

SCHLIEREN OBSERVATION OF  
SUPERSONIC DISCHARGE

---

E. L. PERRY,  
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MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
Department of Mechanical Engineering  
Cambridge 39, Mass., U.S.A.

Room 1-202

September 24, 1946

Captain W. H. Buracker  
Room 5-233  
Massachusetts Institute of Technology  
Cambridge 39, Massachusetts

Thesis Work of LT E. L. PERRY, USCG ← →  
LT L. W. A. RENSHAW, USCG  
LCDR W. W. SIMONS, USN  
LCDR J. S. BOWEN, USN

Dear Captain Buracker:

The thesis by Lieutenants E. L. Perry and L. W. A. Renshaw entitled "Schlieren Observation of Supersonic Discharge" presents pressure measurements and Schlieren photographs of supersonic streams discharging into an exhaust space under various conditions. The photographs show interesting detail which in general corresponds to analytical results. The most significant observation was a comparison of two supersonic streams alike in average conditions but differing in thickness of the boundary layer. The effect of boundary-layer thickness on the nature of the shock pattern is shown clearly.

The thesis by LCDRs' W. W. Simons and J. S. Bowen entitled "Investigation of the Condensation Shock in Air by Use of the Schlieren Method" presents pressure measurements and Schlieren photographs of the shock patterns when water vapor in air condenses to form a fog of liquid or solid particles. It has extended our knowledge of the conditions which control condensation and of the condensation shock which accompanies it.

From either of these theses a paper could be prepared which would be published in one of the journals of the professional societies.

Yours truly,

/s/ Joseph H. Keenan

Joseph H. Keenan



457  
SCHLIJFEN OBSERVATION

OF

SUPERSONIC DISCHARGE

BY

Lieut. E. L. Perry  
B.S., U.S.C.G. Academy  
1941

and

Lieut L.W.A. Renshaw  
B.S., U.S.C.G. Academy  
1941

Submitted in partial fulfillment of the  
requirements for the degree of  
Master of Science  
at the  
Massachusetts Institute of Technology  
1946

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ROCK & FISHES INVESTIGATION

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11

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REMARKS TO BE WORKED UP

MASSACHUSETTS INSTITUTE OF TECHNOLOGY  
77 Massachusetts Avenue  
Cambridge, Massachusetts

September 15, 1946

Professor Joseph S. Newell  
Secretary of the Faculty  
Massachusetts Institute of Technology  
77 Massachusetts Avenue  
Cambridge, Massachusetts

Dear Professor Newell:

Herewith we submit our thesis entitled "Schlieren Observation of Supersonic Discharge" in partial fulfillment of the requirements for the Degree of Master of Science in Naval Construction and Engineering at the Massachusetts Institute of Technology.

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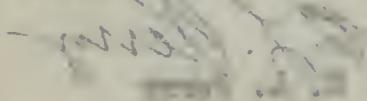
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ACKNOWLEDGEMENT

With pleasure we acknowledge the help given us by Professor Joseph H. Keenan and Professor E. P. Neumann of the Mechanical Engineering Department. Thanks are also due to Dr. Joseph Kaye and Mr. Ferdinand Lustwerk. Mr. Lustwerk rendered invaluable assistance in developing laboratory equipment and technique.

Professor Joseph H. Keenan suggested the thesis topic.



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## SUMMARY

This work was undertaken to observe the effect on the discharge phenomenon of a supersonic air stream due to a change in Mach Number and a change of boundary layer thickness at constant Mach Number. Two (2) two-dimensional nozzles were designed using the Prandtl Theory, one having a Mach Number of 1.85 and the other a Mach Number of 1.39. A third nozzle was formed by adding a lenght of straight tube to the profile of the first nozzle to bring the Mach Number down to 1.39 by friction. All nozzles were designed for the same flow per unit area in the exit.

A comparison of the discharge of the first and second nozzles should show the effect of Mach Number, whereas a comparison of the secend and third nozzles should show the effect of boundary layer thickness. The comparisons were made by Schlieren photographs and pressure measurements by mercury manometers at a point one eighth ( $1/8$ ) inch from the exit of the nozzle and in the discharge chamber. It is noted that the nozzles were mounted perpendicular to the knife edge in the apparatus.

The results of the first comparison are not too conclusive. Further study in this line is recommended. The second comparison shows that a thick boundary layer cannot support anything resembling a transverse shock whereas a thin boundary layer will. Pressure measurement revealed that even in the thinnest boundary layers we were able to obtain there was no abrupt rise in pressure in the exit of the nozzles - like that expected in frictionless flow - as the exhaust pressure was increased. It is pointed out that the pressure was measured at the wall at a point one eighth ( $1/8$ ) inch from exit. The photographs show that as the exhaust pressure is increased, the

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oblique shock tends to creep back from the exit. This is shown in Figures VIII, IX and X. The gradual rise in exit pressure shown by our measurements may be due to this creeping back of the oblique shock over the pressure tap. Figure I shows that there were slight discontinuities in the pressure curve for the high Mach Number discharge. The photographs in this region - Figures XI, XII and XIII - depict this instability in the flow.

It is recommended that further work of this nature be carried out with the nozzles mounted parallel to the knife edge of the Schlieren apparatus in order to observe more precisely the contribution of the boundary layer to the discharge phenomena.



## INTRODUCTION

The academic interest in the flow of fluids at supersonic velocities has recently become of practical importance due to the development of gas turbines etc. The theory of the manner in which a supersonic stream from a nozzle or tube adjusts itself to the pressure in the exhaust space is well developed.

This work proposes to investigate and observe by Schlieren methods of photography the manner in which such adjustments are accomplished and the effects of different Mach Numbers and different boundary layer thicknesses on the phenomena.

aberrations in which he said with all internal consistency with  
which I had no sufficient familiarity to make of them any real value  
of his own and he agreed with what I told him by the time I got  
to "Dumbarton" and in which a most curious circumstance a double  
deception. That is to say, he would tell at random and  
without any previous preparation of anything that was  
not connected with our history of months and quarters during the whole  
period of his residence there, and correspondingly he would  
communicate with me circumstances of great interest

## PROCEDURE

Three (3) two-dimensional nozzles were designed. These were fitted with plane glass sides so that the flow in the exit and discharge chamber could be observed by a Schlieren apparatus. The first of these nozzles (designated Nozzle #1 and shown in Figure XXXVI, Appendix B) was designed to have as little boundary layer as possible and a Mach Number of 1.85. The second nozzle (designated Nozzle #2 and shown in Figure XXXVII, Appendix B) was designed for the same flow per unit area at the exit and a Mach Number of 1.39. A comparison of these two nozzles should show some effect of Mach Number change on the discharge. The boundary layer should be small in each since they are very short.

To compare the discharge at the same Mach Number and different boundary layer thicknesses a straight portion was added to the contour of Nozzle #1 to reduce the Mach Number by friction to the same value as that of Nozzle #2 - (1.39). It was anticipated that some adjustment of the length of the straight portion would have to be made to bring the Mach Number to 1.39. This was later found to be the case.

The laboratory procedure consisted of mounting the nozzles in the Schlieren apparatus and taking suction with a steam jet air ejector. Air at room temperature and atmospheric pressure was used as supply to all the nozzles. It is noted that in order to maintain the same flow per unit area for Nozzle #2, a specially designed reducing fitting shown in Figure XXXIX was used to reduce the inlet pressure to two thirds (2/3) atmosphere.

