$\mathfrak{S m i t h s o n i a n} \mathfrak{C o n t r i b u t i o n s}$ to Kinowledge.

## OBSERVATIONS

## TERRESTRAL MAGETISII

AND ON THE

## deviations of The compasses

## SMITHSONIAN CONTRIBUTIONS TO KNOWLEDGE.

## OBSERVATIONS

ON

# TERRESTRIAL MAGNETISM 

AND on the

## DEVIATIONS 0F THE C0MPASSES

OF THE UNITED STATES IRON CLAD MONADNOCK DURING HER CRUISE FROM PHÍILADELPHIA TO SAN FRANCISCO, IN 1865 AND 1866.

BY
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## INTRODUCTORY NOTE.

This paper was originally an official report presented to the Navy Department by Professor Harkness; but, as that department made no use of it, the National Academy of Sciences, in August, 1867, passed a resolution asking for the manuscript. This request was complied with; and, an abstract of the paper having been read to the Academy in April, 1869, it was referred to a commission consisting of the President of the Academy, Professors J. H. C. Coffin, and F. Rogers, in accordance with whose recommendation it is now published by the Smithsonian Institution.

## Joseph Henry,

Secretary S. I.

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# REPORT ON MAGNETIC OBSERVATIONS. 

SECTION I.<br>INTRODUCTION.

On the fifth of October, 1865, I was ordered to the U. S. Iron-clad Monadnock ${ }^{1}$ for the purpose of making observations on the action of her compasses during the cruise which she was about to undertake from Philadelphia to San Francisco, by way of the Straits of Magellan. She was then fitting out at the Philadelphia Navy Yard, and the work on her was so far advanced that it was expected she would sail in about two weeks. As the department had not previously intimated its intention of assigning me to this duty, and as everything relating to the number and kind of observations to be made, and the instruments required, was left entirely to my own discretion, it will be seen that the time available for making plans and collecting the necessary apparatus was very limited.
The plan of observation ultimately adopted was that at every port in which we remained for more than twenty-four hours the following operations should be gone through with. 1st. The ship should be swung, and as her head pointed successively to each of the thirty-two true magnetic points, the reading of every compass on board should be recorded for each point. 2d. That at such of the compasses as were so situated as to render it possible, the horizontal force and inclination should be determined. 3d. The position of the dividing line between the north and south polarity should be traced on each turret. 4th. The magnetic declination, inclination, and horizontal force should be determined on shore. While at sea it was intended to observe the declination-and consequently the deviation-and horizontal force daily, by means of the standard compass; but this turned out to be impracticable, because the only place in the ship where it was possible to mount that instrument was on top of the after pilot-house; a situation

[^1]where no binnacle could be put, and where the compass was nearly on a level with the top of the smoke-stack. Thus, while at sea, the position occupied by it was almost constantly enveloped in smoke and gas, rendering it absolutely necessary, whenever we left port, to dismount the instrument in order to preserve it from injury.

Owing to the very short time at my disposal previous to sailing, there was great difficulty in providing proper instruments, but I succeeded in obtaining all that were absolutely necessary. The following is a list of them:

```
I Portable Declinometer and stand.
I Five-inch Altitude and Azimuth Instrument.
x Dip Circle, with two needles, each three and a half inches long.
I Pair of eight-inch Bar Magnets.
r Pair of eleven-inch Bar Magnets.
2 Admiralty Standard Compasses, with stands and deflectors.
r Burt's Solar Compass and stand.
x Prismatic Sextant of six inches radius.
x Mercurial Artificial Horizon.
I Pocket Chronometer, Fletcher, No. 906.
x Silver Comparing Watch.
2 Pocket Thermometers.
2 Pocket Compasses.
2 Magnetic Needles, not mounted, each 2.75 inches long, and 0.33 of an inch broad.
i Fifty feet Chesterman's Patent Tape Line.
r Case of Drawing Instruments.
r Gunter's Scale, two feet long.
```

The portable declinometer belonged to the U.S. Coast Survey, and was kindly lent by Prof. J. E. Hilgard.

The small unmounted magnetic needles were intended to be used for measuring the relative horizontal force on shore and at each of the compasses on board ship. For this purpose it was proposed to vibrate one of them on shore, and then taking it on board ship to the compass at which it was desired to measure the relative horizontal force, to remove the compass card from the centre-point, and putting the small needle in its place, vibrate it again. Unfortunately the small needles were not finished till just before we left Philadelphia, and there was no opportunity of trying them till after we were at sea, when, to my great regret, it was found that the jewels were so small that they would not fit on the centre-point of any compass on board, thus rendering them entirely useless. Under the circumstances, for horizontal force on board ship it was necessary to rely entirely upon measures made with the deflectors belonging to the Admiralty standard compasses-a method certainly not so convenient, and, owing to the constant swinging of the ship when at anchor, probably not so accurate as counting the vibrations of a small needle.

The observations on terrestrial magnetism, and for latitude, time, and true bearings, were all made by myself and recorded by Mr. Corrin F. Smith, who was captain's clerk on the Monadnock, and acted as my assistant when I was observing. My best thanks are due to him for the efficient manner in which he performed his duties, sometimes under circumstances of very considerable physical discomfort.

The reductions and discussions in this report have been made by me, so that I am personally responsible, not only for the general plan of the work, but for every figure contained in it. All the results have been very carefully checked, and it is hoped no material error will be found in them; still, absolute accuracy is scarcely to be expected in any work involving so many figures, the more especially as much of it has been done during moments snatched from other and more pressing professional duties.

The observations naturally divide themselves into three classes: 1st. Those relating to astronomy. 2d. Those relating to terrestrial magnetism. 3d. Those relating to the magnetism of the ship. As that is the order in which they must necessarily be reduced, they will be so treated of in the subsequent sections of this report.

## SECTION II.

## DESCRIPTIONSOF STATIONS.

UnLess otherwise stated, the assumed positions of light-houses, forts, etc., have been taken from the English Admiralty Charts, or from the English Admiralty List of Lights, the latest editions obtainable in 1865 being employed. The longitudes are counted from the meridian of Greenwich.
The method used in testing a station for local attraction by means of fore and back sights with a compass, was as follows: The compass was set up at the station, and the bearing of a point distant one hundred yards, or more, was observed. Then the compass was transferred to that point, and the bearing of the station was observed. These two bearings should evidently differ from each other by $180^{\circ}$; if they did not, it was certain that local attraction existed at one or both of the points, and a new station was sought for. This process is almost certain to detect any strictly local magnetic attraction, but it will not suffice to demonstrate the existence of an abnormal state of the magnetic elements extending over a large territory.

Philadelphia, Pa. The magnetic observations were made at a spot on the east bank of the Delaware river, about twenty feet from the water's edge. It is nearly southeast from the U.S. Navy Yard, from which it is distant about three-quarters of a mile. The soil is a dark-nearly black-earth, which appears to have been deposited by the river. The approximate position of the station was

| Lat. | $39^{\circ}$ | $55^{\prime} \mathrm{N}$. |  |
| :--- | ---: | :--- | :--- | :--- |
| Long. | $5^{\mathrm{h}}$ | $0^{\mathrm{m}}$ | $32^{\mathrm{s}} \mathrm{W}$. |

Gosport, Va. The magnetic observations were made on a white sandy beach, on the west bank of the Elizabeth river, about thirty feet from the water's edge. From the place where the instruments stood, the flagstaff in the U.S. Navy Yard bore due north by compass, and was distant about half a mile.

Assuming the position of the flagstaff to be lat. $36^{\circ} 49^{\prime} 32^{\prime \prime}$ N., long. $5^{\mathrm{h}} 5^{\mathrm{m}} 9^{\mathrm{s}} .8 \mathrm{~W}$., as stated by the authorities at the Navy Yard, the position of the spot occupied by the instruments is approximately

$$
\begin{aligned}
& \text { Lat. } 36^{\circ} \quad 49^{\prime} 0^{\prime \prime} \mathrm{N} \text {. } \\
& \text { Long. } 5^{\mathrm{h}} \quad 5^{\mathrm{m}} 9^{\mathrm{s}} .8 \mathrm{~W} \text {. }
\end{aligned}
$$

The ship was swung at the compass station in Hampton Roads, on November 1st, 1865 , in the usual manner. Her position at the time was lat. $36^{\circ} 58^{\prime}$ N., long. $76^{\circ} 20^{\prime} \mathrm{W}$. Joint XII on the after turret was 14.4 inches to port.
(4)

St. Thomas, West Indies. The ship was swung in this harbor, on November 18th, 1865, in the usual manner. Her position at the time was lat. $18^{\circ} 19^{\prime} \mathrm{N}$. , long. $64^{\circ} 56^{\prime}$ W. Joint XII on the after turret was 14.4 inches to port.

The observations on shore were made in Long Bay, at a spot about thirty feet from the water's edge, on a gravelly beach, to the eastward of the town. From the place where the instruments stood the true bearing of Fort Cowell, at the entrance to the harbor, is $\mathrm{S} .34^{\circ} 50^{\prime} \mathrm{W}$., and it is distant about one mile.

Assuming the position of Fort Christian to be lat. $18^{\circ} 20^{\prime} 27^{\prime \prime}$ N., long. $4^{\mathrm{h}} 19^{\mathrm{m}}$ $42^{s} .7$ W., then, according to the English Admiralty Chart, the position of the spot where the instruments were set up is

$$
\begin{array}{lrrr}
\text { Lat. } & 18^{\circ} & 20^{\prime} & 22^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 4^{\mathrm{h}} & 19^{\mathrm{m}} & 40^{2} .6 \mathrm{~W} .
\end{array}
$$

Isle Royal, Salute Islands. An attempt was made to swing the ship here, on November 30th, 1865, in the usual manner, but it failed on account of the continual rain which shut off the view of the distant azimuth mark. The position of the ship at the time was lat. $5^{\circ} 1^{\prime 7^{\prime}}$ N., long. $52^{\circ} 33^{\prime}$ W. Joint XII on the after turret was 0.6 of an inch to starboard.

The magnetic and astronomical observations on shore were made on the southwest side of the island, at a spot from which the corner made by the southeast and southwest faces of the government coal sheds bears N. $64^{\circ} \mathrm{W}$. (true), and is distant one hundred and thirty-two feet. The place was examined carefully for local attraction by taking fore and back sights with a compass, but none could be detected. The position occupied by the instruments is in

$$
\begin{array}{llll}
\text { Lat. } & 5^{\circ} & 17^{\prime} & 29^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 3^{\mathrm{h}} & 30^{\mathrm{m}} & 11^{\mathrm{s}} .4 \mathrm{~W} .
\end{array}
$$

The latitude was determined from a single set of circummeridian altitudes of the sun observed by me, and the longitude was taken from the French chart.

Ceara, Brazil. An attempt was made to swing the ship here, on December 19th, 1865, in the usual manner, but although a very favorable opportunity was chosen, she could only be made to turn through ten points. Her position at the time was lat. $3^{\circ} 44^{\prime}$ S., long. $38^{\circ} 34^{\prime} \mathrm{W}$. Joint XII on the after turret was 0.6 of an inch to starboard. The wind, current, and sea are so strong here that vessels at anchor in the roads always ride with their heads nearly in the same direction, never swinging more than about three points.

At this place there is no harbor whatever, merely an open roadstead. A heavy surf is constantly running on the beach, and as there are almost no facilities for landing in small boats, getting the instruments on shore involved a good deal of trouble and some risk. However, I succeeded in landing them safely, and obtained a very good set of observations on the white sand beach at a spot about one hundred and fifty feet from the water's edge, and from which the true bearing of the southeast corner of the custom-house on the wharf is $\mathrm{N} .53^{\circ} 19^{\prime} \mathrm{W}$., and its distance two hundred feet. From the same spot the true bearing of

Point Macoripe Light-house is N. $75^{\circ} 38^{\prime}$ E. The position occupied by the instruments is in

$$
\begin{array}{llll}
\text { Lat. } & 3^{\circ} & 43^{\prime} & 59^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 2^{\mathrm{h}} & 34^{\mathrm{m}} & 6^{\mathrm{s}} \mathrm{~W} .
\end{array}
$$

The latitude was deduced from my own observations, and the longitude was taken from the list of geographical positions given in Raper's Navigation.

Pernambuco, Brazil. The ship was not swung in this port because there was not room to do it in the position where she took her coal, and as she only remained in the harbor twenty-four hours, there was not time to take up another position in order to swing.

The magnetic and astronomical observations on shore were made on the white sand beach, at a spot from which the true bearing of the salient angle of the southeast bastion of Fort Brum is N. $15^{\circ} 46^{\prime}$ W., and its distance four hundred and thirty feet.

Assuming the position of the light-house, near to Fort Picao, to be lat. $8^{\circ} 3^{\prime} 42^{\prime \prime}$ S., long. $2^{\mathrm{h}} 19^{\mathrm{m}} 26^{\mathrm{s}} .8 \mathrm{~W}$., as it is given in the English Admiralty List of Lights, edition of 1866, then, according to the English Admiralty Chart, the position occupied by the instruments is in

$$
\begin{array}{llll}
\text { Lat. } & 8^{\circ} & 3^{\prime} & 37^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 2^{\mathrm{h}} & 19^{\mathrm{m}} & 28^{\mathrm{s}} .2 \mathrm{~W} .
\end{array}
$$

Bahia, Brazil. The ship was swung in this harbor, on December 30th, 1865, in the usual manner. Her position at the time was lat. $12^{\circ} 59^{\prime}$ S., long. $38^{\circ} 31^{\prime} \mathrm{W}$. Joint XII on the after turret was 0.6 of an inch to starboard.

The magnetic and astronomical observations of December 27th were made at a spot, one hundred and fifty feet from the water's edge, situated in a cocoanut grove on the beach about half-way between Monserat Point and Fort Victoria. The soil is a coarse white sand. It was not possible to get any bearings which would define the exact position, but the above directions are sufficient to enable any one to find the place very nearly.

Assuming the position of Fort St. Antonio Light to be lat. $13^{\circ} 0^{\prime} 55^{\prime \prime}$ S., long. $2^{\mathrm{h}} 34^{\mathrm{m}} 6^{\mathrm{s}} .9 \mathrm{~W}$., then, according to the English Admiralty Chart, the position occupied by the instruments is in

$$
\begin{array}{lrlll}
\text { Lat. } & 12^{\circ} & 56^{\prime} & 55^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 2^{\mathrm{h}} & 34^{\mathrm{m}} & 0^{\mathrm{s}} .5 & \mathrm{~W} .
\end{array}
$$

Rio Janeiro, Brazil. The ship was swung in this harbor, on January 10th, 1866, in the usual manner; but, owing to a strong wind which was blowing at the time, it was not possible to get her through more than seventeen points. Her position was lat. $22^{\circ} 54^{\prime}$ S., long. $43^{\circ} 9^{\prime} \mathrm{W}$. Joint XII on the after turret was 0.8 of an inch to port.

During the whole week we were at Rio there was not one clear day. Consequently it was extremely difficult to make astronomical observations, and it was only by patiently watching for the sun and seizing the opportunities when it was
momentarily visible through breaks in the clouds, that the few sights necessary in order to complete the magnetic observations were obtained.

With a single exception, all the magnetic and astronomical observations were made at a spot from which the true bearing of the entrance on the north face of Fort Caraguata (erroneously spelled Gravata on the English charts) is S. ${ }^{\prime} 0^{\circ}$ W., and its distance fifty-five feet. There were no guns in the fort at the time. The surrounding country is very hilly, the bare, coarse, granite rocks cropping out everywhere from the hill-sides, but in the more level places they are thinly covered with earth. Assuming the position of Fort Villegagnon to be lat. $22^{\circ} 54^{\prime} 42^{\prime \prime}$ S., long. $2^{\mathrm{h}} 52^{\mathrm{m}} 36^{\mathrm{s}} .0 \mathrm{~W}$. , then, according to the English Admiralty Chart, the position occupied by the instruments is in

$$
\begin{aligned}
& \text { Lat. } \quad 22^{\circ} \\
& \text { Long. } \\
& 2^{\mathrm{h}}
\end{aligned} 54^{\prime} \quad 52^{\mathrm{m}} \quad 30^{\prime \prime} .7 .7 \mathrm{~W} .
$$

The exception referred to above is some observations of the sun for time, made on January 9th. They were got on Rat Island, the spot where naval officers usually go to rate their chronometers when lying in this harbor. Assuming the position of Fort Villegagnon as above, then, according to the English Admiralty Chart, the position of Rat Island is

| Lat. | $22^{\circ}$ | $53^{\prime}$ | $45^{\prime \prime}$ |
| :--- | :---: | :---: | :---: |
| Long.. | $2^{\mathrm{h}}$ | $52^{\mathrm{m}}$ | $3^{7^{\mathrm{s}} .9} .9 \mathrm{~W}$. |

Monte Video, Uruguay. The ship was swung in this harbor, on January 24th, 1866 , in the usual manner. We first attempted to get her around about 1 P. M., but owing to the force of the wind and tide we only obtained ten points, viz., those from E. by S. to S.S. W. Just at sunset we tried it again, and succeeded in getting the remainder of the circle. It was nearly dark when we finished, but as the distant object used for an azimuth mark shone plainly against the sky, there was sufficient light to see pretty distinctly when it was in range with the sights of the compass.

The readings of part of the circle on the After Ritchie compass were lost, owing to the failure of daylight and delay in procuring a lantern. The officer who usually read the After Azimuth compass was on shore at the time, and the duty of making the observations at that instrument was assigned to another, but it turned out that he did not understand how to read an azimuth compass, and his observations were worthless.

While we were lying at Monte Video the tide was very irregular. Most of the time the ship only swung to it about $90^{\circ}$, but two or three times she swung $180^{\circ}$. At the time we swung her to obtain the deviation of the compasses her position was lat. $34^{\circ} 55^{\prime}$ S., long. $56^{\circ} 13^{\prime}$ W., and joint XII on the after turret was 4.5 inches to port.

The greater part of the magnetic observations on shore were made on January 18th, at a station on the ground occupied by Tomkinson's slaughtering establishment. The instruments were set up at a spot where there are four large umbu trees standing in a line. The exact position may be recovered by means of the following true bearings. The corner made by the south and west sides of the dwelling-house
bears N. $39^{\circ}$ E., and is distant about one hundred feet. The light-house on the Mount, on the west side of the harbor, bears N. $59^{\circ} 0^{\prime} \mathrm{W}$. The water's edge is distant from the station about four hundred feet. The soil is a thin stratum of very poor earth, covering a greenish-colored slaty rock, which crops out in many places. Assuming the position of the light-house on the Mount to be lat. $34^{\circ} 53^{\prime} 15^{\prime \prime}$ S., long. $3^{\mathrm{h}} 44^{\mathrm{m}} 59^{\mathrm{s}} .0 \mathrm{~W}$., then, according to the English Admiralty Charts, the position occupied by the instruments is in

$$
\begin{array}{lrll}
\text { Lat. } & 34^{\circ} & 53^{\prime} & 39^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 3^{\mathrm{h}} & 44^{\mathrm{m}} & 55^{\mathrm{s}} .8 \mathrm{~W} .
\end{array}
$$

As a check, some magnetic observations were made, on January 19th, at a station from which the true bearing of the light-house on the Mount is N. $89^{\circ} 41^{\prime}$ W., and the true bearing of the light on the Cathedral is $\mathrm{S} .17^{\circ} 42^{\prime} \mathrm{W}$. Assuming the position of the light-house to be as stated above, and the light on the cathedral to be in lat. $34^{\circ} 54^{\prime} 20^{\prime \prime}$ S., long. $3^{\mathrm{h}} 44^{\mathrm{m}} 50^{\mathrm{s}} .0 \mathrm{~W}$., as given in the English Admiralty List of Lights in South America, edition of 1865, the geographical position of this station was

$$
\begin{array}{lrll}
\text { Lat. } & 34^{\circ} & 53^{\prime} & 16^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 3^{\mathrm{h}} & 44^{\mathrm{m}} & 48^{\mathrm{s}} .3 \mathrm{~W} .
\end{array}
$$

It will be observed that the difference of longitude between the lights on the Mount and on the cathedral, as deduced from the Admiralty List cited above, cannot be made to agree with the positions given on the English Admiralty Chart.

On January 24th some observations for time were made on Rat Island. Assuming the position of the light-house on the Mount to be as stated above, then, according to the English Admiralty Chart, the position of the station on Rat Island was

$$
\begin{array}{lrll}
\text { Lat. } & 34^{\circ} & 53^{\prime} & 18^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 3^{\mathrm{h}} & 44^{\mathrm{m}} .52^{3} .9 \mathrm{~W} .
\end{array}
$$

Sandy Point, Straits of Magellan. The ship was swung in this harbor, on February 10th, 1866 , in the usual manner. Her position at the time was lat. $53^{\circ}$ $11^{\prime}$ S., long. $70^{\circ} 55^{\prime} \mathrm{W}$. Joint XII on the after turret was 4.5 inches to port. While we were lying here the ship was perfectly free to swing to the tide, but she generally turned through an arc of only about ninety degrees, namely, from W.N.W. to N.N.E.

The observations on shore were made in the meadow, between the settlement and the beach, at a spot from which the true bearing of the flagstaff was $\mathrm{N} .4^{\prime \prime}{ }^{\circ} 8^{\prime}$ W., and its distance about eight hundred feet. The soil is sandy, and there is no rock anywhere near. The place was examined for local attraction by taking fore and back sights with a compass, but nothing of the kind could be detected.

Assuming the position of the flagstaff to be lat. $53^{\circ} 10^{\prime} 15^{\prime \prime}$ S., long. $4^{\mathrm{h}} 43^{\mathrm{m}} 36^{9} .0$ W., as given on the English Admiralty Chart, edition of 1861, the position occupied by the instruments is in

$$
\begin{array}{lrll}
\text { Lat. } & 53^{\circ} & 10^{\prime} & 20^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 4^{\mathrm{h}} & 43^{\mathrm{m}} & 35^{\mathrm{s}} .3 \mathrm{~W} .
\end{array}
$$

Valparaiso, Chile. The ship was swung in this harbor, on April 4th, 1866, in the usual manner. Her position at the time was lat. $33^{\circ} 2^{\prime}$ S., long. $71^{\circ} 38^{\prime} \mathrm{W}$. Joint XII on the after turret was 4.25 inches to port. While we were lying at Valparaiso the ship was perfectly free to swing to the tide, and she turned in all directions.

The observations taken on shore March 2d were made on the south end of the white sand beach at the Estero de Quilpue, at a spot about two hundred and fifty feet from the rocks. Assuming the position of Fort San Antonio to be lat. $33^{\circ} 1^{\prime}$ $53^{\prime \prime}$ S., long. $4^{\mathrm{h}} 46^{\mathrm{m}} 46^{\mathrm{s}} .0 \mathrm{~W} .$, then, according to the English Admiralty Chart, the position of this station was approximately

$$
\begin{array}{lrl}
\text { Lat. } & 33^{\circ} & 1^{\prime} .4 \mathrm{~S} . \\
\text { Long. } & 4^{\mathrm{h}} & 46^{\mathrm{m}} 31^{\mathrm{s}} \mathrm{~W} .
\end{array}
$$

The observations of March 19th, and all taken subsequently to that date, were made at a spot distant about six hundred and fifty feet, nearly true north, from the most northern of the custom-houses. The instruments were set up, near to the water's edge, on the public road which here runs along under a high bank of rock. The true bearing of the flagstaff at Fort San Antonio, on the top of the hill, was S. $31^{\circ} 45^{\prime}$ W., and its estimated distance was seven hundred feet. Assuming the position of the fort to be as stated above, the position occupied by the instruments is in

$$
\begin{array}{lrrl}
\text { Lat. } & 33^{\circ} & 1^{\prime} & 4^{\prime \prime \prime} \mathrm{S} . \\
\text { Long. } & 4^{\mathrm{h}} & 46^{\mathrm{m}} & 45^{\mathrm{s}} .7
\end{array}
$$

Both this station and that of March 2d were carefully tested for local attraction by taking fore and back sights with a compass, but none could be detected.

In adopting $4^{\mathrm{h}} 46^{\mathrm{m}} 46^{\dot{\mathrm{s}}} .0$ as the longitude of Fort San Antonio, I have followed Raper, but this value is doubtless too large. Capt. Jas. M. Gilliss, U. S. N., from a series of occultations and moon culminations, observed during the years 1850-51-52, determined the longitude of the Observatory on the hill of Santa Lucia, in Santiago, to be $4^{\text {h }} 42^{\mathrm{m}} 33^{\mathrm{s}} .8$. Dr. Moesta, from subsequent observations up to the year 1862, corrected this value to $4^{\mathrm{h}} 42^{\mathrm{m}} 33^{\mathrm{s}} .0$. Capt. Gilliss, by means of the electric telegraph, found the difference of longitude between the Observatory at Santiago and Mr. Mouatt's Observatory at Valparaiso to be $3^{\mathrm{m}} 56^{\mathrm{s}} .5$. Hence, adopting Dr. Moesta's value of the longitude of Santiago, we have

$$
4^{\mathrm{h}} \quad 46^{\mathrm{m}} \quad 29^{\mathrm{s}} .5 \mathrm{~W}
$$

as the longitude of Mr. Mouatt's Observatory; but I have been unable to find any description of its position, and consequently cannot refer this longitude to Fort San Antonio.

Findlay, in his "Directory to the South Pacific Ocean," edition of 1863, gives for the longitude of Fort San Antonio $4^{\text {h }} 46^{\mathrm{m}} 28^{\mathrm{s}} .8$, and quotes Dr. Moesta as the authority. The Connaissance des Temps, for the year 1868, on the same authoritygives $4^{\mathrm{h}} 46^{\mathrm{m}} 2^{7} 7^{\mathrm{s}} .5$ for the same position. Which of the two values is nearest correct I am unable to say.

Callao, Peru. The ship was swung in this harbor, on April 29th, 1866, in the usual manner. Her position at the time was lat. $12^{\circ} 3^{\prime}$ S., long. $7^{\prime} \gamma^{\circ} 14^{\prime}$ W. Joint 2 December, 1871.

XII on the after turret was 5.5 inches to port. While we were lying at Callao the ship was perfectly free to swing to the tide, but the wind and current were so strong that she did not do so, but always lay with her head pointing in a southerly direction.

The observations taken on shore, April 26 th , were made on the northeast side of San Lorenzo Island, about two and a half miles southeast of the light-house. The island is a mass of hills, rising to an elevation of more than a thousand feet, composed of loose friable rock which seems to be of volcanic origin, and which is constantly disintegrating into a fine yellow sand. The place selected for making the observations is at the foot of a gorge where there is a beach, about a quarter of a mile long, of the yellow sand mentioned above. On the beach stand a number of fishermen's huts, and a few steps back, at the foot of the gorge, stands a large, square, two-story house. The spot where the instruments stood is on the southeast end of the beach, a little beyond the fishermen's huts, and just above high-water mark. Assuming the position of the light-house to be lat. $12^{\circ} 4^{\prime} 0^{\prime \prime}$ S., long. $5^{\text {b }}$ $9^{\mathrm{m}} 18^{\mathrm{s}} .0 \mathrm{~W}$., the position occupied by the instruments is in

$$
\begin{array}{lrll}
\text { Lat. } & 12^{\circ} & 5^{\prime} & 14^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 5^{\mathrm{h}} & 9^{\mathrm{m}} & 9^{\mathrm{s}} .1 \mathrm{~W} .
\end{array}
$$

The place was carefully tested for local attraction by taking fore and back sights with a compass, but none could be detected.

Payta, Peru. We remained in this port only from $2^{\mathrm{h}} 30^{\mathrm{m}}$ P. M. of May 6th, 1866 , till $6^{\mathrm{h}}$ P. M. of May 7 th, and there was neither time nor opportunity to swing the ship. However, a complete set of magnetic observations were made on shore at a station on the beach four-tenths of a mile northwest of the large iron building which stands just back from the mole, and is used by the government as a customhouse, etc. As nearly as could be determined from angles carefully measured, and plotted on the English Admiralty Chart, this station is identical with the one occupied by the officers of H. B. M. surveying vessel "Beagle," in the year 1836, when making their observations for determining the position of Payta. According to their determinations it is in

$$
\begin{array}{lcrl}
\text { Lat. } & 5^{\circ} & 5^{\prime} & 36^{\prime \prime} \mathrm{S} . \\
\text { Long. } & 5^{\mathrm{h}} & 24^{\mathrm{m}} & 22^{s} .0 \mathrm{~W} .,
\end{array}
$$

the longitude depending upon the position of the northeast bastion at Panama, New Granada, which is taken to be $5^{\mathrm{h}} 18^{\mathrm{m}} 4^{\mathrm{s}} .6 \mathrm{~W}$.

The instruments were set up, just above high-water mark, on the gray sand beach, about fifty feet back from which the land rises into bluffs, two hundred feet high, composed of a hard yellow earth, alternating with sedimentary rocks. The station was carefully examined for local attraction, by taking fore and back sights with a compass, but none could be detected.

Panama, New Granada. The ship was swung in this roadstead, on May 20th, 1866 , in the usual manner. Her position at the time was lat. $8^{\circ} 55^{\prime} \mathrm{N} .$, long. $79^{\circ}$ $30^{\prime} \mathrm{W}$. Joint XII on the after turret was 5.5 inches to port. While we were lying here the ship was swinging freely in all directions to the wind and tide.

The observations taken on shore, May 14 th, were made on the northern side of Flamenco Island, to the westward of a small cocoanut grove, and northeast of the Naval Cemetery. The instruments were set up about ten feet north of the most western of the ruins which are to be found there. The island is rocky, but at this station the rocks are covered with earth. The spot was carefully tested for local attraction by taking fore and back sights with a compass, but none could be detected.
If we assume the position of the northeast bastion at Panama to be lat. $8^{\circ} 56^{\prime}$ $56^{\prime \prime}$ N., long. $5^{\mathrm{h}} 18^{\mathrm{m}} 4^{\mathrm{s}} .6 \mathrm{~W}$., as given by Capt. H. Kellet, R. N., then, according to the English Admiralty Chart, the position occupied by the instruments is in

$$
\begin{array}{llll}
\text { Lat. } & 8^{\circ} & 54^{\prime} & 31^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 5^{\mathrm{h}} & 18^{\mathrm{m}} & 1^{\mathrm{s}} .8 \mathrm{~W} .
\end{array}
$$

Acapulco, Mexico. The ship was swung in this harbor, on June 1st, 1866, in the usual manner. Her position at the time was lat. $16^{\circ} 50^{\prime} \mathrm{N} .$, long. $99^{\circ} 52^{\prime} \mathrm{W}$. Joint XII on the after turret was 5.5 inches to port. During the three days we were lying at Acapulco the ship was swinging freely to the wind and tide.

At the extreme south end of St. Lucia Bay, in this harbor, are two cocoanut groves, the most western of the two containing the graves of a number of our naval officers. The western end of the eastern grove is the place where the observations taken on shore, on May 30th, were made. The trees come almost close down to high-water mark, and the soil is a gray sand. The instruments were set up about forty feet from high-water mark, at a spot from which the true bearing of the gate of Fort St. Diego is N. $6^{\circ} 22^{\prime} \mathrm{E}$.

If we assume the position of this gate to be lat. $16^{\circ} 50^{\prime} 56^{\prime \prime}$ N., long. $6^{\text {h }} 39^{\mathrm{m}} 29^{\mathrm{s}} .0$ W., as given on the English Admiralty Chart, then, according to that chart, the position occupied by the instruments is in

$$
\begin{array}{llll}
\text { Lat. } & 16^{\circ} & 50^{\prime} & 3^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 6^{\text {b }} & 39^{\mathrm{m}} & 29^{\mathrm{s}} .4 \mathrm{~W} .
\end{array}
$$

Magdalena Bay, Lower California. An attempt was made to swing the ship in this bay, on June 9 th, 1866 , in the usual manner, but owing to a very stiff breeze which was blowing at the time, she could only be turned through fourteen points. Her position was lat. $24^{\circ} 38^{\prime}$ N., long. $112^{\circ} 6^{\prime}$ W. Joint XII on the after turret was 5.5 inches to port. During the three days that we lay in this bay the wind was so strong that the ship did not swing to the tide, but rode with her head constantly to the west.

As it is difficult to describe the land-marks here, the most convenient way of giving positions will be to refer them to the English Admiralty Chart, the position formerly occupied by Capt. Sir Edw. Belcher's observatory being taken to be lat. $24^{\circ} 38^{\prime} 18^{\prime \prime}$ N., long. $7^{\mathrm{h}} 28^{\mathrm{m}} 25^{\mathrm{s}} .4 \mathrm{~W}$., as given on the chart.

On June 8th a landing was effected at a spot on the beach, about a mile south of the position of Capt. Belcher's observatory, for the purpose of making a set of magnetic observations; but, after getting a time sight, it was found that there was a great deal of local attraction, nearly all the stones on the beach being magnetic, and consequently it was useless to attempt anything there. The approximate position of this spot is

```
Lat. 240 38' N.
Long. }\mp@subsup{7}{}{\textrm{h}}\quad2\mp@subsup{8}{}{\textrm{m}}2\mp@subsup{4}{}{\textrm{s}}\textrm{W}
```

On June 9th, after going to the extreme northern end of the bay, and pulling a short distance up a creek, a place was found which, upon careful examination by taking fore and back sights with a compass, seemed to be entirely free from all local attraction. The land there is composed of fine white-sand hillocks, which. are constantly being shifted by the wind, and are so loose that a man will sink halfway to his knees in walking over them. The only place where the surface was sufficiently solid to admit of the instruments being set up was below bigh-water mark, where the sand was wet. A complete set of magnetic observations were made there, which, however, were not as satisfactory as could have been wished, owing to the magnets being disturbed by a.stiff breeze which shook the instruments, and from which there was no shelter. The position of this station was

$$
\begin{array}{lrll}
\text { Lat. } & 24^{\circ} & 39^{\prime} & 36^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 7^{\mathrm{h}} & 28^{\mathrm{m}} & 26^{\mathrm{s}} .2 \mathrm{~W} .
\end{array}
$$

It was on the east side of the creek (on its left-hand bank), at a place where there is a sharp bend in its course, and can easily be found by plotting the position, given above, on the chart.

San Diego Bay, California. We were only in this harbor from 11 A.M. of June 15 th, 1866 , till 11 A. M. of June 16 th, and there was no time to swing the ship. However, during the afternoon of the 15 th a complete and very satisfactory set of magnetic observations were made on shore at a spot on the beach near the extreme southern end of the slightly rising ground at La Playa. The instruments were set up just above high-water mark, and nearly due east of the U.S. Coast Survey Astronomical Station. The true bearing of the light-house on Point Loma was S. $3^{\circ} 56^{\prime}$ W., and its distance exactly two statute miles in a direct line. The spot was tested for local attraction by taking fore and back sights with a compass, but none could be detected.

The position of the station, according to the U.S. Coast Survey Chart, was

$$
\begin{array}{lrll}
\text { Lat. } & 32^{\circ} & 41^{\prime} & 58^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 7^{\mathrm{h}} & 48^{\mathrm{m}} & 52^{\mathrm{s}} .6 \mathrm{~W} .
\end{array}
$$

San Francisco, California. The ship was swung in this harbor, on June 23d, 1866, in the usual manner. Her position at the time was lat. $37^{\circ} 48^{\prime}$ N., long. $122^{\circ} 22^{\prime}$ W. Joint XII on the after turret was 5.3 inches to port. While we were lying here the ship was swinging freely to the wind and tide.

The observations taken on shore June 26th were made on the sand beach in a cove on the east side of Yerba Buena Island, the instruments being set up just at high-water mark, and about one hundred and fifty feet north of a long pier which runs out over a mud flat. The place was tested for local attraction by taking fore and back sights with a compass, but none could be detected.

According to the U.S. Coast Survey Chart the position of this station was

$$
\begin{array}{lccl}
\text { Lat. } & 37^{\circ} & 48^{\prime} & 46^{\prime \prime} \mathrm{N} . \\
\text { Long. } & 8^{\mathrm{h}} & 9^{\mathrm{m}} & 22^{\mathrm{s}} .6 \mathrm{~W} .
\end{array}
$$

## SECTION III.

## ASTRONOMICAL OBSERVATIONS.

The observations contained in this section were all made on the sun, and are for the determination of latitude, local time, and true bearings. The instruments used were a prismatic sextant of six inches radius, by Pistor and Martins; a mercurial artificial horizon; and a pocket mean time chronometer, by Fletcher, marked number 906.

The index correction of the sextant was usually obtained by measuring the diameter of the sun, both on and off the arc. For determining the density of the atmosphere thermometers with Fahrenheit scales, and a mercurial barometer graduated to English inches, were employed.

The refractions have been computed by means of Bessel's tables, as given in Loomis' "Practical Astronomy;" from which book the tabular parts of the reductions to the meridian have also been taken. The necessary fundamental data have been obtained from the American Nautical Almanac.

Observations of circummeridian altitudes of the sun for latitude were made in sets of twelve, so arranged as to eliminate both the sun's semi-diameter, and all errors depending on the roof of the artificial horizon.

Circummeridian Altitudes of the Sun for Latitude, observed at the south front of Fort Christian, St. Thomas, November 17 th, 1865.



Circummeridian Altitudes of the Sun for Latitude, observed at Isle Royal, Salute Islands, November $28 t h, 1865$.


Observations for time were usually made in such a manner as to eliminate both the sun's semi-diameter and all errors which might be produced by the roof of the artificial horizon. For full details of the method see page 33 of the "Reports on Observations of the Total Eclipse of the Sun, August 7, 1869," published by the U. S. Naval Observatory, Washington.

The reduction of the observations for time has been effected by means of the following formulæ:

$$
\begin{gathered}
a=\frac{A+\omega}{2}-r+p \\
S=\frac{a+d+\phi}{2} \\
\sin \frac{1}{2} t=\sqrt{\sin (S-a) \cos S \sec \phi \operatorname{cosec} d} \\
d t=t+\tau-T
\end{gathered}
$$

$T=$ mean of observed chronometer times.
$A=$ mean of observed double altitudes.
$\omega=$ index correction.
$r=$ refraction.
$p=$ parallax .
$a=$ true geocentric altitude of sun's centre.
$d=$ sun's polar distance, measured from the elevated pole.
$\phi=$ latitude of place where observation is made.
$t=$ hour angle at the pole.
$\tau=$ equation of time.
$d t=$ correction of chronometer to reduce the reading of its face to local mean time.

Double Altitudes of the Sun, for Time, observed at the flagstaff in the Navy-yard at Portsmouth, Va., October 29 th, 1865.


Double Altitudes of the Sun for Time, observed at the flagstaff in the Navy-yard at Portsmouth, Va., October 29 th, 1865.


Ex. ther. $55^{\circ}$ At. ther. 79 Bar. 30.36 inches.
Refraction $=-170^{\prime \prime} .1 \quad$ Sun's declination - $13^{\circ} 40^{\prime} 42^{\prime \prime} .0$
Parallax $=+8.0$
Latitude $\quad+3^{6} \quad 49 \quad 32$.
Mean of observed double altitudes . . , . . $39^{\circ} 16^{\prime} 23^{\prime \prime} \cdot 3$
Local apparent time . . . . . . . . $3^{\mathrm{h}} 27^{\mathrm{m}} 5^{\mathrm{s}} .9$

Equation of time . . . . . . . .- $o^{h}{ } 6^{\mathrm{m}}{ }^{11^{8}} .6$
Local mean time . . . . . . . . 3 II 40.3
Mean of chronometer times . . . . . . 3 r6 20.4
Chronometer fast of local mean time . . . . . o 4 40.1
Longitude west .
$\begin{array}{lll}5 & 5 & 9.8\end{array}$
Chronometer slow of Greenwich mean time . . . 5 o 29.7
Double Altitudes of the Sun for Time, observed at Fort Christian, St. Thomas, West Indies, November 13 th, 1865.

| $9^{\mathrm{h}}$ | $\mathrm{o}^{\mathrm{m}}$ | $42^{\mathrm{s}} .5$ |
| :---: | :---: | :---: |
|  | I | 2 I .5 |
| 2 | 2 |  |
| 3 | 2.5 |  |
| 3 | 2.5 |  |
| 4 | 4 |  |
| 4 | 54 |  |
| 6 | 0.5 |  |
| 6 | 4 I |  |
| 7 | 10 |  |
| 7 | 10 |  |
| 7 | 54.5 |  |
| 8 | 2 II .5 |  |
| 8 | 48.5 |  |

$\left.\begin{array}{rrrr}84^{\circ} & 32^{\prime} & 50^{\prime \prime} \\ & 46 & 20 \\ & 57 & 30 \\ 85 & 16 & 50 \\ & 35 & 10 \\ 85 & 51 & 0 \\ 87 & 15 & 20 \\ 28 & 30 \\ & 37 & 0 \\ & 50 & 20 \\ & 59 & 20 \\ 88 & 7 & 0\end{array}\right\} 2 \underline{ }$ Index correction.


Correction $=+16^{\prime} \quad 18^{\prime \prime} .4$
Ex. ther. $84^{\circ}$
Refraction $=-57^{\prime \prime} \cdot 7$
Parallax $=+6.2$
At. ther. $86^{\circ}$
Bar. 30.12 inches.

$$
\begin{array}{llll}
\text { Sun's declination } & -18^{\circ} & 5^{\prime} & 2^{\prime \prime} \cdot 5 \\
\text { Latitude } & +18 & 20^{2} & 27 .
\end{array}
$$

Mean of observed double altitudes . . . . . $86^{\circ} 26^{\prime} 25^{\prime \prime} .8$
Local apparent time . . . . . . . . $10^{\mathrm{h}} \mathrm{I}^{\mathrm{m}} 20^{8} .0$
Equation of time . . . . . . . . - I5 3 I.2
Local mean time . . . . . . . . $94_{5} 48.8$
Mean of chronometer times . . . . . . $9 \quad 5 \quad 5.2$
Chronometer slow of local mean time . . . . 04043.6
Longitude west . . . . . . . . . 4
Chronometer slow of Greenwich mean time . . . 5 ○ 26.3
Double Altitudes of the Sun for Time, observed at Isle Royal, Salute Islands, November 28th, 1865.

| $8^{\text {h }} 47^{\text {m }}$ | $58^{8}$ | $109{ }^{\circ}$ |
| :---: | :---: | :---: |
| 48 | 35 | 110 |
| 49 | ${ }_{58}^{8}$ |  |
| 50 | 31 |  |
| 50 | 56.5 |  |
|  | 44.5 | 112 |
| 52 | 39.5 |  |
|  | i 3.5 |  |
|  | 47 |  |
|  | 19 | 113 |
| 54 | 53.5 |  |
| Ex. ther. $93^{\circ}$ |  |  |
| Refraction $=-36^{\prime \prime} \cdot 3$ |  |  |
|  | allax | 4.9 |


| $109^{\circ}$ | $58^{\prime}$ | $20^{\prime \prime}$ |  |
| :---: | :---: | :---: | :---: |
| 110 | 9 | 50 | 2 ¢ |
|  | 20 | $\bigcirc$ |  |
|  | 35 | 30 |  |
|  | 45 | 50 |  |
|  | 52 | 50 |  |
| 112 | 13 | $\bigcirc$ |  |
|  | 30 | - | $2 \bar{\square}$ |
|  | 40 | $\bigcirc$ |  |
|  | 50 | $\bigcirc$ |  |
| II 3 | $\bigcirc$ | $\bigcirc$ |  |
|  | 10 | $\bigcirc$ |  |

Index correction.


Ex. ther. $93^{\circ}$
Parallax $=+4.9$
At. ther. $85^{\circ}$
Bar. 30.13 inches.

Mean of observed double altitudes
Sun's declination - $21^{\circ} 23^{\prime} 30^{\prime \prime} .3$
Latitude $\quad+\begin{array}{lll} & 17 & 29 .\end{array}$
. . . . . $111^{\circ} 35^{\prime} 26^{\prime \prime} .6$
Local apparent time . . . . . . . . $10^{\mathrm{h}} 33^{\mathrm{m}} 31^{\mathrm{s}} .8$
Equation of time . . . . . . . . - II 43.8
Local mean time . . . . . . . . io 2148.0
Mean of chronometer times . . . . . . 8 5I 28.6

Chronometer slow of local mean time.
$\mathrm{I}^{\mathrm{h}} \quad 30^{\mathrm{m}} 19^{\mathrm{s}} .4$
Longitude west . . . . . . . . . $3 \quad 30$ 11.4
Chronometer slow of Greenwich mean time . . . 5 o 30.8

Double Altitudes of the Sun for Time, observed at Ceara, Brazil, December 13 th, 1865.

| $\mathrm{I}^{\text {in }} \mathrm{I} 5^{\text {m }}$ | $13^{8} \cdot 5$ | $\left.\begin{array}{ccc} 63^{\circ} & 0^{\prime} & 0^{\prime \prime} \\ 62 & 40 & 0 \\ & 20 & 0 \\ & 10 & 0 \end{array}\right\}$ |  |  | $\} 2 \bigcirc$ | Index correction. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 15 | 58.5 41 |  |  |  | $359^{\circ}$ | $1 \mathrm{I}^{\prime} \mathrm{O}^{\prime \prime}$ |  | $16^{\prime} 0^{\prime \prime}$ |
| 17 | $3 \cdot 5$ |  |  |  |  |  | 1050 |  | 10 |
| 17 | 26 | 62 | $\bigcirc$ | $\bigcirc$ |  |  |  | 1040 |  | $\bigcirc$ |
| 18 | 43 | 62 |  | 0 - |  |  |  |  |  |
| 19 | 5 |  |  | $\bigcirc$ |  | 359 | 1050.0 |  | $16 \quad 3 \cdot 3$ |
| 19 | 26.5 |  |  |  | $2 \bar{\odot}$ |  |  |  |  |
| 19 | 50 |  |  | $\bigcirc$ |  |  | Correctio | 16 | $33^{\prime \prime} \cdot 3$ |
| 20 | II. 5 |  |  | $\bigcirc$ |  |  |  |  |  |

Ex. ther. $84^{\circ}$
Refraction $=-89^{\prime \prime} \cdot 5$
Parallax $=+7.4$
At. ther. $82^{\circ} \quad$ Bar. 30.05 inches.

Mean of observed double altitudes . . . . . $62^{\circ} \mathrm{r} 8^{\prime} 0^{\prime \prime} .0$
Mean of chronometer times . . . . . . $\mathrm{I}^{\mathrm{h}} \mathrm{I} 7^{\mathrm{m}} 57^{\mathrm{s}} .8$
Equation of time . . . . . . . .- 520.9
Reducing this observation with latitude $=-3^{\circ} 43^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 29^{\mathrm{s}} .6$ slow of local mean time. Reducing it with latitude $=-3^{\circ} 44^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 32^{\mathrm{s}} .0$ slow of local mean time.

Double Altitudes of the Sun for Time, observed at Ceara, Brazil, December 14th, 1865.


Reducing this observation with latitude $=-3^{\circ} 43^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 33^{\mathrm{s}} .7$ slow of local mean time. Reducing it with latitude $=-3^{\circ} 44^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 30^{\mathrm{s}} .9$ slow of local mean time.

Double Altitudes of the Sun for Time, observed at Ceara, Brazil, December 14th, 1865.


Reducing this observation with latitude $=-3^{\circ} 43^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 30^{\mathrm{s}} .7$ slow of local mean time. Reducing it with latitude $=-3^{\circ} 44^{\prime} 15^{\prime \prime}$, we find the chronometer $2^{\mathrm{h}} 26^{\mathrm{m}} 33^{\mathrm{s}} .1$ slow of local mean time.

In order to determine both the latitude of Ceara and the error of the chronometer from the three observations which have just been given, we proceed as follows:

Comparing the error obtained on the afternoon of December 13th, with that obtained on the afternoon of December 14th, we find that the chronometer was losing 1.17 seconds per day; and this rate is independent of any small change in the adopted value of the latitude.

By means of this rate, reducing all the observed chronometer errors to $2^{\mathrm{h}} 26^{\mathrm{m}}$ P. M. December 14th, and then plotting them according to Sumner's method, we get for the place of observation

Latitude $\quad 3^{\circ} \quad 43^{\prime} \quad 59^{\prime \prime} \mathrm{S}$.
and for the chronometer,
Chronometer slow of local mean time . . . . . $2^{\mathrm{h}} 26^{\mathrm{m}} 32^{\mathrm{s}} .5$
Longitude west . . . . . . . . . 2346
Chronometer slow of Greenwich mean time . . . . 5 o 38.5
Double Altitudes of the Sun for Time, observed at Pernambuco, Brazil, December 23d, 1865 .


Ex. ther. $83^{\circ}$
Refraction $=-3^{\prime \prime} . \mathrm{I}$
Parallax $=+4.5$
Mean of observed double altitudes
Local apparent time.
Equation of time .
Local mean time . . . . . . . . io $8 \quad 32.3$


Double Altitudes of the Sun for Time, observed at Bahia, Brazil, December 27 th, 1865.


Ex. ther. $88^{\circ}$
Refraction $=-45^{\prime \prime} .9$
Parallax $=+5.7$
At. ther.
Bar.
Sun's declination - $23^{\circ} 19^{\prime} \quad 33^{\prime \prime} .8$

Mean of observed double altitudes . . . . . $98^{\circ} 40^{\prime} \mathrm{o}^{\prime \prime}$. o
Local apparent time . . . . . . . . $9^{\mathrm{h}} 14^{\mathrm{m}} 22^{\mathrm{s}} \cdot 5$
Equation of time . . . . . . . . + 127.3
Local mean time . . . . . . . . 9 15 49.8
Mean of chronometer times . . . . . . 653 43.0
Chronometer slow of local mean time . . . . 2226.8
Longitude west .
$\begin{array}{lll}2 & 34 & 0.5\end{array}$
Chronometer slow of Greenwich mean time $\quad$. $\quad 4 \quad 56 \quad 7 \cdot 3$
Double Altitudes of the Sun for Time, observed at the Light-house in Fort St. Antonio, Bahia, Brazil, December 29th, 1865.

Ex. ther. $84^{\circ}$
Refraction $=-22^{\prime \prime}$. 1
二十 3.3

At. ther.

| Bar. |  |  |  |
| :--- | :--- | :--- | :--- |
|  |  |  |  |
| Sun's declination | $-23^{\circ}$ | 1 $3^{\prime}$ | $31^{\prime \prime} . \mathrm{I}$ |
| Latitude | -I 3 | 0 | 55. |

Mean of observed double altitudes

- I $35^{\circ} 10^{\prime} 0^{\prime \prime} .0$

Local apparent time . . . . . . . . $1^{\mathrm{h}} 36^{\mathrm{m}} 25^{\mathrm{s}} \cdot 7$
Equation of time . . . . . . . . + 227.6
Local mean time . . . . . . . . $10 \quad 3853.3$
Mean of chronometer times . . . . . . 8. 16 49.7
Chronometer slow of local mean time . . . . 2223.6
Longitude west . . . . . . . . . 2436.9
Chronometer slow of Greenwich mean time . . . $4 \quad 56$ 10.5

Double Altitudes of the Sun for Time, observed at Rio Janeiro, Brazil, January 9th, 1866.

| $5^{\mathrm{h}} 13^{\mathrm{m}} 17^{\text {s }}$ | $\begin{array}{ccc} 47^{\circ} & 40^{\prime} & 0^{\prime \prime} \\ & 50 & 0 \end{array}$ |  | $359^{\circ}$ | Index correction. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| r3 39 |  |  | $10^{\prime} 40^{\prime \prime}$ | $0^{\circ} 16^{\prime}$ |  |
| $14 \quad 3.5$ | 48 ○ | $0{ }^{2} \times$ |  | 30 | 15 | 50 |
| $14 \quad 26.5$ | 10 | $\bigcirc$ |  |  |  |  |  |
| 1543 | $47 \quad 40$ | $\bigcirc$ | 359 | 1035.0 | - 15 | 55.0 |
| 168 | ${ }^{50}$ |  |  |  |  |  |
| 1629 | 48 ○ | $0\}^{20}$ |  | Correcti | $16^{\prime} 4$ |  |
| 1653 |  | $\bigcirc$ |  |  |  |  |



Mean of observed double altitudes . . . . . $47^{\circ} 55^{\prime} \quad 0^{\prime \prime} .0$ Local apparent time . . . . . . . . $7^{\mathrm{h}} 1 \mathrm{I}^{\mathrm{m}} 19^{3} .5$
Equation of time . . . . . . . . + $7 \quad 23.8$
Local mean time . . . . . . . . $7 \quad 18 \quad 43.3$

Mean of chronometer times . . . . . . 5 i5 4.9
Chronometer slow of local mean time . . . . . $2 \quad 3 \quad 38.4$
Longitude west . . . . . . . . . $25^{2} \quad 30.7$
Chronometer slow' of Greenwich mean time . . . $4 \quad 56$ 9.I

Double Altitudes of the Sun for Time, observed at Rat Island, harbor of Rio Janeiro, January 9th, $\mathbf{1} 866$.

| $7^{\mathrm{h}}$ | $27^{\mathrm{m}}$ | $0^{\mathrm{s}}$ | $108^{\circ}$ |
| :--- | :--- | :--- | :--- |
| 27 | 20 |  |  |
| 27 | 42.5 |  |  |
| 28 | 4.5 |  |  |
| 28 | 26.5 |  |  |
| 29 | 21 | 108 |  |
| 29 | 45 |  |  |
| 30 | 5 |  |  |
| 30 | 26.5 |  |  |
| 30 | 48 |  |  |
|  |  |  |  |
| Ex. ther. |  |  |  |
| Refraction |  |  |  |
| Parallax | $=-35^{\circ}$ |  |  |
|  | $=+5.1$ |  |  |

At. ther. $77^{\circ}$
Bar. 29.94 inches.
Refraction $=-39^{\prime \prime} .8$

Mean of observed double altitudes . . . . . $108^{\circ} 20^{\prime} 0^{\prime \prime} .0$
Local apparent time . . . . . . . . $9^{\mathrm{h}} 25^{\mathrm{m}} 0^{\mathrm{s}} .7$
Equation of time . . . . . . . . + 726.0
Local mean time . . . . . . . . $9 \quad 32 \quad 26.7$
Mean of chronometer times . . . . . . . $7 \quad 28 \quad 53.9$
Chronometer slow of local mean time . . . . $\quad 2 \quad 3 \quad 32.8$
Longitude west . . . . . . . . . $25^{2} 37.9$
Chronometer slow of Greenwich mean time . . . $4 \quad 56$

Double Altitudes of the Sun for Time, observed at Monte Video, Uruguay, January 18th, 1866.



Double Altitudes of the Sun for Time, observed on Rat Island, harbor of Monte Video, Uruguay, January 24th, $\mathbf{I} 866$.


Ex. ther. $74^{\circ}$
Refraction $=-62^{\prime \prime} \cdot 7$
Parallax $=+6.5$
At. ther.
Bar.
Sun's declination - $19^{\circ} \quad 6^{\prime} \quad 33^{\prime \prime} .8$
Latitude $\quad-34 \quad 53 \quad 18$
Mean of observed double altitudes . . . . . $82^{\circ} 10^{\prime} 0^{\prime \prime} . \mathrm{o}$
Local apparent time . . . . . . . . $3^{\mathrm{h}} 3^{0^{\mathrm{m}}} 5^{\mathrm{s}} \cdot 7$
Equation of time . . . . . . . . $\quad$ I2 29.2
Local mean time . . . . . . . . $34^{2} \quad 34.9$
Mean of chronometer times . . . . . . 2 I 8.4
Chronometer slow of local mean time . . . . I II 26.5
Longitude west . . . . . . . . . $3.44 \quad 52.9$
Chronometer slow of Greenwich mean time . . . 4

Double Altitudes of the Sun, for Time, observed at Sandy Point, in the Straits of Magellan, February 7th, 1866.


| Local mean time |  |  | ${ }^{\text {a }} 7^{\text {s }} .7$ |
| :---: | :---: | :---: | :---: |
| Mean of chronometer times | 10 |  | 39.6 |
| Chronometer slow of local mean time | - | 12 | 48.1 |
| Longitude west | 4 | 43 | 35. |
| Chronometer slow of Greenwich mean time | 4 | 56 | 23. |

Double Altitudes of the Sun for Time, observed near Valparaiso, Chile, March 2d, 1866.


Double Altitudes of the Sun for Time, observed in Valparaiso, Chile, March 29th, 1866.


Double Altitudes of the Sun for Time, observed in Valparaiso, Chile, April 7 th, 1866.

| $9^{\text {h }}$ | $36^{\text {m }}$ | $26^{8} \cdot 5$ |  |  | $0^{\prime \prime}$ ) |  | Index | ection. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 37 | 16.5 |  |  | $0\} 2 \bar{\odot}$ | $359{ }^{\circ}$ | $10^{\prime} 50^{\prime \prime}$ | $0^{\circ} 15$ |  |
|  | 38 | 9 |  | $\bigcirc$ | 0 - |  | 50 |  | 10 |
|  | 40 | 1. 5 | 77 | 30 | - ) |  | 50 |  | 10 |
|  | 40 | 53 |  |  | $0\} 2 \odot$ |  |  |  |  |
|  | 41 | 44.5 | 78 | - | $\bigcirc$ | 359 | 1050.0 | - I5 | 10.0 |
|  |  |  |  |  |  |  | Correction | $+17^{\prime}$ | ' .0 |



Double Altitudes of the Sun for Time, observed in Valparaiso, Chile, April 7 th, 1866.


Double Altitudes of the Sun for Time, observed in Valparaiso, Chile, April 14 th, 1866.

| $3^{\mathrm{h}} 50{ }^{\mathrm{m}} \quad 20^{\mathrm{s}} .5$ | $36^{\circ} 33^{\prime} \quad 0^{\prime \prime}$ | Index correction. |  |
| :---: | :---: | :---: | :---: |
| 5 I 1.5 | I5 ○ ${ }^{\circ}$ ¢ | $359^{\circ}$ 10 $0^{\prime} 40^{\prime \prime}$ | $0^{\circ} 14^{\prime} 50^{\prime \prime}$ |
| 5 I 39 | $\bigcirc 0$ | 40 | 45 |
| 537 | $36 \quad 30$ ○ | 45 | 50 |
| 5346 | $15 \bigcirc\}^{2} \odot$ |  |  |
| $54 \quad 24.5$ | $\bigcirc 0$ | 359 Iо 41.6 |  14 48.3 |
|  |  | Correction | $17^{\prime} \mathrm{I} 5^{\prime \prime}$. 0 |

Ex. ther. $65^{\circ}$
Refraction $=-\mathrm{I} 70^{\prime \prime} \cdot 3$
Parallax $=+8.1$

At. ther. $66^{\circ}$
Sun's declination Latitude -33 I 47

Mean of observed double altitudes . . . . . $36^{\circ} 15^{\prime} 0^{\prime \prime} .0$
Local apparent time . . . . . . . . $4^{\text {h }} 3^{\mathrm{m}} \mathrm{I}^{\mathrm{s} .2}$
Equation of time . . . . . . . . + o in.6
Local mean time . . . . . . . . 4 24.8
Mean of chronometer times . . . . . . $35^{2} \quad 23.1$
Chronometer slow of local mean time . . . . o II I.7
Longitude west . . . . . . . . . 446 45.7
Chronometer slow of Greenwich mean time . . . $4 \quad 57 \quad 47.4$

Double Altitudes of the Sun for Time, observed on the Island of San Lorenzo, near Callao, Peru, April 26th, 1866.


Ex. ther. $80^{\circ}$
Refraction $=-29^{\prime \prime} .2$.
Parallax $=+4.0$
At. ther.
Bar.

Mean of observed double altitudes . . . . . $123^{\circ} 15^{\prime} 0^{\prime \prime} .0$
Local apparent time . . . . . . . . $1 \mathrm{I}^{\mathrm{h}} \mathrm{I}^{\mathrm{m}} 33^{\mathrm{s}} \cdot 0$
Equation of time . . . . . . . . - ${ }_{2} 18.8$
Local mean time . . . . . . . . ir ro 14.2
Mean of chronometer times . . . . . . $11 \quad 21 \quad 27.7$
Chronometer fast of local mean time . . . . . o II 13.5
Longitude west . . . . . . . . . 509 9.1
Chronometer slow of Greenwich mean time . . . $4 \quad 57 \quad 55.6$
Double Altitudes of the Sun for Time, observed at Payta, Peru, May 7th, 1866.


| Ex. ther. | $78^{\circ}$ |
| :--- | :--- |
| Refraction | $=-90^{\prime \prime} .7$ |
| Parallax | $=+7.3$ |

At. ther. $80^{\circ}$
Bar. 30.06 inches.
Sun's declination $+16^{\circ} 50^{\prime} 46^{\prime \prime}$
Latitude

- $5 \quad 5 \quad 36$

Mean of observed double altitudes . . . . . $62^{\circ} 15^{\prime} 0^{\prime \prime} .0$
Local apparent time . . . . . . . . $8^{\text {h }} 19^{\mathrm{m}} 22^{8} \cdot 3$
Equation of time . . . . . . . .- 3 38.I
Local mean time . . . . . . . . 8 I5 44.2
Mean of chronometer times . . . . . . 842 26.1
Chronometer fast of local mean time . . . . . $0 \quad 26$ 4I.9
Longitude west . . . . . . . . . 52422.0
Chronometer slow of Greenwich mean time . . . 45740.1
Double Altitudes of the Sun for Time, observed on Flamenco Island, Panama Bay, May 14 th, 1866.


Ex. ther. $85^{\circ}$
Refraction $=-49^{\prime \prime} \cdot 5$
Parallax $=\mp 5.7$

At. iner. 85

| $85^{\circ}$ | Bar. | 30.10 inche |  |
| :--- | :--- | :--- | :--- |
| Sun's declination | $+18^{\circ}$ | $39^{\prime}$ | $49^{\prime \prime}$ |
| Latitude | +8 | 54 | $31^{1}$ |

$$
\text { Latitude } \quad+8543 \mathrm{I}
$$



Double Altitudes of the Sun for Time, observed at Acapulco, Mexico, May 30th, 1866.


Double Altitudes of the Sun for Time, observed in Magdalena Bay, Lower California, June 8th, 1866.


Ex. ther. $69^{\circ}$ At ther. $70^{\circ}$ Bar. 30.02 inches.

| Refraction | $=-46^{\prime \prime} .4$ |
| :--- | :--- |
| Parallax | $=+5 \cdot 4$ |


| Mean of observed double altitudes | . . |  | - |  |  | $30^{\prime}$ | $0^{\prime \prime} .0$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Local apparent time | - . | - | - |  | $2^{\text {b }}$ | $53^{\mathrm{m}}$ | $42^{\text {s }} \cdot 3$ |
| Equation of time | - - |  | - | . |  | 1 | 14.5 |
| Lucal mean time | - . | - | - |  | 2 | 52 | 27.8 |
| Mean of chronometer times |  | - | - |  | 5 | 22 | 32.2 |
| Chronometer fast of local mean time |  |  | - |  | 2 | 30 | 4.4 |
| Longitude west |  |  | - |  | 7 | 28 | 24.0 |
|  | time |  |  |  | 4 | 58 | 19.6 |

4 February, 1872.

Double Altitudes of the Sun for Time, observed at La Playa, San Diego Bay, California, June 15 th, 1866.


Ex. ther. $71^{\circ} \quad$ At. ther. $72^{\circ} \quad$ Bar. 30.12 inches.
Refraction $=-37^{\prime \prime} .4$
Parallax $=+4.7$
Sun's declination $+23^{\circ} 20^{\prime} 22^{\prime \prime}$

Mean of observed double altitudes . . . . . $112^{\circ} 15^{\prime} 0^{\prime \prime} .0$
Local apparent time . . . . . . . . $2^{\mathrm{h}} 27^{\mathrm{m}} 47^{\mathrm{s}} \cdot 3$
Equation of time . . . . . . . . + o ri. 3
Local mean time . . . . . . . . $22^{27} \quad 58.6$
Mean of chronometer times . . . . . . 5 I8 3I.I
Chronometer fast of local mean time . . . . . $2 \quad 50 \quad 32.5$
Longitude west . . . . . . . . . 748 52.6
Chronometer slow of Greenwich mean time . . . $4 \quad 58$ 20.I
Double Altitudes of the Sun for Time, observed on Yerba Buena Island, San Francisco Bay, California, June 26th, 1866.

| $\begin{array}{ll} 4^{\mathrm{h}} & \mathrm{I} 6^{\mathrm{m}} \\ & \mathrm{I} 7 \end{array}$ | $\begin{aligned} & 40^{8} \cdot 5 \\ & 18 \end{aligned}$ | $75^{\circ}$ |
| :---: | :---: | :---: |
| 17 | 55.5 | 75 |
| 19 | 18.5 |  |
| 19 | 54.5 |  |
| 2030 |  |  |
| Ex. ther. $67^{\circ}$ |  |  |
| Refraction |  | $72^{\prime \prime}$ |
| Parallax |  | 6. |




Refraction $=-72^{\prime \prime} \cdot 5$

Mean of observed double altitudes

$$
\begin{array}{llll}
\text { Sun's declination } & +23^{\circ} & 22^{\prime \prime} & 7^{\prime \prime} \\
\text { Latitude } & +37 & 48 & 4^{6}
\end{array}
$$

. . . . . $75^{\circ} 30^{\prime} \quad 0^{\prime \prime} . \mathrm{O}$
Local apparent time . . . . . . . . $8^{\mathrm{h}} 2^{\mathrm{m}} 58^{\mathrm{s}} .4$
Equation of time . . . . . . . . + ${ }_{2} 29.6$
Local mean time . . . . . . . . 8 28.0
Mean of chronometer times . . . . . . 4 I8 $\quad 36.2$
Chronometer fast of local mean time . . . . . 8 i3 8.2
Longitude west . . . . . . . . . $8 \quad 922.6$
Chronometer fast of Greenwich mean time . . . . o 345.6
The chronometer used in making this observation was T. S. and J. D. Negus' No. 1287 .
True bearings were determined by measuring with a sextant the angle between the sun's limb and some well-defined terrestrial object, the time being noted at the instant the angle was observed. If the terrestrial object was much elevated above the horizon its angular altitude was also measured. Knowing the latitude of the place of observation, the local time, and the sun's declination, the sun's zenith distance and true bearing were calculated. Then, having the zenith distance of the sun, the zenith distance of the terrestrial object, and the measured angle between the sun and the terrestrial object, the horizontal angle between them
was computed, and applying it to the sun's true bearing the true bearing of the terrestrial object at once became known.

The formulæ employed were as follows. Let
$T=$ mean of observed chronometer times.
$d t=$ correction of chronometer to reduce the reading of its face to local mean time.
$\tau=$ equation of time.
$t=$ sun's hour angle, or the apparent time.
$\Omega=$ mean of observed angular distances between the sun's limb and the terrestrial object.
$\omega=$ index correction of sextant.
$s=$ sun's semi-diameter.
$a=$ apparent zenith distance of sun's centre.
$b=$ zenith distance of terrestrial object.
$c=$ true angular distance between the sun's centre and the terrestrial object.
$C=$ horizontal angle included between the sun's centre and the terrestrial object.
$\phi=$ latitude of the place of observation.
$A=$ azimuth, or true bearing, of sun's centre.
$\zeta=$ true zenith distance of sun's centre.
$\delta=$ sun's declination.
$r=$ refraction due to apparent altitude of sun's limb.
$B=$ true bearing of terrestrial object.
Then we have

$$
\begin{aligned}
& t=T+d t+\tau \\
& \tan M=\frac{\tan \delta}{\cos t} \\
& \tan A=\frac{\tan t \cos M}{\sin (\phi-M)} \\
& \tan \zeta=\frac{\tan (\phi-M)}{\cos A}
\end{aligned}
$$

where $A$ is to be taken greater or less than $180^{\circ}$, according as $t$ is greater or less than $180^{\circ}$.

$$
\begin{aligned}
& a=\zeta-r \\
& c=\Omega+\omega+s
\end{aligned}
$$

If $b$ is exactly $90^{\circ}$, we have

$$
\cos C=\frac{\cos c}{\sin a}
$$

But if $b$ is either greater or less than $90^{\circ}$, we have

$$
\begin{gathered}
S=\frac{a+b+c}{2} \\
\tan \frac{1}{2} C=\sqrt{\frac{\sin (S-a) \sin (S-b)}{\sin S \sin (S-c)}}
\end{gathered}
$$

Finally

$$
B=A \pm C
$$

In a few instances true bearings were obtained by observing the sun when its apparent elevation above the horizon was equal to its diameter. In that case and then

$$
\begin{gathered}
\zeta=90^{\circ} \\
\cos A=\frac{\sin \delta}{\cos \phi}
\end{gathered}
$$

in which the azimuth will be north or south of the prime vertical according as the sun's declination is north or south.

Observations of the Sun, made October 31st, 1865, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Hampton Roads, Va.


Observations of the Sun, made November 18th, 1865, to determine the true bearing of the object used as an azimuth mark in swinging the ship at St. Thomas, West Indies.


Observations of the Sun, made Novem. er 28th, 1865, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Isle Royal, Salute Islands.


