the metal must average at each end at least 30,000 lbs per square inch; no specimen to be over 37,000 lbs, per square inch; but one specimen from each end may be as low as 28,000 lbs, per square inch. The long extension specimens will not be considered in making up these averages, but must show a good elongation and an ultimate strength, for each specimen, of not less than 24,000 lbs. The density of the metal must be such as to indicate that the metal has been sufficiently refined, but not carried so

high as to impair the other qualities.

night as to impair the other qualities.

Specifications for Grading Pig Iron for Car Wheels by Chill Tests made at the Furnace. (Penna, R. R. Specifications, 1883.)—The chill cup is to be filled, even full, at about the middle of every cast from the furnace. The test-piece so made will be 7½ inches long, 3½ inches wide, and 134 inches thick, and 1s to be broken across the centre when entirely cold. The depth of chill will be shown on the bottom of the testpiece, and is to be measured by the clean white portion to the point where 

wheel mixtures, the average tensile strength of the charcoal iron used being

22,000 lbs.:

				ios, per sq. in
Charc	oal iron	with	21/5% steel	22,467
44	44	66	33/4% steel	26,733
"	66		61/4% steel and 61/4% anthracite	
6.6	6.6	66	71/3% steel and 71/3% anthracite	28,150
44	66		21/6% steel, 21/6% wro't iron, and 61/4% an	
4.0	46	"	5 % steel, 5% wro't iron, and 10 % ant	h 26,500
			(Jour C. I.	W. iii. p. 184.)

Cast Iron Partially Bessemerized .- Car wheels made of partially Bessemerized iron (blown in a Bessemer converter for 31/2 minutes), chilled in a chill-test mould over an inch deep, just as a test of cold-blast

charcoal fron for ear wheels would chill. Car wheels made of this blown iron have run 250,000 miles. (Jour. C. I. W., vi. p. 77) **Bad Cast Iron.**—On October 15, 1891, the east-iron fly-wheel of a large pair of Corliss engines belonging to the Amoskeag Mfg, Co., of Manchester, N. H., exploded from centrifugal force. The fly-wheel was 30 feet diameter and 110 inches face, with one set of 12 arms, and weighed 116,000 lbs. After the accident, the rim castings, as well as the ends of the arms, were found to be full of flaws, caused chiefly by the drawing and shrinking of the metal. Specimens of the metal were tested for tensile strength, and varied from 15.000 lbs. per square inch in sound pieces to 1000 lbs. in spongy ones. None of these flaws showed on the surface, and a rigid examination of the parts before they were erected failed to give any cause to suspect their true nature. Experiments were carried on for some time after the accident in the Amoskeag Company's foundry in attempting to duplicate the flaws, but with no success in approaching the badness of these castings.

#### MALLEABLE CAST IRON.

Malleableized cast iron, or malleable iron castings, are castings made of ordinary cast iron which have been subjected to a process of decarbonization, which results in the production of a crude wrought iron. Handles, latches, and other similar articles, cheap harness mountings, plowshares, iron handles for tools, wheels, and pinions, and many small parts of machinery, are made of malleable cast iron. For such pieces charcoal cast iron of the best quality for other iron of similar chemical composition), should be selected. Coke irons low in silicon and sulphur have been used in place of charcoal irons. The castings are made in the usual way, and are then imbedded in oxide of iron, in the form, usually, of hematite ore, or in peroxide of manganese, and exposed to a full red-heat for a sufficient length of time, to insure the nearly complete removal of the carbon. This decarbonization is conducted in east-iron boxes, in which the articles, if small, are packed in alternate layers with the decarbonizing material. The largest pieces require the longest time. The fire is quickly raised to the maximum temperature, but at the close of the process the furnace is cooled very slowly. The operation requires from three to five days with ordinary small castings, and may take two weeks for large pieces.

Rules for Use of Malleable Castings, by Committee of Master Carbuilders' Ass'n, 1890,

1. Never run abruptly from a heavy to a light section.

2. As the strength of malleable cast iron lies in the skin, expose as much surface as possible. A star-shaped section is the strongest possible from which a casting can be made. For brackets use a number of thin ribs instead of one thick one.

3. Avoid all round sections; practice has demonstrated this to be the weakest form. Avoid sharp angles.

4. Shrinkage generally in castings will be 3/16 in. per foot.

Strength of Malleable Cast Fron.—Experiments on the strength of malleable cast iron, made in 1891 by a committee of the Master Carbuilders' Association. The strength of this metal varies with the thickness, as the following results on specimens from 1/4 in. to 11/2 in. in thickness show:

Dimensions.	Tensile Strength.	Elongation.	Elastic Limit.
in. in. 1.52 by .25 1.52 " .39 1.53 " .5 1.53 " .64 2. " .78 1.54 " .88 1.06 " 1.02 1.28 " 1.3 1.52 " 1.54	1b. per sq. in. 34,700 33,700 32,800 32,100 25,100 33,600 30,600 27,400 28,200	per cent in 4 in.  2 2 2 2 2 2 1/2 1/2 1 1 1 1/4	lb. per sq. in. 21,100 15,260 17,000 19,400 19,400 19,300 17,600

The low ductility of the metal is worthy of notice. The committee gives the following table of the comparative tensile resistance and ductility of malleable cast iron, as compared with other materials:

	Ultimate Strength, lb. per sq. in	Comparative Strength; Cast Iron = 1.	Elongation Per Cent in 4 in.	Comparative Ductility; Malleable Cast Iron = 1.
Cast iron	20,000 32,000 50,000	1 1.6 2.5	0.35 2.00 20.00	0.17 1 10
Steel castings	60,000	3.0	10.00	5

Another series of tests, reported to the Association in 1892, gave the following:

Thick- ness.	Width.	Area.	Elastic Limit.	Ultimate Strength.	Elongation in 8 in.
in. .271 .293 .39 .41 .529 .661	in. 2.81 2.78 2.82 2.79 2.76 2.81	sq. in. .7615 .8145 1.698 1.144 1.46 1.857	lb. per sq. 23.520 22.650 20.595 20.230 19.520 18.840	lb. per sq. in. 32,620 28,160 32,060 28,850 27,875 25,700	1.5 .6 1.5 1.0 1.1
.8 1.025 1.117 1.021	2.76 2.82 2.81 2.82	2.208 2.890 3.138 2.879	18.390 18,220 17,050 18,410	25,120 28,720 25,510 26,950	1.1 1.5 1.3 1.3

#### WROUGHT IRON.

Influence of Chemical Composition on the Properties of Wrought Iron. (Beardslee on Wrought Iron and Chain Cables, Abruigement by W. Kent. Wiley & Sons, 1879.)—A series of 2000 fests of specimens from 14 brands of wrought iron, most of them of high repute, was made in 1877 by Capt. L. A. Beardslee, U.S.N., of the United States Testing Board. Forty-two chemical analyses were made of these irons, Testing Board. Forty-two chemical analyses were made of these irons, with a view to determine what influence the chemical composition had upon the strength, ductility, and welding power. From the report of these tests by A. L. Holley the following figures are taken :

	Average		Chemical Composition.				
Brand.	Tensile Strength.	· S.	· P.	Si.	C.	Mn.	Slag.
L P B J O	66,598 54,363 52,764 51,754 51,134 50,765	trace {0.009 {0.001 0.008 {0.003 }0.005 {0.004 {0.005 0.007	\$ 0.065 \$ 0.084 0.250 0.095 0.231 0.140 0.291 0.067 0.078 0.169	0.080 0.105 0.182 0.028 0.156 0.182 0.321 0.065 0.073 0.154	0.212 0.512 0.033 0.066 0.015 0.027 0.051 0.045 0.042 0.042	0.005 0.029 0.033 0.009 0.017 trace 0.053 0.007 0.005	0.192 0.452 0.848 1.214 0.678 1.724 1.168 0.974

Where two analyses are given they are the extremes of two or more analyses of the brand. Where one is given it is the only analysis. Brand L should be classed as a puddled steel.

ORDER OF QUALITIES GRADED FROM NO. 1 TO NO. 19.

Brand.	Tensile Strength.	of Area.	Elongation.	Welding Power.
L	1	18	19	most imperfect
P	6	6	3	badly.
В	12	16	15	best.
J	16	19	18	rather badly.
0	18	- 1	4	very good.
C	odyr 6 v 19	12	16	

The reduction of area varied from 54.2 to 25.9 per cent, and the elongation from 29.9 to 8.3 per cent.

tion from 23.2 to 3.3 per cent.

Brand O, the pirest iron of the series, ranked No. 18 in tensile strength, but was one of the most ductile; brand B, fquite impure, was below the average both in strength and ductility, but was the best in welding power; P, also quite impure, was one of the best in every respect except welding, while L, the highest in strength, was not the most pure, it had the least ductility, and its welding power was most imperfect. The evidence of the influence of chemical composition upon quality, therefore, is quite contradictory and confusing. The irons differing remarkably in their mechanical properties, it was found that a much more marked influence upon their qualities was caused by different treatment in rolling than by differences in composition.

In regard to slag Mr. Holley says: "It appears that the smallest and most worked iron often has the most slag. It is hence reasonable to con-

clude that an iron may be dirty and yet thoroughly condensed."

In his summary of "What is learned from chemical analysis," he says: "So far, it may appear that little of use to the makers or users of wrought iron has been learned. . . . The character of steel can be surely predicated on the analyses of the materials; that of wrought iron is altered by subtle and unobserved causes "

Influence of Reduction in Rolling from Pile to Bar on the Strength of Wrought Iron.—The tensile strength of the iron used in Beardslee's tests ranged from 46,000 to 62,700 lbs. per sq. in., brand L, which was really a steel, not being considered. Some specimens of I gave figures as high as 70,000 lbs. The amount of reduction of sectional

area in rolling the bars has a notable influence on the strength and elastic limit; the greater the reduction from pile to bar the higher the strength. The following are a few figures from tests of one of the brands;

Size of bar, in, diam .: 1/4 3 80 80 72 25 Area of pile, sq. in.: 15.7 8.88 47,761 2.17 Bar per cent of pile : 4.36 3.14 1.6 46,322 48,280 Tensile strength, lb.: 51,128 52,275 59,585 Elastic limit, lb.: 39,126 23,430 26,400 31.892 36,467

Specifications for Wrought Iron (F. H. Lewis, Engineers' Club of Philadelphia, 1891).—1. All wrought iron must be tough, ductile, fibrous, and of uniform quality for each class, straight, smooth, free from cinderpockets, flaws, buckles, blisters, and injurious cracks along the edges, and must have a workmanlike finish. No specific process or provision of manufacture will be demanded, provided the material fulfils the requirements of these specifications.

2. The tensile strength, limit of elasticity, and ductility shall be determined from a standard test-piece not less than ¼ inch thick, cut from the full-sized bar, and planed or turned parallel. The area of cross-section shall not be less than ¼ square inch. The elongation shall be measured after breaking on an original length of 8 inches.

3. The tests shall show not less than the following results:

	Ultimate Strength, lbs. per sq. inch.	Limit of Elasticity, lbs. per sq. inch.	Elongation in 8 inches, per cent.
For bar iron in tension For shape iron	50,000 48,000 48,000 46,000	26,000 26,000 26,000 25,000	18 15 12 10

4. When full-sized tension members are tested to prove the strength of their connections, a reduction in their ultimate strength of (500 × width of been required root surface).

bar) pounds per square inch will be allowed.

5. All iron shall bend, cold, 180 degrees around a curve whose diameter is twice the thickness of piece for bar iron, and three times the thickness

for plates and shapes.

6. Tron which is to be worked hot in the manufacture must be capable of bending sharply to a right angle at a working heat without sign of fracture.

7. Specimens of tensile iron upon being nicked on one side and bent shall

show a fracture nearly all fibrous.

8. All rivet iron must be tough and soft, and be capable of bending cold until the sides are in close contact without sign of fracture on the convex side of the curve.

Pennsylvania Railroad Specifications for Merchant Bar Iron or Steel.—Miscellaneous merchant bar iron or steel for which no special specifications defining shapes and uses are issued, should have a tensile strength of 50,000 to 55,000 lbs. per square inch and an elongation of 30% in a section originally 2 inches long.

No fron or steel will be accepted under this specification if tensile strength falls below 48,000 lbs. or goes above 60,000 lbs. per square inch, nor if elongation is less than 15% in 2 inches, nor if it shows a granular fracture covering more than 50% of the fractured surface, nor if it shows any difficulty in

welding.

In preparing test-pieces from round or rectangular bars, they will be turned or shaped so that the tested sections may be the central portion of the bar, in all sizes up to 134 inches in any diametrical or side measurement. In larger sizes test-pieces will be made to fall about half-way from centre to circumference.

Bars of iron 1/2 in. thick or less, or tortured forms of iron, such as angle, tee or channel bars, will be accepted if tensile strength is above 45,000 lbs. and elongation above 12%; but the testing of such sizes and sections is optional.

Specifications for Wrought Iron for the World's Fair Buildings. (Eng'g News, March 26, 1892.)—All iron to be used in the tensile members of open trusses, laterals, pins and bolts, except plate iron over 8 inches wide, and shaped iron, must show by the standard test-pieces a tensile strength in lbs. per square inch of:
7.000 × area of original bar in sq. in.

circumference of original bar in inches'

with an elastic limit not less than half the strength given by this formula.

and an elongation of 20% in 8 in.

Lateral or cross-section rods.....

Plate iron 24 inches wide and under, and more than 8 inches wide, must Flate from 2 in fiches who e and under, and more than 6,500 lbs, per sq. in, show by the standard test-pieces a tensile strength of 48,000 lbs, per sq. in, with an elastic limit not less than 26,000 lbs, per square inch, and an elongation of not less than 125. All plates over 24 inches in width must have a tensile strength not less than 46,000 lbs., with an elastic limit not less than 26,000 lbs. per square inch. Plates from 24 inches to 36 inches in width must have an elongation of not less than 10%; those from 36 inches to 48 inches in width, 8%; over 48 inches in width, 5%.

All shaped iron, flanges of beams and channels, and other iron not hereinbefore specified, must show by the standard test-pieces a tensile strength in lbs. per square inch of:

7,000 × area of original bar circumference of original bar'

with an elastic limit of not less than half the strength given by this formula, and an elongation of 15% for bars % inch and less in thickness, and of 12% for bars of greater thickness. For webs of beams and channels, specifications for plates will apply.

All rivet iron must be tough and soft, and pieces of the full diameter of

the rivet must be capable of bending cold, until the sides are in close contact,

without sign of fracture on the convex side of the curve.

Stay-bolt Tron,—Mr. Vauclain, of the Baldwin Locomotive Works, at a meeting of the American Railway Master Mechanics' Association, in at a meeting of the American Rainway master mechanics Association, in 1859, says: Many advocate the softest iron in the market as the best for stay-bolts. He believed in an iron as hard as was consistent with heading the bolt nicely. The higher the tensile strength of the iron, the more vibrations it will stand, for it is not so easily strained beyond the yield-point. The Baldwin specifications for stay-bolt iron call for a tensile strength of 50,000 to 52,000 lbs. per square inch, the upper figure being preferred, and the lower being insisted upon as the minimum.

#### FORMULÆ FOR UNIT STRAINS FOR IRON AND STEEL IN STRUCTURES.

(F. H. Lewis, Engineers' Club of Philadelphia, 1891.)

The following formulæ for unit strains per square inch of net sectional area shall be used in determining the allowable working stress in each member of the structure. (For definitions of soft and medium steel see Specifications for Steel.) Tension Members.

Soft Steel. Wrought Iron. Medium Steel. Floor-beam hangers or suspenders, forged Will not be used Will not be used 7000 bars Counter-ties... 6000 7000 Suspenders, hangers and counters, riveted members, net sec-7000 tion 5000 5500 Solid rolled beams .... Will not be used 8000 8000 Riveted truss members and tension flanges 8% greater than of girders, net sec- $7000\left(1 + \frac{\min}{\max}\right)$  $9000\left(1+\frac{\min}{\max}\right)$ iron Forged eyebars...... Will not be used Will not be used  $9000 \left(1 + \frac{\min}{\max}\right)$ 

16,000

15,000

For eyebars

only, 17,000

#### Shearing.

	Wrought Iron.	Soft Steel.	Medium Steel.		
On pins and shop rivets On field rivets In webs of girders	4800	6600 5200 5000	Will not be used		

	Bearing	g.	
	Wrought Iron.	Soft Steel.	Medium Steel.
On projected semi- intrados of main-pin holes. On projected semi-in- trados of rivet-holes* On lateral pins Of bed-plates on ma-	12,000 12,000 15,000	13,200 13,200 16,500	14,500 14,500 18,000
soury 2	50 lbs. per sq. in.		

<sup>\*</sup> Excepting that in pin-connected members taking alternate stresses, the bearing stress must not exceed 9000 lbs. for iron or steel,

Bending. On extreme fibres of pins when centres of bearings are considered as points of application of strains:

Wrought Iron, 15,000. Soft Steel, 16,000. Medium Steel, 17,000.

#### Compression Wembers

Compression Members.					
	Wrought Iron.	Soft Steel.	Medium Steel.		
Chord sections: Flat ends One flat and one pin end Chords with pin ends and all end-posts All trestle-posts Lateral struts, and compression in coll is or struts, stiff suspender and stiff chords	$7000 \left(1 + \frac{\min}{\max}\right) - 35 \frac{l}{r}$ $7000 \left(1 + \frac{\min}{\max}\right) - 40 \frac{l}{r}$ $7000 \left(1 + \frac{\min}{\max}\right) - 35 \frac{l}{r}$ $7500 - 40 \frac{l}{r}$	10%	20% greater than iron		

In which formulæ l= length of compression member in inches, and r= least radius of gyration of member in inches. No compression member shall have a length exceeding 45 times its least width, and no post should be used in which  $l\rightarrow r$  exceeds 125.

# Members Subject to Alternate Tension and Compression.

	Wrought Iron.	Soft Steel.	Medium Steel.
For compression only For the greatest stress	Use the formulæ above $7000\left(1 - \frac{\text{max. lesser}}{2 \text{ max. greater}}\right)$	8% greater than iron	20% greater than iron

Use the formula giving the greatest area of section. The compression flanges of beams and plate girders shall have the same cross-section as the tension flanges.

W. H. Burr, discussing the formulæ proposed by Mr. Lewis, says: "Taking the results of experiments as a whole, I am constrained to believe that they indicate at least 15% increase of resistance for soft-steel columns over those of wrought iron, with from 20% to 25% for medium steel, rather than 10% and 20% respectively.

"The high capacity of soft steel for enduring torture fits it eminently for

alternate and combined stresses, and for that reason I would give it 15% increase over iron, with about 22% for medium steel.

"Shearing tests on steel seem to show that 15% and 22% increases, for the

two grades respectively, are amply justified.
"I should not hesitate to assign 15% and 22% increases over values for iron for bearing and bending of soft and medium steel as being within the safe limits of experience. Provision should also be made for increasing pin-shearing, bending and bearing stresses for increasing pin-sing loads.

Maximum Permissible Stresses in Structural Materials used in Buildings. (Building Ordinances of the City of Chicago, 1893.) Cast iron, crushing stress: For plates, 15,000 lbs, per square inch; for littles, brackets, or corbels, compression 13,500 lbs, per square inch, and tension 3000 lbs. per square inch. For girders, beams, corbels, brackets, and trusses, 16,000 lbs, per square inch for steel and 12,000 lbs, for iron.

For plate girders :

or plate girders: Flange area = 
$$\frac{\text{maximum bending moment in ft.-lbs.}}{CD}.$$

D = distance between centre of gravity of flanges in feet.

 $C = \begin{cases} 13,500 \text{ for steel.} \\ 10,000 \text{ for iron.} \end{cases}$ 

Web area = 
$$\frac{\text{maximum shear}}{C}$$
.  $C = \begin{cases} 10,000 \text{ for steel,} \\ 6,000 \text{ for iron.} \end{cases}$ 

For rivets in single shear per square inch of rivet area:

For timber girders:

$$S = \frac{cbd^2}{l}.$$

$$b = \text{breadth of beam in inches,}$$

$$d = \text{depth of beam in inches,}$$

$$l = \text{length of beam in feet,}$$

$$l = \frac{beat}{l}$$

$$c = \frac{beat}{l}$$

$$c = \frac{beat}{l}$$

$$l = \frac{beat}{l}$$

Proportioning of Materials in the Memphis Bridge (Geo. S. Morison, Trans. A. S. C. E., 1893).—The entire superstructure of the Memphis bridge is of steel and it was all worked as steel, the rivet-holes being drilled in all principal members and punched and reamed in the lighter members

The tension members were proportioned on the basis of allowing the dead load to produce a strain of 20,000 lbs. per square inch, and the live load a strain of 1,000 lbs. per square inch. In the case of the central span, where the dead load was twice the live load, this corresponded to 15,000 lbs. total

strain per square inch, this being the greatest tensile strain.

The compression members were proportioned on a somewhat arbitrary basis. No distinction was made between live and dead loads. A maximum strain of 14,000 lbs. per square inch was allowed on the chords and other large compression members where the length did not exceed 16 times the least transverse dimension, this strain being reduced 750 lbs, for each additional unit of length. In long compression members the maximum length was limited to 30 times the least transverse dimension, and the strains limited to 6,000 lbs. per square inch, this amount being increased by 200 lbs. for each unit by which the length is decreased.

Wherever reversals of strains occur the member was proportioned to resist the sum of compression and tension on whichever basis (tension or compression) there would be the greatest strain per square inch; and, in addition, the net section was proportioned to resist the maximum tension,

and the gross section to resist the maximum compression.

The floor beams and girders were calculated on the strain being limited to 10,000 lbs. per square inch in extreme fibres. Rivet-holes in cover-plates and flanges were deducted.

The rivets of steel in drilled or reamed holes were proportioned on the basis of a bearing strain of 15,000 lbs. per square inch and a shearing strain of 7500 lbs. per square inch, and special pains were taken to get the double shear in as many rivets as possible. This was the requirement for shop rivets. In the case of field rivets, the number was increased one-half.

The pins were proportioned on the basis of a bearing strain of 18,000 lbs. per square inch in extreme fibre, the diameters of the pins being never made more than one inch

less than the width of the largest eye-bar attaching to them.

The weight on the rollers of the expansion joint on Pier II is 40,000 lbs. per linear foot of roller, or 3,333 lbs. per linear inch, the rollers being 15 ins. in diameter.

As the sections of the superstructure were unusually heavy, and the strains from dead load greatly in excess of those from moving load, it was thought best to use a slightly higher steel than is now generally used for lighter structures, and to work this steel without punching, all holes being drilled. A somewhat softer steel was used in the floor-system and other lighter parts.

The principal requirements which were to be obtained as the results of tests on samples cut from finished material were as follows:

	Max. Ultimate Strength, lbs. per sq. inch.	Min. Ultimate Strength, lbs. per sq. inch.	Min. Elastic Limit, lbs, per sq. in.	Elongation	Min. Per- centage of Reduction at Fracture	
High-grade steel. Eye-bar steel Medium steel Soft steel	78,500 75,000 72,500 63,000	69,000 66,000 64,000 55,000	40,000 38,000 37,000 30,000	18 20 22 28	38 40 44 50	

# TENACITY OF METALS AT VARIOUS TEMPERATURES.

The British Admiralty made a series of experiments to ascertain what lose of strength and ductility takes place in gun-metal compositions when raised to high temperatures. It was found that all the varieties of gun-metal suffer a gradual but not serious loss of strength and ductility up to a certain temperature, at which, within a few degrees, a great change takes place, the strength falls to about one half the original, and the ductility is wholly gone. At temperatures above this point, up to 500, there is little, if any, further loss of strength; the temperature at which this great change and loss of strength takes place, although uniform in the specimens cast from the same pot, varies about 100° in the same composition cast at different temperatures, or with some varying conditions in the foundry process. The temperature at which the change took place in No. 1 series was ascertained to be about 370°, and in that of No. 2, at a little over 250°. Whatever may be the cause of this important difference in the same composition, the fact stated may be taken as certain. Rolled Muntz metal and copper are satisfactory up to 500°, and may be used as securing-bolts with safety. Wrought iron, Yorkshire and remanufactured, increase in strength up to 500°, but lose slightly in ductility up to 300°, where an increase begins and continues up to 500°, where it is still less than at the ordinary temperature of the atmosphere. The strength of Landore steel is not affected by temperature of the atmosphere. The strength of Landore steel is not affected by temperature on half. (fron, Oct.

6, 1877. Tensile Strength of Iron and Steel at High Temperatures.—James E. Howard's tests (Iron Age, April 10, 1890), shows that the tensile strength of steel diminishes as the temperature increases from 0° until a minimum is reached between 200° and 300° F., the total decrease being about 4000 lbs. per square inch in the softer steels, and from 6000 to 5000 lbs. in steels of over \$0,000 lbs. tensile strength. From this minimum point he strength increases up to a temperature of 400° to 560° F., the maximum being reached earlier in the harder steels, the increase amounting to from 1,000 to 20,000 lbs. per square inch above the minimum strength at from 200°.

to 300°. From this maximum, the strength of all the steel decreases steadily at a rate approximating 10,000 lbs. decrease per 100° increase of temperature. A strength of 20,000 lbs. per square inch is still shown by .10 C. steel at about 1000° F. and by .60 to 1.00 C. steel at about 1000° F.

at about 1000° F., and by .60 to 1.00 C. steel at about 1600° F.

The strength of wrought iron increases with temperature from 0° up to a maximum at from 400 to 600° F., the increase being from 8000 to 10.000 lbs. per square inch, and then decreases steadily till a strength of only 6000 lbs.

per square inch is shown at 1500° F.

Cast iron appears to maintain its strength, with a tendency to increase, unt 1 900° is reached, beyond which temperature the strength gradually diminishes. Under the highest temperatures, 1500° to 1600° F., numerous cracks on the cylindrical surface of the specimen were developed prior trupture. It is remarkable that cast iron, so much inferior in strength to the steels at atmospheric temperature, under the highest temperatures has nearly the same strength the high-temper steels then have.

Strength of Iron and Steel Boiler-plate at High Temperatures. (Chas. Huston, Jour. F. I., 1877.)

Average of Three Tests of	EACH.		
Temperature F.	68°	575°	925°
Charcoal iron plate, tensile strength, lbs	55,366	63,080 23	65,343 21
Soft open-hearth steel, tensile strength, lbs	54,600	66,083	64,350
" Crucible steel, tensile strength, lbs	64,000	69,266	68,600
" " contr. %		30	21

Strength of Wrought Iron and Steel at High Temperatures. (Jour, F. I., exii., 1881, p. 241.) Kollmann's experiments at Oberhausen included tests of the tensile strength of iron and steel at temperatures ranging between 70° and 2000° F. Three kinds of metal were tested, viz., fibrous iron having an ultimate tensile strength of 28,280 lbs., and an elongation of 17.5%; fine-grained iron having for the same elements values of 56,892 lbs., 39,113 lbs., and 20%; and Bessener steel having values of 84,826 lbs., 55,029 lbs., and 14.5%. The mean ultimate tensile strength of each material expressed in per cent of that at ordinary atmospheric temperature is given in the following table, the fifth column of which exhibits, for purposes of comparison, the results of experiments carried on by a committee of the Franklin Institute in the years 1832–36.

	Fibrous	Fine-grained	Bessemer	Franklin
Temperature	Wrought	Iron,	Steel,	Institute,
Degrees F.	Iron, p. c.	per cent.	per cent.	per cent.
0	100.0	100.0	100.0	96.0
100	100.0	100.0	100.0	102.0
200	100.0	100.0	100.0	105.0
300	97.0	100.0	100.0	106.0
400	95.5	100.0	100.0	106.0
500	92.5	98.5	98.5	104.0
600	88.5	95.5	92.0	99.5
700	81.5	90.0	68.0	92.5
800	67.5	77.5	44.0	75.5
900	44.5	51.5	36.5	53.5
1000	26.0	36.0	31.0	*36.0
1100	20.0	30.5	26.5	
1200	18.0	28.0	22.0	
1300	16.5	23.0	18.0	
1400	13.5	19.0	15.0	
1500	10.0	15.5	12.0	
1600	7.0	12.5	10.0	
1700	5.5	10.5	8.5	
1800	4.5	8.5	7.5	
1900	3.5	7.0	6.5	
2000	3.5	5.0	5.0	

The Effect of Cold on the Strength of Iron and Steel.— The following conclusions were arrived at by Mr. Styffe in 1865:

(1) That the absolute strength of iron and steel is not diminished by cold, but that even at the lowest temperature which ever occurs in Sweden it is at least as great as at the ordinary temperature (about 60° F.).

(2) That neither in steel nor in iron is the extensibility less in severe cold than at the ordinary temperature.

(3) That the limit of elasticity in both steel and iron lies higher in severe cold.

(4) That the modulus of elasticity in both steel and iron is increased on reduction of temperature, and diminished on elevation of temperature; but that these variations never exceed 0.05 % for a change of temperature of 1.8° F., and therefore such variations, at least for ordinary purposes, are of no special importance.

Mr. C. P. Sandberg made in 1867 a number of tests of iron rails at various Mr. C. F. Sandoerg made in 160, a number of reason was of opinion that, ethoperatures by means of a falling weight, since he was of opinion that, although Mr. Styffe's conclusions were perfectly correct as regards tensibetrength, they might not apply to the resistance of iron to impact at low temperatures. Mr. Sandberg convinced himself that "the breaking strain" of iron, such as was usually employed for rails, "as tested by sudden blows or shocks, is considerably influenced by cold; such iron exhibiting at 10° F, only from one third to one fourth of the strength which it possesses 48° F." Mr. J. J. Webster (Inst. C. E., 1880) gives reasons for doubting the accuracy of Mr. Sandberg's deductions, since the tests at the lower temperature were nearly all made with 2]-f. lengths of rail, while those at the higher temperatures were made with short lengths, the supports in

every case being the same distance apart.

W. H. Barlow (Proc. Inst. C. E.) made experiments on bars of wrought iron, cast iron, malleable cast iron, Bessemer steel, and tool steel. The bars were tested with tensile and transverse strains, and also by impact; one half of them at a temperature of 50° F., and the other half at 5° F. The lower temperature was obtained by placing the bars in a freezing mixture, care being taken to keep the bars covered with it during the whole time of

the experiments.

The results of the experiments were summarized as follows:

1. When bars of wrought iron or steel were submitted to a tensile strain and broken, their strength was not affected by severe cold (5° F.), but their ductility was increased about 1% in iron and 3% in steel.

2. When bars of cast iron were submitted to a transverse strain at a low temperature, their strength was diminished about 3% and their flexibility

about 16%.

3. When bars of wrought iron, malleable cast iron, steel, and ordinary cast iron were subjected to impact at a temperature of 5° F., the force required to break them, and the extent of their flexibility, were reduced as follows, viz.:

	Reduction of Force of Impact, per cent.	Reduction of Flexi- bility, per cent.
Wrought iron, about Steel (best cast tool), about Malleable cast iron, about Cast iron, about		18 17 15 not taken

The experience of railways in Russia, Canada, and other countries where the winter is severe is that the breakages of rails and tires are far more numerous in the cold weather than in the summer. On this account a softer class of steel is employed in Russia for rails than is usual in more temperate climates.

The evidence extant in relation to this matter leaves no doubt that the capability of wrought iron or steel to resist impact is reduced by cold.

capability of wrought from or steet to resist impact is reduced by cold. On the other hand, its static strength is not impaired by low temperatures. **Effect of Low Temperatures on Strength of Railroad Axles.** (Thos. Andrews, Proc. Inst. C. E., 1891.—Axles 6 ft. 6 in, long between centres of journals, total length 7 ft. 3½ in., diameter at middle 4½ in., at wheel-sets 5½ in., journals 3¾ × 7 in. were tested by impact at temperatures of 0° and 100° F. Between the blows each axle was half turned over, and was also replaced for 15 minutes in the water-bath.

The mean force of concussion resulting from each impact was ascertained

as follows:

Let h = height of free fall in feet, w = weight of test ball, hw = W ="energy," or work in foot-tons, x = extent of deflections between bearings,

then 
$$F$$
 (mean force) =  $\frac{W}{x} = \frac{hw}{x}$ .

The results of these experiments show that whereas at a temperature of  $0^\circ$  F, a total average mean force of 179 tons was sufficient to cause the breaking of the axles, at a temperature of 100° F, a total average mean force of 438 tons was requisite to produce fracture. In other words, the resistance to concussion of the axles at a temperature of  $0^\circ$  F, was only about 43% of what it was at a temperature of  $100^\circ$  F.

The average total deflection at a temperature of 0° F, was 6,48 in., as against 15.06 in. with the axies at 100° F, inder the conditions stated; this represents an ultimate reduction of flexibility, under the test of impact, of about 57% for the cold axies at 0° F., compared with the warm axies at

100° F.

#### EXPANSION OF IRON AND STEEL BY HEAT.

James E. Howard, engineer in charge of the U.S. testing-machine at Watertown, Mass., gives the following results of tests made on bars 35 inches long (Iron Age, April 10, 1890):

		(	Chemic	al con	position.	Coefficient of Expansion.
Metal.	Marks.	c.	Mn.	Si.	Fe by difference.	Per degree F. per unit of length.
Wrought iron Steel	1a 2a 3a 4a 5a 6a 7a 8a 9a 10a	.09 .20 .31 .37 .51 .57 .71 .81 .89	.11 .45 .57 .70 .58 .93 .58 .56 .57 .80	.02 .07 .08 .17 .19 .28	99.80 99.85 99.12 98.93 98.89 98.43 98.63 98.76 98.35	.000067302 .000067361 .000006259 .0000065149 .000006597 .000006891 .0000084716 .000062167 .000062335 .000061700 .000062361 .000062361 .000062361

### DURABILITY OF IRON, CORROSION, ETC.

Durability of Cast Iron .- Frederick Graff, in an article on the Philadelphia water-supply, says that the first cast-iron pipe used there was laid in 1820. These pipes were made of charcoal iron, and were in constant use for 53 years. They were uncoated, and the inside was well filled with tubercles. In sait water good cast iron, even uncoated, will last for a certury at least; but it often becomes soft enough to be cut by a knife, as is shown in iron cannon taken up from the bottom of harbors after long submersion. Close-grained, hard white metal lasts the longest in sea water.— Enclo News, April 23, 1887, and March 26, 1892.

Tests of Iron after Forty Years' Service.—A square link 12 inches broad, 1 inch thick and about 12 feet long was taken from the Kieff

bridge, then 40 years old, and tested in comparison with a similar link which had been preserved in the stock-house since the bridge was built. The following is the record of a mean of four longitudinal test-pieces,  $1\times11/8\times8$  inches, taken from each link (Stahl und Eisen, 1890):

	Old Link taken from Bridge.	New Link from Store-house,
Tensile strength per square inch, tons	21.8	22.2
Elastic limit	11.1	11.9
Elongation, per cent		13.42 18.75

**Durability of Iron in Bridges.** (G. Lindenthal, *Eng'g*, May 2, 1881, p. 139.)—The Old Monongahela suspension bridge in Pittsburgh, built in 1815, was taken down in 1882. The wires of the cables were frequently strained to half of their ultimate strength, yet on testing them after 37 years'

use they showed a tensile strength of from 72,700 to 100,000 lbs. per square inch. The elastic limit was from 67,100 to 78,600 lbs, per square inch. duction at point of fracture, 35% to 75%. Their diameter was 0.13 inch.

A new ordinary telegraph wire of same gauge tested for comparison showed: T. S., of 100,000 lbs.; E. L., 81,550 lbs.; reduction, 57%. Iron rods used as stays or suspenders showed: T. S. 43,770 to 49,720 lbs. per square inch; E. L., 26,380 to 29,200. Mr. Lindenthal draws these conclusions from his tests:

"The above tests indicate that iron highly strained for a long number of years, but still within the elastic limit, and exposed to slight vibration, will

not deteriorate in quality.

"That if subjected to only one kind of strain it will not change its texture. even if strained beyond its elastic limit, for many years. It will stretch and behave much as in a testing-machine during a long test.

"That iron will change its texture only when exposed to alternate severe straining, as in bending in different directions. If the bending is slight but

very rapid, as in violent vibrations, the effect is the same."

Corrosion of Iron Bolts .- On bridges over the Thames in London, bolts exposed to the action of the atmosphere and rain-water were eaten away in 25 years from a diameter of % in. to 1/2 in., and from 5/4 in. diameter to 5/16 inch

Wire ropes exposed to drip in colliery shafts are very liable to corrosion. Corrosion of Iron and Steel.—Experiments made at the Riverside Iron Works, Wheeling, W. Va., on the comparative liability to rust of iron and soft Bessemer steel: A piece of iron plate and a similar piece of steel, both clean and bright, were placed in a mixture of yellow loam and sand, with which had been thoroughly incorporated some carbonate of soda, nitrate of soda, ammonium chloride, and chloride of magnesium. The earth as prepared was kept moist. At the end of 33 days the pieces of metal were taken out, cleaned, and weighed, when the iron was found to have lost 0.84% of its weight and the steel 0.72%. The pieces were replaced and after 28 days

of its weight and the steel U.73. The pieces were replaced and after 28 days weighed again, when the iron was found to have lost 2.00% of its original weight and the steel 1.79. (Eng's, June 26, 1891.)

Corrosive Agents in the Atmosphere.—The experiments of F. Crace Calvert (Chemical News, March 3, 1871) show that carbonic acid, in the presence of moisture, is the agent which determines the exidation of iron in the atmosphere. He subjected perfectly cleaned blades of iron and steel to the action of different gases for a period of four months, with

results as follows:

Dry oxygen, dry carbonic acid, a mixture of both gases, dry and damp oxygen and animonia: no oxidation. Damp oxygen: in three experiments

one blade only was slightly oxidized.

Damp carbonic acid: slight appearance of a white precipitate upon the iron, found to be carbonate of iron. Damp carbonic acid and oxygen: oxidation very rapid. Iron immersed in water containing carbonic acid oxidized rapidly.

Iron immersed in distilled water deprived of its gases by boiling rusted

the iron in spots that were found to contain impurities.

Galvanic action is a most active agent of corrosion. It takes place when two metals, one electro-negative to the other, are placed in contact

and exposed to dampness.

Sulphurous acid (the product of the combustion of the sulphur in coal) is an exceedingly active corrosive agent, especially when the exposed iron is coated with soot. This accounts for the rapid corrosion of iron in railway bridges exposed to the smoke from locomotives. (See account of experiments by the author on action of sulphurous acid in *Jour. Frank. Inst.*, June, 1875, p. 437.) An analysis of sooty iron rust from a railway bridge showed the presence of sulphurous, sulphuric, and carbonic acids, chlorine, and ammonia. Bloxam states that ammonia is formed from the nitrogen of the air during the process of rusting.

Rustless Coatings for Iron and Steel.—Tinning, enamelling, lacquering, galvanizing, electro-chemical painting, and other preservative methods are discussed in two important papers by M. P. Wood, in Trans.

A. S. M. E., vols. xv and xvi.

A Method of Producing an Inoxidizable Surface on iron and steel by means of electricity has been developed by M. A. de Meritens (Engineering.) The article to be protected is placed in a bath of ordinary or distilled water, at a temperature of from 15% to 176° F. and an electric current is sent through. The water is decomposed into its elements,

oxygen and hydrogen, and the oxygen is deposited on the metal, while the hydrogen appears at the other pole, which may either be the tank in which the operation is conducted or a plate of carbon or metal. The current has only sufficient electromotive force to overcome the resistance of the circuit and to decompose the water; for if it be stronger than this, the oxygen combines with the iron to produce a pulverulent oxide, which has no adherence. If the conditions are as they should be, it is only a few minutes after the oxygen appears at the metal before the darkening of the surface shows that the gas has united with the iron to form the magnetic oxide Fe<sub>3</sub>O<sub>4</sub>, which it is well known will resist the action of the air and protect the metal beneath it. After the action has continued an hour or two the coating is sufficiently solid to resist the scratch-brush, and it will then take a brilliant polish.

If a piece of thickly rusted iron be placed in the bath, its sesquioxide (Fe<sub>2</sub>O<sub>3</sub>) is rapidly transformed into the magnetic oxide. This outer layer has no adhesion, but beneath it there will be found a coating which is actually a part of the metal itself.

In the early experiments M. de Meritens employed pieces of steel only, but in wrought and cast iron he was not successful, for the coating came off with the slightest friction. He then placed the iron at the negative pol of the apparatus, after it had been already applied to the positive pole. Here the oxide was reduced, and hydrogen was accumulated in the pores of the metal. The specimens were then returned to the anode, when it was found that the oxide appeared quite readily and was very solid. But the result was not quite perfect, and it was not until the bath was filled with distilled water, in place of that from the public supply, that a perfectly satisfactory result was attained.

Mangauese Plating of Iron as a Protection from Rust.

—According to the Italian Progresso, articles of iron can be protected against rust by sinking them near the negative pole of an electric bath composed of 10 litres of water, 50 grammes of chloride of manganese, and 200 grammes of nitrate of ammonium. Under the influence of the current the bath deposits on the articles a film of metallic manganese which prevents

them from rusting.

A Non-oxidizing Process of Annealing is described by H. P. Jones, in *Engly News*, Jan. 2, 1892. The ordinary process of annealing, by means of which hard and brittle iron or steel is rendered soft and tough, by means of winch mard and officier from or steel is reduced soft and todgin, consists in heating the metal to a good red-heat and then allowing it to cool gradually. While the metal is in a heated condition the surface becomes oxidized, and although for many classes of work this scale of oxide is of practical importance, yet in some cases it is very undesirable and even necessitates considerable expense in its removal.

The new process uses a non-oxidizing gas, and is the invention of Mr. Horace K. Jones, of Hartford, Conn. The principal feature of this process consists in keeping the annealing-retort in communication with the gas holder or gas main during the entire process of heating and cooling, the gas thus being allowed to expand back into the main, and being, therefore,

kept at a practically constant pressure.

The retorts used are made from wrought-iron tubes. The gas used is taken directly from the mains supplying the city with illuminating gas. was noticed that if metal which had been blued or slightly oxidized was subjected to the annealing process it came out bright, the oxide being reduced by the action of the gas. Practical use has been made of this fact in deoxidizing metal.

Comparative tests were made of specimens of metal annealed in illuminating gas and of specimens annealed in nitrogen. The results of these tests were compared with the results of tests of specimens annealed in an open

were compared with the Island of specimens of the unannealed metal, and thus the relative efficiency of the gas process was determined. The specimens were made from steel wire .188 in. in diameter and were turned down to diameters of .156 and .150 in. Different lots of wire were tested in order to secure average results. The elongations were in each case referred to an original length of 1.15 ins.

The difference in total per cent of elongation and in breaking load between the specimens annealed in nitrogen and those annealed in illuminating gas

is very slight. The average results were as follows:

Lot.	g	No. Test	Breaking	Elongation.		
1100.	Gas used.		Load, lbs. per sq. in.	Total p. c.	p. c. gained.	
A	Nitrogen Illuminating Nitrogen Illuminating Nitrogen Illuminating Open fire Unannealed	4 4 4 4 5 5 8 5 5	62,140 63,140 60,000 60,400 57,330 57,070 63,090 97,120 80,790	29.12 28.08 28.00 27.20 30.88 29.60 26.76 7.12 8.80	22.00 20.86 19.20 18.40 23.76 22.48 19.64	

Painting Wood and Iron Structures. (E. H. Brown, Eng'rs Club of Phila, Engineering News, April 20, 1893.)—A paint consists of two portions—the pigment and the vehicle or binder. The pigment is a solid substance which is more or less finely ground, so as to be capable (when mixed with the vehicle) of being spread out in a thin layer or coating over the surface to be painted. The vehicle or binder is the liquid in which the pigment is mixed or ground, which serves to spread the pigment over the surface to be painted, and which also holds it to that surface. For ordinary painting the most generally used vehicle is linseed oil.

Linseed oil possesses the peculiar property of drying by uniting with the

Sorgen of the air to form a tough, leather-like compound called linoxin.

For painting on wood, zinc white has valuable pigment properties, but
these seem to be most fully developed when this pigment is used in conjunction with white lead, and then to the best advantage when the mixture is used as a final coat over an elastic undercoating of white lead. So far no other white base has been discovered which possesses at the same time the other properties which render white lead valuable, namely, covering and spreading capacity.

Of the inert pigments, lampblack is probably the most valuable. Being almost pure carbon, it is practically unchangeable except by fire. It has the peculiar property of absorbing great quantities of linseed oil, and hence of spreading over a large surface. French ochre, an earth pigment containing more or less of the hydrated oxide of iron, possesses the property of absorbing a large quantity of oil, and hence has considerable spreading capacity, and also holds very firmly to any wooden surface to which it may be applied

The various mineral and metallic paints are almost all natural or artificial iron oxides. While these are cheap and useful for painting rough wooden structures they are sometimes really quite dangerous for application to iron work, because, instead of preventing oxidation, they are apt to further it.

Coal tar is much used as a paint for the roughest class of work, both wood and iron; in the latter case especially for cast-iron pipes, smoke-stacks, and work to be buried underground. It has the nature both of a resin and an oil. It has the disadvantage of becoming exceedingly brittle by the action of cold, and softening at 115° F. Asphalt permits of somewhat wider range of temper-ature, but otherwise exhibits the same peculiarities. These substances, while they last, are probably the most valuable of paints, especially under water; but they are unfortunate in their tendency to flow or crawl on the surface to which they are applied, finally leaving the upper portions almost or quite bare. This is the case even under ground.

Red lead has long been regarded as the best possible preservative for clean But in order to be most effective, the iron must be perfectly clean and free from any suspicions of rust, and absolutely dry. Red lead should be perfectly pure and of the best and most careful preparation. any well-known corroding house may be depended upon for purity, but not all ways for quality. It is simply a red oxide of lead. The best ype is orange mineral, which is made by roasting white lead. On account of its expensible is not so frequently used as it would deserve. Red lead proper is made directly from the metal, which is first oxidized to the yellow litharge, and then to the red oxide. This, however, does not give as good a paint as that made from the scrap, settlings, and tailings of the white lead works. As red lead saponifies very quickly with linseed oil, it must be used within a few days after being ground, and, moreover, it is rather difficult to work.

Hence there is great temptation to add some substance, such as whiting, to it in order to make it work freer, as well as to cost less money for material.

Before painting iron work it is essential that the iron itself should be absolutely free from rust. Rust has the peculiar property of spreading and extending from a centre, if there be the slightest chance to do so. Hence, a small amount of rust on the iron may grow under the surface of the paint, especially if it be true, as Dr. Dudley asserts, that linsed oil is permeable by air and moisture, and in time the paint will be flaked off by the rust underneath, thus gradually exposing the bare surface of the front ot he action of its destroying agent, oxygen in the presence of water. It is necessary to remove all the scale possible from wrought iron by means of stiff wire brushes, and then to remove the rust by a pickle of very dilute acid, which must atterward be thoroughly washed off before the paint is applied. The surface of the iron should be dry and at least moderately warmed before it is primed. The best method of painting a tin roof is to carefully remove all traces of oil or grease from the surface of the tin while it is yet bright with benzine; then to apply a coat of red lead and linseed oil, or the best quality of metallic paint, and to follow this with one or two coats of graphite paint. The graphite is almost unchangeable by atmospheric action, and is remarkably waterproof as well.

Red Lead as a Preservative of Iron.—A. J. Whitney writes to Engineering News, August, 1891, that in 30 years' experience he has found

red lead to be the best material for preserving from under all circumstances.

Quantity of Paint Required for a Given Surface. (M. P. Wood.)—80, tt. of surface + 200 = gallons of liquid paint for two coats; sq. ft. of surface + 18 = lbs. of pure white lead for three coats.

Qualities of Paints. - The Railroad and Engineering Journal, vols. liv and ly, 1890 and 1891, has a series of articles on paint as applied to wooden structures, its chemical nature, application, adulteration, etc., by Dr. C. B. Dudley, chemist, and F. N. Pease, assistant chemist, of the Penna. R. R. They give the results of a long series of experiments on paint as applied to railway purposes.

Graphite Paint. (M. P. Wood.)-Graphite, mixed with pure boiled linseed oil in which a small percentage of litharge, red lead, manganese, or other metallic salt has been added at the time of boiling to aid in the oxidation of the oil, forms a most effective paint for metallic surfaces, as well as for wood and fibrous substances. Wood surfaces protected by this paint, and exposed to the action of sea-water for a number of years, are found in a perfect state of preservation.

## STEET.

# RELATION BETWEEN THE CHEMICAL COMPOSI-TION AND PHYSICAL CHARACTER OF STEEL,

W. R. Webster (see Trans. A. I. M. E., vols. xxi and xxii, 1893-4) gives results of several hundred analyses and tensile tests of basic Bessemer steel plates, and from a study of them draws conclusions as to the relation of chemical composition to strength, the chief of which are condensed as follows:

The indications are that a pure iron, without carbon, phosphorus, manganese, silicon, or sulphur, if it could be obtained, would have a tensile strength of 34,750 lbs. per square inch, if tested in a 3,4-inch plate. With this as a base, a table is constructed by adding the following hardening effects, as shown by increase of tensile strength, for the several elements named.

Carbon, a constant effect of 800 lbs. for each 0.01%. Sulphur, 500 0.01%

Phosphorus, the effect is higher in high-carbon than in low-carbon steels. With carbon hundreths \$..... 9 10 11 12 13 14 15 16 17 With carbon hundreths \$...... 9 10 11 12 13 14 15 16 17 Each .01\$\% P\$ has an effect of lbs. 900 1000 1100 1200 1300 1400 1500 1500 1500 Manganese, the effect decreases as the per cent of manganese increases.

.00 .15 .20 .25 .30 .35 .40 .45 .50 10 .65

390

Silicon is so low in this steel that its hardening effect has not been considered.

With the above additions for carbon and phosphorus the following table has been constructed (abridged from the original by Mr. Webster). To the figures given the additions for sulphur and manganese should be made as above.

#### Estimated Ultimate Strengths of Basic Bessemer Steel Plates,

For Carbon, .06 to .24; Phosphorus, .00 to .10; Manganese and Sulphur, .00 in

	an cases.										
Carb	on.	.06	.08	.10	.12	.14	.16	.18	.20	.22	.24
Phos	.005 .01 .02 .03 .04	40,350 41,150 41,950 42,750	41,550 41,950 42,750 43,550 44,350 45,150	44,750 45,750 46,750		47,350 48,750 50,150 51,550	49,050 50,550 52,050 58,550	50,650 52,150 53,650 55,150	52,250 53,750 55,250 56,750	53,850 55,350 56,850 58,350	54,700 55,450 56,950 58,450 59,950 61,450
" " " "	.06 .07 .08 .09 .10	44,350 45,150 45,950 46,750 47,550	45,950 46,750 47,550 48,350 49,150	48,750 49,750 50,750 51,750 52,750	51,550 52,750 53,950 55,150 56,350	54,350 55,750 57,150 58,550 59,950	56,550 58,050 59,550 61.050 62,550	58,150 59,650 61,150 62,650 64,150	59,750 61,250 62,750 64,250 65,750	61,350 62,850 64,350 65,850 67,350	62,950 64,450 65,950 67,450 68,950
.001 Ph	os =	80 lbs.	80 lbs.]	100 lb	1120 lb	{140 lb	1150 Ib	150 lb	150 lb	150 lb	150 lb

In all rolled steel the quality depends on the size of the bloom or ingot from which it is rolled, the work put on it, and the temperature at which it is finished, as well as the chemical composition.

The above table is based on tests of plates % inch thick and under 70 inches wide; for other plates Mr. Webster gives the following corrections for thickness and width. They are made necessary only by the effect of thickness and width on the finishing temperature in ordinary practice. Steel is frequently spoiled by being finished at too high a temperature.

### Corrections for Size of Plates.

			lates.	Up to 70 in	s. wide. Over 7	) ins. wide
		Inche	s thick.	Lbs	š.	Lbs.
	3/4					1000
1	1/16			— 17	750 •	<b>-</b> 750
	5/8					- 500
	9/16					- 250
	1/2			10	- 000	- 0
	7/16			:	500 ;	± 500
	3/8				0 -	+ 1000
	5/16	"		+ 30	000 -	+ 5000

Comparing the actual result of tests of 408 plates with the calculated results, Mr. Webster found the variation to range as in the table below.

### Summary of the Differences Between Calculated and Actual Results in 408 Tests of Plate Steel.

In the first three columns the effects of sulphur were not considered; in the last three columns the effect of sulphur was estimated at 500 lbs, for each .01% of S.

	Universal Mill.	Sheared.	Both Mills.	Universal Mill.	Sheared.	Both Mills.	Both Mills, Corrected for Thickness and Width.
Per cent within 1000 lbs	23.4	32.1	28.4	24.6	27.0	26.0	28.4
2000	40.9	48.9	45.6	48.5	54.9	52.2	
" " " 3000 "	62.5	71.3	67.6	67.8	73.0	70.8	74.7
" " 4000 "	75.5	81.0	78.7	82.5		84.1	89.9
" " 5000 "	89.5	91.1	90.4	93.0	92.8	92.9	94.9

The last figure in the table would indicate that if specifications were drawn calling for steel plates not to vary more than 5000 lbs, T. S. from a specified figure (equal to a total range of 10,000 lbs.), there would be a probability of the rejection of 55 of the blooms rolled, even if the whole lot was made from steel of identical chemical analysis. In 1000 heats only 2% of the heats failed to meet the requirements of the orders on which they were graded; the loss of plates was much less than 1%, as one plate was rolled from each heat and tested before rolling the remainder of the heat.

R. A. Hadfield (Jour. Iron & Steel Inst., No. 1, 1894) gives the strength of

K. A. Hadneld Gold. Flot & Steef Hist, No. 1, 1009) gives the steeling the very pure Swedish fron, remelted and tested as cast, 20. 1 toos (45,024 bs.) per sq. in; remelted and forged, 21 toos (47,040 bs.). The analysis of the cast bar was: (0,008; Si, 0,04; S. 0,02; P. 0,02; P. 0,00; Mn. 0,01; Fe, 99,82; Effect of Oxygen upon Strength of Steel,—A. Lantz, of the Peine works, Germany, in a letter to Mr. Webster, says: "We have found during the current year (1893) that oxygen plays an important rôle, till now little observed—such, indeed, that given a like content of carbon, phosphorus, and manganese in the blows, a blow with greater oxygen content gives a greater hardness and less ductility than a blow with less oxygen content." a greater narmiess and less outcomy man a blow with less oxygen content. The method used for determining oxygen is that of Prof. Ledebur, given in Stabl und Eisen, May, 1892, p. 193. The variation in oxygen content may make a difference in strength of nearly one-half ton per square inch. (Jour. Iron & Steel Inst., No. 1, 1894.)

# RANGE OF VARIATION IN STRENGTH OF BESSEMER AND OPEN-HEARTH STEELS.

The Carnegie Steel Co. in 1888 published a list of 1057 tests of Bessemer and open-hearth steel, from which the following figures are selected:

Kind of Steel.	Tests.	Elastic	e Limit.	Ultir Stre	nate ngth.	Elong per 4 in 8 in	cent
	No. of	High't.	Lowest	High't.	Lowest	High't.	Lowest
(c) Bess. angles (d) O. H. fire-box (e) Tank (f) O. H. bridge	170 72 25 19 20	46,570 47,690 41,890	39,230 39,970 32,630	71,300 73,540 63,450 62,790 66,062 69,940	61,450 65,200 56,130 50,350 59,440 63,970	33.00 30.25 34.30 36.00 27.50 30.00	28.75 28.15 26.25 25.62 19.25 22.75

REQUIREMENTS OF SPECIFICATIONS

(a) Elastic limit, 35,000; tensile strength, 62,000 to 70,000; elong, 22% in 8 in. (b) Elastic limit, 40,000; tensile strength, 67,000 to 70,000; elong, 22% in 8 in. (c) Elastic limit, 30,000; tensile strength, 67,000 to 64,000; elong, 20% in 8 in. (d) Tensile strength, 50,000 to 62,000; elong, 20% in 4 in. (e) Tensile strength, 50,000 to 63,000; elong, 15% in 8 in.

Strength of Open-hearth Structural Steel, (Pencoyd Iron Strength of Open-hearth Structural Steel, (Pencoyd I Works.)—As a general rule, the percentage of carbon in steel determines its hardness and strength. The higher the carbon the harder the steel, the higher the tenacity, and the lower the ductility will be. The following list exhibits the average physical properties of good open-hearth steel:

Percentage of Carbon.	Ultimate Tenacity, lbs. per sq. in.	Elastic Limit, lbs. per sq. in.	Stretch in 8 inches,	Reduction of Area, %.
.10	57.000	34,000	28 per cent.	55 per cent.
.15	62,000 67,000	37,000 40,000	26 "	45 "
.25 .30	72,000 77,000	43,000 46,000	22 "	40 " 35 "
.35	82,000 87,000	49,000 52,000	18 "	30 "

The coefficient of elasticity is practically uniform for all grades, and is the same as for iron, viz., 29,000,000 lbs. These figures form the average of a numerous series of tests from rolled bars, and can only serve as an ap399

proximation in single instances, when the variation from the average may be considerable. Steel below 10 carbon should be capable of doubling flat without fracture, after being chilled from a red heat in cold water. Steel of .15 carbon will occasionally submit to the same treatment, but will usually bend around a curve whose radius is equal to the thickness of the specimen; about 995 of specimens stand the later bending test without fracture. As the steel becomes harder its ability to endure this bending test becomes more exceptional, and when the carbon ratio becomes .20, little over 25% of specimens will stand the last-described bending test. Steel having about .405 carbon will usually harden sufficiently to cut soft iron and maintain an edge.

Mehrtens gives the following tables in Stahl und Eisen (Iron Age, April 20,

Basic Bessemer Steel.	Basic Open-hearth Struc-
680 Charges.	tural Steel.
Floatic Limit Charges within	489 Charges.
Elastic Limit, pounds per Range, per cent sq. in. 35.500 to 28,400. 15.0	Elastic Limit, pounds per sq. in. 34,400 to 37,000
sa in of total number	pounds per Range, per cent
25 500 to 28 400	sq. in. of total charges
38,400 to 39,800	34,400 to 37,000
39,800 to 41,200 27.5	37,000 to 38,400 15.6
41,200 to 42,700	38,400 to 39,800 20.3
42,700 to 46,400 9.9	39,800 to 41,200
	41,200 to 42,700
Tensile Strength, Charges within	42,700 to 44,100
pounds per Range, per cent	44,100 to 48,400 8.5
sq. in of total number.	Tensile Strength.
55,600 to 56,900	.55,800 to 56,900 8.0
56,900 to 58,300	56,900 to 58,300
58,300 to 59,700	58,300 to 59,700
59,700 to 61,200	59,700 to 61,200 19.6
61,200 to 62,300	61,200 to 62,600
STRUCTURAL STEEL,	62,600 to 65,100 9.04
	Elongation,
Elongation. Charges within Range, per cent of total number.	per cent.
Elongation. Range, per cent	20 to 25 21.7
21 to 25 2.65	25 to 26
	26 to 27
25 to 26 8.53	27 to 28 11.0
26 to 27	28 to 29 12.0
27 to 28	29 to 30
29 to 30	30 to 37.1 24.3
30 to 32.5 6.62	RIVET STEEL, 19 CHARGES.
50 10 52.5 0.02	Tensile Strength.
RIVET STEEL.	51.800
25,2 to 26 20.0	51,900 to 53,300
26 to 27 15.0	53,300 to 54,900 21.0
27 to 28 25.0	54,900 to 56,300
28 to 29	56,300 to 56,900
29 to 29,8 15.0	Elongation all above 25 per cent.

In the basic Bessemer steel over 90% was below 0.8 phosphorus, and all were below 0.10; manganese was below 0.6 in over 90% and below 0.9 in all; sulphur was below 0.05 in 81%, the maximum being 0.07; carbon was below 0.10, and silicon below 0.01 in all. In the basic open-hearth steel phosphorus was below 0.06 in 96%, the maximum being 0.08; manganese below 0.07 in 88%, the maximum being 0.12. The carbon ranged from 0.09 to 0.14.

Low Tensile Strength of Very Pure Steel.—Swedish nail-rod open-hearth steel, tested by the author in 1881, showed a tensile strength of only 42,591 lbs. per sq. in. A piece of American nail-rod steel showed 45,021 lbs. per sq. in. Both steels contained about .10 carbon and .015 phosphorus, and were very low in sulphun, manganese, and silicon. The pieces tested

were bars about 2 × ¾ in. section.

Low Strength Due to Insufficient Work. (A. E. Hunt, Trans. A. I. M. E., 1883.)—Soft steel ingots, made in the ordinary way for boiler plates, have only from 10,000 to 20,000 lbs. tensile strength per sq. in., an elongation of only about 10% in 8 in., and a reduction of area of less than 20%. Such ingots, properly heated and rolled down from 10 in. to ½ in.

thickness, will give from 55,000 to 65,000 lbs. tensile strength, an elongation in 8 in, of from 23% to 33%, and a reduction of area of from 55% to 70%. Any work stopping short of the above reduction in thickness ordinarily yields intermediate results in its tensile tests.

Hardening of Soft Steel .- A. E. Hunt (Trans. A. I. M. E., 1883, vol. xii), says that soft steel, no matter how low in carbon, will harden to a cer-

hair says that the says the says that the says that the says that the says the say manganese, which gave the following results upon test-pieces from the same 1/4 in, thick plate.

	Maximum	Elongation	Reduction
	Load.	in 8 in.	of Area.
	lbs. per sq. in.	Per cent.	Per cent.
Unhardened	. 55,000	27	62
Hardened in water		25	50
Hardened in brine	. 84,000	22	43
Hardened in oil	67,700	26	49

While the ductility of such hardened steel does not decrease to the extent that the increased tenacity would indicate, and is much superior to that of normal steel of the high tenacity, still the greatly increased tenacity after hardening indicates that there must be a considerable molecular change in the steel thus hardened, and that if such a hardening should be created locally in a steel plate, there must be very dangerous internal strains caused thereby

Effect of Cold Rolling .- Cold rolling of iron and steel increases the elastic limit and the ultimate strength, and decreases the ductility. Major Wade's experiments on bars rolled and polished cold by Lauth's process showed an average increase of load required to give a slight permanent set showed an average increase of load required to give a slight permanent set as follows: Transverse, [6%; toxion, 130%; compression, 161% on short columns 1½ in, long, and 64% on columns 8 in, long; tension, 95%. The hardness, as measured by the weight required to produce equal indentations, was increased 50%; and it was found that the hardness was as great in the centre of the bars as elsewhere. Sir W. Fairbairn's experiments showed an increase in ultimate tensile strength of 50%, and a reduction in the elongation in 50 in, of from 2 in, or 20%; to .79 in, or 7.9%.

Comparison of Tests of Full-size Eye-bars and Sample Test-pieces of Same Steel Used in the Memphis Bridge. (Geo. S. Morison, Trans. A. C. E., 1893.)

Sectio		Sized Ey ide × 1 t	ebars, o 2 3/16"	Sample Bars from Same Melts, about 1 in. area.					
Reduc-	Elong	ation.	Elastic Limit,	Max. Load.	Reduc-	Elon-	Elastic	Max. Load,	
tion of Area, p.c.	Inches.	p.c.	lbs. per	, ·	p. c.	gation, p. c.	Limit, lbs. per	,	
39.6	20.2	16.8	35,100	67,490	47.5	27.5	41,580	78,050	
39.7	26.6	8.2	37,680	70,160	52.6	24.4	42,650	75,620	
44.4	36.8	11.8	39,700	65,500	47.9	28.8	40,280	70,280	
38.5	38.5	17.3	33,140	65,060	47.5	27.5	41,580	73,050	
40.0	32.5	13.5	32,860	65,600	44.5	20.0	43,750	75,000	
39.4	36.8	15.3	31,110	61,060	42.7	28.8	42,210	69,730	
34.6	32.9	13.7	33,990	63,220	52.2	28.1	40,230	69,720	
32.6	13.0	13.5	29,330	63,100	48.3	28.8	38,090	71,300	
7.3	20 8	6.9	28,080	55,160	43.2	24.2	38,320	70,220	
38.1	28.9	14.1	29,670	62,140	59.6	26.3	40,200	71,080	
31.8	24.0	11.8	32,700	65,400	40.3	25.0	39,360	69,360	
48.6	39.4	19.3	30,500	58,870	40.3	25.0	40,910	70,360	
10.3	11.8	12.3	33,360	73,550	51.5	25.5	40,410	69,900	
44.6	32.0	15.7	32,520	60,710	43.6	27.0	40,400	70,490	
46.0	35.8	14.9	28,000	58,720	44.4	29.5	40,000	66,800	
41.8	23.5	13.1	32,290	62,270	42.8	21.3	40,530	72,240	
41 2	47 1	15 1	29.970	58.680	45 7	27 0	40 610	70 480	

The average strength of the full-sized eye-bars was about 8000 lbs. per sq. in., or about 12% less than that of the sample test-pieces,

#### TREATMENT OF STRUCTURAL STEEL.

(James Christie, Trans. A. S. C. E., 1893.)

Effect of Punching and Shearing.—There is no doubt that steel of higher tensile strength than is now accepted for structural purposes should not be punched or sheared, or that the softer material may contain elements prejudicial to its use however treated, but especially if punched. But extensive evidence is on record indicating that steel of good quality, in bars of moderate thickness and below or not much exceeding 80,000 lbs, tensile strength, is not any more, and frequently not as much, injured as wrought iron by the process of punching or shearing.

The physical effects of punching and shearing as denoted by tensile test

are for iron or steel:

Reduction of ductility; elevation of tensile strength at elastic limit; reduc-

tion of ultimate tensile strength.

In very thin material the superficial disturbance described is less than in thick; in fact, a degree of thinness is reached where this disturbance prac-On the contrary, as thickness is increased the injury tically ceases. becomes more evident.

The effects described do not invariably ensue; for unknown reasons there are sometimes marked deviations from what seems to be a general result.

By thoroughly annealing sheared or punched steels the ductility is to a large extent restored and the exaggerated elastic limit reduced, the change

being modified by the temperature of reheating and the method of cooling.

It is probable that the best results combined with least expenditure can It is probable that the next results combined with least expenditure can be obtained by punching all holes where vital strains are not transferred by the rivets; and by reaming for important joints where strains on riveted joints are vital, or wherever perforation may reduce sections to a minimum. The reaming should be sufficient to thoroughly remove the material disturbed by punching; to accomplish this it is best to enlarge punched holes at least 1/2 in diameter with the reamer.

Riveting.—It is the current practice to perforate holes 1/16 in. larger than the rivet diameter. For work to be reamed it is also a usual requirement to punch the holes from 1/8 to 3/16 in. less than the finished diameter, the holes being reamed to the proper size after the various parts are

assembled.

It is also excellent practice to remove the sharp corner at both ends of the reamed holes, so that a fillet will be formed at the junction of the body and head of the finished rivets.

The rivets of either iron or mild steel should be heated to a bright red or yellow heat and subjected to a pressure of not less than 50 tons per square

inch of sectional area.

For rivets of ordinary length this pressure has been found sufficient to completely fill the hole. If, however, the holes and the rivets are exceptionally long, a greater pressure and a slower movement of the closing tool than is used for shorter rivets has been found advantageous in compelling the more sluggish flow of the metal throughout the longer hole.

Welding. No welding should be allowed on any steel that enters into structures

Upsetting. - Enlarged ends on tension bars for screw-threads, eyebars, etc., are formed by upsetting the material. With proper treatment and a sufficient increment of enlarged sectional area over the body of the bar the result is entirely satisfactory. The upsetting process should be performed so that the properly heated metal is compelled to flow without folding or lapping.

Annealing.—The object of annealing structural steel is for the purpose of securing homogeneity of structure that is supposed to be impaired by unequal heating, or by the manipulation necessarily attendant on certain processes. The objects to be annealed should be heated throughout to a uniform temperature and uniformly cooled.

The physical effects of annealing as indicated by tensile tests, depend on the grade of steel, or the amount of hardening elements associated with it; also on the temperature to which the steel is raised, and the method or rate

of cooling the heated material.

The physical effects of annealing medium-grade steel, as indicated by tensile test, are reported very differently by different observers, some claiming directly opposite results from others. It is evident, when all the attendant conditions are considered, that the obtained results must vary both in kind and degree.

The temperatures employed will vary from 1000° to 1500° F.; possibly even a wider range is used. In some cases the heated steel is withdrawn at full temperature from the furnace and allowed to cool in the atmosphere; in others the mass is removed from the furnace, but covered under a muffle, to lessen the free radiation; or, again, the charge is retained in the furnace, and the whole mass cooled with the furnace, and more slowly than by either of the other methods.

The best general results from annealing will probably be obtained by introducing the material into a uniformly-heated oven in which the temperatroughing the material into a unfortuny-neated over in which the temperature is not so high as to cause a possibility of cracking by sudden and unequal changing of temperature, then gradually raising the temperature of the material until it is uniformly about 190° F., then withdrawing the material after the temperature is somewhat reduced and cooling under shelter of a muffle, sufficiently to prevent too free and unequal cooling on

the one hand or excessively slow cooling on the other.

G. G. Mehrtens, Trans. A. S. C. E. 1893, says: "A good mild steel can be worked as readily as wrought iron in the shop or the field, and even bear still harder treatment. It was, however, often thought necessary to require preliminary annealing to remove the initial strains due to rolling. The anhealing is undoubtedly of great advantage to all steel above 64,000 hs. strength sugare inch, but it is questionable whether it is necessary in softer steels. The distortions due to heating cause trouble in subsequent straightening, especially of thin plates. It cannot be denied, however, that

annealing produces greater toughness.

"In a general way all unannealed mild steel for a strength of 56,000 to 64.000 lbs. may be worked in the same way as wrought iron. Rough treatment or working at a blue heat must, however, be prohibited. Such treat ment cannot be borne by wrought iron, although it does not suffer so much as soft steel. Shearing is to be avoided, except to prepare rough plates, which should afterwards be smoothed by machine tools or files before using. britting is also to be avoided, because the edges of holes are thereby strained beyond the yield point. Reaming drilled holes is not necessary, particularly when sharp drills are used and neat work is done. A slight countersinking of the edges of drilled holes is all that is necessary. Working the material while heated should be avoided as far as possible, and the engineer should bear this in mind when designing structures. Upsetting, cranking, and bending ought to be avoided, but when necessary the material should be annealed after completion:

"The riveting of a mild-steel rivet should be finished as quickly as possible. before it cools to the dangerous heat. For this reason machine work is the best. There is a special advantage in machine work from the fact that the pressure can be retained upon the rivet until it has cooled sufficiently to prevent elongation and the consequent loosening of the rivet."

Punching and Drilling of Steel Plates. (Proc. Inst. M. E., Aug. 188; p. 326.—In Prof. Unwin's report the results of the greater num-ber of the experiments made on iron and steel plates lead to the general conclusion that, while thin plates, even of steel, do not suffer very much from punching, yet in those of 1/2 in. thickness and upwards the loss of tenacity due to punching ranges from 10% to 23% in iron plates and from 11% to 33% in the case of mild steel. Mr. Parker found the loss of tenacity in steel plates to be as high as fully one third of the original strength of the plate. In drilled plates, on the contrary, there is no appreciable loss of strength. It is even possible to remove the bad effects of punching by subsequent reaming or annealing.

Working Steel at a Blue Heat.—Not only are wrought iron and

steel much more brittle at a blue heat (i.e., the heat that would produce an oxide coating ranging from light straw to blue on bright steel, 430° to 600° F.), but while they are probably not seriously affected by simple exposure to bineness, even if prolonged, yet if they be worked in this range of temperature they remain extremely brittle after cooling, and may indeed be more brittle than when at blueness; this last point, however, is not certain. (Howe,

"Metallurgy of Steel," p. 534.)

Tests by Prof. Krohn, for the German State Railways, show that working at blue heat has a decided influence on all materials tested, the injury done being greater on wrought iron and harder steel than on the softer steel. The fact that wrought iron is injured by working at a blue heat was reported by Stromeyer. (Engineering News. Jan. 9, 1892.)

A practice among boiler-makers for guarding against failures due to working at a blue heat consists in the cessation of work as soon as a plate which had been red-hot becomes so cool that the mark produced by rubbing a hammer-handle or other piece of wood will not glow. A plate which is not harmmer-harmer or other piece of wood will not glow. A place which is hot enough to produce this effect, yet too hot to be touched by the hand, is most probably blue-hot, and should under no circumstances be hammered or bent. (C. E. Stromeyer, Proc. Inst C. E. 1886.)

or bent. (C. E. Stromever, Proc. Inst C. E. 1886.)

Welding of Steel.—A. E. Hunt (A. I. M. E., 1892) says; I have never seen so-called "welded "pieces of steel pulled apart in a testing-machine or otherwise broken at the joint which have not shown a smooth cleavage plane, as it were, such as in iron would be condemned as an imperfect weld. My experience in this matter leads me to agree with the position taken by Mr. William Metcalf in his paper upon Steel in the Trans. A. S. C. E., vol. xvil., p. 301. Mr. Metcalf says, "I do not believe steel can be welded."

#### INFLUENCE OF ANNEALING UPON MAGNETIC CAPACITY.

Prof. D. E. Hughes (Eng'g, Feb. 8, 1884, p. 130) has invented a "Magnetic Balance," for testing the condition of iron and steel, which consists chiefly of a delicate magnetic needle suspended over a graduated circular index, and a magnet coil for magnetizing the bar to be tested. He finds that the following laws hold with every variety of iron and steel ;

1. The magnetic capacity is directly proportional to the softness, or mo-

lecular freedom.

2. The resistance to a feeble external magnetizing force is directly as the

hardness, or molecular rigidity.

The magnetic balance shows that annealing not only produces softness in iron, and consequent molecular freedom, but it entirely frees it from all strains previously introduced by drawing or hammering. Thus a bar of iron drawn or hammered has a peculiar structure, say a fibrous one, which gives a greater mechanical strength in one direction than another. This bar, if thoroughly annealed at high temperatures, becomes homogeneous in all directions, and has no longer even traces of its previous strains, provided that there has been no actual mechanical separation into a distinct series of fibres.

Effect of Annealing upon the Magnetic Capacity of Different Wires; Tests by the Magnetic Balance.

Description.	Magnetic Capacity.		
pescription.	Bright as sent.	Annealed.	
Best Swedish charcoal iron, first variety.	deg. on scale.	deg. on scale.	
" " second "	236	510	
" " third "	275	503	
Swedish Siemens-Martin iron	165	430	
Puddled iron, best best	212	340	
Bessemer steel, soft	150	291	
" " hard	115	172	
Crucible fine cast steel	50	84	

Crucible Fine Steel, Tempered.	Magnetic Capacity.
Bright-yellow heat, cooled completely in cold water Yellow-red heat, cooled completely in cold water	28 32 33
renow-red hear, cooled completely in cold water	32
Bright yellow, let down in cold water to straw color	33
	43
" cooled completely in oil	51
" cooled completely in oil let down in water to white.	51 58
Debest seeld committee in mater	
Reheat, cooled completely in water	66
" " oil	72
Annealed, " " oil	84

#### SPECIFICATIONS FOR STEEL.

Structural Steel. - There has been a change during the ten years from 1880 to 1890, in the opinions of engineers, as to the requirements in specifications for structural steel, in the direction of a preference for metal of low tensile strength and great ductility. The following specifications of different dates are given by A. E. Hunt and G. H. Clapp, Trans. A. I. M. E. 1890, xix. 926:

TENSION MEMBERS.	1879.	1881.	1882.	1885.	1887.	1888.
Elastic limit						38,000
Tensile strength			70,000	70,000		
Elongation in 8 in			18%	18%		22%
Reduction area			45%	42%		45%
Kind of steel	O.H.	O.H. or B.	О.Н.	Not	O.H. or B.	O.H.or B.
				spec.		

COMPTENSION PREMIUM	, ,				
Elastic limit		50@55,000	50,000	50,000	Same as tension
Tensile strength		80@90,000	80,000	80,000	members.
Elongation in 8 in	ten-	12%	15%	15%	**
Reduction area	sion.	20%	35%	35%	"
Elongation in 8 in	ten-	12%	15%	15%	**

F. H. Lewis (Iron Age, Nov. 3, 1892) says; Regarding steel to be used under the same conditions as wrought iron, that is, to be punched without reaming, there seems to be a decided opinion (and a growing one) among engineers, that it is not safe to use steel in this way, when the ultimate tensile strength is above 65,000 lbs. The reason for this is, not so much because there is any marked change in the material of this grade, but because all steel, especially Bessemer steel, has a tendency to segregations of carbon and phosphorus, producing places in the metal which are harder than they normally should be. As long as the percentages of carbon and phosphorus are kept low, the effect of these segregations is inconsiderable; but when these percentages are increased, the existence of these hard spots in the metal becomes more marked, and it is therefore less adapted to the treatment to which wrought iron is subjected.

There is a wide consensus of opinion that at an ultimate of 64,000 to 65,000 lbs, the percentages of carbon and phosphorus (which are the two hardening elements) reach a point where the steel has a tendency to become tender,

and to crack when subjected to rough treatment.

A grade of steel, therefore, running in ultimate strength from 54,000 to 62,000 lbs., or in some cases to 64,000 lbs., is now generally considered a proper material for this class of work.

Millard Hunsicker, engineer of tests of Carnegie, Phipps & Co., writes as

follows concerning grades of structural steel (Eng'g News, June 2, 1892): Grade of Steel.—Steel shall be of three grades—soft, medium, high. Soft Steel.—Specimens from finished material for test, cut to size speci-

fied above, shall have an ultimate strength of from 54,000 to 62,000 lbs, per sq. in.; elastic limit one half the ultimate strength; minimum elongation of 26% in 8 in.; minimum reduction of area at fracture 50%. This grade of steel to bend cold 180° flat on itself, without sign of fracture on the outside of the bent portion.

Medium Steel.—Specimens from finished material for test, cut to size specified above, shall have an ultimate strength of 60,000 to 68,000 lbs. per specimed above, shan lawe an dollmare strength; minimum elongation 20% in \$\circ\$ least is limit one half the ultimate strength; minimum elongation 20% in \$\circ\$ in; minimum reduction of area at fracture, 40%. This grade of steel to bend cold 180° to a diameter equal to the thickness of the piece tested,

without crack or flaw on the outside of the bent portion.

High Steel.—Specimens from finished material for test, cut to size specified above, shall have an ultimate strength of 66 000 to 74,000 lbs. per sq. in ; elastic limit one half the ultimate strength; minimum elongation, 18% in 8 in.; minimum reduction of area at fracture, 35%. This grade of steel to bend cold 180° to a diameter equal to three times the thickness of the test-piece, without crack or flaw on the outside of the bent portion.

F. H. Lewis, Engineers' Club of Phila., 1891, gives specifications for structural steel as follows: The phosphorus in acid open-hearth steel must be less than 0.10%, and in all Bessemer or basic steel must be less than 0.08%

The material will be tested in specimens of at least one half square inch section, cut from the finished material. Each melt of steel will be tested and each section rolled, and also widely differing gauges of the same section.

Requirements.	Soft Steel.	Medium Steel.
Elastic limit, lbs. per sq. in., at least	54,000 to 62,000	35,000 60,000 to 70,000
Elongation in 8 in., at least	25% 45%	20% 40%

In soft steel for web-plates over 36 in, wide the elongation will be reduced to 20% and the reduction of area to 40%.

It must bend cold 180 degrees and close down on itself without cracking

on the outside.

%-inch holes pitched % inch from a roll-finished or machined edge and 2 inches between centres must not crack the metal; and 1/8-inch holes pitched 11/4 inches between centres and 11/4 inches from the edge must not split the metal between the holes.

Medium steel must bend 180 degrees on itself around a 11/2-inch round bar.

Full-sized eye-bars, when tested to destruction, must show an ultimate strength of at least 56,000 lbs, and stretch at least 10% in a length of 10 feet. A. E. Hunt, in discussing Mr. Lewis's specifications, advises a requirement as to the character of the fracture of tensile tests being entirely silky in sections of less than 7 square inches, and in larger sections the test specimen not to contain over 25% crystalline or granular fracture. He also advises the drifting test as a requirement of both soft and medium steel; the requirement being worded about as follows: "Steel to be capable of having a hole, punched for a ¾' rivet, enlarged by blows of a sledge upon a drift-pin until the hole (which in the first case should be punched 1½' from the rollfinish or machined edge) is 11/4" diameter in the case of soft steel, and 11/4" diameter in the case of medium steel, without fracture." This drifting test is an excellent requirement, not only as a matter of record, but as a measure of the ductility of the steel.

H. H. Campbell, Trans. A. I. M. E. 1893, says: In adhering to the safest

course, engineers are continually calling for a metal with lower phosphorus. The limit has been 0.10%; it is now 0.08%; soon it will be 0.06%; it should be

0.04%.

A. E. Hunt, Trans. A. I. M. E. 1892, says: Why should the tests for steel be so much more rigid than for iron destined for the same purpose? Some of the reasons are as follows: Experience shows that the acceptable qualities of one melt of steel offer no absolute guarantee that the next melt to it, even though made of the same stock, will be equally satisfactory.

Again, good wrought iron, in plates and angles, has a narrow range (from 25,000 to 27,000 lbs.) in elastic limit per square inch, and a tensile strength of from 46,000 to 52,000 lbs. per square inch, whereas for steel the range in elastic limit is from 27,000 to 80,000 lbs., and in tensile strength from 48,000 to 120,000 lbs. per square inch, with corresponding variations in ductility. Moreover, steel is much more susceptible than wrought iron to widely varying effects of treatment, by hardening, cold rolling, or overheating.

It is now almost universally recognized that soft steel, if properly made and of good quality, is for many purposes a safe and satisfactory substitute for wrought iron, being capable of standing the same shop-treatment as wrought iron. But the conviction is equally general, that poor steel, or an unsuitable grade of steel, is a very dangerous substitute for wrought iron

even under the same unit strains.

For this reason it is advisable to make more rigid requirements in selecting material which may range between the brittleness of glass and a duc-

tility greater than that of wrought iron

Specifications for Steel for the World's Fair Buildings, Chicago, 1892.—No steel shall contain more than .08% of phosphorus. From three separate ingots of each cast a round sample bar, not less than 34 in. in diameter, and having a length not less than twelve diameters be-tween jaws of testing machine, shall be furnished and tested by the manufacturer. From these test-pieces alone the quality of the material in the steel works shall be determined as follows;

All the test-bars must have a tensile strength of from 60,000 to 68,000 lbs. per square inch, an elastic limit of not less than half the tensile strength of the test-bar, an elongation of not less than 24%, and a reduction of area of not less than 40% at the point of fracture. In determining the ductility, the elongation shall be measured after breaking on an original length of ten times

the shortest dimension of the test-piece

Rivet steel shall have a tensile strength of from 52,000 to 58,000 lbs. per square inch, and an elastic limit, elongation, and reduction of area at the point of fracture as stated above for test-bars, and be capable of bending double flat, without sign of fracture on the convex surface of the bend.

Boiler, Ship, and Tank Plates. W. F. Mattes (Iron Age, July 9, 1823) recommends that the different qualities of steel plates be classified as follows :

Fire-box.
55,000 to 60,000
25
Flat. Flat.
0.045 0.05 Rigid,
F (

A steel-manufacturing firm in Pittsburgh advertises six different grades of steel as follows:

Fire-box. Tank. Extra fire-box. Extra flange. Flange. Shell. The probable average phosphorus content in these grades is, respectively: .03 .02 0.6 .10. .04

Different specifications for steel plates are the following (1889):

United States Navy.—Shell: Tensile strength, 58,000 to 67,000 lbs. per sq. in.; elongation, 22% in 8-in. transverse section, 25% in 8-in. longitudinal section. Telagre: Tensile strength, 50,000 to 58,000 lbs.; elongation, 36% in 8 inches. Chemical requirements: P. not over .03%; S. not over .040%. Cold-bending test: Specimen to stand being bent flat on itself.

Cold-bending test: Specimen to stand being bent flat on itself. Quenching test: Steel heated to cherry-red, plunged in water 82° F., and to be bent around curve 1½ times thickness of the plate. British Admiratly.—Tensile strength, 58,240 to 67,200 lbs.; elongation in 8 in., 20%; same cold-bending and quenching tests as U. S. Navy. American Boiler-makers' Association.—Tensile strength, 55,000 to 65,000 lbs.; elongation in 8 in., 20% for plates ¾ in. thick and under; 22% for plates ¾ in. to in; 23% for plates ¾ in. thick and under; specimen must bend back on itself without fracture; for plates over ¼ in. thick, specimen must withstand bending 180° around a mandril, 1½ times the thickness of the plate.

plate.

Chemical requirements: P. not over .040%; S. not over .030%.

\*American Shipmasters' Association.—Tensile strength, 62,000 to 72,000

lbs.; elongation, 16% on pieces 9 in. long.

Strips cut from plates, heated to a low red and cooled in water the temperature of which is 82° F., to undergo without crack or fracture being doubled over a curve the diameter of which does not exceed three times the thickness of the piece tested.

Boiler Shell-plates, Front Tube-plate, and Butt-strips. (Penna, R. R., 1892.)—The metal desired is a homogeneous steel having a tensile strength of 60,000 lbs. per sq. in., and an elongation of 25% in a section originally 8 in. long. These plates will not be accepted if the testpiece shows

1. A tensile strength of less than 55,000 lbs. per sq. in.; 2. An elongation in section originally 8 in. long less than 20%; 3. A tensile strength over 65,000 lbs, per sq. in.; should however, the elongation be 27% or over, plates will not be rejected for high strength.

Inside Fire-box Plates, including Back Tube-plate.

(Penna. R. R., 1892.)—The metal should show a tensile strength of 60,000 lbs. per sq. in., and an elongation of 28% in a test section originally 8 in. long.

Chemical Composition,	Desired.	Will be Rejected.
Carbon	. 0.18 per cent.	over 0.25, below 0.15
Phosphorus, not above	. 0.03 "	over 0.01
Manganese, not above	. 0.40 "	over 0.55
Silicon, not above	. 0.02 "	over 0.04
Sulphur, not above		over 0 05
Copper not above	0.03 "	over 0.05

These plates will not be accepted if the test-piece shows: 1. A tensile strength of less than 55,000 lbs. per sq. in.; 2, An elongation in section originally 8 in. long, less than 22% (30% in plates 14 inch thick); 3. A tensile strength over 65,000 lbs. per sq. in. (68,000 for plates 14 in. thick); should, however, the elongation be 30% or over, plates will not be rejected for high strength: 4. Any single seam or cavity more than 1/4 in, long in either of the

three fractures obtained on test for homogeneity, as described below.

Homogeneity test: A portion of the test-piece is nicked with a chisel, or Homogeneity test: A portion of the test-piece is nicked with a chisel, or grooved on a machine, transversely about a sixteenth of an inch deep, in three places about 1½ in. apart. The first groove should be made on one side, 1½ in. from the square end of the piece; the second, 1½ in. from the opposite side; and the third, 1½ in. from the last, and on the opposite side from it. The test-piece is then put in a vise, with the first groove about ½ in, above the jaw, care being taken to hold it firmly. The projecting end of the test-piece is then broken off by means of a haumer, a number of light blows being used, and the bending being away from the groove. The piece is broken at the other two grooves in the same way. The object of this treatment is to open and render visible to the eye any seams due to failure to weld up, or to foreign interposed matter, or actities due to gas bubbles in the higot. After rupture, one side of each fracture is examined, a pocket lens being used if necessary, and the length of the seams and cavities is determined. The length of the blongest seam or

cavity determines the acceptance or rejection of the plate.

Dudley, chemist of the Penna, R. R. (Trans, A. I. M. E. 1892, vol. xx. p. 709), gives as an example of the progressive improvement in specification the following: In the early days of steel bollers the specification in force called for steel of not less than 50,000 lbs. tensile strength and not less than 25% elongation. Some metal was received having 75,000 lbs, tensile strength, and as the elongation was all right it was accepted; but when those plates were being flanged in the boiler-shop they cracked and went to As a result, an upper limit of 65,000 lbs, tensile strength was pieces.

established.

Am. Ry. Master Mechanics' Assn., 1894.—Same as Penna. R. R. Specifica-

Am. kg). Master Mechanics' Assia, 1894.—Same as Fenna. R. R. Specinical tions of 1892, including homogeneity test.

Plate, Tank, and Sheet Steel. (Penna, R. R., 1888.\*)—A test strict taken lengthwise of each plate, ½ in. thick and over, without annealing, should have a tensile strength of 60,000 lbs. per sq. in., and an elongation of 254 in a section originally 2 in. long.

Sheets will not be accepted if the tests show the tensile strength less than

55,000 lbs. or greater than 70,000 lbs. per sq. in., nor if the elongation falls

below 20%

Steel Billets for Main and Parallel Rods, (Penna, R. R., 1884.) -One billet from each lot of 25 billets or smaller shipment of steel for main or parallel rods for locomotives will have a piece drawn from it under the hammer and a test-section will be turned down on this piece to % in. in diameter and 2 in. long. Such test-piece should show a tensile strength of 85,000 lbs. and an elongation of 15%.

No lot will be acceptable if the test shows less than 80,000 lbs. tensile

strength or 12% e'ongation in 2 in.

Locomotive Spring Steel. (Penna R. R., 1887.)—Bars which vary more than 0.01 in. in thickness, or more than 0.02 in. in width, from the size ordered, or which break where they are not nicked, or which, when properly nicked and held, fail to break square across where they are nicked, will be returned. The metal desired has the following composition: Carbon, 1.00%; manganese, 0.25%; phosphorus, not over 0.05%; silicon, not over 0.15%; sulphur, not over 0.03%; copper, not over 0.03%.

Shipments will not be accepted which show on analysis less than 0.90% or over 1.10% of carbon, or over 0.50% of manganese, 0.05% of phosphorus, 0.25%

of silicon, 0.05% of sulphur, and 0.05% of copper

Steel for Locomotive Driving-axles. (Penna, R. R., 1883.)—Steel for driving-axles should have a tensile strength of 85,000 lbs. per sq. in. and an elongation of 15% in section originally 2 in. long and 5% in. diameter, taken midway between centre and circumference of the axle

Axles will not be accepted if tensile strength is less than 80,000 lbs., nor if

elongation is below 12%.

Steel for Crank-pins, (Penna, R. R., 1886.)—Steel ingots for crank-

<sup>\*</sup>The Penna. R. R. specifications of the several dates given are still in force, July, 1894.

pins must be swaged as per drawings. For each lot of 50 ingots ordered, 51 pins must be swaged as per drawings. For each lot of 56 ingoes ordered, or must be furnished, from which one will be taken at random, and two pieces, with test sections 56 in. diameter and 2 in. long, will be cut from any part of it, provided that centre line of test-pieces falls 11/2 in. from centre line of ingot. Such test-pieces should have a tensile strength of 85,000 lbs. per sq. in. and an elongation of 15%. Ingots will not be accepted if the tensile strength

and an 1900gadout 15 mor if the elongation is below 12%.

Dr. Chas. B. Dudley, Chemist of the P. R. R. (Trans. A. I. M. E. 1892), referring to this specification, says: In testing a recent shipment, the piece from one side of the pin showed 88,000 lbs. strength and 22% elongation, and the piece from the opposite side showed 106,000 lbs. strength and 14% elongation. Each piece was above the specified strength and ductility, but the lack of uniformity between the two sides of the pin was so marked that it was finally determined not to put the lot of 50 pins in use. To guard against trouble of this sort in future, the specifications are to be amended to require that the difference in ultimate strength of the two specimens shall not be more than 3000 lbs

Steel Car-axles, (Penna. R. R., 1891.)-For each 100 axles ordered 101 must be furnished, from which one will be taken at random, and subjected

Axles for passenger cars and passenger locomotive and tender trucks must be made of steel and be rough turned throughout. Two test-pieces will be cut from an axle, and the test sections of 5g in. diameter by 2 in. long may fall at any part of the axle provided that the centre line of the test-section is 1 in. from the centre line of the axle. Such test-pieces should have a tensile strength of 80,000 lbs. per sq. in. and an elongation of 20%. Axles will not be accepted if the tensile strength is less than 75,000 lbs. or the elongation below 15%, nor if the fractures are irregular.

Axles for freight cars and freight-locomotive tender trucks must be made of steel, and will be subjected to the following test, which they must stand

without fracture:

AXLES 4 IN. DIAMETER AT CENTRE - Five blows at 20 ft. of a 1640-lb, weight, striking midway between supports 3 ft. apart; axle to be turned over after each blow.

AXLES 43% IN. DIAMETER AT CENTRE-Five blows at 25 ft. of a 1640-lb. weight, striking midway between supports 3 ft. apart: axles to be turned over after each blow.

Steel for Rails .- P. H. Dudley (Trans. A. S. C. E. 1893) recommends the following chemical composition for rails of the weights specified:

Weights per yard.... 60, 65, and 70 lbs. Carbon............ 45 to .55% 75 and 80 lbs. 100 lbs. .65 to .75% .50 to .60% For all weights: Manganese, .80% to 1.00%; silicon, .10% to .15%; phos-

phorus, not over .06%; sulphur, not over .07%.

Carbon by itself up to or over 1% increases the hardness and tensile strength of the iron rapidly, and at the same time decreases the elongation. The amount of carbon in the early rails ranged from 0.25 to 0.5 of 1%, while recent rails and very heavy sections it has been increased to 0.5, 0.6, and 0.75of 1%. With good irons and suitable sections it can run from 0 55 to 0.75 of 1%, according to the section, and obtain fine-grain tough rails with low phosphorus.

Manganese is a necessary ingredient in the first place to take up the oxide of iron formed in the bath of molten metal during the blow. It also is of great assistance to check red shortness of the ingots during the first passes in the blooming train. In the early rails 0.4 to 0.5 of 1% was sufficient when the ingots were hammered or the reductions in the passes in the trains were with the train that oday. With the more rapid rolling of recent years the manganese is very often increased to 1.2% to 1.5%. It makes the rails hard with a coarse crystallization and with a decided tendency to brittleness. Rails high in manganese seem to flow quite easily, especially under severe service or the use of sand, and oxidize rapidly in tunnels. From 0.90 to 1.00%

seems to be all that is necessary for good rolling at the present time.

Steel Rivets. (H. C. Torrance, Amer. Boiler Mfrs. Assa, 1890.)—The
Government requirements for the rivets used in boilers of the cruisers built in 1890 are: For longitudinal seams, 58,000 to 67,000 lbs. tensile strength; elongation, not less than 26% in 8 in., and all others a tensile strength of 50,000 to 58,000 lbs., with an elongation of not less than 30%. They shall be capable of being flattened out cold under the hammer to a thickness of one half the diameter, and of being flattened out hot to a thickness of one third

the diameter without showing cracks or flaws. The steel must not contain more than .035 of 1% of phosphorus, nor more than .04 of 1% of sulphur. A lot of 20 successive tests of rivet steel of the low tensile strength quality

and 12 tests of the higher tensile strength gave the following results:

	Low Steel.	Higher.
Tensile strength, lbs. per sq. in	51,230 to 54,100	59,100 to 61,850
Elastic limit, lbs. per sq. in	31,050 to 33,190	32,080 to 33,070
Elongation in 8 in., per cent	30.5 to 35.25	28.5 to 31.75
Carbon, per cent	.11 to .14	.16 to .18
Phosphorus	.027 to .029	.03
Sulphur	.033 to .035	.033 to .035

The safest steel rivets are those of the lowest tensile strength, since they are the least liable to become hardened and fracture by hammering, or to break from repeated concussion and vibratory strains in a which they are subjected in practice. For calculations of the strength may be taken as the average of the figures above given, or 52,665 lbs., and the shearing strength at 45,000 lbs. per sq. in.

#### MISCELLANEOUS NOTES ON STEEL.

May Carbon be Burned Out of Steel ?—Experiments made at the Laboratory of the Penna. Railroad Co. (Specifications for Springs, 1888) with the steel of spiral springs, show that the place from which the borings are taken for analysis has a very important influence on the amount of car-If the sample is a piece of the round bar, and the borings are taken from the end of this piece, the carbon is always higher than if the borings are taken from the side of the piece. It is common to find a difference of 0.10% between the centre and side of the bar, and in some cases the difference is as high as 0.23%. Furthermore, experiments made with samples taken from the drawn out end of the bar show, usually, less carbon than samples taken from the round part of the bar, even though the borings may be taken out of the side in both cases.

Apparently during the process of reducing the metal from the ingots to the round bar, with successive heatings, the carbon in the outside of the bar is

burned out.

"Recalescence" of Steel.-If we heat a bar of copper by a flame of constant strength, and note carefully the interval of time occupied in passing from each degree to the next higher degree, we find that these intervals increase regularly, i.e., that the bar heats more and more slowly, as its temperature approaches that of the flame. If we substitute a bar of steel for one of copper, we find that these intervals increase regularly up to a certain point, when the rise of temperature is suddenly and in most cases greatly retarded or even completely arrested. After this the regular rise of temperature is resumed, though other like retardations may recur as the temperature rises farther. So if we cool a bar of steel slowly the fall of temperature is greatly retarded when it reaches a certain point in dull red-If the steel contains much carbon, and if certain favoring conditions be maintained, the temperature, after descending regularly, suddenly rises spontaneously very abruptly, remains stationary a while, and then redescends. This spontaneous reheating is known as "recalescence."

These retardations indicate that some change which absorbs or evolves heat occurs within the metal. A retardation while the temperature is rising

neat occurs when the metal. A retardation while the temperature is rising points to a change which absorbs heat; a retardation during cooling points to some change which evolves heat. (Henry M. Howe, on "Heat Treatment of Steel," Trans. A. I. M. E. vol. xxii.)

Effect of Nicking a Steel Bar.—The statement is sometimes made that, owing to the homogeneity of steel, a bar with a surface crack or nick in one of its edges is liable to fail by the gradual spreading of the nick, and thus break under a very much smaller load than a sound bar. With iron it is contended this does not occur, as this metal has a fibrous structure. Sir is contended this does not occur, as this metal has a finorious structure. Sir Benjamin Baker has, however, shown that this theory, at least so far as statical stress is concerned, is opposed to the facts, as he purposely made nicks in specimens of the mild steel used at the Forth Bridge, but found that the tensile strength of the whole was thus reduced by only about one ton per square inch of section. In an experiment by the Union Bridge Company a full-sized steel counter-bar, with a screw-turned buckle connection, was tested under a heavy statical stress, and at the same time a weight weighing 1040 lbs, was allowed to drop on it from various heights. The bar was first broken by ordinary statical strain, and showed a breaking stress of

65,800 lbs. per square inch. The longer of the broken parts was then placed in the machine and put under the following loads, whilst a weight, as already mentioned, was dropped on it from various heights at a distance of five feet from the sleeve-nut of the turn-buckle, as shown below:

Stress in pounds per sq. in.... 50,000 55,000 60,000 63,000 65 000 ft. in. ft. in. ft. in. ft. in. ft. in. 4 0 Height of fall..... 2 1 5 0

The weight was then shifted so as to fall directly on the sleeve-nut, and the test proceeded as follows:

Stress on specimen in lbs. per square inch ...... 65,350 65,350 68,800 ft. ft. ft. 6 Height of fall..... 6

It will be seen that under this trial the bar carried more than when origi-

ally tested statically, showing that the nicking of the bar by screwing had not appreciably weakened its power of resisting shocks.—Eng'g News.

Electric Conductivity of Steel.—Louis Campredon reports in Le Génic Civil the results of a series of experiments made to ascertain the relations between electric resistance and chemical compositions of steel. The wires were No. 17, 3 mm. diameter. The results are given in the table below:

	Car- bon.	Silicon.	Sulphur.	Phos- phorus.	Manga- nese.	Total.	Electric Resist- ance, Ohms.
1 2 3 4 5 6 7 8 9	0.090 0.100 0.100 0.100 0.120 0.110 0.100 0.120 0.110	0.020 0.020 0.020 0.020 0.030 0.030 0.020 0.020 0.030 0.030	0.050 0.050 0.060 0.050 0.070 0.060 0.070 0.070 0.060	0.030 0.040 0.040 0.050 0.050 0.060 0.040 0.070 0.060 0.080	0.210 0.240 0.260 0.310 0.330 0.350 0.400 0.400 0.490 0.540	0.410 0.450 0.480 0.530 0.600 0.610 0.630 0.680 0.750 0.850	127.7 133.0 137.5 140.3 142.7 144.5 149.0 150.3 156.0 173.0

An examination of these series of figures shows that the purer and softer steel the better is its electric conductivity, and, furthermore, that manga-

nese is the element which most influences the conductivity.

Specific Gravity of Soft Steel. (W. Kent, Trans. A. I. M. E., xiv.

585.—Five specimens of boiler-plate of C. 0.14, P. 0.03 gave an average sp. gr. of 7.992, maximum variation 0.008. The pieces were first planed to remove all possible scale indentations, then filed smooth, then cleaned in dilute sulphuric acid, and then boiled in distilled water, to remove all traces

of air from the surface.

The figures of specific gravity thus obtained by careful experiment on bright, smooth pieces of steel are, however, too high for use in determining the weights of rolled plates for commercial purposes. The actual average thickness of these plates is always a little less than is shown by the calipers, on account of the oxide of iron on the surface, and because the surface is not perfectly smooth and regular. A number of experiments on commercial plates, and comparison of other authorities, led to the figure 7.854 as the average specific gravity of open-hearth boiler-plate steel. This figure is easily remembered as being the same figure with change of position of the decimal point (.7854) which expresses the relation of the area of a circle to that of its circumscribed square. Taking the weight of a cubic foot of water at 62° F. as 62.36 lbs. (average of several authorities), this figure gives 489.775 lbs. as the weight of a cubic foot of steel, or the even figure, 490 lbs., may be taken as a convenient figure, and accurate within the limits of the error of observation.

A common method of approximating the weight of iron plates is to consider them to weigh 40 lbs. per square foot one inch thick. Taking this

weight and adding 2% gives almost exactly the weight of steel boiler-plate given above (40 × 12 × 1.02 = 489.6 lbs. per cubic foot).

Occasional Failures of Bessemer Steel.—G. H. Clapp and A. E. Hunt, in their paper on "The Inspection of Materials of Construction in

the United States" (Trans. A. I. M. E., vol. xix), say: Numerous instances could be cited to show the unreliability of Bessemer steel for structural purposes. One of the most marked, however, was the following: A 12-in, I-beam weighing 30 lbs. to the foot, 20 feet long, on being unloaded from a car broke in two about 6 feet from one end.

The analyses and tensile tests made do not show any cause for the failure. The cold and quench bending tests of both the original 34 in round test-pieces, and of pieces cut from the finished material, gave satisfactory re-sults; the cold-bending tests closing down on themselves without sign of

fracture.

Numerous other cases of angles and plates that were so hard in places as to break off short in punching, or, what was worse, to break the punches have come under our observation, and although makers of Bessemer steel claim that this is just as likely to occur in open-hearth as in Bessemer steel, we have as yet never seen an instance of failure of this kind in open-hearth steel having a composition such as C 0.25%, Mn 0.70%, P 0.80%,

J. W. Wailes, in a paper read before the Chemical Section of the British Association for the Advancement of Science, in speaking of mysterious failures of steel, states that investigation shows that "these failures occur

in steel of one class, viz., soft steel made by the Bessemer process."

Segregation in Steel Ingots. (A. Pourcel, Trans. A. I. M. E. 1893.)

-H. M. Howe, in his "Metallurg of Steel." gives a résumé of observations, with the results of numerous analyses, bearing upon the phenomena of seg-

regation.

In 1881 Mr. Stubbs, of Manchester, showed the heterogeneous results of

analyses made upon different parts of an ingot of large section

A test-piece taken 24 inches from the head of the jugot 7.5 feet in length gave by analysis very different results from those of a test-piece taken 30 inches from the bottom.

C. Mn. Si. 0.92 0.535 0.043 0.161 0.261 Top ..... 0 37 0.498 0.006 0.025 Bottom .... 0.096

Windsor Richards says he had often observed in test-pieces taken from different points of one plate variations of 0.05% of carbon. Segregation is specially pronounced in an ingot in its central portion, and around the space of the piping.

It is most observable in large ingots, but in blocks of smaller weight and limited dimensions, subjected to the influence of solidification as rapid as casting within thick walls will permit, it may still be observed distinctly. An ingot of Martin steel, weighing about 1000 lbs., and having a height of 1.10 feet and a section of 10.24 inches square, gave the following:

1. Upper section:	C. *	S.	P.	Mn.
Border	0.330	0.040	0.033	0.420
Centre	0.530	0.077	0.057	0.430
2. Lower section:	C.	S.	P.	Mn.
Border		0.029	0.016	0.390
Centre	0.290	0.030	0.038	0.390
3. Middle section:	C.	S.	P.	Mn.
Border	0.320	0.025	0.025	0.400
Centre	0.320	0.048	0.048	0.400

Segregation is less marked in ingots of extra-soft metal cast in cast-iron moulds of considerable thickness. It is, however, still important, and explains the difference often shown by the results of tests on pieces taken from different portions of a plate. Two samples, taken from the sound part of a flat ingot, one on the outside and the other in the centre, 7.9 inches from the upper edge, gave:

Centre..... 0.14 0.0530.072 0.576 0.11 0.0360.027 Exterior.....

Manganese is the element most uniformly disseminated in hard or soft

For cannon of large calibre, if we reject, in addition to the part cast in sand and called the masselotte (sinking head), one third of the upper part of the ingot, we can obtain a tube practically homogeneous in composition, because the central part is naturally removed by the boring of the tube. With extra-soft steels, destined for ship- or boiler-plates, the solution for practically perfect homogeneity lies in the obtaining of a metal more closely deserving its name of extra-soft metal.

The injurious consequences of segregation must be suppressed by reduc-

ing, as far as possible, the elements subject to liquation,

Earliest Uses of Steel for Structural Purposes, (G. G.
Mehrtens, Trans. A. S. C. E. 1893).—The Pennsylvania Railroad Company first introduced Bessemer steel in America in locomotive boilers in the year 1863, but the steel was too hard and brittle for such use. The first plates made for steel boilers had a tenacity of 85,000 to 92,000 lbs, and an elongation of but 7% to 10%. The results were not favorable, and the steel works were soon forced to offer a material of less tenacity and more ductility. quirements were therefore reduced to a tenacity of 78,000 lbs. or less, and the elongation was increased to 15% or more. Even with this, between the years 1870 and 1880, many explosions occurred and many careful examinations were made to determine their cause. It was found on examining the rivet-holes that there were incipient changes in the metal, many cracks around them, and points near them were corroded with rust, all caused by the shock of tools in manufacturing. It was evident that the material was unsuitable, and that the treatment must be changed. In the beginning of 1878, Mr. Parker, chief engineer of the Lloyds, stated that there was then but one English steamer in possession of a steel boiler; a year later there were 120. In 1878 there were but five large English steamers built of steel, while in 1883 there were 116 building. The use of Bessemer steel in bridge-building was tried first on the Dutch State railways in 1863-64, then in England and Austria. In 1874 a bridge was built of Bessemer steel in Austria. The first use of cast steel for bridges was in America, for the St. Louis Arch Bridge and for the wire of the East River Bridge. These gave an impetus to the use of ingot metal, and before 1880 the Glasgow and Plattsmouth Bridges over the Missouri River were also built of ingot netal. Steel eyebars were applied for the first time in the Glasgow Bridge. Since 1880 the introduction of mild steel in all kinds of engineering structures has steadily increased.

#### STEEL CASTINGS.

(E. S. Cramp, Engineering Congress, Dept. of Marine Eng'g, Chicago, 1893.)

In 1891 American steel-founders had successfully produced a considerable variety of heavy and difficult castings, of which the following are the most noteworthy specimens:

Bed-plates up to 24,000 lbs.; stern-posts up to 54,000 lbs.; stems up to 21,000 lbs.; hydraulic cylinders up to 11,000 lbs.; shaft-struts up to 32,000 lbs.;

hawse-pipes up to 7500 lbs.; stern-pipes up to 8000 lbs.

The percentage of success in these classes of castings since 1890 has ranged from 65% in the more difficult forms to 90% in the simpler ones; the tensile strength has been from 62,000 to 78,000 lbs., elongation from 15% to 25%. best performance recorded is that of a guide, cast in January, 1893, which

developed 84,000 lbs. tensile strength and 15.6% elongation.

developed 84,000 to S. tensies strength and 15.0% elongation.

The first steel castings of which anything is generally known were crossing-frogs made for the Philadelphia & Reading R. R. in July, 1867, by the William Butcher Steel Works, now the Midvale Stvel Co. The moulds were made of a mixture of ground fire-brick, black-lead crucible-pots ground fine, and fire-clay, and washed with a black-lead wash. The steel was melted in crucibles, and was about as hard as tool steel. The surface of these castings was very smooth, but the interior was very much honeycombed. This was before the days when the use of silicon was known for solidifying steel. The sponginess, which was almost universal, was a great obstacle to their general adoption,

The next step was to leave the ground pots out of the moulding mixture and to wash the mould with finely ground fire-brick. This was a great improvement, especially in very heavy castings; but this mixture still clung so strongly to the casting that only comparatively simple shapes could be made with certainty. A mould made of such a mixture became almost as hard as fire-brick, and was such an obstacle to the proper shrinkage of castings, that, when at all complicated in shape, they had so great a tendency to erack as to make their successful manufacture almost impossible. By this time the use of silicon had been discovered, and the only obstacle in the way of making good castings was a suitable moulding mixture. This was ultimately found in mixtures having the various kinds of silica sand as the principal constituent.

One of the most fertile sources of defects in castings is a bad design. Very intricate shapes can be cast successfully if they are so designed as to

cool uniformly. Mr. Cramp says while he is not yet prepared to state that anything that can be cast successfully in iron can be cast in steel, indications seem to point that way in all cases where it is possible to put on suit-

able sinking heads for feeding the casting.

H. L. Gautt (Trans, A. S. M. E., xii. 710) says: Steel castings not only shrink much more than iron ones, but with less regularity. The amount of shrinkage varies with the composition and the heat of the metal; the hotter shrinkage varies with the composition and the heat of the metal, the notiter the metal the greater the shrinkage; and, as we get smoother castings from hot metal, it is better to make allowance for large shrinkage and pour the netal as hot as possible. Allow 3/16 or ¼ in. per ft. in length for shrinkage, and ½ in. for finish on machined surfaces, except such as are cast "up." Cope surfaces which are to be machined should, in large or hard castings, have an allowance of from 3/2 to 3/2 in. for finish, as a large mass of metal slowly rising in a mould is apt to become crusty on the surface, and such a crust is sure to be full of imperfections. On small, soft castings 1/8 in. on drag side and 1/4 in. on cope side will be sufficient. No core should have less than 1/4 in. finish on a side and very large ones should have as much as ½ in, on a side. Blow-holes can be entirely prevented in castings by the addition of manganese and silicon in sufficient quantities; but both of these cause brittleness, and it is the object of the conscientious steel-maker to put no more manganese and silicon in his steel than is just suffi-cient to make it solid. The best results are arrived at when all portions of

the castings are of a uniform thickness, or very nearly so.

The following table will illustrate the effect of annealing on tensile

strength and elongation of steel castings:

Carbon.	Unannea	led.	Annealed.		
	Tensile Strength.	Elongation.	Tensile Strength.	Elongation.	
.23% .37 .53	68,738 85,540 90,121	22.40% 8.20 2.35	67,210 82,228 106,415	31.40% 21.80 9.80	

The proper annealing of large castings takes nearly a week.

The proper steel for roll pinions, hammer dies, etc., seems to be that containing about .60% of carbon. Such castings, properly annealed, have worn well and seldom broken. Miscellaneous gearing should contain carbon .40% to 60%, gears larger in diameter being softest. General machinery castings should, as a rule, contain less than .40% of carbon, those exposed to great shocks containing as low at 20% of carbon. Such castings will give a tensile strength of from 60,000 to 80,000 lbs. per sq. in. and at least 15% extension in a 2 in. long specimen. Machinery and hull castings for war-vessels for the United States Navy, as well as carriages for naval guns, contain from .20% to 30% of carbon.

The following is a partial list of castings in which steel seems to be rapidly taking the place of iron: Hydraulic cylinders, crossheads and pistons for large engines, roughing rolls, rolling-mill spindles, coupling-boxes, roll pinions, gearing, hammer-heads and dies, riveter stakes, castings for ships,

car-couplers, etc.

For description of methods of manufacture of steel castings by the Bessemer, open-hearth, and crucible processes, see paper by P. G. Salom, Trans.

A. I. M. E. xiv, 118.

Specifications for steel castings issued by the U. S. Navy Department, 1889 (abridged): Steel for castings must be made by either the open-hearth or the crucible process, and must not show more than .06% of phosphorus. All castings must be annealed, unless otherwise directed. The tensile strength of steel castings shall be at least 60,000 lbs., with an elongation of at least 15% in 8 in. for all eastings for moving parts of the machinery, and at least 10% in 8 in. for other castings. Bars 1 in. sq. shall be capable of bending cold, without fracture, through an angle of 90°, over a radius not greater than 1½ in. All castings must be sound, free from injurious roughness, sponginess, pitting, shrinkage, or other cracks, cavities, etc.

Pennsylvania Railroad specifications, 1888: Steel castings should have a tensile strength of 70,000 lbs, per sq. in, and an elongation of 15% in section originally 2 in, long. Steel castings will not be accepted if tensile strength

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falls below 60,000 lbs., nor if the elongation is less than 12%, nor if castlings have blow-holes and shrinkage cracks. Castings weighing 50 lbs. or more must have east with them a strip to be used as a test-piece. The dimensions of this strip must be 3½ in. sq. by 12 in. long.

# MANGANESE, NICKEL, AND OTHER "ALLOY" STEELS.

Manganese Steel. (H. M. Howe, Trans. A. S. M. E., vol. xii.)—Manganese steel is an alloy of iron and manganese, incidentally, and probably

unavoidably, containing a considerable proportion of carbon.

The effect of small proportions of manganese on the hardness, strength, and ductility of iron is probably slight. The point at which manganese begins to have a predominant effect is not known: it may be somewhere about 2.5%. As the proportion of manganese rises above 2.5% the strength and ductility diminish, while the hardness increases. This effect reaches a maximum with somewhere about 6% of manganese. When the proportion of this element rises beyond 6% the strength and ductility both increase, while the hardness diminishes slightly, the maximum of both strength and ductility being reached with about 14% of manganese. With this proportion the metal is still so hard that it is very difficult to cut it with steel tools. As the proportion of manganese rises above 15% the ductility falls off abruptly. the strength remaining nearly constant till the manganese passes 18%, when it in turn diminishes suddenly

Steel containing from 4% to 6.5% of manganese, even if it have but 0.37% of carbon, is reported to be so extremely brittle that it can be powdered under

a hand-hammer when cold; yet it is ductile when hot.

Manganese steel is very free from blow-holes; it welds with great diffi-Manganese steel is very free from 1000-holes; it weids with great dim-culty; its toughness is increased by quenching from a yellow heat; its elec-tric resistance is enormous, and very constant with changing temperature; it is low in thermal conductivity. Its remarkable combination of great hard-ness, which cannot be materially lessened by annealing, and great tensile strength, with astonishing toughness and ductility, at once creates and limits its usefulness. The fact that manganese steel cannot be softened, that it ever remains so hard that it can be machined only with great difficulty, sets up a barrier to its usefulness.

The following comparative results of abrasion tests of manganese and

other steel were reported by T. T. Morrell:

ABRASION BY PRESSURE AGAINST A REVOLVING HARDENED-STEEL SHAFT. Loss of weight of manganese steel...... 1.0

	blue-tempered hard tool steel 0.	
66	annealed hard tool steel 7.	5
44	hardened Otis boiler-plate steel 7.	0
66	annealed " " " 14.	Õ
	ABRASION BY AN EMERY-WHEEL.	
Loss of weigh	of hard manganese-steel wheels 1.0	
46"	softer " " 1.1	9
44	hardest carbon-steel wheels 1.5	23
4.6	soft " " 2.8	35

The hardness of manganese steel seems to be of an anomalous kind. alloy is hard, but under some conditions not rigid. It is very hard in its resistance to abrasion; it is not always hard in its resistance to impact.

..... 2.85

Manganese steel forges readily at a yellow heat, though at a bright white hammer. But it offers greater resistance to deformation, i.e., it is harder when hot, than carbon steel.

The most important single use for manganese-steel is for the pins which hold the buckets of elevated dredgers. Here abrasion chiefly is to be

Another important use is for the links of common chain-elevators,

As a material for stamp-shoes, for horse-shoes, for the knuckles of an

automatic car-coupler, manganese steel has not met expectations.

Manganese steel has been regularly adopted for the blades of the Cyclone pulverizer. Some manganese-steel wheels are reported to have run over 300,000 miles each without turning, on a New England railroad.

Nickel Steel.—The remarkable tensile strength and ductility of nickel

steel, as shown by the test-bars and the behavior of nickel-steel armor-plate under shot tests, are witness of the valuable qualities conferred upon steel by the addition of a few per cent of nickel.

The following tests were made on nickel steels by Mr. Maunsel White of the Bethlehem Iron Company (Eng. & M. Jour., Sept. 16, 1893.):

	Specimen from—	Diam., in.	Length, in.	Tensile Str'gth, lbs. per sq. in.		p. c. ex.	p. c. cont.	-
steel.	Forged bars.*	} .625  ( .564	4 " 4	276,800 246,595 105,300 142,800	74,000	2.75 4.25 19.25 13.0		Special treatment. Annealed.
84% nickel steel.	1 <sup>1</sup> / <sub>4</sub> -in. round rolled bar.†		  	143.200 117,600 119,200 91,600 91,200 85,200	74,000 64,000 65,000 51,000 51,000 53,000	12.32 17.0 16.66 22.25 21.62 21.82	27.6 46.0 42.1 53.2 53.4 49.5	
nickel steel.	1½·in. sq. bar, rolled.;	798	8: ::	86,000 115,464 112,600 102,010 102,510	48,000 51,820 60,000 39,180 40,200	21.25 36.25 37.87 41.37 44.00	47.4 66.23 62.82 69.59 68.34	Annealed.
27% nick	1-in. round bar, rolled.§	500	2	114,590 115.610 105,240 106,780	56,020 59,080 45,170 45,170	47.25 45.25 49.65 55.50	68.4 62.3 72.8 63.6	Annealed.

\* Forged from 6 in. ingot to 3/8 in. diam., with conical heads for holding.

†Showing the effect of varying carbon. ‡Rolled down from 14-in. ingot to 1¼-in. square billet, and turned to size.

§ Rolled down from 14-in. ingot to 1/4-in. square office, and turned to size.

Nickel steel has shown itself to be possessed of some exceedingly valuable properties; these are, resistance to cracking, high elastic limit, and homogeneity. Resistance to cracking, a property to which the name of non fissibility has been given, is shown more remarkably as the percentage of nickel increases. Bars of 27% nickel illustrate this property. A 1¼-in, square barwas nicked ¼ in deep and bent double on itself without further fracture than the splintering off, as it were, of the nicked portion. Sudden failure or rupture of this steel would be impossible; it seems to possess the toughness of rawhide with the strength of steel. With this percentage of nickel the steel is practically non corrodible and non-magnetic. The resistance to cracking shown by the lower percentages of nickel is best illustrated in the many trials of nickel steel armor.

The elastic limit rises in a very marked degree with the addition of about 3% of nickel, the other physical properties of the steel remaining unchanged

or perhaps slightly increased.

In such places (shafts, axles, etc.) where failure is the result of the fatigue of the metal this higher elastic limit of nickel steel will tend to prolong indefinitely the life of the piece, and at the same time, through its superior

toughness, offer greater resistance to the sudden strains of shock.

Howe states that the hardness of nickel steel depends on the proportion of nickel and carbon jointly, nickel up to a certain percentage increasing the hardness, beyond this lessening it. Thus while steel with 25 of nickel and 0.9% of carbon cannot be machined, with less than 55 nickel it can worked cold readily, provided the proportion of carbon be low. As the proportion of nickel rises higher, cold-working becomes less easy. It forges easily whether it contain much or little nickel.

The presence of manganese in nickel steel is most important, as it appears that without the aid of manganese in proper proportions, the conditions of

treatment would not be successful.

Tests of Nickel Steel.—Two heats of open hearth steel were made by the Cleveland Rolling Mill Co. one ordinary steel made with 9000 lbs. each scrap and pig, and 165 lbs. ferro-manganese, the other the same with the addition of 3%, or 540 lbs. of nickel. Tests of six plates rolled from each heat., 0.24 to 0.3 in. thick, gave results as follows:

Ordinary steel, T. S. 52,500 to 56,500; E. L. 32,800 to 37,900; elong. 26 to 32%. Nickel steel, "63,370 to 67,100; "47,100 to 48,200; "23½ to 26%.

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The nickel steel averages 31% higher in elastic limit, 20% higher in ultimate tensile strength, with but slight reduction in ductility. (Eng. & M. Jour ...

Feb. 25, 1893.)

Aluminum Steel.-R. A. Hadfield (Trans. A. I. M. E. 1890) says: Aluminum appears to be of service as an addition to baths of molten iron or Animinian appears to be observed as an altist in properly regulated steel manufacture should not often occur. Speaking generally, it rôle appears to be similar to that of silicon, though acting more powerfully. The statement that aluminum lowers the melting-point of iron seams to have no foundation in fact. If any increase of heat or fluidity takes place by the addition of small amounts of aluminum, it may be due to evolution of heat, owing to oxidation of the aluminum, as the calorific value of this metal is very high-in fact, higher than silicon. According to Berthollet, the conversion of aluminum to Al<sub>2</sub>O<sub>3</sub> equals 7900 cal.; silicon to SiO<sub>2</sub> is stated as 7800.

The action of aluminum may be classed along with that of silicon, sulphur,

phosphorus, arsenic, and copper, as giving no increase of hardness to iron, in contradistinction to carbon, manganese, chromium, tungsten, and nickel. Therefore, whilst for some special purposes aluminum may be employed in the manufacture of iron, at any rate with our present knowledge of its properties, this use cannot be large, especially when taking into considera-tion the fact of its comparatively high price. Its special advantage seems to be that it combines in itself the advantages of both silicon and manganese; but so long as alloys containing these metals are so cheap and aluminum

dear, its extensive use seems hardly probable.

J. E. Stead, in discussion of Mr. Hadfield's paper, said: Every one of our trials has indicated that aluminum can kill the most fiery steel, providing, of course, that it is added in sufficient quantity to combine with all the oxygen which the steel contains. The metal will then be absolutely dead, and will pour like dead-melted silicon steel. If the aluminum is added as metalwill pour like dead-metted sincon steet. If the aluminum is added as metal-lic aluminum, and not as a compound, and if the addition is made just be-fore the steel is cast, 1/10% is ample to obtain perfect solidity in the steel. Chrome Steel. (F. L. Garrison, Jour. F. I., espt. 1891.)—Chromium increases the hardness of iron, perhaps also the tensile strength and elastic limit, but it lessens its weldbility. Ferro-chrome, according to Berthler, is made by strongly heating the mixed oxides of iron and chromium in brasqued crucibles, adding powdered

charcoal if the oxide of chromium is in excess, and fluxes to scorify the earthy matter and prevent oxidation. Chromium does not appear to give steel the power of becoming harder when quenched or chilled. Howe states that chrome steels forge more readily than tungsten steels, and when not containing over 0.5 of chromium nearly as well as ordinary carbon steels of like percentage of carbon. On the whole the status of chrome steel is not satisfactory. There are other steel alloys coming into use, which are so much better, that it would seem to be only a question of time when it will drop entirely out of the race. Howe states that many experienced chemists have found no chromium, or but the merest traces, in chrome steel sold in the markets.

J. W. Langley (Trans. A. S. C. E. 1892) says: Chromium, like manganese is a true hardener of iron even in the absence of carbon. The addition of 1% or 2% of chromium to a carbon steel will make a metal which gets excessively hard. Hitherto its principal employment has been in the production of chilled shot and shell. Powerful molecular stresses result during cooling, and the shells frequently break spontaneously months after they are made Tungsten Steel — Mushet Steel . (J. B. Nau, fron Age. Feb. 11, 1892.)

-By incorporating simultaneously carbon and tungsten in iron, it is possible to obtain a much harder steel than with carbon alone, without danger of an extraordinary brittleness in the cold metal or an increased difficulty in the working of the heated metal. When a special grade of hardness is required, it is frequently the custom

to use a high tungsten steel, known in England as special steel. A specimen from Sheffield, used for chisels, contained 9.% of tungsten, 0.% of silver, and 0.6% of carbon. This steel, though used with advantage in its untempered state to turn chilled rolls, was not brittle; nevertheless it was hard enough to scratch glass.

A sample of Mushet's special steel contained 8.3% of tungsten and 1.73% of manganese. The hardness of tungsten steel cannot be increased by the or-

dinary process of hardening.

The only operation that it can be submitted to when cold is grinding. has to be given its final shape through hammering at a red heat, and even 410

then, when the percentage of tungsten is high, it has to be treated very carefully; and in order to avoid breaking it, not only is it necessary to reheat it several times while it is being hammered, but when the tool has acquired the desired shape hammering must still be continued gently and with numerous blows until it becomes nearly cold. Then only can it be cooled en-

Tungsten is not only employed to produce steel of an extraordinary hardness, but more especially to obtain a steel which, with a moderate hardness, allies great toughness, resistance, and ductility. Steel from Assailly, used for this purpose, contained carbon, 0.52%; silicon, 0.04%; tungsten, 0.3%; phosphorus, 0.04%; sulphur, 0.005%.

Mechanical tests made by Styffe gave the following results:

Breaking load per square inch of original area, pounds.. 172,424 Reduction of area, per cent .... Average elongation after fracture, per cent ......

According to analyses made by the Duc de Luynes of ten specimens of the celebrated Oriental damasked steel, eight contained tungsten, two of them in notable quantities (0.518% to 1%), while in all of the samples analyzed nickel was discovered ranging from traces to nearly 4%.

Stein & Schwartz of Philadelphia, in a circular say: It is stated that tungsten steel is suitable for the manufacture of steel magnets, since it retains its magnetism longer than ordinary steel. Mr. Kulesis, since it retains its magnetism longer than ordinary steel. Mr. Kulesis, has made tungsten up to 98% fine a specialty. Dr. Heppe, of Leipsig, has written a number of articles in German publications on the subject. The following instructions are given concerning the use of tungsten: in order to produce cast iron possessing great hardness an addition of one half to one and one half of tungsten is all that is needed. For bar iron it must be carried up to 3½ to 2½, but should not exceed 2½. For puddled steel the range is larger, but an addition beyond 31/4% only increases the hardness, so that it is brought up to 11/2% only for special tools, coinage dies, drills, etc. For tires 21/2% to 5% have proved best, and for axles 1/4 to 11/4%. Cast steel to which tungsten has have proved best, and for axies ½ to 1½%. Cast steet to which tungsten has been added needs a higher temperature for tempering than ordinary steel, and should be hardened only between yellow, red, and white. Chisels made of tungsten steel should be drawn between cherry-red and blue, and stand well on iron and steel. Tempering is best done in a mixture of 5 parts of yellow rosin, 3 parts of tar, and 2 parts of tallow, and then the article is once more heated and then tempered as usual in water of about 15° C.

Whitworth Compressed Steel. (Proc. Inst. M. E., May, 1887, p. 167)—In this system a gradually increasing pressure up to 6 or 8 tons per square inch is applied to the fluid ingot, and within half an hour or less after the application of the pressure the column of fluid steel is shortened 1½ inch per foot or one eighth of its length; the pressure is then kept on for several hours, the result being that the metal is compressed into a perfectly

solid and homogeneous material, free from blow-holes.

In large gun-ring ingots during cooling the carbon is driven to the centre, the centre containing 0.8 carbon and the outer ring 0.3. The centre is bored out until a test shows that the inside of the ring contains the same percentage of carbon as the outside.

Compressed steel is made by the Bethlehem Iron Co. and the Carnegie

Steel Co. for armor-plate and for gun and other heavy forgings.

# CRUCIBLE STEEL.

Selection of Grades by the Eye, and Effect of Heat Treat-ment. (J. W. Langley, Amer. Chemist, November, 1876.)—In 1874, Miller, Metcalf & Parkin, of Pittsburgh, selected eight samples of steel which were believed to form a set of graded specimens, the order being based on the quantity of carbon which they were supposed to contain. They were numbered from one to eight. On analysis, the quantity of carbon was found to follow the order of the numbers, while the other elements present—silicon, phosphorus, and sulphur—did not do so. The method of selection is described as follows

The steel is melted in black-lead crucibles capable of holding about eighty pounds; when thoroughly fluid it is poured into cast-iron moulds, and when cold the top of the ingot is broken off, exposing a freshly-fractured surface. The appearance presented is that of confused groups of crystals, all appearing to have started from the outside and to have met in the centre; this general form is common to all ingots of whatever composition, but to the trained eye, and only to one long and critically exercised, a minute but indescribable difference is perceived between varying samples of steel, and this difference is now known to be owing almost wholly to variations in the amount of combined carbon, as the following table will show. Twelve samples selected by the eye alone, and analyses of drillings taken direct from the ingot before it had been heated or hammered, gave results as below:

Ingot Nos.	Iron by Diff,	Carbon.	Diff. of Carbon.	Silicon.	Phos.	Sulph.
1	99.614	.302		.019	.047	.018
2	99,455	490	.188	.034	.005	.016
1 2 3 4 5 6 7 8	99.363	.529	.039	.043	.047	.018
4	99.270	.649	.120	.039	.030	.012
5	99.119	.801	.152	.029	.035	.016
6	99.086	.841	.040	.039	.024	,010
7	99.044	.867	.026	.057	.014	.018
8	99.040	.871	.004	.053	.024	.012
9	98.900	.955	.084	.059	.070	.016
10	98 861	1.005	.050	.088	.034	.012
11	98.752	1.058	.053	,120	.064	.006
12	98.834	1.079	.021	.039	.044	.004

Here the carbon is seen to increase in quantity in the order of the numbers, while the other elements, with the exception of total iron, bear no relation to the numbers on the samples. The mean difference of carbon is .071.

In mild steels the discrimination is less perfect.

The appearance of the fracture by which the above twelve selections were made can only be seen in the cold ingot before any operation, except

the original one of casting, has been performed upon it. As soon as it is hammered, the structure changes in a remarkable manner, so that all trace

nammered, the structure canages in a remarkable manner, so that all trace of the primitive condition appears to be lost.

Another method of rendering visible to the eye the molecular and chemical changes which go on in steel is by the process of hardening or tempering. When the metal is heated and plunged into water it acquires an increase of hardness, but a loss of ductility. If the heat to which the steel has been raised just before plunging is too high, the metal acquires intense hardness, but it is so brittle as to be worthless; the fracture is of a bright, granular, or sandy character. In this state it is said to be burned, and it granular, or sandy character. In this state it is said to be burned, and it cannot again be restored to its former strength and ductility by annealing; it is ruined for all practical purposes, but in just this state it again shows differences of structure corresponding with its content in carbon. The nature of these charges can be illustrated by plunging a bar highly heated at one end and cold at the other into water, and then breaking it off in pieces of equal length, when the fractures will be found to show appearances characteristic of the temperature to which the sample was raised.

The specific gravity of steel is influenced not only by its chemical analysis, but by the heat to which it is subjected, as is shown by the following

table (densities referred to 60° F.):

Specific gravities of twelve samples of steel from the ingot; also of six hummered bars, each bar being overheated at one end and cold at the other, in this state plunged into water, and then broken into pieces of equal length.

	1	2	3	4	5	6	7	8	9	10	11	12
		* 000						* 010				
Ingot	7.855	7.836	7.841	7.829	7.838	7.824	7.819	7.818	7.813	7.807	7.803	7.805
Bar:												
*Burned 1						7.789		7.752		7.744		7.690
Cold 6			7.844	7.824		7.829		7.825		7.826		7.825

<sup>\*</sup> Order of samples from bar.

Effect of Heat on the Grain of Steel. (W. Metcalf,—Jeans on Steel, p. 642.)—A simple experiment will show the alteration produced in a high-carbon steel by different methods of hardening. If a bar of such steel be nicked at about 9 or 10 places, and about half an inch apart, a suitable specimen is obtained for the experiment. Place one end of the bar in a good fire, so that the first nicked piece is heated to whiteness, while the rest of the bar, being out of the fire, is heated up less and less as we approach the other end. As soon as the first piece is at a good white heat, which of course burns a high carbon steel, and the temperature of the rest of the bar gradually passes down to a very dull red, the metal should be taken out of gradually passes down to a very dun't rea, the metal should be left till the fire and suddenly plunged in cold water, in which it should be left till quite cold. It should then be taken out and carefully dried. An examination with a file will show that the first piece has the greatest hardness, while the last piece is the softest, the intermediate pieces gradually passing from one condition to the other. On now breaking off the pieces at each from one condition to the other. On now breaking off the pieces at each nick it will be seen that very considerable and characteristic changes have been produced in the appearance of the metal. The first burnt piece is very open or crystalline in fracture; the succeeding pieces become closer and closer in the grain until one piece is found to possess that perfectly even grain and velvet-like appearance which is so much prized by experienced steel users. The first pieces also, which have been too much hardened, will probably be cracked; those at the other end will not be hardened through. Hence if it be desired to make the steel hard and strong, the temperature used must be high enough to harden the metal through, but not sufficient to open the crain. not sufficient to open the grain.

Changes in Titimate Strength and Elasticity due to Hammering, Annealing, and Tempering, (J. W. Langley, Trans. A. S. C. E. 182.) - The following table gives the result of tests made on some round steel bars, all from the same ingot, which were tested by

tensile stresses, and also by bending till fracture took place:

Number.	Treatment.	Angle of cold bend, degrees.	Total.	Semi- graphite.	Diameter, in.	Elastic limit, pounds per square inch.	Tensile, pounds per square inch.	Elongation, , per cent.	Red area, per cent.
2	Cold-hammered bar Bar drawn black Bar annealed Bar hardened and drawn black	75 175		.47 .70	.580	92,420 114,700 68,110 152,800	141,500 138,400 98,410 248,700	2.00 6.00 10.00	2.42 12.45 11.69

The total carbon given in the table was found by the color test, which is affected, not only by the total carbon, but by the condition of the carbon.

The analysis of the steel was:

Silicon	.242	Manganese	.24
Phosphorus	.02	Carbon (true total carbon, by	
Sulphur	.009	combustion)	1.31

Heating Tool Steel. (Miller, Metcalf & Parkin, 1877.)-There are three distinct stages or times of heating: First, for forging; second, for

hardening; third, for tempering.

The first requisite for a good heat for forging is a clean fire and pleuty of fuel, so that jets of hot air will not strike the corners of the piece; next, the fire should be regular, and give a good uniform heat to the whole part to be forged. It should be keen enough to heat the piece as rapidly as may be, and allow it to be thoroughly heated through, without being so fierce as to overheat the corners.

Steel should not be left in the fire any longer than is necessary to heat it clear through, as "soaking" in fire is very injurious; and, on the other hand, it is necessary that it should be hot through, to prevent surface cracks.

By observing these precautions a piece of steel may always be heated safely, up to even a bright yellow heat, when there is much forging to be done on it.

The best and most economical of welding fluxes is clean, crude borax, which should be first thoroughly melted and then ground to fine powder.

After the steel is properly heated, it should be forged to shape as quickly as possible; and just as the red heat is leaving the parts intended for cutting edges, these parts should be refined by rapid, light blows, continued until the red disappears.

For the second stage of heating, for hardening, great care should be used: ror the second stage of nearing for naturaling parts from heating more rapidly than the body of the piece; next, that the whole part to be hardened be heated uniformly through, without any part becoming visibly hotter than the other. A uniform heat, as low as will give the required hardness, is the best for hardening.

For every variation of heat, which is great enough to be seen, there will be the property of the property of

result a variation in grain, which may be seen by breaking the piece; and for every such variation in temperature, there is a very good chance for a crack to be seen. Many a costly tool is ruined by inattention to this point.

The effect of too high heat is to open the grain; to make the steel coarse. The effect of an irregular heat is to cause irregular grain, irregular strains,

and cracks. As soon as the piece is properly heated for hardening, it should be promptly and thoroughly quenched in plenty of the cooling medium, water, brine, or oil, as the case may be.

An abundance of the cooling bath, to do the work quickly and uniformly all over, is very necessary to good and safe work.

To harden a large piece safely a running stream should be used.

Much uneven hardening is caused by the use of too small baths.

For the third stage of heating, to temper, the first important requisite is again uniformity. The next is time; the more slowly a piece is brought down to its temper, the better and safer is the operation.

When expensive tools are to be made it is a wise precaution to try small pieces of the steel at different temperatures, so as to find out how low a heat will give the necessary hardness. The lowest heat is the best for any steel.

Heating to Forge.—The trouble in the forge fire is usually uneven heat, and not too high heat. Suppose the piece to be forged has been put into a very hot fire, and forced as quickly as possible to a high yellow heat, so that it is almost up to the scintillating point. If this be done, in a few minutes the outside will be quite soft and in a piec condition for forging, while the middle parts will not be more than red-hot. Now let the piece be placed under the hammer and forged, and the soft outside will yield so much more readily than the hard inside, that the outer particles will be torn asunder, while the inside will remain sound.

Suppose the case to be reversed and the inside to be much hotter than the outside; that is, that the inside shall be in a state of semi-fusion, while the outside is hard and firm. Now let the piece be forged, and the outside will be all sound and the whole piece will appear perfectly good until it is cropped, and then it is found to be hollow inside.

In either case, if the piece had been heated soft all through, or if it had been

only red-hot all through, it would have forged perfectly sound.

In some cases a high heat is more desirable to save heavy labor but in every case where a fine steel is to be used for cutting purposes it must be borne in mind that very heavy forging refines the bars as they slowly cool, and if the smith heats such refined bars until they are soft, he raises the grain, makes them coarse, and he cannot get them fine again unless he has a very heavy steam-hammer at command and knows how to use it well.

Annealing. (Miller, Metcalf & Parkin.)—Annealing or softening is accomplished by heating steel to a red heat and then cooling it very slowly,

to prevent it from getting hard again.

The higher the degree of heat, the more will steel be softened, until the

limit of softness is reached, when the steel is melted.

It does not follow that the higher a piece of steel is heated the softer it will be when cooled, no matter how slowly it may be cooled; this is proved by the fact that an ingot is always harder than a rolled or hammered bar made from it.

Therefore there is nothing gained by heating a piece of steel hotter than a good, bright, cherry-red; on the contrary, a higher heat has several disadvantages; First. If carried too far, it may leave the steel actually harder than a good red heat would leave it. Second. If a scale is raised on the steel, this scale will be harsh, granular oxide of iron, and will spoil the tools used to cut it. Third. A high scaling heat continued for a little time changes the structure of the steel, makes it brittle, liable to crack in hard-

ening, and impossible to refine.

To anneal any piece of steel, heat it red-hot; heat it uniformly and heat it

through, taking care not to let the ends and corners get too hot.

As soon as it is hot, take it out of the fire, the sooner the better, and cool it as slowly as possible. A good rule for heating is to heat it at so low a red that when the piece is cold it will still show the blue gloss of the oxide that was put there by the hamer or the rolls.

Steel annealed in this way will cut very soft; it will harden very hard, without cracking; and when tempered it will be very strong, nicely refined,

and will hold a keen, strong edge,

Tempering.-Tempering steel is the act of giving it, after it has been shaped, the hardness necessary for the work it has to do. This is done by first hardening the piece, generally a good deal harder than is necessary, and then toughening it by slow heating and gradual softening until it is just right for work.

A piece of steel properly tempered should always be finer in grain than the bar from which it is made. If it is necessary, in order to make the piece as hard as is required, to heat it so hot that after being hardened the grain will be as coarse as or coarser than the grain in the original bar, then the steel

itself is of too low carbon for the desired work.

If a great degree of hardness is not desired, as in the case of taps, and most tools of complicated form, and it is found that at a moderate heat the tools are too hard and are liable to crack, the smith should first use a lower heat in order to save the tools already made, and then notify the steelmaker that his steel is too high, so as to prevent a recurrence of the trouble.

For descriptions of various methods of tempering steel, see "Tempering of Metals," by Joshua Rose, in App. Cyc. Mech., vol. ii. p. 883; also, "Wrinkles and Recipes," from the Scientific American. In both of these works Mr. Rose gives a "color scale," lithographed in colors, by which the color to which the temper is to be drawn for different tools is shown. The following is a list of the tools in their order on the color scale, together with the approximate color and the temperature at which the color appears on brightened steel when heated in the air:

Scrapers for brass; very pale yel-

low, 430° F. Steel-engraving tools. Slight turning tools, Hammer faces. Planer tools for steel. Ivory-cutting tools.

Planer tools for iron. Paper-cutters. Wood-engraving tools.

Bone cutting tools. Milling-cutters; straw yellow, 460° F.

Wire-drawing dies. Boring-cutters. Leather-cutting dies.

Screw-cutting dies, Inserted saw-teeth. Taps.

Rock-drills. Chasers. Punches and dies.

Penknives. Reamers. Half-round bits.

Planing and moulding cutters. Stone-cutting tools; brown yellow,

500° F. Gouges.

Hand-plane irons. Twist-drills.

Flat drills for brass. Wood-boring cutters.

Drifts. Coopers' tools. Edging cutters; light purple, 530° F.

Augers. Dental and surgical instruments.

Cold chisels for steel. Axes; dark purple, 550° F.

Gimlets. Cold chisels for cast iron,

Saws for bone and ivory. Needles. Firmer-chisels.

Hack-saws.

Framing-chisels.
Cold chisels for wrought iron. Moulding and planing cutters to be

filed. Circular saws for metal. Screw-drivers.

Springs. Saws for wood. Dark blue, 570° F.

Pale blue, 610° Blue tinged with green, 630°.

## MECHANICS.

### FORCE, STATICAL MOMENT, EQUILIBRIUM, ETC.

MECHANICS is the science that treats of the action of force upon bodies.

A Force is anything that tends to change the state of a body with respect to rest or motion. If a body is at rest, anything that tends to put it in motion is a force; if a body is in motion, anything that tends to change either its direction or its rate of motion is a force.

A force should always mean the pull, pressure, rub, attraction (or repulsion) of one body upon another, and always implies the existence of a simultaneous equal and opposite force exerted by that other body on the first body, i.e., the reaction. In no case should we call anything a force unless we can conceive of it as capable of measurement by a spring-balance, and are able to say from what other body it comes. (I. P. Church.)

Forces may be divided into two classes, extraneous and molecular; extraneous forces act on hodies from without; molecular forces are exerted be-

tween the neighboring particles of bodies.

Extraneous forces are of two kinds, pressures and moving forces: pressures simply tend to produce motion; moving forces actually produce motion. Thus, if gravity act on a fixed body, it creates pressure; if on a free

motion. Thus, if gravity act on a fixed body, it preduces motion. Molecular forces are of two kinds, attractive and repellent: attractive forces tend to bind the particles of a body together; repellent forces tend to thrust them assunder. Both kinds of molecular forces are continually exerted between the molecules of bodies, and on the predominance of one or the other depends the physical state of a body, as solid, liquid, or gaseous. The Unit of Force used in engineering, by English writers, is the

pound avoirdupois. (For some scientific purposes, as in electro-dynamics, forces are sometimes expressed in "absolute units." The absolute unit of force is that force which acting on a unit of mass during a unit of time produces a unit of velocity; in English measures, that force which acting on the mass whose weight is one pound in London will in one second produce a the mass whose weight is one pound in London with in one second produce velocity of one foot per second = 1 + \$2.187 of the weight of the standard pound avoirdupois at London. In the French C. G. S. or centimetre-gramme second system it is the force which acting on the mass whose weight is one gramme at Paris will produce in one second a velocity of one centimetre per second. This unit is called a "dyne" = 1/\$281 gramme at Paris.)

Inertia is that property of a body by virtue of which it tends to continue in the state of rest or motion in which it may be placed, until acted on by

some force.

Newton's Laws of Motion. -ist Law. If a body be at rest, it will remain at rest; or if in motion, it will move uniformly in a straight line till

acted on by some force.

If a body be acted on by several forces, it will obey each as though the others did not exist, and this whether the body be at rest or in motion.

3d Law. If a force act to change the state of a body with respect to rest or motion, the body will offer a resistance equal and directly opposed to the force. Or, to every action there is opposed an equal and opposite reaction, **Graphic Representation of a Force.**—Forces may be represented geometrically by straight lines, proportional to the forces. A force

is given when we know its intensity, its point of application, and the direction in which it acts. When a force is represented by a line, the length of the line represents its intensity; one extremity represents the point of application; and an arrow-head at the other extremity shows the direction of the force.

Composition of Forces is the operation of finding a single force whose effect is the same as that of two or more given forces. The required

force is called the resultant of the given forces.

Resolution of Forces is the operation of finding two or more forces whose combined effect is equivalent to that of a given force. The required

The resultant of two forces applied at a point, and acting in the same direction, is equal to the sum of the forces. If two forces act in opposite directions, their resultant is equal to the resultant is equal to the sum of the forces. direction of the greater.

If any number of forces be applied at a point, some in one direction and others in a contrary direction, their resultant is equal to the sum of those that act in one direction, diminished by the sum of those that act, in the opposite direction; or, the resultant is equal to the algebraic sum of the components.

Parallelogram of Forces. - If two forces acting on a point be rep-Parallelogram of Forces, in two forces acong on a point or resented in direction and intensity by adjacent sides of a parallelogram, their resultant will be represented by that diagonal of the parallelogram which passes through the point. Thus OR, Fig.

Fig. 88.

88, is the resultant of OQ and OP. Polygon of Forces.-If several forces are applied at a point and act in a single plane, their resultant is found as follows:

Through the point draw a line representing the first force; through the extremity of this draw a line representing the second force; and so on, throughout the system; finally, draw a line from the starting-point to the extremity of the last line

drawn, and this will be the resultant required. Suppose the body A, Fig. 89, to be urged in the directions A1, A2, A3, A4, and A5 by forces which are to each other as the lengths of those lines. Suppose these forces to act successively and the body to first move from A to 1; the second force A2 then acts and finding the body at 1 would take it to 2; the third force would then carry it to 3', the fourth to 4', and the fifth to 5'. The line 45' represents in magnitude and direction the resultant of all the forces considered. If there had

been an additional force, Ax, in the group. the body would be returned by that force to its original position, supposing the forces to act successively, but if they had acted simultaneously the body would never 2 have moved at all; the tendencies to motion balancing each other. It follows, therefore, that if the several

forces which tend to move a body can be represented in magnitude and direction by the sides of a closed polygon taken in order, the body will remain at rest; but if the forces are represented by the sides of an open polygon, the body will move and the direction will be represented by the straight line which closes the polygon.

Fig. 89.

Twisted Polygon.—The rule of the polygon of forces holds true even when the forces are not in one plane. In this case the lines A1, 1-2', 2'-3', etc., form a twisted polygon, that is, one whose sides are not in one plane.

Parallelopipedon of Forces.—If three forces acting on a point be

represented by three edges of a parallelopiped on which meet in a common point, their resultant will be represented by the diagonal of the parallelopipedon that passes through their common point. OM is the result-

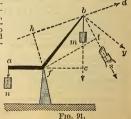
Thus OR, Fig. 90, is the resultant of OQ, OS, and OP. ant of OP and OQ, and OR is the resultant of OM and OS.

Moment of a Force.—The mo-

ment of a force (sometimes called statical moment), with respect to a point, is the product of the force by the perpendicular distance from the point to the direction of the force. point is called the centre of mo-



FIG. 90,



ments; the perpendicular distance is the lever-arm of the force; and the moment itself measures the tendency of the force to produce rotation about the centre of moments.

If the force is expressed in pounds and the distance in feet, the moment is expressed in foot-pounds. It is necessary to observe the distinction between foot-pounds of statical moment and foot-pounds of work or energy.

(See Work.)

In the bent lever, Fig. 91 (from Trautwine), if the weights n and m represent forces, their moments about the point f are respectively  $n \times af$  and  $m \times fc$ . If instead of the weight m a pulling force to balance the weight in  $x \neq 0$ . It is a plant of the restaurance the weight m is applied in the direction bs, or by or bd, s, y, and d being the amounts of these forces, their respective moments are  $s \times ft$ ,  $y \times fb$ ,  $d \times fh$ . If the forces acting on the lever are in equilibrium it remains at rest, and the moments on each side of f are equal, that is,  $n \times af = m \times fc$ , or  $s \times ft$ ,

or  $y \times fb$ , or  $d \times hf$ .

The moment of the resultant of any number of forces acting together in the same plane is equal to the algebraic sum of the moments of the forces

taken separately.

Statical Moment. Stability.—The statical moment of a body is the product of its weight by the distance of its line of gravity from some assumed line of rotation. The line of gravity is a vertical line drawn from its centre of gravity through the body. The stability of a body is that resistance which its weight alone enables it to oppose against forces tending to overturn it or to slide it along its foundation.

To be safe against turning on an edge the moment of the forces tending to overturn it, taken with reference to that edge, must be less than the statical moment. When a body rests on an inclined plane, the line of gravity being vertical, falls toward the lower edge of the body, and the condition of its not being overturned by its own weight is that the line of gravity must fall within this edge. In the case of an inclined tower resting on a plane the same condition holds—the line of gravity must fall within the base. condition of stability against sliding along a horizontal plane is that the horcondition of stability against shding along a horizontal plane is that the horizontal component of the force exerted tending to cause it to slide shall be less than the product of the weight of the body into the coefficient of friction between the base of the body and its supporting plane. This coefficient of friction is the tangent of the angle of repose, or the maximum angle at which the supporting plane might be raised from the horizontal before the body would begin to slide. (See Friction.)

The Stability of a Dam against overturing about its lower edge.

is calculated by comparing its statical moment referred to that edge with the resultant pressure of the water against its upper side. The horizontal pressure on a square foot at the bottom of the dam is equal to the weight of a column of water of one square foot in section, and of a height equal to the distance of the bottom below water-level; or, if H is the height, the pressure at the bottom per square foot =  $62.4 \times H$  lbs. At the water-level the pressure is zero, and it increases uniformly to the bottom, so that the sum of the such as zero, and in increases uniformly to the bottom, so that the sum of the pressures on a vertical strip one foot in breadth may be represented by the area of a triangle whose base is  $62.4 \times H$  and whose altitude is H, or  $62.4 H^2 + 2$ . The centre of gravity of a triangle being  $\frac{1}{2}6$  of its altitude, the resultant of all the horizontal pressures may be taken as equivalent to the sum of the pressures acting at  $\frac{1}{2}H$ , and the moment of the sum of the pressures is therefore  $62.4 \times H^3 + 6$ .

Parallel Forces. - If two forces are parallel and act in the same direction, their resultant is parallel to both, and lies between them, and the intensity of the resultant is equal to the sum of the intensities of the two forces. Thus in Fig. 91 the resultant of the forces n and m acts vertically downward at f, and is equal to n+m.

If two parallel forces act at the extremities of a straight line and in the

same direction, the resultant divides the line joining the points of application of the components, inversely as the components. Thus in Fig. 91, m:n:of the components, inversely as the components, of: fc; and in Fig. 92, P: Q:: SN: SM.

The resultant of two parallel forces acting in opposite directions is parallel

to both, lies without both, on the side and in the direction of the greater, and its intensity is equal to the difference of the intensities of the two forces.



have no resultant. Two such forces constitute what is called a couple.

The tendency of a couple is to produce rotation; the measure of this tendency. called the moment of the couple, is the

product of one of the forces by the distance between the two. Since a couple has no single resultant, no single force can balance a couple. To prevent the rotation of a body acted on by a couple the application of two other forces is required, forming a second couple. Thus in Fig. 94, P and Q forming a couple, may be balanced by a second couple formed by R and S. The

point of application of either R or S may be a fixed pivot or axis.

Moment of the couple PQ = P(c+b+a) =moment of RS = Rb. Also, P + R = Q + S. The forces R and S need not be parallel to P

and Q, but if not, then their components parallel to PQ are to be taken instead of the forces themselves.

Equilibrium of Forces.-A system of forces applied at points of a solid body will be in equilibrium when they have no tendency to produce motion, either of translation or of rotation



The conditions of equilibrium are: 1. The algebraic sum of the components of the forces in the direction of any three rectangular axes must be separately equal to 0.

2. The algebraic sum of the moments of the forces, with respect to any

three rectangular axes, must be separately equal to 0.

If the forces lie in a plane: 1. The algebraic sum of the components of the forces, in the direction of any two rectangular axes, must be separately equal to 0.

2. The algebraic sum of the moments of the forces, with respect to any

point in the plane, must be equal to 0. If a body is restrained by a fixed axis, as in case of a pulley, or wheel and axle, the forces will be in a equilibrium when the algebraic sum of the moments of the forces with respect to the axis is equal to 0.

### CENTRE OF GRAVITY.

The centre of gravity of a body, or of a system of bodies rigidly connected together, is that point about which, if suspended, all the parts will be in equilibrium, that is, there will be no tendency to rotation. It is the point through which passes the resultant of the efforts of gravitation on each of the elementary particles of a body. In bodies of equal heaviness through-

out, the centre of gravity is the centre of magnitude.

(The centre of gravity is the centre of magnitude.

(The centre of magnitude of a figure is a point such that if the figure be divided into equal parts the distance of the centre of magnitude of the whole figure from any given plane is the mean of the distances of the centres, of magnitude of the several equal parts from that plane.)

If a body be suspended at its centre of gravity, it will be in equilibrium in l positions. If it be suspended at a point out of its centre of gravity, it all positions. will swing into a position such that its centre of gravity is vertically beneath its point of suspension.

To find the centre of gravity of any plane figure mechanically, suspend the figure by any point near its edge, and mark on it the direction of a plumb-line hung from that point; then suspend it from some other point, and again mark the direction of the plumb-line in like manner. Then the centre of gravity of the surface will be at the point of intersection of the

two marks of the plumb-line.

The Centre of Gravity of Regular Figures, whether plane or solid, is the same as their geometrical centre; for instance, a straight line, parallelogram, regular polygon, circle, circular ring, prism, cylinder, sphere, spheroid, middle frustums of spheroid, etc. Of a triangle: On a line drawn from any angle to the middle of the opposite side, at a distance of one third of the line from the side; or at the intersection of such lines drawn from any two angles.

Of a trapezium or trapezoid: Draw the two diagonals, dividing it into four triangles. Draw lines joining the centres of gravity of opposite pairs of triangles, and their intersection is the centre of gravity.

Of a sector of a circle: On the radius which bisects the arc,  $\frac{2}{2} \frac{cr}{l}$  from the centre, c being the chord, r the radius, and l the arc.

Of a semicircle: On the middle radius, .4244r from the centre. Of a quadrant: On the middle radius, .6002r from the centre.

Of a segment of a circle:  $c^3 + 12a$  from the centre. c = chord, a = area. Of a parabolic surface: In the axis, 3/5 of its length from the vertex.

Of a semi-parabola (surface): 3/5 length of the axis from the vertex, and 3% of the semi-base from the axis.

Of a cone or pyramid: In the axis, ¼ of its length from the base. Of a paraboloid: In the axis, ¾ of its length from the vertex.

Of a cylinder, or regular prism; In the middle point of the axis, Of a frustum of a cone or pyramid; Let a = length of a line drawn from the vertex of the cone when complete to the centre of gravity of the base, and a' that portion of it between the vertex and the top of the frustum; then distance of centre of gravity of the frustum from centre of gravity of its a 8a' 8a'.

distance of centre of gravity of the frustum from centre of gravity of its base  $=\frac{a}{4}-\frac{3a''^2}{4(a^2+aa'+a'^2)}$ . For two bodies, fixed one at each end of a straight bar, the common centre of gravity is in the bar, at that point which divides the distance between their respective centres of gravity in the inverse ratio of the weights. In this solution the weight of the bar is neglected. But it may be taken as a third body, and allowed for as in the following directions: For more than two bodies connected in one system: Find the common centre of gravity of two of them; and find the common centre of these two jointly with a third body, and so on to the last body of the group. Another method, by the principle of moments: To find the centre of gravity of a system of bodies, or a body consisting of several parts, whose several centres are known. If the bodies are in a plane, refer their several centres to two rectangular co-ordinate axes. Multiply each weight by its distance from one of the axes, add the products, and divide the sum by the

distance from one of the axes, add the products, and divide the sum by the sum of the weights: the result is the distance of the centre of gravity from that axis. Do the same with regard to the other axis. If the bodies are not in a plane, refer them to three planes at right angles to each other, and determine the mean distance of the sum of the weights from each of the three planes.

#### MOMENT OF INERTIA.

The moment of inertia of the weight of a body with respect to an axis is the algebraic sum of the products obtained by multiplying the weight of each elementary particle by the square of its distance from the axis. If the moment of inertia with respect to any axis = I, the weight of any element of the body = v, and its distance from the axis = r, we have  $I = \sum (ur^2)$ . The moment of inertia varies, in the same body, according to the position of the axis. It is the least possible when the axis pages through the axis of th

of the axis. It is the least possible when the axis passes through the centre of gravity. To find the moment of inertia of a body, referred to a given axis, divide the body into small parts of regular figure. Multiply the weight axis, divide the body much shall part by the square of the distance of its centre of gravity from the of each part by the square of the moment of inertia. The value of the moment of inertia thus obtained will be more nearly exact, the smaller and more numerous the parts into which the body is divided.

Momenys of Inertia of Regular Solids.—Rod, or bar, of uniform thickness, with respect to an axis perpendicular to the length of the rod,

$$I = W\left(\frac{l^2}{3} + d^2\right), \qquad (1)$$

W = weight of rod, 2l = length, d = distance of centre of gravity from axis. Thin circular plate, axis in its  $I = W\left(\frac{r^2}{4} + d^2\right)$ ; . . . . . . . (2)

r = radius of plate.

Circular plate, axis perpendicular  $\left\{ I = W\left(\frac{r^2}{2} + d^2\right), \ldots, \left(3\right) \right\}$ 

Circular ring, axis perpendicular  $I = W\left(\frac{r^2 + r'^2}{2} + d^2\right)$ , . . . . (4)

r and r' are the exterior and interior radii of the ring.

Cylinder, axis perpendicular to the axis of the cylinder,  $1 = W\left(\frac{r^2}{4} + \frac{l^2}{8} + d^2\right)$ , . . . . (5)

r = radius of base, 2l = length of the cylinder.

By making d=0 in any of the above formulæ we find the moment of inartia for a parallel exist through the contra of granity

inertia for a parallel axis through the centre of gravity. The moment of inertia,  $\Sigma m^2$ , numerically equals the weight of a body which, if concentrated at the distance unity from the axis of rotation, would require the same work to produce a given increase of angular velocity that the actual body requires. It bears the same relation to angular acceleration which weight does to linear acceleration (Rankine). The term moment of inertia is also used in regard to areas, as the cross-sections of beams under strain. In this case  $I = \Sigma ar^2$ , in which a is any elementary area, and r its distance from the centre. (See Moment of Inertia, under Streugth of Materials, p. 347.)

#### CENTRE AND RADIUS OF GYRATION.

The centre of gyration, with reference to an axis, is a point at which, if the entire weight of a body be concentrated, its moment of inertia will remain unchanged; or, in a revolving body, the point in which the whole weight of the body may be conceived to be concentrated, as if a pound of platinum were substituted for a pound of revolving feathers, the angular velocity and the accumulated work remaining the same. The distance of this point from the axis is the radius of gyration. If W = the weight of a body,  $I = \Sigma wr^2 =$  its moment of inertia, and k = its radius of gyration,

$$I = Wk^2 = \Sigma wr^2; \quad k = \sqrt{\frac{\Sigma wr^2}{W}}.$$

The moment of inertia = the weight × the square of the radius of gyration. To find the radius of gyration divide the body into a considerable number of equal small parts—the more numerous the more nearly exact is the result.—then take the mean of all the squares of the distances of the parts from the axis of revolution, and find the square root of the mean square. Or, if the moment of inertia is known, divide it by the weight and extract the square root. For radius of gyration of an area, as a cross-section of a beam, divide the moment of inertia of the area by the area and extract the square root.

The radius of gration is the least possible when the axis passes through the centre of gravity. This minimum radius is called the principal radius of gyration. If we denote it by k and any other radius of gyration by k', we have for the five cases given under the head of moment of inertia above the following values:

(1) Rod, axis perpento 
$$\begin{cases} k = l \sqrt{\frac{1}{2}}; & k' = \sqrt{\frac{l^2}{3} + d^2}. \end{cases}$$

"(2) Circular plate, axis 
$$\left\{k = \frac{r}{2}; \ k' = \sqrt{\frac{r^2}{4} + d^2}.\right\}$$

(3) Circular plate, axis perpen, to plane, 
$$k = r \sqrt{\frac{1}{2}}; \quad k' = \sqrt{\frac{r^2}{2} + d^2}.$$

(4) Circular ring, axis perpent to plane, 
$$k = \sqrt{\frac{r^2 + r'^2}{2}}; k' = \sqrt{\frac{r^2 + r'^2}{2} + d^2}.$$

(5) Cylinder, axis perpent to length, 
$$k = \sqrt{\frac{r^2}{4} + \frac{l^2}{3}}; \quad k' = \sqrt{\frac{r^2}{4} + \frac{l^2}{3} + d^2}.$$

# Principal Radii of Gyration and Squares of Radii of Gyration.

(For radii of gyration of sections of columns, see page 249.)

Surface or Solid.	Rad. of Gyration.	Square of R. of Gyration.
Parallelogram: axis at its base height h " mid-height	.5773h .2886h	$\frac{1}{3}h^2$ $1/12h^2$
length l, or thin rectang, plate axis at end	.5773 <i>l</i> .2886 <i>l</i>	$\frac{1/3l^2}{1/12l^2}$
Rectangular prism: axes $2a$ , $2b$ , $2c$ , referred to axis $2a$ Parallelopiped: length $l$ , base $b$ , axis $l$	.577 $\sqrt{b^2 + c^2}$ .289 $\sqrt{4l^2 + b^2}$	$(b^2 + c^2) \div 3$ $4l^2 + b^2$
at one end, at mid-breadth	.289 $\sqrt{h^2 + h'^2}$	$ \begin{array}{c} 12 \\ (h^2 + h'^2) \div 12 \\ h^2 \div 6 \end{array} $
very thin, side = $h$ , "  Thin rectangular tube: sides $b$ , $h$ , axis mid-length	$.289h\sqrt{\frac{\overline{h+3b}}{\overline{h+b}}}$	$\frac{h^2 \div b}{12} \cdot \frac{h+3b}{h+b}$
Thin circ. plate: rad. r, diam. h, ax. diam. Flat circ. ring: diams. h, h', axis diam.	$ \frac{\frac{1}{2}r}{\frac{1}{4}\sqrt{h^2+h'^2}} $	$ \frac{1}{4}r^2 = h^2 \div 16 \\ (h^2 + h'^2) \div 16 $
Solid circular cylinder: length l, axis diameter at mid-length	.289 $\sqrt{l^2 + 3r^2}$	$\frac{j_2}{12} + \frac{r^2}{4}$
form thickness, or cylinder of any length, referred to axis of cyl Hollow circ. cylinder, or flat ring:	.7071r	1/2r <sup>2</sup>
l, length; R, r, outer and inner radii. Axis, 1, longitudinal axis; 2, diam, at mid-length	.7071 $\sqrt{R^2 + r^2}$ .289 $\sqrt{l^2 + 3(R^2 + r^2)}$	$\begin{vmatrix} (R^2 + r^2) + 2 \\ \frac{l^2}{12} + \frac{R^2 + r^2}{4} \end{vmatrix}$
Same: very thin, axis its diameter	.289 $\sqrt{l^2 + 6R^2}$	$\frac{l^2}{12} + \frac{R^2}{2}$
Circumf. of circle, axis its centre " " diam  Sphere: radius r, axis its diam	.7071r .6325r	1/5r <sup>2</sup> 2/5r <sup>2</sup>
Spheroid: equatorial radius $r$ , revolving polar axis $a$	.6325r	2/5r2
On axis	$.5773r$ $.4472 \sqrt{b^2 + c^2}$	$\frac{\frac{1}{3}r^2}{\frac{b^2+c^2}{5}}$
Spherical shell: radii R, r, revolving on its diam	$.6325 \sqrt{\frac{R^5 - r^5}{R^3 - r^3}}$	$\frac{2R^5 - r^5}{5R^3 - r^3}$
Same: very thin, radius $r$	.81657	2/31-2
axis	.5477r	$0.3r^{2}$

#### CENTRES OF OSCILLATION AND OF PERCUSSION.

Centre of Oscillation.—If a body oscillate about a fixed horizontal axis, not passing through its centre of gravity, there is a point in the line drawn from the centre of gravity perpendicular to the axis whose motion is the same as it would be if the whole mass were collected at that point and allowed to vibrate as a pendulum about the fixed axis. This point is called the centre of oscillation.

The Radius of Oscillation, or distance of the centre of oscillation from the point of suspension = the square of the radius of gyration + distance of the centre of gravity from the point of suspension or axis. The centres of oscillation and suspension are convertible.

If a straight line, or uniform thin bar or cylinder, be suspended at one end, oscillating about it as an axis, the centre of oscillation is at % the length of

the rod from the axis. If the point of suspension is at 1/3 the length from the end, the centre of oscillation is also at 2/3 the length from the axis, that is, it is at the other end. In both cases the oscillation will be performed in the same time. If the point of suspension is at the centre of gravity, the length of the equivalent simple pendulum is infinite, and therefore the time of vibration is infinite.

For a sphere suspended by a cord, r = radius, h = distance of axis of motion from the centre of the sphere, h' = distance of centre of oscillation

from centre of the sphere,  $l = \text{radius of oscillation} = h + h' = h + \frac{2}{5} \frac{r^2}{h}$ .

If the sphere vibrate about an axis tangent to its surface, h = r, and l = r $+ \frac{2}{5r}$ . If h = 10r,  $l = 10r + \frac{r}{95}$ .

Lengths of the radius of oscillation of a few regular plane figures or thin plates, suspended by the vertex or uppermost point,

1st. When the vibrations are flatwise, or perpendicular to the plane of the figure:

In an isosceles triangle the radius of oscillation is equal to 34 of the height

of the triangle.
In a circle, % of the diameter.
In a parabola, 5/7 of the height.
2d. When the vibrations are edgewise, or in the plane of the figure:

an eircle the radius of oscillation is 4 of the diameter. In a rectangle suspended by one angle, \$\frac{2}{3}\$ of the diagnost.

In a parabola, suspended by the vertex, 5\frac{7}{3}\$ of the height, plus \$\frac{1}{3}\$ of the

parameter.

In a parabola, suspended by the middle of the base, 4/7 of the height plus 1/2 the parameter.

Centre of Percussion.—The centre of percussion of a body oscillating about a fixed axis is the point at which, if a blow is struck by the body, the percussive action is the same as if the whole mass of the body were concentrated at the point. This point is identical with the centre of oscillation.

#### THE PENDULUM.

A body of any form suspended from a fixed axis about which it oscillates by the force of gravity is called a compound pendulum. The ideal body concentrated at the centre of oscillation, suspended from the centre of suspension by a string without weight, is called a simple pendulum. This equivalent simple pendulum has the same weight as the given body, and also the same moment of inertia, referred to an axis passing through the point of suspension, and it oscillates in the same time.

The ordinary pendulum of a given length vibrates in equal times when the

angle of the vibrations does not exceed 4 or 5 degrees, that is, 2° or 2½° each side of the vertical. This property of a pendulum is called its isochronism. The time of vibration of a pendulum varies directly as the square root of the length, and inversely as the square root of the acceleration due to gravity at the given latitude and elevation above the earth's surface. If T= the time of vibration, t= length of the simple pendulum, g= accel-

eration = 32.16,  $T = \pi \sqrt{\frac{l}{g}}$ ; since  $\pi$  is constant,  $T \propto \frac{\sqrt{l}}{\sqrt{g}}$ . At a given loca-

tion g is constant and  $T \propto \sqrt{l}$ . If l be constant, then for any location

 $T \propto \frac{1}{\sqrt{g}}$ . If T be constant,  $gT^2 = \pi^2 l$ ;  $l \propto g$ ;  $g = \frac{\pi^2 l}{T^2}$ . From this equation

the force of gravity at any place may be determined if the length of the simple pendulum, vibrating seconds, at that place is known. At New York this length is 39.1017 inches = 3.2585 ft., whence g=32.16 ft. At London the length is 39.1393 inches. At the equator 39.0152 or 39.0168 inches, according to different authorities.

Time of vibration of a pendulum of a given length at New York

$$= t = \sqrt{\frac{l}{39.1017}} = \frac{\sqrt{l}}{6.253},$$

t being in seconds and l in inches. Length of a pendulum having a given time of vibration,  $l = t^2 \times 39.1017$  inches.

The time of vibration of a pendulum may be varied by the addition of a weight at a point above the centre of suspension, which counteracts the lower weight, and lengthens the period of vibration. By varying the height of the upper weight the time is varied.

To find the weight of the upper bob of a compound pendulum, vibrating seconds, when the weight of the lower bob, and the distances of the weights from the point of suspension are given;

$$w = W \frac{(39.1 + D) - D^2}{(39.1 + d) + d^2}.$$

W = the weight of the lower bob, w = the weight of the upper bob; D = the distance of the lower bob and d = the distance of the upper bob from the point of suspension, in inches.

Thus, by means of a second bob, short pendulums may be constructed to

vibrate as slowly as longer pendulums.

By increasing w or d until the lower weight is entirely counterbalanced. the time of vibration may be made infinite.

Conical Pendulum. - A weight suspended by a cord and revolving at a uniform speed in the circumference of a circular horizontal plane as a uniform speed in the Circumference of a Greunar normalization whose radius is  $r_i$  the distance of the plane below the point of suspension being  $h_i$  is held in equilibrium by three forces—the tension in the cord, the centrifugal force, which tends to increase the radius  $r_i$  and the force of gravity acting downward. If v = the velocity in feet per second, the centre of gravity of the weight, as it describes the circumference, g = 32.16, and r and h are taken in feet, the time in seconds of performing one revolution is

$$t = \frac{2\pi r}{v} = 2\pi \sqrt{\frac{h}{g}}; \quad h = \frac{gt^2}{4\pi^2} = .8146t^2.$$

If t=1 second, h=.8146 foot =9.775 inches. The principle of the conical pendulum is used in the ordinary fly-ball governor for steam-engines. (See Governors.)

#### CENTRIFUGAL FORCE.

A body revolving in a curved path of radius = R in feet exerts a force, called centrifugal force, F, upon the arm or cord which restrains it from moving in a straight line, or "lying off at a tangent." If W = weight of the body in pounds, N = number of revolutions per minute, V = linear electric field the centre of gravity of the body, in feet per second, g = 32.16,

$$v = \frac{2\pi RN}{60}$$
;  $F = \frac{Wv^2}{aR} = \frac{Wv^2}{32.16R} = \frac{W4\pi^2 RN^2}{3600g} = \frac{WRN^2}{2933} = .0003410 WRN^2$  lbs.

If n = number of revolutions per second,  $F = 1.2276WRn^2$ . (For centrifugal force in fly-wheels, see Fly-wheels.)

# VELOCITY, ACCELERATION, FALLING BODIES.

Velocity is the rate of motion, or the distance passed over by a body in

a given time.

If s = space in feet passed over in t seconds, and v = velocity in feet per second, if the velocity is uniform,

$$v = \frac{s}{t}$$
;  $s = vt$ ;  $t = \frac{s}{t}$ .

If the velocity varies uniformly, the mean velocity  $v_0 = \frac{v_1 + v_2}{2}$ , in which  $v_1$  is the velocity at the beginning and  $v_2$  the velocity at the end of the time  $t_2$ 

**Acceleration** is the change in velocity which takes place in a unit of time. Unit of acceleration =a=1 foot per second. The second rescond rescond rescond respectively, the acceleration is a constant quantity, and

If the body start from rest,  $v_1 = 0$ ; then

$$v_0 = \frac{v^2}{2}; \quad v_2 = 2v_0; \quad a = \frac{v_2}{t}; \quad v_2 = at; \quad v_2 - at = 0; \quad t = \frac{v_2}{a}.$$

Combining (1) and (2), we have

$$s = \frac{v_2^2 - v_1^2}{2a}$$
;  $s = v_1 t + \frac{at^2}{2}$ ;  $s = v_2 t - \frac{at^2}{2}$ .

If  $v_1 = 0$ ,  $s = \frac{v_2}{2}t$ .

**Retarded Motion.**—If the body start with a velocity  $v_1$  and come to rest,  $v_2 = 0$ ; then  $s = \frac{v_1}{c_0}t$ .

In any case, if the change in velocity is v,

$$s = \frac{v}{2}t; \quad s = \frac{v^2}{2a}; \quad s = \frac{a}{2}t^2.$$

For a body starting from or ending at rest, we have the equations

$$v = at; \ s = \frac{v}{2}t; \ s = \frac{at^2}{2}; \ v^2 = 2as.$$

**Falling Bodies.**—In the case of falling bodies the acceleration due to gravity is 32.16 feet per second in one second, =g. Then if v = velocity acquired at the end of t seconds, or final velocity, and h = height or space in feet passed over in the same time,

$$v = gt = 32.16t = \sqrt{2gh} = 8.02 \sqrt{h} = \frac{2h}{t};$$

$$h = \frac{gt^2}{2} = 16.08t^2 = \frac{v^2}{2g} = \frac{v^2}{64.32} = \frac{v}{2};$$

$$t = \frac{v}{g} = \frac{v}{29.16} = 4\sqrt{\frac{2h}{g}} = \frac{4\sqrt{h}}{4.01} = \frac{2h}{g};$$

 $u = \text{space fallen through in the } T \text{th second} = g(T - \frac{1}{2}).$ 

**Value of** g.—The value of g increases with the latitude, and decreases with the elevation. At the latitude of Philadelphia,  $40^\circ$ , its value is 32.16. At the sea-level, Everett gives g=32.173-.082 cos 2 lat. -.000003 height in feet.

Values of  $\sqrt{2g}$ , calculated by an equation given by C. S. Pierce, are given in a table in Smith's Hydraulics, from which we take the following: Latitude....... 0° 10° 20° 30° 40° 50° 60°

Value of  $\sqrt{2g}$ . 8.0112 8.0118 8.0137 8.0165 8.0199 8.0235 8.0269

The value of  $\sqrt{2g}$  decreases about .0004 for every 1000 feet increase in ele-

vation above the sea-level.

For all ordinary calculations for the United States, g is generally taken at \$20.15 and \$20.25 pergetical limit.

From the above formula for falling bodies we obtain the following: During the first second the body starting from a state of rest (resistance of the air neglected) falls g+2=16.08 feet; the acquired velocity is g=32.16 ft. per sec.; the distance fallen in two seconds is  $h=\frac{gt^2}{3}=16.08\times 4=$ 

64.32 ft.; and the acquired velocity is v=gt=64.32 ft. The acceleration, or increase of velocity in each second, is constant, and is 32.16 ft. per sec. Solving the equations for different times, we find for

Total height of fall,  $h = \frac{32.16}{2} \times 1 = 4 = 9 = 16 = 25 = 36$ 

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Fig. 95 represents graphically the velocity, space, etc., of a body falling for six seconds. The vertical line at the left is h u v t the time in seconds, the horizontal lines represent one half the acquired velocities at the end of each second. The area of 1 1 2 1''the small triangle at the top represents the height fallen through in the first  $second = \frac{1}{2}g = 16.08$  feet, and each of the other triangles is an equal space. number of triangles between each pair of horizontal lines represents the height of fall in each second, and the number of triangles between any horizontal line and the top is the total height fallen during The figures under h, u, and v the time. adjoining the cut are to be multiplied by 16.08 to obtain the actual velocities and

10 5" heights for the given times. Angular and Linear Velocity

of a Turning Body.-Let r = radius of a 36 12 6" turning body in feet, n = number of revo-Fig. 95. lutions per minute, v = linear velocity of a point on the circumference in feet per second, and 60v = velocity in feetper minute.

 $v = \frac{2\pi rn}{60}$ ,  $60v = 2\pi rn$ .

Angular velocity is a term used to denote the angle through which any radius of a body turns in a second, or the rate at which any point in it having a radius equal to unity is moving, expressed in feet per second. The unit of angular velocity is the angle which at a distance = radius from the centre is subtended by an arc equal to the radius. This unit angle = degrees = 57.3°.  $2\pi \times 57.3^{\circ} = 360^{\circ}$ , or the circumference. If A = angularvelocity, v = Ar,  $A = \frac{v}{r} = \frac{2\pi n}{60}$ .

Height Corresponding to a Given Acquired Velocity.

Velocity.	Height.	Velocity.	Height.	Velocity.	Height.	Velocity.	Height.	Velocity.	Height.	Velocity.	Height.
feet p.sec25 .50 .50 1.25 1.00 1.25 2.5 3 3.5 4 4.5 5 6 7 8 9	feet0010 .0039 .0087 .016 .024 .035 .048 .062 .097 .140 .190 .248 .314 .388 .559 .761	feet p.sec. 13 14 15 16 17 18 20 21 22 23 24 25 26 27 28 29 30	feet. 2.62 3.04 3.49 3.98 4.49 5.61 6.22 6.85 7.52 8.21 8.94 9.71 10.5 11.3 12.2 13.1	feet p sec. 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51	feet. 17.9 19.0 20.1 21.3 32.4 23.6 24.9 26.1 27.4 28.7 30.1 31.4 32.9 34.3 35.8 37.3 38.9 40.4	feet p.sec. 55 56 57 58 59 60 61 62 63 64 65 66 67 71 72	feet. 47.0 48.8 50.5 50.5 52.3 54.1 56.0 57.9 63.7 67.7 69.8 71.9 76.2 78.4 80.6	feet p.sec. 76 77 78 80 81 82 83 84 85 86 87 88 89 90 91 92 93	feet. 89.8 92.2 94.6 97.0 99.5 102.0 104.5 107.1 112.8 115.0 117.7 1120.4 123.2 125.9 128.7 131.6 134.5	feet p. sec. 97 98 99 100 105 110 130 140 150 175 200 400 500 600 700	feet.  146 149 155 171 188 205 224 263 304 476 622 1309 2488 3887 5597 7618
10 11 12	1.55 1.88 2.24	31 32 33	14.9 15.9 16.9	52 58 54	42.0 43.7 45.3	73 74 75	82.9 85.1 87.5	94 95 96	137.4 140.3 143.3	800 900 1000	9952 -12598 -15547

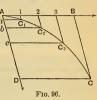
Falling Bodies: Velocity Acquired by a Body Falling a Given Height.

Height.	Velocity.	Height.	Velocity.	Height.	Velocity.	Height.	city.	Height.	Velocity.	Height.	Velocity.
Hei	Velo	Hei	Velo	Hei	Velo	Hei	Velocity	Hei	Velo	Hei	Velo
feet.	feet p.sec. .57	feet.	feet p.sec.	feet.	feet p.sec.	feet.	feet p.sec. 17.9 18.3 18.7 19.0 19.3 19.7	feet.	feet p.sec.	feet.	feet p.sec.
.005	.57	.39	5.01	1 20 1.22 1.24 1.26 1.28 1.30	p.sec. 8.79 8.87 8.94	5. .2	17.9	23.	38.5	72 73	68.1
.010	.98	.40 .41	5.07 5.14	1.24	8.94	.4	18.7	.5 24.	39.3	74	68.5 69.0
.020	1.13	.42	5 20	1.26	9.01	.6	19.0	.5	39.7	75	69.5
.015 .020 .025 .030	1.27	.43 .44	5.26 5.32	1.28	9.08 9.15	.8 6.	19.3	25 26	40.1 40.9	76 77	69.9 70.4
035	.80 .98 1.13 1.27 1.39 1.50 1.60 1.70 1.79 1.88	.45	5.38	1.0%	9.21	.2	20.0	27	41.7	78	70.9
.040 .045 .050	1.60	.46	5.44	1.34	9.29 9.36	.2	20 2	28 29	42.5 43.2	79	71.3
.045	1.70	.47	5.50 5.56	1.36 1.38	9.36	.6	20.6	29 30	43.2	80 81	71.8
.055	1.88	.49	5 61	1.40		7.	21.2	31	44.7	82	72.6
.060	1.97 2.04 2.12 2.20 2.27	.50	5.67 5.78 5.78 5.84	1.42	9.57	.2	21.5	32	45.4	83	73.1
.065	2.04	.51 .52	5.78	1.44 1.46	9.62	.4	21.8 22.1	33 34	46.1	84 85	73.5 74.0
.075	2.20	.53	5.84	1.48	9.77	.8	22.4 22.7	35	47.4	86	74.4
.075	2.27	.54	5.90	1.50	9.82	8.	22.7	36	48.1	87	74.4 74.8 75.3
.085	2.34 2.41	.55 .56	5.95 6.00	1.52 1.54	9.90	.2	23.0 23.3	37 38	48.8 49.4	88 89	75.3
.090 .095 .100	2.47	.57	6.06	1.56	10.0	.6	23.5	39	1 50.1	90	76.1
.100	2.47 2.54	.58	6 11	1.58	10.1	.8	23.8	40	50.7	91	76.5
.105	2.60 2.66	.59 .60	6.16	1.60	10.0 10.1 10.2 10.3	9.	24.1 24.3	41 42	51.4 52.0	92 93	76.9 77.4
.110	2.72	.62	6.16 6.21 6.32	1.70	10.5	.2	24.6	43	52.6	94	77.8
.120	2.72 2.78 2.84	.64	6.42	1.70 1.75	10.6	.6	24.8	44	53.2	95	78.2
.125	2.84	.66 .68	6.52	1.80	10.8	.8	25.1 25.4	45 46	53.8 54.4	96 97	78.6 79.0
14	2.89 3.00 3.11 3.21 3.31	.70	6.61 6.71 6.81 6.90	9	11.4	10. .5 11. .5	26.0	47	55.0	98	79 4
.15	8.11	.70 .72	6.81	$\frac{2.1}{2.2}$	11.4 11.7 11.9	11.	26 6	48	55.6	99	79.8
.16 .17	3.21	.74 .76	6.99	2.2	11.9	.5 12.	27.2 27.8	49 50	56.1 56.7	100 125	79.8 80.2 89.7
.18	3.40	.78	7.09	2.4	12.2 12.4 12.6	.5	28.4	51	57.3	150	98.3
.19	3.50	.80	7.18	2.5	12.6	13.	28.9 29.5	52	57.8	175	106
.20	3.59	.82	7.09 7.18 7.26 7.35	$\frac{2.6}{2.7}$	12.9	.5	29.5	58	58.4	200	114 120
.20 .21 .22	3.76	.84 .86	1 1.44	2.8	12.9 13.2 13.4	14. .5	30.5	54 55	59.0 59.5	225 250	126
99	3.85	.88	7.53	2.8	13.7	15.	31.1	56	60.0	275	133
.24 .25 .26 .27	3.93 4.01	.90 .92	7.61	3.1	13.9	.5 16.	31.6 32.1	57 58	60.6	300 350	139 150
.26	4.09	.94	7.69 7.78	3.2	14.1	.5	32.6	59	61.6	400	160
.27	4 17	.96	7.86 7.94	3.3	114.5	17.	83 1	60	62 1	450	170
.28 .29 .30	4.25 4.32	.98 1.00	7.94 8.02	$\frac{3.4}{3.5}$	14.8 15.0	.5 18.	33.6 34.0	61 62	62.7 63.2	500 550	179 188
.30	4.39	1.02	8.10	3.6	15.2	.5	34.5	63	63.7	600	197
.31	4.47	1.04	8 18	3.7	15 4	19.	35.0	64	64.2	700	212
.31 .32 .33 .34 .35	4.54	1.06 1.08	8.26 8.34 8.41 8.49	3.8	15.6 15.8 16.0	.5 20.	35.4	65 66	64.7	800 900	227 241
.34	4.68	1.10	8.41	4.	16.0	.5	35.9 36.3	67	65.2 65.7	1000	254
.35	4.74	$1.10 \\ 1.12$	8.49	.2	16.4	21.	36.8	68	66.1	2000	359
.36	4.81	1.14 1.16	8.57 8.64	.4	16.8	.5	37.2 37.6	69 70	66.6	3000 4000	439 507
.38	4.94	1.18	8.72	.6	17.2 17.6	.5	38.1	71	67.6	5000	567
		l	1	1		1	1	l	l	l	1

Parallelogram of Velocities.—The principle of the composition and resolution of forces may also be applied to velocities or to distances moved in given intervals of time. Referring to Fig. 88, page 416, if a body at O has a force applied to it which acting alone would give it a velocity represented by OQ per second, and at the same time it is acted on by

another force which acting alone would give it a velocity OP per second, the result of the two forces acting together for one second will carry it to R, OR being the diagonal of the parallelogram of OQ and OP, and the

the result of the two forces acting together for one second with Carry at the resultant velocity. If the two component velocities are uniform, the resultant will be uniform and divergence the will be a straight line; but if either and will be uniform and the two will be a straight line; but if either a superscript one the line will be a straight line; but if either resultant velocities, also the path traversed by a body acted on by two forces, one of which would carry it as a uniform velocity over the intervals 1, 2, 3, B, and the other of which would carry it by an accelerated motion over the intervals a, b, c, D in the same times. At the end of the respective intervals the body will be found at  $C_1$ ,  $C_2$ ,  $C_3$ ,  $C_4$ , and the mean velocity during each interval is represented by the distances between these points. Such a curved path is traversed by a shot, the impelling force from the gun giving it a uniform velocity in the direction the gun is simed, and gravity givdirection the gun is aimed, and gravity giv-ing it an accelerated velocity downward. The path of a projectile is a parabola. The



distance it will travel is greatest when its initial direction is at an angle 45° above the horizontal.

Mass-Force of Acceleration. -The mass of a body, or the quantity of matter it contains, is a constant quantity, while the weight varies according to the variation in the force of gravity at different places. If g = the acceler-

ation due to gravity, and w = weight, then the mass  $m = \frac{w}{w}$ w = mg. Weight here means the resultant of the force of gravity on the particles of a body, such as may be measured by a spring-balance, or by the extension or deflection of a rod of metal loaded with the given weight.

Force has been defined as that which causes, or tends to cause, or to ferrory, motion. It may also be defined (Kennedy's Mechanics of Ma-dehinery) as the cause of acceleration; and the unit of force as the force required to produce unit acceleration in a unit of free mass.

Force equals the product of the mass by the acceleration, or f = ma. Also, if v = the velocity acquired in the time t, ft = mv; f = mv + t; the

acceleration being uniform.

The force required to produce an acceleration of g (that is, 32.16 ft. per sec.) in one second is  $f = mg = \frac{w}{a}g = w$ , or the weight of the body. Also,

$$f=ma=m\frac{v_2-v_1}{t}$$
, in which  $v_2$  is the velocity at the end, and  $v_1$  the velocity at the beginning of the time  $t$ , and  $f=mg=\frac{v}{g}\frac{(v_2-v_1)}{t}=\frac{v}{g}\frac{v_1}{t}$ .

 $\frac{f}{w} = \frac{a}{a}$ ; or, the force required to give any acceleration to a body is to the weight of the body as that acceleration is to the acceleration produced by

gravity. (The weight w is the weight where g is measured.)

gravity. (The weight w is the weight where g is measured.)  $E_{\rm XAMPLE}$ .—Tension in a cord lifting a weight. A weight of 100 lbs. is lifted vertically by a cord a distance of 80 feet in 4 seconds, the velocity uniformly increasing from 0 to the end of the time. What tension must be maintained in the cord? Mean velocity  $v_0 = 20$  ft, per sec.; final velocity  $v_0 = 20$  ft, per sec.; final velocity  $v_0 = 20$  ft.  $v_$ 10 = 31.1 lbs. This is the force required to produce the acceleration only; to it must be added the force required to lift the weight without acceleration, or 100 lbs., making a total of 131.1 lbs.

The Resistance to Acceleration is the same as the force required to pro-

duce the acceleration =  $\frac{w}{v_2 - v_1}$ 

Formulæ for Accelerated Motion .- For cases of uniformly accelerated motion other than those of falling bodies, we have the formulæ already given,  $f = \frac{w}{g}a_1 = \frac{w}{g} \frac{v_2 - v_1}{t}$ . If the body starts from rest,  $v_1 = 0$ ,  $v_2$  =v, and  $f=\frac{w}{g}\frac{v}{t}$ , fgt=wv. We also have  $s=\frac{vt}{2}$ . Transforming and substituting for g its value 32.16, we obtain

$$\begin{split} f &= \frac{wv^2}{64.32s} = \frac{wv}{32.16t} = \frac{ws}{16.08t^2}\,; \quad w = \frac{32.16ft}{v} = \frac{64.32fs}{v^2}\,; \\ s &= \frac{wv^2}{64.32f} = \frac{16.08ft^2}{w} = \frac{vt}{2}\,; \quad v = 8.02\,\sqrt{\frac{fs}{w}} = \frac{32.16ft}{w}\,; \\ t &= \frac{wv}{32.16f} = \frac{1}{4.01}\,\sqrt{\frac{vs}{f}} \end{split}$$

For any change in velocity  $f = w\left(\frac{v_2^2 - v_1^2}{64.32s}\right)$ . (See also Work of Acceleration, under

Motion on Inclined Planes.—The velocity acquired by a body descending an inclined plane by the force of gravity (friction neglected) is equal to that acquired by a body falling freely from the height of the plane. The times of descent down different inclined planes of the same height

vary as the length of the planes.

The rules for uniformly accelerated motion apply to inclined planes. If a is the angle of the plane with the horizontal,  $\sin a =$  the ratio of the height to the length  $=\frac{h}{l}$ , and the constant accelerating force is  $g \sin a$ . The final velocity at the end of t seconds is  $v = qt \sin a$ . The distance passed over in t seconds is  $l = \frac{1}{2}gt^2 \sin a$ . The time of descent is

$$t = \sqrt{\frac{2l}{g \sin a}} = \frac{l}{4.01 \sqrt{h}}.$$

# MOMENTUM, VIS-VIVA.

Momentum, or quantity of motion in a body, is the product of the mass by the velocity at any instant =  $mv = \frac{w}{a}v$ .

Since the moving force = product of mass by acceleration, f = ma; and if the velocity acquired in t seconds = v, or  $a = \frac{v}{t}$ ,  $f = \frac{mv}{t}$ ; ft = mv; that is, the product of a constant force into the time in which it acts equals numer-

ically the momentum.

is like the momentum. Since fl = mv, if t = 1 second mv = f, whence momentum might be defined as numerically equivalent to the number of pounds of force that will stop a moving body in 1 second, or the number of pounds of force which acting during 1 second will give it the given velocity.  $\mathbf{Vis-viva}_3$  or living force, is a term used by early writers on Mechanics to denote the energy stored in a moving body. Some defined it as the product of the mass into the square of the velocity,  $mv^2$ , =  $\frac{w}{v^2}$  others as one half of this quantity or 1/2mv2, or the same as what is now known as energy. The term is now practically obsolete, its place being taken by the word

#### WORK, ENERGY, POWER.

Work is the overcoming of resistance through a certain distance. It is measured by the product of the resistance into the space through which it is overcome. It is also measured by the product of the moving force into the distance through which the force acts in overcoming the resistance. Thus in lifting a body from the earth against the attraction of gravity, the resistance is the weight of the body, and the product of this weight into the height the body is lifted is the work done.

The Unit of Work, in British measures, is the fcot-pound, or the amount of work done in overcoming a pressure or weight equal to one

pound through one foot of space.

energy.

The work performed by a piston in driving a fluid before it, or by a fluid in driving a piston before it, may be expressed in either of the following ways:

> Resistance × distance traversed = intensity of pressure × area × distance traversed; = intensity of pressure × volume traversed.

The work performed in lifting a body is the product of the weight of the

The work perioritied in litting a body is the product of the weight of the body into the height through which its centre of gravity is lifted.

If a machine lifts the centres of gravity of several bodies at once to heights either the same or different, the whole quantity of work performed in so doing is the sum of the several products of the weights and heights; but that quantity can also be computed, by multiplying the sum of all the weights into the height through which their common centre of gravity is lifted. (Rankine.)

rower is the rate at which work is done, and is expressed by the quo-tient of the work divided by the time in which it is done, or by units of work per second, per minute, etc., as foot-pounds per second. The most common unit of power is the horse-power, established by James Watt as the power of a strong London draught-horse to do work during a short interval, and used by him to measure the power of his steam-engines. This unit is 33,000 foot-pounds per minute = 550 foot-pounds per second = 1,980,000 foot-pounds per hour. Power is the rate at which work is done, and is expressed by the quo-

# Expressions for Force, Work, Power, etc.

The fundamental conceptions in Dynamics are:

Force, Time, Space, represented by the letters F, T, S.

**Velocity** = space divided by time,  $V = \frac{S}{T}$ , if V be uniform.

**Work** = product of force into space = FS = W = FVT. (V uniform.) **Power** = rate of work = work divided by time = FS = P = FVT.

force into velocity = FV,

Power exerted for a certain time produces work; PT = FS = FVT = W. Effort is a name applied to a force which acts on a body in the direction of its motion.

Resistance is that which is opposed to a moving force. It is equal and opposite force.

**Horse-power Hours,** an expression for work measured as the product of a power into the time during which it acts = PT. Sometimes it is the summation of a variable power for a given time, or the average power

multiplied by the time.

Energy, or stored work, is the capacity for performing work. It is measured by the same unit as work, that is, in foot-pounds. It may be either potential, as in the case of a body of water stored in a reservoir, either potential, as in the case of a body of water stored in a reservoir, capable of doing work by means of a water-wheel, or actual, sometimes called kinetic, which is the energy of a moving body. Potential energy is measured by the product of the weight of the stored body into the distance through which it is capable of acting, or by the product of the pressure it exerts into the distance through which that pressure is capable of acting. Potential energy may also exist as stored heat, or as stored chemical energy, as in fuel, gunpowder, etc., or as electrical energy, the measure of these energies being the amount of work that they are capable of performing. Actual energy of a moving body is the work which it is capable of performing arginst a retarding resistance hefore being brought to rest, and is equal to against a retarding resistance before being brought to rest, and is equal to the work which must be done upon it to bring it from a state of rest to its actual velocity.

The measure of actual energy is the product of the weight of the body into the height from which it must fall to acquire its actual velocity. If v = the velocity in feet per second, according to the principle of falling bodies,

h, the height due to the velocity =  $\frac{v^2}{2g}$ , and if w = the weight, the energy =

 $\frac{w}{2q} = wh$ . As the quantity  $\frac{w}{q}$  is called the mass = m, energy is equal to half the mass into the square of the velocity =  $\frac{1}{2}mv^2$ . Since energy is the capacity for performing work, the units of work and energy are equivalent, or FS =

 $\frac{1}{2}mv^2 = \frac{wv^2}{2a} = wh$ . Energy exerted = work done.

The actual energy of a rotating body whose angular velocity is A and moment of inertia  $\sum wr^2 = I$  is  $\frac{A^2}{2g}$ , that is, the product of the moment of inertia into the height due to the velocity, A, of a point whose distance from the axis of rotation is unity; or it is equal to  $\frac{wr^2}{2g}$ , in which w is the weight of

the body and v is the velocity of the centre of gyration.

Work of Acceleration.—The work done in giving acceleration to a body is equal to the product of the force producing the acceleration, or of the resistance to acceleration, into the distance moved in a given time. This force, as already stated equals the product of the mass into the acceleration, or  $f=ma=\frac{v}{g}\frac{v_2-v_1}{t}$ . If the distance traversed in the time t=s, then work  $=fs=\frac{v}{g}\frac{v_2-v_1}{t}s$ . Example.—What work is required to move a body weighing 100 lbs. horizontally a distance of 80 ft. in 4 seconds, the velocity uniformly increasing,

friction neglected ?

fraction neglected? Mean velocity  $v_0 = 20$  ft. per second; final velocity  $v_2 = 2v_0 = 40$ ; initial velocity  $v_1 = 0$ ; acceleration,  $a = \frac{v_2 - v_0}{t} = \frac{40}{40} = 10$ ; force  $= \frac{100}{g} = \frac{100}{32.16} \times 10 = 31.1$  lbs.; distance 80 ft.; work  $= fs = 31.1 \times 80 = 2488$  foot-pounds. The energy stored in the body moving at the final velocity of 40 ft. per

second is

$$\frac{1}{2}mv^2 = \frac{1}{2}\frac{w}{a}v^2 = \frac{100 \times 40^2}{2 \times 32.16} = 2488$$
 foot-pounds,

which equals the work of acceleration

$$fs = \frac{w}{q} \frac{v_2}{t} s = \frac{w}{q} \frac{v_2}{t} \frac{v_2}{2} t = \frac{1}{2} \frac{w}{q} v_2^2.$$

If a body of the weight W falls from a height H, the work of acceleration is simply WH, or the same as the work required to raise the body to the same height

Work of Accelerated Rotation.—Let A = angular velocity of a solid body rotating about an axis, that is, the velocity of a particle whose radius is unity. Then the velocity of a particle whose radius is v is v = Av. If the angular velocity is accelerated from  $A_1$  to  $A_2$ , the increase of the velocity of the particle is  $v_2 - v_1 = r(A_1 - A_2)$ , and the work of accelerating

$$\frac{w}{g} \times \frac{v_2^2 - v_1^2}{2} = \frac{wr^2}{g} \frac{A_2^2 - A_1^2}{2},$$

in which w is the weight of the particle.

The work of acceleration of the whole body is

$$\sum \left\{ \frac{w}{g} \times \frac{v_2{}^2 - v_1{}^2}{2} \right\} = \frac{A_2{}^2 - A_1{}^2}{2g} \times \mathbf{S}wr^2.$$

The term  $\Sigma wr^2$  is the moment of inertia of the body.

"Force of the Blow" of a Steam Hammer or Other Falling Weight.—The question is often asked: "With what force does a falling hammer strike?" The question cannot be answered directly, and falling hammer strike  $\hat{r}^n$ . The question cannot be answered directly, and it is based upon a misconception or ignorance of fundamental mechanical laws. The energy, or capacity of doing work, of a body raised to a given height and let fall cannot be expressed in pounds, simply, but only in foot-pounds, which is the product of the weight into the height through which it fails, or the product of its weight +64.32 into the square of the velocity, in feet per second, which it acquires after falling through the given height. If F = weight of the body, M its mass, g the acceleration due to gravity, S the height of fall, and v the velocity at the end of the fall, the energy in the body just before striking, is  $FS = \frac{1}{2}M^{2} = W^{2} + 2g = W^{2} + 44.32$ , which is the general equation of energy of a moving body. Just as the energy of the body is a product of a force into a distance, so the work it does when it strikes is not the manifestation of a force, which can be expressed simply in pounds, but it is the overcoming of a resistance through a certain distance, which is expressed as the product of the average resistance ance into the distance through which it is exerted. If a hammer weighing 100 lbs. falls 10 ft., its energy is 1000 foot-pounds. Before being brought to rest it must do 1000 foot-pounds of work against one or more resistances. These are of various kinds, such as that due to motion imparted to the body These are of various kinds, such as unature to motion imparted to the body struck, penetration against friction, or against resistance to shearing or other deformation, and crushing and heating of both the falling body and the body struck. The distance through which these resisting forces act is generally indeterminate, and therefore the average of the resisting forces. which themselves generally vary with the distance, is also indeterminate.

Impact of Bodies .- If two inelastic bodies collide, they will move on together as one mass, with a common velocity. The momentum of the combined mass is equal to the sum of the momenta of the two bodies before impact. If  $m_1$  and  $m_2$  are the masses of the two bodies and  $v_1$  and  $v_2$  their respective velocities before impact, and v their common velocity after impact,

 $(m_1 + m_2)v = m_1v_1 \times m_2v_2$ 

$$v = \frac{m_1v_1 + m_2v_2}{m_1 + m_2}.*$$

If the bodies move in opposite directions  $v=\frac{m_1v_1-m_2v_2}{m_1+m_2}$ , or, the velocity of two inelastic bodies after impact is equal to the algebraic sum of their momenta before impact, divided by the sum of their masses. If two inelastic bodies of equal momenta impinge directly upon one another from opposite directions they will be brought to rest.

Impact of Inelastic Bodies Causes a Loss of Energy, and this loss is equal to the sum of the energies due to the velocities lost and gained by the bodies, respectively.

$$\frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2 - \frac{1}{2}(m_1 + m_2)v^2 = \frac{1}{2}m_1(v_1 - v)^2 + \frac{1}{2}m_2(v_2 - v)^2.$$

In which  $v_1-v$  is the velocity lost by  $m_1$  and  $v-v_2$  the velocity gained by  $m_2$ . Example—Let  $m_1=10$ ,  $m_2=8$ ,  $v_1=12$ ,  $v_2=15$ .

If the bodies collide they will come to rest, for 
$$v = \frac{10 \times 12 - 8 \times 15}{10 + 8} = 0$$
.  
The energy loss is

 $\frac{1}{10} \times 144 + \frac{1}{10} \times 225 - \frac{1}{10} \times 18 \times 0 = \frac{1}{10} \times 10(12 - 0)^2 + \frac{1}{10} \times 10(15 - 0)^2 = 1620 \text{ ft. lbs.}$ What becomes of the energy lost? Ans. It is used doing internal work on the bodies themselves, changing their shape and heating them.

For imperfectly elastic bodies, let e = the elasticity, that is, the ratio which the force of restitution, or the internal force tending to restore the shape of a body after it has been compressed, bears to the force of compression; and let  $m_1$  and  $m_2$  be the masses,  $v_1$  and  $v_2$  their velocities before impact, and  $v_1v_2$  their velocities after impact, then

$$\begin{split} & v_1{}' = \frac{m_1 v_1 \, + \, m_2 v_2}{m_1 + m_2} \, - \, \frac{m_2 e(v_1 - v_2)}{m_1 + m_2}; \\ & v_2{}' = \frac{m_1 v_1 + m_2 v_2}{m_1 + m_2} \, + \, \frac{m_1 e(v_1 - v_2)}{m_1 + m_2}. \end{split}$$

If the bodies are perfectly elastic, their relative velocities before and after impact are the same. That is:  $v,'-v,'=v_2-v_1$ . In the impact of bodies, the sum of their momenta after impact is the same as the sum of their momenta before impact.

$$m_1v_1' + m_2v_2' = m_1v_1 + m_2v_2$$

For demonstration of these and other laws of impact, see Smith's Mechanics; also, Weisbach's Mechanics.

Energy of Recoil of Guns. - (Eng'g, Jan. 25, 1884, p. 72.)

Let W = the weight of the gun and carriage;

V = the maximum velocity of recoil:

w = the weight of the projectile; v = the muzzle velocity of the projectile.

Then, since the momentum of the gun and carriage is equal to the momentum of the projectile, we have WV = wv, or V = wv + W.

<sup>\*</sup>The statement by Prof. W. D. Marks, in Nystrom's Mechanics, 20th edition, p. 454, that this formula is in error is itself erroneous,

Taking the case of a 10-inch gun firing a 400-lb, projectile with a muzzle velocity of 1400 feet per second, the weight of the gun and carriage being 22 tons = 49,850 lbs., we find the velocity of recoil  $\equiv$ 

$$V = \frac{1400 \times 400}{49,280} = 11$$
 feet per second.

Now the energy of a body in motion is  $WV^2 \div 2g$ .

Therefore the energy of recoil =  $\frac{49,280 \times 11^2}{2 \times 32.2}$  = 92,593 foot-pounds.

The energy of the projectile is  $\frac{400 \times 1400^2}{2 \times 32.2} = 12,173,913$  foot-pounds.

Conservation of Energy.—No form of energy can ever be produced except by the expenditure of some other form, nor annihilated except by being reproduced in another form. Consequently the sum total of energy in the universe, like the sum total of matter, must always remain the same. (S. Newcomb.) Energy can never be destroyed or lost; it can be transformed, can be transferred from one body to another, but no matter what transformations are undergone, when the total effects of the exertion of a given amount of energy are summed up the result will be exactly equal to the amount originally expended from the source. This law is called the Conservation of Energy. (Cotterill and Slade.)

is called the Conservation of Energy. (Cotterill and Slade.)
A heavy body sustained at an elevated position has potential energy.
When it falls, just before it reaches the earth's surface it has actual or
kinetic energy, due to its velocity. When it strikes it may penetrate the
earth a certain distance or may be crushed. In either case friction results
by which the energy is converted into heat, which is gradually radiated
into the earth or into the atmosphere, or both. Mechanical energy and heat
are mutually convertible. Electric energy is also convertible into heat or
mechanical energy, and either kind of energy may be converted into the
other.

other.

Sources of Energy.—The principal sources of energy on the earth's surface are the muscular energy of men and animals, the energy of the wind, of flowing water, and of fuel. These sources derive their energy from the rays of the sun. Under the influence of the sun's rays vegetation grows and wood is formed. The wood may be used as fuel under a steam boiler, its carbon being burned to carbonic acid. Three tenths of its heat energy escapes in the chimney and by radiation, and seven tenths appears as potential energy in the steam. In the steam-engine, of this seven tenths six parts are dissipated in heating the condensing water and are wasted; the remaining one tenth of the original heat energy of the wood is converted into mechanical work in the steam-engine, which may be used to drive machinery. This work is finally, by friction of various kinds, or possibly after data for machine the control of the co

equal to the original.

Perpetual Motion.—The law of the conservation of energy, than which no law of mechanics is more firmly established, is an absolute barrier to all schemes for obtaining by mechanical means what is called "perpetual motion," or a machine which will do an amount of work greater than the equivalent of the energy, whether of heat, of chemical combination, of electricity, or mechanical energy, that is put into it. Such a result would be the creation of an additional store of energy in the universe, which is not possible by any human agency.

The Efficiency of a Machine is a fraction expressing the ratio of the useful work to the whole work performed, which is equal to the energy expended. The limit to the efficiency of a machine is unity, denoting the efficiency of a perfect machine in which no work is lost. The difference between the energy expended and the useful work done, or the loss, is usually expended either in overcoming friction or in doing work on bodies surrounding the machine from which no useful work is received. Thus in an engine propelling a vessel part of the energy exerted in the cylinder

does the useful work of giving motion to the vessel, and the remainder is spent in overcoming the friction of the machinery and in making currents and eddies in the surrounding water.

#### ANIMAL POWER.

#### Work of a Man against Known Resistances. (Rankine.)

Kind of Exertion.	R, lbs.	ft. per	T'' 3600 (hours per day).	RV, ftlbs. per sec.	RVT, ftlbs. per day.
Raising his own weight up stair or ladder      Hauling up weights with rope, and lowering the rope un-	143	0.5	8	72.5	2,088,000
loaded	40	0.75	6	30	648,000
3. Lifting weights by hand	44	0.55	6	24.2	522,720
4. Carrying weights up-stairs and returning unloaded 5. Shovelling up earth to a	143	0.13	6	18.5	399,600
height of 5 ft. 3 in  6. Wheeling earth in barrow up slope of 1 in 12, 1/2 horiz. veloc, 0.9 ft. per sec. and re-		1.3	10	7.8	280,800
turning unloaded	132	0.075	10	9.9	356,400
tally (capstan or oar)	26.5	2.0	8	53	1,526,400
	( 12.5	5.0	?	62.5	
8. Turning a crank or winch	38.0	2.5	8	45	1,296,000
	( 20.0	14.4	2 min.	288	
9. Working pump	13.2	2.5	10	33	1,188,000
10. Hammering	15		8?	?	480,000

EXPLANATION.—R, resistance; V, effective velocity = distance through which R is overcome + total time occupied, including the time of moving unloaded, if any; T'', time of working, in seconds per day; T'' + 3600, same time, in hours per day; RV, effective power, in foot-pounds per second; RVT, daily work.

#### Performance of a Man in Transporting Loads Horizontally. (Rankine.)

Kind of Exertion.	L, lbs.	v, ftsec.	T 3600 (hours per day).	LV, lbs. con- veyed 1 foot.	LVT, lbs. con- veyed 1 foot,			
11. Walking unloaded, transporting his own weight. 12. Wheeling load L in 2-whid. barrow, return unloaded. 13. Ditto in 1-wh, barrow, ditto. 14. Travelling with burden. 15. Carrying burden, returning unloaded. 16. Carrying burden, for 30 seconds only.	140 224 132 90 140	5 1% 1% 21% 21% 1% 0 11.7 23.1	10 10 10 7 6	700 878 220 225 233 0 1474.2	25,200,000 13,428,000 7,920,000 5,670,000 5,032,800			

EXPLANATION.—L, load; V, effective velocity, computed as before; T', time of working, in seconds per day; T'' + 3600, same time in hours per day; LV, transport per second, in lbs. conveyed one foot; LVT, daily transport.

In the first line only of each of the two tables above is the weight of the

man taken into account in computing the work done.

Clark says that the average net daily work of an ordinary laborer at a

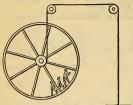


Fig. 97.

pump, a winch, or a crane may be taken at 3300 foot-pounds per minute, or one-tenth of a horse-power, for 8 hours a day; but for shorter periods from four to five times this rate may be exerted.

Mr. Glynn says that a man may exert a force of 25 lbs. at the handle of a crane for short periods; but that for continuous work a force of 15 lbs. is all that should be assumed, moving through 220 feet per minute.

Man-wheel,-Fig. 97 is a sketch of a very efficient man-power hoisting-machine which the author saw in Berne, Switzerland, in 1889. The face of the wheel was wide enough for three men to walk abreast, so that nine men could work in it at one time.

Work of a Horse against a Known Resistance. (Rankine.)

Kind of Exertion.	R.	V.	$\frac{T.}{3600}$	RV.	RVT.
Cantering and trotting, drawing a light railway carriage (thoroughbred)      Horse drawing cart or boat,	mean 301% max. 50	143%	4.	4471/6	6,444,000
walking (draught-horse)	120	3.6	8	432	12,441,600
Horse drawing a gin or mill, walking     Ditto, trotting	100 66	3.0 6.5	8 4½	300 429	8,640,000 6,950,000

EXPLANATION.—R, resistance, in lbs.; V, velocity, in feet per second;  $T'' \rightarrow 3600$ , hours work per day; RV, work per second; RVT, work per day. The average power of a draught-horse, as given in line 2 of the above table, being 432 foot-pounds per second, is 432/550 = 0.785 of the conventional value assigned by Watt to the ordinary unit of the rate of work of prime movers. It is the mean of several results of experiments, and may be considered the average of ordinary performance under favorable circumstances.

#### Performance of a Horse in Transporting Loads Horizontally. (Rankine.)

_	Kind of Exertion.	L.	V.	T.	LV.	LVT.
6.	Walking with cart, always loaded	1500 750	3.6 7.2	10 4½	5400 5400	194,400,000 87,480,000
	ed, returning empty; V, mean velocity	1500 270 180	2.0 3.6 7.2	10 10 7	3000 972 1296	108,000,000 34,992,000 32,659,200

Explanation.—L, load in lbs.; V, velocity in feet per second;  $T \div 3600$ , working hours per day; LV, transport per second; LVT, transport per day. This table has reference to conveyance on common roads only, and those evidently in bad order as respects the resistance to traction upon them.

Horse Gin.-In this machine a horse works less advantageously than in drawing a carriage along a straight track. In order that the best possible results may be realized with a horse-gin, the diameter of the circular track in which the horse walks should not be less than about forty

Oxen, Mules, Asses.—Authorities differ considerably as to the power these animals. The following may be taken as an approximative comof these animals. parison between them and draught-horses (Rankine);

Ox.-Load, the same as that of average draught-horse; best velocity and work, two thirds of horse,

Mule.—Load, one half of that of average draught-horse; best velocity. the same with horse; work one half. Ass.—Load, one quarter that of average draught-horse; best velocity the

Ass.—Loda, one quarter.

Reduction of Draught of Horses by Increase of Grade
of Roads. (Engineering Record, Prize Essays on Roads, 1892.)—Experi-

ments on English roads by Gayffier & Parnell: Calling load that can be drawn on a level 100:

On a rise of. ...... 1 in 100, 1 in 50, 1 in 40, 1 in 30, 1 in 26, 1 in 20, 1 in 10, A horse can draw only 90. 81. 72. 64. 54. 40.

The Resistance of Carriages on Roads is (according to Gen. Morin) given approximately by the following empirical formula:

$$R = \frac{W}{r} [a + b(u - 3.28)].$$

In this formula R = total resistance; r = radius of wheel in inches; W = radius of wheel in inchesgross load; u = velocity in feet per second; while a and b are constants, whose values are: For good broken-stone road, a = .4 to .55, b = .024 to .026; for paved roads, a = .27, b = .0684.

Rankine states that on gravel the resistance is about double, and on

sand five times, the resistance on good broken-stone roads.

#### ELEMENTS OF MACHINES.

The object of a machine is usually to transform the work or mechanical energy exerted at the point where the machine receives its motion into

work at the point where the final resistance is overcome. The specific end may be to change the character or direction of motion, as from circular to rectilinear, or vice versa, to change the velocity, or to overcome a great resistance by the application of a moderate force. In all cases the total energy exerted equals the total work done, the latter including the overcoming of all the frictional resistances of the machine as well as the useful work performed. No increase of power can be obtained from any machine, since this is impossible according to the law of conservation of energy. In a frictionless machine the product of the force exerted at the driving-point into the velocity of the driving-point, or the distance it moves in a given interval of time, equals the product of the resistance into the distance through which the resistance is overcome in the same time.

The most simple machines, or elementary machines, are reducible to three classes, viz., the Lever, the Cord, and the Inclined Plane.

The first class includes every machine con-sisting of a solid body capable of revolving on an axis, as the Wheel and Axle.

The second class includes every machine in which force is transmitted by means of flexi-

ble threads, ropes, etc., as the Pulley.

The third class includes every machine in which a hard surface inclined to the direc-

tion of motion is introduced, as the Wedge and the Screw.

A Lever is an inflexible rod capable of motion about a fixed point, called a fulcrum. The rod may be straight or bent at any angle, or curved. It is generally regarded, at first, as without weight, but its weight may be

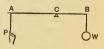


Fig. 98.

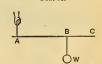


Fig. 99.



Fig. 100.

considered as another force applied in a vertical direction at its centre of gravity. The arms of a lever are the portions of it intercepted between the force.

P, and fulcrum, C, and between the weight, W, and fulcrum.

Levers are divided into three kinds or orders, according to the relative

positions of the applied force, weight, and fulcrum.

In a lever of the first order, the fulcrum lies between the points at which

the force and weight act. (Fig. 98.)
In a lever of the second order, the weight acts at a point between the fulcrum and the point of action of the force. (Fig. 99.)

In a lever of the third order, the point of action of the force is between that of the weight and the fulrcum. (Fig. 100.)
In all cases of levers the relation between the force exerted or the pull,

P, and the weight lifted, or resistance overcome, W, is expressed by the equation  $P \times AC = W \times BC$ , in which AC is the lever-arm of P, and BCis the lever-arm of W, or moment of the force = the moment of the resistance. (See Moment.)

In cases in which the direction of the force (or of the resistance) is not at right angles to the arm of the lever on which it acts, the "lever-arm" is the length of a perpendicular from the fulcrum to the line of direction of the force (or of the resistance). W:P::AC:BC, the ratio of the resistance to the applied force is the inverse ratio of their lever-arms. Also, if  $V^*e$  is the velocity of W, and  $V_p$  is the velocity of P,  $W:P::V_p:V_w$ , and  $P\times V_p=W\times V_w$ .

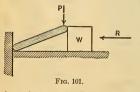
If Sp is the distance through which the applied force acts, and Sw is the distance the weight is lifted or through which the resistance is overcome,  $W:P::Sp:Sw:W\times Sw=P\times Sp$ , or the weight into the distance it is lifted equals the force into the distance through which it is exerted.

These equations are general for all classes of machines as well as for levers, it being understood that friction, which in actual machines increases

the resistance, is not at present considered. The Bent Lever. In the bent lever (see Fig. 91, page 416) the leverarm of the weight m is cf instead of bf. The lever is in equilibrium when  $n \times af = m \times cf$ , but it is to be observed that the action of a bent lever may be very different from that of a straight lever. In the latter, so long as the force and the resistance act in lines parallel to each other, the ratio of the lever-arms remains constant, although the lever itself changes its inclina-tion with the horizontal. In the bent lever, however, this ratio changes: thus, in the cut, if the arm bf is depressed to a horizontal direction, the distance cf lengthens while the horizontal projection of af shortens, the latter becoming zero when the direction of af becomes vertical. As the arm af approaches the vertical, the weight m which may be lifted with a given force s is very great, but the distance through which it may be lifted is very small. In all cases the ratio of the weight m to the weight m to the weight m is the inverse ratio of the horizontal projection of their respective lever-arms.

The Moving Strut (Fig. 101) is similar to the bent lever, except that

one of the arms is missing, and that the force and the resistance to be

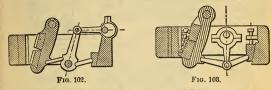


overcome act at the same end of the single arm. The resistance in the single arm. The resistance in the cut is not the weight W, but its resistance to being moved, R, which may be simply that due to its friction on the horizontal plane, or some other op-posing force. When the angle between the strut and the horizontal plane changes, the ratio of the resistance to the applied force changes. When the angle becomes very small, a moderate force will overcome a very great resistance, which tends to become infinite as

the angle approaches zero. If a= the angle,  $P\times\sin a=R\times \text{versin }a$ . If a= 5 degrees,  $\sin a=$  0.8716, versin a= 0.0381, R= 23 R, nearly. The stone-crusher (Fig. 102) shows a practical example of the use of two

moving struts. The Toggle-joint is an elbow or knee-joint consisting of two bars so connected that they may be brought into a straight line and made to produce great endwise pressure when a force is applied to bring them into this

position. It is a case of two moving struts placed end to end, the moving force being applied at their point of junction, in a direction at right angles to the direction of the resistance, the other end of one of the struts resting against a fixed abutment, and that of the other against the body to be moved. If a = the angle each strut makes with the straight line joining the points about which their outer ends rotate, the ratio of the resistance to the applied force is  $R:P::\sin a:2$  versin a:2R versin  $a=P\sin a$ . The



ratio varies when the angle varies, becoming infinite when the angle becomes zero.

The toggle-joint is used where great resistances are to be overcome

through very small distances, as in stone-crushers (Fig. 103). The Inclined Plane, as a mechanical element, is supposed perfectly

hard and smooth, unless friction be considered. It assists in sustaining a heavy body by its reaction. This reaction, however, being normal to the plane, cannot entirely counteract the weight of the body, which acts vertically downward Some other force must therefore

be made to act upon the body, in order that it may be sustained.

If the sustaining force act parallel to the plane (Fig. 104), the force is to the weight as the height of the plane is to its length, measured on the incline.

If the force act parallel to the base of the plane,

the power is to the weight as the height is to the base.

If the force act at any other angle, let i =the angle of the plane with the horizon, and e =the angle of the direction of the applied force with the Fig. 104. angle of the plane.  $P: W: \sin i : \cos e$ ;  $P < \cos e = W \sin i$ .

Problems of the inclined plane may be solved by the parallelogram of

forces thus:

Let the weight W be kept at rest on the incline by the force P, acting in the line bP', parallel to the plane Draw the vertical line ba to represent the weight; also bb' perpendicular to the plane, and complete the parallelogram b'c. Then the vertical weight ba is the resultant of bb', the measure of support given by the plan to the weight, and be, the force of gravity tending to draw the weight down the plane. The force required to maintain the weight in equilibrium is represented by this force be. Thus the force and the weight are in the ratio of be to ba. Since the triangle of forces abe is similar to the triangle of the incline ABC, the latter may be substituted for the former in determining the relative magnitude of the forces, and

The Wedge is a pair of inclined planes united by their bases. In the application of pressure to the head or butt end of the wedge, to cause it to spenetrate a resisting body, the applied force is to the resistance as the thickness of the wedge is to its length. Let t be the thickness, t the length, W the resistance, and P the applied force or pressure on the head of the wedge. Then, friction neglected, P:W::t:t;  $P=\frac{Wt}{t};$   $W=\frac{Pt}{t}$ .

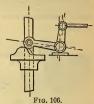
The Screw is an inclined plane wrapped around a cylinder in such a way that the height of the plane is parallel to the axis of the cylinder If the screw is formed upon the internal surface of a hollow cylinder, it is naully called a nut. When force is applied to raise a weight or overcome a resistance by means of a screw and nut, either the screw or the nut may be fixed, the other being movable. The force is generally applied at the end of a wrench or lever-arm, or at the circumference of a wheel. If r = radiusof the wheel or lever arm, and p = pitch of the screw, or distance between

threads, that is, the height of the inclined plane for one revolution of the screw, P = the applied force, and W = the resistance overcome, then, neglecting resistance due to friction,  $2\pi r \times P = Wp$ ; W = 6.283 Pr + p. The ratio of P to W is thus independent of the diameter of the screw. In actual screws, much of the power transmitted is lost through friction.

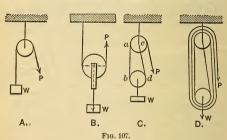


The Cam is a revolving inclined plane. It may be either an inclined plane cam, used in stamp-mills

wrapped around a cylinder in such a way that the height of the plane is ra-dial to the cylinder, such as the ordinary lifting-



(Fig. 105), or it may be an inclined plane curved edgewise, and rotating in a plane parallel to its base (Fig. 106). The relation of the weight to the applied force is calculated in the same manner as in the case of the screw.



Pulleys or Blocks. -P = force applied, or pull; W = weight lifted or resistance. In the simple pulley A (Fig. 107) the point P on the pulling rope descends the same amount that the weight is lifted, therefore P = W. rope descends the same amount that the weight is litted, therefore P = W. In B and C the point P moves twice as far as the weight is litted, therefore W = 2P, In B and C there is one movable block, and two plies of the rope engage with it. In D there are three sheaves in the movable block, each with two plies engaged, or six in all. Six plies of the rope are therefore shortened by the same amount that the weight is littled, and the point P moves six times as far as the weight, consequently W = 6P. In general, the work of W to P is a coult to the number of this e of the rope that are the ratio of W to P is equal to the number of plies of the rope that are shortened, and also is equal to the number of plies that engage the lower block. If the lower block has 2 sheaves and the upper 3, the end of the rope book. If the lower block has a sheaves and the upper s, the end of the lope is fastened to a hook in the top of the lower block, and then there are 5 plies shortened instead of 6, and W = 5P. If V = velocity of W, and v = velocity of P, then in all cases VW = vP, whatever the number of sheaves or their arrangement. If the hanling rope, at the pulling end, passes first around a sheave in the upper or stationary block, it makes no difference in what direction the rope is led from this block to the point at which the pull on the rope is applied; but if it first passes around the movable block, it is necessary that the pull be exerted in a direction parallel to the line of action of the resistance, or a line joining the centres of the two blocks, in order to obtain the maximum effect. If the rope pulls on the lower block at an angle, the block will be pulled out of the line drawn between the weight and the upper block, and the effective pull will be less than the actual pull

on the rope in the ratio of the cosine of the angle the pulling rope makes

with the vertical, or line of action of the resistance, to unity

**Differential Pulley.** (Fig. 108.)—Two pulleys, B and C, of different radii, rotate as one piece about a fixed axis, A. An endless chain, BDECLKH, passes over both pulleys. The rims of the pulleys are shaped so as to hold the chain and prevent it from slipping. One of the bights or loops in which the chain bangs, DE, passes under and supports the running block F. The other loop or bight, HKL, hange freely, and is called the hauling part. It is evident that the velocity of the hauling part is equal to that of the pitch-circle of the pulley B.

In order that the velocity-ratio may be exactly uniform, the radius of the sheave F should be an exact mean be-

tween the radii of B and C.

Consider that the point B of the cord BD moves through Consider that the point B of the cord BD hoves through an arc whose length = AB, during the same time the point C or the cord CE will move downward a distance = AC. The length of the bight or loop BDEC will be shortened by AB = AC, which will cause the pulley F to be raised half of this amount. If F = the pulling force on the cord HK, and W the weight litted at F, then  $P \times AB = W \times \frac{1}{2}(AB - AC)$ , where  $AB = W \times \frac{1}{2}(AB - AC)$ .

To calculate the length of chain required for a differential pulley, take the following sum: Half the circumference of A + half the circumference of B + half the circumference of F + twice the greatest distance of F from A + the least length of loop HKL. The last quantity is fixed

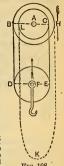




Fig. 109.

least length of convenience, according to convenience. Windlass (Fig. 109) is identical in principle The Differential Windlass (Fig. 109) is identical in principle with the differential pulley, the differential windlass the struction being that in the differential windlass the struction being that in the hight of a rope whose two parts are wound round, and have their ends respec-tively made fast to two barrels of different radii, which rotate as one piece about the axis A. The differential windlass is little used in practice, because of the great length of rope which it requires.

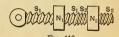
of the great length of rope when it requires.

The Differential Screw (Fig. 110) is a compound screw of different pitches, in which the threads wind the same way, N<sub>1</sub> and N<sub>2</sub> are the two nuts; S<sub>1</sub>S<sub>1</sub>, the longer-pitched thread; S<sub>2</sub>S<sub>2</sub>, the shorter-pitched thread; in the figure both these threads are left-handed. At each turn of the screw the nut N2 advances relatively to N2 through a distance equal to the difference of the pitch. The use of the differential screw is to combine the slowness of advance due to a fine pitch with the strength of thread which can be

obtained by means of a coarse pitch only.

\*\*Myheel and Axle, or Windlass, resembles two pulleys on one axis, having different diameters. It a weight be lifted by means of a rope wound

over the axle, the force being applied at the rim of the wheel, the action is like that of a lever of which the shorter arm is equal to the radius of the axle plus half the thickness of the rope, and the longer arm is equal to the radius of the wheel. A wheel and axle is therefore sometimes classed



as a perpetual lever. If P = the applied force, D = diameter of the wheel, W = the weight lifted, and d the diameter of the axie + the diameter of the rope, PD = Wd.

the rope, FD=Wa. **Toothed—wheel Gearing** is a combination of two or more wheels and axies (Fig. 11). If a series of wheels and pinions gear into each other, as in the cut, friction neglected, the weight lifted, or resistance overcome, is to the force applied inversely as the distances through which they act in a given time. If R, R, R be the radii of the successive wheels, measured to the pitch-line of the teeth, and r, r, r, the radii of the corresponding pinions, P the applied force, and W the weight lifted, P ×

 $R \times R^2 \times R_2 = W \times r \times r_1 \times r_2$ , or the applied force is to the weight as the product of the radii of the pinions is to the product of the radii of the wheels; or, as the product of the numbers expressing the teeth in each pinion is to the product of the numbers expressing the teeth in each wheel.

Endless Screw, or Worm-gear. (Fig. 112.)—This gear is commonly used to convert motion at high speed into motion at very slow

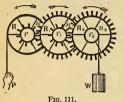




Fig. 112.

speed. When the handle P describes a complete circumference, the pitchline of the cog-wheel moves through a distance equal to the pitch of the screw, and the weight W is lifted a distance equal to the pitch of the screw screw, and the weight "is interest a distance equal to the pitch of the diameter of the axle to the diameter of the pitch-circle of the wheel. The ratio of the applied force to the weight litted is inversely as their velocities, friction not being considered; but the friction in the worm-gear is usually very great, amounting sometimes to three or four times the useful work done,

three or four unies the useful work done. If v= the distance through which the force P acts in a given time, s= second, and V= distance the weight W is lifted in the same time, r= radius of the crank or wheel through which P acts, t= pitch of the screw, and also of the teeth on the cog-wheel, d= diameter of the axle. and D = diameter of the pitch-line of the cog-wheel,  $v = \frac{6.283 \text{ r } D}{D}$  $\times V$ ;  $V = v \times td \div 6.283rd$ . Pv = WV + friction.

#### STRESSES IN FRAMED STRUCTURES.

Framed structures in general consist of one or more triangles, for the reason that the triangle is the one polygonal form whose shape cannot be changed without distorting one of its sides. Problems in stresses of simple framed structures may generally be solved either by the application of the triangle, paralellogram, or polygon of forces, by the principle of the lever, or by the method of moments. We shall give a few examples, referring the or by the method of moments. We shall give a few examples, referring the student to the works of Burr, Dubois, Johnson, and others for more elaborate treatment of the subject.

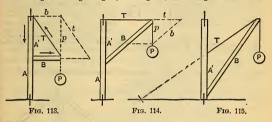
1. A Simple Crane. (Figs. 113 and 114.)—A is a fixed mast, B a brace or boom, T a ue, and P the load. Required the strains in B and T. The weight P, considered as acting at the end of the boom, is held in equilibrium by F, considered a decline at the glownwards; second, the tension in T; and third, the threst of E. Let the length of the line p represent the magnitude of the downward force served by the load, and draw a parallelogram with of the downward force exerted by the load, and draw a parallelogram with sides  $b^{\dagger}$  parallel, respectively, to B and T, such that p is the diagonal of the parallelogram. Then b and t are the components drawn to the same scale as p, p being the resultant. Then if the length p represents the load, t is the tension in the tie, and b is the compression in the brace. Or, more simply, T, B, and that portion of the mast included between them or  $A^{\prime}$  may represent a triangle of forces, and the forces are proportional to the length of the sides of the triangle; that is, if the height of the triangle  $A^{\prime}$  = the load, then B = the compression in the brace, and T = the tension in the a-constant a-constant

tie; or if P = the load in pounds, the tension in  $T = P \times \frac{T}{A'}$ , and the com-

pression in  $B = P \times \frac{B}{A'}$ . Also, if a = the angle the inclined member makes

with the mast, the other member being horizontal, and the triangle being right-angled, then the length of the inclined member = height of the triangle  $\times$  secant a, and the strain in the inclined member = P secant a. Also, the strain in the horizontal member =  $P \tan \alpha$ .

The solution by the triangle or parallelogram of forces, and the equations Teusion in  $T = P \times T/A'$ , and Compression in  $B = P \times B/A'$ , hold true even if the triangle is not right-angled, as in Fig. 115; but the trigonometrical rela-



tions above given do not hold, except in the case of a right-angled triangle. It is evident that as A' decreases, the strain in both T and B increases, tending to become infinite as A' approaches zero. If the tie T's not attached to the mast, but is extended to the ground, as shown in the dotted line, the tension in it remains the same.

2. A Guyed Crane or Derrick. (Fig. 116.)—The strain in B is, as before,  $P \times B/A'$ , A' being that portion of the vertical included between B and T, wherever T may be attached to A. If, however, the tie T is attached to B beneath its extremity, there may be in addition a bending strain in B due to a tendency to turn about the point of attachment of T as a fulcrum.

The strain in T may be calculated by the principle of moments. The moment of P is Pc, that is, its weight  $\times$  its perpendicular distance from the point of rotation of B on the mast. The moment of the strain on T is the product of the strain into the perpendicular distance from the line of its

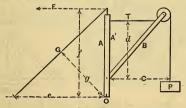


Fig. 116.

direction to the same point of rotation of B, or Td. The strain in T therefore  $= Pc \div d$ . As d decreases the strain on T increases, tending to infin-

for = Pv + d. As a decreases the strain of t increases, tending to form thy as a approaches zero. The strain on the guy-rope is also calculated by the method of moments. The moment of the load about the bottom of the mast O is, as before, Pc. If the guy is horizontal the strain in it is F and its moment is Ff, and F = Pc + f. If it is inclined, the moment is the strain G X the perpendicular distance of the line of its direction from O, or Gg, and G = Pc + g. The guy-rope having the least strain is the horizontal one F, and the strain

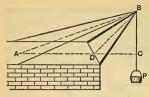


Fig. 117.

in G = the strain in  $F \times$  the secant of the angle between F and G. As G is made more nearly vertical g decreases, and the strain increases, becoming inflnite when q=0.

3. Shear-poles with Guys. (Fig. 109.)—Resultant of strain in both masts =  $P \times BD$ +BC. Resultant strain in both guys= $P \times AB+BC$ . The strain on each mast (or guy) will be half the above, multiplied by the secant of half the angle the masts (or guys) make with each other.

Two Diagonal Braces and a Tie-rod, (Fig. 118.)-Suppose the braces are used to sustain a single load P. Compressive stress on AD = $\frac{1}{2}P \times \frac{AD}{AB}$ ; on  $CA = \frac{1}{2}P \times \frac{CA}{AD}$ This is true only if CB and BD are of equal

 $\frac{1}{2}P \times \frac{1}{AB}$ ; on  $CA = \frac{1}{2}P \times \frac{1}{AB}$ . This is true only if CB and BD are of equal length, in which case  $\frac{1}{2}$  of P is supported by each abutment C and D. If they are unequal in length (Fig. 119), then, by the principle of the lever, find the re-

actions of the abutments  $R_1$  and  $R_2$ . If Pis the load applied at the point B on the lever CD, the fulcrum being D, then  $R_1 \times CD = P \times BD$  and  $R_2 \times CD = P \times BC$  and  $R_3 \times CD = P \times BC + CD$ .

The strain on  $AC = R_1 \times AC + AB$ , and on  $AD = R_2 \times AD + AB$ .

The strain on the tie =  $R_1 \times CB + AB$  $= R_2 \times BD \div AB.$ 

Fig. 118.

When CB = BD,  $R_1 = R_2$ , the strain on CB and BD is the same, whether the braces are of equal length or not, and is equal to  $\frac{1}{2}P \times \frac{1}{2}CD + AB$ .

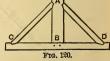
If the braces support a uniform load, as a pair of rafters, the strains caused by such a load are equivalent to that caused by one half of the load applied at the centre. The horizontal thrust of the braces against each other at the

Fig. 119.

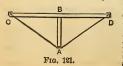
apex equals the tensile strain in the tie.

King-post Truss or Bridge. (Fig. 130.)—If the load is distributed over the whole leugth of the truss, the effect is the same as if half the load were placed at the centre, the other half being carried by the abutments. Let

were placed at one centre, the other half be P = one half the load on the truss, then tension in the vertical tie AB = P. Compression in each of the inclined braces =  $\frac{1}{2}P \times AD + AB$ . Tension in the tie  $CD = \frac{1}{2}P \times BD + AB$ . Horizontal thrust of inclined brace AD at D = the tension in the tie. If W = the total load on one truss uniformly distributed, l = its length and d = its depth, then the tension on the horizontal tie =  $\frac{1}{8d}$ 

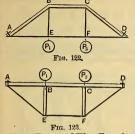


Inverted King-post Truss. (Fig. 121.)-If P = a load applied at B, or one half of a uniformly distributed load, then compression on AB = P



(the floor-beam CD not being considered The non-resistance to a slight bending. Tension on AC or  $AD = \frac{1}{2}P \times AD + AB$ . Compression on  $CD = \frac{1}{2}P \times BD + AB$ . Queen-post Truss. (Fig. 122.)—If uniformly loaded, and the queen-posts di-

vide the length into three equal bays, the load may be considered to be divided into three equal parts, two parts of which, P1 and P2, are concentrated at the panel joints



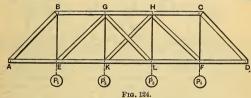
and the remainder is equally divided between the abutments and supported by them directly. The two parts  $P_1$  and  $P_2$  only are considered to affect the members of the truss. Strain in the vertical ties BE and CF each the vertical ties BE and CF each equals  $P_1$  or  $P_2$ . Strain on the tie AE or EF or  $ED = P \times FD + CF$ . Thrust on BC = tension on EF

For stability to resist heavy un-equal loads the queen-post truss should have diagonal braces from

Should have diagonal oraces from Bto F and from Cto E.

Inverted Queen-post Truss, (Fig. 123.)—Compression on EB and FO each = P. Tension on AB and CD each = P. Tension on AE or EF BC =compression on EF. For stability to resist unequal loads, ties should be run from C to E and from B to F.

Burr Truss of Five Panels. (Fig. 124.)—Four fifths of the load may be taken as concentrated at the points E, K, L and F, the other fifth being



supported directly by the two abutments. For the strains in BA and CD supported directly by the two abuttments. For the strains in BA and CD the truss may be considered as a queen-post truss, with the loads  $P_1$ ,  $P_2$  concentrated at E and the loads  $P_3$ ,  $P_4$  concentrated at E. Then, compressive strain on  $AB = (P_1 + P_2) \times AB + BE$ . The strain on CD is the same if the loads and panel lengths are equal. The tensile strain on BE or  $CF = P_1 + P_2$ . That portion of the truss between E and F may be considered as a smaller queen-post truss, supporting the loads  $P_3$ ,  $P_3$  at K and L. The strain on EG or  $FF = P_3 \times EG + GK$ . The diagonals GL and KH receive no strain unless the truss is unequally loaded. The verticals GK and HL each receive a careful attain and E P or P. receive a tensile strain equal to  $P_2$  or  $P_3$ .

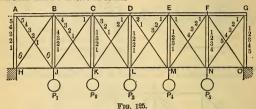
For the strain in the horizontal members: BG and CH receive a thrust

For the strain in the horizontal members: BG and CH receive a thrust equal to the horizontal component of the thrust in  $AB \circ rCD$ ,  $= (P_1 + P_2) \times tan$  angle ABE, or  $(P_1 + P_2) \times AE + BE$ . GH receives this thrust and also, in addition, a thrust equal to the horizontal component of the thrust in EG or HF, or, in all,  $(P_1 + P_2 + P_3) \times AE + BE$ . The tension in AE or FD equals the thrust in BG or HC, and the tension in EK, KL, and LF equals the thrust in GH.

Pratt or Whipple Truss. (Fig. 125.)-In this truss the diagonals are ties, and the verticals are struts or columns.

Calculation by the method of distribution of strains; Consider first the load  $P_1$ . The truss having six bays or panels, 5/6 of the load is transmitted to the abutment H, and 1/6 to the abutment O, on the principle of the lever. As the five sixths must be transmitted through JA and AH, write on these members the figure S. The one sixth is transmitted successively through JC, CK, KD, DL, etc., passing alternately through a tie and a strut. Write on these mappings up to the structure CO inclusing the figure S. on these members, up to the struct GO inclusive, the figure 1. Then consider the load  $P_2$ , of which 4/6 goes to AH and 2/6 to GO. Write on KB,  $B_d$ , J and AH the figure 4, and on KD,  $D_L$ , LE, etc., the figure 2. The load  $P_2$  transmit 3/6 in each direction; write 3 on each of the members through which this stress passes, and so on for all the loads, when the figures on the several members will appear as on the cut. Adding them up, we have the following totals:

Each of the figures in the first line is to be multiplied by  $1/6P \times$  secant of angle HJJ, or  $1/6P \times JJ + AH$ , to obtain the tension, and each figure in the lower line is to be multiplied by 1/6P to obtain the compression. The diagonals HB and FO receive no strain.



It is common to build this truss with a diagonal strut at HB instead of the post HA and the diagonal AJ; in which case 5/6 of the load P is carried through JB and the strut BH, which latter then receives a strain = 15/6 $P \times$ secant of HBJ.

The strains in the upper and lower horizontal members or chords increase from the ends to the centre, as shown in the case of the Burr truss. AB receives a thrust equal to the horizontal component of the tension in AJ, or IJ/BPX tan AJB. BC receives the same thrust I the horizontal component of the tension in BK, and so on. The tension in the lower chord of each panel is the same as the thrust in the upper chord of the same panel. (For calculation of the chord strains by the method of moments, see below.)

The maximum thrust or tension is at the centre of the chords and is equal to  $\frac{WL}{8D}$ , in which W is the total load supported by the truss, L is the length,

and D the depth. This is the formula for maximum stress in the chords of a truss of any form whatever. The above calculation is based on the assumption that all the loads  $P_1$ ,  $P_2$ , The above calculation is passed on the assumption that all the loads  $P_1, P_2$ , etc., are equal. If they are unequal the value of each has to be taken into account in distributing the strains. Thus the tension in AJ, with unequal loads, instead of being  $15 \times 1/6 P_2$  excent  $\theta$  would be see  $\theta \times (5/6P_1 + 4/6 P_2 + 3/6 P_2 + 1/6 P_3)$ . Each panel load,  $P_1$  etc., includes its fraction of the weight of the trues.

General Formula for Strains in Diagonals and Verticals. Let n = total number of panels, x = number of any vertical considered from the nearest end, counting the end as 1, r = rolling load for each panel,

P = total load for each panel,

$$\text{Strain on verticals} = \frac{(n-x) + (n-x)^2 - (x-1) + (x-1)^2 W}{2n} + \frac{r(x-1) + (x-1)^2}{2n}.$$

For a uniformly distributed load, leave out the last term,  $[r(x-1)+(x-1)^2]\div 2n$ .

Strain on principal diagonals = strain on verticals  $\times$  secant  $\theta$ , that is

secant of the angle the diagonal makes with the vertical. Scann of the counterbrace: The strain on the counterbrace in the first Strain on the counterbrace in the first Spanel is 0, if the load is uniform. On the 2d, 3d, 4th, etc., it is P secant θ

 $\times \frac{1}{n}, \frac{1+2}{n}, \frac{1+2+3}{n}$ , etc., P being the total load in one panel.

Strain in the Chords—Method of Moments,—Let the truss be uniformly loaded, the total load acting on it = W. Weight supported at each end, or reaction of the abutinent = W/2. Length of the truss = L. Weight on a unit of length = W/L. Horizontal distance from the nearest abutinent to the point (say M in Fig. 125) in the chord where the strain is to be determined = x. Horizonta, strain at that point (tension on the lower chord, compression in the upper) = R. Depth of the truss = D. By the method of moments we take the difference of the moments, about the point M, of the reaction of the abutment and of the load between and the abutments, and equate that difference with the moment of the resistance, or of the strain in the horizontal chord, considered with reference to a point in the opposite chord, about which the truss would turn if the first chord were

The moment of the reaction of the abutment is Wx/2. The moment of the load from the abutment to M is  $W/Lx \times$  the distance of its centre of gravity from M, which is x/2, or moment =  $Wx^2 + 2L$ . Moment of the stress in the chord =  $HD = \frac{Wx}{2} - \frac{Vx^2}{2L}$ , whence  $H = \frac{W}{2D} \left(x - \frac{x^2}{L}\right)$ . If x = 0 or L,

H=0. If x=L/2,  $H=\frac{WL}{8D}$ , which is the horizontal strain at the middle

of the chords, as before given.

The Howe Truss. (Fig. 126.)—In the Howe truss the diagonals are struts, and the verticals are ties. The calculation of strains may be made

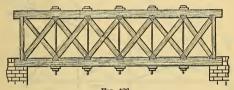
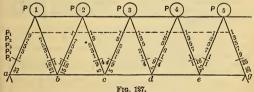


Fig. 126.

in the same method as described above for the Pratt truss.

The Warren Girder. (Fig. 127.)—In the Warren girder, or triangular truss, there are no vertical struts, and the diagonals may transmit either



tension or compression. The strains in the diagonals may be calculated by the method of distribution of strains as in the case of the rectangular truss.

On the principle of the lever, the load  $P_1$  being 1/10 of the length of the span from the line of the nearest support a, transmits 9/10 of its weight to aand 1/10 to g. Write 9 on the right hand of the strut 1a, to represent the and 1/0 to g, write 9 on the right hand of the strict  $l\alpha$ , to represent the compression, and 1 on the right hand of 1b, 2c, 3d, etc., to represent compression, and on the left hand of  $b^2$ , 03, etc., to represent tension. The load  $P_2$  transmits f/10 of its weight to a and 3/10 to g. Write 7 on each member from 2 to g, placing the figures representing compression on the right hand of the member, and those representing tension on the left. Proceed in the same manner with all the loads, then

sum up the figures on each side of each diagonal, and write the difference of each sum beneath, and on the side of the greater sum, to show whether the difference represents tension or compression. The results are as follows: Compression, 1a, 25; 2b, 15; 3c, 5; 3d, 5; 4e, 15; 5g, 25. Tension, 1b, 15; 2c, 5; 4d, 5; 5e, 15. Each of these figures is to be multiplied by 1/10 of one of the loads as P1, and by the secant of the angle the diagonals make with a vertical line.

The strains in the horizontal chords may be determined by the method of moments as in the case of rectangular trusses.

Roof-truss.—Solution by Method of Moments.—The calculation of strains in structures by the method of statical moments consists in taking a cross-section of the structure at a point where there are not more than three members (struts, braces, or chords).

To find the strain in either one of these members take the moment about the intersection of the other two as an axis of rotation. The sum of the moments of these members must be 0 if the structure is in equilibrium. But the moments of the two members that pass through the point of reference or axis are both 0, hence one equation containing one unknown quantity can be found for each cross-section.

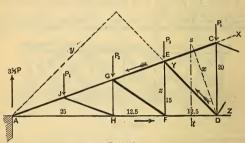


Fig. 128.

In the truss shown in Fig. 128 take a cross-section at ts, and determine the strain in the three members cut by it, viz., CE, ED, and DF. Let X = force exerted in direction CE, Y = force exerted in direction DE, Z = force exerted in direction FD.

For X take its moment about the intersection of Y and Z at D = Xx. For Y take its moment about the intersection of X and Z at A = Yy. For Z take its moment about the intersection of X and Z at A = Yy. For Z take its moment about the intersection of X and Y at E = Zz. Let z = 15, x = 18.6, y = 38.4, AD = 50, CD = 20 ft. Let  $P_1, P_2, P_3, P_4$  be equal loads, as shown, and  $3\frac{1}{2}P$  the reaction of the abutment A.

The sum of all the moments taken about D or A or E will be 0 when the structure is at rest. Then  $-Xx+3.5P\times50-P_3\times12.5-P_2\times25-P_1\times$ 

37.5 = 0

The +. signs are for moments in the direction of the hands of a watch or "clockwise" and - signs for the reverse direction or anti-clockwise. Since -18.6X + 175P - 75P = 0; -18.6X = -100P;

 $P_1 = P_2 - P_3$ , -18  $100P \div 18.6 = 5.376P$ 

 $-Yy + P_3 \times 37.5 + P_2 \times 25 + P_1 \times 12.5 = 0$ ; 38.4Y = 75P;  $Y = 75P \div 38.4 = 1953P$ .  $-Zz + 3.5P \times 37.5 - P_1 \times 25 - P_2 \times 12.5 - P_3 \times 0 = 0$ ; 15Z = 93.75P; Z = 93.75P

6.25P. In the same manner the forces exerted in the other members have been found as follows: EG = 6.73P; GJ = 8.07P; JA = 9.42P; JH = 1.35P; GF = 1.59P; AH = 8.75P; HF = 7.50P.

The Fink Roof-truss. (Fig. 129.)-An analysis by Prof. P. H. Philbrick (Van N. Mag., Aug. 1880) gives the following results:

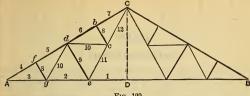


Fig. 129.

W = total load on roof; N = No. of panels on both rafters; $\begin{array}{c} A=\text{NO. of paners on ooth ratters;}\\ W/N=P=\text{load at each joint }b,\ d,f,\text{ etc.;}\\ V=\text{reaction at }A=\frac{1}{2}W=\frac{1}{2}NP=4P;\\ AD=S;\ AC=L;\ CD=D;\\ c_1,c_2,c_3,c_4=\text{compression on }Cb,\ eg,\ g_A,\ \text{respectively;}\\ c_1,c_2,c_3,c_4=\text{compression on }Cb,\ bd,\ df,\ \text{and }fA. \end{array}$ 

Strains in 7, or  $bC = c_1 = 7/2 \ PL/D = 3 \ PD/L$ ; 8, " bc or fg = PS + L; 9, " de = 2PS + L; 10, " cd or  $dg = \frac{1}{2}PS + D$ ; 11, " ec = PS + D; 12, "  $eC = 3/2 \ PS + D$ . 1, or  $De = t_1 = 2PS \div D$ ; or  $De = c_1 = 2PS + D$ ; "  $eg = c_2 = 3PS + D$ ; "  $gA = c_3 = 7/2PS + D$ ; "  $gA = c_4 = 7/2PL + D$ ; "  $fd = c_3 = 7/2PL/D - PD/L$ ; "  $db = c_2 = 7/2PL/D - 2PD/L$ ;

Example .- Given a Fink roof-truss of span 64 ft., depth 16 ft., with four panels on each side, as in the cut; total load 32 tons, or 4 tons each at the points f, d, b, C, etc. (and 2 tons each at A and B, which transmit no strain to the truss members). Here W = 32 tons, P = 4 tons, S = 32 ft., D = 16ft.,  $L = \sqrt{S^2 + D^2} = 2.236 \times D$ . L + D = 2.236, D + L = .4472,  $S \div D = 2$ , S + L = .8944. The strains on the numbered members then are as follows:

```
tons:
       10,
       11,
```

### HEAT.

#### THERMOMETERS.

The Fahrenheit thermometer is generally used in English-speaking countries, and the Centigrade, or French thermometer, in countries that use the metric system. In many scientific treatises in English, however, the Centigrade temperatures are also used, either with or without their Fahrenheit equivalents. The Réaumur thermometer is used in Russia, Sweden, Turkey, and Egypt. (Clark.) In the Fahrenheit thermometer the freezing-point of water is taken at 32°,

and the boiling-point of water at mean atmospheric pressure at the sealevel, 14.7 lbs. per sq. in, is taken at 1929, the distance between these two points being divided into 1809. In the Centigrade and Réaumur thermometers the freezing-point is taken at 0°. The boiling-point is 100° in the Centigrade scale, and 80° in the Réaumur.

= 5/9 deg, Centigrade = 4/9 deg. Réaumur. 1 Fahrenheit degree 1 Centigrade degree = 9/5 deg. Fahrenheit = 4/5 deg. Réaumur

1 Réaumur degree = 9/4 deg. Fahrenheit = 5/4 deg. Centigrade. Temperature Fahrenheit = 9/5 temp. C. +  $32^{\circ}$  = 9/4 R. +  $32^{\circ}$ . Temperature Centigrade = 5/9 (temp. F. -  $32^{\circ}$ ) = 5/4 R. Temperature Réaumur = 4/5 temp. C. = 4/9 (F. -  $32^{\circ}$ )

 $= 4/9 (F. - 32^{\circ}).$ 

Mercurial Thermometer, (Rankine, S. E., p. 234.)-The rate of expansion of mercury with rise of temperature increases as the temperature

becomes higher; from which it follows, that if a thermometer showing the dilatation of mercury simply were made to agree with an air thermometer at 32° and 212°, the mercurial thermometer would show lower temperatures than the air thermometer between those standard points, and higher temperatures beyond them.

For example, according to Regnault, when the air thermometer marked 350° C. (=: 662° F.), the mercurial thermometer would mark 362.16° C. (= 683.89° F.), the error of the latter being in excess 12.16° C. (= 21.89° F.).

Actual mercurial thermometers indicate intervals of temperature proportional to the difference between the expansion of mercury and that of glass. The inequalities in the rate of expansion of the glass (which are very

different for different kinds of glass) correct, to a greater or less extent, the errors arising from the inequalities in the rate of expansion of the mercury. For practical purposes connected with heat engines, the mercurial ther-

mometer made of common glass may be considered as sensibly coinciding with the air-thermometer at all temperatures not exceeding 500° F.

#### PYROMETRY.

Principles Used in Various Pyrometers. - Contraction of clay by heat, as in the Wedgwood pyrometer used by potters. Not accurate, as the contraction varies with the quality of the clay. Expansion of air, as in the air-thermometers, Wiborgh's pyrometer, Ueh-

ling and Steinhart's pyrometer, etc.

Specific heat of solids, as in the copper-ball, platinum-ball, and fire-clay pyrometers. Relative expansion of two metals or other substances, as copper and iron,

as in Brown's and Bulkley's pyrometers, etc. Melting-points of metals, or other substances, as in approximate deter-

minations of temperature by melting pieces of zinc, lead, etc.

Measurement of strength of a thermo-electric current produced by heating the junction of two metals, as in Le Chatelier's pyrometer.

Changes in electric resistance of platinum, as in the Siemens pyrometer. Time required to heat a weighed quantity of water enclosed in a vessel,

as in the water pyrometer.

Thermometer for Temperatures up to 800° F.-Mercury with compressed nitrogen in the tube above the mercury. Made by Queen & Co., Philadelphia,

FAHRENHEIT.													
C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.
-40	-40.	26	78.8	92	197.6	158	316.4	224	435.2	290	554	950	1742
30	-38.2	27	80.6	93	199.4	159	318.2	225	437.	300	572	960	1760
-38	-36.4	28	82.4	94	201.2	160	320.	226	438.8	310	590		1778
-37 -36	$-346 \\ -32.8$	29 30	84.2 86.	95 96	203. 204.8	161 162	321.8 323.6	227 228	440.6 442.4	320 330	608 626	980	1796 1814
$-36 \\ -35$	-31.	31	87.8	97	206.6	163	325.4	229	444.2	340	644	1000	
-34 -33 -32 -31 -30	-29.2	32	89.6	98	208.4	164	327.2	230	446.	350	662	1010	
- 38	$-27.4 \\ -25.6$	33 34	91.4 93.2	99 100	210.2 212.	165 166	329. 330.8	281 282	447.8	360 370	680 698	1020 1030	
-31	-23.81	35	95.	101	213.8	167	332.6	233	451.4	380	716	1040	
-30	-22.	36	96.8	102	215.6	168	334.4	234	453.2	390	734	1050	
-29 -28 -27	$-20.2 \\ -18.4$	37 38	98.6 100.4	103 104	217.4 219.2	169 170	336.2 338.	235 236	455. 456.8	400 410	752 770	1060	1940
-27	-16.6	39	102.2	105	221.	171	339.8	237	458.6	420	788	1080	1976
	-16.6 $-14.8$	40	104.	106	222.8	171 172	341.6	238	460.4	430	806	1000	1004
-25 -24	-13. -11.2	41 42	105.8	107 108	224.6 226.4	173 174	$343.4 \\ 345.2$	239 240	462.2 464.	440 450	824 842	11100	2012 2030
-23	- 9.4	43	107.6 109.4	109	228.2	175	347.	241	465.8	460	860	1120	2048
-23 -22	- 7.6	44	111.2	110	230.	176	348.8	242	467.6	470	878	1130	2066
-21 -20 -19 -18	- 5.8	45	113. 114.8	111	231.8 233.6	177	350.6	243	469.4 471.2	480 490	896	1140	2084 2102
-19	- 4. - 2.2	46	116.6	112 113	235.4	178 179	$352.4 \\ 354.2$	244 245	471.2	500	914		2120
-18	- 2.2 - 0.4	48	118,4	114	237.2	180	356.	246	474.8	510	950	1170	2138
-17 -16 -15 -14	$+\frac{1.4}{3.2}$	49	120.2	115	239.	181	357.8	247	476.6	520	968	1180	2156
-16 -15	5.	50 51	122. 123.8	116 117	240.8 242.6	182 183	359.6 361.4	248 249	478.4 480.2	530 540	986	1200	2174 2192
-14	6.8	52	125,6	118	244.4	184	363.2	250	482.	550	1022	1210	2210
10	8.6	53	127.4 129.2	119	246.2	185	365.	251	483.8	560		1220	
-12 11	10.4 12.2	54 55	131.	120 121	248. 249.8	186 187	366.8 368.6	252 253	485.6 487.4	570 580		1230 1240	
-10	14.	56	132.8	122	251.6	188	370.4	254	489.2		1094	1250	
- 9	15.8	57	134.6	123	253.4	189	372.2	255	491.	600	1112	1260	2300
- 9 - 8 - 7	17.6 19.4	58 59	136.4 138.2	124 125	255.2	190 191	374.	256 257	492.8 494.6	610 620		1270	2318 2336
- 7 - 6 - 5 - 4 - 3 - 2	21.2	60	140.	126	257. 258.8	192	375.8 377.6	258	496.4	630		1290	2354
- 5	23.	61	141.8 143.6	127	260.6	193	379.4	259	498.2	640		1300	2372
- 4 - 3	24.8 26.6	62 63	143.6	128 129	262.4 264.2	194 195	381.2	260 261	500. 501.8	660	1202 1220	1310	2390 2408
- 2 - 1	28.4	64	145.4 147.2	130	266.	196	383. 384.8	262	303.6	670	1238	1330	2426
- 1	30.2	65	149.	131	267.8	197	386.6	263	505.4	680	1256	1340	2444
+ 1	33.8 33.8	66 67	150.8 152.6	132 133	269.6 271.4	198 199	388.4 390.2	264 265	507.2 509.	690	1274 1292		2462
2	35.6	68	154.4	134	278.2	200	392.	266	510.8		1310	1370	2498
3	37.4	69	156.2	135	275.	201	393.8	267	512.6	720	1328	1380	2516
4 5	39.2 41.	70 71	158. 159.8	136 137	276.8 278.6	202 203	395.6 397.4	268 269	514.4 516.2	730 740		1390 1400	
6	42.8	72	161.6	138	280.4	203	399.2	270	518.	750	1382	1410	
7	44.6	73	163.4	139	282.2	205	401.	271	519.8	760	1400	1420	2588
8 9	46.4 48.2	74	165.2	140 141	284.	206 207	402.8	272	521.6 523.4	770 780		1430	
10	50.	75 76	167. 168.8	142	285.8	207	404.6	273 274	525.2	790		1440 1450	2642
11	51.8	77	170.6	143	289.4	209	408.2	275	527.	800	1472	1460	2660
12 13	53.6 55.4	78 79	172.4	144	291.2	210	410.	276 277	528.8 530.6		1490 1508		2678 2696
14	57.2	80	176.	145 146	294.8	211 212	411.8 413.6	278	532.4		1526		2714
15	59.	81	177.8	147	296.6	213	415.4	279	534.2	840	1544	1500	2732
16 17	60.8	82 83	179.6 181.4	148 149	298.4	214 215	417.2	280 281	536. 537.8		1562 1580	1510	2750 2768
18	64.4	84	183.2	150	300.2	216	420.8	282	539.6	870	1598	1530	2786
19	66.2	85	185.	151	303.8	217	422.6	283	541.4	880	1616	1540	2804
20	68.	86 87	186.8 188.6	152	305.6	218 219	424.4	284 285	543.2	890 900	1634 1652	1550	2822 2912
21 22	71.6	88	190.4	158 154	307.4 309.2	219	426.2 428.	286	546.8		1670	1650	3002
23	73.4	89	192.2	155	311.	221	429.8	287	548.6	920	1688	1700	3092
24 25	75.2 77.	90	194. 195.8	156 157	312.8 314.6	222 228	431.6 433.4	288 289	550.4		1706 1724		3182 3272
60	1 11.	91	199.8	101	314.0	220	400.4	8 209	1002.2	940	1123	1000	10012

CENTIGRADE.													
F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.	F.	C.
-40	_40.	26	- 3.3	92	33.3	158	70.	224	106.7	290	143.3		182.2
-39 -38	$-39.4 \\ -38.9$	27 28	- 2.8 - 2.2 - 1.7	93 94	33.9 34.4	159 160	70.6	225 226	107.2 107.8 108.3	291 292	143.9 144.4	370 380	187.8 193.3
-37 -36 -35	-38.3	29	- 1.7	95	35.	161	71.1 71.7 72.2 72.8	227	108.3	293	145.	390	198.9
-36 -35	$-37.8 \\ -37.2$	30 31	-1.1 - 0.6	96 97	35.6 36.1	162 163	72.2	228 229	108.9 109.4	294 295	145.6 146.1	400	204.4 210.
34	-36.7	32	0.	98	36.7	164	73.3	230	110.	296	146.7	420	215.6
-33 -32	-36.1	33	+ 0.6	99	37.2 37.8	165	73.9	231 232	110.6	297	147.2 147.8	430	
-31	-35.6 -35.	34 35	1.1 1.7	100 101	38.3	166 167	74.4	233	111.1 111.7	298 299	148.3	440 450	
-30	34.4	36	2.2	102	38.9	168	75.6	234	112.2	300	148.9	460	237.8
-29 -28	-33.9 -33.3	37 38	2.8 3.3	103 104	39.4	169 170	76.1 76.7	235 236	112.8 113.3	301 302	149.4 150.		243:3 248.9
-27	-32.8	39	3.9	105	40 6	171	77 9	237	113.9	303	150.6	490	254.4
-26 -25 -24 -23 -22 -21 -20	$-32.2 \\ -31.7$	40 41	4.4 5.	106 107	41.1 41.7 42.2 42.8	172 173	77 8 78.3 78.9	238 239	114.4 115.	304 305	151.1 151.7		260. 265,6
-24	-31.1	42	5.6	108	42.2	174	78.9	240	115.6	306	152.2	520	271.1
-23	-30.6	43	6 1	109	42.8	175	79.4	241	116,1	307	152.8	530	276.7
-22 -21	-30. -29.4	44 45	7.2	110 111	43.3 43.9	176 177	80. 80.6	242 243	116.7	308 309	153.3 153.9	540 550	
-20	-28.9	46	6.7 7.2 7.8	112	44.4	177 178 179	81.1	244	117.2 117.8 118.3	310	154.4	560	293 3
-19	$-28.3 \\ -27.8$	47 48	8.3 8.9	113 114	45. 45.6	179 180	81.7	245 246	118.3	311 312	155.6 155.6	570	298.9 304.4
-19 -18 -17	-27.2	49	9.4	115	46.1	181	81.1 81.7 82.2 82.8 83.3	247	119.4	313	156.1	590	310.
-16	-26.7	50	10.	116	46.7 47.2	182	83.3	248	120.	314	156.7		315.6
-15 -14	$-26.1 \\ -25.6$	51 52	10.6	117 118	47.8	188 184	83.9 84.4	249 250	120.6 121.1	315 316	157.2 157.8		321.1 326.7
-13	-25.	53	11.7	119	47.8 48.3	185	85.	251	121.1 121.7	317	158.3	630	332.2
-16 -15 -14 -13 -12 -11	-24.4 $-23.9$	54 55	11.1 11.7 12.2 12.8	120 121	48.9 49.4	186 187	85.6 86.1	252 253	122.2 122.8	318 319	158.9 159.4		337.8 343.3
-10	-23.3	56	13.3	122	50.	188	1 86 7	254	123.3	320	160.	660	348.9
- 9 - 8	-22.8 $-22.2$	57	13.9	123 124	50.6	189 190	87.2 87.8	255 256	123.9 124.4	321 322	160.6	670	354.4
$-\frac{5}{7}$	21.7	58 59	14.4	124	51.7	191	88.3	257	124.4	323	161.1 161.7		360. 365 6
	-21.1	60	15.6	126	52.2 52.8	192	88.9	258	125.6	324	162.2	700	371.1
- 5 - 4	-20.6 -20.	61 62	16.1 16.7	127 128	52.8 53.3	193 194	89.4 90.	259 260	126.1 126.7	325 326	162.8 163.3	710 720	376.7 382.2
- 3	-19.4	63	17.2	129	53.9	195	90.6	261	127.2	327	163.9	730	387.8
- 2 - 1	-18.9	64 65	17.8 18.3	130 131	54.4 55.	196 197	91.1	262 263	127.8 128.3	328 329	164.4 165.		393.3 398.9
0	$-18.3 \\ -17.8$	66	18.9	132	55.6	198	91.7 92.2 92.8	264	128.9	330	165.6	760	404.4
+ 1	$-17.2 \\ -16.7$	67	19.4	133	56.1 56.7	199	92.8 93.3	265	129.4	331	166.1	770	410.
2 3	-16.7	68 69	20. 20.6	134 135	57.2	200 201	93.9	266 267	130. 130.6	332 333	166.7 167.2	780 790	415.6 421.1
4	-15.6	70	21.1	136	57.2 57.8 58.3 58.9	202	94.4	268	121 1	334	167.2 167.8	800	426.7
5 6	-15. -14.4	$\frac{71}{72}$	21.7 22.2	137 138	58.3	203 204	95.	269 270	131.7	335 336	168.3	810 820	432.2 437.8
7	-13.9	73	22.8 23.3	139	59.4	205	95.6 96.1 96.7 97.2 97.8 98.3	271	131.7 132.2 132.8 133.3	337	168.3 168.9 169.4	830	443.3
8 9	-13.3	74 75	23.3 23.9	140 141	60. 60.6	206 207	96.7	272 273	133.3 133.9	338 339	170. 170.6		448.9 454.4
10	-12.2 -11.7	76	24.4	142	61 1	208	97.8	274	134.4	340	171.1	860	460.
11	-11.7	77	25.	143	61.71	209	98.3	275	135.	341	171.7	870	465.6
12 13	$-11.1 \\ -10.6$	78	25.6 26.1	144 145	62.2 62.8	210 211	98.9 99.4	276 277	135.6 136.1	342 343	172.2 172.8		471.1 476.7
14	-10.	80	26.7	146	63.31	212	100.	278		344	172.8 173.3	900	482,2
15 16	-9.4	81 82	27.2 27.8	147 148	63.9 64.4	213 214	100.6 101.1	279 280	137.2 137.8	345 346	173.9 174.4		487.8 493.3
17	- 8.9 - 8.3 - 7.8 - 7.2	83	28.3	149	65.	215	101.7	281	138.3	347	175.	930	498.9
18 19	-7.8	84 85	28.9 29.4	150 151	65.6 66.1	216 217	102.2 102.8	282 283	138,9 139,4	348 349	175.6 176.1	940	504.4
20	- 6.7	86	30.	152	66.7	218	103.3	284	140.	350	176.7	960	515.6
21 22	-6.1 $-5.6$	87 88	30.6 31.1	153 154	67.2 67.8	219 220	103.9 104.4	285 286	140.6 141.1	351 352	177.2	970	521.1 526.7
23 24	<b>—</b> 5.	89	31.7	155	68.3	221	105.	287	141.7	353	176.7 177.2 177.8 178.3	990	532.2
	- 4.4	90	32.2	156	68.9	222 223	105.6	288	149 9	354	178.9	1000	537.8
25	<b>—</b> 3.9	91	32.8	157	69.4	223	106.1	289	142.8	355	179.4	1010	543.3

Platinum or Copper Ball Pyrometer.—A weighed piece of **Platinum or Copper Ball Pyrometer.**—A weighed piece of platinum, copper, or iron is allowed to remain in the furnace or heated chamber till it has attained the temperature of its surroundings. It is then suddenly taken out and dropped into a vessel containing water of a known weight and temperature. The water is stirred rapidly and its maximum temperature taken. Let W = weight of the water, w the weight of the ball,  $t = \text{the original and } T \text{the final heat of the water, } and S \text{the specific heat of the metal; then the temperature of fire may be found from the formula$ 

$$x = \frac{W(T-t)}{wS} + T.$$

For a fuller description, by J. C. Hoadley, see Trans. A. S. M. E., vi, 702. The mean specific heat of platinum above 32° is .03333 or 1/20th that of water, and it increases with the temperature, the increase being about .000305 for each 100° F.

For accuracy corrections are required for variations in the specific heat of the water and of the metal at different temperatures, for loss of heat by radiation from the metal during the transfer from the furnace to the water, and from the apparatus during the heating of the water; also for the heatabsorbing capacity of the vessel containing the water.

Fire-clay or fire-brick may be used instead of the metal ball

Fire-clay or fire-brick may be used instead of the metal Dail.

Le Chatelier's Thermo-electric Pyrometer.—For a very full description see paper by Joseph Struthers, School of Mines Quarterly, vol. xii, 1891; also, paper read by Prof. Roberts-Austen before the Iron and Steel Institute, May 7, 1891.

The principle upon which this pyrometer is constructed is the measurement of a current of electricity produced by heating a couple composed of the produced by the

two wires, one platinum and the other platinum with 10% rhodium—the current produced being measured by a galvanometer.

The composition of the gas which surrounds the couple has no influence on the indications.

When temperatures above 2500° F. are to be studied, the wires must have an isolating support and must be of good length, so that all parts of a furnace can be reached.

For a Siemens furnace, about 11½ feet is the general length. The wires are supported in an iron tube, ½ inch interior diameter and held in place by a cylinder of refractory clay having two holes bored through, in which the wires are placed. The shortness of time (five seconds) allows the temperature to be taken without deteriorating the tube.

Tests made by this pyrometer in measuring furnace temperatures under a great variety of conditions show that the readings of the scale uncorrected are always within 45° F. of the correct temperature, and in the majority of

industrial measurements this is sufficiently accurate. Le Chatelier's pyrometer is sold by Queen & Oo, of Philadelphia.

Graduation of Le Chatelier's Pyrometer.—W. C. Roberts-Austen in his Researches on the Properties of Alloys, Proc. Inst. M. E. 1892, says: The electromotive force produced by heating the thermo-junction to any given temperature is measured by the movement of the spot of light on the scale graduated in millimetres. A formula for converting the divion the scale graduated in millimetres. A formula for converting the divisions of the scale into thermometric degrees is given by M. Le Chateller; but it is better to calibrate the secale by heating the thermo-junction to temperatures the control of the curve from the data so obtained. Many fusion and boiling-points have been established by concurrent evidence of various kinds, and are now very generally accepted. The following table contains certain of these:

Deg. F.	Deg. (	2.	Deg. F.	Deg. (	C.
212	100	Water boils.	1733	945	Silver melts.
618		Lead melts.	1859	1015	Potassium sul-
676	358	Mercury boils.			phate melts.
779	415	Zinc melts.	1913	1045	Gold melts.
838	448	Sulphur boils.	1929	1054	Copper melts.
1157		Aluminum melts.	2732	1500	Palladium melts,
1229	665	Selenium boils.	3227	1775	Platinum melts.
The	Cemn	eratures Develor	ed in Ind	nstri	al Furnaces

M. Le Chatelier states that by means of his pyrometer he has discovered that the temperatures which occur in melting steel and in other industrial operations have been hitherto overestimated.

M. Le Chatelier finds the melting heat of white cast iron 1135° (2075° F.), and that of gray cast iron 1220° (2228° F.). Mild steel melts at 1475° (2887° F.), semi-mild at 1455° (2651° F.), and hard steel at 1410° (2570° F.). The furnace for hard porcelain at the end of the baking has a heat of 1370° (2498° F.). The heat of a normal incandescent lamp is 1800° (2372° F.), but it may be pushed to beyond 2100° (3812° F.).

Prof. Roberts-Austen (Recent Advances in Pyrometry, Trans. A. I. M. E., Chicago Meeting, 1893) gives an excellent description of modern forms of pyrometers. The following are some of his temperature determinations.

GOLD-MELTING, ROYAL MINT.	
Degrees,	Degrees
	Fahr.
Centigrade.	
Temperature of standard alloy, pouring into moulds 1180	2156
Temperature of standard alloy, pouring into moulds (on	
a previous occasion, by thermo-couple) 1147	2097
Annealing blanks for coinage, temperature of chamber 890	1634
Ameung outling for comage, temperature of chambers.	1001
Silver-melting, Royal Mint.	
	4 200 0
Temperature of standard alloy, pouring into mould 980	1796
TEN-TON OPEN-HEARTH FURNACE, WOOLWICH ARSENAL.	
Temperature of steel, 0.3% carbon, pouring into ladle, 1645	2993
Temperature of steel, 0.3% carbon, pouring into large	2000
	0000
mould 1580	2876
Reheating furnace, Woolwich Arsenal, temperature of	
interior 930	1706
Cupola furnace, temperature of No. 2, cast-iron pouring	
into ladle 1600	2912
The following determinations have been effected by M. Le Chatel	lier:

Bessemer Process   Six-ton Converter,   Degrees   Centigrade   Fabruard   Six-ton Converter,   Degrees   Centigrade   Six-ton Converter,   Degrees   Centigrade   Six-ton Converter,   Centigrade   Six-ton Converter,
Degrees   Degrees   Ceptigrands   Ceptigra
Degrees   Degrees   Ceptigrands   Ceptigra
Centigrade   Fabr.   Sept.
A. Bath of slag. 1580 2876 B. Metal in ladle. 1640 2984 C. Metal in ingot mould. 1580 2876 D. Ingot in reheating furnace. 1900 2192 E. Ingot under the hammer 1080 1976  OPEN-HEARTH FURNACE (Siemens). Semi-Mild Steel. A. Fuel gas near gas generator . 720 1328 B. Fuel gas near gas generator . 720 752 C. Fuel gas issuing from regenerator chamber 1000 2192 Air issuing from regenerator chamber . 1200 2192 Air issuing from regenerator chamber . 1200 2192 Air issuing from Pegenerator chamber . 1200 2192 CHIMMEY GASES. Furnace in perfect condition 300 590 OPEN-HEARTH FURNACE. End of the melting of pig charge . 1420 2588 Completion of conversion 1500 2732
B. Metal in ladle.       1640       2984         C. Metal in ingot mould.       1580       2876         D. Ingot in reheating furnace.       1200       2192         OPEN-HEARTH FURNACE (Siemens).         Semi-Mild Steel.         A. Fuel gas near gas generator.       720       1328         B. Fuel gas entering into bottom of regenerator chamber.       1200       752         C. Fuel gas issuing from regenerator chamber.       1200       1882         CHIMNEY GASES.         Furnace in perfect condition.       300       590         OPEN-HEARTH FURNACE.         End of the melting of pig charge.       1420       2588         Completion of conversion.       1500       2732
C. Metal in ingot mould.       1580       2876         D. Ingot in reheating furnace.       1200       2192         E. Ingot under the hammer       1080       1976         OPEN-HEARTH FURNACE (Siemens).         Semi-Mild Steel.         A. Fuel gas near gas generator       720       1328         B. Fuel gas entering into bottom of regenerator chamber 400       752       752         C. Fuel gas issuing from regenerator chamber       1200       2192         Air issuing from regenerator chamber       1000       1832         CHIMMEY GASES.         Furnace in perfect condition       300       590         OPEN-HEARTH FURNACE.         End of the melting of pig charge       1420       2588         Completion of conversion       1500       2732
D. Ingot in reheating furnace
E, Ingot under the hammer
Semi-Mild Steel.   790   1398
Semi-Mild Steel.   790   1398
A. Fuel gas near gas generator       720       1328         B. Fuel gas entering into bottom of regenerator chamber       400       752         C. Fuel gas issuing from regenerator chamber       1200       2192         Air issuing from regenerator chamber       1000       1882         CHIMMEY GASES.         Furnace in perfect condition       300       590         OPEN-HEARTH FURNACE.       End of the melting of pig charge       1420       2588         Completion of conversion       1500       2732
B. Fuel gas entering into bottom of regenerator chamber 400       752         C. Fuel gas issuing from regenerator chamber 1200       2192         Air issuing from regenerator chamber 1000       1832         CHIMNEY GASES.         Furnace in perfect condition 0PEN-HEARTH FURNACE.         End of the melting of pig charge 1420       2588         Completion of conversion 1500       2732
C. Fuel gas issuing from regenerator chamber       1200       2192         Air issuing from regenerator chamber       1000       1882         CHIMMEY GASES.         Furnace in perfect condition       300       590         OPEN-HEARTH FURNACE.         End of the melting of pig charge       1420       2588         Completion of conversion       1500       2732
Air issuing from regenerator chamber.       1000       1832         CHIMNEY GASES.         Furnace in perfect condition       300       590         OPEN-HEARTH FURNACE.         End of the melting of pig charge       1420       2588         Completion of conversion       1500       2732
CHIMNEY GASES.           Furnace in perfect condition         300         590           OPEN-HEARTH FURNACE.         590         1420         2588           End of the melting of pig charge         1420         2588         2588           Completion of conversion         1500         2732
Furnace in perfect condition         300         590           OPEN-HEARTH FURNACE.         1420         2588           Completion of conversion         1500         2732
OPEN-HEARTH FURNACE.           End of the melting of pig charge.         1420         2588           Completion of conversion.         1500         2732
End of the melting of pig charge         1420         2588           Completion of conversion         1500         2732
Completion of conversion
Completion of conversion
MOLTEN STEEL.
In the ladle—Commencement of casting
End of easting
In the moulds
For very mild (soft) steel the temperatures are higher by 50° C.
SIEMENS CRUCIBLE OR POT FURNACE.
18000 C 90190 F

## 1600° C., 2912° F.

#### ROTARY PUDDLING FURNACE. Degrees C. Degrees F ... 1340-1230 2444-2246 Puddled ball—End of operation.....

3506

1930

#### Blast-furnace (Grav-Bessemer Pig).

2552 1400 2858 End, or prior to tapping..... HOFFMAN RED-BRICK KILN.

1100 Burning temperatures ..... 2012

The Wiborgh Air-pyrometer. (E. Trotz, Trans. A. I. M. E. 1892.—The inventor using the expansion-coefficient of air, as determined by Gay-Lussac, Dulon, Rudberg, and Regnault, bases his construction on the following theory: If an air-volume, V. enclosed in a porcelain globe and connected through a capillary pipe with the outside air, be heated to the temperature T (which is to be determined) and thereupon the connection be discontinued, and there be then forced into the globe containing V another volume of air V of known temperature t, which was previously another volume of ar V' of known temperature t, which was previously under atmospheric pressure H, the additional pressure h, due to the addition of the air-volume V' to the air-volume V can be measured by a manueter. But this pressure is of course a function of the temperature T. Before the introduction of V', we have the two separate air-volumes, V at the temperature T, both under the atmospheric pressure H. After the forcing in of V' into the globe, we have, on the contrary, only the volume V of the temperature T, but under the pressure H+h.

The Wiborgh Air-pyrometer is adapted for use at blast-furnaces, smeltingworks, hardening and tempering furnaces, etc., where determinations of

temperature from 0° to 2400° F. are required.

Seger's Fire-clay Pyrometer. (H. M. Howe, Eng. and Mining Jour., June 7, 1890.)—Professor Seger uses a series of slender triangular fire-clay pyramids, about 3 inches high and 95 inch wide at the base, and each a little less fusible than the next: these he calls "normal pyramids" ("normal-kegel"). When the series is placed in a furnace whose temperature is gradually raised, one after another will bend over as its range of plasticity is reached; and the temperature at which it has bent, or "wept," phasticity is reached, and the temperature a winch has occur, a mepo-so far that its apex touches the hearth of the furnace or other level surface on which it is standing, is selected as a point on Seger's scale. These points may be accurately determined by some absolute method, or they may merely serve to give comparative results. Unfortunately, these pyramids afford no indications when the temperature is stationary or falling.

Mesuré and Nouel's Pyrometric Telescope. (Ibid.)-Mesuré and Nouel's pyrometric telescope gives us an immediate determination of the temperature of incandescent bodies, and is therefore much better adapted to cases where a great number of observations are to be made, and at short intervals, than Seger's. Such cases arise in the careful heating of steel. The little telescope, carried in the pocket or hung from the neck, can

be used by foreman or heater at any moment,

It is based on the fact that a plate of quartz, cut at right angles to the axis, rotates the plane of polarization of polarized light to a degree nearly inversely proportional to the square of the length of the waves; and, further, on the fact that while a body at dull redness merely emits red light, as the temperature rises, the orange, yellow, green, and blue waves

successively appear.

If, now, such a plate of quartz is placed between two Nicol prisms at If, now, such a plate or quartz is placed between two fitten prisms as right angles, "a ray of monochromatic light which passes the first, or polarizer, and is watched through the second, or analyzer, is not extinguished as it was before interposing the quartz. Part of the light passes the analyzer, and, to again extinguish it, we must turn one of the Nicols a certain angle," depending on the length of the waves of light, and hence on the temperature of the incandescent object which emits this light. Hence the angle through which we must turn the analyzer to extinguish the light is a measure of the temperature of the object observed.

The instrument is made by Ducretet, of Paris, in two sizes; cost, \$20 and \$25

The Uehling and Steinbart Pyrometer. (For illustrated description see Engineering, Aug. 24, 1894).—The action of the pyrometer is based on a principle which involves the law of the flow of gas through minute apertures in the following manner: If a closed tube or chamber be supplied which aminute inlet and a minute outlet aperture and air be caused by a constant suction to flow in through one and out through the other of these apertures, the tension in the chamber between the apertures will vary with

HEAT.

the difference of temperature between the inflowing and outflowing air. If the inflowing air be made to vary with the temperature to be measured, and the outflowing air be kept at a certain constant temperature, then the tension in the space or chamber between the two apertures will be an exact measure of the temperature of the inflowing air, and hence of the temperature to be measured.

In operation it is necessary that the air be sucked into it through the first minute aperture at the temperature to be measured, through the second aperture at a lower but constant temperature, and that the suction be of a constant tension. The first aperture is therefore located in the end of a platinum tube in the bulb of a porcelain tube over which the hot blast sweeps, or inserted into the pipe or chamber containing the gas whose temperature is to be ascertained.

The second aperture is located in a coupling, surrounded by boiling water. and the suction is obtained by an aspirator and regulated by a column of

water of constant height. The tension in the chamber between the apertures is indicated by a

manometer The Air-thermometer, (Prof. R. C. Carpenter, Eng'g News, Jan. 5, 1893.)—Air is a perfect thermometric substance, and if a given mass of air be considered, the product of its pressure and volume divided by its absolute temperature is in every case constant. If the volume of air remain constant, the temperature will vary with the pressure; if the pressure remain constant the temperature will vary with the volume. As the former condition is more easily attained air-thermometers are usually constructed of constant volume, in which case the absolute temperature

will vary with the pressure.

If we denote pressure by p and p', the corresponding absolute temper-

atures by T and T', we should have

$$p:p'::T:T' \quad \text{and} \quad T'=p'\frac{T}{p}.$$

The absolute temperature T is to be considered in every case 460 higher than the thermometer-reading expressed in Fahrenheit degrees. From the form of the above equation, if the pressure be corresponding to a known absolute temperature, T can be found. The quotient is a constant which may be used in all determinations with the instrument. The pressure on the instrument can be expressed in inches of mercury, and is evidently the atmospheric pressure b as shown by a barometer, plus or minus an additional amount h shown by a manometer attached to the air thermometer.

tional amount h shown by a manometer attached to the air thermometer. That is, in general,  $p=b\times h$ . The temperature of 32° F, is fixed as the point of melting ice, in which case  $T=460\times 32=492^\circ$  F. This temperature can be produced by surrounding the bulb in melting ice and leaving several minutes, so that the temperature of the confined air shall acquire that of the surrounding ice. When the air is at that temperature, note the reading of the attached manometer h, and that of a barometer; the sum will be the value of p corresponding to the absolute temperature of 492° F. The constant of the instrument, K=492-p, once obtained, can be used in all future determinations

High Temperatures judged by Color.—The temperature of a body can be approximately judged by the experienced eye unaided, and M. Pouillet has constructed a table, which has been generally accepted, giving the colors and their corresponding temperature as below:

	_		
Deg. C.	Deg. F.	Deg. C.	Deg. F.
Incipient red heat 525	977	Deep orange heat 1100	2021
Dull'red heat 700	1292	Clear orange heat. 1200	2192
Incipient cherry-red		White heat 1300	2372
heat 800	1472	Bright white heat 1400	2552
Cherry-red heat 900	1652	) 1500	2732
Clear cherry - red		Dazzling white heat > to	to
heat 1000	1832	Dazzling white heat 1500 to 1600	2912

The results obtained, however, are unsatisfactory, as much depends on the susceptibility of the retina of the observer to light as well as the degree of illumination under which the observation is made.

A bright bar of iron, slowly heated in contact with air, assumes the following tints at annexed temperatures (Claudel):

	Cent.	Fahr.	1	Cent.	Fahr.
Yellow at	225	437	Indigo at	288	550
Orange at	243	473	Blue at	293	559
Red at	265	509	Green at		630
Violet at	217	531	"Oxide-gray"	400	752

#### BOILING POINTS AT ATMOSPHERIC PRESSURE. 14.7 lbs. per square inch.

	P	4	
Ether, sulphuric. Carbon bisulphide. Ammonia Chloroform. Bromine Wood spirit. Alcohol.	100° F. 118 140 140 145 150 173	Average sea-water. Saturated brine. Nitric acid Oil of turpentine Phosphorus Sulphur. Sulphuric acid	226 248 315 554 570 590
Benzine	176	Linseed oil	597

The boiling points of liquids increase as the pressure increases. The boiling point of water at any given pressure is the same as the temperature of saturated steam of the same pressure. (See Steam.)

#### MELTING-POINTS OF VARIOUS SUBSTANCES.

The following figures are given by Clark (on the authority of Pouillet, Claudel, and Wilson), except those marked \*, which are given by Prof. Roberts-Austen in his description of the Le Chatelier pyrometer. These latter are probably the most reliable figures.

Sulphurous acid	148° F.	Alloy, 1 tin, 1 lead 370 to 466°	F
Carbonic acid	108	Tin 442 to 446	
Mercury		Cadmium 442	
Bromine +	9.5	Bismuth 504 to 507	
Turpentine	14	Lead 608 to 618*	
Hyponitric acid	16	Zinc 680 to 779*	
Ice		Antimony 810 to 1150	
Nitro-glycerine		Aluminum 1157*	
Tallow	92	Magnesium 1200	
Phosphorus		Calcium Full red heat.	
Acetic acid		Bronze	
Stearine 109 to		Silver 1733* to 1873	
Spermaceti		Potassium sulphate 1859*	
Margaric acid 131 to	140	Gold 1913* to 2282	
Potassium 136 to	144	Copper 1929* to 1996	
Wax 142 to		Cast iron, white 1922 to 2075*	
Stearic acid		" gray 2012 to 2786 2228*	
Sodium 194 to		Steel 2372 to 2532	
Alloy, 3 lead, 2 tin, 5 bismuth		" hard 2570*; mild, 2687*	
Iodine		Wrought iron 2732 to 2912	
Sulphur		Palladium 2732*	
Alloy, 11/6 tin, 1 lead		Platinum 3227*	
zinoj, 1/2 mi, 1 leau	0.01	T. 10011141111111111111111111111111111111	

For melting-point of fusible alloys, see Alloys. Cobalt, nickel, and manganese, fusible in highest heat of a forge. Tung-sten and chromium, not fusible in forge, but soften and agglomerate. Platinum and iridium, fusible only before the oxyhydrogen blowpipe.

#### QUANTITATIVE MEASUREMENT OF HEAT.

Unit of Heat .- The British unit of heat, or British thermal unit (B. T. U.), is that quantity of heat which is required to raise the temperature of 1 lb. of pure water 1° Fahr., at or near 39°.1 F., the temperature of maximum density of water.

The French thermal unit, or calorie, is that quantity of heat which is required to raise the temperature of 1 kilogramme of pure water 1° Cent., at or

about 4° C., which is equivalent to 39°.1 F.

1 French calorie = 3.968 British thermal units; 1 B. T. U. = .252 calorie. The "pound calorie" is sometimes used by English writers; it is the quan456

tity of heat required to raise the temperature of 1 lb. of water 1° C. 1 lb. calorie = 2.2046 B. T. U. = 5/9 calorie. The heat of combustion of carbon, to  $CO_2$ , is said to be 8080 calories. This figure is used either for French calories or (O<sub>2</sub>, 18 still to be observations. This liquid is used entire for the database of ror pound calories, as it is the number of pounds of water that can be raised 1° C, by the complete combustion of 1 lb, of carbon, or the number of kilogrammes of water that can be raised 1° C, by the combustion of 1 kilo. of carbon; assuming in each case that all the heat generated is transferred to the water.

The Mechanical Equivalent of Heat is the number of foot-pounds of mechanical energy equivalent to one British thermal unit, heat and mechanical energy being mutually convertible. Joule's experiments, 1843-50, gave the figure 772, which is known as Joule's equivalent. More re-cent experiments by Prof. Rowland (Proc. Am. Acad. Arts and Sciences, 1880; see also Wood's Thermodynamics) give higher figures, and the most probable average is now considered to be 778.

1 heat-unit is equivalent to 778 ft.-lbs. of energy. 1 ft. lb. = 1/778 = .0012852 heat-units. 1 horse-power = 33,000 ft.-lbs. per minute = 2545 heat-units per hour = 42.416 + per minute = .70694 per second. 1 lb. carbon burned to  $CO_2 = 14.544 \text{ heat-units.}$  1 lb. C. per H.P. per hour =  $2545 + 14544 = 17\frac{1}{2}$ % efficiency (.174986).

Heat of Combustion of Various Substances in Oxygen.

	Heat	units.	Authority.
	Cent.	Fahr.	
	(34,462	69 039	Favre and Silbermann.
Hydrogen to liquid water at 0° C	₹ 33,808	60,854	Andrews.
" to steam at 100° C	( 34,342 28,732	51,717	Thomsen. Favre and Silbermann.
Carbon (wood charcoal) to carbonic	\$ 8,080 7,900		Andrews.
acid, CO <sub>2</sub> ; ordinary temperatures.	( 8,137	14,647	Berthelot.
Carbon, diamond to CO <sub>2</sub>	7,859 7,861		"
" graphite to CO <sub>2</sub>	7,901 2,473	14,222	"Favre and Silbermann.
· ·	( 2,403	4,325	
Carbonic oxide to CO <sub>2</sub> , per unit of CO	2,431 2,385		Andrews. Thomsen.
CO to CO <sub>2</sub> per unit of $C = 2\frac{1}{3} \times 2403$	5,607		Favre and Silbermann. Thomsen.
Marsh-gas, Methane, CH <sub>4</sub> to water and CO <sub>2</sub>	13,108	23,594	Andrews.
	(13,063 (11,858		Favre and Silbermann.
Olefiant gas, Ethylene, C <sub>2</sub> H <sub>4</sub> to water and CO <sub>2</sub>	11,942 11,957	21,496	Andrews. Thomsen.
Benzole gas, C6H6 to water and CO2	1 10,102	18,184	**
Dempore Burst Child to mater and Co.	9,915	17,847	Favre and Silbermann.

In burning 1 pound of hydrogen with 8 pounds of oxygen to form 9 pounds nourning I pound of hydrogen with 5 pounds of oxygen to form 9 pounds of water, the units of heat evolved are 62,032 (Favre and S.); but if the resulting product is not cooled to the initial temperature of the gases, part of the beat is rendered latent in the steam. The total heat of 1 lb. of steam at 212° F. is 1146.1 heat-units above that of water at 32°, and 9×1146 I = 10,315 heat-units, which deducted from 62,032 gives 51,777 as the heat evolved by the combustion of 1 lb. of hydrogen and 8 lbs. of oxygen at 32° F, to form steam at 212° F.

By the decomposition of a chemical compound as much heat is absorbed or rendered latent as was evolved when the compound was formed. If 1 lb. of carbon is burned to CO<sub>2</sub>, generating 14,544 B.T.U., and the CO<sub>2</sub> thus formed is immediately reduced to CO in the presence of glowing carbon, by the reaction  $CO_2 + C = 2CO$ , the result is the same as if the 2 lbs. C had been burned directly to 200, generating 2 × 4451 = 8902 heat-units; consequently 14.544 - 8902 = 5642 heat units have disappeared or become latent, and the

"unburning" of CO2 to CO is thus a cooling operation. (For heats of combustion of various fuels, see Fuel.)

#### SPECIFIC HEAT.

Thermal Capacity. - The thermal capacity of a body is the quantity of heat required to raise its temperature one degree. The ratio of the heat required to raise the temperature of a given substance one degree to that required to raise the temperature of a given substance one degree to maximum density 39.1 is commonly called the specific heat of the substance. Some writers object to the term as being an inaccurate use of the words "specific" and "heat." A more correct name would be "coefficient of thermal capacity."

**Determination of Specific Heat.**—Method by Mixture.—The body whose specific heat is to be determined is raised to a known temperature, and is then immersed in a mass of liquid of which the weight, specific heat, and temperature are known. When both the body and the liquid

have attained the same temperature, this is carefully ascertained.

Now the quantity of heat lost by the body is the same as the quantity of

heat absorbed by the liquid. Let c, w, and t be the specific heat, weight, and temperature of the hot body, and c', w', and t' of the liquid. Let T be the temperature the mix-

ture assumes.

A -- A2--- - ----

Then, by the definition of specific heat,  $c \times w \times (t-T) = \text{heat-units lost}$  by the hot body, and  $c' \times w' \times (T-t') = \text{heat-units gained by the cold liquid. If there is no heat lost by radiation or conduction, these must be$ equal, and

$$cw(t-T)=c'w'(T-t')\quad\text{or}\quad c=\frac{c'w'\left(T-t'\right)}{w(t-T)}.$$

#### Specific Heats of Various Substances.

The specific heats of substances, as given by different authorities, show

considerable lack of agreement, especially in the case of gases.

The following tables give the mean specific heats of the substances named according to Regnault. (From Rontgen's Thermodynamics, p. 134.) These specific heats are average values, taken at temperatures which usually commender observation in technical application. The actual specific heats of all substances, in the solid or liquid state, increase slowly as the body expands or as the temperature rises. It is probable that the specific heat of a body when liquid is greater than when solid. For many bodies this has been verified by experiment.

	So	LI	DS.	
Δ	OFFICE	,	Ctool	(antt)

Copper 0.0951	Steel (hard) 0 1175				
Gold 0.0324	Zinc 0.0956				
Wrought iron 0.1138	Brass 0,0939				
Glass 0.1937	Ice 0.5040				
Cast iron 0.1298	Sulphur 0,2026				
Lead 0.0314	Charcoal 0.2410				
Platinum 0.0324	Alumina 0.1970				
Silver 0.0570	Phosphorus 0.1887				
Tiu 0.0562					
Liquids,					

	24.40	100.	
Water	1.0000	Mercury	0.0333
Lead (melted)	0.0402	Alcohol (absolute)	0.7000
Sulphur "	0.2340	Fusel oil	
Bismuth "	0.0308	Benzine	
Tin "Sulphurio soid	0.0637	Ether	0.5034
	0.3320		

In a (Select Platin (incr Cadmi Brass, Coppe Zinc Nickel Alumi poin

Marbl Chalk Quick Magne Silica Corun Stones Pine (Fir ...

Sulph

Per Spec

HE	AT.	
	SES.	
	onstant Pressure	Constant Volume. 0.16847
Air Oxygen		0.15507
Hydrogen	3.40900	2.41226
Nitrogen	0,24380	0.17273
Superheated steam	0.4805	0.346
Carbonic acid	0.217	0.1535 0.173
Carbonic oxide		0.1758
Ammonia	0.508	0.299
Ether	0.4797	0.3411
Alcohol	0.4534	0.3200
Acetic acid		******
addition to the above, the follo		on other authorities
eted from various sources.)	wing are given t	by other authorities.
MET	ALS.	
um at 32° F	Wrought iron (F	Petit & Dulong)
reased .000305 for each 100° F.)	" 3	2° to 212°
ium	" 35	2° to 212°1098 2° to 392°115 2° to 572°1218
	" 35	2° to 572°
er, 32° to 212° F	Wronght iven (I	C Hoodley
82° to 212° F 0927	A S. M. E. v	i 713)
32° to 572° F	Wrought iron, 8	i. 713), 32° to 200°1129 32° to 600°1327
	" 9	32° to 600°1327
inum, 0° F. to melting-	" 3	2° to 2000°
inum, 0° F. to melting- nt (A. E. Hunt) 0.2185	~ .	
OTHER		*
work and masonry, about20		20 to 241
le	Graphite	
lime	Sulphate of lime	e
esian limestone	Magnesia	
	Soda	
ndum	Quartz	
s generallyz to zz	River sand	
. Wo		
turpentine)		
	Pear	
Liqu	IDS.	
ol. density 793	Olive oil	
uric acid, density 1.87 335	Benzine	
ol, density .793	Turpentine, den	sity .872472
ochloric acid	Bromine	1.111
GA	SES.	
	At Con	
Gulphunoug apid	Press	sure. Volume.
Sulphurous acidLight carburetted hydrogen, ma	rsh cas (CH.) 50	929 .4683
Blast-furnace gases	845 (0114)02	277
Specific Heat of Sal	t solution. (S	chuner.)
cent salt in solution 5 cific heat	06 8000 860	5 20 25 06 .8490 .8078
cine neat	,000	.0400 .0010

Specific Heat of Air .- Regnault gives for the mean value

the specific heat of a fixed gas at constant pressure to the sp. ht. at constant volume is given as follows by different writers (Eng'g, July 12, 1889); Regnantt, 1,3953; Moll and Beck, 1,4985; Szahmari, 1,497; J. Macfarlane Gray, 1.4. The first three are obtained from the velocity of sound in air. The fourth is derived from theory. Prof. Wood says: The value of the ratio for air, as found in the days of La Place, was 1.41, and we have 0.3277 ÷ 1.41 = 0.1866, the value used by Clausius, Hanssen, and many others. But this ratio is not definitely known. Rankine in his later writings used 1.408, and Tait in a recent work gives 1.404, while some experiments gives less than 1.4 and others more than 1.41. Prof. Wood uses 1.406.

Specific Heat of Gases, Experiments by Mallard and Le Chatelier inducate a continuous increase in the specific heat at constant volume of sterm CO. and were of the perfect sases with rise of temperature. The

steam, CO<sub>2</sub>, and even of the perfect gases, with rise of temperature. The variation is inappreciable at 100° C., but increases rapidly at the high temperatures of the gas-engine cylinder. (Robinson's Gas and Petroleum

Engines.)

### Specific Heat and Latent Heat of Fusion of Iron and Steel. (H. H. Campbell, Trans. A. I. M. E., xix, 181.)

			Åkerman.	Troilius.
Specific	heat	pig iron,	0 to 1200° C 0.16	
- 44	66	- "	1200 to 1800° C 0.21	
44	66	66	0 to 1500° C	0.18
44	**	**	1500 to 1800° C	0.20

#### Calculating by both sets of data we have :

Heating from 0 to 1800° C
Hence probable value is about 325 calories per kilo.
Specific heat, steel (probably high carbon)(Troilius) ,1175
" soft iron "
Hence probable value solid rail steel
" " melted rail steel
Akerman, Troilius,

Akarman Troiling

Latent heat of fusion, pig iron, calories per kilo., 46 33

gray pig ..

#### EXPANSION BY HEAT.

In the centigrade scale the coefficient of expansion of air per degree is 0.003665 = 1/273; that is, the pressure being constant, the volume of a perfect gas increases 1/273 of its volume at 0° C. for every increase in temperature of °C. In Falrenheit units it increases 1/491.2 = .002036 of its volume at 32° F. for every increase of 1° F.

#### Expansion of Gases by Heat from 32° to 212° F. (Regnault.)

	Pressur	e Constant. at 32° Fahr.	Increase in Pressure, Volume Constant. Pressure at 32° Fahr. = 1.0, for		
	100° C.	1° F.	100° C.	1° F.	
Hydrogen. Atmospheric air. / Nitrogen Carbonic oxide Carbonic acid Sulphurous acid	0.3661 0.3670 0.3670 0.3669 0.3710 0.3903	0.002034 0.002039 0.002039 0.002038 0.002061 0.002168	0.3667 0.3665 0.3668 0.3667 0.3688 0.3845	0.002037 0.002036 0.002039 0.002037 0.002039 0.002136	

If the volume is kept constant, the pressure varies directly as the absolute temperature.

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### Lineal Expansion of Solids at Ordinary Temperatures.

(British Board of Trade; from CLARK)

	For 1° Fahr,	For 1° Cent.	Coef- ficient of Expan- sion from 32° to 212° F.	According to Other Authorities.
	Length = 1	Length=1		
Aluminum (cast)	.00001234	.00002221	.002221	
Antimony (cryst.)	.00000627	.00001129	.001129	.001083
Brass, cast	.00000957	.00001722	.001722	.001868
" plate	.00001052	.00001894	.001894	
Brick	.00000306	.00000550	,000550	
Bronze (Copper, 17; Tin, 2½; Zinc 1). Bismuth	.00000986	.00001774	.001774	
Bismuth	.00000975	.00001755	.001755	.001392
Cement, Portland (mixed), pure	.00000594	.00001070	.001070	
Concrete: cement, mortar, and pebbles Copper	.00000783	.00001430	.001430	.001718
Ebonite	.00004278	.00007700	007700	.001710
Glass, English flint	.00000451	.00000812	.000812	
" thermometer	.00000199	.00000897	.000897	
" hard	.00000397	.00000714	.000714	
Granite, gray, dry	.00000438	.00000789	.000789	
" red, dry	.00000498	.00000897	.000897	
Gold, pure	.00000786	.00001415	.001415	
Iridium, pure	.00000356	.00000641	.000641	001005
Iron, wrought	.00000556	.00001100	.001166	.001235
Lead	.00000550	.00002828	.002828	.001110
Magnesium	.00001011	.00002040		.002694
Magnesium  Marbles, various from to	.000000308	.00000554	000554	
Marbles, various to	.00000786	.00001415	.001415	
Masonry, brick (from to mercury (cubic expansion)	.00000256	.00000460	.000460	
blasonry, orkk i to	.00000494	.00000890	.000890	12722112
Mercury (cubic expansion)	.00009984	.00017971	.017971	.018018
Nickel Pewter	.00000695	.00001251	.001251	.001279
Plaster, white	.000001129	.00001660	.002033	
Platinum	.00000479	.00000863	.000863	
Platinum, 85 per cent { Iridium, 15 " { Porcelain Ougartz parallel to major axis #00 to				
Iridium, 15 " " (	.00000453	.00000815	.000815	.000884
Porcelain	.000000200	.00000380	.000360	
Quality, paramer to major axis, to to				1
40° C	.00000434	.00000781	.000781	
Quartz, perpendicular to major axis,	.00000788	.00001419	001410	
Silver, pure	.000001079	.00001413	.001419	.001908
Slate	.00000577	.00001038	.001038	.001908
Steel, cast	.00000636	.00001144	.001144	.001079
Steel, cast	00000689	.00001240	.001240	
Stone (sandstone), dry Rauville	.00000652	.00001174	.001174	
Rauville	.00000417	.00000750	.000750	
1111	.00001168	.00002094	.002094	.001938
Wedgwood ware	.00000489	.00000881	.000881	
Zinc	.00000276	.00000496	.000496	.002942
Zinc. 81				.00.8942
Zine, 8 ( Tin, 1 }	.00001496	.00002692	.002692	
	1	1		

Absolute Temperature-Absolute Zero. - The absolute zero of a gas is a theoretical consequence of the law of expansion by heat, assuming that it is possible to continue the cooling of a perfect gas until its volume is

diminished to nothing.

If the volume of a perfect gas increases 1/273 of its volume at 0° C. for If the volume of a perfect gas increases 1/273 of its volume at 0° C, for every increase of temperature of 1° C, and decreases 1/273 of its volume for every decrease of temperature of 1° C, then at  $-2.73^\circ$  C, the volume of the imaginary gas would be reduced to nothing. This point  $-2.73^\circ$  C, or  $491.2^\circ$  F, below the melting-point of ice on the air thermometer, or  $492.66^\circ$  F, below on a perfect gas thermometer  $-49.26^\circ$  F, for  $-460.669^\circ$ ), is called the absolute zero; and absolute temperatures are temperatures measured, on either the Fahrenheit or centigrade scale, from this zero. The freezing point,  $32^\circ$  F, corresponds to  $491.2^\circ$  F, absolute. If  $p_0$  be the pressure and  $v_0$  the volume of a gas at the temperature of  $32^\circ$  F,  $-491.2^\circ$  on the absolute scale  $-T_0$ , and p the pressure, and v the volume of the same quantity of  $v_0$  at a two other absolute temperature T. then

 $\frac{pv}{T} = \frac{T}{T} = \frac{t + 459.2}{491.2}; \quad \frac{pv}{T} = \frac{p_0v_0}{T_0}.$  The value of  $p_0v_0 \neq T_0$  for air is 53.37, and pv = 53.37T, calculated as follows by Prof. Wood:

A cubic foot of dry air at 32° F. at the sea-level weighs 0.080728 lb. The volume of one pound is  $v_0 = \frac{1}{.080728} = 12.387$  cubic feet. The pressure per

square foot is 2116.2 lbs.

$$\frac{p_0 v_0}{T_0} = \frac{2116.2 \times 12.387}{491.13} = \frac{26214}{491.13} = 53.37.$$

The figure 491.13 is the number of degrees that the absolute zero is become the melting-point of ice, by the air thermometer. On the absolute scale, whose divisions would be indicated by a perfect gas thermometer, the calculated value approximately is 492.66, which would make pv = 53.21T. Prof. Thomson considers that  $-273.1^{\circ}$  C.,  $= -491.4^{\circ}$  F., is the most probable value of the absolute zero. See Heat in Ency. Brit.

Expansion of Liquids from  $32^{\circ}$  to  $212^{\circ}$  F.—Apparent expansion in glass (Clark). Volume at  $212^{\circ}$ , volume at  $32^{\circ}$  being 1: The figure 491.13 is the number of degrees that the absolute zero is below

Water saturated with salt... 1.05
Mercury... Nitric acid..... Olive and linseed oils. 1.08
Turpentine and ether 1.07 Mercury ...... 1.0182 Alcohol ..... 1.11 Hydrochlor, and sulphuric acids 1.06 For water at various temperatures, see Water.

For air at various temperatures, see Air,

#### LATENT HEATS OF FUSION AND EVAPORATION.

Latent Heat means a quantity of heat which has disappeared, having been employed to produce some change other than elevation of temperature. By exactly reversing that change, the quantity of heat which has disappeared is reproduced. Maxwell defines it as the quantity of heat which must be communicated to a body in a given state in order to convert it into another state without changing its temperature.

Latent Heat of Fusion .- When a body passes from the solid to the liquid state, its temperature remains stationary, or nearly stationary, at a certain melting point during the whole operation of melting; and in order to make that operation go on, a quantity of heat must be transferred to the substance melted, being a certain amount for each unit of weight of the

substance. This quantity is called the latent heat of fusion.

When a body passes from the liquid to the solid state, its temperature remains stationary or nearly stationary during the whole operation of freezing; a quantity of heat equal to the latent heat of fusion is produced in the body and rejected into the atmosphere or other surrounding bodies.

The following are examples in British thermal units per pound, as given

by Rankine:

MILIO.		
Substances.	Melting Points.	Latent Hear of Fusion.
T ()		142.65
Ice (according to Person)		
Spermaceti		148
Beeswax		175
Phosphorus		9.06
Sulphur		16.86
Tin	426	500

Prof. Wood considers 144 heat units as the most reliable value for the latent heat of fusion of ice. Box gives only 26.6 for tin. Clements gives 233 for cast iron

Latent Heat of Evaporation, -When a body passes from the solid or liquid to the gaseous state, its temperature during the operation remains stationary at a certain boiling point, depending on the pressure of the vapor produced; and in order to make the evaporation go on, a quantity of heat must be transferred to the substance evaporated, whose amount for each unit of weight of the substance evaporated depends on the temperature. That heat does not raise the temperature of the substance, but disappears in causing it to assume the gaseous state, and it is called the latent heat of evaporation.

When a body passes from the gaseous state to the liquid or solid state, its when a body passes from the gaseous state to endure or some state to the temperature remains stationary, during that operation, at the boiling point corresponding to the pressure of the vapor; a quantity of heat equal to the latent heat of evaporation at that temperature is produced in the body; and in order that the operation of condensation may go on, that heat must be

transferred from the body condensed to some other body.

The following are examples of the latent heat of evaporation in British thermal units, of one pound of certain substances, when the pressure of the vapor is one atmosphere of 14.7 lbs. on the square inch:

Substance.	Boiling-point under one atm. Fahr.	Latent Heat in British units.
Water	212.0	965.7 (Regnault.)
Alcohol	172.2	364.3 (Andrews.)
Ether	95.0	162.8 "
Bisulphide of carbon	114.8	156.0 "
The latent heat of eva-coration	of water at a carios	of boiling points or

tending from a few degrees below its freezing-point up to about 375 degrees Fahrenheit has been determined experimentally by M. Regnault. The results of those experiments are represented approximately by the formula, in British thermal units per pound,

$$l \text{ nearly} = 1091.7 - 0.7(t - 32^{\circ}) = 965.7 - 0.7(t - 212^{\circ}).$$

The Total Heat of Evaporation is the sum of the heat which disappears in evaporating one pound of a given substance at a given tem-perature (or latent heat of evaporation) and of the heat required to raise its temperature, before evaporation, from some fixed temperature up to the temperature of evaporation. The latter part of the total heat is called the sensible heat.

In the case of water, the experiments of M. Regnault show that the total heat of steam from the temperature of melting ice increases at a uniform rate as the temperature of evaporation rises. The following is the formula in British thermal units per pound:

$$h = 1091.7 \pm 0.305(t - 32^{\circ}).$$

For the total heat, latent heat, etc., of steam at different pressures, see table of the Properties of Saturated Stram. For tables of total heat, latent heat, and other properties of steams of ether, alcohol, acetone, chloroform, chloride of carbon, and bisulphide of carbon, see Rontgen's Thermodynamics (Dubois's translation.) For ammonia and sulphur dioxide, see Wood's Thermodynamics; also, tables under Refrigerating Machinery, in this book.

#### EVAPORATION AND DRYING.

In evaporation, the formation of vapor takes place on the surface; in boiling, within the liquid: the former is a slow, the latter a quick, method of

evaporation.

If we bring an open vessel with water under the receiver of an air-pump and exhaust the air the water in the vessel will commence to boil, and if we keep up the vacuum the water will actually boil near its freezing-point. The formation of steam in this case is due to the heat which the water takes out of the surroundings.

Steam formed under pressure has the same temperature as the liquid in which it was formed, provided the steam is kept under the same pressure

By properly cooling the rising steam from boiling water, as in the multipleeffect evaporating systems, we can regulate the pressure so that the water b ils at low temperatures.

Evaporation of Water in Reservoirs.—Experiments at the Mount Hope Reservoir, Rochester, N. Y., in 1891, gave the following results:

	July.	Aug. 70.3	Sept.	Oct.
Mean temperature of air in shade	70.5	70.3	68.7	53.3
" water in reservoir		70.2	66.1	54.4
" humidity of air, per cent	67.0	74.6	75.2	74.7
Evaporation in inches during month	5.59	4.93	4.05	3.23
Rainfall in inches during month	3.44	2.95	1.44	2.16

Evaporation of Water from Open Channels. (Flynn's Irrigation Canals and Flow of Water.)—Experiments from 1881 to 1885 in Tulare County, California, showed an evaporation from a pan in the river equal to an average depth of one eighth of an inch per day throughout the

year.

When the pan was in the air the average evaporation was less than 3/16

of an inch per day. The average for the month of August was 1/8 inch per

of an inch per day. The average for the month of August was 1/8 inch per day. day, and for March and April 1/12 of an inch per day. Experiments in Colorado show that evaporation ranges from .088 to .16 of an inch per day during the irrigating season.

In Northern Italy the evaporation was from 1/12 to 1/9 inch per day, while in the south, under the influence of hot winds, it was from 1/6 to 1/5 inch

per day.

In the hot season in Northern India, with a decidedly hot wind blowing. the average evaporation was 1/4 inch per day. The evaporation increases

with the temperature of the water.

Evaporation by the Multiple System.—A multiple effect is a series of evaporating vessels each having a steam chamber, so connected that the heat of the steam or vapor produced in the first vessel heats the second, the vapor or steam produced in the second heats the third, and so on. The vapor from the last vessel is condensed in a condenser. Three vessels are generally used, in which case the apparatus is called a *Triple* Effect. In evaporating in a triple effect the vacuum is graduated so that the

liquid is boiled at a constant and low temperature,

Resistance to Boiling.—Brine. (Rankine.)—The presence in a liquid of a substance dissolved in it (as salt in water) resists ebullition, and raises the temperature at which the liquid boils, under a given pressure; but unless the dissolved substance enters into the composition of the vapor, the relation between the temperature and pressure of saturation of the vapor remains unchanged. A resistance to ebullition is also offered by a vessel of remains unchanged. At established to combine the action of as a material which attracts the liquid (as when water boils in a glass vessel), and the boiling take place by starts. To avoid the errors which causes of this kind produce in the measurement of boiling-points, it is advisable to place the thermometer, not in the liquid, but in the vapor, which shows the true boiling-point, freed from the disturbing effect of the attractive nature of the vessel. The boiling-point of saturated brine under one atmosphere is 226° Fahr., and that of weaker brine is higher than the boiling-point of pure water by 1.2° Fahr., for each 1/32 of salt that the water contains. Average sea-water contains 1/32; and the brine in marine boilers is not suffered to contain more than from 2/32 to 3/32.

Methods of Evaporation Employed in the Manufacture f Salt. (F. E. Engelhardt, Chemist Onondaga Salt Springs; Report for of Salt. (F. E. Engelhardt, Chemist Onondaga Salt Springs; Report for 1889.)—1. Solar heat—solar evaporation. 2. Direct fire, applied to the heating surface of the vessels containing brine—kettle and pan methods. 3. The steam-grainer system-steam-pans, steam-kettles, etc. 4. Use of steam and a reduction of the atmospheric pressure over the boiling brine-vacuum

system.

When a saturated salt solution boils, it is immaterial whether it is done under ordinary atmospheric pressure at 228° F., or under 1/10 atmospheres with a temperature of 320° F., or in a vacuum under 1/10 atmosphere, the

result will always be a fine-grained salt.

The fuel consumption is stated to be as follows: By the kettle method, 40 to 45 bu. of salt evaporated per ton of fuel, anthracite dust burned on perto 45 of the dates; evaporated per found the particular that the p double that amount can be produced.

#### Solubility of Common Salt in Pure Water. (Andreæ.)

Temp, of brine, F	32		86			176
100 parts water dissolve parts	35.63	35.69	36.03	36.82	37.06	38.00
100 parts brine contain salt	26.27	26.30	26.49	26.64	27.04	27.54

According to Poggial, 100 parts of water dissolve at 229.66° F., 40.35 parts of salt, or in per cent of brine, 28.749. Gay Lussac found that at 229.72° F., 100 parts of pure water would dissolve 40.38 parts of salt, in per cent of brine, 28.764 parts.

The solubility of salt at 229° F. is only 2.5% greater than at 32°. Hence we

The solubility of salt at 223° F. is only 2.5% greater than at 32°. Hence we cannot, as in the case of alum, separate the salt from the water by allowing a saturated solution at the boiling point to cool to a lower temperature.

# Solubility of Sulphate of Lime in Pure Water. (Marignac.) Cemperature F. degrees. 32 64.5 89.6 100.4 105.8 127.4 186.8 212

Temperature F. degrees.	32	64.5	89.6	100.4	105.8	127.4	186.8	212
Parts water to dissolve	415	386	371	368	370	375	417	452
Parts water to dissolve 1 ( part anhydrous CaSO <sub>4</sub> )	525	488	470	466	468	474	528	572

In salt brine sulphate of lime is much more soluble than in pure water. In the evaporation of salt brine the accumulation of sulphate of lime tends to stop the operation, and it must be removed from the pans to avoid waste of fuel.

The average strength of brine in the New York salt districts in 1889 was 69.38 degrees of the salinometer.

Strength of Salt Brines,—The following table is condensed from one given in U. S. Mineral Resources for 1888, on the authority of Dr. Englehardt.

Relations between Salinometer Strength, Specific Gravity, Solid Contents, etc., of Brines of Different Strengths.