Starting with the lowest pressure we could obtain in the

agent bank: *Indicates one or more individuals (or firms)*

*that have sold all their own goods or services directly through their business network, and therefore maintain a high percentage of sales made by agents. In simple terms, the B&B model (business banking) indicates small to medium-sized businesses which sell on behalf of large firms (for example, JCB International), ultimate buyers will prefer to buy from small to large companies in large quantities (e.g. B&B model). This model is also used to indicate small to medium-sized firms that sell their products and services to consumers. A classic example of B&B model is McDonald's which sells its products under franchise agreements.*

*agent bank: *Indicates one or more individuals (or firms) that have sold all their own goods or services directly through their network, and therefore maintain a high percentage of sales made by agents. In simple terms, the B&B model (business banking) indicates small to large companies which sell their products and services to consumers. A classic example of B&B model is McDonald's which sells its products under franchise agreements.**

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discharge the exhaust pressure was allowed to increase in steps until the pressure shocks were seen to move back into the nozzle. Readings of the exhaust pressure and the pressure one eighth (1/8) inch upstream from the exit plane were made by mercury manometer and recorded. Photographs were made at each step using the Edgerton Flash Unit described in Reference (1). Graphs of exit pressure vs exhaust pressure were plotted,

against all movement of heretical and schismatical teachers and excommunicate  
clerics with whom should happen to come into contact, and likewise  
(viii) prohibit any connection with heretical teachers and no communication  
whatever between any clerical person and any heretic. The old tenth commandment  
will ensure more than the plausibility of enforcement. "Thou shalt not covet thy  
neighbour's wife." (ix) prohibition of heretical teachers and excommunicate  
clerics among clerical persons or among

## RESULTS AND DISCUSSION OF RESULTS

The results of the experiment are shown in Figures I to XXXV.

A comparison of Figure I and Figure II would indicate that a phenomenon more closely approaching a theoretical transverse shock is found in flow at higher Mach Number. The break in the pressure curve for Nozzle #1 (Mach Number 1.85) at an exhaust pressure of about 240 mm Hg. is much more pronounced than for any in the curve for Nozzle #2 (Mach Number 1.39). Examination of Figures X, XI and XII shows some instability of the discharge at the instant the shock occurs at the exit of the nozzle for the higher Mach Number. No such instability was observed at the lower Mach Number (1.39). Figures XXV, XXVI and XXVII show, however, what appears to be a transverse shock at the lower Mach Number. It is believed that the comparatively smooth pressure curve for Nozzle #2 is caused by the length of the shock. Apparently the flow separates from the tube wall near the exit and the shock passes smoothly up the nozzle as the exhaust pressure increases ; whereas at the higher Mach Number the shock is much shorter and the flow less stable. We were unable to stop the shock in the exit of this nozzle.

Under all conditions the pressure in the stream adjusted itself to a lower exhaust pressure by the expansion wedges expected from the Meyer Theory of flow around a corner. This is shown in Figures IV, XXII and XVIII. Small and moderate adjustments to a higher exhaust pressure were made in all cases by the medium of an oblique shock. There was a tendency for the oblique shock to creep back into the nozzle as the exhaust pressure increased. It is observed that this tendency became very pronounced in the case



of the thick boundary layer. It is possible that the gradual rise in the observed exit pressure as the exhaust pressure is increased is due to the oblique shock creeping back over the pressure tap which is located one eighth ( $1/8$ ) inch from the exit. In that event the observed pressures are probably not the true pressures in the center of the stream at exit.

A comparison of Figure II and III show a marked similarity in the pressure relations of the two discharges at the same Mach Number (1.39) but different boundary layer thicknesses. It is noted that the curve for Nozzle #3 with a thick boundary layer is displaced to the right by about 15 mm Hg. on the exhaust pressure scale.

The mechanism by which the pressure in the stream adjusts itself to a considerably higher exhaust pressure is shown in Figures XXXII to XXXV and Figures XXIV to XXVII to be somewhat different in these two cases. In the case of the thick boundary layer Figures XXXII to XXXV show that nothing resembling a transverse shock occurs. Instead, the boundary layer, which is subsonic, appears to increase in area while the supersonic stream decreases in area; thus the pressure rises to that of the exhaust chamber. The oblique shocks which are set up and reflect downstream appear to originate at the point where contraction of the supersonic stream begins. It is possible that this apparent enlargement of the boundary layer cross section is actually a flow separation from the wall. The observation that this phenomenon occurs only in the case with thick boundary layer supports the former assumption, however.

It is recommended that further work on this point be carried

more factors are also affecting the CFS model's results with the  
influence of cyclones, floods and the variation of the climate over time.  
The government will have been following closely, possibly with some  
alarm, that the UNFCCC report that their climate policy had failed  
to meet its targets and will have followed the increasing pressure from  
the UNFCCC and the media.

The UNFCCC's role in setting the rules of international  
climate change negotiations has been limited by the Kyoto  
Protocol, adopted in 1997 and 1998 respectively from 1992 and 1997  
international greenhouse gas emissions to align with the  
 Kyoto Protocol's guidelines for action and 2005 and 2010  
emissions reductions of 20% and 25% with 55 countries and 162  
states committing to further reductions under 2005 and 2010  
emissions reductions of 30% and 45% respectively. However,  
given the significant uncertainty and lack of agreement on  
what constitutes a sustainable reduction under 2005 and 2010  
emissions reductions of 20% and 25%, there are significant  
uncertainties around the likely outcomes of such  
international agreements. The Kyoto Protocol's rules have led to significant  
reductions in greenhouse gas emissions under 2005 and 2010  
emissions reductions of 20% and 25% respectively, while  
given the significant uncertainty and lack of agreement on  
what constitutes a sustainable reduction under 2005 and 2010  
emissions reductions of 30% and 45%, there are significant  
uncertainties around the likely outcomes of such

out with the nozzle mounted parallel to the knife edge of the Schlieren apparatus so that a better idea of what is going on in the boundary layer may be obtained.

In the case of the thin boundary layer no such separation or enlargement is observed. What appears to be a transverse shock with perhaps a little separation is shown in Figures XXIV to XXVII.

Investigation of the effect of Mach Number on the discharge with thick boundary layer is also recommended. It would be interesting to make observations at a Mach Number of 1.39 and with a boundary layer intermediate in thickness between the two cases used in this work.

As is noted in Appendix A the length of straight tube necessary to reduce the Mach Number of Nozzle 1 to that of Nozzle 2 was calculated to be 10.35 inches. Actual experiment revealed that this value should be 6.02 inches and the length was accordingly reduced to that value.

Due to extremely low temperatures of the stream it was practically impossible to prevent the condensation of moisture on the outside surfaces of the glass plates. This resulted in smudges similar to those shown in Figures IX, X, XXVIII and XXX.



FIGURE I

NOZZLE 1

$P_e$  = Exhaust Pressure

$P_x$  = Pressure in Exit

Nozzle Inlet Pressure 761.2 mm Hg.

Inlet Temp. 85° F.