Observations of the Sun, made December 12 th, 1865 , to determine the true bearing of the object used as an azimuth mark in swinging the ship at Ceara, Brazil.


Observations of the Sun, made December 29th, 1865, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Bahia, Brazil.
When the sun's true zenith distance was about $90^{\circ}$, the angle between its nearest limb and a conspicuous tree was measured and found to be $31^{\circ} 38^{\prime}$, the tree being to the right of the sun.

$$
\phi=-\mathrm{I}_{2}{ }^{\circ} 59^{\prime} \quad \delta=-23^{\circ} \mathrm{I} 2^{\prime}
$$

True bearing of sun
. S. $66^{\circ} 9^{\prime} \mathrm{W}$.
$\angle$ Sun to tree . .

- $\quad 3^{\mathbf{r}} \quad 38$

Sun's semi-diameter

- $\quad 16$

True bearing of tree . . . . . . . N. 8ı 57 W.

Observations of the Sun, made January 7th, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Rio Janeiro, Brazil.


Observations of the Sun, made January 23d, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Monte Video, Uruguay.
Near sunset, when the true zenith distance of the sun was about $90^{\circ}$, the angle between its nearest limb and the Light-house on the Mount, on the west side of the harbor, was measured. The uncorrected reading of the sextant was $69^{\circ} 40^{\prime}$, and the sun was to the left of the Light-house.


True bearing of sun

- S. $66^{\circ} \mathrm{I} 3^{\prime} \mathrm{W}$.
$\angle$ Sun to Light-house .
- $\quad 70 \quad 13$
$\angle$ Hillock to Light-house
$34 \quad 18$
True bearing of hillock.
. N. $775^{2}$ W.
Observations of the Sun, made February 9th, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Sandy Point, in the Straits of Magellan.

|  |  | $\Omega$ | $\begin{array}{ll}119 & \\ & 15^{\prime} \\ 3^{2} \\ 42\end{array}$ |
| :---: | :---: | :---: | :---: |
| 7 <br> Chronometer slow <br> $\tau$ | $9 \quad 15 \quad 19$ |  | 11930 |
|  | - 1248 | $\omega$ | + 17 |
|  | 1430 | $s$ | + 16 |
| Apparent time | $\begin{array}{llll}9 & 1 & & 37\end{array}$ | $c$ | 1203 |
| $t$ | - $41^{\circ} 33^{\prime}$ | $\zeta$ | $50 \quad 32$ |
| $\delta$ | - 1437 | $r$ | - 1 |
| $\phi$ | - 53 II | $a$ | $50 \quad 3 \mathrm{I}$ |
| $M$ | - 19 14 | $b$ | 8934 |
| $\phi-M$ | $33 \quad 57$ | C | 13054 |
| True bearing of | . . |  | N. $56^{\circ} 20^{\prime}$ E. |
| $\angle$ Mount St. Felipe | - | - | 13054 |
| True bearing of | St. Felipe . | - | S. 714 W . |

Observations of the Sun, made April 2d, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Valparaiso, Chile.


Observations of the Sun, made April 27th, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at Callao, Peru.

| $T$ <br> Chronometer fast |  | Om 2 3 | $30^{8}$ 20 50 |  | $100^{\circ}$ IOI | $\begin{gathered} 50^{\prime} \\ 55 \\ \mathbf{I} \end{gathered}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 7 | 2 | 13 | $\Omega$ | 100 | 55 |
|  | $\bigcirc$ | 11 | I | $\omega$ | + | 17 |
|  |  | 2 | 27 | $\stackrel{ }{s}$ |  | - |
| Apparent time | 6 | 53 | 39 | $c$ | IOI | 12 |
| $t$ | - | $76^{\circ}$ | $35^{\prime}$ | $\zeta$ | 80 | 12 |
| $\delta$ |  | 13 | 51 | $r$ | - | 5 |
| $\phi$ | - | 12 | 3 | $a$ | 80 | 7 |
| $M$ |  |  | 44 | $b$ nearly | 90 |  |
| ¢-M $\|$ <br> 8 |  |  |  |  | IOI | 21 |
| True bearing of sun |  |  |  | - - | N. $73{ }^{\circ}$ | $26^{\prime} \mathrm{E}$. |
| $\angle$ Sun to flagstaff |  |  |  | . . | IoI | 2 I |
| $\angle$ Flagstaff to Light-house. |  |  |  | . - | 88 | 34 |
| True bearing of Light-house |  |  |  | - • | S. 83 | 2 I W. |

Observations of the Sun, made May 13 th, 1866 , to determine the true bearing of the object used as an azimuth mark in swinging the ship in Panama Bay, New Granada.

|  |  | I $7^{m}$ I 8 |  | $\Omega$ | $\begin{gathered} 86^{\circ} \quad 56^{\prime} \\ \quad 58 \end{gathered}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $T$ <br> Chronometer fast $\tau$ | 6 | 17 | 39 |  | 86 | 57 |
|  | $\bigcirc$ | 20 | 17 | $\omega$ | + | 17 |
|  | $+$ | 3 | 53 | $s$ |  | - |
| Apparent time(P.M.) | 6 | 1 | I 5 | $c$ | 87 | 14 |
| $t$ | $90^{\circ} \mathrm{I} 9^{\prime}$ |  |  | $\zeta$ | 86 | 54 |
| $\delta$ |  | 18 | 3 I | $r$ | - | 14 |
| $\phi$ |  | 8 | 55 | $a$ | 86 | 40 |
| $M$ |  | 89 | 3 | $b^{\prime}$ nearly | 90 |  |
| $\phi-M$ | - | 80 | 8 | $C$ | 86 | 14 |

$$
\begin{aligned}
& \text { True bearing of sun . . . . . . . N. } 7 \mathrm{I}^{\circ} 49^{\prime} \mathrm{W} \text {. } \\
& \angle \text { Peak to sun . . . . . . . . . } 87 \quad 14 \\
& \text { True bearing of Peak . . . . . . . S. } 20 \quad 57 \text { W. }
\end{aligned}
$$

Observations to determine the true bearing of the object used as an azimuth mark in swinging the ship in the harbor of Acapulco, Mexico.
When determining the magnetic declination with the portable declinometer, on May 30 th, $\mathbf{1 8 6 6}$, an observation of the sun with the theodolite gave N. $6^{\circ} 22^{\prime} \mathrm{E}$. as the true bearing of the gate of Fort St: Diego from the shore station. We then have

True bearing from station to Fort . . . . . N. $6^{\circ}{ }_{22^{\prime}} \mathrm{E}$.
L Monadnock to Fort

- $\cdot$. $\frac{26 \quad 54}{\mathrm{~N} .20 \quad 32 \mathrm{~W}}$.

True bearing from station to Monadnock

- S. $20^{\circ} 32^{\prime} \mathrm{E}$.

True bearing from Monadnock to station
$\angle$ Clump to station

- $\quad 87 \quad 45$

True bearing of clump . . . . . . . N. 7 I 43 E.

Observations of the Sun, made June 9th, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship in Magdalena Bay, Lowerer California.

Owing to a combination of unfortunate circumstances, the only available method of determining a true bearing was by observing with the solar compass, set up on the quarterdeck of the ship. In that way I found

$$
\text { True bearing of Peak . . . . . . . S. } 46^{\circ} 30^{\prime} \text { E. }
$$

which can only be considered as a near approximation to the truth.
Observations of the Sun, made June 23d, 1866, to determine the true bearing of the object used as an azimuth mark in swinging the ship at San Francisco, California.


The following triangulation was made for the purpose of determining the geographical position of some points in and about Ceara, Brazil. The angles were observed on December 14th, 15th, and 16th, 1865. Those between the Powhattan,

Monadnock, and Custom-house were not measured simultaneously, and as the two ships were riding at anchor with a considerable amount of chain out, it is probable that they shifted their positions after the angle at the Powhattan was measured, and before the angles at the Monadnock and Custom-house were taken. This will account for the excess of the sum of the three angles over $180^{\circ}$.

In the accompanying sketch the different points are designated as follows:

$$
\begin{aligned}
& A=\text { Point Macoripie Light-house. } \\
& B=\text { Northeast corner of Custom-house on the wharf. } \\
& C=\mathrm{U} . \text { S. Iron-clad Monadnock. } \\
& D=\mathrm{U} . \mathrm{S} . \text { Sloop of 'War Powhattan. } \\
& E=\text { most southern of the two steeples on the Church of the Conception. } \\
& F=\text { most southern of the two steeples on St. Joseph's Church. } \\
& M=\text { Magnetic and Astronomical Station of December 13th and 14th. }
\end{aligned}
$$



The observed angles were as follows:

| Angles at B. |
| :---: |
| $D$ to $A=55^{\circ}{ }^{12}{ }^{\prime}$ |
| $D$ to $C=84{ }^{17}$ |
| $F$ to $C=73 \quad 12$ |
| $E$ to $C=125$ |
| $E$ to $F=52 \quad 15$ |
| $A$ to $E=95$ |

*Angles at C.
$D$ to $A=55^{\circ} \mathrm{I}^{\prime}{ }^{\prime}$
$D$ to $A=36^{\circ} 19^{\prime}$
$D$ to $B=71 \quad 14$
Angles at D.
$D$ to $C=84 \quad 17$ $B$ to $F=42 \quad 28$
$A$ to $B=101^{\circ} 35^{\prime}$
$E$ to $C=125 \quad 6$
$\begin{array}{lr}E \text { to } F=52 & 15 \\ A \text { to } E=95 & 6\end{array}$
$B$ to $E=\mathbf{I} 540$

From these we obtain the following corrected

| Angles at B. | Angles at $C$. |  | Angles at $D$. |
| :---: | :---: | :---: | :---: |
| $A$ to $E=95^{\circ} \mathrm{Ir}^{\prime}$ | $D$ to $B=70^{\circ}$ |  | $A$ tc $B=10 \mathrm{I}^{\circ} 36^{\prime}$ |
| $E$ to $F=5^{2} \quad 9$ | $D$ to $A=36$ |  | $B$ to $C=2457$ |
| $F$ to $C=73 \quad 14$ | $A$ to $B=34$ | 44 |  |
| $C$ to $D=84 \quad 5$ | $B$ to $E=15$ |  |  |
| $D$ to $A=55 \quad 2 \mathrm{I}$ | $E$ to $F=26$ | 48 |  |

The Powhattan fired a salute, and, from the mean of seven observations, the interval between the flash and report, noted at $B$, was 6.55 seconds. External thermometer $86^{\circ}$. Hence the distance from $B$ to $D$ was 7526 feet.

Distance from $B$ to $M=200$ feet.
Azimuth from $M$ to $A=\mathrm{N} .{ }^{7} 75^{\circ} 38^{\prime} \mathrm{E}$.
Angle $A M B=128^{\circ} 57^{\prime}$.
From these data we find the distances between the several points as follows:

$$
\begin{aligned}
& A D=15814 \text { feet. } \\
& A C=2149 \mathrm{I} \\
& A B=18826 \\
& A M=18702
\end{aligned}
$$

$C E=4355$ feet.
$B C=3358$
$B F={ }_{251} 6$
$B E=1443$ feet.

Angle $B A M=0^{\circ} \quad 28^{\prime} \quad \mid \quad$ Angle $A M B={ }_{12} 8^{\circ} 57^{\prime} \quad \mid \quad$ Angle $A B M=50^{\circ} 35^{\prime}$

، $\quad \because \quad B$ to $A=\mathrm{N} .76 \quad 6 \mathrm{E}$.

$$
B \text { to } F=\mathrm{S} .43 \quad 26 \mathrm{~W}
$$

Assuming the position of $M$ to be

$$
\begin{array}{lllll}
\text { Lat. } & 3^{\circ} & 43^{\prime} & 59^{\prime \prime} . \circ \mathrm{S} \\
\text { Long. } & 2^{\mathrm{h}} & 34^{\mathrm{m}} & 6^{\mathrm{s}} .00 \mathrm{~W}
\end{array}
$$

we get finally

| Station. | Latitude. |  |  | Longitude. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $B$ | 3 | $43^{\prime}$ | $57^{\prime \prime} .8 \mathrm{~S}$. | $2^{\text {b }}$ | $34^{\text {m }}$ | $6^{\text {s }}$. 11 |
| $E$ | 3 | 44 | 12.0 | 2 | 34 | 5.97 |
| $F$ | 3 | 44 |  |  |  |  |
| A | 3 | . 43 | I3.3 | 2 | 33 | 54.10 |

For convenience of reference the results of the observations contained in this section, together with the chronometer comparisons made during the cruise, are here collected and appended.

Observed Latitudes.


Errors of Pocket Chronometer, Fletcher, No. 906.


This chronometer (Fletcher, 906) was habitually carried in my pocket. It was accidentally allowed to run down on the night of December 17th and 18th, 1865, and after remaining stopped twelve hours was wound and compared. Some time between $5^{\text {h }}$ P. M. of April 13th and $3^{\text {h }}$ P. M. of April 14th, 1866, it stopped for about $1^{\mathrm{m}} 37^{7 \text { s }}$, but started again of itself. On June 20 th, 1866 , when its face showed $6^{\mathrm{h}} 45^{\mathrm{m}} \mathrm{P}$. M. it stopped without any apparent cause, and, as it would not run again, it became useless.

In observing at San Francisco the box chronometer T. S. and J. D. Negus, No. 1287 was used. The observations on June 26th, 1866, showed it to be
$8^{\mathrm{h}} \quad 13^{\mathrm{m}} \quad 8^{\mathrm{s}} .2$ fast of local mean time;
and

$$
0^{1} \quad 3^{\mathrm{m}} \quad 45^{\mathrm{s}} .6 \text { fast of Greenwich mean time. }
$$

Chronometer Comparisons


Table showing the True Bearings of the various objects used as azimuth marks in swinging the $U . S$. Iron-clad Monadnock during her cruise from Philadelphia to San Francisco in 1865 and 1866.


## SECTION IV.

## OBSERVATIONS ON TERRESTRIAL MAGNETISM.

The observations of magnetic declination and force were made by means of the same instruments-a portable declinometer, and a transit theodolite.

The Declinometer, kindly lent by the U.S. Coast Survey, and marked D. 22, was originally constructed by Jones, of London, but had been altered in many particulars so as to make it more convenient for field use. It was provided with two collimator magnets which were hollow cylinders of steel, each $0 . \% 0$ of an inch in external diameter, and 0.58 of an inch in internal diameter. One of them, marked C. 32, was 3.92 inches long; while the other, marked S. 8, was 3.25 inches long. Each of these magnets carried in its south end a lens; and in its north end, at the solar focus of the lens just mentioned, a piece of plane glass on which was cut a scale of equal parts containing one hundred and seventy divisions, each division being equal to 0.00255 of an inch. Both magnets were provided with light sliding brass rings which were intended to be used for keeping them horizontal under great changes of magnetic declination, but the slight play which the magnets had in the stirrup was found quite sufficient for that purpose, and the rings were never employed. The same suspension was used during the whole of the observations. It consisted originally of six parallel fibres of unspun silk, each about nine inches long; but at Callao one of the fibres was accidentally broken, and after that the remaining five were used. The torsion circle, which formed part of the suspension apparatus, was 0.88 of an inch in diameter, divided to every three degrees, and read by means of a vernier to single degrees.

The Transit Theodolite, which perhaps might be more correctly called an altitude and azimuth instrument, was provided with a horizontal and a vertical circle, each five inches in diameter, and each reading by means of two opposite verniers to thirty seconds. The telescope had an object-glass with a clear aperture of one inch, and a focal length of about nine inches. It was provided with two eye-pieces; a direct one magnifying about twenty times, which was employed in almost all the observations; and a diagonal one of lower power, which was sometimes used for objects near the zenith. Both these eye-pieces had colored glasses for observing the sun. The system of wires in the focus of the object-glass was a simple rectangular cross, one wire being vertical, the other horizontal.

For the sake of convenience in setting up the instruments, and also for the perfect security which it affords against changes in the angular value of the divisions of the magnet scales depending upon changes in the distance between them and
the telescope, a special table was provided, which was mounted upon a tripod stand, and which carried both the declinometer and theodolite in a fixed and invariable position relatively to each other-the object-glass of the telescope being about three inches from the south end of the magnet.

Pocket Chronometer, Fletcher, No. 906, was always used to note time. Its errors have been already given in detail in Section III.

General remarks on the method of using the instruments. When observations were to be made the tripod stand was set up, and the table, having been placed upon it, was approximately levelled by the eye, and set, by means of a pocket compass, so that its longest side was nearly in the magnetic meridian, the end destined to carry the declinometer being to the north. In packing the declinometer for travelling, the glass suspension tube was never unscrewed from the magnet-box, but when the collimator magnet was lifted from the stirrup a cylinder of wood of the same size was at once substituted, and two pieces of wood, provided for the purpose, were slipped in, one from each side of the magnet-box. These pieces of wood completely filled up the box, and at the same time held the wooden cylinder securely between them in such a manner that it could neither break the suspension fibres, nor allow them to twist in the slightest. With this packing, after the suspension fibres were once thoroughly freed from torsion, they remained so, and it was not necessary to examine them whenever the instrument was used, but only at considerable intervals, thus saving much time in the field. The brass carriers for the deflecting magnet having been screwed, one on each end of the wooden bar, and the bar in its turn having been screwed to the bottom of the magnet-box, the declinometer was placed upon the table in such a position that its three levelling screws fitted into the cavities provided for their reception. Then the packing blocks were taken out of the magnet-box, and the wooden cylinder having been removed from the stirrup, the collimator magnet was put in its place, and left free to assume its proper direction. The magnet-box was next levelled. For that purpose the suspension fibres were used as a plumb line, and the box was assumed to be level when they were seen to hang in the axis of the suspension tube throughout its whole length. Finally, the magnet was made to hang nearly level by moving it a little endwise in its stirrup; its scale was placed horizontal, with the figures erect; it was shaded from the direct rays of the sun by covering the glass top of the box; the mirror was screwed to the back of the box and adjusted so as to illuminate the magnet scale properly; and a thermometer was placed inside the magnet-box. The theodolite was next placed in its proper position on the other end of the table and levelled; particular care being taken that the horizontal axis of the telescope was truly level-especially if the altitude of the sun was considerable. The telescope having been turned towards the magnet and adjusted so as to obtain distinct vision of its scale, the horizontal circle was firmly clamped in such a position that the vertical wire in the field of the telescope cut the magnet scale as nearly as possible at the magnetic axis. By means of the vertical circle the optical axis of the telescope was then placed truly level, and the final adjustment of the magnet for horizontality was
made by shifting it endwise in its stirrup till the scale was seen in the field of the telescope parallel to, and just in contact with, the horizontal wire.

When making my first observations considerable difficulty was experienced in getting a proper illumination of the magnet scale, but after some practice the following perfectly satisfactory plan was adopted. In cloudy weather the light of a white cloud was reflected into the magnet by means of the concave mirror. In clear weather the light of the blue sky, reflected from the mirror, was not sufficient, and it would not do to throw in the direct rays of the sun because of their heating power, which would certainly have led to the use of a wrong value of the magnetic moment; because the magnet would have been at a higher temperature than that shown by the thermometer in the box. Under these circumstances, in place of the mirror a piece of perfectly white paper was substituted, and the direct rays of the sun being allowed to fall upon it, it afforded a beautiful illumination of the magnet scale.

The copper damper, provided to slip into the magnet-box for the purpose of quieting the vibrations of the magnet, was never used. As the observations were all made in the open air, and as there was frequently wind enough to cause the instruments to vibrate perceptibly, the magnets seldom or never came to a state of absolute rest. Hence, the plan adopted to secure accurate readings of the scales was as follows. A screw-driver was slightly magnetized, and by approaching its south pole for an instant towards the south pole of the vibrating magnet, at a time when the magnet was moving towards the screw-driver, the arc of vibration was readily made quite small. Then, placing miy eye to the telescope, I read off, and called out to my assistant, the scale reading at the instant the magnet attained the limit of its excursion in the eastern direction, and again when it attained the limit in a western direction-in other words, the greatest and least readings of the scale were noted. Five complete vibrations were generally observed, thus giving three eastern and three western readings, and the mean of the six was assumed to be the reading which would have been obtained if the magnet had been in a state of perfect rest.

In order to preserve the magnetism of the collimator magnets, they were always packed in a vertical position, with that pole downwards which would be lowest in a dipping needle.

Absolute Declinations were observed as follows: The instruments having been set up and adjusted in the manner already explained, the long magnet, C. 32, was suspended in the magnet-box, the telescope pointed nearly to its magnetic axis, and the horizontal circle of the theodolite firmly clamped. Then, $1^{\circ}$. The horizontal limb of the theodolite was read. $2^{\circ}$. The magnet scale being erect-that is, the figures upon it being right side up-the point upon it cut by the vertical wire of the telescope was observed. $3^{\circ}$. The telescope remaining as before, the magnet scale was inverted-that is, the magnet was turned on its axis through $180^{\circ}$, so that the figures upon its scale were seen inverted-and the point upon it cut by the vertical wire was again noted. $4^{\circ}$. The horizontal circle was unclamped, a colored glass placed upon the eye-piece, and the telescope pointed so that its vertical wire was just in advance of the first limb of the sun. Then the horizontal circle
was clamped, the time of transit of the sun's first limb over the vertical wire noted, and the horizontal circle read. $5^{\circ}$. If the observation was made at a time of day when the sun's azimuth was changing tolerably rapidly, the telescope was not moved in azimuth at all, but, the reading of the horizontal circle remaining precisely as before, the sun was followed by moving the telescope in altitude, and the transit of its second limb was waited for and noted. If, however, the sun was changing its altitude much more rapidly than its azimuth then, in order to save time, the horizontal circle was unclamped, the telescope moved till its vertical wire was just in advance of the sun's second limb, the horizontal circle clamped, the time of transit of the sun's second limb over the vertical wire noted, and the horizontal circle read. $6^{\circ}$. The telescope of the theodolite was reversed in its $Y^{\prime}$ s. 7o. The transit of the sun's first limb over the vertical wire was observed, and the horizontal circle read. $8^{\circ}$. The transit of the sun's second limb over the vertical wire was observed, and the horizontal circle read. $9^{\circ}$. The colored glass was removed from the eye-piece of the telescope, and a reading of the magnet scale (which was still inverted) was taken. $10^{\circ}$. The magnet was revolved on its axis through $180^{\circ}$, so as to place the scale erect, and another reading of the scale was taken. $11^{\circ}$. The horizontal circle was read.

Immediately before, and immediately after, going through with the operations just described, the telescope should be pointed to some well-defined distant object, and the reading of the horizontal circle noted. By so doing a check is afforded against any accidental shift of the horizontal circle; and if the same station is occupied at another time, absolute declinations may be determined without again referring to the sun, thus rendering it possible to observe during cloudy weather.

In the instruments under consideration the reading of the horizontal circle of the theodolite increases from left to right; and in both the magnets, C. 32 and S. 8, when the scale is erect an increase of scale reading indicates a motion of the north end of the magnet towards the east.

Let
$\rho=$ reading of magnet, scale erect.
$\rho^{\prime}=$ reading of magnet, scale inverted.
$R^{\prime}=$ reading of horizontal circle of theodolite at the time the readings $\rho$ and $\rho^{\prime}$ were observed.
$d=$ value, in minutes of arc, of one division of the magnet scale.
$R^{\prime \prime}=$ reading of horizontal circle of the theodolite at the time of transit of sun's first limb over the vertical wire.
$R^{\prime \prime \prime}=$ reading of horizontal circle of the theodolite at the time of transit of sun's second limb over the vertical wire.
$\alpha=$ observed chronometer time of transit of sun's first limb over the vertical wire.
$\alpha^{*}=$ observed chronometer time of transit of sun's second limb over the vertical wire.
$d t=$ correction of chronometer to reduce the reading of its face to local mean time.
$\tau=$ equation of time.
$t=$ the sun's hour angle at the pole.
$\phi=$ latitude of the place of observation; positive when north of the equator.
$A=$ azimuth of sun's centre at the time of its transit over the vertical wire: the azimuth being counted from the south around by the west.
$\delta=$ sun's declination; positive when north.
Then we have

$$
\begin{aligned}
& t=\frac{\alpha+\alpha^{\prime}}{2}+d t+\tau \\
& \tan M=\frac{\tan \delta}{\cos t} \\
& \tan A=\frac{\tan t \cos M}{\sin (\phi-M)}
\end{aligned}
$$

where $A$ is to be taken greater or less than $180^{\circ}$ according as $t$ is greater or less than $180^{\circ}$.

$$
\text { Magnetic declination }=R^{\prime}+\frac{d}{2}\left(\rho-\rho^{\prime}\right)+A-180^{\circ}-\frac{R^{\prime \prime}+R^{\prime \prime \prime}}{2}
$$

in which the declination is east if its sign is positive; west if its sign is negative.
The reading of the magnetic axis of the magnet is

$$
\frac{1}{2}\left(\rho+\rho^{\prime}\right)
$$

which we will designate by $c$. It should be constant. Then, if at any station the magnet has only been observed with its scale erect, if $c$ is known the observation may be reduced by the formula

$$
\text { Magnetic declination }=R^{\prime}+d(\rho-c)+A-180^{\circ}-\frac{R^{\prime \prime}+R^{\prime \prime \prime}}{2}
$$

The following example shows fully the form employed in recording and reducing the observations.

Magnetic Declination.
Station, Acapulco, Mexico. Date, May 30, 1866. Portable Declinometer, D. 22. Magnet C. 32. Observer, Wm. Harkness.

| Circle readings. |  |  |  | Reading of magnet. |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Vernier |  | $12^{\circ} 23^{\prime} 30^{\prime \prime}$ | (1) Scale erect <br> (2) Scale inverted | $\begin{aligned} & 78^{d} \cdot o \\ & 80.3 \end{aligned}$ |
|  |  |  |  | $(\mathrm{I})-(2)=\Delta$ | - 2.3 |
|  |  |  |  | Transit of |  |
|  | Vernier |  | $\begin{array}{lll}75^{\circ} & 25^{\prime} & 30^{\prime \prime} \\ 74 & 55 & 30\end{array}$ | Ist limb <br> 2d limb | $\begin{array}{lll} 8^{\mathrm{h}} & 14^{\mathrm{m}} & 28^{\mathrm{s}} \\ & 15 & 28 \end{array}$ |
|  | Mean . | - | 75 10 30 | Mean | $8 \quad 14 \quad 58.0$ |

6 March, 1872.


Value of one division of magnet scale $=2^{\prime} .349$.
The telescope is direct when the vertical circle is on the left-hand side.
These observations were made before noon, and time was noted by chronometer Fletcher, 906 , which was $1^{\text {h }} 41^{\mathrm{m}} 22^{\mathrm{s}} .2$ fast of local mean time.

At the time the azimuth was observed, the reading of the horizontal circle, telescope direct, to distant referring mark was $10^{\circ} 23^{\prime} 30^{\prime \prime}$.

|  | Telescope direct. | Telescope reversed. |
| :---: | :---: | :---: |
| Equation of time $\begin{aligned} & t \text { (in time) } \\ & t \text { (in arc). } \\ & \delta . . . \end{aligned}$ | $\begin{array}{llll} & o^{\mathrm{h}} & 2^{\mathrm{m}} & 47^{\mathrm{s}} \cdot \mathrm{I} \\ -5 & 23 & 37 \cdot \mathrm{I} \\ -80^{\circ} & 54^{\prime} & 16^{\prime \prime} \\ +2 \mathrm{I} & 47 & 18\end{array}$ | $\begin{array}{lrr}  & \circ^{\mathrm{h}} & 2^{\mathrm{m}} \\ -57^{\mathrm{s}} \cdot \mathrm{I} \\ -5 & 20^{2} & 3 \mathrm{I} .6 \\ -80^{\circ} & 7^{\prime} & 54^{\prime \prime} \\ +2 \mathrm{I} & 47 & 19 \end{array}$ |
|  | $\begin{aligned} & 9.60177 \\ & 0.80111 \end{aligned}$ | $\begin{aligned} & 9.60178 \\ & 0.76602 \end{aligned}$ |
| Tan $M$ | 0.40288 | 0.36780 |
| $\stackrel{\dagger}{M}$. | $\begin{array}{llll}+16^{\circ} & 50^{\prime} & 3^{\prime \prime} \\ +68 & 25 & 21\end{array}$ | $\begin{array}{lll} +16^{\circ} & 50^{\prime} & 3^{\prime \prime} \\ +66 & 47 & 35 \end{array}$ |
| $(\bar{\phi}-M)$. | $\begin{array}{lll}-51 & 35 & \text { 18 }\end{array}$ | $\begin{array}{llll}-49 & 57 & 32\end{array}$ |
| Tan $t$. | 0.79562 | 0.75955 |
| $\operatorname{Cos} M$. | 9.56557 | 9.59556 |
| $\operatorname{Cosec}(\phi-M)$. | -.10592 | 0.11600 |
| $\operatorname{Tan} A$ | 0.46711 | 0.47111 |
| Circle reading to magnet . <br> $\Delta \times 1 / 2$ scale division. | 12 $2^{\circ} \quad 23.5$ $-\quad 2.7$ | $\begin{array}{r} 12^{\circ} \quad 28 . .^{\prime} \\ -\quad 4.8 \end{array}$ |
| Sun's azimuth . . . |  |  |
| Sum . . . . . . . | $263 \quad 30.7$ | $263 \quad 42.8$ |
| $180^{\circ}+$ circle reading to sun | 25510.5 | $255 \quad 2 \mathrm{I} .3$ |
| Magnetic declination . | $8 \quad 20.2$ E. | 8 2I.5 E. |

Observations of Vibrations were made as follows: The instrument having been set up and adjusted in the manner already explained, the long magnet, C. 32, was
suspended in the magnet-box; and the telescope having been pointed so that its vertical wire cut the magnet scale approximately at the magnetic axis, the horizontal limb of the theodolite was firmly clamped. Then, $1^{\circ}$. By quickly approaching and withdrawing the magnetised screw-driver the magnet was caused to vibrate horizontally through an arc extending to about twenty scale divisions on each side of the magnetic axis-that is, through a total arc of about $1^{\circ} 34^{\prime}$. The semi-arc of vibration being only $47^{\prime}$, no correction to the observed time of vibration was ever required on that account. $\quad 2^{\circ}$. My assistant having taken the chronometer, I placed my eye to the telescope, and at the instant the 80th division of the scale (which was very near the magnetic axis) crossed the vertical wire I cried "time," and my assistant noted the minute, second, and fraction of a second indicated by the chronometer. Still keeping my eye at the telescope, I counted the transits of the 80th division over the wire, calling the one at which time was noted 0 , the next 1 , the next 2 , and so on up to the 10th, when I again cried "time," and my assistant once more noted the minute, second, and fraction of a second indicated by the chronometer. The difference of these two chronometer times gave a value for the time of ten vibrations of the magnet which was correct within about half a second. However, to guard against mistakes, the process was always repeated a second or third time. $3^{\circ}$. The temperature indicated by the thermometer in the magnet-box was noted; and then putting my eye to the telescope, I read the scale at the instant the magnet attained the eastern extremity, and again when it attained the western extremity, of its arc of vibration. These were the "extreme scale readings." $4^{\circ}$. The chronometer employed was a pocket one, beating five times in two seconds. Taking it in my hand, I commenced counting its beats at some multiple of ten seconds. Then, holding it to my ear and still mentally counting the beats, I put my eye to the telescope and noted the beat, and fraction of a beat, at which the 80 th scale division crossed the vertical wire. For example, suppose the beat was taken up at the instant the chronometer indicated $10^{\mathrm{h}} 2^{\mathrm{m}} 10^{s}$, and counting the first succeeding beat 1 , the next 2 , and so on, suppose that the 80th division crossed the wire exactly at the 14th beat. Then, as 14.0 beats are equal to 5.6 seconds, the time of transit of the 80th scale division was $10^{\mathrm{h}} 2^{\mathrm{m}} 15^{\mathrm{s}} .6$. The time of transit thus obtained was recorded as the 0 vibration. Adding to it the time of making ten vibrations-before determined-the approximate time when the 10th vibration would be completed became known. Taking up the beat of the chronometer at the nearest even ten seconds before that time, I put my eye to the telescope and observed the time of transit of the 80th division at the completion of the 10 th vibration. In the same manner the time of completing the 20 th, 30 th, 40th, 50 th, 100 th, 150 th, 160 th, 170 th, 180 th, 190 th, and 200 th vibration was observed. Subtracting the time of completing the 0 vibration from the 150 th, the 10 th from the 160 th, \&c., there result six values of the time of making one hundred and fifty vibrations, from the mean of which a very accurate value of the time of making one vibration is obtained. It will not escape notice that when observing in the manner just described there is no risk of making a mistake of one vibration, because the magnet.must, at all subsequent transits, be moving in the same direction as at the first transit, while in order to make a mistake of one vibration it
would be necessary that it should be moving in the opposite direction. $5^{\circ}$. The extreme scale readings attained by the magnet at the eastern and western extremities of its arc of vibration were again observed; and then the thermometer in the magnet-box was read. $6^{\circ}$. The necessary observations for determining the coefficient of torsion of the suspension fibres were made. When the instrument was properly adjusted for observation the torsion circle always read $300^{\circ}$. With it remaining at that reading the arc of vibration of the magnet was reduced to four or five scale divisions (by means of the magnetized screw-driver) and then the scale was read. Next the torsion circle was turned backward one-quarter of a revolution, so as to make it indicate $210^{\circ}$, and the scale was again read. After that, the torsion circle was turned forward half a revolution (passing through the point $300^{\circ}$ ), so as to make it indicate $30^{\circ}$, and the scale was read. Finally, the torsion circle was turned backward one-quarter of a revolution, so as to make it indicate $300^{\circ}$, and the scale was once more read. Subtracting the second scale reading from the first, the second from the third, and the fourth from the third, gave three differences, which were added together and divided by four. The result was the number of scale divisions through which the magnet was deflected by a twist of ninety degrees in the suspension fibres.

Observations of Deflections were made as follows: The instruments having been set up and adjusted in the manner already explained, the short magnet, S. 8, was suspended in the magnet-box, and the telescope having been pointed so that its vertical wire cut the magnet scale approximately at its central division (not necessarily the magnetic axis) the horizontal limb of the theodolite was clamped firmly. Then, $1^{\circ}$. The time was noted. $2^{\circ}$. The thermometer inside the magnet-box was read. $3^{\circ}$. The long magnet C. 32 (which we will now call the deflecting magnet) was placed on the deflecting bar support, with its axis east and west, its centre on a level with and at a distance of two feet to the west of the suspended magnet, and its north end west; the vibrations of the suspended magnet were reduced to four or five scale divisions, by means of the magnetised screw-driver, and then its scale was read. $4^{\circ}$. The deflecting magnet (remaining in the same place on the deflecting bar support as before) was reversed end for end, so as to bring its north end east, and the scale of the suspended magnet was read. $5^{\circ}$. The reversals were repeated twice more, so as to give in all two scale readings with the north end of the deflecting magnet to the west, and two scale readings with it to the east. The mean of the two scale readings obtained with the north end of the deflecting magnet west, were subtracted from the mean of the two scale readings obtained with its north end east. The difference was twice the value of the angle of deflection, as resulting from observations made with the deflecting magnet west of the suspended magnet. $6^{\circ}$. The deflecting magnet was lifted from the deflecting bar support to the west, and placed on that to the east, of the suspended magnet; its distance from the suspended magnet being still two feet, and its north end being to the east, the scale of the suspended magnet. was read. $y^{\circ}$. The deflecting magnet (remaining in the same place on the eastern deflecting bar support) was reversed end for end, so as to bring its north end west, and the scale of the suspended magnet was read. $8^{\circ}$. The reversals were repeated twice more, so to give in all two
scale readings with the north end of the deflecting magnet to the east, and two scale readings with it to the west. From the mean of the two scale readings obtained with the north end of the deflecting magnet east, the mean of the two scale readings obtained with its north end west were subtracted. The difference was twice the value of the angle of deflection, as resulting from observations made with the deflecting magnet east of the suspended magnet. The mean between this result and that obtained from the observations with the deflecting magnet west of the suspended magnet, was adopted as the true value of twice the angle of deflection, with the deflecting magnet at a distance of two feet from the suspended magnet. $9^{\circ}$. The thermometer inside the magnet-box was read. $10^{\circ}$. The time was noted. $11^{\circ}$. All the observations just described were repeated with the deflecting magnet at a distance of two and a half feet from the suspended magnet. $12^{\circ}$. The torsion of the suspension fibres was determined, precisely as described under the head of "observations of vibrations."

Horizontal Force was calculated from the observations of vibrations and deflections by the following formulæ:
$T_{0}=$ observed time of one vibration of the magnet.
$T^{\prime \prime}=$ time of vibration, corrected for rate of chronometer and arc of vibration.
$T=$ time of vibration, corrected for rate of chronometer, arc of vibration, torsion force of the suspending thread, temperature, and induction.
$s=$ daily rate of chronometer. + when gaining, - when losing.
$\alpha, \alpha^{\prime}=$ semiarc of.vibration, at the beginning and end of the observation, expressed in parts of radius.
$\frac{H}{F}=$ ratio of the force of torsion of the suspending thread to the magnetic directive force.
$q=$ coefficient of the decrease of the magnetic moment of the magnet produced by an increase of temperature of $1^{\circ}$ Fah. (This is not constant for all temperatures, and the correction is more exactly expressed by a formula of the form - correction to $t^{\prime}=q\left(t^{\prime}-t\right)+q^{\prime}\left(t^{\prime}-t\right)^{2}$, where $t^{\prime}$ is the observed temperature, and $t$ an adopted standard temperature.)
$K=$ moment of inertia of the magnet, including its suspending stirrup and other appendages. (This is constant for the same magnet and suspension, but varies slightly with the temperature, owing to the expansion of the materials.)
$\pi=$ gatio of the circumference of a circle to its diameter $=3.14159$.
$\mu=$ coefficient of increase in the magnetic moment of the magnet produced by the inducing action of a magnetic force equal to unity of the English system of absolute measurement.
$r_{0}=$ apparent distance between the centres of the deflecting and suspended magnets in the observations of deflections.
$r=$ the same distance corrected for error of graduation and temperature. ( $r=r_{0}\left[1+0.00001\left(t^{\prime}-62^{\circ}\right)\right]+$ correction for scale error.)
$d=$ value, in minutes of arc, of one division of the magnet scale.
$u_{0}=$ observed angle of deflection, in scale divisions.
$u=$ angle of deflection, corrected for torsion force of the suspending thread.
$P=$ a constant depending upon the distribution of magnetism in the deflecting and suspended magnets.
$m=$ magnetic moment of the deflecting or vibrating magnet.
$X=$ horizontal component of the earth's magnetic force.
$\frac{m^{\prime}}{X^{\prime}}=$ value of $\frac{m}{\bar{X}}$ before the application of the correction $\left(1-\frac{P}{r^{2}}\right)$

$$
\left(1+\frac{H}{F}\right)=\frac{5400+v}{5400}
$$

where $v=$ the angle, expressed in minutes of arc, through which the suspended magnet is deflected by a twist of $90^{\circ}$ in the suspension thread.

$$
\begin{aligned}
T^{\prime} & =T_{0}\left(1-\frac{s}{86400}\right)\left(1-\frac{\alpha \alpha^{\prime}}{16}\right) \\
T^{2} & =T^{\prime 2}\left\{1+\frac{H}{F}\right\}\left\{1-\left(t^{\prime}-t\right) q\right\}\left\{1+\mu \frac{X^{\prime}}{m^{\prime}}\right\} \\
m X & =\frac{\pi^{2} K}{T^{2}} \\
u & =d u_{0}\left(1+\frac{H}{F}\right) \\
\frac{m^{\prime}}{\bar{X}^{\prime}} & =\frac{1}{2^{3}} r^{3} \tan u \\
\frac{m}{\bar{X}} & =\frac{m^{\prime}}{\bar{X}^{\prime}}\left(1-\frac{P}{r^{2}}\right) \\
m & =\sqrt{m X} \frac{m}{\bar{X}} \\
X & =\frac{m X}{m}
\end{aligned}
$$

In order to facilitate the finding of $\log$. $\tan u$, in the reduction of observations of deflection, the following table has been prepared. With the argument log. $u$ ( $u$ being expressed in minutes of arc) it gives the quantity (log. $\tan u-\log . u$ ), or, in other words, the quantity which it is necessary to add to log. $u$ in order to obtain log. $\tan u$. The arrangement of the table is such that the quantity (log. $\tan u-\log . u$ ) is to be added to the log. $u$ on the same line with it, or to any other log. $u$ less than the one on the line next below. For example, if it were required to find log. $\tan u$ corresponding to any log. $u$ from 8.0000 to 1.4340 , it would only be necessary to add 6.46373 to the given log. $u$.

| Log. $u$. | Log. $\tan u-$ Log. $u$. | Log. $u$. | Log. $\tan u-$ Log. $u$. |
| :---: | :---: | :---: | :---: |
| 8.0000 | 6.46373 | 2.1159 | 6.46394 |
| 1.434I | 6.46374 | 2.1261 | 6.46395 |
| I. 5957 | 6.46375 | 2.1358 | 6.46396 |
| 1.6874 | 6.46376 | 2.1452 | 6.46397 |
| 1.7517 | 6.46377 | 2.1541 | 6.46398 |
| 1.8014 | 6.46378 | 2.1626 | 6.46399 |
| 1.8414 | 6.46379 | 2.1708 | 6.46400 |
| 1. 8756 | 6.46380 | 2.1787 | 6.46401 |
| 1.9047 | 6.46381 | 2.1864 | 6.46402 |
| 1.9310 | 6.46382 | 2.1937 | 6.46403 |
| r. 9538 | 6.46383 | 2.2008 | 6.46404 |
| 1.9750 | 6.46384 | 2.2079 | 6.46405 |
| 1.9934 | 6.46385 | 2.2146 | 6.46406 |
| 2.0111 | 6. 46386 | 2.2209 | 6.46407 |
| 2.0274 | 6.46387 | 2.227 I | 6.46408 |
| 2.0426 | 6.46388 | 2.2332 | 6.46409 |
| 2.0565 | 6.46389 | 2.2393 | 6.46410 |
| 2.0700 | 6.46390 | 2.2453 | 6.46411 |
| 2.0824 | 6.46391 | 2.2509 | 6.46412 |
| 2.0941 | 6.46392 | 2.2565 | 6.46413 |
| 2.1055 | 6.46393 |  |  |

The following are specimens of the forms employed in recording and reducing the observations of vibrations and deflections.

Horizontal Intensity.
Observations of Vibrations.
Station, Acapulco, Mexico. Date, May 3oth, 1866. Magnet C. 32. Inertia ring No.
Chron. Fletcher 906, rate, $\mathrm{I}^{\mathrm{s}} .38$ losing on mean time.


Coefficient of torsion. Value of one scale div. $=2^{\prime} .349$

| Tor. cir. | Scale. | Diff's. | $\begin{aligned} & \mathrm{v}=8^{\prime} .0 \\ & 5400^{\prime}+\mathrm{v}^{\prime} \\ & 5400 \text { (ar. co.) } \\ & \qquad \mathrm{I}+\frac{\mathrm{H}}{\mathrm{~F}} \end{aligned}$ | Log's. |
| :---: | :---: | :---: | :---: | :---: |
| $300^{\circ}$ | $80^{\text {d }} .1$ | $3{ }^{\text {d }} .4$ |  |  |
| 30 | 83.5 | 3.4 6.8 |  | 3.73304 |
| 210 300 | 76.7 80.1 |  |  | 6.26761 |
| 300 |  |  |  | 0.00065 |
| Mean $=\mathrm{v}=3.40$ |  |  |  |  |

Horizontal Intensity.
Calculation.

$$
\mathrm{T}^{2}=\mathrm{T}^{\prime 2}\left(\mathrm{I}+\frac{\mathrm{H}}{\mathrm{~F}}\right)\left(\mathrm{r}-\left(\mathrm{t}^{\prime}-\mathrm{t}\right) \mathrm{q}\right)
$$

Observed time of 150 vibrations $=799^{\circ} .85$ Time of one vibration

$$
\begin{array}{rr}
= & 5.332 \\
= & .000 \\
= & 5.332
\end{array}
$$



* Ob's of deff'n. Date. May 3oth, 1866.

$\mathrm{t}=84^{\circ} .7 \quad$| $*_{\mathrm{m}}$ | 8.94854 |
| :---: | :---: |
| $\overline{\mathrm{X}}$ |  <br> mX <br> $\mathrm{m}^{2}$ <br> m |

The chronometer used in this observation was $\mathrm{I}^{\mathrm{h}} 4 \mathrm{I}^{\mathrm{m}} \quad 22^{\mathrm{s}} .2$ fast of local mean time.

Horizontal Intensity.
Observations of Deflections.
Station, Acapulco, Mexico. Date, May 30th, 1866. Mag. C. $3^{2}$ deflecting. Mag. S. 8 suspended. Observer, Wm. Harkness.



Horizontal Intensity.
Observations of Deflections.
Station, Acapulco, Mexico. Date, May 3oth, 1866. Mag. C. $3^{2}$ deflecting. Mag. S. 8 suspended. Observer, Wm. Harkness.


April, 1872.

The constants, peculiar to the portable declinometer D 22, were obtained as follows:

The Temperature Coefficients of the magnets were furnished by Mr. Chas. A. Schott, of the U. S. Coast Survey. They had been used with the instrument for some years, and I had no opportunity to redetermine them. They are as follows:

$$
\begin{array}{llll}
\text { For the magnet C } 32 & q=0.00020 \\
" \quad 6 \quad 6 & \mathrm{~S} 8 & q=0.00027
\end{array}
$$

In reducing the observations a correction was always applied to the magnetic moment of the magnet C 32 to reduce it to what it would have been if C 32 had had the same temperature as S 8 . Hence, the temperature coefficient of C 32 was the only one used, and in order to facilitate its application the following table was computed which furnishes the value of log. $\left[1-\left(t^{\prime}-t\right) q\right]$ with the argument $\left(t^{\prime}-t\right)$.

Correction of Magnet C. 32 for Temperature

| $\left(t^{\prime}-t\right)$ | Log. $\left[\mathrm{I}-\left(t^{\prime}-t\right) q\right]$ | $\left(t^{\prime}-t\right)$ | Log. $\left[\mathrm{I}-\left(t^{\prime}-t\right) q\right]$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $+\mathrm{I}^{\circ}$ | 9.9999 ${ }^{\text {I }}$ | $-1^{0}$ | 0.00009 | P. P. |  |
| $+2$ | 9.99983 | - 2 | 0.00017 |  |  |
| $+3$ | 9.99974 | -3 | 0.00026 |  |  |
| $+4$ | 9.99965 | - 4 . | 0.00035 | 0.1 0.2 | I |
|  |  |  |  | 0.3 | 3 |
| $+5$ | 9.99957 | $-5$ | 0.00043 | 0.4 | 4 |
|  |  |  |  | 0.5 | 4 |
| $+6$ | 9.99948 | - 6 | $0.0005^{2}$ | 0.6 | 5 |
|  |  |  |  | 0.7 | 6 |
| $+7$ | 9.99939 | -7 | 0.00061 | 0.8 | 7 |
| $+8$ | 9.99930 | -. 8 | 0.00069 | 0.9 | 8 |
|  | 9.9 ¢ |  |  |  |  |
| $+9$ | 9:99922 | -9 | 0.00078 |  |  |
| +10 | 9.99913 | -10 | 0.00087 |  |  |

The Value of One Division of the Magnet Scale was determined for each magnet in the following manner: The instruments having been set up and adjusted as usual, the magnet was suspended in the magnet-box, and the packing blocks (before described as being used to prevent the suspension fibres from being twisted when the instrument was packed for travelling) were inserted in such a manner as to hold it perfectly steady. Then, the magnet scale being horizontal, the vertical wire of the theodolite telescope was made to coincide with any convenient scale division, and the horizontal circle of the theodolite was read. Next, the vertical wire was made to coincide with some other scale division, and the circle was again read. The difference of the two circle readings, divided by the difference of the two scale readings, gave the angular value of one scale division.

The following are the observations in detail for each magnet:

Magnet C. 32.

| Date. | Circle Rea | dings. | Differences. |  |  | Scale | Diff's. | Value of <br> I Scale |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nov. ı6, 1865 | $4^{\circ} \quad 5^{\prime}$ | $15^{\prime \prime}$ |  |  |  | $50^{\mathrm{d}} .0$ | 100 ${ }^{\text {d }} 0$ |  |
| Nov. 16, 1865 | - 11 | 45 |  |  | 30 | $150.0$ | 100. 0 | $2 \cdot 335$ |
| Nov. ı6, 1865 | 46 | 45 |  |  |  | 50.0 |  |  |
| Nov. 16, 1865 | - II | 45 |  |  | $\bigcirc$ | 150.0 | 100.0 | 2.350 |
| Nov. ı6, 1865 | 10 | 45 |  |  | 30 | 75.0 |  |  |
| Nov. 16, 1865 | 10 | 15 |  |  | 30 | 125.0 | 50.0 | 2.350 |
| Nov. ı6, 1865 Nov. 16,1865 | $\begin{array}{rr}3 & 7 \\ 1 & 10\end{array}$ | 45 I 5 |  |  | 30 | $\begin{array}{r}75.0 \\ \hline\end{array}$ | 50.0 | 2.350 |
| Nov. ı6, 1865 Jan. 18, I 866 | $\begin{array}{ll}\text { I } & 10 \\ 5 & 36\end{array}$ | 15 15 |  |  | 3 | 125.0 50.0 | 50.0 | 2.350 |
| Jan. 18, 8866 | I 40 |  |  | 55 | 45 | 50.0 150.0 | 100.0 | 2.357 |
| Jan. ı8, 1866 | 4 | $\bigcirc$ |  | 57 | 30 | 75.0 | 50.0 | 2.350 |

Hence for the magnet $\mathrm{C}_{32}$, we have x scale division $=2^{\prime} .349 \pm 0^{\prime} .0020$.

Magnet S. 8.

| Date. | Circle Readings. |  | Differences. |  | Scale | Diff's. | Value of <br> I Scale |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Nov. 16, 1865 | $4^{\circ} \quad 9^{\prime}$ |  |  |  | $50^{\text {d }}$. 0 |  |  |
| Nov. 16,1865 | 35926 |  | $4^{\circ} 43$ | 15 | ${ }^{5} 50.0$ | 100 ${ }^{\text {d }}$. | 2.833 |
| Nov. 16, 1865 | 49 |  |  |  |  |  |  |
| Nov. 16, 1865 | $359 \quad 26$ |  | 443 |  | 150.0 | 100.0 | 2.832 |
| Nov. i6, 1865 | 258 | 45 |  |  |  |  |  |
| Nov. 16, 1865 | - 37 |  | 221 | 45 | 125.0 | 50.0 | 2.835 |
| Nov. 16, 1865 | 259 | $\bigcirc$ |  |  |  |  | 2.830 |
| Nov. 16, 1865 | - 37 | 30 | $2 \quad 21$ | 30 | 125.0 | 50.0 | 2.830 |
| Jan. 18, 1866 | $5 \quad 36$ | 30 |  |  | 50.0 | 100.0 | 2.842 |
| Jan. 18, 1866 | - 52 |  | 444 |  | 150.0 | 100.0 | 2.842 |
| Jan. 18, 1866 | 425 |  |  |  | 75.0 |  |  |
| Jan. 18, 1866 | 23 | 30 | 222 | $\bigcirc$ | 125.0 | 50.0 | 2.840 |

Hence, for the magnet $S$ 8, we have
I scale division $=2^{\prime} .835 \pm 0^{\prime} .0013$.
The Moment of Inertia, and its Temperature Coefficient, of the Magnet C 32, was determined as follows: Let,
$K_{\tau}=$ moment of inertia of the magnet, including its suspending stirrup and other appendages, at the temperature $\tau$.
$\Delta K=$ change in the value of $K$ corresponding to a change of temperature of $1^{\circ}$ Fah. in the magnet.
$K_{\tau}^{\prime}=$ moment of inertia of the inertia ring, at the temperature $\tau$.
$d_{i}=$ internal diameter of the inertia ring, expressed in feet, at the temperature $\tau_{0}$.
$d_{e}=$ external diameter of the inertia ring, expressed in feet, at the temperature $\tau_{0}$.
$\varepsilon=$ coefficient of expansion for a change of temperature of $1^{\circ} \mathrm{Fah}$. in the metal composing the inertia ring.
$W=$ weight of the inertia ring expressed in grains.
$t=$ time in which the magnet makes one vibration at the temperature $\tau_{0}$ (corrected for chronometer rate, arc of vibration, and torsion.)
$t^{\prime}=$ time in which the magnet, loaded with the inertia ring, makes one vibration at the temperature $\tau_{0}$ (corrected for chronometer rate, arc of vibration, and torsion)
Then

$$
\begin{gathered}
K_{\tau}^{\prime}=W\left[1+2 \varepsilon\left(\tau-\tau_{0}\right)\right]\left\{\frac{d_{i}^{2}+d_{e}^{2}}{8}\right\} \\
K_{\tau}=K_{\tau_{0}}^{\prime}\left(\frac{t^{2}}{t^{\prime 2}-t^{2}}\right)+\Delta K\left(\tau-\tau_{0}\right)
\end{gathered}
$$

The inertia ring used in making my observations was of bronze. Mr. Joseph Saxton, Assistant Superintendent of the Office of Weights and Measures, very obligingly measured and weighed it, with the following result:

$$
\begin{aligned}
& \text { Internal diameter }=2.385 \text { inches }=0.19875 \text { foot } \\
& \text { External diameter }=2.947 \text { inches }=0.24558 \text { foot } \\
& \text { Weight }=798.72 \text { grains }
\end{aligned}
$$

the temperature of the ring being ${ }^{7} 4^{\circ}$ Fah.
Hence, assuming the coefficient of expansion for an increase of temperature of $1^{\circ}$ Fah. in the metal of this ring to be 0.0000105 , we find by the formula given above

$$
K_{r}^{\prime}=9.9601+\left(\tau-50^{\circ}\right) 0.000209
$$

or

$$
\text { Log. } K_{\tau}^{\prime}=0.99827+\left(\tau-50^{\circ}\right) 0.0000091
$$

The following table contains all the times of vibration which were observed for the purpose of determining the moment of inertia of the magnet, together with the computation of the corresponding values of log. $K$ from them. The value of $t^{\prime}$ was always observed either immediately before, or immediately after, the corresponding value of $t$ which was to be used with it. This was done in order to have the temperature in both cases as nearly as possible the same, so that the correction necessary to reduce $t^{\prime}$ to the same temperature as $t$ was always very small. Then having a sufficient number of values of $K$, obtained from observations made at widely different temperatures, the value of $\Delta K$ was easily found.

| Date. | $\tau$ | Log. $t^{\prime 2}$ | Log. $t^{2}$ | Log. $\left(t^{\prime 2}-t^{2}\right)$ | $\log \cdot\left(\frac{t^{2}}{t^{2}-t^{2}}\right)$ | Log. $K^{\prime \prime}{ }_{\tau}$ | Log. $K_{\tau}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Oct. 28, 1865 | $\stackrel{\circ}{\circ} \mathrm{O}$ | 1.88210 | 1. 66424 | 1.47811 | 0.18613 | 0.99849 | т. 18462 |
| Nov. 16, 1865 | 87.7 | r. 72767 | r.50891 | 1.32504 | -. 18385 | 0.99862 | 1.18247 |
| Nov. 28, 1865 | 90.0. | 1.72835 | 1.51108 | 1. 32345 | 0.18763 | 0.99864 | r.I8627 |
| Dec. 13, 1865 | 89.5 | 1. 74459 | .1. 52673 | 1. 34060 | -.18613 | 0.99864 | ı.18477 |
| Dec. 27, 1865 | 98.0 | 1.76681 | I.548ı0 | 1.36412 | -. 18398 | 0.99872 | r. 18270 |
| Jan. 18, 1866 | 87.2 | 1. 77770 | 1.5592 | 1.37467 | 0.18458 | 0.99861 | 1.18315 |
| March i9, 1866 | 76.2 | I. 75849 | r.54IOI | r. 35391 | 0.18710 | 0.99851 | r.18561 |
| April In, 1866 | 74.0 | 1.75824 | 1. 54019 | r. 35454 | 0.18565 | 0.99850 | 1.18415 |
| May 30, 1866 | 84.7 | 1.6735 | 1. 45405 | 1.27196 | 0.18209 | 0.99859 | 1.18068 |
| Nov. 2, 1866 | 70.0 | I. 90424 | 1.68479 | 1. 50268 | 0.182II | 0.99846 | I. 18057 |
| Nov. 2, 1866 | 70.0 | I.90391 | 1.68450 | 1. 50229 | 0.1822I | 0.99846 | i. 18067 |
| Nov. 2, 1866 | 53.5 | 1. 92843 | 1. 70989 | 1. 52548 | 0.18441 | 0.99830 | 1.1827I |
|  | 79.5 |  |  |  |  |  | 1.18320 |

Let $K_{0}$ represent the mean of all the logarithms of $K$ in the above table; then

$$
K_{0}=1.18320
$$

at a temperature of ${ }^{7} 9^{\circ} .5$. Now, assuming

$$
\text { Log. } K_{\tau}=K_{0}+\left(\tau-79^{\circ} .5\right) \Delta K
$$

we have

$$
0=K_{0}-\log . K_{\tau}+\left(\tau-79^{\circ} .5\right) \Delta K
$$

and each value of log. $K_{\tau}$, given in the table above, will furnish one equation of condition for the determination of $\Delta K$, as follows: the absolute terms being in units of the fifth place of decimals.

| $0=-142-6.5 \Delta K$ | $0=-241-3 \cdot 3 \Delta K$ |
| :--- | :--- |
| $0=+73+8.2 \Delta K$ | $0=-95-5 \cdot 5 \Delta K$ |
| $0=-307+10.5 \Delta K$ | $0=+252+5.2 \Delta K$ |
| $0=-157+10.0 \Delta K$ | $0=+263-9.5 \Delta K$ |
| $0=+50+18.5 \Delta K$ | $0=+253-9.5 \Delta K$ |
| $0=+5+7.7 \Delta K$ | $0=+49-26.0 \Delta K$ |

From these equations of condition we obtain, by the method of least squares, the normal equation
whence

$$
0=-5856.2+1646.0 \Delta K
$$

$$
\text { Log. } \cdot \Delta K=0.55119
$$

$$
\Delta K=+3.56
$$

and finally
Log. $K_{\tau}=1.18320+\left(\tau-79^{\circ} .5\right) 0.0000356 \pm 0.000368$
or
Hence we have

$$
K_{\tau}=15.248+\left(\tau-79^{\circ} .5\right) 0.00125 \pm 0.0129
$$

or

$$
\pi^{2} K_{\tau}=150.49+\left(\tau-79^{\circ} .5\right) 0.01234
$$

$$
\text { Log. } \pi^{2} K_{\tau}=2.17750+\left(\tau-{ }^{7} 79^{\circ} .5\right) 0.0000356
$$

In order to facilitate the reduction of the observations of vibrations, the following table has been computed from the formula last given. It furnishes the value of log. $\pi^{2} K_{\tau}$ to the argument $\tau$.

| 4 | Log. $\pi^{2} K_{\tau}^{\prime}$ | P. P. |  |
| :---: | :---: | :---: | :---: |
| $50^{\circ}$ | 2.17645 | $\mathrm{I}^{\circ}$ | 4 |
|  |  | 2 | 7 |
| 60 | 2.17681 | 3 | II |
|  |  | 4 | 14 |
| 70 | 2.17716 | 5 | 18 |
|  |  | 6 | 21 |
| 80 | 2.17752 | 7 | 25 |
|  |  | 8 | 28 |
| 90 | 2.17787 | 9 | 32 |
| 100 | 2.17823 |  |  |

The Constant $P$, depending upon the distribution of the magnetism in the magnets C 32 and S 8, was determined by means of the formula

$$
P=\frac{A-A^{\prime}}{\frac{A}{r^{2}}-\frac{A^{\prime}}{r^{\prime 2}}}
$$

where
$A=$ value of $\frac{m^{\prime}}{X^{\prime}}$ determined from an observation of deflection with the deflecting magnet at the distance $r$ from the suspended magnet.
$A^{\prime}=$ value of $\frac{m}{X^{\prime}}$ determined from an observation of deflection with the deflecting magnet at the distance $r^{\prime}$ from the suspended magnet.
The following table contains all the observed values of $A$ and $A^{\prime}$, together with the computation of the corresponding values of $P$. The values of $A$ were obtained from deflections at a distance of 2.0 feet: those of $A^{\prime}$ from deflections at a distance of 2.5 feet.

| Date. |  | Log. $A$ | Log. $A^{\prime}$ | $\stackrel{\log }{\left(A-A^{\prime}\right)}$ | Log. $\frac{A}{r^{2}}$ | Log. $\frac{A^{\prime}}{r^{\prime 2}}$ | $\left(\begin{array}{c} \text { Log. } \\ \left(\frac{A}{r^{2}}-\frac{A^{\prime}}{r^{\prime}}\right) \end{array}\right.$ | Log. $P$ | $P$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| October | 30, 1865 | 9.1660 | 9.1669 | $6.4829 n$ | 8.5640 | 8.3711 | 8.1187 | $8.3643 n$ | -0.023I |
| November | I3, 1865 | 9.0084 | 9.0094 | $6.388 \mathrm{r} n$ | $8 . \dot{4} 063$ | 8.2135 | 7.9608 | $8.4274 n$ | 0.0268 |
| November | 16, 1865 | 9.0087 | 9.0088 | 5.1491n | 8.4067 | 8.2129 | 7.9629 | 7.1863n | 0.0015 |
| November | 28, 1865 | 9.0068 | 9.0078 | 6.3989n | 8.4047 | 8.2120 | $7 \cdot 9591$ | $8.4398 n$ | -0.0275 |
| December | 13, 1865 | 9.0234 | 9.0175 | 7.1527 | 8.42 I 3 | 8.2216 | 7.9879 | 9.1649 | +0.1462 |
| December | 23, 1865 | 9.0295 | 9.0317 | $6.7332 n$ | 8.4274 | $8.235^{8}$ | 7.9798 | 8.7534n | -0.0567 |
| December | 27, 1865 | 9.042 I | 9.0413 | 6.3230 | 8.4400 | 8.2454 | 7.9978 | 8.3252 | +0.0211 |
| January | 6, 1 866 | 9.0628 | 9.0633 | $6.0587 n$ | 8.4608 | 8.2674 | 8.0163 | $8.0424 n$ | -0.0110 |
| January | ı8, 1866 | 9.0531 | 9.0536 | 6.1399n | 8.45 II | 8.2578 | 8.0064 | 8.1335n | 0.0136 |
| February | 7, 1866 | 9.0486 | 9.0495 | $6 \cdot 375^{1} n$ | 8.4465 | 8.2536 | 8.0012 | 8.3739n | 0.0237 |
| March | 2, 1866 | 9.0328 | 9.0339 | $6.4250 n$ | 8.4308 | 8.2380 | 7.9852 | $8.4398 n$ | -0.0275 |
| March | 19, 1866 | 9.0350 | 9.0342 | 6.3106 | 8.4330 | 8.2383 | 7.9907 | 8.3199 | +0.0209 |
| March | 29, 1866 | 9.0347 | 90347 | 4.8740 | 8.4326 | 8.2388 | 7.9890 | 6.8850 | +0.0008 |
| April | 7, 1866 | 9.0367 | 9.0373 | 6.1551n | 8.4346 | 8.2414 | 7.9899 | 8.1652n | -0.0146 |
| April | 1ı, 1866 | 9.0356 | 9.0360 | 5.9295n | 8.4336 | 8.2401 | 7.9893 | $7.9402 n$ | 0.0087 |
| April | I3, 1866 | 9.0343 | 9.0368 | $6.785^{2 n}$ | 8.4323 | 8.2409 | 7.9842 | 8.8010 n | -0.0632 |
| April | 26, 1866 | 8.9902 | 8.9896 | 6.1515 | 8.3882 | 8.1937 | 7.9456 | 8.2059 | +0.0161 |
| May | 7, 1866 | 8.9680 | 8.9704 | 6.7188n | 8.3659 | 8.1745 | 7.9178 | 8.8010n | -0.0632 |
| May | 14, 1866 | 8.9468 | 8.9544 | 7.1930n | 8.3447 | 8.1585 | 7.8872 | $9.3058 n$ | . 2022 |
| May | 30, 1866 | 8.9468 | 8.9472 | $5.8890 n$ | 8.3448 | 8.1513 | 7.9004 | $7.9886 n$ | 0.0097 |
| June | 9, 1866 | 8.9775 | 8.9817 | $6.9669 n$ | 8.3754 | 8.1858 | $7 \cdot 9241$ | $9.0427 n$ | -0.1103 |
| June | -5, 1866 | 9.0376 | 9.0346 | 6.8666 | 8.4355 | 8.2387 | 7.9970 | 8.8697 | +0.074 |
| June | 26, 1866 | 9.0810 | 9.0826 | 6.6509n | 8.4790 | 8.2868 | 8.0324 | 8.6185n | -0.0415 |
| November | I, 1866 | 9.1991 | 9.1972 | 6.8414 | 8.5971 | 8.4014 | 8.1568 | 8.6847 | +0.0484 |

The indiscriminate mean of all the observations gives

$$
P=-0.0166 \pm 0.0088
$$

But Peirce's criterion for the rejection of doubtful observations throws out those of December 13 and May 14. Accordingly, excluding them, and taking the mean of all the others, there results

$$
P=-0.0155 \pm 0.0057
$$

and that value I have adopted. Hence, for $r=2.0$ feet, we have

$$
\log .\left(1-\frac{P}{r^{2}}\right)=0.00168
$$

and for $r=2.5$ feet

$$
\log .\left(1-\frac{P}{r^{2}}\right)=0.00108
$$

The Magnetic Moment of the Magnet C 32 was computed as follows: Observations of deflection were always taken at two different distances, viz., at 2.0 feet and at 2.5 feet. In general, the two values of $\frac{m}{X}$ thus obtained differed slightly from each other, and the mean of the two was assumed to be correct. This mean was combined with the value of $m X$, obtained from a set of vibrations observed on the same day, and thus $m$ was determined. In no case was more than one set of observations of deflections taken on any single day, but,in a few instances several sets of observations of vibrations were made. Under such circumstances, the mean of all the observed values of $m X$ was combined with the mean of the two values of $\frac{m}{X}$, and thus a single value of $m$ was deduced.

Let
$m_{\tau}=$ observed value of the magnetic moment at the temperature $\tau$.
$m=$ value of $m_{\tau}$ after being multiplied by $\left[1+\left(\tau-75^{\circ} .8\right) q\right]$, or, in other words, after being reduced to the temperature $75^{\circ} .8$ Fah.
$m_{0}=$ mean of all the observed values of $m$.
$\alpha=$ daily decrease in the value of log. $m$, expressed in units of the fifth decimal place.
$d=$ time in days at which $m$ is taken; $d$ being counted from March 7th, 1866.
The following table contains all the observed values of log. $m_{\tau}$, together with the computation from them of the final values of the same quantity. The column headed "days" gives the time in days counted from October 24th, 1865.

| Date. | $\tau$ | Log. $m_{\tau}$ | $\underset{\left[\mathrm{I}+\left(\tau-75^{\circ} .8\right) q\right]}{\text { Log. }}$ | Log. $m$ | Days. | Concluded Log. $m$ | Concluded <br> $\log . m_{\tau}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| October 24, 1865 | $\stackrel{\circ}{ }{ }^{\circ} \cdot$ | 9.84148 | 9.9984I | 9.83989 | $\bigcirc$ | 9.83990 | 9.84149 |
| October 30, 1865 | 58.7 | 9.84139 | 9.9985 I | 9.83990 | 6 | 9.83979 | 9.84 I 28 |
| November 13,1865 | $85 \cdot 5$ | 9.83908 | 0.00082 | 9.83990 | 20 | 9.8395 I | 9.83869 |
| November 16, 1865 | 87.7 | 9.83951 | 0.00104 | 9.84055 | 23 | 9.83945 | 9.8384 I |
| November 28, 1865 | 90.0 | 9.83773 | 0.0012 I | 9.83894 | 35 | 9.83922 | 9.8380 I |
| December 13,1865 | 89.5 | 9.83645 | 0.00117 | 9.83762 | 50 | 9.83893 | 9.83776 |
| December 23, 1865 | 87.2 | 9.83768 | 0.00100 | 9.83868 | 60 | 9.83873 | 9.83773 |
| December 27, 1865 | 98.0 | 9.83655 | -.00191 | 9.83846 | 64 | 9.83865 | 9.83674 |
| January 6, 1866 | 74.2 | 9.83915 | 9.99986 | 9.83901 | 74 | 9.83846 | 9.83860 |
| January 18, 1866 | 87.2 | 9.83666 | 0.00100 | 9.83766 | 86 | 9.83823 | 9.83723 |
| February 7, 1866 | 69.5 | 9.83783 | 9.99945 | 9.83728 | 106 | 9.83784 | 9.83839 |
| March 2, 1866 | 69.7 | 9.83831 | 9.99947 | 9.83778 | 129 | 9.83739 | 9.83792 |
| March 19, 1866 | 76.2 | 9.83618 | -. 00004 | 9.83622 | 146 | 9.83706 | 9.83702 |
| March 29, 1866 | 68.2 | 9.83780 | 9.99934 | 9.83714 | 156 | 9.83686 | 9.83752 |
| April 7, 8866 | 67.0 | 9.83861 | 9.99923 | 9.83784 | 165 | 9.83669 | 9.83746 |
| April II, 1866 | 74.0 | 9.83716 | 9.99984 | 9.83700 | 169 | 9.83661 | 9.83677 |
| April I3, 1866 | 65.7 | 9.83711 | 9.99912 | 9.83623 | 17 I | 9.83657 | 9.83745 |
| April 26, 1866 | 79.2 | 9.83626 | 0.00030 | 9.83656 | 184 | 9.83632 | 9.83602 |
| May 7, 1866 | 77.0 | 9.83670 | 0.00009 | 9.83679 | 195 | 9.83610 | 9.83601 |
| May I4, 1866 | 82.2 | 9.83448 | 0.00056 | 9.83504 | 202 | 9.83596 | 9.83540 |
| May 30, I866 | 84.7 | 9.83602 | 0.00078 | 9.83680 | 218 | 9.83565 | 9.83487 |
| June 9, i866 | 65.0 | 9.83662 | 9.99906 | 9.83568 | 228 | 9.83546 | 9.83640 |
| June 15, 1866 | 71.0 | 9.83493 | 9.99958 | 9.83451 | 234 | 9.83534 | 9.85576 |
| June 26, 1866 | 63.0 | 9.83548 | 9.99889 | 9.83437 | 245 | 9.83513 | 9.83624 |
| November 1, i866 | 66.2 | 9.83326 | 9.99916 | 9.83242 | 373 | 9.83263 | 9.83347 |
| Means | 75.8 |  |  | 9.83729 | IJ4 |  |  |

The mean of the quantities in the column headed $\tau$ is $75^{\circ} .8$. Accordingly, adding log. $\left[1+\left(\tau-75^{\circ} .8\right) q\right]$ to each log. $m_{\tau}$, we obtain the values of log. $m$ given in the table. Taking the mean of these values, and also the mean of the numbers in the column "days," we find that at 134 days, which corresponds to March 7th, 1866, the value of log. $\dot{m}$ was $9.83729=\log . m_{0}$. Then, assuming

$$
\text { Log. } m=\log \cdot m_{0}-\alpha d
$$

we have

$$
0=9.83729-\log . m-\alpha d
$$

and each value of log. $m$ furnishes an equation of condition for the determination of $\alpha$, as follows.