Salinometer, degrees.	Baumé, degrees.	Specific gravity.	Per cent of salt.	Weight of a gallon of this brine in pounds.	Pounds of salt in a gallon of brine of 231 cubic inches.	Gallons of brine required for a bushel of salt.	Pounds of water to be evaporated to produce a bushel of salt.	Lbs. of coal required to produce a bushel of salt, 1 lb. coal evaporating 6 lbs. of water.	Bushels of salt that can be made with a ton of coal of 2000 pounds.
1	.26 .52 1.04 1.56	1.002	.265 .530 1.060 1.590	8.347	.022 .044 .088 .133 .179 .224 .270 .316 .364 .410 .457 .698 .947 1.206 1.475 1.755	2,531 1,264 629.7	21,076 10,510 5,227 3,466 2,585	3,513 1,752 871.2	.569
2	.52	1.003	.530	8.356 8.389	.044	1,264	10,510	1,752	1.141
4	1.04	1.007	1,000	8.389	.088	629.7	5,227	871.2	1.141 2.295 3.462
6	1.00	1.010	0.100	8.414	.133	418.6	3,466	577.7 430.9	3.462
8	2.08	1.014	2.120	8.447	.179	312.7	2,585	342.9	4.641
10	2.00	1.021	2.120 2 650 3.180	8.447 8.472 8.506	224	249.4 207.0	2,007	284.2	5.833 7.038
14	3 64	1.025	3 710	8.539	216	176.8	1,100	949.9	8 956
16	4 16	1.028	4 940	8 564	364	154.2	1 965	210.8	9.256 9.488
12 14 16 18	4.68	1.025 1 028 1.032	4 770	8.564 8.597	410	136.5	1 118	242.2 210.8 186.3	10.73
.20	2.08 2.60 3.12 3.64 4.16 4.68 5.20 7.80	1.035	3.710 4.240 4.770 5.300	8.622 8.781	.457	122.5	2,585 2,057 1,705 1,453 1,265 1,118 1,001 648.4	176.8	11.99
80	7.80	1.054	-7.950	8.781	.698	80.21	648.4	108.1	18.51
40	10 40	1.073	10.600	8.939	.947	59.09	472.3	78.71	25.41
30 40 50	13.00 15 60 18.20 20.80	1.093	13.250	9.105 9.280	1.206	46.41 37.94	472.3 366.6	61.10	32 73
60	15 60	1.114 1.136	15.900	9.280	1.475	37.94	296.2	49.36	40.51
70	18.20	1.136	18.550	9.464	1.755	31.89 27.38	245.9	40.98	48.80
80	20.80	1.158	$21.200 \\ 23.850$	9.647	2.045 2.348	27.38	208.1	34.69	57.65
90	23.40	1.182	23.850	9.847	2.348	23.84	178.8	29.80	67 11
100	26.00	1.205	26.500	10.039	2.660	21.04	155.3	25.88	77.26

Concentration of Sugar Solutions,\* (From "Heating and Concentrating Liquids by Steam, by John G. Hudson; The Engineer, June 13, 1890.)—In the early stages of the process, when the liquor is of low density, the evaporative duty will be high, say two to three (British) gallons per square foot of heating surface with 10 lbs. steam pressure, but will gradually fall to an almost nominal amount as the final stage is approached. As a generally safe basis for designing, Mr. Hudson takes an evaporation of one gallon per hour for each square foot of gross heating surface, with steam of the pressure of about 10 lbs.

As examples of the evaporative duty of a vacuum pan when performing the earlier stages of concentration, during which all the heating surface can be employed, he gives the following:

COL VACUUM PAN.—4% in copper coils, 528 square feet of surface; steam in coils, 15 lbs.; temperature in pan, 141° to 148°; density of feed, 25° Beaumé, and concentrated to 31° Beaumé.

First Trial.—Evaporation at the rate of 2000 gallons per hour = 3.8 gallons per square foot; transmission, 376 units per degree of difference of tem-

perature.

Second Trial.—Evaporation at the rate of 1503 gallons per hour = 2.8 gallons per square foot; transmission, 265 units per degree.

As regards the total time needed to work up a charge of massecuite from

As regards the total time needed to work up a charge transactine from liquor of a given density, the following figures, obtained by plotting the results from a large number of pans, form a guide to practical working. The pans were all of the coll type, some with and some without Jackets, the gross heating surface probably averaging, and not greatly differing from, 25 square foot per gallon capacity, and the steam pressure 101bs, per square inch. Both plantation and refining pans are included, making various grades of sugar:

	Density 10°	of Feed	(degs.	Beaum 25°	é). 30°
Evaporation required per gallon masse- cuite discharged	6.123		2.26	1.5	.97
Average working hours required per charge	12.	9.	61/4	5.	4.
per square foot of gross surface, as- suming .25 sq. ft. per gallon capacity	2.04	1.6	1.39	1.2	.97
Fastest working hours required per charge	8.5	5.5	3.8	2.75	2.0
hour per square foot	2.88	2.6	2.38	2.18	1.9

The quantity of heating steam needed is practically the same in vacuum as in open paus. The advantages proper to the vacuum system are primarily the reduced temperature of boiling, and incidentally the possibility

of using heating steam of low pressure.

In a solution of sugar in water, each pound of sugar adds to the volume of the water to the extent of .06i gallon at a low density to .0638 gallon at

high densities.

A Method of Evaporating by Exhaust Steam is described by Albert Steams in Trans. A. S. M. E., vol. viii. A pan 17' 6" × 11' × 1' 6", tited with east-iron condensing pipes of about 250 sq. ft. of surface, evaporated 120 gallons per hour from clear water, condensing only about one half of the steam supplied by a plain slide valve engine of 14" x 32" cylinder, making 65 revs. per min., cutting off about two thirds stroke, with steam at 75 lbs. boiler pressure.

It was found that keeping the pan-room warm and letting only sufficient

air in to carry the vapor up out of a ventilator adds to its efficiency, as the average temperature of the water in the pan was only about 165° F. Experiments were made with coils of pipe in a small pan, first with no agitator, then with one having straight blades, and lastly with troughed blades; the evaporative results being about the proportions of one, two, and three respectively.

In evaporating liquors whose boiling point is 220° F., or much above that of water, it is found that exhaust steam can do but little more than bring them up to saturation strength, but on weak liquors, syrups, glues, etc., it should be very useful.

<sup>\*</sup> For other sugar data see Bagasse as Fuel, under Fuel,

HEAT.

**Drying in Vacuum.**—An apparatus for drying grain and other substances in vacuum is described by Mr. Emil Passburg in Proc. Inst. Mech. Engrs., 1889. The three essential requirements for a successf l and economical process of drying are: 1. Cheap evaporation of the moisture; 2. Quick drying at a low temperature; 3. Large capacity of the apparatus

The removal of the moisture can be effected in either of two ways: either

by slow evaporation; or by quick evaporation—that is, by boiling.

Slow Evaporation.-The principal idea carried into practice in machines acting by slow evaporation is to bring the wet substance repeatedly into contact with the inner surfaces of the apparatus, which are heated by steam, while at the same time a current of hot air is also passing through the substances for carrying off the moisture. This method requires much heat, because the hot-air current has to move at a considerable speed in order to shorten the drying process as much as possible; consequently a great quantity of heated air passes through and escapes unused. As a carrier of moisture hot air cannot in practice be charged beyond half its full saturation; and it is in fact considered a satisfactory result if even this proportion be attained. A great amount of heat is here produced which is not used; while, with scarcely half the cost for fuel, a much quicker removal of the water is obtained by heating it to the boiling point.

Quick Evaporation by Boiling .- This does not take place until the water Quick Exaporation by Bourng.—Inis does not take place until the water is brought up to the bolling point and kept there, namely, 212° F., under atmospheric pressure. The vapor generated then escapes freely. Liquids are easily evaporated in this way, because by their motion consequent on boiling the heat is continuously conveyed from the heating surfaces through the liquid, but it is different with solid substances, and many more difficulties have to be overcome, because convection of the heat ceases entirely in the observance convertion of the heat ceases entirely in the content of th The substance remains motionless, and consequently a much greater quantity of heat is required than with liquids for obtaining the

same results.

Evaporation in Vacuum.—All the foregoing disadvantages are avoided if the boiling-point of water is lowered, that is, if the evaporation is carried out under vacuum.

This plan has been successfully applied in Mr. Passburg's vacuum drying apparatus, which is designed to evaporate large quantities of water con-

tained in solid substances.

The drying apparatus consists of a top horizontal cylinder, surmounted by a charging vessel at one end, and a bottom horizontal cylinder with a discharging vessel beneath it at the same end. Both cylinders are encased in steam-jackets heated by exhaust steam. In the top cylinder works a re-volving cast-iron screw with hollow blades, which is also heated by exhaust The bottom cylinder contains a revolving drum of tubes, consisting of one large central tube surrounded by 24 smaller ones, all fixed in tubeplates at both ends; this drum is heated by live steam direct from the boiler. The substance to be dried is fed into the charging vessel through two manholes, and is carried along the top cylinder by the screw creeper to the back noies, and is carried along the top cylinder by the screw creeper to the back end, where it drops through a valve into the bottom cylinder, in which it is lifted by blades attached to the drum and travels forwards in the reverse direction; from the front end of the bottom cylinder it falls into a discharging vessel through another valve, having by this time become dried. The vapor arising during the process is carried off by an air-pump, through a dome and air-valve on the top of the upper cylinder, and also through the threat is also as the top of the laws regimed. a throttle-valve on the top of the lower cylinder; both of these valves are supplied with strainers.

As soon as the discharging vessel is filled with dried material the valve connecting it with the bottom cylinder is shut, and the dried charge taken out without impairing the vacuum in the apparatus. When the charging vessel requires replenishing, the intermediate valve between the two cylinders is shut, and the charging vessel filled with a fresh supply of wet mate-rial; the vacuum still remains unimpaired in the bottom cylinder, and has to be restored only in the top cylinder after the charging vessel has been

closed again.

In this vacuum the boiling-point of the water contained in the wet material is brought down as low as 110° F. The difference between this temperature and that of the heating surfaces is amply sufficient for obtaining good results from the employment of exhaust steam for heating all the surfaces except the revolving drum of tubes. The water contained in the solid substance to be dried evaporates as soon as the latter is heated to about 110° F.

and as long as there is any moisture to be removed the solid substance is not heated above this temperature.

Wet grains from a brewery or distillery, containing from 75% to 78% of water, have by this drying process been converted in some localities from a worthless incumbrance into a valuable food-stuff. The water is removed

by evaporation only, no previous mechanical pressing being resorted to.

At Messrs. Guinness's brewery in Dublin two of these machines are employed. In each of these the top cylinder is 20' 4" long and 2' 8" diam., and the screw working inside it makes 7 revs. per min.; the bottom cylinder is the screw working inside it makes 7 revs. per min.; the bottom cylinder is 19 2" long and 5' 4" diam, and the drum of the tubes inside it makes 5 revs. per min. The drying surfaces of the two cylinders amount together to a total area of about 100 sq. ft., of which about 44% is heated by exhaust steam direct from the boiler. There is only one air-pump, which is made large enough for three machines: it is horizontal, and has only one air-ylinder, which is double-acting, 17% in. diam, and 17% in. stroke; and it is driven at the control of the about 45 revs. per min. As the result of about eight months' experience, the two machines have been drying the wet grains from about 500 cwt. of malt per day of 24 hours.

Roughly speaking, 3 cwt. of malt gave 4 cwt. of wet grains, and the latter yield lewt, of dried grains; 500 cwt, of malt will therefore yield about 670 cwt. of wet grains, or 335 cwt, per machine. The quantity of water to be evaporated from the wet grains is from 75% to 75% of their total weight, or

say about 512 cwt. altogether, being 256 cwt, per machine.

#### RADIATION OF HEAT.

Radiation of heat takes place between bodies at all distances apart, and follows the laws for the radiation of light.

The heat rays proceed in straight lines, and the intensity of the rays radiated from any one source varies inversely as the square of their distance

from the source.

This statement has been erroneously interpreted by some writers, who have assumed from it that a boiler placed two feet above a fire would receive by radiation only one fourth as much heat as if it were only one fourth as much heat as if it were only one fourth as much beat as if it were only one fourth as much beat as if it were only one fourth as much beat as if it were only one fourth as much beat as if it were only one for the fourth of the in radial lines from a single point. When the radiation is from a multitude of points, as from the surface of a fire or flame, the rays from the several points cross each other and cause the intensity at moderate distances to be much greater than the law of inverse squares would indicate. Moreover, in the case of boiler furnaces the side walls reflect those rays that are received at an angle-following the law of optics, that the angle of incidence is equal to the angle of reflection, -with the result that the intensity of heat two feet above the fire is practically the same as at one foot above, instead of only one-fourth as much.

The rate at which a hotter body radiates heat, and a colder body absorbs heat, depends upon the state of the surfaces of the bodies as well as on their temperatures. The rate of radiation and of absorption are increased by darkness and roughness of the surfaces of the bodies, and diminished by smoothness and polish. For this reason the covering of steam pipes and boilers should be smooth and of a light color: uncovered pipes and steam-

cylinder covers should be polished.

The quantity of heat radiated by a body is also a measure of its heatabsorbing power, under the same circumstances. When a polished body is struck by a ray of heat, it absorbs part of the heat and reflects the rest. The reflecting power of a body is therefore the complement of its absorbing

power, which latter is the same as its radiating power.

power, which auter is the same as its ranning power.

The relative radiating and reflecting power of different bodies has been determined by experiment, as shown in the table below, but as far as quantities of heat are concerned, says Prof. Trowbridge (Johnson's Cyclopædia, art. Heat), it is doubtful whether anything further than the said relative determinations can, in the present state of our knowledge, be depended upon, the actual or absolute quantities for different temperatures being still upper the control of the properties of the control of the present of the present of the relative radiation. uncertain. The authorities do not even agree on the relative radiating powers. Thus, Leslie gives for tin plate, gold, silver, and copper the figure 12, which differs considerably from the figures in the table below, given by Clark, stated to be on the authority of Leslie, De La Provostaye and Desains, and Melloni.

#### Relative Radiating and Reflecting Power of Different Substances.

	Radiating or Absorbing Power.	Reflecting Power.		Radiating or Absorbing Power.	Reflecting Power.
Lampblack Water Carbonate of lead. Writing-paper Livory, jet, marble Ordinary glass. Gum lac. Silver-leaf on glass. Cast iron, bright polished. Wrought iron, polished.	90 85 72 27 25 23	0 0 0 2 7 to 2 10 15 28 73 75 77	Zinc, polished. Steel, polished. Platimum, polished. "in sheet." Tin Brass, cast, dead polished. Brass, bright polished. "Copper, varnished." "hammered." Gold, plated" "on polished steel.	19 17 24 17 15 11 7 14 7	81 83 76 83 85 89 93 86 93 95
Exposiments of Du			Silver, polished bright	3	97

Experiments of Dr. A. M. Mayer give the following: The relative radiations from a cube of cast iron, having faces rough, as from the foundry, planed, "drawfiled," and polished, and from the same surfaces oiled, are as below (Prof. Thurston, in Trans. A. S. M. E., vol. xvi.):

Surface.	Oiled.	Dry.
Rough Planed Drawfiled Polished	60	100 32 20 18

It here appears that the oiling of smoothly polished castings, as of cylinder-heads of steam-engines, more than doubles the loss of heat by radiation, while it does not seriously affect rough castings.

#### CONDUCTION AND CONVECTION OF HEAT.

Conduction is the transfer of heat between two bodies or parts of a body which touch each other. Internal conduction takes place between the parts of one continuous body, and external conduction through the surface of confort of a pair of distinct bodies.

The rate at which conduction, whether internal or external, goes on, being proportional to the area of the section or surface through which it takes place, may be expressed in thermal units per square foot of area per hour

Internal Conduction varies with the heat conductivity, which depends upon the nature of the substance, and is directly proportional to the difference between the temperatures of the two faces of a layer, and inversely as its thickness. The reciprocal of the conductivity is called the internal thermal resistance of the substance. If represents this resistance, x the thickness of the layer in inches, T and T the temperatures on the two faces, and q the quantity in thermal units transmitted per hour per square

foot of area,  $q = \frac{T' - T}{r}$ . (Rankine.)

Péclet gives the following v	alues of	r:	
Gold, platinum, silver Copper Iron Zinc	0.0018	Lead	0.0716

# Relative Heat-conducting Power of Metals.

(\* Calvert & Johnson ; † Weidemann & Franz )

Silver — 1000

Metals,		tW. & F.			†W. & F.
Silver	. 1000	1000	Cadmium	577	
Gold	. 981	532	Wrought iron	436	119
Gold, with 1% c	£		Tin	422	145
silver	. 840		Steel	397	116
Copper, rolled	. 845	736	Platinum		84
Copper, cast			Sodium		
Mercury	. 677		Cast iron	359	
Mercury, with 1.25	%		Lead	287	85
of tin	. 412		Antimony:		
Aluminum	. 665		cast horizonta		
Zinc, rolled	. 641		cast vertically	192	
Zine:			Bismuth	61	18
cast vertically	628				
east horizontally.	. 608				

INFLUENCE OF A NON-METALLIC SUBSTANCE IN COMBINATION ON THE CONDUCTING POWER OF A METAL.

Influence of carbon on iron : Wrought iron	436	Influence of arsenic on copper: Cast copper
Steel	397	Copper with 1% of arsenic 570  "with .5% of arsenic 669  "with .25% of arsenic 771
	1	with ,20% of arsenic, 111

Steam-pipe Coverings.

(Experiments by Prof. Ordway, Trans. A. S. M. E., v, 73; also Circular No. 27 of Boston Mfrs. Mutual Fire Ins. Co., 1890.)

It will be observed that several of the incombustible materials are nearly as efficient as wool, cotton, and feathers, with which they may be compared in the following table. The materials which may be considered wholly free from the danger of being carbonized or ignited by slow contact with pipes or boilers are printed in Bonna type. Those which are more or less liable to be carbonized are printed in italics.

TABLE I.

Substance 1 inch thick. Heat applied, 810° F.	Pounds of Water heated 10° F., per hour, through 1 square foot.	Solid Matter in 1 square foot 1 inch thick, parts in 1000.	Air Included, parts in 1000.
1. Loose wool	8.1	56	944
2. Live-geese feathers	9.6	50	950
3. Carded cotton wool	10.4	20	980
4. Hair felt	10.3	185	815
5. Loose lampblack	9.8	56	944
6. Compressed lampblack	10.6	244	756
7. Cork charcoal	11.9	53	947
8. White-pine charcoal	13.9	119	881
9. Anthracite-coal powder	35.7	506	494
10. Loose calcined magnesia	12.4	23	977
11. Compressed calcined magnesia	42.6	285	715
12. Light carbonate of magnesia	13.7	60	940
13. Compressed carbonate of magnesia	15.4	150	850
14. Loose fossil-meal	14.5	60	940
15. Crowded fossil-meal	15.7	112	. 888
16. Ground chalk (Paris white)	20.6	253	747
17. Dry plaster of Paris	30.9	368	632
18. Fine asbestos	49.0	81	919
19. Air alone	48.0	0	1000
20. Sand	62.1	527	471

### TABLE II.

Covering.	Pounds of Water heated 10° F., per hour, by 1 square foot.
21. Best slag-wool	13.
22. Paper	14.
23. Blotting-paper wound tight	21.
24. Asbestos paper wound tight	21.7
25. Cork strips bound on	14.6
26. Straw rope wound spirally	18.
27. Loose rice chaff	18.7
28. Paste of fossil-meal with hair	16.7
29. Paste of fossil-meal with asbestos	22.
30. Loose bituminous-coal ashes	21.
31. Loose anthracite-coal ashes	27.
32. Paste of clay and vegetable fibre	30.9

Professor Ordway's report says: Careful experiments have been made with various non-conductors, each used in a mass one inch thick, placed on a flat surface of iron kept heated by steam to 310° Fahr. Table I gives the amount of heat transmitted per hour through each kind of non-conductor one inch thick, reckoned in pounds of water heated 10° Fahr., the unit of area being one square foot of covering.

The substances given in Table II were actually tried as coverings for two-inch steam-pipe, but for convenience of comparison the results have

been reduced by calculation to the same terms as in Table I.

Later experiments have given results for still air which differ little from those of Nos. 3, 4, and 6. In fact the bulk of matter in the best non-conducthose of Nos. 3, 4 and 6. There are only of matter in the east non-continuous to risk relatively too small to have any specific effect, except to entrap the air and keep it stagnant. These substances keep the air still by virtue of the roughness of their fibres or particles. The asbestos, No. 18, had smooth fibres, which could not prevent the air from moving about.

Later trials with an asbestos of exceedingly fine fibre have made a somewhat better showing, but asbestos is really one of the poorest non-conductors. By reason of its fibrous character it may be used advantageously to hold together other incombustible substances, but the less the better. We have made trials of two samples of a "magnesia covering," consisting we have made trials of two samples of a "magnesia covering," consisting of carbonate of magnesia with a small percentage of good asbestos fibre. One transmitted heat which, reduced to the terms of Table I, would amount to 15 lbs: the denser one gave 20 lbs. The former contained 250/1000 of solid matter; the latter 396/1000. Any suitable substance which is used to prevent the escape of steam heat should not be less than one inch thick.

Any covering should be keet perfectly dry, for not only is water a good carrier of heat, but it has been found that still water conducts heat about

eight times as rapidly as still air.

# Heat-conducting Power of Covering Materials.

(J. J. Coleman, Eng'g, Sept. 5, 1884, p. 237.)

Experiments were made by filling a 10 in. cube with ice, surrounding it with the different materials to be tested, and noting the quantity of ice melted per hour with each insulator. lative results were as follows

The remerie results were no zer			
Silicate cotton (mineral wool)	100 1	Charcoal	140
		Sawdust	
Cotton wool	122	Gas works breeze	530
		Wood and air-space	280
Infusor at earth	136		

The Rate of External Conduction through the bounding surface between a solid body and a fluid is approximately proportional to the difference of temperature, when that is small; but when that difference is considerable the rate of conduction increases faster than the simple ratio of that difference, (Rankine,)

If r, as before, is the coefficient of internal thermal resistance, e and e' the coefficient of external resistance of the two surfaces, x the thickness of the coefficient of earthal resistance of the two fluids in contact with the two surfaces, the total thermal resistance is  $q = \frac{T' - T}{e + e' + rx}$ . According to

Peclet,  $e + e' = \frac{1}{A[1 + B(T' - T)]}$ , in which the constants A and B have

the following values: 

The results of experiments on the evaporative power of boilers agree very well with the following approximate formula for the thermal resistance of boiler plates and tubes :

$$e+e^{\prime}=\frac{a}{(T^{\prime}-T)},$$

which gives for the rate of conduction, per square foot of surface per Lour,  $q=\frac{(T'-T)^2}{a}.$ 

$$q = \frac{(T - T)^2}{a}$$

This formula is proposed by Rankine as a rough approximation, near enough to the truth for its purpose. The value of a lies between 160 and 200. **Convection**, or carrying of heat, means the transfer and diffusion of the heat in a fluid mass by means of the motion of the particles of that

The conduction, properly so called, of heat through a stagnant mass of fluid is very slow in liquids, and almost, if not wholly, inappreciable in gases. It is only by the continual circulation and mixture of the particles of the fluid that uniformity of temperature can be maintained in the fluid mass, or heat transferred between the fluid mass and a solid body.

The free circulation of each of the fluids which touch the side of a solid plate is a necessary condition of the correctness of Rankine's formulæ for the conduction of heat through that plate; and in these formulæ it is implied that the circulation of each of the fluids by currents and eddies is such as to prevent any considerable difference of temperature between the fluid particles in contact with one side of the solid plate and those at considerable

distances from it.

When heat is to be transferred by convection from one fluid to another, through an intervening layer of metal, the motions of the two fluid masses should, if possible, be in opposite directions, in order that the hottest particles of each fluid may be in communication with the hottest particles of the other, and that the minimum difference of temperature between the adjacent particles of the two fluids may be the greatest possible.

Thus, in the surface condensation of steam, by passing it through metal tubes immersed in a current of cold water or air, the cooling fluid should be

make to move in the opposite direction to the condensing steam.

Transmission of Heat, through Solid Plates, from Water to Water. (Clark, S.E.)—M Felet found, from experiments made with plates of wrought iron, cast iron, copper, lead, zinc, and tin, that when the fluid in contact with the surface of the plate was not circulated by artificial means, the rate of conduction was the same for different metals and for plates of the same metal of different thicknesses. But when the water was thoroughly circulated over the surfaces, and when these were perfectly clean, the quantity of transmitted heat was inversely proportional to the thickness, and directly as the difference in temperature of the two faces of the plate. When the metal surface became dull, the rate of transmission of heat through all the metals was very nearly the same.

It follows, says Clark, that the absorption of heat through metal plates is more active whilst evaporation is in progress-when the circulation of the water is more active-than while the water is being heated up to the boiling

point.

Transmission from Steam to Water,—M. Péclet's principle is supported by the results of experiments made in 1867 by Mr. Isherwood on the conductivity of different metals. Cylimdrical pots, 10 inches in diameter, 21½ inches deep inside, and ½ inch, ½ inch, and ¾ inch thick, turned and bored, were formed of pure copper, brass (60 copper and 40 zinc), rolled wrought iron, and remelted cast iron. They were immersed in a steam bath, which was varied from 220° to 320° F. Water at 212° was supplied to the pots, which were kept filled. It was ascertained that the rate of evaporation was in the direct ratio of the difference of the temperatures inside and outside of the pots; that is, that the rate of evaporation per degree of difference of temperatures was the same for all temperatures; and that the rate of evaporation was exactly the same for different thicknesses of the metal. The respective rates of conductivity of the several metals were as follows, expressed in weight of water evaporated from and at 212° F. per square foot of the interior surface of the pots per degree of difference of temperature per hour, together with the equivalent quantities of heat-units:

1	Vater at 212°.	Heat-units.	Ratio.
Copper	665 lb.	642.5	1.00
Brass	577 "	556.8	.87
Wrought iron	387 "	373.6	.58
Cast iron		315.7	.49

Whitham, "Steam Engine Design," p. 283, also Trans. A. S. M. E. ix., 425, in using these data in deriving a formula for surface condensers calls these figures those of perfect conductivity, and multiplies them by a coefficient C, which he takes at 0.323, to obtain the efficiency of condenser surface in ordinary use, i.e., coated with saline and greax deposits.

ordinary use, i.e., coated with saline and greasy deposits.

Transmission of Heat from Steam to Water through
Coils of Iron Pipe.—H. G. C. Kopp and F. J. Meystre (Stevens Indicator, Jan., 1894), give an account of some experiments on transmission of heat through coils of pipe.

They collate the results of earlier experiments as follows, for comparison:

Experimenter.	er of Surface.	degree differ- ence of temper- ature per hour.		densed per square foot per degree difference of temperature per hour.		ed per foot per differ- temper-	Remarks.
Experi	Charact	Heating, pounds.	Evapo- rating, pounds.	Heating, B. T. U.	Evapo- rating B. T. U.	*	
Havrez Perkins.	Copper coils 2 Copper coils Copper coil Iron coil " " Iron tube " " Cast-iron boil- er	.292 .268  .235 .196 .206	.981 1.20 1.26 .24 .22	315 -280  230 207 210 82	974 1120 1200 215 208.2	{Steam pressure = 100. Steam pressure = 10.	

From the above it would appear that the efficiency of iron surfaces is less than that of copper coils, plate surfaces being far inferior.

In all experiments made up to the present time, it appears that the temperature of the condensing water was allowed to rise, a mean between the initial and final temperatures being accepted as the effective temperature. But as water becomes warmer it circulates more rapidly, thereby causing the water surrounding the coil to become agitated and replaced by cooler water, which allows more heat to be transmitted.

Again, in accepting the mean temperature as that of the condensing medium, the assumption is made that the rate of condensation is in direct proportion to the temperature of the condensing water.

In order to correct and avoid any error arising from these assumptions and approximations, experiments were undertaken, in which all the coudi-

tions were constant during each test.

The pressure was maintained uniform throughout the coil, and provision was made for the free outflow of the condensed steam, in order to obtain at all times the full efficiency of the condensing surface. The condensing water was continually stirred to secure uniformity of temperature, which was regulated by means of a steam-pipe and a cold-water pipe entering the tank in which the coil was placed.

The following is a condensed statement of the results

HEAT TRANSMITTED PER SQUARE FOOT OF COOLING SURFACE, PER DEGREE OF DIFFERENCE OF TEMPERATURE. (British Thermal Units.)

Temperature of Condens- ing Water.	1-in. Iron Pipe; Steam inside, 60 lbs. Gauge Pressure.	1½ in. Pipe; Steam inside, 10 lbs. Pressure.	1½ in. Pipe; Steam inside, 10 lbs. Pressure.	1½ in. Pipe; Steam inside, 60 lbs. Pressure.
80	265	128	200	
100	269	130	230	239
120	272	137	260	247
140	277	145	267	276
160	281	158	271	306
180	299	174	270	349
200	313			419

The results indicate that the heat transmitted per degree of difference of temperature in general increases as the temperature of the condensing water is increased.

The amount transmitted is much larger with the steam on the outside of

the coil than with the steam inside the coil. This may be explained in part by the fact that the condensing water when inside the coil flows over the surface of conduction very rapidly, and is more efficient for cooling than when contained in a tank outside of the coil.

This result is in accordance with that found by Mr. Thomas Craddock, which indicated that the rate of cooling by transmission of heat through metallic surfaces was almost wholly dependent on the rate of circulation of

Transmission of Heat in Condenser Tubes, (Eng'g, Dec. 10, 1875, p. 449.).—In 1874 B. C. Nichol, made experiments for determining the rate at which heat was transmitted through a condenser tube. The results went to show that the amount of heat transmitted through the walls of the tube per estimated degree of mean difference of temperature increased considerably with this difference. For example:

Estimated mean difference of Vertical Tube. Horizontal Tube temperature between inside and 128 152.9 outside of tube, degrees Fahr. . 151.9 111.6 146.2 150.4 Heat-units transmitted per hour per square foot of surface per degree of mean diff. of temp.... 422 531 561 610

These results seem to throw doubt upon Mr. Isherwood's statement that the rate of evaporation per degree of difference of temperature is the same

for all temperatures.

Mr. Thomas Craddock found that water was enormously more efficient than air for the abstraction of heat through metallic surfaces in the process of cooling. He proved that the rate of cooling by transmission of heat through metallic surfaces depends upon the rate of circulation of the cooling medium over the surface to be cooled. A tube filled with hot water, moved by rapid rotation at the rate of 59 ft. per second, through air, lost as much heat in one minute as it did in still air in 12 minutes. In water, at a velocity of 3 ft. per second, as much heat was abstracted in half a minute as was abstracted in one minute when it was at rest in the water. Mr. Craddock concluded, further, that the circulation of the cooling fluid became of

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greater importance as the difference of temperature on the two sides of the plate became less. (Clark, R. T. D., p. 461.)

Heat Transmission through Cast-iron Plates Pickled in Nitric Acid.—Experiments by R. C. Carpenter (Trans. A. S. M. E., xii 179) show a marked change in the conducting power of the plates (from steam to water), due to prolonged treatment with dilute nitric acid.

The action of the nitric acid, by dissolving the free iron and not attacking the carbon, forms a protecting surface to the iron, which is largely composed of carbon. The following is a summary of results:

Character of Plates, each plate 8.4 in., by 5.4 in., exposed surface 27 sq. ft.	Increase in Tempera- ture of 3.125 lbs. of Water each Minute.	Proportionate Thermal Units Transmitted for each Degree of Difference of Temperature per Square Foot per Hour.	Rela- tive Trans- mission of Heat.
Cast iron—untreated skin on, but clean, free from rust. Cast iron—nitric acid, 1/5 sol., 9 days.  "" 1/5 sol., 18 days. "" 1/5 sol., 40 days. "" 5/5 sol., 40 days. Plate of pine wood, same dimensions as the plate of cast iron.	13.90 11.5 9.7 9.6 9.93 10.6	113.2 97.7 80.08 77.8 87.0 77.4	100.0 86.3 70.7 68.7 76.8 68.5

The effect of covering cast-iron surfaces with varnish has been investigated by P. M. Chamberlain. He subjected the plate to the action of strong acid for a few hours, and then applied a non-conducting varnish. One surface only was treated. Some of his results are as follows:

170. As finished-greasy.

washed with benzine and dried.

169. Oiled with lubricating oil.

162. After exposure to nitric acid sixteen hours, then oiled (linseed oil.) 166 After exposure to hydrochloric acid twelve hours, then oiled

t. per hour, 1 ach degree,  $\tau - \tau'$ . (linseed oil.)

113. After exposure to sulphuric acid 1, water 2, for 48 hours, then oiled, varnished, and allowed to dry for 24 hours.

Transmission of Heat through Solid Plates from Air or other Dry Gases to Water. (From Clark on the Steam Engine.)

—The law of the transmission of heat from hot air or other gases to water, through metallic plates, has not been exactly determined by experiment. The general results of experiments on the evaporative action of different portions of the heating surface of a steam-boiler point to the general law that the quantity of heat transmitted per degree difference of temperature is practically uniform for various differences of temperature.

The communication of heat from the gas to the plate surface is much

accelerated by mechanical impingement of the gaseous products upon the surface.

Clark says that when the surfaces are perfectly clean, the rate of transmission of heat through plates of metal from air or gas to water is greater for copper, next for brass, and next for wrought iron. But when the surfaces are dimmed or coated, the rate is the same for the different metals. With respect to the influence of the conductivity of metals and of the thickness of the plate on the transmission of heat from burnt gases to

thickness of the plate on the transmission of heat from outling gases to water, Mr. Napier made experiments with small boilers of iron and copper placed over a gas-flame. The vessels were 5 inches in diameter and 3½ inches deep. From three vessels, one of iron, one of copper, and one of iron sides and copper bottom, each of them 1/30 inch in thickness, equal quantities of water were evaporated to dryness, in the times as follows:

Water.	Iron Vessel.	Copper Vessel.	Iron and Copper Vessel.
4 ounces	19 minutes	18.5 minutes 30.75	
51/2 "	50 "	44 "	
4 "	35.7 "		36.83 minutes.

Two other vessels of iron sides 1/30 inch thick, one having a  $\mathcal{Y}_2$ -inch copper bottom and the other a  $\mathcal{Y}_2$ -inch lead bottom, were tested against the iron and copper vessel, 1/30 inch thick. Equal quantities of water were evaporated in 54, 55, and 53½ minutes respectively. Taken generally, the results of these experiments show that there are practically but slight differences between iron, copper, and lead in evaporative activity, and that the activity is not affected by the thickness of the bottom.

Mr. W. B. Johnson formed a like conclusion from the results of his observations of two boilers of 160 horse-power each, made exactly alike, except that one had iron flue-tubes and the other copper flue-tubes. No difference could be detected between the performances of these hollers.

Terence could be detected between the performances of these bollers. Divergencies between the results of different experimenters are attributable probably to the difference of conditions under which the heat was transmitted, as between water or steam and water, and between gaseous matter and water. On one point the divergence is extreme: the rate of transmission of heat per degree of difference of temperature. Whilst from 400 to 600 units of heat are transmitted from water through iron plates, per degree of difference per square foot per hour, the quantity of neat transmitted between water and air, or other dry gas, is only about from 2 to 5 units, according as the surrounding air is at rest or in movement. In a locomotive boiler, where radiant heat was brought into play, 17 units of heat were transmitted through the plates of the fire-box per degree of difference of temperature per square foot per hour.

Transmission of Heat through Plates and Tubes from Stam or Hot Water to Air,—The transfer of heat from steam or water through a plate or tube into the surrounding air is a complex operation, in which the internal and external conductivity of the metal, the radiating power of the surface, and the convection of heat in the surrounding air are all concerned. Since the quantity of heat radiated from a surface varies with the condition of the surface and with the surroundings, according to laws not yet determined, and since the heat carried away by convection varies with the rate of the flow of the air over the surface, it is evident that no ceneral law can be laid down for the total quantity of heat entitled.

no general law can be laid down for the total quantity of heat emitted.

The following is condensed from an article on Loss of Heat from Steam-

pipes, in The Locomotive, Sept. and Oct., 1892.

A hot steam pipe is radiating beat constantly off into space, but at the same time it is cooling also by convection. Experimental data on which to base calculations of the heat radiated and otherwise lost by steam-pipes are

neither numerous nor satisfactory.

In Box's Practical Treatise on Heat a number of results are given for the amount of heat radiated by different substances when the temperature of the air is 19 fahr, lower than the temperature of the radiating body. A portion of this table is given below. It is said to be based on Péclet's experiments.

HEAT UNITS RADIATED PER HOUR, PER SQUARE FOOT OF SURFACE, FOR

1 PAHRENHEIT	EXCE	SS IN LEMPERATURE.	
Copper, polished	.0327	Sheet-iron, ordinary	.5662
Tin, polished	.0440	Glass	,5948
Zinc and brass, polished	.0491	Cast iron, new	.6480
Tinned iron, polished	.0858	Common steam-pipe, inferred	.6400
Sheet-iron, polished	.0920	Cast and sheet iron, rusted	,6868
Sheet lead	1290	Wood building stone and brick	7258

When the temperature of the air is about 50° or 60° Fahr., and the radiating body is not more than about 30° hotter than the air, we may calculate the radiation of a given surface by assuming the amount of heat given off by it in a given time to be proportional to the difference in temperature between the radiating body and the air. This is "Newton's law of cooling." But when the difference in temperature is great, Newton's law does not hold good; the radiation is no longer proportional to the difference in temperature, but must be calculated by a complex formula established experiment, ally by Dulong and Petit. Box has computed a table from this formula, which greatly facilitates its application, and which is given below;

FACTORS FOR REDUCTION TO DULONG'S LAW OF RADIATION.

Differences in Temperature between	Т	emp	eratı	ire o	f the	Air	on tl	ne Fa	hrei	aheit	Sca	le.
Radiating Body and the Air.	330	50°	59°	68°	86°	104°	122°	140°	158°	176°	194°	212°
Deg. Fahr.	1.00	1.07	1.12	1.16	1.25	1.36	1.47	1.58	1.70	1.85	1.99	2.15
36 54	1.07	1.16	1.20	$\frac{1.21}{1.25}$	1.35	1.45	1.58	1.70	1.83	1.99	2.14	2.31
72 90	1.16	1.25	1.31	1.30	1.46	1.58	1.71	1.84	1.98	2.15	2.33	2.51
108 126	1.26	1.36	1.42	$\frac{1.42}{1.48}$	1.50	1.72	1.86	2.00	2.16	2.34	2.52	2.72
. 144 162	1.37	1.48	1.54	1.54	1.73	1.86	2.02	2.17	2.34	2.54	2.74	2.96
180 198	11.50	1.62	1.69	$\frac{1.68}{1.75}$	11.89	2.04	2.21	12.38	12.56	2.78	3.00	3.24
216 234	1.64	1.77	1.84	$\frac{1.83}{1.90}$	2.06	2.28	2.43	2.52	2.80	3.03	3.28	3.46
252 270	1.79	1.93	2.01	$\frac{2.00}{2.09}$	2.22	2.44	2.64	2.84	3.06	3.32	3.58	3.87
288 306	1.98	2.13	2.22	$\frac{2.20}{2.31}$	2.49	2.69	2.90	3.12	3.37	3.66	3.95	4.26
324 342	2.17	2.34	2.44	$\frac{2.42}{2.54}$	2.73	2.95	3.19	3.44	3.70	4.02	4.34	4.68
360 378	2.39	2.57	2.68	$\frac{2.66}{2.79}$	3.00	3.24	3.51	3.78	4.08	4.42	4.77	5.15
396 414	2.63	2.84	2.95	2.93	3.31	3.51	3.87	4.12	4.48	4.87	5.26	5.67
432	2.76	2.98	3.10	3.23	3.47	3.76	4.10	4.32	1.61	5.12	5.33	6.04

The loss of heat by convection appears to be independent of the nature of the surface, that is, it is the same for iron, stone, wood, and other materials. It is different for bodies of different shape, however, and it varies with the position of the body. Thus a vertical steam-pipe will not lose so much heat by convection as a horizontal one will; for the air heated at the lower part of the vertical pipe will rise along the surface of the pipe, protecting it to some extent from the chilling action of the surrounding cooler air. For a similar reason the shape of a body has an important influence on the result hose bodies losing most heat whose forms are such as to allow the cool air free access to every part of their surface. The following table from Box gives the number of heat units that horizontal cylinders or pipes lose by convection per square foot of surface per hour, for one degree difference in temperature between the pipe and the air.

HEAT UNITS LOST BY ('ONVECTION FROM HORIZONTAL PIPES, PER SQUARE FOOT OF SURFACE PER HOUR, FOR A TEMPERATURE DIFFERENCE OF 19 FAHR.

External Diameter of Pipe in inches.	Heat Units Lost.	External Diameter of Pipe in inches.	Heat Units Lost.	External Diameter of Pipe in inches.	Heat Units Lost.
2 3 4 5 6	0.728 0.626 0.574 0.544 0.523	7 8 9 10 12	0.509 0.498 0.489 0.482 0.472	18 24 36 48	0.455 0.447 0.438 0.434

The loss of heat by convection is nearly proportional to the difference in temperature between the hot body and the air; but the experiments of Dulong and Péclet show that this is not exactly true, and we may here also resort to a table of factors for correcting the results obtained by simple proportion.

FACTORS FOR REDUCTION TO DULONG'S LAW OF CONVECTION.

Difference in Temp. between Hot Body and Air.	Factor.	Difference in Temp. between Hot Body and Air.	Factor.	Difference in Temp. between Hot Body and Air.	Factor.
18° F. 36° 54° 72° 90° 108° 126° 144° 162°	0.94 1.11 1.22 1.30 1.37 1.43 1.49 1.53 1.58	180° F. 198° 216° 234° 252° 270° 288° 306° 324°	1.62 1.65 1.68 1.72 1.74 1.77 1.80 1.83 1.85	342° F. 360° 378° 396° 414° 432° 450° 468°	1.87 1.90 1.92 1.94 1.96 1.98 2.00 2.02

EXAMPLE IN THE USE OF THE TABLES.—Required the total loss of heat by both radiation and convection, per foot of length of a steam-pipe 2 11/32 nexternal diameter, steam pressure 60 lbs., temperature of the air in the room 68° Fahr. Temperature corresponding to 60 lbs. equals 307°; temperature difference

 $= 307 - 68 = 239^{\circ}$ 

Area of one foot length of steam-pipe =  $211/32 \times 3.1416 \div 12 = 0.614$  sq.

Heat radiated per hour per square foot per degree of difference, from table, .064.

Radiation loss per hour by Newton's law =  $239^{\circ} \times .614$  ft.  $\times .64 = 93.9$  heat units. Same reduced to conform with Dulong's law of radiation: factor

near units. Same reduced to conform with Dulong's law of radiation: factor from table for temperature of ifference of 2399 and temperature of air 68° = 1.93. 98.9  $\times$  1.93 = 181.2 heat units, total loss by radiation. Convection loss per square foot per hour from a 2 11/32-inch pipe: by interpolation from table, 2'' = .728, 3'' = .626,  $2 \cdot 11/32' = .693$ . Area,  $6.14 \times .693 + 2.99 = 101.7$  heat units. Same reduced to conform with Dulong's law of convection:  $101.7 \times 1.73$  (from table) = 175.9 heat units by hour. Total loss by radiation and convection = 181.2 + 175.9 = 357.1 heat units per hour. Loss per degree of difference of temperature per square foot of surface per hour =  $357.1 \div 239 = 1.494$  heat units.

It is not claimed, says The Locomotive, that the results obtained by this

method of calculation are strictly accurate. The experimental data are not method of calculation are strictly accurate. The experimental data are not sufficient to allow us to compute the heat-loss from steam-pipes with any great degree of refinement; yet it is believed that the results obtained as indicated above will be sufficiently hear the truth for most purposes. An experiment by Prof. Ordway, in a pipe 2 11/32 in, diam. under the above conditions (Trans. A. S. M. E., v. 73), showed a condensation of steam of 181 grammes per hour, which is equivalent to a loss of heat of 385.7 heat units per hour, or within half of one per cent of that given by the above calculations. tion. According to different authorities, the quantity of heat given off by steam

and hot-water radiators in ordinary practice of heating of buildings by direct radiation varies from 1.8 to about 3 heat units per hour per square

foot per degree of difference of temperature.

The lowest figure is calculated from the following statement by Robert Briggs in his paper on "American Practice in Warming Buildings by Steam "Proc. Inst. C. E., 1882, vol. 1xxi): "Each 100 sq. ft. of radiating surface will give off 3 Fahr, heat units per minute for each degree F. of difference in temperature between the radiating surface and the air in which it is exposed."

The figure 2 1/2 heat units is given by the Nason Manufacturing Company

in their catalogue, and 2 to 2 1/4 are given by many recent writers.

For the ordinary temperature difference in low-pressure steam-heating, say 212° - 70° = 142° F., 1 lb. steam condensed from 212° to water at the same temperature gives up 965.7 heat units. A loss of 2 heat units per sq. ft. per hour per degree of difference, under these conditions, is equivalent to  $2 \times 142 + 965 = 0.3$  bs, of steam condensed per hour per sq. ft. of heating surface. (See also Heating and Ventilation.)

Transmission of Heat through Walls, etc., of Buildings (Nason Manufacturing Co.). (See also Heating and Ventilation.)—Heat has the remarkable property of passing through moderate thicknesses of air and gases without appreciable loss, so that air is not warmed by radiant heat, but by contact with surfaces that have absorbed the radiation.

POWERS OF DIFFERENT SUBSTANCES FOR TRANSMITTING HEAT

TOWERS OF DIFFERENT	CODSIA	NCES FOR TRANSMITTING III.	a
Window-glass	1000	Bricks, rough	200 to 250
Oak or walnut	66	Bricks, whitewashed	200
White pine	80	Granite or slate	250
Pitch-pine	100	Sheet iron 1	030 to 1110
Lath or plaster 75	to 100		

A square foot of glass will cool 1.279 cubic feet of air from the temperature inside to that outside per minute, and outside wall surface is generally actimated at one fifth of the rate of glass in accling effect.

estimated at one fifth of the rate of glass in cooling effect.

Box, in his "Practical Treatise on Heat," gives a table of the conducting powers of materials prepared from the experiments of Péclet. It gives the quantity of heat in units transmitted per square foot per hour by a plate 1 inch in thickness, the two surfaces differing in temperature 1 degree.

Fine-grained gray marble	 28,00
Coarse-grained white marble	 22.4
Stone, calcareous, fine	 16.7
Stone, calcareous, ordinary	 13.68
Baked clay, brickwork	 4.83
Brick-dust, sifted	 1.33

Hood, in his "Warming and Ventilating of Buildings," p. 249, gives the results of M. Depretz, which, placing the conducting power of marble at 1.00, give .483 as the value for firebrick.

#### THERMODYNAMICS.

Thermodynamics, the science of heat considered as a form of energy, is useful in advanced studies of the theory of steam, gas, and air engines, refrigerating machines, compressed air, etc. The method of treatment adopted by the standard writers is severely mathematical, involving constant application of the calculus. The student will find the subject thoroughy treated in the recent works by Rontgen (Dubois's translation), Wood, and Peabody.

Wood, and Peabody.

First Law of Thermodynamics.—Heat and mechanical energy are mutually convertible in the ratio of about 778 foot-pounds for the British thermal unit. (Wood.) Heat is the living force or vis viva due to certain molecular motions of the molecules of bodies, and this living force may be stated or measured in units of heat or in foot-pounds, a unit of heat in British measures being equivalent to 772 [78] foot-pounds. (Trowbridge, Trans. A. S. M. E., vii. 727.)

Second Law of Thermodynamics.—The second law has by dif-

Second Law of Thermodynamics.—The second law has by different writers been stated in a variety of ways, and apparently with ideas so diverse as not to cover a common principle. (Wood, Therm., p. 389.)

It is impossible for a self-acting machine, unaided by any external agency, to convert heat from one body to another at a higher temperature. (Clausius)

If all the heat absorbed be at one temperature, and that rejected be at one lower temperature, then will the heat which is transmuted into work be to the entire heat absorbed in the same ratio as the difference between the absolute temperature of the source and refrigerator is to the absolute temperature of the source. In other words, the second law is an expression for the efficiency of the perfect elementary engine. (Wood.)

The living force, or vis viva, of a body (called heat) is always proportional

to the absolute temperature of the body. (Trowbridge.) The expression  $\frac{Q_1-Q_2}{Q_0}=\frac{T_1-T_2}{T_c}$  may be called the symbolical or al-

gebraic enunciation of the second law,—the law which limits the efficiency of heat engines, and which does not depend on the nature of the working medium employed. (Trowbridge.)  $Q_1$  and  $T_1$  = quantity and absolute

temperature of the heat received,  $Q_2$  and  $T_2$  = quantity and absolute temperature of the heat rejected.

The expression  $\frac{T_1 - T_2}{T_1}$  represents the efficiency of a perfect heat engine

which receives all its heat at the absolute temperature  $T_1$ , and rejects heat at the temperature  $T_2$ , converting into work the difference between the quantity received and rejected.

EXAMPLE.—What is the efficiency of a perfect heat engine which receives heat at 388° F. (the temperature of steam of 200 lbs, gauge pressure) and rejects heat at 100° F. (temperature of a condenser, pressure 1 lb. above vacuum).

$$\frac{388 + 459.2 - 100 + 459.2}{388 + 459.2} = 34\%, \text{ nearly.}$$

In the actual engine this efficiency can never be attained, for the difference between the quantity of heat received into the cylinder and that rejected into the condenser is not all converted into work, much of it being lost by radiation, leakage, etc. In the steam engine the phenomenon of cylinder condensation also tends to reduce the efficiency.

# PHYSICAL PROPERTIES OF GASES.

(Additional matter on this subject will be found under Heat, Air, Gas, and Steam.)

When a mass of gas is enclosed in a vessel it exerts a pressure against the walls. This pressure is uniform on every square inch of the surface of the vessel; also, at any point in the fluid mass the pressure is the same in every

In small vessels containing gases the increase of pressure due to weight may be neglected, since all gases are very light; but where liquids are concerned, the increase in pressure due to their weight must always be taken

Expansion of Gases, Marriotte's Law.—The volume of a gas diminishes in the same ratio as the pressure upon it is increased.

This law is by experiment found to be very nearly true for all gases, and

is known as Boyle's or Mariotte's law.

If  $p = \text{pressure at a volume } v_1, p_1v_1 = \text{pressure at a volume } v_1, p_1v_1 = \text{pressure at a volume } v_2, v_3 = v_3$  $pv; p_1 = \frac{v}{v_1}p; pv = a \text{ constant.}$ The constant, C, varies with the temperature, everything else remaining

the same.

Air compressed by a pressure of seventy-five atmospheres has a volume about 2% less than that computed from Boyle's law, but this is the greatest divergence that is found below 160 atmospheres pressure.

**Law of Charles.**—The volume of a perfect gas at a constant pressure is proportional to its absolute temperature. If  $v_t$  be the volume of a gas at 32°  $F_*$ , and  $v_t$  the volume at any other temperature,  $t_i$ , then

$$\begin{split} v_1 &= v_0 \Big( \frac{t_1 + 459.2}{491.2} \Big); \qquad v_1 = \Big( 1 + \frac{t_1 - 32^\circ}{491.2} \Big) v_0, \\ \text{or} \qquad v_1 &= [1 + 0.002036(t_1 - 32^\circ)] v_0. \end{split}$$

If the pressure also change from  $p_0$  to  $p_1$ 

$$v_1 = v_0 \frac{p_0}{p_1} \left( \frac{t_1 + 459.2}{491.2} \right).$$

The Densities of Gases and Vapors are simply proportional to their atomic weights. Avogadro's Law.-Equal volumes of all gases, under the same con-

ditions of temperature and pressure, contain the same number of molecules. To find the weight of a gas in pounds per cubic foot at 32° F., multiply half the molecular weight of the gas by .00559. Thus 1 cu. ft. marsh-gas, CH<sub>4</sub>,

$$=\frac{12+4}{2} \times .00559 = .0447 \text{ lb},$$

When a certain volume of hydrogen combines with one half its volume of oxygen, there is produced an amount of water vapor which will occupy the same volume as that which was occupied by the hydrogen gas when at the

same temperature and pressure.

Saturation-point of Vapors .- A vapor that is not near the saturation-point behaves like a gas under changes of temperature and pressure: but if it is sufficiently compressed or cooled, it reaches a point where it begins to condense: it then no longer obeys the same laws as a gas, but its pressure cannot be increased by diminishing the size of the vessel containing it, but remains constant, except when the temperature is changed. The only gas that can prevent a liquid evaporating seems to be its own vapor.

Dalton's Law of Gaseous Pressures .- Every portion of a mass of gas inclosed in a vessel contributes to the pressure against the sides of the vessel the same amount that it would have exerted by itself had no

other gas been present.

Mixtures of Vapors and Gases .- The pressure exerted against the interior of a vessel by a given quantity of a perfect gas enclosed in it is the sum of the pressures which any number of parts into which such quantity might be divided would exert separately, if each were enclosed in a vessel of the same bulk alone, at the same temperature. Although this law is not exactly true for any actual gas, it is very nearly true for many. Thus if 0.080728 lb. of air at 32° F., being enclosed in a vessel of one cubic foot capacity, exerts a pressure of one atmosphere or 14.7 pounds, on each square capacity, exerts a pressure of the atmosphere of 14.7 pounds, on each square inch of the interior of the vessel, then will each additional 0.080728 lb. of air which is enclosed, at 32°, in the same vessel, produce very nearly an additional atmosphere of pressure. The same law is applicable to mixtures of gases of different kinds. For example, 0.12344 lb. of carbonic-acid gas, at 32°, being enclosed in a vessel of one cubic foot in capacity, exerts a pressure of one atmosphere; consequently, if 0.080728 lb. of air and 0.12344 lb. of carbonic acid, mixed, be enclosed at the temperature of 22°, in a vessel of one cubic foot of capacity, the mixture will exert a pressure of two atmospheres. pheres. As a second example: Let 0.080728 lb. of air, at 212°, be enclosed in a vessel of one cubic foot; it will exert a pressure of

 $\frac{212+459.2}{32+459.2} = 1.366$  atmospheres.

Let 0.03797 lb. of steam, at 212°, be enclosed in a vessel of one cubic foot; it will exert a pressure of one atmosphere. Consequently, if 0.080728 lb. of air and 0.03797 lb. of steam be mixed and enclosed together, at 212°, in a vessel of one cubic foot, the mixture will exert a pressure of 2.366 atmospheres. It is a common but erroneous practice, in elementary books on physics, to de-scribe this law as constituting a difference between mixed and homogeneous gases; whereas it is obvious that for mixed and homogeneous gases the law of pressure is exactly the same, viz., that the pressure of the whole of a gaseous mass is the sum of the pressures of all its parts This is one of the This is one of the laws of mixture of gases and vapors.

A second law is that the presence of a foreign gaseous substance in contact with the surface of a solid or liquid does not affect the density of the vapor of that solid or liquid unless there is a tendency to chemical com-

bination between the two substances, in which case the density of the vapor is slightly increased. (Rankine, S. E., p. 239.) Flow of Gases.—By the principle of the conservation of energy, it may be shown that the velocity with which a gas under pressure will escape into a vacuum is inversely proportional to the square root of its density; that is, oxygen, which is sixteen times as heavy as hydrogen, would, under exactly the same circumstances, escape through an opening only one fourth as fast as the latter gas,

Absorption of Gases by Liquids .- Many gases are readily absorbed by water. Other liquids also possess this power in a greater or less degree. Water will for example, absorb its own volume of carbonic-acid gas, 430 times its volume of ammonia, 21/3 times its volume of chlorine, and

only about 1/20 of its volume of oxygen.

The weight of gas that is absorbed by a given volume of liquid is proportional to the pressure. But as the volume of a mass of gas is less as the pressure is greater, the volume which a given amount of liquid can absorb at a certain temperature will be constant, whatever the pressure. Water, for example, can absorb its own volume of carbonic acid gas at atmospheric pressure; it will also dissolve its own volume if the pressure is twice as great, but in that case the gas will be twice as dense, and consequently twice the weight of gas is dissolved.

#### ATR.

**Properties of Air.**—Air is a mechanical mixture of the gases oxygen and uitrogen; 21 parts O and 79 parts N by volume, 23 parts O and 77 parts N by weight.

The weight of pure air at  $32^\circ$  F. and a barometric pressure of 39.92 inches of mercury, or 14.693 bls. per  $s_4$  in, or 2116.3 bls. per  $s_4$  ft, is, 969728 bls. The volume of 1 lb. is 12.387 cubic feet. At any other temperature and barometric pressure its weight in lbs. per cubic foot is  $W = \frac{1.3253 \times B}{459.2 + T}$  where B = height of the barometer, T = temperature Fahr, and  $1.3253 \times B$  weight in lbs. of  $459.2 \times B$ , cf. of air at  $0^\circ$  F, and one inch barometric pressure. Air expands 1.491.2 of its volume for every increase of  $1^\circ$  F, and its volume varies inversely as the pressure.

Volume, Density, and Pressure of Air at Various Temperatures. (D. K. Clark.)

77.1		at Atmos. sure.	per	ensity, lbs. Cubic Foot at	Pressure at Constan Volume.		
Fahr.	Cubic Feet in 1 lb.	Compara- tive Vol.	Atn	ios. Pressure.	Lbs. per Sq. In.	Compara- tive Pres.	
0 32 40 50 62 70 80 90 100 110 120 130 140	11.583 12.387 12.586 12.840 13.141 13.342 13.593 13.845 14.096 14.344 14.592 14.846 15.100 15.351	.881 .943 .958 .977 1.000 1.015 1.034 1.073 1.073 1.111 1.130 1.149		.086331 .080728 .079439 .077884 .076097 .073565 .072330 .070942 .069721 .065500 .067361 .066221 .066500 .067361 .06688	12.96 18.86 14.08 14.36 14.70 14.92 15.21 15.49 15.77 16.05 16.33 16.61 16.89	.881 .943 .958 .977 1.000 1.015 1.034 1.073 1.073 1.111 1.130 1.149 1.168	
160 170 180 200 210 212	15.603 15.854 16.106 16.606 16.860 16.910	1.187 1.206 1.226 1.264 1.283 1.287		.063089 .062090 .060210 .059313 .059135	17.50 17.76 18.02 18.58 18.86 18.92	1.187 1.206 1.226 1.264 1.283 1.287	

The Air-manometer consists of a long vertical glass tube, closed at the upp: end, open at the lower end, containing air, provided with a scale, and immersed, along with a thermometer, in a transparent liquid, such as water or oil, contained in a strong cylinder of glass, which communicates with the vessel in which the pressure is to be ascertained. The scale shows the volume occupied by the air in the tube.

Let  $v_0$  be that volume, at the temperature of  $32^{\circ}$  Fahrenheit, and mean pressure of the atmosphere,  $p_0$ ; let  $v_1$  be the volume of the air at the temperature t, and under the absolute pressure to be measured  $p_1$ ; then

$$p_1 = \frac{(t + 459.2^{\circ})p_0v_0}{491.2^{\circ}v_1}.$$

# Pressure of the Atmosphere at Different Altitudes.

At the sea-level the pressure of the air is 14.7 pounds per square inch; at 14 of a mile above the sea-level it is 14.02 pounds; at 1½ mile, 13.33; at 34 mile, 12.66; at 1 mile, 12.02; at 114 mile, 11.42; at 114 mile, 10.85; and at 3

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miles, 9.80 pounds per square inch. For a rough approximation we may assume that the pressure decreases 1/2 pound per square inch for every 1000 feet of ascent.

It is calculated that at a height of about 3½ miles above the sea-level the weight of a cubic foot of air is only one half what it is at the surface of the earth, at seven miles only one fourth, at fourteen miles only one sixty-fourth, and at a height of over forty-five miles it becomes so attenuated as to have no appreciable weight.

The pressure of the atmosphere increases with the depth of shafts, equal to about one inch rise in the barrometer for each 900 feet increase in depth; this may be taken as a rough-and-ready rule for ascertaining the depth of shafts.

# Pressure of the Atmosphere per Square Inch and per Square Foot at Various Readings of the Barometer.

RULE.—Barometer in inches × .4908 = pressure per square inch; pressure per square inch × 144 = pressure per square foot.

Barometer.	Pressure per Sq. In.	Pressure per Sq. Ft.	Barometer.	Pressure per Sq. In.	Pressure per Sq. Ft.
in, 28.00 28.25 28.50 28.75 29.00 29.25 29.50	lbs. 13.74 13.86 13.98 14.11 14.23 14.35 14.47	lbs.* 1978 1995 2013 2031 2049 2066 2083	in. 29.75 30.00 30.25 30.50 30.75 31.00	lbs. 14.60 14.72 14.84 14.96 15.09 15.21	1bs.* 2102 2119 2136 2154 2172 2190

\* Decimals omitted.

For lower pressures see table of the Properties of Steam.

### Barometric Readings corresponding with Different Altitudes, in French and English Measures.

Alti- tude.	Read- ing of Barom- eter.	Altitude.	Reading of Barom- eter.	Alti- tude.	Reading of Barom- eter.	Altitude.	Reading of Barom- eter.
meters. 0 21 127 234 342 453 564 678 793 909 1027	mm. 762 760 750 740 730 720 710 700 690 680 670	feet. 0. 68.9 416.7 767.7 1122.1 1486.2 1850.4 2224.5 2599.7 2962.1 3369.5	inches. 30. 29.92 29.52 29.53 28.74 28.35 27.95 27.16 26.77 26.38	meters. 1147 1269 1393 1519 1647 1777 1909 2043 2180 2318 2460	mm. 660 650 640 630 620 610 600 590 580 570	feet. 3763.2 4163.3 4568.3 4568.3 5830.2 6243. 6702.9 7152.4 7605.1 8071.	inches. 25.98 25.59 25.19 24.80 24.41 24.01 23.62 22.83 22.44 22.04

Levelling by the Barometer and by Boiling Water, kind of levelling unreliable where great accuracy is required. It is difficult to read off from an aneroid (the kind of barometer usually employed for engineering purposes) to within from two to five or six feet, depending on its size. The moisture or dryness of the air affects the results; also winds, the vicinity of mountains, and the daily atmospheric tides, which cause incessant and irregular fluctuations in the barometer. A barometer hauging quietly in a room will often vary 1/4 of an inch within a few hours, corresponding to a difference of elevation of nearly 100 feet. No formula can possibly be devised that shall embrace these sources of error,

To Find the Difference in Altitude of Two Places,—Take from the table the altitudes opposite to the two boiling temperatures, or to the two barometer readings. Subtract the one opposite the lower reading from that opposite the upper reading. The remainder will be the required beight, as a rough approximation. To correct this, add together the two thermometer readings, and divide the sum by 2, for their mean. From table of corrections for temperature, take out the number under this mean. Multiply the approximate height just found by this number.

At 70°F, pure water will boil at 1° less of temperature for an average of

At 70° F. pure water will boil at 1° less of temperature for an average of about 550 feet of elevation above sea-level, up to a height of 1/2 a mile. At the height of 1 mile, 1° of boiling temperature will correspond to about 560 feet of elevation. In the table the mean of the temperatures at the two stations is assumed to be 32°F, at which no correction for temperature is

necessary in using the table.

Boiling- point in deg. Fah.	Barom. in,	Altitude above Sea-level, feet,	Boiling- point in deg. Fah.	Barom, in.	Altitude above Sea-level, feet.	Boiling- point in deg. Fah.	Barom. in.	Altitude above Sea-level, feet.
184°	16.79	15,221	196	21.71	8,481	208	27.73	2,063
185	17.16	14,649	197	22.17	7,932	208.5	28.00	1,809
186	17.54	14,075	198	22.64	7,381	209	28.29	1,539
187	17.93	13,498	199	28.11	6,843	209.5°	28.56	1,290
188	18,32	12,934	200	23.59	6,304	210	28.85	1,025
189	18.72	12,367	201	24.08	5,764	210.5	29.15	754
190	19.13	11,799	202	24.58	5,225	211	29,42	512
191	19.54	11,243	203	25.08	4,697	211.5	29,71	255
192	19.96	10,685	204	25,59	4,169	212	30.00	S. L. = 0
193	20.39	10,127	205	26.11	3,642	212.5	30,30	-261
194	20.82	9,579	206	26.64	3,115	213	30.59	-511
195	21.26	9.031	207	27.18	2.589	~10	50.00	-311
150	~1.50	0,001	201	~1.10	1 2,000		(	

# CORRECTIONS FOR TEMPERATURE.

 Mean temp. F. in shade. 0 | 10° | 20° | 30° | 40° | 50° | 60° | 70° | 80° | 90° | 100°

 Multiply by
 .933 | .954 | .975 | .996 | 1.016 | 1.036 | 1.058 | 1.079 | 1.100 | 1.121 | 1.142

Moisture in the Atmosphere.—Atmospheric air always contains a small quantity of carbonic-acid gas and a varying quantity of aqueous vapor. Pure mountain air contains about 3 to 4 parts of carbonic acid in 10,000. A properly ventilated room should contain not more than six parts in 10,000.

The degree of saturation or relative humidity of the air is determined by the use of the dry and wet bulb thermometer. The degree of saturation for a number of different readings of the thermometer is given in the following table:

INDICATIONS OF THE HYGROMETER (DRY AND WET BULB), FROM MR. GLAISHER'S OBSERVATIONS AT GREENWICH.

	Difference of Temperature or Degrees of Cold in the Wetbulb Thermometer.
Temperature of the Air, Fahrenheit.	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24
	Degrees of Humidity, Saturation being 100.
52° 62° 72° 82°	87 75 78 72 66 00 54 49 44 40 36 33 30 27 93 86 80 74 69 64 59 54 50 46 12 30 36 33 30 27 25 94 88 27 72 67 66 25 85 54 50 47 44 11 88 32 30 28 20 28 20 21 94 89 82 77 72 67 68 25 85 54 50 47 44 11 88 32 30 28 20 28 20 28 20 21 95 90 8 90 67 67 26 68 64 60 57 54 51 48 45 23 30 36 44 32 30 28 26 24 23 32 95 94 89 84 77 77 37 70 66 65 55 54 51 48 45 42 40 38 83 33 31 29 27 26 32 95 90 85 80 76 72 68 64 60 57 54 51 48 45 42 40 88 35 33 36 34 32 30 28 26 24 33 28 28 28 28 28 28 28 28 28 28 28 28 28

Weights of Air, Vapor of Water, and Saturated Mixtures of Air and Vapor at Different Temperatures, under the Ordinary Atmospheric Pressure of 29,921 inches of Mercusure

inches of Mercury.											
	Ft.	i,	MIXTUE	RES OF AII	R SATURAT	ED WITH V	APOR.				
. je	ibic iffer Ibs.	ce of Vap Mercury.	Elastic Force of the Air in		of Cubic Fo		Weight of				
Temperature, Fahrenheit.	Painperauite, Rainenheit. Weight of a Cubic Ft. of Dry Air at Different Temperatures, 1bs.		Mixture of Airand Vapor, Inches of Mercury.	Weight of the Air, lbs.	Weight of the Vapor, pounds.	Total W'ght of Mixture, pounds.	Vapor mixed with 1 lb. of Air, pounds.				
0°	.0864	.044	29.877	.0863	.000079	.086379	.00092				
12 22	.0842	.074	29.849 29.803	.0840	.000130	.084130	.00155				
32	.0807	.181	29.740	.0802	.000304	.080504	.00379				
42	.0791	.267	29,654	.0784	.000440	.078840	.00561				
42 52	.0776	.388	29,533	.0766	.000627	.077227	.00819				
62 72 82	.0761	,556	29.365	.0747	.000881	.075581	.01179				
72	.0747	.785	29.136	.0727	.001221	.073921	.01680				
82	.0733	1.092	28.829	.0706	.001667	.072267	.02361				
92	.0720	1.501	28.420	.0684	.002250	.070717	.03289				
102	.0707	2.036	27.885	.0659	.002997	.068897	.04547				
112	.0694	2.731	27.190	.0631	.003946	.067046	.06253				
122 132	.0682	3.621 4.752	26.300 25.169	.0599	.005142	.065042	.08584				
142	.0660	6.165	23.756	.0524	.008473	.060873	.16170				
152	.0649	7.930	21.991	.0324	.010716	.058416	.22465				
162	.0638	10.099	19.822	.0423	.013415	.055715	.31713				
172	.0628	12.758	17.163	.0360	.016682	.052682	.46338				
182	.0618	15.960	13.961	,0288	.020536	.049336	.71300				
192	.0609	19,828	10.093	.0205	.025142	:045642	1.22643				
202	.0600	24.450	5.471	.0109	.030545	.041445	2.80230				
212	.0591	29 921	0.000	.0000	.036820	.036820	Infinite.				

The weight in lbs. of the vapor mixed with 100 lbs. of pure air at any given temperature and pressure is given by the formula

$$\frac{62.3 \times E}{29.92 - E} \times \frac{29.92}{p}$$

where E = elastic force of the vapor at the given temperature, in inches of mercury; p = absolute pressure in inches of mercury, = 29.92 for ordinary atmospheric pressure.

Specific Heat of Air at Constant Volume and at Constant Pressure,—Volume of 1 h, of air at 32° F, and pressure of 14.7 lbs, per sq. in. = 12.387 cu. ft. = a column 1 sq. ft. area × 12.387 ft. high. Raising temperature 1° F. expands it  $\frac{1}{491.2}$ , or to 12.4122 ft. high—a rise of .02522 foot.

Work done = 2116 lbs. per sq. ft.  $\times$  .02522 = 53.37 foot-pounds, or 53.37  $\div$  778 = .0686 heat units.

The specific heat of air at constant pressure, according to Regnault, is 0.2375; but this includes the work of expansion, or .0686 heat units; hence the specific heat at constant volume = 0.2375 - .0686 = 0.1689.

Ratio of specific heat at constant pressure to specific heat at constant volume = .2375 + .1689 = 1.406. (See Specific Heat, p. 458.)

Flow of Air through Orfices,—The theoretical velocity in feet per second of flow of any fluid, liquid, or gas through an orifice is v $\sqrt{2gh} = 8.02 \ \sqrt{h}$ , in which h = the "head" or height of the fluid in feet required to produce the pressure of the fluid at the level of the orifice.  $h = \frac{v^2}{2a}$ . The quantity of flow in cubic feet per second is equal to the product

of this velocity by the area of the orifice, in square feet, multiplied by a "coefficient of flow," which takes into account the contraction of the vein

or flowing stream, the friction of the orifice, etc.

For air flowing through an orifice or short tube, from a reservoir of the pressure  $p_1$  into a reservoir of the pressure  $p_2$ . Weisbach gives the following values for the coefficient of flow, obtained from his experiments.

# FLOW OF AIR THROUGH AN ORIFICE.

# FLOW OF AIR THROUGH A SHORT TUBE.

Orifice rounded.)

FLIEGNER'S EQUATIONS FOR FLOW OF AIR FROM A RESERVOIR THROUGH AN
ORIFICE. (Peabody's Thermodynamics, p. 135.)

Orifice. (Peabody's Thermodynamics, p. 135.)

For 
$$p_1 > 2pa$$
,  $G = 0.530 F \frac{p_1}{\sqrt{T_1}}$ ;

 $p_1 > 2pa$ ,  $G = 1.060 F \sqrt{\frac{pa(p_1 - pa)}{T_1}}$ ;

 $p_1>2pa, \quad G=1.060\ F\sqrt{\frac{pa(p_1-pa)}{T_1}};$  G= flow of air through the orifice in lbs. per sec., F= 6

G= flow of air through the orifice in lbs, per sec., F= area of orifice in square inches,  $p_1=$  pressure in reservoir in lbs, per sq. in.,  $p_a=$  pressure of atmosphere,  $T_1=$  absolute temperature, Fabrenhelt, of air in reservoir. Clark (Rules, Tables, and Data, p. 89) gives, for the velocity of flow of air through an orifice due to small differences of pressure,

$$V = C \sqrt{\frac{2gh}{12} \times 778.2 \times \left(1 + \frac{t - 32}{493}\right) \times \frac{29.92}{p}},$$

or, simplified,

$$V = 352 \ C \sqrt{\left(1 + .00203(t - 32)\frac{h}{p}\right)};$$

in which V= velocity in feet per second; 2g=64.4; h= height of the column water in inches, measuring the difference of pressure;  $\ell=$  the temperature Fahr.; and p= barometric pressure in inches of mercury. 73.2 is the volume of air at  $32^\circ$  under a pressure of 29.92 inches of mercury when that of an equal weight of yater is taken as 1.

For 62° F., the formula becomes V=363C  $\sqrt{\frac{h}{p}}$ , and if p=29.92 inches V=

66.35C  $\sqrt{h}$ 

The coefficient of efflux C, according to Weisbach, is:

For conoidal mouthpiece, of form of the contracted vein, with pressures of from .38 to 1.1 atmospheres. C=.97 to .99 Circular orifices in thin plates. C=.56 to .79 Short cylindrical mouthpieces. C=.81 to .84 The same rounded at the inner end C=.92 to .98 Conical converging mouthpieces C=.90 to .99

Flow of Air in Pipes.—Hawksley (Proc. Inst. C. E., xxxiii, 55) states that his formula for flow of water in pipes  $v = 48 \sqrt{\frac{H\overline{D}}{L}}$  may also

be employed for flow of air. In this case H= height in feet of a column of air required to produce the pressure causing the flow, or the loss of head

for a given flow; v = velocity in feet per second, D = diameter in feet, L =

length in feet.  $p = \frac{1}{2}$  length in feet is expressed in inches of water, h, the air being taken at  $\frac{1}{2}$  F, its weight per cubic foot at atmospheric pressure = .0761 lb. Then

 $H = \frac{62.36}{.0761 \times 12} = 68.3h$ . If d = diameter in inches,  $D = \frac{d}{10}$ , and the formula becomes v=114.5  $\sqrt{\frac{hd}{T}}$ , in which h= inches of water column, d= diam-

eter in inches and L = length in feet;  $h = \frac{Lv^2}{13110d}$ ;  $d = \frac{Lv^2}{13110d}$ 

The quantity in cubic feet per second

$$Q = .7854 \frac{d^2}{144} v = .6245 \sqrt{\frac{hd^5}{L}}; \quad d = \sqrt[5]{\frac{Q^2 L}{.39h}}; \quad h = \frac{Q^2 L}{.30d^5}.$$

The horse-power required to drive air through a pipe is the volume Q in cubic feet per second multiplied by the pressure in pounds per square foot and divided by 550. Pressure in pounds per square foot = P = inches of water column imes 5.196, whence horse-power =

$$HP_{\cdot} = \frac{QP}{550} = \frac{Qh}{105.9} = \frac{Q^3L}{41.3d^5}$$

If the head or pressure causing the flow is expressed in pounds per square inch = p, then h = 27.71p, and the above formulæ become

$$\begin{split} v &= 602.7 \sqrt{\frac{pd}{L}}; \ \ p = \frac{Lv^2}{363,300d}; \ \ d = \frac{Lv^2}{363,300p}; \\ Q &= 3.287 \sqrt{\frac{pd^5}{L}}; \ \ p = \frac{Q^2L}{10.806d^5}; \ \ d = \sqrt[5]{\frac{Q^2L}{10.806p}}; \\ HP. &= \frac{Q144p}{550} = .2618Qp = .02421\frac{Q^2L}{d^5}. \end{split}$$

# Volume of Air Transmitted in Cubic Feet per Minute in Pipes of Various Diameters.

Formula 
$$Q = \frac{.7854}{144} d^2v \times 60$$
.

Actual Diameter of Pipe in Inches.

of O												
Feet p. sec	1	2	3	4	5	6	8	10	12	16	20	24
	-						20.04			00.00		400
1	.327	1.31	2.95		8.18	11.78	20.94	32.73		83.77	130.9	
2 3	.655	2.62	5.89	10.47	16.36	23.56	41 89	65.45		167.5	261.8	
3	.982	3.93		15.7	24.5	35.3	62.8	98.2	141.4	251.3	392.7	565.5
4	1.31		11.78	20.9	32.7	47.1	83.8	131	188	335	523	754
4 5	1.64		14.7	26.2	41	59	104	163	235	419	654	942
6	1.96	7.85	17.7	31.4	49.1	70.7	125	196	283	502	785	1131
7	2.29	9.16		36.6	57.2	82.4	146	229	330	586	916	1319
9	2.62		23.5	41.9	65.4	94	167	262	377	670	1047	1508
9	2.95	11.78	26.5	47	73	106	188	294	424	754	1178	1696
10	3.27	13.1	29.4	52	82	118	209	327	471	838	1309	1885
12	3.93	15.7	35.3	63	98	141	251	393	565	1005	1571	2262
15	4.91	19.6	44.2	78	122	177	314	491	707	1256	1963	2827
18		23.5	53	94	147	212	377	589	848	1508	2356	3393
20		26.2	59	105	164	235	419	654	942	1675	2618	3770
24		31.4	71	125	196	283	502	785	1131	2010	3141	4524
25		32.7	73	131	204	294	523	818	1178	2094	3272	4712
28		36.6	82	146		330	586	916	1319	2346	3665	5278
30	9.8	39.3	88							2513	3927	5655

In Hawksley's formula and its derivatives the numerical coefficients are In Hawksley's formula and its derivatives the numerical coefficients are constant. It is scarcely possible, however, that they can be accurate except within a limited range of conditions. In the case of water it is found that the coefficient of friction, on which the loss of head depends, varies with the length and diameter of the pipe, and with the velocity, as well as with the condition of the interior surface. In the case of air and other gases we have, in addition, the decrease in density and consequent increase in volume and in velocity due to the progressive loss of head from one end of the pipe

Clark states that according to the experiments of D'Aubisson and those of a Sardinian commission on the resistance of air through long conduits or pipes, the diminution of pressure is very nearly directly as the length, and as the square of the velocity and inversely as the diameter. The resistance

is not varied by the density.

If these statements are correct, then the formulæ  $h=\frac{Lv^2}{cd}$  and  $h=\frac{Q^2L}{c'd^5}$ and their derivatives are correct in form, and they may be used when the numerical coefficients c and c' are obtained by experiment.

If we take the forms of the above formulæ as correct, and let C be a variable coefficient, depending upon the length, diameter, and condition of surface of the pipe, and possibly also upon the velocity, the temperature and the density, to be determined by future experiments, then for h = head in inches of water, d = diameter in inches, L = length in feet, v = velocity in feet per second, and Q = quantity in cubic feet per second:

$$v = C\sqrt{\frac{hd}{L}};$$
  $d = \frac{Lv^2}{C^2h};$   $h = \frac{Lv^2}{C^2d};$   $Q = .005454C\sqrt{\frac{hd^5}{L}};$   $d = \sqrt[4]{\frac{33683Q^2L}{C^2h}};$   $h = \frac{33683Q^2L}{C^2d^5};$ 

For difference or loss of pressure p in pounds per square inch,

$$\begin{split} h &= 27.71p & \sqrt{h} = 5.264 \, \sqrt{p}; \\ v &= 5.264 \, C \sqrt{\frac{pd}{L}}; & d &= \frac{Lv^2}{27.71 \, C^2 p}; & p &= \frac{Lv^2}{27.71 \, C^2 U}; \\ Q &= .02871 \, C \sqrt{\frac{pd^5}{L}}; & d &= \sqrt[5]{\frac{1218 \, Q^2 L}{C^2 p}}; & p &= \frac{1213 \, Q^2 L}{C^2 Q^2}. \end{split}$$

(For other formulæ for flow of air, see Mine Ventilation.)

Loss of Pressure in Ounces per Square Inch .- B. F. Sturtevant Company uses the following formulæ:

$$p_1 = \frac{Lv^2}{25000d} \; ; \quad v = \frac{\sqrt{25000dp_1}}{L} \; ; \quad d = \frac{Lv^2}{25000p_1} \; ;$$

in which  $p_1 = loss$  of pressure in ounces per square inch, v = velocity of air in feet per second, and L = length of pipe in feet. If p is taken in pounds per square inch, these formulæ reduce to

$$p = .0000025 \frac{Lv^2}{d}$$
;  $v = \frac{.00158 \sqrt[4]{dp}}{L}$ ;  $d = \frac{.0000025 Lv^2}{p}$ .

These are deduced from the common formula (Weisbach's),  $p = f_{\overline{d}}^{\overline{l}} \frac{v^{5}}{2\sigma^{5}}$ , in which f = .0001608.

The following table is condensed from one given in the catalogue of B. F.

Sturtevant Company.

Loss of pressure in pipes 100 feet long, in ounces per square inch. For any other length, the loss is proportional to the length,

Diameter of Pipe in Inches.												
			Dia	neter o	of Pipe	in In	ches.					
1 2 3 4 5 6 7 8 9 10 11 Loss of Pressure in Ounces.											12	
	Loss of Pressure in Ounces.											
$\begin{array}{cccccccccccccccccccccccccccccccccccc$										.033 .133 .300 .533 .833 1.200 1.633 2.133 3.333		
14	16	18	20	22	24	28	32	36	40	44	48	
			Los	s of Pr	essure	in Ou	inces.					
.029 .114 .257 .457 1.029 1.400 1.829	.026 .100 .225 .400 .900 1.225 1.600	.022 .089 .200 .356 .800 1.089 1.422	.020 .080 .180 .320 .720 .980 1.280	.018 .073 .164 .291 .655 .891 1.164	.017 .067 .156 .267 .600 .817 1.067	.014 .057 .129 .239 .514 .700 .914	.012 .050 .112 .200 .450 .612 .800	.011 .044 .100 .178 .400 .544 .711	.010 .040 .090 .160 .360 .490 .640	.009 .036 .082 .145 .327 .445 .582	.008 .033 .075 .133 .300 .408 .533 .833	
	.400 1.600 3.600 6.400 10. 14.4 14. 14. 14. 257 457 1.029 1.400	400   .200   .800   .	.400 .200 .133 1.600 .800 .133 3.600 1.800 1.200 6.400 3.200 2.133 14.4 7.2 4.85 9.8 6.533 12.8 6.533 120. 13.333 14 16 18	Los    1	Loss of Pr   Loss of Pr   1	Loss of Pressure   Loss of Pre	Loss of Pressure in O	Loss of Pressure in Ounces    400	Loss of Pressure in Ounces.	Loss of Pressure in Ounces.   Loss of Pressure in Ounces.     Loss of Pressure in Ounces.	Loss of Pressure in Ounces.	

Effect of Bends in Pipes. (Norwalk Iron Works Co.)

Radius of elbow, in diameter of pipe =5 3 2 1½ 1½ 1 3 ½ 2 Equivalent lgths. of straight pipe, diams 7.85 8.24 9.03 10.86 12.72 17.51 25.09 121.2

dompressed-air Transmission. (Frank Richards. Am. Mach., March 8, 1894)—The volume of free air transmitted may be assumed to be directly as the number of atmospheres to which the air is compressed. Thus, if the air transmitted be at 75 pounds gauge-pressure, or six atmospheres, the volume of free air will be six times the amount given in the table (page 486). It is generally considered that for economical transmission the velocity in main pipes should not exceed 20 feet per second. In the smaller distributing pipes the velocity should be decidedly less than this. The loss of power in the transmission of compressed air in general is not

The loss of power in the transmission of compressed air in general is not a serious one, or at all to be compared with the losses of power in the operation of compression and in the re-expansion or final application of the air. The formulas for loss by friction are all unsatisfactory. The statements

of observed facts in this line are in a more or less chaotic state, and selfevidently unreliable.

A statement of the friction of air flowing through a pipe involves at least all the following factors: Unit of time volume of air, pressure of air, diameter of pipe, length of pipe, and the difference of pressure at the ends of the pipe or the head required to maintain the flow. Neither of these factors can be allowed its independent and absolute value, but is subject to modifications in deference to its associates. The flow of air being assumed to be uniform at the entrance to the pipe, the volume and flow are not uniform after that. The air is constantly losing some of its pressure and its volume is constantly increasing. The velocity of flow is therefore also somewhat accelerated continually. This also modifies the use of the length of the pipe as a constant factor.

Then, besides the fluctuating values of these factors, there is the condition of the pipe itself. The actual diameter of the pipe, especially in the smaller sizes, is different from the nominal diameter. The pipe may be straight, or it may be crooked and have numerous elbows. Mr. Richards

considers one elbow as equivalent to a length of pipe,

Head or Additional Pressure in pounds per sq. in-required to deliver Air at 75 Pounds Gauge-pressure through Pipes of Various Sizes and Lengths. (Frank Richards.)

		1" F	IPE.			4" PIPE.					
Cubic ft. free air per min.		Leng	gth in	feet.		Cubic ft. free air per min.		Len	gth in	feet.	
Cub fre per	50	100	300	500	1,000	Cubi free per	200	300	400	1,000	2,000
25 50 100 150	.245 .981 3.925	of pre .49 1.962 7.85 17.66	ssure, 1.47 5.886	2.45	sq. in. 4.9	500 750 1,000 1,250	Loss .16 .36 .64	.24 .54 .96 1.5	ssure, .4 .9 1.6 2.5 3.6	lbs.p. .8 1.8 3.2 5.	sq. in. 1.6 3.6 6.4 10.
		11/4"	PIPE.			1,500	1.44	2.16		7.2	14.4
25 50	.056	.112	.336	.561 2.24	1.12			5" ]	PIPE.		
100 150	.224 .897 2.02 3.59	3.94	1.35 5.38 12.11	8.97	4.49		500	1,000	2,000	4,000	5,000
200		11/2"				500 1,000 1,500	.11 .44 .99	.22 .881 1.98	.44 1.76 3.96	3.52 7.92	1.1 4.4 9.9
25 50	.017	.034	.103	.171	.34 1.37	2,000 2,500	$\frac{1.76}{2.75}$	3.52	7.04	14.08	
100	.274	.548	.411 1.64	2.74	5.48 12.33	.,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		6" F			(
150 200	1.09	1.23 2.19	3.69 6.57	6.16	21.9			(	(	1	1
		2" I	PIPE.				1,000	2,000	4,000	5,000	10,000
50 100 150 200 250	.019 .076 .171 .304 .476	.038 .152 .343 .609	.114 .457 1.03 1.83 2.86	.19 .761 1.71 3 04 4.76	38 1.52 3.44 6.09 9.53	2,000	.354 .799 1.417 2.22 3.18	.708 1.599 2.83 4.44 6.37	1.42 3.2 5.67 8.89 12.7	1.77 3.99 7.09 11.1 15.9	3.54 7.99 14.17
250 300	.685		4.11	6.85	13.72	0,000	9.10	8" I		10.0	
		21/2"	Pipe.	9							
	200	300	500	1,000	2,000	2,000	2,000	1.19	8,000	2.99	15,000
100 200 300 400	.087 .347 .781 1.39	.13 .521 1.17 2.08 3.25	.217 .868 1.95 3.47	.434 1.74 3.91 6.94	.87 3.47 7.81 13.89	2,000 2,500 3,000 4.000 5,000	.935 1.25 2.39 3.74	1.87 2.49 4.79 7.48	3.74 4.99 9.58 14.97	4.68 6.24 11.97	7.02 9.36
500	2.17	3.25	5.42	10.85	21.7			10" F	PIPE.		
		3" I				2,500 5,000	.286 1.14	.57	1.14	1.43 5.71	2.15
100 200 300	.0333 .133 .3	.05 .2 .45	.0833 .333 .75	.166 .666	.33 1.33 3	7,500 10,000	2.57 4.57	2.29 5.15 9.14	10.29	12.86	8.56
400 500	.533	.8	$\begin{array}{c} .75 \\ 1.33 \\ 2.08 \end{array}$	2.66 4.16	5.33 8.33			12"	PIPE.		
250	.0832	31/9"	Pipe.		.83		2,000	4,000	8,000	10,000	20,000
500 750 1,000 1,250	.332 .748 1.328 2.08	.125 .499 1.12 1.99 3.12	.832 1.87 3.33 5.2	.416 1.66 3.75 6.66 10.4	3.32 7.49 13.3	2,500 5,000 7,500 10,000	.11 .44 .99 1.76	.92 .88 1.98 3.52	.44 1.76 3.96 7.05	.55 2.2 4.95 8.81	1.101 4.4 9.91 17 6
A 143	onah	37. D	iahaud	a door	dura av	Tr four	mula r	:+b +1	ia tab	lo on	

Although Mr. Richards does not give any formula with this table, an aspection of it shows that for any given diameter the loss of head is

taken to vary directly as the length and as the square of the quantity delivered, but for a given quantity and length the loss of head appears to vary inversely as some higher power of the diameter than the fifth, approximately the 5.5 power; or, in other words, that the coefficient of fric-

tion is variable. If we take the formula of the form  $Q' = c' \sqrt{\frac{pd^5}{L}}$ ,

 $p=rac{Q'^2L}{c'^2d^3}$ , and solve for  $c'=\sqrt{rac{Q'^2L}{d^3p}}$ , in which Q'= cubic feet of free air

per minute, we find values of the coefficient as follows:

For diameter, inches 1 2 4 6 8 10 12 Value of c'= 357 453 552 603 639 664 676

The following table is condensed from one given by F. A. Halsey in the catalogue of the Rand Drill Co.:

Diameter in inches.	Cubic feet of free air compressed to a gauge-pressure of 60 lbs. and passing through the pipe each minute.												
	50	100	200	400	600	800	1000	1500	2000	3000	4000	5000	
Nominal of Pipe,		Loss of pressure in lbs. per square inch for each 1000 ft. of straight pipe.											
1 11/4 11/2 2 21/2 3 4 5 6 8 10 12 14	10.40 2.63 1.22 .35 .14	4.89 1.41 .57 .20	5.64 2.30 .78 .20	9.20 3.14 .80 .26	7.05 1.81 .59 .23	3.22 1.04 .41 .10	5.02 1.63 .64 .16	3,66 1,46 .37 .12	6.50 2.59 .65 .21	5.81 1.47 .47 .19	10.30 2.61 .84 .34	4.08 1.30 .53	

This table appears to follow more closely than does Richards' table the law of the formula  $p = \frac{Q^2 L}{C^2 \cdot Q^3}$ , but the coefficients differ considerably from those of Richards. Solving for C', we obtain—

Comparing some of the losses of pressure in the two tables, we find-

Length, feet 10	000 1000	1000	5000	5000	5000
Quantity, cu. ft 10		1000	4000	4000	4000
Diameter, inches	4 5	6	8	10	12
Loss, Richards 8	3.2 .881	.354	7.48	2.29	.88
" Halsev 5	5.02   1.63   -	64	13.05	4.20	1 70

The two tables are not calculated for the same amount of compression, but the difference is not sufficient to account for the difference in the coefficients. If we multiply the coefficients derived from Halsey's table by 5/4, the ratio of the pressures 75 and 60 lbs., they become for a 2-inch pipe 589, and for a 12-inch pipe 581, against Richards's figures of 483 and 676 for the same pipes. To compare Richards's figures for loss of pressure with Halsey's, the former should be multiplied by 25/16. In the absence of experimental data no opinion can be formed as to which table is the more accurate, but either one is probably of sufficient accuracy for practical purposes.

Mr. Richards, in Am. Mach., Dec. 27, 1894, publishes a new formula, viz.;

$$p = \frac{V^2 L}{10,000 d^5 a}; \quad V = \sqrt{\frac{10,000 d^5 a p}{L}}; \quad L = \frac{10,000 d^5 a p}{V^2}; \quad d^6 a = \frac{V^2 L}{10,000 p};$$

in which V= actual volume of compressed air delivered, in cubic feet per minute (not the volume of free air, as in the other formulæ), L= length of pipe in feet, d= internal diameter of pipe in inches, p= head or additional pressure in pounds per square inch required to maintain the flow, and a is a coefficient varying with the diameter of the pipe. Its value for different nominal diameters of wrought-iron pipe is given by Mr. Richards as follows:

Diam. in.	Val. of α.	Diam. in.	Val. of a.	Diam. in.	Val. of a.	Diam. in.	Val. of a
1	.35	21/2	.65	5	.93	12	1.26
11/4	.5	3	.73	6	1.	16	1.34
11/2	.66	31/2	.79	8	1.125	20	1.4
2	.56	4	.84	10	1.2	24	1.45

The values of a for the 1 and 114 inch pipes appear inconsistent with the values for the other sizes, because the nominal diameters of these two sizes are relatively much less than their actual diameters, 1.38 and 1.61 inches, respectively. The following values of the fifth power of d and of  $d^5a$  are given by Mr.

Fifth Po	wers of $d$ .		Value of d5a.					
1" 1 1.4" 3.05 114" 7.59 2" 32 214" 97.65 3" 248 314" 525 4" 1024	6" 8" 10" 12" 16"	7,776 32,768 100,000 248,832 1.048,576 3.200,000	1" 35 114" 1.525 114" 5.03 2" 18.08 215" 63.47 3" 177.4 315" 413.2 4" 860.2	5" 2,918.75 6" 7,776 8" 36,864 10" 120,000 12" 313,528 16" 1,405,091 20" 4,480,000 24" 11,545,805				

In order to compare Mr. Richards' new formula for volume of compressed air transmitted with the formula  $Q' = c' \sqrt{\frac{pd^3}{L}}$ , in which Q is the volume of free air, = 5V if the air is compressed to 5 atmospheres, we have

$$Q' = 5V = 500 \sqrt{a} \times \sqrt{\frac{pd^5}{L}},$$

and from the values of a given by Mr. Richards we find values of c' as follows:

Measurement of the Velocity of Air in Pipes by an Anemometer,—Tests were made by B. Donkin, Jr. (Inst. Civil Engrs. 1892), to compare the velocity of air in pipes from 8 in, to 24 in, diam., as shown by an anemometer 3% in, diam, with the true velocity as measured by the time of descent of a gas-holder holding 1622 cubic feet. A table of the results with discussion is given in Eng'g News, Dec. 22, 1892. In pipes from 8 in, to 20 in, diam, with air velocities of from 140 to 600 feet per minute the anemometer showed errors varying from 14.5% fast to 10% slow. With a 24-inch pipe and a velocity of 73 ft, per minute, the anemometer gave from 44 to 3 feet, per limits is that anemometers for the second of the per control of the second of the second of the per minute of the second of the second of the second of the per minute of the second of the seco pipes of these diameters should be used with great caution. The percentage of error is not constant, and varies considerably with the diameter of the pipes and the speeds of air. The use of a baffle, consisting of a perforated plate, which tended to equalize the velocity in the centre and at the sides in some cases diminished the error,

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The impossibility of measuring the true quantity of air by an anemometer held stationary in one position is shown by the following figures, given by Wm. Daniel (Proc. Inst. M. E., 1875), of the velocities of air found at different points in the cross-sections of two different airways in a mine.

#### DIFFERENCES OF ANEMOMETER READINGS IN AIRWAYS.

8 ft. square.											
1712	1795	1859	1329								
1622	1685	1782	1091								
1477	1344	1524	1049								
1262	1356	1293	1333								

Average 1469.

5 × 8 ft.											
1170	1209	1288									
948	1104	1177									
1134	1049	1106									

Average 1132.

Equation of Pipes.—It is frequently desired to know what number of pipes of a given size are equal in carrying capacity to one pipe of a larger size. At the same velocity of flow the volume delivered by two pipes of different sizes is proportional to the squares of their diameters; thus, one 4-inch pipe will deliver the same volume as four 2-inch pipes. With the same head, however, the velocity is less in the smaller pipe, and the volume delivered varies about as the square root of the fifth power (i.e., as the 2.5 power). The following table has been calculated on this basis. The figures opposite the intersection of any two sizes is the number of the smaller-sized pipes required to equal one of the larger. Thus, one 4-inch pipe is equal to 5.7.2-inch pipes.

Diam.	1	2	3	4	5	б	7	8	9	10	12	14	16	18	20	24
2 8 4 4 5 6 6 7 7 8 8 9 10 11 12 13 14 15 16 16 17 18 8 80 86 42 48 86 60	5.7 15.6 32 55.9 88.2 130 161 243 316 401 409 609 733 787	55.9 70.9	8 3 11.7 15.6 20.3 25.7 32 39.1 47 55.9 65 7	1 1.7 2.8 4.1 5.7 6.6 9.9 9 122.9 22.9 237.2 32 48 1 555.9 70.9 108 130 499 670 787	8.9 10.9 13.1 15.6 18.3 24.6 28.1 32 40.6 50.5 74.2 88.2 130 205 286 383	7.1 8.3 9.9 11.7 13.5 15.6 17.8 20.3 25.7 32 39.1 47 55.9 88.2 180 181 243	10.6 12.1 13.8 17.5 21.8 26.6 32 38 60 88.2 123 165	6.6 7.6 8.7 9.9 12.5 15.6 19. 22.9 27.2 43 63.2 88.2	1 1.3 1.7 2.5 3.0 4.2 4.9 9.3 17.1 30.2 47 62.7 88.2 115	50.2	32	21.8 23.2	7.6 11.2 15.6 20.9	3.6 5.7 8.3	1 1.3 1.9 2.3 2.8 8.9 12 15.6	1 1.2 1.5 1.7 2.8 4.1 5.7 7.6 9.9

# Loss of Pressure in Compressed Air Pipe-main, at St. Gothard Tunnel.

(E. Stockalper.)

(E. Stockarper.)											
	eter.	second ir equi- me at c pres-	second sed air nsity.	of air.	ow-	d.	Obse	rved I	Pressui		
Experiment.	Air Main Diameter	Volume per se of free air. or e valent volum atmospheric parties and 32° E	Volume per secon of compressed at mean densit	Mean density o	Weight of air flow ing per second.	Mean velocity in feet per second	Pressure at beginning of pipe.	Pressure at end of pipe.	Loss of Pressure.		Value of $c'$ in formula $p = \frac{Q'L}{c'^2d^5}$
2 }	in. 7.87 5.91 7.87 5.91 7.87 5.91	eu.ft. {33.056} {22.002} {18.364}	cu. ft. 6.534 7.063 5.509 5.863 5.262 5.580	den. .00650 .00603 .00514 .00482 .00449	2 669 1.776 1.776	feet. 19.32 37.14 16.30 15.58 29.34	at. 5.60 5.24 4.35 4.13 3.84 3.65	at. 5.24 5.00 4.13  3.65 3.54	lbs. per sq.in. 5.292 3.528 3.234 2.793 1.617	6.4 4.6 5.1  5.0 3.0	610 515 519 
. `											

The length of the pipe 7.87 in diameter was 15,092 ft., and of the smaller pipe 1712.6 ft. The mean temperature of the air in the large pipe was  $70^{\circ}$  F. and in the small pipe  $80^{\circ}$  F.

### WIND.

Force of the Wind.—Smeaton in 1759 published a table of the velocity and pressure of wind, as follows:

VELOCITY AND FORCE OF WIND, IN POUNDS PER SQUARE INCH.

Miles per hour.	Feet per second.	Force per sq. ft. pounds.	Common Appella- tion of the Force of Wind.	Miles per Hour.	Feet per second.	Force per sq. ft. pounds.	Common Appella- tion of the Force of Wind.
1 2	1.47	0.005	i bie.	20	26.4 29.34 36.67	1.55 1.968 3.075	Very brisk.
23456789	4.4 5.87 7.33	0.044 0.079 0.123	Just perceptible.	30 35 40	44.01 51.34 58.68	4.429 6.027 7.873	High wind.
6 7 8	8.8 10.25 11.75	0.177 0.241 0.315	wind.	45 50 55	66.01 73.35 80.7	9.963	Very high storm.
9 10 12	13.2 14.67 17.6	0.400 0.492 0.708		60 66 70	88.02 95.4 102.5	17.71 20.85 24.1	Great Storm.
14 15	20.5 22.00	0.964	gaie.	75 80 100	117.36		Hurricane.
16	23.45	1.25		100	146.67	49.2	Immense hurri- cane.

The pressures per square foot in the above table correspond to the formula  $P=0.0057^{\circ}$ , in which V is the velocity in miles per hour.  $Eng^{ig}$  News, Feb. 9, 1893, says that the formula was never well established, and has floated chiefly on Smeaton's name and for lack of a better. It was put forward only for surfaces for use in windmil practice. The trend of modern evidence is that it is approximately correct only for such surfaces, and that for large solid bodies it often gives greatly too large results. Observations by others are thus compared with Smeaton's formula:

Old Smeaton formula	P =	$.005 V^2$
As determined by Prof. Martin		
" Whipple and Dines		

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At 60 miles per hour these formulas give for the pressure per square foot, At the order to the control of the pressure varying by all of them as the square of the velocity. Lieut. Crosby's experiments  $(Eug\ g, June\ 18, 1890)$ , claiming to prove that P = fV instead of  $P = fV^2$ , are discredited. A. R. Wolff (The Windmill as a Prine Mover, p. 9) gives as the theoretical

pressure per sq. ft. of surface,  $P = \frac{dQv}{a}$ , in which d = density of air in pounds

per cu. ft. =  $\frac{.018743(p+P)}{4}$ ; p being the barometric pressure per square

foot at any level, and temperature of 32° F., t any absolute temperature, Q = volume of air carried along per square foot in one second, v = velocityof the wind in feet per sec., g=32.16. Since Q=v cu. ft. per sec.,  $P=\frac{dv^2}{g}$ . Multiplying this by a coefficient 0.00 feet. Multiplying this by a coefficient 0.93 found by experiment, and substituting

the above value of d, he obtains  $P = \frac{0.017431 \times p}{t \times 32.16 - .018743}$ , and when p

= 2116.5 lbs. per sq ft. or average atmospheric pressure at the sea-level, 36.8929  $P = \frac{1}{t \times 32.16} - 0.18743$ -, an expression in which the pressure is shown to vary

with the temperature; and he gives a table showing the relation between velocity and pressure for temperatures from 0° to 100° F., and velocities from 1 to 80 miles per hour. For a temperature of 45° F the pressures agree with those in Smeaton's table, for 0° F, they are about 10 per cent greater and for 100° 10 per cent less. Prof. H. Allen Hazen, Eng'g News, July 5, 1890, says that experiments with whirling arms, by exposing plates to direct wind, and on locomotives with velocities running up to 40 miles per hour, what, and on obcomotive with velocities framing at 0.50 m/m/s per normal have invariably shown the resistance to vary with  $V^2$ . In the formula  $P = .0055V^2$ , in which P = pressure in pounds, S = surface in square feet, V = velocity in miles per hour, the doubtful question is that regarding the accuracy of the first two factors in the second member of this equation. The first factor has been variously determined from .003 to .005 [it has been determined as low as .0014—Ed. Eng'g News].

The second factor has been found in some experiments with very short

whirling arms and low velocities to vary with the perimeter of the plate, but this entirely disappears with longer arms or straight line motion, and the only question now to be determined is the value of the coefficient. Per-

haps some of the best experiments for determining this value were tried in France in 1886 by carrying flat boards on trains. The resulting formula in this case was, for 44.5 miles per hour,  $p=.00535\,\mathrm{S}^{72}$ . Mr. Crosby's whirling experiments were made with an arm 5.5 ft. long. It is certain that most serious effects from centrifugal action would be set up by using such a short arm, and nothing satisfactory can be learned with

arms less than 20 or 30 ft. long at velocities above 5 miles per hour,

Prof. Kernot, of Melbourne (Engineering Record, Feb. 20, 1894), states that experiments at the Forth Bridge showed that the average pressure on surfaces as large as railway carriages, houses, or bridges never exceeded two thirds of that upon small surfaces of one or two square feet, such as have been used at observatories, and also that an inertia effect, which is frequently endeded, may cause some forms of anemometer to give false results enormously exceeding the correct indication. Experiments of Mr. O. T. enormously exceeding the correct indication. Experiments of Mr. O. T. Crosby showed that the pressure varied directly as the velocity, whereas all the early investigators, from the time of Smeaton onwards, made it vary as the square of the velo ity. Experiments made by Prof. Kernot at speeds varying from 2 to 15 miles per hour agreed with the earlier authorities, and tended to negative Crosby's results. The pressure upon one stabled of a cube, or of a block proportioned like an ordinary carriage, was found to be .9 of that upon a thin plate of the same area. The same result was obtained for a square tower. A square pyramid, whose height was three times its base, experienced, 8 of the pressure upon a thin plate equal to one of its sides, but if an angle was turned to the wind the pressure was increased by fully 30%. A bridge consisting of two plate-girders connected by a deck at the top was A found to experience, 9 of the pressure on a thin plate equal in size to one drider, when the distance between the girders was equal to their depth, and this was increased by one fifth when the distance between the girders was double the depth. A lattice-work in which the area of the openings was 55% agoine the depth. A statice work in which the area of the openings was 35% of the whole area experienced a pressure of 8% of that upon a plate of the same area. The pressure upon cylinders and cones was proved to be equal to half that upon the diametral planes, and that upon an octagonal prism to be 20% greater than upon the circumscribing cylinder. A sphere was subject to a pressure of .36 of that upon a thin circular plate of equal diameter. A hemispherical cup gave the same result as the sphere; when its convexity A hemispherical cup gave the same result as the sphere; when its convexity was turned to the wind the pressure was 1.15 of that on a flat plate of equal diameter. When a plane surface parallel to the direction of the wind was brought nearly into contact with a cylinder or sphere, the pressure on the latter bodies was augmented by about 20%, owing to the lateral escape of the air being checked. Thus it is possible for the security of a tower or chimney to be impaired by the erection of a building nearly inching it on one side.

Pressures of Wind Registered in Storms,—Mr. Frizell has

examined the published records of Greenwich Observatory from 1849 to 1869, and reports that the highest pressure of wind he finds recorded is 41 lbs. per sq. ft., and there are numerous instances in which it was between 30 and do lbs. per sq. ft. Prof. Henry says that on Mount Washington, N. H., a velocity of 135 miles per hour has been observed, and at New York City 60 miles an hour, and that the highest winds observed in 1870 were of 72 and 63

miles per hour, respectively.

Lieut. Dunwoody, U. S. A., says, in substance, that the New England coast is exposed to storms which produce a pressure of 50 lbs. per sq. ft. Engineering News, Aug. 20, 1880.

### WINDMILLS.

Power and Efficiency of Windmills.—Rankine, S. E., p. 215. gives the following: Let  $Q = \text{volume of air which acts on the sail, or part of a sail, in cubic feet per second, <math>v = \text{velocity of the wind in feet per}$ second, s = sectional area of the cylinder, or annular cylinder of wind, through which the sail, or part of the sail, sweeps in one revolution, c = acoefficient to be found by experience; then Q = cvs. Rankine, from experimental data given by Smeaton, and taking c to include an allowance for friction, gives for a wheel with four sails, proportioned in the best manner, rection, gives for a wheel with four sails, proportioned in the best manner, ce 0.75. Let A = weather angle of the sail at any distance from the axis, i.e., the angle the portion of the sail considered makes with its plane of revolution. This angle gradually diminishes from the inner end of the sail to the tip; u = the velocity of the same portion of the sail, and E = the efficiency. The efficiency is the ratio of the useful work performed to whole energy of the stream of wind acting on the surface s of the wheel, which energy is  $\frac{D_{SU}^2}{2g}$ , D being the weight of a cubic foot of air. Rankine's formula

for efficiency is

$$E = \frac{Ru}{\frac{Dsv^3}{2a}} = c\left\{\frac{u}{v}\sin 2A - \frac{u^2}{v^2}\left(1 - \cos 2A + f\right) - f\right\},\,$$

in which c=0.75 and f is a coefficient of friction found from Smeaton's data = 0.016. Rankine gives the following from Smeaton's data:

$$A = \text{weather-angle}.$$
 = 7° 13° 19°  $V + v = \text{ratio}$  of speed of greatest efficiency, for a given weather-angle, to that of the wind. = 2.63 1.86 1.41  $E = \text{efficiency}.$  = 0.24 0.29 0.31

Rankine gives the following as the best values for the angle of weather at different distances from the axis:

But Wolff (p. 125) shows that Smeaton did not term these the best angles, but simply says they "answer as well as any," possibly any that were in existence in his time. Wolff says that they "cannot in the nature of things be the most desirable angles," Mathematical considerations, he says, conclusing the says that the said of the said of the says that the said of the says that the said of be the most desirable angles." Mathematicar considerations, he says, con-clusively show that the angle of impulse depends on the relative velocity of each point of the sail and the wind, the angle growing larger as the ratio be-comes greater. Smeaton's angles do not fulfil this condition. Wolff develops a theoretical formula for the best angle of weather, and from it calculates a table for different relative velocities of the blades (at a distance of one seventh of the total length from the centre of the shaft) and the wind, from which the following is condensed:

Ratio of the	Distance	e from th	ne axis of	the who	eel in sev	enths of	radius.
Speed of Blade at 1/7 of Radius to Velocity of	1	2	3	4	5	6	7
Wind.			Best an	gles of w	eather.		
0.10 0.15 0.20 0.25	42° 9′ 40 44 39 21 37 59	39° 21′ 36° 39 34° 6 36° 43	36° 39′ 32 53 29 31 26 34	34° 6′ 29 31 25 40 22 30	31° 43′ 26 34 22 30 19 20	29° 31′ 24 0 19 54 16 51	27° 30′ 21 48 17 46 14 52
0.30 0.35 0.40 0.45 0.50	36 39 35 21 34 6 32 53 31 43	29 31 27 30 25 40 24 0 22 30	24 0 21 48 19 54 18 16 16 51	19 54 17 46 16 0 14 32 13 17	16 51 14 52 13 17 11 59 10 54	14 32 12 44 11 19 10 10 9 13	12 44 11 6 9 50 8 48 7 58

The effective power of a windmill, as Smeaton ascertained by experiment, varies as s, the sectional area of the acting stream of wind; that is, for simi-

lar wheels, as the squares of the radii.

The value 0.75, assigned to the multiplier c in the formula Q = cvs, is founded on the fact, ascertained by Smeaton, that the effective power of a windmill with sails of the best form, and about 15½ ft. radius, with a breeze of 13 ft. per second, is about 1 horse-power. In the computations founded on that fact, the mean angle of weather is made = 13°. The efficiency of this wheel, according to the formula and table given, is 0.29, at its best speed, when the tips of the sails move at a velocity of 2.6 times that of the wind.

Merivale (Notes and Formulæ for Mining Students), using Smeaton's co-

efficient of efficiency, 0.29, gives the following:

U = units of work in foot-lbs. per sec.;

W = weight, in pounds, of the cylinder of wind passing the sails each second, the diameter of the cylinder being equal to the diameter of the sails;

V = velocity of wind in feet per second;

H.P. = effective horse-power: 0.29 W V2  $WV^2$ 

 $\frac{64}{64}$ ; H.P. =  $\frac{6.2077}{64 \times 550}$ .

A. R. Wolff, in an article in the American Hagineer, gives the following (see also his treatise on Windmills):

Let c =velocity of wind in feet per second;

n = number of revolutions of the windmill per minute;  $b_0, b_1, b_2, b_3$  be the breadth of the sail or blade at distances  $l_0, l_1, l_2$ , l<sub>3</sub>, and l, respectively, from the axis of the shaft;

 $l_0=$  distance from axis of shaft to beginning of sail or blade proper; l= distance from axis of shaft to extremity of sail proper;  $v_0, v_1, v_2, v_3, v_3 =$  the velocity of the sail in feet per second at dis-

tances  $l_0$ ,  $l_1$ ,  $l_2$ , l, respectively, from the axis of the shaft;

 $a_0, a_1, a_2, a_3, a_2$  = the angles of impulse for maximum effect at distances  $l_0$ ,  $l_1$ ,  $l_2$ ,  $l_3$ , l respectively from the axis of the shaft; a = the angle of impulse when the sails or blocks are plane surfaces,

so that there is but one angle to be considered;

N = number of sails or blades of windmill;

K = .93.d = density of wind (weight of a cubic foot of air at average temperature and barometric pressure where mill is erected);

W = weight of wind wheel in pounds;

f = coefficient of friction of shaft and bearings;  $\dot{D} = \text{diameter of bearing of windmill in feet.}$ 

The effective horse-power of a windmill with plane sails will equal

$$\begin{split} \frac{(l-l_0)Kc^2dN}{550g} \times \text{mean of} \left(v_0(\sin\alpha - \frac{v_0}{c}\cos\alpha)b_0\cos\alpha \right. \\ v_x\left(\sin\alpha - \frac{v_x}{c}\cos\alpha\right)b_x\cos\alpha\right) - \frac{fW \times .05236nD}{550}. \end{split}$$

The effective horse-power of a windmill of shape of sail for maximum effect equals

$$\frac{N(l-l_0)Kdc^3}{2200g} \times \text{mean of} \left(\frac{2\sin^2 a_0 - 1}{\sin^2 a_0}b_0, \quad \frac{2\sin^2 a_1 - 1}{\sin^2 a_1}b_1 \dots \right.$$

$$\left. \quad \cdot \quad \cdot \quad \frac{2\sin^2 a_x - 1}{\sin_2 a_x}b_x \right) - \frac{fW \times .05236nD}{550}.$$

The mean value of quantities in brackets is to be found according to Suppson's rule. Dividing l into 7 parts, finding the angles and breadths corresponding to these divisions by substituting them in quantities within brackets will be found satisfactory. Comparison of these formules with the only fairly reliable experiments in windmills (Coulomb's) showed a close agreement of results.

Approximate formulæ of simpler form for windmills of present construc-

Approximate formulæ of simpler form for windmills of present construction can be based upon the above, substituting actual average values for a, c, d, and e, but since improvement in the present angles is possible, it is better to give the formulæ in their general and accurate form. Wolff gives the following table based on the practice of an American manufacturer. Since its preparation, he says, over 1500 windmills have been sold on its guaranty (1888), and in all cases the results obtained did not vary sufficiently from those presented to cause any complaint. The actual results obtained are in close agreement with those obtained by theoretical analysis of the impulse of wind upon windmill blades.

Capacity of the Windmill.

Designation of Mill.	of Wind, in per hour.	ons of Wheel minute.	Gallor	ns of Wa	ater ra n Elev	ised per ation of	r Minu f—	te to	ralent Actual Use- Horse-power de- oped.	No. of Hours during which sult will be ob-
Designat	Velocity miles	Revolutions per mi	25 feet.	50 feet.	75 feet.	i00 feet.	150 feet.	200 feet.	Equivalent ful Horse veloped.	Average per Day this Res tained.
wheel 8½ ft. 10 " 12 " 14 " 16 " 18 " 20 " 25 "	16 16 16 16 16 16 16	70 to 75 60 to 65 55 to 60 50 to 55 45 to 50 40 to 45 85 to 40 30 to 35	64 600 97.682 124.950	52.165 63.750		4.750 8.485 11.246 16.150 24.421 31.248 49.725	5.680 7.807 9.771 17.485 19.284	15.938	0.04 0.12 0.21 0.28 0.41 0.61 0.78 1.34	888888888888888888888888888888888888888

These windmills are made in regular sizes, as high as sixty feet diameter of wheel; but the experience with the larger class of mills is too limited to enable the presentation of precise data as to their performance. If the wind can be relied upon in exceptional localities to average a higher velocity for eight hours a day than that stated in the above table, the performance or horse-power of the mill will be increased, and can be obtained by multiplying the figures in the table by the ratio of the cube of the higher average velocity of wind to the cube of the velocity above recorded.

He also gives the following table showing the economy of the windmill. All the items of expense, including both interest and repairs, are reduced to the hour by dividing the costs per annum by 365 × 8 = 2920; the interest.

the hour by dividing the costs per annum by  $365 \times 8 = 2920$ ; the interest,

etc., for the twenty-four hours being charged to the eight hours of actual work. By multiplying the figures in the 5th column by 584, the first cost of the windmill, in dollars, is obtained.

Economy of the Windmill.									
	aised	tual Useful developed.	of uring ity	Expense of Developed.	Actual U	sefu , per	l Po	wer	per
Designation of Mill,	of Water raised		e Number of s per Day duri t this Quantity e raised.	Cost (First including of Wind-Pump. and r. 5% per n).	Repairs and preciation (5% First Cost per num).	Attendance.			e per Horse
	Gallons o 25 ft.	Equivalent Ac Horse-power	Average Hours which will be	For Inter First C Cost, ii Cost of mill, P Tower,	For Repairs of Pirst Cos annum).	For Att	For Oil.	Total.	Expense power, hour.
81/2 ft. wheel	370	0.04	8	0.25	0.25	0.06	0.04	0.60	15.0
10 " "	1151	0.12	8	0.30	0.30		0.04		5.8
12 " "	2036	0.21	8	0.36	0.36		0.04		3.9 5.8 5.9
14 " "	2708	0.28	8	0.75	0.75		0.07	1.68	5.8
	3876	0.41	8	1.15	1.15				5.9
18 " " "	5861	0 61	8	1.35	1.35		0.07		
25 " "	7497 12743	$0.79 \\ 1.34$	8888888	1.70 2.05	1.70 2.05	0.06	0.10	4.00	4.5 3.2
20	12145	1.54	0	2,05	2.05	0.00	0.10	[4.20]	5.2

Lieut. I. N. Lewis (Eng'q Maq., Dec. 1894) gives a table of results of experiments with wooden wheels, from which the following is taken:

		Velo	city of V	Vind, mile	s per hou	r.	
Diameter of wheel, Feet.	8	10	12 .	16	20	25	30
1 600.		Actua	l Useful I	Horse-pow	er develop	ed.	
12 16 20 25 30	0 1/8 3/4 11/4 2	1/8 3/8 11/4 13/4 3	1/4 3/4 2 3 4	1/2 11/2 8 41/4 51/2	1 214 4 6 7	13/4 31/4 51/2 8 9	2 4 7 10 12

The wheels were tested by driving a differentially wound dynamo. "useful horse-power" was measured by a voltmeter and ammeter, allowing 500 watts per horse-power. Details of the experiments, including the means used for obtaining the velocity of the wind, are not given. The results are so far in excess of the capacity claimed by responsible manufacturers that they should not be given credence until established by further experiments.

A recent article on windmills in the Iron Age contains the following: According to observations of the United States Signal Service, the average velocity of the wind within the range of its record is 9 miles per hour for the year along the North Atlantic border and Northwestern States, 10 miles on the plains of the West, and 6 miles in the Gulf States.

The horse-powers of windmills of the best construction are proportional to the squares of their diameters and inversely as their velocities; for example, a 10-ft, mill in a 16-mile breeze will develop 0.15 horse-power at 65 revolutions per minute; and with the same breeze

A 20-ft. mill, 40 revolutions, 1 horse-power.

A 25-ft. mill, 35 revolutions, 134 horse-power. A 30-ft. mill, 28 revolutions, 3½ horse-power. A 40-ft. mill, 22 revolutions, 7½ horse-power.

A 50-ft, mill, 18 revolutions, 12 horse-power.

The increase in power from increase in velocity of the wind is equal to the square of its proportional velocity; as for example, the 25-ft. mill rated above for a 16-mile wind will, with a 32-mile wind, have its horse-power increased to 4 × 134 = 7 horse-power, a 40-ft. mill in a 32-mile wind will run up to 30 horse-power, and a 50-ft. mill to 48 horse-power, with a small deduction for increased friction of air on the wheel and the machinery.

The modern mill of medium and large size will run and produce work in a

4-mile breeze, becoming very efficient in an 8 to 16-mile breeze, and increase its power with safety to the running-gear up to a gale of 45 miles per hour. Prof. Thurston, in an article on modern uses of the windmill, Engineer-

ing Magazine, Feb. 1893, says: The best mills cost from about \$600 for the 10-ft, wheel of ½ horse-power to \$1200 for the 25-ft, wheel of 1½ horse-power or less. In the estimates a working-day of 8 hours is assumed; but the machine, when used for punping, its most common application, may actually do its work 24 hours a day for days, weeks, and even months together, whenever the wind is "stiff" enough to turn it. It costs, for work done in situations in which its irregularity of action is no objection, only one half or one third as much as steam, hot-air, and gas engines of similar power. At Faversham, it is said, a 15-horse-power mill raises 2,000,000 gallons a month from a depth of 100 ft., saving 10 tons of coal a mouth, which would otherwise be expended in doing the work by steam.

Electric storage and lighting from the power of a windmill has been tested on a large scale for several years by Charles F. Brush, at Cleveland, Ohio. In 1887 he erected on the grounds of his dwelling a windmill 56 ft. in diameter, that operates with ordinary wind a dynamo at 500 revolutions per minute, with an output of 12,000 ampères—16 electric horse-power—charging a storage system that gives a constant lighting capacity of 100 16 to 20 candle-power lamps. The current from the dynamo is automatically regulated to commence charging at 330 revolutions and 70 volts, and cutting the circuit at 75 volts. Thus, by its 24 hours' work, the storage system of 408 cells in 12 parallel series, each cell having a capacity of 100 ampère hours, is best in constant readiness for all the requirements of the establishment it Electric storage and lighting from the power of a windmill has been tested kept in constant readiness for all the requirements of the establishment, it being fitted up with 350 incandescent lamps, about 100 being in use each evening. The plant runs at a mere nominal expense for oil, repairs, and at-(For a fuller description of this plant, and of a more recent one at Marblehead Neck, Mass., see Lieut. Lewis's paper in Engineering Magazine, Dec. 1894, p. 475.)

## COMPRESSED AIR.

Heating of Air by Compression. -Kimball, in his treatise on Physical Properties of Gases, says: When air is compressed, all the work which is done in the compression is converted into heat, and shows itself in the rise in temperature of the compressed gas. As the gas becomes hotter it is compressed with more difficulty; so in practice many devices are employed to carry off the heat as fast as it is developed, and keep the temperature down, But it is not possible in any way to totally remove this difficulty. But, it may be objected, if all the work done in compression is converted into heat, and if this heat is got rid of as soon as possible, then the work may be virtually thrown away, and the compressed air can have no more energy than it had before compression. It is true that the compressed gas has no more energy than the gas had before compression, if its temperature is no higher, but the advantage of the compression lies in bringing its energy into more available form.

The total energy of the compressed and uncompressed gas is the same at the same temperature, but the available energy is much greater in the former. The rise in temperature due to compression is so great that if a mass of air at 32° F. is compressed to one fourth its original volume, its temperature

will be raised 376° F., if no heat is allowed to escape.

When the compressed air is used in driving a rock-drill, or any other piece

of machinery, it gives up energy equal in amount to the work it does, and its temperature is accordingly greatly reduced.

Causes of Loss of Energy in Use of Compressed Air. (Zahner, on Transmission of Power by Compressed Air.)—1. The compression of air always develops heat, and as the compressed air always cools down to the temperature of the surrounding atmosphere before it is used, the mechanical equivalent of this dissipated heat is work lost.

2. The heat of compression increases the volume of the air, and hence it is necessary to carry the air to a higher pressure in the compressor in order that we may finally have a given volume of air at a given pressure, and at the temperature of the surrounding atmosphere. The work spent in effect-

ing this excess of pressure is work lost.

500 ATR.

3. The great cold which results when air expands against a resistance forbids expansive working, which is equivalent to saying, forbids the reali-

formas expansive working, which is equivalent to saying, formas the realization of a high degree of efficiency in the use of compressed air.

4. Friction of the air in the pipes, leakage, dead-spaces, the resistance of fered by the valves, insufficiency of valve-ar-a, inferior workmanship, and slovenly attendance, are all more or less serious causes of loss of power. The first cause of loss of work, namely, the heat developed by compression, is entirely unavoidable. The whole of the mechanical energy which the compressor-piston spends upon the air is converted into heat. This heat is dissipated by conduction and radiation, and its mechanical equivalent is work lost. The compressed air, having again reached thermal equilibrium with the surrounding atmosphere, expands and does work in virtue of its intrinsic energy.

The intrinsic energy of a fluid is the energy which it is capable of exerting against a piston in changing from a given state as to temperature and volume, to a total privation of heat and indefinite expansion.

Volumes, Mean Pressures per Stroke, Temperatures, etc., in the Operation of Air-compression from 1 Atmosphere and 60° Fahr. (F. Richards, Am. Mach., March 30, 1893.)

Gauge-pressure.	Atmospheres.	Volume with Air at Constant Temp.	Volume with Air not cooled.	Mean Pressure per Stroke; Air Con- stant Temp.	Mean Pressure per Stroke; Air not cooled.	Temp. of Air; not	Gauge-pressure,	Atmospheres.	Volume with Air at Constant Temp.	Volume with Air not cooled.	Mean Pressure per Stroke; Air Con- stant Temp.	Mean Pressure per Stroke; Air not cooled.	Temp. of Air; not cooled.
1	2	3	4	5	6	7	1	2	3	4	5	6	7
3 4 5 10 15 20 25 30 35 40 45 50 55 60	1,272 1,34 1,68 2,02 2,36 2,7 3,04 3,381 4,061 4,401 4,741 5,081	1 .9363 .8803 .8805 .7861 .7462 .5952 .495 .4237 .3703 3289 .2957 .2687 .2462 .2272 .2109 .1968	1 .95 .91 .876 .84 .81 .69 .606 .543 .494 .4588 .42 .898 .37 .35 .331 .3144 .301	16.34 17.92 19.32 20.57 21.69	17.01 19.4 21.6 23.66 25.59 27.39 29.11 80.75	60° 71 80.4 88.9 98 106 145 178 207 234 252 281 302 321 339 357 375	80 85 90 95 100 105 110 125 130 135 140 145 150 170 180	6.442 6.782 7.122 7.462 7.802 8.142 8.483 9.163 9.503 9.843 10.183 10.523 10.864 11.204 11.88 12.56	.1404 .134 .1281 .1228 .1178 .1133 .1091 .1052	.267 2566 248 .24 .282 .2254 .2189 .2073 .2020 .1969 .1922 .1878 .1878 .1792 .1792 .1595	27.38 28.16 28.89 29.57 30.21 30.81 31.39 31.98 32.54 33.07 34.05 34.57 34.57 35.09 35.48 36.29 37.2	36.64 37.94 39.18 40.4 41.6 42.78 43.91 44.98 46.04 47.06 48.1 49.1 50.02 51.89 53.65 55.39 57.01	432 447 459 472 485 496 507 518 529 540 550 560 570 589 607 624
70 75	5.423 5.762 6.102	.1844 .1735 .1639	.288 .276	25.67 26.55		405 420	190 200	13.92	.0718	.154	38.68 39.42	58.57 60.14	640 657 672

Column 3 gives the volume of air after compression to the given pressure and after it is cooled to its initial temperature. After compression air loses its heat very rapidly, and this column may be taken to represent the volume of air after compression available for the purpose for which the air has been compressed.

Column 4 gives the volume of air more nearly as the compressor has to deal with it. In any compressor the air will lose some of its heat during compression. The slower the compressor runs the cooler the air and the

smaller the volume.

Column 5 gives the mean effective resistance to be overcome by the aircylinder piston in the stroke of compression, supposing the air to remain constantly at its initial temperature. Of course it will not so remain, but this column is the ideal to be kept in view in economical air-compression.

Column 6 gives the mean effective resistance to be overcome by the piscommin gries the mean elective resistance to go overcoine by the pis-ton, supposing that there is no cooling of the air. The actual mean effec-tive pressure will be somewhat less than as given in this column; but for computing the actual power required for operating air-compressor cylinders the figures in this column may be taken and a certain percentage added say 10 per cent-and the result will represent very closely the power required by the compressor.

The mean pressures given being for compression from one atmosphere

upward, they will not be correct for computations in compound compression

in water initial pressure or for any other initial pressure caused by Heating in Loss Due to Excess of Pressure caused by Heating in the Compression-cylinder,—If the air during compression were kept at a constant temperature, the compression-curve of an indicator-diagram taken from the cylinder would be an isothermal curve, and would follow the law of Boyle and Marriotte, pv = a constant, or  $p_1v_1 = p_0v_0$ , or

 $p_1 = p_0 \frac{v_0}{v_1}$ ,  $p_0$  and  $v_0$  being the pressure and volume at the beginning of

compression, and  $p_1v_1$  the pressure and volume at the end, or at any intermediate point. But as the air is heated during compression the pressure increases faster than the volume decreases, causing the work required for any given pressure to be increased. If none of the heat were abstracted by radiation or by injection of water, the curve of the diagram would be an

adiabatic curve, with the equation  $p_1 = p_0 \left(\frac{v_0}{v_1}\right)^{1.405}$ . Cooling the air dur-

ing compression, or compressing it in two cylinders, called compounding, and cooling the air as it passes from one cylinder to the other, reduces the exponent of this equation, and reduces the quantity of work necessary to effect a given compression. F. T. Gause (Am, Mach., Oct. 20, 1892), describing the operations of the Popp air-compressions in Paris, says: The greatest saving realized in compressing in a single cylinder was 33 per cent of that theoretically possible. In cards taken from the 2000 H.P. compound compressor at Quai De La Gare. Paris, the saving realized is 85 per cent of the theoretical amount. Of this amount only 8 per cent is due to cooling during compression, so that the increase of economy in the compound compressor is mainly due to cooling the air between the two stages of compression. A compression-curve with exponent 1.25 is the best result that was obtained for compression in a single cylinder and cooling with a very fine spray. The curve with exponent 1.15 is that which must be realized in a single cylinder to equal the present economy of the compound compressor at Quai De La Gare.

Horse-power required compress one cubic foot of Free Air per minute to a given Pressure with no cooling of the air during the compression; also the horse-power required, supposing the air to be maintained at constant temperature during the compression. (Richards.)

to Horse - power required deliver one cubic foot of Air per minute at a given Pressure with no cooling of the air during the compression; also the horse-power required, supposing the air to be maintained at constant temperature during the compression. (Richards.)

Gauge-	Air not	Air constant	Gauge-	Air not	Air constant
pressure	cooled.	Temperature.	pressure.	cooled.	Temperature.
100	.22183	.14578	100	1.7317	1.13801
90	.20896	.13954	90	1,4883	.99387
80	.19521	.13251	80	1.25779	.8538
70	.17989	.12606	70	1.03683	.72651
60	.164	.11558	60	.83344	.58729
50	.14607	.10565	50	.64291	.465
40	.12433	.093667	40	.46271	.34859
30	.10346	.079219	30	.31456	.24086
20	.076808	.061188	20	.181279	.14441
10	.044108	.036944	10	.074106	.06069
5	.024007	.020848	5	.032172	.027938

In computing the above table an allowance of 10 per cent has been made for friction of the compressor.

Table for Adiabatic Compression or Expansion of Air.

11

Ratio of Greater Cless to Greater Cless to Cless (Expansion.)		(110c. 11st. 11.1., Jan. 1001, p. 120.)									
Greater to Less to Greater to Less. (Expansion.)  1.2 (S33 1.054 948 1.38 1.375 1.46 1.56 1.186 1.396 1.188 1.56 1.186 1.188 1.58 1.587 1.396 1.189 1.597 1.396 1.189 1.597 1.396 1.189 1.597 1.396 1.189 1.597 1.396 1.189 1.597 1.396 1.189 1.396 1.189 1.396 1.189 1.396 1.189 1.396 1.189 1.396 1.189 1.396 1.189 1.396 1.	Absolute Pressure,		Absolute T	'emperature.	Volume.						
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	Greater to Less. (Expan-	Less to Greater, (Compres-	Greater to Less. (Expan-	Less to Greater. (Compres-	Greater to Less. (Compres-	Less to Greater. (Expan-					
7.0 .143 1.705 .509 3.981 .251 8.0 .125 1.828 5.47 4.877 .228 9.0 .111 1.891 .529 4.759 .210 10.0 .100 1.950 .513 5.129 .195	1.4 1.6 1.8 2.0 2.2 2.4 2.6 2.8 3.0 3.4 3.8 4.0 4.2 4.4 4.6 4.8 5.0 6.0 7.0 8.0	714 625 556 5500 454 4417 385 385 357 833 312 294 278 258 2500 167 143 125 1111	1.102 1.146 1.186 1.222 1.257 1.259 1.319 1.348 1.375 1.401 1.450 1.450 1.473 1.495 1.516 1.557 1.576 1.557 1.595 1.838	. 907 . 853 . 843 . 818 . 796 . 776 . 776 . 778 . 742 . 714 . 701 . 690 . 669 . 669 . 669 . 669 . 651 . 692 . 697 . 595 . 697 . 595 . 695 . 695	1.270 1.396 1.518 1.636 1.750 1.862 1.862 1.862 1.862 2.077 2.182 2.384 2.483 2.580 2.676 2.770 2.863 2.955 3.046 3.135 3.569 4.877 4.759	7.88 7.16 6.59 6.611 6.71 5.71 5.87 5.97 4.81 4.58 4.49 4.03 3.88 3.84 3.81 3.89 3.88 3.89 3.89 3.89 3.89 3.89 3.89					

Mean Effective Pressures for the Compression Part only of the Stroke when compressing and delivering Air from one Atmosphere to given Gauge-pressure in a Single Cylinder. (F. Richards, Am. Mach., Dec. 14, 1893.)

Gauge- pressure.	Adiabatic Compression	Isothermal Compression.	Gauge- pressure.	Adiabatic Compression.	Isothermal Compression.
1	.44	.43	45	13.95	12.62
2 3	.96	.95	50	15.05	13.48
3	1.41	1.4	55	15.98	14.3
4	1.86	1.84	60	16.89	15.05
4 5	2.26	2.22	65	17.88	15.76
10	4.26	4.14	70	18.74	16.43
15	5.99	5.77	65 70 75 80 85	19.54	17.09
20	7.58	7.2	80	20.5	17.7
25	9.05	8.49	85	21.22	18.3
25 30	10.39	9.66	90	22	18.87
35	11.59	10.72	95	22.77	19.4
40	12.8	11.7	100	23.43	19.92

The mean effective pressure for compression only is always lower than the mean effective pressure for the whole work

### Mean and Terminal Pressures of Compressed Air used Expansively for Gauge-pressures from 60 to 100 lbs. (Frank Richards, Am. Mach., April 13, 1893.)

Initial 60. 70. 80. 90. 100. Pressure. Point of Cut-off. oressure. ermina ressure, Terminal ressure ressure Termina oressure ressure. **Fermina** oressure. Termina oressure Mean Mean Air-Mean Mean .25 13.49 23.6 10.65 28.74 12.07 33.89 39 04 14.91 44.19 1.33 28.9 13.77 .6 2.44 46.46 4.27 53.32 34.75 40.61 6.11 .96 1/3 .35 32.13 38.41 3.09 41.69 5.22 50.98 35 57.26 9.48 2.33 33.66  $\frac{40.15}{42.63}$  $\frac{4.38}{6.36}$ 46.64 6.66 53.13 8.95 59.62 11.23 3/8 .40 35.85 49.41 7.88 3.85 56.2 11.39 62.9813.89 37.93 5.64 44.99 8.39 52.05 11.14 59.11 13.88 66.16 16.64 .45 41.75 15.86 64 45 10.71 49.31 12.61 56.9 19.11 72.02 22.36 45.14 13.26 53.16 61.18 20 81 69.19 24.56 77.21 28.3385.82 .60 5/8 2/3 .70 .75 50.75 21:53 59.51 26.4 68.2831.2777.05 36,14 41.01 69.76 34.01 51.92 23.69 60.84 28.8578.6939,16 87.61 44.32 33.03 71.99 73.57 38,68 81.14 82.9 53.67 27.9462.8344.33 90.32 49.97 36.44 48.54 54.93 30.39 64 25 42.49 92.22 54.59 66.05 75.59 48.35 56.52 35.01 41.68 85.12 55.02 94.66 61.69 .80 57.79 59.15 59.46 39.78 67.5 69.03 77.2 78.92 86.91 47.08 54.3861.69 96.61 68,99 .90 .90 72. 47.14 55.43 63.81 88.81 98.7 80.28

79 31 The pressures in the table are all gauge-pressures except those in italics, which are absolute pressures (above a vacuum).

89.24 75.52

66.89

99.17

87.82

69.38 58.27

49.65

# Straight-line Air-compressors, Ingersoll-Sergeant Rock-drill Co.

Diameter Steam- cylinder, inches.	Diameter of Air- cylinder, inches.	Length of Stroke, inches.	No. of Revolu- tions per minute.	Piston Speed in feet per minute.	Cubic Feet Free Air per minute (Theo- retical).	Horse- power of Boiler required.
4 5 6 7 8 9 10	41/4 51/4 61/4 71/4 81/4 91/4 101/4 121/4	10 10 12 12 12 12 12 12 14 14	175 175 160 160 160 160 160 155 155	291 291 320 320 320 320 320 361 361	28 42 66 91 117 148 207 295	6 8 10 12 15 20 30 40
14 16 18 20 22 24	14 <sup>1</sup> / <sub>4</sub> 16 <sup>1</sup> / <sub>4</sub> 18 <sup>1</sup> / <sub>4</sub> 20 <sup>1</sup> / <sub>4</sub> 22 <sup>1</sup> / <sub>4</sub> 24 <sup>1</sup> / <sub>4</sub>	18 18 24 24 24 30 30	120 120 94 94 75 75	360 360 376 376 375 375	398 518 683 840 1011 1202	55 70 100 130 155 200

The same sizes are made to be driven by belt or gearing.

Compressors at High Altitudes .- Cubic feet of compressed air delivered by air-compressors at high altitudes, expressed as a percentage of the air delivered at the sea-level.

Altitude above Sea- level, feet.	0	1000	2000	3000	4000	5000	6000	7000	8000	9000	10000
Air delivered, per cent	100	97	94	91	89	86	84	81	78	76	74

### Standard Air-compressors driven by Steam.

(Norwalk Iron Works Co.)

In the following list the large air-cylinder gives the capacity of the machine. For actual capacity, allowance of 10 per cent may be made for contingencies. The small piston only encounters the pressure of the final compression.

Diameter of Air- cylinder.	Length of Stroke.	Diameter of Com- pressing Cylinder.	Diameter of Steam- cylinder.	Revolutions or Double Strokes per minute.	Theoretical Capacity, cubic feet per minute, Free Air.	Steam-pipe.	Exhaust- pipe.	Air-pipe.	Water-pipe.	Horse- power.
8 10 14 20 26 32	10 12 16 24 30 36	5	8	200 190 150 110 90 80	116 207 427 960 1659	2	2½ 3 4 6 8 10	2 21/2	1/2 3/4	15 28 55 125 215 350
10	18	634	14	150	497	2½ 3	4	4/2	194	28 55
20	24	912 1316 1716 2116	10 14 20 24 30	110	960	5	6	5 6 8	11/4	125
26	30	1713	24	.90	1659	6	8	6	11/4	215
32	36	211/2	30	80	2686	7	10	8	11/2	350

# Double-compound Compressors.

(Norwalk Iron Works Co)

	Length of Stroke.		Diamete	Revolu-	Capac'y		
Diameter Air- cylinder.		Com- pressing cylinder.	High- pressure Steam- cylinder,	Low- pressure Steam- cylinder.	Steam- pipe.	tions	cubic feet Free Air per minute.
10 12 14	12 12 16	5 5 014	71/2 71/2 10	12 12 16	2 2 21/	190 190 150	207 298 427
16 20 20	16 20	912 1312 1312	10 14 14	16 22 22	21/2 21/2 3 3 3	150 120 110	558 872 960
22 26 28 32	24 24 30 30 36	131/2 171/2 171/2 211/2	14 18 18 22	22 28 28 28 35	3 4½ 4½ 6	90 90 90 80	1160 1659 1924 2686

# Mountain or High-altitude Compressors.

(Norwalk Iron Works Co.)

							-	.,				
Air-		of ssing	jo .	ns nte.	At S	Sea- vel.		2000 eet.		8000 et.	At 10	0,000 et.
Diameter , cylinder	Length of Stroke.	Diameter of Compressing Cylinder.	Diameter Steam- cylinder	Revolutions per minute	Capacity. cubic feet.	Horse- power.	Capacity.	Horse- power.	Capacity.	Horse- power.	Capacity.	Horse- power.
12 16	12	7	10	190	298	35 70	280	34	244	32	214	30 60 94 124
16	16	91/2 131/2	14 18 20	150	558 872	70	524	68	462	64	405	60
20	20	131/2	18	120 110	1160	110 145	819 1090	107 140	722 960	100 132	634	94
22 26	24 30	131/2	20	90	1659	215	1560	207	1373	195	843 1200	184
20	1 00	1172	~1	1 00	1 1000	~10	11000	~01	11010	100	1200	104

The delivery and power of the compressors decrease as the height increases. As the capacity decreases in a greater ratio than the power necessary to compress, it follows that operations at a high allitude are more expensive than at sea-level. At 10,000 feet this extra expense amounts to over 20 per cent.

### Rand Drill Co.'s Air-compressors,

	Dimensions	s per	Theoretical Volume of Air delivered in cubic feet per minute, at Sea-level.								
Class.	of Air- cylinders in	of Air-		Comp	pressed	to a Ga	uge-pi	essure	of—		
	inches.	Revo	Free.	10 lbs.	20 lbs.	40 lbs.	60 lbs.	80 lbs.	100 lbs.		
_ (	10×16 { S*	100 100	145.44 290.88	86.56 173.12	61.61 123.23	39.08 78.17	28.62 57.24	22.57 45.15	18.64 37.28		
В	14×22 \ D	85 85	333.20 666.40	198.31 396.61	141.10 282.20	89.51 179.01	65.54 131.07	51.93 103.86	42.67 85.34		
[	16½ × 30 { S. D.	75 75 75	556.83 1113.66 662.68	331.39 662.79 394.39	235.89 471.79 280.73	299.28	109.57 219.15 130.40		71.36 142.72 84.92		
A and	18 × 30 { S	75 50	1325.36 872.66	788.78 519.36	561.46 369.69	356.17 234.51	260.81	205.72 135.46	169.84		
В	20×48 { S D 28×48 { S	50 40	1745.32 1368.34	1038.72 814.36	739.38 579.67	469.03 367.72	$\frac{343.45}{269.27}$	270.92 212.40	223.68 175.36		
. (	32 × 48 { D	40 40 40	2736.68 1787.22	1063.65	1159.34 757.12	480.29	538,54 351.70	277.42	229.05		
and B	32 × 60 \ S D	35	3574.44 1954.77 3909.55	2127.30 1163.37 2326.73	1514.24 828.10 1656.20		703.40 384.67 769.34	303.43	250.52		
Geared (	36 × 60 S	30 30	2120.61 4241.22	1262.07 2524.14	898.35 1796.70	572.07 1144.14	417.72 835.44	$329.16 \\ 658.32$	272.82		
-	8 × 12 10 × 14	120	83.78 139.95	49.86 83.27	35.49 59 29	22:51 37.62	16.49 27.50	13.00 21.72	10.74 17.94		
c	12 × 16, 14 × 22 16 × 24,	100 95 90	209.44 372.40 502.66	124.65 221.64 299.15	88.73 157.70 212.94	56.28 100.04 135.08	41.22 73.25 98.92	32.51 58.04 78.03	26.66 47.69 64.42		
	17½ × 24 20 × 80	90 80	601.29 872.67	357.85 519.36	254.95 369.69	161.60		93.33	77.06		

\* S. Single: D. Duplex.

Practical Results with Compressed Air,—Compressed sir,—System at the Chapin Mines, Iron Mountain, Mich.—These mines are three miles from the falls which supply the power. There are four turbines at the falls, one of 1000 horse-power and three of 900 horse-power ach. The pressure is 60 pounds at 60° Fahr. Each turbine runs a pair of compressors. The pipe to the mines is 40 inches in diameter. The power is applied at the mines to Corliss engines, running pumps, hoists, etc., and direct to rock-drills.

A test made in 1888 gave 1430.27 horse-power at the compressors, and 390.17 horse-power as the sum of the horse-power of the engines at the mines. Therefore, only 27% of the power generated was recovered at the mines. This includes the loss due to leakage and the loss of energy in heat, but not the friction in the engines or compressors. (F. A. Pocock, Trans. A. I. M. E., 1894.)

W.L. Saunders (Jour. F. I. 1892) says: "There is not a properly designed compressed-air installation in operation to-day that loses over 5% by transmission alone. The question is altogether one of the size of pipe; and if the pipe is large enough, the friction loss is a small tiem. The largest compressed-air power plant in America is that at the Chapin Mines in Michigan, where power is generated at Quinnesce Falls, and transmitted three miles. This is is not an economical plant, but the loss of pressure as shown by the gauge is only 2 lbs., and this is the loss which may be laid strictly to transmission.

"The loss of power in common practice, where compressed air is used to drive machinery in mines and tunnels, is about 70%. I refer to cases where common American air-compressors are used, and where the air is transmitted far enough to lose its heat of compression and is exhausted without

AIR.

reheating. In the best practice, with the best air-compressors, and without reheating, the loss is about 60%.
"These losses may be reduced to a point as low as 20% by combining the

best systems of reheating with the best air-compressors.

Prof. Kennedy says compressed air transmission system is now being carried on, on a large commercial scale, in such a fashion that a small motor four miles away from the central station can indicate in round numbers 10 horse-power, for 20 horse power at the station itself, allowing for the value of the coke used in heating the air.

The limit to successful reheating lies in the fact that air-engines cannot

work to advantage at temperatures over 350°.

The efficiency of the common system of reheating is shown by the results obtained with the Popp system in Paris. Air is admitted to the reheater at about 83°, and passes to the engine at about 315°, thus being increased in volume about 42%. The air used in Paris is about 11 cubic feet of Greased in volume about 45%. The an used in Talian year free air per inliute per horse-power. The ordinary practice in America with cold air is from 15 to 25 cubic feet per minute per horse-power. When the Parisengines were worked without reheating the air consumption was increased to about 15 cubic feet per horse-power per minute. The amount of fuel consumed during reheating is trifling.

Efficiency of Compressed-air Engines.—The efficiency of an air-engine, that is, the percentage which the power given out by the air-engine bears to that required to compress the air in the compressor, depends on the loss by friction in the pipes, valves, etc., as well as in the engine itself. This question is treated at length in the catalogue of the Norwalk Iron Works Co., from which the following is condensed. As the friction increases the most economical pressure increases. In fact, for any given friction in a pipe, the pressure at the compressor must not be carried below a certain limit. The following table gives the lowest pressures which should be used at the compressor with varying amounts of friction in the pipe:

Friction, lbs. 2.9 5.8 8.8 11.7 Lbs, at Compressor 20.5 29.4 38.2 47. Efficiency 7. 70.9 64.5 60.6 57.9 8.8 11.7 14.7 17.6 20.5 23,5 26.4 52.8 61.7 70.5 76.4 88.2 55.7

An increase of pressure will decrease the bulk of air passing the pipe and its velocity. This will decrease the loss by friction, but we subject ourselves to a new loss, i.e. the diminishing efficiencies of increasing pressures. Yet as each cubic foot of air is at a higher pressure and therefore carries more power, we will not need as many cubic feet as before, for the same work. With so many sources of gain or loss, the question of selecting the proper

54.0 52.5 51.3 50.2

pressure is not to be decided hastily.

The losses are, first, friction of the compressor. This will amount ordinarily to 15 or 20 per cent, and cannot probably be reduced below 10 per cent. to 15 or 20 per cent, and cannot promably be reduced below 10 per cent. Second, the loss occasioned by pumping the air of the engine-room, rather than the air drawn from a cooler place. This loss varies with the season and amounts from 3 to 10 per cent. This can all be saved. The third loss, or series of losses, arises in the compressing cylinder, viz., insufficient supply, difficult discharge, defective cooling arrangements, poor lubrication, etc. The fourth loss is found in the pipe. This loss varies with the situation, and is subject to somewhat complex influences. The fifth loss is chargeable to fall of temperature in the cylinder of the air-engine. Losses arising from leaks are often serious.

Air should be drawn from outside the engine-room, and from as cool a place as possible. The gain amounts to one per cent for every five degrees that the air is taken in lower than the temperature of the engine-room. The inlet conduit should have an area at least 50% of the area of the air piston, and should be made of wood, brick, or other non-conductor of heat.

Discharge of a compressor having an intake capacity of 1000 cubic feet at atmosper minute, and volumes of the discharge reduced to cubic feet at atmos-

pheric pressure and at temperature of 62 degrees Fahrenheit:

Temperature of Intake, F..... 0° 32° 62° 75° 80° 90° 100° 110° 

Requirements of Rock-drills Driven by Compressed (Norwalk Iron Works Co.)-The speed of the drill, the pressure of air, and the nature of the rock affect the consumption of power of rockdrills.

A three-inch drill using air at 30 lbs. pressure made 300 blows per minute and consumed the equivalent of 64 cubic feet of free air per minute. The same drill, with air of 58 lbs, pressure, made 450 blows per minute and consumed 160 cubic feet of free air per minute. At Hell Gate different machines doing the same work used from 80 to 150 cubic feet free air per minute,

An average consumption may be taken generally from 80 to 100 cubic feet

per minute, according to the nature of the work.

The Popp Compressed-air System in Paris.—A most extensive system of distribution of power by means of compressed air is that of M. Popp, in Paris. One of the central stations is laid out for 24,000 horse-power. For a very complete description of the system, see Engineering, Feb. 15, June 7, 21, and 28, 1889, and March 13 and 29, April 10, and May 1, 1891. Also Proc. Inst. M. E., July, 1889. A condensed description will be found in Madern Machanism. 120. found in Modern Mechanism, p. 12.

Utilization of Compressed Air in Small Motors,-In the earliest stages of the Popp system in Paris it was recognized that no good results could be obtained if the air were allowed to expand direct into the results could be obtained in the latter above to be xpanu direct into the motor; not only did the formation of ice due to the expansion of the air rapidly accumulate and choke the exhaust, but the percentage of useful work obtained, compared with that put into the air at the central station, was so small as to render commercial results hopeless.

After a number of experiments M. Popp adopted a simple form of cast-

iron stove lined with fire-clay, heated either by a gas jet or by a small coke fire. This apparatus answered the desired purpose until some better arrangement was perfected, and the type was accordingly adopted throughout the whole system. The economy resulting from the use of an improved form was very marked, as will be seen from the following table.

EFFICIENCY OF AIR-HEATING STOVES.

	Surface.	ber 1	Tempe of Air i	erature n Oven.	Value o	of Heat Al per Hour.	
Nature of Stove.	Heating Su	Air Heated Hour.	Admission Deg. Fahr.	Exit Deg. Fahr.	Total.	Per Square Foot of Heating Surface.	Per Pound of Coke.
Cast-iron box { stoves Wrought-iron	sq. ft. 14 14	eub.ft, 20,342 11,054	45 45	215 364	cal. 17,900 17,200	cal. 1278 1228	cal. 2032 2058
coiled tubes	46.3	38,428	41	347	39,200	830-	2545

The results given in this table were obtained from a large number of trials. From these trials it was found that more than 70% of the total number of calories in the fuel employed was absorbed by the air and transformed into useful work. Whether gas or coal be employed as the fuel, the amount required is so small as to be scarcely worth consideration; according to the experiments carried out it does not exceed 0.2 lb. per horse-power per hour, but it is scarcely to be expected that in regular practice this quantity is not largely exceeded. The efficiency of fuel consumed in this way is at least six times greater than when utilized in a boiler and steam-engine.

According to Prof. Riedler, from 15% to 20% above the power at the central station can be obtained by means at the disposal of the power users, and it has been shown by experiment that by heating the air to 480° F. an increased efficiency of 30% can be obtained.

A large number of motors in use among the subscribers to the Compressed Air Company of Paris are rotary engines developing 1 horse-power and less, and these in the early times of the industry were very extravagant in their consumption. Small rotary engines, working cold air without expansion, used as high as 2330 cp. ft. of air per brake horse-power per hour, and with heated air 1624 cu. ft. Working expansively, a 1 horse-power rotary engine used 169 cu. ft. of cold air, or 960 cu. ft. of heated air, and a 2-horse-power rotary engine used 1690 cu. ft. of cold air, or 971 cu. ft. of air, heated to about 50° C.

The efficiency of this type of rotary motors, with air heated to 50° C, may now be assumed at 43%. With such an efficiency the use of small motors in

many industries becomes possible, while in cases where it is necessary to have a constant supply of cold air economy ceases to be a matter of the first importance.

The following table shows the results of tests of a small rotary engine used for driving sewing-machines, and indicating about a tenth of a horse-power:

### TRIALS OF A SMALL ROTARY RIEDINGER ENGINE

Numbers of trials. Initial air-pressq. in. Initial temperature, deg. Fahr. Ftlbs, per sec., measured on the brake. Revolutions per minute.	86 54° 51.63 384	II. 71.8 338° 34.07
Consumption of air per 1 horse-power per hour		988

The following table shows the results obtained with a one-half horsepower variable expansive Riedinger rotary engine. These trials represent the best practice that has been obtained up to the present time (1890). The volumes of air were in all cases taken at atmospheric pressure:

TRIALS OF A 5-HORSE-POWER KIEDIN	GER	KOTARY E	NGINE.	
Numbers of trials	I.	II.	III.	IV.
Initial pressure of air, lbs, per sq. in	54	69.7	85	71.8
" temperature of air, deg. Fahr	338	356	388	46
Final " " " " "	77	68		77
Revolutions per minute	335	350	310	243
Ftlbs. per second, measured on brake	271	477	376	316
Consumption of air per horse-power per				
hour	883	791	900	1148

Trials made with an old single-cylinder 80-horse-power Farcot steam-engine, indicating 72 horse-power, gave a consumption of air per brake horse-power as low as 465 cu. ft. per hour. The temperature of admission was 320° F., and of exhaust 95° F. Prof. Elliott gives the following as typical results of efficiency for various

systems of compressors and air-motors:

Simple compressor and simple motor, efficiency	39.1%
Compound compressor and simple motor, "	44.9
" compound motor, efficiency	50.7
Triple compressor and triple motor, "	55.3

The efficiency is the ratio of the indicated horse-power in the motor cylinders to the indicated horse-power in the steam-cylinders of the compressor. The pressure assumed is 6 atmospheres absolute, and the losses are equal to those found in Paris over a distance of 4 miles.

# Summary of Efficiencies of Compressed-air Transmission at Paris, between the Central Station at St. Fargeau and a 10-horse-power Motor Working with Pressure Reduced to 41/2 Atmospheres.

(The figures below correspond to mean results of two experiments cold and two heated.)

1 indicated horse-power at central station gives 0.845 indicated horse-power in compressors, and corresponds to the compression of 348 cubic feet of air per hour from atmospheric pressure to 6 atmospheres absolute. (The weight of this air is about 25 pounds.)

0.845 indicated horse-power in compressors delivers as much air as will do 0.52 indicated horse-power in adiabatic expansion after it has fallen in temperature to the normal temperature of the mains.

The fall of pressure in mains between central station and Paris (say 5 kilometres) reduces the possibility of work from 0.52 to 0.51 indicated horsepower. The further fall of pressure through the reducing valve to 41/2 atmospheres

(absolute) reduces the possibility of work from 0.51 to 0.50.

Incomplete expansion, wire-drawing, and other such causes reduce the actual indicated horse-power of the motor from 0.50 to 0.39.

By heating the air before it enters the motor to about 320° F., the actual indicated horse-power at the motor is, however, increased to 0.54. The ratio 0.54

of gain by heating the air is, therefore,  $\frac{0.54}{0.39} = 1.38$ .

In this process additional heat is supplied by the combustion of about 0.39 pounds of coke per indicated horse-power per hour, and if this be taken into account, the real indicated efficiency of the whole process becomes 0.47 instead of 0.54.

Working with cold air the work spent in driving the motor itself reduces

the available horse-power from 0.39 to 0.26,

Working with heated air the work spent in driving the motor itself reduces the available horse-power from 0.54 to 0.44.

A summary of the efficiencies is as follows:

Efficiency of main engines 0.845.

Efficiency of compressors  $0.52 \div 0.845 = 0.61$ . Efficiency of transmission through mains  $0.51 \div 0.52 = 0.98$ .

Efficiency of reducing valve  $0.50 \div 0.51 = 0.98$ .

The combined efficiency of the mains and reducing valve between 5 and  $4\frac{1}{2}$  atmospheres is thus  $0.98 \times 0.98 = 0.96$ . If the reduction had been to 4, 314, or 3 atmospheres, the corresponding efficiencies would have been 0.93, 0.89, and 0.85 respectively.

Indicated efficiency of motor  $0.39 \div 0.50 = 0.78$ .

Indicated efficiency of whole process with cold air 0.39. Apparent indicated efficiency of whole process with heated air 0.54.

Real indicated efficiency of whole process with heated air 0.47.

Mechanical efficiency of motor, cold, 0.67.

Mechanical efficiency of motor, hot, 0.81.

Most of the compressed air in Paris is used for driving motors, but the work done by these is of the most varied kind. A list of motors driven from St. Fargeau station shows 225 installations, nearly all motors working at from 16 horse-power to 50 horse-power, and the great majority of them more than two miles away from the station. The new station at Quai de la Gare is much larger than the one at St. Fargeau. Experiments on the Riedler air-compressors at Paris, made in December, 1891, to determine the ratio between the indicated work done by the air-pistons and the indicated work in the steam-cylinders, showed a ratio of 0.8997. The compressors are driven

in the steam-cyniners, snowed a ratio of 0.8997. The compressors are arrived by four triple-expansion Corliss engines of 2000 horse-power each.

880, ps. Operated by Compressed Air.—The fron Age, March 2, 1893, describes the shops of the Wuerpel's witch and Signal Co., East St. Louis, the machine tools of which are operated by compressed air, each of the larger tools having its own air engine, and the smaller tools being belted from shafting driven by an air engine. Power is supplied by a composition rated at 55 horse-power. The air engines are of the Kriebel make, rated from 2 to 8 horse-power.

Pneumatic Postal Transmission .- A paper by A. Falkenau, Eng'rs Club of Philadelphia, April 1894, entitled the "First United States Pneumatic Postal System," gives a description of the system used in London and Paris, and that recently introduced in Philadelphia between the main and Paris, and that recently introduced in Philadelphia between the main post-office and a substation. In London the tubes are 2½ and 3 inch lead pipes laid in cast-fron pipes for protection. The carriers used in 2½-inch tubes are but 1½ inches diameter, the remaining space being taken up by packing. Carriers are despatched singly. First, vacuum aloue was used; later, vacuum and compressed air. The tubes used in the Continental cities in Europe are wrought iron, the Paris tubes being 2½ inches diameter. There the carriers are despatched in trains of six to ten, propelled by a piston. In Philadelphia the size of tube adopted is 6½ inches, the tubes being of cast iron bored to size. The lengths of the outgoing and return tubes are 2928 feet each. The pressure at the main station is 71bs., at the substation 1 bs. and at the end of the return pine atmospheric pressure. substation 4 lbs., and at the end of the return pipe atmospheric pressure. The compressor has two air-cylinders  $18\times 24$  in. Each carrier holds about 2000 letters, but 100 to 150 are taken as an average. Eight carriers may be despatched in a minute, giving a delivery of 48,000 to 72,000 letters per hour.

The time required in transmission is about 57 seconds,

The Mekarski Compressed-air Tramway at Berne, Switzerland. (Eng'g News, April 20, 1893.)—The Mekarski system has been introduced in Berne, witzerland, on a line about two miles long, with grades of 0.25% to 3.7% and 5.3%. A special feature of the Mekarski system is the heating of the air, to maintain it at a constant temperature, by passing it through superheated water at 330° F. The air thus becomes saturated with steam, which subsequently partly condenses, its latent heat being absorbed by the expanding air. The pressure in the car reservoirs is 440

lbs. per sq. in.

The engine is constructed like an ordinary steam tramway locomotive.

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and drives two coupled axles, the wheel-base being 5.2 ft. It has a pair of outside horizontal cylinders,  $5.1 \times 8.6$  in.; four coupled wheels, 27.5 in. diameter. The total weight of the car including compressed air is 7.28 tons, and with 30 passengers, including the driver and conductor, about 9.5 tons.

The authorized speed is about 7 miles per hour. Taking the resistance due to the grooved rails and to curves under unfavorable conditions at 30 lbs. per ton of car weight, the engine has to overcome on the steepest grade, tos. per ton of car weight, the engine has to overcome on the steepest grade, 5%, a total resistance of about 0.63 ton, and has to develop 25 H.P. At the maximum authorized working pressure in cylinders of 176 lbs. per sq. in, the motors can develop a tractive force of 0.64 ton. This maximum is, therefore, just sufficient to take the car up the 5.2% grade, while on the flatter sections of the line the working pressure does not exceed 73 to 147 lbs. per sq. in. Sand has to be frequently used to increase the adhesion on the 2% to 5% grades.

Between the two car frames are suspended ten horizontal compressed-air storage-cylinders, varying in length according to the available space, but of uniform inside diameter of 17.7 in., composed of riveted 0.27-in. sheet iron, and tested up to 588 lbs. per sq. in. These cylinders have a collective and tested to 10 t 75 cu. ft., divided into two groups, the working and the reserve battery, the former of 49 cu. ft. the latter of 26 cu. ft. capacity.

From the results of six official trips, the pressure and the mean consump-

tion of air during a double journey per motor car are as follows:

Storage-cylinders.	lbs. per	lbs. per
9 4		sq. in.
Pressure of air on starting	440	440
Pressure of air at end of up journey	176	260
Pressure of air at end of down journey	103	176
Consumption of air at end of up journey	92	
Consumption of air during down journey	31	
	Pressure of air at end of up journey	Working,   Ibs. per

This has been fully confirmed by the working experience of 1891, when the consumption of air per motor car and double journey was as follows: Minimum, 103 lbs..... 28 lbs. per car-mile. Maximum, 154 lbs..... 42 66 Mean, 123 lbs....

The principal advantages of the compressed-air system for urban and suburban tramway traffic as worked at Berne consist in the smooth suburban tramway trame as worked at Berne consist in the smooth and noiseless motion; in the absence of smoke, steam, or heat, of overhead or underground conductors, of the more or less grinding motion of most electric cars, and of the jerky motion to which underground cable traction is subject. On all these grounds the system has vindicated its claims as being preferable to any other so far known system of mechanical traction for street tramways. Its disadvantages, on the other hand, consist in the extremely delicate adjustment of the different parts of the system, in the comparatively small supply of air carried by one motor car, which necessitates the car returning to the depot for refilling after a run of only four miles or 40 minutes, although on the Nogent and Paris lines the cars, which are, moreover, larger, and carry outside passengers on the top, rnn seven miles, and the loading pressure is 547 lbs. per sq. in, as against only 440 lbs, at Berne.

Longer distances in the same direction would involve either more powerful motors, a larger number of storage-cylinders, and consequently heavier cars, or loading stations every four or seven miles; and in this respect the system is manifestly inferior to electric traction, which easily admits of a line of 10 to 15 miles in length being continuously fed from one central station without the loss of time and expense caused by reloading.

The cost of working the Berne line is compared in the annexed table with some other tramways worked under similar conditions by horse and mechanical traction for the year 1891. As is seen, both in the case of compressed air and of electric traction, the cost of working is considerably increased where steam at a high cost of fuel has to be used instead of hydraulic power. Given the latter, the cost of working by air is about the same as that by steam-locomotives or steam-cars; but over both of these last-named, compressed-air offers, at equal cost and for such short lines with constant traffic, certain advantages;

	Constr. Opera-
1891. Length of Line,	Motive Power, and equip't, tion,
miles.	per mile. p. car mi.
Geneva, city 8.68	Horse\$60,800 19.4 cts.
Zurich, city 5.58	Horse39.700 11.6
Geneva, suburban 40.30	Steam locomotive.32,000 13.2
Mulhouse, city 18.00	Steam locomotive, 22,400 17.8
Montreux, suburban 6.82	Hydro-electric 20,800 10.4
Florence, suburban 4.96	Steam-electric32,000 20.0
Tours, suburban 6.20	Steam cars19,200 17.2
Nogent (Paris), suburban 7.44	Steam-compr. air.46,100 25.6
Berne, city 1.86	Hydro-compr. air.48,950 17.8

For description of the Mekarski system as used at Nantes, France, see

For description of the Mekarski system as used at Nantes, France, see paper by Prof. D. S. Jacobus, Trans. A. I. M. E. xix, 553.

Compressed Air for Working Underground Pumps in Mines.—Eng/g Record, May 19, 1894, describes an installation of compressors for working a number of pumps in the Nottingham No. 15 Mines (Plymouth, Pa., which is claimed to be the largest in America. The compressors develop above 2300 H.P., and the piping, horizontal and vertical, is 6000 feet in length. About 25,000 gallons of water per hour are raised,

# FANS AND BLOWERS.

Centrifugal Fans. - The ordinary centrifugal fan consists of a number of blades fixed to arms, revolving on a shaft at high speed. The width of the blade is parallel to the axis of the shaft. Most engineers' reference books quote the experiments of W. Buckle, Proc. Inst. M.E., 1847, as still standard. Mr. Buckle's conclusions are given below, together with data of more recent experiments.

Experiments were made as to the proper size of the inlet openings and on the proper proportions to be given to the vane. The inlet openings in the sides of the fan-chest were contracted from 17½ in., the original diameter,

to 12 and 6 in. diam., when the following results were obtained:

First, that the power expended with the opening contracted to 12 in. diam. was as 2½ to 1 compared with the opening of 17½ in. diam.; the velocity of the fan being nearly the same, as also the quantity and density of air delivered.

Second, that the power expended with the opening contracted to 6 in diam was as 2½ to 1 compared with the opening of 17½ in diam; the velocity of the fan being nearly the same, and also the area of the efflux

pipe, but the density of the air decreased one fourth.

These experiments show that the inlet openings must be made of sufficient size, that the air may have a free and uninterrupted action in its passage to the blades of the fan; for if we impede this action we do so at the expense

of power.

With a vane 14 in. long, the tips of which revolve at the rate of 286.8 ft. per second, air is condensed to 9.4 ounces per square inch above the pressure of the atmosphere, with a power of 9.6 H. P.; but a vane 8 inches long, the diameter at the tips being the same, and having, therefore, the same velocity, condenses air to 6 ounces per square inch only, and takes 12 H. P.

Thus the density of the latter is little better than six tenths of the former, Thus the density of the latter is little better than six tenths of the former, while the power absorbed is nearly 1.25 to 1. Although the velocity of the tips of the vanes is the same in each case, the velocities of the heels of the respective blades are very different, for, while the tips of the blades in each case move at the same rate, the velocity of the heel of the 14-inch is in the ratio of 1 to 1.67 to the velocity of the heel of the 8-inch blade. The longer blades approaching nearer the centre, strikes the air with less velocity, and allows it to enter on the blade with greater freedom, and with considerably less force than the shorter one. The inference is, that the short blade must take more power at the same time that it accumulates a less quantity of air. These experiments lead to the conclusion that the length of the vane demands as great a consideration as the proper diameter of the inlet opening. If there were no other object in view, it ATR.

would be useless to make the vanes of the fan of a greater width than the inlet opening can freely supply. On the proportion of the length and width of the vane and the diameter of the inlet opening rest the three most important points, viz., quantity and density of air, and expenditure of power. In the 14-linch blade the tip has a velocity 2.6 times greater than the heel; and, by the laws of centrifugal force, the air will have a density 2.6 times greater at the tip of the blade than that at the heel. The air cannot

times greater at the tip of the blade than that at the fleet. The air cannot enter on the heel with a density higher than that of the atmosphere; but in its passage along the vane it becomes compressed in proportion to its centrifugal force. The greater the length of the vane, the greater will be the difference of the centrifugal force between the heel and the tip of the blade; consequently the greater the density of the air.

Reasoning from these experiments, Mr. Buckle recommends for easy ref-

receive the following proportions for the construction of the fan:

1. Let the width of the vanes be one fourth of the diameter; 2. Let the
diameter of the inlet openings in the sides of the fan-chest be one half the
diameter of the fan; 3. Let the length of the vanes be one fourth of the
diameter of the fan.

In adopting this mode of construction, the area of the inlet openings in the sides of the fan-chest will be the same as the circumference of the heel of the blade, multiplied by its width; or the same area as the space described by the heel of the blade.

# Best Proportions of Fans. (Buckle.)

PRESSURE FROM 3 OUNCES TO 6 OUNCES PER SQUARE INCH; OR 5,2 INCHES TO 10.4 INCHES OF WATER.

Diameter of Fan.		Vanes.			Diameter of Inlet Open-			Diameter of Fan.						Diameter of Inlet Open-	
		dth.	Ler	igth.	ings.				Width, Length.						
ft. ir	ıs.	ft.	ins.	ft.	ins.	ft.	ins.	ft.	ins.	ft.	ins.	ft.	ins.	ft.	ins.
3 (	)	0	9 101⁄6	0	9	1	6	4 5	6	E	11/2	1	11/2	2 2	8
4	Ó	ĭ	0	1	0/2	2	ŏ	6	ŏ	1	6	î	6	3	ŏ

Pressure from 6 ounces to 9 ounces per square inch, and upwards. OR 10.4 INCHES TO 15.6 INCHES OF WATER.

3 0	0 7	1 0	1 0	4 6	0 10½	1 4½	1 2 6	9
3 6	0 81/6	1 11/2	1 3	5 0	1 0	1 6		0
4 0	0 91/2	1 31/2	1 6	6 0	1 2	1 10		4
	0 0/2	1 0/2	1 0		1 ~	1 10		

The dimensions of the above tables are not laid down as prescribed limits,

but as approximations obtained from the best results in practice.

Experiments were also made with reference to the admission of air into the transit or outlet pipe. By a slide the width of the opening into this pipe was varied from 12 to 4 inches. The object of this was to proportion the opening to the quantity of air required, and thereby to lessen the power necessary to drive the fan. It was found that the less this opening is made, provided we produce sufficient blast, the less noise will proceed from the fan; and by making the tops of this opening level with the tips of the vane. the column of air has little or no reaction on the vanes.

The number of blades may be 4 or 6. The case is made of the form of an arithmetical spiral, widening the space between the case and the revolving blades, circumferentially, from the origin to the opening for discharge.

The following rules deduced from experiments are given in Spretson's treatise on Casting and Founding:

The fan-case should be an arithmetical spiral to the extent of the depth of the blade at least.

The diameter of the tips of the blades should be about double the diameter of the hole in the centre; the width to be about two thirds of the radius of the tips of the blades. The velocity of the tips of the blades should be rather more than the velocity due to the air at the pressure required, say one

eighth more velocity.

In some cases, two fans mounted on one shaft would be more useful than one wide one, as in such an arrangement twice the area of inlet opening is obtained as compared with a single wide fan. Such an arrangement may be adopted where occasionally half the full quantity of air is required, as one of them may be put out of gear, thus saving power.

Pressure due to Velocity of the Fan-blades.—"By increasing the number of revolutions of the fan the head or pressure is increased, the law being that the total head produced is equal (in centrifugal fans) to

twice the height due to the velocity of the extremities of the blades, or

 $H=\frac{v^2}{}$ - approximately in practice " (W. P. Trowbridge, Trans. A. S. M. E.,

vii. 536.) This law is analogous to that of the pressure of a jet striking a plane surface. T. Hawksley, Proc. Inst. M. E., 1882, vol. lxix.. says: "The pressure of a fluid striking a plane surface perpendicularly and then escaping at right angles to its original path is that due to twice the height h due the velocity."

(For discussion of this question, showing that it is an error to take the

(For discussion of this question, showing that it is an error to take the pressure as equal to a column of air of the height  $h = v^2 + 2g$ , see Wolff on Windmills, p. 17. Buckle says: "From the experiments it further appears that the velocity of the tips of the fan is equal to nine tenths of the velocity a body would acquire in failing the height of a homogeneous column of air equivalent to the density." D. K. Clark (R. T. & D., p. 924), paraphrasing Buckle, apparently, says: "It further appears that the pressure generated at the circumference is one ninth greater than that which is due to the actual circumfer-ential velocity of the fan." The two statements, however, are not in

harmony, for if  $v = 0.9 \ \sqrt{2gH}$ ,  $H = \frac{v^2}{0.81 \times 2g} = 1.234 \frac{v^2}{2g}$  and not  $1_{\frac{1}{6}} \frac{v^2}{2g}$ 

If we take the pressure as that equal to a head or column of air of twice the height due the velocity, as is correctly stated by Trowbridge, the paradoxical statements of Buckle and Clark—which would indicate that the actual pressure is greater than the theoretical-are explained, and the

formula becomes  $H = .617 \frac{v^2}{}$ and  $v = 1.273 \sqrt{gH} = 0.9 \sqrt{2gH}$ , in which H is the head of a column producing the pressure, which is equal to twice the

theoretical head due the velocity of a falling body (or  $h = \frac{v^2}{2q}$ ), multiplied

by the coefficient .617. The difference between 1 and this coefficient expresses the loss of pressure due to friction, to the fact that the inner portions of the blade have a smaller velocity than the outer edge, and probably to other causes. The coefficient 1.273 means that the tip of the blade must be given a velocity 1.273 times that theoretically required to produce the

To convert the head H expressed in feet to pressure in lbs. per sq. in. multiply it by the weight of a cubic foot of air at the pressure and temperature of the air expelled from the fan (about .08 lb. usually) and divide by 144. Multiply this by 16 to obtain pressure in ounces per sq. in. or by 2.035 to obtain inches of mercury, or by 27.71 to obtain pressure in inches of water column. Taking .08 as the weight of a cubic foot of air,

> p lbs. per sq. in.  $= .00001066v^2$ ;  $v = 310 \sqrt{p}$  nearly:  $p_1$  ounces per sq. in. = .0001706 $v^2$ ;  $v = 80 \sqrt{p_1}$  $p_2$  inches of mercury = .00002169 $v^2$ ;  $v = 220 \sqrt{p_2}$  $p_3$  inches of water = .0002954 $v^2$ ;  $v = 60 \sqrt{p_3}$

in which v = velocity of tips of blades in feet per second.

Testing the above formula by the experiment of Buckle with the vane 14 inches long, quoted above, we have  $p=.00001060v^2=9.56$  oz. The experiment gave 9.4 oz.

permient gave 9.4-0z.

Testing it by the experiment of H. I. Snell, given below, in which the circumferential speed was about 150 ft. per second, we obtain 3.85 ounces, while the experiment gave from 2.85 to 3.50 ounces, according to the amount of opening for discharge. The numerical coefficients of the above formulæ are all based on Buckle's statement that the velocity of the tips of the fan is equal to nine tenths of the velocity a body would acquire in falling the

height of a homogeneous column of air equivalent to the pressure. Should other experiments show a different law, the coefficients can be corrected accordingly. It is probable that they will vary to some extent with different proportions of fans and different speeds.

Taking the formula  $v = 80 \sqrt{p_1}$ , we have for different pressures in ounces per square inch the following velocities of the tips of the blades in feet per second:

A rule in App. Cyc. Mech, article "Blowers," gives the following velocities of circumference for different densities of blast in ounces: 3, 170; 4, 180; 5, 195; 6, 205; 7, 215.

The same article gives the following tables, the first of which shows that the density of blast is not constant for a given velocity, but depends on the ratio of area of nozzle to area of blades:

Velocity of circumference, feet per second, 150 150 150 170 200 200 220 Area of nozzle + area of blades..... Density of blast, oz. per square inch......

QUANTITY OF AIR OF A GIVEN DENSITY DELIVERED BY A FAN.

Total area of nozzles in square feet × velocity in feet per minute corresponding to density (see table) = air delivered in cubic feet per minute.

Density, ounces per sq. in.	Velocity, feet per minute.	Density, ounces per sq. in,	per min	Density, ounces per sq. in.	Velocity, fee per minute.
1	5000	5	11,000	9	15,000
2	7000	6	12,250	10	15,800
3	8600	7	13,200	11	16,500
4	10.000	8	14 150	19.	17 300

Experiments with Blowers. (Henry I. Snell, Trans. A. S. M. E. ix. 51.)—The following tables give velocities of air discharging through an aperture of any size under the given pressures into the atmosphere. volume discharged can be obtained by multiplying the area of discharge opening by the velocity, and this product by the coefficient of contraction: .65 for a thin plate and .93 when the orifice is a conical tube with a convergence of about 3.5 degrees, as determined by the experiments of Weisbach.

The tables are calculated for a barometrical pressure of 14.69 lbs. (=

235 oz.), and for a temperature of 50° Fahr., from the formula  $V = \sqrt{2gh}$ . Allowances have been made for the effect of the compression of the air.

but none for the heating effect due to the compression.

At a temperature of 50 degrees, a cubic foot of air weighs .078 lbs., and calling q = 32,1602, the above formula may be reduced to

 $V_1 = 60 \sqrt{31.5812 \times (235 - P) \times P}$ 

where  $V_1$  = velocity in feet per minute. P = pressure above atmosphere, or the pressure shown by gauge, in oz. per square inch.

Pressure per sq. in. in inches of water.	Corresponding Pressure in oz. per sq. inch.	Velocity due the Pressure in feet per minute.	Pressure per sq. in. in inches of water.	Corresponding Pressure in oz. per sq. inch.	Velocity due the Pressure in feet per minute.
1/32 1/16 1/8 3/16	.01817 .03634 .07268 .10902	696.78 987.66 1393.75 1707.00	5/8 3/4 2/8 1	.36340 .43608 .50870 .58140	3118.38 3416.64 3690.62 3946.17
5/16 3/8	.14536 .18170 .21804	1971.30 2204.16 2414.70	11/4 11/6 13/4	.7267 .8721 1.0174	4362.62 4836.06 5224.98

Press- ure in oz. per sq. inch.	Velocity due the Pressure in ft. per minute.	Press- ure in oz. per sq. inch.	Velocity due the Pressure in ft, per minute.		Pressure	Pressure in oz, per sq. in.	Velocity due the Pressure in ft. per minute.
.25 .50 .75 1.00 1.25 1.50 1.75 2.00	2,582 3,658 4,482 5,178 5,792 6,349 6,861 7,338	2.25 2.50 2.75 3.00 3.50 4.00 4.50 5.00	7,787 8,213 8,618 9,006 9,739 10,421 11,065 11,676	5.50 6.00 6.50 7.00 7.50 8.00 9.00 10.00	12,259 12,817 13,354 13,873 14,374 14,861 15,795 16,684	11.00 12.00 13.00 14.00 15.00 16.00	17,534 18,350 19,138 19,901 20,641 21,360

Pressure in ounces per square inch.		Pressure in ounces per square inch.	Velocity in feet per minute.
.01	516.90 722.64	.06	1206.24 1367.76
.03	895,26 1033,86	.08	1462.20 1550.70
.05	1155.90	.10	1635.00

# Experiments on a Fan with Varying Discharge-opening. Revolutions nearly constant.

Revolutions per minute.	Area of Discharge in square inches.	Observed Pressure in ounces.	Volume of Air dis- charged per min., cubic feet.	Horse-power.	Actual Number of cu. ft. of Air de- livered per H.P.	Theoret. Vol. per min. that may be discharged with 1H.P. at corresp. Pressure.	Efficiency of Blow- ers as per Experi- ment.
1519 1479 1480 1471 1485 1485 1465 1468 1500 1426	0 6 10 20 28 36 40 44 48 89.5	3.50 3.50 3.50 3.50 3.50 3.40 3.25 3.00 3.00 2.38	0 406 676 1353 1894 2400 2605 2752 3002 3972	.80 1.15 1.30 1.95 2.55 3.10 3.30 3.55 3.80 4.80	353 520 694 742 774 790 775 790 827	1048 1048 1048 1048 1048 1078 1126 1222 1222 1544	.337 .496 .66 .709 .718 .70 .635 .646

The fan wheel was 23 inches in diameter, 65% inches wide at its periphery. and had an inlet of 121/2 inches in diameter on either side, which was partially obstructed by the pulleys, which were 5 9/16 inches in diameter. It had eight blades, each of an area of 45.49 square inches.

The discharge of air was through a conical tin tube with sides tapered at an angle of 3½ degrees. The actual area of opening was 7% greater than given in the tables, to compensate for the venu contracta.

In the last experiment, 89.5 sq. in. represents the actual area of the mouth-

of the blower less a deduction for a narrow strip of wood placed across it for the purpose of holding the pressure-gauge. In calculating the volume of air discharged in the last experiment the value of vena contracta is taken at 80.

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Experiments were undertaken for the purpose of showing the results obtained by running the same fan at different speeds with the discharge-open-

ing the same throughout the series.

The discharge-pipe was a conical tube 81/4 inches inside diameter at the end, having an area of 56.74, which is 7% larger than 58 sq. inches; therefore 53 square inches, equal to .368 square feet, is called the area of discharge, as that is the practical area by which the volume of air is computed.

Experiments on a Fan with Constant Discharge-open-ing and Varying Speed.—The first four columns are given by Mr. Snell, the others are calculated by the author.

Revs. per min.	Pressure in ounces,	Vol. of Air in cu. ft. per minute, V.	Horse-power.	Velocity of Tips of Blades, ft. per sec.	Velocity due Pressure from Formula $v = 80 \text{ V}\overline{p}$ .	Coefficient of Formula $v = x \sqrt{p}$ from Experiment.	Velocity of Air per minute in Efflux Pipe, $V \div .368$ .	Theoretical Horse- power.	Efficiency per cent.
600 800 1000 1200 1400 1600 1800 2000	.50 .88 1.38 2.00 2.75 3.80 4.80 5.95	1836 1787 2245 2712 3177 3670 4172 4674	.25 .70 1.35 2.20 3.45 5.10 8.00 11.40	60.2 80.3 100.4 120.4 140.5 160.6 180.6 200.7	- 56.6 75.0 94. 113. 133. 156. 175. 195.	85.1 85.6 85.4 85.1 84.8 82.4 82.4 83.6	3,630 4,856 6,100 7,370 8,633 9,978 11,337 12,701	.182 .429 .845 1.479 2.283 3.803 5.462 7.586	73 61 63 67 66 74 68 67

Mr. Snell has not found any practical difference between the efficiencies of blowers with curved blades and those with straight radial ones.

on blowers while curved blades and those with straight radial ones. From these experiments, says Mr. Snell, it appears that we may expect to receive back 65% to 75% of the power expended, and no more. The great amount of power often used to run a fan is not due to the fan itself, but to the method of selecting, erecting, and piping it. (For opinions on the relative merits of fans and positive rotary blowers, see discussion of Mr. Snell's paper, Trans. A. S. M. E., ix. 66, etc.)

Comparative Efficiency of Fans and Positive Blowers, (H. M. Howe, Trans. A. I. M. E., x. 482.)—Experiments with faus and positive (Baker) blowers working at moderately low pressures, under 20 ounces, shot that they work more efficiently at a given pressure when delivering large volumes (i.e., when working nearly up to their maximum capacity) than when delivering comparatively small volumes. Therefore, when great variations in the quantity and pressure of blast required are liable to arise, the highest efficiency would be obtained by having a number of blowers, always driving them up to their full capacity, and regulating the amount of blast by altering the number of blowers at work, instead of having one or two very large blowers and regulating the amount of blast by the speed of the blowers.

There appears to be little difference between the efficiency of fans and of Baker blowers when each works under favorable conditions as regards

quantity of work, and when each is in good order.

For a given speed of fan, any diminution in the size of the blast-orifice decreases the consumption of power and at the same time raises the pressure of the blast; but it increases the consumption of power per unit of orifice for a given pressure of blast. When the orifice has been reduced to the normal size for any given fan, further diminishing it causes but slight elevation of the blast pressure; and, when the orifice becomes comparatively small, further diminishing it causes no sensible elevation of the blast pressure, which remains practically constant, even when the orifice is entirely closed

Many of the failures of fans have been due to too low speed, to too small pulleys, to improper fastening of belts, or to the belts being too nearly vertical; in brief, to bad mechanical arrangement, rather than to inherent de-

fects in the principles of the machine.

If several fans are used, it is probably essential to high efficiency to provide a separate blast pipe for each (at least if the fans are of different size or speed), while any number of positive blowers may deliver into the same pipe without lowering their efficiency.

# Capacity of Fans and Blowers.

The following tables show the guaranteed air-supply and air-removal of leading forms of blowers and exhaust fans. The figures given are often exceeded in practice, especially when the blowers and fans are driven at higher speeds than stated. The ratings, particularly of the blowers, are below those generally given in catalogues, but it was the desire to present only conservative and assured practice. (A. R. Wolff on Ventilation.)

QUANTITY OF AIR SUPPLIED TO BUILDINGS BY BLOWERS OF VARIOUS SIZES.

Diameter of Wheel in feet.	of Revs.	Iforse- power to Drive Blower.	Capacity cu, ft. per min, against a Pressure of 1 ounce per sq. in	Diam- eter of Wheel	Number	Horse- power to Drive Blower.	Capacity cu. ft. per min. against a Pressure of 1 ounce per sq. in.
4	350	6.	10,635	9	175	29	56,800
5	325	9.4	17,000	10	160	35.5	70,340
6	275	13.5	29,618	12	130	49.5	102,000
7	230	18.4	42,700	14	110	66	139,000
8	200	24	46,000	15	100	77	160,000

If the resistance exceeds the pressure of one ounce per square inch, of above table, the capacity of the blower will be correspondingly decreased, or power increased, and allowance for this must be made when the distributing ducts are small, of excessive length, and contain many contractions and bends.

QUANTITY OF AIR MOVED BY AN APPROVED FORM OF EXHAUST FAN, THE FAN DISCHARGING DIRECTLY FROM ROOM INTO THE ATMOSPHERE.

eter of Wheel	Ordinary Number of Revs. per min.	power	Capacity in cu. ft, per min.	eter of	Ordinary Number of Revs. per min.	power	Capacity in cu. ft. per min.
2.0	600	0.50	5,000	4.0	475	3.50	28,000
2.5	550	0.75	8,000	5.0	350	4.50	35,000
3.0	500	1.00	12,000	6.0	300	7.00	50,000
3.5	500	2.50	20,000	7.0	250	9.00	80,000

The capacity of exhaust fans here stated, and the horse-power to drive them, are for free exhaust from room into atmosphere. The capacity decreases and the horse-power increases materially as the resistance, resulting from lengths, smallness and bends of ducts, enters as a factor. The difference in pressures in the two tables is the main cause of variation in the respective records. The fan referred to in the second table could not be used with as high a resistance as one ounce per square inch, the rated resistance of the blowers.

### CENTRIFUGAL FANS.

# Pressures, Velocities, Volume of Air, Horse-Power Required, etc. (B. F. Sturtevant Co.) Wad Taraa ladaa Lee Laataa Laay

Pressure per sq. in. in ounces from ¼ to 20 ounces; which in cludes the strongest blast founce on any cupola in this country.	Velocity in feet per minute of Ali (at 50°F.) escaping into open ali through any shaped hole from any pipe or reservoir in which the Air is compressed.	Cubic feet of Air per minute (a 50° R), which may be discharged through a proper staped mouth piece, the diameter of which must be 130° inches, the are being 10° square inches.	Actual H. P. contained in the blast discharged through the month-piece described in column 3.	*Cubic feet of Air per minute that may be disclaraged with one H P., no allowance being made for friction in the blast-machine (whatever power that friction amounts to must be added). I makes no difference how the Ai is disclarged, provided the pressure is seasy, the same as given in the first column.	Number of mouth-pieces described in column 3, required to discharge one H. P. of wind, no allowance heing made for friction in the blast-machine.
1	2	3	4	5	6
14 14 14 14 15 17 18 18 19 10 11 11 12 11 11 11 11 11 11 11 11 11 11	2584,80 3657,60 4482,00 5175,00 5175,00 5175,00 7338,24 9006,42 10421,58 10421,58 13872,72 14861,16 1683,51 17533,50 18350,34 19138,26 20640,48 21360,00 22060,80 22745,40	17. 944 25. 400 31. 124 35. 98 50. 96 62. 54 72. 37 81. 08 89. 01 96. 34 103. 20 109. 69 115. 86 121. 76 127. 43 133. 90 143. 34 148. 33 153. 26	0.001224 0.003463 0.005659 0.005659 0.0058 0.0278 0.0512 0.0789 0.1106 0.1839 0.2251 0.2692 0.3652 0.4170 0.5277 0.5864 0.6473 0.7754	14662.76 7333.70 4889.11 3666.62 1833.00 1222.30 916.27 733.39 611.10 523.81 458.43 407.42 366.69 333.40 305.56 282.05 261.91 244.44 229.17 215.77 203.71 192.98 183.33	817.00 288.70 157.08 102.05 35.970 12.660 9.045 6.867 5.440 4.440 3.715 2.738 2.388 2.130 1.895 1.705 1.545
19 20	23415.00 24070.80	162.60 167.16	0.8426 0.9118	192.98 183.33	1.290 1.187 1.097

<sup>\*</sup>Always give the wind a good wide opening into the furnace or forge; see by this table how much more wind can be discharged with one H. P. at

See by this table now index more wine as a set case get with one H. F. at Dow pressure than at high.

This table shows the great advantage of large tuyeres, large pipes, large blower, and slow speed when the nature of the work will admit.

† Number of forges driven with 1.2 H. P. with Sturtevant blower.

# Engines, Fans, and Steam-coils combined for the Blower System of Heating. (Buffalo Forge Co.)

Size of Engine.	Height, in.	Speed of Engine, revs.	Capacity of Fan per Minute at 1 oz. Pressure.	Weight of Fan and Engine.	Floor-space of Fan and Engine. Inches.	Required H.P. to drive Fan.	Usual Size Heater in ft. of Pipe.	Required H.P. of Boller.
7 × 6 7 × 7 8 × 7 8 × 8	52 60 70 80 90 100 110 120 130 150 170	450 425 390 360 330 290 260 285 210 180 165	8,740 11,000 15,280 19,900 25,900 32,500 39,800 49,161 57,720 81,120 101,250	1,200 1,525 1,700 2,200 2,450 2,700 3,200 3,900 4,500 5,300 6,000	49 × 38 51 × 45 52 × 50 52 × 56 59 × 74 62 × 84 69 × 94 79 × 104 83 × 111 87 × 133 92 × 148	3.1 4.5 6 7.2 9.1 11 13.5 15 20 22	1,000 1,200 1,600 2,000 2,500 3,500 4,000 4,500 5,000 6,000	12 15 20 25 30 35 42 48 54 62 72

### The Sturtevant Steel Pressure-blower, applied to Cupola Furnaces.

Power Saved by Reducing

00 0
Press. H. P.
4 0.6
5 1.1
6 2.
7 3.3
8 5.3
10 9.4
10 12.7
12 22.5
12 31.7

<sup>\*</sup>One square inch of blast is sufficient for one forge-fire, or 90 square inches area of cupola furnaces.

The speed given is regulated so as to give the pressure of blast stated in ounces per square inch.

The term "square inches of blast" refers to the area of a proper shaped

mouth-piece discharging blast into the open air.

The melting capacity per hour in pounds of iron is made up from an average of tests on a few of the best cupolas found, and is reliable in cases where the cupolas are well constructed and driven with the greatest force of blast given in the table.

For tables of the steel pressure-blower as applied to forge-fires, and for sizes, etc., of other patterns of blowers and exhausters, see catalogue of B. F. Sturtevant Co.

(For other data concerning Cupolas, see Foundry Practice.)

### Diameter of Blast-pipes for Pressure-blowers for Cupola Furnaces and Forges. (B. F. Sturtevant Co.)

The following table has been constructed on this basis, namely: Allowing a loss of pressure of 1/2 oz. in the process of transmission through any length of pipe of any size as a standard, the increased friction due to lengthening the pipe has been compensated for by an enlargement of the pipe sufficient to keep the loss still at ½ oz. The quantities of air in the left-hand column of each division indicate the capacity of the given blower when working under pressures of 4, 8, 12, and 16 ozs. Thus a No, 6 Blower will force 2678 cubic ft. of air, at 8 oz. pressure, through 50 ft. of 12½-in, pipe, with a loss of ½ oz. pressure. If it is desired to force the air 300 ft. without an increased loss by friction, the pipe must be enlarged to 17½ in. diameter.

	BLOWER No. 1.							BLOWER	No.	6.	
of Air	Leng	ths of	Blast-p	oipe in	Feet.	of Air ed te.	Leng	ths of	Blast-p	oipe in	Feet.
Cubic Feet of transmitted per minute.	50	100	150	200	300	Subject Freet of transmitted per minute.	50	100	150	200	300
Cubic tran per	Diameter in inches.						Diameter in inches.				
360 515 635 740	53/8 63/8 63/4 71/4	61/4 71/8 73/4 81/4	634 734 8½ 9	71/4 - 81/4 9 91/2	77/8 87/8 95/8 101/4	1872 2678 3302 3848	105/8 121/4 131/4 141/8	121/8 14 151/8 161/8	1314 1518 1616 1712	137/8 16 171/6 181/2	15 1714 1876 2018
Blower No. 2.							I	BLOWER	No.	7.	
504 721 889 1036	61/4 71/4 77/8 83/8	71/8 81/4 9 91/2	73/4 9 93/4 103/8	81/4 91/2 103/8 11	87/8 101/4 11 113/4	2592 3708 4572 5328	12 137/8 151/8 16	1334 1578 1738 1812	15 1714 1878 20	157/8 181/4 197/8 211/4	17½ 19¾ 21½ 23
	В	LOWER	No. 8	l.		Blower No. 8.					
720 1030 1270 1480	714 834 918 958	814 916 1094 11	9 103/8 111/4 12	9½ 11 11% 125%	10¼ 11¾ 12¾ 12¾ 13½	3312 4738 5842 6808	13½ 15½ 165% 175%	151/8 175/8 191/8 201/4	161/2 191/3 203/4 221/8	171/4 201/8 22 233/8	1876 2176 2376 2376 2536
	· I	BLOWER	No.	1.			I	BLOWER	No.	9.	
1008 1442 1778 2072	81/4 91/4 103/8 11	93/8 107/8 117/8 125/8	10½ 11½ 12½ 12½ 13¾	10% 12½ 135% 14½	115/8 133/8 145/8 151/2	4320 6180 7620 8880	1434 17 1838 19½	17 19½ 21½ 22½	18% 21¼ 23½ 24½	198/s 221/2 243/8 26	21½ 24¾ 26½ 26½ 28½
	I	BLOWE	R No.	5.			I	BLOWE	No.	10.	
1440 2060 2540 2960	91 <u>/2</u> 11 117/6 123/4	107/8 125/8 135/8 141/2	117/8 133/4 147/8 157/8	12½ 14½ 155% 1658	133% 151/2 167/8 18	5760 8240 10160 11840	16½ 18% 20% 22½	19 2134 2334 2514	205/8 233/4 257/8 271/2	21% 251% 27% 27% 291%	2334 2714 2956 3115

Centrifugal Ventilators for Mines .- Of different appliances for ventilating mines various forms of centrifugal machines having proved their efficiency have now almost completely replaced all others. Most if not all efficiency have now simost completely replaced all others. Most if not all of the machines in use in this country are of this class, being either open-periphery fans, or closed, with chimney and spiral casing, of a more or less modified Guibal type. The theory of such machines has been demonstrated by Mr. Daniel Murgue in "Theories and Practices of Centrifugal Ventilating Machines," translated by A. L. Stevenson, and is discussed in a paper by R. Van A. Norris, Trans. A. I. M. E. xx. 637. From this paper the following formulæ are taken:

Let a = area in sq. ft. of an orifice in a thin plate, of such area that its resistance to the passage of a given quantity of air equals the resistance of the mine.

o = orifice in a thin plate of such area that its resistance to the pas-o = ornice in a tun plate of such area that its resistance to the sage of a given quantity of air equals that of the machine;
 Q = quantity of air passing in cubic feet per minute;
 V = velocity of air passing through a in feet per second;
 h = head in feet air-column to produce velocity V;
 h\_0 = head in feet air-column to produce velocity V<sub>0</sub>.

$$\begin{split} Q &= 0.65 a V; \quad V = \sqrt{2gh} \; ; \quad Q = 0.65 a \; \sqrt{2gh} \; ; \\ a &= \frac{Q}{0.65 \; \sqrt{2gh}} = \text{equivalent orifice of mine}; \end{split}$$

or, reducing to water-gauge in inches and quantity in thousands of feet per minute.

$$\alpha = \frac{.403Q}{\sqrt{W.G.}}; \quad Q = 0.650V_0; \quad V_0 = \sqrt{2gh_0}; \quad Q = 0.650\sqrt{2gh_0};$$

$$o = \sqrt{\frac{Q^2}{0.65^2h_0^2g}} = \text{equivalent orifice of machine}.$$

The theoretical depression which can be produced by any centrifugal ventilator is double that due to its tangential speed. The formula

$$H = \frac{T^2}{2g} \, - \, \frac{V^2}{2g},$$

in which T is the tangential speed, V the velocity of exit of the air from the space between the blades, and H the depression measured in feet of sirgolumn, is an expression for the theoretical depression which can be produced by an uncovered ventilator; this reaches a maximum when the air leaves the blades without speed, that is, V=0, and  $H=T^2\div 2g$ .

Hence the theoretical depression which can be produced by any uncovered ventilator is equal to the height due to its tangential speed, and one half-that which can be produced by a covered ventilator with expanding chimney.

So long as the condition of the mine remains constant:

The volume produced by any ventilator varies directly as the speed of rotation. The depression produced by any ventilator varies as the square of the

speed of rotation, For the same tangential speed with decreased resistance the quantity of

alr increases and the depression diminishes.

The following table shows a few results, selected from Mr. Norris's paper, giving the range of efficiency which may be expected under different circumstances. Details of these and other fans, with diagrams of the results are given in the paper.

Experiments on Mine-ventilating Fans.

		Exp	erimen	us or	1 MAII	ie=vei	ıtılaı	ing i	rans.		
Fan.	Revolutions per Minute, Fan.	Periphery Speed, Feet per Min.	Cubic Feet Air per Minute.	Cubic Feet Air per-Revolution	Cubical Contents of Fan-blades.	Cub. Feet Air per 100 Feet Periph- ery Motion.	Water-gauge, Inches.	Horse - power in Air.	Indicated Horse- power of Engine.	Efficiency Engine and Fan.	Equivalent Ori- fice of Mine, Square Feet.
A {	84 100 111 123	5517 6282 6973 7727	236,684 336,862 347,396 394,100	2818 3869 3130 3204	3040 3040 3040 3040	4290 5393 5002 5100	1.80 2.50 3.20 3.60	67.13 132.70 175.17 223.56	209.64	83.6	Av'ge 80
В	100 130 59	6282 8167 3702	188,888 274,876 59,587	1889 2114 1010	1520 1520 1520	3007 3366 1610	1.40	41.67	97.99 194.95	42.5	22
c {	83 40	5208 3140	82,969 49,611	1000 1240	1520 1520 3096	1593 1580	1.20 2.15 0.87	27.86 6.80	48.54 13.82	57.38	32
D }	70 50	5495 2749	137,760 147,232 205,761	1825 2944	3096 1522	2507 5356	2.55 0.50	55.35 11.60	67.44 28.55	82.07 40.63	
E	69 96 200	8793 5278 7540	205,761 299,600 133,198	2982 3121 666	1522 1522 746	5451 5676 1767	1.00 2.15 3.35	32.42 101.50 70.30	45.98 120.64 102.79	84.10	83 26.9
F	200 200 200	7540 7540	180,809 209,150	904 1046	746 746	2398 2774	3.05 2.80	86.89 92.50	129.07	67.30	38.3 46.3
	10	785 1570	28,896 57,120	2890 2856	3022 3022	3680 3637	0.10	0.45 1.80	1.30 3.70	35. 49.	1010
- ()	20 25 30 35	1962 2355 2747	66,640 73,080 94,080	2665 2436 2688	3022 3022 3022	3399 3103 3425	0.29 0.40 0.50	2.90 4.60 7.40	6.10 9.70 15.00	47.	52
G {	40 50	3140 3925	112,000 132,700	2800 2654	3022 3022	3567 3381	0.70	12.30 18.80	24.90 38.80	49. 48.	
	60 70 80	4710 5495 6280	173,600 203,280 222,320	2898 2904 2779	3022 3022 3022	3686 3718 3540	1.85 1.80 2.25	36.90 57.70	66 40	55. 54.	
		vne of		2119	Diam	Wid		o Inle		iam 1	Inlote

[ 80   6280   222,820   2779 ]	8022	3540   2.2	25   78.50   152	.60/52. 1
Type of Fan.	Diam.	Width.	No. Inlets.	Diam. Inlets.
A. Guibal, double	20 ft.	6 ft.	4	8 ft. 10 in.
B. Same, only left hand running.	20	6	4	8 10
C. Guibal	20	6	2	8 10
D. Guibal		8	1	11 6
E. Guibal, double	171/2	4	4	8
		10	2	7
G. Guibal	25	8	1	12

An examination of the detailed results of each test in Mr. Norris's table shows a mass of contradictions from which it is exceedingly difficult to draw any satisfactory conclusions. The following, he states, appear to be more or less warranted by some of the figures:

any sanstactory concusions. The following, he states, appear to be more or less warranted by some of the figures:

1. Influence of the Condition of the Airways on the Fan.—Mines with varying equivalent orlices give air per 100 feet periphery-motion of fan, witkin limits as follows, the quantity depending on the resistance of the mine:

Equivalent Orifice.	Cu. Ft. Air per 100 ft. Periphery- speed.	Aver- age.		Cu. Ft. Air per 100 ft. Periphery- speed.	Aver- age.
Under 20 sq. ft 20 to 30 30 to 40 40 to 50	t. 1100 to 1700 1800 to 1800 1500 to 2500 2300 to 3500	1300 1600 2100 2700	60 to 70 70 to 80 80 to 90 90 to 100	3300 to 5100 4000 to 4700 3000 to 5600	4000 4400 4800
50 to 60	2700 to 4800	3500	100 to 114	5200 to 6200	5700

The influence of the mine on the efficiency of the fan does not seem to be very clear. Eight fans, with equivalent orifices over 50 square feet, give

efficien. les over 70%; four, with smaller equivalent mine-orifices, give about the same figures; while, on the contrary, six fans, with equivalent orifices of over 50 square feet, give lower efficiencies, as do ten fans, all drawing from mines with small equivalent orifices.

It would seem that, on the whole, large airways tend to assist somewhat

in attaining large efficiency

2. Influence of the Diameter of the Fan, - This seems to be practically nil, the only advantage of large fans being in their greater width and the lower speed required of the engines

3. Influence of the Width of a Fan.—This appears to be small as regards the efficiency of the machine; but the wider faus are, as a rule, exhausting

more air.

more air.

4. Influence of Shape of Blades.—This appears, within reasonable limits, to be practically nil. Thus, six fans with this of blades curved forward, three fans with flat blades, and one with blades curved back to a tangent with the circumference, all give very high efficiencies—over 70%.

5. Influence of the Shape of the Spiral Casing,—This appears to be considerable. The shapes of spiral casing in use fall into two classes, the first presenting a large spiral, beginning at or near the point of cut-off, and the second a circular casing reaching around three quarters of the circumterence

of the fan, with a short spiral reaching to the evasée chimney. Fans having the first form of casing appear to give in almost every case

large efficiencies.

Fans that have a spiral belonging to the first class, but very much con-tracted, give only medium efficiencies. It seems probable that the prope-shape of spiral casing would be one of such form that the air between each pair of blades could constantly and freely discharge into the space between the fan and casing, the whole being swept along to the evasée chimney. This would require a spiral beginning near the point of cut-off, enlarging by gradually increasing increments to allow for the slowing of the air caused by its friction against the casing, and reaching the chimney with an area such that the air could make its exit with its then existing speed-somewhat less than the periphery-speed of the fan.

6. Influence of the Shutter.—This certainly appears to be an advantage, as

by it the exit area can be regulated to suit the varying quantity of air given by the fan, and in this way re-entries can be prevented. It is not uncommon to find shutterless fans into the chimneys of which bits of paper may be dropped, which are drawn into the fan, make the circuit, and are again thrown out. This peculiarity has not been noticed with fans provided with

Influence of the Speed at which a Fan is Run.—It is noticeable that most of the fans giving high efficiency were running at a rather high periphery velocity. The best speed seems to be between 5000 and 6000 feet per minute.

The fans appear to reach a maximum efficiency at somewhere about the speed given, and to decrease rapidly in efficiency when this maximum point

is passed.

In discussion of Mr. Norris's paper, Mr. A. H. Storrs says; From the "cu-ble feet per revolution" and "cubical contents of fan-blades," as given in the table, we find that the enclosed fans empty themselves from one half to twice per revolution, while the open fans are emptied from one and three-quarter to nearly three times. This for fans of both types, on mines cover-ing the same range of equivalent orifices. One open fan, on a very large orifice, was emptied nearly four times, while a closed fam, on a still larger orifice, only shows one and one-half times. For the open fans the "cubic feet per 100 ft, motion" is greater, in proportion to the fan width and equivalent orifice, than for the enclosed type. Notwithstanding this apparently free discharge of the open fans, they show very low efficiencies.

As illustrating the very large capacity of centrifugal fans to pass air, if the conditions of the mine are made favorable, a 16-ft. diam. fan, 4 ft. 6 in.

wide, at 180 revolutions, passed 360,000 cu. ft. per min., and another of same dimeter, but slightly wider and with larger intake circles, passed 500,000 cu. ft, the water-gauge in both instances being about ½ in.

1. D. Jones says: The efficiency reported in some cases by Mr. Norris is larger than I have ever been able to determine by experiment. My own experiments, recorded in the Pennsylvania Mine Inspectors' Reports from 1875 to 1881, did not show more than 60% to 65%.

### DISK FANS.

Experiments made with a Blackman Disk Fan, 4 ft. diam, by Geo. A. Suter, to determine the volumes of air delivered under various conditions, and the power required; with calculations of efficiency and ratio of increase of power to increase of velocity, by G. H. Babcock. (Trans. A. S. M. E., vii. 547):

Rev. per min.	Cu. ft. of Air delivered per min.,	Horse-power,	Water- gauge, in., h.	Ratio of In- crease of Speed.	Ratio of Increase of Delivery.	Ratio of In- crease of Power.	Exponent $x$ , $HP \propto V^x$ .	Exponent $y$ , $h \propto V^y$ .	Efficiency of Fan.
350 440 534 612	25,797 82,575 41,929 47,756 For	0.65 2.29 4.42 7.41 series		1.257 1.186 1.146 1.749	1.262 1.287 1.139 1.851	3.523 1.843 1.677 11.140	5.4 2.4 3.97 4.		1.682 .9553 1.062 .9358
340 453 536 627	20,372 26,660 31,649 36,543 For	0.76 1.99 3.86 6.47 series		1.332 1.183 1.167 1.761	1.308 1.187 1.155 1.794	2.618 1.940 1.676 8.513	3.55 3.86 3.59 3.63		.7110 .6063 .5205 .4802
340 430 534 570	9,983 13,017 17,018 18,649 For	1.12 3.17 6.07 8.46 series	0.28 0.47 0.75 0.87	1.265 1.242 1.068 1.676	1.304 1.307 1.096 1.704	2.837 1.915 1.394 7.554	3.93 2.25 3.63 3.24	1.95 1.74 1.60 1.81	.3939 .3046 .3319 .3027
830 437 516	8,399 10,071 11,157 For	1.31 3.27 6.00 series	0.26 0.45 0.75	1.324 1.181 1.563	1.199 1.108 1.329	3.142 1.457 4.580	6.31 3.66 5.35	3.06 4.96 3.72	.2631 .2188 .2202

Nature of the Experiments.—First Series: Drawing air through 30 ft. of 48-in. diam. pipe on inlet side of the fan.

Second Series: Forcing air through 30 ft. of 48-in. diam. pipe on outlet side of the fan.

Third Series: Drawing air through 30 ft. of 48-in, pipe on inlet side of the fan—the pipe being obstructed by a diaphragm of cheese-cloth.

Fourth Series: Forcing air through 30 ft. of 48-in, pipe on outlet side of fan

—the pipe being obstructed by a diaphragm of cheese cloth.

Mr. Babcock says concerning these experiments: The first four experiments are evidently the subject of some error, because the efficiency is such

ments are evidently the subject of some error, because the efficiency is such as to prove on an average that the fan was a source of power sufficient to overcome all losses and help drive the engine besides. The second series is questionable, but still the efficiency in the first two experiments is larger than might be expected. In the third and fourth series the resistance of the cheese-cloth in the pipe reduces the efficiency largely, as would be expected. In this case the value has been calculated from the height equivalent to the

water-pressure, rather than the actual velocity of the air.

This record of experiments made with the disk fan shows that this kind of fan is not adapted for use where there is any material resistance to the flow of the air. In the centrifugal fan the power used is nearly proportioned to the amount of air moved under a given head, while in this fan the power required for the same number of revolutions of the fan increases very materially with the resistance, notwithstanding the quantity of air moved is at the same time considerably reduced. In fact, from the inspection of the third and fourth series of tests, it would appear that the power required is very nearly the same for a given pressure, whether more or less air be in motion. It would seem that the main advantage, if any, of the disk fan over the centrifugal fan for slight resistances consists in the fact that the delivery is the full area of the disk, while with centrifugal fans intended to move the same quantity of air the opening is much smaller.

It will be seen by columns 8 and 9 of the table that the power used increased much more rapidly than the cube of the velocity, as in centrifugal fans. The different experiments do not agree with each other, but a general average may be assumed as about the cube root of the eleventh power.

### Cubic Feet of Air removed by Exhaust Disk-wheel per minute. (Buffalo Forge Co.)

Number	Diameter of Wheel.												
of Revo- lutions of Wheel	24 Inch.	30 Inch.	36 Inch.	42 Inch.	48 Inch.	54 Inch.	60 Inch.	72 Inch.					
per minute.		Amount of Air in cubic feet per minute.											
100		2,696 3,338 4,042 4,808 5,636	3,594 4,541 5,550 6.621 7,755 8,950	5,607 7,079 8,621 10,233 11,915 13,967	4,245 6,405 8,686 11,098 13,641 16,315 19,119 22,055	6,059 9,154 12,410 15,822 19,408 23,147 27,048 31,112	*8,387 12,822 17,457 22,292 27,327 32,565 37,997 43,632	14,936 22,926 31,267 39,956 48,996 58,386 67,985 76,900					
500 550 600		6,516 7,446 8,426 9,456	10,210 11,430 12,816 14,265	15,489 17,381 19,345 21,375	25,127 28,325 31,518 34,310	35,338 39,727 44,277 48,992	49,467 55,152 60,401	10,500					
700		10,536	15,776	23,420	36,940	53,858							

Efficiency of Disk Fans, -- Prof. A. B. W. Kennedy (Industries, Jan. 17, 1890) made a series of tests on two disk fans, 2 and 3 ft. diameter, known as the Verity Silent Air-propeller. The principal results and conclusions

are condensed below

In each case the efficiency of the fan, that is, the quantity of air delivered per effective horse power, increases very rapidly as the speed diminishes, so that lower speeds are much more economical than higher ones. On the other hand, as the quantity of air delivered per revolution is very nearly constant, the actual useful work done by the fan increases almost directly with its speed. Comparing the large and small fans with about the same air delivery, the former (running at a much lower speed, of course) is much the more economical. Comparing the two fans running at the same speed, however, the smaller fan is very much the more economical. The delivery of air per revolution of fan is very nearly directly proportional to the area of the fan's diameter.

The air delivered per minute by the 3-ft, fan is nearly 12.5R cubic feet (R being the number of revolutions made by the fan per minute). For the 2-ft. fan the quantity is 5.7R cubic feet. For either of these or any other similar fans of which the area is A square feet, the delivery will be about 1.84R cubic feet. Of course any change in the pitch of the blades might

entirely change these figures.

The net H.P. taken up is not far from proportional to the square of the number of revolutions above 100 per minute. Thus for the 3-ft. fan the net  $(R - 100)^2$  $(R - 100)^2$ 200,000, while for the 2-ft. fan the net H.P. is H.P. is

1,000,000

The denominators of these two fractions are very nearly proportional inversely to the square of the fan areas or the fourth power of the fan diameters. The net H.P. required to drive a fan of diameter D feet or area A square feet, at a speed of R revolutions per minute, will therefore be approximately  $D^4(R-100)^2$  or  $A^2(R-100)^2$ . proximately or

17,000,000 10,400,000

The 2-ft. fan was noiseless at all speeds. The 3-ft. fan was also noiseless up to over 450 revolutions per minute.

		ropelle ft. dia		Propeller, 3 ft. diam.		
Speed of fan, revolutions per minute.	750	676	577	576	459	373
Net H.P. to drive fan and belt	0.42	0.32	0.227	1.02	0.575	0.324
Cubic feet of air per minute Mean velocity of air in 3-ft, flue, feet	4,183	3,830	3,410	7,400		
per minute	593	543	482	1,046	820	632
diameter as fan	1,330	1,220	1.085			
Cu.ft.of air per min.per effective H.P.	9,980	11.970		7.250	10,070	13.800
Motion given to air per rev. of fan, ft.	1.77				1.79	
Cubic feet of air per rev. of fan					12.6	

POSITIVE ROTAR	X B	LO	WE	RS.	(P.	н. &	F. M.	Root	s.)
Size number	1/4	1/6	1	2	3	4	5	6	7
Cubic feet per revolution	3/4	11/2 250	3	. 5	8	13	23	42	65
Revolutions per minute,	(300	250	225	200	175	150	125	100	75
Smith fires	to	to	to	to	to	to	to	to	to
bilital files	350	300	275	250	225	200	175	150	125
Furnishes blast for Smith	( 2	6	10	16	24	32	47	70	80
	to	to	to	to	to	to	to	to	to
fires	4	8	14	20	30	43	67	100	135
Descriptions was adverse for	( ·		275	275	200	185	170	150	137
Revolutions per minute for	?		to	to	to	to	to	to	to
cupola, melting iron	l		375	325	300	275	250	200	175
Size of cupola, inches, in-			18	24	30	36	42	50	72
	?		to	to	to	to	to	to	OF
side lining	1		24	30	36	42	50	60	2-55's
	(		11/2	21/2	3	42/3	8	121/6	17%
Will melt iron per hour, tous-	?		tõ	to	to	to	to	tõ	to
	1		2	3	42/3	7	12	16%	222/3
Horse-power required	1	2	31/6	516	8	111/6	173/	27	40

The amount of iron melted is based on 30,000 cubic feet of air per ton of iron. The horse-power is for maximum speed and a pressure of ¾ pound, ordinary cupola pressure. (See also Foundry Practice.)

### BLOWING-ENGINES.

# Blast-furnace Blowing-engines of the Variable Puppetvalve Cut-off Type. (Philada. Engineering Works.)

three cut of Ziper (I made Engineering World)												
Diameter of Steam- cylinder.	Diameter of Blowing- cylinder.	Stroke.	Shop Weights, approxi- mate.	Revolu- tions, ordinary speed.	Displace- ment of Piston per minute at ordinary speed.	Maximum Blast-pres- sure for Reg- ular Work.						
in.	in,	in.	pounds.		cubic feet.	lbs. per sq.in.						
28	66	36	80,000	60	8,550	10						
28	66	48	90,000	50	9,500	10						
32	72	48	106,000	50	11,308	12						
36	72	48	130,000	50	11,308	15						
36	84	48	140,000	50	15,392	11						
36	84	60	165,000	40	15,392	11						
42	84	48	165,000	50	15,392	15						
42	84	60	190,000	40	15,392	15						
	90	48	170,000	50	17,700	13						
42	90	60	195,000	40	17,700	13						
48	96	48	220,000	50	20,000	15						
42 42 48 48	96	60	280,000	40	20,000	15						

The blowing-engines of the country are usually very wasteful of steam by reason of wire-drawing valve-gear, and especially of slow piston-speed. The latter is perhaps the greatest and the least recognized of all steamengine defects. Almost any expense to increase the economy of blowingengines is warranted. (A. L. Holley, Trans. A. I. M. E., vol. iv. p. 81. The calculations of power, capacity, etc., of blowing-engines are the same as those for air-compressors. They are built without any provision for cooling the air during compression. About 400 feet per minute is the usual piston-speed for recent forms of engines, but with positive air-valves, which have been introduced to some extent, this speed may be increased. The efficiency of the engine, that is, the ratio of the LHL, of the air-cylinder to that of the steam cylinder, is usually taken at 40 per cent, the losses by friction, leakage, etc., being taken at 10 per cent.

# STEAM-JET BLOWER AND EXHAUSTER.

A blower and exhauster is made by L. Schutte & Co., Philadelphia, on the principle of the steam-jet ejector. The following is a table of capacities:

Size No.	Quantity of Air per hour	Dinog in	eter of inches.	Size No.	Quantity of Air per hour	Diameter of Pipes in inches.		
No.	cubic feet.	Steam.	Air.	No.	cubic feet,	Steam.	Air.	
000 00 0 1 2 3 4	1,000 2,000 4,000 6,000 12,000 18,000 24,000	1/2 3/4 1 11/4 11/2 2 2	1 11/2 2 21/2 3 31/2 4	5 6 7 8 9 10	30,000 36,000 42,000 48,000 54,000 60,000	21/2 21/2 3 3 31/2 31/2	5 6 6 7 7 8	

The admissible vacuum and counter pressure, for which the apparatus is constructed, is up to a rarefaction of 20 inches of mercury, and a counterpressure up to one sixth of the steam-pressure.

The table of capacities is based on a steam-pressure of about 60 lbs., and a counter-pressure of about 8 lbs. With an increase of steam-pressure or decrease of counter-pressure the capacity will largely increase.

Another steam-jet blower is used for boile-firing, ventilation, and similar

purposes where a low counter-pressure or rarefaction meets the requirements.

The volumes as given in the following table of capacities are under the supposition of a steam-pressure of 45 lbs, and a counter-pressure of say. 2 inches of water :

Size No,	Cubic feet of Air delivered per hour.	Diameter of Steam- pipe in inches,	inche	eter in es of— Disch.	Size No.	Cubic feet of Air de- livered per hour	of Steam- pipe in	inche	eter in s of—.
00 0 1 2 3	6,000 12,000 30,000 60,000 125,000	3/6 1/2 1/2 3/4 1	4 5 8 11 14	3 4 6 8 10	4 6 8 10	250,000 500,000 1,000,000 2,000,000	1 11/4 11/2 2	17 24 32 42	14 20 27 36

The Steam-jet as a Means for Ventilation,-Between 1810 and 1850 the steam-jet was employed to a considerable extent for ventilating English collieries, and in 1852 a committee of the House of Commons reported that it was the most powerful and at the same time the cheapest method for the ventilation of mines; but experiments made shortly afterwards proved that this opinion was erroneous, and that furnace ventilation

wards proved that this opinion was erroneous, and that furnace ventilation was less than half as expensive, and in consequence the jet was soon abandoned as a permanent method of ventilation.

For an account of these experiments see Colliery Engineer, Feb. 1890, The jet, however, is sometimes advantageously used as a substitute, for instance, in the case of a fan standing for repairs, or after an explosion, when the furnace may not be kept going, or in the case of the fan having become acceptable lates.

been rendered useless.

# HEATING AND VENTILATION.

Ventilation. (A. R. Wolff, Stevens Indicator, April, 1890.)—The popular impression that the impure air falls to the bottom of a crowded room is erroneous. There is a constant mingling of the fresh air admitted with the impure air due to the law of diffusion of gases, to difference of temperthe impure air due to the law of diffusion of gases, to difference of temperature, etc. The process of ventilation is one of dilution of the impure air by the fresh, and a room is properly ventilated in the opinion of the hygienists when the dilution is such that the carbonic acid in the air does not exceed from 6 to 8 parts by volume in 10,000. Pure country air contains about 4 parts CO<sub>2</sub> in 10,000, and badly-ventilated quarters as high as 80 parts. An ordinary man exhales 0.6 of a cubic foot of CO<sub>2</sub> per hour. New York gas gives out 0.75 of a cubic foot of CO<sub>3</sub> per each cubic foot of gas burnt. An ordinary lamp gives out 1 cu. ft. of CO<sub>3</sub> per hour. An ordinary candle gives out 0.3 cu. ft. per hour. One ordinary gaslight equals in vitating effect about 5½ men, an ordinary candle ½ effect about 5½ men, an ordinary candle ½

man. To determine the quantity of air to be supplied to the inmates of an unlighted room, to dilute the air to a desired standard of purity, we can establish equations as follows:

Let v = cubic feet of fresh air to be supplied per hour;
r = cubic feet of CO<sub>2</sub> in each 10,000 cu. ft. of the entering air;
R = cubic feet of CO<sub>2</sub> which each 10,000 cu. ft. of the air in the room may contain for proper health conditions;
n = number of persons in the room;
6 = cubic feet of CO<sub>2</sub> exhaled by one man per hour.

Then  $\frac{v \times r}{10,000} + .6n$  equals cubic feet of CO<sub>2</sub> communicated to the room during one hour.

This value divided by v and multiplied by 10,000 gives the proportion of  $CO_2$  in 10,000 parts of the air in the room, and this should equal R, the standard of purity desired. Therefore

$$R = \frac{10,000 \left[ \frac{v \times r}{10,000} + .6n \right]}{v}, \text{ or } v = \frac{6000n}{R - r}. \quad . \quad . \quad . \quad . \quad (1)$$

If we place 
$$r$$
 at 4 and  $R$  at 6,  $v = \frac{6000}{6-4}n = 3000n$ , . . . . . . . (2)

or the quantity of air to be supplied per person is 3000 cubic feet per hour. If the original air in the room is of the purity of external air, and the cubic contents of the room is equal to 100 cu. ft. per inmate, only 3000 – 100 = 2900 cu. ft. of fresh air from without will have to be supplied the first hour to keep the air within the standard purity of 6 parts of  $CO_2$  in 10,000. If the cubic contents of the room equals 200 cu. ft. per inmate, only 3000 – 200 = 2000 cu. ft. will have to be supplied the first hour to keep the air within the standard purity, and so on.

Again, if we only desire to maintain a standard of purity of 8 parts of carbonic acid in 10,000, equation (1) gives as the required air-supply per hour

$$v = \frac{6000}{8 - 4}n = 1500n$$
, or 1500 cu. ft. of fresh air per inmate per hour.

Cubic feet of air containing 4 parts of carbonic acid in 10,000 necessary per person per hour to keep the air in room at the composition of

If the original air in the room is of purity of external atmosphere (4 parts of carbonic acid in 10,000), the amount of air to be supplied the first hour, for given cubic spaces per immate, to have given standards of purity not exceeded at the end of the hour is obtained from the following table: Proportion of Carbonic Acid in 10,000 Parts of the Air, not to he Exceeded at End of Hour

Cubic Feet of	be Exceeded at End of Hour,							
Space in Room	6	7	8	9	10	15	20	
Individual.	Cubic Feet of Air, of Composition 4 Parts of Carbonic Acid in 10,000, to be Supplied the First Hour.							
100 200 300 400 500 600	2900 2800 2700 2600 2500 2400	1900 1800 1700 1600 1500 1400	1400 1300 1200 1100 1000 900	1100 1000 900 800 700 600	900 800 700 600 500 400	445 345 245 145 45 None	275 175 75 None	
700 800 900 1000 1500	2300 2200 2100 2000 1500	1300 1200 1100 1000 500	800 700 600 500 None	500 400 300 200 None	300 200 100 None			

It is exceptional that systematic ventilation supplies the 3000 cubic feet per inmate per hour, which adequate health considerations demand. Large auditoriums in which the cubic space per individual is great, and in which the atmosphere is thoroughly fresh before the rooms are occupied, and the occupancy is of two or three hours' duration, the systematic air supply may be reduced, and 2000 to 2500 cubic feet per inmate per hour is a satisfactory allowance

Hospitals where, on account of unhealthy excretions of various kinds, the air-dilution must be largest, an air-supply of from 4000 to 6000 cubic feet per inmate per hour should be provided, and this is actually secured in some hospitals. A report dated March 15, 1882, by a commission appointed to examine the public schools of the District of Columbia, says:

2500

500

"In each class-room not less than 15 square feet of floor-space should be allotted to each pupil. In each class-room the window-space should not be less than one fourth the floor-space, and the distance of desk most remote from the window should not be more than one and a half times the height of the top of the window from the floor. The height of the class-room should never exceed 14 feet. The provisions for ventilation should be such as to provide for each person in a class-room not less than 30 cubic feet of fresh air per minute (1800 per hour), which amount must be introduced and thoroughly distributed without creating unpleasant draughts, or causing any two parts of the room to differ in temperature more than 2° Fahr., or the maximum temperature to exceed 70° Fahr."

When the air enters at or near the floor, it is desirable that the velocity of inlet should not exceed 2 feet per second, which means larger sizes of register openings and fines than are usually obtainable, and much higher velocities of inlet than two feet per second are the rule in practice. The velocity of current into vent-flues can safely be as high as 6 or even 10 feet

per second, without being disagreeably perceptible.

The entrance of fresh air into a room is co-incident with, or dependent on, the removal of an equal amount of air from the room. The ordinary means of removal is the vertical vent-duct, rising to the top of the building. Sometimes reliance for the production of the current in this vent-duct is placed solely on the difference of temperature of the air in the room and that of the external atmosphere; sometimes a steam coil is placed within the flue near its bottom to heat the air within the duct; sometimes steam pipes (risers and returns) run up the duct performing the same functions; or steam jets within the flue, or exhaust fans, driven by steam or electric power, act directly as exhausters; sometimes the heating of the air in the flue is accomplished by gas-jets. The draft of such a duct is caused by the difference of weight of the

heated air in the duct, and a column of equal height and cross-sectional area of weight of the external air.

Let d = density, or weight in pounds, of a cubic foot of the external air. Let  $d_1$  = density, or weight in pounds, of a cubic foot of the heated air

within the duct.

Let h = vertical height, in feet, of the vent-duct,  $h(d - d_1) = \text{the pressure}$ , in pounds per square foot, with which the air is forced into and out of the vent-duct.

This pressure can be expressed in height of a column of the air of density within the vent-duct, and evidently the height of such column of equal presssure would be  $h(d-d_1)$ 

Or, if t = absolute temperature of external air, and  $t_1 =$  absolute temperature of the air in vent-duct in the form, then the pressure equals

$$\frac{h(t_1-t)}{t}. \qquad (4)$$

The theoretical velocity, in feet per second, with which the air would travels through the vent-duct under this pressure is

The actual velocity will be considerably less than this, on account of loss The actual velocity will be considerably less than this, on account of loss due to friction. This friction will vary with the form and cross-sectional area of the vent-duct and its connections, and with the degree of smoothness of its interior surface. On this account, as well as to prevent leakage of air through crevices in the wall, tin lining of vent-flues is desirable.

The loss by friction may be estimated at approximately 50%, and so we find for the actual velocity of the air as it flows through the vent-duct:

$$v=\frac{1}{2}\sqrt{2gh\frac{(t_1-t)}{t}},$$
 or, approximately,  $v=4\sqrt{h\frac{(t_1-t)}{t}}$  . . . (6

If V = velocity of air in vent-duct, in feet per minute, and the external air be at 32° Fahr., since the absolute temperature on Fahrenheit scale equals thermometric temperature plus 459.4,

$$V = 240 \sqrt{h \frac{(t_1 - t)}{491.4}}, \dots$$
 (7)

from which has been computed the following table:

Quantity of Air, in Cubic Feet, Discharged per Minute through a Ventilating Duct, of which the Cross-sec-tional Area is One Square Foot (the External Temperature of Air being 32° Fahr.).

Excess of Temperature of Air in Vent-duct above that of Height of External Air. Vent-duct in feet. 25° 50° 100° 150° 

Multiplying the figures in above table by 60 gives the cubic feet of air discharged per hour per square foot of cross-section of vent-duct. Knowing the cross-sectional area of vent-ducts we can find the total discharge; or for a desired air-removal, we can proportion the cross-sectional area of

vent-ducts required

Artificial Cooling of Air for Ventilation. (Engineering News, July 7, 1892.)—A pound of coal used to make steam for a fairly effi-News, July 7, 1892.—A pound of coal used to make steam for a fairly effi-cient refrigerating-machine can produce an actual cooling effect equal to that produced by the melting of 16 to 46 lbs. of ice, the amount varying with the conditions of working. Or, 855 heat-units per lb, of coal converted into work in the refrigerating plant (at the rate of 3 lbs. coal per horse-power hour) will abstract 2275 to 655 heat-units of heat from the refrige-tated body. If we allow 2000 cu, ft. of fresh air per hour per person as suffiated body. If we allow 2000 cu, it, of fresh air per hour per person as sumicent for fair ventilation, with the air at an initial temperature of  $80^\circ$  F, its weight per cubic foot will be .0736 lb.; hence the hourly supply per person will weigh 2000  $\times$  .0736 lb. = 147.2 lb. To cool this  $10^\circ$ , the specific heat of air being 0.238, will require the abstraction of  $147.2 \times 0.238 \times 10 = 350$  heat-units per person per hour.

Taking the figures given for the refrigerating effect per pound of coal as

above stated, and the required abstraction of 350 heat-units per person per hour to have a satisfactory cooling effect, the refrigeration obtained from a pound of coal will produce this cooling effect for  $2275 \div 350 = 6\frac{1}{2}$  hours with the least efficient working, or 6545 + 350 = 18.7 hours with the most efficient working. With ice at \$5 per ton, Mr. Wolff computes the cost of cooling with ice at about \$5 per hour per thousand persons, and concludes that this is too expensive for any general use. With mechanical refrigeration, however, if expensive for any general use. With International refrigeration, however, if we assume 10 hours' cooling per person per pound of coal as a fair practical service in regular work, we have an expense of only 15 cts, per thousand persons per hour, coal being estimated at \$\$ per short ton. This is for fuel alone, and the various items of oil, attendance, interest, and depreciation on the plant, etc., must be considered in making up the actual total cost of mechanical refrigeration.

Mine-ventilation-Friction of Air in Underground Passages. - In ventilating a mine or other underground passage the resistance to be overcome is, according to most writers on the subject, proportional to the extent of the frictional surface exposed; that is, to the product to of the length of the gangway by its perimeter, to the density of the air in circulation, to the square of its average speed, a, and lastly to a coefficient k, whose numerical value varies according to the nature of the sides of the gangway

and the irregularities of its course.

The formula for the loss of head, neglecting the variation in density as unimportant, is  $p = \frac{ksv^2}{a}$ , in which  $p = \log s$  of pressure in pounds per square

foot, s =square feet of rubbing-surface exposed to the air, v the velocity of foot, s = square feet obrubbing surface exposed to the air, it the velocity of the air in feet per minute, a the area of the passage in square feet, and k the coefficient of friction. W. Fairley, in Colliery Engineer, Oct. and Nov. 1893, gives the following formula for all the quantities involved, using the same notation as the above, with these additions: h = horse-power of ventilation; l = length of air-channel; o = perimeter of air-channel; o = quantity of air circulating in cubic feet per minute; n = units of work. In foot-pounds, applied to circulate the air: w = water-gauge in inches. Then,

1. 
$$a = \frac{ksv^2}{p} = \frac{ksv^2}{u} = \frac{ksv^3}{pv} = \frac{u}{pv} = \frac{q}{v}$$
.  
2.  $h = \frac{u}{33,000} = \frac{q}{33,000} = \frac{5}{33,000}$ .  
3.  $k = \frac{pa}{sv^2} = \frac{u}{sv^3} = \frac{p}{sv^2 + a} = \frac{5.2w}{sv^2 + a}$ .  
4.  $l = \frac{s}{o} = \frac{pa}{kv^2o}$ .  
5.  $o = \frac{s}{l} = \frac{pa}{kv^2l}$ .  
6.  $p = \frac{ksv^2}{u} = \frac{u}{a} = 5.2w = \left(\sqrt{\frac{u}{k}}\right)^2 \frac{ks}{a} = \frac{ksv^3}{a} = \frac{u}{av}$ .

7. 
$$pa = ksv^2 = \left(\sqrt[3]{\frac{u}{ks}}\right)^2 ks = \frac{u}{v}; \quad pa^3 = ksq^2.$$
8.  $q = va = \frac{u}{p} = \frac{ksv^3}{p} = \sqrt{\frac{pa}{ks}} a = \sqrt{\frac{u}{ks}} a.$ 
9.  $s = \frac{pa}{kv^2} = \frac{u}{kv^3} = \frac{qp}{kv^3} = \frac{vpa}{kv^3} = lo.$ 
10.  $u = qp = vpa = \frac{ksv^2q}{a} = ksv^3 = 5.2qw = 33,000h.$ 
11.  $v = \frac{u}{pa} = \frac{q}{a} = \sqrt[3]{\frac{u}{ks}} = \sqrt[3]{\frac{qp}{ks}} = \sqrt{\frac{pa}{ks}}.$ 
12.  $v^2 = \frac{pa}{ks} = \left(\sqrt[3]{\frac{u}{ks}}\right)^2.$ 
13.  $v^3 = \frac{u}{ks} = \frac{qp}{ks} = \frac{vpa}{ks}.$ 
14.  $w = \frac{p}{ks} = \frac{ksv^2}{ks^2}$ 

To find the quantity of air with a given horse-power and efficiency (e) of engine:

 $q = \frac{h \times 33,000 \times e}{n}$ .

The value of k, the coefficient of friction, as stated, varies according to the nature of the sides of the gangway. Widely divergent values have been given by different authorities (see Colliery Engineer, Nov. 1833), the most generally accepted one until recently being probably that of J. J. Atkinson, 0000000217, which is the pressure per square foot in decimals of a pound for each square foot of rubbing-surface and a velocity of one foot per minute. Mr. Fairley, in his "Theory and Practice of Ventilating Coal-mines," gives a value less than half of Atkinson's, or .00000001; and recent experiments by D. Murgue show that even this value is high under most conditions. Murgue's results are given in his paper on Experimental Investigations in the Loss of Head of Air-currents in Underground Workings, Thans. A, I. M. E., 1833, vol. xxiii, 63. His coefficients are given in the following table, as determined in twelve experiments:

		Coefficier	at of Loss of
		Head b	y Friction.
		French.	British.
	(Straight, normal section	.00092	.000,000,00486
Rock.	Straight, normal section	.00094	.000,000,00497
gangways.	Straight, large section		.000,000,00549
8 0	Straight, normal section	.00122	.000,000,00645
	(Straight, normal section	.00030	.000,000,00158
Brick-lined	Straight, normal section	.00036	.000,000,00190
arched	Continuous curve, normal section	.00062	.000,000,00328
gangways.	Sinuous, intermediate section	.00051	.009,000,00269
8	(Sinuous, small section		.000,000,00291
(TV)	(Straight, normal section	.00168	.000,000,00888
Timbered	₹ Straight, normal section	.00144	.000,000,00761
gangways.	Slightly sinuous, small section	.00238	.000,000,01257

The French coefficients which are given by Murgue represent the height of water-gauge in millimetres for each square metre of rubbing-surface and a velocity of one metre per second. To convert them to the British measure of pounds per square foot for each square foot of rubbing-surface and a velocity of one foot per minute they have been multiplied by the factor of conversion, 00005283. For a velocity of 1000 feet per minute, since the loss of head varies as  $v^2$ , move the decimal point in the coefficients six places to the right.

Equivalent Orifice. The head absorbed by the working-chambers Equivalent Offines,—Include a priori, because the openings, cross-passages, irregular-shaped gob-piles, and daily changes in the size and shape of the chambers present much too complicated a network for accurate analysis. In order to overcome this difficulty Murgue proposed in 1872 the method of equivalent orifice. This method consists in substituting for the mento of equivarent origine. This method consists in substituting for the mine to be considered the equivalent thin-lipped orifice, requiring the same height of head for the discharge of an equal volume of air. The area of this orifice is obtained when the head and the discharge are known, by means of the following formulæ, as given by Fairley:

Let Q = quantity of air in thousands of cubic feet per minute;

w = inches of water-gauge;

A = area in square feet of equivalent orifice.

$$A = \frac{0.37Q}{\sqrt{w}} = \frac{Q}{2.7\sqrt{w}}; * Q = \frac{A \times \sqrt{w}}{0.37}; w = 0.1369 \times \left(\frac{Q}{A}\right)^{2}.$$

Motive Column or the Head of Air Due to Differences of Temperature, etc. (Fairley.) Let M= motive column in feet;

T =temperature of upcast;

f = weight of one cubic foot of the flowing air;

t = temperature of downcast;

D = depth of downcast.

$$\label{eq:mass_mass_mass_mass_mass} \mathit{M} = D \; \frac{T-t}{T \times 459} \; \text{ or } \; \frac{5.2 \times w}{f}; \; \; p = f \times \mathit{M}; \; \; w = \frac{f \times \mathit{M}}{5.2} = \frac{\mathit{p}}{5.2}.$$

To find diameter of a round airway to pass the same amount of air as a square airway the length and power remaining the same: Let D= diameter of round airway, A= area of square airway; O= perimeter of square airway. Then  $D^3=\sqrt{\frac{A^3\times 3.1416}{.7854^3\times O}}$ .

meter of square airway. Then 
$$D^3 = \sqrt{\frac{A^3 \times 3.141}{.7854^3 \times G}}$$

If two fans are employed to ventilate a mine, each of which when worked separately produces a certain quantity, which may be indicated by A and B then the quantity of air that will pass when the two fans are worked together will be  $\sqrt[3]{A^3 + B^3}$ . (For mine-ventilating fans, see page 521.)

Relative Efficiency of Fans and Heated Chimneys for Ventilation.—W. P. Trowbridge, Trans. A. S. M. E. vii. 531, gives a theoretical solution of the relative amounts of heat expended to remove a given retical solution of the relative amounts of heat expended to remove a given volume of impure air by a fan and by a chinney. Assuming the total efficiency of a fan to be only 1/25, which is made up of an efficiency of 1/10 for the engine, 5/10 for the fan itself, and 8/10 for efficiency as regards friction, the fan requires an expenditure of heat to drive it of only 1/38 of the amount that would be required to produce the same ventilation by a chinney 100 ft. high. For a chinney 500 ft. high the fan will be 7.6 times more efficient. In all cases of moderate ventilation of rooms or buildings where the air is heated before it enters the rooms, and spontaneous ventilation is produced by the passage of this heated air upwards through vertical flues, no special heat is required for ventilation; and if such ventilation be sufficient, the process is faulless as far as cost is concerned. This is a condition of things which may be realized in most dwelling houses, and in many halls, schoolrooms, and public buildings, provided inlet and outlet flues of ample

schoolrooms, and public buildings, provided inlet and outlet flues of ample cross-section be provided, and the heated air be properly distributed.

If a more active ventilation be demanded, but such as requires the smallest amount of power, the cost of this power may outweigh the advantages of the fan. There are many cases in which steam-pipes in the base of a chimney, requiring no care or attention, may be preferable to mechanical ventilation, on the ground of cost, and trouble of attendance, repairs, etc.

<sup>\*</sup> Murgue gives  $A = \frac{0.38Q}{4\sqrt{n}}$ , and Norris  $A = \frac{0.403Q}{4\sqrt{n}}$ . See page 521, ante.

The following figures are given by Atkinson (Coll. Engr., 1889), showing the minimum depth at which a furnace would be equal to a ventilating-machine, assuming that the sources of loss are the same in each case, i.e., that the loss of fuel in a furnace from the cooling in the upcast is equivalent to the power expended in overcoming the friction in the machine, and also assuming that the ventilating-machine utilizes 60% of the engine-power. The coal consumption of the engine per I.H.P. is taken at 8 lbs. per hour:

Average temperature in upcast...... 100° F. 150° F. 200° F. Minimum depth for equal economy... 960 yards. 1040 yards. 1130 yards.

Heating and Ventilating of Large Buildings. Wolff, Jour. Frank. Inst., 1893.)-The transmission of heat from the interior to the exterior of a room or building, through the walls, ceilings, windows, etc., is calculated as follows:

S = amount of transmitting surface in square feet;

 $t = \text{temperature F. inside, } t_0 = \text{temperature outside:}$ K = a coefficient representing, for various materials composing buildings. the loss by transmission per square foot of surface in British thermal units per hour, for each degree of difference of temperature on the two sides of the material:

 $Q = \text{total heat transmission} = SK(t - t_0).$ 

This quantity of heat is also the amount that must be conveyed to the room in order to make good the loss by transmission, but it does not cover the additional heat to be conveyed on account of the change of air for purposes of ventilation. The coefficients K given below are those prescribed by law by the German Government in the design of the heating plants of its public buildings, and generally used in Germany for all buildings. They have been converted into American units by Mr. Wolff, and he finds that they agree well with good American practice:

VALUE OF K FOR EACH SQUARE FOOT OF BRICK WALL.

Thickness of ! 12" 16" 20" 24" 36" 40" brick wall.  $K = 0.68 \ 0.46 \ 0.32 \ 0.26 \ 0.23 \ 0.20 \ 0.174 \ 0.15 \ 0.129 \ 0.115$ 

		-1	-1.00		
1 sq. ft., wooden-bea planked over or 1 sq. ft., fireproo floored over,	ceiled, f constru	etion,	as as	ceiling, flooring, ceiling,	K = 0.104 K = 0.124 K = 0.145
1 sq. ft., single wind	tow				K = 0.776
1 sq. ft., single skyli					
1 sq. ft., double win	dow				K = 0.518
1 sq. ft., double skyl	light				K = 0.621
1 sq. ft., door					K = 0.414

These coefficients are to be increased respectively as follows: 10% when the exposure is a northerly one, and winds are to be counted on as important factors; 10% when the building is heated during the daytime only, and the location of the building is not an exposed one; 30% when the building is heated during the daytime only, and the location of the building is exposed; 50% when the building is heated during the winter months intermittently, with long intervals (say days or weeks) of non-heating.

The value of the radiating-surfaces is about as follows: Ordinary bronzed cast-iron radiating-surfaces, in American radiators (of Bundy or similar type), located in rooms, give out about 250 heat-units per hour for each square foot of surface, with ordinary steam-pressure, say 3 to 5 lbs. per sq. in., and about 0.5 this amount with ordinary hot-water heating.

Non-painted radiating-surfaces, of the ordinary "indirect" type (Climax or pin surfaces), give out about 400 heat-units per hour for each square foot of heating-surface, with ordinary steam-pressure, say 3 to 5 lbs. per sq. in.;

and about 0.6 this amount with ordinary hot-water heating,

A person gives out about 400 heat-units per hour; an ordinary gas-burner, about 4800 heat-units per hour; an incandescent electric (16 candle-power) light, about 1600 heat-units per hour.

The following example is given by Mr. Wolff to show the application of

the formula and coefficients: Lecture-room 40  $\times$  60 ft., 20 ft. high, 48,000 cubic feet, to be heated to 69° F.; exposures as follows: North wall, 60  $\times$  20 ft., with four windows each 14  $\times$  4 feet, outside temperature 0° F. Room beyond west wall and room overhead heated to 69°, except a double skylight in ceiling, 14 × 24 ft., exposed to the outside temperature of 0°. Store-room beyond east wall at 30°. Door 6 × 12 ft. in wall. Corridor beyond south wall heated to 59°. Two doors, 6 × 12, in wall. Cellar below, temperature 36°.

The following table shows the calculation of heat transmission:

$t-t_0$ (Fahr. degrees).	Kind of Transmitting Surface.	Thickness of Wall in inches.	Calculation of Area of Transmitting Surface.	Square feet of Surface.	$K(t-t_0)$ .	Thermal Units.
69° 69 33 33 10 10 10 10 69 69 33	Outside wall. Four windows (single). Inside wall (store-room). Door Inside wall (corridor). Door Inside wall (corridor). Door Roof Oouble skylight. Floor.	36''	$\begin{array}{c} 63 \times 22 - 448 \\ 4 \times 8 \times 14 \\ 42 \times 22 - 72 \\ 6 \times 12 \\ 45 \times 22 - 72 \\ 6 \times 12 \\ 17 \times 22 - 72 \\ 6 \times 12 \\ 32 \times 42 - 336 \\ 14 \times 24 \\ 62 \times 42 \end{array}$	448 852 72 918 72 302 72	9 72 4 19 2 5 1 5 10 43 4	8,442 32,256 3,408 1,368 1,836 360 302 360 10,080 14,448 10,416
Supplementary allowance, north outside wall, 10%						83,276 844 3,226 87,346 26,204

If we assume that the lecture-room must be heated to 69 degrees Fahr, in the daytime when unoccupied, so as to be at this temperature when first persons arrive, there will be required, ventilation not being considered, and brouzed direct low-pressure steam-radiators being the heating media, about 113,550 + 250 = 455 sq. ft. of radiating-surface. (This gives a ratio of about 105 cu. ft. of contents of room for each sq. ft. of heating-surface.)

If we assume that there are 100 persons in the lecture-room, and we provide 2500 cubic feet of fresh air per person per hour, we will supply  $160 \times 400,000$ 

2500 = 400,000 cubic feet of air per hour (i.e.,  $\frac{400,000}{48,000}$  = over eight changes of

contents of room per hour).

To heat this air from 0° Fahr, to 69° Fahr, will require 400,000 × 0.0189 × 69 = 521,640 thermal units per hour (0.0180 being the product of a weight of a cubic foot by the specific heat of air). Accordingly there must be provided \$521,640 + 400 = 1304 sq. ft. of indirect surface, to heat the air required for ventilation, in zero weather. If the room were to be warmed entirely indirectly, that is, by the air supplied to room (including the heat to beconveyed to cover loss by transmission through walls, etc.), there would have to be conveyed to the fresh-air supply \$21,640 + 118,550 = 635, 190 heat-units. This would imply the provision of an amount of indirect heating-surface of the "Climax" type of 635, 190 + 400 = 1589 sq. ft., and the fresh air entering the room would have to be at a temperature of about \$4° Fahr., viz., 60° = 118,550

 $\frac{110,300}{400,000 \times 0.0189}$ , or 69 + 15 = 84° Fahr.

The above calculations do not, however, take into account that 160 persons in the lecture-room give out  $160\times400=64.000$  thermal units per hour; and that, say, 50 electric lights give out  $50\times1600=80.0000$  thermal units per hour; or, say, 50 gaslights,  $50\times4800=240.000$  thermal units per hour. The presence of 160 people and the gas-lighting would diminist considerably the amount of heat required. Practically, it appears that the heat generated by the presence of 160 people 6,4000 heat-units, and by 50 electric lights, 80,000 heat-units, a total of 144,000 heat-units, more than covers the amount of heat transmitted through walls, etc. Moreover, that if the 50 gaslights give out 240,000 thermal units per hour, the air supplied for ventilation must enter considerably below  $69^\circ$  Fahr, or the room will be heated to an unbearably high temperature. If 400,000 cubic feet of fresh air per hour

are supplied, and 240,000 thermal units per hour generated by the gas must be abstracted, it means that the air must, under these conditions, enter 240,000

 $\frac{210.000}{400,000 \times .0189}$  = about  $32^{\circ}$  less than  $84^{\circ}$ , or at about  $52^{\circ}$  Fahr. Furthermore, the additional vitiation due to gaslighting would necessitate a much larger supply of fresh air than when the vitiation of the atmosphere by the people alone is considered, one gaslight vitiating the air as much as five

men.

Various Rules for Computing Radiating-surface.—The following rules are compiled from various sources. They are more in the nature of "rule-of-thumb" rules than those given by Mr. Wolff, quoted above, but they may be useful for comparison.

Divide the cubic feet of space of the room to be heated, the square feet of wall surface, and the square feet of the glass surface by the figures given under these headings in the following table, and add the quotients together; the result will be the square feet of radiating-surface required. (F. Schumann.)

SPACE, WALL AND GLASS SURFACE WHICH ONE SQUARE FOOT OF RADIATING-SURFACE WILL HEAT.

	nre .	cubic		Exposure of Rooms.					
Change.		l cul	All S	Sides.	North	west.	Sout	heast.	
Air Cha	Steam-pr in pour	Space in feet.	Wall Surface, sq. ft,	Glass Surface, sq. ft.	Wall Surface, sq. ft.	Glass Surface, sq. ft.	Wall Surface, sq. ft.	Glass Surface, sq. ft.	
Once per hour.	1 3 5	190 210 225		7 7.7 8.5	15.87 17.25 18.97	8.05 8.85 9.77	16.56 18.00 19.80	8.4 9.24 10.20	
Twice per hour.	1 3 5	75 82 90	11.1 12.1 13.0	5.7 6.2 6.7	12.76 13.91 14.52.	6.55 7.13 7.60	13.22 14.52 15.60	6.84 7.44 8.04	

Emission of Heat-units per square foot per Hour from Cast-iron Pipes or Rapiators. Temp. of Air in Room, 70° F. (F. Schumann.)

Mean Temperature of	By Contact.		By Radi-	By Radiation and Contact.		
Heated Pipe, Radia- tor, etc.	Air quiet.	Air moving.	ation.	Air quiet.	Air moving.	
Hot water	55.51	92.52	59.63	115.14	152 15	
" "160°	65.45	109.18	69.69	135.14	178.87	
	75.68	126.13	80.19	155.87	206.32	
" "170°	86.18	143.30	91.12	177.30	234.42	
	96.93	161.55	102.15	199.43	264.05	
" "	107.90	179.83	114.45	222.35	294.28	
	119.13	198.55	127.00	246.13	325.55	
" or steam 210°	130.49	217.48	139.96	270.49	357.48	
	142.20	237.00	155.27	297.47	392.27	
"230°	153.95	256.58	169.56	323.51	426.14	
"	165.90	279.83	184.58	350.48	464.41	
	178.00	296.65	200.18	378.18	496.81	
"	189.90	316.50	214.36	404.26	530.86	
	202.70	337.83	233.42	436.12	571.25	
"	215.30	358.85	251.21	466.51	610.06	
	228.55	380.91	267.73	496.28	648.64	
"	240.85	401.41	279.12	519.97	680.53	

RADIATING-SURFACE REQUIRED FOR DIFFERENT KINDS OF BUILDINGS. (From practice of the Dubuque Steam Supply Co., External Air 0° F. Chas. A.

Cubic ft. of Roor	n heated	Cubic ft. of Room	n heated
by 1 sq. ft. of Si		by 1 sq. ft. of 8	
Direct	Indirect	Direct	Indirect
System.	System.		System.
Dwellings 50	40	Banks, offices, drug-stores 70	60
Stores, wholesale125	100	Large hotels 125	100
" retail100	80	Churches200	150

The Nason Mfg. Co.'s catalogue gives the following: One square foot of surface will heat from 40 to 100 cu. ft. of space to 75° in - 10° latitudes. This range is intended to meet conditions of exposed or corner rooms of buildings, and those less so, as intermediate ones of a block. As a general rule, 1 sq. ft. of surface will heat 70 cu. ft. of air in outer or front rooms and 100 cu. ft. in inner rooms. In large stores in cities with buildings on each side, 1 to 100 is ample.

### APPROXIMATE PROPORTIONS OF RADIATING-SURFACES.

One square foot radiating-surface will heat:

In dwellings. In hall, stores, In churches, large schoolrooms, lofts, factories, auditoriums. offices, etc. etc. 75 to 100 ft. 50 to 70 " By direct radiation ... 60 to 80 ft. 150 to 200 ft. 40 to 50 " 100 to 140 '

By indirect radiation. Isolated buildings exposed to prevailing north or west winds should have

a generous addition made to the heating-surface on their exposed sides.

The following rule is given in the cating-surface on their exposed sides.

The following rule is given in the cating-surface on their exposed sides.

The following rule is given in the cating-surface on the Resource of the Babcock & Wilcox Co.,

Radiating surface may be calculated by the rule. Add together the square feet of given rule in the surface of external wall and roof; multiply this sum by the chainest the surface of external wall and roof; multiply this sum by the difference between the required temperature of the room and that of the external air at its lowest point, and divide the product by the difference in temperature between the steam in the pipes and the required temperature of the room. The quotient is the required

and the required temperature of the room. The quotient is the required radiating-surface in square feet.

Overhead Steam-pipes. (A. R. Wolff, Stevens Indicator, 1887.)—
When the overhead system of steam-heating is employed, in which system direct radiating-pipes, usually 1½ in. in diam., are placed in rows overhead, suspended upon horizontal racks, the pipes running horizontally, and side by side, around the whole interior of the building, from 2 to 3 ft. from the walls, and from 2 to 4 ft. from the ceiling, the amount of 1½ in. pipe required, according to Mr. C. J. H. Woodbury, for heating mills (for which use this system is deservedly much in vogue), is about 1 ft. in length for every 90 mt. ft. of spage. Of course a great rape of difference exists due every 90 cu. ft. of space. Of course a great range of difference exists, due to the special character of the operating machinery in the mill, both in respect to the amount of air circulated by the machinery, and also the aid to

warning the Theories and Chinace of the journals. Lift warning the Theories Heating surface.—J. H. Kinealy, in Heating and Ventitation, May 15, 1894, gives the following formula, deduced from results of experiments by C. B. Richards, W. J. Baldwin, J. H. Mills, and others, upon indirect heaters of various kinds, supplied with varying amounts of air per

hour per square foot of surface:

$$N = \frac{35.04}{\frac{T_2 - T_1}{T_0 - T_1} - 0.369}; \quad T_2 = (T_0 - T_1) \left( 0.369 + \frac{35.04}{N} \right) + T_1.$$

N = cubic feet of air, reduced to 70° F., supplied to the heater per square

To etome results and related to the  $T_1$ , supplied to the foot of heating-surface per hour;  $T_0 = \text{temperature of the steam or water in the heater;}$   $T_1 = \text{temperature of the air when it enters the heater;}$   $T_2 = \text{temperature of the air when it leaves the heater,}$ 

As the formula is based upon an average of experiments made upon all sorts of indirect heaters, the results obtained by the use of the equation may in some cases be slightly too small and in others slightly too large, although the error will in no case be great. No single formula ought to be expected to apply equally well to all dispositions of heating-surface in indirect heaters, as the efficiency of such heater can be varied between such

wide limits by the construction and arrangement of the surface.

In indirect heating, the efficiency of the radiating-surface will increase, and the temperature of the air will diminish, when the quantity of the air caused to pass through the coil increases. Thus I sq. ft. radiating-surface, with steam at 212, has been found to heat 100 cu. ft. of air per hour from zero to 150°, or 301 cu. ft. from zero to 100° in the same time. The best restills are attained by using indirect radiation to supply the necessary venti-lation, and direct radiation for the balance of the heat. (Steam.) In indirect steam-heating the least flue area should be 1 to 114 sq. in.

to every square foot of heating-surface, provided there are no long horizontal reaches in the duct, with little rise. The register should have twice the area of the duct to allow for the fretwork. For hot water heating from 25%

to 30% more heating-surface and flue area should be given than for low-pressure steam. (Engineering Record, May 26, 1894.)

Boiler Heating-surface Required. (A. R. Wolff, Stevens Indi-cator, 1887.)—When the direct system is used to heat buildings in which the street floor is a store, and the upper floors are devoted to sales and stock-

street floor is a store, and the upper floors are devoted to sales and stockrooms and to light manufacturing, and in which the fronts are of stone or
iron, and the sides and the rear of building of brick—a safe rule to follow is to
supply 1 sq. ft. of boiler heating-surface for each 700 cn. ft., and 1 sq. ft. of
radiating-surface for each 100 cn. ft. of contents of building.
For heating mills, shops, and factories, 1 sq. ft. of boiler heating-surface
should be supplied for each 470 cn. ft. of contents of building; and the same
allowance should also be made for heating exposed wooden dwellings. For
heating foundries and wooden shops, 1 sq. ft. of boiler heating-surface
should be provided for each 400 cn. ft. of contents; and for structures in
which class enters year largely in the construction—such as conservatories. which glass enters very largely in the construction-such as conservatories, exhibition buildings, and the like-1 sq. ft. of boiler heating-surface should

exhibition buildings, and the like—1 sq. ft. of boiler heating-surface should be provided for each 275 cu, ft. of contents of building.

When the indirect system is employed, the radiator-surface and the boiler capacity to be provided will each have to be, on an average, about 25% more than where direct radiation is used. This percentage also marks approximately the increased fuel consumption in the indirect system.

Steam (Babcock & Wilcox Co.) has the following: 1 sq. ft. of boiler-surface

Steam (Baccock & WHCOX (0.)) has the following: 184,16.01 outer straight will supply from 7 to 10 sq. ft. of radiating-surface, depending upon the size of boiler and the efficiency of its surface, as well as that of the radiating-surface. Small boilers for house use should be much larger proportionately than large planuts. Each horse-power of boiler will supply from 200 to 300 ft. of 1-in. steam pipe, or 80 to 120 sq. ft. of radiating surface. Cubic feet of space has little to do with amount of steam or surface required, but is a convenient factor for rough calculations. Under ordinary conditions 1 horse-power will heat, approximately, in-

brick dwellings, in blocks, as in cities	19,000	w	20,000 01	l. LU.	
	10,000		15,000	**	
" dwellings, exposed all round			19,000	44	
" mills, shops, factories, etc			10,000	44	
Wooden dwellings, exposed			10,000	**	
Foundries and wooden shops	6,000		10,000	"	
Exhibition buildings, largely glass, etc	4.000	44	15.000	6.6	

# Proportion of Grate-surface to Radiator-surface.

(J. R. Willett, Heating and Ventilation, Feb. 1894.)

Radiator-surf , ) 100 200 400 600 800 1000 1200 1400 1600 1800 2000 sq. ft ..... Grate-surface, 120 208 362 501 630 754 986 1100 1210 1310 872 sq. in .....

# Steam-consumption in Car-heating.

C., M. & St. Paul Railw	AY TESTS. (Engineerin	g, June 27, 1890, p. 764.)
		Water of Condensation
Outside Temperature.	Inside Temperature.	per Car per Hour.
40	70	70 lbs.
30	70	85
10	70	100

#### Internal Diameters of Steam Supply-mains, with Total Resistance equal to 2 inches of Water-column.\*

Steam, Pressure 10 lbs. per square inch above atm., Temperature 239° F.

Formula,  $d = 0.5374 \sqrt[5]{\frac{Q^2l}{h}}$ ; where d = internal diameter in inches;

Q=9.2 cubic feet of steam per minute per 100 sq. ft. of radiating surface; t= length of mains in feet; h=159.3 feet head of steam to produce flow.

ting	Internal Diameters in inches for Lengths of Mains from 1 ft. to 600 ft.										
Radiating	1 ft.	10 ft.	20 ft.	40 ft.	60 ft.	80 ft.	100 ft.	200 ft.	300 ft.	400 ft.	600 ft.
sq.ft.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.	inch.
1	0.075	0.119	0.136		0.170	0.180		0.216		0.248	0.270
10	0.19	0.30	0.34	0.39	0.43	0.45	0.47	0.54	0.59	0.62	0.68
20	0.25	0.39	0.45	0.52	0.56	0 60	0.62	0.72	0.78	0.82	0.89
40	0.33	0.52	0.60	0.69	0.74	0.79	0.82	0.95	1.03	1.09	1.18
60	0.39	0.61	0.71	.0.81	0.87	0.93	0.97	1.11	1.21	1.28	1.39
80	0.43	0.68	0.79	0.90	0.98	1.04	1.09	1.25	1.35	1.43	1.55
100	0.47	0.75	0.86	0.99	1.07	1.14	1.19	1.36	1.48	1.57	1.70
200	0 62	0.99	1.14	1.30	1.41	1.50	1.57	1.80	1.95	2.07	2.24
300	0.73	1.16	1.34	1.53	1.66	1.76	1.84	2 12	2.30	2.43	2.64
400	0.82	1.30	1.50	1.72	1.86	1.98	2.07	2.37	2.57	2.73	2.96
500	0.90	1.43	1.64	1.88	2.04	2.16	2.26	2.60	2.81	2.98	3.23
600	0.97	1.53	1.76	2.03	2.20	2.33	2.43	2.79	3.03	3.21	3.48
800	1.09	1.72	1.98	2.27	2 46	2.61	2.73	3.13	3.40	3.60	3.90
1,000	1.19	1.88	2.16	2.48	2.69	2.85	2.98	3.43	3.71	3.94	4.27
1,200	1.28	2.04	2.33	2.67	2.90	3.07	3.21	3.68	4.00	4.23	4.59
1,400	1.36	2.15	2.47	2.84	3.08	3.26	3.41	3.92	4.25	4.50	4.88
1,600	1.43	2.27	2.61	3.00	3.25	3.44	3.60	4.13	4.49	4.75	5.15
1,800	1.50	2.38	2.74	3.14	3.41	3.61	3.78	4.34	4.70	4.98	5.40
2,000	1.57	2.48	2.85	3.28	3.55	3.76	3.93	4.52	4.90	5.19	5.63
3,000	1.84	2.92	3.36	3.85	4.18	4.43	4 63	5.32	5.77	6.11	6.63
4,000	2.07	3.28	3.76	4.33	4.69	4.96	5.19	5.96	6.47	6.85	7.44

<sup>\*</sup> From Robert Briggs's paper on American Practice of Warming Buildings by Steam (Proc. Inst. C. E., 1882, vol. lxxi).

For other resistances and pressures above atmosphere multiply by the respective factors below:

Water col . 6 in. 12 in. 24 in. | Press. ab. atm. 0 lbs. 3 lbs. 30 lbs. 60 lbs. Multiply by 0.8027 0.6988 0.6084 | Multiply by 1.023 1.015 0.973 0.948

Registers and Cold-air Ducts for Indirect Steam Heating.—The Locomotive gives the following table of openings for registers and cold-air ducts, which has been found to give satisfactory results. The cold-air boxes should have 1½ sq. in, area for each square foot of radiator suface, and never less than ¾ the sectional area of the hot air ducts. The hot air ducts should have 2 sq. in, of sectional area to each square foot of radiator surface on the first floor, and from 1½ to 2 inches on the second floor.

Heating Surface in Stacks.	Cold-air Supply, First Floor.	Size Supply, 2d Floor.
20 agus na faot	45 square inches = 5 by 9	inches inches 9 by 12 4 by 10
30 square feet		
40 " "	60 " = $6$ by $10$	10 by 14 4 by 14
50 " "	75 " " = 8 by 10	10 by 14 5 by 15
60 " "	90 " " = 9 by 10	12 by 15 6 by 15
70 " "	108 " " = 9 by 12	12 by 19 6 by 18
80 " "	120 " = 10 by 12	12 by 22 8 by 15
90 " "	135 " = 11 by 12	14 by 24 9 by 15
100 " "	150 " = 12 by 12	16 by 20   12 by 12

The sizes in the table approximate to the rules given, and it will be found that they will allow an easy flow of air and a full distribution throughout the room to be heated.

Physical Properties of Steam and Condensed Water, under Conditions of Ordinary Practice in Warming by Steam. (Briggs.)

-							
A ( )	Steam-pressure j above atm per square inch } total	lbs. lbs.	0 14.7	3 17.7	10 24.7	30 44.7	60 74.7
C Te	emperature of steam emperature of air fference = $B - C$	Fahr. Fahr. Fahr.	212° 60° 152°	222° 60 162°	239° 60° 179°	274° 60° 214°	307° 60° 247°
E }	Heat given out per minute per 100 sq. ft. of radiating-sur-	units	456	486	587	642	741
FLE	$face = \mathbf{D} \times 3$ atent heat of steam	Fahr.	965°	958°	946°	921°	898°
H W	olume of 1 lb. weight of steam eight of 1 cubic foot of steam	eu. ft. lb.	$\begin{array}{c} 26.4 \\ 0.0380 \end{array}$	$\begin{array}{c} 22.1 \\ 0.0452 \end{array}$	16.2 0.0618	$\frac{9.24}{0.1082}$	5.70 0.1752
J {	Volume $Q$ of steam per minute to give out $E$ units $= E \times G \div F$ .	cu. ft.	12.48	11.21	9.20	6.44	4.70
K	Weight of 1 cubic foot of con- densed water at tempera- ture B,	} lbs.	59.64	59.51	59.05	58.07	57.03
L	Volume of condensed water to return to boiler per minute $= J \times H \div K$ ,	cu. ft.	0.0079	0.0085	0.0096	0.0120	0.0144
M	Head of steam equivalent to 12 inches water-column $= \mathbf{K} \div \mathbf{H}$ .	feet	1569	1817	955.5	536.7	325.5
	STEAM-SUPPLY MAINS.						
N	Head h of steam, equivalent to assumed 2 inches water-column for producing steam flow $Q_1 = M + 6$ ,	feet	261.5	219.5	159.3	89.45	54.25
P 7	Internal diameter $d$ of tube* for flow $Q$ when $l = 1$ foot,		0.484	ł.		0.461	0.449
R	Do. do. when $l = 100$ feet, atios of values of $d$ .	inch ratio	1.217 1.023		1.190 1.000	1.158 0.978	
	WATER-RETURN MAINS.						
T   }	Head h assumed at ½-inch water-column for producing full-bore water-flow Q,	foot	0.0417	0.0417	0.0417	0.0417	0.0417
U	Internal diameter $d$ of tube* for flow $Q$ when $l = 1$ foot,		0.147			0.173	0.186
WR	Do. do. when $l = 100$ feet, atios of values of $d \dots$	inch ratio	0.368		0.398 1.000		

<sup>\*</sup> P, F, U, V are each determined from the formula  $d=0.5374\sqrt[5]{rac{Q^2l}{h}}$ .

Size of Steam Pipes for Steam Heating. (See also Flow of Steam in Pipes.)—Sizes of vertical main pipes. Direct radiation. (J. R. Willett, Heating and Ventilation, Feb., 1894.)

Diameter of pipe, inches. 1  $\frac{114}{70}$   $\frac{116}{10}$   $\frac{2}{220}$   $\frac{23}{300}$   $\frac{3}{500}$   $\frac{3}{500}$   $\frac{4}{510}$   $\frac{5}{110}$   $\frac{5}{200}$   $\frac{3}{300}$   $\frac{3}{500}$   $\frac{5}{100}$   $\frac{3}{110}$   $\frac{2}{200}$   $\frac{3}{300}$   $\frac{3}{300}$ 

A. R. Wolff (Stevens Indicator, 1887) says: For determining the cross-sectional area of pipes (in square inches) for steam mains and returns will be ample to allow a constant of .375 sq. in. for each hundred square

feet of heating-surface in coils and radiators, when exhaust steam is used, ,19 sq. in, when live steam is used, and .09 sq. in, for the return. If the cross-sectional areas thus obtained are each mulitiplied by 1.278, and the square root extracted from each product, the respective figures obtained will represent the proper diameters in inches of the several steam-pipes referred to.

Steam, by the Babcock & Wilcox Co., says: Where the condensed water is returned to the boiler, or where low pressure of steam is used, the dianieter of mains leading from the boiler to the radiating-surface should be equal in inches to one tenth the square root of the radiating-surface, mains equal in linears to one tenth the square root of the randamy-surface, mains included, in square feet. Thus a 1-inch pipe will supply 100 square feet of surface, itself included. Return-pipes should be at least ¾ inch in diameter, and never less than one half the diameter of the main—longer returns requiring larger pipe. A thorough drainage of steam-pipes will effectually prevent all cracking and pounding noises therein.

The Nason Mfg. Co. gives the following:

Size of Steam-	Size of Return-
pipes,	pipes.
11/1	Î
11/2	11/4
2	113
21/2	2′~
3 ~	21/2
3½	3
	pipes, 114 11/2 21/2

When mains and surfaces are very much above the boiler the pipes need to be as large as given above; under very favorable circumstances and conditions a 4-inch pipe may supply from 2000 to 2500 sq. ft. of surface, a 6-inch pipe for 5000 sq. ft., and a 10-inch pipe for 15,000 to 20,000 sq. ft., if the distance of run from boiler is not too great. Less than 13/4-inch pipe should not be used horizontally in a main unless for a single radiator connection. The return sizes named are large enough in ordinary pipe-work, though when horizontal pipes with many fittings are used they should be of the same diameter as the steam-pipes.

Generally, when condensation is returned to the boiler by gravity, the diameter of mains in inches should equal one tenth of the square root of the radiating-surfaces in square feet; thus a 1-inch pipe will supply 100 sq. ft. of surface, or with 900 sq. ft, the supply-pipe should be  $\sqrt{900} = 30 + 10 = 3''$ 

diameter

Heating a Greenhouse by Steam.—Wm. J. Baldwin answers a question in the American Machinist as below: With five pounds steampressure, how many square feet or inches of heating-surface is necessary to heat 100 square feet of glass on the roof, ends, and sides of a greenhouse in order to maintain a night heat of 55° to 65°, while the thermometer outside ranges at from 15° to 20° below zero; also, what boiler-surface is necessary? What is the best way to set pipes in a greenhouse—hang them or lay them down? Which is the best for the purpose to use—2" pipe or 1½" pipe?

Ans.—Reliable authorities agree that 1.25 to 1.50 cubic feet of air in an

enclosed space will be cooled per minute per sq. ft. of glass as many degrees as the internal temperature of the house exceeds that of the air outside. Between + 65° and - 20° there will be a difference of 85°, or, say, one cubic Between + 65° and - 20° there will be a difference of 85°, or, say, one cubic foot of air cooled 217.5° F, for each sq ft. of glass for the most extreme condition mentioned. Multiply this by the number of square feet of glass and by 60, and we have the number of cubic feet of air cooled 1° per hour within the building or house. Divide the number thus found by 48, and it gives the units of heat required, approximately. Divide again by 95°, and it will give the number of pounds of steam that must be condensed from a pressure and temperature of five pounds above atmosphere to water at the same temperature in an hour to maintain the heat. Each square foot of surface of pipe will condense from ½ to nearly ½ 1b, of steam per hour, according as the coils are exposed or well or poorly arranged, for which an average of 1/3 lb, may be taken. According to this, it will require 3 sq. ft. of pipe surface per lb. of steam to be condensed. Proportion the heatingsurface of the boiler to have about one fifth the actual radiating-surface, if surrace of the boner to have about one first the actual radiating-surrace, it you wish to keep steam over night, and proportion the grate to burn not more than six pounds of coal per sq. ft. of grate per hour. With very slow combustion, such as takes place in base-burning boilers, the grate might be proportioned for four to five pounds of coal per hour. It is cheaper to make coils of 144'' pipe than of 2'', and there is nothing to be gained by using 2'' pipe unless the coils are very long. The pipes in a greenhouse should be under or in front of the benches, with every chance for a good circulation of air. "Header" coils are better than "return-bend" coils for this purpose,

Mr. Baldwin's rule may be given the following form: Let H = heat-unitstransferred per hour, T = temperature inside the greenhouse, t = temperature outside, S = sq. ft. of glass surface; then H = 1.58(T – t). Mr. Wolff's coefficient K for single skylights would give

H = 1.118S(T - t)

Heating a Greenhouse by Hot Water, -W. M. Mackay, of the Richardson & Boynton Co., in a lecture before the Master Plumbers' Association, N. Y., 1889, says: I find that while greenhouses were formerly heated by 4-inch and 3-inch cast-iron pipe, on account of the large body of water which they contained, and the supposition that they gave better satiswater which they contained, and one supposition that they gave obtter satisfaction and a more even temperature, florists of long experience who have tried 4-inch and 3-inch cast-iron pipe, and also 2-inch wrought-iron pipe for a number of years in heating their greenhouses by hot water, and who have also tried steam-heat, tell me that they get better satisfaction, greater economy, and are able to maintain a more even temperature with 2inch wrought-iron pipe and hot water than by any other system they have used. They attribute this result principally to the fact that this size pipe contains less water and on this account the heat can be raised and lowered quicker than by any other arrangement of pipes, and a more uniform temperature maintained than by steam or any other system.

# HOT-WATER HEATING.

(Nason Mfg. Co.)

There are two distinct forms or modifications of hot-water apparatus, de-

pending upon the temperature of the water.

In the first or open-tank system the water is never above 212° temperature, and rarely above 200°. This method always gives satisfaction where the surface is sufficiently liberal, but in making it so its cost is considerably greater than that for a steam-heating apparatus.

In the second method, sometimes called (erroneously) high-pressure hot-water heating, or the closed-system apparatus, the tank is closed. If it is provided with a safety-valve set at 10 lbs. it is practically as safe as the open-

tank system.

Law of Velocity of Flow.—The motive power of the circulation in a hot-water apparatus is the difference between the specific gravities of the ascending and the descending pipes. This effective pressure is very small, and is equal to about one grain for each foot in height for each degree difference between the pipes; thus, with a height of 12" in "up" pipe, and a difference between the temperatures of the up and down pipes of 8°, the difference in their specific gravities is equal to 8.16 grains on each square inch of the section of return-pipe, and the velocity of the circulation is pro-

portioned to these differences in temperature and height.

To Calculate Velocity of Flow.—Thus, with a height of ascending pipe equal to 10' and a difference in temperatures of the flow and return pipes of 8°, the difference in their specific gravities will equal 81.6 grains, or  $\div$  7000 = .01166 lbs., or  $\times$  2.81 (feet of water in one pound) = .0269 ft., and by the law of falling bodies the velocity will be equal to  $8\sqrt{.0269} = 1.312$  ft, per second, or  $\times 60 = 78.7$  ft. per minute. In this calculation the effect of friction is entirely omitted. Considerable deduction must be made on this account. Even in apparatus where length of pipe is not great, and with pipes of larger areas and with few bends or angles, a large deduction for friction must be made from the theoretical velocity, while in large and complex apparatus with small head, the velocity is so much reduced by friction that sometimes as much as from 50% to 90% must be deducted to obtain the true rate of circulation.

Main flow-pipes from the heater, from which branches may be taken, are

to be preferred to the practice of taking off nearly as many pipes from the

heater as there are radiators to supply

It is not necessary that the main flow and return pipes should equal in capacity that of all their branches. The hottest water will seek the highest level, while gravity will cause an even distribution of the heated water if the surface is properly proportioned.

It is good practice to reduce the size of the vertical mains as they ascend,

say at the rate of one size for each floor.

As with steam, so with hot water, the pines must be unconfined to allow

for expansion of the pipes consequent on having their temperatures increased.

An expansion tank is required to keep the apparatus filled with water, which latter expands 1/24 of its bulk on being heated from 40° to 212°, and the cistern must have capacity to hold certainly this increased bulk. It is recommended that the supply cistern be placed on level with or above the highest pipes of the apparatus, in order to receive the air which collects in the mains and radiators, and capable of holding at least 1/20 of the water in the entire apparatus,

# Approximate Proportions of Radiating-surfaces to Cubic Capacities of Space to be Heated.

One Square Foot of Ra- diating-surface will heat with—	In Dwellings, School-rooms, Offices, etc.	In Halls, Stores, Lofts, Facto- , ries, etc.	In Churches, Large Audito- riums, etc.
High temperature direct hot-water radiation	50 to 70 cu. ft.	65 to 90 cu. ft.	130 to 180 cu. ft.
Low temperature di- rect hot-water radi- ation	30 to 50 " "	35 to 65 " "	70 to 130 " "
High temperature in- direct hot-water ra- diation	30 to 60 " ·"	35 to 75 " "	70 to 150 " "
Low temperature in- direct hot-water ra- diation	20 to 40 " "	25 to 50 " "	50 to 100 " "

**Diameter of Main and Branch Pipes** and square feet of coil surface they will supply, in a low-pressure hot-water apparatus (212°) for direct or indirect radiation, when coils are at different altitudes for direct radiation or in the lower story for indirect radiation:

o ct

Diam. of Pip in inches.	Indirec Radiatic	Dir	Direct Radiation. Height of Coil above Bottom of Boiler, in feet.								
Dia	0	10	20	30	40	50	60	70	80	90	100
	sq. ft.	sq. ft.	sq. ft.	sq. ft.	sq ft.	sq. ft.	sq. ft.	sq. ft.	sq.ft.	sq. ft.	sq. ft.
3/4	49	50	52	53	55	57	59	61	63	65	68
1	87	89	92	95	98	101	103	108	112	116	121
11/4	136	140	144	149	153	158	161	169	175	182	189
11/2	196	202	209	214	222	228	235	243	252	261	271
2	349	359	370	380	393	405	413	433	449	465	483
21/2	546	561	577	595	613	633	643	678	701	727	755
3	785	807	835	856	888	912	941	974	1009	1046	1086
31/2	1069	1099	1132	1166	1202	1241	1283	1327	1374	1425	1480
4	1395	1436	1478	1520	1571	1621	1654	1733	1795	1861	1933
41/2	1767	1817	1871	1927	1988	2052	2120	2193	2272	2356	2445
5 6	2185	2244	2309	2376	2454	2531	2574	2713	2805	2907	3019
6	3140	3228	3341	3424	3552	3648	3763	3897	4036	4184	4344
7 8	4276	4396	4528	4664	4808	4964	5132	5308	5496	5700	5920
8	5580	5744	5912	6080	6284	6484	6616	6932	7180	7444	7735
9	7068	7268	7484	7708	7952	8208	8482	8774	9088	9424	9780
10	8740	8976	9236	9516	9816	10124	10296	10852	11220	11628	12076
11	10559	10860	11180	11519	11879	12262	12666	13108	13576	14078	14620
12	12560	12912	13364	13696	14208	14592	15052	15588	16144	16736	17376
13	14748	15169	15615	16090	16591	17126	17697	18307	18961	19633	20420
14	17104	17584	18109		19232	19856	20528	21232		22800	23680
15	19634	20195	20789	21419	22089	22801	23561	24373		26179	27168
16	22320	22978	23643	24320	25136	25936	26464	27728	28720	29776	30928

The best forms of hot-water-heating boilers are proportioned about as follows:

1 sq. ft. of grate-surface to about 40 sq. ft. of boiler-surface.
1 " boiler- " 5 " " radiating-surface.
1 " grate- " 200 " " "

Rules for Hot-water Heating,—J. L. Saunders (Heating and Ventilation, Dec. 15, 1894) gives the following: Allow 1 sq. ft. of radiating surface for every 3 ft. of glass surface, and 1 sq. ft. for every 30 sq. ft. of wall surface, also 1 sq. ft. for the following numbers of cubic feet of space in the several cases mentioned.

In dwelling-houses: Libraries and dining-rooms, first floor.. 35 to 40 cu. ft. | Libraries and diming-rooms, inst noor... 35 to 40 to 50 to 44 66 66 

To find the necessary amount of indirect radiation required to heat a room:

To find the necessary amount of indirect radiation required to heat a room: Find the required amount of direct radiation according to the foregoing method and add 50%. This if wrought-iron pip eoil surface is used; if castion pin indirect-stack surface is used it is advisable to add from 70% to 50%. Sizes of hot-air flues, cold-air ducts, and registers for indirect work.—Hot-air flues, first floor: Make the net internal area of the flue equal to 3% ag, in. to every square foot of radiating surface in the indirect stack. Hot-air flues, second floor: Make the net internal area of the flue equal to 3% ag, in. to every square foot of radiating surface in the indirect stack. Hot-air flues, second floor: Make the net internal area of the flue equal to 3% ag, in. to every square fall of the duct of the duct equal to 3% ag in the flue of the duct equal to 3% ag in the flue experience of the duct equal to 4% ag in the flue experience of the duct equal to 4% ag in the flue experience of the duct equal to 4% ag in the property of the duct equal to 4% ag in the property agree of the flue experience of the duct experience of the duct experience of the duct equal to 4% ag in the property agree for for radiating surface in the indirect stack.

to 1/2 sq. in. to every square foot of radiating surface in the indirect stack. Hot-air registers should have their net area equal in full to the area of the

hot-air flues. Multiply the length by the width of the register in inches ; 36

not air nues. Antippy the length of y new dath of the register in inches; ya of the product is the net area of register.

Arrangement of Mains for Hot-water Heating. (W. M. Mackay, Lecture before Master Plumbers' Assoc., N. Y., 1889)—There are two different systems of mains in general use, either of which, if properly placed, will give good satisfaction. One is the taking of a single large-flow main from the heater to supply all the radiators on the several floors, with a corresponding return main of the same size. The other is the taking of a number of 2-inch wrought-iron mains from the heater, with the same number of return mains of the same size, branching off to the several radiators or coils with 1¼-inch or 1-inch pipe, according to the size of the radiator or coil. A 2-inch main will supply three 1¼-inch or four 1-inch branches, and these branches should be taken from the top of the horizontal main with a nipple and elbow, except in special cases where it is found necessary to retard the flow of water to the near radiator, for the purpose of assisting the circulation in the far radiator; in this case the branch is taken from the side of the horizontal main. The flow and return mains are usually run side by side, suspended from the basement ceiling, and should have a gradual ascent from the heater to the radiators of at least 1 inch in 10 feet. It is customary, and

an advantage where 2 inch mains are used, to reduce the size of the main at every point where a branch is taken off.

The single or large main system is best adapted for large buildings; but there is a limit as to size of main which it is not wise to go beyond—generative.

ally 6-inch, except in special cases.

The proper area of cold-air pipe necessary for 100 square feet of indirect radiation in hot-water heating is 75 square inches, while the hot air pipe should have at least 100 square inches of area. There should be a damper in the cold air pipe for the purpose of controlling the amount of air admitted to the radiator, depending on the severity of the weather,

#### THE BLOWER SYSTEM OF HEATING AND VENTILATING.

The system provides for the use of a fan or blower which takes its supply of fresh air from the outside of the building to be heated, forces it over steam coils, located either centrally or divided up into a number of independent groups, and then into the several ducts or flues leading to the various The movement of the warmed air is positive, and the delivery of the air to the various points of supply is certain and entirely independent For engines, fans, and steam-coils used with the of atmospheric conditions.

blower system, see page 519,

Experiments with Radiators of 60 sq. ft. of Surface.

(Mech. News, Dec., 1893.)—After having determined the volume and temperature of the warm air passing through the flues and radiators from natural causes, a fan was applied to each flue, forcing in air, and new sets of measurements were made. The results showed that more than two and onethird times as much air was warmed with the fans in use, and the falling off in the temperature of this greatly increased air-volume was only about 12.6%. The condensation of steam in the radiators with the forced-air circulation also was only 66% greater than with natural air draught. One of the several sets of test figures obtained is as follows:

<u>, .</u>	Natural	Forced-	
	Draught		
· ·	in Flue.	Circulation.	
Cubic feet of air per minute	457.5	1227	
Condensation of steam per minute in ounces	11.7	19.6	
Steam pressure in radiator, pounds	9	9	
Temperature of air after leaving radiator	1420	124°	
" before passing through radiator	r. 61°	610	
Amount of radiating surface in square feet		60	
Size of flue in both cases	12 ×		

There was probably an error in the determination of the volume of air in these tests, as appears from the following calculation. (W. K.) Assume that 1 lb. of steam in condensing from 9 lbs. pressure and cooling to the temperature at which the water may have been discharged from the radiator gave up 1000 heat-units, or 62.5 h. u. per ounce; that the air weighed .076 lb. per cubic foot, and that its specific heat is .238. We have

Natural Forced Draught. Draught. Heat given up by steam, ounces x 625...... 1225 H.U. 731 Heat received by air, cu, ft. x.076 x diff, of tem, x.238 = 1399

Or, in the case of forced draught the air received 14% more heat than the steam gave out, which is impossible. Taking the heat given up by the steam as the correct measure of the work done by the radiator, the temperature of the steam at 237°, and the average temperature of the air in the case of natural draught at 102° and in the other case at 93°, we have for the temperature difference in the two cases 185° and 144° respectively; dividing these into the heat-units we find that each square foot of radiating surface transmitted 5.4 heat-units per hour per degree of difference of temperature, in the case of natural draught, and 8.5 heat-units in the case of forced draught.

In the Women's Homosopathic Hospital in Philadelphia, 2000 feet of one-inch pipe heats 250,000 cubic feet of space, ventilating as well; this equals one square foot of pipe surface for about 350 cubic feet of space, or less than 3 square feet for 1000 cubic feet. The fan is located in a separate building about 100 feet from the hospital, and the air, after being heated

to about 135°, is conveyed through an underground brick duct with a loss of only five or six degrees in cold weather. (H. I. Snell, Trans. A. S. M. E. ix. 106. Heating a Building to 70° F. Inside when the Outside Temperature is Zero.—It is customary in some contracts for heating to guarantee that the apparatus will heat the interior of the building to 70° in zero weather. As it may not be practicable to obtain zero weather for the purpose of a test, it may be difficult to prove the performance of the guarantee. E. E. Macgovern, in *Engineering Record*, Feb. 3, 1894, gives a calculation tending to show that a test may be made in weather of a higher temperature than zero, if the heat of the interior is raised above 70°. The higher the temperature of the rooms the lower is the efficiency of the radiating-surface, since the efficiency depends upon the difference between the

temperature inside of the radiator and the temperature of the room. concludes that a heating apparatus sufficient to heat a given building to 70° in zero weather with a given pressure of steam will be found to heat the same building, steam-pressure constant, to 110° at 60°, 35° at 50°, 82° at 40°, and 74° at 32°, outside temperature. The accuracy of these figures, however has not been tested by experiment.

The following solution of the question is proposed by the author. It gives results quite different from those of Mr. Macgovern, but, like them, lacks ex-

perimental confirmation.

Let  $S=s_0$ , ft. of surface of the steam or hot-water radiator;  $W=s_0$ , ft. of surface of exposed walls, windows, etc.;  $T_S=$  temp, of the steam or hot water,  $T_1=$  temp, of inside of building or room,  $T_0=$  temp, of outside of building or room; a= heat-units transmitted per  $s_0$ , ft. of surface of radiator per hour per degree of difference of temperature;

b = average heat-units transmitted per sq. ft. of walls per hour, per

degree of difference of temperature, including allowance for ventilation. It is assumed that within the range of temperatures considered Newton's

law of cooling holds good, viz., that it is proportional to the difference of temperature between the two sides of the radiating-surface. Then 
$$aS(T_S-T_1)=bW(T_1-T_0)$$
. Let  $\frac{bW}{aS}=C$ ; then 
$$T_S-T_1=C(T_1-T_0)\;; \quad T_1=\frac{T_S+CT_0}{1+C}\;; \quad C=\frac{T_S-T_1}{T_1-T_0}.$$
 If  $T_1=70$ , and  $T_0=0$ ,  $C=\frac{T_S-70}{70}$ . Let  $T_S=140^\circ$ ,  $T_S=13.5^\circ$ ,  $T_S=140^\circ$ ,  $T_S=13.5^\circ$ ,  $T_S=140^\circ$ 

From these we derive the following:

Temperature of		Out	side Te	mperatu	res, $T_0$ .		
Steam or Hot	- 20°	- 10°	0°	10°	20°	30°	40°
Water, Ts.		Insid	e Temp	peratures	$T_1$ .		
140°	60	65	70	75	80	85	90
213.5	56.6	63.3	70	76.7	83.4	90.2	96.9
308	54.5	62.3	70	77.7	85.5	93.2	100.9

3.4.

Heating by Electricity.—If the electric currents are generated by a dynamo driven by a steam-engine, electric heating will prove very expensive, since the steam-engine wastes in the exhaust-steam and by radiation about 90% of the heat-units supplied to it. In direct steam-heating, with good boiler and properly covered supply-pipes, we can utilize about 60% of the total heat value of the fuel. One pound of coal, with a heating value of 13,000 heat-units, would supply to the radiators about 13,000 × .60 = 7800 heat-units. In electric heating, suppose we have a first-class condensing-engine developing 1 H.P. for every 2 lbs. of coal burned per hour. This would be equivalent to 1,980,000 ft.-lbs. + 778 = 2545 heat-units, or 1272 heat-units for 1 lb. of coal. The friction of the engine and of the dynamo and the loss by electric leakage, and by heat radiation from the conducting wires, might reduce the heat-units delivered as electric current to the elecwhich, highir detection and these converted into heat to 50% of this, or only 636 heat-units, or less than one twelfth of that delivered to the steam-radiators in direct steam-heating. Electric heating, therefore, will prove uneconomical unless the electric current is derived from water or wind power, which would otherwise be wasted. (See Electrical Engineering.)

### WATER.

**Expansion of Water.**—The following table gives the relative volumes of water at different temperatures, compared with its volume at 4° C. according to Kopp, as corrected by Porter.

Cent.	Fahr.	Volume.	Cent.	Fahr.	Volume.	Cent.	Fahr.	Volume.
4°	39.1°	1.00000	35°	95°	1.00586	70°	158°	1.02241
5	41	1.00001	40	104	1.00767	75	167	1.02548
10	50	1.00025	45	113	1.00967	80	176	1.02872
15	59	1.00083	50	122	1.01186	85	185	1.03213
20	68	1.00171	55	131	1.01423	90	194	1.03570
25	77	1.00286	60	140	1.01678	95	203	1.03943
30	86	1.00425	65	149	1.01951	100	212	1.04332

Weight of 1 cu. ft. at 39.1° F. = 62.4245 lb.  $\div$  1.04332 = 59.833, weight of 1 cu. ft. at  $212^\circ$  F.

Weight of Water at Different Temperatures,—The weight of water at maximum density, 39,1°, is generally taken at the figure given by Rankine, 62,425 lbs, per cubic foot. Some authorities give as low as 62,379. The figure 62,5 commonly given is approximate. The highest authoritative figure is 62,425. At 62° F, the figures range from 62,291 to 62,360. The figure 62,355 is generally accepted as the most accurate.

The figure 62 355 is generally accepted as the most accurate.

At 32° F, figures given by different writers range from 62.379 to 62.418.

Clark gives the latter figure, and Hamilton Smith, Jr., (from Rosetti,) gives
62.416.

Weight of Water at Temperatures above 212° F.—Porter (Richards: "Steam-engine Indicator," p. 52° says that nothing is known about the expansion of water above 212°. Applying formulæ derived from experiments made at temperatures below 212° however, the weight and volume above 212° may be calculated, but in the absence of experimental data was are not certain that the formulæ hold even at higher temperatures.

data we are not certain that the formulæ hold good at higher temperatures.

Thurston, in his "Engine and Boller Trials," gives a table from which we take the following (neglecting the third decimal place given by him):

Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Tempera- ture, deg. F.	Weight, Ibs. per cubic foot.						
212	59.71	280	57.90	350	55.52	420	52.86	490	50.03
220 230	59.64 59.37	290 300	57.59 57.26	360 370	55.16 54.79	430 440	52.47 52.07	500 510	49.61 49.20
240	59.10	310	56.93	380	54.41	450	51.66	520	48.78
250	58.81	350	56.58	390	54.03	460	51.26	530	48.78 48.36
260	58 52	330	56.24	400	53.64	470	50.85	540	47.94
270	58.21	840	55.88	410	53.26	480	50.44	550	47.52

Box on Heat gives the following:

Temperature F...... 212° 250° 300° 350° 400° 450° 500° 600° Lbs, per cubic foot.... 59.82 58.85 57.42 55.94 54.34 52.70 51.02 47.64

te At 212° figures given by different writers (see Trans. A. S. M. E., xiii. 409) hange from 59.56 to 59.845, averaging about 59.77. Weight of Water per Cubic Foot, from 32° to 212° F., and headunits per pound, reckoned above 32° F.: The following table, made by interpolating the table given by Clark as calculated from Rankine's formula, with corrections for apparent errors, was published by the author in 1884, Trans. A. S. M. E., vi. 90. (For heat units above 212° see Steam Tables).

Tian	S. A. D.	. ш. ш.,	v1. 50.	(101	near t	unts a	oove 2	see	Steam	Table	5.)
Temp., deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Heat-units.	Tempera- ture, deg. F.	Weight, lbs. per cubic foot.	Heat-units.
32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 51 55 56 57 58 59	62.49 62.39 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30 62.30	0. 1. 2. 3. 4. 5. 6. 7. 8. 9. 10. 11. 12. 13. 14. 15. 16. 17. 18. 20. 21.01 23.01 24.01 25.01 26.01 27.01	78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105	62.25 62.24 62.23 62.22 62.21 62.20 62.19 62.18 62.17 62.16 62.15 62.14 62.13 62.11 62.09 62.08 62.08 62.03 62.02 62.03 62.03 62.09 62.09 62.09 62.09	46.03 47.03 48.04 49.04 50.04 51.04 53.05 54.05 55.05 57.05 58.06 61.06 62.06 63.07 64.07 65.07 65.07 65.07 67.08 68.08 69.08 70.09 71.09 73.19	128 124 125 126 127 128 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 147 147 147 147 147	61.68 61.67 61.65 61.63 61.61 61.60 61.54 61.52 61.51 61.49 61.49 61.45 61.41 61.39 61.41 61.39 61.36 61.30 61.26 61.20 61.20	91.16 92.17 93.17 94.17 95.18 96.18 97.19 98.19 99.20 101.21 102.21 103.22 104.22 105.23 106.23 107.24 109.25 111.26 111.26 111.27 113.28 114.28 114.28 115.29 116.29 117.30	168 169 170 171 172 173 174 175 176 177 180 181 182 183 184 185 186 187 189 191 192 193 194	60.81 60.79 60.77 60.75 60.73 60.70 60.68 60.68 60.69 60.57 60.53 60.50 60.44 60.41 60.41 60.41 60.41 60.42 60.32 60.32 60.32 60.32	136.44 137.45 138.45 138.46 140.47 141.48 142.49 143.50 146.52 146.52 146.52 147.53 148.54 151.57 152.58 153.59 154.60 155.61 156.62 157.63 158.64 159.65 169.67 161.68
59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75	62.38 62.37 62.37 62.36 62.36 62.34 62.33 62.33 62.33 62.31 62.30 62.29 62.28 62.28 62.27 62.26	28.01 29.01 30.01 31.01 32.01 35.02 35.02 37.02 37.02 40.02 41.02 42.03 44.03 44.03	106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 129	61.96 61.95 61.93 61.92 61.91 61.89 61.88 61.85 61.83 61.87 61.77 61.75 61.77	73.10	150 151 152 153 154 155 156 157 158 160 161 162 163 164 165 166	61.16 61.14 61.12 61.08 61.08 61.06 61.06 60.98 60.96 60.94 60.92 60.96 60.87 60.85	118.31 119.31 120.32 121.33 122.33 123.34 124.35 126.36 127.37 128.37 129.38 130.39 131.40 132.41 133.41 134.42 135.43	196 197 198 199 200 201 202 203 204 205 206 207 208 209 210 211	60.15 60.10 60.10 60.07 60.05 60.02 60.00 59.97 59.95 59.98 59.87 59.88	163.70 164.71 165.72 166.73 167.74 168.75 169.77 170.78 171.79 172.80 173.81 174.83 175.84 176.85 177.86 178.87 179.89 180.90

#### Comparison of Heads of Water in Feet with Pressures in Various Units,

One foot of water at 39°.1 Fahr. = 62.425 lbs. on the square foot;
""" = 0.4335 lbs. on the square inch;
"" = 0.0295 atmosphere;
"" = 0.8296 inch of mercury at 32°;
"" = 773.3 { feet of air at 32° and }

One lb, on the square foot, at 39°.1 Fahr = 0.01602 foot of water	r;
One lb. on the square inch " = 2.307 feet of water	r;
One atmosphere of 29.922 inches of mercury = 33.9 " " "	
One inch of mercury at 32°.1 = 1.133 " "	
One foot of air at 32 deg., and one atmosphere = 0.001293 " " "	
One foot of average sea-water = 1.026 foot of pure wa	ter:
One foot of water at 62° F	t:
" " 62° F = 0.43302 lbs. per sq. ir	ich:
One inch of water at 62° F	,
One pound of water on the square inch at 62° F - 2 3094 feet of water	

# Pressure in Pounds per Square Inch for Different Heads of Water.

At 62° F. 1 foot head = 0.433 lb. per square inch,  $.433 \times 144 = 62.352$  lbs. per cubic foot.

Head, feet.	0	1	2	3	4	5	6	7	8	9
0		0.433				2.165				
10 20	4.330 8.660	9.093	9.526	9.959	10 392		11.258	11.691	12.124	12.557
30 40				14.289 $18.619$						
50 60				22.949 27.279						
70	30.310	30.743	31.176	31.609 35.939	32.042	32.475	32.908	33.341	33.774	34.207
				40.269						

### Head in Feet of Water, Corresponding to Pressures in Pounds per Square Inch.

1 lb. per square inch = 2.30947 feet head, 1 atmosphere = 14.7 lbs. per sq. inch = 33.94 ft. head.

Pressure.	0	1	2	3	4	5	6	7	8	9
0		2.309	4.619	6.928	9.238	11.547	13.857	16.166	18,476	20.785
10	23.0947	25.404	27.714	30.023	32.333	34.642	36.952	39.261	41.570	43.880
20	46.1894									
30	69.2841	71.594	73.903	76.213	78.522	80.831	83.141	85.450	87.760	90 069
40	92.3788	94.688	96,998	99.307	101.62	103.93	106.24	108.55	110.85	113 16
50	115.4735	117.78	120.09	122,40	124.71	126.02	129.33	131.64	183 95	136 26
60	138.5682									
70	161.6629	163.97	166.28	168.59	170.90	173 21	175.52	177.83	180.14	182 45
80	184.7576	187.07	189.38	191,69	194 00	196.31	198.61	200.92	203 23	205 54
90	207.8523	210.16	212.47	214.78	217.09	219.40	221.71	224.02	226.33	228.64

Pressure of Water due to its Weight.—The pressure of still water in pounds per square inch against the sues of any pipe, channel, or vessel of any pape, whatever is due solely to the "head," or height of the level surface of the water above the point at which the pressure is considered, and is equal to .43302 lb. per square inch for every foot of head, or 62.355 lbs. per square foot for every foot of head (at 62° F).

The pressure per square inch is equal in all directions, downwards, upwards, or sideways, and is independent of the shape or size of the containing

vessel.

The pressure against a vertical surface, as a retaining-wall, at any point is in direct ratio to the head above that point, increasing from 0 at the level surface to a maximum at the bottom. The total pressure against a vertical strip of a unit's breadth increases as the area of a right-angled triangle

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whose perpendicular represents the height of the strip and whose base represents the pressure on a unit of surface at the bottom; that is, it is creases as the square of the depth. The sum of all the horizontal pressures is represented by the area of the triangle, and the resultant of this sum is equal to this sum exerted at a point one third of the height from the bottom. (The centre of gravity of the area of a triangle is one third of its height.)

The horizontal pressure is the same if the surface is inclined instead of

vertical.

(For an elaboration of these principles see Trautwine's Pocket-Book, or the chapter on Hydrostatics in any work on Physics. For dams, retainingwalls, etc., see Trautwine.)

The amount of pressure on the interior walls of a pipe has no appreciable

effect upon the amount of flow.

effect upon the amount of flow. **Ruoyancy.**—When a body is immersed in a liquid, whether it float or sink, it is buoyed up by a force equal to the weight of the bulk of the liquid displaced by the body. The weight of a floating body is equal to the weight of the bulk of the liquid that it displaces. The upward pressure or buoyancy of the liquid may be regarded as exerted at the centre of gravity of the displaced water, which is called the centre of pressure or of the displaced water, which is called the axis of huvrancy or of flota. A vertical line drawn through it is called the axis of buoyancy or of flota-tion. In a floating body at rest a line joining the centre of gravity and the centre of buoyancy is vertical, and is called the axis of equilibrium. an external force causes the axis of equilibrium to lean, if a vertical line be drawn upward from the centre of buoyancy to this axis, the point where it cuts the axis is called the metacentre. If the metacentre is above the centre of gravity the distance between them is called the metacentric height, and the body is then said to be in stable equilibrium, tending to return to its

original position when the external force is removed. **Bolling=point.**—Water boils at 212° F. (100° C.) at mean atmospheric pressure at the sea-level, 14.696 lbs. per square inch. The temperature at which water boils at any given pressure is the same as the temperature of saturated steam at the same pressure. For boiling-point of water at other pressure than 14.696 lbs. per square inch, see table of the Properties of

Saturated Steam.

The Boiling-point of Water may be Raised .- When water is entirely freed of air, which may be accomplished by freezing or boiling, the cohesion of its atoms is greatly increased, so that its temperature may be raised over 50° above the ordinary boiling-point before ebullition takes place. It was found by Faraday that when such air-freed water did boil, the rupture of the liquid was like an explosion. When water is surrounded by a film of oil, its boiling temperature may be raised considerably above its normal standard. This has been applied as a theoretical explanation in the instance of boiler-explosions.

The freezing-point also may be lowered, if the water is perfectly quiet, to — 10° C., or 18° Fahrenheit below the normal freezing-point. (Hamilton Smith, Jr., on Hydraulies, p. 13.) The density of water at 14° F. is. 98814, its density at 39°. 1 being 1, and at 32°, 99957.

Freezing-point.—Water freezes at 32° F. at the ordinary atmospheric

pressure, and ice melts at the same temperature. In the melting of 1 pound of ice into water at 32° F. about 142 heat-units are absorbed, or become latent; and in freezing 1 lb. of water into ice a like quantity of heat is given out to the surrounding medium,

Sca-water freezes at 27° F. The ice is fresh. (Trautwine.)

Sca-water freezes at 27° F. The ice is fresh. (Trautwine.)

57.50 lbs.; 1 pound of ice at 32° F. has a volume of .0174 cu. ft. = 30.067 cu. in. Relative volume of ice to water at 32° F., 1.0855, the expansion in passion into the solid state being 8.55%. Specific gravity of ice = 0.922, water at 62° F. being I.

At high pressures the melting-point of ice is lower than 32° F., being at the rate of .0133° F. for each additional atmosphere of pressure

The specific heat of ice is .504, that of water being 1.

1 cubic foot of fresh snow, according to humidity of atmosphere; 5 lbs. to 12 lbs. 1 cubic foot of snow moistened and compacted by rain: 15 lbs. to 50 lbs. (Trautwine).

Specific Heat of Water. (From Clark's Steam-engine.)—Calculated by means of Regnault's formula,  $c=1+0.00004+0.0000091^2$ , in which c is the specific heat of water at any temperature t in centigrade degrees, the specific heat at the freezing-point being 1.

Tempera- tures.		ritish Thermal Units above 22° F. pecific Heat at the given Temperature. Item Specific Heat between Heat between 82° F. and the given Temp.		Tem	pera-	sh Ther- Units pound, ve 32° F.	specific Heat at the given Temperature.	Specific between and the Temp,	
Cent.	Fahr.	British mal U per po above	Specific at the granter	Mean Heat 32° F. given	Cent.	Fahr.	British mal U per pc above	Specific at the g Temper	Mean Heat 32° F. given
00	320	0.000	1.0000		120°	2480	217,449	1.0177	1.0067
10	50	18.004	1.0005	1.0002	130	266	235,791	1.0204	1.0076
20	68	36.018	1.0012	1.0005	140	284	254.187	1.0232	1.0087
30	86	54.047	1.0020	1.0009	150	302	272.628	1.0262	1.0097
40	104	72.090	1.0030	1.0013	160	320	291.132	1.0294	1.0109
50	122	90.157	1.0042	1.0017	170	8^3	309,690	1.0328	1.0121
60	140	108.247	1.0056	1.0023	180	350	328.320	1.0364	1.0133
70	158	126.378	1.0072	1.0030	190	374	347.004	1.0401	1.0146
30	176	144.508	1.0089	1.0035	200	392	365.760	1.0440	1.0160
90	194	162.686	1.0109	1.0042	210	410	384.588	1.0481	1.0174
100	212	180.900	1.0130	1.0050	220	428	403.485	1.0524	1.0189
110	230	199.152	1.0153.	1.0058	230	446	422.478	1.0568	1.0204

Compressibility of Water,—Water is very slightly compressible. Its compressibility is from .000040 to .000051 for one atmosphere, decreasing with increase of temperature. For each foot of pressure distilled water will be diminished in volume .0000015 to .0000013. Water is so incompressible that even at a depth of a mile a cubic foot of water will weigh only about half a pound more than at the surface.

### THE IMPURITIES OF WATER.

# (A. E. Hunt and G. H. Clapp, Trans, A. I. M. E. xvii, 338.)

Commercial analyses are made to determine concerning a given water: (1) its applicability for making fram; (2) its hardness, or the facility with which it will "form a lather" necessary for washing; or (3) its adaptation to other manufacturing purposes.

At the Buffalo meeting of the Chemical Section of the A. A. A. S. it was de-

cided to report all water analyses in parts per thousand, hundred-thousand.

and million.

To convert grains per imperial (British) gallons into parts per 100,000, divide by 0.7. To convert parts per 100,000 into grains per U. S. gallon, mul-

tiply by 7/12 or .583.

The most common commercial analysis of water is made to determine its fitness for making steam. Water containing more than 5 parts per 100,000 of free sulphuric or nitric acid is liable to cause serious corrosion, not only of the metal of the boiler itself, but of the pipes, cylinders, pistons, and valves with which the steam comes in contact.

The total residue in water used for making steam causes the interior linings of boilers to become coated, and often produces a dangerous hard scale, which prevents the cooling action of the water from protecting the

metal against burning.

Lime and magnesia bicarbonates in water lose their excess of carbonic acid on bolling, and often, especially when the water contains sulphuric acid, produce, with the other solid residues constantly being formed by the evaporation, a very hard and insoluble scale. A larger amount than 100 parts per 100,000 of total solid residue will ordinarily cause troublesome scale, and should condemn the water for use in steam-boilers, unless a better supply can be obtained.

The following is a tabulated form of the causes of trouble with water for steam purposes, and the proposed remedies, given by Prof. L. M. Norton.

#### CAUSES OF INCRUSTATION.

1. Deposition of suspended matter.

2. Deposition of deposed salts from concentration.

3. Deposition of carbonates of lime and magnesia by boiling off carbonic acid, which holds them in solution,

4. Deposition of suiphates of lime, because sulphate of lime is but slightly soluble in cold water, less soluble in hot water, insoluble above 270° F. 5. Deposition of magnesia, because magnesium salts decompose at high

temperature. 6 Deposition of lime soap, iron soap, etc., formed by saponification of

grease.

### MEANS FOR PREVENTING INCRUSTATION.

1. Filtration.

 Blowing off.
 Use of internal collecting apparatus or devices for directing the circulation.

Harden.

4. Heating feed-water.

5. Chemical or other treatment of water in boiler.

6. Introduction of zinc into boiler.

7. Chemical treatment of water outside of boiler.

	TABULAR VIEW.	
Troublesome Substance.	Trouble.	Remedy or Palliation.
Sediment, mud, clay, etc. Readily soluble salts.	Incrustation.	Filtration; blowing off. Blowing off.
Bicarbonates of lime, magnes iron.	ia, } "	Heating feed. Addition of caustic soda, lime, or magnesia, etc.
Sulphate of lime.	"	Addition of carb. soda, barium chloride, etc.
Chloride and sulphate of magn	ne-} Corrosion.	Addition of carbonate of soda, etc.
Carbonate of soda in lar amounts,	ge Priming.	Addition of barium chlo- ride, etc.
Acid (in mine waters).	Corrosion.	Alkali.
Dissolved carbonic acid a oxygen,	nd} "	Heating feed. Addition of caustic soda, slacked lime, etc.
Grease (from condensed water	er). " -	Slacked lime and filtering. Carbonate of soda. Substitute mineral oil.
Organic matter (sewage).	Priming.	Precipitate with alum or ferric chloride and filter.
Organic matter.	Corrosion.	Ditto.

The mineral matters causing the most troublesome boiler-scales are bicarbonates and sulphates of lime and magnesia, oxides of iron and alumina, and silica. The analyses of some of the most common and troublesome boiler-scales are given in the following table:

### Analyses of Boiler-scale. (Chandler.)

			J.	Sul- phate of Lime.	Mag- nesia.	Silica.	Per- oxide of Iron.	Water.	Carbonate of Lime.
N. Y.	C. & F	I. R. F	Ry., No.	74.07	9.19	0.65 1.76	0.08	1.14	14.78
66	44	44		62.86	18.95	2.60	0.92	1.28	12.62
• 6	44	44	No.	53.05		4.79			
"	"	66		5 4 <b>6</b> .83 30.80	31.17	5.32 7.75	1.08	2.44	26.93
66	64	44	No.	4.95	2.61	2.07	1.03	0.63	86.25
44	44	46	No.		2.84	0.65	0.36	0.15	93.19
	44	6.6	No.			2.92			
66	"	44	No. 1	30.07		8.24			

Analyses in Parts per 100,000 of Water giving Bad Results in Steam-boilers. (A. E. Hunt.)

	Bicarbonate of Lime deposited on Boiling.	Bicarbonate of Mag- nesia depos'd on Boil'g	Total Lime.	Total Magnesia.	Sulphuric Acid.	Chlorine.	Iron.	Organic Matter.	Alumina.	Chloride of Sodium.
Coal-mine water	110	25	119	39	890	590	780	30	640	
Salt-well	151	38	1.90	48	360	990	38	21	30	13.10
Spring	75	89	95	120	310	21	75	10	80	36
Mononganeia River	130	21	161	33	210	38	70			
"	80	70	94	81	219	210	90			
**	82	85	61	1.04	28	1.90	38			
Allegheny R., near Oil-works	30	50	41	68	690	42	23			

Many substances have been added with the idea of causing chemical action which will prevent boiler-scale. As a general rule, these do more harm than good, for a boiler is one of the worst possible places in which to carry on chemical reaction, where it nearly always causes more or less corrosion of the metal, and is liable to cause dangerous explosions.

corrosion of the metal, and is liable to cause dangerous explosions. In cases where water containing large amounts of total solid residue is necessarily used, a heavy petroleum oil, free from tar or wax, which is not acted upon by acids or alkalies, not having sufficient wax in it to cause saponification, and which has a vaporizing-point at nearly 600° F., will give the best results in preventing bolier-scale. Its action is to form a thin greasy film over the boiler linings, protecting them largely from the action of acids in the water and greasing the sediment which is formed, thus preventing the formation of scale and keeping the solid residue from the evaporation of the water in such a plastic suspended condition that it can be easily ejected from the boiler by the process of "blowing off." If the water is not blown off sufficiently often, this sediment forms into a "putty" that will necessitate cleaning the boilers. Any boiler using bad water should

that will necessitate cleaning the boners. Any boner using oad water should be blown off every twelve hours.

Hardness of Water,—The hardness of water, or its opposite quality, indicated by the ease with which it will form a lather with soap, depends almost altogether upon the presence of compounds of lime and magnesia. Almost all soaps consist, chemically, of oleate, stearate, and palmitate, of an alkaline base, usually soda and potash. The more lime and magnesia in a smalled for water the more seen a given volume of the water. sample of water, the more soap a given volume of the water will decompose, so as to give insoluble cleate, palmitate, and stearate of lime and magnesia. and consequently the more soap must be added to a gallon of water in order that the necessary quantity of soap may remain in solution to form the lather. The relative hardness of samples of water is generally expressed in terms of the number of standard soap-measures consumed by a gallon of water in yielding a permanent lather.

The standard soap-measure is the quantity required to precipitate one grain of carbonate of lime.

It is commonly reckoned that one gallon of pure distilled water takes one

It is commonly reckoned that one gainon or pure usuned water takes one soap-measure to produce a lather. Therefore one is deducted from the total number of soap-measures found to be necessary to use to produce a lather in a gallon of water, in reporting the number of soap-measures, or "degrees" of hardness of the water sample. In actually making tests for hardness, the "miniature gallon," or seventy cubic centimetres, is used rather than the inconvenient larger amount. The standard measure is made rather than the monvement ages another. The standard measurers made by completely dissolving ten grammes of pure castlle soap (containing 60 per cent olive-oil) in a litre of weak alcohol (of about 35 per cent alcohol). This yields a solution containing exactly sufficient soap in one cubic centimeter of the solution to precipitate one milligramme of carbonate of lime, or, in other words, the standard soap solution is reduced to terms of the "minia-ture gallon" of water taken.

If a water charged with a bicarbonate of lime, magnesia, or iron is boiled.

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it will, on the excess of the carbonic acid being expelled, deposit a considerable quantity of the lime, magnesia, or iron, and consequently the water will be softer. The hardness of the water after this deposit of lime, after long boiling, is called the *permanent hardness* and the difference between it and the total hardness is called *temporary hardness*,

Lime salts in water react immediately on soap-solutions, precipitating the oleate, palmitate, or stearate of lime at once. Magnesia salts, on the contrary, require some considerable time for reaction. They are, however,

trary, require some considerance time for reaction. They are, nowever, more powerful hardeners; one equivalent of magnesia salts consuming as much soap as one and one-half equivalents of lime. The presence of soda and potash salts softens rather than hardens water. Each grain of carbonate of lime per gallon of water causes an increased expenditure for soap of about 2 ounces per 100 gallons of water. (Eng'g.

News, Jan. 31, 1885.)

Purifying Feed-water for Steam-boilers.—To effect the purification of water before and after being fed into a boiler, a device manufactured by the Albany Steam Trap Company, Albany, N. Y. removes the impurities by the process of a continuous circulation of the water from the boiler, through the filter and back into the boiler. The scale-forming impurities that are held in suspension are thus brought in contact with and "arrested" by the filtering agent contained in the filter while under pressure, and at a temperature limited only by that contained in the boiler.

It is sometimes desirable, in the removal of the sulphates and carbonates from the feed-water, to heat the water up to nearly the same temperature as it is in the boiler, and then to filter the same before feeding it into the boiler. The operation in a general way is: The water is first forced into the usual exhaust-heater by the feed-pump, and there it is heated by the exhaust from the engine, say to 200°, and at this temperature it enters the reheater. The reheater consists of a vertical, cylindrical shell containing a series of water pans or shelves, and so arranged that as the water enters it it delivered into the top pan, and then overflows into the second, and so on down the series to the bottom, and during its transit deposits the scale-forming material. The circulating-pump takes the water from the bottom of the reneater and forces it through the filter on its way into the boiler.

Mr. W. B. Coggswell, of the Solvay Process Co.'s Soda Works in Syracuse.

N. Y., thus describes the system of purification of boiler feed-water in use at these works (Trans. A. S. M. E., xiii. 255):

as these works (1 rans, 18, 28, 31, 28, 241, 259). For purifying, we use a weak soda liquor, containing about 12 to 15 grams  $Na_3Co_2$  per litre. Say 1½ to 2  $M^2$  (or 397 to 530 gals.) of this liquor is run into the precipitating tank. Hot water about 60° C, is then turned in, and the reaction of the precipitation goes on while the tank is filling, which requires about 15 minutes. When the tank is full the water is filtered through the Hyatt (4), 5 feet diameter, and the Jewell (1), 10 feet diameter, filters in 30 minutes. Forty tanks treated per 24 hours.

Soda in purifying reagent. 15 kgs.  $Na_2CO_3$ . Soda used per 1,000 gallons 3.5 lbs.

A sample is taken from each boiler every other day and tested for deg. Baumé, soda and salt. If the deg. B is more than 2, that boiler is blown to reduce it below 2 deg. B.

The following are some ana	lyses given t	by Mr. Coggs	swell:	
	Lake Water, grams per litre.	Mud from Hyatt Filter.	Scale from Boiler- tube.	Scale found in Pump.
Calcium sulphate	.261	3.70	51.24	10.9
Calcium carbonate  Magnesium carbonate  Magnesium chloride	.091 .015 .087	63.37 1.11	19.76 25.21	87.
Salt, NaCl Silica Iron and aluminum oxide	.63	15.17 3.75	.14 2.29 1.10	.8 1.2
Total		87.10	99.74	99.9

Softening Hard Water for Locomotive Use.—A water-softening plant in operation at Fossil, in Western Wyoming, on the Union Patific Railway, is described in Eng'g News, June 9, 1892. It is the invention of Arthur Pennell, of Kansas City. The general plan adopted is to first dissolve the chemicals in a clo-ed tank, and then connect this to the supply main so that its contents will be forced into the main tank, the supply-pipe being so arranged that thorough mixture of the solution with the water is obtained. A waste-pipe from the bottom of the tank is opened from time to time to draw off the precipitate. The pipe leading to the tender is arranged to draw the water from near the surface.

A water-tank 24 feet in diameter and 16 feet high will contain about 46,600 gailons of water. About three hours should be allowed for this amount of water to pass through the tank to insure thorough precipitation, giving a permissible consumption of about 15,000 gallons per hour. Should more

than this be required, auxiliary settling-tanks should be provided.

The chemicals added to precipitate the scale-forming impurities are sodinu carbonate and quickline, varying in proportious according to the relative proportions of sulphates and carbonates in the water to be treated. Sufficient sodium carbonate is added to produce just enough sodium sulphate to combine with the remaining lime and magnesia sulphate and produce glauberite or its corresponding magnesia sait, thereby to get rid of the sodium sulphate, which produces foaming, if allowed to accumulate.

### HYDRAULICS-FLOW OF WATER.

Formulæ for Discharge of Water though Orifices and Weirs.—For rectangular or circular orifices, with the head measured from centre of the orifice to the surface of the still water in the feeding reservoir.

$$Q = C \sqrt{2gH} \times a. \qquad (1)$$

For weirs with no allowance for increased head due to velocity of approach:

$$Q = C_{3}^{2} \sqrt{2gH} \times LH. \qquad (2)$$

For rectangular and circular or other shaped vertical or inclined orifices; formula based on the proposition that each successive horizontal layer of water passing through the orifice has a velocity due to its respective head:

$$Q = cL_{3/3}^{2} \sqrt{2g} \times (\sqrt{Hb^3} - \sqrt{Ht^3}). \qquad (3)$$

For rectangular vertical weirs:

 $Q={\rm quantity}$  of water discharged in cubic feet per second;  $C={\rm approximate}$  coefficient for formulas (1) and (2);  $c={\rm correct}$  coefficient for (3) and (4).

Values of the coefficients c and C are given below.

g=32.16;  $\sqrt{2g}=8.02$ ; H= bead in feet measured from centre of orifice to level of still water; Hb= bead measured from bottom of orifice; H= head measured from top of orifice; h=H, corrected for velocity of approach,  $Va_*=H+\frac{4}{3}\frac{Va^2}{a^2}$ ; a= area in square feet; L= length in feet.

Flow of Water from Orifices,—The theoretical velocity of water flowing from an orifice is the same as the velocity of a falling body which has fallen from a height equal to the head of water, =  $\sqrt{2gH}$ . The actual velocity at the smaller section of the  $vena\ contracta$  is substantially the same as the theoretical, but the velocity at the plane of the orifice is  $C\ V^2qH$ , in which the coefficient C has the nearly constant value of .82. The smallest diameter of the  $vena\ contracta$  is therefore about .79 of that of the orifice, If C be the approximate coefficient = .62, and c the correct coeffi-

cient, the ratio  $\frac{C}{c}$  varies with different ratios of the head to the diameter of the vertical orifice, or to  $\frac{H}{D}$ . Hamilton Smith, Jr., gives the following:

For 
$$\frac{H}{D} = .5$$
 .875 .1 1.5 2. 2.5 5. 10.  $\frac{C}{C} = .9604$  .9849 .9918 .9965 .9980 .9987 .9997 1.