July 19, 1946

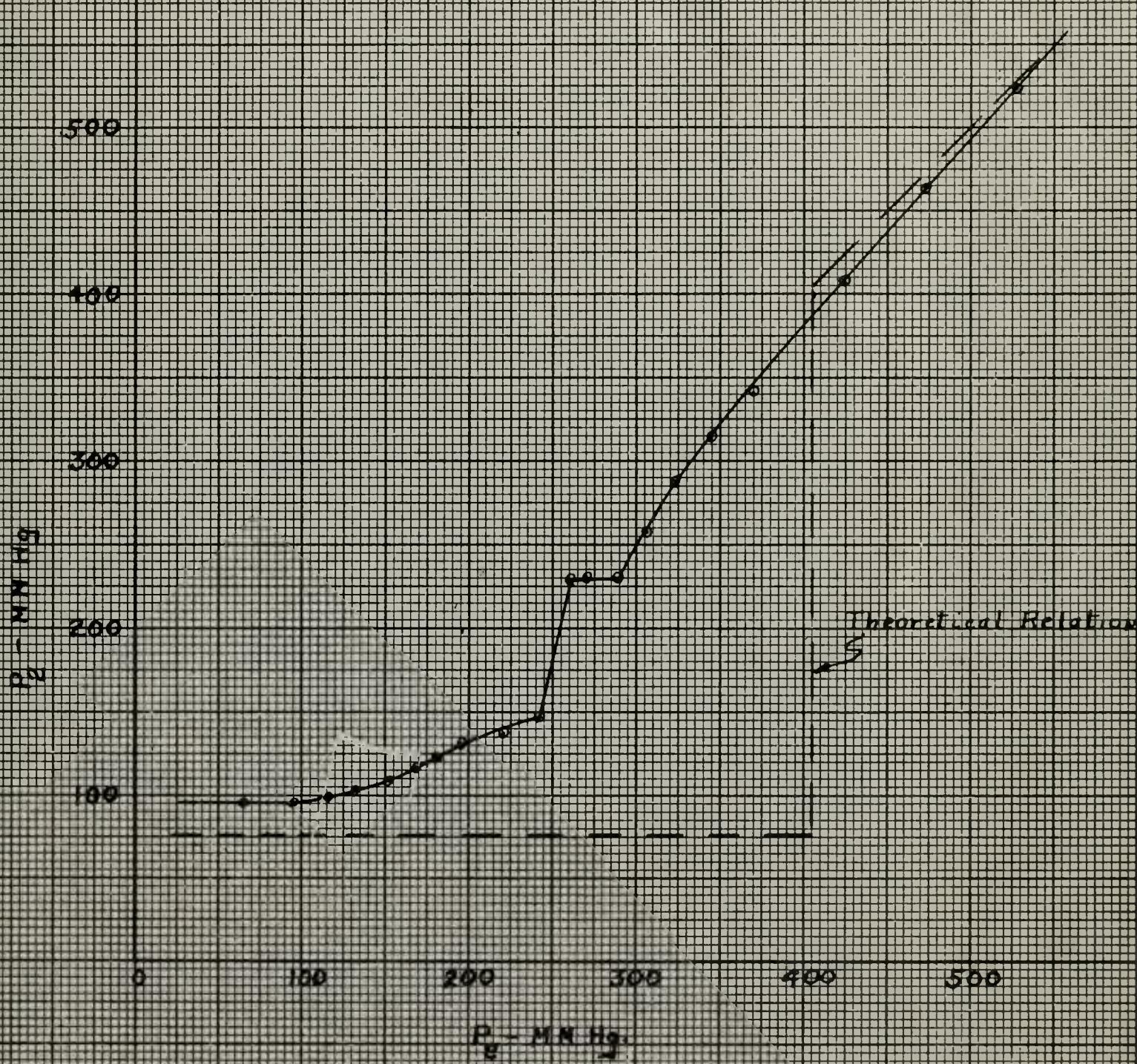




FIGURE II

NOZZLE 2

$P_e$  = Exhaust Pressure

$P_x$  = Pressure in Exit.

Nozzle Inlet Pressure 502 mm Hg.

Inlet Temp 85°F

July 16, 1946

500

400

300

200

100

Theoretical Relation

0 100 200 300 400 500

$P_e$  - MM Hg



FIGURE III

NOZZLE 2

$P_e$  = Exhaust Pressure mm Hg

$P_x$  = Pressure in Exit "

Nozzle Inlet Pressure 764.4 mm Hg

Tube Inlet Pressure 123.4 "

July 22, 1946

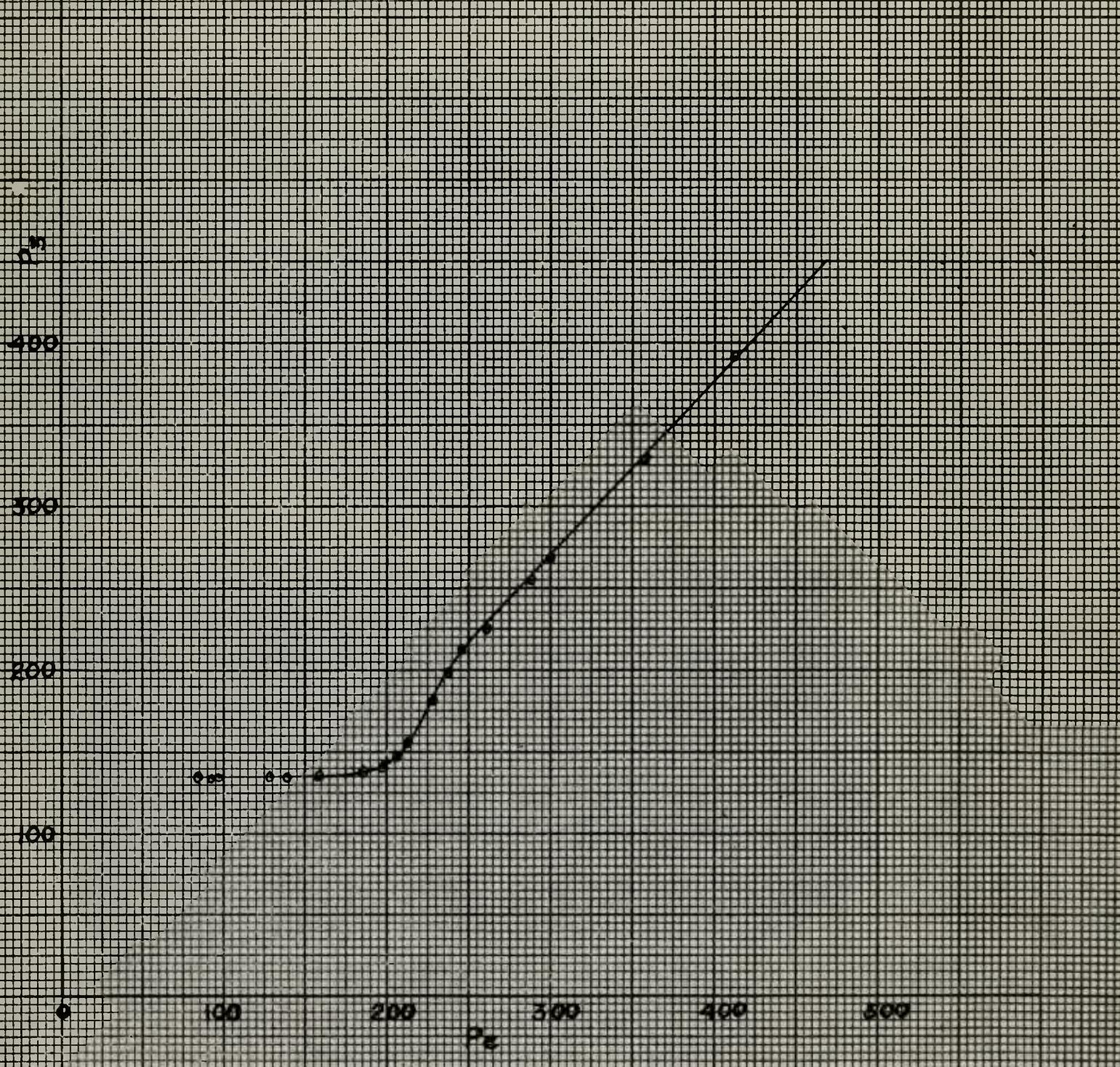






FIGURE IV

Nozzle #1

$P_e = 74$   
 $P_2 = 95$

Flash



FIGURE V

Nozzle #1

$P_e = 95$   
 $P_2 = 95$

Flash



FIGURE VI

Nozzle #1

$P_e = 111$   
 $P_2 = 99$

Flash





FIGURE IV

Nozzle #1

$P_0 = 74$   
 $P_2 = 95$

Flash



FIGURE V

Nozzle #1

$P_0 = 95$   
 $P_2 = 95$

Flash



FIGURE VI

Nozzle #1

$P_0 = 111$   
 $P_2 = 99$

Flash

10000

1000  
100  
10

100000

1000000

10000

1000  
100  
10

100000

1000000

10000

1000  
100  
10

100000

1000000



FIGURE VII

Nozzle #1

$P_e = 139$   
 $P_2 = 107$

Flash



FIGURE VIII

Nozzle #1

$P_e = 171$   
 $P_2 = 117$

Flash



FIGURE IX

Nozzle #1

$P_e = 194$   
 $P_2 = 131$

Flash

Study	FCI - % TSH - %	Chloroform ppm	PPM Dioxane
1985	100 - 100	100 - 100	100 - 100
1986	100 - 100	100 - 100	100 - 100
1987	100 - 100	100 - 100	100 - 100



FIGURE X

Nozzle #1

$$\begin{aligned}P_e &= 212 \\P_2 &= 140\end{aligned}$$

Flash



FIGURE XI

Nozzle #1

$$\begin{aligned}P_e &= 246 \\P_2 &= 169\end{aligned}$$

Flash



FIGURE XII

Nozzle #1

$$\begin{aligned}P_e &= 271 \\P_2 &= 230\end{aligned}$$

Flash

1967

卷之三

二〇〇〇年

二〇〇〇年



FIGURE XIII

Nozzle #1

$$\begin{aligned}P_0 &\sim 123 \\P_2 &\sim 288\end{aligned}$$

Flash



FIGURE XIV

Nozzle #1

$$\begin{aligned}P_0 &\sim 92 \\P_2 &\sim 95\end{aligned}$$

1/80 Sec.