By the method of least squares we obtain the normal equation

$$
0=-397497+203965 \alpha
$$

Solving, we get

$$
\alpha=+1.9488
$$

## Hence

$$
\text { Log. } m=9.83729-0.0000195 d \pm 0.000090
$$

or

$$
m=0.68753-0.0000310 d \pm 0.000144
$$

From the first of these expressions the quantities in the column "concluded log. $m$ " were computed.

If, in the expression for log. $m$, given above, we introduce the correction for temperature, we obtain

$$
\text { Log. } m_{\tau}=9.83729-0.0000195 d-0.000087\left(\tau-75^{\circ} .8\right)
$$

by means of which the quantities in the column "concluded log. $m_{r}$ " were computed.

The probable error of a single observed value of log. $m$ is $\pm 0.000452$, and of a single observed value of $m$ it is $\pm 0.000 \% 19$.

Observations of Inclination were all made with a dip circle by Henry Barrow \& Co., of London. It was provided with two needles, marked A 1 and A 2, each 3.5 inches long, and having axles 0.016 of an inch in diameter. The distance between the agate planes on which they rested was 0.74 of an inch. By means of two microscopes, one opposite each end of the needle-each of which, assuming distinct vision to be obtained at a distance of ten inches, magnified 18 diametersthe inclination of the needle was referred to, and read off upon a vertical circle six inches in diameter, divided to half degrees, and reading by means of two verniers to single minutes. The pointing of the microscopes to the ends of the needle was
effected by means of a clamp and tangent screw. The horizontal circle of the instrument was four inches in diameter, divided to half degrees, and reading by means of one vernier to single minutes. It was provided with a clamp, but no tangent screw.

Readings of the position of the dipping needle were made as follows: In the field of view of each microscope was a plate of glass upon which was engraved three fine parallel lines, the middle one being intended to represent one of the two extremities of a diameter passing through a vertical circle described about the prolongation of the axle of the needle. The north microscope having been turned till the centre line in its field of view coincided with the north end of the needle, the vernier belonging to that microscope was read off, and recorded as the reading of the north end of the needle. Then the south microscope was turned till the centre line in its field of view coincided with the south end of the needle, and the vernier belonging to that microscope was read off, and recorded as the reading of the south end of the needle. In order to distinguish between the two microscopes the letter $N$ was scratched upon one of them, and that one was always, in all positions of the instrument, used to read the north end of the needle.

The instrument having been set up and levelled, before beginning to observe it was necessary to place the plane of the vertical circle in the magnetic meridian. At a few of the earlier stations this was accomplished as follows: The needle was placed on the agate planes, with the side on which the letters were marked facing the microscopes. Then $1^{\circ}$. The microscopes having been turned till they were nearly in a vertical line, the vernier of the lower one was set to $90^{\circ} 0^{\prime}$, and the vertical circle was moved in azimuth-so that its face (by which is meant the side on which the microscopes were) was south-till the lower end of the needle was bisected by the middle line in the lower microscope; the Y's were raised and lowered gently, and if the bisection of the needle was altered, it was corrected by turning the circle in azimuth. Then the horizontal circle was clamped and read off; and this reading was called A. $\quad 2^{\circ}$. The vernier of the upper microscope was set to $90^{\circ} 0^{\prime}$, and the horizontal circle having been unclamped, the vertical circle was moved in azimuth-its face still remaining south-till the upper end of the needle was bisected by the middle line in the upper microscope; the Y's were raised and lowered gently, and if the bisection of the needle was altered, it was corrected by turning the circle in azimuth. Then the horizontal circle was clamped and read off, and this reading was called B. $3^{\circ}$. The horizontal circle was unclamped, and turned in azimuth $180^{\circ}$, so as to bring the face of the instrument to the north, and then the $1^{\circ}$ and $2^{\circ}$ processes just described were repeated; thus giving two more readings of the horizontal circle, which were called C and D . Then

$$
\frac{A+B+C+D}{4}=E
$$

where $E$ is the division of the horizontal circle at which it was necessary to set the vernier in order that the plane of the vertical circle might be at right angles to 8 April, 1872.
the magnetic meridian. Therefore the vernier was set at $90^{\circ}+E$, and the plane of the vertical circle coincided with the magnetic meridian. However, it soon became evident that this process consumed too much time, and the following, which is quite as accurate and much more expeditious, was adopted: A fine line was marked permanently upon the top of the instrument parallel to the plane of the vertical circle; then, after the instrument had been levelled, but before the dipping needle had been placed upon the agate planes, a pocket compass, with a needle about one and a half inches long, was placed with its centre upon the fine line, and the vertical circle was turned in azimuth till the compass needle and line were parallel to each other. That being the case, the plane of the vertical circle was known to be in the magnetic meridian, and the horizontal circle was clamped and read off.

The following is the method which was adopted in making observations of dip: $1^{\circ}$. The agate planes, and those parts of the axle of the needle which would rest upon them, were carefully wiped with a piece of chamois leather (I have since seen reason to believe that a piece of cork would have answered the purpose better), and then the instrument was set up, levelled, and the plane of the vertical circle placed in the magnetic meridian by the process before described. $2^{\circ}$. The needle was secured upon a block, provided for the purpose, and magnetised by means of a pair of eight-inch bar magnets, in such a manner that its marked end acquired north polarity. It was considered to be saturated with magnetism when the bar magnets had been drawn from its centre to its extremities six times, the process being performed upon both of its sides, and then it was removed from the block and placed in position upon the agate planes, with its face (by which is meant that side upon which the letters were marked) towards the east. $3^{\circ}$. The plane of the vertical circle being in the magnetic meridian, with the face of the instrument towards the east, and the needle in position upon the agate planes, with its face also towards the east, the north and south ends of the needle were read. Let these readings be designated respectively as $\phi^{\prime}$ and $\phi^{\prime \prime} .4^{\circ}$. The needle was reversed upon the agate planes, so as to bring its face towards the west, and its north and south ends were read. Let these readings be designated respectively $\phi^{\prime \prime \prime}$ and $\phi^{T V}$. $5^{\circ}$. The horizontal circle was unclamped, the vertical circle turned in azimuth $1 \dot{8} 0^{\circ}$, so as to bring its face towards the west, and the horizontal circle again clamped. The face of the needle now being towards the east, its north and south ends were read. Let these readings be designated respectively as $\phi^{r}$ and $\phi^{\text {ri }}$. $6^{\circ}$. The needle was reversed upon the agate planes, so as to bring its face towards the west, and its north and south ends were read. Let these readings be designated respectively as $\phi^{\text {vII }}$ and $\phi^{\text {VIII }}$. $7^{\circ}$. The time was noted, and then the needle, having been removed from the agate planes, was placed upon the block provided for the purpose, and remagnetised in such a manner that its marked end acquired south polarity; after which it was again placed in position upon the agate planes, with its face towards the west, and its north and south ends were read. Let these readings be designated respectively as $\psi^{\prime}$ and $\psi^{\prime \prime}$. $8^{\circ}$. The needle was reversed upon the agate planes, so as to bring its face towards the east, and its north and south ends were read. Let these readings be designated respectively as $\psi^{\prime \prime \prime}$ and $\psi^{I V}$. $9^{\circ}$. The horizontal circle was unclamped, the vertical circle turned in azimuth $180^{\circ}$,
so as to bring its face to the east, and the horizontal circle again clamped. The face of the needle now being towards the west, its north and south ends were read. Let these readings be designated respectively as $\psi^{\nu}$ and $\psi^{v I}$. $\quad 10^{\circ}$. The needle was reversed upon the agate planes, so as to bring its face towards the east, and its. north and south ends were read. Let these readings be designated respectively as $\psi^{V I I}$ and $\psi^{V I I I}$.

At the first few stations each of the readings $\phi^{\prime}, \phi^{\prime \prime}, \phi^{\prime \prime \prime} \ldots \phi^{v I I I}, \psi^{\prime}, \psi^{\prime \prime}, \psi^{\prime \prime \prime} \ldots . \psi^{\text {vIII }}$, was repeated three times, the Y's being raised and lowered again between each repetition; but after some experience I became convinced that the increase of accuracy obtained by three repetitions, over that obtained by a single careful reading, was not sufficient to warrant the greatly increased expenditure of time, and accordingly the repetitions were abandoned.

The needle A 2 proved to be well balanced, and the observations made with it were therefore reduced by the usual formula, namely

$$
\begin{gathered}
\frac{\phi^{\prime}+\phi^{\prime \prime}+\phi^{\prime \prime \prime}+\phi^{I V}+\phi^{\nu}+\phi^{v I}+\phi^{v I I}+\phi^{v I I I}}{8}=\alpha \\
\frac{\psi^{\prime}+\psi^{\prime \prime}+\psi^{\prime \prime \prime}+\psi^{I V}+\psi^{r}+\psi^{v I}+\psi^{v I I}+\psi^{v I I I}}{8}=\beta \\
\theta=\frac{\alpha+\beta}{2}
\end{gathered}
$$

where $\theta$ is the magnetic inclination or dip.
The needle A 1 proved not to be well balanced, which was shown by the great difference between the values of $\alpha$ and $\beta$ obtaired with it in low magnetic latitudes; although they agreed well enough at places where the dip was large. An examination of all the observations showed that in every case

$$
\frac{\phi^{\prime}+\phi^{\prime \prime}+\phi^{V}+\phi^{V I}}{4}=\frac{\phi^{\prime \prime \prime}+\phi^{I V}+\phi^{V I I}+\phi^{V I I I}}{4}
$$

and

$$
\frac{\psi^{\prime}+\psi^{\prime \prime}+\psi^{V}+\psi^{V I I}}{4}=\frac{\psi^{\prime \prime \prime}+\psi^{I V}+\psi^{V I I}+\psi^{V I I I}}{4}
$$

at least within about one degree. It therefore followed that, although the centre of gravity of the needle did not lie in its axle, it did lie somewhere in the line joining the two extremities of the needle and passing through its axle. In such cases we have

$$
\tan \theta=\frac{\tan \alpha+\tan \beta}{2}
$$

and by that formula all the observations made with this needle were reduced.
At St. Thomas some observations of dip were made with the plane of the vertical circle out of the magnetic meridian. They were reduced by the formula

$$
\tan \theta=\tan \theta^{\prime} \cos \alpha
$$

where $\theta$ is the true dip, and $\theta^{\prime}$ the dip observed with the vertical circle in a plane whose azimuth, measured from the magnetic meridian, was $\alpha$.

The values of the Vertical and Total Force have been computed from the horizontal force and inclination by the formulæ

$$
\begin{aligned}
& Z=X \tan \theta \\
& R=X \sec \theta
\end{aligned}
$$

where

$$
\begin{aligned}
& X=\text { horizontal component of the earth's magnetic force. } \\
& Z=\text { vertical component of the earth's magnetic force. } \\
& R=\text { total magnetic intensity. } \\
& \theta=\text { magnetic inclination. }
\end{aligned}
$$

All values of force are expressed in English units; namely, in terms of grains, feet, and seconds. If it is desired to have them in metric units, expressed in terms of milligrams, millimeters, and seconds, they must be multiplied by 0.46108 .

The observations of magnetic declination, inclination, and force are given in full at the end of this section, but for convenience of reference the following abstract of them is inserted here.

| Station. | Date. | Declination. | Inclination. |  | Log. $\frac{m}{X}$ | Log. $m X$ | Temp. | $X=$ <br> Hor. Force |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | Needle A. r. | Needle A. 2. |  |  |  |  |
| Philadelphia, Pa. | Oct. 24, 1865 | ...... | ...... | ... .. | 9.22363 | 0.45934 | 57.5 | 4.148 |
| Gosport, Va. | Oct. 28, 1865 |  |  |  |  | 0.51303 | 73.0 | 4.709 |
| Gosport, Va. | Oct. 30, 1865 | $2^{\circ} 37^{\prime} .8 \mathrm{~W}$. | $+69^{\circ} 21^{\prime}$ | $+69^{\circ} 54^{\prime}$ | 9.16787 | 0. 51492 | 58.7 | 4.717 |
| St. Thomas, | Nov. 13, 1865 | 39.6 | $+4936$ | +49 32 | 9.01026 | 0.66791 | 85.5 | 6.749 |
| St. Thomas, | Nov. 16, 1865 | - 39.6 E. | +4939 | +49 44 | 9.01014 | 0.66888 | 87.7 | 6.768 |
| Salute Islands, | Nov. 28, 1865 | - 3.8 W . | +34 27 | +34 42 | 9.00868 | 0.66679 | 90.0 | 6.742 |
| Ceara, | Dec. 13, 1865 | $8 \quad 28.8$ W. | +21 26 | +2120 | 9.02178 | 0.65112 | 89.5 | 6.507 |
| Pernambuco, | Dec. 23, 1865 | 10 59.6 W . | +126 | +18 10 | 9.03195 | 0.64340 | 87.2 | 6.392 |
| Bahia, | Dec. 27, 1865 | 7 56.6 W. | + 431 | + 417 | 9.04305 | 0.63005 | 98.0 | 6.213 |
| Rio Janeiro, | Jan. 6, 1866 |  | -II 48 | -II 46 | 9.06444 | 0.61386 | 74.2 | 5.960 |
| Rio Janeiro, | Jan. 9, 1866 | 24 I .8 W. |  |  | ...... | 0.61205 | 80.5 | 5.944 |
| Monte Video, | Jan. 18, 1866 | $9 \quad 16.6 \mathrm{E}$. | -31 11 | -30 58 |  | 0.61892 | 87.2 | 6.049 |
| Monte Video, | Jan. 18, 1866 | ...... | ...... | -3I 8 | 9.05476 | 0.61822 | 87.2 | 6.039 |
| Monte Videoo, | Jan. 19, 1866 | $9 \quad 25.0 \mathrm{E}$. |  |  |  | 0.61754 | 89.5 | 6.033 |
| Sandy Point, | Feb. 7, 1866 | $2 \mathrm{I} \quad 52.0 \mathrm{E}$. | -54 $5^{2}$ | $-55 \quad 2$ | 9.05044 | 0.62523 | 69.5 | 6.121 |
| Valparaiso, | March 2, 1866 | 15 54.3 E. | -34 50 | -35 7 | 9.03474 | 0.64188 | 69.7 | 6.367 |
| Valparaiso, | March 19, 1866 | 15 36.6 E. | -35 28 | -35 28 | 9.03599 | 0.63637 | 76.2 | 6.300 |
| Valparaiso, | March 29, 1866 | I5 54.8 E. | -35 34 | -35 27 | ...... | 0.64126 | 68.2 | $6 \cdot 364$ |
| Valparaiso, | March 29, 1866 | ….. | ...... |  | 9.03607 | 0.63782 | 68.2 | 6.314 |
| Valparaiso, | April 7, 1866 | I5 49.4 E. | -35 26 | -35 23 | 9.03837 | 0.63885 | 67.0 | 6.330 |
| Valparaiso, | April 11, 1866 | 15 57.6 E. | -35 29 | -35 36 | ...... | 0.63697 | 74.0 | 6.312 |
| Valparaiso, | April II, 1866 | ... | ...... | ...... | 9.03720 | 0.63725 | 74.0 | 6.317 |
| Valparaiso, | April 13, 1866 | $15 \quad 53.9 \mathrm{E}$. | -35 40 | -35 12 | 9.03692 | 0.63730 | 65.7 | 6.307 |
| Callao, | April 26, 1866 | IO 29.6 E. | -6 28 | -6 29 | 8.99132 | 0.68120 | 79.2 | 7.001 |
| Payta, | May 7, 1866 | 8 53.0 E. | + 59 | + 447 | 8.97055 | 0.70285 | 77.0 | $7 \cdot 359$ |
| Panama Bay, | May 14, 1866 | $5 \quad 55.8 \mathrm{E}$. | +32 5 | +3147 | 8.95196 | 0.71700 | 82.2 | 7.614 |
| Acapulco, | May 30, 1866 | $8 \quad 20.8$ E. | +39 49 | +39 58 | 8.94841 | 0.72363 | 84.7 | 7.740 |
| Acapulco, | May 30, I866 | $8 \quad 23.6 \mathrm{E}$. | - |  | ...... | … | 6 | 7.7 |
| Magdalena Bay, | June 9, 1866 | Io 40.5 E . | +48 41 | +48 22 |  | 0.69240 | 65.0 | 7.178 |
| Magdalena Bay, | June 9, 1866 | ...... |  |  | 8.98098 | 0.69211 | 65.0 | 7.173 |
| San Diego Bay, | June 15, 1866 | I3 9.4 E. | +57 51 | +5756 | 9.03746 | 0.6324I | 71.0 | 6.261 |
| San Francisco Bay, | June 26, 1866 | $16 \quad 25.5 \mathrm{E}$. | +62 13 | +6231 | 9.08320 | 0. 58777 | 63.0 | 5.643 |
| Washington, D. C. | Nov. I, 1866 | 2 44.2 W. | +7151 | +72 13 | 9.19956 | 0.46695 | 66.2 | 4.300 |
| Washington, D. C. | May 6, 1867 | ...... | +71 55 | +72 5 | ...... | ...... | ...... | ...... |

Taking the means we obtain the final values of the magnetic elements at each station, as follows:

| Station. | Latitude. |  | Date. | Declination. | $\left\lvert\, \begin{aligned} & \dot{0} \\ & \hline 0 \\ & 0 \\ & 0 \\ & 0 \\ & \dot{8} \\ & \dot{Z} \end{aligned}\right.$ |  | clinati | tion. | $\begin{gathered} \dot{0} \\ 0 \\ 0 \\ 0 \\ 0 \\ 0 \\ \dot{\circ} \\ \dot{8} \\ \hline \end{gathered}$ |  |  | u 0 0 4 0 0 $z$ |  |  | - |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Philadelphia, Pa. | $39^{\circ} 5^{\prime \prime} \mathrm{N}$. | $75^{\circ} 7^{\prime}$ | Oct. 24, 1865 | - , |  |  | $\bigcirc$ | , |  |  | 4.148 | 1 |  |  |  |
| Gosport | $36 \quad 49 \mathrm{~N}$. | $76 \quad 17$ | Oct. 29, 1865 | $2 \quad 37.8 \mathrm{~W}$. | I |  | +69 | 38 | 2 |  | 4.713 | 2 |  | 12.696 | 13.542 |
| St. Thomas | $18 \quad 20 \mathrm{~N}$. | $64 \quad 55$ | Nov. 14, 1865 | - $\quad 39.6 \mathrm{E}$. | I |  | +49 | 38 | 4 |  | 6.758 | 2 |  | 7.950 | 10.434 |
| Salute Islands | $\begin{array}{llll}5 & 17 & \mathrm{~N} .\end{array}$ | 5233 | Nov. 28, 1865 | - 3.8 W . | I |  | +34 | 35 | 2 |  | 6.742 | 1 |  | 4.648 | 8.189 |
| Ceara | 3 lll S. | $38 \quad 31$ | Dec. 13, 1865 | $8 \quad 28.8$ W. | I |  | +21 | 23 | 2 |  | 6.507 | 1 |  | 2.548 | 6.988 |
| Pernambuco | 8: 4 S . | $34 \quad 52$ | Dec. 23, 1865 | 1o 59.6 W . | I |  | -12 | 8 | 2 |  | 6. 392 | 1 |  | 1.374 | 6.538 |
| Bahia | $12 \quad 57 \mathrm{~S}$. | $38 \quad 30$ | Dec. 27, 1865 | $7 \quad 56.6 \mathrm{~W}$. | I |  | + 4 | 24 | 2 |  | 6.213 | 1 |  | 0.478 | 6.231 |
| Rio Janeiro | $22 \quad 54 \mathrm{~S}$. | 438 | Jan. 8, 1866 | 24 I .8 W. | I |  | -II | 47 | 2 |  | 5.952 | 2 |  | 1.242 | 6.080 |
| Monte Video | 3453 | 56 | Jan. 18, 1866 | $9 \quad 20.8 \mathrm{E}$. | 2 |  | -31 | 6 | 3 |  | 6.040 | 3 |  | 3.644 | 7.054 |
| Sandy Point | 53 io S. | $70 \quad 54$ | Feb. 7, 1866 | 2152.0 E . | I |  | -54 |  | 2 |  | 6.121 | 1 |  | 8.725 | 10.658 |
| Valparaiso | $33 \quad 2 \mathrm{~S}$. | 7141 | March 29, 1866 | 15 51.1 E. | 6 |  | -35 | 23 | 12 |  | 6.326 | 8 |  | 4.493 | 7.759 |
| Callao | $12 \quad 5 \mathrm{~S}$. | $77 \quad 17$ | April 26, 1866 | 10 29.6 E . | I |  | - 6 | 28 | 2 |  | . 001 | I |  | 0.794 | 7.046 |
| Payta | 56 S . | 81 6 | May 7, 1866 | $8 \quad 53.0 \mathrm{E}$. | I |  | + 4 | 58 | 2 |  | -359 | I |  | 0.640 | 7.387 |
| Panama B | $8 \quad 54 \mathrm{~N}$. | $79 \quad 30$ | May 14, 1866 | $5 \quad 55.8 \mathrm{E}$. | 1 |  | -31 |  | 2 |  | .614 | I |  | 4.745 | 8.972 |
| Acapulco | $16 \quad 50 \mathrm{~N}$. | $99 \quad 52$ | May 30, 1866 | $8 \quad 22.2$ E. | 2 |  | +39 |  | 2 |  | 7.740 | 1 |  | 6.472 | 10.089 |
| Magdalena Bay | $24 \quad 40 \mathrm{~N}$. | 12 | June 9, 1866 | 10 40.5 E. | 1 |  | +48 | 32 | 2 |  | . 176 | 2 |  | 8.120 | 10.837 |
| San Diego Bay | $\begin{array}{lll}32 & 42 \mathrm{~N} .\end{array}$ | 1178 | June 15, 1866 | $13 \quad 9.4 \mathrm{E}$. | 1 |  | +57 | 54 | 2 |  | .261 | 1 |  | 9.981 | 11.782 |
| San Francisco . | $37 \quad 49 \mathrm{~N}$. | $122 \quad 21$ | June 26, 1866 | $16 \quad 25.5$ E. | I |  | +62 | 22 | 2 |  | 5.643 | 1 |  | 10.779 | 12.167 |
| Washington | $38 \quad 54 \mathrm{~N}$. | 773 | Nov. 1 I 1866\| | 244.2 W . | 1 |  | +72 |  | 2 |  | . 300 | 1 |  | 13.260 | 13.940 |

observations 0f magnetic declination.

Magnetic Declination.
Gosport, Va. October 30, 1865.

|  | Circle Readings. |  | Reading of Magnet. |  |
| :---: | :---: | :---: | :---: | :---: |
|  | Vernier . . . . . <br> Vernier . . . . . <br> Vernier . . . . . <br> Mean | $359^{\circ} 59^{\prime} \times 5^{\prime \prime}$ | (i) Scale erect . . . <br> (2) Scale inverted $(\mathrm{I})-(2)=\Delta \ldots$ | $\begin{array}{c\|r} \cdots & \begin{array}{r} 8 \mathrm{I}^{\mathrm{d}} \cdot 7 \\ 76.5 \end{array} \\ \hline+5.2 \end{array}$ |
|  |  |  | Transit of Sun's |  |
|  |  |  | $\begin{aligned} & \text { ist limb . . . } \\ & \text { 2d limb . . . } \\ & \text { Mean . . . . } \end{aligned}$ | $\begin{array}{lll} \mathrm{IO}^{\mathrm{h}} & 40^{\mathrm{m}} & 6^{\mathrm{s}} .2 \\ & 42 & 27.0 \end{array}$ |
|  |  | $162 \quad 1245$ |  | IO 41 I |
|  | Vernier . . . . . <br> Vernier . . . . . <br> Mean . |  | ist limb . . . <br> 2d limb . . . <br> Mean . . . . | $\begin{array}{ccc} \text { Io } & 44^{\mathrm{m}} & 48^{\mathrm{s}} .0 \\ & 47 & 8.8 \end{array}$ |
|  |  | $163^{\circ} 34^{\prime} 45^{\prime \prime}$ |  | $\begin{array}{lll}10 & 45 & 58.4\end{array}$ |
|  | Vernier . . . . . |  | Reading of Magnet. |  |
|  |  |  | (1) Scale inverted <br> (2) Scale erect . . . $(2)-(\mathrm{I})=\Delta \ldots$ | $\begin{array}{r\|r} \mathrm{d} . & 64^{\mathrm{d} .2} \\ . \cdot & 93.5 \\ \hline+29.3 \end{array}$ |
|  |  |  | Telescope Direct. | Telescope Reversed. |
|  |  |  |  |  |
|  |  |  |  |  |
| Circle reading to magnet. $\Delta \times \frac{1}{2}$ scale division. Sun's azimuth . |  | . . . | $359^{\circ} 59^{\prime} .2$ |  |
|  |  | . . . | + 6.1 |  |
|  |  | - • - | 33929.6 |  |
| Sum <br> $180^{\circ}+$ circle reading to sun |  | . - . | $339 \quad 34.9$ |  |
|  |  | - • - | $342 \quad 12.7$ |  |
| Magnetic declination |  | - - | 237.8 W. |  |

These observations were made before noon.
Chronometer $0^{\mathrm{h}} 4^{\mathrm{m}} 40^{\mathrm{s}} .2$ fast of local mean time.



Magnetic Declination.





Magnetic Declination.
Payta, May 7, i 866.


These observations were made before noon.
Chronometer $0^{\text {h }} 20^{\mathrm{m}} 16^{\mathrm{s}} .9$ fast of local mean time.

These observations were made at $9^{\mathrm{h}} 19^{\mathrm{m}}$ A.M., local mean time.
Magnetic Declination.
Magdalena Bay, June 9, 1866 .


observations 0f magnetic inclination.

| Magnetic Dip.Gosport, October 30, 1865. Needle A. $\mathbf{~}$.POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | Magnetic Dip. Gosport, October 30, 1865. Needle A. 2. POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| Circle east. |  |  |  | CIRCLE West. |  |  |  | CIRCLE EASt. |  |  |  | Circle west. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $70^{\circ}$ $39^{\prime}$ <br> 70 49 <br> 70 45 | $70^{\circ}$ $22^{\prime}$ <br> 70 30 <br> 70 27 | $7 \mathrm{I}^{\circ}$ $3^{\prime}$ <br> 7 I 4 <br> 7 I 5 | $70^{\circ}$ $44^{\prime}$ <br> 70 44 <br> 70 47 | 1090 ${ }^{10} 5^{\prime}$ | 109 ${ }^{10} 55^{\prime}$ | (109 ${ }^{\circ} 25^{\prime}$ | 109  <br> 109 $6^{\prime}$ <br> 109 37 <br> 109 50 | $71^{\circ}$ $47^{\prime}$ <br> 72 5 <br> 71 59 <br> 1  | $\begin{array}{ccc}71^{\circ} & 41^{\prime} \\ 7 \mathrm{I} & 5 \mathrm{I} \\ 7 \mathrm{I} & 46\end{array}$ | $\begin{array}{crr}70^{\circ} & 4^{\prime} \\ 70 & 6 \\ 70 & 14\end{array}$ | $69^{\circ}$ $48^{\prime}$ <br> 69 52 <br> 69 60 |  |  |  | $\begin{array}{lll}111^{\circ} & 30^{\prime} \\ \text { III } & 24 \\ \text { III } & 18\end{array}$ |
| $70 \quad 44$ | 7026 | 71 | $70 \quad 45$ | IIO 8 | 11017 | 10926 | 10944 | 7157 | 71 | $70 \quad 8$ | 69 56 | 109 Io | 10932 | III 5 | III. 24 |
|  |  | $45^{70}$ | $55$ |  | $12$ | $\int_{54}^{\mathrm{IO9}}$ |  |  | $\begin{array}{ll} 5 \mathrm{I} & \\ & 70 \end{array}$ | $5^{70}$ | $2$ $.70$ |  | $\begin{array}{ll} 21 & \\ & 110 \end{array}$ | $18^{111}$ |  |
| POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  |
| circle west. |  |  |  | CIRCLE EAST. |  |  |  | CIRCle west. |  |  |  | Circle east. |  |  |  |
| Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $\begin{array}{lr} 11 I^{\circ} & 52^{\prime} \\ 111 & 55 \\ 112 & 2 \end{array}$ | (1120 ${ }^{1} 4^{\prime}$ |  | $\left\lvert\, \begin{array}{lll}112^{\circ} & 29^{\prime} \\ 112 & 26 \\ 112 & 25\end{array}\right.$ | $68^{\circ}$ $49^{\prime}$ <br> 68 47 <br> 68 37 | $68^{\circ} 24^{\prime}$ <br> $68 \quad 27$ <br> $68 \quad$ I7 | $68^{\circ} 45^{\prime}$ <br> $68 \quad 30$ <br> $68 \quad 41$ | $\begin{array}{ll} 68^{\circ} & 26^{\prime} \\ 68 & 13 \\ 68 & 20 \end{array}$ | $\left\lvert\, \begin{array}{ll} 110^{\circ} & 29^{\prime} \\ \text { 1 10 } & 33 \\ \text { 1 } 0 & 41 \end{array}\right.$ | $\left\|\begin{array}{ll} \text { nio } & 40^{\prime} \\ \text { 110 } & 54 \\ 110 & 23 \end{array}\right\|$ |  | $\left\|\begin{array}{ll} 110^{\circ} & 59^{\prime} \\ \text { III } & 12 \\ \text { III } & \mathrm{II} \end{array}\right\|$ | $\begin{array}{ll} 69^{\circ} & 57^{\prime} \\ 69 & 4 \mathrm{I} \\ 69 & 40 \end{array}$ | $\begin{array}{ll} 69^{\circ} & 37^{\prime} \\ 69 & 20 \\ 69 & 18 \end{array}$ | $\begin{array}{lr} 70^{\circ} & 0^{\prime} \\ 70 & 7 \\ 70 & 10 \end{array}$ | $\begin{array}{ll} 69^{\circ} & 37^{\prime} \\ 69 & 42 \\ 69 & 45 \end{array}$ |
| III 56 | 112 Io | 112 10 | $112 \quad 27$ | 6844 | $68 \quad 23$ | $68 \quad 39$ | $68 \quad 20$ | IIO 34 | 110 39 | $110 \quad 50$ | III 7 | 6946 | $69 \quad 25$ | 70.6 | 6941 |
|  | 3112 | Io | $18$ |  | $\begin{array}{ll} \hline 34 & \\ & 68 \end{array}$ | ${ }^{32} \quad 68$ | $30$ |  | $36$ <br> IIO | $\begin{aligned} & \text { IIO } 5 \\ & 47^{2} \end{aligned}$ | $\begin{array}{cc} 58 \\ & \\ & \\ \hline \end{array}$ | $\square$ | $3^{36}$ | $45 \begin{array}{r} 69 \\ 45 \end{array}$ | 54 |
| Resulting Dip: $+69^{\circ}{ }^{21^{\prime}}$ |  |  |  |  |  |  |  | Resulting Dip: $+69^{\circ} 54^{\prime}$ |  |  |  |  |  |  |  |

Magnetic Dip.
St. Thomas, November 13, 1865, Needle A. 2.
POLARITY OF MARKED END NORTH.

| POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| circle east. |  |  |  | circle west. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. |
| $\begin{array}{ll} 50^{\circ} & 2^{\prime} \\ 50 \\ 50 & 35 \\ 50 & 50 \end{array}$ | $\begin{array}{lll} 49^{\circ} & 44^{\prime} \\ 50 & 15 \\ 50 & 24 \end{array}$ | $\begin{aligned} & 50^{\circ} 11^{\prime} \\ & 50 \\ & 50 \\ & 50 \\ & 50 \\ & 15 \end{aligned}$ | $\begin{aligned} & 49^{\circ} \quad 52^{\prime} \\ & 49 \\ & 49 \\ & 49 \\ & 45 \end{aligned}$ |  | $\begin{array}{ll} 130^{\circ} & 30^{\prime} \\ 130 & 30 \\ 130 & 30 \\ 130 & 24 \end{array}$ | $\begin{array}{lll} 130^{\circ} & 12 \\ 130^{\prime} & 6 \\ 130 & 6 \\ 13 & 11 \end{array}$ | $\begin{array}{\|l\|l\|} 130^{\circ} & 281 \\ 130 & 24 \\ 130 & 24 \\ 130 & 26 \end{array}$ |
| $50 \quad 29$ | 50 | $50 \quad 14$ | 4950 | 13012 | 13028 | 130 го | 13026 |
|  | $50 \text { 10 }$ |  | 49 | $\begin{array}{r} 130 \\ 55 \end{array}$ | 20 <br> 130 | ${ }_{\text {I9 }}{ }^{130}$ |  |


$55 \quad 5$
Resulting Dip: $+49^{\circ}$
Azimuth of Dip Circle $26^{\circ}{ }^{1} 6^{\prime}$
Magnetic Dip.

| Magnetic Dip. <br> St. Thomas, November 13, 1865. Needle A. 2. |  |  |  |  |  |  |  | Magnetic Dip. <br> St. Thomas, November 16, 1865. Needle A. i. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| CIRCLE EAST. |  |  |  | CIRCLE WEST. |  |  |  | CIRCLE EAST. |  |  |  | CIRCLE WEST. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $49^{\circ}$ $42^{\prime}$ <br> 49 44 <br> 40 53 | $49^{\circ}$ $21^{\prime}$ <br> 49 20 <br> 49 25 |   <br> 50  <br> 50 10 <br> 51 5 <br> 50 47 | $49^{\circ}$ $55^{\prime}$ <br> 50 42 <br> 50 19 | $130^{\circ}$ 50 <br> 130 40 <br> 130 46 | $131^{\circ}$ $15^{\prime}$ <br> I31 3 <br> 131 11 | I $30^{\circ}$ 561 <br> I30 37 <br> I 30 41 | $\begin{array}{ll} 130^{\circ} & 47^{\prime} \\ 130 & 57 \\ 130 & 66 \\ \hline \end{array}$ | $52^{\circ}$ $16 \prime$ <br> 52 26 <br> 52 40 | $51^{\circ}$ $57^{\prime}$ <br> 52 3 <br> 52 8 <br> 2  | $53^{\circ}$ $\circ^{\prime}$ <br> 53 9 <br> 53 7 | $52^{\circ}$ $40^{\prime}$ <br> 52 47 <br> 52 45 | 1280  <br> 128 28 <br> I28 38 | $128^{\circ}$ $54^{\prime}$ <br> 128 44 <br> 128 42 | $127^{\circ}$ $44^{\prime}$ <br> 127 45 <br> 127 52 | $128^{\circ}$ $5^{\prime}$ <br> I28 1 <br> 128 7 <br> 1  |
| 4946 | $49 \quad 22$ | $50 \quad 40$ | $50 \quad 18$ | $130 \quad 45$ | 13110 | 13045 | 13057 | $\begin{array}{ll}52 & 27\end{array}$ | 523 | $53 \quad 5$ | 5244 | $128 \quad 31$ | $128 \quad 47$ | $127 \quad 47$ | 1284 |
|  | $34$ | ${ }^{50}$ | $29$ |  | $\begin{array}{ll} 57 & \\ & \text { 130 } \end{array}$ | $54^{\mathrm{I} 30}$ | 51 |  | 52 | $355^{52}$ | 55 |  | $39$ <br> 128 | $17^{127}$ | 55 |
| POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  |
| CIRCLE West. |  |  |  | circle east. |  |  |  | circle west. |  |  |  | CIRCLE EAst. |  |  |  |
| Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  |
|  | N. | S. | N. |  | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $\begin{array}{ll} 129^{\circ} & 3^{\prime} \\ 129 & 47 \\ 129 & 47 \end{array}$ | $129^{\circ} 59^{\prime}$ $\begin{array}{ll}130 & \text { II } \\ 130 & 20\end{array}$ | $\begin{array}{rr} 130^{\circ} & 4^{\prime} \\ 130 & 22 \\ 130 & 8 \end{array}$ | $\begin{array}{ll} 130^{\circ} & 30^{\prime} \\ \mathrm{I} 3 \mathrm{O} & 47 \\ \mathrm{I} 30 & 35 \end{array}$ | $\begin{array}{lr} 49^{\circ} & 4^{\prime} \\ 49 & 25 \\ 49 & 20 \end{array}$ | $\begin{array}{lr} 49^{\circ} & \mathbf{I}^{\prime} \\ 49 & 30 \\ 49 & 28 \end{array}$ | $\begin{array}{ll} 50^{\circ} & 26^{\prime} \\ 50 & 36 \\ 50 & 31 \end{array}$ | $\begin{array}{ll} 50^{\circ} & 29^{\prime} \\ 50 & 45 \\ 50 & 32 \end{array}$ | $\left\|\begin{array}{lll} \text { I } 33^{\circ} & 43^{\prime} \\ \text { I } 33 & 47 \\ \text { I } 33 & 36 \end{array}\right\|$ | $\begin{array}{cc} 134^{\circ} & \mathrm{o}^{\prime} \\ \mathrm{I} 34 & \mathrm{o} \\ \mathrm{I} 33 & 50 \end{array}$ | $\left\|\begin{array}{ll} \mathbf{1} 33^{\circ} & \mathbf{1 2} \\ \mathbf{I} 33 & \mathbf{1 6} \\ \mathbf{I} 33 & 24 \end{array}\right\|$ | $\left.\begin{array}{ll} \mathrm{I} 33^{\circ} & 281 \\ \mathrm{I} 33 & 3 \mathrm{I} \\ \mathrm{I} 33 & 43 \end{array} \right\rvert\,$ | $\begin{array}{ll} 47^{\circ} & 34^{\prime} \\ 47 & 28 \\ 47 & 21 \end{array}$ | $\begin{array}{ll} 47^{\circ} & 14^{\prime} \\ 46 & 51 \\ 46 & 53 \end{array}$ | $\begin{array}{ll} 47^{\circ} & 50^{\prime} \\ 47 & 38 \\ 47 & 34 \end{array}$ | $\begin{array}{rrr} 47^{\circ} & 30^{\prime} \\ 47 & 20 \\ 47 & 8 \end{array}$ |
| 12945 | 13010 | 130 II | $130 \quad 37$ | $49 \quad 16$ | 4920 | $50 \quad 3 \mathrm{I}$ | $50 \quad 35$ | 13342 | 13357 | 13317 | 1333 | $47 \quad 28$ | $46 \quad 59$ | $47 \quad 4 \mathrm{I}$ | $47 \quad 19$ |
|  | $58$ <br> 130 | $I^{130}$ | $24$ |  | 18 <br> 49 | $5^{56}$ | $33$ | 133 | 50 <br> 133 | ${ }_{37}{ }^{\text {I } 33}$ | $25$ |  |  | ${ }_{22}{ }^{47}$ | 30 |
| Resulting Dip: $+49^{\circ} 44^{\prime}$ |  |  |  |  |  |  |  | Resulting Dip: $+49^{\circ} 39^{\prime}$ |  |  |  |  |  |  |  |



| Magnetic Dip. <br> Ceara, December I3, 1865. Needle A. 2. |  |  |  |  |  |  |  | Magnetic Dip. Ceara, December 13 , 1865 . Needle A. 1. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  |
| circle east. |  |  |  | CIRCLE West. |  |  |  | circle east. |  |  |  | CIRCLE West. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N | S. | N | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $20^{\circ}$ $30^{\prime}$ <br> 20 17 <br> 20 30 |  | $21^{\circ}$ <br> 21 <br> 21 <br> 21 <br> 21 |  | 159 56 <br> 1560 37 <br> 160 30 |  | [15$156^{\circ}$ $35^{\prime}$ <br> 157 0 <br> 157 0 |  | $17^{\circ}$ $30^{\prime}$ <br> 17 31 <br> 17 45 |  | 160 $5^{\prime}$ <br> 15 $5^{2}$ <br> 15 $5^{2}$ |  | 163  <br> $163^{\circ}$  <br> 163 20 <br> 163 6 |  | $\left\lvert\, \begin{array}{cc}1660 & \\ 160 \\ 165 & 30 \\ 166 & 0\end{array}\right.$ |  |
| $20 \quad 26$ |  | $21 \quad 16$ |  | $160 \quad 21$ |  | 156 ${ }^{52}$ |  | ${ }^{17} 35$ |  | $15 \quad 56$ |  | 16315 |  | 1667 |  |
| 20.51 |  |  |  | $158 \quad 36$ |  |  |  | 1645 |  |  |  | $2 \quad 164 \quad 41$ |  |  |  |
| POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| CIRCLE West. |  |  |  | CIRCLE EASt. |  |  |  | Circle west. |  |  |  | Circle east. |  |  |  |
| Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| 159 $4^{\prime}$ <br> 158  <br> 158  <br> 158 45 |  | $160^{\circ}$ 20 <br> 160 5 <br> 159 23 |  | $22^{\circ}$ $55^{\prime}$ <br> 22 32 <br> 22 28 |  | $22^{\circ}$ $20^{\prime}$ <br> $\mathbf{2 2}$ 8 <br> 22 26 |  | $\begin{array}{cc} 154^{\circ} & 0^{\prime} \\ \mathbf{1 5 4} & 18 \\ 154 & 5 \end{array}$ |  | [153$153^{\circ}$  <br> 154 20 <br> 154 40 <br> 54 40 |  | $\begin{array}{ccc}27^{\circ} & 10 \\ 27 & 10 \\ 27 & 0\end{array}$ |  | $27^{\circ}$ $10^{\prime}$ <br> 27 0 <br> 27 20 |  |
| $158 \quad 50$ |  | 15956 |  | $22^{\circ} 3^{8 \prime}$ |  | $22 \quad 18$ |  | 154 |  | $1 \begin{array}{ll}154 & 18\end{array}$ |  | $27 \quad 7$ |  | 27 10 |  |
| 15923 |  |  |  | $33 \quad 22 \quad 28$ |  |  |  | $154 \quad 13$ |  |  |  | 28 |  | 9 |  |
| Resulting Dip: + $2 \mathbf{1}^{\circ}{ }^{20}$ |  |  |  |  |  |  |  | Resulting Dip: $+2 \mathrm{I}^{\circ} 26^{\prime}$ |  |  |  |  |  |  |  |



| Magnetic Dip. <br> Bahia, December 27, 1865. Needle A. 2. |  |  |  |  |  |  |  | Magnetic Dip. <br> Bahia, December 27, 1865. Needle A. i. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| circle east. |  |  |  | circle west. |  |  |  | circle east. |  |  |  | circle west. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $\begin{array}{lll}3^{\circ} & 3{ }^{\prime \prime} \\ 3 & 45 \\ 3 & 45 \\ 3 & 30\end{array}$ | $3^{\circ}$ $15^{\prime}$ <br> 3 30 <br> 3 35 | $4^{\circ}$ 40 <br> 5 10 <br> 5 10 <br> 5 50 | $4^{\circ} 1{ }^{1 \prime}$  <br> 4  <br> 4 45 <br> 5 20 | $\begin{array}{lll} 176^{\circ} & 30! \\ 176 & 45 \\ 176 & 45 \\ 17 & 45 \end{array}$ | $\begin{array}{lll} 176^{\circ} & 30^{\prime} \\ 176 & 40 \\ 176 & 40 \end{array}$ | $\begin{array}{r} 176^{101} \\ 176 \\ 176 \\ 176 \\ 15 \end{array}$ | $\left\|\begin{array}{rr} 1760^{10} & \mathrm{Iof}^{176} \\ 175 \\ 175 & 50 \end{array}\right\|$ | $\left\lvert\, \begin{array}{ccc} 11^{\circ} & 300^{\prime} \\ 11 & 30 \\ 12 & 30 \\ 12 & 0 \end{array}\right.$ |  | $\left\lvert\, \begin{array}{cc} 1 I^{\circ} & 30^{\prime} \\ 11 & 10 \\ 11 & \text { IO } \\ \text { II } & \end{array}\right.$ |  | $\left\|\begin{array}{ll} 168^{\circ} & 55^{\prime} \\ 169 & 10 \\ 169 & 10 \\ 10 \end{array}\right\|$ |  | $\begin{array}{\|ll} 170^{\circ} & 20 \\ 169 & 50^{\prime} \\ 170 & 55 \end{array}$ |  |
| $\begin{array}{ll}3 & 37\end{array}$ | $3 \quad 27$ | $5 \quad 13$ | 447 | 176 | 176 <br> 7 | 176 | 176 | 1140 |  | $\begin{array}{ll}11 & 17\end{array}$ |  | 169 5 |  | 170 |  |
|  | ${ }_{4}$ | ${ }_{16} 5$ |  | $\left.\right\|_{56} ^{176}$ | ${ }_{176}$ | $24^{176}$ |  | 1128 |  |  |  | $\begin{array}{lll}  & 169 \quad 39 \\ \hline \end{array}$ |  |  |  |
| POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END SOUTH. |  |  |  |  |  |  |  |
| circle west. |  |  |  | circle east. |  |  |  | circle west. |  |  |  | circle east. |  |  |  |
| Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  |
| S. | N. | S. | N. | S. | N . | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $\begin{array}{ll} 174^{\circ} & 45^{\prime} \\ 174 & { }^{\prime} 7 \\ 174 & 40 \end{array}$ | $\begin{array}{ll} 174^{\circ} & 50^{\prime} \\ 174 & 40 \\ 174 & 50 \end{array}$ | $\left\lvert\, \begin{array}{cc} 176^{\circ} & 30 \\ 177 & 0^{\prime} \\ 176 & 15 \\ 17 & 0 \end{array}\right.$ | $\left\|\begin{array}{cc} 176^{\circ} & 301 \\ 177 & 15 \\ 176 & 15 \\ 176 \end{array}\right\|$ | $\begin{array}{ll} 4^{\circ} & 30 \\ 5 & 5 \\ 5 & 5 \\ \hline \end{array}$ | $\begin{array}{ll} 4^{\circ} & \mathrm{IO}^{\prime} \\ 4 & 45 \\ 4 & 40 \\ \hline \end{array}$ | $\begin{array}{lll} 5^{\circ} & 25^{\prime} \\ 5 & 30 \\ 5 & 30 \\ 5 & 30 \\ \hline \end{array}$ | $\begin{array}{ll} 5^{\circ} & o^{\prime} \\ 5 & 5 \\ 5 & 0 \end{array}$ | $\left.\begin{array}{ll} 3^{\circ} & 15^{\prime} \\ 3 & 35 \\ 3 & 5 \end{array} \right\rvert\,$ |  | $\begin{array}{lll} \mathrm{I}^{\circ} & 50^{\prime} \\ \mathrm{I} & 55 \\ \mathrm{I} & 55 \\ \hline \end{array}$ |  | $\left\|\begin{array}{rr} 177^{\circ} & 25^{\prime} \\ 178 \\ 178 & 20 \\ 17 & 5 \end{array}\right\|$ |  | $\left\|\begin{array}{ll} 179^{\circ} & 20 \prime \\ 179 & 10 \\ 179 & 10 \\ 179 & 10 \end{array}\right\|$ |  |
| ${ }^{174} 43$ | 17447 | $176 \quad 35$ | 176 35 | $45^{2}$ | $4{ }^{42}$ | $5 \quad 28$ | $5 \quad 2$ | $\begin{array}{ll}3 & 18\end{array}$ |  | I 53 |  | 177 |  | 179 13 |  |
|  | ${ }^{45}$ | $40^{176}$ | $35$ <br> 4 | $39$ | $42$ $4$ | $5^{5}$ |  |  |  | 35 |  | $\bigcirc$ | - | 7835 |  |
|  |  |  | esulting Dip | $\mathrm{p}:+4^{\circ} \mathrm{I}$ |  |  |  |  |  |  | Iting | $\mathrm{p}:+4^{\circ} 3$ |  |  |  |




Magnetic Dip.
Monte Video, January 18, 1866. Needle A. 2.

| circle east. |  |  |  | circle west. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N . | S. | N. |
|  | $\begin{array}{\|cc} \hline \mathrm{I}_{1} 8^{\circ} & 50^{\prime} \\ \mathrm{I} 49 & 0 \\ 149 & 30 \end{array}$ |  | $\left\lvert\, \begin{aligned} & 149^{\circ} \\ & 100 \\ & 148 \\ & 149 \\ & 140 \\ & 100 \end{aligned}\right.$ |  |  |  | $31^{\circ}$ 0 <br> 31  <br> 31  <br> 31 40 <br> 10  |
|  | 149 |  | 1493 |  | $31 \quad 10$ |  | 3127 |
| 149 |  | ${ }^{1}$ |  | $7 \quad 31 \quad 19$ |  |  |  |
| polarity of marked end south. |  |  |  |  |  |  |  |
| circle west. |  |  |  | circle east. |  |  |  |
| Face West. |  | Face East. |  | Face West. |  | Face East. |  |
| s. | N. | S. | N. | S. | N. | S. | N. |
|  | $\left\|\begin{array}{rr} 32^{\circ} & 0^{\prime} \\ 32 & 0 \\ 3 \mathbf{3}^{1} & 50 \end{array}\right\|$ |  | $\left.\begin{array}{rr} 3 I^{\circ} & 0^{\prime} \\ 3 \mathrm{I} & 20 \\ 3 \mathrm{I} & 40 \end{array} \right\rvert\,$ |  |  |  | $\begin{array}{ll} \mathrm{I} 49^{\circ} & \mathrm{IO}^{\prime} \\ \mathrm{I} 49 & 30 \\ \mathrm{I} 49^{3} & 50 \end{array}$ |
|  | 31 57 |  | 3120 |  | 14913 |  | 14930 |
| $\begin{array}{lll}31 & 39 & 3^{1}\end{array}$ |  |  |  | 8 | 149 | 22 |  |
| Resulting Dip: $-3 \mathrm{I}^{\circ} 8^{\prime}$ |  |  |  |  |  |  |  |







Magnetic Dip.



Magnetic Dip.
Flamenco Island, Pariama Bay, May 14, 1866. Needle A. 2. Flamenco Island, Panama Bay, May 14, 1866. Needle A. i.

| POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| circle east. |  |  |  | circle west. |  |  |  | circle east. |  |  |  | circle west. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $32^{\circ} 40^{\prime}$ | $32^{\circ} \mathrm{Io}$ | $31^{\circ} 35^{\prime} \mid 31^{\circ}$ or |  | $148^{\circ} 50^{\prime}$ I $148^{\circ} 40^{\prime}$ |  | $14^{\circ}{ }^{15} 15^{\prime} 148^{\circ} 10^{\prime}$ |  | $36^{\circ} 20^{\prime}$ |  | $36^{\circ} 40^{\prime}$ |  | $144^{\circ} 25^{\prime}$ |  | $144^{\circ} 25^{\prime}$ |  |
|  | $31 \quad 5 ?$ |  | $31 \quad 18$ | $42$ | 45 <br> 148 | ${ }_{28}^{148}$ |  |  |  |  | 36 | ${ }^{1}$ |  | 25 |  |


| circle west. |  |  | circle east. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Face West. | Face East. |  | Face West. |  | Face East. |  |
| S. N. | S. | N. | S. | N. | S. | N. |
| $153^{\circ} 15^{\prime}$ | $15^{\circ}{ }^{\circ} 10$ |  | $27^{\circ} 40^{\prime}$ |  | $28^{\circ} 50^{\prime}$ |  |
| 152 |  |  | 46 |  | 15 |  |

Resulting Dip: $+32^{\circ} 5^{\prime}$



| Magnetic Dip. <br> San Diego Bay, June 15, 1866. Needle A. 2. |  |  |  |  |  |  |  | Magnetic Dip. <br> San Diego Bay, June 15, I866. Needle A. I. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  | POLARITY OF MARKED END NORTH. |  |  |  |  |  |  |  |
| Circle east. |  |  |  | CIRCLE WEST. |  |  |  | Circle east. |  |  |  | CIRCLE WEST. |  |  |  |
| Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  | Face East. |  | Face West. |  |
| S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. | S. | N. |
| $59^{\circ} 25^{\prime}$ | $59^{\circ} \mathrm{o}^{\prime}$ | $5^{80} 15^{\prime}$ | $57^{\circ} 45^{\prime}$ | $122^{\circ} \mathrm{o}^{\prime}$ | $121^{\circ} 55^{\prime}$ | $122^{\circ} 40^{\prime}$ | $122^{\circ} 40^{\prime}$ | $60^{\circ} 10^{\prime}$ | $59^{\circ} 45^{\prime}$ | $60^{\circ} 30^{\prime}$ | $60^{\circ} \mathrm{o}^{\prime}$ | 121 ${ }^{\circ}{ }^{\prime}$ | $120^{\circ} 45^{\prime}$ | $120^{\circ} 20^{\prime}$ | $120^{\circ} 0^{\prime}$ |
|  | $58$ | $3^{6} \quad 58$ |  |  | $57$ | $18^{122}$ |  |  |  | $6^{60}$ | $15$ | $\left.\right\|_{45} ^{120}$ | $5^{2}$ <br> 120 | $3^{6} 120$ |  |


Magnetic Dip.


| Magnetic Dip. | Magnetic Dip. |
| :---: | :--- |
| U.S. Naval Observatory, Washington, Nov. i, r866. Needle A. i. | U. S. Naval Observatory, Washington, Nov. i, i866. Needle A. 2. | A. . U.S. Nalorn, Washington, Nov. is

 | POLARITY OF MARKED END SOUTH. |  |  |  |
| :---: | :---: | :---: | :---: |
| CIRCle west. |  | circle east. |  |
| Face West. | Face East. | Face West. | Face East. |

 Resulting Dip: $+7 \mathrm{I}^{\circ}{ }^{\circ} 5^{\prime \prime}$

| Magnetic Dip. | Magnetic Dip. |
| :---: | :---: | :---: |
| U. S. Naval Observatory, Washington, May 6, 1867. Needle A. i. | U. S. Naval Observatory, Washington, May 6, i867. Needle A. 2. |



## HORIZONTAL INTENSITY. OBSERVATIONS OF VIBRATIONS.



## Horizontal Intensity. Observations of Vibrations.



Horizontal Intensity. Observations of Vibrations.


Horizontal Intensity. Observations of Vibrations.


Horizontal Intensity. Observations of Vibrations.


Horizontal Intensity. Observations of Vibrations.


Horizontal Intensity. Observations of Vibrations.

| Magdalena Bay, June 9, 8866. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. |  |  |  |  |  |  |  |

In this and the following observation the vibrations of the magnet were very irregular on account of a high wind which shook the instrument.

Magdalena Bay, June 9, 1866.

| No. | Time A. M. | No. | Time A. M. | Time of 150 vibrations. |
| :---: | :---: | :---: | :---: | :---: |
| - | $\mathrm{I}^{\mathrm{h}} 4 \mathrm{I}^{\mathrm{m}} \mathrm{I}^{\text {d }}$ s. 2 | 150 | $\mathbf{I}^{\text {l }} 55^{\text {m }}$ m $4^{\text {s. }} 8$ |  |
| 10 | $\begin{array}{llll}\text { I } & 42 & 7.8\end{array}$ | 160 | $\begin{array}{lll}\text { I } & 56 & 0.4\end{array}$ |  |
| 20 | I 433.0 | 170 | I 5656.0 |  |
| 30 | I 4359.0 | 180 | $\begin{array}{llll}\text { I } & 57 & 51.4\end{array}$ |  |
| 40 | I 4454.0 | 190 | I 5846.4 |  |
| 50 | $\begin{array}{lll}\text { I } & 45 & 48.4\end{array}$ | 200 | I 5941.6 |  |
| 100 | $\begin{array}{llll}\text { I } & 50 & 25.4\end{array}$ |  |  |  |
| Extreme scale readings, |  |  |  |  |
| At beginning . . . . 53.5-98.5 |  |  |  |  |
| Coefficient of torsion . . $v=4.37$ div. |  |  |  |  |
|  |  |  |  |  |
| Temperature . . . . $86^{\circ} .5$ |  |  |  |  |
| Time of one vibration . . $5^{\text {s }} .533$ |  |  |  |  |

San Diego Bay, June $15,1866$.

| No. | Time P. M. |  | No. | Time P. M. | Time of 150 vibrations. |
| :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $6^{\text {h }} 1 \mathrm{I}^{\mathrm{m}}$ | $9^{\text {s. }} 2$ | 150 | $6^{6 \mathrm{~h}} 25^{\mathrm{m}} 5^{88} .2$ | $14^{\mathrm{m}} 4.9{ }^{\text {s.o }}$ |
| 10 | $6 \quad 12$ | 8.3 | 160 | $\begin{array}{llll}6 & 26 & 56.6\end{array}$ | 1448.3 |
| 20 | $6 \quad 13$ | 7.4 | 170 | $\begin{array}{lll}6 & 27 & 55.8\end{array}$ | $14 \quad 48.4$ |
| 30 | $6 \quad 14$ | 7.0 | 180 | $\begin{array}{llll}6 & 28 & 55.4\end{array}$ | $14 \quad 48.4$ |
| 40 | $6 \quad 15$ | 6.2 | 190 | $\begin{array}{llll}6 & 29 & 53.8\end{array}$ | $14 \quad 47.6$ |
| 50 | $6 \quad 16$ | 5.4 | 200 | $6 \quad 30 \quad 53.0$ | I4. 47.6 |
|  |  |  |  | Mean . | $14 \quad 48.22$ |

Extreme scale readings,
At beginning . . . . 94.9- 108.9
At end
$\begin{gathered}\text { At end } \\ \text { Coefficient of torsion }\end{gathered} \cdot . v=30.6088 .0$
Temperature
Time of one vibration . . $5^{\text {s. }} .92 \mathrm{I}$

San Francisco Bay, June 26, 1866.

| No. | Time A. M. |  |  | No. | Time A. M. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ | $3^{\text {h }} 22^{\text {m }}$ m $22^{\text {s }} .7$ |  |  | 150 | $3^{\text {b }} 33^{6 \mathrm{~m}} 57^{\text {s }} \cdot 7$ |  |  | $15^{\text {m }} 35^{\text {s }}$. 0 |  |
| Iо | $\begin{array}{lll}3 & 22 . & 24.7 \\ 3 & 23 & 27.2\end{array}$ |  |  | 160 |  | 38 | 0.0 | $\begin{array}{ll}15 & 35 \cdot 3 \\ 15 & 35 \cdot 3\end{array}$ |  |
| 20 |  |  |  | 170 | 3 | $\begin{array}{llll}3 & 39 & 2.5\end{array}$ |  |  |  |
| 30 |  | 24 | 30.2 | 180 | . 3 | 40 | 4.7 | 15 | 34.5 |
| 40 | 3 3 |  | 32.0 | 190 | 3 |  | 7.2 | 15 | 35.2 |
| 50 |  | $\begin{array}{llll}3 & 26 & 34.7\end{array}$ |  | 200 | 3 | 42 10.0 |  | 15 | $35 \cdot 3$ |
|  |  |  |  |  | n. |  |  | 35.10 |

Extreme scale readings,
$\begin{aligned} & \text { At beginning } \\ & \text { At end }\end{aligned} . \cdot .57 .0-102.0$
Coefficient of torsion . . $v=4.35$ div.
Temperature . . . . . $77^{\circ} .0$
Time of one vibration . . 6 s. 234
U. S. N. Observatory, Washington, Nov. r, 1866.

| No. | Time P. M. | No. | Time P. M. | Time of 150 vibrations. |
| :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ | $5^{\text {h }}$ 19 ${ }^{\text {m }} 55^{\text {as }} .7$ | 150 | $5^{\text {h }} 37^{\text {m }} 4^{68} .5$ | ${ }_{17}{ }^{\mathrm{m}} 53^{\text {s }}$. 8 |
| 10 | $5 \mathrm{llr}_{5} \mathbf{5 1} 5$ | 160 | $\begin{array}{llll}5 & 38 & 58.0\end{array}$ | 1753.0 |
| 20 | $\begin{array}{llll}5 & 22 & 16.0\end{array}$ | 170 | $\begin{array}{llll}5 & 40 & 9.2\end{array}$ | $17 \quad 53.2$ |
| 30 | $\begin{array}{llll}5 & 23 & 27.5\end{array}$ | 180 | $\begin{array}{llll}5 & 41 & 20.7\end{array}$ | $17 \quad 53.2$ |
| 40 | $\begin{array}{llll}5 & 24 & 39.0\end{array}$ | 190 | $\begin{array}{llll}5 & 42 & 31.8\end{array}$ | 1752.8 |
| 50 | $\begin{array}{llll}5 & 25 & 50.7\end{array}$ | 200 | 5 | $17 \quad 52.3$ |
|  |  |  | Mean . . . | $17 \quad 53.05$ |

Extreme scale readings,
At beginning . . . . 52.5-106.0
At end . . . . . 66.6-95.2
Coefficient of torsion . . $v=5.80$ div.
Temperature . . . . . $67^{\circ} .5$
Time of one vibration . . $7^{\text {s. }} 154$

The following sets of observations of vibrations were made in the basement of the Observatory, where there is much iron, and are to be used only to determine the moment of inertia of the magnet.

Set 1. November 2, 1866.

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ | $5^{\text {b }}$ | $37^{\mathrm{m}}$ | $31^{\text {s }} .7$ | 150 | $5^{\text {h }}$ | $54^{\text {m }}$ | $53^{\text {s }} .8$ |  | 22 ${ }^{\text {s. }}$ I |
| ıо | 5 | 38 | 41.2 | 160 | 5 | 56 | 3.2 | 17 | 22.0 |
| 20 | 5 | 39 | 50.7 | 170 |  |  | 12.7 | 17 | 22.0 |
| 30 | 5 | 41 | 0.2 | 180 |  | 58 | 21.5 | 17 | 21.3 |
| 40 | 5 | 42 | 9.7 | 190 |  |  |  | 17 |  |
| 50 |  | 43 | 19.2 | 200 | 6 |  | 40.7 | 17 | 21.5 |
|  |  |  |  |  | Me | an. | . . |  | 21.73 |

Extreme scale readings,


Time of one vibration . . $6^{\mathrm{s}} .945$

## Horizontal Intensity. Observations of Vibrations.

Set No. 2. November 2, 1866.
Inertia ring on magnet

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ | $6^{\text {b }}$ | $17^{m}$ | $25^{\text {s. }} 3$ | 150 | $6^{\text {b }}$ |  | $4^{6} .8$ | $22^{\text {m }}$ | $21^{8} .5$ |
| 10 | 6 | 18 | 55.2 | 160 | 6 | 4I | 16.2 | 22 | 21.0 |
| 20 | 6 | 20 | 24.2 | 170 | 6 | 42 | $45 \cdot 7$ | 22 | 21.5 |
| 30 | 6 | 21 | 54.0 | 180 | 6 | 44 | 14.8 | 22 | 20.8 |
| 40 | 6 | 23 | 23.7 | 190 | 6 | 45 | 44.2 | 22 | 20.5 |
| 50 |  |  | 53.0 | 200 | 6 | 47 | 13.7 | 22 | 20.7 |
|  |  |  |  |  |  | an . | . . . | 22 | 21.00 |

Extreme scale readings,
At beginning . . . . 58.9-100.8
At end . . . . . 68.3-95.5
Coefficient of torsion . . $v=7.58$ div.
Temperature . . . . . $68^{\circ} .5$
Time of one vibration . . $8^{\text {s }} .940$

Set No. 3. November 2, 1866.


Set No. 4. November 2, 1866.
Inertia ring on magnet.

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| O | $7^{\text {h }} 26^{\text {m }}$ I $8^{\text {s. }} 3$ |  |  | 150 | $7^{\text {h }} 44^{\text {mm }} 39^{\text {s }} .0$ |  |  | $22^{\mathrm{m}} 20^{8} .7$ |  |
| 10 | 7 | 27 | 47.7 | 160 | 7 | 50 | 8.5 | 22 | 20.8 |
| 20 | 7 | 29 | 17.2 | 170 | 7 | 51 | 37.9 | 22 | 20.7 |
| 30 | 7 |  | 46.7 | 180 | 7 | 53 | $7 \cdot 3$ | 22 | 20.6 |
| 40 | 7 |  | $\pm 6.0$ | 190 | 7 | 54 | 36.7 | 22 | 20.7 |
| 50 | 7 | 33 | $45 \cdot 5$ | 200 | 7 | 56 | 5.8 |  | 20.3 |
|  |  |  |  |  |  | an | -•• | 22 | $20.63{ }^{\circ}$ |

Extreme scale readings,
At beginning . . . . $56.5-\mathrm{IO} 3.6$
At end . . . . . . 65.1-96.3
Temperature . . . . . $70^{\circ} .0$
Time of one vibration . . $8^{\mathrm{s}} .938$

Set No. 5. November 2, 1866.


Set No. 6. November 2, 1866.

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\bigcirc$ |  | $3 \mathrm{I}^{\mathrm{m}}$ | $5^{88} .2$ | 150 | $12^{\text {b }}$ | $49^{\text {m }}$ | $5^{15} .2$ |  | $53^{\text {s }}$ |
| 10 |  | 33 | 9.2 | 160 |  |  | 2.5 | 17 | 53. |
| 20 |  | 34 | 21.0 | 170 |  |  | 14.2 | 17 | 53. |
| 30 |  | 35 | 32.7 | 180 |  |  | 25.7 | 17 | 53.0 |
| 40 |  | 36 | 44.0 | 190 |  |  | 37.2 | 17 | 53. |
| 50 |  | 37 | $55 \cdot 7$ | 200 |  | 55 | 48.7 | 17 | 53. |
|  |  |  |  |  | Mea | n . |  | 17 | 53. |
|  | Extreme scale readings, |  |  |  |  |  |  |  |  |
|  | At beginning . . . . 59.5 |  |  |  |  |  |  | 99.0 |  |
|  | At end . . . . . . 65.5 |  |  |  |  |  |  | 2.0 |  |
|  | Temperature . . . . . $56^{\circ}$.o |  |  |  |  |  |  |  |  |
|  | Time of one vibration . . $7^{\text {s. }} 154$ |  |  |  |  |  |  |  |  |

Set No. 7. November 2, 1866.
Inertia ring on magnet.