For vertical rectangular orifices of ratio of head to width W:

For 
$$\frac{H}{W}=$$
 .5 .6 .8 .1 1.5 2. 3. 4. 5. 8.   
 $\frac{C}{c}=$  .9428 .9657 .9823 .9890 .9953 .9974 .9988 .9993 .9996 .9998  
For  $H \rightarrow D$  or  $H \rightarrow W$  over S,  $C=c$ , practically.

Weishach gives the following values of c for circular orifices in a thin wall. H = measured head from centre of orifice.

D ft.				H ft.			
D 10.	.066	.33	.82	2.0	3.0	45.	340.
.033 .066 .10	.711	.665	.637 .629 .622 .614	.628 .621 .614 .607	.641	.632	.600

For an orifice of D = .033 ft. and a well-rounded mouthpiece, H being the effective head in feet,

$$H = .066$$
 1.64 11.5 56 33  $c = .959$  .967 .975 .994 .99

Hamilton Smith, Jr., found that for great heads, 312 ft. to 336 ft., with converging mouthpieces, c has a value of about one, and for small circular orifices in thin plates, with full contraction,  $c \equiv$  about .60. Some of Mr. Smith's experimental values of c for orifices in thin plates discharging into air are as follows. All dimensions in feet.

Circular, in steel, 
$$D=.020$$
,  $\begin{cases} H=.739 & 2.43 & 3.19 \\ -6.495 & .6298 & .6298 & .6204 \end{cases}$ 
Circular, in brass,  $D=.050$ ,  $\begin{cases} H=.185 & .536 & 1.74 & 2.73 & 3.57 & 4.63 \\ -6.6525 & .6255 & .6255 & .6113 & .6070 & .6060 & .6051 \end{cases}$ 
Circular, in brass,  $D=.100$ ,  $\begin{cases} H=.189 & .457 & .900 & 1.73 & 2.05 & 3.18 \\ -6.6327 & .615 & .6095 & .6042 & .6038 & .6026 \end{cases}$ 
Circular, in iron,  $D=.100$ ,  $\begin{cases} H=1.80 & 1.81 & 2.81 & 4.68 \\ -6.601 & .6041 & .6038 & .6026 \end{cases}$ 
Square, in brass,  $.05 \times .05$ ,  $\begin{cases} H=.181 & .817 & 1.79 & 2.81 & 3.70 & 4.63 \\ -6.410 & .6938 & .6157 & .6127 & .6113 & .6007 \\ -6.6928 & .6159 & .6094 & .6076 & .6060 & .6065 \\ -6.6928 & .6159 & .6094 & .6076 & .6060 & .6065 \\ -6.6938 & .6159 & .6094 & .6076 & .6060 & .6065 \\ -6.6938 & .6159 & .6094 & .6076 & .6060 & .6065 \\ -6.6938 & .6159 & .6094 & .6076 & .6060 & .6065 \\ -6.6938 & .6159 & .6094 & .6076 & .6060 & .6065 \end{cases}$ 

For the rectangular orifice, L, the length, is horizontal. Mr. Smith, as the result of the collation of much experimental data of others as well as his own, gives tables of the value of c for vertical orifices, with full contraction, with a free discharge into the air, with the inner face of the plate, in which the orifice is pierced, plane, and with sharp inner corners, so that the escaping vein only touches these inner edges. These tables are abridged below. The coefficient c is to be used in the formulæ (3) and (4) above. For formulæ (1) and (2) use the coefficient C found from the

values of the ratios  $\frac{C}{c}$  above.

Values of Coefficient c for Vertical Orifices with Sharp Edges, Full Contraction, and Free Discharge into Air. (Hamilton Smith, Jr.)

Square Orifices. Length of the Side of the Square, in feet.    10	2%	11.	(IIaii	шин	Sum.	ц, эт.	,							
4   6   6.60   6.45   6.83   6.82   6.82   6.16   6.11   6.05   6.01   5.98   5.96     3.0   6.48   6.36   6.30   6.23   6.17   6.18   6.10   6.05   6.01   5.98   5.96     3.0   6.48   6.36   6.28   6.22   6.18   6.13   6.10   6.05   6.03   6.03   6.03   6.03     3.0   6.48   6.36   6.28   6.22   6.18   6.13   6.10   6.08   6.05   6.03   6.03   6.03     4.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     5.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     5.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0   6.0     6.0   6.0   6.0   6.0   6.0     7   7   8   8   8   8   8   8   8   8		Square Orifices. Length of the Side of the Square, in feet.												
1.0	H O O	.02	.03	.04	.05	.07	.10	.12	.15	.20	.40	.60	.80	1.0
1.0	.4										-	,		
3.0	1.0						.617							
6.0	3.0													
100. (*)	6.0	.632			.612									
20.														
H.											.003			
H.	100.(?)													
H.		.000	.000	.000	.000	.000	.000	00	.000	.000	3301	.000	.000	.000
.02 .03 .04 .05 .07 .10 .12 .15 .20 .40 .60 .80 1.0  4 .6 .655 .640 .630 .624 .618 .612 .606 .60 .10 .506 .593 .590 .101  1.0 .644 .631 .623 .617 .612 .008 .605 .601 .506 .593 .590 .591 .22 .632 .624 .614 .610 .607 .601 .601 .600 .598 .595 .593 .591 .591 .4 .623 .614 .610 .607 .601 .601 .600 .599 .599 .597 .596 .595 .606 .618 .611 .607 .604 .602 .600 .599 .599 .595 .597 .596 .595 .606 .618 .611 .607 .604 .602 .600 .599 .599 .595 .597 .596 .595 .596 .595 .591 .506 .595 .590 .595 .595 .595 .595 .595 .595	TI I				Circ	ular (	Drifice	s. D	iamet	ers, i	n feet			
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	11.	.02	.03	.04	.05	.07	.10	.12	.15	.20	.40	.60	.80	1.0
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	1				697	698	618	610	606					
1.0         644         631         .628         .617         .612         .608         .603         .600         .598         .595         .597         .597         .597         .597         .597         .597         .597         .597         .596         .596         .599         .599         .599         .598         .598         .597         .597         .596         .5		655	640	630						601	596	593	590	
2. 632 621 614 610 607 604 601 601 601 600 599 599 597 596 595 66 6 6 618 611 607 604 602 600 599 599 599 597 596 596 6 6 618 611 607 604 602 600 599 599 599 598 598 597 596 596 596 590 599 599 599 599 599 599 599 599 590 597 597 597 596 596 595 500 597 597 597 597 597 596 596 595 500 600 599 599 598 597 597 597 597 597 596 595 598 597 597 596 595 596 596 596 596 596 596 596 596	1.0		.631	.623	.617									.591
4. 623 614 609 605 603 002 600 599 599 599 598 597 597 596 506 506 10 6. 618 611 607 604 602 600 599 599 589 598 598 597 596 506 506 10 6. 611 606 603 601 599 598 598 597 597 597 596 596 596 596 500 600 599 598 597 597 597 597 596 596 596 595 500 601 599 598 597 597 597 597 597 596 596 595 595 595 598 597 598 598 598 597 598 598 598 598 598 598 598 598 598 598	2.	.632										.597	.596	
6. 618 611 607 604 602 600 .599 .599 .598 .598 .597 .596 .596 .596 .590 .597 .596 .596 .596 .596 .597 .597 .597 .597 .596 .596 .595 .20 .601 .600 .599 .598 .597 .596 .596 .596 .596 .596 .596 .596 .596	4,	.623					.602	.600						
20.   .601   .600   .599   .598   .597   .596   .596   .596   .596   .596   .596   .595   .594   .59	6.	.618	.611	.607	.604	.602	.600	.599	.599	.598	.598	.597	.596	.596
50.(2) .596 .596 .595 .595 .594 .594 .594 .594 .594 .594	10.	.611	.606	.603	.601	.599		.598	.597		.597	.596	.596	.595
100.(?)  .598' .598' .592' .592 .592' .592' .592' .592' .592' .592' .592' .592' .592' .592' .592'														
	100.(?)	.598	.593	.592	.592	.592	592	.592	.592	.592	.592	.5921	.592	.592

#### HYDRAULIC FORMULÆ.-FLOW OF WATER IN OPEN AND CLOSED CHANNELS.

Flow of Water in Pipes.—The quantity of water discharged through a pipe depends on the "head;" that is, the vertical distance between the level surface of still water in the chamber at the entrance end of twent the level and the level of the centre of the discharge end of the pipe; also upon the length of the pipe, upon the character of its interior surface as to smoothness, and upon the number and sharpness of the bends; but it is independent of the position of the pipe, as horizontal, or inclined upwards or downwards.

The head, instead of being an actual distance between levels, may be caused by pressure, as by a pump, in which case the head is calculated as a vertical distance corresponding to the pressure 1 lb. per sq. in. = 2.309 ft.

head, or i ft. head = .433 lb. per sq. in.

The total head operating to cause flow is divided into three parts: 1. The velocity-head, which is the height through which a body must fall in vacuo to acquire the velocity with which the water flows into the pipe  $= v^2 + 2g$ , in which v is the velocity in ft. per sec. and 2g = 64.33; 2. the entry-head, that required to overcome the resistance to entrance to the pipe. With sharpedged entrance the entry-head = about 1/6 the velocity-head; with smooth rounded entrance the entry-head is inappreciable; 3. the friction-head, due to the frictional resistance to flow within the pipe.

In ordinary cases of pipes of considerable length the sum of the entry and velocity heads required scarcely exceeds 1 foot. In the case of long pipes with low heads the sum of the velocity and entry heads is generally so small

that it may be neglected.

General Formula for Flow of Water in Pipes or Conduits. Mean velocity in ft. per sec. = c /mean hydraulic radius  $\times$  slope

Do, for pipes running full = 
$$c\sqrt{\frac{\text{diameter}}{4}} \times \text{slope}$$
,

in which c is a coefficient determined by experiment. (See pages 559-564.)

The mean hydraulic radius = Erea of wet cross-section

In pipes running full, or exactly half full, and in semicircular open channels running full it is equal to 1/4 diameter.

The slope = the head for pressure expressed as a head, in feet)  $\rightarrow$  length of pipe measured in a straight line from end to end. In open channels the slope is the actual slope of the surface, or its fall per unit of length, or the sine of the angle of the slope with the horizon. If  $r = \text{mean hydraulic radius}, s = \text{slope} = \text{head} \rightarrow \text{length}, v = \text{velocity in}$ 

feet per second (all dimensions in feet),  $v = c \sqrt{r} \sqrt{s} = c \sqrt{rs}$ ,

Quantity of Water Discharged. -If Q = discharge in cubic feet per second and a = area of channel,  $O = av = ac \sqrt{rs}$ 

a  $\sqrt{r}$  is approximately proportional to the discharge. It is a maximum at 30% corresponding to 19,20 of the diameter, and the flow of a conduit 19,20 full is about 5 per cent greater than that of one completely filled.

### Table giving Fall in Feet per Mile, the Distance on Slope corresponding to a Fall of 1 Ft., and also the Values of s and $\sqrt{s}$ for Use in the Formula $v = c\sqrt{rs}$ .

s = H + L = sine of angle of slope = fall of water-surface(H), in any distance (L), divided by that distance.

Fall in Feet per Mi.	Slope, 1 Foot in	Sine of Slope, s.	√s.	Fall in Feet per Mi.	Slope, 1 Foot in	Sine of Slope,	√s.
0.25	21120 17600	.0000473	.006881	17 18	310.6 293.3	.0032197	.056742
.40	13200	.0000758	.008704	19	277.9	.0035985	.059988
.50	10560	.0000947	.009731	20	264	.0037879	.061546
.60	8800	.0001136	.010660	22	240	.0041667	.064549
702	7520	.0001330	.011532	24	220	.0045455	.067419
.805	6560	.0001524	.012347	26	203.1	.0049242	.070173
.904	5840	.0001712	.013085	28	188.6	.0053030	.072822
1.	5280	.0001894	.013762	30	176	.0056818	.075378
1.25	4224	.0002367	.015386	35.20		.0066667	.081650
1.5	3520	.0002841	.016854	40	132	.0075758	.087039
1.75	3017	.0003314	.018205	44	120	.0083333	.091287
2.	2640	.0003788	.019463	48	110	.0090909	.095346
2.25	2347 2112	.0004261	.020641	52.8 60	100	.010	.1
2.5 2.75	1920	.0004735	.021760	66	88	.0113636	.1066
3.75	1760	.0005208	.023837	70.4	75	.0133333	.115470
3.25	1625	.0006154	.024807	80	66	.0151515	.123091
3.5	1508	.0006631	.025751	88	60	.0166667	1291
3.75	1408	.0007102	.026650	96	55	.0181818	.134839
4	1320	.0007576	.027524	105.6	50	.02	.141421
5	1056	.0009470	.030773	120	44	.0227273	.150756
6	880	.0011364	.03371	132	40	.025	.158114
7 8	754.3	.0013257	.036416	160	33	.0303030	.174077
8	660	.0015152	.038925	220	24	.0416667	.204124
9	586.6	.0017044	.041286	264	20	.05	.223607
10	528	.0018939	.043519	330	16	.0625	.25
11	443.6	.0020833	.045643	440	12	.0833333	.288675
12	440	.0022727	.047673	528	10	.1	.316228
13	406.1	.0024621	.04962	660	8 6	.125	.353558
14 15	377.1 352	.0026515	.051493	880 1056	5	.1666667	.408248
16	330	.0028409	.055048	1320	4	.25	.5
10	990	.0000000	.055048	1020	4	.20	.0

# Values of $\sqrt{r}$ for Circular Pipes, Sewers, and Conduits of different Diameters.

r = mean hydraulic depth =  $\frac{\text{area}}{\text{perimeter}} = \frac{1}{4}$  diam, for circular pipes running full or exactly half full.

Diam., ft. in.	$\sqrt{r}$	Diam., ft, in.	in Feet.	Diam., ft, in,	$\sqrt{r}$	Diam., ft. in.	$\sqrt{r}$
2.0. 111.	in Feet.	10, 111,	in reet.	10, 111,	in Feet.	20. 111.	in Feet.
3/8 1/2 3/4	.088	2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	.707	4 6	1.061	9	1.500
1/9	.102	2 1	.722	4 7	1.070	9 3	1.521
.94	.125	2 2 2 3	.736	4 8 4 9	1.080	9 6	1.541
111	.144	2 3	.750	4 10	1.089		1.561
11/4	.161	2 4	.764 .777		1.099	10 10 3	1.581
122	.177	9 9	.790	4 11	1.118	10 6	1.601
114 1143 134 214 214 3 4 5 6 7 8 9	.204	2 4 2 5 2 6 2 7 2 8 2 9	.804	4 11 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	1.127	10 6	1.620 1.639
91/	.228	5 6	.817	5 9	1.137	11 9	1.658
~72	.251	ñ 6	.829	5 2 5 3	1.146	11 3	1.677
9	.290	2 10	.842	5 4	1.155	11 6	1.696
5	.323	2 11	.854	5 5	1.164	11 9	1.714
6	.354	3 11	.866	5 6	1.173	12	1.732
7	,382	3 1	.878	5 7	1.181	12 3	1.750
8	.408	3 2	.890	5 8	1.190	12 6	1.768
9	.433	3 2 3	.901	5 9	1.199	12 9	1.785
10	.456	3 4	.913	5 10	1.208	13	1.083
11	.479	3 5	.924	5 11	1,216	13 3	1.820
1	.500	3 6	.935	6	1.225	13 6	1.837
1 1	.520	2 11 3 1 3 2 3 3 4 3 5 6 7 3 8 3 10 3 11	.946	6 3	1.250	14	1.871
1 2 1 3	.540	3 8	.957	6 6	1.275	14 6	1.904
1 3	.559	3 9	.968	6 9	1.299	15	1.936
1 4	.577	3 10 3 11	.979	7	1.323	15 6	1.968
1 5	.595	3 11	.990	7 3	1.346	16	2.
1 6	.612	4	1.	7 7 3 7 6 7 9	1.369	16 6	2.031
1 7 1 8 1 9	.629	4 1	1.010	7 9	1.392	17	2.061
1 8	.646	4 1 4 2 4 3 4 4	1.021	8	1.414	17 6	2.091
1 9	.661	4 3	1.031	8 3	1.436	18	2.121
1 10	.677	4 4	1.041	8 8 6 8 9	1.458	19	2.180
1 11	.692	4 5	1.051	8 9	1.479	20	2.236

Values of the Coefficient c. (Chiefly condensed from P. J. Flynn on Flow of Water)—Almost all the old hydraulic formulæ for finding the mean velocity in open and closed channels have constant coefficients, and therefore correct for only a small range of channels. They have often been found to give incorrect results with disastrous effects. Ganguillet and Kutter thoroughly investigated the American, French, and other experiments, and they gave as the result of their labors the formula now generally known as Kutter's formula. There are so many varying conditions affecting the flow of water, that all hydraulic formulæ are only approximations to the correct result.

When the surface-slope measurement is good, Kutter's formula will give results seldom exceeding 71% error, provided the rugosity coefficient of the formula is known for the site. For small open channels D'Arcy's and Bazin's formulæ, and for cast-iron pipes D'Arcy's formulæ, are generally accepted as being approximately correct.

Kutter's Formula for measures in feet is

$$v = \left\{ \frac{\frac{1.811}{n} + 41.6 + \frac{.00281}{s}}{1 + \left(41.6 + \frac{.00281}{s}\right) \times \frac{n}{\sqrt{s}}} \right\} \times \sqrt{rs},$$

in which v = mean velocity in feet per second;  $r = \frac{a}{p} = \text{hydraulic mean}$ 

depth in feet = area of cross-section in square feet divided by wetted perimeter in lineal feet; s = fall of water-surface (h) in any distance (l) divided

by that distance,  $=\frac{n}{l}$ , = sine of slope; n= the coefficient of rugosity, depending on the nature of the lining or surface of the channel. If we let the first term of the right-hand side of the equation equal c, we have Chezy's

formula,  $v = c \sqrt{rs} = c \times \sqrt{r} \times \sqrt{s}$ .

Values of n in Kutter's Formula. The accuracy of Kutter's formula depends, in a great measure, on the proper selection of the coefficient of roughness n. Experience is required in order to give the right value to this coefficient, and to this end great assistance can be obtained, in making this selection, by consulting and comparing the results obtained from experiments on the flow of water already made in different channels.

In some cases it would be well to provide for the contingency of future deterioration of channel, by selecting a high value of n, as, for instance, where a dense growth of weeds is likely to occur in small channels, and also

where channels are likely not to be kept in a state of good repair

The following table, giving the value of n for different materials, is compiled from Kutter, Jackson, and Hering, and this value of n applies also in each instance, to the surfaces of other materials equally rough.

Value of n in Kutter's Formula for Different Channels.

n = .009, well-planed timber, in perfect order and alignment; otherwise, perhaps .01 would be suitable.

n = 0.010, plaster in pure cement; planed timber; glazed, coated, or enamelled stoneware and iron pipes; glazed surfaces of every sort in perfect

n = .011, plaster in cement with one third sand, in good condition; also for

iron, cement, and terra cotta pipes, well joined, and in best order n = .012, unplaned timber, when perfectly continuous on the inside;

n = .013, ashlar and well-laid brickwork; ordinary metal; earthen and stoneware pipe in good condition, but not new; cement and terra-cotta pipe not well jointed nor in perfect order, plaster and planed wood in imperfect or inferior condition; and, generally, the materials mentioned with n=.010, when in imperfect or inferior condition.

n = .015, second class or rough-faced brickwork; well-dressed stonework; foul and slightly tuberculated iron; cement and terra-cotta pipes, with imperfect joints and in bad order; and canvas lining on wooden frames.

n = .017, brickwork, ashlar, and stoneware in an inferior condition; tu-

berculated iron pipes; rubble in cement or plaster in good order; fine graved, well rammed,  $\frac{1}{2}$ 6 to  $\frac{1}{2}$ 6 inch diameter; and, generally, the materials mentioned with n=0.018 when in bad order and condition.

n = .020, rubble in cement in an inferior condition; coarse rubble, rough set in a normal condition; coarse rubble set dry; ruined brickwork and masonry; coarse gravel well rammed, from 1 to 1½ inch diameter; canals with beds and banks of very firm, regular gravel, carefully trimmed and rammed in defective places; rough rubble with bed partially covered with silt and mud; rectangular wooden troughs, with battens on the inside two inches apart; trimmed earth in perfect order.

n = .0225, canals in earth above the average in order and regimen.

n = .025, canals and rivers in earth of tolerably uniform cross-section; slope and direction, in moderately good order and regimen, and free from stones and weeds.

n = .0275, canals and rivers in earth below the average in order and regimen.

n = .030, canals and rivers in earth in rather bad order and regimen, having stones and weeds occasionally, and obstructed by detritus.

 $\bar{n} = .035$ , suitable for rivers and canals with earthen beds in bad order and regimen, and having stones and weeds in great quantities.

n = .05, torrents encumbered with detritus

Kutter's formula has the advantage of being easily adapted to a change in the surface of the pipe exposed to the flow of water, by a change in the value of n. For cast-iron pipes it is usual to use n = .013 to provide for the future deterioration of the surface.

Reducing Kutter's formula to the form  $v = c \times \sqrt{r} \times \sqrt{s}$ , and taking n, the coefficient of roughness in the formula = .011, .012, and .013, and s = .001, we have the following values of the coefficient c for different diameters of

conduit.

# Values of c in Formula $v=c \times \sqrt{r} \times \sqrt{s}$ for Metal Pipes and Moderately Smooth Conduits Generally.

By Kutter's Formula. (s = .001 or greater.)

	- 5					·/	
Diameter	n = .011	n = .012	n = .013	Diameter.	n = .011	n = .012	n = .013
ft. in.	c = 47.1	c =	c =	ft.	c = 152.7	c = 139.2	c = 127.9
2 4 6	61.5 77.4 87.4	77.5	69.5	8 9 10	155.4 157.7 159.7	141.9 144.1 146	130.4 132.7 134.5
1 1 6 2	105.7 116.1 123.6	94.6 104.3 111.3	85.3 94.4 101.1	11 12 14	161.5 163 165.8	147.8 149.3 152	136.2 137.7 140.4
3 4 5	133.6 140.4 145.4	120.8 127.4 132.3	110.1 116.5 121.1	16 18 20	168 169.9 171.6	154.2 156.1 157.7	142.1 144.4 146
6	149.4	136.1	124.8			l	

For circular pipes the hydraulic mean depth r equals  $\frac{1}{2}$  of the diameter. According to Kutter's formula the value of c, the coefficient of discharge, is the same for all slopes greater than 1 in 1000; that is, within these limits c is constant. We further find that up to a slope of 1 in 2640 the value of t is, for all practical purposes, constant, and even up to a slope of 1 in 5000 the difference in the value of c is very little. This is exemplified in the following:

# Value of c for Different Values of $\sqrt{r}$ and s in Kutter's Formula, with n = .013.

	Slopes.								
Vr	1 in 1000 1 in 2500		1 in 3333.3	1 in 5000	1 in 10,000				
1.6	93.6 116.5 142.6	91.5 115.2 142.8	90.4 114.4 143.0	88.4 113.2 143.1	83.3 109.7 143.8				

The reliability of the values of the coefficient of Kutter's formula for pipes of less than 6 in. diameter is considered doubtful. (See note under table on page 564.)

# Values of c for Earthen Channels, by Kutter's Formula, for Use in Formula $v = c \sqrt{rs}$ .

	Co		nt of R = .022		Coefficient of Roughness, $n = .035$ .					
		V	$ar{r}$ in fe	et.	$\sqrt{r}$ in feet.					
	0.4   1.0   1.8   2.5   4.0					0.4	1.0	1.8	2.5	4.0
Slope, 1 in	c	· c	$\overline{c}$	c	c	c	c	c	c	c
1000	35.7	62.5	80.3	89.2	99.9	19.7	37.6	51.6	59.3	69.2
1250 1667	35.5 35.2	62.3 62.1	80.3 80.3	89.3 89.5	100.2	19.6 19.4	37.6	51.6	59.4 59.5	69.4 69.8
2500	34.6	61.7	80.3	89.8	101.4	19.1	37.1	51.6	59.7	70.4
3333	34.	61.2	80.3	90.1	102.2	18.8	36.9	51.6	59.9	71.0
5000	33.	60.5	80.3	90.7	103.7	18.3	36.4	51.6	60.4	72.2
7500	31.6	59.4	80.3	91.5	106.0	17.6	35.8	51.6	60.9	73.9
10000	30.5   58.5   80.3   92.3   107.9					17.1	35.3	51.6	60.5	75.4
15840	28.5	56.7	80.2	93.9	112.2	16.2	34.3	51.6	62.5	78.6
20000	27.4	55.7	80.2	94.8	115.0	15.6	33.8	51.5	63.1	80.6

Mr. Molesworth, in the 22d edition of his "Pocket-book of Engineering Formula," gives a modification of Kutter's formula as follows: For flow in east-iron pipes,  $v = c \sqrt{rs}$ , in which

$$c = \frac{181 + \frac{.00281}{s}}{1 + \frac{.026}{\sqrt{d}} \left(41.6 + \frac{.00281}{s}\right)},$$

in which d = diameter of the pipe in feet.

(This formula was given incorrectly in Molesworth's 21st edition.)

**Molesworth's Formula.**  $-v = \sqrt{krs}$ , in which the values of k are as follows:

	Values of k for Velocities.				
Nature of Channel.	Less than 4 ft. per sec.	More than 4 ft. per sec.			
Brickwork Earth Shingle Rough, with bowlders.	8800 7200 6400 5300	8500 6800 5900 4700			

In very large channels, rivers, etc., the description of the channel affects the result so slightly that it may be practically neglected, and k assumed = from 8500 to 9000.

**Flynn's Formula.**—Mr. Flynn obtains the following expression of the value of Kutter's coefficient for a slope of .001 and a value of n = .013:

$$c = \frac{183.72}{1 + \left(44.41 \times \frac{.013}{\sqrt{r}}\right)}$$

The following table shows the close agreement of the values of c obtained from Kutter's, Molesworth's, and Flynn's formulæ:

Slope.	Kutter.	Molesworth.	Flynn.
1 in 40	71.50	71.48	69.5
1 in 1000	69.50	69.79	69.5
1 in 400	117.	117.	116.5
1 in 1000	116.5	116.55	116.5
	130.5	130.68	130.5
1 in 2600	129.8	129.93	130.5
	1 in 40 1 in 1000 1 in 400 1 in 1000	1 in 40 71.50 1 in 1000 69.50 1 in 400 117. 1 in 1000 116.5 1 in 700 130.5	1 in     40     71.50     71.48       1 in     1000     69.50     69.79       1 in     400     117.     117.       1 in     100     116.5     116.5       1 in     700     180.5     180.68

Mr. Flynn gives another simplified form of Kutter's formula for use with different values of n as follows:

$$v = \left(\frac{K}{1 + \left(44.41 \times \frac{n}{\sqrt{r}}\right)}\right) \sqrt{rs}.$$

In the following table the value of K is given for the several values of n:

n	K	n	K	n	K	n	K	n	K
.009 .010 .011	245.63 225.51 209.05	.013	195.33 183.72 137.77	.016	157.6	.019	139 73	022	196 73

If in the application of Mr. Flynn's formula given above within the limits of n as given in the table, we substitute for n, K, and  $\sqrt{r}$  their values, we have a simplified form of Kutter's formula.

For instance, when n = .011, and d = 3 feet, we have

$$v = \frac{209.05}{1 + \left(44.41 \times \frac{.011}{.866}\right)} \times \sqrt{rs}.$$

Bazin's Formulæ:

For very even surfaces, fine plastered sides and bed, planed planks, etc.,

$$v = \sqrt{1 \div .0000045 \left(10.16 + \frac{1}{r}\right)} \times \sqrt{rs}.$$

For even surfaces such as cut-stone, brickwork, unplaned planking, mortar, etc. :

$$v = \sqrt{1 \div .000013 \left(4.354 + \frac{1}{r}\right)} \times \sqrt{rs}.$$

For slightly uneven surfaces, such as rubble masonry:

$$v = \sqrt{1 \div .00006 \left(1.219 + \frac{1}{r}\right)} \times \sqrt{rs}$$

For uneven surfaces, such as earth;

$$v = \sqrt{1 \div .00035 \left(0.2438 + \frac{1}{r}\right)} \times \sqrt{rs}.$$

A modification of Bazin's formula, known as D'Arcy's Bazin's;

$$v = r \sqrt{\frac{1000s}{.08534r + 0.35}}.$$

For small channels of less than 20 feet bed Bazin's formula for earthen channels in good order gives very fair results, but Kutter's formula is superseding it in almost all countries where its accuracy has been investigated.

The last table on p. 561 shows the value of c, in Kutter's formula, for a wide age of channels in earth, that will cover anything likely to occur in the ordinary practice of an engineer.

D'Arcy's Formula for clean iron pipes under pressure is

$$v = \left\{ \frac{rs}{.00007726 + \frac{.00000162}{r}} \right\}^{\frac{1}{2}}$$

Flynn's modification of D'Arcy's formula is

$$v = \left(\frac{155256}{12d+1}\right)^{1/2} \times \sqrt{rs}$$

in which d = diameter in feet.

D'Arcy's formula, as given by J. B. Francis, C.E., for old cast-iron pipe, lined with deposit and under pressure, is

$$v = \left(\frac{144d^2s}{.0082(12d+1)}\right)^{\frac{1}{2}}$$
.

Flynn's modification of D'Arcy's formula for old cast-iron pipe is

$$v = \left(\frac{70243.9}{12d. + 1}\right) \times \sqrt{rs}.$$

For Pipes Less than 5 inches in Diameter, coefficients (c) in the formula  $v = c \sqrt{rs}$ , from the formula of D'Arcy, Kutter, and Fanning.

Diam. D'Ar in for Cl inches. Pip	lean non	IUI CICan	Diam.	D'Arcy, for Clean Pipes.	Kutter, for $n = .011$ $s = .001$	Fanning, for Clean Iron Pipes.
36 59, 15 65, 34 74, 1 80, 114 84, 115 88.	7 36.1 5 42.6 4 47.4 8 51.9	80.4	13/4 2 21/2 3 4 5	90.7 92.9 96.1 98.5 101.7 103.8	58.8 61.5 66. 70.1 77.4 82.9	92.5 94.8 96.6 103.4

Mr. Flynn, in giving the above table, says that the facts show that the coefficients diminish from a diameter of 5 inches to smaller diameters, and it is a safer plan to adopt coefficients varying with the diameter than a constant coefficient. No opinion is advanced as to what coefficients should be used with Kutter's formula for small diameters. The facts are simply stated, giving the results of well-known authors.

Older Formulæ.—The following are a few of the many formulæ for flow of water in pipes given by earlier writers. As they have constant coefficients, they are not considered as reliable as the newer formulæ.

Prony, 
$$v=97 \sqrt{rs}-.08$$
;  
Eytelwein,  $v=50 \sqrt{\frac{dh}{l+50d}}$ , or  $v=108 \sqrt{rs}-0.13$ ;  
Hawksley,  $v=48 \sqrt{\frac{dh}{l+54d}}$ ; Neville,  $v=140 \sqrt{rs}-11 \sqrt[3]{rs}$ .

In these formulæ d = diameter in feet; h = head of water in feet; l = diameterlength of pipe in feet;  $s = \text{sine of slope} = \frac{h}{l}$ ; r = mean hydraulic depth,

= area 
$$\div$$
 wet perimeter =  $\frac{d}{4}$  for circular pipe.

Mr. Santo Crimp (Eng'g, August 4, 1893) states that observations on flow in brick sewers show that the actual discharge is 33% greater than that calculated by Eytelwein's formula. He thinks Kutter's formula not superior to D'Arcy's for brick sewers, the usual coefficient of roughness in the former, viz., 013, being too low for large sewers and far too small in the case of small sewers.

D'Arcy's formula for brickwork is

$$v=rac{\sqrt{2g}}{m}rs$$
 ;  $m=a\Big(1+rac{B}{r}\Big)$  ;  $a=.0037285$  ;  $B=.229663$ .

# VELOCITY OF WATER IN OPEN CHANNELS.

Irrigation Canals,—The minimum mean velocity required to prevent the deposit of silt or the growth of aquatic plants is in Northern India taken at 1½ feet per second. It is stated that in America a higher velocity is required for this purpose, and it varies from 2 to 3½ feet per second. The maximum allowable velocity will vary with the nature of the soil of the bed. A sandy bed will be disturbed if the velocity exceeds 3 feet per second. Good loam with not too much sand will bear a velocity of 4 feet per second. The Cavour Canal in Italy, over a gravel bed, has a velocity of about 5 per second. (Flymi's "Irrigation Canals.")

Mean Surface and Rottom Velocities.—According to the for-

Mean Surface and Bottom Velocities.-According to the formula of Bazin,

d.

 $v_b = v - 10.87 \sqrt{rs}$ , in which v = mean velocity in feet per second, vmax = maximum surface velocity in feet per second, vb = bottom velocity in feet per second, r = hydraulic mean depth in feet = area of cross-section

In feet per second,  $\gamma$  = nyurating mean depin in feet, z = sine of closes of the in square feet divided by wetted perimeter in feet, z = sine of slope. The least velocity, or that of the particles in contact with the bed, is almost as much less than the mean velocity as the greatest velocity is

greater than the mean.

Rankine states that in ordinary cases the velocities may be taken as bearing to each other nearly the proportions of 3, 4, and 5. In very slow currents they are nearly as 2, 3, and 4.

Safe Bottom and Mean Velocities.—Ganguillet & Kutter give

the following table of safe bottom and mean velocity in channels, calculated

from the formula  $v = v_b + 10.87 \sqrt{rs}$ :

Material of Channel.	Safe Bottom Veloc ity $vb$ , in feet per second.	Mean Velocity $v$ , in feet per second.
Soft brown earth Soft loam Sand Gravel Pebbles Broken stone, flint Conglomerate, soft slate.	0.499 1.000 1.998 2.999 4.003 4.988	0.328 0.656 1.312 2.625 3.938 5.579 6.564
Stratified rock	6.006 10.009	8.204 13.127

Ganguillet & Kutter state that they are unable for want of observations to judge how far these figures are trustworthy. They consider them to be rather disproportionately small than too large, and therefore recommend them more confidently.

Water flowing at a high velocity and carrying large quanties of silt is very destructive to channels, even when constructed of the best masonry.

Resistance of Soils to Erosion by Water.—W. A. Burr, Eng'g News, Feb. 8, 1894, gives a diagram showing the resistance of various soils to

erosion by flowing water.

Experiments show that a velocity greater than 1.1 feet per second will erode sand, while pure clay will stand a velocity of 7.35 feet per second. The greater the proportion of clay carried by any soil, the higher the permissible velocity. Mr. Burr states that experiments have shown that the line describing the power of soils to resist erosion is parabolic. From his diagram the following figures are selected representing different classes of soils:

Pure sand resists erosion by flow of	1.1	feet per	secon
Sandy soil, 15% clay	1.2	4.0	46
Sandy loam, 40% clay	1.8	44	4.6
Loamy soil, 65% clay	3.0	66	66
Clay loam, 85% clay	4.8	44	44
Agricultural clay, 95% clay	6.2	66	6.6
Clay	7 3	5 "	4.6
Can't the care of		•	

Abrading and Transporting Power of Water.—Prof. J. LeConte, in his "Elements of Geology," states:

The erosive power of water, or its power of overcoming cohesion, varies as the square of the velocity of the current.

The transporting power of a current varies as the sixth power of the velocity. \*\* \* If the velocity therefore be increased ten times, the transporting power is increased 1,000,000 times. A current running three feet per second, or about two miles per hour, will bear fragments of stone of the size of a hen's egg, or about three ounces weight. A current of ten miles an hour will bear fragments of one and a half tons, and a torrent of twenty willow the bear fragments of one and a half tons, and a torrent of twenty

miles an hour will carry fragments of 100 tons.

The transporting power of water must not be confounded with its erosive power. The resistance to be overcome in the one case is weight, in the other, cohesion; the latter varies as the square: the former as the sixth power of the velocity.

In many cases of removal of slightly cohering material, the resistance is a

mixture of these two resistances, and the power of removing material will

vary at some rate between v2 and v6.

Baldwin Latham has found that in order to prevent deposits of sewage silt in small sewers or drains, such as those from 6 inches to 9 inches diameter, a mean velocity of not less than 3 feet per second should be produced. Sewers from 12 to 24 inches diameter should have a velocity of not less than 21/6 feet per second, and in sewers of larger dimensions in no case should the

velocity be less than 2 feet per second. The specific gravity of the materials has a marked effect upon the mean velocities necessary to move them. T. E. Blackwell found that coal of a sp. gr. of 1.26 was moved by a current of from 1.25 to 1.50 ft. per second, while stones of a sp. gr. of 2.32 to 3.00 required a velocity of 2.5 to 2.75 ft. per

second.

Chailly gives the following formula for finding the velocity required to move rounded stones or shingle:

$$v = 5.67 \sqrt{ag}$$

in which v = velocity of water in feet per second. a = average diameter in

feet of the body to be moved, g = its specific gravity.

Geo. Y. Wisner, Eng'n News, Jan 10, 1885, doubts the general accuracy of statements made by many authorities concerning the rate of flow of a current and the size of particles which different velocities will move. He says:

The scouring action of any river, for any given rate of current, must be an inverse function of the depth. The fact that some engineer has found that a given velocity of current on some stream of unknown depth will move sand or gravel has no bearing whatever on what may be expected of currents of the same velocity in streams of greater depths. In channels 3 to 5. rents of the same velocity in streams of greater depths. In challenes to the fit deep a mean velocity of 3 to 5 ft. per second may produce rapid seouring, while in depths of 18 ft. and upwards current velocities of 6 to 8 ft. per second often have no effect whatever on the channel bed.

Grade of Sewers.—The following empirical formula is given in Baumeister's "Cleaning and Sewerage of Cities," for the minimum grade for a sewer of clear diameter equal to d inches, and either circular or oval in

section:

Minimum grade, in per cent, 
$$=\frac{100}{5d+50}$$
.

As the lowest limit of grades which can be flushed, 0.1 to 0.2 per cent may be assumed for sewers which are sometimes dry, while 0.3 per cent is allowable for the trunk sewers in large cities. The sewers should run dry as rarely as possible.

Relation of Diameter of Pipe to Quantity Discharged.-In many cases which arise in practice the information sought is the diame-In many cases when a use in plactice in mornation source as the recessary to supply a given quantity of water under a given head. The diameter is commonly taken to vary as the two-fifth power of the discharge. This is almost certainly too large. Hagen's formula, with Prof.

387 , where c = .239 when d and Q Unwin's coefficients, give d = c/

are in feet and cubic feet per second.

Mr. Thrupp has proposed a formula which makes d vary as the .383 power of the discharge, and the formula of M. Vallot, a French engineer, makes d vary as the .375 power of the discharge. (Engineering.)

#### FLOW OF WATER-EXPERIMENTS AND TABLES.

The Flow of Water through New Cast-iron Pipe was recently measured by S. Bent Russell, of the St. Louis, Mo., Water-works. The pipe was 12 inches in diameter, 1631 feet long, and laid on a uniform grade from end to end. Under an average total head of 3.36 feet the flow was 43,200 cubic feet in seven hours; under an average head of 3.37 feet the flow was the same; under an average total head of 3.41 feet the flow was 46,700 cubic feet in 8 hours and 35 minutes. Making allowance for loss of head due to entrance and to curves, it was found that the value of c in

the formula v=c  $\sqrt{rs}$  was from 88 to 93 (Eng'g Record, April 14, 1894. Flow of Water in a 20-inch Pipe 75,000 Feet Long.—A comparison of experimental data with calculations by different formulæ is given by Chas. B. Brush, Trans. A. S. C. E., 1888. The pipe experimented with was that supplying the city of Hoboken, N. J.

RESULTS OBTAINED BY THE HACKENSACK WATER COMPANY, FROM 1882-1887, IN PUMPING THROUGH A 20-IN. CAST-IRON MAIN 75.000 FEET LONG.

Pressu	re in lbs	s, per sq.	in. at p	umping-	station:			
	95	100	105	110	115	120	125	130
Total e		head in						
	55	66	77	89	100	112	123	135
Discha	rge in T	J. S. gall	ons in 24	4 hours,	1 = 1000	:		
	2,848	3,165	3,354	3,566	3,804	3,904	4,116	4,255
Actual	velocit	y in mai	n in feet	per sec	ond:			
	2.00	2.24	2.36	2.52	2,68	2.76	2.92	3.00
Cost o	f coal co	onsumed	in deliv	ering ea	ch millic	n gals. a	t given	velocities:
	\$8.40	\$8.15	\$8.00	\$8.10	\$8.30	\$8.60	\$9.00	\$9.60
Theore	etic <mark>al</mark> di	scharge	by D'Ar	cy's fori	nula:			
	2,743	3,004	3,244	3,488	3,699	3,915	4,102	4,297

Velocities in Smooth Cast-iron Water-pipes from 1 Foot to 9 Feet in Diameter, on Hydraulic Grades of 0.5 Foot to 8 Feet per Mile; with Corresponding Values of c in V=c  $\sqrt{rs}$ . (D. M. Greene, in Eng'g News, Feb. 24, 1894.)

me-	drau- Mean adii.		Hydraulic Grade; Feet per Mile $= h$ .						
Diame-	H. H.	h = 0.5 s = 0.0000947	1.0 0.0001894	1.5 0.0002841	2.0 0.0003788	3.0 0.0005682	4.0 0.0007576		
1.	0.25 {	V = 0.4542 $c = 92.7$	0.6673 97.0	0.8356 99.1	0.9803 100.7	1.2277 103.0	1.4402 104.7		
2.	0.5	V = 0.7359 c = 106.6 V = 0.9733	1.0793 110.9 1.4298	1.3516 113.4 1.7906	1.5856 115.2 2.1017	1.9857 117.9 2.6306	2.3294 119.7 3.0860		
3. 4.	0.75	c = 115.5 V = 1.1883	119.9 1.7456	122.6 2.1861	124.4 2.5645	127.5 3.2116	129.5 3.7676		
5.	1.25	c = 122.1 $V = 1.3872$ $c = 127.5$	126.8 2.0379 132.4	129.7 2.5521 135.5	131.8 2.9939 137.6	134.7 3.7493 140.7	136.9 4.3983 142.9		
6.	1.5	V = 1.5742 $c = 132.1$	2.3126 137.8	2.8961 140.3	3.3975 142.6	4.2548 145.8	4.9913 148.1		
7.	1.75	V = 1.7518 c = 135.9 V = 1.9218	2.5736 141.4 2.8234	3.2230 146.0 3.5358	3.7809 146.8 4.1479	4.7350 150.2 5.1945	5.5546 152.5 6.0936		
8. 9.	2.0 {	c = 139.7 V = 2.0854	145.1 3,0638	148.4 3.8368	150.7 4.5010	154.1 5.6368	156.5 6.6125		
	1	c = 142.9	148.4	151.7	154.2	157.6	160.1		

The velocities in this table have been calculated by Mr. Greene's modifi-The velocities in this table have been calculated by Mr. Greene's modification of the Chezy formula, which modification is found to give results which differ by from 1.29 to -2.65 per cent (average 0.9 per cent) from very carefully measured flows in pipes from 16 to 48 inches in diameter, on grades from 1.68 feet to 10.296 feet per mile, and in which the velocities ranged from 1.57 to 6.195 feet per second. The only assumption made is that the modified formula for V gives correct results in conduits from 4 feet to 9 feet in diameter, as it is known to do in conduits less than 4 feet in diameter. Other articles on Flow of Water I loop tubes are to be found in Engl of Mews as follos a 6.3 carsons. Sept. 23, 153, are to be found in Engl of 23, March 9, 16, and 3, 1889; J. L. Fingerial, Sept. 6 and 13, 1889; Jas. Duane, Jan. 2, 1892; J. T. Fanning, July 11, 1892; A. N. Talbot, Ang. 11, 1892.

Flow of Water in Circular Pipes, Sewers, etc., Flowing Full. Based on Kutter's Formula, with n=.013.

Discharge in cubic feet per second.

Diam-	Slope, or Head Divided by Length of Pipe.								
eter.	1 in 40	1 in 70	1 in 100	1 in 200	1 in 300	1 in 400	1 in 500	1 in 600	
5 in.	.456	.344	.288	.204	.166	.144	.137	.118	
6 "	.762	.576	.482	.341	.278	.241	.280	.197	
7 "	1.17	.889	.744	.526	.430	.372	.355	.304	
8 "	1.70	1.29	1.08	.765	.624	.54	.516	.441	
9 "	2.37	1.79	1.50	1.06	.868	.75	.717	.613	
Slope	1 in 60	1 in 80	1 in 100	1 in 200	1 in 300	1 in 400	1 in 500	1 in 600	
10 in.	2.59	2.24	2.01	1.42	1.16	1.00	.90	.82	
11 "	3.39	2 94	2.63	1.86	1.52	1.31	1.17	1.07	
12 "	4.32	3.74	3.35	2.37	1.93	1.67	1.5	1.37	
13 "	5.38	4.66	4.16	2.95	2.40	2.08	1.86	1.70	
14 "	6.60	5.72	5.15	3.62	2.95	2.57	2.29	2.09	
Slope	1 in 100	1 in 200	1 in 800	1 in 400	1 in 500	1 in 600	1 in 700	1 in 800	
15 in,	6.18	4 37	3.57	3.09	2.77	2.52	2.34	2.19	
16 "	7.38	5.22	4.26	3.69	3.30	3.01	2.79	2.61	
18 "	10.21	7.22	5.89	5.10	4.56	4.17	3.86	3.61	
20 "	13.65	9.65	7.88	6.82	6.10	5.57	5.16	4.83	
22 "	17.71	12.52	10.22	8.85	7.92	7.23	6.69	6.26	
Slope 2 ft. 2 ft. 2 in. 2 " 4 " 2 " 6 " 2 " 8 "	1 in 200	1 in 400	1 in 600	1 in 800	1 in 1000	1 in 1250	1 in 1500	1 in 1800	
	15.88	11.23	9.17	7.94	7.10	6.35	5 80	5.29	
	19.73	13.96	11.39	9.87	8.82	7.89	7.20	6.58	
	24.15	17.07	13.94	12.07	10.80	9 66	8.82	8.05	
	29.08	20.56	16.79	14.54	13.00	11.63	10.62	9.69	
	34.71	24.54	20.04	17.35	15.52	13.88	12.67	11.57	
Slope 2 ft. 10 in. 3 " 2 in. 3 " 4 " 3 " 6 "	1 in 500	1 in 750	1 in 1000	1 in 1250	1 in 1500	1 in 1750	1 in 2000	1 in 2500	
	25.84	21.10	18.27	16.34	14.92	13.81	12.92	11.55	
	30.14	24.61	21.31	19.06	17.40	16.11	15.07	13.48	
	34.90	28.50	24.68	22.07	20.15	18.66	17.45	15.61	
	40.08	32 72	28.34	25.35	23.14	21.42	20.04	17.93	
	45.66	37.28	32.28	28.87	26.36	24.40	22.83	20.41	
Slope 3 ft. 8 in. 3 " 10 " 4 " 4 " 6 iu. 5 "	1 in 500	1 in 750	1 in 1000	1 in 1250	1 in 1500	1 in 1750	1 in 2000	1 in 2500	
	51.74	42.52	36.59	32.72	29.87	27.66	25.87	23.14	
	58.36	47.65	41.27	36 91	33.69	31.20	29.18	26.10	
	65.47	53.46	46.30	41.41	37.80	34.50	32.74	29.28	
	89.75	73.28	63.47	56.76	51.82	47.97	44.88	40.14	
	118.9	97.09	84.08	75.21	68.65	68.56	59.46	53.18	
Slope 5 ft. 6 in. 6 " 6 " 6 " 7 " 7 " 6 "	1 in 750	1 in 1000	1 in 1500	1 in 2000	1 in 2500	1 in 3000	1 in 3500	1 in 4000	
	125.2	108.4	88.54	76.67	68.58	62.60	57.96	54.21	
	157.8	136.7	111 6	96.66	86.45	78.92	73.07	68 35	
	195.0	168.8	137.9	119.4	106.8	97.49	90.26	84.43	
	237.7	205.9	168.1	145.6	130.2	118.8	110.00	102.9	
	285.3	247.1	201.7	174.7	156.3	142.6	132.1	123.5	
Slope 8 ft. 8 " 6 in. 9 " 6 "	1 in 1500 239.4 281.1 327.0 376.9 431.4	1 in 2000 207.3 243.5 283.1 326.4 373.6	1 in 2500 195.4 217.8 253.3 291.9 334.1	1 in 3000 169.3 198.8 231.2 266.5 305.0	1 in 3500 156.7 184.0 214.0 246.7 282.4	1 in 4000 146.6 172.2 200.2 230.8 264.2	1 in 4500 138.2 162.3 188.7 217.6 249.1	1 in 5000 131.1 154.0 179.1 206.4 236.3	

For U. S. gallons multiply the figures in the table by 7.4805. For a given diameter the quantity of flow varies as the square root of the sine of the slope. From this principle the flow for other slopes than those given in the table may be found. Thus, what is the flow for a pipe 8 feet diameter, slope 1 in 125? From the table take Q=207.3 for slope 1 in 2000, The given slope 1 in 125 is to 1 in 2000 as 16 to 1, and the square root of this ratio is 4 to 1. Therefore the flow required is  $207.3 \times 4 = 829.2$  cu, ft.

### Circular Pipes, Conduits, etc., Flowing Full.

Values of the factor ac  $\sqrt{r}$  in the formula Q=ac  $\sqrt{r}\times\sqrt{s}$  corresponding to different values of the coefficient of roughness, n. (Based on Kutter's formula.)

Value of  $ac \sqrt{r}$ .

ë	3		1	1			
ft.		n = .010.	n = .011.	n = .012.	n = .013.	n = .015.	n = .017.
	6	6.906	6.0627	5.3800	4.8216	3,9604	3.329
	9	21.25	18.742	16.708	15.029	12,421	10.50
1	-	46.93	41.487	37.149	33.497	27.803	23 60
î	3	86.05	76.347	68.44	61.867	51.600	43,93
i	6	141.2	125.60	112.79	102.14	85,496	72.99
1	9	214.1	190.79	171.66	155.68	130 58	111.8
5		307.6	274.50	247.33	224.63	130.58 188.77	164
2	3	421.9	377.07	340.10	309.23	260 47	223,9
2	6	559.6	500.78	452.07	411.27	260.47 347.28	299.3
2	9	722.4	647.18	584.90	582.76	451.23	388.8
3		911.8	817.50	739.59	674.09	570.90	493.3
3	3	1128.9	1013.1	917.41	836.69	709.56	613.9
3	3 6	1374.7	1234.4	1118.6	1021.1	866.91	750.8
3	9	1652.1	1484.2	1345.9	1229.7	1045	906
4		1962.8	1764.3	1600.9	1463.9	1245.3	1080.7
111122223333444556667788899	6	2682.1	2413.3	2193	2007	1711.4	1487.3
5		3543	3191.8	2903.6	2659	2272.7	1977
5	6	4557.8	4111.9	3742.7	3429	2934.8	2557.2
6		5731.5	5176.3	4713.9	4322	3702.3	3232.5
6	6	7075.2	6394.9	5825.9	5339	4588.3	4010
7		8595.1	7774.3	7087	6510	5591.6	4893
7	6	10296	9318.3	8501.8	7814	6717	5884.2
8		12196	11044	10083	9272	7978.3	6995.3
8	6	14298	12954	11832	10889	9377.9	8226.3
9		16604	15049	18751	12663	10917	9580.7
	6	19118	17338	15847	14597	12594	11061
10		21858	19834	18134	16709	14426	12678
10	6	24823	22534	20612 23285	18996	16412	14424
11		28020	25444		21464	18555	16333
11 12	6	31482 35156	28593 31937	26179 29254	24139 26981	20879	18395
12	6	39104	35529	32558	30041	26012	20584 22938
13	0	43307	39358	36077	33301	28850	25451
13	6	47751	43412	39802	36752	31860	28117
14	١	52491	47739	43773	40432	35073	30965
14	6	57496	52308	47969	44322	38454	33975
15	0	62748	57103	52382	48413	42040	37147
16		74191	67557	62008	57343	49823	44073
17		86769	79050	72594	67140	58387	51669
18		100617	91711	84247	77932	67839	60067
19		115769	105570	96991	89759	78201	69301
20		132133	120570	110905	102559	89423	79259
FI	011	of Wate	r in Circu	lar Pipes	, Conduit	s, etc., F	lowing

# Flow of Water in Circular Pipes, Conduits, etc., Flowing under Pressure.

Based on D'Arcy's formulæ for the flow of water through cast-iron pipes. With comparison of results obtained by Kutter's formula, with n=.013. (Condensed from Flynn on Water Power.)

Values of a, and also the values of the factors c  $\sqrt{r}$  and ac  $\sqrt{r}$  for use in the formulæ Q = av; v = c  $\sqrt{r} \times \sqrt{s}$ , and Q = ac  $\sqrt{r} \times \sqrt{s}$ .

Q= discharge in cubic feet per second, a= area in square feet, v= velocity in feet per second, r= mean hydraulic depth, ½ diam. for pipes running full, s= site of slope,

(For val	lues of $\sqrt{s}$	see page	558.)			
Size o	f Pipe.	Clean P	Cast-iron ipes	Value of	Old Cast- Lined wit	iron Pipes h Deposit.
d= diam. in ft. in.	in III		For Discharge, $ac \sqrt{r}$ .	$ac \sqrt{r}$ by Kutter's Formula, when $n = .013$ .	For Velocity,	For Discharge, ac $\sqrt{r}$ .
36 34 114 1134 215 134 4 5 5 6 6 6 6 6 7 7 6 6 8 6 6 9 9 6 10	.00077 .00136 .00367 .001862 .002475 .001852 .01227 .011670 .02182 .0341 .0491 .0873 .136 .196 .267 .349 .442 .5445 .660 .17755 .1.000 .1.386 .1.0000 .1.0000 .1.0000 .1.0	5. 251 6. 702 9. 309 113. 68 17. 32 15. 58 17. 32 33. 54 37. 28 33. 54 49. 45 52. 16 54. 63 48. 75 49. 45 55. 16 56. 64 67. 75 77. 77. 73. 22 78. 80 88. 19 99. 99. 99 99. 99.	.00408 .00914 .02855 .06634 .11659 .11659 .19155 .28936 .41357 .74786 .1.2089 2.5630 4.5610 7.3068 20.652 26.952 26.952 34.428 42.918 63.435 88.886 119.72 156.46 198.83 247.57 302.90 365.14 433.93 511.10 7.8686,17 688.67 7.8684 7.87 1011.2 1136.5 1271.4 1414.7 1647.6 1901.9 1276.1 2476.4 2799.7	4.832 15.03 33.50 102.14 224.63 411.37 674.09 1021.1 1463.9 2007 2659 3429	3. 532 4. 507 6. 261 9. 255 11. 65 11. 65 11. 76 16. 56 19. 75 22. 56 25. 07 22. 33 29. 42 33. 26 33. 26 33. 26 33. 26 33. 26 34. 28 35. 26 36. 75 37 48. 34 49. 45 57 48. 34 57 48. 34 57 57 57 57 57 57 57 57 57 57 57 57 57	.00272 .00613 .01922 .04257 .07885 .12845 .12845 .12845 .13841 .17246 .3.0681 .4.9147 .7.2995 .10.271 .13.891 .18.129 .23.158 .28.867 .28.968 .59.788 .6681 .30.681 .40.47 .209.78 .40.68 .59.788 .6681 .66.41 .203.74 .245.60 .278 .29.87 .340.8 .340.
5 6 5 9 6	25.967 28.274	135.4 138.4	3516 3912.8	4322	91.08 93.08	2365 2631.7
6 6 7 7 6	38.183 38.485 44.179	144.1 149.6 154 9	4782.1 5757.5 6841.6	5339 6510 7814 9272	96.93 100.61 104.11 107.61	3216.4 3872.5 4601.9
8 6	50.266 56.745	160 165	8043 9364.7	10889	111	5409.9 6299.1 7967.3
9 9 6 10	63.617 70.882 78.540	169.8 174.5 179.1	10804 12370 14066	12663 14597 16709	114.2 117.4 120.4	7267.3 8320.6 9460.9

Size of Pipe.				Cast-iron ipes.	Value of	Old Cast-iron Pipet Lined with Deposit.			
d= diam. in ft. in.		a = area in square feet.	For Velocity, $c \sqrt{r}$ .	For Discharge,	$\begin{array}{c} ac \sqrt{r} \text{ by } \\ \text{Kutter's } \\ \text{Formula, } \\ \text{when } \\ n = .013 \end{array}$	For Velocity, $c \sqrt{r}$ .	For Discharge, ac √r.		
10	6	86.590	183.6	15893	18996	123.4	10690		
11	v	95.033	187.9	17855	21464	126.3	12010		
11	6	103.869	192.2	19966	24139	129.3	13429		
12	•	113.098	196.3	22204	26981	132	14935		
12	6	122 719	200.4	24598	30041	134.8	16545		
13	•	132.733	204.4	27134	33301	137.5	18252		
13	6	143.139	208.3	29818	36752	140.1	20056		
14	•	153.938	212.2	32664	40432	142.7	21971		
14	6	165.130	216.0	35660	44322	145.2	23986		
15		176.715	219.6	38807	48413	147.7	26103		
15	6	188.692	223.3	42125	52753	150.1	28335		
16		201.062	226.9	45621	57343	152.6	30686		
16	6	213.825	230.4	49273	62132	155	33144		
17		226.981	233.9	53082	67140	157.3	35704		
17	6	240.529	237.3	57074	72409	159.6	38389		
18		254.470	240.7	61249	77932	161.9	41199		
19		283.529	247.4	70154	89759	166.4	47186		
20		314.159	253.8	79736	102559	170.7	53633		

# Flow of Water in Circular Pipes from ¾ inch to 12 inches Diameter.

Based on D'Arcy's formula for clean cast-iron pipes.  $Q = ac \sqrt{r} \sqrt{s}$ .

Value of	Dia.	Slope, or Head Divided by Length of Pipe.									
ac √r.	in.	1 in 10.	1·in 20.	1 in 40.	1 in 60.	1 in 80.	1 in 100.	1 in 150.	1 in 200.		
			Quan	tity in	cubic	feet p	er sec	ond.	-		
.00403	3/6	.00127	.00090	.00064	.00052	.00045	.00040	.00033	.00028		
.00914	1%	.00289	.00204	.00145	.00118	.00102	.00091	.00075	.00065		
.02855	3/8 1/9 3/4	.00903	.00638	.00451	.00369	.00319	.00286	.00233	.00202		
.06334	1	.02003		.01001	.00818	.00708			.00448		
.11659	11/4	03687	.02607	.01843	.01505	.01303	.01166		.00824		
.19115	11/4 13/4	.06044		.03022	.02468	.02137			.01352		
.28936	13/4	.09140	.06470	.04575	.03736	.03235	.02894	.02363	.02046		
.41357	5	.13077	.09247	.06539	.05339	.04624	.04136		.02927		
.74786	21/2	.23647	.16722	.11824	.09655	.08361	.07479	.06106	.05288		
1.2089		.38225	.27031	.19113	.15607	.13515			.08548		
2.5630	4	.81042	.57309		.33088	.28654	.25630		.18123		
4.5610	5	1.4422	1.0198	.72109	.58882				.32251		
7.3068	6	2.3104	1.6338	1.1552	.94331	.81690			.51666		
10.852	7	3.4314	2.4265	1.7157	1.4110	1.2132	1.0852	.88607	.76734		
15.270	8	4.8284 6.5302	3.4143 4.6178	$2.4141 \\ 3.2651$	1.9713	1.7072	1.5270 2.0652	1.2468	1.0797		
20.652 26.952	10	8.5222	6.0265	4.2611	3.4795	3.0132	2.6952	2.2006	1.4603		
34.428	11	10.886	7.6981	5.4431	4.4447	3.8491	3.4428	2.8110	2 4344		
42.918	12	13.571	9.5965	6.7853	5.5407	4.7982	4.2918	3.5043	3.0347		
42.310	110	10.571	0.0000	0.1000	0.0401	1.1000	4.2010	0.0040	5.0041		
Value of 4	/s =	.3162	.2236	.1581	.1291	.1118	.1	.08165	.07071		

Value of	Dia.	Slope, or Head Divided by Length of Pipe.									
ac √r.	in.	1 in 250.	1 in 300.	1 in 350.	1 in 400.	1 in 450.	1 in 500.	1 in 550.	1 in 600,		
.00403	3/6	.00025	.00023	.00022	.00020	.00019	.00018	.00017	.00016		
.00914	12	.00058	.00053	.00049	.00046	.00043	.00041	.00039	.00037		
.02855	3/8 1/2 3/4	.00181	.00165		.00143		.00128				
.06334	1 1 **	.00400	.00366		.00317	.00298	.00283	.00270			
.11659	11/4	.00737	.00673	.00623	.00583	.00549	.00521	.00497	.00476		
.19115	11/6	.01209		.01022	,00956	.00901	.00855	.00815	.00780		
.28936	11/4 11/6 13/4	.01830	.01671	.01547	.01447	.01363	.01294	.01234	.01181		
.41357	12	.02615		.02211	.02068	.01948	.01849	.01763	.01688		
.74786	21/2	.04730	.04318		.03739	.03523	.03344				
1.2089	3	.07645	.06980		.06045						
2.5630	4	.16208	.14799	.13699	.12815		.11461	.10929	.10463		
4.5610	5	.28843			.22805		.20397	.19448			
7.3068	6	.46208	.42189	.39055	.36534	.34422	.32676	.31156	.29830		
10.852	7	.68628	. 62660		.54260		.48530		.44303		
15.270	8	.96567	.88158		.76350		.68286	.65111	.62340		
20.652	9	1.3060	1.1924	1.1038	1.0326	.97292	.92356	.88060			
26.952	10	1.7044	1.5562	1.4405	1.3476	1.2697	1 2053	1.1492	1.1003		
34.428	11	2.1772	1.9878		1.7214	1.6219	1.5396	1.4680	1.4055		
42.918	12	2.7141	2.4781	2.2940	2.1459	2.0219	1.9193	1.8300	1.7521		
	<del>-</del>										
Value of 4	s =	.06324	.05774	.05345	.05	.04711	.04472	.04264	.04082		

For	U.S.	gals.	per	sec.,	multiply	the figures in	1 the	table	by	7.4805
**	"	**	14	min.,	"	н	6.6	4.6		448.83
**	44		"	hom.	6:	44	66	"		26929.8
	**	46	"	24 hi .	., "	44	"	"		646315.

For any other slope the flow is proportional to the square root of the slope; thus, flow in slope of 1 in 100 is double that in slope of 1 in 400.

Flow of Water in Pipes from 3g Inch to 12 Inches Diameter for a Uniform Velocity of 100 Ft. per Min.

Diameter	Area	Flow in Cubic	Flow in U. S	Flow in U. S.
• in	in	Feet per	Gallons per	Gallons per
Inches.	Square Feet.	Minute.	Minute.	Hour.
3/6 1/2 3/4	.00077 .00136 .00307 .00545	0.077 0.136 0.307 0.545	.57 1.02 2.30 4.08	34 61 138 245
11.4	.00852	0.852	6.38	383
11.6	.01227	1.227	9.18	551
13.4	.01670	1.670	12.50	750
2	.02182	2.182	16.32	979
21/2 3 4 5 6	.0341 .0491 .0873 .136	3.41 4.91 8.73 13.6 19.6	25.50 36.72 65.28 102.00 146.88	1,530 2,203 3,917 6,120 8,813
7	.267	26.7	199.92	11,995
8	.349	34.9	261.12	15,667
9	.442	44.2	330.48	19,829
10	.545	54.5	408.00	24,480
11	.660	66.0	493.68	29,621
12	.785	78.5	587.52	35,251

Given the diameter of a pipe, to find the quantity in gallons it will deliver, the velocity of flow being 100 ft, per minute. Square the diameter in inches and multiply by 4.08.

If O' = quantity in gallons per minute and d = diameter in inches, then

$$Q' = \frac{d^2 \times .7854 \times 100 \times 7.4805}{144} = 4.08d^2.$$

For any other velocity, V', in feet per minute,  $Q' = 4.08d^2\frac{V'}{100} = .0408d^2V'$ .

Given diameter of pipe in inches and velocity in feet per second, to find discharge in cubic feet and in gallons per minute.

$$Q' = \frac{d^2 \times .7854 \times v \times 60}{144} = 0.32725 d^2 v \text{ cubic feet per minute.}$$
  
= .32725 × 7.4805 or 2.448 $d^2 v$  U. S. gallons per minute.

To find the capacity of a pipe or cylinder in gallons, multiply the square of the diameter in inches by the length in inches and by .0034. Or multiply the square of the diameter in inches by the length in feet and by .0041.

$$Q = \frac{.7854d^2l}{231} = .0034d^2l$$
 (exact)  $.0034 \times 12 = .0408$ .

#### LOSS OF HEAD.

The loss of head due to friction when water, steam, air, or gas of any kind flows through a straight tube is represented by the formula

$$h=f\frac{4l}{d}\,\frac{v^2}{2g}; \qquad \text{whence } v=\sqrt{\frac{64.4}{4f}\,\frac{hd}{l}},$$

in which l= the length and d= the diameter of the tube, both in feet; v= velocity in feet per second, and f is a coefficient to be determined by experiment. According to Weisbach, f=.0064, in which case

$$\sqrt{\frac{64.4}{4f}} = 50$$
, and  $v = 50$ ,  $\sqrt{\frac{hd}{l}}$ ,

which is one of the older formulæ for flow of water (Downing's). Prof. Unwin says that the value of f is possibly too small for tubes of small bore, and he would put f=.006 to .01 for 4-inch tubes, and f=.0084 to .012 for 2-inch tubes. Another formula by Weisbach is

$$h = \left(.0144 + \frac{.01716}{\sqrt{v}}\right) \frac{l}{d} \frac{v^2}{2g}.$$

Rankine gives

$$f = .005 \left(1 + \frac{1}{12d}\right).$$

From the general equation for velocity of flow of water  $v=c\ V\bar{r}\ \sqrt[4]{s}$ , for round pipes  $c\sqrt{\frac{d}{d}}\ \sqrt[4]{\tilde{h}}$ , we have  $v^2=c^2\frac{d}{d}\ \frac{h}{\tilde{l}}$  and  $h=\frac{dv^2}{d}$ , in which

e is the coefficient of D'Arcy's, Bazin's, Kutter's, or other formula, as found by experiment. Since this coefficient varies with the condition of the inner surface of the tune, as well as with the velocity, it is to be expected that values of the loss of head given by different writers will vary as much as those of quantity of flow. Two tables for loss of head per 100 ft. in length in pipes of different diameters with different velocities are given below. The first is given by Clark, based on Ellis' and Howland's experiments; the second is from the Pelton Water-wheel Co.'s catalogue, authority not stated. The loss of head as given in these two tables for any given diameter and velocity differs considerably. Either table should be used with caution and the results compared with the quantity of flow for the given diameter and head as given in the tables of flow based on Kutter's and D'Arcy's formulæ.

#### Relative Loss of Head by Friction for each 100 Feet Length of Clean Cast-iron Pipe.

(Based on Ellis and Howland's experiments.)

Velocity		Diameter of Pipes in Inches.													
in Feet per	3	4	5	6	7	8	9	10	12	14					
Second.		Loss of Head in Feet, per 100 Feet Long.													
Feet	Feet	Feet	Feet	Feet	Feet	Feet	Feet	Feet	Feet	Feet					
1000	Head		Head				Head		Head	Head					
2 2.5	.97 1.49	.55	.41	.32	.27	.23	.19	.18	.15	.12					
3 3.5	1.9	1.2	1.2	1.0	.61	.51 .71	.44	.39	.33	.27					
4.5	3.3	2.2	1.7	1.3	1.2	1.2	1.01	.69	.59	.49					
5 5.5							1.2	1.1	.90	.76					
6															
	15	18	21	24	27	30	33	36	42	48					
2	.11	.095	.075	.065	.055	.052	.049	.047	.036	.030					
2.5	.25	.21	.17	.15	.13	.12	.108	.10	.081	.067					
3.5	.34	.29	.23	.20	.18	.16	.15	.14	.111	.092					
4.5 5	.56	.58	.39	.34	.30	.28	.25	.22	.18	.15					
5.5 6	.84	.70	.59	.50 .59	.44	.39	.36	.32	.27	.22					

Loss of Head in Pipe by Friction.—Loss of head by friction in each 100 feet in length of different diameters of pipe when discharging the following quantities of water per minute (Pelton Water-wheel Co.):

per	Inside Diameter of Pipe in Inches.													
	1		1	2		3		4		5		6		
Velocity in Feet Second.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Cubic Feet per Minute.	Loss of Head in Feet.	Cubic Feet per Minute.		
2.0 3.0 4.0 5.0 6.0 7.0	12.33 17.23	.65 .99 1.32 1.65 1.98 2.31	1.185 2.44 4.10 6.17 8.61 11.45	2.62 3.92 5.23 6.54 7.85 9.16	.791 1.62 2.73 4.11 5.74 7.62	5.89 8.83 11.80 14.70 17.70 20.6	.593 1.22 2.05 3.08 4.31 5.72	10.4 15.7 20.9 26.2 31.4 36.6	.474 .978 1.64 2.46 3.45 4.57	16.3 24.5 32.7 40.9 49.1 57.2	2.87	23.5 35.3 47.1 58.9 70.7 82.4		

		Inside Diameter of Pipe in Inches.													
	7		8		9		1	0	1	1	1	2			
V	h	Q	h	Q	h	Q	h	Q	h	Q	h	Q			
2.0 3.0	.338	32.0 48.1	.296	41.9 62.8	.264	53 79.5	.237	65.4 98.2	.216		.198	94.2			
4.0 5.0	1.175 1.76	64.1 80.2	1.027	83.7	.913 1.37	106 132	.822 1.23	131	.747 1.122	158	.685 1.028	188			
6.0	2.46	96.2 112.0	2.15 2.85	125 146	1.92 2.52	159 185	1.71 2.28	196	1.56	237	1.48	283 330			

Inside	Diameter	of Pipe	in Inches.
--------	----------	---------	------------

	13		13 14		1	.5	1	.6	1	.8	20	
v	h	Q	h	Q	h	Q	h	Q	h	Q	h	Q
2.0	.375	166	.169	192	.158	147 221	.147	167 251	.132	212 318	.119	262 393
4.0 5.0 6.0 7.0	.949 1.325		.587 .881 1.229 1.63	256 321 385 449	.548 .822 1.148 1.52	294 368 442 515	.513 .770 1.076 1.43	335 419 502 586	.456 .685 .957	424 530 636 742	.410 .617 .861	523 654 785 916
1.0	1.10	001	1.00	110	1.00	010	1.10	000	11.00	170	11.140	310

Inside Diameter of Pipe in Inches.

	22		22 24		26		2	8	30		36	
v.	h	Q	h	Q	h	Q	h	Q	h	Q	h .	Q
2.0 3.0 4.0 5.0 6.0 7.0	.873 .561 .782	633 792 950	.098 .204 .342 .513 .717 .953	377 565 754 942 1131 1319	.091 .188 .315 .474 .662 .879	442 663 885 1106 1327 1548	.084 .174 .298 .440 .615 .817	513 770 1026 1283 1539 1796	.079 .163 .273 .411 .574 .762	1178 1472 1767	.066 .135 .228 .342 .479 .636	848 1273 1697 2121 2545 2868

Example.—Given swo it. nead and 600 ft. of 11-inch pipe, carrying 119 cubic feet of water per minute. To find effective head: In right-hand column, under 11-inch pipe, find 119 cubic ft.; opposite this will be found the loss by friction in 100 ft. of length for this amount of water, which is .444. Multiply this by the number of hundred feet of pipe, which is 6, and we have 2.66 ft., which is the loss of head. Therefore the effective head is 200 — 2.66 = 197.34. Example.—Given 200 ft. head and 600 ft. of 11-inch pipe, carrying 119 cubic

EXPLANATION.—The loss of head by friction in pipe depends not only upon diameter and length, but upon the quantity of water passed through it. The head or pressure is what would be indicated by pressure rauge attached to the pipe near the wheel. Readings of gauge shutle to taken while the

water is flowing from the nozzle.

To reduce heads in feet to pressure in pounds multiply by .433. To reduce pounds pressure to feet multiply by 2.300.

Cox's Formula.-Weisbach's formula for loss of head caused by the friction of water in pipes is as follows:

Friction-head = 
$$\left(0.0144 + \frac{0.01716}{\sqrt{V}}\right) \frac{L.V^2}{5.367d}$$

where L = length of pipe in feet; V = velocity of the water in feet per second;

d = diameter of pipe in inches.

William Cox (Amer. Mach., Dec. 28, 1893) gives a simpler formula which gives almost identical results:

dentical results : 
$$H = \text{friction-head in feet} = \frac{L}{d} \frac{4V^2 + 5V - 2}{1200}$$
 . . . . (1)  $\frac{Hd}{L} = \frac{4V^2 + 5V - 2}{1200}$  . . . . . (2)

$$\frac{Hd}{L} = \frac{4V^2 + 5V - 2}{1200}, \dots, \dots, \dots (2)$$

He gives a table by means of which the value of  $\frac{4V^2 + 5V - 2}{1200}$  is at once obtained when V is known, and vice versa.

Values of 
$$\frac{4V^2 + 5V - 2}{1200}$$
.

						1200				
v	0.0	0.1	0.2	0.3	0.4	0.5	0.6	0.7	0.8	0.9
1 2 3 4 5 6 7 8 9	.00583 .02000 .04083 .06833 .10250 .14333 .19083 .24500	.00695 .02178 .04328 .07145 .10628 .14778 .19595 .25078	.00813 .02363 .04580 .07463 .11013 .15230 .20113 .25663 .31880	.00938 .02555 .04838 .07788 .11405 .15688 .20638 .26255 .32548	.01070 .02753 .05103 .08120 .11803 .16153 .21170 .26853 .3328	.02958 .05375 .08458 .12208 .16625 .21708 .27458 .33875	.03170 .05653 .08803 .12620 .17103 .22253 .28070 .34553	.01505 .03388 .05938 .09155 .13038 .17588 .22805 .28688 .35238	.06230 .09513 .13463 .18080 .22363 .29313 .35930	.03845 .06528 .09878 .13895 .18578 .23928 .29945 .36628
10 11 12 13 14 15 16 17 18 19 20 21	1.15333 1.28083 1.41500	.62495 .71978 .82128	1.17830 1.30713 1.44263	.64338 .73955 .84238 .95188 1.06805 1.19088 1.32038 1.45655	.65270 .74953 .85302 .96320 1.08003 1.20353 1.33370 1.47053	.48708 .57125 .66208 .75958 .86375 .97458 1.09208 1.21625 1.34708 1.48458	.58003 .67153 .76970 .87453 .98603 1.10420 1.22903 1.36053 1.49870	1.37405 1.51288	.59780 .69063 .79013 .89630 1.00913 1.12863 1.25480 1.38763 1.52713	.60678 .70028 .80045 .90728 1.02078 1.14095 1.26778 1.40128 1.54145

The use of the formula and table is illustrated as follows: Given a pipe 5 inches diameter and 1000 feet long, with 49 feet head, what

will the discharge be?

If the velocity V is known in feet per second, the discharge is  $0.32725d^2V$ 

cubic foot per minute.

By equation 2 we have

$$\frac{4V^2 + 5V - 2}{1200} = \frac{Hd}{L} = \frac{49 \times 5}{1000} = 0.245;$$

whence, by table, V= real velocity = 8 feet per second. The discharge in cubic feet per minute, if V is velocity in feet per second and d diameter in inches, is  $0.32725d^2V$ , whence, discharge

= 
$$0.32725 \times 25 \times 8 = 65.45$$
 cubic feet per minute.

The velocity due the head, if there were no friction, is  $8.025 \sqrt{H} = 56.175$  feet per second, and the discharge at that velocity would be

$$0.32725 \times 56.175 \times 8 = 460$$
 cubic feet per minute.

Suppose it is required to deliver this amount, 460 cubic feet, at a velocity of 2 feet per second, what diameter of pipe will be required and what will be the loss of head by friction?

the loss of head by friction?
$$d = \text{diameter} = \sqrt{\frac{Q}{V \times 0.32725}} = \sqrt{\frac{460}{2 \times 0.32725}} = \sqrt{708} = 26.5 \text{ inches.}$$

Having now the diameter, the velocity, and the discharge, the friction-head is calculated by equation 1 and use of the table; thus,

$$H = \frac{L}{d} \frac{4V^2 + 5V - 2}{1200} = \frac{1000}{26.5} \times 0.02 = \frac{20}{26.5} = 0.75 \text{ foot,}$$

thus leaving 49 - 0.75 = say 48 feet effective head applicable to power-producing purposes.

Problems of the loss of head may be solved rapidly by means of Cox's Pipe Computer, a mechanical device on the principle of the slide-rule, for sale by Keuffel & Esser, New York.

## Frictional Heads at Given Rates of Discharge in Clean Cast-iron Pipes for Each 1000 Feet of Length.

(Condensed from Ellis and Howland's Hydraulic Tables.)

	(Co	ndense	d fron	1 Ellis	and H	owlan	a's Hy	draul	ic Ta	bles.	)	
<i>v</i>	4-in Pip	eh pe.	6-in Pi <sub>l</sub>	ch e.	8-in Pij	eh pe.	10-iı Piţ	ach e.	12-i Pi	nch pe.	14-i Pi	nch pe.
U. S. Gallons Discharged per Minute.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity, in ft. per sec.	Friction- head, feet.	Velocity, in ft. per sec.	Friction- head, feet.
25 50 100 200 250 300 350 400 500 600 700 800 1000 1400 1400 1500 2500 300 300 400 400	.64 1.28 2.55 3.83 5.11 6.37 7.66 8.94 10.21 12.77 15.32 17.87	,59 2.01 7.36 16.05 28.09 43.47 62.20 84.26 109.68 170.53 244.76 332.36	.28 .57 1.13 1.70 2.27 2.84 3.40 3.40 4.54 5.67 6.81 7.94 9.08 10.21 11.35 13.61 15.88 18.15 20.42 22.69	.11 .32 1.08 2.28 3.92 6.00 8.52 11.48 14.89 23.01 32.89 44.54 57.95 73.12 90.05 175.38 228.60 2288.90 356.22	.16 .32 .64 .96 1.28 1.60 1.91 2.23 2.55 3.19 3.83 4.47 5.09 5.74 6.38 7.66 8.94 10.21 11.47 12.77 15.96	.04 .10 .29 .01 .1.52 2.13 2.85 3.68 5.64 8.03 10.83 14.05 17.68 21.74 42.13 54.84 69.82 85.27 132.70	.10 .20 .41 .61 .82 1.02 1.23 1.43 1.63 2.04 2.45 2.86 3.27 3.68 4.90 5.72 6.53 7.35 8.17	4.73 5.93 7.28	.07 .14 .28 .43 .57 .71 .85 .89 .1.13 1.42 2.27 2.55 2.84 3.97 4.54 5.11 5.67 7.09 8.51	17.82	2.08 2.50 2.91 3.33 3.75 4.17 5.21	
	16-i Pi	nch pe.	18-i Pi	nch pe.	20-i Pi	nch pe.	24-i Pij		30-	inch pe.	6.25 8.34 36- Pi	inch ipe.
U. S. Gallons Discharged per Minute.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.	Velocity in ft. per sec.	Friction- head, feet.
500 1000 1500 2000 2500 3500 3500 4500 5000 5000 6000 7000 9000 12000 14000 16000 18000	.80 1.60 2.39 3.19 3.99 4.79 5.59 6.38 7.18 7.98	.22 .76 1.63 2.82 4.34 6.19 8.37 10.87 13.70 16.85	.63 1.26 1.89 2.52 3.15 3.78 4.41 5.64 5.67 6.30 7.57	.13 .44 .93 1.60 2.45 3.48 4.70 6.09 7.67 9.43 13.49	.51 1.02 1.53 2.04 2.55 3.06 3.57 4.08 4.59 5.11 6.13 7.15	.08 .27 .56 .96 .96 .1.47 .2.09 .2.81 .3.64 .4.58 .5.62 .8.03 .10.86	355 .71 1.06 1.42 1.77 2.13 2.48 2.84 3.19 3.55 4.26 4.96 5.67 6.38	.04 12 .24 .41 .62 .87 1.16 1.50 1.88 2.31 3.28 4.43 5.75 7.25	.23 .45 .68 .91 1.13 1.36 1.59 1.82 2.04 2.27 2.72 3.18 3.163 4.08 4.54 6.36	.01 .04 .09 .15 .22 .30 .40 .52 .64 .78 1.11 1.49 1.93 2.48 2.98 4.25 5.75	.63 .79 .95	.27 .33 .46 .62 .80 1.00 1.23 1.74

Effect of Bends and Curves in Pines.-Weisbach's rule for bends: Loss of head in feet = .131 + 1.847  $\left(\frac{r}{R}\right)^{\frac{7}{2}} \times \frac{v^2}{64.4} \times \frac{a}{180}$ , in which r

= internal radius of pipe in feet, R = radius of curvature of axis of pipe, v = velocity in feet per second, and a = the central angle, or angle subtended

by the bend.

Hamilton Smith, Jr., in his work on Hydraulics, says; The experimental data at hand are entirely insufficient to permit a satisfactory analysis of this quite complicated subject; in fact, about the only experiments of value are those made by Bossut and Dubuat with small pipes.

Curves.—If the pipe has easy curves, say with radius not less than 5 diameters of the pipe, the flow will not be materially diminished, provided the tops of all curves are kept below the hydraulic grade-line and provision

be made for escape of air from the tops of all curves. (Trautwine.)

Hydraulic Grade-line.—In a straight tube of uniform diameter throughout, running full and discharging freely into the air, the hydraulic grade-line is a straight line drawn from the discharge end to a point immediately over the entry end of the pipe and at a depth below the surface equal to the entry and velocity heads. (Trautwine.)

In a pipe leading from a reservoir, no part of its length should be above the hydraulic grade-line.

Flow of Water in House-service Pipes. Mr. E. Kuichling, C.E., furnished the following table to the Thomson

Merer Co.:										
Condition	Main, per nch.	Discl	harge, Cul der the	or Qua pic Fee condi	antity t per I tions s	capable linute, pecifie	e of be from d in th	eing de the Pi e first	livered pe, colum	i, in
of Discharge.	Pressure in Ma pounds per square inch.	No	minal I	Diame		Iron or	r Lead	Servi	ce-pipe	in
	P.	1/2	5/8	3/4	1	11/2	2	3	4	6
Through 35 feet of service- pipe, no back pressure.	30 40 50 60 75 100	1.10 1.27 1.42 1.56 1.74 2.01	1.92 2.22 2.48 2.71 3.03 3.50	3.01 3.48 3.89 4.26 4.77 5.50	6.18 7.08 7.92 8.67 9.70 11.20	16.58 19.14 21.40 23.44 26.21 30.27	43.04 47.15 52.71 60.87	101.80 113.82 124.68 139.39 160.96	224 .44 245 .87 274 .89 317 .41	513.42 574.02 628.81 703.03 811.79
Through 100 feet of service- pipe, no back pressure.	30 40 50 60 75 100 130	0.66 0.77 0.86 0.94 1.05 1.22 1.39	3.99 1.16 1.34 1.50 1.65 1.84 2.13 2.42	1.84 2.12 2.37 2.60 2.91 3.36 3.83	3.78 4.36 4.88 5.34 5.97 6.90 7.86	34.51 10.40 12.01 13.43 14.71 16.45 18.99 21.66	21.30 24.59 27.50 30.12 33.68	58.19 67.19 75.13 82.30 92.01 106.24	118.13 136.41 152.51 167.06 186.78 215.68	925.58 317.23 366.30 409.54 448.63 501.58 579.18 660.36
Through 100 feet of service- pipe and 15 feet vertical rise.	30 40 50 60 75 100 130	0.55 0.66 0.75 0.83 0.94 1.10 1.26	0.96 1.15 1.31 1.45 1.64 1.92 2.20	1.52 1.81 2.06 2.29 2.59 3.02 3.48	3.11 3 72 4.24 4.70 5.32 6.21 7.14	8.57 10.24 11.67 12.94 14.64 17.10 19.66	35.00	65.18 72.28 81.79 95.55	116.01 132.20 146 61 165.90 193.82	260.56 311.09 354.49 393.13 444.85 519.72 597.31
Through 100 feet of service- pipe, and 30 feet vertical rise.	30 40 50 60 75 100 130	0.44 0.55 0.65 0.73 0.84 1.00 1.15	0.77 0.97 1.14 1.28 1.47 1.74 2.02	1,22 1,53 1,79 2,02 2,32 2,75 3,19	2.50 3.15 3.69 4.15 4.77 5.65 6.55	6.80 8.68 10.16 11.45 13 15 15.58 18.07	20.82 23.47 26.95 31.98	56,98 64,22 73,76 87,38	98.98 115.87 130.59 149.99 177.67	211.54 3 266.59 312.08 351.73 9 403.98 478.55 554.96

In this table it is assumed that the pipe is straight and smooth inside: that the friction of the main and meter are disregarded; that the inlet from the main is of ordinary character, sharp, not flaring or rounded, and that the outlet is the full diameter of pipe. The deliveries given will be increased if, first, the pipe between the meter and the main is of larger diameter than the outlet; second, if the main is tapped, say for 1-inch pipe, but is enlarged from the tap to 114 or 114 inch, or, third, if pipe on the outlet is larger than that on the inlet side of the meter. The exact details of the conditions given are rarely met in practice; consequently the quantities of the table may be expected to be decreased, because the pipe is liable to be throttled at the joints, additional bends may interpose, or stop-cocks may be used, or the

joints, additional bends may litterpose, or stop-cocks may be used, or the back-pressure may be increased.

Air-bound Pipes.—A pipe is said to be air-bound when, in consequence of air being entrapped at the hign points of vertical curves in the line, water will not flow out of the pipe, although the supply is higher than the outlet. The remedy is to provide cocks or valves at the high points, through which the air may be discharged. The valve may be made auto-

matic by means of a float.

Vertical Jets. (Molesworth.)—H = head of water, h = height of jet, d = diameter of jet, K = coefficient, varying with ratio of diameter of jet to head; then <math>h = KH.

If  $H = d \times 300$ 600 1000 1500 1800 2800 3500 4500. .9 .85 .7 .6 .5 .25 .8

Water Delivered through Meters. (Thomson Meter Co.). - The best modern practice limits the velocity in water-pipes to 10 lineal feet per second. Assume this as a basis of delivery, and we find, for the several sizes of pipes usually metered, the following approximate results:

Nominal diameter of pipe in inches:

3/9 5% 1 11/6 Quantity delivered, in cubic feet per minute, due to said velocity:

1.28 1.85 3.28 7.36 13.1 29.5

Prices Charged for Water in Different Cities (National Meter Co.):

Extremes, 21/2 cents to .....

## FIRE-STREAMS.

## Discharge from Nozzles at Different Pressures.

(J. T. Fanning, Am. Water-works Ass'n, 1892, Eng'g News, July 14, 1892,)

Nozzle diam., in.	Height of stream, ft.	Pressure at Play- pipe, lbs.	Horizon- tal Pro- jection of Streams, ft.	Gallons per minute.	Gallons per 24 hours.	Friction per 100 ft. Hose, lbs.	Friction per 100 ft. Hose, Net Head, ft.
1	70	46.5	59.5	203	292,298	10.75	24.77
1	80	59.0	67.0	230	331,200	13.00	31.10
1	90	79.0	76.6	267	384,500	17.70	40.78
1	100	130.0	88.0	311	447,900	22.50	54.14
11/6	70	44.5	61.3	249	358,520	15.50	35.71
11/8 11/8	80	55.5	69.5	281	404,700	19.40	44.70
11%	90	72.0	78.5	324	466,600	25.40	58.52
11/8	100	103.0	89.0	376	541,500	33.80	77.88
11/4	70	43.0	66.0	306	440,613	22.75	52.42
11/4	80	53.5	72.4	343	493,900	28.40	65.43
11/4	90	68.5	81.0	388	558,800	35.90	82.71
11/4	100	93.0	92.0	460	662,500	57.75	86.98
13/8	70	41.5	77.0	368	530,149	32,50	74.88
13/8	80	51.5	74.4	410	590,500	40.00	92.16
1%	90	65.5	82.6	468	674,000	51.40	118.43
13/8	100	88.0	92.0	540	777,700	72.00	165.89

Friction Losses in Hose .- In the above table the volumes of water discharged per jet were for stated pressures at the play-pipe.

In providing for this pressure due allowance is to be made for friction

losses in each hose, according to the streams of greatest discharge which are

The loss of pressure or its equivalent loss of head (h) in the hose may be

found by the formula  $h = v^2(4m)\frac{\epsilon}{2ad}$ .

In this formula, as ordinarily used, for friction per 100 ft. of 2½-in. hose there are the following constants: 2% in. diameter of hose d=2093 ft. elength of hose l=100 ft., and 2g=64.4. The variables are: v= velocity in feet per second;  $h \equiv loss$  of head in feet per 100 ft. of hose; m= a coefficient found by experiment; the velocity v is found from the given discontinuous  $h \equiv loss$  for  $h \equiv$ charges of the jets through the given diameter of hose.

Head and Pressure Losses by Friction in 100-ft. Lengths of Rubber-lined Smooth 21/4-in. Hose.

Discharge per minute, gallons.	Velocity per second, ft.	Coefficient, $m$ .	Head Lost,	Pressure Lost, lbs. per sq. in.	Gallons per 24 hours.
200	13,072	.00450	22.89	9.93	288,000
250	16.388	.00446	35.55	15.43	360,000
300	18.858	.00442	46.80	20.31	432,000
347	21.677	.00439	61.53	26.70	499,680
350	22.873	.00439	68.48	29.73	504,000
400	26.144	.00436	88.83	38.55	576,000
450	29.408	.00434	111.80	48.52	648,000
500	32.675	.00432	137.50	59.67	720,000
520	33.982	.00431	148.40	64.40	748,800

These frictions are for given volumes of flow in the hose and the velocities respectively due to those volumes, and are independent of size of The changes in nozzle do not affect the friction in the hose if there is no change in velocity of flow, but a larger nozzle with equal pressure at the nozzle augments the discharge and velocity of flow, and thus materially

increases the friction loss in the hose.

Loss of Pressure (p) and Head (h) in Rubber-lined Smooth  $2\frac{1}{2}$ -in. Hose may be found approximately by the formulæ

 $\frac{lq^2}{4150d^5}$  and  $h = \frac{lq^2}{1801d^5}$ , in which p = pressure lost by friction, in

pounds per square inch: l = length of hose in feet; q = gallons of water discharged per minute: d = diam, of the hose in inches,  $2\frac{1}{2}$  in.; h = friction-head in feet. The coefficient of  $d^2$  would be decreased for rougher hose. The loss of pressure and head for a  $1\frac{1}{2}$ -in. stream with power to reach a height of 80 ft. is, in each 100 ft. of  $2\frac{1}{2}$ -in. hose, approximately 20 lbs., or 45 ft. net, or, say, including friction in the hydrant,  $\frac{1}{2}$  ft. loss of head for each foot of hose.

If we change the nozzles to 11/4 or 13/6 in. diameter, then for the same 80 ft. height of stream we increase the friction losses on the hose to approximately % ft. and 1 ft. head, respectively, for each foot-length of hose.

These computations show the great difficulty of maintaining a high

stream through large nozzles unless the hose is very short, especially for a

gravity or direct-pressure system.

This single 1½-in, stream requires approximately 56 lbs pressure, equiva-lent to 129 ft. head, at the play-pipe, and 45 to 50 ft. head for each 100 ft. length of smooth 2½-in, hose, so that for 100, 200, and 300 ft. of hose we must have available heads at the hydrant or fire-engine of 166, 156, and 266 ft. respectively. If we substitute 1½-in, nozzles for same height of stream we must have available heads at the hydrants or engine of 185, 255 and 325 ft., respectively, or we must increase the diameter of a portion at least of the long hose and save friction-loss of head.

Rated Capacities of Steam Fire-engines, which is perhaps one third greater than their ordinary rate of work at fires, are substantially

as follows:

3d size,	550 gals	s. per min	or 792,000,	gals, per	24 hours.
2d "	700 "	* "	1,008,000	- "	**
1st "	900 "	44	1,296,000		66 .
1 ext.,	1,100 "	44	1,584,000	44	46

Pressures required at Nozzle and at Pump, with Quantity and Pressure of Water Necessary to throw Water Various Distances through Different-sized Nozzles using 2½-inch Rubber Hose and Smooth Nozzles,

(From Experiments of Ellis & Leshure, Fanning's "Water Supply.")

Size of Nozzles.		1 II	nch.		1½ Inch.			
Pressure at nozzle, lbs. per sq. in  * Pressure at pump or hydrant with 100 ft. 2½ inch rubber hose. Gallons per minute. Horizontal distance thrown, feet. Vertical distance thrown, feet.	48 155 109	142	219	121 245 186	196 113		175	310 193
Size of Nozzles		114	Inah			13/ 1	Inah	

Size of Nozzles,		1¼ I	nch.		13% Inch.			
Pressure at nozzle, lbs. per sq. in	61 242 118	297 156	123 842 186	383 207	293 124	358 166	144 413 200	224
Vertical distance thrown, feet	82							

<sup>\*</sup>For greater length of 2½-inch hose the increased friction can be obtained by noting the differences between the above given "pressure at nozzle" and "pressure at pump or hydrant with 100 feet of shose." For instance, if it requires at hydrant or pump eight pounds more pressure than it does at nozzle to overcome the friction when pumping through 100 feet of 2½-inch hose (using 1-inch nozzle, with 40-pound pressure at said nozzle) then it requires 16-pounds pressure to overcome the friction in forcing through 200 feet of same size hose.

Decrease of Flow due to Increase of Length of Hose. (J. R. Freeman's Experiments, Trans. A. S. C. E. 1889.)—If the static pressure is 80 lbs. and the hydrant ripes of such size that the pressure at the hydrant is 70 lbs., the hose 2½ in. nominal diam., and the nozzle 1½ in. diam., the height of effective fire-stream obtainable and the quantity in gallons per minute will be:

							Linen	Hose.		Hose.
							Height,	Gals.	Height,	Gals.
							feet.	per min.	feet.	per min.
With	50	ft.	of	21/2-in.	hose	9	. 73	261	81	282
64	250	66	6.6		6.		. 42	184	61	229
**	500		66	**	66		. 27	146	46	192

With 500 ft. of smoothest and best rubber-lined hose, if diameter be exactly 2½ in., effective height of stream will be 39 ft. (177 gals.); if diameter be ½ in. larger, effective height of stream will be 46 ft. (192 gals.)

## THE SIPHON.

The Siphon is a bent tube of unequal branches, open at both ends, and is used to convey a liquid from a higher to a lower level, over an intermediate point higher than either. Its parallel branches being in a vertical plane and plunged into two bodies of liquid whose upper surfaces are at different levels, the fluid will stand at the same level both within and without each branch of the tube when a vent or small opening is made at the bend. If the air be withdrawn from the siphon through this vent, the water will rise in the branches by the atmospheric pressure without, and when the two columns unite and the vent is closed, the liquid will flow from the upper reservoir as long as the end of the shorter branch of the siphon is below the surface of the liquid in the reservoir.

If the water was free from air the height of the bend above the supply

level might be as great as 33 feet.

If A = area of cross-section of the tube in square feet. H = the difference in level between the two reservoirs in feet. D the density of the liquid in pounds per cubic foot, then ADH measures the intensity of the force which causes the movement of the fluid, and  $V=\sqrt{2gH}=8.02$   $\sqrt{H}$  is the theoretical velocity, in feet per second, which is reduced by the loss of head for entry and friction, as in other cases of flow of liquids through pipes. In the case of the difference of level being greater than 33 feet, however, the velocity of the water in the shorter leg is limited to that due to a height of 33 feet, or that due to the difference between the atmospheric pressure at the entrance and the vacuum at the bend.

Leicester Allen (Am. Mach., Nov. 2, 1893) says: The supply of liquid to a siphon must be greater than the flow which would take place from the discharge end of the pipe, provided the pipe were filled with the liquid, the supply end stopped, and the discharge end opened when the discharge end

is left free, unregulated, and unsubmerged.

To illustrate this principle, let us suppose the extreme case of a siphon having a calibre of 1 foot, in which the difference of level, or between the point of supply and discharge, is 4 inches. Let us further suppose this siphon to be at the sea-level, and its highest point above the level of the supply to be 27 feet. Also suppose the discharge end of this siphon to be unregulated, unsubmerged. It would be inoperative because the water in the longer leg would not be held solid by the pressure of the atmosphere against it, and it would therefore break up and run out faster than it could be replaced at the inflow end under an effective head of only 4 inches.

Long Stphons.—Prof. Joseph Torrey, in the Amer. Machinist,

describes a long siphon which was a partial failure.

The length of the pipe was 1792 feet. The pipe was 3 inches diameter, and rose at one point 9 feet above the initial level. The final level was 30 feet below the initial level. No automatic air valve was provided. The highest point in the siphon was about one third the total distance from the pond and point in the siphon was about one third the total distance from the pond and nearest the pond. At this point a pump was placed, whose mission was to fill the pipe when necessary. This siphon would flow for about two hours and then cease, owing to accumulation of air in the pipe. When in full operation it discharged 43½ gallons per minute. The theoretical discharge from such a sized pipe with the specified head is 55½ gallons per minute.

Siphon on the Water-supply of Mount Vernon, N. Y. (Englo News, May 4, 1893.)—A 12-inch siphon, 925 feet long, with a maximum lift of 22,12 feet and a 45° change in alignment, was put in use in 1893 by the New York City Suburban Water Co., which supplies Mount Vernon, N. Y. At its summit the siphon crosses a supply main, which is tapped to charge

At its summit the siphon crosses a supply main, which is tapped to charge

the siphon. The air-chamber at the siphon is 12 inches by 16 feet long. A 1/2-inch tap and cock at the top of the chamber provide an outlet for the collected air.

It was found that the siphon with air-chamber as desc.ibed would run It was found that the spinon with air-chamber as desc. bed would run until 125 cubic feet of air had gathered, and that this took place only half as soon with a 14-foot lift as with the full lift of 22.12 feet. The siphon will operate about 12 hours without being recharged, but more water can be gotten over by charging every six hours. It can be kept running 23 hours out of 24 with only one man in attendance. With the siphon as described above it is necessary to close the valves at each end of the siphon to veolouse it. recharge it.

It has been found by weir measurements that the discharge of the siphon before air accumulates at the summit is practically the same as through a

straight pipe.

## MEASUREMENT OF FLOWING WATER.

Piezometer.—If a vertical or oblique tube be inserted into a pipe containing water under pressure, the water will rise in the former, and the vertical height to which it rises will be the head producing the pressure at the then neight to when it rises will be the head producing the pressure at the point where the tube is attached. Such a tube is called a plezometer or pressure measure. If the water in the piezometer falls below its proper level it shows that the pressure in the main pipe has been reduced by an obstruction between the piezometer and the reservoir. If the water rises above its proper level, it indicates that the pressure there has been increased by an obstruction beyond the piezometer.

If we imagine a pipe full of water to be provided with a number of piezometer.

zometers, then a line joining the tops of the columns of water in them is

the hydraulic grade-line.

Pitot Tube Gauge.—The Pitot tube is used for measuring the velocity of fluids in motion. It has been used with great success in measuring the flow of natural gas. (S. W. Robinson, Report Ohio Geol. Survey, 1890.) (See also Van Nostrand's Mag., vol. xxxv.) It is simply a tube so bent that a short leg extends into the current of fluid flowing from a tube, with the plane of the entering orifice opposed at right angles to the direction of the current. The pressure caused by the impact of the current is transmitted through the tube to a pressure gauge of any kind, such as a column of water or of mercury, or a Bourdon spring-gauge. From the pressure thus indicated and the known density and temperature of the flowing gas is obtained the head corresponding to the pressure, and from this the velocity. In a modification of the Pitot tube described by Prof. Robinson, there are two tubes inserted into the pipe conveying the gas, one of which has the plane of the orifice at right angles to the current, to receive the static pressure plus the pressure due to impact; the other has the plane of its orifice parallel to the current, so as to receive the static pressure only. These tubes are connected to the legs of a U tube partly filled with mercury, which then registers the difference in pressure in the two tubes, from which the velocity may be calculated. Comparative tests of Pitot tubes with gasmeets, for measurement of the flow of natural gas, have shown an agreement within 3%.

The Venturi Meter, invented by Clemens Herschel, and described in a pamphlet issued by the Builders' Iron Foundry of Providence, R. I., is named from Venturi, who first called attention, in 1796, to the relation between the velocities and pressures of fluids when flowing through converging

and diverging tubes.

It consists of two parts—the tube, through which the water flows, and the recorder, which registers the quantity of water that passes through the

tube.

The tube takes the shape of two truncated cones joined in their smallest diameters by a short throat-piece. At the up-stream end and at the throat

there are air-chambers, at which points the pressuees are taken.

The action of the tube is based on that property which causes the small section of a gently expanding frustum of a cone to receive, without material resultant loss of head, as much water at the smallest diameter as is discharged at the large end, and on that further property which causes the pressure of the water flowing through the throat to be less, by virtue of its greater velocity, than the pressure at the up-stream end of the tube, each pressure being at the same time a function of the velocity at that point and of the hydrostatic pressure which would obtain were the water motionless within the pipe.

The recorder is connected with the tube by pressure-pipes which lead to it from the chambers surrounding the up-stream end and the throat of the tube. It may be placed in any convenient position within 1000 feet of the

tube. It is operated by a weight and clockwork,

The difference of pressure or head at the entrance and at the throat of the meter is balanced in the recorder by the difference of level in two columns of mercury in cylindrical receivers, one within the other. The inner carries a float, the position of which is indicative of the quantity of water flowing through the tube. By its rise and fall the float varies the time of contact between an integrating drum and the counters by which the successive readings are registered.

There is no limit to the sizes of the meters nor the quantity of water that may be measured. Meters with 24-inch, 36-inch, 48-inch, and even 20-foot

tubes can be readily made

Measurement by Venturi Tubes. (Trans. A. S. C. E., Nov., 187, and Jan, 1885.)—Jir. Herschel recommends the use of a Venturi tube in serted in the force-main of the pumping engine; for determining the quantity of water discharged. Such a tube applied to a 24-inch main has a total length of about 20 feet. At a distance of 4 feet from the end nearest the engine the inside diameter of the tube is contracted to a throat having a diameter of about 8 inches. A pressure-gauge is attached to each of two chambers, the one surrounding and communicating with the entrance or main pipe, the other with the throat. According to experiments made upon two tubes of this kind. one-4 in, indiameter at the throat and 12 in, at the entrance, and the other about 30 in, in diameter at the throat and 9 feet at its entrance, the quantity of water which passes through the tube is very nearly the theoretical discharge through an opening having an area equal to that of the throat, and a velocity which is that due to the difference in head shown

by the two gauges. Mr. Herschel states that the coefficient for these two widely-varying sizes of tubes and for a wide range of velocity through the pipe, was found to be within two per cent, either way, of 98s. In other words, the quantity of water flowing through the tube per second is expressed within two per cent by the formula  $W = 0.98 \times A \times \sqrt{2gh}$ , in which A is the area of the throat of the tube, h the head, in feet, corresponding to the difference in the pressure of the water entering the tube and that

ing to the difference in and g=32.16.

Measurement of Discharge of Pumping-engines by Means of Nozzles. (Trans. A. S. M. E., xill, 557).—The measurement of water by computation from its discharge through orifices, or through the nozzles of fire-hose, furnishes a means of determining the quantity of water nozzles of fire-hose, furnishes a means of determining the quantity of water delivered by a pumping-engine which can be applied without much difficulty. John R. Freeman, Trans. A. S. C. E., Nov., 1889, describes a series of experiments covering a wide range of pressures and sizes, and the results showed that the coefficient of discharge for a smooth nozzle of ordinary good form was within one half of one per cent, either way, of 0.977; the diameter of the nozzle being accurately calipered, and the pressures being determined by means of an accurate gauge attached to a suitable piezometer at the base of the play-pipe.

In order to use this method for determining the quantity of water discharged by a pumping-engine, it would be necessary to provide a pressure-box, to which the water would be conducted, and attach to the box as many nozzles as would be required to carry off the water. According to Mr. Freeman's estimate, four 1½-inch nozzles, thus connected, with a pressure of 80 lbs. per square inch, would discharge the full capacity of a two-and aof 80 lbs. per square inch, would discharge the toll capacity of a two-and a half-million engine. He also suggests the use of a portable apparatus with a single opening for discharge, consisting essentially of a Siamese nozzle, so-called, the water being carried to it by three or more lines of fire-hose. To insure reliability for these measurements, it is necessary that the shuttend value in the force-main, or the several shut-off valves, should be tight, so that all the water discharged by the engine may pass through the nozzles.

## Flow through Rectangular Orifices. (Approximate, Seep. 556.)

CUBIC FEET OF WATER DISCHARGED PER MINUTE THROUGH AN ORIFICE ONE INCH SQUARE, UNDER ANY HEAD OF WATER FROM 3 TO 72 INCHES.

For any other orifice multiply by its area in square inches. Formula,  $Q' = .624 \sqrt{h''} \times a$ . Q' = cu. ft. per min.;  $\alpha = \text{area in sq. in.}$ 

Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads   in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heg in i	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.	Heads in inches.	Cubic Feet Discharged per min.
3	1.12	13 14	2,20 2,28	23 24	2.90 2.97	33 34	3.47	43 44	3 95 4.00	53 54	4.39	63 64	4.78 4.81
5	1.40	15	2.36	25	3.03	35	3.57	45	4 05	55	4.48	65	4.85
6	1.52	16	2.43	26	3.08	36	3.62	46	4.09	56	4.52	66	4.85 4.89
7 8 9	1.64	17	2.51	27	3.14	37	3.67	47	4.12	57	4 55	67	4.92
8	1.75	18	2.58	28	3.20	38	8.72	48	4.18	58	4.58	68	4.97
9	1.84	19	2.64	29	3 25	39	3.77	49	4.21	59	4.63	69	5.00
10	1.94	20	2.71	30	3.31	40	3.81	50	4.27.	60	4.65	70	5.03
11	2.03	21	2.78	31	3.36	41	3.86	51	4.30	61	4.72	71	5.07
12	2.12	22	2.84	32	3.41	42	3.91	52	4.34	62	4.74	72	5.09

Measurement of an Open Stream by Velocity and Cross-section.—Measure the depth of the water at from 6 to 12 points across the stream at equal distances between. Add all the depths in feet together and divide by the number of measurements made; this will be the average depth of the stream, which multiplied by its width will give its area or cross-section. Multiply this by the velocity of the stream in feet per minute, and the result will be the discharge in cubic feet per minute of the stream.

The velocity of the stream can be found by laying off 100 feet of the bank and throwing a float into the middle, noting the time taken in passing over the 100 ft. Do this a number of times and take the average; then, dividing this distance by the time gives the velocity at the surface. As the top of the stream flows faster than the bottom or sides—the average velocity being about 8% of the surface velocity at the middle—it is convenient to measure a distance of 120 feet for the float and reckon it as 100.

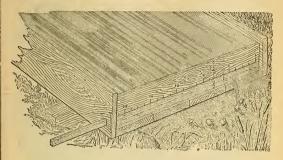


Fig. 130.

## Miners' Inch Measurements. (Pelton Water Wheel Co.)

The cut, Fig. 130, shows the form of measuring-box ordinarily used, and the following table gives the discharge in cubic feet per minute of a miner's inch of water, as measured under the various heads and different lengths and heights of apertures used in California,

Length	Openin	gs 2 Inche	s High.	Openi	ngs 4 Inche	s High.						
of Opening in inches.	Head to Centre, 5 inches.	Head to Centre, 6 inches.	Head to Centre, 7 inches.	Head to Centre, 5 inches.	Head to Centre, 6 inches.	Head to Centre, 7 inches.						
4 6 8 10 12 14 16	Cu. ft. 1.348 1.355 1.359 1.361 1.363 1.364 1.365	Cu. ft. 1.473 1.480 1.484 1.485 1.487 1.488	Cu. ft. 1.589 1.596 1.600 1.602 1.604 1.604 1.605	Cu. ft. 1.320 1.336 1.344 1.349 1.352 1.354 1.356	Cu, ft. 1.450 1.470 1.481 1.487 1.491 1.494 1.496	Cu. ft. 1.570 1.595 1.608 1.615 1.620 1.623 1.626						
18 20 22 24	1.365 1.365 1.366 1.366	1:489 1.490 1.490 1.490	1.606 1.606 1.607 1.607	1.357 1.359 1.359 1.360	1.498 1.499 1.500 1.501	1.628 1.630 1.631 1.632						
26 28 30 40	1.366 1.367 1.367 1.367	1.490 1.491 1.491 1.492	1.607 1.607 1.608 1.608	1.361 1.361 1.362 1.363	1.502 1.508 1.508 1.505	1.633 1.634 1.635 1.637						
50 60 70 80	1.368 1.368 1.368 1.368	1.498 1.493 1.493 1.493	1.609 1.609 1.609 1.609	1.364 1.365 1.365 1.366	1.507 1.508 1.508 1.508 1.509	1.639 1.640 1.641 1.641						
90 100	1.369 1.369	1.493 1.494	1.610 1.610	1.366 1.366	1.509 1.509	1.641 1.642						

Note.-The apertures from which the above measurements were obtained

were through material 11/4 inches thick, and the lower edge 2 inches above

were through material 12 ments there are twee edge s menes above the bottom of the measuring-box, thus giving full contraction. Flow of Water Over Weirs, Weir Dam Measurement. (Felton Water Wheel Co.)—Place a board or plank in the stream, as shown

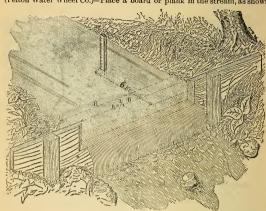


Fig. 131.

in the sketch, at some point where a pond will form above. The length of the notch in the dam should be from two to four times its depth for small quantities, The edges and longer for large quantities. The edges of the potch should be bevelled toward the intake side, as shown. The overfall below the notch should not be less than twice its depth, that is, 12 inches if the notch is 6 inches deep, and so on,

In the pond, about 6 ft. above the dam, drive a stake, and then obstruct the water until it rises precisely to the bottom of the notch and mark the stake at this level. Then complete the dam so as to cause all the water to flow through the notch, and, after time for the water to settle, mark the stake again for this new level. If preferred the stake can be driven with its top precisely level with the bottom of the notch and the depth of the water be measured with a rule after the water is flowing free, but the marks are preferable in most cases. The stake can then be withdrawn; and the distance between the marks is the theoretical depth of flow corresponding to the quantities in the table.

Francis's For	mulæ for weirs.	
	As given by Francis.	As modified by Smith.
Weirs with both end contractions suppressed	$Q = 3.33lh^{\frac{3}{2}}$	$3.29\left(l+\frac{h}{7}\right)h^{\frac{3}{2}}$
Weirs with one end contraction suppressed	$Q = 3.33(l1h)h^{\frac{3}{2}}$	$3.29lh^{\frac{3}{2}}$
Weirs with full contraction	$O = 3.33(l2h)h^{\frac{3}{2}}$	$3.29 \left( l - \frac{h}{10} \right) h^{\frac{3}{2}}$

The greatest variation of the Francis formulæ from the values of c given by Smith amounts to 34%. The modified Francis formule, says Smith, will give results sufficiently exact, when great accuracy is not required, within the limits of h, from .5 ft. to 2 ft., t being not less than 3 h.

Q = discharge in cubic feet per second, l = length of weir in feet, h = effectivetive head in feet, measured from the level of the crest to the level of still

water above the weir.

If Q' = discharge in cubic feet per minute, and l' and h' are taken in inches, the first of the above formulæ reduces to  $Q' = 0.4 l' h'^{\frac{3}{2}}$ . From this formula the following table is calculated. The values are sufficiently accurate for ordinary computations of water-power for weirs without end contrate for ordinary computations of water-power for weirs without end contraction, that is, for a weir the full width of the channel of approach, and are approximate also for weirs with end contraction when l = at least 10h, but about 6% in excess of the truth when l=4h.

## Weir Table.

GIVING CUBIC FEET OF WATER PER MINUTE THAT WILL FLOW OVER A WEIR ONE INCH WIDE AND FROM 1/4 TO 20% INCHES DEEP.

For other widths multiply by the width in inches.

		1/8 in.	1/4 in.	3% in.	½ in.	5/8 in.	3/4 in.	% in.
in.	cu. ft.	cu. ft.	eu. ft.	cu. ft.				
0	.00	.01	.05	.09	.14	.19	.26	.32
1	.40	.47	.55	.64	.73	.82	.92	1.02
2	1.13	1.23	1.35	1.46	1.58	1.70	1.82	1.95
3	2.07	2.21	2.34	2.48	2.61	2.76	2.90	3.05
4	3.20	3.35	3.50	3.66	3.81	3.97	4.14	4.30
1 2 3 4 5 6 7 8	4.47	4.64	4.81	4.98	5.15	5.33	5.51	5.69
6	5.87	6.06	6.25	6.44	6.62	6.82	7.01	7.21
7	7.40	7.60	7.80	8.01	8.21	8.42	8.63	8.83
8 -	9.05	9.26	9.47	9.69	9.91	10.13	10.35	10.57
9	10.80	11.02	11.25	11.48	11.71	11.94	12.17	12.41
10	12.64	12.88	13.12	13.36	13.60	13.85	14.09	14.34
11	14.59	14.84	15.09	15 34	15.59	15.85	16.11	16.36
12	16.62	16.88	17.15	17.41	17.67	17.94	18.21	18.47
13	18.74	19.01	19.29	19.56	19.84	20.11	20.39	20.67
14	20.95	21.23	21.51	21.80	22.08	22.37	22.65	22.94
15	23.23	23.52	23.82	24.11	24.40	24.70	25.00	25.30
16	25.60	25.90	26.20	26.50	26.80	27.11	27.42	27.72
17	28.03	28.34	28.65	28.97	29.28	29.59	29.91	30.22
18	30.54	30.86	31.18	31.50	31.82	32.15	32.47	32.80
19	33.12	33.45	33.78	34 11	34.44	34.77	35.10	35.44
20	35.77	36.11	36.45	36.78	37.12	37.46	37.80	38.15

For more accurate computations, the coefficients of flow of Hamilton Smith, Jr., or of Bazin should be used. In Smith's hydraulics will be found a collection of results of experiments on orifices and weirs of various shapes made by many different authorities, together with a discussion of their

made by many different authorities, together with a discussion of their several formulæ. (See also Trautwine's Pocket Book.) **Bazin's Experiments.**—M. Bazin (Annales des Ponts et Chaussées, Oct., 1888, translated by Marichal and Trautwine, Proc. Engrs. Club of Phila., Jan., 1890), made an extensive series of experiments with a sharp-crested weir without lateral contraction, the air being admitted freely behind the falling sheet, and found values of m varying from 0.42 to 0.50, with variations of the length of the weir from 19% to 784 in., of the height of the crest above the bottom of the channel from 0.79 to 2.46 ft., and of the head from 1.37 to 23.62 in. From these experiments he deduces the following formula:

$$Q = \left[0.425 + 0.21 \left(\frac{H}{P+H}\right)^2\right] LH \sqrt{2gH},$$

in which P is the height in feet of the crest of the weir above the bottom of the channel of approach, L the length of the weir, H the head, both in feet, and Q the discharge in cu. ft. per sec. This formula, says M. Bazin, is entirely practical where errors of 2% to 3% are admissible. The following table is condensed from M. Bazin's paper:

Values of the Coefficient m in the Formula  $G = mLH \sqrt{2aH}$ , for a SHARP-CRESTED WEIR WITHOUT LATERAL CONTRACTION; THE AIR BEING ADMITTED FREELY BEHIND THE FALLING SHEET.

Head,	Heigl	Height of Crest of Weir Above Bed of Channel.										
H.	Feet0.66 Inches 7.87	0.98 11.81		1.64 19.69		2.62 31.50	3.28 39.38	4.92 59.07		89		
Ft. In164 1.97 .230 2.76 .295 3.54 .394 4.72 .525 6.30 .656 7.87 .787 9.45	0.455 0.457 0.462 0.471 0.480 0.488	0.448 0.447 0.448 0.453 0.459 0.465	$\begin{array}{c} 0.445 \\ 0.442 \\ 0.442 \\ 0.444 \\ 0.447 \\ 0.452 \end{array}$	0.448 0.438 0.438 0.440 0.444	$\begin{array}{c} 0.442 \\ 0.438 \\ 0.436 \\ 0.435 \\ 0.436 \\ 0.438 \end{array}$	0.441 0.436 0.433 0.431 0.431 0.432	0.440 0.436 0.482 0.429 0.428 0.428	0.440 $0.435$ $0.430$ $0.427$ $0.425$ $0.424$	0.439 $0.434$ $0.430$ $0.426$ $0.423$ $0.422$	m $0.4481$ $0.4391$ $0.4340$ $0.4291$ $0.4246$ $0.4215$ $0.4194$		
.919   11.02 1.050   12.60 1.181   14.17 1.812   15.75 1.444   17.82 1.575   18.90 1.706   20.47 1.837   22.05 1.969   23.62		0.478 0.483 0.489 0.494	0.462 0.467 0.472 0.476 0.480 0.483 0.487	$\begin{array}{c} 0.452 \\ 0.456 \\ 0.459 \\ 0.463 \\ 0.467 \\ 0.470 \\ 0.473 \end{array}$	0.444 0.448 0.451 0.454 0.457 0.460 0.463	0.436 0.438 0.440 0.442 0.444 0.446 0.448	0.430 0.432 0.433 0.435 0.436 0.438 0.439	0.424 0.424 0.425 0.425 0.426 0.426	0.421 0.421 0.421 0.421 0.421 0.421 0.421	0.4112		

A comparison of the results of this formula with those of experiments. A comparison of the results of this formula with those of experiments, says M. Bazin, justifies us in believing that, except in the unusual case of a very low weir (which should always be avoided), the preceding table will give the coefficient m in all cases within 1%; provided, however, that the arrangements of the standard weir are exactly reproduced. It is especially important that the admission of the air behind the falling sheet be perfectly assured. If this condition is not compiled with, m may vary within much wider limits. The type adopted gives the least possible variation in the coefficient.

## WATER POWER.

a Power of a Fall of Water-Efficiency.—The gross power of a fine into the total head, i.e., the difference of vertical elevation of the upper surface of the water at the points where the fall in question begins and ends. The term "head" used in connection with water-wheels is the difference in height from the surface of the water in the wheel-pit to the surface in the pen-stock when the wheel is running.

If Q = cubic feet of water discharged per second, D = weight of a cubic foot of water = 62.36 lbs. at 60° F., H = total head in feet; then

DQH =gross power in foot-pounds per second, and DQH + 550 = .1134QH =gross horse-power. If Q' is taken in cubic feet per minute, H. P. =  $Q'H \times 62.36$ 

A water-wheel or motor of any kind cannot utilize the whole of the head H, since there are losses of head at both the entrance to and the exit from the wheel. There are also losses of energy due to friction of the water in The wheel. There are also losses of energy due to friction the water its passage through the wheel. The ratio of the power developed by the wheel to the gross power of the fall is the efficiency of the wheel. For 75% efficiency, net horse-power = .00142Q'H =  $\frac{Q'H}{706}$ .

A head of water can be made use of in one or other of the following ways viz. :

1st. By its weight, as in the water-balance and overshot-wheel.

2d. By its pressure, as in turbines and in the hydraulic engine, hydraulic

2d. By its pressure, as in turbines and in the hydraunic engine, hydraunic press, crane, etc. as the undershot-wheel, and in the Pelton wheel. 4th. By a combination of the above. Stream.—The gross horse-power is, H. P. =  $QH \times 62.36 \div 500 = .1134QH$ , in which Q is the discharge in cubic feet per second actually impinging on the float or bucket, and H = theoretical head due to the velocity of the stream =  $\frac{v_0}{2} = \frac{v_0}{64.4}$ , in which v is the velocity in feet per second. If Q' be taken in cubic feet per minute, H P. = .00189QH. Thus, if the floats of an undershot-wheel driven by a current alone be feet  $\times$  1 foot, and the velocity of stream = 210 ft, per minute, or  $3\frac{v}{2}$  ft, per sec., of which the theoretical head is .19 ft., Q = 5 sq. ft.  $\times$  210 = 1050 cu. ft. per minute; H = .19 ft.; H P. = .1650  $\times$  .19  $\times$  .00189 = .377 H. P. The wheels would realize only about 4 of this power, on account of friction and slip, or .151 H. P., or about .03 H. P. per square foot of float, which is equivalent to 33 sq. ft. of float per H. P.

Current Motors, -A current motor could only utilize the whole power of a running stream if it could take all the velocity out of the water, so that of a running stream it is could take an in evolutive out of the water, so that it would leave the floats or buckets with no velocity at all; or in other words, it would require the backing up of the whole volume of the stream until the actual head was equivalent to the theoretical head due to the velocity of the stream. As but a small fraction of the velocity of the stream can be taken up by a current motor, its efficiency is very small. Current motors may be used to obtain small amounts of power from large streams, but for large powers they are not practicable.

Horse-power of Water Flowing in a Tube.—The head due to

the velocity is  $\frac{v^2}{2g}$ ; the head due to the pressure is  $\frac{f}{w}$ ; the head due to actual height above the datum plane is h feet. The total head is the sum of these =  $\frac{v^2}{2a} + h + \frac{f}{w}$ , in feet, in which v = velocity in feet per second, f = pressurein lbs. per sq. ft., w= weight of 1 cu. ft. of water = 62.36 lbs. If p= pressure in lbs. per sq. in.,  $\frac{f}{v}=2.309p$ . In hydraulic transmission the velocity

and the height above datum are usually small compared with the pressure-head. The work or energy of a given quantity of water under pressure z = z its volume in cubic feet z = z its pressure in lbs. per sq. ft.; or if Q = z quantity in cubic feet per second, and z = z pressure in lbs. per square inch,  $W = \frac{1}{2} \frac{1}{2}$ 144pQ, and the H. P. =  $\frac{144pQ}{550}$  = .2618pQ.

**Maximum Efficiency of a Long Conduit.**—A. L. Adams and R. G. Gemmel (Eug y News, May 4, 1893), show by mathematical analysis that the conditions for securing the maximum amount of power through a long conduit of fixed diameter, without regard to the economy of water, is that the draught from the pipe should be such that the frictional loss in the pipe will be equal to one third of the entire static head.

Mill-Power,—A "mill-power" is a unit used to rate a water-power for the purpose of renting it. The value of the unit is different in different

the purpose of renting it. The value of the unit is different in different localities. The following are examples (from Emerson):

Holyoke, Mass.—Each mill-power at the respective falls is declared to be the right during 16 hours in a day to draw 38 cu. ft. of water per second at the upper fall when the head there is 20 feet, or a quantity proportionate to the height at the falls. This is equal to 86.2 hours in the day so much water as shall give a power equal to 25 cu. ft. a second at the great fall, when the fall there is 30 feet. Equal to 85 H. P. maximum.

Lawrence, Mass.—The right to 67 H. P. maximum.

water as shall give a horse-power equal to 30 cu. ft. per second when the head is 25 feet. Equal to 85 H. F. maximum.

Minneapolis, Minn.—30 cu. ft. of water per second with head of 22 feet.

Equal to 748 H. P.

Manchester, N. H.—Divide 725 by the number of feet of fall minus 1, and

the quotient will be the number of cubic feet per second in that fall. For 20

feet fall this equals 38.1 cu. ft., equal to 86.4 H. P. maximum.

Cohoes, N. Y.—"Mill-power" equivalent to the power given by 6 cu. ft.
per second, when the fall is 20 feet. Equal to 13.6 H. P., amaximum.

Passaic, N. J.—Mill-power: The right to draw 8½ cu. ft. of water per sec.,

fall of 22 feet, equal to 21.2 horse-power. Maximum rental \$700 per year for

each mill-power = \$33.00 per H. P.

The horse-power maximum above given is that due theoretically to the The horse-power maximum above given is that due theoretically to weight of water and the height of the fall, assuming the water-wheel to have perfect efficiency. It should be multiplied by the efficiency of the wheel, say 75% for good turbines, to obtain the H. P. delivered by the wheel. Value of a Water-power,—In estimating the value of a water-power, especially where such value is used as testimony for a plaintiff whose

water-power has been diminished or confiscated, it is a common custom for the person making such estimate to say that the value is represented by a sum of money which, when put at interest, would maintain a steam-plant

of the same power in the same place

Mr. Charles T. Main (Trans. A. S. M. E. xiii. 140) points out that this system of estimating is erroneous; that the value of a power depends upon a great number of conditions, such as location, quantity of water, fall or head, uniformity of flow, conditions which fix the expense of dams, canals, founda-tions of buildings, freight charges for fuel, raw materials and finished prod-uct, etc. He gives an estimate of relative cost of steam and water-power

for a 500 H. P. plant from which the following is condensed:

The amount of heat required per H. P. varies with different kinds of business, but in an average plan cotton-mill, the steam required for heating and slashing is equivalent to about 25% of steam exhausted from the high-pressure cylinder of a compound engine of the power required to run that

mill, the steam to be taken from the receiver.

The coal consumption per H. P. per hour for a compound engine is taken at 134 lbs. per hour, when no steam is taken from the receiver for heating purposes. The gross consumption when 25% is taken from the receiver is about 2.06 lbs.

75% of the steam is used as in a compound engine at 1.75 lbs. = 1.31 lbs. 25% " " high-pressure " 3.00 lbs. = .75 " 3.00 lbs. = .75

2.06

8 13

The running expenses per H. P. per year are as follows; 2.06 lbs. coal per hour = 21.115 lbs. for 101/4 hours or one day = 6503.42 \$8 71 lbs. for 308 days, which, at \$3.00 per long ton = Attendance of boilers, one man @ \$2.00, and one man @ \$1.25 = "engine, " " \$3.50. 2 00 2 16 80

Oil, waste, and supplies.
The cost of such a steam-plant in New England and vicinity of 500
H. P. is about \$65 per H. P. Taking the fixed expenses as 45 on
engine, 55 on boilers, and 25 on other portions, repairs at 25, i

portion, the total average per cent is about 121/2%, or \$65 × .121/2 = Gross cost of power and low-pressure steam per H. P. \$21 80

Comparing this with water-power, Mr. Main says: "At Lawrence the cost of dam and canals was about \$550,000, or \$65 per H. P. The cost per H. P. of wheel-plant from canal to river is about \$15 per H. P. Or plant, or about \$65 per H. P. used, the additional \$20 being caused by making the plant large enough to compensate for fluctuation of power due to rise and fall of river. The total cost per H. P. of developed plant is then about \$130 per H. P. Placing the depreciation on the whole plant at 2%, repairs at 1%, interest at 5%, taxes and insurance at 1%, or a total of 9%, gives:

Fixed expenses per H. P.  $$130 \times .09 = $1170$ Running " " (Estimated) 2 00 Running "

\$13 70

"To this has to be added the amount of steam required for heating purposes, said to be about 25% of the total amount used, but in winter months the consumption is at least 37½%. It is therefore necessary to have a boiler plant of about 37½% of the size of the one considered with the steam-plant.

costing about \$20 × .375 = \$7.50 per H. P. of total power used. The expense of running this boiler-plant is, per H. P. of the the total plant per year;

Fixed expenses 121/2% on \$7.50	 \$0.94 3.26
Labor	 1.23
Total	 \$5.43

Making a total cost per year for water-power with the auxiliary boiler plant \$13.70 + \$5.43 = \$19.13 which deducted from \$21.80 make a difference in favor of water-power of \$2.67, or for 10,000 H. P. a saving of \$26,700 per vear.

"It is fair to say," says Mr. Main," that the value of this constant power is a sum of money which when put at interest will produce the saving; or if 6%

is a fair interest to receive on money thus invested the value would be  $$26,700 \div .06 = $445,000.$ 

Mr. Main nakes the following general statements as to the value of a water-power: "The value of an undeveloped variable power is usually nothing if its variation is great, unless it is to be supplemented by a steam-plant. It is of value then only when the cost per horse-power for the double-plant is less than the cost of steam-power under the same conditions as mentioned for a permanent power, and its value can be represented in the same manner as the value of a permanent power has been represented.

"The value of a developed power is as follows: If the power can be run cheaper than steam, the value is that of the power, plus the cost of plant, less depreciation. If it cannot be run as cheaply as stand, considering its cost, etc., the value of the power itself is nothing, but the value of the plate its such as could be paid for it new, which would bring the total cost of run-

ining down to the cost of steam-power, less depreciation." Mr. Samuel Webber, Iron Age, Feb. and March, 1893, writes a series of articles showing the development of American turbine wheels, and incidentally criticises the statements of Mr. Main and others who have made comparisons of costs of steam and of water-power unfavorable to the latter, Hesays: "They have based their calculations on the cost of steam, on large compound engines of 1000 or more H. P. and 120 pounds pressure of steam in their boilers, and by careful 10-hour trials succeeded in figuring down steam to a cost of about \$20 per H. P., ignoring the well-known fact that its seems to a cost of about \$20 per H. P., ignoring the well-known fact that its average cost in practical use, except near the coal mines, is from \$40 to \$50. In many instances dams, canals, and modern turbines can be all completed for a cost of \$100 per H. P.; and the interest on that, and the cost of attendance and oil, will bring water-power up to but about \$10 or \$12 per annum; and with a man competent to attend the dynamo in attendance, it can probably be safely estimated at not over \$15 per H. P."

## TURRINE WHEELS.

Proportions of Turbines.-Prof. De Volson Wood discusses at length the theory of turbines in his paper on Hydraulic Reaction Motors, Trans. A. S. M. E. xiv. 266. His principal deductions which have an immediate bearing upon practice are condensed in the following:

Notation.

Q = volume of water passing through the wheel per second,

 $h_1 = \text{head in the supply chamber above the entrance to the buckets,}$ 

 $h_2$  = head in the tail-race above the exit from the buckets,

= fall in passing through the buckets.

 $\dot{H} = h_1 + z_1 - h_2$ , the effective head,  $\mu_1 = \text{coefficient of resistance along the guides}$ ,

 $\mu_2$  = coefficient of resistance along the buckets,

 $r_1 = \text{radius of the initial rim.}$ 

 $r_2^1$  = radius of the terminal rim, V = velocity of the water issuing from supply chamber,

 $v_1 = \text{initial velocity of the water in the bucket in reference to the bucket,}$   $v_2 = \text{terminal velocity in the bucket,}$ 

 $\omega$  = angular velocity of the wheel,  $\alpha$  = terminal angle between the guide and initial rim = CAB, Fig. 132,

 $\gamma_1=GFI$ , the angle between the terminal rim and terminal element of bucket and initial rim =EAD, the bucket.

a = eb, Fig. 133 = the arc subtending one gate opening,

 $a_1$  = the arc subtending one bucket at entrance. (In practice  $a_1$  is larger than a.)

 $a_2 = gh$ , the arc subtending one bucket at exit, K = bf, normal section of passage, it being assumed that the passages and buckets are very narrow,

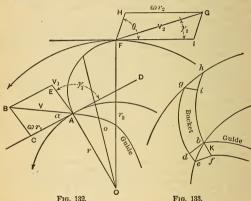
 $k_1 = bd$ , initial normal section of bucket,

 $k_2 = gi$ , terminal normal section,

 $\kappa_2 = y_s$ , terminal firm,  $\omega_1 = \text{velocity of initial rim}$ ,  $\omega_1 = \text{velocity of terminal rim}$ ,  $\omega_2 = \text{velocity of terminal rim}$ ,  $\theta = HFI$ , angle between the terminal rim and actual direction of the water at exit,

 $Y = \text{depth of } K. y, \text{ of } a_1, \text{ and } y_2 \text{ of } K_2, \text{ then}$ 

 $K = Ya \sin \alpha$ ;  $K_1 = y_1 a_1 \sin \gamma_1$ ;  $K_2 = y_2 a_2 \sin \gamma_2$ .



Three simple systems are recognized,  $r_1 < r_2$ , [called outward flow;  $r_1 > r_2$ , called inward flow;  $r_1 = r_2$ , called parallel flow. The first and second may be combined with the third, making a mixed system. Value of  $r_2$  (the quitting angle).—The efficiency is increased as  $r_2$  decreases, and is greatest for  $r_2 = 0$ . Hence, theoretically, the terminal element of the bucket should be tangent to the quitting rim for best efficiency. This, however, for the discharge of a full quantity of water, the results of the discharge of  $r_1$  and  $r_2$  and  $r_3$  are a full evalue. The large the diameter of the terminal rim to smaller may be this angle for a given dental matter of the terminal rim to smaller may be this angle for a given dental matter. may be this angle for a given depth of wheel and given quantity of water discharged. In practice  $\gamma_2$  is from 10° to 20°.

In a wheel in which all the elements except  $\gamma_2$  are fixed, the velocity of

the wheel for best effect must increase as the quitting angle of the bucket

decreases.

Values of  $a + \gamma_1$  must be less than 180°, but the best relation cannot be determined by analysis. However, since the water should be deflected from its course as much as possible from its entering to its leaving the wheel, the angle a for this reason should be as small as practicable.

In practice, a cannot be zero, and is made from 20° to 30°.

The value  $r_1 = 1.4r_2$  makes the width of the crown for internal flow about the same as for  $r_1 = r_2 \sqrt{\frac{1}{2}}$  for outward flow, being approximately 0.3 of the external radius.

Values of  $\mu_1$  and  $\mu_2$ .—The frictional resistances depend upon the construction of the wheel as to smoothness of the surfaces, sharpness of the angles, regularity of the curved parts, and also upon the speed it is run. These values cannot be definitely assigned beforehand, but Weisbach gives for good conditions  $\mu_1 = \mu_2 = 0.05$  to 0.10.

They are not necessarily equal, and \( \mu\_1 \) may be from 0.05 to 0.075, and \( \mu\_2 \)

from 0.06 to 0.10 or even larger. Values of  $\gamma_1$  must be less than  $180^{\circ} - \alpha_1$ 

To be on the safe side, y, may be 20 or 30 degrees less than 180°-2a, giving

$$\gamma_1 = 180^\circ - 2\alpha - 25$$
 (say) =  $155 - 2\alpha$ .

Then if  $\alpha=30^\circ$ ,  $\gamma_1=95^\circ$ . Some designers make  $\gamma_1$  90°; others more, and still others less, than that amount. Weisbach suggests that it be less, so that the bucket will be shorter and friction less. This reasoning appears to that the bucket will be shorter and friction less. This reasoning appears to be correct for the inflow wheel, but not for the outflow wheel. In the Tremont turbines, described in the Lowell Hydraulic Experiments, this angle is  $90^\circ$ , the angle  $\alpha$   $20^\circ$ , and  $\gamma_3$   $10^\circ$ , which proportions insured a positive pressure in the wheel. Fourneyron made  $\gamma_1 = 90^\circ$ , and  $\alpha$  from  $30^\circ$  to  $32^\circ$ , which values made the initial pressure in the wheel near zero. Form of Bucket.—The form of the bucket cannot be determined analytically. From the initial and terminal directions and the volume of the water flowing through the wheel, the area of the normal sections may be found.

The normal section of the buckets will be :

$$K = \frac{Q}{V}\,; \ k_1 = \frac{Q}{v_1}; \ k_2 = \frac{Q}{v_2}.$$

The depths of those sections will be:

$$Y = \frac{K}{a \sin a}; \quad y_1 = \frac{k_1}{a_1 \sin \gamma_1}; \quad y_2 = \frac{k_2}{a_2 \sin \gamma_2}.$$

The changes of curvature and section must be gradual, and the general form regular, so that eddies and whirls shall not be formed. For the same reason the wheel must be run with the correct velocity to secure the best effect. In practice the buckets are made of two or three arcs of circles.

The Value of  $\omega$ .—So far as analysis indicates, the wheel may run at any speed; but in order that the stream shall flow smoothly from the supply chamber into the bucket, the velocity V should be properly regulated. If  $\mu_1 = \mu_2 = 0.10$ ,  $r_2 + r_1 = 1.40$ ,  $\alpha = 25^\circ$ ,  $\gamma_1 = 95^\circ$ ,  $\gamma_2 = 12^\circ$ , the velocity of the initial rim for outward flow will be for maximum efficiency 0.614 of the

velocity due to the head, or  $\omega r_1 = 0.614 \sqrt{2gH}$ .

The velocity due to the head would be  $\sqrt{2qH} = 1.414 \sqrt{qH}$ .

For an inflow wheel for the case in which  $r_1^2 = 2r_2^2$ , and the other dimen

sions as given above,  $\omega r_1 = 0.682 \sqrt{2gH}$ .

The highest efficiency of the Tremont turbine, found experimentally, was 0.79375, and the corresponding velocity, 0.62645 of that due to the head, and for all velocities above and below this value the efficiency was less.

In the Tremont wheel  $a = 20^{\circ}$  instead of 25°, and  $\gamma_2 = 10^{\circ}$  instead of 12°. These would make the theoretical efficiency and velocity of the wheel some-

These would make the theoretical emicency and velocity or the wheel somewhat greater. Experiment showed that the velocity might be considerably larger or smaller than this amount without much diminution of the efficiency. It was found that if the velocity of the initial (or interior) rim was not less than 44% nor more than 75% of that due to the fall, the efficiency was 75% or more. This wheel was allowed to run freely without any brake except its own friction, and the velocity of the initial rim was observed to be 1.335  $\sqrt{2gH}$ , half of which is 0.6675  $\sqrt{2gH}$ , which is not far from the velocity giving maximum effect; that is to say, when the gate is fully raised the coefficient of effect is a maximum when the wheel is moving with about half its maximum velocity.

maximum velocity.

Number of Buckets.—Successful wheels have been made in which the distance between the buckets was as small as 0.75 of an inch, and others as much as 2.75 inches. Turbines at the Centennial Exposition had buckets from 4½ inches to 9 inches from centre to centre. If too large they will not work properly. Neither should they be too deep. Horizontal partitions are sometimes introduced. These secure more efficient working in case the gates are only partly opened. The form and number of buckets for commercial purposes are chiefly the result of experience.

Ratio of Radii.-Theory does not limit the dimensions of the wheel. In practice.

> for outward flow,  $r_2 \div r_1$  is from 1.25 to 1.50; for inward flow,  $r_2 + r_1$  is from 0.66 to 0.80.

It appears that the inflow-wheel has a higher efficiency than the outwardflow wheel. The inflow-wheel also runs somewhat slower for best effect, The centrifugal force in the outward-flow wheel tends to force the water outward faster than it would otherwise flow; while in the inward-flow wheel it has the contrary effect, acting as it does in opposition to the velocity in the buckets.

It also appears that the efficiency of the outward-flow wheel increases slightly as the width of the crown is less and the velocity for maximum efficiency is slower; while for the inflow-wheel the efficiency slightly increases for increased width of crown, and the velocity of the outer rim at the

same time also increases. Efficiency.-The exact value of the efficiency for a particular wheel must

be found by experiment.

It seems hardly possible for the effective efficiency to equal, much less exceed, 86%, and all claims of 90 or more per cent for these motors should be

discarded as improbable. A turbine yielding from 75% to 80% is extremely good. Experiments with higher efficiencies have been reported.

good. Experiments with impact endicates have been reported. The celebrated Tremont turbine gave '194%' without the 'diffuser,' which might have added some 2%. A Jouval turbine (parallel flow) was reported as yielding 0.75 to 0.90, but Morin suggested corrections reducing it to 0.63 to 0.71. Weisbach gives the results of many experiments, in which the efficiency ranged from 50% to 84%. Numerous experiments give E = 0.60 to 0.65, The efficiency, considering only the energy imparted to the wheel, will exceed by several per cent the efficiency of the wheel, for the latter will include the friction of the support and leakage at the joint between the sluice and wheel, which are not included in the former; also as a plant the resist-

and wheel, which are not included in the former; also as a plant for lessiances and losses in the supply-chamber are to be still further deducted.

The Crowns.—The crowns may be plane annular disks, or conical, or curved. If the partitions forming the buckets be so thin that they may be discarded, the law of radial flow will be determined by the form of the crowns. If the crowns be plane, the radial flow (or radial component) will diminish, for the outward flow-wheel, as the distance from the axis increases

-the buckets being full-for the angular space will be greater.

Prof. Wood deduces from the formulæ in his paper the tables on page 595. It appears from these tables: 1. That the terminal angle, a, has frequently

been made too large in practice for the best efficiency.

2. That the terminal angle, a, of the guide should be for the inflow less than 10° for the wheels here considered, but when the initial angle of the bucket is 90°, and the terminal angle of the guide is 5° 28′, the gain of effi-ciency is not 2% greater than when the latter is 25°.

That the initial angle of the bucket should exceed 90° for best effect for

outflow-wheels.

4. That with the initial angle between 60° and 120° for best effect on inflow

wheels the efficiency varies scarcely 1%.

5. In the outflow-wheel, column (9) shows that for the outflow for best effect the direction of the quitting water in reference to the earth should be nearly radial (from 76° to 97°), but for the inflow wheel the water is thrown forward in quitting. This shows that the velocity of the rim should somewhat exceed the relative final velocity backward in the bucket, as shown in columns (4) and (5),

6. In these tables the velocities given are in terms of \(\sqrt{2gh}\), and the cob. In these tables the velocines given are in terms of 1 forms and produce efficients of this expression will be the part of the head which would produce that velocity if the water issued freely. There is only one case, column 15, where the coefficient exceeds unity, and the excess is so small it may be dissipated in the coefficient exceeds unity, and the excess is so small it may be dissipated in the coefficient exceeds unity, and the produce the coefficient exceeds unity, and the excess is so small it may be dissipated in the coefficient exceeds unity, and the excess is so that the coefficient exceeds unity, and the excess is so that the coefficient exceeds unity and the excess is so that the coefficient exceeds unity and the excess is so that the coefficient exceeds unity and the excess is so that the coefficient exceeds unity and the excess is so that the exces carded; and it may be said that in a properly proportioned turbine with the conditions here given none of the velocities will equal that due to the head

in the supply-chamber when running at best effect.
7. The inflow turbine presents the best conditions for construction for producing a given effect, the only apparent disadvantage being an increased first cost due to an increased depth, or an increased diameter for producing a given amount of work. The larger efficiency should, however, more than

neutralize the increased first cost.

# Outward-flow Turbine.

i	$\sqrt{gH}$	111	0.67 0.76 0.84 1.00
$k_1 v_1 = k_2 v_2 = KV = Q = 1.$	Head Equivalent of Energy in quitting $w_2$ $w_2$	10	0.051H 0.039H 0.031H 0.022H
$1^{U_1} = k_2$	Direction of quitting Water.	6	76° 82° 97°
k	Terminal Angle of Guide.	œ	31° 17' 23° 56' 19° 5' 13° 31'
Parallel Crowns.	$\begin{array}{c} \text{Velocity of Exit} \\ \text{from supply} \\ \text{Chamber.} \\ \end{array}$	1-	0.595 \\ \frac{\pi_2gH}{\pi_2gH} \\ 0.749 \\ \frac{\pi_2gH}{\pi_2gH} \\ 0.749 \\ \frac{\pi_2gH}{\pi_2gH} \\ 0.886 \\ \ell_2gH}
	Relative Veloc- Relative Veloc- from supply. Ity of Exit. ity of Entrance. Chamber. $v_2$	9	0.356 \square \lambda 2gH 0.374 \square \lambda 2gH 0.286 \square \lambda 2gH 0.416 \square \lambda 2gH
$\gamma_2 = 19^{\circ}$ .		o.	1.048 \(\sqrt{2gH}\) 0.931 \(\sqrt{2gH}\) 0.843 \(\sqrt{2gH}\) 0.707 \(\sqrt{2gH}\)
$\mu_1 = \mu_2 = 0.10.$	Velocity Inner Rim. $r_1\omega'=V^{\frac{1}{2}}r_2\omega'$	4	0.687 \(\sigma\)29H 0.619 \(\sigma\)29H 0.565 \(\sigma\)29H 0.501 \(\sigma\)29H
μ1	Velocity Outer Rim. $r_2\omega'$	82	0.872 \(\frac{\partial \text{2gH}}{\partial \text{0.874}}\) \(\frac{\partial \text{2gH}}{\partial \text{0.798}}\) \(\frac{\partial \text{2gH}}{\partial \text{0.709}}\) \(\frac{\partial \text{2gH}}{\partial \text{0.709}}\)
14.	Effi- ciency.	C5	0.804 0.828 0.839 0.921
r1 = r2 1/3.	Initial Angle.	-	60° 90° 120° 150°

## Inward-flow Turbine.

$k_1v_1 = k_2v_2 = KV = Q = 1.$	$a$ $\theta$ $\frac{w^2}{2g}$ $k_2 \sqrt{gH}$	7° 0′ 110° 0.010 <i>H</i> 1.48 5° 28′ 106° 0.010 <i>H</i> 1.50 4° 46′ 108° 0.010 <i>H</i> 1.50
Parallel Crowns.	A	0.672 \(\frac{\psi_{2gH}}{\psi_{2gH}}\)
Paral	$v_1$	0.089 \(\frac{12gH}{2gH}\)
$\gamma_2 = 19^{\circ}$ .	202	0.476 \(\sqrt{2gH}\) 0.470 \(\sqrt{2gH}\) 0.456 \(\sqrt{2gH}\)
$\mu_1 = \mu_2 = 0.10.$	Velocity Inner Rim. $r_2\omega'$	0.501 \(\sqrt{2gH}\) 0.487 \(\sqrt{2gH}\) 0.473 \(\sqrt{9gH}\)
$\mu_1 =$	Velocity Outer Rim. $r_1\omega'$	$\begin{array}{c} 0.709 \ \sqrt{2gH} \\ 0.688 \ \sqrt{2gH} \\ 0.668 \ \sqrt{2gH} \end{array}$
/9r <sub>2</sub> .	E.	0.920
1,1 = 1	1,7	900

Tests of Turbines. - Emerson says that in testing turbines it is a rare thing to find two of the same size which can be made to do their best at the same speed. The best speed of one of the leading wheels is invariably wide from the tabled rate. It was found that a 54-in. Leffel wheel under 12 ft. head gave much better results at 78 revolutions per minute than at 90.

Overshot wheels have been known to give 75% efficiency, but the average

performance is not over 60%.

A fair average for a good turbine wheel may be taken at 75%. In tests of 18 wheels made at the Philadelphia Water-works in 1859 and 1860, one wheel gave less than 50% efficiency, two between 50% and 60%, six between 60% and 70%, seven between 71% and 77%, two 82%, and one 87.77%. (Emerson.)

Tests of Turbine Wheels at the Centennial Exhibition, 1876. (From a paper by R. H. Thurston on The Systematic Testing of Turbine Wheels in the United States, Trans. A. S. M. E., vili, 359.)—In 1876 the judges at the International Exhibition conducted a series of trials of turbines. Many of the wheels offered for tests were found to be more or less defective in fitting and workmanship. The following is a statement of the results of all turbines entered which gave an efficiency of over 75%. Seven other wheels were tested, giving results between 65% and 75%.

		_					
Maker's Name, or Name the Wheel is Known By.	Per Cent at Full Gate or Dis- charge.	Per Cent at about 9/10 of Full Discharge.	Per Cent at about % of Full Discharge.	Per Cent at about % of Full Discharge.	Per Cent at about 5% of Full Discharge.	Per Cent at about 15, of Full Discharge.	Per Cent at about 4/10 of Full Discharge.
Risdon National Geyelin (single)	87.68 83.79 83.30		86.20	82,41 70.79		75.85	
Thos. Tait	82.13 81.21		71.01	70.40 55.90	66.35		55.00
Rodney Hunt Mach. Co	78.70 79.59 77.57	71.66	81.24	68.60 79.92	51.03 67.23	69.59	
Knowlton & Dolan E. T. Cope & Sons	77.43 76.94	74.25	69,92		62.75		
Barber & Harris	76.16 75.70 75.15	73.33	67.08 71.90	67.57 70.52	70.87 62.06	71.74 66.04	

The limits of error of the tests, says Prof. Thurston, were very uncertain; they are undoubtedly considerable as compared with the later work done in

the permanent flume at Holyoke-possibly as much as 45 or 55.

Experiments with "dranght-tubes," or "suction-tubes," which were actually "diffusers" in their effect, so far as Prof. Thurston has analyzed them, indicate the loss by friction which should be anticipated in such cases, this loss decreasing as the tube increased in size, and increasing as its diameter approached that of the wheel-the minimum diameter tried. It was sometimes found very difficult to free the tube from air completely, and next to impossible, during the interval, to control the speed with the brake. Several trials were often necessary before the power due to the full head could be obtained. The loss of power by gearing and by belting was variable with the proportions and arrangement of the gears and pulleys, length of belt, etc., but averaged not far from 30% for a single pair of bevelgears, uncut and dry. but smooth for such gearing, and but 10% for the same gears, well lubricated, after they had been a short time in operation. The amount of power transmitted was, however, small, and these figures are probably much higher than those representing ordinary practice. Introducing a second pair—than those representing ordinary practice. Introducing a second pair—than those representing ordinary practice. although the difference between the case in which the larger gear was the driver, and the case in which the small wheel was the driver, was perceivable, and was in favor of the former arrangement. A single straight belt gave a loss of but 2% or 3%, a crossed belt 6% to 8%, when transmitting 14 horse-power with maximum tightness and transmitting power. A "quarter turn" wasted about 10% as a maximum, and a "quarter twist" about 5%.

Dimensions of Turbines .- For dimensions, power, etc., of standard makes of turbines consult the catalogues of different manufacturers. The wheels of different makers vary greatly in their proportions for any given capacity.

The Pelton Water-wheel. - Mr. Ross E. Browne (Eng'a News, Feb. 20, 1892) thus outlines the principles upon which this water-wheel is

constructed:

The function of a water-wheel, operated by a jet of water escaping from a nozzle, is to convert the energy of the jet, due to its velocity, into useful work In order to utilize this energy fully the wheel-bucket, after catching the jet, must bring it to rest before discharging it, without inducing turbu-

lence or agitation of the particles.

lence or agitation of the particles.

This cannot be fully effected, and unavoidable difficulties necessitate the loss of a portion of the energy. The principal losses occur as follows: First, in sharp or angular diversion of the jet in entering, or in its course through the bucket, causing impact, or the conversion of a portion of the energy into heat instead of useful work. Second, in the so-called frictional resistance offered to the motion of the water by the wetted surfaces of the buckets, causing also the conversion of a portion of the energy into heat instead of useful work. Third, in the velocity of the water, as it leaves the bucket, representing energy which has not been converted into work.

Hence, in seeking a high efficiency: 1. The bucket-surface at the entrance should be approximately parallel to the relative course of the jet, and the bucket should be curved in such

a manner as to avoid sharp angular deflection of the stream. If, for example, a jet strikes a surface at an angle and is sharply deflected, a portion of the water is backed, the smoothness of the stream is disturbed, and there results considerable loss by impact and otherwise. The entrance and deflection in the Pelton bucket are such as to avoid



Fig. 135.

these losses in the main. (See Fig. 136.)

2. The number of buckets should be small, and the path of the jet in the bucket short; in other words, the total wetted surface should be small, as the loss by friction will be proportional to this. 3. The discharge end of the bucket should be as nearly tangential to the

wheel periphery as compatible with the clearance of the bucket which follows; and great differences of velocity in the parts of the escaping water should be avoided. In order to bring the water to rest at the discharge end of the bucket, it is shown, mathematically, that the velocity of the bucket

should be one half the velocity of the jet.

A bucket, such as shown in Fig. 135, will cause the heaping of more or less dead or turbulent water at the point indicated by dark shading. This dead water is subsequently thrown from

the wheel with considerable velocity, and represents a large loss of energy. The introduction of the wedge in the Pelton bucket (see Fig. 134) is an efficient means of avoiding this loss.

A wheel of the form of the Pelton conforms closely in

construction to each of these requirements.

construction to each of these requirements.

In a test made by the proprietors of the Idaho mine, near Grass Valley, Cal., the dimensions and results were as follows: Main supply-pipe, 22 in, diameter, 6900 ft. long, with a head of 386½ feet above centre of nozzle. The loss by friction in the pipe was 1.8 ft., reducing the effective head to 384.7 ft. The Pelton wheel used in the test was 6 ft. in diameter and the nozzle was 1.89 in, diameter. The work done was measured by a Prony brake, and the mean of 13 tests showed a useful effect of 87.3%.

The Pelton wheel is also used as a motor for small powers. A test by M. E. Cooley of a 12-inch wheel, with a 3\(\frac{2}{2}\)-inth nozzle, under 100 lbs. pressure, gave 1.9 horse-power. The theoretical discharge was .0935 cubic feet per second, and the theoretical horse-power 2.45; the efficiency being 80 per cent. Two other styles of water-motor tested at the same time each gave

efficiencies of 55 per cent.

## Pelton Water-wheel Tables. (Abridged.)

The smaller figures under those denoting the various heads give the spouting velocity of the water in feet per minute. The cubic-feet measurement is also based on the flow per minute.

Head in ft.	Size of Wheels.	6 in. No.1	12 in. No. 2	18 in. No. 3	18 in. No. 4	24 in. No. 5	gt.	ft.	5 ft.	6 ft.
20 2151.97	Horse-power. Cubic feet Revolutions	.05 1.67 684	.12 3.91 342	.20 6.62 228	.37 11.72 228	.66 20.83 171	1 50 46.93 114	2.64 83.32 85	4.18 130.36 70	6.00 187.72 57
30 2635.62	Horse-power. Cubic feet Revolutions	.10 2.05 837	.23 4.79 418	.38 8.11 279	.69 14.36 279	1.22 25.51 209	2.76 57.44 139	4.88 102.04 104	7.69 159.66 83	11.04 229.76 69
40 3043.39	Horse-power. Cubic feet, Revolutions	.15 2.37 969	.35 5.53 484	.59 9.37 323	1.06 16.59 323	1.89 29.46 242	4.24 66.36 161	7.58 107.84 121	11.85 184.36 96	16.96 265.44 80
50 3402.61	Horse-power. Cubic feet Revolutions	.21 2.64 1083	.49 6.18 541	.84 10.47 361	1.49 18.54 361	2.65 32.93 270	5.98 74.17 180	10.60 131.72 135	16.63 206.13 108	23.93 296.70 90
60 3727.37	Horse-power. Cubic feet Revolutions	.28 2.90 1185	.65 6.77 592	1.10 11.47 395	1.96 20.31 395	3.48 36.08 296	7.84 81.25 197	13.94 144.32 148	21.77 225.80 118	31.36 325.00 98
70 4026.00	Horse-power. Cubic feet Revolutions	.35 3.13 1281	.82 7.31 640	1.39 12.39 427	2.47 21.94 427	4.39 38.97 320	9.88 87.76 213	17.58 155.88 160	27.51 243.89 130	39.52 351.04 106
80 4303,99	Horse-power. Cubic feet Revolutions	.43 3.35 1368	1.00 7.82 684	1.70 13 25 456	3.01 23.46 456	5.36 41.66 342	12.04 93.84 228	21.44 166.64 171	33.54 260.73 137	48.16 375.36 114
90 4565.04	Horse-power. Cubic feet Revolutions	.51 3.55 1452	1.20 8.29 726	2.03 14.05 484	3.60 24.88 484	6.39 44.19 363	14.40 99.52 242	25.59 176.75 181	40.04 276.55 145	57.60 398.08 121
100 4812.00	Horse-power. Cubic feet Revolutions	.60 3.74 1580	1.40 8.74 765	2.32 14.81 510	4.21 26.22 510	7.49 46.58 382	16.84 104.88 255	29.93 186.32 191	46.85 291.51 152	67.36 419.52 127
120 5271.30	Horse-power. Cubic feet Revolutions	.79 4.10 1677	1 84 9.57 838	3.12 16.21 559	5.54 28.72 559	9.85 51.02 419	22.18 114.91 279	39.41 204.10 209	61.66 319.33 167	88.75 459.64 139
140 5693.65	Horse-power. Cubic feet. Revolutions	.99 4.43 1812	2.33 10.34 906	3.94 17.53 604	6.99 31.03 604	12.41 55.11 453	27.96 124.12 302	49.64 220.44 226	77.71 844.92 181	111.85 496.48 151
160 6086 74	Horse-power. Cubic feet Revolutions	4.73	2.84 11.05 969	4.82 18.74 646	8.54 33.17 646	15.17 58.92 484	34.16 132.68 323	60.68 235.68 242	94.94 368.73 193	136.65 530.75 161
180 6455.97	Horse power. Cubic feet Revolutions	5.02	3.39 11.72 1024	5.75 19.87 683	10.19 35.18 683	18.10 62.49 513	40.77 140.74 342	72.41 249.97 256	113,30 391,10 206	163.08 562.96 171
200 6805.17	Horse-power. Cubic feet Revolutions	5.29	3.97 12.36 1080	6.74 20.94 720	11.93 37.08 720	21.20 65.87 540	47.75 148.35 360	84.81 263.49 270	132.70 412 25 216	191.00 593.40 180
250 7608.44	Horse-power. Cubic feet Revolutions	5.92	5.56 13.82 1209	9.42 23.42 806	16.68 41.46 806	29.63 73.64 605	165.86	118.54 294.59 302	185.47 460.91 241	266.96 663.45 202

Pelton Water-wheel Tables .- Continued.

Head in ft.	Size of Wheels,	6 in. No.1	12 in. No. 2	18 in. No. 3	18 in, No. 4	24 in. No. 5	3 ft.	4 ft.	5 ft.	ft.
300 8334.62		3.13 6.48 2652	7.31 15.13 1326	12.38 25.66 884	21.93 45.42 884	38.95 80.67 663	87.73 181.69 442	155.83 322.71 331	243.82 504.91 265	350.94 726.76 221
350 9002.43	Horse-pow'r Cubic feet Revolutions	3.94 7.00 2865	9.21 16.35 1432	15.61 27.71 955	27.64 49.06 955		110.56 196.25 477		307.25 545.36 285	442.27 785.00 238
400 9624.00	Horse-pow'r Cubic feet Revolutions	7.49	11.25 17.48 1581	29.63	33.77 52.45 1021		135.08 209.80 510	239.94 372.64 382	375.40 583.02 306	540.35 839.20 255
450 10207.79	Horse-pow'r Cubic feet Revolutions	5.75 7.94 3249	18.54	31.42	40.29 55.63 1083	71.57 98.81 812	161.19 222.52 541	286.31 395.24 406	447.95 618.38 324	644.78 890.11 270
500 10759.96	Horse-pow'r Cubic feet Revolutions	6.74 8.37 3426	19.54	33.12	47.20 58.64 1142		188.80 234.56 571		524.66 651.83 342	755.20 938.25 285
600 11786.94	Horse-pow'r Cubic feet Revolutions				62.04 64.24 1251		248.16 256.95 625		689.63 714.05 375	992.65 1027.80 312
650 12268.24	Horse-pow'r Cubic feet Revolutions			:::::			279.82 267.44 651	497.01 475.02 488	777.62 743.21 390	1119.29 1069.77 325
700 12731.34	Horse-pow'r Cubic feet Revolutions							555.46 492.95 506	869.06 771.26 405	1250.92 1110.16 337
750 13178.19	Horse-pow'r Cubic feet Revolutions						287.28	616.03 510.25 524		1387.34 1149.13 349
800 13610.40	Horse-pow'r Cubic feet Revolutions				95.52 74.17 1444		296.70	526.99	1061.81 824.51 433	
900	Horse-pow'r Cubic feet Revolutions				113.98 78.67 1532	139.74	314.70	558.96	1267.02 874.53 459	
1000 15216.89	Horse-pow'r Cubic feet Revolutions					147.30	331.78	589.19		1326.91

## THE POWER OF OCEAN WAVES.

Albert W. Stahl, U. S. N. (Trans. A. S. M. E., xiii. 438), gives the following formulæ and table, based upon a theoretical discussion of wave motion: The total energy of one whole wave-length of a wave H feet high, L feet long, and one foot in breadth, the length being the distance between successive crests, and the height the vertical distance between the crest and the trough, is  $E=8LH^2\left(1-4.935\,\frac{L^2}{L^2}\right)$  foot-pounds,

The time required for each wave to travel through a distance equal to its own length is  $P = \sqrt{\frac{L}{5.193}}$  seconds, and the number of waves passing any

given point in one minute is  $N = \frac{60}{P} = 60 \sqrt{\frac{5.123}{L}}$ . Hence the total energy

of an indefinite series of such waves, expressed in horse-power per foot of breadth, is

$$\frac{E \times N}{33000} = .0329H^2L\left(1 - 4.935\frac{H^2}{L^2}\right).$$

By substituting various values for  $H \div L$ , within the limits of such values actually occurring in nature, we obtain the following table of

TOTAL ENERGY OF DEEP-SEA WAVES IN TERMS OF HORSE-POWER PER FOOT OF BREADTH.

Ratio of Length of	Length of Waves in Feet.										
Waves to Height of Waves.	25	50	75	100	150	200	[300	400			
50 40 30 20 15 10 5	.04 .06 .12 .25 .42 .98 3.30	.23 .36 .64 1.44 2.83 5.53 18.68	.64 1.00 1.77 3.96 6.97 15.24 51 48	1.31 2.05 3.64 8.13 14.31 31.29 105.68	3.62 5.65 10.02 21 79 39.43 86.22 291.20	7.43 11.59 20.57 45.98 80.94 177.00 597.78	20.46 31.95 56.70 120.70 223.06 487.75 1647.31	42.01 65.58 116.38 260.08 457.89 1001.25 3381.60			

The figures are correct for trochoidal deep-sea waves only, but they give a close approximation for any nearly regular series of waves in deep water

and a fair approximation for waves in shallow water. The question of the practical utilization of the energy which exists in ocean waves divides itself into several parts:

1. The various motions of the water which may be utilized for power

purposes.

2. The wave motor proper. That is, the portion of the apparatus in direct contact with the water, and receiving and transmitting the energy thereof; together with the mechanism for transmitting this energy to the machinery for utilizing the same.

Regulating devices, for obtaining a uniform motion from the irregular and more or less spasmodic action of the waves, as well as for adjusting the

apparatus to the state of the tide and condition of the sea.

4. Storage arrangements for insuring a continuous and uniform output of

power during a calm, or when the waves are comparatively small.

power during a calm, or when the waves are comparatively small. The motions that may be utilized for power purposes are the following: 1. Vertical rise and fall of particles at and near the surface. 2. Horizontal to-and-fro motion of particles at and near the surface. 3. Varying slope of surface of wave. 4. Impetus of waves rolling up the beach in the form of breakers. 5. Motion of distorted verticals. All of these motions, except the last one mentioned, have at various times been proposed to be utilized for power purposes; and the last is proposed to be used in apparatus described

by Mr. Stahl.

The motion of distorted verticals is thus defined: A set of particles, origination of distorted verticals in the water is at rest, does not nally in the same vertical straight line when the water is at rest, does not remain in a vertical line during the passage of the wave; so that the line connecting a set of such particles, while vertical and straight in still water, becomes distorted, as well as displaced, during the passage of the wave, its upper portion moving farther and more rapidly than its lower portion.

Mr. Stahl's paper contains illustrations of several wave-motors designed upon various principles. His conclusions as to their practicability is as follows: "Possibly none of the methods described in this paper may ever prove commercially successful; indeed the problem may not be susceptible of a financially successful solution. My own investigations, however, so far as I have yet been able to carry them, incline me to the belief that wave-power can and will be utilized on a paying basis."

Continuous Utilization of Tidal Power. (P. Decœur, Prop. List (I. W. 1800).—It conventions with the training walls to be accurrated in

Inst. C. E. 1890.)-In connection with the training-walls to be constructed in

the estuary of the Seine, it is proposed to construct large basins, by means of which the power available from the rise and fall of the tide could be utilized. The method proposed is to have two basins separated by a bank rising above high water, within which turbines would be placed. The upper basin would be in communication with the sea during the higher one third of the would be in communication with the sea during the higher one third of the tidal range, rising, and the lower basin during the lower one third of the tidal range, falling. If H be the range in feet, the level in the upper basin would never fall below \(^2\)\_{\begin{subarray}{c} ML}\$ measured from low water, and the level in the lower basin would never rise above \(^4\)\_{\begin{subarray}{c} ML}\$. The available head varies between 0.53H and 0.80H, the mean value being \(^3\)\_{\begin{subarray}{c} ML}\$. If S square feet be the area of the lower basin, and the above conditions are fulfilled, a quantity 1/38H c. of, to water is delivered through the turbines in the space of \(^3\)\_{\begin{subarray}{c} ML}\$ hours. The mean flow is, therefore, \(^3M\)\_{\begin{subarray}{c} ML}\$ and \(^3M\)\_{ the mean fall being 34H, the available gross horse-power is about 1/30S'H2, where S' is measured in acres. This might be increased by about one third where s' is measured in acres. This might be increased by about one third if a variation of level in the basins amounting to \( \frac{1}{2} \) Mere permitted. But to reach this end the number of turbines would have to be doubled, the mean head being reduced to \( \frac{1}{2} \) And it would be more difficult to transmit a constant power from the turbines. The turbine proposed is of an improved model designed to utilize a large flow with a moderate diameter. One has been designed to produce 300 horse-power, with a minimum head of 5 ft. 3 in, at a speed of 15 revolutions per minute, the vanes having 13 ft. internal diameter. The speed would be maintained constant by regulating sluices.

## PUMPS AND PUMPING ENGINES.

**Theoretical Capacity of a Pump.**—Let Q' = cu. ft. per min.; G' = Amer. gals. per min. = 7.4805Q'; d = diam. of pump in inches; l = stroke in inches; N = number of single strokes per min.

in inches; 
$$N=$$
 number of single strokes per min. Capacity in cu. ft. per min.  $=Q'=\frac{\pi}{4}\cdot\frac{d^2}{144}\cdot\frac{lN}{l2}=.0004545Nd^2l;$  Capacity in gals. per min.  $G'=\frac{\pi}{4}\cdot\frac{Nd^2l}{231}\cdot\dots\dots=.0034Nd^2l;$  Capacity in gals. per hour ....= $204Nd^2l$ .

Capacity in gals. per min. 
$$G' = \frac{\pi}{4}$$
.  $\frac{Nd^2l}{221}$ .... = .0034 $Nd^2l$ ;

Diameter required for a given capacity per min. 
$$d=46.9\sqrt{\frac{Q'}{Nl}}=17.15\sqrt{\frac{G'}{Nl}}.$$

If 
$$v = \text{piston speed in feet per min.}$$
,  $d = 13.54 \sqrt{\frac{Q'}{v}} = 4.95 \sqrt{\frac{G'}{v}}$ .

If the piston speed is 100 feet per min .:

$$Nl = 1200$$
, and  $d = 1.354 \sqrt{Q'} = .495 \sqrt{G'}$ ;  $G' = 4.08d^2$  per min.

The actual capacity will be from 60% to 95% of the theoretical, according to the tightness of the piston, valves, suction-pipe, etc.

Theoretical Horse-power required to raise Water to a given Height.-Horse-power =

$$\frac{\text{Volume in cu. ft. per min.} \times \text{pressure per sq. ft.}}{33,000} = \frac{\text{Weight } \times \text{height of lift}}{33,000}$$

 $Q'=\mathrm{cu.}$ ft. per min.;  $G'=\mathrm{gals.}$  per min.;  $W=\mathrm{wt.}$  in lbs.;  $P=\mathrm{pressure}$  in lbs. per sq. ft.;  $p=\mathrm{pressure}$  in lbs. per sq. ft.;  $H=\mathrm{height}$  to lift in ft.;  $W=0.36Q',\,P=144p,\,p=.433H,\,H=2.300p,\,G'=7.4806Q'.$ 

$$\begin{split} \text{HP} &= \frac{Q'P}{33,000} = \frac{Q'H \times 144 \times .433}{33,000} = \frac{Q'H}{529.2} = \frac{G'H}{3958.7}; \\ \text{HP} &= \frac{WH}{33,000} = \frac{Q' \times 62.36 \times 2.309p}{33,000} = \frac{Q'p}{229.2} = \frac{G'p}{1714.5}; \end{split}$$

For the actual horse-power required an allowance must be made for the friction, slips, etc., of engine, pump, valves, and passages,

**Depth of Suction.**—Theoretically a perfect pump will draw water from a height of nearly 34 feet, or the height corresponding to a perfect vacuum (14.7 lbs. × 2.30) = 33,95 feet); but since a perfect vacuum cannot be obtained, on account of valve-leakage, air contained in the water, and the vapor of the water itself, the actual height is generally less than 30 feet. When the water is warm the height to which it can be lifted by suction decreases, on account of the increased pressure of the vapor. In pumping hot water, therefore, the water must flow into the pump by gravity. The following table shows the theoretical maximum depth of suction for different temperatures, leakage not considered:

Temp.	Absolute Pressure of Vapor, lbs. per sq. in,	in		Temp. F.	Absolute Pressure of Vapor, lbs. per sq. in.	vacuum	
101.4	1	27.88	31.6	183.0	8	13.63	15.5
126.2	2	25.85	29.3	188.4	9	11.59	13.2
144.7	3	23.81	27.0	193.2	10	9.55	10.9
153.3	4	21.77	24.7	197.6	11	7.51	8.5
162.5	5	19.74	22.4	201.9	12	5.48	6.2
170.3	6	17.70	20.1	205.8	13	3.44	3.9
177.0	7	15.66	17.8	209.6	14	1.40	1.6

Amount of Water raised by a Single-acting Lift-pump.

—It is common to estimate that the quantity of water raised by a single-acting bucket-valve pump per minute is equal to the number of strokes in one direction per minute, multiplied by the volume traversed by the piston in a single stroke, on the theory that the water rises in the pump only when the piston or bucket ascends; but the fact is that the column of water does not cases flowing when the bucket descends, but flows on continuously through the valve in the bucket, so that the discharge of the pump, if it is operated at a high speed, may amount to nearly double that calculated from the displacement multiplied by the number of single strokes in one direction.

Proportioning the Steam-cylinder of a Direct-acting Pump.-Let

A =area of steam-cylinder:

a = area of pump-cylinder; $D = \text{diameter of steam-cylinder}; \quad d = \text{diameter of pump-cylinder};$ 

P = steam-pressure, lbs. per sq. in.; p = resistance per sq. in. on pumps; H = head = 2.309n; p = .433H;

H = head = 2.309p; p = .433H; p = .433H;  $E = \text{efficiency of the pump} = \frac{p}{\text{work done in pump-cylinder}}$ 

$$A = \frac{ap}{EP}; \ a = \frac{EAP}{p}; \ D = d\sqrt{\frac{p}{EP}}; \ d = D\sqrt{\frac{EP}{p}}; \ P = \frac{ap}{EA}; \ p = \frac{EAP}{a}.$$

$$\frac{A}{a} = \frac{p}{EP} = \frac{.433H}{EP}; \ H = 2.309EP\frac{A}{a}; \ \text{If } E = 75\%, H = 1.732P\frac{A}{a}.$$

E is commonly taken at 0.7 to 0.8 for ordinary direct-acting pumps. For the highest class of pumping-engines it may amount to 0.9. The steampressure P is the mean effective pressure, according to the indicator-diagram; the water-pressure p is the mean total pressure acting on the pump plunger or piston, including the suction, as could be shown by an indicatordiagram of the water-cylinder. The pressure on the pump-piston is frequently much preater than that due to the height of the lift, on account of the triction of the valves and passages, which increases rapidly with velocity

Speed of Water through Pipes and Pump-passages,— The speed of the water is commonly from 100 to 200 feet per minute. If 200 feet per minute is exceeded, the loss from friction may be considerable.

The diameter of pipe required is  $4.95\sqrt{\frac{\text{gallons per minute}}{\text{velocity in feet per minute}}}$ 

For a velocity of 200 feet per minute, diameter = 35 × 1 gallons per min.

PUMPS. 603

Sizes of Direct-acting Pumps.—The two following tables are selected from catalogues of manufacturers, as representing the two common types of direct-acting pump, viz., the single-cylinder and the duplex. Both types are now made by most of the leading manufacturers.

## The Deane Direct-acting Pump. STANDARD SIZES FOR ORDINARY SERVICE.

	STANDARD SIZES FOR ORDINARY SERVICE.												
Diameter of Steam- cylinder in In. Diameter of Water- cylinder in In.	Length of Stroke.	Gallons per Stroke.	Strokes per Minute.	per M	acity Iinute liven eed. Gals.	Extreme Length in Inches.	Extreme Width in Inches.	Size of Steam Supply-pipe.	Size of Steam Exhaust-pipe.	Size of Suction.	Size of Discharge.		
4 4 4 4 4 4 4 4 5 5 5 4 5 5 7 7 7 7 7 7	5 7 7 7 7 7 7 10 10 12 12 12 12 12 12 12 12 18 18 12 18 16 16 16 16 16 16 16 16 16 16 16 16 16	1.14 2.77 3.99 5.11 1.64 1.20 2.01 2.01 2.01 2.01 2.01 2.01 2.01	1 to 300 1 to 250 1 to 175 1 to 175 1 to 150 1 to 175 1 to 155 1 to 175 1 t	130 130 125 125 110 110 110 100 100 100 100 100 100 10	18 35 49 49 64 49 90 180 210 230 210 230 210 261 408 261 408 428 408 428 408 408 428 408 408 411 1114 1322 11044 1322 1164 1322 1975	33 33 34 45 45 45 58 58 58 58 68 68 68 68 68 68 68 68 68 68 68 68 68	91/2/2 91/2 91/2 115 115 117 117 117 117 117 120/2/2 30/2 30/2 30/2 30/2 30/2 30/2 30/	1 1 1 1 1 1 1 1 1 2 2 2 2 2 2 2 2 2 2 2	**************************************	2233355554558888888888888888888888888888	11/2/2 21/2 21/2 24/4 4 4 4 4 4 4 4 4 4 4 4 4 4 10 10 10 10 10 10 10 10 10 10 10 10 10		

Efficiency of Small Direct-acting Pumps,—Chas. E. Emery, in Reports of Judges of Philadelphia Exhibition, 1856, Group xx., says: "Experiments made with steam-pumps at the American Institute Exhibition of 1867 showed that average stized steam-pumps do not, on the average, utilifying more than 50 per cent of the indicated power in the steam-cylinders, the remainder being absorbed in the friction of the engine, but more particularly in the passage of the water through the pump. Again, all ordinary steam-pumps for miscellaneous uses require that the steam-cylinder shall have three to four times the area of the water-cylinder to give sufficient power

when the steam is accidentally low; hence as such pumps usually work against the atmospheric pressure, the net or effective pressure forms as mall percentage of the total pressure, which, with the large extent of radiating surface exposed and the total absence of expansion, makes the expenditure of steam very large. One pump tested required 120 pounds weight of steam per indicated horse-power per hour, and it is believed that the cost will rarely fall below 60 pounds; and as only 50 per cent of the indicated power is utilized, it may be safely stated that ordinary steam-pumps rarely require less than 120 pounds of steam per hour for each horse-power utilized in raising water, equivalent to a duty of only 15,000,000 foot-pounds per 100 pounds of coal. With larger steam-pumps, particularly when they are proportioned for the work to be done, the duty will be materially increased."

## The Worthington Duplex Pump.

STANDARD SIZES FOR ORDINARY SERVICE.

DIAMPARE DIES FOR ORDINARI DERVICE.											
inders.	s per ser. Ser. Ser. Ser. Ser. Ser. Ser. Ser. S				Minute by	equired in ump to do ne speed.	Sizes of Pipes for Short Lengths. To be increased as length increases.				
Diameter of Steam-cylinders.	Diameter of Water-plungers	Length of Stroke.	Displacement in Gallous per Stroke of One Plunger.	Proper Strokes per Minute of One Plunger, varying with kind of work and pressure.	Gallons delivered per Minute by both Plungers at stated Num- ber of Strokes.	Diameter of Plunger required in any single-cylinder pump to do the same work at same speed.	Steam-pipe.	Exhaust-pipe.	Suction-pipe,	Discharge-pipe.	
3 41/5 51/4 6 71/5 71/5 71/5 9 10 10 10 12 14 16 181/5 20 14 16 181/5 20	2 342 4 4 5 4 5 4 5 6 7 7 7 8 8 8 8 8 9 10 14 10 14 10 14 11 11 11 11 11 11 11 11 11 11 11 11	3 4 5 6 6 6 6 10 10 10 10 10 10 10 10 10 10 10 10 10	.04 .10 .20 .33 .42 .51 .69 .93 1.22 1.66 1.66 2.45 2.45 2.45 2.45 3.57 3.57 3.57 4.89	100 to 250 100 to 250 100 to 200 100 to 200 100 to 150 100 to 150 100 to 150 75 to 125	8 to 20 20 to 40 40 to 80 70 to 100 85 to 120 100 to 150 100 to 150 100 to 170 135 to 230 145 to 410 245 to 410 245 to 410 245 to 610 365 to 610 365 to 610 365 to 610 530 to 890 530 to 890 530 to 890 530 to 120 730 to 1220	712 812 978 978 978 12 12 12 1414 1414 1414	\$6\234 1\1\22 2\22\22\22\22 2\22\22\22 3\4\22\23 4\22\23 4\22\23 4\22\23 4\22\23 4\22\23 4\22\23 4\22\23 4\23\	11/2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2	11/4 21/2 3 4 4 4 4 4 5 6 6 6 6 6 6 6 8 8 8 8 8 8 10 10	11123333455555555577778888810	
14 16 181/2 20 181/2 20 17 20 20 25	12 12 14 14 10 12 15 15	10 10 10 15 15 15 15	4.89 4.89 6.66 6.66 5.10 7.34 11.47	75 to 125 75 to 125 75 to 125 75 to 122 50 to 100 50 to 100 50 to 100 50 to 100	730 to 1220 730 to 1220 990 to 1660 990 to 1660 510 to 1020 730 to 1460 1145 to 2290 1145 to 2290	17 1934 1934 14 17 21 21	21/2 21/2 3 4 3 4 3 4 	5 5 31/2 5 31/2 5 31/2	10 10 12 12 12 10 12	8 10 10 8 10	

PUMPS. 605

Speed of Piston .- A piston speed of 100 feet per minute is commonly assumed as correct in practice, but for short-stroke pumps this gives too high a speed of rotation, requiring too frequent a reversal of the valves. For long stroke pumps, 2 feet and upward, this speed may be considerably exceeded, if valves and passages are of ample area.

Number of Strokes required to Attain a Piston Speed from 50 to 125 Feet per Minute for Pumps having Strokes from 3 to 18 Inches in Length.

Strokes from 5 to 10 Inches in Length.														
Pis- feet		Length of Stroke in Inches.												
d of in min	3	4	5	6	7	8	10	12	15	18				
Speed ton, i	Number of Strokes per Minute.													
50	200	150	120	100	86	75	60	50	40	33				
55	220	165	132	110	94	82.5	66	55	44	37				
60	240	180	144	120	103	90	72	60	48	40				
65	260	195	156	130	111	97.5	78	65	52	43				
70	280	210	168	140	120	105	84	70	56	47				
75	300	225	180	150	128	112.5	90	75	60	50				
80	320	240	192	160	137	120	96	80	64	53				
85	340	255	204	170	146	127.5	102	85	68	57				
90	360	270	216	180	154	135	108	90	72	60				
95	380	285	228	190	163	142.5	114 .	95	76	63				
100	400	300	240	200	171	150	120	100	80	67				
105	420	315	252	210	180	157.5	126 -	105	84	70				
110	440	330	264	220	188	165	132	110	88	73				
115	460	345	276	230	197	172.5	138	115	92	77				
120	480	360	288	-240	206	180	144	120	96	80				
125	500	375	300	250	214	187.5	150	125	100	83				

Piston Speed of Pumping-engines. (John Birkinbine, Trans. A. I. M. E., v. 459.)—In dealing with such a ponderous and unyielding substance as water there are many difficulties to overcome in making a pump work with a high piston speed. The attainment of moderately high speed is, however, easily accomplished. Well-proportioned pumping-engines of large capacity, provided with ample water-ways and properly constructed sarge capacity, provided with ample water-ways and properly constructed valves, are operated successfully against heavy pressures at a speed of \$50 ft. per minute, without "thug," concussion, or injury to the apparatus, and there is no doubt that the speed can be still further increased.

Speed of Water through Valves,—If areas through valves and water passages are sufficient to give a velocity of \$20 ft. per min. or less, they are ample. The water should be carefully guided and not too abruptly deflected. (F. W. Dean. Eng. Ners. Aug. 10, 1863.)

Boiler-feed Pumps.—Practice has shown that 100 ft. of piston speed per minute is the limit if excessive wear and tear is to be excellent.

per minute is the limit, if excessive wear and tear is to be avoided.

The velocity of water through the suction-pipe must not exceed 200 ft. per minute, else the resistance of the suction is too great.

The approximate size of suction-pipe, where the length does not exceed

25 ft. and there are not more than two elbows, may be found as follows: 7/10 of the diameter of the cylinder multiplied by 1/100 of the piston speed in feet. For duplex pumps of small size, a pipe one size larger is usually In feet. For duplex pumps of small size, a pipe one size maps is a small employed. The velocity of flow in the discharge-pipe should not exceed 500 ft, per minute. The volume of discharge and length of pipe vary so greatly in different installations that where the water is to be forced more than 50 ft, the size of discharge-pipe should be calculated for the particular conditions, allowing no greater velocity than 500 ft, per minute. The size of discharge minute is calculated in single-ordinate number from \$50 to 400 ft, per discharge-pipe is calculated in single-cylinder pumps from 250 to 400 ft. per minute. Greater velocity is permitted in the larger pipes.

In determining the proper size of pump for a steam-boiler, allowances must be made for a supply of water sufficient to cover all the demands of engines, steam-heating, etc., up to the capacity of generator, and should not be calculated simply according to the requirements of the engine. In practice engines use all the way from 12 up to 50, or more, pounds of steam per H.P. per hour when being worked up to capacity. When an engine is overloaded or underloaded more water per H.P. will be required than when operating at its rated capacity. The average run of horizontal tubular boilers will evaporate from 2 to 3 lbs. of water per sq. ft. of heating-surface per hour, but may be driven up to 6 lbs. if the grate-surface is too large or the draught too great for economical working.

the draught too great for economical working.

Pump-Valves.—A. F. Nagle (Trans. A. S. M. E., x. 521) gives a number of designs with dimensions of double-beat or Cornish valves used in large pumping-engines, with a discussion of the theory of their proportions. The following is a summary of the proportions of the valves described.

## SUMMARY OF VALVE PROPORTIONS

SUMMARY OF VALVE PROPORTIONS.									
Location of Engine.	Diam. of Valve in inches.	Weight in Water per square inch of Inside Un- balanced Area, in lbs.	Ratio of Seat- area to Inside Un- balanced Arca.	Pressure upon Seat per sq. in., in lbs.	Action.				
Providence high-service engine	12	1 lb. reduced to .66 lb.	16%	377 lbs.	Good				
Providence Cornish- engine St. Louis Water Wks.	16 16	1.28 1.86	12 67	680 250	Good Some noise				
Milwaukee " "	7	.40	88	120	Some noise at high speed.				
Chicago " "	25 15	1.41 1.31	75 85	151 140	Noisy				
wood seats Chicago Water Wks.	15 8	1.16 .96	94 75	132 151	: 4				

Mr. Nagle says: There is one feature in which the Cornish valves are necessarily defective, namely the lift must always be quite large, unless great power is sacrificed to reduce it. It is undeniable that a small lift is preferable to a great one, and hence it naturally leads to the substitution of numerous small valves for one or several large ones. To what extreme reduction of size this view might safely lead must be left to the judgment of the engineer for the particular case in hand, but certainly, theoretically, we must adopt small valves. Mr. Corliss at one time carried the theory so far as to make them only 1½ inches in diameter, but from 3 to 4 inches is the more common practice tow. A small valve presents proportionately a larger surface of discharge with the same lift than a larger valve, so that whatever the total area of valve-seat opening, its full contents can be discharged with less lift through numerous small valves than with one large

Henry R. Worthington was the first to use numerous small rubber valves in preference to the larger metal valves. These valves work well under all the conditions of a city pumping-engine. A volute spring is generally used to limit the rise of the valve.

In the Leavitt high-duty sewerage-engine at Boston (Am. Machinist, May 31, 1884), the valves are of rubber, 34-inch thick, the opening in valve-seat being 13½ × 4½ inches. The valves have iron face and back-plates, and form their own hinges.

## CENTRIFUGAL PUMPS.

Relation of Height of Lift to Velocity.—The height of lift depends only on the tangential velocity of the circumference, every tangential velocity giving a constant height of lift—sometimes termed "head"—whether the pump is small or large. The quantity of water discharged is in proportion to the area of the discharging orifices at the circumference, or in proportion to the square of the diameter, when the breadth is kept the same, R. H. Buel (App. Cyc. Mech., ii, 66) gives the following:

proportion to the square of the diameter, when the breadth is kept the same, R. H. Buel (App. Cyc. Mech., ii, 606) gives the following:
Let Q represent the quantity of water, in cubic feet, to be pumped per minute, h the height of suction in feet, h' the height of discharge in feet, and the diameter of suction-pipe, equal to the diameter of discharge-pipe, in

feet; then, according to Fink,  $d = .036 \sqrt{\frac{Q}{\sqrt{2g(h+h')}}}$ , g being the accel-

eration due to gravity.

If the suction takes place on one side of the wheel, the inside diameter of the wheel is equal to 1.2d, and the outside to 2.4d. If the suction takes place at both sides of the wheel, the inside diameter of the wheel is equal to 0.85d, and the outside to 1.7d. Then the suction-pipe will have two branches, the area of each equal to half the area of d. The suction-pipe should be as short as possible, to prevent air from entering the pump. The tangential velocity of the outer edge of wheel for the delivery Q is equal to 1.25  $\sqrt{2g(h+h')}$  feet per second.

The arms are six in number, constructed as follows: Divide the central angle of 60°, which incloses the outer edges of the two arms, into any number of equal parts by dividing the radii, and divide the breadth of the wheel in the same manner by drawing concentric circles. The intersections of the several radii with the corresponding circles give points of the arm.

In experiments with Appold's pump, a velocity of circumference of 500 ft. per min. raised the water 1 ft. high, and maintained it at that level without discharging any; and double the velocity raised the water to four times the height, as the centrifugal force was proportionate to the square of the velocity; consequently,

500 ft. per min. raised the water 1 ft. without discharge.

The greatest height to which the water had been raised without discharge, in the experiments with the 1-ft, pump, was 67.7 ft., with a velocity of 4183 ft. per min., being rather less than the calculated height, owing probably to leakage with the greater pressure. A velocity of 1128 ft, per min. raised the water 5½ ft. without any discharge, and the maximum effect from the power employed in raising to the same height 5½ ft. was obtained at the velocity of 1678 ft. per min., giving a discharge of 1400 gals, per min. from the 1-ft, pump. The additional velocity required to effect a discharge of 1400 gals, per min. through a 1-ft. pump working at a dead level without any height of lift, is 550 ft. per min. Consequently, adding this number in each case to the velocity given above, at which no discharge takes place, the following velocities are obtained for the maximum effect to be produced in each case:

Or, in general terms, the velocity in feet per minute for the circumference of the pump to be driven, to raise the water to a certain height, is equal to  $550+500\ V$  height of lift in feet.

Lawrence Centrifugal Pumps, Class B-For Lifts from

20 10 00 20											
	Size of	Pipes.	Economical Capacity,	Total Capacity,	Horse-power per Ft. Lift,						
	Suction.	Dis- charge.	in gallons per min.	in gallons per min.	for smaller quantity.						
No. 11/2	2 in.	1½ in.	20 to 50	150	.024						
" 2	21/4 31/4 41/2 6	2 3	60 to 80	300	.035						
" 3	31/2		80 to 160	650	.055						
	41/2	4	160 to 350	1,250	.075						
" 5	6	5	330 to 600	1,850	.175						
" 6	6 8	6	500 to 900	2,600	.22						
" 8		4 5 6 8	1,100 to 2,000	4,750	.45						
" 10	10	10	1,600 to 3,000	7.500	.62						
" 12	12	12	2,000 to 3,000	10,000	1.00						
" 14	14	14	3,000 to 5,000	14,000	1.25						
" 15	15	15	3,500 to 7,000	16,000	1.40						
" 18	18	18	6,000 to 11,000	22,000	9 40						

Table of Diameters and Width of Pulleys, Width of Belts, and Number of Revolutions per Minute Necessary to raise Minimum Quantity of Water to Different Heights with Different Sizes of Pumps of Class B.

Size.	ameter Pulley.	sh of np.	th of	num ntity ater.	Height in Feet and Revolutions per Minute.								er	of up.
Siz	Diam of Pu	Width or Pump.	Width Belt.	Minim Quant of Wa	6	8	10	12	16	20	25	30	35	No. of Pump.
Ins.	Ins.	Ins.	Ins.											
11/2	5	5	3	40	465	515	560	605	680	745	820	885	945	11/2
2	5	5	4	60	425	475	515	560	625	680	750	810	870	2
2 3 4 5 6 8	71/2 71/2	7	6	80	390	435	475	510	575	630	695	750	800	3
4	71/2	7	7	160	365	405	445	475	585	590	645	700	745	4
5	12	11	8 9	330	320	355	390	415	470	520	570	610	750	5
6	14	11		500	285	315	345	370	415	460	500	540		6
8	16	12	10	1100	215	240	260	280	310	340	375	410		8
10	18	12	10	1600	170	190	210	225	250	275	300	325	350	
12	22	14	12	2000	150	165	185	195		240	265	285	310	12
14	24	14	12	3000	135	150	165	175	195	215	240	295	275	
15	28	15	14	3500	125	145	155	165	190	210	230	245	360	
18	28	16	14	6000	110	120	130	135	160	175	190	255	220	18

Efficiencies of Centrifugal and Reciprocating Pumps.-W. O. Webber (Trans. A. S. M. E., vii. 598) gives diagrams showing the relative efficiencies of centrifugal and reciprocating pumps, from which the following figures are taken for the different lifts stated: Lift, feet:

10 15 20 25 30 35 40 50 60 80 100 120 160 200 280 Efficiency reciprocating pump:

.30 .45 .55 .61 .66 .68 .71 .75 .77 .82 .85 .87 .90 .89 .88 .85

Efficiency centrifugal pump: .50 .56 .64 .68 .69 .68 .66 .62 .58 .50 .40 ...

The term efficiency here used indicates the value of W. H. P. + I. H. P. or horse-power of the water raised divided by the indicated horse-power of the steam-engine, and does not therefore show the full efficiency of the pump, but that of the combined pump and engine. It is, however, a very simple way of showing the relative values of different kinds of pumping-engines

way of showing the relative values of different kinds of pumping-engines having their motive power forming a part of the plant.

The highest value of this term, given by Mr. Webber, is .9164 for a lift of 170 ft., and 3615 gals, per min. This was obtained in a test of the Leavitt pumping engine at Lawrence, Mass., July 24, 1879.

With reciprocating pumps, for higher lifts than 170 ft., the curve of efficiencies falls, and from 200 to 300 ft. lift the average value seem; about .84. Below 170 ft. the curve also falls reversely and slowly, until at about 90 ft. its descent becomes more rapid, and at 35 ft. .727 appears the best recorded performance. There are not any very satisfactory records below this lift, but some figures are given for the yearly coal consumption and total number of gallons pumped by engines in Holland under a 16-ft. lift, from which an efficiency of .44 has been deduced.

With centrifugal pumps, the lift at which the maximum efficiency is ob-

With centrifugal pumps, the lift at which the maximum efficiency is obtained is approximately 17 ft. At lifts from 12 to 18 ft. some makers of large experience claim now to obtain from 65% to 70% of useful effect, but

The drainage claim in the best done at a public test under 14.7 ft. head.

The drainage-pumps constructed some years ago for the Haarlem Lake were designed to lift 70 tons per min. 15 ft., and they weighed about 150 tons. Centrifugal pumps for the same work weigh only 5 tons. The weighed about 67 a centrifugal pump and engine to lift 10,000 gals. per min. 35 ft. high is

The pumps placed by Gwynne at the Ferrara Marshes, Northern Italy, in 1865, are, it is believed, capable of handling more water than other set of pumping-engines in existence. The work performed by these pumps is the lifting of 2000 tons per min.—over 600,000,000 gals. per 24 hours—on a mean lift of about 10 ft. (maximum of 12.5 ft.). (See Engineering, 1876.)

The efficiency of centrifugal pumps seems to increase as the size of pump

pump 64% efficiency.

## Tests of Centrifugal Pumps.

W. O. Webber, Trans. A. S. M. E., ix. 237.

Maker.	An- drews.	An- drews.	An- drews.	Heald & Sisco.	Heald & Sisco.	Heald & Sisco.	Berlin. Schwartz- kopff.			
Size	934" 26" 191.9 1513.12 12.25 4.69 10.09	No. 9. 918" 934" 26" 195.5 2023.82 12.62 6.47 12.2 53.0	200.5 2499.33	12.33 5.22	No. 10. 10" 12" 30.5" 202.7 2044.9 12.58 6.51 10.74 60.74	No. 10. 10" 12" 30.5" 213.7 2371.67 13.0 7.81 14.02 55.72	No. 9. 914'' 10.3'' 20.5'' 500 1944.8 16.46 11 73.1			

Vanes of Centrifugal Pumps.—For forms of pump vanes, see paper by W. O. Webber, Trans. A. S. M. E., ix. 228, and discussion thereon by Profs. Thurston, Wood, and others.

The Centrifugal Pump used as a Suction Dredge,—The Andrews centrifugal pump was used by Gen. Gillmore, U. S. A., in 1871, in deepening the channel over the bar at the mouth of the St. John's River, Florida. The pump was a No. 9, with suction and discharge pipes each 9 inches diam. It was driven at 300 revolutions per minute by belt from an engine developing 36 useful horse-power.

Although 200 revolutions of the pump disk per minute will easily raise 3000 gallons of clear water 12 ft. high, through a straight vertical 9-inch pipe, 300 revolutions were required to raise 2500 gallons of sand and water 11 ft. high, through two inclined suction-pipes having two turns each, dis-

charged through a pipe having one turn.

The proportion of sand that can be pumped depends greatly upon its specific gravity and fineness. The calcareous and argillaceous sands flow more freely than the silicious, and fine sands are less liable to choke the pipe than those that are coarse. When working at high speed, 5% to 55% of sand can be raised through a straight vertical pipe, giving for every 10 cubic yards of material discharged 5 to 51/g cubic yards of compact sand. With the appliances used on the St. John's bar, the proportion of sand seldom exceeded 45%, generally ranging from 30% to 35% when working under the most favorable conditions.

In pumping 2500 gallons, or 12.6 cubic yards of sand and water per minute, there would therefore be obtained from 3.7 to 4.3 cubic yards of sand. During the early stages of the work, before the teeth under the drag had been properly arranged to aid the flow of sand into the pipes, the yield was considerably below this average. (From catalogue of Jos. Edwards & Co.,

Mfrs. of the Andrews Pump, New York.)

## DUTY TRIALS OF PUMPING-ENGINES.

A committee of the A. S. M. E. (Trans., xii. 530) reported in 1891 on a standard method of conducting duty trials. Instead of the old unit of duty of foot-pounds of work per 100 lbs. of coal used, the committee recommend a new unit, foot-pounds of work per million heat-units furnished by the boiler. The variations in quality of coal make the old standard unit as a basis of duty ratings. The new unit is the precise equivalent of 100 lbs. of coal in cases where each pound of coal imparts 10,000 heat-units to the water in the boiler, or where the evaporation is  $10,000 \div 965.7 = 10355$  lbs. of water from and at 212° per pound of fuel. This evaporative result is readily obtained from all grades of Cumberland bituminous coal, used in horizontal return tubular boilers, and, in many cases, from the best grades of anthracite coal.

The committee also recommend that the work done be determined by plunger displacement, after making a test for leakage, instead of by measurement of flow by weirs or other apparatus, but advise the use of such apparatus when practicable for obtaining additional data. The following extracts are taken from the report. When important tests are to be made the complete report should be consulted.

The necessary data having been obtained, the duty of an engine, and other quantities relating to its performance, may be computed by the use of the

following formulæ:

2. Percentage of leakage =  $\frac{C \times 144}{A \times L \times N} \times 100$  (per cent).

3. Capacity = number of gallons of water discharged in 24 hours

$$=\frac{A\times L\times N\times 7.4805\times 24}{D\times 144}=\frac{A\times L\times N\times 1.24675}{D} \text{ (gallons)}.$$

4. Percentage of total frictions.

$$= \begin{bmatrix} \text{I.H.P.} - \frac{A(P \pm p + s) \times L \times N}{D \times 60 \times 33,000} \\ \text{I.H.P.} \end{bmatrix} \times 100$$

$$= \begin{bmatrix} 1 - \frac{A(P \pm p + s) \times L \times N}{As \times M \text{ E.P.} \times Ls \times N_s} \end{bmatrix} \times 100 \text{ (per cent)};$$

or, in the usual case, where the length of the stroke and number of strokes of the plunger are the same as that of the steam-piston, this last formula becomes:

Percentage of total frictions =  $\left[1 - \frac{A(P \pm p + s)}{A_0 \times M + P}\right] \times 100$  (per cent).

In these formulæ the letters refer to the following quantities:

A = Area, in square inches, of pump plunger or piston, corrected for area of piston rod or rods;

P = Pressure, in pounds per square inch, indicated by the gauge on the

force main:

p = Pressure, in pounds per square inch, corresponding to indication of the vacuum-gauge on suction main (or pressure gauge, if the suction-pipe is under a head). The indication of the vacuum-gauge, in inches of mercury, may be converted into pounds by dividing it by

s = Pressure, in pounds per square inch, corresponding to distance between the centres of the two gauges. The computation for this pressure is made by multiplying the distance, expressed in feet, by the weight of one cubic foot of water at the temperature of the pump-well, and dividing the product by 144;

L = Average length of stroke of pump-plunger, in feet;  $N = \text{Total number of single strokes of pump-plunger made during the trial;} A_s = Area of steam-cylinder, in square inches, corrected for area of piston-rod. The quantity <math>A_s \times M.E.P_s$ , in an engine having more than one cylinder, is the sum of the various quantities relating to the respections. tive cylinders;

L<sub>8</sub> = Average length of stroke of steam-piston, in feet;  $N_8$  = Total number of single strokes of steam-piston during trial; M.E.P. = Average mean effective pressure, in pounds per square inch, measured from the indicator-diagrams taken from the steam-cylin-

I.H.P. = Indicated horse-power developed by the steam-cylinder; C = Total number of cubic feet of water which leaked by the pump-plunger during the trial, estimated from the results of the leakage test;

D = Duration of trial in hours;

 $H\!=\!$  Total number of heat-units (B. T. U.) consumed by engine = weight of water supplied to boiler by main feed-pump  $\times$  total heat of steam of boiler pressure reckoned from temperature of main feed-water + weight of water supplied by jacket-pump  $\times$  total heat of steam of boiler-pressure reckoned from temperature of jacket-water + weight of any other water supplied  $\times$  total heat of steam reckoned from its temperature of supply. The total heat of the steam is corrected for the moisture or superheat which the steam may contain. No allowance is made for water added to the feed water, which is derived from any source, except the engine or some accessory of the engine. Heat added to the water by the use of a flue-heater at the boiler is not to be deducted. Should heat be abstracted from the flue by means of a steam reheater connected with the intermediate receiver of the engine, this heat must be included in the total quantity

supplied by the boiler.

Leakage Test of Pump.—The leakage of an inside plunger (the only type which requires testing) is most satisfactorily determined by making the test with the cylinder-head removed. A wide board or plank may be temporarily bolted to the lower part of the end of the cylinder, so as to hold back the water in the manner of a dam, and an opening made in the temporary head thus provided for the reception of an overflow-pipe. The plunger is blocked at some intermediate point in the stroke (or, if this posipumper is noticed at some intermediate point in the stroke (or, if this posi-tion is not practicable, at the end of the stroke), and the water from the force main is admitted at full pressure behind it. The leakage escapes through the overflow-pipe, and it is collected in barrels and measured. The test should be made, if possible, with the plunger in various positions. In the case of a pump so planned that it is difficult to remove the cylinder-head, it may be desirable to take the leakage from one of the openings

which are provided for the inspection of the suction-valves, the head being

allowed to remain in place.

It is assumed that there is a practical absence of valve leakage. Examination for such leakage should be made, and if it occurs, and it is found to be due to disordered valves, it should be remedied before making the plunger test. Leakage of the discharge valves will be shown by water passing down into the empty cylinder at either end when they are under pressure. age of the suction-valves will be shown by the disappearance of water which covers them.

If valve leakage is found which cannot be remedied the quantity of water thus lost should also be tested. One method is to measure the amount of water required to maintain a certain pressure in the pump cylinder when this is introduced through a p pe temporarily erected, no water being allowed to enter through the discharge valves of the pump.

Table of Data and Results. - In order that uniformity may be secured, it is suggested that the data and results, worked out in accordance with the standard method, be tabulated in the manner indicated in the following scheme :

#### DUTY TRIAL OF ENGINE.

#### DIMENSIONS.

1. Number of steam-cylinders
2. Diameter of steam-cylinders
4. Nominal stroke of steam-pistons ft.
5. Number of water-plungers
6. Diameter of plungers
7. Diameter of piston-rods of water-cylinders
9. Net area of steam-pistons sq. ins.
10. Net area of plungers
11. Average length of stroke of steam-pistons during trial ft.
12. Average length of stroke of plungers during trial ft. (Give also complete description of plant.)
(Give also complete description of plants.)

TEMPERATURES.	
13. Temperature of water in pump-well	degs.
14. Temperature of water supplied to boiler by main feed-pump	degs.
15 Tomposeture of water applied to beiler from various other	

#### FEED-WATER

FEED-WATER.
Weight of water supplied to boiler by main feed-pump
PRESSURES.
19. Boiler pressure indicated by gauge
MISCELLANEOUS DATA.
25. Duration of trial hrs.  26. Total number of single strokes during trial.  27. Percentage of moisture in steam supplied to engine, or number of degrees of superheating.  30. Total leakage of pump during trial, determined from results of
leakage test lbs.  29. Mean effective pressure, measured from diagrams taken from steam-cylinders M.E.P.
PRINCIPAL RESULTS.
30. Duty ft. lbs. 31. Percentage of leakage \$
32. Capacity gals. 33. Percentage of total friction gals.
ADDITIONAL RESULTS.
34. Number of double strokes of steam-piston per minute 35. Indicated horse-power developed by the various steam-cylinders I.H.P. 36. Feed-water consumed by the plant per hour
per hour
per minuteB.T.U.  40. Steam accounted for by indicator at cut-off and release in the various steam-cylinderslbs.  41. Proportion which steam accounted for by indicator bears to
the feed-water consumption
42. Number of double strokes of pump per minute. 43. Mean effective pressure, measured from pump diagrams M.E.P. 44. Indicated horse-power exerted in pump-cylinders I.H.P. 45. Work done (or duty) per 100 lbs, of coal ft, lbs.
SAMPLE DIAGRAM TAKEN FROM STEAM-CYLINDERS.

(Also, if possible, full measurement of the diagrams, embracing pressures at the initial point, cut off, release, and compression; also back pressure, and the proportions of the stroke completed at the various points noted.)

SAMPLE DIAGRAM TAKEN FROM PUMP-CYLINDERS.

These are not necessary to the main object, but it is desirable to give them.

DATA AND RESULTS OF BOILER TEST.

(In accordance with the scheme recommended by the Boiler-test Committee of the Society.)

#### VACUUM PUMPS-AIR-LIFT PUMP.

The Pulsometer.—In the pulsometer the water is raised by suction into the pump-chamber by the condensation of steam within it, and is then forced into the delivery-pipe by the pressure of a new quantity of steam on the surface of the water. Two chambers are used which work alternately, one raising while the other is discharging.

Test of a Pulsometer.—A test of a pulsometer is described by De Volson Wood in Trans. A. S. M. E. xiii. It had a 3½-inch suction-pipe, stood 40 in.

high, and weighed 695 lbs.

The steam-pipe was 1 inch in diameter. A throttle was placed about 2 feet

from the pump, and pressure gauges placed on both sides of the throttle, and a mercury well and thermometer placed beyond the throttle. The wire drawing due to throttling caused superheating.

The pounds of steam used were computed from the increase of the tem

perature of the water in passing through the pump.

Pounds of steam × loss of heat = lbs, of water sucked in × increase of temp.

The loss of heat in a pound of steam is the total heat in a pound of saturated steam as found from "steam tables" for the given pressure, plus the

The loss of neat in a pound of steam is the total neat in a pound of saturated steam as found from "steam tables" for the given pressure, plus the heat of superheating, minus the temperature of the discharged water; or

Pounds of steam =  $\frac{\text{lbs. water} \times \text{increase of temp.}}{H - 0.48t - T.}$ 

The results for the four tests are given in the following table:

Data and Results.	Number of Test.				
	1	2	3	4	
Strokes per minute	71 114 19 270.4 3.1 1617 404,786 75.15 4.47 29.90 12.26 42.16 32.8	60 110 30 277 3.4 931 186.362 80.6 5.5 54.05 12.26 66.31 57.80	57 127 43.8 309.0 17.4 1518 228,425 76.3 7.49 54.05 19.67 73.72 66.6	64 104.3 26.1 270.1 1.4 1019.9 248.053 70.25 4.55 29.90 19.67 49.57 41.60	
Coeff. of friction of plant $(h) \div (H)$ Efficiency of pulsometer	0.777 0.012	0.877 0.0155	0.911 0.0126	0.839	
Effic, of plant exclusive of boiler Effic, of plant if that of boiler be 0.7	0.0093 0.0065	0.0136 0.0095		0.0116	
Duty, if 1 lb. evaporates 10 lbs. water					

Of the two tests having the highest lift (54.05 ft.), that was more efficient which had the smaller saction (12.26 ft.), and this was also the most efficient of the four tests. But, on the other hand, the other two tests having the same lift (29.9 ft.), that was the more efficient which had the greater suction (19.67), so that no law in this regard was established. The pressures used, 19, 30, 43.8, 26.1, follow the order of magnitude of the total heads, but are not proportional thereto. No attempt was made to determine what pressure would give the best efficiency for any particular head. The pressure used was intrusted to a practical runner, and he judged that when the pump was running regularly and well, the pressure then existing was the proper one. It is peculiar that, in the first test, a pressure of 19 lbs. of steam should produce a greater number of strokes and pump over 50% more water than 26.1 lbs., the lift being the same, as in the fourth experiment.

duce a greater number of strokes and pump over 50g more water than 26.1 lbs., the lift being the same, as in the fourth experiment.

Class, E. Emery in discussion of Prof. Wood's paper says, referring to tests made by himself and others at the Centennial Exhibition in 1876 (see Report of Judges, Group xx.), says that a vacuum-pump tested by him in Experiment of the same part of

and 140 millions.

A very high record of test of a pulsometer is given in  $Eng^ig$ , Nov. 24, 1893, p. 639, viz.: Height of suction 11.27 ft.; total height of lift, 102.6 ft.; horizontal length of delivery-pipe, 118 ft.; quantity delivered per hour, 26,138 British gallons. Weight of steam used per H. P. per hour, 92.76 lbs.; work

done per pound of steam 21,345 foot-pounds, equal to a duty of 21,345,000 foot-pounds per 100 lbs. of coal, if 10 lbs of steam were generated per

pound of coal

The Jet-pump. This machine works by means of the tendency of a stream or jet of fluid to drive or carry contiguous particles of fluid along with it. The water-jet pump, in its present form, was invented by Projames Thomson, and first described in 1832. In some experiments on a small scale as to the efficiency of the jet-pump, the greatest efficiency was found to take place when the depth from which the water was drawn by the suction-pipe was about nine tenths of the height from which the water fell to form the jet; the flow up the suction-pipe being in that case about one fifth of that of the jet, and the efficiency, consequently,  $9/10 \times 1/5 = 0.18$ . This is but a low efficiency; but it is probable that it may be increased by improvements in proportions of the machine. (Rankine, S. E.)

The Injector when used as a pump has a very low efficiency. (See

Injectors, under Steam-boilers.)

Air-lift Pump.—The air-lift pump consists of a vertical water-pipe with its lower end submerged in a well, and a smaller pipe delivering air into it at the bottom. The rising column in the pipe consists of air mingled with water, the air being in bubbles of various sizes, and is therefore lighter than a column of water of the same height; consequently the water in the pipe is raised above the level of the surrounding water. This method of raising water was proposed as early as 1797, by In Josecher, of Freiberg, and was mentioned by Collon in lectures in Paris in 1876, but its first practical application probably was by Werner Siemens in Berlin in 1885. Dr. J. G. Pohle experimented on the principle in California in 1886, and U. S. patents on apparatus involving it were granted to Pohle and Hill in the same year. A paper describing tests of the air-lift pump made by Randall, Browne and

Behr was read before the Technical Society of the Pacific Coast in Feb. 1890. The diameter of the pump-column was 3 in., of the air-pipe 0.9 in, and of the air-discharge nozzale % in. The air-pipe had four sharp bends and a

length of 35 ft. plus the depth of submersion.

The water was pumped from a closed pipe-well (55 ft. deep and 10 in. in The efficiency of the pump was based on the least work theoretically required to compress the air and deliver it to the receiver. If the efficiency of the compressor be taken at 70%, the efficiency of the pump and compressor together would be 70% of the efficiency found for the pump alone.

For a given submersion (h) and lift (H), the ratio of the two being kept within reasonable limits, (H) being not much greater than (h), the efficiency was greatest when the pressure in the receiver did not greatly exceed the head due to the submersion. The smaller the ratio H 
ightharpoonup h, the higher was

the efficiency.

The pump, as erected, showed the following efficiencies: For  $H \div h = 0.5$  1.0 1.5

25% Efficiency = 50% 40% 30%

The fact that there are absolutely no moving parts makes the pump especially fitted for handling dirty or gritty water, sewage, mine water, and acid or alkali solutions in chemical or metallurgical works,

In Newark, N. J., pumps of this type are at work having a total capacity of 1,000,000 gallons daily, lifting water from three 8-in. artesian wells. Newark Chemical Works use an air-lift pump to raise sulphuric acid of 1.72° gravity. The Colorado Central Consolidated Mining Co., in one of its mines

at Georgetown, Colo., lifts water in one case 250 ft., using a series of lifts. For a full account of the theory of the pump, and details of the tests above referred to, see Eng'g News, June 8, 1893.

#### THE HYDRAULIC RAM.

**Efficiency.**—The hydraulic ram is used where a considerable flow of water with a moderate fall is available, to raise a small portion of that flow to a height exceeding that of the fall. The following are rules given by Eytelwein as the results of his experiments (from Rankine): Let Q be the whole supply of water in cubic feet per second, of which q is

lifted to the height h above the pond, and Q-q runs to waste at the depth H below the pond; L, the length of the supply-pipe, from the pond to the waste-clack; D, its diameter in feet; then

 $D = \sqrt{(1.63Q)}$ ;  $L = H + h + \frac{h}{H} \times 2$  feet;

Efficiency, 
$$\frac{qh}{(Q-q)H}=1.12-0.2\sqrt{\frac{h}{H}}$$
 when  $\frac{h}{H}$  does not exceed 20,

or

$$1 \div \left(1 + \frac{h}{10H}\right)$$
 nearly, when  $\frac{h}{H}$  does not exceed 12.

D'Aubisson gives 
$$\frac{qh}{QH} = 1.42 - .28 \sqrt{\frac{h}{H}}.$$

Clark, using five sixths of the values given by D'Aubisson's formula, gives: Ratio of lift to fall. . . . 4 6 8 10 12 14 16 18 20 22 24 26 Efficiency per cent. . . . . 72 61 52 44 37 31 25 19 14 9 4 0

highest efficiency.

The efficiency, 74.9, the highest realized, was obtained when the clack-valve travelled a distance equal to 60% of its full stroke, the full travel being 15/16 of one inch.

Quantity of Water Delivered by the Hydraulic Ram. (Chadwick Lead Works.)—From 80 to 100 feet conveyance, one seventh of supply from spring can be discharged at an elevation five times as high as the fall to supply the ram; or, one fourteenth can be raised and discharged say ten times as high as the fall applied.

Water can be conveyed by a ram 3000 feet, and elevated 200 feet. The

drive-pipe is from 25 to 50 feet long.

The following table gives the capacity of several sizes of rams, the dimensions of the pipes to be used, and the size of the spring or brook to which they are adapted:

	0	Caliber of Pipes.		Weight of Pipe (Lead), if Wrought Iron, then of Ordinary Weight.			
Size of Ram.	Quantity of Water Furnished per Min. by the Spring or Brook to which the Ram is Adapted.	Drive.	Discharge.	Drive-pipe for head or fall not over 10 ft.	Discharge- pipe for not over 50 ft. rise.	Discharge- pipe for over 50 ft. and not ex- ceeding 100 ft. in height.	
No. 2 " 3 " 4 " 5 " 6 " 7	Gals. per min.  34 to 2  11/2 " 4  3 " 7  6 " 14  12 " 25  20 " 40  25 " 75	inch.  34 1 11/4 2 21/2 21/2 4	inch. 3/8 1/2 1/2 3/4 1 11/4 2	per foot. 2 lbs. 3 " 5 " 8 " 13 " 13 " 21 "	per foot. 10 ozs. 12 " 12 " 1 lb. 4 " 2 " 3 " 7 "	per foot. 1 lb. 1 " 4 ozs. 1 " 4 ozs. 2 " 4 ozs. 3 " 4 " 8 "	

### HYDRAULIC-PRESSURE TRANSMISSION.

Water under high pressure (700 to 2000 lbs. per square inch and upwards) affords a very satisfactory method of transmitting power to a distance, especially for the movement of heavy loads at small velocities, as by cranes and elevators. The system consists usually of one or more pumps capable of developing the required pressure; accumulators, which are vertical cylinders with heavily-weighted plungers passing through stuffing-boxes in the upper end, by which a quantity of water may be accumulated at the pressure to which the plunger is weighted; the distributing-pipes; and the presses, cranes, or other machinery to be operated.

The earliest important use of hydraulic pressure probably was in the Bramah hydraulic press, patented in 1796. Sir W. G. Armstrong in 1846 was one of the pioneers in the adaptation of the hydraulic system to cranes. The use of the accumulator by Armstrong led to the extended use of hydraulic machinery. Recent developments and applications of the system are largely due to Raiph Tweddell, of London, and Sir Joseph Whitworth. Sir Henry Bessemer, in his patent of May 13, 1856, No. 1292, first suggested the use of hydraulic pressure for compressing steel ingots while in the fluid state.

The Gross Amount of Energy of the water under pressure stored in the accumulator, measured in foot-pounds, is its volume in cubic feet X its pressure in pounds per square foot. The horse-power of a given quantity  $\frac{144pQ}{}=$  .2618pQ, in which Q is the quantity flowing steadily flowing is H.P. =

in cubic feet per second and p the pressure in pounds per square inch.

The loss of energy due to velocity of flow in the pipe is calculated as follows (R. G. Blaine, Eng'g, May 22 and June 5, 1891): According to D'Arcy, every pound of water loses  $\frac{\lambda 4L}{D}$  times its kinetic energy, orenergy due to its velocity in passing along a straight pipe L feet

in length and D feet diameter, where  $\lambda$  is a variable coefficient. For clean cast-iron pipes it may be taken as  $\lambda = .005 \left(1 + \frac{1}{12D}\right)$ , or for diameter in

inches = d. d =1/6

 $\lambda = .015$ .01 .0075 .00667 .00625 .006 .00583 .00571 .00563 .00556 .0055 .00542 The loss of energy per minute is  $60 \times 62.36Q \times \frac{\lambda 4L}{D} \frac{v^2}{2g}$ , and the horse-

power wasted in the pipe is  $W = \frac{.6363\lambda L(H.P.)^3}{.6363\lambda L(H.P.)^3}$ , in which  $\lambda$  varies with the  $p^3D^5$ diameter as above. p = pressure at entrance in pounds per square inch.

Values of .6363\(\lambda\) for different diameters of pipe in inches are:

Efficiency of Hydraulic Apparatus.—The useful effect of a direct hydraulic plunger or ram is usually taken at 93%. The following is given as the efficiency of a ram with chain-and-pulley multiplying gear properly proportioned and well lubricated: Multiplying.... 2 to 1 4 to 1 6 to 1 8 to 1 10 to 1 12 to 1 14 to 1 16 to 1 Efficiency %.... 80 59 54 50 With large sheaves, small steel pins, and wire rope for multiplying gear

the efficiency has been found as high as 66% for a multiplication of 20 to 1. Henry Adams gives the following formula for effective pressure in cranes

and hoists: P = accumulator pressure in pounds per square inch;

m = ratio of multiplying power;

E = effective pressure in pounds per square inch, including all allowances for friction:

E = P(.84 - .02m).

J. E. Tuit (Eng'g, June 15, 1888) describes some experiments on the friction of hydraulic jacks from 3½ to 1355-inch diameter, fitted with cupped leather packings. The friction loss varied from 5.8% to 18.8% according to the condition of the leather, the distribution of the load on the ram, etc. The friction increased considerably with eccentric loads. With hemp packing a plunger, 14 inch diameter, showed a friction loss of from 11.4% to 3.4%, the load being central, and from 15.0% to 7.6% with eccentric load, the percentage of loss decreasing in both cases with increase of load.

Thickness of Hydraulic Cylinders. - From a table used by Sir W. G. Armstrong we take the following, for cast-iron cylinders, for an interior pressure of 1000 lbs. per square inch:

Diam. of cylinder, inches. 2 4 6 8 10 12 16 20 24 Thickness, inches. . . . . . . 0.832 1.146 1.552 1.875 2.222 2.578 3.19 3.69 4.11 10

For any other pressure multiply by the ratio of that pressure to 1000. These figures correspond nearly to the formula t = 0.175d + 0.48, in which t =thickness and d =diameter in inches, up to 16 inches diameter, but for 20 inches diameter the addition 0.48 is reduced to 0.19 and at 24 inches it disappears. For formulæ for thick cylinders see page 287, ante.

disappears. For ionities for thick cylinders see page 28% of the Cast iron should not be used for pressures exceeding 2000 lbs, per square inch. For higher pressures steel castings or forged steel should be used. For working pressures of 750 lbs, per square inch the test pressure should be 2500 lbs, per square inch, and for 1500 lbs, the test pressure should not be less than 3500 lbs.

Speed of Hoisting by Hydraulic Pressure.—The maximum allowable speed for warehouse cranes is 6 feet per second; for platform cranes 4 feet per second; for passenger and wagon hoists, heavy loads, : feet per second. The maximum speed under any circumstances should never exceed 10 feet per second.

The Speed of Water Through Valves should never be greater

The Speed of Water Through Pipes.—Experiments on water at 1600 lbs. pressure per sequare inch flowing into a flanging-machine ram, 20-inch diameter, through a ½-inch pipe contracted at one point to ½-inch gave a velocity of 14 feet per second in the pipe, and 456 feet at the reduced section. Through a ½-inch pipe reduced to ½-inch at one point the velocity of 12 feet per second in per reduced to 5-inch at one point the velocity of 12 feet per second in 13 feet per second in 15 fe

1/2-inch pipe without contraction the velocity was 355 feet per second. For many of the above notes the author is indebted to Mr. John Platt,

consulting engineer, of New York

High-pressure Hydraulic Presses in Iron-works are described by R. M. Daelen, of Germany, in Trans. A. I. M. E. 1892. The following distinct arrangements used in different systems of high-pressure hydraulic work are discussed and illustrated:

Steam-pump, with fly-wheel and accumulator.
 Steam pump, without fly-wheel and with accumulator.
 Steam-pump, without fly-wheel and without accumulator.

In these three systems the valve-motion of the working press is operated in the high-pressure column. This is avoided in the following:

4. Single-acting steam-intensifier without accumulator.

5. Steam-pump with fly-wheel, without accumulator and with pipe-circuit. 6. Steam-pump with fly-wheel, without accumulator and without pipe-

circuit.

The disadvantages of accumulators are thus stated: The weighted plungers which formerly served in most cases as accumulators, cause violent shocks in the pipe-line when changes take place in the movement of the water, so that in many places, in order to avoid bursting from this cause, the pipes are made exclusively of forged and bored steel. The seats and cones of the metallic valves are cut by the water (at high speed), and in such cases only the most careful maintenance can prevent great losses of power

Hydraulic Power in London.-The general principle involved is pumping water into mains laid in the streets, from which service-pipes are carried into the houses to work lifts or three-cylinder motors when rotatory power is required. In some cases a small Pelton wheel has been tried, working under a pressure of over 700 lbs. on the square inch. Over 55

miles of hydraulic mains are at present laid (1892).

The reservoir of power consists of capacious accumulators, loaded to a pressure of 800 lbs, per square inch, thus producing the same effect as if large supply-tanks were placed at 1700 feet above the street-level. The water is taken from the Thames or from wells, and all sediment is removed therefrom by filtration before it reaches the main engine-pumps.

There are over 1750 machines at work, and the supply is about 6,500,000

gallons per week.

It is essential that the water used should be clean. The storage-tank extends over the whole boiler-house and coal-store. The tank is divided, and a certain amount of mud is deposited here. It then passes through the surface condenser of the engines, and it is turned into a set of filters, eight in number. The body of the filter is a cast-iron cylinder, containing a layer of granular filtering material resting upon a false bottom; under this is the distributing arrangement, affording passage for the air, and under this the real bottom of the tank. The dirty water is supplied to the filters from an overhead tank. After passing through the filters the clean effluent is pumped into the clean-water tank, from which the pumping-engines derive their supply. The cleaning of the filters, which is done at intervals of 44 hours, is effected so thoroughly in situ that the filtering material never requires to be

removed.

The engine-house contains six sets of triple-expansion engines. The cylinders are 15-inch, 22-inch, 36 inch × 24-inch. Each cylinder drives a single plunger-pump with a 5-inch ram, secured directly to the cross-head, the connecting rod being double to clear the pump. The boiler-pressure is the connecting rou being double to clear the pump. The bother-pressure 150 lbs. on the square inch. Each pump will deliver 300 gallons of water per minute under a pressure of 800 lbs, to the square inch, the engines making about 61 revolutions per minute. This is a high velocity, considering the heavy pressure; but the valves work silently and without perceptible shock. The consumption of steam is 14.1 pounds per horse per hour.

The water delivered from the main pumps passes into the accumulators. The rams are 20 inches in diameter, and have a stroke of 23 feet. They are

each loaded with 110 tons of slag, contained in a wrought-iron cylindrical box suspended from a cross-head on the top of the ram.

One of the accumulators is loaded a little more heavily than the other, so that they rise and fall successively; the more heavily loaded actuates a stop-valve on the main steam-pipe. If the engines supply more water than is wanted, the lighter of the two rams first rises as far as it can go; the other then ascends, and when it has nearly reached the top, shuts off steam and checks the supply of water automatically.

The mains in the public streets are so constructed and laid as to be per-

fectly trustworthy and free from leakage.

Every pipe and valve used throughout the system is tested to 2500 lbs. per square inch before being placed on the ground and again tested to a reduced pressure in the trenches to insure the perfect tightness of the joints, jointing material used is gutta-percha.

Jointing materiar used is guita-percua.

The average rate obtained by the company is about 3 shillings per thousand gallons. The principal use of the power is for intermittent work in cases where direct pressure can be employed, as, for instance, passenger elevators,

cranes, presses, warehouse hoists, etc.

An important use of the hydraulic power is its application to the extinguishing of fire by means of Greathead's injector hydrant. By the use of these hydrants a continuous fire-engine is available.

Hydraulic Riveting-machines.—Hydraulic riveting was intro-duced in England by Mr. R. H. Tweddell. Fixed riveters were first used about

Portable riveting-machines were introduced in 1872.

The riveting of the large steel plates in the Forth Bridge was done by small

portable machines working with a pressure of 1000 bs. per square inch. In exceptional cases 3 tons per inch was used. (Proc. Inst. M. E., May, 1882.) An application of hydraulic pressure invented by Andrew Higginson, of Liverpool, dispenses with the necessity of accumulators. It consists of a three-throw pump driven by sharting or worked by steam, and depending upon the work accumulated in a heavy fly-wheel. The water is its passage from the pumps and back to them is in constant circulation at a very feeble pressure, requiring a minimum of power to preserve the tube of water ready for action at the desired monient, when by the use of a tap the current is stopped from going back to the pumps, and is thrown upon the piston of the tool to be set in motion. The water is now confined, and the driving-belt or steam-engine, supplemented by the momentum of the heavy fly-wheel, is employed in closing up the rivet, or bending or forging the ob-

ject subjected to its operation.

Hydraulie Forging.—In the production of heavy forgings from cast ingots of mild steel it is essential that the mass of metal should be operated on as equally as possible throughout its entire thickness. employing a steam-hammer for this purpose it has been found that the external surface of the ingot absorbs a large proportion of the sudden impact of the blow, and that a comparatively small effect only is produced on the central portions of the ingot, owing to the resistance offered by the inertia of the mass to the rapid motion of the falling hammer-a disadvantage that is entirely overcome by the slow, though powerful, compression of the hydraulic forging-press, which appears destined to supersede the steam-

hammer for the production of massive steel forgings.

In the Allen forging-press the force-pump and the large or main cylinder of the press are in direct and constant communication. There are no intermediate valves of any kind, nor has the pump any clack-valves, but it simply forces its cylinder full of water direct into the cylinder of the press, and receives the same water, as it were, back again on the return stroke. Thus, when both cylinders and the pipe connecting them are full, the large ram of the press rises and falls simultaneously with each stroke of the pump, keeping up a continuous oscillating motion, the ram, of course, travelling the shorter distance, owing to the larger capacity of the press (Journal Iron and Steel Institute, 1891. See also illustrated article in "Modern Mechanism," page 668.)

For a very complete illustrated account of the development of the hydraulic forging-press, see a paper by R. H. Tweddell in Proc. Inst. C. E., vol.

cxvii. 1893-4.

Hydraulic Forging-press.—A 2000-ton forging-press erected at the Coullet forges in Belgumin is described in Eng. and M. Jour., Nov. 25, 1893. The press is composed essentially of two parts—the press itself and the compressor. The compressor is formed of a vertical steam-cylinder and a hydraulic cylinder. The piston-rod of the former forms the piston of the The hydraulic piston discharges the water into the press proper. The distribution is made by a cylindrical balanced valve; as soon as the pressure is released the steam-piston falls automatically under the action of gravity. During its descent the steam passes to the other face of the piston

gravity. During its descent the steam passes to the other ace of the piston to reheat the cylinder, and finally escapes from the upper end.

When steam enters under the piston of the compressor-cylinder the piston rises, and its rod forces the water into the press proper. The pressure thus exerted on the piston of the latter is transmitted through a cross-head to the forging which is upon the anvil. To raise the cross-head two small single-acting steam-cylinders are used, their piston-rods being connected to the cross-head; steam acts only on the pistons of these cylinders from below. The admission of steam to the cylinders, which stand on top of the press frame, is regulated by the same lever which directs the motions of the compressor. The movement given to the dies is sufficient for all the ordinary purposes of forging.

A speed of 30 blows per minute has been attained. A double press on the

A speed of 30 nows per minute has seen attained. A dottone press of the same system, having two compressors and giving a maximum pressure of 6000 tons, has been erected in the Krupp works, at Essen.

The Alken Intensifier. (From Age, Ang. 1890)—The object of the machine is to increase the pressure obtained by the ordinary accumulator which is necessary to operate powerful hydraulic machines requiring very high pressures, without increasing the pressure carried in the accumulator and the general hydraulic system.

The Aiken Intensifier consists of one outer stationary cylinder and one inner cylinder which moves in the outer cylinder and on a fixed or stationary hollow plunger. When operated in connection with the hydraulic bloomshear the method of working is as follows: The inner cylinder having been filled with water and connected through the hollow plunger with the hydraulic cylinder of the shear, water at the ordinary accumulator-pressure is admitted into the outer cylinder, which being four times the sectional area of the plunger gives a pressure in the inner cylinder and shear cylinder connected therewith of four times the accumulator-pressure—that is, if the accumulator-pressure is accumulator-pressure is admitted into the outer pressure in the plunger pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted into the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure is admitted in the outer pressure in the outer pressure in the outer pressure in the outer cumulator-pressure is 500 lbs. per square inch the pressure in the intensifier

will be 2000 lbs, per square inch.

Hydraulic Engine driving an Air-compressor and a
Forging-hammer. (Iron Age, May 12, 1892.)—The great hammer in
Terni, near Rome, is one of the largest in existence. Its falling weight amounts to 100 tens, and the foundation belonging to it consists of a block of cast iron of 1000 tons. The stroke is 16 feet 434 inches; the diameter of the cylinder 6 feet 336 inches; diameter of piston-rod 1334 inches; total height of the hammer, 62 feet 4 inches. The power to work the hammer, as well as the two cranes of 100 and 150 tons respectively, and other auxiliary appliances belonging to it, is furnished by four air-compressors coupled together and driven directly by water-pressure engines, by means of which the air is compressed to 73.5 pounds per square inch. The cylinders of the water-pressure engines, which are provided with a bronze lining, have a 13%-inch bore. The stroke is 47% inches, with a pressure of water on the piston amounting to 2646 pounds per square inch. The compressors are bored out to 31½ inches diameter, and have 47% inch stroke. Each of the four cylinders requires a power equal to 280 horse-power. The compressed air is deFUEL.

livered into huge reservoirs, where a uniform pressure is kept up by means

of a suitable water-column.

The Hydraulic Forging Plant at Bethlehem, Pa., is described in a paper by R. W. Davenport, read before the Society of Navel Engineers and Marine Architects, 1893. It includes two hydraulic forging-presses complete, with engines and pumps, one of 1500 and one of 4500 tocapacity, together with two Whitworth hydraulic travelling forging-cranes capacity, together with two with word in dramatic travelling regarders and other necessary appliances for each press, and a complete fluid-compression plant, including a press of 7000 tons capacity and a 125 ton hydrault travelling orane for serving it (the upper and lower heads of this press weighing respectively about 135 and 120 tons).

A new forging-press has been designed by Mr. John Fritz, for the Bethlehem Works, of 14,000 tons capacity, to be run by engines and pumps of 15,000 horse-power. The plant is served by four open-hearth steel furnaces of a

united capacity of 120 tons of steel per heat.

Some References on Hydraulic Transmission,—Reuleaux's "Constructor;" "Hydraulic Motors, Turbines, and Pressure-engines," G. Bodner, London, 1889; Robinson's "Hydraulic Power and Hydraulic Machinery," London, 1885; Colyer's "Hydraulic Steam, and Hand-power Lifting and Pressing Machinery," London, 1881. See also Engineering (London), Aug. 1, 1884, p. 99; March 13, 1885, p. 262; May 22 and June 5, 1891, pp. 612, 665; Feb. 19, 1893, p. 170.

### FUEL.

Theory of Combustion of Solid Fuel. (From Rankine, somewhat altered.)-The ingredients of every kind of fuel commonly used may be thus classed: (1) Fixed or free carbon, which is left in the form of charcoal or coke after the volatile ingredients of the fuel have been distilled away. These ingredients burn either wholly in the solid state (C to Co<sub>2</sub>), or away. These ingleateness out a claim wholly in the solid state (C to  $CO_2$ ), or part in the solid state and part in the gaseous state (CO + O =  $CO_2$ ), the latter part being first dissolved by previously formed carbonic acid by the reaction  $CO_3$  + C = 2CO. Carbonic oxide, CO, is produced when the supply of air to the fire is insufficient.

(2) Hydrocarbons, such as olefiant gas, pitch, tar, naphtha, etc., all of

which must pass into the gaseous state before being burned.

If mixed on their first issuing from amongst the burning carbon with a large quantity of hot air, these inflammable gases are completely burned with a transparent blue flame, producing carbonic acid and steam. When mixed with cold air they are apt to be chilled and pass off unburned. When raised to a red heat, or thereabouts, before being mixed with a sufficient quantity of air for perfect combustion, they disengage carbon in fine powder, and pass to the condition partly of marsh gas, and partly of free hydrogen; and the higher the temperature, the greater is the proportion of carbon thus disengaged.

If the disengaged carbon is cooled below the temperature of ignition before coming in contact with oxygen, it constitutes, while floating in the gas,

smoke, and when deposited on solid bodies, soot.

But if the disengaged carbon is maintained at the temperature of ignition, and supplied with oxygen sufficient for its combustion, it burns while floating in the inflammable gas, and forms red, yellow, or white flame. The flame from fuel is the larger the more slowly its combustion is effected. The flame itself is apt to be chilled by radiation, as into the heating surface of a steam-hoiler, so that the combustion is not completed, and part of the gas and smoke pass off unburned.

(3) Oxygen or hydrogen either actually forming water, or existing in combination with the other constituents, in the proportions which form water. Such quantities of oxygen and hydrogen are to left be out of account in determining the heat generated by the combustion. If the quantity of water actually or virtually present in each pound of fuel is so great as to make its latent heat of evaporation worth considering, that heat is to be deducted

from the total heat of combustion of the fuel

(4) Nitrogen, either free or in combination with other constituents. This substance is simply inert.

(5) Sulphuret of iron, which exists in coal and is detrimental, as tending to cause spontaneous combustion.

(6) Other mineral compounds of various kinds, which are also inert, and form the ash left after complete combustion of the fuel, and also the clinker or glassy material produced by fusion of the ash, which tends to choke the grate.

Total Heat of Combustion of Fuels. (Rankine.)—The following table shows the total heat of combustion with oxygen of one pound of each of the substances named in it, in British thermal units, and also in lbs. of water evaporated from 212°. It also shows the weight of oxygen required to combine with each pound of the combustible and the weight of air necessary in order to supply that oxygen. The quantities of heat are given on the authority of MM. Favre and Sibermann.

Combustible.	Lbs.Oxy- gen per lb. Com- bustible.	Lb. Air	Total British Heat- units.	Evapora- tive Power from 212° F., lbs.
Hydrogen gas	8	36	62,032	64.2
to make carbonic oxide	11/3	6	4,400	4.55
make carbonic acid	22/3	12 15 3/7	14,500 21,344	15.0 22.1
Various liquid hydrocarbons, 1 lb.		{	from 21,700 to 19,000	from 221/2
Carbonic oxide, as much as is made by the imperfect combustion of 1 lb of carbon, viz., 21/3 lbs	11/6	6	10,000	10.45

The imperfect combustion of carbon, making carbonic oxide, produces tess than one third of the heat which is yielded by the complete combustion. The total heat of combustion of any compound of hydrogen and carbon is nearly the sum of the quantities of heat which the constituents would produce separately by their combustion. (Marsh-gas is an exception.) In computing the total heat of combustion of compounds containing oxygen as well as hydrogen and carbon, the following principle is to be observed: When hydrogen and oxygy weight one part of mydrogen to eight of containing the combustions of the combustion of the combu of oxygen), these constituents have no effect on the total heat of combustion. If hydrogen exists in a greater proportion, only the surplus of hydrogen above that which is required by the oxygen is to be taken into account. The following is a general formula (Dulong's) for the total heat of combustion of any compound of carbon, hydrogen, and oxygen:

Let C. H. and O be the fractions of one pound of the compound, which

consists respectively of carbon, hydrogen, and oxygen, the remainder being nitrogen, ash, and other impurities. Let h be the total heat of combustion of one pound of the compound in British thermal units. Then

$$h = 14,500 \left\{ C + 4.28 \left( H - \frac{O}{8} \right) \right\}$$

The following table shows the composition of those compounds which are of importance, either as furnishing oxygen for combustion, as entering into the composition, or as being produced by the combustion of fuel:

Names.	Symbol of	Proportions	Chemical	Proportions
	Chemical	of Element	Equivalent	of Elements
	Composition.	by Weight.	by Weight.	by Volume.
Air. Water. Ammonia. Carbonic oxide. Carbonic acid. Oleflant gas. Marsh-gas or fire-damp. Sulphurous acid. Sulphuretted hydrogen. Sulphuret of carbon.	CH <sub>4</sub> SO <sub>2</sub> SH <sub>2</sub>	$\begin{array}{l} \text{N 77} + \text{O 23} \\ \text{H 2} + \text{O 16} \\ \text{H 3} + \text{N 14} \\ \text{C 12} + \text{O 16} \\ \text{C 12} + \text{O 32} \\ \text{C 12} + \text{H 2} \\ \text{C 12} + \text{H 3} \\ \text{S 32} + \text{O 32} \\ \text{S 32} + \text{H 2} \\ \text{S 64} + \text{C 12} \end{array}$	100 18 17 28 44 14 16 64 34 76	N 79 + O 21 H 2 + O H 3 + N C + O C + O 2 C + H 2 C + H 4

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Since each lb, of C requires 2% lbs. of O to burn it to CO2, and air contains 23% of O, by weight, 2% ÷ 0.23 or 11.6 lbs. of air are required to burn 1 lb. of C.

Analyses of Gases of Combustion.—The following are selected from a large number of analyses of gases from locomotive boilers, to show the range of composition under different circumstances (P. H. Dudley, Trans. A. I. M. E., iv. 250):

			_		
Test.	$CO_2$	co	0	N	
			_		
1	13.8	2.5	2.5	81.6	No smoke visible.
2	11.5		6.	82.5	Old fire, escaping gas white, engine working hard.
3	8.5		8.	83.	Fresh fire, much black gas, " " "
4	2.3		17.2		Old fire, damper closed, engine standing still,
1 2 3 4 5 6	5.7		14.7		" smoke white, engine working hard.
6	8.4			82.	New fire, engine not working hard.
7	12	1	4.4	82.6	Smoke black, engine not working hard.
8	3.4			76.8	
9	6			81.5	

In analyses on the Cleveland and Pittsburgh road, in every instance when the smoke was the blackest, there was found the greatest percentage of unconsumed oxygen in the product, showing that something besides the mere presence of oxygen is required to effect the combustion of the volatile carbon of fuels.

J. C. Hoadley (Trans. A. S. M. E., vi. 749) found as the mean of a great number of analyses of flue gases from a boiler using anthracite coal:

CO<sub>c</sub>, 13.10; CO, 0.30; O, 11.94; N, 74.66.

The loss of heat due to burning C to CO instead of to CO<sub>2</sub> was 2.13%. The surplus oxygen averaged 113.3% of the O required for the C of the fuel, the

average for different weeks ranging from 88.6% to 137%.

Analyses made to determine the CO produced by excessively rapid firing gave results from 2.5% to 4.8% to 2.0 and 5.1% to 8.0% CO<sub>2</sub>; the ratio of C in the CO to total carbon burned being from 43.8% to 48.55%, and the number of pounds of air supplied to the furnace per pound of coal being from 32 to 19.3 lbs. The loss due to burning C to CO was from 37.84% to 30.86% of the

full power of the coal.

Temperature of the Fire. (Rankine, S. E., p. 283.)-By tempera comperature of the Fire, (Kankine, S. E., p. 283.)—By temperature of the fire is meant the temperature of the products of combustion at the instant that the combustion is complete. The elevation of that temperature above the temperature at which the air and the fuel are supplied to the furnace may be computed by dividing the total heat of combustion of one lb. of tuel by the weight and by the mean specific heat of the whole products of combustion, and of the air employed for their dilution under constant pressure. The specific heat under constant pressure of these products is about as follows:

Carbonic-acid gas, 0.217; steam, 0.475; nitrogen (probably), 0.245; &r, 0.238; asles, probably about 0.200. Using these data, the following results are obtained for pure earbon and for olefiant gas burned, respectively, first, in just sufficient air, theoretically, for their combustion, and, second, when an equal amount of air is supplied in addition for dilution.

Fuel.	Products	undiluted.	Products diluted.	
r uer.	Carbon.	Olefiant Gas.	Carbon.	Olefiant Gas.
Total heat of combustion, per lb Wt. of products of combustion, lbs		21,300 16.43	14,500 25	21,300 31.86
Their mean specific heat	3.08	0.257 4.22	0.238 5.94	0.248 7.9
Elevation of temperature, F	4580°	5050°	2440°	2710°

[The above calculations are made on the assumption that the specific heats of the gases are constant, but they probably increase with the increase of temperature (see Specific Heat), in which case the temperatures would be less than those above given. The temperature would be further reduced by the heat rendered latent by the conversion into steam of any

reduced by the hear rendered latent by the conversion line scalar of any water present in the fuel.] **Rise of Temperature in Combustion of Gases.** (Eng'g, March 12 and April 2, 1886.)—It is found that the temperatures obtained by experiment fall short of those obtained by calculation. Three theories have been given to account for this: 1. The cooling effect of the sides of the containing vessel; 2. The retardation of the evolution of heat caused by dissociation; 3. The increase of the specific heat of the gases at very high temperatures. The calculated temperatures are obtainable only very light temperatures. The calculated temperatures are obtained to on the condition that the gases shall combine instantaneously and simultaneously throughout their whole mass. This condition is practically impossible in experiments. The gases formed at the beginning of an explosion dilute the remaining combustible gases and tend to retard or check the combustion of the remainder.

### CLASSIFICATION OF SOLID FUELS.

Gruner classifies solid fuels as follows (Fra'a and M'a Jour, July 1874):

0.1.4	(	3
Name of Fuel.	Ratio $\frac{O}{H}$ or $O + N *$ .	Proportion of Coke or Charcoal yielded by the Dry Pure Fuel.
Pure cellulose	H 8 7 6 @ 5	0.28 @ 0.30 .30 @ .35 .35 @ .40
Lignite,† or brown coal	4 @ 1 1 @ 0.75	.40 @ .50 .50 @ .90

The hituminous coals he divides into five classes as below:

	Elementary Composition.			Proportion of Coke	Nature and
C.	Н.	0.	or O+N*.	yielded by Dis- tilla- tion.	Appearance of Coke.
75@80	5.5@4.5	19.5@15	4@3	0.50@.60	Pulveru- lent.
80@85	5.8@5	14.2@10	3@2	.60@.68	Melted, but friable.
84@80	5 @4.5	11 @5.5	2@1	.68@.74	Melted;
88@91	5.5@4.5	6.5@5.5	1	.74@.82	Melted; very com- pact.
90@98	4.5@4	5.5@3	1	.82@.90	Pulveru-
	C 75@80 - 80@85 - 84@80	Composit  C. H.  75@80 5.5@4.5  80@85 5.8@5  84@80 5 @4.5	Composition.  C. H. O.  75@80 5.5@4.5 19.5@15  80@85 5.8@5 14.2@10  84@80 5 @4.5 11 @5.5  88@91 5.5@4.5 6.5@5.5	$\begin{array}{ c c c c c c }\hline \text{Composition.} & \text{Ratio} \frac{O}{H} \\\hline C. & H. & O. \\\hline 75@80 5.5@4.5 19.5@15 & 4@3 \\ 80@85 5.8@5 & 14.2@10 & 3@2 \\\hline 84@80 5 @4.5 & 11 @5.5 & 2@1 \\\hline 88@91 5.5@4.5 & 6.5@5.5 & 1 \\\hline \end{array}$	Composition.   Ratio   O   Coke   C

<sup>\*</sup> The nitrogen rarely exceeds 1 per cent of the weight of the fuel,

<sup>+</sup> Not including bituminous lightes, which resemble petroleums.

Rankine gives the following: The extreme differences in the chemical composition and properties of different kinds of coal are very great. The composition and properties of different Rinds of coal are very great. The proportion of free carbon ranges from 30 to 39 per cent; that of hydrocarbons of various kinds from 5 to 58 per cent; that of water, or oxygen and hydrogen in the proportions which form water, from an inappreciably small quantity to 27 per cent; that of ash, from 1½ to 26 per cent.

The numerous varieties of coal may be divided into principal classes as follows: 1, anthractic coal; 2, semi-bitumicous coal; 3, bituminous coal; 4, long flaming or cannel coal; 5, lignite or brown coal.

### Diminution of H and O in Series from Wood to Anthracite.

(Groves and Thorp's Chemical Technology, vol. i., Fuels, p. 58.)

Substance.	Carbon.	Hydrogen.	Oxygen.
Woody fibre	52.65	5.25	42.10
Peat from Vulcaire	59.57	5.96	34.47
Lignite from Cologne	66.04	5.27	28.69
Earthy brown coal	73.18	5.88	21.14
Coal from Belestat, secondary	75.06	5.84	19.10
Coal from Rive de Gier	89.29	5.05	5.66
Anthracite, Mayenne, transition formation	91.58	3.96	4.46

### Progressive Change from Wood to Graphite.

(J. S. Newberry in Johnson's Cyclopedia.)

	Wood.	Loss.	Lig- nite.	Loss	Bitumi- nous coal.	Loss.	Anthra-	Loss.	Graph- ite.	
Carbon	49.1	18.65	30.45	12.35	18.10	3.57	14.53	1.42	13.11	
Hydrogen	6.3	3,25	3.05	1.85	1.20	0.93	0.27	0.14	0.13	
Oxygen	44.6	24.40	20.20	18.13	2.07	1.32	0.65	0.65	0.00	
	100.0	46.30	53.70	32.33	21.37	5.82	15.45	2.21	13.24	

Classification of Coals, as Anthracite, Bituminous, etc.— Prof. Persifer Frazer (Trans. A. I. M. E., vi, 430) proposes a classification of coals according to their "fuel ratio," that is, the ratio the fixed carbon bears to the volatile hydrocarbon.

In arranging coals under this classification, the accidental impurities, such as sulphur, earthy matter, and moisture, are disregarded, and the fuel constituents alone are considered.

	Carbon	Fixed	Volatile
	Ratio.	Carbon.	Hydrocarbon.
I. Hard dry anthracite.	100 to 12	100. to 92.31%	0. to 7.69%
II. Semi-anthracite III. Semi-bituminous	12 to 8	92.31 to 88.89	7.69 to 11.11
	8 to 5	88.89 to 83.33	11.11 to 16.67
IV. Bituminous	5 to 0	83.33 to 0.	16.67 to 100

It appears to the author that the above classification does not draw the line at the proper point between the semi-bituminous and the bituminous coals, viz., at a ratio of C + V.H.C. = 5, or fixed carbon 83.3%, volatile hydrocarbon 16.6%, since it would throw many of the steam coals of Clearfield and Somerset counties, Penn., and the Cumberland, Md., and Pocahontas, Va., coals, which are practically of one class, and properly rated as semi-bituminous coals, into the bituminous class. The dividing line between the semi-anthracite and semi-bituminous coals, C + V.H.C. = 3, would place several coals known as semi-anthracite in the semi-bituminous class. The following is proposed by the author as a better classification:

Ca	arbon Ratio.	Fixed Carbon.	Vol. H.C.
I. Hard dry anthracite	100 to 12	100 to 92.31%	0 to 7.69%
II. Semi-anthracite	12 to 7	92.31 to 87.5	7.69 to 12.5
III. Semi-bituminous	7 to 3	87.5 to 75	12.5 to 25
IV. Bituminous	3 to 0	75 to 0	25 to 100

Rhode Island Graphitic Anthracite.—A peculiar graphite is found at Cranston, near Providence, R. L. It resembles both graphite and anthracite coal, and has about the following composition (A. E. Hunt, Trans. A. I. M. E., xvii, 678): Graphitic carbon, 78%; volatile matter, 2.60%; silica, 15.06%; phosphorus, -045%. It burns with extreme difficulty.

#### ANALYSES OF COALS.

Composition of Pennsylvania Anthracites. (Trans. A. I. M. E., xiv., 706.)—Samples weighing 100 to 200 lbs. were collected from lots of 100 to 200 tons as shipped to market, and reduced by proper methods to laboratory samples. Thirty-three samples were analyzed by McCreath, giving results as follows. They show the mean character of the coal of the more important coal-beds in the Northern field in the vicinity of Wilkesbarre, in the Eastern Middle (Lehigh) field in the vicinity of Hazleton, in the Western

Middle field in the vicinity of Shenandoah, and in the Southern field between Manch Chunk and Tamaqua.

Name of Bed.	Name of Field.	Water.	Volatile Matter.	Fixed Carbon.	Ash.	Sulphur.	Vol. Matter. Per cent of total com- bustible.	Ratio, C+V.H.C.
Wharton Mammoth Primrose Mammoth Primrose F Buck Mtn Seven Foot Manmoth Mammoth B. Coal Bed	E. Middle W. Middle W. Middle Southern W. Middle W. Middle Southern	3.71 4.12 3.54 3.16 3.01 3.04 3.41 8.09 3.42 1.30	3.08 3.08 3.72 3.72 4.13 3.95 3.98 4.28 4.38 8.10	86.40 86.38 81.59 81.14 87.98 82.66 80.87 83.81 83.27 83.34	6.22 5.92 10.65 11.08 4.38 9.88 11.23 8.18 8.20 6.23	.58 .49 .50 .90 .50 .46 .51 .64 .78 1.03	3.44 3.45 4.36 4.38 4.48 4.56 4.69 4.85 5.00 8.86	28.07 27.99 21.93 21.83 21.83 20.93 20.32 19.62 19.00 10.29

The above analyses were made of coals of all sizes (mixed). When coal is screened into sizes for shipment the purity of the different sizes as regards ash varies greatly. Samples from one mine gave results as follows:

		seneu	Analyses.		
Name of	Through	Over	Fixed		
Coal.	inches.	inches.	Carbon.	Ash.	
Egg		1.75	88.49	5.66	
Stove	1.75	1.25	83.67	10.17	
Chestnut		.75	80.72	12.67	
Pea	.75	.50	79 05	14.66	
Buckwheat	.50	.25	76.92	16.62	

# Bernice Basin, Pa., Coals.

		voi. H.C.		Ash.	Sulphur,
Domino Dasin Cullings	and (0.96	3.56	82.52	3.27	0.24
Dernice Dasin, Funivan	and to	to	to	to	to
Bernice Basin, Fullivan Lycoming Cos.; range of	1.97	8.56	89.39	9.34	1.04

This coal is on the dividing-line between the anthracites and semi-anthracites, and is similar to the coal of the Lykens Valley district. More recent analyses (Trans. A. I. M. E., xiv. 721) give :

Vol. H.C. Fixed Carb. Water. Ash. Sulphur. Working seam..... 0 65 60 ft. below seam.... 3.67 9.40 83.69 5.34  $0.91 \\ 0.59$ 8 97

The first is a semi-anthracite, the second a semi-bituminous.

Space Occupied by Anthracite Coal. (J. C. I. W., vol. iii.)—The cubic contents of 2240 lbs. of hard Lehigh coal is a little over 36 feet; an average Schuylkill W. A., 37 to 38 feet; Shamokin, 38 to 39 feet; Lorberry, nearly 41.

According to measurements made with Wilkesbarre anthracite coal from the Wyoming Valley, it requires 32.2 cu. ft. of lump, 33.9 cu. ft. broken, 34.5 cu. ft. egg, 34.8 cu. ft. of sept. ft. of chestuit, and 36,7 cu. ft. of pea, to make one ton of coal of 2240 lbs.; while it requires 28.8 cu. ft. of lump, 30.3 cu. ft. of broken, 30.8 cu. ft. of egg, 31.1 cu. ft. of stove, 31.9 cu. ft. of chestnut, and 32.8 cu. ft. of pea, to make one ton of 2000 lbs. Composition of Anthracite and Semi-bituminous Coals.

(Trans. A. I. M. E., vi. 430.)—Hard dry anthracites, 16 analyses by Rogers, show a range from 94.10 to 82.47 fixed carbon, 1.40 to 9.53 volatile matter, and 4.50 to 8.00 ash, water, and impurities. Of the fuel constituents alone, the fixed carbon ranges from 98.53 to 89.63, and the volatile matter from 1.47 to 10.37, the corresponding carbon ratios, or C + Vol. H.C. being from 67.02 to 8.64.

Semi-anthracites.-12 analyses by Rogers show a range of from 90,23 to 74.55 fixed carbon, 7.07 to 13.75 volatile matter, and 2.20 to 12.10 water, ash, and impurities. Excluding the ash, etc., the range of fixed carbon is 92.75 to 84.42, and the volatile combustible 7.27 to 15.58, the corresponding carbon

ratio being from 12.75 to 5.41.

FUEL.

Semi-bituminous Coals, -10 analyses of Penna, and Maryland coals give fixed carbon 68.41 to 84.80, volatile matter 11.2 to 17.28, and ash, water, and impurities 4 to 13.99. The percentage of the fuel constituents is fixed carbon 79.84 to 88.80, volatile combustible 11.20 to 20.16, and the carbon ratio 11.41 to 3.96.

### American Semi-bituminous and Bituminous Coals. (Selected chiefly from various papers in Trans. A. I. M. E.)

	Moist- ure.	Vol. Hydro- arbon.	Fixed Carbon	Ash.	Sul- phur.
Penna. Semi-bituminous ;					
	( .79	13.84	78.46	6.00	.91
Broad Top, extremes of 5	7.78	17.38	76.14	4.81	.88
	1.27	14.33	77.77	6.63	0.66
Somerset Co., extremes of 5	11.89	18.51	65,90	10.62	3.08
Blair Co., average of 5	1.07	26.72	60.77	9.45	2.20
Blair Co., average of 5 Cambria Co., average of 7, 1 lower bed, B.	0.74	21,21	68.94	7.51	
lower bed, B.	0.74	21.21	00.94	7.51	1.98
Cambria Co., 1,	1.14	17.18	73.42	6.58	1.41
upper bed, C.	1.14				1.41
Cambria Co., South Fork, 1	2722	15.51	78.60	5.84	
Centre Co., 1	0.60	22.60	68.71	5.40	2.69
Clearfield Co., average of 9,	0.70	23.94	69.28	4.62	1.42
Clearfield Co., average of 8, 1 lower bed, D.	0.81	21.10	74.08	3.36	0.42
lower bed, D.	(0.41	20.09	66.69	2.65	0.43
Clearfield Co., range of 17 anal	to to	to.03	to	to	to
Clear near co., range of 11 anai	1.94	25.19	74.02	7.65	1.79
Bituminous:	(2.02	W0.10	11.00	*.00	2.10
Jefferson Co., average of 26	1.21	32.53	60.99	3.76	1.00
Clarion Co., average of 7	1.97	38.60	54.15	4.10	1.19
Armstrong Co., 1	1.18	42.55	49.69	4.58	2.00
Connellsville Coal	1.26	30.10	59.61	8.23	.78
Coke from Conn'ville (Standard)	.49	0.01	87.46	11.32	.69
Youghiogheny Coal	1.03	36.49	59.05	2.61	.81
Pittsburgh, Ocean Mine	.28	39.09	57.33	3.30	

The percentage of volatile matter in the Kittaning lower bed B and the Freeport lower bed D increases with great uniformity from east to west: thus:

			Jolatile Matter.	Fixed Carbon.
Clearfield Co.	bed	D	20.09 to 25.19	68.73 to 74.76
66 66			22.56 to 26.13	64.37 to 69.63
Clarion Co.,	6.6	B	35,70 to 42,55	47.51 to 55.44
44	66		37 15 to 40 80	51 30 to 56 36

Connellsville Coal and Coke. (Trans. A. I. M. E., xiii. 332.)— The Connellsville coal-field, in the southwestern part of Pennsylvania, is a strip about 3 miles wide and 60 miles in length. The mine workings are confined to the Pittsburgh seam, which here has its best development as to size, and its quality best adapted to coke-making. It generally affords from 7 to 8 feet of coal.

The following analyses by T. T. Morrell show about its range of composition .

	Moisture.	Vol. Mat.	Fixed C.	Ash.	Sulphur.	Phosph's.
Herold Mine	1.26	28.83	60.79	8.44		.013
Kintz Mine	0.79	31.91	56.46	9.52	1.32	.02

In comparing the composition of coals across the Appalachian field, in the western section of Pennsylvania, it will be noted that the Connellsville variety occupies a peculiar position between the rather dry semi-biruminous coals eastward of it and the fat biruminous coals flanking it on the west. Beneath the Connellsville or Pittsburgh coal-bed occurs an interval of from 400 to 600 feet of "barren measures," separating it from the lower than the connells of the coal was accounted to the connel of the coal was accounted to the coal

productive coal measures of Western Pennsylvania. The following tables

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show the great similarity in composition in the coals of these upper and lower coal-measures in the same geographical belt or basin.

#### Analyses from the Upper Coal-measures (Penna.) in a Westward Order.

Localities.	Moisture.	Vol. Mat.	Fixed Carb.	Ash.	Sulphur,
Anthracite	1.35	3.45	89.06	5.81	0.30
Cumberland, Md	0.89	15.52	74.28	9.29	0.71
Salisbury, Pa	1.66	22.35	68.77	5.96	1.24
Connellsville, Pa		31.38	60.30	7.24	1.09
Greensburg, Pa		33.50	61.34	3.28	0.86
Irwin's Pa		37.66	54.44	5.86	0.64

#### Analyses from the Lower Coal-measures in a Westward Order.

Localities.	Moisture.	Vol. Mat.	Fixed Carb.	Ash.	Sulphur.
Anthracite	1.35	8.45	89.06	5.81	0.30
Broad Top	0.77	18.18	73.34	6.69	1.02
Bennington	1.40	27.23	61.84	6.93	2.60
Johnstown	1.18	16.54	74.46	5.96	1.86
Blairsville	0.92	24.36	62.22	7.69	4.92
Armstrong Co	0.96	38.20	52.03	5.14	3.66

Pennsylvania and Ohio Bituminous Coals, Variation in Character of Coals of the same Beds in different Districts,—From 50 analyses in the reports of the Pennsylvania Geological Survey, the following are selected. They are divided into different groups, and the extreme analysis in each group is given, ash and other impurities being neglected, and the percentage in 100 of combustible matter being alone considered.

	No. of Analyses	Fixed Carbon	Vol. H. C.	Carbon Ratio.
Waynesburg coal-bed, upper bench  Jefferson township, Greene Co  Hopewell township, Washington Co	5	59.72 53.22	40.28 46.78	1.48
Waynesburg coal-bed, lower bench Morgan township, Greene Co Pleasant Valley, Washington Co Sewickley coal-bed.	9	60.69 54.31	39.31 45.69	1.54 1.19
Whitely Creek, Greene Co. Gray's Bank Creek, Greene Co. Pittsburgh coal-bed:		64.39 60.35	35.61 39.65	1.80 1.52
Upper bench, Washington Co  Lower bench, """	5	\$60.87 \$59.11 \$63.54	39.13 40.89 36.46	1.65 1.20 1.74
Main bench, Greene Cc	3	50.97 61.80 54.33	49.03 38.20 45.67	1.04 1.61 1.19
Frick & Co., Washington Co., average Lower bench, Greene Co Somerset Co., semi-bituminous (showing decrease of vol. mat. to the eastward).	1	66.44 57.88 {79.73 {75.47	33.56 42.17 20.27 24.53	1.98 1.37 3.93 3.07
Beaver Co., Pa Diehl's Bank, Georgetown. Bryan's Bank, Georgetown.	•	40.68 62.57	59.32 37.43	0.68 1.66
Оню. Pittsburgh coal-bed in Ohio: Jefferson Co., Ohio		61.45	38.55	1.59
Belmont Co., Ohio		63.46 66.14 63.46	36.54 33.86 36.54	1.73 1.95 1.78
Pomeroy Co., Ohio		64.93 60.92 62.33	35.07 39.08 37.67	1.85 1.55 1.65

### Analyses of Southern and Western Coals,

	THE CAME TO A	u vi csec	III Coul	E3.0	
	Moisture.	Vol. Mat.	Fixed C.	Ash.	Sul- phur.
OHIO. Hocking Valley MARYLAND.	{ 5.00 7.40		53.15 60.45	9.05 2.95	0.44 0.93
CumberlandVirginia.		19.13 15.47	72.70 73.51	6.40 9.09	0.78 0.70
South of James River, 23 analyses, range Average of 23 North of James River, eastern	to 2.46	27.28 38.60 32.24 18.60	46.70 67.83 58.89 71.00	2.00 15.76 7.72 10.00	0.58 2.89 1.45
outerop, Carbonite or Natural Coke	1.79		59.98 79.93	14.28 8.86	
Western outcrop, 11 analyses, range	1.00	21.33 30.50	81.61 54.97 70.80	2.24 3.35 22.60	0.23
Average of 11  Pocahontas Flat-top* (Castner & Curran's Circular) WEST VIRGINIA (New River.)	{ 0.52 0.62		63.75 74.20 75.22	10.06 1.38 5.68	0.52 0.28
Quinnimont,† 3 analyses	from 0.76 to 0.94	18.19	75.89 79.40 69.00	1.11 4.92 1.07	0.23 0.30
Nuttalburgh † Virginia and Kentucky.	1.35	25.35	70.67	2.10	0.08
Big Stone Gap Field, ‡ 9 anal- yses, range	from 0.80 to 2.01	31.44 36.27	54.80 63.50	1.73 8.25	0.56 1.72
Kentucky. Pulaski Co., 3 analyses, range Muhlenberg Co., 4 analyses,	1 10 1.34	39.44	60.85 52.48 58.80	1.23 5.52 3.40	0.40 1.00 0.79
range Kentucky Cannel Coals,§ 5 an- alyses, range	1 to 7.06	38.70 40.20 63.30	53.70 59.80 coke 33.70 coke		3.16 0.96 1.32
TENNESSEE. Scott Co., Range of several. T		41.29	46.61 61.66	16.94	3.37
Roane Co., Rockwood.  Hamilton Co., Melville.  Marion Co., Etna  Sewanee Co., Tracy City.	2.74 94	26.50 28.72	60.11 67.08 63.94 61.00	11.52 3.68 11.40	1.49 91 1.19
Kelly Co., Whiteside			74.20	7.80 2.70	
Dade Co	1.20	23.05	60.50	15.16	0.84
Warren Field: Jefferson Co., Birmingham "Black Creek	.12	26.11	48.30 71.64	3.21 2.03	2.72
Tuscaloosa Co Cahaba Field, (Helena Vein. Bibb Co) Coke Vein	2.00	32.90	54.64 53.08 66.58	5.45 11.34 1.09	1.33 .68 .04
* Analyses of Pocahontas Coa	al by John F	attinson, I	F.C.S., 1889	):	37-1

Vol. C. H. 0. N. S. Ash. Water. Coke. Mat. 0.66 78.8 Lumps... 86.51 4.44 4.95 0.61 1.54 1.29 21.2 0.66 1.40 Small 83.13 4.29 5.33 0.564.63 79.8 20.2

Calorific value, by Thomson's Calorimeter: Lumps = 15.4 lbs. of water evaporated from and at 212; small = 14.7 lbs.
† These coals are coked in beehvie ovens, and yield from 63% to 64% of coke, † This field covers about 120 square miles in Virginia, and about 30 square

miles in Kentucky.

§ The principal use of the cannel coals is for enriching illuminating-gas.

Volatile matter including moisture.

¶ Single analyses from Morgan, Rhea, Anderson, and Roane counties fall within this range.

Ultimate.

Alabama Coals. (W. B. Phillips, Eng. & M. J., June 3, 1893.)

Proximate.

Name of Seam.	Location.	Vol. and Combust. Matter.	Fixed Carbon.	Carbon.	Hydrogen.	Oxygen.	Nitrogen.	Sulphur.	Ash.	Moisture.
	Helena Pratt mines	34.30 33.45				11.92 7.51	$\frac{1.07}{1.73}$		3.3	50 1.70 00 1.35
Brookwood	Brookwood	27.80				1.60	0.40	1.65	11.9	0 1.60
	Blocton	34.80				11.12	1.48	1.44	2.0	35 1.95
Underwood	Don't win in			70.82			1.31			25 1.80 35 1.15
	Pratt mines Brookwood			73.96		0.90	1.62	1 15	2.	20 1.00
mindale	Blue Creek			72.68			1.39			30 1.50
	Coalburg	32.55		74.59			1.31			90 0.82
Cahaba							1		1	
Field		30.15	52.90	60.37	10.70	9.00	1.26	1.72	16.	80 0.65
				_				-		
			Mois	ture.	Vol. M	at. Fi	xed (	c.	Ash.	Şul-
										phur.
Eagle Mine	TEXAS.			3.54	30.8	4	50.69		14.93	
Sabinas Fiel	d, Vein I			.91	20.0		62.7		15.35	
66 66	" II		1 1	.37	16.4		68.18	3	13.02	
46 46			1	0.84	29.3		50.18	8	19.68	
	" IV		(	.45	21.6		45.73	5	29.1	3.15
	Indiana.									
	average.*			2.10	37.3		57.9		2.60	
	Lafayette	• • • • • • •	18	3.05	32.3	4	48.7	5	5.81	
	Sand Creekt		1 4	1.50		91.00			4.50	
	LLINOIS.‡		1			1			1.00	
	LLLINUIS.		8	3.22	39.4	0	43.9	5	8.43	
Streator			1 7	7.20	38.8	8	45.30	0	8.60	i
				.00	32.5		53.00		3.65	
				.78	43.7		45.3		6.15	
				3 45	34.9		44.50		12.06	
Carbondele				0.80 5.36	27.3 26.4		44.78		17.10 7.40	
Du Quoin				8.86	23.5		60.6		7.40	
Mt. Carbon				.12	24.6		66.50		2.70	
Staunton				900	57 1		06 20		10 20	

<sup>\*</sup>Indiana Block Coal (J. S. Alexander, Trans. A. I. M. E., iv. 100).—The typical block coal of the Brazil (Indiana) district differs in chemical composition but little from the coking coals of Western Pennsylvania. The physical difference, however, is quite marked; the latter has a cuboid structure made up of bituminious particles lying against each other, so that under the action of heat fusion throughout the mass readily takes place, while block coal is formed of alternate layers of rich bituminous matter and a charcoal-like substance, which is not only very slow of combustion, but so retards the transmission of heat that agglutination is prevented, and the coal burns away layer by layer, retaining its form until consumed. + Analysis by E. T. Cox: C, 72.94; H, 4.50; O, 11.77; N, 1.79; ash, 4.50;

6.27

57.11

26.30

10.32 ... ..

moisture, 4.50.

Staunton....

<sup>#</sup> The Illinois coals are extremely variable in character. The above analyess are given in D. L. Barnes's paper on "American Locomotive Practice," Trans. A. S. C. E. 1893, except the last, the Staunton coal, which is by Hunt and Clapp (Trans. A. S. M. E., v. 266). The Staunton coal is remarkable for the high percentage of volatile matter, but it is excelled in this respect by

	Moisture.	Vol. Mat.	Fixed C.	Ash. Sul- phur.
Iowa.*				
Hiteman	4.99	35.27	25.37	34.37
Keb	9.81	37.49 40.16	44.75 37.69	7.95
Flaglers	9.84 9.18	40.16	39.58	12 31
	3.10	40.46	99.90	10.02
MISSOURI.*	4.04	40.00	FO 00	
Brookfield.	4.34 9.03	40.27 37.48	50.60 46.24	4.79 7.25
Mendota	5.06	34.24	47.69	7.25
Lingo	7.33	38.29	47.24	7.14
	1.00	90.20	41.24	1.14
NEBRASKA.*	0.21	27.82	60.88	11.09
Hastings	0.21	27.82	00.88	11.09
Wyoming.*	4.0	10.0		
Cambria	4.2 2.5	40.6	41.5 37.9	13.7
Goose Creek.	$\frac{2.5}{9.7}$	37.4 40.2	46.3	
Goose Creek	13.92	36.78	42.03	7.27
Deek Creek	12.8	35.0	47.7	3.6
Sheridau	6.04	42.37	35.57	16.02
	0.01	10.01	00.01	10.00
Colorado.‡	2.8	36.3	37.1	23.8
Nowgette " "	1.7	37.95	48.6	11.6
Fl Moro	1.32	38.23	55.86	3.59
Sunshine, Colo, average.  Newcastle, " " El Moro, " " Crested Buttes, "	1.10	23.20	72.60	3.10
UTAH (Southern).				0.11
Castledale	3.43	42.81	47.81+	9.73
Cedar City	3.50	43.66	43.11+	5.95
OREGON.				
	15.45	41.55	34.95	8.05 2.53
Coos Bay	17.27	44.15	32.40	6.18 1.37
Yaquina Bay	13.03	46.20	32.60	7.10 1.07
John Day River	4.55	40.00	48.19	7.26 .60
John Day River	6.54	34.45	52.41	5.95 .65
VANCOUVER ISLAND.				
Comox Coal	1.7	27.17	68.27	2.861

the Boghead coal of Linlithgowshire, Scotland, an analysis of which by Dr. Penny is as follows: Proximate—moisture 0.84; vol. 67.95; fixed C, 9.54, ash, 21.4; Ultimate—C,63.94; H, 8.86; O, 4.70; N, 0.96; which is remarkable for the

high percentage of H.

\*The analyses of Iowa, Missouri, Nebraska, and Wyoming coals are selected from a paper on The Heating Value of Western Coals, by Wm. Forsyth, Mech. Engr. of the C., B. & Q. R. R., Engly News, Jan. 17, 1895, † Includes sulphur, which is very high. Coke from Cedar City analyzed:

Water and volatile matter, 1.42; fixed carbon, 76.70; ash, 16.61; sulphur, 5.27.

# Colorado Coals.—The Colorado coals are of extremely variable composition, ranging all the way from lignite to anthracite. G. O. Hewit Trans. A. I. M. E., xvii. 377) says: The coal seams, where unchanged by heat and flexure, carry a lignite containing from 5% to 20% of water. In the south-eastern corner of the field the same have been metamorphosed so that in four miles the same seams are an anthracite, coking, and dry coal. In the basin of Coal Creek the coals are extremely fat, and produce a hard, bright, sonorous coke. North of coal basin half a mile of development shows a gradual change from a good coking coal with patches of dry coal to a dry coal that will barely agglutinate in a beeinve oven. In another half mile the same seam is dry. In this transition area, a small cross-fault makes the coal fat for twenty or more feet on either side. The dry seams makes the coal rat for twenty or more teet on enter side. The dry seam also present wide chemical and physical changes in short distances. A soft and loosely bedded coal has in a hundred feet become compact and hard without the intervention of a fault. A couple of hundred feet has reduced the water of combination from 12% to 5%.

Western Arkanas and Indian Territory. (H. M. Chance, Trans. A. I. M. E. 1890.)—The Choctaw coal-field is a direct westward exten-

sion of the Arkansas coal-field, but its coals are not like Arkansas coals, except in the country immediately adjoining the Arkansas line.

The western Arkansas coals are dry semi-bituminous or semi-anthracitic

The western Arkansas coals are dry sent-bituminous or semi-anthracitic coals, mostly non-coking, or with quite feeble coking properties, ranging from 14% to 16% in volatile matter, the highest percentage yet found, according to Mr. Minslow's Arkansas report, being 17 655.

In the Mitchell basin, about 10 miles west from the Arkansas line, coal recently opened shows 19% volatile matter; the Mayberry coal, about 8 miles farther west, contains 23% volatile matter; and the Bryan Mine coal, about the same distance west, shows 26% volatile matter. About 30 miles farther west, the coal shows from 38% to 41½% volatile matter, which is also about the percentage in coals of the McAlester and Lehigh districts.

Western Lignites. (R. W. Raymond, Trans. A. I. M. E., vol. ii 1873)

·	C.	н.	N.	0.	s.	Mois- ture.	Ash.	Calorific Power, calories.
Monte Diabolo	59.72			15.69	3.92	8.94	5.64	5757
Weber Cañon, Utah	64.84			15.52			3.00	5912
Echo Cañon, Utah	69.84			10.99		9.17	3.40	6400
Carbon Station, Wyo	64.99			15.20	1.07	11.56	1.68	5738
							6.62	6578
Coos Bay, Oregon	56.24					13.28	4.05	4565
Alaska	55.79	3.26	0.61	19.01	0.63	16.52	4.18	4610
**	67.67	4.66	1.58	12.80	0.92	3.08	9.28	6428
Canon City, Colo	67.58			13.42	0.63	5.18	5.77	7330
Baker Co., Ore	60.72	4.30		14.42	2.08	14.68	3.80	5602

The calorific power is calculated by Dulong's formula.

$$8080C + 34462 \left(H - \frac{O}{8}\right),$$

deducting the heat required to vaporize the moisture and combined water, that is, 537 calories for each unit of water. 1 calorie = 1.8 British thermal units.

Analyses of Foreign Coals. (Selected from D. L. Barnes's paper on American Locomotive Practice, A. S. C. E., 1893.)

	Volatile Matter.	Fixed Carbon.	Λsh.	
Great Britain:				
South Wales	8.5	88.3	3.2	
46 46	6.2	92.3	1.5	
Lancashire, Eng	17.2	80.1	2.7	
Derbyshire, "	17.7	79.9	2.4	
Durham, "	15 05	86.8	1.1	Semi-bit. coking coal.
Scotland	17.1	63.1	19.8	Boghead cannel gas coal.
**	17.5	80.1	2.4	Semi-bit. steam-coal.
Staffordshire, Eng	20.4	78.6	1.0	
South America:				
Chili, Conception Bay		70.55	7.52	
" Chiroqui	24.11	38.98	36.91	
Patagonia	24.35	62 25	13.4	
Brazil	40.5	57.9	1.6	
Canada:				
Nova Scotia	26.8	60.7	12.5	
Cape Breton	26.9	67.6	5.5	
Australia				
Australian lignite	15.8	64.3	10.0	
Sydney, South Wales	14.98	82.39	2.04	
Borneo	26.5	70.3	14.2	,
Van Diemen's Land	6.16	63.4	30.45	

An analysis of Pictou, N. S., coal, in Trans. A. I. M. E., xiv. 560, is: Vol., 29.63; carbon, 56.98; ash, 13.39; and one of Sydney, Cape Breton, coal is: vol., 34.07; carbon, 61.43; ash, 4.50.

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Nixon's Navigation Weish Coal is remarkably pure, and contains not more than 3 to 4 per cent of ashes, giving 88 per cent of hard and lustrous coke. The quantity of fixed carbon it contains would classify it among the dry coals, but on account of its coke and its intensity of com-

among the dry coats, but on account of us coke and us intensity of combustion it belongs to the class of fat, or long flaming coals.

Chemical analysis gave the following results: Carbon, 90.27; hydrogen, 4,39; sulphur, 69; nitrogen, 49; oxygen (difference, 4,16.

The analysis showed the following composition of the volatile parts: Carbon, 22.53; hydrogen, 34,96; O + N + S, 4,25.

The heat of combustion was found to be, as a result of several experience. ments, 8864 calories for the unit of weight. Calculated according to its composition, the heat of combustion would be 8805 calories = 15,849 British

thermal units per pound.

This coal is generally used in trial-trips of steam-vessels in Great Britain. Sampling Coal for Analysis.—J. P. Kimball, Trans. A. I. M. E., xii. 317, says: The unsuitable sampling of a coal-seam, or the improper preparation of the sample in the laboratory, often gives rise to errors in determinations of the ash so wide in range as to vitiate the analysis for all practical purposes; every other single determination, excepting moisture, showing its relative part of the error. The determination of sulphur and ash are especially liable to error, as they are intimately associated in the

Wm. Forsyth, in his paper on The Heating Value of Western Coals (Eng'a News, Jan. 17, 1895), says: This trouble in getting a fairly average sample of anthracite coal has compelled the Reading R. R. Co., in getting their samples, to take as much as 300 lbs. for one sample, drawn direct from the chutes, as

it stands ready for shipment.

The directions for collecting samples of coal for analysis at the C., B. & Q.

laboratory are as follows:

Two samples should be taken, one marked "average," the other "select," Each sample should contain about 10 lbs., made up of lumps about the size of an orange taken from different parts of the dump or car, and so selected that they shall represent as nearly as possible, first, the average lot; second, the best coal.

An example of the difference between an "average" and a "select"

sample, taken from Mr. Forsyth's paper, is the following of an Illinois coal:

Moisture. Vol. Mat. Fixed Carbon. Ash.

Average ... 1.36 27.69 35.41 35.54

35.54

Chestnut..... \$2.75 1.25 Buckwheat..... 0.75 0.25 0.10

But when coal is reduced to an impalpable dust, a method of burning it becomes possible to which even the finest of these sizes is wholly unadapted; the coal may be blown in as dust, mixed with its proper proportion

of air, and no grate at all is then required.

Presset Fuel. (E. F. Loiseau, Trans. A. I. M. E., viii. 314.)—Pressed fuel has been made from anthracite dust by mixing the dust with ten per eent of its bulk of dry pitch, which is prepared by separating from tar at a temperature of 572° F. the volatile matter it contains. The mixture is kept heated by steam to 212°, at which temperature the pitch acquires its cementing properties, and is passed between two rollers, on the periphery of which are milled out a series of semi-oval cavities. The lumps of the mixture, about the size of an egg, drop out under the rollers on an endless belt which carries them to a screen in eight minutes, which time is sufficient to

cool the lumps, and they are then ready for delivery.

The enterprise of making the pressed fuel above described was not commercially successful, on account of the low price of other coal. In France, however, "briquettes" are regularly made of coal-dust (bituminous and

semi-bituminous).

#### RELATIVE VALUE OF STEAM COALS.

The heating value of a coal may be determined, with more or less approximation to accuracy, by three different methods.

Ist, by chemical analysis; 2d. by combustion in a coal calorimeter; 3d, by actual trial in a steam-boiler. The first two methods give what may be

called the theoretical heating value, the third gives the practical value.

The accuracy of the first two methods depends on the precision of the method of analysis or calorimetry adopted, and upon the care and skill of the operator. The results of the third method are subject to numerous sources of variation and error, and may be taken as approximately true only for the particular conditions under which the test is made. Analysis and calorimetry give with considerable accuracy the heating value which may be obtained under the conditions of perfect combustion and complete absorption of the heat produced. A boiler test gives the actual result under conditions of more or less imperfect combustion, and of numerous and va-riable wastes. It may give the highest practical heating value, if the conditions of grate bars, draft, extent of heating surface, method of firing, etc., are the best possible for the particular coal tested, and it may give results far beneath the highest if these conditions are adverse or unsuitable to the

The results of boiler tests being so extremely variable, their use for the purpose of determining the relative steaming values of different coals has frequently led to false conclusions. A notable instance is found in the record of Prof. Johnson's tests, made in 1844, the only extensive series of tests of American coals ever made. He reported the steaming value of the Lehigh Coal & Navigation Co's coal to be far the lowest of all the anthraunder which he made the test, which were entirely unsuited to that coal. He also reported a result for Pittsburgh coal which is far beneath that now obtainable in every-day practice, his low result being chiefly due to the use of an improper furnace.

In a paper entitled Proposed Apparatus for Determining the Heating Power of Different Coals (Trans. A. T. M. E., xi v. 27) the author described and illustrated an apparatus designed to test fuel on a large scale, avoiding the errors of a steam-boiler test. It consists of a fire-brick furnace enclosed in a water casing, and two cylindrical shells containing a great number of tubes, which are surrounded by cooling water and through which the gases of combustion pass while being cooled. [No steam is generated in the apparatus, but water is passed through it and allowed to escape at a temperature below 200° F. The product of the weight of the water passed through the apparatus by its increase in temperature is the measure of the heating value of the fuel.

There has been much difference of opinion concerning the value of chemical analysis as a means of approximating the heating power of coal. It was found by Scheurer-Kestner and Meunier-Dollfus, in their extensive series of tests, made in Europe in 1868, that the heating power as determined by calorimetric tests was greater than that given to chemical analysis accord-

ing to Dulong's law.

Recent tests made in Paris by M. Mahler, however, show a much closer agreement of analysis and calorimetric tests. A brief description of these tests, translated from the French, may be found in an article by the author in The Mineral Industry, vol. i. page 97.

Dulong's law may be expressed by the formula,

Heating Power in British Thermal Units =  $14,500C + 62,500 \left(H - \frac{O}{e}\right),*$ 

in which C, H, and O are respectively the percentage of carbon, hydrogen, and oxygen, each divided by 100. A study of M. Mahler's calorimetric tests shows that the maximum difference between the results of these tests and the calculated heating power by Dulong's law in any single case is only a little over 3%, and the results of 31 tests show that Dulong's formula gives an average of only 47 thermal units less than the calorimetric tests, the average total heating value being over 14,000 thermal units, a difference of less than 4/10 of 1%.

Heating Power =  $14,650C + 62,025 \left(H - \frac{(O + N) - 1}{8}\right)$ .

<sup>\*</sup> Mahler gives Dulong's formula with Berthelot's figure for the heating value of carbon, in British thermal units,

634 FUEL.

Mahler's calorimetric apparatus consists of a strong steel vessel or bomb' immersed in water, proper precaution being taken to prevent radiation. One gram of the coal to be tested is placed in a platinum boat within this bomb, oxygen gas is introduced under a pressure of 20 to 25 atmospheres, and the coal ignited explosively by an electric spark. Combustion is complete and instantaneous, the heat is radiated into the surrounding water, weighing 2000 grams, and its quantity is determined by the rise in temperature of this water, due corrections being made for the heat capacity of the apparatus itself. The accuracy of the apparatus is remarkable, duplicate tests giving results varying only about 2 parts in 1000.

The close agreement of the results of calorimetric tests when properly

The close agreement of the results of calorimetric tests when properly conducted, and of the heating power calculated from chemical analysis, indicates that either the chemical or the calorimetric method may be accepted as correct enough for all practical purposes for determining the total heating power of coal. The results obtained by either method may be taken as a standard by which the results of a boiler test are to be compared, and the difference between the total heating power, and the result of the boiler test is a measure of the inefficiency of the boiler under the con-

ditions of any particular test.

In practice with good anthracite coal, in a steam-boiler properly proportioned, and with all conditions favorable, it is possible to obtain in the steam 80% of the total heat of combustion of the coal. This result was nearly obtained in the tests at the Centennial Exhibition in 1876, in five different boilers. An efficiency of 70% to 75% may easily be obtained in regular practice. With bituminous coals it is difficult to obtain as close an approach to the theoretical maximum of economy, for the reason that some of the volatile combustible portion of the coal escapes unburned, the difficulty increasing rapidly as the content of volatile matter increases beyond 20%. With most coals of the Western States it is with difficulty that as much as 60% or 65% of the theoretical efficiency can be obtained without the use of gas-producers.

The chemical analysis heretofore referred to is the ultimate analysis, or the percentage of carbon, hydrogen, and oxygen of the dry coal. It is found, however, from a study of Mahler's tests that the proximate analysis, which gives fixed carbon, volatile matter, moisture, and ash, may be relied on as giving a measure of the heating value with a limit of error of only about 32. After deducting the moisture and ash, and calculating the fixed carbon as a percentage of the coal dry and free from ash, the author has constructed the following table:

APPROXIMATE HEATING VALUE OF COALS.

Percentage F. C. in Coal Dry and Free from Ash.	Heating Value B.T.U. per lb. Comb'le.	Equiv. Water Evap. from and at 212° per 1b. Combustible.	F. C. in Coal Dry and Free	Heating Value B.T.U. per lb. Comb'le.	Equiv. Water Evap. from and at 212° per lb. Combustible.						
100 97 94 90 87 80 72	14500 14760 15120 15480 15660 15840 15660	15.00 15.28 15.65 16.03 16.21 16.40	68 63 60 57 54 51 50	15480 15120 14580 14040 13320 12600 12240	16.03 15.65 15.09 14.53 13.79 13.04						

Below 50% the law of decrease of heating-power shown in the table apparently does not hold, as some cannel coals and lignites show much higher heating-power than would be predicted from their chemical constitution.

The use of this table may be shown as follows:

Given a coal containing moisture 2%, ash 8%, fixed carbon 61%, and volatile matter 20%, what is its probable heating value? Deducting moisture and ash we find the fixed carbon is 61/90 or 68% of the total of fixed carbon and volatile matter. One pound of the coal dry and free from ash would, by the table, have a heating value of 15/480 thermal units, but as the ash and moisture, having no heating value, are 10% of the total weight of the coal, the coal would have 90% of the table value, or 13/323 thermal units. This divided by 966, the latent heat of steam at 212° gives an equivalent evaporation per 1b, of coal of 11.42 be.

The heating value that can be obtained in practice from this coal would depend upon the efficiency of the boiler, and this largely upon the difficulty of thoroughly burning its volatile combustible matter in the boiler furnace If a boiler efficiency of 65% could be obtained, then the evaporation per lb. of

coal from and at 212° would be  $14.42 \times .65 = 9.37$  lbs.

With the best anthracite coal, in which the combustible portion is, say, 97% fixed carbon and 3% volatile matter, the highest result that can be expected in a boiler-test with all conditions favorable is 12.2 lbs. of water evaporated in a conter-test with an conditions tavorane is 12.2 be, of water evaporated from and at 212° per b. of combustible, which is 80% of 15.28 lbs. the theoretical heating-power. With the best semi-bituminous coals, such as Curberland and Pocahontals, in which the fixed carbon is 80% of the total combustible, 12.5 lbs., or 76% of the theoretical 16.4 lbs., may be obtained. For Pittsburgh coal, with a fixed carbon ratio of 08%, 11 lbs., or 60% of the theoretical 16.4 lbs., and the condition of the c retical 16.03 lbs., is about the best practically obtainable with the best boilers. With some good Ohio coals, with a fixed carbon ratio of 60%, 10 lbs., or 66% of the theoretical 15.09 lbs., has been obtained, under favorable conditions, with a fire-brick arch over the furnace. With coals mined west of Ohio, with lower carbon ratios, the boiler efficiency is not apt to be as high as 60%.

From these figures a table of probable maximum boiler-test results from coals of different fixed carbon ratios may be constructed as follows:
Fixed carbon ratio 97 80 68 60 54 50

maximum in boiler-tests: 8.3 11 10 76 Boiler efficiency, per cent..... 80 66 55 Loss, chimney radiation, imperfect combustion, etc:

20 24 31

40 45 The difference between the loss of 20% with anthracite and the greater losses with the other coals is chiefly due to imperfect combustion of the bituminous coals, the more highly volatile coals sending up the chimney the greater quantity of smoke and unburned hydrocarbon gases. It is a measure surface caused by the deposition of soot, the latter being primarily caused by the imperfection of the ordinary furnace and its unsuitability to the proper burning of bituminous coal. If in a boller-test with an ordinary furnace lower results are obtained than those in the above table, it is an indication of unfavorable conditions, such as bad firing, wrong proportions of boiler, defective draft, and the like, which are remediable. Higher results can be expected only with gas-producers, or other styles of furnace especially designed for smokeless combustion.

Kind of Furnace Adapted for Different Coals. (From the author's paper on "The Evaporative Power of Bituminous Coals," Trans. A. S. M. E., iv, 257.)—Almost any kind of a furnace will be found well adapted to burning anthracite coals and semi-bituminous coals containing adapted to forming admiracter coars and semi-forminous coars containing less than 20% of volatile matter. Probably the best furnace for burning those coals which contain between 20% and 40% volatile matter, including the Scotch, English, Welsh, Nova Scotca, and the Pittsburgh and Monongahela river coals, is a plain grate-bar furnace with a fire-brick arch thrown over it, for the purpose of keeping the combustion-chamber thoroughly hot. The best furnace for coals containing over 40% volatile matter will be a furnace snrrounded by fire-brick with a large combustion-chamber, and some special appliance for introducing very hot air to the gases distilled from the coal, or, preferably, a separate gas-producer and combustion-chamber, with facilities for heating both air and gas before they unite in the combustion-chamber. The character of furnace to be especially avoided in burning all bituminous coals containing over 20% of volatile matter is the ordinary furnace, in which the boiler is set directly above the grate bars, and in which the heating-surfaces of the boiler are directly exposed to radiation from the coal on the grate. The question of admitting air above the grate is still un-settled. The London Engineer recently said: "All our experience, extending over many years, goes to show that when the production of smoke is prevented by special devices for admitting air, either there is an increase in the consumption of first or a diminution in the production of steam. \*\* \* The best smoke-preventer yet devised is a good fireman." **Downward-draught Furnaces.**—Recent experiments show that

with bituminous coal considerable saving may be made by causing the draught to go downwards from the freshly-fired coal through the hot coal on the grate. Similar good results are also obtained by the upward draught by feeding the fresh coal under the bed of hot coal instead of on top. (See

Boilers.)

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Calorimetric Tests of American Coals.—From a number of tests of American and foreign coals, made with an oxygen calorimeter, by Geo. H. Barrus (Trans. A. S. M. E., vol. xiv. 816), the following are selected, showing the range of variation:

Percentage of Ash.		Total Heat reduced to Fuel free from Ash.
1 0.0	14,217 12,874	15,141 14,085
0.2	14,603 13,608	15,086 14,507 14,427
7.8	13,858 13,180	14.696 14,295
		14,714 13,752
10.2 17.7	11,664 10,506	12,988 12,765
6.8 10.5	12,122 11,521	13,602 13,006 12,873 14,509
	of Ash.    1	of Ash. bustion, B.T. U.    6.1   14,217   8.6   12,874     8.6   12,874     6.2   13,608     3.5   13,922     5.7   13,558     7.8   12,180     7.7   12,581     5.9   12,941     10,2   11,664     17.7   10,506     8.7   12,420     6.8   12,122     10,5   11,521     11,521     11,521     12,521     12,522     13,531     14,532     15,532

## Evaporative Power of Bituminous Coals.

(Tests with Bahcock & Wilcox Boilers, Trans. A. S. M. E., iv. 267.)

(Tests with Babe	ock & W	neoz	DO.	ners,	Tra	ns. A.	S. M. I	5., IV. X	307.)	
Name of Coal.	Duration of Test.	Grate Surface, sq. ft.	Heating Surface, sq. ft.	Percentage of Refuse.	Coal burned per sq. ft. of Grate, pounds.	Water evaporated per sq. ft. of Heating Surface per hour, pounds.	Water per pound Coal from and at 212°, lbs.	Water per pound Combustible from and at 212°.	Rated Horse-power.	Horse-power develope 1.
1. Welsh 2. Anthracite ser's 1/5	131/2 hrs		1679	7.5			11.53	12.46	146	96
Powelton, Pa., Semi-bit, 4/5,	10¼ h	60	3126	8.8	17.6	4.32	11.32	12,42	272	448
3. Pittsbg'h fine slack	4 hrs.	33.7			21.9		8.12	9.29	146	250
" 3d Pool lump 4. Castle Shannon, nr	10 "	43.5	2760	4.8	27.5	4.76	10.47	11.00	240	419
Pittsb'gh, 3/8 nut,	\\ 421/4 h	69.1	4784	10.5	27.9	4.13	10.00	11.17	416	570
5% lump, 5. Ill. "run of mine"	6 days.		1196			1.41	9.49		104	54
" Ind. block, "very	3 d'ys		1196			2.95	9.47		104	111
good " 6. Jackson, O., nut	8 hrs.	48	3358	9.6	32.1	4.11	8.93	9.88	292	460
" Staunton, Ill., nut	8 "	60	3358	17.7	25.1	2.27	5.09	6.19	292	246
7. Renton screenings.	5 h 50 m	21.2	1564	13.8	31.5	2.95	6.88	7.98	136	151
" Wellington scr'gs	6 h 30 m	21.2	1564	18.3	27	2.93	7.89	9.66	136	150
" Black Diani, ser'gs	5 h 58 m	21.2	1564	19.3	36.4	3.11	6.29	7.80	136	160
" Seattle screenings.	6 h 24 m					2.91	6.86	7.92	136	150
" Wellington lump	6 h 19 m					3.52	9.02	10.46	136	171
" Cardiff lump	6 h 47 m	21.2	1564	11.7	26.7	3.69	10.07	11.40	136	189
*****	7 h 23 m	21.2	1564	19.1	20.6	3.35	9.62	11.89	136	174
South Lame minp.	6 h 35 m 6 h 5 m	21.2	1564	0.5	20.9	8.53	8.96 7.68	10.41 8.49	136 136	182 184
" Seattle lump	me no	21.2	11004	9.0	94.1	0.07	1 1.05	0.49	190	104

Place of Test: 1. London, England; 2. Peacedale, R. I.; 3. Cincinnati, O.; 4. Pittsburgh, Pa.; 5. Chicago, Ill.; 6. Springfield, O.; 7. San Francisco,

In all the above tests the furnace was supplied with a fire-brick arch for preventing the radiation of heat from the coal directly to the boiler. Weathering of Coal. (I. P. Kimball, Trans. A. I. M. E., viii. 204.)—The practical effect of the weathering of coal, while sometimes increasing its absolute weight, is to diminish the quantity of carbon and disposable hydrogen and to increase the quantity of oxygen and of indisposable hydrogen. Hence a reduction in the calorific value.

An excess of pyrites in coal tends to produce rapid oxidation and mechanical disintegration of the mass, with development of heat, loss of coking

power, and spontaneous ignition.

The only appreciable results of the weathering of anthracite within the ordinary limits of exposure of stocked coal are confined to the oxidation of its accessory pyrites. In coking coals, however, weathering reduces and finally destroys the coking power, while the pyrites are converted from the state of bisulphide into comparatively innocuous sulphates.

Richters found that at a temperature of 158° to 180° Fahr., three coals lost in fourteen days an average of 3.6% of calorific power. (See also paper by R. P. Rothwell, Trans. A. I. M. E., iv. 55.)

#### COKE.

Coke is the solid material left after evaporating the volatile ingredients of coal, either by means of partial combustion in furnaces called coke ovens, or by distillation in the retorts of gas-works.

Coke made in ovens is preferred to gas coke as fuel. It is of a dark-gray color, with slightly metallic lustre, porous, brittle, and hard.

The proportion of coke yielded by a given weight of coal is very different

for different kinds of coal, ranging from 0.9 to 0.35. Being of a porous texture, it readily attracts and retains water from the atmosphere, and sometimes, if it is kept without proper shelter, from 0.15 to 0.20 of its gross weight consists of moisture

#### Analyses of Coke.

(From report of John R. Procter, Kentucky Geological Survey.)

• 7	Vhere Ma	de.			Fixed Carbon	Ash.	Sul- phur.
Connellsville, Pa. Chattanooga, Tenn. Birmingham, Ala. Pocahontas, Va.	(Average	of 3	samples	s)	88.96 80.51 87.29 92.53	9.74 16.34 10.54 5.74	0.810 1.595 1.195 0.597
New River, W. Va. Big Stone Gap, Ky.	"	" 8 " 7	"		92.38 93.23	7.21 5.69	0.562

### Experiments in Coking, Connellsville Region. (John Fulton Amer Mfr Feb 10 1893)

	(boin 1 diton, 11mer. 2011., 100.10, 100.)										
est.	·a ·	ed.	de.	Coke de.	ket made	Coke	Pe	r cent	of Yie	ld.	Cent st.
of Test.	Time i Oven.	Charge	made.			- ਨੇ	j.	e e	ket	e al	Per Cer Lost.
No.	EO	ರ್	Ash	Fine	Mai	Total	Ash.	Fine Coke.	Market Coke	Total Coke,	Pel
	h. m.	lb.	lb.	lb.	lb.	lb.					
1	67 00			385	7,518	7,903	00.80		60.53	63.63	35.57
*2 3 4	68 00			359	6,580	6,939	00.81	3.24	59.33	62.57	36.62
3	45 00		77	272	5,418	5,690	00.84	2.98	59.41	62.39	36 77
4	45 00	9,020	74	349	5,334	5,683	00.82	3.87	59.13	63.00	36.18
	J	41,650	340	1365	24,850	26,215	00.82	3.28	59.66	62.94	36.24

These results show, in a general average, that Connellsville coal carefully coked in a modern beehive oven will yield 66,17% of marketable coke, 2,30% of small coke or braize, and 0.82% of ash.

638 FUEL.

The total average loss in volatile matter expelled from the coal in coking amounts to 30.71%.

The modern beehive coke oven is 12 feet in diameter and 7 feet high at

crown of dome. It is used in making 48 and 72 hour coke.

In making these tests the coal was weighed as it was charged into the oven; the resultant marketable coke, small coke or braize and ashes

weighed dry as they were drawn from the oven.

Coal Washing .- In making coke from coals that are high in ash and sulphur, it is advisable to crush and wash the coal before coking it. A coal-washing plant at Brookwood, Ala., has a capacity of 50 tons per hour. The average percentage of ash in the coal during ten days' run varied from 14% to 21%, in the washed coal from 48% to 8.1%, and in the coke from 6.1% to 10.5%. During three months the average reduction of ash was 60.9%. (Eng. and Mining Jour., March 25, 1893.)

Recovery of By-products in Coke Manufacture.-In Germany considerable progress has been made in the recovery of by products. The Hoffman-Otto oven has been most largely used, its principal feature

The Hoffman-Otto oven has been most largely used, its principal feature being that it is connected with regenerators. In 1884 40 ovens on this system were running, and in 1892 the number had increased to 1209.

A Hoffman-Otto oven in Westphalia takes a charge of 64 tons of dry coal and converts it into coke in 48 hours. The product of an oven annually is 1025 tons in the Ruhr district, 1170 tons in Silesia, and 960 tons in the Saar district. The yield from dry coal is 75% to 77% of coke, 2.5% to 3% of tar, and 1.1% to 1.2% of sulphate of anmonia in the Ruhr district, 520 to 70% of coke, 4% to 4.5% of tar, and 1% to 1.25% of sulphate of ammonia in the Upper Silesia region and 68% to 72% of coke, 4% to 4.3% of tar and 1.8% to 1.9% of sulphate of ammonia in the Saar district. A group of 60 Hoffman ovens, therefore, yields annually the following:

District.	Coke, tons.	Tar, tons.	Sulphate Ammonia, tons.
uhr	51,200	1860	780
Opper Silesia	48,000	3000	840
aar	40,500	2400	492

An oven which has been introduced lately into Germany in connection with the recovery of by-products is the Semet-Solvay, which works hotter than the Hoffman-Otto, and for this reason 7% to 7% of gas coal can be mixed with 2% to 2% of coal low in volatile matter, and yet yield a good coke. Mixtures of this kind yield a larger percentage of coke, but, on the other hand, the amount of gas is lessened, and therefore the yield of tar and ammonia is not so great.

In the manufacture of coke from soft coal in retort ovens, particularly in those constructed so as to save the by-products formed in the coking operations, the coke has the disadvantage of being more porous, softer, with more easily crushed cell-walls than when the same coal is coked in the ordinary beehive-oven.

R U

References: F. W. Luerman, Verein Deutscher Eisenhuettenleute 1891, Iron Age, March 31, 1892; Amer. Mfr., April 28, 1893. An excellent series of articles on the manufacture of coke, by John Fulton, of Johnstown, Pa.,

is published in the Colliery Engineer, beginning in January, 1893.

Making Hard Coke.—J. J. Fronheiser and C. S Price, of the Cambria Iron Co., Johnstown, Pa., have made an improvement in coke manufacture by which coke of any degree of hardness may be turned out. It is accomplished by first grinding the coal to a coarse powder and mixing it with a hydrate of lime (air or water slacked caustic lime) before it is charged into the coke-ovens. The caustic lime or other fluxing material used is mechanically combined with the coke, filling up its cell-walls. It has been found that about 5% by weight of caustic lime mixed with the fine coal gives the best results. However, a larger quantity of lime can be added to coals entaining more than 5% to 7% of ash (Amer. Mfr.)

Generation of Steam from the Waste Heat and Gases of

**Coke-ovens.** (Erskine Ramsey, Amer. Mfr., Feb. 16, 1894.)—The gases from a number of adjoining ovens of the beehive type are led into a long horizontal flue, and thence to a combustion chamber under a battery of boilers. Two plants are in satisfactory operation at Tracy City, Tenn., and

two at Pratt Mines, Ala.

A Bushel of Coal. - The weight of a bushel of coal in Indiana is 70 lbs., in Penna. 76 lbs.; in Ala., Colo., Ga., Ill., Ohio, Tenn., and W. Va. it is 80 lbs. A Bushel of Coke is almost uniformly 40 lbs., but in exceptional cases, when the coke is very light, 38, 36, and 33 lbs, are regarded as a bushel, In others, from 42 to 50 lbs are given as the weight of a bushel; in this case

the coke would be quite heavy

Products of the Distillation of Coal.—S. P. Sadler's Handbook of Industrial Organic Chemistry gives a diagram showing over 50 chemical of industrial organic Chemisary gives a diagram showing over so chemical products that are derived from distillation of coal. The first derivatives are coal-gas, gas-liquor, coal-tar, and coke. From the gas-liquor are derived ammonia and sulphate, chloride and carbonate of ammonia. The coal-tar is split up into oils lighter than water or crude naphtha, oils heavier than water—otherwise dead oil or tar, commonly called creosote,—and pitch.
From the two former are derived a variety of chemical products,

From the coal-tar there comes an almost endless chain of known combinations. The greatest industry based upon their use is the manufacture of dyes, and the enormous extent to which this has grown can be judged from the fact that there are over 600 different coal-tar colors in use, and many more which as yet are too expensive for this purpose. Many medicinal prepara-tions come from the series, pitch for paving purposes, and chemicals for the photographer, the rubber manufacturers and tanners, as well as for

preserving timber and cloths.

The composition of the hydrocarbons in a soft coal is uncertain and quite complex; but the ultimate analysis of the average coal shows that it approaches quite nearly to the composition of CH<sub>4</sub> (marsh-gas), (W. H. Blauvelt, Trans. A. I. M. E., xx. 625.)

#### WOOD AS FUEL.

Wood, when newly felled, contains a proportion of moisture which varies very much in different kinds and in different specimens, ranging between 30% and 50%, and being on an average about 40%. After 8 or 12 months' ordinary drying in the air the proportion of moisture is from 20 to 25%. This degree of dryness, or almost perfect dryness if required, can be produced by a few days' drying in an oven supplied with air at about 240° F. When coal or coke is used as the fuel for that oven, 1 lb. of fuel suffices to expel coal or coke is used as the their for that over, 1 to 0 their sumes to expel about 3 lbs, of moisture from the wood. This is the result of experiments on a large scale by Mr. J. R. Napier. If air-dried wood were used as fuel for the over, from 2 to 2½ lbs. of wood would probably be required to produce the same effect.

The specific gravity of different kinds of wood ranges from 0.3 to 1.2.

Perfectly dry wood contains about 50% of carbon, the remainder consisting almost entirely of oxygen and hydrogen in the proportions which form water. The conference family contain a small quantity of turpentine, which is a hydrocarbon. The proportion of ash in wood is from 1% to 5%. The total heat of combustion of all kinds of wood, when dry, is almost exactly the same, and is that due to the 50% of carbon.

The above is from Rankine; but according to the table by S. P. Sharpless

in Jour. C. I. W., iv. 36, the ash varies from 0.03% to 1.20% in American woods, and the fuel value, instead of being the same for all woods, ranges from 2667 (for white oak) to 5546 calories (for long-leaf pine) = 6600 to 9883 British thermal units for dry wood, the fuel value of 0.50 lbs. carbon being 7272

B. T. U

Heating Value of Wood .- The following table is given in several books of reference, authority and quality of coal referred to not stated.

The weight of one cord of different woods (thoroughly air-dried) is about as follows:

Hickory or hard maple.... 4500 lbs. equal to 1800 lbs. coal. (Others give 2000.) ... 3850 " 1540 " 1300 " White oak.... Beech, red and black oak .. 3250 " 66 66 1450.) Poplar, chestnut, and elm.. 2350 The average pine...... 2000 6.6 940 6.6 66 1050. 46 800

Referring to the figures in the last column, it is said :

From the above it is safe to assume that 21/4 lbs. of dry wood are equal to 1 lb. average quality of soft coal and that the full value of the same weight 1 lb, average quality of soir contains that is, a pound of hickory is of different woods is very nearly the same—that is, a pound of hickory is worth no more for fuel than a pound of pine, assuming both to be dry. It is important that the wood be dry, as each 10% of water or moisture in wood will detract about 12% from its value as fuel.

Taking an average wood of the analysis C 51%, H 6.5%, O 42.0%, ash 0.5%,

perfectly dry, its fuel value per pound, according to Dulong's formula, V =

 $\left[14,500 \text{ C} + 62,000 \text{ (H} - \frac{\text{O}}{\text{S}})\right]$ , is 8170 British thermal units. If the wood, as

ordinarily dried in air, contains 25% of moisture, then the heating value of a pound of such wood is three quarters of 8170 = 6127 heat-units, less the heat required to heat and evaporate the ¼1 b. of water from the atmospheric temperature, and to heat the steam made from this water to the temperature of the chimney gases, say 150 heat-units per pound to heat the water to 212°, 966 units to evaporate it at that temperature, and 100 heat-units to raise the temperature of the steam to 420° F., or 1216 in all = 304 for 14 lb., which subtracted from the 6127, leaves 5821 heat-units as the net fuel value of the wood per pound, or about 0.4 that of a pound of carbon.

### Composition of Wood.

(Analysis of Woods, by M. Eugene Chevandier.)

Woods.	Composition.							
, ,	Carbon.	Hydrogen,	Oxygen.	Nitrogen.	Ash.			
Beech Oak Birch Poplar Willow	49.36% 49.64 50.20 49.37 49.96	6.01% 5.92 6.20 6.21 5.96	42.69% 41.16 41.62 41.60 39.56	0.91% 1.29 1.15 0.96 0.96	1.06% 1.97 0.81 1.86 3.37			
Average	49.70%	6.06%	41.30%	1.05%	1.80%			

The following table, prepared by M. Violette, shows the proportion of water expelled from wood at gradually increasing temperatures:

Temperature,	Water Expelled from 100 Parts of Wood.						
Temperature,	Oak.	Ash.	Elm.	Walnut.			
257° Fahr	15.26 17.93 32.13 35.80 44.31	14.78 16.19 21.22 27.51 33.38	15.32 17.02 86.94? 33.38 40.56	15.55 17.43 21.00 41.77? 36.56			

The wood operated upon had been kept in store during two years. When wood which has been strongly dried by means of artificial heat is left exposed to the atmosphere, it reabsorbs about as much water as it contains in its air-dried state.

A cord of  $vood=4\times4\times8=128$  cu. ft. About 56% solid wood and 44% interstitial spaces. (Marcus Bull, Phila., 1829. J. C. I. W., vol. i. p. 293.) B. E. Fernow gives the per cent of solid wood in a cord as determined officially in Prussia (J. C. I. W., vol. iii. p. 20):

Timber cords, 74.07% = 80 cu, ft, per cord;

Firewood cords (over 6" diam.), 69.44% = 75 cu. ft. per cord; "Billet" cords (over 3" diam.), 55.55% = 60 cu. ft. per cord;

"Brush" woods less than 3" diam., 18.52%; Roots, 37.00%.

#### CHARCOAL.

Charcoal is made by evaporating the volatile constituents of wood and peat, either by a partial combustion of a conical heap of the material to be charred, covered with a layer of earth, or by the combustion of a separate portion of fuel in a furnace, in which are placed retorts containing the material to be charged.

According to Peclet, 100 parts by weight of wood when charred in a heap yield from 17 to 22 parts by weight of charcoal, and when charred in a

retort from 28 to 30 parts.

This has reference to the ordinary condition of the wood used in charcoalmaking, in which 25 parts in 100 consist of moisture. Of the remaining 75 parts the carbon amounts to one half, or 371/5% of the gross weight of the wood, Hence it appears that on an average nearly half of the carbon in the

wood is lost during the partial combustion in a heap, and about one quarter

during the distillation in a retort.

To char 100 parts by weight of wood in a retort, 12½ parts of wood must be burned in the furnace. Hence in this process the whole expenditure of wood to produce from 25 to 30 parts of charcoal is 112½ parts; so that if the weight of charcoal obtained is compared with the whole weight of wood expended, its amount is from 25% to 25%; and the proportion lost is on an

average 11½ + 37½ = 0.3, nearly.

According to Peclet, good wood charcoal contains about 0.07 of its weight of ash. The proportion of ash in peat charcoal is very variable, and is estimated on an average at about 0.18. (Rankine.)

Much information concerning charcoal may be found in the Journal of the

Much information concerning charcoan may be found in time Journal of the Charcoal-iron Workers' Assn., vols. i. to vi. From this source the following notes have been taken:

Yield of Charcoal from a Cord of Wood.—From 45 to 50 bushels to the cord in the kiln, and from 30 to 35 in the meiler. Prof. Eglevion in Trans. A. I. M. E., viii. 395, says the yield from kilns in the Lake Champlain region is often from 50 to 60 bushels for hard wood and 50 for soft wood; the coveres is about 50 bushels. soft wood: the average is about 50 bushels.

The apparent yield per cord depends largely upon whether the cord is a

full cord of 128 cu. ft. or not.

In a four months' test of a kiln at Goodrich, Tenn., Dr. H. M. Pierce found results as follows: Dimensions of kilm—inside diameter of base, 28 ft. 8 in.; diam. at spring of arch, 26 ft. 8 in.; height of walls, 8 ft.; rise of arch, 5 ft.; capacity, 30 cords. Highest yield of charcoal per cord of wood (measured) 59.27 bushels, lowest 50.14 bushels, average 53.65 bushels.

No. of charges 12, length of each turn or period from one charging to another 11 days. (J. C. I. W., vol. vi. p. 26.)

### Results from Different Methods of Charcoal-making.

Coaling Methods,	Character of Wood used.	In Volume per cent.	In Weight p	Bushels of Charcoal per Cord of Wood.	Weight in Lbs. per Bushel of Charcoal,
Odelstjerna's experiments			35.9		
Mathieu's retorts, fuel ex- cluded	Air dry, av. good yel-	77.0	28.3	63.4	15.7
Mathieu's retorts, fuel in- cluded	abt. 28 lbs. per cu. ft.	65.8	24.2	54.2	15.7
Swedish ovens, av. results	Good dry fir and pine, mixed.	81.0	27.7	66.7	13.3
Swedish ovens, av. results	Poor wood, mixed fir	70.0	25 8	62.0	13.3
Swedish meilers excep-		72.2	24 7	59.5	13.3
Swedish meilers, av. results	( lbs. per cu. ft. )		18 3		13.3
American kilns, av. results American meilers, av. re-		54.7	22.0	45.0	17 5
sults	per cu. ft.	42.9	17.1	35 0	17.5

Consumption of Charcoal in Blast-furnaces per Ton of Pig Iron; average consumption according to census of 1880, 1.14 tons charcoal per ton of pig. The consumption at the best furnaces is much

charcoal per ton o. pig. The consumption at the best infraces is much below this average. As low as 0 833 ton, is recorded of the Morgan furnace; Bay furnace, 0.888; Elk Rapids, 0.884. (1892.)

Absorption of Water and of Gases by Charcoal.—Svedlius, in his hand-book for charcoal-burners, prepared for the Swedish Governent, says: Fresh charcoal also reheated charcoal, contains scarcely any water but when cooled fit absorbs it very rapidly, so that after twenty-four hours, it may contain 4% to 8% of water. After the lapse of a few weeks the moisture of charcoal may not increase perceptibly, and may be estimated at 10% to 15%, or an average of 12%. A thoroughly charred piece of charcoal ought, then, to contain about 84 parts carbon 12 parts water, 3 parts ash, and 1 part hydrogen.

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M. Saussure, operating with blocks of fine boxwood charcoal, freshly burnt, found that by simply placing such blocks in contact with certain gases they absorbed them in the following proportion:

	Volumes.	Volumes.
Ammonia		Carbonic oxide 9.42
Hydrochloric-acid gas		Oxygen 9.25
Sulphurous acid		Nitrogen 6.50 Carburetted hydrogen 5.00
Nitrous oxide (laughing-gas)		Hydrogen
Carbonic acid	35.00	

It is this enormous absorptive power that renders of so much value a comparatively slight sprinkling of charcoal over dead animal matter, as a preventive of the ascape of oders arising from decomposition.

comparatively signs sprinking of earlied over east animal matter, as a preventive of the escape of odors arising from decomposition. In a box or case containing one cubic foot of charcoal may be stored without mechanical compression a little over nine cubic feet of oxygen, representing a mechanical pressure of one hundred and twenty-six pounds to the square inch. From the store thus preserved the oxygen can be drawn by a small hand-pump.

### Composition of Charcoal Produced at Various Temperatures. (By M. Violette.)

		C	Composition of the Solid Product.							
	Temperature of Car bonization.	Carbon.	Hydro- gen.	Oxygen,	Nitrogen and Loss.	Ash.				
_										
	Cent, Fahr.	Per cent.	Per cent.	Per cent.	Per cent.	Per cent.				
1	150° 302°	47.51	6.12	46.29	0.08	47.51				
2 3	200 392	51.82	3.99	43.98	0.23	39.88				
3	250 482	65.59	4.81	28.97	0.63	32.98				
4	300 592	73.24	4.25	21.96	0.57	24.61				
5	350 662	76.64	4.14	18.44	0.61	22.42				
4 5 6	432 810	81.64	4.96	15.24	1.61	15.40				
7	1023 1873	81.97	2.30	14.15	1.60	15.30				

The wood experimented on was that of black alder, or alder buckthorn, which furnishes a charcoal suitable for gunpowder. It was previously dried at 150 deg. C. = 302 deg. F.

#### MISCELLANEOUS SOLID FUELS.

Dust Fuel - Dust Explosions, -Dust when mixed in air burns with such extreme rapidity as in some cases to cause explosions. Explosions of flour-mills have been attributed to ignition of the dust in confined passages. Experiments in England in 1876 on the effect of coal-dust in carrying flame in mines showed that in a dusty passage the flame from a blown-out shot may travel 50 yards. Prof. F. A. Abel (Trans, A. I. M. E. xiii. 260) says that coal-dust in mines much promotes and extends explosions, and that it may readily be brought into operation as a ferely burning agent which will carry flame rapidly as far as its mixture with air extends, and will operate as an explosive agent through the medium of a very small proportion of fire-damp in the air of the mine. The explosive violence of the combustion of dust is largely due to the instantaneous heating and consequent expansion of the air. (See also paper on "Coal Dust as an Explosive Agent." by Dr. R. W. Raymond, Trans. A. I. M. E. 1894.) Experiments made in Germany in 1893, show that pulverized fuel may be burned without smoke, and with high economy. The fuel, instead of being introduced into the fire-box in the ordinary manner, is first reduced to a powder by pulverizers of any construction. In the place of the ordinary boller fire-box there is a combustion chamber in the form of a closed furnace lined with fire-brick and provided with an air-injector similar in construction to those used in oil-burning furnaces. The nozzle throws a constant stream of the fuel into the chamber.

space of the fire-box. When this powder is once ignited, and it is very readily done by first raising the lining to a high temperature by an open fire, the combustion continues in an intense and regular manner under the

nue, the combustion continues in an intense and regular manner under the action of the current of air which carries it in. (Mfrs. Record, April, 1893.) Powered fuel was used in the Crompton rotary puddling-furnace at Woolwich Arsenal, England, in 1873. [Jour. I. & S. I., I. 1873, p. 91.)

Peat or Turf, as usually dried in the air, contains from 25% to 30% of water, which must be allowed for in estimating its heat of combustion. This water having been evaporated, the analysis of M. Regnaut gives, in 100 parts of perfectly dry peat of the best quality: C 58%. H 6%. O 31%, Ash 5%.

In some examples of peat the quantity of ash is greater, amounting to 7% and sometimes to 11%

The specific gravity of peat in its ordinary state is about 0.4 or 0.5. It can be compressed by machinery to a much greater density. (Rankine.)

Clark (Steam-engine, i. 61) gives as the average composition of dried Irish peat: C 59%, H 6%, O 30, N 1,25%, Ash 4. Applying Dulong's formula to this analysis, we obtain for the heating value of perfectly dry peat 10,260 heat-units per pound, and for air-dried peat containing 25% of moisture, after making allowance for evaporating the water,

7391 heat-units per pounds.