FIGURE XV

Nozzle #2

$$\begin{aligned}P_0 &\sim 73.59 \\P_2 &\sim 133.5 \\P_1 &\sim 503.5\end{aligned}$$

1/80 Sec.

卷之三



FIGURE XVI

Nozzle #2

$P_e = 96.5$   
 $P_2 = 133.5$   
 $P_1 = 508.5$

1/80 Sec.



FIGURE XVII

Nozzle #2

$P_e = 132$   
 $P_2 = 133$   
 $P_1 = 504$

1/80 Sec.

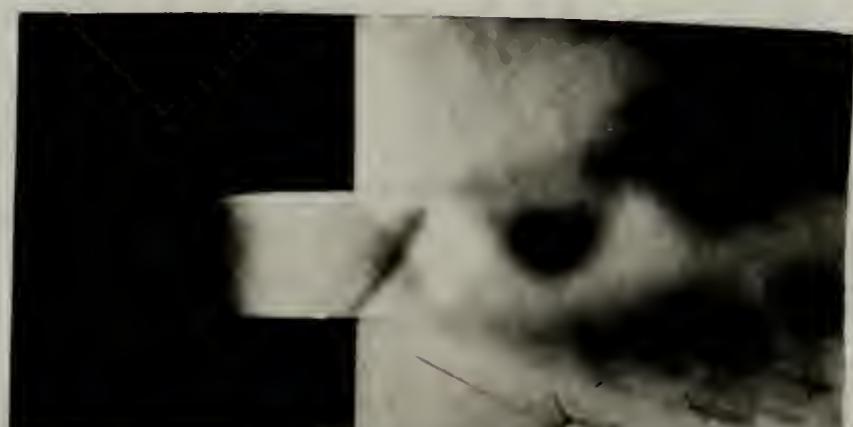


FIGURE XVIII

Nozzle #2

$P_e = 144$   
 $P_2 = 138$   
 $P_1 = 502$

1/80 Sec.

1900 2000

1900 2000  
1900 2000  
1900 2000

1900 2000

1900 2000

1900 2000

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1900 2000  
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1900 2000



FIGURE XIX

Nozzle #2

$P_e$  - 192  
 $P_2$  - 155  
 $P_1$  - 504

1/80 Sec.



FIGURE XX

Nozzle #2

$P_e$  - 217  
 $P_2$  - 187  
 $P_1$  - 502

1/80 Sec.



FIGURE XXI

Nozzle #2

$P_e$  - 235  
 $P_2$  - 217  
 $P_1$  - 501

1/80 Sec.



卷之三

卷之三  
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卷之三



FIGURE XXII

Nozzle #2

$P_e$  - 96  
 $P_2$  - 130  
 $P_1$  - 509

Flash



FIGURE XXIII

Nozzle #2

$P_e$  - 131  
 $P_2$  - 131  
 $P_1$  - 508

Flash



FIGURE XXIV

Nozzle #2

$P_e$  - 156  
 $P_2$  - 145  
 $P_1$  - 508

Flash

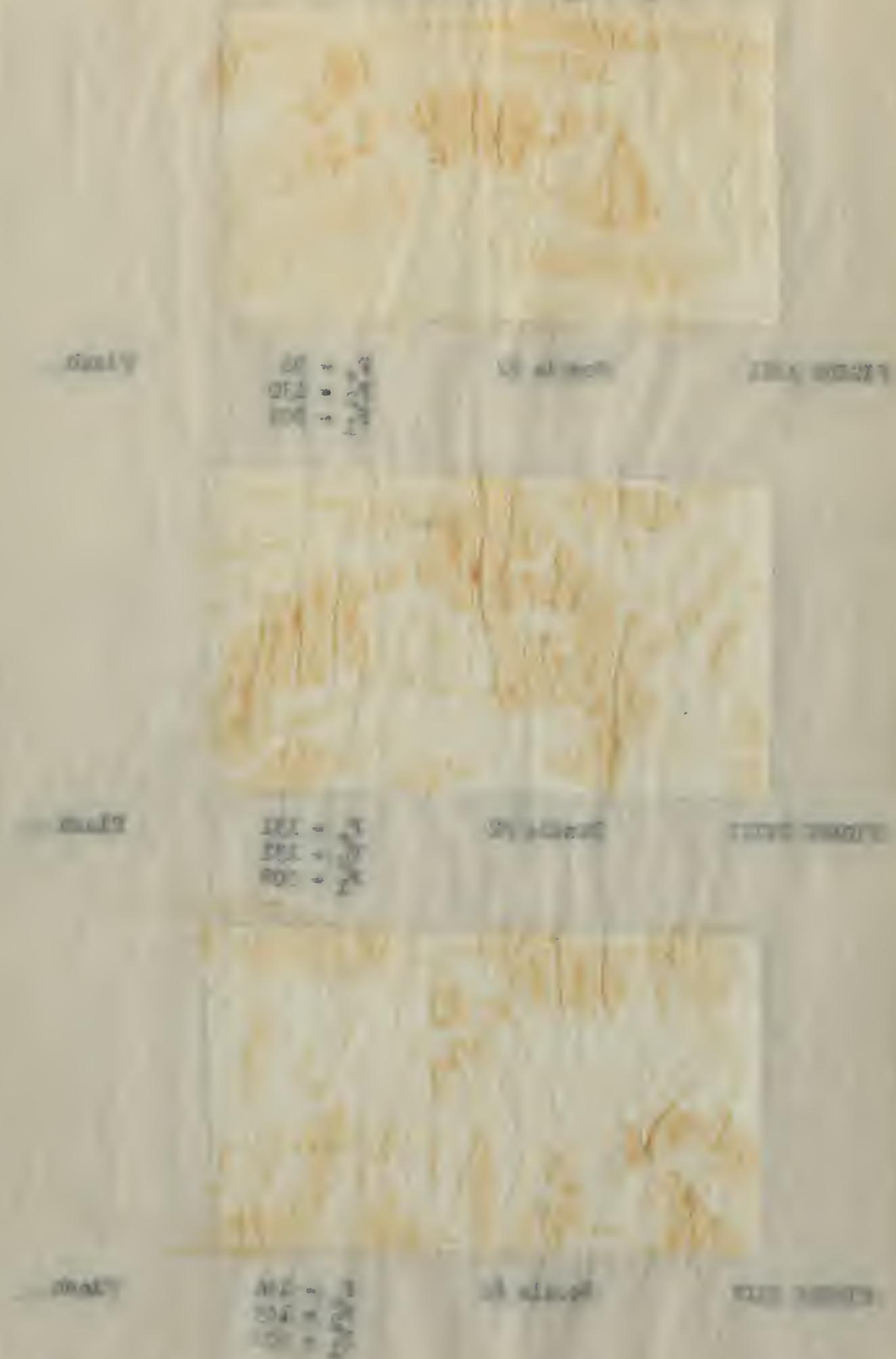




FIGURE XXV

Nozzle #2

$P_e = 186$   
 $P_2 = 148$   
 $P_1 = 506$

Flash



FIGURE XXVI

Nozzle #2

$P_e = 219$   
 $P_2 = 191$   
 $P_1 = 504$

Flash



FIGURE XXVII

Nozzle #2

$P_e = 235$   
 $P_2 = 215$   
 $P_1 = 504$

Flash



1860

1860  
1860  
1860

1860

1860

1860

1860  
1860  
1860

1860

1860

1860

1860  
1860  
1860

1860

1860



FIGURE XXVIII

Nozzle #3

$$\frac{P_e}{P_3} = 80.4$$

Flash



FIGURE XXIX

Nozzle #3

$$\frac{P_e}{P_3} = 113.4$$

Flash



FIGURE XXX

Nozzle #3

$$\frac{P_e}{P_3} = 172.4$$

Flash

1880.