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $\mathrm{I}^{\text {b }}$ | $3^{\mathrm{m}}$ | $23^{\text {s }} \cdot 5$ | 150 |  | $26^{\text {m }}$ | $22^{3} .7$ | $22^{\text {m }}$ | $59^{\text {s. }} 2$ |
| io | I | 4 | 55.2 | 160 | 1 | 27 | 54.2 | 22 | 59.0 |
| 20 | I |  | 27.5 | 170 |  | 29 | 26.7 | 22 | 59.2 |
| 30 | 1 | 7 | 59.2 | 180 | I | 30 | 58.5 | 22 | $59 \cdot 3$ |
| 40 | I |  | 31.3 | 190 |  | 32 | 30.2 |  | 58.9 |
| 50 | I |  | 3.2 | 200 |  | 34 | 2.5 | 22 | $59 \cdot 3$ |
|  |  |  |  |  |  | n | -• | 22 | 59.15 |

Extreme scale readings,
At beginning . . . . 58.2 - IOI. 0
At end . . . . . . 68.0-97.2
Tcmperature . . . . . $\quad 53^{\circ} \cdot 5$
Time of one vibration . . $\quad 9^{\mathrm{g}} .194$

Horizontal Intensity. Observations of Vibrations.
Set No. 8. November 2, 1866.

| No. | Time. |  |  | No. | Time. |  |  | Time of 150 vibrations. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 0 | $\mathrm{I}^{\text {b }}$ | $40^{\text {m }}$ | $19^{8} .2$ | 150 | $I^{\text {h }}$ | $5^{8 \mathrm{~m}}$ | I $1^{\text {s }}$. 5 |  | $52^{\text {s }} \cdot 3$ |
| 10 | I | 41 | 30.7 | 160 | 1 | 59 | 23.0 | 17 | 52.3 |
| 20 | 1 |  | 42.2 | 170 | 2 | 0 | 34.5 | 17 | 52.3 |
| 30 | 1 | 43 | 53.7 | 180 | 2 | 1 | 46.0 | 17 | 52.3 |
| 40 | I | 45 | 5.2 | 190 |  | 2 | 57.5 | 17 | 52.3 |
| 50 | I | 46 | 16.7 | 200 | 2 | 4 |  | 17 | 52.3 |
|  |  |  |  |  |  | an | - . | 17 | 52.30 |

Extreme scale readings,
At beginning . . . . 60.0- 101.0
At end . . . . . . 68.0-92.8
Temperature .. . . . . $52^{\circ} .5$
$\begin{array}{cc}\text { Temperature } \\ \text { Time of one vibration } & \bullet \\ 7^{s} .149\end{array}$

## horizontal intensity. observations of derlections.

Philadelphia, October 24, 1865.

| $\begin{aligned} & \dot{せ} \\ & \mathbb{E}_{0} \\ & \text { ت} \end{aligned}$ |  | Time. | Temp. |  |  | Diff's. | Dist. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \dot{\Delta} \\ & \stackrel{y}{0} \end{aligned}$ | W. <br> E. <br> W. <br> E. | $4^{\text {h }} 40^{\text {m }}$ | $59 .{ }^{\circ}$ | $\begin{array}{r} \mathrm{I} 4 \mathrm{I}^{\mathrm{d}} \cdot 5 \\ 4 \mathrm{I} .5 \\ \mathrm{I} 4 \mathrm{I} .4 \\ 4 \mathrm{I} .4 \end{array}$ | $\begin{gathered} 141^{\mathrm{d}} \cdot 5 \\ 4 \mathrm{I} .5 \end{gathered}$ | 100d.o |  |
|  | E. <br> W. <br> E. <br> W. | $4 \quad 58$ | 56. | $\begin{array}{r} 40.5 \\ \mathbf{1 4 1 . 8} \\ 40.5 \\ \mathbf{4 4 . 6} \end{array}$ | $\begin{array}{r} 40.5 \\ 141.7 \end{array}$ | 101.2 | $\begin{gathered} \stackrel{\sim}{i} \\ \text { II. } \end{gathered}$ |
|  | eans |  | 57.5 |  | $2 \mathrm{u}^{\text {d }}$ | 100.60 |  |



Horizontal Intensity．Observations of Deflections．
St．Thomas，November 13 ， 1865.
St．Thomas，November I3， 1865 ．


St．Thomas，November 16, I 865.

| $\begin{aligned} & \stackrel{\rightharpoonup}{\ddot{0}} \\ & \text { E. } \\ & \text { تٌ } \end{aligned}$ | 吂 | Time． | Temp． <br> $t$ |  |  | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \dot{\ddot{0}} \\ & \stackrel{y}{3} \end{aligned}$ | W． <br> E． <br> W． <br> E． | $12^{\text {h }} 10^{\text {m }}$ | $90 .{ }^{\circ}$ | $\begin{array}{r} 43^{\mathrm{d}} .6 \\ 10.3 \\ 43.7 \\ 105.3 \end{array}$ | $\begin{aligned} & 43^{\mathrm{d}} .6 \\ & 105 \cdot 3 \end{aligned}$ | $61^{\text {d }} .7$ | $\begin{aligned} & \text { せ } \\ & 0 \\ & \dot{i} \\ & \\| \\ & i \end{aligned}$ |
|  | $\begin{aligned} & \text { E. } \\ & \text { W. } \\ & \text { E. } \\ & \text { W. } \end{aligned}$ | $12 \quad 20$ | 87. | $\begin{array}{r} \text { 105.6 } \\ 43.9 \\ \text { 105.5 } \\ 43.8 \end{array}$ | $\begin{array}{r} 105.5 \\ 43.8 \end{array}$ | 61.7 |  |
|  | eans |  | 88.5 |  | $2 u^{\text {d }}$ | 61.70 |  |

Coefficient of torsion，$v=4.55$ div．

| Salute Islands，November 28， 1865. |  |  |  |  |  |  |  | Salute Islands，November 28， 8865. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | تٌ 둔 | Time． | Temp． <br> $t$ |  | 華菏 | Diff＇s． | Dist． |  | 둥멸 | Time． | Temp． $t$ |  |  | Diff＇s． | Dist． |
| $\begin{aligned} & \dot{0} \\ & \stackrel{\rightharpoonup}{0} \end{aligned}$ | W． <br> E． <br> W． <br> E． | $12^{\text {h }} 15$ | $91 .{ }^{\circ}$ | $\begin{array}{r} 4 \mathrm{I}^{\mathrm{d}} .1 \\ 102.5 \\ 4 \mathrm{II} . \mathrm{I} \\ 102.5 \end{array}$ | $\begin{aligned} & 4 \mathrm{I}^{\mathrm{d}} \cdot \mathrm{I} \\ & 102.5 \end{aligned}$ | $61^{\text {d }} \cdot 4$ |  | 苞 | W． E． W． E． L | $12^{\text {h }} 25^{\text {m }}$ | 90．${ }^{\circ}$ | $\begin{aligned} & 56^{\mathrm{d}} .3 \\ & 87.8 \\ & 56.3 \\ & 87.8 \end{aligned}$ | $\begin{aligned} & 56^{\mathrm{d}} \cdot 3 \\ & 87.8 \end{aligned}$ | $31^{\text {d }} \cdot 5$ |  |
|  | E． <br> W． <br> E． <br> W． | $12 \quad 25$ | 90. | 102． <br> 14 <br> 41.3 <br> 102.9 <br> 41.3 | 102.8 41.3 | 61．5 | $\begin{aligned} & \text { io } \\ & \text { il } \\ & \text { in } \end{aligned}$ | $\begin{aligned} & \dot{y} \\ & \text { 舀 } \end{aligned}$ | $\begin{aligned} & \mathrm{E} \\ & \mathrm{~W} . \\ & \mathrm{E} . \\ & \mathrm{W} . \end{aligned}$ | 1235 | 89. | 88.0 56.4 88.0 56.4 | 88.0 56.4 | 31.6 | $\begin{aligned} & \text { N } \\ & \\| \\ & \\| \end{aligned}$ |
|  | eans |  | 90.5 |  | $2 u^{\text {d }}$ | 61.45 |  |  | Ceans |  | 89.5 |  | $2 \mathrm{u}^{\text {d }}$ | 31.55 |  |

St．Thomas，November i6， 1865.

|  |  | Time． | Temp． $t$ |  |  | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \stackrel{\rightharpoonup}{0} \\ & \stackrel{y}{*} \end{aligned}$ | $\begin{aligned} & \text { W. } \\ & \text { E. } \\ & \text { W. } \\ & \text { E. } \end{aligned}$ | $12^{\text {h }} 20^{\text {m }}$ | $87 .{ }^{\circ}$ | $\begin{aligned} & 5^{\mathrm{d}} .7 \\ & 90.4 \\ & 58.6 \\ & 90.4 \end{aligned}$ | $\begin{aligned} & 5^{8 \mathrm{~d} .6} \\ & 90.4 \end{aligned}$ | $31^{\text {d }} .8$ |  |
| $\begin{gathered} \text { 菏 } \\ \text { 第 } \end{gathered}$ | $\begin{aligned} & \text { E. } \\ & \text { W. } \\ & \text { E. } \\ & \text { W. } \end{aligned}$ | 1230 | 87. | $\begin{aligned} & 90.4 \\ & 59.1 \\ & 90.5 \\ & 58.9 \end{aligned}$ | $\begin{aligned} & 90.4 \\ & 59.0 \end{aligned}$ | 31.4 | $\begin{aligned} & \text { n } \\ & \\| \\ & i \end{aligned}$ |
|  | eans |  | 87.0 |  | $2 \mathrm{u}^{\text {d }}$ | 31.60 |  |

Salute Islands，November 28， 5865.

Horizontal Intensity. Observations of Deflections.


Horizontal Intensity．Observations of Deflections．

Rio Janeiro，January 6， 1866.


| Monte Video，January 18 ， 1866. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 茫 | Time． | Temp． |  | 苞 | Diff＇s． | Dist． |
| $\begin{aligned} & \dot{B} \\ & \stackrel{B}{B} \end{aligned}$ | $\begin{aligned} & \text { W. } \\ & \text { E. } \\ & \text { W. } \\ & \text { E. } \end{aligned}$ | $4^{\mathrm{h}} 35^{\mathrm{m}}$ | $87^{\circ}$ | $\begin{array}{r} 37^{\mathrm{d}} .2 \\ 155.9 \\ 37.4 \\ 106.0 \end{array}$ | $37^{\text {d }} \cdot 3$ ro6．0 | 68d． 7 |  |
| $\begin{aligned} & \text { 荡 } \\ & \text { 品 } \end{aligned}$ | $\begin{aligned} & \text { E. } \\ & \text { W. } \\ & \text { E. } \\ & \text { W. } \\ & \hline \end{aligned}$ | 445 | 87 | $\begin{array}{r} 106.0 \\ 37.7 \\ 105.9 \\ 38.3 \end{array}$ | 106.0 38.0 | 68.0 | $\stackrel{\text { II }}{\text {－}}$ |
|  | eans |  | 87.0 |  | $2 \mathrm{u}^{\text {d }}$ | 68.35 |  |

Coefficient of torsion，$v=4.50 \mathrm{div}$ ．

| Sandy Point，February 7, I 866 ． |
| :--- |

Rio Janeiro，January 6， 1866.

|  | ت | Time． | Temp． |  | 苂宊 | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \dot{w} \\ & \stackrel{\rightharpoonup}{0} \end{aligned}$ | W． E． W． E． | $6^{\mathrm{h}} 1 \mathrm{I}^{\mathrm{mm}}$ | $74^{\circ}$ | $\begin{aligned} & 56^{\mathrm{d} .2} \\ & 92.0 \\ & 56.2 \\ & 9 \mathrm{I} .8 \end{aligned}$ | $\begin{aligned} & 56^{\mathrm{d}} .2 \\ & 9 \mathrm{I} .9 \end{aligned}$ | $35^{\text {d }} \cdot 7$ | $$ |
|  |  |  | 2 |  |  |  |  |
| $\begin{aligned} & \text { 菏 } \\ & \text { un } \end{aligned}$ | E． W． E． W． | $6 \quad 20$ | 74 | 92.0 56.2 92.2 56.2 | 92.1 56.2 | $35 \cdot 9$ |  |
| Means |  |  | 74.0 |  | $2 \mathrm{u}^{\text {d }}$ | 35.80 |  |

Monte Video，January 18， 1866.

|  |  | Time． | Temp． |  |  | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \dot{y} \\ & \stackrel{y}{0} \end{aligned}$ | W． <br> E． <br> W． <br> E． | $4^{\text {h }} 45^{m}$ | $87^{\circ}$ | $\begin{aligned} & 54^{\mathrm{d}} \cdot 4 \\ & 89.5 \\ & 54.4 \\ & 89.4 \end{aligned}$ | $\begin{aligned} & 54^{\mathrm{d}} \cdot 4 \\ & 89.5 \end{aligned}$ | $35^{\text {d }}$ ． 1 | $\pm$ <br>  <br>  <br> $i$ <br> $i$ |
| $\begin{aligned} & \text { 䓲 } \\ & \text { 號 } \end{aligned}$ | E． <br> W． <br> E． <br> W． | 455 | 88 | $\begin{aligned} & 89.7 \\ & 54.7 \\ & 89.6 \\ & 54.6 \end{aligned}$ | $\begin{aligned} & 89.6 \\ & 54.6 \end{aligned}$ | 35.0 |  |
|  | eans |  | 87.5 | $2 u^{\text {d }}$ |  | 35.05 |  |

Sandy Point，February 7， 1866.

15 Juty， 1872.

Horizontal Intensity. Observations of Deflections.
Valparaiso, March 2, 1866.
Valparaiso, March 2, 1866.



Horizontal Intensity. Observations of Deflections.


Horizontal Intensity．Observations of Deflections．
Sarı Lorenzo Island，April 26， 1866.

|  |  | Time． | Temp． $t$ |  | 苂号 | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 苍 | W． E． W． E． | $\mathrm{II}^{\text {h }} 4 \mathrm{O}^{\text {m }}$ | $79^{\circ}$ | $\begin{array}{r} 51^{\mathrm{d} .0} \\ \text { 109.7 } \\ 50.9 \\ \text { 109.6 } \end{array}$ | $\begin{array}{r} 50^{d} .9 \\ 109.6 \end{array}$ | $5^{88.7}$ |  |
|  | E． W． W． E． W． | II 52 | 82 | 110.4 50.9 IIO．4 50.7 | 110.4 50.8 | 59.6 | $\stackrel{\text { iI }}{\stackrel{1}{n}}$ |
|  | eans |  | 80.5 |  | $2 \mathrm{u}^{\text {d }}$ | 59.15 |  |
| Coefficient of torsion，$v=4.25$ div． |  |  |  |  |  |  |  |

San Lorenzo Island，April 26， 1866.

|  | 殸 | Time． | Temp． |  | 苂菏 | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | W． E． W． E． | $1 \mathrm{I}^{\mathrm{h}} 5^{\text {m }}$ | $82^{\circ}$ | 65.3 95.4 65.0 94.9 | $\begin{gathered} 65^{\mathrm{d}} \cdot \mathrm{I} \\ 95 \cdot \mathrm{I} \end{gathered}$ | $30^{\text {d }}$ ． | $\begin{aligned} & \dot{4} \\ & \text { N } \\ & \text { i } \\ & \\| \\ & i \end{aligned}$ |
| $\begin{aligned} & \dot{H} \\ & \text { 菏 } \end{aligned}$ | E． W． E． W． | 127 | 74 | 95.4 64.8 95.4 65.0 | 95.4 64.9 | 30.5 |  |
|  | eans |  | 78.0 |  | $2 u^{\text {d }}$ | 30.25 |  |



Flamenco Island，Panama Bay，May 14， 1866.

|  | 㐖艺 | Time． | Temp． $t$ |  | 苂 | Diff＇s． | Dist． |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $\begin{aligned} & \dot{0} \\ & \dot{3} \end{aligned}$ | W． <br> E． <br> W． <br> E． | $7^{\text {h }} 55^{\text {m }}$ | ． $83^{\circ}$ | $\begin{array}{r} 55^{\mathrm{d} .7} \\ \text { 104.6 } \\ 51.0 \\ \text { 104.7 } \end{array}$ | $\begin{array}{r} 50^{\mathrm{d}} .8 \\ 104.6 \end{array}$ | $53^{\text {d }} .8$ |  |
| $\begin{aligned} & \stackrel{\rightharpoonup}{4} \\ & \text { 舀 } \end{aligned}$ | E． <br> W． <br> E． <br> W． | 85 | 82 | $\begin{array}{r} 105.6 \\ 5.4 \\ 105.5 \\ 50.1 \end{array}$ | 105.5 52.2 | 53.3 | $\begin{aligned} & \text { O} \\ & \text { í } \\ & \\| \end{aligned}$ |
|  | eans |  | 82.5 |  | $2 \mathrm{u}^{\text {d }}$ | 53.55 |  |



Horizontal Intensity. Observations of Deflections.

| Acapulco, May 30, I 866. |
| :--- |

Horizontal Intensity. Observations of Deflections.


## SECTION V. OBSERVATIONS ON THE MAGNETISM OF THE SHIP.

The Monadnock is a second rate iron-clad vessel, of the Monitor type, of 1564 tons old or 1091 tons new measurement. On deck her length is 260.5 feet, and her breadth 52.0 feet. She has a wooden hull, but her deck is covered by three layers of iron plates, each one inch thick; and her sides, for a depth of five feet from the deck, are covered by six layers of iron plates, each one inch thick. Thus the deck is protected by three, and the sides by six inches of iron. She is provided with two iron turrets, cylindrical in form, each 22.8 feet in outside diameter, 9.0 feet high, and 11 inches thick. On top of each of them stands an iron pilot-house, 7.7 feet in outside diameter, 6.4 feet high, and 11 inches thick. Each of these pilot-houses is cylindrical in form, and so placed that its axis coincides with the axis of the turret upon which it stands. The sides of the turrets and pilot-houses are not solid, but are composed of iron plates, each one inch thick, placed one upon the other and bolted together till a total thickness of eleven inches is attained. To each of the iron pilot-houses are bolted wooden stanchions, which carry wooden pilot-houses whose floors are about nine and a half feet above the tops of the iron pilot-houses. The centres of the wooden pilot-houses are respectively in the same vertical lines with the centres of the turrets and iron pilot-houses over which they stand. The centres of the turrets coincide with the midships line. The distance from the stern of the vessel to the centre of the after turret is 84.5 feet; from the centre of the after turret to the centre of the forward turret, 99.1 ; and from the centre of the forward turret to the cut-water, 76.9 feet. Passing forward from the after turret, we come first to the ventilator, which is 6.5 feet in diameter, and 22.8 feet high above the deck; and then to the smoke-stack, which is 9.9 feet in diameter, and 31.0 feet high above the deck, both it and the ventilator being of iron. The distance from the centre of the after turret to the centre of the ventilator is 31.3 feet; from the centre of the ventilator to the centre of the smoke-stack, 16.5 feet; and from the centre of the smoke-stack to the centre of the forward turret, 51.3 feet.

At St. Thomas, before the magnetic observations on board ship were made at that place, a wooden mast 77.7 feet high was placed on the ship in order to enable her to carry some sail. Its centre is 22 feet forward of the centre of the forward turret, and what little iron was used in its construction is so placed that it is not at all probable that it affected the deviation of the compasses in its neighborhood in the slightest.

The following are the designations and positions of the compasses which were used during the cruise:--

The Forward Alidade was a Sands Alidade Compass, and was on top of the forward wooden pilot-house, 33.5 feet above the iron deck.

The Forward Binnacle was a Ritchie Liquid Compass, and was in the binnacle of the forward wooden pilot-house, 27.2 feet above the iron deck.

The Forward Ritchie was a Ritchie Monitor Compass, and was 6.7 feet above the top of the iron pilot-house on the forward turret. It was 22.1 feet above the iron deck.

Of these three compasses, the Forward Alidade and Forward Ritche were placed exactly in the vertical line passing through the centre of the forward turret, and the Forward Binnacle was placed about two feet further forward, but nearly in the same vertical plane.

The Admiralty Standard Compass was on top of the after wooden pilot-house, 37.0 feet above the iron deck.

The After Binnacle was a Ritchie Liquid Compass, and was in the binnacle of the after wooden pilot-house, 27.2 feet above the iron deck.

The After Ritchie was a Ritchie Monitor Compass, and was 6.7 feet above the top of the iron pilot-house on the after turret. It was 22.1 feet above the iron deck.

Of these three compasses, the Admiralty Standard and After Ritchie were placed exactly in the vertical line passing through the centre of the after turret, and the After Binnacle was placed about two feet futher forward, but nearly in the same vertical plane.

The After Azimuth was a common Azimuth Compass which was set up temporarily on the quarter deck every time the ship was swung; small cavities having been cut in the iron surface of the deck for the reception of the feet of the tripod, so as to make sure that the instrument always occupied precisely the same position. It stood 47.5 feet abaft the centre of the after turret, and there were two vertical iron stanchions, each two inches in diameter, 10.3 feet high above the deck, and 12.1 feet distant from the compass, one of them being directly forward and the other directly aft of it. This compass was elevated 4.6 feet above the iron deck; but when observations of magnetic force were made, it was necessary to remove it and substitute an Admiralty Standard Compass, which occupied precisely the same position, except that it was 4.8 feet above the deck. When the dip circle was used it also stood 4.8 feet above the deck.

It will be observed that all the compasses stood in the midships line, no matter what their elevation above the deck might be.

All the observations for determining the deviations of the compasses were made by swinging the ship in the following manner: The true azimuth of a well defined distant. object was determined by a solar bearing, as explained in Section III, page 26 , and the declination of the magnetic needle having been applied to it, its true magnetic azimuth became known; then, supposing the sight vanes of the Admiralty Standard Compass to be kept pointed steadily to that object while the ship was swung, the reading which they would indicate on the azimuth circle attached to
the cover of the compass, as the ship's head pointed successively to each of the true magnetic points, was computed by means of the formula

$$
R=180^{\circ}+A-\zeta
$$

where
$R=$ reading of sight vanes on the azimuth circle attached to the cover of the compass.
$A=$ true magnetic azimuth of the distant object; the azimuth being counted from the south around by the west.
$\zeta=$ azimuth of the ship's head, counted from the correct magnetic north around by the east.

This having been done, on a tolerably calm day steam was got up in the boilers, and, the vessel riding at a single anchor, slack water was waited for. As soon as the tide ceased to run, the executive officer took the deck; an officer was stationed at each of the compasses; I went to the Admiralty Standard; and a quartermaster was stationed at the ship's bell. Then the helm was put hard-a-starboard, or hard-a-port, depending on the direction in which it was desired to have her head swing, and the engines having bẹen started, one forward and the other backward (the Monadnock was provided with twin screws which were entirely independent of each other), the vessel at once began to turn, without bringing any considerable strain on her cable. Her motion was perfectly under control, and could be made fast or slow at pleasure by merely varying the speed of the engines. I then set the sight vanes of the Admiralty Standard Compass to the reading (on the azimuth circle) of the point at which the ship's head would first arrive, and placing my eye to them I watched for the instant when they pointed to the distant object chosen as an azimuth mark. As the thread of the sight vane approached the object I cautioned the quartermaster to be ready, and at the instant it covered the object I made a signal, by dropping my outstretched arm, and the quartermaster struck a single stroke on the bell. Upon hearing this, every officer at once read off and recorded the heading of the ship, as indicated by the compass at which he was stationed. Then, the engines not having been stopped, I turned the sight vanes forward to the reading of the next point, and the same process was repeated; and so on, till the readings of all the compasses had been observed at each of the thirty-two points, which was generally accomplished in about an hour, or an hour and a half. The difference between any observed reading and the true point to which the vessel's head was rirected at the time that reading was made, was of course the deviation of the compass on that point.

The forward iron and woqden pilot-houses were fixed and did not revolve with the turret, so that the lubber lines of the compasses in them always remained in the same position. But with the after iron and wooden pilot-houses the case was different. They were attached to the turret and revolved with it, and by so doing caused the lubber lines of the compasses in them also to revolve. As the turrets were frequently turned, it became necessary to establish marks by which the position of the after one could always be referred to some fixed position, so that a correction could be applied to the readings of the compasses in its pilot-houses to

16 August, 1872.
reduce them to what they would have been if their lubber lines had not moved For this purpose, whenever the ship was swung, a fixed line on the under side of the hurricane deck was produced till it touched the after turret, and then the distance from its point of contact with the turret to a joint (marked number XII) on the outside of the turret was measured. This distance, having been converted into degrees and minutes by means of the known diameter of the turret, was the correction to be applied to the position of the lubber lines. The following table gives the measured distance, and its angular equivalent, at every station where the ship was swung; but it must be noticed that these corrections apply only to the After Binnacle and After Ritchie Compasses. The lubber line of the Admiralty Standard Compass was always properly adjusted before beginning to observe.


When the ship was being swung, I always read the Admiralty Standard Compass myself. Each of the other compasses was usually read by the officer whose name is set opposite to it in the following table.

> Forward Alidade, Forward Binnacle, Forward Ritchie, After Binnacle, After Ritchie, After Azimuth,

Lieutenant M. Miller.
Lieut. Miller, assisted by a Quartermaster.
Lieutenant Geo. Smith.
Ensign F. Wildes.
Master Wm. Barrymore.
Mate Jno. Ponte.

My instruments for the measurement of magnetic force restricted me to the method of deflections, and the only compasses on board at which that method could be applied were the Admiralty Standard and the After Azimuth. As the ship was always riding at anchor, and of course swinging a little, when such observations were made, in order to render them as accurate as possible the following plan was adopted.

The deflecting bar was screwed to the movable circle which carried the sight vanes of the Admiralty Standard Compass in such a position as to be at right angles to them. That is, when the sight vanes pointed north and south the deflecting bar pointed east and west. Then, $1^{\circ}$. The sights being directed exactly
north and south, as indicated by the compass card, the point, which we will designate by $H$, cut by them on the northern or southern horizon, as might be most convenient, was noted. $2^{\circ}$. The deflecting magnets were placed in the carriers, one to the east and the other to the west of the compass card, both being at the same distance from the centre of the card, and with their similar poles pointing in the same direction. Then, keeping the sight vanes pointed steadily to the object $H$, as soon as the compass card ceased to vibrate it was read off by means of the prism attached to the sight vane. Let this reading be designated as $A .3^{\circ}$. Each deflecting magnet was reversed, end for end, in its own carrier, and, the sight vanes being still kept directed to the object $H$, the card was again read. Let this reading be designated as $B$. Then the observed angle of deflection is $\frac{A-B}{2}$.

The dip was obtained by removing the Admiralty Standard Compass with which the deflections had been observed, and putting in its place a dip circle; the axle of the dipping needle occupying precisely the same position that had previously been occupied by the pivot of the compass card.

The observations of the deviations of the compasses made during the cruise have been compared with the following theory, which is taken from the English Admiralty Manual of the Deviations of the Compass, edition of 1863.
Let
$X, Y, Z$, represent the force of the earth's magnetism drawing the north point of the compass needle to the ship's head, to the starboard side and vertically downwards.
$X^{\prime}, Y^{\prime}, Z^{\prime}$, represent the combined force of the magnetism of the earth and ship in the same directions.
$a, b, c, d, e, f, g, h, k$, represent constant coefficients depending on the amount and arrangement of the soft iron of the ship.
$P, Q, R$, represent constant coefficients depending on the amount, arrangement, and independent magnetism of the hard iron of the ship.
$H=$ the horizontal force of the earth.
$H^{\prime}=$ the horizontal force of the earth and ship.
$\theta=$ the dip.
$\zeta=$ azimuth of the ship's head measured eastward from the correct magnetic north.
$\zeta^{\prime}=$ azimuth of the ship's head measured from the direction of the disturbed needle.
$\delta=\zeta-\zeta^{\prime}=$ the deviation of the compass.
Then the whole mathematical theory of the deviations of the compass is comprised in the three following equations:

$$
\begin{align*}
& X^{\prime}=X+a X+b Y+c Z+P  \tag{1}\\
& Y^{\prime}=Y+d X+e Y+f Z+Q  \tag{2}\\
& Z^{\prime}=Z+g X+h Y+k Z+R \tag{3}
\end{align*}
$$

We have also

$$
\begin{array}{ll}
\mathbf{X}=H \cos \zeta, & Y=-H \sin \zeta,
\end{array} \quad Z=H \tan \theta
$$

Substituting these values in equations (1), (2), and (3), and dividing by $H$, we have

$$
\begin{align*}
\frac{H^{\prime}}{H} \cos \zeta^{\prime} & =(1+a) \cos \zeta-b \sin \zeta+c \tan \theta+\frac{P}{\bar{H}}  \tag{4}\\
-\frac{H}{H} \sin \zeta^{\prime} & =d \cos \zeta-(1+e) \sin \zeta+f \tan \theta+\frac{Q}{H}  \tag{5}\\
\frac{Z^{\prime}}{\bar{H}} & =g \cos \zeta-h \sin \zeta+(1+k) \tan \theta+\frac{R}{\bar{H}} \tag{6}
\end{align*}
$$

Equation (6) may be written

$$
\begin{equation*}
0=1-\frac{Z^{\prime}}{Z}+g \frac{\cos \zeta}{\tan \theta}-\pi \frac{\sin \zeta}{\tan \theta}+\pi+\frac{R}{Z} \tag{6a}
\end{equation*}
$$

From equations (4) and (5) we obtain the following:
(4) $\cos \zeta-(5) \sin \zeta$ gives after some reductions

$$
\begin{gather*}
H^{\prime} \cos \delta=1+\frac{a+e}{2}+\left(c \tan \theta+\frac{P}{H}\right) \cos \zeta-\left(f \tan \theta+\frac{Q}{H}\right) \sin \zeta \\
+\frac{a-e}{2} \cos 2 \zeta-\frac{a+b}{2} \sin 2 \zeta
\end{gather*}
$$

(4) $\sin \zeta+(5) \cos \zeta$ gives after some reductions

$$
\begin{gather*}
\frac{H^{\prime}}{H} \sin \delta=\frac{d-b}{2}+\left(c \tan \theta+\frac{P}{H}\right) \sin \zeta+\left(f \tan \theta+\frac{Q}{H}\right) \cos \zeta \\
+\frac{a-e}{2} \sin 2 \zeta+\frac{d+b}{2} \cos 2 \zeta \tag{8}
\end{gather*}
$$

Now let

$$
\begin{array}{rlrl}
1+\frac{a+e}{2} & =\lambda & \frac{d-b}{2} & =\lambda \mathfrak{H} \\
\frac{a-e}{2} & =\lambda \mathfrak{D} & \frac{d+b}{2} & =\lambda \mathfrak{G} \\
c \tan \theta+\frac{P}{H} & =\lambda \mathfrak{B} & f \tan \theta+\frac{Q}{H} & =\lambda \mathfrak{C}
\end{array}
$$

Then from equations (7) and (8) we get the following:

$$
\begin{align*}
\frac{H}{\lambda H} \cos \delta & =1+\mathfrak{B} \cos \zeta-\mathfrak{C} \sin \zeta+\mathfrak{D} \cos 2 \zeta-\mathfrak{C} \sin 2 \zeta  \tag{9}\\
\frac{H^{\prime}}{\lambda H} \sin \delta & =\mathfrak{A}+\mathfrak{B} \sin \zeta+\mathfrak{C} \cos \zeta+\mathfrak{D} \sin 2 \zeta+\mathfrak{E} \cos 2 \zeta \tag{10}
\end{align*}
$$

Dividing (10) by (9),

$$
\begin{equation*}
\tan \delta=\frac{\mathfrak{A}+\mathfrak{B} \sin \zeta+\mathfrak{C} \cos \zeta+\mathfrak{D} \sin 2 \zeta+\mathfrak{C} \cos 2 \zeta}{1+\mathfrak{B} \cos \zeta-\mathfrak{C} \sin \zeta+\mathfrak{D} \cos 2 \zeta-\mathfrak{C} \sin 2 \zeta} \tag{11}
\end{equation*}
$$

From (11) we easily get

$$
\begin{align*}
\sin \delta & =\mathfrak{A} \cos \delta+\mathfrak{B} \sin \zeta^{\prime}+\mathfrak{C} \cos \zeta^{\prime}+\mathfrak{D} \sin \left(\zeta+\zeta^{\prime}\right)+\mathfrak{F} \cos \left(\zeta+\zeta^{\prime}\right)  \tag{12}\\
& =\mathfrak{A} \cos \delta+\mathfrak{B} \sin \zeta^{\prime}+\mathfrak{C} \cos \zeta^{\prime}+\mathfrak{D} \sin \left(2 \zeta^{\prime}+\delta\right)+\mathfrak{C} \cos \left(2 \zeta^{\prime}+\delta\right)
\end{align*}
$$

Of the last three equations (11) is used when the deviations are given on the correct magnetic points, (12) when the deviations are given on the compass points affected by deviation.

Equation (12) may be put under the following form, which is sometimes convenient, and which is very nearly exact, viz.:
$\sin \delta=\frac{1}{1-\mathfrak{D} \cos 2 \zeta^{\prime}}\left\{\mathfrak{N}+\mathfrak{B} \sin \zeta^{\prime}+\mathfrak{C} \cos \zeta^{\prime}+\mathfrak{D} \sin 2 \zeta^{\prime}+\mathfrak{C} \cos 2 \zeta^{\prime}\right\}$
By means of the expressions for $\sin \delta$ we may calculate the values of the coefficients $\mathfrak{A}, \mathfrak{B}, \mathfrak{C}, \mathfrak{D}$, $\mathfrak{C}$, if we know the deviations on five points. If we have the deviations on more than five points, we may determine the most probable values of the coefficients by the method of least squares; but the calculation will in general be long and difficult.

If, however, the compass points on which the deviations are given divide the circumference into equal parts, we may determine the exact coefficients $\mathfrak{A}, \mathfrak{F}, \mathfrak{C}, \mathfrak{D}, \mathfrak{G}$, with great ease, and a sufficient degree of approximation, by determining first the approximate coefficients $A, B, C, D, E$, and then deducing from them the values of the exact coefficients. For that purpose we proceed as follows:

If the coefficients are less than $20^{\circ}$ their squares and products may be neglected, and equation (12) may be put under the form

$$
\begin{equation*}
\delta=A+B \sin \zeta^{\prime}+C \cos \zeta^{\prime}+D \sin 2 \zeta^{\prime}+E \cos 2 \zeta^{\prime} \tag{13}
\end{equation*}
$$

Let $\delta_{0} \delta_{1} \delta_{2} \ldots \delta_{31}$ be the deviations observed on the 32 points, by compass, $S_{1} S_{2} S_{3}$ $\ldots S_{7}$ the natural sines of the rhumbs or of the angles $11^{\circ} 15^{\prime}, 22^{\circ} 30^{\prime} \ldots 78^{\circ} 45^{\prime}$ respectively, then if the observations have been made on the 32 points we have the following 32 equations from which to determine $A, B, C, D, E$.

| Compass Courses. | Deviation. | $A$ | $+B \sin \zeta^{\prime}$ | $+C \cos \zeta^{\prime}$ | + D and $2 \zeta$ | $+E \cos 2 \zeta^{\prime}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| North | $\delta_{0}$ | A |  | + C |  | + E |
| N. by E. | $\delta_{1}$ | A | $+\mathrm{BS}$ | $+\mathrm{CS}_{7}$ | $+\mathrm{DS}$ | $+\mathrm{ES}_{6}$ |
| N. N. E. | $\delta_{2}$ | A | + $\mathrm{BS}_{2}$ | $+\mathrm{CS}_{6}$ | $+\mathrm{DS}_{4}$ | $+\mathrm{ES}_{4}$ |
| N. E. by N. | $\delta_{3}$ | A | $+B S_{3}$ | $+\mathrm{CS}_{5}$ | + D S | $+\mathrm{ES}_{2}$ |
| N. E. | $\delta_{4}$ | A. | + B $\mathrm{S}_{4}$ | $+\mathrm{CS}_{4}$ | $+\mathrm{D}$ |  |
| N. E. by E. | $\delta_{5}$ | A | + B S | $+\mathrm{CS}_{3}$ | $+\mathrm{DS}_{6}$ | - $\mathrm{ES}_{2}$ |
| E. N. E. | $\delta_{6}$ | A | + B $\mathrm{S}_{6}$. | $+\mathrm{CS}_{2}$ | $+\mathrm{DS}_{4}$ | $-\mathrm{ES}_{4}$ |
| E. by N. | $\delta_{7}$ | A | + B S ${ }_{7}$ | + $\mathrm{CS} \mathrm{S}_{1}$ | $+\mathrm{DS}$ | - E S ${ }_{6}$ |
| East | $\delta_{8}$ | A | + B |  |  | - E |
| E. by S. | $\delta_{9}$ | A | $+\mathrm{BS}{ }_{7}$ | $-\mathrm{CS}_{1}$ | $-\mathrm{DS}_{2}$ | - E S ${ }_{6}$ |
| E. S. E. | $\delta_{10}$ | A | + $\mathrm{BS}_{6}$ | $-\mathrm{CS}_{2}$ | - D S ${ }_{4}$ | $-\mathrm{ES}_{4}$ |
| S. E. by E. | $\delta_{11}$ | A | + B S | $-\mathrm{CS}_{3}$ | - D S | $-\mathrm{ES}_{2}$ |
| S. E. | $\delta_{12}$ | A | + B S | - $\mathrm{CS}_{4}$ | $-\mathrm{D}$ |  |
| S. E. by S. | $\delta_{13}$ | A | + $\mathrm{BS}_{3}$ | $-\mathrm{CS}_{5}$ | $-\mathrm{DS}_{6}$ | $+\mathrm{ES}_{2}$ |
| S. S. E. | $\delta_{14}$ | A | $+\mathrm{BS}_{2}$ | $-\mathrm{CS}_{6}$ | $-\mathrm{DS}_{4}$ | $+\mathrm{ES}_{4}$ |
| S. by E. | $\delta_{15}$ | A | + B S | $-\mathrm{CS}_{7}$ | -D S | $+\mathrm{ES}_{6}$ |
| South | $\delta_{16}$ | A |  | - C |  | $+\mathrm{E}$ |
| S. by W. S. S. W. | $\delta_{17}$ | A | - B S | $-\mathrm{CS}_{7}$ | $+\mathrm{DS}_{2}$ | $+\mathrm{ES}_{6}$ |
| S. S. W. S. W. by S. | $\delta_{18}$ $\delta_{89}$ | A | - $\mathrm{BS}_{2}$ | - $\mathrm{CS}_{6}$ | $+\mathrm{DS}_{4}$ +DS | $+\mathrm{ESS}_{4}$ +ESS |
| S. W. by S. S. W. | $\delta_{19}$ $\delta_{20}$ | A | - ${ }^{-\mathrm{BS}_{3}}$ | - $\mathrm{CS}_{5}$ | + ${ }^{\text {D }} \mathrm{S}_{6}$ +D | $+\mathrm{ES}_{2}$ |
| S. W. by W. | $\delta_{21}$ | A | - B $\mathrm{S}_{5}$ | $-\mathrm{CS}_{3}$ | $+\mathrm{DS}_{6}$ | $-\mathrm{ES}_{2}$ |
| W. S. W | $\delta_{22}$ | A | - B $\mathrm{S}_{6}$ | $-\mathrm{CS}_{2}$ | $+\mathrm{DS}_{4}$ | - E S |
| W. by S. | $\delta_{23}$ | A | - B S | - $\mathrm{CS}_{1}$ | $+\mathrm{DS}_{2}$ | - E S ${ }_{6}$ |
| West | $\delta_{24}$ | A | - B |  |  | - E |
| W. by N. | $\delta^{25}$ | A | - B Sy | $+\mathrm{CS}_{1}$ | - D S | - E S ${ }_{6}$ |
| W. N. W. | $\delta_{26}$ | A | - B S ${ }_{6}$ | $+\mathrm{CS}_{3}$ | $-\mathrm{DS}_{4}$ | - E S |
| N. W. by W. | $\delta_{27}$ | A | - B S ${ }_{5}$ | $+\mathrm{CS}_{3}$ | $-\mathrm{D} \mathrm{S}_{6}$ | $-\mathrm{ES}_{3}$ |
| N. W. | $\delta^{23}$ | A | - B S | $+\mathrm{CS}_{4}$ | -D |  |
| N. W. by N. | $\delta_{29}$ | A | - $\mathrm{BS}_{3}$ | + $\mathrm{CS}_{5}$ | $-\mathrm{DS}_{6}$ | $+\mathrm{ES}_{2}$ |
| N. N. W. N. by W. | $\delta_{30}$ | A | - $\mathrm{BS}_{2}$ | $+\mathrm{CS}_{6}$ | $-\mathrm{DS}_{4}$ | $+\mathrm{ES}_{4}$ |
| N. by W. | $\delta_{31}$ | A | - B S | $+\mathrm{CS}_{7}$ | -D $\mathrm{S}_{2}$ | + E S ${ }_{6}$ |

By the method of least squares we obtain, from these 32 equations of condition, the five normal equations

$$
\begin{aligned}
& \delta_{0}+\delta_{1}+\delta_{2} \ldots \ldots . . . . . .+\delta_{31}=32 A . \\
& \delta_{1} S_{1}+\delta_{2} S_{2}+\delta_{3} S_{3}+\& c \ldots \ldots=16 B . \\
& \delta_{1}+\delta_{1} S_{7}+\delta_{2} S_{6}+\& c . \ldots . . . .=16 C . \\
& \delta_{1} S_{2}+\delta_{2} S_{4}+\delta_{3} S_{6}+\& c . \cdots \ldots=16 D . \\
& \delta_{0}+\delta_{1} S_{6}+\delta_{2} S_{4}+\& c . \ldots . . . . .
\end{aligned}
$$

For çonvenience of computation these equations have been put under the form

$$
\begin{aligned}
8 A= & \frac{1}{2}\left(\frac{\delta_{0}+\delta_{16}}{2}+\frac{\delta_{8}+\delta_{24}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{1}+\delta_{17}}{2}+\frac{\delta_{9}+\delta_{25}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{2}+\delta_{18}}{2}+\frac{\delta_{10}+\delta_{26}}{2}\right)
\end{aligned}
$$

$$
\begin{aligned}
& +\frac{1}{2}\left(\frac{\delta_{3}+\delta_{19}}{2}+\frac{\delta_{11}+\delta_{27}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{4}+\delta_{20}}{2} \left\lvert\,+\frac{\delta_{12}+\delta_{28}}{2}\right.\right) \\
& +\frac{1}{2}\left(\frac{\delta_{5}+\delta_{21}}{2}+\frac{\delta_{13}+\delta_{29}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{6}+\delta_{22}}{2}+\frac{\delta_{14}+\delta_{30}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{7}+\delta_{23}}{2}+\frac{\delta_{15}+\delta_{31}}{2}\right) \\
8 B= & \frac{\delta_{8}+\delta_{24}}{2} \\
& +\frac{\delta_{1}-\delta_{17}}{2} S_{1}+\frac{\delta_{9}-\delta_{25}}{2} S_{7} \\
& +\frac{\delta_{2}-\delta_{18}}{2} S_{2}+\frac{\delta_{10}-\delta_{25}}{2} S_{6} \\
& +\frac{\delta_{3}-\delta_{19}}{2} S_{3}+\frac{\delta_{11}-\delta_{27}}{2} S_{5} \\
& +\frac{\delta_{4}-\delta_{20}}{2} S_{4}+\frac{\delta_{12}-\delta_{28}}{2} S_{4} \\
& +\frac{\delta_{5}-\delta_{21}}{2} S_{5}+\frac{\delta_{13}-\delta_{29}}{2} S_{3} \\
& +\frac{\delta_{6}-\delta_{22}}{2} S_{6}+\frac{\delta_{14}-\delta_{30}}{2} S_{2} \\
& +\frac{\delta_{7}-\delta_{23}}{2} S_{7}+\frac{\delta_{15}-\delta_{31}}{2} S_{15} \\
8 C= & \frac{\delta_{0}-\delta_{16}}{2} \\
& +\frac{\delta_{1}-\delta_{17}}{2} S_{7}-\frac{\delta_{9}-\delta_{25}}{2} S_{1} \\
& +\frac{\delta_{2}-\delta_{18}}{2} S_{6}-\frac{\delta_{10}-\delta_{26}}{2} S_{2} \\
& +\frac{\delta_{3}-\delta_{19}}{2} S_{5}-\frac{\delta_{11}-\delta_{27}}{2} S_{3} \\
& +\frac{\delta_{4}-\delta_{20}}{2} S_{4}-\frac{\delta_{12}-\delta_{28}}{2} S_{4} \\
& +\frac{\delta_{7}-\delta_{22}}{2} S_{3}-\frac{\delta_{13}-\delta_{29}}{2} S_{5}-\frac{\delta_{14}-\delta_{30}}{2} S_{5} \\
2 & \frac{\delta_{15}-\delta_{31}}{2} S_{7}
\end{aligned}
$$

$$
\begin{aligned}
4 D= & +\frac{1}{2}\left(\frac{\delta_{4}+\delta_{20}}{2}-\frac{\delta_{12}+\delta_{28}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{1}+\delta_{17}}{2}-\frac{\delta_{9}+\delta_{25}}{2}\right) S_{2}+\frac{1}{2}\left(\frac{\delta_{5}+\delta_{21}}{2}-\frac{\delta_{13}+\delta_{29}}{2}\right) S_{5} \\
& +\frac{1}{2}\left(\frac{\delta_{2}+\delta_{18}}{2}-\frac{\delta_{10}+\delta_{26}}{2}\right) S_{4}+\frac{1}{2}\left(\frac{\delta_{6}+\delta_{22}}{2}-\frac{\delta_{11}+\delta_{30}}{2}\right) S_{4} \\
& +\frac{1}{2}\left(\frac{\delta_{3}+\delta_{19}}{2}-\frac{\delta_{11}+\delta_{27}}{2}\right) S_{6}+\frac{1}{2}\left(\frac{\delta_{7}+\delta_{23}}{2}-\frac{\delta_{15}+\delta_{31}}{2}\right) S_{2} \\
4 E= & \frac{1}{2}\left(\frac{\delta_{0}+\delta_{16}}{2}-\frac{\delta_{8}+\delta_{24}}{2}\right) \\
& +\frac{1}{2}\left(\frac{\delta_{1}+\delta_{17}}{2}-\frac{\delta_{9}+\delta_{25}}{2}\right) S_{6}-\frac{1}{2}\left(\frac{\delta_{5}+\delta_{21}}{2}-\frac{\delta_{13}+\delta_{29}}{2}\right) S_{2} \\
& +\frac{1}{2}\left(\frac{\delta_{2}+\delta_{18}}{2}-\frac{\delta_{10}+\delta_{26}}{2}\right) S_{4}-\frac{1}{2}\left(\frac{\delta_{6}+\delta_{22}}{2}-\frac{\delta_{14}+\delta_{30}}{2}\right) S_{4} \\
& +\frac{1}{2}\left(\frac{\delta_{3}+\delta_{19}}{2}-\frac{\delta_{11}+\delta_{27}}{2}\right) S_{2}-\frac{1}{2}\left(\frac{\delta_{7}+\delta_{23}}{2}-\frac{\delta_{15}+\delta_{31}}{2}\right) S_{6}
\end{aligned}
$$

But the deviations about to be discussed were all observed, not on the compass points, but on the correct magnetic points. Treating them in the manner which has just been described, we obtain the approximate coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, which belong to the correct magnetic points. Then, from equation (11) we get, going to terms of the third order inclusive,

$$
\begin{align*}
& \delta=\mathfrak{A}  \tag{14}\\
& +(\mathfrak{B}+\mathfrak{A} \mathfrak{C}) \sin \zeta+(\mathfrak{C}-\mathfrak{A} \mathfrak{B} \cos \zeta \\
& +\left\{\mathfrak{D}-\frac{\mathfrak{B}^{2}-\mathfrak{C}^{2}}{2}\right\} \sin 2 \zeta+\{\mathfrak{C}-\mathfrak{B} \mathfrak{C}-\mathfrak{A} \mathfrak{D}\} \cos 2 \zeta \\
& +\left\{-\mathfrak{B} \mathfrak{D}+\mathfrak{C} \mathfrak{C}+\frac{\mathfrak{B}^{3}}{3}-\mathfrak{B}^{2}\right\} \sin 3 \zeta \\
& +\left\{-\mathfrak{B} \mathfrak{C}-\mathfrak{C} \mathfrak{D}-\frac{\mathfrak{C}^{3}}{3}+\mathfrak{B}^{2} \mathfrak{C}\right\} \cos 3 \zeta \\
& +\left\{-\frac{D^{2}}{2}+\left(\mathfrak{B}^{2}-\mathfrak{C}^{2}\right) \mathfrak{D}\right\} \sin 4 \zeta+\{-\mathfrak{D} \mathfrak{C}+2 \mathfrak{B} \mathfrak{C} \mathfrak{D}\} \cos 4 \zeta \\
& +\mathfrak{B} \mathfrak{D}^{2} \sin 5 \zeta+\mathfrak{C} \mathfrak{D}^{2} \cos 5 \zeta \\
& +\frac{1}{3} \mathfrak{D}^{3} \sin 6 \zeta
\end{align*}
$$

where $\delta$ is expressed in terms of the arc which is equal to radius. If we suppose the complete expression for $\delta$ to be

$$
\begin{align*}
\delta=A_{1} & +B_{1} \sin \zeta+C_{1} \cos \zeta+D_{1} \sin 2 \zeta+E_{1} \cos 2 \zeta  \tag{15}\\
& +F_{1} \sin 3 \zeta+G_{1} \cos 3 \zeta+H_{1} \sin 4 \zeta+K_{1} \cos 4 \zeta \\
& +L_{1} \sin 5 \zeta+M_{1} \cos 5 \zeta+N_{1} \sin 6 \zeta
\end{align*}
$$

Ther, comparing equation (14) with equation (15), we find, to terms of the third order inclusive,

$$
\begin{aligned}
& \mathfrak{A}=A_{1} \\
& \mathfrak{B}=B_{1}-A_{1} C_{1} \\
& \mathfrak{C}=C_{1}+A_{1} B_{1} \\
& \mathfrak{D}=D_{1}+\frac{B_{1}^{2}-C_{1}^{2}}{2} \\
& \mathfrak{F}=E_{1}+B_{1} C_{1}+A_{1} D_{1} \\
& F_{1}=-B_{1} D_{1}+C_{1} E_{1}-\frac{B_{1}^{3}}{6}-\frac{B_{1} C_{1}^{2}}{2} \\
& G_{1}=-C_{1} D_{1}+B_{1} E_{1} \frac{C_{1}^{3}}{6}+\frac{C_{1} B_{1}^{2}}{2} \\
& H_{1}=-\frac{D_{1}^{2}}{2}+\frac{D_{1} B_{1}^{2}}{2}-\frac{D_{1} C_{1}^{2}}{2} \\
& K_{1}=-D_{1} E_{1}+2 B_{1} C_{1} D_{1} \\
& L_{1}=B_{1} D_{1}^{2} \\
& M_{1}=C_{1} D_{1}^{2} \\
& N_{1}=\frac{1}{3} D_{1}^{3}
\end{aligned}
$$

"When the deviation of the compass is small, the several parts of which it is composed are simply added together; these parts are,

1. $A$, the constant deviation.
2. $B \sin \zeta^{\prime}+C \cos \zeta^{\prime}$, the semicircular deviation.
3. $D \sin 2 \zeta^{\prime}+E \cos 2 \zeta^{\prime}$, the quadrantal deviation.
"When the deviation is large, $\mathfrak{N}, \mathfrak{B}, \mathfrak{C}, \mathfrak{D}, \mathfrak{C}$, or the angles of which these quantities are the natural sines, may still be considered as the constant and as the several parts of the semicircular and the quadrantal deviation, each of these angles being in fact the maximum deviation which would exist if all the other coefficients were zero; but their effects are no longer combined by simple addition."

Before submitting the observed deviations to comparison with the theory, it is necessary to free them from constant errors. These errors originated in two ways.
$1^{\circ}$. When the ship was swung, the variation of the needle at the port where she was lying was seldom accurately known. Hence, in order to obtain the true magnetic azimuth of the object used as an azimuth mark, it was necessary to adopt, for the time being, the best value of the variation which happened to be accessible. In order to facilitate the setting of the sight vanes of the Admiralty Standard Compass while the ship was being swung, the value thus adopted was always so taken that, when the ship's head pointed successively to each of the true magnetic points, the reading of the sight vanes on the azimuth circle attached to the cover of that compass was always either some whole degree or some quarter of a degree. When the declinometer observations were reduced, the true value of the variation of the compass at each port became known, and then it was discovered

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that in some cases the adopted value was in error by more than three degrees. But an error in the adopted value of the variation produced an error of the same amount in the magnetic azimuth of the distant object used as an azimuth mark, and, therefore, in the pointing of the ship's head to each of the true magnetic points. Bearing in mind that the observed deviations were obtained by simply taking the difference between the heading of the ship and the reading of the compass, it will be apparent that if we apply to each observed deviation the difference between the true and adopted variation of the compass, with its proper sign, we shall obtain the true deviations for the directions in which the ship's head actually pointed at the time the readings of the compasses were made. From these corrected deviations the deviations on the true magnetic points can be found by simple interpolation. Therefore, if we let
$m=$ the true, minus the adopted, magnetic azimuth of the distant object used as an azimuth mark: the azimuths being taken as increasing from the south around by the west.
$\delta^{\prime}=$ the observed deviation of the compass when the ship headed in the direction $A$.
$\delta^{\prime \prime}=$ the observed deviation of the compass when the ship headed in the direction $A \mp 11^{\circ} 15^{\prime}$; the upper sign being taken when $m$ is positive, the lower when $m$ is negative.
$\delta=$ the deviation of the compass when the ship heads to the true magnetic point which lies between $A$ and $A \mp 11^{\circ} 15^{\prime}$; that point being of the same name as $A$ was intended to be when the ship was swung.
Then we shall have with sufficient accuracy

$$
\delta=\delta^{\prime}+m \mp \frac{m\left(\delta^{\prime}-\delta^{\prime \prime}\right)}{11^{0} 15^{\prime}}
$$

the upper sign being taken when $m$ is positive, the lower when $m$ is negative. By this formula the deviations of the Forward Alidade, Forward Binnacle, Forward Ritchie, Admiralty Standard, and After Azimuth Compasses, on the true magnetic points, have been computed from the observed deviations.
$2^{\circ}$. In addition to the correction which has just been explained, the observed deviations of the After Binnacle and After Ritchie Compasses require a further correction on account of the lubber lines of these instruments revolving with the after turret, and thus being frequently out of their true position. This correction, which we will represent by $L$, is constant, and is equal in amount to the displacement of the lubber line. Its sign is + if the lubber line is to starboard, - if it is to port, of its true position. The deviations of the After Binnacle and After Ritchie Compasses, on the true magnetic points, were therefore computed from the observed deviations by the formula

$$
\delta=\delta^{\prime}+(m+L) \mp \frac{m\left(\delta^{\prime}-\delta^{\prime \prime}\right)}{11^{\circ} 15^{\prime}}
$$

the upper sign being taken when $m$ is positive, the lower when $m$ is negative.
To have computed numerically all the values of $\delta$ for each compass by means of the expressions just given, would have involved a great amount of labor; it was therefore done graphically as follows:


On a piece of cardboard of suitable size a horizontal line $a b, 5 \frac{5}{8}$ inches long, was drawn, and divided into eighths of an inch ; each half inch representing one degree, and the whole line representing $11^{\circ} 15^{\prime}$, or one point of the compass. Touching the extremities of the line $a b$, and at right angles to it, were drawn the line $c d$ and $e f$; and each of them was divided, upward and downward from the line $a b$, into points and eights of points; ${ }^{1}$ each point occupying the space of $2 \frac{1}{1} \frac{3}{6}$ of an inch. Finally, a straight slip of drawing paper was divided on its edge into degrees and sixths of a degree, each degree occupying a space of one-quarter of an inch; and the graduation was numbered from the middle towards each extremity.
Then, to compute the values of $\delta$ for any compass at any place, the paper scale was laid down parallel to, and to the right of, $c d$, and at a distance from it (measured on the line $a b$ ) equal to $m$; next, without moving the paper scale at all in the direction $a b$, it was slipped up or down, as might be necessary, in the direction parallel to $c d$, till the line $a b$ cut the division on it which was equal to $(m+L)$; the zero of the scale being above the line $a b$ if $(m+L)$ was negative, below it if

[^2]( $m+L$ ) was positive. Things being thus arranged, a weight was placed on the paper scale to prevent it from moving. Then a ruler being laid so that, while it crossed the line $c d$ at a distance from $a$ equal to $\delta^{\prime}$, it also crossed the line $e f$ at a distance from $b$ equal to $\delta^{\prime \prime}$ (the distances $\delta^{\prime}$ and $\delta^{\prime \prime}$ being taken above the line $a b$ if they were positive, below it if they were negative), the reading of the point on the paper scale where the ruler crossed its edge was the required value of $\delta$. In that way, without again moving the paper scale, the values of the deviations on each of the thirty-two true magnetic points were computed from the observed values.

The following table contains the constants which were used in computing from the observed deviations the deviations on the true magnetic points. The first column gives the name of the station. The second column, the distance in miles from the ship to the object used as an azimuth mark. The third column, the assumed magnetic azimuth of the object used as an azimuth mark; the azimuth being counted from the south around by the west. The fourth column, the true magnetic azimuth of the same object, found by applying the magnetic declination given in the table on page 61 , section IV, to the true azimuth given in the table on page 36 , section III. The fifth column, the value of $m$. The sixth column, the value of $L$; and the seventh column, the value of $(m+L)$.

| Station. | Dista ace of Object in Miles. | Assumed Magnetic Azimuth. | True Magnetic Azimuth. | 112 | $L$ | $(m+L)$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | $6 \frac{1}{4}$ | $9^{\circ} \mathrm{I} 5^{\prime}$ | $13^{\circ} \mathrm{I} 2^{\prime}$ | $+3^{\circ} 57^{\prime}$ | $0^{\circ} 0^{\prime}$ | $+3^{\circ} 57^{\prime}$ |
| St. Thomas | $4 \frac{1}{2}$ | 32730 | 32745 | +o 15 | $\bigcirc$ | +o 15 |
| Salute Islands | 25 | 11 ○ | 10. 58 | -0 2 | +6 18 | + 6 ı6 |
| Ceara. | 4 | 26845 | $270{ }^{6}$ | + $15{ }^{1}$ | +618 | + 89 |
| Bahia . | 5 | 10330 | 106 0 | +230 | +618 | + 848 |
| Rio Janeiro . | 5 | 12630 | 12914 | + 244 | + 543 | +827 |
| Monte Video | 5 | 93 ○ | 9247 | - 0 I3 | $+49$ | + 356 |
| Sandy Point. | 26 | 345 I 5 | $345 \quad 22$ | +○ 7 | + 49 | + 4 i 6 |
| Valparaiso | $3 \frac{1}{2}$ | 195 I5 | 195 16 | +or | + 417 | + 418 |
| Callao | $5 \frac{1}{2}$ | 7245 | 72 5 | +o6 | + 344 | $+350$ |
| Panama . | 7 | 15 - | 15 I | + 0 | +344 | + 345 |
| Acapulco. | 4 | 24315 | 243 2 1 | +o6 | + 344 | + 350 |
| Magdalena Bay. | 8 | $3033^{\circ}$ | 30250 | -0 40 | + 344 | + 34 |
| San Francisco | 9 | 15030 | 14945 | -○ 45 | + 349 | + 34 |

The following tables contain all the deviations of the compasses which were observed during the cruise. In each table the first column contains the assumed magnetic azimuth of the ship's head at the time the reading of the compass, given on the same line in the second column, was taken. The third column contains the observed deviation of the compass for each point, obtained by subtracting the readings in the second column from those in the first column, Hence, a deviation of the north point of the compass to the east is designated by the sign + ; a deviation to the west by the sign -. The fourth column contains the deviation of the compass on each of the thirty-two true magnetic points. obtained from the observed deviations in the manner already explained.
Observations for Determining the Deviations of the Admiralty Standard Compass on the U. S. Iron Clad Monadnock.

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A deviation of the North Point of the Compass to the East is designated by the sign +; A deviation of the North Point of the Compass to the East is designated by the sign + ;
a deviation to the West by the sign From the observations given above, the following values of the coefficients of the $\begin{gathered}\text { From the observations given above, the following values of the coefficients of the } \\ \text { deviation are obtained: }\end{gathered}$, obtained:
 Assumed magnetic bearing of Nipple S. $32^{\circ} \quad 30^{\prime}$ E. Distant $4 \frac{1}{2}$ miles.
Observations for Determining the Deviations of the Admiralty Standard Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 5865. <br> Assumed Magnetic Bearing of Object $=\mathrm{S} . \mathrm{I}^{\circ}{ }^{\circ} \mathrm{o}^{\prime}$ W. <br> Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Ceara, December 19, 1865. <br> Assumed Magnetic Bearing of Object $=$ N. $88^{\circ} 45^{\prime} \mathrm{E}$. <br> Correction for Object $=+\mathrm{I}^{\circ} 51^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Bearing of Object by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected <br> Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Bearing of Object by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. |  |  | a ${ }^{\circ}{ }^{4 \prime}$ <br> $+5{ }^{\prime}$ | + $5^{\circ}{ }^{40}$ +520 | NORTH. <br> N. by E. <br> N. N. E. N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> WEST. <br> W. by N. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. NORTH. |  |  |  |  |

[^3]
Observations for Determining the Deviations of the Admiralty Standard Compass on the U. S. Iron Clad Monadnock.

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[^4]Observations for Determining the Deviations of the Admiralty Standard Compass on the U. S. Iron Clad Monadnock.