Sawdust as Fuel .- The heating power of sawdust is naturally the same per pound as that of the wood from which it is derived, but if allowed to get wet it is more like spent tan (which see below). The conditions necessary for burning sawdust are that plenty of room should be given it in the furnace, and sufficient air supplied on the surface of the mass. The same applies to shavings, refuse lumber, etc. Sawdust is frequently burned in saw-mills, etc., by being blown into the furnace by a fan-blast,

Horse-manure has been successfully used as fuel by the Cable Railway Co. of Chicago. It was mixed with soft coal and burned in an ordinary

way 00. of Chicago. It was mixed with soft coal and burned in an ordinary urnace provided with a fire-brick arch.

Wet Tan Bark as Fuel.—Tan, or oak bark, after having been used in the processes of tanning, is burned as fuel. The spent tan consists of the fibrous portion of the bark. According to M. Peelet, five parts of oak bark produce four parts of dry tan; and the heating power of perfectly dry tan, containing 15% of ash, is 6100 English units; whilst that of tan in an ordinary state of dryness, containing 30% of water, is only 48% English units. The weight of water evaporated from and at 212° by one pound of tan, equivalent to the control of the product of the product of the control of the product lent to these heating powers, is, for perfectly dry tan, 5.46 lbs., for tan with Experiments by Prof. R. H. Thurston (Jour. Frank. 30% moisture, 3.84 lbs. Inst., 1874) gave with the Crockett furnace, the wet tan containing 59% of water, an evaporation from and at 212° F. of 4.24 lbs. of water per pound water, an evaporation from and at 212° F. of 4.24 lbs. of water per pound of the wet tan, and with the Thompson furnace an evaporation of 3.19 lbs. per pound of wet tan containing 55% of water. The Thompson furnace consisted of six fire-brick ovens, each 9 feet × 4 feet 4 inches, containing 234 square feet of grate in all, for three boliers with a total heating surface of 2000 square feet, a ratio of heating to grate surface of 9 to 1. The tan was fed through holes in the top. The Crockett furnace was an ordinary fire-brick furnace, 6 × 4 feet, built in front of the boller, instead of under it, the ratio of heating surface to grate being 14.6 to 1. According to Prof. Thurston the conditions of success in burning wet fuel are the surrounding of the mass so completely with heated surfaces and with burning fuel that it may mass so completely with heated surfaces and with burning fuel that it may be rapidly dried, and then so arranging the apparatus that thorough combustion may be secured, and that the rapidity of combustion be precisely equal to and never exceed the rapidity of desiccation. Where this rapidity of combustion is exceeded the dry portion is consumed completely, leaving an uncovered mass of fuel which refuses to take fire.

Straw as Fuel. (Eng'g Mechanics, Feb., 1893, p. 55.)—Experiments in Russia showed that winter-wheat straw, dried at 230° F., had the following composition: C, 46.1; H, 5.6: N, 0.42: O, 43.7; Ash, 4.1. Heating value in British thermal units: dry straw, 6290; with % water, 5770; with 10% water, 5448. With straws of other grains the heating value of dry straw ranged

5448. With straws of other grains the heating value of dry straw ranged from 5590 for buckwheat to 6750 for flax.

Clark (8, E., vol. 1, p. 69) gives the mean composition of wheat and barley straw as C, 36; H, 5; O, 38; O, 0.50; Ash, 4.75; water, 15.75, the two straws varying less than 12. The heating value of straw of this composition, according to Dulong's formula, and deducting the heat lost in evaporating the water, is 5155 heat units. Clark erroneously gives it as \$144 heat, units.

Bagasse as Fuel in Sugar Manufacture, -- Bagasse is the name given to refuse sugar-cane, after the juice has been extracted. Prof. L. A.

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Becuel, in a paper read before the Louisiana Sugar Chemists' Association, in 1892, says; "With tropical cane containing 12.5% woody fibre, a juice contain-ing 16.13% solids, and \$3.57% water, bagasse of, say, 66% and 72% mill extraction would have the following percentage composition:

	Woody Fibre.	Combustible Salts.	Water.
66% bagasse	37	10	53
72% bagasse	45	9	46

"Assuming that the woody fibre contains 51% carbon, the sugar and other combustible matters an average of 42.1%, and that 12.906 units of heat are generated for every pound of carbon consumed, the 66% bagasse is capable of generating 297.834 heat units as against 345,200, or a difference of 47,366 units in favor of the 72% bagasse.

"Assuming the temperature of the waste gases to be 450° F., that of the surrounding atmosphere and water in the bagasse at 86° F., and the quantity of air necessary for the combustion of one pound of carbon at 24 lbs., the lost heat will be as follows: In the waste gases, heating air from 86° to 450° F., and in vaporizing the moisture, etc., the 66% bagasse will require 112,546 heat units, and 116,150 for the 72% bagasse.

"Subtracting these quantities from the above, we find that the 66% bagasse will produce 185,288 available heat units, or nearly 38% less than the 72% bagasse, which gives 299,050 units. Accordingly, one ton of cane of 2000 lbs. at 66% mill extraction will produce 680 lbs. bagasse, equal to 125,995,840 available heat units, while the same cane at 72% extraction will produce 560 lbs.

bagasse, equal to 167,468,000 units.

A similar calculation for the case of Louisiana cane containing 10% woody fibre, and 16% total solids in the juice, assuming 75% mill extraction, shows that bagasse from one ton of cane contains 157,395,640 heat units, from

which 56,146,500 have to be deducted.

"This would make such bagasse worth on an average nearly 92 lbs. coal per ton of cane ground. Under fairly good conditions, 1 lb. coal will evaporate 71/2 lbs. water, while the best boiler plants evaporate 10 lbs. Therefore, the bagasse from 1 ton of cane at 75% mill extraction should evaporate from she begasser in a former and a first market action should exposure to the second tions contain 1260 lbs. of water. If we assume that the water added during the process of manufacture is 10% (by weight) of the vacet and the total water handled is 1410 lbs. From the juice legense and in this case, the total water handled is 1410 lbs. From the juice legense in this case, the commercial massecuite would be about 15% of the weight of the original mill juice, or say 225 lbs. Said mill juice 1500 lbs., plus 10%, equals 1650 lbs. liquor handled; and 1650 lbs., minus 225 lbs., equals 1425 lbs., the quantity of water to be evaporated during the process of manufacture. To effect a 71/6-lb. evaporation requires 190 lbs. of coal, and 1421/6 lbs. for a 10lb. evaporation.

"To reduce 1650 lbs. of juice to syrup of, say, 27° Baumé, requires the evaporation of 1770 lbs of water, leaving 480 lbs. of syrup. If this work be accomplished in the open air, it will require about 156 lbs. of coal at 71/2 lbs.

boiler evaporation, and 117 at 10 lbs. evaporation.

"With a double effect the fuel required would be from 59 to 78 lbs., and with a triple effect, from 36 to 52 lbs.

"To reduce the above 480 lbs. of syrup to the consistency of commercial massecute means the further evaporation of 255 lbs. of water, requiring the expenditure of 34 lbs. coal at 7½ lbs. boiler evaporation, and 25½ lbs. with a 10-lb. evaporation. Hence, to manufacture one ton of cane into sugar and molasses, it will take from 145 to 190 lbs. additional coal to do the work by the open evaporator process; from 85 to 112 lbs. with a double effect, and only 7% lbs. evaporation in the boilers, while with 10 lbs. boiler evaporation the bagasse alone is capable of furnishing % more heat than is actually required to do the work. With triple-effect evaporation depending on the excellence of the boiler plant, the 1425 lbs. of water to be evaporated from the Juice will require between 62 and 86 lbs. of coal. These values are from 6 to 30 lbs. of coal can be spared from the value of the bagasse to run engines, grind cane, etc.

"It accordingly appears." says Prof. Becuel, "that with the best boiler plants, those taking up all the available heat generated, by using this heat economically the bagasse can be made to supply all the fuel required by our

sugar-houses."

#### PECEROLIEITE.

### Products of the Distillation of Crude Petroleum.

Crude American petroleum of sp. gr. 0.800 may be split up by fractional distillation as follows (Robinson's Gas and Petroleum Engines):

Temp. of Distillation Fahr.	Distillate.	Percentages.	Specific Gravity.	Flashing Point. Deg. F.
113° 113 to 140° 140 to 158° 158 to 248° 248° to	Rhigolene. } Chymogene. } Gasolene (petroleum spirit) Benzine, naphtha C, benzolene. } Benzine, naphtha B	traces.  1.5 10. 2.5 2.	.590 to .625 .636 to .657 .680 to .700 .714 to .718 .725 to .737	14
347° 338° and ( upwards.) 482°	( Polishing oils.  Kerosene (lamp-oil).  Lubricating oil Paraffine wax.  Residue and Loss.	50. 15. 2. 16.	.802 to .820 .850 to .915	230

Lima Petroleum, produced at Lima, Ohio, is of a dark green color, very fluid, and marks 48° Baumé at 15° C. (sp. gr., 0.792).

The distillation in fifty parts, each part representing 2% by volume, gave

the r	OHOWIT	g resu	mes:								
Per	Sp.	Per	Sp.	Per	Sp.	Per	Sp.	Per	Sp.	Per	Sp.
cent.	Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.	cent.	Gr.
2	0.680	18	0.720	34	0.764	50	0.802	68	0.820	88	0.815
4	.683	20	.728	36	.768	52)		70	.825	90	.815
4 6 8	.685	22	.730	38	.772	to	.806	72	.830		
8	.690	24	.735	40	.778	58		73	.830	921	Residuum
10	.694	26	.740	42	.782	60 1	.800	76	.810	to >	5
10 12	.698	28	.742	44	.788	62	.804	78	.820	100	ij
14	.700	30	.746	46	.792	64	.808	82	.818	,	es
16	.706	32	.760	48	.800	66	.812	86	.816		ద
					RE	TURNS.					

16 per cent naphtha, 70° Baumé. 6 per cent paraffine oil. burning oil. 10 residuum.

68 "burning oil. 10" "residuum.

The distillation starred at 23° C., this being due to the large amount of naphtha present, and when 60% was reached, at a temperature of 310° C., the hydrocarbons remaining in the retort were dissociated, then gases escaped, lighter distillates were obtained, and, as usual in such cases, the temperature decreased from 310° C. down gradually to 200° C., until 73% of oil was obtained, and from this point the temperature remained constant until the end of the distillation. Therefore these hydrocarbons in statu unril the end of the distillation. Therefore these hydrocarbons in statu unril the end of the distillation. Therefore these hydrocarbons in statu unril the end of the distillation. Therefore these hydrocarbons in statu unril the properties of the constant until the end of the distillation. Therefore these hydrocarbons in status unriled the properties of the constant until the end of the theoretical evaporative power of petroleum in comparison with that of coal, as determined by Messrs Favre & Silbermann:

Messrs, Favre & Silbermann:

Fuel.	Specific Gravity Chem. Comp.				Heating- power,	Theoret. Evap., lbs. Water per	
r det.	32° F., Water = 1.000.	C.	н.	0.	British Thermal Units.	lb. Fuel, from and at 212° F.	
Penna, heavy crude oil Caucasian light crude oil heavy "". Petroleum refuse Good English Coal, Mean	0.884 0.938 0.928	p. c. 84.9 86.3 86.6 87.1	p. c. 13.7 13.6 12.3 11.7	p. c. 1.4 0.1 1.1 1.2	Units. 20,736 22,027 20,138 19,832	lbs. 21.48 22.79 20.85 20.53	
of 98 Samples	1.380	80.0	5.0	8.0	14,112	14.61	

In experiments on Russian railways with petroleum as fuel Mr. Urquhart obtained an actual efficiency equal to 82% of the theoretical heating-value. The petroleum is fed to the furnace by means of a spray-injector driven by An induced current of air is carried in around the injector-nozzle,

and additional air is supplied at the bottom of the furnace

Oil vs. Coal as Fuel. (Iron Age, Nov. 2, 1893.)—Test by the Twin City Rapid Transit Company of Minneapolis and St. Paul. This test showed City Rapid Transit Company of Minneapolis and St. Paul. This test showed that with the ordinary Lima oil weighing 6 6/10 pounds per gallon, and costing 2½ cents per gallon, and cosl that gave an evaporation of 7½ lbs. of water per pound of coal, the two fuels were equally economical when the price of coal was 83 85 per ton of 2000 lbs. With the same coal at \$2.00 per ton, the coal was 3% more economical, and with the coal at \$4.85 per ton, the coal was 20% more expensive than the oil. These results include the difference in the cost of handling the coal, asines, and oil.

In 1892 there were reported to the Engineers' Club of Philadelphia some

comparative figures, from tests undertaken to ascertain the relative value

of coal, petroleum, and gas.

, powercam, and gues	Lbs. Water, from and at 212° F.
1 lb. anthracite coal evaporated	
1 lb. bituminous coal	10.14
1 lb. free oil, 36° gravity	16 48
1 cubic foot gas, 20 C. P	1.28

The gas used was that obtained in the distillation of petroleum, having about the same fuel-value as natural or coal-gas of equal candle-power,

Taking the efficiency of bituminous coal as a basis, the calorific energy of petroleum is more than 60% greater than that of coal; whereas, theoretically, petroleum exceeds coal only about 45%—the one containing 14,500 heat-units, and the other 21,000.

Crude Petroleum vs. Indiana Block Coal for Steam-raising at the South Chicago Steel Works. (E. C. Potter, Trans. A. I. M. E., xvii, 87).—With coal, 14 tubular boilers 16 ft. x 6 ft. required 25 men to operate them; with fuel oil, 6 men were required, a saving

of 19 men at \$2 per day, or \$38 per day.

For one week's work 2731 barrels of oil were used, against 848 tons of coal required for the same work, showing 322 barrels of oil to be equivalent to 1 ton of coal. With oil at 60 cents per barrel and coal at \$2.15 per ton, the relative cost of oil to coal is as \$1.93 to \$2.15. No evaporation tests were made.

Petroleum as a Metallurgical Fuel.—C. E. Felton (Trans. A. I. M. E., xvii, 809) reports a series of trials with oil as fuel in steel-heating and open-hearth steel-furnaces, and in raising steam with results as follows: 1. open-hearth steel-turnaces, and in raising steam with results as follows: In a run of six weeks the consumption of oil, partly refined (the paraffine and some of the naphtha being removed), in heating 14-inch ingots in Siemens furnaces was about 645 gallons per ton of blooms. 2. In melting in a 30-ton open-hearth furnace 48 gallons of oil were used per ton of ingots. 3. In a six weeks' trial with Lima oil from 47 to 54 gallons of oil were required per ton of ingots. 4. In a six months' trial with Siemens heating-furnaces the ton of linguis. 4, in a six months tria with Siemen's heating turnaces inconsumption of Linia oil was 6 gallons per ton of linguis. Under the most favorable circumstances, charging bot ingots and running full capacity, 49.6 to 5 gallons per ton were required. 5. In raising steam in two 100 H.P. tubular boilers, the feed-water being supplied at 169° F., the average evaporation was about 12 pounds of water per pound of oil, the best 12 hours? work being 16 pounds.

In all of the trials the oil was vaporized in the Archer producer, an apparatus for mixing the oil and superheated steam, and heating the mixture to a high temperature. From 0.5 lb. to 0.75 lb. of pea-coal was used per gallon

of oil in the producer itself.

#### FUEL GAS.

The following notes are extracted from a paper by W. J. Taylor on "The

Energy of Fuel" (Trans. A. I. M. E., xviii. 205): Carbon Gas.—In the old Siemens producer, practically, all the heat of orimary combustion—that is, the burning of solid carbon to carbon monoxide, or about 30% of the total carbon energy—was lost, as little or no steam was used in the producer, and nearly all the sensible heat of the gas was dissipated in its passage from the producer to the furnace, which was usually placed at a considerable distance.

Modern practice has improved on this plan, by introducing steam with the

air blown into the producer, and by utilizing the sensible heat of the gas in the combustion-furnace. It ought to be possible to oxidize one out of every four lbs. of carbon with oxygen derived from water-vapor. The thermic reactions in this operation are as follows:

Heat-units.

3,519

The steam which is blown into a producer with the air is almost all condensed into finely divided water before entering the fuel, and consequently

is considered as water in these calculations.

The 1.5 bs, of water liberates 187 b, of hydrogen, which is delivered to the gas, and yields in combustion the same heat that it absorbs in the producer by dissociation. According to this calculation, therefore, 60% of the heat of primary combustion is theoretically recovered by the dissociation of steam, and, even if all the sensible heat of the gas be counted, with radiation and other minor items, as loss, yet the gas must carry 4 × 14,500 – (3748 + 3519) = 50,733 heat-units, or 8% of the calorific energy of the carbon. This estimate shows a loss in conversion of 13%, without crediting the gas with its sensible heat, or charging it with the heat required for generating the necessary steam, or taking into account the loss due to oxidizing some of the carbon to CO<sub>2</sub>. In good producer-practice the proportion of CO<sub>2</sub> in the gas represents from 4½ to 7% of the C burned to CO<sub>2</sub>, but the extra heat of this combustion should be largely recovered in the dissociation of more water-vapor, and therefore does not represent as much loss as it would indicate. As a conveyer of energy, this gas has the advantage of carrying 4.46 bs, less nitrogen than would be present if the fourth pound of coal had been gasified with air; and in practical working the use of steam reduces the amount of clinkering in the producer.

water-vapor, and therefore does not represent as much loss as it would indicate. As a conveyer of energy, this gas has the advantage of carrying 4.46 lbs. less nitrogen than would be present if the fourth pound of coal had been gasified with air; and in practical working the use of steam reduces the amount of clinkering in the producer.

Anthractic Gas.—In anthracite coal there is a volatile combustible varying in quantity from 1.5% to over 7%. The amount of energy derived from the coal is shown in the following theoretical gasification made with coal of assumed composition: Carbon, 85%; vol. HC, 5%; ash, 10%; 80 lbs. carbon assumed to be burned to CO; 5 lbs. carbon burned to CO; three fourths of the necessary oxygen derived from air, and one fourth from water.

		Products	
Process.	Pounds.	Cubic Feet.	Anal, by Vol.
80 lbs. C burned to	186.66	2529.24	33.4
5 lbs, C burned to CO2		157.64	2.0
5 lbs. vol. HC (distilled)	5.00	116.60	1.6
120 lbs. oxygen are required, of which			
30 lbs. from H <sub>2</sub> O liberateH	3.75	712.50	9.4
90 lbs, from air are associatied with N	301.05	4064.17	53.6
	514.79	7580.15	100.0

3.75 " H 232,500 "

The sum of CO and H exceeds the results obtained in practice. The sensible heat of the gas will probably account for this discrepancy, and, therefore, it is safe to assume the possibility of delivering at least 82% of the energy of the anthracite.

Bituminous Gas.—A theoretical gasification of 100 lbs. of coal, containing 55% of carbon and 32% of volatile combustible (which is above the average of Pittsburgh coal), is made in the following table. It is assumed that 50 lbs. of C are burned to CO and 5 lbs. to CO<sub>2</sub>; one fourth of the O is

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derived from steam and three fourths from air; the heat value of the volatile combustible is taken at 20,000 heat-units to the pound. In computing volumetric proportions all the volatile hydrocarbons, fixed as well as condensing, are classed as marsh-gas, since it is only by some such tentative assumption that even an approximate idea of the volumetric composi-tion can be formed. The energy, however, is calculated from weight:

		Products	
Process.	Pounds,	Cubic Feet.	Anal. by Vol.
50 lbs, C burned toCO	116.66	1580.7	27.8
5 lbs. C burned to	18.33	157.6	2.7
32 lbs. vol. HC (distilled)	32.00	746.2	13.2
80 lbs. O are required, of which 20 lbs.,			
derived from H <sub>2</sub> O, liberate H	2.5	475.0	8.3
60 lbs. O, derived from air, are asso-			
ciated withN	200.70	2709.4	47.8
	370.19	5668.9	99.8
Energy in 116.66 lbs. CO	504,	554 heat-units	
" " 32.00 lbs. vol. HC	640.0	000 "	
" " 2.50 lbs. H	155,0	000 "	
		_	
	1,299,	554 "	
Energy in coal	1,437,5	500 "	
Por cont of anarow delivered	in mag	00.4	0

gy delivered in gas..... Heat-units in 1 lb, of gas.....

Water-gas,-Water-gas is made in an intermittent process, by blowing up the fuel-bed of the producer to a high state of incandescence (and in one cases utilizing the resulting gas, which is a lean producer-gas), then shutting off the air and forcing steam through the fuel, which dissociates the water into its elements of oxygen and hydrogen, the former combining with the carbon of the coal, and the latter being liberated.

This gas can never play a very important part in the industrial field, owing to the large loss of energy entailed in its production, yet there are places

and special purposes where it is desirable, even at a great excess in cost per unit of heat over producer-gas; for instance, in small high-temperature furnaces, where much regeneration is impracticable, or where the "blow-up" gas can be used for other purposes instead of being wasted.

The reactions and energy required in the production of 1000 feet of watergas, composed, theoretically, of equal volumes of CO and H, are as follows:

 500 cubic feet of H weigh
 2.635 lbs.

 500 cubic feet of CO weigh
 36.89 "

Total weight of 1000 cubic feet...... 39.525 lbs.

Now, as CO is composed of 12 parts C to 16 of O, the weight of C in 36.89 lbs. is 15.81 lbs. and of O 21.08 lbs. When this oxygen is derived from water its liberates, as above, 2.035 lbs. of hydrogen. The heat developed and absorbed in these reactions (roughly, as we will not take into account the energy required to elevate the coal from the temperature of the atmosphere to say 1800°) is as follows:

Heat-units. 2,635 lbs. H absorb in dissociation from water  $2.635 \times 62,000... = 163,370$ 15.81 lbs. C burned to CO develops 15.81 × 4400..... = 69,564 Excess of heat-absorption over heat-development .... = 93,806

If this excess could be made up from C burnt to CO<sub>2</sub> without loss by radiation, we would only have to burn an additional 4.83 lbs. C to supply this heat, and we could then make 1000 feet of water-gas from 20.64 lbs. of carbon (equal 24 lbs. of 85% coal). This would be the perfection of gas-making, as the gas would contain really the same energy as the coal; but instead, we require in practice more than doubt this amount of coal, and do not deliver more than 50% of the energy of the fuel in the gas, because the supporting heat is obtained in an indirect way and with imperfect combustion. Besides this, it is not often that the sum of the CO and H exceed 90% the balance being CO<sub>2</sub> and N. But water-gas should be made with much less loss of energy by burning the "blow-up" (producer) gas in brick regenerators, the stored-up heat of which can be returned to the producer by the air used in blowing-up.

The following table shows what may be considered average volumetric

analyses, and the weight and energy of 1000 cubic feet, of the four types of gases used for heating and illuminating purposes:

	Natural Gas.	Coal- gas.	Water- gas.	Produc	er-gas.
				Anthra.	Bitu.
CO	0.50	6.0	45.0	27.0	27.0
H	2.18	46.0	45.0	12.0	12.0
CH <sub>4</sub>	92.6	40.0	2.0	1.2	2.5
C <sub>2</sub> H <sub>4</sub>		4.0			0.4
CO2		0.5	4.0	2.5	2.5
N		1.5	2.0	57.0	56.2
0	0.34	0.5	0.5	0.3	0.3
		1.5	1.5	0.0	0.0
Pounds in 1000 cubic feet.	d 45 0	32.0	45.6	65.6	65.9
Heat units in 1000 cubic feet	[1,100,000]	735,000	322,000	137,455	156,917

### Natural Gas in Ohio and Indiana.

(Eng. and M. J., April 21, 1894.)

	Ohio.			Indiana.				
Description.	Fos- toria.	Findlay	St. Mary's.	Muncie.	Ander- son.	Koko- mo,	Mar- ion.	
Hydrogen	1.89	1.64	1.94	2.35	1.86	1.42	1.20	
Marsh-gas.	92.84	93.35	93.85	92.67	93.07	94.16	93.57	
Olefiant gas.	.20	.35	.20	.25	.47	.30	.15	
Carbon monoxide	.55	.41	.44	.45	.73	.55	.60	
Carbon dioxide	.20	.25	.23	.25	.26	.29	.30	
Oxygen	.35	.39	.35	.35	.42	.30	.55	
Nitrogen	3.82	3.41	2.98	3.53	3.02	2.80	3.42	
Hydrogen sulphide	.15	.20	.21	.15	.15	.18	.20	

Approximately 30,000 cubic feet of gas have the heating power of one ton of coal.

## Producer-gas from One Ton of Coal.

(W. H. Blauvelt, Trans. A. I. M. E., xviii, 614.)

Analysis by Vol.	Per lent.	Cubic Feet.	Lbs.	Equal to—
H	25.3 9.2 3.1 0.8 3.4 58.2	33,213.84 12,077.76 4,069.68 1,050.24 4,463.52 76,404.96	174.66 77.78	174.66 " CH <sub>4</sub> . 77.78 " C <sub>2</sub> H <sub>4</sub> . 141.54 " C+377.44 lbs. O.

Calculated upon this basis, the 131,280 ft. of gas from the ton of coal contained 20,311,162 B.T.U., or 155 B.T.U. per cubic ft., or 2270 B.T.U., per lb. The composition of the coal from which this gas was made was as follows: Water, 1.29%; volatile matter, 36.22%; fixed carbon, 57,39%; sulphur, 0.70%; ash, 3.78%. One ton contains 1139.6 lbs. carbon and 744.4 lbs. volatile companies of the comp bustible, the energy of which is 31,302,200 B.T.U. Hence, in the processes of gasification and purification there was a loss of 35.2% of the energy of the coal.

The composition of the hydrocarbons in a soft coal is uncertain and quite complex; but the ultimate analysis of the average coal shows that it approaches quite nearly to the composition of CH4 (marsh-gas).

Mr. Blauvelt emphasizes the following points as highly important in soft-

coal producer-practice:

650 FÜEL.

First. That a large percentage of the energy of the coal is lost when the gas is made in the ordinary low producer and cooled to the temperature of the air before being used. To prevent these sources of loss, the producer should be placed so as to lose as little as possible of the sensible heat of the gas, and prevent condensation of the hydrocarbon vapors. A high fuel-bed should be carried, keeping the producer cool on top, thereby preventing the breaking-down of the hydrocarbons and the deposit of soot, as well as keeping the carbonic acid low.

Second. That a producer should be blown with as much steam mixed with Second. That a producer should be nown with as much steam mixed with the air as will maintain incandescence. This reduces the percentage of nitrogen and increases the hydrogen, thereby greatly enriching the gas. The temperature of the producer is kept down, diminishing the loss of heat by radiation through the walls, and in a large measure preventing clinkers. The Combustion of Producer-gas. (H. H. Campbell, Trans.

A. I. M. E., xix, 128.)-The combustion of the components of ordinary producer-gas may be represented by the following formulæ:

 $C_2H_4 + 6O = 2CO_2 + 2H_2O;$   $CH_4 + 4O = CO_2 + 2H_2O;$  $^{2H} + ^{O} = ^{H_2O};$  $^{CO} + ^{O} = ^{CO_2}.$ 

AVERAGE COMPOSITION BY VOLUME OF PRODUCER-GAS: A, MADE WITH OPEN GRATES, NO STEAM IN BLAST; B, OPEN GRATES, STEAM-JET IN BLAST. 10 SAMPLES OF EACH.

	CO2.	Ο.	C2H4.	CO.	H.	CH4.	N.
A min	$3.\overline{6}$	0.4	0.2	20.0	5.3	3.0	58.7
A max	5.6	0.4	0.4	24.8	8.5	5.2	64.4
A average	4.84	0.4	0.34	22.1	6.8	3.74	61.78
B min		0.4	_ 0.2	20.8	6.9	2.2	57.2
B max	6.0	0.8	0.4	24.0	9.8	3.4	62.0
B average	5.3	0.54	0.36	22.74	8.37	2.56	60.13

The coal used contained carbon 82%, hydrogen 4.7%.

The following are analyses of products of combustion:

	CO <sub>2</sub> .	Ο.	CO.	CH <sub>4</sub> .	н.	N.	
Minimum	15.2	0.2	trace.	trace.	trace.	80.1	
Maximum	17.2	1.6	2.0	0.6	2.0	83.6	
Average		0.8	0.4	0.1	0.2	82.2	

Use of Steam in Producers and in Boiler-furnaces. (R. W. Raymond, Trans. A. I. M. E., xx. 635.)—No possible use of steam can cause a gain of heat. If steam be introduced into a bed of incandescent carbon it is decomposed into hydrogen and oxygen.

carbon it is decomposed into hydrogen and oxygen that absorbed by the reduction of one pound of steam to hydrogen is much greater in amount than the heat generated by the union of the oxygen thus set free with carbon, forming either carbonic oxide or carbonic acid. Consequently, the effect of steam alone upon a bed of incandescent fuel is to chill it. In every water-gas apparatus, designed to produce by means of the decomposition of steam a fuel-gas relatively free from nitrogen, the loss of heat in the producer must be compensated by some reheating device.

This loss may be recovered if the hydrogen of the steam is subsequently This loss may be recovered it the hydrogen of the steam is subsequently burned, to form steam again. Such a combustion of the hydrogen is contemplated, in the case of fuel-gas, as secured in the subsequent use of that gas. Assuming the oxidation of H to be complete, the use of steam will cause neither gain nor loss of heat, but a simple transference, the heat absorbed by steam decomposition being restored by hydrogen combustion. In practice, it may be doubted whether this restoration is ever complete. But it is contain that an excess of steam would defer the weating the But it is certain that an excess of steam would defeat the reaction altogether, and that there must be a certain proportion of steam, which permits the realization of important advantages, without too great a net loss in

heat. The advantage to be secured (in boiler furnaces using small sizes of anthracite) consists principally in the transfer of heat from the lower side of the fire, where it is not wanted, to the upper side, where it is wanted. The decomposition of the steam below cools the fuel and the grate-bars, whereas a blast of air alone would produce, at that point, intense combustion (forming at first  $CO_2$ ), to the injury of the grate, the fusion of part of

the fuel, etc.

The proportion of steam most economical is not easily determined. temperature of the steam itself, the nature of the fuel mixture, and the use or non-use of auxiliary air-supply, introduced into the gases above or

beyond the fire-bed, are factors affecting the problem. (See paper by R. J. Foster on the Use of the McClave Grate and Argand Steam Blower, etc., in Trans. A. I. M. E., xx. 625.)

Gas-fuel for Small Furnaces. E. P. Reichhelm (Am. Mach., Jan. 10, 1895) discusses the use of gaseous fuel for forge fires, for dropforging, in annealing-ovens and furnaces for melting brass and copper, for case-hardening, muffle-furnaces, and kilns. Under ordinary conditions, in such furnaces he estimates that the loss by draught, radiation, and the heating of space not occupied by work is, with coal, 80%, with petroleum 70%, and with gas above the grade of producer-gas 25%. He gives the following table of comparative cost of fuels, as used in these furnaces :

Kind of Gas.	No. of Heat- units in 1,000 cu. ft. used.	No. of Heatunits in Furnaces after Deducting 25% Loss.	Average Cost per 1,000 Ft.	Cost of 1,000,- 000 Heat- units Ob- tained in Fur- naces.
Natural gas. Coal-gas, 20 candle-power. Carburetted water-gas. Gasolene gas, 20 candle-power. Water-gas from coke. Water-gas from bituminous coal. Water-gas and producer-gas mixed. Producer-gas. Naphtha-gas, fuel 2½ gals. per 1000 ft.	675,000 646,000 690,000 313,000 377,000 185,000	506,250 484,500 517,500 234,750 282,750 138,750 112,500	\$1.25 1.00 .90 .40 .45 .20 .15	2.06 1.73 1.70 1.59 1.44 1.33
Coal, \$4 per ton, per 1,000,000 heat-unit Crude petroleum, 3 cts. per gal., per 1,	s utilized	at-units.		.73 .73

Mr. Reichhelm gives the following figures from practice in melting brass with coal and with naphtha converted into gas: 1800 lbs. of metal require with coar and with naphtna converted into gast; 1500 108.0 in the require 1080 lbs. of coal, at \$4.65 per ton, equal to \$2.51, or, say, 15 cents per 100 lbs. Mr. T.'s report: 2500 lbs. of metal require 47 gals. of naphtha, at 6 cents per gal, equal to \$2.82, or, say, 114/2 cents per 100 lbs.

### ILLUMINATING-GAS.

Coal-gas is made by distilling bituminous coal in retorts. The retort is usually a long horizontal semi-cylindrical or a shaped chamber, holding from 160 to 300 lbs. of coal. The retorts are set in "benches" of from 3 to 9, heated by one fire, which is generally of coke. The vapors distilled from the coal are converted into a fixed gas by passing through the retort,

which is heated almost to whiteness.

The gas passes out of the retort through an "ascension-pipe" into a long The gas passes one to the hydraulic main, where it deposits a proton of the tar it contains: thence it goes into a condenser, a series of iron tubes surrounded by cold water, where it is freed from condensable vapors, as ammonia-water, then into a washer, where it is exposed to jets of water, and into a scrubber, a large chamber partially filled with trays made of wood or iron, containing coke, fragments of brick or paving-stones, which are wet with a spray of water. By the washer and scrubber the gas is freed from the last portion of tar and ammonia and from some of the sulphur compounds. The gas is then finally purified from sulphur compounds by passing it through lime or oxide of iron. The gas is drawn from the hydraulic main and forced through the washer, scrubber, etc., by an exhauster or gas pump.

The kind of coal used is generally caking bituminous, but as usually this coal is deficient in gases of high illuminating power, there is added to it a

portion of cannel coal or other enricher.

The following table, abridged from one in Johnson's Cyclopedia, shows the analysis, candle power, etc., of some gas-coals and enrichers:

Gas-coals, etc.	Matter.	d Carb.		per ton 2240 lbs. cu. ft.	Candpow'r of Gas.	ton c	e per of 2240 bs.	purified bush. of incu.ft.
-	Vol. 1	Fixed	Ash.	Gas 1 of 2 in c	Cand of 6	lbs.	bush.	Gas by 1 lime
Pittsburgh, Pa Westmoreland, Pa Sterling, O. Despard, W. Va Darlington, O. Petonia, W. Va Grahamite, W. Va.	36.76 36.00 37.50 40.00 43.00 46.00 53.50	40.00 41.00	5.60 6.70 17.00 13.00	10,642 10,528 10,765	16.62 18.81 20.41 34.98 42.79 28.70	1544 1480 1540 1320 1380 1056	40 36 36 36 32 32 44	6420 3993 2494 2806 4510

The products of the distillation of 100 lbs, of average gas-coal are about as follows. They vary according to the quality of coal and the temperature of distillation.

Coke, 64 to 65 lbs.; tar, 6.5 to 7.5 lbs.; ammonia liquor, 10 to 12 lbs.; puri-

fied gas, 15 to 12 lbs.; impurities and loss, 4.5% to 3.5%. The composition of the gas by volume ranges about as follows: Hydrogen, 38% to 45%; carbonic oxide, 28 to 14%; marsh-gas (Methane,  $\mathrm{CH_4}$ ), 43% to 31%; heavy hydrocarbons ( $\mathrm{CH_4}$ ), 4, 4, 4, below, propylene, benzole vapor, etc.), 7.5% to 4.5%; nitrogen, 1% to 3%.

In the burning of the gas the nitrogen is inert; the hydrogen and carbonic oxide give heat but no light. The luminosity of the flame is due to the decomposition by heat of the heavy hydrocarbons into lighter hydrocarbons and carbon, the latter being separated in a state of extreme subdivision. By the heat of the flame this separated carbon is heated to intense whiteness, and the illuminating effect of the flame is due to the light of incandescence of the particles of carbon.

The attainment of the highest degree of luminosity of the flame depends upon the proper adjustment of the proportion of the heavy hydrocarbons (with due regard to their individual character) to the nature of the diluent

mixed therewith.

Investigations of Percy F. Frankland show that mixtures of ethylene and hydrogen cease to have any luminous effect when the proportion of ethylene does not exceed 10% of the whole. Mixtures of ethylene and carbonic oxide cease to have any luminous effect when the proportion of the former does not exceed 20%, while all mixtures of ethylene and marsh-gas have more or less luminous effect. The luminosity of a mixture of 10% ethylene and 90% marsh-gas being equal to about 18 candles, and that of one of 20% ethylene and 80% marsh-gas about 25 candles. The illuminating effect of marsh-gas alone, when burned in an argand burner, is by no means inconsiderable.

atone, when burned in an argand burner, is by no means inconsiderable. For further description, see the Treatises on Gas by King. Richards, and Huzhes; also Appleton's Cyc. Mech., vol. i. p. 900.

\*Water-gas.\* — Water-gas is obtained by passing steam through a bed of coal, coke, or charcoal heated to redness or beyond. The steam is decomposed, its hydrogen being liberated and its oxygen burning the carbon of the fuel, producing carbonic-oxide gas. The chemical reaction is,  $C + H_2O = C + C + Q_2 + 4H$ , followed by a splitting up of the CO, making 2CO + 4H. By weight the normal gas CO + 2H is composed of C + O + H = 28 parts CO and 2 parts H, or 93.3% CO and 6.6% H; by volume it is composed of equal parts of carbonic oxide and hydrogen.

by volume it is composed of equal parts of carbonic oxide and hydrogen. Water-gas produced as above described has great heating-power, but no illuminating-power. It may, however, be used for lighting by causing it to heat to whiteness some solid substance, as is done in the Welsbach incan-

descent light.

An illuminating-gas is made from water-gas by adding to it hydrocarbon gases or vapors, which are usually obtained from petroleum or some of its products. A history of the development of modern illuminating water-gas processes, together with a description of the most recent forms of apparatus, is given by Alex. C. Humphreys, in a paper on "Water-gas in the United States," read before the Mechanical Section of the British Association for Advancement of Science, in 1889. After describing many earlier patents, he states that success in the manufacture of water-gas may be said to date

from 1874, when the process of T. S. C. Lowe was introduced. All the later most successful processes are the modifications of Lowe's, the essential features of which were "an apparatus consisting of a generator and superheater internally fired; the superheater being heated by the secondary combustion from the generator, the heat so stored up in the loose brick of the superheater being used, in the second part of the process, in the fixing or rendering permanent of the hydrocarbon gases; the second part of the process consisting in the passing of steam through the generator fire, and the admission of oil or hydrocarbon at some point between the fire of the generator and the loose filling of the superheater."

generator and the loose initing of the appericator.

The water-gas process thus has two periods: first the "blow," during which air is blown through the bed coal in the generator, and the partially burned gaseous products are completely burned in the superheater, giving up a great portion of their heat to the fire-brick work contained in it, and then pass out to a chimney; second, the "rum" during which the air blast is stopped, the opening to the chimney closed, and steam is blown through the incandescent bed of the chimney closed, and steam is blown through the complete of the comp

The specific gravity of water-gas increases with the increase of the heavy hydrocarbons which give it illuminating power. The following figures, taken from different authorities, are given by F. H. Shelton in a paper on Water-gas, read before the Ohio Gas Light Association, in 1894:

Candle-power . . 19.5 20. 22.5 24. 25.4 26.3 28.3 29.6 .30 to 31.9 Sp. gr. (Air = 1). . .571 .630 .589 .60 to .67 .64 .602 .70 .65 .65 to .71

Analyses of Water-gas and Coal-gas Compared.

The following analyses are taken from a report of Dr. Gideon E. Moore on the Granger Water-gas, 1885:

	Composition by Volume,			Composition by Weight.		
	Water-gas. Coal-gas		Coal-gas.	Water-	Coal-	
	Wor- cester.	Lake.	berg.	Wor- cester.	Lake.	gas.
Nitrogen Carbonic acid	2.64 0.14 0.06	3.85 0.30 0.01	2.15 3.01	0.04402 0.00365	0.06175 0.00758	0.04559 0.09992
Oxygen	11.29	12.80	0.65 2.55 1.21	0.00114 0.18759	0.00018 0.20454	0.01569 0.05389 0.03834
Benzole vapor Carbonic oxide Marsh-gas	1.53 28.26 18.88	2.63 23.58 20.95	1.33 8.88 34.02	0.07077 0.46934 0.17928	0.11700 0.37664 0.19133	0.41087
Hydrogen	37.20	35.88	100.00	1.00000	1.00000	1.00000
Density: Theory. Practice.	0.5825 0.5915	0.6057 0.6018	0.4580			
B. T. U. from 1 cu. ft.: Water liquid. "vapor.	650.1 597.0	688.7 646.6	642.0 577.0			
Flame-temp	5311.2°F.	5281.1°F.	5202.9°F.			
Av. candle-power.	22.06	26.31			1	

The heating values (B. T. U.) of the gases are calculated from the analysis by weight, by using the multipliers given below (computed from results of

J. Thomsen), and multiplying the result by the weight of 1 cu. ft. of the gas at 62° F., and atmospheric pressure.

The flame temperatures (theoretical) are calculated on the assumption of

complete combustion of the gases in air, without excess of air.

The candle-power was determined by photometric tests, using a pressure The candie-power was determined by photometric tests, using a pressure of \$\frac{1}{2}\epsilon\$, water-column, a candle consumption of \$120 grains of spermaceti per hour, and a meter rate of 5 cu. ft. per hour, the result being corrected for a temperature of 62° F. and a banometric pressure of 30 in. It tappears that the candle-power may be regulated at the pleasure of the person in charge of the apparatus, the range of candle-power being from 20 to 29 candles, according to the manipulation employed.

#### Calorific Equivalents of Constituents of Illuminatinggag.

Water Water Water Water Liquid Vapor.	I	Ieat-units	from 1 lb.	I	Heat-units	from 1 lb.
Liquid, Vapor, Liquid, Vapor,		Water	Water	•	Water	Water
		Liquid.	Vapor.		Liquid.	Vapor.
Ethylene 21,524.4 20,134.8 Carbonic oxide 4,395.6 4,395.6	Ethylene	21,524.4	20,134.8	Carbonic oxide	4,395.6	4,395.6
Propylene 21,222.0 19,834.2 Marsh-gas 24,021.0 21,592.8	Propylene	21,222.0				
Benzole vapor 18,954.0 17,847.0 Hydrogen 61,524.0 51,804.0	Benzole vapor	18,954.0	17,847.0	Hydrogen	61,524.0	51,804:0

Efficiency of a Water-gas Plant.—The practical efficiency of an imminating water-gas setting is discussed in a paper by A. G. Glasgow (Proc. Am. Gaslight Assn., 1890), from which the following is abridged:

The results refer to 1000 cu. ft. of unpurified carburetted gas, reduced to 60° F. The total anthracite charged per 1000 cu. ft. of gas was 33.4 lbs., ash and unconsumed coal removed 9.9 lbs., leaving total combustible consumed 23.5 lbs., which is taken to have a fuel-value of 14500 B. T. U. per pound, or a total of 340,750 heat-units.

	Composition by Volume.	Weight per 100 cu, ft.	Composi- tion by Weight.	Specific Heat.
I. Carburetted Water-gas. $\begin{bmatrix} \mathrm{CO_2} + \mathrm{H_2S} \\ \mathrm{C_1H_{2a}} \\ \mathrm{CO} \\ \mathrm{CO} \\ \mathrm{CH_4} \\ \mathrm{N} \\ \end{bmatrix}$	14.6 28.0 17.0 35.6 1.0	.465842 1.139968 2.1868 .75854 .1991464 .078596	.09647 .23607 .45285 .15710 .04124 .01627	.02088 .08720 .11226 .09314 .14041 .00397
II. Uncarburetted gas.	3.5 43.4 51.8 1.3	.429065 3.389540 .289821 .102175	.1019 .8051 .0688 .0242	.45786 .02205 .19958 .23424 .00591
III. Blast products cscaping from superheater.	100.0 17.4 3.2 79.4 100.0	4.210601 2.133066 .2856096 6.2405224 8.6591980	.7207	.46178 .05342 .00718 .17585
$ \begin{tabular}{ll} IV. & Generator \\ & blast-gases. \end{tabular} \left\{ \begin{tabular}{ll} CO_2 & \dots & \\ CO & \dots & \\ N & \dots & \\ \hline \end{tabular} \right. \\ \end{tabular} $	9.7 17.8 72.5	1.189123 1.390180 5.698210 8.277513	.1436 .1680 .6884	.031075 .041647 .167970

The heat energy absorbed by the apparatus is  $23.5 \times 14,500 = 340,750$  heatunits = A. Its disposition is as follows:

P, the energy of the CO produced;C, the energy absorbed in the decomposition of the steam;

D, the difference between the sensible heat of the escaping illuminatinggases and that of the entering oil;

E, the heat carried off by the escaping blast products;

F, the heat lost by radiation from the shells;

G, the heat carried away from the shells by convection (air-currents);

H, the heat rendered latent in the gasification of the oil;
L the sensible heat in the ash and unconsumed coal recovered from the generator.

The heat equation is A = B + C + D + E + F + G + H + I; A being known. A comparison of the CO in Tables I and II show that  $\frac{200}{434}$ , or 64.5% of the volume of carburetted gas is pure water-gas, distributed thus: CO  $_2$  , 2.3%; CO, 28.0%; H, 33.4%; N, 0.8%; = 64.5%. 1 b. of CO at 60° F. = 13.531 cu. ft. CO per 1000 cu. ft. of gas = 280 - 13.531 cu. 9.094 lbs. Energy of the CO = 20.094  $\times$  4395.6 = 91,043 heat-units, = B. 1 lb. of H at 60° F. = 189.2 cu. ft. H per M of gas = 334 + 189.2 = 1.7653 lbs. Energy of the H per lb. (according to Thomsen, considering the steam generated by its combustion to be condensed to water at 75° F.) = 61,534 B. T. U. in Mr. Glasgow's experiments the steam entered the generator at 33° F.; the heat required to raise the product of combustion of 1 lb, of H, viz., 8.98 lbs, H<sub>2</sub>O, from water at 75° to steam at 331° must therefore be deducted from Thomsen's figure, or  $61,524 - (8.98 \times 1140.2) = 51,285$  B. T. U. per lb, of H. Energy of the H, then, is  $1.7653 \times 51,285 = 90,533$  heat-units, = C. The heat lost due to the sensible heat in the illuminating gases, their temperature being 1450° F., and that of the entering oil  $235^\circ$  F., is 48.29 (weight)  $\times$  .45786 sp. heat  $\times$  1215 (rise of temperature) = 26,864 heat -units = D.

(The specific heat of the entering oil is approximately that of the issuing

gas.)
The heat carried off in 1000 cu. ft. of the escaping blast products is 86.592 (weight) × .23645 (sp. heat) × 1474° (rise of temp.) = 30,180 heat-units: the temperature of the escaping blast gases being 1550° F., and that of the entering air 76° F. But the amount of the blast gases, by registration of an anemometer, checked by a calculation from the analyses of the blast gases, was 2457 cubic feet for every 1000 cubic feet of carburetted gas made. Hence the heat carried off per M. of carburetted gas is  $30,180 \times 2.457 = 74,152$  heat-units = E.

Experiments made by a radiometer covering four square feet of the shell of the apparatus gave figures for the amount of heat lost by radiation = 13.454 heat-units = F, and by convection = 15.696 heat-units = G.

The heat rendered latent by the gasefication of the oil was found by taking the difference between all the heat fed into the carburetter and superheater and the total heat dissipated therefrom to be 12,841 heat-units = H. The sensible heat in the ash and unconsumed coal is 9.9 lbs. × 1500° × .25 (sp. ht.) = 3712 heat-units = I.

The sum of all the items B+C+D+E+F+G+H+I=327,295 heatunits, which substracted from the heat energy of the combustible consumed, 340,750 heat-units, leaves 13,455 heat-units, or 4 per cent, unaccounted for.

Of the total heat energy of the coal consumed, or 340,750 heat-units, the energy wasted is the sum of items D, E, F, G, and I, amounting to 132,878 heat-units, or 39 per cent; the remainder, or 207,872 heat-units, or 61 per cent, being utilized. The efficiency of the apparatus as a heat machine is

therefore 61 per cent.

Five gallons, or 35 lbs. of crude petroleum were fed into the carburetter per 1000 cu. ft. of gas made; deducting 5 lbs. of tar recovered, leaves 30 lbs.  $\times$  20,000 = 600,000 heat-units as the net heating value of the petroleum used. Adding this to the heating value of the coal, 340,750 B. T. U., gives 940,750 heat-units, of which there is found as heat energy in the carburetted gas, as in the table below, 764,050 heat units, or 81 per cent, which is the commercial efficiency of the apparatus, i.e., the ratio of the energy contained in the finished product to the total energy of the coal and oil consumed.

The heating power per M. cu. ft. of 1 The heating power per M. of the the carburetted gas is uncarburetted gas is  $CO_2$ 35.0  $434.0 \times .078100 \times 4395.6 = 148991$  $\begin{array}{c} 280.0 \times .078100 \times 4395.6 = 96120 \text{ H} \\ 170.0 \times .044620 \times 24021.0 = 182210 \text{ N} \\ 356.0 \times .005594 \times 61524.0 = 122520 \end{array}$  $518.0 \times .005594 \times 61524.0 = 178277$ CH4 13.0 N 10.0 1000.0 327268 764050

<sup>\*</sup> The heating value of the illuminants CnH2n is assumed to equal that of C<sub>3</sub>H<sub>6</sub>.

The candle-power of the gas is 31, or 6.2 candle-power per gallon of oil sed. The calculated specific gravity is .6355, air being 1.

used. The calculated specific gravity is 10000, an oring 1. For description of the operation of a modern carburetted water-gas plant, see paper by J. Stelfox, Eng'g, July 20, 1894, p. 89.

Space required for a Water-gas Plant.—Mr. Shelton, taking

15 modern plants of the form requiring the most floor-space, figures the average floor-space required per 1000 cubic feet of daily capacity as follows:

Water-gas Plants of Capacity Require an Area of Floor-space for in 24 hours of each 1000 cn ft of about

100,000	cubic	feet		 	4 sau	are feet.
200,000	66	66				
400,000	6.6	"		 	2.75 "	
600,000	44	"		 	2 to 5	2.5 sq. ft.
7 to 10	millio	n cubic	feet	 	1.25 to	1.5 sq. ft.

These figures include scrubbing and condensing rooms, but not boiler and engine rooms. In coal-gas plants of the most modern and compact forms one with 16 benches of 9 retorts each, with a capacity of 1,500,000 cubic feet per 24 hours, will require 4.8 sq. ft. of space per 1000 cu. ft. of gas, and one of 6 benches of 6 retorts each, with 300,000 cu. t. capacity per 24 hours will require 6 sq. ft. of space per 1000 cu. ft. The storage-room required for the gas-making materials er: 100 cu. ft. cubic feet of gas made; for water-gas made from coke, I cubic foot of room for every 373 cu. ft. of gas made; and for water-gas made from anthracite, I cu. ft. of room for every 645 cu. ft. of gas made.

The comparison is still more in favor of water-gas if the case is considered

of a water-gas plant added as an auxiliary to an existing coal-gas plant, for, instead of requiring further space for storage of coke, part of that already required for storage of coke produced and not at once sold can be cut off, by reason of the water-gas plant creating a constant demand for more or less of the coke so produced.

Mr. Shelton gives a calculation showing that a water-gas of .625 sp. gr. would require gas-mains eight per cent greater in diameter than the same quantity coal-gas of .425 sp. gr. if the same pressure is maintained at the holder. The same quantity may be carried in pipes of the same diameter if the pressure is increased in proportion to the specific gravity. With the same pressure the increase of candle-power about balances the decrease of flow. With five feet of coal-gas, giving, say, eighteen candle-power, 1 cubic foot equals 3.6 candle-power; with water-gas of 23 candle-power, 1 cubic foot equals 4.6 candle-power, and 4 cubic feet gives 18.4 candle-power, or more than is given by 5 cubic feet of coal-gas. Water-gas may be made from oven-coke or gas-house coke as well as from anthracite coal. A watergas plant may be conveniently run in connection with a coal-gas plant, the surplus retort coke of the latter being used as the fuel of the former.

In coal-gas making it is impracticable to enrich the gas to over twenty candle-power without causing too great a tendency to smoke, but water-gas of a high as thirty candle-power is quite common. A mixture of coal-gas and water-gas of a higher C.P. than 20 can be advantageously distributed.

Fuel-value of, Illuminating-gas.—E. G. Love (School of Mines Qtly, January, 1892) describes F. W. Hartley's calorimeter for determining the calorific power of gases, and gives results obtained in tests of the carthe catoring ower or gases, and gives results obtained in tests of the cap-buretted water-gas made by the municipal branch of the Consolidated Co. of New York. The tests were made from time to time during the past two years, and the figures give the heat-units per cubic foot at 60° F. and 30 inches pressure: 715, 603, 725, 732, 691, 738, 735, 703, 734, 730, 731, 737. Average, 721 heat units. Similar tests of mixtures of coal- and water-gases made by other branches of the same company give 694, 715, 684, 692, 727, 665, 695, and 686 heat-units per foot, or an average of 694.7. The average of all these tests was 710.5 heat-units, and this we may fairly take as representing the calorific power of the Illuminating gas of New York. One thousand feet of this gas, costing \$1.25, would therefore yield 710,500 heat-units, which would be equivalent to 565,460 heat-units for \$1.00.

The common coal-gas of London, with an illuminating power of 16 to 17 candles, has a calorific power of about 668 units per foot, and costs from 60

to 70 cents per thousand.

The product obtained by decomposing steam by incandescent carbon, as effected in the Motay process, consists of about 40% of CO, and a little over 50% of H.

This mixture would have a heating-power of about 300 units per cubic foot. and if sold at 50 cents per 1000 cubic feet would furnish 600,000 units for \$1.00, as compared with 568,400 units for \$1.00 from illuminating gas at \$1.25 per 1000 cubic feet. This illuminating gas if sold at \$1.15 per thousand would therefore be a more economical heating agent than the fuel-gas mentioned, at 50 cents per thousand, and be much more advantageous than the latter, in that one main, service, and meter could be used to furnish gas for both lighting and heating.

A large number of fuel-gases tested by Mr. Love gave from 184 to 470 heat-

A large number of rulergases tested by arr. Love gave from 184 to 440 heat-units per foot, with an average of 309 units.

Taking the cost of heat from illuminating-gas at the lowest figure given by Mr. Love, viz., \$1.00 for 600,000 heat-units, it is a very expensive fuel, equal to coal at \$40 per ton of 2000 flbs, the coal having a calorific power of only 12,000 heat-units per pound, or about \$35 of that of pure carbon:

600,000 : (12,000 × 2000) :: \$1 : \$40.

### FLOW OF GAS IN PIPES.

The rate of flow of gases of different densities, the diameter of pipes required, etc., are given in King's Treatise on Coal Gas, vol. ii. 374, as follows:

Molesworth gives  $Q = 1000 \sqrt{\frac{d^5h}{al}}$ .

J. P. Gill, Am. Gas-light Jour. 1894, gives 
$$Q=1291\sqrt{\frac{d^3h}{s(l+d)}}$$
.

This formula is said to be based on experimental data, and to make allowance for obstructions by tar, water, and other bodies tending to check the flow of gas through the pipe.

A set of tables in Appleton's Cyc. Mech. for flow of gas in 2, 6, and 12 in. pipes is calculated on the supposition that the quantity delivered varies

as the square of the diameter instead of as  $d^2 \times \sqrt[3]{d}$ , or  $\sqrt[3]{d^3}$ . These tables give a flow in large pipes much less than that calculated by the formulæ above given, as is shown by the following example. Length of pipe 100 yds., specific gravity of gas .042, pressure 1-in. water-column.

An experiment made by Mr. Clegg, in London, with a 4-in. pipe, 6 miles long, pressure 3 in. of water, specific gravity of gas. 398, gave a discharge into the amosphere of 852 cu. ft. per hour, after a correction of 35 cu. ft. was made for leakage.

Substituting this value, 852 cu. ft., for Q in the formula Q=C  $\sqrt{d^5h+sl}$ , we find C, the coefficient, = 997, which corresponds nearly with the formula given by Molesworth.

### Services for Lamps. (Molesworth.)

1.5	Ft. from	Require		Ft. from	Require
Lamps.	Main.	Pipe-bore.	Lamps.	Main.	Pipe-bore.
2	40	3% in.	15	130	1 in.
4	40	½ in.	20	150	11/4 in.
	50	5% in.	25	180	11/2 in.
	100	3/4 in.		200	13% in.

(In cold climates no service less than 34 in. should be used.)

# Maximum Supply of Gas through Pipes in cu. ft. per Hour, Specific Gravity being taken at .45, calculated from the Formula $Q = 1000 \sqrt{d^3h} + sI_*$ (Molesworth.)

### LENGTH OF PIPE = 10 YARDS.

Diameter of Pipe in	Pressure by the Water-gauge in Inches.									
Inches.	.1	.2	.8	.4	.5	.6	.7	.8	.9	1.0
36 1/2 3/4	13 26 73	18 37 103	22 46 126	26 53 145	29 59 162	31 64 187	34 70 192	36 74 205	38 79 218	41 83 230
1 11/4 11/4 11/2 2	149 260 411	211 368 581	258 451 711	298 521 821	333 582 918	365 638 1006	394 689 1082	422 737 1162	447 781 1232	471 823 1299
2,2	843	1192	1460	1686	1886	2066	2231	2385	2530	2667

### LENGTH OF PIPE = 100 YARDS.

		Pressure by the Water-gauge in Inches.											
	.1	1 .2 .3 .4 .5 .75 1.0 1.25 1.5 2 2.5											
1/6 3/4	8 23	12 32	14 42	17 46	19 51	23 68	26 73	29 81	32 89	36 103	· 42		
1	47 82	67 116	85	94 165	105 184	129 225	149 260	167 291	183 319	211 368	236 412		
11/4 11/2 2	130 267	184 377		260 533	290 596	356 730	411 843	459 943,	503 1033	581 1193	649 1333		
21/2	466 735	659 1039	807 1270	932 1470	1042 1643	1276 2012	1473 2323	1647 2598	1804 2846	2083 3286	2329 3674		
3½ 4		$\frac{1528}{2133}$	$\frac{1871}{2613}$	$\frac{2161}{3017}$	2416 3373	2958 4131	3416 4770	3820 5333	4184 5842	4831 6746	5402 7542		

#### LENGTH OF PIPE = 1000 VARDS.

		Pressure by the Water-gauge in Inches.											
	.5	.5 .75 1.0 1.5 2.0 2.5 3.0											
1	38	41	47	58	67	75	82						
1½	92	113	130	159	184	205	226						
2	189	231	267	327	377	429	462						
2½	329	403	466	571	659	737	807						
3	520	636	735	900	1039	1162	1273						
4	1067	1306	1508	1847	2133	2385	2613						
5	1863	2282	2635	3227	3727	4167	4564						
6	2939	3600	4157	5091	5879	6573	7200						

LENGTH OF PIPE = 5000 YARDS.

Diameter of Pipe	Pressure by the Water-gauge in Inches.								
Inches.	1.0	1.5	2.0	2.5	3.0				
2 3	119	146	169	189	207				
3	329	402	465	520	569				
4	675	826	955	1067	1168				
5	1179	1443	1667	1863	2041				
4 5 6 7	1859	2277	2629	2939	3220				
7	2733	3347	3865	4321	4734				
8 9	3816	4674	5397	6034	6610				
9	5123	6274	7245	8100	8873				
10	6667	8165	9428	10541	11547				
12	10516	12880	14872	16628	18215				

Mr. A. C. Humphreys says his experience goes to show that these tables give too small a flow, but it is difficult to accurately check the tables, on account of the extra friction introduced by rough pipes, bends, etc. For bends, one rule is to allow 1/42 of an inch pressure for each right-angle bend.

Where there is apt to be trouble from frost it is well to use no service of less diameter than 34 in., no matter how short it may be. In extremely cold climates this is now often increased to 1 in., even for a single lamp. The best practice in the U.S. now condemns any service less than 3/4 in.

# STEAM.

The Temperature of Steam in contact with water depends upon the pressure under which it is generated. At the ordinary atmospheric pressure (14.7 lbs. per sq. in.) its temperature is 212° F. As the pressure is increased, as by the steam being generated in a closed vessel, its temperature, and that of the water in its presence, increases,

Saturated Steam is steam of the temperature due to its pressurenot superheated.

Superheated Steam is steam heated to a temperature above that due to its pressure. Dry Steam is steam which contains no moisture. It may be either

saturated or superbeated.

Wet Steam is steam containing intermingled moisture, mist, or spray, It has the same temperature as dry saturated steam of the same pressure.

Water introduced into the presence of superheated steam will flash into vapor until the temperature of the steam is reduced to that due its pressure. Water in the presence of saturated steam has the same temperature as the steam. Should cold water be introduced, lowering the temperature of the whole mass, some of the steam will be condensed, reducing the pressare and temperature of the remainder, until an equilibrium is established.

Temperature and Pressure of Saturated Steam.—The relation between the temperature and the pressure of steam, according to Regnault's experiments, is expressed by the formula (Buchanan's, as given by Clarks).

by Clark)  $t = \frac{8000.10}{6.1993544 - \log p} - 371.85$ , in which p is the pressure in pounds

6.1993544 —  $\log p$  per square inch and the temperature of the steam in Fahrenheit degrees. It applies with accuracy between  $120^{\circ}$  F. and  $446^{\circ}$  F., corresponding to pressures of from 1.68 lbs. to 445 bs. per square inch. (For other formulæ see Wood's and Peabody's Thermodynamics.)

Total Heat of Saturated Steam (above  $32^{\circ}$  F.).—According to Regnault's experiments, the formula for total heat of steam is H=1091.7+309(t-32), in which t is temperature Fahr, and H the heat-units. (Rankine and many others; Clark gives 1091.7+3091.

mula, in Fahrenheit units, as given by Clark, is  $L = 1092.6 - .708(t - 32^{\circ})$ .

The total heat in steam (above 32°) includes three elements: 1st. The heat required to raise the temperature of the water to the tem-

internal latent heat. 3d. The latent heat of volume, or the external work done by the steam in

2d. The heat required to evaporate the water at that temperature, called

making room for itself against the pressure of the superincumbent atmosphere (or surrounding steam if inclosed in a vessel).

The sum of the last two elements is called the latent heat of steam. In Buel's tables (Weisbach, vol. ii., Dubois's translation) the two elements are

given separately.

perature of the steam.

Latent Heat of Volume of Saturated Steam. (External Work.)-The following formulas are sufficiently accurate for occasional use within the given ranges of pressure (Clark, S. E.):

From 14.7 lbs. to 50 lbs. total pressure per square inch... 55.900 + .0772t. From 50 lbs. to 200 lbs. total pressure per square inch... 59.191 + .0655t.

### Heat required to Generate 1 lb. of Steam from water at 32° F.

Heat-units. Sensible heat, to raise the water from 32° to 212° = .... 180.9 Latent heat, 1, of the formation of steam at 212° = .... 894.0 2, of expansion against the atmospheric pressure, 2116.4 lbs. per sq. ft. ×26.36 cu. ft. = 55,786 foot-pounds ÷ 778 = ..... 965.7 Total heat above 32° F..... 1146.6

The Heat Unit, or British Thermal Unit.-The definition of the heat-unit used in this work is that of Rankine, accepted by most modern writers, viz., the quantity of heat required to raise the temperature of 1 lb. of water 1° F. at or near its temperature of maximum density (39.1° F.) Peabody's definition, the heat required to raise a pound of water from 62° to 63° F. is not generally accepted. (See Thurston, Trans. A. S. M. E., xiii. 351.)

Specific Heat of Saturated Steam .- The specific heat of saturated steam is .305, that of water being 1; or it is 1.281, if that of air be 1. The expression .305 for specific heat is taken in a compound sense, relating to changes both of volume and of pressure which takes place in the eleva-

tion of temperature of saturated steam. (Clark, S. E.)

This statement by Clark is not strictly accurate. When the temperature of saturated steam is elevated, water being present and the steam remaining saturated, water is evaporated. To raise the temperature of 1 lb. of water 1° F. requires 1 thermal unit, and to evaporate it at 1° F. higher would require 0.695 less thermal unit, the latent heat of saturated steam decreasing 0.695 B.T.U. for each increase of temperature of 1° F. Hence 0.305 is the specific heat of water and its saturated vapor combined.

When a unit weight of saturated steam is increased in temperature and in

pressure, the volume decreasing so as to just keep it saturated, the specific heat is negative, and decreases as temperature increases. (See Wood, Therm., p. 147; Peahody, Therm., p. 93.)

Density and Volume of Saturated Steam.—The density of

steam is expressed by the weight of a given volume, say one cubic foot; and the volume is expressed by the number of cubic feet in one pound of steam. Mr. Brownlee's expression for the density of saturated steam in terms of

p.941 the pressure is  $D = \frac{p}{330.36}$ , or log  $D = .941 \ p - 2.519$ , in which D is the den-

sity, and p the pressure in pounds per square inch. In this expression,  $p^{*94}$  is the equivalent of p raised to the 16/17 power, as employed by Rankine. The volume v being the reciprocal of the density,

$$v = \frac{330.36}{p^{.941}}$$
, or  $\log v = 2.519 - .941 \log p$ .

Relative Volume of Steam .- The relative volume of saturated steam is expressed by the number of volumes of steam produced from one

volume of water, the volume of water being measured at the temperature 39° F. The relative volume is found by multiplying the volume in cu. ft. of one lb, of steam by the weight of a cu, ft, of water at 39° F., or 62.425 lbs.

Gaseous Steam .- When saturated steam is superheated, or surcharged with heat, it advances from the condition of saturation into that of gaseity. The gaseous state is only arrived at by considerably elevating the

gaseny. In gaseons state is only arrived at by considerably elevating the temperature, supposing the pressure remains the same. Steam thus sufficiently superheated is known as gaseous steam or steam gas.

Total Heat of Gaseous Steam,—Regnault found that the total heat of gaseous steam increased, like that of saturated steam, uniformly with the temperature, and at the rate of .475 thermal units per pound for

The general feature, under a constant pressure.

The general formula for the total heat of gaseous steam produced from 1 pound of water at 33° F. is H=1074.6+4.75t. [This formula is for vapor generated at 32°. It is not true if generated at 212°, or at any other temperature than 33°. (Prof. Wood.)]

thre than 32°. (Prof. Wood.)]

The Specific Heat of Gaseous Steam is .475, under constant pressure, as found by Regnault. It is identical with the coefficient of increase of total heat for each degree of temperature. [This is at atmospheric pressure and 312° temperature. He found it not true for any other pressure. Theory indicates that it would be jess at higher temperatures. [Prof. Wood.)]

The Specific Density of Gaseous Steam is .62, that of air being 1. That is to say, the weight of a cubic foot of gaseous steam is about five eighbles of that of a cubic foot of are mere and temperature.

The density or weight of a cubic foot of gaseous steam is expressible by the same formula as that of air, except that the multiplier or coefficient is less in proportion to the less specific density. Thus,

$$D' = \frac{2.7074p \times .622}{t + 461} = \frac{1.684p}{t + 461},$$

in which D' is the weight of a cubic foot of gaseous steam, p the total pressure per square inch, and t the temperature Pahrenheit. Superheated Steam.—The above remarks concerning gaseous steam are taken from Clark's Steam engine. Wood gives for the total heat (above 32) of superheated steam  $H = 1091.7 + 0.48(t - 32^o)$ .

The following is abridged from Peabody (Therm., p. 115, etc.).

When far removed from the temperature of saturation, superheated steam follows the laws of perfect gases very nearly, but near the temperature of saturation the departure from those laws is too great to allow of calculations by them for engineering purposes.

The specific heat at constant pressure, Cp, from the mean of three experi-

ments by Regnault, is 0.4805.

Values of the ratio of Cp to specific heat at constant volume:

100 Pressure p, pounds per square inch.. 50 200 300 Ratio  $Cp \div Cv = k = 1.335 \ 1.332 \ 1.330 \ 1.324$ 1.316

Zeuner takes k as a constant = 1.333.

SPECIFIC HEAT AT CONSTANT VOLUME, SUPERHEATED STEAM.

200 300 .344

It is quite as reasonable to assume that  $C_v$  is a constant as to suppose that Cp is constant, as has been assumed. If we take Cv to be constant, then Cp will appear as a variable.

If p = pressure in lbs. per sq. ft., v = volume in cubic feet, and T =temperature in degrees Fahrenheit + 460.7, then  $pv = 93.5T - 971p_4$ .

Total heat of superheated steam,  $H = 0.4805(T - 10.38p^{\frac{1}{2}}) + 857.2$ .

The Rationalization of Regnault's Experiments on Steam. (J. McFarlane Gray, Proc. Iust. M. E., July, 1889.)--The formulæ constructed by Regnault are strictly empirical, and were based entirely on his experiments. They are therefore not valid beyond the range of temper-

atures and pressures observed

Mr. Gray has made a most elaborate calculation, based not on experiments but on fundamental principles of thermodynamics, from which he deduces formulæ for the pressure and total heat of steam, and presents tables calcu662 STEAM.

lated therefrom which show substantial agreement with Regnault's figures. He gives the following examples of steam-pressures calculated for temperatures beyond the range of Regnault's experiments.

Tempe	rature.	Pounds per	Tempe	rature.	Pounds per sq. in.	
C.	Fahr.	sq. in.	C.	Fahr		
230 240 250 260 280 300 320	446 464 482 500 536 572 608	406.9 488.9 579.9 691.6 940.0 1261.8 1661.9	340 360 380 400 415 427	644 680 716 752 779 800.6	2156.2 2742.5 3448.1 4300.2 5017.1 5659.9	

These pressures are higher than those obtained by Regnault's formula.

which gives for 415° C. only 4067.1 lbs. per square inch.

Table of the Properties of Saturated Steam.—In the table Table of the Properties of Saturated Steam.—In the table of properties of saturated steam on the following pages the figures for temperature, total heat, and latent heat are taken, up to 210 lbs. absolute pressure, from the tables in Porter's Steam-engine Indicator, which tables have been widely accepted as standard by American engineers. The figures for total heat, given in the original as from 0° F., have been changed to heat above 32° F. The figures for weight per cubic foot and for cubic feet per pound have been taken from Dwelshauvers-Derry's table, Trans. A. S. M. E., vol. xi., as being probably more accurate than those of Porter. The figures for relative volume are from Buel's table, in Dubois's translation of Weisbach, vol. ii. They agree quite closely with the relative volumes calculated from weights as given by Dery. From 211 to 219 lbs. the figures for temperature, total heat, and latent heat are from Dery's table; and from 220 to 1000 lbs. all the figures are from Buel's table. The figures have not been carried out to as many declinal places as they are in most of the tables given by the different authorities; but any figure beyond the fourth significant figure is unnecessary in practice, and beyond the limit of error of the observations and of the formulæ from which the figures were derived.

Weight of 1 Cubic Foot of Steam in Decimals of a Pound. Comparison of Different Authorities.

ssure, sr sq. in	Weight of 1 cubic foot according to—						w	bic foo	ot		
Absol Press Ibs. per	Por- ter.	Clark	Buel.	Dery.	Pea- body.	Absolute Pressure 1bs. per sq.	Por- ter.	Clark	Buel.	Dery.	Pea- body
-1	.0030	.003	.00303	.00299			.27428	.2738	.2735	.2724	
14.7 20	.03797	.0380		.0507	.0376	140 160	.31386	.3162	.3163	.3147	
40	.0994	.0974	.0972	.0972	.0964	180	.38895	.4009	.4012	.3983	.3945
60	.1457		.1424	.1422	.1409	200	.42496		.4433	.4400	
80	.19015			.1862	.1843	220		.4842	.4852		.4772
100	.23302	.2307	.2303	1.2296	.2271	240		.5248	.5270		.5186

There are considerable differences between the figures of weight and volume of steam as given by different authorities. Porter's figures are based on the experiments of Fairbairn and Tate. The figures given by the other authorities are derived from theoretical formulæ which are believed to give more reliable results than the experiments. The figures for temperature, total heat, and latent heat as given by different authorities show a practical agreement, all being derived from Regnault's experiments. See Peabody's Tables of Saturated Steam; also Jacobus, Trans. A. S. M. E., vol. xii, 593.

a roperties of Saturated Section											
Vacuum Gauge, Inches of Mer- cury.	Press- per nch.	ure eit.	Total above		at L.	Relative Volume. Vol. of Water at 39° F. = 1.	Volume. Cu. ft. in I lb. of Steam.	1 cu. n, lb.			
am o	bsolute Pres ure, lbs. per square inch.	emperature Fahrenheit.	In the Water	In the Steam	atent Heat $I = H - h$ . Heat-units.	vol. of vat 39° F.	ne. b. of	ht of Stean			
Vacuum Inches cury.	Absolute Pressure, lbs. per square inch.	Temperature Fahrenheit.	h Heat- units.	Heat- units.	1	Relat Vol at 3	Volur in 11	Weight of 1 cu. ft. Steam, lb.			
29.74 29.67	.089 .122	32 40 50 60	0 8.	1091.7 1094.1	1091.7 1086.1 1079.2 1072.2	208080 154330	3333.3 2472.2	.00030			
29.56 29.40	.122 .176 .254	50 60	18. 28.01	1097.2 1100.2		107630 76370	2472.2 1724.1 1223.4	.00058 .00082			
29.19 28.90 28.51	.359 .502	70 80	38.02 48.04	1103.3 1106.3	1065.3 1058.3 1051.3	54660 39690	875.61 635.80	.00115 .00158			
28.51 28.00	.692 .943	90 100	58.06 68.08	1109.4 1112.4	1051.3 1044.4	29290 21830	469.20 349.70	.00213			
27.88 25.85	1 2 3 4	102.1 126.3 141.6 153.1	70.09 94.44 109.9	1113.1 1120.5	1043.0 1026.0	20623 10730	334.23 173.23 117.98 89.80	.00299 .00577			
23.83 21.78	3 4	141.6 153.1	109.9 121.4	1125.1 1128.6	1026.0 1015.3 1007.2	7325 5588	117.98 89.80	.00848 .01112			
19.74 17.70	5 6	162.3 170.1 176.9 182.9	130.7 138.6	1131.4 1133.8	1000.7 995.2	4530 3816	72.50 61.10 53.00	.01373 .01631			
17.70 15.67 13.63 11.60	5 6 7 8 9	176.9 182.9 188.3	138.6 145.4 151.5 156.9	1135.9 1137.7 1139.4	990.5 986.2 982.4	3302 2912 2607	53.00 46.60 41.82	.01887 .02140 .02391			
	10 11	193.2 197.8	161.9 166.5	1140.9 1142.3	ł.	2361	37.80 34.61	.02641			
9.56 7.52 5.49 3.45	11 12 13 14	197.8 202.0 205.9	166.5 170.7 174.7	1142.3 1143.5 1144.7	979.0 975.8 972.8 970.0	2159 1990	34.61 31.90 29.58	.02889 .03136 .03381			
1.41		209.6	178.4	1145.9	967.4	1846 1721	27.59	.03625			
Gauge Pressure lbs. per sq. in.	14.7	212	180.9	1146.6	965.7	1646	26,36	.03794			
0.304 1.3	15 16	213.0 216.3	181.9 185.3	1146.9 1147.9 1148.9 1149.8	965.0 962.7	1614 1519 1434 1359	25.87 24.33	.03868 .04110			
1.3 2.3 3.3 4.3	16 17 18 19	219.4 222.4 225,2	188.4 191.4 194.3	1148.9 1149.8 1150.6	960.5 958.3 956.3	1434 1359 1292	25.87 24.33 22.98 21.78 20.70	.04352 .04592 .04831			
	20	227.9	197.0 199.7		954.4			.05070			
5.3 6.3 7.3 8.3 9.3	21 22 23	230.5 233.0 235.4	199.7 202.2 204.7	1151.5 1152.2 1153.0 .7	952.6 950.8 949.1	1231 1176 1126 1080 1038	19.72 18.84 18.03 17.30 16.62	.05308 .05545 .05782			
	24	237.8	207.0	1154.5	947.4			.06018			
10.3 11.3 12.3	25 26 27 28 29	240.0 242.2 244.3	209.3 211.5 213.7	.8 1156.4	945.8 944.3 942.8	998.4 962.3 928.8	15.99 15.42 14.88 14.38	.06253 .06487 .06721			
11.3 12.3 13.3 14.3	28 29	244.3 246.3 248.3	213.7 215.7 217.8	1157.1	942.8 941.3 939.9	928.8 897.6 868.5	14.38 13.91	.06955 .07188			
15.3 16.3	30 31	250.2 252.1	219.7 221.6	1158.3	938.9 937.2	841.3 815 8	13.48 13.07	.07420			
15.3 16.3 17.3 18.3 19.3	30 31 32 33 34	252.1 254.0 255.7 257.5	219.7 221.6 223.5 225.3 227.1	.8 1159.4 .9 1160.5	935.9 934.6 933.4	791.8 769.2 748.0	13.48 13.07 12.68 12.32 11.98	.07652 .07884 .08115 .08346			
20.3 21.3		259.2	228 8	1161.0	932.2	727.9	11.66	.08576			
21.3 22.3	35 36 37	260.8 262.5	230.5 232.1	1161.5 1162.0	931.0 929.8	708.8 690.8	11.36 11.07	.08806			

Total Heat   Section   S		Properties of Saturated Steam.										
23.3   38   261.0   233.8   1162.5   928.7   673.7   10.79   0.0264	sure, q. in.	ess- per ch.	it.	Total above	Heat 32° F.	t L.	hume. ater = 1.	Ju. ft. Steam	, lb.			
23.3   38   261.0   233.8   1162.5   928.7   673.7   10.79   0.9264   243.8   39   265.6   235.4   9   927.6   675.5   10.53   .09493   285.8   41   268.6   238.5   1.69.5   928.7   673.7   10.79   0.9264   267.5   268.3   41   268.6   238.5   1.99.5   4   627.3   3   10.5   0.8949   27.3   42   270.1   240.0   1164.3   924.4   613.3   9.83   1018   229.8   44   272.9   242.9   1163.2   922.3   587.0   9.61   1.063   293.3   44   272.9   242.9   1163.2   922.3   587.0   9.61   1.063   30.3   45   277.3   244.3   245.7   1166.2   922.3   587.0   9.61   1.063   31.3   46   275.7   245.7   1166.2   922.3   587.0   9.61   1.063   33.3   46   275.7   245.7   1166.2   922.3   587.0   9.61   1.063   33.3   46   275.7   245.7   1166.2   917.5   530.5   8.50   1176   333.3   48   278.3   248.4   8   919.4   551.7   8.84   1133   34.8   49   279.6   249.7   1167.2   917.5   530.5   8.50   1176   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.67   1153   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.67   1153   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.19   1221   373.3   56   283.3   255.5   7.7   914.0   492.8   7.90   1263   39.3   54   285.7   256.0   1169.1   913.1   484.2   7.76   1288   44.3   56   288.1   259.5   1170.1   910.6   400.2   7.38   1353   44.3   58   290.3   261.5   517.0   8.99   1264   44.3   58   290.4   261.8   8.909.0   445.5   7.14   400.2   44.3   58   290.4   261.8   8.909.0   445.5   7.14   400.2   44.3   56   285.7   266.1   7.8   909.5   485.5   7.76   1288   44.3   58   290.3   262.9   117.2   908.2   438.5   7.76   1288   43.3   56   285.7   286.1   250.5   1170.1   910.6   400.2   7.38   1355   433.3   66   292.5   262.9   117.2   908.2   438.5   7.76   1288   43.3   58   290.3   266.2   1172.1   900.6   446.5   6.63   1353   66   298.8   290.3   360.9   379.3   400.0   6.66   6.53   1357   6.62   294.7   266.1   8.900.0   379.3   6.09   344.5   6.77   14.00   344.3   66   296.8   296.2   2172.1   908.2   438.5   6.17   1621   56.3   77   200.6   277.3	Pres	bs. ]	ratu	In the	In the	Hes - h.	of Wo	of;	eam			
23.3   38   261.0   233.8   1162.5   928.7   673.7   10.79   0.9264   243.8   39   265.6   235.4   9   927.6   675.5   10.53   .09493   285.8   41   268.6   238.5   1.69.5   928.7   673.7   10.79   0.9264   267.5   268.3   41   268.6   238.5   1.99.5   4   627.3   3   10.5   0.8949   27.3   42   270.1   240.0   1164.3   924.4   613.3   9.83   1018   229.8   44   272.9   242.9   1163.2   922.3   587.0   9.61   1.063   293.3   44   272.9   242.9   1163.2   922.3   587.0   9.61   1.063   30.3   45   277.3   244.3   245.7   1166.2   922.3   587.0   9.61   1.063   31.3   46   275.7   245.7   1166.2   922.3   587.0   9.61   1.063   33.3   46   275.7   245.7   1166.2   922.3   587.0   9.61   1.063   33.3   46   275.7   245.7   1166.2   917.5   530.5   8.50   1176   333.3   48   278.3   248.4   8   919.4   551.7   8.84   1133   34.8   49   279.6   249.7   1167.2   917.5   530.5   8.50   1176   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.67   1153   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.67   1153   333.3   51   282.1   292.2   1168.0   915.7   510.9   8.19   1221   373.3   56   283.3   255.5   7.7   914.0   492.8   7.90   1263   39.3   54   285.7   256.0   1169.1   913.1   484.2   7.76   1288   44.3   56   288.1   259.5   1170.1   910.6   400.2   7.38   1353   44.3   58   290.3   261.5   517.0   8.99   1264   44.3   58   290.4   261.8   8.909.0   445.5   7.14   400.2   44.3   58   290.4   261.8   8.909.0   445.5   7.14   400.2   44.3   56   285.7   266.1   7.8   909.5   485.5   7.76   1288   44.3   58   290.3   262.9   117.2   908.2   438.5   7.76   1288   43.3   56   285.7   286.1   250.5   1170.1   910.6   400.2   7.38   1355   433.3   66   292.5   262.9   117.2   908.2   438.5   7.76   1288   43.3   58   290.3   266.2   1172.1   900.6   446.5   6.63   1353   66   298.8   290.3   360.9   379.3   400.0   6.66   6.53   1357   6.62   294.7   266.1   8.900.0   379.3   6.09   344.5   6.77   14.00   344.3   66   296.8   296.2   2172.1   908.2   438.5   6.17   1621   56.3   77   200.6   277.3	uge bs. p	solut re, 1 quar	hpe	h Heat-	Heat.	tent = H Heat	lativ 7ol. rt 39	lum 1 lb	right t. St			
25.3         40         267.1         236.9         1163.4         926.5         642.0         10.28         .09721           26.3         41         228.6         238.5         .9         925.4         627.3         10.05         .09421           28.3         42         271.5         241.4         .7         923.3         599.9         9.61         .1040           29.3         44         272.9         242.9         1165.2         292.3         557.0         9.41         .1063           30.3         45         274.3         244.3         .6         921.3         574.7         .9.21         .1086           31.3         46         275.7         245.7         1160.0         920.4         563.0         9.02         .1108           32.3         47         277.0         247.0         4         919.4         551.7         8.84         .1131           33.3         48         278.3         248.4         8         918.5         540.9         9.02         .1108           34.3         49         279.6         249.7         1167.2         917.5         530.5         8.67         .1153           35.3         50	Ga	a a a	Tei	units.	units.	<u> </u>			<b>≱</b>			
30.3         45         274.3         244.3         6         921.3         574.7         9.21         .1086           31.3         46         275.7         245.7         1166.0         920.4         563.0         9.02         .1108           32.3         47         277.0         247.0         4         919.4         551.7         8.84         .1131           33.3         48         278.3         248.4         8         918.5         540.9         8.67         .1153           34.3         49         279.6         249.7         1167.2         917.5         530.5         8.50         .1153           36.3         51         282.1         252.2         1166.0         916.6         520.5         8.34         .1198           37.3         52         283.3         255.5         .4         914.9         501.7         8.04         .1243           38.8         53         284.5         254.7         .7         914.0         492.8         7.90         .1266           40.8         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1	23 <u>.3</u> 24.3	38 39	264.0 265.6	233.8 235.4	1162.5 .9		657.5	10.79 10.53	.09264 .09493			
30.3         45         274.3         244.3         6         921.3         574.7         9.21         .1086           31.3         46         275.7         245.7         1166.0         920.4         563.0         9.02         .1108           32.3         47         277.0         247.0         4         919.4         551.7         8.84         .1131           33.3         48         278.3         248.4         8         918.5         540.9         8.67         .1153           34.3         49         279.6         249.7         1167.2         917.5         530.5         8.50         .1153           36.3         51         282.1         252.2         1166.0         916.6         520.5         8.34         .1198           37.3         52         283.3         255.5         .4         914.9         501.7         8.04         .1243           38.8         53         284.5         254.7         .7         914.0         492.8         7.90         .1266           40.8         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1	25.3 26.3	40 41	267.1 268.6	236.9 238.5	1163.4	926.5 925.4	642.0 627.3	10.28 10.05	.09949			
30.3         45         274.3         244.3         6         921.3         574.7         9.21         .1086           31.3         46         275.7         245.7         1166.0         920.4         563.0         9.02         .1108           32.3         47         277.0         247.0         4         919.4         551.7         8.84         .1131           33.3         48         278.3         248.4         8         918.5         540.9         8.67         .1153           34.3         49         279.6         249.7         1167.2         917.5         530.5         8.50         .1153           36.3         51         282.1         252.2         1166.0         916.6         520.5         8.34         .1198           37.3         52         283.3         255.5         .4         914.9         501.7         8.04         .1243           38.8         53         284.5         254.7         .7         914.0         492.8         7.90         .1266           40.8         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1	27.3 28.3	42	270.1 271.5	240.0 241.4		924.4 923.3	613.3 599.9	9.83 9.61	.1018			
35.8         50         280.9         251.0         6         916.6         50.5         8.34         1198           36.3         51         282.1         252.2         1165.0         915.7         510.9         8.19         1221           37.3         52         283.3         253.5         .4         914.9         501.7         8.04         1243           38.8         53         284.5         284.7         .7         914.0         492.8         7.90         1266           40.3         55         286.9         257.2         .4         912.3         475.9         7.63         1311           41.3         56         288.1         226.5         1170.1         910.6         400.2         7.38         1333           42.3         57         289.1         259.5         1170.1         910.6         400.2         7.38         1353           43.3         58         290.3         200.7         5         900.8         402.7         7.26         1387           44.3         59         291.4         261.8         8         900.0         445.5         7.03         1422           46.3         61         223.6         <		44	272.9	242.9	1165.2		587.0		.1063			
35.8         50         280.9         251.0         6         916.6         50.5         8.34         1198           36.3         51         282.1         252.2         1165.0         915.7         510.9         8.19         1221           37.3         52         283.3         253.5         .4         914.9         501.7         8.04         1243           38.8         53         284.5         284.7         .7         914.0         492.8         7.90         1266           40.3         55         286.9         257.2         .4         912.3         475.9         7.63         1311           41.3         56         288.1         226.5         1170.1         910.6         400.2         7.38         1333           42.3         57         289.1         259.5         1170.1         910.6         400.2         7.38         1353           43.3         58         290.3         200.7         5         900.8         402.7         7.26         1387           44.3         59         291.4         261.8         8         900.0         445.5         7.03         1422           46.3         61         223.6         <	30.3 31.3	45 46	274.3 275.7	244.3 245.7	.6 1166.0	921.3 920.4	574.7 563.0	9.21 9.02	.1086			
35.8         50         280.9         251.0         6         916.6         50.5         8.34         1198           36.3         51         282.1         252.2         1165.0         915.7         510.9         8.19         1221           37.3         52         283.3         253.5         .4         914.9         501.7         8.04         1243           38.8         53         284.5         284.7         .7         914.0         492.8         7.90         1266           40.3         55         286.9         257.2         .4         912.3         475.9         7.63         1311           41.3         56         288.1         226.5         1170.1         910.6         400.2         7.38         1333           42.3         57         289.1         259.5         1170.1         910.6         400.2         7.38         1353           43.3         58         290.3         200.7         5         900.8         402.7         7.26         1387           44.3         59         291.4         261.8         8         900.0         445.5         7.03         1422           46.3         61         223.6         <	32.3 33.3	47	277.0 278.3	247.0 248.4	.8	919.4 918.5	551.7 540.9	8.84 8.67	.1131			
40.3         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1         255.3         .8         911.5         467.9         7.50         .1831           43.8         57         289.1         259.5         .1170.1         910.6         460.2         7.38         .1355           43.8         58         290.3         260.7         .5         909.8         492.7         7.26         .1877           44.3         59         291.4         261.8         .8         909.0         445.5         7.14         .1400           45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         236.6         264.0         .5         907.5         431.7         6.92         .1444           48.3         63         295.7         266.2         1172.1         905.2         418.8         6.72         .1489           49.3         64         226.8         297.8         280.3         1173.1         905.2         412.6         6.62 <t></t> .1511           50.3 <td< td=""><td></td><td></td><td></td><td>249.7</td><td></td><td></td><td></td><td></td><td></td></td<>				249.7								
40.3         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1         255.3         .8         911.5         467.9         7.50         .1831           43.8         57         289.1         259.5         .1170.1         910.6         460.2         7.38         .1355           43.8         58         290.3         260.7         .5         909.8         492.7         7.26         .1877           44.3         59         291.4         261.8         .8         909.0         445.5         7.14         .1400           45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         236.6         264.0         .5         907.5         431.7         6.92         .1444           48.3         63         295.7         266.2         1172.1         905.2         418.8         6.72         .1489           49.3         64         226.8         297.8         280.3         1173.1         905.2         412.6         6.62 <t></t> .1511           50.3 <td< td=""><td>36.3</td><td>50 51</td><td>282.1</td><td>252.2</td><td>1168.0</td><td>915.7</td><td>510.9</td><td>8.34</td><td>.1198</td></td<>	36.3	50 51	282.1	252.2	1168.0	915.7	510.9	8.34	.1198			
40.3         55         286.9         257.2         .4         912.3         475.9         7.63         .1811           41.3         56         288.1         255.3         .8         911.5         467.9         7.50         .1831           43.8         57         289.1         259.5         .1170.1         910.6         460.2         7.38         .1355           43.8         58         290.3         260.7         .5         909.8         492.7         7.26         .1877           44.3         59         291.4         261.8         .8         909.0         445.5         7.14         .1400           45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         236.6         264.0         .5         907.5         431.7         6.92         .1444           48.3         63         295.7         266.2         1172.1         905.2         418.8         6.72         .1489           49.3         64         226.8         297.8         280.3         1173.1         905.2         412.6         6.62 <t></t> .1511           50.3 <td< td=""><td>38.3</td><td>52 53</td><td>284.5</td><td>254.7</td><td>.7</td><td>914.0</td><td>492.8</td><td>7.90</td><td>.1245</td></td<>	38.3	52 53	284.5	254.7	.7	914.0	492.8	7.90	.1245			
45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         293.6         284.0         .5         907.5         431.7         6.92         .1444           47.3         62         294.7         255.1         .8         907.7         432.2         6.92         .1444           48.8         63         295.7         286.2         .1172.1         905.2         412.6         6.62         .1448           49.3         64         296.8         267.2         .4         905.2         412.6         6.62         .1511           50.8         65         297.8         268.3         .8         904.5         406.6         6.53         .1533           51.3         66         298.8         299.3         1173.1         903.7         400.8         6.43         .1553           52.3         67         299.8         270.4         .4         903.0         335.2         6.34         .1553           54.3         69         301.8         272.4         1174.0         902.3         389.8         6.25         .1599           55.3         70         30						912.3						
45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         293.6         284.0         .5         907.5         431.7         6.92         .1444           47.3         62         294.7         255.1         .8         907.7         432.2         6.92         .1444           48.8         63         295.7         286.2         .1172.1         905.2         412.6         6.62         .1448           49.3         64         296.8         267.2         .4         905.2         412.6         6.62         .1511           50.8         65         297.8         268.3         .8         904.5         406.6         6.53         .1533           51.3         66         298.8         299.3         1173.1         903.7         400.8         6.43         .1553           52.3         67         299.8         270.4         .4         903.0         335.2         6.34         .1553           54.3         69         301.8         272.4         1174.0         902.3         389.8         6.25         .1599           55.3         70         30	41.3	56	288.1	258.3 259.5	1170.1	911.5 910.6	467.9	7.50	.1333			
45.3         60         292.5         262.9         1171.2         908.2         438.5         7.03         .1422           46.3         61         293.6         284.0         .5         907.5         431.7         6.92         .1444           47.3         62         294.7         255.1         .8         907.7         432.2         6.92         .1444           48.8         63         295.7         286.2         .1172.1         905.2         412.6         6.62         .1448           49.3         64         296.8         267.2         .4         905.2         412.6         6.62         .1511           50.8         65         297.8         268.3         .8         904.5         406.6         6.53         .1533           51.3         66         298.8         299.3         1173.1         903.7         400.8         6.43         .1553           52.3         67         299.8         270.4         .4         903.0         335.2         6.34         .1553           54.3         69         301.8         272.4         1174.0         902.3         389.8         6.25         .1599           55.3         70         30	43.3 44.3	58 59	290.3 291.4	260.7 261.8	.5	909.8	452.7	7.26	.1377			
48.8 63 295.7 250.2 1172.1 905.9 418.8 6.72 14888 63 295.8 1250.2 44 905.2 412.6 6.62 1.5511 50.8 65 297.8 268.8 295.3 1173.1 903.7 400.8 6.43 1553 51.3 66 298.8 299.3 1173.1 903.7 400.8 6.43 1555 52.3 67 299.8 270.4 4.4 903.0 385.2 6.34 1557 543.3 68 300.8 271.4 4.7 902.3 389.8 6.25 1599 54.3 69 301.8 272.4 1174.0 901.6 394.5 6.17 1621 55.3 70 302.7 273.4 1.6 900.2 374.3 56.2 1169.5 56.3 71 303.7 274.4 6.8 900.2 374.3 6.09 1.663 57.3 72 304.6 275.3 889.5 389.4 5.93 1687 59.3 74 306.5 277.2 4.8 988.2 300.0 5.78 1781 59.3 74 306.5 277.2 4.9 988.2 300.0 5.78 1781 60.3 75 307.4 278.2 179 1176.0 806.9 361.1 5.63 1775 60.3 76 308.3 279.1 1176.0 806.9 361.1 5.63 1775 62.3 77 309.2 280.0 12 806.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 380.9 586.9 30.0 5.78 11862 64.3 79 310.9 281.8 1176.8 895.0 388.5 5.37 1862 67.3 82 313.5 284.5 6 83.3 89.3 7.3 30.6 5.31 1884 67.3 82 313.5 284.5 6 83.1 26.8 5.25 190.6 69.3 84 315.2 286.2 1178.1 891.9 319.5 5.13 1950		60	292.5			908.2	438.5	7 03				
48.8 63 295.7 250.2 1172.1 905.9 418.8 6.72 14888 63 295.8 1250.2 44 905.2 412.6 6.62 1.5511 50.8 65 297.8 268.8 295.3 1173.1 903.7 400.8 6.43 1553 51.3 66 298.8 299.3 1173.1 903.7 400.8 6.43 1555 52.3 67 299.8 270.4 4.4 903.0 385.2 6.34 1557 543.3 68 300.8 271.4 4.7 902.3 389.8 6.25 1599 54.3 69 301.8 272.4 1174.0 901.6 394.5 6.17 1621 55.3 70 302.7 273.4 1.6 900.2 374.3 56.2 1169.5 56.3 71 303.7 274.4 6.8 900.2 374.3 6.09 1.663 57.3 72 304.6 275.3 889.5 389.4 5.93 1687 59.3 74 306.5 277.2 4.8 988.2 300.0 5.78 1781 59.3 74 306.5 277.2 4.9 988.2 300.0 5.78 1781 60.3 75 307.4 278.2 179 1176.0 806.9 361.1 5.63 1775 60.3 76 308.3 279.1 1176.0 806.9 361.1 5.63 1775 62.3 77 309.2 280.0 12 806.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 62.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 280.9 586.9 361.1 5.63 1775 63.3 78 310.1 380.9 586.9 30.0 5.78 11862 64.3 79 310.9 281.8 1176.8 895.0 388.5 5.37 1862 67.3 82 313.5 284.5 6 83.3 89.3 7.3 30.6 5.31 1884 67.3 82 313.5 284.5 6 83.1 26.8 5.25 190.6 69.3 84 315.2 286.2 1178.1 891.9 319.5 5.13 1950	$\frac{46.3}{47.3}$	61 62	293.6 294.7	965 1	.8	906.7	431.7 425.2	6.92	.1444			
55.3         70         302.7         273.4         .3         900.9         379.3         6.09         .1643           56.3         71         303.7         274.4         .6         900.2         374.3         6.01         .1663           57.3         72         304.6         275.3         .8         899.5         389.4         5.93         .1687           58.3         73         305.6         276.3         .175.1         808.9         380.4         5.85         .1709           59.3         74         306.5         277.2         .4         808.2         300.0         5.78         .1731           60.3         75         307.4         278.2         7         807.5         355.5         5.71         1753           61.3         76         308.3         271.1         1176.0         806.9         351.1         5.63         1175           62.3         77         309.2         280.0         2         806.2         331.1         5.63         1175           64.3         79         310.9         281.8         1176.8         805.6         342.8         5.50         1819           66.3         80         311.8	48.3 49.3	63 64	295.7 296.8	266.2 267.2	1172.1		418.8 412.6	6.72	.1488			
55.3         70         302.7         273.4         .3         900.9         379.3         6.09         .1643           56.3         71         303.7         274.4         .6         900.2         374.3         6.01         .1663           57.3         72         304.6         275.3         .8         899.5         389.4         5.93         .1687           59.3         74         306.5         277.2         .4         808.2         300.0         5.78         .1731           60.3         75         307.4         278.2         7         897.5         355.5         5.71         1753           61.3         76         308.3         271.1         1176.0         886.9         351.1         5.63         1.175           62.3         77         309.2         280.0         2         806.2         316.1         5.63         1175           63.3         78         310.1         280.9         5         805.6         342.8         5.57         1175           64.3         79         310.9         281.8         1176.8         895.0         336.5         5.43         1840           66.3         80         311.8	50.3 51.3	65 66	297.8 298.8	268.3 269.3	.8	903 7	400.8	6.53	.1533			
55.3         70         302.7         273.4         .3         900.9         379.3         6.09         .1643           56.3         71         303.7         274.4         .6         900.2         374.3         6.01         .1663           57.3         72         304.6         275.3         .8         899.5         389.4         5.93         .1687           59.3         74         306.5         277.2         .4         808.2         300.0         5.78         .1731           60.3         75         307.4         278.2         7         897.5         355.5         5.71         1753           61.3         76         308.3         271.1         1176.0         886.9         351.1         5.63         1.175           62.3         77         309.2         280.0         2         806.2         316.1         5.63         1175           63.3         78         310.1         280.9         5         805.6         342.8         5.57         1175           64.3         79         310.9         281.8         1176.8         895.0         336.5         5.43         1840           66.3         80         311.8	52.3 53.3	67	299.8 300.8	270.4 271.4	.4	903 0	395.2 389.8	6.34	.1577			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		69	301.8			901.6	384.5	6.17	.1621			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	55.3 56.3	70 71	303.7	273.4 274.4	.3	900.2	379.3 374.3	6.01	.1665			
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	57.3 58.3	72 73	305.6	275.3	1175.1	898.9	369.4 364.6	5.93 5.85	.1687 .1709			
65,3         80         311.8         282.7         1177.0         894.3         334.5         5.37         .1862           66.3         81         312.7         283.6         .3         893.7         330.6         5.31         .1884           67.3         82         313.5         284.5         .6         893.1         326.8         5.25         .1906           68.3         83         314.4         285.3         .8         892.5         323.1         5.18         .1928           69.3         84         315.2         286.2         1178.1         891.9         319.5         5.13         .1950			1		.4		360.0	5.78	.1731			
65,3         80         311.8         282.7         1177.0         894.3         334.5         5.37         .1862           66.3         81         312.7         283.6         .3         893.7         330.6         5.31         .1884           67.3         82         313.5         284.5         .6         893.1         326.8         5.25         .1906           68.3         83         314.4         285.3         .8         892.5         323.1         5.18         .1928           69.3         84         315.2         286.2         1178.1         891.9         319.5         5.13         .1950	60.3 61.3	75 76	307.4 308.3	278.2 279.1	1176.0	897.5 896.9	355.5 351.1	5.71 5.63	.1753 .1775			
65,3         80         311.8         282.7         1177.0         894.3         334.5         5.37         .1862           66.3         81         312.7         283.6         .3         893.7         330.6         5.31         .1884           67.3         82         313.5         284.5         .6         893.1         326.8         5.25         .1906           68.3         83         314.4         285.3         .8         892.5         323.1         5.18         .1928           69.3         84         315.2         286.2         1178.1         891.9         319.5         5.13         .1950	62.3 63.3	77	309.2 310.1	280.9	.2	896.2 895.6	346.8 342.6	5.57	.1797			
68.3 83 314.4 285.3 .8 892.5 323.1 5.18 .1928 69.3 84 315.2 286.2 1178.1 891.9 319.5 5.13 .1950		1		1				5.43				
68.3 83 314.4 285.3 .8 892.5 323.1 5.18 .1928 69.3 84 315.2 286.2 1178.1 891.9 319.5 5.13 .1950	66.3	81	312.7	282.7	.3	893.7	330.6	5.37	.1862			
	68.3	83	314.4	285.3	1178 1	892.5	323.1	5.18	.1928			

Properties of Saturated Steam.

ssure, q. in.	Press- per nch.	re sit.	Total above	Heat 32° F.	ut L.	Relative Volume. Vol. of Water at 39° F. = 1.	7olume, Cu. ft. in 1 lb. of Steam	1 cu.
auge Pressure Ibs. per sq. in.		emperature Fahrenheit	In the Water	In the Steam	Latent Heat $= H - h$ . Heat-units.	telative Volume Vol. of Water at 39° F. = 1.	ne. (b. of	ht of Steam
Gauge Pressure, lbs. per sq. in.	Absolute ure, lbs square	Temperature Fahrenheit.	h Heat- units.	H Heat- units.	Later = I Hea	Relat Vol at 3	Volume, in 1 lb. o	Weight of 1 cu. ft. Steam, lb.
71.3	86	316.8	287.9	1178.6	890.7	312.5	5 02	.1998
72.3	87	317.7	288.7	.8	890.1	309.1	4.96	.2015
73.3	88	318.5	289.5	1179.1	889.5	305.8	4.91	.2036
74.3	89	319.3	290.4	.3	888.9	302.5	4.86	.2058
75.3	90	320.0	291.2	.6	888.4	299.4	4.81	.2080
76.3	91	320.8	292.0	.8	887.8	296.3	4.76	.2102
77.3	92	321.6	292.8	1180.0	887.2	293.2	4.71	.2123
78.3	93	322.4	293.6	.3	886.7	290.2	4.66	.2145
79.3	94	323.1	294.4	.5	886.1	287.3	4.62	.2166
80.3	95	323.9	295.1	.7	885.6	284.5	4.57	.2188
81.3	96	324.6	295.9	1181.0	885.0	281.7	4.53	.2210
82.3	97	325.4	296.7	.2	884.5	279.0	4.48	.2231
83.3	98	326.1	297.4	.4	884.0	276.3	4.44	.2253
84.3	99	326.8	298.2	.6	883.4	273.7	4.40	.2274
85.3	100	327.6	298.9	.8	882.9	271.1	4.36	.2296
86.3	101	328.3	299 7	1182.1	882.4	268.5	4.32	.2317
87.3	102	329.0	300.4	.3	881.9	266.0	4.28	.2339
88.3	103	329.7	301.1	.5	881.4	263.6	4.24	.2360
89.3	104	330.4	301.9	.7	880.8	261.2	4.20	.2382
90.8	105	331.1	302.6	.9	880.3	258.9	4.16	.2403
91.3	106	331.8	303.3	1183.1	879.8	256.6	4.12	.2425
92.3	107	332.5	304.0	.4	879.3	254.3	4.09	.2446
93.3	108	333.2	304.7	.6	878.8	252.1	4.05	.2467
94.3	109	333.9	305.4	.8	878.3	249.9	4.02	.2489
95.3	110	334.5	306.1	1184.0	877.9	247.8	3.98	.2510
96.3	111	335.2	306.8	.2	877.4	245.7	3.95	.2531
97.3	112	335.9	307.5	.4	876.9	243.6	3.92	.2553
98.3	113	336.5	308.2	.6	876.4	241.6	3.88	.2574
99.3	114	337.2	308.8	.8	875.9	239.6	3.85	.2596
100.8	115	337.8	309.5	1185.0	875.5	237.6	3.82	.2617
101.3	116	338.5	310.2	.2	875.0	235.7	3.79	.2638
102.3	117	339.1	310.8	.4	874.5	233.8	3.76	.2660
103.3	118	339.7	311.5	.6	874.1	231.9	3.73	.2681
104.3	119	340.4	312.1	.8	873.6	230.1	3.70	.2703
105.3	120	341.0	312.8	.9	873.2	228.3	3.67	.2724
106.3	121	341.6	313.4	1186.1	872.7	226.5	3.64	.2745
107.3	122	342.2	314.1	.3	872.3	224.7	3.62	.2766
108.3	123	342.9	314.7	.5	871.8	223.0	3.59	.2788
109.3	124	343.5	315.3	.7	871.4	221.3	8.56	.2809
110.3 111.8 112.3 113.3 114.3	125 126 127 128 129	344.1 344.7 345.3 345.9 346.5	316 0 316.6 317.2 317.8 318.4	1187.1 .3 .4 .6	870.9 870.5 870.0 869.6 869.2	219.6 218.0 216.4 214.8 213.2	3.53 3.51 3.48 3.46 3.43	.2830 .2851 .2872 .2894 .2915
115.3	130	347.1	319.1	.8	868.7	211.6	3.41	.2936
116.3	131	347.6	319.7	1188,0	868.3	210.1	3.38	.2957
117.8	132	348.2	320.3	.2	867.9	208.6	3.36	.2978
118.3	133	348.8	320.8	.3	867.5	207.1	3.33	.3000
119.3	184	349.4	321.5	.5	867.0	205.7	3.31	.3021

		Proper	rties of	Satur	ated S	team.		
Gauge Pressure. Ibs. per sq. in.	Absolute Press- ure, lbs. per square inch.	Temperature Fahrenheit.	In the Water h Heat-units.	Heat 32° F. In the Steam H Heat- units.	Latent Heat $L$ . $= H - h$ . Heat-units.	Relative Volume. Vol. of water at 39° F. = 1.	Volume. Cu. ft. in 1 lb. of Steam.	Weight of 1 cu. ft. Steam, 1b.
120.3	135	350.0	322.1	1188.7	866.6	204.2	3.29	.3042
121.3	136	350.5	322.6	.9	866.2	202.8	3.27	.3063
122.3	137	351.1	323.2	1189.0	865.8	201.4	3.24	.3084
123.3	138	351.8	323.8	.2	865.4	200.0	3.22	.3105
124.3	139	352.2	324.4	.4	865.0	198.7	3.20	.3126
125.3	140	352.8	325.0	.5	864.6	197.3	3.18	.3147
126.3	141	353.3	325.5	.7	864.2	196.0	3.16	.3169
127.3	142	353.9	326.1	.9	863.8	194.7	3.14	.3190
128.3	143	354.4	326.7	1190.0	863.4	193.4	3.11	.3211
129.3	144	355.0	327.2	.2	863.0	192.2	3.09	.3232
130.3	145	355.5	327.8	.4	862.6	190.9	3.07	.3253
131.3	146	356.0	328.4	.5	862.2	189.7	3.05	.3274
132.3	147	356.6	328.9	.7	861.8	185.5	3.04	.3295
133.3	148	357.1	329.5	.9	861.4	187.3	3.02	.3316
134.3	149	357.6	330.0	1191.0	861.0	186.1	3.00	.3337
135.3	150	358.2	330.6	.2	860.6	184.9	2.98	.3358
136.3	151	358.7	331.1	.3	860.2	183.7	2.96	.3379
137.3	152	359.2	331.6	.5	859.9	182.6	2.94	.3400
138.3	153	359.7	332.2	.7	859.5	181.5	2.92	.3421
139.3	154	360.2	332.7	.8	859.1	180.4	2.91	.3442
140.3	155	360.7	333.2	1192.0	858.7	179.2	2.89	.3463
141.3	156	361.3	333.8	.1	858.4	178.1	2.87	.3483
142.3	157	361.8	334.3	.3	858.0	177.0	2.85	.3504
143.3	158	362.3	334.8	.4	857.6	175.0	2.84	.3525
144.3	159	362.8	335.3	.6	857.2	174.9	2.82	.3546
145.3	160	363.3	335.9	.7	856.9	173.9	2.80	.3567
146.3	161	363.8	336.4	.9	856.5	172.9	2.79	.3588
147.3	162	364.3	336.9	1193.0	856.1	171.9	2.77	.3609
148.3	163	364.8	337.4	.2	855.8	171.0	2.76	.3630
149.3	164	365.3	337.9	.3	855.4	170.0	2.74	.3650
150.3	165	365.7	338.4	.5	855.1	169.0	2.72	.3671
151.3	166	366.2	338.9	.6	854.7	168.1	2.71	.3692
152.8	167	366.7	339.4	.8	854.4	167.1	2.69	.3713
153.3	168	367.2	339.9	.9	854.0	166.2	2.68	.3734
154.3	169	367.7	340.4	1194.1	853.6	165.3	2.66	.3754
155.3	170	368.2	340.9	.2	853.3	164.3	2.65	.3775
156.3	171	368.6	341.4	.4	852.9	163.4	2.63	.3796
157.3	172	369.1	341.9	.5	852.6	162.5	2.62	.3817
158.3	173	369.6	342.4	.7	852.3	161.6	2.61	.3838
159.3	174	370.0	342.9	.8	851.9	160.7	2.59	.3858
160.3	175	370.5	343.4	.9	851.6	159.8	2.58	.3879
161.3	176	371.0	343.9	1195.1	851.2	158.9	2.56	.3900
162.3	177	371.4	344.3	.2	850.9	158.1	2.55	.3921
163.3	178	371.9	344.8	.4	850.5	157.2	2.54	.3942
164.3	179	372.4	345.3	.5	850.2	156.4	2.52	.3962
165.3	180	372.8	345.8	.7	849.9	155.6	2.51	.3983
166.3	181	373.3	346.3	.8	849.5	154.8	2.50	.4004
167.3	182	373.7	346.7	.9	849.2	154.0	2.48	.4025
168.3	183	374.2	347.2	1196.1	848.9	158.2	2.47	.4046

	Troposition of Street Street									
Gauge Pressure, lbs. per sq. in.	Absolute Pressure, Ibs. per square inch.	it.	Total above	Heat 32° F.	atent Heat $L$ . = $H - h$ . Heat-units.	Relative Volume. Vol. of water at 39° F.= 1.	Volume. Cu. ft. in 1 lb. of Steam	Weight of 1 cu. ft. Steam, 1b.		
se se	Absolute Presure, 15s. pe	emperatur Fahrenheit	In the	In the	Heg h.	Wa 1.	of	# H		
P P	re par	ere	Water	Steam	ETE.	of of F.=	p. p.	rea		
s. Is	sol na	O di	h Heat-	H Heat-	ten E.E.	at.	21	2002		
Ga	Ab ur sq	Temperature Fahrenheit.	units.	units.	Latent Heat $= H - h.$ Heat-units	Rela Vol 39°	Voi	Weig ft.		
169.3	184	374.6	347.7	1196.2	848.5	152.4	2.46	.4066		
170.3 171.3 172.3 173.3 174.3	185 186	375.1 375.5	348.1 348.6	.3	848.2 847.9	151.6 150.8	2.45 2.43	.4087		
172.3	187	375.9	349.1	.3 .5 .6 .7	847.6	150.8	2.40	.4108		
173.3	187 188	375.9 376.4	349.5	.7	847.6 847.2	149.2	2.42 2.41 2.40	.4129 .4150		
	189	376.9	350.0		846.9	148.5		.4170		
175.3 176.3 177.3 178.3 179.3	190	377.3 377.7 378.2	350.4 350.9	1197.0	846.6	147.8 147.0	2.39	.4191 .4212		
177.3	191 192	378.2	351.3	.1	846.3 845.9	146.3	2.37 2.36	4233		
178.3	193	378.6	351.8	.4	845.6	145.6	2.35 2.34	.4254		
	194	379.0	352.2	.5	845.3	144.9		.4275		
180.3 181.3 182.3 183.3 184.3	195 196	379.5	352.7 353.1	.7 .8	845.0 844.7	144.2 143.5	2.33 2.32 2.31 2.29 2.28	.4296		
182.3	197	380.0 380.3 380.7	353.6	.9	844.4	142.8	2.31	.4337		
183.3	197 198	380.7	353.6 354.0	1198.1	844.1	142.8 142.1 141.4	2.29	.4358		
	199	381.2	354.4	.2	843.7			.4379		
185.3 186.3 187.3 188.3 189.3	200 201	381.6 382.0	354.9 355.3	.3	843.4 843.1	140.8 140.1	2.27 2.26	.4400		
187.3	202	382.4	355.8	.6	842.8	139.5	2.25	.4441		
188.3	203	382.4 382.8	356.2	.6 .7 .8	842.5 842.2	138.8	2.25 2.24 2.23	.4462		
	204	383.2	356.6			138.1		.4482		
190.3	205	383.7 384.1	357.1 357.5	1199.0	841.9	137.5 136.9 136.3	2.22	.4503		
192.3	206 207	384.5	357.5 357.9	.1 .2 .3	841.6 841.3	136.3	2.20	.4523 .4544		
191.3 192.3 193.3 194.3	208	384.9	358.3	.8	841 0	135.7	2.21 2.20 2.19 2.18	.4564		
	209	385.3	358.8	.5	840.7	185,1		.4585		
195.3 196.3	210 211	385.7 386.1	359.2 359.6	.6 .7 .8 .9 1200.1	840.4 840.1	134.5 133.9	2.17 2.16 2.15 2.14 2.13	.4605 .4626		
197.3 198.3 199.3	212 213	386.5 386.9	360.0	.8	839.8 839.5	133.3	2.15	.4646		
198.3	213 214	386.9 387.3	360.4 360.9	.9	839.5 839.2	132.7 132.1	2.14	.4667		
200.3	215 216	387.7 388.1	361.3 361.7 362.1	.2	838.9 838.6	131.5 130.9	2.12 2.12 2.11	.4707		
201.3 202.3	217	388.5	362.1	.4	838.3	130.3	2.11	.4728 .4748		
203.3	218	388.9	362.5	.6	838.1	129.7	2.10	.4768		
204.3	219	389.3	362.9		837.8	129.2		Ì		
205.3 215.3	220 230	389.7 393.6	362.2* 366.2 370.0	1200.8 1202.0	838.6* 835.8	128.7	2.06	.4852		
225.3	240	397.3	370.0	1203.1	833.1	123.3 118.5	1.98 1.90	.5270		
235.3	250	400.9	373.8	1204.2	830.5	114.0	1.83	.5478		
245.3	260	404.4	377.4	1205.3	827.9	109.8	1.76	.5686		
255.3 265.3	270 280	407.8 411.0	380.9 384.3	1206.3 1207.3	825.4 823.0	105.9	1.70	.5894		
255.3 265.3 275.3	290	414.2	387.7	1208.3	820.6	102.3 99.0	1.76 1.70 1.64 1.585	.6308		
285.3	300	417.4	390.9	1209.2	818.3	95.8 82.7	1.535	.6515		
335.3	350	432.0	406.3	1213.7	807.5	82.7	1.325	.7545		

 $<sup>\</sup>ast$  The discrepancies at 205.3 lbs. gauge are due to the change from Dery's to Buel's figures.

Pressure, r sq. in.	ம் உ		Total above		T.	Volume. ater at 1.	#1:2:	-i
in.	Press	0 .	above	ъz-г.		25		cu. lb.
res sq.	ute Pres lbs. pe	Temperature Fahrenheit.			ant Heat $H-h$ . eat-units	Volu water	in 1.	Weight of 1 ft. Steam, 1
T. S.		p at	In the	In the	HID			of an
Gauge Pr lbs per s		<u>6</u> 6	Water	Steam			lume. Steam	re e
σ	Absol ure, squa	84	h	H	Latent = H Heat	F. F.	1 2 2	5000
bs	2 1 5	-Fa	Heat-	Heat-	出事	Rela Vol 39°	600	t.
20	4 - 2	E-	units.	units.	12	12 m	Volume. of Steam	= -
385.3	400	444.9	419.8	1217.7	797.9	72.8	1.167	.8572
435.3	450	456.6	432.2	1221.3	789.1	65.1	1.042	.9595
10				1.00110	1	00.1	11010	
485.3	500	467.4	443.5	1224.5	781.0	58.8	.942	1.062
535.3	550	477.5	454.1	1227.6	773.5	53.6	.859	1.164
585.3	600	486.9	464.2	1230.5	766.3	49.3	.790 .731	1.266
635.3	650	495.7	473.6	1233.2	759.6	45.6	.731	1.368
685.3	700	504.1	482.4	1235.7	753.3	42.4	.680	1.470
735.3	750	512.1	490.9	1238.0	747.2	39.6	.636	1.572
785.3	800	519.6	498.9	1240.3	741.4	37.1	.597	1.674
885.8	850	526.8	506.7	1242.5	735.8	34.9	.563	1.776
885.3	900	533.7	514.0	1244.7	730.6	99.0	532	1.878
935.3	950	540.3	521.3	1246.7	725.4	33.0 31.4	.505	1.980
985.3	1000	546.8	528.3	1248.7	720.3	30.0	.480	2.082
0.00.0	1000	0.000	1 0.0.0	1240.1	120.0	00.0	1 .400	1 2.002

#### FLOW OF STEAM.

Flow of Steam through a Nozzle. (From Clark on the Steam-nengine.)—The flow of steam of a greater pressure into an atmosphere of a less pressure increases as the difference of pressure is increased, until the external pressure becomes ouly 5% of the absolute pressure in the boiler. The flow of steam is neither increased nor diminished by the fall of the external pressure below 58%, or about 4/7ths of the inside pressure, even to the extent of a perfect vacuum. In flowing through a nozzle of the best form, the steam expands to the external pressure, and to the volume due to this pressure, so long as it is not less than 5% of the internal pressure. For an external pressure of 55%, and for lower percentages, the ratio of expansion is 1 to 1.624. The following table is selected from Mr. Brownlee's data exemplifying the rates of discharge under a constant internal pressure, into various external pressures:

### Outflow of Steam; from a Given Initial Pressure into Various Lower Pressures.

	Absolute initial pressure in boiler, 75 lbs. per sq. in.										
Absolute Pressure in Boiler per square inch.	External Pressure per square inch.	Ratio of Expansion in Nozzle,	Velocity of Outflow at Constant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orifice per minute.						
lbs.	lbs.	ratio.	feet per sec.	feet p. sec.	lbs.						
75	74	1.012	227.5	230	16.68						
75	72	1.037	386.7	401	28.35						
75	70	1.063	490	521	35.93						
75	65	1.136	660	749	48.38						
75	61.62	1.198	736	876	53.97						
75	60	1.219	765	933	56.12						
75	50	1.434	873	1252	64						
75	45	1.575	890	1401	65.24						
75	3.46 by the second seco	1.624	890.6	1446.5	65.3						
75	15	1.624	890.6	1446.5	65.3						
75	0	1.624	890.6	1446.5	65.3						

When steam of varying initial pressures is discharged into the atmosphere—the atmospheric pressure being not more than 5% of the initial pressure—the velocity of outflow at constant density, that is, supposing the initial density to be maintained, is given by the formula  $V=3.5953\,\mu$ h.

V = the velocity of outflow in feet per minute, as for steam of the initial density:

h= the height in feet of a column of steam of the given absolute initial pressure of uniform density, the weight of which is equal to the pressure on the unit of base.

The lowest initial pressure to which the formula applies, when the steam is discharged into the atmosphere at 14.7 lbs, per square inch, is  $(14.7 \times 100.758 =) 25.37$  lbs, per square inch. Examples of the application of the formula are given in the table below.

From the contents of this table it appears that the velocity of outflow into the atmosphere, of steam above 25 lbs. per square inch absolute pressure, or 10 lbs. effective, increases very slowly with the pressure, obviously because the density, and the weight to be moved, increase with the pressure, An average of 900 feet per second may, for approximate calculations, be taken for the velocity of outflow as for constant density, that is, taking the volume of the steam at the initial volume.

Outflow of Steam into the Atmosphere,—External pressure per square inch 14.7 lbs. absolute. Ratio of expansion in nozzle, 1.624.

Absolute Initial Pressure per square inch.	Velocity of Out- flow as at Con- stant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orifice per min	Horse-power per sq in. of Orifice if H. P. = 30 lbs. per hour.	Absolute Initial Pressure per square inch.	Velocity of Outflow as at Constant Density.	Actual Velocity of Outflow Expanded.	Discharge per square inch of Orifice per minute.	Horse-power per sq.in. of Orlifice if H. P. = 30 lbs. per hour.
lbs.	feet p.sec.	feet per sec.	lbs.	H.P.	lbs.	feet p.sec.	feet per sec.	lbs.	H.P.
25.37	863	1401	22.81	45.6	90	895	1454	77.94	155.9
30	867	1408	26.84	53.7	100	898	1459	86.34	172.7
40	874	1419	35.18		115	902	1466	98.76	197.5
50	880	1429	44.06	88.1	135	906	1472	115.61	231.2
60 .	885	1437	52.59	105.2	155	910	1478	132.21	264.4
70 75	889	1444	61.07	122.1	165	912	1481	140.46	280.9
75	891	1447	65.30	130.6	215	919	1493	181.58	363.2

**Napier's Approximate Rule.**—Flow in pounds per second = absolute pressure  $\times$  area in square inches  $\div$  70. This rule gives results which closely correspond with those in the above table, as shown below.

Prof. Peabody, in Trans A. S. M. E., xi, 187, reports a series of experiments on flow of steam through tubes 14 inch in diameter, and 14, 14, and 14, inch long, with rounded entrances, in which the results agreed closely with Napier's formula, the greatest difference being an excess of the experimental over the calculated result of 3.2%. An equation derived from the theory of thermodynamics is given by Prof. Peabody, but it does not agree with the experimental results as well as Napier's rule, the excess of the actual flow being 6.6%.

Flow of Steam in Pipes.—A formula commonly used for velocity of flow of steam in pipes is the same as Downing's for the flow of water in

smooth cast-iron pipes, viz.,  $V = 50 \sqrt{\frac{H}{L}}D$ , in which V = velocity in feet

per second, L= length and D= diameter of pipe in feet, H= height in feet of a column of steam, of the pressure of the steam at the entrance,

which would produce a pressure equal to the difference of pressures at the two ends of the pipe. (For derivation of the coefficient 50, see Briggs on "Warning Buildings by Stean," Proc. Inst. 0. E. 1882.) If Q = quantity in cubic feet per minute, d = diameter in inches, L and H being in feet, the formula reduces to

$$Q = 4.7233 \sqrt{\frac{H}{L}} d^5, \quad H = .0448 \frac{Q^2 L}{d^5}, \quad d = .5374 \sqrt[5]{\frac{Q^2 L}{H}}.$$

(These formulæ are applicable to air and other gases as well as steam.) If  $p_1 =$  pressure in pounds per square inch of the steam (or gas) at the entrance to the pipe,  $p_2 =$  the pressure at the exit, then  $144(p_1 - p_2) =$  difference in pressure per square foot. Let w = density or weight per cubic foot  $f_2$  steam at the pressure  $p_1$ , then the height of column equivalent to the difference in pressures

$$= H = \frac{144(p_1 - p_2)}{w}, \ \ \text{and} \ \ Q = 60 \times .7854 \times 50 D^2 \sqrt{\frac{144(p_1 - p_2)\overline{D}}{wL}}.$$

If W = weight of steam flowing in pounds per minute = Qw, and d is taken in inches, L being in feet,

$$\begin{split} W &= 56.68 \sqrt{\frac{w(p_1-p_2)d^5}{L}}; \quad Q &= 56.68 \sqrt{\frac{(p_1-p_2)d^5}{Lw}}; \\ d &= 0.199 \sqrt[5]{\frac{W^2L}{w(p_1-p_2)}} = 0.199 \sqrt[5]{\frac{Q^2wL}{p_1-p_2}}. \end{split}$$

Velocity in feet per minute =  $V = Q \div .7854 \frac{d^2}{144} = 10392 \sqrt{\frac{(p_1 - p_2)d}{v_0 L}}$ .

For a velocity of 6000 feet per minute,  $d = \frac{wL}{3(p_1 - p_2)}$ ;  $p_1 - p_2 = \frac{wL}{3d}$ .

For a velocity of 6000 feet per minute, a steam-pressure of 100 lbs. gauge, or w=264, and a length of 100 feet,  $d=\frac{8}{p_1}=\frac{2}{p_2}$ ;  $p_1-p_2=\frac{8}{2}$ . That is, a pipe 1 inch diameter, 100 feet long, carrying steam of 100 lbs, gauge-pressure at 6000 feet velocity per minute, would have a loss of pressure of 8.8 lbs. per 50 are inch, while steam traveling at the same velocity in a pipe 8.5 inches diameter would lose only 1 lb. pressure.
G. H. Babcock, in "Steam," gives the formula

$$W = 87 \sqrt{\frac{w(p_1 - p_2)d^5}{L\left(1 + \frac{3.6}{d}\right)}}.$$

In earlier editions of "Steam" the coefficient is given as 300,—evidently an error,—and this value has been reprinted in Clark's Pocket-Book (1892 edition). It is apparently derived from one of the numerous formulæ for flow of water in pipes, the multiplier of L in the denominator being used for an expression of the increased resistance of small pipes. Putting this formula

in the form  $W = c_1 / \frac{(p_1 - p_2)d^5}{T}$ , in which c will vary with the diameter

of the pipe, we have,

For diameter, inches.... Value of c.....

instead of the constant value 56.68, given with the simpler formula.

One of the most widely accepted formulæ for flow of water is D'Arcy's,

 $V=c\sqrt{\frac{HD}{L\,4}}$ , in which c has values ranging from 65 for a  $\frac{1}{2}$ -inch pipe up to

111.5 for 24-inch. Using D'Arcy's coefficients, and modifying his formula to make it apply to steam, to the form

$$Q=c\sqrt{\frac{(p_1-p_2)d^b}{wL}}, \ \ {\rm or} \ \ W=c\sqrt{\frac{w(p-p_1)d^b}{L}},$$

we obtain.

In the absence of direct experiments these coefficients are probably as accurate as any that may be derived from formulæ for flow of water.

Loss of pressure in lbs. per sq. in. = 
$$p_1 - p_2 = \frac{Q^2wL}{c^2d^5}$$
.

Loss of Pressure due to Radiation as well as Friction.— E. A. Rudiger (Mechanics, June 30, 1883) gives the following formulæ and tables for flow of steam in pipes. He takes into consideration the losses in pressure due both to radiation and to friction.

Loss of power, expressed in heat-units due to friction,  $Hf = \frac{W^s fl}{10p^2 d^5}$ . Loss due to radiation, Hr = 0.262rld.

In which W is the weight in lbs. of steam delivered per hour, f the coefficient of friction of the pipe, l the length of the pipe in feet, p the absolute terminal pressure, d the diameter of the pipe in inches, and r the coefficient of radiation. f is taken as from .0165 to .0175, and r varies as follows:

TABLE OF VALUES FOR r.

Die Gestelle	Absolute Pressure.								
Pipe Covering.	40 lbs.	65 lbs.	90 lbs.	115 lbs.					
Uncovered pipe 2-inch cement composition 2 " asbestos 2 " asbestos flock 2 " wooden log 4 " mineral wool	437	555	620	684					
	146	178	193	209					
	157	192	202	222					
	150	185	197	210					
	100	122	145	151					
2 " mineral wool	61	76	85	93					
	48	58	66	73					

The appended table shows the loss due to friction and radiation in a steampipe where the quantity of steam to be delivered is 1000 lbs. per hour, l=1000 feet, the pipe being so protected that loss by radiation r=64, and the absolute terminal pressure being 90 lbs.:

Diameter of Pipe, inches.	Loss by Friction, Hf.	Loss by Radia- tion, Hr.	Total Loss, L.	Diam. of Pipe, inches.	Loss by Friction, Hf.	Loss by Radia- tion, Hr.	Total Loss, L.
1 11/4 11/2 13/4 2 21/2 3	197,531 64,727 26,012 12,035 6,173 2,023 813	16,768 20,960 25,152 29,344 33,536 41,920 50,304	214,300 85,687 51,164 41,379 39,709 43,943 51,117	31/2 4 5 6 7 8	376 193 63 25 12 6	58,688 67,072 83,840 100,608 117,376 134,144	59,064 67,265 83,903 1:0,623 117,388 134,150

If the pipes are carrying steam with minimum loss, then for same r, l, and p, the loss of pressure L for pipes of different diameters varies in-

versely as the diameters.

The general equation for the loss of pressure for the minimal loss from

friction and radiation is

$$L = \frac{0.0007023}{W} \frac{drlp}{dr}$$

The loss of pressure for pipes of 1 inch diameter for different absolute terminal pressures when steam is flowing with minimal loss is expressed by the formula  $L = Cl_4/r^2$ , in which the coefficient C has the following values:

Tilo m	a=	1ha	aba	town			α_	0.0000099#
For	75	ios.	aus.	term.	pressure	·		0.00093684
			66		44	•••••		0.00099573
		66		66	44			0.00103132
66	115	46	66	6.6	44			0.00108051

In order to find the loss of pressure for any other diameter, divide the loss of pressure in a 1-inch pipe for the given terminal pressure by the given diameter, and the quotient will be the loss of pressure for that diameter.

The following is a general summary of the results of Mr. Rudiger's inves-

tigation:
The flow of steam in a pipe is determined in the same manner as the flow of water, the formula for the flow of steam being modified only by substituting the equivalent loss of pressure, divided by the density of the steam, for the loss of head.

The losses in the flow of steam are two in number—the loss due to the friction of flow and that due to radiation from the sides of the pipe. The sum of these is a minimum when the equivalent of the loss due to friction of flow is equal to one fifth of the loss of heat by radiation. For a greater or less loss of pressure—i.e., for a less or greater diameter of pipe the total loss increases very rapidly.

—the total loss increases very rapidly.

For delivering a given quantity of steam at a given terminal pressure,

with minimal total loss, the better the non-conducting material employed,

the larger the diameter of the steam-pipe to be used.

The most economical loss of pressure for a pipe of given diameter is equal to the most economical loss of pressure in a pipe of I inch diameter for same conditions, divided by the diameter of the given pipe in inches.

The following table gives the capacity of pipes of different diameters, to

deliver steam at different terminal pressures through a pipe one half mile long for loss of pressure of 10 lbs., and a mean value of f=0.0175. Let Wdenote the number of pounds of steam delivered per hour:

Diameter of Pipe,	Abs. T	erm. Pr	essure.	Diameter of Pipe,	Abs. Term. Pressure.			
inches.	65 lbs.	80 lbs. 100 lbs.		inches.	65 lbs.	80 lbs.	100 lbs.	
1	1,595	W 113 198 312 459 641 1,121 1,768 2,599 3,629	W 125 219 346 508 710 1,240 1,956 2,875 4,042	414	5,721 9,024 13,268 18,526 24,870 32,364	W 4,872 6,339 10,000 14,701 20,528 27,556 35,860 45,507 56,564	W 5,390 7,013 11,063 16,265 22,711 30,488 39,675 50,349 62,581	

Resistance to Flow by Bends, Valves, etc. (From Briggs on Warming Buildings by Steam.)—The resistance at the entrance to a tube when no special bell-mouth is given consists of two parts. The head  $v^2 \div 2g$ is expended in giving the velocity of flow; and the head 0.505

coming the resistance of the mouth of the tube. Hence the whole loss of head at the entrance is 1.505  $\frac{v^2}{2a}$ . This resistance is equal to the resistance

of a straight tube of a length equal to about 60 times its diameter.

The loss at each sharp right-angled elbow is the same as in flowing through a length of straight tube equal to about 40 times its diameter. For a globe steam stop-valve the resistance is taken to be 11/6 times that of the right-angled elbow.

Sizes of Steam-pipes for Stationary Engines .- Authorities on the steam-engine generally agree that steam-pipes supplying engines should be of such size that the mean velocity of steam in them does not exceed 6000 feet per minute, in order that the loss of pressure due to friction may not be excessive. The velocity is calculated on the assumption that the cylinder is filled at each stroke. In very long pipes, 100 feet and upward, it is well to make them larger than this rule would give, and to place a large steam receiver on the pipe near the engine, especially when the engine cuts off early in the stroke.

An article in *Power*, May, 1893, on proper area of supply-pipes for engines gives a table showing the practice of leading builders. To facilitate comparison, all the engines have been rated in horse-power at 40 pounds mean effective pressure. The table contains all the varieties of simple engines, from the slide-valve to the Corliss, and it appears that there is no general difference in the sizes of pipe used in the different types, The averages selected from this table are as follows:

Diam. of pipe, in . . . . 2 2½ Av. H.P. of engines . . . 25 39 Calculated, formula (1) 23 36 3 3½ 56 77 51 70 4 4½ 100 126 10 156 225 306 400 506 625 91 116 143 206 366 463 571 formula (2) 24 87.5 54 78 96 121 150 216 294 600

Formula (1) is: 1 H P. requires .1375 sq. in. of steam-pipe area. Formula (2) is: Horse-power =  $6d^2$ . d = diam. of pipe in id = diam. of pipe in inches.

The factor .1375 in formula (1) is thus derived: Assume that the linear velocity of steam in the pipe should not exceed 6000 feet per minute, then pipe area = eyl. area × piston-speed + 6000 (a). Assume that the av. mean effective pressure is 40 lbs. per sq. in., then cyl. area × piston-speed × 40 + 33,000 = horse-power (b). Dividing (a) by (b) and cancelling, we have pipe area + H.P. = .1375 sq. in. If we use 8000 ft. per min, as the allowable velocity, then the factor .1375 becomes .1031; that is, pipe area + H.P. = .1031, or pipe area × .97 = horse-power. This, however, gives areas of pipe smaller than are used in the most recent practice. A formula which gives results closely agreeing with practice, as shown in the above table is

Horse-power = 
$$6d^2$$
, or pipe diameter =  $\sqrt{\frac{H.P.}{6}}$  = .408  $\sqrt{H.P.}$ 

DIAMETERS OF CYLINDERS CORRESPONDING TO VARIOUS SIZES OF STEAM-PIPES BASED ON PISTON-SPEED OF ENGINE OF 600 FT. PER MINUTE. AND ALLOWABLE MEAN VELOCITY OF STEAM IN PIPE OF 4000, 6000, AND 8000 FT. PER MINUTE.

Diam. of pipe, inches	2	21/2	3	31/2	4	41/2	5	6
Vel. 4000.	5.2	6.5	7.7	9.0	10.3	11.6	12.9	15.5
" 6000	6.3	7.9	9.5	11.1	12.6	14.2	15.8	19.
" 8000	7.3	9.1	10.9	12.8	14.6	16.4	18.3	21.9
Horse-power, approx	20	31	45	62	80	100	125	180
Diam. of pipe, inches	7	8	9	10	11	12	13	14
Vel. 4000	18.1	20.7	23.2	25.8	28.4	31.0	33.6	36.1
" 6000	22.1	25.3	28.5	31.6	34.8	37.9	41.1	44.3
" 8000		29.2	32.9	36.5	40.2	43.8	47.5	51.1
Horse-power, approx		320	406	500	606	718	845	981

Formula. Area of pipe =  $\frac{\text{Area of cylinder} \times \text{piston-speed}}{\text{mean velocity of steam in pipe}}$ 

For piston-speed of 600 ft. per min. and velocity in pipe of 4000, 6000, and 8000 ft. per min. area of pipe = respectively .15, .10, and .075 × area of cylinder. Diam. of pipe = respectively .35, 3.102, and .2739 × diam. of cylinder. Reciprocals of these figures are 2.882, 3.162, and 3.651.

The first line in the above table may be used for proportioning exhaust-

pipes, in which a velocity not exceeding 4000 ft. per minute is advisable. The last line, approx. H.P. of engine, is based on the velocity of 6000 ft. per min. in the pipe, using the corresponding diameter of piston, and taking H.P. = 1/2 (diam. of piston in inches)2.

Sizes of Steam-pipes for Marine Engines. - In marine-engine practice the steam pipes are generally not as large as in stationary practice

for the same sizes of cylinder. Seaton gives the following rules:

Main Steam-pipes should be of such size that the mean velocity of flow does not exceed 8000 ft. per min. In large engines, 1000 to 2000 H.P., cutting off at less than half stroke, the steam-pipe may be designed for a mean velocity of 9000 ft., and 10,000 ft. for still larger engines.

In small engines and engines cutting later than half stroke, a velocity of less than 8000 ft. per minute is desirable.

Taking 8100 ft. per min. as the mean velocity, S speed of piston in feet per min., and D the diameter of the cyl.,

Diam, of main steam-pipe = 
$$\sqrt{\frac{D^2S}{8100}} = \frac{D}{90}\sqrt{S}$$
.

Stop and Throttle Valves should have a greater area of passages than the area of the main steam-pipe, on account of the friction through the circuitous passages. The shape of the passages should be designed so as to avoid abrupt changes of direction and of velocity of flow as far as possible. Area of Steam Ports and Passages =

$$\frac{\text{Area of piston} \times \text{speed of piston in ft. per min.}}{6000} = \frac{(\text{Diam.})^2 \times \text{speed}}{7639}.$$

Opening of Port to Steam.—To avoid wire-drawing during admission the area of opening to steam should be such that the mean velocity of flow does not exceed 10,000 ft, per min. To avoid excessive clearance the width of port should be as short as possible, the necessary area being obtained by length (measured at right angles to the line of travel of the valve). In practice this length is usually 0.6 to 0.8 of the diameter of the cylinder, but

in long-stroke engines it may equal or even exceed the diameter.

Exhaust Passages and Pipes.—The area should be such that the mean velocity of the steam should not exceed 6000 ft. per min., and the area should be greater if the length of the exhaust-pipe is comparatively long.

should be greater it the length of the exhaust-pipe is comparablely long. The area of passages from cylinders to receivers should be such that the velocity will not exceed soon from the soon from the soon purpose. The following table is computed on the basis of a mean velocity of flow of 8000 ft. per min. for the main steam-pipe, 10,000 for opening to steam, and 6000 for exhaust. A = area of piston, D its diameter.

STEAM AND EXHAUST OPENINGS.

Piston- speed, ft. per min.	Diam. of Steam-pipe $\div D$ .	Area of Steam-pipe ÷ A.	Diam. of Exhaust ÷ D.	Area of Exhaust + A.	Opening to Steam ÷ A.
300	0.194	0.0375	0.223	0.0500	0.03
400	0.224	0.0500	0.258	0.0667	0 04
500	0.250	0.0625	0.288	0.0833	0.05
600	0.274	0.0750	0.316		0.06
700 800	0.296 0.316	0.0875	0.341 0.365	0.1167 0.1333	0.07
900	0.335	0.1125	0.387	0.1500	0.09
1000	0.353	0.1250	0.400	0.1667	0.10

#### STEAM PIPES.

Bursting-tests of Copper Steam-pipes. (From Report of Chief Engineer Melville, U. S. N., for 1892.)—Some tests were made at the New York Navy Yard which show the unreliability of brazed seams in cop-per pipes. Each pipe was 8 in, diameter inside and 3 ft. 156 in. long. Both ends were closed by ribbed heads and the pipe was subjected to a hot-water pressure, the temperature being maintained constant at 371° F. Three

of the pipes were made of No. 4 sheet copper ("Stubbs" gauge) and the fourth was made of No. 3 sheet.

The following were the results, in lbs, per sq, in., of bursting-pressure:

Pipe number	1	2	3	4	4'
Actual bursting-strength	835	785	950	1225	1275
Calculated "	1336	1336	1569	1568	1568
Difference	501	551	619	343	293

The theoretical bursting-pressure of the pipes was calculated by using the

The encorrection oursing-pressure of the pipes was calculated by using the figures obtained in the tests for the strength of copper sheet with a brazed joint at 350° F. Pipes 1 and 2 are considered as having been annealed. The tests of specimens cut from the ruptured pipes show the injurious action of heat upon copper sheets; and that, while a white heat does not change the character of the metal, a heat of only slightly greater degree causes it to lose the fibrous nature that it has acquired in rolling, and a serious reduction in its tensile strength and ductility results.

All the brazing was done by expert workmen, and their failure to make a pipe-joint without burning the metal at some point makes it probable that,

with copper of this or greater thickness, it is seldom accomplished.

That it is possible to make a joint without thus injuring the metal was proven in the cases of many of the specimens, both of those cut from the pipes and those made separately, which broke with a fibrous fracture.

\*\*Rule for Thickness of Copper Steam-pipes\*\*. (U. S. Supervising Inspectors of Steam Vessels)—Multiply the working steam-pressure in lbs. per sq. in, allowed the boiler by the diameter of the pipe in inches, the distribution of the pipe in inches, the distribution of the pipe in inches. then divide the product by the constant whole number 8000, and add .0625 to the quotient; the sum will give the thickness of material required.

Example.—Let 175 lbs. = working steam-pressure per sq. in, allowed the boiler, 5 in. = diameter of the pipe; then  $\frac{175 \times 5}{100}$  $\frac{8000}{8000}$  + .0625 = .1718 + inch.

thickness required.

Reinforcing Steam-pipes. (Eng., Aug. 11, 1893.)-In the Italian Navy copper pipes above 8 in. diam, are reinforced by wrapping them with a close spiral of copper or Delta-metal wire. Two or three independent spirals are used for safety in case one wire breaks. They are wound at a

tension of about 114 tons per sq. in.

Wire-wound Steam-pipes.—The system instituted by the British Admiratly of winding all steam-pipes over 8 in. in diameter with 3/16-in. copper wire, thereby about doubling the bursting-pressure, has within recopper wire, thereby about couning the bursting-pressure, has within recent years been adopted on many merchant steamers using high-pressure steam, says the London Engineer. The results of some of the Admiratty tests showed that a wire pipe stood just about the pressure it ought to have stood when unwired, had the copper not been injured in the brazing.

Riveted Steel Steam-pipes have recently been used for high pressures. See paper on A Method of Manufacture of Large Steam-pipes, by Chas. H. Manuing, Trans. A. S. M. E., vol. xv.

Valves in Steam-pipes.—Should a globe-valve on a steam-pipe have

the steam-pressure on top or underneath the valve is a disputed question. With the steam-pressure on top, the stuffing-box around the valve-stem cannot be repacked without shutting off steam from the whole line of pipe; on the other hand, if the steam-pressure is on the bottom of the valve it all has to be sustained by the screw-thread on the valve-stem, and there is danger

of stripping the thread

A correspondent of the American Machinist, 1892, says that it is a very uncommon thing in the ordinary globe-valve to have the thread give out, but by water-hammer and merciless screwing the seat will be crushed down quite frequently. Therefore with plants where only one boiler is used he advises placing the valve with the boiler-pressure underneath it. On plants where several boilers are connected to one main steam-pipe he would reverse the position of the valve, then when one of the valves needs repacking the valve can be closed and the pressure in the boiler whose pipe it controls can be reduced to atmospheric by lifting the safety-valve. The repacking can then be done without interfering with the operation of the other boilers

He proposes also the following other rules for locating valves: Place valves with the stems horizontal to avoid the formation of a water-pocket. Never put the junction-valve close to the boiler if the main pipe is above the boiler, but put it on the highest point of the junction-pipe. If the other 676

plan is followed, the pipe fills with water whenever this boiler is stopped and the others are running, and breakage of the pipe may cause serious results. Never let a junction-pipe run into the bottom of the main pipe, but into the side or top. Always use an angle-valve where convenient, as there is more room in them. Never use a gate valve under high pressure unless a by-pass is used with it. Never open a blow-off valve on a boiler a little and then shut it; it is sure to catch the sediment and ruin the valve; throw it well open before closing. Never use a globe-valve on an indicator-pipe. For water, always use gate or angle valves or stop-cocks to obtain a clear pas-Buy if possible valves with renewable disks. Lastly, never let a man go inside a boiler to work, especially if he is to hammer on it, unless you break the joint between the boiler and the valve and put a plate of steel between the flanges.

Flanges for Steam-nozzles and Steam-pipe, used with the

Gill Water-tube Boiler, Phila., 1892.							
Size of pipe	3	4	5	6	7	8	9
Outside diameter of flange, inches	9	10	11	12	13	14	15
Pitch-circle for bolts, diam., "	7	8	9	10	11	12	13
Outside diam. of gaskets, "	51/6	61/6	71/2	816	91/2	101/6	111/6
Inside diam. of gaskets, "	31/6	61/2	51/2	61/2	71/2	81/2	916
Number of bolts	5	6	7	8	9	10	11
Ci	10	44	10	10	< 1	45	10
Size of pipe	10	11	12	13	14	15	16
Outside diameter of flange, inches	16	17	18	19	20	21	22
Pitch-circle for bolts, diam., "	14	15	16	17	18	19	20
Outside diam, of gaskets, "	121/6	131/6	141/6	151/6	1616	171/6	1816
Inside diam. of gaskets, "	101/3	1116	121/2	131/2	141/6	151/2	1616
Number of bolts	12	13	14	15	16 ~	17~	18

All holes drilled 15/16 in., with a jig accurately laid out,

All bolts to be % in. diam. by 31/2 in. long under the head. All bolts to have square heads and hexagon nuts.

The "Steam Loop?" is a system of piping by which water of condensation in steam-pipes is automatically returned to the boiler. In its simplest form it consists of three pipes, which are called the riser, the horizontal, and the drop-leg. When the steam-loop is used for returning to the boiler the water of condensation and entrainment from the steam pipe through which the steam flows to the cylinder of an engine, the riser is generally attached to a separator; this riser empties at a suitable height into the horizontal, and from thence the water of condensation is led into the drop-leg, which is connected to the boiler, into which the water of condensation is fed mo the drop-leg, which is connected to the boiler, into which the water of condensation is fed as soon as the hydrostatic pressure in drop-leg in connection with the steam-pressure in the pipes is sufficient to overcom- the boiler-pressure. The action of the device depends on the following principles: Difference of pressure may be balanced by a water-column: vapors or liquids tend to flow to the point of lowest pressure; rate of flow depends on difference of pressure and mass; decrease of static pressure in a steam-pipe or chamber is proportional to rate of condensation; in a steam-current water will be carried or swept along rapidly by friction. (Illustrated in Modern Mechanism, p. 807.)

Loss from an Uncovered Steam-pipe. (Bjorling on Pumpingengines.)-The amount of loss by condensation in a steam-pipe carried down a deep mine shaft has been ascertained by actual practice at the Clay Cross Colliery, near Chesterfield, where there is a pipe 7½ in. internal diam. 1100 ft. long. The loss of steam by condensation was ascertained by direct measurement of the water deposited in a receiver, and was found to be equivalent to about 1 lb, of coal per I.H.P. per phour for every 100 ft. of seam-pipe; but there is no doubt that if the pipes had been in the upoast shaft, and well covered with a good non-conducting material, the loss would

have been less. (For Steam-pipe Coverings, see p. 469, ante.)

### THE STEAM-BOILER.

The Horse-power of a Steam-boiler.-The term horse power has two meanings in engineering: First, an absolute unit or measure of the rate of work, that is, of the work done in a certain definite period of time, by a source of energy, as a steam-boiler, a waterfall, a current of air or water, or by a prime mover, as a steam-engine, a water-wheel, or a wind-mill. The value of this unit, whenever it can be expressed in foot-pounds of energy, as in the case of steam-engines, water-wheels, and waterfalls, is 33,000 foot-pounds per minute. In the case of boilers, where the work done, the conversion of water into steam, cannot be expressed in foot-pounds of available energy, the usual value given to the term horse-power is the evaporation of 30 !bs. of water of a temperature of 100° F. into steam at 70 lbs. pressure above the atmosphere. Both of these units are arbitrary; the first, 33,000 foot-pounds per minute, first adopted by James Watt, being considered equivalent to the power exerted by a good London draught-borse, and the 30 lbs. of water evaporated per hour being considered to be the steam requirement per indicated horse-power of an average engine.

quirement per indicated horse-power of an average engine.

The second definition of the term horse-power is an approximate measure of the size, capacity, value, or "rating" of a boiler, engine, water-wheel, other source or conveyer of energy, by which measure it may be described, bought and sold, advertised, etc. No definite value can be given to this measure, which varies largely with local custom or individual opinion of makers and users of machinery. The nearest approach to unformly which can be arrived at in the term" horse power, "used in this sense, is to say those power should be capable of steadily developing that horse-power for a long period of time under ordinary conditions of use and wratice, leaving norse-power, should be capable of steadiny developing that norse-power for a long period of time under ordinary conditions of use and practice, leaving to local custom, to the judgment of the buyer and seller, to written contracts of purchase and sale, or to legal decisions upon such contracts, the interpretation of what is meant by the term "ordinary conditions of use and practice." (Trans. A. S. M. E., vol. vii. p. 236.)

The committee of the A. S. M. E. on Trials of Steam-bollers in 1884 (Trans.,

vol. vi. p. 265) discussed the question of the horse-power of boilers as follows: The Committee of Judges of the Centennial Exhibition, to whom the trials of competing boilers at that exhibition were intrusted, met with this same problem, and finally agreed to solve it, at least so far as the work of that committee was concerned, by the adoption of the unit, 30 lbs. of water evaporated into dry steam per hour from feed-water at 100° F., and under a pressure of 70 lbs. per square inch above the atmosphere, these conditions being considered by them to represent fairly average practice. The quantity of heat demanded to evaporate a pound of water under these conditions is 110.2 British thermal units, or 1.14% units of evaporation. The unit of power proposed is thus equivalent to the development of 33,305 heat units per hour, or 34 488 units of evaporation.

Your committee, after due consideration, has determined to accept the Centennial Standard, the first above mentioned, and to recommend that in all standard trials the commercial horse-power be taken as an evaporation of 30 lbs. of water per hour from a feed-water temperature of 100° F. into steam at 70 lbs. gauge pressure, which shall be considered to be equal to 341/2 units of evaporation, that is, to 341/6 lbs. of water evaporated from a feed-

water temperature of 212° F, into steam at the same temperature. This standard is equal to 33,305 thermal units per hour. It is the opinion of this committee that a boiler rated at any stated number of horse-powers should be capable of developing that power with easy firing, moderate draught, and ordinary fuel, while exhibiting good economy; and further, that the boiler should be capable of developing at least one third more than its rated power to meet emergencies at times when maximum

economy is not the most important object to be attained.

Unit of Evaporation.—It is the custom to reduce results of boilertests to the common standard of weight of water evaporated by the unit weight of the combustible portion of the fuel, the evaporation being considered to have taken place at mean atmospheric pressure, and at the temperature due that pressure, the feed-water being also assumed to have been supplied at that temperature. This is, in technical language, said to be the equivalent evaporation from and at the boiling-point at atmospheric pressure, or "from and at 212° F." This unit of evaporation, or one pound of water evaporated from and at 212°, is equivalent to 965.7 British thermal units.

Measures for Comparing the Buty of Boilers.—The measure of the efficiency of a boiler is the number of pounds of water evaporated per pound of combustible, the evaporation being reduced to the standard of "from and at 3129;" that is, the equivalent evaporation from feed-water at a temperature of 212° F. into steam at the same temperature.

The measure of the capacity of a boiler is the amount of "boiler horse-power" developed, a horse-power being defined as the evaporation of 30 lbs, of water per hour from 100° F, into steam at 70 lbs, pressure, or 34½ lbs, per

hour from and at 212°.

The measure of relative rapidity of steaming of boilers is the number of pounds of water evaporated per hour per square foot of water-heating sur-

The measure of relative rapidity of combustion of fuel in boiler-furnaces is the number of pounds of coal burned per hour per square foot of gratesurface.

### STEAM-BOILER PROPORTIONS.

Proportions of Grate and Heating Surface required for a given Horse-power.—The term horse-power here means capacity to evaporate 30 lbs. of water from 100° F., temperature of feed-water, to steam of 70 lbs., gauge-pressure = 34.5 lbs. from and at 212° F.

Average proportions for maximum economy for land boilers fired with

good a

anthracite coai:		
Heating surface per horse-power	11.5	sq. ft.
Grate " "	1/3	**
Ratio of heating to grate surface	34.5	
Water evap'd from and at 212° per sq. ft. H.S. per hour	3	lbs.
Combustible burned per H.P. per hour	3	**
Coal with 1/6 refuse, lbs. per H.P. per hour	5.6	66
Combustible burned per sq. ft. grate per hour	9	**
Coal with 1/6 refuse, lbs. per sq. ft. grate per hour	10.8	66
Water evap'd from and at 212° per lb, combustible	11.5	66
Water evap'd from and at 212° per lb. combustible "coal (1/6 refuse)	9.6	44

The rate of evaporation is most conveniently expressed in pounds evaporated from and at 212° per sq. ft. of water-heating surface per hour, and the rate of combustion in pounds of coal per sq. ft. of grate-surface per hour.

Heating-surface.—For maximum economy with any kind of fuel a boiler should be proportioned so that at least one square foot of heating-surface should be given for every 3 lbs. of water to be evaporated from and at 212° F. per hour. Still more liberal proportions are required if a portion of the heating-surface has its efficiency reduced by: 1. Tendency of the heated gases to short-circuit, that is, to select passages of least resistance and flow through them with high velocity, to the neglect of other passages.

2. Deposition of soot from smoky fuel.

3. Incrustation. If the heating-surfaces are clean, and the heated gases pass over it uniformly, little if any increase in economy can be obtained by increasing the heating-surface beyond the proportion of 1 sq. ft. to every 3 lbs. of water to be evaporated, and with all conditions favorable but little decrease of economy will take place if the proportion is I sq. ft. to every 4 lbs. evaporated; but in order to provide for driving of the boiler beyond its rated capacity, and for possible decrease of efficiency due to the causes above named, it is better to adopt 1

sq. ft. to 3 lbs. evaporation per hour as the minimum standard proportion.
Where economy may be sacrificed to capacity, as where fuel is very cheap, it is customary to proportion the heating-surface much less liberally. following table shows approximately the relative results that may be ex-

pected with different rates of evaporation, with anthracite coal.

Lbs. water evapor'd from and at 212° per sq. ft. heating-surface per hour: 3.5 Sq. ft. heating-surface required per horse-power: 8.6 13.8 11.5 9.8 6.8 5.8 4.3 38 3.5 Ratio of heating to grate surface if 1/3 sq. ft, of G. S. is required per H.P.; 29.4 25.8 13.7 34.5 20.4 17.4 10.5 41.4 11.4 Probable relative economy: 100 80 60 100 Probable temperature of chimney gases, degrees F.:

450 518 585 652 855 922 990

The relative economy will vary not only with the amount of heating-surface per horse-power, but with the efficiency of that heating-surface as regards its capacity for transfer of heat from the heated gases to the water, which will depend on its freedom from soot and incrustation, and upon the circulation of the water and the heated gases.

With bituminous coal the efficiency will largely depend upon the thorough-

ness with which the combustion is effected in the furnace.

The efficiency with any kind of fuel will greatly depend upon the amount of air supplied to the furnace in excess of that required to support combustion. With strong draught and thin fires this excess may be very great,

causing a serious loss of economy.

Measurement of Heating-surface.—Authorities are not agreed as to the methods of measuring the heating-surface of steam-bollers. The usual rule is to consider as heating-surface all the surfaces that are surrounded by water on one side and by flame or heated gases on the other, but there is a difference of opinion as to whether tuoular heating-surface should be figured from the inside or from the outside diameter. Some writers say, measure the heating-surface always on the smaller side—the fire side of the tube in a horizontal return tubular boiler and the water side in a water-tube boiler. Others would deduct from the heating-surface thus measured an allowance for portions supposed to be ineffective on account of being cov-

ered by dust, or being out of the direct current of the gases.

For the sake of uniformity, however, it would appear to be the best method to consider all surfaces as heating-surfaces which transmit heat from the flame or gases to the water, making no allowance for different degrees of effectiveness; also, to use the external instead of the internal diameter of tubes, for greater convenience in calculation, the external diameter of boiler-tubes usually being made in even inches or half inches. There would seem to be no good reason for considering the smaller surface in a tube as the heating-surface, for the transmission of heat through plates that are ribbed or corrugated on one side does not appear to be proportional to the smaller surface, but rather to the larger. Thus the Serve ribbed tube transmits more heat to the water per foot of length than a plain tube of same external diameter, and a ribbed steam-radiator radiates more heat than a plain radiator having the same internal or smaller surface.

Rule for finding the heating-surface of vertical tubular boilers: Multiply the circumference of the fire-box (in inches) by its height above the grate; multiply the combined circumference of all the tubes by their length, and to these two products add the area of the lower tube-sheet; from this sum subtract the area of all the tubes, and divide by 144; the quotient is the

number of square feet of heating-surface.

Rule for finding the heating-surface of horizontal tubular boilers; Multi-ply too thirds of the circumference of the shell (in inches) by its length; multiply the combined length of the tubes by their combined circumference, to the sum of these products add two thirds of the area of both tube sheets; from this sum subtract the combined area of all the tubes, and divide the remainder by 144: the result is the number of square feet of heating-surface.

RULE for finding the square feet of heating surface in tubes: Multiply the number of tubes by the diameter of a tube in inches, by its length in feet,

and by .2618.

Horse-power, Builder's Rating. Heating-surface per Horse-power.—It is a general practice among builders to furnish about 12 square feet of heating-surface per horse-power, but as the practice is not uniform, bids and contracts should always specify the amount of heating-surface to be furnished. Not less than one third square foot of grate-surface should be furnished per horse-power.

Engineering News, July 5, 1894, gives the following rough-and-ready rule for finding approximately the commercial horse-power of tubular or water-tube boilers: Number of tubes  $\times$  their length in feet  $\times$  their nominal diameter in inches  $\div$  50 = nLd  $\div$  50. The number of square feet of surface

in the tubes is  $\frac{n\pi dL}{12} = \frac{nLd}{3.82}$ , and the horse-power at 12 square feet of surface of tubes per horse power, not counting the shell, = nLd + 45.8. If 15 square feet of surface of tubes be taken, it is nLd + 57.3. Making allowance for the heating-surface in the shell will reduce the divisor to about 50.

Horse-power of Marine and Locomotive Boilers.-The term horse-power is not generally used in connection with boilers in marine practice, or with locomotives. The boilers are designed to suit the engines, and are rated by extent of grate and heating-surface only,

Grate-surface. The amount of grate-surface required per horse ower, and the proper ratio of heating-surface to grate-surface are ex-tremely variable, depending chiefly upon the character of the coal and upon the rate of draught. With good coal, low in ash, approximately equal results may be obtained with large grate-surface and light draught and with small grate-surface and strong draught, the total amount of coal burned per hour being the same in both cases. With good bituminous coal, like Pittsburgh, low in ash, the best results apparently are obtained with strong draught in asin, one cess resums apparency are obtained with stong draught and high rates of combustion, provided the grate-surfaces are cut down so that the total coal burned per hour is not too great for the capacity of the heating-surface to absorb the heat produced.

With coals high in ash, especially if the ash is easily fusible, tending to choke the grates, large grate-surface and a slow rate of combustion are

required, unless means, such as shaking grates, are provided to get rid of

the ash as fast as it is made.

The amount of grate-surface required per horse-power under various conditions may be estimated from the following table:

Lbs. Water	at 212° per 1b., Coal.	Lbs. Coal per H.P. per hour.	Pounds of Coal burned per square foot of Grate per hour.							_	
			Sq. Ft. Grate per H. P.								
Good coal and boiler,	10	3.45 3.83	.43	.35	.28	.23	.17	.14	.11	.10	.09
Fair coal or	8.61	4.	.50	.40	.33	.26	.19	.16	.13	.12	.10
boiler,	8 7	4.31 4.93	.54	.43	.36	.29	.22	.17	.14	.13	.11
Poor coal or	6.9	5. 5.75	.63	.50	.42	.34	.25	.20	.17	.15	.13
boiler,	6 5	6.9	.86	.69	58	.46	.35	.28	.19	.22	.17
Lignite and poor boiler,	3.45	10.	1.25	1.00	.83	.67	.50	.40	.33	.29	.25

In designing a boiler for a given set of conditions, the grate-surface should be made as liberal as possible, say sufficient for a rate of combustion of 10 lbs. per square foot of grate for anthracite, and 15 lbs. per square foot for bituminous coal, and in practice a portion of the grate-surface may be bricked over if it is found that the draught, fuel, or other conditions render it advisable.

Proportions of Areas of Flues and other Gas-passages. -Rules are usually given making the area of gas-passages bear a certain ratio to the area of the grate-surface; thus a common rule for horizontal tubular boilers is to make the area over the bridge wall 1/7 of the grate-

surface, the flue area 1/8, and the chimney area 1/9.

For average conditions with anthracite coal and moderate draught, say a rate of combustion of 12 lbs. coal per square foot of grate per hour, and a ratio of heating to grate surface of 30 to 1, this rule is as good as any, but it is evi-dent that if the draught were increased so as to cause a rate of combustion of 24 lbs., requiring the grate-surface to be cut down to a ratio of 60 to 1, the areas of gas-passages should not be reduced much, because the grate-surface is reduced. The coal burned being the same under the changed conditions, and there being no reason why the gases should travel at a higher velocity, the actual areas of the passages should remain as before, but the ratio of the area to the grate-surface would in that case be doubled.

Mr. Barrus states that the highest efficiency with anthractic coal is obtained when the tube area is 1/9 to 1/10 of the grate-surface, and with bituminous coal when it is 1/6 to 1/7, for the conditions of medium rates of combustion, such as 10 to 12 lbs, per square foot of grate per hour, and 12 square feet of heating surface allowed to the horse-power.

The tube area should be made large enough not to choke the draught, and so lessen the capacity of the boiler; if made too large the gases are apt to select the passages of least resistance and escape from them at a high velocity and high temperature.

This condition is very commonly found in horizontal tubular boilers where

the gases go chiefly through the upper rows of tubes; sometimes also in vertical tubular boilers, where the gases are apt to pass most rapidly

through the tubes nearest to the centre.

Air-passages through Grate-bars,—The usual practice is, air-opening = 30% to 50% of area of the grate; the larger the better, to avoid stoppage of the air-supply by elimker; but with coal free from clinker much smaller air-space may be used without detriment. See paper by F. A. Scheffler, Trans. A. S. M. E., vol. xv. p. 503.

#### PERFORMANCE OF BOILERS.

Clark (Steam-engine, vol. i. p. 327) gives the following formulas for the relation of coal and water consumed in steam-boilers per square foot of grate-area per hour, and the ratio of the heating-surface to the area of the fire-grate. Water taken as evaporated from and at 212° F.

In which w = weight of water in pounds per square foot of grate per hour; c = pounds of fuel per square foot of grate per hour;

r = ratio of heating to grate surface.

There are minimum rates of consumption of fuel below which these formulas are not applicable. The limit varies for each kind of boiler, and it varies with the surface-ratio. It is imposed by the fact that the maximum evaporative power of fuel is a fixed quantity, and is naturally at that point where the reduction of the rate of combustion for a given ratio procures the absorption into the boiler of the whole of the proportion of the heat which is available for evaporation. In the combustion of good coal the limit of evaporative efficiency may be taken as measured by 12½ lbs. of water from and at 212° F. Based on these formulæ Clark gives the following table:

Evaporative Performance of Steam-boilers for increasing Rates of Combustion and different Surface-ratios, For best coal; surface-ratio 30,

Kind of Boiler.	Water from and at 212° F. per hour.	Fuel per Square Foot of Grate per hour, in pounds.							
		5	10	15	20	30	40	50	
Stationary. Marine. Portable. Locomotive.	Per sq. ft. of grate Per lb. of coal Per sq. ft. of grate Per lb. of coal Per sq. ft. of grate Per lb. of coal Per sq. ft. of grate Per lb. of coal	12.5 62.5* 12.5 50 10	lbs. 116 11.56 117 11.69 93 9.3 105 10.5	lbs. 163 10.89 168 11.25 136 9.01 154 10.26	lbs. 211 10.56 219 10.95 179 8.95 202 10.10	322	424 10.61 351 8.77 396	lbs. 498 9.96 527 10.54 437 8.74 493 9.86	
Guille a matic 50									

Surface-ratio 50. 10 15 20 30 40 50 lbs. lbs. lbs. lbs. lbs. lbs. lhs. Per sq. ft. of grate 62.5\* Per lb. of coal..... 12.5 187.5\* 247 Stationary. 125\* 342 438 534 12.5 12.5 12.33 11.41 10.95 10.67 Marine. Per sq. ft. of grate 62.5\* 125\* 187.5\* 245 348 450 552 Per lb. of coal ..... 11.58 11.25 11.05 12.5 12.5 12,25 Per sq. ft. of grate 62.5\* 278 Portable. 106 149 192 364 450 Per lb. of coal.. ... 12.5 Per sq. ft. of grate 62.5\* 9.93 9.10 9.00 10.6 9.6 9.27 120 168 217 508 Locomotive. 314 411

11.95 11.20

10.85 10 45 10.26 10.15

Per lb. of coal ..... 12.5

<sup>\*</sup> These quantities fall below the scope of the formulæ for the water, as explained in the text.

Surface ratio 75.

		30	40	50	60	75	90	100
Locomotive.	Per sq. ft, of grate. Per lb. of coal	342	439	536	633		927	102C

General Conditions which secure Economy of Steambollers,—In general, the highest results are produced where the temperature of the escaping gases is the least. An examination of this question is made by Mr. G. H. Barrus in his book on "Boiler Tests," by selecting those tests made by him, six in number, in which the temperature exceeds the average, that is, 375° F., and comparing with five tests in which the temperature is less than 375°. The boilers are all of the common horizontal type, and all use anthractic coal of either egg or broken size. The average frue temperatures in the two series was 444° and 343° respectively, and the difference was 101°. The average evaporations are 10.40 bls, and 11.02 bls, respectively, and the lowest result corresponds to the case of the highest flue temperature. In these tests it appears, therefore, that a reduction of 101° in the temperature of the waste gases secured an increase in the evaporation of 6%. This result corresponds quite closely to the effect of lowering the temperature of the gases by means of a flue-heater where a reduction of 107° was attended by a increase of 7% in the evaporation per pound of coal.

A similar comparison was made on horizontal tubular boilers using Cumberland coal. The average flut temperature in four tests is 450° and the average evaporation is 11.34 lbs. Six boilers have temperatures below 415°, the average of which is 383°, and these give an average evaporation of 11.5 lbs. With 65° less temperature of the escaping gases the evaporation is

higher by about 4%.

The wasteful effect of a high flue temperature is exhibited by other boilers than those of the horizontal tubular class. This source of waste was shown to be the main cause of the low economy produced in those vertical boilers which are deficient in heating-surface.

Relation between the Henting-surface and Grate-surface to obtain the Highest Efficiency.—A comparison of three tests of horizontal tubular boilers with anthracite coal, the ratio of heating-surface to grate-surface being 344 to 1, with three other tests of similar boilers, in which the ratio was 48 to 1, showed practically no difference in the results. The evidence shows that a ratio of 36 to 1 provides a sufficient quantity of heating-surface to secure the full efficiency of anthracite coal where the rate of combustion

is not more than 12 lbs. per sq. ft. of grate per hour.

In other than 12 lbs. per sq. ft. of grate per hour.

In other than 12 lbs. per sq. ft. of grate per hour.

In other than 12 lbs. per sq. ft. of grate per hour.

In other than 12 lbs. per sq. ft. of grate pound of coal, and a high temperature of the escaping gases indicated that a still further increase would be beneficial. Among the high results produced on common horizontal tubular boilers using bituminous coal, the highest occurs where the ratio is 53.1 to 1. This boiler gave an evaporation of 12.47 lbs. A double-deck boiler furnishes another example of high performance, an evaporation of 12.49 lbs. having been obtained with bituminous coal, and in this case the ratio is 65 to 1. These examples indicate that a much larger amount of heating-surface is required for obtaining the full efficiency of bituminous coal than for boilers using anthracite coal. The temperature of the escaping gases in the same toller is invariably higher when bituminous coal is used than when anthracite coal is used. The deposit of soot on the surfaces when bituminous coal is used interferes with the full efficiency of the surface, and an increased area is demanded as an offset to the loss which this deposit occasions. It would seem, then, that if a ratio of 36 to 1 is sufficient for anthracite coal, from 45 to 59 should be provided when bituminous coal is burned, especially in cases where the rate of combustion is above 10 or 12 lbs, per sq. ft. of grate per hour.

The number of tubes controls the ratio between the area of grate-surface and area of tube opening. A certain minimum amount of tube-opening is

required for efficient work.

The best results obtained with anthracite coal in the common horizontal boiler are in cases where the ratio of area of grate-surface to area of tube-opening is larger than 9 to 1. The conclusion is drawn that the highest efficiency with anthracite coal is obtained when the tube-opening is from 1/9 to 1/10 of the grate-surface.

When bituminous coal is burned the requirements appear to be different. The effect of a large tube opening does not seem to make the extra tubes inefficient when bituminous coal is used. The highest result on any boiler of the horizontal tubular class, fired with bituminous coal, was obtained where the tube-opening was the largest. This gave an evaporation of 12.47 lbs., the ratio of grate-surface to tube-opening being 5.4 to 1. The next highest result was 12.42 lbs., the ratio being 5.2 to 1. Three high results, averaging 12.01 lbs., were obtained when the average ratio was 7.1 to 1. Without going to extremes, the ratio to be desired when bituminous coal is used is that which gives a tube-opening having an area of from 1/6 to 1/7 of the gratesurface. This applies to medium rates of combustion of, say, 10 to 12 lbs. per sa, ft. of grate per hour, 12 sq, ft. of water-heating surface being allowed per horse-power.

A comparison of results obtained from different types of boilers leads to the general conclusion that the economy with which different types of boilers operate depends much more upon their proportions and the conditions under which they work, than upon their type; and, moreover, that when these proportions are suitably carried out, and when the conditions are favorable, the various types of boilers give substantially the same eco-

nomic result.

Efficiency of a Steam-boiler.—The efficiency of a boiler is the percentage of the total heat generated by the combustion of the fuel which is utilized in heating the water and in raising steam. With anthracite coal the heating-value of the combustible portion is very nearly 14,500 B. T. U. per lb., equal to an evaporation from and at 212 of 14,500 + 966 13 lbs. of water. A boiler which when tested with anthracite coal shows an evaporation of 12 lbs. of water per lb. of combustible, has an efficiency of 12 + 15 = 80%, a figure which is approximated, but scarcely ever quite reached, in the best practice. With bituminous coal it is necessary to have a determination of its heating-power made by a coal calorimeter before the

a determination of its neating-power made by a coal calorimeter before the efficiency of the boiler using it can be determined, but a close estimate may be made from the chemical analysis of the coal. (See Coal.)

The difference between the efficiency obtained by test and 100% is the sum of the numerous wastes of heat, the chief of which is the necessary loss due to the temperature of the chimney-gases. If we have an analysis and a calorimetric determination of the heating-power of the coal (properly samially according to the coal properly according to the pled), and an average analysis of the chimney-gases, the amounts of the several loses may be determined with approximate accuracy by the method

described below. Dota given

Data given:		
1. Analysis of the Coal. Cumberland Semi-bituminous.	2. Analysis of the Dry Ch gases, by Weight.	IMNEY-
Carbon 80.55	С. О.	N.
Hydrogen 4.50	$CO_2 = 13.6 = 3.71  9.89$	
Oxygen 2.70	$CO^{\circ} = .2 = .09$ .11	
Nitrogen 1.08	$O = 11.2 = \dots 11.20$	
Moisture 2.92	N = 75.0 =	75.00
Ash 8.25		
Programme and the same	100.0 3.80 21.20	75.00
100.00		

Heating-value of the coal by Dulong's formula, 14,243 heat-units.

The gases being collected over water, the moisture in them is not determined. 3. Ash and refuse as determined by boiler-test, 10.25, or 2% more than that

found by analysis, the difference representing carbon in the ashes obtained in the boiler-test.

Temperature of external atmosphere, 60° F. 5. Relative humidity of air, 60%, corresponding (see air tables) to .007 lb. of vapor in each lb. of air

6. Temperature of chimney-gases, 560° F.

Calculated results:

The carbon in the chimney-gases being 3.8% of their weight, the total the carbon burned is 80.35 - 2 = 78.55% of the weight of the coal, the weight of the dry gases per lb. of coal is  $28.32 \times 78.55 + 100 = 20.67$  lbs. Each pound of coal furnishes to the dry chimney-gases .2555 lb. C, .0108N, and  $\left(2.70 - \frac{4.50}{3.00}\right) + \frac{100}{3.00} = \frac{20.11}{3.00}$ weight of dry gases per lb. of carbon burned is  $100 \div 3.8 = 26.32$  lbs. Since

+ 100 = .0214 lb, O; a total of .8177, say .82 lb. This sub-

tracted from 20.67 lbs, leaves 19.85 lbs, as the quantity of dry air (not including moisture) which enters the furnace per pound of coal, not counting the air required to burn the available hydrogen, that is, the hydrogen minus one air required to burn the available hydrogen, that is, the hydrogen minus one eighth of the oxygen chemically combined in the coal. Each lb. of coal burned contained .045 lb. H, which requires .045  $\times$  8 = .36 lb. O for its combustion. Of this, .027 lb. is furnished by the coal itself, leaving .333 lb. 10 come from the air. The quantity of air needed to supply this oxygen (air containing 2% by weight of oxygen) is .333 + .23 = 1.45 lb., which added to the 19.85 lbs. already found gives 21.30 lbs. as the quantity of dry air supplied to the furnace per lb. of coal burned.

The air carried in as vapor is .0071 lb. for each lb. of dry air, or 21.3 × .0071 = 0.15 lb. for each lb. of coal. Each lb. of coal contained .029 lb. of moisture, which was evaporated and carried into the chimney-gases. The .045 lb.

of H per lb. of coal when burned formed  $.045 \times 9 = .405$  lb. of H<sub>2</sub>O. From the analysis of the chimney-gas it appears that  $.09 \div 3.80 = 2.3\%$  of the carbon in the coal was burned to CO instead of to  $CO_2$ .

We now have the data for calculating the various loses of heat as follows,

for each pound of coar burned:			
		Heat- units.	Per cent of Heat-value of the Coal.
21.3 lbs. dry air × (560° - 60°) × sp. heat .238	=	2534.7	17.80
.15 lb. vapor in air $\times$ (560° - 60°) $\times$ sp. heat .48	=	36.0	0.25
.029 lb. moisture in coal heated from 60° to 212°	=	4.4	0.03
" evaporated from and at 212°; .029 × 966	=	28.0	0.20
" steam (heated from 212° to 560°) $\times$ 348 $\times$ .48	=	4.8	0.03
.405 lb, H <sub>2</sub> O from H in coal $\times$ (560° - 60°) $\times$ .48	=	97.2	0.68
.0237 lb. C burned to CO; loss by incomplete com-			
bustion, $.0237 \times (14544 - 4451)$	=	239.2	1.68
.02 lb. coal lost in ashes; .02 × 14544	=	290.9	2.04
Radiation and unaccounted for, by difference	=	712.1	5.00
		3,947.3	27.71
Utilized in making steam, equivalent evaporation			
10.66 lbs. from and at 212° per lb. of coal	=	10,295.7	72.29
		112.2.2	
		14,243.0	100.00

The heat lost by radiation from the boiler and furnace is not easily determined directly, especially if the boiler is enclosed in brickwork, or is protected by non-conducting covering. It is customary to estimate the heat lost by radiation by difference, that is, to charge radiation with all the heat lost which is not otherwise accounted for.

One method of determining the loss by radiation is to block off a portion of the grate-surface and build a small fire on the remainder, and drive this fire with just enough draught to keep up the steam-pressure and supply the heat lost by radiation without allowing any steam to be discharged, weighted ing the coal consumed for this purpose during a test of several hours' dura-

tion. Estimates of radiation by difference are apt to be greatly in error, as in this difference are accumulated all the errors of the analyses of the coal and of the gases. An average value of the heat lost by radiation from a boiler set in brickwork is about 4 per cent. When several boilers are in a battery and enclosed in a boiler-house the loss by radiation may be very much less, since much of the heat radiated from the boiler is returned to it

much less, since much of the heat radiated from the boiler is returned to it in the air supplied to the furnace, which is taken from the boiler-room. An important source of error in making a "heat balance" such as the one above given, especially when highly bituminous coal is used, may be due to the non-combustion of part of the hydrocarbon gases distilled from the coal immediately after firing, when the temperature of the furnace may be reduced below the point of ignition of the gases. Each pound of hydrogen which escapes burning is equivalent to a loss of heat in the furnace of 63,000 heat-units.

In analyzing the chimney gases by the usual method the percentages of the constituent gases are obtained by volume instead of by weight. To reduce percentages by volume to percentages by weight, multiply the per-centage by volume of each gas by its specific gravity as compared with air, and divide each product by the sum of the products.

The pounds of air required to burn a pound of carbon may be obtained directly from the analysis by volume by the following formula:

Lbs. of air required to burn  $\frac{4}{3} = \frac{4}{3} \left\{ \frac{2CO_2 + O) + CO}{CO_2 + CO} \right\} + 0.23;$ 

In which O, CO<sub>2</sub>, and CO are the percents, by volume, of the several constituents of the flue gases.

Lbs. of air per pound  $= \{Lbs. of air per pound\} \times \{Per cent of carbon of coal\}$ 

To reduce to volume at temperature of 32° F. make use of the formula  $V_0 = 12.387 \times lbs$ , of air per pound of coal.

# TESTS OF STEAM-BOILERS.

Boiler-tests at the Centennial Exhibition, Philadelphia, 1876.—(See Reports and Awards Group XX, International Exhibi-

phia, 1876; also, Clark on the Steam-engine, vol. i, page 253, Competitive tests were made of fourteen boilers, using good anthracite coal, one boiler, the Galloway, being tested with both anthracite and semi-bituminous coal. Two tests were made with each boiler: one called the capacity trial, to determine the economy and capacity at a rapid rate of driving; and the other called the economy trial, to determine the economy and capacity at a rapid rate of maximum economy and rated capacity. The following table gives the principal results obtained in the economy trial, together with the capacity and economy figures of the capacity rial for comparison.

	Economy Tests.								Tests.		
Name of Boiler.	Ratio Water-heating Surface to Grate-surface.	Coal burned per sq ft. Grate per hour.	Per cent Ash and Refuse.	Water evap, from 100° to 70 lbs. p. s.ft. H.S.per hr.	Water evap. from and at 212° p. lb. comb' ble cor. for Quality of Steam.	Temperature in Uptake.	Moisture in Steam.	Superheating of Steam.	Horse-power.	Horse-power.	Water evap. from and at 212° per lb. Com- bustible.
Rogers & Black	34.6 64.3 30.6 45.8 87.7 23.7 23.7 15.6 27.3 30.7 17.5 20.9 33.5 14.0	12.0 6.8 12.1 10.0 9.6 7.9 8.0 12.4 12.3 9.7 10.8 9.3 8.0	10.4 11.3 11.1 11.0 11.1 8.8 10.3 8.5 9.5 9.3 9.0 11.4 11.0 9.9	1.68 1.87 2.42 2.43 3.63 3.20 2.32 2.75 3.30 2.64 3.82 1.38 4.44 3.43	9.613	deg 393 415 333 411 296 303 325 420 517 524 417  430 374 572	1.3 2.7 0.3 0.9	de g 41.4 32.6 9.4  1.4 71.7 20.5 15.7	57.8 47.0 99.8 135.6 103.3 90.9 42.6 82.4 147.5 98.0 72.1 51.7 45.7	125.0 186.6 133.8 125.1 58.7 108.4 162.8 132.8 99.9 108.0 67.8 67.2	9.145 9.568 8.397 9.974 9.865 9.429
Averages	0			2.77	11.123				85.0	110.8	10.251

The comparison of the economy and capacity trials shows that an average increase in capacity of 30 per cent was attended by a decrease in economy of 8 per cent, but the relation of economy to rate of driving varied greatly in the different boilers. In the Kelly boiler an increase in capacity of 22 per cent was attended by a decrease in economy of over 18 per cent, while the Smith boiler with an increase of 32 per cent in capacity showed a slight increase in economy.

One of the most important lessons gained from the above tests is that there is no necessary relation between the type of a boiler and economy. Of the five boilers that gave the best results, the total range of variation between the highest and lowest of the five being only 2.3%, three were water-tube boilers, one was a horizontal tubular boiler, and the fifth was a combination of the two types. The next boiler on the list, the Galloway, was an internally fired boiler, all of the others being externally fired. The following is a brief description of the principal constructive features of the fourteen boilers:

boilers:	• •
Root	4-in. water-tubes, inclined 20° to horizontal; reverse
Firmenich	draught. 3-in, water-tubes, nearly vertical; reversed draught
Lowe	Cylindrical shell, multitubular flue.
Smith	Cylindrical shell, multitubular flue—water-tubes in
SIIII	side flues.
Babcock & Wilcox	31/2-in. water-tubes, inclined 15° to horizontal; re
Galloway	versed draught. Cylindrical shell, furnace-tubes and water-tubes.
Andrews	Square fire-box and double return multitubular flues
Harrison	§ 8 slabs of cast-iron spheres, 8 in. in diameter; re
220772001777777777777777777777777777777	versed draught,
Wiegand	4-in. water-tubes, vertical, with internal circulating
Anderson	
Kelly	3-in. flue-tubes, nearly horizontal; return circulation (\$\frac{1}{3}\)-in. water-tubes, slightly inclined; each divided by internal diaphragm to promote circulation.
Easter	internal diaphragm to promote circulation.
Exeter	27 hollow rectangular cast-iron slabs. Rotating horizontal cylinder, with flue-tubes,
Rogers & Black	Vertical cylindrical boiler, with external water-tubes
	To Dollara The following tobles one given by 6

Tests of Tubulous Boilers.—The following tables are given by S. H. Leonard, Asst. Engr. U. S. N., in Jour. Am. Soc. Naval Engrs. 1890. The tests were made at different times by boards of U. S. Naval Engineers, except the test of the locomotive-torpedo boiler, which was made in England.

		per sq. ft. hour.	Evaporation from and at 212° F. Weights, lbs.			from and at			Weights, lbs.			in. of	e, lbs.	B, Bit.
No.	Type.	Coal burned per so Grate per hour	Per lb. Com'ble.	Per sq. ft. H. Surface.	Per cu. ft. Space.	E, Empty. S, Steaming Level.	Per I.H.P.	Per sq. ft. H. Surface.	Per lb. Water evaporated.	Air-pressure, i Water.	Steam-pressure,	Coal. A, Anth.;		
						E 40,670	_					-		
1	Belleville	12.8	10.42	5.2	6.4	E 40,670 S 42,770	204	53.2	10.1	Nat'l.	111	В.		
2	Herreshoff	\$ 9.3 25.8	10.23 8.68	3.1 8	$\frac{9.1}{23.8}$	E 2,945 S 3,050	96 33	14.8	4.8 1.8	Jet. Jet.	120 195	A.		
3	Towne	1 4.3 24.5	13.4 6 77	2.7 8.2	10 30.4	E 1,380 S 1,640	172 56	21.8	$\frac{8.1}{2.6}$	Nat'l. 1.14	152	A. A.		
4	Ward	7.9 15.5 62.5	10.77 10.01 7.01	1.7 3.2 10	5.8 11 34.2	E 1,682 S 1,930	154 82 26	13.2	7.7 4.07 1.3	Nat'l. Jet. Jet.	17 161	A. A. B.		
5	Scotch	j 24.8 j 38	9.98 9.06	8.6 12.8	11 16.3	E 18,900 S 30,000		41.2	4.7 3.1	2.08 4.01	77 78	A. A.		
6	Locom'tive	98.3		17.1 20.05	30.5	S 34,990	47.7 33.3	31.3	1.8	3.13 4.95	125 123	В.		
	torpedo,	1 120.8	8.44		36.2	E 26,533				4.95	160			
7 8	Ward Thorny-	55.04	0.44	9.47	32.1	S 30,474	26	12.3	1.3	z	100	ь.		
0	eroft. (U. S.S.Cush-	45		··· •		E 20,160 S 24,640	*31	10 3		3	245	В.		
_	ing.)	ij		4 4								_		

\* Approximate.

Per cent moisture in steam: Belleville, 6.31; Herreshoff (first test), 3.5; Scotch, 1st, 3.44; 2d, 4.29; Ward, 11.6; others not given.

### DIMENSIONS OF THE BOILERS.

Length, ft, and in., 8' 6" 4' 9" 2' 6" 3'			
Width, " " 7 0 3 8 2 6 1	8 31.16 6 727	10' 3''* 4 6 † 11 8 729.3 66.5 2490 37.4	10' 0''‡ 7 0‡ 8 0‡ 560‡ 38.3 2375 62

\* Diameter. † Diam. of drum. # Approximate.

The weight per I.H.P. is estimated on a basis of 20 lbs. of water per hour for all cases expecting the Scotch boiler, where 25 lbs. have been used, as this boiler was limited to 80 lbs. pressure of steam.

The following approximation is made from the large table, on the assump-

tion that the evaporation varies directly as the combustion, and 25 lbs. of

coal per square foot of grate per hour used as the unit.

Type of Boiler.	Com bustion,	Evapora- tion per cu. ft. of Space.	Weight per I.H.P.	Weight per sq. ft, Heating- surface.	Weight per lb. Water Evapo- rated.			
Belleville	0.50 1.00 1.00 1.00 3.90 2.20	0.50 0.95 1.20 0.44 0.31 0.58	2.02 0.72 1.12 2.40 3.70 1.27	2.10 0.60 0.87 1.64 1.25 0.50	2.50 0.90 1.30 2.30 3.50 1.53			

The Belleville boiler has no practical advantage over the Scotch either in space occupied or weight. All the other tubulous boilers given greatly exceed the Scotch in these advantages of weight and space.

Some High Rates of Evaporation,—Eng'g, May 9, 1884, p. 415. Locomotive. Torpedo-boat. 20.74 Water evap. per sq. ft. H.S. per hour. ...
" " lb. fuel from and at 212°. 12.57 13.73 12.54 8.22 8.94 8.37 7.04 Thermal units transf'd per sq. ft. of H.S. 12,142 13,263 12,113 20 034 .542 .468 Efficiency . 586 .637

It is doubtful if these figures were corrected for priming.

Economy Effected by Heating the Air Supplied to Boiler-furnaces. (Clark, S. E.)—Meunier and Scheurer-Kestner obtained about 7% greater evaporative efficiency in summer than in winter, from the same boilers under like conditions, -an excess which had been explained by the difference of loss by radiation and conduction. But Mr. Poupardin, surmising that the gain might be due in some degree also to the greater temperature of the air in summer, made comparative trials with two groups of three boilers, each working one week with the heated air, and the next week with cold air. The following were the several efficiencies:

FIRST TRIALS: THREE BOILERS; RONCH	IAMP COAL.
Water per lb.	of Water per lb. of
Coal.	
With heated air (128° F.) 7.77 lbs	
With cold air (69°.8)	8.63 **
Difference in favor of heated air 0.44 "	0.32 ''

SECOND TRIALS: SAME COAL: THREE OTHER BOILERS.

With heated air (120°.4 F.)	8.70 lbs.	10.08 lbs.
		9.34 "
	0.61 "	0.64 "

These results show economies in favor of heating the air of 6% and 71/6%. Mr. Poupardin believes that the gain in efficiency is due chiefly to the better combustion of the gases with heated air. It was observed that with heated air the flames were much shorter and whiter, and that there was

notably less smoke from the chimney.

notably less smoke from the chimney.

An extensive series of experiments was made by J. C. Hoadley (Trans. A. S. M. E., vol. vi., 676) on a "Warm-blast Apparatus," for utilizing the heat of the waste gases in heating the air supplied to the furnace. The apparatus, as applied to an ordinary horizontal tu ular boiler 60 in. diameter, 21 feet long, with 63 ½-inch tubes, consisted of 240 2-inch tubes, 18 feet long, through which the hot gases passed while the air circulated around them. The net saving of fuel effected by the warm blast was from 10.7% to 15.5% of the fuel used with cold blast. The comparative temperatures averaged as follows, in degrees F.:

	Cold-blast Boiler.	Warm-blast Boiler.	Difference.
In heat of fire	2493	2793	300
At bridge wall	1340	1600	260
In smoke box		375	2 .
Air admitted to furnace	32	332	300
Steam and water in boiler		300	0
Gases escaping to chimney	373	162	211
External air	32	32	0

With anthracite coal the evaporation from and at 212° per lb. combustible was, for the cold-blast boiler, days 10.85 lbs., days and nights 10.51; and for the warm-blast boiler, days 11.83, days and nights 11.03.

# Results of Tests of Heine Water-tube Boilers with Different Coals.

(Communicated by E. D. Meier, C.E., 1894.)

Number	1	2	3	4	5	6	7	8
Kind of Coal.	Cumberland, Semi-bitum.	2d Pool, Youghiogh- eny.		Turkey Hill, Ill.	Carbon Hill, Wash.	Hocking Val., Ohio.	Gillespie, Lump, Ill.	Collinsville, Ill.
Per cent ash Heating-surface, sq. ft Grate-surface, sq. ft	5.1 2900 54	4.89 2040 44 8	2040 44.8	11.6 2300 50	16.1 1260 21	11.5 3730 73.3	91.8 1168 27.9	12.8 2770 50
Ratio H.S. to G.S Coal per sq. ft. G.per hr. Water per sq. ft. H.S.per	53.7 24.7	45.5 23.5	45.5 22.7	46 35	60 33.7	50,9 26.2	41.9 27.7	55.4 36
hr. from and at 212° Water evap, from and at	5.03	5.14	5.24	5.56	4.26	4.28	4.86	5.08
212° per lb. coal Per lb. combustible	10.91 11.50	9.94	10.51	7.31 8.27	7.59 9.05	8.33 9.41	7.36 9.41	7.81 8.96
Temp. of chimney gases Calorific value of fuel	13,800	12,936		567 10,487			609 9,739	707 10,359
Efficiency of boiler per c.	77.0	74.3	78.5	67.2	62.5	69.3	73.0	72.6

Tests Nos. 7 and 8 were made with the Hawley Down-draught Furnace, the others with ordinary furnaces.

These tests confirm the statement already made as to the difficulty of obtaining, with ordinary grate-furnaces, as high a percentage of the calorific value of the fuel with the Western as with the Eastern coals.

Test No 3, 78.5% efficiency, is remarkably good for Pittsburgh (Youghlogheny) coal. If the Washington coal had given equal efficiency, the saving of = 20.2%. The results of tests Nos. 7 and 8 indicate fuel would be -

78.5 that the downward-draught furnace is well adapted for burning Illinois coals.

Maximum Boiler Efficiency with Cumberland Coal .-About 12.5 lbs, of water per 1b. combustible from and at 212° is about the highest evaporation that can be obtained from the best steam fuels in the Ingnest evaporation that can be obtained from the best scenar rues in the United States, such as Cumberland, Pocahontas, and Clearfield. In exceptional cases 13 lbs. has been reached, and one test is on record (F. W. Dean, Eng/y News, Feb. 1, 1894) giving 13.23 lbs. The boiler was internally fired, of the Belpaire type, 82 inches diameter, 31 feet long, with 160–3-inch tubes of the Benare type, countries manners, 12 feet, grate-surface, 45 square feet, 12% feet long. Heating surface, 1998 square feet, Double furnace, with fire-brick arches and a long combustion-chamber. Feed-water heater in smoke-box. The following are the principal results:

	lst Test.	2d Test.
Dry coal burned per sq. ft. of grate per hour, lbs	8.85	16.06
Water evap, per sq. ft. of heating-surface per hour, lbs		3.00
Water evap, from and at 212° per lb, combustible, in-		
cluding feed-water heater	13.17	13.23
Water evaporated, excluding feed-water heater	12.88	12.90
Temperature of gases after leaving heater, F	360°	4630

### BOILERS USING WASTE GASES.

Proportioning Boilers for Blast-Furnaces.-(F. W. Gordon. Trans. A. I. M. E., vol. xii., 1883.)

Mr. Gordon's recommendation for proportioning boilers when properly set for burning blast-furnace gas is, for coke practice, 30 sq. ft. of heating-sur-face per ton of fron per 24 hours, which the furnace is expected to make, calculating the heating-surface thus: For double-fued boilers, all shell-surface exposed to the gases, and half the flue-surface; for the French type, all the exposed surface of the upper boiler and half the lower boilersurface; for cylindrical boilers, not more than 60 ft, long, all the heatingsurface.

To the above must be added a battery for relay in case of cleaning, repairs. etc., and more than one battery extra in large plants, when the water carries

much lime.

For anthracite practice add 50% to above calculations. For charcoal practice deduct 20%.

In a letter to the author in May, 1894, Mr. Gordon says that the blast-furnace practice at the time when his article (from which the above extract is taken) was written was very different from that existing at the present time; besides, more economical engines are being introduced, so that less than 30 sq. ft. of boiler-surface per ton of iron made in 24 hours may now be adopted. He says further: Blast-furnace gases are seldom used for other than furnace requirements, which of course is throwing away good fuel. In this case a furnace in an ordinary good condition, and a condition where it can take its maximum of blast, which is in the neighborhood of 200 to 225 cubic ft., atmospheric measurement, per sq. ft. of sectional area of hearth, will generate the necessary H.P. with very small heating-surface, owing to the high heat of the escaping gases from the boilers, which frequently is 1000 degrees.

A furnace making 200 tons of iron a day will consume about 900 H.P. in blowing the engine. About a pound of fuel is required in the furnace per

pound of pig metal.

In practice it requires 70 cu. ft. of air-piston displacement per lb. of fuel consumed, or 22,400 cu, ft. per minute for 200 tons of metal in 1400 working minutes per day, at, say, 10 lbs. discharge-pressure. This is equal to 94 lbs. M.E.P. on the steam-piston of equal area to the blast-piston, or 300 l.H.P. To this add 20% for hoisting, pumping and other purposes for which steam is employed around blast-furnaces, and we have 1100 H.P., or say 5½ H.P. per ton of iron per day. Dividing this into 30 gives approximately 5½ sq. ft. of heating-surface of boiler per H.P.

heating-surface of noner per H.P.

Water-tube Boilers using Blast-furnace Gases.—D. S.
Jacobus (Trans. A. I. M. E., xvii. 50) reports a test of a water tube boiler using blast-furnace gas as fuel. The heating surface was 2535 q. ft. It developed 238 H.P. (Centennial standard), or 5.01 lbs. of water from and at 212° per sq. ft. of heating-surface per hour. Some of the principal data obtained were as follows: Calorific value of 1 lb. of the gas. 1418 B T.U., including the effect of its initial temperature, which was 650° F. Amount of air used to burn 1 lb. of the gas = 0.9 lb. Chimney draught, 1½ in. of water. Area of gas inlet, 300 sq. in.; of air inlet, 100 sq. in. Temperature of the chimney

gases, 775° F. Efficiency of the boiler calculated from the temperatures and analyses of the gases at exit and entrance, 61%. The average analyses were as follows, hydrocarbons being included in the nitrogen:

	By We	ight.	By Volume.			
	At Entrance.	At Exit.	At Entrance.	At Exit.		
CO <sub>2</sub>	.11	26.37 3.05	7.08	18.64 2.96		
CONitrogen	62.48	1.78 68.80	27.80 65.02	1.98 76.42		
C in CO <sub>2</sub>	2.92 11.45	7.19 .76				
Total C	14.37	7.95	1 1			

Steam-boilers Fired with Waste Gases from Puddling and Heating Furnaces,—The Iron Age, April 6, 1893, contains a report of a number of tests of steam-boilers utilizing the waste heat from puddling and heating furnaces in rolling-mills. The following principal data are selected: In Nos. 1, 2, and 4 the boiler is a Babcock & Wilcox water-tube boiler, and in No. 3 it is a plain cylinder boiler, 42 in. diam, and 26 ft. long, No. 4 boiler was considered with a heating-furnace, the others with puddling furnaces.

	No. 1.	No. 2.	No. 3.	No. 4.
Heating-surface, sq. ft	1026	1196	143	1380
Grate-surface, sq. ft	19.9	13 6	13.6	16.7
Ratio H.S. to G.S.	52	87.2	10.5	82.8
Water evap, per hour, lbs,	3358	2159	1812	3055
" per sq. ft. H.S. per hr., lbs	3.3	1.8	12.7	2.2
" per lb, coal from and at 212°.	5.9	6,24	3.76	6.34
" " comb. " " "	• • • • •	7.20	4.31	8.34

In No. 2, 1,38 lbs. of iron were puddled per lb. of coal.

In No. 3, 1.14 lbs, of iron were puddled per lb. of coal. No. 3 shows that an insufficient amount of heating-surface was provided for the amount of waste heat available.

### RULES FOR CONDUCTING BOILER-TESTS.

The Committee of the A. S. M. E. on Boiler-tests, consisting of Wm. Kent (chairman), J. C. Hoadley, R. H. Thurston, Chas. E. Emery, and Chas. T. Porter, recommended the following code of rules for boiler-tests (Trans., vol. vi. p. 256):

### PRELIMINARIES TO A TEST.

I. In preparing for and conducting trials of steam-boilers the specific object of the proposed trial should be clearly defined and steadily kept in

II. Measure and record the dimensions, position, etc., of grate and heating surfaces, flues and chimneys, proportion of air-space in the grate-surface, kind of draught, natural or forced.

III. Put the boiler in good condition. Have heating-surface clean inside and out, grate-bars and sides of furnace free from clinkers, dust and ashes removed from back connections, leaks in masonry stopped, and all obstructions to draught removed. See that the damper will open to full extent, and that it may be closed when desired. Test for leaks in masonry by firing a little smoky fuel and immediately closing damper. The smoke will then escape through the leaks.

IV. Have an understanding with the parties in whose interest the test is to be made as to the character of the coal to be used. The coal must be dry, or, if wet, a sample must be dried carefully and a determination of the amount of moisture in the coal made, and the calculation of the results of the test corrected accordingly. Wherever possible, the test should be made with standard coal of a known quality. For that portion of the country east of the Alleghany Mountains good anthracite egg coal or Cumberland semi-bituminous coal may be taken as the standard for making tests. West

of the Alleghany Mountains and east of the Missouri River, Pittsburgh lump coal may be used.\*

V. In all important tests a sample of coal should be selected for chemical

analysis.

WI. Establish the correctness of all apparatus used in the test for weighing and measuring. These are: J. Scales for weighing coal, ashes, and water. 2. Tanks, or water-meters for measuring water. Water-meters, as a rule, should only be used as a check on other measurements. For accurate work the water should be weighed or measured in a tank. 3. Thermometers and pyrometers for taking temperatures of air, steam, feed-water, waste gases,

c. 4. Pressure-gauges, draught-gauges, etc.
VII. Before beginning a test, the boiler and chimney should be thoroughly heated to their usual working temperature. If the boiler is new, it should be in continuous use at least a week before testing, so as to dry the mortar

thoroughly and heat the walls.

thoroughly and heat the walls.

VIII. Before beginning a test, the boiler and connections should be free from leaks, and all water connections, including blow and extra feed pipes, should be disconnected or stopped with blank flanges, except the particular pipe through which water is to be fed to the boiler during the trial. In locations where the reliability of the power is so important that an extra feed-pipe must be kept in position, and in general when for any other reason water-pipes other than the feed-pipes cannot be disconnected, such pipes may be drilled so as to leave openings in their lower sides, which should be been the such as the second of the other water pipes are proposed to the second of the other parts of the other parts of the second of the other parts of the parts of the other parts kept open throughout the test as a means of detecting leaks, or accidental or unauthorized opening of valves. During the test the blow-off pipe should remain exposed.

If an injector is used it must receive steam directly from the boiler being

tested, and not from a steam-pipe or from any other boiler

See that the steam-pipe is so arranged that water of condensation cannot run back into the boiler. If the steam-pipe has such an inclination that the water of condensation from any portion of the steam-pipe system may rnn back into the boiler, it must be trapped so as to prevent this water getting into the boiler without being measured.

# STARTING AND STOPPING A TEST.

A test should last at least ten hours of continuous running, and twentyfour hours whenever practicable. The conditions of the boiler and furnace in all respects should be, as nearly as possible, the same at the end as at the beginning of the test. The steam-pressure should be the same, the water-level the same, the fire upon the grates should be the same in quantities. tity and condition, and the walls, flues, etc., should be of the same temperature. To secure as near an approximation to exact uniformity as possible in conditions of the fire and in temperatures of the walls and flues, the following method of starting and stopping a test should be adopted:

X. Standard Method.—Steam being raised to the working pressure, remove rapidly all the fire from the grate, close the damper, clean the ash-pit, and as quickly as possible start a new fire with weighed wood and coal,

and as quicary as possible start a new life with weighed wood and coar, noting the time of starting the test and the height of the water-level while the water is in a quiescent state, just before lighting the fire. At the end of the test remove the whole fire, clean the grates and ash-pit, and note the water-level when the water is in a quiescent state; record the time of hauling the fire as the end of the test. The water-level should be as nearly as possible the same as at the beginning of the test. If it is not the same, a correction should be made by computation, and not by operating pump after test is completed. It will generally be necessary to regulate the discharge of steam from the boiler tested by means of the stop-valve for a time while fires are being hauled at the beginning and at the end of the test, in order to keep the steam-pressure in the boiler at those times up to the average during the test.

XI. Alternate Method.—Instead of the Standard Method above described,

the following may be employed where local conditions render it necessary: At the regular time for slicing and cleaning fires have them burned rather low, as is usual before cleaning, and then thoroughly cleaned; note the amount of coal left on the grate as nearly as it can be estimated; note the

<sup>\*</sup> These coals are selected because they are about the only coals which contain the essentials of excellence of quality, adaptability to various kinds of furnaces, grates, boilers, and methods of firing, and wide distribution and general accessibility in the markets.

pressure of steam and the height of the water-level-which should be at the medium height to be carried throughout the test-at the same time; and note this time as the time of starting the test. Fresh coal, which has been weighed, should now be fired. The ash pits should be thoroughly cleaned at once after starting. Before the end of the test the fires should be burned low, just as before the start, and the fires cleaned in such a manner as to leave the same amount of fire, and in the same condition, on the grates as at the start. The water-level and steam-pressure should be brought to the same point as at the start, and the time of the ending of the test should be noted just before fresh coal is fired.

# DURING THE TEST.

XII. Keep the Conditions Uniform .- The boiler should be run continuously, without stopping for meal-times or for rise or fall of pressure of steam due to change of demand for steam. The draught being adjusted to the rate of evaporation or combustion desired before the test is begun, it should be retained constant during the test by means of the damper.

If the boiler is not connected to the same steam pipe with other boilers, an extra outlet for steam with valve in same should be provided, so that in case the pressure should rise to that at which the safety-valve is set it may be reduced to the desired point by opening the extra outlet, without check-

ing the fires.

If the boiler is connected to a main steam-pipe with other boilers, the safety-valve on the boiler being tested should be set a few pounds higher than those of the other boilers, so that in case of a rise in pressure the other boilers may blow off, and the pressure be reduced by closing their dampers, allowing the damper of the boiler being tested to remain open,

and firing as usual.

All the conditions should be kept as nearly uniform as possible, such as force of draught, pressure of steam, and height of water. The time of cleaning the fires will depend upon the character of the fuel, the rapidity of combustion, and the kind of grates. When very good coal is used, and the combustion not too rapid, a ten-hour test may be run without any cleaning of the grates, other than just before the beginning and just before the end of the test. But in case the grates have to be cleaned during the test, the

intervals between one cleaning and another should be uniform.

XIII. Keeping the Records.—The coal should be weighed and delivered to the firemen in equal portions, each sufficient for about one hour's run, and a fresh portion should not be delivered until the previous one has all been fired. The time required to consume each portion should be noted, the time being recorded at the instant of firing the first of each new portion. It is desirable that at the same time the amount of water fed into the boiler should be accurately noted and recorded, including the height of the water in the boiler and the average pressure of steam and temperature of feed during the time. By thus recording the amount of water evaporated by successive portions of coal, the record of the test may be divided into several divisions, if desired, at the end of the test, to discover the degree of uniformity of combustion, evaporation, and economy at different stages of the test.

XIV. Priming Tests.—In all tests in which accuracy of results is important, calorimeter tests should be made of the percentage of moisture in the steam, or of the degree of superheating. At least ten such tests should be made during the trial of the boiler, or so many as to reduce the probable average error to less than one per cent, and the final records of the boile"test corrected according to the average results of the calorimeter tests.

On account of the difficulty of securing accuracy in these tests, the greatest care should be taken in the measurements of weights and temperatures. The thermometers should be accurate within a tenth of a degree, and the scales on which the water is weighed to within one hundredth of a pound.

#### Analyses of Gases. - Measurement of Air-supply, etc.

XV. In tests for purposes of scientific research, in which the determination of all the variables entering into the test is desired, certain observations should be made which are in general not necessary in tests for commercial purposes. These are the measurement of the air-supply, the determination of its contained moisture, the measurement and analysis of the flue gases, the determination of the amount of heat lost by radiation, of the amount of infiltration of air through the setting, the direct determination by calorimeter experiments of the absolute heating value of the fuel, and (by condensation of all the steam made by the boiler) of the total heat imparted to the

water.

The analysis of the flue-gases is an especially valuable method of determining the relative value of different methods of firing, or of different kinds of furnaces. In making these analyses great care should be taken to procure average samples—since the composition is ant to vary at different points of the flue, and the analyses should be intrusted only to a thoroughly proceed that the composition of the flue, and the analyses should be intrusted only to a thoroughly the composition of the flue, and the analyses should be intrusted only to a thoroughly the composition of the flue.

competent clemist, who is provided with complete and accurate apparatus. As the determinations of the other variables mentioned above are not likely to be undertaken except by engineers of high scientific attainments, and as apparatus for making them is likely to be improved in the course of scientific research, it is not deemed advisable to include in this code any

specific directions for making them.

### RECORD OF THE TEST.

XVI. A "log" of the test should be kept on properly prepared blanks, containing headings as follows:

	Pressures.			Temperatures.				Fuel.		Feed- water.		
Time.	Barome- ter.	Steam- gauge.	Praught- gauge.	External Air.	Boiler- room.	Flue.	Feed- water.	Steam.	Time.	Lbs.	Time.	Lbs. or cu. ft.

# REPORTING THE TRIAL.

Boiler at.....

	To determine			
1. D 2. D	ate of trialuration of trial	hours.		
eave	DIMENSIONS AND PROPORTIONS. space for complete description.			
3. G 4. W	rate-surfacewidelongarea Vater-heating surface	sq. ft.		
5. Si 6. R	uperheating surface	sq. ft.		
	AVERAGE PRESSURES.			
*8. A	team-pressure in boiler, by gauge bsolute steam-pressure	lbs.		
*9. A 10. F	tmospheric pressure, per barometer orce of draught in inches of water	in. in.		
	AVERAGE TEMPERATURES.			
11. 0	f external air	deg.		
12. O	f fire-room	deg.		
13. O	f steam	deg.	-	
14. O 15. O	f escaping gasesf feed-water	deg.	1	

<sup>\*</sup> See reference in paragraph preceding table.

FUEL.  16. Total amount of coal consumed †			1	
16. Total amount of coal consumed †				
17. Moisture in coal.  18. Dry coal consumed.  19. Total refuse, dry.  20. Total combustible (dry weight of coal, item 18; less refuse, Item 19).  *21. Dry coal consumed per hour.  *22. Combustible consumed per hour.  *23. Quality of steam, dry steam being taken as unity.  24. Percentage of moisture in steam.  25. Number of degrees superheated.  **26. Total weight of water pumped into boiler and apparently evaporated;.  27. Water actually evaporated; corrected for quality of steam \$\frac{1}{2}\$.  28. Equivalent water evaporated into dry steam from and at 212° F. \$\frac{1}{2}\$.  **29. Equivalent water evaporated into dry steam british thermal units \$\frac{1}{2}\$.  **30. Equivalent total heat derived from fuel in British thermal units \$\frac{1}{2}\$.  **B. Equivalent total heat derived from fuel in British thermal units \$\frac{1}{2}\$.  **B. Equivalent water evaporated into dry steam of the properties	FUEL.			
20. Total combustible (dry weight of coal, Item 18; less refuse, Item 19)	17. Moisture in coal	per cent.		
*22 Combustible consumed per hour.   Ibs.  RESULTS OF CALORIMETRIC TESTS.  23 Quality of steam, dry steam being taken as unity.  24. Percentage of moisture in steam.   per cent. deg.  WATER.  25. Number of degrees superheated.   lbs.  WATER.  26. Total weight of water pumped into boiler and apparently evaporated;   lbs.  27. Water actually evaporated;   lbs.  28. Equivalent water evaporated into dry steam from and at 212° F. \$   lbs.  *29. Equivalent total heat derived from fuel in British thermal units \$   lbs.  B.T.U.  B.T.U.	<ol> <li>Total combustible (dry weight of coal, Item</li> </ol>	*		
23. Quality of steam, dry steam being taken as unity. 24. Percentage of moisture in steam	*22. Combustible consumed per hour			
unity.  24. Percentage of moisture in steam	RESULTS OF CALORIMETRIC TESTS.			
24. Percentage of moisture in steam	unity			
26. Total weight of water pumped into boiler and apparently evaporated;	24. Percentage of moisture in steam			
apparently evaporated:  7. Water actually evaporated corrected for quality of steam s.  8. Equivalent water evaporated into dry steam from and at 212° F. s.  8. Equivalent total heat derived from fuel in British thermal units \$\frac{1}{2}\$.  8. Equivalent water evaporated into dry steam b.  8. T.U.	WATER.	-  -		
quality of steam \$   lbs.   88. Equivalent water evaporated into dry steam   from and at 212° F. \$   lbs.   *29. Equivalent total heat derived from fuel in   British thermal units \$   B.T.U.   80. Equivalent water evaporated into dry steam	apparently evaporated:	lbs.		
*29. Equivalent total heat derived from fuel in British thermal units \$\\ \). So, Equivalent was revaporated into dry steam	quality of steam §	lbs.		
30. Equivalent water evaporated into dry steam	from and at 212° F. §			
from and at 212 F. per nour	30. Equivalent water evaporated into dry steam			
	from and av 212- r. per nour	108.		
ECONOMIC EVAPORATION.	ECONOMIC EVAPORATION.			
31. Water actually evaporated per pound of dry coal, from actual pressure and temperature \$	coal, from actual pressure and tempera-			

\* See reference in paragraph preceding table. † Including equivalent of wood used in lighting fire. 1 pound of wood equals 0.4 pound coal. Not including unburnt coal withdrawn from fire at end of test.

Corrected for inequality of water-level and of steam-pressure at beginning and end of test.

§ The following shows how some of the items in the above table are derived from others:

Item  $27 = \text{Item } 26 \times \text{Item } 23.$ Item 28 = Item 27 × Factor of evaporation,

Factor of evaporation =  $\frac{H-h}{965.7}$ , H and h being respectively the total heat-

units in steam of the average observed pressure and in water of the average observed temperature of feed, as obtained from tables of the properties of steam and water.

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Item 29 = Item 27 \times (H - h).
Item 31 = Item 27 ÷ Item 18.
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Item 32 = Item 28 + Item 18, or = Item 31 × factor of evaporation.

Item 33 = Item 28  $\rightarrow$  Item 20, or = Item 32  $\rightarrow$  (per cent 100  $\rightarrow$  Item 19). Items 36 to 38. First term = Item 29  $\times$  6/5. Items 40 to 42. First term = Item 30  $\times$  0.8698.

Item 30, or Item 29, 33,305. Item  $43 = \text{Item } 29 \times 0.00003, \text{ or } = 3$ 

Item  $45 = \frac{\text{Difference of Items } 43 \text{ and } 44}{\text{Difference of Items}}$ Item 44

	Equivalent water evaporated per pound of dry coal from and at 212° F. §	lbs.	
34.	COMMERCIAL EVAPORATION.  Equivalent water evaporated per pound of		
	dry coal with one sixth refuse, at 70 pounds gauge-pressure, from temperature of 100° F. = Item 33 × 0.7249	lbs.	
	RATE OF COMBUSTION.	,	
35.	Dry coal actually burned per square foot of grate-surface per hour.	lbs.	
:36.	Consumption of dry Per sq. ft. of grate- surface	lbs.	
37. 38.	coal per hour. Coal Per sq.ft. of water- assumed with one heating surface	lbs.	
00.	sixth refuse. §   Per sq. ft. of least area for draught.	lbs.	
	RATE OF EVAPORATION.		
39.	Water evaporated from and at 212° F. per sq. ft. of heating-surface per hour	lbs.	
¥40.	( Water even and Per sq. ft. of grate-	lbs.	
41. 42.	per hour from temperature of 100° F. into steam of 70 lbs.	lbs.	
40.	gauge-pressure. § Per sq. ft. of least area for draught.	lbs.	
	COMMERCIAL HORSE-POWER.		
43.	On basis of thirty pounds of water per hour evaporated from temperature of 100° F.		
	into steam of 70 pounds gauge-pressure (= 34½ lbs. from and at 212°) \$	H.P.	
44.	Horse-power, builders' rating, atsquare feet per horse-power	H.P.	
45.	Per cent developed above, or below, rating§.	per cent	

Factors of Evaporation.—The table on the following pages was originally published by the author in Trans. A. S. M. E., vol. vi., 1884, under the title, Tables for Facilitating Calculations of Boiler-tests. The table gives the factors for every 3° of temperature of feed-water from 3° to 21° F., and for every two pounds pressure of steam within the limits of ordinary

working steam-pressures.

The difference in the factor corresponding to a difference of 3° temperator of feed is always either .0031 or .0032. For interpolation to find a factor for a feed-water temperature between 32° and 312°, not given in the table, take the factor for the nearest temperature and add or subtract, as the case may be, .0010 if the difference is .0031, and .0011 if the difference is .0032. As in nearly all cases a factor of evaporation to three decimal places is accurate enough, any error which may be made in the fourth decimal place by interpolation is of no practical importance.

The tables used in calculating these factors of evaporation are those given

in Charles T. Porter's Treatise on the Richards' Steam-engine Indicator. The formula is Factor  $=\frac{H-h}{965,7}$ , in which H is the total heat of steam at the observed pressure, and h the total heat of feed-water of the observed

temperature.

Part	-										
Freedward   Free				20 +				50 +	52 +	54 +	56 +
	Absolute pres	sures 15	25	35	45	99	60	65	67	69	. 71
					FACTO	RS OF I	EVAPOR	ATION.			
206		1.0003	1.0088	1.0149	1.0197	1.0237	1.0254	1.0271	1.0277	1.0283	1.0290
2008	209	35	1.0120	80	1.0228	68	86	1.0302	1.0309	1.0315	
1.0199   1.0214   75   1.0323   62   80   97   1.0461   1.0406   1.0416     194											52
194											C. 3
1	197										47
188	201										
185											
179	185		71				37			66	
176											
173											
167		1.0411	97	57	1.0605	45	63	79	85	92	98
161					1						
161         37 1.0622         82 1.0730         70         88 1.0804 1.0811 1.0817 1.0823         155         99         84         45         93         33         50         67         73         80         85         155         10.631 1.0716         76 1.0824         64         82         98 1.0905 1.0911 1.0917         149         62         47 1.0808         55         50         1.0913 1.0980         36         42         48         18         146         93         78         39         87 1.0926         44         61         67         73         79         143         1.0724 1.0810         70 1.9918         58         75         92         98 1.1005 1.1011         100         149         89 1.1007 1.1023 1.1030         36         42         48         11         140         56         41 1.0901         49         89 1.1007 1.1023 1.1030         36         42         143         134         1.0818 1.0903         64 1.1012         51         69         86         92         98         1.103         42         43         1.102         14         1114         32         44         55         66         67         73         79         86         92         98         1.1103         1.1122								42 78			
155	101	37	1.0622	82	1.0730	70	88	1.0804	1.0811	1.0817	1.0823
1.62											
149         62         471,0808         55         95         1.0913         1.0920         36         42         48           146         93         78         39         87         1.0926         44         61         67         73         79           143         1.0724         1.0810         70         1.9918         55         75         92         98         1.1005         1.005         1.005         1.005         1.001         1.002         38         55         61         67         73         79         33         80         1.102         61         66         67         73         38         80         1.102         61         66         66         67         73         38         80         1.102         61         66         66         92         98         81         66         61         102         66         1.113         30         48         48         55         66         66         67         73         1.113         30         1.122         80         68         69         29         98         67         69         1.114         1.113         1.1130         30         1.122         81         1											
143         1.07241.0810         70 1.0918         58         75         92         98 1.10051.1011           137         87         72         33         80 1.1020         38         55         61         67         73           134         1.08181.0036         64         1.1012         51         69         86         92         98 1.1104           131         49         34         95         43         83 1.1106         1.1117 1.1133         1.130         36           125         1.0912         97         57         1.1105         45         63         79         86         92         98         1.12           125         1.0912         97         57         1.1105         45         63         79         86         92         98         68         69         1.12         1.12         1.1211         1.1217         1.1233         1.1233         1.1233         1.1233         1.1233         1.1233         1.1242         86         69         2         98         1.24         48         54         60         69         2         13         36         1.1223         1.1233         1.1233         1.1233         1.1233         1.123											
140					87						
137			1.0810		1.0918						
134											
128		1.0818	1.0903	64	1.1012	51	69	86	92	98	1.1104
125	131										
$\begin{array}{cccccccccccccccccccccccccccccccccccc$											
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	122	43						1.1211	1.1217	1.1223	1.1229
113											
$\begin{array}{cccccccccccccccccccccccccccccccccccc$											
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	4.40										54
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$											
98											
$\begin{array}{cccccccccccccccccccccccccccccccccccc$			77								
$\begin{array}{cccccccccccccccccccccccccccccccccccc$											
86         1.1317         1.1402         63         1.1510         50         68         84         91         92         71.1603           80         79         64         1.1525         73         1.1612         1.1630         47         53         1.658         34           777         1.1410         95         56         1.1604         44         61         78         84         90         96           74         41         1.1526         87         35         75         92         1.1709         1.1719         1.1719         1.1712         1.7222         1.1728           68         1.1504         89         49         78         35         75         71         78         84         90           65         35         1.1620         80         1.1723         40         46         33         59           65         35         1.1620         80         1.1723         40         46         33         59           65         35         1.1620         80         1.1723         1.819         48         60         1.1722         1.1815         1.1722         1.1815         48         90				1.1400							
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		1.1317				50				97	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	83	48									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$											
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$							92				
65         351.1020         80 1.1728         68         86 1.1802 1.1809 1.1815 1.1821           62         66         51 1.1711         59         90 1.1817         33         40         46         52           59         97         82         43         90 1.1830         48         61         77         83         49           56         1.1028 1.1718         74 1.1821         61         79         96 1.1902 1.1908 1.1914           50         90         75         36         81 1.1923         41         58         64         70         78           47         1.1721 1.1806         67 1.1915         54         72         89         95 1.2001 1.2007           44         52         37         98         46         86 1.2032 1.2020 1.2020         32         39           41         83         68 1.1929         77 1.2017         34         51         57         64         70           35         1.1814 1.1900         60 1.2038         48         65         82         88         95 1.22101           35         45         31         91         39         79         96 1.2113 1.2119 1.2126         32	71	72	58	1.1618	66	1.1706	1.1723	40	46	53	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$										1 1815	
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$						-					
53         69         441,1805         52         021,1910,1927         33         39         45           50         90         75         36         84         1.023         41         58         64         70         76           47         1.1721         1.806         67         1.1915         54         72         89         95         1.2001         1.2007           44         52         37         98         46         86         1.2033         1.2020         1.2026         32         39           41         83         681,1929         77         1.2017         34         51         57         64         70           38         1.1814         1.1900         601,2008         48         65         82         88         95         1.2011           35         45         31         91         39         79         961,2113         1219         129         32	59	97	82	43	90	1.1830	48	64	. 71	77	83
$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		1.1628									
$ \begin{array}{cccccccccccccccccccccccccccccccccccc$											
44 52 37 98 46 861.20031.20201.20206 32 39 41 41 83 681.1929 7771.2017 34 51 57 64 70 38 1.1814[1.1900] 601.2008 48 65 82 88 951.2101 35 45 31 91 39 79 601.21131.21191.2126 32						54	72	89			1.2007
38   1.1814   1.1900   60   1.2008   48   65   82   88   95   1.2101   85   45   31   91   39   79   96   1.2113   1.2119   1.2126   32	44	52	37		46					32	39
85   45 31 91 39 79 96 1.2113 1.2119 1.2126 32								51 82	57 88		
32   76  62/1.2022; 70 1.2110 1.2128  44  51  57  63	85	45	31	91	39	79	96	1.2113	1.2119	1.2126	32
	32	76	62/	1.2022	70	1.2110	1.2128	44	51	57	63

		FACT	ORS	OF E	VAPO	ORAT	ION.			697
Gauge-press., Absolute Pres	lbs. 58 + ssures73.	60 +	62 +   77	64 +   79	66 +   81	68 +	70 +   85	72 +   87	74 +   89	76 + 91
Feed-water Temp.				FACTOR	s of I	EVAPOR.	ATION.			
212° F.	1.0295	1.0301	1.0307	1.0312	1.0318	1.0223	1.0329	1.0334	1.0339	1.0344
209 206	1.0327 58	33 64	38 70	44 75	49 81	55 86	60 -91	65 97	70 1.0403	75 1.0407
203 200	90 1.0421	1.0427	1.0401 83	1.0407	1.0412 44	1.0418 49	1.0423	1.0428 59	33 65	38 69
197 194	53 84	58 90	64 96	70 1.0501	75 1.0507	80 1.0512	86 1.0517	91 1.0522	96 1.0527	1.0501
191 188	1.0515		1.0527	33 64	38 69	43 75	49 80	54 85	59 90	64 95
185	78	84	90	95 1.0627	1.0601	1.0606	1.0611	1.0616	1.0622	1.0626
179	1.0610	47	52	58	63	69	74	79	53 84	89
176 173	1.0704		84 1.0715	1.0721	95 1.0726	1.0700	1.0705	1.0711 42 73	1.0716	1.0721
170 167	35	72	46 78	52 83	57 89	63 94	68	1.0805	1.0810	1.0815
164 161	1.0829	35	1.0809	1.0815	1.0820 51	1.0825 57	1.0831 62	36 67	41 72	46 77
158 155	9:2 9:2	66 97	$\frac{72}{1.0903}$	77 1.0909	83 1.0914	$\frac{88}{1.0919}$	93 1.0925	98 1.0930	1.0904	1.0908
152 149	1.0923	1.0929	34 66	40 71	45 77	51 82	56 87	61 92	66 97	71 1.1002
146 143	85 1.1017	91 1.1022	97 1.1028		1.1008	1.1013 44		1.1024 55	1.1029	34 65
140	48 79	54 85	59 91	65 96	70 1.1102	76 1.1107	81 1.1112	86 1.1117	91	96 1.1127
134 131	1.1110		$1.1122 \\ 53$	1.1127 59	33 64	38 69	43 75	49 80	54 85	59 90
128 125	73 1.1204	79	$\frac{56}{84}$ 1.1215	90 1.1221	95 1,1226	1.1201	1.1206	1.1211	1,1216	1.1221
122	35	41	47	52	58	63	68	73	78	83
119 116	98		78 1. <b>13</b> 09	83 1.1315	89 1.1320	94 1.1325	1.1331	1.1305 36	41	1.1315
113 110	1,1329	34 66	40 71	46 77	51 82	57 88	62 93	67 98	72 1.1403	1.1408
107 104	91 1.1422	1.1428	1.1403 34	1.1408 39	1.1414 45	1.1419 50	1.1424 55	1.1429 60	34 65	39 70
101 98	53 85	59 90	65 96	70 1.1502	76 1.1507	81 1.1512	86 1.1518	92 1.1523	97 1.1528	1.1502
95 92	1.1516	1.1521	1.1527	33 64	38 69	43 75	49 80	54 85	59 90	64 95
89 86	1.1609	84	89 1.1621	95 1.1626	1.1600	1.1606	1.1611 42	1.1616 47	1.1621 52	1.1626
83 80	40	46 77	52 83	57 88	63 94	68 99	73 1.1704	78 1.1710	83	1.1720
77 74	1.1702		1.1714 45	1.1719 51	1.1725 56	1.1730 61	35 67	41 72	46 77	51 82
71 68	65 96	70	76 1.1807	82 1.1813	87 1.1818	92 1.1824	98	1.1803	1.1808	1.1813
65	1.1827	33	38	44	49	55	60	65	70	75
62 59	58 89		$\frac{69}{1.1901}$	75 1.1906	80 1.1912	1.1917	91 1.1922	96 1.1927	1.1901	1.1906
56 53	1.1920	1.1926	32 63	37 68	43 74	48 79	53 84	58 89	63 94	68 99
50 47	1.2013	1.2019	$94 \\ 1.2025$	99 1.2030	1.2005 36	1.2010 41	1.2015 46	1.2021 52	1.2026	1.2031
44 41	44 76	50 81	56 87	61 93	67 98	72 1.2103	78 1.2109	83 1.2114	88 1.2119	93 1.2124
38 35	1.2107	1.2112	1.2118 49	1.2124 55	1.2129	34 65	40 71	45 76	50 81	55 86
32	69	75	80	86	91	97			1.2212	

Gauge-pressures   10
Pressures, 93   95   97   99   101   103   105   107   109   111   113   115
$ \begin{array}{ c c c c c c c c c c c c c c c c c c c$
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$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$
188     1.0600     1.0605     1.0610     1.0614     1.0619     1.0623     1.0628     32     36     40       185     31     36     41     46     50     55     59     63     68     72
185 31 36 41 46 50 55 59 68 68 72
182   63   68   72   77   81   86   90   951   991 070311 0
179 94 99 1 0704 1 0708 1 0713 1 0717 1 0722 1 0726 1 0730 35
176   1.0725   1.0730   35   40   44   49   53   57   62   66
173   57   62   66   71   75   80   84   89   93   97   1.01   1.02   1.080
167 1.0819 1.0824 1.0829 34 38 43 47 51 56 60
164   51   56   60   65   69   74   78   S3   87   91   161   82   87   92   96   1.0901   1.0905   1.0910   1.0914   1.0918   1.0923   1.09
158   1.0913   1.0918   1.0923   1.0927   32   37   41   45   50   54
155
149 1.1007 1.1012 1.1017 1.1021 1.1026 1.1030 35 39 43 48
146 38 48 48 58 57 62 66 70 75 79 143 70 74 79 84 88 93 97 1.1102 1.1106 1.1110 1.1
140   1.1101   1.1106   1.1110   1.1115   1.1120   1.1124   1.1129
137   32   37   42   46   51   55   60   64   68   73   134   63   68   73   78   82   87   91   95   1.1200   1.1204   1.1
131 95 99 1.1204 1.1209 1.1213 1.1218 1.1222 1.1227 31 35
128   1.1226   1.1231   35   40   45   49   53   58   62   66   125   57   62   67   71   76   80   85   89   93   98   1.1
122 88 93 98 1.1302 1.1307 1.1311 1.1316 1.1320 1.1325 1.1329
119 1.1320 1.1324 1.1329 34 38 43 47 51 56 60 116 51 55 60 65 69 74 78 83 87 91
118 82 87 91 96 1.1401 1.1405 1.1409 1.1414 1.1418 1.1422 1.1
110   1.1413   1.1418   1.1422   1.1427   32   36   41   45   49   53   107   44   49   54   58   63   67   72   76   80   85
104 75 80 85 89 94 99 1.1503 1.1507 1.1512 1.1516 1.1
101   1.1506   1.1511   1.1516   1.1521   1.1525   1.1530   34   38   43   47   98   38   42   47   52   56   61   65   70   74   78
95 69 74 78 83 87 92 96 1.1601 1.1605 1.1609 1.1
92   1.1600   1.1605   1.1609   1.1614   1.1619   1.1623   1.1628   32   36   40   41   45   50   54   59   63   67   72
86 62 67 72 76 81 85 90 94 98 1.1703 1.1
83   93   98   1.1703   1.1707   1.1712   1.1717   1.1721   1.1725   1.1730   34   80   1.1724   1.1729   34   39   43   48   52   56   61   65
77 56 60 65 70 74 79 83 88 92 96 1.1
74 87 91 96 1.1801 1.1805 1.1810 1.1814 1.1819 1.1823 1.1827 71 1.1818 1.1823 1.1827 32 36 41 45 50 54 58
68 49 54 58 63 68 72 77 81 85 89
65 80 85 89 94 99 1.1903 1.1908 1.1912 1.1916 1 1920 1.1 62 1.1911 1.1916 1.1921 1.1925 1.1930 34 39 43 47 52
59 42 47 52 56 61 65 70 74 78 83
56 73 78 83 87 92 96 1.2001 1.2005 1.2010 1.2014 1.2 53 1.2004 1.2009 1.2014 1.2018 1.2023 1.2028 32 36 41 45
50   35   40   45   50   54   59   68   67   72   76
47   66   71   76   81   85   90   94   98   1.2103   1.2107   1.2112   1.2116   1.2121   1.2125   1.2130   34   38
41 1.2129 33 38 43 47 52 56 61 65 69
88   60   64   69   74   78   83   87   92   96   1.2200   1.2 35   91   96   1.2200   1.2205   1.2209   1.2214   1.2218   1.2223   1.2227   31
32   1.2222   1.2227   31   36   41   45   49   54   58   62

			FACT	rors	OF I	EVAP	ORAT	10N.			699
Gauge-	pressures		1				1	1			
16	s. 100 + te Press,	105 +	110 +	115 +	120 +	125 +	130 +	135 +	140 +	145 +	150 +
Feed-w	lbs. 115.	120	125	130	135	140	145	150	155	160	165
Tem	р.					RS OF I					
212° 209	1.0397	1.0407	1.0417	1.0427	1.0436	1.0445	1.0458		1.0470		
206	60	70	80	89	99	1.0508	1.0516	1.0525	33	41	48
203 200	1.0523	1.0502	1.0511	1.0521	1.0530	39 70	48 79		64 96	1.0604	
197	55	65	74	84	93	1.0602	1.0610	1.0619	1.0627	35	43
194 191	1.0617		1.0606	1.0615	1.0624	33 65	42 73	50 82		66 98	
188	49	59	69	78	87	96	1.0705	1.0718	1.0721	1.0729	37
185 182	1.0712		1.0700	1.0709	1.0719	1.0727	36 67	44 76	53 84	61 92	1.0800
179	43	53	63	72	81	90	99	1.0807	1.0815	1.0823	31
176 173	1.0806	1.0816	1.0825	1.0803	1.0813	1.0821	1.0830	39	47 78	55 86	
170	37	47	57	66	75	84		1.0901	1.0909	1.0917	1.0925
167 164	1.0900	78 1.0910	1.0919	97 1.0929	1.0907	1.0915 47	1.0924	32 64	41 72	49 80	56 88
161	31	41	51	60	69	78	87	95	1.1003	1.1011	1.1019
158 155	62 93	1.1003	82 1.1013	1 1000	1.1000	1.1009	1.1018 49	1.1026	35 66	48 74	50 82
152	1.1025	35	44	54	63	72	81	89	97	1.1105	
149	56	66	76	85	94	1.1103	1.1112	1.1120	1.1128 60	36	44
146 143	1.1118	1.1129	1.1107	1.1116	1.1126	34 66	43 74	51 83	91	68 99	1.1207
140	50	60	70	79	88		1.1206			1,1230	38
137 134	81 1.1212	91 1.1222	1.1201 32	1.1210 41	1.1219 51	1.1228 59	37 68	45 76	53 85	61 93	1,1300
131	43	53	63	73	82	91	99	1.1308	1.1316	1.1324	32
128 125	75 1.1306	85 1.1316	94 1.1326	1.1304	1.1313	1.1322 53	1.1331	39 70	47 78	55 86	63 94
122	37	47	57	66	75	84	93	1.1401	1.1409	1.1417	1.1425
119 116	68 99	78 1.1409	88 1.1419	97 1.1429	1.1407	1.1415 47	1.1424 55	32 64	41 72	49 80	56
113	1.1431	41	50	60	69	78	86	95	1.1508	1.1511	88 1.1519
110	62	72	82	91	1.1500		1.1518	1.1516	34 65	42	50
104	93 1.1524	1.1503	44	1.1522 53	31 62	40 71	49 80	57 88	22	73 1.1605	81 1.1612
101 98	55 86	65 96	75 1.1606	84 1.1616	94	1.1602	1.1611	1.1620	1.1628	36	43
95		1.1628	37	47	1.1625 56	65	42 73	51 82	59 90	67 98	75 1.1706
92	49	50	68	78	87	96	1.1705		1.1721	1.1729	37 -
89 86		90 1.1721	31	40	1.1718	1.1727	36 67	44 75	52 83	60 91	68 99
83 80	42 73	52 83	62	71	80	1 1000	98	1.1806	1.1815	1.1823	1.1830
77			93	1.1802	1.1812	1.1820	1.1829	37 69	46 77	54 85	61 93
74	35	45	55	65	74	83	91	1.1900	1.1908	1.1916	1.1924
71 68	67 98	1.1908	1.1917	$\frac{96}{1.1927}$	1.1905 36	1.1914 45	1.1922	31 62	39 70	47 78	55 86
65	1.1929	39	49	58	62	76	85	93			1.2017
62 59	60 91	70 1.2001	80 1.2011	89 1.2020	1.2029	1.2007	1.2016 47	1.2024	32 63	40	48 79
56	1.2022	35	42	51	60	69	78	86	94		1.2110
53 50	53 84	63 94	$\frac{73}{1.2104}$	$\frac{82}{1.2113}$	91 1 2123	1.2100	1.1209 40	1.2117	1.2126	34 65	41 72
47	1.2115	1.2125	35	44	54	63	71	80	88		1.2203
44 41	. 46 77	56 87	66	76	85	94	1.2202	1.2211	1.2219	1.2227	35
38	1.2208		1.2228	38	47	1.2225	33 64	42 73	50 81	58 89	66 97
35 32	40 71	50 81	59	69	78	87	95	1.2304	1.2312	1.2320	1.2328
0.4	(1)	01	901	1.2000	1.2309	1.2518	1.2020	35	43	51	59

### STRENGTH OF STEAM-HOILERS, VARIOUS RULES FOR CONSTRUCTION.

There is a great lack of uniformity in the rules prescribed by different writers and by legislation governing the construction of steam-boilers In the United States, boilers for merchant vessels must be constructed according to the rules and regulations prescribed by the Board of Supervising Inspectors of Steam Vessels; in the U. S. Navy, according to rules of the Navy Department, and in some cases according to special acts of Congress. On land, in some places, as in Philadelphia, the construction of boilers is governed by local laws; but generally there are no laws upon the subject, and boilers are constructed according to the idea of individual engineers and and boilers are constructed according to the idea of individual engineers and boiler-makers. In Europe the construction is generally regulated by stringent inspection laws. The rules of the U. S. Supervising Inspectors of Steam-vessels, the British Lloyd's and Board of Trade, the French Bureau Verttas, and the German Lloyd's are ably reviewed in a paper by Nelson Foley, M. Inst. Naval Architects, etc., read at the Chicago Engineering Congress, playing not since and Naval Engineering. From this paper the following notes are taken, chiefly with reference to the U. S. and British rules: (Abbreviations.-T. S., for tensile strength; El., elongation; Contr., contraction of area.)

Hydraulic Tests .- Board of Trade, Lloyd's, and Bureau Veritas .-

Twice the working pressure.

United States Statutes.—One and a half times the working pressure. Mr. Foley proposes that the proof pressure should be 11/2 times the work-

ing pressure + one atmosphere.

Established Nominal Factors of Safety.—Board of Trade.—

5 for a boller of moderate length and of the best construction and workmanship.

Hausing.

Lloyd's.—Not very apparent, but appears to lie between 4 and 5.

United States Statutes.—Indefinite, because the strength of the joint is not considered, except by the broad distinction between single and double

riveting. Bureau Veritas: 4.4.

German Lloyd's: 5 to 4.65, according to the thickness of the plates.

Material for Riveting.—Board of Trade.—Tensile strength of rivet bars between 26 and 30 tons, el. in 10" not less than 25%, and contr. of

area not less than 50%.

Lloyd's .- T. S., 26 to 30 tons; el. not less than 20% in 8". The material must stand bending to a curve, the inner radius of which is not greater than 1½ times the thickness of the plate, after having been uniformly heated to

a low cherry-red, and quenched in water at 82° F.
United States Statutes.—No special provision.
Rules Connected with Riveting.—Board of Trade.—The shearing resistance of the rivet steel to be taken at 23 tons per square inch, 5 to be used for the factor of safety independently of any addition to this factor for the plating. Rivets in double shear to have only 1.75 times the single section taken in the calculation instead of 2. The diameter must not be less than the thickness of the plate and the pitch never greater than 81/6". The thickness of double butt-straps (each) not to be less than 3/8 the thickness of the plate; single butt-straps not less than 9/8.

Distance from centre of rivet to edge of hole = diameter of rivet  $\times 1\frac{1}{2}$ .

Distance between rows of rivets

= 
$$2 \times \text{diam. of rivet or} = [(\text{diam.} \times 4) + 1] + 2$$
, if chain, and  
=  $\frac{\sqrt{[(\text{pitch} \times 11) + (\text{diam.} \times 4)] \times (\text{pitch} + \text{diam.} \times 4)}}{10}$  if zigzag.

Diagonal pitch = (pitch  $\times$  6 + diam.  $\times$  4) + 10. Lloyd's.—Rivets in double shear to have only 1.75 times the single section taken in the calculation instead of 2. The shearing strength of rivet steel to be taken at 85% of the T. S. of the material of shell plates. In any case where the strength of the longitudinal joint is sati-factorily shown by experiment to be greater than given by the formula, the actual strength may be taken in the calculation.
United States Statutes.—No rules.

Material for Cyindrical Shells Subject to Internal Pressure.—Board of Trade.—T. Stetween 27 and 32 tons. In the normal condition, el. not less than 18% in 10", but should be about 25%; if annealed, not less than 20%. Strips 2" wide should stand bending until the sides are parallel at a distance from each other of not more than three times the plate's thickness.

plate s thickness. —T. S. between the limits of 26 and 30 tons per square inch. El. not less than 20% in 8". Test strips heated to a low cherry-red and plunged into water at 82° F. must stand bending to a curve, the inner radius of which is not greater than 1½ times the plate's thickness.

U. S. Statutes.—Plates of ½" thick and under shall show a contr. of not less than 50%; when over ½" and up to ¾", not less than 45%; when over ½" and up to ¾", not less than 45%; when over

y, not less than 40%.
Mr. Foley's comments: The Board of Trade rules seem to indicate a steel of too high T. S. when a lower and more ductile one can be got: the lower tensile limit should be reduced, and the bending test might with advantage be made after tempering, and made to a smaller radius. Lloyd's rule for quality seems more satisfactory, but the temper test is not severe. The United States Statutes are not sufficiently stringent to insure an entirely satisfactory material.

Mr. Foley suggests a material which wou'd meet the following: 25 tons lower limit in tension; 25% in 8" minimum elongation; radius for bending test after tempering = the plate's thickness.

**Shell-plate Formulæ.**—Board of Trade: 
$$P = \frac{T \times B \times t \times 2}{D \times F \times 100}$$
.

D = diameter of boiler in inches;

P = working-pressure in lbs. per square inch:

t =thickness in inches ;

B =percentage of strength of joint compared to solid plate;

T =tensile strength allowed for the material in lbs. per square inch; F = a factor of safety, being 4.5, with certain additions depending on method of construction.

Lloyd's: 
$$P = \frac{C \times (t-2) \times B}{D}$$

t = thickness of plate in sixteenths; B and D as before; C = a constant depending on the kind of joint.

When longitudinal seams have double butt-straps, C = 20. When longitudinal seams have double butt-straps of unequal width, only covering on one side the reduced section of plate at the outer line of rivets, C=19.5. When the longitudinal seams are lap-jointed, C=18.5. U. S. Statutes.—Using same notation as for Board of Trade,

$$P=rac{t imes2 imes T}{D imes6}$$
 for single-riveting ; add 20% for double-riveting ;

where T is the lowest T. S. stamped on any plate.

Mr. Foley criticises the rule of the United States Statutes as follows : The rule ignores the riveting, except that it distinguishes between single and double, giving the latter 20% advantage; the circumferential riveting or class of seam is altogether ignored. The rule takes no account of workmanship or method adopted of constructing the joints. The factor, one sixth, simply covers the actual nominal factor of safety as well as the loss of strength at the joint, no matter what its percentage; we may therefore dismiss it as unsatisfactory.

**Rules for Flat Plates.** – Board of Trade;  $P = \frac{C(t+1)^2}{S-6}$ .

P = working pressure in lbs. per square inch;

S =surface supported in square inches; t =thickness in sixteenths of an inch;

C = a constant as per following table: C=125 for plates not exposed to heat or flame, the stays fitted with nuts and washers, the latter at least three times the diameter of the stay

and  $\frac{2}{3}$  the thickness of the plate; C = 187.5 for the same condition, but the washers  $\frac{2}{3}$  the pitch of stays in diameter, and thickness not less than plate;

C = 200 for the same condition, but doubling plates in place of washers, the width of which is ¾ the pitch and thickness the same as the plate;

C = 112.5 for the same condition, but the stays with nuts only; C = 75 when exposed to impact of heat or flame and steam in contact with the plates, and the stays fitted with nuts and washers three times the diameter of the stay and % the plate's thickness;

C=67.5 for the same condition, but stays fitted with nuts only; C=100 when exposed to heat or fiame, and water in contact with the plates, and stays screwed into the plates and fitted with nuts;

C = 66 for the same condition, but stays with riveted heads.

U. S. Statutes.—Using same notation as for Board of Trade.  $P = \frac{C \times C}{C \times C}$ , where p = greatest pitch in inches, P and t as above;

C = 112 for plates 7/16" thick and under, fitted with screw stay-bolts and nuts, or plain bolt fitted with single nut and socket, or

riveted head and socket; C = 120 for plates above 7/16'', under the same conditions;

C = 140 for flat surfaces where the stays are fitted with nuts inside

and outside:

C = 200 for flat surfaces under the same condition, but with the addition of a washer riveted to the plate at least ½ plate's thickness, and of a diameter equal to 2/5 pitch.

N.B.—Plates fitted with double angle-irons and riveted to plate, with leaf at least 36 the thickness of plate and depth at least 14 of pitch, would be allowed the same pressure as determined by formula for plate with washer riveted on.

N.B.—No brace or stay-bolt used in marine boilers to have a greater pitch

than 101/6" on fire-boxes and back connections.

Certain experiments were carried out by the Board of Trade which showed that the resistance to bulging does not vary as the square of the plate's that the resistance to outging does not vary as the square of the plate's thickness. There seems also good reason to believe that it is not inversely as the square of the greatest pitch. Bearing in mind, says Mr. Foley, that mathematicians have signally failed to give us true theoretical foundations for calculating the resistance of bodies subject to the simplest forms of stresses, we therefore cannot expect much from their assistance in the matter of flat plates.

The Board of Trade rules for flat surfaces, being based on actual experiment, are especially worthy of respect; sound judgment appears also to

have been used in framing them.

Furnace Formulæ. -Board of Trade. -Long Furnaces. -

 $P = \frac{C \times t^2}{(L+1) \times D}$ , but not where L is shorter than (11.5t - 1), at which length the rule for short furnaces comes into play.

P = working-pressure in pounds per square inch; t = thickness in inches; $D = \text{outside diameter in inches}; \ L = \text{length of furnace in feet up to 10 ft.};$ 

C = a constant, as per following table, for drilled holes: C = 99,000 for welded or butt-jointed with single straps, double-

riveted;

C = 88,000 for butts with single straps, single-riveted; C = 99,000 for butts with double straps, single-riveted.

Provided always that the pressure so found does not exceed that given by the following formulæ, which apply also to short furnaces:

 $P = \frac{C \times t}{D}$  for all the patent furnaces named;

 $P = \frac{C \times t}{3 \times D} \left( 5 - \frac{L \times 12}{67.5 \times t} \right)$  when with Adamson rings.

C=8,800 for plain furnaces; C=14,000 for Fox; minimum thickness 5/16'', greatest 56''; plain part not to exceed 6" in length:

C = 13,500 for Morison; minimum thickness 5/16'', greatest 5/6''; plain part not to exceed 6" in length;

C = 14,000 for Purves-Brown; limits of thickness 7/16" and 5%"; plain part 9" in length;

C = 8.800 for Adamson rings; radius of flange next fire 11/6".

U. S. Statutes.—Long Furnaces.—Same notation.

 $P = \frac{89,600 \times t^2}{L \times D}$ , but L not to exceed 8 ft.

N.B.-If rings of wrought iron are fitted and riveted on properly around and to the flue in such a manner that the tensile stress on the rivets shall not exceed 6000 lbs. per sq. in., the distance between the rings shall be taken as the length of the flue in the formulæ,

Short Furnaces, Plain and Patent .- P, as before, when not 8 ft.  $89,600 \times t^2$ 

long = - $P = \frac{L \times D}{L \times C};$   $P = \frac{t \times C}{D} \text{ when}$ 

C=14,000 for Fox corrugations where D= mean diameter; C=14,000 for Purves-Brown where D= diameter of flue; C=5677 for plain flues over 16'' diameter and less than 40'', when not over 3 ft. lengths.

Mr. Foley comments on the rules for long furnac s as follows: The Board of Trade general formula, where the length is a factor, has a very limited range indeed, viz., 10 ft. as the extreme length, and 135 thicknesses - 12", as the short limit. The original formula,  $P = \frac{G \times t^2}{L \times D}$  is that of Sir W. Fairbairn, and was I believe navagintaries.

Fairbairn, and was, I believe, never intended by  $\lim_{n\to\infty} V$  by the short furnaces. On the very face of it, it is apparent, on the other hand, that if it is true for moderately long furnaces, it cannot be so for very long ones. We are therefore driven to the conclusion that any formula which includes simple L as a factor must be founded on a wrong basis.

With Mr. Traill's form of the formula, namely, substituting (L+1) for L, the results appear sufficiently satisfactory for practical purposes, and in-deed, as far as can be judged, tally with the results obtained from experi-ment as nearly as could be expected. The experiments to which I refer were six in number, and of great variety of length to diameter; the actual factors of safety ranged from 4.4 to 6.2, the mean being 4.78, or practically 5. It seems to me, therefore, that, within the limits prescribed, the Board of Trade formula may be accepted as suitable for our requirements.

Trade forming may be accepted as suitable for our requirements.

The United States Statutes give Fairbairn's rule pure and simple, except
that the extreme limit of length to which it applies is fixed at 8 feet. As
far as can be seen, no limit for the shortest length is prescribed, but the
rules to me are by no means clear, flues and furnaces being mixed or not well distinguished.

Material for Stays .- The qualities of material prescribed are as follows:

Board of Trade.—The tensile strength to lie between the limits of 27 and

32 tons per square inch, and to have an elongation of not less than 20% in 10". Steel stays which have been welded or worked in the fire should not be used. Lloyd's.-26 to 30 ton steel, with elongation not less than 20% in 8".

U. S. Statutes.—The only condition is that the reduction of area must not

be less than 40% if the test bar is over 3/11 diameter. Loads allowed on Stays.—Board of Trade.—9000 lbs. per square

inch is allowed on the net section, provided the tensile strength ranges from 27 to 32 tons. Steel stays are not to be welded or worked in the fire,

Lloyd's.—For screwed and other stays, not exceeding 1½" diameter effective, 8000 lbs. per square inch is allowed; for stays above 1½", 9000 lbs. No stays are to be welded.

U. S. Statutes.—Braces and stays shall not be subjected to a greater stress

than 6000 lbs. per square inch.

than 6000 los. per square incin. [Rankine, S. E., p. 439, says: "The iron of the stays ought not to be exposed to a greater working tension than 3000 lbs, on the square inch, in order to provide against their being weakened by corrosion. This amounts to making the factor of safety for the working pressure about 20." It is evident, however, that an allowance in the factor of safety for corrosion may reasonably be decreased with increase of diameter.

 $C \times d^2 \times t$ 

[ **Girders.**—Board of Trade.  $P = \frac{C \times d^2 \times t}{(W - p)D \times L}$ . P = working pressure in lbs. per sq. in.; W = width of flame-box in inches; L = length of girder in inches; p = pitch of bolts in inches; D = distance between girders from centre to centre in inches; d = depth of girder in inches; t = thickness of sum of same in inches; C = a constant = 6600 for 1 bolt, 9900 for 2 or 3 bolts, and 11,220 for 4 bolts.

Lloyd's.—The same formula and constants, except that C = 11,000 for 4 or

5 bolts, 11,550 for 6 or 7, and 11,880 for 8 or more.

U. S. Statutes.—The matter appears to be left to the designers,

 $P = \frac{t(D-d) \times 20,000}$ Tube-Flates .- Board of Trade.  $W \times D$ 

horizontal distance between centres of tubes in inches; d = inside diameter of ordinary tubes; t = thickness of tube-plate in inches; W = extreme width of combustion-box in inches from front tube-plate to back of firebox, or distance between combustion-box tube plates when the boiler is double-ended and the box common to both ends.

The crushing stress on tube-plates caused by the pressure on the flame-

box top is to be limited to 10,000 lbs, per square inch.

Material for Tubes .- Mr. Foley proposes the following: If iron, the quality to be such as to give at least 22 tons per square inch as the minimum tensile strength, with an elongation of not less than 15% in 8°. If steel, the elongation to be not less than 26% in 8° for the material before being rolled into strips; and after tempering, the test bar to stand completely closing together. Provided the steel welds well, there does not seem to be any object in providing tensile limits.

The ends should be annealed after manufacture, and stay-tube ends should be annealed before screwing

Holding-power of Boiler-tubes. - Experiments made in Washington Navy Yard show that with 21/2 in. brass tubes in no case was the holdingpower less, roughly speaking, than 6000 lbs., while the average was upwards of 20,000 lbs. It was further shown that with these tubes nuts were superof 20,000 lbs. West atturned to the tube simply expanded into the tube-plate and fitted with a ferrule. When nuts were fitted it was shown that they drew off without injuring the threads.

In Messrs. Yarrow's experiments on iron and steel tubes of 2" to 21/4" diameter the first 5 tubes gave way on an average of 23,740 lbs., which would appear to be about % the ultimate strength of the tubes themselves. In all these cases the hole through the tube plate was parallel with a sharp edge to it, and a ferrule was driven into the tube.

Tests of the next 5 tubes were made under the same conditions as the first 5, with the exception that in this case the ferrule was omitted, the tubes being simply expanded into the plates. The mean pull required was 15,270 lbs., or considerably less than half the ultimate strength of the tubes.

or consideraby less than han the unmake strength of the those the Effect of beading the tubes, the holes through the plate being parallel and ferrules omitted. The mean of the first 3, which are tubes of the same kind, gives \$6.876 lbs. as their holding-power, under these conditions, as compared with 23,740 lbs. for the tubes fitted with ferrules only. This high figure is, however, mainly due to an exceptional case where the holdingpower is greater than the average strength of the tubes themselves.

It is disadvantageous to cone the hole through the tube-plate unless its sharp edge is removed, as the results are much worse than those obtained

with parallel holes, the mean pull being but 16,031 lbs., the experiments being made with tubes expanded and ferruled but not beaded over.

In experiments on tubes expanded into tapered holes, beaded over and fitted with ferrules, the net result is that the holding-power is, for the size experimented on, about 34 of the tensile strength of the tube, the mean pull being 28,797 lbs.

With tubes expanded into tapered holes and simply beaded over, better results were obtained than with ferrules; in these cases, however, the sharp edge of the hole was rounded off, which appears in general to have a good

effect.

In one particular the experiments are incomplete, as it is impossible to repoduce on a machine the racking the tube get by the expansion of a boiler as it is heated up and cooled down again, and it is quite possible, therefore, that the fastening giving the best results on the testing-machine may not prove so efficient in practice.

N.B.—It should be noted that the experiments were all made under the cold condition, so that reference should be made with caution, the circumstances in practice being very different, especially when there is scale on the tube-plates, or when the tube-plates are thick and subject to intense heat

Fron versus Steel Boiler-tubes. (Foley.) — Mr. Blechynden prefers iron tubes to those of steel, but how far he would go in attributing the leaky-tube defect to the use of steel tubes we are not aware. It appears, however, that the results of his experiments would warrant him in going a considerable distance in this direction. The test consisted of heating and cooling two tubes, one of wrought iron and the other of steel. Both tubes were 234 in. in diameter and .16 in. thickness of metal. The tubes were

put in the same furnace, made red-hot, and then dipped in water. The length was gauged at a temperature of 46° F.

This operation was twice repeated, with results as follows:

	Steel.	Iron.
Original length	55,495 in.	55,495 in.
Heated to 186° F.; increase	0.52 "	0.48 "
Coefficient of expansion per degree F	.0000067	.0000062
Heated red-hot and dipped in water; decrease	.007 in.	.003 in.
Second heating and cooling, decrease	.031 in.	.004 in.
Third heating and cooling, decrease	.017 in.	.006 in.
Total contraction	.055 in.	.013 in.

Mr. A. C. Kirk writes: That overheating of tube ends is the cause of the leakage of the tubes in boilers is proved by the fact that the ferrules at present used by the Admiralty prevent it. These act by shielding the tube ends from the action of the flame, and consequently reducing evaporation, and so allowing free access of the water to keep them cool.

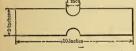
Although many causes contribute, there seems no doubt that thick tube-

plates must bear a share of causing the mischief.

# Rules for Construction of Boilers in Merchant Vessels in the United States.

(Extracts from General Rules and Regulations of the Board of Supervising Inspectors of Steam-vessels (as amended 1893 and 1894).)

Tensile Strength of Plate. (Section 3.)-To ascertain the tensile strength and other qualities of iron plate there shall be taken from each sheet to be used in shell or other



parts of boiler which are subject to tensile strain a test piece prepared in form according to the following diagram, viz.: 10 inches in length, 2 inches in width, cut out in the centre in the manner indicated. To ascertain the tensile strength

and other qualities of steel plate, there shall be taken from each sheet to be used in shell or other parts of boiler which are subject to tensile strain, a testpiece prepared in form according

to the following diagram, the length of straight part in centre varying as called for by different thickness of material, as follows:

The straight portion shall be in

length at least eight times the width multiplied by the thickness of said part. and have a reduction of area as called for by the present rules of the Board and an elongation of at least 2.%. The straight part shall be of a width of I inch. This rule to take effect on and after July 1, 1894.

Provided, that where contracts for boilers for ocean-going steamers require a test of material in compliance with the British Board of Trade, British Lloyd's, or Bureau Veritas rules for testing, the inspectors shall

make the tests in compliance with the following rules:

Steel plates shall in all cases to have an ultimate elongation not less than 20% in a length of 8 inches. It is to be capable of being bent to a curve of which the inner radius is not greater than one and a half times the thickness of the plates after having been heated uniformly to a low cherry-red, and quenched in water of 82° F.

[Prior to 1894 the shape of test-piece for steel was the same as that for iron, viz., the grooved shape. This shape has been condemned by authorities on strength of materials for over twenty years. It always gives results which are too high, the error sometimes amounting to 25 per cent. See pages 243, 213, ante; also, Strength of Materials, W. Kent, Van N. Science Series No. 41,

and Beardslee on Wrought-iron and Chain Cables.]

Ductility. (Section 6.)-To ascertain the ductility and other lawful qualities, iron of 45,000 lbs. tensile strength shall show a contraction of area quanties, from 04 \$2,000 for closure strength and another than 150 for 15 per cent, and cach additional 1000 fbs, tensile strength shall show 1 per cent additional contraction of area, up to and including 55,000 tensile strength. Ton of 55,000 tensile strength and upwards, showing 35 per cent reduction of area, shall be deemed to have the lawful duttility. All steel plate of ½ inch thickness and under shall show a contraction of area of not less than 50 per cent. Steel plate over ½ inch in thickness, up to ¾ inch in thickness, shall show a reduction of not less than 45 per cent. All steel plate

over ¼ inch thickness shall show a reduction of not less than 40 per cent. **Bumped Heads of Boilers**, (Section 17 as anended 1894) — **Pressure Allored on Bumped Heads.**—Multiply the thickness of the plate by one sixth of the tensile strength, and divide by six tenths of the radius to which head is bumped, which will give the pressure per square inch of steam allowed.

Pressure Allowable for Concaved Heads of Boilers.—Multiply the pressure per square inch allowable for bumped heads attached to boilers or drums convexly, by the constant .6, and the product will give the pressure per square inch allowable in concaved heads.

The pressure on unstayed flat-heads on steam-drums or shells of boilers, when flanged and made of wrought iron or steel or of cast steel,

shall be determined by the following rule:

The thickness of plate in inches multiplied by one sixth of its tensile

strength in pounds, which product divided by the area of the head in square
inches multiplied by .09 will give pressure per square inch allowed. The
material used in the construction of flat-heads when tensile strength has not been officially determined shall be deemed to have a tensile strength of 45,000 lbs.

# Table of Pressures allowable on Steam-boilers made of Riveted Iron or Steel Plates.

(Abstract from a table published in Rules and Regulations of the U.S. Board of Supervising Inspectors of Steam-vessels.)

Plates 1/4 inch thick. For other thicknesses, multiply by the ratio of the thickness to 1/4 inch.

-	**										
of s.	55,000 Tensile Strength. Strength.				Tensile ength.		Tensile ngth.	70,000 Tensile Strength.			
Diameter of Boiler, ins.	Pressure.	20% Additional.	Pressure.	20% Ad- ditional.	Pressure.	20% Ad- ditional.	Pressure.	20% Additional.	Pressure.	20% Additional.	
36 38 40 42 44 46 48 54 60 66 72 78	115.74 109.64 104.16 99.2 94.69 90.57 86.8 77.16 69.44 63.13 57.87 53.41 49.6	124.99 119.04 113.62 108.68 104.16 92.59 83.32	127.31 120.61 114.58 109.12 104.16 99.63 95.48 84.87 76.38 69.44 63.65 58.76 54.56	130.94 124.99	138.88 131.57 125 119.04 113.63 108.69 104.16 92.59 83.33 75.75 69.44 64.4 59.52	124.99 111.10 99.99	150.46 142.54 135.41 128.96 123.1 117.75 112.84 100.3 90.27 82.07 75.22 69.44 64.48	180.55 171.04 162.49 154.75 147.72 141.3 135.4 120.36 108.32 98.48 90.26 83.32 77.37	162.03 153.5 145.83 138.88 132.56 126.8 121.52 108.02 97.22 88.37 81.01 74.78 69.44	194.43 184.20 174.99 166.65 159.07 152.16 145.82 129.62 116.66 106.04 97.21 89.73 83.32	
96	46.29 43.4	55.44 52.08	50.92 47.74	61.1 57.28	55.55 52.08	66.66 62.49	60.18 56.42	72.21 67.67	64.81 60.76	77.77 72.91	

The figures under the columns headed "pressure" are for single-riveted boilers. Those under the columns headed "20% Additional" are for doubleriveted.

### U. S. Rule for Allowable Pressures.

The pressure of any dimension of boilers not found in the table annexed to these rules must be ascertained by the following rule:

Multiply one sixth of the lowest tensile strength found stamped on any plate in the cylindrical shell by the thickness (expressed in inches or parts of an inch) of the thinnest plate in the same cylindrical shell, and divide by the radius or half diameter (also expressed in inches), and the sum will be the pressure allowable per square inch of surface for single-riveting, to which add twenty per centum for double-riveting.

The author desires to express his condemnation of the above rule, and of the tables derived from it, as giving too low a factor of safety. (See also criticism by Mr. Foley, page 701, ante.)

If Pb = bursting-pressure, t = thickness, T = tensile strength, c = coefficient of strength of riveted joint, that is, ratio of strength of the joint to that of the solid plate, d = diameter, Pb =  $\frac{2tTc}{d}$ , or if c be taken for double-

riveting at 0.7, then 
$$Pb = \frac{1.4tT}{d}$$
.

By the U. S. rule the allowable pressure  $Pa = \frac{1/6tT}{1/6t} \times 1.20 = \frac{0.4tT}{d}$ ; whence Pb = 3.5Pa; that is, the factor of safety is only 3.5, provided the "tensile strength found stamped in the plate" is the real tensile strength of the material. But in the case of iron plates, since the stamped T.S. is obtained from a grooved specimen, it may be greatly in excess of the real T.S., which would make the factor of safety still lower. According to the table, a boiler 40 in, diam,  $\frac{1}{2}$  in, thick, made of iron stamped 60,000 T.S., would be licensed to carry 150 lbs. pressure if double-riveted. If the real T.S. is only 50,000 lbs. the calculated burstine, strength would be the calculated bursting-strength would be

$$P = \frac{2tTc}{d} = \frac{2 \times 50,000 \times .25 \times .70}{40} = 437.5 \text{ lbs.,}$$

and the factor of safety only  $437.5 \div 150 = 2.911$ 

The author's formula for safe working-pressure of externally-fired boilers with longitudinal seams double-riveted, is  $P = \frac{14000t}{d}$ ;  $t = \frac{Pd}{14000t}$ ; P = gauge

what indigitudinal scalins double-freeter, is  $I=\frac{d}{d}$ ,  $t=\frac{1}{14000}$  if I=3 gauge pressure in lbs, per sq. in; t= thickness and d= diam, in inches. This is derived from the formula  $P=\frac{2tTc}{fd}$ , taking c at 0.7 and f=5 for steel of 50,000 lbs. T.S., or 6 for 60,000 lbs. T.S.; the factor of safety being increased in the ratio of the T.S., since with the higher T.S. there is greater danger of cracking at the rivet-holes from the effect of punching and riveting and of expansion and contraction caused by variations of temperature. For external shells of internally-fired boilers, these shells not being exposed to the fire, with rivet-holes drilled or reamed after punching, a lower factor of safety and steel of a higher T.S. way be allowable. of safety and steel of a higher T.S. may be allowable.

If the T.S. is 60,000, a working pressure  $P = \frac{16000t}{d}$  would give a factor of safety of 5.25.

The following table gives safe working pressures for different diameters of shell and thicknesses of plate calculated from the author's formula.

# Safe Working Pressures in Cylindrical Shells of Boilers, Tanks, Pipes, etc., in Pounds per Square Inch.

Longitudinal seams double-riveted. (Calculated from formula  $P = 14,000 \times \text{thickness} \div \text{diameter.}$ )

			1	Diamet	ter in I	nches.				
24	30	36	38	40	42	44	46	48	50	52
36.5	29.2	24.3	23.0	21.9	20.8	19.9	19.0	18.2	17.5	16 8 33.7
109.4	87.5	72.9	69.1	65.6	62.5	59.7	57.1	54.7	52.5	50.5
182.3	145.8	121.5	115.1	109.4	104.2	99.4	95.1	91.1	87.5	84.1 101.0
255.2	204.1	170.1	161.2	153.1	145.9	139.2	133.2	127.6	122.5	117.8 134.6
328.1	262.5	218.8	207.2	196.9	187.5	179.0	171.2	164.1	157.5	151.4 168.3
401.0	320.8	267.4	253.3	240.6	229.2	218.7	209.2	200.5	192.5	185.1 201.9
473.9	379.2	316.0	299.3	284.4	270.9	258.5	247.3	337.0	227.5	218.8 235.6
546.9	437.5	364.6	345.4	328.1	312.5	298 3	285.3	273.4	266.5	252.4 269.2
	36.5 72.9 109.4 145.8 182.3 218.7 255.2 291.7 328.1 364.6 401.0 437.5 473.9 410.4 546.9	36.5 29.2 72.9 58.3 109.4 87.5 145.8 116.7 182.3 145.8 218.7 175.0 255.2 204.1 291.7 233.3 328.1 262.5 364.6 291.7 401.0 320.8 437.5 350.0 473.9 379.2 473.9 379.2	36.5 29.2 24.3 72.9 58.3 48.75 72.9 145.8 116.7 97.2 9 145.8 116.7 97.2 9 145.8 116.7 97.2 9 15.2 12.5 12.5 12.5 12.5 12.5 12.5 12.5	24 30 36 38 38 36.5 29.2 24.3 23.0 19.2 19.2 19.2 19.2 19.2 19.3 19.2 19.2 19.2 19.2 19.2 19.2 19.2 19.2	24 30 36 38 40  36.5 29.2 24.3 23.0 21.9  72.9 58.3 48.6 46.1 43.8  109.4 87.5 72.9 69.1 65.6  145.8 116.7 97.2 92.1 87.5  128.7 175.0 145.3 138.2 115.1 109.4  218.7 175.0 145.3 138.2 115.1 291.7  233.3 194.4 184.2 175.0  291.7 233.3 194.4 184.2 175.0  364.6 291.7 24.1 230.3 218.8  401.0 320.8 267.4 233.3 240.6  437.5 350.0 291.7 276.3 262.5  437.5 350.0 291.7 276.3 262.4  437.5 350.0 38.3 30.3 324.6  447.4 408.3 340.3 324.4 366.3	24 80 86 88 40 42  36.5 29.2 24.3 23.0 21.9 20.8 72.9 58.3 48.6 44.1 43.8 41.7 109.4 87.5 72.9 68.1 65.6 62.5 145.8 116.7 97.2 92.1 87.5 83.3 182.3 145.8 115.1 115.1 109.4 104.2 218.7 75.0 145.8 138.2 131.3 125.0 255.2 204.1 170.1 161.2 138.1 135.0 291.7 233.3 194.4 184.2 175.0 166.7 292.1 87.5 166.6 291.7 233.3 194.4 184.2 175.0 166.7 83.6 20.2 20.8 20.7 20.3 25.3 20.6 292.2 437.5 20.0 291.7 276.3 262.5 250.0 41.7 276.3 262.5 250.0 41.7 276.3 262.5 250.0 41.7 276.3 262.5 250.0 41.7 38.8 20.3 21.6 292.2 2437.5 250.2 216.0 293. 284.4 276.3 262.5 250.0 410.4 408.3 340.3 322.4 306.3 291.7 276.9 30.3 284.4 20.3 24.5 40.9 40.3 33.3 34.4 38.8 131.5 546.9 437.5 364.6 31.4 328.1 312.5	24 30 36 38 40 42 44  36.5 29.2 24.3 23.0 21.9 20.8 19.9 72.9 58.3 48.6 46.1 43.8 41.7 39.8 109.4 87.5 72.9 58.3 48.6 46.1 43.8 41.7 39.8 109.4 87.5 72.9 69.1 65.6 62.5 59.7 145.8 116.7 97.2 92.1 87.5 83.3 79.5 182.3 145.8 121.5 115.1 109.4 104.2 99.4 218.7 175.0 145.8 138.2 131.3 125.0 119.3 295.2 294.1 170.1 161.2 153.1 145.9 139.2 291.7 233.3 14.1 84.2 175.0 166.7 159.1 328.1 202.3 128.8 207.2 196.9 187.5 179.0 464.6 291.7 243.1 230.3 128.8 205.3 198.9 401.0 320.8 267.4 253.3 240.6 229.2 218.7 437.5 350.0 291.7 276.3 262.5 250.0 293.6 410.4 408.3 340.3 322.4 366.3 291.7 278.4 546.9 437.5 364.6 33.4 428.1 312.5 298.3	36.5 29.2 24.3 23.0 21.9 20.8 19.9 19.0 77.9 58.3 48.6 46.1 43.8 41.7 39.8 38.0 19.9 19.0 48.7 57.2 9 61.1 65.6 62.5 59.7 57.1 45.8 116.7 97.2 92.1 87.5 83.3 79.5 76.1 145.8 116.7 97.2 92.1 87.5 83.3 79.5 76.1 191.3 17.7 17.5 11.5 11.5 11.5 11.5 11.5 11.5	24 80 36 88 40 42 44 46 48 36.5 29.2 24.3 23.0 21.9 20.8 19.9 19.0 18.2 72.9 58.3 48.6 46.1 43.8 41.7 39.8 38.0 36.5 109.4 87.5 72.9 68.1 65.6 62.5 59.7 57.1 54.7 45.8 116.7 97.2 92.1 87.5 83.3 79.5 76.1 72.9 121.7 75.0 14.5 115.1 109.4 104.2 99.4 95.1 91.1 218.7 175.0 145.8 138.2 131.3 125.0 119.3 114.1 109.4 255.2 204.1 170.1 161.2 138.1 145.9 139.2 133.3 127.6 129.7 233.3 14.4 184.2 175.0 166.7 159.1 152.2 145.8 281.3 125.2 138.2 27.2 196.9 187.5 179.0 171.2 164.1 41.0 164.2 165.2 204.0 165	24 80 86 88 40 42 44 46 48 50 86.5 29.2 24.3 23.0 21.9 20.8 19.0 19.0 19.0 18.2 17.5 72.9 58.3 48.6 46.1 43.8 41.7 30.8 38.0 36.5 25.1 19.4 87.5 72.9 69.1 65.6 62.5 59.7 57.1 54.7 52.5 145.8 116.7 97.2 92.1 87.5 83 97.5 76.1 72.9 70.0 182.3 143.5 115.1 109.4 104.2 99.4 95.1 91.1 87.5 218.7 173.0 145.3 121.5 115.1 109.4 104.2 99.4 95.1 91.1 87.5 218.7 173.0 145.3 138.2 131.3 125.0 119.3 114.1 109.4 105.0 255.2 204.1 170.1 161.2 153.1 145.9 139.2 133.3 127.6 122.5 291.7 233.3 194.4 184.2 175.0 166.7 159.1 132.2 145.8 140.0 38.1 295.5 218.8 207.2 196.9 187.5 179.0 172.2 145.1 152.3 145.8 140.0 38.1 295.6 291.7 213.1 230.3 216.6 292.2 218.7 209.2 200.5 192.5 437.5 55.0 291.7 276.3 262.5 250.0 233.6 228.8 218.7 210.0 473.9 379.2 316.0 293.3 244.4 20.9 285.5 247.3 337.0 270.0 473.9 379.2 316.0 293.3 244.4 20.9 285.5 247.3 337.0 270.0 473.9 379.2 316.0 293.3 244.4 20.9 285.5 247.3 337.0 270.0 410.4 408.3 34.3 324.4 364.3 21.7 278.4 266.3 255.2 245.0 546.9 437.5 586.6 238.3 273.4 486.4 388.1 317.5 288.3 273.4 486.0

Thickness in 16thsof an Inch.	Diameter in Inches.											
an I	54	60	66	72	78	84	90	96	102	108	114	120
1	16.2	14.6	13.3	12.2	11.2	10.4	9.7	9.1	8.6	8.1	7.7	7.3
2 3 4 5 6 7 8 9	32.4 48.6	29.2	26.5 39.8	24.3	22.4	20.8	19.4	18.2	17.2	16.2	15 4	14.6
0	64.8	43.7 58.3	53.0	36.5 48.6	33.7 44.9	31.3 41.7	$\frac{29.2}{38.9}$	27.3 36.5	25.7 34.3	24.3 32.4	23 .0 30.7	21.9
5	81.0	72.9	66.3	60.8	56.1	52.1	48.6	45.6	42.9	40.5	38.4	29.2 36.5
6	97.2	87.5	79.5	72.9	67.3		58.3	54.7	51.5	48.6	46.1	43.8
7	113.4	102.1	92.8	85.1	78.5	72.9	68.1	63.8	60.0	56.7	53.7	51.0
8	129.6	116.7	106.1	97.2	89.7	83.3	77.8		68.6	64.8	61.4	58.3
9	145.8	131.2	119.3	109.4	101.0		87.5		77.2	72.9	69.1	65.6
10	162.0	145.8	132.6	121.5	112.2		97.2		85.8	81.0	76.8	72.9
11 12	178.2	160.4	145.8	133.7	123.4	114.6	106.9	100.3	94.4	89.1	84.4	80.2
13	194.4 210.7	175.0 189.6	$159.1 \\ 172.4$	145.8 158.0	134.6	125.0	116.7	109.4	102.9 111.5	97.2	92.1	87.5
14	226.9	204.2	185.6	170.1	157 1	145 8	126.4	197 6	120.1		99.8 107.5	94.8
15	243.1	218.7	198.9	182.3	168 2	156 3	145 8	126 7	128.7	113 4	115 1	100.1
16	259.3	233.3	212.1	194.4	179.5	166 7	155 6	145.8	137.3	120 6	199 8	116 7

# Rules governing Inspection of Boilers in Philadelphia.

In estimating the strength of the longitudinal seams in the cylindrical shells of boilers the inspector shall apply two formulæ, A and B:

 $\Delta$ ,  $\left\{ \frac{\text{Pitch of rivets} - \text{diameter of holes punched to receive the rivets}}{\text{pitch of rivets}} \right\}$ 

percentage of strength of the sheet at the seam.

Area of hole filled by rivet  $\times$  No. of rows of rivets in seam  $\times$  shearing strength of rivet

B, | pitch of rivets × thickness of sheet × tensile strength of sheet percentage of strength of the rivets in the seam.

Take the lowest of the percentages as found by formulæ A and B and apply that percentage as the "strength of the seam" in the following formula C, which determines the strength of the longitudinal seams:

safe working pressure.

Table of Proportions and Safe Working Pressures with Formulæ A

Diameter of rivet.	5/6''	11/16	3/4	13/16	7/6
Diameter of rivet-hole.	11/16"	3/4	13/16	7/6	15/16
Pitch of rivets	9//	2 1716		2 3716	
	.656	.636	21/8 .62		21/4
Strength of seam, %				.60	.58
Thickness of plate	1/4"	5/16	3,6	7/16	1/6

Diameter of boiler, in... Safe Working Pressure with Longitudinal Seams, Single-riveted.

Diameter of boner, in,		Si	ngle-rivete	d.	
24	137	165	193	220	242
30	109	132	154	176	194
32	102	124	144	165	182
34	96	117	136	155	171
36	91	110	129	147	161
38	86	104	122	139	153
40	82	99	116	132	145
44	74	91	105	120	132
48	68	83	96	110	121
54	60	73	86	98	107
60	55	66	77	88	97

122

11/16

3/4

94

13/16

108

5/6/1

64

Diameter of rivet-hole Pitch of rivets Strength of seam, % Thickness of plate	11/16" 8" .77 14"	3/4 31/8 .76 5/16	13/16 31/4 .75 3/8	7/8 83/8 .74 7/16	15/16 31/3 .73 1/2
		king Press		ongitudir	al Seams,
24	160	198	235	269	305
30	127	158	188	215	243
32	119	148	176	202	228
84	112	140	166	190	215
36	106	132	156	179	203
38	101	125	148	170	192
40	96	119	141	161	183
44	87	108	128	147	166
48	79	99	118	135	152
ž A	1 20	00	104	100	105

Flues and Tubes for Steam-boilers. -(From Rules of U. S. Supervising Inspectors. Steam-pressures per square inch allowable on riveted and lap-welded flues made in sections. Extract from table in Rules of U. S. Supervising Inspectors.)

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T = least thickness of material allowable, D = greatest diameter in inches, P = allowable pressure. For thickness greater than T with same diameter P is increased in the ratio of the thickness.

Diameter of rivet.

T = in. P = lbs.121 120 119 117 116 115 115 114 112 112 110 110 109 109 108 108 107

For diameters not over 10 inches the greatest length of section allowable is 5 feet; for diameters 10 to 23 inches, 3 feet; for diameters 23 to 40 inches, 30 inches. If lengths of sections are greater than these lengths, the allowable

pressure is reduced proportionately.

The U.S. rule for corrugated flues, as amended in 1894, is as follows: Rule II, Section 14. The strength of all corrugated flues, when used for furnaces or steam chimneys (corrugation not less than 11/2 inches deep and not exceeding 8 inches from centres of corrugation), and provided that the plain parts at the ends do not exceed 6 inches in length, and the plates are not less than 5/16 inch thick, when new, corrugated, and practically true circles, to be calculated from the following formula:

$$\frac{14,000}{D}$$
 ×  $T = \text{pressure}$ .

T = thickness, in inches: D = mean diameter in inches.

Ribbed Flues.—The same formula is given for ribbed flues, with rib projections not less than 1% inches deep and not more than 9 inches apart.

Flat Stayed Surfaces in Steam-boilers.—Rule II., Section 6, of the rules of the U.S. Supervising Inspectors provides as follows: No braces or stays hereafter employed in the construction of boilers shall be allowed a greater strain than 6000 lbs. per square inch of

section.

Clark, in his treatise on the Steam-engine, also in his Pocket-book, gives the following formula: p = 407ts + d, in which p is the internal pressure in pounds per square inch that will strain the plates to their elastic limit, t is the thickness of the plate in inches, d is the distance between two rows of stay-bolts in the clear, and s is the tensile stress in the plate in tons of 22d bs. per square inch, at the elastic limit. Substituting values of s for iron, steel, and copper, 12, 14, and 8 tons respectively, we have the following:

FORMULÆ FOR ULTIMATE ELASTIC STRENGTH OF FLAT STAYED SURFACES.

Or Or

to

	Iron.	Steel.	Copper.
Pressure	$p = 5000 \frac{t}{d}$	$p = 5700 \frac{t}{\bar{d}}$	$p = 3300 \frac{t}{d}$
Thickness of plate	$t = \frac{p \times d}{5000}$	$t = \frac{p \times d}{5700}$	$t = \frac{p \times d}{3300}$
Pitch of bolts	$d = \frac{5000t}{p}$	$d = \frac{5700t}{p}$	$d = \frac{3300t}{p}$

For Diameter of the Stay-bolts, Clark gives  $d' = .0024 \sqrt{\frac{PP'p}{p}}$ 

in which d' = diameter of screwed bolt at bottom of thread, P = longitudi-In Which  $\alpha' =$  diameter of sevened on a foction of threat, i = 0 internal and P' transverse pitch of stay-bolts between centres, p = internal pressure in lbs. per sq. in. that will strain the plate to its elastic limit, s = elastic strength of the stay-bolts in lbs. per sq. in. Taking s = 12, 14, and 8tons, respectively for iron, steel, and copper, we have

For iron, 
$$d' = .00069 \sqrt{PP'p}$$
, or if  $P = P'$ ,  $d' = .00069P \sqrt{p}$ ; For steel,  $d' = .00064 \sqrt{PP'p}$ , "  $d' = .00064P \sqrt{p}$ ; For copper,  $d' = .00084 \sqrt{PP'p}$ , "  $d' = .00084P \sqrt{p}$ .

In using these formulæ a large factor of safety should be taken to allow for reduction of size by corrosion. Thurston's Manual of Steam-boilers, p. 144, recommends that the factor be as large as 15 or 20. The Hartford Steam Boiler Insp. & Ins. Co. recommends not less than 10.

Strength of Stays.—A. F. Yarrow (Engr., March 20, 1891) gives the

following results of experiments to ascertain the strength of water-space stays:

Description.	Length between Plates.	Diameter of Stay over Threads.	Ulti- mate Stress.
Hollow stays screwed into j plates and hole expanded i Solid stays screwed into j plates and riveted over.		1 in.(hole 7/16 in. and 5/16 in. 1 in.(hole 9/16 in. and 7/16 in. 76 in. 78 in.	

The above are taken as a fair average of numerous tests.

Stay-bolts in Curved Surfaces, as in Water-legs of Vertical Boilers.—The rules of the U.S. Supervising Inspectors provide as follows: All vertical boiler-furnaces constructed of wrought iron or steel plates, and having a diameter of over 42 in, or a height of over 40 in, shall be stayed with bolts as provided by \$6 of Rule II, for flat surfaces; and the thickness of material required for the shells of such furnaces shall be determined by the distance between the centres of the stay-bolts in the furnace and not in the shell of the boiler; and the steam-pressure allowable shall be determined by the distance from centre of stay-bolts in the furnace

snai be determined by the distance from centre of saly-bons in the furnace and the diameter of such stay-bolts at the bottom of the thread.

The Hartford Steam-boiler Insp. & Ins. Co. approves the above rule (The Locomotive, March, 1892) as far as it states that curved surfaces are to be computed the same as flat ones, but prefers Clark's formule for flat stayed surfaces to the rules of the U.S. Supervising Inspectors.

Fusible-plugs.—Fusible-plugs should be put in that portion of the heating-surface which first becomes exposed from lack of water. The rules

neating-surface which first becomes exposed from lack of water. The rules of the U. S. Supervising Inspectors specify Banca tin for the purpose. Its melting-point is about 445° F. The rule says: All steamers shall have inserted in their boilers plugs of Banca tin, at least ½ in. In diameter at the smallest end of the internal opening, in the following manner, to wit. Cylinder-boilers with flues shall have one plug inserted in one flue of each boiler; and also one plug inserted in the shell of each boiler from the inside, immediately before the fire line and not less than 4 ft. from the forward end of the boiler. All fire-box boilers shall have one plug inserted in the covery of the box box procession or in the highest forestriction of the boiler. crown of the back connection, or in the highest fire-surface of the boiler.

All upright tubular boilers used for marine purposes shall have a fusible plug inserted in one of the tubes at a point at least 2 in, below the lower gauge-cock, and said plug may be placed in the upper head sheet when deemed advisable by the local inspectors.

Steam-domes. - Steam domes or drums were formerly almost universally used on horizontal boilers, but their use is now generally discontinued, as they are considered a useless appendage to a steam-boiler, and unless

properly designed and constructed are an element of weakness.

Height of Furnace.—Recent practice in the United States makes the height of furnace much greater than it was formerly. With large sizes of anthracite there is no serious objection to having the furnace as low as 12 of anthracite there is no serious objection to making the turnace as to be a few to 18 in., measured from the surface of the grate to the nearest portion of the heating surface of the boiler, but with coal containing much volatile matter and moisture a much greater distance is desirable. With very volations of the properties of the surface and moisture a tile coals the distance may be as great as 4 or 5 ft. Rankine (S. E., p. 457) says. The clear height of the "crown" or roof of the furnace above the grate-bars is seldom less than about 18 in., and often considerably more. In the fire-boxes of locomotives it is on an average about 4 ft. The height of 18 in. is suitable where the crown of the furnace is a brick arch. Where the crown of the furnace, on the other hand, forms part of the heating-surface of the. boiler, a greater height is desirable in every case in which it can be obtained; for the temperature of the boiler-plates, being much lower than that of the flame, tends to check the combustion of the inflammable gases which rise from the fuel. As a general principle a high furnace is favorable to complete combustion.

### IMPROVED METHODS OF FEEDING COAL.

Mechanical Stokers. (William R. Roney, Trans. A. S. M. E., vol. xi).—Mechanical stokers have been used in England to a limited extent since 1785. In that year one was patented by James Watt. It was a simple device to push the coal, after it was coked at the front end of the grate, back towards the bridge. It was worked intermittently by levers, and was designed primarily to prevent smoke from bituminous coal. (See D. K. Clark's Treatise on the Steam-engine.)

After the year 1840 many styles of mechanical stokers were patented in England, but nearly all were variations and modifications of the two forms of stokers patented by John Jukes in 1841, and by E. Henderson in 1843,

The Jukes stoker consisted of longitudinal fire-bars, connected by links, so as to form an endless chain, similar to the familiar treadmill horse-power. The small coal was delivered from a hopper on the front of the boiler, on to the grate, which slowly moving from front to rear, gradually advanced the fuel into the furnace and discharged the ash and clinker at the back.

The Henderson stoker consists primarily of two horizontal fans revolving

on vertical spindles, which scatter the coal over the fire.

Numerous faults in mechanical construction and in operation have limited the use of these and other mechanical stokers. The first American stoker was the Murphy stoker, brought out in 1878. It consists of two coal magazines placed in the side walls of the boiler furnace, and extending back from the boiler front 6 or 7 feet. In the bottom of these magazines are rectangular from boxes, which are moved from side to side by means of a rack and pinion, and serve to push the coal upon the grates, which incline at an angle of about 35° from the inner edge of the coal magazines, forming a V-shaped receptacle for the burning coal. The grates are composed of narrow parallel bars, so arranged that each alternate bar lifts about an inch at the lower end, while at the bottom of the V, and filling the space between the ends of the grate-bars, is placed a cast-iron toothed bar, arranged to be turned by a crank. The purpose of this bar is to grind the clinker coming in contact Over this V-shaped receptacle is sprung a fire-brick arch. with it.

In the Roney mechanical stoker the fuel to be burned is dumped into a hopper on the boller front. Set in the lower part of the hopper is a "pusher" to which is attached the "feed-plate" forming the bottom of the hopper. The "pusher," by a vibratory motion, carrying with it the "feed-plate," gradually forces the fuel over the "dead-plate" and on the grate. The grate-bars, in their normal condition form a series of steps, to the top step of which coal is fed from the "dead-plate." Each bar rests in a concave seat in the bearer, and is capable of a rocking motion through an adjustable angle. All the grate-bars are coupled together by a "rocker-bar." A variable back-and-forth motion being given to the "rocker-bar," through a con-

necting-rod, the grate-bars rock in unison, now forming a series of steps, necting-rod, the grate-bars rock in unison, now forming a series of steps, and now approximating to an inclined plane, with the grates partly overlapping, like shingles on a roof. When the grate-bars rock forward the fire will tend to work down in a body. But before the coal can move too far the bars rock back to the stepped position, checking the downward motion breaking up the cake over the whole surface, and admitting a free volume of air through the fire. The rocking motion is slow, being from 7 to 10 strokes per minute, according to the kind of coal. This alternate starting and checking motion is continuous, and finally lands the cinder and ash on the dumping-grate below.

Mr. Roney gives the following record of six tests to determine the comparative economy of the Roney mechanical stoker and hand-firing on return tubular boilers, 60 inches × 20 feet, burning Cumberland coal with natural

draught. Rating of boiler at 12.5 square feet, 105 H. P.

Three tests, hand-firing. Three tests, Stoker. Evaporation per pound, dry 10.36 10.44 11.00 11.89 12.25 12.54 coal from and at 212° lbs H.P. developed above rating, % 5.8 13.5 54.6 66.7 84.3

Results of comparative tests like the above should be used with caution in drawing generalizations. It by no means follows from these results that a stoker will always show such comparative excellence, for in this case the results of hand-firing are much below what may be obtained under favor-

able circumstances from hand-firing with good Cumberland coal.

The Hawley Down-draught Furnace.—A foot or more above
the ordinary grate there is carried a second grate composed of a series of
water-tubes, opening at both ends into steel drums or headers, through while
water is circulated. The coal is feed on this second grate, and as it is partially consumed falls through it upon the lower grate, where the combustion is completed in the ordinary manner. The draught through the coal on the upper grate is downward through the coal and the grate. The yolatile gases upper grate is downward through the coal and the grate. The volation are therefore carried down through the bed of coal, where they are thoroughly heated, and are burned in the space beneath, where they neet the Chicago, from 30 to 45 lbs. of coal were burned per square foot of grate upon

Cincago, from 30 to 45 los. of coal were burned per square foot of grate upon this system, with good economical results. (See catalogue of the Hawley Down Draught Furnace Co., Chicago, 1894.)

\*\*Under-feed Sto kers.\*\* — Results similar to those that may be obtained with downward draught are obtained by feeding the coal at the bottom of the bed, pushing upward the coal already on the bed which has had its volatile matter distilled from it. The volatile matter of the freshly fired coal then has to pass through a body of ignited coke. (See circular of the Jones Under-feed Stoker, Fraser & Chalmers, Chicago, 1894.)

### SMOKE PREVENTION.

A committee of experts was appointed in St. Louis in 1891 to report on the smoke problem. A summary of its report is given in the *Iron Age* of April 7. 1892. It describes the different means that have been tried to prevent smoke, such as gas-fuel, steam-jets, fire-brick arches and checker-work, hollow walls for preheating air, coking arches or chambers, double combustion furnaces, and automatic stokers. All of these means have been more or less effective in diminishing smoke, their effectiveness depending largely upon the skill with which they are operated; but none is entirely satisfac-tory. Fuel-gas is objectionable chiefly on account of its expense. The average quality of fuel-gas made from a trial run of several car-loads of Illinois coal, in a well-designed fuel-gas plant, showed a calorific value of 243,391 heat-units per 1000 cubic feet. This is equivalent to 5052.8 heat-units per lb. of coal, whereas by direct calorimeter test an average sample of the coal gave 11,172 heat-units. One lb. of the coal showed a theoretical evaporation of 11.56 lbs. water, while the gas from 1 lb. showed a theoretical evaporation of 5.23 lbs. 48.17 lbs. of coal were required to furnish 1000 cubic feet of the gas. In 39 tests the smoke-preventing furnaces showed only 74% of the capacity of the common furnaces, reduced the work of the boilers 28%, and required about 2% more fuel to do the same work. In one case with steam-jets the fuel consumption was increased 12% for the same work. Prof. O. H. Landreth, in a report to the State Board of Health of Tennes-

see (Engineering News, June 8, 1893), writes as follows on the subject of

smoke prevention:

As pertains to steam-boilers, the object must be attained by one or more of the following agencies:

1. Proper design and setting of the boiler-plant. This implies proper grate area, sufficient draught, the necessary air-space between grate-bars and

through furnace, and ample combustion-room under boilers

2. That system of firing that is best adapted to each particular furnace to secure the perfect combustion of bituminous coal. This may be either: (a) "coke-firing," or charging all coal into the front of the furnace unit par-tially coked, then pushing back and spreading; or (b) "alternate side fing"; or (c) "spreading," by which the coal is spread over the whole grate area in thin, uniform layers at each charging.

3. The admission of air through the furnace-door, bridge-wall, or side walls. 4. Steam-jets and other artificial means for thoroughly mixing the air and

combustible gases.

5 Preventing the cooling of the furnace and boilers by the inrush of cold air when the furnace-doors are opened for charging coal and handling the

fire.

Establishing a gradation of the several steps of combustion so that the coal may be charged, dried, and warmed at the coolest part of the furnace, and then moved by successive steps to the hottest place, where the final combustion of the coked coal is completed, and compelling the distilled combustible gases to pass through this hottest part of the fire

7. Preventing the cooling by radiation of the unburned combustible gases

until perfect mixing and combustion have been accomplished.

8. Varying the supply of air to suit the periodic variation in demand.

9. The substitution of a continuous uniform feeding of coal instead of

intermittent charging. Down-draught burning or causing the air to enter above the grate and pass down through the coal, carrying the distilled products down to the high

temperature plane at the bottom of the fire. The number of smoke-prevention devices which have been invented is

legion. A brief classification is :

(a) Mechanical stokers. They effect a material saving in the labor of firing, and are efficient smoke preventers when not pushed above their capacity, and when the coal does not cake badly. They are rarely susceptible to the sudden changes in the rate of firing frequently demanded in service.

(b) Air-flues in side walls, bridge-wall, and grate-bars, through which air when passing is heated. The results are always beneficial, but the flues are

difficult to keep clean and in order.

(c) Coking arches, or spaces in front of the furnace arched over, in which the fresh coal is coked, both to prevent cooling of the distilled gases, and to force them to pass through the hottest part of the furnace just beyond the arch. The results are good for normal conditions, but ineffective when the fires are forced. The arches also are easily burned out and injured by working the fire.

(d) Dead-plates, or a portion of the grate next the furnace-doors, reserved for warming and coking the coal before it is spread over the grate. These

give good results when the furnace is not forced above its normal capacity. This embodies the method of "coke-firing" mentioned before.

(e) Down-draught furnaces, or furnaces in which the air is supplied to the coal above the grate, and the products of combustion are taken away from beneath the grate, thus causing a downward draught through the coal, carrying the distilled gases down to the highly heated incandescent coal at the bottom of the layer of coal on the grate. This is the most perfect manner of producing combustion, and is absolutely smokeless.

(f) Steam jets to draw air in or inject air into the furnace above the grate, and also to mix the air and the combustible gases together. A very efficient smoke-preventer, but one liable to be wasteful of fuel by inducing too rapid

a draught.

(g) Baffle-plates placed in the furnace above the fire to aid in mixing the

combustible gases with the air.

(h) Double furnaces, of which there are two different styles; the first of which places the second grate below the first grate; the coal is coked on the first grate, during which process the distilled gases are made to pass over the second grate, where they are ignited and burned; the coke from the first grate is dropped onto the second grate; a very efficient and economical smoke-preventer, but rather complicated to construct and maintain. In the second form the products of combustion from the first furnace pass through the grate and fire of the second, each furnace being charged with fresh fuel when needed, the latter generally with a smokeless coal or coke: an irra10 5

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tional and unpromising method.
Mr. C. F. White, Consulting Engineer to the Chicago Society for the Pre-vention of Smoke, writes under date of May 4, 1893:

The experience had in Chicago has shown plainly that it is perfectly easy to equip steam-boilers with furnaces which shall burn ordinary soft coal in such a manner that the making of smoke dense enough to obstruct the vision

shall be confined to one or two intervals of perhaps a couple of minutes' duration in the ordinary day of 10 hours.

Gas-fired Steam-boilers.—Converting coal into gas in a separate producer, before burning it under the steam-boiler, is an ideal method of smoke-prevention, but its expense has hitherto prevented its general introduction. A series of articles on the subject, illustrating a great number of devices, by F. J. Rowan, is published in the Colliery Engineer, 1889-90. See also Clark on the Steam-engine.

## FORCED COMBUSTION IN STEAM-BOILERS.

For the purpose of increasing the amount of steam that can be generated by a boiler of a given size, forced draught is of great importance. It is by a boiler of a given size, forced graught is of great importance. It is universally used in the locomotive, the draught being obtained by a steamjet in the smoke-stack. It is now largely used in ocean steamers, especially in ships of war, and to a small extent in stationary boilers. Economy of fuel is generally not attained by its use, its advantages being confined to the securing of increased capacity from a boiler of a given bulk, weight, or cost. The subject of forced draught is well treated in a paper by James Howden, entitled, "Forced Combustion in Steam-boilers" (Section G. Engineering

Congress at Chicago, in 1893, from which we abstract the following: Edwin A. Stevens at Bordentown, N. J., in 1827, in the steamer "North America," fitted the boilers with closed ash-pits, into which the air of combustion was forced by a fan. In 1828 Ericsson fitted in a similar manner the steamer "Victory," commanded by Sir John Ross.

steamer "Victory," commanded by Sir John Ross.
Messrs, E. A. and R. L. Stevens continued the use of forced draught for
a considerable period, during which they tried three different modes of using
the fan for promoting combustion: 1, blowing direct into a closed ash-pit;
2, exhausting the base of the funnel by the suction of the fan; 3, forcing air
into an air-tight boiler-room or stoke-hold. Each of these three methods
was attended with serious difficulties.
In the use of the alexander with the blast was a strended with serious difficulties.

In the use of the closed ash-pit the blast-pressure would frequently force the gases of combustion, in the shape of a serrated flame, from the joint around the furnace doors in so great a quantity as to affect both the effi-

ciency and health of the firemen.

The chief defect of the second plan was the great size of the fan required to produce the necessary exhaustion. The size of fan required grows in a rapidly increasing ratio as the combustion increases, both on account of the reater air-supply and the higher exit temperature enlarging the volume of the waste gases.

The third method, that of forcing cold air by the fan into an air-tight boiler-room-the present closed stoke-hold system-though it overcame the difficulties in working belonging to the two forms first tried, has serious detects of its own, as it cannot be worked, even with modern high-class boiler-construction, much, if at all, above the power of a good chimney

obler-construction, much, if at all, above the power or a good chimney draught, in most boilers, without damaging them.

In 1875 John I. Thornycroft & Co., of London, began the construction of torpedo-boats with boilers of the locomotive type, in which a high rate of combustion was attained by means of the air-tight boiler-room, into which air was forced by means of a fan,

In 1882 H.B.M. ships "Satellite" and "Conqueror" were fitted with this

system, the former being a small ship of 1500 I.H.P., and the latter an iron-clad of 4500 I.H.P. On the trials with forced draught, which lasted from two to three hours each, the highest rates of combustion gave 16.9 I.H.P. per square foot of fire-grate in the "Satellite," and 13.41 I.H.P. in the "Con-

None of the short trials at these rates of combustion were made without injury to the seams and tubes of the boilers, but the system was adopted,

and it has been continued in the British Navy to this day (1893).

In Mr. Howden's opinion no advantage arising from increased combustion over natural-draught rates is derived from using forced draught in a closed ash-pit sufficient to compensate the disadvantages arising from difficulties in working, there being either excessive smoke from bituminous coal or reduced evaporative economy.

In 1880 Mr. Howden designed an arrangement intended to overcome the

defects of both the closed ash-pit and closed stoke-hold systems. An air-tight reservoir or chamber is placed on the front end of the boiler and surrounding the furnaces. This reservoir, which projects from 8 to 10 inches from the end of the boiler, receives the air under pressure, which is passed by the valves into the ash-pits and over the fresh in proportions suited to the kind of fuel used and the rate of combustion required. The air nsed above the fires is admitted to a space between the outer and inner furnace-doors, the inner having perforations and an air-distributing box through which the air passes under pressure.

By means of the balance of air-pressure above and below the fires all tendency for the fire to blow out at the furnace-door is removed.

By regulating the admission of the air by the valves above and below the fires, the highest rate of combustion possible by the air-pressure used can be effected, and in same manner the rate of combustion can be reduced to far below that of natural draught, while complete and economical combus-

ition at all rates is secured.

A feature of the system is the combination of the heating of the air of combustion by the waste gases with the controlled and regulated admission of air to the furnaces. This arrangement is effected most conveniently by passing the hot fire-gases after they leave the boiler through stacks of vertical tubes enclosed in the uptake, their lower ends being immediately above the smoke-box doors.

Installations on Howden's system have hitherto been arranged for a rate of combustion to give at full sea-power an average of from 18 to 22 I.H.P. per square foot of fire-grate with fire-bars from 5' 0" to 5' 6" in length.

It is believed that with suitable arrangement of proportions even 80

I.H.P. per square foot can be obtained.

For an account of recent uses of exhaust-fans for increasing draught, see paper by W. R. Roney, Trans. A. S. M. E., vol. xv.

### FUEL ECONOMIZERS.

Green's Fuel Economizer.-Clark gives the following average results of comparative trials of three boilers at Wigan used with and without economizers:

Monitzers.	Without	With
	Economizers.	Economizers.
Coal per square foot of grate per hour	. 21.6	21.4
Water at 100° evaporated per hour	73.55	79.32
Water at 212° per pound of coal	9.60	10.56

Showing that in burning equal quantities of coal per hour the rapidity of evaporation is increased 9.3% and the efficiency of evaporation 10% by the addition of the economizer.

The average temperatures of the gases and of the feed-water before and after passing the economizer were as follows:

to pacong the economizer were us r	one mo.			
	With 6-ft	grate.	With 4-f	t. grate.
	Before.	After.	Before.	After.
Average temperature of gases	649	340	501	312
Average temperature of feed-water.	47	157	41	137 -

Taking averages of the two grates, to raise the temperature of the feed-

water 100° the gases were cooled down 250°.

Performance of a Green Economizer with a Smoky Coal. Performance of a creen Economizer with a Shorty Coan,

The action of Green's Economizer was tested by M. W. Grosseteste for a
period of three weeks. The apparatus consists of four ranges of vertical
pipes, 6½ feet high, 3½ inches in diameter outside, nine pipes in each range,
connected at top and bottom by horizontal pipes. The water enters all the
tubes from below, and leaves them from above. The system of pipes is en
tubes from below, and leaves them from above. The system of pipes is en
are introduced from above, and which the greater production combination

are introduced from above, and which the greater of the pipe is the control of the combination of the combinat are cleared of soot externally by automatic scrapers. The capacity for water is 24 cubic feet, and the total external heating-surface is 290 square feet. The apparatus is placed in connection with a boiler having 355 square feet of surface.

This apparatus had been at work for seven weeks continuously without having been cleaned, and had accumulated a 1/2-inch coating of soot and ash, when its performance, in the same condition, was observed for one week. During the scoond week it was cleaned twice every day; but during the third week, after having been cleaned on Monday morning, it was worked continuously without further cleaning. A smoke-making coal was used. The consumption was maintained sensibly constant from day to day.

GREEN'S ECONOMIZER.—RESULTS OF EXPERIMENTS ON ITS EFFICIENCY AS AFFECTED BY THE STATE OF THE SURFACE. (W. Grosseteste.)

	Temperature of Feed- water.			Temperature of Gas- eous Products.		
TIME (February and March).	Enter- ing Feed- heater.	Leav- ing Feed- heater.	Differ- ence.	Enter- ing Feed- heater.	Leav- ing Feed- heater.	Differ- ence.
1st Week	Fahr. 73.5° 77.0 73.4 73.4 79.0 80.6 80.6 79.0	Fahr. 161.5° 230 0 196.0 181 4 178.0 170.6 169 0 172.4	Fahr. 88.0° 153.0 122.6 108.0 99.0 90.0 88.4 93.4	Fahr. 849° 882 831 871 952 889 901	Fahr. 261° 297 284 309 338 351	Fahr. 588° 585 547 562 623 551 550

1st Week. 2d Week. 3d Week. ... 214 lbs. 216 lbs. 213 lbs.

It is apparent that there is a great advantage in cleaning the pipes daily—the elevation of temperature having been increased by it from 88° to 158°. In the third week, without cleaning, the elevation of temperature relapsed in three days to the level of the first week; even on the first day it was quickly reduced by as much as half the extent of relapse. By cleaning the pipes daily an increased elevation of temperature of 65° F., was obtained, whilst a gain of 65° was effected in the evaporative efficiency.

### INCRUSTATION AND CORROSION.

Incrustation and Scale.—Incrustation (as distinguished from mere sediments due to dirty water, which are easily blown out, or gathered up, by means of sediment collectors) is due to the presence of salts in the feed-water (carbonates and sulphates of lime and magnesia for the most part), which are precipitated when the water is heated, and form hard deposits upon the boiler-plates. (See Impurities in Water, p. 551, ante.)

Where the quantity of these salts is not very large (12 grains per gallon, say) scale preventives may be found effective. The chemical preventives either form with the salts other salts soluble in hot water; or precipitate them in the form of soft mud, which does not adhere to the plates, and can be washed out from time to time. The selection of the chemical must depend upon the composition of the water, and it should be introduced regularly with the feet.

EXAMPLES.—Sulphate-of-lime scale prevented by carbonate of soda: The sulphate of soda produced is soluble in water; and the carbonate of lime falls down in grains, does not adhere to the plates, and may therefore be blown out or gathered into sediment-collectors. The chemical reaction is:

 $\begin{array}{c} \text{Sulphate of lime} + \text{Carbonate of soda} = \text{Sulphate of soda} + \text{Carbonate of lime} \\ \text{CaSO}_4 & \text{NA}_2\text{CO}_3 & \text{NA}_2\text{SO}_4 & \text{CaCO}_3 \end{array}$ 

Sodium phosphate will decompose the sulphates of lime and magnesia: Sulphate of lime + Sodium phosphate = Calcium phos. + Sulphate of soda.  $CaSO_4$   $Na_3FO_4$   $CaHPO_4$   $Na_3SO_4$ 

 $\begin{array}{ccc} Sul. of magnesia + Sodium phosphate = Phosphate of magnesia + Sul. of soda. \\ MgSO_4 & Na_2HPO_4 & MgHPO_4 & Na_2SO_4 \end{array}$ 

Where the quantity of salts is large, scale preventives are not of much use. Some other source of supply must be sought, or the bad water purified before it is allowed to enter the boilers. The damage done to boilers by un-

suitable water is enormous.

Pure water may be obtained by collecting rain, or condensing steam by means of surface condensers. The water thus obtained should be mixed with a little bad water, or treated with a little alkali, as undiluted, pure water corrodes iron; or, after each periodic cleaning, the bad may be used

for a day or two to put a skin upon the plates.

Carbonate of lime and magnesia may be precipitated either by heating the water or by mixing milk of line (Porter Clark process) with it, the water

being then filtered.

Corrosion may be produced by the use of pure water, or by the presence of acids in the water, caused perhaps in the engine-cylinder by the action of high-pressure steam upon the grease, resulting in the production of fatty acids. Acid water may be neutralized by the addition of lime.

Amount of Sediment which may collect in a 100-H.P. steam-boiler, evaporating 3000 lbs. of water per hour, the water containing different amounts of impurity in solution, provided that no water is blown off:

Grains of solid impurities per gallon: 100 10 20 30 60 Equivalent parts per 100,000: 8.57 17.14 34.28 51.42 68.56 85.71 102.85 120 137.1 154.3 171.4 Sediment deposited in 1 hour, pounds: 5.14 10.28 15.42 20.56 25.71 30,85 36 41.1 46.3 51.4 In one day of 10 hours, pounds: 51.4 102.8 154.2 205.6 257.1 308.5 411 463 514 In one week of 6 days, pounds: 154.3 308.5 617.0 925.5 128 1851 2468 3085

If a 100-H.P. boiler has 1200 sq. ft. heating-surface, one week's running without blowing off, with water containing 100 grains of solid matter per gallon in solution, would make a scale nearly 1/5 in. thick, if evenly deposited all over the heating-surface, assuming the scale to have a sp. gr. of 2.5 = 156 lbs. per cu. ft.;  $1/5 \times 120 \times 156 \times 1/12 = 3120$  lbs. **Boiler-scale Compounds.**—The Bavarian Steam-boiler Inspection

Assn. in 1885 reported as follows:

Generally the unusual substances in water can be retained in soluble form or precipitated as mud by adding caustic soda or lime. This is especially

desirable when the boilers have small interior spaces.

It is necessary to have a chemical analysis of the water in order to fully determine the kind and quantity of the preparation to be used for the above purpose. All secret compounds for removing boiler-scale should be avoided. (A list

of 27 such compounds manufactured and sold by German firms is then given which have been analyzed by the association.)

Such secret preparations are either nonsensical or fraudulent, or contain either one of the two substances recommended by the association for removing scale, generally soda, which is colored to conceal its presence, and sometimes adulterated with useless or even injurious matter.

These additions as well as giving the compound some strange, fanciful name, are meant simply to deceive the boiler owner and conceal from him the fact that he is buying colored soda or similar substances, for which he is

paying an exorbitant price

The Chicago, Milwaukee & St. P. R. R. uses for the prevention of scale in locomotive-boilers an alkaline compound consisting of 3750 gals, of water, 2600 lbs. of 70% caustic soda, and 1600 lbs. of 58% soda-ash. Between Milwau-kee and Madison the water-supply contains from 1 to 4½ lbs. of incrusting solids per 1600 gals., principally calcium carbonate and sulphate and mag-nesium sulphate. The amount of compound necessary to prevent the in-crustation is 1½ to 7 pints per 1600 gals. of water. This is really only one fourth of the quantity needed for chemical combination, but the action of the compound is regenerative. The soda-ash (sodium carbonate) extracts carbonic acid from the carbonates of lime and magnesia and precipitates them in a granular form. The bicarbonate of soda thus formed, however, losest searbonic acid by the heat, and is again changed to the active carbonate form. Theoretically this action might continue indefinitely; but on account of the loss by blowing off and the presence of other impurities in the water, it is found that the soda-ash will precipitate only about four times the theoretical quantity. Scaling is entirely prevented. One engine made 122,000 miles, and inspection of the boiler showed that it was as clean as when new. This compound precipitates the impurities in a granular form, and careful attention must be paid to washing out the precipitate. The practice is to change the water every 600 miles and wash out the boiler every 1200 miles, using the blow-off cocks also whenever there is any indication of foaming, which seems to be caused by the precipitate in the water,

but not by the alkali itself. (Eng' g News, Dec. 5, 1891.)

Kerosene and other Petroleum Oils; Foaming.—Kerosene has recently been highly recommended as a scale preventive. See paper by L. F. Lyne (Trans. A. S. M. E., ix. 247). The Am. Mach., May 22, 1890, says: Kerosene used in moderate quantities will not make the boiler foam; it is recommended and used for loosening the scale and for preventing the formation of scale. Neither will a small quantity of common oil always cause foaming; it is sometimes injected into small vertical boilers to preventing, and is supposed to have the same effect on the disturbed surface of the water that oil has when poured out he rough sea. Yet oil in boilers will not have the same effect, and give the desired results in all cases. The presence of oil in combination with other impurities increases the tendency of many boilers to foam, as the oil with the impurities inpredes the free escape of sets an from the water surface. The use of common oil not only tends to cause foaming, but is dangerous otherwise. The grease appears to combine with the impurities of the water, and when the boiler is a treat this compound sinks to the plates and clings to them in a loose, spongy mass, prevening the water from coming in contact with the plates, and thereby pround sinks to the plates and clings to them in a loose, spongy mass, prevening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from coming in contact with the plates, and thereby provening the water from comin

necessary for obtaining the desired results.

R. C. Carpenter (Trans, A. S. M. E., vol. xi.) says: The boilers of the State Agricultural College at Lansing, Mich., were badly incrusted with a hard scale. It was fully three eighths of an inch thick in many places. The first application of the oil was made while the boilers were being but little used, by inserting a gallon of oil, filling with water, heating to the boiling-point and allowing the water to stand in the boiler two or three weeks before removal. By this method fully one half the scale was removed during the warm s-sason and before the boilers were needed for heavy firing. The oil was then added in small quantities when the boiler was in actual use. For boilers 4 ft. in diam, and 12 ft. long the best results were obtained by the use of 2 qts. for each boiler per week, and for each boiler 5 ft. in diam, 3 qts. per week. The water used in the boilers has the following analysis:

 $\begin{array}{ccccc} {\rm CaCO_3~(carbonate~calcium)}, & & 206~{\rm parts~in~1,000,000}, \\ {\rm MgCO_3~(carbonate~magnesium)}, & & 78 & " & " & " \\ {\rm F_2O_3~(carbonate~iron)}, & & 22 & " & " & " \\ {\rm Traces~of~sulphates~and~chlorides~of~potash~and~soda}, & & & & & \\ \end{array}$ 

Total solid parts, 325 to 1,000,000.

Tannate of Soda Compound. -T. T. Parker writes to Am. Mach.:
Should you find kerosen not doing my good try this recine: 50 hs. sal-soda.

Tannate of soda Compound,—1. T. Parker writes to Am. Mach.: Should you find kerosene not doing any good, try this recipe: 50 lbs. sal-soda, 35 lbs. japonica; put the ingredients in a 50-gal. barrel, fill half full of water, and rum a steam hose into it until it dissolves and boils. Remove the hose, fill up with water, and allow to settle. Use one quart per day of ten hours for a 40-H.P. boiler, and, if possible, introduce it as you do cylinder-oil to your engine. Barr recommends tannate of soda as a remedy for scale composed of sulphate and carbonate of lime. As the japonica yields the tannic acid, I think the resultant equivalent to the tannate of soda.

Petroleum Oils heavier than kerosene have been used with good results. Crude oil should never be used. The more volatile oils it contains make explosive gases, and its tarry constituents are apt to form a spongy

incrustation.

Removal of Hard Scale.—When boilers are coated with a hard scale difficult to remove the addition of ½ lb. caustic soda per horse-power, and steaming for some hours, according to the thickness of the scale, just before cleaning, will greatly facilitate that operation, rendering the scale

soft and loose. This should be done, if possible, when the boilers are not

otherwise in use. (Steam.)

Corrosion in Marine Boilers. (Proc. Inst. M. E., Aug. 1884).—The investigations of the Committee on Boilers served to show that the internal corrosion of boilers is greatly due to the combined action of air and seawater when under steam, and when not under steam to the combined action of air and moisture upon the unprotected surfaces of the metal. There are other deleterious influences at work, such as the corrosive action of fatty acids, the galvanic action of copper and brass, and the inequalities of temperature; these latter, however, are considered to be of minor importance.

Of the several methods recommended for protecting the internal surfaces of boilers, the three found most effectual are: First, the formation of a thin layer of hard scale, deposited by working the boiler with sea-water; second, the coating of the surfaces with a thin wash of Portland cement, partially wherever there are signs of decay; third, the use of zinc slabs

suspended in the water and steam spaces.

As to general treatment for the preservation of boilers in store or when laid up in the reserve, either of the two following methods is adopted, as may be found most suitable in particular cases. First, the boilers are dried as much as possible by airing-stoves, after which 2 to 3 cwt, of quick-lime, according to the size of the boiler, is placed on suitable trays at the bottom of the boiler and on the tubes. The boiler is then closed and made as air-tight as possible. Periodical inspection is made every six months, when if the lime be found slacked it is renewed. Second, the other method is to fill the boilers up with sea or fresh water, having added soda to it in the proportion of 1 lb. of soda to every 100 or 120 lbs, of water. The sufficiency of the saturation can be tested by introducing a piece of clean new iron and leaving it in the boiler for the or twelve hours; if it shows signs of rusting, more soda should be added. It is essential that the boilers be entirely filled, to the complete exclusion of air.

Great care is taken to prevent sudden changes of temperature in boilers. Directions are given that steam shall not be raised rapidly, and that care shall be taken to prevent a rush of cold air through the tubes by too suddenly opening the smoke-box doors. The practice of emptying boilers by blowing out is also prohibited, except in cases of extreme urgency. As a rule the water is allowed to remain until it becomes cool before the boilers

are emptied.

Mineral oil has for many years been exclusively used for internal lubrication of engines, with the view of avoiding the effects of fatty acid, as this oil

does not readily decompose and possesses no acid properties.

Of all the preservative methods adopted in the Eritish service, the use of zinc properly distributed and fixed has been found the most effectual in saving the iron and steel surfaces from corrosion, and also in neutralizing by its own deterioration the hurtful influences met with in water as ordinarily supplied to boilers. The zinc slabs now used in the navy boilers are 12 in. long, 6 in, wide, and ½ inch thick; this size being found convenient for general application. The amount of zinc used in new boilers at present is one slab of the above size for every 20 I.H.P., or about one square foot of zinc surface to two square feet of grate surface. Rolled zinc is found the most suitable for the purpose. To make the zinc properly efficient as a protector especial care must be taken to insure perfect metallic contact between the slabs and the stays or plates to which they are attached. The slabs should be placed in such positions that all the surfaces in the boiler shall be protected. Each slab should be periodically examined to see that its connection remains perfect, and to renew any that may have decayed; this examination is usually made at intervals not exceeding three months. Under ordinary circumstances of working these zinc slabs may be expected to last in fit condition from sixty to innety days, immersed in hot sea-water; but in new boilers they at first decay more rapidly. The slabs are generally secured by means of iron straps 2 in, wide and 36 inch thick, and long enough to reach the nearest stay, to which the strap is firmly attached by serve-bolts.

To promote the proper care of boilers when not in use the following order has been issued to the French Navy by the Government: On board all ships in the reserve, as well as those which are laid up, the boilers will be completely filled with fresh water. In the case of large boilers with large tubes there will be added to the water a certain amounts of milk of lime, or a solution of soda may be used instead. In the case of tubulous boilers with small tubes milk of lime or soda may be added, but the solution will not be

so strong as in the case of the larger tube, so as to avoid any danger of contracting the effective area by deposit from the solution; but the strength of the solution will be just sufficient to neutralize any acidity of the water.

(Iron Age, Nov. 2, 1893.)

Use of Zinc.—Zinc is often used in boilers to prevent the corrosive action of water on the metal. The action appears to be an electrical one, the iron being one pole of the battery and the zinc being the other. The hydrogen goes to the iron shell and escapes as a gas into the steam.

oxygen goes to the zinc.

On account of this action it is generally believed that zinc will always prevent corrosion, and that it cannot be harmful to the boiler or tank. Some experiences go to disprove this belief, and in numerous cases zinc has not only been of no use, but has even been harmful. In one case a tubular boiler had been troubled with a deposit of scale consisting chiefly of organic matter and lime, and zinc was tried as a preventive. The beneficial action of the zinc was so obvious that its continued use was advised, with frequent opening of the boiler and cleaning out of detached scale until all the old scale should be removed and the boiler become clean. Eight or ten months later the water supply was changed, it being now obtained from another stream supposed to be free from lime and to contain only organic matter. Two or three months after its introduction the tubes and shell were found to be coated with an obstinate adhesive scale, and composed of zinc oxide and the organic matter or sediment of the water used. The deposit had become so heavy in places as to cause overheating and bulging of the plates over the fire. (The Locomotive.)

Effect of Deposit on Flues, (Rankine.)—An external crust of a carbonaceous kind is often deposited from the flame and smoke of the furnaces in the flues and tubes, and if allowed to accumulate seriously impairs the economy of fuel. It is removed from time to time by means of scrapers and wire brushes. The accumulation of this crust is the probable cause of the fact that in some steamships the consumption of coal per indicated horse-power per hour goes on gradually increasing until it reaches one and a half times its original amount, and sometimes more.