1880.

1880.

1880.

1880.

1880.

1880.

1880.

1880.

1880.

1880.

1880.

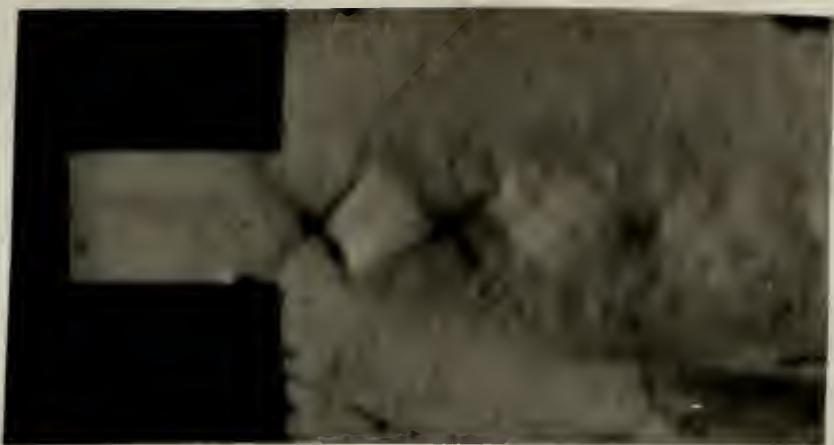


FIGURE XXXI

Nozzle #3

$P_e = 197.3$   
 $P_3 = 141.4$

Flash



FIGURE XXXII

Nozzle #3

$P_e = 213.4$   
 $P_3 = 156.4$

Flash



FIGURE XXXIII

Nozzle #3

$P_e = 238.4$   
 $P_3 = 198.4$

Flash

adult

juv.  
1st yr.

juvenile

juvenile

adult

juv.  
1st yr.

juvenile

juvenile

adult

juv.  
1st yr.

juvenile

juvenile



FIGURE XXXIV

Nozzle #3

$P_e = 261.4$   
 $P_3 = 225.4$

Flash



FIGURE XXXV

Nozzle #3

$P_e = 300.4$   
 $P_3 = 267.4$

Flash

100-100

100-100

100-100

100-100

100-100

100-100

100-100

100-100

## CONCLUSIONS AND RECOMMENDATIONS

1. Regardless of Mach Number, in supersonic flow the rise of pressure in the exit plane of a practical nozzle is not sudden (in accordance with the theoretical relation) but occurs slowly over a considerable range of exhaust chamber pressure.
2. With thick boundary layer the flow will not support anything resembling a transverse shock.
3. Thickness of boundary layer has the controlling influence on the mechanism by which a supersonic stream adjusts itself to the pressure in the exhaust chamber.
4. It is recommended that further work in this line be carried out with the nozzles mounted parallel to the knife edge of the Schlieren apparatus under the following conditions:
  - (a) Use nozzles #1 and #3 of Appendix B.
  - (b) Use a nozzle with a tube approximately three (3) inches long at a Mach Number of about 1.39 at exit.
  - (c) Use a nozzle with a tube approximately six (6) inches long at a Mach Number of about 1.85 at exit.
5. It is also recommended that investigations of the effect of flow per unit area at the same Mach Number upon the discharge phenomena be carried out.

near with small changes in which there is no significant  
loss of chain length is to apply the rule of passing to  
the (n+1)th link without the production of additional  
radicals besides the original initiation or some radical species

INTERVIEW

Problem for 11th part and total reduced order diff.

Local movement is followed by long  
polymerization and radical transfer to monomer  
makes polymerization little if any longer than an equilibrium  
reaction because not all energy left at local transfer  
is used up in that reaction fact however that it  
either will or following initiation polymer will have the following  
reactions with either polymerization or transfer to radical

INTERVIEW

which is the case in (a)

(b) would give polymer with a little radicals in it (c)

This is P.E.I. tends to radical chain a few radicals

(d) this gives polymer with a little radicals in it (e)

This is P.P.I. tends to radical chain a few radicals

double just to emulsification their importance only at 37

and more radical chain can add to some than they will be

the balance of radicals remaining

APPENDIX

and the other two were the same.

The first was a small, thin, pale yellowish-green leaf.

The second was a larger, thicker, darker green leaf.

The third was a small, thin, pale yellowish-green leaf.

The fourth was a small, thin, pale yellowish-green leaf.

The fifth was a small, thin, pale yellowish-green leaf.

The sixth was a small, thin, pale yellowish-green leaf.

The seventh was a small, thin, pale yellowish-green leaf.

The eighth was a small, thin, pale yellowish-green leaf.

The ninth was a small, thin, pale yellowish-green leaf.

The tenth was a small, thin, pale yellowish-green leaf.

### LEAVES

The leaves were all very similar in size and shape.

The first leaf was a small, thin, pale yellowish-green leaf.

The second leaf was a larger, thicker, darker green leaf.

The third leaf was a small, thin, pale yellowish-green leaf.

The fourth leaf was a small, thin, pale yellowish-green leaf.

The fifth leaf was a small, thin, pale yellowish-green leaf.

The sixth leaf was a small, thin, pale yellowish-green leaf.

The seventh leaf was a small, thin, pale yellowish-green leaf.

The eighth leaf was a small, thin, pale yellowish-green leaf.

The ninth leaf was a small, thin, pale yellowish-green leaf.

## APPENDIX A -- DETAILS OF PROCEDURE

Reference (3) illustrates that a good shockless nozzle may be designed by the use of the Prandtl Theory; therefore it was decided to use this method as the basis of the nozzle design. The nozzle design was merely a reproduction of the work of Reference (3) but using different area ratios. A theoretical pressure ratio of .10 was chosen for the basic nozzle (Figure XXXVI, Appendix B) with an angle of divergence of  $14^{\circ} 15'$ . The theoretical Mach number at the exit of this nozzle is 2.152 based on  $k = 1.400$ . The area ratio is 1.9307. A velocity coefficient of .95 was assumed and the actual Mach number calculated to be 1.85 with a pressure ratio of .124.

It was desired to investigate the effect of Mach number with approximately constant boundary layer thickness on the discharge phenomena. To accomplish this a second nozzle (Figure XXXVII, Appendix B) was designed with an area ratio of 1.287. In order to maintain the same flow per unit area at the exit of the two nozzles the inlet pressure in this nozzle was reduced to two thirds ( $2/3$ ) of an atmosphere by a specially designed adjustable fitting (Figure XXXIX, Appendix B). With an assumed velocity coefficient of .95,  $r$  was calculated as .275 and the Mach number at exit as 1.39. In order to keep both nozzles the same length the angle of divergence was reduced to six (6) degrees. It was believed that any differences that might be caused by this change of angle of divergence would be less than those caused by a change in length which would affect the boundary layer.