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[^5]Observations for Determining the Deviations of the Admiralty Standard Compass on the U. S. Iron Clad Monadnock.

| Valparaiso, April 4, 1866. <br> Assumed Magnetic Bearing of Object $=\mathrm{N} .15^{\circ} 15^{\prime} \mathrm{E}$. <br> Correction for Object $=+o^{\circ} 1^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Callao, April 29, 1866. <br> Assumed Magnetic Bearing of Object $=$ S. $72^{\circ} 45^{\prime} \mathrm{W}$, Correction for Object $=+o^{\circ} 6^{\prime}$. Correction for Lubber Line $=0$, |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Bearing of Object by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass | Assumed Magnetic Direction of Ship's Head. | Bearing of Object by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. | N. $15^{\circ}{ }^{\prime \prime} 0^{\prime} \mathrm{E}$. |  | - ${ }^{\circ} 15^{\prime}$ | - $0^{\circ} 1{ }^{\prime \prime}$ | NORTH. | S. $72^{\circ} 40^{\prime} \mathrm{W}$. |  |  |  |
| N. by E. | N. 14 O E. |  | +1 | +120 | N. by E. | S. 7240 W . |  | $\circ$ |  |
| N. N. E. | N. I4 $\bigcirc$ E. |  | +115 | +120 | N. N. E. | S. 7140 W . |  | I 5 | +10 |
| N. E. by N. | N. $133_{3} \mathbf{3 0} \mathrm{E}$ E. |  | $\begin{array}{r}\text { r } \\ +145 \\ +215 \\ \hline\end{array}$ | +150 | N. ${ }_{\text {N. }}^{\text {E. by }}$ N. | S. 710 W. |  | $\begin{array}{r}+15 \\ +1.45 \\ \hline\end{array}$ | +150 |
| N. N . E. E. by E. | $\begin{array}{ll}\text { N. } 13 & \circ \\ \text { N. } 13 & \text { O. } \\ \text { O. }\end{array}$ |  | $\begin{array}{r}\text { a } \\ +215 \\ +215 \\ \hline\end{array}$ | $\begin{array}{r}\text { + } \\ +2 \\ +2 \\ \hline\end{array} 20$ | N. ${ }_{\text {N. E. by E. }}$ | $\begin{array}{lll}\text { S. } 70 & 20 & \mathrm{~W} . \\ \text { S. } 70 & 20 & \mathrm{~W} .\end{array}$ |  | $\begin{array}{r}1 \\ +2.25 \\ +\quad 2 \quad 25 \\ \hline\end{array}$ | +230 |
| N. ${ }_{\text {N. }}$ N. E. by E. |  |  | r +215 +235 | a +20 $+\quad 240$ | N. ${ }_{\text {N. }}^{\text {E. }}$ N. by E. |  |  | $\begin{array}{r}\text { P } \\ +25 \\ +245 \\ \hline\end{array}$ | $\begin{array}{r}\text { r } \\ +230 \\ +230 \\ \hline\end{array}$ |
| E. by N. | N. I2 40 E . |  | + | +240 +240 | E. by N . | S. 7030 W. |  |  | +250 +250 |
| EAST. | N. $13 \bigcirc \mathrm{E}$. |  | +215 | +220 | EAST. | S. 710 W . |  | +145 | +150 |
| E. by S. | N. 144 N. 13 |  | $\begin{array}{r}1 \\ +115 \\ +1 \quad 15 \\ \hline\end{array}$ | +120 | E. by S. | S. 7040 W . |  | +25 | +210 |
| S. S. E. by E. |  |  | $\begin{array}{r}\text { r } \\ +135 \\ +055 \\ \hline\end{array}$ | +140 | E. S. E. by E. | S. 71180 W |  | +15 | + 10 |
| S. E. ${ }^{\text {d }}$. | N. 1440 \% E. |  | $\begin{array}{r}\text { + } \\ + \\ + \\ +035 \\ \hline\end{array}$ | +180 | S. E. |  |  | + +15 +0 | $\begin{array}{r}\text { + } \\ +10 \\ +0 \\ \hline\end{array}$ |
| S. E. by S. | N. $15 \bigcirc$ E. |  | + +015 +015 | +020 | S. E. by S. | S. 7240 W . |  | + +05 +05 | + |
| S. S. E. E. | N. 15 O E. |  | $\begin{array}{r}\text { a } \\ +015 \\ +0 \\ \hline\end{array}$ | +0 20 | S. S. E. | S. 7240 W . |  | +0.5 | +0 10 |
| SOUTH. | N. 1440 E . |  |  | $\begin{array}{r}\text { + } \\ + \\ +0 \\ \hline\end{array}$ | South. |  |  | -0 15 | (10 |
| S. by W. | N. 1420 E . |  | + | + I o | S. by W. | S. $73 \circ \mathrm{~W}$. |  | -0 15 | 二-10 |
| S. S. W. by | N. 1440 E. |  | P +035 +035 | +040 | S. S. W. | S. $73 \bigcirc \mathrm{~W}$. |  | -0 15 | - 10 |
| S. W. by S. | $\begin{array}{cc}\text { N. } 14 & 40 \\ \text { N. } 15 & \text { O. } \\ \text { O. }\end{array}$ |  | $\begin{array}{r}\text { a } \\ +035 \\ +\quad 015 \\ \hline\end{array}$ | + +040 +0.20 | S. W. by S. | S. $73 \bigcirc \bigcirc$ |  | -0 15 | 10 |
| S. w. by w. | N. I4 30 E . |  | + | $\begin{array}{r}\text { P } \\ +0 \\ +0 \\ \hline\end{array}$ | S. w. by w. | S. $74 \times$ O. |  | -1 15 <br> 1 15 | -1 10 <br> 1 10 |
| W. S. W. | N. 15 20 E. |  | -0 5 | - 0 | w. s. W. | S. 74 ○ W. |  | (15 | - 10 |
| W. by s . | N. 15040 E . |  | -0 25 | -0 20 | W. by S. | S. 7530 W. |  | -245 | -240 |
| WEST. N . | N. 15 <br> N. 16 <br> 160 <br> 30 <br> 0 |  | -19 | - 10 | WEST. | S. 76 ○ ${ }_{\text {S }} 75$ W. |  |   <br> -3 15 <br> -255  <br> -3 5 | -3 10 |
| W. N. W. | N. 1640 E . |  | $\begin{array}{ll}\text {-1 } & 15 \\ -1 & 25\end{array}$ | $\begin{array}{ll}-1 & 10 \\ -1 & 20\end{array}$ | W. N. W. |  |  | - 2155  <br> -3 15 <br>  15 | - <br> -3 <br> -30 |
| N. W. by W. | N. 1640 E . |  | -1 25 | - 120 | N. W. by W. | S. 7530 W. |  | [ | -2 20 |
| N. W. W. by N . |  |  | -1 45 <br> - 15  <br> 15  | $\begin{array}{ll}-1 & 40 \\ -1 & 10\end{array}$ | N. W. b. by N . | S. 75 Sto W. |  | -2 <br> -25 <br> -15 | - 2150 |
| N. N. W. | N. 15 20 E. |  | (1) | 二110  <br> 0 0 | N. N. W. ${ }^{\text {N }}$. |  |  |  | -210  <br>  10 |
| N. by W. | N. 1540 E . |  | [10 | -0 20 | N. by W. | S. 7320 W . |  | -0 35 | - -130 $-\quad 30$ |
| NORTH. | N. 1530 E . |  | -0 15 | - 0 | NORTH. | S. 7240 W . |  | +o 5 | +0 10 |

[^6]18
August, 1872.
Observations for Determining the Deviations of the Admiralty Standard Compass on the U．S．Iron Clad Monadnock．

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{\begin{tabular}{l}
Panama，May 20， 1866. \\
Assumed Magnetic Bearing of Object \(=\) S． \(15^{\circ} o^{\prime} \mathrm{W}\) Correction for Object \(=+0^{\circ} \mathbf{1}^{\prime}\) ．Correction for Lubber Line \(=0\).
\end{tabular}} \& \multicolumn{5}{|l|}{\begin{tabular}{l}
Acapulco，June 1， 1866. \\
Assumed Magnetic Bearing of Object \(=\mathrm{N} .63^{\circ}{ }^{15^{\prime}} \mathrm{E}\) ． \\
Correction for Object \(=+o^{\circ} 6^{\prime}\) ．Correction for Lubber Line \(=0\) ．
\end{tabular}} \\
\hline Assumed Magnetic Direction of Ship＇s Head． \& Bearing of Object by
Compass． \& Deviation of Compass in Points． \& Deviation of Compass in Degrees． \& Corrected Deviation of Compass． \& Assumed Magnetic Direction of Ship＇s Head． \& Bearing of Object by
Compass． \& Deviation of Compass in Points． \& Deviation of Compass in Degrees． \& \[
\begin{gathered}
\text { Corrected } \\
\text { Deviation of } \\
\text { Compass. }
\end{gathered}
\] \\
\hline NORTH． \& S． \(14^{\circ} \mathrm{o}^{\prime} \mathrm{W}\) ． \& \& \(+\mathrm{I}^{\circ} \mathrm{o}^{\prime}\) \& \(+\mathrm{r}^{\circ} \mathrm{o}^{\prime}\) \& NORTH． \& N． \(63^{\circ} 4^{\prime} \mathrm{E}\) ． \& \& －\({ }^{\circ}{ }^{25^{\prime}}\) \& － \(0^{\circ}{ }^{20}\) \\
\hline N．by E． \& S． 1330 W ． \& \& ＋130 \& ＋130 \& N．by E． \& N． 63 ○ E： \& \& ＋\({ }^{\circ} \mathrm{L}\) \& ＋o \({ }^{\circ}\) \\
\hline N．N．E．\({ }_{\text {d }}\) \&  \& \& ＋220 \& ＋220 \& N．N．E． \& N． 62 Io E． \& \& ＋ 15 \& ＋110 \\
\hline N．E．by \& S． 12 II 20 W ． \& \& \(\begin{array}{r}\text {＋} \\ +3 \\ +3 \\ \hline\end{array}\) \& a
+240
+340 \& N．E．by \&  \& \& \(\begin{array}{r}\text {＋1 } \\ +15 \\ +2 \\ \hline\end{array}\) \& ＋150 \\
\hline N．E．by E． \& S． 1120 W ． \& \& ＋340 \& ＋340 \& N．E．by E． \& N． 60 50 E． \& \& \(\begin{array}{r}\text { Pr } \\ +215 \\ +\quad 2 \quad 25 \\ \hline\end{array}\) \& ＋
+20
+230 \\
\hline E．N．E． \& S． 11 o W． \& \& ＋40 \& ＋40 \& E．N．E． \& N． 6040 E ． \& \& ＋235 \& ＋ \\
\hline E．by N． \& S． \(11 \bigcirc 0 \mathrm{~W}\) ． \& \& ＋40 \& ＋40 \& E．by N． \& N． 6050 E ． \& \& ＋225 \& ＋230 \\
\hline EAST． \&  \& \& a
+30
+30 \& ＋
+30
+30 \& \({ }_{\text {EAST．}}\) Ey S． \&  \& \& \(\begin{array}{r}125 \\ +155 \\ \hline 15\end{array}\) \& P
+230
+130 \\
\hline E．S．E． \& S． 12 o W． \& \& ＋ \& ＋ \& E．S．E． \& N． 62 O E． \& \& \(\begin{array}{r}\text {＋1 } \\ +15 \\ +1 \\ \hline\end{array}\) \& ＋
+130
+120 \\
\hline S．E．by E． \& S． \(13 \circ \mathrm{~W}\) ． \& \& ＋20 \& ＋20 \& S．E．by E． \& N． 6220 E ． \& \& ＋
+155
\(+\quad 155\) \& ＋100 \\
\hline S．E． \& S． 1330 W ． \& \& ＋130 \& ＋130 \& S．E． \& N． 6320 E ． \& \& －0 5 \& －o \\
\hline S．E．by S． \& S．I4 \({ }_{\text {S }}\) O W． \& \& \& \& S．E．by S． \& N． 6330 E ． \& \& －0 15 \& －0 10 \\
\hline S．S．by E． \&  \& \& ＋
+10
+0 \& ＋
+10
+040 \& S．S．E．\({ }_{\text {S }}\) S． \&  \& \&  \& ［ \\
\hline South． \& S． 1420 W ． \& \& ＋o40 \& ＋ \& South． \& N． 63 50 E． \& \& 二－0 45 \& －0 40 \\
\hline S．by W． \& S． 1420 W ． \& \& ＋040 \& ＋0 40 \& S．by W． \& N． 6350 E ． \& \& 二－ 35 \& （ \\
\hline S．S．W． \& S． 1440 W \& \& ＋0 20 \& ＋o 20 \& S．S．W． \& N． 64 Io E． \& \& －0 55 \& －0 50 \\
\hline S．W．by S．
S．W． \&  \& \& \(\begin{array}{r}0 \\ -\mathrm{o} \\ \hline\end{array}\) \& \(\begin{array}{r}\circ \\ - \\ \hline\end{array}\) \& S．W．by S．
S．W． \& N． 64
N． 65

O \& \& －1 15 \& －1 10 <br>

\hline S．w．by w． \& S． $16{ }_{20}{ }^{\text {S }}$ \& \& －${ }^{0} 180$ \& 二0 ${ }^{1} 20$ \& S．W．by w． \& N． 6530 E ． \& \& | －1 |
| :--- |
| － 245 | \& 二1 140 <br>

\hline w．s．w． \& S． 1640 W ． \& \& －1 40 \& －1 40 \& w．s．w． \& N． 66 O E． \& \& － 245 \& $\begin{array}{ll}-2 & 10 \\ -2 & 40\end{array}$ <br>
\hline W．by S． \& S． 1750 W ． \& \& －2 50 \& －2．50 \& W．by S． \& N． 66.40 E. \& \& －325 \& －3 20 <br>
\hline WEST． \& S．${ }_{\text {S．}} 18$ ¢ 17 W W． \& \& －3 0 \& －3 0 \& WEST． \& N． 67 ○ E． \& \& －345 \& －340 <br>
\hline W．by N． W ． \&  \& \& －${ }^{2}{ }^{3} \mathrm{3} 0$ \& －${ }^{2}$ 30 ${ }^{30}$ \& W．by $\mathrm{N} . \mathrm{N}$ ． \&  \& \& -345
-445 \& －3 40 <br>

\hline N．W．by W． \& S． 18 ○ W． \& \& －3 0 \& －3 \& N．W．by w． \& N． 67 o E． \& \& | － 44 |
| :--- |
| -34 | \& $\begin{array}{rl}-4 & 0 \\ -3 & 40\end{array}$ <br>

\hline N．W． \& S． 17 10 W． \& \& －2 ${ }^{2} 10$ \& －2 ${ }^{10}$ \& N．W． \& N． 6640 E ． \& \& －325 \& －320 <br>
\hline N．W．by N． \&  \& \& －${ }^{1} \mathrm{I}$ 0 \& － 20. \& N．W．by
N．W． \&  \& \& － $\begin{array}{r}\text { 2 } \\ -25 \\ \hline-15\end{array}$ \& － 250 <br>

\hline N．by w． \& S． 1520 W ． \& \& 二－${ }^{1}$ \& 二－${ }^{1}$ \& N．by w． \& N． 6440 E ． \& \& | － |  |
| :--- | :--- |
| 1 | 5 | \& － $\begin{array}{rr} & 0 \\ -1 & 20\end{array}$ <br>

\hline NORTH． \& S． 14 ○ W． \& \& ＋ 10 \& ＋ 1 \& NORTH． \& N． 6340 E ． \& \& ［ \& 二－1 20 <br>
\hline
\end{tabular}

[^7]Observations for Determining the Deviations of the Admiralty Standard Compass on the U．S．Iron Clad Monadnock．

| Magdalena Bay，June 9， 1866. <br> Assumed Magnetic Bearing of Object $=$ S． $56^{\circ} \quad 30^{\prime} \mathrm{E}$ ． <br> Correction for Object $=-0^{\circ} 41^{\prime}$ ．Correction for Lubber Line $=0$ ． |  |  |  |  |  | San Francisco，June 23， 1866. <br> Assumed Magnetic Bearing of Object $=\mathrm{N} \cdot 29^{\circ} 30^{\prime} \mathrm{W}$ ． <br> Correction for Object $=-0^{\circ} 45^{\prime}$ ．Correction for lubber Line $=0$ ． |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship＇s Head． | Bearing C | of Object by mpass． | Deviation of Compass in Points | Deviation of Compass in Degrees． | Corrected Deviation of Compass． | Assumed Magnetic Direction of Ship＇s Head． | Bearing of Object by Compass． | Deviation of Compass in Points． | Deviation of Compass in Degrees． | Corrected Deviation o Compass． |
| NORTH． |  |  |  |  |  | NORTH． |  |  |  |  |
| N．by E． | S． | 40 E ． |  | ＋o ıо | 二口 ${ }^{\circ}{ }^{\circ}$ | N．by E． | N． 29830 w ． |  | cor -10 0 0 |  |
| N．N．E． |  |  |  |  |  | N．N．E． | N .3 I |  | ＋${ }^{\circ} \mathrm{O}$ | ＋${ }^{\circ} \mathrm{O} 50$ |
| N．E．by N． |  |  |  |  |  | N．E．by N． |  |  | 1 +230 +330 | ＋ 150 |
| N．E．by E． |  |  |  |  |  | N．E．by E． |  |  | ＋330 | ＋ +20 +320 |
| E．N．E．${ }^{\text {E }}$ |  |  |  |  |  | E．N．E．${ }^{\text {N }}$ | N． 3430 W ． |  | ＋ 40 | a +310 +410 |
| E．by N ． |  |  |  |  |  | E．by N． | N． 3430 W W． |  | ＋50 | ＋4 10 |
| E．by S ． |  |  |  |  |  | E．by S． |  |  | ＋445 | ＋4 0 |
| E．S．E． |  |  |  |  |  | E．S．E． | N． 34 ow ． |  | +4 +430 +4 | a +320 +340 |
| S．E．by E． |  |  |  |  |  | S．F．by E． | N． 33330 W ． |  | ＋40 | a +320 +320 |
| S．E．by S． |  |  |  |  |  | $\stackrel{\text { S．}}{\text { S．E．by S．}}$ |  |  | ＋4 | ＋ |
| S．S．E． |  |  |  |  |  | S．S．E． | N． $3^{3} 20 \mathrm{~W}$. |  | +330 +230 | ＋${ }^{2} 80$ |
| S．by E． |  |  |  |  |  | S．by E． | N． 3 ll 30 W ． |  | ＋20 | ＋10 |
| SOUTH． |  |  |  |  |  | SOUTH． |  |  | ＋ 130 | ＋ |
| S．by W． |  |  |  |  |  | S．by W． S．S．w． |  |  | r +030 +010 | －0 20 |
| S．W．by S． |  |  |  |  |  | S．W．by S． | N． 2840 W W． |  | r |  |
| S．W． |  | $\bigcirc \mathrm{E}$ ． |  | ＋o 30 | －0 20 | S．W． | N． 28 ○ W． |  | －1 30 | 二 2420 |
| S．W．by w． | S． 56 | 20 E ． |  | －0 10 | －I ${ }^{1}$ | S．W．by W． | N． 27 ○ W． |  | －230 | －320 |
| W．by S． | S． 55 | 30 E． |  | －I 0 | $\begin{array}{ll}-1 & 50 \\ -200\end{array}$ | W．S．W． | N． 26 N .25 20 20 |  | －3 10 | －4 0 |
| WEST． | S． 54 | 20 E ． |  | －1 | －${ }^{1} 200$ | WEST． | N． 25 ¢ ${ }^{\text {o }}$ W． |  | －${ }^{4} 110$ | －5 ${ }^{5} \mathrm{O}$ |
| W．by N ． | S． 53 | 20 E ． |  | －3 10 | －3 50 | W．by N． | N． 2430 W ． |  | －5 ${ }^{4}$ | －5 50 |
| N．W．by w． | S． 53 | ${ }^{20} \mathrm{E}$ O． |  | －3 <br> -30 | －3 50 <br> -410 | W．N．W．by． |  |  | －5 30 | － 620 |
| N．W． | S． 53 | 30 E ． |  | 二3 30 | $\begin{array}{ll}-4 & 10 \\ -3 & 40\end{array}$ | N．W．by | N． 24 l \％W． |  | － 6 \％${ }^{\circ}$ | －6 50 |
| N．W．by N． | S． 53 | 30 E ． |  | －3 0 | －340 | N．W．by N ： | N． 2515 W ． |  | －415 | －5 ${ }^{\text {o }}$ |
| N． N ．Wy W． | S． 54 | $30 \mathrm{E}$. |  | －${ }^{2}$ | － 240 <br> -140 | N．N．W． N．by W． |  |  | －3 30 | －4 10 |
| NORTH． | S． 56 | 30 E ． |  | －1 | -1 40 <br> -0 40 | NORTH． |  |  | $\begin{array}{cc}\text {－} & \\ -1 & \\ \text { 10 }\end{array}$ | 二 2150 <br> 150 |

[^8]Observations for Determinlng the Deviations of the After Binnacle Compass on the U. S. Iron Clad Monadnock.

| Hampton Roads, November r, 1865. <br> Correction for Object $=+3^{\circ} 57^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | St. Thomas, November 18, 1865. <br> Correction for Object $=+0^{\circ} 16^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N: <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{3}{8} \mathrm{E}$. <br> N. by E. $\frac{1}{8} \mathrm{E}$. <br> N. N. E. <br> N. E. by N. $\frac{1}{8} \mathrm{~N}$. <br> N. E. $\frac{1}{2} \mathrm{~N}$ N. <br> N. E. by E. 5 E. <br> E. $\frac{3}{2} \mathrm{~N}$. <br> E. by S. $\frac{3}{4}$ S. <br> S. E. by $\mathrm{E} . \frac{1}{8} \mathrm{E}$. <br> S. E. <br> S. E. by S. <br> S. by E. $\frac{7}{8}$ E. <br> S. <br> S. <br> . <br> $\frac{3}{8}$ E W. <br>  <br> S. W. $\frac{1}{2}$ S. S. S. w . W. W. <br> S. W. by $W \cdot \frac{3}{4} \mathrm{~W}$. W. by S. $\frac{1}{4}$ S. <br> w. <br> W. by N . <br> w. N. W. <br> N. W. $\frac{7}{8} \mathrm{~W}$. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. $\frac{1}{4} \mathrm{~W}$ W W. <br> N. $\frac{1}{2} \mathrm{~W}$. |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. <br> N: E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. | NORTH. <br> N. $\frac{3}{4} \mathrm{E}$. <br> N. N. E. $\frac{1}{4} \mathrm{E}$. N. E. by N. <br> N. E. $\frac{1}{2}$ E. <br> N. E. by E. $\frac{1}{4}$ E. <br> E. by N. <br> E. $\frac{1}{2} \mathrm{~N}$. <br> E. by S. $\frac{3}{4} \mathrm{~S}$. <br> S. E. by E. <br> S. E. by S. $\frac{1}{2}$ S. <br> S. S. E. $\frac{1}{4}$ S. <br> S. $\frac{1}{4}$ E. <br> S. $\frac{1}{4} \mathrm{E}$. S. W . <br> S. S. W. $\frac{1}{4}$ W. <br> S. W. by S. $\frac{1}{4}$ W. <br> S. W. by W. <br> S. W. by W. $\frac{1}{2}$ W. W. S. W. $\frac{1}{2}$ W. <br> W. by S. $\frac{1}{2}$ W. <br> W. $\frac{3}{4} \mathrm{~N}$. <br> W. by ${ }^{\text {N. }} \frac{1}{2} \mathrm{~N}$. W. N. <br> N. W. $\frac{1}{2}$ W. $\mathrm{N} . \mathrm{W} . \frac{1}{2} \mathrm{~N}$ <br> N. W. by N. $\frac{1}{2}$ N. <br> N. $\frac{3}{4}$ W. |  |  | - , |

[^9]Observations for Determining the Deviations of the After Binnacle Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 1865. <br> Correction for Object $=-0^{\circ} \quad 2^{\prime}$. Correction for Lubber Line $=+6^{\circ} \quad 18^{\prime}$. |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+1^{\circ} 51^{\prime}$. Correction for Lubber Line $=+6^{\circ} \quad 18^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | EAST. <br> E. by S. | $\bigcirc$ | - | $+6{ }^{\circ} 2$ +620 | NORTH <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by'N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. by E. $\frac{3}{8}$ E. <br> N. E. by N. $\frac{3}{4}$ N. <br> N. E. $\frac{7}{8}$ N. <br> N. E. <br> N. E. by E. $\frac{1}{8}$ E. <br> E. by N. $\frac{7}{8}$ N. <br> E. $\frac{7}{8} \mathrm{~N}$. <br> E. $\frac{3}{8} \mathrm{~S}$. <br> E. by S. $\frac{3}{2}$ S. <br> S. E. by $\frac{8}{\text { E. }} \frac{1}{2}$ E. |  | - |  |

[^10]Observations for Determining the Deviations of the After. Binnacle Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865. Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=+6^{\circ} \quad 18^{\prime}$. |  |  |  |  | Rio Janeiro, January 10, 1866. <br> Correction for Object $=+2^{\circ} 44^{\prime}$ Correction for Lubber Line $=+5^{\circ} 43^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | $\begin{aligned} & \text { Corrected } \\ & \text { Deviation of } \\ & \text { Compass. } \end{aligned}$ |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S . WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{1}{2} \mathrm{E}$. <br> N. by E. $\frac{1}{2} \mathrm{E}$. <br> N. N. E. ${ }_{1}^{1} \mathrm{E}$ E. <br> N. E. ${ }^{3}+\frac{3}{4} \mathrm{~N}$. <br> N. E. by E. $\frac{1}{4} \mathrm{E}$. <br> E. $\begin{aligned} & \text { E. E. E. } \\ & \text { N. }\end{aligned}$ <br> E. $\frac{1}{8} \mathrm{~S}$. <br> E. by S. 2 s . <br> S. E. by E. $\frac{3}{4}$ E. <br> S. E. . S. E. E. E. <br> S. S. E. $\frac{1}{2} \mathrm{E}$. <br> S. S. E. S. by E. $\frac{1}{8}$ E. E. <br> S. ${ }^{3}$ E. <br> S. 홍 W. <br>  <br> S. W. $\frac{1}{4}$ S. S. W . W. S. W. <br> W. S. W. w. by S. <br> $\mathrm{W} . \frac{1}{8} \mathrm{~N}$. <br> W. by N. $\frac{1}{2}$ N. N. W. by W. $\frac{3}{4}$ W. <br> N. W. $\frac{3}{4} \mathrm{~W}$. <br> N. N. $\frac{4}{W} \cdot \frac{3}{4} \mathrm{~W}$. <br> N. N. W. <br> N. $\frac{1}{4} \mathrm{~W}$. <br> N. by W. $\frac{1}{8}$ W. |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. E. $\frac{3}{4}$ N. <br> N. E. $\frac{1}{8}$ E. <br> E. by N. $\frac{7}{8}$ N. <br> N. E. by E. $\frac{1}{8}$ E. <br> E. $\frac{3}{4} \mathrm{~N}$. <br> E. by S. $\frac{1}{4}$ S. <br> S. E. by E. $\frac{5}{8}$ E. <br> S. E. $\frac{5}{8}$ E. <br> S. S. $\frac{1}{2}$ E. $\frac{1}{2}$ E <br> S. by E. $\frac{3}{8} \mathrm{E}$ <br> S. $\frac{3}{8} \mathrm{E}$. S. $\frac{5}{8} \mathrm{~W}$. <br> S. by W. $\frac{3}{4}$ W. <br> S. S. W. $\frac{3}{4}$ W. <br> S. W. $\frac{1}{4}$ S. |  |  |  |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign - <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign - <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  |

Observations for Determining the Deviations of the After Binnacle Compass on the U. S. Iron Clad Monadnock.

| Monte Video, January 24, 1866. <br> Correction for Object $=-0^{\circ} \quad 13^{\prime}$. Correction for Lubber Line $=+4^{\circ} 9^{\prime}$. |  |  |  |  | Sandy Point, February io, 1866. <br> Correction for Object $=+\circ^{\circ} 7^{\prime}$. Correction for Lubber Line $=+4^{\circ} 9^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic 'Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. N. E. by N <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E . <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | ${ }^{\mathrm{N}} \frac{3}{8} \mathrm{E}$. <br> N. by E. $\frac{7}{\text { I }} \mathrm{E}$. <br> N. by E. $\frac{7}{\text { I }}$ E. . <br> N. E. $\begin{gathered}1 \\ \text { N. } \\ \text { N. } \\ \text { N. }\end{gathered}$ <br> N. E. by E. $\frac{5}{8} \mathrm{E}$. <br> E. by N. $\frac{3}{8} \mathrm{~N}$. <br> E. <br> E. <br> E. by S. $\frac{\pi}{\frac{\pi}{S}}$ S. <br> S. E. $\frac{1}{8}$ S. <br> S. E. by S. $\frac{1}{4}$ S. <br> S. by E. <br> S. $\frac{5}{3} \mathrm{E}$ E. <br>  <br> S. W. $\frac{5}{\frac{5}{2}} \mathrm{~S}^{2} \mathrm{~W}$. <br> S. W. by W. $\frac{1}{2} \mathrm{~W}$. <br> $\mathrm{W} . \frac{\mathrm{by}}{} \mathrm{s}$ S. $\mathrm{W} . \frac{3}{4} \mathrm{~S} \mathrm{~N}$. <br> W. by N. ${ }_{4}^{3} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4} \mathrm{~W}$. <br> N. W. $\frac{1}{2} \mathrm{~W}$. <br> N. N. W. ${ }^{4} \mathrm{~B}$ N. by W. <br> $\xrightarrow{\text { N. by }} \mathrm{W}$. $\frac{1}{2}$ W. | $-\frac{3}{8}$ |  |  | NORTH. <br> N. E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. <br> N. W. by W. <br> N.W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{1}{2} \mathrm{E}$. <br> N. by E. $\frac{1}{8} \mathrm{E}$. <br> N. N. E. $\frac{1}{\text { d }}$ E. <br> N. E. $\frac{1}{3}$ N. <br> N. E. ${ }_{\text {B }}^{\text {B }} \mathrm{E}$. <br> E. by N. by $\frac{7}{8}$ E. <br> E. $\frac{1}{8} \mathrm{~N}$. <br> E. by S. <br> S. E. $\frac{7}{8} \mathrm{E}$. <br> S. E. by S. $\frac{1}{4}$ S. <br> S. by E. $\frac{5}{8}$ E. <br> S. ${ }^{\frac{5}{3} \mathrm{E}} \mathrm{E}$. <br> S. by W. $\frac{3}{8} \mathrm{~W}$. S. S. W. $\frac{1}{3} \mathrm{~W}$. <br> S. S. W. $\frac{1}{2}$ S. W. $\frac{1}{2}$ W. <br> S. W. 喜W. S. W. Wy W. $\frac{5}{8} \mathrm{~W}$. <br> W. by'S. $\frac{1}{4}$ S. ${ }^{8}$ <br> W. . $\frac{1}{3} \mathrm{~S}$. N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. W. W. <br> N. $\frac{3}{8} \mathrm{~W}$. |  |  |  |

[^11]Observations for Determining the Deviations of the After Binnacle. Compass on the U. S. Iron Clad Monadnock.

| Valparaiso, April 4, 1866. <br> Correction for Object $=+0^{\circ} 1^{\prime}$. Correction for Lubber Line $=+4^{\circ} \quad 17^{\prime}$. |  |  |  |  | Callao, April 29, 1866. Correction for Object $=+0^{\circ} \quad 6^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. N. E. by.N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. W. by S. <br> S. W. <br> S. W. by W. <br> W. by W. <br> WEST. <br> W. by N. <br> W. N. W. N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W <br> NORTH. | N. $\frac{3}{8} \mathrm{E}$. <br> N. by E. $\frac{1}{4} \mathrm{E}$. <br> N. N. E. $\frac{1}{8}$ E. <br> N. E. $\frac{1}{\frac{1}{8}} \mathrm{~N}$. <br> N. E. by E. $\frac{7}{8}$ E. <br> E. by N. <br> E. by S. $\frac{1}{4}$ S. <br> S. E. by E. $\frac{7}{8} \mathrm{E}$. <br> S. E. $\frac{3}{4} \mathrm{E}$. <br> S. E. by S. $\frac{3}{8}$ S. <br> S. by E. $\frac{5}{8}$ E. <br> S. $\frac{5}{3} \mathrm{E}$. <br> S. by W. $\frac{3}{8} \mathrm{~W}$. S. S. W. $\frac{3}{8} \mathrm{~W}$. <br> S. W. $\frac{5}{8}$ S. S. W. $\frac{1}{2} \mathrm{~W}$ W. <br> S. W. by W. $\frac{1}{2} \mathrm{~W}$. <br> W. by S. $\frac{3}{8}$ S. ${ }^{2}$ <br> W. $\frac{3}{3} \frac{3}{4} \mathrm{~S}$. <br> W. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4} \mathrm{~W}$. <br> N. W. N. W. $\frac{1}{3}$ W N <br> N. N. W. $\frac{1}{4} \mathrm{~W}$. N. by W. <br> N. by W. N. $\frac{1}{2}$ W. |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by $N$. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{3}{8} \mathrm{E}$. <br> N. by E. $\frac{1}{4} \mathrm{E}$. <br> N. N. E. $\frac{1}{8}$ E. <br> N. E. $\frac{1}{8}$ N. <br> N. E. $\frac{7}{8} \mathrm{E}$. <br> E. by N . <br> EAST. <br> E. by S. $\frac{1}{8}$.S. <br> S. E. by E. $\frac{7}{8}$ E. <br> S. E. $\frac{3}{4}$ E. <br> S. S. E. $\frac{5}{8}$ E. S. by E. $\frac{5}{8}$ E. <br> S. $\frac{5}{3} \mathrm{E}$. <br> S. by W. $\frac{3}{8} \mathrm{~W}$. S. S. W. $\frac{3}{8} \mathrm{~W}$. <br> S. W. $\frac{1}{2} \mathrm{~W}$. <br> S. W. by W. $\frac{1}{2}$ W. W. by S. $\frac{3}{8}$ S. <br> W. by S. $\frac{3}{8}$ S. <br> W. $\frac{3}{8} \mathrm{~S}$.. <br> W. by N. $\frac{7}{8}$ N. <br> N. W. by W. $\frac{1}{8}$ W. <br> N. W. $\frac{1}{8}$ W. N. W. $\frac{7}{8}$ N. <br> N. N. W. $\frac{1}{4}$ W. N. by W. $\frac{3}{8} \mathrm{~W}$. <br> N. $\frac{1}{2}$ W. |  |  |  |

[^12]Observations for Determining the Deviations of the After Binnacle Compass on the U. S. Iron Clad Monadnock.

| Panama, May 20, 1866. <br> Correction for Object $=+0^{\circ} \quad 1^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  | Acapulco, June 1, 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | $\begin{gathered} \text { Corrected } \\ \text { Deviation of } \\ \text { Compass. } \end{gathered}$ |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. S. E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. b. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{3}{8} \mathrm{E}$. <br> N. by E. 1 E . <br> N. E. by N. $\frac{7}{8}$ N. <br> N. E. by N . <br> N. E. by E. <br> N. E. by E. $\frac{7}{8}$ E. E. by N. <br> E. $\frac{1}{8} \mathrm{~S}$. <br> E. by S. $\frac{1}{8}$ S. <br> S. E. by E. $\frac{3}{4} \mathrm{E}$. <br> S. E. $\frac{3}{3} \mathrm{E}$ E. <br> S. E. by S. $\frac{5}{8}$ S. <br> S. $\stackrel{+}{\stackrel{1}{2} \mathrm{E}} \mathrm{E}$. <br> S. by w. $\frac{3}{8}$ W. <br> S. W. by S. $\frac{5}{8}$ S. <br>  <br> S. W. by $\mathrm{W} \cdot \frac{1}{2} \mathrm{~W}$. <br> W. by S. $\frac{1}{2}$ S. <br> W. ${ }^{\frac{1}{3}} \mathrm{~S}$. N . <br> W. by N. ${ }_{4}^{3} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{8}$ W. <br> N. W. $\mathrm{N} . \mathrm{W}$ $\frac{1}{3}$ B N N <br>  <br> $\stackrel{\text { N. }}{\text { Ny }} \mathrm{W}$. |  | $\bigcirc$ |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{3}{4} \mathrm{E}$. <br> N. by E. $\frac{1}{4} \mathrm{E}$. <br> N. E. $\frac{7}{8}$ N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. $\frac{7}{8} \mathrm{~N}$. <br> E. by S. $\frac{1}{4}$ S. <br> S. E. by E. $\frac{3}{4}$ E. <br> S. E. $\frac{5}{8}$ E. S. E. $\frac{3}{8}$ S. <br> S. S. E. $\frac{1}{2}$ E. S. by E. $\frac{1}{2}$ E. <br> S. $\frac{1}{2} \mathrm{E}$. S. $\frac{3}{8} \mathrm{~W}$. <br> S. by W. $\frac{3}{8}$ W. S. S. W. $\frac{3}{8}$ W. <br> S. W. $\frac{5}{8}$ S. S. W. $\frac{3}{8}$ W. <br> S. W. by W. $\frac{1}{2}$ W. W. by S. $\frac{1}{2}$ S. <br> W. $\frac{3}{8} \mathrm{~S}$. W. $\frac{3}{4} \mathrm{~N}$. <br> W. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by ${ }_{\mathrm{W}}^{\mathrm{W}} \mathrm{W} . \frac{1}{4} \mathrm{~W}$. <br> N. W. $\frac{1}{8}$ W. N. W. $\frac{3}{4}$ N. <br> N. N. W. $\frac{1}{4}$ W. <br> N. by W. $\frac{1}{4} \mathrm{~W}$. <br> N. $\frac{1}{2} \mathrm{~W}$. |  |  |  |

A deviation of the North Point of the Compass to the East is designated by the sign + ;
deviation to the West by the sign - A deviation of the North Point of the Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the

Observations for Determining the Deviations of the After Binnacle Compass on the U．S．Iron Clad Monadnock．

| Magdalena Bay，June 9， 1866. <br> Correction for Object $=-0^{\circ} 41^{\prime}$ ．Correction for Lubber Line $=+3^{\circ} 44^{\prime}$ ． |  |  |  |  | San Francisco，June 23， 1866. <br> Correction for Object．$=-0^{\circ} 45^{\prime}$ ．Correction for Lubber Line $=+3^{\circ} 49^{\prime}$ ． |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship＇s Head． | Bearing of Object by Compass． | Deviation of Compass in Points． | Deviation of Compass in Degrees． | Corrected Deviation of Compass． | Assumed Magnetic Direction of＇Ship＇s Head． | Bearing of Object by Compass． | Deviation of Compass in Points． | Deviation of Compass in Degrees． | Corrected Deviation of Compass． |
| NORTH． <br> N．by E． <br> N．N．E <br> N．E．by N． <br> N．E． <br> N．E．by E． <br> E．N．E． <br> E．by N． <br> EAST． <br> E．by S ． <br> E．S．E． S．E．by E． <br> S．E． <br> S．E．by S． <br> S．S．E． <br> S．by E． <br> SOUTH． <br> S．by W． S．S．W． <br> S．W．by S． <br> S．W． <br> S．W．by W． <br> W．S．W． <br> WEST． <br> W．by N ． <br> W．N．W． <br> N．W．by W． <br> N．W． <br> N．W．by N． <br> N．N．W． <br> N．by W． | N．$\frac{1}{2}$ E． <br> N．by E．$\frac{3}{8}$ E． <br> S．W．$\frac{1}{4} \mathrm{~W}$ ． <br> S．W．by W．$\frac{1}{4}$ W． <br> W．by S．$\frac{5}{8}$ S． <br> W．$\frac{1}{2} \mathrm{~S}$ ． <br> W．by N．$\frac{3}{4} \mathrm{~N}$ ． <br> N．W．by W．$\frac{1}{4}$ W． <br> N．W．$\frac{1}{4} \mathrm{~W}$ ． <br> N．W．$\frac{3}{4}$ N． <br> N．N．W．$\frac{1}{4}$ W． <br> N．by W．$\frac{4_{4}^{4}}{4} \mathrm{~W}$ ． <br> N．$\frac{3}{8} \mathrm{~W}$ ． | 二章 ${ }^{\text {a }}$ |  |  | NORTH． <br> N．by E． <br> N．N．E． <br> N．E． <br> N．E．by E． <br> E．N．E． <br> E．by N． <br> EAST． <br> E．by S． <br> S．F．by E． <br> S．E． <br> S．E．by S． <br> S．S．E． <br> S．by E． <br> SOUTH． <br> S．by W． <br> S．S．W． S．W．by S． <br> S．W． <br> S．W．by W． <br> W．S．W． <br> W．by S． <br> W．by N． <br> W．N．W． <br> N．W．by W． <br> N．W． <br> N．W．by N． <br> N．N．W． <br> NORTH． | N．$\frac{1}{2} \mathrm{E}$ ． <br> N．by E．$\frac{3}{3} \mathrm{E}$ ． <br> N．E．by N．$\frac{3}{4}$ N． <br> N．E． N．.$\frac{7}{8}$ $\frac{2}{8}$ N． E． <br> N．E．by E．$\frac{1}{8}$ E． <br> E．N．E． <br> E．by N ． <br> E．by S ． <br> S．E．by E．$\frac{7}{8}$ E． <br> S．E． $\begin{aligned} & \text { T．} \\ & \text { In } \\ & \text { E．} \\ & \text { E．} \\ & \text { ．}\end{aligned}$ <br> S．E．By E．$\frac{1}{8}$ S． <br> S．by E． <br> S．i $\frac{1}{8} \mathrm{~W}$ ． <br> S．by W．$\frac{1}{8}$ W． S．W．by S． S． <br> S． $\mathrm{W} . \frac{7}{7} \mathrm{~S}$ S． <br> S．W．by W．$\frac{3}{3}$ W． <br> W．by S．童S． <br> W．$\frac{1}{2} \mathrm{~S}$ ． <br> W．by N．$\frac{3}{4} \mathrm{~N}$ ． <br> N．W．by W．$\frac{1}{4} \mathrm{~W}$ ． <br> N．W． <br> $\mathrm{N} . \mathrm{W}$ <br> $\frac{4}{8} \mathrm{~W}$ <br> N ． <br> N．W．by N．$\frac{7}{3}$ N． N．by W． $\frac{1}{4}$ W． <br> N．$\frac{3}{8} \mathrm{~W}$ ． |  |  |  |
| A deviation of the North Point of the Compass to the East is designated by the sign + ； a Geviation to the West by the sign－． <br> From the observations given above，the following values of the coefficients of the deviation are obtained： $\begin{array}{llll} \mathrm{A}=-\mathrm{I}^{\circ} & \begin{array}{l} 10^{\prime} .7 \\ \mathrm{D}=+2^{\circ} \\ \mathrm{IO}=+2 \end{array} & \begin{array}{l} \mathrm{I} 6^{\prime} .0 \\ \mathrm{E}=0^{\prime} .0 \end{array} & \mathrm{C}=0^{\circ} \\ 3^{\prime} \cdot 5 \end{array} \mathrm{I}^{\circ} 1^{16^{\prime} .8}$ |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign＋； a deviation to the West by the sign－． <br> From the observations given above，the following values of the coefficients of the deviation are obtained： |  |  |  |  |

Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Hampton Roads, November I, 1865. <br> Correction for Object $=+3^{\circ} 57^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | St. Thomas, November 18, 1865. <br> Correction for Object $=+0^{\circ} 16^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | $\begin{gathered} \text { Corrected } \\ \text { Deviation of } \end{gathered}$ Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N . <br> EAST. <br> E. by S. <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{1}{8} \mathrm{~W}$. N. $\frac{5}{8} \mathrm{E}$. <br> N. by E. $\frac{1}{4}$ E. <br> N. E. by N. <br> N. E. $\frac{1}{4}$ N. N. E. $\frac{3}{4} \mathrm{E}$. <br> N. E. by E. $\frac{1}{2}$ E. E. by N. <br> E. by N. $\frac{1}{4}$ N. <br> E. $\frac{1}{2} \mathrm{~N}$. E. $\frac{3}{4} \mathrm{~S}$. <br> E. S. E. $\frac{1}{4}$ E. <br> S. E. <br> S. E. by E. <br> S. by E. $\frac{1}{2}$ E. <br> S. $\frac{1}{2}$ E. S. $\frac{3}{4}$ W. <br> S. $\frac{3}{4}$ W. W. <br> S. W. $\frac{3}{4}$ S. <br> S. W. $\frac{1}{2}$ W. <br> S. W. by W. W. by S. $\frac{1}{8}$ S. <br> W. $\frac{1}{2} \mathrm{~S}$. W. $\frac{1}{2} \mathrm{~N}$. <br> W. by N. $\frac{1}{2} \mathrm{~N}$. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{5}{8}$ N. <br> N. N. W. $\frac{1}{2}$ W. N. by W. $\frac{3}{4}$ W. <br> N. $\frac{7}{8} \mathrm{~W}$. | + <br> + <br> $+\frac{3}{3}$ <br> $+\frac{3}{4}$ <br> + |  |  | NORTH. <br> N. by E. <br> N. N.E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{3}{8}$ W. <br> N. by E. $\frac{1}{4}$ E. <br> N. E. by N. <br> N. E. $\frac{1}{8} \mathrm{~N}$. <br> N. E. by E. $\frac{7}{8}$ E. <br> E. by N. <br> E. $\frac{1}{8} \mathrm{~N}$. E. by S. <br> S. E. by E. $\frac{7}{8}$ E. <br> S. E. $\frac{5}{8}$ E. S. E. $\frac{1}{2}$ S. <br> S. E. by S. $\frac{5}{8} \mathrm{~S}$. <br> S. by E. $\frac{1}{4}$ E. <br> S. $\frac{1}{8} \mathrm{E}$. S. $\frac{7}{8} \mathrm{~W}$. <br> S. S. W. <br> S. W. by S. <br> S. W. $\frac{1}{8}$ W. S. W. by W. $\frac{1}{8}$ W. <br> W. by S. $\frac{7}{8}$ S. <br> W. $\frac{3}{4} \mathrm{~S}$. W. $\frac{3}{8} \mathrm{~N}$. <br> W. by N. $\frac{1}{2}$ N. N. W. by W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2}$ W. N. W. $\frac{3}{8}$ N. <br> N.W. by N. $\frac{1}{4}$ N. <br> N. N. W. N. by W. $\frac{1}{8}$ W. |  |  |  |

[^13]Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 1865. Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=+6^{\circ} 1^{\prime}$. |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+\mathrm{r}^{\circ}, 5^{\prime}$ Correction for Lubber Line $=+6^{\circ} 18^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> SOUTE <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by w. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | E. ${ }_{\text {E }} \frac{1}{4} \frac{1}{4} \mathrm{~N}$. | + | - , | + $11^{\circ}{ }^{50}$ +14 | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{2} \mathrm{E}$. N. N. E E. $\frac{1}{2} \mathrm{E}$. N. <br> N. E. by N. $\frac{1}{4}$ E. <br> N. E. $1 .{ }^{1} \mathrm{E}$. <br> N. E. by E. <br> E. by N. $\frac{3}{4} \mathrm{~N}$. <br> E. $\frac{1}{3} \mathrm{~N}$. <br> E. by $\mathrm{S} . \frac{3}{4} \mathrm{~S}$. |  |  |  |

[^14]Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865. <br> Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=+6^{\circ} 18^{\prime}$. |  |  |  |  | Rio Janeiro, January 10, I866. <br> Correction for Object $=+2^{\circ} 44^{\prime}$. Correction for Lubber Line $=+5^{\circ} 43^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N.W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N . <br> N $\frac{3}{4}$ E. <br> N. N. E. $\frac{1}{4}$ N. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ E. <br> N. E. by E. $\frac{1}{4}$ E. <br> E. by N. $\frac{3}{4}$ N. <br> E. $\frac{1}{2}$ N. <br> E. $\frac{1}{2}$ S. <br> E. by S. $\frac{1}{2}$ S. <br> S. E. by E. $\frac{1}{2}$ E. <br> S. E. $\frac{1}{4}$ E. <br> S. E. $\frac{3}{4}$ S. <br> S. S. E. $\frac{1}{4}$ E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. $\frac{1}{4}$ W. <br> S. W. by W. $\frac{1}{4}$ W. <br> W. by S. $\frac{1}{2}$ S. <br> W. $\frac{1}{2}$ S. <br> W. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4}$ W. <br> N. W. $\frac{1}{4}$ W. <br> N. W. $\frac{3}{4}$ N. <br> N. N. W. $\frac{1}{2}$ W. <br> N. by W. $\frac{3_{3}^{3}}{4} \mathrm{~W}$. <br> N. $\frac{3}{4}$ W. |  <br>  <br> + <br> + <br> + <br> + <br> + <br> + | - 1 |  | NORTH. <br> N. by E. <br> N. N. E <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N.. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. E. by N. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2} \mathrm{~N}$. <br> N. E. $\frac{1}{2} \mathrm{E}$. <br> N. E. by E. $\frac{1}{4}$ E. <br> E. by N. $\frac{3}{4}$ N. <br> E. $\frac{1}{2} \mathrm{~N}$. <br> E. S. E. $\frac{1}{8}$ E. <br> S. E. by $\underset{\text { E. }}{\frac{1}{8}} \mathrm{E}$. <br> S. E. $\frac{1}{8}$ E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. | + <br> + <br> + <br> + <br> + <br> + <br> + | - 1 | $\begin{array}{lr} +14^{\circ} & 0^{\prime} \\ +14 & 0 \\ +14 & 0 \\ +16 & 10 \\ +16 & 50 \\ +14 & 40 \\ +12 & 0 \\ +10 & 10 \\ +9 & 50 \\ + & 50 \\ +8 & 30 \\ +8 & 30 \\ +8 & 30 \\ +8 & 30 \\ +8 & 30 \\ +8 & 30 \\ +8 & 30 \end{array}$ |

[^15]Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Monte Video, January 24, 1866. <br> Correction for Object $=-0^{\circ} 13^{\prime} . \quad$ Correction for Lubber Line $=+4^{\circ} 9^{\prime}$. |  |  |  |  | Sandy Point, February ıо, 1866. <br> Correction for Object $=+0^{\circ} 7^{\prime}$. Correction for Lubber Line $=+4^{\circ} 9^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected <br> Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. $\frac{1}{2}$ E. <br> N. by E. $\frac{1}{2}$ E. <br> N. E. by N. $\frac{3}{4}$ N. <br> N. E. $\frac{3}{4} \mathrm{~N}$. <br> N. E. $\frac{1}{4}$ E. <br> N. E. by E. <br> E. N. E. <br> E. $\frac{1}{2}$ N. <br> E. by S. <br> E. S. E. <br> S. E. by E. $\frac{1}{4}$ S. <br> S. E. $\frac{3}{4}$ S. <br> S. E. by S. $\frac{1}{2}$ S. <br> S. S. E. <br> SOUTH. <br> S. $\frac{3}{4}$ W. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. <br> S. W. <br> S. W. $\frac{1}{2} \mathrm{~W}$. |  | - 1 | $\begin{array}{lcc} + & 4^{\circ} & o^{\prime} \\ + & 9 & 30 \\ + & 3 & 30 \\ + & 12 & 20 \\ +12 & 20 \\ + & 12 & 20 \\ +15 & 10 \\ +15 & 0 \\ + & 9 & 20 \\ + & 4 & 0 \\ + & 3 & 50 \\ + & 1 & 0 \\ - & 4 & 30 \\ \hline+ & 1 & 40 \\ + & 4 & 0 \\ + & 4 & 0 \\ + & 4 & 0 \\ + & 6 & 50 \\ + & 6 & 50 \\ + & 4 & 0 \\ + & 4 & 0 \\ + & 9 & 30 \end{array}$ | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8} \mathrm{~W}$. <br> N. $\frac{3}{4} \mathrm{E}$. <br> N. by E. $\frac{1}{2}$ E. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ N. N. E. $\frac{1}{1} \mathrm{E}$. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{2}$ N. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> E. by S. $\frac{1}{4}$ S. <br> E. S. E. $\frac{1}{8}$ S. <br> S. E. by E. $\frac{1}{4}$ S. <br> S. E. $\frac{1}{8}$ S. <br> S. E. by S. $\frac{1}{8}$ S. <br> S. by E. $\frac{3}{4}$ E. <br> S. $\frac{1}{2} \mathrm{E}$. <br> S. $\frac{1}{3}$ W. <br> S. by W. $\frac{1}{4}$ W. <br> S. W. by S. $\frac{3}{4} \mathrm{~S}$. <br> S. W. $\frac{1}{2}$ S. <br> S. W. W.S. $\frac{3}{4} \mathrm{~W}$ W. <br> W. by S . <br> WEST. <br> W. by N. $\frac{1}{8}$ N. <br> W. N. W. $\frac{1}{8}$ N. <br> N. W. $\frac{3}{4}$ W. <br> N. W. $\frac{1}{4}$ N. <br> N. N. W. $\frac{3}{4}$ W. <br> N. N. W. $\frac{1}{8}$ N. <br> N. by W. | + <br> + <br> + <br> + <br> + |  |  |

A deviation of the North Point of the Compass to the East is designated by the sign + ; $\quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign } \\ & \text { a deviation to the West by the sign - }\end{aligned}$
deviation to the West by the sign From the observations given above, the following values of the coefficients of the $\begin{gathered}\text { From the observations given above, the following values of the coefficients of the } \\ \text { deviation are obtained: }\end{gathered}$

Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Valparaiso, April 4, 1866. <br> Correction for Object $=+0^{\circ} \quad 1^{\prime}$. Correction for Lubber Line $=+4^{\circ} \quad 17^{\prime}$. |  |  |  |  | Callao, April 29, 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by.N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W <br> NORTH. | NORTH. <br> N. $\frac{3}{4} \mathrm{E}$. <br> N. by E. $\frac{3}{4}$ E. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ E. <br> E. N. E. $\frac{1}{4}$ N. <br> E. by N. $\frac{1}{2}$ N. <br> E. $\frac{1}{4} \mathrm{~N}$. <br> E. $\frac{3}{4}$ S. <br> E. S. E. $\frac{1}{4}$ E. <br> S. E. by E. $\frac{1}{4}$ E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> S. $\frac{1}{4} \mathrm{~W}$. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. $\frac{3}{4} \mathrm{~S}$. <br> W. $\frac{1}{2} \mathrm{~N}$. <br> W. by N. $\frac{1}{2}$ N. <br> N. W. by W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{4} \mathrm{~N}$. <br> N. W. by N. $\frac{1}{2} \mathrm{~N}$. <br> N. by W. $\frac{3}{4}$ W. <br> N. by W. |  |  |   <br> +  <br> +  <br> +7 20 <br> +7 0 <br> +7 0 <br> +9 50 <br> +9 50 <br> +9 50 <br> +7 0 <br> +9 50 <br> +7 0 <br> +7 0 <br> +7 0 <br> +7 0 <br> +4 20 <br> +4 20 <br> +4 20 <br> +4 20 <br> +1 30 <br> +4 20 <br> +4 20 <br> +4 20 <br> +4 20 <br> +4 20 <br> +4 20 <br> +1 30 <br> -1 20 <br> -1 20 <br> -1 20 | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8}$ W. <br> N. $\frac{1}{2} \mathrm{E}$. <br> N. by E. $\frac{1}{2}$ E. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2} \mathrm{~N}$. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{2}$ N. <br> E. $\frac{1}{2} \mathrm{~N}$. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> E. by S. $\frac{3}{4} \mathrm{~S}$. <br> S. E. by ${ }^{4}$. $\frac{1}{4}$ E. <br> S. E. $\frac{1}{2}$ E. <br> S. E. $\frac{3}{4} \mathrm{~S}$. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. $\frac{1}{4}$ W. <br> S. W. by W. $\frac{1}{4}$ W. <br> W. by S. $\frac{1}{2}$ S. <br> W. $\frac{1}{2}$ S. <br> W. $\frac{1}{2} \mathrm{~N}$. <br> W. by N. $\frac{1}{2}$ N. <br> N. W. by W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2}$ W. N. W. $\frac{1}{2}$ N. <br> N. W. by N. ${ }^{\frac{1}{2}} \mathrm{~N}$. <br> N. sby W. $\frac{3}{4}$ W. <br> N . by W. |  | - 1 | $\begin{array}{lc} +5^{\circ} & 20^{\prime} \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +9 & 30 \\ +6 & 40 \\ +6 & 40 \\ +9 & 30 \\ +6 & 40 \\ +6 & 40 \\ +3 & 50 \\ +3 & 50 \\ +3 & 50 \\ +3 & 50 \\ +3 & 50 \\ +1 & 0 \\ +1 & 0 \\ \hline 1 & 0 \\ \hline-1 & 50 \\ -1 & 50 \\ \hline-1 & 50 \\ \hline-1 & 50 \\ \hline-1 & 50 \\ \hline-1 & 50 \\ \hline \end{array}$ |

[^16]Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock

| Panama, May 20, 1866. <br> Correction for Object $=+0^{\circ} \quad 1^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  | Acapulco, June I, 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$. Correction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of <br> Compass in Points. | Deviation of Compass in Degrees | $\begin{gathered} \text { Corrected } \\ \text { Deviation of } \\ \text { Compass. } \end{gathered}$ |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | NORTH. <br> N. $\frac{3}{4} \mathrm{E}$. <br> N. by E. $\frac{3}{4}$ E. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. N. E. $\frac{1}{2}$ N. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{3}{4}$ N. <br> E. $\frac{3}{4}$ N. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> S. Ey S. $\frac{1}{2}$ S. <br> S. E. $\frac{1}{8}$ E. <br> S. E. by S. $\frac{3}{4}$ S. <br> S. by E. <br> SOUTH. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. by S. <br> W. $\frac{1}{8} \mathrm{~N}$. <br> W. by N. $\frac{1}{8}$ N. <br> N. W. W. $\frac{3}{4}$ W. ${ }^{\frac{1}{8}}$. <br> N. W. $\frac{1}{8} \mathrm{~N}$. <br> N.W. by N. $\frac{1}{4}$ N. <br> N. by W. N. $\frac{3}{4}$ W. |  |  |  | NORTH. <br> N. by E. <br> N. N. E. N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> EAST. <br> E. by N. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. NORTH. | N. $\frac{1}{1} \mathrm{~W}$. <br> N. by E. $\frac{3}{4} \mathrm{E}$. <br> N. E. by N. $\frac{1}{2}$ N. <br> N. E. ${ }^{\frac{1}{2}} \mathrm{~N}$ N. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{2}$ N <br> E. ${ }^{1} \mathrm{~N}$ N. <br> E. ${ }^{4}$. E. $1 \frac{1}{4}$ E. <br> S. E. by E. $\frac{1}{4} \mathrm{E}$ <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. ${ }_{\frac{1}{4}}$ W. <br> $\underset{\text { W. Wy by }}{ }$ W. $\frac{1}{2} \mathrm{~W}$. <br> W. by S. $\frac{1}{2}$ S. <br> W. ${ }^{\frac{1}{2}} \mathrm{~S}$ S. <br> W. by N. $1+\mathrm{N}$. N. W. by W. $\frac{3}{4}$ W. <br> N. W. N N $\frac{1}{2} \mathrm{~W}$ W N <br> N. W. by N. $\frac{1}{4} \mathrm{~N}$. <br> N. by w. |  |  |  |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -. <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign +; a deviation to the West by the sign -. <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  |

Observations for Determining the Deviations of the After Ritchie Compass on the U. S. Iron Clad Monadnock.

| Magdalena Bay, June 9, 1866. <br> Correction for Object $=-0^{\circ} 4 \mathbf{I}^{\prime}$. Corréction for Lubber Line $=+3^{\circ} 44^{\prime}$. |  |  |  |  | San Francisco, June 23, 1866. <br> Correction for Object $=-0^{\circ} 45^{\prime}$. Correction for Lubber Line $=+3^{\circ} 49^{\prime}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. F. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8}$ E. N. by E. <br> S. W. $\frac{1}{8}$ W. <br> S. W. by W. <br> W. S. W. <br> W. by S . <br> W. $\frac{1}{8} \mathrm{~N}$. <br> W. by N. $\frac{1}{2} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4}$ W. <br> N. W. $\frac{1}{4} \mathrm{~W}$. <br> N. W. $\frac{1}{2} \mathrm{~N}$. <br> N. W. by N. $\frac{1}{2}$ N. <br> N. by W. $\frac{1}{2}$ W. <br> N. 咅 W. | $-0^{\frac{1}{8}}$ <br>  <br>  <br>  <br>  <br>  <br>  <br>  <br>  | - 1 |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8}$ E. <br> N. $\frac{3}{4} \mathrm{E}$. <br> N. by E. ${ }_{4}^{4} \mathrm{E}$. <br> N. N. E. $\frac{1}{2}$ E. <br> N. E. $\frac{3}{4} \mathrm{~N}$. <br> N. E. $\frac{1}{4}$ E. <br> N. E. by E. $\frac{1}{4}$ E. <br> E. by N. $\frac{3}{4}$ N. <br> E. $\frac{3}{4} \mathrm{~N}$. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> E. by S. $\frac{1}{2}$ S. <br> S. E. by E. $\frac{1}{2}$ E. <br> S. E. $\frac{1}{2}$ E. <br> S. E. $\frac{3}{4} \mathrm{~S}$. <br> S. by E. $\frac{1}{4} \mathrm{E}$ <br> S. S. E. $\frac{1}{4}$ E. <br> S. $\frac{1}{4} \mathrm{E}$. <br> S. $\frac{3}{4} \mathrm{~W}$. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. $\frac{1}{4}$ S. <br> S. W. <br> S. W. by W. $\frac{1}{4}$ W. <br> W. by S. $\frac{3}{4}$ S. <br> W. $\frac{1}{2} \mathrm{~S}$. <br> W. $\frac{1}{2}$ N. <br> W. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4}$ W. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2}$ N. <br> N. W. by N. $\frac{1}{2}$ N. <br> N. N. W. $\frac{1}{2}$ N. <br> N. $\frac{3}{4}$ W. |  | - |  |

A deviation of the North Point of the Compass to the East is designated by the sign +; A deviation of the North Point of the Compass to the East is designated by the sign + ;
a deviation to the West by the sign - West by the sign From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
 $\mathrm{A}=+3^{\circ} \frac{35^{\prime} .5}{\mathrm{D}=+\mathrm{I}^{\circ}} \stackrel{\mathrm{B}=+4^{\circ}}{50^{\prime} .7} \stackrel{27^{\prime} \cdot 3}{\mathrm{E}=3}=+\mathrm{o}^{\circ} \underset{\mathrm{IO}^{\prime} .6}{\mathrm{C}=-2^{\circ}} 5 \mathrm{I}^{\prime} .0$
20
October, 1872.
Observations for Determining the Deviations of the After Azimuth Compass on the U. S. Iron Clad Monadnock.

| Hampton Roads, November I, 1865. Correction for Object $=+3^{\circ} 57^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | St. Thomas, November 18, 1865. <br> Correction for Object $=+o^{\circ} 16^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points | Deviation of <br> Compass in <br> Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> WEST. <br> W. by N. <br> W. N. W. N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. <br> N. by W. | $\begin{array}{llll}\text { N. } & 3 \\ \text { N }\end{array}$ |  |  |  |  |  |  |  |  $0^{\circ} 10{ }^{\prime}$ |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -. <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -. <br> From the observations given above, the following values of the cofficients of the deviation are obtained: |  |  |  |  |

Observations for Determining the Deviations of the After Azimuth Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 1865. Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=0$ |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+\mathrm{I}^{\circ} 5^{\prime \prime} \quad$ Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected <br> Deviation of <br> Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. WEST. <br> W. by N . <br> W. N. W. <br> N. W. <br> N. W. by W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | S. S. $_{60} \mathrm{mo}^{\circ} \mathrm{E}$ E. |  | - $20^{\circ} \mathrm{o}$ -15 | - ${ }^{20} 0^{\circ} \mathrm{O}^{\prime}$ -15 | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $4^{\circ}$ E. <br> N. $\mathrm{I}^{2}$ E. <br> N. 24 E.  <br> N. 38 E. <br> N. 45 E.  <br> N. 58 E.  <br> N. 78 E.  <br> S. 69 E.  <br> S. 59 E.  <br> S. 48 E.  | traverse well be worth the |  |  |

[^17]Observations for Determining the Deviations of the After Azimuth Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865. <br> Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=\mathrm{c}$. |  |  |  |  | Rio Janeiro, January 10, 1866. <br> Correction for Object $=+2^{\circ} \quad 44^{\prime}$. Correction for Lubber Line $=0^{\circ}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | $\begin{aligned} & \text { Corrected } \\ & \text { Deviation of } \\ & \text { Compass. } \end{aligned}$ |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST.. <br> E. by S. <br> E. S. E. S. E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N.W. by N. <br> N. N. W. <br> NORTH. |  |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. |  |  |  |  |

[^18]Observations for Determining the Deviations of the After Azimuth Compass on the U．S．Iron Clad Monadnock．

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{\begin{tabular}{l}
Sandy Point，February io， 1866. \\
Correction for Object \(=+0^{\circ} 7^{\prime}\) ．Correction for Lubber Line \(=0\).
\end{tabular}} \& \multicolumn{5}{|l|}{\begin{tabular}{l}
Valparaiso，April 4， 1866. \\
Correction for Object \(=+0^{\circ} \mathbf{I}^{\prime}\) ．Correction for Lubber Line \(=0\).
\end{tabular}} \\
\hline Assumed Magnetic Direction of Ship＇s Head． \& Ship＇s Head by
Compass． \& Deviation of Compass in Points． \& Deviation of Compass in Degrees． \& Corrected Deviation of Compass． \& Assumed Magnetic Direction of Ship＇s Head． \& Ship＇s Head by
Compass． \& Deviation of Compass in Points． \& \begin{tabular}{l}
Deviation of \\
Compass in \\
Degrees．
\end{tabular} \& \begin{tabular}{l}
Corrected \\
Deviation of \\
Compass．
\end{tabular} \\
\hline NORTH． \& N． \(\mathrm{I}^{\circ} \mathrm{E}\) ． \& \& － \(\mathrm{r}^{\circ} \mathrm{o}^{\prime}\) \& － \(0^{\circ} 5^{\prime}\) \& NORTH． \& N． \(2^{\circ} \mathrm{E}\) ． \& \& \(2^{\circ} \mathrm{o}^{\prime}\) \& － \(2^{\circ}{ }^{\prime}\) \\
\hline N．by E． \& N． 11 E． \& \& ＋0 15 \& ＋0 20 \& N．by E． \& N．ic E． \& \& ＋ 15 \& ＋ 120 \\
\hline N．N．E． \& N． 19 E． \& \& ＋330 \& ＋340 \& N．N．E． \& N． 21 E ． \& \& ＋ 130 \& ＋130 \\
\hline N．E．by N ． \& N． 30 E． \& \& ＋345 \& ＋ \& N．E．by N． \& N． 33 E ． \& \& ＋+45 \& ＋\({ }^{+} 50\) \\
\hline N．E． \& N． 40 E． \& \& ＋ \& ＋ 10 \& N．E．\({ }_{\text {cher }}\) \& N． 45 E ． \& \& \(\bigcirc\) \& \(\bigcirc\) \\
\hline N．\({ }_{\text {N．}}^{\text {E．}}\) N．by E． \& \(\begin{array}{ll}\text { N．} \& 54 \\ \text { N．} \\ 64 \& \text { E．} \\ \text { E．}\end{array}\) \& \& \(\begin{array}{r}+215 \\ +\quad 430 \\ \hline\end{array}\) \& +220
+440 \& N．E．by E． \&  \& \& 二 045 \& － 040 \\
\hline E．\({ }_{\text {E．}}^{\text {E．N．E．}}\) \& \(\begin{array}{ll}\text { N．} \\ \text { N．} 80 \& \text { E．} \\ \text { cer }\end{array}\) \& \& \(\begin{array}{r}\text {＋} \\ +130 \\ \hline 15\end{array}\) \& \(\begin{array}{r}\text {＋} \\ +10 \\ \hline 10\end{array}\) \& E．\({ }_{\text {E．}}^{\text {b．}}\) N．E． \&  \& \& 二 230 \& － 230 \\
\hline EAST． \& S． 89 E ． \& \& －1 \& 二－ 50 \& EAST． \& S． 82 E ． \& \& 二 8 \％ \& 二 80 \\
\hline E．by S． \& S． 71 E ． \& \& －745 \& －740 \& E．by S． \& S． 66 E ． \& \& － 1245 \& － 1240 \\
\hline E．S．E． \& S． 60 E ． \& \& － 730 \& －7 20 \& E．S．E． \& S．\({ }^{56} \mathrm{E}\) E． \& \& （11 \({ }^{11}\) \& －1130 \\
\hline \begin{tabular}{l}
S．E．by E． \\
S．E．
\end{tabular} \& S．\({ }_{\text {S．}} 46 \mathrm{E}\) E． \& \& －9 \({ }^{15}\) \& －9 \({ }^{10}\) \& S．E．\({ }_{\text {S．}}\) S． \& S．
S．
S \& \& － 1115 \& － 11 \\
\hline S．E．by S． \& S． 27 E ． \& \& －645 \& －640 \& S．E．by S． \& S． 24 E ． \& \& － 945 \& － 940 \\
\hline S．S．E． \& S．\({ }_{8}^{66} \mathrm{E}\) ． \& \& －630 \& －620 \& S．S．E． \& S． 16 E ． \& \& － 630 \& － 630 \\
\hline S．by E． \& S． 8 E． \& \& \(\begin{array}{lll}-3 \& 15\end{array}\) \& －3 10 \& S．by E． \& S． \(6 \underset{\mathrm{~W}}{\mathrm{E}}\) ， \& \& \& － 5 10 \\
\hline SOUTH． \& S．\({ }_{\text {c }}^{\text {I }}\) E． \& \& ＋10 \& ＋ 110 \& SoUTH． \& S．\({ }^{2} \mathrm{~W}\) ． \& \& －\({ }^{2} 0\) \& － 20 \\
\hline S．by w．
S．s．W． \& \& \& ＋ 15 \& ＋ 520 \& S．by W．
S．S．w． \& S． 11 W W． \& \& ＋ 115 \& ＋ 0 \\
\hline S．S．W．by s． \&  \& \& ＋
+530
+745 \& ＋
\(+\quad 40\)
+750 \& S．S．W．\({ }_{\text {S }}\) S． \& S． 20
S．
29
2 \& \& ＋
\(+\quad 30\)
\(+\quad 45\) \& \(+\quad 230\)
\(+\quad 450\) \\
\hline S．w． \& S． 37 w ． \& \& ＋80 \& ＋810 \& s．w． \& S． 38 W ． \& \& ＋\({ }^{4}{ }^{4}\) \& ＋ 4 \％ \\
\hline S．W．by w． \& S． 47 W ． \& \& ＋915 \& ＋920 \& S．W．by w． \& S． 50 W ． \& \& ＋615 \& ＋ 620 \\
\hline W．S．W． \& S． 58 W． \& \& \& \& W．S．W． \& S．， 60 W ． \& \& ＋ 730 \& +730 \\
\hline W．by S． \&  \& \& +935
+445
+40 \& +950
+410 \& W．by S．
WEST． \& \begin{tabular}{l} 
S． \\
S． \\
S． \\
87 \\
87 \\
\hline
\end{tabular} \& \&  \& a
\(+\quad 450\)
\(+\quad 30\) \\
\hline W．by N ． \& N． 80 w ． \& \& ＋115 \& ＋120 \& W．by N ． \& N． 78 W． \& \& －\({ }^{3} 45\) \& －\({ }^{1}\) \\
\hline W．N．W． \& N． 66 W ． \& \& －130 \& －120 \& w．N．W．\({ }^{\text {d }}\) \& N． 65 W ． \& \& － 230 \& － 230 \\
\hline N．W．by W． \& N． 50 W． \& \& \begin{tabular}{ll}
-6 \& 15 \\
\hline-6 \& 0
\end{tabular} \& \(\begin{array}{ll}-6 \& 10 \\ -5 \& 50\end{array}\) \& N．W．by W． \&  \& \& \& － 410 \\
\hline \(\stackrel{\text { N．W．}}{\text { N．W．by }}\) \& N．
N． 28

28 \& \& － 60 \& | -5 |
| :--- |
| -50 | \& N．W．by n． \& N．${ }_{\text {N．}}{ }^{49}$ \％W． \& \& － 50 \& － 50 <br>

\hline N．N．W． \& N． 18 W． \& \& －430 \& －4 20 \& N．N．W． \& N．${ }^{19} \mathrm{~W}$ W． \& \& － 330 \& － 330 <br>

\hline N．by W． \& N． 6 w． \& \& －5 $\begin{aligned} & 15\end{aligned}$ \&  \& | $\mathrm{N} . \mathrm{by} \mathrm{W}$ ． |
| :--- |
| NORTH | \& \& \& －315 \& － 210 <br>

\hline
\end{tabular}

[^19]Observations for Determining the Deviations of the After Azimuth Compass on the U. S. Iron Clad Monadnock.

| $\begin{gathered} \text { Callao, April 29, } 1866 . \\ \text { Correction for Object }=+o^{\circ} \\ 6^{\prime} . \end{gathered} \text { Correction for Lubber Line }=0 .$ |  |  |  |  | $\begin{gathered} \text { Panama, May 20, } 1866 . \\ \text { Correction for Object }=+0^{\circ} 1^{\prime} \text {. Correction for Lubber Line }=0 . \end{gathered}$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. by S. <br> WEST. <br> W. by N. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. |  |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. |  |  |  |  |

[^20]Observations for Determining the Deviations of the After Azimuth Compass on the U．S．Iron Clad Monadnock．

| Acapulco，June I， 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$ ．Correction for Lubber Line $=0$. |  |  |  |  | Magdalena Bay，June 9， 1866.Correction for Object $=-0^{\circ} 4 \mathrm{I}^{\prime}$ ．Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship＇s Head． | Ship＇s Head by Compass． | Deviation of Compass in Points． | Deviation of Compass in Degrees． | Corrected Deviation of Compass． | Assumed Magnetic Direction of Ship＇s Head． | Ship＇s Head by Compass． | Deviation of Compass in Points． | Deviation of Compass in Degrees． | $\begin{array}{\|c} \text { Corrected } \\ \text { Deviation of } \\ \text { Compass. } \end{array}$ |
| NORTH． | N． $2^{\circ} \mathrm{E}$ ． |  | － $2^{\circ}$ | － $\mathrm{I}^{\circ}{ }^{5}{ }^{\prime}$ | NORTH． | $7{ }^{\circ} \mathrm{E}$ ． |  |  |  |
| N．by E． | N． 13 E ． |  | － 145 | －I 40 | N．by E． | N． 15 E ． |  | －345 | － $4{ }^{30}$ |
| N．N． N ．E．by N ． | N． 23 N .33 E ． |  | 工甭 30 | ＋ $\begin{array}{r}\circ \\ \hline\end{array}$ | N．N．E．${ }_{\text {N．}}$ |  |  |  |  |
| N．E． | N． 45 E． |  | $\begin{array}{r}+0 \\ \hline\end{array}$ | ＋ | N．E．by |  |  |  |  |
| N．E．by E． | N． 57 E ． |  | － 045 | 二 ${ }^{1} 40$ | N．${ }_{\text {N．}}$ ．by E． |  |  |  |  |
| E．by N ． | N．${ }^{70}$ E ${ }^{\text {E }}$ E． |  | 二 ${ }^{2} 380$ | 二 $2^{20} 10$ | E．N．${ }_{\text {E．}}^{\text {E．}}$ N． |  |  |  |  |
| EAST． | S． 82 E ． |  | －80 | － 750 | EAST． |  |  |  |  |
| E．by S． | S． 69 E ． |  | － 945 | － 940 | $\stackrel{\text { E．by }}{ }$ S． |  |  |  |  |
| S．E．by E． | S．${ }^{56}$ E． |  | 二11130 | 11 <br> 11 <br> 11 | ${ }_{\text {E．}}^{\text {E．E．E．by E．}}$ |  |  |  |  |
| S．E． | S． 34 E ． |  | － 11 \％ | － 1050 | S．E． |  |  |  |  |
| S．E．by S． | S． 24 E ． |  | －9．45 | － 940 | S．E．by S． |  |  |  |  |
| S．by E． | $\begin{array}{llll}\text { S．} & 14 & \mathrm{E} . \\ \mathrm{S} . & 5 \\ 5 & \text { E．}\end{array}$ |  | －8 ${ }^{8} \mathbf{3 0}$ | －8 ${ }^{80}$ | S．S．E． |  |  |  |  |
| SOUTH． | S． 3 W． |  | － 3 \％ | － 250 | SOUTH． |  |  |  |  |
| S．by w． | S． 11 W ． |  | ＋ 15 | ＋${ }^{1} 20$ | S．by W． |  |  |  |  |
| S．W．W．by． | S． $21 . \mathrm{W}$ S． |  | 1 $+\quad 130$ $+\quad 45$ | $\begin{array}{r}140 \\ +\quad 350 \\ \hline\end{array}$ | S．S．W．${ }_{\text {S }}$ W． |  |  |  |  |
| S．w． | S． 40 w ． |  | ＋${ }^{1}$ | ＋ | S．w．by | S． 34 W ． |  | ＋ 110 |  |
| S．W．by W． W．S．W． | S． 51 w S． |  |  | a $+\quad 50$ $+\quad 40$ | S．W．by w． | S． 47 W ． |  | ＋ 915 | ＋ 840 |
| W．S．W． | S． 63 W ． |  | ＋ | $+\quad 440$ $+\quad 150$ | W．S．W． | S． 58 W ． |  | +930 | ＋ 840 |
| WEST． | N． 89 w ． |  | ＋ 145 | ＋ | WEST． | S． 71 W． |  | ＋ 745 | a $+\quad 7$ +430 |
| W．by N． | N． 76 W ． |  | － 245 | － 240 | W．by N ． | N． 87 W ． |  | ＋ 815 | P $+\quad 430$ $+\quad 730$ |
| W．N．W．w． | N． 62 <br> N． |  | 二 5130 | － $5^{20}$ | W．N．W． | N． 73 W ． |  | ＋ 530 | ＋ 4.40 |
| N．W． | N． 38 w． |  | 二 7 \％ | 二 615 | N．W．by w． | N．${ }_{\text {N }}{ }_{4} 98 \mathrm{~W}$ W． |  | \％ 245 <br> $\quad 40$ | 140 $+\quad 410$ |
| N．W．by N． | N． 28 W． |  | － 545 | － 540 | N．W．by N ． | N． 38 W． |  |  | a <br>  <br> $+\quad 340$ |
| N．N．W． | $\stackrel{\text { N．}}{ }{ }^{\text {c }}{ }_{6} \mathrm{~W}$ W． |  | － 530 | － $5^{20}$ | N．N．W． | N． 27 W ． |  | ＋ 430 | a <br> $+\quad 310$ |
| N．by W． |  |  | － 515 |  | N．by w． NORTH． | N． 4 W． |  | － 715 | －80 |