Dangerous Steam-boilers discovered by Inspection.—The Hartford Steam-boiler Inspection and Insurance Co. reports that its

inspectors during 1893 examined 163,328 boilers, inspected 66,698 boilers, both internally and externally, subjected 7861 to hydrostatic pressure, and found 597 unsafe for further use. The whole number of defects reported was 122,893, of which 12,390 were considered dangerous. A summary is given below. (The Locomotive, Feb. 1894.)

SUMMARY, BY DEFECT	s, for the Year 1893.	
Nature of Defects. Whole Dan- No. gerous.	Nature of Defects. Whole I	Dan- rous.
Deposit of sediment 9,774 548		2,909
Incrustation and scale18,369 865	Leakage at seams 5,424	482
Internal grooving 1,249 148	Water-gauges defective. 3,670	660
	Blow outs defective 1,620	425
External corrosion 8,600 536	Deficiency of water 204	107
	Safety-valves overloaded 723	203
	Safety-valves defective 942	300
Furnaces out of shape 4,575 254	Pressure-gauges def'tive 5,953	552
	Boilers without pressure-	
Burned plates 2,762 325	gauges 115	115
Blistered plates 3,331 164	Unclassified defects 755	4
Defective rivets 17,415 1,569		
Defective heads 1,357 350	Total122,893 1	2,390

The above-named company publishes annually a classified list of boilerexplosions, compiled chiefly from newspaper reports, showing that from 200 to 300 explosions take place in the United States every year, killing from 200 to 300 persons, and injuring from 300 to 450. The lists are not pretended to be complete, and may include only a fraction of the actual number of explosions

Steam-boilers as Magazines of Explosive Energy, - Prof. H. Thurston (Trans. A. S. M. E., vol. vi.), in a paper with the above title, presents calculations showing the stored energy in the hot water and s eam of various boilers. Concerning the plain tubular boiler of the form and dimensions adopted as a standard by the Hartford Steam boiler Insurance Co., he says: It is 60 inches in diameter, containing 66 3-inch tubes, and is 15 feet long. It has 850 feet of heating and 30 feet of grate tubes, and is 15 feet long. It has 850 feet of heating and 30 feet of grale surface; is rated at 60 horse-power, but is oftener driven up to 75; weighs 9500 pounds, and contains nearly its own weight of water, but only 21 pounds of steam when under a pressure of 75 pounds per square inch, which is below its safe allowance. It stores 52,000,000 foot-pounds of energy, of which but 4 per cent is in the steam, and this is enough to drive the boiler just about one mile into the air, with an initial velocity of nearly 600 feet per second.

### SAFETY-VALVES.

## Calculation of Weight, etc., for Lever Safety-valves,

Let W = weight of ball at end of lever, in pounds; w = weight of lever itself, in pounds; V = weight of valve and spindle, in pounds;

g = " " " " " A = area of valve, in square inches;

P = pressure of steam, in lbs. per sq. in., at which valve will open.

$$\begin{aligned} \text{Then} \quad PA \times l &= W \times L + w \times g + V \times l; \\ \text{whence} \quad P &= \frac{WL + wg + Vl}{Al}; \\ W &= \frac{PAl - wg - Vl}{L}; \\ L &= \frac{PAl - wg - Vl}{W}. \end{aligned}$$

EXAMPLE.—Diameter of valve, 4"; distance from fulcrum to centre of ball, 36"; to centre of valve, 4"; to centre of gravity of lever, 15½"; weight of valve and spindle, 3 lbs.; weight of lever, 7 lbs.; required the weight of ball to make the blowing-off pressure 80 lbs. per sq. in.; area of 4" valve = 12.566

$$W = \frac{PAl - wg - Vl}{L} = \frac{80 \times 12.566 \times 4 - 7 \times 151/2 - 4 \times 4}{36} = 108.2 \text{ lbs.}$$

The following rules governing the proportions of lever-valves are given by the U.S. Supervisors. The distance from the fulcrum to the valve-stem must in no case be less than the diameter of the valve-opening; the length of the lever must not be more than ten times the distance from the fulcrum to the valve-stem; the width of the bearings of the fulcrum must not be less than three quarters of an inch; the length of the fulcrum-link must not less than three quarters or an inch; the length of the fulcrunn-link must be one less than four inches; the lever and fulcrunn-link must be made of wrought iron or steel, and the knife-edged fulcrunn points and the bearings for these points must be made of steel and hardened; the valve must be guided by its spindle, both above and below the ground seat and above the lever, through supports either made of composition (gun-metal) or bushed with it; and the spindle must fit loosely in the bearings or supports.

### Rules for Area of Safety-valves.

(Rule of U. S. Supervising Inspectors of Steam-vessels (as amended 1894).)

Lever safety-valves to be attached to marine boilers shall have an area of not less than 1 sq. in. to 2 sq. ft. of the grate surface in the boiler, and the seats of all such safety-valves shall have an angle of inclination of 45° to the centre line of their axes.

Spring-loaded safety-valves shall be required to have an area of not less than 1 sq. in, to 3 sq. ft. of grate surface of the boiler, except as hereinafter otherwise provided for water-tube or coil and sectional boilers, and each spring-loaded valve shall be supplied with a lever that will raise the valve from its seat a distance of not less than that equal to one eighth the diameter of the valve-opening, and the seats of all such safety-valves shall have an angle of inclination to the centre line of their axes of 45°. All spring-loaded safety-valves for water-tube or coil and sectional boilers required to

carry a steam-pressure exceeding 175 lbs, per square inch shall be required to have an area of not less than 1 sq. in, to 6 sq. ft, of the grate surface of the boiler. Nothing herein shall be construed so as to prohibit the use of two safety-valves on one water-tube or coil and sectional boiler, provided the combined area of such valves is equal to that required by rule for one

such valve

Rule in Philadelphia Ordinances: Bureau of Steam-engine and Boiler Inspection.—Every boller when fired sepa-ratery, and every set or series of boilers when placed over one fire, shall have attached thereto, without the interposition of any other valve, two or more safety-valves, the aggregate area of which shall have such relations to the area of the grate and the pressure within the boiler as is expressed in schedule A.

SCHEDULE A .- Least aggregate area of safety-valve (being the least sectional area for the discharge of steam) to be placed upon all stationary boil-

ers with natural or chimney draught [see note a].

$$A = \frac{22.5G}{P + 8.62},$$

in which A is area of combined safety-valves in inches; G is area of grate in square feet; P is pressure of steam in pounds per square inch to be carried in the boiler above the atmosphere.

The following table gives the results of the formula for one square foot of

grate, as applied to boilers used at different pressures:

Area corresponding to one square foot of grate:

1.21 0.79 0.58 0.46 0.38 0.33 0.29 0.25 0.23 0.21

[Note a.] Where boilers have a forced or artificial draught, the inspector

[Note a.] Where bollers have a forced or artificial draught, the inspector must estimate the area of grate at the rate of one square foot of grate-surface for each 16 lbs. of fuel burned on the average per hour.

Comparison of Various Rules for Area of Lever Safety-valves. (From an article by the author in American Machinist, May 24, 1891, with some alterations and additions.)—Assume the case of a boiler rated at 100 horse-power; 40 sq. ft. grate; 1200 sq. ft. heating-surface; using 400 lbs. of coal per hour, or 10 lbs. per sq. ft. of grate per hour, and evaporating 8000 lbs. of water, or 3 lbs. per sq. ft. of heating-surface per hour; steam-pressure by gauge, 100 lbs. What size of safety-valve, of the lever type, should be required? type, should be required?

A compilation of various rules for finding the area of the safety-vale disk,

from The Locomotive of July, 1892, is given in abridged form below, together with the area calculated by each rule for the above example.

Disk Area in sq. in. U. S. Supervisors, heating-surface in sq. ft. +25\* 48 English Board of Trade, grate-surface in sq. ft. +2 20 Molesworth, four fifths of grate-surface in sq. ft. 33 Thurston, 4 times coal burned per hour  $\times$  (gauge pressure + 10). 14.5 1 (5 × heating-surface) Thurston,  $\frac{1}{2}$  gauge pressure +10... 

Suppose that, other data remaining the same, the draught were increased so as to burn 13½ lbs. coal per square foot of grate per hour, and the grate-surface cut down to 30 sq. ft. to correspond, making the coal burned per hour 400 lbs., and the water evaporated 3600 lbs., the same as before; then the English Board of Trade rule and Molesworth's rule would give an area of disk of only 15 and 24 sq. in., respectively, showing the absurdity of making the area of grate the basis of the calculation of disk area.

Another rule by Prof. Thurston is given in American Machinist, Dec. 1877,

viz.:

Disk area =  $\frac{1}{2}$  max. wt. of water evap. per hour gauge pressure + 10

This gives for the example considered 16.4 sq. in.

<sup>\*</sup> The edition of 1893 of the Rules of the Supervisors does not contain this rule, but gives the rule grate-surface + 2.

One rule by Rankine is 1/150 to 1/180 of the number of pounds of water

one rme by rankine is 1/100 to respectively

The Philadelphia rule for 100 lbs. gauge pressure gives a disk area of 0.21 sq. in, for each sq. ft. of grate area, which would give an area of 8.4 sq. in, for 40 sq. ft. grate, and only 6.3 sq. in. if the grate is reduced to 30 sq. ft.

According to the rule this aggregate area would have to be divided between two valves. But if the boiler was driven by forced draught, then the inspector "must estimate the area of grate at 1 sq. ft. for each 16 lbs. of fuel burned per hour.

Under this condition the actual grate-surface might be cut down to 400 + 16 = 25 sq. ft., and by the rule the combined area of the two safety-valves would be only  $25 \times 0.21 = .25$  sq. in.

Nystrom's Pocket-book, edition of 1891, gives 34 sq. in. for 1 sq. ft. grate; also quoting from Weisbach, vol. ii, 1/3000 of the heating-surface, This in the case considered is 1200/3000 = .4 sq. ft. or 57.6 sq. in.

We thus have rules which give for the area of safety-valve of the same 100-

horse-power boiler results ranging all the way from 5.25 to 57.6 sq. in. All of the rules above quoted give the area of the disk of the valve as the thing to be ascertained, and it is this area which is supposed to bear some direct ratio to the grate-surface, to the heating-surface, to the water evaporated, etc. It is difficult to see why this area has been considered even approximately proportional to these quantities, for with small lifts the area of actual opening bears a direct ratio, not to the area of disk, but to the circumference.

Thus for various diameters of valve .

Diameter	1	2	3	4١	4	6	7
Area	.785	3.14	7.07	12.57	19.64	28.27	38.48
Circumference		6.28	9.42	12.57	15.71	18.85	21.99
Circum. X lift of 0.1 in	.31	.63	.94	1.26	1.57	1.89	2.20
Ratio to area	.4	.2	.13	.1	.08	.067	.057

The apertures, therefore, are therefore directly proportional to the diameter or to the circumference, but their relation to the area is a varying one.

If the lift = 1/4 diameter, then the opening would be equal to the area of the disk, for circumference × 1/4 diameter = area, but such a lift is far beyond the actual lift of an ordinary safety-valve.

A correct rule for size of safety-valves should make the product of the

diameter and the lift proportional to the weight of steam to be discharged.

A' logical' method for calculating the size of safety-valve is given in

A' Locomotive. July, 1892, based on the assumption that the actual opening should be sufficient to discharge all the steam generated by the boiler. Napier's rule for flow of steam is taken, viz., flow through aperture of one sq. in, in lbs. per second = absolute pressure  $\div$  70, or in lbs. per hour = 51.43 × absolute pressure.

If the angle of the seat is 45°, as specified in the rules of the U. S. Supervisors, the area of opening in sq. in. = circumference of the disk x the lift

 71, 71 being the cosine of 45°; or diameter of disk × lift × 2.23.
 A. G. Brown in his book on The Indicator and its Practical Working (London, 1894) gives the following as the lift of the ordinary lever safetyvalve for 100 lbs. gauge-pressure:

Diam, of valve ... 2 3 31/6 41/2 

The lift decreases with increase of steam-pressure; thus for a 4-inch valve: 135 85 Abs. pressure, lbs. 45 65 105 195 The effective area of opening Mr. Brown takes at 70% of the rise multiplied

by the circumference,

An approximate formula corresponding to Mr. Brown's figures for diameters between 21/2 and 6 in. and gauge-pressures between 70 and 200 lbs. is

Lift =  $(.0603 - 0031d) \times \frac{110}{\text{abs. pressure}}$ , in which d = diam. of valve in in,

If we combine this formula with the formulæ

Flow in lbs. per hour = area of opening in sq. in,  $\times$  51.43 $\times$  abs. pressure, and Area = diameter of valve  $\times$  lift  $\times$  2.23, we obtain the following, which the author suggests as probably a more correct formula for the discharging

capacity of the ordinary lever safety-valve than either of those above given. Flow in lbs, per hour =  $d(.0603 - .0031d) \times 115 \times 2.23 \times 51.43 = d(.795 - 41d)$ .

From which we obtain:

Dia.value, in

Lift, inches.

160

180

200

.125

1696 2064 4760 6794 9175 11900 14955 18355

1883 3400

Diameter, inches .... Flow, lbs. per hour.. 754 1426 2016 2524 2950 3294 3556 37 47 76 Horse-power ..... 25 58 84 98 110 119

the horse-power being taken as an evaporation of 30 lbs. of water per hour. If we solve the example, above given, of the boiler evaporating 3600 lbs. of water per hour by this table, we find it requires one 7-inch valve, or a 21/2-and a 3-inch valve combined. The 7-inch valve has an area of 38.5 sq. in., and the two smaller valves taken together have an area of only 12 sq. iu.; another evidence of the absurdity of considering the area of disk as the

factor which determined the capacity of the valve. It is customary in practice not to use safety-valves of greater diameter than 4 in. If a greater diameter is called for by the rule that is adopted,

then two or more valves are used instead of one,

Spring-loaded Safety-valves.—Instead of weights, springs are sometimes employed to hold down safety-valves. The calculations are similar to those for lever safety-valves, the tension of the spring corresponding to a given rise being first found by experiment (see Springs, page 347).

The rules of the U. S. Supervisors allow an area of 1 sq. in. of the valve to 3 sq. ft. of grate, in the case of spring-loaded valves, except in water-tube, coil, or sectional boilers, in which 1 sq. in. to 6 sq. ft. of grate is allowed.

Spring-loaded safety-valves are usually of the reactionary or "pop" type, in which the escape of the steam is opposed by a lip above the valve-seat, against which the escaping steam reacts, causing the valve to lift higher than the ordinary valve.

A. G. Brown gives the following for the rise, effective area, and quantity of steam discharged per hour by valves of the "pop" or Richardson type. The effective is taken at only 50% of the actual area due to the rise, on account of the obstruction which the lip of the valve offers to the escape of steam. 21/6

200 .225 .250 .275 .300 .325 .375

22095 30595

24520 33950

26855 37185

.200

Arces, sq. m.	1 .100	1 .001	1 .000	1 .100	, 1.001	11.010	1 2.100	1 ~.1~1	0.000
Gauge-pres.,		Steam discharged per hour, lbs.							
30 lbs.	474	856	1330	1897	2563	3325	4178	5128	6173 8578
50	669	1209	1878	2680	3620	4695	5901	7242	8718 12070
70	861	1556	2417	3450	4660	6144	7596	9324	11220 15535
90	1050	1897	2947	4207	5680	7370	9260	11365	13685 18945
100	1144	2065	3208	4580	6185	8322	10080	12375	14895 20625
120	1332	2405	3736	5332	7202	9342	11735	14410	17340 24015
140	1516	9790	4954	6070	8-200	10625	19965	16105	10745 07940

2062 3724 5786 8258 11150 14465 18175 22310 If we take 30 lbs. of steam per hour, at 100 lbs. gauge-pressure = 1 H.P., we have from the above table

11/2 Diameter, inches... 1 1½ Horse-power..... 38 69 21/6 107 153 206 336 412 277 496 687

7540 10180 13250 16595 20370

A safety-valve should be capable of discharging a much greater quantity of steam than that corresponding to the rated horse-power of a boiler, since a boiler having ample grate surface and strong draught may generate more than double the quantity of steam its rating calls for.

The Consolidated Safety-valve Co.'s circular gives the following rated capacity of its nickel-seat 'pop' safety-valves. Size, in ... 1 1/4 11/5 2 2/5 3 3/5 4 4/5 5 5/63

21/2 60 Boiler | from 10 200 50 to 10 30 100 150 200

The figures in the lower line from 2 inch to 5 inch, inclusive, correspond to the formula H.P. = 50(diameter - 1 inch).

### THE INJECTOR. Equation of the Injector.

Let S be the number of pounds of steam used:

W the number of pounds of water lifted and forced into the boiler: h the height in feet of a column of water, equivalent to the absolute pressure in the boiler;

he the height in feet the water is lifted to the injector;

- $t_i$  the temperature of the water before it enters the injector;  $t_i$  the temperature of the water after leaving the injector;  $t_i$  the temperature of the water after leaving the injector;  $t_i$  the total heat above  $33^{\circ}$  F, in one pound of steam in the boiler, in heat-units:
- L the lost work in friction and the equivalent lost work due to radiation and lost heat;
  778 the mechanical equivalent of heat.

Then

$$S[H - (t_2 - 32^\circ)] = W(t_2 - t_1) + \frac{(W + S)h + Wh_0 + L}{778}.$$

An equivalent formula, neglecting  $Wh_0 + L$  as small, is

$$\begin{split} S &= \left[ W(t_2 - t_1) + \frac{W + S}{d} \cdot p \cdot \frac{144}{778} \right] \frac{1}{H - (t_2 - 32^5)^5} \\ \text{or} \quad S &= \frac{W[(t_2 - t_1)d + .1851p]}{H - (t_2 - 32^2)d - .1851p}, \end{split}$$

in which d = weight of i cu. ft. of water at temperature  $t_2$ ; p = absolute pressure of steam, lbs. per sq. in. The rule for finding the proper sectional area for the narrowest part of

the nozzles is given as follows by Rankine, S. E. p. 477:

Area in square inches = cubic feet per hour gross feed-water 800 / pressure in atmospheres

An important condition which must be fulfilled in order that the injector will work is that the supply of water must be sufficient to condense the steam. As the temperature of the supply or feed-water is higher, the amount of water required for condensing purposes will be greater.

The table below gives the calculated value of the maximum ratio of water

to the steam, and the values obtained on actual trial, also to be highest admissible temperature of the feed-water as shown by theory and the highest admissible temperature of the feed-water as shown by theory and the highest actually found by trial with several injectors.

	MAXIMUM TO	RATIO		TER		MA	XIMUM FEI	TEMP ED-W			OF
Gauge- pres-		Acti	ıal F	Expe-	Gauge- pres- sure,	Theor	etical.	Exp	eri'ta	l Re	sults.
pounds per sq. in.	Calculated from Theory.		P.		pounds per sq. in.	Temp. discharge 180°.	Temp. discharge	н.	Р.	М.	S.
10 20 30 40 50 60 70 80 90 100	36.5 25.6 20.9 17.87 16.2 14.7 13.7 12.9 12.1 11.5	19.0 15.8 13.3 11.2 12.3	19.9 17.2 15.0 14.0 11.2 11.7	19.0 15.86 13.3 12.6 12.9	10 20 30 40 50 60 70 80 90 100 120 150	142° 132 126 120 114 109 105 99 95 87	173° 162 156 150 143 139 134 129 125 117 107	135° 140 141* 141*	120° 113 115 118	130° 125 123 123 122	182°. 184 134 132 181 130 130 131 132* 182* 184* 121*

<sup>\*</sup> Temperature of delivery above 212°. Waste-valve closed.

H. Hancock inspirator; P, Park injector; M, Metropolitan injector; S, Sellers 1876 injector.

Efficiency of the Injector .- Experiments at Cornell University, described by Prof. R. C. Carpenter, in Cassier's Magazine, Feb. 1892, show that the injector, when considered inerely as a pump, has an exceedingly low efficiency, the duty ranging from 161,000 to 2,732,000 under different circumstances of steam and delivery pressure. Small direct-acting pumps, such as are used for feeding boilers, show a duty of from 4 to 8 million lbs, and the best pumping-engines from 100 to 140 million. When used for feeding water into a boiler, however, the injector has a thermal efficiency of 100%, less the trifling loss due to radiation, since all the heat rejected passes into the water which is carried into the boiler.

The loss of work in the injector due to friction reappears as heat which is carried into the boiler, and the heat which is converted into useful work in

the injector appears in the boiler as stored-up energy.

Although the injector thus has a perfect efficiency as a boiler-feeder, it is nevertheless not the most economical means for feeding a boiler, since it can draw only cold or moderately warm water, while a pump can feed water which has been heated by exhaust steam which would otherwise be wasted.

Performance of Injectors.—In Am. Mach., April 13, 1893, are a number of letters from different manufacturers of injectors in reply to the question: "What is the best performance of the injector in raising or lifting water to any height?" Some of the replies are tabulated below.

W. Sellers & Co. -25.51 lbs. water delivered to boiler per lb. of steam; temperature of water, 64°; steam pressure, 65 lbs.

Schaeffer & Budenberg—1 gal, water delivered to boile for 0.4 to 0.8 lb.

Injector will lift by suction water of

136° to 133° 140° F. 122° to 180° 113° to 107° If boiler pressure is. 30 to 60 lbs. 60 to 90 lbs. 90 to 120 lbs. 120 to 150 lbs.

If the water is not over 80° F., the injector will force against a pressure 75 lbs. higher than that of the steam.

Hancock Inspirator Co.: 22 22 Lift in feet..... Boiler pressure, absolute, lbs..... 75.8 54.1 95.5 75.4 Temperature of suction ..... 34.90 35.4° 47.3° 173.7° 53.2° Temperature of delivery ...... 134° Water fed per lb. of steam, lbs... 11.0 117.40 131.1 11.02 13.67 8.18 13.3

The theory of the injector is discussed in Wood's, Peabody's, and Rontgen's treatises on Thermodynamics. See also "Theory and Practice of the Injector," by Strickland L. Kueass, New York, 1895.

Injector," by Strickland L. Kneass, New York, 1895.

Roiler-feeding Pumps,—Since the direct-acting pump, commonly used for feeding boilers, has a very low efficiency, or less than one tenth that of a good engine, it is generally better to use a pump driven by belt from the main engine or driving shaft. The mechanical work needed to feed a boiler may be estimated as follows: If the combination of boiler and engine is such that half a cubic foot, say 32 lbs, of water, is needed per horse-power, and the boiler-pressure is 100 lbs, × 144 sq, in, × 194 ft.-lbs, per hour = 120 ft.-lbs, per min. = 120/33,000 = .0036 H.P., or less than 4/10 of 1/8 of the power exerted by the engine. If a direct-acting pump, which discharges its evaluate texam into the atmosphere, is used for feeding, and it has only 1/10. exhaust steam into the atmosphere, is used for feeding, and it has only 1/10 the efficiency of the main engine, then the steam used by the pump will be equal to nearly 4% of that generated by the boiler.

The following table by Prof. D. S. Jacobus gives the relative efficiency of steam and power pumps and injector, with and without heater, as used upon a boiler with 80 lbs. gauge-pressure, the pump having a duty of 10,000,000 ft.-lbs. per 100 lbs. of coal when no heater is used; the injector heating the water from 60 to 150 F.

Direct-acting pump feeding water at 60°, without a heater..... 1.000 Injector feeding water at 150°, without a heater. .985Injector feeding water through a heater in which it is heated from 150° to 200°..... .938

Direct-acting pump feeding water through a heater, in which it is heated from 60° to 200°. .879

Geared pump, run from the engine, feeding water through a heater, in which it is heated from 60° to 200°..... .868

### FEED-WATER HEATERS.

Percentage of Saving for Each Degree of Increase in Tem-perature of Feed-water Heated by Waste Steam.

Initial Temp.	Pressure of Steam in Boiler, lbs. per sq. in. above Atmosphere.									Initial Temp,		
Feed.	0	20	40	60	80	100	120	140	160	180	200	Tomp.
320	.0872	.0861	0855	.0851	.0847	0844	.0841	.0839	.0837	.0835	.0833	32
40						.0850			.0843		.0839	40
50				.0864		.0857			.0850		.0846	50
60						.0864				.0855	.0853	60
70	.0902	.0890	.0884	.0879	.0875	.0872	.0869	.0867	.0864	.0862	.0860	70
80	.0910	.0898				.0879	.0877	.0874	.0872	.0870	.0868	80
90	.0919	.0907	.0900	.0895	.0888	.0887	.0884	.0883	.0879	.0877	.0875	90
100	.0927					.0895			.0887		.0883	100
110				.0911		.0903						110
120		.0932		.0919		.0911						120
130						.0920						130
140						.0929						140
150	.0973					.0937						150 •
160 ·						.0946					.0933	160
170	.0992					.0955						170
180	.1002					.0965						180
190	.1012					.0974			.0964		0960	190
200	.1022					.0984			.0974			200
210	.1033					.0994				.0981	.0979	210
220			.1019		.1008				.0994		.0989	220
230			.1031			. 1012				.1001	.0999	230
240			.1041			.1024					.1009	240
250		1.1063	1.1052	1.1045	. 1040	1035	1.1031	.1027	.1025	1.1022	. 1019	250

An approximate rule for the conditions of ordinary practice is a saving of 1% is made by each increase of 11° in the temperature of the feed-water.

This corresponds to .0909% per degree.

The calculation of saving is made as follows: Boiler-pressure, 100 lbs. gauge; total heat in steam above 32° = 1185 B.T.U. Feed-water, original temperature 60°, final temperature 200° F. Increase in heat-units, 150, Heat-units above 32° in feed water of original temperature = 28. Heatunits in steam above that in cold feed-water, 1185 - 28 = 1157. Saving by the feed-water heater = 150/1157 = 12.96%. The same result is obtained by the use of the table. Increase in temperature 150°  $\times$  tabular figure .0864 = 12.96%. Let total heat of 1 lb. of steam at the boiler-pressure = H; total heat of 1 lb. of feed-water before entering the heater  $= h_1$ , and after pass-

ing through the heater =  $h_2$ ; then the saving made by the heater is  $\frac{n_2 - n_1}{H - h_1}$ 

Strains Caused by Cold Feed-water.-A calculation is made in The Locomotive of March, 1893, of the possible strains caused in the section of the shell of a boiler by cooling it by the injection of cold feed-water. Assuming the plate to be cooled 200° F, and the coefficient of expansion of steel to be .0000067 per degree, a strip 10 in. long would contract .013 in., if it were free to contract. To resist this contraction, assuming that the strip is firmly held at the ends and that the modulus of elasticity is 29,000,000, would require a force of 37,700 lbs. per sq. in. Of course this amount of strain cannot actually take place, since the strip is not firmly held at the ends, but is allowed to contract to some extent by the elasticity of the surrounding metal. But, says The Locomotive, we may feel pretty confident that in the case considered a longitudinal strain of somewhere in the neighborhood of \$600 or 10,000 lbs. per sq. in. may be produced by the feed-water striking directly upon the plates; and this, in addition to the normal strain produced by the steam-pressure, is quite enough to tax the girth-seams beyond their elastic limit, if the feed-pipe discharges anywhere near them. Hence it is not surprising that the girth seams develop leaks and cracks in 99 cases out of every 100 in which the feed discharges directly upon the firesheets.

### STEAM SEPARATORS.

If moist steam flowing at a high velocity in a pipe has its direction suddenly changed, the particles of water are by their momentum projected in their original direction against the bend in the pipe or wall of the chamber in which the change of direction takes place. By making proper provision for drawing off the water thus separated the steam may be dried to a greater or less extent.

For long steam-pipes a large drun should be provided near the engine for trapping the water condensed in the pipe. A drun 3 feet diameter, 15 feet high, has given good results in separating the water of condensation of

a steam-pipe 10 inches diameter and 800 feet long

Efficiency of Steam Separators.—Prof. R. C. Carpenter, in 1891, made a series of tests of six steam separators, fu nishing them with steam containing different percentages of moisture, and testing the quality of steam before entering and after passing the separator. A condensed table of the principal results is given below.

of ttor.	Test with	Steam of ab Moisture.	out 10% of	Tests with	Varying Me	oisture.
Make of Separator.	Quality of Steam before.	Quality of Steam after.	Efficiency per cent.	Quality of Steam before.	Quality of Steam after.	Av'ge Effi- ciency.
. B	87.0%	98.8%	90.8	66,1 to 97.5%	97.8 to 99%	87.6
	90.1	98.0	80.0	51.9 " 98	97.9 " 99.1	76.4
A D C E	89.6	95.8	59.6	72.2 " 96.1	95.5 " 98.2	71.7
Ċ	90.6	93.7	33.0	67.1 " 96.8	93,7 " 98.4	63.4
E	88.4	90.2	15.5	68.6 " 98.1	79.3 " 98.5	36.9
F	88.9	92.1	28.8	70.4 " 97.7	84.1 " 97.9	28.4

Conclusions from the tests were: 1. That no relation existed between the volume of the several sepurators and their efficiency.
2. No marked decrease in pressure was shown by any of the separators,

the most being 1.7 lbs. in E.

3. Although changed direction, reduced velocity, and perhaps centrifugal

force are necessary for good separation, still some means must be provided to lead the water out of the current of the steam. The high efficiency obtained from B and A was largely due to this feature.

In B the interior surfaces are corrugated and thus catch the water thrown out of the steam and readily lead it to the bottom.

out of the steam and readily lead it to the bottom.

In A, as soon as the water falls or is precipitated from the steam, it comes

in contact with the perforated diaphragm through which it runs into the space below, where it is not subjected to the action of the steam.

In D, the next in efficiency, this is accomplished by means of a >-shaped

In D, the next in efficiency, this is accomplished by means of a >-shaped diaphragm which throws the water back into the corners out of the current of steam.

### DETERMINATION OF THE MOISTURE IN STEAM— STEAM CALORIMETERS.

In all boiler-tests it is important to ascertain the quality of the steam, i.e., 1st, whether the steam is "saturated" or contains the quantity of heat due to the pressure according to standard experiments; 2d, whether the quantity of heat is deficient, so that the steam is wet; and 3d, whether the heat is in excess and the steam superheated. The best method of ascertaining the quality of the steam is undoubtedly that employed by a committee which tested the boilers at the American Institute Exhibition of 1871-2, of which Prof. Thurston was chairman, i.e., condensing all the water evaporated by the boiler by means of a surface condenser, weighing the condensing water, and taking its temperature as it enters and as it leaves the condenser; but this plan cannot always be adopted.

A substitute for this method is the barrel calorimeter, which with careful operation and fairly accurate instruments may generally be relied on to give results within two per cent of accuracy (that is, a sample of steam which gives the apparent result of 2% of moisture may contain anywhere be tween 0 and 4%). This calorimeter is described as follows: A sample of the steam is taken by inserting a perforated ½-linch pipe into and through the main pipe near the boiler, and led by a hose, thoroughly felted, to a barrel, holding preferably 400 lbs, of water, which is set upon a platform scale and

provided with a cock or valve for allowing the water to flow to waste, and

with a small propeller for stirring the water

To operate the calorimeter the barrel is filled with water, the weight and temperature ascertained, steam blown through the hose outside the barrel until the pipe is thoroughly warmed, when the hose is suddenly thrust into the water, and the propeller operated until the temperature of the water is increased to the desired point, say about 110° usually. The hose is then withdrawn quickly, the temperature noted, and the weight again taken.

An error of 1/10 of a pound in weighing the condensed steam, or an error of 1/2 degree in the temperature, will cause an error of over 1% in the calcu-

lated percentage of moisture. See Trans. A. S. M. E., vi. 293.

When all the steam generated is not condensed, the method of making the connection for the purpose of taking out a sample is of the utmost importance. Unless great care be exercised, the results will frequently show that the steam is superheated when the boiler has no superheating surface. The samples should be taken from the main steam-pipe, but not from the

bottom, as this would take all the water draining to that point.

The calculation of the percentage of moisture is made as below:

$$Q = \frac{1}{H-T} \left[ \frac{W}{w} (h_1 - h) - (T - h_1) \right],$$

Q= quality of the steam, dry saturated steam being unity. H= total heat of 1 lb. of steam at the observed pressure. T= " " water at the temperature of steam of the observed pressure.

66 h =" condensing water, original.

46 .. W = Wfinal. = weight of condensing water, corrected for water-equivalent of the apparatus.

w = weight of the steam condensed.

Percentage of moisture = 1 - Q.

If Q is greater than unity, the steam is superheated, and the degrees of superheating = 2.0833 (H - T) (Q - 1).

Coil Calorimeters. - Instead of the open barrel in which the steam is condensed, a coil acting as a surface-condenser may be used, which is placed in the barrel, the water in coil and barrel being weighed separately. For description of an apparatus of this kind designed by the author, which he has found to give results with a probable error not exceeding ½ per cent of moisture, see Trans. A. S. M. E., vi. 294. This calorimeter may be used continuously, if desired, instead of internitiently. In this case a continuous flow of condensing water into and out of the barrel must be established, and the temperature of inflow and outflow and of the condensed steam read at short intervals of time.

Throttling Calorimeter .- For percentages of moisture not exceeding 3 per cent the throttling calorimeter is most useful and convenient and remarkably accurate. In this instrument the steam which reaches it in a ½-inch pipe is throttled by an orifice 1/16 inch diameter, opening into a chamber which has an outlet to the atmosphere. The steam in this chamber has its pressure reduced nearly or quite to the pressure of the atmosphere, but the total heat in the steam before throttling causes the steam in the chamber to be superheated more or less according to whether the steam before throttling was dry or contained moisture. The only observations required are those of the temperature and pressure of the steam on each side of the orifice

The author's formula for reducing the observations of the throttling calorimeter is as follows (Experiments on Throttling Calorimeters, Am. Mach., Aug. 4, 1892):  $w = 100 \times \frac{H - h - K(T - t)}{4}$ , in which w = percent-

age of moisture in the steam; H= total heat, and L= latent heat of steam in the main pipe; h= total heat due the pressure in the discharge side of the calorimeter, = 1146 6 at atmospheric pressure: K= specific heat of superheated steam; T= temperature of the throttled and superheated steam in the calorimeter; t = temperature due the pressure in the calorimeter,

= 212° at atmospheric pressure. Taking K at 0.48 and the pressure in the discharge side of the calorimeter as atmospheric pressure, the formula becomes

$$w = 100 \times \frac{H - 1146.6 - 0.48(T - 212^{\circ})}{L}$$

From this formula the following table is calculated:

MOISTURE IN STEAM-DETERMINATIONS BY THROTTLING CALORIMETER.

Super-					Ga	uge-p	ressu	res.			-	
	5	10	20	30	40	50	60	70	75	80	85	90
Degree of heatin $T = 21$				Per	Cent o	of Mo	isture	in St	eam.			
0° 10° 20° 30° 40° 50° 60° 70°	0.51	0 90 0.39	1.54 1.02 .51 .00	2.06 1.54 1.02 .50	2.50 1.97 1.45 .92 .39	2.90 2.36 1.83 1.30 .77 .24	3.24 2.71 2.17 1.64 1.10 .57	3.56 3.02 2.48 1.94 1.40 .87	3.71 3.17 2.63 2.09 1.55 1.01 .47	3.86 3.32 2.77 2.23 1.69 1.15 .60	3.99 3.45 2.90 2.35 1.80 1.26 .72 .17	4.13 3.58 3.03 2.49 1.94 1.40 .85
Dif.p.deg	.0503	.0507	.0515	.0521	.0526	.0531	.0535	.0539	.0541	.0542	.0544	.0546
uper-					Ga	uge-r	ressu	res.				
Degree of Superheating $T = 212^{\circ}$ .	100	110	120	130	140	150	160	170	180	190	200	250
Degra				Per	Cent	of Mo	isture	in S	team.			
0° 10° 20° 30° 40° 50° 60° 70° 80° 90° 110°	4.39 3.84 3.29 2.74 2.19 1.64 1.09 .55 .00	4.63 4.08 3.52 2.97 2.42 1.87 1.32 .77 .22	4.85 4.29 3.74 3.18 2.63 2.08 1.52 .97 .42	5.08 4.52 3.96 3.41 2.85 2.29 1.74 1.18 .63 .07	5 29 4.78 4.17 3.61 3.05 2.49 1.98 1.38 .82 .26	5.49 4.93 4.87 3.80 3.24 2.68 2.12 1.56 1.00 .44	5.68 5.12 4.56 3.99 3.43 2.87 2.30 1.74 1.18 .61	5.87 5.30 4.74 4.17 8.61 8.04 2.48 1.91 1.34 .78	6.05 5.48 4.91 4.34 3.78 3.21 2.64 2.07 1.50 .94	6.22 5.65 5.08 4.51 3.94 3.37 2.80 2.23 1.66 1.09 .52	6.39 5.82 5.25 4.67 4.10 3.53 2.96 2.38 1.81 1.24 .67	7.16 6.58 6.00 5.41 4.83 4.25 3.67 3.09 2.51 1.93 1.34 .76

**Separating Calorimeters.**—For percentages of moisture beyond the range of the throttling calorimeter the separating calorimeter is used, which is simply a steam separator on a small scale. An improved form of this calorimeter is described by Prof. Carpenter in *Power*. Feb. 1893.

which is simply a steam separator on a small scale. An improved form of this calorimeter is described by Prof. Carpenter in Power, Feb. 1893. For fuller information on various kinds of calorimeters, see papers by Prof. Peabody, Prof. Carpenter, end Mr. Barrus in Trans. A. S. M. E., vols. x, xi, xii, 1889 to 1891; Appendix to Report of Com. on Boiler Tests, A. S. M. E., vol. vi, 1884; Circular of Schaeffer & Budenberg, N. Y., "Calorimeters, Throttling and Separating," 1894.

Identification of Dry Steam by Appearance of a Jet.— Prof. Denton (Trans. A. S. M. E., vol. x.) found that jets of steam show unmistakable change of appearance to the eye when steam varies less than 1% from the condition of saturation either in the direction of wetness or super-

heating.

If a jet of steam flow from a boiler into the atmosphere under circumstances such that very little loss of heat occurs through radiation, etc., and the jet be transparent close to the orifice, or be even a grayish-white color, the steam may be assumed to be so nearly dry that no portable condensing calorimeter will be capable of measuring the amount of water in the steam. If the jet be strongly white, the amount of water may be roughly jindged up to about 2%, but beyond this a calorimeter only can determine the exact amount of moisture.

A common brass pet-cock may be used as an orifice, but it should, if possible, be set into the steam-drum of the boiler and never be placed further away from the latter than 4 feet, and then only when the intermediate reser-

voir or pipe is well covered.

Usual Amount of Moisture in Steam Escaping from a Boiler.—In the common forms of horizontal tubular land boilers and water-tube boilers with ample horizontal drums, and supplied with water free from substances likely to cause foaming, the moisture in the steam does not generally exceed 2% unless the boiler is overdriven or the waterlevel is carried too high.

### CHIMNEYS.

Chimney Draught Theory.—The commonly accepted theory of chimney draught, based on Peclet's and Rankine's hypotheses (see Rankine, S. E.), is discussed by Prof. De Volson Wood in Trans. A. S. M. E., vol. xi. Peclet represented the law of draught by the formula

$$h = \frac{u^2}{2q} \left( 1 + G + \frac{fl}{m} \right),$$

in which h is the "head," defined as such a height of hot gases as, if added to the column of gases in the chimney, would produce the same pressure at the furnace as a column of outside air, of the same area of base, and a height equal to that of the chimney;

u is the required velocity of gases in the chimney;

G a constant to represent the resistance to the passage of air through the coal;

I the length of the flues and chimney;

m the mean hydraulic depth or the area of a cross-section divided by the perimeter;

f a constant depending upon the nature of the surfaces over which the gases pass, whether smooth, or sooty and rough.

Rankine's formula (Steam Engine, p. 288), derived by giving certain values to the constants (so-called) in Peclet's formula, is

$$h = \frac{\frac{\tau_0}{\tau_2}\Big(0.0807\Big)}{\frac{\tau_0}{\tau_0}\Big(0.084\Big)}\,H - H = \Big(0.96\frac{\tau_1}{\tau_2} - 1\Big)H;$$

in which H = the height of the chimney in feet;

 $\tau_0 = 493^{\circ}$  F., absolute (temperature of melting ice);

 $\tau_1$  = absolute temperature of the gases in the chimney;  $\tau_2$  = absolute temperature of the external air.

Prof. Wood derives from this a still more complex formula which gives the height of chimney required for burning a given quantity of coal per second, and from it he calculates the following table, showing the height of chimney required to burn respectively 24, 20, and 16 lbs. of coal per square foot of grate per hour, for the several temperatures of the chimney gases given.

	Chimne	ey Gas.	Coal per sq. f	t. of grate p	er hour, lbs.
Outside Air. $\tau_2$	$ au_1$ Absolute.	Temp.	24	20	16
	Absolute.	Fahr.	He	ight $H$ , feet.	
520° absolute or 59° F.	700 800 1000 1100 1200 1400 1600 2000	239 339 539 639 739 939 1139 1589	250.9 172.4 149.1 148.8 152.0 159.9 168.8 206.5	157.6 115.8 100.0 98.9 100.9 105.7 111.0 132.2	67.8 55.7 48.7 48.2 49.1 51.2 53.5 63.0

Rankine's formula gives a maximum draught when  $\tau=2.1/12\tau_2$ , or 622° F., when the outside temperature is 60°. Prof. Wood says: "This result is not a fixed value, but departures from theory in practice do not affect the result largely. There is, then, in a properly constructed chimney, properly working, a temperature giving a maximum draught,\* and that temperature is not far from the value given by Rankine, although in special cases it may be 50° or 75° more or less."

All attempts to base a practical formula for chimneys upon the theoretical formula of Peclet and Rankine have failed on account of the impossibility of assigning correct values to the so-called "constants" G and f. (See Trans. A, S, M. E., xi. 984.)

Force or Intensity of Draught .- The force of the draught is equal to the difference between the weight of the column of hot gases inside of the chimney and the weight of a column of the external air of the same height. It is measured by a draught-gauge, usually a U-tube partly filled with water, one leg connected by a pipe to the interior of the flue, and the other open to

If D is the density of the air outside, d the density of the hot gas inside, in lbs. per cubic foot, h the height of the chimney in feet, and .192 the factor for converting pressure in lbs. per gq. ft. into inches of water column, then the formula for the force of draught expressed in inches of water is,

$$F = .192h(D - d)$$
.

The density varies with the absolute temperature (see Rankine).

$$d = \frac{\tau_0}{\tau_1} \, 0.084 \, ; \quad D = 0.0807 \, \frac{\tau_0}{\tau_2}, \label{eq:delta_total}$$

where  $\tau_0$  is the absolute temperature at 32° F.. = 493.,  $\tau_1$  the absolute temperature of the chimney gases and  $\tau_2$  that of the external air. Substituting these values the formula for force of draught becomes

$$F = .192h \Big( \frac{39.79}{\tau_2} \; - \; \frac{41.41}{\tau_1} \Big) = h \Big( \frac{7.64}{\tau_2} \; - \; \frac{7.95}{\tau_1} \Big).$$

To find the maximum intensity of draught for any given chimney, the heated column being 600° F, and the external air 60°, multiply the height above grate in feet by .00°3, and the product is the draught in inches of water.

# Height of Water Column Due to Unbalanced Pressure in Chimney 100 Feet High. (The Locomotive, 1884.)

					-		(2110 2				
Temp. in the Chimney.	Temperature of the External Air—Barometer, 14.7 lbs. per sq. in.										
Temp th Chimi	00	10°	20°	30°	40°	50°	600	700	80°	90°	100°
200	.458	.419	.384	.353	.321	.292	.263	.234	.209	.182	.157
220	.488	.453	.419	.388	.355	. 326	.298	. 269	.244	.217	.192
240	.520	.488	.451	.421	.388	. 359	.330	.301	.276	.250	.225
260	.555	.528	.484	.453	.420	.392	.363	.334	.309	.282	.257
280	.584	.549	.515	.482	.451	.422	.394	.365	.340	.313	.288
300	.611	.576	.541	.511	.478	.449	.420	.392	.367	.340	.315
320	.637	.603	.568	.538	. 505	.476	.447	.419	.394	.367	.342
340	.662	.638	.593	.563	.530	.501	.472	.443	.419	.392	.367
360	.687	.653	.618	.588	.555	.526	.497	.468	.444	. 417	.392
380	.710	.676	.641	.611	.578	.549	.520	.492	.467	.440	.415
400	.732	.697	.662	.632	.598	.570	.541	.513	.488	.461	.436
420	. 753	.718	.684	.653	.620	.591	.563	.534	.509	.482	.457
440	.774	.739	.705	.674	.641	.612	.584	.555	.530	.503	.478
460	.793	.758	.724	.694	.660	.632	.603	.574	. 549	.522	.497
480	.810	.776	.741	.710	.678	.649	. 620	.591	.566	.540	.515
500	. 829	.791	.760	.730	.697	.669	.639	.610	.586	.559	.534

<sup>\*</sup> Much confusion to students of the theory of chimneys has resulted from their understanding the words maximum draught to mean maximum intensity or pressure of draught, as measured by a draught-gauge. It here means maximim quantity or weight of gases passed up the chimney. The maximum intensity is found only with maximum temperature, but after the temperature reaches about 622° F. the density of the gas decreases more rapidly than its velocity increases, so that the weight is a maximum about 622° F., as shown by Rankine.—W. K.

For any other height of chimney than 100 ft, the height of water column is found by simple proportion, the height of water column being directly proportioned to the height of chimney.

The calculations have been made for a chimney 100 ft, high, with various temperatures outside and inside of the flue, and on the supposition that the temperature of the chimney is uniform from top to bottom. This is the basis on which all calculations respecting the draught-power of chimneys basis on which an Carcination's respecting the transpirepower. Crimmeys have been made by Rankhie and other writers, but it is very far from the truth in most cases. The difference will be shown by comparing the reading of the draught-gauge with the table given. In one case a chimney 132 ft. high showed a temperature at the base of 320°, and at the top of 230°. Box, in his "Treatise on Heat," gives the following table:

Draught Powers of Chimneys, etc., with the Internal Air at 552°, and THE EXTERNAL AIR AT 62°, AND WITH THE DAMPER NEARLY CLOSED.

nt of ey in t.	ght n ins. ter.	Theoretica in feet pe		nt of ey in t.	ght in ins. ter.	Theoretica in feet per	
Heigh Chimm fee	Drau Poweri of wa	Cold Air Entering.	Hot Air at Exit.	Heigh Chimm fee	Dran Power of wa	Cold Air Entering.	Hot Air at Exit.
10	.073	17.8	35.6	80	.585	50.6	101.2
20	.146	25.3	50.6	90	.657	53.7	107.4
30	.219	31.0	62.0	100	.730	56.5	113.0
40	.292	35.7	71.4	120	.876	62.0	124.0
50	.365	40.0	80.0	150	1.095	69.3	138.6
60	.438	43.8	87.6	175	1.277	74.3	149.6
70	.511	47.3	94.6	200	1.460	80.0	160.0

Rate of Combustion Due to Height of Chimney.— Trowbridge's "Heat and Heat Engines" gives the following table showing the heights of chimney for producing certain rates of combustion per sq. ft. of section of the chimney. It may be approximately true for anthractic in moderate and large sizes, but greater heights than are given in the table are needed to secure the given rates of combustion with small sizes of anthractic, and for bituminous coal smaller heights will suffice if the coal is reasonably free from ash-5% or less.

Heights in feet.	Lbs. of Coal Burned per Hour per Sq. Ft. of Section of Chimney.	Lbs. of Coal Burned per Sq. Ft. of Grate, the Ratio of Grate to Sec- tion of Chimney be- ing 8 to 1.	Heights in feet.	Lbs. of Coal Burned per Hour per Sq. Ft. of Section of Chimney.	Lbs. of Coal Burned per Sq. Ft. of Grate, the Ratio of Grate to Sec- tion of Chimney be- ing 8 to 1.
20	60	7.5	70	126	15.8
25	68	8.5	75 80 85 90	131	16.4
30 35 40	76	9.5	80	135	16.9
35	84	10.5	85	139	17.4
40	93	11.6	90	144	18.0
45	99	12.4	95	148	18.5
50	105	13.1	100	152	19 0
55	111	13.8	105	156	19.5
60	116	14.5	110	160	20 0
65	121	15.1			

Thurston's rule for rate of combustion effected by a given height of chimney (Trans. A. S. M. E., xi. 991) is: Subtract 1 from twice the square root of the height, and the result is the rate of combustion in pounds per square foot of grate per hour, for anthracite. Or rate =  $2\sqrt{h} - 1$ , in which h is the height in feet. This rule gives the following:

h = 5060 70 80 90 100 110 125 150  $2\sqrt{h} - 1 = 13.14$  14.49 15.73 16.89 17.97 19 19.97 21.36 23.49 25.45 27.28

The results agree closely with Trowbridge's table given above. In prac-

tice the high rates of combustion for high chimneys given by the formula are not generally obtained, for the reason that with high chimneys there are usually long horizontal flues, serving many boilers, and the friction and the interference of currents from the several boilers are apt to cause the intensity of draught in the branch flues leading to each boiler to be much less than that at the base of the chimney. The draught of each boiler is also usually restricted by a damper and by bends in the gas-passages. In a battery of several boilers connected to a chimney 150 ft. high, the author found a draught of 34-inch water-column at the boiler nearest the chimney, and only 14-inch at the boiler farthest away. The first boiler was wasting fuel from too high temperature of the chimney-gases, 900, having too large a grate-surface for the draught, and the last boiler was working below its

Tated capacity and with poor economy, on account of insufficient draught.

The effect of changing the length of the flue leading into a chimney 60 ft, high and 2 ft. 9 in. square is given in the following table, from Box on " Heat":

Length of Flue in feet.	Horse-power.	Length of Flue in feet.	Horse-power.
50	107.6	800	56.1
100	100.0	1.000	51.4
200	- 85,3	1,500	43.3
400	70.8	2,000	38.2
600	62.5	3,000	31.7

The temperature of the gases in this chimney was assumed to be 552° F... and that of the atmosphere 62°.

High Chimneys not Necessary.—Chimneys above 150 ft. in height are very costly, and their increased cost is rarely justified by increased efficiency. In recent practice it has become somewhat common to build two or more smaller chimneys instead of one large one. A notable example is the Speckels Sugar Refinery in Philadelphia, where five separate chimneys are used for one boiler-plant of 7500 H.P. The five chimneys are said to have cost several thousand dollars less than a single chimney of their combined capacity would have cost. Very tall chimneys have been characterized by one writer as "monuments to the folly of their builders."

Heights of Chimney required for Different Fuels.—The minimum height necessary varies with the fuel, wood requiring the least, then good bituminous coal, and fine sizes of anthracite the greatest. It also varies with the character of the boiler—the smaller and more circuitous the gas-passages the higher the stack required; also with the number of boilers, a single boiler requiring less height than several that discharge into a horizontal flue. No general rule can be given.

### SIZE OF CHIMNEYS.

The formula given below, and the table calculated therefrom for chimneys up to 96 in. diameter and 200 ft. high, were first published by the author in 1884 (Trans. A. S. M. E. vi, 81). They have met with much approval since that date by engineers who have used them, and have been frequently published in boiler-makers' catalogues and elsewhere. The table is now extended to cover chimneys up to 12 ft. diameter and 300 ft. high. The sizes corresponding to the given commercial horse-powers are believed to be ample for all cases in which the draught areas through the boiler-flues and connections are sufficient, say not less than 20% greater than the area of the chimney, and in which the draught between the boilers and chimney is not checked by long horizontal passages and right-angled bends.

Note that the figures in the table correspond to a coal consumption of 5 lbs. of coal per horse-power per hour. This liberal allowance is made to cover the contingencies of poor coal being used, and of the boilers being driven beyond their rated capacity. In large plants, with economical boilers and engines, good fuel and other favorable conditions, which will reduce the maximum rate of coal consumption at any one time to less than 5 lbs, per H. P. per hour, the figures in the table may be multiplied by the ratio of 5 to the maximum expected coal consumption per H.P. per hour. Thus, with conditions which make the maximum coal consumption only 2.5 lbs, per hour, the chimney 300 ft. high  $\times$  12 ft. diameter should be sufficient for 6155  $\times$  2 = 12,310 horse-power. The formula is based on the following data:

# Size of Chimneys for Steam-boilers.

	Equivalent	Square Chimney. Side of Square	VE + 4 inches.	31 22 23 45 45	8882	54 4 38 54 8 3 4 54 8 3 8	2204.2	8858	101	
(.		300 ft.					2002	2318 2654 3012 3393	3797 4223 5144 6155	
er nour		250 ft.					1565 1830	2116 2423 2750 3098	3466 3855 4696 5618	ble by 5.
rned pe		225 ft.					1253 1485 1736	2008 2298 2609 2939	3288 3657 4455 5331	n the ta
oal bu		200 ft.					981 1181 1400 1637	1893 2167 2459 2771	3100 3448 5026	enres in
ps. of c		175 ft.	Boiler.			595 748	918 1105 1310 1531	2027 2300 2592	2900 3226 3929 4701	ly the f
(Assuming 1 H. P. = 5 lbs. of coal burned per hour.)	imney.	150 ft.	Commercial Horse-power of Boller.			316 551 692	849 1023 1418	1639 1876 2130 2399	2685 2986 3637 4352	multin
; 1 H. F	Height of Chimney.	125 ft.	Torse-pc		204 245	288 288 288 288 288 288 288 288 288 288	776 934 1107 1294	1496 1712 1944 2090		himner
suming	Heigh	110 ft.	nercial I		156 191 229	27.1 365 47.2 593	728 876 1038 1214			algo of o
		100 ft.	Comm		119 1182 219	258 348 449 565	835			tr onlar on
$= 3.33(A - 0.6 \sqrt{A}) \sqrt{H}$		90 ft.		98	8255 825 835 835 835 835 835 835 835 835 835 83	245 330 427 536				6000
7 9.0		80 ft.		8438	107 163 196 196	311				1
¥ –		70 ft.		2488	5252	216				000
3.33	i .			88.48	2611					
- I-		50 ft. 60 ft.		88838	22					900
Formula, H.P.		Effective Area. $E = A - 0.6 \sqrt{A}.$	sq. ft.	1.47 2.08 2.78	8.54 6.47 6.57	7.76 10.44 13.51 16.98	20.83 25.08 34.76	40.19 46.01 52.23 58.83	65.83 73.88 74.18 75.73 77.73	zon
		Area A. sq. ft.		2.41 2.41 3.14 3.98	26.75 20.07 20.08	9.62 15.90 15.90	28.88.88 72.88.88 81.88	50.27 56.75 63.62	70.88 78.54 95.03	07.077
		Diam.		18	8888	3332	8228	8388	1881	1

For pounds of coal burned per hour for any given size of chimney, multiply the figures in the table by

1. The draught power of the chimney varies as the square root of the

height.

neight.

2. The retarding of the ascending gases by friction may be considered as equivalent to a diminution of the area of the chimney, or to a lining of the chimney by a layer of gas which has no velocity. The thickness of this lining is assumed to be 2 inches for all chimneys, or the diminution of area equal to the perimeter  $\times 2$  inches (neglecting the overlapping of the corners of the lining). Let D= diameter in feet, A= area, and E= effective area in square feet.

For square chimneys, 
$$E = D^2 - \frac{8D}{12} = A - \frac{2}{3}\sqrt{A}$$
.

For round chimeys, 
$$E = \frac{\pi}{4} \left( D^2 - \frac{8D}{12} \right) = A - 0.591 \sqrt{A}$$
.

For simplifying calculations, the coefficient of  $\sqrt{A}$  may be taken as 0.6 for both square and round chimneys, and the formula becomes

$$E = A - 0.6 \sqrt{A}.$$

3. The power varies directly as this effective area E.

4. A chimney should be proportioned so as to be capable of giving sufficient draught to cause the boiler to develop much more than its rated power, in case of emergencies, or to cause the combustion of 5 lbs, of fuel per rated

borse-power of boiler per hour.

5. The power of the chimney varying directly as the effective area, E, and as the square root of the height, H, the formula for horse-power of boiler for a given size of chimney will take the form H.P. =  $CE\sqrt{H}$ , in which C is a constant, the average value of which, obtained by plotting the results obtained from numerous examples in practice, the author finds to be 3.33.

The formula for horse-power then is

H.P. = 
$$3.33E\sqrt{H}$$
, or H.P. =  $3.33(A - .6\sqrt{A})\sqrt{H}$ .

If the horse-power of boiler is given, to find the size of chimney, the height being assumed,

$$E = \frac{0.3 \text{ H. P.}}{\sqrt{H}}; = A - 0.6 \sqrt{A}.$$

For round chimneys, diameter of chimney = diam. of E + 4''.

For square chimneys, side of chimney =  $\sqrt{E} + 4''$ . If effective area E is taken in square feet, the diameter in inches is d =13.54  $\sqrt{E}$  + 4", and the side of a square chimney in inches is  $s = 12 \sqrt{E}$  + 4". If horse-power is given and area assumed, the height  $H = \left(\frac{0.3 \text{ H. P}}{E}\right)^2$ .

In proportioning chimneys the height is generally first assumed, with due consideration to the heights of surrounding buildings or hills near to the proposed chimney, the length of horizontal flues, the character of coal to be used, etc., and then the diameter required for the assumed height and horse-power is calculated by the formula or taken from the table.

The Protection of Tall Chimney-shafts from Lightning, —C, Molyneux and J. M. Wood (Ludustries, March 28, 1890) recommend for tall chimneys the use of a coronal or heavy band at the top of the chimney, with copper points 1 ft. in height at intervals of 2 ft. throughout the circumwith copper points 1 ft. in height at intervals of 2 ft. throughout the circum-ference. The points should be gilded to prevent oxidation. The most ap-proved form of conductor is a copper tape about 34 in. by 14 in. thick, weighing 6 ozs. per ft. If iron is used it should weigh not less than 24 lbs. per ft. There must be no insulation, and the copper tape should be fastened to the chinney with holdrasts of the same material, to prevent voltaic action. An allowance for expansion and contraction should be made, say 1 in. in 40 ft. Slight bends in the tape, not too abrupt, answer the purpose. For an earth terminal a plate of metal at least 3 ft. sq. and 1/16 in. thick should be buried as deep as possible in a damp spot. The plate should be of the same metal as the conductor, to which it should be soldered. The best earth terminal is water, and when a deep well or other large body of water is at hand, the conductor should be carried down into it. Right-angled

bends in the conductor should be avoided. No bend in it should be over 30°,

### Some Tall Brick Chimneys.

		Diam.	Outs Diam	siue		y by the nor's nula.
	Height.	Internal	Base.	Top.	н. Р.	Pounds Coal per hour.
1. Hallsbrückner Hütte, Sax.	460	15.7′	33'	16′	13,221	66,105
2. Townsend's, Glasgow	454 435	13′ 6′′	32 40		9,795	48,975
Eng 5. Fall River Iron Co., Boston	367½ 350	13′ 2′′ 11	33′10′′ 30	21	8,245 5,558	41,225 27,790
6. Clark Thread Co., Newark, N. J.	335	11	28′ 6′′	14	5,435	27,175
7. Merrimac Mills, Low'l, Mass 8. Washington Mills, Law-		12			5,980	29,900
9. Amoskeag Mills, Manches-	250	10			3,839	19,195
ter, N. H		10			3,839	19,195
Providence, R. I 11. Lower Pacific Mills, Law-		14			7,515	37,575
rence, Mass 12. Passaic Print Works, Pas-	214	8			2,248	11,240
saic, N. J	200 150	9  50'' × 120''		each	2,771	13,855

Notes on the Above Chimneys.—1. This chimney is situated near Freiberg, on the right bank of the hulde, at an elevation of 219 feet above that of the foundry works, so that its total height above the sea will be 71134. feet. The works are situated on the bank of the river, and the furnace-gases are conveyed across the river to the chimney on a bridge, through a pipe 3227 feet in length. It is built throughout of brick, and will cost about \$40,000.—Mfr. and Bldr.

2. Owing to the fact that it was struck by lightning, and somewhat damaged, as a precautionary measure a copper extension subsequently was

added to it, making its entire height 488 feet.

1, 2, 3, and 4 were built of these great heights to remove deleterious gases from the neighborhood, as well as for draught for boilers.

gases from the neighborhood, as wen as for draught for bonets.

5. The structure rests on a solid granite foundation, 55 × 30 feet, and
16 feet deep. In its construction there were used 1,700,000 bricks, 2000 tons
of stone, 2000 barrels of mortar, 1000 loads of sand, 1000 barrels of Portland
cement, and the estimated cost is \$40,000. It is arranged for two flues, 9 feet 6 inches by 6 feet, connecting with 40 boilers, which are to be run in connection with four triple-expansion engines of 1350 horse-power each.

connection with four triple-expansion engines of 1350 horse-power each, 6. It has a uniform batter of 2.85 inches to every 10 feet, Designed for 21 boilers of 200 H. P. each. It is surmounted by a cast-iron coping which weighs six tons, and is composed of thirty-two sections, which are bolted together by inside flanges, so as to present a smooth exterior. The foundation is in concrete, composed of crushed limestone 6 parts, sand 3 parts, and Portland cement 1 part. It is 40 feet square and 5 feet deep, Two qualities of brick were used; the outer portions were of the first quality North River, and the backing up was of good quality New Jersey brick. Every twenty feet in vertical measurement an iron ring, 4 inches wide and 34 to 14 inch thick, placed edgewise, was built into the walls about 8 inches from the outer circle. As the chimney starts from the base it is double. The outer wall is 5 feet 2 inches in thickness, and inside of this is a second wall 20 inches thick and snaced off about. ness, and inside of this is a second wall 20 inches thick and spaced off about 20 inches from main wall. From the interior surface of the main wall eight buttresses are carried, nearly touching this inner or main flue wall in order to keep it in line should it tend to sag. The interior wall, starting with the thickness described, is gradually reduced until a height of about 90 feet is reached, when it is diminished to 8 inches. At 165 feet it ceases.

and the rest of the chimney is without lining. The total weight of the chimney and foundation is 5000 tons. It was completed in September, 1888.

Connected to 12 boilers, with 1200 square feet of grate-surface. Draught-Degauge 1 9/16 inches.

8. Connected to 8 boilers, 6' 8" diameter × 18 feet. Grate-surface 448 square feet.

9. Connected to 64 Manning vertical boilers, total grate surface 1810 sq. ft.

Designed to burn 18,000 lbs. anthracite per hour.

esigned to burn 15,000 108; animache per 15011.

10. Designed for 12,000 H.P. of engines; (compound condensing).

11. Grate-surface 431 square feet; H.P. of boilers (Galloway) about 2500.

13. Eight boilers (water-tube) each 450 H.P.; 12 engines, each 300 H.P. Plant designed for 36,000 incandescent lights. For the first 60 feet the exterior wall is 28 inches thick, then 24 inches for 20 feet, 20 inches for 30 feet, 16 inches for 20 feet, and 12 inches for 20 feet. The interior wall is 9 inches thick of fire-brick for 50 feet, and then 8 inches thick of red brick for the next 30 feet. Illustrated in from Age, January 2, 1890.

A number of the above chimneys are illustrated in Power, Dec., 1890. Chimney at Knoxville, Tenn., illustrated in Eng'g News, Nov. 2, 1898. 6 feet diameter, 120 feet high, double wall:

height 20 feet, 30 feet, 30 feet, 40 feet; thickness 21½ in., 17 in., 13 in., 8½ in.; height 85 ft., 25 ft., 29 ft., 21 ft.; Exterior wall, height Interior wall, height thickness 131/4 in., 81/4 in., 4 in., 0.

Exterior diameter, 15' 6" at bottom; batter, 7/16 inch in 12 inches from bottom to 8 feet from top. Interior diameter of inside wall, 6 feet uniform to top of interior wall. Space between walls, 16 inches at bottom, diminishing to 0 at top of interior wall. The interior wall is of red brick except a lining

of 4 inches of fire-brick for 20 feet from bottom.

Stability of Chimneys.—Chimneys must be designed to resist the maximum force of the wind in the locality in which they are built, (see Weak Chimneys, below). A general rule for diameter of base, of brick chimneys, approved by many years of practice in England and the United States, is to make the diameter of the base one tenth of the height. If the States, is to make the diameter of the base one tenth of the height. It he chimney is square or rectangular, make the diameter of the inscribed circle of the base one tenth of the height. The "batter" or taper of a chimney should be from 1/16 to ½ inch to the foot on each side. The brickwork should be one brick (8 or 9 inches) thick for the first 25 feet from the top, increasing ½ brick (4 or 4½ inches) for each 25 feet from the top downwards. If the inside diameter exceed 5 feet, the top length should be 1½ bricks; and if under 3 feet, it may be 1½ brick for ten feet.

(From The Locomotive, 1884 and 1886.) For chimneys of four feet in diameter exceed 5 feet, the top length should be 1½ bricks; and is the feet.

eter and one hundred feet high, and upwards, the best form is circular, with a straight batter on the outside. A circular chimney of this size, in addition to being cheaper than any other form, is lighter, stronger, and looks much

better and more shapely

Chimneys of any considerable height are not built up of uniform thickness from top to bottom, nor with a uniformly varying thickness of wall, but the wall, heaviest of course at the base, is reduced by a series of steps.

Where practicable the load on a chimney foundation should not exceed two

tons per square foot in compact sand, gravel, or loam. Where a solid rock-bottom is available for foundation, the load may be greatly increased. If the rock is sloping, all unsound portions should be removed, and the face dressed to a series of horizontal steps, so that there shall be no tendency to

slide after the structure is finished

All boiler-chimneys of any considerable size should consist of an outer stack of sufficient strength to give stability to the structure, and an inner stack or core independent of the outer one. This core is by many engineers extended up to a height of but 50 or 60 feet from the base of the chimney, but the better practice is to run it up the whole height of the chimney; it may be stopped off, say, a couple feet below the top, and the outer shell contracted to the area of the core, but the better way is to run it up to about 8 or 12 inches of the top and not contract the outer shell. But under no circumstances should the core at its upper end be built into or connected with the outer stack. This has been done in several instances by bricklayers, and the result has been the expansion of the inner core which lifted the top of the outer stack squarely up and cracked the brickwork.

For a height of 100 feet we would make the outer shell in three steps, the first 20 feet high, 16 inches thick, the second 30 feet high, 12 inches thick, the third 50 feet high and 8 inches thick. These are the minimum thicknesses admissible for chimneys of this height, and the batter should be not less than 1 in 36 to give stability. The core should also be built in three steps nan 11 no to give stability. The core should also be built in three steps each of which may be about one third the height of the chinner, the lowest 12 inches, the middle 8 inches, and the upper step 4 inches thick. This will insure a good sound core. The top of a chimney may be protected by a castiron cap; or perhaps a cheaper and equally good plan is to lay the ornamental part in some good cement, and plaster the top with the same material.

material.

Weak Chimneys,—James B. Francis, in a report to the Lawrence Mfg. Co. in 1873 (Eng'g News, Aug. 28, 1880), gives some calculations concerning the probable effects of wind on that company's chimney as then constructed. Its outer shell is octagonal. The inner shell is cylindrical, with an air-space between it and the outer shell; the two shells not being bonded together, except at the openings at the base, but with projections in the brickwork, at intervals of about 20 ft, in height, to afford lateral support by contact of the two shells. The principal dimensions of the chimney are as follows :

Diameter of the inscribed circle of the octagon near the ground, 15 Diameter of the inscribed circle of the octagon near the top... 10 ft. 11/2 in. Thickness of the outer shell near the base, 6 bricks, or. 23\(\frac{2}{3}\) in.
Thickness of the outer shell near the top, 3 bricks, or. 11\(\frac{2}{3}\) in Thickness of the inner shell near the base, 4 bricks, or. 15
Thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thickness of the inner shell near the top, 1 brick, or. 3\(\frac{2}{3}\) in thi

One tenth of the height for the diameter of the base is the rule commonly adopted. The diameter of the inscribed circle of the base of the Lawrence Manufacturing Company's chimney being 15 ft., it is evidently much less than is usual in a chimney of that height.

Soon after the chimney was built, and before the mortar had hardened, it was found that the top had swayed over about 29 in. toward the east. This was evidently due to a strong westerly wind which occurred at that time. It was soon brought back to the perpendicular by sawing into some of the

joints, and other means.

The stability of the chimney to resist the force of the wind depends mainly on the weight of its outer shell, and the width of its base. The cohesion of the mortar may add considerably to its strength; but it is too uncertain to be relied upon. The inner shell will add a little to the stability, but it may be cracked by the heat, and its beneficial effect, if any, is too uncertain to be taken into account.

The effect of the joint action of the vertical pressure due to the weight of the chimney, and the horizontal pressure due to the force of the wind is to shift the centre of pressure at the base of the chimney, from the axis toward one side, the extent of the shifting depending on the relative magnitude of the two forces. If the centre of pressure it brought too near the side of the chimney, it will crush the brickwork on that side, and the chimney will fall. A live depart through the centre of pressure. ney will fall. A line drawn through the centre of pressure, perpendicular to the direction of the wind, must leave an area of brickwork between it and the side of the chimney, sufficient to support half the weight of the chimney; the other half of the weight being supported by the brickwork on the windward side of the line.

Different experimenters on the strength of brickwork give very different Different experimenters on the strength of Drickwork give very different results. Kirkaldy found the weights which caused several kinds of bricks, laid in hydraulic lime mortar and in Roman and Portland cements, to fail slightly, to vary from 19 to 60 tons (of 2000 lbs.) per sq. ft. If we take in this case 25 tons per sq. ft., as the weight that would cause it to begin to fail, we shall not err greatly. To support half the weight of the outer shell of the chimney, or \$25 tons, at this rate, requires an area of 12.88 sq. ft. of brick-work. From these data and the drawings of the chimney, Mr. Francis calculates that the area of 12.88 sq. ft. is contained in a portion of the chimney extending 2.428 ft. from one of its octagonal sides, and that the limit to which the centre of pressure may be shifted is therefore 5.072 ft. from the axis. If shifted beyond this, he says, on the assumption of the strength

of the brickwork, it will crush and the chimney will fall.

Calculating that the wind-pressure can affect only the upper 141 ft. of the chimney, the lower 70 ft. being protected by buildings, he calculates that a wind-pressure of 44.02 lbs. per sq. ft. would blow the chimney down.

Rankine, in a paper printed in the transactions of the Institution of Engi-

neers, in Scotland, for 1867-68, says: "It had previously been ascertained by observation of the success and failure of actual chimneys, and especially by observation of the success and tailure of actual chimneys, and especially of those which respectively stood and fell during the violent storms of 1856, that, in order that a round chimney may be sufficiently stable, its weight should be such that a pressure of wind, of about 55 lbs, per sq. ft, of a plane surface, directly facing the wind, or 27% lbs, per sq. ft, of the plane projection of a cylindrical surface, shall not cause the resultant pressure at any bed\_joint to deviate from the axis of the chimney by more than one quarter of the outside diameter at that joint,"

According to Rankine's rule, the Lawrence Mfg. Co,'s chimney is adapted to a maximum pressure of wind on a plane acting on the whole height of 18.80 lbs. per sq. ft., or of a pressure of 21.70 lbs. per sq. ft. acting on the uppermost 141 ft. of the chimney.

Steel Chimneys are largely coming into use, especially for tall chimneys of iron-works, from 150 to 300 feet in height. The advantages claimed are: greater strength and safety; smaller space required; smaller cost, by 30 to 50 per cent, as compared with brick chimneys; avoidance of infiltration of air and consequent checking of the draught, common in brick chimneys. They are usually made cylindrical in shape, with a wide curved flar for 10 to 25 feet at the bottom. A heavy cast-iron base-plate is provided, to which the cleimary is riveted, and the plate is secured to a massive founda-tion by holding-down bolts. No guys are used. F. W. Gordon, of the Phile Engineering Works, gives the following method of calculating their resistance to wind pressure (Power, Oct. 1893):

In tests by Sir William Fairbairn we find four experiments to determine

the strength of thin hollow tubes. In the table will be found their elements, with their breaking strain. These tubes were placed upon hollow blocks, and the weights suspended at the centre from a block fitted to the inside of

the tube.

	Clear Span, ft. in.	Thick- ness Iron, in.	Outside Diame- ter, in.	Sectional Area, in.	Breaking Weight, Ibs.	Breaking W't, lbs., by Clarke's Formula, Constant 1.2.
I.	17	.037	12	1.3901	2,704	2,627
II.	15 71/2	.113	12.4	4.3669	11,440	9,184
III.	23 5	.0631	17.68	3.487	6,400	7,802
IV.	23 5	.119	18.18	6.74	14,240	13,910

Edwin Clarke has formulated a rule from experiments conducted by him during his investigations into the use of iron and steel for hollow tube bridges, which is as follows:

Center break-  $\frac{1}{2}$  Area of material in sq.in.  $\times$  Mean depth in in.  $\times$  Constant ing load, in tons. Clear span in feet.

When the constant used is 1.2, the calculation for the tubes experimented upon by Mr. Fairbairn are given in the last column of the table. D. K. Clark's "Rules, Tables, and Data," page 513, gives a rule for hollow tubes as follows:  $W = 3.14D^2TS + L$ . W = breaking weight in pounds in centre; <math>D = extreme diameter in inches; T = thickness in inches; L = length be-

tween supports in inches; S = ultimate tensile strength in pounds per sq. in.

Baking S, the strength of a square inch of a riveted joint, at 35,000 lbs.

Per, sq. in., this rule figures as follows for the different examples experimented upon by Mr. Fairbairn: I, 2870; II, 10,190; III, 17709; IV, 15,230.

This shows a close approximation to the breaking weight obtained by

experiments and that derived from Edwin Clarke's and D. K. Clark's rules. We therefore assume that this system of calculation is practically correct, and that it is eminently safe when a large factor of safety is provided, and from the fact that a chimney may be standing for many years without receiving anything like the strain taken as the basis of the calculation, viz., fifty pounds per square foot. Wind pressure at fifty pounds per square foot may be assumed to be travelling in a horizontal direction, and be of the same velocity from the top to the bottom of the stack. This is the extreme assumption. If, however, the chimney is round, its effective area would be only half of its diameter plane. We assume that the entire force may be concentrated in the centre of the height of the section of the chimney under consideration.

Taking as an example a 125-foot iron chimney at Poughkeepsie, N. Y., the Taking as an example a 125-foot iron chimney at Poughkeepsie, N. Y., une average diameter of which is 90 inches, the effective surface in square feet upon which the force of the wind may play will therefore be 7½ times 125 divided by 2, which multiplied by 50 gives a total wind force of 23,437 pounds. The resistance of the chimney to breaking across the top of the foundation would be 3-14  $\times$  168° (that is, diameter of base)  $\times$  25  $\times$  35,00-1750  $\times$  41  $\times$  41  $\times$  42  $\times$  55  $\times$  35,00-10  $\times$  45  $\times$  45  $\times$  50  $\times$  50 1750×4) = 258,486, or 10.6 times the entire force of the wind. We multiply the half height above the joint in inches, 750, by 4, because the chimney is considered a fixed beam with a load suspended on one end. In calculating considered a fixed beam with a load suspended on one end. In calculating its strength half way up, we have a beam of the same character. It is a fixed beam at a line half way up the chimney, where it is 90 inches in diameter and .187 inch thick. Taking the diametrical section above this line, and the force as concentrated in the centre of it, or half way up from the point under consideration, its breaking strength is:  $3.14 \times 90^2 \times .187 \times 35,000 \rightarrow (381 \times 4) = 109,230$ ; and the force of the wind to tear it apart through its

+ (881 × 4) = 109/320; and the lorde of the wind it the art a spate through its cross-section, 74 × 63/4 × 50 + 2 = 11,852, or a little more than one tenth of the strength of the stack.

The Babcock & Wilcox Co.'s book "Steam" illustrates a steel chimney at the works of the Maryland Steel Co., Sparrow's Point, Md. It is \$25 ft. in height above the base, with internal brick lining 13' 9' uniform inside diameter. The shell is 25 ft, diam, at the base, tapering in a curve to 17 ft. 25 ft. above the base, thence tapering almost imperceptibly to 14 % of at the top. The upper 40 feet is of ½-inch plates, the next four sections of 40 ft. each are respectively 9/32, 5/16, 11/32, and ½-inch.

### Sizes of Foundations for Steel Chimneys.

(Selected from circular of Phila, Engineering Works,)

### HALF-LINED CHIMNEYS.

Diameter, clear, feet	3	4	5	6	7	91	11
Height, feet	100	100	150	150	150	150	150
Least diameter foundation	15'9"	16'4"	20'4'	21'10"	22'7''	23'8"	24'8'1
Least depth foundation	6'	6'	9'	8′	9′	10'	10'
Height, feet		125	200	200	250	275	300
Least diameter foundation		18'5"	23'8"	25'	29'8''	33'6"	36'
Least depth foundation		7'	10'	10'	12'	12'	14'

### Weight of Sheet-iron Smoke-stacks per Foot. (Porter Mfg. Co.)

Diam., inches.	Thick- ness W. G.		Diam., inches.	Thick- ness W. G.	Weight per ft.	Diam. inches.	Thick- ness W. G.	Weight per ft.
10 12 14 16	No. 16	7.20 8.66 9.58 11.68	26 28 30 10	No. 16 " No. 14	17.50 18.75 20.00 9.40	20 22 24 26	No. 14	18.33 20.00 21.66 23.33
20 22 24	66 66 60	13.75 15.00 16.25	12 14 16	"	11.11 13.69 15.00	28 30	"	25.00 26.66

## Sheet-iron Chimneys. (Columbus Machine Co.)

Diameter Chimney, inches.	Length Chimney, feet.	Thick- ness Iron, B. W. G.	Weight,	Diameter Chimney, inches.	Length Chimney, feet.	Thick- ness Iron, B. W. G	Weight, lbs.
10 15 20 22 24 26 28	20 20 20 20 20 40 40 40	No. 16 " 16 " 16 " 16 " 16 " 16 " 16 " 16 "	160 240 320 350 760 826 900	30 32 34 36 38 40	40 40 40 40 40 40 40	No. 15 15 14 14 14 12 12	960 1,020 1,170 1,240 1,800 1,890

### THE STEAM-ENGINE

Expansion of Steam. Isothermal and Adiabatic .- According to Mariotte's law, the volume of a perfect gas, the temperature being

 $\frac{1}{2}$ ; pv = a constant.kept constant, varies inversely as its pressure, or p &

The curve constructed from this formula is called the isothermal curve, or curve of equal temperatures, and is a common or rectangular hyperbola. The relation of the pressure and volume of saturated steam, as deduced from Regnault's exp-riments, and as given in Steam tables, is approximately, according to Rankine (S. E., p. 403), for pressures not exceeding 120

 $\frac{1}{\sqrt{12}}$ , or  $p \propto v^{-\frac{17}{16}}$ , or  $pv^{-\frac{17}{16}} = pv^{-\frac{1.0625}{16025}} = a$  constant. Zeuner has

found that the exponent 1.0646 gives a closer approximation.

When steam expands in a closed cylinder, as in an engine, according to Rankine (S. E., p. 385), the approximate law of the expansion is p

 $p \propto v^{-\frac{1}{2}}$ , or  $pv^{-1.111} = a$  constant. The curve constructed from this formula is called the adiabatic curve, or curve of no transmission of heat. Peabody (Therm., p. 112) says: "It is probable that this equation was obtained by comparing the expansion lines on a large number of indicatoridagrams, ... There does not appear to be any good reason for using an exponential equation in this connection, . . . and the action of a lagged steamengine cylinder is far from being adiabatic. . . . For general purposes the hyperbola is the best curve for comparison with the expansion curve of an indicator-card. . . ." Wolff and Denton, Trans. A. S. M. E., ii. 175, say: "From a number of cards examined from a variety of steam-engines in current use, we find that the actual expansion line varies between the 10/9 adiabatic curve and the Mariotte curve."

Prof. Thurston (A. S. M. E, ii. 203), says he doubts if the exponent ever becomes the same in any two engines, or even in the same engines at dif-ferent times of the day and under varying conditions of the day.

Expansion of Steam according to Mariotte's Law and to the Adiabatic Law. (Trans. A. S. M. E., ii. 156.)—Mariotte's law:  $pv = p_1v_1$ ; values calculated from formula  $\frac{1}{p_1} = \frac{1}{R}(1 + \text{hyp log } R)$ , in which  $R=v_2+v_1,\ p_1=$  absolute initial pressure,  $P_m=$  absolute mean pressure,  $v_1=$  initial volume of steam incylinder at pressure  $p_1, v_2=$  final volume of steam at final pressure. Adiabatic law:  $pv^{V_0}=p_1v_1^{V_0}$ ; values calculated from formula  $\frac{P_m}{p_1}=10R^{-1}-9R^{-\frac{V_0}{2}}$ .

	$p_1$								
Ratio of Expan- sion R.	Ratio of Mean to Initial Pressure.		Ratio of Expan-		f Mean nitial sure.	Ratio of Expan-	Ratio of Mean to Initial Pressure.		
	Mar.	Adiab.	sion R.	Mar.	Adiab.	sion R.	Mar.	Adiab.	
1.00	1.000	1.000	3.7	.624	.600	6.	.465	.438	
1.25	.978	.976	3.8	.614	.590	6.25	.453	.425	
1.50	.937	.981	3.9	.605	.580	6.5	.442	.413	
1.75	.891	.881	4.	.597	.571	6.75	.431	.403	
2.	.847	.834	4.1	.588	.562	7.	.421	.393	
2.2	.813	.798	4.2	.580	.554	7.25	.411	.383	
2.4	.781	.765	4.3	.572	.546	7.5	.402	.374	
2.5	.766	.748	4.4	.564	.538	7.75	.393	.365	
2.6	.752	.733	4.5	.556	.530	8.	.385	.357	
- 2.8	.725	.704	4.6	.549	.523	8.25	.377	.349	
3.	.700	.678	4.7	.542	.516	8.5	.369	.342	
3.1	.688	.666	4.8	.535	.509	8.75	.362	.335	
3.2	.676	.654	4.9	.528	.502	9.	.355	.328	
3.3	.665	.642	5.05	.522	.495	9.25	.349	.321	
3.4	.654	.630	5 2	.506	.479	9.5	.342	.315	
3.5	.644	.620	5.5	.492	.464	9.75	.336	.309	
3.6	634	610	5.75	478	450	10	990	303	

Mean Pressure of Expanded Steam.—For calculations of engines it is generally assumed that steam expands according to Mariotte's law, the curve of the expansion line being a hyperbola. The mean pressure, measured above vacuum, is then obtained from the formula

$$P_m = p_1 \frac{1 + \text{hyp log } R}{R}$$

in which  $P_m$  is the absolute mean pressure,  $p_1$  the absolute initial pressure taken as uniform up to the point of cut-off, and R the ratio of expansion. If l = length of stroke to the cut-off, L = total stroke,

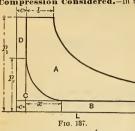
$$P_m = \frac{p_1 l + p_1 l \operatorname{hyp} \log \frac{L}{l}}{L}; \quad \text{and if } R = \frac{L}{l}, \quad P_m = p_1 \frac{1 + \operatorname{hyp} \log R}{R}.$$

Mean and Terminal Absolute Pressures,—Mariotte's Law.—The values in the following table are based on Mariotte's law, except those in the last column, which give the mean pressure of superheated steam, which, according to Rankine, expands in a cylinder according to the law  $p \propto v = \frac{16}{5}$ . These latter values are calculated from the formula  $\frac{P_m}{p_1} = \frac{17 - 16R - \frac{1}{16}}{p_1}$ .  $R - \frac{1}{16}$  may be found by extracting the square root of  $\frac{1}{R}$  four times. From the mean absolute pressures given deduct the mean back

pressure (absolute) to obtain the mean effective pressure.

Rate of Expan- sion.	Cut- off.	Ratio of Mean to Initial Pressure.	Ratio of Mean to Terminal Pressure.	Ratio of Terminal to Mean Pressure.	Ratio of Initial to Mean Pressure.	Ratio of Mean to Initial Dry Steam,
30	0.033	0.1467	4.40	0.227	6.82	0.186
28	0.036	0.1547	4.33	0.231	6.46	
26	0.038	0.1638	4.26	0.285	6.11	
24	0.042	0.1741	4.18	0.239	5.75	
22	0.045	0.1860	4.09	0.244	5.38	
20	0.050	0.1998	4.00	0.250	5.00	
18	0.055	0.2161	3.89	0.256	4.68	0.254
16	0.062	0.2358	3.77	0.265	4.24	
15	0.066	0.2472	3.71	0.269	4.05	
14	0.071	0.2599	3.64	0.275	3.85	
13.33	0.075	0.2690	3.59	0.279	3.72	
13	0.077	0.2742	3.56	0.280	3.65	0.314
12	0.083	0.2904	3.48	0.287	3.44	
11	0.091	0.3089	3.40	0.294	3.24	
10	0.100	0.3303	3.30	0.303	3.03	
9	0.111	0.3552	3.20	0.312	2.81	
8	0.125	0.3849	3.08	0.321	2.60	
6.66 6.00 5.71 5.00 4.44	0.143 0.150 0.166 0.175 0.200 0.225	0.4210 0.4347 0.4653 0.4807 0.5218 0.5608	2.95 2.90 2.79 2.74 2.61 2.50	0.339 0.345 0.360 0.364 0.383 0.400	2.37 2.30 2.15 2.08 1.92 1.78	0.417
4.00 3.63 3.33 3.00 2.86 2.66	0.250 0.275 0.300 0.333 0.350 0.375	0.5965 0.6308 0.6615 0.6995 0.7171 0.7440	2.39 2.29 2.20 2.10 2.05 1.98	0.419 0.437 0.454 0.476 0.488 0.505	1.68 1.58 1.51 1.43 1.39 1.34	0.582 0.648 0.707
2.50 2.22 2.00 1.82 1.66 1.60	0.400 0.450 0.500 0.550 0.600 0.625	0.7664 0.8095 0.8465 0.8786 0.9066 0.9187	1.91 1.80 1.69 1.60 1.51 1.47	0.528 0.556 0.591 0.626 0.662 0.660	1.31 1.24 1.18 1.14 1.10 1.09	0.756 0.800 0.840 8.874 0.900
1.54	0.650	0.9292	1.43	0.699	1.07	0.926
1.48	0.675	0.9405	1.39	0.718	1.06	

Calculation of Mean Effective Pressure, Clearance and Compression Considered.—In the above tables no account is taken



of clearance, which in actual standard and an actual standard and the mean pressure; nor of compression and back-pressure, which diminish the mean effective pressure. In the following calculation these elements are considered.

L = length of stroke, l = length before cut-off, x = length of compression part of stroke, c = clearance,  $p_1$  = initial pressure,  $p_b$  = back pressure,  $p_c$  = pressure of clearance steam at end of compression. All pressures are absolute, that is, measured from a perfect vacuum.

Fig. 187.  $\text{Area of ABCD} = p_1(l+c)\Big(1+\text{hyp}\log\frac{L+c}{l+c}\Big);$   $\text{B} = p_b(L-x);$ 

 $C = p_c c \left( 1 + \text{hyp log } \frac{x+c}{c} \right) = p_b (x+c) \left( 1 + \text{hyp log } \frac{x+c}{c} \right);$   $D = (p_1 - p_c) c = p_1 c - p_b (x+c).$ 

Area of A = ABCD - (B + C + D)

 $= p_1(l+c)\left(1 + \text{hyp log } \frac{L+c}{l+c}\right)$ 

$$\begin{split} &-\left[p_b(L-x)\,+\,p_b(x+c)\Big(1+\operatorname{hyp}\,\log\frac{x+c}{c}\Big)+p_1c\,-\,p_b(x+c)\right]\\ &=p_1(l+c)\Big(1+\operatorname{hyp}\,\log\frac{L+c}{l+c}\Big) \end{split}$$

 $-p_b \Big[ (L-x) + (x+c) \text{ hyp log } \frac{x+c}{c} \Big] - p_1 c.$ 

Mean effective pressure =  $\frac{\text{area of A}}{L}$ 

Example.—Let  $L=1,\ l=0.25,\ x=0.25,\ c=0.1,\ p_1=60$  lbs.,  $p_b=2$  lbs. Area A =  $60(.25+.1)\Big(1+{\rm hyp}\log\frac{1.1}{.25}\Big)$ 

 $-2\left[(1-.25)+.35 \text{ hyp log } \frac{.35}{.1}\right]-60\times.1$ 

 $= 21(1 + 1.145) - 2[.75 + 35 \times 1.253] - 6$ = 45.045 - 2.377 - 6 = 36.668 = mean effective pressure.

The actual indicator-diagram generally shows a mean pressure considerably less than that due to the initial pressure and the rate of expansion. The causes of loss of pressure are: 1. Friction in the stop-valves and steampipes. 2. Friction or wire-drawing of the steam during admission and cut-off, due chiefly to defective valve-gear and contracted steam-passages. 3. Liquefaction during expansion. 4. Exhausting before the engine has completed its stroke. 5. Compression due to early closure of exhaust. 6. Friction in the exhaust-ports, passages, and pipes.

Completed its stroke. O Complession due to Confice the Confice of the Confice of

the diagram and increase the mean pressure.

If the theoretical mean pressure be calculated from the initial pressure and the rate of expansion on the supposition that the expansion curve fol-

lows Mariotte's law, pv = a constant, and the necessary corrections are made for clearance and compression, the expected mean pressure in practice may be found by multiplying the calculated results by the factor in the following table, according to Seaton.

Part	iculars of Engine.	ractor.	
cut-off valve, cylinder		0.94	
dinary valves, cylinde	ng large ports, etc., and good or- ers jacketed	0.9 to 0.92	
in general practice, a	nd unjacketed	0.8 to 0.85	
der; cylinders jackete	ed, and with large ports, etc th ordinary slide-valves, cylinders	0.9 to 0.92	
jacketed, and good p	orts, etc	0.8 to 0.85	
service, with early c jackets and expansio	ut-off in both cylinders, without on-valves	0.7 to 0.8	

If no correction be made for clearance and compression, and the engine is in accordance with general modern practice, the theoretical mean pressure may be multiplied by 0.96, and the product by the proper factor in the table, to obtain the expected mean pressure.

### Given the Initial Pressure and the Average Pressure, to Find the Ratio of Expansion and the Period of Admission.

P= initial absolute pressure in lbs. per sq. in.; p= average total pressure during stroke in lbs. per sq. in.; L= length of stroke in inches; l= period of admission measured from beginning of stroke;

c = clearance in inches;

$$R = \text{actual ratio of expansion} = \frac{L+c}{l+c}$$
. . . . . . . . . (1)  $p = \frac{P(1+\text{hyp log }R)}{R}$ .

To find average pressure p, taking account of clearance,

$$p = \frac{P(l+c) + P(l+c) \text{ hyp log } R - Pc}{L}, \dots$$
 (2)

whence

$$pL + Pc = P(l+c)(1 + \text{hyp log } R);$$

hyp log 
$$R = \frac{pL + Pc}{Pl + Pc} - 1 = \frac{\frac{p}{P}L + c}{l + c} - 1$$
. (3)

Given p and P, to find R and l (by trial and error).-There being two unknown quantities R and l, assume one of them, viz., the period of admission l, substitute it in equation (3) and solve for R. Substitute this value of R in the formula (1), or  $l = \frac{L+c}{R} - c$ , obtained from formula (1), and find l. If

the result is greated than the assumed value of l, then the assumed value of the period of admission is too long; if less, the assumed value is too short. Assume a new value of l, substitute it in formula (3) as before, and continue by this method of trial and error till the required values of R and l are obtained.

Example.—P = 70, p = 42.78, L = 60'', c = 3'', to find l. Assume l = 21 in

hyp log 
$$R = \frac{\frac{p}{P}L + c}{l + c} - 1 = \frac{\frac{42.78}{70} \times 60 + 3}{21 + 3} - 1 = 1.653 - 1 = .653;$$

hyp log R = .653, whence R = 1.92,

$$l = \frac{L+c}{R} - c = \frac{63}{192} - 3 = 29.8,$$

which is greater than the assumed value, 21 inches.

Now assume l = 15 inches:

hyp log 
$$R = \frac{\frac{42.78}{70} \times 60 + 3}{15 + 3} - 1 = 1.204$$
, whence  $R = 3.5$ ;

$$l=\frac{L+c}{R}-c=\frac{63}{3.5}-3=18-3=15$$
 inches, the value assumed.

Therefore R = 3.5, and l = 15 inches,

Period of Admission Required for a Given Actual Ratio of Expansion:

$$l = \frac{L+c}{R} - c$$
, in inches . . . . . . . . . (4)

In percentage of stroke, 
$$l = \frac{100 + \text{p.ct. clearance}}{R} - \text{p. ct. clearance}$$
. (5)

Pressure at any other Point of the Expansion.—Let  $L_1 = \text{length of stroke}$ up to the given point.

### WORK OF STEAM IN A SINGLE CYLINDER.

To facilitate calculations of steem expanded in cylinders the table on the next page is abridged from Clark on the Steam-engine. The actual ratios of expansion, column I, range from 1.0 to 8.0, for which the hyperbolic logarithms are given in column 2. The 3d column contains the periods of admission relative to the actual ratios of expansion, as percenges of the stroke, excellent the stroke of expansion, as percenges of the stroke of the stroke of the stroke of expansion, as percenges of the stroke of expansion, column 1. The 6th column, are such as would be arrived at by the continued expansion of the whole of the stram to the end of the stroke, the initial pressure being equal to 1. They are the reciprocals of the ratios of expansion, column 1. The 6th column contains the relative total performances of equal weights of steam worked with the several actual ratios of expansion; the total performance, when steam is admitted for the whole of the stroke, without expansion, being equal to 1. They are obtained by dividing the figures in column 4 by those in column 5.

The pressures have been calculated on the supposition that the pressure steam, admitted for the whole of the stroke. The relative branch is column 5 to the order of the stroke of the effect of compressive action.

The calculations have been made for periods of admission ranging from 100%, or the whole of the stroke, to 6.4%, or 1/16 of the stroke. And though, nominally, the expansion is 16 times in the last instance, it is actually only 8 times, as given in the first column. The great difference between the nominal and the actual ratios of expansion is caused by the clearance, which is equal to 7% of the stroke, and causes the nominal volume of steam admitted, namely, 6.4%, to be sugmented t To facilitate calculations of steam expanded in cylinders the table on the

not at half-stroke.

### Expansive Working of Steam—Actual Ratios of Expansion, with the Relative Periods of Admission, Pressures, and Performance.

Steam-pressure 100 lbs. absolute. Clearance at each end of the cylinder 7% of the stroke.

(SINGLE CYLINDER.)

1	2	3	4	5	6	7	8	9
Actual Ratio of Expansion, or No. of Volumes to which the Initial Volume is Expanded.	Hyperbolic Logarithm of Actual Ratio of Expansion.	Period of Admission or Cut-off, 7% Clearance.	Average Total Press- ure, Initial Pressure = 1.	Total Final Press- ure, Initial Pressure = 1.	Ratio of Total Performance of Equal Weights of Steam. (Col. 4 + Col 5.)	Actual Work done by 1 lb. of 100 lbs. Steam. Ftlbs.	Quantity of Steam Consumed per H.P. of Actual Work done per hour	Net Capacity of Cyl- inder per lb. of 100 lbs. Steam ad- mitted in 1 stroke. Cubic feet.
1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	.0000 .0953 .1698 .2070 .2624 .3293 .3716 .4700 .5595 .6314 .8755 .9745 1.163 1.209 1.281 1.385 1.163 1.4705 1.169 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.504 1.505 1.609 1.705 1.705 1.705 1.705	100 90.3 83.3 80 75.3 70 66.8 62.5 59.9 54.1 50 46.5 40.5 4	1.000 1.996 .986 .989 .953 .942 .925 .913 .883 .866 .786 .766 .726 .632 .632 .637 .648 .589 .569 .569 .559 .488 .476 .457 .438 .432	1.000 909 847 813 769 649 625 551 5 439 417 377 377 375 328 228 268 268 268 268 268 268 278 288 268 268 268 278 288 288 288 288 288 288 288 288 28	1.000 1.086 1.164 1.206 1.261 1.325 1.365 1.425 1.461 1.546 1.616 1.672 1.793 2.088 2.088 2.088 2.129	58,273 63,850 67,886 70,246 73,513 77,242 79,555 85,125 90,115 94,200 112,290 116,885 121,386 124,066 127,450 138,139 140,920 142,180 142,180 142,180 143,730 144,186	14.05 13.92 13.78	4.05 4.478 4.78 4.98 5.26 5.63 5.87 6.27 7.08 9.72 10.72 11.74 12.95 13.56 14.57 15.87 10.72 11.74 12.95 13.56 14.57 15.87 16.23 17.00 18.21 19.23 19.71 19.23 19.71 19.72 19.73 19.
6.2 6.3 6.6 7 7.3 7.6 7.8 8	1.825 1.841 1.887 1.946 1.988 2.028 2.054 2.079	10.3 10 9.2 8.3 7.7 7.1 6.7 6.4	.419 .413 .398 .381 .369 .357 .348 .342	.169 .161 .159 .152 .143 .137 .132 .128 .125	2.597 2.619 2.664 2.693 2.711 2.719 2.736	150,630 151,370 152,595 155,200 156,960 157,975 158,414 159,433	13.08 12.98 12.75 12.61 12.53 12.50	25.09 25.49 26.71 28.33 29.54 30.76 31.57 32.38

ASSUMPTIONS OF THE TABLE.—That the initial pressure is uniform; that the expansion is complete to the end of the stroke; that the pressure in expansion varies inversely as the volume; that there is no back-pressure of exhaust or of compression, and that clearance is % of the stroke at each end of the cylinder. No allowance has been made for loss of steam by cylinder-condensation or leakage.

 Volume of 1 lb. of steam of 100 lbs. pressure per sq. in., or 14,400
 4.33 cu. ft.

 Ibs. per sq. ft.
 4.33 cu. ft.

 Product of initial pressure and volume
 62,352 ft.-lbs,

 62,352 ft.-lbs,
 62,352 ft.-lbs,

Though a uniform clearance of 7% at each end of the stroke has been assumed as an average proportion for the purpose of compiling the table, stee clearance of cylinders with ordinary slides varies considerably—say from 5½ to 10%. (With Corliss engines it is sometimes as low as 2%,) With the clearance, 7%, that has been assumed, the table gives approximate results sufficient for most practical purposes, and more trustworthy than results deduced by calculations based on simple tables of hyperbolic logarithms, where clearance is neglected.

Weight of steam of 100 lbs. total initial pressure admitted for one stroke, per cubic foot of net capacity of the cylinder, in decimals of a pound =

reciprocal of figures in column 9.

Total actual work done by steam of 100 lbs. total initial pressure in one stroke per cubic foot of net capacity of cylinder, in foot-pounds = figures in column 7 + figures in column 9.

Rull 1: To find the net capacity of cylinder for a given weight of steam

admitted for one stroke, and a given actual ratio of expansion. (Column 9 of table.)-Multiply the volume of 1 lb. of steam of the given pressure by the given weight in pounds, and by the actual ratio of expansion. Multiply the product by 100, and divide by 100 plus the percentage of clearance. The quotient is the net capacity of the cylinder.

RULE 2: To find the net capacity of cylinder for the performance of a given amount of total actual work in one stroke, with a given initial presswe and actual ratio of expansion—Divide the given work by the total actual work done by 1 lb. of steam of the same pressure, and with the same actual ratio of expansion; the quotient is the weight of steam necessary to

do the given work, for which the net capacity is found by Rule 1 preceding, Norz.—1. Conversely, the weight of steam admitted per cubic foot of net capacity for one stroke is the reciprocal of the cylinder-capacity per pound

of steam, as obtained by Rule 1.

2. The total actual work done per cubic foot of net capacity for one stroke is the reciprocal of the cylinder-capacity per foot-pound of work done, as obtained by Rule 2.

3. The total actual work done per square inch of piston per foot of the stroke is 1/144th part of the work done per cubic foot

4. The resistance of back pressure of exhaust and of compression are to be added to the net work required to be done, to find the total actual work.

APPENDIX TO ABOVE TABLE-MULTIPLIERS FOR NET CYLINDER-CAPACITY, AND TOTAL ACTUAL WORK DONE.

(For steam of other pressures than 100 lbs, per square inch.)

	75.74	11		75 141	11	
	Muiti	pliers.		Multipliers.		
Total Pressures per square inch.	For Col. 7. Total Work by 1 lb. of Steam.	For Col. 9. Capacity of Cylinder.	Total Pressures per square inch.	For Col. 7. Total Work by 1 lb. of Steam.		
lbs.			lbs.			
65	.975	1.50	100	1.000	1.00	
70	.981	1.40	110	1.009	.917	
75 80 85	.986	1.31	120	1.011	.843	
80	.988	1.24	130	1.015	.781	
85	.991	1.17	140	1.022	.730	
90	.995	1.11	150	1.025	.683	
95	.998	1.05	160	1.031	.644	

The figures in the second column of this table are derived by multiplying the total pressure per square foot of any given steam by the volume in cubic feet of 1 lo. of such steam, and dividing the product by 62,352, which is the product in foot-pounds for steam of 100 lbs, pressure. The quotient is the multiplier for the given pressure.

The figures in the third column are the quotients of the figures in the

second column divided by the ratio of the pressure of the given steam to 100

lbs

Measures for Comparing the Duty of Engines .- Capacity is measured in horse powers, expressed by the initials, H.P.: 1 H.P. = 33,000 ft.-lbs. per minute, = 550 ft.-lbs. per second, = 1,980,000 ft.-lbs. per hour. 1 ft.-lb. = a pressure of 1 lb. exerted through a space of 1 ft. Economy is measured, 1, in pounds of coal per horse-power per hour; 2, in pounds of steam per horse-power per hour. The second of these measures is the more accurate and scientific, since the engine uses steam and not coal, and it is

independent of the economy of the boller.

In gas-engine tests the common measure is the number of cubic feet of gas (measured at atmospheric pressure) per horse-power, but as all gas is not of the same quality, it is necessary for comparison of tests to give the analysis of the gas. When the gas for one engine is made in one gas-producer, then the number of pounds of coal used in the producer per hour per horse-power of the engine is the proper measure of economy.

Economy, or duty of an engine, is also measure or economy.

Economy, or duty of an engine, is also measured in the number of footpounds of work done per pound of fuel. As I horse-power is equal to 1,980,
00 ft.-lbs, of work in an hour, a duty of I lb. of coal per H.P. per hour
would be equal to 1,980,000 ft.-lbs, per lb. of fuel; 2 lbs, per H.P. per hour
equals 990,000 ft.-lbs, per lb. of fuel, etc.

The duty of pumping-engines is commonly expressed by the number of
foot-pounds of work done per 100 lbs, of coal.

When the duty of a pumping-engine is thus given, the equivalent number

of pounds of fuel consumed per horse-power per hour is found by dividing 198 by the number of millions of foot-pounds of duty. Thus a pumpingengine giving a duty of 99 millions is equivalent to 198/99 = 2 lbs. of fuel per

horse-power per hour.

Efficiency Measured in Thermal Units per Minute.—
Some writers express the efficiency of an engine in terms of the number of thermal units used by the engine per minute for each indicated horse-power,

instead of by the number of pounds of steam used per hour.

The heat chargeable to an engine per pound of steam is the difference between the total heat in a pound of steam at the boiler-pressure and that in a pound of the feed-water entering the boiler. In the case of condensing engines, suppose we have a temperature in the hot-well of 101° F., corresponding to a vacuum of 28 in. of mercury, or an absolute pressure of 1 lb. per sq. in. above a perfect vacuum: we may feed the water into the boiler at that temperature. In the case of a non-condensing-engine, by using a portion of the exhaust steam in a good feed-water heater, at a pressure a trifle above the atmosphere (due to the resistance of the exhaust passages through the heater), we may obtain feed-water at 212°. One pound of steam used by the engine then would be equivalent to thermal units as follows:

Pressure of steam by gauge: 100 125 150 175 200

Total heat in steam above 32°: 1172.8 1179.6 1185.0 1189.5 1193.5 1197.0 1200.2

Subtracting 69.1 and 180.9 heat-units, respectively, the heat above 32° in feed water of 101° and 212° F., we have-

Heat given by boiler: Feed at 101°.... 1103.7 1110.5 1115.9 1120.41124.4 1127.9 1131.1 998.7 1016.1 Feed at 212°..... 991.9 1004.1 1008.6 1012.6 1019.3

Thermal units per minute used by an engine for each pound of steam used per indicated horse-power per hour:

Feed at 101°.. ... 18.40 18.51 18.60 18.67 15.74 13.80 18.85 Feed at 2120 ..... 16.88 16.53 16.65 16.74 16.81 16.94 16.99

Ex.MPLES.—A triple-expansion engine, condensing, with steam at 175 bs., gauge and vacuum 28 in., uses 13 bs. of water per LH.P. per hour, and a high-speed non-condensing engine, with steam at 100 bs. gauge, uses 30

lbs. How many thermal units per minute does each consume?

Ans.  $-13 \times 18.80 = 244.4$ , and  $30 \times 16.74 = 502.2$  thermal units per minute. A perfect engine converting all the heat-energy of the steam into work would require 33,000 ft.-lbs. + 778 = 42.4164 thermal units per minute per indicated horse-power. This figure, 42.4164, therefore, divided by the number of thermal units per minute per I.H.P. consumed by an engine, gives its efficiency as compared with an ideally perfect engine. In the examples above, 42.4164 divided by 244.4 and by 502.2 gives 17.85% and 8.45% efficiency, respectively

Total Work Done by One Pound of Steam Expanded in a Single Cylinder. (Column 7 of table)—If 1 pound of water ue converted into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure into steam of atmospheric pressure = 2116.8 lbs. per sq. ft., if occured into steam of atmospheric pressure into steam of atmosph pies a volume equal to 26.36 cu. ft. The work done is equal to 2116.8 lbs.

 $\times$  26.36 ft. = 55,788 ft.·lbs. The heat equivalent of this work is (55,788  $\pm$  778  $\pm$  )71,7 units. This is the work of 1 lb. of steam of one atmosphere acting on a piston without expansion.

on a piston without expansion.

The gross work thus done on a piston by 1 lb. of steam generated at total pressures varying from 15 lbs. to 100 lbs. per sq., in varies in round numbers from 55,000 to 62,000 ft.-lbs., equivalent to from 72 to 80 units of heat.

This work of 1 lb. of steam without expansion is reduced by elearance according to the proportion it bears to the net capacity of the cylinder. If the clearance be 7% of the stroke, the work of a given weight of steam without expansion, admitted for the whole of the stroke, is reduced in the ratio of 107 to 100.

Having determined by this ratio the quantity of work of 1 lb, of steam without expansion, as reduced by clearance, the work of the same weight of steam for various ratios of expansion may be found by multiplying it by the relative merformance of equal weights of steam given in the fith column of the table

performance of equal weights of steam, given in the 6th column of the table. **Quantity of Steam Consumed per Horse-power of Total Work per Hour.** (Column 8 of table.)—The measure of a horse-power is the performance of 33,000 ft.-lbs. per hour. This work, divided by the work of 1 lb of steam, gives the weight of steam required per horse-power per hour. For example, the total actual work done in the cylinder by 1 lb. of 100 lbs. steam, without expansion and with % of clearance, is 58,273 ft.-lbs.; and 1,980,000 1.

7% of clearance, is 58,273 ft.-10s.; and 58,273 = 34 lbs. of steam, is the weight of steam consumed for the total work done in the cylinder per horse-power per hour. For any shorter period of admission with expansion the weight of steam per horse-power is less, as the total work of 1 lb. of steam is more, and may be found by dividing 1,980,000 ft.-lbs. by the respective total work done; or by dividing 34 lbs. by the ratio of performance, column 6 in the table.

Real Ratios of Expansion with Clearances from 0 to 7%.

	Lette	1015 0				2010			210,			. // .
Per Cent Clear ce.					Point	s of C	ut-off.					
Per	.10	.125	.20	.25	.30	.333	.375	.40	.50	.60	.625	.70
.0 .01 .0125 .0150 .0175			5 4.809 4.764 4.720 4.677	4 3.884 3.875 3.830 3.803	3.333 3.258 3.24 3.222 3.204	3 2.944 2.930 2.916 2.902	2.667 2.623 2.612 2.602 2.592	2.5 2.463 2.454 2.445 2.436	2 1.983 1.975 1.970 1.966	1.66 1.65 1.65	$\frac{1.59}{1.58}$	1.42 1.42 1.42
.02 .0225 .0250 .0275	8.2	6.833	4.635 4.595 4.555 4.516	3.777 3.752 3.727 3.702	3.187 3.170 3.153 3.137	2.889 2.876 2.863 2.850	2.582 2.574 2.562 2.552	2.420	1.961 1.956 1.952 1.947	1.64	1.58	1.41
.03 .0325 .0350 .0375	7.666 7.545	6.555 6.468 6.390	4.417 4.440 4.404 4.484	3.678 3.654 3.631 3.608	3.121 3.105 3.089 3.074	2.837 2.824 2.812 2.800	2 543 2.533 2.524 2.515	2.395 2.387 2.379 2.371	1.943 1.938 1.934 1.930	1.63 1.63 1.63	1.57 1.57 1.57	1.41 1.41 1.41
.04 .0425 .0450 .0475	7.206 7.102	6.229 6.147 6.082	4.333 4.298 4.256 4.232	3.58 3.564 3.542 3.521	3.058 3.043 3.028 3.014	2.788 2.776 2.764 2.752	2.506 2.497 2.488 2.479	2.340	1.921 1.917 1.913	1.62 1.62 1.62	1.56 1.56 1.56	1.40 1.40 1.40
.05 .0525 .0550 .0575	6.806 6.714	5.861 5.794	4.2 4.168 4.130 4.106	3.439	3 2 986 2.971 2.957	2.719 2.708	2.458 2.445	2.325 2.318 2.311	1.904 1.900 1.896	1.61 1.61 1.61	1.55 1.55 1.55	1.40 1.40 1.40
.06 .0625 .0650 .0675	6,454	5.666 5.605 5.545	4.047 4.045 3.990	3 407 3.380 3.362	2.944 2.931 2.917 2.904 2.892	2.686 2.675 2.665	2.428 2.420 2.412	2.297 2.290 2.283	1.888 1.884 1.881	1.60 1.60 1.60	1.54 1.34 1.54	1.39 1.39 1.39
.07	0.294	0.482	0.905	0.542	≈.೧9°	2.000	2.404	2.270	1.000	1.00	1.04	1.89

Relative Efficiency of 1 lb. of Steam with and without Clearance; back pressure and compression not considered.

$$\label{eq:meantotal} \text{Mean total pressure} = p = \frac{P(l+c) + P(l+c) \text{ hyp. log. } R - Pc}{L}.$$
 Let  $P=1;~L=100;~l=25;~c=7.$ 

$$p = \frac{32 + 32 \text{ hyp. log.} \frac{107}{32} = 7}{100} = \frac{32 + 32 \times 1,209 - 7}{100} = .637.$$

If the clearance be added to the stroke, so that clearance becomes zero, the same quantity of steam being used, admission l being then = l+c=32, and stroke L+c=107.

$$p_1 = \frac{32 + 32 \text{ hyp. log.} \frac{107}{32} - 0}{107} = \frac{32 + 32 \times 1.209}{107} = .707.$$

That is, if the clearance be reduced to 0, the amount of the clearance 7 being added to both the admission and the stroke, the same quantity of steam will do more work than when the clearance is 7 in the ratio 707:637. or 11% more

Back Pressure Considered.—If back pressure = .10 of P, this amount has to be subtracted from p and p, giving p = .53,  $p_1 = .60$ 7, the work of a given quantity of steam used without clearance being greater than when clearance is 7 per cent in the ratio of 607; 537, or 138 more. Effect of Compression.—By early closure of the exhaust, so that a

portion of the exhaust-steam is compressed into the clearance-space, much of the loss due to clearance may be avoided. If expansion is continued down to the back pressure, if the back pressure is uniform throughout the exhaust-stroke, and if compression begins at such point that the exhauststeam remaining in the cylinder is compressed to the initial pressure at the end of the back stroke, then the work of compression of the exhaust-steam equals the work done during expansion by the clearance-steam. The clearance-space being filled by the exhaust-steam thus compressed, no new steam is required to fill the clearance-space for the next forward stroke, and the work and efficiency of the steam used in the cylinder are just the same as if work and efficiency of the steam used in the cylinder are just the same as it there were no clearance and no compression. When, however, there is a drop in pressure from the final pressure of the expansion, or the terminal pressure, to the exhaust or back pressure (the usual case), the work of compression to the initial pressure is greater than the work done by the expansion of the clearance-steam, so that a loss of efficiency results. In this case a greater efficiency can be attained by inclosing for compression a less quantity of steam than that needed to fill the clearance-space with steam of quantity of steam than that needed to in the clearance-space with steam of the initial pressure. (See Clark, S. E., p. 399, et seq, ; also F. H. Ball, Trans. A. S. M. E., xiv. 1067.) It is shown by Clark that a somewhat greater efficiency is thus attained whether or not the pressure of the steam be carried down by expansion to the back exhaust-pressure. As a result of calculations to determine the most efficient periods of compression for various percentages of back pressure, and for various periods of admission, he gives the other than extract.

percentages of back pressure, and for various periods of admission, he gives the table on the next page: 
Clearance in Low and High-speed Engines. (Harris Tabor, Am. Mach., April 17, 1891.)—The construction of the high-speed engine is such, with its relatively short stroke, that the clearance must be much larger than in the releasing-valve type. The short-stroke oughe is, of necessity, an engine with large clearance, which is aggravated when a variable compression is a feature. Our clearance with the strong prover is obtainable from long stroke, and small clearance is a feature in its construction. In one case the clearance will vary from 8% to 12% of the histor-disobtainable from long stroke, and small dearance is a reature in its construc-tion. In one case the clearance will vary from 8% to 12% of the piston-dis-placement, and in the other from 2% to 3%. In the case of an engine with a clearance equalling 10% of the piston-displacement the waste room becomes enormous when considered in connection with an early cut-off. The system of compounding reduces the waste due to clearance in proportion as the steam is expanded to a lower pressure. The farther expansion is carried through a train of cylinders the greater will be the reduction of waste due to clearance. This is shown from the fact that the high-speed engine, expanding

steam much less than the Corliss, will show a greater gain when changed from simple to compound than its rival under similar conditions.

COMPRESSION OF STEAM IN THE CYLINDER.

Post Periods of Compression: Clearance 7 per cent.

	Dest 1	erious o	Compi	ession,	Clearan	e i pei c	seno.	
Cut-off in	Total Back Pressure, in percentages of the total initial pressure.							
Percent- ages of the	21/2	5	10	15	20	25	30	35
Stroke.	Periods of Compression, in parts of the stroke.							
10% 15 20 25 30 35 40 45	65% 58 52 47 42 39 36 33	57% 52 47 42 39 35 32 30	44% 40 37 34 32 29 27 25	32% 29 27 26 25 23 21 20	23% 22 21 20 19 18 17	17% 16 15 14 14	14% 13 13 13 12	12% 11 11 10
50 55 60 65 70 75	30 27 24 22 19 17	27 24 22 20 17 16	28 21 19 17 16 14	18 17 15 15 14 14	16 15 14 14 14 14 12	18 13 12 12 12 12	12 11 11 10 10 9	10 9 9 8 8 8

Notes to Table.-1. For periods of admission, or percentages of back pressure, other than those given, the periods of compression may be readily found by interpolation.

2. For any other clearance, the values of the tabulated periods of compression are to be altered in the ratio of 7 to the given percentage of clearance.

Cylinder-condensation may have considerable effect upon the best point of compression, but it has not yet (1893) been determined by experiment. (Trans. A. S. M. E., xiv. 1078.)

(Arans, A. S. M. E. XW. 1968) **Cylinder-condensation.**—Rankine, S. E., p. 421, says: Conduction of heat to and from the metal of the cylinder, or to and from liquid water contained in the cylinder, has the effect of lowering the pressure at the beginning and raising it at the end of the stroke, the lowering effect being on the whole greater than the raising effect. In some experiments the quantity of steam wasted through alternate liquefaction and evaporation in the cylinder has been found to be greater than the quantity which performed the work.

Percentage of Loss by Cylinder-condensation, taken at Cut-off. (From circular of the Ashcroft Mfg. Co. on the Tabor Cut-off. (Fr. Indicator, 1889.)

ge of ipleted off.	Percent. of for by t	of Feed-wate he Indicator	r accounted diagram.	Percent. of Feed-water Consumption due to Cylinder-condensat'n.			
Percenta Stroke con at Cut	Simple Engines.	Compound Engines, h.p. cyl.	Triple-ex- pansion Engines, h.p. cyl.	Simple Engines.	Compound Engines, h.p. cyl.	Triple-ex- pansion Engines, h.p. cyl.	
5	58			42			
10	66	74		34	26		
15	71	76	78	34 29	24	22	
20	74	78	80	26	22	20	
15 20 30	78	74 76 78 82	84	22	18	16	
40	82	85	87	18	15	13	
50	86	85 88	90	14	12	10	

Theoretical Compared with Actual Water-consumption, Single-cylinder Automatic Cut-off Engines. (From the catalogue of the Buckeye Engine Co.)-The following table has been prepared on the basis of the pressures that result in practice with a constant boller-pressure of 80 lbs. and different points of cut-off, with Buckeye engines and others with similar clearance. Fractions are omitted, except in the percentage column, as the degree of accuracy their use would seem to imply is not attained or aimed at.

Cut-off Part of Stroke.	Mean Effective Pressure.	Total Terminal Pressure.	Indicated Rate, lbs. Water, per I.H.P. per hour.	Assumed.		
				Act'l Rate.	Per ct. Loss.	
.10 .15 .20 .25	18	11	20	32	58	
.15	18 27 35 42 48 53 57 61	15 20	19	27	41 31.5	
,20	35	20	19	25	31.5	
.25	42	25	20	25	25	
.30	48	30 35 38	20	24	21.8	
.35	53	35	21 22	25	19	
.40	57	38	22	26	16.7	
.40 .45 .50	61	43	23	27	15	
.50	64	48	24	27	13.6	

It will be seen that while the best indicated economy is when the cut-off is about at .15 or .20 of the stroke, giving about 30 lbs. M.E.P., and a terminal 3 or 4 lbs. above atmosphere, when we come to add the percentages due to a constant amount of unindicated loss, as per sixth column, the most economical point of cut-off is found to be about 30 of the stroke, giving 48 lbs. M.E.P. and 30 lbs. terminal pressure. This showing agrees substantially with modern experience under automatic cut-off regulation.

Experiments on Cylinder-condensation.-Experiments by Major Thos. English (Eng'g, Oct. 7, 1887, p. 386) with an engine  $10 \times 14$  in., jacketed in the sides but not on the ends, indicate that the net initial condensation (or excess of condensation over re-evaporation) by the clearance surface varies directly as the initial density of the steam, and inversely as the square root of the number of revolutions per unit of time. The mean the square root of the number of revolutions per unit of time. The mean results gave for the net initial condensation by clearance-space per sq. ft. of surface at one rev. per second 6.06 thermal units in the engine when run non-condensing and 5.75 units when condensing.

G. R. Bodmer (Eng/g, March 4, 1892, p. 299) says; Within the ordinary limits of expansion desirable in one cylinder the expansion ratio has practically no influence on the amount of condensation per stroke, which for

simple engines can be expressed by the following formula for the weight of water condensed [per minute, probably; the original does not state]:

S(T-t)

 $(L_{\sqrt[3]{N^2}})$ , where T denotes the mean admission temperature, t the

mean exhaust temperature, S clearance-surface (square feet), N the number of revolutions per second, L latent heat of steam at the mean admission temperature, and C a constant for any given type of engine.

Mr. Bodmer found from experimental data that for high-pressure non-jacketed engines C = about 0.11, for condensing non-jacketed engines 0.085 to 0.033. The figures for jacketed engines apply to those jacketed in the usual way, and not at the ends.

C varies for different engines of the same class, but is practically constant for any given engine. For simple high-pressure non-jacketed engines it was found to range from 0.1 to 0.112.

Applying Mr. Bodmer's formula to the case of a Corliss non-jacketed noncondensing engine, 4-ft. stroke, 24 in. diam., 60 revs. per min., initial pressure 20 lbs, gauge, exhaust pressure 2 lbs, we have  $T-t=112^{\circ}$ , N=1, L=880, S=7 sq. ft.; and, taking C=.112 and W= lbs. water condensed per minute,  $W=\frac{.112\times112\times7}{1\times800}=.09$  lb. per minute, or 5.4 lbs. per hour. If

 $1 \times 880$ 

the steam used per I.H.P. per hour according to the diagram is 20 lbs., the actual water consumption is 25.4 lbs., corresponding to a cylinder condensation of 27%.

### INDICATOR-DIAGRAM OF A SINGLE-CYLINDER ENGINE.

**Definitions.**—The Atmospheric Line, AB, is a line drawn by the pencil of the indicator when the connections with the engine are closed and both sides of the piston are open to the atmosphere.

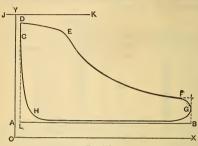


Fig. 138.

The Vacuum Line, OX, is a reference line usually drawn about 14 7/10

pounds by scale below the atmospheric line. The Clearance Line, OY, is a reference line drawn at a distance from the end of the diagram equal to the same per cent of its length as the clearance and waste room is of the piston-displacement.

The Line of Boiler-pressure, JK, is drawn parallel to the atmospheric line, and at a distance from it by scale equal to the boiler-pressure shown by the gauge.

The Admission Line, CD, shows the rise of pressure due to the admission

of steam to the cylinder by opening the steam-valve,

The Steam Line, DE, is drawn when the steam-valve is open and steam is being admitted to the cylinder.

The Point of Cut-off, E, is the point where the admission of steam is stopped by the closing of the valve. It is often difficult to determine the exact point at which the cut-off takes place. It is usually located where the outline of the diagram changes its curvature from convex to concave. The Expansion Curve, EF, shows the fall in pressure as the steam in the cylinder expands daine work.

cylinder expands doing work.

The Point of Release, F, shows when the exhaust-valve opens.

The Exhaust Line, FG, represents the change in pressure that takes place when the exhaust-valve opens.

The Back-pressure Line, GH, shows the pressure against which the piston acts during its return stroke.

The Point of Exhaust Closure, H, is the point where the exhaust-valve It cannot be located definitely, as the change in pressure is at first due to the gradual closing of the valve.

The Compression Curve, HC, shows the rise in pressure due to the compression of the steam remaining in the cylinder after the exhaust-valve has closed.

The Mean Height of the Diagram equals its area divided by its length. The Mean Effective Pressure is the mean net pressure urging the piston forward = the mean height × the scale of the indicator-spring.

To find the Mean Effective Pressure from the Diagram—Divide the length, LB, into a number, say 10, equal parts, setting off half a part at L, half a part at B, and nine other parts between; erect ordinates perpendicular to the atmospheric line at the points of division of LB, cutting the diagram; add together the lengths of these ordinates intercepted between the upper and lower lines of the diagram and divide by their number. This

gives the mean height, which multiplied by the scale of the indicator-spring gives the M.E.P. Or find the area by a planimeter, or other means (see Mensuration, p. 55), and divide by the length *LB* to obtain the mean height. *The Imitial Pressure* is the pressure acting on the piston at the beginning

of the stroke.

The Terminal Pressure is the pressure above the line of perfect vacuum that would exist at the end of the stroke if the steam had not been released earlier. It is found by continuing the expansion-curve to the end of the

### INDICATED HORSE-POWER OF ENGINES, SINGLE-

Indicated Horse-power I.H.P. =  $\frac{PLan}{33.000}$ ,

in which P = mean effective pressure in lbs. per sq. in.; L = length of stroke in feet; a = area of piston in square inches. For accuracy, one half of the sectional area of the piston-rod must be subtracted from the area of the piston if the rod passes through one head, or the whole area of the rod if it passes through both heads; n = No. of single strokes per min. =  $2 \times \text{No.}$  of revolutions.

I.H.P. = 
$$\frac{PaS}{33,000}$$
, in which  $S$  = piston speed in feet per minute.  
I.H.P. =  $\frac{FLd^2n}{\frac{d^2}{d^2}017} = \frac{Pd^2S}{\frac{d^2}{d^2}017} = .0000238PLd^2n = .0000238Pd^2S$ ,

in which d= diam, of cyl. in inches. (The figures 238 are exact, since 74+43=23.8 exactly.) If product of piston-speed x-mean effective pressure  $\pm 43.017$ , then the horse-power would equal the square of the

diameter in inches. diameter in inches. Handy Kule for Estimating the Horse-power of a Single-cylinder Engine. Square the diameter and divide by 2. This is correct whenever the product of the mean effective pressure and the piston-speed =  $\frac{1}{2}$  of  $\frac{4}{2}$ ,017, or, say,  $\frac{2}{1}$ ,000, viz., when M.E.P. =  $\frac{3}{2}$ 0 and  $\frac{5}{2}$  = 700; when M.E.P. =  $\frac{3}{2}$ 3 and  $\frac{5}{2}$ 500; These conditions correspond to those of ordinary practice with both Corliss engines and shaft-governor high-speed engines. Given Horse-power, Mean Effective Pressure, and Piston-speed, to find Size of Cylinder.—

Area = 
$$\frac{33,000 \times I.H.P.}{PLn}$$
. Diameter = 205  $\sqrt{\frac{I.H.P.}{PS}}$ . (Exact.)

Brake Horse-power is the actual horse-power of the engine as measured at the fly-wheel by a friction-brake or dynamometer. It is the

indicated horse-power minus the friction of the engine.

Table for Roughly Approximating the Horse-power of a Compound Engine from the Diameter of its Low-pressure Cylinder.—The indicated horse-power of an engine being

 $\frac{1}{42.017}$ , in which P = mean effective pressure per sq. in., s = piston-speed in42.017

42.017

42.017

42.017

42.017

42.017

42.017

43.03 - possonspeed in the per min., which is approximately the speed of modern stationary engines, and P=35 lbs., which is an approximately average figure for the M.E.P. of single-cylinder engines, and of compound engines referred to the low-pressure cylinder, then I.H.P. =  $\frac{1}{2}k^{2}t^{2}$ : hence the rough-and-ready rule for horse-power given above: Square the diameter in inches and divide by 2. This applies to triple and quadruple expansion engines as well as to single cylinder and compound. For most economical loading, the M.E.P. referred to the low-pressure cylinder of compound engines is usually not greater than that of simple engines; for the greater economy is obtained by a greater number of expansions of steam of higher pressures, and the greater the number of expansions for a given initial pressure the lower the mean effective pressure. The following table gives approximately the figures of mean total and effec-The following table gives approximately the figures of mean total and effective pressures for the different types of engines, together with the factor by which the square of the diameter is to be multiplied to obtain the horsepower at most economical loading, for a piston-speed of 600 ft, per minute,

Type of Engine.	Initial Absolute Steam- pressure. Number of Expansions.	Absolute Press., lbs. Ratio Mean Total to Initial Pressure. Mean Total	lbs. Total Back Pressure, Mean, lbs. Mean Effec- tive Pressure, lbs. Piston- speed, ft.	Horse- power = diam. <sup>2</sup> ×
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#### Non-condensing.

Single Cylinder.	100	5.	20	.522	52.2	15.5	36.7	600	.524
Compound	120	7.5	16	.402	48.2	15.5	32.7	44	.467
Triple		10.	16	.330	52.8	15.5	37 3	66	.533
			16					44	
Quadruple	200	12.5	16	.282	56.4	15.5	40.9	"	.584

### Condensing Engines.

For any other piston-speed than 600 ft. per min., multiply the figures in the last column by the ratio of the piston-speed to 600 ft.

Nominal Horse-power.—The term "nominal horse-power" originated in the time of Watt, and was used to express approximately the power of an engine as calculated from its diameter, estimating the mean pressure in the cylinder at 7 lbs. above the atmosphere. It has long been obsolete in America, and is nearly obsolete in England.

Horse-power Constant of a given Engline for a Fixed

Speed = product of its area of piston in square inches, length of stroke in feet, and number of single strokes per minute divided by 33,000, or 33,000

The product of the mean effective pressure as found by the diagram and this constant is the indicated horse-power.

Horse-power Constant of a given Engine for Varying Speeds = product of its area of piston and length of stroke divided by 33,000. This multiplied by the mean effective pressure and by the number of single strokes per minute is the indicated horse-power.

Horse-power Constant of any Engine of a given Diameter of Cylinder, whatever the length of stroke = area of piston + 33,000 = square of the diameter of piston in inches × .0000238. A table of constants derived from this formula is given below.

The constant multiplied by the piston-speed in feet per minute and by

the M.E.P. gives the I.H.P.

Errors of Indicators. - The most common error is that of the spring, which may vary from its normal rating; the error may be determined by proper testing apparatus and allowed for. But after making this correction even with the best work, the results are liable to variable errors which may amount to 2 or 3 per cent. See Barrus, Trans. A. S. M. E., v. 310; Denton, A. S. M. E., x. 329; David Smith, U. S. N., Proc. Engg Congress, 1893, Marine Division.

Indicator "Rigs," or Reducing-motions; Interpretation of Diagrams for Errors of Steam-distribution, etc. For these see circulars of manufacturers

of Indicators; also works on the Indicator.

Table of Engine Constants for Use in Figuring Horsepower .- "Horse-power constant" for cylinders from 1 inch to 60 inches in diameter, advancing by 8ths, for one foot of piston-speed per minute and one pound of M.E.P. Find the diameter of the cylinder in the column at the side. If the diameter contains no fraction the constant will be found in the column headed Even Inches. If the diameter is not in even inches, follow the line horizontally to the column corresponding to the required fraction, The constants multiplied by the piston-speed and by the M.E.P. give the horse-power.

Diameter		+ 16	+14	+ 3/8	+16	+ 5%	+ 34	+ 7/6
of	Even Inches.	+ 1/8 or	+1/4 or	or	+1/2 or	+ 5% or	+ 3/4 or .75.	+ 1/8 or
Cylinder.	inches.	.125.	.25.	.375.	.5.	.625.	.75.	.875.
1	.0000238	,0000301	.0000372	.0000450	.0000535	,0000628	.0000729	.0000837
1 2 3 4 5 6 7 8 9	.0000952	.0001074	.0001205	.0001342	.0001487	.0001640	.0001800	0001967
3	.0002142	.0002324	.0002514	.0002711	.0002915	.0003127	.0003347	.0003574
4	.0003808	.0004050 .0006251	.0004299 .0006560	0004554 0006876	.0004819	.0005091 .0007530	.0005370	.0005656
8	.0005950	.0008929	.0009397	.0009672	.0010055	.0010445	.0007869	.0008215
7	.0011662	.0012082	.0012510	.0012944	.0013387	.0013837	.0014295	.0014759
8	.0015232	.0015711	.0012510 .0016198	.0016693	.0017195	.0017705	.0018222	.0018746
9	.0019278	.0019817	.0020363	.0020916	.0021479	.0022048	.0022625	.0023209
10	$0023800 \\ 0028798$	.0024398	.0025004	.0025618	.0026239	.0026867	.0027502	.0028147
11 12 13 14	.0026196	.0029450	.0035714	.0036447	.0037187	.0032163 .0037934	.0038690	.0039452
18	.0040222	.0040999	.0041783	.0042576	.0043375	0044182	.0044997	.0045819
14	.0046648	.0047484	.0048328	.0049181	:0050039	.0050906	.0051780	.0052661
15	.0053550	.0054446	.0055349	.0056261	.0057179	.0058105	.0059039	.0059979
16	.0060928	.0061884	.0062847	.0063817	.0064795	.0065780	.0066774	.0067774
17	.0068782	.0069797	.0070819	0.0071850 $0.0080360$	.0072887 .0081452	0073932 $0082560$	.0074985	.0076044
19	.0085918			.0089343	.0090499	.0091663	.0092835	.0094013
20	.0095200	.0096393	.0097594	.0098803	.0100019	.0101243 .0111299	.0102474	.0103712
21	.0104958	.0106211	.0107472	.0108739	.0110015	.0111299	.0112589	.0113886
22	.0115192	.0116505	.0117825	.0119152	.0120487	.0121830	.0123179	.0124537
28	.0125902	.0127274	.0128654 .0139959	.0130040	.0131435 .0142859	.0132837 .0144321	.0134247	.0135664 .0147266
95	.0148750	.0150241	.0151739	.0153246	0154750	.0156280	.0157809	.0159345
26	.0160888		.0163997	.0165563	.0154759 .0167135	.0168716	.0170304	.0171899
27	.0173502	.0175112	.0176729	.0178355	.0179988	.0181627	.0183275	.0184929
28	.0186592	.0188262	.0189939	.0191624	.0193316	.0195015	.0196722	.0198436
16 17 18 19 20 21 22 25 26 27 28 29 30 31 32 33 34 35 36 37 38	.0200158 .0214200	.0201887	.0203624	.0205368 $.0219588$	.0221399	.0208879	.0210645	.0212418
30 31	.0228718	.0215988	.0232422	.0234285	.0236155	.0238033	.0225044	.0226877
32	.0243712	.0245619	.0247535	.0249457	.0251387	.0253325	.0255269	.0257222
33	.0259182	.0261149	.0263124	.0265106	.0267095	.0269092	.0271097	.0273109
34	.0275128	.0277155	.0279189	.0281231	.0283279	.0285356	.0287399	.0289471
35	.0291550	.0293636	.0295729	.0297831	.0299939	.0302056	.0304179	.0306309
30 27	.0308448	.0328027	.0312747	.0314908 .0332460	.0317075 .0334687	.0319251 .0336922	.0321434	.0323624
38	.0343672	.0345937	.0348209	.0350489	.0352775	0255070	.0357372	.0359681
39	.0361998	.0364322	.0366654	.0368993	0352775 0371339	0373694	.0376055	.0378424
40	.0380800	.0383184		.0387973	.0390379	0392793	.0395214	.0397642
41	.0400078	.0402521	.0404972	.0407430	.0409895	.0412368	.0414849	.0417337
42 43	.0419832	.0422335	.0424845 .0445194	.0427362 .0447771	.0429887 $.0450355$	.0432420	.0434959	.0437507 .0458154
44	.0460768	.0463389	.0466019	.0468655	.0471299	.0473951	.0476609	.0479276
45	.0481950	.0484631	.0487320	.0490016	.0492719	.0495430	.0498149	.0500875
45 46 47 48 49	.0503608	.0506349	.0509097	.0511853	.0514615	.0517386	.0520164	.0522949
47	.0525742	.0528542	.0531349	.0534165	.0536988	.0539818	.0542655	.0545499
48	.0548352 .0571438	.0551212 .0574357	.0554079 .0577284	.0556953 .0580218	.0559835 .0583159	0.0562725 0.0586109	.0565622	.0568526
50	.0595000	.0597979	.0600965	.0603959	.0606959	.0609969	.0612984	.0616007
51	.0619038	.0622076	.0625122	.0628175	.0632235	.0634304	.0637379	.0640462
52 53	.0643552	.0646649	.0649753	.0652867	.0655987	.0659115	.0662250 $.0687597$	.0665392
53	.0668542	.0671699	.0674864	.0678036	.0681215	.0684402	.0687597	.0690799
54	.0694008	.0697225 .0724226	.0700449 .0726510	.0703681	.0705293 $.0733099$	.0710166 .0736406	.0713419	.0716681 .0743039
55 56 57	.0719950	.0749704	.0753047	.0729801 .0756398	0759755	.0763120	.0766494	.0769874
57	.0773262	.0776657	.0780060	.0783476	.0786887	.0790312	.0793745	.0797185
58	.0800632	.0804087	.0807549	.0811019	.0814495	.0817980	.0821472	.0824971
59	.0828478	.0831992		.0839043	0842579	.0846123	.0849675	.0853234
60	.0856800	.0860374	.0863955	.0867543	.0871139	.0874743	.0878354	.0881973

# 

5						33,000	,				
Mathematics	Diam. of			Speed	of Pis	ton in	feet pe	r min	ite.		
4		100	940	300	400	450	500	550	600	650	750
446         .048         .115         .144         .192         .216         .24         .264         .288         .312         .36         5.5         .00         .144         .18         .24         .27         .30         .33         .36         .393         .45         .55         .66         .000         .2056         .256         .288         .324         .36         .496         .432         .468         .41         .513         .555         .56         .66         .66         .206         .256         .396         .409         .404         .512         .568         .614         .698         .555         .64         .60         .60         .655         .401         .584         .682         .614         .698         .80         .806         .966         .756         .87         .912         .402         .577         .770         .866         .966         .969         .735         .802         .869         .112         .936         .172         .413         .516         .688         .774         .866         .966         .966         .966         .969         .1032         .1118         .1298         .121         .118         .1292         .111         .191	-			-							
5		.048	.115		.192	.216		.264	.288	.312	.360
6	5	.06		.18	.04	.27	.30	. 33	.36	.39	.450
64\( 6\) 102\( 2\) 245\( 1.307\) 409\( 1.404\) 512\( 5.83\) 634\( 1.40\) 6.98\( 1.507\) 77\( 1.34\) 321\( 1.401\) 534\( 1.602\) 66\( 6.735\) 5.08\( 2.869\) 1.02\( 1.344\) 321\( 1.401\) 534\( 1.602\) 66\( 6.735\) 5.08\( 2.869\) 1.02\( 8.54\) 1.172\( 1.413\) 3.516\( 1.608\) 6.08\( 1.655\) 7.61\( 1.877\) 99\( 1.12\) 1.24\( 1.335\) 5.16\( 6.88\) 6.08\( 1.655\) 7.61\( 1.877\) 99\( 1.12\) 1.24\( 1.35\) 6.68\( 8.774\) 86\( 6.946\) 1.082\( 1.172\) 1.118\( 1.299\) 1.12\( 1.462\) 5.577\( 1.777\) 7.70\( 1.866\) 66\( 9.63\) 1.05\( 9.118\) 1.125\( 1.144\) 9\( 1.25\) 2.15\( 1.515\) 6.44\( 1.859\) 9.66\( 1.074\) 1.181\( 1.128\) 1.395\( 1.151\) 1.44\( 1.785\) 1.14\( 1.884\) 1.72\( 1.785\) 1.14\( 1.884\) 1.72\( 1.785\) 1.14\( 1.884\) 1.72\( 1.785\) 1.14\( 1.884\) 1.72\( 1.785\) 1.296\( 1.444\) 1.70\( 1.785\) 1.288\( 1.477\) 1.78\( 1.785\) 1.296\( 1.444\) 1.70\( 1.785\) 1.288\( 1.466\) 1.19\( 1.395\) 1.366\( 1.510\) 1.70\( 1.785\) 1.88\( 1.807\) 2.21\( 1.241\) 2.21\( 1.241\) 2.613\( 2.307\) 3.43\( 1.855\) 1.285\( 1.608\) 2.131\( 2.409\) 2.677\( 2.945\) 2.312\( 2.345\) 2.393\( 2.356\) 2.395\( 1.235\) 1.385\( 1.608\) 2.331\( 2.564\) 2.777\( 2.945\) 3.312\( 2.346\) 2.741\( 2.367\) 3.312\( 2.564\) 2.777\( 3.945\) 3.301\( 3.865\) 4.295\( 4.277\) 3.39\( 3.644\) 3.766\( 4.108\) 4.450\( 5.138\) 1.85\( 1.487\) 2.312\( 3.867\) 3.301\( 3.865\) 4.295\( 4.277\) 3.39\( 3.644\) 3.766\( 4.108\) 4.450\( 5.138\) 1.85\( 1.152\) 2.292\( 2.855\) 1.606\( 2.131\) 2.499\( 2.677\) 2.945\( 2.747\) 3.312\( 2.564\) 2.777\( 3.495\) 3.301\( 3.865\) 4.295\( 4.277\) 3.39\( 3.644\) 3.766\( 4.108\) 4.450\( 5.138\) 3.303\( 3.483\) 3.854\( 4.239\) 4.634\( 5.076\) 5.785\( 2.277\) 1.152\( 2.764\) 3.303\( 3.483\) 3.854\( 4.297\) 3.301\( 3.865\) 4.295\( 3.485\) 5.314\( 3.497\) 2.312\( 3.667\) 3.456\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\( 3.857\) 4.285\(	51/2			.216	.288		. 36		.432		.540
7	6		.205			.385	.428	.471			.641
746 1344 321 401 534 602 609 735 802 869 1.02 8	072		970				.512 588	641		756	
9\( \) 1.72 \ .413 \ .516 \ .688 \ .774 \ .86 \ .946 \ 1.082 \ 1.118 \ 1.29 \ 9\ 9\ .192 \ .462 \ .577 \ .770 \ .866 \ .963 \ 1.059 \ 1.154 \ 1.251 \ 1.44 \ 9\ 9\ .215 \ .515 \ .644 \ .859 \ .966 \ 1.074 \ 1.181 \ 1.288 \ 1.395 \ 1.61 \ 10 \ 2.88 \ .571 \ .714 \ .86 \ .966 \ 1.074 \ 1.181 \ 1.288 \ 1.395 \ 1.61 \ 10 \ 2.88 \ .571 \ .714 \ .86 \ .952 \ 1.025 \ 1.351 \ 1.44 \ 1.584 \ 1.782 \ 1.875 \ 1.741 \ 1.781 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.286 \ 1.44 \ 1.584 \ 1.782 \ 1.872 \ 1.61 \ 1.361 \ 1.161 \ 1.705 \ 1.885 \ 1.286 \ 1.152 \ 1.366 \ 1.161 \ 1.705 \ 1.785 \ 1.286 \ 1.44 \ 1.584 \ 1.728 \ 1.872 \ 2.163 \ 3.01 \ 1.351 \ 1.366 \ 1.510 \ 1.891 \ 2.311 \ 2.211 \ 2.412 \ 2.613 \ 3.01 \ 3.481 \ 1.525 \ 1.286 \ 1.152 \ 1.366 \ 1.360 \ 1.311 \ 3.495 \ 2.677 \ 2.381 \ 2.564 \ 2.797 \ 3.029 \ 3.485 \ 1.555 \ 1.885 \ 1.805 \ 1.891 \ 2.393 \ 2.677 \ 2.381 \ 2.564 \ 2.797 \ 3.991 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 3.895 \ 4.895 \ 3.895	71/6		.321			.602		.735			1.002
9\( \) 1.72 \ .413 \ .516 \ .688 \ .774 \ .86 \ .946 \ 1.082 \ 1.118 \ 1.29 \ 9\ 9\ .192 \ .462 \ .577 \ .770 \ .866 \ .963 \ 1.059 \ 1.154 \ 1.251 \ 1.44 \ 9\ 9\ .215 \ .515 \ .644 \ .859 \ .966 \ 1.074 \ 1.181 \ 1.288 \ 1.395 \ 1.61 \ 10 \ 2.88 \ .571 \ .714 \ .86 \ .966 \ 1.074 \ 1.181 \ 1.288 \ 1.395 \ 1.61 \ 10 \ 2.88 \ .571 \ .714 \ .86 \ .952 \ 1.025 \ 1.351 \ 1.44 \ 1.584 \ 1.782 \ 1.875 \ 1.741 \ 1.781 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.288 \ 1.395 \ 1.61 \ 1.161 \ 1.286 \ 1.44 \ 1.584 \ 1.782 \ 1.872 \ 1.61 \ 1.361 \ 1.161 \ 1.705 \ 1.885 \ 1.286 \ 1.152 \ 1.366 \ 1.161 \ 1.705 \ 1.785 \ 1.286 \ 1.44 \ 1.584 \ 1.728 \ 1.872 \ 2.163 \ 3.01 \ 1.351 \ 1.366 \ 1.510 \ 1.891 \ 2.311 \ 2.211 \ 2.412 \ 2.613 \ 3.01 \ 3.481 \ 1.525 \ 1.286 \ 1.152 \ 1.366 \ 1.360 \ 1.311 \ 3.495 \ 2.677 \ 2.381 \ 2.564 \ 2.797 \ 3.029 \ 3.485 \ 1.555 \ 1.885 \ 1.805 \ 1.891 \ 2.393 \ 2.677 \ 2.381 \ 2.564 \ 2.797 \ 3.991 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 4.995 \ 3.684 \ 3.965 \ 3.895 \ 4.895 \ 3.895	8 ~	. 152	. 365	.456	.608	685	.761	.837	.912	.989	1.121
9\( 9\) 281 5 5.51 5 6.644 .859 .966 1.074 1.181 1.188 1.395 1.61 10 288 6.91 .864 1.152 1.296 1.494 1.584 1.782 1.877 1.78 11 2.888 6.91 .864 1.152 1.296 1.494 1.584 1.782 1.872 1.16 12 3.42 8.20 1.025 1.366 1.10 1.70 1.808 0.2050 2.22 2.56 13 4.40 2.964 1.200 1.608 1.809 2.01 1.70 1.78 1.182 1.872 2.16 13 4.402 1.964 1.19 1.398 1.804 2.07 2.331 2.564 2.797 3.093 3.49 15 5.385 1.285 1.285 1.206 1.809 2.01 2.211 2.412 2.613 3.01 15 5.535 1.285 1.285 1.206 2.313 2.409 2.677 2.945 3.212 3.479 4.00 16 6.009 1.461 1.827 2.436 2.741 3.045 3.949 3.654 3.958 4.55 1.485 1.499 2.312 3.3081 3.494 3.766 4.108 4.450 5.13 18 .771 1.849 2.312 3.833 3.408 3.854 4.293 4.624 5.009 5.78 19 8.559 2.061 2.577 3.436 3.803 4.88 3.854 4.293 4.624 5.09 5.78 19 8.559 2.061 2.577 3.496 3.803 4.838 3.854 4.295 4.573 1.618 6.86 2.29 2.2553 3.807 4.285 4.759 5.245 5.321 5.606 6.820 7.85 11 1.099 2.518 3.148 4.197 4.722 5.247 5.771 6.206 6.820 7.85 221 1.049 2.518 3.848 4.197 4.722 5.247 5.771 6.206 6.820 7.85 23 1.259 3.021 3.76 5.035 5.604 6.294 6.923 7.552 8.181 9.46 1.370 3.289 4.111 5.492 6.052 7.436 8.65 8.203 8.809 10.27 2.25 1.487 3.369 4.461 5.496 6.632 7.438 8.194 8.962 1.046 8.65 2.25 1.487 3.369 4.461 5.496 6.632 7.438 8.194 8.962 1.046 1.046 8.65 2.25 1.487 3.369 4.461 5.496 6.837 7.799 8.066 9.532 1.0399 11.385 12.99 2.002 4.805 6.435 7.799 8.066 9.532 1.0399 11.385 12.99 2.002 4.805 6.435 7.799 8.064 8.508 8.203 8.909 10.27 1.333 4.159 5.196 6.808 9.099 10.01 11.011 12.012 13.013 15.00 2.25 1.385 3.408 6.216 7.708 6.808 9.099 10.01 11.011 12.012 13.013 15.00 2.25 1.385 3.408 6.216 7.708 6.808 9.099 10.01 11.011 1.011 12.012 13.013 15.00 3.25 1.239 1.239 1.240 5.141 6.430 5.808 1.238 1.239 1.239 1.239 1.239 1.230 1.230 1.231 1	81/2	.172		.516	.688	.774		.946	1.032	1.118	1.290
10		.192	.462	.517	.770	.866	1.963	1.059	1.154	1.251	1.444
11	10										
12									1.728	1.872	2.160
14	12	.342	.820	1.025	1.366	1.540	1.708	1.880	2.050	2.222	2.564
156	13		.964	1.206				2.211		2.613	3.015
16					1.864			2.564		3.029	3.495
18	15				9 426			2.945	3.212	3 058	
18	17			2.054	2.739	3.081	3.424	3.766	4.108		5.135
90	18	.771	1.849	2.312	3.083	3.468	3.854	4.239	4,624	5.009	5.780
21	19	.859	2.061	2.577				4.724	5.154	5.583	6.442
23	20		2.292	2.855	3.807	4.285	4.759	5.234	5.731	6.186	7.138
23			2.518		4.197	5 193	5 750	6 994			
24 1,370 3,289 4,111 5,482 6,167 6,853 7,538 8,223 8,90810,22 25 1,467 3,656 4,466 5,948 6,692 7,436 8,179 8,933 9,566 11,05 26 1,609 3,861 4,826 6,435 7,239 8,044 8,848 9,652 10,456 12,05 27 1,733 4,159 5,199 6,932 7,729 8,066 9,522 10,399 11,265 12,99 28 1,865 4,477 5,596 7,462 8,395 9,328 10,261 11,103 12,125 13,99 29 2,002 4,805 6,006 8,008 9,009 10,01 11,101 12,012 13,013 15,01 30 2,142 5,141 6,426 8,008 9,039 10,71 11,781 12,852 13,923 16,00 31 2,288 5,546 6,865 9,144 10,287 11,143 12,573 13,776 14,866 17,14 32 2,285 5,546 6,865 9,144 10,287 11,43 12,573 13,776 14,866 17,14 32 2,286 5,846 6,865 9,144 10,287 11,43 12,573 13,776 14,868 17,14 32 2,298 5,846 6,865 9,944 10,571 11,478 12,852 13,923 16,00 33 2 2,496 6,598 8,238 10,394 12,357 13,73 15,103 16,466 18,834 18,27 33 2,234 6,598 8,742 11,666 13,113 4,57 16,627 17,484 18,88 19,42 33 32 2,946 6,598 8,285 10,394 12,357 13,73 15,103 16,466 17,149 13,368 3,368 8,246 10,308 13,744 15,662 17,18 18,898 20,616 23,334 25,77 33 36 3,608 8,246 10,308 13,744 15,462 17,18 18,898 20,616 23,334 25,77 33 36 3,608 8,468 10,864 13,68 14,16 48,16 29 17,91 9,15 48 21,77 24,43 38 13,468 8,246 10,308 13,744 15,462 17,18 18,898 20,616 23,334 25,77 34 40 3,808 9,139 11,424 15,323 17,136 19,04 20,944 22,848 24,752 28,56 44 40 0,808 9,139 11,424 15,323 17,136 19,04 20,944 22,848 24,752 28,56 14 10,661 11,661 31,318 18,424 20,727 23,03 25,33 27,15 38 12,15 14,454 19,22 2,161 12,409 26,399 25,08 33 17,36 14 40 40 40 40 40 40 40 40 40 40 40 40 40		1.259	3.021	3 776		5.664	6.294		7.552	8.181	
26			3.289			6.167	6.853	7.538	8.223	8.908	
28		1.487	3.569	4.461	5.948	6.692	7 436	8.179	8.923	9.566	11.053
28				4.826	6.435	7.239	8.044	8.848	9.652	10.456	12.065
-29         2,002         4,805         6,006         8,008         9,009         10,01         11,011         12,012         13,013         15,013           31         2,288         5,486         6,865         9,144         10,267         11,43         12,283         13,293         16,063         11,48         12,283         13,293         16,063         11,48         12,283         13,283         14,265         14,245         15,54         16,603         14,245         15,54         16,866         17,11         33         2,590         6,216         7,770         10,360         11,655         12,959         14,245         15,54         16,883         18,48         18,285         18,948         20,50         38,288         11,656         13,113         14,57         16,027         17,444         18,949         12,58         18,384         18,48         18,48         19,48         20,58         18,48         11,056         13,113         14,57         16,027         17,444         18,49         16,027         17,444         18,49         18,48         19,49         18,48         19,49         18,44         14,40         18,44         14,40         18,43         18,43         18,43         17,99         18,543	27				7 460	9 905	0.000	9.532			
90			4.977								
32 2.436 5.846 7.308 9.744 10.962 12.18 13.398 14.616 15.834 18.27 38 2.736 6.59 8.285 10.984 12.357 13.73 15.108 16.476 17.849 20.55 35 2.944 6.959 8.742 11.666 13.1814 1.57 16.627 17.484 18.385 19.42 36 38.04 7.401 9.252 12.336 13.878 15.42 16.962 18.504 20.046 23.13 23 37 32.53 7.819 9.771 13.032 14.861 15.29 17.919 19.548 21.772 44.43 38 3.436 8.246 10.308 13.744 15.462 17.18 18.898 20.616 23.334 25.77 39 9.734 18.45 1			5.141	6.426	8.568	9.639	10.71	11.781	12.852	13.923	16.065
33 2,590 6,216 7,770 10,560 11,655 12,959 14,245 15,54 16,838 19,42   344 2,746 6,59 8,238 10,941 12,357 13,73 15,103 16,476 17,849 120,55   355 2,914 6,993 8,742 11,656 13,113 14,57 16,027 17,444 18,941 21,58   366 3,081 7,401 9,252 12,336 13,878 15,42 16,922 18,504 20,040 23,13   37 3,253 7,819 9,774 13,032 14,861 16,39 17,919 19,548 21,777 24,43   383 3,436 8,246 10,303 13,744 15,467 17,18 18,88 80,616 22,33 34,25,77   399 3,630 8,648 10,86 14,48 16,39 18,1 19,91 21,62 23,53 27,15   40 3,808 9,13 11,421 15,232 17,136 19,04 20,944 22,848 24,752 28,56   41 4,092 9,004 12,006 16,008 18,009 20,00 22,011 24,02 16,23 13,30   42 4,198 10,655 12,534 16,792 18,901 30,90 23,089 25,188 17,872 28,56   44 4,09 10,56 12,534 16,792 18,901 30,90 23,089 25,188 17,878 28,31 48   44 4,09 10,56 12,534 16,792 18,901 30,90 23,089 25,188 17,878 31,48   44 4,09 10,56 12,534 16,792 18,901 30,90 23,089 25,188 17,878 31,48   44 4,09 10,56 12,534 16,792 18,901 30,90 23,089 25,188 17,878 31,48   44 4,09 10,56 12,534 10,792 18,901 30,90 23,089 25,188 17,317 36,13   45 4,00 10,56 12,534 10,792 18,901 30,90 23,089 25,188 17,317 36,13   46 5,043 12,066 15,192 30,144 22,662 25,18 27,668 30,216 32,754 37,77   47 5,043 12,064 15,768 10,042 36,562 25,18 27,668 30,216 32,758 37,74   47 5,043 12,064 16,108 10,042 36,562 25,18 27,668 30,216 32,758 37,74   48 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,152 35,638 41,14   49 5,744 12,18 17,142 28,86 28,86 28,76 28,88 28,98 31,538 34,41 41 42,88   5,744 12,18 17,142 28,86 28,660 27,41 30,151 33,152 35,638 41,11   49 5,744 12,18 17,142 28,86 28,660 27,41 30,151 33,152 38,638 41,11   49 5,744 12,18 17,142 28,86 28,660 27,41 30,151 33,152 38,638 41,11   49 5,744 12,18 17,142 28,86 28,86 28,761 38,87 34,741 42,88 1			5.486	6.865		10.287		12.573	13.716	14.866	17.145
34 2,746 6,59 8,288 10,984 12,367 13,73 15,108 16,476 17,849 20,58 35 2,94 6,993 8,742 11,666 13,118 14,57 16,027 17,484 18,94 21,88 36 3,084 7,401 9,252 12,336 13,878 15,42 16,962 18,504 20,046 23,13 37 3,253 7,819 9,771 31,302 14,861 16,29 17,919 19,548 21,772 44,43 38 3,436 8,246 10,308 13,744 15,462 17,18 18,898 20,616 22,334 25,77 39 36,620 8,648 10,86 14,48 16,29 17,19 18,1 19,91 12,62 23,53 27,15 40 3,508 9,139 11,424 15,322 17,136 19,04 20,944 22,848 24,752 28,56 41 40,02 9,044 12,006 16,008 18,009 9,00 22,011 24,012 26,103 30,01 42 44,01 0,05 12,594 16,792 18,901 20,99 23,089 25,188 27,287 31,48 44 40 10,55 13,20 17,6 19,8 22,00 24,2 26,4 28,6 33,00 44 42,48 14,01 10,55 13,20 17,6 19,8 22,00 24,2 26,4 28,6 33,00 44 44 4,601 10,66 11,56 13,20 17,6 19,8 22,00 24,2 26,4 28,6 33,00 44 48 18,18 11,563 14,454 19,22 21,612 14,09 26,389 25,968 31,718 61,38 46 5,043 12,086 15,128 20,144 22,662 25,18 27,688 30,216 32,764 37,76 47 5,256 12,641 15,768 19,022 21,612 40,9 26,389 25,968 31,718 61,39 44 5 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,162 35,633 41,44 28,5 48,5 21,846 16,446 21,928 24,669 27,41 30,151 33,162 35,633 41,44 28,56 27,18 28,77 38,87 38,38 44 45 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,162 35,633 41,44 28,56 24,88 28,58 37,748 24,848 31,748 28,88 31,744 42,88 34,88 3				7.308	9.744	10.962	12.18	13.398	14.616	15.834	18.270
35								15 109	16.04	10.850	20 505
36 3,084 7,401 9,252 12,336 13,878 15,42 16,962 18,504 20,046 28,13 37 37 3,253 7,819 9,774 13,032 14,861 16,29 17,791 9,548 21,772 44,43 38 3,436 8,246 10,308 13,744 15,462 17,18 18,898 20,616 22,334 25,77 39 36,60 8,246 10,861 44 48 16,29 18,1 19,91 12,162 23,53 27,15 40 3,508 9,139 11,424 15,232 17,136 19,04 20,944 22,848 24,752 28,56 41 40,02 9,604 12,006 16,008 18,009 20,00 22,011 24,012 26,103 30,01 42 4,198 10,065 12,594 16,792 18,901 20,99 23,089 25,188 27,287 31,44 44 4,001 5,51 32,20 17,6 19,8 22,00 24,2 26,4 28,6 33,00 44 44 4,606 11 046 18,318 18,842 49,727 23,03 25,333 27,636 29,938 34,54 45 4,818 11,536 14,454 19,22 21,612 40,9 26,398 28,96 31,317 36,13 44,54 19,22 21,612 40,9 26,398 28,96 31,317 36,13 44,54 19,22 21,612 40,9 26,398 28,96 31,317 36,13 44,54 18,18 11,56 14,454 19,22 21,612 40,9 26,398 28,96 31,317 36,13 44,54 18,18 11,52 31,641 19,22 21,611 19,26 25,28 28,96 89,88 31,563 34,164 39,42 48 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,162 33,633 41,14 28,86 24,669 27,41 30,151 33,162 33,633 41,14 42,86 23,86 24,86 27,47 30,18 28,86 28,86 31,14 42,86 24,86 27,48 30,18 28,86 28,86 31,363 34,14 44,86 24,86		2 914						16.027	17.484	18 941	21 855
38			7.401	9,252	12.336	13.878	15.42	16.962	18.504	20.046	23.130
39         3,620         8,648         10,86         14,48         16,29         18,1         19,91         21,62         23,58         27,15           40         3,808         9,139         11,424         15,222         17,161         10,04         20,442         28,48         24,752         28,56           41         4,002         9,644         12,006         16,008         18,009         20,00         22,011         24,012         26,112         36,113         30,00           42         4,198         10,55         13,20         17,6         19,8         22,00         24,2         26,4         27,287         31,46           44         4,606         11,046         13,818         18,424         20,727         23,03         25,188         27,287         31,48           45         4,818         11,563         14,454         19,222         1,612         24,09         2,638         29,383         34,53           46         5,043         12,086         15,128         20,144         22,662         25,18         27,663         39,289         38,317         36,138           47         5,256         12,044         3,652         30,289         20,333 <th< th=""><th></th><th>3.253</th><th>7.819</th><th>9.774</th><th>13.032</th><th>14.861</th><th>16.29</th><th>17.919</th><th>19.548</th><th>21.177</th><th>24.435</th></th<>		3.253	7.819	9.774	13.032	14.861	16.29	17.919	19.548	21.177	24.435
40 3, 508 9, 139 11, 424 15, 323 17, 136 19, 04 20, 944 92, 848 24, 752 28, 56 44 12, 046 16, 081 8, 099 20, 00 22, 011 24, 012 26, 183 20, 142 4, 198 10, 065 12, 594 16, 792 18, 901 20, 99 23, 089 25, 188 97, 287 31, 44 44 10, 10, 55 13, 20 17, 6 19, 8 29, 00 24, 2 26, 4 26, 6 38, 00 44 4, 6 10, 6 11, 046 18, 318 18, 424 20, 727 23, 03 25, 333 27, 636 29, 938 34, 54 45 48, 181 81, 153 14, 454 19, 272 21, 631 24, 09 26, 389 28, 908 31, 373 61, 31 46 5, 194 22, 26, 27 24, 29 25, 28 28, 28 98, 38 27, 636 29, 638 27, 638 29, 638 31, 536 34, 64 16, 39, 42 48 5, 482 12, 846 16, 446 21, 928 24, 669 27, 41 30, 151 33, 152 35, 638 41, 199			8.246				17.18				
42 4, 198 10,065 12,594 16,792 18,301 20,39 23,089 25,188 37,287 31,48 44 4,60 10,55 13,20 17,6 19,8 2,20 0 24,2 26,4 28,6 33,00 44 4,60 6 11 046 13,818 18,818,18,242 07,727 33,03 25,333 27,636 29,939 34,54 45 48,18 11,563 144,451 9,722 21,681 24,09 26,389 28,908 31,317 36,13 46 5,043 12,066 15,128 20,144 22,662 25,18 27,668 30,216 32,764 37,74 47 5,256 12,644 15,768 12,1024 36,562 36,88 28,280 81,356 34,461 39,42 48 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,152 35,638 41,11 49 5,744 12,28 12,34 12,34 22,566 25,718 28,77 31,74 142,28 54,669 27,41 30,151 33,152 35,638 41,11 41,28 54,648 24,28 25,648 24,2			0.120	10.86	15 999	17 136	10.1	90 044	21.02	26.08	27.150
42 4, 198 10,065 12,594 16,792 18,301 20,39 23,089 25,188 37,287 31,48 44 4,60 10,55 13,20 17,6 19,8 2,20 0 24,2 26,4 28,6 33,00 44 4,60 6 11 046 13,818 18,818,18,242 07,727 33,03 25,333 27,636 29,939 34,54 45 48,18 11,563 144,451 9,722 21,681 24,09 26,389 28,908 31,317 36,13 46 5,043 12,066 15,128 20,144 22,662 25,18 27,668 30,216 32,764 37,74 47 5,256 12,644 15,768 12,1024 36,562 36,88 28,280 81,356 34,461 39,42 48 5,482 12,846 16,446 21,928 24,669 27,41 30,151 33,152 35,638 41,11 49 5,744 12,28 12,34 12,34 22,566 25,718 28,77 31,74 142,28 54,669 27,41 30,151 33,152 35,638 41,11 41,28 54,648 24,28 25,648 24,2			9.604	12,006	16.008	18.009	20.00	22.011	24.012	26.013	30.015
43 4.40 10.55 13.20 17.6 19.8 22.00 24.2 26.4 28.6 33.00 44.4 46.6 11 046 13.818 18.424 20.727 23.03 25.383 27.686 29.389 34.54 45 4.818 11.563 14.454 19.272 21.651 24.09 26.389 28.908 31.317 86.13 46 5.043 12.086 15.128 20.144 22.662 25.18 27.689 80.216 32.754 37.77 45.256 12.614 15.768 21.024 23.652 26.28 28.908 31.536 34.164 39.42 48 5.482 12.846 16.446 21.928 24.669 27.41 30.151 33.152 35.633 41.14 42.8 57 14.14 22.8 57 14.14 22.8 58.25 25.28 28.28	42	4.198	10.065	12.594	16.792	18.901	20.99	23.089	25.188	27.287	31.485
45 4.818 11.563 14.45419.27221.651124.09 26.38928.908.31.317186.137 46 5.043 12.086 15.12820.144122.662125.18 27.68830.216.32.754187.77 47 5.256 12.614 15.768121.024 23.652 26.28 28.2808 31.536 34.16439.42 48 5.482 12.846 16.446.21.928124.669127.41 30.151 33.152 35.633141.11 49 5.714 12.913 17.142 28.586 25.7138.5 57 31.42734.284 37.14142.88			10.56					24.2	26.4	28.6	33.00
46 5,043 12,066 15,128 20,144 [22,662 25,18 [27,668 80,16 32,764 87,77] 47 5,256 12,044 15,768 17,042 36,52 96,28 28,908 81,3568 41,64 [39,42 48 5,482 12,846 16,446 21,988 24,669 27,41 80,151 83,162 35,638 41,11 49 5,744 12,91 17,142 2,86 25,78 25,86 25,71 32,8 5,7 31 42,2 85	44			13.818	18.424	20.727	23.08				
47   5,256   12,614   15,768 21,024 23,652 26,28   28,908 31,536,34,164 39,42,44   68,482   12,846   16,446 21,928 24,669 27,41   30,151 33,152 35,633 41,41   49   5,714 12,913 17,142 23,856 25,713 28,57 31,427 34,264 37,141 42,85				15 198	20 144	22.662	25.18	27.698	30.216	32 754	37,770
48   5,482   12,846   16,446   21,928   24,669   27,41   30,151   33,152   35,633   41,11   49   5,714   12,913   17,142   22,856   25,713   28,57     31,427   34,284   37,141   42,85   43,245	47	5.256	12.614	15.768	21.024	23.652	26.28	28.908	31.536	34.164	39.420
49   5 714   12.913   17.142   22.856   25.713   28.57   31.427   34.284   37.141   42.85		5.482	12.846	16,446	21.928	24.669	27.41	30.151	33.152	,35.633	41.115
	49		12.913	17.142	22.856	25.713	28.57	31.427	34.284	37.141	42.855
50   5.950   14.28   17.55   25.5   20.775   29.15   32.725   35.7   35.075   44.02   51   6.180   14.832   18.54   24.76   27.855   30.95   34.045   37.08   40.205   46.42	50	5.950	14.28 14.832	17.85 18.54	23.8	26.775	29.75	32.725	35.7	38.675	44.625
51   6.180   14.832   18.54   24.76   27.855   30.95   34.045   37.08   40.205   46.42   52   6.432   15.437   19.296   25.728   28.944   32.16   35.376   38.592   41.808   48.24			15 487	19 296	25 728	28 944	32 16	35 376	38 592	41 808	48 940
53 6.684 16.041 20.052 26.736 30.078 33.42 36.762 40.104 48.446 50.18				20.052	26.736	30.078	33.42	36.762	40.104	43.446	50.130
54 6.940 16.656 20.82 27.76 31.23 34.7 38.17 41.64 45.11 52.05	54	6.940	16.656	20.82	27.76	31.23	34.7	38.17	41.64	45.11	52.05
55   7.198   17.275   21.594   28.792   32.391   35.99   39.589   43.188   46.787   53.98	55	7.198	17.275	21.594	28.792	32.391	35 99	39.589	43.188	46.787	53.985
56 7.462 17.909 22.386 29.848 33.579 37.31 41.041 44.772 48.503 55.96 57 7.732 18.557 28.196 30.928 34.794 38.66 42.526 46.392 50.258 57.99	56	7.462	17.909	22.386	29.848	33.579	37.31	41.041	44.772	148.503	55.965
57   7.732   18.557   28.196 30.928 34.794   38.66   42.526   46.392   50.258   57.99   58   8.006   19.214   24.018   32.024   36.027   40.03   44.038   48.036   52.039   60.04			19 214					44 033	48 036	52 039	60 045
59 . 8.284 19.902 24.852 33.136 37.278 41.42 45.562 48.704 53.846 62.13								45.562	48,704	53.846	62.13
60 8.566 20.558 25.698 34.264 38.547 42.83 47.113 51.396 55.679 64.24		8.566						47.113	51.396	55.679	64.245

To draw the Clearance-line on the Indicator-diagram, the actual clearance not being known.—The clearance-line may be obtained approximately by drawing a straight line, chad, across the compression curve, first having drawn OX parallel to the atmospheric line and 14.7 lbs. below. Measure from a the distance ad, equal to cb, and draw YO perpendicular to OX through d; then will TB divided by AT be the percentage of

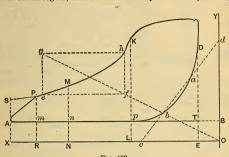


Fig. 139.

clearance. The clearance may also be found from the expansion-line by constructing a rectangle *eflig*, and drawing a diagonal *gf* to intersect the line XO. This will give the point O, and by erecting a perpendicular to XO we obtain a clearance-line OY

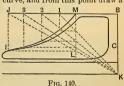
Both these methods for finding the clearance require that the expansion and compression curves be hyperbolas. Prof. Carpenter (Power, Sept. 1893) says that with good diagrams the methods are usually very accurate,

and give results which check substantially,

The Buckeye Engine Co., however, say that, as the results obtained are seldom correct, being sometimes too little, but more frequently too much and as the indications from the two curves seldom agree, the operation has little practical value, though when a clearly defined and apparently undistorted compression curve exists of sufficient extent to admit of the application of the process, it may be relied on to give much more correct results than the expansion curve.

To draw the Hyperbolic Curve on the Indicator-diagram. - Select any point I in the actual curve, and from this point draw a

line perpendicular to the line JB, meeting the latter in the point J. The line JB may be the line of boiler-pressure, but this is not material; it may be drawn at any convenient height near the top of diagram and parallel to the atmospheric line. From J draw a diagonal to K, the latter point being the intersection of the vacuum and clearance lines; from I the vacuum and clearance mass, from I draw IL parallel with the atmospheric line. From L, the point of intersection of the diagonal JK and the horizontal line IL, draw the vertical line LM. The



point M is the theoretical point of cut-off, and LM the cut-off line. Fix upon any number of points 1, 2, 3, etc., on the line JB, and from these points draw diagonals to K. From the intersection of these diagonals with LM draw horizontal lines, and from 1, 2, 3, etc., vertical lines. Where these lines meet will be points in the hyperbolic curve.

**Pendulum Indicator Rig.**—Power (Feb. 1893) gives a graphical representation of the errors in indicator-diagrams, caused by the use of in-

correct form of the pendulum rigging. It is shown that the "brumbo" pulley on the pendulum, to which the cord is attached, does not gener-



ally give as good a reduction as a simple pin attachment. When the end of the pendulum is slotted, working in a pin on the crosshead, the stoucu, working in a pin of the crossnead, the error is apt to be considerable at both ends of the card. With a vertical slot in a plate fixed to the crosshead, and a pin on the pendulum working in this slot, the reduction is perfect, when the cord is attached to a pin on the pendulum, a slight error being introduced if the brumb, pulley is used. With the connection between the pendulum and the crosshead made by means of a horizontal link, the reduction is

by means of a horizontal link, the reduction is nearly perfect, if the construction is such that the connecting link vibrates equally above and below the horizontal, and the cord is attached by a pin. If the link is horizontal at mid-stroke a serious error is introduced, which is magnified if a brumbo pulley also is used. The adjoining figures show the two forms recommended.

Theoretical Water-consumption calculated from the Indicator-card,—The following method is given by Prof. Carpenter (Power, Sept. 1893): p = mean effective pressure, l = length of stroke in feet, a = area of piston in square inches, a + 144 = area in square feet, c = percentage of clearance to the stroke, b = percentage of stroke at point where water rate is to be computed, n = number of strokes per minute, 60n = number of strokes per minute, 60n = number of strokes diagram corresponding to that at the point where sure as shown by the diagram corresponding to that at the point where water rate is required, w' = that corresponding to pressure at end of compression.

Number of cubic feet per stroke =  $l\left(\frac{b+c}{100}\right)\frac{a}{144}$ .

Corresponding weight of steam per stroke in lbs.  $= l \left( \frac{b+c}{100} \right) \frac{a}{144} w$ ,

Volume of clearance =  $\frac{lca}{14\ 400}$ .

Weight of steam in clearance =  $\frac{lcaw'}{14.400}$ .

Total weight of steam  $= \frac{60nla}{14,400} [(b+c)w - cw'].$ 

The indicated horse-power is  $p \mid a \mid n + 33,000$ . Hence the steam-consumption per indicated horse-power is

$$\frac{60nla}{\frac{60nla}{14,400}} \left[ (b+c)w - cw' \right] = \frac{137.50}{\frac{p \ l \ a \ n}{30,000}} \left[ (b+c)w - cw' \right].$$
ing the formula to a rule, we have: To find the restance.

Changing the formula to a rule, we have: To find the water rate from the

indicator diagram at any point in the stroke. RULE.—To the percentage of the entire stroke which has been completed RULE.—To the percentage of the entire stroke which has been completed by the piston at the point under consideration add the percentage of clearance. Multiply this result by the weight of a cubic foot of steam, having a pressure of that at the required point. Subtract from this the product of percentage of clearance multiplied by weight of a cubic foot of steam having a pressure equal to that at the end of the compression. Multiply this result by 137.50 divided by the mean effective pressure. Nore.—This method only applies to points in the expansion curve or between multiplication.

tween cut-off and release.

<sup>\*</sup> For compound or triple-expansion engines read: divided by the equivalent mean effective pressure, on the supposition that all work is done in one cylinder.

The beneficial effect of compression in reducing the water-consumption of an engine is clearly shown by the formula. If the compression is carried to such a point that it produces a pressure equal to that at the point under consideration, the weight of steam per cubic root is equal, and we w. In this case the effect of clearance entirely disappears, and the formula becomes  $\frac{137.5}{n}(bw)$ .

In case of no compression, w' becomes zero, and the water-rate =

$$\frac{137}{p} \frac{5}{2} [(b+c)w].$$

Prof. Denton (Trans. A. S. M. E., xiv. 1363) gives the following table of theoretical water-consumption for a perfect Mariotte expansion with steam at 150 lbs. above atmosphere, and 2 lbs. absolute back pressure :

Ratio of Expansion, r.	M.E.P., lbs. per sq. in.	Lbs. of Water per hour per horse-power, W.
10	52.4	9.68
15	38.7	8.74
20	30.9	8.20
25	25.9	7.84
30	22.2	7.63
35	19.5	7.45

The difference between the theoretical water-consumption found by the formula and the actual consumption as found by test represents "water not accounted for by the indicator," due to cylinder condensation, leakage through ports, radiation, etc.

Leakage of Steam. - Leakage of steam, except in rare instances, has so lutle effect upon the lines of the diagram that it can scarcely be detected. The only satisfactory way to determine the tightness of an engine is to take it when not in motion, apply a full boiler-pressure to the valve, placed in a closed position, and to the piston as well, which is blocked for the purpose at some point away from the end of the stroke, and see by the eye whether leakage occurs. The indicator-cocks provide means for bringing into view steam which leaks through the steam-valves, and in most cases that which leaks by the piston, and an opening made in the exhaust-pipe or observa-

tions at the atmospheric escape-pipe, are generally sufficient to determine the fact with regard to the exhaust-valves.

The steam accounted for by the indicator should be computed for both the cut-off and the release points of the diagram. If the expansion-line departs much from the hyperbolic curve a very different result is shown at one point from the hyperbolic curve a very different result is shown at one point from the hyperbolic curve a very different result is shown at one point from the state of the control of the co loss occasioned by cylinder condensation and leakage is indicated in a much more truthful manner at the cut-off than at the release. (Tabor Indicator

Circular.)

### COMPOUND ENGINES.

Compound, Triple- and Quadruple-expansion Engines. —A compound engine is one having two or more cylinders, and in which the steam after doing work in the first or high-pressure cylinder completes

the scannish in the other cylinder or cylinders. The term "compound" is commonly restricted, however, to engines in which the expansion takes place in two stages only—high and low pressure, the terms triple-expansion and quadruple-expansion engines being used when the expansion takes place respectively in three and four stages. The number the expansion takes place respectively in three and four stages. The number of cylinders may be greater than the number of stages of expansion, for constructive reasons; thus in the compound or two-stage expansion engine the low-pressure stage may be effected in two cylinders so as to obtain the advantages of nearly equal sizes of cylinders and of three cranks at angles of 120°. In triple-expansion engines there are frequently two low-pressure cylinders, one of them being placed tandem with the high-pressure, and the other with the intermediate cylinder, as in mill engines with two cranks at 90°. In the triple-expansion engines of the steamers Campania and Lucania, with three cranks at 120°, there are five cylinders, two high, one intermediate, and two low, the high-pressure cylinders being tandem with the low.

Advantages of Compounding. - The advantages secured by dividing the expansion into two or more stages are twofold: 1. Reduction of wastes of steam by cylinder-condensation, clearance, and leakage; 2. Dividing the of steam by cylinder-condensation, clearance, and leakage; 2. Dividing the pressures on the cranks, shafts, etc., in large engines so as to avoid excessive pressures and consequent friction. The diminished loss by cylinder-condensation is effected by decreasing the range of temperature of the metal surfaces of the cylinders, or the difference of temperature of the steam admission and exhaust. When high-pressure steam is admitted into a single-cylinder engine a large portion is condensed by the comparatively cold metal surfaces; at the end of the stroke and during the exhaust the water is re-evaporated, but the steam so formed escapes into the atmosphere or into the condenser, doing no work; while if it is taken into a second cylinder, as in a compound engine, it does work. The steam lost in the first retired to the condenser of the condenser of the condenser of the condenser of the condenser. cylinder by leakage and clearance also does work in the second cylinder. cylinder by leakage and clearance also does work in the second cylinder. Also, if there is a second cylinder, the temperature of the steam exhausted from the first cylinder is higher than if there is only one cylinder, and the metal surfaces therefore are not cooled to the same degree. The difference in temperatures and in pressures corresponding to the work of steam of 150 lbs, gauge-pressure expanded 20 times, in one, two, and three cylinders, is shown in the following table, by W. H. Weightman, Am. Mach., July 28, 1000. 1892:

	Single Cyl- inder.	Compound Cylinders.		Triple-expansion Cylinders.		
Diameter of cylinders, in	60	33	61	28	46	61
Area ratios		5	3.416		2.70	4.746
Expansions	20	5	4	2.714	2.714	2.714
Initial steam - pressures-						
absolute-pounds	165	165	33	165	60.8	22.4
Mean pressures, pounds	32.96	86.11	19.68	121.44	44.75	16.49
Mean effective pressures,						
pounds	28.96	53.11	15.68	60.64	22.35	12.49
Steam temperatures into						
cylinders	366°	366°	259°.9	366°	293°.5	234°.1
Steam temperatures out of						
the cylinders	184°.2	2590.9	184°.2	2930.5	234°.1	184°.2
Difference in temperatures	181.8	106.1	175.7	72.5	59.4	49.9
Horse-power developed	800	399	403	269	268	264
Speed of piston	322	290	290	238	238	238
Total initial pressures on						
pistons, pounds		112,900	84,752	64.162	63,817	53,773

44 Woolf? and Receiver Types of Compound Engines,— The compound steam-engine, consisting of two cylinders, is reducible to two forms, 1, in which the steam from the h.p. cylinder is exhausted direct into the l. p. cylinder, as in the Woolf engine; and 2, in which the steam from the h. p. cylinder is exhausted into an intermediate reservoir, whence the steam is supplied to, and expanded in, the l. p. cylinder, as in the "receiverengine."

If the steam be cut off in the first cylinder before the end of the stroke, the total ratio of expansion is the product of the ratio of expansion in the first cylinder, into the ratio of the volume of the second to that of the first

cylinder; that is, the product of the two ratios of expansion.

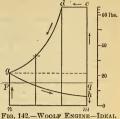
Thus, let the areas of the first and second eylinders be as 1 to 3½, the strokes being equal, and let the steam be cut off in the first at% stroke; then Expansion in the 1st cylinder .....

..... 1 to 31/2 Total or combined expansion, the product of the two ratios... 1 to 7

Woolf Engine, without Clearance-Ideal Diagrams .-The diagrams of pressure of an ideal Woolf engine are shown in Fig. 142, as they would be described by the indicator, according to the arrows. In these diagrams pq is the atmospheric line, m the vacuum line, cd the admission line, dg the hyperbolic curve of expansion in the first cylinder, and gh the con-

secutive expansion-line of back pressure for the return-stroke of the first piston, and of positive pressure for the steam-stroke of the second piston. At the point h, at the end of the stroke of the second piston, the steam is exhausted into the condenser, and the pressure falls to the level of perfect vacuum, mn.

The diagram of the second cylinder, below gh, is characterized by the absence of any specific period of admission; the whole of the steam-line gh being expansional, generated by the expansion of the initial body of steam contained in the first cylinder into the second. When the return-stroke is completed, the whole of the steam transferred from the first is shut into the second cylinder. The final pressure and volume of the steam in the second cylinder are the



INDICATOR-DIAGRAMS.

same as if the whole of the initial steam had been admitted at once into the second cylinder, and then expanded to the end of the stroke in the manner of a single-cylinder engine,

The net work of the steam is also the same, according to both distributions. Receiver-engine, without Clearance—Ideal Biagrams.— In the ideal receiver-engine the pistons of the two cylinders are con-nected to cranks at right angles to each other on the same shaft. The receiver takes the steam exhausted from the first cylinder and supplies it to the second, in which the steam is cut off and then expanded to the end of the stroke. On the assumption that the initial pressure in the second cylinder is equal to the final pressure in the first, and of course equal to the pressure in the first, and of course equal to the pressure in the receiver, the volume cut off in the second cylinder must be equal to the volume of the first cylinder, for the second cylinder must admit as much steam at each stroke as is discharged from the first cylinder. In Fig. 143 cd is the line of admission and hg the exhaust-line for the first

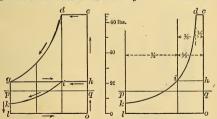


FIG. 143 .- RECEIVER-ENGINE, IDEAL Fig. 144.—Receiver Engine, INDICATOR-DIAGRAMS. DIAGRAMS REDUCED AND COMBINED.

cylinder; and dg is the expansion-curve and pg the atmospheric line. In the region below the exhaust-line of the first cylinder, between it and the line of perfect vacuum, ol, the diagram of the second cylinder is formed; hi, the second line of admission, coincides with the exhaust-line hg of the first cylinder, showing in the ideal diagram no intermediate fall of pressure, and ik is the expansion-curve. The arrows indicate the order in which the diagrams are formed.

In the action of the receiver-engine, the expansive working of the steam, though clearly divided into two consecutive stages, is, as in the Woolf engine, essentially continuous from the point of cut-off in the first cylindor to the end of the stroke of the second cylinder, where it is delivered to the condenser; and the first and second diagrams may be placed together and

combined to form a continuous diagram. For this purpose take the second diagram as the basis of the combined diagram, namely, hido, Fig. 144. The period of admission, hi, is one third of the stroke, and as the ratios of the cylinders are as 1 to 3, h is also the proportional length of the first diagram as applied to the second. Produce oh upwards, and set off oc equal to the total height of the first diagram above the vacuum-line; and, upon the shortened base hi, and the height hc, complete the first diagram with the steam-line dt, and the expansion-line di.

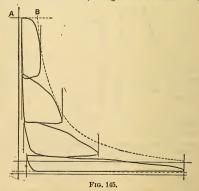
It is shown by Clark (S. E., p. 432, et seq.) in a series of arithmetical calculations, that the receiver-engine is an elastic system of compound engine, in which considerable latitude is afforded for adapting the pressure in the receiver to the demands of the second cylinder, without considerably diminishing the effective work of the engine. In the Woolf engine, on the contrary, it is of much importance that the intermediate volume of space between the first and second cylinders, which is the cause of an intermediate fall of pressure, should be reduced to the lowest machicalle amount.

between the first and second cylinders, which is the chace of an amount, diate fall of pressure, should be reduced to the lowest practicable amount. Supposing that there is no loss of steam in passing through the engine, by cooling and condensation, it is obvious that whatever steam passes through the first cylinder must also find its way through the second cylinder. By varying, therefore, in the receiver-engine, the period of admission in the second cylinder, and thus also the volume of steam admitted for each stroke, the steam will be measured into it at a higher pressure and of a less bulk, or at a lower pressure and of a greater bulk; the pressure and density naturally adjusting themselves to the volume that the steam from the receiver is permitted to occupy in the second cylinder. With a sufficiently restricted admission, the pressure in the receiver may be maintained at the pressure of the steam as exhausted from the first cylinder. On the contrary, with a wider admission, the pressure in the receiver may be maintained at the pressure of the team as exhausted from the first cylinder. On the contrary, with a wider admission, the pressure in the receiver may be maintained at the steam from the first cylinder.

(For a more complete discussion of the action of steam in the Woolf and

receiver engines, see Clark on the Steam-engine,

Combined Diagrams of Compound Engines.—The only way of making a correct combined diagram from the indicator-diagrams of the several cylinders in a compound engine is to set off all the diagrams on the same horizontal scale of volumes, adding the clearances to the cylinder ca-



pacities proper. When this is attended to, the successive diagrams fall exactly into their right places relatively to one another, and would compare properly with any theoretical expansion-curve. (Prof. A. B. W. Kennedy, Proc. Inst. M. E., Oct. 1886.)

This method of combining diagrams is commonly adopted, but there are objections to its accuracy, since the whole quantity of steam consumed in the first cylinder at the end of the stroke is not carried forward to the second, but a part of it is retained in the first cylinder for compression. For a method of combining diagrams in which compression is taken account of, a method of combitting diagrams in which compression is taken account of, 1887, p. 48. The usual method of combining diagrams is also criticised by Frank H. Ball as inaccurate and misleading (Am. Mach., April 12, 1891; Trans, A. S. M. E., xiv. 1405, and xv. 403).

Figure 15 shows a combined diagram of a quadruple-expansion engine,

drawn according to the usual method, that is, the diagrams are first reduced in length to relative scales that correspond with the relative piston-displacement of the three cylinders. Then the diagrams are placed at such distances from the clearance-line of the proposed combined diagram as to correctly represent the clearance in each cylinder.

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## Calculated Expansions and Pressures in Two-eylinder Compound Engines, (James Tribe, Am. Mach., Sept. & Oct. 1891.)

TWO-CYLINDER COMPOUND NON-CONDENSING.

Back pressure	2 10. a	oove a	unospi	nere.					
Initial gauge- pressure Initial absolute	100	110	120	130	140	150	160	170	175
pressure Total expansion.	115	125 7.84	135 8,41	145 9	155 9.61	165 10.24	175 10.89	185	190 11.9
Expansions in each cylinder		2.8	2.9	3	3.10	3.2	3.3	3.4	3.45
Hyp. log. plus 1. Forward   High.	1.993			2.028	2.131 106.5	2.163 111.5		2.223	
pressures   Low Back   High.	31.3	32.3 44.6	33.1 46.5			34.8	35.2 53	35.6	35.7 55
pressures   Low	15.5	15.5 45.9	15.5 49.5	15.5 53.1	15.5	15.5	15.5	15.5	15.5
effective High.	15.8	16.8	17.6	18.2	56.5 18.8		$63.3 \\ 19.7$		$\frac{68.2}{20.2}$
Ratio-cylinder areas		2.73	2.81	2.91	3	3.11	3.21	3.31	3.37

#### TWO-CYLINDER COMPOUND CONDENSING.

Back pressure, 6.5 lbs. above	Back pressure, 6.5 lbs. above vacuum.						
Initial gauge-pressures	90	100	110	120	130	140	150
Initial absolute pressures	105	115	125	135	145	155	165
Probable per cent of loss	2.6	2.9	3.3	3.6	3.8	4.0	4.3
Total expansions	15.7	17	18.5	20	21.5	22.7	24.2
Exps. in each cylinder	3.96	4.13	4.3	4.47	4.64	4.77	4.92
Hyp. log. plus 1	2.376						2.593
Mean forward j High		67.3	71.4				87
pressures \ Low		15.55	15.9	16.2		16.75	17.05
Mean back   High		27.8		30.2		32.4	33.5
pressures   Low	4.3	4.3	4.3	4.3	4.3	4.3	4.3
Mean High	36 4	39.5	42.4	45.2	47.9	50.8	58.5
errective J I on				11.9		12.45	12.75
pressures (							
Terminal   High							33 5
pressures   Low	6.4	6.45	6.45	6.5	6.55	6.55	6.6
Initial pressure in l. p. cyl	25.3						32.4
Ratio of cylinder areas	3.32	3.51	3.66	3.8	3.92	4.08	4.19

The probable percentage of loss, line 3, is thus explained: There is always a loss of heat due to condensation, and which increases with the pressure of steam. The exact percentage cannot be predetermined, as it depends largely upon the quality of the non-conducting covering used on the cylinder, receiver, and pipes, etc. but will probably be about as shown.

Proportions of Cylinders in Compound Engines.—Authorities differ as to the proportions by volume of the high and low pressure

cylinders v and V. Thus Grashof gives  $V + v = 0.85 \sqrt{r}$ ; Krabak, 0.90  $\sqrt{r}$ ;

Werner,  $\sqrt{r}$ ; and Rankine,  $\sqrt{r^2}$ , r being the ratio of expansion. Busley makes the ratio dependent on the boiler-pressure thus:

Lbs. per sq. in...
 60
 90
 105
 120

 
$$V \div v$$
 = 3
 4
 4.5
 5

(See Seaton's Manual, p. 95, etc., for analytical method; Sennett, p. 496, etc.; Clark's Steam-engine, p. 445, etc.; Clark, Rules, Tables, Data, p. 849, etc.) Mr. J. McFarlane Gray states that he finds the mean effective pressure in the compound engine reduced to the low-pressure cylinder to be approxi-

mately the square root of times the boiler-pressure.

Approximate Horse-power of a Modern Compound
Marine-engine. (Seaton.)—The following rule will give approximately the horse-power developed by a compound engine made in accordance with

modern marine practice. Estimated H.P. =  $\frac{D^2 \times \sqrt{p} \times R \times S}{2}$ 

D = diameter of l.p. cylinder; p = boiler-pressure by gauge;R = revs. per min.; S = stroke of piston in feet.

Ratio of Cylinder Capacity in Compound Marine Engines. (Seaton.)—The low-pressure cylinder is the measure of the power of a compound engine, for so long as the initial steam-pressure and rate of expansion are the same, it signifies very little, so far as total power only is concerned, whether the ratio between the low and high-pressure cylinders is 3 or 4; but as the power developed should be nearly equally divided be-tween the two cylinders, in order to get a good and steady working engine, there is a necessity for exercising a considerable amount of discretion in fixing on the ratio.

In choosing a particular ratio the objects are to divide the power evenly and to avoid as much as possible "drop" and high initial strain.

If increased economy is to be obtained by increased boiler pressures, the rate of expansion should vary with the initial pressure, so that the pressure at which the steam enters the condenser should remain constant. In this case, with the ratio of cylinders constant, the cut-off in the high-pressure cylinder will vary inversely as the initial pressure.

Let R be the ratio of the cylinders; r, the rate of expansion;  $p_1$  the initial pressure: then cut-off in high-pressure cylinder =  $R \div r$ ; r varies with  $p_1$ ,

so that the terminal pressure  $p_n$  is constant, and consequently  $r = p_1 + p_n$ ; therefore, cut-off in high-pressure cylinder  $= R \times p_n + p_1$ .

Ratios of Cylinders as Found in Marine Practice.—The rate of expansion may be taken at one tenth of the boiler pressure for about one twelfth the absolute pressure), to work economically at full speed. Therefore, when the diameter of the low-pressure cylinder does not exceed 100 inches, and the boiler-pressure 70 bs., the ratio of the low-pressure to the high-pressure cylinder should be 3.5; for a boiler-pressure of 80 bs., 3.75 for 90 bs., 4.0; for 100 lbs., 4.5. If these proportions are adhered to, there will be no need of an expansion-valve to either cylinder. If, however, to avoid "drop," the ratio be reduced, an expansion-valve should be fitted to the high-pressure cylinder.

Where economy of steam is not of first importance, but rather a large power, the ratio of cylinder capacities may with advantage be decreased, so that with a boiler-pressure of 100 lbs. it may be 3.75 to 4.

In tandem engines there is no necessity to divide the work equally. The

ratio is generally 4, but when the steam-pressure exceeds 90 lbs, absolute 4.5 is better, and for 100 lbs, 5.0. When the power requires that the l. p. cylinder shall be more than 100 in.

diameter, it should be divided in two cylinders. In this case the ratio of the

combined capacity of the two 1, p. cylinders to that of the h. p. may be 3.0 for 85 lbs, absolute, 3.4 for 95 lbs., 3.7 for 105 lbs., and 4.0 for 115 lbs.

Receiver Space in Compound Engines should be from 1 to 1.5 times the capacity of the high-pressure cylinder, when the cranks are at an angle of from 90° to 120°. When the cranks are at 180° or nearly this, the space may be very much reduced. In the case of triple-compound engines with capacity the 190° capacity the space may be very much reduced. In the case of triple-compound engines with capacity 190° cand the intermediate acting the adding the highgines, with cranks at 120°, and the intermediate cylinder leading the high-pressure, a very small receiver will do. The pressure in the receiver should never exceed half the boiler-pressure. (Seaton.)

### Formula for Calculating the Expansion and the Work of Steam in Compound Engines,

(Condensed from Clark on the "Steam-engine.")

 $\alpha =$  area of the first cylinder in square inches; a' = area of the second cylinder in square inches;

r = ratio of the capacity of the second cylinder to that of the first;

τ = rans or the capacity of the second cylinder to that of the first;
 L = length of stroke in feet, supposed to be the same for both cylinders;
 l = period of admission to the first cylinder in feet, excluding clearance;
 c = clearance at each end of the cylinders, in parts of the stroke, in feet;
 L = period of admission plus the clearance, in feet;
 = length of a given part of the stroke of the second cylinder, in feet;
 = tool white a measurement in the fort white on the process of the second cylinder, in feet;

 $P = \text{total initial pressure in the first cylinder, in lbs. per square inch, sup$ posed to be uniform during admission;

P' = total pressure at the end of the given part of the stroke s:

p = average total pressure for the whole stroke; R = nominal ratio of expansion in the first cylinder, or L + l; R' = actual ratio of expansion in the first cylinder, or L' + l'; R'' = actual combined ratio of expansion, in the first and second cylinders

"a actual combined ratio of expansion, in the first cylinder to any intermediate fall of pressure between the first and second cylinders;

N = ratio of the final pressure in the first and second cylinders;

N = ratio of the volume of the intermediate space in the Woolf engine, reckoned up to, and including the clearance of, the second piston, to the capacity of the first cylinder plus its clearance. The value of N is correctly expressed by the actual ratio of the volumes as stated, on the assumption that the intermediate space is a vacuum when it receives the exhaust-steam from the first cylinder. In point of fact, there is a residuum of unexhausted steam in the intermediate space, at low pressure, and the value of N is thereby practically reduced below the ratio here stated.

w = whole net work in one stroke, in foot-pounds.

Ratio of expansion in the second cylinder:

In the Woolf engine, 
$$\frac{\left(r\frac{L}{L}\right) + N}{1 + N}$$
;

In the receiver engine,  $\frac{(n-1)r}{n}$ .

Total actual ratio of expansion = product of the ratios of the three consecutive expansions, in the first cylinder, in the intermediate space, and in the second cylinder,

In the Woolf engine, 
$$R'\left(r\frac{L}{L'}+N\right)$$
;  
In the receiver-engine,  $r\frac{L'}{L'}$ , or  $rR'$ .

Combined ratio of expansion behind the pistons =  $\frac{n-1}{r}R' = R''$ .

Work done in the two cylinders for one stroke, with a given cut-off and a given combined actual ratio of expansion:

Woolf engine, 
$$w = aP[l'(1 + \text{hyp log } R'') - c];$$
  
Receiver engine,  $w = aP\Big[l'(1 + \text{hyp log } R'') - c\Big(1 + \frac{r-1}{R'}\Big)\Big],$ 

when there is no intermediate fall of pressure.

When there is an intermediate fall, when the pressure falls to 34, 36, 16 of the final pressure in the 1st cylinder, the reduction of work is 0.2%, 1.0%, 4.6% of that when there is no fall,

Total work in the two cylinders of a receiver-engine, for one stroke for any intermediate fall of pressure.

$$w = aP \left[ l' \left( \frac{n+1}{n} + \text{hyp log } R'' \right) - c \left( 1 + \frac{(n-1)(r-1)}{nR'} \right) \right].$$

Example.—Let a=1 sq. in., P=63 lbs., l'=2.42 ft., n=4, R''=5.969, c=.42 ft., r=3, R'=2.653;

$$w = 1 \times 63 \left[ 2.42(5/4 \text{ hyp log } 5.969) - .42 \left( 1 + \frac{3 \times 2}{4 \times 2.653} \right) \right] = 421.55 \text{ ft.-lbs.}$$

Calculation of Diameters of Cylinders of a compound con-densing engine of 2000 H.P. at a speed of 700 feet per minute, with 100 lbs.

boiler-pressure. 100 lbs. gauge-pressure = 115 absolute, less drop of 5 lbs. between boiler and cylinder = 110 lbs. initial absolute pressure. Assuming terminal pressure in l. p. cylinder = 6 lbs., and taking the expansion in each cylinder to vary as the square root of the total expansion, we have:

Total expansion of steam in both cylinders =  $110 \div 6 = 18.33$ .

Expansion in each cylinder =  $\sqrt{18.33}$  = 4.28.

Point of cut-off in each cylinder, per cent of stroke,  $\frac{100}{4.98} = 23.36$ .

1 + hyp log of expansion in each cylinder = 1 + hyp log 4.28 = 2.454.

Terminal and back pressure of h. p. cyl. and initial of l. p. cyl.,  $\frac{110}{4.98}$ 

Average absolute pressure in h. p. cylinder, 
$$25.7 \times 2.454 = 63.07$$
 lbs. "effective " in "  $63.07 - 25.70 = 37.37$  " absolute " in l. p. "  $6 \times 2.454 = 14.72$  " effective " in "cyl. assum'g 3 lbs. back pres.=11.72

Assuming half the work, or 1000 H.P., to be done in the low-pressure cylinder,

Area of l. p. cyl. = 
$$\frac{33000 \times \text{H.P.}}{\text{piston-speed} \times \text{av. effective pressure}}$$

$$= \frac{33000 \times 1000}{700 \times 11.72} = 4023 \text{ sq. in.} = 71.6 \text{ in. diam.}$$

Area of h, p, cyl. =  $4023 \times \frac{11.72}{37.37} = \frac{33000 \times 1000}{700 \times 37.37} = 1262 \text{ sq. in.} = 40.1 \text{ in.} \text{ diam.}$ 

Ratios of cylinder areas =  $\frac{11.72}{37.87}$  = 1 to 3.189.

In this calculation no account is taken of clearance, nor of drop between cylinders, nor of area of piston-rod. It also assumes that the diagrams in both cylinders are the full theoretical diagrams, with hyperbolic expansion

ornes, with no allowance for rounding of the corners.

Culculation of Danmeters of Cylinders of a 500 H.P. Compound Non-condensing Engine.—Assuming initial pressure 170 lbs. above atmosphere, back pressure 15.5 lbs., absolute piston-speed 600 feet per minute.

Total Expansions  $=185 \div 15.5 = 11.9.$ Expansions in each cylinder  $= \sqrt{11.9} = 3.45$ ; hyp log = 1.238. =  $185 \div 3.45 = 53.6$  lbs. Terminal pressure h. p. cyl. Mean total pressure, " = 53.6 × (1 + 1.238) = 120.0. = terminal pressure 53.6 lbs. = 120 - 53.6 = 66.4 lbs. = 53.6 ÷ 3.45 = 15.5 lbs. = 15.5 × 2.238 = 34.7 lbs. Back pressure h. p. cyl. Mean effective pressure

Terminal pressure l. p. cyl. Mean total pressure Mean effective pressure l. p. cyl, = 34.7 - 15.5 = 19.2 lbs.

 $=\frac{10.2}{66.4}=1$  to 3.46. Ratio of areas of cylinders

Area of l. p. cvl. = 33000 × H.P.  $\frac{33000 \times 250}{600 \times 19.2}$  = 716 sq. in. = 30.2" diam, piston-speed × M.E.P.

Area of h. p. cyl.,  $716 \div 3.46 = 207$  sq. in. = 16.2 in, diameter,

### TRIPLE-EXPANSION ENGINES.

Proportions of Cylinders .- H. H. Suplee, Mechanics, Nov. 1887, gives the following method of proportioning cylinders of triple-expansion

engines:

As in the case of compound engines the diameter of the low-pressure cylinder is first determined, being made large enough to furnish the entire power required at the mean pressure due to the initial pressure and expansion ratio given; and then this cylinder is only given pressure enough to per-form one third of the work, and the other cylinders are proportioned so as to

divide the other two thirds between them.

Let us suppose that an initial pressure of 16 lbs. is used and that a 900 H.P. is to be developed at a piston-speed of 800 ft. per min., and that an expansion ratio of 16 is to be reached with an absolute back pressure of 2 lbs. The theoretical M.E.P. with an absolute initial pressure of 150 ts.

164.7 lbs. initial at 16 expansions is

$$\frac{P(1 + \text{hyp log 16})}{16} = 164.7 \times \frac{3.7726}{16} = 38.83,$$

less 2 lbs. back pressure, = 38.83 - 2 = 36.83. In practice only about 0.7 of this pressure is actually attained, so that  $36.83 \times 0.7 = 25.781$  lbs. 1s the M.E.P. proposition which the engine is to be proportioned.

To obtain 900 H.P. we must have  $33,000 \times 900 = 29,700,000$  foot-pounds, and this divided by the mean pressure (25.78) and by the speed in feet (800) will

give

$$\frac{33000 \times 900}{800 \times 25.78} = 1440$$
 sq. in.

for the area of the l. p. cylinder, which is about equivalent to 43 in. diam.

Now as one third of the work is to be done in the l. p. cylinder, the M.E.P.

in it will be  $25.78 \div 3 = 8.59$  lbs.

The cut-off in the high-pressure cylinder is generally arranged to cut off

The cut-off in the high-pressure cylinder is generally arranged to cut off at 0.6 of the stroke, and so the ratio of the h. p. to the 1. p. cylinder is equal to  $16 \times 0.6 = 9.6$ , and the h. p. cylinder will be 140 + 6 = 150 sq. in, area, or about 14 in diameter, and the M.E.P. in the h. p. cylinder is equal to  $9.6 \times 5.59 = 82.46$  lbs.

If the first meditate cylinder is made a mean size between the other two, its size would be determined by dividing the area of the l. p. cylinder by the square root of the ratio between the low and the high; but in practice this is found to give a result too large to equalize the stresses, so that instead the area of the l. p. cylinder is found by dividing the area of the l. p. piston by 1.1 times the square root of the ratio of l. p. to h. p. cylinder, which in this

case is  $1440 \div (1.1 \sqrt{9.6}) = 422.5 \text{ sq. in.}$ , or a little more than 23 in. diam. To put the above into the form of rules, we have

Area h. p. cyl. = 
$$\frac{\text{Area of low-pressure piston}}{\text{Cut-off in h. p. cyl.} \times \text{rate of expansion.}}$$

Area intermediate cyl. = 
$$\frac{\text{Area of low-pressure p'ston}}{1.1 \times \sqrt{\text{ratio of l. p. to h. p. cyl.}}}$$

The choice of expansion ratio is governed by the initial pressure, and is generally chosen so that the terminal pressure in the l. p. cylinder shall be about 10 lbs, absolute

Annular Ring Method, -Jay M. Whitham, Trans. A. S. M. E., x. 577, gives the following method of ascertaining the diameter of pistons of

triple expansion engines:

Lay down a theoretical indicator-diagram of a simple engine for the particular expansion desired. By trial find (with the polar planimeter or otherwise) the position of horizontal lines, parallel to the back-pressure line, such that the three areas into which they divide the diagram, representing low, intermediate, and high pressure diagrams, marked respectively A, B, and C,

Find the mean ordinate of each area: that of "C" will be the mean unbalanced pressure on the small piston; that of "B" will be the mean unbalanced pressure on the area remaining after subtracting the area of the small piston from that of the intermediate; and that of the area "A" will denote the mean unbalanced pressure on a square inch of the annular ring of the large piston obtained by subtracting the intermediate from the large piston. We thus see that the mean ordinates of the two lower cards act on annular rings.

Let H = area of small piston in square inches;

I = " intermediate piston in square inches; L = " large piston in square inches;

 $\dot{S}$  = piston-speed in feet per minute; (I.H.P.) = indicated horse-power of engine.

Then for equal work in each cylinder we have:

Area of small piston = 
$$H = 33,000 \times \frac{\text{I.H.P.}}{3} + (ph \times S);$$
 . . . . (2)

Area of annular ring of  $\left\{ = 33,000 \times \frac{\text{I.H.P.}}{3} \div (p_i \times S); \right\}$ 

Area of intermediate piston 
$$= I = H + 33,000 \times \frac{I.H.P.}{3} + (p_l \times S);$$
 . . (5)

Area of annular ring of large piston =  $33,000 \times \frac{\text{I.H.P.}}{3} + (p \times 8)$ ;

Area of large piston = 
$$L = I + 33,000 \times \frac{\text{I.H.P.}}{3} + (p_l \times S);$$
 . (3)

This method is illustrated by the following example: Given I.H.P. = 3000, piston-speed S = 900 ft, per min., ratio of expansion 10, initial steam-ressure at cylinder 127 lbs. absolute, and back-pressure in large cylinder 4 lbs. absolute. Find cylinder diameters for equal work in each.

The mean ordinate of "C" is found to be 
$$ph = 37.414$$
 lbs. per sq. in.
"""" "B""" """  $pi = 11.730$ """"

Then by (1), (2), and (3) we have:

$$H = 33,000 \times \frac{3000}{3} \div 37.414 \times 900 = 980$$
 sq. in., diam.  $85\%$ ";

$$I = 980 + 33,000 \times \frac{3000}{3} + 15.782 \times 900 = 3303$$
 sq. in., diam. 65";

$$L=3303+33,000\times\frac{300}{30}+11.730\times 900=6432~{\rm sq.\ in.,\ diam.\ 9014}$$
 Mr. Whitham recommends the following cylinder ratios when the piston-speed is from 750 to 1000 ft. per min., the terminal pressure in the large cylinder being about 10 lbs. absolute.

CYLINDER RATIOS RECOMMENDED FOR TRIPLE-EXPANSION ENGINES.

Boiler-pressure (Gauge).	Small.	Intermediate.	Large.
130	1	2.25	5.00
140	i	2.40	5.85
150	î	2.55	6.90
160	Ĩ	2.70	7.25
	ards—quadruple-q	expansion engine to b	

He gives the following ratios from examination of a number of actual engines:

No. of Engines	Steam-boiler		Cylinder Ratios.	
Averaged.	Pressure.	h. p.	int.	l. p.
9	130	1	2.10	4.88
3	135	1	2.07	5.00
11	140	1	2.40	5.84
2	145	1	2.35	5.23
28	150	ï	2.54	6.90
27	160	1	2.66	7.24

A Common Rule for Proportioning the Cylinders of multiple-expansion engines is: for two-cylinder compound engines, the cylinder ratio is the square root of the number of expansions, and for triple-expansion engines the ratios of the high to the intermediate and of the intermediate to the low are each equal to the cube root of the number of expansions, the ratio of the high to the low being the product of the two ratios, that is, the square of the cube root of the number of expansions. Applying this rule to the pressures above given, assuming a terminal pressure (absolute) of 10 lbs. and 8 lbs. respectively, we have, for triple-expansion engines:

Boiler-	Terminal	Pressure, 10 lbs.	Termina	l Pressure, 8 lbs.
(Absolute).	No. of Expansions.	Cylinder Ratios, areas.	No. of Expansions.	Cylinder Ratios, areas.
130 140 150 160	13 14 15 16	1 to 2.35 to 5.53 1 to 2.41 to 5.81 1 to 2.47 to 6.08 1 to 2.52 to 6.35	16¼ 17½ 18¾ 20	1 to 2.53 to 6.42 1 to 2.60 to 6.74 1 to 2.66 to 7.06 1 to 2.71 to 7.37

The ratio of the diameters is the square root of the ratios of the areas, and the ratio of the diameters of the first and third cylinders is the same as the

ratio of the areas of first and second.

Seaton, in his Marine Engineering, says: When the pressure of steam employed exceeds 115 lbs, absolute, it is advisable to employ three cylinders, through each of which the steam expands in turn. The ratio of the lowpressure to high-pressure cylinder in this system should be 5, when the steam-pressure is 125 lbs. absolute; when 135 lbs. absolute, 5.4; when 145 lbs, absolute, 5.8; when 155 lbs. absolute, 6.2; when 165 lbs. absolute, 6.6. The ratio of low-pressure to intermediate cylinder should be about one half The Faulto I low-pressure and high-pressure, as given above. That is, if the ratio of I. p. to h. p. is 6, that of I. p. to int, should be about 3, and consequently that of int, to h. p. about 2. In practice the ratio of int to h. p. is nearly 2.25, so that the diameter of the int. cylinder is 1.5 that of the h. p. The introduction of the triple-compound engine has admitted of ships being propelled at higher rates of speed than formerly obtained without exceeding the consumption of fuel of similar ships fitted with ordinary compound engines; in such cases the higher power to obtain the speed has been developed by decreasing the rate of expansion, the low-pressure cylinder being only 6 times the capacity of the high-pressure, with a working pressure of 170 lbs. absolute. It is now a very general practice to make the diameter of the low pressure cylinder equal to the sum of the diameters of the h. p. and int. cylinders; hence,

> Diameter of int, cylinder = 1.5 diameter of h, p, cylinder: Diameter of l, p, cylinder = 2.5 diameter of h, p, cylinder.

In this case the ratio of l. p. to h. p. is 6.25; the ratio of int. to h. p. is 2.25;

and ratio of 1, p. to int. is 2.78.

Ratios of Cylinders for Different Classes of Engines.

(Proc. inst. M. E., Feb. 1887, p. 36).—As to the best ratios for the cylinders in a triple engine there seems to be great difference of opinion. Considerable latitude, however, is due to the requirements of the case, inasmuch as it would not be expected that the same ratio would be suitable for an economical land engue, where the space occupied and the weight were of minor importance, as in a war-ship, where the conditions were reversed. In the land engine, for example, a theoretical terminal pressure of about 7 lbs, above absolute vacuum would probably be aimed at, which would give a ratio of capacity of high pressure to low pressure of 1 to 8½ or 1 to 8½ will at a war-ship a terminal pressure would be required of 12 to 13 lbs. which would need a ratio of capacity of 1 to 5; yet in both these instances the cylinders were correctly proportioned and suitable to the requirements of the case. It is obviously unwise, therefore, to introduce any hard-andfast rule.

Types of Three-stage Expansion Engines.—1. Three cranks at 120 deg. 2. Two cranks with 1st and 2d cylinders tandem. 3. Two cranks with 1st and 2d cylinders tandem. first, with cylinders arranged in the sequence high, intermediate, low.

Sequence of Cranks,-Mr. Wyllie (Proc. Inst. M. E., 1887) favors the sequence high, low, intermediate, while Mr. Mudd favors high, intermediate, low. The former sequence, high, low, intermediate, gave an approximately horizontal exhaust-line, and thus minimizes the range of temperature and the initial load; the latter sequence, high, intermediate, low, increased the range and also the load.

Mr. Morrison, in discussing the question of sequence of cranks, presented a diagram showing that with the cranks arranged in the sequence high, low, intermediate, the mean compression into the receiver was 191/2 per cent of the stroke; with the sequence high, intermediate, low, it was 57 per cent,

In the former case the compression was just what was required to keep the receiver-pressure practically uniform; in the latter case the compression caused a variation in the receiver-pressure to the extent sometimes of

2394 lbs. **Velocity of Steam through Passages in Compound Velocity of Steam through Passages in Compound Engines.** (Proc. lust. M. E., Feb. 1887.)—In the SS. *Para*, taking the area of the cylinder multiplied by the piston-speed in feet per second and dividing by the area of the port the velocity of the initial steam through the high-pressure cylinder port would be about 100 feet per second; the exhaust would be about 90. In the intermediate cylinder the initial steam had a velocity of about 180, and the exhaust of 120. In the low-pressure cylinder the initial steam entered through the port with a velocity of 250, and in the exhaust-port the velocity was about 140 feet per second.

### QUADRUPLE-EXPANSION ENGINES.

H. H. Suplee (Trans. A. S. M. E., x. 583) states that a study of 14 different quadruple-expansion engines, nearly all intended to be operated at a pressure of 180 lbs. per sq. in., gave average cylinder ratios of 1 to 2, to 3.78, to 7.70, or nearly in the proportions 1, 2, 4, 8.

If we take the ratio of areas of any two adjoining cylinders as the fourth root of the number of expansions, the ratio of the 1st to the 4th will be the cube of the fourth root. On this basis the ratios of areas for different pres-

sures and rates of expansion will be as follows:

		THE PERSON NAMED OF THE PE		
Gauge- pressures.	Absolute Pressures.	Terminal Pressures.	Ratio of Expansion.	Ratios of Areas of Cylinders.
160	175	12 10 8 12	14.6 17.5 21.9	1:1.95:3.81: 7.43 1:2.05:4.18: 8.55 1:2.16:4.68:10.12
180	195	12 10 8 12	16.2 19.5 24.4	1:2.01:4.02:8.07 1:2.10:4.42:9.28 1:2.22:4.94:10.98
200	215	10 8	17.9 21.5 26.9	1:2.06:4.23:8.70 1:2.15:4.64:9.98 1:2.28:5.19:11.81
220	235	12 10 8	19.6 23.5 29.4	1:2.10:4.43: 9.31 1:2.20:4.85:10.67 1:2.33:5.42:12.62

Seaton says: When the pressure of steam employed exceeds 190 lbs, absolute, four cylinders should be employed, with the steam expanding through each successively; and the ratio of l. p. to h. p. should be at least 7.5, and if economy of fuel is of prime consideration it should be 8; then the ratio

it economy or tuel is of prime consideration it should be 8; then the ratio of first intermediate to h. p. should be 1.8; that of second intermediate to first int. 2, and that of l. p. to second int. 2.3; In a paper read before the North East Coast Institution of Engineers and Shipbuilders, 1890, William Russell Cummins advocates the use of a four-cylinder engine with four cranks as being more suitable for high speeds than the three-cylinder three-crank engine. The cylinder ratios, he claims, should be designed so as to obtain equal initial loads in each cylinder. The ratios determined for the triple engine are 1, 2.04, 6.54, and for the quadruple 1, 2.08, 4.46, 10.47. He advocates long stroke, high piston speed, 100 revolutions per minute, and 250 lbs. boiler-pressure, unjacketed cylinders, and separate steam and exhaust valves.

### Diameters of Cylinders of Recent Triple-expansion Engines, Chiefly Marine.

Compiled from several sources, 1890-1893.

Diam. in inches: H = high pressure, I = intermediate, L = low pressure.

H	I	L	H	I	L	H	I	L	H	I	L
3 434 5 6.5 7 7.1 7.5 8 9 9.8 10 11 11 11.5 11.5 12.13	5 7.5 8 10.5 9 11.8 12.5 14.5 15.7 16 18 18 17.5 19.2 22.4	8 13 16.5 12.5 18.9 19 16 22.5 25.6 25 24 25 30 30.5 30.7 33.5	16 16!4 16.5 17 17 18 18 18.7 1834 19.7 20 20 20 21 21	25.6 287/8 24.5 27 26.5 28 27 29.5 29.5 29.6 30 32.5 33 32.5	41 38.5 31 44 42 45 40 48 51 43.3 35.4 47.3 45 46 51 36 52 48	23 23.5 24 25 26 26 28 29.5 29.5	36 38 38 37 40 42 42.5 44 44 48 46 51 54 55 55.1	40 61 60 56 64 69 70 77 78 77 70 82 82 88 84 69 90	36 38 28 28 39 40 40 41 4138 42 43 43 43 43 32.5 47	58 61.5 56 61 59 67 66 66 67 59 66 68 67 71 68	94 100 86 97 88 106 100 101 10634 92 110 1064 113 (85.7 (81.5
14 14.5 15 15	22.4 24 24 24.5	39 39 38	21.7 21.9 22	33.5 34 34	51 49.2 57 51	34.5 34.5	51 57	90 85 92	37 } 37 }	79	) 98 ) 98

Where the figures are bracketed there are two cylinders of a kind. Two 38'' = one 39.6'', two 31'' = one 43.8'', two 32.5'' = one 46.0', two 36'' = one 52.8'', two 37'' = one 52.8'', two 40'' = one 56.6'', two 81.5'' = one 15'', two 85.7'' = one 140''. The average ratio of diameters of cylinders of all the engines in the above table is nearly 1 to 1.60 to 2.56 and the ratio of areas nearly 1 to 2.56 to 6.55.

The Progress in Steam-engines between 1876 and 1893 is shown

The Progress in Steam-engines between 1876 and 1893 is shown in the following comparison of the Corliss engine at the Centennial Exhibition in 1876 and the Allis-Corliss quadruple-expansion engine at the Chicago

Exhibition.

	1893.	1876.
Engine	Quadruple-	Simple
Cylinders, number	4	2
" diameter	24, 40, 60, 70 in.	40 in.
" stroke	72 in.	120 in.
Fly-wheel, diameter	30 ft.	30 ft.
" width of face	76 in.	24 in.
" weight	136,000 lbs.	125,440 lbs.
Revolutions per minute	60	36
Capacity, economical	2000 H.P.	1400 H.P.
" maximum	3000 H.P.	2500 H.P.
Total weight	650,000 lbs.	1,360,588 lbs.

The crank-shaft body or wheel-seat of the Allis engine has a diameter of 21 inches, journals 19 inches, and crank bearings 18 inches, with a total length of 18 feet. The crank-disks are of cast iron and are 8 feet in diameter. The crank-pins are 9 inches in diameter by 9 inches long.

A Double-tandem Triple-expansion Engine, built by Watts, Campbell & Co., Newark, N. J., is described in An. Mack., April 20, 1894. It is two three-cylinder tandem engines coupled to one shaft, cranks at 90°, cylinders 21, 32 and 48 by 60 in. stroke, 65 revolutions per minute, rated H.P. 2000; fly-wheel 28 feet diameter, 12 ft. face, weight 174/000 bbs; main shaft 22 in. diameter at the swell; main journals 19 × 38 in.; crank-pins 9½ × 10 in.; distance between centre lines of two engines 24 ft. 1½ in.; Corliss valves, with separate eccentrics for the exhaust-valves of the 1.p. cylinder.

	Weight of En- gine, lbs.	65,000 55,000
93.	Size of Ex-	200 1 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2
m, 18	Size of Steam- pipe,	5
ositio	Revolutions per Minute,	64 1.2 2 11.2 2
an Exp	Driv. Pulley. Diameter in. Face, in.	888 8 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9 9
igun	I.H.P. Maxi- mum Load.	12.000 11.2500 11.2500 11.2500 12.0000 12.000 12.000 12.000 12.000 12.000 12.000 12.000 12.000 12.0000 12.000 12.00
CO.	I.H.P. Maxi- mum Econ- omy.	1,000 1,000
ne World?	Cylinders, ins. Diameters and Stroke.	H. 99, 93, 96, 70, 70, 70, 70, 70, 70, 70, 70, 70, 70
32	Horizontal or Vertical,	H:
Engines in the Fower, Flant at the World's Columbian Exposition,	Type of Engine.	quad, exp condensing— popule thank comp. cond. Double thank comp. cond. Comp. to the des media Comple tend, e engines Double tend, comp. cond. Proble tend, comp. cond. Comp. comp. and cond. Comp. cond. Double tend, comp. cond. Comp. comp. cond. Double tend, comp. cond. Comp. comp. cond. Double tend, comp. cond. Thirdie exp. condensing Thanden comp. cond. Thirdie exp. condensing Thirdie comp. cond. Thirdie cond. Thirdie comp. cond. Thirdie cond. Thirdie comp. Thirdie cond. Thirdie c
Frincipal Engines in	Name of Engine and where Built.	P. P. Allico, Milwouten  Pracer & Challmers, Chicago Modroscoperation, Allicano, Moscal Massallon, O.  Restalghouse, Pitfsburg, Ph.  Rassall, Massallon, O.  Basse, Parasilon, O.  Basse, Parasilon, O.  Basse, Massallon, O.  Selvichan, Germany, N.  N. Safety Steam-Power Co.  Selvichan, Germany, O.  Selvichan, Germany, N.  Massallon, Masse, O.  Basse, Massallon, O.  Basser, Massallo

\* Engine and dynamo.

### ECONOMIC PERFORMANCE OF STEAM-ENGINES. Economy of Expansive Working under Various Conditions, Single Cylinder.

(Abridged from Clark on the Steam Engine.)

1. SINGLE CYLINDERS WITH SUPERHEATED STEAM, NONCONDENSING.—Inside cylinder locomotive, yilinders and steam-pipes enveloped by the hot gases in the smoke-box. Net boiler pressure 100 lbs.; net maximum pressure in cylinders 80 lbs, per sq. in.

Cut-off, per cent..... 25 30 35 50 Actual ratio of expansion 3.91 3.31 2.87 2.53 2.26 1.86 1.59 1.39 1.23

20 21.2 22.2 24.5 20 2. SINGLE CYLINDERS WITH SUPERHEATED STEAM, CONDENSING.—The best 2. SIGGLE CYLINDERS WITH, with a cylinder 2334 % 67 in. and steam super-leated 150° F., expansion ratio 334 to 4½, total maximum pressure in cylinder 63 to 69 lbs. were 15.03 and 15.03 lbs. of water per I,H.P. per hour. 3. SINGLE CYLINDERS OF SMALL SIZE, 8 OR 9 IN. DIAM., JACKETED, NON-CONDENSING.—The best results are obtained at a cut-off of 20 per cent, with

75 lbs, maximum pressure in the cylinder; about 25 lbs, of water per I.H.P. per hour.

4. Single Cylinders, not Steam-Jacketed, Condensing, -Best results.

Engine.	Cylinder, Diam. and Stroke.	Cut-off.	Actual Expan- sion Ratio.	Total Maxi- mum Pressure in Cylin- der per sq. in.	Water as Steam per I.H.P. per hour.
Corliss and Wheelock Hirn, No. 6. Mair, M. Bache Dexter. Dallas Gallatin	$\begin{array}{c} \text{ins.} \\ 18 \times 48 \\ 2334 \times 67 \\ 32 \times 66 \\ 25 \times 24 \\ 26 \times 36 \\ 36 \times 30 \\ 30.1 \times 30 \end{array}$	per cent. 12.5 16.3 24.6 15.5 18.3 13.3 15.0	ratio. 6.95 5.84 3.84 5.32 4.46 5.07 4.94	lbs. 104.4 61.5 54.5 87.7 80.4 46.9 81.7	lbs. 19.58 19.93 26.46 26.25 23.86 26.69 21.89

SAME ENGINES, AVERAGE RESULTS.

Long Stroke.	Inches.	Cut-off, Per cent.	Lbs.	Lbs.
Corliss and Wheelock	18 × 48 23¾ × 67	12.5 16.3	104.4 61.5	19.58 19.93
Short Stroke.				
Bache	$25 \times 24$	15.5	87.7	26.25
Dexter, Nos. 20, 21, 22, 23	$26 \times 36$	18.3 to 33.3 } average 25 {	79.0	24.05
Dallas, Nos. 27, 28, 29	$36 \times 30$	3 13.3 to 26.4 i	46.8	26.86
Gallatin, Nos, 24, 25, 22, 1	30.1 × 30	( 40 0 - 40 - 1	78.2	23.50

Feed-water Consumption of Different Types of Engines. The following tables are taken from the circular of the Tabor Indicator —The following tables are taken from the circular of the Taoor Inducator (Ashcroft Mfg, Co., 1889). In the first of the two columns under Feed-water required, in the tables for simple engines, the figures are obtained by computation from nearly perfect indicator diagrams, with allowance for cylinder condensation according to the table on page 752, but without allowance for leakage, with back-pressure in the non-condensing table taken at 16 lbs, above zero, and in the condensing table at 3 lbs, above zero. The compression curve is supposed to be hyperbolic, and commences at 0.91 of the return-stroke, with a clearance of 3% of the piston-displacement.

Table No. 2 gives the feed-water consumption for jacketed compound-con-

densing engines of the best class. The water condensed in the jackets is included in the quantities given. The ratio of areas of the two cylinders are as 1 to 4 for 120 lbs, pressure; the clearance of each cylinder is 3%; and the cut off in the two cylinders occurs at the same point of stroke. The initial pressure in the l. p. cylinder is 10, per sq. in, below the back-pressure of the h. p. cylinder. The average back pressure of the whole stroke in the l. p. cylinder is 4.5 lbs, for 10% cut-off. 4.75 lbs, for 20% cut-off. The steam accounted for by the indicator at cut-off in the h. p. cylinder is allowing a small amount for leakage) is .74 at 10% cut-off. 7.8 at 20%, and .82 at 30% cut-off. The loss by condensation between the cylinders is such that the steam accounted for at cut-off in the 1. see 1 colliners. is such that the steam accounted for at cut-off in the l. p. cylinder, expressed in proportion of that shown at release in the h. p. cylinder, is .85 at

10% cut-off., 37 at 20% cut-off, and .89 at 30% cut-off.
The data upon which table No. 3 is calculated are not given, but the feed-water consumption is somewhat lower than has yet been reached (1894), the lowest steam consumption of a triple-exp. engine yet recorded being 11.7 lbs.

TABLE No. 1.

	Fred-water Consumption, Simple Engines.  Non-condensing Engines.    b   g   Fred-water Re-													
	Atmos-	Pressure,	Feed-wa quired pe per I	er I.H.P.		Atmos-	Pressure,	Feed-wa quired p per I	er I.H.P.					
Per Cent Cut-off.	Initial Pressure above Atmosphere, lbs.	Mean Effective Pr lbs.	Corresponding to Diagrams with no Leakage, lbs.	Corresponding to Actual Results Attained in Practice, assuming Slight Leakage.	Per Cent Cut-off.	Initial Pressure above Atmosphere, lbs.	Mean Effective Pr lbs.	Corresponding to Diagrams with no Leakage, Ibs.	Corresponding to Actual Results Attained in Practice, assuming Slight Leakage.					
10 {	60 70 80 90 100	8.70 12.39 16.07 19.76 23.45	37.26 30.99 27.61 25.43 23.90	40.95 33.68 29.88 27.43 25.73	5{	60 70 80 90 100	14.42 16.96 19.50 22.04 24.58	18.22 17.96 17.76 17.57 17.41	20.00 19.69 19.47 19.27 19.07					
20 {	60 70 80 90 100	21.12 26.57 32.02 37.47 42.92	27.55 25.44 21.04 23.00 22.25	29.43 27.04 25.68 24.57 28.77	10	60 70 80 90 100	22.34 26.03 29.72 33.41 37.10	17.68 17.47 17.30 17.15 17.02	19.34 19.09 18.89 18.70 18.56					
30 {	60 70 30 90 100	30.47 37.21 43.97 50.73 57.49	27.24 25.76 24.71 23.91 23.27	29.10 27.43 26.29 25.38 24.68	15 {	60 70 80 90 100	29.00 33.65 38.28 42.92 47.56	17.93 17.75 17.60 17.45 17.32	19.51 19.27 19.09 18.91 18.74					
407	60 70 80 90 100	37.75 45.50 53.25 61.01 68.76	27.92 26.66 25.76 25.03 24.47	29.63 28.18 27.17 26.35 25.73	20 {	60 70 80 90 100	34.73 40.18 45.63 51.08 56.58	18.58 18.40 18.27 18.14 18.02	20.09 19.85 19.69 19.51 19.36					
50 {	60 70 80 90 100	48.42 51.94 60.44 68.96 77.48	28.94 27.79 26.99 26.32 25.78	30.66 29.31 28.38 27.62 26.99	30 {	60 70 80 90 100	44.06 50.81 57.57 64.32 71.08	20.19 20.04 19.91 19.78 19.67	21.64 21.41 21.25 21.06 20.93					
					40 {	60 70 80 90 100	51.35 59.10 66.85 74.60 82.36	21.63 21.49 21.36 21.24 21.13	22.96 22.74 22.56 22.41 22.24					

TABLE No. 2. FEED-WATER CONSUMPTION FOR COMPOUND CONDENSING ENGINES.

Cut-	off.	Initial Pres Atmos	sure above phere.	Mean Effect Atmos	Feed-water Required		
per cent.		H.P. Cyl., lbs.	L.P. Cyl., lbs.	H.P. Cyl., lbs.	L.P. Cyl., lbs.	per I.H.P. per Hour, Lbs.	
10	{	80 100 120	4.0 7 3 11.0	11.67 15.33 18.54	2.65 3.87 5.23	16.92 15.00 13.86	
20	{	80 100 120	4.3 8.1 12.1	26.73 33.18 39.29	5.48 7.56 9.74	14.60 13.67 13.09	
30	}	80 100 120	4.6 8.5 11.7	37.61 46.41 56.00	7.48 10.10 12.26	14.99 14.21 13.87	

TABLE No. 3.

FRED-WATER CONSUMPTION FOR TRIPLE-EXPANSION CONDENSING ENGINES.

Cut-off,			Pressure mospher		Mean Ef	Feed-water Required			
	per cent.	H.P. Cyl., lbs.	I. Cyl., lbs.	L.P. Cyl., lbs,	H.P. Cyl., lbs.	I. Cyl., lbs.	L.P. Cyl., lbs.	per I.H.P. per Hour, lbs.	
	30 {	120 140 160	37.8 43.8 49.3	1.3 2.8 3.8	38.5 46.5 55.0	17.1 18.6 20.0	6.5 7.1 8.0	12.05 11.4 10.75	
	40 {	120 140 160	38.8 45.8 51.3	2.8 3.9 5.3	51.5 59.5 70.0	22.8 23.7 25.5	8.6 9.1 10.0	11.65 11.4 10.85	
	50 {	120 140 160	39.8 46.8 52.8	3.7 4.8 6.3	60.5 70.5 82.5	26.7 28.0 30.0	10.1 10.8 11.8	12.2 11.6 11.15	

Most Economical Point of Cut-off in Steam-engines. (See paper by Wolff and Denton, Trans, A. S. M. E., vol. ii, p. 147-281; also, Ratio of Expansion at Maximum Efficiency, R. H. Thurston, vol. ii, p. 128.)
—The problem of the best ratio of expansion is not one of economy of consumption of fuel and economy of cost of boiler alone. The question of interest on cost of engine, depreciation of value of engine, repairs of engine, etc., enters as well; for as we increase the rate of expansion, and thus, within certain limits fixed by the back-pressure and condensation of steam, demonstrate the amount of fuel regulard and expect of boiler per unit of work. decrease the amount of fuel required and cost of boiler per unit of work, we have to increase the dimensions of the cylinder and the size of the engine, to attain the required power. We thus increase the cost of the engine, etc., as we herease the rate of expansion, while at the same time we de-creave set herease the rate of expansion, while at the same time we de-creave set herease the rate of expansion, while at the rate of the re-very engine some point of cut-off, determinable by calculation and praphi-cal ture of money, taking into consideration the cost of fuely, wages of engineer and firemen, interest on cost, depreciation of value, repairs to and insurance of boiler and engine, and oil, waste, etc., used for engine. In case of freightcarrying vessels, the value of the room occupied by fuel should be considered in estimating the cost of fuel.

Sizes and Calculated Performances of Vertical High-Sizes and Calculated Performances of Vertical High-speed Engines.—The following tables are taken from a circular of the Field Engineering Co., New York, describing the engines made by the Lake Eric Engineering Works, Buffalo, N. Y. The engines are fair representatives of the type now coming largely into use for driving dynamos directly with-out belts. The tables were calculated by E. F. Williams, designer of the engines. They are here somewhat abridged to save space:

### Simple Engines-Non-condensing.

Diam. of Cyl- inder, inches.	Stroke, inches.	Revs. per Min- ute.	H.P. when Cutting off at 1/5 stroke.			H.P. when Cutting off at ¼ stroke.  70   80   90   1bs. lbs.			70 80 90			Dime sions Whee diam,	of els.	Steam-pipe, in.	Exhaust-pipe.
71/2 81/2 101/2 12 131/2 16 18 22 241/2 27	10 12 14 16 18 20 24 28 32 34	370 318 277 246 222 181 158 138 120 112	20 27 41 53 66 95 119 179 221 269	80 115 144	261 322	26 34 52 67 84 120 151 227 281 342	31 41 62 81 100 144 181 272 336 409	93	41 63 82 102 146 183 276 340	37 48 74 96 120 172 215 324 400 487	43 56 85 111 138 198 248 373 460 560	5'9'' 6'8'' 71'6 8'4'' 10 11'8''	34	21/2 23/4 31/2 4 4 41/2 5 6 7 8	3 31/2 4 41/2 5 6 7 8 9
Mean eff. press.lb. Ratio of expans'n Terminal pressure (about)lbs Cyl.condensat'n, Steam per I.H.P per hourlbs			17.9 26	26	22.3	30.5 36.5 42			29.8 21	33.3 21 31.4	36.8 21	NOTE The nominal-power rating of the er			

### Compound Engines - Non-condensing - High - pressure Cylinder and Receiver Jacketed.

Diam. Cylinder, inches.		hes.	inches. ons per ute.		H.P.when cutting H.P.when cutting off at ¼ Stroke in h.p. Cylinder, in h.p. Cylinder.					off	off at 1/2 Stroke				
inches	5.	Stroke, inc	Revolutions Minute.	Ra	Cyl. Ratio, 31/3:1.		Cyl. Ratio, 4½:1.		yl. tio, : 1.	Cyl. Ratio, 4½:1.		Cyl. Ratio, 31/3:1.		Cyl. Ratio 4½:1	
н.Р.	L.P.	Str	Rev	80 lbs.	90 lbs.	130 lbs.	150 lbs.	80 lbs.	90 lbs.	130 lbs.		80 lbs.	90 lbs.	130 lbs.	150 lbs.
	12 13½	10 12	370 318	7 9	15 19	19 24	32 40		31 39	35 45	59			81	79 101
9 101/2	16½ 19 22½	14 16 18	277 246 222	14 18 26	28 37 53	36 47 68	60 78 112	43 57 81	58 76 109	87 125	87 114 164	156	104 136 195	158 226	159 196 281
131/6 151/8	25 28½ 33½	20 24 28	185 158 138	32 43 57	65 88 118	84 112 151	139 186 249	100 135 180	135 181 242	154 206 277	202 271 363	192 258 346	241 323 433	279 374 502	346 464 623
18 2012 20 2212	38 43	32 34	120 112	74 94	152 194	194 249	321 412	232 297	312 400	357 457	468 601	446 572	558 715	647 829	803 1030
2812   33	52 60	42 48	93 80	138 180	285 374	365 477	603 789	436 570	767	670 877	880 1151	838 1096	1370	1215 1589	
Mean eff	Mean effec. presslbs		lbs		6.8			10.4	_	16	21	20	25	29	36
	Ratio of expansion				1/2		1/4		14_		334_	6		91	
Cyl. condensation, % Ter. press. (about).lbs				14 7.3	$\frac{14}{7.7}$	$\frac{16}{7.9}$	16 9	12 9.2	$\frac{12}{10.4}$	13 10.5	13 12	10 14	10 15.5	$^{11}_{14.6}$	11 17.8
Loss from expanding below atmosphere, & St per I.H.P. p. hr.lbs				34 55	15 42	17 47	3 29	5 33.3	$\frac{0}{27.7}$	0 28.7	0 25.4	0 30	$\frac{0}{26.2}$	0 21	0 20

The original table contains figures of horse-power, etc., for 110 and 120 lbs., cylinder ratio of 4 to 1; and 140 lbs., ratio  $4\frac{1}{2}$  to 1.

### Compound-engines-Condensing-Steam-jacketed.

		ber ;	off	whe at ½ .p. C	Str	ting oke der.	off at 1/3 Stroke in h.p. Cylinder.				off	H.P. when cutting off at 1/2 Stroke in h.p. Cylinder.				
Inches.		er, s.	Stroke, inc	Revolutions Minute.	Cyl. Ratio, 31/3:1.		Cyl. Ratio, 4:1.		Cyl, Ratio, 3½: 1.		Cyl. Ratio, 4:1.		Cyl. Ratio, 3½: 1.		Cyl. Ratio, 4:1.	
H.P.	H.P.	L.P.	Str	Rev	80 lbs.	110 lbs.	115 lbs.	125 lbs.	80 Ibs.	110 lbs.	115 lbs.	125 lbs.	80 lbs.	110 lbs.	115 lbs.	125 lbs.
6 6½ 8½ 814	61/2 71/2 9	12 131/6 161/6	10 12 14	370 318 277	44 56 83	59 76 112	53 67 100	62 78 116	55 70 104	70 90 133	68 87 129	75 95 141	70 90 133	97 123 183	120	134
9½ 11 12½	10½ 12 13½	19 22½	16 18 20	246 222 185	109 156 192		131 187 231	152 218 269			169 242 298	185 265 327	174 250 308	343	335	374
14 17	151/2 181/2	281/2 331/2	24 28	158 138	258 346	348 467	310 415	361 484	323 433	413 554	400 536	439 588	413 554	568	555 744	619 830
19 21 26	201/2 221/2 281/6	43	32 34 42	120 112 93	446 572 838	602 772 1131	686	624 801 1174	558 715 1048	915	691 887 1299	758 972 1425	714 915 1341	1258	959 1230 1801	1373
30 Mag				$\frac{1480}{27}$	1316	1534	1370 25	1757 32	1699 31	1863 34	1757 32	2411	2356	2632		
Rati	Ratio of Expansion			on	131/2		16	31/4	1	0	1214		63/4		81/4	
Cyl. St. 1	Cyl. condensation, % St. per I.H.P. p. hr.lbs				$ ^{18}_{17.3}$	$ ^{18}_{16.6}$	20 16.6	$\frac{20}{15.2}$	15 17.0	15 16.4	18 16.3		12 17.5	$\frac{12}{17.0}$	14 16.8	14 16.0

The original table contains figures for 95 lbs., cylinder ratio 31/4 to 1; and 120 lbs., ratio 4 to 1.

## Triple-expansion Engines, Non-condensing.—Receiver only Jacketed.

Diameter Cylinders, inches.		ke, inches.	Revolutions per Minute.	when off at cent of in Firs	-power Cutting 42 per Stroke t Cylin- er.	when off at cent of in First	power Cutting 50 per Stroke t Cylin- er.	Horse-power when Cutting off at 67 per cent of Stroke in First Cylin- der.			
Н. Р.	I. P.	L. P.	Stroke,	Rev	180 lbs.	200 lbs.	180 lbs.	200 lbs.	180 lbs.	200 lbs	
43/4	71/2	12	10	370	55	64	70	84	95	108	
516	81/5	131/2	12	318		81	90	106	120	137	
51/2 61/2 71/2	81/2 101/2	161%	14	277	104	121	133	158	179	204	
71/2	12	19	16	246	136	158	174	207	234	267	
9 ~	141/2	221/6	18	222	195	226	250	296	335	382	
10	16	25	20	185	241	279	308	366	414	471	
111/2	18	281/2	24	158		374	413	490	555	632	
13	22	331/6	28	138	433	502	554	657	744	848	
15	241/2	38	32	120	558	647	714	847	959	1093	
17	27 ~	43	34	112	715	859	915	1089	1230	1401	
20	33	52	42	93	1048	1215	1341	1592	1801	2053	
231/2	38	60	48	80	1370	1589	1754	2082	2356	2685	
Mean	effectiv	ve pres	ss.,	lbs.	25	29	32	38_	43	49	
	No. of expansions			6 -	1		1				
Per cent cyl. condens		1	4	1	2	10	)				
Steam	p. I.H	.P. p.1	r.,	lbs.	20.76	19.36	19.25	17.00	17.89	17.20	
					2.59	2.39	2.40	2.12	2.23	2.15	
	Lbs. coal at 8 lb. evap. lbs.   2.59   2.39   2.40   2.12   2.23   2.15										

#### Triple-expansion Engines-Condensing-Steam-Jacketed.

Diameter Cylinders, inches.		when Cut-			Horse-power when Cut- ting off at ½ Stroke in First Cylin- der.			when Cut- ting off at 1/2 Stroke in			Horse-power when Cut- ting off at 34 Stroke in First Cylin- der.					
H.P.	I.P.	L.P.	Stroke,	Revolutions Minute.	120 lbs.			120 lbs.				140 lbs.	160 lbs.	120 lbs.	140 lbs.	
43/ 51/3 61/3 71/2 9 10 111/3 13 15 17 20	14½ 16 18 22 24½ 27 33	16½ 19	10 12 14 16 18 20 24 28 32 34 42 48	870 318 277 246 222 185 158 138 120 112 93 80	206 277 357 458 670	53 79 103 148 183 245 329 424 543 796	62 92 120 172 212 284 381 491 629	56 83 109 156 192 258 346 446 572 888		76 112 147 211 260 348 467 602 772 1181	73 108 141 203 250 335 450 580 744 1089		84 107 159 208 299 368 494 663 854 1095 1605 2099	289 356 477 640 825 1058	183 239 343 423 568 761 981 1258 1844	272 390 481 645 865 1115 1430 2096
Mea	23½ 38  60   48   80  Mean effec. press.,lbs.  No. of expansions			,lbs.	16			20		27	26		38.3	37		-
Per cent cyl. condens. St. p. I.H.P. p. hr., lbs. Coal at 8 lb. evap., lbs.		14.7	13.9	19 13.3 1.66	16 14.3 1.78	16 13.98	16 13.2 1.65	12 14.3 1.78	12 13.6 1.70	$12 \\ 13.0 \\ 1.62$	8 15.7 1.96	8 14.9 1.86	8 14.2 1.77			

Type of Engine to be used where Exhaust-steam is needed for Heating,—In many factories more or less of the steam exhausted from the engines is utilized for boiling, drying, heating, etc. Where all the exhaust-steam is so used the question of economical use of steam in the engine itself is eliminated, and the high-pressure simple engine is entirely suitable. Where only part of the exhaust-steam is used, and the quantity so used varies at different times, the question of adopting a simple, a condensing, or a compound engine becomes more complex. This problem is treated by C. T. Main in Trans. A. S. M. E., vol. x. p. 48. He shows that the ratios of the volumes of the cylinders in compound engines should vary according to the amount of exhaust-steam that can be used for heating. A case is given in which three different pressures of steam are required or could be used, as in a worsted dye-house: the high or boiler pressure for the engine, an intermediate pressure for cabbing, and low-pressure for boiling, drying, etc. If it did not make too much complication of parts in the engine, the boiler-pressure might be used in the high-pressure cylinder, exhausting into a receiver from which steam could be taken for running small engines and crabbing, the steam remaining in the receiver passing into the intermediate cylinder and expanded there to from 5 to 10 lbs, above the atmosphere and exhausted into a second receiver. From this receiver is drawn the low-pressure steam needed for drying, boiling, warming mills; etc., the steam remaining in treceived condensing cylinder.

Comparison of the Economy of Compound and Singlecylinder (orliss Condensing Engines, each expanding about Sixteen Times. (D. S. Jacobus, Trans. A. S. M. E., xii. 945.)

The engines used in obtaining comparative results are located at Stations I. and II. of the Pawtucket Water Co.

The tests show that the compound engine is about 30% more economical than the single-cylinder engine. The dimensions of the two engines are as follows: Single 20"  $\times$  48"; compound 15" and 301%"  $\times$  30". The steam used per horse-power per hour was: single 20.35 lbs., compound 13.73 lbs.

Both of the engines are steam-jacketed, practically on the barrels only, with steam at full boiler-pressure, viz. single 106.3 lbs., compound 127.5 lbs.

The steam-pressure in the case of the compound engine is 127 lbs., or 21 lbs. higher than for the single engine. If the steam-pressure be raised this amount in the case of the single engine, and the indicator-cards be increased accordingly, the consumption for the single-cylinder engine would be 19,97

lbs, per hour per horse-power.

Two-cylinder vs. Three-cylinder Compound Engine.—
A Wheelock triple-expansion engine, built for the Merrick Thread Co.,
Holyoke, Mass., is constructed so that the intermediate cylinder may be cut out of the circuit and the high-pressure and low-pressure cylinders run as a two-cylinder compound, using the same conditions of initial steam-pressure and load. The diameters of the cylinders are 12, 16, and 2443 inches, the stroke of the first two being 36 in. and that of the low-pressure cylinder 48 in. The results of a test reported by S. M. Green and G. I. Rockwood, Trans. A. S. M. E., vol. xiii. 647, are as follows: In lbs. of dry steam used per I.H.P. per hour, 12 and 2413 in. cylinders only used, two tests 13.06 and 12.76 lbs., average 12.91. All three cylinders used, two tests 12.67 and 12.90 lbs., average 12.79. The difference is only 1%, and would indicate that more than two cylinders are unnecessary in a compound engine, but it is pointed out by Prof. Jacobus, that the conditions of the test were especially favorable for the two-cylinder engine, and not relatively so favorable for the three cylinders. The steam-pressure was 142 lbs. and the number of expansions about 25. (See also discussion on the Rockwood type of engine, Trans. A. S. M. E., vol. xvi.)

Effect of Water contained in Steam on the Efficiency of the Steam-engine. (From a lecture by Walter C. Kerr, before the Franklin Institute, 1891.) -Standard writers make little mention of the effect of entrained moisture on the expansive properties of steam, but by common consent rather than any demonstration they seem to agree that moisture produces an ill effect simply to the percentage amount of its presence. That is, 5g moisture will increase the water rate of an engine 5g. Experiments reported in 1893 by R. C. Carpenter and L. S. Marks, Trans.

A. S. M. E., xv., in which water in varying quantity was introduced into the steam-pipe, causing the quality of the steam to range from 99% to 58% dry, showed that throughout the range of qualities used the consumption of dry steam per indicated horse-power per hour remains practically constant, and indicated that the water was an inert quantity, doing neither good nor harm.

It appears that the extra work done by the heat of the entrained water during expansion is sensibly equal to the extra negative work which it does during exhaust and compression, that the heat carried in by the entrained

during exhaust and compression, that the near carried in by the entrained water performs no useful function, and that a fair measure of the economy of an engine is the consumption of dry and saturated steam.

Relative Commercial Economy of Best Modern Types of Compound and Triple-expansion Engines. (J. E. Denton, American Machinist, Dec. 17, 1891.)—The following table and deductions show the relative commercial economy of the compound and triple type for the best stationary practice in steam plants of 500 indicated horse-power. The table is based on the tests of Prof. Schröter, of Munich, of engines built at Augsburg, and those of Geo. H. Barrus on the best plants of America, and of detailed estimates of cost obtained from several first-class builders.

Trip motion, or Corliss engines of the twin-compound-receiver condensing type, expanding 16 times. Boiler pressure 120 lbs. Trip motion, or Corliss engines of

	Lbs. coal per hour per	)
	H.P., assuming 8.5 lbs.	- 1.6
	actual evaporation.	)
2	Lbs. water per hour per	12.5
	H.P., by measurement.	۱۵.0
	Lbs. coal per hour per	
	H.P., assuming 8.5 lbs.	- 1.4
	actual evaporation.	)

H.P., by measurement.

Lbs. water per hour per 13.6

14.0

1.65

12.80

1.50

the triple-expansion four-cylinder-receiver condensing type, expanding 22 times. Boiler pressure, 150 lbs.

The figures in the first column represent the best recorded performance (1891), and those in the second column the probable reliable performance. Increased cost of triple-expansion plant per horse-power, including boilers, chimney, heaters, foundations, piping and erection ..... \$4.50

The following table shows the total annual cost of operation, with coal at \$4.00 per ton, the plant running 300 days in the year, for 10 hours and for 24 hours per day:

Hours running per day	10	24
Expense for coal. Compound plant Expense for coal. Triple plant	Per H.P. \$9.90 9.00 0.90	Per H.P. \$28.50 25.92 2.60
Annual interest at 5% on \$4.50	\$0.23 0.23	\$0.23 0.23
day, at \$0.50, or 15% of extra fuel cost Annual extra cost of repairs at 3% on \$4.50 per 24 hours	0.15 0.06	0.36 0.14
	\$0.67	\$0.96
Annual saving per H.P.	\$0.23	\$1.64

The saving between the compound and triple types is much less than that involved in the step from the single-expansion condensing to the compound engine. The increased cost per horse-power of the triple plant over the compound is due almost entirely to the extra cost of the triple engine and its foundations, the boilers costing the same or slightly more, owing to their extra strength. In the case of the single versus the compound, however, about one third of the increased cost of the compound engine is offset by the less cost of the latter's boilers.

Taking the total cost of the plants at \$33.50, \$36.50 and \$41 per horsepower respectively, the figures in the table imply that the total annual sav-

ing is as follows for coal at \$4 per ton:

1. A compound 500 horse-power plant costs \$18,250, and saves about \$1630 for 10 hours' service, and \$485 for 24 hours' service, per year over a single plant costing \$16,750. That is, the compound saves its extra cost in 10-hour service in about one year, or in 24-hour service in four months.

2. A triple 500 horse-power plant costs \$20,500, and saves about \$114 per year in 10-hour service, or \$826 in 21-hour service, over a compound plant, thereby saving its extra cost in 10-hour service in about 19% years, or in 24-

hour service in about 23/4 years

Triple - expansion Pumping-engine at Milwaukee-Highest Economy on Record, 1893. (See paper on "Maxinum Contemporary Economy of the Steam-engine," by R. H. Thurston, Trans. A. S. M. E. xv. 313.)—Cylinders 28, 48 and 74 in. by 60 in. stroke; ratios of volumes 1 to 3 to 7; total number of expansions 19.55; clearances, h.p. 1.4%; int. 1.5%; l. p. 0.77%; volume of receivers: 1st, 101.3 cu. ft.; 2d, 181 cu. ft.; steam-pressure gauge during test, average 121.5 lbs.; vacuum 13.84 lbs. absolute; revolutions 20.3 per minute; indicated horse-power, b.p. 175.4, int. 169.6, l. p. 228.9; total, 573.9; total friction, horse-power 52.91 = 9.225; dry steam per LH.P. per hour 11.678; B.T.U. per LH.P. per min. 217.6; duty in foot-pounds per 100 lbs. of coal, 143,306,000; per million B.T.U., 137,656,000.

Steam per I.H.P. per hour, from diagram, at cut-off	9.35	9.12	8,37
" " " " release	10.1		8.92
Steam accounted for by indicator at cut-off, per cent	87.1	85.0	78.2
" " release, "	94.0	93.2	83.2
Per cent of total steam used by jackets	9.25		

Highest Economy of the Two-cylinder Compound Pumping-engines.—Repeated tests of the Pawtucket-Corliss engine, 15 and 30½ by 30 in. stroke, gave a water consumption of 13.69 to 14.16 lbs. per hour. Steam-pressure 123 lbs.; revolutions per min. 49 lbs.; expansions about 16. Cylinders jacketed. The lowest water rate was with jackets in use; both jackets supplied with steam of boiler pressure. average saving due to jackets was only about 21/2 per cent. (Trans. A. S. M. E., xi. 328 and 1038; xiii. 176.)

This record was beaten in 1894 by a Leavitt pumping-engine at Louisville, Ky. (Trans. A. S. M. E. xvi.) Cylinders 27.21 and 54,13 in. diam. by 10 ft stroke; revolutions per min. 18.57; piston speed 37.15 ft.; expansions 20.4; steam-pressure, gauge, 140 lbs. Cylinders and receiver jacketed. Steam

used per I.H.P. per hour, 12.223 lbs. Duty per million B.T.U. = 138,126,000 ft.-lbs.

Test of a Triple-expansion Pumping-engine with and without Jackets, at Laketon, Ind., by Prof. J. E. Denton (Trans. A. S. M. E., xiv. 1340).—Cylinders 24, 34 and 54 in. by 36 in. stroke; 28 revs. per min.; H. P. developed about 329; bolier-pressure 150 lbs. Tests made on eight different days with different sets of conditions in jackets. At 150 lbs, boiler-pressure, and about 29 expansions, with any pressure above 43 lbs, in all of the jackets and reheaters, or with no pressure in the high jacket, the performance was as follows: With 2.5% of moisture in the steam entering the engine, the jackets used 16% of the total feed-water. About 20% of the latter was condensed during admission to the high cylinder, and about 13.85 lbs. of feed-water was consumed per hour per indicated horse-power. With no jackets or reheaters in action the feed-water consumption was 14.99 lbs, or 8.3% more than with jackets and reheaters. The consumption of lubricating oil was two thirds of a gallon of machine oil and one and three quarter gallons of cylinder oil per 24 hours. The friction of the engine in eight tests on different days varied from 5.1% to 8.7%.

If we regard the measurements of indicated horse-power and water as liable to an error of one per cent, which is probably a minimum allowance for the most careful determinations, the steam economy is the same for the

following conditions:

(a) Any pressure from 43 to 131 in the intermediate and low jackets and receivers.

(b) Any pressure from 0 to 151 in the jacket of high cylinder.
(c) Any cut-off from 21s to 23s in high cylinder, from 39s to 43s in intermediate cylinder, from 40s to 53s in low cylinder.

### Water Consumption of Three Types of Sulzer Engines.

(B. Donkin, Jr., Eng'g, Jan. 15, 1892, p. 77.)

SUMMARY AND AVERAGES OF TWENTY-ONE PUBLISHED EXPERIMENTS OF THE SULZER TYPE OF STEAM-ENGINE. ALL HORIZONTAL CONDENSING AND STEAM-JACKETED. From 1872 to 1891.

Type of Engine.	Steam-pressure above Atmos- phere.	Piston-speed.	Indicated Horse-power.	Steam Consump- tion, pounds per I.H.P. per hour, including Steam- pipe water and Jacket Water.	Steam Consump- tion, pounds per I.H.P. per hour, exclud'g Steam- pipe water, but including Jacket Water.	arks,
Single {    Cyl, {    Com. }    pound. }  Triple {	lbs. 72 to 95 84 to 104 104 to 156	ft. per min 272 to 433 384 to 689 444 to 607	157 to 400 133 to 524 198 to 615	lbs. { 18.7 to 19 8 } Mean 19.4 { 13.35 to 16.0 } Mean 14.44 } 11.85 to 12.86 } Mean 12.36	lbs. 17.9 to 19.2 Mean 18.95 13.4 to 15.5 Mean 14.8 11.7 to 12.7 Mean 12.18	5 exp. 1872-78 10 exp. 1888-91 6 exp. 1888-89

Triple-expansion Corliss engine at Narragansett E. L. Co., Providence, R. I., built by E. P. Allis Co. Cylinder 14, 25 and 33 in, by 48 in, stroke tested at 99 revs. per min.; 125 lbs. steam-pressure; steam per I.H.P. per hour 12. 94 lbs.; H.P. 516. A full account of this engine, with records of tests is given by J. T. Henthorn, in Trans. A. S. M. E., xii. 643.

Buckeye-cross compound engine, tested at Chicago Exposition, by Geo.

Relative Economy of Compound Non-condensing Engines under Variable Loads,—F. M. Rites, in a paper on the Steam bistribution in a Form of Single-acting Engine (Trans. A. S. M. E. xiii. 537), discusses an engine designed to meet the following problem: Given an

extreme range of conditions as to load or steam-pressure, either or both, to fluctuate together or apart, violently or with easy gradations, to construct an engine whose economical performance should be as good as though the engine were specially designed for a momentary condition—the adjustment to be complete and automatic. In the ordinary non-condensing compound engine with light loads the high-pressure cylinder is frequently forced to supply all the power and in addition drag along with it the low-pressure piston, whose cylinder indicates negative work. Mr. Rites shows the peculiar value of a receiver of predetermined volume which acts as a clearance chamber for compression in the high-pressure cylinder. The Westinghouse compound single-acting engine is designed upon this principle. The following results of tests of one of these engines rated at 175 H.P. for most economical load are given:

WATER RATES UNDER VARVING LOADS, LBS. PER H.P. PER HOUR.

Horse-power 2	10 17	0 140	115	100	80	50
Non-condensing 29	2.6 21.	9 22.2	22.2	22.4	24.6	28.8
Condensing 18						

Efficiency of Non-condensing Compound Engines, (W. Lee Church, Am. Mach., Nov. 19, 1891.)—The compound engine, non-condensing, at its best performance will exhaust from the low-pressure cylinder at a pressure 2 to 6 pounds above atmosphere. Such an engine will be limited in its economy to a very short range of power, for the reason that its valve-motion will not permit of any great increase beyond its rated power, and any condensity and the state of the reason that its valve-motion will not permit of any great the recease beyond its rated expensive cylinders at the property of the reason that the control of the reason of load tells upon the compound engine. The loss commences the moment the expansion line crosses a line parallel to the atmospheric line, and at a distance above it representing the mean effective pressure necessary to carry the frictional load of the engine. When expansion falls to this point the low-pressure cylinder becomes an air-pump over more or less of its stroke, the power to drive which must come from the high pressure cylinder alone. Under the light loads common in many industries the low-pressure cylinder is thus a positive resistance for the greater portion of its stroke. A careful study of this problem revealed the functions of a fixed intermediate clearance, always in communication with the high-pressure cylinder that the high-pressure cylinder becomes an interpret and the subsequent performance of the engines, of which some 600 have been built, have fully confirmed the judgment of the designes.

The effect of this constant clearance is to supply sufficient steam to the low-pressure cylinder under light loads to hold its expansion curve up to atmosphere, and at the same time leave a sufficient clearance volume in the high-pressure cylinder to permit of governing the engine on its compression

under light loads.

Economy of Engines under Varying Loads. (From Prof. W. C. Unwin's lecture before the Society of Arts, London, 1892.)—The general result of numerous trials with large engines was that with a constant load an indicated horse-power should be obtained with a consumption of 1½ pounds of coal per indicated horse-power for a condensing engine, and 1½ pounds for a non-condensing engine, figures which correspond to about 1½ pounds to 2½ pounds of coal per effective horse-power. It was much more difficult to ascertain the consumption of coal in ordinary every-day work, but such facts as were known showed it was more than on trial.

but such facts as were known showed it was more than on trial.

In electric-lighting stations the engines work under a very fluctuating load, and the results are far more unfavorable. An excellent Williams non-condensing engine, which on full-load trials worked with under 2 pounds per effective horse-power hour, in the ordinary daily working of the station used 7½ pounds per effective horse-power hour in 1886, which was reduced to 4.3 pounds in 1890 and 3.8 pounds in 1891, Probably in very few cases were the engines at electric-light stations working under a consumption of 4½ pounds per effective horse-power hour. In the case of small isolated motors working with a fluctuating load, still more extravagant results were obtained.

### Engines in Electric Central Stations.

Year	1886.	1890.	1892.
Coal used per hour per effective H.P	8.4	5.6	4.9
" " " indicated "	6.5	4.35	3.8

At electric-lighting stations the load factor, viz., the ratio of the average load to the maximum, is extremely small, and the engines worked under very unfavorable conditions, which largely accounted for the excessive fuel consumption at these stations.

In steam-engines the fuel consumption has generally been reckoned on the indicated horse-power. At full-power trials this was satisfactory enough, as the internal friction is then usually a small fraction of the total.

Experiment has, however, shown that the internal friction is nearly constanding the property of the property

Experiments on a Corliss engine at Creusot gave the following results:  $0.75 \\ 0.79$ 0.50 0.125Effective power at full load ..... 1.0 0.82 0.74 0.48 Condensing, mechanical efficiency..... 0.63 ..... 0.86 0.83 0.78 0.52 0.67 Non condensing,

At light loads the economy of gas and liquid fuel engines fell off even more rapidly than in steam-engines. The engine friction was large and nearly constant, and in some cases the combustion was also less perfect at light loads. At the Dresden Central Station the gas-engines were kept working at nearly their full power by the use of storage-batteries. The results of some experiments are given below:

Brake load, per Gas-engine, cu. ft. of Gas per Brake Petroleum Eng., Petroleum Eng., cent of full Lbs.of Oil per Lbs. of Oil per B.H.P. per hr. 0.96 H.P. per hour. B.H.P. per hr. 0.88 Power. 100 75 23.8 1.11 0.9959 28.0 1.44 1.20 20 40.8 2.38 1.82 66.3 4.25 3.07

Steam Consumption of Engines of Various Sizes,—W. C. Unwin (Cassier's Magazine, 1894) gives a table showing results of 49 tests of engines of different types. In non-condensing simple engines, the steam consumption ranged from 65 lbs, per hour in a 5-horse-power engine to 22 lbs, in a 134-H.P. Harris-Corliss engine. In non-condensing compound engines, the only type tested was the Wilans, which ranged from 27 lbs. in a 10 H.P. slow-speed engine, 122 ft. per minute, with steam-pressure 67 84 lbs. to 192 lbs. in a 40-H.P. engine, 40 ft. per minute, with steam-pressure 165 lbs. A. Willans triple-expansion non-condensing engine, 39 H.P., 172 lbs. pressure, and 400 ft. piston speed per minute, gave a consumption of 18.5 lbs. In condensing engines, nine tests of simple engines gave results ranging only from 18.4 to 22 lbs., and, leaving out a beam pumping-engine running at slow speed (240 ft. per minute) and low steam-pressure (45 lbs.), the range is only from 18.4 to 19.8 lbs. In compound-condensing engines over 100 H.P., in 13 tests the range is from 18.9 to 20 lbs. In three triple-expansion engines the figures are 11.7, 12 2, and 12.45 lbs., the lowest being a Sulzer engine of 360 H.P. In marine compound engines, the Fusiyama and Colchester, tested by Prof. Kennedy, gave steam consumption of 21.2 and 21.7 lbs.; and the Meteor and Tartar triple-expansion engines gave 15.0 and 19.8 lbs.

Taking the most favorable results which can be regarded as not exceptional, it appears that in test trials, with constant and full load, the expenditure of steam and coal is about as follows:

Per Indicated HorsePer Effective Horse-

Kind of Engine.		Hour.	power Hour.		
Kind of Engine.	Coal, lbs.	Steam, lbs.	Coal,		
Non-condensing	. 1.80	16.5 13.5	2.00 1.75	18.0 15.8	

These may be regarded as minimum values, rarely surpassed by the most efficient machinery, and only reached with very good machinery in the favorable conditions of a test trial.

ravorance conditions of a rest trial.

Small Engines and Engines with Fluctuating Loads are usually very wasteful of fuel. The following figures, illustrating their low economy, are given by Prof. Unwin, Cassier's Magazine, 1894.

COAL CONSUMPTION PER INDICATED HORSE-POWER IN SMALL ENGINES.

#### In Workshops in Birmingham, Eng.

45 Probable I.H.P. at full load... Average I.H.P. during obser-12 45 60 60 60 2.96 7.37 8.2 8 6 23 64 19.08 20.08 vation.

Coal per I.H.P. per hour during observation, lbs...... 36.0 21,25 22,61 18.13 11.68 9.53 8.50

It is largely to replace such engines as the above that power will be distributed from central stations.

### Steam Consumption in Small Engines.

Tests at Royal Agricultural Society's show at Plymouth, Eng. Engineering, June 27, 1890.

Rated H.P.		Diam. of Cylinders.		Stroke,	Max. Steam-	Per Bi	rater er lb.,	
	Simple.	h.p.	l.p.	ins.	pressure.	Coal.	Water.	¥ % O
5 3	simple compound		6	10 6	75 110	4.82	78.1 lbs. 42.03 "	8.72 "
2	simple	41/2		71/9	75	11.77	89.9 "	7.64 "

Steam-consumption of Engines at Various Speeds. (Profs. Denton and Jacobus, Trans. A. S. M. E., x. 722)—17 × 30 in. engine, non-condensing, fixed cut-off, Meyer valve.

STEAM-CONSUMPTION, LBS. PER I.H.P. PER HOUR.

Figures taken from plotted diagram of results.

8 12 16 20 24 32 72 88 Revs. per min..... 40 56 1/8 cut-off, lbs..... 39 35 32 30 29.3 29 28.7 28.5 28.3 28 39 34 31 29.5 29 28.428 26.3 36 39 34 33 30.8 29.8 29.2 28.8

STEAM-CONSUMPTION OF SAME ENGINE; FIXED SPEED, 60 REVS. PER MIN.

Varying cut-off compared with throttling-engine for same horse-power and boiler-pressures:

Cut-off, fraction of stroke 0.1 0.15 0.2 0.25 0.3 0.4 0.5 0.6 0.7 27 Boiler-pressure, 90 lbs... 29 27.5 27.2 27.8 28.5 60 lbs... 39 34.2 32.2 31.5 31.4 31.6 32.2 34.1 36.5 39

THROTTLING-ENGINE, % CUT-OFF, FOR CORRESPONDING HORSE-POWERS. Boiler-pressure, 90 lbs... 42 37 33.8 31.5 29.8 60 lbs... .... 50.1 49 46.8 44.6 41

Some of the principal conclusions from this series of tests are as follows: 1. There is a distinct gain in economy of steam as the speed increases for 25, 5, and ½ cut-off at 90 lbs, pressure. The loss in economy for about ½ cut-off is at the rate of 1/12 lb. of water per H.P. for each decrease of a revolution per minute from 80 to 26 revolutions, and at the rate of 55 lb. of water below 26 revolutions. Also, at all speeds the ½ cut-off is more economical than either the ½ or ½ cut-off.

2. At 90 lbs. boller-pressure and above ½ cut-off, to produce a given H.P.

requires about 20% less steam than to cut off at % stroke and regulate by the

throttle.

3. For the same conditions with 60 lbs. boiler-pressure, to obtain, by throttling, the same mean effective pressure at 76 cut-off that is obtained by

cutting off about 1/2, requires about 30% more steam than for the latter condition.

High Piston-speed in Engines. (Proc. Inst. M. E., July, 1883, p. 321).—The torpedo bat is an excellent example of the advance towards high speeds, and shows what can be accomplished by studying lightness and strength in combination. In running at 22½ knots an hour, an engine with cylinders of 16 in. stroke will make 480 revolutions per minute, which gives 1280 ft, per minute for piston-speed; and it is remarked that engines running at that high rate work much more smoothly than at lower speeds, and that the difficulty of lubrication diminishes as the speed increases.

A High-speed Corliss Engine. -A Corliss engine, 20 × 42 in., has been running a wire-rod mill at the Trenton Iron Co.'s works since 1877, at 160 revolutions or 1120 ft. piston-speed per minute (Trans. A. S. M. E., ii. 72). A piston-speed of 1200 ft. per min. has been realized in locomotive practice

The Limitation of Engine-speed. (Chas. T. Porter, in a paper on the Limitation of Engine-speed, Trans. A. S. M. E., xiv. 806.)—The practical limitation to high rotative speed in stationary reciprocating steamengines is not found in the danger of heating or of excessive wear, nor, as is generally believed, in the centrifugal force of the fly-wheel, nor in the is generally believed, in the centritugal force of the ny-wheel, nor in the tendency to knock in the centres, nor in vibration. He gives two objections to very high speeds: First, that "engines ought not to be run as fast as they can be;" second, the large amount of waste room in the port, which is required for proper steam distribution. In the important respect of economy of steam, the high-speed engine has thus far proved a failure. Large gain was looked for from high speed, because the loss by condensation on a given surface would be divided into a greater weight of steam, but this expectation has not been realized. For this unsatisfactory result we have to lay the blame chiefly on the excessive amount of waste room, ordinary method of expressing the amount of waste room in the percentage added by it to the total piston displacement, is a misleading one. It should be expressed as the percentage which it adds to the length of steam admis-For example, if the steam is cut off at 1/5 of the stroke, 8% added by the waste room to the total piston displacement means 40% added to the volume of steam admitted. Engines of four, five and six feet stroke may properly be run at from 700 to 800 ft. of piston travel per minute, but for ordinary sizes, says Mr. Porter, 600 ft. per minute should be the limit.

Influence of the Steam-jacket.—Tests of numerous engines with

and without steam-jackets show an exceeding diversity of results, ranging all the way from 30% saving down to zero, or even in some cases showing au actual loss. The opinions of engineers at this date (1894) is also as diverse as the results, but there is a tendency towards a general belief that the jacket is not as valuable an appendage to an engine as was formerly supposed. An extensive résumé of facts and opinions on the steam-jacket is given by Prof. Thurston, in Trans. A. S. M. E., xiv. 462. See also Trans. A. S. M. E., xiv. 462. See also Trans. A. S. M. E., xiv. 473 and 1340; xiii. 176; xiii. 426 and 1340; xiii. 476; xiii. 426 and 1340; xiii. 476; xiii. 426 and 1340; xiii. 476; xiii. 486 and 1340; xiii. 476; xiii. 486 and xiii. 476; xiii. 476;

The following are a few statements selected from these papers.

The results of tests reported by the research committee on steam-jackets appointed by the British Institution of Mechanical Engineers in 1886, indicate an increased efficiency due to the use of the steam-jacket of from 1% to

over 30%, according to varying circumstances.

Sennett asserts that "it has been abundantly proved that steamjackets are not only advisable but absolutely necessary, in order that high rates of expansion may be efficiently carried out and the greatest possible

economy of heat attained."

Isherwood finds the gain by its use, under the conditions of ordinary practice, as a general average, to be about 20% on small and 8% or 9% on large engines, varying through intermediate values with intermediate sizes, it being understood that the jacket has an effective circulation, and that both heads and sides are jacketed.

Professor Unwin considers that "in all cases and on all cylinders the jacket is useful; provided, of course, ordinary, not superheated, steam is used; but the advantages may diminish to an amount not worth the interest

on extra cost."

Professor Cotterill says: Experience shows that a steam-jacket is advantageous, but the amount to be gained will vary according to circumstances. In many cases it may be that the advantage is small. Great caution is necessary in drawing conclusions from any special set of experiments on the influence of jacketing.

Mr. E. D. Leavitt has expressed the opinion that, in his practice, steam-jackets produce an increase of efficiency of from 15% to 20%. In the Pawtucket pumping engine, 15 and 20½ × 30 in., 50 revs, per min., steam-pressure 125 lbs. gauge, cut-off ½ in h.p. and ½ in l.p. cylinder, the barrels only jacketed, the saving by the jackets was from ½ to 4%. The superintendent of the Holly Mfg. Co. (compound pumping-engines) says: "In regard to the benefits derived from steam-jackets on our steam-cylinders, I am somewhat of a skeptic. From data taken on our own engines and tests made I am yet to be convinced that there is any practical value in the steam-jacket." . "You might practically say that there is no difference." is no difference.

Professor Schröter from his work on the triple-expansion engines at Augs-Professor Schröder from his work on the triple-expansion engines at Augsburg, and from the results of his tests of the jacket efficiency on a small engine of the Sulzer type in his own laboratory, concludes: (1) The value of the jacket may vary within very wide limits, or even become negative. (2) The shorter the cut-off the greater the gain by the use of a jacket. (3) The use of higher pressure in the jacket than in the cylinder produces an advantage. The greater this difference the better. (4) The high-pressure cylinder may be left unjacketed without great loss, but the others should always be jacketed.

others should always be jacketed.

The test of the Laketon triple-expansion pumping-engine showed a gain
of 8.3% by the use of the jackets, but Prof. Denton points out (Trans. A., M. E., xiv. 1412) that all but 1.3% of the gain was ascribable to the greater

range of expansion used with the jackets.

Test of a Compound Condensing Engine with and with-out Jackets at different Loads, R. C. Carpenter, Trans. A. S. M. E., xiv. 428, — Cylinder 9 and 10 in. X14 in. stroke; 112 lbs. boller-pressure; rated capacity 100 H.P.; 265 revs. per min. Vacuum, 23 in. From the results of several tests curves are plotted, from which the following principal figures are taken.

Indicated H.P....... 30 40 50 60 70 80 90 Steam per I.H.P. per hour:

This table gives a clue to the great variation in the apparent saving due to the steam-jacket as reported by different experimenters. With this particular engine it appears that when running at its most economical rate of 100 H.P., without jackets, very little saving is made by use of the jackets. When running light the jacket makes a considerable saving, but when overloaded it is a detriment.

At the load which corresponds to the most economical rate, with no steam in jackets, or 100 H.P., the use of the jacket makes a saving of only 1% but at a load of 60 H.P. the saving by use of the jacket is about 11%, and the shape of the curve indicates that the relative advantage of the jacket would be still greater at lighter loads than 60 H.P.

Counterbalancing Engines.—Prof. Unwin gives the formula for counterbalancing vertical engines:

in which  $W_1$  denotes the weight of the balance weight and p the radius to its centre of gravity,  $W_2$  the weight of the crank-pin and half the weight of the connecting-rod, and r the length of the crank. For horizontal engines:

$$W_1 = \frac{2}{3}(W_2 + W_3)\frac{r}{p}$$
 to  $\frac{3}{4}(W_2 + W_3)\frac{r}{p}$ , . . . . . (2)

in which  $W_3$  denotes the weight of the piston, piston-rod, cross-head, and the other half of the weight of the connecting-rod.

The American Machinist, commenting on these formulæ, says: For horizontal engines formula (2) is often used; formula (1) will give a counterbalance too light for vertical engines. We should use formula (2) for computing the counterbalance for both horizontal and vertical engines, excepting locomotives, in which the counterbalance should be heavier.

Preventing Vibrations of Engines .- Many suggestions have been made for remedying the vibration and noise attendant on the working of the big engines which are employed to run dynamos. A plan which has given great satisfaction is to build hair-felt into the foundations of the An electric company has had a 90-horse-power engine removed from its foundations, which were then taken up to the depth of 4 feet. A layer of felt 5 inches thick was then placed on the foundations and run up 2 feet on all sides, and on the top of this the brickwork was built up. -Safety Valve.

Steam-engine Foundations Embedded in Air. - In the sugarrefinery of Claus Spreckels, at Philadelphia, Pa., the engines are distributed practically all over the buildings, a large proportion of them being on upper floors. Some are bolted to iron beams or girders, and are consequently innocent of all foundation. Some of these engines ran noiselessly and satisfactorily, while others produced more or less vibration and rattle. To correct the latter the engineers suspended foundations from the bottoms of the engines, so that, in looking at them from the lower floors, they were literally

hanging in the air.—Iron Age, Mar. 13, 1890.

Cost of Coal for Steam-power.—The following table shows the amount and the cost of coal per day and per year for various horse-powers, from 1 to 1000, based on the assumption of 4 lbs, of coal being used per hour per horse-power. It is useful, among other things, in estimating the saving that may be made in fuel by substituting more economical boilers and engines for those already in use. Thus with coal at \$3.00 per ton, a saving of \$9000 per year in fuel may be made by replacing a steam plant of 1000 H.P., requiring 4 lbs. of coal per hour per horse-power, with one requiring only 2 lbs.

	Coa per H day	l Consu i.P. per y ; 300 d	mption hour; lays in a	, at 4 l 10 hou a Year	bs. irs a	\$1.	50.	\$2	.00.	\$3	.00.	\$4.	00.
Horse-power.	Lbs.	Long	Tons.	She		Per Short Ton.		Per Short Ton.		Per Short Ton.		Per Short Ton,	
Horse	Per Day.	Per Day.	Per Year.	Per Day.	Per Year	Cos Doll	Per	Per	st in lars.	Per	st in llars.	Per	Per
1 10 25 56 75 100 150 200 250 300 350 400 450 500	40 1,000 2,000 3,000 4,000 6,000 10,000 12,000 14,000 16,000 18,000 20,000	4.4642 5.3571 6.2500 7.1428 8.0356 8.9285	5.357 53.57 133.92 267.85 401.78 535.71 800.56 1,071.42 1,339.27 1,607.13 1,874.98 2,112.84 2,410.69 2,678.55	.02 .20 .50 1.50 2.00 3.00 4.00 5.00 6.00 7.00 9.00	6 60 150 300 450 600 900 1,200 1,800 2,100 2,400 2,700 3,000	.03 .30 .75 1.50 2.25 3.00 4.50 6.00 7.50 9.00 10.50 12.00 13.50	Year 99 90 225 450 675 900 1,850 1,850 2,250 2,700 3,150 3,600 4,050 4,050 4,500	.04 .40 1.00 2.00 3.00 4.00 6.06 8.00 12.00 14.00 18.00 18.00 20.00 20.00	120 300 600 900 1,200 2,400 3,000 4,200 4,800 5,400 6,000	Day.  .06 .60 1.50 3.00 4.50 6.00 12.00 12.00 12.00 21.00 21.00 27.00 30.00	18 180 450 900 1,350 1,800 2,700 4,500 5,400 6,200 7,200 8,100 9,000 1,0	40.00	9,600 10,800 12,000
600 700 800 900 1,000	28,000 32,000 36,000	12.4999 14.2856 16.0713	3,214.26 3,749.97 4,285.68 4,821.39 5,357.10	12,00 14,00 16,00 18,00 20,00	3,690 4,200 4,800 5,400 6,000	18.00 21.00 24.00 27.00 30.00	5,400 6,300 7,200 8,100 9,000	24.00 28.00 32.00 36.00 40.00	7,200 8,400 9,600 10,800 12,000	36,00 42,00 48,00 54,00 60,00	10,800 11,600 12,400 14,200 18,000	56.00 64.00 72.00	14,400 16,800 19,200 21,600 24,000

Storing Steam Heat .- There is no satisfactory method for equalizing the load on the engines and boilers in electric-light stations. Storage-batteries have been used, but they are expensive in first cost, repairs, and attention, Mr. Halpin, of London, proposes to store heat during the day in specially constructed reservoirs. As the water in the boilers is raised to 250 lbs. pressure, it is conducted to cylindrical reservoirs resembling English horizontal boilers, and stored there for use when wanted. In this way a comparatively small boiler plant can be used for heating the water to 250 lbs. pressure all through the twenty-four hours of the day, and the stored water may be drawn on at any time, according to the magnitude of the demand. The drawn on at any time, according to the magnitude of the demand.

steam-engines are to be worked by the steam generated by the release of precsure from this water, and the valves are to be arranged in such a way that the steam shall work at 130 lbs, pressure. A reservoir 8 ft. in diameter and 30 ft. long, containing 84,000 lbs, of heated water at 250 lbs, pressure, would supply 5250 lbs, of steam at 130 lbs, pressure. As the steam consumption of a condensing electric-light engine is about 18 lbs, per horse-power hour, such a reservoir would supply 286 effective horse-power hours. In 1878, in France, this method of storing steam was used on a tramway. M. Francq, the engineer, designed a smokeless locomotive to work by steam-power supplied by a reservoir containing 400 gallons of water at 220 lbs, pressure. The reservoir was charged with steam from a stationary boiler at one end of the transway.

Cost of Steam-power. (Chas. T. Main, A. S. M. E., x. 48.)—Estimated costs in New England in 1888, per horse-power, based on engines of 1000 H.P.

		Compound		Non-con- densing
		Engine.	ing Engine.	Engine.
1.	Cost engine and piping, complete	\$25.00	\$20.00	\$17.50
	Engine-house		7.50	7.50
3.	Engine foundations	7.00	5.50	4.50
4.	Total engine plant	40.00	33.00	29.50
			==	
	Depreciation, 4% on total cost		1.32	1.18
	Repairs, 2% " " "		0.66	0.59
			1.65	1.475
	Taxation, 1.5% on 34 cost		0.371	0.332
9.	Insurance on engine and house	0.165	0.138	0.125
10.	Total of lines 5, 6, 7, 8, 9	5.015	4.139	3,702
44	Clark hallows for A service and	0.22	10.00	16.00
11.	Cost boilers, feed-pumps, etc	9.33 2.92	13.33 4.17	5.00
	Chimney and flues		7.30	8.00
10.	Ciliminey and nues	0.12	1.00	0.00
14.	Total boiler-plant	18,36	24.80	29.00
15	Depreciation, 5% on total cost		1.240	1.450
	Repairs, 2% " " "	367	.496	.580
	Repairs, 2% " " "	918	1.240	1.450
18.	Taxation, 1.5% on 34 cost		.279	.326
	Insurance, 0.5% on total cost		.124	.145
20.	Total of lines 15 to 19	2.502	3.379	3.951
			2.50	
21.	Coal used per I.H.P. per hour, lbs	1.75	2.50	3.00
22.	Cost of coal per I.H.P. per day of 1	01/4 cts.	cts.	cts.
	hours at \$5.00 per ton of 2240 lbs	4.00	5.72	6.86
	Attendance of engine per day	0.60	0.40	0.35
24.	" " boilers " "		0.75	0.90
25.	Oil, waste, and supplies, per day	0.25	0.22	0.20
26.	Total daily expense	5,38	7.09	8.31
27.	Yearly running expense, 308 days, 1	er \$16.500	\$21.837	\$25.595
98	I.H.P. Total yearly expense, lines 10, 20, and 2	7 24.087	29,355	33,248
29.	Total yearly expense per I.H.P. for pov	ver		
	if 50% of exhaust-steam is used for he	at-		
	ing	12.597	14.907	16.663
30.	Total if all exsteam is used for heating	8.624	7.916	7.700

When exhaust-steam or a part of the receiver-steam is used for heating, or if and used for other purposes than power, the value of such steam should

he deducted from the cost of the total amount of steam generated, in order to arrive at the cost properly chargeable to power. The figures in lines 29 and 30 are based on an assumption made by Mr. Main of losses of heat amounting to 25% between the boiler and the exhaust-pipe, an allowance which is probably too large.

### ROTARY STEAM-ENGINES.

Steam Turbines .- The steam turbine is a small turbine wheel which rnns with steam as the ordinary turbine does with water. (For description of the Parsons and the Dow steam turbines see Modern Mechanism, p. 298, etc.) The Parsons turbine is a series of parallel-flow turbines mounted side by side on a shaft; the Dow turbine is a series of radial outward-flow turbines, placed like a series of concentric rings in a single plane, a stationary guide-ring being between each pair of movable rings. The speeds of the steam turbines enormously exceed those of any form of engine with reciprocating piston, or even of the so-called rotary engines. The three- and foureylinder engines of the Brotherhood type, in which the several cylinders are usually grouped radially about a common crank and shaft, often exceed 1000 revolutions per minute, and have been driven, experimentally, above 2000; but the steam turbine of Parsons makes 10,000 and even 20,000 revolutions, and the Dow turbine is reputed to have attained 25,000. (See Trans. A. S. M. E., vol. x. p. 680, and xii. p. 888; Trans. Assoc. of Eng'g Societies, vol. viii. p. 583; Eng'g, Jan. 13, 1888, and Jan. 8, 1892; Eng'g News, Feb. 27, 1892.) A Dow turbine, exhibited in 1889, weighed 68 lbs., and developed 10 H P., with a consumption of 47 lbs. of steam per H. P. per hour, the steam pressure being 70 lbs. The Dow turbine is used to spin the fly-wheel of the Howell torpedo. The dimensions of the wheel are 13.8 In. diam., 6.5 in. per min. is 500,000 ft.-lbs.

The De Laval Steam Turbine, shown at the Chicago exhibition. cylinder engines of the Brotherhood type, in which the several cylinders

The De Laval Steam Turbine, shown at the Chicago exhibition, 1893, is a reaction wheel somewhat similar to the Pelton water-wheel. The steam jet is directed by a nozzle against the plane of the turbine at quite a small angle and tangentially against the circumference of the medium periphery of the blades. The angle of the blades is the same at the side of admission and discharge. The width of the blade is constant along the

entire thickness of the turbine.

The steam is expanded to the pressure of the surroundings before arriving at the blades. This expansion takes place in the nozzle, and is caused simply by making its sides diverging. As the steam passes through that channel its specific volume is increased in a greater proportion than the cross section of the channel, and for this reason its velocity is increased, and also its momentum, till the end of the expansion at the last sectional area of the nozzle. The greater the expansion in the nozzle the greater its velocity at this point. A pressure of 75 lbs. and expansion to an absolute pressure of one atmosphere give a final velocity of about 2625 ft. per second.

Expansion is carried further in this steam turbine than in ordinary steam-engines. This is on account of the steam expanding completely during its

work to the pressure of the surroundings

For obtaining the greatest possible effect the admission to the blades must be free from blows and the velocity of discharge as low as possible. conditions would require in the steam turbine an enormous velocity of periphery—as high as 1300 to 1650 ft. per second. The centrifugal force, nevertheless, puts a limit to the use of very high velocities. In the 5 horsepower turbine the velocity of periphery is 574 ft. per second, and the num-

ber of revolutions 30,000 per minute.

However carefully the turbine may be manufactured it is impossible, on account of unevenness of the material, to get its centre of gravity to correspond exactly to its geometrical axle of revolution; and however small this difference may be, it becomes very noticeable at such high velocities. De Laval has succeeded in solving the problem by providing the turbine with a flexible shaft. This yielding shaft allows the turbine at the high rate of speed to adjust itself and revolve around its true centre of gravity, the centre line of the shaft meanwhile describing a surface of revolution.

In the gearing-box the speed is reduced from 30,000 revolutions to 3000

by means of a driver on the turbine shafts, which sets in motion a cog-wheel of 10 times its own diameter. These gearings are provided with spiral cogs placed at an angle of about 45°. The shaft of the larger cog-wheel, running at a speed of 3000 revolutions, is provided at its outer end with a pulley for the further transmission of the power.

Rotary Steam-engines, other than steam turbines, have been invented by the thousands, but not one has attained a commercial success. The possible advantages, such as saving of space, to be gained by a rotary engine are overbalanced by its waste of steam.

The Tower Spherical Engine, one of the most recent forms of rotary-engine, is described in Proc. list. M. E., 1885, also in Modern Mechanism, p. 296.

### DIMENSIONS OF PARTS OF ENGINES.

The treatment of this subject by the leading authorities on the steam-engine is very unsatisfactory, being a confused mass of rules and formulæ based partly upon theory and partly upon practice. The practice of builders shows an exceeding diversity of opinion as to correct dimensions. The treatment given below is chiefly the result of a study of the works of Rankine, treatment given below is chieff the result of a study of the works of Rankine, Seaton, Unwin, Thurston, Marks, and Whitham, and is largely a condensa-tion of a series of articles by the author published in the American Ma-chinist, in 1894, with many alterations and much additional matter. In or-

chivist, in 1894, with many alterations and much additional matter. In order to make a comparison of many of the formulæ they have been applied to the assumed cases of six engines of different sizes, and in some cases this comparison has led to the construction of new formulæ.

Cylinder. (Whitham.)—Length of bore = stroke + breadth of piston-ring - ½ to ½ in; length between heads = stroke + thickness of piston + sum of clearances at both ends; thickness of piston = breadth of ring + thickness of flange on one side to carry the ring = + thickness of follower-

plate.

Thickness of flange or follower... 3% to ½ in. For cylinder of diameter..... 8 to 10 in. 34 in. 36 in. 60 to 100 in.

Clearance of Piston. (Seaton.)—The clearance allowed varies with the size of the engine from ½ to ¾ in. for roughness of castings and 1/16 to ¼ in. for each working joint. Naval and other very fast-running engines have a larger allowance. In a vertical direct-acting engine the parts which wear so as to bring the piston nearer the bottom are three, viz., the shaft journals, the crank-pin brasses, and biston-rod gndgeon-brasses.

Thickness of Cylinder. (Thurston.)—For engines of the older types and under moderate steam-pressures, some builders have for many years restricted the stress to about 2550 lbs, per sq. in.

is a common proportion; t, D, and b being thickness, diam., and a constant sadded quantity varying from 0 to  $\frac{1}{2}$  in., all in inches;  $p_1$  is the initial unbalance steam-pressure per sq. in. In this expression b is made larger for horizontal than for vertical cylinders, as, for example, in large engines 0.5 in the one case and 0.2 in the other, the one requiring re-boring more than the other. The constant a is from 0.0004 to 0.0005; the first value for vertical cylinders, or short strokes; the second for horizontal engines, or for long strokes.

Thickness of Cylinder and its Connections for Marine Engines. (Seaton). - D = the diam, of the cylinder in inches: p = load on the safety-valves in lbs. per sq. in.; f, a constant multiplier = thickness of

barrel + .25 in.

Thickness of metal of cylinder barrel or liner, not to be less than  $p \times D$  + 3000 when of cast iron.\* . . .

" liner =  $1.1 \times f$ ...... (4)

Thickness of liner when of steel  $p \times D \div 6000 + 0.5$  "metal of steam-ports =  $0.6 \times f$ .
"valve-box sides =  $0.65 \times f$ .

<sup>\*</sup> When made of exceedingly good material, at least twice melted, the thickness may be 0.8 of that given by the above rules.

Whitham gives the following from different authorities:

$$\begin{aligned} & \text{Van Buren: } \left\{ \begin{array}{l} t = 0.0001Dp + 0.15 \, \sqrt{D}; & (5) \\ t = 0.03 \, \sqrt{Dp}. & (6) \end{array} \right. \\ & \text{Tredgold: } t = \frac{(D+2.5)p}{1900}. & (7) \\ & \text{Weisbach: } t = 0.8 + 0.00033pD. & (8) \\ & \text{Seaton: } t = 0.5 + 0.0004pD. & (9) \\ & \text{Haswell: } \left\{ \begin{array}{l} t = 0.0004pD + \frac{1}{2}6 \, (\text{vertical}); & (10) \\ t = 0.0005pD + \frac{1}{2}6 \, (\text{horizontal}). & (11) \end{array} \right. \end{aligned}$$

Whitham recommends (6) where provision is made for the reboring, and where ample strength and rigidity are secured, for horizontal or vertical cylinders of large or small diameter; (9) for large cylinders using steam under 100 lbs. gauge-pressure, and

This is a smaller value than is given by the other formulæ quoted; but Marks says that it is not advisable to make a stcam-cylinder less than 0.75 in, thick under any circumstances.

The following table gives the calculated thickness of cylinders of engines of 10, 30, and 50 in. diam., assuming p the maximum unbalanced pressure on the piston = 100 lbs. per sq. in. As the same engines will be used for calculation of other dimensions, other particulars concerning them are here given for reference.

### DIMENSIONS, ETC., OF ENGINES.

Engine No	1 and 2.	3 and 4.	5 and 6.
Indicated horse-power I.H.P. Diam. of cyl., in $D$ Stroke, feet $L$ Levs. per min. $r$ Piston speed, ft. per min. $S$ Area of piston, sq. in $a$ Mean effective pressure $M$ Max. total unbalanced press $P$ Max. total $p$ P Max. $p$ Max. $p$ P Max. $p$ Max.	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	450 30 21/2 5 130 65 650 706.86 32.3 70,686 100	1950 50 4 8 90 45 700 1963.5 30 196,350 100

THICKNESS OF CYLINDER BY FORMULA.	1 and 2.	3 and 4.	5 and 6.
(1) .0004pD + 0.5, short stroke	.90	1.70	2.50
(1) $.0005pD + 0.5$ , long stroke	1.00	2.00	3.00
(2) .00033pD	.33	.99	1 67
(3) $.0002pD + 0.6$	.80	1.40	1.60
(5) $.0001pD + .15 \sqrt{D}$	.57	1.12	1.56
(6) .03 \(\sqrt{Dp}\)	.95	1.64	2.12
(7) $\frac{(D+2.5)}{1900} p$	.66	1.71	2.76
(8) $.00033pD + 0.8$	1.13	1.79	2.45
(9) $.0004pD + 0.5$	.90	1.70	2.50
$10) .0004pD + \frac{1}{2}$ (vertical)	.53	1.33	2.13
11) $.0005pD + \frac{1}{8}$ (horizontal)	.63	1.63	2.63
12) $.003D \sqrt{p}$ (small engines)	.30(?)		
13) .00028pD	.28(?)	.84(?)	1.40(?)
Average of first eleven	.76	1.48	2.26

The average corresponds nearly to the formula t = .00037Dp + 0.4 in. convenient approximation is t = .0004Dp + 0.3 in., which gives for

10 20 30 40 50 Diameters ..... 60 in. Thicknesses..... .70 1.10 1.50 .1.90 2.30 2.70 in.

The last formula corresponds to a tensile strength of cast iron of 12,500 lbs., with a factor of safety of 10 and an allowance of 0.3 in. for reboring. Cylinder-heads, -Thurston says: Cylinder-heads may be given a

Cylinder-neads, a line deges and in the flanges, exceeding somewhat that of the cylinder. An excess of not less than 25% is usual. It may be thinner in the middle. Where made, as is usual in large engines, of two disks with intermediate radiating, connecting ribs or webs, that section which is safe against shearing is probably ample. An examination of the designs of experienced builders, by Professor Thurston, gave

Thurston also gives  $t = .005D \sqrt{p} + 0.25$ .

He also says a good practical rule for pressures under 100 lbs, per sq. in. is to make the thickness of the cylinder-heads 1½ times that of the walls; and applying this factor to his formula for thickness of walls, or .00025pD, we have

$$t = .00035pD.$$
 . . . . . . . . . . . . . . . (4)

Whitham quotes from Seaton,

$$t = \frac{pD + 500}{2000}$$
, which is equal to .0005pD + .25 inch. . . . (5)

Seaton's formula for cylinder bottoms, quoted above, is

t = 1.1f, in which f = .0002pD + .85 inch, or t = .00022pD + .93. . (6) Applying the above formulæ to the engines of 10, 30, and 50 inches diameter, with maximum unbalanced steam-pressure of 100 lbs. per sq. in., we have

Cylinder diameter, inches	=	10	30	50
(1) $t = .00033Dp + .25$	=	.53	1.25	1.82
(2) $t = .0050Dp + .25$	=	.75	1.75	2.75
(3) $t = .003D \sqrt{p}$	=		.90	1.50
(4) $t = .00035Dp$ (5) $t = .0005Dp + .25$	=	.35	1.05	1.75 2.75
(6) $t = .00022Dp + .93$		1.15	1.59	2.03
Average of 6		65	1.38	2.10

The average is expressed by the formula t = .00036Dp + .31 inch. Meyer's "Modern Locomotive Construction," p. 24, gives for locomotive cylinder-heads for pressures up to 120 lbs.;

9 to 10

Taking the pressure at 120 lbs, per sq. in., the thicknesses 1½ in. and ¾ in. for cylinders 22 and 10 in. diam., respectively, correspond to the formula t = .00035Dn + .33 inch.

Web-stiffened Cylinder-covers.—Seaton objects to webs for stiffening cast-iron cylinder-covers as a source of danger. The strain on the web is one of tension, and if there should be a nick or defect in the outer edge of the web the sudden application of strain is apt to start a crack. He recommends that high-pressure cylinders over 24 in, and low-pressure cylinders over 40 in. diam. Should have their covers cast hollow, with two thicknesses of metal. The depth of the cover at the middle should with two thicknesses of metal. The depth of the cover at the middle should be about ½ the diam, of the piston for pressures of 80 lbs, and upwards, and that of the low-pressure cylinder-cover of a compound engine equal to that of the high-pressure cylinder. Another rule is to make the depth at the middle not less than 1.3 times the diameter of the piston-rod. In the British Navy the cylinder-covers are made of steel castings, 34 to 114 in. thick, generally cast without webs, stiffness being obtained by their form, thick, generally cast without webs, sumers being which is often a series of corrugations. Cylinder-head Bolts,—Diameter of bolt-circle for cylinder-head diameter of cylinder + 2× thickness of cylinder + 2× thickness of self-active the bolts should not be more than 6 inches apart (Whitham).

Marks gives for number of bolts  $b = \frac{.754D^2}{5000c} = .000157(\frac{D^2p}{c})$ , in which  $c = \frac{.754D^2}{5000c} = .000157(\frac{D^2p}{c})$ , is kicken in the control of the self-active the se

area of a single bolt, p = boiler-pressure in lbs. per sq. in.; 5000 lbs. is taken

as the safe strain per sq. in. on the nominal area of the bolt. Seaton says: Cylinder-cover studs and bolts, when made of steel, should be of such a size that the strain in them does not exceed 5000 lbs. per sq. in. When of less than % inch diameter it should not exceed 4500 lbs. per sq. in. When of iron the strain should be 20% less.

Thurston says: Cylinder flanges are made a little thicker than the cylinder, and usually of equal thickness with the flanges of the heads. Cylinderbolts should be so closely spaced as not to allow springing of the flanges and leakage, say, 4 to 5 times the thickness of the flanges. Their diameter should be proportioned for a maximum stress of not over 400 to 5000 lbs.

Brother of proper square inch. If D = diameter of cylinder, p = maximum steam-pressure, b = number of bolts, s = size or diameter of each bolt, and 5000 lbs. be allowed per sq. in, of nominal area of the bolt,  $.7854D^2p = 3927bs^2$ ; whence  $bs^2 = .0002D^2p$ ;

$$b = .0002 \frac{D^2 p}{s^2}$$
;  $s = .01414 \sqrt{\frac{p}{b}}$ . For the three engines we have:

Diameter of cylinder, inches ...... Diameter of bolt-circle, approx .... 10 30 13 57.5 Circumference of circle, approx.... Minimum No. of bolts, circ. + 6..... 110 180 18 30 Diam, of bolts,  $s = .01414D\sqrt{\frac{p}{b}}......34$  in. 1.00

The diameter of bolt for the 10 inch cylinder is 0.54 in. by the formula, but 34 inch is as small as should be taken, on account of possible overstrain

by the wrench in screwing mp the mut.

The Piston. Details of Construction of Ordinary Pistons. (Seaton.)—Let D be the diameter of the piston in inches, p the effectors. tive pressure per square inch on it, x a constant multiplier, found as follows:

$$x = \frac{D}{50} \times \sqrt{p} + 1.$$

The thickness of front of	of nicton near the h	noss - 0.9 × 2	
THE CHICKINGS OF FROM		$\lim_{x \to 0} = 0.17 \times x$	
" back		$= 0.18 \times x$	
	ound the rod	$=0.3 \times x$	
	inside packing-ring		
	at edge	$= 0.25 \times x$	
" packin		$= 0.25 \times x$ . = $0.15 \times x$ .	
" Junk ri	ng at edge	$= 0.13 \times x$ . $= 0.23 \times x$ .	
" Junk-ri	inside packing-r		
	at bolt-holes	$= 0.35 \times x$ .	
th motel e	round piston edge		
		$= 0.23 \times x$ = $0.63 \times x$	
The breadth of packing			
" depth of piston at c		$=1.4 \times x$	
	the piston	$=0.45\times x$ .	
" space between pisto	n body and packing-	$ring = 0.3 \times x$ .	0.05 1
diameter of Jank-11	ng bolts	$=0.1 \times x +$	
DICH		= 10 diameter	
number of webs in t	ne piston	$= (D + 20) \div 1$	.2.
" thickness " "	••	$= 0.18 \times x$	

Marks gives the approximate rule: Thickness of piston-head  $= \sqrt{ld}$ , in which l = length of stroke, and d = diameter of cylinder in inches. ham says in a horizontal engine the rings support the piston, or at least a part of it, under ordinary conditions. The pressure due to the weight of the piston upon an area equal to 0.7 the diameter of the cylinder × breadth of ring-face should never exceed 300 lbs, per sq. in. He also gives a formula much used in this country: Breadth of ring-face = 0.15 × diameter of cylinder.

For our engines we have diameter = ..... 10 30 50

Thickness of piston-head.

Diameter of Piston Packing-rings.—These are generally turned, before they are cut, about ½ inch diameter larger than the cylinder, for cylinders up to 30 inches diameter, and then enough is cut out of the ring to spring them to the diameter of the cylinder. For larger cylinders the rings are turned proportionately larger. Seaton recommends an excess of 1% of the diameter of the cylinder.

Cross-section of the Rings .- The thickness is commonly made 1/30th of the diam. of cyl.  $+\frac{1}{26}$  inch, and the width = thickness  $+\frac{1}{26}$  inch. For an eccentric ring the mean thickness may be the same as for a ring of uniform thickness, and the minimum thickness = 3/8 the maximum.

and the control of th if the surface of the ring and cylinder are smooth.

As regards the width of rings, authorities "scatter" from very narrow to very wide, the latter being fully ten times the former. For instance, Unwingives  $W = d \cdot 0.14 + 0.8$ , Whitham's formula is  $W = d \cdot 1.5$ . In both formulæ W is the width of the ring in inches, and d the diameter of the cylinder milities wistine whath of the ring in inches, and a the diameter of the cylinder in inches. Unwin's formula makes the width of a  $20^{\circ}$  ring  $W = 20 \times .014 + .08 = .30^{\circ}$ , while Whitham's is  $20 \times .15 = 3^{\circ\prime}$  for the same diameter of ring. There is much less difference in the practice of engine-builders in this respect, but there is still room for a standard width of ring. It is believed that for cylinders over 16° diameter  $94^{\circ\prime}$  is a popular and practical width, and  $140^{\circ}$  for cylinders of that size and under. Seaton.)—The most convenient of the standard of the standard right with the standard right of 176 for cylinders of the size and under.

and reliable practice is to turn the piston-rod end with a shoulder of 1/16 inch for small engines, and 1/2 inch for large ones, make the taper 3 in. to

the foot until the section of the rod is three fourths of that of the body, then the root than the section of the root is three fourths of that of the body, then turn the remaining part parallel; the rod should then fit into the piston so as to leave ½ inch between it and the shoulder for large pistons, and 1/16 in, for small. The shoulder prevents the rod from splitting the piston, and allows of the rod being turned true after long wear without encroaching on

the taper. The piston is secured to the rod by a nut, and the size of the rod should be such that the strain on the section at the bottom of the thread does not exceed 5500 lbs, per sq. in. for iron, 7000 lbs. for seel. The depth of this nut need not exceed the diameter which would be found by allowing these strains. The nut should be locked to prevent its working loose.

Diameter of Piston-rods.—Unwin gives

$$d'' = bD \sqrt{p}, \ldots \ldots \ldots \ldots (1$$

in which D is the cylinder diameter in inches, p is the maximum unbalanced pressure in lbs. per sq. in., and the constant b=0.0167 for iron, and b=0.0144 for steel. Thurston, from an examination of a considerable number of rods in use, gives

$$d'' = \sqrt[4]{\frac{D^2 p L^2}{a} + \frac{D}{80}}$$
, nearly, . . . . . . . (2)

(L in feet, D and d in inches), in which  $\alpha = 10,000$  and upward in the various types of engines, the marine screw engines or ordinary fast engines on shore giving the lowest values, while "low-speed engines" being less liable to accident from shock give a=15,000, often.

Connections of the piston-rod to the piston and to the crosshead should have a factor of safety of at least 8 or 10. Marks gives

$$d'' = 0.0179D \sqrt{p}$$
, for iron; for steel  $d'' = 0.0105D \sqrt{p}$ ; . . (3)

and 
$$d'' = 0.03901 \sqrt[4]{D^2 l^2 p}$$
, for iron; for steel  $d'' = 0.03525 \sqrt[4]{D^2 l^2 p}$ , (4)

in which l is the length of stroke, all dimensions in inches. Deduce the diameter of piston-rod by (3), and if this diameter is less than 1/12l, then use (4).

Seaton gives: Diameter of piston-rod = 
$$\frac{\text{Diameter of cylinder}}{F} \sqrt{p}$$
.

The following are the values of F:

Note.-Long and very long, as compared with the stroke usual for the power of engine or size of cylinder.

In considering an expansive engine p, the effective pressure should be taken as the absolute working pressure, or 15 lbs. above that to which the boiler safety-valve is loaded; for a compound engine the value of p for the high-pressure piston should be taken as the absolute pressure, less 15 lbs., night-pressure pistor should be taken as the absolute pressure, less 16 lbs., or the same as the load on the safety-valve; for the medium-pressure the load may be taken as that due to half the absolute boiler-pressure; and for the low-pressure cylinder the pressure to which the escape-valve is loaded + 15 lbs., or the maximum absolute pressure, which can be got in the receiver, or about 25 lbs. It is an advantage to make all the rods of a compound engine alike, and this is now the rule.

Applying the above formulæ to the engines of 10, 30, and 50 in, diameter,

both short and long stroke, we have:

## Diameter of Piston-rods.

Diameter of Cylinder, inches	10		30		50	
Stroke, inches	12	21	30	60	48	93
Unwin, iron, .0167 $D\sqrt{p}$	1.67	1.67	5.01	5.01	8.35	8.35
Unwin, steel, .0144 $D\sqrt{\hat{p}}$	1.44	1.44	4.32	4.32	7.20	7.20
Thurston $\sqrt[4]{\frac{\overline{D^2pL^2}}{10,000}} + \frac{D}{80}$ (L in feet).	1.13		3.12		5.10	
Thurston, same with $a = 15,000$		1.40		3,88		6.35
Marks, iron, .0179 $D\sqrt{p}$	1.79		5.37	5.37	8.95	8.95
Marks, iron, .03901 $\sqrt[4]{D^2 l^2 p}$	1.35	1.91	3.70	5.13	6.04	8.54
Marks, steel, .0105 $D\sqrt{p}$	(1.05)		(3.15)		(5.25)	
Marks, steel, .03525 $\sqrt[4]{D^2 l^2 p}$	1.22	1.73	3.34	4.72	5.46	7.72
Seaton, naval engines, $\frac{D}{60} \sqrt{p}$	1.67		5.01		8.35	
Seaton, land engine, $\frac{D}{45}\sqrt{p}$		2.22		6.67		11.11
Average of four for iron	1.49	1.82	4.30	5.26	7.11	8.74

The figures in brackets opposite Marks' third formula would be rejected since they are less than ½ of the stroke, and the figures derived by his fourth formula would be taken instead. The figure 1.79 opposite his first formula would be taken engine of 24-inch stroke.

An empirical formula which gives results approximating the above aver-

ages is  $d'' = .013 \sqrt{Dlp}$ .

The calculated results from this formula, for the six engines, are, respectively, 1.42, 1.88, 3.90, 5.61, 6.37, 9.01.

Piston-rod Guides .- The thrust on the guide, when the connectingrod is at its maximum angle with the line of the piston-rod, is found from the formula: Thrust = total load on piston  $\times$  tangent of maximum angle of connecting rod =  $p \tan \theta$ . This angle is the angle whose tangent = half stroke of piston + length of connecting-rod.

Ratio of length of connecting-rod to stroke  Maximum angle of connecting-rod with line of	2	21/2	3
piston-rod	14° 29′	11° 19′	9° 36′
Tangent of the angle Secant of the angle	.25 1.0308	.20 1.0198	.1667 1.0138

Seaton says: The area of the guide-block or slipper surface on which the thrust is taken should in no case be less than will admit of a pressure of 400 lbs, on the square inch; and for good working those surfaces which take the thrust when going ahead should be sufficiently large to prevent the maximum pressure exceeding 100 lbs, per sq. in. When the surfaces are kept well lubricated this allowance may be exceeded.

Thurston says: The rubbing surfaces of guides are so proportioned that

if V be their relative velocity in feet per minute, and p be the intensity of pressure on the guide in lbs. per sq. in., pV < 60,000 and pV > 40,000. The lower is the safer limit; but for marine and stationary engines it is allowable to take p = 60,000 + V. According to Rankine, for locomotives,

 $p = \frac{1}{V+20}$ , where p is the pressure in lbs. per sq. in. and V the velocity of rubbing in feet per minute. This includes the sum of all pressures forcing the two rubbing surfaces together.

Some British builders of portable engines restrict the pressure between the guides and cross-heads to less than 40, sometimes 35 bs. per square inch. For a mean velocity of 900 feet per minute, Prof. Thurston's formulas give, p < 100, p > 66.7; Rankine's gives p = 72.2 lbs. per sq. in. Whitham gives,

$$A = \text{area of slides in square inches} = \frac{P}{p_0 \sqrt{n^2 - 1}} = \frac{.7854 d^2 p_1}{p_0 \sqrt{n^2 - 1}},$$

in which P= total unbalanced pressure,  $p_1=$  pressure per square inch on piston, d= diameter of cylinder,  $p_0=$  pressure allowable per square inch on slides, and n= length of connecting-rod + length of crank. This is equivalent to the formula, A=P tan  $\theta+p_0$ . For n=5,  $p_1=100$  and  $p_0=80$ ,  $A=2004d^2$ . For the three engines 10, 30 and 50 in. diam., this would = 80,  $A=2004d^2$ . For the three engines 10, 30 and 50 in, diam, this would give for area of slides, A=20, 180 and 500 sq. in, respectively. Whitham says: The normal pressure on the slide may be as high as 500 lbs, per sq. in, but this is when there is good lubrication and freedom from dust. Stationary and marine engines are usually designed to carry 100 lbs, per sq. in, and the area in this case is reduced from  $50^\circ$  to  $50^\circ$  by grooves. In locomotive engines the pressure ranges from 40 to 50 lbs, per sq. in. of slide, on account of the inaccessibility of the slide, durt, cinder, etc.

There is perfect agreement among the authorities as to the formula for area of the slides, A=P tan  $\theta+p_0$ ; but the value given to  $p_0$ , the allowable pressure per square inch, ranges all the way from 35 lbs, to 500 lbs.

The Connecting-rod. Ratio of length of connecting-rod to length of stroke.—Experience has led generally to the ratio of 2 or  $29^\circ_0$  to 1, the latter giving a long and easy-working rod, the former a rather short, but yet a manageable one (Thurston). Whitham gives the ratio of from 2 to  $49^\circ_0$  and Marks from 2 to  $49^\circ_0$ .

yet a manageable one (murstor). Whichain gives use rank of the diameter of and Marks from 2 to 4. Dimensions of the Connecting-rod.—The calculation of the diameter of a connecting-rod on a theoretical basis, considering it as a strut subject to both compressive and bending stresses, and also to stress due to its inertia, in high-speed engines, is quite complicated. See Whitham, Steam-engine Design, p. 217; Thurston, Manual of S. E., p. 100. Empirical formulas are as follows: For circular rods, largest at the middle, D = diam, of cylinder, l = the connection rotssure per sq. in. length of connecting-rod in inches, p = maximum steam-pressure per sq. in.

- (1) Whitham, diam. at middle,  $d'' = 0.0272 \ \sqrt{Dl \ \sqrt{p}}$ . (2) Whitham, diam. at necks, d'' = 1.0 to  $1.1 \times$  diam. of piston-rod. (3) Sennett, diam. at middle,  $d'' = \frac{D}{55} \sqrt[4]{p}$ .
- (4) Sennett, diam. at necks,  $d'' = \frac{D}{\epsilon_0} \sqrt{p}$ .
- (5) Marks, diam.,  $d'' = 0.0179D \sqrt{p}$ , if diam. is greater than 1/24 length.
- (6) Marks, diam.,  $d'' = 0.02758 \sqrt{Dl \sqrt{p}}$  if diam. found by (5) is less than 1/24 length.
- (7) Thurston, diam. at middle,  $d'' = a \sqrt{DL} \sqrt{p} + C$ , D in inches, L in feet, a = 0.15 and  $C = \frac{1}{2}$  inch for fast engines, a = 0.08 and  $C = \frac{3}{4}$  inch for moderate speed.
- (8) Seaton says: The rod may be considered as a strut free at both ends, and, calculating its diameter accordingly,

diameter at middle = 
$$\frac{\sqrt{R(1+4 ar^2)}}{48.5}$$

where R = the total load on piston P multiplied by the secant of the maximum angle of obliquity of the connecting-rod.

For wrought iron and mild steel a is taken at 1/3000. The following are

the values of r in practice: Naval engines-Direct-acting

aval engines—Direct-acting 
$$r=9$$
 to 11;  $r=9$  to 10;  $r=10$  to 13, old;  $r=8$  to 9, modern;  $r=8$  to 9, modern;  $r=11.5$  to 13. Proceedings or  $r=11.5$  to 14. Proceedings or  $r=11.5$  to 15. Proceedings or  $r=13$  to 16.

(9) The following empirical formula is given by Seaton as agreeing closely with good modern practice:

Diameter of connecting-rod at middle =  $\sqrt{lK} \div 4$ , l = length of rod in inches, and K = 0.03 Veffective load on piston in pounds,

The diam, at the ends may be 0.875 of the diam, at the middle, Seaton's empirical formula when translated into terms of D and p is the

same as the second one by Marks, viz.,  $d'' = 0.02758 \sqrt{Dl \sqrt{p}}$ . Whitham's

(1) is also practically the same.

(10) Taking Seaton's more complex formula, with length of connecting  $rod = 2.5 \times length$  of stroke, and r = 12 and 16, respectively, it reduces to: Diam. at middle = .02294  $\sqrt{P}$  and .02411  $\sqrt{P}$  for short and long stroke engines, respectively.

Applying the above formulas to the engines of our list, we have

# Diameter of Connecting-rods.

Diameter of Cylinder, inches	10		-30		5	0
Stroke, inches.  Length of connecting-rod l	12 30	24 60	30 75	60 150	48 120	96 240
(3) $d'' = \frac{D}{55} \sqrt{p} = .0182D \sqrt{p}$	1.82	1.82	5.46	5.46	9.09	9.09
(5) $d'' = .0179D \sqrt{p} \dots$	1.79		5.37		8.95	
(6) $d'' = .02758 \sqrt{Dl \sqrt{p}}$		2.14		5.85		9.51
(7) $d'' = 0.15 \sqrt{DL} \sqrt{\bar{p}} + \frac{1}{2} \dots$	2.87		7.00		11.11	
(7) $d'' = 0.08 \sqrt{DL \sqrt{p}} + 34$		2.54		5.65		8.75
(9) $d'' = .03 \sqrt{P}$	2.67	2.67	7.97	7.97	13.29	13.29
(10) $d'' = .02294 \sqrt{P}$ ; .02411 $\sqrt{P}$	2.03	2.14	6.09	6.41	10.16	10.68
Average	2.24	2.26	6.38	6.27	10.52	10.26

Formulæ 5 and 6 (Marks), and also formula 10 (Seaton), give the larger diameters for the long-stroke engine; formulæ 7 give the larger diameters for the short-stroke engines. The average figures show but little difference in diameter between long- and short-stroke engines; this is what might be expected, for while the connecting-rod, considered simply as a column, would require an increase of diameter for an increase of length, the load remaining the same, yet in an engine generally the shorter the connecting-rod the greater the number of revolutions, and consequently the greater the truib the greater to the following and to recommend the greater the strains due to inertia. The influences tending to increase the diameter therefore tend to balance each other, and to render the diameter to some extent independent of the length. The average figures correspond nearly to the simple formula  $d''=021D\sqrt{p}$ . The diameters of rod for the three diameters of engine by this formula are, respectively, 2.10, 6.30, and 10.50 in. Since the total pressure on the piston  $P=.7854D^2p$ , the formula is equivalent to  $d' = .0287 \sqrt{P}$ .

Connecting-rod Ends.—For a connecting-rod end of the marine type, where the end is secured with two bolts, each bolt should be proportioned for a safe tensile strength equal to two thirds the maximum pull or

thrust in the connecting-rod.

thrust in the connecting-rod.

The cap is to be proportioned as a beam loaded with the maximum pull of the connecting-rod, and supported at both ends. The calculation should be made for rigidity as well as strength, allowing a maximum deflection of 1/100 inch. For a strap-and-key connecting-rod end the strap is designed for tensile strength, considering that two thirds of the pull on the connecting-rod any come once arm. At the point where the metal is slotted for the key and glb, the straps must be thickened to make the cross-section equal to that of the remainder of the strap. Between the end of the strap and the slot the strap is liable to fail in double shear, and sufficient metal must be provided at the end to prevent such failure.

The breadth of the key is generally one fourth of the width of the strap, and the length, parallel to the strap, should be such that the cross-section will have a shearing strength equal to the tensile strength of the section of the strap. The taper of the key is generally about % inch to the foot.

Tapered Connecting-rods.—In modern high-speed engines it is customary to make the connecting-rods of rectangular instead of circular section, the sides being parallel, and the depth increasing regularly from the crosshead end to the crank-pin end. According to Grashof, the bending action on the rod due to its inertia is greatest at 6/10 the length from the crosshead end, and, according to this theory, that is the point at which the section should be greatest, although in practice the section is made greatest at the crank-pin end.

Professor Thurston furnishes the author with the following rule for tapered connecting rod of rectangular section: Take the section as computed by the

formula  $a'' = 0.1 \sqrt{DL \ Vp} + 3/4$  for a circular section, and for a rod 4/3 the actual length, placing the computed section at 2/3 the length from the small end, and carrying the taper straight through this fixed section to the large end. This brings the computed section at the surge point and makes it heavier than the rod for which a tapered form is not required. Taking the above formula, multiplying L by 4/3, and changing it to l in

inches, it becomes d=1/30  $\sqrt[4]{Dl}$   $\sqrt[4]{p}+3/4''$ . Taking a rectangular section of the same area as the round section whose diameter is d, and making the depth of the section h= twice the thick ress t, we have  $-.78542^2=h$   $+.16=2t^2$ ,

whence  $t=.627d=.0209 \ \sqrt{Dl \ \sqrt{p}}+.47''$ , which is the formula for the thickness or distance between the parallel sides of the rod. Making the depth at the crosshead end = 1.54, and at 2/3 the length = 2t, the equivalent depth at the crank end is 2.25t. Applying the formula to the short-stroke engines of our examples, we have

Diameter of cylinder, inches	12 30	30 30 75	59 48 120
Thickness, $t=.0209$ $\sqrt{Dl\sqrt{p}}+.47=$	2.42	3.60	5.59
Depth at crosshead end, $1.5t=$		5.41	8.39
Depth at crank end, $2\frac{1}{4}t$		8.11	12.58

The thicknesses t, found by the formula  $t = .0209 \sqrt{Dl \sqrt{p} + .47}$ , agree closely with the more simple formula  $t = .01D \sqrt{p} + .60''$ , the thicknesses calculated by this formula being respectively 1.6, 3.6, and 5.6 inches.