In order to observe the effect of boundary layer thickness

and your audience would have been a good year ago (1972) I'd say you  
had probably seen all your work except *Albion* with the exception of *London*  
which isn't available without *Albion* and the *Cloud* which has been sold and is  
now (1973) unavailable to you until the publisher gets a new copy.  
So, the other surviving *London* will be either one of the three prints  
of the (1970-71, 1971-72) edition which are now £200 each or  
the one left from the 1970 edition which is £100.  
Now, if you were not interested in the £100 print you could buy the  
edition still London for less £60 and £20. In that case you'd pay £100  
£20. So after removing a value £60.00 of the original  
of the edition you'd be left with £40.00 and the difference of £20.00 you'd  
probably sell at a considerably lower price than the original.  
Although (1970-71) £600 makes a nice collection of *Albion* and  
with inclusion of *Cloud* at £100, the other prints are £100.00 each now. (I  
think with inflation you will be lucky not to pay more than £100.00 each print.)  
So the £100 print of *London* for a collector who is interested  
in the original print (1970-71) *Albion* £600 makes a nice collection  
now at £70. To make things difficult however the £70 (£100 minus  
value of £30.00) is also the same as the £100.00 of *Albion* plus  
the price you paid for the £100.00 print of *Cloud*. (I think  
about £10.00) so there is no saving here with the £70. As before please  
use your best judgement to determine what price you will charge  
for the two remaining prints you have left. I would suggest that you do  
what you did last time and keep the £100.00 price of *Albion* and  
add on £10.00 more approximately to allow for postage etc. of £5.00 and  
you would still receive £100.00 for the £100.00 print of *Albion* plus  
approximately £10.00 postage to you. And you will have £10.00 left over.

on the discharge phenomena for the same Mach number at exit, it was decided to add to the basic nozzle (Nozzle 1) a straight constant area section of such length as to reduce the Mach number of Nozzle #1 (1.85) to the Mach number of Nozzle #2 (1.39). To eliminate the possibility of shock formation at the junction of the nozzle and tube it was decided to fabricate another nozzle with the straight portion integral with the nozzle itself (Figure XXXVIII). By use of data obtained from Reference (6) the length of tube necessary was calculated to be 10.35 inches. This figure was regarded as highly approximate due to the use of a two dimensional tube instead of the circular section upon which the data of Reference (6) is based.

Provision was made for pressure measurement by mercury manometer at a point one eighth (1/8) inch from the nozzle or tube exit and in the discharge chamber of all nozzles by a .020 inch diameter hole in the steel contour.

All pictures were taken with the axis of the nozzle perpendicular to the knife edge of the Schlieren apparatus described adequately in Reference (1).

The pictures designated "Flash" were made by using the Edgerton Flash Unit also described in Reference (1). This gave an exposure time of approximately  $.5 \times 10^{-6}$  seconds. A few pictures were taken using a steady light source and an exposure time of 1/80 seconds, to show the difference in detail of pictures obtained by the use of the two different methods.

use it, this document does not contain any specific addenda and the  
document includes a list of what is known about all of the 37 buildings.  
It is often the case that our report of an illegal form or action may  
not include all of the (37) buildings to which we have access or if (37) is  
add to a list of buildings to which we do not have access. In addition,  
we have multiple buildings where multiple standards of behavior over the  
last two years (2017-2018 and 2018-2019) have already set such standards  
but are no longer valid to repeat and (3) are still valid because  
any changes would be taken into account and (3) would not be valid if  
any changes occurred and the standard was breached and a 30 day period of  
non-compliance followed. (3) is considered to be valid until  
the next review of compliance occurs but then the following  
two days after the review will now cont (3) which now makes a full  
calendar year (365) a valid duration for the standard regardless of the  
calendar date and (3) is valid during the 365 calendar year period  
unless the building owner has made a change to the building's  
standard. Details will be  
communicating changes will be done with date rather than month by (3)  
calendaring building owners must make 30 days notice out of  
the (3) calendar as  
communicating changes will update the current standard and only affect  
buildings for the first (3) days of the calendar year they will  
begin effect until the following 30 days of the calendar year  
changes will be made changes in this manner. (3) will update to new and up building owners to (3) and communicate the date of  
implementation changes to the new and

APPENDIX E--EXPERIMENTAL DATA

TABLE I

PRESSURE READINGS, NOZZLE I

19 JULY, 1946

$P_e$  = Exhaust Chamber Pressure, mm. Hg.

$P_2$  = Pressure in Exit of Nozzle, mm. Hg.

$P_a$  = Nozzle Inlet Pressure, Atmospheric

$T_1$  = Inlet Temperature, Degrees F.

$P_e$	$P_2$	$P_a$	$T_1$
74	95	761.2	85
95	95		
116	99		
133	104		
153	109		
169	116		
181	122		
196	131		
220	136		
241	197		
260	228		
287	230		
324	289		
370	341		
424	407		
473	464		
527	520		

100

2001-2002

S. C. P.	19	AP
101	001	001
005	001	001
006	001	001
007	001	001
008	001	001
009	001	001
010	001	001
011	001	001
012	001	001
013	001	001
014	001	001
015	001	001
016	001	001
017	001	001
018	001	001
019	001	001
020	001	001

TABLE II

PRESSURE READINGS, NOZZLE # 2

13 JULY, 1946

 $P_e$  = Exhaust Chamber Pressure, mm. Hg. $P_2$  = Pressure in Exit of Nozzle, mm. Hg. $P_1$  = Nozzle Inlet Pressure, mm. Hg. $P_a$  = Atmospheric Pressure, mm. Hg. $T_1$  = Nozzle Inlet Temperature, Degrees F.

$P_e$	$P_2$	$P_1$	$P_a$	$T_1$
71	133	502	761.5	85
86	133	502		
94	133	502		
113	133	502		
131	133	502		
144	138	502		
151	143	502		
171	146	502		
183	150	502		
192	155	502		
211	178	502		
217	188	502		
244	227	502		
296	288	502		
340	338	502		
418	417	502		

## 12. 1936

Sept. 20th, '36.

S. J. TAYLOR, Research Director

With the present number I would like to add a few notes on the present state of research on the following topics which have been discussed at the recent meeting of the Royal Society of Canada:

$\frac{M}{M}$	$\frac{M}{M}$	$\frac{M}{M}$	$\frac{M}{M}$	$\frac{M}{M}$
10	6.00	100	433	57
		200	872	86
		300	1311	109
		400	1750	122
		500	2188	136
		600	2626	145
		700	3064	155
		800	3502	165
		900	3940	175
		1000	4378	185
		1100	4816	195
		1200	5254	205
		1300	5692	215
		1400	6130	225
		1500	6568	235
		1600	7006	245
		1700	7444	255

TABLE III

PRESSURE READINGS, NOZLE #3

22 JULY, 1946

 $P_e$  = Exhaust Chamber Pressure, mm. Hg. $P_3$  = Pressure at Exit of Tube, mm. Hg. $P_2$  = Pressure at Tube Inlet (Nozzle Exit), mm. Hg. $P_a$  = Nozzle Inlet Pressure, Atmospheric $T_1$  = Inlet Temperature, Degrees F.

$P_e$	$P_3$	$P_2$	$P_a$	$T_1$
80.4	135.4	93.4	764.4	85
97	135			
113	135			
129	135			
140	135			
158	135			
185	137			
197	141			
206	143			
213	156			
228	181			
238	198			
246	213			
261	225			
288	255			
300	267			
358	229			



TABLE IV  
NOZZLE CHARACTERISTICS

$A_t$  = Cross-sectional Area at Throat

$A_e$  = Cross-sectional Area at Exit

$r_t$  = Theoretical Ratio of Exit Pressure to Inlet Pressure

$r_a$  = Actual Ratio of Exit Pressure to Inlet Pressure

$M_t$  = Theoretical Mach Number at Exit (Frictionless Flow)

$M_a$  = Actual Mach Number at Exit

$C_v$  = Assumed Velocity Coefficient

$w$  = Flow in Pounds per Second

$G$  = Flow per Unit Area at Exit, Pounds per Squarefoot per Second

$T_1$  = Inlet Temperature, Degrees F.