[^21]Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

| Hampton Roads, November 1 , 1865. <br> Correction for Object $=+3^{\circ} 57^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | St. Thomas, November 18, 1865. <br> Correction for Object $=+0^{\circ} 16^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{3}{8} \mathrm{E}$. <br> N. by E. $\frac{3}{8} \mathrm{E}$. <br> N. E. by N. $\frac{5}{8} \mathrm{~N}$. <br> N. E. $\frac{3}{4}$ N. <br> N. E. $\frac{3}{8}$ E. <br> N. E. by E. $\frac{3}{8}$ E. <br> E. by N. $\frac{5}{8}$ N. <br> E. $\frac{3}{8}$ N. <br> E. $\frac{3}{8} \mathrm{~S}$. <br> E. S. E. $\frac{3}{4} \mathrm{E}$. <br> S. E. by E . $\frac{5}{8} \mathrm{E}$. <br> S. E. $\frac{5}{8} \mathrm{E}$. <br> S. E. $\frac{1}{4} \mathrm{~S}$. <br> S. S. E. $\frac{3}{4}$ E. <br> S. $\frac{7}{8} \mathrm{E}$. <br> SOUTH. <br> S. $\frac{7}{8} \mathrm{~W}$. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. $\frac{1}{4}$ S. <br> S. W. $\frac{1}{4}$ S. <br> S. W. $\frac{7}{8}$ W. <br> S. W. by W. $\frac{7}{8} \mathrm{~W}$. <br> W. by S. $\frac{1}{8}$ S. <br> WEST. <br> W. by N . <br> N. W. by W. $\frac{7}{8}$ W. <br> N . W. $\frac{3}{4} \mathrm{~W}$. <br> N. N. W. ${ }^{\frac{3}{4}} \mathrm{~W}$. <br> N. by W. $\frac{3}{4} \mathrm{~W}$. <br> N. $\frac{3}{4}$ W. |  | - 1 | $+0^{\circ}$ $10^{\prime}$ <br> 0 20 <br> 0 20 <br> +0 40 <br> +0 10 <br> 0 20 <br> 0 20 <br> 0 20 <br> 0 20 <br> +0 40 <br> +0 10 <br> 0 20 <br> +0 40 <br> +1 10 <br> +2 10 <br> +2 30 <br> +3 30 <br> +4 50 <br> +6 20 <br> +6 40 <br> +6 40 <br> +5 50 <br> +5 20 <br> +5 20 <br> +4 30 <br> +4 0 <br> +3 0 <br> +1 40 <br> 1  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTII. | N. <br> N. $\frac{7}{8}$ E. <br> N. by E. $\frac{7}{8}$ E. <br> N. E. by N. $\frac{1}{8}$ N. <br> N. E. $\frac{1}{8}$ N. <br> N. E. $\frac{7}{8}$ E. <br> N. E. by E. $\frac{7}{8}$ E. <br> E. by N. <br> E. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. $\frac{1}{4}$ E. <br> S. $\frac{1}{4} \mathrm{E}$. <br> S. $\frac{3}{4} \mathrm{~W}$. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. $\frac{1}{4}$ S. <br> S. W. $\frac{3}{8}$ S. <br> S. W. $\frac{3}{4} \mathrm{~W}$. <br> S. W. by W. $\frac{3}{4}$ W. <br> W. S. W. $\frac{7}{8}$ W. <br> W. $\frac{1}{8}$ S. <br> W. $\frac{7}{8}$ N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. |  | - 1 | $\begin{array}{ll} -0^{\circ} & 10 \\ +1 & 10 \\ +1 & 10 \\ +1 & 10 \\ +1 & 10 \\ +1 & 10 \\ +1 & 10 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ \hline 0 & 10 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +3 & 50 \\ +2 & 30 \\ +2 & 30 \\ +1 & 10 \\ +1 & 10 \\ +1 & 10 \\ \hline 0 & 20 \\ \hline 0 & 20 \\ -0 & 20 \\ -0 & 20 \\ \hline 0 & 20 \\ \hline 0 & 20 \\ -0 & 20 \end{array}$ |

A deviation of the North Point of the Compass to the East is designated by the sign + ; A deviation of the North Point of the Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the a deviation to the West by the sign -. From the observations given above, the following values of the coefficients of the
 deviation are obtained:
$\mathrm{A}=+2^{\circ}$
Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

|  | Isle Royal, Salute Islands, November 30, 1865. <br> Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=0^{\circ}$ |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+1^{\circ} .5 I^{\prime}$. Correction for Lubber Line $=0^{\circ}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | $\begin{aligned} & \text { Deviation of } \\ & \text { Compass in } \\ & \text { Points. } \end{aligned}$ | Deviation of Compass in Degrees. | $\begin{gathered} \text { Corrected } \\ \text { Deviation of } \\ \text { Compass. } \end{gathered}$ | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | $\begin{gathered} \text { Corrected } \\ \text { Deviation of } \\ \text { Compass. } \end{gathered}$ |
|  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N . <br> EAST. <br> E. by S. <br> S. E. by E <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. <br> NORTH. | EAST. |  | - , | - , | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. NORTH. |  | $\begin{aligned} & +\frac{1}{9} \\ & + \\ & +\frac{1}{4} \\ & +\frac{1}{4} \\ & +\frac{1}{9} \\ & +\frac{8}{8} \\ & 0 \\ & 0 \\ & 0 \\ & \hline \\ & \hline \frac{1}{8} \end{aligned}$ |  | $\begin{array}{r}+30 \\ +30 \\ +430 \\ +440 \\ +430 \\ +330 \\ \hline 320 \\ \hline\end{array}$ |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -. <br> From the observations given above, the following values of the coefficients of the deviation are obtained: $\mathrm{A}=\quad \mathrm{D}=\quad \mathrm{B}=\quad \mathrm{E}=\quad \mathrm{C}=$ |  |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign +; a deviation to the West by the sign - <br> From the observations given above, the following values of the coefficients of the deviation are obtained: $\mathrm{A}=+2^{\circ} \stackrel{3^{\prime} \cdot 6}{\mathrm{D}}=+\mathrm{I}^{\circ} \stackrel{\mathrm{B}}{2 \mathrm{I}^{\prime} \cdot 4}=+\mathrm{o}^{\circ} \quad \mathrm{o}^{\prime} \cdot \mathrm{I} \quad \mathrm{E}=+\mathrm{o}^{\circ}=\underset{2^{\prime} \cdot 4}{+\mathrm{I}^{\circ}} 4^{\prime} \cdot 7$ |  |  |  |  |

Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865 . <br> Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Rio Janeiro, January 10, 1866. <br> Correction for Object $=+2^{\circ} 44^{\prime}$. Correction for Lubber Line $=0^{\circ}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N . <br> EAST. <br> E. by S. $\frac{1}{8}$ S. <br> S. E. by E. $\frac{7}{8}$ E. <br> S. E. $\frac{7}{8}$ E. <br> S. E. $\frac{1}{8}$ S. <br> S. S. E $\frac{7}{8}$ E. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. $\frac{7}{8}$ W. <br> S. by W. $\frac{7}{8}$ W. <br> S. W. by S. $\frac{1}{8}$ S. <br> S. W. $\frac{1}{8}$ S. <br> S. W. $\frac{7}{8}$ W. <br> S. W. by W. $\frac{7}{8}$ W. <br> W. by S. <br> WEST. <br> W. by N. $\frac{1}{4}$ N. <br> N. W. by ${ }^{4} \mathrm{~W} . \frac{3}{4} \mathrm{~W}$. <br> N. W. $\frac{7}{8}$ W. <br> N. W. $\frac{1}{8} \mathrm{~N}$. <br> N. W. by N. $\frac{1}{8}$ N. <br> N. by W. $\frac{7}{8}$ W. <br> N. $\frac{7}{8} \\|$. |  | - , |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N N. W. <br> N. by W. <br> NORTH. | N. E. by N. $\frac{1}{8}$ N. <br> N. E. $\frac{1}{8}$ N. <br> N. E. $\frac{7}{8} \mathrm{E}$. <br> E. N. E. <br> E. by N . <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. $\frac{1}{8}$ E. <br> E. $\frac{1}{8} \mathrm{E}$. <br> S. $\frac{3}{4} \mathrm{~W}$. <br> S. by W. $\frac{3}{4} \mathrm{~W}$. <br> S. S. W. $\frac{3}{4}$ W. | + <br> + <br> + <br> + <br> + | 。 | $\begin{aligned} & +4^{\circ} 10^{\prime} \\ & +4 \\ & 10 \\ & +4 \\ & +3 \\ & +3 \\ & +2 \\ & +20 \\ & +2 \end{aligned} 40$ |

[^22]Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

| Monte Video, January 24, 1866. <br> Correction for Object $=-0^{\circ} \quad 13^{\prime}$ Correction for Lubber Line $=0$. |  |  |  |  | Sandy Point, February io, 1866. <br> Correction for Object $=+o^{\circ} 7^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N . by E . <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N.W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. $\frac{7}{8}$ E. <br> N. by E. ${ }_{4}^{3}$ E. <br> N. E. by N. $\frac{3}{8}$ N. <br> N. E. $\frac{3}{8}$ N. <br> E. N. E. $\frac{3}{8}$ N.. <br> E. by N. $\frac{3}{8}$ N. <br> E. $\frac{1}{4} \mathrm{~N}$. <br> E. $\stackrel{4}{S}$. E. $\frac{1}{4}$ E. <br> S. E. by E. $\frac{1}{8}$ E. <br> S. E. $\frac{1}{4}$ E. S. E. $\frac{3}{4}$ S. <br> S. S. E. $\frac{1}{4}$ E. <br> S. by E. $\frac{1}{4}$ E. <br> S. $\frac{1}{4}$ E. <br> S. $\frac{1}{2}$ W. <br> S. by W. $\frac{5}{8}$ W. <br> S. W. by $\stackrel{3}{8}$ S. <br> S. W. $\frac{1}{4}$ S. <br> S. W. $\frac{3}{4}$ W. <br> S. W. by W. $\frac{3}{4}$ W. <br> W. by S. $\frac{1}{8} \mathrm{~S}$. <br> W. $\frac{1}{8} \mathrm{~S}$. <br> W. $\frac{7}{8} \cdot \mathrm{~N}$. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. $\frac{7}{8} \mathrm{~W}$. |  <br>  <br> + <br> + <br> + <br> + <br> + | - 1 |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. $\frac{7}{8} \mathrm{E}$. <br> N. by E. $\frac{3}{4} \mathrm{E}$. <br> N. N. E. $\frac{3}{4}$ E. <br> N. E. N. $\frac{1}{4}$ $\frac{3}{4} \mathrm{E}$. <br> N. E. by E. $\frac{5}{8}$ E. <br> E. by N. $\frac{3}{8}$ N. <br> E. $\frac{3}{8} \frac{\mathrm{~N}}{4} \mathrm{~N}$. <br> E. by S. $\frac{3}{4}$ S. <br> S. E. by E. $\frac{1}{4}$ E. <br> S. E. $\frac{1}{4} \mathrm{E}$. <br> S. E. $\frac{7}{8}$ S. <br> S. S. E. $\frac{1}{4}$ E. <br> S. by E. $\frac{4}{8} \mathrm{E}$. <br> S. $\frac{3}{8} \mathrm{E}$. <br> S. $\frac{5}{8} \mathrm{~W}$. <br> S. by W. $\frac{5}{8}$ W. <br> S. W. by S. $\frac{1}{2}$ S. <br> S. W. $\frac{3}{8}$ S. <br> S. W $\frac{5}{8}$ W. <br> S. W. by W. $\frac{3}{4}$ W. <br> W. by S. $\frac{1}{4}$ S. <br> W. $\frac{1}{4} \mathrm{~S}$. <br> W. by N . <br> W. N. W. <br> N. W. $\frac{7}{8}$ W. <br> N W. $\frac{1}{8}$ N. <br> N. W. by N. $\frac{1}{8}$ N. <br> N. N. W. $\frac{1}{8}$ N. <br> N. $\frac{7}{8} \mathrm{~W}$. |  | - | $\begin{array}{lr} +0 & 10^{\prime} \\ +1 & 30 \\ +3 & 0 \\ +3 & 0 \\ +3 & 0 \\ +3 & 0 \\ +4 & 20 \\ +4 & 20 \\ +4 & 20 \\ +3 & 0 \\ +3 & 0 \\ +3 & 0 \\ +3 & 0 \\ +1 & 30 \\ +3 & 0 \\ +4 & 20 \\ +4 & 20 \\ +4 & 20 \\ +4 & 20 \\ +5 & 50 \\ +4 & 20 \\ +4 & 20 \\ +3 & 0 \\ +3 & 0 \\ +3 & 0 \\ +0 & 10 \\ +0 & 10 \\ \hline-1 & 20 \\ \hline 1 & 20 \\ \hline 1 & 20 \\ \hline 1 & 20 \\ \hline 1 & 20 \\ \hline 0 & 10 \end{array}$ |

[^23]Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.


A deviation of the North Point of the Compass to the East is designated by the sign +; $\quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }+ \text {; }\end{aligned}$ From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
 $\mathrm{D}=+\mathrm{r}^{\circ} 29^{\prime} .0 \quad \mathrm{E}=-\mathrm{o}^{\circ} 6^{\prime} .8$
Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

| Panama, May 20, 1866. <br> Correction for Object $=+o^{\circ} \mathbf{1}^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Acapulco, June I, 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Snip's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. N. W. by W. <br> N. W. <br> N. W. by N. <br> $\stackrel{N}{N}$ N. N. W. <br> NORTH. | NORTH. <br> N. $\frac{7}{8}$ E. <br> N. by E. $\frac{3}{4}$ E. <br> N. E. 1 N. $\frac{1}{4}$ N. <br> N. E. $\frac{3}{4}$ E. <br> N. E. by E. $\frac{7}{8}$ E. <br> E. by N. $\frac{1}{4}$ N. <br> E. $\frac{1}{4} \mathrm{~N}$. E. $\frac{7}{8} \mathrm{~S}$. <br> E. by S. $\frac{7}{8}$ S. <br> S. E. by E. $\frac{1}{8}$ E. <br> S. E. $\frac{1}{4}$ E. S. E. $\frac{3}{4}$ S. <br> S. S. $\underset{\text { E. }}{ } \frac{1}{4}$ E. S. by E. $\frac{1}{4}$ E. <br> S. $\frac{1}{4}$ E. <br> S. by W. $\frac{5}{8} \mathrm{~W}$. <br> S. W. by $\stackrel{8}{8} . \frac{3}{8}$ S. <br> S. W. $\frac{3}{8} \mathrm{~S}$. S. W. $\frac{5}{8} \mathrm{~W}$. <br> S.W. by W. $\frac{5}{8}$ W. <br> W. by S. $\frac{3}{8}$ S. $^{8}$ <br> W. $\frac{1}{4} \mathrm{~S}$. <br> W. W. N. N. N. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. | $\begin{aligned} & +\frac{1}{8} \\ & + \\ & +\frac{1}{4} \\ & +\frac{1}{2} \\ & + \\ & +\frac{1}{1} \\ & + \\ & +\frac{1}{8} \\ & + \\ & \hline \end{aligned}$ |  | $\begin{array}{cc}0^{\circ} & 0^{\prime} \\ +1 \\ +1 & 30 \\ +2 & 50 \\ +2 & 50 \\ +2 & 50 \\ +2 & 50 \\ +1 & 30 \\ +2 & 50 \\ +2 & 50 \\ +1 & 30 \\ +1 & 30 \\ +1 & 30 \\ +2 & 50 \\ +2 & 50 \\ +2 & 50 \\ +2 & 50 \\ +2 & 50 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +4 & 10 \\ +2 & 50 \\ +1 & 30 \\ 0 & \\ 0\end{array}$ | NORTH <br> N. by E. <br> N. E. by N <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W <br> NORTH. | NORTH. <br> N. $\frac{7}{8} \mathrm{E}$. <br> N. by E. $\frac{7}{8}$ E. <br> N. E. by N. $\frac{1}{8}$ N. <br> N. E. $\frac{1}{8} \mathrm{~N}$. <br> N. E. by E. $\frac{7}{8}$ E. <br> E. by <br> E. $\frac{1}{8}$ S. <br> S. E. by $\frac{1}{8}$ E. $\frac{7}{8}$ E. <br> S. E. $\frac{7}{8}$ E. <br> S. E. by S. $\frac{1}{8}$ S. <br> S. by E. $\frac{1}{8}$ E. <br> S. $\frac{1}{8} \mathrm{E}$. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. 3 S . $\frac{3}{8} \mathrm{~S}$. <br> S. W. $\frac{8}{8}$ S. <br> S. W. by W. $\frac{5}{8} \mathrm{~W}$. <br> W. $\frac{1}{4} \mathrm{~S}$. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. by W. |  |  |  |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -. <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  | A deviation of the North Point of the Compass to the East is designated by the sign +; a deviation to the West by the sign - <br> From the observations given above, the following values of the coefficients of the deviation are obtained: |  |  |  |  |

Observations for Determining the Deviations of the Forward Alidade Compass on the U. S. Iron Clad Monadnock.

| Magdalena Bay, June 9, 1866. <br> Correction for Object $=-0^{\circ} 4 \mathrm{I}^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | San Francisco, June 23, 1866. <br> Correction for Object $=-0^{\circ} 45^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by WV. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. $\frac{7}{8}$ E. <br> S. W. $\frac{1}{2}$ S. <br> S. W. $\frac{\frac{3}{8}}{8}$ W. <br> S. W. by W. $\frac{5}{8}$ W. <br> W. by S. $\frac{1}{4}$ S. <br> W. $\frac{1}{4} \mathrm{~S}$. <br> W. $\frac{5}{8} \mathrm{~N}$. <br> W. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{4}$ W. <br> N. W. $\frac{1}{8}$ W. <br> N. W. $\frac{7}{8}$ N. <br> N. N. W. <br> N. by W. |  |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTII. | N. $\frac{1}{8}$ E. <br> N. by E. $\frac{1}{8} \mathrm{E}$. <br> N. N. E. $\frac{1}{8}$ E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. $\frac{7}{8}$ N. <br> E. $\frac{1}{8} \mathrm{~S}$. <br> E. by S. $\frac{1}{8}$ S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. $\frac{7}{8}$ S. <br> S. S. E. S. by E. $\frac{1}{4}$ $\frac{3}{8}$ E. <br> S. $\frac{3}{8} \mathrm{E}$. <br> S. $\frac{5}{8}$ W. <br> S. by W. $\frac{1}{2}$ W. <br> S. W. by S. $\frac{1}{2}$ S. <br> S. W. $\frac{1}{2}$ S. <br> S. W. $\frac{1}{2}$ W. <br> S. W. by W. $\frac{5}{8}$ W. <br> W. by S. $\frac{1}{4}$ S. <br> W. $\frac{1}{4} \mathrm{~S}$. <br> W. ${ }^{\frac{3}{4}} \mathrm{~N}$. <br> W. N. W. <br> N. W. by W. $\frac{1}{4}$ W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. $\frac{7}{8} \mathrm{~W}$. |  | - |  |

[^24]Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock.

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[^25]Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 1865. Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+\mathrm{I}^{\circ} 5^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH <br> N . by E . <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | EAST. | 0 | - |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. $\frac{1}{8}$ N. <br> N. E. by E. <br> E. N. E. <br> E. $\frac{7}{8} \mathrm{~N}$. <br> E. $\frac{1}{4} \mathrm{~S}$. <br> E. by S. $\frac{3}{8}$ S. <br> S. E. by E. $\frac{5}{8}$ E. | $\begin{gathered} o \\ o \\ +\quad \\ +\quad \frac{1}{8} \\ o \\ \circ \\ \hline \\ \hline \\ \hline \end{gathered}$ | - | $\begin{array}{lc} +1 & 50 \\ +1 & 50 \\ +1 & 50 \\ +3 & 0 \\ +2 & 10 \\ +1 & 50 \\ +0 & 40 \\ -0 & 40 \\ -2 & 10 \\ -2 & 20 \end{array}$ |

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Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865. <br> Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Rio Janeiro, January 10, 1855. <br> Correction for Object $=+2^{\circ} 44^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. F. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S, <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> E. $\frac{1}{8} \mathrm{~S}$. <br> E. by S. $\frac{1}{8}$ S. <br> S. E. by E. $\frac{3}{4}$ E. <br> S. E. $\frac{3}{4}$ E. <br> S. E. $\frac{1}{4}$ S. <br> S. E. by S. $\frac{1}{4}$ S. <br> S. by E. $\frac{3}{4}$ E. <br> S. $\frac{7}{8} \mathrm{E}$. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. $\frac{7}{8}$ S. <br> W. $\frac{8}{4} \mathrm{~N}$. <br> W. by N. $\frac{1}{8} \mathrm{~N}$. <br> N. W. $\frac{1}{2}$ W. <br> N W. $\frac{1}{2} \mathrm{~N}$. <br> N. W. by N. $\frac{1}{2} \mathrm{~N}$. <br> N. N. W. $\frac{1}{2}$ N. <br> N. $\frac{3}{4} \mathrm{~W}$. |  | - 1 | $\begin{array}{lr} +1^{\circ} & 50^{\prime} \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +1 & 30 \\ +1 & 10 \\ 0 & 0 \\ -0 & 20 \\ -0 & 20 \\ -0 & 20 \\ \hline 0 & 20 \\ +0 & 50 \\ +2 & 10 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +2 & 30 \\ +1 & 30 \\ 0 & 0 \\ +0 & 50 \\ +2 & 10 \\ \hline 1 & 50 \\ \hline 3 & 10 \\ \hline 3 & 10 \\ \hline & 10 \\ \hline 1 & 0 \\ \hline 1 & 0 \end{array}$ | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N.W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. E. by N. N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. $\frac{1}{8}$ S. <br> E. S. E. <br> S. E. $\frac{7}{8}$ E. <br> S. E. $\frac{1}{4}$ S. <br> S. E. by S. $\frac{1}{8}$ S. <br> S. by E. $\frac{7}{8}$ E. <br> SOUTH. <br> S. by W. $\frac{1}{8} \mathrm{~W}$. S. S. W. $\frac{1}{8} \mathrm{~W}$. <br> S. W. $\frac{7}{8}$ S. |  | - 1 | $\begin{array}{lc} +2^{\circ} & 40^{\prime} \\ +2 & 40 \\ +2 & 40 \\ +2 & 40 \\ +2 & 40 \\ +2 & 40 \\ +1 & 40 \\ +2 & 20 \\ +1 & 40 \\ +0 & 20 \\ +1 & 0 \\ +1 & 20 \\ +1 & 20 \\ +2 & 20 \\ +1 & 40 \\ +1 & 20 \\ +1 & 20 \end{array}$ |

[^27]Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock.

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[^28]Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock.

| Valparaiso, April 4, 1866 . <br> Correction for Object $=+0^{\circ} \quad \mathbf{I}^{\prime} . \quad$ Correction for Lubber Line $=0$. |  |  |  |  | Callao, April 29, 1866. <br> Correction for Object $=+0^{\circ} 6^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by. W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8} \mathrm{E}$. <br> N. by E. <br> N. N. E. <br> N. E. by N. $\frac{1}{8}$ N. <br> N. E. $\frac{1}{4} \mathrm{~N}$. <br> N. E. by E. $\frac{3}{4}$ E. <br> E. by N. $\frac{1}{8}$ N. <br> E. $\frac{1}{\frac{1}{8}} \mathrm{~N}$. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> S. $\frac{1}{8} \mathrm{E}$. <br> S. $\stackrel{7}{8} \mathrm{~W}$. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. $\frac{1}{4} \mathrm{~N}$. <br> W. by N. $\frac{1}{4} \mathrm{~N}$. <br> W. N. W. $\frac{1}{4}$ N. <br> N. W. $\frac{3}{4} \mathrm{~W}$. <br> N. W. $\frac{3}{8}$ N. <br> N. W. by N. ${ }^{\frac{1}{4}} \mathrm{~N}$. <br> N. by W. $\frac{3}{4}$ W. <br> N. $\frac{3}{4} \mathrm{~W}$. |  | - 1 | 10  <br> $-1^{\circ}$ 20 <br> 0 0 <br> 0 0 <br> +1 30 <br> +2 50 <br> +2 50 <br> +2 50 <br> +1 30 <br> +1 30 <br> +1 30 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> +1 0 <br> +1 30 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> 0 0 <br> -2 50 <br> 2 50 <br> 2 50 <br> 2 50 <br> 4 10 <br> 2 50 <br> 2 50 <br> 2 50 <br> 1  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{4} \mathrm{E}$. <br> N. by E. $\frac{1}{8}$ E. <br> N. N. E. $\frac{1}{8}$ E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. $\frac{7}{8}$ E. <br> S. E. $\frac{7}{8}$ E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> S. $\frac{1}{\frac{1}{3}} \mathrm{E}$ W <br> S. $\frac{7}{8}$ W. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. $\frac{1}{4}$ S. <br> S. W. $\frac{1}{8}$ S. <br> S. W. by W. <br> W. S. W. <br> W. $\frac{7}{8} \mathrm{~S}$. <br> W. $\frac{1}{4} \mathrm{~N}$. <br> W. by N. $\frac{3}{8} \mathrm{~N}$. <br> N. W. by W. $\frac{5}{8} \mathrm{~W}$. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2} \mathrm{~N}$. <br> N. N. W. $\frac{1}{2} \mathrm{~W}$. <br> N. by W. $\frac{1}{2}$ W. <br> N. $\frac{3}{4} \mathrm{~W}$. |  | - 1 |  |

$\begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }+ \text {; }\end{aligned} \begin{array}{r}\text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{array}+$; From the observations given above, the following values of the coefficients of the
deviation are obtained: $\begin{aligned} & \text { aram the observations given above, the following values of the coefficients of the } \\ & \text { deviation are obtained: }\end{aligned}$

Observations for Determining the Deviations of the Forward Binnacle Compass on the U. S. Iron Clad Monadnock

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[^29]Obeervations for Deiécining the Deviations of the Forward Binnacle Compass on the U．S．Iron Clad Monadnock．

\begin{tabular}{|c|c|c|c|c|c|c|c|c|c|}
\hline \multicolumn{5}{|l|}{\begin{tabular}{l}
Magdalena Bay，June 9， 1866. \\
Correction for Object \(=-0^{\circ} 41^{\prime}\) ．Correction for Lubber Line \(=0\) ．
\end{tabular}} \& \multicolumn{5}{|l|}{\begin{tabular}{l}
San Francisco，June 23， 1866. \\
Correction for Object \(=-0^{\circ} 45^{\prime}\) ．Correction for Lubber Line \(=0\) ．
\end{tabular}} \\
\hline Assumed Magnetic Direction of Ship＇s Head． \& Ship＇s Head by
Compass． \& Deviation of Compass in Points． \& Deviation of Compass in Degrees． \& Corrected Deviation of Compass． \& Assumed Magnetic Direction of Ship＇s Head． \& Ship＇s Head by
Compass． \& Deviation of Compass in Points． \& Deviation of Compass in Degrees． \& Corrected Deviation of Compass． \\
\hline \begin{tabular}{l}
NORTH． \\
N．by E． \\
N．N．E． \\
N．E．by N． \\
N．E． \\
N．E．by E． \\
E．N．E． \\
E．by N． \\
E．by S． \\
E．S．E． \\
S．E．by E． \\
S．E． \\
S．E．by S． \\
S．S．E． \\
S．by E． \\
SOUTH． \\
S．by W． \\
S．S．W． \\
S．W． \\
S．W．by W． \\
W．S．W． \\
W．by S． \\
WEST． \\
W．by N． \\
N．W．by W． \\
N．W． \\
N．W．by N． \\
N．N．W． \\
N．by W． \\
NORTH．
\end{tabular} \& \begin{tabular}{l}
N．\(\frac{1}{2}\) E． \\
N．by E．\(\frac{3}{8}\) E． \\
S．W．\(\frac{1}{2}\) S． \\
S．W．\(\frac{1}{2} \mathrm{~W}\) ． \\
S．W．by W．\(\frac{5}{8}\) W． \\
W．by S．\(\frac{3}{8}\) S． \\
W．\(\frac{1}{4}\) S． \\
W．by N． \\
N．W．by W．\(\frac{7}{8}\) W． \\
N．W．\(\frac{3}{4}\) W． \\
N．W．\(\frac{3}{8}\) N． \\
N．by W．\(\frac{1}{2}\) W． \\
N．W．by N．\(\frac{1}{2}\) N． \\
N．\(\frac{1}{2}\) W．
\end{tabular} \& 二 \({ }^{\frac{1}{3}}{ }^{\frac{1}{8}}\)

a \& －， \& $\begin{array}{cc}\text {－} 6^{\circ} 110 \\ -4 & 50 \\ & \\ \\ & \\ \\ \end{array}$ \& \begin{tabular}{l}
NORTH． <br>
N．by E． <br>
N．N．E． <br>
N．E．by N． <br>
N．E． <br>
N．E．by E． <br>
E．N．E． <br>
E．by N． <br>
EAST． <br>
E．by S． <br>
E．S．E． <br>
S．E． <br>
S．E．by S． <br>
S．S．E． <br>
S．by E． <br>
SOUTH． <br>
S．by W． <br>
S．S．W． <br>
S．W．by S． <br>
S．W． <br>
S．W．by W． <br>
W．S．W． <br>
W．by S． <br>
W．by N <br>
W．N．W． <br>
N．W．by W． <br>
N．W． <br>
N．W．by N． <br>
N．N．W． <br>
N．by W．
NORTH．

 \& 

N．$\frac{1}{2} \mathrm{E}$ ． <br>
N．by E．$\frac{1}{2}$ E． <br>
N．E．by N．$\frac{1}{2}$ N． <br>
N．E．$\frac{3}{8} \frac{1}{8} \mathrm{~N}$ ． <br>
N．E．by E．$\frac{1}{2}$ E．
E．by N．$\frac{3}{\mathrm{~N}} \mathrm{~N}$. <br>
E．${ }^{2} \mathrm{~N}$ N． <br>
E．by S．$\frac{3}{4}$ S． <br>
S．E．by．E．$\frac{3}{8}$ E． <br>
S．E．$\frac{1}{2} \mathrm{E}$ E． <br>
S．E．by S．$\frac{1}{4}$ S． <br>
S．by E．$\frac{3}{4}$ E． <br>
S． 1 E． <br>
S．${ }^{3}$ 3．W． W ． <br>
S．by W．豪W．
S．W． <br>
S．W． 1 S．S．$\frac{1}{2}$ S． <br>
S．W．$\frac{1}{2}$ 立． <br>
S．W．by $\mathrm{W} . \frac{5}{5} \mathrm{~W}$ ．
W. by S．$\frac{1}{4} \mathrm{~S}$ ． <br>
W．by S．$\frac{1}{8}$ s． <br>
W．by N ． <br>
N．W．by W．$\frac{7}{8}$ W． <br>
N．W．
N．
N．W．
$\frac{1}{4}$ N． <br>
N．W．by N．${ }^{\frac{3}{3}} \mathrm{~N}$ ．
N．by W．$\frac{1}{2}$ W． <br>
N．by W．
\end{tabular} \&  \& \&  <br>

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\end{tabular}

[^30]Observations for Detiermining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Hampton Roads, November r, 1865. Correction for Object $=+3^{\circ} 57^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | St. Thomas, November 18, 1865. <br> Correction for Object $=+0^{\circ} 16^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{4} \mathrm{E}$. <br> N. by E. $\frac{1}{8}$ E. <br> N. N. E. <br> N. E. by N. <br> N. E. $\frac{1}{8} \mathrm{~N}$. <br> N. E. $\frac{7}{8}$ E. <br> N. E. by E. $\frac{3}{4}$ E. <br> E. by N. $\frac{1}{8}$ N. <br> E. $\frac{1}{8}$ N. <br> E. by S. <br> E. by S. $\frac{7}{8}$ S. <br> S. E. by E. $\frac{1}{8}$ E. <br> S. E. $\frac{1}{8}$ E. <br> S. S. E. $\frac{1}{4}$ E <br> S. by E. $\frac{4}{8} \mathrm{E}$. <br> S. $\frac{1}{2}$ E. <br> S. $\frac{1}{2}$ W. <br> S. by W. $\frac{5}{8} \mathrm{~W}$. <br> S. W. by S. $\frac{1}{2}$ S. <br> S. W. $\frac{3}{8}$ S. <br> S. W. $\frac{3}{4} \mathrm{~W}$. <br> W. S. W. <br> W. by S. <br> W. $\frac{1}{8} \mathrm{~N}$. <br> W. by N. $\frac{3}{8} \mathrm{~N}$. <br> N. W. by W. $\frac{3}{4}$ W. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{2}$ N. <br> N. W. by N. $\frac{1}{2}$ N. <br> N. by W. $\frac{5}{8}$ W. <br> N. $\frac{3}{4} \mathrm{~W}$. |  | - 1 |   <br> $+11^{\circ}$ 10 <br> +2 0 <br> +3 30 <br> +4 0 <br> +4 50 <br> +5 20 <br> +6 20 <br> +5 50 <br> +5 20 <br> +4 30 <br> +4 50 <br> +5 20 <br> +5 20 <br> +6 10 <br> +6 40 <br> +7 40 <br> +9 0 <br> +9 30 <br> +8 40 <br> +9 0 <br> +8 40 <br> +7 10 <br> +5 0 <br> +4 0 <br> +3 0 <br> +0 40 <br> +0 40 <br> 0 40 <br> 1 40 <br> 1 40 <br> 0 50 <br> 0 40 <br> +1 10 | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S . <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8} \mathrm{~W}$. <br> N. by E. <br> N. by E. $\frac{3}{4} \mathrm{E}$. <br> N. E. by ${ }^{4} \mathrm{~N} . \frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2}$ E. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{4}$ N. <br> E. $\frac{1}{4}$ N. <br> E. $\frac{3}{4}$ S. <br> E. S. E. <br> S. E. by E. $\frac{1}{4}$ E. <br> S. E. $\frac{1}{4}$ E. <br> S. E. $\frac{3}{4}$ S. <br> S. S. $\stackrel{4}{2}$. <br> S. by E. <br> S. <br> S. $\frac{7}{8}$ W. <br> S. by W. $\frac{3}{4}$ W. <br> S. W. by S. $\frac{1}{2}$ S. <br> S. W. $\frac{1}{2}$ S. <br> S. W. $\frac{1}{2}$ W. <br> S. W. by W. $\frac{3}{4}$ W. <br> W. $\frac{7}{8}$ S. <br> W. $\frac{1}{8} \mathrm{~N}$. <br> W. by N. <br> N. W. by W. $\frac{3}{4}$ W. <br> N. W. $\frac{1}{2}$ W. <br> N. W. $\frac{1}{4}$ N. <br> N. W. by N. $\frac{1}{2}$ N. <br> N. by W. $\frac{3}{4}$ W. <br> N. $\frac{3}{4}$ W. |  | - | $+1^{\circ}$ 10 <br> +0 10 <br> +2 40 <br> +5 20 <br> +5 20 <br> +5 20 <br> +5 20 <br> +2 30 <br> +2 30 <br> +2 30 <br> +0 10 <br> +2 30 <br> +2 30 <br> +2 30 <br> -0 10 <br> -0 20 <br> -0 20 <br> +1 10 <br> +2 40 <br> +5 20 <br> +5 20 <br> +5 20 <br> +2 40 <br> -1 40 <br> -1 40 <br> -0 20 <br> -3 0 <br> 5 50 <br> -3 10 <br> 5 50 <br> 3 0 <br> 3 0 <br> 1 10 |

[^31][^32]Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Isle Royal, Salute Islands, November 30, 1865. Correction for Object $=-0^{\circ} 2^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Ceara, December 19, 1865. <br> Correction for Object $=+\mathrm{r}^{\circ} 5_{5} \mathrm{I}^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Compass. <br> Ship's Head by | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. WEST. <br> W. by N. <br> w. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. <br> NORTH. | E. $\frac{1}{2} \mathrm{~N}$. | + $\frac{1}{2}$ | $\cdots$ | $+540$ | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $\frac{1}{2} \mathrm{E}$. <br> N. by E. $3^{-}$E. <br> N. E. by N. $\frac{3}{4}$ N. <br> N. E. ${ }^{\frac{1}{2}}$ N. <br> N. E. by E. $\frac{3}{3} \mathrm{E}$. <br> E. by $\mathrm{N} \frac{1}{2} \mathrm{~N}$. <br> EAST <br> E. by S. $\frac{1}{8}$ S. <br> S. E. by E . $\frac{7}{8} \mathrm{E}$. |  | - / | $\begin{array}{rrr} \circ & \prime \\ +7 & 10 \\ +8 & 40 \\ +10 & 0 \\ +8 & 0 \\ + & 6 & 20 \\ + & 5 & 0 \\ + & 0 \\ + & 0 \\ + & 50 \\ + & 40 \\ + & 30 \end{array}$ |

[^33]Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Bahia, December 30, 1865. <br> Correction for Object $=+2^{\circ} 30^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Rio Janeiro, January 10, 1855. <br> Correction for Object $=+2^{\circ} 44^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Compass. <br> Corrected Deviation of Compass. |
| NORTH <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. F. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | N. $1 \frac{1}{4} \mathrm{E}$. <br> N. N. E. <br> N. by E. $\frac{1}{4} \mathrm{E}$. <br> N. E. by N. $\frac{1}{8} \mathrm{~N}$. <br> N. E. N. E. $\frac{1}{2}$ N. E. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{2}$ N. <br> E. $\frac{1}{8} \mathrm{~N}$. <br> E. by S. $\frac{7}{8}$ S. <br> S. E. by ${ }_{\text {B }}^{\text {E. }}$. <br> S. E. <br> S. E. by S. <br> S. by E. $\frac{1}{8}$ E. <br> S. ${ }^{\frac{1}{8}} \mathrm{E}$. E . <br> S. by W. $\frac{7}{8}$ W. <br> S. W. by S. $\frac{1}{8}$ S. <br> S. W. $\frac{1}{8}$ S. <br> W. by S. $\frac{7}{8}$ S. <br> W. ${ }^{\frac{3}{2}} \mathrm{~S}$ S. <br> W. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. W. by W. $\frac{1}{2} \mathrm{~W}$. <br> N. W. ${ }_{\text {N }}^{\frac{3}{4}} \mathrm{~W}$ W. <br> N. W. by N. $\frac{1}{2}$ N. <br> N. by W. $\mathrm{N} . \frac{3}{4} \mathrm{~W}$. |  |  | - $0^{\circ} 201$ <br> 00 <br> +1 <br> 1 50 | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. N. W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. |  |  |  |  |
| A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign - . <br> From the observations given above, the following values of the coefficients of the deviation are obtained: $\begin{gathered} \mathrm{A}=+2^{\circ} 6^{6^{\prime} \cdot 2} \underset{\mathrm{D}=+2^{\circ}}{\stackrel{\mathrm{B}}{35^{\prime} \cdot 7}+3^{\circ}} \stackrel{29^{\prime} \cdot \mathrm{I}}{\mathrm{E}=0^{\circ}} \stackrel{\mathrm{C}=\mathrm{o}^{\prime} \cdot 5}{\mathrm{C}}=\mathrm{I}^{\circ} 33^{\prime} \cdot 9 \end{gathered}$ |  |  |  |  | a deviation to the West by the sign - <br> A deviation of the North Point of the Compass to the East is designated by the sign +; deviations are obtained: <br> From the observations given above, the following values of the coefficients of the $\mathrm{A}=+3^{\circ} \stackrel{14^{\prime} .0}{\mathrm{D}}=+2^{\circ} \mathrm{B}=+4^{\circ} \stackrel{23^{\prime} \cdot 5}{\mathrm{IO}^{\prime} \cdot 5}=-0^{\circ} \stackrel{\mathrm{C}=-1^{\circ}{ }^{\circ} \cdot 10^{\prime} \cdot 4}{ }$ |  |  |  |  |

Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Monte Video, January 24, 1866. <br> Correction for Object $=-0^{\circ} \quad 13^{\prime}$ Correction for Lubber Line $=0$. |  |  |  |  | Sandy Point, February iо, 1866. <br> Correction for Object $=+0^{\circ} 7^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's. Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{4} \mathrm{~W}$. <br> N. $\frac{1}{2}$ E. <br> N. by E. ${ }_{4}^{3} \mathrm{E}$. <br> N. E. by N. $\frac{3}{4} \mathrm{~N}$. <br> N. E. $\frac{3}{4} \mathrm{~N}$. <br> N. E. $\frac{1}{4} \mathrm{E}$. <br> N. E. by E. $\frac{1}{4}$ E. <br> E. by N. $\frac{7}{8}$ N. <br> E. $\frac{3}{4} \mathrm{~N}$. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> E. by S. $\frac{1}{2}$ S. <br> S. E. by E. $\frac{3}{8}$ E. <br> S. E. $\frac{3}{8}$ E. <br> S. E. $\frac{5}{8}$ S. <br> S. S. E. $\frac{3}{8}$ E. <br> S. by E. $\frac{3}{8} \mathrm{E}$. <br> S. $\frac{1}{4} \mathrm{E}$. <br> S. $\frac{3}{4}$ W. <br> S. by W. $\frac{3}{4} \mathrm{~W}$. <br> S. S. W. $\frac{3}{4}$ W. <br> S. W. $\frac{1}{4}$ S. S. W. $\frac{3}{3} \mathrm{~W}$. <br> S. W. by W. $\frac{3}{4}$ W. <br> W. by S. $\frac{1}{8}$ S. <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. $\frac{3}{4} \mathrm{~W}$. <br> N. W. $\frac{1}{8}$ N. <br> N. W. by N. <br> N. N. W. <br> N. be W. | + <br> + <br> + <br> + <br> + | - 1 |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> WEST. <br> W. by N. <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | N. $\frac{1}{8} \mathrm{E}$. <br> N. by E. <br> N. by E. $\frac{7}{8}$ E. <br> N. E. $\frac{1}{2}$ N. <br> N. E. $\frac{1}{2} \mathrm{E}$. <br> N. E. by E. $\frac{1}{2}$ E. <br> E. by N. $\frac{1}{2}$ N. <br> E. $\frac{1}{2} \mathrm{~N}$. <br> E. $\frac{1}{2} \mathrm{~S}$. <br> E. by S. ${ }_{8} \mathrm{~S}$. <br> S. E. by E. $\frac{3}{8}$ E. <br> S. E. $\frac{1}{4} \mathrm{E}$. <br> S. E. $\frac{5}{8} \mathrm{~S}$. <br> S. E. by S. $\frac{1}{2}$ S. <br> S. by E. $\frac{3}{8}$ E. <br> S. $\frac{3}{5} \mathrm{E}$. <br> S. by W. $\frac{3}{4} \mathrm{~W}$. <br> S. W. by S. $\frac{3}{8}$ S. <br> S. W. $\frac{1}{4}$ S. <br> S. W. $\frac{7}{8}$ W. <br> W. S. W. $\frac{1}{8}$ S. <br> W. by S . <br> W. $\frac{1}{8} \mathrm{~N}$. <br> W. by N. $\frac{1}{4}$ N. <br> N. W. by ${ }^{4} \mathrm{~W} . \frac{1}{2} \mathrm{~W}$. <br> N. W. $\frac{1}{2} \mathrm{~W}$. <br> N. W. $\frac{1}{2}$ N. <br> N. W. by $N . \frac{3}{8} \mathrm{~N}$. <br> N. by W. $\frac{3}{4}$ W. <br> N. $\frac{3}{4} \mathrm{~W}$. |  | $\bigcirc 1$ | $\begin{array}{lc} -\mathrm{I}^{\circ} & 20^{\prime} \\ +0 & 10 \\ +\mathrm{I} & 30 \\ +3 & 0 \\ +5 & 50 \\ +5 & 50 \\ +5 & 50 \\ +5 & 50 \\ +5 & 50 \\ +5 & 50 \\ +4 & 20 \\ +4 & 20 \\ +3 & 0 \\ +4 & 20 \\ +5 & 50 \\ +4 & 20 \\ +4 & 20 \\ +4 & 20 \\ +3 & 0 \\ +4 & 20 \\ +3 & 0 \\ +1 & 30 \\ +1 & 30 \\ +0 & 10 \\ \hline 1 & 20 \\ \hline 2 & 40 \\ \hline-5 & 30 \\ \hline-5 & 30 \\ \hline-4 & 30 \\ \hline-2 & 10 \\ \hline 2 & 40 \\ \hline 1 & 40 \\ \hline \end{array}$ |

[^34]November, 1872.
Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Valparaiso, April 4, 1866. <br> Correction for Object $=+o^{\circ} 1^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Callao, April 29, 1866. <br> Correction for Object $=+o^{\circ} \quad 6^{\prime}$. Correction for Lubber Line $=0$ |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees | Corrected Compass Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. by S . <br> WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. N. by W. <br> NORTH. | N. ${ }^{\frac{1}{3}} \mathrm{~W}$ W. <br> N. by E. $\frac{5}{8} \mathrm{E}$. <br> N. N. E. $\frac{1}{2}$ E. <br> N. E. $\frac{1}{2}{ }^{2} \mathrm{~N}$. <br> E. N. ${ }^{\text {B }}$ E. $\frac{5}{8} N$ <br> E. by N. $\frac{8}{4} \mathrm{~N}$. <br> E. $\frac{1}{2} \mathrm{~N}$. <br> E. by S. $\frac{5}{\text { B }}$ S. <br> S. E. by E. $\frac{1}{2}$ E. <br> S. E. $\frac{1}{4} \mathrm{E}$. <br> S. $\mathrm{E} . \frac{.0}{4} \mathrm{~S}$. <br> S. S. E. $\frac{3}{3} \mathrm{E}$. <br> S. $\frac{1}{2} \mathrm{E}$. <br> S. by w. $\frac{1}{2} \mathrm{~W}$. <br> S. W. by $\frac{1}{5}$. $\frac{5}{8} \mathrm{~S}$. <br> S. W. $\frac{1}{2}$ S. S. W. W. <br> W. S. W. $\frac{3}{8}$ S. <br> W. by S. $\frac{2_{4}^{8}}{4}$ S. <br> W. $\frac{1}{8} \frac{1}{8} \mathrm{~S}$. <br> w. 옹. W. <br> N. W. $\frac{7}{8}$ W. <br> N. w. <br> N. W. by N. <br> N. N. W. <br> N. by W. $\frac{1}{8} \mathrm{~W}$. | $+\frac{1}{1}$ <br> + <br> + <br> + |  |  | NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. <br> NORTH. | NORTH. <br> N. $\stackrel{7}{8} \mathrm{E}$ E. ${ }^{3}$. <br> N. B. by N. $\frac{3}{8}$ N. <br> N. E. $\frac{1}{2} \mathrm{~N}$. <br> E. N. E. $\frac{1}{2}$ N. <br> E. ${ }^{\frac{3}{8}} \mathrm{~N}$ N. <br> E. by S. $\frac{3}{4} \mathrm{~S}$. <br> S. E. by $\frac{9}{}$. $\frac{1}{4}$ E. <br> S. E. $\frac{1}{4} \mathrm{E}$. <br> S. S. $\mathrm{E}^{4} \frac{1}{4} \mathrm{E}$. <br> S. by E. $\frac{\frac{1}{8}}{} \mathrm{E}$. <br> S. $\frac{1}{2} \mathrm{E}$. <br> S. by W. $\frac{5}{8} \mathrm{~W}$. <br> S. W. by S. $\frac{1}{2}$ S. <br> S. W. S. W. $\frac{3}{8}$ S. W. <br> W. S. W. $\frac{1}{4} \mathrm{~S}$. <br> W. by S. $\frac{1}{8}$ S. <br> WEST. <br> W. by N. $\frac{1}{8} \mathrm{~N}$. <br> W. N. W. $\frac{1}{4}$ N. <br> N. W. $\frac{3}{4}$ N. <br> N. W. by N. $\frac{1}{8}$ N. <br> N. by W. <br> N. by W. $\frac{7}{8} W^{8}$. |  | - , |  |

[^35]Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.

| Panama, May 20, 1866. <br> Correction for Object $=+0^{\circ} 1^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  | Acapulco, June I, 1866. <br> Correction for Object $=+0^{\circ} \quad 6^{\prime}$. Correction for Lubber Line $=0$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points | Deviation of Compass in Degrees | Corrected Deviation of Compass. | Assumed Magnetic Direction of Ship's Head. | Ship's Head by Compass. | Deviation of Compass in Points. | Deviation of Compass in Degrees. | Corrected Deviation of Compass. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N. W. <br> N. W. by N. <br> N. N. W. <br> NORTH. | NORTH. <br> N. by E. <br> N. by E. $\frac{7}{8} \mathrm{E}$. <br> N. E. by N. $\frac{1}{8}$ N. <br> N. E. $\frac{1}{4}$ N. <br> N. E. by E. $\frac{3}{4} \mathrm{E}$. <br> E. by N. E. $\frac{1}{8}$ N. <br> E. by S. <br> E. by S. $\frac{7}{8}$ S. <br> S. E. by E. $\frac{1}{8}$ E. <br> S. E. $\frac{3}{4}$ S. <br> S. S. ${ }^{4}$ E. $\frac{1}{4} \mathrm{E}$. S. by E. $\frac{1}{4} \mathrm{E}$. <br> S. $\frac{1}{8} \mathrm{E}$. <br> S. by W. $\frac{3}{4} \mathrm{~W}$. <br> S. W. by $\stackrel{4}{4} . \frac{3}{8}$ S. <br> S. W. $\frac{1}{2}$ S. S. W. $\frac{1}{2}$ W. <br> S. W. by W. $\frac{5}{8}$ W. <br> W. by S. $\frac{3}{8}$ S. <br> W. $\frac{1}{8} \mathrm{~S}$. W. by N . <br> N. W. by W. $\frac{7}{8}$ W. <br> N. W. $\frac{3}{4} \mathrm{~W}$. N. W. $\frac{1}{4}$ N. <br> N. W. by $N . \frac{1}{8}$ N. N. by W. $\frac{7}{8}$ W. <br> N. $\frac{7}{8}$ W. |  <br> 0 <br> 0 <br> + <br> + <br> + <br> + | - , |  | NORTH. <br> N. by E. <br> N. N. E. N. E. by <br> N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. <br> EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. <br> S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. <br> SOUTH. <br> S. by W. <br> S. W. W. by S. <br> S. W. <br> S. W. by W. <br> W. S. W. <br> W. by S. <br> W. by N . <br> W. N. W. <br> N. W. by W. <br> N . W. <br> N. W. by N. <br> $\stackrel{N}{N}$ N. W. <br> NORTH. | NORTH. <br> N. $\frac{7}{8} \mathrm{E}$. <br> N. by E. $\frac{7}{8}$ E. <br> N. E. by N. $\frac{1}{4}$ N. <br> N. E. $\frac{1}{4}$ N. N. $\frac{5}{8} \mathrm{E}$. <br> E. N. E. $\frac{1}{4}$ N. <br> E. by N. $\frac{\frac{1}{4}}{4} \mathrm{~N}$. <br> E. $\frac{1}{8} \mathrm{~N}$. <br> E. $\frac{7}{8} \mathrm{~S}$. <br> S. E. by E. $\frac{1}{8}$ E. <br> S. E. $\frac{1}{8} \mathrm{E}$. <br> S. S. E. $\frac{1}{4}$ E. <br> S. by E. $\frac{1}{4} \mathrm{E}$ E. <br> S. $\frac{3}{8}$ E. <br> S. by W. $\frac{1}{2}$ W. <br> S. W. by $\stackrel{1}{2} \stackrel{1}{2}$ S. <br> S. W. $\frac{1}{2}$ S. <br> W. S. ${ }^{8}$ W. $\frac{1}{4}$ S. <br> W. by $S . \frac{1}{8} \mathrm{~S}$. <br> W. $\frac{1}{8}$ S. <br> W. N. W. $\frac{1}{8}$ N. <br> N. W. $\frac{3}{4} \mathrm{~W}$. <br> N. W. by N. $\frac{1}{8}$ N. <br> N. $\frac{7}{8}$ W. |  | $\bigcirc$ |  |

A deviation of the North Point of the Compass to the East is designated by the sign +;
a deviation to the West by the sign - $\quad \begin{gathered}\text { A deviation of the North Point of the Compass to the East is designated by the sign } \\ \text { a deviation to the West by the sign - }\end{gathered}$ From the observations given above, the following values of the coefficients of the $\begin{gathered}\text { From the observations given above, the following values of the coefficients of the } \\ \text { deviation are }\end{gathered}$
 $\begin{array}{lll}34^{\prime} .0 \\ \mathrm{D}=+2^{\circ} & \mathrm{B}=+0^{\circ} & \mathrm{IO}^{\prime} .8\end{array} \quad \begin{aligned} & \mathrm{I} 2^{\prime} .2 \\ & \mathrm{E}=-0^{\circ} \\ & \mathrm{C}=-4^{\prime} .0\end{aligned} \mathrm{I}^{\circ} 53^{\prime} .8$ deviation are obtaned:
Observations for Determining the Deviations of the Forward Ritchie Compass on the U. S. Iron Clad Monadnock.


[^36]The observations made at stations where the deviations had been determined on all of the thirty-two points were first discussed. For that purpose the values of the coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, for each compass, at each station, were computed from the deviations on the true magnetic points by means of the equations given on pages 126 to 128. A specimen of the form employed in making these computations is appended. It sufficiently explains itself.

Admiralty Standard Compass. Computation of Coefficients $B_{1}$ and $C_{1}$, from Deviations observed on 32 Points, on the U. S. Iron Clad Monadnock.

Bahia, December 30, 1865.

| True Magnetic Direction of Ship's Head. | Observed <br> Deviation of <br> Compass. | True Magnetic Direction of Ship's Head. | II. <br> Observed <br> Deviation of Compass. | $\begin{array}{\|c} \text { III. } \\ \text { Half Sum } \\ \text { of } \\ \text { Quantities } \\ \text { in Cols. I } \\ \text { and II. } \\ \text { Unchanging } \\ \text { Part of } \\ \text { Deviation. } \end{array}$ | IV. <br> Half Sum of Cols. I and II, (changing Signs of Col. II.) Semicircular Deviation. | V. <br> Computation of $B_{1}$. |  | VI. <br> Computation of $\mathrm{C}_{1}$. |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  | Products of Col. IV by Multipliers. |  | Products of Col. IV by Multipliers. |
| NORTH. <br> N. by E. <br> N. N. E. <br> N. E. by N. | $+1{ }^{\circ}{ }^{\prime}$ +320 +340 +430 | SOUTH. <br> S. by W. <br> S. S. W. <br> S. W. by S. | $+1^{\circ}$ $+10^{\prime}$ +1 +0 +0 | $\begin{aligned} & +1^{\circ} \\ & +20^{\prime} \\ & +2 \end{aligned} 20$ | $\begin{array}{cc}0^{\circ} & 0^{\prime} \\ +1 & 0 \\ +1 & \\ +1 & 0 \\ +2\end{array}$ | O $\mathrm{S}_{1}$ $\mathrm{~S}_{2}$ $\mathrm{~S}_{3}$ | $\begin{array}{rr}0^{\circ} & \mathrm{o}^{\prime} \\ +0 & 12 \\ +\mathrm{o}^{\prime} & 31 \\ +1 & 7\end{array}$ | 1 $\mathrm{~S}_{7}$ $\mathrm{~S}_{6}$ $\mathrm{~S}_{5}$ | $\begin{array}{r}0 \\ +0 \\ +0 \\ +1 \\ +14 \\ +14 \\ \hline\end{array}$ |
| N. E. <br> N. E. by E. <br> E. N. E. <br> E. by N. | +430 +55 +530 +540 | S. W. S. W. by W. W. S. W. W. by S. | 0  <br> -0  <br> -1 40 <br> -1 10 | +230 +210 +210 +155 | +220 +250 +320 +3.45 | S $\mathrm{S}_{4}^{4}$ $\mathrm{~S}_{5}$ $\mathrm{~S}_{7}$ | + +139 +231 +35 +341 | $\mathrm{S}_{4}$ $\mathrm{~S}_{3}$ $\mathrm{~S}_{2}$ $\mathrm{~S}_{1}$ | + +139 +134 +13 +0 |
| EAST. <br> E. by S. <br> E. S. E. <br> S. E. by E. | +520 +510 +440 +420 | WEST. <br> W. by N . <br> W. N. W. <br> N. W. by W. | - 2 0 <br> - 2 10 <br> - 2 0 | + +130 +130 +130 +1 | + 310 +340 +320 +310 | 1 <br> $\mathrm{~S}_{7}$ <br> $\mathrm{~S}_{6}$ <br> $\mathrm{~S}_{5}$ | +340 +336 +33 +238 |  | $\begin{array}{rr}0 & 0 \\ \text { - } & 43 \\ \text { - } & 17 \\ -1 & 46\end{array}$ |
| S. E. <br> S. E. by S. <br> S. S. E. <br> S. by E. | +320 +240 +210 +20 | N. W. <br> N. W. by N. <br> N. N. W. <br> N. by W. | -2 0 <br> 二1 10 <br> ¢ 10 <br> 0 30 | + +0 +0 +10 +15 +1 | +240 +155 +110 +0.45 | S $\mathrm{S}_{4}$ $\mathrm{~S}_{3}$ $\mathrm{~S}_{2}$ $\mathrm{~S}_{1}$ | $\begin{array}{rrr}+1 & 53 \\ +\mathbf{1} & 4 \\ +0 & 27 \\ +0 & 9\end{array}$ | - $\mathrm{S}_{4}$ $-\mathrm{S}_{5}$ $-\mathrm{S}_{6}$ $-5_{7}$ | $\begin{array}{rrr}\text { I } & 53 \\ \text {-1 } & 36 \\ \text {-1 } & 5 \\ \text { - } & 44\end{array}$ |
|  |  |  |  |  | Sum of + Sum of Divisor | $\begin{aligned} & \mathrm{erms} \\ & \mathrm{erms} \\ & 8 \\ & \mathrm{~B}_{1}= \end{aligned}$ | $\begin{aligned} & =+298 \\ & +298 \\ & +338.5 \end{aligned}$ | $\begin{aligned} & +\quad 907 \\ & \hline 8 \begin{array}{r} 9 \\ \hline \end{array} \begin{array}{l} 9 \\ \hline \end{array} \\ & \mathrm{C}_{1}=+0 \\ & \hline \end{aligned}$ |  |

N. B.-Easterly deviations are to be entered in this table with the sign + ; Westerly deviations with the sign - .

Computation of Coefficients $A_{1}, \mathrm{D}_{1}, \mathrm{E}_{1}$, from Deviations observed on 32 Points.


Nоте. $-S_{1}=.195 . \quad S_{2}=.383 . \quad S_{3}=.556 . \quad S_{4}=.707 . \quad S_{5}=.83 \mathrm{I} . \quad S_{6}=.924 . \quad S_{7}=.98 \mathrm{I}$.
The resulting values of the coefficients for each compass, at each station, are given in the following tables:

Coefficients of the Deviations of the Admiralty Standard Compass.

| SŢATION. | DATE. | $\mathrm{A}_{1}$ | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | $+\mathrm{I}^{\circ} 37^{\prime} .4$ | $+9^{\circ} 4^{\prime} .6$ | - $0^{\circ} 33^{\prime} .1$ | $+0^{\circ} 29^{\prime} .2$ | -o ${ }^{\circ} 7^{\prime} \cdot 5$ |
| St. Thomas | November 18, 1865 | +o 14.6 | + 545.5 | +o 33.5 | +o 3.2 | -o 48.2 |
| Bahia | December 30, 1865 | + 140.2 | + 338.5 | +or 0.4 | +o 47.8 | - 0.0 |
| Monte Video | January 24, 1866 | + I 32.8 | + 34.8 | +o 5.8 | + 19.5 | +o 14.5 |
| Sandy Point | February 10, 1866 | +o 35.9 | + I 20.6 | -o 40.6 | +o53.5 | +or 1.5 |
| Valyaraiso. | April 4, I866 | +o 35.6 | + I 20.2 | -o 6.9 | +o54.2 | -0 10.2 |
| Callao | April 29, 1866 | +o9.1 | +221.1 | -o 1.8 | +o52.5 | +o 5.8 |
| Panama | May 20, 1866 | +o31.6 | + 3 2.1 | +or 1.9 | +o55.0 | +o88.0 |
| Acapulco | June I, 1866 | -o 36.9 | +245.4 | +o 5.5 | +o56.8 | +o8.0 |
| San Francisco. | June 23, 1866 | - - 39.6 | + 4 53.2 | $\begin{array}{lll}\text { - } & 15\end{array}$ | +0.51.2 | +o 5.8 |

Coefficients of the Deviations of the After Binnacle Compass.

| STATION. | DATE. |  | $\mathrm{A}_{1}$ |  | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ |  | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November | I, 'ı 865 | $+$ | $7^{\prime} \cdot 5$ | $+7^{\circ}{ }^{16}{ }^{\prime} .8$ |  | $14^{\prime} \cdot 1$ | $+1^{\circ} 39^{\prime} .2$ |  | $6{ }^{\prime} .2$ |
| St. Thomas | November | 18, 1865 |  |  |  |  |  |  |  |  |
| Bahia | December | 30, 1865 | + 1 |  | + 543.6 | - |  | + I 4 I .5 | + | 7.8 |
| Monte Video . | January | 24, 1866 | $\underline{1}$ | 3.1 | + +53.6 | $+$ | 41.9 | +157.5 | - | 42.5 |
| Sandy Point Valparaiso | February | 10, 1866 4,1866 | +0 | 24.5 | +534.4 $+\quad 388$ | + | 14.6 7 | $\begin{array}{r}\text { I } \\ +18.5 \\ +2 \\ \hline\end{array}$ | $\pm$ | 0.2 0.2 |
| Valparaiso . Callao . | April April | 4, 1866 29 29 | +o |  | +358.8 +45.5 | $\pm$ | $7.9$ | +21.5 +297.5 | $\stackrel{+}{+}$ |  |
| Panama. | May | 20, 1866 | - 0 | 50.0 | + | $+$ | 22.0 | + 232.7 |  | 18.0 |
| Acapulco | June | I, I866 | -1 |  | + 3 4.4 |  | 17.1 | +215.2 |  | 17.2 |
| San Francisco . | June | 23, 1866 | - 0 |  | + ${ }^{\text {2 }} 28.2$ |  | 13.9 | + 147.5 | + | 10.2 |

Coefficients of the Deviations of the After Ritchie Compass.

| STATION. | DATE. | $\mathrm{A}_{1}$ | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | + $7^{\circ}{ }^{4} 0^{\prime} .0$ | $+11^{\circ} 26^{\prime} .5$ | - $\mathrm{I}^{\circ} .44^{\prime} .1$ | $+0^{\circ}{ }_{15}{ }^{\prime} 5$ | - $0^{\circ} 54^{\prime} .5$ |
| St. Thomas | November 18, 1865 | + 314.4 | + 8.26 .9 | +o40.4 | +154.2 | -0 37.2 |
| Bahia | December 30, 1865 | + 8 47.1 | + 655.6 | -o 57.2 | + I 59.7 | +o 14.2 |
| Monte Video | January 24, 1866 |  |  |  | ..... |  |
| Sandy Point | February 10, 1866 | +818.4 | + 43.2 | -3 25.6 | + I 14.5 | +o 58.5 |
| Valparaiso. | April 4, 1866 | + 421.9 | + 349.1 | +o 12.4 | +221.0 | +o 7.5 |
| Callao | April 29, 1866 | + 419.4 | + 5 50.1 | +oris 1 | + 130.5 | +o52.0 |
| Panama. | May 20, 1866 | + 5 20.6 | + 4 3.1 | -0 10.2 | +137.0 | - 1333.0 |
| Acapulco | June 1, 1866 | +40.6 | + 429.1 | + I 12.8 | +112.2 | +o 47.0 |
| San Francisco . | June 23, 1866 | + 4 11.6 | + 646.2 | -I 31.4 | +2 28.5 | +o 21.2 |

Coefficients of the Deviations of the After Azimuth Compass.

| STATION. | DATE. | $\mathrm{A}_{1}$ | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | - $\mathrm{I}^{\circ} 5^{\prime} .0$ | $-4^{\circ} 53^{\prime} .0$ | - $0^{\circ} \quad 9^{\prime} \cdot 1$ | $+5^{\circ} 35^{\prime} .2$ | $+0^{\circ}{ }_{17}{ }^{\prime} .0$ |
| St. Thomas | November 18, 1865 | - 117.5 | $\begin{array}{lll}-3 & 0.9\end{array}$ | + 120.0 | +649.2 | +o 12.2 |
| Bahia | December 30, 1865 | $\begin{array}{lll}-3 & 36.9\end{array}$ | -4 28.6 | -o 19.5 | + 722.0 | - 15.5 |
| Monte Video . | January 24, 1866 |  |  | ...... |  |  |
| Sandy Point | February 10, 1866 | -o 5.6 | -2 57.8 | -o 47.2 | +7 10.2 | -o 25.5 |
| Valparaiso. | April 4, 1866 | -2 16.2 | -4 54.1 | +o 20.9 | + 552.5 | +o 37.5 |
| Callao | April 29, 1866 | -3 ${ }^{56.2}$ | -2 0.6 | -o ${ }^{0} 49.6$ | +56.5 | +o 35.7 |
| Panama. | May 20, 1866 | - 26.9 |  | + I 44.6 |  | -o 34.0 |
| $\underset{\text { San Francisco }{ }^{\text {Acapalco }} \text {. }}{ }$ | $\begin{array}{rr}\text { June } & \text { 1, } 1866 \\ \text { Jume } & 23,1866\end{array}$ | -3 11.2 | $\begin{array}{lll}-3 & 25.8\end{array}$ | -o 0.8 | + 5 54.2 | +o 23.8 |

Coefficients of the Deviations of the Forward Alidade Compass.

| STATION. | DATE. | $\mathrm{A}_{1}$ | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | $+2^{\circ} 8^{\prime} .1$ | - $2^{\circ} 28^{\prime \prime} .4$ | - $\mathrm{I}^{\circ} 5^{2 \prime} .0$ | + $\mathrm{I}^{\circ} 4^{\prime} .2$ | $0^{\circ} 0.0$ |
| St. Thomas | November 18, 1865 | +o 50.9 | -o 35.1 | -o 46.2 | +115.7 | +o 20.5 |
| Bahia | December 30, 1865 | $\begin{array}{lll}+2 & 9.4\end{array}$ | -o 6.0 | -o 34.1 | + 115.0 | +o 14.5 |
| Monte Video | January 24, 1866 | + 27.1 | +o 57.2 | 15.0 | + 123.0 | - o 9.8 |
| Sandy Point | February 10, 1866 | + 225.6 | +o 58.5 | - I 54.4 | + 184.0 | -0 20.2 |
| Valparaiso . | April 4, 1866 | + I 55.2 | +o 30.0 | -o 53.9 | + 14.2 | -o 5.2 |
| Callao | April 29, 1866 | +o 21.0 | +o 40.9 | - I 36.4 | +129.0 | - 6.8 |
| Panama. | May 20, 1866 | +2 15.2 | + 1.1 | -1-1 22.1 <br> -0 3.1 | +1 21.0 | $\begin{array}{ll}-0 & 6.8\end{array}$ |
| Acapulco . | June ri, 1866 | r +18.1 $+\quad 0$ | - 1 28.4 <br> I 54.2 | -0 333.1 | +152.8 $+\quad 588.0$ |  |
| San Francisco . | June 23, 1866 | +o 40.6 | - I 54.2 | - 2 25.1 | +o58.0 | +o 21.5 |

Coefficients of the Deviations of the Forward Binnacle Compass.