The Crank-pin.—A crank pin should be designed (1) to avoid heating, (2) for strength, (3) for rigidity. The heating of a crank-pin depends on the pressure on its rubbing-surface, and on the coefficient of friction, which latter varies greatly according to the effectiveness of the lubrication. It also depends upon the facility with which the heat produced may be carried away: thus it appears that locumotive crank-pins may be prevented to some degree from overheating by the cooling action of the air through which they pass at a high speed.

Marks gives 
$$l = .0000247 \, fp ND^2 = 1.038 f \frac{(\text{I.H.P.})}{L}$$
 . . . . . . (1)

Whitham gives 
$$l = 0.9075f$$
  $\frac{(\text{I.H.P.})}{L}$ , . . . . . . . . (2)

in which l= length of crank-pin journal in inches, f= coefficient of friction, which may be taken at .03 to .05 for perfect lubrication, and .08 to .10 for imperfect; p= mean pressure in the cylinder in pounds per square inch; D= diameter of cylinder in inches; N= number of single strokes per minute; LH.P.= indicated horse-power; L= length of stroke in fect. These formulæ are independent of the diameter of the pin, and Marks states as a constal law with the executed with the constant of the diameter of the pin, and Marks states as a constal law with the executed with the constant of the pin. commuse are undependent of the diameter of the pin, and Marks states as a general law, within reasonable limits as to pressure and speed of rubbing, the longer a bearing is made, for a given pressure and number of revolutions, the cooler it will work; and its diameter las no effect upon its heating. Both of the above formulæ are deduced empirically from dimensions of crank-pins of existing marine engines. Marks says that about one-fourth the length required for crank-pins of propeller engines will serve for the pins of side-wheel engines, and one tenth for locomotive engines, making the

formula for locomotive crank-pins  $l=.00000247 fpND^2$ , or if p=150, f=.06, and N=600,  $l=.018D^2$ . Whitham recommends for pressure per square inch of projected area, for naval engines 500 pounds, for merchant engines 400 pounds, for paddle-wheel

bearings are used.

Thurston also says: The size of crank-pins required to prevent heating of the journals may be determined with a fair degree of precision by either of the formulæ given below:

$$l = \frac{P(V+20)}{44,800d}$$
 (Rankine, 1865); . . . . . . . (4

$$l = \frac{PV}{60,000d}$$
 (Thurston, 1862); . . . . . . . . (5)

$$l = \frac{PN}{350,000}$$
 (Van Buren, 1866). . . . . . . . (6)

The first two formulæ give what are considered by their authors fair work-

The first two formulae give what are considered by their authors har working proportions, and the last gives minimum length for iron pins. (V = velocity of rubbing-surface in feet per minute.)Formula (1) was obtained by observing locomotive practice in which great liability exists of annoyance by dust, and great risk occurs from inaccessibility while running, and (2) by observation of crank-pins of naval screwengines. The first formula is therefore not well suited for marine practice.

Steel can usually be worked at nearly double the pressure admissible with

iron running at similar speed.
Since the length of the crank-pin will be directly as the power expended upon it and inversely as the pressure, we may take it as

$$l = a \frac{\text{I.H.P.}}{l}, \dots \dots \dots \dots$$

in which a is a constant, and L the stroke of piston, in feet. The values of the constant, as obtained by Mr. Skeel, are about as follows: a=0.04 where water can be constantly used; a=0.045 where water is not generally used; a=0.05 where water is seldom used; a=0.06 where water is never needed. Unwin gives

in which r= crank radius in inches, a=0.3 to a=0.4for iron and for marine engines, and a=0.060 to a=0.1 for the case of the best steel and for locomotive work, where it is often necessary to shorten up outside pins as much

J. B. Stanwood (Eng'g, June 12, 1891), in a table of dimensions of parts of American Corliss engines from 10 to 30 inches diameter of cylinder, gives sizes of crank-pins which approximate closely to the formula

By calculating lengths of iron crank-pins for the engines 10, 30, and 50 inches diameter, long and short stroke, by the several formule above given, it is found that there is a great difference in the results, so that one formula in certain cases gives a length three times as great as another. Nos. (4), (5), and (6) give lengths much greater than the others. Marks (1), Whitham (2), Thurston (7),  $l = .06.1 \, \mathrm{H.P.} + L$ , and Unwin (8),  $l = 0.4 \, \mathrm{L.H.P.} + L$ , give results which agree more closely.

The calculated lengths of iron crank-pins for the several cases by formulæ (1), (2), (7), and (8) are as follows:

# Length of Crank-pins.

Diameter of cylinder	10	10	30	30	50	50
Stroke L (ft.)		2	21/2	5	4	8
Revolutions per minuteR		125	130	65	90	45
Horse-powerI.H.P.	50	50	450	450		
Maximum pressure			70,686			
Mean pressure per cent of max	42	42	32.3	32.3	30	30
	3,299				58,905	
Mean pressureP.	0,299	5,299	22,002	22,002	50,905	30, 903
Length of crank-pin.	0.40	4 00	0 40	4 00	44 40	~ 00
(1) Whitham, $l = .9075 \times .05 \text{ I.H.P.} + L.$	2.18	1.09	8.17	4.08	14.18	
(2) Marks, $l = 1.038 \times .05  \text{I.H.P.} \div L.$		1.30	9.34		16.22	
(7) Thurston, $l = .06$ I.H.P. $\div L$	3.00	1.50	10.80		18.75	
(8) Unwin, $l = .4 \text{ I.H.P.} \div r$	3.33	1.67	12.0	6.0	20.83	
(8) " $l = .3 \text{ I.H.P.} \div r$	2.50	1.25	9.0	4.5	15.62	7.81
Average	2.72	1.36	9.86	4.93	17.12	8.56
(8) Unwin, best steel, $l=.1\frac{\mathrm{I.H.P.}}{r}$	.83	.42	3.0	1.5	5.21	2.61
(3) Thurston, steel, $l = \frac{PR}{600,000}$	1.37	.69	4.95	2.47	8.84	4.42

The calculated lengths for the long-stroke engines are too low to prevent excessive pressures. See "Pressures on the Crank-pins," below.

The Strength of the Crank-pin is determined substantially as is that of the erank. In overhung cranks the load is usually assumed as carried at its extremity, and, equating its moment with that of the resistance of the pin.

$$\frac{1}{2}Pl = \frac{1}{32}t\pi d^3$$
, and  $d = \sqrt[3]{\frac{5.1Pl}{t}}$ ,

in which d= diameter of pin in inches, P= maximum load on the piston, t= the maximum allowable stress on a square inch of the metal. For iron it may be taken at 9000 lbs. For steel the diameters found by this formula may be reduced 10%. (Thurston.)

Unwin gives the same formula in another form, viz.:

$$d = \sqrt[3]{\frac{5.1}{t}}\sqrt[3]{Pl} = \sqrt{\frac{5.1}{t}}\sqrt{\frac{l}{Pl}},$$

the last form to be used when the ratio of length to diameter is assumed. For wrought iron, t = 6000 to 9000 lbs. per sq. in.,

$$\sqrt[3]{\frac{\overline{5.1}}{t}} = .0947 \text{ to } .0827; \qquad \sqrt{\frac{\overline{5.1}}{t}} = .0291 \text{ to } .0238.$$

For steel, t = 9000 to 13,000 lbs. per sq. in.,

$$\sqrt[3]{\frac{5.1}{t}} = .0827 \text{ to } .0723; \qquad \sqrt{\frac{5.1}{t}} = .0238 \text{ to } .0194.$$

Whitham gives 
$$d=0.0827 \sqrt[3]{Pl}=2.1058 \sqrt[3]{\frac{\overline{l}\times\overline{\text{I.H.P.}}}{LR}}$$
 for strength, and

 $d=0.405\sqrt[6]{Pl^9}$  for rigidity, and recommends that the diameter be calculated by both formulae, and the largest result taken. The first is the same as Unwin's formula, with t taken at 9000 lbs. per sq. in. The second is based upon an erreneous assumption.

Marks, calculating the diameter for rigidity, gives

$$d = 0.066 \sqrt[4]{p l^3 D^2} = 0.945 \sqrt[4]{\frac{(\text{H.P.}) l^3}{LN}};$$

p = maximum steam-pressure in pounds per square inch, D = diameter of cylinder in inches, L = length of stroke in feet, N = number of single strokes per minute. He says there is no need of an investigation of the strength of a crank-pin, as the condition of rigidity gives a great excess of strength. Marks's formula is based upon the assumption that the whole load may be

concentrated at the outer end, and cause a deflection of .01 inch at that

It is serviceable, he says, for steel and for wrought iron alike,

Using the average lengths of the crank-pins already found, we have the following for our six engines :

# Diameter of Crank-pins.

Diameter of cylinder	10	10	30	30	50	50
Diameter of cylinderStroke, ftLength of crank-pin.	$\frac{1}{2.72}$	1.36	9.86	4.93	4 17.12	8.56
Unwin, $d = \sqrt[3]{\frac{5.1Pl}{t}}$	2.29	1.82	7.34	5.82	12.40	9.84
Marks, $d = .066 \sqrt[4]{pl^3D^2}$	1.39	.85	6.44	3.78	12.41	7.39

Pressures on the Crank-pins. - If we take the mean pressure upon the crank-pin = mean pressure on piston, neglecting the effect of the varying angle of the connecting rod, we have the following, using the average lengths already found, and the diameters according to Unwin and Marks:

Engine No	1	2	3	4	5	6
Diameter of cylinder, inches	1 3,299 6.23 3.78 530	10 2 3,299 236 1.16 1,398 2,845	30 21/ <sub>2</sub> 22,832 72.4 63.5 315 360	30 5 22,832 28.7 18.6 796 1,228		84.2

The results show that the application of the formulæ for length and diameter of crank-pins give quite low pressures per square inch of projected area for the short-stroke high-speed engines of the larger sizes, but too high pressures for all the other engines. It is therefore evident that after calculating the dimensions of a crank-pin according to the formulæ given that the results should be modified, if necessary, to bring the pressure per square inch down to a reasonable figure.

In order to bring the pressures down to 500 pounds per square inch, we divide the mean pressures by 500 to obtain the projected area, or product of length by diameter. Making l=1.5d for engines Nos. 1, 2, 4 and 6, the

revised table for the six engines is as follows:

Crosshead-pin or Wrist-pin.—Whitham says the bearing surface for the wrist-pin is found by the formula for crank-pin design. Seaton says the diameter at the middle must, of course, be sufficient to writhstand the bending action, and generally from this cause ample surface is provided for good working; but in any case the area, calculated by multiplying the diameter of the journal by its length, should be such that the pressure does not exceed 1200 lbs. per sq. in., taking the maximum load on the piston as the total pressure on it. total pressure on it.

For small engines with the gudgeon shrunk into the jaws of the connect-

ing-rod, and working in brasses fitted into a recess in the piston-rod end and secured by a wrought-iron cap and two bolts, Seaton gives:

Diameter of gudgeon =  $1.25 \times \text{diam}$ , of piston-rod, Length of gudgeon =  $1.4 \times \text{diam}$ , of piston-rod.

If the pressure on the section, as calculated by multiplying length by

If the pressure on the section, as calculated by multiplying length of diameter, exceeds 1200 lbs, per sq. in., this length should be increased.

J. B. Stanwood, in his "Ready Reference" book, gives for length of crosshead-pin v25 to 0.3 diam. of piston, and diam. = 0.18 to 0.2 diam. of piston, Since he gives for diam. of piston, rod 0.14 to 0.17 diam. of piston, his dimensions for diameter and length of crosshead-pin are about 1.25 and 1.8 diam. of piston-rod respectively. Taking the maximum allowable pressure at 1200 lbs. per sq. in. and making the length of the crosshead-pin = 4/3 of its diameter, we have  $d=\sqrt[l]{P}+40$ ,  $l=\sqrt[l]{P}+30$ , in which  $P=\max$ innum total load on piston in lbs., d= diam. and l= length of pin in inches. For the engines of our example we have:

Diameter of piston, inches	10	30	50
Maximum load on piston, lbs	7854	70,686	196,350
Diameter of crosshead-pin, inches	2.22	6.65	11.08
Length of crosshead-pin, inches	2.96	*8.86	14.77
Stanwood's rule gives diameter, inches	1.8 to 2	5.4 to 6	9.0 to 10
Stanwood's rule gives length, inches	2.5 to 3	7.5 to 9	12.5 to 15
Stanwood's largest dimensions give pressure			
per sq. in., lbs	1309	1329	1309

Which pressures are greater than the maximum allowed by Seaton. The Crank-arm.—The crank-arm is to be treated as a lever, so that if a is the thickness in direction parallel to the shaft-axis and b its breath at a section x inches from the crank-pin centre, then, bending moment M at that section = Pc, P being the thrust of the connecting-rod, and f the safe strain per square inch,

$$Px = \frac{fab^2}{6}$$
 and  $\frac{a \times b^2}{6} = \frac{T}{f}$ , or  $a = \frac{6T}{b^2 \times f}$ ;  $b = \sqrt{\frac{6T}{fa}}$ .

If a crank-arm were constructed so that b varied as  $\sqrt{x}$  (as given by the above rule) it would be of such a curved form as to be inconvenient to manufacture, and consequently it is customary in practice to find the maximum value of b and draw tangent lines to the curve at the points; these lines are generally, for the same reason, tangential to the boss of the crankarm at the shaft.

The shearing strain is the same throughout the crank-arm; and, consequently, is large compared with the bending strain close to the crank-pin; quentry, is large compared with the bending strain close to the crank-pin; and so it is not sufficient to provide there only for bending strains. The section at this point should be such that, in addition to what is given by the calculation from the bending moment, there is an extra square inch for every 8000 lbs. of thrust on the connecting-rod (Seaton). The length of the boss h into which the shaft is fitted is f so of the diameter of the shaft D, and its thickness e must be calculated from the twisting strain PL, (L = length of crank). For different values of length of boss h, the following values of thickness e for a great given by Seaton.

of boss e are given by Seaton;

When h=D, then e=0.35 D; if steel, 0.3. h=0.9 D, then e=0.38 D, if steel, 0.32. h=0.8 D, then e=0.40 D, if steel, 0.33. h=0.7 D, then e=0.41 D, if steel, 0.34.

The crank-eye or boss into which the pin is fitted should bear the same relation to the pin that the boss does to the shaft.

The diameter of the shaft-end onto which the crank is fitted should be

1.1  $\times$  diameter of shaft.

Thurston says: The empirical proportions adopted by builders will commonly be found to fall well within the calculated safe margin. These proportions are, from the practice of successful designers, about as follows:

For the wrought-iron crank, the hub is 1.75 to 1.8 times the least diameter of that part of the shaft carrying full load; the eye is 2.0 to 2.25 the diameter of the inserted portion of the pin, and their depths are, for the hub, 1.0 1.2 the diameter of shaft, and for the eye, 1.25 to 1.5 the diameter of pin. The web is made 0.7 to 0.75 the width of adjacent hub or eye, and is given a

The web is made 0.7 to 0.75 the width of adjacent hub or eye, and is given a depth of 0.5 to 0.6 that of adjacent hub or eye. a little larger, ranging in diameter respectively from 1.8 to 2 and from 2 to 2.2 times the diameters of shaft and pin. The flanges are made at either end of nearly the full depth of hub or eye. (2ast-iron has, however, fallen very generally into disuse.

The crank-shaft is usually enlarged at the seat of the crank to about 1.1 is diameter at the journal. The size should be nicely adjusted to allow for the shrinkage or forcing ou of the crank. A difference of diameter of one of the first of the crank control of the shrinkage or forcing ou of the crank. A difference of diameter of one

the shrinkage of forcing on of the crank. A difference of diameter of one fifth of 18, will usually suffice; and a common rule of practice gives an allowance of but one half of this, or .001.

The formulæ given by different writers for crank-arms practically agree, since they all consider the crank as a beam loaded at one end and fixed at the other. The relation of breadth to thickness may vary according to the taste of the designer. Calculated dimensions for our six engines are as fol lows:

## Dimensions of Crank-arms.

Diam. of cylinder, ins Stroke S, ins	10 12	10 24	30 30	30 60	50 48	50 96
Max. pressure on pin $P$ , (approx.) lbs	7854	7854	70,686	70,686	196,350	196,350
Diam, shaft, $a \sqrt[3]{\frac{\text{I.H.P.}}{R}} D$	2.10	2.10	7.34	5.58	12.40	8.87
(a = 4.69, 5.09  and  5.22)	2.74		7.70	9.70	12.55	15.82
Length of boss, .8D Thickness of boss, .4D	2.19	2.77	6.16	7.76	10.04	12.65
Diam. of boss, 1.8D	1.10	1.39 6.23	3.08 13.86	3.88 17.46	5.02 22.59	6.32 28.47
Length crank-pineye, .8d Thickness of crank-pin	1.76	1.76	5.87	4.46	9.92	7.10
eye, .4d Max. mom. T at distance	.88	.88	2.94	2.23	4.46	3.55
<sup>1</sup> ⁄ <sub>2</sub> S − ½D from centre of pin, inch-lbs	37, 149	80,661	788,149	1,848,439	3,479,322	7,871,671
Thickness of crank-arm $a = .75D$	2.05	2.60	5.78	7.28	9.41	11.87
$/\overline{6T}$						
$b = \sqrt{9000a}$	3.48	4.55	9.54	13.0	15.7	21.0
Min.mom. $T_0$ at distance $d$ from centre of pin= $Pd$ Least breadth,	16,493	16,493	528,835	394,428	2,434,740	1,741,625
$b_1 = \sqrt{\frac{6T_0}{9000a}}$	2.32	2.06	7.81	6.01	13.13	9.89

The Shaft.-Twisting Resistance.-From the general formula for torsion, we have:  $T = \frac{\pi}{16} d^3S = .19635 d^3S$ , whence  $d = \frac{3}{4} / \frac{5.1T}{S}$ , in which

T= torsional moment in inch-pounds, d= diameter in inches, and S= the shearing resistance of the material in pounds per square inch. If a constant force P were applied to the crank-pin tangentially to its path, the work done per minute would be

$$P \times L \times \frac{2\pi}{12} \times R = 33,000 \times I.H.P.,$$

in which L= length of e<sup>-</sup>ank in inches, and R= revs. per min., and the mean twisting moment  $T=\frac{I.H.P.}{L} imes 63,025$ . Therefore

$$d = \sqrt[3]{\frac{5.1T}{S}} = \sqrt[3]{\frac{321,427 \text{I.H.P.}}{RS}}$$

This may take the form

$$d = \sqrt[3]{\frac{\text{I.H.P.}}{R} \times F}$$
, or  $d = a \sqrt[3]{\frac{\text{I.H.P.}}{R}}$ ,

in which F and a are factors that depend on the strength of the material and on the factor of safety. Taking S at 45,00 eoutse per square inch for wrought iron, and at 60,000 for steel, we have, for simple twisting by a uniform tangential force.

Unwin, taking for safe working strength of wrought iron 9000 lbs., steel 18,500 lbs., and east iron 4500 lbs., gives a=3.294 for wrought iron, 2.877 for steel, and 4.15 for cast iron. Thurston, for crank-axles of wrought iron, gives a=4.15 or more.

steet, and a low Case to the Indiscount, for chain-takes of wrongen but gives a = 4.15 or more ught iron, f, the safe strain per square inch, should not exceed 9000 lbs., and when the shafts are more than 10 inches diameter, 8000 lbs. Steel, when made from the ingot and of good materials, will admit of a stress of 12,000 lbs. for small shafts, and 10,000 lbs. for those above

10 inches diameter.

The difference in the allowance between large and small shafts is to compensate for the defective material observable in the heart of large shafting,

owing to the hammering failing to affect it.

The formula 
$$d=a\sqrt[3]{\frac{\overline{1.H.P.}}{R}}$$
 assumes the tangential force to be uniform

and that it is the only acting force. For engines, in which the tangential force varies with the angle between the crank and the connecting-rod, and with the variation in steam-pressure in the cylinder, and also is influenced by the inertia of the reciprocating parts, and in which also the shaft may be subjected to bending as well as torsion, the factor a must be increased, to provide for the maximum tangential force and for bending.

Seaton gives the following table showing the relation between the maximum and mean twisting moments of engines working under various conditions, the momentum of the moving parts being neglected, which is allow-

able:

D	escription of	Engine.		Steam Cut-off at	Max. Twist Divided by Mean Twist. Mome't	Cube Root of the Ratio.
Single-cran	k expansive			0.2	2.625 2.125	1.38 1.29
46	"	•••••		0.6	1.835	1.22
46	٠.		• • • • • • • • • • • • • • • • • • • •	0.8	1.698	1.20
Two-evlind.	er expansive.	cranks at	900	0.2	1.616	1.17
2 0 00	66	44		0.3	1,415	1.12
44	66	44		0.4	1.298	1.09
66	46	44		0.5	1.256	1.08
•	46	46		0.6	1.270	1.08
66	46	66		0.7	1.329	1.10
66	46	44		0.8	1.357	1.11
Three-cylin	der compour	d, cranks 1	120°	h.p. 0.5, l.p. 0.66	1.40	1.12
		1. p. cra	nks [	66 66	1.26	1.08
opposite o	ne a other, a	nd h.p. mic	dway {		1.20	1.00

Seaton also gives the following rules for ordinary practice for ordinary two-cylinder marine engines;

Diameter of the tunnel-shafts = 
$$\sqrt[3]{\frac{\text{I.H.P.}}{R} \cdot \times F_{*}}$$
 or  $\alpha \sqrt[3]{\frac{\text{I.H.P.}}{R}}$ .

Compound engines, cranks at right angles:

Boiler pressure 70 lbs., rate of expansion 6 to 7, F=70, a=4.12. Boiler pressure 80 lbs., rate of expansion 7 to 8, F=72, a=4.16. Boiler pressure 90 lbs., rate of expansion 8 to 9, F=75, a=4.22.

Triple compound, three cranks at 120 degrees:

Boiler pressure 150 lbs., rate of expansion 10 to 12, F=62,  $\alpha=3.96$ . Boiler pressure 160 lbs., rate of expansion 11 to 13, F=64,  $\alpha=4$ . Boiler pressure 170 lbs., rate of expansion 12 to 15, F=67,  $\alpha=4.06$ .

Expansive engines, cranks at right angles, and the rate of expansion 5, boiler-pressure 60 lbs., F = 90,  $\alpha = 4.48$ .

Single-crank compound engines, pressure 80 lbs., F = 96, a = 4.58. For the engines we are considering it will be a very liberal allowance for ratio of maximum to mean twisting moment if we take it as equal to the ratio of the maximum to the mean pressure on the piston. The factor a, then, in the formula for diameter of the shaft will be multiplied by the cube

then, in the formula for diameter of the shaft will be multiplied by the cube root of this ratio, or 
$$\sqrt[3]{\frac{100}{42}} = 1.34$$
,  $\sqrt[3]{\frac{100}{32.3}} = 1.45$ , and  $\sqrt[3]{\frac{100}{30}} = 1.49$  for the

10, 30, and 50-in, engines, respectively. Taking a=3.5, which corresponds to a shearing strength of 60,000 and a factor of safety of 8 for steel, or to 45,000 and a factor of 6 for iron, we have for the new coefficient  $a_i$  in the

formula  $d_1 = a_1 \sqrt[8]{\frac{\text{I.H.P.}}{R}}$ , the values 4.69, 5.08, and 5.22, from which we

These diameters are calculated for twisting only. When the shaft is also subjected to bending strain the calculation must be modified as below:

Resistance to Bending.—The strength of a circular-section shaft to resist bending is one half of that to resist twisting. If B is the bending moment in inch-lbs., and d the diameter of the shaft in inches

$$B = \frac{\pi d^3}{32} \times f$$
; and  $d = \sqrt[3]{\frac{B}{f} \times 10.2}$ ;

f is the safe strain per square inch of the material of which the shaft is composed, and its value may be taken as given above for twisting (Seaton).

Equivalent Twisting Moment.—When a shaft is subject to

both twisting and bending simultaneously, the combined strain on any section of it may be measured by calculating what is called the equivalent twisting moment; that is, the two strains are so combined as to be treated as a twisting strain only of the same magnitude and the size of shaft calculated accordingly. Rankine gave the following solution of the combined action of the two strains.

If T = the twisting moment, and B = the bending moment on a section of

a shaft, then the equivalent twisting moment  $T_1=B+\sqrt{B^2+T^2}$ . Seaton says: Crank-shafts are subject always to twisting, bending, and shearing strains; the latter are so small compared with the former that they are usually neglected directly, but allowed for indirectly by means of the factor f.

The two principal strains vary throughout the revolution, and the maxinum equivalent twisting moment can only be obtained accurately by a series of calculations of bending and twisting moments taken at fixed intervals, and from them constructing a curve of strains.

Considering the engines of our examples to have overhung cranks, the

maximum bending moment resulting from the thrust of the connecting-rod on the crank-pin will take place when the engine is passing its centres (neglecting the effect of the inertia of the reciprocating parts), and it will be the product of the total pressure on the piston by the distance between two parallel lines passing through the centres of the crank-pin and of the shaft bearing, at right angles to their axes; which distance is equal to \$\frac{1}{2}\tength of crank-pin bearing + \tength of hub + \frac{1}{2}\tength of shaft bearing + any clearance that may be allowed between the crank and the two bearings. any clearance man may be anowed observed in the craim and the two bearings for our six engines we may take this distance as equal to ½ length of crank-pin + thickness of crank-arm + 1.5 × the diameter of the shaft as already found by the calculation for twisting. The calculation of diameter is then as below:

Engine No.	1	2	3	4	5	6
Diam. of cyl., in	10	10	30	30	50	50
Horse-power	10 50	50	450	450	1250	1250
Revs. per min	250	125	130	65	90	45
Max.press. on pis, P		7.854	70,686	70,686	196,350	196,350
Leverage,* Lin	6.32	7.94	22.20	26.00	36.80	42.25
Bd.mo.PL=Binlb		62,361	1,569,222	1,837,836	7,225,680	8,295,788
Twist, mom, T	47,124	94,248	1,060,290	2,120,580	4,712,400	9,424,800
Equiv.Twist. mom.						
$T_1=B+\sqrt{B^2+T^2}$						
(approx.)	118.000	175.000	3.463.000	4.647.000	15.840.000	20.850.000

\*Leverage = distance between centres of crank-pin and shaft bearing =  $\frac{1}{6}l + 2.25d$ .

Having already found the diameters, on the assumption that the shafts were subjected to a twisting moment T only, we may find the diameter for resisting combined bending and twisting by multiplying the diameters already found by the cube roots of the ratio  $T_1 \div T$ , or

1.36 1.40 1.27 1.46 1.34 1.64 Giving corrected diameters  $d_1 = \dots 3.84$ 4.39 11.35 12,99 20.58 21.52

By plotting these results, using the diameters of the cylinders for abscissas 

of Corliss engines in American practice for cylinders 10 to 30 in. diameter. The diameters range from 4 15/16 to 14 15/16, following precisely the equation,

diameter of shaft = 1/4 diameter of cylinder - 1/16 inch.

Fly-wheel Shafts .- Thus far we have considered the shaft as resisting the force of torsion and the bending moment produced by the pressure on the crank-pin. In the case of fly-wheel engines the shaft on the opposite on the crains-pin. In the case of ny-wheel engines the shatt on the opposite side of the bearing from the crains, pin has to be designed with reference to the bending moment caused by the weight of the fly wheel, the weight of the shaft itself, and the strain of the belt. For engines in which there is an ontboard bearing, the weight of fly-wheel and shaft being supported by two bearings, the point of the shaft at which the bending moment is a maximum may be taken as the point midway between the two bearings or at the middle of the fly-wheel hub, and the amount of the moment is the product of the weight supported by one of the bearings into the distance from the centre of that bearing to the middle point of the shaft. The shaft is thus to be treated as a beam supported at the ends and loaded in the middle. In the case of an overhung fly-wheel, the shaft having only one bearing, the point of maximum moments should be taken as the middle of the bearing, and its amount is very early the product of half the weight of the fly-wheel and the shaft into the distance from the middle of its hub from the middle of the bearing. The bending moment should be calculated and combined with the twisting moment as above shown, to obtain the equivalent twisting moment, and the diameter necessary at the point of maximum moment calculated therefrom.

In the case of our six engines we assume that the weights of the flywheels, together with the shaft, are double the weight of fly-wheel rim

obtained from the formula  $W = 785,400 \frac{\text{I.H.P.}}{R^3 D^2}$  (given under Fly-wheels);

that the shaft is supported by an outboard bearing, the distance between the two bearings being 2½, 5, and 10 feet for the 10-in., 30-in., and 50-in. engines, respectively. The diameters of the fly-wheels are taken such that their rim velocity will be a little less than 6000 feet per minute.

Engine No	1	2	3	4	5	6
Diam. of cyl., inches	10	10	30	30	50	50
Diam. of fly-wheel, ft	7.5	15	14.5	29	21	42
Revs. per min	250	125	130	65	90	45
Half wt.fly-wh'l and shaft,lb.		536	5,968	11,936	26,470	52,940
Lever arm for max.mom.,in.		15	30	30	60	60
Max. bending moment, inlb.	4020	8040	179,040	358,080	1,588,200	3,176,400

As these are very much less than the bending moments calculated from the pressures on the crank-pin, the diameters already found are sufficient for the diameter of the shaft at the fly-wheel hub.

In the case of engines with heavy band fly-wheels and with long fly-wheel shafts it is of the utmost importance to calculate the diameter of the shaft with reference to the bending moment due to the weight of the fly-wheel

and the shaft.

B. H. Coffey (Power, October, 1892) gives the formula for combined bending and twisting resistance,  $T_1=196d^3S$ , in which  $T_1=B+\sqrt{B^2+T^2}$ ,  $T_2$  being the maximum, not the mean twisting moment; and finds empirical working values for .1963 as below. He says: Four points should be considered in determining this value: First, the nature of the material; second, the manner of applying the loads, with shock or otherwise; third, the ratio of the bending moment to the torsional moment—the bending moment in a revolving shaft produces reversed strains in the material, which tend to rupture it; fourth, the size of the section. Inch for inch, large sections are weaker than small ones. He puts the dividing line between large and small sections at 10 in. diameter, and gives the following safe values of  $S \times$  .196 for steel, wrought iron, and cast iron, for these conditions.

Value of  $S \times .196$ .

Ratio.		avy Sh th Sho		Light shafts with Shock. Heavy Shafts No Shock.			Light Shafts No Shock.		
B to $T$ .	Steel.	Wro't Iron.	Cast Iron.	Steel.	Wro't Iron.	Cast Iron.	Steel.	Wro't Iron.	Cast Iron.
3 to 10 or less 3 to 5 or less 1 to 1 or less B greater than T	1045 941 855 784	880 785 715 655	440 393 358 328	1566 1410 1281 1176	1320 1179 1074 984	660 589 537 492	2090 1882 1710 1568	1760 1570 1430 1310	880 785 715 655

Mr. Coffey gives as an example of improper dimensions the fly-wheel shaft of a 1500 H.P. engine at Willimantic, Conn., which broke while the engine was running at 425 H.P. The shaft was 17 ft. 5 in, long between centres of bearings, 18 in, diam, for 8 ft. in the middle, and 15 in, diam, for the remainder, including the bearings. It broke at the base of the fillet connecting the two large diameters, or 56½ in, from the centre of the bearing. He calculates the mean torsional moment to be 446,651 inch-pounds, and the maximum at twice the mean; and the total weight on one bearing at 87,530 lbs., which, multiplied by 56½ in, gives 4,945,445 in.-lbs. bending moment at the fillet. Applying the formula  $T_1 = B + VB^2 + T^2$ , gives for equivalent twisting moment 9,97,405 in.-lbs. Substituting this value in the formula  $T_1 = 196$ ,  $8d^3$  gives for S the shearing strain 15,070 lbs. per sq. in., or if the metal had a shearing strength of 45,000 lbs., a factor of safety of only 3. Mr. Coffey considers that 6000 lbs, is all that should be allowed for S under these circumstances. This would give d = 2.0.25 in. If we take from Mr. Coffey's table a value of .196S = 100, we obtain  $d^3 = 9000$  nearly, or d = 20.8 in. justead of 15 in., the actual diameter.

Length of Shaft-bearings,—There is as great a difference of opinion among writers, and as great a variation in practice concerning length of journal-bearings, as there is concerning crank-pins. The length of a

journal being determined from considerations of its heating, the observa-tions concerning heating of crank-pins apply also to shaft-bearings, and the formulæ for length of crank-pins to avoid heating may also be used, using for the total load upon the bearing the resultant of all the pressures brought upon it, by the pressure on the crank, by the weight of the fly-wheel, and by the pull of the belt. After determining this pressure, however, we must resort to empirical values for the so-called constants of the formulæ, really variables, which depend on the power of the bearing to carry away heat, variables, which depend on the power of the bearing to carry away heat, and upon the quantity of heat generated, which latter depends on the pressure, on the number of square feet of rubbing surface passed over in a minute, and upon the coefficient of friction. This coefficient is an exceedingly variable quantity, ranging from .01 or less with perfectly polished journals, having end-play, and lubricated by a pad or oil-bath, to .10 or more with ordinary oil-cup lubrication.

with ordinary oil-cup lubrication. For shafts resisting torsion only, Marks gives for length of bearing  $l=0.900247f_DND^2$ , in which f is the coefficient of friction, p the mean pressure in pounds per square inch on the piston, N the number of single strokes per minute, and D the diameter of the piston. For shafts under the combined stress due to pressure on the crank-pin, weight of fly-wheel, etc., he gives the following: Let Q = reaction at bearing due to weight, S = stress due steam pressure on piston, and R, = the resultant force; for horizontal engines,  $R_1 = \sqrt{Q^2 + S^2}$ , for vertical engines  $R_1 = Q + S$ , when the pressure on the crank is in the same direction as the pressure of the shaft on its bearings, crain is in the same direction as the pressure of the shaft on its obarings, and  $R_1 = Q - S$  when the steam pressure tends to lift the shaft from its bearings. Using empirical values for the work of friction per square inch of projected area, taken from dimensions of crank-pins in marine vessels, he finds the formula for length of shaft-journals l = .0000325/R, N, and recommends that to cover the defects of workmanship, neglect of oiling, and the introduction of dust, f be taken at .16 or even greater. He says that 500 lbs pages in of projected area may hapled well for steal or wought. that 500 lbs. per sq. in, of projected area may be allowed for steel or wrought-iron shafts in brass bearings with good results if a less pressure is not attain able without inconvenience. Marks says that the use of empirical rules that do not take account of the number of turns per minute has resulted in bear-ings much too long for slow-speed engines and too short for high-speed

Whitham gives the same formula, with the coefficient .00002575

Thurston says that the maximum allowable mean intensity of pressure may be, for all cases, computed by his formula for journals,  $l = \frac{l}{60,000d}$ , or

by Rankine's,  $l = \frac{P(V+20)}{44,800d}$ , in which P is the mean total pressure in pounds,

V the velocity of rubbing surface in feet per minute, and d the diameter of the shaft in inches. It must be borne in mind, he says, that the friction work on the main bearing next the crank is the sum of that due the action of the on the main dearing next the crank is the sum of that due the action of the piston on the pin, and that due that portion of the weight of wheel and shaft and of pull of the belt which is carried there. The outboard bearing carries practically only the latter two parts of the total. The crank-shaft journals will be made longer on one side, and perhaps shorter on the other, than that of the crank-pin, in proportion to the work falling upon each, i.e., to their respective products of mean total pressure, speed of rubbing surfaces and specificative of the side of the crank-pin than the control of the crank product faces, and coefficients of friction.

Unwin says: Journals running at 150 revolutions per minute are often only one diameter long. Fan shafts running 150 revolutions per minute have journals six or eight diameters long. The ordinary empirical mode of proportioning the length of journals is to make the length proportional to the diameter, and to make the ratio of length to diameter increase with the

speed. For wrought-iron journals:

Revs. per min. = 50 100 150 200 250 500 1000 
$$\frac{l}{\bar{d}} = .004R + 1$$
.  
Length +- diam. = 1.2 1.4 1.6 1.8 2.0 3.0 5.0.

Cast-iron journals may have l + d = 9/10, and steel journals  $l + d = 1\frac{1}{4}$ , of the above values.

Unwin gives the following, calculated from the formula  $l = \frac{0.4 \text{ H.P.}}{r}$ , in which r is the crank radius in inches, and H.P. the horse-power transmitted to the crank-pin.

### THEORETICAL JOURNAL LENGTH IN INCHES.

Load on Journal	Revolutions of Journal per minute.									
in pounds.	50	100	200	300	500	1000				
1,000 2,000	.2	.4 .8 1.6	.8	1.2	2.	4. 8. 16.				
4,000 5,000	.4 .8 1.0	2.	3.2	4.8 6. 12.	4. 8. 10.	20.				
10,000 15,000 20,000	2. 3.	4. 6. 8. 12.	4. 8. 12. 16.	18.	20. 30. 40.	40.				
30,000 40,000	2. 3. 4. 6. 8.	12. 16.	24. 32.	24. 36.	40.					
50,000	10.	20.	40.							

Applying these different formluæ to our six engines, we have:

Engine No	1	2	3	4	5	6
Diam. cyl.  Horse-power.  Revs. per min.  Mean pressure on crank-pin = $S$ Half wt. of fly-wheel and $\operatorname{shaft} = Q$ .	10 50 250 3,299 268	10 50 125 3,299 536	30 450 130 23,185 5,968	30 450 65 23,185 11,936	50 1,250 90 58,905 26,470	50 1,250 45 58,905 52,940
Resultant press, on bearing $\sqrt{Q^2 + S^2} = R_1$ . Diam, of shaft journal.	3,310 3.84	3,335 4.39	,	26,194	64,580	79,200
Length of shaft journal:  Marks, $l = .0000325fR_1N(f=.10)$ Whitham, $l = .0000515fR_1R(f=.10)$ .	5.38	2.71	20.87	11.07	37.78	
Thurston, $l = \frac{PV}{60,000d}$	3.61	1.82	14.00			
Rankine, $l = \frac{P(V + 20)}{44,800d}$	7.68	2.78 6.59	21.70 17.25	16.36	27.99	25.39
Unwin, $l = \frac{0.4 \text{ H.P.}}{r}$	3.33 4.92	2.99	12.00		20.83	

If we divide the mean resultant pressure on the bearing by the projected area, that is, by the product of the diameter and length of the journal, using the greatest and smallest length out of the seven lengths for each journal given above, we obtain the pressure per square inch upon the bearing, as follows:

Engine No	1	2	3	4	5 .	6
Pressure per sq. in., shortest journal. Longest journal. Average journal. Journal of length = diam.	112 175	254	176 97 124	336 123 202 155	151 83 106	353 145 191 175

Many of the formulæ give for the long-stroke engines a length of journal less than the diameter, but such short journals are rarely used in practice. The last line in the above table has been calculated on the supposition that

the journals of the long-stroke engines are made of a length equal to the

diameter.

In the dimensions of Corliss engines given by J. B. Stanwood (Eng., June In the dimensions of Coruss engines given by J. B. Stanwood (Eng., June 12, 1891), the lengths of the journals for engines of diam. of cyl. 10 to 20 in. are the same as the diam. of the cylinder, and a little more than twice the diam, of the journal. For engines above 20 in. diam. of cyl. the ratio of length to diam, is decreased so that an engine of 30 in, diam, has a journal 20 in. long, its diameter being 14½ in. These lengths of journal are greater than those given by any of the formulæ above quoted.

There thus appears to be a hopeless confusion in the various formulæ for

length of shaft journals, but this is no more than is to be expected from the variation in the coefficient of friction, and in the heat-conducting power of journals in actual use, the coefficient varying from .10 (or even .16 as given by Marks) down to .01, according to the condition of the bearing surfaces

and the efficiency of lubrication. Thurston's formula,  $l = \frac{r}{60,000d}$ , reduces to

the form l = .00004363PR, in which P = mean total load on journal, and R = revolutions per minute. This is of the same form as Marks' and Whitham's formulæ, in which, if f the coefficient of friction be taken at .10, the coefficients of PR are, respectively, 0000065 and 000000515. Taking the mean of these three formulæ, we have l = 0000053PR, if f = 10 or l = 000053PR for any other value of f. The author believes this to be asset as formula as any for length of journals, with the limitation that if it brings a formula as any for length of journals, with the limitation that it is oring a result of length of journal less than the diameter, then the length should be made equal to the diameter. Whenever with f = .10 it gives a length which is inconvenient or impossible of construction on account of limited space, then provision should be made to reduce the value of the coefficient of friction below .10 by means of forced lubrication, end play, etc., and to carry away the heat, as by water-cooled journal-boxes. The value of Pshould be taken as the resultant of the mean pressure on the crank, and the load brought on the bearing by the weight of the shaft, fly-wheel, etc., as calculated by the formula already given, viz.,  $R_1=\sqrt{Q^2+S^2}$  for horizontal engines, and  $R_1=Q+S$  for vertical engines. For our six engines the formula l=.0000053PR gives, with the limitation

for the long-stroke engines that the length shall not be less than the diam-

eter, the following:

Engine No... Length of journal.... Pressure per square inoh on journal.. 4.39 16.48 30.80 21.52 4.39 12.99 196 173 128 155

Crank - shafts with Centre-crank and Double-crank Arms. -In centre-crank engines, one of the crank-arms, and its adjoining journal, called the after journal, usually transmit the power of the engine to the work to be done, and the journal resists both twisting and bending moments, while the other journal is subjected to bending moment only. For the after crank-journal the diameter should be calculated the same as for an overhung crank, using the formula for combined bending and twisting moment,  $T_1=B+\sqrt{B^2+T^2}$ , in which  $T_1$  is the equivalent twisting moment, B the bending moment, and T the twisting moment. This value

of  $T_1$  is to be used in the formula diameter =  $\sqrt[3]{\frac{5.1T}{8}}$ . The bending mo-

ment is taken as the maximum load on piston multiplied by one fourth of the length of the crank-shaft between middle points of the two journal bearings, if the centre crank is midway between the bearings, or by one bearings, it the centre crain is minimal between the bearings, or by one half the distance measured parallel to the shaft from the middle of the crain pin to the middle of the after bearing. This supposes the crain-shaft to be a beam loaded at its middle and supported at the ends, but Whitham would make the bending moment only one half of this, considering the shaft to be a beam secured or fixed at the ends, with a point of contrallexure one fourth of the length from the end. The first supposition is the order to the contrallexure to the contrallexure one fourth of the length from the end. the safer, but since the bending moment will have case be much less than the twisting moment, the resulting diameter will be but little greater than if Whitham's supposition is used. For the forward journal, which is sub-

jected to bending moment only, diameter of shaft =  $\sqrt[3]{\frac{10.2B}{S}}$ , in which B

is the maximum bending moment and S the safe shearing strength of the

metal per square inch.

For our six engines, assuming them to be centre-crank engines, and considering the crank-shaft to be a beam supported at the ends and loaded in the middle, and assuming lengths between centres of shaft bearings as given below, we have:

Engine No	1	2	3	4	5	6
Length of shaft, assumed, inches, $L$	20 7,854 39,270 47,124	49,637	848,232	60 70,686 1,060,290 2,120,580	3,729,750	4,712,400
Equiv. twisting moment, $B + \sqrt{B^2 + T^2}$ Diameter of after journal,	101,000	156,000	2,208,000	3,430,000	9,740,000	15,240,000
$d = \sqrt[3]{\frac{5.1T_1}{8000}}$	3.98	4.60	11.15	13.00	18.25	21.20
Diam. of forward journal, $d_1 = \sqrt[3]{\frac{10.2B}{8000}}$	1	3.99	10.28	11.16	16.82	18.18

The lengths of the journals would be calculated in the same manner as in the case of overhung cranks, by the formula l=0.00085PPC, in which P is the resultant of the mean pressure due to pressure of steam on the piston, and the load of the fly-wheel, shaft, etc., on each of the two bearings. Unless the pressures are equally divided between the two bearings, the calculated lengths of the two will be different; but it is usually customary to make them both of the same length, and in no case to make the length less than the diameter. The diameters also are usually made alike for the two journals, using the largest diameter found by calculation.

The crank-pin for a centre crank should be of the same length as for an overhung crank, since the length is determined from considerations of heating, and not of strength. The diameter also will usually be the same, since it is made great enough to make the pressure per square inch on the projected area (product of length by diameter) small enough to allow of free inbrication, and the diameter so calculated will be greater than is re-

quired for strength.

Crank-shaft with Two Cranks coupled at 90°.— If the after crank-shaft, the greatest twisting moment is equal to 1.414 times the maximum twisting moment the total the pressure on one of the crank-pins. If T = the maximum twisting moment produced by the steam-pressure on one of the plasmos, then T<sub>1</sub> the maximum twisting moment produced by the steam-pressure on one of the plasmos, then T<sub>1</sub> the maximum twisting moment on the after part of the erank-shaft, and on the line-shaft, produced when each crank makes an angle of 45° with the centre line of the engine, is 1.4147. Substituting this value in the formula for diameter to resist simple torsion, viz., d =

 $\sqrt[3]{\frac{5.17}{S}}$ , we have  $d = \sqrt[3]{\frac{5.1 \times 1.414T}{S}}$ , or  $d = 1.932 \sqrt[3]{\frac{T}{S}}$ , in which T is

the maximum twisting moment produced by one of the pistons, a= diameter in inches, and S= safe working shearing strength of the material. For the forward journal of the after crank, and the after journal of the forward crank, the torsional moment is that due to the pressure of steam on the forward piston only, and for the forward journal of the forward crank, if none of the power of the engine is transmitted through it, the torsional moment is zero, and its diameter is to be calculated for bending moment only.

For Combined Torsion and Flexure.—Let  $B_1=$  bending moment on either journal of the forward crank due to maximum pressure on

forward piston,  $B_2$  = bending moment on either journal of the after crank due to maximum pressure on after piston,  $T_1=$  maximum twisting moment on after journal of forward crank, and  $T_2=$  maximum twisting moment on

after journal of after crank due to pressure on the after piston.

Then equivalent twisting moment on after journal of forward crank  $= B_1$ 

 $+\sqrt{B_1^2+T_1^2}$ 

On forward journal of after crank =  $B_2 + \sqrt{B_2^2 + T_1^2}$ .

On after journal of after crank =  $B_2 + \sqrt{B_2^2 + (T_1 + T_2)^2}$ .

These values of equivalent twisting moment are to be used in the formula

for diameter of journals  $d = \sqrt[3]{\frac{5.1T}{S}}$ . For the forward journal of the forward crank-shaft  $d = \sqrt[3]{\frac{10.2B_1}{S}}$ .

It is customary to make the two journals of the forward crank of one distincter, viz., that calculated for the after journal. For a Three-cylinder Engine with cranks at 120°, the greatest

twisting moment on the after part of the shart, if the maximum pressures on the three pistons are equal, is equal to twice the maximum pressure on any one piston, and it takes place when two of the cranks make angles of any one piston, and it takes piace when two of the craiss make angies of 30° with the centre line, the third crank being at right angles to it. (For demonstration, see Whitham's "Steam-engine Design," p. 252.) For combined torsion and flexure the same method as above given for two crank engines is adopted for the first two cranks; and for the third, or after crank, if all the power of the three cylinders is transmitted through it, we have the equivalent twisting moment on the forward journal =  $B_3 + \sqrt{B_3^2 + (T_1 + T_2)^2}$ , and on the after journal =  $B_3 + \sqrt{B_3^2 + (T_1 + T_2)^2 + T_3^2}$ ,  $B_3$  and  $T_3$  being respectively the bending and wisting moments due to the pressure on the third piston.

Crank shafts for Triple-expansion Marine Engines, according to an article in *The Engineer*, April 25, 1890, should be made larger than the formulæ would call for, in order to provide for the stresses due to the racing of the propeller in a sea-way, which can scarcely be calculated. A kind of unwritten law has sprung up for fixing the size of a crank-shaft, according to which the diameter of the shaft is made about 0.45D, where D is the diameter of the high-pressure cylinder. This is for

0.307, where we have a single of the stroke short, the formula becomes 0 4D, even for hollow shafts.

The Valve-stem or Valve-rod.—The valve-rod should be designed to move the valve under the most unfavorable conditions, which are when the stem acts by thrusting, as a long column, when the valve is unbalanced (a balanced valve may become unbalanced by the joint leaking) and when it is imperfectly lubricated. The load on the valve is the product of the area. is in the greatest unbalanced pressure upon it per square inch, and the coefficient of friction may be as high as 20%. The product of this coefficient and the load is the force necessary to move the valve, which equals the maximum thrust on the valve-rod. From this force the diameter of the valve-rod may be calculated by Hodgkinson's formula for columns. An

empirical formula given by Seaton is: Diam. of rod =  $d = \sqrt{\frac{lbp}{k^2}}$ , in which

l = length and b = breadth of valve, in inches; p = maximum absolute pressure on the valve in lbs. per sq in, and F a coefficient whose values are, for iron: long rod 10,000, short 12,000; for steel: long rod 12,000, short 14,500. Whitham gives the short empirical rule: Diam. of valve-rod = 1/30 diam. of cyl. = ½ diam of piston-rod.

Size of Slot-link. (Seaton.)—Let D be the diam. of the valve-rod

 $D = \sqrt{\frac{lbp}{12,000}};$ 

then Diameter of block-pin when overhung = D.

"secured at both ends =  $0.75 \times D$ .

"secured at both ends =  $0.71 \times D$ . eccentric-rod pins

suspension-rod pins =  $0.55 \times D$ . " pin when overhung =  $0.75 \times D$ .

= 0.8 to  $0.9 \times D$ . = 1.8 to  $1.6 \times D$ . Breadth of link Length of block

Thickness of bars of link at middle  $= 0.7 \times D$ .

If a single suspension rod of round section, its diameter  $= 0.7 \times D$ .

If two suspension rods of round section, their diameter  $= 0.55 \times D$ .

Size of Double-bar Links.—When the distance between centres of eccentric pins = 6 to 8 times throw of eccentrics (throw = eccentricity = half-travel of valve at full gear) D so before:

 $\begin{array}{lll} \text{Depth of bars} &=& 1.25 \times D + 34 \text{ in.} \\ \text{Thickness of bars} &=& 0.5 \times D + 34 \text{ in.} \\ \text{Length of sliding-block} &=& 2.5 \text{ to } 3 \times D. \\ \text{Diameter of eccentric-rod pins} &=& 0.8 \times D + 14 \text{ in.} \\ \text{``entre of sliding-block} &=& 1.3 \times D. \end{array}$ 

When the distance between eccentric-rod pins = 5 to 51/6 times throw of eccentrics:

=  $1.25 \times D + \frac{1}{2}$  in. =  $0.5 \times D + \frac{1}{4}$  in. =  $2.5 \text{ to } 3 \times D$ . Depth of bars Thickness of bars Length of sliding-block

Diameter of eccentric-rod pins =  $0.75 \times D$ .

Diameter of eccentric bolts (top end) at bottom of thread =  $0.42 \times D$  when

The Eccentric.—Diam. of eccentric-sheave =  $2.4 \times$  throw of eccentric + 1.2 × diam. of shaft, D as before

Breadth of the sheave at the shaft..... = 1.15  $\times$  D + 0.65 inch Breadth of the Sheave at the strap. = D + 0.6 inch. Thickness of metal around the shaft  $= 0.7 \times D + 0.5$  inch. Thickness of metal arctreumference  $= 0.6 \times D + 0.4$  inch. Breadth of key  $= 0.7 \times D + 0.5$  inch. Thickness of key  $= 0.7 \times D + 0.5$  inch. Diameter of bolts connecting parts of strap  $= 0.6 \times D + 0.4$  inch.

# THICKNESS OF ECCENTRIC-STRAP.

When of bronze or malleable cast iron:

Thickness of eccentric-strap at the middle.... =  $0.4 \times D + 0.6$  inch.  $0.3 \times D + 0.5$  inch.

When of wrought iron or cast steel:

Thickness of eccentric-strap at the middle  $= 0.4 \times D + 0.5$  inch.  $= 0.27 \times D + 0.4$  inch.

The Eccentric-rod.—The diameter of the eccentric-rod in the body and at the eccentric end may be calculated in the same way as that of the connecting-rod, the length being taken from centre of strap to centre of pin. Diameter at the link end = 0.8D + 0.2 inch. This is for wrought-iron; no reduction in size should be made for steel.

Eccentric-rods are often made of rectangular section.

Reversing-gear should be so designed as to have more than sufficient strength to withstand the strain of both the valves and their gear at the same time under the most unfavorable circumstances; it will then have the

stiffness requisite for good working. Assuming the work done in reversing the link-motion, W, to be only that due to overcoming the friction of the valves themselves through their whole travel, then, if T be the travel of valves in inches; for a compound engine

$$W = \frac{T}{12} \left( \frac{l \times b \times p}{5} \right) + \frac{T}{12} \left( \frac{l^1 \times b^1 \times p^1}{5} \right);$$

l¹, b¹ and p¹ being length, breadth and maximum steam-pressure on valve of the second cylinder; and for an expansive engine

$$W = 2 \times \frac{T}{12} \left( \frac{l \times b \times p}{5} \right); \text{ or } \frac{T}{30} (l \times b \times p).$$

To provide for the friction of link-motion, eccentrics and other gear, and for abnormal conditions of the same, take the work at one and a half times the above amount.

To find the strain at any part of the gear having motion when reversing. divide the work so found by the space moved through by that part in feet; the quotient is the strain in pounds; and the size may be found from the ordinary rules of construction for any of the parts of the gear. (Seaton.)

Engine-frames or Bed-plates.—No definite rules for the design

of engine-frames have been given by authors of works on the steam-engine. The proportions are left to the designer who uses "rule of thumb." or copies from existing engines. F. A. Halsey (Am. Mach., Feb. 14, 1895) has made a comparison of proportions of the frames of horizontal Corliss engines of several builders. The method of comparison is to compute from the measurements the number of square inches in the smallest cross-section of the frame, that is, immediately behind the pillow-block, also to compute the total maximum pressure upon the piston, and to divide the latter quantity by the former. The result gives the number of pounds pressure upon the piston allowed for each square inch of metal in the frame. He finds that the number of pounds per square inch of smallest section of frame ranges from 217 for a 10×30-in. engine up to 575 for a  $28 \times 48$ -inch. A  $30 \times 60$ -inch engine shows 350 lbs., and a 32-inch engine which has been running for many years shows 667 lbs. Generally the strains increase with the size of the engine, and more cross-section of metal

is allowed with relatively long strokes than with short ones.

From the above Mr. Halsey formulates the general rule that in engines of moderate speed, and having strokes up to one and one half times the diameter of the cylinder, the load per square inch of smallest section should be for a 10-inch engine 300 pounds, which figure should be increased for larger bores up to 500 pounds for a 30-inch cylinder of same relative stroke. For high speeds or for longer strokes the load per square inch should be reduced.

## FLY-WHEELS.

The function of a fly-wheel is to store up and to restore the periodical fluctuations of energy given to or taken from an engine or machine, and thus to keep approximately constant the velocity of rotation. Rankine calls the

quantity  $\frac{2E_0}{2E_0}$ - the coefficient of fluctuation of speed or of unsteadiness, in

which  $E_0$  is the mean actual energy, and  $\Delta E$  the excess of energy received or of work performed, above the mean, during a given interval. The ratio of the periodical excess or deficiency of energy  $\Delta E$  to the whole energy exerted in one period or revolution General Morin found to be from 1/6 to  $\frac{1}{2}$  for in one period or revolucin central moin found to be find a fact of the single-cylinder engines using expansion; the shorter the cut-off the higher the value. For a pair of engines with cranks coupled at 90° the value of the ratio is about 14, and for three engines with cranks at 120°, 1/12 of its value for single cylinder engines. For tools working at intervals, such as punching, slotting and plate-cutting machines, coining-presses, etc.,  $\Delta E$  is nearly equal to the whole work performed at each operation.

A fly-wheel reduces the coefficient  $\frac{\Delta E}{2}$  to a certain fixed amount, being about 1/32 for ordinary machinery, and 1/50 or 1/60 for machinery for fine

If m be the reciprocal of the intended value of the coefficient of fluctuation of speed,  $\Delta E$  the fluctuation or energy, I the moment of inertia of the fly-wheel alone, and  $a_0$  its mean angular velocity,  $I=rac{mg\Delta E}{c}$ As the rim of

a fly-wheel is usually heavy in comparison with the arms, I may be taken to equal  $Wr^2$ , in which W = weight of rim in pounds, and r the radius of the

wheel; then  $W = \frac{mg\Delta E}{a_0^2 r^2} = \frac{mg\Delta E}{v^2}$ , if v be the velocity of the rim in feet per second. The usual mean radius of the fly-wheel in steam-engines is from

three to five times the length of the crank. The ordinary values of the prod-uction, the unit of time being the second, lie between 1000 and 2000 feet. (Abridged from Ranking, S. E., p. 62.) Thurston gives for engines with automatic valve-gear W = 250,000

 $\frac{2DP}{R^2D^2}$ , in which A= area of piston in square inches, S= stroke in feet, p=mean steam pressure in lbs. per sq. in., R = revolutions per minute, D = outside diameter of wheel in feet. Thurston also gives for ordinary forms of non-condensing engine with a ratio of expansion between 3 and 5, W = $\frac{62.5}{R^2D_2^2}$  in which a ranges from 10,000,000 to 15,000,000, averaging 12,000.000.

For gas-engines, in which the charge is fired with every revolution, the American Machinist gives this latter formula, with a doubled, or 24,000,000. Presumably, if the charge is fired every other revolution, a should be again doubled.

Rankine ("Useful Rules and Tables," p. 247) gives  $W = 475,000 \frac{ASp}{VD^2R^2}$ , in which V is the variation of speed per cent. of the mean speed. Thurston's first rule above given corresponds with this if we take Vat 1.9 per cent. Hartnell (Proc. Inst., M. E. 1882, 427) says: The value of V, or the

Hatthen (Froc. list., M. E. 1852, 427) says: The value of V, of the variation permissible in portable engines, should not exceed 8 per cent. with an ordinary load, and 4 per cent when heavily loaded. In fixed engines, for ordinary purposes,  $V = 2\frac{1}{2}$  to 3 per cent. For good governing or special purposes, such as cotton-spinning, the variation should not exceed  $1\frac{1}{2}$  to 2per cent.

per cent. F. M. Ritcs (Trans. A. S. M. E., xiv. 100) develops a new formula for weight of rim, viz.,  $W = \frac{C \times \text{I.H.P.}}{R^3 D^2}$ , and weight of rim per horse-power  $= \frac{C}{R^3 D^2}$ ; which C varies from 10,000,000,000 to 20,000,000,000; also using the latter value of C, he obtains for the energy of the fly-wheel  $\frac{Mv^2}{2} = \frac{W}{64.4} \frac{3.14^3 D^3 R^2}{3600} = \frac{1.000}{1.000}$ 

 $\frac{C \times \text{H.P.}(3.14)^{\circ}D^{\circ}R^{\circ}}{R^{\circ}D^{\circ} \times 64.4 \times 3600} = \frac{850,000 \text{ H.P.}}{R}$ . Fly wheel energy per H.P. = 850,000

The limit of variation of speed with such a weight of wheel from excess of

power per fraction of revolution is less than .0023.

The value of the constant C given by Mr. Rites was derived from practice of the Westinghouse single-acting engines used for electric-lighting. For double-acting engines in ordinary service a value of C = 5,000,000,000 would probably be ample.

From these formulæ it appears that the weight of the fly-wheel for a given horse-power should vary inversely with the cube of the revolutions and the

square of the diameter.

J. B. Stanwood (Eng'g, June 12, 1891) says: Whenever 480 feet is the lowest piston-speed probable for an engine of a certain size, the fly-wheel weight for that speed approximates closely to the formula

$$W = 700,000 \frac{d^2s}{D^2R^2}$$

W = weight in pounds, d = diameter of cylinder in inches, s = stroke in inches, D = diameter of wheel in feet, R = revolutions per minute, corre-

sponding to 480 feet piston-speed.

In a Ready Reference Book published by Mr. Stanwood, Cincinnati, 1892, he gives the same formula, with coefficients as follows: For slide-valve engines, ordinary duty, 350,000; same, electric-lighting, 700,000; for automatic high-speed engines, 1,000,000; for Corliss engines, ordinary duty 700,000, electric-lighting 1,000,000.

Thurston's formula above given,  $W = \frac{aAS}{R^2D^2}$ , with a = 12,000,000, when reduced to terms of d and s in inches, becomes  $W = 785,400 \frac{d^2s}{R^2D^2}$ 

If we reduce it to terms of horse-power, we have I.H.P. =  $\frac{2.2451 \text{ A}}{33.000}$ in which P = mean effective pressure. Taking this at 40 lbs., we obtain  $W = 5,000,000,000 \frac{\text{I.H.P.}}{R^3 D^2}.$   $6,666,000,000 \frac{\text{I.H.P.}}{R^3 D^2}.$ If mean effective pressure = 30 lbs., then W =

Emil Theiss (Am. Mach., Sept. 7 and 14, 1893) gives the following values or d, the coefficient of steadiness, which is the reciprocal of what Rankine calls the coefficient of fluctuation:

For engines operating-

Hammering and crushing machinery	d	=	5		
Pumping and shearing machinery	d	=	20	to	30
Weaving and paper-making machinery	d	=	40		
Milling machinery	d	=	50		
Spinning machinery	d	=	50	to	100
Ordinary driving-engines (mounted on bed-plate),					

where d is the coefficient of steadiness, V the mean velocity of the flywheel rim in feet per second, n the number of revolutions per minute, i a coefficient obtained by graphical solution, the values of which for different conditions are given in the following table. In the lines under "out off," p means "compression to initial pressure," and O "no compression":

VALUES OF i. SINGLE-CYLINDER NON-CONDENSING ENGINES.

Piston- speed, ft. per min.	Cut-of	f, 1/6.	Cut-o	ff, ¼.	Cut-o	ff, ½.	Cut-off, 1/2.		
Pist spee per	$\mathop{\mathrm{Comp.}}_{p}$	0	$_{p}^{\mathrm{Comp.}}$	o	$_{p}^{\mathrm{Comp.}}$	0	$\operatorname*{Comp.}{p}$	0	
200 400 600 800	272,690 240,810 194,670 158,200	187,430 145,400	208,200 168,590	179,460 136,460		170,040	174,630		

### SINGLE-CYLINDER CONDENSING ENGINES.

on- 1, ft. nin.	Cut-off, 1/8.		Cut-off, 1/6.		Cut-off, 1/4.		Cut-off, 1/3.		Cut-off, 1/2.	
Pist speed per 1	Comp.	0	$\mathop{\mathrm{comp}}_p$	0	$\mathop{\mathrm{Comp.}}_{p}$	0	$\operatorname*{Comp.}{p}$	0	$_{p}^{\mathrm{Comp.}}$	0
400	194,550	117,870	174,380	118,350	204,210 164,720	133,080	189,600 174,630	161,830 151,680	172,690	156,990

### TWO-CYLINDER ENGINES, CRANKS AT 90°.

d, ft.	Cut-off, 1/6.		Cut-off, ¼.		Cut-off, 1/2.		Cut-off, 1/2.	
Pistc speed per n	$\operatorname*{Comp.}_{p}$	0	$\operatorname*{Comp.}{p}$	0	$_{p}^{\operatorname*{Comp.}}$	0	Comp.	0
200 400 600 800	71,980 70,160 70,040 70,040	Mean 60,140	59,420 57,000 57,480 60,140	Mean 54,340		Mean   50,000	37,920 35,500	} Mean } 36,950

# THREE-CYLINDER ENGINES, CRANKS AT 120°.

d, ft. Min.	Cut-off, 1/6.		Cut-off, 1/4.		Cut-off, 1/3.		Cut-off, 1/2.	
Pist speed per	$\operatorname*{Comp.}{p}$	0	Comp.	0	$\mathop{\mathrm{Comp.}}_{p}$	0	p	0
200 800	33,810 30,190	32,240 31,570	33,810 35,140	35,500 33,810	34,540 36,470	33,450 32,850	35,260 33,810	32,370 32,370

As a mean value of i for these engines we may use 33,810.

Centrifugal Force in Fly-wheels.—Let W = weight of rim in pounds; R = mean radius of rim in teet; r = revolutions per minute, g =32.16;  $v = \text{velocity of rim in feet per second} = 2\pi Rr \div 60$ .

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Centrifugal force of whole rim  $= F = \frac{Wv^2}{}$  $\frac{Wv^2}{qR} = \frac{4W\pi^2Rr^2}{3600q}$  $- = .000341 WRr^{2}$ .

The resultant, acting at right angles to a diameter of half of this force, tends to disrupt one half of the wheel from the other half, and is resisted by the section of the rim at each end of the diameter. The resultant of half the radial forces taken at right angles to the diameter is  $1 \div \frac{1}{2} = \frac{2}{\pi}$  of the sum

of these forces; hence the total force F is to be divided by  $2 \times 2 \times 1.5708$ 6.2832 to obtain the tensile strain on the cross-section of the rim, or, total strain on the cross-section  $S=0.000543'WR^{2}$ . The weight  $W_{1}$  of a rim of east iron 1 inch square in section is  $2\pi R \times 3.125 = 19.635R$  pounds, whence strain per square inch of sectional area of rim  $= S_1 = .0010556R^2 \cdot ^2 = .0020564D^2 \cdot ^2 = .000276V^2$ , in which D = diameter of wheel in feet, and V is velocity of rim in feet per minute.  $S_1 = .007224$ , if V is taken in feet per second.

 $\begin{array}{lll} \text{For wrought iron.} & S_1 = .0011366R^2 r^2 = .0002842D^2 r^2 = .000288V^2. \\ \text{For steel.} & S_1 = .0011558R^2 r^2 = .0002901D^2 r^2 = .0000294V^2. \\ \text{For wood.} & S_1 = .0000888R^2 r^2 = .00002291P^2 r^2 = .0000225V^2. \end{array}$ 

The specific gravity of the wood being taken at 0.6 = 37.5 lbs. per cu. ft., or 1/12 the weight of cast iron.

Example.—Required the strain per square inch in the rim of a cast-iron

wheel 30 ft, diameter, 60 revolutions per minute, Answer.  $15^2 \times 60^2 \times .0010656 = 863.1$  lbs.

Required the strain per square inch in a cast-iron wheel-rim running a mile a minute. Answer. .000027 × 52802 = 752.7 lbs.

In cast-iron fly-wheel rims, on account of their thickness, there is difficulty in securing soundness, and a tensile strength of 10,000 lbs. per sq. in. is as much as can be assumed with safety. Using a factor of safety of 10 gives a maximum allowable strain in the rim of 1000 lbs. per sq. in., which corresponds to a rim velocity of 6085 ft. per minute,

For any given material, as cast iron, the strength to resist centrifugal force depends only on the velocity of the rim, and not upon its bulk or weight.

Chas. E. Emery (Cass. Mag., 1892) says: By calculation half the strength of the arms is available to strengthen the rim, or a trifle more if the fly-wheel centres are relatively large. The arms, however, are subject to transverse strains, from belts and from changes of speed, and there is, moreover, no certainty that the arms and rim will be adjusted so as to pull exactly

no certainty that the arms and rim will be adjusted so as to buil exactly together in resisting disruption, so the plan of considering the rim by itself and making it strong enough to resist disruption by centrifugal force within safe limits, as is assumed in the calculations above, is the safer way. It does not appear that fly-wheels of customary construction should be unsafe at the comparatively low speeds now in common use if proper materials are used in construction. The cause of rupture of fly-wheels that have falled is usually either the "running away" of the engine, such as may be caused by the breaking or slackness of a governor-belt, or incorrect

design or defective materials of the fly-wheel.

Clas. T. Porter (Trans. A. S. M. E., xiv. 808) states that no case of the bursting of a fly-wheel with a solid rim in a high-speed engine is known. He attributes the bursting of wheels built in segments to insufficient strength of the flanges and bolts by which the segments are held together. (See also Thurston, "Manual of the Steam-engine," Part II, page 413, etc.)

Arms of Fly-wheels and Pulleys, - Professor Torrey (Am. Mack., July 30, 1891) gives the following formula for arms of elliptical cross-

section of cast-iron wheels: W = load in pounds acting on one arm; S = strain on belt in pounds per

inch of width, taken at 56 for single and 112 for double belts; v = width of belt in inches; n = number of arms; L = length of arm in feet; b = breadth of arm at hub; d = depth of arm at hub, both in inches:

The breadth of the arm is its least dimension = minor axis of the ellipse, and the depth the major axis. This formula is based on a factor of safety of 10.

In using the formula, first assume some depth for the arm, and calculate the required breadth to go with it. If it gives too round an arm, assume the breadth a little greater, and repeat the calculation. A second trial will

use oreacm a nuture greater, and repeat the calculation. A second trial will almost always give a good section.

The size of the arms at the hub having been calculated, they may be somewhat reduced at the time and. The actual amount cannot be calculated, as there are too many unknown quantities. However, the depth and breadth can be reduced about one third at the rim without danger, and this will give a well-shaped arm.

Pulleys are often each of the control of the c

Pulleys are often east in halves, and bolted together. When this is done the greatest care should be taken to provide sufficient metal in the boltz. This is apt to be the very weakest point in such pulleys. The combined area of the bolts at each joint should be about 28/100 the cross-section of the pulley at that point. (Torrey.)

Unwin gives 
$$d=0.6337\sqrt[2]{\frac{BD}{n}} \text{ for single belts ;}$$
 
$$d=0.798 \sqrt{\frac{BD}{n}} \text{ for double belts;}$$

D being the diameter of the pulley, and B the breadth of the rim, both in inches. These formulæ are based on an elliptical section of arm in which be 0.44 or d=2.5b on a width of belt =4/5 the width of the pulley rim, a maximum driving force transmitted by the belt of 56 lbs, per inch of width for a single belt and 112 lbs, for a double belt, and a safe working stress of east iron of 2250 lbs, per square inch.

If in Torrey's formula we make b = 0.4d, it reduces to

$$b=\sqrt[3]{\frac{\overline{WL}}{187.5}}; \quad d=\sqrt[3]{\frac{\overline{WL}}{12}}.$$

Example.—Given a pulley 10 feet diameter; 8 arms, each 4 feet long; face, 36 inches wide; belt, 30 inches; required the breath and depth of the arm at the hub. According to Unwin,

$$d = 0.6337 \sqrt[3]{\frac{\overline{BD}}{n}} = 0.633 \sqrt[3]{\frac{36 \times 120}{8}} = 5.16 \text{ for single belt, } b = 2.06;$$

$$d = 0.798 \sqrt[3]{\frac{\overline{BD}}{n}} = 0.798 \sqrt[3]{\frac{36 \times 120}{8}} = 6.50 \text{ for double belt, } b = 2.60.$$

According to Torrey, if we take the formula  $b=\frac{WL}{30d^2}$  and assume d=5

and 6.5 inches, respectively, for single and double belts, we obtain b = 1.08and 1.33, respectively, or practically only one half of the breadth according to Unwin, and, since transverse strength is proportional to breadth, an arm

only one half as strong.

Torrey's formula is said to be based on a factor of safety of 10, but this Torrey's formula is said to be based on a factor of safety or 10, but that factor can be only apparent and not real, since the assumption that the strain on each area is equal to the strain on the belt divided by the number of arms, is, to say the least, inaccurate. It would be more nearly correct to say that the strain of the belt is divided among half the number of arms. Unwin makes the same assumption in developing his formula, but says it is only in a rough sense true, and that a large factor of safety must be allowed. He therefore takes the low figure of \$250 lbs. per square inch for the safe working strength of cast iron. Unwin says that his equations agree well with practice.

**Diameters of Fly-wheels for Various Speeds.**—If 6000 feet per minute be the maximum velocity of rim allowable, then  $6000 = \pi B D$ , which R = revolutions per minute, and D = diameter of wheel in feet,

whence  $D = \frac{6000}{\pi R} = \frac{1910}{R}$ .

MAXIMUM DIAMETER OF FLY-WHEEL ALLOWABLE FOR DIFFERENT NUMBERS

Revolutions	Assuming Maxi 5000 feet p	mum Speed of er minute	Assuming Maximum Speed of 6000 feet per minute.			
per minute.	Circum. ft.	Diam. ft.	Circum, ft.	Diam. ft.		
40	125	39.8	150.	47.7		
50	100	31.8	120.	38.2		
60	83.3	26.5	100.	31.8		
70	71.4	22.7	85.72 75.00	27.3		
80 90	62.5 55.5	19.9 17.7	66.66	23.9 21.2		
100	50.	15.9	60.00	19.1		
120	41.67	13.3	50.00	15.9		
140	35.71	11.4	42.86	13.6		
160	31.25	9.9	37.5	11.9		
180	27.77	8.8	33.33	10.6		
200	25.00	8.0	30.00	9.6		
220	22.73	7.2	27.27	8.7		
240	20.83	6.6	25.00	8.7 8.0		
260	19.23	6.1	23.08	7.3		
280	17.86	5.7	21.43	6.8		
300	16.66	5.3	20.00	6.4		
350	14.29	4.5	17.14	5.5		
400	12.5	4.0	15.00	4.8		
450	11.11	3.5	13.33	4.2		
500	10.00	3.2	12.00	3.8		

Strains in the Rims of Fly-band Wheels Produced by Centrifugal Force, James B. Stanwood, Trans. A. S. M. E., xiv. 251.)

-Mr. Stanwood mentions one case of a fly-band wheel where the periphery velocity on a 17' 9" wheel is over 7500 ft. per minute.

In band saw-mills the blade of the saw is operated successfully over

In band saw-mills the blade of the saw is operated successfully over wheels 8 and 9 ft. in diameter, at a periphery velocity of 9000 to 10,000 ft. per minute. These wheels are of cast iron throughout, of heavy thickness, with a large number of arms.

In shingle-machines and chipping-machines where cast-iron disks from 2 to 5 ft. in diameter are employed, with knives inserted radially, the speed is frequently 10,000 to 1,000 ft. per minute at the periphery.

If the rim of a fly-wheel alone be considered, the tensile strain in pounds

If the rim of a fly wheel alone be considered, the tensile strain in pounds per square inch of the rim section is  $T = \frac{V^2}{40}$  nearly, in which V = velocity

in feet per second; but this strain is modified by the resistance of the arms, which prevent the uniform circumferential expansion of the rim, and induce a bending as well as a tensile strain. Mr. Stanwood discusses the strains in band-wheels due to transverse bending of a section of the rim between a pair of arms.

When the arms are few in number, and of large cross-section, the ring will be strained transversely to a greater degree than with a greater number of lighter arms. To illustrate the necessary rim thicknesses for various rim velocities, pulley diameters, number of arms, etc., the following table is given, based upon the formula

$$t = \frac{.475d}{N^2 \left(\frac{F}{V^2} - \frac{1}{10}\right)},$$

in which t= thickness of rim in inches, d= diameter of pulley in inches, N= number of arms, V= velocity of rim in feet per second, and F= the greatest strain in pounds per square inch to which any fibre is subjected. The value of F is taken at 6000 lbs. per sq. in,

## Thickness of Rims in Solid Wheels.

Diameter of Pulley in inches.	Velocity of Rim in feet per second.	Velocity of Rim in feet per minute.	No. of Arms.	Thickness in inches.
24	50	3,000	6	2/10 15/32
24	50 88 88	5,280 5,280	6	15/32
48	88	5,280	6	15/16
24 48 108	184	11,040	16	21/2
108	184	11,040	36	1/2

If the limit of rim velocity for all wheels be assumed to be 88 ft. per second, equal to 1 mile per minute, F = 6000 lbs., the formula becomes

$$t = \frac{.475d}{.67N^2} = 0.7 \frac{d}{N^2}$$

When wheels are made in halves or in sections, the bending strain may be such as to make t greater than that given above. Thus, when the joint comes half way between the arms, the bending action is similar to a beam supported simply at the ends, uniformly loaded, and t is 50% greater. Then the formula becomes

$$t = \frac{.712d}{N^2 \left(\frac{F}{V^2} - \frac{1}{10}\right)}.$$

or for a fixed maximum rim velocity of 88 ft, per second and F = 6000 lbs.In segmental wheels it is preferable to have the joints opposite

the arms. Wheels in halves, if very thin rims are to be employed, should have double arms along the line of separation,

have double arms along the line of separation,
Attention should be given to the proportions of large receiving and tightening pulleys. The thickness of rim for a 48-in, wheel (shown in table) with
a rim velocity of 88 ft. per second, is 15/16 in. Many wrecks have been
caused by the failure of receiving or tightening bulleys whose rims have been
too thin. Fly-wheels calculated for a given coefficient of steadness are frequently lighter than the minimum safe weight. This is true especially of
large wheels. A rough guide to the minimum weight of wheels can be de-Guently lighter than the minimum saie weight. This is the especially of large wheels. A rough guide to the minimum weight of wheels can be deduced from our formulæ. The arms, bub, logs, etc., usually form from one quarter to one third the entire weight of the wheel. If b represents the fact of a wheel in inches, the weight of the rim (considered as a simple annular ring) will be w = .824tb lbs. If the limit of speed is 88 ft, per second, then for solid wheels  $t = 0.74 + N^2$ . For sectional wheels (joint between arms,  $t = .0564 + N^2$  in pounds. Weight of rim for solid wheels,  $w = .5642b + N^2$  in pounds. Weight of rim to sectional wheels with joints between arms,  $w = .8662b + N^2$  in pounds. Total weight of wheel: for solid wheels  $w = .7642b + N^2$  to  $.8662b + N^2$  to  $.1242b + N^2$ ; in pounds. (This subject is further discussed by Mr. Stanwood, in vol. xv., and by Prof. Gaetano Lanza, in vol. xvi, Trans. A. S. M. E.;)

A Wooden Kim Fly-wheel, built in 1891 for a pair of Corliss engines at the Amoskeag Mr. Co.'s mill. Manchester, N. H., is described by C. H. Manning in Trans. A. S. M. E., xiii, 68. It is 30 ft. dam, and 108 in face. The rim is 12 inches thick, and is built up of 44 courses of ash plank, 2, 3, and 4 inches thick, reduced about  $\frac{1}{2}$  inch in dressing, set edgewise, so as the break joints, and glued and bolied together. There are two hubs and two sets of arms, 12 in each, all of cast iron. The weights are as follows: Weight (calculated) of ash rim.

Weight (calculated) of ash rim	31,855 lbs.
" of 24 arms (foundry 45,020)	40,349 "
" 2 hubs ( " 35,030)	31,394 "
Counter-weights in 6 arms	664 "
Total, excluding bolts and screws	104,262+ "

The wheel was tested at 76 revs. per min., being a surface speed of nearly 7200 feet per minute.

Mr. Manning discusses the relative safety of cast iron and of wooden wheels as follows: As for safety, the speeds being the same in both cases, the hoop tension in the rim per unit of cross-section would be directly as the weight per cubic unit; and tis capacity to stand the strain directly as the tensile strength per square unit; therefore the tensile strengths divided by the weights will give relative values of different materials. Cast iron weighing 450 lbs, per cubic foot and with a tensile strength of 1,440,000 lbs, per square foot would give a value of 1,440,000 + 450 = 3200, whilst ash, of which the rim was made, weghing 34 lbs, per cubic foot, and with 1,152,000 lbs, tensile strength per square foot, gives a result 1,152,000 + 34 = 33,882, and 33,882 + 3200 = 10.56, or the wood-rimmed pulley is ten times safer than the cast-iron when the castings are good. This would allow the wood-rimmed pulley to increase its speed to \footnote{10.58} = 3.25 times that of a sound cast-iron one with equal safety.

Wooden Fly-wheel of the Willimantic Linen Co. (filus-

Wooden Fly-wheel of the Willimantic Linen Co. (Illustrated in *Power*, March, 1893.)—Rim 28 ft. diam., 110 in. face. The rim is carried upon three sets of arms, one under the centre of each belt, with 12

arms in each set.

The material of the rim is ordinary whitewood, ½ in. in thickness, cut into segments not exceeding 4 feet in length, and either 5 or 8 inches in width. These were assembled by building a complete circle 13 inches in width, first with the 8 inch inside and the 5-inch outside, and then beside it another circle with the widths reversed, so as to break joints. Each piece as it was added was brushed over with glue and nailed with three-inch wire nails to the pieces already in position. The nails pass through three and into the fourth thickness. At the end of each arm four 14-inch bolts secure the rim, the ends being covered by wooden plugs glued and driven into the face of the wheel.

Wire-wound Fly-wheels for Extreme Speeds. (Engly News, August 2, 1880).—The power required to produce the Mannesmann tubes is very large, varying from 2000 to 10,000 H.P., according to the dimensions of the tube. Since this power is only needed for a short time (it takes only 30 to 45 seconds to convert a bar 10 to 12 ft. long and 4 in. in diameter into a tube), and then some time elapses before the next bar is ready, an engine of 1200 H.P. provided with a large fly-wheel for storing the energy will supply power enough for one set of rolls. These fly-wheels are so large and run at such great speeds that the ordinary method of constructing them cannot be followed. A wheel at the blannesmann Works, made in Komotau, Hungary, in the usual mannet, broke at a tangential velocity of 125 ft. per second. The fly-wheels designed to hold at more than double this speed consist of a cast-iron hub to which two steel disks, 20 ft. in diameter, are bolted; around the circumference of the wheel thus formed 70 tons of No, 5 wire are wound under a tension of 50 fbs. In the Mannesmann Works at Landore, Wales, such a wheel makes 240 revolutions a minute, corresponding to a tangential velocity of 15,690 ft. or 2.85 miles per minute.

# THE SLIDE-VALVE.

Definitions.-Travel = total distance moved by the valve.

Throw of the Eccentric = eccentricity of the eccentric = distance from the centre of the shaft to the centre of the eccentric disk = 3½ the travel of the valve. (Some writers use the term "throw" to mean the whole travel of the valve).

Lap of the valve, also called outside lap or steam-lap = distance the outer or steam edge of the valve extends beyond or laps over the steam edge of

the port when the valve is in its central position.

Inside lap, or exhaust-lap = distance the inner or exhaust edge of the valve extends beyond or laps over the exhaust edge of the port when the valve is in its central position. The inside lap is sometimes made zero, or even negative, in which latter case the distance between the edge of the valve and the edge of the port is sometimes called exhaust clearance, or inside clearance.

Lead of the valve = the distance the steam-port is opened when the engine

is on its centre and the piston is at the beginning of the stroke

Lead-angle = the angle between the position of the crank when the valve begins to be opened and its position when the piston is at the beginning of the stroke.

The valve is said to have lead when the steam-port opens before the piston

begins its stroke. If the piston begins its stroke before the admission of steam begins the valve is said to have negative lead, and its amount is the lap of the edge of the valve over the edge of the port at the instant when the piston stroke begins.

Lup-angle = the angle through which the eccentric must be rotated to cause the steam edge to travel from its central position the distance of the

lap.

Angular advance of the eccentric = lap-angle + lead angle.

 $Linear\ advance = lap + lead$ .

Reflected the property of the steam Distribution. Given valve tax  $a_i$   $b_i$   $b_i$ 

If a valve has neither lap nor lead, the line joining the centre of the eccen-

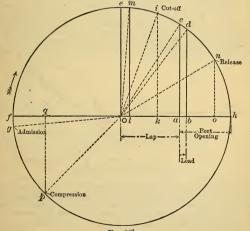


Fig. 146.

tric disk and the centre of the shaft being at right angles to the line of the crank, the engine would follow full stroke, admission of steam beginning at the troke and ending at the end of the stroke.

Adding lap to the valve enables us to cut off steam before the end of the

Adding lap to the valve enables us to cut off steam before the end of the stroke; the eccentric being advanced on the shaft an amount equal to the lap-angle enables steam to be admitted at the beginning of the stroke, as

before lap was added, and advancing it a further amount equal to the lead angle causes steam to be admitted before the beginning of the stroke. Having given lap to the valve, and having advanced the eccentric on the shaft from its central position at right angles to the crank, through the angular advance = lap-angle and lead-angle, the four events, admission, augular advance = lap-angle and lead-angle, the four events, admission, cut-off, release or exhaust-opening, and compression or exhaust-closure, take place as follows: Admission, when the crank lacks the lead-angle of having reached the centre; cut-off, when the crank lacks two lap-angles and one lead-angle of having reached the centre. During the admission of steam the crank turns through a semicircle less twice the lap-angle. greatest port opening is equal to half the travel of the valve less the lap. Therefore for a given port-opening the travel of the valve must be increased if the lap is increased. When exhaust-lap is added to the valve it delays the opening of the exhaust and hastens its closing by an angle of rotation equal to the exhaust-lap angle, which is the angle through which the eccentric rotates from its middle position while the exhaust edge of the valve uncovers its lap. Release then takes place when the crank lacks one lap-angle and one lead-angle minus one exhaust-lap angle of having reached the centre, and compression when the crank lacks lap-angle + lead-angle + exhaust-lap angle of having reached the centre.

The above discussion of the relative position of the crank, piston, and valve for the different points of the stroke is accurate only with a connect-

ing-rod of infinite length.

For actual connecting-rods the angular position of the rod causes a distortion of the position of the valve, causing the events to take place too late in the forward stroke and too early in the return. The correction of this distortion may be accomplished to some extent by setting the valve so as to give equal lead on both forward and return stroke, and by altering the exhaust-lap on one end so as to equalize the release and compression. F. A. Halsey, in his Slide-valve Gears, describes a method of equalizing the cut-off without at the same time affecting the equality of the lead. In designing slide-valves the effect of angularity of the connecting-rod should be studied on the drawing-board, and preferably by the use of a model.

Sweet's Valve-diagram .- To find outside and inside lap of valve for different cut-offs and compressions (see Fig. 147); Draw a circle whose

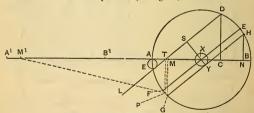


Fig. 147.—Sweet's Valve-diagram.

diameter equals travel of valve. Draw diameter BA and continue to A1, so that the length  $AA^1$  bears the same ratio to XA as the length of connecting rod does to length of engine-crank. Draw small circle E with a diameter equal to lead. Lay off AC so that ratio of AC to AB = cut-off in parts of the stroke. Erect perpendicular CD. Draw DL tangent to E;

parts of the stroke. Erect perpendicular (DL) praw DL tangent to E; draw XS perpendicular to DL; XS is then outside lap of valve. To find release and compression: If there is no inside lap, draw FE through X parallel to DL. F and E will be position of crank for release and compression. If there is an inside lap, draw a circle about X, in which radius XY equals inside lap. Draw HG tangent to this circle and parallel to DL; then H and G are crank position for release and compression D and MG, then AN is piston position at release and AM piston position at compression, AB being considered stroke of engine.

To make compression alike on each stroke it is necessary to increase the inside lap on crank end of valve, and to decrease by the same amount the inside lap on back end of valve. To determine this amount, through M with a radius  $MM' = AA^{1}$ , draw are MP, from P draw PT perpendicular to AB, then TM is the amount to be added to inside lap on crank end, and to be deducted from inside lap on back end of valve, inside lap being XY. For the  $Bilgram\ Valve\ Diagram$ , see Halsey on Slide-valve Gears. The Zeuner Valve-diagram is given in most of the works on the

steam-engine, and in treatises on valve-gears, as Zeuner's, Peabody's, and

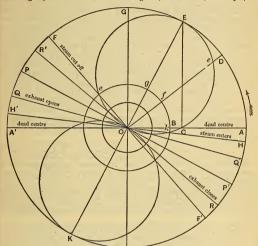


Fig. 148.—Zeuner's Valve-diagram.

Spangler's. The following is condensed from Holmes on the Steam-engine: Describe a circle, with radius OA equal to the half travel of the valve. From O measure off OB equal to the outside lap, and BC equal to the lead. When the crank-pin occupies the dead centre A, the valve has already when the trains pin occupies the dead centre  $A_1$ , the valve has already moved to the right of its central position by the space OB + BC. From C erect the perpendicular CE and join OE. Then will OE be the position cocupied by the line joining the centre of the eccentric with the centre of the crank-shaft at the commencement of the stroke. On the line OE as diameter describe the circle OCE; then any chords, as Oe, OE, Oe, OH, with represent the spaces travelled by the valve from its central position when the crank-pin occupies respectively the positions opposite to D, E, and F. Before the port is opened at all the valve must have moved from its central position by an amount equal to the lap OB. Hence, to obtain the scan which the port is opened, subtract from each of the arcs Oe, OE, etc., a length equal to OB. This is represented graphically by describing from centre O a circle with radius equal to the lap OB; then the spaces fe. gE, etc., intercepted between the circumferences of the lap-circle Bfe' and the valve-circle OCE, will give the extent to which the steam-port is opened. At the point k, at which the choil Ok is common to both valve and lap

circles, it is evident that the valve has moved to the right by the amount of the lap, and is consequently just on the point of opening the steam-port. Hence the steam is admitted before the commencement of the stroke, when the crank occupies the position OH, and while the portion HA of the revolution still remains to be accomplished. When the crank-pin reaches the position A, that is to say, at the commencement of the stroke, the port is already opened by the space OC - OB = BC, called the lead. From this point forward till the crank occupies the position OE the port continues to open, but when the crank is at OE the valve has reached the furthest limit of its travel to the right, and then commences to return, till when in the position OF the edge of the valve just covers the steam-port, as is shown by the chord Oe', being again common to both lap and valve circles. Hence when the crank occupies the position OF the cut-off takes place and the steam commences to expand, and continues to do so till the exhaust opens. For the return stroke the steam-port opens again at E' and closes at E'

For the return stroke the steam-port opens again at H' and closes at F'. There remains the exhaust to be considered. When the line joining the centres of the eccentric and crank-shaft occupies the position opposite to OG at right angles to the line of ead centres, the crank is in the line OF at right angles to the line of dead centres, the crank is in the line OF at right angles to OE: and as OF does not intersect either valve-circle the amount of the inside lap. The crank must therefore move through such an angular distance that its line of direction OF must intercept a chord on the valve-circle OF described by the amount of the inside lap, the intercept a chord on the valve-circle OF and length to the inside lap before the port can be opened to the exhaust. This point is ascertained precisely in the same manner as for the outside lap, namely, by drawing a circle from centre OF with a radius equal to the inside lap; this is the small inner circle in the figure. Where this circle intersects the two valve-circles we get four points which show the positions of the crank when the exhaust opens and closes during each revolution. Thus at OF the valve opens the exhaust on the side of the piston which we have been considering, while at F the exhaust closes and compression commences and continues till the fresh steam is readmitted at F.

Thus the diagram enables us to ascertain the exact position of the crank when each critical operation of the valve takes place. Making a résumé of these operations of one side of the piston, we have: Steam admitted before the commencement of the stroke at H. At the dead centre A the valve already opened by the amount BC. At E the port is fully opened, and valve has reached one end of its travel. At F steam is cut off, consequently admission lasted from H to F. At F valve occupies central position, and ports are closed both to steam and exhaust. At Q exhaust opened, consequently expansion lasted from F to Q. At K exhaust opened to maximum extent, and valve reached the end of its travel to the left. At R exhaust closed, and compression begins and continues till the fresh steam is admitted

at H.

PROBLEM.—The simplest problem which occurs is the following: Given the length of throw, the angle of advance of the secentric, and the laps of the vaive, find the angles of the crank at which the steam is admitted and cut off and the exhaust opened and closed. Draw the line OE, representing the half-travel of the valve or the throw of the eccentric at the given angle of advance with the perpendicular OG. Produce OE to K. On OE and OK as diameters describe the two valve-circles. With centre and radii equal to the given laps describe the outside and inside lap-circles. Then the intersection of these circles with the two valve-circles give points through which the lines OH, OF, OQ, and OR can be drawn. These lines give the required positions of the crank.

Numerous other problems will be found in Holmes on the Steam-engine, including problems in valve-setting and the application of the Zeuner dia-

gram to link motion and to the Meyer valve-gear.

Port Opening.—The area of port opening should be such that the velocity of the steam in passing through it should not exceed 6000 ft. per min. The ratio of port area to piston area will then vary with the piston-speed as follows:

For speed of piston, 100 200 300 400 500 600 700 800 900 1000 1200 ft. per min.

Port area = piston \ .017 .033 .05 .067 .083 .1 .107 .133 .15 .167 ..2 area X \ for a velocity of 6000 ft. per min.,

Port area = sq. of diam. of cyl. × piston-speed

The length of the port opening may be equal to or something less than the diameter of the cylinder, and the width = area of port opening + its length. The bridge between steam and exhaust ports should be wide enough to

prevent a leak of steam into the exhaust due to overtravel of the valve.

Auchincloss gives: Width of exhaust port = width of steam port +

1/2 travel of valve - width of bridge.

Lead. (From Peabody's Valve-gears.)-The lead, or the amount that the valve is open when the engine is on a dead point, varies, with the type and size of the engine, from a very small amount, or even nothing, up to 3% of an inch or more. Stationary-engines running at slow speed may have from 1/64 to 1/16 inch lead. The effect of compression is to fill the waste from 1/64 to 1/16 inch lead. The effect of compression is to fill the waste space at the end of the cylinder with steam; consequently, engines having much compression need less lead Locomotive-engines having the valves controlled by the ordinary form of Stephenson link-motion may have a small lead when running slowly and with a long cut-off, but when at speed with a short cut-off the lead is at least ½ inch; and locomotives that have valve-gear which gives constant lead commonly have ½ inch lead. The lead angle is the angle the crank makes with the line of dead points at admission. It may vary from 0° to 8°.

Inside Lead.—Weisbach (vol. ii. p. 296) says: Experiment shows that the earlier opening of the exhanst ports is especially of advantage, and in the best argines the lead of the vylue upon the side of the exhaust, or the

the best engines the lead of the valve upon the side of the exhaust, or the linside lead, is 1/25 to 1/15; i.e., the slide-valve at the lowest or highest position of the piston has made an opening whose height is 1/25 to 1/15 of the whole throw of the slide-valve. The outside lead of the slide-valve or the lead on the steam side, on the other hand, is much smaller, and is often only 1/100 of the whole throw of the valve.

Effect of Changing Outside Lap, Inside Lap, Travel and Angular Advance. (Thurston.)

	Admission	Expansion	Exhaust	Compression
Incr.	is later,	occurs earlier,	is unchanged	begins at
O.T.	ceases sooner	continues longer		same point
Incr.	unchanged	begins as before,	occurs later,	begins sooner,
I.L.		continues longer	ceases earlier	continues longer
Incr.	begins sooner,	begins later,	begins later,	begins later,
T.	continues longer	ceases sooner	ceases later	ends sooner
Incr.	begins earlier,	begins sooner,	begins earlier,	begins earlier,
A.A.	period unaltered	per, the same	per. unchanged	per. the same

Zeuner gives the following relations (Weisbach-Dubois, vol. ii, p. 307):

If S = travel of valve, p = maximum port opening; L = steam-lap, l = exhaust-lap;

$$R = \text{ratio of steam-lap to half travel} = \frac{L}{5S'}$$
  $L = \frac{R}{2} \times S;$ 

$$r = \text{ratio of exhaust lap to half travel} = \frac{1}{1.58}, \quad l = \frac{2}{2} \times S;$$

$$S = 2p + 2L = 2p + 2R + S; S = \frac{2p}{1 - R}$$

If a = angle HOF between positions of crank at admission and at cut-off, and  $\beta$  = angle QOR between positions of crank at release and at compression, then  $R = \frac{1}{2} \frac{\sin{(180^{\circ} - \alpha)}}{\sin{\frac{1}{2}\alpha}}; r = \frac{1}{2} \frac{\sin{(180^{\circ} - \beta)}}{\sin{\frac{1}{2}\beta}}.$ 

Ratio of Lap and of Port-opening to Valve-travel.-The table on page 831, giving the ratio of lap to travel of valve and ratio of travel to port opening, is abridged from one given by Buel in Weisbach-Dubois, vol. ii. It is calculated from the above formulæ. Intermediate values may vol. ii. It is calculated from the above formulæ. Intermediate values may be found by the formulæ, or with sufficient accuracy by interpolation from the figures in the table. By the table on page 830 the crank-angle may be tound, that is, the angle between its position when the engine is on the centre and its position at cut-off, release, or compression, when these are known in fractions of the stroke. To illustrate the use of the tables the following example is given by Buel: width of port = 2.2 in.; width of port point = 9.3 in.; over overtravel = 2.5 in.; length of connecting rod =  $\frac{13}{2}$ 6 times stroke; cut-off. 75 of stroke; release, 35 stroke; lead-angle, 10°. From the first table we find crank-angle =  $\frac{114}{2}$ 6; stroke; lead-angle, 10°. add lead-angle, making 124.6.° From the second table, for angle between admission and cut-off, 125°, we have ratio of travel to port-opening =3.72, or for 124.6° =3.74, which, multiplied by port-opening 2.5, gives 9.45 in travel. The ratio of lap to travel, by the table, is .3324, or 9.45  $\times$  .3324 =2.2 in, lap. For exhaust-lap we have, for release at .35, crank-angle  $=151.3^\circ$ , add lead-angle  $10^\circ=161.3^\circ$ . From the second table, by interpolation, ratio of lap to travel = .0811, and .0811  $\times$  9.45 = 0.77 in, the exhaust-lap.

Lap-angle =  $\frac{1}{2}$  (180° - lead-angle - crank-angle at cut-off); =  $\frac{1}{2}$  (180° - 10 - 114.6) = 27.7°.

Angular advance = lap-angle  $\times$  lead-angle = 27.7 + 10 = 37.7°. Exhaust lap-angle = crank-angle at release + lap-angle + lead-angle - 180°;

 $= 151.3 + 27.7 + 10 - 180^{\circ} = 9^{\circ}.$ Crank-angle at compression measured  $= 180^{\circ} - 1$  ap-angle  $= 180^{\circ} - 180^{\circ} - 180^{\circ}$  ap-angle  $= 180^{\circ$ 

pression measured  $\rangle = 180^{\circ} - 1$ ap-angle - lead-angle - exhaust lap-angle; on return stroke  $\rangle = 180 - 27.7 - 10 - 9 = 133.8^{\circ}$ ; corresponding, by

table, to a piston position of .81 of the return stroke; or Crank-angle at compression = 180° - (angle at release - angle at cut-off) + lead-angle;

+ lead-angle; =  $180 - (151.3 - 114.6) + 10 = 133.3^{\circ}$ .

The positions determined above for cut-off and release are for the forward stroke of the piston. On the return stroke the cut-off will take place at the same angle, 114.6°, corresponding by table to 66.6% of the return stroke, instead of 75%. By a slight adjustment of the angular advance and the length of the eccentric rod the cut-off can be equalized. The width of the bridge should be at least 2.5+0.25-2.2=0.55 in.

Crank Angles for Connecting-rods of Different Length.

FORWARD AND RETURN STROKES

FORWARD AND RETURN STROKES.													
of om nent.	Ratio of Length of Connecting-rod to Length of Stroke.												
Fraction of Stroke from mmencemer		2	21/2		3		3½		4		5		Infi- nite.
Fraction of Stroke from Commencement,	For.	Ret.	For.	Ret.	For.	Ret.	For.	Ret.	For.	Ret.	For.	Ret.	For. or Ret.
.01	10.3 14.6	13.2 18.7	10.5 14.9	12.8 18.1	10.6	12.6 17.8	10.7 15.2	12.4 17.5	10.8 15.3	12.3 17.4	10.9	12.1 17.1	11.5 16.3
.03	17.9 20.7	22.9	18.2	22.2	18.5	21.8	18.7	21.5	18.8	21.3	19.0	21.0	19.9
.04	23.2	26.5 29.6	21.1 23.6	$\frac{25.7}{28.7}$	21.4 24.0	28.2	21.6 24.2	$\frac{24.9}{27.8}$	24.4	24.6 27.5	24.7	27.2	25.8
.10	33.1 41	41.9	33.8 41.9	40.8 50.2	34.3 42.4	40.1	34 6 42.9	39.6 48.7	34.9 43.2	39.2 48.3		38.7 47.7	36.9 45.6
.20	48	59.6 66.9	48.9	58.2	49.6	57.3 64.4	50.1	56.6 63.7	50.4 57.0	56.2		55.5	53.1 60.0
.25	54.3 60.3	73.5	55.4 61.5	65.4 72.0	56.1 62.2	71.0	62.8	70.3	63.3	69.8	63.9	69.1	66.4
.35 .40	66.1	79 8 85.8	67.3 73.0	78.3 84.3	68.1 73.9	77.3 83.3	68.8 74.5	76.6 82.6	69 2 75.0	76.1 82.0	69.9 75.7	75.3 81.3	72.5 78.5
.45	77.2 82.8	91.5 97.2	78.6		79.6	89.1	80.2	88.4	80.7	87.9	81.4	87.1 92.9	84.3 90.0
.55	88.5	102.8	89.9	101.4	90.9	100.4	91.6	99.8	92.1	99.3	92.9	98.6	95.7
.60	$\frac{94.2}{100.2}$	108.3 $113.9$	95.7 $101.7$	107.0 $112.7$		106.1 111.9	97.4 103.4	105.5 $111.2$		105.0 110.8		104.3 $110.1$	$101.5 \\ 107.5$
.70 .75	106.5 113.1		108.0	118.5	109.0	117.8	109.7 116.3	117.2	110.2	116.7	110.9		113.6
.80	120.4	132	121.8	131.1	122.7	130.4	123.4	129.9	123.8	129.6	124.5	129.1	126.9
.85	128.5 138.1	$ 139 \\ 146.9$	$129.8 \\ 139.2$	$138.1 \\ 146.2$	130.7 $139.9$	137.6 $145.7$	131.3 140.4	137.1 145.4	131.7	136.8 145.1	132.3 $141.3$	136.4	134.4 $143.1$
.95	150.4	156.8	151.3	156.4	151.8	156.0	152.2 155.1	155.8	152.5	155.6	152.8	155.3	154.2
.97	157.1	162.1	157.8	161.8	158.2	161.5	158.5	161.3	158.7	161.2	159.0	161.0	160.1
.98	166.8	169.7	167.2	169.5	167.4	169.4	$162.5 \\ 167.6$	169.3	167.7	109.2	167.9		168.5
1.00	180	180	180	1180	180	180	180	180	180	180	180	180	180

**Relative Motions of Cross-head and Crank.**—If L = length of connecting-rod, R = length of crank,  $\theta = \text{augle of crank with centre line}$  of eugine, D = displacement of cross-head from the beginning of its stroke,

 $D = R(1 - \cos \theta) = L - \sqrt{L^2 - R^2 \sin^2 \theta}.$ 

#### Lap and Travel of Valve.

Angle between Positions of Crank at Points of Admission and Cut-off, or Release and Com- pression.	Ratio of Lap to Travel of Valve,	Ratio of Travel of Valve to Width of Port-open- ing.	Angle between Positions of Crank at Points of Admission and Cut-off, or Release and Compression.	Ratio of Lap to Travel of Valve.	Ratio of Travel of Valve to Width of Port-open- ing.	Angle between Positions of Crank at Points of Admission and Cut-off, or Release and Compression.	Ratio of Lap to Travel of Valve.	Ratio of Travel of Valve to Width of Port-open- ing.
30° 35 40 45 50 55 60 65 70 75 80	.4830 .4769 .4699 .4619 .4532 .4435 .4330 .4217 .4096 .3967 .3830	58.70 43.22 33.17 26.27 21.34 17.70 14.93 12.77 11.06 9.68 8.55	85° 90 95 100 105 110 115 120 125 130	.3686 .3536 .3378 .3214 .3044 .2868 .2687 .2500 .2309 .2113	7.61 6.83 6.17 5.60 5.11 4.69 4.32 4.00 3.72 3.46	135° 140 145 150 155 160 165 170 175 180	.1913 .1710 .1504 .1294 .1082 .0868 .0653 .0436 .0218	3.24 3.04 2.86 2.70 2.55 2.42 2.30 2.19 2.09 2.00

## PERIODS OF ADMISSION, OR CUT-OFF, FOR VARIOUS LAPS AND TRAVELS OF SLIDE-VALVES.

The two following tables are from Clark on the Steam-engine. In the first table are given the periods of admission corresponding to travels of valve of from 12 in. to 2 in., and laps of from 2 in. to 3 in., with 14 in. and 14 in. of lead. With greater leads than those tabulated, the steam would be cut off earlier than exclosur in the table.

earlier than as shown in the table.

earlier than as shown in the table, the influence of a lead of 5/16 in. for travels of from 15/3 in. to 6 in., and laps of from 15/4 in. to 15/4 in., as calculated for in the second table, is exhibited by comparison of the periods of admission in the table, for the same lap and travel. The greater lead shortens the period of admission, and increases the

range for expansive working.

Periods of Admission, or Points of Cut-off, for Given Travels and Laps of Slide-valves.

	·										
Travel of Valve.	Periods of Admission, or Points of Cut-off, for Laps of Valves in inches.							for th	e follo	wing	
Tr	Ä	2	13/4	11/2	11/4	1	3/8	3/4	5/8	1/2	3/8
in. 12	in.	% 88	% 90	% 93	% 95	% 96	% 97	% 98	% 98	% 99	% 99
10	14 14 14	82 72	87 78	89 84	92 88	95 92	96 . 94	97 95	98 96	98 98	99
10 8 6 51/2 5	74	50 43	62 56	71 68	79 77	86 85	89 88	91 91	94 94	96 96	97 97
5 4½ 4	1/8 1/8	32 14	47 35 17	61 51 39	72 66 57	82 78 72	86 83 78	89 87 83	92 90 88	95 94 92	97 96 95
31/2	1/8 1/8 1/6			20	44 23	63 50	71 61	79 71	84 79	90 86	94 91
31/2 3 21/2 2	1/8 1/8 1/8					27	43	57 33	70 52	80 70	88 81

#### Periods of Admission, or Points of Cut-off, for given Travels and Laps of Slide-valves.

Constant lead, 5/16,

Travel.		Lap.							
Inches.	1/2	5/8	3/4	7/8	1	11/8	11/4	13/8	11/2
15/8 13/4	19 39								
1%	47	17							
2	55	34							
21/8	61	42	14						
21/4	65	50	30						
29/8	68	55 59	38	13 27		•••••	•••••		
252	71 74	63	45 49	36	12			• • • • • • •	
93%	76	67	56	43	26				
274	78	70	59	47	32	1i			
31/4	80	73	62	50	38	23			
31/8	81	74	65	55	44	30	10		
31/4	83	76	68	59	48	34	22		
33/8	84	78	71	62	51	40	29	9	
31/2	85 86	80	73	64	53	45	34	20	
3%	86	81	75	66	57	49	38	26	9
39/4	87	82	76 78	68 70	60	52 55	42 46	32 36	19 25
0/8	87 88	84	79	72	66	58	49	40	90
41/4	89	86	81	76	70	63	56	47	29 37
41/6	90	87	83	79	73	67	61	54	45
43%	92	89	85	81	76	70	65	58	51
5	93	90	87	83	78	73	67	62	51 56
5½ 6	94	92	89	86	82	78	73	68	63 69
6	95	93	91	88	85	82	78	74	69

Diagram for Port-opening, Cut-off, and Lap.—The diagram on the opposite page was published in *Power*, Aug., 1893. It shows at a glance the relations existing between the outside lap, steam port-opening, and cut-off in slide valve engines.

and cut-off it sinds valve engines. In order to use the diagram to find the lap, having given the cut-off and maximum port-opening, follow the ordinate representing the latter, taken on the horizontal scale, until it meets the oblique line representing the given cut-off. Then read off this height on the vertical lap scale. Thus, with a port-opening of 1¼ inch and a cut-off of .50, the intersection of the two lines occurs on the horizontal 3. The required lap is therefore 3 in.

If the cut off and lap are given, follow the horizontal representing the latter until it meets the oblique line representing the cut-off. Then vertically below this read the corresponding port-opening on the horizontal scale.

If the lap and port-opening are given, the resulting out-off may be ascertained by finding the point of intersection of the ordinate representing the port-opening with the horizontal representing the lap. The oblique line passing through the point of intersection will give the cut-off.

If it is desired to take lead into account, multiply the lead in inches by the

If it is desired to take lead into account, multiply the lead in inches by the numbers in the following table corresponding to the cut-off, and deduct the result from the lap as obtained from the diagram:

Cut-off.	Multiplier.	Cut-off.	Multiplier.
.20	4.717	.60	1.358
.25	3,731	.625	1.288
.30	3.048	.65	1.222
.38	2.717	.70	1.103
.375	2.381	.75	1.000
.40	2.171	.80	0.904
.45	1.930	.85	0.815
.50	1.706	.875	0.772
.55	1.515	.90	0.731

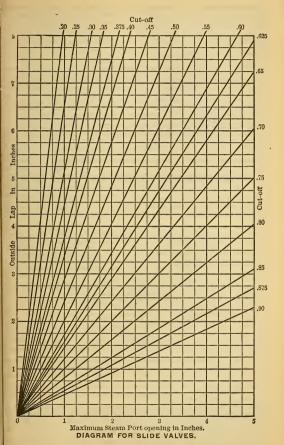


Fig. 149,

Piston-valve.—The piston-valve is a modified form of the slide valve. The lap, lead, etc., are calculated in the same manner as for the common slide-valve. The diameter of valve and amount of port-opening are calculated on the basis that the most contracted portion of the steam-passage between the valve and the cylinder should have an area such that the velocity of steam through it will not exceed 6000 ft. per minute. The area of the opening around the circumference of the valve should be about double the area of the steam-passage, since that portion of the opening that is opposite from the steam-passage is of little effect.

Setting the Valves of an Engine.—The principles discussed

above are applicable not only to the designing of valves, but also to adjust-ment of valves that have been improperly set; but the final adjustment of the eccentric and of the length of the rod depend upon the amount of lost motion, temperature, etc., and can be effected only after trial. After the valve has been set as accurately as possible when cold, the lead and lap for the forward and return strokes being equalized, indicator diagrams should be taken and the length of the eccentric-rod adjusted, if necessary, to cor-

rect slight irregularities

To Put an Engine on its Centre.—Place the engine in a position where the piston will have nearly completed its outward stroke, and opposite some point on the cross-head, such as a corner, make a mark upon the guide. Against the rim of the pulley or crank-disk place a pointer and mark a line with it on the pulley. Then turn the engine over the centre until the cross-head is again in the same position on its inward stroke. This will bring the crank as much below the centre as it was above it before. With the pointer in the same position as before make a second mark on the pulleyrim. Divide the distance between the marks in two and mark the middle point. Turn the engine until the pointer is opposite this middle point, and it will then be on its centre. To avoid the error that may arise from the looseness of crank-pin and wrist-pin bearings, the engine should be turned a little above the centre and then be brought up to it, so that the crank pin will press against the same brass that it does when the first two marks are made.

Link-motion.-Link-motions, of which the Stephenson link is the most commonly used, are designed for two purposes: first, for reversing the motion of the engine, and second, for varying the point of cut-off by varying the travel of the valve. The Stephenson link motion is a combination of two eccentrics, called the forward and back eccentric, with a link connecting the extremeties of the eccentic-rods; so that by varying the position of the link the valve-rod may be put in direct connection with either eccentric, or may be given a movement controlled in part by one and in part by the other eccentric. When the link is moved by the reversing lever into a position such that the block to which the valve-rod is attached is at either end of the link, the valve receives its maximum travel, and when the link is in mid-gear the travel is the least and cut-off takes place early in the stroke.

In the ordinary shifting-link with open rods, that is, not crossed, the lead of the valve increases as the link is moved from full to mid-gear, that is, as the period of steam admission is shortened. The variation of lead is equalized for the front and back strokes by curving the link to the radius of the eccentric-rods concavely to the axles. With crossed eccentric-rods the lead decreases as the link is moved from full to mid-gear. In a valve-motion with stationary link the lead is constant. (For illustration see Clark's Steam-

engine, vol. ii. p. 22.)

The linear advance of each eccentric is equal to that of the valve in full gear, that is, to lap + lead of the valve, when the eccentric-rods are attached to the link in such position as to cause the half-travel of the valve to equal the eccentricity of the eccentric.

The angle between the two eccentric radii, that is, between lines drawn from the centre of the eccentric disks to the centre of the shaft equals 180°

less twice the angular advance.

Buel, in Appleton's Cyclopedia of Mechanics, vol. ii. p. 316, discusses the Stephenson link as follows: "The Stephenson link does not give a perfectly correct distribution of steam; the lead varies for different points of cut-off. The period of admission and the beginning of exhaust are not alike for both ends of the cylinder, and the forward motion varies from the backward.

"The correctness of the distribution of steam by Stephenson's link-motion depends upon conditions which, as much as the circumstances will permit, ought to be fulfilled, namely: 1. The link should be curved in the arc of a circle whose radius is equal to the length of the eccentric-rod. 2. The eccentric-rods ought to be long; the longer they are in proportion to the eccentricity the more symmetrical will the travel of the valve be on both sides of the centre of motion. 3. The link ought to be short, Each of its sides of the centre of motion. 3. The link ought to be short. Each of its points describes a curve in a vertical plane, whose ordinates grow larger the farther the considered point is from the centre of the link; and as the horizontal motion only is transmitted to the valve, vertical oscillation will cause irregularities. 4. The link-hanger ought to be long. The longer it is the nearer will be the arc in which the link swings to a straight line, and thus the less its vertical oscillation. If the link is suspended in its centre, the curves that are described by points equidistant on both sides from the centre are not alike, and hence results the variation between the forward and backward gear. If the link is suspended at its lower end, its lower half will have less vertical oscillation and the upper half more. 5. The centre from which the link-hanger swings changes its position as the link is lowered or raised, the link-hanger swings changes its position as the link is lowered to change and also causes irregularities. To reduce them to the smallest amount the arm of the lifting-shaft should be made as long as the eccentric-rod, and the centre of the lifting-shaft should be placed at the height corresponding to the central position of the centre on which the link-hanger swings."

All these conditions can never be fulfilled in practice, and the variations in the lead and the period of admission can be somewhat regulated in an artificial way, but for one gear only. This is accomplished by giving different lead to the two eccentries, which difference will be smaller the longer the eccentric-rods are and the shorter the link, and by suspending 'he link not exactly on its centre line but at a certain distance from it, giving what is called "the offset."

For application of the Zeuner diagram to link-motion, see Holmes on the Steam-eigine, p. 290. See also Clark's Railway Machinery (1855), Clark's Steam-engine and Zeuner's and Auchincloss's Treatises on Slide-valve Gears.

The following rules are given by the American Machinist for laying out a link for an upright slide-valve engine. By the term radius of link is meant the radius of the link-arc ab, Fig. 150, drawn through the centre of the slot;

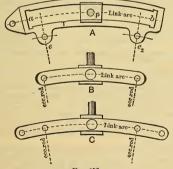


Fig. 150.

this radius is generally made equal to the distance from the centre of shaft to centre of the link-block pin P when the latter stands midway of its travel. The distance between the centres of the eccentric-rod pins  $e_1 e_2$  should not be less than 21/2 times, and, when space will permit, three times the throw of the eccentric. By the throw we mean twice the eccentricity of the eccentric. The slot link is generally suspended from the end next to the forward eccer-eric at a point in the link-arc prolonged. This will give comparatively a mail amount of slip to the link-block when the link is in forward gear; but this slip will be increased when the link is in backward gear. This increase

of slip is, however, considered of little importance, because marine engines, or sip is, however, considered of interimportance, because marine engines, as a rule, work but very little in the backward gear. When it is necessary that the motion shall be as efficient in backward gear as in forward gear, then the link should be suspended from a point midway between the two eccentric-rod pins; in marine engine practice this point is generally located on the link-arc; for equal cut-offs it is better to move the point of suspen-

sion a small amount towards the eccentries.

For obtaining the dimensions of the link in inches; Let L denote the length of the valve, B the breadth, p the absolute steam-pressure per sq. in., and R a factor of computation used as below; then  $R = .01 \ V L \times B \times p$ .

Breadth of the link	=	$R \times 1.6$
Thickness T of the bar	=	$R \times .8$
Length of sliding-block	=	$R \times 2.5$
Diameter of eccentric-rod pins	=	$(R \times .7) + \frac{1}{4}$
Diameter of eccentric-rod pins	=	$(R \times .6) + \frac{1}{4}$
Diameter of suspension-rod pin when overhung	: =	$(R \times .8) + \frac{1}{4}$
Diameter of block-pin when overhung Diameter of block-pin when secured at both en	=	$R + \frac{1}{4}$
Diameter of block-pin when secured at both en	ds =	$(R \times .8) + 1/4$

The length of the link, that is, the distance from a to b, measured on a straight line joining the ends of the link-arc in the slot, should be such as to straight the joining the chart of the mix-a bit in the stock should be such as a lilow the centre of the link-block pin P to be placed in a line with the eccentric-rod pins, leaving sufficient room for the slip of the block. Another type of link frequently used in marine engines is the double-bar link, and this type is again divided into two classes: one class embraces those links which have the eccentric-rod ends as well as the valve-spindle end between the bars, as shown at B (with these links the travel of the valve is less than the throw of the eccentric); the other class embraces those links, shown at C, for which the eccentric-rods are made with fork-ends, so as to connect to studs on the outside of the bars, allowing the block to slide to the end of the link, so that the centres of the eccentric-rod ends and the block-pin are in line when in full gear, making the travel of the valve equal to the throw of the eccentric. The dimensions of these links when the distance between the eccentric-rod pins is 2½ to 2¾ times the throw of eccentrics can be found as follows:

Depth of bars Thickness of bars	$= (R \times 1.25) + \frac{1}{2}$
Thickness of bars	$= (R \times .5) + \frac{1}{4}$ "
Diameter of centre of sliding-block	$= R \times 1.3$

When the distance between the eccentric-rod pins is equal to 3 or 4 times the throw of the eccentrics, then

All the other dimensions may be found by the first table. These are empirical rules, and the results may have to be slightly changed to suit given conditions. In marine engines the eccentric-rod ends for all classes of links have adjustable brasses. In locomotives the slot-link is usually employed, have adjustable prasses. In occupances the second in these the pin-holes have case-hardened bushes driven into the pin-and in these the pin-holes have case-hardened bushes driven into the pinlink in B is generally suspended by one of the eccentric-rod pins; and the link in C is suspended by one of the pins in the end of the link, or by one of the eccentric-rod pins.

the eccentric-rod pins.

Other Forms of Valve-Gear, as the Joy, Marshall, Hackworth, Brenme, Walschaert, Coriss, etc., are described in Clark's Steam-engine, vol. ii. The design of the Reynolds-Coriiss valve-gear is discussed by A. H. Eldridge in Power, Sep. 1893. See also Henthorn on the Coriiss engine. Rules for laying down the centre lines of the Joy valve-gear are given in American Machinist, Nov. 13, 1890. For Joy's "Fluid-pressure Reversing-valve," see Eng'g, May 25, 1894.

#### GOVERNORS.

Pendulum or Fly-ball Governor.-The inclination of the arms of a revolving pendulum to a vertical axis is such that the height of the point of suspension h above the horizontal plane in which the centre of gravity of the balls revolve (assuming the weight of the rods to be small

compared with the weight of the balls) bears to the radius r of the circle described by the centres of the balls the ratio

$$\frac{h}{r} = \frac{\text{weight}}{\text{centrifugal force}} = \frac{w}{\frac{wv^2}{gr}} = \frac{gr}{v^2},$$

which ratio is independent of the weight of the balls, v being the velocity of the centres of the balls in feet per second. If T= number of revolutions of the balls in 1 second,  $v=2\pi rT=ar$ , in which a= the angular velocity, or  $2\pi T$ , and

$$h=\frac{gr^2}{v^2}=\frac{g}{4\pi^2T^2}, \ \ {\rm or} \ \ h=\frac{0.8146}{T^2}\,{\rm feet}=\frac{9.775}{T^2}\,{\rm inches},$$

g being taken at 32.16. If N = number of revs. per minute,  $h = \frac{35190}{N^2}$ inches

Number of turns per minute required to cause the arms to take a given angle with the vertical axis: Let l = length of the arm in inches from the centre of suspension to the centre of gyration, and a the required angle;

$$N = \sqrt{\frac{35190}{l \cos a}} = 187.6 \sqrt{\frac{1}{l \cos a}} = 187.6 \sqrt{\frac{1}{h}}$$

The simple governor is not isochronous; that is, it does not revolve at a uniform speed in all positions, the speed changing as the angle of the arm changes. To remedy this defect loaded governors, such as Porter's, are changes. To remedy this defect loaded governors, such as Porter's, are used. From the balls of a common governor whose collective weight is A let there be hung by a pair of links of lengths equal to the pendulum arms a load B capable of sliding on the spindle, having its centre of gravity in the axis of rotation. Then the centrifugal force is that due to A alone, and the effect of gravity is that due to A + 2B; consequently the altitude for a given speed is increased in the ratio (A + 2B) : A, as compared with that of a simple revolving pendulum, and a given absolute variation in altitude produces a smaller proportionate variation in speed than in the common governor. (Rankine, S. E., p. 551), b. (A + B) : A, and (A + B) : A are from the point of suspension to the centre of gravity of the ball, and let the length of the suspension (A + B) : A and (A + B) : A are from the point of suspension to the centre of gravity of the ball, and let the length of the suspension of the sum from the rount of

suspension to the centre of gravity of the oan, and let the segret of the suspension for the arm from the point of suspension of the arm to the point of attachment of the link; Q = that fith ewight of the sliding weight, h = the height of the governor from the point of snspension to the plane of revolution of the balls, a = the angular velocity =  $2\pi T$ , T being the number of revolutions per

second; then 
$$a=\sqrt{\frac{32.16}{\hbar}}\Big(1+\frac{2l_1}{l}\frac{Q}{G}\Big);\; h=\frac{32.16}{\alpha^2}\left(1\times\frac{2l_1}{l}\frac{Q}{G}\right)^2$$
 in feet, or

 $h = \frac{35190}{N^2} \left(1 + \frac{2l_1}{l} \frac{Q}{Q}\right)^2$  in inches, N being the number of revolutions per

For various forms of governor see App. Cycl. Mech., vol. ii. 61, and Clark's

Steam-engine, vol. ii., p. 65.

To Change the Speed of an Engine Having a Fly-ball Governor.—A slight difference in the speed of a governor changes the position of its weights from that required for full load to that required for position of its weights from that required for full load to that required for no load. It is evident therefore that, whatever the speed of the engine, the normal speed of the governor must be that for which the governor was designed; i.e., the speed of the governor must be kept the same. To change the speed of the engine the problem is to so adjust the pulleys which drive the governor that the engine at its new speed shall drive it just as fast as it was driven at its original speed. In order to increase the engine-speed we must decrease the pulley upon the shaft of the engine, i.e., the driver, or increase that on the governor, i.e., the driven, in the proportion that the speed of the engine is to be increased. engine is to be increased.

Fly-wheel or Shaft Governors .- At the Centennial Exhibition in 1870 there were shown a few steam-engines in which the governors were contained in the fig-wheel or band-wheel, the fly-balls or weights revolving around the shaft in a vertical plane with the wheel and shifting the eccentric so as automatically to vary the travel of the valve and the point of cuttric so as automatically to vary the travel of the vaive and the point of cut-off. This form of governor has since come into extensive use, especially for high-speed engines. In its usual form two weights are carried on arms the ends of which are pivoted to two points on the pulley near its circum-ference, 180° apart. Links connect these arms to the eccentric. The eccentric is not rigidly keyed to the shaft but is free to move trans-versely across it for a certain distance, having an oblong hole which allows of this movement. Centrifugal force causes the weights to fly towards the circumference of the wheel and to pull the eccentric into a position of minimum eccentricity. This force is resisted by a spring attached to each arm which tends to pull the weights towards the shaft and shift the eccentric to the position of maximum eccentricity. The travel of the valve is thus varied, so that it tends to cut off earlier in the stroke as the engine increases its speed. Many modifications of this general form are in use. For discussions of this form of governor see Hartneil, Proc. Inst. M. E., 1882, p. 408; Trans. A. S. M. E., ix. 300; xi. 1081; xiv. 92; xv. 929; Modern Mechanism. p. 399; Whitham's Constructive Steam Engineering; J. Begrup, Am. Mach.. Oct. 19 and Dec. 14, 1893, Jan. 18 and March 1, 1894.

Calculation of Springs for Shaft-governors. (Wilson Hartnell, Proc. Inst. M. E., Aug. 1882.)—The springs for shaft-governors may be conveniently calculated as follows, dimensions being in inches:

Let W = weight of the balls or weights, in pounds;

 $r_1$  and  $r_2$  = the maximum and minimum radial distances of the centre of the balls or of the centre of gravity of the weights;

 $l_1$  and  $l_2$  = the leverages, i.e., the perpendicular distances from the centre of the weight-pin to a line in the direction of the centrifugal force, drawn through the centre of gravity of the weights or balls at radii r, and ro:

 $m_1$  and  $m_2$  = the corresponding leverages of the springs;  $C_1$  and  $C_2$  = the centrifugal forces, for 100 revolutions per minute, at

radii  $r_1$  and  $r_2$ : the corresponding pressures on the spring; (It is convenient to calculate these and note them down for reference.)

 $C_3$  and  $C_4$  = maximum and minimum centrifugal forces; S = mean speed (revolutions per minute);

 $S_1$  and  $S_2$  = the maximum and minimum number of revolutions per

minute: Pa and  $P_4$  = the pressures on the spring at the limiting number of revolutions  $(S_1$  and  $S_2)$ ;  $P_4 - P_3 = D$  = the difference of the maximum and minimum pressures

on the springs; V = the percentage of variation from the mean speed, or the sensitiveness;

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t = the travel of the spring; u = the initial pressure on the spring;

v = the stiffness in pounds per inch; w =the maximum pressure = u + t.

The mean speed and sensitiveness desired are supposed to be given. Then

$$\begin{split} S_1 &= S - \frac{SV}{100}; & S_2 &= S + \frac{SV}{100}; \\ C_1 &= 0.28 \times r_1 \times W; & C_2 &= 0.28 \times r_2 \times W; \\ P_1 &= C_1 \times \frac{l_1}{m_1}; & P_2 &= C_2 \times \frac{l_2}{m_2}; \\ P_3 &= P_1 \times \left(\frac{S_1}{100}\right)^2; & P_4 &= P_2 \times \left(\frac{S_2}{100}\right)^2; \\ v &= \frac{D}{t}, \ u &= \frac{P_3}{v}, \ w &= \frac{P_4}{v}. \end{split}$$

It is usual to give the spring-maker the values of  $P_4$  and of v or w. To ensure proper space being provided, the dimensions of the spring should be

calculated by the formulæ for strength and extension of springs, and the least length of the spring as compressed be determined.

The governor-power = 
$$\frac{P_3 + P_4}{2} \times \frac{t}{12}$$
.

With a straight centripetal line, the governor-power

$$=\frac{C_3+C_4}{2}\times\left(\frac{r_2-r_1}{12}\right).$$

For a preliminary determination of the governor-power it may be taken as equal to this in all cases, although it is evident that with a curved centripetal line it will be slightly less. The difference D must be constant for the same spring, however great or little its initial compression. Let the spring be screwed up until its minimum pressure is  $P_5$ . Then to find the speed  $P_6 = P_5 + D$ ,

$$S_5 = 100 \sqrt{\frac{P_5}{P_1}}; \qquad S_6 = 100 \sqrt{\frac{P_6}{P_2}}.$$

The speed at which the governor would be isochronous would be

$$100\sqrt{\frac{D}{P_2-P_1}}.$$

Suppose the pressure on the spring with a speed of 100 revolutions, at the maximum and minimum radii, was 200 lbs, and 100 lbs, respectively, then the pressure of the spring to suit a variation from 95 to 105 revolutions will be  $100 \times \left(\frac{95}{100}\right)^2 = 90.2$  and  $200 \times \left(\frac{105}{100}\right)^2 = 220.5$ . That is, the increase of resistance from the minimum to the maximum radius must be 220 - 90 = 100

The extreme speeds due to such a spring, screwed up to different pressures, are shown in the following table:

Revolutions per minute, balls shut  Pressure on springs, balls shut Increase of pressure when balls open fully. Pressure on springs, balls open fully Revolutions per minute, balls open fully	64 130 194 98	81 130 211 102	90 130 220 105	100 130 230 107	121 130 251	130 274 117
Variation, per cent of mean speed	10	6	5	3	112	-1

The speed at which the governor would become isochronous is 114. Any spring will give the right variation at some speed, hence in experimenting with a governor the correct spring may be found from any wrong one by a very simple calculation. Thus, if a governor with a spring whose stiffness is 50 lbs. per inch acts best when the engine runs at 95, 90 being its proper speed, then  $50 \times \left(\frac{90}{95}\right)^2 = 45$  lbs. is the stiffness of spring required.

To determine the speed at which the governor acts best, the springs may be screwed up until it begins to "hunt" and then slackened until the governor is as sensitive as is compatible with steadiness.

#### CONDENSERS, AIR-PUMPS CIRCULATING-PUMPS, ETC.

The Jet Condenser. (Chiefly abridged from Seaton's Marine Engineering.)—The jet condenser is now uncommon, being generally supplanted by the surface condenser. With the jet condenser a vacuum of 24 h. was considered fairly good, and 25 in. as much as was possible with most condensers; the temperature corresponding to 24 in. vacuum, or 3 hs. pressure absolute, is 140°. In practice the temperature in the hot-well varies from 110 130°, and occasionally as much as 130° is maintained. To find the quantity of injection-water per pound of steam to be condensed: Let T<sub>1</sub> = temperature of the cooling-temperature of the cooling-

water;  $T_2$  = temperature of the water after condensation, or of the hot-well: Q = pounds of the cooling-water per lb. of steam condensed; then

$$Q = \frac{1114^{\circ} + 0.3(T_{1} - T_{2})}{T_{2} - T_{0}}.$$

 $Q=\frac{1114^{o}+0.3(T_1-T_2)}{T_2-T_0}.$  Another formula is:  $Q=\frac{WH}{K}$  , in which W is the weight of steam condensed, H the units of heat given up by 1 lb. of steam in condensing, and R the rise in temperature of the cooling-water.

This is applicable both to jet and to surface condensers. The allowance made for the injection-water of engines working in the temperate zone is usually 27 to 30 times the weight of steam, and for the tropics 30 to 35 times; 30 times is sufficient for ships which are occasionally in the tropics, and this is what was usual to allow for general traders.

Area of injection orifice = weight of injection-water in lbs, per min. ÷ 650 to 780.

A rough rule sometimes used is: Allow one fifteenth of a square inch for

every cubic foot of water condensed per hour. Another rule: Area of injection orifice = area of piston + 250. The volume of the jet condenser is from one fourth to one half of that of the cylinder. It need not be more than one third, except for very quick-

running engines. Ejector Condensers. - For ejector or injector condensers (Bulkley's, Schutte's, etc.) the calculations for quantity of condensing-water is the same

as for jet condensers.

The Surface Condenser-Cooling Surface.—Peclet found that with cooling water of an initial temperature of 68° to 77°, one sq. ft. of copper plate condensed 21.5 lbs. of steam per hour, while Joule states that 100 lbs. per hour can be condensed. In practice, with the compound engine, brass condenser-tubes, 18 B.W. G thick, 18 lbs. of steam per sq. ft. per hour, with the cooling-water at an initial temperature of 60°, is considered very fair work when the temperature of the feed-water is to be maintained at 120°. It has been found that the surface in the condenser may be half the beating surface of the holler and under some circumstances considerably less than surface of the boiler, and under some circumstances considerably less than this. In general practice the following holds good when the temperature of sea-water is about 60°:

For ships whose station is in the tropics the allowance should be increased by 20%, and for ships which occasionally visit the tropics 10% increase will give satisfactory results. If a ship is constantly employed in cold climates 10% less suffices

10% less suffices Within (Steam-engine Design, p. 283, also Trans. A. S. M. E., ix. 431) gives the following:  $S = \frac{WL}{ck(T_r - \epsilon)}$ , in which S = condensing-surface-in sq. ft.;  $T_r = \text{temperature Fabr.}$  of steam of the pressure indicated by the vacuum-gauge;  $t = \text{mean temperature of the circulating water, or the arithmetical mean of the initial and final temperatures; <math>L = \text{latent heat of the mean temperature of the circulating water, or the arithmetical steam at temperature <math>T_r$ ; k = perfect conductivity of 1 sq. ft. of the metal used for the condensing surface for a range of 1° F, (or 55° B.T. U. per hour for brass, according to Isherwood's experiments); c = fraction denoting the efficiency of the condensing surface; W = pounds of steam condensed per hour. From experiments by Loring and Emery, on U.S.S. Dallas, c is found to be 0.323, and ck = 180; and the equation becomes

$$S = \frac{WL}{180(T_1 - t)}.$$

Whitham recommends this formula for designing engines having independent circulating pumps. When the pump is worked by the main engine the value of S should be increased about 10%.

Taking  $T_1$  at 135° F., and L=1020, corresponding to 25 in. vacuum, and t=1020 m and t=1020 m and t=1020 m. for summer temperatures at 75°, we have:  $S = \frac{1020 W}{180(135 - 75)} = \frac{17W}{180}$ 

Condenser Tubes are generally made of solid-drawn brass tubes, and tested both by hydraulic pressure and steam. They are usually made of a composition of 68% of best selected copper and 32% of best Silesian spelter.

The Admiralty, however, always specify the tubes to be made of 70% of best selected copper and to have 1% of tin in the composition, and test the tubes

to a pressure of 300 lbs. per sq. in. (Seaton.)

The diameter of the condenser tubes varies from ½ inch in small condenser. sers, when they are very short, to I inch in very large condensers and long sets, when they are very short, or first in very large contracts and rolls tubes. In the mercantile marine the tubes are, as a rule 34 inch diameter externally, and 18 B.W.G. (0.05), under some exceptional circumstances. In the British Navy the tubes are also, as a rule, 3/4 inch diameter, and 18 to 19 B.W.G. thick, tinned on both sides; when the condenser is made of brass the Admiralty do not require the tubes to be tinned. Some of the smaller engines have tubes 5% inch diameter, and 19 B.W.G. thick. The smaller the tubes, the larger is the surface which can be got in a certain space.

In the merchant service the almost universal practice is to circulate the

water through the tubes

Whitham says the velocity of flow through the tubes should not be less

than 400 nor more than 700 ft. per min.

than 490 nor more than 700 ft. per min.

Tube-plates are usually made of brass. Rolled-brass tube-plates should be from 1.1 to 1.5 times the diameter of tubes in thickness, depending on the method of packing. When the packings go completely through the plates the latter, but when only partly through the former, is sufficient. Hence, for \$\frac{4}{2}\$-tinch tubes the plates are usually \$\frac{6}{2}\$ to 1 inch thick with glands and tape-packings, and 1 to 1/4 inch thick with wooden ferrules and the complete should be secured to their seatings by brass studs and the complete should be secured to their seatings by brass studs and the complete should be secured to their seatings by brass studs and the complete should be secured to the seating should be secured to their seatings by brass studs and the study of the secure of the seating should be seated by the se

kind inside a condenser. When the tube-plates are or large area to search able to stay them by brass-rods, to prevent them from collapsing.

Spacing of Tubes, etc.—The holes for ferrules, glands, or indiarrubber are usually ¼ inch larger in diameter than the tubes; but when absolutely necessary the wood ferrules may be only 3/32 inch thick.

The pitch of tubes when packed with wood ferrules is usually ¼ inch more than the diameter of the ferrule-hole. For example, the tubes are generally arranged zigzag, and the number which may be fitted into a square foot of plate is as follows:

Pitch of Tubes.	No. in a sq. ft.	Pitch of Tubes.	No. in a sq. ft.	Pitch of Tubes.	No. in a sq. ft.
1"	172	1 5/32"	128	1¼''	110
1 1/16"	150	1 3/16"	121	1 9/82''	106
11/8"	137	1 7/32"	116	1 5/16''	99

Quantity of Cooling Water .- The quantity depends chiefly upon its initial temperature, which in Atlantic practice may vary from 40° in the winter of temperate zone to 80° in subtropical seas. To raise the temperature to 100° in the condenser will require three times as many thermal units in the former case as in the latter, and therefore only one third as much cooling-water will be required in the former case as in the latter.

 $T_1$  = temperature of steam entering the condenser;  $T_0$  = "circulating-water entering the  $T_2$  = " "leaving the condensed from the steep "water condensed from the steep "water condensed from the steep "..." " circulating-water entering the condenser; " leaving the condenser; " water condensed from the steam;

 $Q = \text{quantity of circulating water in lbs.} = \frac{1114 + 0.3(T_1 - T_3)}{T_2 - T_2}$ .

It is usual to provide pumping power sufficient to supply 40 times the weight of steam for general traders, and as much as 50 times for ships stationed in subtropical seas, when the engines are compound. If the circulating-pump is double-acting, its capacity may be 1/33 in the former and 1/42 in the latter case of the capacity of the low-pressure cylinder.

Air-pump.—The air-pump in all condensers abstracts the water con-

densed and the air originally contained in the water when it entered the boiler. In the case of jet-condensers it also pumps out the water of con-densation and the air which it contained. The size of the pump is calculated from these conditions, making allowance for efficiency of the pump.

Ordinary sea-water contains, mechanically mixed with it, 1/20 of its volume of air when under the atmospheric pressure. Suppose the pressure in the condenser to be 2 lbs. and the atmospheric pressure 15 lbs., neglecting the effect of temperature, the air on entering the condenser will be expanded to 15/2 times its original volume; so that a cubic foot of sea-water, when it to 13/2 times its original volume; so that a cubic foot of sea-water, when it has entered the condenser, is represented by 19/20 of a cubic foot of water and 15/40 of a cubic foot of air. Let q be the volume of water condensed per minute, and Q the volume of sea-water required to condense it; and let  $T_c$  be the temperature of the condenser, and  $T_c$  that of the sea-water. Then 19/20 (q+Q) will be the volume of water to be pumped from the condenser per minute,

and 
$$\frac{15}{40}(q+Q) \times \frac{T_2 + 461^{\circ}}{T_1 + 461^{\circ}}$$
 the quantity of air.

If the temperature of the condenser be taken at 120°, and that of seawater at 60°, the quantity of air will then be .418(q+Q), so that the total volume to be abstracted will be

$$.95(q + Q) + .418(q + Q) = 1.368(q + Q).$$

If the average quantity of injection-water be taken at 26 times that condensed, q+Q will equal 27q. Therefore, volume to be pumped from the condenser per minute = 37q, nearly. In surface condensation allowance must be made for the water occasion-

ally admitted to the boilers to make up for waste, and the air contained in it, also for slight leak in the joints and glands, so that the air-pump is made

about half as large as for jet-condensation, so generally taken at 0.5, and that of a double-acting pump at 0.35. When the temperatur of the sea is 60°, and that of a double-acting pump at 0.35. When the temperatur of the sea is 60°, and that of the (jet) condenser is 10°. Q being the volume of the cooling water and q the volume of the condenser water in cubic feet, and n the number of strokes per minute.

The volume of the single-acting pump = 
$$2.74 \left( \frac{Q+q}{n} \right)$$
.

The volume of the double-acting pump = 
$$4\left(\frac{Q+q}{n}\right)$$

The following table gives the ratio of capacity of cylinder or cylinders to that of the air-pump; in the case of the compound engine, the low-pressure cylinder capacity only is taken,

Description of Punn	p	Description of Engine.					
66 66	Sur Jet Sur Sur tal. Jet Sur Jet Sur	face " face " face "	g, expansion "" compoun expansion "" compoun	11/2 t 3 t d n 11/2 t 11/2 t 3 t	0 2 0 5 0 5	6 to 8 8 to 10 10 to 12 12 to 15 15 to 18 10 to 13 13 to 16 16 to 19 19 to 24 24 to 28	

The Area through Valve-seats and past the valves should not be less than will admit the full quantity of water for condensation at a velocity not exceeding 400 ft. per minute. In practice the area is generally in excess of this.

Area through foot-valves  $= D^2 \times S \div 1000$  square inches. Area through head-valves  $= D^2 \times S \div 800$  square inches. Diameter of discharge-pipe =  $D \times \sqrt{S} + 35$  inches. D = diam. of air-pump in inches, S = its speed in ft. per min.

James Tribe (Am. Mach., Oct. 8, 1891) gives the following rule for air-

pumps used with jet-condensers: Volume of single-acting air-pump driven by main engine = volume of low-pressure cylinder in cubic feet, multiplied by 3.5 and divided by the number of cubic feet contained in one pound of exhaust-steam of the given density. For a double-acting air-pump the same rule will apply, but the volume of steam for each stroke of the pump will be but one half. Should the pump be driven independently of the engine, then the relative speed must be considered. Volume of jet-condenser = volume of air-pump × 4. Area of injection valve = vol. of air-pump in cubic inches + 550.

Circulating-spump. — Let Obe the generating of actions.

Circulating-pump.—Let Q be the quantity of cooling water in cubic fert, n the number of strokes per minute, and S the length of stroke in feet.

Capacity of circulating-pump =  $Q \div n$  cubic feet.

Diameter " " = 13.55 
$$\sqrt{\frac{Q}{n \times S}}$$
 inches.

The following table gives the ratio of capacity of steam-cylinder or cylinders to that of the circulating pump:

Description	n of Pump.	Description of Engine.	Ratio.
Single-a	eting.	Expansive 11/2 to 2 times.	13 to 16
44-	46	" 3 to 5 "	20 to 25
44	"	Compound.	25 to 30
Double	66	Expansive 11/2 to 2 times.	25 to 30
	"	" 3 to 5 "	36 to 46
44	"	Compound.	46 to 56

The cear area through the valve-seats and past the valves should be such that the mean velocity of flow does not exceed 450 fet per minute. The flow through the pipes should not exceed 500 ft. per min. in small pipes and 600 in larce pines

600 in large pipes.

For Centrifugal Circulating-pumps, the velocity of flow in the inlet and outlet pipes should not exceed 400 ft, per min. The diameter of the fan-wheel is from 3½ to 3 times the diam. of the pipe, and the speed at its periphery 450 to 500 ft, per min. If W = quantity of water per minute, in American gallons, d = diameter of pipes in inches, R = revolutions of wheel per min.

gallons, 
$$d = \text{diameter of pipes in inches, } R = \text{revolutions of wheel per min.,}$$

$$d = \sqrt{\frac{170}{16.44}}; \text{ diam. of fan-wheel} = \text{not less than } \frac{1700}{R}.$$
 Breadth of blade at

tip =  $\frac{W}{36d}$ . Diam. of cylinder for driving the fan = about 2.8  $\sqrt{\text{diam. of pipe}}$ ,

and its stroke =  $0.28 \times \text{diam.}$  of fan. Feed-pumps for Marine Engines.—With surface-condensing engines the amount of water to be fed by the pump is the amount condensed from the main engine plus what may be needed to supply auxiliary engines and to supply leakage and waste. Since an accident may happen to the surface-condenser, requiring the use of jet-condensation, the pumps of engines fitted with surface-condensers must be sufficiently large to do duty under such cfreumstances. With jet-condensers and boilers using salt water the dense salt water in the boiler must be blown off at intervals to keep the density so low that deposits of salt will not be formed. Sea-water contains about 1/32 of its weight of solid matter in solution. The boiler of a surface-condensing engine may be worked with safety when the quantity of salt is four times that in sea-water. If Q = net quantity of feed-water required in a given time to make up for what is used as steam,  $n = \text{number of times the saltness of the water in the boiler is to that of sea-water, then the gross feed-saltness of the water in the boiler is to that of sea-water, then the gross feed-saltness of the water in the boiler is to that of sea-water, then the gross feed-$ 

water  $= \frac{n}{n-1}Q$ . In order to be capable of filling the boiler rapidly each feed-pump is made of a capacity equal to twice the gross feed-water. Two feed-pumps should be supplied, so that one may be kept in reserve to be used while the other is out of repair. If Q be the quantity of net feed-water in cubic feet, l the length of stroke of feed-pump in feet, and n the number of strokes per minute,

Diameter of each feed-pump plunger in inches =  $\sqrt{\frac{550 \times Q}{n \times l}}$ .

If W be the net feed-water in pounds,

Diameter of each feed-pump plunger in inches = 
$$\sqrt{\frac{8.9^{\circ} \times \overline{W}}{n \times l}}$$
.

An Evaporative Surface Condenser built at the Virginia Agri cultural College is described by James H. Fitts (Trans. A. S. M. E., xiv. 690). It consists of two rectangular end chambers connected by a series of horizontal rows of tubes, each row of tubes immersed in a pan of water. Through the spaces between the surface of the water in each pan and the bottom of the pan above air is drawn by means of an exhaust-fan. At the top of one of the end-chambers is an inlet for steam, and a horizontal diaphragm about midway causes the steam to traverse the upper half of the tubes and back through the lower. An outlet at the bottom feads to the air-pump. The condenser, exclusive of connection to the exhaust-fan, occupies a floor space of 5'4½'' × 1'9¾'', and 4'1½'' high. There are 27 rows of tubes, 8 in some and 7 in others; 210 tubes in all. The tubes are of brass, No. 20 B. W G., ¾'' external diameter and 4'9½'' in length. The cooling surface (internal) is 176.5 sq. ft. There are 27 cooling pans, each 4'9½'' × 1'9¾'', and 17/16'' deep. These pans have galvanized iron bottoms which slide into horizontal grooves ¼'' wide and ¼'' deep, planed into the tube-sheets. The total evaporating surface is 234.8 sq. ft. Water is fed to every third pan through small cocks, and overflow-pipes feed the rest. A wood casing connects one side with a 30'' Buffalo Forge Co.'s disk-wheel. This wheel is belted to a 3'' × 4'' vertical engine. The air-pump is 5¾'' diameter with a 6'' stroke, is vertical and single-acting.

The action of this condenser is as follows: The passage of air over the

The action of this condenser is as follows: The passage of air over the water surfaces removes the vapor as it rises and thus hastens evaporation. The heat necessary to produce evaporation is obtained from the steam in the tubes, causing the steam to condense. It was designed to condense 800 lbs. steam per hour and give a vacuum of 22 in., with a terminal pressure in the

cylinder of 20 lbs. absolute.

Results of tests show that the cooling water required is practically equal in amount to the steam used by the engine. And since consumption of steam is reduced by the application of a condenser, its use will actually reduce the total quantity of water required. From a curve showing the rate of evaporation per square foot of surface in still air, and also one showing the rate when a current of air of about 2500 ft., per min. velocity is passed over its surface, the following approximate figures are taken:

Temp.	Evaporation sq. ft. p	on, lbs. per er hour.	Temp.	Evaporation, lbs. per sq. ft. per bour.			
F.	Still Air.	Current.	Γ.	Still Air.	Current.		
100°	0.2	1.1	140°	0.8	5.0		
110	0.25	1.6	150	1.1	6.7		
120	0.4	2.5	160	1.5	9.5		
130	0.6	3.5	170	2.0			

The Continuous Use of Condensing-water is described in a series of articles in *Power*, Aug.—Dec., 1892. It finds its application in situations where water for condensing purposes is expensive or difficult to obtain.

In san Francisco J. C. H. Stuf cools the water after it has left the hot-well by means of a system of pans upon the root. These pans are shallow troughs of galvanized iron arranged in tiers, on a slight incline, so that the water flows back and forth for 1500 o. 1000 ft., cooling by evaporation and radiation as it flows. The pans are about 5 ft. in width, and the water as it flows has a depth of about half an inch, the temperature being reduced from about 140° to 90°. The water from the hot-well is pumped up to the highest point of the cooling system and allowed to flow as above described, discharging finally into the main tank or reservoir, whence it again flows to the condenser as required. As the water in the reservoir lowers from evaporation, an auxiliary feed from the city mains to the condenser is operated, thereby keeping the amount of water in circulation practically constant. An accumulation of oil from the engines, with dust from the surrounding streets, makes a cleaning necessary about once in six weeks or two months. It is found by comparative trials, running condensing and non condensing, that

about 50% less water is taken from the city mains when the whole apparatus is in use than when the engine is run non-condensing. 22 to 23 in. of vacuum are maintained. A better vacuum is obtained on a warm day with a brisk breeze blowing than on a cold day with but a slight movement of the air.

In another plant the water from the hot-well is sprayed from a number of fountains, and also from a pipe extending around its border, into a large pond, the exposure cooling it sufficiently for the obtaining of a good vacuum

by its continuous use.

by its continuous use. In the system patented by Messirs. See, of Lille, France, the water is discharged from a pipe laid in the form of a rectangle and elevated above a pond through a series of special nozzles, by which it is projected into a fine spray. On coming into contact with the air in this state of extreme division the water is cooled 40° to 50°, with a loss by evaporation of only one tenth of its mass, and produces an excellent vacuum. A 3000-H.P. cooler upon this system has been erected at Lannoy, one of 2500 H.P. at Madrid, and one of 1200 H.P. at Liege, as well as others at Roubaix and Tourcoing. The system could be used upon a roof if ground space were limited.

In an arrangement adopted by the Worthington Pump Co. for supplying

water to condensers attached to vacuum pans, the injection-water is taken from a tank, and after having passed through the condenser is discharged in a heated condition to the top of a cooling tower, where it is scattered by means of distributing-pipes. The water falling from top to bottom of the tower is lowered in temperature by the cooling effect of the atmosphere and the absorption of heat caused by a portion of the water being vaporized, and

the absorption of near causes of a power of the state of the ward of carries away the heat necessary to be abstracted to condense the steam inside. The condensing pipes are fitted with corrugations mounted with circular ribs, whereby the radiating or cooling surface is largely increased. The pipes, which are cast in sections about 76 in. long by 31/2 in. bore, have a cooling surface of 26 sq. ft., which is found sufficient under favorable conditions to permit of the condensation of 20 to 30 lbs. of steam per hour when producing a vacuum of 13 lbs. per sq. in. In a condense of the three per sq. in, In a condense of the type at Rixdorf, near farlin, a vacuum ranging from 24 to 26 in. of mercury was constantly maintained during the hottest weather 10 to in, or mercury was constantly maintained utiring the notices weather to full distributions. The initial temperature of the cooling-water used in the apparatus under notice ranged from 80° to 85° F, and the temperature in the sun, to which the condenser was exposed, varied each day from 100° to 115° F. During the experiments it was found that it was possible to run one engine under a load of 100 horse-power and maintain the full vacuum without the use of any cooling water at all on the pipes, radiation afforded by the pipes

alone sufficing to condense the steam for this power.

In Klein's condensing water-cooler, the hot water coming from the condenser enters at the top of a wooden structure about twenty feet in height, and is conveyed into a series of parallel narrow metal tanks. The water overflowing from these tanks is spread as a thin film over a series of wooden partitions suspended vertically about 3½ inches apart within the tower. The upper set of partitions, corresponding to the number of metal tanks, reaches half-way down the tower. From there down to the well is usepended a second set of partitions placed at right angles to the first set. This impedes the rapidity of the downflow of the water, and also thoroughly mixes the water, thus affording a better cooling. A fan-blower at the base of the tower drives a strong current of air with a velocity of about twenty feet per second against the thin film of water running down over the partitions. It is estimated that for an effectual cooling two thousand times more air than water must be forced through the apparatus. With such a velocity than water must be forced inrough the apparatus. With such a velocity the air absorbs about two per cent of aqueous vapor. The action of the strong air-current is twofold; first, it absorbs heat from the hot water by being fiself warmed by radiation; and, secondly, it increases the evaporation, which process absorbs a great amount of heat. These two cooling effects are different during the different seasons of the year. During the winter months the direct cooling effect of the cold air is greater, while during summer the heat absorption by evaporation is the more important factor. Taking all the year round, the effect remains very much the same. The evaporation is never so great that the deficiency of water would not be supplied by the additional amount of water resulting from the condensed steam, while in very cold winter months it may be necessary to occasionally rid the cistern of surplus water. It was found that the vacuum obtained by this continual use of the same condensing-water varied during the year between 27.5 and 28.7 inches. The great saving of space is evident from the fact that only the five-hundredth part of the floor-space is required as if cooling tanks or ponds were used. For a 100-horse-power engine the floor-space required is about four square yards by a height of twenty feet. For one horse-power 3.6 square yards cooling-surface is necessary. The vertical suspension of the partitions is very essential. With a ventilator 50 vertical suspension of the partitions is very essential. With a centralization inches in diameter and a tower 6 by 7 feet and 20 feet high, 10,500 gailions of water per hour were cooled from 104 F, to 68° F. The following reconstant was made at Mannheim, Germany: Vacuum in condenser, 28.1 inches; temperature of condensing-water entering at top of tower, 104° to 108° F.; temperature of water leaving the cooler, 66.2° to 71.6° F. The engine was of the Sulzer compound type, of 120 horse-power. The amount of power necessary for the arrangement amounts to about three per cent of the total horse-power of the engine for the ventilator, and from one and one half to three per cent for the lifting of the water to the top of the cooler, the total

being four and one half to six per cent.

A novel form of condenser has been used with considerable success in Germany and other parts of the Continent. The exhaust-steam from the engine passes through a series of brass pipes immersed in water, to which it gives up its heat. Between each section of tubes a number of galvanized disks are caused to rotate. These disks are cooled by a current of air supplied by a fan and pass down into the water, cooling it by abstracting the heat given out by the exhaust-steam and carrying it up where it is driven off by the air-current. The disks serve also to agitate the water and thus aid it in abstracting the heat from the steam. With 85 per cent vacuum the temperature of the cooling water was about 130° F., and a consumption of water for condensing is guaranteed to be less than a pound for each pound of steam condensed. For an engine  $40 \text{ in.} \times 50 \text{ in.}$ , 70 revolutions per minute, 90 lbs. pressure, there is about 1150 sq. ft, of condensingsurface. Another condenser, 1600 sq. ft. of condensing-surface, is used for three engines, 32 in. × 48 in., 27 in. × 40 in., and 30 in. × 40 in., respectively.

-The Steamship.

The Increase of Power that may be obtained by adding a condenser giving a vacuum of 26 inches of mercury to a non-condensing engine may be approximated by considering it to be equivalent to a net gain of 12 pounds mean effective pressure per square inch of piston area. If A = area of piston

in square inches, S = piston-speed in ft. per minute, then  $\frac{12AS}{33.000} = \frac{AS}{2750} = \text{H.P.}$ made available by the vacuum. If the vacuum = 13.2 lbs. per sq. in. = 27.9

The saving of steam for a given horse-power will be represented approximately by the shortening of the cut-off when the engine is run with the condenser. Clearance should be included in the calculation. To the mean effective pressure non-condensing, with a given actual cut-off, clearance considered, add 3 lbs. to obtain the approximate mean total pressure, condensing. From tables of expansion of steam find what actual cut-off will give this mean total pressure. The difference between this and the original actual cut-off, divided by the latter and by 100, will give the percentage of saving.

The following diagram (from catalogue of H. R. Worthington) shows the percentage of power that may be gained by attaching a condenser to a non-condensing engine, assuming that the vacuum is 12 lbs. per sq. in. The mean effective pressures are those of a non-condensing engine exhausting

at atmospheric pressure, clearance and compression not considered.

The left-hand vertical column of figures are the initial steam-pressures
(above the atmosphere), and the upper horizontal column the several points of cut-off that represent the point of the stroke at which the steam is shut off and admission ceases; directly under this column is a similar one of the mean effective pressures. To determine the mean effective pressure produced by 90 pounds steam, cut-off at one quarter, find 90 in the initialpressure column, and follow the line to the rig..t until it intersects the oblique line that corresponds to the 1/2 cut-off. Now read the mean effective pressure from the figures directly above, which in this case is 49 pounds. By glancing down and reading on the lower scale the figure that corresponds with this point of intersection the percentage of gain in power will be seen to be between 25 and 30 per cent of the power of the engine when running non-condensing.

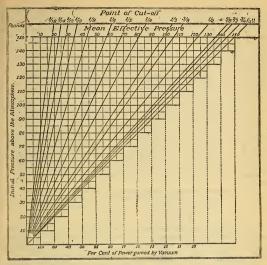


Fig. 151.

Evaporators and Distillers are used with marine engines for the

by apprators and Distillers are used with marine engines for the purpose of providing fresh water for the boilers or for drinking purposes. We'n's Evaporator consists of a small horizontal boiler, contrived so as to be easily taken to pieces and cleaned. The water in it is evaporated by the steam from the main boilers passing through a set of tubes placed in its bottom. The steam generated in this boiler is admitted to the low-pressure valve-box, so that there is no loss of energy, and the water condensed in it is returned to the main boilers.

In Weir's Feed-heater the feed-water before entering the boiler is heated up very nearly to boiling-point by means of the waste water and steam

from the low-pressure valve-box of a compound engine.

## GAS, PETROLEUM, AND HOT-AIR ENGINES.

Gas-engines .- For theory of the gas-engine, see paper by Dugald Clerk, Proc. Inst. C. E. 1882, vol. lxix.; and Van Nostrand's Science Series, No. 62. See also Wood's Thermodynamics. For construction of gas-engines, see Robinson's Gas and Petroleum Engines; articles by Albert Spies in Cassier's Magazine, 1893; also Appleton's Cyc. of Mechanics, and Modern Mechanism.

In the ordinary type of single-cylinder gas-engine (for example the Otto) known as a four-cycle engine one ignition of gas takes place in one end of the cylinder every two revolutions of the fly-wheel, or every two double strokes. The following sequence of operations takes place during four consecutive strokes: (a) inspiration during an entire stroke; (b) compression during the second (return) stroke; (c) ignition at the dead-point, and expansion during the third stroke; (d) expulsion of the burnt gas during the fourth (return) stroke. Beau de Rochas in 1862 laid down the law that there are

four conditions necessary to realize the best results from the elastic force of gas: (1) The cylinders should have the greatest capacity with the smallest circumferential surface; (2) the speed should be as high as possible; (3) the circumferential surface; (2) the speed should be as high as possible; (3) the cut-off should be as early as possible; (4) the initial pressure should be as high as possible. In modern engines it is customary for ignition to take place, not at the dead point, as proposed by Beau de Rochas, but somewhat later, when the piston has already made part of its forward stroke. At first sight it might be supposed that this would entail a loss of power, but experience shows that though the area of the diagram is diminished, the power registered by the friction-brake is greater. Starting is also made easier by this method of working, (The Simplex Engine, Proc. Inst. M. E. 1889.)

In the Otto engine the mixture of gas and air is compressed to about 3 atmospheres. When explosion takes place the temperature suddenly rises

atmospheres. When explosion takes place the temperature suddenly rises to somewhere about 2900° F. (Robinson.)

The two great sources of waste in gas-engines are: 1. The high temperature of the rejected products of combustion; 2. Loss of heat through the cylinder walls to the water-jacket. As the temperature of the water-jacket

is increased the efficiency of the engine becomes higher.

is increased the efficiency of the engine becomes higher. With ordinary coal-gas the consumption may be taken at 20 cu, ft. per hour per I.H.P., or 24 cu, ft. per brake H.P. The consumption will vary with the quality of the gas. When burning Dowson producer-gas the consumption of anthracite (Welsh) coal is about 1.3 lbs. per I.H.P. per hour for ordinary working. With large twin engines, 100 H.P., the consumption is reduced to about 1.1 lb. The mechanical efficiency or B.H.P. + I.H.P. in ordinary engines is about 58%; the friction loss is less in larger engines.

Efficiency of the Gas-engine. (Thurston on Heat as a Form of

Energy.)

•)			
Heat	transferred into useful work		17%
44	" to the jacket-water	52	
44	lost in the exhaust-gas	16	
66	" by conduction and radiation	15	
			83%

This represents fairly the distribution of heat in the best forms of gasengine. The consumption of gas in the best engines ranges from a minimum of 18 to 20 cu. ft. per I.H.P. per hour to a maximum exceeding in the smaller engines 25 cu. ft. or 30 cu. ft. In small engines the consumption per brake horse-power is one third greater than these figures.

The report of a test of a 170-H.P. Crossley (Otto) gas-engine in England, 1892, using producer-gas, shows a consumption of but .85 lb. of coal per H.P. hour, or an absolute combined efficiency of 21.3% for the engine and pro-The efficiency of the engine alone is in the neighborhood of 25%.

The Taylor gas-producer is used in connection with the Otto gas-engine at The Taylor gas-producer is used in connection with the Otto gas-engine at the works of Schleicher, Schumm & Co., of Philadelphia. The only loss is due to radiation through the walls of the producer and a small amount of heat carried off in the water from the scrubber. Experiments on a 100-H.P. engine show a consumption of 97/100 lb. of carbon per I.H.P. per hour. This result is superior to any ever obtained on a steam-engine. (From Age, 1883).

Tests of the Simplex Gas-engine, (Proc. Inst. M. E. 1889).—
Cylinder 73/8 × 153/4 in., speed 160 revs. per min. Trials were made with town gas of a heating value of 607 heat-units per cubic foot, and with Dowson

gas, rich in CO, of about 150 heat-units per cubic foot.

	Т	own G	as.	Dowson Gas.				
Effective H.P. Gas per H.P. per hour, cu. ft Water per H.P. per hour, lbs. Temp. water entering, F "effluent	54.7 51°	2. 8.67 20.12 44.4 51° 144°	3. 9.28 20.73 43.8 51° 172°	1. 7.12 88.03 58.3 48° 144°	2. 3.61 114.85	3. 5.26 97.88		

The gas volume is reduced to 32° F, and 30 in barometer. A 50-H.P. engine working 35 to 40 effective H.P. with Dowson generator consumed 51 lbs. English anthracite per hour, equal to 1.48 to 1.3 lbs. per effective H.P. A 16-H.P. engine working 12 H.P. used 19.4 cu, ft. of gas per effective H.P. A 320-H.P. Gas-engine.—The flour-mills of M. Leblanc, at Pantin, France, have been provided with a 320-horse-power fuel-gas engine of the Simplex type. With coal-gas the machine gives 450 horse-power. There is one cylinder, 34.8 in. diam.; the piston-stroke is 40 in.; and the speed 100 revs.

per min. Special arrangements have been devised in order to keep the different parts of the machine at appropriate temperatures. The coal used is 0.81° lb, per indicated or 1.03° lb, per brake horse-power. The water used is 83′ gallons per brake horse-power per hour.

\*\*Test of an Otto Cas-engine.\* (Jour. F. I., Feb. 1890, p. 115.)—Engine 7° l1.P. nominal; working capacity of cylinder .2594 cu. ft.; dearance

space .1796 cu. ft.

Temperature of gas supplied. 62.2 " " exhaust 774.3	Heat-units. Per cent of Heat received.
" exhaust. 774.3  " enteringwater 50.4  " exit water. 89.2  Pressure of gas, in, of water. 3.06  Revolution per min, av'ge 161.6  Explosions missed per min., average. 6.8  Mean effective pressure, ibs. per sq. in 59.  Horse-power, indicated. 4.94  Work per explosion, footpounds. 2204.  Explosions per minute. 74.	$ \begin{array}{llllllllllllllllllllllllllllllllllll$
Gas used per I.H.P. per hour, cu. ft	H 51.57 9.021 N 9.06 22.273 99.96 99.995

Temperatures and Pressures developed in a Gas-engine. (Clerk on the Gas-engine.)-Mixtures of air and Oldham coal-gas. Temperature before explosion, 17° C.

Mi:	xture.	Max. Press above Atmos.,	sion calculated	Temp, of Explo-
Gas.	Air.	lbs. per sq. in.	from observed Pressure.	sion if all Heat were evolved.
1 vol.	14 vols.	40.	806° C.	1786° C.
1 "	13 "	51.5	1033	1912
1 "	12 "	60.	1202	2058
1 ."	11 "	61.	1220	2228
1 "	9 "	78.	1557	2670
1 "	7 "	87.	1733	3334
1 "	6 "	90.	1792	3808
1 "	5 "	91.	1812	
1 "	4 "	80.	1595	

Test of the Clerk Gas-engine. (Proc. Inst. C. E. 1882, vol. lxix.)—Cylinder 6 × 12 in., 150 revs. per min.; mean available pressure 70.11bs.; LH.P.; maximum pressure, 220 lbs. per sq. in. above atmosphere; pressure before ignition, 41 lbs. above atm.; temperature before compression 60° F., after compression, 313° F.; temperature after ignition calculated from pressure, 280° F.; gas required per 1.H.P. per low. 20° C. don Inray, in discussion of Mr. Clerk's paper on Theory of the Gas-engine, says: The change which Mr. Otto introduced, and which rendered the engine a success, was that, instead of burning in the cylinder an explosive mixture of reas and

was that, instead of burning in the cylinder an explosive mixture of gas and air, he burned it in company with, and arranged in a certain way in respect of, a large volume of incombustible gas which was heated by it, and which diminished the speed of combustion. W. R. Bousfield, in the same discussion, says: In the Otto engine the charge varied from a charge which was an explosive mixture at the point of ignition to a charge which was merely an inert fluid near the piston. When ignition took place there was n explosion close to the point of ignition that was gradually communicated throughout the mass of the cylinder. As the ignition got farther away from the primary point of ignition the rate of transmission became slower, and if the engine were not worked too fast the ignition should gradually catch up to the piston during its travel, all the combustible gas being thus consumed. This theory of slow combustion is, however, dispute by Mr. Clerk, who holds that the whole quantity of combustible gas is ignited in an instant.

Use of Carburetted Air in Gas-engines.—Air passed over

gasoline or volatile petroleum spirit of low sp. gr., 0.65 to 0.70, liberates some of the gasoline, and the air thus saturated with valor is equal in heating or lighting power to ordinary coal-gas. It may therefore be used as fuel for gas-engines. Since the vapor is given off at ordinary temperatures gasoline is very explosive and dangerous, and should be kept in an underground tank out of doors. A defect in the use of carburetted air for gasengines is that the more volatile products are given off first, leaving an oily residue which is often useless. Some of the substances in the oil that are taken up by the air are apt to form troublesome deposits and incrustations when hurned in the engine cylinder.

The Otto Gasoline-engine. (Eng'g News, May 4, 1893.)—It is claimed that where but a small gasoline-engine is used and the gasoline bought at retail the liquid fuel will be on a par with a steam-engine using 6 lbs. of coal per horse-power per hour, and coal at \$3.50 per ton, and will besides save all the handling of the solid fuel and ashes, as well as the attendance for the boilers. As very few small steam-engines consume less than 6 lbs. of coal per hour, this is an exceptional showing for economy. At 8 cts, per gallon for gasoline and 1/10 gal, required per H.P. per hour, the

cost per H.P. per hour will be 0.8 cent.

The Priestman Petroleum-engine. (Jour. Frank. Inst., Feb. 1883) —The following is a description of the operation of the engine: Any ordinary high-test (usually 150° test) oil is forced under air-pressure to an ordinary high-test (usually 100 test) oil is forced under air-pressure to an atomizer, where the oil is met by a current of air and broken up into atoms and sprayed into a mixer, where it is mixed with the proper proportion of supplementary air and sufficiently heated by the exhaust from the cylinder passing around this chamber. The mixture is then drawn by suction into the cylinder, where it is compressed by the piston and ignited by an electric spark, a governor controlling the supply of oil and air proportionately to the work performed. The burnt products are discharged through an exhaust-valve which is actuated by a cam. Part of the air supports the conbustion of the oil, and the heat generated by the combustion of the oil expands the air that remains and the products resulting from the explosion, and thus develops its power from air that it takes in while running. In other words, the engine exerts its power by inhaling air, heating that air, and expelling the products of combustion when done with. In the largest engines only the 1/250 part of a pint of oil is used at any one time, and in the smallest sizes the fuel is prepared in correct quantities varying from 1/7000 of a pint upward, according to whether the engine is running on light or full duty. The cycle of operations is the same as that of the Otto gasengine.

Trials of a 5-H.P. Priestman Petroleum-engine. (Prof. W. Unwin, Proc. Inst. C. E. 1892.)—Cylinder, 8½-12 in., making normally 90 revs, per min. Two oils were used, Russian and American. The more

important results were given in the following table;

	Trial V. Full Power.	Trial I. Full Power.	Trial IV. Full Power.	Trial II. Half Power.	Trial III. Light.
Oil used	Day-	Russo-	Russo-	Russo-	Russo-
On used	light.	lene.	lene.	lene.	lene.
Brake H.P	7.722	6.765	6.882	3.62	
I.H.P	9.369	7.408	8,332	4.70	0.889
Mechanical efficiency	0.824	0.91	0.876	0.769	
Oil used per brake H.P.	0.00.	1	0.000	01100	
hour, lb	0.842	0.946	0.988	1.381	
Oil used per brake H.P.	0.040	0.010	0.000	1.001	
hour, lb	0.694	0.864	0.816	1.063	5.784
Lb. of air per lb. of oil	33.4	31.7	43.2	21.7	10.1
		91.7	45.2	21.7	10.1
Mean explosion pressure,		404.0	400 =	10 =	0.0
lbs. per sq. in	151.4	134.3	128.5	48.5	9.6
Mean compression pres-					
sure, lbs. per sq. in	35.0	27.6	26.0	14.8	6.0
Mean terminal pressure,					
lbs. per sq in	35.4	23.7	25.5	15.6	

To compare the fuel consumption with that of a steam-engine, 1 lb, of oil might be taken as equivalent to 11/4 lbs. of coal. Then the consumption

in the oil-engine was equivalent, in Trials I., IV., and V., to 1.18 lbs., 1.23 lbs., and 1.02 lbs. of coal per brake horse-power per hour. From Trial IV. the following values of the expenditure of heat were obtained:

	•	r	er cent.
Useful work at brak	ce		13.31
Engine friction		· · · · · · · · · · · · · · · · · · ·	2.81
Heat shown on indie	cator-diagram		16.12
Rejected in jacket-	water	• • • • • • • • • • • • • • • • • • • •	47.54
Radiation and unac	watert-gases		9.61
Total			99.99

Naphtha-engines are in use to some extent in small yachts and launches. The naphtha is vaporized in a boiler, and the vapor is used expansively in the engine-cylinder, as steam is used; it is then condensed and teturned to the boller. A portion of the napitha vapor is used for fuel under the boller. According to the circular of the builders, the Gas Engine and Power Co, of New York, a 2-H.P. engine requires from 3 to 4 quarts of naphtha per hour, and a 4-H.P. engine from 4 to 5 quarts. The chief advantages of the naphtha-engine and boller for launches are the saving of weight and the quickness of operation. A 2-H.P. engine weight 300 lbs., a 4-H.P. 300 lbs. It takes only about two minutes to get under headway. (Modern Mechanism, p. 270.)

Hot-air or Calorie Engines.—Hot-air engines are used to some extent, but their bulk is enormous compared with their effective power. For

extent, but their bulk is enormous compared with their effective power. For an account of the largest hot-air engine ever built (a total failure) see Church's Life of Ericsson. For theoretical investigation, see Rankine's Steam-engine and Rontgen's Thermodynamics. For description of constructions, see Appleton's Cyc. of Mechanics and Modern Mechanism, and Babcock on Substitutes for Steam, Trans. A. S. M. E., vii., p. 698.

Test of a Hot-air Engine (Robinson).—A vertical double-cylinder (Caloric Engine Co.'s) 12 nominal H. P. engine gave 20.19 J. H. P. in the working cylinder and 11.38 L.H. P. in the pump, leaving 8.81 net I.H. P.; while the Constraint of the Working of the Robert B. P. was 5.0 giving a machanical efficiency of Formation.

ing cylinder and 11.38 l.H.P. in the pump, leaving 8.81 net l.H.P.; while the effective brake H.P. was 5.9, giving a mechanical efficiency of 675. Consumption of coke, 3.7 lbs. per brake H.P. per hour. Mean pressure on pistons 15.37 lbs. per square inch, and in pumps 15.9 lbs., the area of working cylinders being twice that of the pumps. The hot air supplied was about 1160° F, and that rejected at end of stroke about 890° F.

The b st result of Stirling's hert-engine was 2.7 lbs. per brake H.P. per hour. Bailey's hot-air engine, 2 H.P. nominal, gave 4.2 l.H.P., 2.6 B.H.P.; mechanical efficiency 62%; estimated temperature at highest pressure 1500° F, and at atmospheric pressure 700° F. Highest pressure, 14 lbs. per square inch above atmosphere. Consumption of fuel, 7 lbs. per hour per brake.

inch above atmosphere. Consumption of fuel, 7 lbs. per hour per brake H.P., and of cooling water, 30 lbs.

### LOCOMOTIVES.

Efficiency of Locomotives and Resistance of Trains, (George R. Henderson, Proc. Engrs. Club of Phila. 1886.)—The efficiency of locomotives can be divided into two principal parts: the first depending upon the size of the cylinders and wheels, the valve-gear, boiler and steampassages, of which the tractive power is a function; and the second upon the speed, grade, curvature, and friction, which combine to produce the resistance.

The tractive power may be determined as follows:

Let P = tractive power;

p = average effective pressure in cylinder;
 S = stroke of piston;

d = diameter of cylinders; D = diameter of driving-wheels. Then

$$P = \frac{4\pi d^2 pS}{4\pi D} = \frac{d^2 pS}{D}.$$

The average effective pressure can be obtained from an indicator-diagram, or by calculation, when the initial pressure and ratio of expansion are known, together with the other properties of the valve-motion. The sub-joined table from "Auchincloss" gives the proportion of mean effective pressure to boiler-pressure above atmosphere for various proportions of cut-off.

Stroke, Cut off at—	M.E.P. (Boiler- pres. = 1).	Stroke, Cut off at—	(M.E.P. Boiler- pres. = 1).	Stroke, Cut off at—	M.E.P. (Boiler- pres. = 1).
$ \begin{array}{c} .1 \\ .125 = \frac{1}{8} \\ .15 \\ .175 \\ .2 \\ .25 = \frac{1}{4} \end{array} $	.15 .2 .24 .28 .32 .4 .46	$.333 = \frac{1}{3}$ $.375 = \frac{3}{8}$ $.4$ $.45$ $5 = \frac{1}{2}$ $.55$	.5 = ½ .55 .57 .62 .67 .72	$.625 = \frac{5}{8}$ $.666 = \frac{2}{3}$ $.7$ $.75 = \frac{3}{4}$ $.875 = \frac{7}{8}$	.79 .82 .85 .89 .93

These values were deduced from experiments with an English locomotive by Mr. Gooch. As diagrams vary so much from different causes, this table will only fairly represent practical cases. It is evident that the cut-off must be such that the boiler will be capable of supplying sufficient steam at the given speed

In the following calculations it is assumed that the adhesion of the engine is at least equal to the tractive power, which is generally the case—if the engine be well designed—except when starting, or running at a very low rate of speed, with a small expansive ratio. When running faster, economy, and also the size of the boiler, necessitate a higher ratio of expansion, thus reducing the tractive power below the adhesion. If the adhesion be less than the tractive power, substitute it for the latter in the following for-

The resistances can be computed in the following manner, first considering the train:

There is a resistance due to friction of the journals, pressure of wind, etc., which increases with the speed. Most of the experiments made with a view of determining the resistance of trains have been with European rolling-stock and on European railways. The few trials that have been made here seem to prove that with American systems this resistance is less.

The following table gives the resistance at different speeds, assumed for American practice :

Speed in miles per hour:

Coefficient of resistance in terms of load : l = .0015 .0017 .0020 .0024 .0029 .0035 .0043 .0051 .0060 .0071 .0084 .0096

$$l = .0015 \Big( 1 + \frac{s^2}{650} \Big).$$

The resistance due to curvature is about .5 lb. per ton per degree of curvature, or the coefficient = .00025c, where c = the curvature in degrees

The effect of grades may be determined by the theory of the inclined

Consider a load L on a grade of m feet per mile. The component of the weight L acting in the line of traction, or parallel to the track, is

$$L \sin \theta = \frac{Lm}{5280} = .00019 Lm.$$

To combine these coefficients in one equation representing the resistance of the train:

Let L = weight of train, exclusive of engine, in pounds; R = resistance of train, in pounds.

$$R = \text{resistance of train, in pounds.}$$
  
 $s, c, \text{ and } m, \text{ as above. Then}$   
 $R = L \left[ .0015 \left( 1 + \frac{s^2}{650} \right) + .00025c \pm .00019m \right],$ 

the ± sign meaning that this coefficient is positive for ascending and negative for descending grades.

To find a grade upon which a train would descend by itself, take the last coefficient minus and make R = 0, whence

$$m = 7.9 \left( 1 + \frac{s^2}{650} \right) + 1.3c.$$

As locomotives usually have a long rigid wheel-base, the coefficient for curvature had better be doubled. The resistance due to the friction of the working parts will be considered as being proportional to the tractive power. so that the effective tractive power will be represented by uP, the resistance being (1-u)P

Combining all these values, there results the equation between the tractive power and the weight of the train and engine:

$$uP - W(.0005c + .00019m) = Ll + .00025c \pm .00019m,$$

W being weight of engine and tender, and u being probably about .8. Transforming, we have

$$L = \frac{uF - W(.0005c \pm .00019m)}{l + .00025c \pm .00019m},$$

and

$$P = \frac{L(l + .00025c \pm .00019m) + W(.0005c \pm .00019m)}{u}.$$

These deductions, says Mr. Henderson, agree well with railroad practice.

The figures given above for resistances are very much less than those given by the old formulæ (which were certainly wrong), but even Mr. Henderson's figures for high speed are too high, according to a diagram given by D. L. Barnes in Eng'g Mag., June, 1894, from which the following figures are derived:

Eng'g News, March 8, 1894, gives a formula which for high speeds gives figures for resistance between those of Mr. Barnes and Mr. Henderson. See tests reported in Eng'g News of June 9, 1892. The formula is, resistance in pounds per ton  $=\frac{1}{2}$  velocity in niles per hour +2. This gives for

Speed ...... 5 10 15 20 25 30 35 40 45 50 60 70 80 90 100 Resistance. 3½ 4.5 5¾ 7 8½ 9.5 10¾ 12 13½ 14.5 17 19.5 22 24.5 27 70 80 90 100

For tables showing that the resistance varies with the area exposed to the resistance and friction of the air per ton of load, see Dashiell, Trans. A. S.

M. E., vol. xiii. p. 371. Inertia and Resistances of Railroad Trains at Increasing Speeds.—A series of tables and diagrams is given in R. R. Gaz., Oct. 31. 1890, to show the resistances due to inertia in starting trains and accelerat-

ing their speeds.

The mechanical principles and formulæ from which these data were calculated are as follows:

S = speed in miles per hour to be acquired at the end of a mile.

S + 2 = average speed in miles per hour during the first mile run.  $V = \text{velocity in feet per second at the end of a mile; then } V \div 2 = \text{aver-}$ 

age velocity in feet per second during the first mile run.

5280 + V/2 = time in seconds required to run first mile = 10560 + V.  $V + (10560 + V) = V^2 + 10560 = .0000947 V^2 =$  Constant gain in velocity or acceleration in feet per second necessary to the acquirement of a velocity V at the end of a mile.

as the end of a fine. g = acceleration due to the force of gravity, i.e., 32.2 feet per second. The forces required to accelerate a given mass in a given time to different velocities are in proportion to those velocities. The weight of a body is the measure of the force which accelerates it in the case of gravity, and as we are considering 1 lb., or the unit of weight, as the mass to be accelerated, we have  $g : (7^2 + 0560) : 1$  is to the force required to accelerate 1 lb. to the velocity V at the end of a mile run, or, what is the same, to accelerate it at the rate of  $V^2 + 0560$  feet her second the rate of  $V^2 \div 10560$  feet per second.

From this the pull on the drawbar—it is the same as the force just mentioned, and is properly termed the inertia—in pounds per pound of train weight is  $V^2 + (10500 \times 32.2)$ , which equals  $0.0000294V^2$ .

This last formula also gives the grade in per cent which will give a resistance equal to the inertia due to acceleration.

The grade in feet per mile is  $.00000294V^2 \times 5280 = .01558V^2$ . The resistance offered in pounds per ton is 2000 times as much as per

pound, or .00588 V2.

When the adhesion of locomotive drivers is 600 lbs, per ton of weight thereon—this is about the maximum—then the tons on drivers necessary to overcome the inertia of each ton of total train load are  $.00588V^2 \div 600 =$ .0000098 V2. In this determination of resistances no account has been taken of the rotative energy of the wheels.

Efficiency of the Mechanism of a Locomotive. — Druitt Halpin (Froc. Inst. M. E., January, 1889), writes as follows, concerning the tractive efficiency of locomotives; With simple two-cylinder engines, havtractive enciency of locomotives; with simple two-cylinder engines, having four wheels coupled, experiments have been made by the late locomotive superintendent of the Eastern Railway of France, M. Regray, with the greatest possible care and with the best apparatus, and the result arrived at was that out of 100 LH.P in the cylinders 43 H.P. only was available on the draw-bar. The loss of 5% was rather a high price to pay for the efficiency of the engine. How much of that loss was due to coupling rods no one could yet say; but a considerable amount of it must be due to the rods, because it was known that large engines with a single pair of driving-wheels not coupled were doing their work more economically, while advanced locomotive engineers who had not yet gone in for compounding were at any rate going back to the single pair of driving-wheels. Moreover, that astonishing going back to the single pair of driving-wheels. Moreover, that astonishing loss of 5% had been confirmed independently on the Pennsylvania Railroad, trials made with an engine having 184 × 24 in. cylinders and 6 ft. 6 in wheels four-coupled; by taking indicator diagrams up to 65 miles an hour, which were professed to be taken correctly, the power on the draw-bar was found to be only 42% of that in the cylinders, or only 1% less than in the French experiments.

The Size of Locomotive Cylinders is usually taken to be such that the engine will just overcome the adhesion of its wheels to the rails un-

der favorable circumstances.

The adhesion of the wheel is about one third the weight when the rail is

clean and sanded, but is usually assumed at 0.25. (Thurston.)

A committee of the American Association of Master Mechanics, after studying the performance reports of the best engines, proposes the following formula for weight on driving-wheels: W = in which the mean pressure in the cylinder is taken at 0.85 of the boiler-pressure at starting, C is a numerical coefficient of adhesion, d the diameter of cylinder

starting, C is a numerical coefficient of adhesion, a the diameter of cylinder in inches, D that of the drivers in inches, P the pressure in the boiler in pounds per square inch, S the stroke of piston in inches. C is taken as 0.24 for passenger engines, 0.24 for freight, and 0.29 for "switching" engines. The common builder's rule for determining the size of cylinders for the locomotive is the following, in which we accept Mr. Forney's assumption that the steam-pressure at the engine may be taken as nine tenths that in the boiler: The tractive force is, approximately,  $F = \frac{0.9p_1 \times 4 \times 48}{C}$  where

C is the circumference of tires of driving-wheels, S = the stroke in inches, C is the circumference of thres of driving wheels, S= the stoke in horizon  $p_1=$  the initial runbalanced steam-pressure in the cylinder in pounds per square inch, and A= the area of one cylinder in square inches. If D= diameter of driving wheel and d= diameter of cylinder,  $F=\frac{0.9p_1\times d^2S}{D}$ . Taking the adhesion at one fourth the weight W

$$F = 0.25W = \frac{0.9p_1 \times A \times 4S}{C} = \frac{0.9p_1d^2S}{D}$$
;

whence the area of each piston is

$$A = \frac{0.25CW}{0.9 \times 4 \times p_1 S}; \quad \hat{d} = \sqrt{\frac{0.25DW}{0.9p_1 S}}.$$

The above formulæ give the maximum tractive force; for the mean tractive force substitute for  $p_1$  in the formulæ the mean effective pressure.

Von Borries's rule for the diameter of the low-pressure cylinder of a compound locomotive is  $d^2 = \frac{2ZD}{2}$ 

where d = diameter of l.p. cylinder in inches; D = diameter of driving-wheel in inches;

p = mean effective pressure per sq. in., after deducting internal machine friction:

h = stroke of piston in inches:

Z = tractive force required, usually 0.14 to 0.16 of the adhesion.

The value of p depends on the relative volume of the two cylinders, and from indicator experiments may be taken as follows:

Class of Engine. Ratio of Cylinder p in percentage p for Boiler-press ure of 176 lbs. Volumes. of Boiler-pressure. 1:2 or 1:2.05 Large-tender eng's 1:2 or 1:2.2 40 Tank-engines.....

The Size of Locomotive Bollers. (Forney's Catechism of the Locomotive.)—They should be proportioned to the amount of adhesive weight and to the speed at which the locomotive is intended to work. Thus a locomotive with a great deal of weight on the driving-wheels could pull a heavier load, would have a greater cylinder capacity than one with little adhesive weight, would consume more steam, and therefore should have a larger boiler.

The weight and dimensions of locomotive boilers are in nearly all cases determined by the limits of weight and space to which they are necessarily confined. It may be stated generally that within these limits a locomotive boiler cannot be made too large. In other words, boilers for locomotives

should always be made as large as is possible under the conditions that de-termine the weight and dimensions of the locomotives.

Wootten's Locomotive. (Clark's Steam-engine: see also Jour.
Frank. Inst. 1891, and Modern Mechanism, p. 485.—J. E. Wootten designed and constructed a locomotive boiler for the combustion of anthractic and lignite, though specially for the utilization as fuel of the waste produced in the mining and preparation of authracite. The special feature of the engine is the fire-box, which is made of great length and breadth, extending clear over the wheels, giving a grate-area of from 64 to 85 sq. ft. The draught diffused over these large areas is so gentle as not to lift the fine particles of diffused over these large areas is so gentle as not to lift the fine particles of the fuel. A number of express-engines having this type of boiler are engaged on the fast trains between Philadelphia and Jersey City. The fire-box sies 8 ft. 8 in, wide and 10 ft. 5 in. long; the fire-box is 8×9½ ft., making 76 sq. ft. of grate-area. The grate is composing of bars and water-tubes altermately. The regular types of cast-ron shaking grates are also used. The height of the fire-box is only 2 ft. 5 in, above the grate. The grate is terminated by a bridge of fire-brick, beyond which a combustion-chamber, 27 in. long, leads to the flue-tubes, about 184 in number, 134 in. diam. The cylinders are 21 in. diam., with a stroke of 22 inches. The driving-wheels, four-coupled, are 5 ft. 8 in. diam. The engine weighs 44 tons, of which 29 tons are on driving wheels. The heating-surface of the fire-box is 135 sq. ft., that of the flue-tubes is 982 sq. ft.; together, 1117 sq. ft., or 14.7 times the grate-area. Hauling 15 passenger-cars, weighing with passengers 360 tons, at an average speed of 42 miles per hour, over ruling gradients of 1 in 89, the engine con-

speed of 5 lines, per hour core rating grantents of 1 m s, the tegine con-sumes 62 bs. of fuel per mile, or 314 bs. per sq. ft. of grate per hour. **Qualities Essential for a Free-steaming Locomotive**, (From a paper by A. E. Mitchell, read before the N. Y. Railroad Club, Eng'y News, Jan. 24, 1891.)—Square feet of boiler-heating surface for bituminous coal should not be less than 4 times the square of the diameter in inches of a cylinder 1 inch larger than the cylinder to be used. One tenth of this should be in the fire-box. On anthracite locomotives more heatingsurface is required in the fire-box, on account of the larger grate-area required, but the heating-surface of the flues should not be materially

decreased.

Grate-surface, Smoke-stacks, and Exhaust-nozzles for Locomotives. (Am. Mach., Jan. 8, 1891.)—For grate-surface for antiractic coal: Multiply the displacement in cubic feet of one piston during a stroke by 8.5; the product will be the area of the grate in square feet.

Exp. blumpings coal: Multiply the displacement.

For bluminous coal: Multiply the displacement in feet of one piston during a stroke by 055; the product will be the grate-area in square feet for engines with cylinders 12 in. in diameter and upwards. For engines with

smaller cylinders the ratio of grate-area to piston-displacement should be 71/2 to 1, or even more, if the design of the engine will admit this proportion. The grate-areas in the following table have been found by the foregoing

rules, and agree very closely with the average practice :

Smoke-stacks.-The internal area of the smallest cross-section of the stack

should be 1/1° of the area of the grate in soft-coal-burning engines.

A. E. Mitchell, Supt. of Motive Power of the N. Y. L. E. & W. R. R., says that recent practice varies from this rule. Some roads use the same size of stack, 13½ in. diam. at throat, for all engines up to 20 in. diam. of cylinder.

The area of the orifices in the exhaust-nozzles depends on the quantity and quality of the coal burnt, size of cylinder, construction of stack, and the condition of the outer atmosphere. It is therefore impossible to give rules for computing the exact diameter of the orifices. All that can be done is to give a rule by which an approximate diameter can be found. The exact diameter can only be found by trial. Our experience leads us to believe that the area of each orifice in a double exhaust-nozzle should be equal to 1/400 part of the grate-surface, and for single nozzles 1/200 of the grate-surface. These ratios have been used in finding the diameters of the nozzles given in the following table. The same sizes are often used for either hard or soft coal-burners.

Size of Cylinders, in inches.	Grate-area for Anthra- cite Coal, in sq. in.	Grate-area for Bitumin- ous Coal, in sq. in.	Diameter of Stacks, in inches.	Double Nozzles.  Diam. of Orifices, in inches.	Single Nozzles.  Diam. of Orifices, in inches.
$\begin{array}{c} 12 \times 20 \\ 13 \times 20 \\ 14 \times 20 \\ 15 \times 22 \\ 16 \times 24 \\ 17 \times 24 \\ 18 \times 24 \\ 19 \times 24 \\ 20 \times 24 \end{array}$	1591 1873 2179 2742 3415 3856 4321 4810 5337	1217 1432 1666 2097 2611 2948 3304 3678 4081	914 1014 1114 1214 1214 15 15 1534 1614 1715	21/5 21/5 2 5/16 2 9/16 27/6 3 1/16 31/4 3 7/16 35/6	2 13/16 3 31/4 3 11/16 4 1/16 4 5/16 45/6 4 13/16 5 1/16

Exhaust-nozzlos in Locomotive Boilers.—A committee of the Am. Ry. Master Mechanics' Assn. in 1890 reported that they had, after two years of experiment and research, come to the conclusion that, owing to the great diversity in the relative proportions of cylinders and boilers, together with the difference in the quality of fuel, any rule which does not recognize each and all of these factors would be worthless.

The committee was unable to devise any plan to determine the size of the exhaust-nozzle in proportion to any other part of the engine or boiler, and believes that the best practice is for each user of locomotives to adopt a nozzle that will make steam freely and fill the other desired conditions, best determined by an intelligent use of the indicator and a check on the fuel account. The conditions desirable are: That it must create draught enough on the fire to make steam, and at the same time impose the least possible amount of work on the pistons in the shape of back pressure. It should be large enough to produce a nearly uniform blast without lifting or tearing the fire, and be economical in its use of fuel.

Fire-brick Arches in Locomotive Fire-boxes.—A com-

mittee of the Am. Ry. Master Mechanics' Assn. in 1890 reported strongly in favor of the use of brick arches in locomotive fire-boxes. They say: It is the unanimous opinion of all who use bituminous coal and brick arch, that it is most efficient in consuming the various gases composing black smoke, It is most emerical in consuming the various gases composing that almost and by impeding and delaying their passage through the tubes, and mingling and subjecting them to the heat of the furnace, greatly lessens the volume ejected, and intensifies combustion, and does not in the least check but rather augments draught, with the consequent saving of fuel and increased steaming capacity that might be expected from such results. This in particular when used in connection with extension front.

Size, Weight, Tractive Power, etc., of Different Sizes of Locomotives. (J. G. A. Meyer, Modern Locomotive Construction. Am.

Mach., Aug. 8, 1885.)-The tractive power should not be more or less than the adhesion. In column 3 of each table the adhesion is given, and since the adhesion and tractive power are expressed by the same number of pounds. these figures are obtained by finding the tractive power of each engine, for this purpose always using the small diameter of driving wheels given in column 2. The weight on drivers is shown in column 4, which is obtained by multiplying the adhesion by 5 for all classes of engines. Column 5 gives the weights on the trucks, and these are based upon observations. Thus, the weight on the truck for an eight-wheeled engine is about one half of that placed on the drivers.

For Mogul engines we multiply the total weight on drivers by the decimal .2, and the product will be the weight on the truck.

For ten-wheeled engines the total weight on the drivers, multiplied by the decimal .32, will be equal to the weight on the truck.

And lastly, for consolidation engines, the total weight on drivers multi-

plied by the decimal .16, will determine the weight on the truck. In column 6 the total weight of each engine is given, which is obtained by

adding the weight on the drivers to the weight on the truck. Dividing the adding the weight on the drivers to the weight on the truck. Dividing the adhesion given in column 1 by 7½ will give the number of tons of 2000 lbs, that the engine is capable of hauling on a straight and level track, column 7. The weight of engines given in these tables will be found to agree generally with the actual weights of locomotives recently built, although it must not be expected that these weights will agree in every case with the actual weights, because the different builders do not build the engines alike.

The actual weight on trucks for eight-wheeled or ten-wheeled engines will not differ much from those given in the tables, because these weights depend greatly on the difference between the total and rigid wheel-base, and these are not often changed by the different builders. The proportion between the rigid and total wheel-base is generally the same.

The rule for finding the tractive power is :

Square of dia. of \ \times \ Mean effect, steam \ \times \ stroke \ \ piston in inches \ \ press. per sq. in. \ \ in feet \

= tractive power. Diameter of wheel in feet.

E	EIGHT-WHEELED LOCOMOTIVES.							TEN-WHEELED ENGINES.					
Cylinders—Dia- meter, Stroke.	Diameter of Driving- wheels.	Adhesion,	Weight on Drivers.	Weight on Truck,	Total Weight.	Hauling Capacity on Level Track in tons of 2000 lbs., includ- ing Tender.	Cylinders—Diameter, Stroke.	Diameter of Driving- wheels.	Adhesion.	Weight on Drivers,	Weight on Truck.	Total Weight, with Water and Fuel.	Hauling Capacity on Level Track in tons of 2000 lbs., includ- ing Tender.
1	2	3	4	5	6	7	1	2	3	4	5	6	7
in. 10×20 11×22 12×22 13×22 14×24 15×24 16×24 17×24 18×24	in. 45-51 45-51 48-54 49-57 55-61 53-66 58-66 60-66 61-66	lbs. 4000 5324 5940 6828 7697 8836 9533 10404 11472	lbs. 20000 26620 29700 34140 38485 44180 47665 52020 57360	lbs. 10000 13310 14850 17070 19242 22090 23832 26010 28680	1bs. 30000 39930 44550 51210 57727 66270 71497 78030 86040	- 533 709 792 910 1026 1178 1271 1387 1529	in. 12×18 13×18 14×20 15×22 16×24 17×24 18×24 19×24			41023 49500 57600 61200 68611	lbs, 9570 10683 13127 15840 18432 19584 21955 23104	1bs, 39477 44070 54150 65340 76032 80784 90566 95304	
		Mogt	JL EN	GINES			(	Conso	LIDA		Engi		

Mogul Engines.							Consolidation Engines.						
in, 11×16 12×18 13×18 14×20 15×22 16×24 17×24	42-47 45-51	9046 10607 12288 12739 13722		lbs. 4978 6480 7399 9046 10607 12288 12739 13722 14440	1bs. 29869 38880 44396 54276 63642 73738 76436- 82333 86610	663 864 986 1206 1414 1638 1698 1829 1925	in. 14×16 15×18 20×24 22×24	48-50	10125 18000	50625 90000			1045 1350 2400 2787

## Leading American Types of Locomotive for Freight and Passenger Service.

1. The eight-wheel or "American" passenger type, having four coupled driving-wheels and a four-wheeled truck in front. 2. The "ten-wheel" type, for mixed traffic, having six coupled drivers and

a leading four-wheel truck.

3. The "Mogul" freight type, having six coupled driving-wheels and a

pony or two-wheel truck in front.
4. The "Consolidation" type, for heavy freight service, having eight

4. The "Consolidation" type, for heavy freight service, having eight coupled driving wheels and a pony truck in front.

Besides these there is a great variety of types for special conditions of service, as four-wheel and six-wheel switching-engines, without trucks; the Forney type used on elevated railroads, with four coupled wheels under the engine and a four-wheeled rear truck carrying the water-tank and fuel; locomotives for local and suburban service with four coupled driving-wheels, with a two-wheel truck front and rear, or a two-wheel truck front and a four-wheel truck rear, etc. "Decapod" engines for heavy freight service have ten coupled driving-wheels and a two-wheel truck in front.

### Steam-distribution for High-speed Locomotives.

(C. H. Quereau, Eng'q News, March 8, 1894.)

Balanced Valves.—Mr. Philip Wallis, in 1886, when Engineer of Tests for the C., B. & Q. R. R., reported that while 6 H.P. was required to work unbalanced valves at 40 miles per hour, for the balanced valves 2.2 H.P. only

Effect of Speed on Average Cylinder-pressure.—Assume that a locomotive has a train in motion, the reverse lever is placed in the running notch, and the track is level; by what is the maximum speed limited? The resistance of the train and the load increase, and the power of the locomotive decreases with increasing speed till the resistance and power are equal, when the speed becomes uniform. The power of the engine depends on the average pressure in the cylinders. Even though the cut-off and boilerpressure remain the same, this pressure decreases as the speed increases; because of the higher piston-speed and more rapid valve-travel the steam has a shorter time in which to enter the cylinders at the higher speed. The following table, from indicator-cards taken from a locomotive at varying speeds, shows the decrease of average pressure with increasing speed:

Miles per hour.		51	51	53	54	57	60	66
Speed, revolutions	224	248	248	258	263	277	292	321
Average pressure per sq. in.:								
Actual								
Calculated		46.5	46.5	44.7	43.8	41.6	39.5	35.9

The "average pressure calculated" was figured on the assumption that the mean effective pressure would decrease in the same ratio that the speed increased. The main difference lies in the higher steam-line at the lower speeds, and consequent higher expansion-line, showing that more steam entered the cylinder. The back pressure and compression-lines agree quite closely for all the cards, though they are slightly better for the slower speeds. That the difference is not greater may safely be attributed to the large exhaust-ports, passages, and exhaust tip, which is 5 in. diameter. These are matters of great importance for high speeds.

Boiley-pressure.—The increase of train resistance with increased speed is not as the square of the velocity, as is commonly supposed. It is more likely that it increases as the speed after about 20 miles an hour is reached. Assuming that the latter is true, and that an average of 50 lbs, per square inch is the greatest that can be realized in the cylinders of a given engine at 40 miles an hour, and that this pressure furnishes just sufficient power to keep the state of the pressure of the the train at this speed, it follows that, to increase the speed to 50 miles, the mean effective pressure must be increased in the same proportion. To increase the capacity for speed of any locomotive its power must be increased, and at least by as much as the speed is to be increased. One way to accomplish this is to increase the boiler-pressure. That this is generally realized, is shown by the increase in boiler-pressure in the last ten years. For twenty-three single-expansion locomotives described in the rallway journals they year the steam-pressures are as follows: 3, 160 lbs.; 4, 165 lbs.; 2, 170 lbs.; 13, 180 lbs.; 1, 190 lbs,

Valve-travel. - An increased average cylinder-pressure may also be obtained by increasing the valve-travel without raising the boiler-pressure, and better y results will be obtained by increasing both. The longer travel gives a higher steam-pressure in the cylinders, a later exhaust-olosine, and a larger exhaust-opening—all necessary opening heeps and economy. I believe that a 20-in, port and 6½-in, (or even 7-in.) travel could be successfully used for high-speed engines, and that frequently by so doing the cylinders could be economically reduced and the counterbalance lightened. Or, better still, the diameter of the drivers increased,

securing lighter counterbalance and better steam-distribution.

Size of Drivers.—Economy will increase with increasing diameter of drivers, provided the work at average speed does not necessitate a cut-off longer than one fourth the stroke. The piston-speed of a locomotive with 68-in. drivers at 55 miles per hour is the same as that of one with 68-in.

drivers at 61 miles per hour.

Steam-ports.-The length of steam-ports ranges from 15 in. to 23 in., and has considerable influence on the power, speed, and economy of the locomotive. In cards from similar engines the steam-line of the card from the engine with 23-in, ports is considerably nearer boiler-pressure than that of the card from the engine with 17¼-in, ports. That the higher steam-line is due to the greater length of steam-port there is little room for doubt. The 23-in, port produced 53! H.P. in an 18½-fn, cylluder at a cost of 23.5 lbs of indicated water per I.H.P. per hour. The 17½-in, port, 44! H.P., at the rate of 22 9 lbs. of water, in a 19-in. cylinder.

Allen Valves.—There is considerable difference of opinion as to the advan-

tage of the Allen ported-valve (See Eng. News, July 6, 1893.)

Speed of Railway Trains.—In 1834 the average speed of trains on the Liverpool and Manchester Railway was twenty miles an hour; in 1838 it was twenty-five miles an hour. But by 1840 there were engines on the Great was twenty-tive lines an nour. But by 1840 there were engines on the Great Western Railway capable of running fifty miles an hour with a train, and eighty miles an hour without. A speed of 86 miles per hour was made in England with the T. W. Worsdell compound locomotive. The total weight of the engine, tender, and train was 695,000 lbs.; indicator-cards were taken showing 1098.6 H.P. on the level. At a speed of 75 miles per hour on a level, and the same train, the indicator-cards showed 1040 H.P. developed.

(Trans. A. S. M. E., vol. xiii., 363.).

The limitation to the increase of speed of heavy locomotives seems at present to be the difficulty of counterbalancing the reciprocating parts. The unbalanced vertical component of the reciprocating parts causes the pressure of the driver on the rail to vary with every revolution. Whenever the speed is high, it is of considerable magnitude, and its change in direction is so rapid that the resulting effect upon the rall is not inappropriately called a "hammer blow." Heavy rails have been kinked, and bridges have been shaken to their fall under the action of heavily balanced drivers revolving snake to their tail under the action of nearly solanced circles revolving at high speeds. The means by which the evil is to be overcome has not yet been made clear. See paper by W. F. M. Goss, Trans. A. S. M. E., vol. xvi. Engine No. 999 of the New York Central Railroad ran a mile in 32 seconds,

equal to 112 miles per hour, May 11, 1893.

 $Speed\ in\ miles \} = \frac{circum.\ of\ driving-wheels\ in\ in.\ \times\ no.\ of\ rev.\ per\ min.\ \times\ 60}{co.\ 200}$ 63,360

= diam, of driving-wheels in in. × no. of rev. per min. × .003 (approximate, giving result 8/10 of 1 per cent too great).

#### DIMENSIONS OF SOME LARGE AMERICAN LOCOMOTIVES, 1893.

The four locomotives described below were exhibited at the Chicago Exposition in 1893. The dimensions are from Engineering News, June, 1893. The first, or Decapod engine, has ten-coupled driving-wheels. It is one of the heaviest and most powerful engines ever built for freight service. The Philadelphia & Reading engine is a new type for passenger service, with our-coupled drivers. The Rhode Island engine has six drivers, with a 4-wheel leading truck and a 2-wheel trailing truck. These three engines have all compound cylinders. The fourth is a simple engine, of the standard Ameri-can 8-wheel type, 4 driving-wheels, and a 4-wheel truck in front. This engine holds the world's record for speed (1893) for short distances, having run a mile in 32 seconds.

	Baldwin.	Baldwin.	Rhode Isl.	N. Y. C. &		
	N. Y., L. E.	Phila.	Locomoti'e	H. R. R.		
		Read, R. R	Works.	Empire		
	W. R. R.		Heavy	State		
	Decapod Freight.	Express Passenger.	Express.	Express, No. 999.		
	Troight.	- moongor.				
Running-gear:						
Driving-wheels, diam	4 ft. 2 in.	6 ft. 6 in.	6 ft. 6 in.	7 ft. 2 in.		
Truck " "	2 " 6 "	4 " 0 "	9 " 9 "	3 " 4 "		
Journals, driving-axles	9 × 10 in.	8½×12 in.	8 × 834 in. 51/2×10 "	9 × 121/gin.		
" truck- "	5 × 10 " 4½ × 9 "	61%×10 " 41%× 8 "	01/6 × 10 "	614×10 " 418× 8 "		
Wheel-base:	172 × 3	472 ^ 0	41/4×8 "	478× 0		
Driving	18 ft. 10 in.	6 ft. 10 in.	13 ft, 6 in.	8 ft. 6 in.		
Driving		93 " 4 "	13 ft. 6 in. 29 " 914 " 15 " 0 "	23 " 11 "		
tender	16 " 8 "	16 " 0 "	15 " 0 "	15 ft. 21/2 "		
" engine and tender	53 " 4 "	47 " 3 "	50 " 634 "	8 ft. 6 in. 23 " 11 " 15 ft. 2½ " 47 " 8½ "		
Wt. in working-order:	100 000 11	00 C00 11-	00 500 11-			
On drivers	170,000 lbs. 29,500 "	82,700 lbs.	88,500 lbs. 54,500 "	84,000 lbs. 40,000 "		
Engine, total	192,500 "	47,000 " 129,700 " 80,573 "	143,000 "	124,000 "		
Tender "	192,500 '' 117,500 ''	80,573 "	75,000 "	80,000 "		
Engine and tender, loaded	310,000 ''	210,273 ''	218,000 "	204,000 "		
Cylinders:						
h.p. (2)	16 × 28 in.	13 × 24 in.	one 21 × 26	19 × 24 in.		
l.p. (2).	27×28 :" 7 ft. 5 "	22 × 24 " 7 ft. 4½ in.	one 31 × 26 7 ft, 1 in.	6 ft. 5 in.		
Distance centre to centre. Piston-rod, diam	4 in.	3½ in.	3½ in.	33% in.		
Connecting rod, length	9' 8 7/16"	8 ft. 01/2 in.		8 ft. 1½ in.		
			11/2 × 20 and 11/2 × 25 3 × 20 in.			
Steam-ports	28½×2 in.	24 × 11/2 in.	$11\sqrt{2} \times 25$	1½×18 in.		
Exhaust-ports	28½×8 "	24 × 41/2 "	3 × 20 in.	23/4 × 18 "		
Slide-valves, out. lap, h.p.	% in.	% in.	11/4 in.	1 in.		
Exhaust-ports	% in. 5% "	% in. 5% (neg.) 1% in.	1 in.	1 /10 in		
" in, lap, h.p " in, lap, l.p		None None		1/10 in.		
" max. travel.	6 in.	5 in.	61/4 in.	5½ in.		
" " lead, h.p	1/16 in.	1/8 "	61/4 in. 3/32 "			
" " lead. l.p	5/16 "	1/8 " 3/8 "				
Boiler-Type Diam. of barrel inside	Straight	Straight	Wagon top	Wagon top		
Diam. of barrel inside	6 ft. 2½ in. ¾ in.	4 ft. 814 in.	5 ft. 2 in. 5% in.	4 ft. 9 in.		
Thickness of barrel-plates Height from rail to centre	% III.	5% in.	98 III.	9/16 in.		
line	8 ft. 0 in.		8 ft. 11 in.	7 ft. 1116 in.		
line Length of smoke-box	8 ft. 0 in. 5 " 77/8 " _180 lbs.		8 ft. 11 in. 6 " 1 "	7 ft. 11½ in.		
Working steam-pressure	180 lbs.	180 lbs.	200 lbs.	190 lbs.		
Firebox-type	Wootten	Wootten	Radial stay	Buchanan		
Length inside	10' 11 9/16"	9 ft. 6 in. 8 " 018 " 3 " 234 "	10 ft. 0 in. 2 " 936" 6 " 1034"	9 ft. 63% in. 3 " 47% " 6 " 114 "		
Width "Depth at front	8 ft. 21/8 in.	3 " 93/ "	6 " 1032 "	6 " 111 "		
Thickness of side plates	5/16 in.	5/16 111.	5/16 in.			
Thickness of side plates "back plate	5/16 **	5/16 "	3/6 "	5/16 "		
Thickness of crown-sheet.		5/16 " 5/16 " 12 "	3/8 " 3/8 " 1/8 "	5/16 "		
	1/2	1/2 "				
Grate-area Stay-bolts, diam., 11/8 in	89.6 sq. ft.	76.8 sq. ft.	28 sq. ft.	30.7 sq. ft.		
Tubes—iron	254 piten, 4½ in.	324	4 in. 272	4 in. 268		
Pitch	23/4 in.	2 1/16 in.	234 in.			
Diam., outside	2 4 11.	11/6 in.	2	2 in.		
Length betw'n tube-plates	11 ft. 11 in.	10 ft. 0 in.	12 ft. 85% in.	12 ft. 0 in.		
Heating-surface:						
Tubes, exterior	2,208.8 ft.	1,262 sq. ft.		1,697 sq. ft.		
Missellaneous	234.3 ''	178 " "		233		
Miscellaneous : Exhaust-nozzle, diam	5 in.	5½ in.		314 in		
Smokestack, smal'st diam.	1 ft. 6 "	1 ft. 6 in.	1 ft. 3 in.	31/2 in. 1 ft. 31/4 in.		
neight from						
rail to top	15 " 61/2 "	14 ft. 0¾ in.	15 " 2 "	14 " 10 "		
7,2 12,20,74,20,1 22 17 17						

nesion, inder-power to Weight, Avail-able for Ad-Ratio of Cyl-·uı 03 03 03 2 ರು ಎಲ್ಲಿ ಎಂದು ಎ : oo oo oo Diam.of Tubes ft. and in. 04%00000 Length of 'sqi Atmospheric, ure per sq. in. -ssand-muans surface, sq. it. Tube Heatingsq. it. 143.7 186 186 141.2 88 845348 ing-surface, Firebox Heat-·11 ·bs Area of Grate, wheels, ibs. On Driving-Total Weight of Engine, lbs. Total Weight \*\*\*\*\*\*\* \*\*\*\*\*\* 19×28 21×28 21×28 20×26 19×26 10 ×26 10 ×27 mg-wneeis, m. Diam, of Driv-Truck-wheels. No. of Front 29949499000000000000<del>0</del>49 No. of Drivers. Passenger or Freight Engine ; Reading Name of Railroad. & Q. & St. P. Y. & Pa. of N. J. R. Iphia & 1 अद्भ अ R. R. o nn. R. j niladelp 

Dimensions of Some American Locomotives.—The table on page 861 is condensed from one given by D. L. Barnes, in his paper on "Distinctive Features and Advantages of American Locomotive Practice," Trans. A.S.C.E., 1893. The formula from which column marked "Ratio of cylinder-power to weight available for adhesion" is calculated as follows:

2 × cylinder area × boiler-pressure × stroke

Weight on drivers × diameter of driving-wheel

(Ratio of cylinder-power of compound engines cannot be compared with

that of the single-expansion engines.)

Where the boiler-pressure could not be determined from the description

of the locomotives, as given by the builders and operators of the locomotives, it has been assumed to be 160 lbs, per sq. in. above the atmosphere. For compound locomotives the figures in the last column of ratios are based on the capacity of the low-pressure cylinders only, the volume of the high-pressure being omitted. This has been done for the purpose of comparison, and because there is no accurate simple way of comparing the cylinder-power of single-expansion and compound locomotives.

## Dimensions of Standard Locomotives on the N. Y. C. & H. R. R. and Penna. R. R., 1882 and 1893.

C. H. Quereau, Eng'a News, March 8, 1894.

	N. Y. C. & H. R. R.			Pennsylvania R. R.				
	Through Passenger.		Through Freight,		Through Passenger,		Through Freight.	
	1882.	1893.	1882.	1893.	1882.	1893.	1882.	1893.
Grate surface, sq. ft Heating surface, sq. ft Boiler, diam., in	17.87 1353 50 70	27.3 1821 58 78, 86	17.87 1353 50 64	29.8 1763 58 67	17.6 1057 50 62	33.2 1583 57	23. 1260 54 50	31.5 1498 60 50
Driver, diam., in	$150 \\ 17 \times 24$	180 19×24	$150 \\ 17 \times 24$	$160 \\ 19 \times 26$	$125 \\ 17 \times 24$	78 175 18½×24	$^{125}_{20 \times 24}$	$^{140}_{20 \times 24}$
Valve-travel, ins Lead at full gear, ins Outside lap	51/4 1/16 7/8 0	5½ 1/16 1	1/16	53/4 1/16 7/8 3/32 <i>l</i>	1/16 3/4 0	5½ 0	5 1/8 3/4 1/32 <i>l</i>	5 1/16 3/4 1/32 <i>l</i>
Inside lap or clearance Steam-ports, length width	151/2	11/4	1/16l 151/2 11/4	18 11/4	16		16	16 15/8
Type of engine	Am.	Am.	Am.	Mog.	Am.	Am.	Cons.	Cons.

# Indicated Water Consumption of Single and Compound Locomotive Engines at Varying Speeds,

C. H. Quereau, Eng'a News, March 8, 1894.

0. 1. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0. 0.							
Two-cylinder Compound.			Single-expansion.				
Revolu- tions.	Speed, miles per hour.	Water per I.H.P. per hour.	Revolu- tions.	Miles per Hour.	Water.		
100 to 150 150 " 200 200 " 250 250 " 275	21 to 31 31 " 41 41 " 51 51 " 56	18.33 lbs. 18.9 " 19.7 " 21.4 "	151 219 253 307 321	31 45 52 63 66	21.70 20.91 20.52 20.23 20.01		

It appears that the compound engine is the more economical at low speeds, the economy decreasing as the speed increases, and that the single engine increases in economy with increase of speed within ordinary limits, becoming more economical than the compound at speeds of more than 50 miles per hour.

The C., B. & Q. two-cylinder compound, which was about 30% less economical than the compound of the compound of

nomical than simple engines of the same class when tested in passenger service, has since been shown to be 15% more economical in freight service

than the best single-expansion engine, and 29% more economical than the average record of 40 simple engines of the same class on the same division.

Indicator-tests of a Locomotive at High Speed. (Locomotive Eng'g, June, 1893.)—Cards were taken by Mr. Angus Sinclair on the locomotive drawing the Empire State Express.

RESULTS OF INDICATOR-DIAGRAMS.

Card No.	Revs.	Miles per hour.	I.H.P.	Card No.	Revs.	Miles. I.	H.P.
1	160	37.I	648.3	7	304	70.5	977
2	260	60.8	728	8	296	68.6	972
3	190	44	551	9	300	69.6 1	045
4	250	58	891	10	304	70.5 1	059
5	260	60	960	11	340	78.9 1	120
6	298	69	983	12	310	71.9 1	026

The locomotive was of the eight-wheel type, built by the Schenectady Locomotive Works, with 19 × 24 in, cylinders, 78-in, drivers, and a large boiler and fire-box. Details of important dimensions are as follows: Heating-surface of fire-box, 150.8 sq. ft.; of tubes, 1670.7 sq. ft.; of boiler, 1821.5 sq. ft. Grate area, 27.3 sq. ft. Fire-box: length, 8 ft.; width, 3 ft. 4/5 in. Tubes, 268; outside diameter, 2 in. Ports: steam, 18 × ½ fin.; exhaust, 18 × 23½ in. Valve-travel, 5½ in. Outside lap, 1 in.; inside lap, 1/64 in. The train consisted of four coaches, weighing, with estimated load, 340,000 lbs. The locomotive and tender weighed in working order 200,000 lbs, making the total weight of the train about 270 tons. During the time that the arotice was first lifting the train into speed diagram No. 1 was taken. It

the engine was first lifting the train into speed diagram No. I was taken. It shows a mean cylinder-pressure of 59 lbs. According to this, the power exerted on the rails to move the train is 6553 lbs., or 24 lbs. per ton. The speed is 37 miles an hour. When a speed of nearly 60 miles an hour was reached the average cylinder-pressure is 40.7 lbs., representing a total traction force of 4520 lbs., without making deductions for internal friction. traction force of \$552 fist, without making deductions for internal friction, it leaves 15 lbs, per ton to keep the train going at the speed named. Cards 6, 7, and 8 represent the work of keeping the train running 70 miles an hour. They were taken three miles apart, when the speed was almost uniform. The average cylinder-pressure for the three the speed was almost uniform. The average cylinder-pressure for the three cards is 47.6 bls. Deducting 10% again for friction, this leaves 17.6 bls. per ton as the power exerted in keeping the train up to a velocity of 70 miles. Throughout the trip 7 bls. of water were evaporated per lb. of coal. The work of pulling the train from New York to Albany was done on a coal consumption of about 3½ lbs. per H.P. per hour. The highest power recorded was at the rate of 1120 H.P.

Locomotive-testing Apparatus at the Laboratory of Purdue University. (W. F. M. Goss, Trans. A. S. M. E., vol. xiv. 826)— The locomotive is mounted with its drivers upon supporting wheels which are carried by shafts turning in fixed bearings, thus allowing the engine to be run without changing its position as a whole. Load is supplied by four friction-brakes fitted to the supporting shafts and offering resistance to the turning of the supporting wheels. Traction is measured by a dynamometer attached to the draw-bar. The boiler is fired in the usual way, and an exhaust-blower above the engine, but not in pipe connection with it, carries

off all that may be given out at the stack.

A Standard Method of Conducting Locomotive-tests is given in a report by a Committee of the A. S. M. E. in vol. xiv. of the Transactions, page 1312.

Waste of Fuel in Locomotives.—In American practice economy of fuel is necessarily sacrificed to obtain greater economy due to heavy train-loads. D. L. Barnes, in Eng. Mag., June, 1894, gives a diagram showing the reduction of efficiency of boilers due to high rates of combustion, from which the following figures are taken:

Lbs. of coal per sq. ft. of grate per hour..... 12 80 40 120 160 200 Per cent efficiency of boiler ...... A rate of 12 lbs. is given as representing stationary-boiler practice, 40 lbs.

is English locomotive practice, 120 lbs. average American, and 200 lbs. max-

imum American, locomotive practice. Advantages of Compounding. - Report of a Committee of the American Railway Master Mechanics' Association on Compound Locomotives (Am. Mach., July 3, 1890) gives the following summary of the advantages gained by compounding: (a) It has achieved a saving in the fuel burnt averaging 18% at reasonable boiler pressures, with encouraging possibilities

of further improvement in pressure and in fuel and water economy. (b) It of further improvement in pressure and in their and water economy. (b) that (c) the tender and its load are materially reduced in weight. (d) It has increased the possibilities of speed far beyond 60 miles per hour, without unduly straining the motion, frames, axles, or axle-boxes of the engine. (e) It has increased the continuous H.P. developed, per given weight of engine and boiler. (f) In some classes has increased the starting-power. (g) It has materially lessened the slide-valve friction per H.P. developed. (h) It has equalized or distributed the turning force on the crank-pin, over a longer portion of its path. which, of course, tends to lengthen the repair life of the engine. (i) In the two-cylinder type it has decreased the oil consumption, and has even done so in the Woolf four-cylinder engine. (j) Its smoother and steadler draught on the fire is favorable to the combustion of all kinds of soft coal; and the sparks thrown being smaller and less in number, it lessens the risk to property from destruction by fire. (k) These advantages and economies are gained without having to improve the man handling the engine, less being left to his discretion (or careless indifference) than in the simple engine. (1) Valve-motion, of every locomotive type, can be used in its best working and most effective position. (m) A wider elasticity in locomotive design is permitted: as, if desired, side-rods can be dispensed with, or articulated engines of 100 tons weight, with independent trucks, used for sharp curves on mountain service, as suggested by Mallet and Brunner,

Of 27 compound locomotives in use on the Phila, and Reading Railroad (in 1892, 12 are in use on heavy mountain grades, and are designed to be the equivalent of 22 × 24 in, simple consolidations; 10 are in somewhat lightnesservice and correspond to 20 × 24 in, consolidations; 5 are in fast passenger

service. The monthly coal record shows:

Class of Engine.	No.	Gain in Fuel Economy.
Mountain locomotives	12	25% to 30%
Heavy freight service	10	12% to 17%
Fast passenger	5	9% to 11%

(Report of Com. A. R. M. M. Assn. 1892.) For a description of the various types of compound locomotive, with discussion of their relative merits, see paper by A. Von Borries, of Germany, The Development of the Compound Locomotive, Trans. A. S. M. E. 1893, vol. xiv., p. 1172.

Counterbalancing Locomotives.—The following rules, adopted by different locomotive-builders, are quoted in a paper by Prof. Lanza

(Trans. A. S. M. E., x. 302): A. "For the main drivers, place opposite the crank-pin a weight equal to one half the weight of the back end of the connecting-rod plus one half the one had bee weight of the back end of the connecting-rod, piston, piston-rod, and cross-head. For balancing the coupled wheels, place a weight opposite the earlier pin equal to one half the parallel rod plus one half of the weights of the front end of the main-rod, piston, piston-rod, and cross-head. The centres of gravity of the above weights must be at the same distance from the

axles as the crank-pin."

B. The rule given by D. K. Clark: "Find the separate revolving weights of crank-pin boss, coupling-rods, and connecting-rods for each wheel, also the reciprocating weight of the piston and appendages, and one half the connecting-rod, divide the reciprocating weight equally between each wheel connecting rot, write the reciprocating weight equally between each wheel: the sums thus obtained are the weights to be placed opposite the crank-pin, and at the same distance from the axis. To find the counterweight to be used when the distance of its centre of gravity is known, multiply the above weight by the length of the crank in inches and divide by the given distance." This rule differs from the preceding in that the same weight is placed in each wheel.

C. " $W = \frac{S \times \left(w - \frac{w}{f}\right)}{G}$ , in which S = one half the stroke, G = distance

from centre of wheel to centre of gravity in counterbalance, w = weight at crank-pin to be balanced, W = weight in counterbalance, f = coefficient of friction so called, = 5 in ordinary practice. The reciprocating weight is found by adding together the weights of the piston, piston-rod, cross-head, and one half of the main rod. The revolving weight for the main wheal found by adding together the weights of the crank-pin hub, crank-pin, one half of the main rod, and one half of each parallel-rod connecting to this wheel; to this add the reciprocating weight divided by the number of wheels. The revolving weight for the remainder of the wheels is found in the same manner as for the main wheel, except one half of the main rod is not added. The weight of the crank pin hub and the counterbalance does not include the weight of the spokes, but of the metal inclosing them. This calculation is based for one cylinder and its corresponding wheels."

D. "Ascertain as nearly as possible the weights of crank-pin, additional weight of wheel boss for the same, add side rod, and main connections, piston-rod and head, with cross-head on one side: the sum of these multiplied by the distance in inches of the centre of the crank-pin from the centre of the wheel, and divided by the distance from the centre of the wheel to the common centre of gravity of the counterweights, is taken for the total counterweight for that side of the locomotive which is to be divided among

the wheels on that side."

E. "Balance the wheels of the locomotive with a weight equal to the weights of crank-pin, crank-pin hub, main and parallel rods, brasses, etc., plus two thirds of the weight of the reciprocating parts (cross-head, piston and rod and packing)."

f: "Balance the weights of the revolving parts which are attached to each wheel with exactness, and divide equally two thirds of the weights of the reciprocating parts between all the wheels. One half of the main rod is computed as reciprocating, and the other as revolving weight."

See also articles on Counterbalancing Locomotives, in R. R. & Eng. Jour., March and April, 1890, and a paper by W. F. M. Goss, in Trans. A. S. M. E.,

Maximum Safe Load for Steel Tires on Steel Rails, (A. S. M. E., vii., p. 786.)—Mr. Chantel's experiments led to the deduction that 12,000 lbs, should be the limit of load for any one driving-wheel. Mr. Angus Sinclair objects to Mr. Chantule's figure of 12,000 lbs, and says that a locomotive tire which has a light load on it is more injurious to the rail than one which has a heavy load. In English practice 8 and 10 tons are safely used. Mr. Oberlin Smith has used steel castings for cam-rollers 4 in. diam, and 3 in. face, which stood well under loads of from 10,000 to 20,000 lbs. Mr. C. Shaler Smith proposed a formula for the rolls of a pivot-bridge which may be reduced to the form: Load = 1760 × face × \(\sqrt{\text{diam.}}\), all in lbs, and inches.

See dimensions of some large American locomotives on pages 860 and 861. On the "Decaped" the load on each driving-wheel is 17,000 lbs., and on "No. 999," 21,000 lbs.

Narrow-gauge Railways in Manufacturing Works.—
A tramway of 18 mehes gauge, several miles in length, is in the works of the Lanca-hire and Yorkshire Railway. Curves of 18 feet radius are used. The locomotives used have the following dimensions (Proc. Inst. M. E., July, The locomotives used have the following dimensions (Proc. Inst. M. E.. July, 1888); The cylinders were 5 in, diameter with 6 in, stroke, and 2 ft. 3½ in, centre to centre. The wheels were 16½ in, diameter, the wheel-base 2 ft. 9 in; the frame 7 ft. 4½ in, long, and the extreme width of the engine 3 feet. The boiler, of steel, 2 ft. 3 in, outside diameter and 2 ft. long between tube plates, containing 55 tubes of 13½ in, outside diameter; the fire-box, of iron and cylindrical, 2 ft. 3 in, long and 17 in, inside diameter. The heating surface 10 42 sq. ft. in the fire-box and 36.12 in the tubes, total 46.54 sq. ft.; the grate-area, 1.78 sq. ft.; capacity of tank, 26½ gallons; working-pressure, 170 lbs. per sq. in.; tractive power, say, 1412 lbs., or 9.22 lbs. per lb. of effective pressure per sq. in, on the piston. Weight, when empty, 2.80 tons; when full and in working order, 3.19 tons.

For description of a system of narrow-gauge railways for manufactories, see circular of the C. W. Hunt Co., New York.

Light Locomotives,—For dimensions of light ocomotives used for, mining, etc., and for much valuable information concerning them, see cata-

mining, etc., and for much valuable information concerning them, see catalogue of H K. Potter & Co., Pittsburgh Petroleum-burning Locomotives. (From Clark's Steam-engine.)—The combustion of petroleum refuse in locomotives has been success fully practised by Mr. Thos. Urouhart, on the Grazi and Tsaritsin Railway, Southeast Russia. Since November, 1884, the whole stock of 148 locomotives under his superintendence has been fired with petroleum refuse. The oil is injected from a nozzle through a tubular opening in the back of the fire-box, by means of a jet of steam, with an induced current of air.

A brickwork cavity or "regenerative or accumulative combustion-chamber" is formed in the fire-box, into which the combined current breaks as spray against the rugged brickwork slope. In this arrangement the brickwork is maintained at a white heat, and combustion is complete and smoke-The form, mass, and dimensions of the brickwork are the most important elements in such a combination.

Compressed air was tried instead of steam for injection, but no appreciable

Compressed air was tried instead of steam for injection, outling appreciatole reduction in consumption of fuel was noticed.

The heating-power of petroleum refuse is given as 19,832 heat-units, equivalent to the evaporation of 20,53 lbs. of water from and at 212° F., or to 17.1 lbs. at 8½ atmospheres, or 125 lbs. per sq. in., effective pressure. The highest evaporative duty was 14 lbs. of water under 8½ atmospheres per lb. of the fuel, or nearly 82% efficiency.

There is no probability of any extensive use of petroleum as fuel for locomotives in the United States, on account of the unlimited supply of coal and

the comparatively limited supply of petroleum.

Fireless Locomotive. - The principle of the Francy locomotive is that it depends for the supply of steam on its spontaneous generation from a body of heated water in a reservoir. As steam is generated and drawn off the pressure falls; but by providing a sufficiently large volume of water heated to a high temperature, at a pressure correspondingly high, a margin of surplus pressure may be secured, and means may thus be provided for supplying the required quantity of steam for the trip.

The fireless locomotive designed for the service of the Metropolitan Railway of Paris has a cylindrical reservoir having segmental ends, about 5 ft. 7 in, in diameter, 261/4 ft. in length, with a capacity of about 620 cubic feet. Four fifths of the capacity is occupied by water, which is heated by the aid of a powerful jet of steam supplied from stationary boilers. The water is heated until equilibrium is established between the boilers and the reservoir. The temperature is raised to about 390° F., corresponding to 225 lbs. per sq. in. The steam from the reservoir is passed through a reducing-valve, by which the steam is reduced to the required pressure. It is then passed through a tubular superheater situated within the receiver at the upper part, and thence through the ordinary regulator to the cylinders. The exhaust-steam is expanded to a low pressure, in order to obviate noise of escape. In certain cases the exhaust-steam is condensed in closed vessels, which are only in part filled with water. In the upper free space a pipe is placed, into which the steam is exhausted. Within this pipe another pipe is fixed, perforated, from which cold water is projected into the surrounding steam, so as to effect the condensation as completely as may be. The heated water falls on an inclined plane, and flows off without mixing with the cold water. The condensing water is circulated by means of a

centrifugal pump driven by a small three-cylinder engine.

In working of the steam from a pressure of 225 lbs, to 67 lbs, 530 cubic feet of water at 390° F, is sufficient for the traction of the trains, for working the circulating pump for the condensers, for the brakes, and for electric lighting of the train. At the stations the locomotive takes from 2200 to 3300 lighting of the train. At he same as the weight of steam consumed during the run between two consecutive charging stations. There is 210 cubic feet of condensing water. Taking the initial temperature at 60° F., the tempera-

ture rises to about 180° F, after the longest runs underground. The locomotive has ten wheels, on a base 24 ft. long, of which six are

coupled, 4½ ft. in diameter. The extreme wheels are on radial axles. The cylinders are 23½ in, in diameter, with a stroke of 23½ in.

The engine weighs, in working order, 53 tons, of which 36 tons are on the coupled wheels. The speed varies from 15 miles to 25 miles per hour. The

trains weigh about 140 tons.

Compressed-air Locomotives .- For an account of the Mekarski system of compressed-air locomotives see page 509, ante.

## SHAFTING.

(See also Torsional Strength: also Shafts of Stram-engines.)

For diameters of shafts to resist torsional strains only. Molesworth gives  $d = \sqrt[3]{\frac{Pl}{E}}$ , in which d = diameter in inches, P = twisting force in pounds

applied at the end of a lever-arm whose length is l in inches, K = a coefficient whose values are, for cast iron 1500, wrought iron 1700, cast steel 3200, gun-bronze 460, brass 425, copper 380, tin 220, lead 170. The value given for cast steel probably applies only to high-carbon steel.

Thurston gives:

supported springing:

For head shafts well principles: 
$$\begin{cases} \text{H.P.} = \frac{d^3R}{125}; \ d = \sqrt{\frac{125 \text{ H.P.}}{R}}; \text{ for iron;} \\ \text{H.P.} = \frac{d^3R}{75}; \ d = \sqrt{\frac{75 \text{ H.P.}}{R}}; \text{ for cold-rolled iron.} \end{cases}$$

H.P. = 
$$\frac{d^3R}{75}$$
;  $d = \sqrt{\frac{10 \text{ H.P.}}{R}}$ , for cold-rolled iron.

For line shafting, hangers 8 ft. apart: 
$$\begin{cases} \dot{\mathbf{H}}.\mathbf{P}. = \frac{d^3R}{90}; \ d = \sqrt[3]{\frac{90 \ \mathbf{H}.\mathbf{P}}{R}}, \text{ for iron;} \\ \\ \mathbf{H}.\mathbf{P}. = \frac{d^3R}{55}; \ d = \sqrt[3]{\frac{55 \ \mathbf{H}.\mathbf{P}}{R}}, \text{ for cold-rolled iron.} \end{cases}$$

ply, no pulleys:

For transmission sim-  
ly, no pulleys: 
$$\begin{cases} \text{H.P.} = \frac{d^3R}{62.5}; \ d = \sqrt[3]{\frac{62.5 \text{ H.P.}}{R}}, \text{ for iron;} \\ \text{H.P.} = \frac{d^3R}{35}; \ d = \sqrt[3]{\frac{35 \text{ H.P.}}{R}}, \text{ for cold-rolled iron.} \end{cases}$$

H.P. = horse-power transmitted, d = diameter of shaft in inches, R = revolutions per minute.

J. B. Francis gives for turned-iron shafting  $d = \sqrt[3]{\frac{100 \text{ H.P.}}{D}}$ .

Jones and Laughlins give the same formulæ as Prof. Thurston, with the following exceptions: For line shafting, hangers 8 ft. apart:

cold-rolled iron, H.P. = 
$$\frac{d^3R}{50}$$
,  $d = \sqrt[3]{\frac{50}{R}}$ .

For simply transmitting power and short counters:

turned iron, H.P. = 
$$\frac{d^3R}{50}$$
,  $d = \sqrt[3]{\frac{50 \text{ H.P.}}{R}}$ ; cold-rolled iron, H.P. =  $\frac{d^3R}{20}$ ,  $d = \sqrt[3]{\frac{30 \text{ H.P.}}{R}}$ .

They also give the following notes: Receiving and transmitting pulleys should always be placed as close to bearings as possible; and it is good pracshould always be placed as close to dealing as possible, and it is good in a tice to frame short "headers" between the main tie-beams of a mill so as to support the main receivers, carried by the head shafts, with a bearing close to each side as is contemplated in the formulæ. But fit is preferred, or necessary, for the shaft to span the full width of the "bay" without intermediate bearings, or for the pulley to be placed away from the bearings towards or at the middle of the bay, the size of the shaft must be largely increased to secure the stiffness necessary to support the load without undue deflection. Shafts may not deflect more than 1/80 of an inch to each foot of clear length with safety.

To find the diameter of shaft necessary to carry safely the main pulley at the centre of a bay: Multiply the fourth power of the diameter obtained by above formulæ by the length of the "bay," and divide this product by the distance from centre to centre of the bearings when the shaft is supported as required by the formula. The fourth root of this quotient will be the diameter required.

The foil	owing ta	ble, com	puted by	this ru	le, is pra	etically o	eorrect a	nd safe
neter of the given the For- ilæ for id Shafts.	Dianie	ter of Sh a Bay, w	aft neces	ssary to rom Cen	carry th	e Load a	it the Ce Bearings	ntre of
Dian Sha by Hear	2½ ft.	3 ft.	3½ ft.	4 ft.	5 ft.	6 ft.	8 ft.	10 ft.
in. 2 21/2 3 31/2 4 41/2 5 51/2	in. 2½ 2½ 2½ 3	in. 2½4 25% 3½ 3½ 4	in. 23% 23% 234 314 358 41% 5	in. 21/4 27/4 33/8 33/4 41/4 45/8 51/8	in. 25% 3 31/2 4 41/2 47/8 53/4 63/4	in. 23/4 31/8 33/4 41/4 43/4 51/8 55/8 6	in. 27/8 33/8 4 41/2 51/8 61/6 71/6	in. 3 35/8 41/4 43/4 53/8 61/8 67/8

As the strain upon a shaft from a load upon it is proportional to the product of the parts of the shaft multiplied into each other, therefore, should the load be applied near one end of the span or bay instead of at the centre, multiply the fourth power of the diameter of the shaft required to carry the load at the centre of the span or bay by the product of the two parts of the shaft when the load is near one end, and divide this product by the product of the two parts of the shaft when the load is carried at, the centre. The fourth root of this quotient will be the diameter required.

The shaft in a line which carries a receiving pulley, or which carries a transmitting pulley to drive another line, should always be considered head-shaft, and should be of the size given by the rules for shafts carrying main pulleys or gears.

main puners or galas.

Deflection of Shafting. (Pencoyd Iron Works.)—As the deflection of steel and iron is practically alike under similar conditions of dimensions and loads, and as shafting is usually determined by its transverse stiffness rather than its ultimate strength, nearly the same dimensions should be

used for steel as for iron.

For continuous line-shafting it is considered good practice to limit the deflection to a maximum of 1/100 of an inch per foot of length. The weight of bare shafting in pounds =  $2.6d^2L = W$ , or when as fully loaded with pulleys as is customary in practice, and allowing 40 lbs, per inch of width for the vertical pull of the belts, experience shows the load in pounds to babut 1842 ± W. Taking the modulus of transverse elasticity at 25,000,000 lbs., we derive from authoritative formulæ the following:

$$L = \sqrt[3]{873}d^3, \ d = \sqrt{\frac{L^3}{873}}, \text{ for bare shafting;}$$

$$L = \sqrt[3]{175}d^2, \ d = \sqrt{\frac{L^3}{155}}, \text{ for shafting carrying pulleys,'etc.;}$$

L being the maximum distance in feet between bearings for continuous

shafting subjected to bending stress alone,  $d=\dim$  in linehes. The torsional stress is inversely proportional to the velocity of rotation, while the bending stress will not be reduced in the same ratio. It is therefore impossible to write a formula covering the whole problem and suffi-

ciently simple for practical application, but the following rules are correct

within the range of velocities usual in practice.

For continuous shafting so proportioned as to deflect not more than 1/100 of an inch per foot of length, allowance being made for the weakening effect of key-seats,

$$d=\sqrt[3]{\frac{50\,\mathrm{H.P.}}{R}},\ L=\sqrt[3]{720d^2},\ \mathrm{for\ bare\ shafts};$$
 
$$d=\sqrt[3]{\frac{70\,\mathrm{H.P.}}{R}},\ L=\sqrt[3]{140d^2},\ \mathrm{for\ shafts\ carrying\ pulleys,\ etc.}$$

d= diam, in inches, L= length in feet, R= revs, per min. The following table (by J. B. Francis) gives the subject to no transverse strain except from their own weight, as would be the case were the power given off from the shaft equal on all sides, and at an equal distance from the hanger-bearings.

ı		Bearings, i			Bearings, i	
ı						
1	Diam, of Shaft,	Wrought-iron	Steel	Diam.of Shaft,	Wrought-iron	Steel
ı	in inches.	Shafts.	Shafts.	in inches.	Shafts,	Shafts.
ı	2	15.46	15.89	6	22,30	22.92
ı	3	17.70	18.19	7	23.48	24.13
ı	4	19.48	20.02	8	24.55	25.23
ı	5	20.99	21.57	9	25.53	26.24

These conditions, however, do not usually obtain in the transmission of power by belts and pulleys, and the varying circumstances of each case render it impracticable to give any rule which would be of value for univer-

For example, the theoretical requirements would demand that the bearings be nearer together on those sections of shafting where most power ings be leader together on mose sections of standard where mose power is delivered from the shaft, while considerations as to the location and desired contiguity of the driven machines may render it impracticable to separate the driving-pulleys by the intervention of a hanger at the theoretically required location. (Joshua Rose.)

### Horse-power Transmitted by Turned Iron Shafting at Different Speeds.

AS PRIME MOVER OR HEAD SHAFT CARRYING MAIN DRIVING-PULLEY OR GEAR. WELL SUPPORTED BY BEARINGS. Formula: H.P. =  $d^3R + 125$ .

ft.n		Number of Revolutions per Minute.									
Diam. of Shaft.	60	80	100	125	150	175	200	225	250	275	300
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.
	2.6	3.4	4.3	5.4	6.4	7.5	8.6	9.7	10.7	11.8	12.9
134 2 214	3.8	5.1 7.3	6.4 8.1	8	9.6 12	11.2 14	12.8 16	14.4 18	16 20	17.6 22	19.2
21/2 23/4 3	7.5 10	10 13	12.5 16	15 20	18 24	22 28	25 32	28 36	31 40	34 44	37 48
31/4	13	17	20	25	30	35	40	45	50	55	60
	16	22	27	34	40	47	54	61	67	74	81
31/2	20	27	34	42	51	59	68	76	85	93	102
33/4	25	33	42	52	63	73	84	94	105	115	126
4 41/2	30	41	51	64	76	89	102	115	127	140	153
	43	58	72	90	108	126	144	162	180	198	216
5	60	80	100	125	150	175	200	225	250	275	300
5½	80	106	133	166	199	233	266	299	333	366	400

As Second Movers or Line-shafting, Bearings 8 ft. apart. Formula; H.P. =  $d^3R + 90$ .

ft.	Number of Revolutions per Minute.										
Diam of Shaft	100	125	150	175	200	225	250	275	300	325	350
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.
13/4	6	7.4	8.9	10.4	11.9	13.4	14.9	16.4	17.9	19.4	20.9
1%	7.3	9.1	10.9	12.7	14.5	16.3	18.2	20	21.8	23.6	25.4
2	8.9	11.1	13.3	15.5	17.7	20	22.2	24.4	26.6	28.8	31
1% 17% 21/8 21/4 23/4 23/4 23/4 33/4	10.6	13.2	15.9	18.5	21.2	23.8	26.5	29.1	31.8	34.4	37
21/4	12.6	15.8	19	22	25	28	31	35	38	41	44
23/2	15	18	22	26	29	33	37	41	44	48	52
21/6	17	21	26	30	34	39	43	47	52	56	60
23%	23	29	34	40	46	52	58	64	69	75	81
3	30	37	45	52	60	67	75	82	90	97	105
31/4	38	47	57	66	76	85	95	104	114	123	133
31/4 31/2 33/4	47	59	71	83	95	107	119	131	143	155	167
33%	58	73	88	102	117	132	146	162	176	190	205
4	71	89	107	125	142	160	178	196	213	231	249

For Simply Transmitting Power. Formula: H.P. =  $d^3R \div 50$ .

Formula: H.P. = $a^3R \div 50$ .												
ft.		Number of Revolutions per Minute.										
Diam. of Shaft.	100	125	150	175	200	233	267	300	332	367	400	
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	
	6.7	8.4	10.1	11.8		15.7	17.9	20.3	22.5	24.8	27.0	
11/2 15/8	8.6	10.7	12.8		17.1	20	22.8	25.8	28.6	31.5	34.9	
134 178 2 218	10.7	13.4	16	18.7	21.5	25	28	32	36	39	43	
17/8	13.2	16.5	19.7	23	26.4	31	35	39	44	48	52	
2	16	20	24	28	32	37	42	48	53	58	64	
21/8	19	24	29	33	38	44	51	57	63	70	76	
21/4	22	28	34	39	45	52	60	68	75	83	90	
23/8	27	33	40	47	53	62	70	79	88	96	105	
21/2	31	39	47	54	62	73	83	93	104	114	125	
23/4	41	52	62	73	83	97	111	125	139	153	167	
3	54	67	81	94	108	126	144	162	180	198	216	
31/4	68	86	103	120	137	160	182	205	228	250	273	
31/2	85	107	128	150	171	200	228	257	285	313	342	

# Horse-power Transmitted by Cold-rolled Iron Shafting at Different Speeds.

As Prime Mover or Head Shaft carrying Main Driving-pulley or Gear, well supported by Bearings. Formula : H.P. =  $d^3R + 75$ .

e. ±	Number of Revolutions per Minute.										
Diam. of Shaft.	60	80	100	125	150	175	200	225	250	275	300
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.
11/6	2.7	3.6	4.5	5.6	6.7	7.9	9.0	10	11	12	13
11/2 13/4	4.3	5.6	7.1	8.9	10.6	12.4	14.2	16	18	19	21 32
21/4 21/4 21/2 23/4 3	6.4	8.5	10.7	13	16	19	21	24	26 38	29	32
21/4	9	12	15	19	23	26	30	34	38	42	46
21/6	12	17	21	26	31	36	41	47	52	57	62
234	16	22	27	35	41	48	55	62	70	76	82
3 *	21	29	36	45	54	63	72	81	90	98	108
31/4	27	36	45	57	68	80	91	103	114	126	136
31/2 33/4	34	45	57	71	86	100	114	129	142	157	172
33%	42	56	70	87	105	123	140	158	174	193	210
4	51	69	85	106	128	149	170	192 -	212	244	256
41/2	73	97	121	151	182	212	243	273	302	333	364

As Second Movers or Line-shafting, Bearings 8 ft. apart.

Formula: H.P. =  $d^3R + 50$ .

Number of Revolutions per Minute.								
325	350							
H.P.	H.P.							
28.9	23.6							
42.8	39 46							
62	56 67							
86	80 94							
135	109 145							
222	189 240 300							
	H.P. 21.9 28.9 34.8 42.8 52 62 74 86 101 135 175							

FOR SIMPLY TRANSMITTING POWER AND SHORT COUNTERS.

Formula: H.P. =  $d^3R + 30$ .

if "i			N	umber	of Re	volutio	ns per	Minut	e.		
Diam. of Shaft.	100	125	150	175	200	233	267	300	,333	367	400
Ins.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.	H.P.
	6.5	8.1	9.7	11.3	13	15.2	17.4	19.5	21.7	23.9	26
18%	8.5	10.7	12.8	15	17	19.8	22.7	25.5	28.4	31	34
	11.2	14	16.8	19.6	22.5	26	30	33	37	41	45
11/4 18/8 11/6 15/8 13/4 17/8	14.2	17.7	21.2 27		28.4 35	33 41	38 47	42 53	47 59	52 65	57 71
17/8	22	27	33	38	44	51	58	65	72	79	87
	26	33	40	46	53	62	71	80	88	97	106
21/8	32	40	47	55	63	73	84	95	105	116	127
	38	47	57	66	76	89	101	114	127	139	152
21/8 21/4 23/6 21/2 23/4	44 52	55 65	66 78	77 91	88 104	103 121	118 138	133	148 172	163 190	178 207
23/4	69	84	99	113	138	161	184	207	231	254	277
	90	112	135	157	180	210	240	270	300	330	360
	100	1~		201	1 200	7-10		~.0	000	550	000

 Wood-working
 250 to 300

 Cotton and woollen mills
 300 to 400

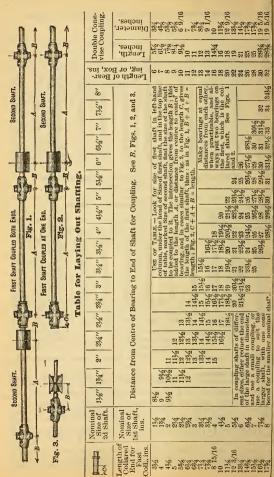
There are in some factories lines 1000 ft. long, the power being applied at the middle.

**Hollow Shafts.**—Let d be the diameter of a solid shaft, and  $d_1d_2$  the external and internal diameters of a hollow shaft of the same material Then the shafts will be of equal torsional strength when  $d^3 = \frac{d_1^4 - d_2^4}{d_1^4 - d_2^4}$ 

Then the shafts will be of equal torsional strength when  $d^3 = \frac{c_1 - c_2}{d}$ . A 10-inch hollow shaft with internal diameter of 4 inches will weigh 16% less than a solid 10-inch shaft, b at its strength will be only 2.56% less. If the hole were increased to 5 inches diameter the weight would be 23% less than that of the solid shaft, and the strength 4.25% less.

Table for Laying Out Shafting.—The table on the opposite page from the Steens Indicated 1.1892) is used by Wm. Sellers & Co. to fall the strength of Shafting 1.1892 is used by Wm. Sellers & Co. to fall wood-cuts at the head of this table show the position of the hangers and position of containings, either for the case of extension in both dimensions.

and position of couplings, either for the case of extension in both directions from a central head-shaft or extension in one direction from that head-shaft.



## PULLEYS.

Proportions of Pulleys, (See also Fly-wheels, pages 820 to 823.)-Let n = number of arms, D = diameter of pulley, S = thickness of belt, t = hickness of rim at edge, T = thickness in middle, B = width of rim,  $\beta =$ vidth of belt, h = breadth of arm at hub,  $h_1 =$  breadth of arm at rim, e =hickness of arm at hub  $e_1$  = thickness of arm at rim, c = amount of crownng: dimensions in inches.

The number of arms is really arbitrary, and may be altered if necessary.

Pulleys with two or three sets of arms may be considered as two or three separate pulleys combined in one, except that the proportions of the arms should be 0.8 or 0.7 time that of single-arm pulleys. (Reuleaux.)

Example.—Dimensions of a pulley 60" diam., 16" face, for double belt 1/2" thick.

Solution by... 
$$n$$
  $h$   $h_1$   $e$   $e_1$   $t$   $T$   $L$   $M$   $c$  Unwin....  $9$  3.79 2.53 1.52 1.01 .65 1.97 10.7 3.8 .67

Reuleaux . . . 4 5.0 4.0 2.5 2.0 1.25 16 5

The following proportions are given in an article in the Amer. Machinist, authority not stated:

 $h = .0625D + .5 \text{ in.}, h_1 = .04D + 3125 \text{ in.}, e = .025D + .2 \text{ in.}, e_1 = .016D + .2 \text{ in.}$ 125 in.

These give for the above example: h = 4.25 in.,  $h_1 = 2.71$  in., e = 1.7 in., = 1.09 in. The section of the arms in all cases is taken as elliptical.  $e_1=1.09$  in. The section of the arms in all cases is taken as empirear. The following solution for breadth of arm is proposed by the author: Assume a belt pull of 45 lbs, per inch of width of a single belt, that the whole strain is taken in equal proportions on one half of the arms, and that the arm is a beam loaded at one end and fixed at the other. We have the

formula for a beam of elliptical section  $fP = .0982 \frac{Rbd^2}{l}$ , in which P = the

load, R= the modulus of rupture of the cast iron, b= breadth, d= depth, and l= length of the beam, and f= factor of safety. Assume a modulus of rupture of 86,000 lbs., a factor of safety of 10, and an additional allowance for safety in taking  $l=\frac{1}{2}$  the diameter of the pulley instead of  $\frac{1}{2}D$ less the radius of the hub. Take d=h, the breadth of the arm at the hub, and b=e=0.4h, the thickness. We then have  $fP=10\times\frac{45B}{n+2}=900\frac{B}{n}=\frac{3535\times0.4h^2}{\frac{1}{2}6D}$ , whence

 $h = \sqrt[3]{\frac{900BD}{3535n}} = .633\sqrt[3]{\frac{BD}{n}}$ , which is practically the same as the value

reached by Unwin from a different set of assumptions.

Convexity of Pulleys .- Authorities differ. Morin gives a rise equal to 1/10 of the face; Molesworth, 1/24; others from 1/2 to 1/96. Scott A. Smith says the crown should not be over 1/2 inch for a 24-inch face. Pulleys for shifting belts should be "straight," that is, without crowning,

#### CONE OR STEP PULLEYS.

To find the diameters for the several steps of a pair of cone-pulleys:

1. Crossed Belts.—Let D and d be the diameters of two pulleys connected by a crossed belt, L = the distance between their centres, and  $\beta =$ the angle either half of the belt makes with a line joining the centres of the pulleys: then total length of belt =  $(D+d)\frac{\pi}{2} + (D+d)\frac{\pi\beta}{180} + 2L \cos \beta$ .

$$\beta = \text{angle whose sine is } \frac{D+d}{2L}$$
.  $\cos \beta = \sqrt{\frac{L^2 - \left(\frac{D+d}{2}\right)}{L^2}}$ . The length of

the belt is constant when D+d is constant; that is, in a pair of step-pulleys the belt tension will be uniform when the sum of the diameters of each opposite pair of steps is constant. Crossed belts are seldom used for cone-pulleys, on account of the friction between the rubbing parts of the

To design a pair of tapering speed-cones, so that the belt may fit equally tight in all positions: When the belt is crossed, use a pair of equal

and similar cones tapering opposite ways.

2. Open Belts.—When the belt is uncrossed, use a pair of equal and similar conoids tapering opposite ways, and bulging in the middle, according to the following formula: Let \( L\) denote the distance between the axes of the conoids; \( R\) the radius of the larger end of each; \( r\) the radius of the smaller end; then the radius in the middle, \( r\_0\), is found as follows;

$$r_0 = \frac{R+r}{2} + \frac{(R-r)^2}{6.28L}$$
. (Rankine.)

If  $D_0$  = the diameter of equal steps of a pair of cone-pulleys, D and d = the diameters of unequal opposite steps, and L = distance between the axes,  $D_0 = \frac{D+d}{2} + \frac{(D-d)^2}{12.566L}$ . If a series of differences of radii of the steps, R-r, be assumed, then for each pair of steps  $\frac{R+r}{2} = r_0 - \frac{(R-r)^2}{6.32L}$ , and the radii of each may be computed from their half sum and half difference, as follows:

$$R = \frac{R+r}{2} + \frac{R-r}{2}; \quad r = \frac{R+r}{2} - \frac{R-r}{2}.$$

A. J. Frith (Trans. A. S. M. E., x. 298) shows the following application of Rankine's method: If we had a set of cones to design, the extreme diameters of which, including thickness of belt, were 40" and 10", and the ratio desired 4, 3, 2, and 1, we would make a table as follows, L being 100":

Trial Sum of	Ratio.	Trial Dia	ameters.	Values of $(D-d)^2$	Amount to be	Corrected	d Values.
D+d.	Italio.	D	d	12.56L.	Added.	D	d
50 50	3	40 37.5	10 12.5	.7165 .4975	.0000	40 37.2190	10 12.2190
50 50	2	33.333 25	16.666 25	.2212	.4953 .7165	33.8286 25.7165	17.8286 25.7165

The above formulæ are approximate, and they do not give satisfactory results when the difference of diameters of opposite steps is large and when

results when the difference of diameters or opposite steps is large and when the axes of the pulleys are near together, giving a large belt-angle. The following more accurate solution of the problem is given by C. A. Smith (Trans. A. S. M. E., x. 299) (Fig 152). Lay off the centre distance C or EF, and draw the circles  $D_1$  and  $d_1$  equal to the first pair of pulleys, which are always previously determined by known conditions. Draw HI tangent to the circles  $D_1$  and  $d_2$ . From  $B_1$  mildway between E and F, erect the perpendicular BG, making the length

BG = .314C. With G as a centre, draw a circle tangent to HI. Generally this circle will be outside of the belt-line, as in the cut, but when C is short and the first pulleys  $D_1$  and  $d_1$  are large, it will fall on the inside of the belt-line. The belt-line of any other pair of pulleys must be tangent to the circle  $G_2$ ; hence any line, as JK or LM, drawn tangent to the circle  $G_2$ ; will give

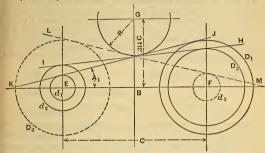


Fig. 152.

the diameters  $D_2$ ,  $d_2$  or  $D_3$ ,  $d_3$  of the pulleys drawn tangent to these lines from the centres E and F.

The above method is to be used when the belt-angle A does not exceed.

When it is between 18° and 30° a slight modification is made. In that case, in addition to the point G, locate another point m on the line BG. 298 C above B. Draw a tangent line to the circle G, making an angle of 18° to the line of centres EF, and from the point m draw an arc tangent to this tangent line. All belt-lines with angles greater than 18° are tangent to this arc. The following is the summary of Mr. Smith's mathematical method:

 $A \equiv$  angle in degrees between the centre line and the belt of any pair of pulleys:

a = .314 for belt-angles less than 18°, and .298 for angles between 18°

 $B^{\circ} \stackrel{!}{=}$  an angle depending on the velocity ratio;

C = the centre distance of the two pulleys; D, d = diameters of the larger and smaller of the pair of pulleys;

 $E^{\circ} =$  an angle depending on  $B^{\circ}$ ;

L = the length of the belt when drawn tight around the pulleys; r = D + d, or the velocity ratio (larger divided by smaller).

(1) Sin 
$$A = \frac{D-d}{2C}$$
; (2)  $\tan B^{\circ} = \frac{2a(r-1)}{r+1}$ ;  
(3) Sin  $E^{\circ} = \sin B^{\circ} \left(\cos A - \frac{D+d}{4aC}\right)$ ;

(4)  $A = B^{\circ} - E^{\circ}$  when sin  $E^{\circ}$  is positive;  $= B^{\circ} + E^{\circ}$  when sin  $E^{\circ}$  is negative;

(5) 
$$d = \frac{2C \sin A}{r-1}$$
; = .3183(L - 2C) when  $A = 0$  and  $r = 1$ ;

(6) D = rd;

(7)  $L = 2C \cos A + .01745d[180 + (r - 1)(90 + A)].$ 

Equation (1) is used only once for any pair of cones to obtain the constant  $\cos A$ , by the aid of tables of sines and cosines, for use in equation (3).

### BELTING.

Theory of Belts and Bands.—A pulley is driven by a belt by means of the friction between the surfaces in contact. Let  $T_i$  be the tension on the driving side of the belt,  $T_i$  the tension on the droving side of the belt,  $T_i$  the tension on the loose side; then  $S_i = T_i$ ,  $T_j$ , is the total friction between the band and the pulley, which is equal to the tractive or driving force. Let f = the coefficient of friction,  $\theta$  the ratio of the length of the arc of contact to the length of the radius, a = the angle of the arc of contact in degrees, e = the base of the Naperian logarithms = 2.71828, m = the modulus of the common logarithms = 0.434295. The following formulæ are derived by calculus (Rankine's Mach'y & Millwork, p. 351; Carpenter's Exper. Eng'g, p. 173):

$$\begin{split} \frac{T_1}{T_2} &= e^{f\theta}; \ T_2 = \frac{T_1}{e^{f\theta}}; \ T_1 - T_2 = T_1 - \frac{T_1}{e^{f\theta}} = T_1(1 - e^{-f\theta}), \\ T_1 - T_2 &= T_1(1 - e^{-f\theta}) = T_1(1 - 10^{-f\theta m}) = T_1(1 - 10^{-00758fa}); \\ \frac{T_1}{T_2} &= 10^{\cdot 00758fa}; \ T_1 = T_2 \times 10^{\cdot 00758fa}; \ T_2 = \frac{T_1}{10^{\cdot 00758fa}}. \end{split}$$

If the arc of contact between the band and the pulley expressed in turns and fractions of a turn = n,  $\theta = 2\pi n$ ;  $e^{j\theta} = 10^{2.7285/n}$ , that is,  $e^{j\theta}$  is the natural number corresponding to the common logarithm 2.7288fn.

natural number corresponding to the common logarithm 2.7285/n. The value of the coefficient of friction f depends on the state and material of the rubbing surfaces. For leather belts on iron pulleys, Morin found f=.56 when dry, 36 when wet. 32 when greasy, and 15 when oily, I calculating the proper mean tension for a belt, the smallest value, f=.15, is to be taken if there is a probability of the belt becoming wet with oil. The experiments of Henry R. Towne and Robert Briggs, however (Jour, Frank. Inst., 1868), show that such a state of lubrication is not of ordinary occurrence; and that in designing machinery we may in most cases safely take f=0.42. Reuleaux takes f=0.55. The following table shows the values of the coefficient 2.7285f, by which n is multiplied in the last equation, corresponding to different values of f; also the corresponding values of various ratios among the forces, when the arc of contact is half a circumference:

2.7288f = 0.41	0.68	0.15	1.53
Let $\theta = \pi$ and $n = \frac{1}{2}$ , then			
$T_1 \div T_2 = 1 608$	2.188	3.758	5.821
$T_1 + S = 2.66$	1 84	1.86	1.21
$T_1 + T_2 \div 2S = 2.16$	1.34	0.86	0.71

In ordinary practice it is usual to assume  $T_2=2S$ ;  $T_1=2S$ ;  $T_1+T_2+2S=1.5$ . This corresponds to f=0.22 nearly. For a wire rope on cast fron f may be taken as 0.15 nearly; and if the groove of the pulley is bottomed with gutta percha, 0.25. (Kankine) Centrifugal Tension of Belts.—When a belt or band runs at a

high velocity, centrifugal force produces a tension in addition to that exist-ing when the belt is at rest or moving at a low velocity. This centrifugal tension diminishes the effective driving force. Rankine says: If an endless band, of any figure whatsoever, runs at a

namine says: If an entires band, or any figure matsoever, runs at a given speed, the centrifugal force produces a uniform tension at each cross-section of the band, equal to the weight of a piece of the band whose length is twice the height from which a heavy body must fall, in order to acquire the velocity of the band. (See Cooper on Belting, p. 101.)

If To = centrifugal tension;

V = velocity in feet per second;

g = acceleration due to gravity = 32.2; W = weight of a piece of the belt 1 ft. long and 1 sq. in. sectional area,—

Leather weighing 56 lbs. per cubic foot gives  $W = 56 \div 144 = .388$ .

$$To = \frac{WV^2}{g} = \frac{.388V^2}{32,2} = .012V^2$$

Belting Practice. Handy Formulæ for Belting. - Since in the practical application of the above formulæ the value of the coefficient of friction must be assumed, its actual value varying within wide limits (15% to 135%), and since the values of  $T_1$  and  $T_2$  also are fixed arbitrarily, it is customary in practice to substitute for these theoretical formulæ more simple empirical formulæ and rules, some of which are given below.

Let d= diam, of pulley in inches;  $\pi d=$  circumference; V= velocity of belt in ft. per second; v= vel. in ft. per minute; a= angle of the arc of contact. L= length of arc of contact in feet  $=\pi dn+(12\times360)$ ; F= treative force per square inch of sectional area of belt; w= width in inches;  $\ell=$  thickness; S= treative force per inch of width =F+t;

rpm. = revs. per minute: rps. = revs. per second = rpm.  $\div$  60.

$$\begin{split} V &= \frac{\pi d}{12} \times \text{rps.} = \frac{\pi d}{12} \times \frac{\text{rpm.}}{60} = .004363d \times \text{rpm.} = \frac{d \times \text{rpm.}}{229.2}; \\ v &= \frac{\pi d}{12} \times \text{rpm.}; = .2618d \times \text{rpm.} \end{split}$$

Horse-power, H.P. =  $\frac{Svw}{33000} = \frac{SVw}{550} = \frac{Swd \times rpm}{126050} = .000007933Swd \times rpm$ .

If F = working tension per square inch = 275 lbs., and t = 7/32 inch, S =60 lbs. nearly, then

H.P. 
$$=\frac{vw}{550} = .109Vw = .000476wd \times \text{rpm.} = \frac{wd \times \text{rpm.}}{2101}$$
. (1

If F = 180 lbs, per square inch, and t = 1/6 inch, S = 30 lbs., then

H.P. = 
$$\frac{vw}{1100}$$
 = .055  $Vw$  = .000238 $wd \times \text{rpm.}$  =  $\frac{vd \times \text{rpm.}}{4202}$ . . (2)

If the working strain is 60 lbs, per inch of width, a belt 1 inch wide travelling 550 ft, per minute will transmit 1 horse-power. If the working strain is 30 lbs. per inch of width, a belt 1 inch wide, travelling 1100 ft. per minute, will transmit 1 horse-power. Numerous rules are given by different writers on belting which vary between these extremes. A rule commonly used is: 1 inch wide travelling 1000 ft. per min. = I.H.P.

H.P. = 
$$\frac{vw}{1000}$$
 = .06 $Vw$  = .000262 $wd \times \text{rpm.}$  =  $\frac{wd \times \text{rpm.}}{3820}$ . . . . (3)

This corresponds to a working strain of 33 lbs. per inch of width. Many writers give as safe practice for single belts in good condition a working tension of 45 lbs. per inch of width. This gives

H.P. = 
$$\frac{wv}{733}$$
 = .0818 $Vw$  = .000357 $wd \times \text{rpm}$ , =  $\frac{wd \times \text{rpm}}{2800}$  . (4)

For double belts of average thickness, some writers say that the transmitting efficiency is to that of single belts as 10 to 7, which would give

H.P. of double belts = 
$$\frac{wv}{513}$$
 = .1169  $Vw$  = .00051  $wd \times \text{rpm.}$  =  $\frac{wd \times \text{rpm.}}{1960}$ . (5)

Other authorities, however, make the transmitting-power of double belts twice that of single belts, on the assumption that the thickness of a doublebelt is twice that of a single belt.

Rules for horse-power of belts are sometimes based on the number of

square feet of surface of the belt which pass over the pulley in a minute, Sq. ft. per min. = vv + 12. The above formulæ translated into this form

- For S=60 lbs. per inch wide ; H.P. = 46 sq. ft. per minute, " S=30 " " H.P. = 93 " " " S=30 " " " H.P. = 83 " " " S=30 " " " H.P. = 81 " " " " S=45 " " " H.P. = 61 " " " (double belt).

The above formulæ are all based on the supposition that the arc of contact is 180° For other arcs, the transmitting power is approximately pro-

tact is 180°. For other arcs, the transmitting power is approximately proportional to the ratio of the degrees of arc to 180°. Some rules base the horse-power on the length of the arc of contact in feet. Since  $L = \frac{\pi da}{12 \times 360}$  and H. P.  $= \frac{8 \text{rw}}{33000} = \frac{8 \text{Jw}}{33000} \times \frac{\pi d}{12} \times \text{rpm.} \times \frac{\pi}{180}$ , we

obtain by substitution H.P. =  $\frac{Sw}{16500} \times L \times \text{rpm.}$ , and the five formulæ then take the following form for the several values of S:

$$\begin{aligned} \mathbf{H.P} &= \frac{wL \times \mathbf{rpm.}}{275} \text{ (1); } \frac{wL \times \mathbf{rpm.}}{550} \text{ (2); } \frac{wL \times \mathbf{rpm.}}{500} \text{ (3); } \frac{wL \times \mathbf{rpm.}}{367} \text{ (4);} \\ \mathbf{H.P.} \text{ (double belt)} &= \frac{wL \times \mathbf{rpm.}}{987} \text{ (5).} \end{aligned}$$

None of the handy formulæ take into consideration the centrifugal tension of belts at high velocities. When the velocity is over 3000 ft. per minute the effect of this tension becomes appreciable, and it should be taken account of as in Mr. Nagle's formula, which is given below.

## Horse-power of a Leather Belt One Inch wide. (NAGLE.)

Formula: H.P. =  $CVtw(S - .012V^2) \div 550$ .

For 
$$f = 40$$
,  $a = 180^{\circ}$ ,  $C = .715$ ,  $w = 1$ .

	L	CED	BEL	TS, S	l = 2	75.		RIVETED BELTS, $S = 400$ .							
ty in	Thickness in inches = $t$ .								$ \begin{array}{c c} \exists \phi \\ \geq 0 \\ \hline \end{array} $ Thickness in inches = t.						
Velocity ft. per s	1/7 .143			7/32 .219				Velocity ft. per s	7/32 219	1/4 .250		1/3 .333	3/8 .375	7/16 .437	1/2
10 15 20 25 30 35 40 45 50 55	1.47 1.69 1.90 2.09 2.27	1.17 1.43 1.72 1.97 2.22 2.45 2.65	1.00 1.82 1.61 1.93 2.22 2.49 2.75 2.98	.73 1.16 1.54 1.88 2.25 2.59 2.90 3.21 3.48 3.72	1.32 1.75 2.16 2.58 2.96 3.32 3.67 3.98	2.19 2.69 3.22 3.70 4.15 4.58 4.97	1.77 2.34 2.86 3.44 3.94 4.44 4.89 5.30	20 25 30 35 40 45 50 55	2.24 2.79 3.31 3.82 4.33 4.85 5.26 5.68	3.19 3.79 4.37 4.95 5.49	5.46 6.19 6.86 7.51 8.12	3.42 4.25 5.05 5.83 6.60 7.32 8.02 8.66	5.85 4.78 5.67 6.56 7.42 8.43 9.02 9.74	5.57 6.62 7.65 8.66	9 90 10.98 12.03 13.00
60 65 70 75 80 85 90	2.58 2.71 2.81 2.89 2.94 2.97 2.97	3.01 3.16 3.27 3.37 3.43 3.47 3.47	3.38 3.55 3.68 3.79 3.86 3.90 3.90	3.95 4.14 4.29 4.42 4.50 4.55 4.55	4.51 4.74 4.91 5.05 5.15 5.20 5.20	5.64 5.92 6.14 6.31 6.44 6.50 6.50	6.02 6.32 6.54 6.73 6.86 6.93 6.93	65 70 75 80 85 90 100	6.45 6.78 7.09 7.36 7.58 7.74 7.96	7.37 7.75 8.11 8.41 8.66 8.85 9.10	9.22 9 69 10.13 10 51 10.82 11.06 11.37	9.88 10.83 10.84 11.21 11.55 11.80 12.13	11.06 11.62 12.16 12.61 13.00 13.27 13.65	12.90 13.56 14.18 14.71 15.16 15.48 15.92	14.75 15.50 16.21 16.81 17.32 17.69 18.20
				es a										ximu er mi	

In the above table the angle of subtension, a, is taken at 180°.

A. F. Nagle's Formula (Trans. A. S. M. E., vol. ii., 1881, p. 91. Tables published in 1882.)

H.P. = 
$$CVtw\Big(\frac{S - 0.012V^2}{550}\Big);$$

 $C = 1 - 10^{-.00758fa}$ ;

a =degrees of belt contact; f = coefficient of friction;

w = width in inches;

t= thickness in inches; V= velocity in feet per second;  $S=T_1-T_2=$  stress upon belt per

square inch.

Taking S at 275 lbs, per sq. in. for laced belts and 400 lbs, per sq in. for lapped and riveted belts, the formula becomes

 $H.P. = CVtw(.50 - .0000218V^2)$  for laced belts;

 $H.P. = CVtw(.727 - .0000218V^2)$  for riveted belts.

Values of 
$$C = 1 - 10^{-.00758fa}$$
. (Nagle.)

coeffi- ent of ction.	Degrees of contact = $a$ .											
$f = \cos t$	90°	100°	110°	120°	130°	140°	150°	160°	170°	180°	200°	
.15	.210	.230	.250	.270	.288	.307	.325	.342	.359	.376	.408	
.20 .25 .30	.270 .325 .376	.295 .354 .408	.319 .581 .438	.407	.432	.520	.480	.503	.524	.467 .544 .610	.503 .582 .649	
.35 .40	.423	.457	.489	.520	.548	.575	.600	.624	.646	.667	.705	
.45	.507	.544	.579 .652	.610 .684	.640 .713	.667 .739	.692	.715 .785	.737	.757 .822	.792 .853	
.60 1.00	.610 .792	.649 .825	.684 .853	.715 .877	.744 .897	.769 .913	.792	.813 .937	.832 .947	.848 .956	.877 .969	

The following table gives a comparison of the formulæ already given for the case of a belt one inch wide, with arc of contact 180°.

## Horse-power of a Belt One Inch wide, Arc of Contact 180°.

ity in r sec.	ity in min.	ft, of o. min.	Form. 1 H.P. =		Form. 3 H.P. =	Form. 4 H.P. =	Form. 5 dbl.belt H.P. =	Nagle' 7/32"sir	s Form.
Velocity ft. per se	Velocity ft. p. m	Sq. f	$\frac{wv}{550}$ .	$\frac{wv}{1100}$ .	$\frac{wv}{1000}$ .	$\frac{wv}{733}$ .	$\frac{wv}{513}$	Laced.	Riveted
10	600	50	1.09	.55	.60	.82	1.17	.73	1.14
20	1200	100	2.18	1.09	1.20	1.64	2.34	1.54	2.24
30	1800	150	3.27	1.64	1.80	2.46	3.51	2.25	3.31
40	2400	200	4.36	2.18	2.40	3.27	4.68	2.90	4.33
50	3000	250	5.45	2.73	3.00	4.09	5.85	3.48	5.26
60	3600	300	6.55	3.27	3.60	4.91	7.02	3.95	6.09
70	4200	350	7.63	3.82	4.20	5.73	8.19	4.29	6.78
80	4800	400	8.73	4.36	4.80	6.55	9.36	4.50	7.36
90	5400	450	9.82	4.91	5.40	7.37	10.53	4.55	7.74
100	6000	500	10.91	5.45	6.00	8.18	11.70	4.41	7.96
110	6600	550						4.05	7.97
120	7200	600	1	1	1	J		3.49	7.75

width of Belt for a Given Horse-power.—The width of belt required for any given horse-power may be obtained by transposing the formulæ for horse-power so as to give the value of w. Thus:

\* For double belts.

Many authorities use formula (1) for double belts and formula (2) or (3) for single belts.

To obtain the width by Nagle's formula,  $w = \frac{300 \text{ H.I.}}{CVt(S - .012V^2)}$ , or divide the given horse-power by the figure in the table corresponding to the given

thickness of belt and velocity in feet per second

The formula to be used in any particular case is largely a fight property of the property of the property of the formula (1), if tightly stretched, and if the surface is in good condition, will transmit the horse-power calculated by the formula, but one so proportioned is objectionable, first, because it requires so great an initial tension that it is apt to stretch, slip, and require frequent restretching and relacing; and second, stretch, sip, and require frequent restretching and relating; and second, because this tension will cause an undue pressure on the pulley-shaft, and therefore an undue loss of power by friction. To avoid these difficulties, formula (2), (3), or (4,) or Mr. Nagle's table, should be used; the lattre especially in cases in which the velocity exceeds 4000 ft. per min.

Taylor's Rules for Belting.-F. W. Taylor (Trans. A. S. M. E., xv. 234) describes a nine years' experiment on belting in a machine-shop, giving results of tests of 42 belts running night and day. Some of these

belts were run on cone pulleys and others on shifting, or fast-and-loose, pulleys. The average net working load on the shifting belts wasonly 4/10 of

that of the cone belts.

The shifting belts varied in dimensions from 39 ft. 7 in. long, 3.5 in. wide, .25 in. thick, to 51 ft. 5 in. long, 6.5 in. wide, .37 in. thick. The cone belts varied in dimensions from 24 ft. 7 in. long, 2 in. wide, .25 in. thick, to 31 ft.

10 in. long, 4 in. wide, .37 in. thick.

Belt-clamps were used having spring-balances between the two pairs of clamps, so that the exact tension to which the belt was subjected was accurately weighed when the belt was first put on, and each time it was tightened.

The tension under which each belt was spliced was carefully figured so as to place it under an initial strain-while the belt was at rest immediately after tightening-of 71 lbs. per inch of width of double belts. This is equiv-

alent, in the case of

Oak tanned and fulled belts, to 192 lbs. per sq. in. section; Oak tanned, not fulled belts, to 229 " " " " " Semi-raw-hide belts, to 253 " " " " Semi-raw-hide belts, .. to 284 " 44 66 Raw-hide belts,

From the nine years' experiment Mr. Taylor draws a number of conclusions, some of which are given in an abridged form below.

In using belting so as to obtain the greatest economy and the most satisfactory results, the following rules should be observed:

	Oak Tanned and Fulled Leather Belts.	Other Types of Leather Belts and 6- to 7-ply Rubber Belts.
A double belt, having an arc of contact of 180°, will give an effective pull on the face of a pulley per inch of width of belt of Or, a different form of same rule: The number of sq. ft. of double Belt passing	35 lbs.	30 lbs.
around a pulley per minute required to transmit one horse power is	80 sq. ft.	90 sq. ft.
per minute required to transmit one horse- power is	950 ft. 30 H.P.	1100 ft. 25 H.P.

The terms "initial tension," "effective pull," etc., are thus explained by Mr. Taylor: When pulleys upon which belts are tightened are at rest, both strands of the belt (the upper and lower) are under the same stress per in. of width. By "tension," initial tension," or "tension while at rest," we mean the stress per in, of width, or sq, in, of section, to which one of the strands of the belt is tightened, when at rest. After the belts are in motion and transmitting power, the stress on the slack side, or strand, of the belt becomes less, while that on the tight side—or the side which does the pulling—becomes greater than when the belt was at rest. By the term "tetal load" we mean the total stress per in. of width, or sq. in. of section, on the tight side of belt while in motion.

The difference between the stress on the tight side of the belt and its slack side, while in motion, represents the effective force or pull which is transmitted from one pulley to another. By the terms "working load," or "effective pull," we mean the difference in the tension of the tight and slack sides of the belt per in. of width, or sq. in. section, while in motion, or the net effective force that is transmitted from one pul-

The discovery of Messrs. Lewis and Bancroft (Trans. A. S. M. E., vii. 749) that the "sum of the tension on both sides of the belt does not remain constant," upsets all previous theoretical belting formulæ. The belt speed for maximum economy should be from 4000 to 4500 ft. per

minute.

The best distance from centre to centre of shafts is from 20 to 25 ft. Idler pulleys work most satisfactorily when located on the slack side of

the belt about one quarter way from the driving-pulley.

Belts are more durable and work more satisfactorily made narrow and

thick, rather than wide and thin.

It is safe and advisable to use: a double belt on a pulley 12 in. diameter or larger; a triple belt on a pulley 20 in. diameter or larger; a quadruple belt on a pulley 30 in. diameter.

As belts increase in width they should also be made thicker.
The ends of the belt should be fastened together by splicing and cementing, instead of lacing, wiring, or using hooks or clamps of any kind.

A V-splice should be used on triple and quadruple belts and when idlers

are used. Stepped splice, coated with rubber and vulcanized in place, is best

for rubber belts.

For double belting the rule works well of making the splice for all belts up to 10 in. wide, 10 in. long; from 10 in. to 18 in. wide the splice should be the same width as the belt, 18 in. being the greatest length of splice required for double belting.

Belts should be cleaned and greased every five to six months.

Double leather belts will last well when repeatedly tightened under a strain (when at rest) of 71 lbs. per in. of width, or 240 lbs. per sq. in. section. They will not maintain this tension for any length of time, however, Belt-clamps having spring-balances between the two pairs of clamps

should be used for weighing the tension of the belt accurately each time it is tightened.

The stretch, durability, cost of maintenance, etc., of belts proportioned (A) according to the ordinary rules of a total load of 111 lbs. per inch of (A) according to the ordinary rules of a total load of 111 lbs, per inch of width corresponding to an effective pull of 65 lbs, per inch of width, and (B) according to a more economical rule of a total load of 54 lbs., corresponding to an effective pull of 26 lbs, per inch of width, are found to be as follows:
When it is impracticable to accurately weight the tension of a belt in tightening it, it is safe to shorten a double belt one half inch for every 10 ft, of length for (A) and one inch for every 10 ft, for (B), if if requires tightening, Double leather belts, when treated with great care and run night and day at moderate speed, should last for 7 years (A), 18 years (B).

The cost of all labor and materials used in the maintenance and repairs of

double belts, added to the cost of renewals as they give out, through a term of years, will amount on an average per year to 37% of the original cost of the belts (A); 14% or less (B).

In figuring the total expense of belting, and the manufacturing cost chargeable to this account, by far the largest item is the time lost on the

machines while belts are being relaced and repaired.

The total stretch of leather belting exceeds 6% of the original length. The stretch during the first six months of the life of belts is 36% of their

entire stretch (A); 15% (B).

A double belt will stretch 47/100 of 1% of its length before requiring to be tightened (A); 81/100 of 1% (B).

The most important consideration in making up tables and rules for the use and care of belting is how to secure the minimum of interruptions to manufacture from this source.

The average double belt (A), when running night and day in a machineshop, will cause at least 26 interruptions to manufacture during its life, or 5 interruptions per year, but with (B) interruptions to manufacture will not average oftener for each belt than one in sixteen months.

The oak-tanned and fulled belts showed themselves to be superior in all respects except the coefficient of friction to either the oak-tanned not fulled, the semi-raw-hide, or raw-hide with tanned face.

Belts of any width can be successfully shifted backward and forward on tight and loose pulleys. Belts running between 5000 and 6000 ft. per min. and driving 300 H.P. are now being daily shifted on tight and loose pulleys, to throw lines of shafting in and out of use.

The best form of belt-shifter for wide belts is a pair of rollers twice the

width of belt, either of which can be pressed onto the flat surface of the belt on its slack side close to the driven pulley, the axis of the roller making

an angle of 75° with the centre line of the belt.

Remarks on Mr. Taylor's Rules. (Trans. A. S. M. E., xv., 242.) The most notable feature in Mr. Taylor's paper is the great difference be-tween his rules for proper proportioning of belts and those given by earlier writers. A very commonly used rule is, one horse-power may be transmitted by a single belt 1 in. wide running x ft. per min., substituting for x various values, according to the ideas of different engineers, ranging usually from 550 to 1100.

The practical mechanic of the old school is apt to swear by the figure 600 as being thoroughly reliable, while the modern engineer is more apt to use the figure 1000. Mr. Taylor, however, instead of using a figure from 55 to 1100 for a single belt, uses 950 to 1100 for double belts. If we assume that a double belt is twice as strong, or will carry twice as much power, as a single belt, then he uses a figure at least twice as large as that used in modern practice, and would make the cost of belting for a given shop twice as large as if the belting were proportioned according to the most liberal of

the customary rules.

This great difference is to some extent explained by the fact that the problem which Mr. Taylor undertakes to solve is quite a different one from that which is solved by the ordinary rules with their variations. The problem of the latter generally is, "How wide a belt must be used, or how narrow a belt may be used, to transmit a given horse-power?" Mr. Taylor's problem is: "How wide a belt must be used so that a given horse-power may be transmitted with the minimum cost for belt repairs, the longest life may be transmitted with a smallest loss and inconvenience from stopping the machine while the belt is being tightened or repaired?"

The difference between the old practical mechanic's rule of a 1-in-wide

single belt, 600 ft. per min., transmits one horse-power, and the rule commonly used by engineers, in which 1000 is substituted for 600, is due to the belief of the engineers, not that a horse-power could not be transmitted by the belt proportioned by the older rule, but that such a proportion involved undue strain from overtightening to prevent slipping, which strain entailed too much journal friction, necessitated frequent tightening, and decreased

the length of the life of the belt.

Mr. Taylor's rule substituting 1100 ft. per min. and doubling the belt is a further step, and a long one, in the same direction. Whether it will be taken in any case by engineers will depend upon whether they appreciate the extent of the losses due to slippage of belts slackened by use under overstrain, and the loss of time in tightening and repairing belts, to such a degree as to induce them to allow the first cost of the belts to be doubled in order to avoid these losses.

It should be noted that Mr. Taylor's experiments were made on rather narrow belts, used for transmitting power from shafting to machinery, and his conclusions may not be applicable to heavy and wide belts, such as

engine fly-wheel belts.

#### MISCELLANEOUS NOTES ON BELTING.

Formulæ are useful for proportioning belts and pulleys, but they furnish no means of estimating how much power a particular belt may be transmitting at any given time, any more than the size of the engine is a measure of the load it is actually drawing, or the known strength of a horse is a measure of the load on the wagon. The only reliable means of determining the power actually transmitted is some form of dynamometer. (See Trans. A. S. M. E., vol. xii, p. 707.)

If we increase the thickness, the power transmitted ought to increase in proportion; and for double belts we should have half the width required for a single belt under the same conditions. With large pulleys and moderate velocities of belt it is probable that this holds good. With small pulleys, however, when a double belt is used, there is not such perfect contact between the pulley face and the belt, due to the rigidity of the latter, and more work is necessary to bend the belt-fibres than when a thinner and more pliable belt is used. The centrifugal force tending to throw the belt from the pulley also increases with the thickness, and for these reasons the width of a double belt required to transmit a given horse-power when used with small pulleys is generally assumed not less than seven tenths the width of a single belt to transmit the same power. (Flather on "Dynamometers and Measurement of Power.")

F. W. Taylor. however, finds that great pliability is objectionable, and favors thick belts even for small pulleys: The power consumed in bending the belt around the pulley he considers inappreciable. According to Ranline's formula for centrifugal tension, this tension is proportional to the sectional area of the belt, and hence it does not increase with increase of If we increase the thickness, the power transmitted ought to increase in

sectional area of the belt, and hence it does not increase with increase of thickness when the width is decreased in the same proportion, the sectional

area remaining constant.

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Scott A. Smith (Trans. A. S. M. E., x. 765) says: The best belts are made from all oak-tanned leather, and curried with the use of cod oil and tallow, all to be of superior quality. Such belts have continued in use thirty to forty years when used as simple driving-belts, driving a proper amount of power, and having had suitable care. The flesh side should not be run to the pulley-face, for the reason that the wear from contact with the pulley should come on the grain side, as that surface of the belt is much weaker in its tensile strength than the flesh side; also as the grain is hard it is more enduring for the wear of attrition; further, if the grain is actually worn off, then the belt may not suffer in its integrity from a ready tendency of the

hard grain side to crack.

The most intimate contact of a belt with a pulley comes, first, in the smoothness of a pulley-face, including freedom from ridges and hollows left by turning-tools; second, in the smoothness of the surface and evenness in the texture or body of a belt; third, in having the crown of the driving and re ceiving pulleys exactly alike.—as nearly so as is practicable in a commercial sense; fourth, in having the crown of pulleys not over 1%? for a 24" face, that is to say, that the pulley is not to be over 1\(\frac{1}{2}\)? I arger in diameter in its centre; fifth, in having the crown other than two planes meeting at the centre; sixth, the use of any material on or in a belt, in addition to those necessarily used in the currying process, to keep them pliable or increase their tractive quality, should wholly depend upon the exigencies arising in the use of belts: non-use is safer than over-use; seventh, with reference to the lacing of belts, it seems to be a good practice to cut the ends to a convex shape by using a former, so that there may be a nearly uniform stress on the lacing through the centre as compared with the edges. For a belt 10" wide, the centre of each end should recede 1/10".

centre of each end should recede 1/10".

Lacing of Beits.—In punching a belt for lacing use an oval punch, the longer diameter of the punch being parallel with the sides of the belt. Punch two rows of holes in each end, placed zigzag. In a 3-in. belt there should be four holes in each end,—two in each row. In a 6-inch belt, seven holes—four in the row nearest the end. A 10-inch belt should have nine holes. The edge of the holes should not come nearer than 3/4 of an inch from the sides, nor % of an inch from the ends of the belt. The second row should be at least 134 inches from the end. On wide belts these distances should

be even a little greater.

Begin to lace in the centre of the belt and take care to keep the ends exactly in line, and to lace both sides with equal tightness. The lacing should not be crossed on the side of the belt that runs next the pulley. In

taking up belts, observe the same rules as putting on new ones.

Setting a Belt on Quarter-twist.—A belt must run squarely on to the pulley. To connect with a belt two horizontal shafts at right angles with each other, say an engine-shaft near the floor with a line attached to the ceiling, will require a quarter-turn. First, ascertain the central point on the face of each pulley at the extremity of the horizontal diameter where the belt will leave the pulley, and then set that point on the driven pulley plumb over the corresponding point on the driver. This will cause the belt to run squarely on to each pulley, and it will leave at an angle greater or less, according to the size of the pulleys and their distance from each other.

In quarter-twist belts, in order that the belt may remain on the pulleys, In quarter-twist bons, in other that the best may remain on the point of delivery of the central plane on each pulley must pass through the point of delivery of the other pulley. This arrangement does not admit of reversed motion.

To find the Length of Belt required for two given

To find the Length of Belt required for two given Pulleys.—When the length cannot be measured directly by a tape-line, the following approximate rule may be used: Add the diameter of the two pulleys together, divide the sum by 2, and multiply the quotient by 3½, and add the product to twice the distance between the centres of the shafts. (See accurate formula below.)

(See accurate formula below.)

To find the Angle of the Arc of Contact of a Belt.—Divide the difference between the radii of the two pulleys in inches by the distance between their centres, also in inches, and in a table of natural sines find the angle most nearly corresponding with the quotient. Multiply this angle by 2, and add the product to 180° for the angle of contact with the larger pulley, or subtract it from 180° for the smaller pulley.

Or, let R= radius of larger pulley, r= radius of smaller; L= distance between centres of the pulleys; a= angle whose sine is (R-r)+L.

Are of contact with smaller pulley =  $180^{\circ}-2a$ ; "larger pulley =  $180^{\circ}+2a$ .

To find the Length of Belt in Contact with the Pulley,— For the larger pulley, multiply the angle a, found as above, by .0849, to the product add 3.1416, and multiply the sum by the radius of the pulley. Or length of belt in contact with the pulley

= radius 
$$\times (\pi + .0349a)$$
 = radius  $\times \pi \left(1 + \frac{a}{90}\right)$ .

For the smaller pulley, length = radius  $\times (\pi - .0349a)$  = radius  $\times \pi \left(1 - \frac{a}{co}\right)$ 

The above rules refer to Open Belts. The accurate formula for length of an open belt is,

Length = 
$$\pi R \left( 1 + \frac{a}{90} \right) + \pi r \left( 1 - \frac{a}{90} \right) + 2L \cos a$$

$$= R(\pi + .0349a) + r(\pi - .0349a) + 2L \cos a$$

in which R = radius of larger pulley, r = radius of smaller pulley, L = distance between centres of pulleys, and a = angle whose sine is

$$(R-r) \div L$$
;  $\cos a = \sqrt{L^2 - (R-r)^2}$ .

For Crossed Belts the formula is

Length of belt = 
$$\pi R \left(1 + \frac{\beta}{90}\right) + \pi r \left(1 + \frac{\beta}{90}\right) + 2L \cos \beta$$
,  
=  $(R + r) \times (\pi + .0349\beta) + 2L \cos \beta$ ,

in which 
$$\beta$$
 = angle whose sine is  $(R+r) + L : \cos \beta = \sqrt{L^2 - (R+r)^2}$ .

To find the Length of Belt when Closely Rolled.—The sum of the diameter of the roll, and of the eye in inches, × the number of turns made by the belt and by 1809, = length of the belt in feet

To find the Approximate Weight of Belts — Multiply the length of belt, in feet, by the width in inches, and divide the product by 13 for single, and 8 for double belt.

Relations of the Size and Speeds of Driving and Driven Pulleys.—The driving pulley is called the driver, D, and the driven pulley the driven, d. If the number of teeth in gears is used instead of diameter, in these calculations, number of teeth must be substituted wherever diameter occurs. R = revs. per min. of driver, r = revs. per min. of driven

$$D = dr + R$$
;

Diam. of driver = diam. of driven × revs. of driven + revs. of driver.

$$d = DR \div r$$
:

Diam. of driven = diam. of driver × revs. of driver + revs. of driven.

$$R = dr \div D;$$

Revs. of driver = revs. of driven × diam. of driven + diam. of driver.

#### $r = DR \div d$ :

Revs. of driven = revs. of driver × diam, of driver ÷ diam, of driven.

Evils of Tight Belts. (Jones and Laughlins.)—Clamps with powerful servis of Tight Betts. (Jones and Laugnins.)—Clamps with powerries serves are often used to put on belts with extreme tightness, and with most injurious strain upon the leather. They should be very judiciously used for horizontal belts, which should be allowed sufficient slackness to move with a loose undulating vibration on the returning side, as a test that they have no more strain imposed than is necessary simply to transmit the power. On this subject a New England cotton-mill engineer of large experience.

On this subject a New Engand couton-min engineer of large experience, says: I believe that three quarters of the trouble experienced in broken pulleys, hot boxes, etc., can be traced to the fault of tight belts. The enormous and useless pressure thus put upon pulleys must in time break them, if they are made in any reasonable proportions, besides wearing out the whole out fit, and causing heating and consequent destruction of the bearings. Below are some figures showing the power it takes in average modern mills with first-class shafting, to drive the shafting alone :

	Whole	Shafting	g Alone.	Mill, No.	Whole	Shafting Alone.			
Mill, No.	Load, H.P.	Horse- power.	Per cent of whole,		Load, H.P.	Horse- power.	Per cent of whole.		
1 2 8 4	199 472 486 677	51 111.5 134 190	25.6 23.6 27.5 28.1	5 6 7 8	759 235 670 677	172.6 84.8 262.9 182	22.7 36.1 39.2 26.8		

These may be taken as a fair showing of the power that is required in many of our best mills to drive shafting. It is unreasonable to think that all that power is consumed by a legitimate amount of friction of bearings and belts. I know of no cause for such a loss of power but tight belts. These, when there are hundreds or thousands in a mill, easily multiply the friction on the bearings, and would account for the figures.

Sag of Belts .- In the location of shafts that are to be connected with each other by belts, care should be taken to secure a proper distance one This distance should be such as to allow of a gentle sag to from the other. the belt when in motion.

A general rule may be stated thus: Where narrow belts are to be run over small pulleys 15 feet is a good average, the belt having a sag of 11/6 to 2 inches. For larger belts, working on larger pulleys, a distance of 20 to 25 feet does well, with a sag of 2½ to 4 inches. For main belts working on very large pulleys, the distance should be 25 to 30 feet, the belts working well with a sag of 4 to 5 inches.

If too great a distance is attempted, the belt will have an unsteady flapping

motion, which will destroy both the belt and machinery.

Arrangement of Belts and Pulleys.-If possible to avoid it, connected shafts should never be placed one directly over the other, as in such case the belt must be kept very tight to do the work. For this purpose belts should be carefully selected of well-stretched leather.

It is desirable that the angle of the belt with the floor should not exceed 45°. It is also desirable to locate the shafting and machinery so that belts should run off from each shatt in opposite directions, as this arrangement will relieve the bearings from the friction that would result when the belts all

pull one way on the shaft.

In arranging the belts leading from the main line of shafting to the counters, those pulling in an opposite direction should be placed as near counters, those pulling in an opposite direction should be piaced as heart each other as practicable, while those pulling in the same direction should be separated. This can often be accomplished by changing the relative posi-tions of the pulleys on the counters. By this procedure much of the friction on the journals may be avoided.

If possible, machinery should be so placed that the direction of the belt motion shall be from the top of the driving to the top of the driven pulley, when the sax will increase the area of counterf.

when the sag will increase the arc of contact.

The pulley should be a little wider than the belt required for the work.

The motion of driving should run with and not against the laps of the helts Tightening or guide pulleys should be applied to the slack side of belts and near the smaller pulley.

Jones & Laughlins, in their Useful Information, say: The diameter of the pulleys should be as large as can be admitted, provided they will not pro-

duce a speed of more than 3750 feet of belt motion per minute.

They also say: It is better to gear a mill with small pulleys and run them at a high velocity, than with large pulleys and to run them slower. A mill thus geared costs less and has a much neater appearance than with large heavy pulleys.

M. Arthur Achard (Proc. Inst. M. E., Jan. 1881, p. 62) says: When the belt is wide a partial vacuum is formed between the belt and the pulley at a high velocity. The pressure is then greater than that computed from the tensions in the belt, and the resistance to slipping is greater. This has the advantage of permitting a greater power to be transmitted by a given belt, and of diminishing the strain on the shafting.

On the other hand, some writers claim that the belt entraps air between itself and the pulley, which tends to diminish the friction, and reduce the tractive force. On this theory some manufacturers perforate the belt with numerous holes to let the air escape.

Care of Belts .- Leather belts should be well protected against water and even loose steam and other moisture. Belts of coarse, loose leather will do better service in dry warm places: for

wet or moist situations the finest and firmest leather should be used.

Hoyt & Co.) Do not allow oil to drip upon the belts. It destroys the life of the leather.

Leather belting cannot safely stand above 110° of heat.

Strength of Belting.—The ultimate tensile strength of belting does not generally enter as a factor in calculations of power transmission.

The strength of the solid leather in belts is from 2000 to 5000 lbs, per square inch; at the lacings, even if well put together, only about 1000 to 1500. If riveted, the joint should have half the strength of the solid belt. The working strain on the driving side is generally taken at not over one third of the strength of the lacing, or from one eighth to one sixteenth of the strength of the solid belt. Dr. Hartig found that the tension in practice varied from 30 to 532 lbs. per square inch, averaging 33 lbs.

Adhesion Independent of Diameter. (Schultz Belting Co.)—

The adhesion of the belt to the pulley is the same-the arc or number of

degrees of contact, aggregate tension or weight being the same—without reference to width of belt or diameter of pulley. 2. A belt will slip just as readily on a pulley four feet in diameter as it will on a pulley two feet in diameter, provided the conditions of the faces of the pulleys, the arc of contact, the tension, and the number of feet the belt travels per minute are the same in both cases.

3. A belt of a given width, and making any given number of feet per minute, will transmit as much power running on pulleys two feet in diameter as it will on pulleys four feet in diameter, provided the arc of contact.

tension, and conditions of pulley faces are the same in both cases.

4. To obtain a greater amount of power from belts the pulleys may be covered with leather; this will allow the belts to run very slack and give 25% more durability

Endless Belts.—If the belts are to be endless, they should be put on and drawn together by "belt clamps" made for the purpose. If the belt is made endless at the belt factory, it should never be run on to the pulleys, lest the irregular strain spring the belt. Lift out one shaft, place the belt on the

pulleys, and force the shaft back into place.

Belt Data.—A fly-wheel at the Amoskeag Mfg. Co., Manchester, N. H.,

30 feet diameter, 110 inches face, running 61 revolutions per minute, carried
two heavy double-leather belts 40 inches wide each, and one 24 inches wide.

The engine indicated 1950 H. P., of which probably 1850 H.P., was transmitted by the belts. The belts were considered to be heavily loaded, but not overtaxed.

 $30 \times 3.14 \times 104 \times 61 = 323$  feet per minute for 1 H.P. per inch of width.

Samuel Webber (Am. Mach., Feb. 22, 1894) reports a case of a belt 30 inches wide, 34 inch thick, running for six years at a velocity of 2900 feet per minute, on to a pulley 5 feet diameter, and transmitting 550 H.P. This gives a velocity of 210 feet per minute for 1 H.P. per inch of width. By Mr. Nagle's table of riveted belts this belt would be designed for 332 H.P. By Mr. Taylor's

rule it would be used to transmit only 123 H.P.

The above may be taken as examples of what a belt may be made to do, but they shou d not be used as precedents in designing. It is not stated how much power was lost by the journal friction due to over-tightening of these

Belt Dressings.—We advise, when the belt is pliable, and only dry and husky, the application of blood-warm tallow. This applied, and dried in by heat of fire or sun, will tend to keep the leather in good working condition. The oil of the tallow passes into the tallow of the leather, serving to soften it, and the stearine is left on the outside, to fill the pores and leave a smooth surface. The addition of resin to the tallow for belts, if used in wet or damp places, will be of service and help preserve their strength. Belts which have become hard and dry should have an application of neat's-foot or liver oil, mixed with a small quantity of resin. This prevents the oil from injuring the belt and helps to preserve it. There should not be so much resin as to leave the belt sticky. (J. B. Hoyt & Company.)

Belts should not be soaked in water before oiling, and penetrating oils

Belts should not be soaked in water before oiling, and penetrating oils should but seldom be used, except occasionally when a belt gets very dry and husky from neglect. It may then be moistened a little, and have neat's-foot oil applied. Frequent applications of such oils to a new belt render the leather soft and flabby, thus causing it to stretch, and making it liable to run out of line. A composition of tailow and oil, with a little resin or beeswax, is better to use. Prepared castor-oil dressing is good, and may be applied with a brush or rag while the belt is running. (Alexander Bros.)

Cement for Cloth or Leather. (Molesworth.)—16 parts guttapercha, 4 india-rubber, 2 pitch, 1 shellac, 2 linseed-oil, cut small, melted to-

gether and well mixed.

Rubber Belling.—The advantages claimed for rubber belting are perfect uniformity in width and thickness; it will endure a great degree of heat and cold without injury; it is also specially adapted for use in damp or wet places, or where exposed to the action of steam; it is very durable, and has great tensile strength, and when adjusted for service it has the most perfect hold on the pulleys, hence is less liable to slip than leather.

Never use animal oil or grease on rubber belts, as it will greatly injure and

soon destroy them.

Rubber belts will be improved, and their durability increased, by putting on with a painter's brush, and letting it dry, a composition made of equal parts of red lead, black lead. French yellow, and litharge, mixed with boiled inseed-oil and japan enough to make it dry quickly. The effect of this will be to produce a finely polished surface. If, from dust or other cause, the belt should slip, it should be lightly moistened on the side next the pulley with boiled linseed-oil. (From circulars of manufacturers.)

## GEARING.

#### TOOTHED-WHEEL GEARING.

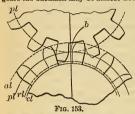
Pitch, Pitch-eircle, etc.—If two cylinders with parallel axes are pressed together and one of them is rotated on its axis, it will drive the other by means of the friction between the surfaces. The cylinders may be considered as a pair of spur-wheels with an infinite number of very small teeth. If actual teeth are formed upon the cylinders, making alternate elevations and depressions in the cylindrical surfaces, the distance between the axes remaining the same, we have a pair of gear-wheels which will drive one another by pressure upon the faces of the teeth, if the teeth are properly shaped. In making the teeth the cylindrical surface may entirely disappear, but the position it occupied may still be considered as a cylindrical surface, which is called the "pitch-surface," and its trace on the end of the wheel, or on a plane cutting the wheel at right angles to its axis, is called the "pitch-circle" or "pitch-line." The diameter of this circle is called the "pitch-diameter, and the distance from the face of one tooth to the corresponding face of the next tooth on the same wheel, measured on an arc of the pitch-circle, is called the "pitch of the tooth," or the circular pitch.

If two wheels having teeth of the same pitch are geared together so that their pitch-circles touch, it is a property of the pitch-circles that their diameters are proportional to the number of teeth in the wheels, and vice versa;

thus, if one wheel is twice the diameter (measured on the pitch-circle) of the other, it has twice as many teeth. If the teeth are properly shaped the linear velocity of the two wheels are equal, and the angular velocities, or speeds of rotation, are inversely proportional to the number of teeth and to the diameter. Thus the wheel that has twice as many teeth as the other will revolve just half as many times in a minute.

The "pitch," or distance measured on an arc of the pitch-circle from the face of one tooth to the face of the next, consists of two parts—the "thick-ness" of the tooth and the "space" between it and the next tooth. The space is larger than the thickness by a small amount called the "back-lash," which is allowed for imperfections of workmanship. In finely cut

gears the backlash may be almost nothing.



The length of a tooth in the direction of the radius of the wheel is called the "depth," and this is divided into two parts: First, the "addendum," the height of the tooth above the pitch line; second, the dedendum," the depth below the pitch line, which is an amount equal to the addendum of the mating gear. The depth of the space is usually given a little "clearance" to allow for inaccuracies of workmanship, especially in east gears.

Referring to Fig. 153, pl, pl are the pitch-lines, al the addendum-line, rl the root-line or dedendum-line, cl the clearance-line, and b the back-

ash. The addendum and dedendum are usually made equal to each other.

No. of teeth

3.1416

Diametral pitch = 
$$\frac{\text{No. of teeth}}{\text{diam. of pitch-circle in inches}} = \frac{3.1416}{\text{circular pitch}};$$
Circular pitch =  $\frac{\text{diam. } \times 3.1416}{\text{No. of teeth}} = \frac{3.1416}{\text{diametral pitch}};$ 

Some writers use the term diametral pitch to mean  $\frac{\text{diam.}}{\text{No. of teeth}}$ 

circular pitch 3.1416 but the first definition is the more common and the more convenient. A wheel of 12 in. diam, at the pitch-circle, with 48 teeth is 48/12 4 diametral pitch, or simply 4 pitch. The circular pitch of the same wheel is  $\frac{12 \times 8.1416}{40} = .7854$ , or  $\frac{3.1416}{20} = .7854$  in

## Relation of Diametral to Circular Pitch.

	Relat	ion of	Diamet	ral to C	ircular	Pitch.	
Diame- tral Pitch.	Circular Pitch.	Diame- tral Pitch.	Circular Pitch.	Circular Pitch.	Diame- tral Pitch.	Circular Pitch.	Diame- tral Pitch.
1	3.142 in.	11	.286 in.	3	1.047	15/16	3.351
1½ 2	2.091	12	.262	21/2	1.257	3/8	3.590
2 ~	1.571	14	.224	2 ~	1.571	7/8 13/16	3.867
21/4	1.396	16	.196	17/8	1.676	3/4	4.189
21/2 23/4 3	1.257	18	.175	13/4	1.795	11/16	4.570
23/4	1.142	20	.157	15%	1.933	5/8	5.027
	1.047	22	.143	11/2	2.094	9/16	5.585
31/2	.898	24	.131	1 7/16	2.185	1/2	6.283
4	.785	26	.121	13/8	2.285	7/16	7.181
4 5 6 7	.628	28	.112	1 5/16	2.394	3/8 5/16	8.378
6	.524	30	.105	11/4	2.513	5/16	10.053
7	.449	32	.098	1 3/16	2.646	1/4	12.566
8 9	.393	36	.087	11/8	2.793	3/16	16.755
9	.349	40	.079	1 1/16	2.957	1/8 1/16	25.133
10	.314	48	.065	1	3.142	1/16	50.266

Since circular pitch =  $\frac{\text{diam.} \times 3.1416}{\text{No. of teeth}}$ , diam. =  $\frac{\text{circ. pitch} \times \text{No. of teeth}}{3.1416}$ 

which always brings out the diameter as a number with an inconvenient

fraction if the pitch is in even inches or simple fractions of an inch. By the diametral-pitch system this inconvenience is avoided. The diameter may be in even inches or convenient fractions, and the number of teeth is usually an even multiple of the number of inches in the diameter.

## Diameter of Pitch-line of Wheels from 10 to 100 Teeth of 1 in, Circular Pitch,

No. Teeth.	Diam., in.	No. Teeth.	Diam., in.	No Teeth.	Diam., in.	No. Teeth.	Diam., in.	No. Teeth.	Diam.,	No. Teeth.	Diam., in.
10	3.183	26	8.276	41	13.051	56	17.825	71	22,600	86	27.375
11	3.501	27	8.594	42	13.369	57	18.144	72	22.918	87	27.693
12	3.820	28	8.913	43	13.687	58	18.462	73	22,236	88	28.011
13	4.138	29	9.231	44	14.006	59	18.781	74	23.555	89	28.329
14	4.456	30	9.549	45	14.324	60	19,099	75	23.873	90	28.648
15	4.775	31	9.868	46	14.642	61	19.417	76	24.192	91	28.966
16	5.093	32	10.186	47	14.961	62	19.735	77	24.510	95	29.285
17	5.411	33	10.504	48	15.279	63	20.054	78	24.828	93	29.603
18	5.730	34	10.823	49	15.597	64	20.372	79	25.146	94	29.921
19	6.048	35	11.141	50	15.915	65	20.690	80	25.465	95	30.239
20	6.366	36	11.459	51	16.234	66	21.008	81	25.783	'96	30.558
21	6.685	37	11.777	52	16.552	67	21.327	82	26,101	97	30.876
22	7.003	38	12.096	53	16.870	68	21.645	83	26.419	. 98	31.194
23	7.321	39	12 414	54	17.189	69	21.963	84	26.738	99	31.512
24	7.639	40	12.732	55	17.507	70	22.282	85	27.056	100	31.831
25	7.958										

For diameter of wheels of any other pitch than 1 in., multiply the figures in the table by the pitch. Given the diameter and the pitch, to find the number of teeth. Divide the diameter by the pitch, look in the table under diameter for the figure nearest to the quotient, and the number of teeth will be found opposite.

## Proportions of Teeth. Circular Pitch = 1.

	1.	2.	3.	4.	5.	6.
Depth of tooth above pitch-line	.35	.30	.37	.33	.30	.30
	.40	.40	.43	1	.40	.35
Working depth of tooth	.70	.60	.73	.66	***	
Total depth of tooth	.75	.70 .10	.80	.75	.70	.65
Thickness of tooth	.45	.45	.47	.45	.475	.485
Width of space		.55	.53	.55	.525	.515
Backlash	.10	.09	.07	.10	.05	.03
Thickness of rim			.47	.45	.70	. 65
		1	_		-	
	7.	8.		9.	1	0.*
					-	
Depth of tooth above pitch-line	.25 to .33	.30		.318	-	$\pm P$
Depth of tooth above pitch-line			08"	.318	1.15	
Working depth of tooth			08′′	.369 .637	1.15	(÷P ÷P
Working depth of tooth Total depth of tooth	.6 to .75	.65+.	08''	.369 .637 .687	2.15	(÷P è÷P (÷P
Working depth of tooth.  Total depth of tooth.  Clearance at root.	.6 to .75	.65+.	08''	.369 .637 .687 04 to .05	1.15 2.15 .157	(+P +P (+P (+P
Working depth of tooth Total depth of tooth	.6 to .75	.65+.	08''	.369 .637 .687	1.15 2.15 .157 1.51	7÷P 2÷P 7÷P 7÷P 1÷P to
Working depth of tooth	.6 to .75	.65+.	08'' 08'' 	.369 .637 .687 04 to .05 48 to .5	1.15 2.15 .157 1.51 1.57 1.57	$\begin{array}{l} ?+P \\ \div P \\ ?+P \\ \div P \\ \div P \\ \div P \\ + P \\ to \\ \div P \\ \div P \\ + P \\ to \end{array}$
Working depth of tooth.  Total depth of tooth.  Clearance at root.	.6 to .75	.65+. 5 .48	08'' 08'' 03''	.369 .637 .687 04 to .05 48 to .5	1.15 2.15 .157 1.51 1.57 1.57 1.68	$\begin{array}{l} ?+P \\ \div P \\ ?+P \\ \div P \\ \div P \\ \div P \\ + P \\ to \\ \div P \\ \div P \\ + P \\ to \end{array}$

\* In terms of diametral pitch.

AUTHORITIES.—1. Sir Wm, Fairbairn. 2, 3. Clark, R. T. D.; "used by engineers in good practice." 4. Molesworth. 5, 6. Coleman Sellers: 5 for cast, 6 for cut wheels. 7, 8. Unwin. 9, 10. Leading American manufacturers of cut gears.

The Chordal Pitch (erroneously called "true pitch" by some authors) is the length of a straight line or chord drawn from centre to centre of two adjacent teeth. The term is now but little used.

Chordal pitch = diam. of pitch-circle  $\times$  sine of  $\frac{160}{\text{No. of teeth}}$ Chordal pitch of a wheel of 10 in. pitch diameter and 10 teeth,  $10 \times \sin 18^\circ = 3.0902$  in. Circular pitch of same wheel = 3.1416. Chordal pitch is used with chain or sprocket wheels, to conform to the pitch of the chain.

## Formulæ for Determining the Dimensions of Small Gears. (Brown & Sharpe Mfg. Co.)

P = diametral pitch, or the number of teeth to one inch of diameter of pitch-circle;

D' = diameter of pitch circle $D$ = whole diameter $N$ = number of teeth $V$ = velocity.	Wheel.	These wheels
d' = diameter of pitch-circle	Smaller Wheel,	run together.

a =distance between the centres of the two wheels; b = number of teeth in both wheels;

t =thickness of tooth or cutter on pitch-circle;

s = addendum;

D''= working depth of tooth; f= amount added to depth of tooth for rounding the corners and for clearance:

D''+f = whole depth of tooth;  $\pi = 3.1416.$ 

P' = circular pitch, or the distance from the centre of one tooth to the centre of the next measured on the pitch-circle.

Formulæ for a single wheel:

$$\begin{split} P &= \frac{N+2}{D}; \quad D' = \frac{D \times N}{N+2}; \quad D'' = \frac{2}{P} = 2s; \quad s = \frac{1}{P} = \frac{P'}{\pi} = .3183P'; \\ P &= \frac{N}{D}; \qquad D' = \frac{N}{P}; \qquad N = PD'; \quad s = \frac{D}{N} = \frac{D}{N+2}; \\ P' &= \frac{\pi}{P}; \qquad D = \frac{N+2}{P}; \qquad f = \frac{t}{10}; \qquad s + f = \frac{1}{P} \Big( 1 + \frac{\pi}{20} \Big) = .3685P. \\ P &= \frac{\pi}{P}; \qquad D = D' + \frac{2}{P}; \qquad t = \frac{1.57}{P} = \frac{1}{2}P'. \end{split}$$

Formulæ for a pair of wheels:

$$\begin{split} b &= 2aP; & n &= \frac{PD'V}{v} & D &= \frac{2a(N+2)}{b}; \\ N &= \frac{nv}{V}; & v &= \frac{PD'V}{n}; & d &= \frac{2a(n+2)}{b}; \\ n &= \frac{NV}{v}; & v &= \frac{NV}{n}; & a &= \frac{b}{2P}; \\ N &= \frac{bv}{v+V}; & V &= \frac{nv}{N}; & a &= \frac{D'+d'}{2}; \\ n &= \frac{bV}{v+V}; & D' &= \frac{2aV}{v+V}; & d' &= \frac{2aaV}{v+V}. \end{split}$$

The following proportions of gear wheels are recommended by Prof. Coleman Sellers. (Stevens Indicator, April, 1892.)

## Proportions of Gear-wheels.

			Inside of I	Pitch-line,	Width o	f Space.							
Diametral Pitch.	Circular Pitch.	Outside of Pitch-line, $P \times .3$	For Cast or Cut Bevels or for Cast Spurs. P × .4	For Cut Spurs. P × .35	For Cast Spurs or Bevels. P × .525	For Cut Bevels or Spurs. P × .51							
	1/1	.075	.100	.088	.131	.128							
12	.2618	.079	.105	.092	.137	.134							
10	.31416	.094	.126	.11	.165	.16							
	3/8	.113	. 150	.131	.197	.191							
8 7	.3927	.118	.157	.137	.206	.2							
7	.4477	.134	.179	.157	.235	.228							
	.5236	.15	.20	.175	. 263	.255							
6	.5286	.157	.209	.183	.275	.267							
	9/16	.169	.225	.197	.295	.287							
	.62832	.188	.25	.219	.328	.319							
5	.62832	.188 .225	.251	.22	.33	.32							
	3/4 .7854	.225	.3	.263	.394	.383							
4		.236	.314	.275	.412	.401							
	7/8	.263	.35	.307	.459	.446							
	1	.3	.4	.35	.525	.51							
3	1.0472	.314	.419	.364	.55	.534							
	11/8 1.1424	.338	.45	.394	.591	.574							
23/4	1.1424	.343 .375 .377	.457	.40	.6	.583							
01.4	11/4 1.25664	-010	.5	.438	.656	.638							
21/2	1.25564	.413	.503 .55	.44 .481	.66	.641							
	19/8	.45	.6	.525	.722	.701							
2	13/8 11/5 1.5708	.471	.628	.55	.788	.765							
2	13/4	.525	.0.60	.613	.919	.893							
	2 2 4	.6	.7	.7	1.05	1.02							
11/2		.628	.838	.733	1 1	1.068							
172	91/4	.675	.000	.788	1.1	1.148							
	912	.75	1.0	.875	1.313	1.275							
	237	.825	1.1	.963	1.444	1,403							
	3 4	.9	1.2	1.05	1,575	1.53							
1	3.1416	.942	1.257	1.1	1.649	1.602							
•	- 31/4	.975	1.3	1.138	1.706	1 657							
	31/6	1.05	1.4	1.225	1.838	1.785							
	-/2	,			1 -7000	1							

Thickness of rim below root = depth of tooth.

Width of Teeth.—The width of the faces of teeth is generally made from 2 to 3 times the circular pitch = from 6.28 to 9.42 divided by the diametral pitch. There is no standard rule for width.

The following sizes are given in a stock list of cut gears in "Grant's Gears:"

Diametral pitch.... 3 4 6 8 12 16 Face, inches.... ... 3 and 4  $2\frac{1}{2}$  134 and 2  $1\frac{1}{4}$  and  $1\frac{1}{2}$  34 and 1  $\frac{1}{2}$  and  $\frac{5}{8}$ 

The Walker Mfg. Co. give:

Circular pitch, in.. 16 56 34 76 1 116 2 2 216 3 4 5 6 Face, in....... 114 114 114 2 216 6 716 9 12 16 20

Rules for Calculating the Speed of Gears and Pulleys.— The relations of the size and speed of driving and driven gear wheels are the same as those of belt pulleys. In calculating for gears, multiply or divide by the diameter of the pitch-circle or by the number of teeth, as may be required. In calculating for pulleys, multiply or divide by their diameter in inches.

If D = diam, of driving wheel, d = diam, of driven, R = revolutions per minute of driver, r = revs, per min. of driven.

 $R = rd + D; \quad r = RD + d; \quad D = dr + R; \quad d = DR + r.$ If N =number of teeth of driver and n =number of teeth of driven,  $N = nr + R; \quad n = NR + r; \quad R = rn + N; \quad r = RN + n.$ 

To find the number of revolutions of the last wheel at the end of a train of spur-wheels, all of which are in a line and mesh into one another, when the revolutions of the first wheel and the number of teeth or the diameter of the first and last are given: Multiply the revolutions of the first wheel by its number of teeth or its diameter, and divide the product by the number of teeth or the diameter of the last wheel.

To find the number of teeth in each wheel for a train of spur-wheels, each to have a given velocity: Multiply the number of revolutions of the driving-wheel by its number of teeth, and divide the product by the number

of revolutions each wheel is to make.

or revolutions each wheel is to make.

To find the number of revolutions of the last wheel in a train of wheels and pinions, when the revolutions of the first or driver, and the diameter, the teeth, or the circumference of all the drivers and pinions are given:
Multiply the diameter, the circumference, or the number of teeth of all the driving-wheels together, and this continued product by the number of revolutions of the first wheel, and divide this product by the continued product of the diameter, the circumference, or the number of teeth of all the driven wheels, and the quotient will be the number of revolutions of the last wheel.