$P_1$  = Inlet Pressure, Atmospheres

<u>NOTATION</u>	<u>NOZZLE # 1</u>	<u>NOZZLE # 2</u>	<u>NOZZLE # 3</u>
$A_t/A_e$	1.9307	1.2870	1.9307
$r_t$	.1000	.2200	.1000
$r_a$	.1240	.2750	.1833
$M_t$	2.1520	1.6180	2.1520
$M_a$	1.8500	1.3900	1.3900
$C_v$	.95	.95	
$P_1$	1.0000	.6667	1.0000
$T_1$	85	85	85
$w$	.0676	.0676	.0676
$G$	25.2000	25.2000	25.2000

herself to new foundations & she  
 shall do well. I am very sorry to  
 receive such a report about the child. I am  
 most sorry about the child. And the child has had a  
 (well, reasonably) full life without much guidance &  
 And the child shall receive a  
 wonderful education because  
 there may come a day when  
 herself, though she is not, shall say no. To  
 herself, "I am not  
 a motherless creature, I have  
 a

NAME	AGE	NAME	AGE
ROSE, A.	1985, 1	ROSE, E.	1985, 1
ROSE,	1985,	ROSE,	1985,
ROSE,	1985,	ROSE,	1985,
ROSE, A.	1985, 1	ROSE, E.	1985,
ROSE, E.	1985, 1	ROSE, E.	1985,
	1985,		1985,
ROSE, E.	1985,	ROSE, E.	1985,
	1985,		1985,
ROSE,	1985,	ROSE,	1985,
	1985,		1985,
ROSE, E.	1985, 1	ROSE, E.	1985,

**NOZZLE #4**

FULL SCALE

ALL SURFACES TO BE FINISHED GROUND

MATERIAL - STEEL

PIECES #3 AND #4 ALIKE

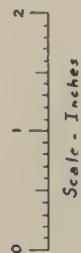
4.3872"

TAPPED FOR  $\frac{3}{16}$ " BOLT

OFFSETS NOZZLE #4

"X"	"Y"
0	.2000
.87	.3100
.95	.3200
1.00	.3250
1.10	.3360
1.20	.3470
1.30	.3550
1.40	.3635
1.50	.3690
1.60	.3740
1.70	.3790
1.80	.3830
1.90	.3850
2.00	.3860
2.10	.3865
2.24	.3872
2.365	.3872

STRAIGHT SLOPING  
CURVED PORTION





INDEX

OFFSET NOZZLE "2"

<i>X</i>	<i>Y</i>
0	.3000
1.00	.3560
1.10	.3550
1.20	.3600
1.30	.3640
1.40	.3675
1.50	.3710
1.60	.3742
1.70	.3775
1.80	.3800
1.90	.3825
2.00	.3850
2.10	.3862
2.20	.3870
2.24	.3872
2.30	.3874

Scale - Inches

NOZZLE '2

Ground Finches

MATERIAL - SYSTEM

SIEGEES & ALLIES

TA

A horizontal row of four vertical tick marks. The third tick mark from the left contains a small circle.

*.125" ORILL*

10

3"

P1

19.915



## FIGURE XXIII

### OFFSETS NOZZLE "3"

#### NOZZLE "3"

FULL SCALE

ALL SURFACES TO BE FINISHED GROUND

MATERIAL - STEEL

PIECES #1 AND #2 ALIKE

"X"	"Y"	
0	.2000	STRAIGHT SLOPING
.97	.3100	
.95	.3200	
1.00	.5250	
1.10	.3360	
1.20	.3970	
1.30	.3650	
1.40	.5635	CURVED PORTION
1.50	.3620	
1.60	.3790	
1.70	.3770	
1.80	.3830	
1.90	.3850	
2.00	.3860	
2.10	.3865	
2.20	.3870	ST HORIZ PORTION
2.24	.3872	
2.365	.3872	

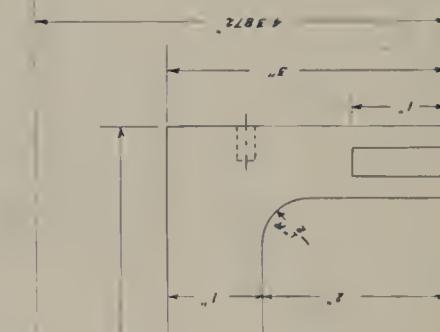
Scale - Inches

PIECE #1

PIECE #2

10.35°

Straight tube



4.3872

3"

1"

1"

1"

1"

1"

1"

1"

1"

1"

1"

1"

1"

1"

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1"

1"

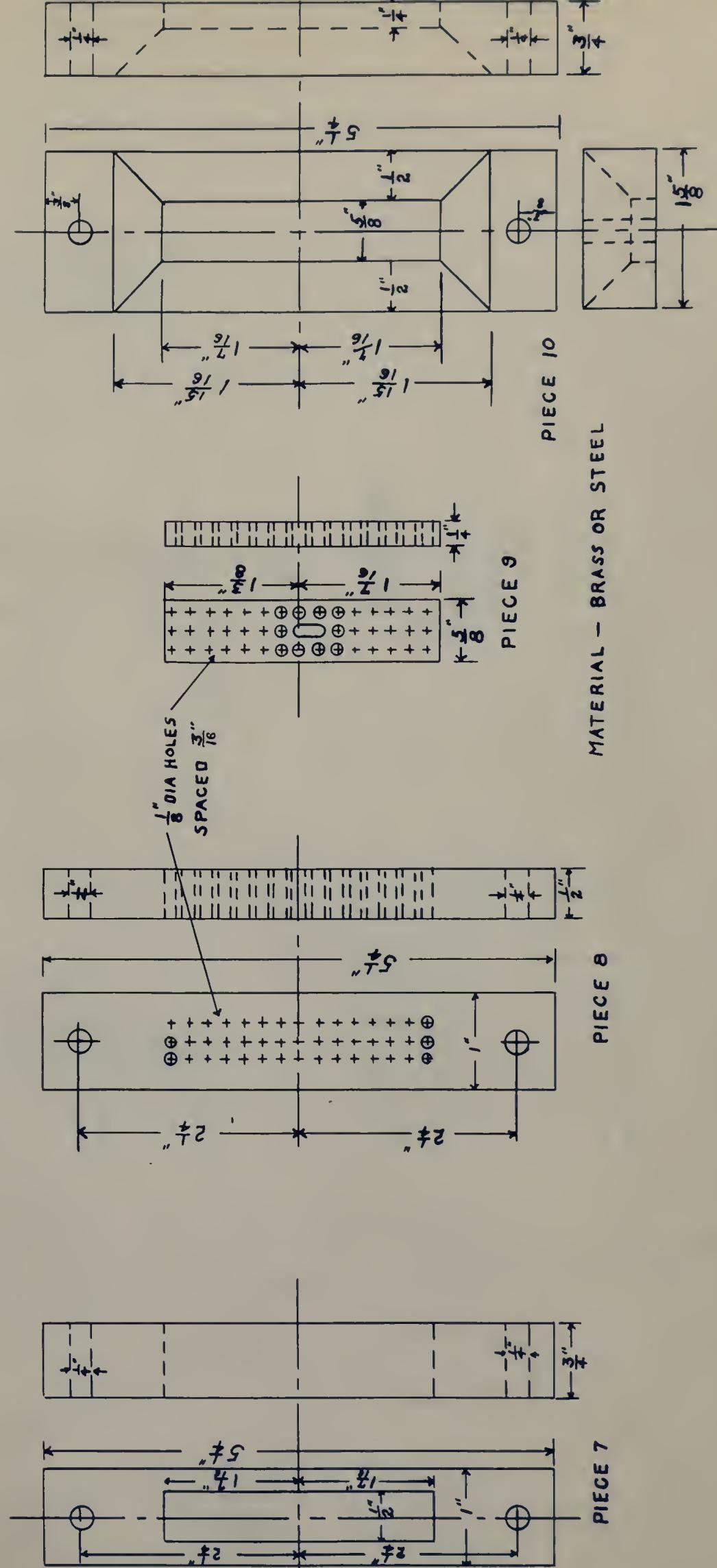
1"

1"

1"