Coefficients of the Deviations of the Forward Ritchie Compass.

| STATION. | DATE. | $\mathrm{A}_{1}$ | $\mathrm{B}_{1}$ | $\mathrm{C}_{1}$ | $\mathrm{D}_{1}$ | $\mathrm{E}_{1}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | $+4^{\circ} 22^{\prime} .5$ | $+\mathrm{I}^{\circ} 19^{\prime} .2$ | $-3^{\circ} 37^{\prime} .2$ | $+2^{\circ}{ }^{1} 7^{\prime} .2$ | $+0^{\circ} 27^{\prime} .5$ |
| St. Thomas | November 18, 1865 | + I 3.7 | + 24.0 | - 1 | $+316.0$ | -o 25.5 |
| Bahia | December 30, 1865 | + 26.2 | + 3 29.I | I $\quad 33.9$ | +235.7 | -0 0.5 |
| Monte Video | January 24, 1866 | + 323.8 | + 3 48.0 | - 0.4 | +2 11.0 | -o 28.5 |
| Sandy Point | February 10, 1866 | + 146.2 | + 349.5 | - 244.2 | +2 $\begin{array}{r}11.2 \\ \hline\end{array}$ | -0 10.0 |
| Valparaiso . | April 4, 1866 | + 333.4 | + 120.2 | - 129.0 | + 27.8 | +o31.2 |
| Callao | April 29, 1866 | +237.1 | + I 52.8 | - 158.0 | + 230.5 | + 012.0 |
| Panama. | May 20, 1866 | + 134.0 | +o. 12.2 | - 153.8 | + 210.8 | -0 14.0 |
| Acapulco | June 1, 1866 | + I 52.8 | +o38.2 | $\begin{array}{ll}2 & 11.8\end{array}$ | +224.2 | +o 26.2 |
| San Francisco. | June 23, 1866 | $\begin{array}{ll}\text { + } & 3\end{array}$ | O 16.2 | -6 41.6 | + 148.5 | - 33.5 |

In the case of the Admiralty Standard Compass, for some not very evident reason, the variations in the value of the coefficient $A_{1}$ are greater than might have been expected. The After Binnacle, Forward Alidade, and Forward Binnacle Compasses were frequently removed from their places, and the fittings were not sufficiently exact to give any certainty of replacing them with their lubber lines always precisely in the same position. This source of error sufficiently accounts for the variations in the values of the $A_{1}$ s belonging to them. The Forward and After Ritchie Compasses were firmly fixed in their places, and were not removed during the cruise, except at Valparaiso; but the arrangements for reading off their cards were such that an improper position of the eye of the observer might easily introduce a large parallax, which accounts for the changes in the values of the $A_{1} \mathrm{~s}$ belonging to them. The After Azimuth Compass was always taken down after each swing, and as there was no fixed mark by which to adjust its lubber line, the changes in the value of its $A_{1}$ are not surprising.

It now becomes necessary to determine the probable errors of the values of the coefficients which have just been given. To do this for any compass, at any particular station, the value of $\delta$ at each of the thirty-two points must be computed from the coefficients for that station. Comparing the values thus found with the corrected observed values, a series of thirty-two residuals are obtained, from which the probable error of $\delta$ for that station is deduced by means of the formula

$$
r=0.6745 \sqrt{\frac{[v v]}{m-\mu}}
$$

where $r$ is the probable error of a single observed value of $\delta$; [ $v v$ ] the sum of the squares of the thirty-two residuals; $m$ the number of the residuals, in this case thirty-two; and $\mu$ the number of the coefficients, in the present instance five. Then, letting $p_{A}, p_{B}, p_{C}, p_{D}, p_{E}$, represent respectively the weights, and $r_{A}, r_{B}, r_{C}, r_{D}, r_{E}$, the probable errors, of the values of $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, when determined from a set of deviations observed on each of the thirty-two true magnetic points; we have

$$
r_{A}=\frac{r}{\sqrt{p_{A}}} \quad r_{B}=\frac{r}{\sqrt{p_{B}}}
$$

$\& c$.

From the normal equations on page 126, we also have,

$$
\begin{array}{ll}
p_{A}=32 & p_{D}=16 \\
p_{B}=16 & p_{E}=16 \\
p_{C}=16 &
\end{array}
$$

It is therefore evident that the probable errors of $B_{1}, C_{1}, D_{1}$, and $E_{1}$, will all be equal to each other.

The probable error of a single observed value of $\delta$ has been computed in this way, for each compass, at three stations; namely, Bahia, Sandy Point, and Panama, and the results are given in the following table. The column headed "mean value of $r$ " was obtained by adding together, for each compass, the sum of the squares of the residuals at Bahia, Sandy Point, and Panama; dividing the result by three; and then computing the value of $r$ from the mean value of $[v v]$ thus found. The column headed " $\frac{r}{\sqrt{32}}$ " gives the probable error of $A_{1}$; and the column headed " $\frac{r}{\sqrt{16}}$ " gives the probable error of $B_{1}, C_{1}, D_{1}$, and $E_{1}$, for each compass, when these coefficients have been computed from a set of deviations observed on thirty-two points.

| Compass. | Value of $r$. |  |  | Mean <br> value of $r$. | $\frac{r}{\sqrt{32}}$ | $\frac{r}{\sqrt{16}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Bahia. | Sandy Point. | Panama. |  |  |  |
| Admiralty Standard | $\pm \quad 9^{\prime} .8$ | $\pm 12^{\prime} .2$ | $\pm 1 \mathrm{I}^{\prime} \cdot 3$ | $\pm \mathrm{II} .1$ | $\pm 2^{\prime} .0$ | $\pm \quad 2^{\prime} .8$ |
| After Binnacle . . | $\pm 25.8$ | $\pm 20.1$ | $\pm 26.2$ | $\pm 24.2$ | $\pm 4.3$ | $\pm 6.1$ |
| After Ritchie | $\pm 30.6$ | $\pm 56.6$ | $\pm 38.8$ | $\pm 43.4$ | $\pm \quad 7.7$ | $\pm 10.8$ |
| After Azimuth | $\pm 39.3$ | $\pm 5 \mathrm{r} .1$ | $\pm 32.6$ | $\pm 41.7$ | $\pm .7 \cdot 4$ | $\pm 10.4$ |
| Forward Alidade | $\pm 19.0$ | $\pm 24.5$ | $\pm 23.6$ | $\pm 22.5$ | $\pm 4.0$ | $\pm 5.6$ |
| Forward Binnacle . | $\pm 40.2$ | $\pm 31.2$ | $\pm 25.3$ | $\pm 32.8$ | $\pm 5.8$ | $\pm 8.2$ |
| Forward Ritchie . | $\pm 59.7$ | $\pm 30.2$ | $\pm 37.8$ | $\pm 44.4$ | $\pm 7.8$ | $\pm \mathrm{II} .1$ |

As an incidental result, this table shows that for ordinary steering compasses (such as the Forward Alidade, Forward Binnacle, and After Binnacle) when read to the nearest eighth of a point, the probable accidental error of a single reading is about half a degree; for Ritchie Monitor Compasses (such as the Forward and After Ritchie) when read to the nearest eighth of a point, the probable accidental error of a single reading is about three-quarters of a degree; and for Admiralty Standard Compasses, read to the nearest ten minutes, the probable accidental error of a single reading is about eleven minutes.

From the mathematical theory of the deviations of the compass, given in a preceding part of this section, we have

$$
\mathfrak{B}=B_{1}-A_{1} C_{1}
$$

and also

$$
\mathfrak{B}=\frac{c}{\lambda} \tan \theta+\frac{P}{\lambda} \times \frac{1}{H}
$$

Hence

$$
0=-B_{1}+A_{1} C_{1}+\frac{c}{\lambda} \tan \theta+\frac{P}{\lambda} \times \frac{1}{H}
$$

But as $P$ is liable to undergo a slow change, we introduce a term depending upon the time, and the equation becomes

$$
\begin{equation*}
0=-B_{1}+A_{1} C_{1}+\frac{c}{\lambda} \tan \theta+\frac{P}{\lambda} \times \frac{1}{H}+\frac{\Delta P}{\lambda} \times \frac{t}{\bar{H}} \tag{17}
\end{equation*}
$$

where $\Delta P$ is the change of the value of $P$ in one day, and $t$ is the elapsed time in days, counted from November 1st, 1865.

We have further
and also

$$
\mathfrak{C}=C_{1}+A_{1} B_{1}
$$

$$
\aleph=\frac{f}{\lambda} \tan 0+\frac{Q}{\lambda} \times \frac{1}{H}
$$

Hence

$$
0=-C_{1}-A_{1} B_{1}+\frac{f}{\lambda} \tan \theta+\frac{Q}{\lambda} \times \frac{1}{H}
$$

But as $Q$ is liable to undergo a slow change, we introduce a term depending upon the time, in the same manner as above, and the equation becomes

$$
\begin{equation*}
0=-C_{1}-A_{1} B_{1}+\frac{f}{\lambda} \tan \theta+\frac{Q}{\lambda} \times \frac{1}{H}+\frac{\Delta Q}{\lambda} \times \frac{t}{H} \tag{18}
\end{equation*}
$$

Each observed value of $B_{1}$ and $C_{1}$ gives two equations of condition; one of the same form as (17), the other of the same form as (18); and from all the equations of condition thus obtained for any compass, the values of $A_{1}, \frac{c}{\lambda}, \frac{P}{\lambda}, \frac{\Delta P}{\lambda}, \frac{f}{\lambda}, \frac{Q}{\lambda}$, and $\frac{\Delta Q}{\lambda}$, for that compass, have been computed by the method of least squares.

The value of $A_{1}$ thus found we will designate as the "true $A_{1}$ " in order to distinguish it from the "apparent $A_{1}$ " obtained directly from the corrected observed values of the deviations. The value of the true $A_{1}$ depends only upon the value of the constants $a, b, d$, and $e$, in equations (1) and (2); but the apparent $A_{1}$ is made up of the true $A_{1}$, together with any errors that may exist in the placing of the lubber line of the compass, or in the determination of the true magnetic bearing of the distant object used as an azimuth mark in swinging the ship.

The equations of condition, formed in the manner just explained; the normal equations derived from them by the method of least squares; and the resulting values of the constants, $A_{1}, \frac{c}{\lambda}, \frac{P}{\lambda}, \frac{\Delta P}{\lambda}, \frac{f}{\lambda}, \frac{Q}{\lambda}$, and $\frac{\Delta Q}{\lambda}$, for each compass are as follows: the values of $B_{1}$ and $C_{1}$ being expressed in parts of radius.

Admiralty Standard Compass．
Equations of Condition．

| Absolute Terms． | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\Delta Q$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.158$ | － 0.010 | ＋ 2.694 | ＋ 0.212 |  |  |  |  |
| $\mathrm{o}=-\mathrm{o} .100$ | ＋ 0.010 | $\underline{1.176}$ | ＋ 0.148 | ＋ 2.520 |  |  |  |
| $0=-0.064$ | 0.000 +0.002 | ＋ 0.077 | 1 $+\quad 0.161$ +0.166 | ＋ 9.516 |  |  |  |
| $0=-0.054$ $0=-0.023$ | ＋ 0.002 +0.012 | － 0.603 | ＋0．166 | ＋13．933 |  |  |  |
| $0=-0.023$ $0=-0.023$ | 二0．012 | － 1.426 | $\begin{array}{r}+\quad 0.164 \\ +\quad 0.158 \\ \hline\end{array}$ | ＋ 16.522 |  |  |  |
| $0=-0.0231$ | 二0．002 | － 0.711 | $+\quad 0.158$ $+\quad 0.143$ | +24.375 $+\quad 25.68$ |  |  |  |
| ． $0=-0.053$ | ＋0．001 | ＋0．623 | ＋ 0.132 | ＋ 26.316 |  |  |  |
| $0=-0.048$ | ＋ 0.002 | ＋ 0.836 | ＋ 0.129 | ＋27．440 |  |  |  |
| $0=-0.085$ | －0．022 | ＋1．910 | ＋ 0.177 | ＋41．519 |  |  |  |
| $0= \pm 0.010$ $0=-0.010$ | $\begin{array}{r}\text {－} 0.158 \\ \hline 0.100\end{array}$ |  |  |  | a $+\quad 2.694$ $+\quad 1.176$ | ＋ 0.212 <br> $+\quad 0.148$ |  |
| $0=0.000$ | －0．064 |  |  |  | $+\quad 1.1767$ $+\quad 0.77$ | +0.128 $+\quad 0.161$ | $+\quad 9.516$ |
| $0=-0.002$ | －0．054 |  |  |  | － 0.603 | ＋ 0.166 | ＋ 13.933 |
| $0=+0.012$ | －0．023 |  |  |  | － 1.426 | ＋ 0.164 | ＋16．522 |
| $0=+0.002$ | －0．023 |  |  |  | － 0.710 | ＋0158 | ＋ 24.375 |
| $0=+0.001$ | －0．041 |  |  |  | －0．113 | ＋ 0.143 | ＋ 25.608 |
| $0=-0.001$ | －0．053 |  |  |  | ＋ 0.623 | ＋0．132 | ＋ 26.316 |
| $0=-0.002$ | －0．048 |  |  |  | $+0.836$ | ＋ 0.129 | ＋ 27.440 |
| $0=+0.022$ | －0．085 |  |  |  | － 1.910 | ＋ 0.177 | ＋41．519 |

Normal Equations．

| $0=0.000$ | ＋ 0.058 |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.699$ | －0．037 | ＋16．294 |  |  |  |  |  |
| $0=-0.109$ $0=-9.869$ | － 0.006 -1.057 | ＋ $+\quad 0.826$ $+\quad 0.177$ | $+\quad 0.258$ $+\quad 28.85$ | ＋ 4983 |  |  |  |
| $0=+0.037$ | －1．057 | 70.17 |  | $+4983.3$ |  |  |  |
| $0=+0.006$ | －0．109 |  |  |  | $+\quad 0.826$ $+\quad$ | ＋ 0.258 |  |
| $0=+\mathrm{r} .057$ | $-9.869$ |  |  |  | ＋ 70.177 | ＋ 28.825 | ＋ 4983.3 |

Hence

$$
\begin{array}{llrl}
A_{1} & =0.000 & \frac{P}{\lambda} & =+0.460 \\
\frac{c}{\lambda} & =+0.0240 & \frac{\Delta P}{\lambda} & =+0.00102
\end{array}
$$

After Binnacle Compass．
Equations of Condition．

| Absolute Terms． | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.127$ | －0．022 | ＋ 2.694 | ＋ 0.212 |  |  |  |  |
| $0=-\mathrm{o} .100$ | －0．002 | ＋ 0.077 | ＋0．161 | ＋ 9.516 |  |  |  |
| $0=-0.096$ | ＋ 0.012 | － 0.603 | ＋0．166 | ＋ 13.933 |  |  |  |
| $0=-\mathrm{o} .100$ | －0．004 | － 1.426 | ＋0．164 | ＋16．522 |  |  |  |
| $0=-0.070$ | ＋0．002 | －0．710 | ＋0．158 | ＋ 24.375 |  |  |  |
| $0=-0.073$ | －0．001 | －0．113 | ＋0．143 | ＋ 25.608 |  |  |  |
| $0=-0.058$ | ＋0．006 | ＋0．623 | ＋0．132 | ＋ 26.316 |  |  |  |
| $0=-0.054$ | －0．005 | ＋0．836 | ＋0．129 | ＋ 27.440 |  |  |  |
| $0=-0.061$ $0=+0.022$ | －0．039 | ＋ 1.910 | ＋0．177 | ＋41．519 |  |  |  |
| $0=+0.002$ | 二－0．127 － 0.100 |  |  |  | ＋ +0.694 +0.077 | ＋ 0.212 +0.161 |  |
| $0=-0.012$ | －0．096 |  |  |  | －0．603 | a +0.166 +0.161 | a $+\quad 9.516$ +13.933 |
| $0=+0.004$ | －0．100 |  |  |  | － 1.426 | ＋ 0.164 | ＋ +16.522 |
| $0=-0.002$ | －0．070 |  |  |  | －0．710 | ＋0158 | ＋ 24.375 |
| $\mathrm{o}=+\mathrm{o} .001$ | －0．073 |  |  |  | －0．113 | ＋0．143 | ＋ 25608 |
| $0=-0.006$ | －0．058 |  |  |  | ＋0．623 | ＋0．132 | ＋ 26.316 |
| $0=+0.005$ | －0．054 |  |  |  | ＋0．836 | ＋0．129 | ＋ 27.440 |
| $0=+0.039$ | －0．061 |  |  |  | ＋1．910 | ＋0．177 | ＋ 41.519 |

After Binnacle Compass．
Normal Equations．

| Absolute Terms． | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=0.000$ | ＋ 0.068 |  |  |  |  |  |  |
| $0=-0.288$ | －0．136 | $+14.910$ |  |  |  |  |  |
| $0=$－ 0 | 二 $\begin{array}{r}0.010 \\ \text { 1．478 }\end{array}$ | $+\quad 0.652$ $+\quad 67.212$ | a $+\quad 0.236$ +28.451 | ＋4977．0 |  |  |  |
| $0=+0.136$ | － 0.288 |  |  |  | ＋ 14.910 |  |  |
| $0=+0.010$ | －0．122 |  |  |  | ＋ 0.652 | $\underline{0.236}$ |  |
| $\mathrm{o}=+\mathrm{I} .478$ | － 13.033 |  |  |  | ＋67．212 | ＋ 28.45 I | －4977．0 |

Hence

$$
\begin{aligned}
A_{1} & =-0.010 & \frac{P}{\lambda} & =+0.664 \\
\frac{c}{\lambda} & =-0.0048 & \frac{\Delta P}{\lambda} & =-0.00112
\end{aligned}
$$

After Ritchie Compass．
Equations of Condition．

| Absolute Terms． | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.200$ | － 0.030 | ＋ 2.694 | ＋ 0.212 |  |  |  |  |
| $0=-0.148$ | ＋ 0.012 | $\underline{1.176}$ | $\underline{+0.148}$ | ＋ 2.520 |  |  |  |
| $0=-0.121$ | － 0.017 | ＋ 0.077 | $\underline{0.161}$ | ＋ 9.516 |  |  |  |
| $0=-0.071$ | － 0.060 | － 1.426 | ＋0．164 | ＋ 16.522 |  |  |  |
| $0=-0.067$ $0=0.102$ | ＋ $+\quad 0.004$ $+\quad 0.004$ | － 0.710 | $+\quad 0.168$ $+\quad 0.143$ | +24.375 +25.608 |  |  |  |
| o エー0．071 | ［ 0.003 | ＋ $+\quad 0.623$ | $+\quad 0.132$ $+\quad 0.132$ | ＋ 26.316 +26.314 |  |  |  |
| $0=-0.078$ | ＋ 0.021 | ＋ 0.836 | ＋ 0.129 | ＋ 27.440 |  |  |  |
| $0=-0.118$ | － 0.027 | ＋ 1.910 | ＋ 0.177 | ＋41．519 |  |  |  |
| $0=+0.030$ | － 0.200 |  |  |  | ＋ 2.694 | ＋ 0.212 |  |
| $0=-0.012$ | － 0.148 |  |  |  | ＋ 1.176 | ＋ 0.148 | ＋ 2.520 |
| $0=+0.017$ | 0．121 |  |  |  | ＋ 0.077 | ＋0．161 | ＋ 9.516 |
| $0=+0.060$ | － 0.071 |  |  |  | － 1.426 | ＋0．164 | ＋ 16.522 |
| $0=-0.004$ | － 0.067 |  |  |  | － 0.710 | ＋0．158 | ＋ 24.375 |
| $0=-0.004$ | 二 0.102 |  |  |  | － $\begin{array}{r}0.113\end{array}$ | ＋0．143 | ＋ 25.608 |
| $0= \pm 0.003$ $0=-0.021$ | 二 $\begin{array}{r}0.071 \\ 0.078\end{array}$ |  |  |  | ＋ $+\quad 0.623$ $+\quad 0.836$ | $+\quad 0.132$ $+\quad 0.129$ | ＋ 26.316 +27.440 |
| $0=+0.027$ | o．118 |  |  |  | ＋ 1.910 | ＋ 0.177 | ＋41．519 |

Normal Equations．


Hence

$$
\left.\begin{array}{llrl}
A_{1} & =0.000 & \frac{P}{\lambda} & =+0.766 \\
\frac{c}{\lambda} & =+0.0178 & \frac{\Delta P}{\lambda} & =-0.00122
\end{array}\right) \frac{\frac{f}{\lambda}}{}=+0.0052
$$

After Azimuth Compass.
Equations of Condition.

| Absolute Terms. | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=+0.085$ | -0.003 | +2.694 | +0.212 |  |  |  |  |
| $0=+0.053$ | +0.023 | +1.176 | +0.148 | + 2.520 |  |  |  |
| $0=+0.078$ | -0.006 | + 0.077 | +0.161 | + 9.516 |  |  |  |
| $0=+0.052$ | -0.014 | - 1.426 | +0.164 | + 16.522 |  |  |  |
| $0=+0.086$ | +0.006 | -0.710 | +0.158 | +24.375 $+\quad 25.608$ |  |  |  |
| $0=+0.035$ $0=+0.066$ | -0.014 | -0.113 | +0.143 | +25.608 |  |  |  |
| $0=+0.066$ $0=+0.060$ | +0.030 0.000 | +0.623 +0.836 | +0.132 $+\quad 0.1329$ | $\begin{aligned} & +26.316 \\ & +27.440 \end{aligned}$ |  |  |  |
| $0=+0.003$ | + 0.085 |  |  |  | +2.694 | +0.212 |  |
| $0=-0.023$ | +0.053 |  |  |  | + 1.176 | +0.148 | + 2.520 |
| $0=+0.006$ | +0.078 |  |  |  | + 0.077 | + 0.161 | + 9.516 |
| $0= \pm 0.014$ $0=-0.006$ | +0.052 +0.086 |  |  |  | 1.426 -0.710 | +0.164 $+\quad 0.158$ | +16.522 $+\quad 24.375$ |
| $\mathrm{o}=+\mathrm{o} .014$ | +0.035 |  |  |  | $-0.113$ | +0.148 $+\quad .143$ | + 25.608 |
| $0=-0.030$ | +0.066 |  |  |  | a +0.623 +0.836 | +0.132 $+\quad 0.129$ | + 26.316 +27.440 |


| Normal Equations. |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=0.000$ | +0.037 |  |  |  |  |  |  |
| $0=+0.250$ | +0.055 | +12.282 |  |  |  |  |  |
| $0=+0.082$ | +0.003 | + 0.588 | $+0.200$ |  |  |  |  |
| $0=+8.100$ | +0.352 | $-0.725$ | +19.147 | $+3065.3$ |  |  |  |
| $0=-0.055$ $0=-0.003$ | +0.350 $+\quad 0.082$ |  |  |  | $+\quad 12.282$ $+\quad 0.588$ | + 0.200 |  |
| $\mathrm{o}=-0.352$ | +8.100 |  |  |  | -0.725 | +19.147 | $+3065.3$ |

Hence


Forward Alidade Compass.
Equations of Condition.

| Absolute Terms. | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=+0.043$ | -0.033 | + 2.694 | +0.212 |  |  |  |  |
| $0=+0.010$ | -0.013 | +1.176 | +0.148 | + 2.520 |  |  |  |
| $0=+0.002$ | -0.010 | + 0.077 | +0.161 | + 9.516 |  |  |  |
| $0=-0.017$ | -0.019 | -0.603 | +0.166 | + 13.933 |  |  |  |
| $\mathrm{o}=$-0.017 | -0.033 | - 1.426 | +0.164 | + 16.522 |  |  |  |
| $0=-0.009$ | -0.016 | -0.710 | +0.158 | + 24.375 |  |  |  |
| $0=-0.012$ | -0.028 | -0.113 | +0.143 | + 25.608 |  |  |  |
| $0=0.000$ | -0.024 | +0.623 | +0.132 | + 26.316 |  |  |  |
| $0=+0.026$ | - 0.010 | +0.836 | +0.129 | + 27.440 |  |  |  |
| $0=+0.033$ | -0.042 | + 1.910 | +0.177 | + 41.519 |  |  |  |
| $0=+0.033$ | +0.043 |  |  |  | +2.694 | +0.212 |  |
| $0=+0.013$ | + 0.010 |  |  |  | + 1.176 | +0.148 | + 2.520 |
| $0=+0.010$ | + 0.002 |  |  |  | + 0.077 | +0.161 | + 9.516 |
| $\mathrm{o}=+\mathrm{o} .019$ | -0.017 |  |  |  | -0.603 | +0.166 | +13.933 |
| $0=+0.033$ | -0.017 |  |  |  | - 1.426 | +0.164 | + 16.522 |
| $0=+0.016$ | -0.009 |  |  |  | -0.710 | +0.158 | + 24.375 |
| $0=+0.028$ | -0.012 |  |  |  | -0.113 | +0.143 | +25.608 |
| $0=+0.024$ | 0.000 |  |  |  | +0.623 | +0.132 | + 26.316 |
| $0=+0.010$ | +0.026 |  |  |  | +0.836 | +0.129 | + 27.440 |
| $0=+0.042$ | +0.033 |  |  |  | + 1.910 | +0.177 | + 41.519 |

Forward Alidade Compass.
Normal Equations.

| Absolute Terms. | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=0.000$ | + 0.011 |  |  |  |  |  |  |
| $0=+0.255$ | -0.135 | +16.294 |  |  |  |  |  |
| $0=+0.012$ $0=+1.089$ | $\begin{array}{r}\text {-0.037 } \\ \hline 4.686\end{array}$ | $+\quad 0.826$ $+\quad 70.177$ | a $+\quad 0.258$ +28.825 | + 4983.3 |  |  |  |
| $\mathrm{o}=+0.135$ | +0.255 |  |  | + 4983.3 | +16.294 |  |  |
| $0=+0.037$ | +0.012 |  |  |  | + 0.826 | $+0.258$ |  |
| $\mathrm{o}=+4.686$ | +1.089 |  |  |  | + 70.177 | +28.825 | + 4983.3 |

Hence

| $A_{1}=-0.025$ | $\frac{P}{\lambda}=+0.014$ |
| :--- | :--- |
| $\frac{c}{\lambda}=-0.0162$ | $\frac{\Delta P}{\lambda}=-0.00010$ |


| $\frac{f}{\lambda}$ | $=-0.0012$ |
| ---: | :--- |
| $\frac{Q}{\lambda}$ | $=-0.106$ |
| $\frac{\Delta Q}{\lambda}$ | $=-0.0003 I$ |

Forward Binnacle Compass.
Equations of Condition.

| Absolute Terms. | A | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=+0.099$ | -0.045 | +2.694 | + 0.212 |  |  |  |  |
| $0=+0.034$ | -0.004 | + 1.176 | +0.148 | + 2.520 |  |  |  |
| $0=-0.008$ | - o.oro | + 0.077 | +0.161 | + 9.516 |  |  |  |
| $0=-0.051$ | -0.012 | -0.603 | +0.166 | + 13.933 |  |  |  |
| $0=-0.092$ | -0.038 | - 1.426 | +0.164 | + 16.522 |  |  |  |
| $0=-0.031$ | -0.013 | -0.710 | +0.158 | + 24.375 |  |  |  |
| $0=-0.020$ | -0.037 | -0.113 | +o.143 | + 25.608 |  |  |  |
| $0=+0.018$ | -0.027 | +0.623 | +0.132 | + 26.316 |  |  |  |
| $0=+0.036$ $0=+0.082$ | - 0.029 | + 0836 $+\quad 1.910$ | +0.129 +0.177 | +27.440 |  |  |  |
| $0=+0.045$ | +0.099 |  |  |  | +2.694 | +0.212 |  |
| $0=+0.004$ | + 0.034 |  |  |  | + 1.176 | +0.148 | + 2.520 |
| $0=+0.010$ | - 0.008 |  |  |  | + 0.077 | +0.161 | + 9.516 $+\quad .933$ |
| $0=+0.012$ | -0.051 |  |  |  | -0.603 | +0.166 | + 13.933 |
| $0=+0.038$ | -0.092 |  |  |  | - 1.426 | + o.164 | + 16.522 |
| $0=+0.013$ | -0.031 |  |  |  | -0.710 | +0.158 | + 24.375 |
| $0=+0.037$ | - 0.020 |  |  |  | -0.113 | +0.143 | + 25.608 |
| $0=+0.027$ | +0.018 |  |  |  | +0.623 | +0.132 | + 26.316 |
| $\begin{aligned} & o=+0.029 \\ & 0=+0.062 \end{aligned}$ | +0.036 $+\quad 0.082$ |  |  |  |  | + +0.129 +0.177 | $+\quad 27.440$ +41.519 |
|  |  |  |  |  |  |  |  |
| Normal Equations. |  |  |  |  |  |  |  |
| $0=0.000$ | + 0.043 |  |  |  |  |  |  |
| $0=+0.690$ $0=+0.015$ | -0.211 | 16.294 $+\quad 0.826$ |  |  |  |  |  |
| $0=+0.015$ $0=+1.334$ | - 0.046 -6.283 | $+\quad 0.826$ $+\quad 70.177$ | $+\quad 0.258$ +28.825 | + 4983.3 |  |  |  |
| $0=+0.211$ | +0.690 |  |  |  | + 16.294 |  |  |
| $o=+0.046$ $0=+6.283$ | +0.015 |  |  |  | $+\quad 0.826$ $+\quad 70.177$ | + 0.258 |  |
| $0=+6.283$ | + 1.334 |  |  |  | + 70.177 | + 28.825 | + 4993.3 |

Hence

$$
\begin{aligned}
& A_{1}=0.000 \\
& \frac{c}{\lambda}=-0.0477
\end{aligned}
$$



Forward Ritchie Compass.
Equations of Condition.

| Absolute Terms. | $A_{1}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{\Delta P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.023$ | -0.063 | +2.694 | + 0.212 |  |  |  |  |
| $0=-0.036$ | -0.022 | +1.176 | +0.148 | + 2.520 |  |  |  |
| $0=-0061$ | -0.027 | + 0.077 | +0.161 | + 9.516 $+\quad .533$ |  |  |  |
| $0=-0.066$ | 0.000 | -0.603 | +0.166 | + 13.933 |  |  |  |
| $0=-0.067$ | -0.048 | - I. 426 | +0.164 | +16.522 |  |  |  |
| $0=-0.023$ | -0.026 | -0.710 | +0.158 | + 24.375 |  |  |  |
| $0=-0.033$ | -0.034 | -0.113 | +0.143 | + 25.608 |  |  |  |
| $0=-0.004$ $0=-0.011$ | -0.033 | + +0.623 +0.836 | +0.132 | + 26.316 |  |  |  |
| $0=$ - 0.005 | -0.317 | + +1.830 +1.910 | +0.32 +0.177 | +27.360 $+\quad 41.519$ |  |  |  |
| $0=+0.063$ | -0.023 |  |  |  | +2.694 | +0.212 |  |
| $0=+0.022$ | -0.036 |  |  |  | +1.176 | +0.148 | + 2.520 |
| $0=+0.027$ | -0.061 |  |  |  | + 0.077 | +0.161 | +9.516 |
| $\begin{aligned} & 0= \\ & 0\end{aligned}=\begin{array}{r}0.000 \\ 0.048\end{array}$ | -0.066 |  |  |  | - 0.603 | +0.166 | + 13.933 |
| $0=+0.048$ $0=+0.026$ | -0.067 |  |  |  | - 1.426 | +0:164 | + 16.522 |
| $\mathrm{o}=+\mathrm{o} .034$ | -0.033 |  |  |  | -0.113 | +0.158 $+\quad 0.143$ | + +25.308 +25.608 |
| $0=+0.033$ | -0.004 |  |  |  | +0.623 | +0.132 | +26.316 |
| $\mathrm{o}=+0.038$ | -0.011 |  |  |  | + 0.836 | +0.129 | + 27.440 |
| $\mathrm{o}=+\mathrm{o.117}$ | +0.005 |  |  |  | + 1.910 | +0.177 | + 41.519 |
| Normal Equations. |  |  |  |  |  |  |  |
| $0=0.000$ | +0.042 |  |  |  |  |  |  |
| $0=+0.044$ | -0.384 | +16.294 |  |  |  |  |  |
| $0=-0.052$ $0=-4.306$ | -0.068 -0.388 | $+\quad 0.826$ $+\quad 0.177$ | + 0.258 +28.825 |  |  |  |  |
| $\begin{aligned} & o=-4.306 \\ & o=+0.384 \end{aligned}$ | - 9.388 +0.044 | + 70.177 |  | + 4983.3 | + 16.294 |  |  |
| $0=+0.068$ | -0.052 |  |  |  | + 0.826 | +0.258 |  |
| $o=+9.388$ | $-4.306$ |  |  |  | + 70.177 | +28.825 | + 4983.3 |

Hence

$$
\begin{aligned}
A_{1} & =0.000 & \frac{P}{\lambda} & =+0.367 \\
\frac{c}{\lambda} & =-0.0169 & \frac{\Delta P}{\lambda} & =-0.00102
\end{aligned}
$$

The value of the true $A_{1}$ having thus become known for each compass, the values of the coefficients $\mathfrak{B}, \mathfrak{\Im}, \mathfrak{D}$, and $\mathfrak{E}$, for each compass, at each station, were next computed by means of the formulæ (16). The results, expressed in parts of radius, are as follows:

Coefficients of the Deviations of the Admiralty Standard Compass.

| STATION. | DATE. | $\mathfrak{2}$ | $\mathfrak{F}$ | (1) | ( | (5) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | 0.000 | +0.158 | - о.010 | +0.021 | -0.004 |
| St. Thomas . | November 18, 1865 | 0.000 | +o.100 | + 0.010 | +0.006 | -0.013 |
| Bahia | December 30, 1865 | 0.000 | +0.064 | 0.000 | +0.016 | 0.000 |
| Monte Video | January 24, 1866 | 0.000 | +0.054 | +0.002 | +0.024 | +0.004 |
| Sandy Point | February 10, 1866 | 0.000 | +0.023 | -0.012 | +0.016 | 0.000 |
| Valparaiso. | April 4, 8866 | 0.000 | +0.023 | -0.002 | + 0.0.16 | -0.003 |
| Callao . . | April 29, 1866 | 0.000 | +0.041 | 0.000 | +0.016 | +0.002 |
| Panama. | May 20, 1866 | 0.000 | +0.053 | +0.001 | +0.017 | +0.002 |
| Acapulco | June 1, 1866 | 0.000 | +0.048 | +0.002 | +0.018 | + 0.002 |
| San Francisco. | June 23, 1866 | 0.000 | +0.085 | - 0.022 | + 0.018 | 0.000 |
| Means |  |  |  |  | $+0.017$ | -0.001 |

Coefficients of the Deviations of the After Binnacle.

| STATION. | DATE. | 31 | 3 | 5 | ( ${ }^{\text {d }}$ | (3) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November I, 1865 | - 0.010 | +0.127 | -0.023 | +0.037 | - 0.001 |
| St. Thomas | November 18, 1865 | - 0.010 | ..... | ...... |  |  |
| Bahia ${ }^{\text {a }}$. | December 30, 186́5 | - 0.010 | +0.100 | -0.003 | +0.034 | +0.002 |
| Monte Video | January 24, 1866 | - o.010 | +0.096 | +0.011 | +0.039 | -0.012 |
| Sandy Point | February io, 180.0 | - o.010 | +0.100 | -0.005 | +0.040 | -0.001 |
| Valparaiso . | April 4, I36) | - 0.010 | + 0.070 | +0.002 | +0.038 | 0.000 |
| Callao . . | April 29,130. | - 0.010 | +0.073 | -0.002 | +0.040 | +0.002 |
| Panama. | May 20, I 360 | - 0.010 | +0.058 | +0.006 | +0.046 | -0.005 |
| Acapulco . ${ }^{\text {- }}$ |  | -0.010 | +0.054 $+\quad 0.060$ | -0.006 | +0.041 +0.032 | -0.006 0.000 |
| San Francisco. | June 23, 1866 | -0.010 | +0.060 | -0.040 | +0.032 | 0.000 |
| Means |  |  |  |  | +0.038 | -0.002 |

Coefficients of the Deviations of the After Ritchie Compass.

| STATION. | DATE. | 91 | $\mathfrak{F}$ | 5 | (5) | $\mathfrak{G}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, I865 | 0.000 | +0.200 | -0.030 | +0.024 | -0.022 |
| St. Thomas . . . . | November 18, 1865 | 0.000 | + 0.148 | +0.012 | +0.044 | $-0.009$ |
| Bahia . . . . . . | December 30, 1865 | 0.000 | +0.121 | -0.017 | + 0.042 | + 0.002 |
| Monte Video . . . . | January 24, 1866 | ...... | ...... |  | ... | ...... |
| Sandy Point . . . | February 10, 1866 | 0.000 | +0.071 | -0.060 | + 0.022 | $+0.013$ |
| Valparaiso . . . . | April 4, 1866 | 0.000 | +0.067 | +0.004 | + 0.043 | $+0.002$ |
| Callao . . | April 29, 1866 | 0.000 | +0.102 | +0.004 | +0.032 | + 0.016 |
| Panama. | May 20, 1866 | 0.000 | +0.071 | -0.003 | +0.025 | -0.027 |
| Acapulco . | June I, i866 | 0.000 | +0.078 | +0.021 | +0.024 | +0.015 |
| San Francisco . | June 23, 1866 | 0.000 | +o.118 | -0.027 | + 0.050 | +0.003 |
| Means |  |  |  |  | + 0.034 | - 0.001 |

Coefficients of the Deviations of the After Azimuth Compass.

| STATION. | DATE. | $\mathfrak{2}$ | $\mathfrak{P}$ | 5 | (1) | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, 1865 | 0.000 | -0.085 | -0.003 | +o.101 | +0.005 |
| St. Thomas . | November 18, 1865 | 0.000 | -0.053 | +0.023 | +0.120 | +0.002 |
| Bahia $\cdot$. | December 30, 1865 | 0.000 | $-0.078$ | - 0.006 | +0.132 | - 0.019 |
| Monte Video | January 24, 1866 | $\ldots$ | ...... | ...... |  | ...... |
| Sandy Point | February 10, 1866 | 0.000 | -0.052 | -0.014 | + 0.126 | $-0.007$ |
| Valparaiso . | April 4, 1866 | 0.000 | -0.086 | + 0.006 | +0.106 | +0.010 |
| Callao . . | April 29, 1866 | 0.000 | -0.035 | $\underline{+}$ | +0.090 | + 0.011 |
| Panama. | May 20, 1866 | 0.000 | -0.066 | + 0.030 | +0.113 | -0.012 |
| Acapulco . | June 1, 1856 | o.000 | - 0.060 | 0.000 | + 0.105 | +0.007 |
| San Francisco . | June 23, 1866 | ...... | ...... | ...... | ...... | ...... |
| Means |  |  |  |  | +0.112 | 0.000 |

Coefficients of the Deviations of the Formard Alidade Compass.

| STATION. | DATE. | $\mathfrak{Y}$ | $\mathfrak{F}$ | $\bigcirc$ | ( | @ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, 1865 | - 0.025 | - 0.044 | -0.032 | + 0.019 | + 0.001 |
| St. Thomas | November 18, 1865 | -0.025 | - 0.010 | -0.013 | +0.022 | + 0.006 |
| Bahia ${ }^{\text {a }}$. | December 30, 1865 | -0.025 | -0.002 | - 0.010 | +0.022 | + 0.004 |
| Monte Video | January 24, 1866 | -0.025 | +0.016 | -0.019 | +0.024 | -0.004 |
| Sandy Point | February 10, 1866 | -0.025 | +0.017 | -0.034 | +0.031 | $-0.007$ |
| Valparaiso . | April 4, 1866 | -0.025 | +0.008 | -0.016 | +0.019 | -0.002 |
| Callao . | April 29, 1866 | - 0.025 | +0.012 | -0.029 | +0.026 | -0.003 |
| Panama. | May 20, 1866 | -0.025 | - 0.001 | -0.024 | +0.023 | $-0.003$ |
| Acapulco | June I, 1866 | -0.025 | -0.026 | -0.009 | +0.033 | +0.002 |
| San Francisco. | June 23, 1866 | -0.025 | -0.034 | -0.041 | +0.017 | +0.007 |
| Means |  |  |  |  | + 0.024 | 0.000 |

Coefficients of the Deviations of the Forward Binnacle Compass.

| STATION. | DATE. | 21 | $\mathfrak{F}$ | 5 | ( ${ }^{\text {d }}$ | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | 0.000 | -0.099 | - 0.045 | + 0.044 | + 0.007 |
| St. Thomas | November 18, 1865 | 0.000 | -0.034 | -0.004 | +0.035 | -0.002 |
| Bahia | December 30, 1865 | 0.000 | +0.008 | - 0.010 | +0.037 | -0.003 |
| Monte Video | January 24, 1866 | 0.000 | +0.051 | -0.012 | +0.032 | -0.001 |
| Sandy Point | February 10, 1866 | 0.000 | +0.092 | -0.038 | +0.039 | -0.004 |
| Valparaiso. | April 4, 1866 | 0.000 | +0.031 | -0.013 | +0.028 | -0.003 |
| Callao | April 29, 1866 | 0.000 | + 0.020 | -0.037 | +0.037 | +0.006 |
| Panama. | May 20, 1866 | 0.000 | -0.018 | -0.027 | +0.037 | $-0.006$ |
| Acapulco | June 1, 1866 | 0.000 | -0.036 | -0.029 | $\underline{+0.046}$ | +0.004 |
| San Francisco. | June 23, 1866 | 0.000 | -0.082 | -0.062 | $+0.035$ | +0.014 |
| Means |  |  |  |  | + 0.037 | + 0.001 |

Coefficients of the Deviations of the Forward Ritchie Compass.

| STATION. | DATE. | 31 | $\mathfrak{F}$ | $\bigcirc$ | ( |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, 1865 | 0.000 | +0.023 | - 0.063 | $+0.038$ | + 0.006 |
| St. Thomas | November 18, 1865 | 0.000 | +0.036 | -0.022 | + 0.057 | -0.008 |
| Bahia ${ }^{\text {a }}$ - | December 30, 1865 | 0.000 | +0.061 | -0.027 | + 0.047 | -0.002 |
| Monte Video | January 24, 1866 | 0.000 | + 0.066 | 0.000 | + 0.040 | - 0.008 |
| Sandy Point | February 10, 1866 | 0.000 | +0.067 | -0.048 | +0.039 | -0.006 |
| Valparaiso . | April 4, 1866 | 0.000 | +0.023 | - 0.026 | +0.037 | +0.008 |
| Callao . | April 29, 1866 | 0.000 | +0.033 | -0.034 | +0.044 | +0.002 |
| Panama. | May 20, 1866 | 0.000 | +0.004 | -0.033 | +0.038 | $-0.004$ |
| Acapulco . | June 1, 1866 | 0.000 | +0.011 | -0.038 | +0.041 | +0.007 |
| San Francisco. | June 23, 1866 | 0.000 | -0.005 | -0.117 | + 0.025 | -0.009 |
| Means |  |  |  |  | +0.041 | -0.001 |

The values of the coefficients $\mathfrak{D}$ and $\mathbb{E}$ for any compass should be constant. Therefore the mean of all the observed values has been assumed as the truth, and is given on the line marked "means" in the case of each compass.

The constants thus far determined furnish the data with which to compute the values of the coefficients $\mathfrak{A}, \mathfrak{B}, \mathfrak{C}, \mathfrak{D}, \mathfrak{\bigotimes}$, in any part of the world, for any of the compasses under discussion. For convenience of reference these constants are collected in the following table:

| Compass. | $\mathrm{A}_{1}=3 \mathfrak{2}$ | $\frac{c}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{P}{\lambda}$ | $\frac{f}{\lambda}$ | $\frac{Q}{\lambda}$ | $\frac{\Delta Q}{\lambda}$ | ( $)$ | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Admiralty Standard | 0.000 | + 0.0240 | +0.460 | - 0.00102 | -0.0016 | + 0.006 | -0.00023 | +0.017 | -0.001 |
| After Binnacle . | 0.010 | -0.0048 | + 0.664 | -0.00112 | -0.0084 | +0.002 | -0.00022 | +0.038 | -0.002 |
| After Ritchie | 0.000 | +0.0178 | + 0.766 | -0.00122 | +0.0052 | - 0.149 | +0.00042 | +0.034 | - 0.001 |
| After Azimuth | 0.000 | -0.0026 | $-0.373$ | -0.00032 | + 0.0066 | -0.044 | +0.00039 | +0.112 | 0.000 |
| Forward Alidade . | - 0.025 | -0.0162 | +0.014 | - o.000ı0 | -0.0012 | -0.106 | -0.00031 | +0.024 | 0.000 |
| Forward Binnacle . | 0.000 | -0.0477 | +0.140 | -0.0004 | -0.0059 | -0.075 | -0.00074 | +0.037 | + 0.001 |
| Forward Ritchie | 0.000 | -0.0169 | +0.367 | -0.00102 | -0.0141 | -0.083 | -0.00120 | + 0.041 | - 0.001 |

The values of the coefficients $\mathfrak{A}, \mathfrak{F}, \mathfrak{C}, \mathfrak{D}, \mathfrak{E}$, for each compass at each station, were next computed from the quantities given in this table, in the following manner. The coefficients $\mathfrak{A}, \mathfrak{D}$, and $\mathfrak{C}$ are constant for each compass, and were taken 25 December, 1872.
directly from the table; while the coefficients $\mathfrak{B}$ and $\mathfrak{C}$ were obtained by means of the formulæ

$$
\begin{aligned}
\mathfrak{B} & =\frac{c}{\lambda} \tan \theta+\frac{P}{\lambda} \times \frac{1}{H}+\frac{\Delta P}{\lambda} \times \frac{t}{\bar{H}} \\
\mathfrak{S} & =\frac{f}{\lambda} \tan \theta+\frac{Q}{\lambda} \times \frac{1}{H}+\frac{\Delta Q}{\lambda} \times \frac{t}{H}
\end{aligned}
$$

where $\theta$ is the true magnetic dip; $H$ the earth's magnetic horizontal force, expressed in English units, namely, in feet, grains, and seconds; and $t$ the time in days, counted from November 1st, 1865. The results, expressed in parts of radius, are as follows:

Coefficients of the Deviations of the Admiralty Standard Compass.

| STATION. | DATE. | $\mathfrak{2}$ | $\mathfrak{P}$ | $\bigcirc$ | (1) | (6) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | 0.000 | +0.162 | -0.003 | +0.017 | -0.001 |
| St. Thomas | November 18, 1865 | 0.000 | +0.004 | -0.002 | +0.017 | -0.001 |
| Bahia | December 30, 1865 | 0.000 | +0.066 | -0.001 | +0.017 | - 0.001 |
| Monte Video | January 24, 1866 | 0.000 | +0.048 | -0.001 | +0.017 | - 0.001 |
| Sandy Point | February 10, 1866 | 0.000 | +0.024 | 0.000 | +0.017 | -0.001 |
| Valparaiso. | April 4, 1866 | 0.000 | +0.031 | -0.003 | +0.017 | - 0.001 |
| Callao | April 29, 1866 | 0.000 | +0.037 | -0.005 | +0.017 | - 0.001 |
| Panama. | May 20,1866 | 0.000 | +0.049 | -0.006 | +0.017 | - 0.001 |
| Acapulco | June 1, 1866 | 0.000 | +0.052 | -0.007 | $+0.017$ | - 0.001 |
| San Francisco . | June 23, 1866 | 0.000 | + 0.085 | -0.011 | +0.017 | - 0.001 |

Coefficients of the Deviations of the After Binnacle Compass.

| STATION. | DATE. | 91 | $\mathfrak{B}$ | C | (1) | (3) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | - 0.010 | +0.128 | -0.022 | +0.038 | -0.002 |
| St. Thomas | November 18, 1865 | ...... | …… | ..... |  | .... |
| ${ }_{\text {M }}^{\text {Bahia }}$ ( ${ }^{\text {ante }}$ Video | December 30, 1865 | - 0.010 | +0.096 $+\quad 0.098$ | - 0.002 +0.002 | +0.038 | -0.002 |
| Monte Video Sandy Point | $\begin{array}{ll}\text { January } \\ \text { February } & \text { 24, } 1866 \\ \text { 10, } & 1866\end{array}$ | -0.010 | +0.098 $+\quad 0.097$ | + 0.002 +0.009 | +0.038 +0.038 | - 0.002 |
| Valparaiso. | April 4, 1866 | -0.010 | + 0.081 | $\begin{array}{r}\text { + } \\ +0.001 \\ \hline\end{array}$ | +0.38 +0.038 $+\quad 0.038$ | -0.002 |
| Callao . . | April 29, 1866 | - 0.010 | + 0.067 | -0.004 | +0.038 | -0.002 |
| Panama | May 20, 1866 | - 0.010 | + 0.055 | -0.011 | +0.038 | -0.002 |
| Acapulco | June 1, 1866 | -0.010 | +0.051 | -0.013 | +0.038 | -0.002 |
| San Francisco. | June 23, 1866 | - 0.010 | + 0.062 | -0.025 | +0.038 | -0.002 |

Coefficients of the Deviations of the After Ritchie Compass.

| STATION. | DATE. | $\mathfrak{Y}$ | $\mathfrak{B}$ | © | ( | ほ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, 1865 | 0.000 | + 0.211 | -0.018 | + 0.034 | - 0.001 |
| St. Thomas . | November 18, 1865 | 0.000 | +0.131 | -0.015 | +0.034 | - 0.001 |
| Bahia $\cdot$. | December 30, 1865 | 0.000 | +0.113 | -0.020 | +0.034 | - 0.001 |
| Monte Video | January 24, 1866 | ...... | ...... | - |  | ...... |
| Sandy Point | February 10, 1866 | 0.000 | +0.080 | -0.025 | +0.034 | -0.001 |
| Valparaiso. | $\begin{array}{lr}\text { April } & 4,1866 \\ \text { April } & 29, \mathrm{I} 866\end{array}$ | 0.000 0.000 | +0.079 $+\quad 0.076$ | -0.017 | +0.034 | -0.001 |
| Callao . . | April 29, 1866 | 0.000 | +0.076 $+\quad 0.080$ | -0.011 | +0.034 +0.034 | -0.001 |
| Panama. | May June | 0.000 | +0.080 +0.080 | -0.005 | +0.034 +0.034 | -0.001 |
| $\xrightarrow[\text { San Francisco. }]{ }$ | $\begin{array}{rr}\text { June } & \text { I, } 1866 \\ \text { June } \\ \text { 23, }\end{array}$ | 0.000 0.000 | +0.080 $+\quad 0.119$ | -0.003 +0.001 | + $+\quad 0.034$ +0.034 | - 0.001 |
|  |  | 0.000 | +0.119 | + 0.001 | +0.034 | - 0.001 |

Coefficients of the Deviations of the After Azimuth Compass.

| STATION. | DATE. | 31 | $\mathfrak{F}$ | 5 | 5 | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . . . | November 1, 1865 | 0.000 | - 0.086 | +0.008 | $+0.112$ | 0.000 |
| St. Thomas . . . . | November 18, 1865 | 0.000 | -0.059 | +0.002 | +0.112 | 0.000 |
| Bahia $\dot{\text { a }}$. | December 30, 1865 | 0.000 | -0.063 | -0.003 | +0.112 | 0.000 |
| Monte Video . | January 24, 1866 | ... | ...... | ...... | ...... | ...... |
| Sandy Point | February 10, 1866 | 0.000 | -0.062 | -0.010 | +0.112 | 0.000 |
| Valparaiso. | April 4, 8666 | 0.000 | -0.065 | -0.002 | +0.112 | 0.000 |
| Callao . . | April 29, 866 | 0.000 | -0.061 | +0.003 | +0.112 | 0.000 |
| Panama. | May 20, 1866 | 0.000 | -0.059 | +0.009 | +0.112 | 0.000 |
| Acapulco . - | June ri, i866 | 0.000 | -0.059 | + 0.011 | +0.112 | 0.000 |
| San Francisco . . . . | June 23, I866 | -• | - | + | ...... | ...... |

Coefficients of the Deviations of the Forward Alidade Compass.


Coefficients of the Deviations of the Forward Binnacle Compass.

| STATION. | DATE. | $\mathfrak{H}$ | $\mathfrak{F}$ | $\bigcirc$ | 5 | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 | 0.000 | -0.099 | -0.032 | +0.037 | $+0.001$ |
| St. Thomas | November 18, 1865 | 0.000 | $-0.036$ | -0.020 | +0.037 | + 0.001 |
| Bahia . | December 30, 1865 | 0.000 | +0.015 | - 0.020 | +0.037 | + 0.001 |
| Monte Video | January 24, 1866 | o.oóo | +0.046 | -0.019 | +0.037 | +0.001 |
| Sandy Point | February 10, i866 | 0.000 | +0.084 | -0.016 | +0.037 | +0.001 |
| Valparaiso . | April 4, 1866 | 0.000 | +0.046 | -0.026 | +0.037 | +0.001 |
| Callao . | April 29, 1866 | 0.000 | + 0.015 | -0.029 | +0.037 | + 0.001 |
| Panama. | May 20, 1866 | 0.000 | -0.022 | -0.033 | +0.037 | +0.001 |
| ${ }_{\text {Acapulco }}$. ${ }^{\text {a }}$ | June I, 1866 | 0.000 | -0.033 | -0.035 | +0.037 | +0.001 |
| San Francisco. | June 23, 1866 | 0.000 | -0.083 | -0.056 | +0.037 | + 0.001 |

Coefficients of the Deviations of the Forward Ritchie Compass.

| STATION. | DATE. | 91 | $\mathfrak{9}$ | 5 | 5 | (3) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November r, r 865 | 0.000 | +0.032 | -0.056 | + 0.04 r | - 0.001 |
| St. Thomas . | November 18, 1865 | 0.000 | +0.032 | -0.032 | +0.041 | - 0.001 |
| Bahia . $\cdot$ | December 30, 1865 | 0.000 | + 0.048 | -0.026 | +0.041 | - 0.001 |
| Monte Video . | January 24, 1866 | 0.000 | + 0.057 | -0.022 | +0.041 | -0.001 |
| Sandy Point | February 10, 1866 | 0.000 | + 0.067 | -0.013 | $+0.041$ | -0.001 |
| Valparaiso. | April 4, 1866 | 0.000 | + 0.045 | -0.032 | +0.041 | - 0.001 |
| Callao . . | April 29, 1866 | 0.000 | + 0.028 | -0.041 | +0.041 | -0.001 |
| Panama. . . | May 20, 1866 | 0.000 | $\underline{+0.011}$ | -0.051 | +0.041 | - 0.001 |
| Acapulco . . | June I, i866 | 0.000 | +0.005 | -0.056 | +0.041 | -0.001 |
| San Francisco . | June 23, 1866 | 0.000 | - o.010 | -0.092 | $+0.041$ | - 0.001 |

Comparing these computed values with the values before founa directly from the observations, the following residuals are obtained:

Value of the Computed minus the Observed Coefficients of the Deviations of the Admiralty Standard Compass.


Value of the Computed minus the Observed Coefficients of the Deviations of the After Binnacle Compass.

| STATION. | DATE. | 31 | $\mathfrak{F}$ | $\bigcirc$ | 5 | © |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . . . | November 1, I865 |  | + 0.00I | + 0.001 | + 0.001 | - 0.001 |
| St. Thomas . . . . | November 18, 1865 |  | ...... |  |  | ...... |
| Bahia . . . . . | December 30, 1865 |  | $-0.004$ | +0.001 | +0.004 | -0.004 |
| Monte Video . . . . | January 24, 1866 |  | +0.002 | -0.009 | -0.001 | +0.010 |
| Sandy Point . . . . | February 10, 1866 |  | $-0.003$ | +0.014 | -0002 | -0.001 |
| Valparaiso . . . . . | April 4, 1866 |  | +0.011 | -0.001 | 0.000 | $-0.002$ |
| Callao . . . . . - | April 29, 1866 |  | -0.006 | -0.002 | -0.002 | $-0.004$ |
| Panama'. . . . . . | May 20, 1866 |  | $-0.003$ | -0.017 | -0.008 | $+0.003$ |
| Acapulco . . . . . | June I, I866 |  | $-0.003$ | $-0.007$ | -0.003 | + 0.004 |
| San Francisco. - . - | June 23, 1866 |  | +0.002 | +0.015 | + 0.006 | $-0.002$ |

Value of the Computed minus the Observed Coefficients of the Deviations of the After Ritchie Compass.

| STATION. | DATE. | 91 | $\mathfrak{F}$ | 5 | (3) | (3) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads . | November 1, 1865 |  | +0.011 | +0.012 | + 0.010 | +0.021 |
| St. Thomas . . | November 18, 1865 |  | -0.017 | -0.027 | -0.010 | + 0.008 |
| Bahia ${ }^{\text {a }}$. | December 30, 1865 |  | -0.008 | -0.003 | -0.008 | -0.003 |
| Monte Video . | January 24, 1866 |  | ...... | ...... | ...... | ...... |
| Sandy Point . | February 10, 1866 |  | $+0.009$ | $+0.035$ | +0.012 | -0.014 |
| Valparaiso. | April 4, 1866 |  | + 0.012 | -0.021 | -0.009 | -0.003 |
| Callao . | April 29, 1866 |  | -0.026 | -0.015 | $+0.002$ | -0.017 |
| Panama'. | May 20, 1866 |  | + 0.009 | -0.002 | +0.009 | $+0.026$ |
| Acapulco | June I, I866 |  | +0.002 | -0.024 | + 0.010 | -0.016 |
| San Francisco. | June 23, I866 |  | $+0.001$ | $+0.028$ | $-0.016$ | -0.004 |

Value of the Computed minus the Observed Coefficients of the Deviations of the After Azimuth Compass.


Value of the Computed minus the Observed Coefficients of the Deviations of the Forward Alidade Compass.

| STATION. | DATE. | $\mathfrak{H}$ | $\mathfrak{B}$ | 5 | (5) | 3 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 |  | +0.003 | + 0.006 | + 0.005 | - o.cor |
| St. Thomas | November 18, 1865 |  | -0.007 | - 0.005 | +0.002 | -0.006 |
| Bahia | December 30, 1865 |  | +0.002 | - 0.010 | +0.002 | -0.004 |
| Monte Video ${ }^{\circ}$. | January 24, 1866 |  | -0.005 | -0.002 | 0.000 | +0.004 |
| Sandy Point . | February 10, 1866 |  | +0.007 | +0.013 | -0.007 | +0.007 |
| Valparaiso. | April 4, 1866 |  | +0.003 | -0.007 | +0.005 | +0.002 |
| Callao | April 29, 1866 |  | -0.011 | +0.006 | $\underline{-1.002}$ | +0.003 |
| Panama. | May 20, 1866 |  | -0.010 | +0.001 | + 0.001 | +0.003 |
| Acapulco . | June 1, 1866 |  | +0.012 | $-0.014$ | $\underline{-0.009}$ | -0.002 |
| San Francisco. | June 23, 1866 |  | +0.002 | +0.007 | +0.007 | $-0.007$ |

Value of the Computed minus the Observed Coefficients of the Deviations of the Forward Binnacle Compass.

| STATION. | DATE. | 91 | $\mathfrak{B}$ | C | ( $)$ | 6 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 |  | 0.000 | + 0.013 | -0.007 | -0.006 |
| St. Thomas | November 18, 1865 |  | -0.002 | -0.016 | +0.002 | +0.003 |
| Bahia | December 30, r 865 |  | +0.007 | - o.010 | 0.000 | +0.004 |
| Monte Video | January 24, 1866 |  | -0.005 | -0.007 | +0.005 | +0.002 |
| Sandy Point | February 10, 1866 |  | -0.008 | + 0.022 | -0.002 | + 0.005 |
| Valparaiso . | April 4, 1866 |  | +0.015 | $\underline{-0.013}$ | +0.009 | + 0.004 |
| Callao . | April 29, 1866 |  | -0.005 |  | 0.000 | -0.005 |
| Panama. | May 20, 1866 |  | $-0.004$ | -0.006 | 0.000 | +0.007 |
| Acapulco . ${ }^{\text {S }}$ | June 1, 1866 |  | +0.003 | - 0.006 | - 0.009 | $-0.003$ |
| San Francisco. | June 23, 1866 |  | - 0.001 | +0.006 | +0.002 | -0.013 |

Value of the Computed minus the Observed Coefficients of the Deviations of the Forward Ritchie Compass.

| STATION. | DATE. | 91 | $\mathfrak{F}$ | $\bigcirc$ | (1) |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Hampton Roads | November 1, 1865 |  | + 0.009 | +0.007 | +0.003 | -0.007 |
| St. Thomas | November 18, 1865 |  | -0.004 | -0.010 | -0.016 | +0.007 |
| Bahia ${ }^{\text {a }}$ - | December 30, 1865 |  | -0.013 | +0.001 | -0.006 | +0.001 |
| Monte Video | January 24, 1866 |  | -0.009 | -0.022 | +0.001 | +0.007 |
| Sandy Point | February 10, 1866 |  | 0.000 | +0.035 | +0.002 | +0.005 |
| Valparaiso. | April 4, I866 |  | +0.022 | -0.006 | +0.004 | -0.009 |
| Callao : | April 29, 1866 |  | $-0.005$ | -0.007 | $\bigcirc 0.003$ | $\pm 0.003$ |
| Panama. | May 20, I866 |  | +0.007 | -0.018 | +0.003 | +0.003 |
| Acapulco . | June rer 1866 |  | -0.006 | - 0.018 | 0.000 +0.016 | + 0.008 |
| San Francisco. | June 23, 1866 |  | -0.005 | +0.025 | +0.016 | + 0.008 |

In the following table the columns headed $r_{\mathfrak{B}}, r_{⿷}, r_{\mathfrak{D}}, r_{\mathbb{E}}$, contain respectively the probable errors of a single observed value of $\mathfrak{B}, \mathfrak{C}, \mathfrak{D}$, and $\mathbb{E}$, for each compass, computed from the residuals just given. But as these residuals were got by subtracting the computed from the observed values of the coefficients, and as each observed value was found from a set of deviations observed on all the thirty-two points, it follows that the probable errors here given belong to the coefficients when they have been computed from a set of deviations observed on all the thirtytwo points. For convenience of reference we will designate these as the probable errors derived from all the observations of the cruise.

| Compass. | $r_{\mathfrak{B}}$ | ${ }^{\text {e }}$ | $r_{D}$ | ${ }_{\text {c }}$ | $\frac{r}{\sqrt{16}}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Admiralty Standard. | $\pm 0.0033$ | $\pm 0.0053$ | $\pm 0.0032$ | $\pm 0.0033$ | $\pm 0.0008$ |
| After Binnacle . . | $\pm 0.0036$ | $\pm 0.0069$ | $\pm 0.0026$ | $\pm 0.0028$ | $\pm 0.0018$ |
| After Ritchie . | $\pm 0.0090$ | $\pm 0.0153$ | $\pm 0.0072$ | $\pm 0.0106$ | $\pm 0.0031$ |
| After Azimuth | $\pm 0.0100$ | $\pm 0.0100$ | $\pm 0.0094$ | $\pm 0.0074$ | $\pm 0.0030$ |
| Forward Alidade | $\pm 0.0050$ | $\pm 0.0059$ | $\pm 0.0035$ | $\pm 0.0031$ | $\pm 0.0016$ |
| Forward Binnacle | $\pm 0.0046$ | $\pm 0.0084$ | $\pm 0.0036$ | $\pm 0.0043$ | $\pm 0.0024$ |
| Forward Ritchie . | $\pm 0.0070$ | $\pm 0.0127$ | $\pm 0.0056$ | $\pm 0.0047$ | $\pm 0.0032$ |
| Means | $\pm 0.006 \mathrm{r}$ | $\pm 0.0092$ | $\pm 0.005^{\circ}$ | $\pm 0.005^{2}$ | $\pm 0.0023$ |

But we have before found the probable errors of $B_{1}, C_{1}, D_{1}$, and $E_{1}$, when computed from observations made at a single station on each of the thirty-two points, by a totally different process, namely, from the thirty-two observed deviations the values of $A_{1}, B_{1}, C_{1}, D_{1}$, and $E_{1}$, were computed; next, with the values of $A_{1}, B_{1}$, $C_{1}, D_{1}$, and $E_{1}$, thus found, the deviations were computed for each point; then, comparing these computed values of the deviation with the observed values, a series of residuals were obtained from which the probable errors in question (which are given in the table on page 185) were easily got. These we will designate as the probable errors obtained from observations at a single station; and it will be remembered that it was shown that, no matter what their numerical values might be, the probable errors of $B_{1}, C_{1}, D_{1}$, and $E_{1}$ must all be equal to each other. Although the difference between the probable errors of $B_{1}, C_{1}, D_{1}, E_{1}$, and those of $\mathfrak{B}, \mathfrak{C}, \mathfrak{D}, \mathfrak{\bigotimes}$, can never be great, yet, in general, it would not be rigorously correct to assume that they are equal to each other. However, in the case of the compasses under discussion we will make this assumption, for by so doing no error greater than the uncertainty of the probable errors themselves will be introduced. In order to facilitate the comparison of the two sets of probable errors, those of $B_{1}$, $C_{1}, D_{1}, E_{1}$ are given in the table above, in the column headed $\frac{r}{\sqrt{16}}$. This column is identical with the column headed in the same manner in the table on page 185 , except that the quantities are here expressed in parts of radius instead of minutes of arc.

Now, comparing the probable errors derived from all the observations of the cruise with those derived from observations at any single station, we see that, taking the mean of the results for all the compasses, $r_{\Phi}$ and $r_{\mathbb{E}}$ are almost identical, as they should be, but they are each more than twice as great as $\frac{\hat{r}}{\sqrt{16}}$. On the other hand,
$r_{\mathfrak{B}}$ and $r_{\mathbb{C}}$ are neither equal to each other, nor yet to $r_{\otimes}$ and $r_{\mathscr{E}}$, but are, the one nearly three, and the other four, times as great as $\frac{r}{\sqrt{16}}$. Assuming the theory employed in this discussion to be correct, we should have expected to find $r_{\mathfrak{B}}, r_{\mathbb{E}}$, $r_{\sqrt{ }}, r_{\mathbb{E}}$ sensibly equal to each other, and all sensibly equal to $\frac{r}{\sqrt{ } 16}$. Such, however, is not the case; and, as the results for each compass all tend in precisely the same direction as the mean result, a doubt naturally arises whether or not the theory really represents the semi-circular deviation as accurately as it does the quadrantal. As this doubt is founded upon observations which may possibly have been affected by some unknown cause of constant error-as they were all made on a single vessel during a single cruise-perhaps it would not be well to insist upon it too strongly; but at all events, it shows the necessity for further investigation of the subject, and especially the great want of more observations.

The probable errors of the coefficients $\mathfrak{B}, \mathfrak{C}, \mathfrak{D}, \mathfrak{C}$, for each compass, when computed from the values of $A_{1}, \frac{c}{\lambda}, \frac{P}{\lambda}, \frac{\Delta P}{\lambda}, \frac{f}{\lambda}, \frac{Q}{\lambda}, \frac{\Delta Q}{\lambda}, \mathfrak{D}$, and $\mathfrak{E}$, given in the table on page 193, are as follows:


The following table shows, for each compass, the place at which the maximum value of its deviation, $\delta$, was the greatest, together with the point on which that maximum value occurred, and its amount. Also, the place at which the maximum value of its deviation was the least, together with the point on which that maximum occurred, and its amount. These deviations are given on the compass points, and in computing them the true $A$ was used.



The following table shows, for each compass, the maximum change, $\Delta \delta$, in its deviation, which occurred on any single point, together with the azimuth at which, and the places between which that change occurred.


In order to show the difference between the values of the deviation computed from observations made at a single station, and those computed from all the observations of the cruise, or, in other words, the difference between the theory and the observations, let $\delta$ be the deviation of a compass on any point, $\zeta$, at a given station, as computed from values of $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, derived from all the observations of that compass made during the cruise; and also let $\delta^{\prime}$ be the deviation of the same compass, on the same point, at the same station, as computed from values of $A_{1}$, $B_{1}, C_{1}, D_{1}, E_{1}$, derived from observations of that compass made on each of the thirty-two points at the station in question. Then the following table shows, for each compass, the maximum value attained by $\delta-\delta^{\prime}$ during the cruise, together with the point on which, and the station at which, that maximum occurred.