Example. -1. A train of wheels consists of four wheels each 12 in, diameter of pitch-circle, and three pinions 4, 4, and 3 in. diameter. The large wheels are the drivers, and the first makes 36 revs. per min. Required the speed

of the last wheel.

$$\frac{36\times12\times12\times12}{4\times4\times3}=1296~\mathrm{rpm}.$$

2. What is the speed of the first large wheel if the pinions are the drivers, the 3-in, pinion being the first driver and making 36 revs, per min.?

$$\frac{36 \times 3 \times 4 \times 4}{12 \times 12 \times 12} = 1 \text{ rpm. } Ans.$$

Milling Cutters for Interchangeable Gears.—The Pratt & Whitney Co. make a series of cutters for cutting epicycloidal teeth. The number of cutters to cut from a pinion of 12 teeth to a rack is 24 for each pitch coarser than 10. The Brown & Sharpe Mfg. Co. make a similar series, and also a series for involute teeth, in which eight cutters are made for each pitch, as follows:

No	1.	2.	3.	4.	5.	6.	7.	8.
Will cut from	135	55	35	26	21	17	14	12
to	Rack	134	54	34	25	20	16	13

#### FORMS OF THE TEETH.

In order that the teeth of wheels and pinions may run together smoothly and with a constant relative velocity, it is necessary that their working faces shall be formed of certain curves called odontoids. The essential property of these curves is that when two teeth are in contact the common normal to the tooth curves at their point of contact must pass through the pitch-point, or point of contact of the two pitch circles. Two such curves

are in common use-the cyloid and the involute.

are in common use—the cyloid and the involute.

The Cycloidal Tooth.—In Fig. 154 tet PL and pl be the pitch-circles of two gear-wheels; GC and gc are two equal generating-circles, whose radii should be taken as not greater than one half of the radius of the smaller pitch-circle. If the circle gc be rolled to the left on the larger pitch-circle PL, the point O will describe an epicycloid, ocfgh. If the other generating-circle GC be rolled to the right on PL, the point O will describe a hypocycloid oabcd. These two curves, which are tangent at O, form the two parts of a tooth curve for a gear whose pitch-circle is PL. The upper part oh is called the face and the lower part od is called the flank, If the same circles be rolled on the other pitch-circle od, they will describe the curve for a nooth be rolled on the other pitch-circle pl, they will describe the curve for a tooth

be rolled on the other pitch-circle  $p_t$ , they will describe the curve for a tooth of the gear  $p_t$ , which will work properly with the tooth on PL. The cycloidal curves may be drawn without actually rolling the generating-circle, as follows: On the line PL, from 0, step off and mark equal distances, as 1, 2, 3, 4, etc. From 1, 2, 3, etc., draw radial lines toward the centre of PL, and from 6, 7, 8, etc., draw radial lines from the same centre, but beyond PL. With the radius of the generating-circle, and with centres successively placed on these radial lines, draw arcs of circles tangent to PL at 1 2 3, 6 7 8, etc. With the dividers set to one of the equal divisions, as  $O_1$ ,

step off 1a and 6e; step off two such divisions on the circle from 2 to b, and from 7 to f; three such divisions from 3 to c, and from 8 to g; and so on, thus locating the several points abcdH and efgk, and through these points draw the tooth curves.

The curves for the mating tooth on the other wheel may be found in like manner by drawing arcs of the generating-circle tangent at equidistant

points on the pitch-circle pl.

The tooth curve of the face oh is limited by the addendum-line r or  $r_1$ ,

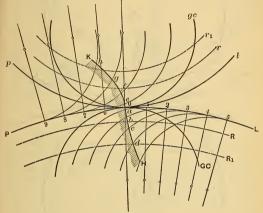


Fig. 154. 7

and that of the flank oH by the root curve R or R. R and r represent the root and addendum curves for a large number of small teeth, and  $R_f$  the like curves for a small number of large teeth. The form or appearance of the tooth therefore varies according to the number of teeth, while the pitch-

circle and the generating-circle may remain the same.

In the cycloidal system, in order that a set of wheels of different diameters but equal pitches shall all correctly work together, it is necessary that the generating-circle used for the teeth of all the wheels shall be the same, and it should have a diameter not greater than half the diameter of the pitchline of the smallest wheel of the st. The customary standard size of the generating-circle of the cycloidal system is one having a diameter equal to the radius of the pitch-circle of a wheel having 12 teeth. (Some gearmakers adopt 15 teeth.) This circle gives a radial flank to the teeth of a wheel having 12 teeth. A pinion of 10 or even a smaller number of teeth can be made, but in that case the flanks will be undercut, and the tooth will not be as strong as a tooth with radial flanks. If in any case the describing circle be half the size of the pitch-circle, the flanks will be radial; if it be less, they will spread out toward the root of the tooth, giving a stronger form; but if greater, the flanks will curve in toward each other, whereby the teeth become weaker and difficult to make.

In some cases cycloidal teeth for a pair of gears are made with the gener-

In some cases cycloidal teeth for a pair of gears are made with the generating-circle of each gear, having a radius equal to half the radius of its pitch-circle. In this case each of the gears will have radial flanks. This method makes a smooth working gear, but a disadvantage is that the wheels are not interchangeable with other wheels of the same pitch but different number of the production.

bers of teeth.

The rack in the cycloidal system is equivalent to a wheel with an infinite number of teeth. The pitch is equal to the circular pitch of the mating gear. Both faces and flanks are cycloids formed by rolling the generating-circle of the mating gear-wheel on each side of the straight pitch-line of the rack.

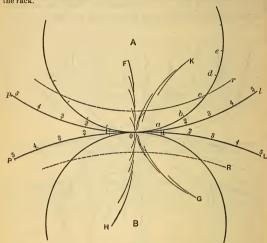


Fig. 155.

Another method of drawing the cycloida, curves is shown in Fig. 155. It is known as the method of tangent arcs. The generating-circles, as before, are drawn with equal radii, the length of the radius being less than half the radius of  $p_1$ . It estimaller pitch-circle. Equal divisions 1, 2, 3, 4, etc., are marked off on the pitch-circles and divisions of the same length stepped off on one of the generating-circles, as aabc, etc. From the points 1, 2, 8, 4, 5 on the line  $p_0$ , with radii successively equal to the chord distances aa, ab, ac, a

If the generating-circle had a radius just one half of the radius of pl, the hypocycloid F would be a straight line, and the flank of the tooth would have been radial.

The Involute Tooth.—In drawing the involute tooth curve, the angle of obliquity, or the angle which a common tangent to the teeth, when they are in contact at the pitch-point, makes with a line joining the centres of the wheels, is first arbitrarily determined. It is customary to take it at 15°, The pitch-lines pl and PL being drawn in contact at 0, the line of obliquity AB is drawn through O normal to a common tangent to the tooth curves, or at the given angle of obliquity to a common tangent to the pitch-circles. In

the cut the angle is  $20^\circ$ . From the centres of the pitch-circles draw circles c and d tangent to the line AB. These circles are called base-lines or base-circles, from which the involutes F and K are drawn. By laying off convenient distances 0, 1, 2, 3, which should each be less than 1/10 of the diameter of the base-circle, small arcs can be drawn with successively increasing radil, which will form the involute. The involute extends from the points F

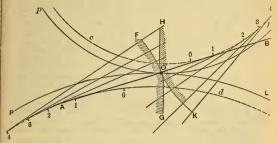


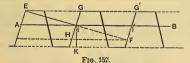
Fig. 156.

and K down to their respective base-circles, where a tangent to the involute becomes a radius of the circle, and the remainders of the tooth curves,

as G and H, are radial straight lines.

In the involute system the customary standard form of tooth is one having an angle of obliquity of 15° (Brown and Sharpe use 14½°), an addendum of about one third the circular pitch, and a clearance of about one eighth of the addendum. In this system the smallest gear of a set has 12 teeth, this being the smallest number of teeth that will gear together when made with this angle of obliquity. In gears with less than 30 teeth the points of the teeth must be slightly rounded over to avoid interference (see Grant's Teeth of Gears). All involute teeth of the same pitch and with the same angle of obliquity work smoothly together. The rack to gear with an involute-toothed wheel has straight faces on its teeth, which make an angle with the middle line of the tooth equal to the angle of obliquity, or in the standard form the faces are inclined at an angle of 30° with each other.

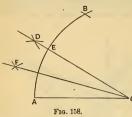
To draw the teeth of a rack which is to gear with an involute wheel (Fig. 157).—Let AB be the pitch-line of the rack and AI = II'=the pitch, Through



the pitch-point I draw EF at the given angle of obliquity. Draw AE and I'F perpendicular to EF. Through E and F draw lines EGG' and FH parallel to the pitch-line. EGG' will be the addendum-line and HF the flank-line. From I draw IK perpendicular to AB equal to the greatest addendum in the set of wheels of the given pitch and obliquity plus an allowance for clearance equal to  $\frac{1}{2}$ 0 of the addendum. Through K, parallel to AB, draw the clearance-line. The fronts of the teeth are planes perpendicular to EF, and the backs are planes inclined at the same angle to AB in the contrary direction. The outer half of the working face AE may be slightly curved. Mr. Grant makes it a circular arc drawn from a centre on the pitch-line

with a radius = 2.1 inches divided by the diametral pitch, or .67 in, × circular pitch.

To Draw an Angle of 15° without using a Protractor.-From C, on the



line AC, with radius AC, draw an arc AB, and from A, with the same radius, cut the arc at Bisect the arc BA by drawing small arcs at D from A and B as centres, with the same radius, as centres, with the same radius, which must be greater than one half of AB. Join DC, cutting BA at E. The angle ECA is 30°. Bisect the arc AE in like manner, and the angle FCA will be 15°. A property of involute-toothed wheels is that the distance between

the axes of a pair of gears may be altered to a considerable extent without interfering with their ac-The backlash is therefore variable at will, and may be ad-

justed by moving the wheels farther from or nearer to each other, and may thus be adjusted so as to be no greater than is necessary to prevent jamming of the teeth.

The relative merits of cycloidal and involute-shaped teeth are still a subject of dispute, but there is an increasing tendency to adopt the involute

tooth for all purposes. Clark (R. T. D., p. 734) says: Involute teeth have the disadvantage of being too much inclined to the radial line, by which an undue pressure is exerted on the bearings.

Unwin (Elements of Machine Design, 8th ed., p. 265) says: The obliquity of action is ordinarily alleged as a serious objection to involute wheels. Its importance has perhaps been overrated.

George B. Grant (Am. Mach., Dec. 26, 1885) says:

1. The work done by the friction of an involute tooth is always less than

the same work for any possible epicycloidal tooth.

2. With respect to work done by friction, a change of the base from a

gear of 12 teeth to one of 15 teeth makes an improvement for the epicycloid of less than one half of one per cent. 3. For the 12-tooth system the involute has an advantage of 1 1/5 per

cent, and for the 15-tooth system an advantage of 34 per cent.

4. That a maximum improvement of about one per cent can be accom-

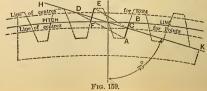
plished by the adoption of any possible non-interchangeable radial flank tooth in preference to the 12-tooth interchangeable system. 5. That for gears of very few teeth the involute has a decided advantage.

6. That the common opinion among millwrights and the mechanical public in general in favor of the epicycloid is a prejudice that is founded on long-continued custom, and not on an intimate knowledge of the properties of that curve.

Wilfred Lewis (Proc. Engrs. Club of Phila., vol. x., 1893) says a strong reaction in favor of the involute system is in progress, and he believes that an involute tooth of 221/2° obliquity will finally supplant all other forms.

Approximation by Circular Arcs.—Having found the form of

the actual tooth-curve on the drawing-board, circular arcs may be found by trial which will give approximations to the true curves, and these may be



used in completing the drawing and the pattern of the gear-wheels. root of the curve is connected to the clearance by a fillet, which should be as large aspossible to give increased strength to the tooth, provided it is not

large enough to cause interference.

large enough to cause interference. Molesworth gives the following method of construction by circular arcs: From the radial line at the edge of the tooth on the pitch-line, lay off the line HK at an angle of 75° with the radial line; on this line will be the centres of the root AB and the point EF. The lines struck from these centres are shown in thick lines. Circles drawn through centres thus found will give the lines in which the remaining centres will be. The radius DA for striking the root AB is = pitch + the thickness of the tooth. The radius CE for striking the point of the tooth EF = the pitch.

George B. Grant says: It is sometimes attempted to construct the curve by some handy method or empirical rule, but such methods are generally

worthless.

Stepped Gears. -- Two gears of the same pitch and diameter mounted side by side on the same shart will act as a single gear. If one gear is keyed on the shaft so that the teeth of the two wheels are not in line, but the teeth of one wheel slightly in advance of the other, the two gears form a stepped gear. If mated with a similar stepped gear on a parallel shart the number of teeth in contact will be twice as great as in an ordinary gean, which will increase the strength of the gear and its smoothness of action.

Twisted Teeth.—If a great number of very thin gears were placed together, one slightly in advance of the other, they would still act as a stepped gear. Continuing the subdivision until the

thickness of each separate gear is infinitesimal, the faces of the teeth instead of being in steps take the form of a spiral or twisted surface, and we have a twisted gear. The twist may take any shape, and if it is in one direction for half the width of the gear and in the opposite direction for the other half, we have what is known as the herring-bone or double helical tooth. The obliquity of the twisted tooth if twisted in one direction causes an end thrust on the shaft, but if the herring-bone twist is used, the opposite obliquities neutralize each other. This form of tooth is much used in heavy rolling-mill practice, where great strength and resistance to shocks are necessary. They are frequently made of steel castings (Fig. 160). The angle of the tooth with a line parallel to the axis of the gear is usually 30°.

Fig. 160.

**Spiral Gears.**—If a twisted gear has a uniform twist it becomes a spiral gear. The line in which the pitch-surface intersects the face of the tooth is part of a helix drawn on the pitch-surface. A spiral wheel may be made with only one helical tooth wrapped around the cylinder several times, in which it becomes a screw or worm. If it has two or three teeth so wrapped, it is a double- or triple-threaded screw or worm. A spiral-gear meshing into a rack is used to drive the table of some forms of planingmachine

Worm-gearing. - When the axes of two spiral gears are at right angles, and a wheel of one, two, or three threads works with a larger wheel of many threads, it becomes a worm-gear, or endless screw, the smaller

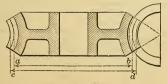


Fig. 161.

vheel or driver being called the worm, and the larger, or driven wheel, the worm-wheel. With this arrangement a high velocity ratio may be obtained with a single pair of wheels. For a one-threaded wheel the velocity ratio is the number of teeth in the worm-wheel. The worm and wheel are commonly so constructed that the worm will drive the wheel, but the wheel will not drive the worm.

To find the diameter of a worm-wheel at the throat, number of teeth and pitch of the worm being given; Add 2 to the number of teeth, multiply the

sum by 0.3183, and by the pitch of the worm in inches.

To find the number of teeth, diameter at throat and pitch of worm being given: Divide 3.1416 times the diameter by the pitch, and subtract 2 from the quotient.

the quotient.

In Fig. 16i ab is the diam. of the pitch-circle, cd is the diam, at the throat, EXAMPLE.—Pitch of worm ½ im., number of teeth 70, required the diam, at the throat. (70 + 2) × 3.183 × 25 = 5.73 in. Machinery and Millwork.)—

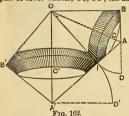
Teeth of Bevel-wheels. (Rankine's Machinery and Millwork.)—
The teeth of a bevel-wheel have acting surfaces of the conical kind, generated by the motion of a line traversing the apex of the conical pitch-surface, while a point in it is carried round the traces of the teeth upon a spherical surface described about that apex.

The operations of drawing the traces of the teeth of bevel-wheels exactly. whether by involutes or by rolling curves, are in every respect analogous to those for drawing the traces of the teeth of spur-wheels; except that in the case of bevel-wheels all those operations are to be performed on the surface of a sphere described about the apex, instead of on a plane, substituting poles for centres and great circles for straight lines.

In consideration of the practical difficulty, especially in the case of large wheels, of obtaining an accurate spherical surface, and of drawing upon it when obtained, the following approximate method, proposed originally by

Tredgold, is generally used: Let O, Fig. 162, be the common apex of the pitch-cones, OBI, OB'I, of a pair of bevel-wheels; OC, OC', the axes of those cones; OI their line of con-

tact.



make the outer rims of the patterns and of the wheels portions of the cones ABI, A'B'I, of which the narrow zones occupied by the teeth will be sufficiently near for practical pur-poses to a spherical surface described about O. As the cones ABI, A'B'I cut the pitch-cones at right angles in the outer pitch-circles IB, IB', they may be called the normal cones. To find the traces of the teeth upon the normal cones, draw on a flat surface circular arcs, ID, ID', with the radii AI, A'I; those arcs will be the developments of arcs of the pitch-circles IB, IB' when the conical sur-

Perpendicular to OI draw cutting the axes in A, A';

faces ABI, A'B'I are spread out flat. Describe the traces of teeth for the developed arcs as for a pair of spur-wheels, then wrap the developed arcs on the normal cones, so as to make them coincide with the pitch-circles, and

trace the teeth on the conical surfaces

For formulæ and instructions for designing bevel-gears, and for much other valuable information on the subject of gearing, see "Practical Treatise on Gearing," and "Formulas in Gearing," published by Brown & Sharpe Mfg Co.; and "Teeth of Gears," by George B. Grant, Lexington, Mass. The student may also consult Rankine's Machinery and Millwork, Reuleaux's Constructor, and Unwin's Elements of Machine Design. See also article on Gearing, by C. W. MacCoul in App. Cyc. Mech., vol. ii.

Annular and Differential Gearing. (S. W. Balch., Am. Mach.,

Aug. 24, 1893.)—In internal gears the sum of the diameters of the describing circles for faces and flanks should not exceed the difference in the pitch diameters of the pinion and its internal gear. The sum may be equal to this difference or it may be less; if it is equal the faces of the teeth of each wheel will drive the faces as well as the flanks of the teeth of the other The teeth will therefore make contact with each other at two points at the same time.

Cycloidal tooth-curves for interchangeable gears are formed with describing circles of about 56 the pitch diameter of the smallest gear of the series. To admit two such circles between the pitch-circles of the pinion and internal gear the number of teeth in the internal gear should exceed the number in the pinion by 12 or more, if the teeth are of the customary proportions and curvature used in interchangeable gearing.

Very often a less difference is desirable, and the teeth may be modified in

several ways to make this possible.

First. The tooth curves resulting from smaller describing circles may be employed. These will give teeth which are more rounding and narrower at their tops, and therefore not as desirable as the regular forms.

This is a

Second. The tips of the teeth may be rounded until they clear. This is a cut-and-try method which aims at modifying the teeth to such outlines as

smaller describing circles would give

Third. One of the describing circles may be omitted and one only used, which may be equal to the difference between the pitch-circles. This will permit the meshing of gears differing by six teeth. It will usually prove inexpedient to put wheels in inside gears that differ by much less than 12 teeth.

If a regular diametral pitch and standard tooth forms are determined on, the diameter to which the internal gear-blank is to be bored is calculated by subtracting 2 from the number of teeth, and dividing the remainder by the

diametral pitch.

The tooth outlines are the match of a spur-gear of the same number of teeth and diametral pitch, so that the spur-gear will fit the internal gear as a punch fits its die, except that the teeth of each should fail to bottom in the tooth spaces of the other by the customary clearance of one tenth the thickness of the tooth.

Internal gearing is particularly valuable when employed in differential action. This is a mechanical movement in which one of the wheels is mounted on a crank so that its centre can move in a circle about the centre of the other wheel. Means are added to the device which restrain the wheel on the crank from turning over and confine it to the revolution of the crank.

The ratio of the number of teeth in the revolving wheel compared with the difference between the two will represent the ratio between the revolving wheel and the crank-shaft by which the other is carried. The advantage in accomplishing the change of speed with such an arrangement, as compared with ordinary spur gearing, lies in the almost entire absence of friction and consequent wear of the teeth.

But for the limitation that the difference between the wheels must not be too small, the possible ratio of speed might be increased almost indefinitely, and one pair of differential gears made to do the service of a whole train of wheels. If the problem is properly worked out with bevel-gears this limitation may be completely set aside, and external and internal bevel-gears, differing by but a single tooth if need be, made to mesh perfectly with each other.

Differential bevel-gears have been used with advantage in mowing-machines. A description of their construction and operation is given by Mr. Balch in the article from which the above extracts are taken.

#### EFFICIENCY OF GEARING.

An extensive series of experiments on the efficiency of gearing, chiefly worm and spiral gearing, is described by Wilfred Lewis in Trans. A. S. M. E., vii. 273. The average results are shown in a diagram, from which the following approximate average figures are taken:

FEBRUARY OF SHIP SPIRE IND WORM GELDING

Gearing.	Pitch.	Velocity at Pitch line in feet per min.							
dourne,	I ROLL	3	10	40	100	200			
Spur pinion Spiral pinion "" " "" " " " " " Spiral pinion or worm"	45° 30 20 15 10 7	.90 .81 .75 .67 .61 .51 .43	.935 .87 .815 .75 .70 .615 .53	.97 .93 .89 .845 .805 .74 .72 .60	.98 .955 .93 .90 .87 .82 .765 .70	.985 .965 .945 .92 .90 .86 .815 .765			

The experiments showed the advantage of spur-gearing over all other kinds in both durability and efficiency. The variation from the mean results rarely exceeded 55 in either direction, so long as no cutting occurred, but the variation became much greater and very irregular as soon as cutting began. The loss of power varies with the speed, the pressure, the temperature, and the condition of the surfaces. The excessive friction of worm and spiral gearing is largely due to thee nd thrust on the collars of the shaft. This may be considerably reduced by roller-bearings for the collars.

When two worms with opposite spirals run in two spiral worm-gears that also work with each other, and the pressure on one gear is opposite that on the other, there is no thrust on the shaft. Even with light loads a worm will begin to heat and cut if run at too high a speed, the limit for safe working being a velocity of the rubbing surfaces of 200 to 300 ft. per minute, the former being preferable where the gearing has to work continuously. The wheel teeth will keep cool, as they form part of a casting having a large radiating surface; but the worm itself is so small that its heat is dissipated slowly. Whenever the heat generated increases faster than it can be conducted and radiated away, the cutting of the worm may be expected to begin. A low efficiency for a worm-gear means more than the loss of power, since the power which is lost reappears as heat and may cause the rapid destruction of the worm.

Unwin (Elements of Machine Design, p. 294) says: The efficiency is greater the less the radius of the worm. Generally the radius of the worm = 1.5 to 3 times the pitch of the thread of the worm or the circular pitch of the worm-wheel. For a one-threaded worm the efficiency is only 2/5 to 1/4; for a two-threaded worm, 4/7 to 2/5; for a three-threaded worm, 3/4 to 1/4. Since so much work is wasted in friction it is not surprising that the wear is excessive. The following table gives the calculated efficiencies of worm-wheels of 1, 2, 3, and 4 threads and ratios of radius of worm to pitch of teeth

of from 1 to 6, assuming a coefficient of friction of 6.15:

No. of			Radi	ius of W	orm + 1	Pitch.			
Threads.	1	11/4	11/2	13/4	2	21/2	3	4	6
1 2 3 4	.50 .67 .75 .80	.44 .62 .70	.40 .57 .67 .73	.36 .53 .63 .70	.33 .50 .60 .67	.28 .44 .55 .62	.25 .40 .50 .57	.20 .33 .43 .50	.14 .25 .33 .40

#### STRENGTH OF GEAR-TEETH.

The strength of gear-teeth and the horse-power that may be transmitted by them depend upon so many variable and uncertain factors that it is not surprising that the formulas and rules given by different writers show a wide variation. In 1879 John H. Cooper (Jour. Frank. Inst., July, 1879) found that there were then in existence about 48 well-established rules for horse-power and working strength, differing from each other in extreme cases about 500s. In 1886 Prof. Win. Harkness (Proc. A. A. A. S. 1886), from an examination of the bibliography of the subject, beginning in 1796, from the according to the constants and formulae used by various authors there were differences of 15 to 1 in the power which could be transmitted by a given pair of geared wheels. The various elements which enter into the constitution of a formula to represent the working strength of a toothed wheel are the following: 1. The strength of the metal, usually cast iron, which is an extremely variable quantity. 2. The shape of the tooth, and especially the relation of its thickness at the root or point of ieast strength to the pitch and to the length. 3. The point at which the load is taken to be applied, assumed by some authors to be at the pitch-line, by others at the extreme end, along the whole face, and by still others at a single outer corner. 4. The consideration of whether the total load is at any time received by a single tooth or whether it is divided between two teeth. 5. The findence of velocity in causing a tendency to break the teeth by shock, 6. The factor of safety assumed to cover all the uncertainties of the other elements of the problem.

Prof. Harkness, as a result of his investigation, found that all the formulæ on the subject might be expressed in one of three forms, viz.:

Horse-power = 
$$CVpf$$
, or  $CVp^2$ , or  $CVp^2f$ ;

in which C is a coefficient, V = velocity of pitch-line in feet per second, p = pitch in inches, and f = face of tooth in inches. From an examination of precedents he proposed the following formula

From an examination of precedents he proposed the following formula for cast-iron wheels:

H.P. = 
$$\frac{0.910Vpf}{4/1 + 0.65V}$$

He found that the teeth of chronometer and watch movements were subject to stresses four times as great as those which any engineer would dare

to use in like proportion upon cast-iron wheels of large size.

It appears that all of the earlier rules for the strength of teeth neglected the consideration of the variations in their form; the breaking strength, as aid by Mr. Cooper, being based upon the thickness of the teeth at the pitchline or circle, as if the thickness at the root of the tooth were the same in

all cases as it is at the pitch-line. Wiffred Lewis (Proc. Eng'rs Club, Phila., Jan. 1893; Am. Mach., June 22, 1893) seems to have been the first to use the form of the tooth in the construction of a working formula and table. He assumes that in well-constructed machinery the load can be more properly taken as well distributed across the tooth thau as concentrated in one corner, but that it cannot be safely taken as concentrated at a maximum distance from the root less than the extreme end of the tooth. He assumes that the whole load is taken upon one tooth, and considers the tooth as a beam loaded at one end, and from a series of drawings of teeth of the involute, cycloidal, and radial flank systems, determines the point of weakest cross-section of each, and the ratio of the thickness at that section to the pitch. He thereby obtains the general formula.

$$W = spfy;$$

in which W is the load transmitted by the teeth, in pounds; s is the safe working stress of the material, taken at 8000 lbs. for cast iron, when the working speed is 100 ft. or less per minute; p = p pitch; f = f ace, in inches; y = a factor depending on the form of the tooth, whose value for different cases is given in the following table:

No. of	Factor	for Streng	th, y.	No. of	Factor for Strength, y.					
Teeth.	Involute 20° Obliquity.	Involute 15° and Cycloidal	Radial Flanks.	Teeth.	Involute 20° Obliquity,	Involute 15° and Cycloidal	Radial Flanks.			
12	.078	.067	.052	27	.111	.100	.064			
13	.083	.070	.053	30	.114	102	.065			
14	.088	.072	.054	34	.118	.104	.066			
15	.092	.075	.055	38	.122	.107	.067			
16	.094	.077	.056	43	126	.110	.068			
17	.096	.080	.057	50	730	.112	.069			
18	.098	.083	.058	60	134	.114	.070			
19	.100	.087	.059	75	.138	.116	.071			
20	.102	.090	.060	100	.142	.118	.072			
21	.104	.092	.061	150	146	.120	.073			
23	.106	.094	.062	300	.150	122	.074			
25	.108	.097	.063	Rack.	.154	.124	.075			

SAFE WORKING STRESS, 8, FOR DIFFERENT SPEEDS.

Speed of Teeth in ft. per minute.	100 or less.	:000	300	600	900	1200	1800	2400
Cast ironSteel		6000 15000				2400 6000	2000 5000	



The values of s in the above table are given by Mr. Lewis tentatively, in the absence of sufficient data upon which to base more definite values, but they have been found to give satisfactory results in practice.

Mr. Lewis gives the following example to illustrate the use of the tables: Let it be required to find the working strength of a 12-toothed pinion of 1-inch pitch, 25g-inch face, driving a wheel of 90 teet hat 190 feet or less per minute, and let the teeth be of the 20-degree involute form. In the formula W = spfy we have for a cast-iron pinion s = sponds, s = sponds

measure of strength. measure of strength.

For bevel-wheels Mr. Lewis gives the following, referring to Fig. 168: D= large diameter of bevel; d= small diameter of bevel; p= pitch at large diameter; n= actual number of teeth; f= face of bevel; N= formative number of teeth p= face of bevel; N= formative number of teeth p= factor depending upon shape of teeth and formative number N; y= factor depending upon the formative number N; y= working load on teeth.

$$W=spfy\,\frac{D^3-d^3}{3D^2(D-d)}; \ \, {\rm or, more \, simply,} \ \, W=spfy\frac{d}{D},$$

which gives almost identical results when d is not less than  $\frac{2}{3}$  D, as is the case in good practice.

In Am, Mach, June 22, 1893, Mr. Lewis gives the following formulæ for the working strength of the three systems of gearing, which agree very closely with those obtained by use of the table:

For involute, 20° obliquity, 
$$W = spf\left(.154 - \frac{.912}{n}\right)$$
;

For involute 15°, and cycloidal, 
$$W = spf\left(.124 - \frac{.684}{n}\right)$$
;

For radial flank system, 
$$W = spf\left(.075 - \frac{.276}{n}\right);$$

in which the factor within the parenthesis corresponds to y in the general formula. For the horse-power transmitted, Mr. Lewis's general formula

W = spfy,  $= \frac{33,000 \text{ H.P.}}{v}$ , may take the form H.P.  $= \frac{spfyv}{33,000}$ , in which v =velocity in feet per minute; or since  $v = d\pi \times \text{rpm.} + 12 = .2618d \times \text{rpm.}$ , in which d = diameter in inches and rpm. = revolutions per minute,

H.P. = 
$$\frac{Wv}{33,000} = \frac{spfy \times d \times \text{rpm.}}{126,050} = .000007933dspfy \times \text{rpm.}$$

It must be borne in mind, however, that in the case of machines which consume power intermittently, such as punching and shearing machines, the gearing should be designed with reference to the maximum load W, which can be brought upon the teeth at any time, and not upon the average horse-power transmitted

Comparison of the Harkness and Lewis Formulas.— Take an average case in which the safe working strength of the material, s = 6000, v = 200 ft. per min., and y = .100, the value in Mr. Lewis's table for an involute tooth of  $15^{\circ}$  obliquity, or a cycloidal tooth, the number of teeth in the wheel being 27.

H.P. = 
$$\frac{spfyv}{33,000} = \frac{6000pfv \times .100}{33,000} = \frac{pfv}{55} = 1.091pfV$$
,

if V is taken in feet per second. Prof. Harkness gives H.P.=  $\frac{0.910Vpf}{\sqrt{1+0.65V}}$ . If the V in the denominator be taken at  $200 + 60 = 3\frac{1}{3}$  feet per second,  $\sqrt{1 + 0.65V} = \sqrt{3.167} = 1.78$ . and H.P. =  $\frac{.910}{1.78}Vpf = .571pfV$ , or about 52% of the result given by Mr. Lewis's

formula. This is probably as close an agreement as can be expected, since Prof. Harkness derived his formula from an investigation of ancient precedents and rule-of-thumb practice, largely with common cast gears, while Mr. Lewis's formula was derived from considerations of modern practice with machine moulded and cut gears.

Mr. Lewis takes into consideration the reduction in working strength of a tooth due to increase in velocity by the figures in his table of the values of the safe working stress s for different speeds. Prof. Harkness gives expression to the same reduction by means of the denominator of his formula

 $V\overline{1+0.65}V$ . The decrease in strength as computed by this formula is somewhat less than that given in Mr. Lewis's table, and as the figures given in the table are not based on accurate data, a mean between the values given by the formula and the table is probably as near to the true values as may be obtained from our present knowledge. The following table gives the values for different speeds according to Mr. Lewis's table and Prof. Harkness's formula, taking for a basis a working stress s, for cast-iron 8000, and for steel 20,000 lbs. at speeds of 100 ft. per minute and less;

v = speed of teeth, ft. per min., V = ft. per.sec..	100 1%	200 3½3	300 5	600 10	900 15	1200 20	1800 30	2400 40
Safe stress $s$ , cast-iron, Lewis Relative do., $s \div 8000$	8000	6000				2400		1700 .2125
$c = 1 + \sqrt{1 + 0.65V}$	.6930	.5621	.4850	.3650	.3050	.2672	.2208	.1924
Relative val. $c \div .693$		6488	5600		3512	3080	2544	2216
	20000	15500	13000	10300	8100	6800	5700	4900
Safe stress for steel, Lewis	20000	15000	12000	10000	7900	6000	5000	4300

Comparing the two formulæ for the case of s = 8000, corresponding to a speed of 100 ft, per min., we have

Harkness: H.P. =  $1 + \sqrt{1 + 0.65V} \times .910Vpf = .695 \times .91 \times 1\frac{1}{3}pf = 1.051pf'$ 

 $\text{H.P.} = \frac{spfyv}{33,000} = \frac{spfyV}{550} = \frac{8000 \times 1\% pfy}{550} = 24.24 pfy,$ Lewis:

in which y varies according to the shape and number of the teeth.

For radial-flank gear with 12 teeth y=.052; 24.24pfy=1.260pf : For 20° involute, 19 teeth, or 15° inv., 27 teeth y=.100; 24.24pfy=2.424pf; For 15° involute, 300 teeth y=.150; 24.24pfy=3.636pf.

Thus the weakest-shaped tooth, according to Mr. Lewis, will transmit 20 per cent more horse-power than is given by Prof. Harkness's formula, in which the shape of the tooth is not considered, and the average-shaped tooth, according to Mr. Lewis, will transmit more than double the horse-power given by Prof. Harkness's formula.

Comparison of Other Formulæ,-Mr. Cooper, in summing up Comparison of Other Formulæ.—Mr. Cooper, in summing up his examination, selected an old English rule, which Mr. Lewis considers as a passably correct expression of good general averages, viz. : X = 2000pf. X = breaking load of tooth in pounds, <math>p = pitch, f = face. If a factor of safety of 10 be taken, this would give for safe working load W = 200pf. George B. Grant, in his Teeth of Gears, page 33, takes the breaking load at 3500pf, and, with a factor of safety of 10, gives W = 350pf. Nystrom's Pocket-Book, 20th ed., 1891, says: ''The strength and durability of cast-iron teeth require that they shall transmit a force of 80 lbs, per inch of pitch and per inch breadth of face.'' This is equivalent to W = 80pf, or only 404 of that given by the English rule.

only 40% of that given by the English rule. F. A. Halsey (Clark's Pocket Book) gives a table calculated from the formula H.P. =  $p/d \times \text{rpm.} + 850$ . Jones & Laughlins give H.P. =  $p/d \times \text{rpm.} + 550$ .

These formulæ transformed give W = 128pf and W = 218pf, respectively,

Unwin, on the assumption that the load acts on the corners of the teeth, derives a formula  $p = K \sqrt{W}$ , in which K is a coefficient derived from exis ting wheels, its values being: for slowly moving gearing not subject to much vibration or shock K = .04; in ordinary mill-gearing, running at greater speed and subject to considerable vibration, K = .05; and in wheels subjected to excessive vibration and shock, and in mortise gearing, K = .06. Reduced to the form  $W=C_0f$ , assuming that f=2p, these values of K give W=202pf, 300pf, and 139pf, respectively. Unwin also gives the following formula, based on the assumption that the

pressure is distributed along the edge of the tooth:  $p = K_1 \sqrt{\frac{p}{f}} \sqrt{W}$ ,

where  $K_1 =$  about .0707 for iron wheels and .0848 for mortise wheels when the breadth of face is not less than twice the pitch. For the case of f = 2p and the given values of  $K_1$  this reduces to W = 200pf and W = 130pf, respectively.

Box, in his Treatise on Mill Gearing, gives H.P. =  $\frac{12p^2f\sqrt{dn}}{1000}$ , in which n = number of revolutions per minute. This formula differs from the more modern formulæ in making the H.P. vary as  $p^2f$ , instead of as pf, and in this respect it is no doubt incorrect.

Making the H.P. vary as  $\sqrt{dn}$  or as  $\sqrt{v}$ , instead of directly as v, makes the velocity a factor of the working strength as in the Harkness and Lewis formulæ, the relative strength varying as  $\frac{\sqrt{v}}{v}$ , or as  $\frac{1}{\sqrt{v}}$ , which for different

velocities is as follows:

Speed of teeth in ft. per min., v = 100 200 300 600 1800 2400 Relative strength = 1 .707 .574 .408 .333 .289 .204

Showing a somewhat more rapid reduction than is given by Mr. Lewis. For the purpose of comparing different formulæ they may in general be reduced to either of the following forms:

$$\text{H.P.} = Cpfv, \quad \text{H.P.} = C_1pfd \times \text{rpm.}, \quad W = cpf,$$

in which p= pitch, f= face, d= diameter, all in inches; v= velocity in feet per minute, rpm. revolutions per minute, and C,  $C_1$  and c coefficients. The formulæ for transformation are as follows:

H.P. = 
$$\frac{Wv}{33000} = \frac{W \times d \times \text{rpm.}}{126,050}$$
;

$$W = \frac{33,000 \text{ H.P.}}{v} = \frac{126,050 \text{ H.P.}}{d \times \text{rpm.}} = 33,000 Cpf \; ; \; pf = \frac{\text{H.P.}}{Cv} = \frac{\text{H.P.}}{C_1 d \times \text{rpm.}} = \frac{W}{c}.$$

$$C_1 = .2618C; \quad c = 33,000C; \quad C = 3.82C_1, = \frac{c}{33.000}; \quad c = 126,050C_1.$$

In the Lewis formula C varies with the form of the tooth and with the speed, and is equal to sy + 33,000, in which y and s are the values taken from the table, and c = sy.

In the Harkness formula C varies with the speed and is equal to  $\sqrt{1+0.65V}$ 

(V being in feet per second), = \_\_\_\_.01517  $\sqrt{1 + .011v}$ .

In the Box formula C varies with the pitch and also with the velocity,

and equals  $\frac{12p\sqrt{d} \times \text{rpm.}}{1000v} = .02345 \frac{p}{\sqrt{v}}$ ,  $c = 33,000C = 774 \frac{p}{\sqrt{v}}$ . For v = 100 ft. per min. C = 77.4p; for v = 600 ft. per minute c = 31.6p. In the other formulæ considered C, C, and c are constants. Reducing the several formulæ to the form W = cpf, we have the following :

COMPARISON OF DIFFERENT FORMULÆ FOR STRENGTH OF GEAR-TEETH.

Safe working pressure per inch pitch and per inch of face, or value of c in

Torinula $W = cpj$ .	v = 100  ft.	v = 600  ft.
	per min.	per min.
Lewis: Weak form of tooth, radial flank, 12 teeth	c = 416	208
Medium tooth, inv. 15°, or cycloid, 27 teeth.	c = 800	400
Strong form of tooth, or cycloid, 300 teeth	c = 1200	600
Harkness: Average tooth		184
Box: Tooth of 1 inch pitch	c = 77.4	31.6
" " " 3 inches pitch	c = 232	95

Various, in which c is independent of form and speed: Old English rule, c=200; Grant, c=350; Nystron, c=80; Halsey, c=128; Jones & Laughlins, c=218; Unwin, c=262, 200, or 130, according to speed, shock,

and vibration.

The value given by Nystrom and those given by Box for teeth of small pitch are so much smaller than those given by the other authorities that they puten are so much smaller than those given by the other authorities that they may be rejected as having an entirely unnecessary surplus of strength. The values given by Mr. Lewis seem to rest on the most logical basis, the form of the teeth as well as the velocity being considered; and since they are said to have proven satisfactory in an extended machine practice, they may be considered reliable for gears that are so well made that the pressure bears along the face of the teeth instead of upon the corners. For rough ordinary work the old English rule W = 200p is probably as good as any, except that the figure 200 may be too high for weak forms of tooth and for high speeds.

The formula W = 200pf is equivalent to H.P.  $= \frac{pfd \times rpm}{630} = \frac{pfv}{165}$ , or

 $H.P. = .0015873pfd \times rpm. = .006063pfv.$ 

Maximum Speed of Gearing .- A. Towler, Eng'g, April 19, 1889, p. 388, gives the maximum speeds at which it was possible under favorable conditions to run toothed gearing safely as follows:

													r	t,	ber mi
Ordinary	cast-	iron	wheels												1800
Helical	66	66	6.6		Ċ										2400
Mortise	46	64	66												9400
Ordinary	anat	ctool	whoole		•		••••	• • • • •	• • • • • •	• • •	•••	• • • •	• • •	•••	9600
Helical	Cast-	SICCI	WILEGIS		•	• • • •	• • • •	• • • •	• • • •	• • •	• • •	•••	• • •	•••	2000
nencai					٠.		• • • •	• • • • •					• • •	٠.	5000
Special c	east-ir	on m	achine	-cut whe	e.	ls								٠.	3000

Prof. Coleman Sellers (Stevens Indicator, April, 1892) recommends that gearing be not run over 1200 ft. per minute, to avoid great noise. The Walker Mfg. Co., Cleveland, O., say that 2200 ft. per min. for iron gears and 8000 ft. for wood and iron (mortise gears) are excessive, and should be avoided if possible. The Corliss engine at the Philadelphia Exhibition (1876) had a fly-wheel 30 ft. in diameter running 35 rpm. geared into a pinion 12 ft.
diam. The speed of the pitch-line was 3300 ft. per min.

A Heavy Machine-cut Spur-gear was made in 1891 by the Walker Mfg. Co., Cleveland, O., for a diamond mine in South Africa, with dimensions as follows: Number of teeth, 192; pitch diameter, 30°6.66"; face, 30"; pitch, 6"; bore, 2"; diameter of hub, 9'2"; weight of hub, 15 tons; and total weight of gear, 66% tons. The rim was made in 12 segments, the joints of the segments being fastened with two bolts each. The spokes were bolted to the middle of the segments and to the hub with four bolts in each end.

Frictional Gearing,—In frictional gearing the wheels are toothless, Prof. Coleman Sellers (Stevens Indicator, April, 1892) recommends that

Frictional Gearing.—In frictional gearing the wheels are toothless, and one wheel drives the other by means of the friction between the two surfaces which are pressed together. They may be used where the power to be transmitted is not very great; when the speed is so high that toothed wheels would be noisy; when the shafts require to be frequently put into and out of gear or to have their relative direction of motion reversed; or when it is closed to the character that the character when it is not a considerable that the contraction of the when it is desired to change the velocity-ratio while the machinery is in mo-tion, as in the case of disk friction-wheels for changing the feed in machine tools.

Let P = the normal pressure in pounds at the line of contact by which wo wheels are pressed together, T = tangential resistance of the driven wheel at the line of contact, f = the coefficient of friction, V = the velocity of the pitch-surface in feet per second, and H.P. = horse-power; then T may be equal to or less than P; H.P. = TV+ 550. The value of f for

metal on metal may be taken at .15 to .30; for wood on metal .25 to .30; and for wood on compressed paper, .30. The tangential driving force T may be as high as 80 lbs, per luch width of face of the driving surface, but this is ac-

companied by great pressure and friction on the journal-bearings. In frictional grooved gearing circumferential wedge-shaped grooves are cut in the faces of two wheels in contact. If P = the force pressing the wheels together, and N = the normal pressure on all the grooves, P = N (sin a + f cos ab, in which 2a = the inclination of the sides of the grooves, and the maximum tangential available force T = fN. The inclination of the sides of the grooves to a plane at right angles to the axis is usually 30°.

Frictional Grooved Gearing.—A set of friction gears for transmitting 150 H.P. is on a steam-dredge described in Proc. Inst. M. E., July, 1883. Two grooved pinions of 54 in. diam., with 9 grooves of 134 in. pitch and angle of 40° cut on their face, are geared into two wheels of 1274 in diam. similarly grooved. The wheels can be thrown in and out of gear by levers operating eccentric bushes on the large wheel-shaft. The circumferential speed of the wheels is about 500 ft, per min. Allowing for engine-friction, if half the power is transmitted through each set of gears the tangential force at the rims is about 500 lbs., requiring, if the angle is 40° and the coefficient of friction 0.18, a pressure of 7524 lbs. between the wheels and pinion to prevent slipping.

The wear of the wheels proving excessive, the gears were replaced by spurgear wheels and brake-wheels with steel brake-bands, which arrangement has proven more durable than the grooved wheels. Mr. Daniel Adamson states that if the frictional wheels had been run at a higher speed the results would have been better, and says they should run at least 30 ft. ber second.

### HOISTING.

Approximate Weight and Strength of Cordage. (Boston and Lockport Block Co.)—See also pages 339 to 345.

Size in Circum- ference.	Size in Diam- eter.	Weight of 100 ft. Manila, in lbs.	Strength of Manila Rope, in lbs.		Size in Diam- eter.	Weight of 100 ft, Manila, in lbs.	Strength of Manila Rope, in lbs.
inch. 2 2!44 2!42 234 3 3!44 3!42 4 4!46	inch.  5/8  3/4  13/16  7/8  1 1/16  11/8  11/4  1 5/16  13/8  11/6	13 16 20 24 28 33 38 45 51 58 65	4,000 5,000 6,250 7,500 9,000 10,500 12,250 14,000 18,062 20,250	inch. 43/4 5 51/2 6 61/2 7 71/2 8 81/2 9	inch. 1 9/16 15/8 13/4 2 21/8 21/4 21/4 21/6 25/8 3	72 80 97 113 133 153 184 211 236 262	22,500 25,000 30,250 36,000 42,250 49,000 56,250 64,000 72,250 81,000

# Working Strength of Blocks. (B. & L. Block Co.)

Regular Mortise-blocks Single and Wide Mortise and Extra Heavy
Double, or Two Double Iron.
Single and Double, or Two Double,
strapped Blocks, will hoist about—
Iron-strapped Blocks, will hoist
about—

inch.	lbs.	inch.	lbs
F	250	8	2,000
6	350	10	6,000
7	600	12	12,000
8	1,200	14	24,000
9	2,000	16	36,000
10	4,000	18	50,000
12	10,000	20	90,000
14	16.000		

Where a double and triple block are used together, a certain extra proportioned amount of weight can be safely hoisted, as larger hooks are used.

# Comparative Efficiency in Chain-blocks both in Hoisting and Lowering.

(Tests by Prof. R. H. Thurston, Hoisting, March, 1892.)

	, , , , , ,											
	Work of Hoisting. Load of 2000 lbs.				Work of Lowering. Load of 2000 lbs., lowered 7 ft. in each case  Exclusive of Factor of Time. Inclusive of							
놽	on l	3.			Exclusi	ve or ra	ictor of	rime.	Tin	ne.		
Number of Block.	Waste by Friction per cent.	Actual Efficiency per cent.	Relative Effi- ciency.	Velocity-ratio	Pull on Hand Chain, lbs.	Length of Hand Chain, feet.	Work performed, ftlbs.	Relative Force expended by Operator.	Time in Min.	Relative Efficiency.		
1	20.50	79.50		32.50		227.	1,816	1.00		1.000		
2	68.00	32.00	.40	62.44		436.	6,104	3.33		.186		
3	69.00	31.00		30 00		196.	18,090	10.00		.050		
4	71.20	28.80	.36	28.00		168.	15,556	8.60		.035		
1 2 3 4 5 6	73.96			48.00								
6	75.66	24.34		53.00								
7	77.00			44.30								
- 8	81.03	18.97	.24	61.00	48.50	426.	20,000	11.60	3.75	.018		

No. 1 was Weston's triplex block; No. 3, Weston's differential; No. 4, Weston's imported. The others were from different makers, whose names are not given. All the blocks were of one-ton capacity.

Proportions of Hooks,—The following formulæ are given by Henry R. Towne, in his Treatise on Cranes, as a result of an extensive experimental and mathematical investi-

experimental and mathematical investigation. They apply to hooks of capacities from 250 bs. to 20,000 bs. Each size of hook is made from some commercial size of round iron. The basis in each case is, therefore, the size of iron of which the hook is to be made, indicated by A in the diagram. The dimension D is arbitrarily assumed. The other dithose which, while preserving a proper bearing-face on the interior of the hook for the ropes or chains which may be passed through it, give the greatest resistance to spreading and to ultimate rupture, which the amount of material in the original bar admits of. The symbol \( \Delta \) is used to indicate the nominal cap pacty of the hook in tons of 2000 lbs. The formulae which determine the lines of the other parts of the hooks of the several sizes are as follows, the measurements being all expressed in inches:

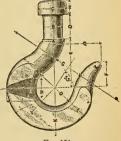


Fig. 164.

$$\begin{array}{lll} H = 1.08A & L = 1.05A \\ I = 1.33A & M = .50A \\ J = 1.20A & N = .85B - .16 \\ K = 1.13A & U = .866A \end{array}$$

The dimensions A are necessarily based upon the ordinary merchant sizes of round iron. The sizes which it has been found best to select are the following:

Capacity of hook:  $\frac{1}{16}$ :  $\frac{1}{16}$ :

Experiment has shown that hooks made according to the above formulæ will give way first by opening of the jaw, which, however, will not occur except with a load much in excess of the nominal capacity of the hook. This yielding of the hook when overloaded becomes a source of safety, as it constitutes a signal of danger which cannot easily be overlooked, and which must proceed to a considerable length before rupture will occur and the load be dropped.

#### POWER OF HOISTING-ENGINES.

required to raise a Load at a Given Horse-power Speed. - H.P. = Gross weight in lbs × speed in ft, per min. To this add 33,000

35,000 weight of case, rope, etc. In a shaft with two cases balancing each other use the net load + weight of core, rope, instead of the gross weight. To find the load which a given pair of engines will start.—Let A= area of cylinder in square inches, or total area of both cylinders, if there are two; P= mean effective pressure in cylinder in lbs. per sq. in, S= stroke of cylinder in inches; C= circumference of hoisting-drum in inches; C=lifted by hoisting-rope in lbs.; F = friction, expressed as a diminution of

the load. Then  $L = \frac{AP2S}{C} - F$ .

An example in Colly Engr., July, 1891, is a pair of hoisting-engines 24" X An example in Cot g Early, 3 day, 1937, 18 a pair to holsting-lengthes  $4^{\circ}$  do", drum 12 ft. diam., average steam-pre-sure in cylinder = 59,5 lbs.; A = 904.8; P = 59.5; S = 40; C = 452.4. Theoretical load, not allowing for friction, AP2S + C = 9589 lbs. The actual load that could just be lifted on trial was 1988 lbs., making friction loss F = 1001 lbs., or 20 + 1000 per cent of the actual load

lifted, or 16%% of the theoretical load.

The above rule takes no account of the resistance due to inertia of the load, but for all ordinary cases in which the acceleration of speed of the load, but for all ordinary cases in which the accordance t is easier eage is moderate, it is covered by the allowance for friction, etc. The resistance due to inertia is equal to the force required to give the load the velocity acquired in a given time, or, as shown in Mechanics, equal to the  $\frac{dr}{dT}$ , in which R = resistproduct of the mass by the acceleration, or R =

ance in lbs. due to inertia; W = weight of load in lbs.; V = maximum velocity in feet per second; T = time in seconds taken to acquire the velocity V;

g = 32.16.

Effect of Slack Rope upon Strain in Hoisting.—A series of tests with a dynamometer are published by the Trenton Iron Co., which show that a dangerous extra strain may be caused by a few inches of slack In one case the cage and full tubs weighed 11,300 lbs.; the strain when

rope. In one case the cage and thil this weighed 11,300 lbs.; the strain when the load was lifted gently was 11,525 lbs.; with 3 in. of slack chain it was 19,025 lbs, with 6 in. slack 25,750 lbs. and with 9 in. slack 27,950 lbs.

Limit of Depth for Hoisting.—Taking the weight of a cast-steel floisting-rope of 1½ inches diameter at 2 lbs. per running foot, and its breaking strength at 84,000 lbs., it should, theoretically, sustain itself until 42,000 feet long before breaking from its own weight. But taking the usual factor of safety of 7, then the safe working length of such a rope would be only 6000 feet. If a weight of 3 tons is now hung to the rope, which is equivalent to that of a cage of moderate capacity with its loaded cars, the maximum length at which such a rope could be used, with the factor of safety of 7, is 3000 feet, or

$$2x + 6000 = \frac{84,000}{7}$$
;  $\therefore x = 3000 \text{ feet.}$ 

This limit may be greatly increased by using special steel rope of higher This limit may be greatly increased by using special steel rope of higher strength, by using a smaller factor-of safety, and by using taper ropes, (See paper by H. A. Wheeler, Trans. A. I. M. E., xix. 107.)

Large Hoisting Records.—At a collery in North Derbyshire during the first week in June, 1890, 6309 tons were raised from a depth of 509 yards, the time of winding being from 7 a.m. to 3.30 p.m.

At two other Derbyshire pits, 170 and 140 yards in depth, the speed of winding and changing has been furught to such perfection that tubs are

drawn and changed three times in one minute. (Proc. Inst. M. E., 1890.)

At the Nottingham Colliery near Wilkesbarre, Pa., in Oct. 1891, 70,152 tons

At the Nottinghain Colinery hear winkesbarrie, ra., in Oct. 1597, 0,132 tons were shipped in 24,15 days, the average hoist per day being 1318 mine cars. The depth of hoist was 470 feet, and all coal came from one opening. The engines were fast motion, 22 × 48 inches, conical drums 4 feet 1 inch long, 7 feet diameter at small end and 9 feet at large end. (Eng'g News, Nov. 1891.)

Pneumatic Hoisting, (H. A. Wheeler, Trans, A. I. M. E., xix, 107.)—A pueumatic hoist was installed in 1876 at Epinac, France, consisting of two A pneumatic noist was installed in 1850 at Epinac, France, consisting of two continuous air-tight iron cylinders extending from the bottom to the top of the shaft. Within the cylinder moved a piston from which was hung the cage. It was operated by exhausting the air from above the piston, the lower side being open to the atmosphere. Its use vas discontinued on a count of the failure of the mine. Mr. Wheeler gives a description of the system, but criticises it as not being equal on the wholes to hoisting by steel ropes. Pneumatic hoisting-cylinders using compressed air have been used at

blast-furnaces, the weighted piston counterbalancing the weight of the day and the two being connected by a wire rope passing over a pulley-sheave above the top of the cylluder. In the more modern furnaces steam-eighte

hoists are generally used.

Counterbalancing of Winding-engines. (H. W. Hughes, Co-lumbia Coll. Qly.)—Engines running unbalanced are subject to enormous variations in the load; for let W = weight of cage and empty tubs, say 8270 lbs.; c = weight of coal, say 4480 lbs.; r = weight of hoisting rope, say 6000 lbs.; r'= weight of counterbalance rope hanging down pit, say 6000 lbs. The weight to be lifted will be:

If weight of rope is unbalanced. If weight of rope is balanced.

W + c - (W + r) or minus 1520 lbs. W + c + r' - (W + r)

That counterbalancing materially affects the size of winding-engines is shown by a formula given by Mr. Robert Wilson, which is based on the fact that the greatest work a winding-engine has to do is to get a given mass into a certain velocity uniformly accelerated from rest, and to raise a load the distance passed over during the time this velocity is being obtained.

Let W = the weight to be set in motion; one cage, coal, number of empty tubs on cage, one winding rope from pit head-gear to bottom, and one rope from banking level to bottom.

v = greatest velocity attained, uniformly accelerated from rest;

v = g reactive 32.2; g = g ravity = 32.2; t = t time in seconds during which v is obtained; L = unbalanced load on engine;

R = ratio of diameter of drum and crank circles:

P = average pressure of steam in cylinders;

N = number of cylinders;

S =space passed over by crank-pin during time t;

S = space present over by crank, to the distance passed through by crank, to the distance passed through by the piston during the time t;

A = area of one cylinder, without margin for friction. To this an addition for friction, etc., of engine is to be made, varying from 10

to 30% of A.

1st. Where load is balanced,

$$A = \frac{\left\{ \left( \frac{Wv^2}{2gt} \right) + \left( L\frac{vt}{2} \right) \right\} R}{PNSC}$$

2d. Where load is unbalanced:

The formula is the same, with the addition of another term to allow for the variation in the lengths of the ascending and descending ropes. In this case

 $h_1=$  reduced length of rope in t attached to ascending cage;  $h_2=$  increased length of rope in t attached to descending cage; w= weight of rope per foot in pounds. Then

$$A = \underbrace{\left\lceil \left(\frac{Wv^2}{2gt}\right) + \left\{ \left(\frac{vt}{L^2}\right) - \frac{h_1w + h_2w}{2} \right\} \right] \! R}_{PNSC.}$$

Applying the above formula when designing new engines, Mr. Wilson found that 30 inches diameter of cylinders would produce equal results, when balanced, to those of the 36-inch cylinder in use, the latter being unbalanced.

Counterbalancing may be employed in the following methods:

(a) Tapering Rope.—At the initial stage the tapering rope enables us to wind from greater depths than is possible with ropes of uniform section. The thickness of such a rope at any point should only be such as to safely bear the load on it at that point.

With tapering ropes we obtain a smaller difference between the initial and final load, but the difference is still considerable, and for perfect equalization of the load we must rely on some other resource. The theory of taper ropes is to obtain a rope of uniform strength, thinner at the cage end where the weight is least, and thicker at the drum end where it is greatest.

the weight is least, and thicker at the drum end where it is greatest.

(b) The Counterpoise System consists of a heavy chain working up and down a staple pit, the moit of the properties of the system as a special small drum placed on the same axis as the winding drum. It is so arranged that the chain hangs in full length down the staple pit at the commencement of the winding; in the centre of the run the whole of the chain rests on the bottom of the pit, and, finally, at the end of the winding the counterpoise has been rewound upon the small drum, and is in the same condition as it was at the commencement.

(c) Loaded-wagon System. — A plan, formerly much employed, was to have a loaded wagon running on a short incline in place of this heavy chain; the rope actuating this wagon being connected in the same manner as the above to a subsidiary drum. The incline was constructed steep at the commencement, the inclination gradually decreasing to nothing. At the beginning of a wind the wagon was at the top of the incline, and during a portion of the run gradually passed down it till, at the meet of cages, no pull was exerted on the engine—the wagon by this time being at the bottom. In the latter part of the wind the resistance was all against the engine, owing to its having to pull the wagon up the incline, and this resistance increased from nothing at the meet of cages to its greatest quantity at the conclusion

(d) The Endless-rope System is preferable to all others, if there is sufficient sump room and the shaft is free from tubes, cross timbers, and other impediments. It consists in placing beneath the cages a tail rope, similar in diameter to the winding rope, and, after conveying this down the pit, it is

attached beneath the other cage.

(e) Fiat Ropes Coiling on Reels—This means of winding allows of a certain equalization, for the radius of the coil of tascending rope continues to increase, while that of the descending one continues to diminish. Consequently, as the resistance decreases in the ascending load the leverage increases, and as the power increases in the other, the leverage diminishes. The variation in the leverage is a constant quantity, and is equal to the thickness of the rope where it is wound on the drum.

By the above means a remarkable uniformity in the load may be obtained, the only objection being the use of flat ropes, which weigh heavier and only last about two thirds the time of round ones.

(f) Conical Drums.—Results analogous to the preceding may be obtained by using round ropes coiling on conical drums, which may either be smooth, with the successive coils lying side by side, or they may be provided with a spiral groove. The objection to these forms is, that perfect equalization is not obtained with the conical drums unless the sides are very steep, and consequently there is great risk of the rope slipping; to obviate this, scroll drums were proposed. They are, however, very expensive, and the lateral displacement of the winding rope from the centre line of pulley becomes

very great, owing to their necessary large width.

(g) The Koepe System of Winding.—An iron pulley with a single circular groove takes the place of the ordinary drum. The winding rope passes from one cage, over its head-gear pulley, round the drum, and, after pass-

ing over the other head-gear pulley, is connected with the second cage. The winding rope thus encircles about half the periphery of the drum in the same manner as a driving-belt on an ordinary pulley. There is a balance rope beneath the cages, passing round a pulley in the sump; the arrangement may be likened to an endless rope, the two cages being simply points of attachment.

#### BELT-CONVEYORS.

Grain-elevators. - American Grain-elevators are described in a paper by E. Lee Heidenreich, read at the International Engineering Congress at Chicago (Trans. A. S. C. E. 1880.). See also Trans. A. S. M. E. vil, 600. **Bands for earrying Grain.** — Flexible-rubber bands are exten-

sively used for carrying grain in and around elevators and warehouses. article on the grain-storage warehouses of the Alexandria Dock, Liverpool (Proc. Inst. M. E., July, 1891), describes the performance of these bands, aggregating three miles in length. A band 16½ inches wide, 1270 feet long, running 9 to 10 feet per second has a carrying capacity of 50 tons per hour. See also paper on Belts as Grain Conveyors, by T. W. Hugo, Trans. A. S. M. E., vi. 400.

Carrying-bands or Belts are used for the purpose both of sorting coal and of removing impurities. These carrying-bands may be said to be confined to two descriptions, namely, the wire belt, which consists of an endless length of woven wire; and the steel-plate belt, which consists of two or three endless chains, carrying steel plates varying in width from 6 inches to 14 inches. (Proc. Inst. M. E., July, 1890.)

#### CRANES.

Classification of Cranes. (Henry R. Towne, Trans. A. S. M. E., iv. 288. Revised in *Hoisting*, published by The Yale & Towne Mfg. Co.)
A Hoist is a machine for raising and lowering weights. A Crane is a

hoist with the added capacity of moving the load in a horizontal or lateral direction.

Cranes are divided into two classes, as to their motions, viz., Rotary and Rectilinear, and into four groups, as to their source of motive power, viz.:

Hand.—When operated by manual power.

Power.—When driven by power derived from line shafting.
Steam, Electric, Hydraulic, or Pneumatic.—When driven by an engine or motor attached to the crane, and operated by steam, electricity, water, or air transmitted to the crane from a fixed source of supply.

Locomotive.—When the crane is provided with its own boiler or other generator of power, and is self-propelling; usually being capable of both rotary and rectilinear motions.

Rotary and Rectilinear Cranes are thus subdivided:

#### ROTARY CRANES.

Swing-cranes.—Having rotation, but no trolley motion.

 (2) Jib-cranes.—Having rotation, and a trolley travelling on the jib.
 (3) Column-cranes.—Identical with the jib-cranes, but rotating around a fixed column (which usually supports a floor above).

(4) Pillar-cranes. - Having rotation only; the pillar or column being supported entirely from the foundation.

(5) Pillar Jib-cranes.—Identical with the last, except in having a jib and trolley motion.

(6) Derrick-cranes.-Identical with jib-cranes, except that the head of the

mast is held in position by guy-rods, instead of by attachment to a roof or ceiling.
(7) Walking-cranes.—Consisting of a pillar or jib-crane mounted on wheels

and arranged to travel longitudinally upon one or more rails.

(8) Locomotive-cranes.—Consisting of a pillar crane mounted on a truck, and provided with a steam-engine capable of propelling and rotating the

crane, and of hoisting and lowering the load.

#### RECTILINEAR CRANES.

(9) Bridge-cranes.-Having a fixed bridge spanning an opening, and a trolley moving across the bridge.

(10) Tram-cranes.-Consisting of a truck, or short bridge, travelling lon-

gitudinally on overhead rails, and without trolley motion. (11) Travelling-cranes.—Consisting of a bridge moving longitudinally on overhead tracks, and a trolley moving transversely on the bridge.

(12) Gantries.-Consisting of an overhead bridge, carried at each end by a trestle travelling on longitudinal tracks on the ground, and having a trolley moving transversely on the bridge.

(13) Rotary Bridge-cranes.—Combining rotary and rectilinear movements and consisting of a bridge pivoted at one end to a central pier or post, and supported at the other end on a circular track; provided with a trolley moving transversely on the bridge.

For descriptions of these several forms of cranes see Towne's "Treatise

on Cranes.

Stresses in Cranes.—See Stresses in Framed Structures, p. 440, ante. Position of the Inclined Brace in a Jib-crane.—The most economical arrangement is that in which the inclined brace intersects the iib at a distance from the mast equal to four fifths the effective radius of

the crane. (Hoisting.)

A Large Travelling-crane, designed and built by the Morgan Engineering Co, Alliance, O., for the 12-inch-gun shop at the Washington Navy Yard, is described in American Machinist, June 12, 1890. Capacity, 150 net tons; distance between centres of inside rails, 59 ft. 6 in.; maximum eross travel, 44 ft. 2 in.; effective lift, 40 ft.; four speeds for main hoist, 1, 2, 4, and 8 ft. per min.; loads for these speeds, 150, 75, 37½, and 18¾ tons respectively; traversing speeds of trolley on bridge, 25 and 50 ft, per minute; speeds of bridge on main track, 30 and 60 ft. per minute. Square shafts are employed for driving

A 150-ton Pillar-crane was erected in 1893 on Finnieston Quay, Glasgow. The jib is formed of two steel tubes, each 39 in. diam. and 30 ft. long. The radius of sweep for heavy lifts is 65 ft. The jib and its load are counterbalanced by a balance-box weighted with 100 tons of iron and steel punchings. In a test a 130-ton load was lifted at the rate of 4 ft. per minute, and a complete revolution made with this load in 5 minutes. Eng'g News,

July 20, 1893.

Compressed-air Travelling-cranes. -Compressed-air overhead travelling-cranes have been built by the Lane & Bodley Co., of Cincinnati. They are of 20 tons nominal capacity, each about 50 ft. span and 400 ft. length of travel, and are of the triple-motor type, a pair of simple reversing-engines being used for each of the necessary operations, the pair of engines for the being used to the pair for the trolley travel being each 5-inch bore by 7-inch stroke, while the pair for hoisting is 7-inch bore by 9-inch stroke, alr is furnished by a compressor having steam and air cylinders each 10-in. diam. and 12-in. stroke, which with a boiler-pressure of about 80 pounds gives an air-pressure when required of somewhat over 100 pounds. The air-compressor is allowed to run continuously without a governor, the speed being regulated by the resistance of the air in a receiver. From a pipe extending from the receiver along one of the supporting trusses communication is continuously maintained with an auxiliary receiver on each traveller by means of a oneinch hose, the object of the auxiliary receiver being to provide a supply of air near the engines for immediate demands and independent of the hose connection, which may thus be of small dimension. Some of the advantages said to be possessed by this type of crane are: simplicity; absence of all moving parts, excepting those required for a particular motion when that motion is in use; no danger from fire, leakage, electric shocks, or freezing; case of repair; variable speeds and reversal without gearing; almost entire absence of noise; and moderate cost.

Quay-cranes. - An illustrated description of several varieties of stationary and travelling cranes, with results of experiments, is given in a paper on Quay-cranes in the Port of Hamburg by Chas. Nehls, Trans. A. S. C. B., Chicago Meetime, 1893.

E., Chicago Meeting, 1893.

Hydraulic Cranes, Accumulators, etc.—See Hydraulic Pressure Transmission, page 616, ante.

Electric Cranes.-Travelling-cranes driven by electric motors have largely supplanted cranes driven by square shafts or flying-ropes. Each of the three motions, viz., longitudinal, traversing and hoisting, is usually accomplished by a separate motor carried upon the crane.

### WIRE-ROPE HAULAGE.

Methods for transporting coal and other products by means of wire rope, though varying from each other in detail, may be grouped in five classes:

1. The Self-acting or Gravity Inclined Plane.

II. The Simple Engine-plane.

III. The Tail-rope System.
IV. The Endless-rope System.
V. The Cable Tramway.

The following brief description of these systems is abridged from a pamphlet on Wire-rope Haulage, by Wm. Hildenbrand, C.E., published by John A. Roebling's Sons Co., Trenton, N. J.

I. The Self-acting Inclined Plane.—The motive power for the self-acting inclined plane is gravity; consequently this mode of transporting coal finds application only in places where the coal is conveyed from a higher to a lower point and where the plane has sufficient grade for the loaded descending cars to raise the empty cars to an upper level.

At the head of the plane there is a drum, which is generally constructed of wood, having a diameter of seven to ten feet. It is placed high enough to allow men and cars to pass under it. Loaded cars coming from the pit are either singly or in sets of two or three switched on the track of the plane, and their speed in descending is regulated by a brake on the drum.

Support and represent the state of the support of t 30 feet, steeper planes requiring less rollers than those with easy grades. Considering only the reduction of friction and what is best for the preservation of rope, a general rule may be given to use rollers of the greatest possible diameter, and to place them as close as economy will permit. The smallest angle of inclination at which a plane can be made self-acting

will be when the motive and resisting forces balance each other. The motive forces are the weights of the loaded car and of the descending rope. The resisting forces consist of the weight of the empty car and ascending rope, of the rolling and axle friction of the cars, and of the axle friction of the supporting rollers. The friction of the drun, stiffness of rope, and resistance of air may be neglected. A general rule cannot be given, because a change in the length of the plane or in the weight of the cars changes the proportion of the forces; also, because the coefficient of friction, depending on the condition of the road, construction of the cars, etc., is a very uncertain factor

For working a plane with a 54-inch steel rope and lowering from one to four pit cars weighing empty 1400 lbs. and loaded 4000 lbs., the rise in 100 feet necessary to make the plane self-acting will be from about 5 to 10 feet, decreasing as the number of cars increase, and increasing as the length of plane increases.

A gravity inclined plane should be slightly concave, steeper at the top than at the bottom. The maximum deflection of the curve should be at an inclination of 45 degrees, and diminish for smaller as well as for steeper

inclinations.

11. The Simple Engine-plane.—The name "Engine-plane" is given to a plane on which a load is raised or lowered by means of a single wire rope and stationary steam-engine. It is a cheap and simple method of conveying coal underground, and therefore is applied wherever circumstances permit it.

Under ordinary conditions such as prevail in the Pennsylvania mine region, a train of twenty-five to thirty loaded cars will descend, with reasonable velocity, a straight plane 5000 feet long on a grade of 134 feet in 100, while it would appear that 21/4 feet in 100 is necessary for the same number of empty cars. For roads longer than 5000 feet, or when containing sharp

curves, the grade should be correspondingly larger.

III. The Tail-rope System .- Of all methods for conveying coal underground by wire rope, the tail-rope system has found the most applica-tion. It can be applied under almost any condition. The road may be straight or curved, level or undulating, in one continuous line or with side branches. In general principle a tail-rope plane is the same as an engineplane worked in both directions with two ropes. One rope, called the "main phanesotken would understood a state of full cars outward; the other, called the "tall-rope," is necessary to take back the empty set, which on a level or undulating road cannot return by gravity. The two drums may be located at the opposite ends of the road, and driven by separate engines, but more frequently they are on the same shaft at one end of the plane. In the first case each rope would require the length of the plane, but in the second case the tall rope must be twice as long, being led from the drum around a sheave at the other end of the plane and back again to its starting-

point. When the main rope draws a set of full cars out, the tail-rope drum point. When the main rope draws a set of full cars out, the tail-rope drum runs loose on the shaft, and the rope, being attached to the rear car, unwinds itself steadily. Going in, the reverse takes place. Each drum is provided with a brake to check the speed of the train on a down grade and prevent its overrunning the forward rope. As a rule, the tail rope is strained less than the main rope, but in cases of heavy grades dipping outward it is possible that the strain in the former may become as large, or even larger, than in the latter, and in the selection of the sizes reference should be had to this circumstance.

IV. The Endless-rope System. - The principal features of this system are as follows:

1. The rope, as the name indicates, is endless.

2. Motion is given to the rope by a single wheel or drum, and friction is obtained either by a grip-wheel or by passing the rope several times around

the wheel.

3. The rope must be kept constantly tight, the tension to be produced by artificial means. It is done in placing either the return-wheel or an extra tension wheel on a carriage and connecting it with a weight hanging over a pulley, or attaching it to a fixed post by a screw which occasionally can be shortened.

4. The cars are attached to the rope by a grip or clutch, which can take hold at any place and let go again, starting and stopping the train at will,

without stopping the engine or the motion of the rope.

5. On a single-track road the rope works forward and backward, but on a double track it is possible to run it always in the same direction, the full

cars going on one track and the empty cars on the other,

This method of conveying coal, as a rule, has not found as general an introduction as the tail-rope system, probably because its efficacy is not so apparent and the opposing difficulties require greater mechanical skill and apparent and the opposing difficulties require greater mediatineal some aim more complicated appliances. Its advantages are, first, that it requires one third less rope than the tail-rope system. This advantage, however, is partially counterbalanced by the circumstance that the extra tension in the rope requires a heavier size to move the same load than when a main tail rope are used. The second and principal advantage is that it is possible to start and stop trains at will without signalling to the engineer. On the other hand, it is more difficult to work curves with the endless system, and still more so to work different branches, and the constant stretch of the rope under tension or its elongation under changes of temperature frequently causes the rope to slip on the wheel, in spite of every attention,

causing delay in the transportation and injury to the rope.

V. Wire-rope Tramways.—The methods of conveying products on a suspended rope tramway find especial application in places where a mine is located on one side of a river or deep ravine and the loading station on the other. A wire rope suspended between the two stations forms the track on which material in properly constructed "carriages" or "buggies" is transported. It saves the construction of a bridge or trestlework, and is practical for a distance of 2000 feet without an intermediate support,

There are two distinct classes of rope tramways:

1. The rope is stationary, forming the track on which a bucket holding the material moves forward and backward, pulled by a smaller endless

wire rope.

2. The rope is movable, forming itself an endless line, which serves at

the same time as supporting track and as pulling rope.

Of these two the first method has found more general application, and is especially adapted for long spans, steep inclinations, and heavy loads. The second method is used for long distances, divided into short spans, and is only applicable for light loads which are to be delivered at regular intervals.

For detailed descriptions of the several systems of wire-rope transportation, see circulars of John A. Roebling's Sons Co., The Trenton Iron Co., and

tion, see circulars of John A. Roebling's Sons Co., The Trenton Iron Co., and other wire-rope manufacturers. See also paper on Two-rope Haulage Systems, by R. Van A. Norris, Trans. A. S. M. E., xii. 626.

In the Bleichert System of wire-rope tramways, in which the track rope is stationary, loads of 1000 pounds each and upward are carried. While the average spans on a level are from 150 to 200 feet, in crossing rivers, ravines, etc., spans up to 1500 feet are frequently adopted. In a tramway on this system at Granite, Montana, the total length of the line is 9750 feet, with a fall of 1225 feet. The descending loads, amounting to a constant weight of about 11 tons, develop over 14 horse-power, which is sufficient to haul the empty buckets as well as about 50 tons of supplies per day up the line, and

also to run the ore crusher and elevator. It is capable of delivering 250 tops of material in 10 hours.

# SUSPENSION CABLEWAYS OR CABLE HOISTS.

In quarrying, rock-cutting, stripping, piling, dam-building, and many other operations where it is necessary to hoist and convey large individual loads economically, it frequently happens that the application of a system of derricks is impracticable, by reason of the limited area of their efficiency and the room which they occupy.

To meet such conditions cable hoists are adapted, as they can be efficiently operated in clear spans up to 1500 feet, and in lifting individual loads up to 15 tons. Two types are made—one in which the hoisting and conveying are done by separate running ropes, and the other applicable only to inclines, in which the carriage descends by gravity, and but one running rope is required. The moving of the carriage in the former is effected by means of an endless rope, and these are commonly known as "endless-rope" cable-hoists to distinguish them from the latter, which are termed "inclined" cable-hoists.

The general arrangement of the endless-rope cable-hoists consists of a main cable passing over towers, A frames or masts, as may be most convenient, and anchored firmly to the ground at each end, the requisite tension in the cable being maintained by a turnbuckle at one anchorage.

Upon this cable travels the carriage, which is moved back and forth over the line by means of the endless rope. The hoisting is done by a separate rope, both ropes being operated by an engine specially designed for the purpose, which may be located at either end of the line, and is constructed in such a way that the hoisting-rope is coiled up or paid out automatically as the carriage is moved in and out. Loads may be picked up or discharged at any point along the line. Where sufficient inclination can be obtained in the main cable for the carriage to descend by gravity, and the loading and unloading is done at fixed points, the endless rope can be dispensed with. The carriage, which is similar in construction to the carriage used in the endless-rope cableways, is arrested in its descent by a stop-block, which may be clamped to the main cable at any desired point, the speed of the descending carriage being under control of a brake on the engine-drum.

Stress in Hoisting-ropes on Inclined Planes.
(Trenton Iron Co.)

Rise per 100 ft. horizontal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.	Rise per 100 ft. horizontal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.	Rise per 100 ft. horizoutal.	Angle of inclination.	Stress in lbs. per ton of 2000 lbs.
ft. 5 10 15 20 25 30 35 40 45 50	2° 52′ 5° 43′ 8° 32′ 11° 10′ 14° 03′ 16° 42′ 19° 18′ 21° 49′ 24° 14′ 26° 34′	140 240 336 432 527 613 700 782 860 933	ft. 55 60 65 70 75 80 85 90 95	28° 49′ 30° 58′ 33° 02′ 35° 00′ 36° 53′ 38° 40′ 40° 22′ 42° 00′ 43° 32′ 45° 00′	1003 1067 1128 1185 1288 1287 1332 1375 1415 1450	ft. 110 120 130 140 150 160 170 180 190 200	47° 44′ 50° 12′ 52° 26′ 54° 28′ 56° 19′ 58° 00′ 59° 33′ 60° 57′ 62° 15′ 63° 27′	1516 1573 1620 1663 1699 1730 1758 1782 1804 1822

The above table is based on an allowance of 40 bs, per ton for rolling friction, but an additional allowance must be unade for stress due to the weight of the rope proportional to the length of the plane. A factor of safety of 5 to 7 should be taken.

In hoisting the slack-rope should be taken up gently before beginning the lift, otherwise a severe extra strain will be brought on the rope.

The best rope for inclined planes is composed of six strands of seven wires each, laid about a hempen centre. The wires are much coarser than those of the 114-wire rope of the same diameter, and for this reason the 42-wire rope is better adapted to withstand the rough usage and surface wear encountered upon inclined planes.

A Double-suspension Cableway, carrying loads of 26 tons, erected near

Williamsport, Pa., by the Trenton Iron Co., is described by E. G. Spilsbury in Trans. A. I. M. E. xx. 766. The span is 733 feet, crossing the Susquehanna in Trans, A. I. M. E. xx. 766. The span is 735 feet, crossing the Susquehanna River. Twojsteel cables, each 2 in. diam., are used. On these cables runs a carriage supported on four wheels and moved by an endless cable 1 inch in diam. The load consists of a cage carrying a railroad-car loaded with lumber, the latter weighing about 12 tons. The power is furnished by a 50-H.P.

ber, the latter weighing about 12 tons. The power is furnished by a 50-H.P. engine, and the trip across the river is made in about three minutes. A hoisting cableway on the endless-rope system, erected by the Lidger, wood Mfg. Co, at the Austin Dam, Texas, had a single span 1350 ft, in length, with main cable 2½ in, diam, and hoisting-rope 1¾ in, diam. Loads of 7 to 8 tons were handled at a speed of 600 to 800 ft, per minute.

Tension required to Prevent Slipping of Wire on Drum. (Trenton Iron Co.)—The amount of artificial tension to be applied in an endless rope to prevent slipping on the driving-drum depends on the character of the drum, the condition of the rope and number of laps which it makes. If T and S represent respectively the tensions in the taut and slack lines of the rope; W the necessary weight to be applied to the tail-sheave; R, the resistance of the cars and rope, allowing for friction; n, the number of half-laps of the rope on the driving-drum; and f, the coefficient of friction, the following relations must exist to prevent slipping:

$$T=Se^{fn\pi}, \quad W=T+S, \quad \text{and} \quad R=T-S;$$
 from which we obtain 
$$W=\frac{e^{fn\pi}+1}{e^{fn\pi}-1}R,$$

in which e = 2.71828, the base of the Naperian system of logarithms. The following are some of the values of f:

	Dry.	Wet.	Greasy.
Rope on a grooved iron drum	.120	.085	.070
Rope on wood-filled sheaves	235	.170	.140
Rope on rubber and leather filling	.495	.400	,205

The values of the coefficient  $\frac{e^{fn\pi}+1}{e^{fn\pi}-1}$ , corresponding to the above values

of f, for one up to six half-laps of the rope on the driving-drum or sheaves. are as follows:

f	$n={ m Number}$ of Half-laps on Driving-wheel.								
	1	2	3	4	5	6			
.070	9.130	4.623	3,141	2.418	1,999	1.729			
.085	7.536	3.833	2.629	2.047	1.714	1.505			
.120	5.345	2.777	1.953	1.570	1.358	1.232			
.140	4.623	2.418	1.729	1.416	1.249	1.154			
.170	3.833	2.047	1.505	1.268	1.149	1.085			
.205	3.212	1.762	1.338	1.165	1.083	1.043			
.235	2.831	1.592	1.245	1.110	1.051	1.024			
.400	1.795	1.176	1.047	1.013	1.004	1.001			
.495	1.538	1.093	1.019	1.004	1.001				

The importance of keeping the rope dry is evident from these figures. When the rope is at rest the tension is distributed equally on the two lines of the rope, but when running there will be a difference in the tensions of

of the rope, but when running there will be a difference in the tensions of the taut and slack lines equal to the resistance, and the values of T and S may be readily computed from the foregoing formulæ. Taper Ropes of Uniform Tensile Strength,—Prof. A. S. Herschel in The Engineer, April, 1880. p. 267, gives an elaborate mathematical investigation of the problem of making a taper hoisting-rope of uniform tensile strength at every point in its length. Mr. Charles D. West, commenting on Prof. Herscher's paper, gives a similar solution, and derives therefrom the following formula, based on a breaking strain of 80,000 lbs. per sq. in. of the rope, core included, with a factor of safety of 10:

$$F = 3680[\log G - \log g]; \log G = \frac{F}{3680} + \log g;$$

in which F = length in fathoms, and G and g the girth in inches at any two sections F fathoms apart,

Example.—Let it be required to find the dimensions of a steel-wire rope to draw 6720 lbs.—cage, trams, and coal—from a depth of 400 fathoms. Area of section at lower end = 6720 + 8000 = .84 sq. in.; therefore girth =  $3\frac{1}{2}$  in. at bottom.

 $Log G = 400 \div 3680 + log 3.25 = .10869 + .51188 = .62057;$ 

therefore G = 4.174, or, say, 43/16 in. girth at top.

The equations show that the true form of rope is not a regular taper or truncated cone, but follows a logarithmic curve, the girth rapidly increasing towards the upper end.

## Relative Effect of Various-sized Sheaves or Drums on the Life of Wire Ropes.

(Thos. E. Hughes, Coll'y Eng., April, 1893.) CAST-STEEL ROPES FOR INCLINES.

Made of 6 strands, of 7 wires each, laid around a hemp core,

Diam, of Rope in	Diame	Diameters of Sheaves or Drums in feet, showing percentages of life for various diameters.									
inches.	100%.	90%.	80%.	75%.	60%.	50%.	25%.				
1½ 1¾ 1¾ 1¼	16 14 12	14 12 10	12 10 8	11 8.5 7.25	9 7 6.5	7 6 5.5	4.75 4.5 4.25				
11/8 1 7/8	10 8.5 7.75	*8.5 7.75 7	7.75 6.75 6.25	7 6 5.75	6 5 4.5	5 4.5 3.75	3.75 3.25				
3/4 5/8 1/6	7 6 5	6.25 5.25 4.5	5.5 4.5 4	5 4 3,5	4.25 3.25 2.75	3.5 3 2.25	2.75 2.5 1.75				

The use of iron ropes for inclines has been generally abandoned, steel ropes being more satisfactory and economical.

CAST-STEEL HOISTING-ROPES.

Made of 6 strands, of 19 wires each, laid around a hemp core.

Diam. of Rope in	Diame	Diameters of Sheaves or Drums in feet, showing percentages of life for various diameters.									
inches.	100%.	90%.	80%.	75%.	60%.	50%.	25%.				
11/6 13/8 11/4 11/8 1 1/8 1 1/8 1/8 1/8 1/8 1/8 1/8 1/	14 12 10 9 8 7.5 5.5 4.5	12 10 8.5 7.5 7 6.75 4.5	10 8 7.5 6.5 6 5.75 4 3.75	8.5 7 6.75 6 5.5 5 3.75 3.25 2.75	7 6 5.5 5 4.5 4.25 3.25 3 2.25	6 5.25 5 4.5 4.5 4.5 3.5 3 2.5 2.1,5	4.5 4 25 4 3.75 3.50 3 2.25 2				

# WIRE-ROPE TRANSMISSION.

The following data and formulæ are taken from a paper by Wm. Hewitt, of the Trenton Iron Co., 1890. (See also circulars of John A. Roebling's Sons Co., Trenton, N. J.; "Transmission of Power by Wire Ropes," by A. W. Stahl, Van Nostrand's Soience Series No. 28; and Reuleaux's Constructor.)

The Section of Wire Hope best suited, under ordinary conditions, for the transmission of power is composed of 6 strands of 7 wires each, laid together about a hempen centre. Ropes of 12 and 19 wires to the strand are also used. They are more flexible, and may be applied with advantage under conditions which do not allow the use of large transmission wheels, but admit of high speed. They are not as well adapted to stand surface wear, however, on account of the smaller size of the wires.

The Driving-wheels (Fig. 165) are usually of cast iron, and are made as light as possible consistent with the requisite strength. Various materials have been used for filling the bot-

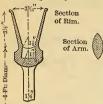


Fig. 16a.

materials have been used for filling the bottom of the groove, such as tarred oakum, juteyarn, hard wood, Indiarnibberand leather. The filling which gives the best satisfaction, however, consists of segments of leather and blocks of India-rubber, soaked in tar and packed alternately in the groove, and then turned to a true surface.

In long spans, intermediate supporting wheels are frequently used, and it is usually sufficient to support only the slack or follow ing side of the rope; but whatever the distance that the power is transmitted, the driving side of the rope will require a less number of supports than the slack side. The sheaves sup-porting the driving side, however, should in all cases be of equal diameter with the drivingwheels. With the slack side smaller wheels

may be used, but their diameter should not be less than one half that of the driving-sheaves.

The system of carrying sheaves may generally be replaced to advantage by that of intermediate stations. The rope thus, instead of running the whole length of the transmission, runs only from one station to the other; and it is advisable to make the stations equidistant, so that a rope may be kept on hand, ready spliced, to put on the wheels of any span, should its rope give out. This method is to be preferred where there is sometimes a jerking motion to the rope, as it prevents sudden movements of this kind from being transmitted over the entire line.

Gross horse-power transmitted =  $N_0 = .0003702D^2v\left(k - \frac{ED}{18R}\right)$ , in which

D= diameter of rope in inches (= 9 times diameter of single wire); v= velocity of rope in feet per second; k= safe stress per square inch on wires for iron \$2,700 lbs.; E= modulus of elasticity = 28,500,000 for iron; R= radius of driving-wheels in inches. The term  $\frac{ED}{18R}=$  the stress per square

inch due to bending of wires around sheaves

ch due to bending or wiles around sneaves. Loss due to centrifugal force =  $N_1 = .0000124D^2v^3$ ; Loss due to journal friction of driving-wheels =  $N_2 = .0000045(1650N_0 + vv)$ ; "intermediate-wheels = .0000045(W + v)v; in which W = total weight of rope; w = weight of wheel and axle.

Net horse-power transmitted,

$$N = N_0 - N_1 - N_2 = D^2 v \left[ .0003675 \left( k - \frac{ED}{18R} \right) - .0000424 v \right] - .0000045 w v.$$

For a maximum value of N the diameter of the wheels should be approximately from 185 to 192 times the diameter of the rope, and for the latter ratio of diameters an approximate formula for the actual horse-power transmitted is  $N=3~0148D^3V$ , in which V= number of revolutions of wheels per minute.

The proper deflections when the rope is at rest are obtained from the formula Deflection = .00005765 span2, and are as follows:

50 100 150 200 250 300 350 400 450 134" 7" 1' 3½" 2' 358" 3' 7½" 5' 2½" 7' 58" 9' 258" 11 '8" Span in feet... Deflection . . . .

It has been found in practice that when the deflection of the rope at rest is less than 3 inches the transmission cannot be effected with satisfaction, and shafting or belting is to be preferred. This deflection corresponds to a span of about 54 feet. It is customary to make the under side of the rope the driving side. The maximum limit of span is determined by the maximum deflection that may be given to the upper side of the rope when in motion. Assuming that the clearance between the upper and lower sides of the rope should not be less than two feet, and that the wheels are at least 10 feet in diameter, we have a maximum deflection of the upper side of 8 feet, which corresponds to a span of about 370 feet.

Much greater spans than this are practicable, in cases where the contour of the ground is such that the upper side of the rope may be made the driver, as in crossing gullies or valleys, and there is nothing to interfere with obtaining the proper deflections. Some very long transmissions of power have been effected in this way without an intervening support. There is one at Lockport, N. Y., for instance, with a clear span of about 1700 feet.

In a later circular of the Trenton Iron Co. (1892) the above figures are somewhat modified, giving lower values for the power transmitted by a given

rope, as follows:

The proper ratio between the diameters of rope and sheaves is that which will permit the maximum working tension to be obtained without overstraining the wires in bending. For rope of 7-wire strands this ratio is about 1:50; for rope of 12-wire strands, 1:15; and for rope of 19-wire strands, 1:16; and for rope of 19-wire strands, 1:90; which gives the following minimum diameter of sheaves, in inches, corresponding to maximum efficiency.

Diam. rope, in inches.	1/4	5/16	3/8	7/16	1/2	9/16	5/8	11/16	3/4	7/8	1	11/8
7-wire strands 12 " " " 19 " "	37	47 36	56 43 34	66 50 39	75 57 45	84 65 51	94 72 56	78	112 86 68	101	115	101

Assuming the sheaves are of equal diameter, and not smaller than consistent with maximum efficiency as determined by the preceding table, the actual horse-power transmitted approximately equals 3.1 times the square of the diameter of the rope in inches multiplied by the velocity in feet per second.

From this rule we deduce the following:

## Horse-power of Wire-rope Transmission.

Velocity, in feet ( per second.	20	30	40	50	60	70	80
Diam. Rope, in inches.		F	Iorse-po	wer Tra	nsmitted		
1/4 5/16 3/8 7/16 1/2 9/16 5/8	4 6 9 12 16 20 24	6 9 13 18 23 29 36	8 12 17 24 31 39 48	10 15 22 30 39 49 61	12 18 26 36 47 59	14 21 31 42 54 69 85	16 24 35 47 62 78 97
11/16 3/4 7/8 1	29 35 48 62	44 52 71 93	59 70 95 124	73 87 119 155	88 105 142 186	103 122 166 217	117 140 190 248

The proper deflection to give the rope in order to secure the necessary tension is

 $h = .0000695S^2$ .

h = the deflection with the rope at rest, and S = the span, both in feet.

Durability of Wire Ropes,—At the Risdon Iron Works, San Francisco, a steel wire rope 2½ inches in circumference running over 10-foot sheaves at 5000 ft, per minute has transmitted 40 H.P. for six years without renewing the rope. At the wire-mills a steel-wire rope 2½ in. in circumference running over 8-foot sheaves has been running steadily for a period of three years at a velocity of 4500 ft, per minute, transmitting 80 H.P.

ence running over stoots sneaves has been running steadily for a period of three years at a velocity of 4500 ft., per minute, transmitting 80 H.P.

In Inclined Transmissions, when the angle of inclination is great, the proper deflections cannot be readily determined, and the rope becomes more sensitive to the ordinary variations in the deflections, so that tightening sheaves must be resorted to for producing the requisite tension, as in the case of very short spans. When the horizontal distance between the two wheels is less than 60 ft., or when the angle of inclination exceeds 30 to 45 degrees, it will be found desirable to use tightening sheaves.

Tightening pulleys should be placed on the slack side of the rope.

The Wire-rope Catenary. (From an article on Wire-rope Transmission, by M. Arthur Achard, Proc. Inst. M. E., Jan. 1881.)—The wires have to bear two distinct molecular strains: First, the tension 8

resulting from the maximum tension T necessary to transmit the motion. whose value in pounds per square inch is  $S = \frac{1}{4/\pi d^2 i}$ , d being the diameter of the wires and i their number; second, the strain produced by flexure upon the pulley, which is approximately  $Z = E \frac{d}{2R}$ , R being the radius of the pulley and E the modulus of elasticity of the metal. The approximate values allowed in practice for iron-wire ropes are S=14,220 lbs. per square inch, and Z = 11,380 lbs. per square inch. S + Z should not exceed say 11 tons (24,640 lbs.) per square inch.

The curve in which the rope hangs is a catenary; and it is upon the form of the particular catenary in which it hangs, whether more or less deep, as well as upon its lineal weight, that the tension to which it is subjected de-By fixing the weight of the rope and its length, the forms which its two spans assume in common, when at rest, is determined, and consequently their common tension; which latter must be such as to produce in running the two unequal tensions, T and t, necessary for the transmission of the power. The driving force = T - t.

Moreover, the tension in either span is not the same throughout its whole length; it is a minimum at the lowest point of the curve and goes on increasing towards the two extremities. The calculation of the tension at the lowest point is very complicated if based upon the true form of the catenary; but by substituting a parabola for the catenary, which is allowable in almost all cases, the calculation becomes simple. If the two pulleys are on the same level, the lowest point is midway between them, and the tension at this point is  $S_0 = \frac{pl^2}{8h}$ , p being the lineal weight, or pounds per foot, of the

rope, l its horizontal projection, which is approximately equal to the distance between the centres of the pulleys, and h the deflection in the middle. The catenary possesses the remarkable mechanical property that the difference between the tensions at any two points is equal to the weight of a length of rope corresponding to the difference in level between the two points.

tensions therefore at the two ends will be  $S_1 = S_0 + ph = \frac{pl^2}{8h} + ph$ . substituting for  $S_1$  in the above equation the required values of T and t, and solving it with relation to  $h_1$  the deflections  $h_1$  and  $h_2$  of the driving and trailing spans will be obtained. The deflection  $h_0$ , common to the two spans at rest, is given by the equation  $h_0 = \sqrt{1/2h_1^2 + 1/2h_2^2}$ . If w = the sectional area of the iron portion of the rope, and S the unit strain which the maximum

tension T produces on it, we have  $wS = T = \frac{pl^2}{8h_1} + ph_1$ . Taking the sectional

area w of the rope in square inches, and its weight p in pounds per foot run, the ratio w + p differs little from a mean value of 0.24. The safe limit of working tension usually assigned for iron-wire ropes is S = 14,220 lbs. per square inch. Hence  $ws + p = 0.24 \times 14,220 = 3410$ ; and we have the approx-

imate equation  $\frac{v}{8h_1} + h_1 = 3410$ , which is useful as giving a relation between the length l and deflection  $h_1$  for the driving-span of a rope. In the case of leather, w + p = 2.53 approximately, and it is impossible to give S a higher value than about 355 lbs. per square inch; the relation obtained would be

 $l^2$  $-+h_1=900$ , which with equal deflections would give much shorter spans.

If the working tension S were reduced to the American limit of 185 lbs. per square inch for leather belts, the above figure 900 would be reduced to 470,

which would further shorten the span one half.

It is therefore owing to the great strength which iron-wire ropes possess in proportion to their weight that they admit of long spans, with a smaller number of supports, and consequently smaller loss of power by friction. They may therefore be expected to yield a high efficiency. The experiments of M. Ziegler on the transmission of power at Oberusel give for the mean efficiency of a single relay = 96.2 per cent. The efficiency of transmission by relays, including m intermediate stations, is approximately obtained by raising the efficiency of a single relay to the power of

It often happens that the two pulleys of a single relay are at different levels, in which case neither span of the rope has the same tension at its

two extremities; the tension at the upper end of each exceeds that at the lower by the quantity pH, H being the difference in level between the two extremities, or, which is approximately the same, between the centres of the two pilleys. It is evidently the tension of the driving-span at title ow-end which must be regulated so as to obtain the proper driving tension if for the transmission, so that there is a certain excess of tension at the upper pulley. Large diameter of pulleys tends to preserve the ropes, makes the effect of stiffness insignificant, and diminishes the effect of friction on the bearings.

Another formula for the teusion at the ends of a catenary (assuming it to be a parabola) is  $S_1 = \frac{W}{2h} \sqrt{(\frac{1}{2}l)^2 + (2h)^2}$ , in which S = the tension in lbs;

W = weight of the rope in lbs.; l = span, and h = deflection, in feet. Diameter and Weight of Pulleys for Wire Rope, Ordi-

narv: 12.4 Diameter, ft.... 14.9

17

17

11/16 3/4 

11/16 3/4

7/8

11/8

11/6

1 140

) 176 ) 185

Double groove, lbs 8267	6988	4078	1164
Table of Transmission	of Power	by Wire	Ropes.
(J. A. Roebling	's Sons Co., 1	(886.)	

Single groove, lbs...

1/6 

1/6 

9/16 

9/16 

9/16 

Diameter of Rope. Wheel feet. Number of Revo-lutions. Number of Revo-lutions. Diameter Whet feet. of Trade power. of of 9/16 5/8 5/8 31/2 41/2 } 20 } 19 3/8 9/16 5% j 20 19 3/8 9/16 5% 19 19 19 18 18 19 18 19 18 19 18 19 18 19 9/16 5/8 3/2 7/16 9/16 5/2 7/16 5% 11/16 7/16 56 11/16 7/16 56 11/16 1/2 5% 11/16 1/9 11/16 34

Long-distance Transmissions. (From Circular of the Trenton Long-distance Transmissions. (From Circular of the Frenton Iron Co., 1822)—In very long transmissions of power the conditions do not always admit of obtaining the proper tensions required in the ordinary system, or "diying transmission of power," as it is termed. In other words, to obtain the proper conditions, it would necessitate numerous and expensive intermediate stations. In case, for instance, it is desired to utilize the power of a tunbine to drive a factory, say a mile away, the best method is to employ a larger rope than would ordinarily be used, running it at a moderate

speed. The rope may be in one continuous length, supported, at intervals speed. The rope may be in one commons length, supported, at intervals of about 100 ft., on sheaves of comparatively small diameter, since the greater rigidity of these ropes preserves them from undue bending strains. Where sharp angles occur in the line, however, sheaves must be used of a size corresponding to the safe limit of tension due to bending. The rope is run under a high working tension, far in excess of what in the ordinary system would cause the rope to slip on the sheaves. The working tension system would cause the rope to sup on the sheaves. The working tension may be four or five times as great as the tension in the slack portion of the rope, and in order to prevent slipping, the rope is wrapped several times about grooved drums, or a series of sheaves at each end of the line. To provide for the slack due to the stretch of the rope, one of the sheaves is placed on a slide worked by long-threaded bolts, or, better still, on a carriage provided with counterweights, which runs back and forth on a track. The latter preserves a uniform tension in the slack portion of the rope, which is very important.

Wire-rope tramways are practically transmissions of power of this kind. in which the load, however, instead of being concentrated at one terminal, is distributed uniformly over the entire line. Cable railways are also transmissions of this class. The amount of horse-power transmitted is given by

the formula

$$N = [4.755D^2 - .000006 (W + g + g_2)]v;$$

in which D = diameter of the rope in inches; v = velocity in ft. per second; W = weight of the rope; g = weight of the terminal sheaves and axles, and  $q_0$  = weight of the intermediate sheaves and axles.

# ROPE-DRIVING.

The transmission of power by cotton or manila ropes promises to become a formidable competitor with gearing and leather belting for use where the amount of power is large, or the distance between the power and the work is comparatively great. The following is condensed from a paper by Charles W. Hunt, Trans. A. S. M. E., vol. xii. p. 230:

But few accurate data are available, on account of the long period resistant of the standard process of the standard process.

quired in each experiment, a rope lasting from three to six years. In many of the early applications so great a strain was put upon the rope that the wear was rapid, and success only came when the work required of the rope was greatly reduced. The strain upon the rope has been decreased until it is approximately known what it should be to secure reasonable durability. Installations which have been successful, as well as those in which the wear of the rope was destructive, indicate that 200 lbs, on a rope one inch in diameter is a safe and economical working strain. When the strain is materially increased, the wear is rapid.

In the following equations

C = circumference of rope in inches;

g = gravity; H = horse-power;

D = sag of the rope in inches;F = centrifugal force in pounds;

L = distance between pulleys in ft. w =working strain in pounds:

P =pounds per foot of rope; w =workin R =force in pounds doing useful work;

S =strain in pounds on the rope at the pulley;

T = tension in pounds of driving side of the rope;t = tension in pounds on slack side of the rope;

v = velocity of the rope in feet per second; W = ultimate breaking strain in pounds.

 $W = 720C^2$ ;  $P = .32C^2$ :  $w = 20C^2$ .

This makes the normal working strain equal to 1/36 of the breaking strength, and about 1/25 of the strength at the splice. The actual strains are ordinarily much greater, owing to the vibrations in running, as well as from imperfectly adjusted tension mechanism.

For this investigation we assume that the strain on the driving side of a rope is equal to 200 lbs. on a rope one inch in diameter, and an equivalent strain for other sizes, and that the rope is in motion at various velocities of

from 10 to 140 ft, per second. The centrifugal force of the rope in running over the pulley will reduce the amount of force available for the transmission of power. The centrifu-

gal force  $F = Pv^2 + q$ .

gal force  $F = Fv^2 + g$ . At a speed of about 50 ft, per second, the centrifugal force increases faster than the power from increased velocity of the rope, and at about 140 ft, per second equals the assumed allowable tension of the rope. Computing this force at various speeds and then subtracting it from the assumed maximum tension, warious speeds and the actual training in the dissumed maximizetension, we have the force available for the transmission of power. The whole of this force around the use of the second of tension of the slack side of the rope is needed to give adhesion to the pulley. What tension should be given to the rope for this purpose is uncertain, as there are experiments which give accurate data. It is known from considerable are no experiments which give accurate data. It is known from considerable experience that when the rope runs in a groove whose sides are inclined toward each other at an angle of  $45^{\circ}$  there is sufficient adhesion when the ratio of the tensions  $T \cdot t = 2$ . For the present purpose, T can be divided into three parts: 1. Tension doing useful work; 2. Tension from centrifugal froce; 3. Tension to balance the strain for adhesion.

The tension t can be divided into two parts; 1. Tension for adhesion; 2. Tension from centrifugal force.

It is evident, however, that the tension required to do a given work should not be materially exceeded during the life of the rope.

There are two methods of putting ropes on the pulleys; one in which the ropes are single and spliced on, being made very taut at first, and less so as the rope lengthens, stretching until it slips, when it is respliced. The other method is to wind a single rope over the pulley as many turns as needed to neutrons so wind a single rope over the pulsey as maint turns as needed to obtain the necessary adhesion and also take up the wear. The tension t required to transmit the normal horse-power for the ordinary speeds and sizes of rope is computed by formula (1), below. The total tension T on the driving side of the rope is assumed to be the same at all speeds. The centrifugal force, as well as an amount equal to the tension for adhesion on the slack side of the rope, must be taken from the total tension T to ascertain the amount of force available for the transmission of power.

It is assumed that the tension on the slack side necessary for giving It is assumed that the tension of the state size necessary for some adhesion is equal to one half the force doing useful work on the driving side of the rope; hence the force for useful work is  $R = \frac{2(T-F)}{3}$ ; and the tension of the rope; hence the force for useful work is  $R = \frac{2(T-F)}{3}$ .

sion on the slack side to give the required adhesion is  $\frac{1}{3}(T-F)$ . Hence

$$t = \frac{(T - F)}{3} + F.$$
 (1)

The sum of the tensions T and t is not the same at different speeds, as the equation (1) indicates.

As F varies as the square of the velocity, there is, with an increasing speed of the rope, a decreasing useful force, and an increasing total tension, t, on the slack side.

With these assumptions of allowable strains the horse-power will be

Transmission ropes are usually from 1 to 13/4 inches in diameter. A computation of the horse-power for four sizes at various speeds and under

putation of the horse-power for four sizes at various speeds and under ordinary conditions, based on a maximum strain equivalent to 200 lbs. for a rope one inch in diameter, is given in Fig. 166. The horse-power of other sizes is readily obtained from these. The maximum power is transmitted, under the assumed conditions, at a speed of about 80 feet per second.

The wear of the rope is both internal and external; the internal is caused by the movement of the fibres on each other, under pressure in bending over the sheaves, and the external is caused by the slipping and the wedging in the grooves of the pulley. Both of these causes of wear are, within the limits of ordinary practice, assumed to be directly proportional to the speed. Hence, if we assume the coefficient of the wear to be k. the wear speed. Hence, if we assume the coefficient of the wear to be k, the wear will be kv, in which the wear increases directly as the velocity, but the horse-power that can be transmitted, as equation (2) shows, will not vary at the same rate.

The rope is supposed to have the strain T constant at all speeds on the driving side, and in direct proportion to the area of the cross-section; hence

the catenary of the driving side is not affected by the speed or by the diameter of the rope

eter of the rope.

The deflection of the rope between the pulleys on the slack side varies with each change of the load or change of the speed, as the tension equation

The deflection of the rope is computed for the assumed value of T and t

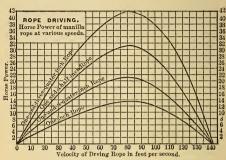


Fig. 166.

by the parabolic formula  $S=\frac{PL^2}{8D}+PD$ , S being the assumed strain T on the driving side, and t, calculated by equation (1), on the slack side. The tension t varies with the speed.

# Horse-power of Transmission Rope at Various Speeds.

Computed from formula (2), given above.

iam. of Ropes.	Speed of the Rope in feet per minute.									llest n. of leys iches		
Diam. Rop	1500	2000	2500	3000	3500	4000	4500	5000	6000	7000	8000	Sma Diar Pul in in
1/2/8/4/8	1.45 2.3	1.9	2.3	2.7	3 4.6	3.2 5.0 7.2	3.4 5.3	3.4 5.3 7.7	3.1 4.9 7.1	2.2 3.4 4.9	0	20 24 30
3/4 7/8	3.3 4.5 5.8	4.3 5.9 7.7	5.2 7.0 9.2	5.8 8.2 10.7	6.7 9.1 11.9	9.8 12.8	7.7 10.8 13.6	10.7 13.7	9.3 12.5	4.9 6.9 8.8	0	36 42 54
11/4 11/6 13/4	9.2 13.1	12.1 17.4	14.3 20.7	16.8	18.6 26.8	20.0 28.8	30.6		19.5 28.2 37.4	13.8 19.8 27.6	0 0	54 60 72
13/4	18	23.7	28.2	32.8	36.4 47.6	39.2 51 2		41.8 54.8		35.2		84

The following notes are from the circular of the C. W. Hunt Co., New York:

For a temporary installation, when the rope is not to be long in use, it might be advisable to increase the work to double that given in the table.

For convenience in estimating the necessary clearance on the driving and on the slack sides, we insert a table showing the sag of the rope at different speeds when transmitting the horse-power given in the preceding table. When at rest the sag is not the same as when running, being greater on the driving and less on the slack sides of the rope. The sag of the driving side when transmitting the normal horse-power is the same no matter what size of rope is used or what the speed driven at, because the assumption is that the strain on the rope shall be the same at all speeds when transmitting the

assumed horse-power, but on the slack side the strains, and consequently the sag, vary with the speed of the rope and also with the horse-power. The table gives the sag for three speeds. If the actual sag is less than given

in the table, the rope is strained more than the work requires.

This table is only approximate, and is exact only when the rope is running at its normal speed, transmitting its full load and strained to the assumed amount. All of these conditions are varying in actual work, and the table

must be used as a guide only.

Sag of the Rope between Pulleys.

Distance between	Driving Side.	Slack Side of Rope.							
Pulleys in feet.	All Speeds.	80 ft. per sec.	60 ft. per sec.	40 ft. per sec.					
40	0 feet 4 inches	0 feet 7 inches	Ofeet 9 inches	0 feet 11 inches					
60 80	0 " 10 "	1 " 5 "	1 " 8 "	1 " 11 "					
80	1 " 5 "	2 " 4 "	1 " 10 "	3 " 3 "					
100	2 " 0 "	3 " 8 "	4 " 5 "	5 " 2 "					
120	2 " 11 "	5 " 3 "	6 " 3 "	7 " 4 "					
140	3 " 10 "	7 " 2 "	8 " 9 "	9 " 9 "					
160	5 " 1 "	9 " 3 "	11 " 3 "	14 " 0 "					

The size of the pulleys has an important effect on the wear of the ropethe larger the sheaves, the less the fibres of the rope slide on each other, and consequently there is less internal wear of the rope. The pulleys should not consequency there is less internal wear of the rope. The punicys should nobe less than forty times the diameter of the rope for economical wear, and as much larger as it is possible to make them. This rule applies also to the idle and tension pulleys as well as to the main driving-pulley.

The angle of the sides of the grooves in which the rope runs varies, with different engineers, from 45° to 60°. It is every important that the sides of these grooves should be carefully polished, as the fibres of the rope rubbing

on the metal as it comes from the lathe tools will gradually break fibre by fibre, and so give the rope a short life. It is also necessary to carefully avoid all sand or blow holes, as they will cut the rope out with surprising rapidity.

Much depends also upon the arrangement of the rope on the pulleys, es-cially where a tension weight is used. Experience shows that the pecially where a tension weight is used. increased wear on the rope from bending the rope first in one direction and then in the other is similar to that of wire rope. At mines where two cages are used, one being hoisted and one lowered by the same engine doing the same work, the wire ropes, cut from the same coil, are usually arranged so that one rope is bent continuously in one direction and the other rope is bent first in one direction and then in the other, in winding on the drum of the engine. The rope having the opposite bends wears much more rapidly than the other, lasting about three quarters as long as its mate. This difference in wear shows in manila rope, both in transmission of power and in coal-hoisting. The pulleys should be arranged, as far as possible, to bend the rope in one direction.

The wear of the rope is independent of the distance apart of the shafts,

since the wear takes place only on the pulleys; hence in transmitting power any distance within the limits of rope-driving, the life of the rope will be the same whether the distance is small or great, but the first cost will be in

proportion to the distance.

TENSION ON THE SLACK PART OF THE ROPE.

Speed of Rope, in feet Diameter of the Rope and Pounds Tension on the Slack I										
per second.	1/2	5/8	3/4	₹8	1	11/4	11/2	13/4	2	
20	10	27	40	54	71	110	162	216	283	
30	14	29	42	56	74	115	170	226	296	
40	15	31	45.	60	79	123	181	240	315	
50	16	33	49	65	85	132	195	259	339	
60	18	36	53	71	93	145	214	285	373	
70		39	59	78	101	158	236	310	406	
80	21	43	64	85	111	173	255	340	445	
90	24	48	70	93		190	279	372	487	

For large amounts of power it is common to use a number of ropes lying side by side in grooves, each spliced separately. For lighter drives some engineers use one rope wrapped as many times around the pulleys as is necessary to get the horse-power required, with a tension pulley to take up the slack as the rope wears when first put in use. The weight put upon this tension pulley should be carefully adjusted, as the overstraining of the rope from this cause is one of the most common errors in rope driving. We therefore give a table showing the proper strain on the rope for the various sizes, from which the tension weight to transmit the horse-power in the tables is easily deduced. This strain can be still further reduced if the horse-power transmitted is usually less than the nominal work which the rope was proportioned to do, or if the angle of groove in the pulleys is acute.

DIAMETER OF PULLEYS AND WEIGHT OF ROPE.

Diameter of	Smallest Diameter	Length of Rope to	Approximate
Rope,	of Pulleys, in	allow for Splicing,	Weight, in lbs. per
in inches.	inches.	in feet.	foot of rope.
1/3	20	6 6 7 8	.12
5/8	24		.18
3/4	30		.24
5/8	36		.32
1 11/4 11/2 13/4 2	42 54 60 72 84	10 12 13 14	.49 .60 .83 1.10 1.40

With a given velocity of the driving-rope, the weight of rope required for transmitting a given horse-power is the same, no matter what size rope is adopted. The smaller rope will require more parts, but the weight will be the same.

Miscellaneous Notes on Rope-driving,—W. H. Booth communicates to the Amer. Machinist the following data from English practice with cotton ropes. The calculated figures are based on a total allowable tension on a 134-inch rope of 600 lbs., and an initial tension of 1/10 the total allowed stress, which corresponds fairly with practice.

Diameter of rope	11/4"	13/8"	1½" .72	15%'' .844	134'' .98	17/8" 1,125	2"
Weight per foot, lbs	.5	.6	.72	.844	.98	1,125	1.3
Centrifugal tension = $V^2$ divided by		53	44	38	23	28	25
" for $V = 80$ ft. per sec., lbs.	100	121	145	170	193	228	256
Total tension allowable	300	360	430	500	600	675	780
Initial tension	30	36	43	50	60	67	78
Net working tension at 80 ft. velocity	170	203	242	280	347	380	446
Horse-power per rope " "	24	28	34	41	49	54	63

The most usual practice in Lancashire is summed up roughly in the following figures: 134-inch cotton ropes at 5000 ft, per minute velocity = 50 H.P. per rope. The most common sizes of rope now used are 134 and 154 in. The maximum horse-power for a given rope is obtained at about 80 to 82 feet per second. Above that speed the power is reduced by centrifugal tension. At a speed of 2500 ft, per minute four ropes will do about the same work as three at 5000 ft. per min.

Cotton ropes do not require much lubrication in the sense that it is required by ropes made of the rough fibre of manila hemp. Merely a slight surface dressing is all that is required. For small ropes, common in spinning machinery, from ½ to ¾ inch diameter, it is the custom to prevent the fuffing of the ropes on the surface by a light application of a mixture of black-lead and molasses,—but only enough should be used to lay the fibres,—but mone of the nulleys in a series of light dabs.

black-lead and molasses,—but only enough should be used to lay the fibres, put upon one of the pulleys in a series of light dabs. Reuleaux's Constructor gives as the "specific capacity" of hemp rope in actual practice, that is, the horse-power transmitted per square inch of cross-section for each foot of linear velocity per minute, .04 to .002, the ropes. For a 1¾-in, rope, with a cross-section of 2.405 q. in., at a velocity of 5000 ft. per min., this gives a horse-power of from 24 to 48, as against 41.8 by Mr. Hunt's table and 49 by Mr. Booth's.

Reuleaux gives formulæ for calculating sources of loss in hemp-rope transmission due to (1) journal friction, (2) stiffness of ropes, and (3) creep of ropes. The constants in these formulæ are, however, uncertain from lack of experimental data. He calculates an average case giving loss of power due to journal friction = 4%, to stiffness 7.8%, and to creep 5%, or 16.8% in all, and says this is not to be considered higher than the actual loss.

T. Spencer Miller (Eng'g News, Dec. 6, 1890) says: In England hemp and manila ropes have been largely superseded by ropes of cotton; and I am satisfied that one reason for this is that dry manila ropes wear out too fast, while lubricated ropes give too low a coefficient of friction. The angle of 45° for the groove has been in use for 33 years, having been first introduced by Jas. Combe in Belfast, Ireland; but if we are to use tallow-laid or other lubricated ropes, we should certainly use a sharper angle in the groove. especially in the American system, which employs a continuous rope with

many wraps.

Mr. Hunt's formula, Tension of driving side of rope + tension of slack side of rope = 2, implies a coefficient of friction of only 10. But I have obtained a coefficient of friction of .26, and have found one authority giving Reuleaux advises for single-line transmission 30° angle of groove. 2.25. Remeaux advises for single-line transmission 30° angle of groove. Ramsbottom, an English engineer, and Yale & Towne use a 30° groove in transmission-wheels of travelling-cranes, and I hope to see the best American practice use 30° or 35° as a standard groove angle. The work done in pulling out a greasy manila rope from a 30° groove is not worth consideration, although we hear a great deal about the loss of power on this account. I am strongly in favor of using the continuous-rope system, and also of using smaller ropes than are recommended in Mr. Hunt's paper.

using smaller ropes than are recommended in air. Hunt's paper. The most perfect small transmission I have ever seen (about 20 H.P.) employs 5/16-in, manila rope on wheels 30 in, in diameter, using a tension car-riage. Rather than use large ropes I think it wiser to replace small ones oftener, for by so doing a great gain may be made in efficiency, thus saving

fuel.

A large majority of failures in the continuous-rope plan have occurred where the driving and driven sheaves were of widely different diameters, as for example, driving dynamos, or driving a line-shaft from an engine flywheel. As ordinarily installed the ropes will not pull alike, and by calculation or by experiment we may find one rope pulling twice or three times as

much as the others on the sheave.

An installation designed by the writer employs an engine-driving sheave about three times the diameter of the driven sheave. To equalize the pull on the different ropes the grooves of the large driving-sheaves were made with an angle of 30° and those of the small sheaves with an angle of 46°. This change of groove angle has entirely remedied the unequal pulling com-

plained of.

It has been observed that in sheaves of the same diameter, by the use of a proper tension weight, the ropes may all pull alike; while, where the sheaves are of unequal diameter, the pull is unequal. The only difference of condi-tions in the two cases lies in the different arc of contact of the rope on the two sheaves, which leads to a greater frictional hold of the rope on the large To equalize the frictional hold on the two sheaves we may sharpen

the angle of the small sheave or increase the angle of the large sheave.

The Walker Mfg. Co. adopts a curved form of groove instead of one with straight sides inclined to each other at 45°. The curves are concave to the rope. The rope rests on the sides of the groove in driving and driven pulrope. The rope rests on the sides of the groove in driving and driven pul-leys. In idler pullers the rope rests on the bottom of the groove, which is semicircular. The Walker Mrg. Co. also uses a "differential" drum for heavy rope drives, in which the grooves are contained each in a separate ring which is free to slide on the turned surface of the drum in case one rope

pulls more than another.

A heavy rope-drive on the separate, or English, rope system is described and illustrated in *Power*, April, 1892. It is in use at the India Mill at Darwen, England. This mill was originally driven by gears, but did not prove successful, and rope-driving was resorted to. The \$5.000 spindles and preparation are driven by a 2000 horse-power tandem compound engine, with cylinders 23 and 44 inches in diameter and 72-inch stroke, running at 54 revolutions per minute. The fly-wheel is 30 feet in diameter, weighs 65 tons and is arranged with 30 grooves for 134-inch ropes. These ropes lead off to receive the control of the ing-pulleys upon the several floors, so that each floor receives its power direct from the fly-wheel. The speed of the ropes is 5089 feet per minute, and five 7-foot receivers are used, the number of ropes upon each being proportioned

to the amount of power required upon the several floors. Lambeth cotton ropes are used.

# FRICTION AND LUBRICATION.

Friction is defined by Rankine as that force which acts between two bodies at their surface of contact so as to resist their sliding on each other, and which depends on the force with which the bodies are pressed together. Coefficient of Friction.—The ratio of the force required to slide a

body along a horizontal plane surface to the weight of the body is called the coefficient of friction. It is equivalent to the tangent of the angle of repose, which is the angle of inclination to the horizontal of an inclined plane on which the body will just overcome its tendency to slide. The angle is usually

denoted by  $\theta_i$  and the coefficient by  $f_i$ ,  $f_i = \tan \theta_i$ .

Friction of **Rest and of Motion**.—The force required to start a body sliding is called the friction of rest, and the force required to continue its sliding after having started is called the friction of motion.

Rolling Friction is the force required to roll a cylindrical or spherical body on a plane or on a curved surface. It depends on the nature of the car only on a pane of our actived started. It are pressed together, but is essentially different from ordinary, or sliding, friction.

Friction of Solids,—Rennie's experiments (1839) on friction of solids,

usually unlubricated and dry, led to the following conclusions:

lubricant rather than by that of the solids themselves,

1. The laws of sliding friction differ with the character of the bodies

rubbing together.

2. The friction of fibrous material is increased by increased extent of

2. The Fitchion of Information is inderelated by Increased extent.

3. With wood, metal, and stones, within the limit of abrasion, friction varies only with the pressure, and is independent of the extent of surface, time of contact and velocity.

4. The limit of abrasion is determined by the hardness of the softer of the

two rubbing parts
5. Friction is greatest with soft and least with hard materials.
6. The friction of lubricated surfaces is determined by the nature of the

#### Friction of Rest. (Rennie.)

		(-								
Pressure,	Values of f.									
lbs. per square inch.	Wrought iron on Wrought Iron.	Wrought on Cast Iron.	Steel on Cast Iron.	Brass on Cast Iron.						
187 224	.25 .27	.28	.30	.23						
336 448	.31 .38	.33	.33 .35 .35	.22 .21 .21						
560 672	.41 Abraded	.28 .29 .33 .37 .37	.36 .40	.23						
784	**	Abraded	Abraded	93						

Law of Unlubricated Friction.—A. M. Wellington, Eng'g News, April 7, 1888, states that the most important and the best determined of all the laws of unlubricated friction may be thus expressed:

The coefficient of unlubricated friction decreases materially with velocity,

is very much greater at minute velocities of 0 +, falls very rapidly with minute increases of such velocities, and continues to fall much less rapidly with higher velocities up to a certain varying point, following closely the laws which obtain with lubricated friction.

Friction of Steel Tires Sliding on Steel Rails. (Westing-

house & Galton.)

Speed, miles per hour	10	15	25	38	45	50
Coefficient of friction	0.110	.087	.080	.051	.047	.040
Adhesion, lbs. per ton (2240 lbs.)	246	195	179	128	114	90

Rolling Friction is a consequence of the irregularities of form and the roughness of surface of bodies rolling one over the other. Its laws are not yet definitely established in consequence of the uncertainty which exists in experiment as to how much of the resistance is due to roughness of

made the value of f for iron on iron .002.

For wagons on soft soil Morin found f = .065, and on hard smooth roads .02.

A Committee of the Society of Arts (Clark, R. T. D.) reported a loaded omnibus to exhibit a resistance on various loads as below:

1	Pavement	Speed per hour.	Coefficient.	Resistance.
	Granite	2.87 miles.	.007	17.41 per ton.
	Asphalt	3.56 "	.0121	27.14 "
	Wood	3.34 "	.0185	41.00
ı	Macadam, gravelled	0.40	.0199	44.48 "
	" granite, new	3.51 "	.0451	101.09

Thurston gives the value of f for ordinary railroads, .003, well-laid railroad track, .002; best possible railroad track, .001.

The few experiments that have been made upon the coefficients of rolling friction, apart from axle friction, are too incomplete to serve as a basis for

practical rules. (Trautwine).

practical rules. (Trauwine).

Laws of Fluid Friction.—For all fluids, whether liquid or gaseous, the resistance is (1) independent of the pressure between the masses in contact; (2) directly proportional to the area of rubbing-surface; (3) proportional to the square of the relative velocity at moderate and high speeds, and to the velocity nearly at low speeds; (4) independent of the nature of the surfaces of the solid against which the stream may flow, but dependent to some extent upon their degree of roughness; (5) proportional to the density of the fluid, and related in some way to its viscosity. (Thurston.)

The Friction of Lubricated Surfaces approximates to that of solid friction as the journal is run dry, and to that of fluid friction as it is flooded

with oil.

Angles of Repose and Coefficients of Friction of Building Materials. (From Rankine's Applied Mechanics.)

	θ.	$f = \tan \theta$ .	$\frac{1}{\tan \theta}$ .
Dry masonry and brickwork Masonry and brickwork with	31° to 35°	.6 to .7	1.67 to 1.4
damp mortar	36½°	.74	1.35
Timber on stone	226	about .4	2.5
Iron on stone	35° to 16%°	.7 to .3	1.43 to 3.3
Timber on timber	261/3° to 111/3°	.5 to .2	2 to 5
metals	31° to 111/3°	.6 to .2	1.67 to 5
Metals on metals	14° to 81/2°	.25 to .15	4 to 6.67
Masonry on dry clay " moist clay	270 ~~	.51	1.96
moist clay	18¼°	.33	3.
Earth on earth	14° to 45°	.25 to 1.0	4 to 1
" " dry sand, clay,			
and mived earth	21° to 37°	.38 to .75	2.63 to 1.33
Earth on earth, damp clay	45°	1.0	1
" " wet clay	170	.31	3.23
Earth on earth, damp clay " " wet clay shingle and			
gravel	39° to 48°	.81	1.23 to 0.9

Friction of Motion. - The following is a table of the angle of repose  $\theta$ , the coefficient of friction  $f = \tan \theta$ , and its reciprocal, 1 + f, for the materials of mechanism—condensed from the tables of General Morin (1831), and other sources, as given by Rankine:

No.	Surfaces.	θ.	f.	$1 \div f$ .
1	Wood on wood, dry	14° to 26½°	.25 to .5	4 to 2
2	" " soaped	111/2° to 2°	.2 to .04	5 to 25
1 2 3	Metals on oak, dry	261%° to 31°	5 to 6	2 to 1.67
4	" " wet	13½° to 14°	.24 to .26	4.17 to 3.85
5	" " soapv	11½°	.2	5
6	" " elm, dry	11½° to 14°	.2 to .25	5 to 4
7	Hemp on oak, dry	28°	.53	1.89
4 5 6 7 8	" " wet	181⁄6°	.33	3
9	I oothor on oolr	15° to 1916°	.27 to .38	3.7 to 2.86
10	" " metals, dry	29160	.56	1.79
ii	" " wet	291/30° ~ 20°	.36	2.78
12	" " greasy		.23	4.35
13	" " " oily	81%°	.15	6.67
14	Metals on metals, dry	81/6° to 11°	15 to .2	6.67 to 5
15	" wet	161/60	3 .~	3.33
16	Smooth surfaces, occa-	1072	,	0.00
10	sionally greased	4° to 41/6°	.07 to .08	14.3 to 12.5
17	Smooth surfaces, con-	4 10 479	.01 10 .00	14.0 00 12.0
11	tinuously greased	30	.05	20
18	Smooth surfaces, best		.00	20
18			09 40 090	
40	results	1¾° to 2°	.03 to .036	
19	Bronze or lignum vitæ,	20.0	05.0	
	constantly wet	3° ?	.05 ?	

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# Coefficients of Friction of Journals. (Morin.)

Statust 1	TT	Lubrication.				
Material.	Unguent.	Intermittent.	Continuous.			
Cast iron on cast iron	Oil, lard tallow. Unctuous and wet. Oil, lard, tallow. Unctnous and wet. Oil, lard, Oil, lard, Oil, lard, Unctnous. Oilve-oil. Lard.	.07 to .08 .14 .07 to .08 .16 .07 to .08 .11 .19 .10	.03 to .054 .08 to .054 .09 .03 to .054			

Prof. Thurston says concerning the above figures that much better results are probably obtained in good practice with ordinary machinery. Those here given are so greatly modified by variations of speed, pressure, and temperature, that they cannot be taken as correct for general purposes.

Average Coefficients of Friction. Journal of cast iron in bronze bearing; velocity 720 feet per minute; temperature 70° F.; intermittent feed through an oil-hole. (Thurston on Friction and Lost Work.)

0.77-	Pressures, pounds per square inch.										
Oils.	8 16		32		-	48					
Sperm, lard, neat's-foot,etc. Olive. cotton-seed, rape, etc. Cod and menhaden Mineral lubricating-oils	.160 "	.283	.107		.245	.101	**	.168	.079 081	"	.131

With fine steel journals running in bronze bearings and continuous lubrication, coefficients far below those above given are obtained. Thus with sperm-oil the coefficient with 50 lbs. per square inch pressure was .0034; with 200 lbs., .0051; with 300 lbs., .0057,

For very low pressures, as in spindles, the coefficients are much higher. Thus Mr. Woodbury found, at a temperature of 100° and a velocity of 600 feet per minute.

Pressures, lbs. per sq. iu,..... .18 Coefficient ....

These high coefficients, however, and the great decrease in the coefficient at increased pressures are limited as a practical matter only to the smaller pressures which exist especially in spinning machinery, where the pressure is so light and the film of oil so thick that the viscosity of the oil is an import-

ant part of the total frictional resistance.

Experiments on Friction of a Journal Lubricated by an Oll-bath (reported by the Committee on Friction, Proc. Inst. M. E., Nov. 1883) show that the absolute friction, that is, the absolute tangential force per square inch of bearing, required to resist the tendency of the brass to go round with the journal, is nearly a constant under all loads, within ordinary working limits. Most certainly it does not increase in direct proportion to the load, as it should do according to the ordinary theory of solid friction. The results of these experiments seem to show that the friction of a perfectly lubricated journal follows the laws of liquid friction much more closely than those of solid friction. They show that under these circumstances the friction is nearly independent of the pressure per square inch. and that it increases with the velocity, though at a rate not nearly so rapid as the square of the velocity.

The experiments on friction at different temperatures indicate a great diminution in the friction as the temperature rises. Thus in the case of lard-oil, taking a speed of 450 revolutions per minute, the coefficient of friction at a temperature of 120° is only one third of what it was at a temperature of 60.

The journal was of steel, 4 inches diameter and 6 inches long, and a gun-metal brass, embracing somewhat less than half the circumference of the journal, rested on its upeer side, on which the load was applied. When the bottom of the journal was immersed in oil, and the oil therefore carried under the brass by rotation of the journal, the greatest load carried with rape-oil was 573 lbs. per square inch, and with mineral oil 625 lbs.

In experiments with ordinary lubrication, the oil being fed in at the centre of the top of the brass, and a distributing groove being cut in the brass parallel to the axis of the journal, the bearing would not run cool with only 100 lbs. per square inch, the oil being pressed out from the bearing-surface and through the oil-hole, instead of being carried in by it. On introducing the oil at the side through two parallel grooves, the lubrication appeared to be satisfactory, but the bearing seized with 380 lbs. per square inch.

When the oil was introduced through two oil-holes, one near each end of the brass, and each connected with a curved groove, the brass refused to take its oil or run cool, and seized with a load of only 200 lbs. per square

inch

With an oil-pad under the journal feeding rape-oil, the bearing fairly carried 551 lbs. Mr. Tower's conclusion from these experiments is that the friction depends on the quantity and uniformity of distribution of the oil, and may be anything between the oil-bath results and seizing, according to the perfection or imperfection of the lubrication. The lubrication may be very small, giving a coefficient of 1/100; but it appeared as though it could not be diminished and the friction increased much beyond this point with-out imminent risk of heating and seizing. The oil-bath probably represents the most perfect lubrication possible, and the limit beyond which friction cannot be reduced by lubrication; and the experiments show that with speeds cannot be reduced by indirection; and the experiments show that with species of from 100 to 200 feet per minute, by properly proportioning the bearing-surface to the load, it is possible to reduce the coefficient of friction to as low as 1/1000. A coefficient of 1/1500 is easily attainable, and probably is frequently attained, in ordinary engine-bearings in which the direction of the force is rapidly alternating and the oil given an opportunity to get between the surfaces, while the duration of the force in one direction is not sufficient to allow the force in the surfaces. to allow time for the oil film to be squeezed out.

Observations on the behavior of the apparatus gave reason to believe that with perfect lubrication the speed of minimum friction was from 100 to 150 feet per minute, and that this speed of minimum friction tends to be higher with an increase of load, and also with less perfect lubrication. By the speed of minimum friction is meant that speed in approaching which from

rest the friction diminishes, and above which the friction increases.

Coefficients of Friction of Journal with Oil-bath,—Abstract of results of Tower's experiments on friction (Proc. Inst. M. E., Nov. 1883). Journal, 4 in. diam., 6 in. long; temperature, 90° F.

Lubricant in Bath.	Nominal Load, in pounds per square inch.						
gastour in bank	625	520	415	310	205	153	100
	Coefficients of Friction.						
Lard-oil : 157 ft. per min			.0012				
157 ft. per min,	1	.0022	.0016 .0027				
157 ft. per min	(573 lb )	seiz'd	.0015 .0021	.0011	.0016 .0027	.0019	.003 .006
157 ft. per min	.001	.001	.0009 .0016	.0008	.0014 .0024	.002 .004	.004
157 ft. per min	.0013	.0012 .0018	.0012 .002		.0021 .0035		
157 ft. per min				1.0068	.0077		.015
Rape-oil, pad under journal: 157 ft. per min				.0099	.0105		.009

Comparative friction of different lubricants under same circumstances, temperature 90°, oil-bath:

Sperm-oil	100 per cent.	Lard	135 per cen
Rape-oil	106 "	Olive-oil	135 "
Mineral oil	129 "	Mineral grease	217 "

Journal.—A cast-iron journal in steel boxes, tested by Prof. Thurston at a speed of rubbing of 150 feet per minute, with lard and with sperm oil, gave the following: Coefficients of Friction of Motion and of Rest of a

Pressures per sq. in., lbs 50 Coeff., with sperm	100 .008 .0137	250 .005 .0085	500 .004 .0053	750 .0043 .0066	1000 .009 .0125
The coefficients at starting were:					
With sperm	.135	.14	.15	.185	.18

The coefficient at a speed of 150 feet per minute decreases with increase of pressure until 500 lbs. per sq. in. is reached; above this it increases. The coefficient at rest or at starting increases with the pressure throughout the

range of the tests.

Value of Anti-friction Metals. (Denton.)—The various white metals available for lining brasses do not afford coefficients of friction lower than can be obtained with bare brass, but they are less liable to "overheating," because of the superiority of such material over bronze in ability to permit of abrasion or crushing, without excessive increase of

friction.

Thurston (Friction and Lost Work) says that gun-bronze, Babbitt, and Thursion (Friction and Lost work) says that gun-pronze, Brobitt, and other soft white alloys have substantially the same friction; in other words, the friction is determined by the nature of the unguent and not by that of the rubbing-surfaces, when the latter are in good order. The soft metals run at higher temperatures than the bronze. This, however, does not necessarily indicate a serious defect, but simply deficient conductivity. The value of the white alloys for bearings lies mainly in their ready reduction to a smooth surface after any local or general injury by alteration of either surface or form.

Cast-iron for Bearings. (Joshua Rose.)-Cast iron appears to be an exception to the general rule, that the harder the metal the greater the resistance to wear, because cast iron is softer in its texture and easier to cut with steel tools than steel or wrought iron, but in some situations it is far more durable than hardened steel; thus when surrounded by steam it will wear better than will any other metal. Thus, for instance, experience will wear occurrent unan will any other inetal. Thus, for instance experience has demonstrated that piston-rings of cast from will wear smoother, better, and equally as long as those of steel, and longer than those of either wrought iron or brass, whether the cylinder in which it works be composed of brass, steel, wrought iron, or cast from the latter being the more noteworthy, since two surfaces of the same metal do not, as a rule, wear or work well together. So also slide-valves of brass are not found to wear so long or so smoothly as those of cast iron, let the metal of which the seating is composed be whatever it may; while, on the other hand, a cast iron slidevalve will wear longer of itself and cause less wear to its seat, if the latter is of cast iron, than if of steel, wrought iron, or brass.

Friction of Metals under Steam-pressure.-The friction of

brass upon iron under steam-pressure is double that of tron upon iron. (6. H. Baboock, Trans, A. S. M. E., l. 151.)

Morin's "Laws of Friction."—1. The friction between two bodies is directly proportioned to the pressure; i.e., the coefficient is constant for ali pressures.

2. The coefficient and amount of friction, pressure being the same, is in-

dependent of the areas in contact.

3 The coefficient of friction is independent of velocity, although static friction (friction of rest) is greater than the friction of motion.

Eng'g News, April 7, 1888, comments on these "laws" as follows: From 1831 till about 1876 there was no attempt worth speaking of to enlarge our knowledge of the laws of friction, which during all that period was assumed to be complete, although it was really worse than nothing, since it was for the most part wholly false. In the year first mentioned Morin began a series of experiments which extended over two or three years, and which resulted in the enunciation of these three 'fundamental laws of friction,'

no one of which is even approximately true.

For fifty years these laws were accepted as axiomatic, and were quoted as such without question in every scientific work published during that whole period. Now that they are so thoroughly discredited it has been attempted to explain away their defects on the ground that they cover only a very limited range of pressures, areas, velocities, etc., and that Morin himself only announced them as true within the range of his conditions. It is now clearly established that there are no limits or conditions within which any one of them even approximates to exactitude, and that there are many conditions under which they lead to the wildest kind of error, while many of the constants were as inaccurate six the laws. For example, in Morin's "Table of Coefficients of Moving Friction of Smooth Plane Surfaces, perfectly lubricated," which may be found in hundreds of text-books now in use, the coefficient of wrought iron on brass is given as .075 to .103, which would make the rolling friction of railway trains 15 to 20 lbs. per ton instead of the 3 to 6 lbs. which it actually is.

General Morin, in a letter to the Secretary of the Institution of Mechanical Engineers, dated March 15, 1879, writes follows concerning his experiments on friction made more than forty years before: "The results furnished by my experiments as to the relations between pressure, surface, and speed on the one hand, and sliding friction on the other, have always been regarded by myself, not as mathematical laws, but as close approximations to the truth, within the limits of the data of the experiments themselves. The same holds. in my opinion, for many other laws of practical mechanics, such as those of

rolling resistance, fluid resistance, etc.

Prof. J. E. Denton (Stevens Indicator, July, 1890) says: It has been generally assumed that friction between lubricated surfaces follows the simple law that the amount of the friction is some fixed fraction of the pressure between the surfaces, such fraction being independent of the intensity of the pressure per square inch and the velocity of rubbing, between certain limits of practice, and that the fixed fraction referred to is represented by the coefficients of friction given by the experiments of Morin or obtained from experimental data which represent conditions of practical lubrication, such as those given in Webber's Manual of Power.

By the experiments of Thurston, Woodbury, Tower, etc., however, it appears that the friction between lubricated metallic surfaces, such as machine bearings, is not directly proportional to the pressure, is not independent of the speed, and that the coefficients of Morin and Webber are about

tenfold too great for modern journals.

Prof. Denton offers an explanation of this apparent contradiction of authorities by showing, with laboratory testing machine data, that Morin's laws hold for bearings lubricated by a restricted feed of lubricant, such as safforded by the oil-cups common to machinery; whereas the modern experiments have been made with a surplus feed or superabundance of lubricants. cant, such as is provided only in railroad-car journals, and a few special cases of practice

That the low coefficients of friction obtained under the latter conditions are realized in the case of car journals, is proved by the fact that the temperature of car-boxes remains at 100° at high velocities; and experiment shows that this temperature is consistent only with a coefficient of friction of a fraction of one per cent. Deductions from experiments on train resistance also indicate the same low degree of friction. But these low co-efficients do not account for the internal friction of steam-engines as well as do the coefficients of Morin and Webber.

In American Machinist, Oct. 23, 1890, Prof. Denton says: Morin's measurement of friction of lubricated journals did not extend to light pressures.

They apply only to the conditions of general shafting and engine work. He clearly understood that there was a frictional resistance, due solely to the viscosity of the oil, and that therefore, for very light pressures, the laws which he enunciated did not prevail.

He applied his dynamometers to ordinary shaft-journals without special preparation of the rubbing-surfaces, and without resorting to artificial

methods of supplying the oil

Later experimenters have with few exceptions devoted themselves exclusively to the measurement of resistance practically due to viscosity alone. They have eliminated the resistance to which Morin confined his measurements, namely, the friction due to such confact of the rubbing-surfaces as prevail with a very thin film of lubricant between comparatively rough surfaces.

Prof. Denton also says (Trans. A. S. M. E., x. 518): "I do not believe there is a particle of proof in any investigation of friction ever made, that Morin's laws do not hold for ordinary practical oil-cups or restricted rates of feed."

of well-lubricated Journals.-John Laws of Friction of well-lubricated Journals.—John Goodman (Trans. Inst. C. E. 1886, Eng'g News, Apr. 7 and 14, 1889), reviewing the results obtained from the testing-machines of Thurston, Tower, and Stroudley, arrives at the following laws:

# LAWS OF FRICTION: WELL-LUBRICATED SURFACES.

#### (Oil-bath.)

1. The coefficient of friction with the surfaces efficiently lubricated is from

1/6 to 1/10 that for dry or scantily lubricated surfaces.
2. The coefficient of friction for moderate pressures and speeds varies approximately inversely as the normal pressure; the frictional resistance varies as the area in contact, the normal pressure remaining constant.

3. At very low journal speeds the coefficient of friction is abnormally high; but as the speed of sliding increases from about 10 to 100 ft. per min.

the friction diminishes, and again rises when that speed is exceeded, varying approximately as the square root of the speed.

4. The coefficient of friction varies approximately inversely as the temperature, within certain limits, namely, just before abrasion takes place.

The evidence upon which these laws are based is taken from various modern experiments. That relating to Law 1 is derived from the "First Report on Friction Experiments," by Mr. Beauchamp Tower.

Method of Lubrication.	Coefficient of Friction.	Comparative Friction.
Oil-bath Siphon lubricator Pad under journal	.0098	1.00 7.06 6.48

With a load of 293 lbs. per sq. in, and a journal speed of 314 ft. per min. Mr. Tower found the coefficient of friction to be .0016 with an oil-bath, and .0097, or six times as much, with a pad. The very low coefficients obtained by Mr. Tower will be accounted for by Law 2, as he found that the frictional resistance per square inch under varying loads is nearly constant. as below:

310 Load in lbs. per sq. in.... 529 468 415 363 205 153 100 .498 .472 .464 .438 .43 Frictional resist, per sq. in, .416 .514 .458 .45

The frictional resistance per square inch is the product of the coefficient of friction into the load per square inch on horizontal sections of the brass. Hence, if this product be a constant, the one factor must vary inversely as the other, or a high load will give a low coefficient, and vice versa.

For ordinary labrication, the coefficient is more constant under varying loads; the frictional resistance then varies directly as the load, as shown by Mr. Tower in Table VIII of his report (Proc. Inst. M. E. 1883).

With respect to Law 3, A. M. Wellington (Trans. A. S. C. E. 1884), in experiments on journals revolving at very low velocities, from that the friction was then very great, and nearly constant under varying conditions of the lubrication, load, and temperature. But as the speed increased the friction fell slowly and regularly, and again returned to the original amount when the velocity was reduced to the same rate. This is shown in the following table:

Speed, feet per minute: 0+ 2.16 3.33 4

4.86 8.82 21.42 35.37 53.01 89.28 106.02 Coefficient of friction: .118 .094 .070 .069 .055 .047 .040 .035.030 .026

It was also found by Prof. Kimball that when the journal velocity was increased from 6 to 110 ft, per minute, the friction was reduced 70%; in another case the friction was reduced 67% when the velocity was increased from 1 to 100 ft. per minute; but after that point was reached the coefficient varied approximately with the square root of the velocity.

The following results were obtained by Mr. Tower:

Feet per minute	209	262	314	366	419	471	Nominal Load per sq. in.
Coeff. of friction	.0010	.0012	.0013	.0014	.0015	.0017	520 lbs.
	.0013	.0014	.0015	.0017	.0018	.002	468 "
	.0014	.0015	.0017	.0019	.0021	.0024	415 "

The variation of friction with temperature is approximately in the inverse ratio, Law 4. Take, for example, Mr. Tower's results, at 262 ft, per minute:

Temp. F.	110°	100°	90°	80°	70°	60°
Observed Calculated	.0044	.0051 .00518	.006	.0073 .00733	.0092 .00964	.0119 .01252

This law does not hold good for pad or siphon lubrication, as then the coefficient of friction diminishes more rapidly for given increments of temperature, but on a gradually decreasing scale, until the normal temperature has been reached; this normal temperature increases directly as the load per sq in. This is shown in the following table taken from Mr. Stroudley's experiments with a pad of rape oil:

Coefficient Decrease of coeff	.022	.0180	.0160	.0140 0020	.0125 .0015	.0115 .0010	.0110 .0005	.0106	.0102 .0002

In the Galton-Westinghouse experiments it was found that with velocities below 100 ft. per min., and with low pressures, the frictional resistance varied directly as the normal pressure; but when a velocity of 100 ft. per min. was exceeded, the coefficient of friction greatly diminished; from the same experiments Prof. Kennedy found that the coefficient of friction for high pressures was sensibly less than for low.

Allowable Pressures on Bearing-surfaces. (Proc. Inst. M. E., May, 1888.)—The Committee on Friction experimented with a steel ring of

rectargular section, pressed between two cast-iron disks, the annular bearing-surfaces of which were covered with gun-metal, and were 12 in inside ling-suffraces of which were covered with guir-inetal, and were term, moute diameter and 14 in, outside. The two disks were rotated together, and the steel ring was prevented from rotating by means of a lever, the holding force of which was measured. When olled through grooves cut in each face of the ring and tested at from 50 to 130 revs. per min., it was found that a pressure of 75 lbs. per sq. in. of bearing-surface was as much as it would bear safely at the highest speed without seizing, although it carried 90 lbs. per sq. in. at the lowest speed. The coefficient of friction is also much higher than for a cylindrical bearing, and the friction follows the law of the friction of solids much more nearly than that of liquids. This is doubtless due to the much less perfect lubrication applicable to this form of bearing compared with a cylindrical one. The coefficient of friction appears to be about the same with the same load at all speeds, or, in other words, to be independent of the speed; but it seems to diminish somewhat as the load is increased, and may be stated approximately as 1/20 at 15 lbs. per sq. in., diminishing to 1/30 at 75 lbs. per sq. in.

The high coefficients of friction are explained by the difficulty of lubricating a collar-bearing. It is similar to the slide-block of an engine, which can carry only about one tenth the load per sq. in. that can be carried by the

crank-pins.

In experiments on cylindrical journals it has been shown that when a cylindrical journal was lubricated from the side on which the pressure bore, 100 lbs. per sq. in. was the limit of pressure that it would carry; but when it came to be lubricated on the lower side and was allowed to drag the oil in with it, 600 lbs. per sq. in. was reached with impunity; and if the 600 lbs. per sq. in., which was reckoned upon the full diameter of the bearing, came to be reckoned on the sixth part of the circle that was taking the greater proportion of the load, it followed that the pressure upon that part of the circle amounted to about 1200 lbs. per sq. in.

In connection with these experiments Mr. Wicksteed states that in drilling-machines the pressure on the collars is frequently as high as 336 lbs. per sq. in., but the speed of rubbing in this case is lower than it was in any of the experiments of the Research Committee. In machines working very slowly and intermittently, as in testing-machines, very much higher pres-

sures are admissible.

Mr. Adamson mentions the case of a heavy upright shaft carried upon a small footstep-bearing, where a weight of at least 20 tons was carried on a sman rootstep-oearing, where a weight of at least 20 tons wijs carried on a shaft of 5 in. diameter, or, say, 20 sq. in, area, giving a pressure of 1 ton per sq. in. The speed was 190 to 200 revs. per min. It was necessary to force the oil under the bearing by means of a pump. For heavy horizontal shafts, such as a fly-wheel shaft, carrying 100 tons on two journals, his practice for getting oil into the bearings was to flatten the journal along one side throughout its whole length to the extent of about an eighth of an inch in width for each inch in diameter, along the great pather. width for each inch in diameter up to 8 in. diameter; above that size rather less flat in proportion to the diameter. At first sight it appeared alarming to get a continuous flat place coming round in every revolution of a heavily loaded shaft; yet it carried the oil effectually into the bearing, which ran much better in consequence than a truly cylindrical journal without a flat

In thrust-bearings on torpedo-boats Mr. Thornycroft allows a pressure of

never more than 50 lbs. per sq. in.

Prof. Thurston (Friction and Lost Work, p. 240) says 7000 to 9000 lbs. pressure per square inch is reached on the slow-working and rarely-moved pivots of swing bridges.

Mr. Tower says (Proc. Inst. M. E., Jan. 1884): In eccentric-pins of punching and shearing machines very high pressures are sometimes used without

seizing. In addition to the alternation in the direction, the pressure is applied for only a very short space of time in these machines, so that the oil has no time to be squeezed out.

In the discussion on Mr. Tower's paper (Proc. Inst. M. E. 1885) it was stated that it is well known from practical experience that with a constant load on an ordinary journal it is difficult and almost impossible to have more than 200 lbs. per square inch, otherwise the bearing would get hot and the oil go out of it; but when the motion was reciprocating, so that the load was alternately relieved from the journel, as with crank-pins and similar journals, much higher loads might be applied than even 700 or 800 lbs. per square inch.

Mr. Goodman (Proc. Inst. C. E. 1886) found that the total frictional resistance is materially reduced by diminishing the width of the brass.

The lubrication is most efficient in reducing the friction when the brass subtends an angle of from 120° to 60°. The film is probably at its best be-

tween the angles 80° and 110°.

In the case of a brass of a railway axle-bearing where an oil-groove is cut along its crown and an oil-hole is drilled through the top of the brass into it, the wear is invariably on the off side, which is probably due to the oil escaping as soon as it reaches the crown of the brass, and so leaving the off side almost dry, where the wear consequently ensues.

In railway axles the brass wears always on the forward side. The same observation has been made in marine engine journals, which always wear in exactly the reverse way to what they might be expected. Mr. Stroudley thinks this peculiarity is due to a film of lubricant being drawn in from the under side of the journal to the aft part of the brass, which effectually lubricates and prevenis wear on that side; and that when the lubricant reaches

the forward side of the brass it is so attenuated down to a wedge shape that there is insufficient lubrication, and greater wear consequently follows.

there is insufficient lubrication, and greater wear consequently follows. Prof. J. E. Denton (Am. Much., Oct. 30, 1890) says: Regarding the pressure to which oil is subjected in railroad car-service, it is probably more severe than in any other class of practice. Car brasses, when used bare, are so imperfectly fitted to the journal, that during the early stages of their use the area of bearing may be but about one square inch. In this case the pressure per square inch is upwards of 6000 lbs. But at the slowest speeds of freight service the wear of a brass is so rapid that, within about thirty minutes the area is either increased to about three inches, and is thereby able to relieve the oil so that the latter can successfully prevent overheating of the journal, or else overheating takes place with any oil, and measures of relief must be taken which eliminate the question of differences of lubricating power among the different lubricants available. A brass which has been run about fifty miles under 5000 lbs. load may have extended the area of bearing-surface to about three square inches. The pressure is then about 1700 lbs. per square inch. It may be assumed that this is an average minimum area for car-service where no violent and unmanageable overheating has occurred during the use of a brass for a short time. This area will very slowly increase with any lubricant.

C. J. Field (Power, Feb. 1839) says: One of the most vital points of an engine for electrical service is that of main bearings. They should have a surface velocity of not exceeding 350 feet per minute, with a mean bearing pressure per square inch of projected area of journal of not more than 80 lbs. This is considerably within the safe limit of cool performance and easy operation. If the bearings are designed in this way, it would admit the use of grease on all the main wearing-surface, which in a large type of engines

for this class of work we think advisable.

Oil-pressure in a Bearing,—Mr. Beauchamp Tower (Proc. Inst. M. E. Jan. 1885) made experiments with a brass bearing 4 inches diameter by 6 inches long, to determine the pressure of the oil between the brass and the journal. The bearing was half immersed in oil, and had a total load of 8008 lbs. upon it. The journal rotated 150 revolutions per minute. The pressure of the oil was determined by drilling small holes in the bearing at different points and connecting them by tubes to a Bourdon gauge. It was found that the pressure varied from 310 to 625 lbs, per square inch. the greatest pressure being a little to the "off" side of the centre line of the top of the bearing, in the direction of motion of the journal. The sum of the upward force exerted by these pressures for the whole lubricated area was nearly equal to the total pressure on the bearing. The speed was reduced from 150 to 20 revolutions, but the oil-pressure remained the same, showing that the brass was as completely oil-borne at the lower speed:

The nominal load per square inch is the total load divided by the product of the diameter and length of the journal. At the same low speed of 20 revolutions per minute it was increased to 676 lbs. per square inch without any signs of heating or seizing.

Friction of Car-journal Brasses. (J. E. Denton, Trans. A. S. M. E., xii. 405.)—A new brass dressed with an emery-wheel, loaded with 5000 lbs., may have an actual bearing-surface on the journal, as shown by the polish

of a portion of the surface, of only 1 square inch. With this pressure of 5000 lbs, per square inch, the coefficient of friction may be 6%, and the brass may be overheated, scarred and cut but, on the contrary, it may wear down evenly to a smooth bearing, giving a highly polished area of contact of 3 square inches, or more, inside of two hours of running, gradually decreasing the pressure per square inch of contact, and a coefficient of friction of less than 0.5%. A reciprocating motion in the direction of the axis is of importance in reducing the friction. With such polished surfaces any oil will lubricate, and the coefficient of friction then depends on the viscosity of the oil. With a pressure of 1000 lbs per square inch, revolutions from 170 to 320 per minute, and temperatures of 75 to 113° F. with both sperm and parraffine oils, a coefficient of as low as 0.11% has been obtained, the oil being fed continuously by a pad.

Experiments on Overheating of Bearings,—Hot Hoxes, (Denton.)—Tests with car brasses loaded from 1100 to 4500 lbs. per square inch gave 7 cases of overheating out of 32 trials. The tests show how purely a matter of chance is the overheating, as a brass which ran hot at 5000 lbs. load on one day would run cool on a later date at the same or higher pressure. The explanation of this apparently arbitrary difference of behavior is that the accidental variations of the smoothness of the surfaces, almost infinitesimal in their magnitude, cause variations of friction which are always tending to produce overheating, and it is solely a matter of chance when these tendencies preponderate over the lubricating influence of the oil. There is no appreciable advantage shown by sperm-oil, when there is no tendency to overheat—that is, parafilm can lubricate under the highest pressures which occur, as well as sperm, when the surfaces are within the conditions affording the minimum coefficients of friction.

Sperm and other oils of high heat-resisting qualities, like vegetable oil and petroleum cylinder stocks, only differ from the more volatile lubricants, like paraffine, in their ability to reduce the chances of the continual acci-

dental infinitesimal abrasion producing overheating.

The effect of emery or other gritty substance in reducing overheating of a

bearing is thus explained:

The effect of the emery upon the surfaces of the bearings is to cover the latter with a series of parallel grooves, and apparently after such grooves are made the presence of the emery does not practically increase the friction over the amount of the latter when pure oil only is between the surfaces. The infinite number of grooves constitute a very perfect means of insuring a uniform oil supply at every point of the bearings. As long as grooves in the journal match with those in the brasses the friction appears to amount to only about 10% to 15% of the pressure. But if a smooth journal is placed between a set of brasses which are grooved, and pressure be applied, the journal crushes the grooves and becomes brazed or coated with brass, and then the coefficient of friction becomes upward of 40%. If then emery is applied, the friction is made very much less by its presence, because the grooves are made to match each other, and a uniform oil supply prevails at every point of the bearings, whereas before the application of the emery many spots of the latter receive no oil between them.

### Moment of Friction and Work of Friction of Slidingsurfaces, etc.

	Moment of Fric- tion, inch-lbs.	Energy lost by Friction in ftlbs. per min.
Flat surfaces	1/2 f W d 2/3 f W r	fWS .2618 $fWdn$
Flat pivots		.1745 fWrn
Collar-bearing	$\frac{2}{3} f W \frac{r_2^3 - r_1^3}{r_2^2 - r_1^2}$	$.1745 fWn \frac{r_2^3 - r_1^3}{r_2^2 - r_1^2}$
Conical pivot	$\frac{2}{3}fWr$ cosec $a$ $\frac{2}{3}fWr$ sec $a$	.1745 $fWrn$ cosec $a$ .1745 $fWrn$ sec $a$
Truncated-cone pivot	$\frac{2}{3}fW\frac{r_2^3-r_1^3}{r_2\sin a}$	$.1745 f W \frac{r_2^3 - r_1^3}{r_2 \sin \alpha}$
Hemispherical pivot Tractrix, or Schiele's "anti-	fWr	.2618 fWr
friction " pivot	fWr	.2618fWr.

In the above f = coefficient of friction; W = weight on journal or pivot in pounds;

r = radius, d = diameter, in inches;

 $r = \text{radius}, t = \text{diameter}, \text{ in incres}, \\ S = \text{space in feet through which sliding takes place}; \\ r_2 = \text{outer radius}, r_1 = \text{inner radius}; \\ n = \text{number of revolutions per minute};$ 

a = the half-angle of the cone, i.e., the angle of the slope

with the axis.

To obtain the horse-power, divide the quantities in the last column by

33,090. Horse-power absorbed by friction of a shaft =  $\frac{fWdn}{126050}$ The formula for energy lost by shafts and journals is approximately true

for loosely fitted bearings. Prof. Thurston shows that the correct formula varies according to the character of fit of the bearing; thus for loosely fitted journals, if U = the energy lost,

$$U = \frac{2f\pi r}{\sqrt{1+f^2}}Wn \text{ inch-pounds} = \frac{.2618fWdn}{\sqrt{1+f^2}} \text{ foot-lbs.}$$

For perfectly fitted journals  $U=2.54/\pi rWn$  inch-lbs. = .3325fWdn, ft.-lbs. For a bearing in which the journal is so grasped as to give a uniform pressure throughout,  $U=f\pi^2 FWn$  inch-lbs. = .4112 fWdn, ft.-lbs. Resistance of railway trains and wagons due to friction of trains:

Pull on draw-bar =  $\frac{f \times 2240}{R}$  pounds per gross ton,

in which R is the ratio of the radius of the wheel to the radius of journal. A cylindrical journal, perfectly fitted into a bearing, and carrying a total load, distributes the pressure due to this load unequally on the bearing, the maximum pressure being at the extremity of the vertical radius, while at the extremities of the horizontal diameter the pressure is zero. At any point of the bearing-surface at the extremity of a radius which makes an angle  $\theta$  with the vertical radius the normal pressure is proportional to  $\cos \theta$ . If p = normal pressure on a unit of surface, w = total load on a unit oflength of the journal, and r = radius of journal,

$$w\cos\theta = 1.57rp, \quad p = \frac{w\cos\theta}{1.57r}.$$

#### PIVOT-BEARINGS.

The Schiele Curve.-W. H. Harrison, in a letter to the Am. Machin-The Schiele Curve,—W. H. Harrison, in a letter to the Am. Machinist, 1891, says the Schiele curve is not as good a form for a bearing as the segment of a sphere. He says: A mill-stone weighing a ton frequently bears its whole weight upon the flat end of a hard-steel pivot 1½" diameter, or one square inch area of bearing; but to carry a weight of 3000 lbs. he advises an end bearing about 4 inches diameter, made in the form of a segment of a sphere about ½ inch in height. The die or fixed bearing should be dished to fit the pivot. This form gives a chance for the bearing to adjust itself, which it does not have when made flat, or when made with the Schiele curve. If a side bearing is necessary it can be arranged farther up the shaft. The pivot and die should be of steel, hardened; cross-gutters should be in the die to allow oil to flow and a central collable should be should be in the die to allow oil to flow, and a central oil-hole should be made in the shaft.

The advantage claimed for the Schiele bearing is that the pressure is uniformly distributed over its surface, and that it therefore wears uniformly. Wilfred Lewis (Am. Mach., April 19, 1894) says that its merits as a thrust-bearing have been vastly overestimated; that the term "anti-friction" applied to it is a misnomer, since its friction is greater than that of a flat step or collar of the same diameter. He advises that flat thrust-bearings should always be annular in form, having an inside diameter one half of the external diameter

Friction of a Flat Pivot-bearing.—The Research Committee on Friction (Proc. Inst. M. E. 1891) experimented on a step-bearing, flatended, 3 in. diam. the oil being forced into the bearing through a hole in its centre and distributed through two radial grooves, insuring thorough lubrication. The step was of steel and the bearing of manganese-bronze.

At revolutions per min	. 50	128	194	290	353
The coefficient of friction varied	.0181	.0053	.0051	.0044	.0053
between	and .0221	.0113	.0102	.0178	.0167

With a white-metal bearing at 128 revolutions the coefficient of friction was a little larger than with the manganese-bronze. At the higher speeds the coefficient of friction was less, owing to the more perfect lubrication, as shown by the more rapid circulation of the oil. At 128 revolutions the bronze bearing heated and seized on one occasion with a load of 260 pounds and on another occasion with 300 pounds per square inch. The white-metal bearing under similar conditions heated and seized with a load of 240 pounds per square inch. The steel footstep on manganese-bronze was afterwards tried, lubricating with three and with four radial grooves; but the friction was from one and a half times to twice as great as with only the two

grooves. (See also Allowable Pressures, page 936.)

Mercury-bath Pivot. —A nearly frictionless step-bearing may be obtained by floating the bearing with its superincumbent weight upon mercury. Such an apparatus is used in the lighthouses of La Heve, Havre. It

is thus described in Eng'g, July 14, 1893, p. 41:

The optical apparatus, weighing about 1 ton, rests on a circular cast-iron table, which is supported by a vertical shaft of wrought iron 2.36 in.

diameter.

This is kept in position at the top by a bronze ring and outer iron support. and at the bottom in the same way, while it rotates on a removable steel pivot resting in a steel socket, which is fitted to the base of the support. To the vertical shaft there is rigidly fixed a floating cast-iron ring 17.1 in. diam ter and 1.8 in. In depth, which is plunged into and rotates in a mercury bath contained in a fixed outer drum or tank, the clearance between the vertical surfaces of the drum and ring being only 0.2 in., so as to reduce as much as possible the volume of niercury (about 220 lbs.), while the horizontal clearance at the bottom is 0.4 in.

# BALL-BEARINGS, FRICTION ROLLERS, ETC.

A. H. Tyler (Eng'g, Oct. 20, 1893, p. 483), after experiments and comparison with experiments of others arrives at the following conclusions:

That each ball must have two points of contact only.
The balls and race must be of glass hardness, and of absolute truth.
The balls should be of the largest possible diameter which the space at

disposal will admit of. Any one ball should be capable of carrying the total load upon the bearing.

Two rows of balls are always sufficient.

A ball-bearing requires no oil, and has no tendency to heat unless overloaded.

Until the crushing strength of the balls is being neared, the frictional re-

sistance is proportional to the load.

The frictional resistance is inversely proportional to the diameter of the balls, but in what exact proportion Mr. Tyler is unable to say. Probably it varies with the square.

The resistance is independent of the number of balls and of the speed. No rubbing action will take place between the balls, and devices to guard

against it are unnecessary, and usually injurious.

The above will show that the ball-bearing is most suitable for high speeds and light loads. On the spindles of wood-carring machine some make as much as 30,000 revolutions per minute. They run perfectly cool, and never have any oil upon them. For heavy loads the balls should not be less than two thirds the diameter of the shaft, and are better if made equal to it.

Ball-bearings have not been found satisfactory for thrust-blocks, for

the reason apparently that the tables crowd together. Better results have been obtained from coned rollers. A combined system of rollers and balls

is described in Eng'o, Oct. 6, 1893, p. 429.

Friction-rollers. — If a journal instead of revolving on ordinary bearings be supported on friction-rollers the force required to make the journal revolve will be reduced in nearly the same proportion that the diameter nal revolve will be reduced in nearly the same proportion that the diameter of the axies of the rollers is less than the diameter of the rollers themselves. In experiments by A. M. Wellington with a journal 3½ in, diam, supported on rollers 8 in, diam., whose axies were 1½ in, diam., the friction in starting from rest was ½ the friction of an ordinary 3½-in, bearing, but at a car speed of 10 miles per hour it was ½ that of the ordinary bearing. The ratio of the diam, of the axie to diam, of roller was 1¾:8, or as 1 to 4.6.

Bearings for Very High Rotative Speeds. (Proc. Inst. M. E., Oct. 1888, p. 482.)—In the Parsons steam-turbine, which has a speed of as high as 18,000 iev. per min., as it is impossible to secure absolute accuracy of balance, the bearings are of special construction so as to allow of a certain very small amount of lateral freedom. For this purpose the bearing is sur-rounde I by two sets of steel washers 1/16 inch thick and of different diamters, the larger fitting close in the casing and about 1/32 inch clear of the bearing, and the smaller fitting close on the bearing and about 1/32 inch clear of the casing. These are arranged alternately, and are pressed together by a spiral spring. Consequently any lateral movement of the bearing causes them to slide mutually against one another, and by their friction to check or damp any vibrations that may be set up in the spindle. The tendency of the spindle is then to rotate about its axis of mass, or principal axis as it is called; and the bearings are thereby relieved from excessive pressure, and the machine from undue vibration. The finding of the centre of gyration, or rather allowing the turbine itself to find its own centre of gyration, is a well-known device in other branches of mechanics: as in the instance of the centrifugal hydro-extractor, where a mass very much out of balance is allowed to find its own centre of gyration; the faster it ran the more steadily did it revolve and the less was the vibration. Another illustration is to be found in the spindles of spinning machinery, which run at about 10,000 or 11,000 revolutions per minute: they are made of hardened and tempered steel, and although of very small dimensions, the outside diameter of the largest portion or driving whorl being perhaps not more than 1½ in., it is found impracticable to run them at that speed in what might be called a hard-and-fast bearing. They are therefore run with some elastic substance surrounding the bearing, such as steel springs, hemp, or cork. Any elastic substance is sufficient to absorb the vibration, and permit of absolutely steady running.

# FRICTION OF STEAM-ENGINES.

Distribution of the Friction of Engines.-Prof. Thurston in h's "Friction and Lost Work," gives the following:

· ·	1.	2.	3.
Main bearings	47.0	35.4	35.0
Piston and rod	32.9	25.0	21.0
Crank-pin	6.8	5.1)	13.0
Cross-head and wrist-pin	5.4	4.1	10.0
Valve and rod	2.5	26.4)	22.0
Eccentric strap	- 5.3	4.0 \$	
Link and eccentric			9.01
Total			
	100.0	100.0	100.0

No. 1, Straight-line,  $6'' \times 12''$ , balanced valve; No. 2, Straight-line,  $6'' \times 12''$ , unbalanced valve; No. 3,  $7'' \times 10''$ , Lansing traction locomotive valve-gear. Prof. Thurston's tests on a number of different styles of engines indicate that the friction of any engine is practically constant under all loads.

(Trans. A. S. M. E., vill. 86; 18. 74", I.H.P. from 7.41 to 57.54, the friction H. P. varied irregularly between 1.97 and 4.02, the variation being independent of the load. With 50 H.P. on the brake the I.H.P. was only 52.6, the friction being only 2.6 H.P., or about 52.

In a compound condensing engine, tested from 0 to 102.6 brake H.P., gave H.P. from 14.92 to 117.8 H.P., the friction H.P. varying only from 14.92 to 17.42. At the maximum load the friction was 15.2 H.P., or 12.9%.

The friction increases with increase of the boiler-pressure from 30 to 70 bls., and then becomes constant. The friction generally increases with in-

crease of speed, but there are exceptions to this rule. Prof. Denton (Stevens Indicator, July, 1890), comparing the calculated friction of a number of engines with the friction as determined by measurement, finds that in one case, a 75-ton ammonia ice-machine, the friction of the compressor, 171/2 H.P., is accounted for by a coefficient of friction of 71/28 on all the external bearings, allowing % of the entire friction of the machine for the friction of pistons, stuffing-boxes, and valves. In the case of the Pawtucket pumping-engine, estimating the friction of the external bearings with a coefficient of friction of 6% and that of the pistons, valves, and stuffing-boxes as in the case of the ice-machine, we have the total friction

distributed as follows:

	Horse- power.	Per cent of Whole
Crank-pins and effect of piston-thrust on main shaft. Weight of fly-wheel and main shaft	1.95	11.4 32.4
Steam-valves Eccentric Pistons	0.07	$\frac{3.7}{1.2}$
Stuffing-boxes, six altogether Air-pump	0.72	$\frac{11.3}{32.8}$
Total friction of engine with load		100.0

The friction of this engine, though very low in proportion to the indicated power, is satisfactorily accounted for by Morin's law used with a coefficient of friction of 5%. In both cases the main items of friction are those due to the weight of the fly-wheel and main shaft and to the piston-thrust or crank-pins and main-shaft bearings. In the ice-machine the latter items are the larger owing to the extra crank pin to work the pumps, while in the Pawtucket engine the former preponderates, as the crank-thrusts are partly absorbed by the pump-pistons, and only the surplus effect acts on the crank-shaft.

Prof. Denton describes in Trans. A. S. M. E., x. 392, an apparatus by which he measured the friction of a piston packing-ring. When the parts of the piston were thoroughly devoid of lubricant, the coefficient of friction was found to be about 7½%; with an oil-feed of one drop in two minutes the coefficient was about 5½; with one drop per minute it was about 3½. These rates of feed gave unsatisfactory lubrication, the piston groaning at the ends of the stroke when run slowly, and the flow of oil left upon the surfaces was found by analysis to contain about 55% of iron. A feed of two drops per minute reduced the coefficient of friction to about 1½, and gave practically perfect lubrication, the oil retaining its natural color and purity.

### LUBRICATION.

Measurement of the Durability of Lubricants, (J. E. Denton, Trans. A. S. M. E., xi. 1013.)-Practical differences of durability of lubricants depend not on any differences of inherent ability to resist being "worn out" by rubbing, but upon the rate at which they flow through and away from the bearing surfaces. The conditions which control this flow are so delicate in their influence that all attempts thus far made to measure durability of lubricants may be said to have failed to make distinctions of lubricating value having any practical significance. In some kinds of service the limit to the consumption of oil depends upon the extent to which dust or other refuse becomes mixed with it, as in railroad-car lubrication and in the case of agricultural machinery. The economy of one oil over another, so far as the quality used is concerned—that is, so far as durability is concerned—is simply proportional to the rate at which it can insinuate itself into and flow out of minute orifices or cracks. Oils will differ in their ability to do this, first, in proportion to their viscosity, and, second, in proportion to the ca-pillary properties which they may possess by virtue of the particular ingre-dients used in their composition. Where the thickness of film between rub-bing-surfaces must be so great that large amounts of oil pass through bearings in a given time, and the surroundings are such as to permit oil to be fed at high temperatures or applied by a method not requiring a perfect fluidity, it is probable that the least amount of oil will be used when the viscosity is as great as in the petroleum cylinder stocks. When, however, the oil must flow freely at ordinary temperatures and the feed of oil is restricted, as in the case of crank-pin bearings, it is not practicable to feed

such heavy oils in a satisfactory manner. Oils of less viscosity or of a fluidity approximating to lart-oil must then be used.

Relative Value of Lubricants. (J. E.Denton, Am. Mach., Oct. 30, 1890,—The three elements which determine the value of a lubricant are the cost due to consumption of lubricants, the cost spent for coal to overcome the frictional resistance caused by use of the lubricant, and the cost due to the metallic wear on the journal and the brasses. In cotton-mills the cost of the power is alone to be considered; in rolling-mills and marine engines the cost of the quantity of lubricant used is the only important factor; lut in railroads not only do both these elements enter the problem as tangible

factors, but the cost of the wearing away of the metallic parts enters in ad-

factors, but the cost of the wearing away of the metanic parts enters in a difficing and furthermore, the latter is the greatest element of cost in the case.

The Qualifications of a Good Lubricant, as laid down by M. H. Bailey, in Proc. Inst. C. E., vol. xlv., p. 372, are: 1. Sufficient body to keep the surfaces free from contact under maximum pressure, 2. The careatest possible fluidity consistent with the foregoing condition. 3. The reatest possible fluidity consistent with the foregoing condition. 3. The lowest possible coefficient of friction, which in bath lubrication would be for fluid friction approximately. 4. The greatest capacity for storing and carrying away heat. 5. A high temperature of decomposition. 6. Power to resist oxidation or the action of the atmosphere. 7. Freedom from corrosive action on the metals upon which used.

# Best Lubricants for Different Purposes. (Thurston.)

Low temperatures, as in rock-drills { Light mineral lubricating-oils. driven by compressed air: Graphite, soapstone, and other solid Very great pressures, slow speed ... lubricants. The above, and lard, tallow, and other Heavy pressures, with slow speed ... { Heavy pressures and high speed.... Sperm-oil, castor-oil, and heavy mineral oils. Light pressures and high speed.... Sperm, refined petroleum, olive, rape, Lard-oil, tallow-oil, heavy mineral oils, Ordinary machinery .... and the heavier vegetable oils. Steam-cylinders..... . Heavy mineral oils, lard, tallow. Watches and other delicate mecha- | Clarified sperm, neat's-foot, porpoise. olive, and light mineral lubricating nism:

For mixture with mineral oils, sperm is best; lard is much used; olive and cotton-seed are good.

oils.

cotton-seed are good.

Amount of Oil needed to Ran an Engine,—The Vacuum Oil
Co. in 1892, in response to an inquiry as to cost of oil to run a 1000-H.P.
Corliss engine, wrote: The cost of running two engines of equal size of the
same make is not always the same. Therefore while we could furnish
figures showing what it is costing some of our customers having Corliss
engines of 1000 H.P., we could only give a general idea, which in itself
might be considerably out of the way as to the probable cost of cylinderand engine-oils per year for a particular engine. Such an engine ought to
run readily on less than 8 days of 600 oil per minner. If 3000 drops are
two and one half barrels (825 gallons) of 600 W cylinder-oil, at 65 cents per
evolution of a point 885 for cylinder-oil per year, running 6 days a week and 10 two and one had barres (see gamons) of now a crimeter on, as we can be gallon, or about \$85 for cylinder-oll per year, running 6 days a week and 10 hours a day. Engine-oil would be even more difficult to guess at what the cost would be, because it would depend upon the number of cups required on the engine, which varies somewhat according to the style of the engine. It would doubtless be safe, however, to calculate at the outside that not more than twice as much engine-oil would be required as of cylinder-oil,

The Vacuum Oil Co, in 1892 published the following results of practice

with "600 W" cylinder-oil:

Corliss compound engine, 20 and 33 × 48; 83 revs. per min.; 1 drop of oil triple exp.

| Quanta 5/2 45, 55 revs. per limit, 1 drop of on | Quanta 5/2 45, 5 revs. per limit, 2 drops of oil | Quanta 6/2 85; 1 drop every 2 mint, 2 drops of oil | Quanta 6/2 85; 143 revs. per mint, 2 drop per min, reduced afterwards to 1 drop per min | 15/2 25/2 15; 240 revs. per mint, 1 drop every 4 Porter-Allen Ball minutes.

Results of tests on ocean-steamers communicated to the author by Prof. Denton in 1892 gave: for 1200-H.P. marine engine, 5 to 6 English gallons (6 to 7.2 U. S. gals.) of engine-oil per 24 hours for external lubrication; and for a 1500-H.P. marine engine, triple expansion, running 75 revs. per min., 6 to 7 English gals, per 24 hours. The cylinder-oil consumption is exceedingly variable,—from 1 to 4 gals, per day on different engines, including cylinder-

oil used to swab the piston-rods.

Quantity of Oil used on a Locomotive Crank-pin.—Prof.
Denton. Trans. A. S. M. E., xi, 1020, says: A very economical case of practical
oil-consumption is when a locomotive main crank-pin consumes about six

cubic inches of oil in a thousand miles of service. This is equivalent to a consumption of one milligram to seventy square inches of surface rubbed

The Examination of Lubricating-oils. (Prof. Thos. B. Stillman, Stevens Indicator, July, 1890.)—The generally accepted conditions of a good lubricant are as follows: 1. "Body" enough to prevent the surfaces, to which it is applied, from

coming in contact with each other. (Viscosity.)

Freedom from corrosive acid, either of mineral or animal origin.
 As fluid as possible consistent with "body."

A minimum coefficient of friction.
 High "flash" and burning points.

6. Freedom from all materials liable to produce oxidation or "gumming." The examinations to be made to verify the above are both chemical and mechanical, and are usually arranged in the following order:

1. Identification of the oil, whether a simple mineral oil, or animal oil, or a mixture. 2. Density. 3. Viscosity. 4. Flash-point. 5. Burning-point. 6. Acidity. 7. Coefficient of friction. 8. Cold test.

Detailed directions for making all of the above tests are given in Prof.

Stillman's article

Weights of Oil per Gallon .- The following are approximately the

weights per gallon of different kinds of oil (Penn. R. R. Specifications): Lard-oil, tallow-oil, neat's-foot oil, bone-oil, colza-oil, mustard-seed oil, rape-seed oil, paraffine-oil, 500° fire-test oil, engine-oil, and cylinder lubricant,

7½ pounds per gallon. Well-oil and passenger-car oil, 7.4 pounds per gallon; navy sperm-oil, 7.2 pounds per gallon; signal-oil, 7.1 pounds per gallon; 300° burning-oil, 6.9

pounds per gallon; and 150° burning oil, 6.6 pounds per gallon.

Penna. R. R. Specifications for Petroleum Products.

1889.—Five different grades of petroleum products will be used.

The materials desired under this specification are the products of the dis-

tillation and refining of petroleum unnixed with any other substances. 150° Fire-test Oit.—This grade of oil will not be accepted if sample (1) is not "water-white" in color; (2) flashes below 150° Fahrenheit; (3) burns below 151° Fahrenheit; (4) is cloudy or shipment has cloudy barrels when received, from the presence of glue or suspended matter; (5) becomes opaque or shows cloud when the sample has been 10 minutes at a temperature of 0° Fahrenheit.

The flashing and burning points are determined by heating the oil in an open vessel, not less than 120 per minute, and applying the test flame every 70, beginning at 1230 Fahrenheit. The cold test may be conveniently made by having an ounce of the oil, in a four-onnee sample bottle, with a thermometer suspended in the oil, and exposing this to a freezing mixture of ice and salt. It is advisable to stir with the thermometer while the oil is

to and sait. It is advisable to sur with the thermometer while the oil is cooling. The oil must remain transparent in the freezing mixture ten minutes after it has cooled to zero.

300° Fire-lest Oil.—This grade of oil will not be accepted if sample (1) is not "water white" in color; (2) flashes below 249° Fabrenheit; (3) burns below 249° Fabrenheit; (4) is cloudy or shipment has cloudy barrels when received, from the presence of glue or suspended matter; (5) becomes opaque or shows cloud when the sample has been 10 minutes at a temper-

ature of 32° Fahrenheit.

The flashing and burning points are determined the same as for 150° fire-test oil, except that the oil is heated 15° per minute, test-flame being applied first at 21° Fahrenheit. The cold test is made the same as above, except

that ice and water are used.

Paraffine-oil .- This grade of oil will not be accepted if the sample (1) is Transfer-on.—Ins. grade of our more than 65 seconds when tested as viscosity less than 40 seconds or more than 65 seconds when tested as described under "Well Oil" at 100° Fahrenheit throughout the year; (4) has gravity at 60° Fahrenheit, below 24° Baumé, or above 29° Baumé; (5) from October 1st to May 1st has a cold test above 10° Fahrenheit.

The flashing-point is determined same as for 300° fire-test oil. The cold test is determined as follows: A couple of onness of oil is put in a four-onnes sample bottle, and a thermometer placed in it. The oil is then frozen, a freezing mixture of ice and salt being used if necessary. When the oil has become hard, the bottle is removed from the freezing mixture and the frozen oil allowed to soften, being stirred and the foreign mixture and the time by means of the thermometer, until the mass will run from one end of

the bottle to the other. The reading of the thermometer when this is the

case is regarded as the cold test of the oil,

Well Oil, This grade of oil will not be accepted if the sample (1) flashes, Well Oil.—This grade of on will not be accepted if the sample (1) lassies, from May 1st to October 1st, telow 249° Fahrenheit, of from October 1st to May 1st below 200° Fahrenheit; (2) has a gravity, at 60° Fahrenheit, below 28° Baumé, or above 30°; (3) from October 1st to May 1st has a cold test above 10° Fahrenheit; (4) shows any precipitation in 10 minutes when 5 cubic centimetres are mixed with 55 cubic centimetres of 85° gasoline; (5) shows a viscosity less than 55 seconds, or more than 100 seconds, when tested as described below. From October 1st to May 1st the test must be made at 100° Fahrenheit, and from May 1st to October 1st at 110° Fahrenheit.

For summer oil the flashing-point is determined the same as for paraffineoil; and for winter oil the same, except that the test-flame is applied first

at 193° Fahrenheit. The cold test is made the same as for parafine oil.

The precipitation test is to exclude tarry and suspended matter. It is easiest made by putting 5 cubic centimetres of the oil in a 100-cubic-centimetre graduate, then filling to the mark with gasoline, and thoroughly shaking

The viscosity test is made as follows: A 100 cubic-centimetre pipette of the long bulb form is regraduated to hold just 100 cubic centimetres to the bottom The size of the aperture at the bottom is then made such that 100 cubic centimetres of water at 100° Fahrenheit will run out the pipette down to the bottom of the bulb in 34 seconds. Pipettes with bulbs varying from 135 inches to 1½ inches in diameter outside, and about 4½ inches long give almost exactly the same results, provided the aperture at the bottom is the proper size. The pipette being obtained, the oil sample is heated to the required temperature, care being taken to have it uniformly heated, and then is drawn up into the pipette to the proper mark. The time occupied by the oil in running out, down to the bottom of the bulb, gives the test figures.

500° Fire-test Oil.—This grade of oil will not be accepted if sample (1) flashes below 445° Fahrenheit; (2) shows precipitation with gasoline when

tested as described for well-oil.

The flashing-point is determined the same as for well-oil, except that the test flame is applied first at 438° Fahrenheit.

#### SOLID LUBRICANTS.

Graphite in a condition of powder and used as a solid lubricant, so called, to distinguish it from a liquid lubricant, has been found to do well

where the latter has failed.

where the latter has faued.

Rennie, in 1829, says: "Graphite lessened friction in all cases where it was used." General Morin, at a later date, concluded from experiments that it could be used with advantage under heavy pressures; and Prof. Thurston found it well adapted for use under both light and heavy pressures when mixed with certain oils. It is especially valuable to prevent abrasion and cutting under heavy loads and at low velocities.

Soapstone, also called talc and steatite, in the form of powder and mixed with oil or fat, is sometimes used as a lubricant. Graphite or soapstone, mixed with soap, is used on surfaces of wood working against either

iron or wood.

Fibre-graphite.—A new self-lubricating bearing known as fibre-graphite is described by John H. Cooper in Trans. A. S. M. E., xiii. 374, as the invention of P. H. Holmes, of Gardiner, Me. This bearing material is composed of selected natural graphite, which has been finely divided and freed from foreign and gritty matter, to which is added wood-fibre or other growth mixed in water in various proportions, according to the purpose to be served, and then solidified by pressure in specially prepared moulds; after removal from which the bearings are first thoroughly dried, then saturated with a drying oil, and finally subjected to a current of hot, dry air for the purpose of oxidizing the oil, and hardening the mass. When finished they may be "machined" to size or shape with the same facility and means employed on metals.

Metaline is a solid compound, usually containing graphite, made in the form of small cylinders which are fitted permanently into holes drilled in the surface of the bearing. The bearing thus fitted runs without any other

lubrication.

# THE FOUNDRY.

### CUPOLA PRACTICE.

The following notes, with the accompanying table, are taken from an article by Simpson Bolland in American Machinist, June 30, 1892. The table shows heights, depth of bottom, quantity of fuel on bed, proportion of fuel and iron in charges, diameter of main blast-pipes, number of tuyeres. blast-pressure, sizes of blowers and power of engines, and melting capacity per hour, of cupolas from 24 inches to 84 inches in diameter.

Capacity of Cupola.—The accompanying table will be of service in determining the capacity of cupola needed for the production of a given quantity

of iron in a specified time.

First, ascertain the amount of iron which is likely to be needed at each cast, and the length of time which can be devoted profitably to its disposal; and supposing that two hours is all that can be spared for that purpose, and that ten tons is the amount which must be melted, find in the column, Melting Capacity per hour in Pounds, the nearest figure to five tons per hour, which is found to be 10,760 pounds per hour, opposite to which in the column Diameter of Cupolas, Inside Lining, will be found 48 inches; this will be the size of cupola required to furnish ten tons of molten iron in two hours.

Or suppose that the heats were likely to average 6 tons, with an occasional or suppose that the nears were likely to average o tons, which an occasional increase up to ten, then it might not be thought wise to incur the extra expense consequent on working a 48-inch cupola, in which case, by following the directions given, it will be found that a 40-inch cupola would answer the purpose for 6 tons, but would require an additional hour's time for melting

whenever the 10-ton heat came along.

The quotations in the table are not supposed to be all that can be melted in the hour by some of the very best cupolas, but are simply the amounts which a common cupola under ordinary circumstances may be expected to melt in the time specified.

Height of Cupola .- By height of cupola is meant the distance from the

base to the bottom side of the charging hole.

Depth of Bottom of Cupola.—Depth of bottom is the distance from the Sand-bed, after it has been formed at the bottom of the cupola, up to the under side of the tuyeres.

All the amounts for fuel are based upon a bottom of 10 inches deep, and any departure from this depth must be met by a corresponding change in the quantity of fuel used on the bed; more in proportion as the depth is increased, and less when it is made shallower.

increased, and less when it is made snailower.

Amount of Fuel Required on the Bed.—The column "Amount of Fuel required on Bed, in Pounds" is based on the supposition that the cupola is a small through, and that the bottom is 10 inches deep. If the bottom be more, as in those of the Colliau type, then additional fuel will be

The amounts being given in pounds, answer for both coal and coke, for, should coal be used, it would reach about 15 inches above the tuyeres; the same weight of coke would bring it up to about 22 inches above the tuyeres, which is a reliable amount to stock with.

First Charge of Iron.—The amounts given in this column of the table are

safe figures to work upon in every instance, yet it will always be in order, after proving the ability of the bed to carry the load quoted, to make a slow and gradual increase of the load until it is fully demonstrated just how much

burden the bed will carry.

Succeeding Charges of Fuel and Iron.—In the columns relating to succeed-Succeeding Charges of Fuel and Iron.—in the counting relating to the land iron, it will be seen that the highest proportions are not favored, for the simple reason that successful melting with any greater not favored, for the simple reason that successful melting with any greater not favored, for the simple reaches the rule, but, rather, the exception. Whenever we see that iron has been melted in prime condition in the proportion of 12 pounds of iron to one of fuel, we may reasonably expect that the talent, material, and cupola have all been up to the highest degree of excellence. Diameter of Main Blast-pipe.—The table gives the diameters of main

blast-pipes for all cupolas from 24 to 84 inches diameter. The sizes given opposite each cupola are of sufficient area for all lengths up to 100 feet.

Melting Ca- pacity per bour.	Pounds,	1,500	2,000	2,500	0000	4,000	4,830	5,640	6,460	7,550	8,640	9,730	10,760	083,11	12.820	19,000	14,880	016,61	10,940	10,270	21,200	22.630	24,060	26.070	27,980	29,890	31,800	33,710	35,620	87.580
H.P. of Engine to drive Stortevant Blower.	H.P.	-	-	c	٥ د	२ ०१	ಣ	တ	တ	21%	27%	27/2	86	934	£ 5	9;	16	92 9	2 6	000	63	66	Si Si	200	322	35	355	32	35	48
Sizes of Sturtevant Blower,	No.	es.	25	ତଃ ଚ	00	0 00	4	7	4	ъ.	က	20:	9	90	9	- ;	<b>!</b>	- a	0	00	00	000	000	6	6	6	6	6	6	10
H.P. of En- gine to drive RootBl'wer.	Н.Р.	%	_	7	250	4	21%	37%	4	9	200	81%	0,	22 (	2	± :	91	200	2/0	9 8	88	25	63	33	£6	90	40	45	45	47.
Revolutions per minute		550	335	210	3 6	2000	341	282	352	335	270	808	213	236	250	2	170	200	26.0	9.60	070	145	150	163	175	18.	200	140	148	160
Sizes of Root Blower re- quired.	No.	120	72		-, ,	-	. CS	જ	CS.	ಕಾ	00	ೲ	4.	4.	4.	4.	ro i	ıC r	G X	. w	240	0 90	9	9	9	9	9	ž-	2-	<b>2-</b>
Blast-press. required,	Oz.	9	9	30	- 6	- 5-	œ	œ	00	2	10	9	22	2	2	14	7	4:	= =	17	17	7	7	16	16	16	16	16	16	16
Number and Dimensions of flat Tuyeres equivalent to the 6-inch round ones.	Dimensions.	×	×	× >	< :		×	×	×	111/2" × 21/2"	×	×	×	×	× :	×	×	× :	× ;	( )	: ×	: ×	×	X	×	×	×	×	×	16" × 3½"
Num of flat to the	No.	<b>cs</b> (	25 0	30 O	> <	r 4	4	9	9	9	9	စ	90	00	00	0 0	200	00	00	0 00	000	9	9	9	2	22	22	€.	14	16
Number of Tuyeres 6 inches diam, required for eachCup'la,	No.	1.5	જ	0; c	000	0 00	2.7	īĊ.	5.	20.0	20	90		200	10.2	70.0	25.5	2 2 2	10.0	15.7	15.4	17.1	19.	19.	23.9	23.9	36.	36.	.88	31.
Diam, Main Blast - pipe when notex- ceed'g 100ft, in length,	Inches.	10	2	25	35	3 53	14	14	14	16	16	91	200	200	200	0.0	25	₹8	3 8	33	60	8	88	57	500	57	57	25	24	58
Succeeding charges of Iron,		200	858	1,206	1,004	2.340	2,718	3,096	3,474	3,852	4,230	4,608	4,986	5,804	5,74%	0,120	6,498	9,8,6	4,50	2,00	000	8,766	9.144	9.522	006.6	10,278	10,656	11,134	11,412	11,790
Succeeding charges of Fuel,	Pounds	20	8	134	010	280	305	344	386	458	470	512	554	260	688	000	22.	100	000	000	989	974	1.016	1.058	1,100	1.142	1.184	1,236	1,268	1.310
First charge of Iron,	Pounds.	900	1,170	1,440	1,1	2.250	2,520	2,790	3,060	3,330	3,600	3,870	4,140	4,410	089,	008,4	0,2,0	5,490	000,00	9000	6,520	6,840	7.110	7.880	7,650	7,920	8.190	8,460	8,730	9,000
Am't of Fuel required in bed.	Pounds.	300	000	084	000	067	840	880	1,020	1,110	1,200	1,390	3,33	1,470	096,1	000,1	1,750	1,830	0,000	00100		2.280	2.370	2.460	2,550	2,640	2.730	2.850	2,910	3,000
Depth, from sand-bed to under side of Tuyeres,	Inches,	10	10	25	07	22	10	10	10	2	10	20	2;	0,	29	0.5	0.5	29	95	2	20	10	10	10	10	10	10	10	10	10
Heightof.Cu- pola from bot'm plate to bottom of charging door.	Feet.	10	10	23	2 2	2 0	12	22	13	13	133	133	13		4.7	£1;	14	5 H	3 #	3 12	100	15	16	16	16	16	16	16	16	16
Diam, of Cu- pola inside lining,	Inches.	24	92	80 6	9 6	3 65	36	38	40	45	44	46	200	83	22	7 7	90	200	3 9	3 5	99	89	2.0	22	7.4	92	282	80	85	84

Tuyeres for Cupola.-Two columns are devoted to the number and sizes of tuyeres requisite for the successful working of each cupola; one gives the number of pipes 6 inches diameter, and the other gives the number and dimensions of rectangular tuyeres which are their equivalent in area.

From these two columns any other arrangement or disposition of tuyeres may be made, which shall answer in their totality to the areas given in the

table.

When cupolas exceed 60 inches in diameter, the increase in diameter should begin somewhere above the tuveres. This method is necessary in all common cupolas above 60 inches, because it is not possible to force the blast to the middle of the stock, effectively, at any greater diameter.

On no consideration must the tuyere area be reduced; thus, an 84-inch cupola must have tuyere area equal to 31 pipes 6 inches diameter, or 16 flat

tuyeres 16 inches by 181/2 inches.

If it is found that the given number of flat tuyeres exceed in circumference If it is found that the given number of nat tuyeres exceed in circumterence that of the diminished part of the cupola, they can be shortened, allowing the decreased length to be added to the depth, or they may be built in one only by so doing, we arrive at a modified form of the Blakeney cupola. Another important point in this connection is to arrange the tuyeres in such a manner as will concentrate the fire at the melting-point into the smallest possible compass, so that the metal in fusion will have less space

to traverse while exposed to the oxidizing influence of the blast.

To accomplish this, recourse has been had to the placing of additional rows of tuyeres in some instances—the "Stewart rapid cupola" having three rows, and the "Colliau cupola furnace" having two rows, of tuyeres.

Blast-pressure.-Experiments show that about 30,000 cubic feet of air are consumed in melting a ton of iron, which would weigh about 2400 pounds, or more than both iron and fuel. When the proper quantity of air is supplied, the combustion of the fuel is perfect, and carbonic-acid gas is the result. When the supply of air is insufficient, the combustion is imperfect, and carbonic-oxide gas is the result. The amount of heat evolved in these two cases is as 15 to 41/2 showing a loss of over two thirds of the heat by imperfect combustion.

It is not always true that we obtain the most rapid melting when we are forcing into the cupola the largest quantity of air. Some time is required to elevate the temperature of the air supplied to the point that it will enter into combustion. If more air than this is supplied, it rapidly absorbs heat, reduces the temperature, and retards combustion, and the fire in the cupola

may be extinguished with too much blast,

Slag in Cupolas.—A certain amount of slag is necessary to protect the molten iron which has fallen to the bottom from the action of the blast; if

it was not there, the iron would suffer from decarbonization.
When slag from any cause forms in too great abundance, it should be led
away by inserting a hole a little below the tuyeres, through which it will

find its way as the iron rises in the bottom.

In the event of clean iron and fuel, slag seldom forms to any appreciable extent in small heats; this renders any preparation for its withdrawal un-necessary, but when the cupola is to be taxed to its utmost capacity it is then incumbent on the melter to flux the charges all through the heat, carrying it away in the manner directed.

The best flux for this purpose is the chips from a white marble yard. About 6 pounds to the ton of iron will give good results when all is clean.

When fuel is bad, or iron is dirty, or both together, it becomes imperative

that the slag be kept running all the time.

Fuel for Cupolas.—The best fuel for melting iron is coke, because it requires less blast, makes hotter iron, and melts faster than coal. When coal must be used, care should be exercised in its selection. All anthracites which are bright, black, hard, and free from slate, will melt iron admirably. The size of the coal used affects the melting to an appreciable extent, and, for the best results, small cupolas should be charged with the size called "egg," a still larger grade for medium-sized cupolas, and what is called "lump" will answer for all large cupolas, when care is taken to pack it carefully on the charges.

Charging a Cupola.—Chas. A. Smith (Am. Mach., Feb. 12, 1891) gives the following: A 28-in. cupola should have from 300 to 400 pounds of coke on bottom bed; a 36-in. cupola, 750 to 800 pounds; a 48-in. cupola, 1500 lbs.; and a 60-in. cupola should have one ton of fuel on bottom bed. To every pound of fuel on the bed, three, and sometimes four pounds of metal can be added with safety, if the cupola has proper blast; in after-charges, to every

pound of fuel add 8 to 10 pounds of metal; any well-constructed cupola will

stand ten

F. P. Wolcott (Am. Mach., Mar. 5, 1891) gives the following as the practice of the Colwell Iron-works, Carteret, N. J.: "We melt daily from twenty to forty tons of iron, with an average of 11.2 pounds of iron to one of fuel. In 30-in, cupola seven to hine peducity is good melting, but in a cupola that harrange up 48 to 60 inches, any cupola that harrange of the cupola

Oregon.

Cupola Charges in Stove-foundries. (Iron Age, April 14, 1892.) No two cupolas are charged exactly the same. The amount of fuel on the bed or between the charges differs, while varying amounts of iron are used in the charges. Below will be found charging-lists from some of the prominent stove-foundries in the country :

A—Bed of fuel, coke  First charge of iron All other charges of iron  First and second charges of coke, each	5,000 1,000	Four next charges of coke, each	150 120 100

Thus for a melt of 18 tons there would be 5120 lbs. of coke used, giving a ratio of 7 to 1. Increase the amount of iron melted to 24 tons, and a ratio of 8 pounds of iron to 1 of coal is obtained.

B	Second and third charges of fuel	130 100
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For an 18-ton melt 5060 lbs. of coke would be necessary, giving a ratio of 7.1 lbs. of iron to 1 pound of coke.

C—Bed of fuel, coke	l other charges of iron
---------------------	-------------------------

In a melt of 18 tons 4100 lbs, of coke would be used, or a ratio of 8.5 to 1.

D-Bed of fuel, coke 1,800		lbs.
	All other charges of iron	

In a melt of 18 tons, 3900 lbs. of fuel would be used, giving a ratio of 9.4 pounds of iron to 1 of coke. Very high, indeed, for stove-plate.

Ibs.	All other charges of iron, each 2,000
	All other charges of roal, each 2,000
First charge of coal 200	The other charges or com, once

In a melt of 18 tons 4700 lbs. of coal would be used, giving a ratio of 7.7 lbs. of iron to 1 lb. of coal.

These are sufficient to demonstrate the varying practices existing among different stove-foundries. In all these places the iron was proper for stoveplate purposes, and apparently there was little or no difference in the kind

of work in the sand at the different foundries.

of work in the sain at the otherent foundres. **Results of Increased Driving.** (Eric City Iron-works, 1891.)—

May—Dec, 1890: 60-in, cupola, 100 tons clean castings a week, melting 8 tons per hour; iron per pound of fuel, 74 bls.; per cent weight of good castings to iron charged, 7534. Jan.—May, 1891: Increased rate of melting to 11½ tons per hour; iron per lb. fuel, 9½; per cent weight of good castings, 55: one week, 13½ tons per hour, 10.3 lbs. Iron per lb. fuel; per cent weight of good castings, 75: a. The increase was made by putting in an additional row of tuyeres and using stronger blast, 14 ounces. Coke was used as fuel. (W. O. Webber, Teach & M. E. vii 1045.) Trans. A. S. M. E. xii, 1045.)

# Buffalo Steel Pressure-blowers. Speeds and Capacities as applied to Cupolas.

			***									
Sq. in. Blast.	No. of Blower.	Diameter inside of Cupola, in.	Pressure in oz.	Speed—No. of Revolutions per minute.	Melting Capacity in pounds, per hour.	Cubic Feet of Air required per minute.	Horse-power re- quired.	Pressure in oz.	Speed—No. of Revolutions. per minute.	Melting Capacity in Pounds, per hour.	Cubic Feet of Air required per minute.	Horse-power required.
4	4	20	8	4793	1545	412	1.0	9	5095	1647	438	1.3
4 6 8	4 5	25	88888	3911	2321	412 619 825	1.0 1.2 2.05	9 10	4509	2600	694	1.3 2.2 3.1
8	6	30	8	3456	3093	825	2.05	10	3974	3671	926	3.1
11	7	35	8	3092	4218	1125	3.1	10	3476	4777	1274	4.25
14 18 26	8	40	8	2702	5425	1444	3.9	10 12	3034	6082	1622	5.52
18	9	45	10	2617	7818	2085	7.1	12	2916	8598	2293	9.36
26	10	55	10	2139	11295	3012		12	2353	12378	3301	12.
46	11	73	12	1639	21978	5861	23.9	14	1777	23838	6357	30.3
68	12	88	12	1639	32395	8636	35.2	14	1777	<b>3</b> 5190	9384	43.7

In the table are given two different speeds and pressures for each size of blower, and the quantity of iron that may be melted, per hour, with each. In all cases it is recommended to use the lowest pressure of blast that will do the work. Run up to the speed given for that pressure, and regulate quantity of air by the blast-gate. The tuyere area should be at least one hinth of the area of cupola in square inches, with not less than four tuyeres at equal distances around cupola, so as to equalize the blast throughout. riations in temperature affect the working of cupolas materially, hot weather requiring increase in volume of air. (For tables of the Sturtevant blower see pages 519 and 520.)

Loss in Melting Iron in Cupolas,—G. O. Vair, Am. Mach., March 5, 1891, gives a record of a 45-in. Colliau cupola as follows:

#### Ratio of fuel to iron, 1 to 7.42.

Good castings	
New scrap	3,005 **
Millings	200 "
Loss of metal	1,481 "

..... 26,000 lbs. Amount melted... Loss of metal, 5.69%. Ratio of loss, 1 to 17.55,

Use of Softeners in Foundry Practice. (W. Graham, Iron Age, June 27, 1893.)—In the foundry the problem is to have the right proportions of combined and graphitic carbon in the resulting casting; this is done by getting the proper proportion of silicon. The variations in the proportions of silicon afford a reliable and inexpensive means of producing a cast iron of any required mechanical character which is possible with the material. employed. In this way, by mixing suitable irons in the right proportions, a required grade of casting can be made more cheaply than by using irons

in which the necessary proportions are already found. If a strong machine casting were required, it would be necessary to keep the phosphorus, sulphur, and manganese within certain limits. Professor Turner found that cast iron which possessed the maximum of the desired qualities, contained, graphite, 2.59%; silicon, 1.43%; phosphorus, 0.39%; sul-

phur, 0.06%; manganese, 0.58%.

A strong casting could not be made if there was much increase in the amount of phosphorus, sulphur, or manganese. Irons of the above percentages of phosphorus, sulphur, and manganese would be most suitable for this purpose, but they could be of different grades, having different percentages of silicon, combined and graphitic carbon. Thus hard irons, mottled and white irons, and even steel scrap, all containing low percentages of silicon and high percentages of combined carbon, could be employed if an iron having a large amount of silicon were mixed with them in sufficient amount. This would bring the silicon to the proper proportion and would cause the combined carbon to be forced into the graphitic state, and the resulting

casting would be soft. High-silicon irons used in this way are called "soft-

The following are typical analyses of softeners:

		Fer	o-silicon	١.	Softene	rs, Am	Scotch Irons, No. 1.		
	Fore	ign.	American.		Well- ston.	Globe	Globe Belle- fonte.		Colt- ness.
Silicon Combined C Graphitic C Manganese Phosphorus Sulphur	1.84 0.52 3.86 0.04	9.80 0.69 1.12 1.95 0.21 0.04	0.76 0.48	10.34 0.07 1.92 0.52 0.45 Trace	6.67 2.57 0.50 Trace	5.89 0.30 2.85 1.00 1.10 0.02	3 to 6 0.25 3. 0.53 0.35 0.08	2.15 0.21 3.76 2.80 0.62 0.03	2.59 1.70 0.85 0.01

(For other analyses, see pages 371 to 373.)

Ferro-silicons contain a low percentage of total carbon and a high percentage of combined carbon. Carbon is the most important constituent of cast iron, and there should be about 3.4% total carbon present. By adding ferro-silicon which contains only 2% of carbon the amount of carbon in the

rerro-sincon winen contains only 2% of carbon the amount of carbon in the resulting mixture is lessened.

Mr. Keep found that more silicon is lost during the remelting of pig of over 10% silicon than in remelting pig iron of lower percentages of silicon. He also points out the possible disadvantage of using ferro-silicons containing as high a percentage of combined carbon as 0.70% to overcome the bad effects of combined carbon in other irons.

The Scotch irons generally contain much more phosphorus than is desired in irons to be employed in making the strongest castings. It is a mistake to mix with strong low-phosphorus irons an iron that would increase the amount of phosphorus for the sake of adding softening qualities, when softness can be produced by mixing irons of the same low phosphorus,

(For further discussion of the influence of silicon see page 365.)

Shrinkage of Castings,—The allowance necessary for shrinkage varies for different kinds of metal, and the different conditions under which they are east. For eastings where the thickness runs about one inch, cast under ordinary conditions, the following allowance can be made:

For	cast-iron, 1/8 brass, 3/16	inch	per	foot.	For	zinc,	5/16	inch	per	foot.
66	brass, 3/16	• •	-64	66	66			***	- "	**
66	steel. 1/4	"	66	66		aluminum,	3/16	"	44	66
"	steel, 14 mal. iron, 18	44	66	"	"	Britannia,	1/32	66	**	6.6

Thicker castings, under the same conditions, will shrink less, and thinner ones more, than this standard. The quality of the material and the manner

ones more, than this standard. The quanty of the material and the manner of moulding and cooling will also make a difference.

Numerous experiments by W. J. Keep (see Trans. A. S. M. E., vol. xvi.) showed that the shrinkage of cast iron of a given section decreases as the percentage of silicon increases, while for a given percentage of silicon the shrinkage decreases as the section is increased. Mr. Keep gives the following table showing the approximate relation of shrinkage to size and per-

centage of silicon:

		Sectional Area of Casting.											
Percentage of Silicon.	½″ □	1′′ 🗆	1" × 2"	2" 🏻	3′′ □	4" 🗆							
	Shrinkage in Decimals of an inch per foot of Length.												
1. 1.5 2. 2.5 3.	.183 .171 .159 .147 .135 .123	.158 .145 .133 .121 .108 .095	.146 .133 .121 .108 .095 .082	.130 .117 .104 .092 .077 .065	.113 .098 .085 .073 .059 .046	.102 .087 .074 .060 .045 .032							

Mr. Keep also gives the following "approximate key for regulating fourdry mixtures" so as to produce a shrinkage of 1/4 in. per ft. in castings of different sections:

Size of casting..... in. sq. 2.75 2.25 1.75 1.25 per cent. .165 in. per ft. Silicon required, per cent..... .135 .155 Shrinkage of a 1/2-in, test-bar. .125 .145

### Weight of Castings determined from Weight of Pattern. (Rose's Pattern-maker's Assistant,)

	Will weigh when cast in							
A Pattern weighing One Pound, made of—	Cast Iron.	Zinc.	Copper.	Yellow Brass.	Gun- metal.			
Mahogany—Nassau Honduras Spanish Pine, red white yellow	lbs. 10.7 12.9 8.5 12.5 16.7 14.1	lbs. 10.4 12.7 8.2 12.1 16.1 13.6	lbs. 12.8 15.3 10.1 14.9 19.8 16.7	lbs. 12.2 14.6 9.7 14.2 19.0 16.0	lbs. 12.5 15. 9.9 14.6 19.5 16.5			

Moulding Sand. (From a paper on "The Mechanical Treatment of Moulding Sand." by Walter Bagshaw, Proc. Inst. M. E. 1891.)—The chemical composition of sand will affect the nature of the casting, no matter what treatment it undergoes. Stated generally, good sand is composed of 94 parts silica, 5 parts alumina, and traces of magnesia and oxide of iron. Sand containing much of the metallic oxides, and especially lime, is to be avoided. Geographical position is the chief factor governing the selection of sand; and whether weak or strong, its deficiencies are made up for by the skill of the moulder. For this reason the same sand is often used for both heavy and light castings, the proportion of coal varying according to the nature of the casting. A common mixture of facing-sand consists of six parts by weight of old sand, four of new sand, and one of coal-dust. Floor-sand requires only half the above proportions of new sand and coal-dust to renew it. German founders adopt one part by measure of new sand to two of old sand; man founders adopt one part by measure or new sand to two of old sand; to which is added coal-dust in the proportion of one tenth of the bulk for large castings, and one twentieth for small castings. A few founders mix street-sweepings with the coal in order to get porosity when the metal in the mould is likely to be a long time before setting. Plumbago is effective in preventing destruction of the sand; but owing to its refractory nature, it must not be dusted on in such quantities as to close the pores and prevent free axis of the caster. Bowdows freench solls construct a very delice with free exit of the gases. Powdered French chalk, soapstone, and other substances are sometimes used for facing the mould; but next to plumbago, oak charcoal takes the best place, notwithstanding its liability to float occasionally and give a rough casting.

For the treatment of sand in the moulding-shop the most primitive method is that of hand-riddling and treading. Here the materials are roughly prois that of main-funning and creating. There are materials are roughly portioned by volume, and riddled over an iron plate in a flat heap, where the nixture is trodden into a cake by stamping with the feet; it is turned over with the shovel, and the process repeated. Tough sand can be obtained in this manner, its toughness being usually tested by squeezing a handful into a ball and then breaking it; but the process is slow and tedous. Other things being equal, the chief characteristics of a good moulding-sand are toughness and porosity, qualities that depend on the manner of mixing as

well as on uniform ramming.

Toughness of Sand.—In order to test the relative toughness, sand mixed in various ways was pressed under a uniform load into bars 1 in, sq. and about 12 in, long, and each bar was made to project further and further over the edge of a table until its end broke off by its own weight. Old sand from the shop floor had very irregular cohesion, breaking at all lengths of projections from ½ in. to 1½ in. New sand in its natural state held together until an overhang of 2½ in, was reached. A mixture of old sand, new sand, and coal-dust

Mixed under rollers..... broke at 2 in the centrifugal machine...... through a riddle....

Showing as a mean of the tests only slight differences between the last three methods, but in favor of machine-work. In many instances the frac-

three measures and in a sum and the measurements were not taken.

Dimensions of Foundry Ladles,—The following table gives the dimens one, inside the Iming, of ladles from 25 lbs. to 16 tons capacity. All the ladles are supposed to have straight sides. (Am. Mach., Aug. 4, 1892.)

Capacity.	Diam.	Depth.	Capacity.	Diam.	Depth.
16 tons	in. 54 52 49 46 43 39 34 31 27 241/2	in. 56 53 50 48 44 40 35 32 28 25 22	34 ton	in. 20 17 131/2 111/2 103/4 10 9 8 7 61/2 51/2	in. 20 17 131/2 11/2 11/2 11/2 11/2 6/2 6/2

# THE MACHINE-SHOP.

# SPEED OF CUTTING-TOOLS IN LATHES, MILLING MACHINES, ETC.

Relation of diameter of rotating tool or piece, number of revolutions, and cutting-speed: Let d = diam, of rotating piece in inches, n = No, of revs. per min.;

S =speed of circumference in feet per minute:

$$S = \frac{\pi dn}{12} = .2618 dn$$
;  $n = \frac{S}{.2618 d} = \frac{3.82S}{d}$ ;  $d = \frac{3.82S}{n}$ .

Approximate rule: No. of revs. per min. = 4 x speed in ft. per min. + diam, in inches.

Speed of Cut-for Lathes and Planers. (Prof. Coleman Sellers, Stevens' Indicator, April, 1892.)—Brass may be turned at high speed like

Bronze.—A speed of 18 feet per minute can be used with the soft alloys say 8 to 1, while for hard mixtures a slow speed is required-say 6 feet per

minute. Wrought Iron can be turned at 40 feet per minute, but planing-machines that are used for both cast and forged iron are operated at 18 feet per minute.

Machinery Steel.—Ordinary, 14 feet per minute; car-axles, etc., 9 feet per

Wheel Tires .- 6 feet per minute; the tool stands well, but many prefer

to run faster, say 8 to 10 feet, and grind the tool more frequently.

\*\*Lathes.—The speeds obtainable by means of the cone-pulley and the back gearing are in geometrical progression from the slowest to the fastest. In a well-proportioned machine the speeds hold the same relation through all the steps. Many lathes have the same speed on the slowest of the cone and

the fastest of the back-gear speeds. The Speed of Counter-shaft of the lathe is determined by an assumption of a slow speed with the back gear, say 6 feet per minute, on the largest

diameter that the lathe will swing.

Example, -A 30-inch lathe will swing 30 inches =, say, 90 inches circumfer-

EXAMPLE.—A 30-inch lathe will swing 30 inches =, say, 90 inches circumference =? 6"; the lowest triple gear should give a speed of 5 or 6 per minute. In turning or planing, if the cutting-speed exceed 30 ft. per minute, so much heat will be produced that the temper will be drawn from the tool. The speed of cutting is also governed by the thickness of the shaving, and by the hardness and tenacity of the metal which is being cut; for instance, in cutting nild steel, with a traverse of \$4 in, per revolution or stroke, and with a shaving about \$6 in. thick, the speed of cutting must be reduced to about \$ft. per minute. A good average cutting-speed for wrought or cast

iron is 20 ft per minute, whether for the lathe, planing, shaping, or slotting machine. (Proc. Inst. M. E., April, 1883, p. 248.)

### Table of Cutting-speeds.

Table of Cutting-speeds.												
				Fe	et per	minut	е.					
Diameter, inches.	5	10	15	20	25	30	35	40	45	50		
				Revol	utions	per m	inute.					
	76.4 50.9 38.2 25.5 21.5 21.5 21.5 21.5 21.5 21.5 21	152.8 101.9 76.4 61.1 50.9 34.0 34.0 30.6 27.8 21.8 21.8 117.0 15.3 13.9 9.6 6.9 6.9 6.9 4.2 4.2 4.2 4.2 4.2 4.3 4.3 4.3 4.3 4.3 4.3 4.3 4.3 4.3 4.3	20.8 19.1 16.4 14.3 12.7 11.5 10.4 9.5 8.2 7.2	305 6 203.7 152.8 122.2 101.8 87.3 76.4 67.9 61.1 55.6 50.9 43.7 38.2 34.0 30.6 27.8 21.8 21.8 21.8 21.8 21.9 21.7 11.7 11.7 9.6 8.7	382.0 254.6 191.0 152.8 1127.3 109.1 95.5 84.9 69.5 63.6 64.6 47.8 42.5 38.2 23.9 21.2 117.4 117.4 117.4 117.4 117.4 117.4	458.4 305.6 229.2 183.4 152.8 130.9 1114.6 101.8 91.7 83.3 57.3 50.9 45.8 32.7 25.5 22.9 20.8 19.1 14.3 12.7 11.5 11.	534.8 356.5 267.4 213.9 178.2 152.8 133.7 118.8 106.9 97.2 59.4 59.4 59.5 48.6 44.6 38.2 29.7 24.3 22.3 116.7 14.8 13.3	611.2 407.4 305.6 203.7 174.6 152.8 135.8 122.2 1101.8 67.3 7 67.9 9 43.7 25.6 25.6 27.8 25.5 25.5 25.5 25.5 27.8 27.8 27.8 27.8 27.8 27.8 27.8 27.8	687.6 458.3 343.8 275.0 229.1 171.9 152.8 137.5 125.0 114.5 98.2 86.0 76.4 68.8 62.5 57.3 49.1 49.1 34.4 31.2 28.6 21.5 17.1	764.0 509.3 382.0 805.6 254.6 218.3 191.0 169.7 152.8 188.9 127.2 95.5 84.9 76.4 69.5 63.7 54.6 47.8 42.5 38.1 31.8 27.3 21.8 21.8 21.8 21.8 21.8 21.8 21.8 21.8		
10 11 12 13 14 15 16 18 20 22 24 26 28 30 36 42 48 54	1.9 1.7 1.6 1.5 1.4 1.3 1.2 1.1 1.0 .9 .8 .7 .6 .5 .5 .4 .4 .4 .3	3.8 3.5 3.2 2.9 2.7 2.5 2.4 1.9 1.7 1.6 1.3 1.1 1.9 8.7 7.6	5.7 5.2 4.8 4.4 4.1 3.8 3.6 2.9 2.6 2.4 2.2 2.0 1.9 1.6 1.1	7.6 6.9 6.4 5.5 5.1 4.8 3.5 2.7 2.5 2.1 1.6 1.4	9.6 8.7 8.0 7.8 6.4 6.0 5.3 4.3 4.0 7.3 2.7 2.0 1.8 1.6	10.4 9.5 8.2 6.4 5.7 6.4 4.1 8.2 2.7 4.1	12.2 11.1 10.8 9.5 8.9 8.4 6.7 6.1 5.1 4.5 3.7 3.2 2.5	15.3 13.9 12.7 11.8 10.9 10.2 9.5 7.6 6.9 6.4 5.5 5.1 4.2 2.8 2.8	15.6 14.3 13.2 12.3 11.5 10.7 9.5 8.6 7.8 7.2 6.6 6.1	17.4 15.9 14.7 13.6 12.7 11.9 10.6 8.7 8.7 8.0 7.3 6.8 6.4 4.5 4.5 4.5		

Speed of Cutting with Turret Lathes.—Jones & Lamson Machine Co. give the following cutting-speeds for use with their flat turret lathe:

	Ft. per minute	Э.
	( Tool steel and taper on tubing	
Threading -	Machinery 15	
	Very soft steel	
	Cut which reduces the stock to 1/2 of its original diam 20	
mahinaur	Cut which reduces the stock to 34 of its original diam 25	
machinery -	Cut which reduces the stock to % of its original diam 30 to 3	35

steel Cnt which reduces the stock to 15/16 of its original diam. 40 to 45 Turning very soft machinery steel, light cut and cool work....... 50 to 60

Forms of Metal-cutting Tools,—"Hutte," the German Engineers' Pocket-book, gives the following cutting-angles for using least power.

Top Rake, Angle of Cutting-edge,

 Wrought iron
 3°
 51°

 Cast iron
 4°
 51°

 Bronze
 4°
 66°

The American Machinist comments on these figures as follows: We are not able to give the best nor even the generally used angles for tools, because these vary so much to suit different circumstances, such as degree of hardness of the metal being cut, quality of steel of which the tool made, depth of cut, kind of finish desired, etc. The angles that cut with the least expenditure of power are easily determined by a few experiments, but the best angles must be determined by good judgment, guided by experience. In nearly all cases, however, we think the best practical angles are greater than those given.

For illustrations and descriptions of various forms of cutting-tools, see articles on Lathe Tools in App. Cyc. App. Mech., vol. ii., and in Modern Mechanism.

Cold Chisels.—Angle of cutting-faces (Joshua Rose): For cast steel, about 65 degrees; for gun-metal or brass, about 50 degrees; for copper and

soft metals, about 30 to 35 degrees.

Rule for Gearing Lathes for Screw-cutting. (Garvin Machine Co.)—Read from the lathe mdex the number of threads per inch cut by equal gears, and multiply it by any number that will give for a product a gear on the index; put this gear upon the stud, then multiply the number of threads per inch to be cut by the same number, and put the resulting gear upon the screw.

EXAMPLE.—To cut 11½ threads per inch. We find on the index that 48 into 48 cuts 6 threads per inch, then  $6\times 4=24$ , gear on stud, and  $11'_2\times 4=46$ , gear on serew. Any multiplier may be used so long as the products include gears that belong with the lathe. For instance, instead of 4 as a multiplier we may use 6. Thus,  $6\times 6=36$ , gear upon stud, and  $11½\times 6=69$ , gear

upon screw.

Rules for Calculating Simple and Compound Gearing where there is no Index. (Am Mach.)-If the lathe is simplegeared, and the stud runs at the same speed as the spindle, select some gear for the sciew, and multiply its number of teeth by the number of threads per inch in the lead-screw, and divide this result by the number of threads per inch to be cut. This will give the number of teeth in the gear for the stud. If this result is a fractional number, or a number which is not among the gears on hand, then try some other gear for the screw. Or, select the gear for the stud first, then multiply its number of teeth by the number of threads per inch to be cut, and divide by the number of threads per inch on the lead-screw. This will give the number of teeth for the grar on the screw. If the lathe is compound, select at random all the driving-gears, multiply the numbers of their teeth together, and this product by the number of threads to be cut. Then select at random all the driven gears except one; multiply the numbers of their teeth together, and this product by the number of threads per inch in the lead-screw. Now divide the first result by the second, to obtain the number of teeth in the remaining driven gear. Or, select at random all the driven gears. Multiply the numbers of their teeth together, and this product by the number of threads per inch in the lead-screw. Then select at random all the driving gears except one. Multiply the numbers of their teeth together, and this result by the number of threads per inch of the screw to be cut. Divide the first result by the last, to obtain the number of teeth in the remaining driver. When the gears on the com-pounding stud are fast together, and cannot be changed, then the driven one has usually twice as many teeth as the other, or driver, in which case in the calculations consider the lead-screw to have twice as many threads per inch caucinations consider the lead-screw to have twice as many threads per inch as it actually has, and then ignore the compounding entirely. Some lathes are so constructed that the stud on which the first driver is placed revolves only half as fast as the spindle. This can be ignored in the eaclualitions by distilling the number of threads of the lead-screw. If both the last conditions are present ignore them the calculations by distilling the number of the calculations of the lead-screw is fractional one, or if the pitch of the lead-screw is fractional, or if both are fractional, then reduce the fractions to a common denominator. fractional, then reduce the fractions to a common denominator, and use the numerators of these fractions as if they equalled the pitch of the screw

to be cut, and of the lead-screw, respectively. Then use that part of the rule given above which applies to the lathe in question. For instance, suppose it is desired to cut a thread of 25/32-inch pitch, and the lead-screw has 4 It is desired to cut a thread of 25/32-inch pitch, and the leaf acserve with 8 threads per inch. Then the pitch of the lead-screw will be 4/ inch, which is equal to 8/32 inch. We now have two fraction, 25/32 and 8/32, and the two screws will be in the proportion of 25 to 8, and the gears can be figured by the above rule, assuming the number of threads to be cut to be 8 per inch, and those on the lead-screw to be 35 per inch. But this latter number may be further modified by conditions named above, such as a reduced speed of the stud, or fixed compound gears. In the instance given, if the lead-screw had been 2½ threads per inch, then its pitch being 4/10 inch, we have the fractions 4/10 and 25/32, which, reduced to a common denominator, are 64/160 and 125/160, and the gears will be the same as if the lead-screw had 125 threads per inch, and the screw to be cut 64 threads per inch.

On this subject consult also "Formulas in Gearing," published by Brown

& Sharpe Mfg. Co., and Jamieson's Applied Mechanics.

Change-gears for Screw-cutting Lathes.—There is a lack of uniformity among lathe-builders as to the change-gears provided for screw-cutting. W. R. Macdonald, in Am. Mach., April 7, 1892, proposes the follow-ing series, by which 33 whole threads (not fractional) may be cut by changes of only nine gears:

Screw.					Ep	indle.		- 1		Wh	ole '	Thre	ads.
Sc	20	30	40	50	60	70	110	120	130				
20 30	18	8	6 9	4 4/5 7 1/5	4 6	3 3/7 5 1/7	2 2/11 3 3/11	2 3	1 11/13 2 10/13	2 3	11 12	22 24	44 48
40 50	24 30	16 20	12 15	9 3/5	8 10	6 6/7 8 4/7	4 4/11 5 5/11	4 5	3 9/13 4 8/13	4 5	13 14	26 28	52 66
60 70	36 42	24 28	18 21	14 2/5 16 4/5	14	10 2/7	$\frac{6}{7} \frac{6}{7/11}$	6	5 7/13 6 6/13	6	15 16	30 33	72 78
110 120 130	66 72 78	44 48 52	33 36 39	26 2/5 28 4/5 31 1/5	22 24 26	18 6/7 20 4/7 22 3/7	13 1/11 14 2/11	11	10 2/13 11 1/18	8 9 10	18 20 21	36 39 42	

Ten gears are sufficient to cut all the usual threads, with the exception of perhaps 1116, the standard pipe-thread; in ordinary practice any fractional thread between 11 and 12 will be near enough for the customary short pipethread; if not, the addition of a single gear will give it.

In this table the pitch of the lead-screw is 12, and it may be objected to as too fine for the purpose. This may be rectified by making the real pitch 6 or any other desirable pitch, and establishing the proper ratio between the

lathe spindle and the gear-stud.

Metric Screw-threads may be cut on lathes with inch-divided lead-

ing-screws, by the use of a change-wheel with 127 teeth; for 127 millimetres equal 5 inches (168 × .03337 = 4.99993 in.).

Rule for Setting the Taper in a Lathe. (Am. Mach.)—No rule can be given which will produce exact results, owing to the fact that the centres enter the work an indefinite distance. If it were not for this circumstance in the contract of the fact that the centres enter the work an indefinite distance. If it were not for this circumstance in the contract of the contract o cumstance the following would be an exact rule, and it is an approximation as it is. To find the distance to set the centre over: Divide the difference in the diameters of the large and small end of the taper by 2, and multiply this quotient by the ratio which the total length of the shaft bears to the length of the tapered portion. Example: Suppose a shaft three feet long is to have a taper turned on the end one foot long, the large end of the taper being two

 $\frac{2-1}{2} \times \frac{3}{1} = 1\% \text{ inches.}$ inches and the small end one inch diameter.

Electric Drilling-machines—Speed of Drilling Holes in Steel Plates, (Proc. Inst. M. E., Aug. 1887, p. 329.)—In drilling holes in the shell of the S.S. "Albania," after a very small amount of practice the men working the machines drilled the X-inch holes in the shell with great rapidity, doing the work at the rate of one hole every 69 seconds, inclusive of the time occupied in altering the position of the machines by means of differential pulley-blocks, which were not conveniently arranged as slings for this purpose. Repeated trials of these drilling-machines have also shown that, when using electrical energy in both holding-on magnets and motor

el.

amounting to about ¾ H.P., they have drilled holes of 1 inch diameter through 1½ inch thickness of solid wrought iron, or through 1½ inch of mild steel in two plates of 13/16 inch each, taking exactly 1¾ minutes for each

Speed of Twist-drills. - The cutting-speeds and rates of feed recommended by the Morse Twist-drill and Machine Company are given in the following table.

Revolutions per minute for drills 1/16 in, to 2 in, diam., as usually applied:

Diameter of Drills.	Speed for Steel.	Speed for Iron.	Speed for Brass.	Diameter of Drills.	Speed for Steel.	Speed for Iron.	Speed for Brass.
inch.			-	inch.			
1/16	940	1280	1560	1 1/16	54	75	95
1/8	460	660	785	11/8	52	70	90
3/16	316	420	540	1 3/16	49	66	85
1/4	230	320	400	11/4	46	62	80
5/16	190	260	320	1 5/16	44	60	75
3/8 7/16	150	220	260	13/8	42	58	72
	130	185	230	1 7/16	40	56	69
1/2	115	160	200	11/2	39	54	66
9/16	100	140	180	1 9/16	37	51	63
5% 11/16	95	130	160	15%	36	49	60
11/16	85	115	145	1 11/16	34	47	58
3/4	75	105	130	13/4	33	45	56
13/16	70	100	120	1 13/16	32	43	54
7/8 15/16	65	90	115	17/8	31	41	52
15/16	65	85	110	1 15/16	30	40	51
1	58	80	100	2	29	39	49

To drill one inch in soft cast iron will usually require: For 1/4-in. drill, 125 revolutions; for 1/2 in. drill, 120 revolutions; for 3/4 in. drill, 100 revolutions; for 1-in. drill, 95 revolutions.

The rates of feed for twist drills are thus given by the same company: Diameter of drill..... 1/16 11/6 1/4 3/4

125 Revs. per inch depth of hole. 125 120 to 140 1 inch feed per min.

# MILLING-CUTTERS.

George Addy. (Proc. Inst. M. E., Oct. 1890, p. 537), gives the following: **Analyses of Steel.**—The following are analyses of milling-cutter blanks, made from best quality crucible cast steel and from self-hardening "Ivanhoe" steel:

	Crucible Cast Steel,	Ivanhoe Ste
	per cent.	per cent.
Carbon	1.2	1.67
Silicon	0.112	0.252
Phosphorus	0.018	0.051
Manganese	. 0.36	2.557
Sulphur	0.02	0.01
Tungsten		4.65
Iron, by difference	98.29	90.81
	100.000	100.000

The first analysis is of a cutter 14 in. diam., 1 in. wide, which gave very good service at a cutting-speed of 60 ft. per min. Large milling-cutters are sometimes built up, the cutting-edges only being of tool steel. A cutter 22 in. diam. by 51/6 in. wide has been made in this way, the teeth being clamped between two cast-iron flanges. Mr. Addy recommends for this form of tooth one with a cutting-angle of 70°, the face of the tooth being set 10° back of a radial line on the cutter, the clearance-angle being thus 10°. At the Clarence Fron. works, Leeds, the face of the tooth is set 10° back of the radial line for cutting wrought fron and 30° for steel.

Pitch of Tecth.—For obtaining a suitable pitch of teeth for milling-cutters of various diameters there exists no standard rule, the pitch being

usually decided in an arbitrary manner, according to individual taste.

For estimating the pitch of teeth in a cutter of any diameter from 4 in. to 15 in., Mr. Addy has worked out the following rule, which he has found capable of giving good results in practice:

Pitch in inches =  $\sqrt{\text{(diam. in inches} \times 8)} \times 0.0625 = .177 \sqrt{\text{diam.}}$ 

J. M. Gray gives a rule for pitch as follows: The number of teeth in a milling-cutter ought to be 100 times the pitch in inches; that is, if there were 27 teeth, the pitch ought to be 0.27 in. The rules are practically the same, for if  $d = \dim_n n = \text{No. of teeth}, p = \text{pitch}, c = \text{circumference}, c = \frac{n}{2} \frac{100n^2}{100n^2}$ 

 $pn; d = \frac{pn}{\pi} = \frac{100p^2}{\pi} = 31.83p^2; p = \sqrt{.0314d} = .177 \sqrt{d}; \text{ No. of teeth, } n, = 3.14d + p.$ 

Number of Teeth in Hills or Cutters. (Joshua Rose.)—The teeth of cutters must obviously be spaced wide enough apart to admit of the emerywheel grinding one tooth without touching the next one, and the front faces of the teeth are always made in the plane of a line radiating from the axis of the cutter. In cutters up to 3 in. in diam. It is good practice to provide 8 teeth per in. of diam., while in cutters above that diameter the spacing may be coarser, as follows:

Diameter of cutter, 6 in.; number of teeth in cutter, 40

Speed of Cuttors.—The cutting speed for milling was originally fixed very low; but experience has shown that with the improvements now in use it may with advantage be considerably increased, especially with cutters of large diameter. The following are recommended as safe speeds for cutters of 6 in. and upwards, provided there is not any great depth of material to cut away:

Should it be desired to remove any large quantity of material, the same cutting-speeds are still recommended, but with a finer feed. A simple rule for cutting-speed is: Number of revolutions per minute which the cutter spindle should make when working on cast iron = 240, divided by the diam-

eter of the cutter in inches.

Speed of Milling-cutters, (Proc. Inst. M. E., April, 1883, p. 248.)—
The cutting-speed which can be employed in milling is much greater than
that which can be used in any of the ordinary operations of turning in the
lathe, or of planing, shaping, or slotting. A milling-cutter with a plentiful
supply of oil, or soap and water, can be run at from 80 to 100 ft. per min.,
when cutting wrought iron. The same metal can only be turned in a lathe,
with a tool-holder having a good cutter, at the rate of 30 ft. per min., or at
about one third the speed of milling. A milling-cutter will cut cast steel at
the rate of 25 to 30 ft. per min.

The following extracts are taken from an article on speed and feed of milling-outters in Engly, Oct. 22, 1891; Milling-outters are successfully employed on cast iron at a speed of 250 ft, per min.; on wrought iron at from 80 ft, to 100 ft, per min. The latter materials need a copious supply of good labricant, such as oil or soapy water. These rates of sneed are not approached by other tools. The usual cutting-speeds on the latte, planing, shaping, and slotting machines rarely exceed about one third of those given above, and frequently average about a fifth, the time lost in back strokes not

being reckoned.

The feed in the direction of cutting is said by one writer to vary, in ordinary work, from 40 to 70 revs. of a 4-in. cutter per in. of feed. It must always to an extent depend on the character of the work done, but the above gives shavings of extreme thinness. For example, the circumference of a 4-in. cutter being, say, 12½ in., and having, say, 60 teeth, the advance corresponding to the passage of one cutting-tooth over the surface, in the coarser of the above-named feed-motions, is  $1/40 \times 1/60 = 1/2400$  in.; the finer feed gives an advance for each tooth of only  $1/70 \times 1/60 = 1/2400$  in. Such fine feeds as these are used only for light fluishing cuts, and the same authority recommends, also for fini-hing, a cutter about 3 in. in circumference, or nearly 3 in. in diameter, which should be run at about 60 revs, per min. to cut tough wrought steel, 120 for ordinary cast iron, about 80 for wrought

iron, and from 140 to 160 for the various qualtities of gun-metal and brass. With cutters smaller or larger the rates of revolution are increased or diminished to accord with the following table, which gives these rates of cutting-speeds and shows the lineal speed of the cutting-edge:

Steel, Wrought Iron. Cast Iron, Gun-metal. Brass. Feet per minute...

These speeds are intended for very light finishing cuts, and they must be reduced to about one half for heavy cutting.

The following results have been found to be the highest that could be attained in ordinary workshop routine, having due consideration to economy and the time taken to change and grind the cutters when they become dull; Wrought iron—36 ft. to 40 ft. per min.; depth of cut, i. in.; feed, § in. per min. Tough gun-metal—80 ft. per min.; depth of cut, ½ in.; feed, ¾ in. per min. Tough gun-metal—80 ft. per min.; depth of cut, ½ in.; feed, ¾ in. per min. Cast-iron gear-wheels—26½ ft. per min.; depth of cut, ½ in.; feed, ¾ in.; f and the time taken to change and grind the cutters when they become dull:

way, the object being to ascertain definitely the relative amount of work done by a high speed and a light feed, as compared with a low speed and a heavy cut. The machine was used single-geared and double-geared, and in

both cases the width of cut was 101/2 in.

both cases the width of cut was 10½ in.

Single-gear, 42 ft. per min., 5/16 in. depth of cut; feed, 1.3 in. per min. = 4.16 cu. in. per min. Double-gear, 19 ft. per min.; 3½ in. depth of cut; feed, ½ in. per min. = 2.40 cu. in. per min.

Extreme Results with Milling-machines. — Horace L. Arnold (Am. Mach., Dec. 28, 1893) gives the following results in flat-surface milling, obtained in a Pratt & Whitney milling-machine: The mills for the flat cut were 5" diam., 12 teeth, 40 to 50 revs. and 4½" feed per min. One single cut was run over this piece at a feed of 9" per min., but the mills showed plainly at the end that this rate was greater than they could endure. At 50 revs. for these mills the figures are as follows, with 4½" feed: Surface speed, 6 ft., nearly; feed per tooth, 0.00812"; cuts per inch, 133. And with 9" feed per min.: Surface speed, 64 ft. per min.; feed per tooth, 0.015"; cuts per inch, 66%.

per inch, 66%.

At a feed of 47%" per min, the mills stood up well in this job of cast-iron surfacing, while with a 9" feed they required grinding after surfacing one piece; in other words, it did not damage the mill-teet to do this job with 13% cuts per in, of surface finished, but they would not endure 60% cuts per inch. In this cast-iron milling the surface speed of the mills does not seem to be the factor of mill destruction: it is the increase of feed per tooth that prohibits increased production of finished surface. This is precisely the reverse of the action of single-pointed lathe and planer tools in general: with such tools there is a surface-speed limit which cannot be economically exceeded for dry cuts, and so long as this surface-speed limit is not reached, the cut per tooth or feed can be made anything up to the limit of the driving power of the lathe or planer, or to the safe strain on the work itself,

which can in many cases be easily broken by a loo great feed.

In wrought metal extreme figures were obtained in one experiment made in cutting keyways 5/10" wide by ½" deep in a bank of 8 shafts 1½" diam, at once, on a Pratt & Whitney No. 3 column milling-machine. The 8 mills were successfully operated with 45 ft. surface speed and 19½ in. per min. feed; the cutters were 5" diam., with 28 teeth, giving the following figures, in steel: Surface speed, 45 ft. per min.; feed per tooth. 0.02024"; cuts per inch, 50, nearly. Fed with the revolution of mill. Flooded with oil, that is, a large stream of oil running constantly over each mill. Face of tooth radial. The resulting keyway was described as having a heavy wave or cutter-mark in the bottom, and it was said to have shown no signs of being heavy work on the cutters or on the machine. As a result of the experiment it was decided for economical steady work to run at 17 revs., with a feed of 4" per min., flooded cut, work fed with mill revolution, giving the following figures: Surface speed, 22½ ft. per min.; feed per tooth, 0.004"; cuts per inch, 119,

An experiment in milling a wrought-iron connecting-rod of a locomotive An experiment in milling a wrought-iron connecting-rod of a locomotive on a Pratt & Whitney double head milling-machine is described in the Iron Age, Ang. 27, 1891. The amount of metal removed at one cut measured 314 in, wide by 1 3/16 in, deep in the groove, and across the top ½ in, deep by 432 in, wide. This represented a section of nearly 4½ sq. in. This was done at the rate of 13½ in, per min. Nearly 8 cu, in, of metal were cut up into chips every minute. The surface left by the cutter was very perfect. The cutter moved in a direction contrary to that of ordinary practice; that is, it cut down from the upper surface instead of up from the bottom.

Milling "with" or "against" the Feed.—Tests made with the Brown & Sharpe No. 5 milling-machine (described by H. L. Arnold, in Am. Mach., Oct. 18, 1894) to determine the relative advantage of running the milling-cutter with or against the feed—"with the feed" meaning that the milling-cutter with or against the feed—"with the feed "meaning that the teeth of the cutter strike on the top surface or "scale" of cast-iron work in process of being milled, and "against the feed" meaning that the teeth begin to cut in the clean, newly cut surface of the work and cut upwards toward the scale—showed a decided advantage in favor of running the cutter against the feed. The result is directly opposite to that obtained in tests of a Pratt & Whitney machine, by experts of the P. & W. Co!

In the tests with the Brown & Sharpe machine the cutters used were 6 inches face by 4½ and 3 inches diameter respectively, 15 teeth in each mill, 42 revolutions per minute in each case, or nearly 50 feet near minute.

42 revolutions per minute in each case, or nearly 50 feet per minute surface speed for the 41/4-inch and 33 feet per minute for the 3-inch mill. The revospeed for the 432-inch and 35 feet per limitee for the 3-lien limit. The revo-lution marks were 6 to the inch, giving a feed of 7 inches per minute, and a cut per tooth of .011". When the machine was forced to the limit of its driving the depth of cut was 11/32 inch when the cutter ran in the "old" way, or against the feed, and only 4 inch when it ran in the "new" way, or with the feed. The endurance of the milling-cutters was much greater when they were run in the "old" way.

Spiral Milling-cutters.—There is no rule for finding the angle of the spiral; from 10° to 15° is usually considered sufficient; if much greater

the end thrust on the spindle will be increased to an extent not desirable for some machines.

Milling-cutters with Inserted Teeth.-When it is required to use milling cutters of a greater diameter than about 8 in., it is preferable to insert the teeth in a disk or head, so as to avoid the expense of making solid cutters and the difficulty of hardening them, not merely because of the risk of breakage in hardening them, but also on account of the difficulty

in obtaining a uniform degree of hardness or temper.

Milling - machine versus Planer. - For comparative data of work done by each see paper by J. Grant, Trans. A. S. M. E., ix. 259. He says: The advantages of the milling machine over the planer are many, among which are the following: Exact duplication of work; rapidity of production — the cutting being continuous; cost of production, as several machines can be operated by one workman, and he not a skilled mechanic; and cost of tools for producing a given amount of work.

#### POWER REQUIRED FOR MACHINE TOOLS.

Resistance Overcome in Cutting Metal, (Trans. A. S. M. E., viii, 308.)—Some experiments made at the works of William Sellers & Co. viii. 305.)—Some experiments made at the works of white selects a showed that the resistance in cutting steel in a lathe would vary from 180,000 to 700,000 pounds per square inch of section removed, while for cast iron the resistance is about one third as much. The power required to remove a given amount of metal depends on the shape of the cut and on remove a given amount of mean depends on the shape of the cut and on the shape and the sharpness of the tool used. If the cut is nearly square in section, the power required is a minimum; if wide and thin, a maximum. The dulness of a tool affects but little the power required for a heavy cut. Heavy Work on a Planer.—Wm. Sellers & Co, write as follows to the American Machinist: The 120° planer table is geared to run 18 ft, per

minute under cut, and 72 feet per minute on the return, which is equivalent, without allowance for time lost in reversing, to continuous cut of 14.4 feet per minute. Assuming the work to be 28 feet long, we may take 14 feet as the continuous cutting speed per minute, the .8 of a foot being much more than sufficient to cover time loss in reversing and feeding. The machine carries four tools. At  $\frac{1}{2}$  feed per tool, the surface planed per hour would be 35 square feet. The section of metal cut at  $\frac{3}{4}$  depth would be .75"  $\times$  $125'' \times 4 = .375$  square inch, which would require approximately 30,000 lbs.

pressure to remove it. The weight of metal removed per hour would be  $14 \times 12 \times 375 \times 26 \times 60 = 1082.8$  lbs. Our earlier form of 36'' planer has removed with one tool on 34'' cut on work 200 lbs. of metal per hour, and the 120'' machine has more than five times its capacity. The total pulling power of the planer is 45,000 lbs.

Horse-power Required to Run Lathes. (J. J. Flather, Am. Mach., April 23, 1891.)—The power required to do useful work varies with the depth and breadth of chip, with the shape of tool, and with the nature and density of metal operated upon; and the power required to run a machine amprix is often a variable quantity.

chine empty is often a variable quantity.

For instance, when the machine is new, and the working parts have not become worn or fitted to each other as they will be after running a few months, the power required will be greater than will be the case after the

months, the power required will be greater than will be the case after the running parts have become better fitted.

Another cause of variation of the power absorbed is the driving-belt; a tight belt will increase the friction, hence to obtain the greatest efficiency of a machine we should use wide belts, and run them just tight enough to prevent slip. The belts should also be soft and pliable, otherwise power is consumed in bending them to the curvature of the pulleys.

A third cause is the variation of journal-friction, due to slacking up or tightening the cap-screws, and also the end-thrust bearing screw.

Hartig's investigations show that it requires less total power to turn off a viven weight of metal in a given time than it does to plane off the same

given weight of metal in a given time than it does to plane off the same amount; and also that the power is less for large than for small diameters. The following table gives the actual horse-power required to drive a lathe empty at varying numbers of revolutions of main spindle.

#### HORSE-POWER FOR SMALL LATHES.

Without E	ack Gears.	With Ba	ck Gears.	
Revs. of Spindle per min.	H.P. required to drive empty.	Revs. of Spindle per min.	H.P. required to drive empty.	Remarks.
132.72	.145	14.6	.126	20" Fitchburg lathe.
219.08	.197	24.33	.141	
365.00	.310	38.42	.274	
47.4	.159	4.84	.132	Smallla the (13½"), Chemnitz. Germany. New machine.
125.0	.259	12.8	.187	
188	.339	19.2	.230	
54.6	.206	6.61	.157	17½" lathe do. New machine.
122	.339	14.8	.206	
183	.455	22.1	.249	
18.8	.086	2.31	.035	26" lathe do.
54.6	.210	6.72	.063	
82.2	.326	10.8	.087	

If H.P.<sub>0</sub> = horse-power necessary to drive lathe empty, and N = number of revolutions per minute, then the equation for average small lathes is  $H.P._0 = 0.095 + 0.0012N$ 

For the power necessary to drive the lathes empty when the back gears are in, an average equation for lathes under 20" swing is

$$H.P._0 = 0.10 + 0.006N.$$

The larger lathes vary so much in construction and detail that no general rule can be obtained which will give, even approximately, the power required to run them, and although the average formula shows that at least 0.095 horse-power is needed to start the small lathes, there are many American lathes under 20" swing working on a consumption of less than ,05 horse-power,

The amount of power required to remove metal in a machine is determinable within more accurate limits.

Referring to Dr. Hartig's researches, H.P., = CW, where C is a constant, and W the weight of chips removed per hour.

Average values of C are .030 for cast-iron, .032 for wrought-iron, .047 for steel.

The size of lathe, and, therefore, the diameter of work, has no apparent effect on the cutting power. If the lathe be heavy, the cut can be increased, and consequently the weight of chips increased, but the value of C appears to be about the same for a given metal through several varying sizes of lathes.

Horse-power required to remove Cast Iron in a 20-inch Lathe.
(J. J. Hobart.)

Descriptive No.	Number of Trials.	Tool used.	Average Cutting- speed in feet per minute.	Depth of Cut in inches.	Average Breadth of Cut in inches.	Average H.P. required to remove Metal.	Average pounds Metal turned off per hour.	Value of Constant C.
1	22	Side tool	37.90	.125	.015	.342 .218	13.30	.025
2	15	Diamond	30.50	.125	.015	218	10.70	.020
1 2 3 4	17	Round nose	42.61	.125	.015	.352	14.95	.023
4	2	Left - hand round	14.01	. 1.00	1 .010	.00.	14.00	.020
*	1 ~		26.29	. 125	.015	.237	9.22	000
5		nose Square-faced tool	20.29	. 120	.015	.281	9.22	.026
Э	4	Square-raced tool	02 00	045	405	000		000
		1/2" broad	25.82	.015	.125	. 255	9.06	.028
6	1		25.27	.048	.048	.200	10.89	.018
7	1	"	25.64	.125	.015	.246	8.99	.027

The above table shows that an average of .26 horse-power is required to turn off 10 pounds of cast-iron per hour, from which we obtain the average value of the constant C=.034.

Most of the cuts were taken so that the metal would be reduced ¼" in mathetr; with a broad surface cut and a coarse feed, as in No. 5, the power required per pound of chips removed in a given time was a maximum; the least power per unit of weight removed being required when the chip was square, as in No. 6.

# Horse-power required to remove Metal in a 29-inch Lathe. (R. H. Smith.)

Number of Experiments.	Metal.	Cutting-speed. ft, per min.	Depth of Cut, in.	Average Breadth of Cut, in.	Avereage H.P. required to re- move Metal.	Average pounds Metal removed per hour.	Value of C.
4 4 4 4 4 4 4 4	Cast iron	12.7	.05	.046	.105	5.49	.019
4	Cast iron	11.1	.135	.046	.217	12.96	.017
2	Cast iron	12.85	.04	.038	.098	3.66	.027
4	Wrought iron	9.6	.03	.046	.059	2.49	.023
4	Wrought iron	9.1	.06	.046	.138	4.72	.029
4	Wrought iron	7.9	.14	.046	.186	9.56	.019
2	Wrought iron	9.35	.045	.038	.092	2.99	.031
4	Steel	6.00	.02	.046	.043	1.03	.042
4	Steel	5.8	.04	.046	.085	2.00	.042
4	Steel	5.1	.06	.046	.108	2.64	.040

1.32 H.P.

The small values of C, .017 and .019, obtained for cast iron are probably due to two reasons: the iron was soft and of fine quality, known as pulley metal, requiring less power to cut; and, as Prof. Smith remarks, a lower

cutting-speed also takes less horse-power.

Hardness of metals and forms of tools vary, otherwise the amount of chips turned out per house per because would be practically constant, the

higher cutting speeds decreasing but slightly the visible work done.

Taking into account these variations, the weight of metal removed per hour, multiplied by a certain constant, is equal to the power necessary to do the work.

This constant, according to the above tests, is as follows:

	Cast Iron.	Wrought Iron.	Steel.
Hartig	030	.032	.047
Smith	023	.028	.042
Hobart	024		
Average	026	.030	.044

The power necessary to run the lathe empty will vary from about .05 to .3 H.P., which should be ascertained and added to the useful horse-power, to obtain the total power expended.

Power used by Machine-tools. (R. E. Dinsmore, from the Electrical World.)

 Shop shafting 2 3/16" × 180 ft. at 160 revs., carrying 26 pulleys from 6" diam. to 36", and running 20 idle machine belts.

2. Lodge-Davis upright back-geared drill-press with table, 28"

0.78 H.P.
0.29 H.P.
1.06 H.P.
0.37 H.P.
0.43 H.P.
0.23 H.P.
0.8 H.P.
3.2 H.P.

The table on the next page compiled from various sources, principally from Hartig's researches, by Prof. J. J. Flather (Am. Mach., April 12, 1894), may be used as a guide in estimating the power required to run a given machine; but it must be understood that these values, although determined by dynamometric measurements for the individual machines designated, are not necessarily representative, as the power required to drive a machine are not necessarily representative, as the power required to drive a machine itself is dependent on the construction. The character of the work to be done may also affect the power required to operate; thus a machine to be used exclusively for brass work may be speeded from 10% to 15% higher than fit twere to be used for iron work of speeding from 10% to 15% higher than fit twere to be used for iron work of the power required will be proportionately greater. Where power is to be transmitted to the machines by means of shafting and countershafts, an additional amount, varying from 30% to 50% of the total

power absorbed by the machines, will be necessary to overcome the friction

of the shafting.

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> Horse-power required to drive Shafting, -Samuel Webber, Horse-power required to drive snatting,—samuel webber, in his "Manual of Power" gives among numerous tables of power required to drive textile machinery, a table of results of tests of shafting. A line of \$2\%'' shafting, \$42 ft. long, weighing 3098 lbs, with pulleys weighing 5331 lbs., or a total of 9429 lbs., supported on 47 bearings, 216 revolutions per minute, required 1.858 H.P. to drive it. This gives a coefficient of friction of 5.52%. In seventeen tests the coefficient ranged from 3.34% to 11.4%, averaging 5.73%.

# Horse-power Required to Drive Machinery.

	Observe	ed Horse-power.
Name of Machine.	Total Work.	Running Light.
Small screw-cutting lathe 131/6" swing, B. G	0.41	0.18; 0.15*-0.34†
Sman screw-cutting lattle 15-25' Swing, B. G. Screw-cutting lattle 120' (Fitchburg), B. G. Screw-cutting lattle 20' (B. G. Lattle, 80' face plate, will swing 108', T. G. Large facing blue, will swing 69', T. G.	0.867	0.207; 0.16-0.466
Screw-cutting lathe 20" (Fitchburg), B. G	0.47	0.12; 0.12 to 0.31
Lathe 80" face plate will swing 108" T G	0.462 0.53	0.05; 0.05 to 0.55
Large facing lathe, will swing 68", T. G	0.91	0.05; 0.03 to 0.33 0.187; 0.12to 0.66 0.37; 0.39 to 0.81
Wheel lathe 60" swing. Small shaper (stroke 4", traverse 11"). Small shaper, Richards (9½" × 22").		0.23 to 3.40
Small shaper (stroke 4", traverse 11")	0.16 0.24	0.086 to 0.26 0.07; 0.07 to 0.12
Shaper (15" stroke Gould & Eberhardt).	0.63	0.21; 0.01 to 0.47
Shaper (15" stroke Gould & Eberhardt).  Large shaper, Richards (29" × 91").  Crank planer (capacity 23" × 27" × 28½" stroke).  Planer (capacity 36" × 36" × 11 feet)	1.14	0.26; 0.15 to 0.73
Crank planer (capacity 23" × 27" × 281/2" stroke).	0.24	0.12; 0.12 to 0.40
Planer (capacity 36" × 36" × 11 feet)	0 84	0.27 0.60
Small drill press	1.47	0.39
Small drill press	0.41	0.15; 0.15 to 0.43
Medium drill press	1.33	0.62
Large drill press	1.24	0.62
Radial drill 816 feet swing	0.67	0.30; 0.12*-0.80+
Radial drill 8¼ feet swing Radial drill press Slotter (8" stroke)	1.08	0.46
Slotter (8" stroke)	0.28	0.09; 0.05 to 0.25
Slotter (9½" stroke)	0.44	0.22; 0.15 to 0.65 0.57; 0.43 to 0.94
Universal milling mach (Brown & Sharpe No. 1)	0.28	0.01; 0.003-0.13
Slotter (9\frac{1}{2}'' stroke). Slotter (15'' stroke). Universal milling mach (Brown & Sharpe No. 1) Milling machine (13'' cutter-head, 12 cutters).	0.66	0.26; 0.26 to 0.55
Sman nead traversing mining machine (cutter-nead		0.10
11" diameter, 16 cutters)	0.18	0.10 0.11
Horizontal boring machine for iron, 2216" swing	1 .	0.12; 0.10-0.12*;
		0.10 to 0.25† 0 37
Hydraulic shearing machine	7.12	0.67
Large punch press, over-reach 28", 3" stroke, 11/2"		
stock can be punched. Small punch and shear comb'd, 7½" knives, 1½" str.	4.41 0.79	1.00
Circular saw for hot iron (3014" diameter of saw)	4.12	0.61
Plate-bending rolls, diam. of rolls 13", length 91/6 ft.	2.70	.54
Wood planer 131/2" (rotary knives, 2 hor'l 2 vert	4.24	3.35
Wood planer 1714" (rotary knives)	3.03 4.63	1 42 1.25
Wood planer 28" (rotary knives)	5.00	0.74‡-0.17§
Small punch and shear comb'd, 74%" knives, 13%" str. Circular saw for hot iron (304%" diameter of saw). Plate-bending rolls, diam, of rolls 13", length 9½ ft. Wood planer 134" (rotary knives, 2 hor 12 vert Wood planer 24" (rotary knives) Wood planer 13" (rotary knives) Wood planer 28" (rotary knives) Wood planer 28" (Daniel's pattern). Wood planer 28" (Daniel's pattern).	3.20	1.45
Wood planer and matcher (capacity 141/2 × 43/4"). Circular saw for wood (23" diameter of saw)	6.91	4.18
Circular saw for wood (35" diameter of saw)	3.23 5.64	0.70
Circular saw for wood (35" diameter of saw) Band saw for wood (34" band wheel)	0.96	0.19
Wood-mortising and boring machine	0.49	0.34
Hor'l wood-boring and mortising machine, drill 4"	3,68	1 67: 0 65 to 2 0
Tenon and mortising machine	2.11	1.67; 0.65 to 2.0 1.42
diam, mortise 8½ deep × 11½" long Tenon and mortising machine. Tenon and mortising machine. Tenon and mortising machine.	2.73.	0.61
Tenon and mortising machine	2.25	2.17
Edge-molder and shaper. (Vertical spindle)	2.00 2.45	1.30
Grindstone for tools, 31" diam., 6" face. Velocity	~.40	~.00
		0.32
Grindstone for stock, 42"×12". Vel. 1680 ft. per min. Emery wheel 11½" diameter × ¼". Saw grinder.	3.11 0.56	0.24
Elliery wheel 1132 drameter x 34 . Saw grinder	1 0.00	0.40

<sup>\*</sup> With back gears. † Without back gears. ‡ For surface cutters. § With side cutters. B. G., back-geared. T. G., triple-geared.

Horse-power consumed in Machine-shops.—How much power is required to drive ordinary machine-tools? and flow many men can be employed per horse-power? are questions which it is impossible to answer by any fixed rule. The power varies greatly according to the conditions in each shop. The following table given by J. J. Flather in his work on Dynamometers gives an idea of the variation in several large works. The percentage of the total power required to drive the shafting varies from 15 to 80, and the number of men employed per total H.P. varies from 0.62 to 6.04.

# Horse-power; Friction; Men Employed.

Horse-power, Friction, men Employed.										
Name of Firm.	Kind of Work.	Total.	Required to drive	Required to drive of Machinery.	Per cent to drive	len.	No. of Men per Total H.P.	No. of Men per Effec- tive H.P.		
Lane & Bodley.  J. A. Fay & Co Union Iron Works. Frontier Iron & Brass W'ks Frontier Iron & Brass W'ks Taylor Mig. Co. Baldwin Loco, Works. W. Sellers & Co. (one department). Pond Machine Tool Co Pratt & Whitney Co. Brown & Sharpe Co. Yale & Towne Co. T. B. Wood's Sons. Bridgeport Forge Co. Singer Mfg. Co. Howe Mig. Co. Worcester Mach. Screw Co Hartford " " Nicholson File Co.	E. & W. W. W. W. W. W. W. E., M. M. M. E., etc. L. H. M. T. "C. & L. P. & D. P. & S. H. F. S. M. M. S. F.	58 100 400 25 95 2500 102 180 120 230 135 15 15 130 40 400 850	75 67 11 75	85 305 17 500 61 105 68 24 75	15 28 32 80 40 41 49 31 50	300 1600 150 230 4100 300 432 725 900 700 90 30 130 8500 80 250	6.00 2.42 1.64 2.93 2.40 6.04 8.91 5.11 2.57 2.50	4.11 - 10.25 3.75 1.73		
Averages		346.4			38.6%	818.3	2.96	5.13		

Abbreviations; E., engine; W.W., wood-working machinery; M. M., mining machinery; M. E., marine engines; L., locomotives; H. M., heavy machinery; M. T., machine tools; C. & L., cranes and locks; P. & D., presses and dies; P. & S., pulleys and shafting; H. F., heavy forgings; S. M., sewingmachines; M. S., machine-screws; F., files.

J.T. Henthorn states (Trans. A. S. M. E., vi. 462) that in print-mills which examined the friction of the shafting and engine was in 7 cases below

he examined the friction of the shafting and engine was in 7 cases below 20% and in 35 cases between 20% and 30%, in 11 cases from 30% to 35% and in 2 cases above 35%, the average being 25.9%. Mr. Barrus in eight cotton-mills found the range to be between 15% and 25.7%, the average being 22%, Mr. Flather believes that for shops using heavy machinery the percentage of power required to drive the shafting will average from 40% to 50% of the total power expended. This presupposes that under the head of shafting are

# included elevators, fans, and blowers.

#### ABRASIVE PROCESSES.

Abrasive cutting is performed by means of stones, sand, emery, glass, corundum, carborundum, crocus, rouge, chilled globules of iron, and in some cases by soft, friable iron alone. (See paper by John Richards, read before the Technical Society of the Pacific Coast, Am. Mach., Aug. 20, 1891, and Eng. & M. Jour., July 25 and Aug. 15, 1891.)

The "Cold Saw."-For sawing any section of iron while cold the cold saw is sometimes used. This consists simply of a plain soft steel or iron disk without teeth, about 42 inches diameter and 3/16 inch thick. The velocity of the circumference is about 15,000 feet per minute. One of these saws will saw through an ordinary steel rail cold in about one minute. In this saw the steel or iron is ground off by the friction of the disk, and is not cut as with the teeth of an ordinary saw. It has generally been found more profitable, however, to saw iron with disks or band-saws fitted with cuttingteeth, which run at moderate speeds, and cut the metal as do the teeth of a milling-cutter

Reese's Fusing-disk.—Reese's fusing-disk is an application of the cold saw to cutting iron or steel in the form of bars, tubes, cylinders, etc., in which the piece to be cut is made to revolve at a slower rate of speed than the saw. By this means only a small surface of the bart to be cut is presented at a time to the circumference of the saw. The saw is about the same size as the cold saw above described, and is rotated at a velocity of about 25,000 feet per minute. The heat generated by the friction of this saw against the small surface of the bar rotated against it is so great that the against the sman surface of the oar rotated against it is so great that the particles of iron or steel in the bar are actually fused, and the "sawdust" welds as it falls into a solid mass. This disk will cut either cast iron, wrought iron, or steel. It will cut a bar of steel 136 inch diameter in one minute, including the time of setting it in the machine, the bar being rotated about 200 turns per minute.

Cutting Stone with Wire.—A plan of cutting stone by means of a wire cord has been tried in Europe. While retaining sand as the cutting where cord has been tried in Europe. While retaining sand as the cutting agent, M. Paulin Gay, of Marseilles, has succeeded in applying it by mechanical means, and as continuously as formerly the sand-blast and band-saw, with both of which appliances his system—that of the "helicoldal wire cord"—has considerable analogy. An engine puts in motion a continuous wire cord (varying from five to seven thirty-seconds of a inch in diameter, according to the work, composed of three mild-steel wires twisted at a certification but is found to give the host wealth in processing the control of the tain pitch, that is found to give the best results in practice, at a speed of

The Sand-blast.—In the sand-blast, invented by B. F. Tilghman, of Philadelphia, and first exhibited at the American Institute Fair, New York. in 1871, common sand, powdered quartz, emery, or any sharp cutting material is blown by a jet of air or steam on glass, metal, or other comparatively brittle substance, by which means the latter is cut, drilled, or engraved. To protect those portions of the surface which it is desired shall not be abraded it is only necessary to cover them with a soft or tough material, such as lead, rubber, leather, paper, wax, or rubber-paint. (See description in App. Cyc. Mech.; also U.S. report of Vienna Exhibition, 1873, vol. iii. 216.) A "jet of sand" impelled by steam of moderate pressure, or even by the

blast of an ordinary fan, depolishes glass in a few seconds; wood is cut quite rapidly; and metals are given the so-called "frosted" surface with great rapidity. With a jet issuing from under 300 pounds pressure, a hole was cut through a piece of corundrum 1½ inches thick in 25 minutes. The sand-blast has been applied to the cheaning of metal castings and

The sand-blast has been applied to the cleaning of metal castings and sheet metal, the graining of zinc plates for lithingraphic purposes, the frosting of silverware, the cutting of figures on stone and glass, and the cutting of devices on monuments or tombstones, the recutting of files, etc. The time required to sharpen a worn-out 14-inch bastard file is about four minutes. About one pint of sand, passed through a No. 120 sieve, and four horse-power of 60-lb, steam are required for the operation. For cleaning castings compressed air at from 8 to 10 pounds pressure per square inch is employed. Chilled-iron globules instead of quartz or flint-sand are used with word expulse both as to smooth of wording and cost of material, when with good results, both as to speed of working and cost of material, when the operation can be carried on under proper conditions. With the expenditure of 2 horse-power in compressing air, 2 square feet of ordinary scale on the surface of steel and iron plates can be removed per minute. The surface thus prepared is ready for tinning, galvanizing, plating, bronzing, painting, etc. By continuing the operation the hard skin on the surface of castings, which is so destructive to the cutting edges of milling and other tools, can be removed. Small castings are placed in a sort of slowly rotating barrel, open at one or both ends, through which the blast is directed downward against them as they tumble over and over. No portion of the surface escapes the action of the sand. Plain cored work, such as valve-bodies, can be cleaned perfectly both inside and out. 100 lbs. of castings can be cleaned in from 10 to 15 minutes with a blast created by 2 horsepower. The same weight of small forgings and stampings can be scaled in from 20 to 30 minutes. - Iron Age, March 8, 1894.

### EMERY-WHEELS AND GRINDSTONES.

The Selection of Emery-wheels,—A pamphlet entitled "Emery-wheels, their Selection and Use," published by the Brown & Sharpe Mfg. Co., after calling attention to the fact that too much should not be expected. of one wheel, and commenting upon the importance of selecting the proper

wheel for the work to be done, says :

Wheels are numbered from coarse to fine; that is, a wheel made of No. Wheels are numbered from coarse to fine; that is, a wheel made of No. 100. Within certain limits, and other things being equal, a coarse wheel is less liable to change the temperature of the work and less liable to glaze than a fine wheel. As a rule, the harder the stock the coarser the wheel required to produce a given finish. For example, coarser wheels are required to produce a given surface upon hardened steel than upon soft steel, while finer wheels are required to produce this surface upon brass or copper than upon either hardened or soft steel.

nardened or soit sides.

Wheels are graded from soft to hard, and the grade is denoted by the letters of the alphabet, A denoting the softest grade. A wheel is soft on hard chiefly on account of the amount and character of the material combined in its manufacture with emery or corundum. But other characteristics being equal, a wheel that is composed of fine emery is more compact and harder than one made of coarser emery. For instance, a wheel of No. 100 emery, grade B, will be harder than one of No. 60 emery, same grade.

The softness of a wheel is generally its most important characteristic. soft wheel is less apt to cause a change of temperature in the work, or to become glazed, than a harder one. It is best for grinding hardened steel, cast-iron, brass, copper, and rubber, while a harder or more compact wheel is better for grinding soft steel and wrought iron. As a rule, other things being equal, the harder the stock the softer the wheel required to produce

a given finish.

Generally speaking, a wheel should be softer as the surface in contact with the work is increased. For example, a wheel 1/16-inch face should be harder than one ½-inch face. If a wheel is hard and heats or chatters, it can often be made somewhat more effective by turning off a part of its entting surface; but it should be clearly understood that while this will cutting surface; but it should be clearly understood that while this will sometimes prevent a hard wheel from heating or chattering the work, such a wheel will not prove as economical as one of the full width and proper grade, for it should be borne in mind that the grade should always bear the proper relation to the width. (See the pamphlet referred to for other information. See also lecture by T. Dunkin Paret, Prest of The Tanite Co., on Emery-wheels, Jour. Frank. Inst., March, 1890.)

Speed of Emery-wheels,—The following) speeds are recommended

by different makers:

of	Rev	olutions	per min	ute.	of nes.	Revolutions per minute.			
Diameter of Wheel, incl	Waltham E. W. Co.	Tanite Co.	Grant Corundum Wheel Co.	Norton E. W. Co	Diameter o Wheel, inch	Waltham E. W. Co.	Tanite Co.	Grant Corundum Wheel Co.	Norton E. W. Co.
1 11/2 2 21/2 3 4 5 6 7 8	19,000 12,500 9,500 7,600 6,400 4,800 3,800 3,200 2,700 2,400 2,150	14,400 10,800 8,640 7,200 5,400 4,320 3,600 3,080 2,700 2,400	7,400 5,400 4,400 3,600 3,200 2,700 2,400	12,000 10,000 8,500 7,400 5,450 4,400 3,150 2,750 2,450	10 12 14 16 18 20 22 24 26 30	1,950 1,600 1,400 1,200 1,050 950 875 800 750 675	2,160 1,800 1,570 1,350 1,222 1,080 1,000 917	2,200 1,800 1,600 1,400 1,250 1,100 1,000 925 600 500 400	2,200 1,850 1,600 1,400 1,250 1,100 1,000 925 825 735 550

<sup>&</sup>quot;We advise the regular speed of 5500 feet per minute." (Detroit Emerywheel Co.)

"Experience has demonstrated that there is no advantage in running

solid emery-wheels at a higher rate than 5500 feet per minute peripheral

speed." (Springfield E. W. Mfg. Co.)
"Although there is no exactly defined limit at which a wheel must be run to render it effective, experience has demonstrated that, taking into account safety, durability, and liability to heat, 5500 feet per minute at the periphery gives the best results. All first-class wheels have the number of revolutions necessary to give this rate marked on their labels, and a column of figures in the price-list gives a corresponding rate. Above this speed all wheels are unsafe. If run much below it they wear away rapidly in proportion to

what they accombined. Northampton E. W. Co.)

Grades of Emery.—The numbers representing the grades of emery

un from 8 to 120, and the degree of smoothness of surface they leave may

be compared to that left by files as follows:

8 and 10 represent the cut of a wood rasp. 16 " " a coarse rough file. 20 24 " " an ordinary rough file. 44 66 30 36 " .. 66 44 " a bastard file. 40 46 " " " a second-cut file. 66 70 " 66 " a smooth 80 90 " .. 66 6.6 " a superfine 100 44 66 44 " a dead-smooth file, 120 F and FF

### Speed of Polishing-wheels.

Safe Speeds for Grindstones and Emery-wheels.-G. D. Hiscox (Iron Age, April 7, 1892), by an application of the formula for centrif-ugal force in fly-wheels (see Fly-wheels), obtains the figures for strains in grindstones and emery-wheels which are given in the tables below. His formulæ are:

of a grindstone =  $(.7071D \times N)^2 \times .0000795$ "an emery-wheel =  $(.7071D \times N)^2 \times .00010226$ Stress per sq. in. of section of a grindstone

D = diameter in feet, N = revolutions per minute. He takes the weight of sandstone at .078 lb, per cubic inch, and that of an emery-wheel at 0.1 lb, per cubic inch; Ohio stone weighs about .081 lb, and Huron stone about .089 lb, per cubic inch. The Ohio stone will bear a speed at the periphery of .2500 to .3000 ft, per min, which latter should never be exceeded. The Huron stone can be trusted up to 4000 ft., when properly clamped between flanges and not excessively wedged in setting. Apart from the speed of grindstones as a cause of bursting, probably the majority of accidents have really been caused by wedging them on the shaft and over-wedging to true them. The holes being square, the excessive driving of wedges to true the stones starts cracks in the corners that eventually run out until the centrifugal strain becomes greater than the tenacity of the remaining solid stone. Hence the necessity of great caution in the use of wedges, as well as the holding of large quick-running stones between large flanges and leather washers.

#### Strains in Grindstones.

LIMIT OF VELOCITY AND APPROXIMATE ACTUAL STRAIN PER SQUARE INCH OF SECTIONAL AREA FOR GRINDSTONES OF MEDIUM TENSILE STRENGTH.

Diam-		F	Revolution	s per min	nte.		
eter.	100	150	200	250	300	350	400
feet. 2 21/2	lbs. 1.58 2.47	lbs. 3.57 5.57	lbs. 6.35 9.88	lbs. 9.93 15.49	lbs. 14.30 22.29	lbs. 18.36 28.64	lbs. 25.42 39.75
2 21/2 3 31/2 4	3.57 4.86 6.35	8.04 10.98 14.30	14.28 19.44 27.37	22.34 30.38	32.16		
41/2 5 6 7	8.04 9.93 14.30 19.44	18.08 22.34 32.17	32.16	times th	ximate b ne strain om figure	for size	opposite

The figures at the bottom of columns designate the limit of velocity (in revolutions per minute), at the head of the columns for stones of the diameter in the first column opposite the designating figure.

A general rule of safety for any size grindstone that has a compact and

strong grain is to limit the peripheral velocity to 47 feet per second.
There is a large variation in the listed speeds of emery-wheels by different makers—4000 as a minimum and 5600 maximum feet per minute, while others claim a maximum speed of 10,000 feet per minute as the safe speed of their best emery-wheels. Rim wheels and iron centre wheels are specialties that require the maker's guarantee and assignment of speed.

#### Strains in Emery-wheels.

ACTUAL STRAIN PER SQUARE INCH OF SECTION IN EMERY-WHEELS AT THE VELOCITIES AT HEAD OF COLUMNS FOR SIZES IN FIRST COLUMN.

	VELOCITIES AT TIEAD OF COLUMNS FOR DIZES IN TIRST COLUMN.											
n., es.	Revolutions per minute.											
Diam., inches.	600	800	1000	1200	1400	1600	1800	2000	2200	2400	2600	
4 6 8								22.67 51.13		73.62	38.31 86.40	
8			22.67 35.47	32 65 51.08	44.45 69.51	58.05 90.81	73.47			130.62	153.30	
12 14	18.40 24.80	32.72 43.90		73.62	100.21	130.88	165.65					
16 18	32.57 41.41	57.65	90.24	130.31 165.65	177.80				Diam	Revs	per	
20	50.98	90.23	141.22							2800	3000	
22 24	61.81 73.62	130.88							in.			
26 30	86.36 115.04	152.85							6	44.43 $100.21$	115.03	
36	165.64						1		8	177.80		

Joshua Rose (Modern Machine-shop Practice) says: The average speed of grindstones in workshops may be given as follows:

For grinding machinists' tools, about ..... 900 feet per minute.
"" carpenters' "" ..... 600 """

The following table, from the Mechanical World, is for the diameter of stones and the number of revolutions they should run per minute (not to be exceeded), with the diameter of change of shift-pulleys required, varying each shift or change 2½ inches, 2½ inches, or 2 inches in diameter for each reduction of 6 inches in the diameter of the stone.

Diameter of Stone.	Revolutions	Shift of Pulleys, in inches.					
of Stone.	per minute.	21/2	21/4	2			
ft. in.	135	40	36	32			
7 6	144 154	371/2	3334 3116	30			
6 6	166	321/2	291/4 27	26			
6 6 6 0 5 6 5 0	180 196	271/2	243/4	22			
5 0 4 6	216 240	25 22½	221 <u>6</u> 201 <u>4</u>	32 30 28 26 24 22 20 18 16			
7 0 6 6 6 0 5 6 5 0 4 6 4 0 3 0	270 308	371/2 35 321/2 30 271/2 25 221/2 20 171/2 15	18 153/4	16 14 12			
8 0	360	15	131/2	12			
1	2	3	4	5			

Columns 3, 4, and 5 are given to show that if we start an 8-foot stone with, say, a countershaft pulley driving a 46-inch pulley on the grindstone spindle, and the stone makes the right number (135) of revolutions per minute, the reduction in the diameter of the pulley on the grinding-stone spindle, when the stone has been reduced 6 inches in diameter, will require to be also reduced 2½ inches in diameter, or to shift from 40 inches to 37½ inches, and so on similarly for columns 4 and 5. Any other suitable dimensions of pulley may be used for the stone when eight feet in diameter, but the number of inches in each shift named, in order to be correct, will have to be proportional to the numbers of revolutions the stone should run, as given in column 2 of the table.

# Varieties of Grindstones.

(Joshua Rose.)

FOR GRINDING MACHINISTS' TOOLS.

Name of Stone.	Kind of Grit.	Texture of Stone.	Color of Stone.
	Medium to finest	Soft and sharp	Blue or yellowish gray Uniformly light blue Reddish;

### FOR WOOD-WORKING TOOLS.

Wickersley	Medium to fine	Very soft	Grayish yellow
Wickersley Liverpool or Melling.	Medium to fine {	Soft, with sharp	Reddish
Bay Chaleur (New ( Brunswick), ( Huron, Michigan	Medium to finest	Soft and sharp	Uniform light blue
Huron, Michigan	Fine	Soft and sharp	Uniform light blue

# FOR GRINDING BROAD SURFACES, AS SAWS OR IRON PLATES.

Newcastle	Connacto modima	The houd ones	Mallows.
Newcashe	Coarse to med in	The hard ones	renow
Independence	Convoc	Hand to madina	Cuarrich white
Independence	Coarse	maru to medium	Grayish white
Massillon	Connac	Hard to medium Hard to medium	Wallowich white
massmon	Coarse	naru to medium	renowish white

### TAP DRILLS.

# Taps for Machine-screws. (The Pratt & Whitney Co.)

The state of the s					
Approx. Diameter, fractions of an inch.	Wire Gauge.	No. of Threads to inch.	Approx. Diameter, fractions of an inch.	Wire Gauge,	No. of Threads to inch.
	No. 1	60, 72		No. 13	20, 24
	2	48, 56, 64	1/4	14	16, 18, 20, 22, 24
	3	40, 48, 56		15	18, 20, 24
7/64	4	32, 36, 40	17/64	16	16, 18, 20, 22
	5	30, 32, 36, 40	9/32	18	16, 18, 20
9/64	4 5 6 7 8	30, 32, 36, 40		18 19 20	16, 18, 20
	7	24, 30, 32	5/16	20	16, 18, 20
5/32	8	24, 30, 32, 36, 40		22	16, 18
		24, 28, 30, 32	3/8	24	14, 16, 18
3/16	10	20, 22, 24, 30, 32		26	16
	11	22, 24		28 30	16
7/32	12	20, 22, 24		30	16

The Morse Twist Drill and Machine Co. gives the following table showing the different sizes of drills that should be used when a full thread is to be tapped in a hole. The sizes given are practically correct.

Tap Drills.
(The Morse Twist Drill and Machine Co.)

Drill for U. S. S. Thread,	15/16 11/16 15/32 19/32 19/3 19/3 19/3 19/3
Drill for V Thread.	29,9% 15/16 11/28
No. Threads to inch.	00000 ::::::::::::::::::::::::::::::::
Diam. of Tap.	7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-7-
Drill for U.S. S. Thread.	9.16 776 89.78 19.78 19.78 19.78
Drill for V Thread.	5.82 5.72 11/64 7.72 15/62 13/64 7.72 15/62 13/64 7.72 15/62 13/64 13/64 11/62 13/64 15/62 5/64 13/64 15/62 5/64 13/62 15/62 5/64 15/62 5/64 15/64 5/64
No. Threads to inch.	表表表表注注工工员员员员会员工工员会员员会会会会会会会会会会会会会会会会会会会会
Diam. of Tap.	2007 48 70 70 70 70 70 70 70 70 70 70 70 70 70

### TAPER BOLTS, PINS, REAMERS, ETC.

Taper Bolts for Locomotives,—Bolt-threads, American standard, except stay-bolts and boiler-studs, V threads, 12 per inch; valves, cocks, and plugs, V threads, 14 per inch, and ½-inch taper per 1 inch. Standard bolt taper 1/16 inch per foot.

Taper Heamers,—The Pratt & Whitney Co. makes standard taper reamers for locomotive work taper 1/16 inch per foot from ½ inch diam; 7 in. length of flute to 1¾ inch diam; 16 in. length of flute of 1 ¼ inch diam; 16 in. length of flute, diameters advancing by 16ths. P. & W. Co.'s standard taper pin reamers taper ¼ in. per foot, are made in 14 sizes of diameters, 0.135 to 1.009 in.; length of flute 1 5/16 in. to 12 in.

DIMENSIONS OF THE PRATT & WHITNEY COMPANY'S REAMERS FOR MORSE STANDARD-TAPER SOCKET.

No.	Diameter Small End, inches.	Diameter Large End, inches.	Gauge Diam.,la'ge end, inches	L'ngth.	Length Flute, inches.	Total L'ngth.	Taper per foot, inches.
1 2 3	0.374 0.574 0.783	0.525 0.749 0.982	0.481 0.699 0.950	21/8 21/2 3 5/16	3 3½ 4	51/4 61/4 71/2 83/4	0.605 0.600 0.605
4 5 6	1.027 1.484 2.117	1.288 1.796 2.566	1.232 1.746 2.500	4 5 71/4	5 6 8½	83/4 10 121/2	0.615 0.625 0.634

Standard Steel Taper-pins. - The following sizes are made by the Pratt & Whitney Co .: 

0	1	2	3	4	5	6	7	8	9	10	
Diameter l	large e .172	nd: .193	.219	.250	.289	.341	.409	.492	.591	.706	
Approxima 5/32	ate fra	ctions	al size	s:	19/64	11/32	13/32	1/6	19/32	23/32	
Lengths fr	om	3/4						11/4	116	11/2	
To* 1	3/4 11/4	11/2	3/4 13/4		-74	3/4 31/4	1 33/4	41/2	11/2 51/4	-6~	

Diameter small end of standard taper-reamer: 125 .146 .162 .183 .208 .240 .279 .331 .398 .482 .581

Standard Steel Mandrels. (The Pratt & Whitney Co.)—These mandrels are made of tool-steel, hardened, and ground true on their centers. The ends are of a form best adapted to resist injury likely to be caused by driving. They are slightly taper. Sizes, ¼ in. diameter by 3% in, long to 3 in. diam. by 14% in. long, diameters advancing by 16ths.

## PUNCHES AND DIES, PRESSES, ETC.

Clearance between Punch and Die. - For computing the amount Clearance between Funch and Die.—For computing the amount of clearance that a die should have, or, in other words, the difference in size between die and punch, the general rule is to make the diameter of die-hole equal to the diameter of the punch, plus 2/10 the thickness of the plate. Or,  $D=d\times 3/4$ , in which D=d almeter of die-hole, d=d amerier of punch, and t= thickness of plate. For very thick plates some mechanics prefer to make the die-hole a little smaller than called for by the above rule. For or the plate is made from 1/10 to 3/10 of the thickness of the control of the plate of t punch fits in the die. (Am. Machinist.

Konnedy's Spiral Punch. (The Pratt & Whitney Co.)—B. Martell, Chief Surveyor of Lloyd's Register, reported tests of Kennedy's spiral punches in which a 76-inch spiral punch penetrated a 56-inch plate at a pressure of 22 to 25 tons, while a flat punch required 33 to 35 tons. Steel boilerplates punched with a flat punch gave an average tensile strength of 58,579

<sup>\*</sup>Taken 1/2" from extreme end, each size overlaps smaller one about 1/2". Taper 14" to the foot. + Lengths vary by 14" each size.

lbs, per square inch, and an elongation in two inches across the hole of 5.2% while plates punched with a spiral punch gave 63,929 lbs., and 10.6% elonga-

The spiral shear form is not recommended for punches for use in metal of a thickness greater than the diameter of the punch. This form is of greatest benefit when the thickness of metal worked is less than two thirds the

diameter of punch.

Size of Blanks used in the Drawing-press, Oberlin Smith (John. Frank. Inst., Nov. 1886) gives three methods of finding the size of blanks. The first is a tentative method, and consists simply in a series of experiments with various blanks, until the proper one is found. This is for use mainly in complicated cases, and when the cutting portions of the die and punch can be finally sized after the other work is done. The second method is by weighing the sample piece, and then, knowing the weight of the sheet metal per square inch, computing the diameter of a piece having the required area to equal the sample in weight. The third method is by computation, and the formula is  $x = \sqrt{d^2 + 4dh}$  for sharp-cornered cup, where x = diameter of blank, d = diameter of cup, h = height of cup. For round-cornered cup where the corner is small, say radius of corner less than  $\frac{1}{4}$  height of cup, the formula is  $x = (\sqrt{d^2 + 4dh}) - r$ , about; r being the radius of the corner. This is based upon the assumption that the thickness of the metal is not to be altered by the drawing operation.

Pressure attainable by the Use of the Drop-press. (R. H. Thurston, Trans. A. S. M. E., v. 53.)-A set of copper cylinders was prepared, Thurston, trans. A. S. M. E., V. 35.)—A set of copper cylinders was prepared, of pure Lake Superior copper; they were subjected to the action of presses of different weights and of different heights of fall. Companion specimens of copper were compressed to exactly the same amount, and measures were obtained of the loads producing compression, and of the amount of work done in producing the compression by the drop. Comparing one with the other it was found that the work done with the hammer was 90% of the work which should have been done with perfect efficiency. That is to say, 90% of the work done in the testing-machine was equal to that due the weight of

the drop falling the given distance.

Formula: Mean pressure in pounds =  $\frac{\text{Weight of drop} \times \text{fall} \times \text{efficiency}}{\text{Mean pressure in pounds}}$ compression. For pressures per square inch, divide by the mean area opposed to crush-

ing action during the operation

Flow of Metals. (David Townsend, Jour. Frank, Inst., March, 1878.) -In punching holes 7/16 inch diameter through iron blocks 134 inches thick, it was found that the core punched out was only 1 1/16 inch thick, and its volume was only about 32% of the volume of the hole. Therefore, 68% of the metal displaced by punching the hole flowed into the block itself, increasing its dimensions.

#### FORCING AND SHRINKING FITS.

Forcing Fits of Pins and Axles by Hydraulic Pressure. -A 4-inch axle is turned .015 inch diameter larger than the hole into which it is to be fitted. They are pressed on by a pressure of 30 to 35 tons. (Lec-

ture by Coleman Sellers, 1872.)

For forcing the crank-pin into a locomotive driving wheel, when the pinhole is perfectly true and smooth, the pin should be pressed in with a pressure of 6 tons for every inch of diameter of the wheel fit. When the hole is not perfectly true, which may be the result of shrinking the tire on the wheel centre after the hole for the crank-pin has been bored, or if the hole is not perfectly smooth, the pressure may have to be increased to 9 tons for every inch of diameter of the wheel-fit. (Am. Machinist.)

Shrinkage Fits.—In 1886 the American Railway Master Mechanics' Association recommended the following shrinkage allowances for times of

standard locomotives. The tires are uniformly heated by gas-flames, slipped over the cast-iron centres, and allowed to cool. The centres are turned to a diameter equal to the inside diameter of the tire plus the shrinkage allow-

ance:

Diameter of tire, in...... 38 Shrinkage allowance, in... .040 44 50 .047 .053 .060 .066 .070

This shrinkage allowance is approximately 1/80 inch per foot, or 1/960. A common allowance is 1/1000. Taking the modulus of elasticity of steel at

30,000,000, the strain caused by shrinkage would be 30,000 lbs. per square inch, which is well within the elastic limit of machinery steel.

# SCREWS, SCREW-THREADS, ETC.\*

Efficiency of a Screw.-Let a = angle of the thread, that is, the angle whose tangent is the pitch of the screw divided by the circumference of a circle whose diameter is the mean of the diameters at the top and bottom of the thread. Then for a square thread

Efficiency = 
$$\frac{1 - f \tan a}{1 + f \cot a},$$

in which f is the coefficient of friction. (For demonstration, see Cotterill and Slade, Applied Mechanics, p. 146.) Since  $\cot a = 1 + \tan n$ , we may substitute for cotan a the reciprocal of the tangent, or if  $p = \operatorname{pitch}$ , and  $c = \operatorname{mean} \operatorname{circ}$ cumference of the screw.

Efficiency = 
$$\frac{1 - f\frac{p}{c}}{1 + f\frac{c}{p}}.$$

Example. - Efficiency of square-threaded screws of 1/4 in. pitch.

Diameter at bottom of thread, in 1 2 3	4
" top " " 1½ 2½ 3½ 41 Mean circumference " " 3.927 7.069 10.21 13.	1/2 .35
	.35
Cotangent $a = c \div p$ = 7.854 14.14 20.42 26.	.70
	575
Efficiency if $\hat{f} = .10 = 55.3\%$ 41.2% 32.7% 27.	.2%
" $f = .15 = 45\%$ 31.7% 24.4% 19.	.9%

The efficiency thus increases with the steepness of the pitch. The above formulæ and examples are for square-threaded screws, and consider the friction of the screw-thread only, and not the friction of the collar or step by which end thrust is resisted, and which further reduces the efficiency. The efficiency is also further reduced by giving an inclination to the side of the thread, as in the V-threaded screw. For discussion of this subject, see paper by Wilfred Lewis, Jour. Frank. Inst. 1880; also Trans. A. S. M. E., vol. xii. 784.

Efficiency of Screw-bolts.—Mr. Lewis gives the following approximate formula for ordinary screw-bolts (V threads, with collars): p = pitch of screw, d = outside diameter of screw, F = force applied at circumference to lift a unit of weight, E = efficiency of screw. For an average case, in which the coefficient of friction may be assumed at .15,

$$F = \frac{p+d}{3d}, \qquad E = \frac{p}{p+d}.$$

For bolts of the dimensions given above, ½-in. pitch, and outside diameters 1½, 2½, 3½, 34, and 4½ in., the efficiencies according to this formula would be, respectively, 25, 167, 125, and 10.

James McBride (Trans. A. S. M. E., xii, 781) describes an experiment with an ordinary 2-in, screw-bolt, with a V thread, 4½ threads per inch, raising a weight of 7500 lbs., the force being applied by turning the nut. Of the power applied 89.85 was absorbed by friction of the nut on its supporting washer and of the threads of the bolt in the nut. The nut was not faced,

and had the flat side to the washer.

The flux was not laced, and had the flat side to the washer.

The flux was not laced, and had the flat in his "Experimental Mechanics" says: "Experiments showed in two cases respectively about \$\frac{2}{3}\$ and \$\frac{2}{3}\$ of the power was lost." Trautwine says: "In practice the friction of the screw (which under heavy loads becomes very great) make the theoretical calculations of but little value.

Weisbach says: "The efficiency is from 19% to 30%."

Efficiency of a Differential Screw.—A correspondent of the American Machinist describes an experiment with a differential screw-punch, consisting of a notter screw 2 in. diam., 3 threads per in., and an inner screw 136 in. diam., 31/2 threads per inch. The pitch of the outer screw

KEYS.

being  $\frac{1}{16}$  in, and that of the inner screw 2/7 in., the punch would advance in one revolution  $\frac{1}{16} - 2/7 = 1/21$  in. Experiments were made to determine the force required to punch an 11/16-in, hole in iron  $\frac{1}{16}$  in, thick, the force being applied at the end of a lever-arm of 4/34 in. The leverage would be  $4734 \times 27 \times 21 = 6300$ . The mean force applied at the end of the lever was 95 lbs., and the force at the punch, if there was no friction, would be  $6300 \times 95 = 598,500$  lbs. The force required to punch the iron assuming a shearing resistance of 50,000 lbs per 84, in, would be  $50,000 \times 11/16 \times \pi \times 11/16 \times 11/1$ shearing resistance of 50,000 lbs, per sq. in., would be  $50,000 \times 11/16 \times \pi \times 42 = 27,000$  lbs, and the efficiency of the punch would be 27,000 + 588,500 = only 4.5%. With the larger screw only used as a punch the mean force at the end of the lever was only 82 lbs. The leverage in this case was  $4734 \times 2\pi \times 3 = 900$ , the total force referred to the punch, including friction,  $900 \times 22 \times 2\pi \times 3 = 900$ , and the efficiency 27,000 + 73,800 = 36.7%. The screws were of tool-steel, well fitted, and lubricated with lard-oil and plumbago. **Powell's New Screw-thread**.—A M. Powell (4nn. Mach., Jan. 24, 1895) has designed a new screw-thread to replace the square form of thread, giving the advantages of greater ease in making fits, and provision for 'take up' 'in case of wear. The dimensions are the same as those of square-thread screws with the avecarion that the sides of the thread screws.

thread screws, with the exception that the sides of the thread, instead of being series, with the exception that the sides of the thread, histead of being perpendicular to the axis of the screw, are inclined 14% to such perpendicular; that is, the two sides of a thread are inclined  $29^6$  to each other. The formulae for dimensions of the thread are the following: Depth of thread = 1% pitch; width of top of thread = width of space at bottom = 3.077 + pitch; thickness at root of thread = width of space at top = .6293 +

The term pitch is the number of threads to the inch.

#### PROPORTIONING PARTS OF MACHINES IN A SERIES OF SIZES.

(Stevens Indicator, April, 1892.)

The following method was used by Coleman Sellers while at William Sellers & Co.'s to get the proportions of the parts of machines, based upon the size obtained in building a large machine and a small one to any series of machines. This formula is used in getting up the proportion-book and arranging the set of proportious from which any machine can be constructed of intermediate size between the largest and smallest of the series.

Rule to Establish Construction Formula. - Take difference between the nominal sizes of the largest and the smallest machines that have been designed of the same construction. Take also the difference between the sizes of similar parts on the largest and smallest machines selected. Divide the latter by the former, and the result obtained will be a "factor," which, multiplied by the nominal capacity of the intermediate machine, and increased or diminished by a constant "increment," will give the size of the part required. To find the "increment :" Multiply the nominal capacity of some known size by the factor obtained, and subtract the result from the size of the part belonging to the machine of nominal capacity selected.

EXAMPLE.—Suppose the size of a part of a 72-in. machine is 3 in., and the EXAMPLE—Suppose the size of a part of a 12-in, machine is  $s^{-1}$ , and the corresponding part of a 42-in, machine is 1/8, or 1.875 in; then 12 - 42 = 30, and 3 in. -1/3 in. =1/3 in. =1.125.  $-1.125 + 30 = .0375 = the "factor." and <math>.0375 \times 42 = 1.575$ . Then 1.875 - 1.575 = .3 = the "increment" to beadded. Let D = nominal capacity; then the formula will read: x =

antied: Dev D = 100 min are talked, y = 1.875, y =part to be found.

#### KEYS.

Sizes of Keys for Mill-gearing. (Trans. A. S. M. E., xiii, 229.)—E. G. Parkhurst's rule: Width of key = 1/8 diam. of shaft, depth = 1/9 diam. of shaft; taper 1/3 in, to the foot.

Custom in Michigan saw-mills: Keys of square section, side = 1/4 diam. of

shaft, or as nearly as may be in even sixteenths of an inch.

J. T. Hawkins's rule: Width = ½ diam. of hole; depth of side abutment

in shaft = 1/8 diam. of hole. W. S. Huson's rule: ½-inch key for 1 to 1½ in. shafts, 5/16 key for 1½ to 1½ in. shafts, 3/16, key for 1½ to 13/4 in. shafts, and so on. Taper ½ in. to the foot. Total thickness at large end of splice, 4/5 width of key.

Unwin (Elements of Machine Design) gives: Width =  $\frac{1}{4}d + \frac{1}{8}$  in. Thickness =  $\frac{1}{6}d + \frac{1}{8}$  in., in which d = diam, of shaft in inches. When wheels or pulleys transmitting only a small amount of power are keyed on large shafts, he says, these dimensions are excessive. In that case, if H.P. = horse-power transmitted by the wheel or pulley, <math>N = revs. per min, P = force acting at the circumference, in lbs., and R = radius of pulley in inches, take

$$d = \sqrt[3]{\frac{\overline{100 \text{ H.P.}}}{N}} \text{ or } \sqrt[3]{\frac{PR}{630}}.$$

Prof. Coleman Sellers (Stevens Indicator, April, 1892) gives the following: Prof. Coleman Sellers (Stevens Indicator, April, 1892) gives the following: The size of keys, both for shafting and for machine tools, are the proportions adopted by William Sellers & Co., and rigidly adhered to during a period of nearly forty years. Their practice in making keys and fitting them is, that the keys shall always bind tight sidewise, but not top and bottom; that is, not necessarily touch either at the bottom of the key-seat in the shaft or touch the top of the slot cut in the gear-wheel that is fastened to the shaft; but in practice keys used in this manner depend upon the fit of the wheel upon the shaft being a forcing fit, or a fit that is so tight as to require screw-pressure to put the wheel in place upon the shaft.

## Size of Keys for Shafting.

Dia	meter o	f Shaft, in.	Size of Key, in
11/4 1	7/16	1 11/16	5/16 × 3/8
1 15/16 2	3/16	1 11/16	7/16× ½
2 7/16			9/16 × 5/8
2 11/16 2	15/16	3 3/16 3 7/16	11/16× 3⁄4
3 15/16 4	7/16	4 15/16	13/16 × 3/8
5 7/16 5	15/16	6 7/16	15/16×1
6 15/16 7	7/16	7 15/16 8 7/16 8 15/1	6 1 1/16 × 11/6

Length of key-seat for coupling = 11/2 × nominal diameter of shaft.

## Size of Keys for Machine Tools.

Diam. of Shaft, in. Size of Key, in. sq.	Diam. of Shaft, in. Size of Key,
15/16 and under 1/8	4 to 5 7/16 13/16
1 to 1 3/16 3/16	5½ to 6 15/16 15/16
1½ to 1 7/16	7 to 8 15/16 1 1/16
1½ to 1 11/16 5/16	9 to 10 15/16 1 3/16
13% to 2 3/16 7/16	11 to 12 15/16 1 5/16
2½ to 2 11/16 9/16	13 to 14 15/16 1 7/16
934 to 3 15/16	·

John Richards, in an article in Cassier's Magazine, writes as follows: There are two kinds or system of keys, both proper and necessary, but widely dif-ferent in nature. 1. The common fastening key, usually made in width one ferent in fature. I. The common fastering key, usually made in width one fourth of the shaft's diameter, and the depth five eighths to one third the width. These keys are tapered and fit on all sides, or, as it is commonly described, "bear all over." They perform the double function in most cases of driving or transmitting and fastening the keyed-on member against movement endwise on the shaft. Such keys, when properly made, drive as a strut, diagonally from corner to corner.

2. The other kind or class of keys are not tapered and fit on their sides only, a slight clearance being left on the back to insure against wedge action or redula strain. These keys drive by shearing strain

or radial strain. These keys drive by shearing strain.

For fixed work where there is no sliding movement such keys are commonly made of square section, the sides only being planed, so the depth is more than the width by so much as is cut away in finishing or fitting.

For sliding bearings, as in the case of drilling-machine spindles, the depth should be increased, and in cases where there is heavy strain there should

be two keys or feathers instead of one.

The following tables are taken from proportions adopted in practical use. Flat keys, as in the first table, are employed for fixed work when the parts are to be held not only against torsional strain, but also against movement endwise; and in case of heavy strain the strut principle being the strongest and most secure against movement when there is strain each way, as in the case of engine cranks and first movers generally. The objections to the system for general use are, straining the work out of truth, the care and expense required in fitting, and destroying the evidence of good or bad attinger the lequire joint. When the part is fastened at the part is the part is the part of this kind there is no means of the part is work is well fitted or not. For this reason such keys are not employed by machine tool-makers, and in the case of accurate work of any kind, indeed, cannot be, because of the wedging strain, and also the difficulty of inspecting completed work.

## I. DIMENSIONS OF FLAT KEYS, IN INCHES.

## II. DIMENSIONS OF SQUARE KEYS, IN INCHES.

## III. DIMENSIONS OF SLIDING FEATHER-KEYS, IN INCHES.

Diam. of shaft 1	11/4 11/6	13 <u>4</u>	2	21/4	21/2	3	3½	4	41/5
Breadth of keys	1/4 1/4	5/16	5/16	3/8	3/8	1/2	9/16	9/16	5/8
Depth of keys:	3/8 3/8	7/16	7/16	1/2	1/2	5/8	3⁄4	3/4	7/8

P. Pryibil furnishes the following table of dimensions to the Am. Machinist. He says: On special heavy work and very short hubs we put in two keys in one shaft 90° apart. With special long hubs, where we cannot use keys with noses, the keys should be thicker than the standard.

Diameter of Shafts,		Thick-	Diameter of Shafts,	Width,	Thick-
inches.		ness, in.	inches.	inches.	ness, in.
34 to 1 1/16 11/6 to 1 5/16 1 7/16 to 1 11/16 1 15/16 to 2 3/16 2 7/16 to 2 11/16 2 15/16 to 3 3/16	3/16 5/16 3/8 1/2 5/8 3/4	3/16 14 5/16 3/8 1/2 9/16	3 7/16 to 3 11/16 3 15/16 to 4 3/16 4 7/16 to 4 11/16 47/8 to 53/8 57/8 to 63/8 67/8 to 73/8	7/8 1 11/6 11/4 11/4 11/4 13/4	5/8 11/16 3/4 15/16 1 11/8

Keys longer than 10 inches, say 14 to 16", 1/16" thicker; keys longer than 10 inches, say 18 to 20",  $\frac{1}{2}$ 6" thicker; and so on. Special short hubs to have two keys.

For description of the Woodruff system of keying, see circular of the Pratt & Whitney Co.; also Modern Mechanism, page 455.

### HOLDING-POWER OF KEYS AND SET-SCREWS.

Tests of the Holding-power of Set-screws in Pulleys, (G. Lanza, Traus, A. S. M. E., x. 230.)—These tests were made by using a pulley fastened to the shaft by two set-screws with the shaft keyed to the holders; then the load required at the rim of the pulley to cause it to slip was determined, and this being multiplied by the number 6.03° (obtained by adding to the radius of the pulley one-half the diameter of the wire rope, and dividing the sum by twice the radius of the shaft, since there were two set-screws in action at a time) gives the holding-power of the set-screws. The set-screws used were of wrought-iron, 5% of an inch in diameter, and ten threads to the inch; the shaft used was of steel and rather hard, the set-screws making but little impression upon it. They were set up with a force of 75 lbs. at the end of a ten-inch monkey-wirend. The set-screws used were of four kinds, marked respectively A, B, C, and D. The results were as follows:

A, ends perfectly flat, 9/16-in, diameter. 1412 to 2294 lbs.; average 2064. B, radius of rounded ends about 1/2 inch, 2747 " 3079 " 1902 " 3079 " 2912.

1962 " 2958 D ends cup-shaped and case-hardened.

REMARKS .- A. The set-screws were not entirely normal to the shaft; hence they bore less in the earlier trials, before they had become flattened by wear.

B. The ends of these set-screws, after the first two trials, were found to be flattened, the flattened area having a diameter of about 1/4 inch.

C. The ends were found, after the first two trials, to be flattened, as in B. D. The first test held well because the edges were sharp, then the holdingpower fell off till they had become flattened in a manner similar to B, when

the holding-power increased again.

Tests of the Holding-power of Keys. (Lanza.)—The load was applied as in the tests of set-screws, the shaft being firmly keyed to the holders. The load required at the rinn of the pulley to shear the keys was determined, and this, multiplied by a suitable constant, determined in a similar way to that used in the case of set-screws, gives us the shearing strength per square inch of the keys.

The keys tested were of eight kinds, denoted, respectively, by the letters

A, B, C, D, E, F, G and H, and the results were as follows: A, B, D and F, each 4 tests; E, 3 tests; C, G, and H, each 2 tests.

A, Norway iron,  $2'' \times 14'' \times 15/32''$ , B, refined iron,  $2'' \times 14'' \times 15/32''$ , C, tool steel,  $1'' \times 4i'' \times 15/32''$ , D, machinery steel,  $2'' \times 4i'' \times 15/32''$ , E, Norway iron,  $1156'' \times 56'' \times 7/16''$ , F, cast-iron,  $2'' \times 4i'' \times 15/32''$ , H, cast-iron,  $1156'' \times 15/32'' \times 7/16''$ , H, cast-iron,  $1156'' \times 15/32'' \times 7/16''$ , 40,184 to 47,760 lbs.; average, 42,726. 36,482 " 39,254; " 38,059. 91,344 & 100,056. 64,630 to 70,186; 66,875. 36,850 " 66 37,222; 37,036. 30,278 '' 37,222 & 36,944; 33,034. 38,700. 29,814 & 38,978.

In A and B some crushing took place before shearing. In E, the keys being only 7/16 in. deep, tipped slightly in the key-way. In H, in the first test, there was a defect in the key-way of the pulley.

# DYNAMOMETERS.

Dynamometers are instruments used for measuring power. They are of several classes, as: 1. Traction dynamometers, used for determining the power required to pull a car or other vehicle, or a plough or harrow. 2. Brake or absorption dynamometers, in which the power of a rotating shaft or wheel is absorbed or converted into heat by the friction of a brake; and, 3. Transmission dynamometers, in which the power in a rotating shaft is measured during its transmission through a belt or other connection to

another shaft, without being absorbed.

Traction Dynamometers generally contain two principal parts: (1) A spring or series of springs, through which the pull is exerted, the extension of the spring measuring the amount of the pulling force; and (2) a papercovered drum, rotated either at a uniform speed by clockwork, or at a speed covered drum, rotated either at a uniform speed by clockwork, or at a speed proportional to the speed of the traction, through gearing, on which the extension of the spring is registered by a pencil. From the average height of the diagram drawn by the pencil above the zero-line the average pulling force in pounds is obtained, and this multiplied by the distance traversed, in feet, gives the work done, in foot-pounds. The product divided by the time in minutes and by 33,000 gives the horse-power.

The Prony brake is the typical form of absorption dynamometer. (See Fig. 167, from Flather on Dynamometers and the Measurement of

Power.)

Primarily this consists of a lever connected to a revolving shaft or pulley in such a manner that the friction induced between the surfaces in contact will tend to rotate the arm in the direction in which the shaft revolves. This rotation is counterbalanced by weights P, hung in the scale-pan at the end of the lever. In order to measure the power for a given number of revolutions of pulley, we add weights to the scale-pan and screw up on bolts bb, until the friction induced balances the weights and the lever is maintained in its horizontal position while the revolutions of shaft per minute remain constant.

For small powers the beam is generally omitted—the friction being measured by weighting a band or strap thrown over the pulley. Ropes or cords

are often used for the same purpose.

Instead of hanging weights in a scale-pan, as in Fig. 167, the friction may be weighed on a platform-scale; in this case, the direction of rotation being

the same, the lever-arm will be on the opposite side of the shaft.

In a modification of this brake, the brake-wheel is keyed to the shaft, and its rim is provided with inner flanges which form an annular trough for the retention of water to keep the pulley from heating. A small stream of water constantly discharges into the trough and revolves with the pulley-the centrifugal force of the

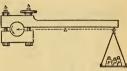


Fig. 167.

particles of water overcoming the action of gravity; a waste-pipe with its end flattened is so placed in the trough that it acts as a scoop, and removes all surplus water. The brake consists of a flexible strap to which are fitted blocks of wood forming the rubbing surface; the ends of the strap are connected by an adjustable bolt-clamp, by means of which any desired tension may be obtained.

The horse-power or work of the shaft is determined from the following:

Let W = work of shaft, equals power absorbed, per minute;

P = unbalanced pressure or weight in pounds, acting on lever-armat distance L;

L = length of lever-arm in feet from centre of shaft;

V =velocity of a point in feet per minute at distance L, if arm were allowed to rotate at the speed of the shaft;

N = number of revolutions per minute;

H.P. = horse-power.

Then will  $W = PV = 2\pi LNP$ . Since H.P.  $= 2\pi LNP \div 33,000$ , we have H.P.  $= 2\pi LNP \div 33,000$ , If  $L = \frac{33}{2\pi}$ , we obtain H.P.  $= \frac{NP}{1000}$ .  $33 + 2\pi$  is practically 5 ft. 3 in., a value often used in practice for the length of arm.

If the rubbing-surface be too small, the resulting friction will show great irregularity—probably on account of insufficient lubrication—the jaws being allowed to seize the pulley, thus producing shocks and sudden vibrations of the lever-arm.

Soft woods, such as bass, plane-tree, beech, poplar, or maple are all to be preferred to the harder woods for brake-blocks. The rubbing-surface should be well lubricated with a heavy grease.

The Alden Absorption-dynamometer. (G. I. Alden, Trans. A. S. M. E., vol. xi. 958; also xii, 700 and xii, 429.—This dynamometer is a friction-brake, which is capable in quite moderate sizes of absorbing large powers with unusual steadiness and complete regulation. A smooth cast-iron disk is keyed on the rotating shaft. This is enclosed in a cast-iron shell, formed of two disks and a ring at their circumference, which is free to revolve on the shaft. To the interior of each of the sides of the shell is to revolve on the shaft. To the interior of each of the sides of the shell is fitted a copper plate, enclosing between itself and the side a water-tight space. Water under pressure from the city pipes is admitted into each of these spaces, forcing the copper plate against the central disk. The chamber enclosing the disk is filled with oil. To the outer shell is fixed a weighted arm, which resists the tendency of the shell to rotate with the shaft, caused by the friction of the plates against the central disk. Four brakes of this type, 56 in, diam, were used in testing the experimental locomotive at Purdue University (Trans. A. S. M. E., xili. 429). Each was designed for a maximum moment of 10,500 foot-pounds with a water-pressure of 40 lbs. per sq. in.

The area in effective contact with the copper plates on either side is represented by an annular surface having its outer radius equal to 28 inches, and its inner radius equal to 10 inches. The apparent coefficient of friction

between the plates and the disk was 31/2%.

W. W. Beaumont (Proc. Inst. C. E. 1889) has deduced a formula by means of which the relative capacity of brakes can be compared, judging from the amount of horse-power ascertained by their use.

If W =width of rubbing-surface on brake-wheel in inches; V =vel. of point on circum, of wheel in feet per minute; K = coefficient; then

K = WV + H.P.

Capacity of Friction-brakes.-Prof. Flather obtains the values of K given in the last column of the subjoined table :

•										
Horse-power.	R. P. M. Brake- pulley.		Diameter, in feet.	Length of Arm.	Design of Brake.	Value of K.				
21 19 20 40 33 150 24 180 475 125 ( 250)	150 148.5 146 180 150 150 142 100 76.2 290 (	24	5 9 6 5 7 4	33" 33.38" 32.19" 32" 32" 38.31" 126.1" 191" 63"	Royal Ag. Soc., compensating McLaren, compensating water-cooled and comp. Garrett, """ Schoenheyder, water-cooled Balk Gately & Kletsch, water-cooled Webber, water-cooled Westinghouse, water-cooled.	785 858 802 741 749 282 1385 209 84.7 465				
40 ( 125 (	322 (	13	4	2734"	" "	847				

The above calculations for eleven brakes give values of K varying from 84 7 to 1385 for actual horse-powers tested, the average being K = 655. Instead of assuming an average coefficient, Prof. Flather proposes the following:

Water-cooled brake, non-compensating, K=400; W=400 H.P. + V. Water-cooled brake, compensating, K=750; W=750 H.P. + V. Non-cooling brake, with or without compensating device, K=900; W=900 H.P. + V.

Transmission Dynamometers are of various forms, as the Transmission Dynamometers are of various forms, as the Batchelder dynamometer, in which the power is transmitted through a "train-arm" of bevel gearing, with its modifications, as the one described by the author in Trans. A. I. M. E., viii. 177, and the one described by Samuel Webber in Trans. A. S. M. E., x. 514: belt dynamometers, as the Tatham; the Van Winkle dynamometer, in which the power is transmitted from a revolving shaft to another in line with it, the two almost touching, through the medium of coiled springs fastened to arms or disks keyed to the shafts; the Brackett and the Webb cradle dynamometers, used for measuring the power required to run dynamo-electric machines. Descriptions of the four last named are given in Flather on Dynamometers.

When information an warious forms of dynamometers will be found in

Much information on various forms of dynamometers will be found in Trans. A. S. M. E., vol. vii. to xv., inclusive, indexed under Dynamometers.

# ICE-MAKING OR REFRIGERATING MACHINES.

References.—An elaborate discussion of the thermodynamic theory of the action of the various fluids used in the production of cold was published by M. Ledoux in the Annales des Mines, and translated in Van Nostrand's Magazine in 1879. This work, revised and additions made in the light of recent experience by Professors Denton, Jacobus, and Riesenberger, was reprinted in 1892. (Van Nostrand's Science Series, No. 46.) The work is largely mathematical, but it also contains much information of immediate practical value, from which some of the matter given below is taken. Other references are Wood's Thermodynamics, Chap. V., and numerous papers by Professors Wood, Denton, Jacobus, and Linde in Trans. A. S. M. E., vols. x. to xiv.; Johnson's Cyclopædia, article on Refrigerating-machines; also Eng'g, June 18, July 2 and 9, 1886; April 1, 1887; June 15, 1888; July 31, Aug. 28, 1889; Sept. 11 and Dec. 4, 1891; May 6 and July 8, 1892. For properties of Ammonia and Sulphur Dioxide, see papers by Professors Wood and Jacobus, Trans. A. S. M. E., vols. x. and xii,

For illustrated articles describing refrigerating-machines, see Am. Mach., May 29 and June 26, 1890, and Mfrs. Record, Oct. 7, 1892; also catalogues of builders, as Frick & Co., Waynesboro, Pa.; De La Vergne Refrigerating-machine Co., New York; and others.

Operations of a Refrigerating-machine,—Apparatus designed for refrigerating is based upon the following series of operations: Compress a gas or vapor by means of some external force, then relieve it of its heat so as to diminish its volume; next, cause this compressed gas or vapor to expand so as to produce mechanical work, and thus lower its temperature. The absorption of heat at this stage by the gas, in resuming its original condition, constitutes the refrigerating effect of the apparatus.

A refrigerating-machine is a heat-engine reversed.

From this similarity between heat-motors and freezing-machines it results that all the equations deduced from the mechanical theory of heat to determine the performance of the first, apply equally to the second.

The efficiency depends upon the difference between the extremes of tem-

perature. The useful effect of a refrigerating-machine depends upon the ratio between the heat-units eliminated and the work expended in compressing and expanding.

This result is independent of the nature of the body employed.

Unlike the heat-motors, the freezing-machine possesses the greatest efficiency when the range of temperature is small, and when the final temperature is elevated.

If the temperatures are the same, there is no theoretical advantage in em-

ploying a gas rather than a vapor in order to produce cold.

The choice of the intermediate body would be determined by practical considerations based on the physical characteristics of the body, such as the greater or less facility for manipulating it, the extreme pressures required for the best effects, etc.

Air offers the double advantage that it is everywhere obtainable, and that we can vary at will the higher pressures, independent of the temperature of the refrigerant. But to produce a given useful effect the apparatus must be of larger dimensions than that required by liquefiable vapors.

The maximum pressure is determined by the temperature of the condenser and the nature of the volatile liquid; this pressure is often very high.

When a change of volume of a saturated vapor is made under constant pressure, the temperature remains constant. The addition or subtraction of heat, which produces the change of volume, is represented by an increase or a diminution of the quantity of liquid mixed with the vapor.

On the other hand, when vapors, even if saturated, are no longer in contact with their liquids, and receive an addition of heat either through com-

pression by a mechanical force, or from some external source of heat, they comport themselves nearly in the same way as permanent gases, and become superheated.

It results from this property, that refrigerating-machines using a liquefiable gas will afford results differing according to the method of working, and depending upon the state of the gas, whether it remains constantly sat-

urated, or is superheated during a part of the cycle of working.

The temperature of the condenser is determined by local conditions. The interior will exceed by 9° to 18° the temperature of the water furnished to the exterior. This latter will vary from about 52° F., the temperature of water from considerable depth below the surface, to about 95° F., the temperature of surface-water in hot climates. The volatile liquid employed in the machine ought not at this temperature to have a tension above that which can be readily managed by the apparatus.

On the other hand, if the tension of the gas at the minimum temperature

is too low, it becomes necessary to give to the compression-cylinder large dimensions, in order that the weight of vapor compressed by a single stroke

of the piston shall be sufficient to produce a notably useful effect.

These two conditions, to which may be added others, such as those depending upon the greater or less facility of obtaining the liquid, upon the dangers incurred in its use, either from its inflammability or unhealthfulness, and finally upon its action upon the metals, limit the choice to a small number of substances.

The gases or vapors generally available are: sulphuric ether, sulphurous

oxide, ammonia, methylic ether, and carbonic acid.

The following table, derived from Regnault, shows the tensions of the vapors of these substances at different temperatures between - 22° and + 104°.

#### Pressures and Boiling-points of Liquids available for Use in Refrigerating-machines.

Temp, of Ebullition,	Tension of Vapor, in lbs. per sq. in., above Zero.									
Deg. Fahr.	Sul- phuric Ether.	Sulphur Dioxide.	Ammonia.	Methylic Ether.	Carbonic Acid,	Pictet Fluid.				
- 40 - 31 - 22 - 13 - 4 5 11 23 32	1.30 1.70 2.19 2.79 3.55	5.56 7.23 9.27 11.76 14.75 18.31 22.53	10.22 13.23 16.95 21.51 27.04 33.67 41.58 50.91 61.85	11.15 13.85 17.06 20.84 25.27 30.41 36.34	251.6 292.9 340.1 393.4 453.4 520.4	13.5 16.2 19.3 22.9 26.9				
41 50 59 68 77 86 95	4.45 5.54 6.84 8.38 10.19 12.31 14.76 17.59	27.48 33.26 39.93 47.62 56.39 66.37 77.64 90.32	74.55 89.21 105.99 125.08 146.64 170.83 197.83 227.76	43.13 50.84 59.56 69.35 80.28 92.41	594.8 676.9 766.9 864.9 971.1 1085.6 1207.9 1338.2	31.2 36.2 41.7 48.1 55.6 64.1 73.2 82.9				

The table shows that the use of ether does not readily lead to the production of low temperatures, because its pressure becomes then very feeble. Ammonia, on the contrary, is well adapted to the production of low tem-

peratures.

Methylic ether yields low temperatures without attaining too great pressures at the temperature of the condenser. Sulphur dioxide readily affords temperatures of -14 to -5, while its pressure is only 3 to 4 atmospheres at the ordinary temperature of the condenser. These latter substances then lend themselves conveniently for the production of cold by means of mechanical force.

The "Pictet fluid" is a mixture of 97% sulphur dioxide and 3% carbonic cid. At atmospheric pressure it affords a temperature 14° lower than acid.

sulphur dioxide.

Carbonic acid is as yet (1895) in use but to a limited extent, but the relatively greater compactness of compressor that it requires, and its inoffensive character, are leading to its recommendation for service on shipboard, where economy of space is important.

Certain ammonia plants are operated with a surplus of liquid present during compression, so that superheating is prevented. This practice is known

as the "cold system" of compression.

Nothing definite is known regarding the application of methylic ether or of the petroleum product chymogene in practical refrigerating service. The inflammability of the latter and the cumbrousness of the compressor required are objections to its use.

"Ice-melting Effect."—It is agreed that the term "ice-melting

effect" means the cold produced in an insulated bath of brine, on the assumption that each 142.3 B.T.U.\* represents one pound of ice, this being the latent heat of fusion of ice, or the heat required to melt a pound of ice at

32° to water at the same temperature.

The performance of a machine, expressed in pounds or tons of "ice-melting capacity," does not mean that the refrigerating-machine would make the same amount of actual ice, but that the cold produced is equivalent to the effect of the melting of ice at 32° to water of the same temperature.

In making artificial ice the water frozen is generally about 70° F, when submitted to the refrigerating effect of a machine; second, the ice is chilled from 12° to 20° below its freezing-point; third, there is a dissipation of cold, from the exposure of the brine tank and the manipulation of the ice-cans; therefore the weight of actual ice made, multiplied by its latent heat of fusion, 142.2 thermal units, represents only about three fourths of the cold produced in the brine by the refrigerating fluid per I.H.P. of the engine driving the compressing-pumps. Again, there is considerable fuel consumed to operate compressing pumps. Again, mere is consideration the constituent of operative the brine-circulating pump, the condensing-water and feed-pumps, and to reboil, or purify, the condensed steam from which the ice is frozen. This finel, together with that wasted in leakage and drip water, amounts to about one half that required to drive the main steam-engine. Hence the pound of actual ice manufactured from distilled water is just about half the equivalent of the refrigerating effect produced in the brine per indicated horsewhen ice is made directly from natural water by means of the "plate"

system," about half of the fuel, used with distilled water, is saved by avoiding the reboiling, and using steam expansively in a compound engine

Ether-machines, used in India, are said to have produced about 6

lbs. of actual ice per pound of fuel consumed.

The ether machine is obsolete, because the density of the vapor of ether, at the necessary working-pressure, requires that the compressing-cylinder shall be about 6 times larger than for sulphur dioxide, and 17 times larger than for ammonia.

Air-machines require about 1.2 times greater capacity of compressing cylinder, and are, as a whole, more cumbersome than ether machines, but they remain in use on ship-board. In using air the expansion must take place in a cylinder doing work, instead of through a simple expansion-cock which is used with vapor machines. The work done in the expansion-cylin-

der is utilized in assisting the compressor.

Ammonia Compression-machines.-"Cold" vs. "Dry" Systems Ammonia compression—In the "cold" system or "humid" system one of the ammonia entering the compression-cylinder is liquid, so that the heat developed in the cylinder is absorbed by the liquid and the temperature of the ammonia thereby confined to the boiling-point due to the condenser-pressure. No jacket is therefore required about the cylinder.