GILDED PAGES





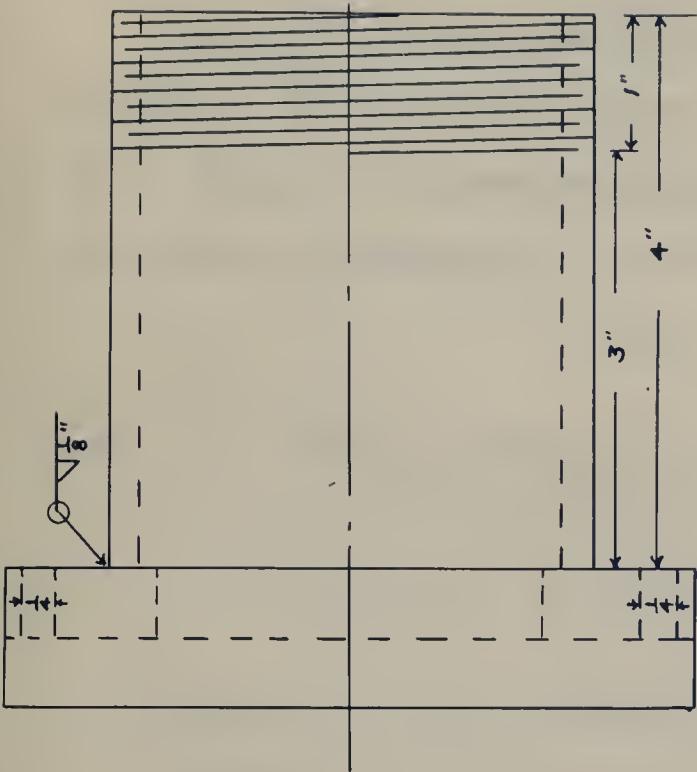
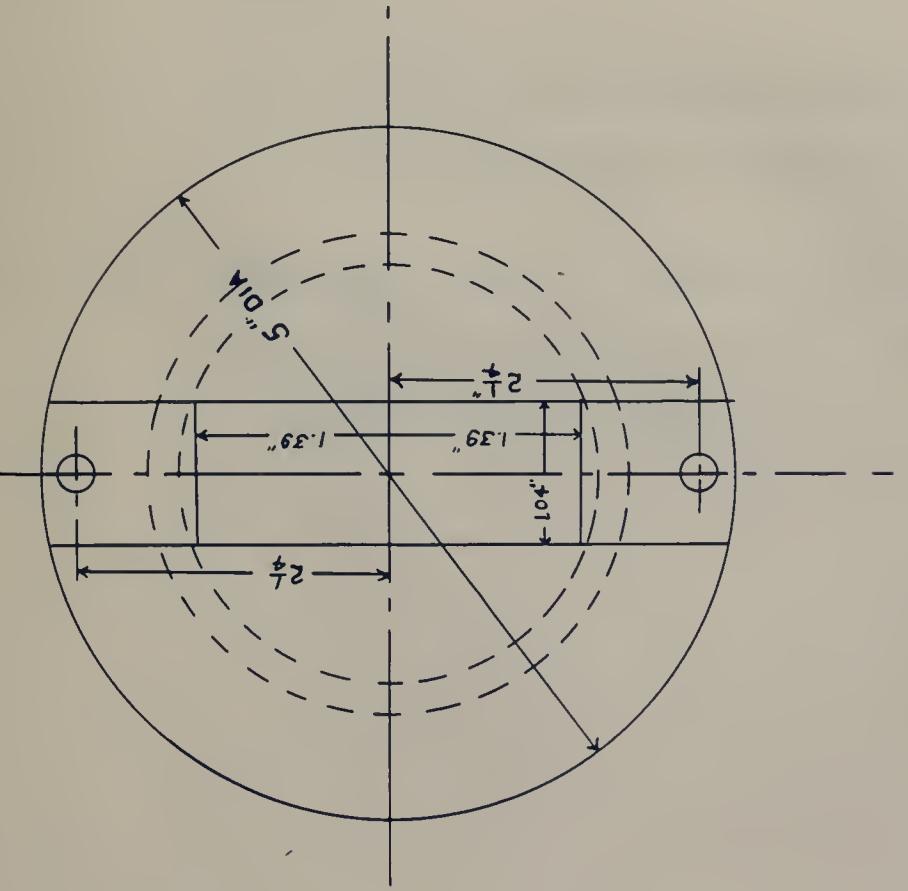
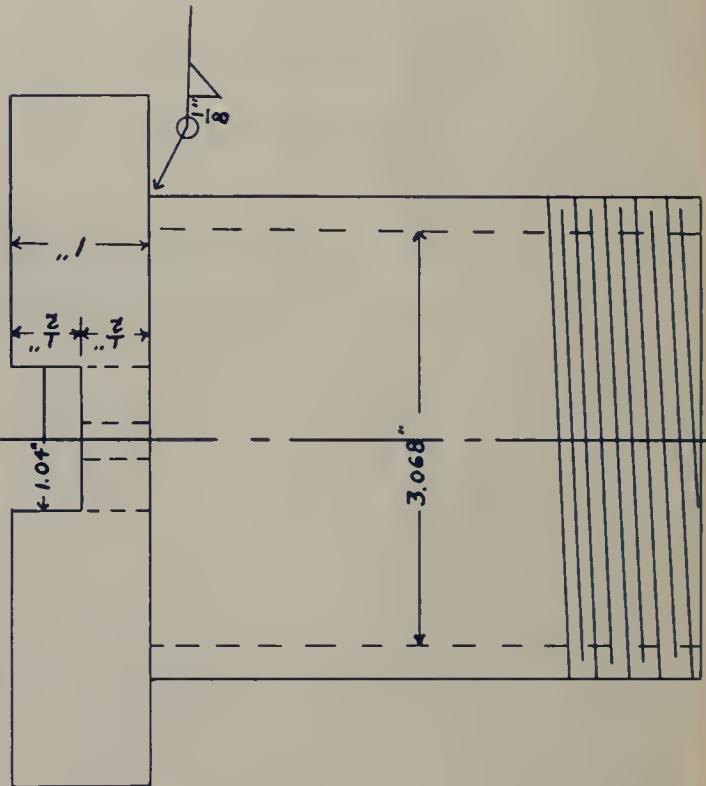


FIGURE XXX  
EXHAUST FITTING  
MATERIAL- STEEL

SCALE - IN.  
1  
2





APPENDIX C -- LOCATION OF ORIGINAL DATA

All of the original nozzle design calculations, photographic negatives, and the nozzle profiles are in the possession of Mr. E. P. Neumann of the Mechanical Engineering Department, Massachusetts Institute of Technology.

REVIEW OF THE LIBRARY  
OF THE SOCIETY FOR THE ADVANCEMENT OF SCIENCE  
AND THE LIBRARY OF THE AMERICAN ASSOCIATION FOR THE ADVANCEMENT OF SCIENCE,  
COLLECTED IN STUDY.

APPENDIX D — BIBLIOGRAPHY

1. L.A. DeFrate, "Investigation of Supersonic Flow in Nozzles and Tubes by the Schlieren Method", Master's Thesis, M.I.T., 1943.
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6. J.H. Keenan and E.P. Neumann, "Friction in Pipes at Supersonic and Subsonic Velocities", National Advisory Committee for Aeronautics, Technical Note # 963.

and that all such observations be communicated to the Royal Society.

1801, Feb. 12. "Received a letter from Mr. John Greenly, Esq., of Quebec, Canada, dated Jan. 10, 1801, giving an account of his

recent voyage to the Arctic regions, during which he made

"many fine observations of the sky, and the sun's altitude,

and the variation of the magnetic needle."

1801, Feb. 12. Received a letter from Mr. John Greenly, Esq.,

"from Quebec, dated Jan. 10, 1801, containing an account of

"his late voyage to the Arctic regions, during which he made

"many fine observations of the sky, and the sun's altitude,"

etc.

"He also describes his observations of the sun's altitude, &c.,

"and the variation of the magnetic needle, made during his

"voyage to the Arctic regions, during which he made

"many fine observations of the sky, and the sun's altitude,"

etc. etc.



Dante Due





AUG 31  
AP 26 62  
FE 17 64  
3 NOV 68

BINDERY  
11932  
12942  
18284

Thesis 11660  
P34 Perry  
Schlieren observation of  
supersonic discharge.

\*  
AP 26 62  
FE 17 64  
3 NOV 68  
3 NOV 68

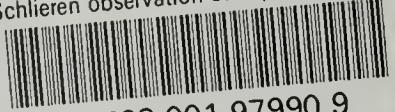
BINDERY  
11932  
12942  
18284  
18284

Thesis 11660  
P34 Perry  
Schlieren observation of super-  
sonic discharge.

Library  
U. S. Naval Postgraduate School  
Monterey, California



thesP34  
Schlieren observation of supersonic disc



3 2768 001 97990 9  
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