In the "dry" or "hot" system all ammonia entering the compressor is the "dry" or "hot" system all ammonia entering the compressor is the "dry" or "hot" system all ammonia entering the compressor is the system of t

gaseous, and the temperature becomes by compression several hundred degrees greater than the boiling-point due to the condenser-pressure. A waterjacket is therefore necessary to permit the cylinder to be properly lubri-

Relative Performance of Ammonia Compression and Absorption-machines, assuming no Water to be Entrained with the Ammonia-gas in the Condenser. (Penton and Jacobus, Trans. A. S. M. E., xill.)—It is assumed in the calculation for both machines that 1 h. of coal imparts 10,000 B.T.U. to the boiler. The

<sup>\*</sup>The latent heat of fusion of ice is 144 thermal units (Phil. Mag., 1871, xll., 182); but it is customary to use 142. (Prof. Wood, Trans, A. S. M. E., xl. S34.)

condensed steam from the generator of the absorption-machine is assumed to be returned to the boller at the temperature of the steam entering the generator. The engine of the compression-machine is assumed to exhaust through a feed-water heater that heats the feed-water to 212° F. The engine is assumed to consume 264 dbs. of water per hour per horse-power. The figures for the compression-machine include the effect of friction, which is taken at 15% of the net work of compression,

Condenser.   Refrigerating Coils   Absorption   Absorpt										
Temp. in degrees False   Temp. in degrees   Tem	Cond	enser.	Refri	gerat- Joils.	Fri	Pot	ands of	f Ice-melti r lb. of Co	ng Effect al.	or of per
Temp. in degrees False   Temp. in degrees   Tem		1				Com	press. hine.	Abso	rption- chine.*	nerate B.T.U ated.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	fahr.		ahr.	1	, deg	per l	coal P.	onia onia gen-	mm. usts here ter, mp.	ge ine, ircul
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	ees ]	ssure	ees ]	ssure	orbei			achir amm oumi the	exha nosp hea ye te	ed to
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	degr		degr		Abs			on-m the ting-l		rnish tion-r mmo
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	p. in	olute in.	p. in	olute in.	p. of	g 3 ll	r hou	orption nich cula usts ator.	which of the rough	sorpi of a
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	Tem	Abs	Tem	Abs	Tem	Usir	Usir	Abse wł cin ba	EXPERS.	Hea ab lb.
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	61.2	110.6	5	33.7	61.2	38.1	71.4	38.1	33.5	969
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	59.0	106.0	5	33.7	59.0	39.8	74.6	38.3	33,9	967
86.0         170.8         5         33.7         186.0         25.0         46.9         35.4         28.6         988.           86.0         170.8         5         33.7         130.0         25.0         46.9         36.2         29.2         966           86.0         170.8         -22         16.9         86.0         16.5         30.8         33.3         26.5         1025           86.0         170.8         -22         16.9         130.0         16.5         30.8         34.1         27.0         1002           104         0 29.7         7         5         33.7         104.0         19.6         36.8         33.4         25.1         1002	59.0		5	33.7	130.0	39.8	74.6	39.8		931
86.0   170.8   5   33.7   130.0   25.0   46.9   36.2   29.2   966 86.0   170.8   -22   16.9   86.0   16.5   30.8   33.3   36.5   1025 86.0   170.8   -22   16.9   130.0   16.5   30.8   34.1   27.0   1002 104   0   29.7   5   33.7   104.0   19.6   36.8   33.4   25.1   1002	59.0	106.0	-23	16.9	59.0	23.4	43.9	36.3	31.5	1000
86.0   170.8   -22   16.9   86.0   16.5   30.8   33.3   26.5   1025   86.0   170.8   -22   16.9   130.0   16.5   30.8   34.1   27.0   1002   104   0   227.7   5   33.7   104.0   19.6   36.8   33.4   25.1   1002	86.0	170.8	5	33.7	86.0	25.0	46.9	35.4	28.6	988
86.0   170.8   -22   16.9   130.0   16.5   30.8   34.1   27.0   1002   104.0   227.7   5   33.7   104.0   19.6   36.8   33.4   25.1   1002	86.0	170.8	99	16 0	150.0			99 9	29.2	
104 0 227.7 5 33.7 104.0 19.6 36.8 33.4 25.1 1002	86.0	170.8	-22 -22				30.8	24.1	27.0	1020
104.0 227.7 -22 16.9 104.0 13.5 25.3 31.4 23.4 1041	104 0			33.7			36.8	33.4	25.1	1002
		227.7	-22	16.9	104.0	13.5	25.3		23.4	1041

The Ammonia Absorption-machine comprises a generator which contains a concentrated solution of ammonia in water; this generator is heated either directly by a fire, or indirectly by pipes leading from a steam-boiler. The condenser communicates with the upper part of the generator by a tube; it is cooled externally by a current of cold water. The cooler or brine-tank is so constructed as to utilize the cold produced; the upper part of it is in communication with the lower part of the condenser.

An absorption-chamber is filled with a weak solution of ammonia: a tube

puts this chamber in communication with the cooling-tank.

The absorption-chamber communicates with the boiler by two tubes; one leads from the bottom of the generator to the top of the chamber, the other leads from the bottom of the chamber to the top of the generator. Upon the latter is mounted a pump, to force the liquid from the absorption chamber, where the pressure is maintained at about one atmosphere, into the generator, where the pressure is from 8 to 12 atmospheres.

To work the apparatus the ammonia solution in the generator is first heated. This releases the gas from the solution, and the pressure rises. When it reaches the tension of the saturated gas at the temperature of the condenser there is a liquefaction of the gas, and also of a small amount of steam. By means of a cock the flow of the liquefied gas into the refrigerating-coils contained in the cooler is regulated. It is here vaporized by absorbing the heat from the substance placed there to be cooled. As fast as it is vaporized it is absorbed by the weak solution in the absorbing-chamber.

Under the influence of the heat in the boiler the solution is unequally sat-

urated, the stronger solution being uppermost.

The weaker portion is conveyed by the pipe entering the top of the absorbing-chamber, the flow being regulated by a cock, while the pump sends an equal quantity of strong solution from the chamber back to the boiler.

<sup>\* 5%</sup> of water entrained in the ammonia will lower the economy of the absorption-machine about 15% to 20% below the figures given in the table.

The working of the apparatus depends upon the adjustment and regulation of the flow of the gas and liquid; by these means the pressure is varied, and consequently the temperature in the cooler may be controlled.

The working is similar to that of compression-machines. The absorptionchamber fills the office of aspirator, and the generator plays the part of

compressor.

The mechanical force producing exhaustion is here replaced by the affinity of water for ammonia gas; and the mechanical force required for compression is replaced by the heat which severs this affinity and sets the gas at

(For discussion of the efficiency of the absorption system, see Ledoux's work; paper by Prof. Linde, and discussion on the same by Prof. Jacobus, Trans. A. S. M. E., xiv. 1416, 1496; and papers by Denton and Jacobus, Trans. A. S. M. E. x. 792; xili, 507.
Sulphur-Dioxide Machines.—Results of theoretical calculations.

Temp, in degrees Fahr.

are given in a table by Ledoux showing an ice-melting capacity per hour per horse-power ranging from 134 to 63 lbs., and per pound of coal ranging from 44.7 to 21.1 lbs., as the temperature corresponding to the pressure of the vapor in the condenser rises from 50 to 104 F. The theoretical results do not represent the actual. It is necessary to take into account the loss occasioned by the pipes, the waste spaces in the cylinder, loss of time in opening of the valves, the leakage around the piston and valves, the reheating by the external air, and finally, when the ice is being made, the quantity of the ice melted in removing the blocks from their moulds. Manufacturers estimate that practically the sulphur-dioxide apparatus using water at 55° or 60° F. produces 56 lbs. of ice, or about 10,000 heat-units, per hour per horse-power, measured on the driving-shaft, which is about 55% of the theoretical useful effect. In the commercial manufacture of ice about 7 lbs. are produced per pound of coal. This includes the fuel used for re-

7 lbs, are produced per pound of coal. This includes the tuel used for re-boiling the water, which, together with that wasted by the pumps and lost oy radiation, amounts to a considerable portion of that used by the engine. Prof. Denton says concerning Ledoux's theoretical results: The figures given are higher than those obtained in practice, because the effect of superheating of the gas during admission to the cylinder is not considered. This superheating may cause an increase of work of about 25%. There are other losses due to superheating the gas at the brine-tank, and in the pipe leading from the brine-tank to the compressor, so that in actual practice a sulphur-dioxide machine, working under the conditions of an absolute pressure in the condenser of 56 lbs. per sq. in, and the corresponding tem-perature of 7° F, will give about 22 lbs. of ice-melting capacity per pound of coal, which is about 60% of the theoretical amount neglecting friction, or 10% including friction. The following tests, selected from those made by Prof. Schröter on a Pictet ice-machine having a compression-cylinder 11.3 in. bore and 24.4 in. stroke, show the relation between the theoretical and

actual ice-melting capacity.

Ice-melting capacity per pound of coal. corresponding to assuming 3 lbs. per hour per H.P. pressure of vapor. No. of Per cent loss due to Test. Theoretical cylinder super-Condenser. Suction. friction Actual. heating, or differincluded.\* ence between cols. 4 and 5. 77.3 28.5 41.3 38.1 19.9 12 76.2 14.4 31.2  $\frac{24.1}{17.5}$ 22.8 13 75.2 -2.523.0 23.9 -15.914 80.6 16.6 10.1 39.2

The Refrigerating Coils of a Pictet ice-machine described by Ledoux had 79 sq. ft. of surface for each 100,000 theoretic negative heat-units produced per hour. The temperature corresponding to the pressure of the dioxide in the coils is 10.4° F., and that of the bath (calcium chloride solution) in which they were immersed is 19 4°.

<sup>\*</sup> Friction taken at figure observed in the test, which ranged from 23% to 26% of the work of the steam-cylinder,

Ammonia Compression-machines.—Ammonia gas possesses the advantage of affording about three times the useful effect of sulphur dioxide for the same volume described by the piston.

The perfection of ammonia apparatus now renders it so convenient and reliable that no practical advantage results from the lower pressures afforded by sulphur dioxide.

The results of the calculations for ammonia are given in the table below:

Gas superheated during compression as in ordinary practice. Temperature of condenser, 64.4° Fahr. Pressure in condenser, PERFORMANCE OF AMMONIA COMPRESSION-MACHINES. 117.44 lbs per sq. in. (Ledoux.)

	-sv	Per T city, of Te	Condensing - water. of Ice-melting Capa suming 30° F. Range perature.	Gals.	1290 1310 1410
	10	per H.P. H.P.	Ice-melting Capacity of Coal, assuming Coal per hour per Steam-cylinder. Wi	Lbs.	39.6 35.6 21.6
	r 9 -si	ty p	Ice - melting Capaci Cubic Foot of Pist placement.	Tons.	.000244 .000221 .000115
-	ance in	Thermal Juits.	Per hour per Horse- power. With Friction.		16,900 15,170 9,230
	Performance	British Thermal Units.	Fer ftlb. of Work of Work With Friction.		.00854
	ent.	of Compression.	With Friction, or power.	Ftlbs.	8130 8190 6990
	Cubic Foot of Piston Displacement	Work of Cc sion	Without Frietion.	Ftlbs.	7070 7120 6080
	of Piston		Number of Nega Thermal Units veloped.	B.T.U.	69.41 62.77 32.58
	Jubic Foot	1s	Condenser.	B.T.U.	78.56 71.98 40.45
	Per (	-wo;	Weight of Gas C pressed.	Lbs.	.1329
	pu	I ts s	Temperature of Ga	Deg. F.	158.9 170.1 241.3
	-93		Absolute Pressure + frigerating-coils.	Lbs. per sq. in.	37.76 33.67 16.95
	-bı	t vap	Temperature Corv ing to Pressure o in Refrigerating	Deg. F.	9.66

Prof. Deuton, and the amount found to agree with that indicated by theory. In these experiments the aumonia circulated in a 75-ton refrigerating machine was measured directly by means of a special meter, so that in addition to determining the effect of The theoretical results for ammonia are higher than the actual, for the same reasons that have been stated for sulphur dioxide. In the case of ammonia the action of the cylinder-walls in superheating the entering vapor has been determined experimentally by superheating, the latent heats can be calculated at the suction and condenser pressure.

Reprigerating Effect of 1 cu. ft. or .13061 le. of Amnonia Exeanded through a Simple Cock to 83.67 les. absolute Pressure per 8q. in., and taken into the Compressor at this Pressure and the Corresponding Temperature of 5º F. Economy of Ammonia Compression-machines at Various Condenser Temperatures. (Ledoux.)

	AMM	IONIA COMPE	ESSI	· M.O.	MA	CHI	N ES.			987
ater.	Ca-	Per Minute per of Ice-melting pacity in 24 ho	Gals.	(6T) (88)	86. 76.	1.08	SSURE	(19) (9)	9.65	1.09
sing-w	-tlən	Per Ton of Ice-r ing Capacity.	Gals.	(18)	1330 1350	1380 1410 1440	PRE PRE	(18)	1,470	1,540
Condensing-water.	-se '	Per cu. ft. of Pi Displacement suming 30° Ra of Temp.	Gals.			.2898 .2904 .2910	ABSOLUTE PRESSURE 5 OF - 22° F.	·		.1649
y.		Per cu. ft. of Pi Displacement	Tons.	(16)	.000219	.000206	TO 16.95 LBS.	.000116	0000114	.000105
Ice-melting Capacity.	Pound Coal.	With Frietion.	Lbs.	39.8	38.4 4.7.	25.0 19.0 19.6		33.4	20.6 18.4 5.4	18.5
Iting C	Per F	Without Fric-	Lbs.			28.83 25.33 25.33	A SIMPLE COCK CORRESPONDING	(14)	25.25	17.1
em-eo	Hour H.P.	With Friction,	Lbs.	(13)	80	75.0 66.1 58.9	SIMPI	.0 .0 .0 .0	85.1.8 8.1.8	44.7
	Per ]	Without Fric-	Lbs.			86.7.6 67.0 7.0 7.0	THROUGH A	£2%	63.3	51.4
ffect is.	I.P., tion.	Fer Hour per I oirf gaibuloai	B.T.U.	(11)	14,250 12,240	10,660 9,400 8,380		9,980	2,840	6,360
Refrigerating Effect in Heat Units.	Jao Jao	Per ftlb. of N Expended, inc ing Friction.	B.T.U.			.00538	EXPANDED PRESSURE	(10)	.00396	.00321
Refrig	nout Jork	Per ftlb. of <i>W</i> Expended, wit Friction,	B.T.U.	(9)	72800.	.00619 .00546 .00486		.00580	.00455	.00369
-tpu	or l	Work of Con with Friction, cated Steam-p	Ftlbs.	(8)	8,660 9,890	11,130 12,360 13,590		(8)	8,000	9,480
, noi	npress	Work of Con Without Fricti	Ftlbs.	6,450	7,530 8,600	9,680 10,750 11,830	FT. OR .06386 LBS. OF A INTO THE COMPRESSOR	(7) 5,680	6,960	8,240 8,870
ged.	rating negari	Ratio of Refrige fect to Heat E				3.4.4 3.22 3.76	FT. OR.	(6)	80 80 9 80 80 4	2.85
αi	тепест	Refrigerating 1 Heat Units.	B.T.U.	(5)	62.31	59.93 58.70 57.45	TAKEN I			30.41 29.75
mor	nsy t	Heat Carried a Condenser.	B.T.U.	T.	22.53	72.46 72.61 72.74	EFFECT OF	2.0	3 4 4	41.07
lo f	uI I	Temperature a Compression,	Deg. F.	(8)	205.1	230.3 255.4 280.3	ING EFF	324.1	252.52	336.2 364.0
-uog	ni ər	Absolute Pressú denser.	Lbs.per sq. in.			170.8 197.8 227.8	REFRIGERATING EFFECT OF 1 CU. PER SQ. IN., AND TAKEN	106.0	135.1	197.8
lo .	Press	Temp. Due to Vapor in Cond	Deg. F.	(E)	85	104	REFR	(1)	8228	10,83

The following is a comparison of the theoretical ice-melting capacity of an ammonia compression machine with that obtained in some of Prof. Schröter's tests on a Linde machine having a compression-cylinder 9.9-in. bore and 16.5 in. stroke, and also in tests by Prof. Denton on a machine having two single-acting compression cylinders 12 in. × 30 in.:

No.	Temp. in I Correspo Pressure	nding to	Ice-melting Capacity per lb. of Coal, assuming 3 lbs per hour per Horse-power.					
of Test.	Condenser.	Suction.	Theoretical, Friction * in- . cluded.	Actual.	Per Cent of Loss Due to Cylinder Superheating.			
Schröter { 2 3 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4	72.3 70.5 69.2 68.5	26.6 14.3 0.5 -11.8	50.4 37.6 29.4 22.8	40.6 30.0 22.0 16.1	19.4 20.2 25.2 29.4			
Denton (24 26 25 25	84.2 82.7 84.6	$^{15.0}_{-3.2}_{-10.8}$	27.4 21.6 18.8	24.2 17.5 14.5	11.7 19.0 22.9			

Refrigerating Machines using Vapor of Water, (Ledoux.)—In these machines, sometimes called vacuum machines, water, at ordinary temperatures, is injected into, or placed in connection with, a chamber in which a strong vacuum is maintained. A portion of the water vaporizes, the heat to cause the vaporization being supplied from the water not vaporized, so that the latter is chilled or frozen to ice. If brine is used instead of pure water, its temperature may be reduced below the freezing-point of water. The water vapor is compressed from, say, a pressure of one tenth of a pound per square inch to one and one half pounds, and discharged into a condenser. It is then condensed and removed by means of an ordinary air-pump. The principle of action of such a machine is the same as that of volatile-vapor machines.

A theoretical calculation for ice-making, assuming a lower temperature of 33° F., a pressure in the condenser of 1½ lbs. per square inch, and a cook consumption of 3 lbs. per LH.P. per hour, gives an ice-melting effect of 34.5 lbs. per pound of coal, neglecting friction. Ammonia for ice-making conditions gives 40.9 lbs. The volume of the compressing cylinder is about 150 times the theoretical volume for an ammonia machine for these conditions.

Relative Efficiency of a Refrigerating Machine.—The efficiency of a refrigerating machine is sometimes expressed as the quotient of the quantity of heat received by the ammonia from the brine, that is, the quantity of useful work done, divided by the heat equivalent of the mechanical work done in the compressor. Thus in column 1 of the table of performance of the 75-ton machine (page 198), the heat given by the brine to the ammonia per minute is 14,776 B.T.U. The horse-power of the ammonia cylinders is 65.7, and its heat equivalent = 65.7 × 33,004 - 778 = 2786 B.T.U. The difference of the ammonia cylinders are some summan of the summan of the efficiency is greater than unity, which is impossible in any machine, is thus explained. The working fluid, as ammonia, receives heat from the brine and rejects heat into the condenser. (If the compressor is jacketed, a portion is rejected into the jacket-water.) The heat rejected into the condenser is greater than that received from the brine; the difference (plus or minus a small difference radiated to or from the atmosphere) is heat received by the ammonia from the compressor. The work to be done by the compressor is not the mechanical equivalent of the refrigeration of the brine, but only that necessary to supply the difference between the heat rejected by the ammonia into the condenser and that received from the brine. If cooling water colder than the brine were available, the brine might transfer its heat directly into the conjugaters, and there would be no need of ammonia or of a compressor; but

<sup>\*</sup> Friction taken at figures observed in the tests, which range from 14% to 20% of the work of the steam-cylinder.

since such cold water is not available, the brine rejects its heat into the colder ammonia, and then the compressor is required to heat the ammonia to such a temperature that it may reject be the colling water.

to such a temperature that it may reject heat into the cooling water.

The efficiency of a refrigerating plant referred to the amount of fuel consumed is

The ice-melting capacity is expressed as follows:

Tons (of 2000 lbs.) ice-melting capacity per 24 hours  $= \frac{\begin{cases} 24 \times \text{pounds} \\ \times \text{ specific heat} \\ \times \text{ range of temp.} \end{cases}$  of brine circulated per hour.

The analogy between a heat-engine and a refrigerating-machine is as follows: A steam-engine receives heat from the boiler, converts a part of it into mechanical work in the cylinder, and throws away the difference into the condenser. The ammonia in a compression refrigerating machine receives heat from the brine-tank or cold-room, receives an additional amount of heat from the mechanical work done in the compression-cylinder, and throws away the sum into the condenser. The efficiency of the steam-engine work done + heat received from boiler. The efficiency of the refrigerating-machine = heat received from the brine-tank or cold-room + heat required to produce the work in the compression-cylinder. In the ammonia

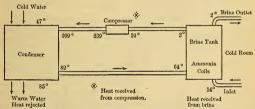


DIAGRAM OF AMMONIA COMPRESSION MACHINE.

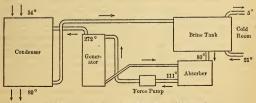


DIAGRAM OF AMMONIA ABSORPTION MACHINE.

absorption-apparatus, the ammonia receives heat from the brine-tank and additional heat from the boiler or generator, and rejects the sum into the condenser and into the cooling water supplied to the absorber. The efficiency = heat received from the brine +- heat received from the boiler,

## TEST-TRIALS OF REFRIGERATING-MACHINES.

(G. Linde, Trans. A. S. M. E., xiv. 1414.)

The purpose of the test is to determine the ratio of consumption and production, so that there will have to be measured both the refrigerative effect and the heat (or mechanical work) consumed, also the cooling water. The refrigerative effect is the product of the number of heat-units (Q) abstracted

from the body to be cooled, and the quotient  $\frac{T_0 - T}{T}$ ; in which  $T_0 =$  absolute terms (Q) abstracted

lute temperature at which heat is transmitted to the cooling water, and T =absolute temperature at which heat is taken from the body to be cooled.

The determination of the quantity of cold will be possible with the proper exactness only when the machine is employed during the test to refrigerate a liquid; and if the cold be found from the quantity of liquid circulated per unit of time, from its range of refrigeration, and from its specific heat. Sufficient exactness cannot be obtained by the refrigeration of a current of circulating air, nor from the manufacture of a certain quantity of ice, nor from a calculation of the fluid circulating within the machine (for instance, the quantity of ammonia circulated by the compressor). Thus the refrigeration of brine will generally form the basis for tests making any pretension to accuracy. The degree of refrigeration should not be greater than necessary for allowing the range of temperature to be measured with the necessary exactness; a range of temperature of from to to 6° Fahr, will suffice. The condenser measurements for cooling water and its temperatures will

be possible with sufficient accuracy only with submerged condensers. The measurement of the quantity of brine circulated, and of the cooling water, is usually effected by water-meters inserted into the conduits. If the necessary precautions are observed, this method is admissible. For quite

precise tests, however, the use of two accurately gauged tanks must be advised, which are alternately filled and emptied.

To measure the temperatures of brine and cooling water at the entrance and exit of refrigerator and condenser respectively, the employment of specially constructed and frequently standardized thermometers is indispensable; no less important is the precaution of using at each spot simultaneously two thermometers, and of changing the position of one such thermometer series from inlet to outlet (and vice versa) after the expiration of one half of the test, in order that possible errors may be compensated.

It is important to determine the specific heat of the brine used in each instance for its corresponding temperature range, as small differences in the composition and the concentration may cause considerable variations.

As regards the measurement of consumption, the programme will not have any special rules in cases where only the measurement of steam and cooling water is undertaken, as will be mainly the case for trials of absorption-ma-chines. For compression-machines the steam consumption depends both on the quality of the steam-engine and on that of the refrigerating-machine, while it is evidently desirable to know the consumption of the former separately from that of the latter. As a rule steam-engine and compressor are coupled directly together, thus rendering a direct measurement of the power absorbed by the refrigerating-machine impossible, and it will have to suffice to ascertain the indicated work both of steam-engine and compressor. By further measuring the work for the engine running empty, and by comparing the differences in power between steam-engine and compressor resulting ing the differences in power between steam-engine and compressor resulting for wide variations of condenser-pressures, the effective consumption of work Le for the refrigerating-machine can be found very closely. In general, it will suffice to use the indicated work found in the steam-cylinder, especially as from this observation the expenditure of heat can be directly determined. Ordinarily the use of the indicated work in the compressor-cylinder, for purposes of comparison, should be avoided; firstly, because there are usually certain accessory apparatus to be driven (agitators, etc.), belonging to the refrigerating-machine proper; and secondly, because the external friction would be excluded.

Heat Balance.—We possess an important aid for checking the correctness of the results found in each trial by forming the balance in each case for the heat received and rejected. Only such tests should be regarded as correct beyond doubt which show a sufficient conformity in the heat balance. It is true that in certain instances it may not be easy to account fully for the transmission of heat between the several parts of the machine and its environment by radiation and convection, but generally (particularly for compression machines) it will be possible to obtain for the heat received and rejected a balance exhibiting small discrepancies only.

neat received and rejected a balance exhibiting small discrepancies only.

Report of Test.—Reports intended to be used for comparison with
the figures found for other machines will therefore have to embrace at least
the following observations:

 $\begin{tabular}{ll} Refrigerator: & Quantity of brine circulated per hour. & Quantity of brine circulated per hour. & Brine temperature at inlet to refrigerator. & Brine temperature at outlet of refrigerator. & t Specific gravity of brine (at <math>64^\circ$  Fahr.) & Specific heat of brine & Heat abstracted (cold produced). & Qe Absolute pressure in the refrigerator. & Condenser: & Quantity of cooling water per hour & Qe Absolute pressure & Condenser & Condense & Condense

 $\begin{array}{c} \textit{Condenser}: \\ \textit{Quantity of cooling water per hour} \\ \textit{Temperature at inlet to condenser}. \\ \textit{Temperature at outlet of condenser}. \\ \textit{Hoat abstracted}. \\ \textit{Absolute pressure in the condenser}. \\ \textit{Q}_1 \\ \textit{Absolute pressure in the condenser}. \\ \textit{Q}_1 \\ \textit{Temperature of gases entering the condenser}. \\ \end{array}$ 

Temperature at outlet of condenser.
Heat abstracted.
Absolute pressure in the condenser.
Temperature of gases entering the condenser.

ABSORPTION-MACHINE.

Still :

Steam consumed per hour.

Abs. pressure of heating steam.
Temperature of condensed steam at outlet.
Heat imparted to still.

Absorber :

Quantity of cooling water per hour.

Temperature at inlet.

Temperature at outlet.
Heat removed.

Quantity for Ammonia Liquor :
Indicated work of steam-engine Steam-consumption for pump.
Thermal equivalent for work of pump.
Total sum of losses by radiation

and convection ..... ± Q3

Heat Balance:

# COMPRESSION-MACHINE.

Condensing water per hour...

Temperature of da...

Total sum of losses by radiation and convection...  $\pm Q_3$ Heat Balance:  $Qe + ALc = Q_1 \pm Q_3$ .

 $Qe + Q'e = Q_1 + Q_2 \pm Q_3$ . For the calculation of efficiency and for comparison of various tests, the actual efficiencies must be compared with the theoretical maximum of efficiency  $\left(\frac{Q}{4L}\right)$  max. =  $\frac{T}{T_0 - T}$  corresponding to the temperature range.

Temperature Range. — As temperatures (T and Tc) at which the heat is abstracted in the refrigerator and imparted to the condenser, it is correct to select the temperature of the brine leaving the refrigerator and that of the cooling water leaving the condenser, because it is in principle impossible to keep the refrigerator pressure higher than would correspond to the lowest brine temperature, or to reduce the condenser pressure below that corresponding to the outlet temperature of the cooling water.

Prof. Linde shows that the maximum theoretical efficiency of a compression-machine may be expressed by the formula

$$\frac{Q}{AL} = \frac{T}{T_c - T},$$

in which Q = quantity of heat abstracted (cold produced); AL = thermal equivalent of the mechanical work expended;

L = the mechanical work, and A = 1 + 778;
T = absolute temperature of heat abstraction (refrigerator);
T = """ rejection (condenser)

Tc = " " rejection (condenser). If u = ratio between the heat equivalent of the mechanical work AL, and the quantity of heat Q' which must be imparted to the motor to produce the work L, then

$$\frac{AL}{Q'}=u, \text{ and } \frac{Q'}{Q}=\frac{Tc-T}{uT}.$$

It follows that the expenditure of heat Q' necessary for the production of the quantity of cold Q in a compression-machine will be the smaller, the smaller the difference of temperature  $T_{c}-T$ .

Metering the Ammonia.—For a complete test of an ammonia refrigerating-machine it is advisable to measure the quantity of ammonia circulated, as was done in the test of the 75-ton machine described by Prof. Denton. (Trans. A. S. M. E., xii. 336.)

# PROPERTIES OF SULPHUR DIOXIDE AND AMMONIA GAS.

Ledoux's Table for Saturated Sulphur-dioxide Gas.
Heat-units expressed in B.T.U. per pound of sulphur dioxide.

Heat-units expressed in B.1.C. per pound of surphur dioxide.											
Temperature of Ebullition in deg. F.	Absolute Pressure in lbs. per sq. in. $P + 144$	Total Heat reckoned from 32° F.	Heat of Liquid reckoned from 32° F.	Latent Heat of Evaporation	Heat Equiva- lent of Exter- nal Work.	Internal Latent Heat.	Increase of Volume during Evaporation.	Density of Vapor or Weight of 1 cu. ft. $1 + v$			
Deg. F.	Lbs.	B.T.U.	B.T.U.	B.T.U.	B.T.U.	B.T.U.	Cu. ft.	Lbs.			
-22	5.56	157.43	-19.56	176.99	13.59	163.39	13.17	.076			
-13	7.23	158.64	-16.30	174,95	13.83	161.12	10.27	.097			
_ 4	9.27	159,84	-13.05	172.89	14.05	158.84	8.12	.123			
- 4 5	11.76	161.03	- 9.79	170.82	14.26	156.56	6.50	.153			
14 23	14.74	162,20	-6.53	168.73	14.46	154.27	5.25	.190			
23	18.31	163.36	- 3.27	166.63	14.66	151.97	4.29	.232			
32	22.53	164.51	0.00	164.51	14.84	149.68	3.54	.282			
41	27.48	165.65	3.27	162.38	15.01	147.37	2.93	.340			
50	33.25	166.78	6.55	160.23	15.17	145.06	2.45	.407			
59	39,93	167.90	9.83	158,07	15.32	142.75	2.07	.483			
68	47.61	168.99	13.11	155.89	15.46	140.43	1.75	.570			
77	56.39	170.09	16.39	153.70	15.59	138.11	1.49	.669			
86	66.36	171.17	19.69	151.49	15.71	135.78	1.27	.780			
95	77.64	172.24	22.98	149.26	15.82	133.45	1.09	.906			
104	90.31	173.30	26.28	147.02	15.91	131.11	.91	1.046			

Density of Liquid Ammonia. (D'Andreff, Trans. A. S. M. E., x. 641.)

These may be expressed very nearly by

$$\delta = 0.6364 - 0.0014t^{\circ}$$
 Centigrade;

 $\delta = 0.6502 - 0.000777T^{\circ}$  Fahr.

Latent Heat of Evaporation of Ammonia. (Wood, Trans. A. S. M. E., x. 641.)

 $he = 555.5 - 0.613T - 0.000219T^2$  (in B.T.U., Fahr. deg.); Ledoux found  $he = 583.33 - 0.5499T - 0.0001173T^2$ .

For experimental values at different temperatures determined by Prof. Denton, see Trans. A. S. M. E., xii. 356. For calculated values, see

vol. x. 646.

Density of Ammonia Gas.—Theoretical, 0.5894; experimental, 0.596. Regnault (Trans. A. S. M. E., x. 633).

0.596. Regnant (Trans. A. S. M. E., x. 038). Specific Heat of Liquid Ammonia. (Wood, Trans. A. S. M. E., x. 645)—The specific heat is nearly constant at different temperatures, and about equal to that of water, or unity. From  $0^{\circ}$  to  $100^{\circ}$  F, it is

c = 1.096 - .0012T, nearly.

In a later paper by Prof. Wood (Trans. A. S. M. E., xii. 136) he gives a higher value, viz., c = 1.13136 + 0.000438T.

Dr. Von Strombeck, in 1890, found from the mean of eight experiments, at a temperature about 80° F., c = 1.22876,—about 6% greater than that cal-

culated from this formula.

In Prof. Wood's Thermodynamics (edition of 1894) in addition to the above figures he gives the mean of six determinations by Ludeking and Starr, 0.886. This, says Prof. Wood, leaves the correct result in doub, and one may consider it as unity until determined by further experiments.

## Properties of the Saturated Vapor of Ammonia.

(Wood's Thermodynamics.)

Degs.   Abso   Lbs.per	Tempe	rature.	Pres Abso	sure, dute.	Heat of Vaporiza-	Volume of Vapor	Volume of Liquid	Weight of a cu.
F. lute, F. sq. ft. sq. fn.   10.69   579.67   24.372   0.234   0.410   0.69   359.66   173.6   12.31   576.69   21.319   0.236   0.462   0.358.8   14.13   573.69   18.097   0.237   0.635   0.308.8   14.13   573.69   18.097   0.238   0.685   0.308.8   14.13   573.69   18.097   0.238   0.685   0.308.8   14.13   573.69   18.097   0.238   0.685   0.308.8	Dece	A hea-	Lhe ner	Lhe ner	tion, ther-	per lb.,	per lb.,	
	F.				mal units.	cu. It.	cu. ft.	
- 30						24.372		
- 25 435.66 2829.5 16.17 570.68 16.445 0.288 0.008   - 20 440.66 2657.5 18.45 567.67 14.507 0.240 0.089   - 15 445.66 3022.5 20.99 564.64 12.834 0.242 0.779   - 5 455.66 8877.2 26.93 554.64 12.834 0.243 0.787   - 5 455.66 8877.2 26.93 558.56 10.125 0.244 0.988   - 4 60.66 4373.5 30.37 555.50 9.027 0.246 10.88   + 5 466.66 4920.5 34.17 552.43 8.099 0.247 1.239   + 10 470.66 5522 3.834 549.35 7.229 0.249 1383   + 15 475.66 6182.4 42.93 546.26 6.492 0.250 1.544   - 20 480.66 6053 47.95 513.15 5.842 0.252 1.742   - 25 485.66 7695.2 53.43 540.03 5.269 0.253 1.898   - 35 495.66 7695.2 53.43 540.03 5.269 0.253 1.898   - 35 495.66 594.1 556.92 4.763 0.254 1.290   - 35 495.66 594.1 585.92 4.763 0.254 1.290   - 35 495.66 59.41 58.95 530.83 3.914 0.257 2.555   - 45 505.66 161616 80.66 57.47 3.559 0.259 1.200   - 55 515.66 14102 97.43 524.30 3.42 0.266 0.267 2.308   - 55 515.66 1693 118.03 524.12 2.988 0.243 3.381   - 70 530.66 1594 107.60 517.33 2.476 0.266 3.098   - 65 525.66 1693 118.03 524.12 2.988 0.243 3.381   - 70 530.66 180.57 1.29 1.54 1.10 0.265 3.698   - 85 545.66 2630 118.9 1.51 15.5 0.271 0.206 3.098   - 85 545.66 2830 118.9 1.51 15.5 0.271 0.207 2.272 5.098   - 85 545.66 2830 18.9 1.2 15.15 0.277 0.265 3.698   - 85 545.66 2830 118.9 1.51 15.5 0.271 0.207 2.274 6.288   - 85 545.66 2836 144.25 508.29 2.087 0.270 4.763   - 80 540.66 2292 15.4 11 10.50 0.5 1.990 0.272 5.098   - 85 545.66 2830 18.8 8.77 495.29 1.510 0.277 6.623   - 85 545.66 2830 18.8 8.77 495.29 1.510 0.277 6.623   - 80 540.66 2926 385.16 488.75 1.199 0.272 5.008   - 85 545.66 6.2506 18.9 14.9 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0 1.0								
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- 5 455.66 8877.2 26.93 558.56 10.125 0.244 .0988 0.466.66 4970.5 34.17 552.43 8.099 0.247 1239			3022.5	20.99		12.834		
0 460.66 4920.5 34.17 555.50 9.027 .0.246 .1108  + 5 466.66 4920.5 34.17 555.50 9.027 .0.247 .1239  + 10 470.66 5522.2 38.34 549.35 7.229 .0.249 .1388  + 20 480.66 6905.3 47.55 543.15 5.842 .0.250 .1584  + 20 480.66 6905.3 47.55 543.15 5.842 .0.252 .1712  + 25 485.66 7696.2 53.43 540.03 5.269 .0.253 .1892  + 30 490.66 8556.6 594.1 536.92 4.763 .0.254 .2100  + 35 495.66 9499.9 65.93 583.78 4.133 .0.256 .2319  + 40 500.66 10512 73.00 530.63 3.914 .0.257 .2.255  - 50 510.66 12811 88.96 524.30 3.242 .0.261 .3.2085  - 50 510.66 12811 88.96 524.30 3.242 .0.261 .3.2085  - 50 510.66 15494 107.60 517.33 2.704 .0.265 .3.3881  - 60 520.66 15494 107.60 517.33 2.704 .0.265 .3.3881  - 60 520.66 15494 107.60 517.33 2.704 .0.265 .3.3881  - 70 530.66 18005 129.21 511.152 2.271 .0.208 .4403  - 80 540.66 22492 134.11 505.89 .0.270 .4703 .3.484  - 80 540.66 22492 134.11 505.89 .0.270 .0.270 .4703  - 80 540.66 2380 182.3 498.11 1.682 .0.274 .0.273 .5.208  - 90 350.66 28365 199.4 488.29 1.128 .0.370 .0.271 .6.388  - 90 350.66 28365 199.4 488.29 1.128 .0.370 .0.272 .5.208  - 90 350.66 28365 199.4 488.29 1.1.288 .0.270 .0.271 .6.388  - 10 566.66 38360 32.44 488.79 1.1.388 .0.279 .0.271 .6.388  - 10 566.66 38360 32.44 488.79 1.1.388 .0.279 .0.271 .6.388  - 110 576.66 28365 199.4 488.29 1.1.388 .0.29 .0.274 .0.288 .812  - 115 576.66 39188 .272.44 488.79 1.1.388 .0.29 .0.274 .0.288 .812  - 115 576.66 39188 .272.44 488.79 1.1.393 .0.287 .0.287 .0.279 .4.388  - 110 576.66 3888 .272.44 488.79 1.1.393 .0.288 .812  - 115 576.66 39188 .272.44 488.75 1.1.393 .0.287 .0.289 1.1.390  - 120 586.66 63508 .386.14 488.75 0.1.485 .0.299 1.0.399  - 120 586.66 63508 .386.14 487.74 5.0.970 .0.289 1.1.394  - 120 586.66 63508 .392.24 488.75 0.791 .0.285 .8.371  - 120 586.66 63508 .392.44 488.75 0.791 .0.285 .8391  - 120 586.66 63508 .392.44 488.75 0.791 .0.285 .8.391  - 120 586.66 63508 .392.44 488.75 0.791 .0.285 .8.391  - 120 586.66 63508 .392.44 488.75 0.791 .0.285 .8.391  - 120 586.66 6366 6366 .392.66 385.16 488.75 0.791 .0.295 .0.291 1.1.049  - 120 5								
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29         490,66         6905.3         47.55         543,15         5.842         .0252         17128           -85         485.66         7694,25         53,43         540,03         5.269         .0253         11898           -80         490,66         8556.6         59,41         536,92         4,763         .0256         2319           -40         500,66         19151         73.00         530,63         3,914         .0257         .255           -45         505,66         11616         80,66         524,430         3,242         .0261         .3085           -50         510,66         12811         88,96         524,30         3,242         .0261         .3085           -60         520,66         15194         107.60         517,33         2,704         .0265         .3698           -70         530,66         1805         129,21         511,73         2,476         .0266         .3698           -65         525,66         1693         118,03         514,73         2,476         .0266         .3698           -70         530,66         18005         129,21         511,52         2,271         .0268         .4403	T 15							
- 80 990.00 850.0 949.9 65.33 653.78 4.763 .0234 .2100 .2266 .23319 .40 500.66 10512 73.00 850.63 3.914 .0257 .2555 .255 .255 .255 .255 .255 .255	I 20			47.95				
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+ 35         495.66         9493.9         65.33         533.78         4.313         .0256         .2355           + 40         500.66         1616         80.66         527.47         3.59         .0257         .2555           + 55         505.66         11616         80.66         527.47         3.599         .0261         .3085           + 55         515.66         14102         97.43         524.30         3.242         .0261         .3085           + 60         520.66         15194         107.60         517.93         2.704         .0265         .3689           + 65         525.66         16993         118.03         514.73         2.476         .0268         .403           + 70         530.66         20336         141.25         508.29         2.087         .0270         .4703           + 80         546.66         2217         1.050         50         .2271         .0268         .403           + 85         545.66         28965         198.13         1.170         .0272         .5298           + 85         545.66         28656         198.37         495.29         1.510         .0274         .6128           + 95	+ 30			59.41	536.92	4.763		.2100
4 5         505.66         11616         80.66         527.47         3.559         0.259         2809           5 5         515.66         14102         97.43         524.12         2.988         0.263         3385           - 60         520.66         1549         107.60         511.12         2.988         0.263         33881           - 65         525.66         16993         118.03         514.73         2.476         0.266         4093           - 70         530.66         1805         129.21         511.52         2.271         0.268         403           - 75         535.66         20.36         141.25         508.29         2.087         0.270         2508           - 80         540.66         2219         154.11         505.05         1.920         0.272         5298           - 85         545.66         2478         167.86         501.81         1.770         0.0272         5298           - 85         545.66         28565         198.37         495.29         1.510         0.274         6128           - 95         555.66         28565         198.37         495.29         1.510         0.277         6623	+ 35				533.78			
-50         510.66         12811         88.96         524.80         3.242         .0261         .3085           -55         515.66         14102         97.193         521.12         2.988         .0263         .3381           -60         520.66         15194         107.60         517.93         2.704         .0265         .3698           -70         530.66         18005         129.21         511.52         2.971         .0268         .4089           -70         530.66         18005         129.21         511.52         2.971         .0268         .4408           -80         540.66         22192         154.11         .505.05         1.920         .0272         .5208           -90         550.66         23636         188.81         187.80         .1770         .0273         .5650           -90         550.66         23656         198.37         .495.39         .1072         .0274         .6182           -90         550.66         23656         198.37         .495.39         .1072         .0277         .6183           -100         560.66         30808         215.14         .492.01         1.3388         .0279         .7183	+ 40		10512	73.00	530.63	3.914	.0257	.2555
-55         515.66         14102         97.43         521.12         2.958         .0263         .3381           -60         520.66         15494         107.60         517.93         2.704         .0265         .3698           -65         525.66         16993         118.03         514.73         2.476         .0268         .403           -70         530.66         18005         129.21         511.52         2.271         .0268         .403           -85         546.66         2219         154.11         505.05         1.920         .0272         .508           -85         546.66         2217         1.505         .05         1.990         .0272         .508           -80         546.66         2219         154.11         .050         .05         1.990         .0272         .508           -80         546.66         2219         18.81         1.770         .0273         .5650           -80         555.66         28565         198.37         .495.19         1.510         .0274         .6128           -95         555.66         28565         198.37         .495.29         1.510         .0279         .7153           -	+ 45							
- 60 520,66 15494 107.60 517.93 2.704 .0.265 .3698 .765 525,66 16993 118.03 514.73 2.476 .0.265 .3698 .770 530,66 18005 129.21 514.73 2.476 .0.266 .4039 .775 535,66 20.36 141.25 050.829 2.087 .0.270 .4793 .80 540,66 22192 154.11 .505.05 1.1.920 .0.272 .5208 .85 545,66 24378 167.86 501.81 1.770 .0.273 .5208 .99 0.50.66 28300 182.8 498.11 1.632 .0.274 .6128 .90 550.66 28306 188.3 498.11 1.632 .0.274 .6128 .90 550.66 28306 182.3 498.11 1.632 .0.274 .6128 .90 550.66 28306 283.8 498.11 1.632 .0.274 .6128 .91 0.00 560.66 30.986 215.14 492.01 1.338 .0.279 .7153 .91 0.00 560.66 30.986 215.14 492.01 1.338 .0.279 .7153 .91 0.00 560.66 30.986 215.14 492.01 1.338 .0.279 .7153 .91 0.00 560.66 30.986 215.14 492.01 1.396 .0.281 .7716 .91 0.00 560.66 30.986 251.04 485.44 1.206 .0.281 .7716 .91 0.00 560.66 30.986 251.04 485.44 1.206 .0.281 .7716 .91 0.00 560.66 30.986 251.04 485.44 1.206 .0.281 .7716 .91 0.00 560.66 30.986 251.04 485.44 1.206 .0.281 .7716 .91 0.00 560.66 30.986 251.04 485.44 1.206 .0.291 1.1040 .91 0.00 560.66 30.986 30.51 0.4875.45 1.0.970 .0.291 1.1040 .91 0.00 560.66 30.986 30.51 0.4875.45 1.0.970 .0.291 1.1040 .91 0.00 560.66 30.00 0.00 0.00 0.00 0.00 0.00 0.0	+ 50				524.80			
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+ 70	T 65			118 03	511.73			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$					511.52			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$		585.66	20336	141.25	508.29	2.087	.0270	
-90         550.66         26300         182.8         498.11         1.632         .0274         .6128           -95         55.56         28565         198.37         495.29         1.510         .0277         .6823           -100         566.66         30986         215.14         492.01         1.398         .0279         .7153           -105         566.66         38250         392.98         488.72         1.296         .0281         .7716           -110         570.66         392.84         251.07         485.42         1.293         .0283         .8312           +120         580.66         42267         293.49         478.79         1.045         .0287         .8937           +125         585.66         45328         316.16         475.45         0.970         .0289         1.0393           +135         505.66         52026         365.16         468.75         0.815         .0291         1.1049           +135         505.66         56236         365.16         465.39         0.791         .0295         1.2642           +136         605.66         60550         420.49         462.01         0.741         .0297         1.3495	+ 80					1.920		
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 85							
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 120				478.79			
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$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 135				468.75			
$\begin{array}{cccccccccccccccccccccccccccccccccccc$	+ 140							
+ 155   615.66   69341   481.54   455.22   0.652   .0302   1.5337 + 160   620.66   74086   514.40   451.81   0.618   .0304   1.6343	T 150							
+ 160   620.66   74086   514.40   451.81   0.618   .0304   1.6348	+ 155							
	+ 160	620.66			451.81	0.613	.0304	1.6343
+ 100   025.00   79071   549.04   448.39   0.577   .0500   1.7338	+ 165	625.66	79071	549.04	448.39	0.577	.0306	1.7333

Specific Heat of Ammonia Vapor at the Saturation Point. (Wood, Trans. A. S. M.; E., x. 644.)—For the range of temperatures ordinarily used in engineeering practice, the specific heat of saturated amounts of the saturation o nonia is negative, and the saturated vapor will condense with adiabatic expansion, and the liquid will evaporate with the compression of the vapor, and when all is vaporized will superheat.

Regnault (Rel. des. Exp., ii. 162) gives for specific heat of ammonia-gas 0.50836. (Wood, Trans, A. S. M. E., xii. 133.)

Properties of Brine used to absorb Refrigerating Effect of Ammonia. (J. E. Denton, Trans. A. S. M. E., x. 499.)—A solution of Liverpool salt in well-water having a specific gravity of 1.17, or a weight per cubic foot of 73 lbs., will not sensibly thicken or congeal at 0° Fahrenheit. (It is reported that brine of 1.17 gravity, made with American salt, begins to conceal at about 24° Fahr.)

The mean specific heat between 39° and 16° Fahr, was found by Denton to be 0.805. Brine of the same specific gravity has a specific heat of 0.805 at

65° Fahr., according to Naumann.

Naumann's values are as follows (Lehr-und Handbuch der Thermochemie, 1882):

Chloride-of-calcium solution has been used instead of brine. According to Naumann, a solution of 1.0255 sp. gr. has a specific heat of .957. A solution of 1.163 sp. gr. in the test reported in Eng'g, July 22, 1887, gave a specific heat of .827.

# ACTUAL PERFORMANCES OF ICE-MAKING MACHINES.

The table given on page 996 is abridged from Denton, Jacobus, and Riesenberger's translation of Ledoux on Ice-making Machines. The following shows the class and size of the machines tested, referred to by letters in the table, with the names of the authorities:

Class of Machines.	Authority,	Dimensions of Compression-cylinder in inches.			
		Bore.	Stroke.		
A. Ammonia cold-compression. B. Pictet fluid dry-compression. C. Bell-Coleman air D. Closed cycle air E. Ammonia dry-compression. F. Ammonia absorption	" " " " " " " " " " " " " " " " " " "	9.9 11.3 28.0 10. 12.0	16.5 24.4 23.8 18.0 30.0		

**Performance of a 75-ton Ammonia Compression-machine**, (J. E. Denton, Trans. A. S. M. E., xii, 326.)—The machine had two single-acting compression cylinders  $12^{\nu} \times 30^{\nu}$ , and one Corliss steam-cylinder, double-acting,  $18^{\nu} \times 36^{\nu}$ . It was rated by the manufacturers as a 50-ton machine, but it showed 75 tons of ice-refrigerating effect per 24 hours during the test.

The most probable figures of performance in eight trials are as follows:

of Trial.	Amm Pressu Ibs. at Atmosp	ove	Ten	rine npera- ires, rees F.	sity Tons rigerating of per 24 rs.	per lb. of lat 3 lbs. l per hour l per hour H.P.	consump- gals. of erpermin. ton of Ca-	of Actual ights of monia cir-	of Capac-
o.	Con- densing	Suc-	Inlet.	Outlet.	Capac Refi Effe hou	Efficie Coa Coa per	Water tion Wat per paci	Ratio W e Ami	Ratio
1	151	28	36.76	28.86	70.3	22,60	0.80	1.0	1.0
8	161	27.5	36.36		70.1	22.27	1.09	1.0	1.0
7	147	13.0	14.29		42.0	16.27	0.83	1.70	1.66
4	152	8.2	6.27		36.43	14.10	1.1	1.93	1.92
6	105	7.6	6.40	-2.22	37.20	17.00	2.00	1.91	1.88
2	135	15 7	4 62	3 22	27.2	13.20	1.25	2.59	2.57

The principal results in four tests are given in the table on page 998. The fuel economy under different conditions of operation is shown in the following table:

-SSS-	ıre,	Pour	Pounds of Ice-melting Effect with Engines—						B.T.U. per lb. of Steam with Engines—			
Condensing Press- ure, lbs. Suction-pressure,		Per lb. Coal. Steam.		pound	Per lb. Coal. Steam. Steam.		Compound Coal.  Per lb. Steam. Steam.		Condensing.	Compound Condensing.		
150 150 105 105	28 7 28 7	24 14 34.5 22	2.90 1.69 4.16 2.65	30 17.5 43 27.5	3.61 2.11 5.18 3.31	37.5 21.5 54 34.5	4.51 2.58 6.50 4.16	393 240 591 376	513 300 725 470	640 366 928 591		

The non-condensing engine is assumed to require 25 lbs, of steam per horse-power per hour, the non-compound condensing 20 lbs., and the comdensing 16 lbs., and the boiler efficiency is assumed at 8.3 lbs. of water per lb. coal under working conditions. The following conclusions were derived

from the investigation:

1. The capacity of the machine is proportional, almost entirely, to the weight of ammonia circulated. This weight depends on the suction-pressure and the displacement of the compressor-pumps. The practical suction-pressures range from 7 lbs. above the atmosphere, with which a temperature of 0° F. can be produced, to 28 lbs. above the atmosphere, with which the temperatures of refrigeration are confined to about 28° F. At the lower pressure only about one half as much weight of ammonia can be circulated as at the upper pressure, the proportion being about in accordance with the ratios of the absolute pressures, 22 and 42 lbs. respectively. For each with the ratios of the assolute pressures, 22 and 42 tos. Respectively. For each cubic foot of piston-displacement per minute a capacity of about one sixth of a ton of "refrigerating effect" per 24 hours can be produced at the lower pressure, and of about one third of a ton at the upper pressure. No other elements practically affect the capacity of a machine, provided the cooling surface in the brine-tank or other space to be cooled is equal to about 36 sq. 16, per ton of capacity at 28 lbs. back pressure. For example, a difference of 100% in the rate of circulation of brine, while producing a proportion tional difference in the range of temperature of the latter, made no practical difference in capacity.

The brine-tank was  $104 \times 13 \times 1936$  ft., and contained 8000 lineal feet of 1-in. pipe as cooling-surface. The condensing-tank was  $12 \times 10 \times 10$  ft., and contained 5000 lineal feet of 1-in. pipe as cooling-surface.

2. The economy in coal-consumption depends mainly upon both the suc-on-pressures and condensing-pressures. Maximum economy, with a given tion-pressures and condensing pressures. Maximum economy, with a given type of engine, where water must be bought at average city prices, is obtained at 28 lbs. suction-pressure and about 150 lbs. condensing pressure. Under these conditions, for a non-condensing steam-engine, consuming coal at the rate of 3 lbs, per hour per I.H.P. of steam-cylinders, 24 lbs, of ice-refrigerating effect are obtained per lb. of coal consumed. For the same condensing pressure, and with 7 lbs. suction-pressure, which affords temperatures of 0° F., the possible economy falls to about 14 lbs. of "refrigerating effect" per lb. of coal consumed. The condensing-pressure is determined by the amount of condensing-water supplied to liquefy the ammonia in the condenser. If the latter is about 1 gallon per minute per ton of refrigerating effect per 24 hours, a condensing-pressure of 150 lbs. results, if the initial temperature of the water is about 56° F. Twenty-five per cent less water causes the condensing-pressure to increase to 190 lbs. The work of compression is thereby increased about 20g, and the resulting "economy" is reduced to about 18 lbs, of "ice effect" per lb, of coal at 28 lbs, suction-pressure and 11.5 at 7 lbs. If, on the other hand, the supply of water is made 3 gallons per winter the condensity the condensity of the conden per minute, the condensing-pressure may be confined to about 105 lbs. The work of compression is thereby reduced about 25% and a proportional increase of economy results. Minor alterations of economy depend on the initial temperature of the condensing-water and variations of latent heat, but these are confined within about 5% of the gross result, the main element of control being the work of compression, as affected by the back pressure and con-densing-pressure, or both. If the steam engine supplying the motive power may use a condenser to secure a vacuum, an increase of economy of 25% is available over the above figures, making the bls of "ice effect" per lb. of coal for 150 lbs, condensing-pressure and 28 lbs, suction-pressure 30.0, and for 7 lbs, suction-pressure, 17.5. It is, however, impracticable to use a condenser in cities where water is bought. The latter must be practically free of cost to be available for this purpose. In this case it may be assumed free of cost to be available for this purpose. In this case it may be assumed that water will also be available for condensing the ammonia to obtain as low a condensing-pressure as about 100 lbs., and the economy of the refrigerating-machine becomes, for 28 lbs. back pressure, 43.0 lbs. of "ice effect" per lb. of coal, for for 7 lbs. back-pressure, 27.5 lbs. of ice effect per lb. of coal, for a compound condensing-engine can be used with a steam-consumption per hour per horse-power of 16 lbs. of water, the economy of the refrigerating-machine may be 28% higher than the figures last named, making for 28 lbs. back pressure a refrigerating effect of 34.0 lbs. per lb. of coal, and for 7 lbs. back pressure a refrigerating effect of 34.0 lbs. per lb. of coal.

		Act	tual	P	erfor	ma	nce	of	Ice	-ma	kir	ng M	achin	es.			
		Absolute Press-	square inch.	Temperature	Temperature corresponding to Pressure, in degrees Fahr.		Temperature corresponding to Pressure, in degrees Fahr.		Temperature of Brine, in degrees Fahr.		Steam-cylinder.	orse-power of Steam-cylinder.  Per cent of Indicated Power of Steam-cylinder lost in Friction.		Ice-melting Capacity in pounds per pound of Coal. Actual.+	Difference between theoretical Ice- melting Capacity, no Cylinder Heating or Friction, and actual. Per cent.;	Per cent of Theo- unt with Friction.§	Mean Effective Pressure, in lbs. per square inch.
Machine.	Number of Test.	Condenser.	Suction.	Condenser.	Suction.	Inlet,	Outlet.	Revolutions per minute.	Horse-power of	Per cent of Indi Steam-cylinde	Ice-melting Capacity, in tons per 24 hours.	Ice-melting Capacity per pound of Coal.	Difference between theore melting Capacity, no Heating or Friction, an Per cent.;	Heat losses. Per cent retical Amount with	Mean Effective Pre		
A: " " " " " " " " " " " " " " " " " " "	1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	135 131 128 126 200 136 131 126 117 130 57 56 60 91 61 59 59	55 42 30 22 42 60 45 24 41 60 21 15 10 7 15 22 16	72 70 69 68 72 71 68 64 70 77 76 81 104 81 80 75 103	27 14 1 -12 14 30 18 - 9 13 31 28 14 - 2 - 16 14 31 16	43 28 28 44 28 44 28 43 43 28 44 28 44 28 43 28 44 28 28 44 28 28 44 28 28 43 28 44 28 43 28 44 43 28 44 43 43 44 44 45 46 46 46 46 46 46 46 46 46 46 46 46 46	37 23 9 - 6 23 37 23 - 6 37	44.9 45.1 44.8 44.8 44.7 45.2 45.1 44.7 45.0 81.7 57.6 831.7 57.6 85.7 85.7 85.7 85.7 85.7 85.7 85.7 85.7	21.5 20.6 18.5 15.7 27.2 21.6 20.5 15.9 12.4	22.9 22.9 24.0 25.7 16.9 14.0 12.8 21.1 22.3	25.6 17.9 11.6 5.7 15.7 28.1 19.3 6.8	45.01 33.07 24.11 17.47 10.14 16.05 36.19 26.24 11.93 38.04 16.68	39.9 41.8 42.2 54.5	19.1 20.2 25.2 29.1 28.5 19.9 21.9 28.3 22.9 22.9 23.8 22.9 24.0 25.2 24.0 25.2 23.8 24.0 25.2 26.5 27.0	54.8 53.3 44.7 77.0 56.8 56.4 46.1 23.1 20.4 16.8 31.5 26.8 25.6 18.0 22.6 32.7		
CDE:	21 22 23 24 25 26 27 28	62 59 175 166 167 162 176 152	6 15 54 43 23 28 42 40	82 65* 81* 84 85 83 88 79	16 -17 -58* -40* 15 -11 - 3 14 13	37 6 14 36 21	28 28 2	58 1 57.7 57.9	9.9 83.2 38.1 85.0 72.6 73.6	24.3 21.9 32.1	3.5 10.3 4.9 73.9 37.9 46.5 74.4	9.86 3.42 3.0 24.16 14.52 17.55 23.31 20.1	54.2 71.7 80. 32.8 37.4 34.9 30.5 47.8	39.5 56.9 63. 11.7 22.7 18.6 13.5	17.7 26.6 89.2 65.9 57.6 59.9 70.5		

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<sup>\*</sup> Temperature of air at entrance and exit of expansion-cylinder.

t On a basis of 3 lbs. of coal per hour per H.P. of steam-cylinder of compression-machine and an evaporation of 11.1 lbs. of water per pound of combustible from and at 212° F. in the absorption-machine.

<sup>†</sup> Per cent of theoretical with no friction. § Loss due to heating during aspiration of gas in the compression-cylinder and to radiation and superheating at brine-tank.

Actual, including resistance due to inlet and exit valves.

In class A, a German machine, the ice-melting capacity ranges from 46.29 to 16.14 lbs. of ice per pound of coal, according as the suction pressure varies from about 45 to 8 lbs, above the atmosphere, this pressure being the condition which mainly controls the economy of compression-machines. These results are equivalent to realizing from 72% to 57% of theoretically perfect performances. The higher per cents appear to occur with the higher suction pressures, indicating a greater loss from cylinder heating (a phenomenon the reverse of cylinder condensation in steam-engines), as the range of the temperature of the gas in the compression-cylinder is greater.

In E. an American compression-machine, operating on the "dry system." the percentage of theoretical effect realized ranges from 69.5% to 62.6%. The friction losses are higher for the American machine. The latter's higher efficiency may be attributed, therefore, to more perfect displacement.

The largest "ice-melting capacity" in the American machine is 24.16 lbs.

This corresponds to the highest suction-pressures used in American practice for such refrigeration as is required in beer-storage cellars using the directexpansion system. The conditions most nearly corresponding to American brewery practice in the German tests are those in line 5, which give an "ice-melting capacity" of 19.07 lbs.

For the manufacture of artificial ice, the conditions of practice are those of lines 3 and 4, and lines 25 and 26. In the former the condensing pressure used requires more expense for cooling water than is common in American practice. The ice-melting capacity is therefore greater in the German machine, being 22.03 and 16.14 lbs. against 17.55 and 14.52 for the American

apparatus.

Class B. Sulphur Dioxide or Pictet Machines.—No records are available for determination of the "ice-melting capacity" of machines using pure for determination of the "ice-inelting capacity" of machines using pure sulphur dioxide. This fluid is in use in American machines, but in Europe it has given way to the "Pictet fluid," a mixture of about 9% of sulphur dioxide and 3% of carbonic acid. The presence of the carbonic acid affords a temperature about 14 Fahr, degrees lower than is obtained with pure sul-phur dioxide at atmospheric pressure. The latent heat of this mixture has dioxide

For brewery refrigerating conditions, line 17, we have 26.24 lbs. "ice-melting capacity" and for ice-making conditions, line 13, the "ice-ming capacity" is 17.4 lbs. These figures are practically as economical as those for ammonia, the per cent of theoretical effect realized ranging from 65.4 to 57.8. At extremely low temperatures, -15° Fahr., lines 14 and

18, the per cent realized is as low as 42.5.

18, the per cent realized is as low as 42.5.

Cylinder-heating.—In compression-machines employing volatile vapors the principal cause of the difference between the theoretical and the practical result is the heating of the ammonia, by the warm cylinder walls, during its entrance into the compressor, thereby expanding it, so that to compress a pound of ammonia a greater number of revolutions must be made by the compressing-pumps than corresponds to the density of the ammonia-gas as it issues from the brine-tank.

Tests of Ammonia Absorption-machine used in storage-ware-houses under approaches to the New York and Brooklyn Bridge. (Eng. July 22, 1887).—The circulated fluid consisted of a solution of chloride of cal-

cium of 1.163 sp. gr. Its specific heat was found to be .827.

The efficiency of the apparatus for 24 hours was found by taking the product of the cubic feet of brine circulating through the pipes by the averproduct of the color teer of order circular introgen and outgoing currents, as observed at request intervals by the specific heat of the brine (82) and its weight per crubic foot (73.48). The final product, applying all allowances for corrections from various causes, amounted to 6,218,816 heat-unit as the amount abstracted in 24 hours, equal to the melting of 43,505 lbs. of ice in the same time

The theoretical heating-power of the coal used in 24 hours was 27,000,000 heat-units; hence the efficiency of the apparatus was 23%. This is equivalent to an ice-melting effect of 16.1 lbs. per lb. of coal having a heating value of

10,000 B.T.U. per lb.

A test of a 35-ton absorption-machine in New Haven, Conn., by Prof. Denton (Trans. A. S. M. E., x. 792), gave an ice-melting effect of 20.1 lbs. per lb. of coal on a basis of boiler economy equivalent to 3 lbs. of steam per LH.P. in a good non-condensing steam-engine. The ammonia was worked between 198 and 28 lbs. pressure above the atmosphere.

# Performance of a 75-ton Refrigerating-machine.

	₽ <i>i</i> ;	o, o	등 주목	ರ :
	and lbs.	Maximum Capacity and Economy at Zero, Brine, and 8 1bs. Back Pressure.	Maximum Capacity and Economy for Zero, Brine, 13 lbs. Back Pressure.	and lbs.
	Finn	-eg	M o W	540
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	885	E E. & Y	8 5 5	B € €
	aximum Capac Economy at Back Pressure	faximum Capacit Economy at Z Brine, and 8 Back Pressure.	Iaximum Capacit Economy for Z Brine, 13 lbs. Pressure.	aximum Cape Economy at Back Pressur
	\$ 5 € E.	で記る芸	es io	E o ii
	Be Ba	Saga	X SS TO TO	Se Se
	Maximum Capacity Economy at 28 Back Pressure.	ž-	£	Maximum Capacity Economy at 27.5 Back Pressure.
Av. high ammonia press, above atmos	151 lbs.	152 lbs.	147 lbs.	161 lbs.
Av. back ammonia press, above atmos	28 "	8.2 "	13 "	27.5 "
Av. temperature brine inlet	36.76°	6.270	14.29°	
Av. temperature brine outlet	28.86°	2.03°	2.29°	28.45°
Av. range of temperature	7.90	4.240	12.00°	7.91°
Lbs. of brine circulated per minute	2281	2173	943	2374
Av. temp. condensing-water at inlet	44.650	56.65°	46.90	54.00°
Av. temp. condensing-water at outlet	83.66°	85.4°	85.46°	82.86°
Av. range of temperature	39.01°	28.75°	38.56°	28.80°
Lbs. water circulated p. min. thro' cond'ser	442	315	257	601.5
Lbs. water per min. through jackets	25 24.0°	44 16.2°	40 16,4°	14 29,1°
Range of temp rature in jackets	*28.17	14.68	16.4	28.32
Lbs. ammonia circulated per min Probable temperature of liquid ammonia,	. 20.11	14.00	10.01	20.02
entrance to brine-tank	*71.3°	*68°	*63.70	76.7°
Temp. of amm. corresp. to av. back press.	+14°	- 8°	- 5°	140
Av. temperature of gas leaving brine-tanks	34.20	14.70	3 00	29.2°
Temperature of gas entering compressor	*390	25°	10.13°	340
Av. temperature of gas leaving compressor	213°	263°	239°	2210
Av. temp. of gas entering condenser	200°	218°	209°	168°
Temperature due to condensing pressure	84.5°	84.0°	82.5°	88.0°
Heat given ammonia:				
By brine, B T.U. per miniute	14776	7186	8824	14647
By compressor, B.T.U. per minute	2786	2320	2518	3020
By compressor, B.T.U. per minute By atmosphere, B.T.U. per minute	140	147	167	141
Total near rec. by amin., b.t.o. per min.	17702	9653	11409	17708
Heat taken from ammonia:	10010	0050	0010	100-0
By condenser, B.T.U per min	17242 608	9056	9910	17359
By jackets, B.T.U. per min	182	712 338	656 250	406 252
By atmosphere, B.T.U. per min	18032	10106	10816	18017
Total heat rej. by amm., B.T U. per min Dif. of heat rec'd and rej., B.T.U. per min	330	453	407	309
% work of compression removed by jackets.	22%	31%	26%	13%
Av. revolutions per min	58.09	57.7	57.88	58.89
Mean eff. press. steam-cyl., lbs. per sq. in	32.5	57.7 27.17	27.83	32.97
Mean eff. press. ammcyl., lbs. per sq. in	65.9	53,3	59.86	70.54
Av. H.P. steam-cylinder	85.00	71.7	73.6	88.63
Av. H.P. ammonia-cylinder	65.7	54.7	59.37	71.20
Av. H.P. ammonia-cylinder. Friction in per cent of steam H P	23.0	24.0	20.0	19.67
Total cooling water, gallons per min. per				
ton per 24 hours	0.75	1.185	0.797	0,990
Tons ice-melting capacity per 24 hours	74.8	36.43	44.64	74.56
Lbs. ice-refrigerating eff. per lb. coal at 3	01.1	11.1	10' 00'	00.00
lbs. per H.P. per hour	24.1	14.1	17.27	23.37
Cost coal per ton of ice-refrigerating effect	20 166	@0.000	\$0.004	20 100
at \$4 per ton	\$0.166	\$0.283	\$0.231	\$0.170
at \$1 per 1000 cu. ft	\$0.128	\$0,200	\$0,136	\$0.169
Total cost of 1 ton of ice-refrigerating eff	\$0.294	\$0.483	\$0.467	\$0.339
Total Cost of I con of ice leftingerating en	₩0.204	WO. 100	Ψ0,301	\$0.500

Figures marked thus (\*) are obtained by calculation; all other figures are obtained from experimental data; temperatures are in Fahrenheit degrees.

## Ammonia Compression-machine.

ACTUAL RESULTS OBTAINED AT THE MUNICH TESTS. (Prof. Linde, Trans. A. S. M. E., xiv. 1419.)

No. of Test,	1	2	3	4	5
Temp. of refrig- \ Inlet, deg. F erated brine \ Outlet, t deg. F		28.344 22.885	8.771	-0.279 -5.879	23.072
Specific heat of brine	342,909	0.851 908.84 263,950 260.83	633.89	121,474	800.93 220,284
Cold pro- Per I.H.P. in compcyl. duced per Per I H.P. in steam-cyl.	15.80 24,813	16.47 18,471 16,026	15.28 12,770	14.24	21.61 11,151
h., B.T.U. Per lb. of steam					

Means for Applying the Cold. (M. C. Bannister, Liverpool Eng'g Soc'y, 1890.)—The most useful means for applying the cold to various uses is a saturated solution of brine or chloride of magnesium, which remains liquid at 5° Fahr. The brine is first cooled by being circulated in contact with the refrigerator-tubes, and then distributed through coils of pipes, arranged either in the substances requiring a reduction of tempera-ture, or in the cold stores or rooms prepared for them; the air coming in contact with the cold tubes is immediately chilled, and the moisture in the air deposited on the pipes. It then falls, making room for warmer air, and so circulates until the whole room is at the temperature of the brine in the

pipes.
In a recent arrangement for refrigerating made by the Linde British Refrigeration Co., the cold brine is circulated through a shallow trough, in which revolve a number of shafts, each geared together, and driven by mechanical means. On the shafts are fixed a number of wrought-iron disks, partly immersed in the brine, which cool them down to the brine temperature as they revolve; over these disks a rapid circulation of air is passed by a fan, being cooled by contact with the plates; then it is led into the chambers requiring refrigeration, from which it is again drawn by the same fan; thus all moisture and impurities are removed from the chambers, and deposited in the brine, producing the most perfect antiseptic atmosphere yet invented for cold storing; while the maximum efficiency of the brine tem-perature was always available, the brine being periodically concentrated by suitable arrangements.

Air has also been used as the circulating medium. The ammonia-pipes refrigerate the air in a cooling-chamber, and large wooden conduits are used to convey it to and return it from the rooms to be cooled. An advantage of this system is that by it a room may be refrigerated more quickly than by brine-coils. The returning air deposits its moisture in the form of snow on the ammonia-pipes, which is removed by mechanical brushes.

#### ARTIFICIAL ICE-MANUFACTURE.

Under summer conditions, with condensing water at 70°, artificial ice-machines use ammonia at about 190 lbs. above the atmosphere condenser-pressure, and 15 lbs. suction-pressure.

In a compression type of machine the useful circulation of ammonia, allowing for the effect of cylinder-heating, is about 13 lbs. per hour per indicated horse-power of the steam cylinder. This weight of ammonia produces about 32 lbs, of ice at 15° from water at 70°. If the ice is made from distilled water, as in the "can system," the amount of the latter supplied by the boilers is about 33% greater than the weight of ice obtained. This excess represents steam escaping to the atmosphere, from the re-boiler and steam-condenser, to purify the distilled water, or free it from air; also, the loss through leaks and drips, and loss by melting of the ice in extracting it from the cans. The total steam consumed per horse-power is, therefore, about  $32 \times 1.33 = 43.0$  lbs. About 7.0 lbs. of this covers the steam-consumption of the steam-engines driving the brine circulating-pumps, the several

cold-water pumps, and leakage, drips, etc. Consequently, the main steamengine must consume 36 lbs. of steam per hour per I.H.P., or else live steam must be condensed to supply the required amount of distilled water. There is, therefore, nothing to be gained by using steam at high rates of expansion in the steam-engines, in making artificial ice from distilled water. If the cooling water for the ammonia-coils and steam-condenser is not too bard for use in the boilers, it may enter the latter at about 175° F., by restricting the quantity to 1½ gallons per minute per ton of ice. With good coal 8½ bis. of feed-water may then be evaporated, on the average, per lb. of coal.

The ice made per pound of coal will then be  $32 + \frac{43.0}{8.5} = 6.0$  lbs. This cormust be condensed to supply the required amount of distilled water. There

responds with the results of average practice.
If ice is manufactured by the "plate system," no distilled water is used for freezing. Hence the water evaporated by the boilers may be reduced to the amount which will drive the steam-motors, and the latter may use steam expansively to any extent consistent with the power required to compress the ammonia, operate the feed and filter pumps, and the hoisting machinery. The latter may require about 15% of the power needed for compressing the ammonia.

If a compound condensing steam-engine is used for driving the compressors, the steam per indicated steam horse-power, or per 32 lbs. of net ice, may be 14 lbs. per hour. The other motors at 50 lbs. of steam per horse-power will use 7.5 lbs. per hour, making the total consumption per steam horse-power of the compressor 21.5 lbs. Taking the evaporation at 8 lbs., norse-power of the compressor 31.5 los. Taking the evaporation at 8 los., the feed-water temperature being limited to about  $110^\circ$ , the coal per horse-power is 2.7 lbs, per hour. The net ice per lb. of coal is then about 32 + 2.7 = 11.8 lbs. The best results with "plate-system" plants, using a compound steam-engine, have thus far afforded about  $10\frac{1}{2}$  lbs. of ice per lb. of coal. In the "plate system" the ice gradually forms, in from 9 to 14 days, to a thickness of about 14 inches, on hollow plates  $10 \times 14$  feet in area, in which the coalise of high simple coals.

the cooling fluid circulates.

In the "can system" the water is frozen in blocks weighing about 300 lbs. In the "can system" the water is frozen in blocks weighing about 300 lbs. each, and the freezing is completed in from 50 to 60 hours. The freezing-tank area occupied by the "plate system" is, therefore, about four times, and the cubic contents about twelve times, as much as is required in the

"can system."

The investment for the "plate" is about one third greater than for the "can" system. In the latter system ice is being drawn throughout the 24 hours, and the hoisting is done by hand tackle. In the "plate system" the entire daily product is drawn, cut, and stored in a few hours, the hoisting being performed by power. The distribution of cost is as follows for the two systems, taking the cost for the "can" or distilled-water system as 100, which represents an actual cost of about \$1.25 per net ton:

	Can System.	Plate System.
Hoisting and storing ice	14.2	2.8
Engineers, firemen, and coal-passer	15.0	13.9
Coal at \$3.50 per gross ton	42.2	20.0
Water pumped directly from a natural source		
at 5 cts. per 1000 cubic feet	1.3	2.6
Interest and depreciation at 10%	24.6	32.7
Repairs		3.4
	100.00	75.4

A compound condensing engine is assumed to be used by the "plate sys-

tem."

Test of the New York Hygeia Ice-making Plant.—(By Messrs. Hupfel, Griswold, and Mackenzie; Stevens Indicator, Jan. 1891.)
The final results of the tests were as follows:

Net ice made per pound of coal, in pounds	7.12
Pounds of net ice per hour per horse-power	37.8
Net ice manufactured per day (12 hours) in tons	97
Av. pressure of ammonia-gas at condenser, lbs. per sq. in. ab. atmos.	135.2
Average back pressure of ammgas, lbs. per sq. in. above atmos	15.8
Average temperature of brine in freezing-tanks, degrees F	19.7
Total number of cans filled per week	4389
Ratio of cooling-surface of coils in brine-tank to can-surface	7 to 10
Ratio of cooling-surface of coils in brine-tank to can-surface	7 to 10

Ratio of brine in tanks to water in cans Ratio of circulating water at condensers to distilled water Pounds of water evaporated at boilers per pound of coal	26 to 1 8.085
Total horse-power developed by compressor-engines	$\frac{444}{2.2}$
APPROXIMATE DIVISION OF STEAM IN PER CENTS OF TOTAL AMOUN	T.
Compressor-engines. Live steam admitted directly to condensers	60.1 19.7

Steam for pumps, agitator, and elevator engines .....,... Live steam for reboiling distilled water...
Steam for blowers furnishing draught at boilers..... Sprinklers for removing ice from cans.....

The precautions taken to insure the purity of the ice are thus described: The water which finally leaves the condenser is the accumulation of the The water which mally leaves the condenser is the accumulation of the exhausts from the various pumps and engines, together with an amount of live steam injected into it directly from the boilers. This last quantity is used to make up any deficit in the amount of water necessary to supply the ice-cans. This water on leaving the condensers is violently reboiled, and afterwards cooled by running through a coil surface-cooler. It then passes through an oil-separator, after which it runs through three charcoal-filters and deodorizers, placed in series and containing 28 feet of charcoal. It next passes into the supply-tank in which there is an electrical attachment for detecting salt. Nitrate-of-silver tests are also made for salt daily. From this tank it is fed to the ice-cans, which are carefully covered so that the water cannot possibly receive any impurities.

## MARINE ENGINEERING.

Rules for Measuring Dimensions and Obtaining Ton-age of Vessels. (Record of American & Foreign Shipping. American Sipmasters' Assn., N. Y. 1890.)—The dimensions to be measured as follows: I. Length, L—From the fore side of stem to the after side of stem-post measured at middle line on the upper deck of all vessels, except those hav-

ing a continuous hurricane-deck extending right fore and aft, in which the length is to be measured on the range of deck immediately below the hurricane-deck.

Vessels having clipper heads, raking forward, or receding stems, or raking stern-posts, the length to be the distance of the fore side of stem from aft-side of stern-post at the deep-load water-line measured at middle line.

(The inner or propeller-post to be taken as stern-post in screw-steamers. II. Breadth, B.—To be measured over the widest frame at its widest part;

in other words, the moulded breadth.

III. Depth, D .- To be measured at the dead-flat frame and at middle line of vessel. It shall be the distance from the top of floor-plate to the upper side of upper deck-beam in all vessels except those having a continuous hurricane-deck, extending right fore and aft, and not intended for the American coasting trade, in which the depth is to be the distance from top of floor-plate to midway between top of hurricane deck-beam and the top of deck-beam of the deck immediately below hurricane-deck.

In vessels fitted with a continuous hurricane deck, extending right fore and aft, and intended for the American coasting trade, the depth is to be the distance from top of floor-plate to top of deck-beam of deck immedia

ately below hurricane-deck,

**Eule for Obtaining Tonnage.**—Multiply together the length, breadth, and depth, and their product by .75; divide the last product by 10; the quotient will be the tonnage.  $L \times B \times D \times .75 = \text{tonnage}$ .

100 The U. S. Custom-house Tonnage Law, May 6, 1864, provides that "the register tomage of a vessel shall be her entire internal cubic capacity in tons of 100 cubic feet each." This measurement includes all the space between upper decks, however many there may be. Explicit directions for making the measurements are given in the law.

The Displacement of a Vessel (measured in tons of 2240 lbs.) is the weight of the volume of water which it displaces. For sea-water it is equal to the volume of the vessel beneath the water-line, in cubic feet, divided by 35, which figure is the number of cubic feet of sea-water at 60° F. in a ton of 2240 lbs. For fresh water the divisor is 35.93. The U. S. register tonnage will equal the displacement when the entire internal cubic

capacity bears to the displacement the ratio of 100 to 35.

capacity bears to the displacement the ratio of 100 to 35. The displacement or gross tonnage is sometimes approximately estimated as follows: Let L denote the length in feet of the boat, B its extreme breadth in feet, and D the mean draught in feet; the product of these three dimensions will give the volume of a parallelopipedon in cubic feet. Putting V for this volume, we have  $V = L \times B \times B$ . The volume of displacement may then be expressed as a percentage of the volume V, known as the "block coefficient." This percentage varies for different classes of ships. In racing yachts with very deep keels it varies to be consistent of the volume of the volume V, the volume of the volume V is the volume V and V is the volume V and V is the volume V is the volume of displacement in consistent of V in V is the volume of displacement in the volume of V is V in V

Coefficient of Fineness.—A term used to express the relation be-tween the displacement of a ship and the volume of a rectangular prism or box whose lineal dimensions are the length, breadth, and draught of the

ship.

Coefficient of fineness =  $\frac{D \times 35}{L \times B \times W}$ ; D being the displacement in tous of 35 cubic feet of sea-water to the ton, L the length between perpendiculars, B the extreme breadth of beam, and W the mean draught of water, all in feet.

Coefficient of Water-lines.—An expression of the relation of the displacement to the volume of the prism whose section equals the midship section of the ship, and length equal to the length of the ship.

Coefficient of water-lines =  $\frac{1}{\text{area of immersed water section}} \times L$ Seaton gives the following values:

	Coefficient of Fineness.	Coefficient of	
Finely-shaped ships	0.55	0.63	
Fairly-shaped ships	0.61	0.67	
Ordinary merchant steamers for speeds of 10 to	)		
11 knots	0.65	0.72	
Cargo steamers, 9 to 10 knots		0.76	
Modern cargo steamers of large size	0.78	0.83	

Resistance of Ships.—The resistance of a ship passing through water may vary from a number of causes, as speed, form of body, displacement, midship dimensions, character of wetted surface, fineness of lines, etc. The resistance of the water is twofold: ist. That due to the displacement of the water at the bow and its replacement at the stern, with the consequent formation of waves. 2d. The friction between the wetted surface of the ship and the water, known as skin resistance. A common approximate formula for resistance of vessels is

Resistance = speed<sup>2</sup> ×  $\sqrt[3]{\text{displacement}^2}$  × a constant, or  $R = S^2D^3 \times C$ .

If D =displacement in pounds, S =speed in feet per minute, R =resistance in foot-pounds per minute,  $R = CS^2D^2$ . The work done in overcoming the resistance through a distance equal to S is  $R \times S = CS^3D^3$ ; and if E is the efficiency of the propeller and machinery combined, the indicated

CS3 D3 horse-power I.H.P. =  $\frac{1}{E \times 33,000}$ 

If S = speed in knots, D = displacement in tons, and C a constant which includes all the constants for form of vessel, efficiency of mechanism, etc.,

I.H.P. =  $\frac{S^3D^{\frac{2}{3}}}{C}$ The wetted surface varies as the cube root of the square of the displacement; thus, let L be the length of edge of a cube just immersed, whose displacement is D and wetted surface W. Then  $D = L^3$  or  $L = \sqrt[3]{D}$ , and

 $W = 5 \times L^2 = 5 \times (\sqrt[3]{D})^2$ . That is, W varies as  $D_3^2$ .

Another approximate formula is

I.H.P. = 
$$\frac{\text{area of immersed midship section} \times S^3}{K}$$

The usefulness of these two formulæ depends upon the accuracy of the so-called "constants" C and K, which vary with the size and form of the ship, and probably also with the speed. Scaton gives the following, which may be taken roughly as the values of C and K under the conditions expressed:

General Description of Ship.	Speed, knots.	Value of C.	Value of K.
Ships over 400 feet long, finely shaped	15 to 17 15 " 17 13 " 15 11 " 13	240 190 240 260	620 500 650 700 650
Ships over 300 feet long, fairly shaped  Ships over 250 feet long, finely shaped  """  """  """  """  """  """	9 " 11 13 " 15 11 " 13 9 " 11	240 260 200 240 260	700 580 660 700
Ships over 250 feet long, fairly shaped.  Ships over 200 feet long, finely shaped.  Ships over 200 feet long, fairly shaped.	11 " 13 9 " 11 11 " 12 9 " 11 9 " 11	220 250 220 240 220	620 680 600 640 620
Ships under 200 feet long, fairly shaped  "" " " " " " " " " " " " " " " " " "	9 " 11 11 " 12 10 " 11 9 " 10 9 " 10	200 210 230 200	550 580 620 600

## Coefficient of Performance of Vessels .-- The quotient

gives a quotient of performance which represents the comparative cost of propulsion in coal expended. Sixteen vessels with three-stage expansion-engines in 1839 gave an average coefficient of 14,810, the range being from 12,150 to 16,700.

In 1881 seventeen vessels with two-stage expansion-engines gave an aver-In 105 seventeen vessels with two-stage expansion-engines gave an average coefficient of 11,710. In 1881 the length of the vessels tested ranged from 200 to 320, and in 1890 from 295 to 400. The speed in knots divided by the square root of the length in feet in 1881 averaged 0.539; and in 1890, 0.578; ranging from 0.520 to 0.641. (Proc. Inst. M. E., July, 1891, p. 329.).

Defects of the Common Formula for Resistance.—Modern

experiments throw doubt upon the truth of the statement that the resistance

experiments throw doubt upon the truth of the statement that the resistance varies as the square of the speed. (See Robt, Mansel's letters in Engineering, 1891; also his paper on The Mechanical Theory of Steamship Propulsion, read hefore Section G of the Engineering Congress, Chicago, 1893.)
Seaton says: In small steamers the chief resistance is the skin resistance in very fine steamers at high speeds the amount of power required seems excessive when compared with that of ordinary steamers at ordinary speeds. In torpedo-launches at certain high speeds the resistance increases at a

lower rate than the square of the speed.

In ordinary sea-going and river steamers the reverse seems to be the case. Rankine's Formula for total resistance of vessels of the "waveline" type is:

$$R = ALBV^{2}(1 + 4\sin^{2}\theta + \sin^{4}\theta),$$

in which equation  $\theta$  is the mean angle of greatest obliquity of the streamlines, A is a constant multiplier, B the mean wetted girth of the surface exposed to friction. L the length in feet, and V the speed in knots. The power demanded to impel a ship is thus the product of a constant to be determined by experiment, the area of the wetted surface, the cube of the speed, and the quantity in the parenthesis, which is known as the "coefficient of augmentation." The last term of the coefficient may be neglected in calculating the resistance of ships as too small to be practically important. In applying the formula, the mean of the squares of the sines of the angles of maximum obliquity of the water-lines is to be taken for  $\sin^2 \theta$ , and the rule will then read thus:

To obtain the resistance of a ship of good form, in pounds, multiply the length in feet by the mean immersed girth and by the coefficient of augmentation, and then take the product of this "augmented surface," as Rankine termed it, by the square of the speed in knots, and by the proper constant coefficient selected from the following:

> For clean painted vessels, iron hulls...... A = .01For clean coppered vessels...... A = .009 to .008 For moderately rough iron vessels...... A = .011 +

The net, or effective, horse-power demanded will be quite closely obtained by multiplying the resistance calculated, as above, by the speed in knots and dividing by 326. The gross, or indicated, power is obtained by multiplying the last quantity by the reciprocal of the efficiency of the machinery and propeller, which usually should be about 0.6. Rankine uses as a divisor in

this case 200 to 260.

The form of the vessel, even when designed by skilful and experienced naval architects, will often vary to such an extent as to cause the above constant coefficients to vary somewhat; and the range of variation with good forms is found to be from 0.8 to 1.5 the figures given.

For well-shaped iron vessels, an approximate formula for the horse-power required is H.P.  $= \frac{SV^2}{20,000}$ , in which S is the "augmented surface." The ex-

pression  $\frac{SV^3}{\text{H.P.}}$  has been called by Rankine the coefficient of propulsion. In the Hudson River steamer "Mary Powell," according to Thurston, this coefficient was as high as 23,500.

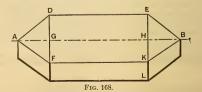
 $D^{\frac{2}{3}}V^{3}$ The expression has been called the locomotive performance. (See H.P. Rankine's Treatise on Shipbuilding, 1864; Thurston's Manual of the Steamengine, part ii. p. 16; also paper by F. T. Bowles, U.S.N., Proc. U. S. Naval Institute, 1883.)

Rankine's method for calculating the resistance is said by Seaton to give more accurate and reliable results than those obtained by the older rules, but it is criticised as being difficult and inconvenient of application.

Dr. Kirk's Method.—This method is generally used on the Clyde.

The general idea proposed by Dr. Kirk is to reduce all ships to so definite
and simple a form that they may be easily compared; and the magnitude of certain features of this form shall determine the suitability of the ship for

speed, etc. The form consists of a middle body, which is a rectangular parallelopiped, and fore body and after body, prisms having isosceles triangles for bases, as shown in Fig. 168.



This is called a block model, and is such that its length is equal to that of the ship, the depth is equal to the mean draught, the capacity equal to the displacement volume, and its area of section equal to the area of im-

mersed midship section. The dimensions of the block model may be obtained as follows:

$$\begin{array}{ll} \text{Let } AG = HB = \text{length of fore-or after-body} = F; \\ GH = \text{length of middle body} & = M; \\ KL = \text{mean draught} & = H; \\ EK = \frac{\text{area of immersed midship section}}{KL} & = B. \end{array}$$

Volume of block =  $(F + M) \times B \times H$ ; Midship section =  $B \times H$ ;

Displacement in tons = volume in cubic ft. + 35.

$$AH = AG + GH = F + M = \text{displacement} \times 35 + (B \times H).$$

The wetted surface of the block is nearly equal to that of the ship of the same length, beam and draught; usually 2% to 5% greater. In exceedingly fine hollow-line ships it may be 5% greater.

Area of bottom of block = 
$$(F + M) \times B$$
;  
Area of sides =  $2M \times H$ .

Area of sides of ends = 
$$4\sqrt{F^2 + \left(\frac{B}{2}\right)^2} \times H$$
;

Tangent of half angle of entrance 
$$=\frac{\frac{1}{2}B}{F}=\frac{B}{2F}$$
.

From this, by a table of natural tangents, the angle of entrance may be obtained:

Angle of Entrance Fore-body in of the Block Model, parts of length.

E. R. Mumford's Method of Calculating Wetted Surfaces is given in a paper by Archibald Denny, Eng'g, Sept. 21, 1894. The following is his formula, which gives closely accurate results for medium draughts, beams, and finenesses:

$$S = (L \times D \times 1.7) + (L \times B \times C),$$

in which S = wetted surface in square feet;

L = length between perpendiculars in feet;

D = middle draught in feet:

B = beam in feet;C = block coefficient.

The formula may also be expressed in the form S = L(1.7D + BC).

The formula may also be expressed in the form S = L(I,D + BC). In the case of twin-screw ships having projecting shaft-casings, or in the case of a ship having a deep keel or bilge keels, an addition must be made for such projections. The formula gives results which are in general much more accurate than those obtained by Kirk's method. It underestimates the surface when the beam, draught, or block coefficients are excessive; but the error is small except in the case of abnormal forms, such as stern-wheel steamers having very excessive beams (nearly one fourth the length), and also very full block coefficients. The formula gives a surface about 6% too small for such forms.

To Find the Indicated Horse-power from the Wetted Surface. (Seaton.)—In ordinary cases the horse-power per 100 feet of wetted surface may be found by assuming that the rate for a speed of 10 knots is 5, and that the quantity varies as the cube of the speed. For example: To find the number of I.H.P. necessary to drive a ship at a speed of 15

knots, having a wetted skin of block model of 16,200 square feet:

When the ship is exceptionally well-proportioned, the bottom quite clean, and the efficiency of the machinery high, as low a rate as 4 I.H.P. per 100 feet of wetted skin of block model may be allowed

The gross indicated horse-power includes the power necessary to over-come the friction and other resistance of the engine itself and the shafting, and also the power lost in the propellor. In other words, I.H.P. is no meas-ure of the resistance of the ship, and can only be relied on as a means of deciding the size of engines for speed, so long as the efficiency of the engine and propellor is known definitely, or so long as similar engines and propellers are employed in ships to be compared. The former is difficult to obtain, and it is nearly impossible in practice to know how much of the power shown in the cylinders is employed usefully in overcoming the resistance of the ship. The following example is given to show the variation in the efficiency of propellers:

Knots. I.H.P H.M.S. "Amazon," with a 4-bladed screw, gave.......... H.M.S. "Amazon," with a 2-bladed screw, increased pitch, 12,064 with 1940 H.M.S. "Iris," with a 4-bladed screw.
H.M.S. "Iris," with 2-bladed screw, increased pitch, less 12.396 1663 16,577 7503

18.587 revolutions per knot..... 7556 Relative Horse-power Required for Different Speeds of

Vessels. (Horse-power for 10 knots = 1.)—The horse-power is taken usually to vary as the cube of the speed, but in different vessels and at different speeds it may vary from the 2.8 power to the 3.5 power, depending upor the lines of the vessel and upon the efficiency of the engines, the propeller, etc.

Speed, knots.	4	6	8	10	12	14	16	18	20	22	24	26	28	30
S3-4	.0769 .0701 .0640 .0584 .0533 .0486	.227 .216 .205 .195 .185 .176	.524 .512 .501 .490 .479 .468	1. 1. 1. 1. 1.	1.697 1.728 1.760 1.792 1.825 1.859	2.653 2.744 2.838 2.985 3.036 3.139	3.908 4.096 4.293 4.500 4.716 4.943	5.185 5.499 5.832 6.185 6.559 6.957 7.378 7 824	7.464 8. 8.574 9.189 9.849 10.56	9.841 10.65 11.52 12.47 13.49 14.60	12.67 13.82 15.09 16.47 17.98 19.62	15.97 17.58 19.34 21.28 23.41 25.76	19.80 21.95 24.33 26 97 29.90 33.14	24.19 27. 30.14 33.63 37.54 41.90

Example in Use of the Table.—A certain ressel makes 14 knots speed with 1857 I.H.P. and 16 knots with 900 I.H.P. What I.H.P. will be required at 18 knots, the rate of increase of horse-power with increase of speed remaining constant? The first step is to find the rate of increase, thus:  $14^x$ :  $16^x$ : 587: 900.

> $x \log 16 - x \log 14 = \log 900 - \log 587$ ; x(0.204120 - 0.146128) = 2.954243 - 2.768638

whence x (the exponent of S in formula H.P.  $\propto S^{x}$ ) = 32. From the table, for  $S^{3\cdot 2}$  and 16 knots, the I H.P. is 4.5 times the I.H.P. at

10 knots, ... H.P. at 10 knots =  $900 \div 4.5 = 200$ . From the table, for  $S^{3\cdot 2}$  and 18 knots, the I.H.P. is 6.559 times the I.H.P. at

10 knots; .: H.P. at 18 knots = 2.0 × 6.559 = 1312 H P.

Resistance per Horse-power for Different Speeds, (One horse-power = 33.000 lbs. resistance overcome through 1 ft. in 1 min.)—The resistances per horse-power for various speeds are as follows: For a speed of 1 knot, or 6080 feet per hour =  $101\frac{1}{2}$  ft. per min.,  $33,000 + 101\frac{1}{2} = 325,658$  lbs. per horse-power; and for any other speed 325,658 lbs. divided by the speed in knots; or for

1 knot 325.66 lbs. 11 knots 29.61 lbs. 16 knots 20.35 lbs. 6 knots 54.28 lbs. 2 knots 162.83 " 46.52 " 27.14 25.05 12 19.16 66 .. 66 40.71 66 3 108.55 18 .. 66 9 64 36.18 66 23.26 46 17.14 81.41 14 19 66 66 65.13 10 32.57 21.71 16.28 20

# Results of Trials of Steam-vessels of Various Sizes.

(From Seaton's Marine Engineering.)

(From Seaton	Sman	ne Engi	meering	••)		
	S.S. "Torpedo."	P.S. "John Penn."	S.S. "Africa."	P.S. "Mary Powell"	S.S. "Harrar."	R.M.P.S.
Length, perpendiculars	90' 0'' 10' 6'' 2' 6'' 29 73 24? 903	171' 9'' 18' 9'' 6' 91'2'' 280 99 3793	130' 0" 21' 0" 8' 10" 370 148 3754	286' 0" 34' 3" 6' 0" 800 200 8222	230′ 0″ 29′ 0″ 13′ 6″ 1500 340 10,075	327' 0" 35' 0" 13' 0" 1900 336 15,782
Wetted skin	45′ 0′′	72′ 00′′	42' 6"	143′ 0′′	79′ 6′′	129′ 0′′
Angle of entrance Displacement × 35	12° 40′	11° 30′	23° 50′	13° 21′	17° 0″	11° 26′
Length × Imm, mid area	0.481	0.576	0.608	0.489	0.671	0.605
Speed (knots) Indicated horse-power. I.H.P. per 100 ft. wetted skin I.H.P. per 100 ft. wetted skin, re-	22 01 460 50.9	15.3 798 21.04	10.74 371 9.88	17.20 1490 18.12	10.04 503 5.00	17.8 4751 30.00
duced to 10 knots	4.78	5.87	7.97	3.56	4.90	5.32
$\frac{D^{\frac{2}{3}} \times S^3}{\text{I.H.P.}}$	223	192	172.8	293.7	266	182
$\frac{\text{Immersed mid area} \times S^3}{\text{I.H.P.}}$	556?	445	495	683	690	399
1.11.1.	1					
	-		<u> </u>		-	
	H.M.S.	H.M.S.	H.M.S.	"S.S.	H.M.S.	R.M.S.S.
Length, perpendiculars	H.M.S. Active.	300' 0'' 46' 0'' 18' 2'' 3290 700	300° 0° 46° 0° 18' 2° 3:90 700° 18,168		392. 0" 399. 0" 21' 4" 5767 738 26,235	"." "." "." "." "." " " " "
Breadth, extreme.  Mean draught water. Displacement (tons).  Area Imm. mid. section.  Wetted skin.  Length, fore-body.	270' 0'' 42' 0'' 18' 10'' 3057 632	300' 0'' 46' 0'' 18' 2'' 3290 700	300' 0'' 46' 0'' 18' 2'' 3:90 700	370' 0'' 41' 0'' 18' 11'' 4635 656	392. 0'' 39. 0'' 21' 4'' 5767 738	8500 926 926 926
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section.  ** **Example ** ** ** ** ** ** ** ** ** ** ** ** **	870° 0° 42° 0° 42° 0° 18° 10° 632 16,008	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168	300' 0" 46' 0" 18' 2" 3:90 700' 18,168	370′ 0′′ 41′ 0′′ 41′ 0′′ 18′ 11′′ 4635 656 22,633	392. 0" 39 0" 21' 4" 5767 738 26,235	8500 926 32,578
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section.  Wetted skin. Length, fore-body.	270' 0'' 42' 0'' 18' 10'' 3057 632 16,008	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168 135' 6'' 16° 16' 0.548	300' 0" 46' 0" 18' 2" 3:90 700' 18,168 135' 6" 16° 16' 0.548	370′ 0″ 41′ 0″ 18′ 11″ 4635 656 22,633 123′ 0″ 16° 4′ 0.668	392. 0" 392. 0" 39. 39 0" 5767 738 26,235 118' 0" 16° 30'	450' 0" 45' 2" 8500 926 32,578 129' 0"
Breadth, extreme. Mean draught water. Displacement (tons). Area Imm. mid. section.  2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	270' 0" 42' 0" 18' 10" 3057 632 16,008 101' 0' 18° 44' 0.629 14.966 4015 25.08	300′ 0″ 46′ 0″ 18′ 2″ 3290 700 18,168 135′ 6″ 16° 16′ 0.548 18.573 7714 42.46	300' 0" 46' 0" 18' 2" 3:90 700' 18,168 135' 6" 16° 16' 0.548 15.746 3958 21.78	370' 0'' 41' 0'' 18' 11'' 4635 656 22,633 123' 0'' 16° 4' 0.668 13.80 2500 11.04	392. 0" 39 0" 21' 4" 738 26,235 118' 0" 0.698 12.054 1758 6.7	**Signature**  **Signature**  **Test
Breadth, extreme Mean draught water. Displacement (tons). Area Imm. mid. section  \$\frac{2}{2} \frac{2}{3} \	270' 0'' 42' 0'' 18' 10'' 3057 632 16,008 101' 0'' 18° 44' 0.629 14.966 4015 25.08 7.49	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168 135' 6'' 16° 16' 0.548 18,573 7714 42,46 6.634	300' 0'' 46' 0'' 18' 2'' 3:90 700 18,168 135' 6'' 16° 16' 0.548 15.746 3958 21.78	370' 0" 41' 0" 18' 11" 4635 656 22,633 123' 0" 16° 4' 0.668 13.80 2500 11.04 4.20	392. 0" 399. 0" 399. 21' 4" 5767 738 26,235 118' 0" 16° 30' 0.698 12.054 1758 6.7 3.83	25 0 0 0 0 1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1
Breadth, extreme.  Mean draught water. Displacement (tons). Area Imm. mid. section.  2 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	270' 0" 42' 0" 18' 10" 3057 632 16,008 101' 0' 18° 44' 0.629 14.966 4015 25.08	300′ 0″ 46′ 0″ 18′ 2″ 3290 700 18,168 135′ 6″ 16° 16′ 0.548 18.573 7714 42.46	300' 0" 46' 0" 18' 2" 3:90 700' 18,168 135' 6" 16° 16' 0.548 15.746 3958 21.78	370' 0'' 41' 0'' 18' 11'' 4635 656 22,633 123' 0'' 16° 4' 0.668 13.80 2500 11.04	392. 0" 39 0" 21' 4" 738 26,235 118' 0" 0.698 12.054 1758 6.7	**Signature**  **Signature**  **Test
Breadth, extreme.  Mean draught water. Displacement (tons). Area Imm. mid. section.  \$\frac{3}{2} \frac{7}{2} \fra	270' 0'' 42' 0'' 18' 10'' 3057 632 16,008 101' 0'' 18° 44' 0.629 14.966 4015 25.08 7.49	300' 0'' 46' 0'' 18' 2'' 3290 700 18,168 135' 6'' 16° 16' 0.548 18,573 7714 42,46 6.634	300' 0'' 46' 0'' 18' 2'' 3:90 700 18,168 135' 6'' 16° 16' 0.548 15.746 3958 21.78	370' 0" 41' 0" 18' 11" 4635 656 22,633 123' 0" 16° 4' 0.668 13.80 2500 11.04	392. 0" 399. 0" 399. 21' 4" 5767 738 26,235 118' 0" 16° 30' 0.698 12.054 1758 6.7 3.83	25 0 0 0 0 1 1 2 1 2 1 2 1 2 1 2 1 2 1 2 1

# Results of Progressive Speed Trials in Typical Vessels,

(Eng'g, April 15, 1892, p. 463.)

	Torpedo-boat.	Torpedo- gunboat, "Sharp- shooter" Class.	"Medusa," 3d-cl. Cruiser.	"Terpsichore," 2d-cl. Cruiser.	"Edgar," 1st-cl. Cruiser,	"Blenheim," 1st-cl. Cruiser.	Atlantic Passenger Steamer.
Length (in feet) Breadth " Draught (mean) on trial Displacement (tons). L.H.P10 knots " 14 " " 18 " " 20 "	135	230	265	300	360	375	525
	14	27	41	43	60	65	63
	5' 1"	8' 3''	16' 6"	16' 2''	23' 9''	25′ 9′′	21' 3''
	103	735	2800	3330	7390	9100	11550
	110	450	700	800	1000	1500	2000
	260	1100	2100	2400	3000	4000	4600
	870	2500	6400	6000	7500	9000	10000
	1130	3500	10000	9000	11000	12500	14500
Speed   Ratio of speeds   10   1	1	1	1	1	1	1	1
	2.36	2.44	3	3	3	2.67	2.3
	7.91	5.56	9.14	7.5	7.5	6.	5
	10.27	7.78	14.14	11.25	11	8.42	7.25
Admiralty coeff. $C = \frac{D^{\frac{2}{3}} \times S^{3}}{\text{I.H.P.}}$ $\begin{cases} 10 \text{ knots.} \\ 14 \\ 18 \\ 20 \end{cases}$	200	181	284	279	380	290	255
	232	203	259	255	347	298	304
	147	190	181	217	295	282	297
	156	186	159	198	276	278	281

The figures for I.H.P. are "round." The "Medusa's" figures for 20 knots are from trial on Stokes Bay, and show the retarding effect of shallow water. The figures for the other ships for 20 knots are estimated for deep water.

More accurate methods than those above given for estimating the horse-power required for any proposed ship are: 1. Estimations calculated from the results of trials of "similar" vessels driven at "corresponding" speeds; "similar" vessels being those that have the same ratio of length to speeds; "similar" vessels being toose that have the same ratio of length of breadth and to draught, and the same coefficient of fineness, and "corresponding" speeds those which are proportional to the square roots of the lengths of the respective vessels. Froude found that the resistances of such vessels varied almost exactly as wetted surface × (speed)<sup>2</sup>.

2. The method employed by the British Admiralty and by some Clyde shipbuilders, viz., ascertaining the resistance of a model of the vessel, 12 to 20 ft. long, in a tank, and calculating the power from the results obtained.

Speed on Canals. A great loss of speed occurs when a steam-vessel

passes from open water into a more or less restricted channel. The average speed of vessels in the Suez Canal in 1882 was only 51/4 statute miles per hour.

(Eng'g. Feb. 15, 1884, p. 139.)
Estimated Displacement, Horse-power, etc.-The table on the next page, calculated by the author, will be found convenient for mak-

ing approximate estimates.

The figures in 7th column are calculated by the formula H.P.  $= S^3D^{\frac{3}{2}} + c$ , in which c = 200 for vessels under 200 ft. long when C = .65, and 210 when C = .55; c = 200 for vessels 200 to 400 ft. long when C = .75, 220 when C = .65, 240 when C = .55; c = 230 for vessels over 400 ft. long when C = .75, 250 when C = .65, 260 when C = .55,

The figures in the 8th column are based on 5 H.P. per 100 sq. ft. of wetted

surface

The diameters of screw in the 9th column are from formula D =3.31  $\sqrt[5]{I.H.P.}$ , and in the 10th column from formula  $D=2.71 \sqrt[5]{I.H.P.}$ 

To find the diameter of screw for any other speed than 10 knots, revolutions being 100 per minute, multiply the diameter given in the table by the 5th root of the cube of the given speed + 10. For any other revolutions per minute than 100, divide by the revolutions and multiply by 100.

To find the approximate horse-power for any other speed than 10 knots,

multiply the horse-power given in the table by the cube of the ratio of the

given speed to 10, or by the relative figure from table on p. 1006.

# Estimated Displacement, Horse-power, etc., of Steam-

3256	1111	·····	DIS	vesse	ls of Var	ions Si	zes.	., 01	steam-
-	1=~	3-	Ē	Displace-			d Horse-		Screw for 10
Length, feet.	Breadth,	Draught, feet, D	Coefficient of Fine- ness, C	$LBD \times C$	Wetted Surface $L(1.7D + BC)$	Calc.	Cale, trom		eed and 100 r minute.
fe e	3re	ran	f F	35	sq. ft.	from Dis-	Wetted	If Pitch =	If Pitch =
-		Q#	201	tons.		placem't.	Surface.	Diam,	1.4 Diam.
12	3	1.5	.55	.85	48	4.3	2.4	4.4	3.6
16 {	3	1.5	.55	1.13	64	5.2	3.2	4.6	3.8
10 {	4	2	.65	2.38	96	8.9	4.8	5.1	4.2
20 {	3	1.5	.55	1.41	80	6.0	4.0	4.7	3.9
1	4	1.5	.65	2.97 1.98	120 104	10.3	6.0 5.2	5.3 5	4.3
24 {	3.5	2	.65	4.01	152	7.5 12.6	7.6	5.5	4.1 4.5
	4	2	.55	3.77	168	11.5	8.4	5.4	4.4
30 {	5	2.5	.65	6,96	224	18.2	11.2	5.9	4.8
40 }	4.5	2	.55	5.66	235	15.1	11.8	5.7	4.7
40 }	6	2.5	.65	11.1	326	24.9	16.3	6.3	5.2
50 }	6	3	.55	14.1 26	420 558	27.8	21.0	6.4	5.4
1	8	3.5	.65 .55	26.4	621	43.9 42.2	27.9 31.1	7.1 7.0	5.8 5.7
60 }	10	4	.65	44.6	798	62.9	39.9	7.6	6.2
	iŏ	4	.55	44	861	59.4	43.1	7.5	6.1
70 }	12	4.5	.65	70.2	1082	85.1	54.1	8.1	6.6
80 ₹	12	4.5	.55	67.9	1140	79.2	57.0	7.9	6.5
00)	14	5	.65	104.0	1408	111	70 4	8.5	7.0
90 }	13 16	5 6	.55 .65	91.9 160	1408 1854	97 147	70.4 92.7	8.3	6.8 7.3
1	13	5	.55	103	1565	104	78.3	8.4	6.9
100	15	5.5	.65	153	1910	143	95.5	8.9	7 9
100)	17	6	.75	219	2295	202	115	9.6	7.8
ì	14	5.5	.55	145	2046	131	102	8.8	7.8 7.2 7.6
120 <	16	6	.65	214	2472	179	124	9.4	· 7.6
(	18	6.5	.75	301	2946	250	147	10	8.2
140	16 18	6.5	.55 .65	211 306	2660 3185	169 227	133 159	9.2 9.8	$\frac{7.4}{8.0}$
1403	20	7	.75	420	3766	312	188	10.5	8.5
1	17	6.5	.55	278	3264	203	163	9.6	7.8
160≺	19	7	.65	395	3880	269	194	10.1	8.3
1	21	7.5	.75	540	4560	368	228	10.8	8.8
100	20	7.5	.55	396	4122	257	206	10.1	8.2
180	22 24	7.5 8	.65 .75	552 741	4869 5688	337 455	243 284	10.6 11.3	8.2 8.7 9.2
}	22	7	.55	484	4800	257	240	10.1	8.2
200	25	7 8	.65	743	5970	373	299	10.8	8.8
1	28	9	.75	1080	7260	526	363	11.6	9.5
- (	28	8	.55	880	7250	383	363	10.9	8.9
250 {	32	10	.65	1486	9450	592	473	11.9	9.7
-	36 32	12 10	.75 .55	2314 1509	11850 10380	875 548	593 519	12.8 11.7	10.5 9.6
300 }	36	12	.65	2407	13140	806	657	12.6	10.4
1	40	14	.75	3600	17140	1175	857	13.6	11.1
ì	38	12	.55	2508	14455	769	723	12.5	10.2
350 ⊰	42	14	.65	3822	17885	1111	894	13.5	11.0
(	46	16	.75	5520 3872	21595 19200	1562 1028	1080 960	14.4 13.3	11.8 10.8
400	44 48	14 16	.55 .65	5705	23360	1451	1168	14.2	11.6
4007	52	18	.75	8023	27840	2006	1392	15.2	12.4
(	50	16	.55	5657	24515	1221	1226	13.7	11.2
450	54	18	.65	8123	29565	1616	1478	14.5	11.9
(	58	20	.75	11157	34875	2171	1744	15.4	12.6
F00 (	52	18	.55	7354	29600	1454	1480	14.2	11.6
500}	56 60	20 22	.65	10400 14143	35200 41200	1966 2543	1760 2060	15.1 15.9	12.4 13.0
{	56	20	.55	9680	36245	1747	1812	14.7	12.0
550	60	22	.65	13483	42735	2266	2137	15 5	12.7
1	64	24	.75	18103	49665	2998	2483	16.4	13.4
	60	22	.55	12446	42900	2065	2145	15.2	12.5
600 ₹	64	24 26	.65	17115	50220	2656	2511	15.4	13.1
- 1	68	126	.75	22731	58020	3489	2901	16.9	13.8

### THE SCREW-PROPELLER.

The "pitch" of a propeller is the distance which any point in a blade, describing a helix, will travel in the direction of the axis during one revolution, the point being assumed to move around the axis. The pitch of a propeller with a uniform pitch is equal to the distance a propeller will advance during one revolution, provided there is no slip. In a case of this kind, the term "pitch" is analogous to the term "pitch of the thread" of

an ordinary single-threaded screw.

an ordinary single-threader screw. Let P = pitch of screw in feet, R = number of revolutions per second,  $V = \text{velocity of stream from the propeller} = P \times R$ , v = velocity of the ship in feet per second, V - v = slip,  $A = \text{area in square feet of section of stream from the screw, approximately the area of a circle of the same diameter,$ From the screw, approximately the area of a circle of the same diameter,  $A \times V = \text{volume of water projected astern from the ship in cubic feet per second. Taking the weight of a cubic foot of sea-water at 64 lbs., and the force of gravity at 32, we have from the common formula for force of acceleration, viz.: <math>F = M \frac{v_1}{t} = \frac{W}{y} \frac{v_1}{t}$ , or  $F = \frac{W}{y} v_1$ , when t = 1 second,  $v_1$  being

the acceleration.

Thrust of screw in pounds = 
$$\frac{64AV}{22}(V-v) = 2AV(V-v)$$
.

Rankine (Rules, Tables, and Data, p. 275) gives the following: To calculate the thrust of a propelling instrument (jet, paddle, or screw) in pounds, multiply together the transverse sectional area, in square feet, of the stream driven astern by the propeller; the speed of the stream relatively to the snip in knots; the real slip, or part of that speed which is impressed on that stream by the propeller, also in knots; and the constant 5.66 for sea-water, or 5.5 for fresh water. If  $S = \mathrm{speed}$  of the screw in knots,  $s = \mathrm{speed}$  of ship in knots,  $s = \mathrm{speed}$  of the stream in square feet (of sea-water),

### Thrust in pounds = $A \times S(S - s) \times 5.66$ ,

The real slip is the velocity (relative to water at rest) of the water projected sternward; the apparent slip is the difference between the speed of the ship and the speed of the screw; i.e., the product of the pitch of the screw by the number of revolutions.

This apparent slip is sometimes negative, due to the working of the screw in disturbed water which has a forward velocity, following the ship. Negative apparent slip is an indication that the propeller is not suited to the

The apparent slip should generally be about 8% to 10% at full speed in wellformed vessels with moderately fine lines; in bluff cargo boats it rarely

exceeds 5%.

The effective area of a screw is the sectional area of the stream of water laid hold of by the propeller, and is generally, if not always, greater than the actual area, in a ratio which in good ordinary examples is 1.2 or thereabouts, and is sometimes as high as 1.4; a fact probably due to the stiffness of the water, which communicates motion laterally amongst its particles. (Rankine's Shipbuilding, p. 89.)

Prof. D. S. Jacobus, Trans. A. S. M. E., xi. 1028, found the ratio of the effective to the actual disk area of the screws of different vessels to be as

follows:

Size of Screw.-Seaton says: The size of a screw depends on so many things that it is very difficult to lay down any rule for guidance, and much must always be left to the experience of the designer, to allow for all the circumstances of each particular case. The following rules are given for ordinary cases. (Seaton and Rounthwaite's Pocket-book):

10133SP= pitch of propeller in feet  $=\frac{101338}{(1000-x)}$ , in which S= speed in knots, R= revolutions per minute, and x= percentage of apparent slip. For a slip of 10%, pitch  $=\frac{112.68}{R}$ .

$$D = \text{diameter of propeller} = K \sqrt{\frac{\text{I.H.P.}}{\left(\frac{P \times R}{100}\right)^3}}, K \text{ being a coefficient given}$$

in the table below. If 
$$K = 20$$
,  $D = 20000 \sqrt{\frac{\text{I.H.P.}}{(P \times R)^3}}$ 

Total developed area of blades =  $C_1 \sqrt{\frac{\overline{1.H.P.}}{R}}$ , in which C is a coefficient

to be taken from the table.

Another formula for pitch, given in Seaton's Marine Engineering, is  $P = \frac{C}{R} \sqrt[3]{\frac{\text{I.H.P.}}{D^2}}$ , in which C = 737 for ordinary vessels, and 660 for slow-

speed cargo vessels with full lines. Thickness of blade at root =  $\sqrt{\frac{d^3}{nb}} \times k$ , in which d = diameter of tail-

shaft in inches, n= number of blades, b= breadth of blade in inches where it joins the boss, measured parallel to the shaft axis; k=4 for cast iron, 1.5 for east steel, 3 for gun-metal, 1.5 for high-class bronze. Thickness of blade at tip: Cast iron, 40D+4 in.; cast steel .03D+4 in.; gun-metal, .03D+3 in.; high-class bronze, .02D+3 in., where D= diameter

of propeller in feet.

### Propeller Coefficients.

Description of Vessel.	Approximate Speed in knots.	Number of Screws.	Number of Blades per Screw.	Values of K.	Values of C.	Usual Material of Blades.
Bluff cargo boats	8-10	One	4	17 -17 5	19 -17-5	Cast iron
Cargo, moderate lines	10-13		4	18 -19	17 -15,5	
Pass, and mail, fine lines.	13-17	46	4	19.5-20.5	15 -13	C. I. or S.
6. 16 66 66 66	13-17	Twin	4	20.5-21-5	14.5-12.5	66 66 66
" " very fine.	17-22	One	4 3	21 -22	12.5-11	G. M. or B
	17-22	Twin	3	22 -23	10.5- 9	44 44 44
Naval vessels, " "	16-22	6.6	4	21 -22.5	11.5-10.5	46 66 66
	16-22	44	3	22 -23.5	8.5-7	
Torpedo-boats, " "	20-26	One	3	25	7- 6	B. or F. S.

C.,I., east iron; G. M., gun-metal; B., bronze; S., steel; F. S., forged steel. From the formulæ  $D=20000\sqrt{\frac{\text{I.H.P.}}{(P\times R)^3}}$  and  $P=\frac{737}{R}\sqrt[3]{\frac{\text{I.H.P.}}{D^2}}$ , if P=D

and R = 100, we obtain  $D = \sqrt[6]{400 \times \text{I.H.P.}} = 331 \sqrt[6]{\text{I.H.P.}}$ 

If P=1.4D and R=100, then  $D=\sqrt[6]{145.8\times I.H.P.}=2.71\sqrt[6]{I.H.P.}$  prom these two formulæ the figures for diameter of screw in the table on page 1009 have been calculated. They may be used as rough approximations to the correct diameter of screw for any given horse-power, for a speed of

to the correct diameter of screw for any given horse-power, for a speed of lo knots and 100 revolutions per minute.

For any other number of revolutions per minute multiply the figures in the table by 100 and divide by the given number of revolutions. For any other speed than 10 knots, since the 1.H.P., varies approximately as the cube of the speed, and the diameter of the screw as the 5th root of the LH.P., multiply the diameter given for 10 knots by the 5th root of the cube of one tenth of the given speed. Or, multiply by the following factors:

For speed of knots: 11 12 13 14 16 = .577 .660 .736 .807 .875 .939 1.059 1.116 1.170 1.224 1.275 1.327

Speed: 17 18 19 20  $\sqrt[5]{(S + 10)^3}$ 

= 1.375 1.423 1.470 1.515 1.561 1.605 1.648 1.691 1.733 1.774 1.815 1.855

For more accurate determinations of diameter and pitch of screw, the formulæ and coefficients given by Seaton, quoted above, should be used.

Efficiency of the Propeller.—According to Rankine, if the slip of the water be s, its weight W, the resistance R, and the speed of the ship v,

$$R = \frac{Ws}{a}$$
;  $Rv = \frac{Wsv}{a}$ .

This impelling action must, to secure maximum efficiency of propeller, be effected by an instrument which takes hold of the fluid without shock or disturbance of the surrounding mass, and, by a steady acceleration, gives the the required final velocity of discharge. The velocity of the propeller overcoming the resistance R would then be

$$\frac{v+(v+s)}{2}=v+\frac{s}{2};$$

and the work performed would be

$$R\left(v+\frac{s}{2}\right) = \frac{Wvs}{a} + \frac{Ws^2}{2a},$$

the first of the last two terms being useful, the second the minimum lost work; the latter being the wasted energy of the water thrown backward. The efficiency is

$$E = v \div \left(v + \frac{s}{2}\right);$$

and this is the limit attainable with a perfect propelling instrument, which

and this is the limit attainable with a perfect propeiling instrument, which ilmit is approached the more nearly as the conditions above prescribed are the more nearly fulfilled. The efficiency of the propelling instrument is probably rarely much above 0.80, and never above 0.80. In designing the screw-propeller, as was shown by Dr. Froude, the best angle for the surface is that of 45° with the plane of the disk; but as all parts of the blade cannot be given the same angle, it should, where practicable, be so proportioned that the "pitch-angle at the centre of effort" should be made 45°. The maximum possible efficiency is then, according

to Froude, 77%. In order that the water should be taken on without shock and discharged with maximum backward velocity, the screw must have an axially increas-

ing pitch. The true screw is by far the more usual form of propeller, in all steamers, both merchant and naval. (Thurston, Manual of the Steam-engine, part ii...

p. 176.) The combined efficiency of screw, shaft, engine, etc., is generelly taken at 5%. In some cases it may reach 60% or 65%. Rankine takes the effective H.P. to equal the I.H.P. ÷ 1.63.

### Pitch-ratio and Slip for Screws of Standard Form.

Pitch-ratio.	Real Slip of Screw.	Pitch-ratio.	Real Slip of Screw.
.8° .9 1.0 1.1	15.55 16.22 16.88 17.55	1.7 1.8 1.9 2.0	21.3 21.8 22.4 22.9
1.2 1.3 1.4 1.5	18.2 18.8 19.5 20.1 20.7	2.1 2.2 2.3 2.4 2.5	23.5 24.0 24.5 25.0 25.4

Results of Recent Researches on the efficiency of screw-propel-lear are summarized by S. W. Barnaby, in a paper read before section G of the Engineering Congress, Chicago, 1893. He states that the following gen-

eral principles have been established:

(a) There is a definite amount of real slip at which, and at which only, maximum efficiency can be obtained with a screw of any given type, and this amount varies with the pitch-ratio. The slip-ratio proper to a given ratio of pitch to diameter has been discovered and tabulated for a screw of a standard type, as below (see table on page 1012):

(b) Screws of large pitch-ratio, besides being less efficient in themselves, add to the resistance of the hull by an amount bearing some proportion to their distance from it, and to the amount of rotation left in the race.

(c) The best pitch-ratio lies probably between 1.1 and 1.5.
 (d) The fuller the lines of the vessel, the less the pitch-ratio should be.
 (e) Coarse-pitched screws should be placed further from the stern than

fine-pitched ones,

(f) Apparent negative slip is a natural result of abnormal proportions of propellers.

(g) Three blades are to be preferred for high-speed vessels, but when the diameter is unduly restricted, four or even more may be advantageously employed.

(h) An efficient form of blade is an ellipse having a minor axis equal to

four tenths the major axis.

(i) The pitch of wide-bladed screws should increase from forward to aft, but a uniform pitch gives satisfactory results when the blades are narrow, and the amount of the pitch variation should be a function of the width of the blade.

(j) A considerable inclination of screw shaft produces vibration, and with right-handed twin-screws turning outwards, if the shafts are inclined at

all, it should be upwards and outwards from the propellers.

For results of experiments with screw-propellers, see F. C. Marshall, Proc. Inst. M. E. 1881; R. E. Froude, Trans. Institution of Naval Architects, 1886; G. A. Calvert, Trans. Institution of Naval Architects 1887; and S. W. Barnaby, Proc. Inst. Civil Eng'rs 1890, vol. cii.

One of the most important results deduced from experiments on model screws is that they appear to have practically equal efficiencies throughout a wide range both in pitch-ratio and in surface-ratic; so that great latitude is left to the designer in regard to the form of the propeller. Another important feature is that, although these experiments are not a direct guide to the selection of the most efficient propeller for a particular ship, they support the selection of the most efficient propeller for a particular ship, they support the selection of the most efficient propeller for a particular ship, they support the selection of the most efficient propeller for a particular ship, they support and the selection of the most efficient propeller for a particular ship, they support and the selection of the most efficient propeller for a particular ship, they support and the selection of the most efficient propeller for a particular ship. ply the means of analyzing the performances of screws fitted to vessels, and of thus indirectly determining what are likely to be the best dimensions of screw for a vessel of a class whose results are known. Thus a great advance has been made on the old method of trial upon the ship itself, which was the origin of almost every conceivable erroneous view respecting the screw-propeller. (Proc. Inst. M. E., July, 1891.)

### THE PADDLE-WHEEL.

Paddle-wheels with Radial Floats. (Seaton's Marine Engineering.)-The effective diameter of a radial wheel is usually taken from the centres of opposite floats; but it is difficult to say what is absolutely that diameter, as much depends on the form of float, the amount of dip, and the waves set in motion by the wheel. The slip of a radial wheel is from 15 to 30 per cent, depending on the size of float.

Area of one float = 
$$\frac{\text{I.H.P.}}{D} \times C$$
.

D is the effective diameter in feet, and C is a multiplier, varying from 0.25 in tugs to 0.175 in fast-running light steamers.

The breadth of the float is usually about ¼ its length, and its thickness about ¼ its breadth. The number of floats varies directly with the diameter, and there should be one float for every foot of diameter.

(For a discussion of the action of the radial wheel, see Thurston, Manual

of the Steam-engine, part ii., p, 182.)

Feathering Paddle - wheels. (Seaton.) - The diameter of a feathering-wheel is found as follows: The amount of slip varies from 12 to 20 per cent, although when the floats are small or the resistance great it

is as high as 25 per cent; a well-designed wheel on a well-formed ship should not exceed 15 per cent under ordinary circumstances.

If K is the speed of the ship in knots, S the percentage of slip, and R the revolutions per minute,

Diameter of wheel at centres = 
$$\frac{K(100 + S)}{3.14 \times R}$$
.

The diameter, however, must be such as will suit the structure of the ship, so that a modification may be necessary on this account, and the revolutions altered to suit it.

The diameter will also depend on the amount of "dip" or immersion of

float.

When a ship is working always in smooth water the immersion of the top edge should not exceed \( \frac{5}{2} \) the breadth of the float; and for general service at sea an immension of \( \frac{5}{2} \) the breadth of the float is sufficient. If the ship is intended to earry cargo, the immersion when light need not be more than 2 or 3 inches, and should not be more than the breadth of float when at the deepest draught; indeed, the efficiency of the wheel falls off rapidly with the immersion of the wheel.

Area of one float = 
$$\frac{\text{I.H.P.}}{D} \times C$$
.

 $\it C$  is a multiplier, varying from 0.3 to 0.35;  $\it D$  is the diameter of the wheel to the float centres, in feet.

The number of floats  $= \frac{1}{2}(D+2)$ . The breadth of the float  $= 0.35 \times$  the length.

The thickness of floats = 1/12 the breadth.

Diameter of gudgeons = thickness of float. Seaton and Rounthwaite's Pocket-book gives:

Number of floats =  $\frac{60}{\sqrt{R}}$ ,

Number of floats = 
$$\frac{1}{\sqrt{R}}$$

where R is number of revolutions per minute.

Area of one float (in square feet) = 
$$\frac{\text{I.H.P.} \times 33000 \times K}{N \times (D \times R)^3}$$
,

where N = number of floats in one wheel.

For vessels plying always in smooth water K = 1200. For sea-going steamers K = 1400. For tugs and such craft as require to stop and start frequently in a tide-way K = 1600. It will be quite accurate enough if the last four figures of the cube

 $(D \times R)^3$  be taken as ciphers.

For illustrated description of the feathering paddle-wheel see Seaton's Marine Engineering, or Seaton and Rounthwaite's Pocket-book. The diameter of a feathering-wheel is about one half that of a radial wheel for equal efficiency. (Thurston.)

Efficiency of Paddle-wheels.—Computations by Prof. Thurston of the efficiency of propulsion by paddle-wheels give for light river steamers with ratio of velocity of the vessel,  $v_i$  to velocity of the paddle-float at centre of pressure,  $V_i$  or  $\frac{v}{V^i} = \frac{3}{4}$ , with a dip = 3/20 radius of the wheel, and a slip of 25 per cent, an efficiency of .714; and for ocean steamers with the same slip and ratio of  $\frac{v}{V}$ , and a dip =  $\frac{1}{3}$  radius, an efficiency of .685.

### JET-PROPULSION.

Numerous experiments have been made in driving a vessel by the reaction of a jet of water pumped through an orifice in the stern, but they have all resulted in commercial failure. Two jet-propulsion steamers, the "Waterwitch," 1100 tons, and the "Squirt," a small torpedo-boat, were built by the British Government. The former was tried in 1867, and gave an efficiency of apparatus of only 18 per cent. The latter gave a speed of 12 knots, as against 17 knots attained by a sister-ship having a screw and equal steam-power. The mathematical theory of the efficiency of the jet was discussed by Rankine in The Engineer, Jan. 11, 1867, and he showed that the greater the quantity of water operated on by a jet-propeller, the greater

is the efficiency. In defiance both of the theory and of the results of earlier experiments, and also of the opinions of many naval engineers, more than \$200,000 were spent in 1888-90 in New York upon two experimental boats, the "Prima Vista" and the "Evolution," in which the jet was made of very small Frina vista and the Evolution, in which the jet was made of very small size, in the latter case only 3/4-inch diameter, and with a pressure of 2500 lbs. per square inch. As had been predicted, the vessel was a total failure. (See article by the author in Mechanics, March, 1891.)

The theory of the jet-propeller is similar to that of the screw-propeller. If A = the area of the jet in square feet, V its velocity with reference to the The work does not the jet in square rees, 7 its velocity with reference to the earth, then the thrust of the jet (see Screw propeller, ante) is 2AV(V-v)v. The work done on the vessel is 2AV(V-v)v, and the work wasted on the rearward projection of the jet is  $\frac{1}{2}(2AV(V-v)^2)$ . The efficiency is  $\frac{2AV(V-v)v}{2}$ .

This expression equals unity when

 $2.4V(V-v)v + AV(V-v)^{2} = \frac{2.5}{V+v}.$ V=v, that is, when the velocity of the jet with reference to the earth, or V=v, that is, when the velocity of the jet with reference to the earth, or  $V=v_1=0$ ; but then the thrust of the propeller is also 0. The greater the value of V as compared with v, the less the efficiency. For V=20v, as was proposed in the "Evolution," the efficiency of the jet would be less than 10 per cent, and this would be further reduced by the friction of the pumping mechanism and of the water in pipes.

The whole theory of propulsion may be summed up in Rankine's words: "That propeller is the best, other things being equal, which drives astern the largest body of water at the lowest velocity."

It is practically impossible to devise any system of hydraulic or jet propulsion which can compare favorably, under these conditions, with the screw or the paddle-wheel.

Reaction of a Jet .- If a jet of water issues horizontally from a vessel, the reaction on the side of the vessel opposite the orifice is equal to the weight of a column of water the section of which is the area of the orifice, and the height is twice the head.

The propelling force in jet-propulsion is the reaction of the stream issuing from the orifice, and it is the same whether the jet is discharged under water, in the open air, or against a solid wall. For proof, see account of trials by C. J. Everett, Jr., given by Prof. J. Burkitt Webb, Trans. A. S. M. E., xii, 904.

### RECENT PRACTICE IN MARINE ENGINES.

(From a paper by A. Blechynden on Marine Engineering during the past Decade, Proc. Inst. M. E., July, 1891.)

Since 1881 the three-stage-expansion engine has become the rule, and the boiler-pressure has been increased to 160 lbs. and even as high as 200 lbs. per square inch. Four-stage-expansion engines of various forms have also been adopted.

Forced Draught has become the rule in all vessels for naval service, and is comparatively common in both passenger and cargo vessels. By this means it is possible considerably to augment the power obtained from a given boiler: and so long as it is kept within certain limits it need result in no injury to the boiler, but when pushed too far the increase is sometimes

purchased at considerable cost

In regard to the economy of forced draught, an examination of the appended table (page 1018) will show that while the mean consumption of coal in those steamers working under natural draught is 1.573 lbs. per indicated horse-power per hour, it is only 1,336 lbs. in those fitted with forced draught. This is equivalent to an economy of 15%. Part of this economy, however, may be due to the other heat-saving appliances with which the latter steamers are fitted.

Boilers. - As a material for boilers, iron is now a thing of the past, though it seems probable that it will continue yet awhile to be the material for tubes. Steel plates can be procured at 132 square feet superficial area and 11/2 inches thick. For purely boiler work a punching-machine has be-

come obsolete in marine-engine work,

The increased pressures of steam have also caused attention to be directed to the furnace, and have led to the adoption of various artifices in the shape of corrugated, ribbed, and spiral flues, with the object of giving increased strength against collapse without abnormally increasing the thickness of the plate. A thick furnace-plate is viewed by many engineers with great suspicion; and the advisers of the Board of Trade have fixed the limit of thickness for furnace-plates at §§ incl; ) but whether this limitation will stand in the light of prolonged experience remains to be seen. It is a fact generally accepted that the conditions of the surfaces of a plate are far greater factors in its resistance to the transmission of heat than either the material or the thickness. With a plate free from lamination, thickness being a mere secondary element, it would appear that a furnace-plate might be increased from ½ inch to §§ in the thickness without increasing its resistance more than 1½%. So convinced have some engineers become of the soundness of this view that they have adopted flues §§ inch thick.

Piston-valves.—Since higher steam: pressures have become common, piston-valves have become the rule for the high-pressure cylinder, and are not unusual for the intermediate. When well designed they have the great advantage of being almost free from friction, so far as the valve itself is concerned. In the earlier piston-valves it was customary to fit spring rings, which were a frequent source of trouble and absorbed a large amount of power in friction; but in recent practice it has become usual to fit spring-

less adjustable sleeves

For low-pressure cylinders piston-valves are not in favor; if fitted with spring rings their friction is about as great as and occasionally greater than that of a well-balanced slide-valve; while if fitted with springless rings there is always some lenkage, which is irrecoverable. But the large port-clearances inseparable from the use of piston-valves are most objectionable; and with triple engines this is especially so, because with the customary late cut-off it becomes difficult to compress sufficiently for insuring economy and smoothness of working when in "full gear," without some special device.

Steam-pipes.—The failures of copper steam-pipes on large vessels have drawn serious attention both to the material and the modes of construction of the pipes. As the brazed joint is liable to be imperfect, it is proposed to substitute solid drawn tubes, but as these are not made of large sizes two or more tubes may be needed to take the place of one brazed tube. Reinforcing the ordinary brazed tubes by serving them with steel or copper wire, or by hooping them at intervals with steel or iron bands, has been

tried and found to answer perfectly.

Auxiliary Supply of Fresh Water—Evaporators,—To make up the losses of water due to escape of steam from safety-valves leakage at glands, joints, etc., either a reserve supply of fresh water is carried in tanks, or the supplementary feed is distilled from sea-water by special apparatus provided for the purpose. In practice the distillation is effected by passing steam, say from the first receiver, through a nest of tubes inside a still or evaporator, of which the steam-space is connected either with the second receiver or with the condenser. The temperature of the steam inside the tubes being higher than that of the steam either in the second receiver or in the condenser, the result is that the water inside the still is evaporated, and passes with the rest of the steam into the condenser, energy the production of the steam into the condenser, there it is condensed and serves to make up the loss. This plan localizes the trouble of the deposit, and frees it from its dangerous character, because an evaporator cannot become overheated like a boiler, even though it be neglected until its salts up solid; and if the same precautions are taken in working the evaporator which used to be adopted with low-pressure boilers when they were feel with salt water, no serious trouble should result.

fed with salt water, no serious trouble should result.

Welr's Feed-water Heater,—The principle of a method of heating feed-water introduced by Mr. James Weir and widely adopted in the marine service is founded on the fact that, if the feed-water as it is drawn from the hot-well be raised in temperature by the heat of a portion of steam introduced into it from one of the steam-receivers, the decrease of the coal necessary to generate steam from the water of the higher temperature bears a greater ratio to the coal required without feed-heating than the power which would be developed in the cylinder by that portion of steam would be are to the whole power developed when passing all the steam through all the cylinders. Suppose a triple-expansion engine were working under the following conditions without feed-heating; bolier-pressure 150 lbs; It H.P. in high-pressure cylinder 398, in intermediate and low-pressure cylinders together 790, total 1188. The temperature of hot-well 100° F. Then with feed-heating the same engine might work as follows: the feed might be heated to 230° F., and the percentage of steam from the first receiver required to heat it would be 10.9%; the I.H.P. in the h.p. cylinder would be as before 398, and in the three cylinders it would be 10.3, or 38% of the power developed without

feed-heating. Meanwhile the heat to be added to each pound of the feed-water at 200° F. for converting it into steam would be 1005 units against 1125 units with feed at 100° F., equivalent to an expenditure of only 89.4% of the heat required without feed-heating. Hence the expenditure of heat in relation to power would be 89.4 + 93.0 = 96.4%, equivalent to a heat economy of 3.6%. If the steam for heating can be taken from the low-pressure receiver, the economy is about doubled.

### Passenger Steamers fitted with Twin Screws.

Vessels.	th be- in Per- liculars.		Cylinders, tw in all.	o sets	r- sure sq. in,	ated e-power
	Lengi twee	Beam.	Diameters.	Stro.	Boile pres per	Indicated Horse-po
	Feet	Feet	Inches	In.	Lbs.	I.H.P.
City of New York }	525	631/4	45, 71, 113	60	150	20,000
Majestic (	565	58	43, 68, 110	60	180	18,000
Normannia	500 463½	571/2 551/2	40, 67, 106 41, 66, 101	66 66	160 160	11,500 12,500
" "Japan	440	51	32, 51, 82	54	160	10,125
OrelScot	415 460	48 54½	34, 54, 85 34½, 57½, 92	51 60	160 170	10,000 11,656

# Comparative Results of Working of Marine Engines, 1872, 1881, and 1891.

Boilers, Engines, and Coal.	1872.	1881.	1891.
Boiler-pressure, lbs. per sq. in Heating-surface per horse-power, sq. ft. Revolutions per minute, revs. Piston-speed, feet per min. Coal per horse-power per hour, lbs.	4.410 55.67 376	77.4 3.917 59.76 467 1.828	158.5 3.275 63.75 529 1 522

### Weight of Three-stage-expansion Engines in Nine Steamers in Relation to Indicated Horse-power and to Cylinder-capacity.

er.		eight chine		Rela	ıtive We	ight of	Machin	iery.	
No. of Steamer.	Engine- room.	Boiler- room.	Total.		licated F power.	Iorse.	e-room 3u. ft. linder- acity.	0 sq. ft.	Type of Machinery.
No. 0	Eng	Bo	T	Engine- room.	Boiler- room.	Total	Engine-r per cu. of Cylin capaci	Boile per 10 of He	
	tons.	tons.	tons.	lbs.	lbs.	lbs.	tons.	tons.	
1	681	662	1343	226	220	446	1.30	3.75	Mercantile
1 2 3 5 6	638	619	1257	259	251	510	1.46	4.10	
3	134	128	262	207	198	405	1.23	3.23	
5	38.8			170	203	373	1.29	3.30	
9	719	695	1414	167	162	329	1.41	3.44	
6	75.2	107.8	183	141	202	343	1.37	3.37	
7	44	61	105	77	108	185	1.21	2.72	Naval horizontal
8	73.5	109	182.5	78	116	194	1.11	2.78	do.
9	565	429	691	62.5	102	165	0.82	2.70 {	Naval vertical

		ks.	Remar	ншшш	н	шш	нн	рапри	
Sugen.)		ana .q.	Coal bn Per I.H per hou	1.836 1.836 1.836 1.836	1.75	1.494	1.510	1,558 1,400 1,400 1,400 1,400 1,230 1,242 1,235	1.522
(A. Biecnynden.)	-	10.J	Coal bu per sq. f grate l grate l	į.				28.55.55.55.55.55.55.55.55.55.55.55.55.55	17.08 13.92 28.15
	rials.	r sq.	og H.H.I 13 lo Ji	1.H.P. 6.86 7.03 6.65 7.08	2 % & C	38.8	12.03 12.03 12.03 12.03	10000 888 100000 100000 100000	8.91 20.98
earme	Results of Trials	ng-	Per Ib. of Coal per hour.	<del></del>				852383828888888888888888888888888888888	2.25 1.72
	Res	Heating- surface.	Per A.H.I	sq. ft. 4.11 4.21 3.95	486	3.055	323223	40.49.90.90.19.90.90.00.00.00.00.00.00.00.00.00.00.00	3.275 3.560 2.412
I wenty-eight steamers.		pə	teoibal .q.H	LH.P. 4295 4402 3587 3822	2008	2850 2800 2800	1100 1100 1680 2360 556	2000 1727 1727 1727 1250 1250 1250 1800 1800 1800 2600 2600 2600 2600 2600	
Me		,nim	Piston-sp Ft. per	ff. 627 630 630 631	3822	50 <del>4</del> 553	258 258 258 258 258 258 258 258 258 258	55555555555555555555555555555555555555	ıt.
111			JalovəX rəq Junim	revs. 52.2 51.3 57.3	25.45 8.45 8.45	56 61.5	53.8 53.8 5.8 5.8 5.8	#886445 <b>48888</b> 66	Average of all twenty-eight " natural draught " forced draught
Engines in			Stean	155 155 155 155 155 155	2823	388	22222	222222222222222222222222222222222222222	f all twe
	Boilers.	ere.	rg-9-ri4 39-rA	sq. ft. 626 626 540 540		398	186888	2 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1 1	erage o
Sing		.9g	Heati	sq. ft. 17,640 17,640 15,107 15,107	8,972 6,162 8,350	8,000	20,192 6,164 6,950 960 960	8,5,24 6,618 6	Av
e-ex	dler.		Pitch	78888 8886 9666				233287763265555 000000000000000000000000000000000	
Amree-stage-expansion	Propeller	ter.	Disme	T22288			:	2677777777575	
	Con- denser	-ang	Cooling face.	3q. ft. 11,586 11,000 11,000	3,209	3,900	12,2,2,4 2,5,6,2 2,0,0 2,0,0 2,0,0 2,0,0 2,0,0 2,0,0 2,0,0 2,0 3,0 3,0 3,0 3,0 3,0 3,0 3,0 3,0 3,0 3	2,700 2,700	
2		.92	Strop	ins. 66 22 23.	3288	22.23	22223	241848358483584 466848354848354	
r at ticulars	Cylinders.		Diameter.	ins. 66 61 61	8444	3444	:8:2 <b>:</b> 2:3:3	23. 24. 04. 174. 174. 174. 174. 174. 174. 174. 17	
								828888888888888888888888888888888888888	

Remarks.-D, forced draught; H, feed-heater.

Dimensions, Indicated Horse - power, and Cylinder - capacity of Three-stage - expansion Engines in Nine

St	eamer	s.										
er of mer.	de or Screws.		Cyli	nde	rs.	Revolutions per minute.	r- ssure sq.jin.	Indicated orse-power. Cylinder-capacity.		Heating-sur- face.		
Number of Steamer.	Single o	Diameters.		Stroke	Revol per n	Boiler pres per s	Indi	Cylinde	Total.	Per I.H.P.		
			ins.		ins.	revs.	lbs.	I.H.P.	cu.ft.	sq. ft.	sa. ft.	
1	Single	40	66	100	72	64.5	160	6751	522	17,640	sq. ft. 2.62	
2 3 4 5 6 7 8 9	**	39	61	97	66	67.8	160	5525	436	15,107	2.73	
3	44	23	38	61	42	83		1450	109	3,973	2.73	
4	41	17	261	6 42	24	90	150	510	30	1,403	2.75	
5	Twin	33	54	85	54	88	160	9625	508	20,193	2.10	
6	**	15	24	38	27	113	150	1194	55	3,200	2.68	
7	Single	20 30 45			191	145	1265	36.3	2,227	1.76		
8	Twin	181/2 29 43		24	182.5	140	2105	66.2	3,928	1.87		
9	**	331/2	49	74	39	145	150	9400	319	15,882	1.62	

## CONSTRUCTION OF BUILDINGS.\*

(Extract from the Building Laws of the City of New York, 1893.)

Walls of Warehouses, Stores, Factories, and Stables.—25 feet or less in width between walls, not less than 12 in, to height of 40 ft.; If 40 to 60 ft. in height, not less than 16 in, to 40 ft., and 12 in, thence to top; 60 to 80 "" 20 " 25 ", and 12 in, thence to top;

44 75 to 85 .. 24

20 ft.; 20 in. to 60 ft., and 16 in. to top:

85 to 100 ft. in height, not less than 28 in. to 25 ft.; 24 in. to 50 ft.; 20 in to 75 ft., and 16 in. to top; Over 100 ft. in height, each additional 25 ft. in height, or part thereof, next

above the curb, shall be increased 4 inches in thickness, the upper 100 feet remaining the same as specified for a wall of that weight.

If walls are over 25 feet apart, the bearing-walls shall be 4 inches thicker than above specified for every 12½ feet or fraction thereof that said walls are more than 25 feet apart

Strength of Floors, Roofs, and Supports.

Floors calculated to bear safely per sq. ft., in addition to their own weight.

Floors of dwelling, tenement, apartment-house or hotel, not less than ... 70 lbs. 100 \*\* 64 120 150 6.0 store, factory, warehouse, etc., not less than ... ... Roofs of all buildings, not less than ... .... 50

Every floor shall be of sufficient strength to bear safely the weight to be imposed thereon, in addition to the weight of the materials of which the floor is composed.

Columns and Posts. - The strength of all columns and posts shall be computed according to Gordon's formulæ, and the crushing weights in pounds, to the square inch of section, for the following-named materials, shall be taken as the coefficients in said formulæ, namely: Cast iron, 80,000;

\*The limitations of space forbid any extended treatment of this subject. Much valuable information upon it will be found in Trautwine's Civil Engineer's Pocket-book, and in Kidder's Architect's and Builder's l'ocket-book. The latter in its preface mentions the following works of reference: "Notes The latter in its preface mentions the following works of reference: "Notes on Building Construction," 3 vols., Rivingtons, publishers, Boston, 'Building Superintendence,' by T. M. Clark (J. R. Osgood & Co., Boston), "The American House Carpenter," by R. G. Hatfield; "Graphical Analysis of Roof-trusses," by Prof. C. E. Greene; "The Fire Protection of Mills," by C. J. H. Woodbury; "House Drainage and Water Service," by James C. Bayles; "The Builder's Guide and Estimator's Price-book," and "Plaster-by West-based (Carpenter)." In Proceedings of the Control of Carpenter (Carpenter). ing Mortars and Cements," by Fred. T. Hodgson; "Foundations and Concrete Works," and "Art of Building," by E. Dobson, Weale's Series, London.

wrought or rolled iron, 40,000; rolled steel, 48,000; white pine and spruce, 3500; pitch or Georgia pine, 5000; American oak, 6000. The breaking strength of wooden beams and girders shall be computed according to the formulæ in which the constants for transverse strains for central load shall be as follows, namely: Hemlock, 400; white pine, 450; spruce, 450; pitch or Georgia pine, 550; American oak, 550; and for wooden beams and girders carrying a uniformly distributed load the constants will be doubled. The factors of safety shall be as one to four for all beams, girders, and other pieces subject to a transverse strain; as one to four for all posts, columns, and other vertical supports when of wrought iron or rolled steel; as one to five for other materials, subject to a compressive strain; as one to six for tierods, tie-beams, and other pieces subject to a tensile strain. Good, solid, natural earth shall be deemed to safely sustain a load of four tons to the superficial foot, or as otherwise determined by the superintendent of buildings, and the width of footing-courses shall be at least sufficient to meet this requirement. In computing the width of walls, a cubic foot of brickwork shall be deemed to weigh 115 lbs. Sandstone, white marble, granite, and other kinds of building-stone shall deemed to weigh 160 lbs. per cubic foot. The safe-bearing load to apply to good brickwork shall be taken at 8 tons per superficial foot when good lime mortar is used, 11½ tons per superficial foot when good lime and cement mortar mixed is used, and 15 tons per sup-

erficial foot when good cement mortar is used

Fire-proof Buildings-Iron and Steel Columns,-All castiron, wrought-iron, or rolled-steel columns shall be made true and smooth at both ends, and shall rest on iron or steel bed-plates, and have iron or steel cap-plates, which shall also be made true. All iron or steel trimmerbeams, headers, and tail-beams shall be suitably framed and connected together, and the iron girders, columns, beams, trusses, and all other ironwork of all floors and roofs shall be strapped, bolted, anchored, and connected together, and to the walls, in a strong and substantial manner. Where beams are framed into headers, the angle-irons, which are bolted to the tail-beams, shall have at least two bolts for all beams over 7 inches in depth, and three bolts for all beams 12 inches and over in depth, and these bolts shall not be less than 34 inch in diameter. Each one of such angles or knees, when bolted to girders, shall have the same number of bolts as stated for the other leg. The angle-iron in no case shall be less in thickness than the header or trimmer to which it is bolted, and the width of angle in no case shall be less than one third the depth of beam, excepting that no angle-knee shall be less than 2½ inches wide, nor required to be more than 6 inches wide. All wroughtiron or rolled-steel beams 8 inches deep and under shall have bearings equal to their depth, if resting on a wall: 9 to 12 inch beams shall have a bearing of 10 inches, and all beams more than 12 inches in depth shall have bearings of not less than 12 inches if resting on a wall. Where beams rest on iron supports, and are properly tied to the same, no greater bearings shall be required than one third of the depth of the beams. Iron or steel floor-beams shall be so arranged as to spacing and length of beams that the load to be supported by them, together with the weights of the materials used in the construction of the said floors, shall not cause a deflection of the said beams of more than 1,30 of an inch per linear foot of span; and they shall be tight together at intervals of not more than eight times the depth of the beam.

Under the ends of all iron or steel beams, where they rest on the walls, a stone or cast-iron template shall be built into the walls. Said template shall be 8 inches wide in 12 inch walls, and in all walls of greater thickness said template shall be 12 inches wide; and such templates, if of stone, shall not be in any case less than 21/2 inches in thickness, and no template shall be less

than 12 inches long.

No cast-iron post or column shall be used in any building of a less average thickness of shaft than three quarters of an inch, nor shall it have an unsupported length of more than twenty times its least lateral dimensions or diameter. No wrought-iron or rolled-steel column shall have an unsupported length of more than thirty times its least lateral dimension or diameter, nor

shall its metal be less than one fourth of an inch in thickness.

Lintels, Bearings and Supports,—All iron or steel lintels shall have bearings proportionate to the weight to be imposed thereon, but no lintel used to span any opening more than 10 feet in width shall have a bearing less than 12 inches at each end, if resting on a wall; but if resting on an iron post, such lintel shall have a bearing of at least 6 inches at each end, by the thickness of the wall to be supported

Strains on Girders and Rivets .- Rolled iron or steel beam gir-

ders, or riveted iron or steel plate girders used as lintels or as girders, carrying a wall or floor or both, shall be so proportioned that the loads which may come upon them shall not produce strains in tension or compression upon the flanges of more than 12,000 lbs. for iron, nor more than 15,000 lbs. for steel per square inch of the gross section of each of such lagon loss. For steen per square inch of the gross section of each of steen flanges, nor a shearing strain upon the web-plate of more than 6000 lbs. per square inch of section of such web-plate, if of iron, nor more than 7000 pounds if of steel; but no web-plate shall be less than ½ inch in thickness. Rivets in plate girders shall not be less than ½ inch in diameter, thickness. Rivers in plate gracers shall not be less than \( \gamma\_1 \) inch in diameter, and shall not be spaced more than 6 inches apart in any case. They shall be so spaced that their shearing strains shall not exceed 9000 lbs, per square inch, on their diameter, multiplied by the thickness of the plates through which they pass. The riveted plate girders shall be proportioned upon the supposition that the bending or corod strains are resisted entirely by the upper and lower flanges, and that the shearing strains are resisted entirely by the web-plate. No part of the web shall be estimated as flange area, nor more than one half of that portion of the angle-iron which lies against the web. The distance between the centres of gravity of the flange areas will be considered as the effective depth of the girder.

The building laws of the City of New York contain a great amount of detail in addition to the extracts above, and penalties are provided for viola-tion. See An Act creating a Department of Buildings, etc., Chapter 275, Laws of 1892. Pamphlet copy published by Baker, Voorhies & Co., New

York.

### MAXIMUM LOAD ON FLOORS.

(Eng'g, Nov. 18, 1892. p. 644.)—Maximum load per square foot of floor surface due to the weight of a dense crowd. Considerable variation is apparent in the figures given by many authorities, as the following table shows:

Authorities.	Weight of Crov
French practice, quoted by Trautwine and Stoney	41
Hatfield ("Transverse Strains," p. 80)	
Mr. Page, London, quoted by Trautwine	84
Maximum load on American highway bridges according	to
Waddell's general specifications	100
Mr. Nash, architect of Buckingham Palace	
Experiments by Prof. W. N. Kernot, at Melbourne	126
Experiments by Mr. B. B. Stoney ("On Stresses," p. 617)	147.4

The highest results were obtained by crowding a number of persons previously weighed into a small room, the men being tightly packed so as to resemble such a crowd as frequently occurs on the stairways and platforms of a theatre or other public building.

### STRENGTH OF FLOORS.

(From circular of the Boston Manufacturers' Mutual Insurance Co.) (From circular of the boston manufacturers mutual insurance Co.)
The following tables were prepared by C. J. H. Woodbury, for determining
safe loads on floors. Care should be observed to select the figure giving the
greatest possible amount and concentration of load as the one which may
be put upon any beam or set of floor-beams; and in no case should beams be
subjected to greater loads than those specified, unless, a lower factor of safety is warranted under the advice of a competent engineer.

Whenever and wherever solid beams or heavy timbers are made use of in the construction of a factory or warehouse, they should not be painted, varnished or olled, filled or eneased in impervious concrete, air-proof plastering, or metal for at least three years, lest fermentation should destroy them by what is called "dry rot."

It is, on the whole, safer to make floor-beams in two parts, with a small

open space between, so that proper ventilation may be secured, even if the outside should be inadvertently painted or filled.

These tables apply to distributed loads, but the first can be used in respect to floors which may carry concentrated loads by using half the figure given in the table, since a beam will bear twice as much load when evenly distributed over its length as it would if the load was concentrated in the centre

The weight of the floor should be deducted from the figure given in the table, in order to ascertain the net load which may be placed upon any floor. The weight of spruce may be taken at 36 lbs. per cubic foot, and that of Southern pine at 48 lbs. per cubic foot.

Table I was computed upon a working modulus of rupture of Southern pine at 2160 lbs., using a factor of safety of six. It can also be applied to ascertaining the strength of spruce beams if the figures given in the table are multiplied by 0.76; or in designing a floor to be sustained by spruce beams, multiply the required load by 1.28, and use the dimensions as given by the table

Theses tables are computed for beams one inch in width, because the strength of beams increases directly as the width when the beams are broad

enough not to cripple.

EXAMPLE.—Required the safe load per square foot of floor, which may be safely sustained by a floor on Southern pine  $10 \times 14$  inch beams, 8 feet on entres, and 20 feet span. In Table I a I  $\times$  14 inch beam, 20 feet span, will sustain 118 lbs. per foot of span; and for a beam 10 inches wide the load would be 1180 lbs. per foot of span; or 147% lbs, per square foot of floor for Southern-pine beams. From this should be deducted the weight of the floor. which would amount to 171/2 lbs. per square foot, leaving 130 lbs. per square foot as a safe load to be carried upon such a floor. If the beams are of spruce, the result of 147½ lbs, would be multiplied by 0.78, reducing the load to 115 lbs. The weight of the floor, in this instance amounting to 16 lbs., would leave the safe net load as 90 lbs, per square foot for spruce beams,

Table II applies to the design of floors whose strength must be in excess of that necessary to sustain the weight, in order to meet the conditions of

of that necessary to sustain the weight, in order to meet the conditions of delicate or rapidly moving machinery, to the end that the vibration or distortion of the floor may be reduced to the least practicable limit. In the table the limit is that of load which would cause a bending of the beams to a curve of which the average radius would be 1250 feet.

This table is based upon a modulus of elasticity obtained from observations upon the deflection of loaded storchouse floors, and is taken at 2,000,000 lbs. for Southern pine; the same table can be applied to spruce, whose modulus of elasticity is taken as 1,200,000 lbs., if six tenths of the load for Southern pine is taken as the proper load for spruce; or, in the matter of designing, the load should be increased one and two thirds times, and the dimension of timbers for this increased load as found in the table should be

used for spruce.

It can also be applied to beams and floor-timbers which are supported at each end and in the middle, remembering that the deflection of a beam supported in that manner is only four tenths that of a beam of equal span which rests at each end; that is to say, the floor-planks are two and one half times as stiff, cut two bays in length, as they would be if cut only one bay in length. When a floor-plank two bays in length is evenly loaded, three sixteenths of the load on the plank is su-tained by the beam at each end of the plank, and ten sixteenths by the beam under the middle of the plank; so that for a completed floor three eighths of the load would be sustained by the beams under the joints of the plank, and five eighths of the load by the beams under the middle of the plank: this is the reason of the importance of breaking joints in a floor-plank every three feet in order that each beam shall receive an identical load. If it were not so, three eighths of the whole load upon the floor would be sustained by every other beam, and five eighths of the load by the corresponding afternate beams.

Repeating the former example for the load on a mill floor on Sonthern-pine beams 10 × 14 inches, and 20 feet span, laid 8 feet on centres: In Table II a 1 × 14 inch beam should receive 61 lbs. per foot of span, or 75 lbs. per sq. ft. of floor, for Southern-pine beams. Deducting the weight of the floor, 174 bs. per sq. ft., leaves 57 lbs. per sq. ft. as the advisable load. If the beams are of spruce, the result of 75 bs. should be multiplied by 0.6, reducing the load to 48 lbs. The weight of the floor, in this instance amount-ing to 16 lbs., would leave the cit load as 20 lbs. for spruce beams.

If the beams were two spans in length, they could, under these conditions, support two and a half times as much load with an equal amount of deflec-

tion, unless such load should exceed the limit of safe load as found by Table I, as would be the case under the conditions of this problem.

Mill Columns. - Timber posts offer more resistance to fire than iron pillars, and have generally displaced them in millwork. Experiments made on the testing-machine at the U. S. Arsenal at Watertown, Mass, show that sound timber posts of the proportions customarily used in millwork yield by direct crushing, the strength being directly as the area at the smallest part. The columns yielded at about 4500 lbs. per square inch, confirming the general practice of allowing 600 lbs. per square inch, as a safe load. Square columns are one fourth stronger than round ones of the same diameter.

# I. Safe Distributed Loads upon Southern-pine Beams One Inch in Width,

(C. J. H. Woodbury.)

(If the load is concentrated at the centre of the span, the beams will sustain half the amount as given in the table.)

	and the desired of given in the desire,														
feet.	Depth of Beam in inches.														
Span, f	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16
$^{\mathrm{S}}$	Load in pounds per foot of Span.														
5	38	86	154		346						1	Ì			
5 6 7 8	27	60	107	167	240			540	667	807					
7	20	44	78	122	176				490	593					
8	15	34	60	94	135				375	454			735	0.00	-
		27	47	74	107	145		240	296	359	427	501	581	667	759
10		22	38		86			194	240	290	346	406	470	540	614
11			32	50	71	97	127	161	198	240	286	335	389	446	508
12			27	42	60	82	107	135	167	202	240	282	327	875	474
13				36	51	70	90	115	142	172	205	240	278	320	364
14	• • • •			31	44	60	78	99	123	148 129	176	207 180	240 209	276 240	314 273
15				27	38	52	68	86 76			154 135				
16 17					34 30	46	60 53	67	94 83	113 101	120	158 140	184 163	211 187	240
18						41 36	47	60	74	90	107	125	145	167	217 190
19	• • • •	• • • • •			• • •	30	43	54	66	80	96	112	130	150	170
20		•••			• •		38	49	60	73	86	101	118	135	154
21	• • • • •						90	44	541	66	78	92	107	122	139
22	• • • •	•••			•••			44	50	60	71	84	97	112	127
23	• • • • •	••			• • • • •				45	55	65	77	89	102	116
24	••••	• • • •				• • •				50	60	70	82	94	107
25					-				••	46	55	65	75	86	98
20 1							1	1		401	JUJ	0.01	(10)	00 1	90

# II. Distributed Loads upon Southern-pine Beams suffi-cient to produce Standard Limit of Deflection.

(C. J. H. Woodbury.)

-	_															
set.		-				Dept	h of	Bear	m in	inch	es.					on,
Span, feet.	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	Deflection, inches.
Sp	_				Loa	d in	poun	ds p	er fo	ot of	Spa	n.				Dei
5 6 7 8 9 10 11 12 13 14 15	3	10	23	44	77	122	182	259	0.00					1	<u> </u>	.0300
0	2	7 5	16	31 23	53 39	85	126 93	180 132	247 181	0.41						.0432
8		4	9	17	30	62 48	71	101	139	241 185	240	305				.0588
ă		4	7	14	24	38	56	80		146	190	241	301			.0972
10			6	îĩ	19	30	46	65	.89	118	154	195	244	300		.1200
11			l	9	16	25	38	54	73	98	127	161	505	248	301	.1452
12					13	21	32	45	62	82	107	136		208	253	.1728
13					11	18	27	38	53	70	91	116	144	178	215	.2028
14						16	23	33	45	60	78	100	124	153	186	.2352
15						14	20	29	40	53	68	87	108	133	162	.2700
16							18	25	35	46	60	76	95	117	147	.3072
17							16	22	3,1	41	53	68	84	104	126	.3468
18								20	27	37	47	60	75	93	112	.3888
19 20	•••				• • • • •		• • • •	18	25	33 30	43 38	54 49	68	83	101	.4332
21	• •							••••	22	27	35	49	55	75 68	91 83	.4800
99									20	24	32	40	.50	62	75	.5808
22 23										22	29	37	46	57	69	.6348
24											27	34	42	52	63	.6912
25		1.									25	31	39	48	58	7500
730	-								-							******

### ELECTRICAL ENGINEERING.

### STANDARDS OF MEASUREMENT.

# C.G.S. (Centimetre, Gramme, Second) or "Absolute" System of Physical Measurements:

Unit of space or distance = 1 centimetre, cm.; Unit of mass = 1 gramme, gm.;

Unit of time = 1 second, s.:

Unit of velocity = space + time = 1 centimetre in 1 second; Unit of acceleration = change of 1 unit of velocity in 1 second;

Unit of acceleration = change of 1 third of vectory in 1 second; Acceleration due to gravity, at Paris, = 981 centimetres in 1 second; Unit of force = 1 dyne =  $\frac{1}{981}$  gramme =  $\frac{.0020946}{981}$  lb. = .000002247 lb.

A dyne is that force which, acting on a mass of one gramme during one second, will give it a velocity of one centimetre per second. The weight of one gramme in latitude 40° to 45° is about 980 dynes, at the equator 973 dynes, and at the poles nearly 984 dynes. Taking the value of g, the acceleration due to gravity, in British measures at 32.185 feet per second at Paris, and the metre = 39.37 inches, we have

 $1 \text{ gramme} = 32.185 \times 12 + .3937 = 981.00 \text{ dynes}.$ 

Unit of work = 1 erg = 1 dyne-centimetre = .00000007373 foot-pound;

Unit of power = 1 watt = 10 million ergs per second, = .7373  $\frac{1}{550} = \frac{1}{746}$  of 1 horse-power = .00134 H.P.

C.G.S. Unit of magnetism = the quantity which attracts or repels an equal quantity at a centimetre's distance with the force of 1 dyne.

C.G.S. Unit of electrical current = the current which, flowing through a length of 1 centimetre of wire, acts with a force of 1 dyne upon a unit of magnetism distant 1 centimetre from every point of the wire. The ampere, the commercial unit of current, is one tenth of the C.G.S. unit.

The Practical Units used in Electrical Calculations are:

Ampere, the unit of current strength, or rate of flow, represented by C.

Volt, the unit of electro-motive force, electrical pressure, or difference of potential, represented by E.

Ohm, the unit of resistance, represented by R.
Coulomb (or ampere-second, the unit of quantity, Q.
Ampere-horse 260 coulombs, Q.
Watt (ampere-volt, or volt-ampere), the unit of power, P.
Joule (volt-coulomb), the unit of energy or work, W.

Joint (off-country), represented by K.

Henry, the unit of capacity, represented by K.

Henry, the unit of induction. expressed by the following formulæ, in which t represents one second and T one hour:

$$C=rac{E}{R}, \quad Q=Ct, \quad Q'=CT, \quad K=rac{Q}{E}, \quad W=QE, \quad P=CE.$$

As these relations contain no coefficient other than unity, the letters may represent any quantities given in terms of those units. For example, if E represents the number of volts electro-motive force, and R the number of ohms resistance in a circuit, then their ratio E+R will give the number of amperes current strength in that circuit. The above six formulæ can be combined by substitution or elimination, so as to give the relations between any of the quantities. The most important of these are the following:

$$\begin{split} Q &= \frac{E}{R}t, \quad K = \frac{C}{E}t, \quad W = CEt = \frac{E^2}{R}t = C^2Rt = Pt, \\ P &= \frac{E^2}{R} = C^2R = \frac{W}{t} = \frac{QE}{t}, \end{split}$$

The definitions of these units as adopted at the International Electrical Congress at Chicago in 1893, and as established by Act of Congress of the

United States, July 12, 1894, are as follows:
The ohm is substantially equal to 10 (or 1,000,000,000) units of resistance of the C.G.S. system, and is represented by the resistance offered to an unvarying electric current by a column of mercury at 32° F., 14.4521 grammes in mass, of a constant cross-sectional area, and of the length of 106.3 centimetres.

The ampere is 1/10 of the unit of current of the C.G.S. system, and is the practical equivalent of the unvarying current which when passed through a solution of nitrate of silver in water in accordance with standard speci-

fications deposits silver at the rate of .001118 gramme per second.

The volt is the electro-motive force that, steadily applied to a conductor whose resistance is one ohm, will produce a current of one ampere, and is practically equivalent to 1000/1434 (or. 6974) of the electro-motive force between the poles or electrodes of a Clark's cell at a temperature of 15° C, and prepared in the manner described in the standard specifications.

The coulomb is the quantity of electricity transferred by a current of one

ampere in one second.

The farad is the capacity of a condenser charged to a potential of one

volt by one coulomb of electricity.

The joule is equal to 10,000,000 units of work in the C.G.S. system, and is practically equivalent to the energy expended in one second by an ampere in an ohm.

The watt is equal to 10,000,000 units of power in the C.G.S. system, and is practically equivalent to the work done at the rate of one joule per second. The heavy is the induction in a circuit when the electro-motive force in-

duced in this circuit is one volt, while the inducing current varies at the rate

of one ampere per second.

of one ampere per second.

The olm, volt, etc., as above defined, are called the "international" ohm, volt, etc., to distinguish them from the "legal" ohm, B.A. unit, etc.

The value of the ohm, determined by a committee of the British Association in 1863, called the B.A. unit, was the resistance of a certain piece of copper wire preserved in London. The so-called "legal" ohm, as adopted at the International Congress of Electricians in Paris in 1884, was a correction of the B.A. unit, and was defined as the resistance of a column of mercury 1 square millimetre in section and 106 centimetres long, at a temperature of 32° F.

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1 legal ohm = 1.0112 B.A. units, 1 B.A. unit = 0.9889 legal ohm;
1 international ohm = 1.0136 " " 1 " " = 0.9866 int. ohm;
                            = 1.0023 legal ohm, 1 legal ohm = 0.9977 "
```

### DERIVED UNITS.

1 megohm = 1 million ohms: 1 microhm = 1 millionth of an ohm; 1 milliampere = 1/1000 of an ampere; 1 micro-farad = 1 millionth of a farad.

### RELATIONS OF VARIOUS UNITS.

1 ampere..... = 1 coulomb per second; = 1 watt = 1 volt-coulomb per second; = .7373 foot-pound per second, = .0009477 heat-units per second (Fahr.), = 1/746 of one horse-power; = .7373 foot-pound, = work done by one watt in one second, = .0009477 heat-unit; 1 joule... 1 British thermal unit ... ... = 1055.2 joules; = 737.3 foot-pound per second, = .9477 heat-units per second, = 1000/746 or 1.3405 horse-powers; 1 kilowatt, or 1000 watts..... 1 Kilowatt-hours, = 1.3405 horse-power hours, 1000 volt-ampere hours, = 2,654,200 foot-pounds, 1 British Board of Trade unit, = 3416 heat-units; = 746 watts = 746 volt-amperes,

The ohm, ampere, and volt are defined in terms of one another as follows: Ohm, the resistance of a conductor through which a current of one ampere will pass when the electro-motive force is one volt. Ampere, the quantity

# Equivalent Values of Electrical and Mechanical Units.

nits.	Equivalent Value in Other Units.	1,05	.0176 K. W. per sq. ft.	7.333 ftlbs. .00000365 H.P. hour. .0000272 K. W. hour. .0033 hear-units.	14,544 heat-units. 1.11 lb. Anth'cite coal ox. 2.5 lbs. dry wood oxidized. 21 cn. ft. illuminating-gas. 4.36 K. W. hours.	11,315,000 ftlbs. from: 11,315,000 ftlbs. of water evap. from and at 312° F.	288 K. W. hour. 873 H.P. hour. 108 800 K. F. m. 1,019,000 F. F. m. 701,900 F. W. 701,900 H. W. 1,019,000 H. W.			
anical	Unit.	Heat- unit ==	per Sq. Ft. per min. =	1 Kilogram Metre =	1 lb. Carbon Oxidized	fect Effi- ciency =	11. 40.	Fvapor'ed from and at 212° F. =		
Equivalent values of Electrical and Mechanical Units,	Unit. Equivalent Value in Other Units.	746 watts. 38,000 ft10s. per minute. 550 ft10s. per second. 42, 14est-units per hour. 42, 14est-units per hour. 707 heat-units per second. 175 lbs. carbon oxidized per hour. 2, 61 lbs. watter evap. per hour. from and at 212° Ft.	1 watt second.	.000000278 K. W. hour. .102 k. g. m. .0009477 heat-units. .7373 ft -1b.	1.356 joules. .1383 k. g. m. .00000377 K. W. hours. .001285 heat-units. .000005 H.P. hour.	1 joule per second00134 H.P. 8.412 beat-units per hour.	. 0035 lbs. water evap. per hr. 44.24 ft. lbs. per minute.	8.19 heat-units per sq. ft. per minute. 6371 ftlbs. per sq. ft. per min- ute. .193 H.P. per sq. ft.		
nie	Unit.	H.P. =		Joule=	1 Ftlb.	Mott	1	1 Watt per sq in. =		
Equivalen	Unit. Equivalent Value in Other Units.	1,000 watt hours. 2,664,300 ft18 horse-power hours. 8,600,000 joules. 3,412 hear-units. 867,000 kilogram metres. 235 lb. carbon oxidized. 235 lb. swarer evap. from an and str279 F. 22,75 lbs. of water maked.	from 62° to 212° F.	1,980,000 ftlbs. 2,545 hear-units. 273,740; g. m. varidized	with perfect efficiency. 2.64 lbs, water evaporated from and at 212° F. 17.0 lbs. water raised from 62° F. to 212° F.	1,000 watts. 1.34 horse-power. 2,654,900 ftlbs. per hour. 44,240 ftlbs. ner minute	737.3 ftlbs. per second. 3,418 heat-units per hour. 56 9 heat-units nor minute	948 hear-unit per second. 2775 lb. carbon oxidized 1 Watt per hour. 95.33 lbs. water evap. per in. = hour from and at 212° F.		
	Unit.	1 K. W. Hour =		- p	Hour =		Tilo-	watt =		

of current which will flow through a resistance of one ohm when the electromotive force is one volt. Volt, the electro-motive force required to cause a current of one ampere to flow through a resistance of one ohm.

Units of the Magnetic Circuit. (See Electro-magnets, page 1058.)
For Methods of making Electrical Measurements, Testing, etc., see Munroe & Janieson's Poket-Book of Electrical Rules, Tables, and Data; S. P. Thompson's Dynamo-Electric Machinery; and works

on Electrical Engineering.

Equivalent Electrical and Mechanical Units.-H. Ward Leonard published in The Electrical Engineer, Feb. 25, 1895, a table of useful equivalents of electrical and mechanical units, from which the table on page 1026 is taken, with some modifications.

### ANALOGIES BETWEEN THE FLOW OF WATER AND ELECTRICITY.

WATER.

Head, difference of level, in feet. Difference of pressure per sq. in., in .

Resistance of pipes, apertures, etc., increases with length of pipe, with contractions, roughness, etc.; de-creases with increase of sectional area. The law of increase and decrease is expressed by complex formulæ. See Flow of Water.

Rate of flow, as cubic ft. per second, gallons per minute, etc., or volume divided by the time. In the mining regions sometimes expressed in " miners' inches."

Quantity, usually measured in cubic feet or gallons, but is also equivalent to rate of flow x time, as cubic feet per second for so many

Work, or energy, measured in foot-pounds; product of weight of fall-ing water into height of fall; in pumping, product of quantity in cubic feet into the pressure in lbs. per square foot against which the water is pumped.

Power, rate of work, Horse-power,ft.lbs, of work done in 1 min. + 33,000.

In falling water, pounds falling in one second ÷ 550. In water flowing in pipes, rate of flow in cubic feet per second × pressure resisting the

flow in lbs. per sq. ft. + 550.

ELECTRICITY. Volts; electro-motive force; difference of potential or of pressure; E. or E.M.F

Ohms, resistance, R. The resistance increases directly as the length of the conductor or wire and inversely as its sectional area,  $R \propto l + s$ . It varies with the nature or quality of the conductor.

Conductivity is the reciprocal of specific resistance,

Amperes; current; current strength; intensity of current; rate of flow; i ampere = 1 coulomb per second.

Amperes =  $\frac{\text{volts}}{\text{ohms}}$ ;  $C = \frac{E}{R}$ ; E = CR.

Coulomb, unit of quantity, Q, = rate of flow x time, as ampere-seconds. 1 ampere-hour = 3600 coulombs.

Joule, volt-coulomb, W, the unit of work, = product of quantity by the electro-motive force = volt-amperesecond. 1 joule = .7373 foot-pound.

If C (amperes) = rate of flow, and E (volts) = difference of pressure between two points in a circuit, energy expended = CEt, =  $C^2Rt$ , since E = CR.

Watt, unit of power,  $P_{\star} = \text{volts} \times$ amperes, = current or rate of flow × difference of potential.

1 watt = .7373 foot-pound per second = 1/746 of a horse-power.

Analogy between the Ampere and the Miner's Inch. (T. O'Conner Sloane.)—The miner's inch is defined as the quantity of water which will flow through an aperture an inch square in a board two inches thick, under a head of water of six inches. Here, as in the case of the amplitude of the control of the contr pere, we have no reference to any abstract quantity, such as gallons or pounds. There is no reference to time. It is simply a rate of flow. We may consider the head of water, six inches, as the representative of electrical pressure; i.e., one volt. The aperture restricting the flow of water may be assumed to represent the resistance of one ohm; the flow through a resistance of one ohm under the pressure of one volt is one ampere; the flow through the resistance of a one-inch hole two inches long under the pressure of six inches to the upper edge of the opening is one miner's inch.

The miner's inch-second is the correct analogue of the ampere-second; the one denotes a specific quantity of water, 0.194 gallon; the other a specific quantity of electricity, a coulomb.

### ELECTRICAL RESISTANCE.

Laws of Electrical Resistance. - The resistance. R. of any conductor varies directly as its length, t, and inversely as its sectional area, s,

Example.—If one foot of copper wire .01 in. diameter has a resistance of .033 ohm, what will be the resistance of a mile of wire .3 in. diam. at the same temperature? The sectional areas being proportional to the squares of the diameters, the ratio of the areas is .3 $^{\circ}$ : .0 $^{\circ}$ 2 = 900 to 1. The lengths are as 5290 to 1. The resistances being directly as the lengths and inversely as the sectional areas, the resistance of the second wire is  $.10323 \times 5280 \div$ 900 = .6056 ohm.

Conductance, c, is the inverse of resistance.  $R = \frac{l}{sc}$ ,  $c = \frac{l}{sR}$ . If c and  $c_2$ represent the conductances, and R and  $R_2$  the respective resistance of two substances of the same length and section, then  $c:c_2: R_2:c_3:R_3$ . Equivalent Conductors,—With two conductors of length  $l, l_2$ , or

Equivalent Conductors,—with two conductors of length  $l_i$ ,  $l_i$ , of conductances  $c_i$ ,  $c_i$ , and sectional areas  $s_i$ , we have the same resistance, and one may be substituted for the other when  $\frac{l_i}{cs} = \frac{l_i}{c_i s_i}$ .

The specific resistance, also called resistivity,  $a_i$ , of a material of unit length and section is its resistance as compared with the resistance of a standard conductor, such as pure copper. Conductivity, or specific conductance, is the reciprocal of resistivity.

$$R = \frac{l}{sc}, \quad R = \frac{al}{s}.$$

If two wires have lengths l,  $l_1$ , areas s,  $s_1$ , and specific resistances a,  $a_1$ , their

actual resistances are  $R = \frac{al}{s}$ ,  $R_1 = \frac{a_1 l_1}{s_1}$ , and  $\frac{R}{R_2} = \frac{al s_1}{a_1 l_2 s_2}$ 

Electrical Conductivity of Different Metals and Alloys.

-Lazare Weiler presented to the Société Internationale des Électriciens the results of his experiments upon the relative electrical conductivity of certain metals and alloys, as here appended :

1. Pure silver	100	17. Phosphor tin	17.7
2. Pure copper		18. Alloy of gold and silver	
2. Pule copper	100		16.12
3. Refined and crystallized	00.0	(50%)	
copper	99.9	19. Swedish iron	16
4. Telegraphic silicious bronze	98	20. Pure Banca tin	15.45
5. Alloy of copper and silver		21. Antimonial copper	12.7
(50%)	86.65	22. Aluminum bronze (10%):	12.6
6. Pure gold	78	23. Siemens steel	12
7. Silicide of copper, 4% Si	75	24. Pure platinum	10.6
8. Silicide of copper, 12% Si	54.7	25, Copper with 10% of nickel.	10.6
9. Pure aluminum	54.2	26. Cadmium amalgam (15%).	10.2
10. Tin with 12% of sodium	46.9	27. Dronier mercurial bronze	10.14
11. Telephonic silicious bronze	35	28. Arsenical copper (10%)	9.1
12. Copper with 10% of lead	30	29. Pure lead	8.88
13. Pure zinc	29.9	30. Bronze with 20% of tin	8.4
<ol> <li>Telephonic phosphor -</li> </ol>		31. Pure nickel	7.89
bronze	29	32. Phosphor-bronze, 10% tin	6.5
15. Silicious brass, 25% zinc	26.49	33. Phosphor-copper, 9% phos	4.9
16. Brass with 35% of zinc	21.5	34. Antimony	3.88
,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,		• • • • • • • • • • • • • • • • • • • •	

The above comparative resistances may be reduced to ohms on the basis that a wire of soft copper one milimetre in diameter at a temperature of 0° C. has a resistance of .02029 international ohms per metre; or a wire .001 inch diam, has a resistance of 9.59 international olims per foot.

# Relative Conductivities of Different Metals at $0^{\circ}$ and $100^{\circ}$ C. (Matthiessen.)

	Conduc	ctivities.		Condu	ctivities.
Metals.	At 0° C. " 32° F.	At 100° C. " 212° F.	Metals.	At 0° C. " 32° F.	At 100° C. " 212° F.
Silver, hard Copper, hard Gold, hard Zinc, pressed Cadmium Platinum, soft	100 99.95 77.96 29.02 23.72 18.00 16.80	71.56 70.27 55.90 20.67 16.77	Tin Lead Arsenic Antimony Mercury, pure. Bismuth	12.36 8.32 4.76 4.62 1.60 1.245	8.67 5.86 3.33 3.26

# and Insulators in Order of their Value.

Conductors and Insulat	ors in orner	or their va
Conductors.	Insulators (N	ion-conductors).
All metals	Dry Air	Ebonite
Well-burned charcoal	Shellac	Gutta-percha
Plumbago	Paraffin	India-rubber
Acid solutions	Amber	Silk
Saline solutions	Resins	Dry Paper
Metallic ores	Sulphur	Parchment
Animal fluids	Wax	Dry Leather
Living vegetable substances	Jet	Porcelain
Moist earth	Glass	Oils
Water	Mica	

According to Culley, the resistance of distilled water is 6754 million times

According to Citiey, the resistance of distinct water is 6.34 million times as great as that of copper.

Resistance Varies with Temperature.—For every degree Centigrade the resistance of copper increases about 0.4%, or for every degree F. 0.2222%. Thus a piece of copper wire having a resistance of 10 ohms at 82° example.

The following table shows the amount of resistance of a few substances used for various electrical purposes by which I ohm is increased by a rise of temperature 1° F., or 1° C.

1º F.	1° C.
00013	.00021
00018	.00031
00024	.00044
00036	.00065
00044	.00080
	.00400
	1° F. 00013 00018 00024 00036 00044

Annealing,—The degree of hardness or softness of a metal or alloy affects its resistance. Resistance is lessened by annealing. Matthiessen gives the following relative conductivities for copper and silver, the comparison being made with pure silver at 100° C.:

Metals.	Temp. C.	Hard.	Annealed.
Copper	110	95.31 95.36	97.83 103.33
Silver	14.0-	95.50	100.00

Dr. Siemens compared the conductivities of copper, silver, and brass with pure mercury at 0° C., with the following results:

Metal.	Hard.	Annealed.
Copper	52,207	55.253
Silver	56,252	64,380
Brass		13,502

Edward Weston (Proc. Electrical Congress 1893, p. 179) says that the resistance of German silver depends on its composition. Mathiessen gives it as nearly 13 times that of copper, with a temperature coefficient of .0004433 per degree C. Weston, however, has found copper-nickel-zinc alloys (German silver) which had a resistance of nearly 28 times that of copper, and a temperature coefficient of about one half that given by Matthiessen. Kennelly and Fessenden (Proc. Elec. Cong., p. 186) find that copper has a uniform temperature coefficient of 0.40% per degree C., between the limits of 20° and 250° C.

Standard of Resistance of Copper Wire. (Trans. A. I. E. E., Sept. and Nov. 1890.)—Matthiessen's standard is: A hard-drawn copper wire 1 metre long, weighing 1 gramme has a resistance of 0.1469 B.A. unit at 0° C. (1 B.A. unit = 0.9889 legal ohm = 0.9866 international ohm.) Resistance of hard copper = 1.0226 times that of soft copper. Relative conducting power (Matthiessen): silver, 100; hard or unannealed copper, 99.95; soft or annealed copper, 102.21. Conductivity of copper at other temperatures than 0° C...

 $C_t = C_0(1 - .00387t + .000009009t^2).$  The resistance is the reciprocal of the conductivity, and is

 $Rt = R_0(1 + .00387t + .00000597t^2).$ 

A committee of the Am. Inst. Electrical Engineers recommend the following as the most correct form of the Matthiessen standard, taking 8.89 as the sp. gr. of pure copper :

A soft copper wire I metre long and 1 mm, diam, bas an electrical resistance of .02057 B.A. unit at 0° C. From this the resistance of a soft copper wire I foot long and .001 in, diam, (mill-foot) is found to be 9,720 B.A. units at 0° C.

Standard Resistance	e at 0° C.	B.A. Units.	Legal Ohms.	Internat. Ohms.
Metre-millimetre, soft c	opper	.02057	.02034	.02029
Cubic centimetre "	***	.000001616	.000001598	.000001593
Mil-foot "	44	9.720	9.612	9.590
1 mil-foot, of soft coppe	er at 10°.22 C.	or 50°.4 F	10	9.977
11 11 11 11	" 15°.5 "	59°.9 F	10.20	10.175
ee ee ee ee	" 23°.9 "	75° F	10.53	10.505
27 ( ) 7 ( ) 7			210	1

For tables of the resistance of copper wire, see pages 218 to 220, also pp. 1034, 1035. Taking Matthiessen's standard of pure copper as 100%, some refined metal

has exhibited an electrical conductivity equivalent to 103%.

Matthiessen found that impurities in copper sufficient to decrease its density from 8.94 to 8.90 produced a marked increase of electrical resistance.

### ELECTRIC CURRENTS.

Ohm's Law.-This law expresses the relation between the three fundamental units of resistance, electrical pressure, and current. It is:

$$\text{Current} = \frac{\text{electrical pressure}}{\text{resistance}}; \quad C = \frac{E}{R}; \quad \text{whence} \quad E = CR, \text{ and } R = \frac{E}{C}$$

In terms of the units of the three quantities,

Amperes = 
$$\frac{\text{volts}}{\text{ohms}}$$
; volts = amperes × ohms; ohms =  $\frac{\text{volts}}{\text{amperes}}$ 

EXAMPLES: Simple Circuits.—1. If the source has an effective electrical pressure of 100 volts, and the resistance is two ohms, what is the current?

$$C = \frac{E}{R} = \frac{100}{2} = 50$$
 amperes.

2. What pressure will give a current of 50 amperes through a resistance of 2 ohms?  $E=CR=50\times2=100$  volts.

3. What resistance is required to obtain a current of 50 amperes when the

pressure is 100 volts?  $R = \frac{E}{C} = \frac{100}{50} = 2$  ohms.

The following examples are from R. E. Day's "Electric Light Arithmetic:" 1. The inflowing relations of a certain Brush dynamo-machine is 10.9 ohms, and the external resistance of a certain Brush dynamo-machine is 10.9 ohms, and the external resistance of a certain Brush dynamo-motive force of the machine being 83 volts. Find the strength of the current flowing in the circuit.

E = 839; R = 73 + 10.9 = 83.9 ohms;  $C = E \div R = 839 + 83.9 = 10$  amperes.

2. Three arc lamps in series have a resistance of 9.36 ohms, while the resistance of the leading wires is 1.1 ohm, and that of the dynamo is 2.8 ohms. Find what must be the electro-motive force of the machine when the strength of the current produced is 14.8 amperes.

$$R = 2.8 + 9.36 + 1.1 = 13.26$$
 ohms;  $C = 14.8$  amperes;  $E = C \times R = 13.26 \times 14.8 = 196.3$  volts.

3. Calculate from the following data the average resistance of each of three arc lamps arranged in series. The electro-motive force of the machine is 244 volts and its resistance is 3.7 ohms, while that of the leading wires is 2

is 244 volts and its resistance is 3.7 ohms, while that of the leading wires is 2 ohms, and the strength of current through each lamp is 21 amperes. If x represent the average resistance in ohms of each lamp, then the total resistance of the circuit is R=3x+2+3.7. But by Ohm's law R=E+C,  $\therefore 3x+5.7=244/21=11.61$  ohms, whence x=1.97 ohms, nearly. 4. Three Maxim incandescent lamps were placed in series. The average resistance, when hot, of each lamp was 39.3 ohms, and that of the dynamo and leading wires 11.2 ohms. What electro-motive force was required to maintain a current of 1.2 amperes through this circuit?

In this case we have

$$R = 3 \times 39.3 + 11.2 = 129.1$$
 ohms, and  $C = 1.2$  ampere;

and therefore, by Ohm's law,

$$E = C \times R = 1.2 \times 129.1 = 154.9$$
 volts.

5. The resistance of the arc of a certain Brush lamp was 3.8 ohms when a current of 10 amperes was flowing through it. What was the electro-motive force between the two terminals

$$E = C \times R = 10 \times 3.8 = 38$$
 volts.

6. Twenty-five exactly similar galvanic cells, each of which had an average internal resistance of 15 ohms, were joined up in series to one incandescent lamp of 70 ohms resistance, and produced a current of 0.112 amperes. What would be the strength of current produced by a series of 30 such cells through 2 lamps, each of 30 ohms resistance?

The data of the first part of the problem enable us to determine the average electro-motive force of each cell of the battery. Let this be represented the control of the co

sented by E; then we have

$$25E = C \times R = .112 \times (25 \times 15 + 70) = .112 \times 445;$$

$$\therefore E = \frac{.112 \times 445}{25} = 2 \text{ volts, nearly.}$$

Then from the data in the second part of the problem, we have, by Ohm's law,

$$C = \frac{30 \times 2}{30 \times 15 + 2 \times 30} = \frac{60}{510} = 0.118$$
 ampere.

**Divided Circuits.**—If the circuit has two paths, the total current in both divides itself inversely as the resistances.

If R and  $R_1$  are the resistances of the two branches, and C and  $C_1$  the currents,  $C \times R = C_1 \times R_1$ , and  $\frac{C}{C} = \frac{R_1}{R}$ , whence

$$C = \frac{C_1 R_1}{R}; \quad C_1 = \frac{CR}{R_1}; \quad R = \frac{C_1 R_1}{C}; \quad R_1 = \frac{CR}{C_1}.$$

In the case of the double circuit, one circuit is said to be in shunt to the other, or the circuits are in multiple arc or in parallel.

Conductors in Series,—If conductors are arranged one after the other they are said to be in series, and the total resistance is the sum of their several resistances.  $R_1 + R_2 + R_3$ .

Internal Resistance. —In a simple circuit we have two resistances,

that of the circuit R and that of the internal parts of the source, called in-

ternal resistance, r. The formula of Ohm's law when the internal resistance is considered is  $C = \frac{E}{R+r}$ .

Total or Joint Resistance of Two Branches,—Let C be the total current, and  $C_1$ ,  $C_2$  the currents in branches whose resistances respectively are  $R_1$ ,  $R_2$ . Then  $C = C_1 + C_2$ ;  $C = \frac{E}{R}$ ;  $C_1 = \frac{E}{R_1}$ ;  $C_2 = \frac{E}{R_2}$ ; or, if E = 1,  $C = \frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2}$ , whence  $R = \frac{R_1 R_2}{R_1 + R_2}$ , which is the joint resistance of

 $R_1$  and  $R_2$ . Similarly, the joint resistances of three branches have resistances respect-

ively of  $R_1$ ,  $R_2$ ,  $R_3$ , is  $R = \frac{R_1R_2R_3}{R_1R_2 + R_1R_3 + R_2R_3}$ .

When the branch resistances are equal, the formula becomes

$$\frac{R_1^n}{R_1^{n-1}\times n} = \frac{R_1}{n},$$

where  $R_1$  = the resistance of one branch, and n = the number of branches. where  $R_1$  = the resistance of one orienta, and n = the immore of oranges. **Kirchhoff's Laws**.—1. The sum of the currents in all the wires which meet in a point is nothing.
2. The sum of all the products of the currents and resistances in all the

branches forming a closed circuit is equal to the sum of all the electrical pressures in the same circuit.

When  $E=E_1+E_2+E_3$ , etc., and  $C=C_1+C_2+C_3$ , etc., and R is the total resistance of  $R_1R_2R_3$ , etc., then

$$E_1 + E_2 + E_3$$
, etc. =  $C_1R_1 + C_2R_2 + C_3R_3$ , etc.

**Power of the Circuit.**—The power, or rate of work, in watts = current in amperes  $\times$  resistance in ohms =  $C \times E$ . Since  $C = E \div R$ , watts =  $\frac{E^2}{R}$  = electro-motive force<sup>2</sup> ÷ resistance.

EXAMPLE... What H.P. is required to supply 100 lamps of 40 ohms resistance each, requiring an electro-motive force of 60 volts?

The number of volt-amperes for each lamp is  $\frac{E^2}{R} = \frac{60^2}{40}$ , 1 volt-amperes

.00134 H.P.; therefore  $\frac{60^2}{40} \times 100 \times .00134 = 12$  H.P. (electrical) very nearly.

If the loss in the dynamo is 20 per cent, then 12 H.P. is 80 per cent of the actual H.P. required; which therefore is  $\frac{12}{80} = 15$  H.P.

Heat Generated by a Current,—Joule's law shows that the heat developed in a conductor is directly proportional, 1st, to its resistance; 2d, to the square of the current strength; and 3d, to the time during which the current flows, or  $H = C^2Rt$ . Since C = E + R,

$$C^2Rt = \frac{E}{R}CRt = ECt = E\frac{E}{R}t = \frac{E^2t}{R}$$

Or, heat = current2 × resistance × time

= electro-motive force × current × time = electro-motive force<sup>2</sup> × time ÷ resistance.

 $Q = \text{quantity of electricity flowing} = Ct = \frac{E}{R}t$ .

H = EQ; or heat = electro-motive force  $\times$  quantity.

The electro-motive force here is that causing the flow, or the difference in

potential between the ends of the conductor. The electrical unit of heat, or "joule" =  $10^7$  ergs = neat generated in one second by a current of 1 ampere flowing through a resistance of one olm = 239 gramme of water raised 1° C.  $H = C^2Rt \times .239$  gramme calories =  $C^2Rt \times .0009478$  British thermal units.

In electric lighting the energy of the current is converted into heat in the lamps. The resistance of the lamp is made great so that the required quantity of heat may be developed, while in the wire leading to and from

the lamp the resistance is made as small as is commercially practicable, so that as little energy as possible may be wasted in heating the wire. The transformations of energy from the fuel burned in the boiler to the electric light are the following:

Heat energy is transformed into mechanical energy by means of the boiler and engine. Mechanical energy is transformed into electrical energy in the dynamo.

Electrical energy is transformed into heat in the electric light. The heat generated in a conductor is the equivalent of the energy causing

The read generated in a conductor is the equivalent of the energy causing the flow. Thus, rate of expenditure of energy in watts = electro-motive force in volts  $\times$  current in amperes = EC, and the energy in joules = watts  $\times$  time in seconds = ECt. Heat =  $C^2Rt = ECt$ .

Heating of Conductors. (From Kapp's Electrical Transmission of Energy.)—It becomes a matter of great importance to determine beforehand what rise in temperature is to be expected in each given case, and if nand what rise in temperature is to be expected in each given case, and in that rise should be found to be greater than appears safe, provision must be made to increase the rate at which heat is carried off. This can generally be done by increasing the superficial area of the conductor. Say we have one circular conductor of I square inch area, and find that with 1000 amperes flowing it would become too hot. Now by splitting up this conductor into 10 separate wires each one teuth of a square inch cross-sectional area, we have not altered the total amount of energy transformed into heat, but we have increased the surface exposed to the cooling action of the surrounding air in the ratio of 1: \(\sqrt{10}\), and therefore the ten thin wires can dissipate more than three times the heat, as compared with the single thick wire,

### Heating of Wires of Subaqueous and Aerial Cables (insulated with Gutta-percha). (Prof. Forbes.)

Diameter of cable + Diameter of conductor = 4. Temperature of air = 20° C. = 68° F. t =excess of temperature of conductor over air.

	ter in centi- s and mils.	ŕ	Cu	rrent in am	peres.	
Cm.	Mils.	t = 1° C. = 1.8° F.	t = 9° C. = 16.2° F.	t = 25° C. = 45° F.	t = 49° C. = 92.2° F.	$t = 81^{\circ} \text{ C.}$ = 145.8° F.
.1 .2 .3 .4 .5 .6 .7 .7 .9 1.0 2.0 3.0 4.0 5.0 6.0 7.0 8.0	40 80 120 160 200 240 280 310 350 780 1180 1570 2360 2750 3150	3.7 9.1 •15.0 21.2 27.4 33.7 40.1 46.4 52.9 59.3 124 189 254 319 385 450 514	11.0 27.0 44.4 62.5 81.0 100 119 187 187 175 367 559 753 945 1138 1330 1525	17.8 43.8 72.1 102 181 164 192 223 253 253 285 595 998 1221 1534 1846 2158 2472	24.0 59.0 97.3 137 177 219 259 301 342 384 803 1225 1646 2068 2491 2846 3335	29.5 72.5 119 168 218 268 319 369 420 472 988 1503 2021 2523 3058 8575 4094
9.0	3540 3940	580 645	1716 1909	2785 3097	8755 4178	4611 5130

Prof. Forbes states that an insulated wire carries a greater current without overheating than a bare wire if the diameter be not too great. Assuming overheating than a bare wire it the diameter be not too great. Assuming the diameter of the cable to be twice the diam. of the conductor, a greater current can be carried in insulated wires than in bare wires up to 1.9 inch diam. of conductor. If diam. of cable = 4 times diam. of conductor, this is the case up to 1.1 inch diam. of conductor.

Copper-wire Table.—The table on pages 1034 and 1035 is abridged from one computed by the Committee on Units and Standards of the American Institute of Electrical Engineers (Trans. Oct. 1893).

1	in the	
	O. per ft., at 80° C., 176° F.	0.000000000000000000000000000000000000
wires.	O. per ft., at 50° C., 122° F.	0.000000000000000000000000000000000000
Resistance.	O. per ft., at 20° C., 68° F.	0.00004899 0.00004899 0.00004739
Length.	Ohms per Lb. at 20° C., 68° F.	0.000000000000000000000000000000000000
gth.	Ft. per Ohm, at 20°C.,68°F.	8 17787178 6 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4 4
Length.	Feet per Lb.	4 - 4 - 4 - 4 - 4 - 4 - 6 - 6 - 7 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5 - 5
Diam- Area, Weight.	Lbs. per Ohm, at 20° C., 68° F.	E STANDER STAN
N (2)	Lbs. per Foot.	0.0 6468 0.0
Area,	mils.	11.100 11
Diam-	eter, inches.	6.545 6.
	B. W. G. Stubbs'.	000000000000000000000000000000000000000
Gauges.	A. W. G. B. & S.	000 000

Weights, Lengths, and Resistances of Cool, Warm, and Hot Copper Wires.—(Continued.)

Length, Resistance.	m, Feet per Ft. per Ohm, Ohms per Tb. Ohms per ft. Ohms per ft. Ohms per ft. Thus p	161.3 197.8 0.00505 0.00505 0.00529 185.3 170.4 1.099 0.00707 0.00729 205.4 186.9 1.286 0.00574 0.007287 0.007287	118.3 2.279 0.008452 98.90 3.252 0.01011 98.66 3.278 0.01011	78.24 5.212 0.01278 0.01428 75.72 5.565 0.01321 0.01475 62.05 8.287 0.01475	60.36 8.756 0.0167 0.01851 49.21 13.18 0.02032 0.02271	46.75 14.60 0.02139 0.02390 39.02 20.95 0.02563 0.02863	31.29 32.58 0.02196 0.03570 30.357 0.02196 0.02570	24.73 52.19 0.04045 0.04519 24.54 52.97 0.04075 0.04519	84.23 0.05138 0.05740 89.04 0.05283 0.05902	15-52 1.035.9 0.00427 0.0055.0 15-52.9 15-52.9 0.07239 0.07239 15-52.9 155.0 0.0047.0 0.0050.0	213.0 0.08170 0.09128 338.6 0.1030 0.1151	7.823 521.3 0.1278 0.1428	6.181 835.1 0.1539	4.841 1,361 0.2066 0.2308	3.835 2,165 0.2605 9.2310	2.414 5.473 0.4142 0.4027	20,650 1.545 13,360 0.6471 0.7230	21,010 1.519 13,870 0.6585 0.7357
iges.   Diam. Aman Weight.	Lbs. per   Lbs. per Ohm, Foot. at 20° C., 68° F.	0.005200 0.005340 0.005340 0.004917 0.004917		0.002452 0.1919 0.002373 0.1797 0.001945 0.1207			0.0003311 0.04678 0.0009808 0.03069 0.0009699 0.03002		0.0005933 0.01123			0.0002452 0.001918 0.0002452 0.001918						
Anno dans	Circular mils.	2,048 1,764 1,624	1,225	810.1 784.0 642.4	625.0 509.5	484.0 404.0	324.0 324.0 320.4	256.0 254.1	196.0	159.8	126.7	20.0 20.0 20.0 20.0 20.0 20.0 20.0 20.0	0.75	50.13	39.75	25.0	16.	19.72
Diam		0.04526	0.03200 0.03200 0.03196	0.02846 0.02800 0.02535	0.0250	0.0220	0.0180	0.0160	0.0140	0.01264	0.01126	0.0000	0.0080	0.007080	0.006305	0.0050	0.0040	0.003965
Gauges.	W. G. B. W. G.	19	273	55	83	77 10	8 8	27	88 8	3 8	3	38	88	1.5	;	35	36	

The data from which the foregoing table has been computed are as follows: Matthiessen's standard resistivity, Matthiessen's temperature coefficients, specific gravity of copper = 8.89. Resistance in terms of the international ohm.

Matthiessen's standard 1 metre-gramme of hard-drawn copper = 0.1469 B. A. U. @ 0° C. Ratio of resistivity hard to soft copper 1.0226.

Matthlessen's standard I metre-gramme of soft-drawn copper = 0.14365 B. A. U. @ 0° C. One B. A. U. = 0.9806 international ohm. Matthlessen's standard I metre-gramme of soft-drawn copper = 0.141729

international ohm @ 0° C.
Temperature coefficients of resistance for 20° C., 50° C., and 80° C., 1.07968. 1.20625, and 1.33681 respectively. 1 foot = 0.3048028 metre, 1 pound = 453.59256 grammes.

Heating of Coils .- To calculate the heating of a coil, given the cool-

ing surface and its resistance. (Forbes.) Let  $\rho$  = the resistance of a coil in ohms at the permissible temperature ρ = the resistance (cold) must be increased by 1/5 of its value togive ρ; S = the surface exposed to the air measured in square centimetres (I square cm. = .155 square inc); I sq. ln. = 6.45 square cm.);

t =the rise in temperature, centigrade scale;

C = the current in amperes.

 $24C^2\rho$  = heat generated = etS. where e is McFarlane's constant, varying from .0002 to .0003. The latter value may be taken. If 50° C. be the permissible rise in temperature.

$$C = \sqrt{\frac{.0003 \times 50 \times S}{.24 \times \rho}} = .25 \sqrt{\frac{S}{\rho}}.$$

Example. - The resistance of the field-magnets of a dynamo is 1.5 ohms cold, and the surface exposed to the air is 1 square metre; find the current to heat it not more than 50° C.

Here 
$$S=10{,}000;~\rho=1.8~{\rm ohms};~{\rm and}~C=.25\sqrt{\frac{\overline{10{,}000}}{1.8}}=33.5~{\rm amperes}.$$

For the heating of coils of field-magnets Mr. C. Hering gives 1 watt of energy dissipated for every 223 square inches of cooling-surface for each degree F. of difference between the temperature of the coil and the surrounding air. W = CE = 1/2:3TS = 0.004476TS, in which W = watts lost in coil, T =

degrees Fahr., and S = square inches.

 $C = \frac{1.6}{223E}$  is the greatest current which can be used in the magnet coils of a shunt machine having a certain pressure in order that they do not heat above a certain temperature. Thus for a rise of temperature of 50° F. above the surrounding air,

 $C = \frac{508}{223E} = .224 \frac{\dot{S}}{E}$ . Substituting for E its equivalent CR, we get

$$C = \sqrt{.224 \frac{8}{R}}$$
.

If 80° F. is the maximum difference of temperature.

$$C = \frac{80S}{223E} = .36\frac{S}{E} = .60 \sqrt{\frac{S}{R}}$$

The formula can be used for series machines when C is known, for writing

$$C^2R = 1/223TS$$
, we get  $R = \frac{TS}{223C^2}$ .

With a permissible rise of 50° F. or 80° F., we have respectively,

$$R = \frac{.224S}{C^2}$$
; and  $R = .36\frac{S}{C^2}$ .

The surface area of the coil in square inches may be found from

$$S = \frac{223 \, W}{T} = \frac{223 CE}{T} = \frac{223 C^2 R}{T}.$$

For a rise of temperature of 50° F. or 80° F., respectively, the surface will be

$$S = \frac{223\,W}{50} = 4.46\,W; \ \ \text{and} \ S = \frac{223\,W}{80} = 2.8\,W.$$

**Fusion of Wires.**—W. H. Preece gives a formula for the current required to fuse wires of different metals, viz.:  $C = ad^{\frac{3}{2}}$ : in which d is the diameter in inches and a a coefficient whose value for different metals is as follows: Copper 102+1; aluminum 7585; platinum 5172; German silver 5290; platinoid 4750; iron 3148; tin, 1612; lead, 1879; alloy of 2 lead and 1 tin, 1818.

# Diameters of Various Wires which will be Fused by a given Current.

Formula,  $d=\left(\frac{C}{a}\right)^{\frac{3}{4}}$ ; a= 1642 for tin = 1379 for lead = 10244 for copper = 3148 for iron.

Current,	Tin Wire.		Lead Wire.		Copper Wire.		Iron Wire.	
in amperes.	Diam. inches.	Approx. S.W. G.	Diam. inches.	Approx. S.W. G.	Diam. inches,	Approx. S.W. G.	Diam. inches.	Approx. S.W. G.
1 2 3 4 5	.0072	36	.0081	35	.0021	47	.0047	40
2	.0113	81	.0128	80	.0034	43	.0074	36
3	.0149	28 26	.0168	27 25	.0044	41	.0097	33 31
4	.0181	25	.0203	23	.0053	39 38	.0117	29
10	.0334	21	.0375	20	.0098	33	.0216	24
15	.0437	19	.0491	18	.0129	30	.0283	22
20	.0529	17	.0595	17	.0156	28	.0343	20.5
. 25	.0614	16	.0690	15	.0181	26	.0398	19
30	.0694	15	.0779	14	.0205	25	.0450	18.5
35	.0769	14.5	.0864	13.5	.0227	24	.0498	18
40	.0840	13.5	.0944	13	.0248	23	.0545	17
45	.0909	13	.1021	12	.0268	22	.0589	16.5
50	.0975	12.5	.1095	11.5	.0288	22	.0632	16
60	.1101	11	. 1237	10	.0325	21	.0714	15
70	. 1220	10	.1371	9.5	.0360	20	.0791	14
80	.1334	9.5	.1499	8.5	.0394	19	.0864	13.5
90	.1443	9	.1621	8 7 6	.0426	18.5	.0935	13
100	.1548	8.5	.1739	7	.0457	18	.1003	12
120	.1748	7	.1964	6	.0516	17.5	.1133	11
140	.1937	6	.2176	5	.0572	17	.1255	10
160	.2118	5 4	.2379	5 4 8 2	.0625	16	.1372	9.5
180 200	.2291	9 5	.2573 .2760	8	.0676	16	.1484	9 8
250 250	.2457	3.5 1.5	.3203	ő	.0841	15 13.5	.1848	6.5
800	.3220	0.5	.3617	00.5	.0950	12.5	.2086	5

# Current in Amperes Required to Fuse Wires According to the Formula $C = ad^{\frac{3}{2}}$ .

S.W. G.	Diameter, inches.	$d^{\frac{3}{2}}$ .	Tin. $a = 1642$ .	Lead $a = 1379$ .	Copper $a = 10244$	a = 3148.
14	.080	.022627	37.15	31.20	231.8	71.92
16 18 20	.064 .048 .036	.016191 .010516 .006831	26.58 17.27 11.22	22.32 14.50	165.8 107.7 69.97	50.96 33.10 21.50
20 22 24	.028	.004685	7.692 5.357	9.419 6.461 4.499	48.00 33.43	14.75 10.27
26 28	.018	.002415	3.965 2.956	3.330 2.483	24.74 18.44	7.602 5.667
30 32	.0124	.001381	2.267 1.843	1.904 1.548	14.15	4.347

### ELECTRIC TRANSMISSION.

Cross-section of Wire Required for a Given Current. -Constant Current (Series) System. -- The cross-sectional area of copper Constant Current (Series) System.—The cross-sectional area of copper necessary in any circuit for a given constant current depends on the differ-ence between the pressure at the generating station and the maximum pressure required by all the apparatus on the circuit, and on the total length of the circuit. The following formulæ are given in "Practical Electrical Engineering:"

If V = pressure in volts at generators; v = sum of all the pressures (in volts) required by apparatus supplied in the circuit

n = total length (going and return) of circuit in miles;

c=0 current in amperes; c=0 copper-conductor of 1 square inch sectional c=0area in ohms:

α = required cross-sectional area of copper in square inches,—

$$a = \frac{nrC}{V - v}$$
.

If we take the temperature of the conductor when the current has been flowing for some time through it, as 80° F.,

$$r = 0.0455 \text{ ohm}, \text{ and } a = \frac{0.0455nC}{V - v}.$$

It generally happens, however, that we are not tied down to a particular value of V, as the pressure at the generators can be varied by a few volts to suit requirements. In this case it is usual to fix upon a current density and determine the cross-sectional area of copper in accordance with it.

If D = current density in amperes per square inch determined upon.

$$a = \frac{C}{D}.$$

The current density is frequently taken at 1000 amperes to the square inch, but should in general be determined by economical considerations for

but should in general be determined by economical considerations for every case in question. Allowable Current Density in Insulated Cables.—Experiments on insulated cables in casing gave the results shown below, but they need confirmation or correction of the current densities permissible in different sizes of insulated cables run underground. C and D are the current in amperes and the current density in amperes per square inch, respectively, which will raise the temperature of the conductor by the number of degrees Fahr. indicated by the suffix.

No. Strands.	S.W.G.* of each Wire.	Area of Strand in square inches.	$C_{18}$	$D_{18}$	$C_{50}$	$D_{50}$ .
7	20	0.0072	18	2,500	28	3,900
7	14	0.0357	59	1,400	95	2,700
19	14	0.0975	126	1,300	205	2,100
37	14	0.191	210	1,100	339	1,800

Constant Pressure (Parallel System) .- To determine the loss in pressure in a feeder of given size in the case of two-wire parallel distribution,

Let  $\alpha = cross-sectional$  area of copper of one conductor of the feeder in square inches:

n = length of feeder (going and return) in miles;

C = current in amperes;

V-v= loss of pressure in feeder in volts; r= resistance of 1 mile of copper conductor of 1 square inch sectional area in ohms.

$$V - v = \frac{nrC}{a}$$
.

<sup>\*</sup> Standard (British) Wire-gauge.

If the temperature of the conductor with this current flowing in it is assumed to be 80° F.,

$$r = 0.0455$$
 ohm, and  $V - v = \frac{0.0455nC}{a}$ .

Three-wire Feeder.-In the case of a three-wire feeder, let  $p_1q_1$  and  $p_{2}q_{2}$  represent the two outer conductors, and let p'q' represent the middle conductor,  $p_{1}$ , p',  $p_{2}$  being at the feeding-point and  $q_{1}$ , q',  $q_{2}$  at the generating station, and let

a= cross-sectional area of each of the outer conductors in square inches; a'= cross-sectional area of middle conductor;

 $\alpha$  = tross-sectional area of made tomation,  $\gamma$  = length in miles of each conductor of feeder;  $V_{-1}$  = pressure between  $p_1$  and  $p_2$  in volts at generating station;  $v_2$  = pressure between  $p_1$  and  $p_2$  in volts at generating station;  $v_1$  = pressure between  $q_1$  and q' in volts at feeding-point;  $v_2$  = pressure between q' and  $q_2$  in volts at feeding-point;

 $c_1$  = current in  $p_1q_1$  in amperes;  $C_2$  = current in  $p_2q_3$  in amperes;  $C_2$  = current in  $p_2q_3$  in amperes;  $c_3$  = current in  $p_2q_3$  in mile of copper conductor of 1 square inch sectional area in ohms.

Then

$$V_1 - v_1 = nr \left\{ \frac{C_1}{a} + \frac{C_1 - C_2}{a'} \right\}; \qquad V_2 - v_2 = nr \left\{ \frac{C_2}{a} - \frac{C_1 - C_2}{a'} \right\}.$$

It will be noticed that if  $v_1 = v_2$ , and if  $C_1$  is greater than  $C_2$ ,  $V_1$  is greater than  $V_2$  by twice the loss of pressure in the middle wher; this result shows that the regulators must be in circuit with the two outer conductors.

that the regulations must be included in the two observables of the loads of the two sections of the three-wire system is  $m^*$  per cent of the maximum load of the more heavily loaded section, and if  $C_1$  is the maximum current in either of the outer conductors of the feeder under consideration,

 $C_2$  will not be less than  $C_1\left(1-\frac{m}{100}\right)$ , and consequently  $C_1-C_2$  will not be

greater than  $\frac{mC_1}{100}$ .

We have then

$$V_1 - v_1 = \frac{nrC_1}{a} \times \frac{200 + m}{200}; \quad V_2 - v_2 = \frac{nrC_1}{a} \times \frac{200 - m}{200};$$

so that if  $v_1$  and  $v_2$  are each equal to V—the pressure required to be maintained constant at the feeding-point—we can calculate  $V_1$  and  $V_2$  for given values of n, a, and  $C_1$ , employing the value of m, which we estimate should be the maximum it can have.

These last expressions show that the difference in the pressures required at the station across the two sections of a three-wire feeder increases with the current carried by the feeder; hence the regulators on each of the outer conductors should be equivalent to a variable resistance having at least nrm ohms as a maximum. 100a

It is usual to make the area of the middle conductor one half of that of each of the outer conductors, but this is not invariably the case.

**Short-circuiting.**—From the law  $C = \frac{E}{R}$  it is seen that with any pressure E the current C will become very great if R is made very small. In short-circuiting the resistance becomes small and the current therefore great. Hence the dangers of short-circuiting a current.

**Economy of Electric Transmission.** (R. G. Blaine, Eng'g, June 5, 1891.)—Sir W. Thomson's rule for the most economical section of conductor

<sup>\*</sup> The value to be assigned to m may vary from 10 to 25, according to the case exercised in connecting customers to one section or the other, or both, and according to the local conditions. At a certain station supplying current on the three-wire low-pressure system to about 25,000 8-c.p. lamps, we were informed that m had never exceeded 7 or 8.

is that for which the "annual interest on capital outlay is equal to the annual cost of energy wasted," and its practical outcome is that the area of the copper conductor should be such that its resistance per mile =  $\frac{11}{G}$ 

(C being the current in amperes).

(C) being the current in amperes).

Tables have been compiled by Professor Forbes and others in accordance with modifications of Sir W. Thomson's rule. For a given entering horse-power the question is merely one as to what current density, or how many amperes per square inch of conductor, should be employed. Sir W. Thomson's rule gives about 398 amperes per square inch, and Professor Forbes's tables—for a medium cost of one electrical horse-power per hour—give a

current density of about 380 amperes per square inch as most economical.

When a given horse-power is to be delivered at a given distance, the case is somewhat different, and Professors Ayrton and Perry (Electrician, March, 1886) have shown that in that case both the current and resistance are variables, and that their most economical values may be found from the fol-

lowing formulæ:

$$C = \frac{w}{P}(1 + \sin \phi)$$
, and  $r = \frac{P^2}{nw} \frac{\sin \phi}{(1 + \sin \phi)^2}$ ,

in which C= the proper current in amperes; r= resistance in ohms per mile which should be given to the conductor; P= pressure at entrance in volts; n= number of miles of conductor; w= power delivered in watts;  $\phi=$  such an angle that  $\tan\phi=nt+P$ , t being a constant depending on the price of copper, the cost of one electrical horse-power, interest, etc.: it may be taken as about 17.

In this case the current density should not remain constant, but should diminish as the length increases, being in all cases less than that calculated by Sir W. Thomson's rule.

Example.—If the current for an electric railway is sent in at 200 volts, 100 horse-power being delivered, find the waste of power in heating the conductor, the distance being 5 miles and there being a return conductor. Here n=10, t=17, P=200;  $\tan\phi=170+200=.85, \phi=40^{\circ}$  22′,  $\sin\phi=170$ 

Hence most economical resistance

$$r = \frac{200^2}{10 \times 74600} \times \frac{.6477}{1.6477^2} = .01279$$
 ohm per mile,

or .1279 ohm in its total length.

The most economical current,  $C=\frac{74600}{200}\times 1.6477=614.58$  amperes, and W, the power wasted in heat,  $=\frac{C^2R}{746}=\frac{614.58^2\times.1279}{746}=64.75$  horse-power.

The following tables show the power wasted as heat in the conductor.

HORSE-POWER WASTED IN TRANSMITTING POWER ELECTRICALLY TO A GIVEN DISTANCE, THE ENTERING POWER BEING FIXED. PRESSURE AT ENTRANCE, 200 VOLTS. CURRENT DENSITY, 380 AMPERES PER SQUARE INCH.

Horse-power sent in.*		Horse-power Wasted, the Distance to which the Power is Transmitted being one Mile (there being a Return Conductor).	Horse-power Wasted. Distance Five Miles.	
	10	1.663	8.318	
	10 20	3.327	16 636	
	40	6.654	33.27	
	40 50 80	8.318	41.59	
	80	13.308	66.54	
	100	16.636	83.18	
	200	33 272	166.36	

<sup>\*</sup> That is, horse-power at the generator terminals.

PRESSURE AT ENTRANCE, 2000 VOLTS.

Horse- power sent in.	Horse-power Wasted. Distance One Mile (there being a Return Conductor).	Horse- power Wasted. Dis- tauce Five Miles.	Horse- power Wasted. Distance Ten Miles.	Horse-power Wasted, Distance Twenty Miles.
100	1.663	8.318	16.636	83.27
200	3.327	16.636	33.272	66.54
400	6.654	33.272	66.54	133.08
500	8.318	41.59	83.18	166.36
800	13.308	66.54	133.08	266.17
1000	16.636	83.18	166.36	332.72
2000	33.272	166.36	332.72	665.44

It will be seen from these numbers that when the current density is fixed the power wasted is proportional to the entering horse-power and the length of the conductor, and is inversely proportional to the potential. For a copper conductor the rule may be simply stated as

$$W = 16.6358 \frac{E}{P} \times l,$$

 ${\cal E}$  being the horse-power and  ${\cal P}$  the pressure at entrance, and l the length of the conductor in miles.

HORSE-POWER WASTED IN ELECTRIC TRANSMISSION TO A GIVEN DISTANCE, THE POWER TO BE DELIVERED AT THE DISTANT EXD BEING FIXED. PRESSURE AT ENTRANCE, 200 VOLTS. CURRENT AND RESISTANCE CALCULATED BY AYRTON AND PERRY'S RULES.

Horse-power Delivered.	Horse-power Wasted, the Distance to which the Power is Transmitted being One Mile (there being a Return Conductor).	Horse-power Wasted. Distance Five Miles.	Horse-power Wasted. Distance Ten Miles.	
10	1.676	6.476	8.620	
20	3.352	12.952	17.24	
40	6.704	25.904	34.48	
50	8.38	32.38	43.10	
40 50 80	13.408	51.808	68.96	
100	16.76	64.86	86.20	
200	33.52	129.52	172.4	

### PRESSURE AT ENTRANCE, 2000 VOLTS.

Horse-power Delivered.	Horse-power Wasted. Distance One Mile.	Horse-power Wasted, Distance Five Miles.	Horse-power Wasted. Distance Ten Miles.
100	1.716	8.484	16,763
200	3.432	16.968	33.526
400	6.864	33.938	67.052
500	8.58	42.42	83.815
800	13.728	67.87	134,104
1000	17.16	84.84	167 63
2000	34.32	169.68	335.26

If H= horse-power sent in, w= power delivered in watts, C= current in amperes, r= resistance in ohms per mile, P= pressure at entrance in volts, and n= number of miles of conductor,

$$(w + C^2r) \div 746 = H$$
;  $w = 746H - C^2r$ ;

and the formulæ for best current and resistance become

$$C = \frac{746H - C^2r}{P}(1+\sin\phi); \quad r = \frac{P^2}{n(746H - C^2r)} \times \frac{\sin\phi}{1+\sin\phi}$$

Energy wasted as heat in watts per mile =  $C^{2}r = \frac{746H \sin \phi}{v + \sin \phi}$ 

Horse-power wasted per mile =  $W_1 = \frac{H \sin \phi}{n + \sin \phi}$ 

 $(\phi = \text{angle whose tangent} = nt + P, \text{ and the value of } t \text{ corresponding to a current density of 380 amperes per sq. in, is 16.636.})$ 

### TABLE OF ELECTRICAL HORSE-POWERS.

Formula:  $\frac{\text{Volts} \times \text{Amperes}}{746} = \text{H.P.}$ , or 1 volt-ampere = .0013405 H.P.

Read amperes at top and volts at side, or *vice versa*.

Amperes or Volts. Volts or Amperes. 10 20 30 40 50 60 70 90 100 110 80 120 .0670 .1341 .1206 .1341 00134 .0134 .0268 0402 .0536 .0804 .0938 .1072 .1475 .1609 00268 .0268 .0536 0804 .1072 .1609 .1877 .2145 .2413 .2949 .3217 00402 .0402 .0804 .1206 .1609 .2011 .2413 .2815 .3619 .4022 .4424 4826 .1072 .2145 .4290 .00536 .0536 1609 .2681 .3217 5362 .6434 .7373 5 .00670 .0670 .1341 .2011 .2681 .3351 .4022 4692 .6032 .6703 .8043 .2413 .4826 6 .00804 .0804 .1609 5630 6434 .7239 .8043 .3217 .40228847 9659 9384 .00938 .0938 .1877 .2815 ,4692 5630 6568 7507 .032 1.126 01072 .1072 .2145 3217 .42905362 .6434 .7507 9652 1.072 1 180 .01206 .1206 .2413 3619 .4826 6032 8445 9652 1.086 1.206 1.327 1.475 448 .2681 .4022 .5362 .8043 .9383 1.072 1,206 1.341 10 .01341 .1341 .6703 1 609 .7373 .4424 1.180 1.327 1.475 11 .01475 .1475 .2949 5898 8847 1.032 1.622 .769 1.609 1.287 .01609 .1609 .3217 .4826 .5228 6434 8043 9652 1.126 1.448 1.769 .930 1.743 .1743 2485 .6970 .8713 1.046 1.220 1.394 1.568 1.917 2.091 .01877 .1877 .3753 .5630 .7507 9384 1.126 1.314 1.501 1.689 2.064 15 .02011 .4022 .6032 .8043 1.005 1.206 1.408 1.609 1.810 2.011 2.212 2.413 .2145 .4290 .6434 .8579 1.072 1.287 1.716 1.930 2.145 2.359 .02145 1.501 2.574 .4558 .6837 1.595 1.823 2.051 2.279 .02279 .2279 1.139 1.367 2.507 2.735 1.930 2.413 18 .02413 .2413 .4826.7239 9652 1,206 1.448 1.689 2.654 2.895 3.056 3.217 19 .02547 .2547 .5094 .7641 1.019 1.528 1.783 2.037 2.292 2.801 20 .02681 .2681 .5362 ,8043 1.072 1.340 1.609 2.681 2,949 21 .02815 .2815 1.971 .5630 .5898 .8445 1.126 1,408 1.689 2.252 2.533 2.815 3.097 3.244 3.378 2.949 8847 2.359 22 .02949 .2949 1.180 1.475 1.769 2.064 2.654 3.539 1.850 3.083 3.217 .9249 1.542 2.158 2.467 3.391 23 .03083 .3083 .6166 3.700 1 930 24 .03217 .3217 6434 9652 1.609 2.895 3 539 .03351 .3351 .6703 1.005 1.341 1.676 2.011 2.346 2.681 3.016 3.351 3.686 4.022 .3485 .6971 2.788 3.834 26 03485 1 046 1 394 1 743 2.091 2,440 3 137 3 485 4.182 03619 3619 .7239 .7507 1.810 2.534 9 895 3.257 3.619 3.753 1.086 1.448 .343 2.252 2.332 1.126 3.003 .03753 .3753 1.501 4.129 4.504 29 .03887 .3887 1.166 1.555 4.276 2 887 4.665 30 .04022 .4022 .8043 1.206 1,609 2.011 2.413 2.815 3.217 4.022 4.424 4.826 .04156 ,4156 ,8311 2.909 4.571 31 1.247 1.662 2.078 2.493 3.324 3.740 4.156  $\frac{4.987}{5.148}$ 2.145 3 432 .04290 .8579 1.716 3 861 4.290 .42902.003 4.7191.327 .04424 .8847 2.212 2.654 3.986 4.424 4.866 5.013 .4424 3.097 5.308 3,646 .04558 .4558 9115  $\frac{2.735}{2.815}$ 3,190 4.102 .469 .04692 .4692 .9384 1.408 1.877 2.346 3.284 4.692 5.161 5.630 .4826 2 895 3.861 04826 9652 1 448 1.930 2 413 3,378 4.343 4 826 5 308 5 791 4.960 5.094 4960 9920  $\frac{1.488}{1.528}$ 1.984 2.480 2.976 3,968  $\frac{4.464}{4.585}$ 5 959 .04960 5.456 2.038 2.547 3.056 38 .05094 5094 1.019 3,566 5.603 6.113 4.705 1.568 5,228 .05228 1.046 2.091 2.614 3,660 6.27440 .05362 .5362 1.609 2.145 2 681 4.290 4.826 5.362 5.898 6.434 41 .05496 .5496 1.099 1.649 2.198 2.748 3,298 3.847 4.397 4.946 5.496 6.046 6.595  $\frac{1.126}{1.153}$ 4.504 5.067 5.187 5.3085.630 5.764 5.898 6.756 .05630 .5630 1.689 3.941 6.193 .5764 1.729 3.458 4.035 4.129 4.611 4.719 4.826 6.341 43 .05764 2,306 2.882 6.917 .05898 2.949 7.078 7.239 1.180 6.488 6.635 45 .06032 .6032 1.206 1.810 2.413 3.016 4.223 5.439 6.032 6.166 6.300 6.434 6.568 6.703 7.400 7.560 7.721 7.882 46 .06166 .6166 1.233 1.850 2.467 3.083  $3.700 \\ 3.780 \\ 3.861$ 4.316 4.933 5.550 6.783 5.040 5.148 5.255 5.362 .06300 .6300  $\frac{1.260}{1.287}$ 1.890 2,520 3.150  $\frac{4.410}{4.504}$  $\frac{4.504}{4.598}$ 5,670 6.930 48 .06434 .6434 1.930 2.574  $\frac{3.217}{3.284}$ 5.791 5.91206568 .6568 1 970 3.941 2.627 .6703 1.341 8.043 50 .06703 2.011 2.681 4.0224.692 6.032

# TABLE OF ELECTRICAL HORSE-POWERS-(Continued.)

Amperes or Volts.	Volts or Amperes.												
Amj or V	1	10	20	30	40	50	60	70	80	90	100	110	120
55 60 65	.08713	.7373 .8043 .8713	1.609	2.413	3.217	3.686 4.022 4.357	4.424 4.826 5,228	5.161 5.630 6.099	5.898 6.434 6.970	6.635 7.239 7.842	7.373 8.043 8.713	8.110 8.847 9.584	8.847 9.652 10.46
70 75	.10054	.9384 1.005	1.877 2.011	2.815 3.016	3.753 4.021	4.692 5.027	5.630 6.032	6.568 7.037	7.507 8.043	8.445 9.048	9.384 10.05	$\frac{10.32}{11.06}$	11.26 12.06
80 85 90 95		1.072 1.139 1.206 1.273	2.145 2.279 2.413 2.547		4.290 4.558 4.826 5.094	5.362 5.697 6.032 6.367	6.434 6.836 7.239 7.641	7.507 7.976 8.445 8.914		9.652 10.26 10.86 11.46	10.72 11.39 12.06 12.73	11.80 12.53 13.27 14.01	12.87 13.67 14.48 15.28
100 200 300	.13405	1.341 2.681 4.022	2.681 5.362	4.022 8.043	5,362 10.72 16,09	6.703 13.41 20.11	8.043 16.09 24.13	9.384 18.77 28.15	10.72 21.45 32.17	12.06 24.13 36.19	13.41 26.81 40.22	14.75 29.49 44.24	16.09 32.17 48.26
400 500 600	.53620	5.362 6.703	10.72	16.09 20.11 24.13	21.45 26.81 32.17	26.81 33.51 40.22	32.17 40.22 48.26	37.53 46.92 56.30	42.90 53.62 64.34	48.26 60.32 72.39	53.62 67.03 80.43	58.98 73.73 88.47	64.34 80.43 96.52
700 800 900	.93835 1.0724 1.2065	9.384 10.72 12.06	18.77 21.45 24.13	36.19	37.53 42.90 48.26	$46.92 \\ 53.62 \\ 60.32$	56.30 64.34 72.39	65.68 75.07 84.45	75,07 85,79 96,52	84.45 96.52 108.6	93.84 107.2 120.6	103.2 118.0 132.7	112.6 128.7 144.8
1,000 2,000 3,000	1.3405 2.6810 4.0215	13.41 26.81 40.22	26.81 53.62		53.62 107.2 160.9	67.03 134.1 201.1	80.43 160.9 241.3	93.84 187.7 281.5	107.2 214.5 321.7	120.6 241.3 361.9	124.1 268.1 402.2	147.5 294.9 442.4	160.9 321.7 482.6
4,000 5,000 6,000	5.3620 6.7025 8.0430	53.62 67.03 80.43		160.9 201.1 241.3	214.5 268.1	268.1 335.1 402.2	321.7 402.2 482.6	375.3 469.2 563.0	429.0 536.2 643.4	482.6 603.2 723.9	536.2 670.3 804.3	589.8 737.3 884.7	643.4 804.3 965.2
7,000 8,000	9.3835 10.724	93.84	187.7 214.5	281.5 321.7	375.3 429.0	469.2 536.2	563.0 643.4	656.8 750.7	750.7 857.9	844.5 965.2	938.4 1072	1032 1180	1126 1287
	12.065 13.495	120.6 131.1	241.3 268.1	361.9 402.2		603.2 670.3	723.9 804.3	844.5 938.3	965.2 1072	1086 1206	1206 1341	1327 1475	1448 1609

Wire Table. - The wire table on the following page (from a circular of the Westinghouse El. & Mfg. Co.) shows at a glance the size of wire necessary for the transmission of any given current over a known distance with a given amount of drop, for 100-volt and 500-volt circuits, with varying losses. The formula by which this table has been calculated is

$$\frac{D \times 1000}{C \times 2L} = R$$

in which D equals the volts drop in electro-motive force, C the current, L the distance from the dynamo to the point of distribution, and R the line resistance in ohms per thousand feet.

Example 1.—Required the size of wire necessary to carry a current of 60

amperes a distance of 650 feet with a loss of 5% at 100 volts.

Referring to the table, under 60 amperes, we find the given distance, 650 feet. In the same horizontal line and under 5% drop at 100 volts, we find No. 000 wire, which is the size required.

EXAMPLE 2.—What size will be required for 10 amperes 2000 feet, with a

drop of 10% at 500 volts.

Under 10 amperes find 1930-the nearest figure to 2000-and in the same

horizontal line under 10% at 500 voits find No. 11, the size required.

Wiring Formulæ for Incandescent Lighting. (W. D. Weaver, Elec. World, Oct. 15, 1892.)—A formula for calculating wiring

tables is

$$A = \frac{2150 W}{aE^2} LN$$
, or,  $A = \frac{2150 LC}{aE}$ ,

where A = section in circular mils; W = watt rating of lamps; E = voltage; L = distance to centre of distribution, in feet; N = number of lamps; a = percentage of drop; C = current in amperes.

EXAMPLE.-Volts, 50; amperes, 100; feet to centre of distribution, 100; drop, 2%.

 $2150 \times 100 \times 100 = 215,000$  eircular mils,

# Wire Table for 100 and 500 Volt Circuits.

1   2   5   10   12.5   5   10   12.5   1   12.5   5   10   12.5   1   12.5   5   10   12.5   1   12.5   5   10   12.5   1   12.5   5   10   12.5   1   1   1   1   1   1   1   1   1											
1   2   6   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8			400		352232 2012 2012 2012 2012 2012 2012 2012	1:2388		ed /ire.			
1   2   6   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8   10   12.8			350				eres.	sulat ise W	5385858	3248888	855048
1   2   6   10   128   10   128   10   128   10   128   14   15   18   18   19   18   18   18   18   18			300			-	Amp	Hou			
1   2   6   10   128   10   128   10   128   10   128   14   15   18   18   19   18   18   18   18   18			275		356 284 178 141	H85%#	in	ad.			
1   2   6   10   128   10   128   10   128   10   128   14   15   18   18   19   18   18   18   18   18			250		392 312 247 196 155	88F84	ren	Bare	888888888888888888888888888888888888888	388888	3488850
1   2   6   10   128   10   128   10   128   10   128   14   15   18   18   19   18   18   18   18   18			225				e Cun	<u> </u>			
1   2   6   10   12.8			006	3			Saf	ze.	8880=00	- - - - - - - - - - - - - - - - - - -	227228
1   2   6   10   128			175								
1   2   6   10   128			150	100							
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		į.	195	160							
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15	;	ontio	10	3	280 480 390						
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		istri	8	8	et. 870 830 830 830						
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		of D	00	8	n Fe 1220 1220 770 610 490			-			
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		tre	9	2	288 1110 1110 100 100 100 100 100 100 100						
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15	,	Çer	00	8	Stan 1080 50 50 650		191	25 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2 2			
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		es to	8	8							
1   2   5   10   12   8   10   12   14   15   18   19   18   10   12   14   15   15   10   12   14   15   15   15   10   12   14   15   15   15   15   15   15   15		nper	1	G#	872.00						
1   2   6   10   12   8   10   12   8   10   12   12		Ψ	5	#0	2450 1950 1540 1230 970						
1   2   6   10   12   8   10   12   8   10   12   12			, i	8	2810 2240 1770 1400 1110		-		4		
1   2   5   10   12   5   10   12   14   15   14   15   15   15   15   15			9	20	252 252 253 253 253 253 253 253 253 253	1030 643 405 11030					_
Court Drop at 500 Yolks.   Court Drop at 500 Yolks.   Court Drop at 500 Yolks.   Court Drop at 100 Yolks.   Y			i d	82	3920 3115 2470 1960 1550	1228 976 774 615 488					
Court Drop at 500 Yolks.   Court Drop at 500 Yolks.   Court Drop at 500 Yolks.   Court Drop at 100 Yolks.   Y			8	25	4900 3910 3990 2450 1950	1550 1280 1650 1650 1650 1650 1650 1650 1650 165					
1   2   5   10   128   14   16   16   17   18   18   18   18   18   18   18			9	2	2730 2175	1355 1072 1072 852 675					
1   2   5   10   12   14   14   15   15   15   15   15   15			5	9	6100 3900 3450 2450	1206 1206 959 760					
Fer cent Drop at 500 Volts.  Fer cent Drop at 500 Volts.  Fer cent Drop at 100 Volts.  Fer cent Drop at 100 Volts.  Fer cent Drop at 100 Volts.  Brown & Sharp of			1	#	2800 2800 2800	2200 1740 1378 1095 867					
Er Cent Drop at 500 Volts.    1			1	12	\$200 6500 5160 3240	2600 2033 1608 1278 1013	804				
Er cent Drop at 500 Volts.  1   2   5   10   12.8  1   2   5   10   12.8  1   3   5   10   12.8  1   4   5   5   10   12.8  1   5   5   10   12.8  1   5   5   10   12.8  1   5   5   10   12.8  1   5   5   5   10   12.8  1   5   5   5   5   10   12.8  1   5   5   5   5   5   5   5   5   5			1	2	9800 7800 6200 3900	2440 1930 1530 1216	965	835 609 481	302 240 189 152 189	25 27 88 38 45 88 33 88	*******
Er cent Drop at 500 Volts  The cent Drop at 500 Volts  The cent Drop at 100 Volts  The		12.8						8118	20 2		
1   2   5   5   5   5   5   5   5   5   5	olts.	10	olts.		90 0,41℃0 ⊱∞	02H22	2	1292	20 21 28		
Per cent   Prop a   Prop	200 V	5	100 A		G-000 410						
Per cent	at	65	at 1	10	000	•					
	Drop		Drog	∞	22 00	H0:00410					60
	sent	-	ent	ı,	u 900	•					
0000 010004 P60000 011111 HENNE	Per		Pere	4	Brd						
				CS		9000	3	0100	# 12 G t - 00 Q	2222	22222

The horse-power and efficiency of a motor being given, the size of the conducting wire in circular mils can be found from the following formula:

$$A = \frac{160,400,000 \times \text{H.P.} \times L}{aE^2 \times \text{efficiency}}.$$

Example.—Horse-power, 10; volts, 500; drop, 3%; feed to distributing point, 600; efficiency of motor, 75%.

 $A = \frac{160,400,000 \times 10 \times 600}{3 \times 500 \times 500 \times 75} = 17,109$  circular mils, or about No. 8 B. & S.

# Cost of Copper for Long-distance Transmission. (Westinghouse El. & Mfg. Co.)

COST OF COPPER REQUIRED FOR THE DELIVERY OF ONE MECHANICAL HORSE-POWER AT MOTOR SHAFT WITH 1000, 2000, 3000, 4000, 5000, AND 10,000 VOLTS AT MOTOR TERMINALS, OR AT TERMINALS OF LOWERING TRANSFORMERS.

Loss of energy in conductors (drop), equals 20%.

Distances equal one to twenty miles.

Motor efficiency equals 90%.

Length of conductor per mile of single distance, 11,000 feet, to allow for sag.

Cost of copper equals 16 cents per pound

Cost of copper equals to cents per pound.									
Miles.	1000 v.	2000 v.	3000 v.	4000 v.	5000 v.	10,000 v.			
1	\$2.08	\$0.52	\$0.23	\$0.13	\$0.08	\$0.02			
2	8.33	2.08	0.93	0.52	0.33	0.08			
3	18.70	4.68	2.08	1.17	0.75	0.19			
4	33.30	8.32	3.70	2.08	1.33	0.33			
5	52.05	13.00	5.78	3.25	2.08	0.52			
6	74.90	18.70	8.32	4.68	3.00	0.75			
7	102.00	25.50	11.30	6.37	4.08	1.02			
1 2 3 4 5 6 7 8 9	133.25	33.30	14.80	8.32	5.33	1.33			
9	168.60	42.20	18.70	10.50	6.74	1.69			
10	208.19	52.05	23.14	13.01	8.33	2.08			
11	251.90	63.00	28.00	15.75	10.08	2.52			
12	299.80	75.00	33.30	18.70	12.00	3.00			
13	352.00	88.00	39.00	22.00	14.08	3.52			
` 14	408 00	102.00	45.30	25.50	16.32	4.08			
15	468.00	117.00	52.00	29,25	° 18.72	4.68			
16	533.00	133.00	59.00	33.30	21.32	5.33			
17	600.00	150.00	67.00	37.60	24.00	6.00			
18	675.00	169.00	75.00	42.20	27.00	6.75			
19	750.00	188.00	83.50	47.00	30.00	7.50			
20	833.00	208.00	92.60	52.00	33.32	8.33			

A Graphical Method of calculating leads for wiring for electric lighting is described by Carl Hering in Trans. A. I. E. I. 1891. He furnishes a chart containing three sets of diagonal straight-line diagrams so connected that the examples under the general formula for wiring may be solved without calculation by simply locating three points in succession on the chart.

The general principle upon which the chart is based is that for any formula containing three variable quantities, one of which is the product or the quotient of the other two, the "curves" representing their relative values may always be represented by a series of straight diagonal lines drawn through the centre or zero-point. Such a set of lines will therefore enable one to make any calculations graphically for that formula. For instance, horse-power = volts × amperes; the constant 746 does not concern us at present. A series of diagonal lines properly spaced will therefore give directly either the horse-power, the volts, or the amperes, when the other two are given.

One scale is vertical, the other horizontal, and the diagonal lines (or the hyperbolas) each represent one unit (or a number of units) of the third scale. To make the "curves" straight lines the diagonals must be made

COST OF COPPER REQUIRED TO DELIVER ONE MECHANICAL HORSE-POWER AT MOTOR-SHAFT WITH VARYING PERCENTAGES OF LOSS IN CONDUCTORS, UPON THE ASSUMPTION THAT THE POTENTIAL AT MOTOR TERMINALS IS IN EACH CASE 3000 VOLTS.

Distances equal one to twenty miles.

Motor efficiency equals 90%.

Length of conductor per mile of single distance, 11,000 feet, to allow for sag.

Cost of conner equals 16 cents per pound

con or copper equations council per pound.										
Miles.	10%	15%	20%	25%	30%					
1 9	\$0.52	\$0.33	\$0.23	\$0.17	\$0.13					
	2.08	1.31	0.93	0.69	0.54					
3	4.68	2.95	2.08	1.55	1.21					
4	8.32	5.25	3.70	2.77	2.15					
1 2 3 4 5 6 7 8	13.00 18.70 25.50	8.20 11.75 16.00	5.78 8.32 11.30	4.33 6.23 8.45	3.37 4.85 6.60					
8	33.30	21.00	14.80	11.00	8.60					
9	42.20	26.60	18.75	14.00	10.90					
10	52.05	32.78	23.14	17.31	13.50					
11	63.00	39.75	28.00	21.00	16.30					
12	75.00	47.20	33.30	24.90	19.40					
13	88.00	55.30	39.00	29.20	22.80					
14	102.00	64.20	45.30	33.90	26.40					
15	117.00	73.75	52.00	38.90	30.30					
16	133.00	83.80	59.00	44.30	34.50					
17	150.00	94.75	67.00	50.00	39.00					
18	169.00	106.00	75.00	56.20	43.80					
19	188.00	118.00	83.50	62.50	48.70					
20	208.00	131.00	92.60	69.25	54.00					

to represent one of the two quantities which is equal to the quotient of the other two, and not the one which is equal to the product of the other two, because the curves would then be hyperbolas. In the example given the diagonals must represent volts or amperes, but not horse-powers. The constants in such formule affect only the positions of the diagonals; although they increase considerably the work of arithmetically calculating the results, they do not affect in the least the graphical calculations after the diagrams are once drawn.

The general formula for wiring is:

 $Cross-section = \frac{current\ for\ one\ lamp \times No.\ of\ lamps \times distance \times constant}{constant}$ loss in volts

containing six quantities only, one of which is always constant, being equal containing six quantities only, one of which is always constant, being equal to twice the mil-foot resistance of copper, if the cross-section is in circular mils. Calculations involving three of these five quantities may readily be made graphically by means of a single set of diagonal lines. In Mr. Hering's method the formula is split up into three smaller ones, each of which contains no more than three variable quantities. Each formula can then be calculated separately by a simple diagram, as described, thus permitting the whole formula to be calculated graphically. To do this, let the first diagram perform the calculation,

 $x = \frac{\text{current for one lamp}}{}$ loss in volts

in which x is a mere auxiliary quantity. Let a second similar diagram perform the next calculation,

 $y = x \times \text{number of lamps};$ 

and a third diagram the final calculation,

cross-section =  $y \times$  distance.

The constant may be combined with any one of these, it is immaterial which one. This triple calculation may at first seem to complicate matters on account of the new quantities, x and y. These, however, are easily oil account of the new quantities, and y. These, however, are easily eliminated by the simple device of placing the three diagrams together, side by side, in such a position that the two x scales coincide, and similarly the two y scales. By doing this one has merely to pass directly from one set of diagonals to the next to perform the successive steps of the calculation, without being concerned about the intermediate auxiliary quantities. These intermediate quantities correspond, and are equal to the successive products or quotients which are obtained in the successive arithmetical multiplications and divisions of these five quantities in the formula, which cannot, of course, be eliminated in making the calculations arithmetically.

Weight of Copper required for Long-distance Transmission,—W. F. C. Hasson (Trans. Tech. Socy. of the Pacific Coast, vol. x, No. 4) gives the following formula:

$$W = \frac{D^2}{E^2}$$
 H.P.  $\frac{(100 - L)}{L}$  266.5,

where W is the weight of copper wire in pounds; D, the distance in miles; E, the E.M.F. at the motor in hundreds of volts; H.P., the horse-power delivered to the motor; L, the per cent of line loss.

Thus, to transmit 200 horse-power ten miles with 10 per cent loss, and

have 3000 volts at the motor, we have

$$W = \frac{10 \times 10}{30 \times 30} \times 200 \times \frac{(100 - 10)}{10} \times 266.5 = 53,300 \text{ lbs.}$$

Efficiency of Long-distance Transmission. (F. R. Hart, Power, Feb. 1892.)—The mechanical efficiency of a system is the ratio of the Foucer, Feb. 1892.—The mechanical efficiency of a system is the ratio of the power delivered to the dynamo-electric machines at one end of the line to the power delivered by the electric motors at the distant end. The commercial efficiency of a dynamo or motor varies with its load. The maximum efficiency of good machines should not be under 90% and is seldom above 92%. Under the most favorable conditions, then, we must expect a loss of say 9% in the dynamo and 9% in the motor. The loss in transmission, due to fall in electrical pressure or "drop" in the line, is governed by the size of the wires, the other conditions remaining the same. For a long-distance transmission plant this will vary from 5% upwards. With a loss of 5% in the line, the total efficiency of transmission will be slightly under 79%. With a loss of 10% in the line, the efficiency would be slightly under 77%. We may call 80% the practical limit of the efficiency with the apparatus of to-day. The methods for long-distance power transmission by electricity may be divided into three general classes: (1) Those using continuous current; (2) those using alternating current; and (3) regenerating or "motor-dynamo" systems. The subdivisions of each of these general classes are tabulated as follows: rollows:

The relative advantages of these systems vary with each particular transmission problem, but in a general way may be tabulated as below.

	System.	Advantages.	Disadvantages.		
	2-wire Low voltage.	Safety, simplicity.	Expense for copper.		
	High voltage.	Economy, simplicity.	Danger, difficulty of building machines.		
Continuous.	3-wire.	Low voltage on machines and saving in copper.	Not saving enough in copper for long dis-		
О	Multiple-wire.	Low voltage at machines and saving in copper.			
	Single phase.	Economy of copper.	Cannot start under load. Low efficiency.		
Alternating.	Multiphase.	Multiphase.  Economy of copper, synchronous speed unnecessary; applicable to very long distances.			
Alt	Motor-dynamo.	High-voltage transmis- sion. Low-voltage de- livery.	Expensive. Low efficiency.		

There are many factors which govern the selection of a system. For each problem considered there will be found certain fixed and certain unfixed conditions. In general the fixed factors are: (1) capacity of source of power; (2) cost of power at source; (3) cost of power by other means at point of delivery: (4) danger considerations at motors: (5) operation conditions: (6) construction conditions (length of line, character of country, etc.). The partly fixed conditions are: (7) power which must be delivered, i.e., the efficiency of the system; (8) size and number of delivery units. The variable ciency of the system; (8) size and number of delivery units. The variable conditions are: (9) initial voltage; (10) pounds of copper on line; (11) original cost of all apparatus and construction; (12) expenses, operating (fixed charges, interest, depreciation, taxes, insurance, etc.); (13) liability of trouble and stoppages; (14) danger at station and on line; (15) convenience in operating, making changes, extensions, etc. Assuming that the cost of dynamos, motors, etc., will be approximately the same whatever the initial pressure, the great variation in the cost of wire at different pressures is shown by Mr. Hart in the following figures, giving the weights of copper required for transmitting 100 house, ower 5 miles. required for transmitting 100 horse-power 5 miles:

Voltage,	Drop 10 per cent.	Drop 20 per cent.
2,000	16,800 lbs.	8,400 lbs.
3.000	7,400 ''	3,700 ''
10,000	6-90 "	210 "

Efficiency of a Combined Engine and Dynamo. — A compound double - crank Willians engine mounted on a single base with a dynamo of the Edison-Hopkinson type was tested in 1890, with results as follows: The low-pressure cylinder is 14 in. diam., 16 in. stroke; steam-pressure 190 lbs. It is coupled to a dynamo constructed for an output of 475 amperes at 110 volts when driven at 430 revolutions per minute. The armature is of the low construction is a bain plant wound, and is fitted with a ture is of the bar construction, is plain shunt-wound, and is fitted with a commutator of hard-drawn copper with mica insulation. Four brushes are carried on each rocker-arm.

Resistance of magnets	
Resistance of armature	
I.H.P	
E.H.P	72.2
Total efficiency	86.7 per cent
Consumption of water per I.H.P. hour	21.6 pounds
Consumption of water per E.H.P. hour	25 "

The engine and dynamo were worked above their full normal output, which fact would tend to slightly increase the efficiency.
The electrical losses were: Loss in magnet coils, 756 watts, equal to 1.4%;

loss in armature coil, 1386 watts, equal to 2.6%; so that the electrical efficiency

of the machine due to ohmic resistance alone was 96%. The remainder of the losses, a little over 8 horse-power, is due to friction of engine and dynamo, hysteresis, and the like.

dynamo, hysteresis, and the like.

Electrical Efficiency of a Generator and Motor.—A twelvemile transmission of power at Bodie, Cal., is described by T. H. Leggett
(Trans. A. I. M. E. 1894). A single-phase alternating current is used. The
generator is a Westinghouse 120 K. W. constant-potential 12-pole machine,
speed 890 to 870 revs. per min. The motor is a synchronous constant-potential machine of 120 horse-power. It is brought up to speed by a 10-H.P.
Tesla starting motor. Tests of the electrical efficiency of the generator and motor gave the following results:

TEST ON GENERATOR.

5	Amperes	Volts.	Watts.
Self-excited field		60 78	948 1419.6
C <sup>2</sup> R, loss in armature. Total loss in machine. Load.		3414	664.72 3032.32 68280

### Apparent electrical efficiency of generator, 95.559%.

### TEST ON MOTOR.

	Amperes	Volts.	Watts.
Self-excited field		62.4	3244.8 560.0
Total loss in machine.			3804.08 62200

## Apparent electrical efficiency of motor, 93,883%.

Efficiency of an Electrical Pumping-plant. (Eng. & M. Jour., Feb. 7, 1891.)—A pumping-plant at a mine at Normanton, England, was tested, with results given below:

Above ground there is a pair of 201/2 × 48-in, engines running at 20 revs. per min., driving two series dynamos giving 690 volts and 59 amperes. The current from each dynamo is carried into the mine by an insulated cable about rent from each dynamo is carried into the mine by an insulated cable about 3000 feet long. There they are connected to two 50-hp, motors which operate a pair of differential ram-pumps, with rams 6 in. and 4½ in. diam. and 24 in. stroke. The total head against which the pumps operate is 890 feet. Connected to the same dynamos there is also a set of gearing for driving a hauling plant on a continuous-rope system, and a set of three-throw rampumps with 6-inch rams and 12-inch stroke can also be thrown into gear. The connections are so made that either motor can operate any or all three of the sets of machinery just described. Indicator-diagrams gave the following the sets of machinery just described. lowing results:

Friction of engine	6.9 H.P.	9.4%
Belt and dynamo friction	4.8 "	6.5%
Leads and motor	6.7 "	9.4%
Motor belt, gearing and pumps empty	10.2 "	14.0%
Load of 117 gallons through 890 feet	31.5 "	43.1%
Water friction in pumps and rising main	12.9 "	17.6%
	73 0 H P	100 0%

At the time when these data were obtained the total efficiency of the plant was 43.1%, but in a later test it rose to 47%.

References on Power Distribution.—Kapp, Electric Transmission of Energy; Badt, Electric Transmission Handbook; Martin and Wetzler, Sin of Energy; Badt, Electric Transmission Handbook; Martin and Wetzler, The Electric Motor and its Applications; Hospitalier, Polyphased Electric Currents.

### ELECTRIC RAILWAYS.

Space will not admit of a proper treatment of this subject in this work. Consult Crosby and Bell, The Electric Railway in Theory and Practice, price \$2.00; Merrill, Reference Book of Tables and Formulæ for Street Railway Engineers, price \$1.00.

Test of a Street Railway Plant.—A test of a small electric-railway plant is reported by Jesse M. Smith in Trans. A. S. M. E., vol. xv. The following are some of the results obtained:

Friction of engine, air-pump, and holler feed-pump; main belt off 9.22 I.H.P. Friction of engine, air and feed pumps, and dynamo, brushes off. 11.34 I.H.P. Power required to charge fields of dynamo..... 3.00 I.H.P. 

Average I.H.P. del'd to pulley of dynamo, estimating friction of armature shaft to be the same as friction of belt...... 59.8 I.H.P. Number of single trips of cars..... 64 Average number of passengers on cars per single trip...... 15.2

Weight of cars ... 14.500 lbs. Est. total weight of cars and persons.... 15,900 lbs. 45,950 lbs. Average weight in motion ...... 0.98 E.H.P.

Average electrical horse-power per 1000 lbs. of weight moved... Average horse-power developed by engine per 1000 lbs. of weight moved..... ...... 1.52 I.H.P.

Average watts required per car. 11,615 watts
Average electrical horse-power per car. 15,54 E.H.P.
Average horse-power developed in engine per car 24,25 I.H.P.
Length of road. 10.5 miles.
Average speed, including all stops, 21 miles in 1.5 hours = 14 miles per hour.
Average speed between stops, 21 m. in 1.366 hours = 15.38 miles per hour.

Proportioning Boiler, Engine, and Generator for Powerstations. — Wm. Lee Church (Street Railway Journal, 1892) gives a diagram showing the abrupt variations in the current required for an electric railway with variable grades. For this case, in which the maximum current for a minute or two at a time is 175 amperes, ranging from that to zero, and averaging about 50 amperes, he advises that the nominal capacity of the generator be 100 amperes. The reason of this is found in the fact of that an electric generator can stand an overload, or even an excessive overload, provided it does not have to stand it long. The question is simply one of heat. The overload here was seen to continue for only about one minute, during which time the generator could carry it with ease with no perceptible rise of temperature to injure the insulation. Had this load been continuous for an hour or so, as would occur in an electric-lighting station, a much higher relative generating capacity would be required, approximating the

maximum load. An engine has no such capacity for excessive overload as a generator. In other words, the element of time does not enter into the engine problem, but it becomes a question of how much the engine can actually lift by main strength without taking the governor to an extreme which shall slow down the speed. In general terms, the engine should not be called to perform, even for a short time, more than 2%, or possibly 25%, above its rating.

The engine capacity, therefore, would have a nominal rating greater than that of the generator, say about 25% greater.

The capacity of the engine should be determined without reference to condensation. This is for the obvious reason that a condenser may become choked, or disabled, or leaky, and the vacuum may be poor, or lost entirely

under sudden fluctuations. The boiler has to deal only with the average of the total load. In this particular electric railways exactly resemble rolling - mills, saw - mills,

and kindred industries, where the load is spasmodic, with variations lasting but a few seconds, or at most but a few minutes. The stored heat in the water of a boiler is enormous in quantity, and responds instantly to a release of pressure. That is to say, the boiler is an immense reservoir of power, and provided the drain upon it is not continued too long, it will stand exactions far beyond its nominal capacity, and without any effect

whatever upon the firing,

The actual size of the boiler will depend upon the type of engine. With the compound engine described by Mr. Church, running non-condensing, an allowance of 30 pounds of water actually evaporated per LH.P. per hour will give a margin for all contingencies. The engine duty under an average uniform load is a very different thing from the duty under a variable load represented by the average. Under the uniform load, 32 pounds of water would be the actual engine performance, and the boiler could be proportioned with reference to this figure. Under the violent fluctuations of railway service, the average duty of the engine will rise to about 28 pounds, and if the maximum average load is taken, and the boiler proportioned for 30 pounds, there will be a sufficient margin. Other compound engines not least 45 pounds under light loads, and often to 60 pounds, and represent an average duty not better than 35 to 40 pounds. The same is true of every form of non-compounded engine, whether high speed or low speed, both of which show a tremendous falling back of fuel duty under variable load.

### ELECTRIC LIGHTING.

Quantity of Energy required to produce Light.—According to Mr. Preece, the quantity of energy, measured in watts, required to produce light equivalent to one candle-power, measured by the light given out by the standard candle, is as follows for different light-giving substances:

Tallow	124	watts	Coal gas	68	watts
Wax	94	**	Cannel gas	48	4.6
Spermaceti	86		Incandescent lamp	15	44
Mineral oils	80	44	Are lamp		
Vegetable oils	57	44			

And the relative costs of production are about 1 for the arc lamp; 6 for the incandescent lamp; 5 for the mineral-oil lamp; 10 for the gas-light; 67 for the

spermaceti candle.

Life of Incandescent Lamps. (Engig. Sept. 1, 1893, p. 282.)—From experiments made by Messrs. Siemens and Halske, Berlin, it appears that the average life of incandescent lamps at different expenditure of watts per candle-power is as follows:

Life and Efficiency Tests of Lamps. (P. G. Gossler, Elec. World, Sept. 17, 1892.)—Lamps burning at a voltage above that for which they are rated give a much greater illuminating power than 16 candles, but at the same time their life is very considerably shortened. It has been observed that lamps received from the factory do not average the same candlepower and efficiency for different invoices; that is, lamps which are received in one invoice are usually quite uniform throughout that lot, but they vary considerably from lamps made at other times.

The following figures show the different illuminating-powers of a 16.c.p.,

50-volt, 52-watt lamp, for various voltages from 25 to 80 volts:

Volts: 34.8 40 48 50 52.5 55.6 59.5 62 68.2 80 Amperes: .561 .774 .898 .968 1.097 1.161 1.4191.484 1.58 Candles: 2.47 5.1 12.6 15.8 20.5 28.439.3 50.7 74.5103.2Watts: 14.03 26.94 35.92 46.34 52.75 57.57 64.55 72.93 79.98 96.78 126.4 Watts per c.p.; 10.81 7.04 3.68 3.34 2.81 2.30 1.96 1.58 1.30 1.04 35.1

Street-lighting. (H. Robinson, M. I.C.E., Eng'g News, Sept. 12, 1891.)

—For street-lighting the arc-lamp is the most economical. The smallest

size of arc-lamp at present manufactured requires a current of about 5 amperes; but for steadiness and efficiency it is desirable to use not less than amperes, or to second a control of arc-lamps varies considerably, according to the angle at which it is measured. The greatest intensity with continuous-current lamps is found at an angle of about 40° below the horizontal line. The following table gives the approximate candle-power at various angles. The height of the lamps should be arranged so as to give an angle of not less than 7° to the most distant point it is intended to give an angle of not less than 7° to the most distant of the most distant point it is intended to give an angle of the point point it is intended to give an angle of the point point it is intended to give an angle of the point point in the point point is a second point point

### Lighting-power of Arc-lamps.

Qt	Candle-power.									
Current in Amperes.	Horizontal	At Angle	At Angle	At Angle	Maximum at					
-		of 7°.	of 10°.	of 20°.	Angle of 40°.					
6	92	175	207	322	460					
.8	156	300	350	546	780					
10	220	420	495	770	1100					

The following data enable the coefficient of minimum lighting-power in streets to be determined:

Let P = candle-power of lamps;

 $L = \max_{x \in \mathcal{X}} \min_{x \in \mathcal{X}}$ 

The light falling on the unit area of pavement varies inversely as the square of the distance from the lamp, and is directly proportional to the angle at which it falls. This angle is nearly proportional to the height of the lamp divided by the distance. Therefore

$$X = \frac{P}{L^2} \times \frac{H}{L} \quad \text{or} \quad X = \frac{PH}{L^3}.$$

The usual standard of gas-lighting is represented by the amount of light falling on the unit area of pavement 50 feet away from a 12-c.p. gas-lamp 9 feet high, which gives a coefficient as follows:

$$X = \frac{12 \times 9}{50^3} = 0.000864,$$

The minimum standard represents the amount of light on a unit area 50

feet away from a 24-c.p. lamp, 9 ft. high, and gives the coefficient. 001728.
Adopting the first of the above coefficients. Mr. Robinson calculates that the before-mentioned sizes of arc-lights will give the same standard of light at the heights and distances stated in Table A. Table B gives the corresponding distances, assuming the minimum standard to be adopted.

Т	ABLE	Α.				Тав	LE B.		
Hgt. of Lamps.	20 ft.	25 ft.	30 ft.	35 ft.	Height	20 ft.	25 ft.	30 ft.	35 ft.
Current in Amperes.		dista m la		served a ft.	Amperes.		distar	ces se Lamp.	rved
6 8 10	160 185 205	175 202 225	190 220 243	202 235 260	6 8 10	130 150 170	144 165 190	155 180 205	166 198 220

The distances the lamps are apart would, of course, be double the distances mentioned in Tables A and B. One arc-lamp will take the place of from 3 to 6 gas-lamps, according to the locality, arrangement, and standard of light adopted. A scheme of arc-lighting, based on the substitution of one arc-light on the average for 31/2 to 4 gas-lamps, would double the minimum standard of light, while the average standard would be increased 10 or 12 times.

Candle-power of the Are-light. (Elihu Thomson, *El. World*, Feb. 28, 1591.)—With the long are the maximum intensity of the light is from 40° to 60° downward from the horizontal. The spherical candle-power is only a fraction of the rated c.p., which is generally taken at the maximum obtainable in the best direction. For this reason the term 2000 c.p. has little

significance as indicating the illuminating-power of an arc. It is now generally taken to mean an arc with 10 amperes and not less than 45 volts between any taken to mean an arc with 10 amperes and not less than 45 voits between the carbons, or a 450-watta arc. The quality of the carbons will determine whether the 450 watts are expended in obtaining the most light or not, or whether that light will have a maximum intensity at one angle or another within certain limits. The larger the current passing in an arc, the less is its resistance. Well-developed arcs with 4 amperes will have about 11 ohms, with 10 amperes 4.5 ohms, and with 100 amperes .45 ohm.

It is not unusual to run from 50 to 60 lights in a series, each demanding

from 45 to 50 volts, or a total of, say, 3000 volts. In going beyond this the

difficulties of insulation are greatly increased.

Reference Books on Electric Lighting.—Noll, How to Wire Buildings, \$1.00; Hedges, Continental Electric-light Central Stations, \$6.00; Fleming, Alternating Current Transformers in Theory and Practice, 2 vols., \$8.00; Atkinson, Elements of Electric Lighting, \$1.50; Algave and Boulard, Electric Light: its History, Production, and Application, \$5.00.

### ELECTRIC WELDING.

The apparatus most generally used consists of an alternating-current dynamo, feeding a comparatively high-potential current to the primary coil of an induction coil or transformer, the secondary of which is made so large in section and so short in length as to supply to the work currents not exceeding two or three volts, and of very large volume or rate of flow. The welding clamps are attached to the secondary terminals. Other forms of apparatus, such as dynamos constructed to yield alternating currents direct from the armature to the welding-clamps, are used to a limited

The conductivity for heat of the metal to be welded has a decided influence on the heating, and in welding iron its comparatively low heat conduc-tion assists the work materially. Goe papers by Sir F. Branwell, Proc. Inst. C. E., part iv., vol. cii. p. 1; and Elihu Thomson, Trans. A. I. M. E., xix. 877.)

Fred. P. Royce, Iron Age. Nov. 28, 1892, gives the following figures show-

ing the amount of power required to weld axles and tires;

### AXLE-WELDING.

	Seconds
1-inch round axle requires 25 H.P. for	45
1-inch square axle requires 30 H.P. for	
11/4-inch round axle requires 35 H.P. for	. 60
11/4-inch square axle requires 40 H.P. for	70
2-inch round axle requires 75 H.P. for	95
2-inch square axle requires 90 H.P. for	100

The slightly increased time and power required for welding the square exie is not only due to the extra metal in it, but in part to the care which it is best to use to secure a perfect alignment.

### minn mar nine

$\begin{array}{llllllllllllllllllllllllllllllllllll$
$\begin{array}{llllllllllllllllllllllllllllllllllll$
114 × 34-inch tire requires 23 H.P. for
114 × 34-inch tire requires 23 H.P. for
$1\frac{1}{6} \times \frac{3}{6}$ -inch tire requires 20 H.P. for
$1\frac{1}{6} \times \frac{3}{6}$ -inch tire requires 20 H.P. for
$1\frac{1}{6} \times \frac{3}{6}$ -inch tire requires 20 H.P. for
1½ × 3/6-inch tire requires 20 H.P. for
114 × 14 inch tire requires 23 H P for 40
114 × 14-inch tire requires 23 H P for 40
2 × ½-inch tire requires 29 H.P. for
$2 \times 34$ -inch tire requires 42 H.P. for

The time above given for welding is of course that required for the actual application of the current only, and does not include that consumed by placing the axles or tires in the machine, the removal of the upset and other finishing processes. From the data thus submitted, the cost of welding can be readily figured for any locality where the price of fuel and cost of labor are known.

In almost all cases the cost of the fuel used under the boilers for producing power for electric welding is practically the same as the cost of fuel used in forges for the same amount of work, taking into consideration the difference in price of fuel used in either case.

Prof. A. B. W. Kennedy found that 2½-inch iron tubes ¼ inch thick were

welded in 61 seconds, the net horse-power required at this speed being 23.4 (say 33 indicated horse-power) per square inch of section. Brass tubing required 21.2 net horse-power. About 60 total indicated horse-power would be required for the welding of angle irons  $3 \times 3 \times \frac{1}{2}$  inch in from two to three minutes. Copper requires about 80 horse-power per square inch of section, and an inch bar can be welded in 25 seconds. It takes about 90 seconds to weld a steel bar 2 inches in diameter.

### ELECTRIC HEATERS.

Wherever a comparatively small amount of heat is desired to be automatically and uniformly maintained, and started or stopped on the instant without waste, there is the province of the electric heater.

The elementary form of heater is some form of resistance, such as coils of thin wire introduced into an electric circuit and surrounded with a substance, which will permit the conduction and radiation of heat, and at the

same time serve to electrically insulate the resistance. This resistance should be proportional to the electro-motive force of the current used and to the equation of Joule's law :

$$H = C^2Rt \times 0.24$$
.

where C is the current in amperes; R, the resistance in ohms; t, the time in

seconds; and h, the heat in gram-centigrade units.

Since the resistance of metals increases as their temperature increases, a thin wire heated by current passing through it will resist more, and grow hotter and hotter until its rate of loss of heat by conduction and radiation equals the rate at which heat is supplied by the current. In a short wire, before heat enough can be dispelled for commercial purposes, fusion will begin; and in electric heaters it is necessary to use either long lengths of thin wire, or carbon, which alone of all conductors resists fusion. In the majority of heaters, coils of thin wire are used, separately embedded in some substance of poor electrical but good thermal conductivity.

The Consolidated Car-heating Co.'s electric heater consists of a galvanized iron wire wound in a spiral groove upon a porcelain insulator. Each heater is 305% in long, 87% in high, and 65% in wide. Upon it is wound 625 ft. of wire. The weight of the whole is 231% lbs.

Each heater is designed to absorb two amperes of a 500-volt current. heaters are the complement for an ordinary electric car. For ordinary weather the heaters may be combined by the switch in different ways, so that five different intensities of heating-surface are possible, besides the position in which no heat is generated, the current being turned entirely off.

For heating an ordinary electric car the Consolidated Co. states that from 2 to 12 amperes on a 500-volt circuit is sufficient. With the outside temperature at 20° to 30°, about 6 amperes will suffice. With zero or lower temperature, the full 12 amperes is required to heat a car effectively.

Compare these figures with the experience in steam-heating of railway-

cars, as follows:

1 B.T.U. = 0.29084 watt-hours.

6 amperes on a 500-volt circuit = 3000 watts.

A current consumption of 6 amperes will generate 3000 ÷ 0.29084 = 10,315

B.T.U. per hour.

In steam-car heating, a passenger coach usually requires from 60 lbs, of steam in freezing weather to 100 lbs. in zero weather per hour. Supposing the steam to enter the pipes at 20 lbs. pressure, and to be discharged at 200° F., each pound of steam will give up 983 B.T.U. to the car. Then the equivalent of the thermal units delivered by the electrical-heating system in pounds of steam, is 10,315 ÷ 983 = 10½, nearly.

Thus the Consolidated Co,'s estimates for electric-heating provide the

equivalent of 101/2 lbs. of steam per car per hour in freezing weather and 21

lbs, in zero weather.

Suppose that by the use of good coal, careful firing, well designed boilers. and triple-expansion engines we are able in daily practice to generate 1 H.P. delivered at the fly-wheel with an expenditure of 21/2 lbs. of coal per hour.

We have then to convert this energy into electricity, transmit it by wire to the heater, and convert it into heat by passing it through a resistance-coll. We may set the combined efficiency of the dynamo and line circuit at \$5%, and will suppose that all the electricity is converted into heat in the resistance-coils of the radiator. Then 1 brake H.P. at the engine = 0.85 electrical H.P. at the resistance-coil = 1,683,000 ft.-lbs. energy per hour = 2180 heatunits. But since it required 21/2 lbs. of coal to develop 1 brake H.P., it follows that the heat given out at the radiator per pound of coal burned in the boiler furnace will be 2180 + 2 $\frac{1}{2}$  = 872 H.U. An ordinary steam-heating system utilizes 9652 H.U. per 1b. of coal for heating; hence the efficiency of the electric system is to the efficiency of the steam-heating system as 872 to 9652, or about 1 to II. (Eng'g News, Ang. 9,  $^{9}g$ ; Mar. 30,  $^{9}g$ ; May 15,  $^{9}g$ 3.

### ELECTRICAL ACCUMULATORS OR STORAGE-BATTERIES.

Storage-batteries may be divided into two classes; viz., those in which the active material is formed from the substance of the element itself, either by direct chemical or electro-chemical action, and those in which the chemical formation is accelerated by the application of some easily reducible salt of lead. Elements of the former type are usually called Planté, and those of the latter "Faure," or "pasted."

Faraday when electrolyzing a solution of acetate of lead found that per-oxide of lead was produced at the positive and metallic lead at the negative oxide of feat was produced at the positive and metanic read at the legative pole. The surfaces of the elements in a newly and fully and fully charged Planté cell consists of nearly pure peroxide of lead, PbO<sub>2</sub>, and spongy metallic lead, Pb<sub>1</sub>, respectively on the positive and negative plates.

During the discharge, or if the cell be allowed to remain at rest, the sulphuric acid (H<sub>8</sub>SO<sub>4</sub>) in the solution enters into combination with the percoide and spongy lead, and partially converts it into sulphate. The acid being continually abstracted from the electrolyte as the discharge proceeds, the density of the solution becomes less. In the charging operation this action is reversed, as the reducible sulphates of lead which have been formed are apparently decomposed, the acid being reinstated in the liquid and therefore causing an increase in its density.

The difference of potential developed by lead and lead peroxide immersed

in dilute H<sub>2</sub>SO<sub>4</sub> is, as nearly as may be, two volts.

A lead-peroxide plate gradually loses its electrical energy by local action, the rate of such loss varying according to the circumstances of its prepara-tion and the condition of the cell. Various forms of both Planté and Faure batteries are illustrated in "Practical Electrical Engineering."

In the Faure or pasted cells lead plates are coated with minium or litharge made into a pasted cells lead plates are coated with minium or litharge made into a paste with acidulated water. When dry these plates are placed in a bath of dilute H<sub>2</sub>SO<sub>4</sub> and subjected to the action of the current, by which the oxide on the positive plate is converted into peroxide of lead and that on the negative plate reduced to finely divided or porous

Gladstone and Tribe found that the initial electro-motive force of the Faure cell averaged 2.25 volts, but after being allowed to rest some little time it was reduced to about 2.0 volts. The following tables show the size and capacity of two types of Faure cells, known as the E. P. S. cells. (English.)

### "E. P. S." Storage-cells, L Type.

	ription of Cell.	of yte.	Workin	ng Rate.	ity.	Appronal	oxim Dim	ate ensi	Exterons.	Cell
No. of Plates.	Material of Box.	rot	Charge	Dis- charge.	Capacity Ampere hou	Length.	Width.	Height.	Height over all,	Weight of C complete v Acid.
		lbs.	Amper.	Amper.		in.	in.	in.	in.	lbs.
7 {	Wood	18	10 to 13	1 to 13	130	51/4	131/4	181/4	201/2	74
. 1	Glass	25	10 " 13	1 " 13	130	51/2	111/2	133/8	1534	68
- 11 {	Wood	25	16 " 22	1 " 22	220	71/2			201/2	107
}	Glass	35	16 " 22	1 " 22	220	8		133%	153/4	101
15	Wood	35	25 " 30	1 " 30	330	91/2		181/4	201/2	143
10)	Glass	47	25 " 30	1 " 30	330	95%	113/4	133%	1534	128
23 {	Wood	53	38 " 46	1 " 46	500	143/4	131/5	1814	201/2	228
~0)	Glass	67	38 " 46	1 " 46	500	141/4	1134	133/	157%	211
04	Wood	70	50 ** 60	1 " 60	660	1914	133/4	1814	201/2	286
31 }	Glass	88	50 " 60	1 " 60	660	181/6	12	133/4	15%	265

### "E. P. S." Cells, T Type.

ription of Cell.	of te.	Workin	g Rate	y.	App	rox. Dime	Ex	ternal ns.	ith
Material of Box.	Weight Electroly	Charge	Dis- charge.	Capacit Ampere ho	Length.	Width.	Height.	Height over all.	Weight of C complete w Acid.
" (with lid) Ebonite (no lid) Wood (no lid) " (with lid) Ebonite (no lid),	10 10 14 14 14	16 to 20 16 " 20 16 " 20 24 " 28 24 " 28 24 " 28	1 to 20 1 " 20 1 " 20 1 " 30 1 " 30 1 " 30	66 66 66 95 95	in. 67/8 67/8 6 83/4 87/8 8	in. 834 834 734 834 834 734	in. 115% 113% 11 115% 1115% 113%	in, 13½ 13¾ 12¾ 13¼ 13¾ 13¾ 12¾	1bs. 37 38 30 52 53 42
" (with lid) Ebonite (no lid) Wood (no lid)	18 18 22	30 " 35 30 " 35 38 " 42	1 " 40 1 " 40 1 " 50	120 120 145	10½ 13½	87/8 87/8 73/4 87/8	115/8 113/8 11 115/8	13½ 13¾ 12¾ 13¼ 13½	65 66 54 79 80
	Material of Box.  Wood (no lid) " (with lid) " (boile id) " (boile id) " Ebonite (no lid) " (with lid) " (with lid) "	Material of Box.    Material of Box.	Material of Box. Charge   10   10   10   10   10   10   10   1	Material of Box.   Dis-	Material of   2   2   2   2   2   2   2   2   2	Material of Box.   Sign   Si	Material of Box.   Section   Secti	Material of Box.   Modern   Modern	Material of

For a very full description of various forms of storage-batteries, see "Practical Electrical Engineering," part xii. For theory of the battery and

practice with the Julien battery, see paper on Electrical Accumulators by P. G. Salom, Trans. A. I. M. E., xviii. 348. Use of Storage-batteries in Power and Light Stations. (Iron Age, Nov. 2, 1893.)—The storage-batteries in the Edison station, in Fifty-third Street, New York, relieve the other stations at the hours of heavy load, by delivering into the mains a certain amount of current that would otherwise have to come, and at greater loss or "drop," from one or another of the stations connecting with the network of mains. Hence the load may be varied more or less arbitrarily at these stations according to the proportion of load that the larger stations are desired or able to carry.

The battery consists of 140 cells each of about 1000 ampere-hour capacity, weighing some 750 lbs., and of about 48 inches in length, 21 inches in width, and 15 inches in depth. The battery has a normal discharge rate of about

and to inches in depth. The batterly has a normal discharge rate of about 200 amperes, but can be discharged, if necessary, at 500 amperes. A test made when the station was running only 12 hours per day, from noon to midnight, showed that the battery furnished about 23.3% of the total energy delivered to the mains. The maximum rate of discharge attained by the battery was about 270 amperes. Thus, in this case, we have an example of a battery which is used for the purpose: 1. Of giving a load to station machinery that would otherwise be idle. 2. Utilizing the stored energy to increase the rate of output of the station at the time of heavy load, which would otherwise necessitate greater dynamo capacity.

The Working Current, or Energy Efficiency, of a storage-cell is the ratio between the value of the current or energy expended in the charging operation, and that obtained when the cell is discharged at any specified rate.

In a lead storage cell, if the surface and quantity of active material be accurately proportioned, and if the discharge be commenced immediately after the termination of the charge, then a current efficiency of as much as 98% may be obtained, provided the rate of discharge is low and well regulated. In practice it is found that low rates of discharge are not economical, and as the current efficiency always decreases as the discharge rate in creases, it is found that the normal current efficiency seldom exceeds 90%, and averages about 85%.

As the normal discharging electro-motive force of a lead secondary cell never exceeds 2 volts, and as an electro-motive force of from 2.4 to 2.5 volts is required at its poles to overcome both its opposing electro-motive force and its internal resistance, there is an initial loss of 20% between the energy

required to charge it and that given out during its discharge. As the normal discharging potential is continually being reduced as the rate of discharge increases, it follows that an energy efficiency of 80% can

never be realized. As a matter of fact, a maximum of 75% and a mean of 60% is the usual energy efficiency of lead-sulphuric-acid storage-cells.

### ELECTRO-CHEMICAL EQUIVALENTS.

Elements,	Valency.*	Atomic Weight,+	Chemical Equivalent.	Electro-chemical Equivalent (mil- ligrammes per coulomb).	Coulombs per gramme.	Grammes per ampere hour.
ELECTRO-POSITIVE.						
Hydrogen Potassium Sodium Aluminum Magnesium Gold Sliver Copper (cuprie) (cuprous) Mercurry (mercuries) " (stannous) " (stannous) " (ferrous) " (ferrous) " (ferrous) " (Linc Lead	H <sub>1</sub> K <sub>1</sub> Na <sub>1</sub> Al <sub>3</sub> Mg <sub>2</sub> Au <sub>3</sub> Ag <sub>1</sub> Cu <sub>2</sub> Cu <sub>1</sub> Hg <sub>1</sub> Hg <sub>1</sub> Fe <sub>4</sub> Fie <sub>2</sub> Ni <sub>2</sub> ZPb <sub>2</sub>	1.00 39.04 22.99 27.3 23.94 196.2 107.66 63.00 63.00 199.8 117.8 117.8 55.9 58.6 64.9	1.00 39.04 22.99 9.1 11.97 65.4 107.66 31.5 63.00 99.9 199.8 29.45 58.9 18.64 27.95 29.8 32.45 19.8	.010384 .40539 .23873 .09449 .12430 .67911 1.11800 .32709 .65419 1.03740 2.07470 .30581 .61162 .19356 .29035 .33696 1.07160	96293.00 2467.50 4188.90 1058.30 804.03 1473.50 894.41 3058.60 1525.30 963.99 481.99 3270.00 1635.00 5166.4 3445.50 3286.80 2967.10	0.03738 1.45950 0.85942 3.40180 4.47470 2.44480 4.02500 1.17700 2.35500 7.46900 1.10090 2.20180 0.69681 1.04480 1.09530 1.21330 3.85780
ELECTRO-NEGATIVE.						
Oxygen	$\begin{array}{c} \mathrm{O_2} \\ \mathrm{Cl_1} \\ \mathrm{I_1} \\ \mathrm{Br_1} \\ \mathrm{N_3} \end{array}$	15.96 35.37 126.53 79.75 14.01	7.98 35.37 126.53 79.75 4.67	.08286 .36728 1.31390 .82812 .04849		

<sup>\*</sup> Valency is the atom-fixing or atom-replacing power of an element compared with hydrogen, whose valency is unity. † Atomic weight is the weight of one atom of each element compared with

hydrogen, whose atomic weight is unity.

‡ Becquerel's extension of Faraday's law showed that the electro-chemical

the equivalent of an element is proportional to its chemical equivalent. The latter is equal to its combining weight, and not to atomic weight + valency, as defined by Thompson, Hospitalier, and others who have copied their tables. For example, the ferric salt is an exception to Thompson's rule, as are sesqui-salts in general.

### ELECTROLYSIS.

The separation of a chemical compound into its constituents by means of an electric current. Faraday gave the nomenclature relating to electrolysis. He called the compound to be decomposed the Electrolyte, and the process Electrolysis. The plates or poles of the battery he called Electrodes. The plate where the greatest pressure exists he called the Anode, and the other pole the Cathode. The products of decomposition he called Ions.

Lord Rayleigh found that a current of one ampere will deposit 0.017253 grain, or 0.001118 gramme, of silver per second on one of the plates of a silver voltameter, the liquid employed being a solution of silver nitrate containing from 15% to 20% of the salt.

The weight of hydrogen similarly set free by a current of one ampere is

.00001038 gramme per second.

Knowing the amount of hydrogen thus set free, and the chemical equivalents of the constituents of other substances, we can calculate what weight of their elements will be set free or deposited in a given time by a given current.

Thus the current that liberates 1 gramme of hydrogen will liberate 8 grammes of oxygen, or 107.7 grammes of silver, the numbers 8 and 107.7

grammes of oxygen, or 107.7 grammes of silver, the numbers 8 and 107.7 being the chemical equivalents for oxygen and silver respectively. To find the weight of metal deposited by a given current in a given time, find the weight of hydrogen liberated by the given current in the given time, and multiply by the chemical equivalent of the metal. Thus: Weight of silver deposited in 10 seconds by a current of 10 amperes = weight of hydrogen liberated per second × number seconds × current strength × 107.7 = .00001038 × 10 × 10 × 107.7 = .11178 gramme. Weight of copper deposited in 1 hour by a current of 10 amperes =

 $.00001038 \times 3600 \times 10 \times 31.5 = 11.77$  grammes.

Since 1 ampere per second liberates .00001038 gramme of hydrogen, strength of current in amperes

> weight in grammes of H. liberated per second .00001038

weight of element liberated per second  $=\frac{0.00001038 \times \text{chemical equivalent of element}}{0.00001038 \times \text{chemical equivalent of element}}$ 

The table on page 1057 (from "Practical Electrical Engineering") is calculated upon Lord Rayleigh's determination of the electro-chemical equivalents and Roscoe's atomic weights.

### ELECTRO-MAGNETS.

### Units of Electro-magnetic Measurements.

C.G.S. unit of force = 1 dyne = 1.01936 milligrammes in localities in which C.G.s. unit of lorce = 1 type = 1.0) so immigratimes in locarities in wine the acceleration due to gravity is 981 centimetres, or 32.185 feet, per second. C.C.S. unit of energy = 1 erg = energy required to overcome the resistance of 1 dyne at a speed of 1 centimetre per second. 1 watt =  $10^{\circ}$  ergs.

Unit magnetism = that amount of magnetic matter which, if concentrated in a point, will repel an equal amount of magnetic matter concentrated in

another point one centimetre distant with the force of one dyne. Unit strength of field = that flow of magnetic lines which will exert unit

mechanical force upon unit pole, or a density of 1 line per square centimetre.

The following definitions of practical units of the magnetic circuit are given in Houston and Kennelly's "Electrical Engineering Leaflets."

Gilbert, the unit of magneto-motive force; such a M.M.F. as would be

produced by  $\frac{10}{4\pi}$  or 0.7958 ampere-turn.

If an air-core solenoid or hollow anchor-ring were wound with 100 turns of insulated wire carrying a current of 5 amperes, the M.M.F. exerted would be 500 ampere-turns = 628.5 gilberts.

Weber, the unit of magnetic flux; the flux due to unit M.M.F. when the reluctance is one oersted.

Gauss, the unit of magnetic flux-density, or one weber per normal square centimetre. The flux-density of the earth's magnetic field in the neighborhood of

New York is about 0.6 gauss, directed downwards at an inclination of about

Oersted, the unit of magnetic reluctance; the reluctance of a cubic centimetre of an air-pump vacuum.

Reluctance is that quantity in a magnetic circuit which limits the flux under a given M.M.F. It corresponds to the resistance in the electric circuit.

The reluctivity of any medium is its specific reluctance, and in the C.G.S. system is the reluctance offered by a cubic centimetre of the body between opposed parallel faces. The reluctivity of nearly all substances, other than the magnetic metals, is sensibly that of vacuum, is equal to unity, and is independent of the flux density.

Permeability is the reciprocal of magnetic reluctivity.

The fundamental equation of the magnetic circuit is

Webers =  $\frac{\text{gilberts}}{\text{persteds}}$ ;

magnetic flux = magneto-motive force + magnetic reluctance. From this equation we have

Gilberts = webers × oersteds; oersteds = gilberts + webers.

There are therefore two ways of increasing the magnetic flux: 1. by in-

easing the M.M.F.; 2, by decreasing the reluctance.

Lines and Loops of Force.—In discussing magnetic and electrical enomena it is conventionally assumed that the attractions and repulsions shown by the action of a magnet or of a conductor upon iron filings are the to "lines of force" surrounding the magnet or conductor. The "numous of the tor of lines indicates the magnitude of the forces acting. As the iron ups arrange themselves in concentric circles, we may assume that the "ces may be represented by close curves or "loops of force." The followz assumptions are made concerning the loops of force in a conductive cuit:

1. That the lines or loops of force in the conductor are parallel to the axis

the conductor.

2. That the loops of force external to the conductor are proportional in mber to the current in the conductor, that is, a definite current generates a lefinite number of loops of force. These may be stated as the strength of field in proportion to the current.

3. That the radii of the loops of force are at right angles to the axis of

the conductor

The magnetic force proceeding from a point is equal at all points on the race of an imaginary sphere described by a given radius about that dist. A sphere of radius 1 cm. has a surface of  $4\pi$  square centimetres. If = total field strength, expressed as the number of lines of force emanatary from a pole containing M units of magnetic matter,

$$F = 4\pi M$$
:  $M = F \div 4\pi$ .

Magnetic moment of a magnet = product of strength of pole M and its length, or distance between its poles L. Magnetic moment = -

If B = number of lines flowing through each square centimetre of cross-section of a bar-magnet, or the "specific induction," and A = cross-section,

Magnetic moment = 
$$\frac{LAB}{4\pi}$$
.

If the bar-magnet be suspended in a magnetic field whose induction is H, d so placed that the lines of the field are all horizontal and at right angles the axis of the bar, the north pole will be pulled forward, that is, in the direction in which the lines flow, and the south pole will be pulled in the posite direction, the two forces producing a torsional moment or torque,

Torque = 
$$MLH = LABH + 4\pi$$
, in dyne-centimetres.

Magnetic attraction or repulsion emanating from a point varies inversely the square of the distance from that point. The law of inverse squares, wever, is not true when the magnetism proceeds from a surface of ap-eciable extent, and the distances are small, as in dynamo-electric achines. (For an analogy see "Radiation of Heat," page 467.)

Strength of an Electro-magnet. - In an electric magnet made by biling a current-carrying conductor around a core of soft iron, the space which the loops of force have influence is called the magnetic field, and is convenient to assume that the strength of the field is proportional to be number of loops of magnetic force surrounding the magnet. Under this assumption, if we take a given current passing through a given number conductor-turns, the number of magnetic loops will depend upon the sistance of the magnetic circuit, just as the current with a given pressme in the conductive circuit depends upon the resistance of the circuit.

The following laws express the most important principles concerning

e ectro-magnets :

(1) The magnetic intensity (strength) of an electro-magnet is nearly pro-ortional to the strength of the magnetizing current, provided the core is - ot saturated.

(2) The magnetic strength is proportional to the number of turns of wire in the magnetizing coil; that is, to the number of ampere turns.

(3) The magnetic strength is independent of the thickness or material of

the conducting wires.

These laws may be embraced in the more general statement that the strength of an electro-magnet, the size of the magnet being the same, is proportional to the number of its ampere turns.

proportional to the number of its ampere turns. Force in the Gap between Two Poles of a Magnet.—If P = force exerted by one of the poles upon a unit pole in the gap, and m = density of lines in the field (that is, that there are m absolute or C.G.S. units on each square centimetre of the polar surface of the magnet, the polar surface being large relative to the breadth of the gap,  $P = 2\pi m$ . The total force exerted upon the unit pole by both north and south poles of the magnet is  $2P = 4\pi m$ , in dynes = B, or the induction in lines of force per square centimetre. If S = number of square centimetres in each polar surface, SB = total flow of force, or field strength = F; Sm = total pole strength = M, spread over each of the polar surfaces. We then have  $F = 4\pi M$ , as before; that is, the total field is  $4\pi$  times the total pole strength. Total attractive force between the two opposing poles of a magnet, when the distance apart is small,  $= \frac{SB^2}{8\pi}$ , in dynes.

This formula may be used to determine the lifting-power of an electro-

magnet, thus:

A bent magnet provided with a keeper is 3 cm. square on each pole, and the induction B = 20,000 lines per square centimetre. The attractive force of each limb on the keeper in dynes =  $\frac{9 \times 20000^2}{8 \times 3.14}$ , or in kilogrammes for

both limbs,  $\frac{9 \times 400 \times 10^6}{25.12 \times 981000} \times 2 = 292$  kilogrammes.

The Magnetic Circuit.—In the conductive circuit we have  $C = \frac{E}{C}$ ;

 $Current = \frac{electro-motive\ force}{resistance} = \frac{volts}{ohms}$ In the magnetic circuit we have

Number of lines, or loops, of force, or magnetism

 $= \frac{\text{Current} \times \text{conductor turns}}{\text{Resistance of magnetic circuit}} = \frac{\text{Ampere turns}}{\text{Resistance of magnetic circuit}}$ 

Or, in the new notation, webers =  $\frac{\text{gilberts}}{\text{oersteds}}$ .

Let N = No, of lines of force, Rm = total magnetic resistance, At =ampere turns, then  $N = \frac{At}{Rm}$ .

The magnetic pressure due to the ampere turns =  $\frac{4}{10}\pi TC = 1.257 Tc$ , where T = turns and C = amperes, whence  $N = \frac{4\pi TC}{Rm} = \frac{1}{Rm}$ 

If Rm = total magnetic resistance, and Ra, RA, RF the magnetic resistances of the air-spaces, the armature, and the field-magnets, respectively,

$$Rm = Ra + R_A + R_F$$
; and  $N = \frac{4\pi TC}{Ra + R_A + R_F}$ 

Determining the Polarity of Electro-magnets.—If a wire is wound around a magnet in a right-handed helix, the end at which the current flows into the helix is the south pole. If a wire is wound around an ordinary wood screw, and the current flows around the helix in the direction from the head of the screw to the point, the head of the screw is the south pole. If a magnet is held so that the south pole is opposite the eye of the observer, the wire being wound as a right-handed helix around it, the worst flows in a vight handed direction with the hande of a clock. current flows in a right-handed direction, with the hands of a clock.

### DYNAMO-ELECTRIC MACHINES.

There are four classes of dynamo-electric machines, viz.:

1. The dynamo, in which mechanical energy of rotation is converted into the energy of a direct current. 2. The alternator, in which mechanical energy of rotation is converted into

the energy of an alternating current.

3. The motor, in which the energy of a direct current is converted into mechanical energy of rotation.

4. The alternate-current motor, in which the energy of one or more alter-

nating currents is converted into mechanical energy of rotation,

For a steady direct current the product of the potential difference and the current strength is a true measure of the energy given off. With alternating currents the product of voltage into current strength is greater than the true energy, since the conductor has the property of reacting upon itself, called "self-induction."

Kinds of Dynamo-electric Machines as regards Man-

ner of Winding. (Houston's Electrical Dictionary.)
1. Dynamo-electric Machine.—A machine for the conversion of mechanical energy into electrical energy by means of magneto-electric induction.

2. Compound-wound Dynamo.—The field-magnets are excited by more

than one circuit of coils or by more than a single electric source,
3. Closed-coil Dynamo.—The armature-coils are grouped in sections com-

municating with successive bars of a collector, so as to be connected continuously together in a closed circuit. 4. Open-coil Dynamo.—The armature-coils, though connected to the suc-

cessive bars of the commutator, are not connected continuously in a closed circuit.

5. Separate-coil Dynamo.—The field-magnets are excited by means of coils on the armature separate and distinct from those which furnish current to the external circuit. 6. Separately-excited Dynamo, -The field-magnet coils have no connec-

tion with the armature-coils, but receive their current from a separate

machine or source.

7. Series-wound Dynamo.-The field-current and the external circuit are connected in series with the armature circuit, so that the entire armature current must pass through the field-coils.

Since in a series-wound dynamo the armature-coils, the field, and the external-series circuit are in series, any increase in the resistance of the external circuit will decrease the electro-motive force from the decrease in the magnetizing currents. A decrease in the resistance of the external circuit will, in a like manner, increase the electro-motive force from the increase in the magnetizing current. The use of a regulator avoids these changes in the electro-motive force.

8. Series and Separately-excited Compound-wound Dynamo.—There are two separate circuits in the field-magnet cores, one of which is connected in series with the field-magnets and the external circuit, and the other with

some source by which it is separately excited.

9. Shunt-wound Dynamo.—The field-magnet coils are placed in a shunt to the armature circuit, so that only a portion of the circuit generated passes through the field magnet coils, but all the difference of potential of the armature acts at the terminals of the field-circuit.

In a shunt-dynamo machine an increase in the resistance of the external circuit increases the electro-motive force, and a decrease in the resistance

of the external circuit decreases the electro-motive force. This is just the reverse of the series-wound dynamo.

In a shunt-wound dynamo a continuous balancing of the current occurs, The current dividing at the brushes between the field and the external circuit in the inverse proportion to the resistance of these circuits, if the resistance of the external circuit becomes greater, a proportionately greater current passes through the field-magnets, and so causes the electro-motive force to become greater. If, on the contrary, the resistance of the external circuit decreases, less current passes through the field, and the electromotive force is proportionately decreased.

10. Series- and Shunt-wound Compound-wound Dynamo.—The field-magnets are wound with two separate coils, one of which is in series with the armature and the external circuit, and the other in shunt with the armature. This is usually called a compound-wound machine.

11. Shunt and Separately-excited Compound-wound Dynamo, -The field

is excited both by means of a shunt to the armature circuit and by a current produced by a separate source.

Current Generated by a Dynamo-electric Machine. - Unit current in the C.G.S system is that current which, flowing in a thin wire forming a circle of one centimetre radius, acts upon a unit pole placed in the centre with a force of  $2\pi$  dynes. One tenth of this unit is the unit of current used in practice, called the ampere.

A wire through which a current passes has, when placed in a magnetic field, a tendency to move perpendicular to itself and at right angles to the lines of the field. The force producing this tendency is P = leB dynes, in which l = length of the wire, c = the current in C.G.S. units, and B the in-

duction in the field in lines per square centimetre. If the current C is taken in amperes,  $P = lCB10^{-1}$ .

If  $P_{L}$  is taken in kilogrammes,

$$P_k = \frac{lCB}{9810000} = 10.1937lCB10^{-8}$$
 kilogrammes.

Example.—The mean strength of field, B, of a dynamo is 5000 C.G.S. lines; a current of 100 amperes flows through a wire; the force acts upon 10 centimetres of the wire =  $10.1937 \times 10 \times 100 \times 5000 \times 10^{-8}$  = .5097 kilogrammes. In the "English" or Kapp's system of measurement a total flow of 6000 C.G.S. lines is taken to equal one English line. Calling  $B_B$  the induction in English, or Kapp's, lines per square inch, and B the induction in C.G.S. lines per square centimetre,  $B_E=B\to930.04$ ; and taking l'' in inches and  $P_P$  in

pounds,  $P_n = 531 Cl'' B_E 10^{-6}$  pounds.

Torque of an Armature,  $-P_2$  in the last formula, = the force tending to move one wire of length l'', which carries a current of  $\ell$  amperes through the field whose induction is  $B_R$  English lines per square inch. The current through a drum-armature splits at the commutator into two branches, each half going through half of the wires or bars. The force exerted upon one of the wires under the infinence of a pole-piece =  $\frac{1}{2}T_P$ . If t=t in the thin the pole-pieces, then the total force =  $\frac{1}{2}\frac{T_P}{2}$ . If t=t in adjust of the armature to the centre of the conductors, expressed in feet, then the torque =  $\frac{1}{2}P_{p}tr$ , =  $\frac{1}{2}\times531\times Cl''B_{E}\times10^{-6}\times tr$  foot-pounds of moment, or pounds acting at a radius of 1 foot.

Example.—Let the length l of an armsture = 20 in., the radius = 6 in. or .5 ft., number of conductors = 120, of which t = 80 are under the influence of the two pole-pieces at one time, the average induction or magnetic flux through the armature-field  $B_E = 5$  English lines per square inch, and the

current passing through the armature = 400 amperes; then

Torque = 
$$\frac{1}{2} \times 531 \times 400 \times 20 \times 5 \times 80 \times .5 \times 10^{-6} = 424.8$$
.

The work done in one revolution = torque  $\times$  circumference of a circle of 1 foot radius =  $424.8 \times 6.28 = 2670$  foot-pounds.

Let the revolutions per minute = 500, then the horse-power

$$=\frac{2670\times500}{33000}=40.5$$
 H.P.

Electro-motive Force of the Armature Circuit.-From the horse-power, calculated as above, together with the amperes, we can obtain the E.M.F., for  $CE = \text{H.P.} \times 746$ , whence E.M.F. or  $E = \text{H.P.} \times 746 + C$ .

If H.P., as above, = 40.5, and C = 400,  $E = \frac{40.5 \times 746}{100} = 75.5$  volts. 400

The E.M.F. may also be calculated more directly by the following formulæ given by Gisbert Kapp:

C = Total current through armature; c, current through single armature conductor;

 $e_a = E.M.F.$  in armature in volts;

au= Number of active conductors counted all around armature; p= Number of pairs of poles (p=1 in a two-pole machine);

n =Speed in revolutions per minute; F =Total induction in C.G.S. lines; Z = Total induction in English lines.

$$\begin{array}{l} \text{Electro-motive} \left\{ \begin{array}{l} e_a = F \tau \frac{n}{60} 10^{-8} \\ e_a = Z \tau n 10^{-6} \\ \end{array} \right\} \text{ for two-pole machines.} \\ e_a = Z \tau n 10^{-6} \\ e_a = p F \tau \frac{n}{60} 10^{-1} \\ e_a = p Z \tau n 10^{-6} \end{array} \right\} \text{ for multipolar machines with} \\ \text{ series-wound armature.}$$

 $\texttt{Example}.-\tau=120,\ n=500,\ \text{length}$  of armature l=20 in., diameter d=12 in., cross-section =  $20\times12=240$  sq. in., induction per sq. in.  $B_E=5$  lines per sq. in., total induction  $Z=240\times5=1200;$  then

$$E = Z_7 n_{10-6} = 1200 \times 120 \times 500 \times 10-6 = 72$$
 volts.

A formula for horse-power given by Kapp is

H.P. = 
$$1/746 \ ZNtn10 - {}^{6}Ca$$
  
=  $1/746 \ 2abmNtn10 - {}^{6}Ca$ .

Ca = current in amperes, n = revs. per min., 2ab = sectional area of armature-core, m = average density of lines per sq. in. of armature-core, Nt = total number of external wires counted all around the circumference, t = number of wires corresponding to one plate in the commutator, N = number of plates, Z = 2abm = total number of English lines of force. Kapp says that experience has shown that the density of lines m in the

core cannot exceed a certain limit, which is reached when the core is saturated with magnetism. This value is reached when m=30. A fair average value in modern dynamos and motors is m = 20, and the area ab must be value in modern dynamos and motors is m = 20, and the street at miss be taken as that actually filled by iron, and not the gross area of the core. 20 English lines per sq. in. = 18,000 C.G.S. lines per square centimetre. Silvanus P. Thompson says it is not advisable in continuous-current machines to push the magnetization further than B = 17,000 C.G.S. lines per square centimetre.

centimetre. Thompson gives as a rough average for the magnetic field in the gap-space of a dynamo or motor 6300 lines per sq. cm., or 40,000 lines per sq. in., and the drag per inch of conductor .00354 lb. for each ampere of current carried.

Provide appears drag per conductor  $H.P. \times 33,000$  in which C is the

Pounds average drag per conductor =  $\frac{H.1. \times 35,000}{\text{ft, per min.} \times C}$ , in which C is the

number of conductors around the armature.

Strength of the Magnetic Field,—Kapp gives for the total number of lines of force (Kapp's lines = C.G.S. lines + 6000) in the magnetic circuit.  $Z = \frac{A}{Ra + RA + RF}$ , in which Z = number of magnetic lines, X = the

exciting pressure due to the ampere turns =  $.4\pi TC$ , Ra, RA, and RF = respectively the resistances of the air-spaces, the armature, and the field-magnets.

Kapp gives the following empirical values of Ra, RA, and RF, for dynamos and motors made of well-annealed wrought iron, with a permeability of  $\mu =$ 940:

$$Ra=1440\,\frac{28}{\lambda b};\ RA=\frac{l}{ab};\ RF=2\,\frac{L}{AB};$$

in which  $\delta$  = distance across the span between armature-core and polar surface, b = breadth of armature measured parallel to axis,  $\lambda$  = length of arc embraced by polar surface, so that  $\lambda b$  = the polar area out of which magnetic lines issue, a = radial depth of armature-core, so that ab = section of armature-core (space actually occupied by iron only being reckoned, AB = area of field-magnet core, t = length of magnetic circuit within armature, L = length of magnetic circuit within armature, L = length of magnetic circuit in field magnet; all dimensions in inches or square inches,

For cast-iron magnets,  $Z = \frac{0.8X}{1800\frac{2\delta}{\lambda b} + \frac{l}{ab} + \frac{3L}{AB}}$ .

For double horse-shoe magnets of wrought iron,

rse-shoe magnets of wrought iron, 
$$\frac{Z}{2} = \frac{X}{1440\frac{2b}{\lambda b} + \frac{2l}{ab} + \frac{2L}{AB}};$$
 and of cast iron, 
$$\frac{Z}{2} = \frac{0.8X}{1800\frac{28}{\lambda b} + \frac{2l}{ab} + \frac{3L}{AB}}$$

These formulæ apply only to cases in which the intensity of magnetization is not too great—say up to 10 Kapp's lines per square inch. Silvanus P. Thompson gives the following method of calculating the strength of the field, or the magnetic flux, MF, or the whole number of magnetic lines flowing in the circuit in C.G.S. lines:

The magnetic resistance of any magnetic conductor is proportional directly to its length and inversely to its cross-section and its permeability.

Magnetic resistance  $=\frac{L}{S\mu}$ , in which L= length of the magnetic circuit

passing through any piece of iron, S= section of the magnetic circuit passing through any piece of iron,  $\mu=$  permeability of that piece of iron. In a dynamo-machine in which the resistances are three, viz.: 1. The field-magnet cores; 2. The armature-core; 3. The gaps or air-spaces between them .-

let Lm, Sm, µm refer to the field-magnet part of the circuit; Las. Sas, was refer to the air-space part of the circuit: La, Sa,  $\mu a$  refer to the armature part of the circuit:

the lengths across each of the air-spaces being Las, and the exposed area of polar surface at either pole being Sas.

Total magnetic resistance = 
$$\frac{Lm}{Sm\mu m} + \frac{Las}{Sas\mu as} + \frac{La}{Sa\mu a}$$

Magnetic flux, or total number of magnetic lines, =

$$MF = \frac{1.257TwC}{\frac{Lm}{Sm\mu_m} + \frac{Las}{Sas\mu as} + \frac{La}{Sa\mu a}}.$$

Tw = turns of wires, or number of turns in the spiral;

The turns of wires, or number of turns in the spiral,

C = current in amperes passing through spiral.

Application to Designing of Dynamos,

Suppose in designing a dynamo it has been decided what will be a convenient speed, how many conductors shall be wound upon the armature, and what quantity of magnetic lines there must be in the field, it then becomes necessary to calculate the sizes of the iron parts and the quantity of excita-Hecessary to calculate the sizes of the foundation and the quantum of exact tion to be provided for by the field-magnet coils. It being known what  $M_T$  is to be, the problem is to design the machine so as to get the required value. Experience shows that in every type of dynamo there is magnetic leakage; also, that it is not wise to push the saturation of the armature-core to more than 16,000 lines to the square centimetre at the most highly saturated part, and that the induction in the field-magnet ought to be not greater than this, even allowing for leakage. Leakage may amount to ½ of the whole: hence, if the magnet-cores are made of same quality of iron as the armature-cores, their cross-section ought to be at least 5/4 as great as that of the armature-core at its narrowest point. If the field-magnets are of cast iron, the section ought to be at least twice as great.

Now, Ba (the induction in the armature-core) = Ma + Sa (or magnetic flux through armature + cross-sectional area of the armature; hence, if this is fixed at 16,000 lines per centimetre of cross-section, we at once get 8a = Ma + Ba. This fixes the cross-section of the armature-core. (Example: If Ma = 4,000,000 of lines, then there must be a cross-section equal to 250 square centimetres for  $\frac{4,000,000}{16,000} = 250.$ )

Magnetic Length of Armature Circuit.—The size of wires on the armature is fixed by the number of amperes which it must carry without risk Remembering that only half the current (in ring or drum armatures) passes through any one coil, and as the number is supposed to have been fixed bethrough any one con, and as the immore is supposed no have obeen faced of-forehand, this practically settles the quantity of copper that must be put on the armature, and experience dictates that the core should be made so large that the thickness of the external winding does not exceed 1/6 of the radial depth of the iron core. This settles the size of the armature-core, from which an estimate of La, the average length of path of the magnetic lines

which an estimate of  $L_a$ , the average length of path of the magnetic lines in the core, can be made. Surface Area of Air-space.—Experience further dictates the requisite clearance, and the advantage of making the polepieces subtend an arc (in two-pole machines) of at least 135° each, so as to gain a large polar area. This settles Las and Sas.

Length of Field-magnet Iron Cores, etc.—As shown above, the minimum value of Sm is settled by leakage and materials; Lm therefore remains to be decided. It is clear that the magnete-cores must be longer. As a rule, they are made as stouched and the state of the circuit, then a little value of the regulation of the circuit, then a little value of the state of the circuit, then a little value engit is such at the sequence of the circuit, then a little value engit is such at the expension of the circuit, then a little value engit is sumed in the calculation does not matter much. It now only remains to calculate the number of ampere-turns of excitation for which it will be needful to provide.

It will now be more convenient to rewrite the formula of the magnetic

circuit as follows:

$$A\times T_{mw} = Ma \frac{\left\{ \lambda \frac{L_m}{S_{m}\mu_m} + 2 \frac{Las}{Sas.\mu as} + \frac{La}{Sa.\mu a} \right\}}{1.257};$$

where A = amperes of current passing through the field-magnet coils;  $T_{mw} = \text{total turns of the magnet wire};$  $\lambda = \text{leakage coefficient (say 5/4)}.$ 

Or.

$$4 \times Tmw = Ma \frac{\lambda Rm + Ras + Ra}{1.257}.$$

Or, as before,

$$Ma = 1.257 \frac{A \times Tmw}{\lambda Rm + Ras + Ra},$$

where  $R_m$ ,  $R_{as}$ ,  $R_a$  stand for the magnetic resistance of magnets, air-space, and armature, respectively.

But we cannot use this formula yet, because the values of  $\mu$  in it depend on the degree of saturation of the iron in the various parts. These have to be found from the Hopkinson tables, given below; and, indeed, it is preferable first to rearrange the formula once more, by dividing it into its separate members, ascertaining separately the amprer-curns requisite to force the required number of magnetic lines through the separate parts, and then add them together.

- 1. Ampere-turns required for magnet-cores =  $\lambda \frac{Ma}{Sm} \times \frac{Lm}{tm} + 1.257$ .
- 2. Ampere-turns required for air-spaces  $=\frac{Ma}{Sas} \times 2\frac{Las}{\mu as} \div 1.257$ .
- 3. Ampere-turns required for armature-core =  $\frac{Ma}{Sa} \times \frac{La}{aa} \div 1.257$ .

Now  $\lambda \frac{Ma}{Sm}$  is the value of B in the magnet-cores, and reference to the table of permeability will show what the corresdonding value of  $\mu m$  must be. Similarly,  $\frac{Ma}{Sa}$  will afford a clue to  $\mu_a$ . When the total number of ampereturns to be allowed for is thus ascertained, the size and length of wire will be determined by the permissible rise of temperature, and the mode of exciting the field-magnets, whether in series, or as a shunt machine, or with a compound-winding.

Permeability.- Materials differ in regard to the resistance they offer to the passage of lines of force; thus iron is more permeable than air. The permeability of a substance is expressed by a coefficient  $\mu$ , which denotes its relation to the permeability of air, which is taken as 1. If H = numberof magnetic lines per square centimetre which will pass through an airspace between the poles of a magnet, and B the number of lines which will pass through a certain piece of iron in that space, then  $\mu=B+H$ . The permeability varies with the quality of the iron, and the degree of saturation, reaching a practical limit for soft wronght from when B= about 18,000 and for cast iron when B = about 10,000 C.G.S. lines per square centimetre.

The following values are given by Thompson as calculated from Hopkin-

Annea	aled Wrough	nt Iron.	Gr	ay Cast Iron.	
В	H	μ	В	. H	μ
5,000	2	2,500	4,000	5	800
9,000 10,000	5	2,250 2,000	5,000 6,000	10 21.5	500 279
11,000	6.5 8.5	1,692	7,000	42	133
12,000	8.5	1,412	8,000	80	100
13,000	12	1,083	9,000	127	71
14,000	17	823	10,000	188	53
15,000	28.5	526	11,000	292	37
16,000	52	308			
17,000	105	161			
18,000	200	90			
19,000	350	54			

Permissible Amperage and Permissible Depth of Winding for Magnets with Cotton-covered Wire. (Walter S. Dix, El. Engineer, Dec. 21, 1892.)—The tables on pp. 1068, 1069, abridged from those of Mr. Dix, are calculated from the formula

$$C = \sqrt{\frac{12 \times W}{\frac{\omega_{mf}}{M} \times T \times L}},$$

where C = current; W = emissivity in watts per square inch;

 $\omega_m f = \text{ohms per mil-foot}$ ;

M = circular mils:

T = turns per linear inch;

L = number of layers in depth.

The emissivity is taken at .4 watt per sq. in. for stationary magnets for a rise of temperature of 35° C. (63° F.). For armatures, according to Esson's experiments, it is approximately correct to say that .9 watt per sq. in. will be dissipated for a rise of 35° C.

The insulation allowed is .007 inch on No. 0 to No. 11 B. & S.; .005 inch on No. 12 to No. 24; and .0045 inch on No. 25 to No. 31 single; twice these values for insulation of double-covered wires. Fifteen per cent is allowed for imbedding of the wires.

The standard of resistance employed is 9.612 ohms per mil-foot at 0°. The running temperature of tables is taken at  $25^{\circ} + 35^{\circ} = 60^{\circ}$  C. The column giving the depth for one layer is the diameter over insulation.

### Formulæ of Efficiency of Dynamos.

(S. P. Thompson in "Munro and Jamieson's Pocket-Book.")

Total Electrical Energy (per second) of any dynamo (expressed in watts) is the product of the whole E.M.F. generated by armature-coils into the whole current which passes through the armature

Useful Electrical Energy (per second), or useful output of the machine, is the product of the useful part of the E.M.F. (i.e., that part which is available at the terminals of the machine) into the useful part of the current (i.e., that part of the current which flows from the terminals into the exter-

nal circuit).

Economic Coefficient or "electrical efficiency" of a dynamo is the ratio of the useful energy to the total energy,

Commercial Efficiency of a dynamo is the ratio of the useful energy or output to the power actually absorbed by the machine in being driven.

Let  $E_a = \text{total E.M.F.}$  generated in armature;  $E_e = \text{useful E.M.F.}$  available at terminals:

 $C_a = \text{total current generated in armature};$  $C_8$  = current sent round shunt-coils;

Ce = useful current supplied to external circuit:

The abstraction represents the state of the state of armsture-coils;  $R_m = \text{resistance of magnet-coils in main circuit (series)};$   $R_s = \text{resistance of magnet-coils in shunt;}$   $R_s = \text{resistance of external circuit (lamps, mains, etc.)};$ 

Wa = Watts lost in armature;

Wm = Watts lost in magnet-coils:

Vi = lost volts:

Te = total electrical energy (per second);

IIe = useful electrical output; c = economic coefficient;

p = commercial efficiency (percentage).

When only one circuit (series machine) Ce = Ca.

In shunt machines Cs should not be more than 5% of Ce. Ca = Ce + Cs. In all dynamos, Ra ought to be less than 1/40 as great as the working

value of Re. In series (and compound) machines, Rm should be not greater than Ra.

and preferably only % as great. In shunt (and compound) machines, Rs should be not less than 300 times as great as  $R_a$  and preferably 1000 to 1200 times as great.

	Series Machine.	Shunt Machine.	Compound Machine (Short Shunt).
$W_a$	$C_a^2 R_a$	$C_a^2 R_a$	$C_a^2 R_a$
$W_{m}$	$C_a^2R_m$	$C_{\mathcal{S}}^{2}R_{\mathcal{S}}=E_{e}^{2}\div R_{\mathcal{S}}$	$C_a^2 R_m + C_s^2 R_s$
$v_l$	$C_a R_a$	$C_a R_a$	$C_aR_a+C_eR_m$
$T_e$	$E_a C_a = C_a^2 (R_a + R_m + R_e)$	$E_aC_a = \frac{C_a^2 \left(R_a + \frac{R_s R_e}{R_s + R_e}\right)}{C_a^2 \left(R_a + \frac{R_s R_e}{R_s + R_e}\right)}$	$ = E_a C_a = C_a^2 \left( R_a + \frac{R_s (R_m + R_e)}{R_s + R_m + R_e} \right) $
$U_e$	$E_e C_a = C_a^2 R_e$	$E_e C_e = C_e^2 R_e$	$E_{e}C_{e}=C_{e}^{2}R_{e}$
c	$\frac{E}{E_a} = \frac{R_e}{R_a + R_m + R_e}$	$\frac{C_e^2 R_e}{C_e^2 R_e + C_a^2 R_a + C_s^2 R_s} *$	$\frac{C_e^2 R_e}{C_e^2 R_e + C_a^2 R_a + C_s^2 R_s + C_e^2 R_m}$
p	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	$100 \times E_e C_e \div \text{(H.P.} \times 746)$	$100 \times E_e C_e$ ÷(H.P.×746)
	is converted into watts (so as to com-	maximum when $Re$ is a mean proportional between $Rs$ and $R_a$ .	In well-constructed compound machines the difference between "short shunt" and "long shunt" is very slight, as $R_m$ is so small.

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Permissible Amperage and Permissible Depth of Winding for Magnets with Double Cotton-covered Wire.

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	30		Depth	5.23	4.79	4.76	4.43	4.27	4.10	3.84	8.80	3.44	3.40	3.14	3.09	2.84	3.78	2.59	3.50	2.35	2.32
	टर		Amp.	91.9	19.1	18.9	16.8	16.0	15.0	13.5	13.4	11.4	11.2	9.82	9.61	8.41	8.10	7.27	6.84	6.20	5.75
			Depth.	2.63	2.41	5.40	2.31	2.15	20.2	1.93	1.95	1.73	1.71	1.58	1.55	1.43	1.40	1.31	1.26	1.18	1.13
Layers.	10	1	Amp.	81.0	27.1	8.98	53.9	25.7	21.3	19.1	18.9	16.1	15.8	13.9	13.6	11.9	11.5	10.3	9.70	8.78	8.14
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			Amp.	43.7	38.1	37.7	33.6	31.9	30.0	56.9	26.7	25.2	55.3	19.7	19.1	16.8	16.1	14.5	13.6	12.3	11.5
		1	Depth.	.298	.973	.2716	.252	.2434	.234	.2183	.217	961.	.194	.179	.176	.162	.1583	.148	.1425	.134	.1384
			Amp.	87.8	85.4	84.6	75.4	21.5	67.2	60.3	59.8	8.02	50.0	44.1	45.9	37.6	36.2	32.5	30.6	27.7	25.7
	Turns	per	inch.	3.36	3.66	8.68	3.97	4.11	4.27	4.58	4.61	5.10	5.16	5.59	5.68	6.17	6.82	6.76	7.02	7.46	7.79
r foot.		:	over'd		_	_	_	_	_	159		3			.0942		9620		.0617		.0505
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Alternating Currents, Multiphase Currents, Transformers, etc.—The proper discussion of these subjects would take more space than can be afforded in this work. Consult S. P. Thompson's "Dynamo-Electric Machinery," Bedell and Crehore on "Alternating Currents," Fleming on "Alternating Currents," and Kapp on "Dynamos, Alternations and Transformers."

The Electric Motor.—The electric motor is the same machine as the dynamo, but with the nature of its operation reversed. In the dynamo mechanical energy, such as from a belt, is converted into electric current; in the motor the current entering the machine is converted into mechanical energy, which may be taken off by a belt. The difference in the action of the machine as a dynamo and as a motor is thus explained by Prof. F. B. Crocker, (Cassier's Mag., March, 1895):
In the case of the dynamo there exists only one E.M.F., whereas in the

motor there must always be two.

One kilowatt dynamo, C = E + R; 10 amperes = 100 volts + 10 ohms.

One kilowatt motor, 
$$C = \frac{E-e}{R_1}$$
; 10 amperes =  $\frac{100 \text{ volts} - 90 \text{ volts}}{1 \text{ ohm}}$ .

C is the current; E, the direct E.M.F.; e, the counter E.M.F.; R, the total resistance of the circuit;  $R_1$ , the resistance of the armature. resistance of the circuit; A<sub>1</sub>, the resistance of the armature. The current and direct E.M.F. are the same in the two cases, but the resistance is only one tenth as much in the case of the motor, the difference being replaced by the counter E.M.F., which acts like resistance to reduce the current. In the case of the motor the counter E.M.F. represents the amount of the electrical energy converted into mechanical energy. The so-called electrical efficiency or conversion factor = counter E.M.F. + direct E.M.F. The actual or commercial efficiency is somewhat less than this, owing to friction, Foucault currents, and hysteresis.

For full discussions of the theory and practice of electric motors see S. P. Thompson's "Dynamo-Electric Machinery," Kapp's "Electric Transission of Energy," Martin and Wetzler's "The Electric Motor and its Applications," Cox's "Continuous Current Dynamos and Motors," and Crocker and Wheeler's "Practical Management of Dynamos and Motors,"

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