As the After Azimuth Compass was a very poor instrument, the descrepancy between theory and observation in the case of its deviations is not surprising. In the case of all the other compasses, except perhaps the Forward and After Ritchie, the agreement of the observed and computed values of the deviations is much more satisfactory; and indeed the differences between them are so small as to be of very little consequence for the ordinary purposes of navigation; still, viewed from a purely scientific stand-point, they are larger than might have been expected.

The hard and soft iron forces involved in the production of the semi-circular deviation were next examined in order to ascertain whether or not their relations to each other were such as to render it possible, in the case of a vessel swung for the first time, to predict from the observed deviations of her standard compass what the deviations would be at any other place. The coefficients of the semi-circular deviation are $\mathfrak{B}$ and $\mathfrak{C}$, and the components of the hard iron force involved in their production are $\frac{P}{\lambda}$ and $\frac{Q}{\lambda}$; while the components of the soft iron force are $\frac{c}{\lambda}$ and $\frac{f}{\lambda}$. As these components act at right angles to each other, the total hard iron force will be

$$
\sqrt{\frac{P^{2}}{\lambda^{2}}+\frac{Q^{2}}{\lambda^{2}}}
$$

and if we let $\alpha$ represent the direction in which it acts, measured from the ship's head toward the right hand, we have

$$
\tan \alpha=\frac{\frac{Q}{\lambda}}{\frac{P}{\lambda}}
$$

In the same way the total soft iron force will be

$$
\sqrt{\frac{c^{2}}{\lambda^{2}}+\frac{f^{2}}{\lambda^{2}}}
$$

and to determine its direction we have

$$
\tan \alpha^{\prime}=\frac{\frac{f}{\lambda}}{\frac{c}{\lambda}}
$$

By means of these formule the following table was computed. It shows the amount and direction of the hard and soft iron forces acting on each compass on November 1, 1865, and June 23, 1866.


The following table shows the change, in amount and direction, of the hard iron force between November 1, 1865, and June 23, 1866; the ratio of the hard to the soft iron force on each of these dates; and also the mean ratio of the same forces.

| Compass. | Change of Hard Iron Force. |  | Ratio of Hard to Soft Iron Force. |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  | Amount. | Direction. | Nov. 1, 1865. | June 23, 8666. | Mean. |
| Admiralty Standard. | -0.234 | - $122^{\circ} .8$ | 19.2 | $9 \cdot 4$ | 143 |
| After Binnacle | -0.025 | - 7.2 | 68.8 | 66. 1 | 67.4 |
| After Ritchie . | -0.299 | + 5.0 | 42.1 | 26.0 | 34.0 |
| After Azimuth. | +0.074 | - 12.9 | 52.6 | 62.8 | 57.7 |
| Forward Alidade | +0.071 | $-10.3$ | 6.6 | 11.0 | 8.8 |
| Forward Binnacle | +0.095 | --51.8 | $3 \cdot 3$ | $5 \cdot 3$ | 4.3 |
| Forward Ritchie | +0.011 | $-58.1$ | 17.1 | 17.6 | 17.3 |

An examination of the last two tables shows that during the whole cruise the hard iron force was changing in a very remarkable manner, both in amount and direction. In the case of the three compasses mounted above the forward turret, the force was increasing: while in the case of those mounted above the after turret, it was decreasing. In other words, there seems to have been a transfer of hard iron force from aft forward. Now, looking at the change in direction of the force, we see that in every case, excepting only that of the After Ritchie, it took place in such a manner as to correspond to a rotation from right to left. Further, the ratio of the hard to the soft iron force was slowly varying at each compass; and for the different compasses it ranged between 4.3 and 6\%.4. Finally, there was not a single compass on board at which the direction of the hard and soft iron force coincided; from which it follows that in no case was the ratio of the hard and soft iron forces the same in the coefficient $\mathfrak{B}$ as it was in the coefficient $\mathbb{C}$. Under these circumstances we are forced to conclude that, so far as can be judged from the observations here given, in the case of a vessel swung for the first time it is impossible to make any reliable estimate of the ratio of the hard to the soft iron force in the coefficients $\mathfrak{B}$ and $\mathfrak{C}$; and, therefore, it is also impossible to make any reliable estimate as to what changes her deviations will undergo upon a change of magnetic latitude. As a further proof of this, we see that the After Azimuth Compass, with a maximum deviation of $10^{\circ} 5^{\prime}$, changed its deviation during the cruise by only $1^{\circ} 43^{\prime}$, that is, by about one-sixth of its whole amount; while the Forward Binnacle Compass, with a maximum deviation of only $7^{\circ} 43^{\prime}$ changed its deviation during the cruise by $9^{\circ} 42^{\prime}$, that is, by about one and a quarter times its whole amount.
In the beginning of this section it was stated that, at the positions occupied by the Admiralty Standard and After Azimuth Compasses, observations of deflection and dip were made in order to determine the absolute magnetic force; and the details of the method followed in taking these observations were explained. We will now proceed to reduce and discuss the observations themselves, and for that purpose the first thing necessary to be known is the magnetic moment of the deflecting magnets. For its determination we have the observations recorded in the following table, which were all made on shore. The first and second columns
of the table give the place where, and the date when, each observation was made. The third and fourth columns give respectively the observed deflections when the north ends of the deflecting magnets were directed towards the west and towards the east; the distance of their centres from the centre of the compass needle being in both cases eleven inches. The fifth column gives the mean of the four observed deflections recorded in the third and fourth columns. The sixth, seventh, and eighth columns contain, in precisely the same manner, the observed deflections, and their mean, when the centres of the deflecting magnets were at a distance of fifteen inches from the centre of the compass needle. Now, let $r$ be the distance, expressed in feet, between the centres of the deflecting magnets and the centre of the compass ncedle; $u$, the observed angle of deflection given for each value of $r$ in the column headed "mean"; $m$, the combined magnetic moment of the two deflecting magnets; and $H$, the earth's horizontal force at the place where the observation was made, taken from the table on page 61. Then we shall have

$$
\frac{1}{2} r^{3} \tan u=\frac{m}{\bar{H}}
$$

and the ninth column contains the mean of the two values of $\log . \frac{m}{H}$ computed respectively from the angles of deflection observed with $r=11$ inches $=0.917$ foot, and $r=15$ inches $=1.250$ feet. The tenth column contains the value of $\log . m$, found by adding to $\log . \frac{m}{H}$ the known value of $\log . H$.

| Station. | Date. | Deflections. |  |  |  |  |  | Log. $\frac{m}{H}$. | Log. $m$. |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | $r=11$ inches. |  |  | $r=15$ inches. |  |  |  |  |
|  |  | West. | East. | Mean. | West. | East. | Mean. |  |  |
| Gosport. . . . . | Oct. 30, 1865 | $19^{\circ} 30^{\prime}$ | $22^{\circ} 40^{\prime}$ |  | $14^{\circ} 33^{\prime}$ | $17^{\circ} 30^{\prime}$ |  |  |  |
| St. Thomas |  | 19 o | $22 \quad 20$ | $20^{\circ} 52!$ | $14 \quad 20$ | 1740 | $\because 6^{\circ} \quad 9^{\prime}$ | 9.1617 | 9.8344 |
|  | Nov. 13, 1865 | $\begin{array}{ll}15 & 20 \\ 15 & 30\end{array}$ | $\begin{array}{ll}14 & 50 \\ 14 & 40\end{array}$ |  | $\begin{array}{ll}4 & 20 \\ 4 & 30\end{array}$ | 640 640 |  | 8.9961 | 9.8251 |
| Salute Islands . | Nov. 28, 1865 | 14 <br> 15 | 150 |  | 5 | 5 20 |  |  |  |
| Bahia. . . . . | Dec. 27, 1865 | 1435 | $15 \quad 5$ | $14 \quad 49$ |  | 5 20 | $5 \quad 14$ | 8.9799 | 9.8079 |
|  |  | 15 15 16 | 16 |  |  | $5{ }_{5} 30$ |  |  |  |
| Rio Janeiro | Jan. 6, 1866 | $\begin{array}{lr}16 & 40 \\ 17 & 0\end{array}$ | $\begin{array}{cc}16 & 10 \\ 17 & \text { o }\end{array}$ | 16 ıo | $\begin{array}{ll}5 & 40 \\ 6 & 40\end{array}$ | $\begin{array}{ll}5 & 30 \\ 6 & 0\end{array}$ | 542 | 9.0184 | 9.8108 |
|  | Jan. 18, 1866 | 17 o | 17 ı | $17 \quad 2$ | 6 o | 6 o | 6 וо | 9.0476 | 9.8216 |
| Monte Video |  | 1640 | $16 \quad 40$ |  | 620 | 530 |  |  |  |
| Sandy Point | Feb. 7, 1866 | 170 | 1640 | $16 \quad 45$ | 6 Iо | 530 | $5 \quad 52$ | 9.0328 | 9.8130 |
|  |  | $16 \quad 30$ | $16 \quad 20$ |  | 540 | 640 |  |  |  |
| Valparaiso . | March 2, 1866 | 1640 | 1620 | $16 \quad 27$ | 6 o | 630 | $6 \quad 12$ | 9.0408 | 9.8270 |
|  |  | $17 \quad 0$ | $15 \quad 0$ |  | $\begin{array}{ll}7 & 20 \\ 7 & 30\end{array}$ | $\begin{array}{ll}5 & 0 \\ 5 & 0\end{array}$ | $6 \quad 12$ | 9.0320 | 9.8326 |
| Valparaiso . | April 7, 1866 | 1440 | $\begin{array}{ll}17 & 40\end{array}$ |  | 430 | 730 |  |  |  |
|  | April 26, 1866 | $14 \quad 30$ | $17 \quad 30$ | 16 | 420 |  | 6 o | 9.0284 | 9.8290 |
| Callao |  | $14 \quad 30$ | 1430 |  |  | 5 10 |  |  |  |
|  | May 14, 1866 | 1430 | 1430 | $14 \quad 30$ |  |  | 5-18 | 8.9777 | 9.8222 |
| Panama |  | $\begin{array}{ll}12 & 50 \\ 13 & 10\end{array}$ | $\begin{array}{lll}13 & 30 \\ 13 & 30\end{array}$ |  |  | $\begin{array}{cc}5 & 20 \\ 5 & 0\end{array}$ |  | 8.9387 | 9.8195 |
| Acapulco | May 30, 1866 | $\begin{array}{ll}13 & 10 \\ 12 & 30\end{array}$ | $\begin{array}{lll}13 & 30 \\ \text { I2 } & 20\end{array}$ |  |  | 430 |  |  |  |
|  |  | 1240 | 1210 | $12 \quad 25$ |  | 440 | 450 | 8.9227 | 9.8107 |
| San Francisco | June 26, 1866 | 1740 | 170 |  | 7 \% | 6 <br> 6 |  |  |  |
|  |  |  | 1640 |  |  |  |  | 9.0698 | 9.8208 |

* In this observation $r=12$ inches.

The observed values of log. $m$ show no trace whatever of any change depending upon the time, and therefore the indiscriminate mean of them all has been taken as the truth, and we have

$$
\text { Log. } m=9.8211 \pm 0.0016
$$

The probable error of a single observed value of log. $m$ is $\pm 0.0058$.
The following table contains all the observations which were made at the position occupied by the Admiralty Standard Compass on board the Monadnock, for the determination of absolute force. The first nine columns contain quantities precisely similar to those in the columns headed in the same manner in the table last given. The column headed "Log. $H^{\prime}$ " gives the logarithm of the combined horizontal force of the earth and ship, obtained by subtracting log. $\frac{m}{H^{\prime}}$ from the value of log. $m$ given above. The column " $\theta^{\prime}$ " contains the dip, which was observed immediately after the deflections. The column "Log. $Z^{\prime \prime}$ " contains the logarithm of the combined vertical force of the earth and ship, computed from the quantities in the tenth and eleventh columns by the formula $Z^{\prime}=H^{\prime} \tan \theta^{\prime}$. The columns "Log. $\frac{H^{\prime}}{H}$," and "Log. $\frac{Z}{Z}$ ", explain themselves when it is stated that $H$ represents the horizontal force of the earth; $H^{\prime}$ the combined horizontal force of the earth and ship; $Z$ the earth's vertical force; and $Z^{\prime}$ the combined vertical force of the earth and ship. 'The column " $\zeta$ "" contains the azimuth of the ship's head as read off from the compass card at the time the deflections were observed; and the column " $\zeta$ " contains the same azimuth, counted from the true magnetic north.
Admiralty Standard Compass.


The following table contains, in precisely the same manner, all the observations which were made for the determination of absolute force at the position occupied by the After Azimuth Compass on board the Monadnock.
After Azimuth Compass.


From the data already given, the value of $\lambda$ was next computed by means of the formulæ

$$
\begin{aligned}
\sin \delta & =\frac{1}{1-\mathfrak{D} \cos 2 \zeta^{\prime}}\left[\mathfrak{Y}+\mathfrak{B} \sin \zeta^{\prime}+\mathfrak{C} \cos \zeta^{\prime}+\mathfrak{D} \sin 2 \zeta^{\prime}+\mathfrak{C} \cos 2 \zeta^{\prime}\right] \\
\lambda & =\frac{H^{\prime}}{H} \times \frac{\sin \delta}{\mathfrak{A}+\mathfrak{B} \sin \zeta+\mathfrak{C} \cos \zeta+\mathfrak{D} \sin 2 \zeta+\mathfrak{C} \cos 2 \zeta}
\end{aligned}
$$

The individual results obtained from the observed values of $\frac{H^{\prime}}{H}$ are as follows:


Taking the means, for the Admiralty Standard Compass, we have finally

$$
\lambda=0.924 \pm 0.0036
$$

and the probable error of a single observed value of $\lambda$ is $\pm 0.013$. For the After Azimuth compass we have finally

$$
\lambda=0.864 \pm 0.0107
$$

and the probable error of a single observed value of $\lambda$ is $\pm 0.034$.
In order to determine these coefficients which depend upon the value of $\frac{Z^{\prime}}{Z}$, we have equation (6 a), which is

$$
0=1-\frac{Z^{\prime}}{Z}+g \times \frac{\cos \zeta}{\tan \theta}-h \times \frac{\sin \zeta}{\tan \theta}+\dot{k}+R \times \frac{1}{Z}
$$

But as $R$ is liable to a slow change, a term depending upon the time is introduced, and then we get

$$
\begin{equation*}
0=1-\frac{Z^{\prime}}{Z}+g \times \frac{\cos \zeta}{\tan \theta}-h \times \frac{\sin \zeta}{\tan \theta}+k+R \times \frac{1}{Z}+\Delta R \times \frac{t}{Z} \tag{6~b}
\end{equation*}
$$

where $\Delta R$ is the daily change in the value of $R$, and $t$ is the time in days, counted from November 1, 1865. Each observed value of $\frac{Z^{\prime}}{Z}$ furnishes an equation of condition of the same form as ( 6 b ), and from all the equations of condition thus obtained the most probable values of $g, h, k, R$, and $\Delta R$, can be found by the method of least squares.

The following are the equations of condition, formed in the manner just explained, for the Admiralty Standard Compass.

| Absolute Term. | $g$ | $h$ | $k$ | $R$ | $\Delta R$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-0.160$ | + 0.008 | - 1.448 | $+1.000$ | $+0.215$ | + 6.24 |
| $\bigcirc$ - - 0.899 | + 10.23 | -8.007 | +1.000 | + 2.097 | + 125.8 |
| $0 .+0.320$ | 4.779 | $-0.376$ | $+1.000$ | $-0.806$ | - 51.61 |
| $0-\mathrm{O}-\mathrm{o.141}$ | + 4.791 | -0.164 | $+1.000$ | -0.806 | - 51.6I |
| 0--0.108 | + 1.561 | +0.558 | $+1.000$ | -0.275 | 23.10 |
| $0=-0.129$ | $+0.545$ | -0.442 | +1.000 | -0.115 | - II.48 |
| $0=-0.149$ | + 1.322 | -0.485 | $+1.000$ | -0.223 | - 30.76 |
| $0=-0.016$ | 1.401 | 0.140 | $+1.000$ | -0.223 | - 34.32 |
| $0=-0.068$ | $+8.822$ | -0.033 | $+1.000$ | - 1.263 | - 227.3 |
| $0=-0.175$ | + 1.132 | +1.136 | $+1.000$ | +0.211 | + $+\quad 4.59$ |
| $0=$-0.118 | -1.046 | -0.580 | $+1.000$ | $+0.155$ | + 32.66 |
| $0=-0.058$ | -. 497 | -0.165 | +1.000 | +0.093 | + 21.74 |

From these equations of condition, the following normal equations have been obtained by the method of least squares.

| Absolute Term. | $g$ | h | $k$ | $R$ | $100 \Delta R$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-12.462$ | $+237.337$ |  |  |  |  |
| $0=+7.286$ | - 79.068 | + 68.794 |  |  |  |
| $0=$ 1.701 | + 20.688 | - 10.147 | + 12.000 |  |  |
| $0=$ - 1.957 | + 9.858 | - 16.45 I | -0.941 | $+7.605$ |  |
| $0=-1.112$ | $7 \cdot{ }^{\text {I }} 3$ | - 9.444 | - 2.022 | $+6.735$ | $+7.892$ |

Solving, we find

$$
\begin{aligned}
& g=+0.04070 \\
& h=+0.00504
\end{aligned}
$$

$$
\begin{array}{r}
k=+0.1006 \\
R=+0.1665 \\
100 \Delta R=+0.0694
\end{array}
$$

Substituting these results in the equations of condition, we find that the probable error of a single observed value of $\frac{Z^{\prime}}{Z}$ is $\pm 0.024$, and the probable error of a computed value of $\frac{Z^{\prime}}{Z}$ is $\pm 0.007$.

In a precisely similar manner, from the values of $\frac{Z^{\prime}}{Z}$ observed at the position of the After Azimuth Compass, we obtain the following equations of condition.

| Absolute Term. | $g^{\circ}$ | $h$ | ¢ | $R$ | $\Delta R$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0=+0.501$ | $-4.790$ | +0.173 | $+1.000$ | -0.806 | 5 I .61 |
| $0=-0.625$ | + 4.663 | -1.114 | +1.000 | -0.806 | - 51.61 |
| $0=-0.115$ | + 0.979 | +1.338 | $+1.000$ | -0.275 | -- 23.10 |
| $0=+0.059$ | +0.358 | -0.603 | $+1.000$ | -0.115 | - 11.48 |
| $0=-0.101$ | +1.370 | -0.324 | $+1.000$ | -0.223 | - 30.76 |
| $0=+0.152$ | - 1.393 | -0.205 | +1.000 | -0.223 | - 34.32 |
| $0=-0.602$ | +8.823 | +0.031 | +1.000 | - 1.263 | - 227.3 |
| $\bigcirc=-0.165$ | +1.250 | $+1.006$ | $+1.000$ | + 0.21 I | + 41.59 |
| $0=-0.049$ | +0.314 | +1.154 | $+1.000$ | $+0.155$ | + 32.66 |
| $0=+0.094$ | -0.257 | -0.456 | $+1.000$ | +0.093 | + 21.74 |

And the resulting normal equations are -

| Absolute Term. | $g$ | $h$ | $k$ | $R$ | $100 \Delta R$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $0=-11.313$ | + 129.164 |  |  |  |  |
| $0=+0.311$ | - 3.078 | $+6.125$ |  |  |  |
| $0=-0.85 \mathrm{r}$ | + 11.317 | $+1.000$ | + 10.000 |  |  |
| $0=+0.840$ | - 11.053 | + 0.888 | - 3.253 | +3.161 |  |
| $0=+1.367$ | - 19.634 | + 1.042 | - 3.342 | + 4.084 | $+6.305$ |

Solving, we find

$$
\begin{array}{rr}
g=+0.11398 & k=-0.0509 \\
h=+0.00981 & R=-0.3918 \\
& 100 \Delta R=+0.3634
\end{array}
$$

Substituting these results in the equations of condition, the probable error of a single observed value of $\frac{Z^{\prime}}{Z}$ comes out $\pm 0.030$, and the probable error of a computed value of $\frac{Z^{\prime}}{Z}$ comes out $\pm 0.010$.

For the Admiralty Standard Compass we found $\mathfrak{N}=0.000, \mathfrak{D}=+0.017$, and $\mathfrak{E}=-0.001$. We have also

$$
\begin{aligned}
& a=\lambda(1+\mathfrak{D})-1 \\
& e=\lambda(1-\mathfrak{D})-1 \\
& b=\lambda(\mathfrak{C}-\mathfrak{A}) \\
& d=\lambda(\mathfrak{C}+\mathfrak{2})
\end{aligned}
$$

Hence

$$
\begin{array}{ll}
a=-0.0605 & e=-0.0917 \\
b=-0.0008 & d=-0.0008
\end{array}
$$

For the After Azimuth Compass we found $\mathfrak{H}=0.000$, $\mathfrak{D}=+0.112$, and EF $=0.000$. Hence, in the same manner,

$$
\begin{array}{ll}
a=-0.0396 & e=-0.2324 \\
b=0.0000 & d=0.0000
\end{array}
$$

Collecting our results, we have the following final values of the coefficients of the
Admiralty Standard Compass.
$\mathfrak{A l}=0.000$
$\mathfrak{B}=+0.0240 \tan \theta+0.460 \frac{\mathrm{r}}{H}-0.00102 \frac{t}{H} \pm 0.001$
$\Subset=-0.0016 \tan \theta+0.006 \frac{\mathrm{I}}{H}-0.00023 \frac{t}{H} \pm 0.002$
$D=+0.017 \pm 0.001$
(2) $=-0.001 \pm 0.001$
${ }^{\prime} Z^{\prime}{ }^{\prime}=\mathrm{I}+0.0407 \frac{\cos \zeta}{\tan \theta}-0.0050 \frac{\sin \zeta}{\tan \theta}+0.1006+0.1665 \frac{1}{Z}+0.000694 \frac{t}{Z} \pm 0.007$
27 December, 1872.

| $\lambda=+0.924 \pm 0.004$ |  |  |
| :--- | :---: | :---: |
| $\frac{c}{\lambda}=+0.0240$ | $c=+0.0221$ |  |
| $\frac{P}{\lambda}=+0.460$ | $P=+0.425$ | $b=-0.0008$ |
| $\frac{\Delta P}{\lambda}=-0.00102$ | $\Delta P=+0.00094$ | $d=-0.0008$ |
| $\frac{f}{\lambda}=-0.0016$ | $f=-0.0015$ | $e=-0.0917$ |
| $\frac{Q}{\lambda}=+0.006$ | $Q=+0.006$ | $g=+0.0407$ |
| $\frac{\Delta Q}{\lambda}=-0.00023$ | $\Delta Q=-0.00021$ | $h=+0.0050$ |
|  | $a=-0.0605$ | $k=+0.1006$ |
|  |  | $R=+0.166$ |
|  | $\Delta R=+0.00069$ |  |

Hence, the general equations for the determination of the deviations of this compass are

$$
\begin{aligned}
X^{\prime} & =X-0.0605 X-0.0008 Y+0.0221 Z+0.425-0.00094 t \\
Y^{\prime} & =Y-0.0008 X-0.0917 Y-0.0015 Z+0.006-0.00021 t \\
Z^{\prime} & =Z+0.0407 X+0.0050 Y+0.1006 Z+0.166+0.00069 t
\end{aligned}
$$

The following are the final values of the coefficients of the
After Azimuth Compass.
$\mathfrak{A}=0.000$
$\mathfrak{B}=-0.0026 \tan \theta-0.373 \frac{\mathrm{x}}{H}-0.00032 \frac{t}{H} \pm 0.004$
$\Subset=+0.0066 \tan \theta-0.044 \frac{\mathbf{1}}{H}+0.00039 \frac{t}{H} \pm 0.004$
(D) $=+0.112 \pm 0.003$
$\mathfrak{C}=0.000 \pm 0.003$
$\frac{Z^{\prime}}{Z}=1+0.1140 \frac{\cos \zeta}{\tan \theta}-0.0098 \frac{\sin \zeta}{\tan \theta}-0.0509-0.3918 \frac{1}{Z}+0.00363 \cdot \frac{t}{Z} \pm 0.010$
$\lambda=+0.864 \pm 0.011$

| $\frac{c}{\lambda}=-0.0026$ | $c=-0.0022$ | $b=0.0000$ |
| :--- | :---: | :---: |
| $\frac{P}{\lambda}=-0.373$ | $P=-0.322$ | $d=0.0000$ |
| $\frac{\Delta P}{\lambda}=-0.00032$ | $\Delta P=-0.00027$ | $e=-0.2324$ |
| $\frac{f}{\lambda}=+0.0066$ | $f=+0.0058$ | $g=+0.1140$ |
| $\frac{Q}{\lambda}=-0.044$ | $Q=-0.038$ | $h=+0.0098$ |
| $\frac{\Delta Q}{\lambda}=+0.00039$ | $\Delta Q=+0.00034$ |  |
|  | $a=-0.0396$ | $k=-0.0509$ |
| $R=-0.392$ |  |  |
|  |  | $\Delta R=+0.00363$ |

Hence, the general equations for the determination of the deviations of this compass are

$$
\begin{aligned}
X^{\prime} & =X-0.0396 X-0.0000 Y-0.0022 Z-0.322-0.00027 t \\
Y^{\prime} & =Y-0.0000 X-0.2324 Y-0.0058 Z-0.038+0.00034 t \\
Z^{\prime} & =Z+0.1140 X+0.0098 Y-0.0509 Z-0.392+0.00363 t
\end{aligned}
$$

The constants $P, Q, R$, are the resolved values of the hard iron magnetism of the ship; and in order to show as clearly as possible how it varied during the cruise, at the positions occupied by the two compasses under discussion, the following table is appended. The columns headed " $F$ " contain the values of the total hard iron force, computed by means of the formula

$$
F=\sqrt{P^{2}+Q^{2}+R^{2}}
$$

| Date. | Admiralty Standard Compass. |  |  |  | After Azimuth Compass. |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $P$. | $Q$. | $R$. | $F$. | $P$. | $Q$. | $R$. | $F$. |
| November 1, 1865 | +0.425 | $+0.006$ | +0.166 | 0.456 | -0.322 | -0.038 | -0.392 | 0.509 |
| June 23, 1866 | +0.205 | - 0.043 | +0.327 | 0.388 | $-0.385$ | +0.042 | +0.457 | 0.599 |

Thus it appears that in the interval between November 1, 1865, and June 23, 1866, the total hard iron force had decreased fifteen per centum at the position of the Admiralty Standard Compass, while it had increased eighteen per centum at the position of the After Azimuth Compass; and in both cases the changes in the direction of the force were very great. On the whole, the so-called permanent and sub-permanent magnetism of the Monadnock seem to have been in a very unstable condition.

There were some places where observations of the deviations of the compasses were obtained on a number of points less than thirty-two, because the ship could not be made to swing completely around. In order to deduce from these observations the corresponding values of the coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, we remark that each observed deviation furnishes an equation of condition of the form

$$
0=-\delta+A_{1}+B_{1} \sin \zeta+C_{1} \cos \zeta+D_{1} \sin 2 \zeta+E_{1} \cos 2 \zeta
$$

and from all the equations thus obtained the values of the coefficients must be found by the method of least squares. As all the compasses were observed simultaneously; the deviations at each place are given on the same points in the case of each compass. Hence, although the absolute terms in the equations of condition will be different, the numerical coefficients of the unknown quantities $A_{1}, B_{1}, C_{1}$, $D_{1}, E_{1}$, will be identical for all the compasses at any one station. Advantage has been taken of this circumstance in forming the following table, which gives the equations of condition for all the compasses at Ceara. The absolute terms of the equations of condition belonging to any compass will be found in the column headed with the name of that compass, while the coefficients of the remaining terms of the equations will be found in the columns headed $A_{1}, B_{1}, C_{1}, D, E_{1}$. For example, the first equation of condition for the Admiralty Standard Compass is

$$
0=-170+A_{1}+0.195 B_{1}+0.981 C_{1}+0.383 D_{1}+0.924 E_{1}
$$

In the same way，the first equation of condition for the After Binnacle Compass is

$$
0=-220+A_{1}+0.195 B_{1}+0.981 C_{1}+0.383 D_{1}+0.924 E_{1}
$$

Equations of Condition at Ceara．

| Absolute Terms． |  |  |  |  |  | Coefficients of the Unknown Quantities． |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  | 家忽范 |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | $A_{1}$ | $B_{1}$ | $C_{1}$ | $D_{1}$ | $E_{1}$ |
| －170 | －220＇ | －820＇ | －180＇ | －110＇ | － $430^{\prime}$ | ＋1．000 | ＋0．195 | ＋0．981 | ＋0．383 | ＋0．924 |
| － 210 -260 | 二 ${ }^{310}$ | －820 | 二 270 | － 110 | － 520 | ＋1．000 | ＋＋ <br> + <br> +0.383 | +0.982 <br> +0.924 | ＋0．707 | ＋ +0.707 $+\quad 0.38$ |
| － 350 | 二 ${ }^{390}$ | 二 820 | － 288 | 二 110 | 二600 | ＋1．000 | ＋ | $\begin{array}{r}\text { a } \\ +0.831 \\ +0.707 \\ \hline\end{array}$ | $\begin{array}{r}\text {＋} \\ +0.924 \\ +1.000 \\ \hline\end{array}$ | ＋ $\begin{array}{r}0.383 \\ 0.000\end{array}$ |
| － 340 | －420 | － 990 | －211 | － 130 | －380 | ＋1．000 | ＋0．831 | ＋0．556 | ＋0．924 | －0．383 |
| －330 | 二410 | － 1140 | － 200 | － 110 | －300 | ＋ 1.000 | ＋0．924 | ＋0．383 | $\begin{array}{r}+1.904 \\ +0.707 \\ \hline\end{array}$ | －0．707 |
| －310 -230 | 二 ${ }^{410}$ | － 1020 | － 130 | －${ }^{40}$ | －420 | ＋1．000 | ＋0．981 | ＋o．195 | ＋0．383 | －0．924 |
| － 230 | －${ }^{260}$ | －850 | － 110 | ＋ 40 | － 170 | ＋1．000 | ＋1．000 | －0．000 | 0．000 | － 1.000 |
| －${ }^{217}$ | 二 ${ }^{240}{ }^{240}$ | － 690 | － 110 | a +130 +140 | 二 ${ }^{40}$ | ＋1．000 +1.000 | ＋ | － $\begin{aligned} & \text {－0．195 } \\ & -0.383\end{aligned}$ | － $\begin{aligned} & \text {－0．383 } \\ & -0.707\end{aligned}$ | 二－0．924 |

From these equations of condition five normal equations were obtained for each compass by the method of least squares；but on attempting to solve them the numerical coefficients of $D_{1}$ and $E_{1}$ came out so small that no confidence could be placed in the resulting values of these quantities；and moreover，the uncertainty of them vitiated the values of $A_{1}, B_{1}$ ，and $C_{1}$ ．It was therefore considered best to reject the normal equations in $D_{1}$ and $E_{1}$ ，and to employ in their stead the equations

$$
\begin{aligned}
& 0=-\mathfrak{D}+\mathrm{D}_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}{ }^{2}\right) \\
& 0=-\mathbb{E}+\mathrm{E}_{1}+B_{1} C_{1}+A_{1} D_{1}
\end{aligned}
$$

using for $\mathfrak{D}$ and $\mathfrak{F}$ the numerical values already found．The following are the normal equations thus formed，and the resulting values of $A_{1}, B_{1}, C_{1} D_{1}$ ，and $E_{1}$ ，for each compass．For convenience of computation，the unit of the absolute terms of the normal equations has been changed from minutes of arc to radius．

Admiralty Standard Compass．

$$
\begin{aligned}
& \circ=-0.7505+10.000 A_{1}+7.482 B_{1}+3.999 C_{1}+3.938 D_{1}-2.63 \mathrm{I} E_{1} \\
& \circ=-0.5789+7.482 A_{1}+6.317 B_{1}+1.969 C_{1}+2.334 D_{1}-3.774 E_{1} \\
& \circ=-0.3183+3.999 A_{1}+1.969 B_{1}+3.685 C_{1}+3.708 D_{1}+\mathrm{1} .665 E_{1} \\
& \circ=-0.0169+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}^{2}\right) \\
& \circ=+0.0009+E_{1}+B_{1} C_{1}
\end{aligned}
$$

Hence

$$
\begin{aligned}
& A_{1}=-0.0102=-0^{\circ} 35^{\prime} \cdot \mathrm{r} \\
& B_{1}=+0.0833=+4 \quad 46.3 \\
& C_{1}=+0.0405=+2 \quad 19.2 \\
& D_{1}=+0.0142=+0 \quad 48.8 \\
& E_{1}=-0.0043=-0 \quad 14.8
\end{aligned}
$$

## After Binnacle Compass.

$0=-0.9599+10.000 A_{1}+7.482 B_{1}+3.999 C_{1}+3.938 D_{1}-2.631 E_{1}$ $0=-0.7253+7.482 A_{1}+6.317 B_{1}+1.969 C_{1}+2.334 D_{1}-3.774 E_{1}$ $0=-0.44 \mathrm{I} 3+3.999 A_{1}+1.969 B_{1}+3.685 C_{1}+3.708 D_{1}+\mathrm{r} .665 E_{1}$ $0=-0.0385+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=+0.0018+E_{1}+B_{1} C_{1}+0.0047\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$

$$
\begin{array}{lr}
A_{1}=+0.0062=+\circ^{\circ} & 2 \mathrm{I}^{\prime} \cdot 3 \\
B_{1}=+0.0801=+4 & 35.2 \\
C_{1}=+0.0362=+2 & 4.6 \\
D_{1}=+0.0360=+2 & 3.6 \\
E_{1}=-0.0048=-0 & 16.3
\end{array}
$$

## After Ritchie Compass.

$0=-2.5540+10.000 A_{1}+7.482 B_{1}+3.999 C_{1}+3.938 D_{1}-2.63 \mathrm{I} E_{1}$ $0=-\mathrm{r} .9282+7.482 A_{1}+6.317 B_{1}+1.969 C_{1}+2.334 D_{1}-3.774 E_{1}$ $0=-\mathrm{r} .0844+3.999 A_{1}+1.969 B_{1}+3.685 C_{1}+3.708 D_{1}+1.665 E_{1}$ $0=-0.0340+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=+0.0008+E_{1}+B_{1} C_{1}$
Hence

$$
\begin{aligned}
& A_{1}=+0.1030=+5^{\circ} 54^{\prime} .2 \\
& B_{1}=+0.1385=+7556.0 \\
& C_{1}=+0.0859=+455.4 \\
& D_{1}=+0.028 \mathrm{I}=+1 \\
& E_{1}=-0.0127=-0 \quad 43.7
\end{aligned}
$$

## Forward Alidade Compass

$0=-0.5265+10.000 A_{1}+7.482 B_{1}+3.999 C_{1}+3.938 D_{1}-2.631 E_{1}$ $0=-0.3589+7.482 A_{1}+6.317 B_{1}+1.969 C_{1}+2.334 D_{1}-3.774 E_{1}$ $0=-0.3022+3.999 A_{1}+1.969 B_{1}+3.685 C_{1}+3.708 D_{1}+1.665 E_{1}$ $0=-0.0235+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$
$0=-0.0007+E_{1}+B_{1} C_{1}+0.0125\left(B_{1}{ }^{2}-C_{1}{ }^{3}\right)$
Hence

$$
\begin{array}{lr}
A_{1}=+0.0359=+2^{\circ} & 3^{\prime} \cdot 5 \\
B_{1}=+0.000 \mathrm{I}=+0 & 0.2 \\
C_{1}=+0.0188=+1 & 4.8 \\
D_{1}=+0.0237=+1 & 21.4 \\
E_{1}=+0.0007=+0 & 2.4
\end{array}
$$

## Forward Binnacle Compass.

$0=-0.1396+10.000 A_{1}+7.482 B_{1}+3.999 C_{1}+3.938 D_{1}-2.63 \mathrm{I} E_{1}$ $0=-0.0593+7.482 A_{1}+6.317 B_{1}+1.969 C_{1}+2.334 D_{1}-3.774 E_{1}$ $0=-0.183 \mathrm{r}+3.999 A_{1}+1.969 B_{1}+3.685 C_{1}+3.708 D_{1}+1.665 E_{1}$ $0=-0.0369+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=-0.001 \mathrm{I}+E_{1}+B_{1} C_{1}$
Hence

$$
\begin{array}{lr}
A_{1}=-0.0159=-\circ^{\circ} & 54^{\prime} \cdot 7 \\
B_{1}=+0.0072=+\circ & 24.6 \\
C_{1}=+0.0253=+1 & 26.9 \\
D_{1}=+0.037^{2}=+2 & 7.8 \\
E_{1}=+0.0009=+\circ & 3.2
\end{array}
$$

Forward Ritchie Compass．

$$
\begin{aligned}
& 0=-0.0407+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right) \\
& 0=+0.0013+E_{1}+B_{1} C_{1} \\
& \text { Hence } \\
& A_{1}=+0.0614=+3^{\circ} 3 \mathrm{r}^{\prime} .0 \\
& B_{1}=-0.0076=-0 \quad 26 . \mathrm{r} \\
& C_{1}=+0.063 \mathrm{I}=+3 \quad 36.9 \\
& D_{1}=+0.0427=+2 \quad 26.6 \\
& E_{1}=-0.0011=-0 \quad 3.9
\end{aligned}
$$

The following are the equations of condition，together with the resulting normal equations，and the values of the coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$ ，as determined for each compass from the observations made at Rio Janeiro．

Equations of Condition at Rio Janeiro．

| Absolute Terms． |  |  |  |  |  |  | Coefficients of the Unknown Quantities． |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  | $\begin{gathered} \text { 邑 } \\ \text { 苞淢 } \end{gathered}$ |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  |  | $A_{1}$ | $B_{1}$ | $C_{1}$ | $D_{1}$ | $E$, |
| ＋ 2901 | － $32{ }^{\prime}$ | － $840^{\prime}$ | －160＇ | － $250^{\prime}$ | －160＇ | －500＇ | ＋ 1.000 |  | ＋0．83I |  | ＋0．383 |
| ＋360 | 410 | － 840 | 120 | － 250 | －160 | － 500 | ＋ 1.000 | ＋0．707 | ＋0．707 | ＋1．000 | 0．000 |
| ＋390 | －430 | － 840 | － 20 | － 250 | － 160 | －370 | ＋ 1.000 | ＋0．831 | ＋0．556 | ＋0．924 | －0．383 |
| ＋350 | －430 | － 970 | ＋130 | － 180 | － 160 | － 460 | ＋1．000 | ＋0．924 | ＋0．383 | ＋0．707 | －0．707 |
| ＋ 330 | － 360 | － 1010 | ＋160 | 160 | 160 | － 500 | ＋1．000 | ＋0．981 | ＋o．195 | ＋0．383 | －0．924 |
| ＋320 | － 340 | 880 | ＋ 280 | 160 | 160 | － 440 | ＋1．000 | ＋1．000 | 0.000 | 0.000 | － 1.000 |
| ＋ 300 <br> +280 | － 340 | $\begin{array}{r}720 \\ -610 \\ \hline\end{array}$ | ＋ 390 | $\begin{array}{r}160 \\ -160 \\ \hline\end{array}$ | 100 | － 420 | $+1.000$ | ＋0．981 | －0．195 | $-0.383$ | －0．924 |
| ＋ 280 +260 | － 280 | 610 | ＋ 410 | 160 160 | － 140 | － 350 | $+1.000$ | ＋0．924 | －0．383 | －0．707 | －0．707 |
| ＋ 260 +240 | － 260 | －590 | +440 +400 | 160 -160 | 100 -20 | － 330 | ＋ 1.000 +1.000 | +0.831 +0.707 | $-0.556$ | －0．924 | －0．383 |
| ＋ 200 | － 170 | －510 | ＋ | 160 | － 60 | a -330 -330 | ＋1．000 | ＋0．556 | －0．731 | － | a +0.38 +0.383 |
| $+210$ | － 110 | － 510 | ＋200 | － 230 | － 80 | － 330 | ＋1．000 | ＋ +0.383 | －0．924 | － 0.707 | ＋ 0.707 $+\quad 0.707$ |
| ＋170 | － 90 | 510 | ＋ 70 | － 250 | － 80 | － 270 | ＋ 1.000 | ＋o．195 | －0．981 | －0．383 | ＋0．924 |
| ＋150 | 90 | 510 | － 20 | － 250 | － 140 | － 250 | ＋1．000 | 0．000 | －1．000 | 0．000 | ＋1．000 |
| ＋ 140 | 20 | －510 | － 190 | － 310 | － 100 | － 180 | ＋ 1.000 | －0．195 | －0．98I | ＋0．383 | ＋0．924 |
| $+120$ | － 10 | － 510 | － 290 | －330 | 80 | － 230 | ＋1．000 | $-0.383$ | －0．924 | ＋0．707 | ＋0．707 |
| +90 | 10 | － 510 | －310 | －330 | 80 | － 250 | ＋ 1.000 | $-0.556$ | －0．831 | ＋ 0.924 | ＋o．3 |

Normal Equations．
Admiralty Standard Compass．
$0=-1.2217+17.000 A_{1}+8.442 B_{1}-5.641 C_{1}+0.924 D_{1}+0.383 E_{1}$ $0=-0.799 \mathrm{I}+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-1.205 D_{1}-4.543 E_{1}$ $0=+0.1662-5.641 A_{1}+0.462 B_{1}+8.691 C_{1}+3.900 D_{1}-4.438 E_{1}$ $0=-0.0169+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right)$ $0=+0.0009+E_{1}+B_{1} C_{1}$
Hence

$$
\begin{aligned}
& A_{1}=+0.0453=+2^{\circ} 35^{\prime} \cdot 7 \\
& B_{1}=+0.0519=+2 \\
& C_{1}=+0.5 \\
& C_{1}=+0.0015=+0 \\
& D_{1}=+0.2 \\
& E_{1}=-0.0009=-0 \quad 33 \cdot 5 \\
& \hline 0.1
\end{aligned}
$$

## After Binnacle Compass.

$$
\begin{aligned}
& \circ=-1.1228+17.000 A_{1}+8.442 B_{1}-5.641 C_{1}+0.924 D_{1}+0.383 E_{1} \\
& \circ=-0.8724+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-1.205 D_{1}-4.543 E_{1} \\
& \circ=-0.0346-5.641 A_{1}+0.462 B_{1}+8.691 C_{1}+3.900 D^{1}-4.438 E_{1} \\
& \circ=-0.0385+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right) \\
& \circ=+0.0018+E_{1}+B_{1} C_{1}+0.0047\left(B_{1}^{2}-C_{1}^{2}\right)
\end{aligned}
$$

$$
\begin{array}{lr}
A_{1}=+0.0148=+0^{\circ} & 50^{\prime} .8 \\
B_{1}=+0.0947=+5 & 25.4 \\
C_{1}=-0.0073=-0 & 25.2 \\
D_{1}=+0.0340=+1 & 57 . \mathrm{r} \\
E_{1}=-0.0012=-0 & 4 . \mathrm{I}
\end{array}
$$

After Ritchie Compass.

$$
\begin{aligned}
& \circ=-3.3336+\mathrm{r} 7.000 A_{1}+8.442 B_{1}-5.64 \mathrm{I} C_{1}+0.924 D_{1}+0.383 E_{1} \\
& \circ=-\mathrm{I} .9499+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-\mathrm{I} .205 D_{1}-4.543 E_{1} \\
& \circ=+0.6086-5.64 \mathrm{I} A_{1}+0.462 B_{1}+8.69 \mathrm{I} C_{1}+3.900 D_{1}-4.438 E_{1} \\
& \circ=-0.0340+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right) \\
& \circ=+0.0008+E_{1}+B_{1} C_{1}
\end{aligned}
$$

$$
\begin{array}{lr}
A_{1}=+0.1684=+9^{\circ} & 39^{\prime} .0 \\
B_{1}=+0.0659=+3 & 46.6 \\
C_{1}=+0.0203=+\mathrm{r} & 9.8 \\
D_{1}=+0.0320=+\mathrm{r} & 50 . \mathrm{I} \\
E_{1}=-0.0021=-0 & 7.4
\end{array}
$$

## After Azimuth Compass.

$0=+0.4916+17.000 A_{1}+8.442 B_{1}-5.641 C_{1}+0.924 D_{1}+0.383 E_{1}$ $0=+0.6880+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-1.205 D_{1}-4.543 E_{1}$ $0=-0.2024-5.641 A_{1}+0.462 B_{1}+8.691 C_{1}+3.900 D_{1}-4.438 E_{1}$ $0=-0.1116+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=+0.0002+E_{1}+B_{1} C_{1}$

$$
\begin{aligned}
& A_{1}=-0.0434=-2^{\circ} \\
& B_{1} 9^{\prime} \cdot 3 \\
& C_{1}=-0.0199=-1 \\
& C_{1}=0.055^{\prime}=-3 \\
& D_{1}=+0.1129=+6 \\
& E_{1}=-0.0013=-0 \\
& \hline 0.7 \\
& E_{1}=0.5
\end{aligned}
$$

## Forward Alidade Compass.

$0=-\mathrm{r} .0908+17.000 A_{1}+8.442 B_{1}-5.641 C_{1}+0.924 D_{1}+0.383 E_{1}$ $0=-0.411 \mathrm{II}+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-1.205 D_{1}-4.543 E_{1}$ $0=+0.4058-5.64 \mathrm{I} A_{1}+0.462 B_{1}+8.691 C_{1}+3.900 D_{1}-4.438 E_{1}$ $0=-0.0235+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=-0.0007+E_{1}+B_{1} C_{1}+0.0125\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$
Hence

$$
\begin{aligned}
& A_{1}=+0.06 \mathrm{I}_{5}=+3^{\circ} 3^{\mathrm{I}^{\prime} .5} \\
& B_{1}=-0.0084=-0 \\
& 28.8 \\
& C_{1}=-0.0166=-0 \quad 57.2 \\
& D_{1}=+0.0236=+\mathrm{r} \\
& 2 \mathrm{I.1} \\
& E_{1}=+0.0006=+\circ \quad 1.9
\end{aligned}
$$

## Forward Binnacle Compass.

$0=-0.5643+17.000 A_{1}+8.442 B_{1}-5.64 \mathrm{I} C_{1}+0.924 D_{1}+0.383 E_{1}$ $0=-0.3228+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-1.205 D_{1}-4.543 E_{1}$ $0=+0.0861-5.64 \mathrm{I} A_{1}+0.462 B_{1}+8.691 C_{1}+3.900 D_{1}-4.438 E_{1}$ $0=-0.0369+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right)$ $0=-0.001 \mathrm{I}+E_{1}+B_{1} C_{1}$
Hence

$$
\begin{array}{lr}
A_{1}=-0.0050=-\circ^{\circ} & 17^{\prime} .1 \\
B_{1}=+0.05^{2} 3=+2 & 59.8 \\
C_{1}=-0.0307=-\mathrm{I} & 45.5 \\
D_{1}=+0.0360=+2 & 3.7 \\
E_{1}=+0.0027=+\circ & 9.3
\end{array}
$$

## Forward Ritchie Compass.

$$
\begin{aligned}
& \circ=-\mathrm{r} .7570+\mathrm{r} 7.000 A_{1}+8.442 B_{1}-5.64 \mathrm{I} C_{1}+0.924 D_{1}+0.383 E_{1} \\
& \circ=-\mathrm{r} .0582+8.442 A_{1}+8.310 B_{1}+0.462 C_{1}-\mathrm{r} .205 D_{1}-4.543 E_{1} \\
& \circ=+0.3 \mathrm{I} 28-5.64 \mathrm{I} A_{1}+0.462 B_{1}+8.69 \mathrm{I} C_{1}+3.900 D_{1}-4.438 E_{1} \\
& \circ=-0.0407+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right) \\
& \circ=+0.0013+E_{1}+B_{1} C_{1}
\end{aligned}
$$

## Hence

$$
\begin{aligned}
& A_{1}=+0.0564=+3^{0} 14^{\prime} .0 \\
& B_{1}=+0.0766=+4 \quad 23.5 \\
& C_{1}=-0.0205=-1 \quad 10.4 \\
& D_{1}=+0.0380=+2 \\
& E_{1}=0.0000=0
\end{aligned}
$$

The following are the equations of condition for the determination of the cients of the After Ritchie Compass at Monte Video.

$$
\begin{aligned}
& 0=-240^{\prime}+1.000 A_{1} \quad 0.000 B_{1}+1.000 C_{1} \quad 0.000 D_{1}+1.000 E_{1} \\
& \mathrm{o}=-570+\mathrm{m} .000 A_{1}+0.195 B_{1}+0.98 \mathrm{I} C_{1}+0.383 D_{1}+0.924 E_{1} \\
& 0=-570+1.000 A_{1}+0.383 B_{1}+0.924 C_{1}+0.707 D_{1}+0.707 E_{1} \\
& 0=-740+1.000 A_{1}+0.556 B_{1}+0.831 C_{1}+0.924 D_{1}+0.383 E_{1} \\
& 0=-740+1.000 A_{1}+0.707 B_{1}+0.707 C_{1}+1.000 D_{1} \quad 0.000 E_{1} \\
& 0=-740+\mathrm{m} .000 A_{1}+0.83 \mathrm{I} B_{1}+0.556 C_{1}+0.924 D_{1}-0.383 E_{1} \\
& 0=-910+1.000 A_{1}+0.924 B_{1}+0.383 C_{1}+0.707 D_{1}-0.707 E_{1} \\
& 0=-900+1.000 A_{1}+0.981 B_{1}+0.195 C_{1}+0.383 D_{1}-0.924 E_{1} \\
& 0=-560+1.000 A_{1}+1.000 B_{1} \quad 0.000 C_{1} \quad 0.000 D_{1}-1.000 E_{1} \\
& 0=-240+1.000 A_{1}+0.981 B_{1}-0.195 C_{1}-0.383 D_{1}-0.924 E_{1} \\
& 0=-230+1.000 A_{1}+0.924 B_{1}-0.383 C_{1}-0.707 D_{1}-0.707 E_{1} \\
& 0=-60+\mathrm{m} .000 A_{1}+0.83 \mathrm{I} B_{1}-0.556 C_{1}-0.924 D_{1}-0.383 E_{1} \\
& 0=+270+1.000 A_{1}+0.707 B_{1}-0.707 C_{1}-1.000 D_{1} \quad 0.000 E_{1} \\
& 0=+100+\mathrm{I} .000 A_{1}+0.556 B_{1}-0.831 C_{1}-0.924 D_{1}+0.383 E_{1} \\
& 0=-240+1.000 A_{1}+0.383 B_{1}-0.924 C_{1}-0.707 D_{1}+0.707 E_{1} \\
& 0=-240+1.000 A_{1}+0.195 B_{1}-0.981 C_{1}-0.383 D_{1}+0.924 E_{1} \\
& 0=-240+1.000 A_{1} \quad 0.000 B_{1}-1.000 C_{1} \quad 0.000 D_{1}+1.000 E_{1} \\
& \mathrm{o}=-410+\mathrm{1} .000 A_{1}-0.195 B_{1}-0.98 \mathrm{I} C_{1}+0.383 D_{1}+0.924 E_{\mathrm{i}} \\
& 0=-410+1.000 A_{1}-0.383 B_{1}-0.924 C_{1}+0.707 D_{1}+0.707 E_{1} \\
& 0=-240+\mathrm{r} .000 A_{1}-0.556 B_{1}-0.83 \mathrm{r} C_{1}+0.924 D_{1}+0.383 E_{1} \\
& 0=-240+\mathrm{x} .000 A_{1}-0.707 B_{1}-0.707 C_{1}+1.000 D_{1} \quad 0.000 E_{1} \\
& 0=-570+\mathrm{r} .000 A_{1}-0.83 \mathrm{I} B_{1}-0.556 C_{1}+0.924 D_{1}-0.383 E_{1}
\end{aligned}
$$

The resulting normal equations are

$$
\begin{aligned}
& \circ=-2.5365+22.000 A_{1}+7.482 B_{1}-3.999 C_{1}+3.938 D_{1}+2.63 \mathrm{I} E_{1} \\
& \circ=-\mathrm{I} .0294+7.482 A_{1}+9.685 B_{1}+\mathrm{I} .969 C_{1}-2.334 D_{1}-3.774 E_{1} \\
& \circ=-0.3901-3.999 A_{1}+\mathrm{1} .969 B_{1}+\mathbf{1 2 . 3 1 6} C_{1}+3.708 D_{1}-\mathrm{I} .665 E_{1} \\
& \circ=-0.0340+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}^{2}\right) \\
& \circ=+\mathrm{o} .0008+E_{1}+B_{1} C_{1}
\end{aligned}
$$

Hence

$$
\begin{array}{lr}
A_{1}=+0.1143=+6^{\circ} & 3^{\prime} .8 \\
B_{1}=+0.0146=+0 & 50.3 \\
C_{1}=+0.0555=+3 & 10.9 \\
D_{1}=+0.0354=+2 & 1.8 \\
E_{1}=-0.0016=-0 & 5.5
\end{array}
$$

The following are the equations of condition, together with the resulting normal equations, and the values of the coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, as determined for each compass from the observations made in Magdalena Bay.

Equations of Condition at Magdalena Bay.

| Absolute Terms. |  |  |  |  |  | Coefficients of the Unknown Quantities. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  |  |  |  |  |  |  |  |
|  |  |  |  |  |  | $A_{1}$ | $B_{\mathrm{i}}$ | $C_{1}$ | $D_{1}$ | $E_{1}$ |
| $+20^{\prime}$ | - 10' | - 100' | $-300{ }^{\prime}$ | - 300' | - 540' | +1.000 | -0.707 | -0.707 | + 1.000 | 0.000 |
| + 60 | - 10 | - 180 | -370 | - 290 | -460 | +1.000 | -0.831 | -0.556 | + 0.924 | -0.383 |
| + 110 | + 80 | - 180 | ${ }^{210}$ | 210 | - 380 | $\underline{1} 1.000$ | -0.924 | $-0.383$ | + 0.707 | -0.707 |
| +140 | +160 | - 180 | - 130 | - 210 | - 290 | +1.000 | -0.981 | -0.195 | +0.383 | -0.924 |
| +180 | +170 | - 80 | - 130 | $-120$ | - 200 | +1.000 | - 1.000 | 0.000 | 0.000 | - 1.000 |
| + 230 | + 320 | +170 | - 210 | + 50 | + 50 | +1.000 | -0.981 | +0.195 | $-0.383$ | -0.924 |
| + 230 | +320 | + 330 | - 130 | +130 | + 210 | +1.000 | -0.924 | +0.383 | -0.707 | -0.707 |
| + 250 | +320 | + 320 | - 120 | + 210 | +210 | +1.000 | -0.831 | +0.556 | -0.924 | $-0.383$ |
| +220 | +320 +320 | +160 | - 40 | +300 | +210 | +1.000 | -0.707 | +0.707 | - 1.000 | -. 000 |
| + 220 | +320 | +160 | - 40 | + 380 | + 300 | +1.000 | -0.556 | +0.831 | - 0.924 | +0.383 |
| +160 | +320 +3 | +150 |  | + 380 | + 370 | $\underline{+1.000}$ | -0.383 | +0.924 | -0.707 | +0.707 |
| +100 | + 230 +150 | $\begin{array}{r}\text { + } 60 \\ \hline \mathbf{1 0 0}\end{array}$ | $+\quad 40$ $+\quad 40$ | +380 +370 | +210 $+\quad 210$ | +1.000 | -0.195 | +0.981 | -0.383 | +0.924 |
| $+\quad 40$ $+\quad 30$ | + 150 $+\quad 70$ |  | $+\quad 40$ $+\quad 50$ | +380 $+\quad 390$ | + 210 +120 | a +1.000 +1.000 | 0.000 +0.195 | +1.000 $+\quad 0.981$ | 0.000 +0.383 | +1.000 +0.924 |
| $+30$ | + 70 | - 190 | - 50 | + 290 | +120 | +1.000 | + 0.195 | + 0.981 | + 0.383 | + 0.924 |

## Normal Equations.

Admiralty Standard Compass.

$$
\begin{aligned}
& \circ=+0.5789+14.000 A_{1}-8.825 B_{1}+4.717 C_{1}-\mathrm{r} .631 D_{1}-\mathrm{r} .090 E_{1} \\
& \circ=-0.4310-8.825 A_{1}+7.545 B_{1}-0.816 C_{1}+0.934 D_{1}+4.272 E_{1} \\
& \circ=+0.2352+4.717 A_{1}-0.816 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1} \\
& \circ=-0.0169+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}^{2}\right) \\
& \circ=+0.0009+E_{1}+B_{1} C_{1}
\end{aligned}
$$

Hence

$$
\begin{aligned}
& A_{1}=+0.0026=+\circ^{\circ} \quad 9^{\prime} \cdot \mathrm{I} \\
& B_{1}=+0.0559=+3 \quad 12 . \mathrm{I} \\
& C_{1}=-0.0204=-\mathrm{I} \\
& D_{1}=+0.0156=+\circ \\
& E_{1}=+0.0002=+\circ \\
& E_{1}=0.5 \\
& \hline 0.0
\end{aligned}
$$

## After Binnacle Compass.

$\mathrm{o}=+0.8029+14.000 A_{1}-8.825 B_{1}+4.717 C_{1}-\mathrm{m} .63 \mathrm{I} D_{1}-\mathrm{1} .090 E_{1}$ $0=-0.529 \mathrm{I}-8.825 A_{1}+7.545 B_{1}-0.816 C_{1}+0.934 D_{1}+4.272 E_{1}$ $0=+0.4497+4.7$ I7 $A_{1}-0.816 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1}$ $0=-0.0385+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=+0.0018+E_{1}+B_{1} C_{1}+0.0047\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$

## Hence

Hence

> | $A_{1}=-0.0208=-\mathrm{I}^{\circ}{ }^{\circ} \mathrm{II}^{\prime} .4$ |
| :--- |
| $B_{1}=+0.0393=+2$ |
| $C_{1}=-0.0222=-\mathrm{I} 5.0$ |
| $D_{1}=+0.0380=+2$ |
| $E_{1} 6.2$ |
| $E_{1}=-0.0010=-0$ |
| 0.5 |

After Ritchie Compass.
$0=+0.0989+14.000 A_{1}-8.825 B_{1}+4.717 C_{1}-1.63 \mathrm{I} D_{1}-1.090 E_{1}$ $0=-0.1171-8.825 A_{1}+7.545 B_{1}-0.816 C_{1}+0.934 D_{1}+4.272 E_{1}$ $0=+0 . \ddot{2} 38+\dot{4} .717 A_{1}-0.8 \mathrm{~m} 6 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1}$ $0=-0.0340+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=+0.0008+E_{1}+B_{1} C_{1}$

$$
\begin{aligned}
& A_{1}=+0.0627=+3^{0} 35^{\prime} \cdot 5 \\
& B_{1}=+0.0778=+4 \\
& C_{1}=-0.0497=-2 \\
& D_{1}=+0.0322=+\mathbf{1} 5 \\
& E_{1}=+0.003 \mathrm{I}=+0 \\
& E_{1}=10.6
\end{aligned}
$$

## Formard Alidade Compass.

$$
\begin{gathered}
\circ=-0.4683+14.000 A_{1}-8.825 B_{1}+4.7 \mathrm{I} 7 C_{1}-\mathrm{I} .63 \mathrm{I} D_{1}-\mathrm{I} .090 E_{1} \\
0=+0.41 \mathrm{I} 5-8.825 A_{1}+7.545 B_{1}-0.8 \mathrm{I} 6 C_{1}+0.934 D_{1}+4.272 E_{1} \\
0=+0.1082+4.7 \mathrm{I} 7 A_{1}-0.8 \mathrm{I} 6 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1} \\
0=-0.0235+D_{1}+\frac{1}{2}\left(B_{1}^{2}-C_{1}^{2}\right) \\
0=-0.0007+E_{1}+B_{1} C_{1}+0.0125\left(B_{1}^{2}-C_{1}^{2}\right) \\
A_{1}=+0.0200=+\mathrm{I}^{\circ} 8^{\prime} .8 \\
B_{1}=-0.036 \mathrm{I}=-2 \\
C_{1}=-0.0197=-\mathrm{I} \quad 7.6 \\
D_{1}=+0.0230=+\mathrm{I} 19.2 \\
E_{1}=0.0000=000.0
\end{gathered}
$$

Hence

## Forward Binnacle Compass.

$0=+0.3956+14.000 A_{1}-8.825 B_{1}+4.717 C_{1}-1.63 \mathrm{I} D_{1}-1.090 E_{1}$ $0=+0.0125-8.825 A_{1}+7.545 B_{1}-0.816 C_{1}+0.934 D_{1}+4.272 E_{1}$ $0=+0.7497+4.7 \mathrm{I} 7 A_{1}-0.8 \mathrm{I} 6 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1}$. $0=-0.0369+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}{ }^{2}\right)$ $0=-0.001 \mathrm{I}+E_{1}+B_{1} C_{1}$
Hence

$$
\begin{array}{lr}
A_{1}=-0.0298=-\mathrm{I}^{0 .} & 42^{\prime} .6 \\
B_{1}=-0.0478=-2 & 44.3 \\
C_{1}=-0.07 \mathrm{I} 9=-4 & 7.3 \\
D_{1}=+0.0384=+2 & 1 \mathrm{I} .8 \\
E_{1}=-0.0023=-0 & 7.9
\end{array}
$$

Forward Ritchie Compass.

$$
\begin{aligned}
& \circ=+0.0058+14.000 A_{1}-8.825 B_{1}+4.717 C_{1}-\mathrm{1.631} D_{1}-\mathrm{1.090} E_{1} \\
& \circ=+0.2058-8.825 A_{1}+7.545 B_{1}-0.816 C_{1}+0.934 D_{1}+4.272 E_{1} \\
& \circ=+0.6749+4.717 A_{1}-0.816 B_{1}+6.456 C_{1}-4.554 D_{1}+3.784 E_{1} \\
& \circ=-0.0407+D_{1}+\frac{1}{2}\left(B_{1}{ }^{2}-C_{1}^{2}\right) \\
& \circ=+0.0013+E_{1}+B_{1} C_{1}
\end{aligned}
$$

Hence

$$
\begin{array}{lr}
A_{1}=+0.0477=+2^{\circ} & 43^{\prime} .8 \\
B_{1}=+0.0116=+0 & 39.9 \\
C_{1}=-0.105 \mathrm{I}=-6 & \mathrm{I} .3 \\
D_{1}=+0.0462=+2 & 38.7 \\
E_{1}=-0.0004=-0 & \mathrm{I} .3
\end{array}
$$

For convenience of reference the values of the coefficients $A_{1}, B_{1}, C_{1}, D_{1}, E_{1}$, obtained at stations where the compasses were not read on all the thirty-two points, have been collected in the following table. No use has been made of them.


At a number of the ports visited during the cruise, the line dividing the north from the south polarity, on the exterior of the turrets, was traced out; but as the boundary between the two kinds of magnetism was frequently very badly defined, and the observations were otherwise unsatisfactory; and further, as they throw no light whatever on the theory of the deviations of the compasses, and can only be shown by means of drawings on a rather large scale, it has not been deemed worth while to insert them here.

In conclusion, the results of the observations made during the cruise may be briefly recapitulated as follows:
$1^{\circ}$. The latitudes of seven points have been determined.
$2^{\circ}$. The magnetic declination, inclination, and horizontal force, have been determined at eighteen places.
$3^{\circ}$. The deviations of seven compasses have been observed, and compared with the theory, at ten places so situated as to afford very great changes in the terrestrial magnetic elements. For all these compasses the coefficients depending upon the hard and soft iron have been so far separated from each other as to render it possible to predict the deviations in any part of the world; and for the Admiralty Standard and After Azimuth Compasses every one of the coefficients in Poisson's general equations has been determined separately with a considerable degree of accuracy.

The conclusions drawn from the discussion of the observations are that, in the case of the Monadnock,
$a$. The agreement between the theoretical and observed deviations is sufficiently exact for the purposes of navigation, but is not entirely satisfactory in a scientific point of view.
b. It is questionable whether the theory really represents the semicircular as well as it does the quadrantal deviation; and to settle this point there is great need of more observations.
$c$. The so-called permanent and subpermanent magnetism of the ship were undergoing a constant and rapid change such as would correspond to a transfer of magnetism from aft forward; and to a rotation from right to left in the direction of the force.
d. The ratio of the hard to the soft iron force was slowly varying at each compass; and, for the different compasses it ranged between 4.3 and 67.4.
$e$. There was not a compass on board at which the direction of the hard and soft iron forces coincided; from which it follows that in no case was the ratio of the hard to the soft iron force the same in the coefficient $\mathfrak{ß}$ as it was in the coefficient $\mathfrak{C}$.
$f$. So far as can be judged from the observations discussed in this report, in the case of a vessel swung for the first time, it is impossible to make any reliable estimate of the ratio of the hard to the soft iron force in the coefficients $\mathfrak{B}$ and $\mathbb{C}$; and therefore, it is also impossible to make any reliable estimate of the changes the deviations of the compasses will undergo upon a change of magnetic latitude.


[^0]:    Colfins, Printer,
    philadelphia.

[^1]:    ${ }^{1}$ The Monadnock is a double-turreted vessel of the monitor type. During the cruise in question, Lieutenant Commander Francis M. Bunce, U.S. N., was her captain, and she was attached to the squadron commanded by Commodore (now Rear-Admiral) Jöhn Rogers, U.S. N., at whose special request I was detailed by the Navy Department to make the observations which are the subject of this paper.

    1 December, 1871.

[^2]:    ${ }^{1}$ For computing the deviations of the Admiralty Standard and After Azimuth Compasses the lines $c d$ and $e f$ were divided into degrees and sixths of a degree, each degree occupying the space of one-quarter of an inch.

[^3]:    a deviation to the West by the sign -.
    From the observations given above, the following values of the coefficients of the
    deviation are obtained:
    
    $=\mathrm{G}$

[^4]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the $\underset{53^{\prime} \cdot 5}{\mathrm{~B}=+2^{\circ}} \underset{\mathrm{E}=5}{58^{\prime} \cdot 5} \underset{\mathrm{O}^{\circ}}{\mathrm{C}=\mathrm{I}}=+0^{\circ} \quad 0^{\prime} .2$

[^5]:    | A deviation of the North Point of the Compass to the East is designated by the sign $+;$ | $\begin{array}{c}\text { A deviation of the North Point of the Compass to the East is designated by the sign } \\ \text { a deviation to the West by the sign - }\end{array}$ |
    | :--- | :--- | :--- | From the observations given above, the following values of the coefficients of the

    From the observations given above, the following values of the coefficients of the
    deviation are obtained:
    

[^6]:    A deviation of the North Point of the Compass to the East is designated by the sign +;
    a deviation to or the West by the sign From the observations given above, the following values of the coefficients of the
    deviation are oltained:
     From the observations given above, the following values of the coefficients of the
    deviation are obtained:
    

[^7]:     From the observations given above，the following values of the coefficients of the
    deviation are obtained： $\begin{aligned} & \text { From the observations given above，the following values of the coefficients of the } \\ & \text { deviation are obtained：}\end{aligned}$
    deviation are obtained：

[^8]:    A deviation of the North Point of the Compass to the East is designated by the sign + ；
    a deviation to the West by the sign $\quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{aligned}$ ； From the observations given above，the following values of the coefficients of the From the observations given above，the following values of the coefficients of the
     deviation are obtained：

[^9]:    A deviation of the North Point of the Compass to the East is designated by the sign +; $\quad \begin{gathered}\text { A deviation of the North Point of the Compass to the East is designated by the sign }+ \text {; }\end{gathered}$ From the observations given above, the following values of the coefficients of the The officer who usually read this compass was on shore when the ship was swung. He $\stackrel{27^{\prime} \cdot 5}{D=}+1^{\circ}{ }_{39^{\prime} \cdot 2}^{B}=+7^{\circ} \stackrel{16^{\prime} .8}{E}=+0^{\circ}{ }_{6^{\prime} \cdot 2}^{C=}-1^{\circ} 14^{\prime} \cdot 1$ $\begin{aligned} & \text { deviation are obtained: } \\ & A=+\circ^{\circ}\end{aligned}$

[^10]:    A deviation of the North Point of the Compass to the East is designated by the sign +; A deviation of the North Point of the Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the $\quad$ From the observations given above, the following values of the coefficients of the
    deviation are obtained: $\begin{array}{ll}2 I^{\prime} \cdot 5 \\ \mathrm{D}=+2^{\circ} & \stackrel{\mathrm{B}}{3^{\prime} \cdot 4}=+4^{\circ} \\ \mathrm{E}=34^{\prime} \cdot 9 \\ = & \mathrm{C}=0^{\circ} \\ \mathrm{I}^{\prime} \cdot 5\end{array}+2^{\circ} 4^{\prime} .8$

[^11]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; $\begin{array}{r}\text { A deviation of the North Point of the Compass to the East is designated by the sign } \\ \text { a deviation to the West by the sign - }\end{array}$ From the observations given above, the following values of the coefficients of the $\begin{aligned} & \text { Fram the observations given above, the following values of the coefficients of the } \\ & \text { deviations are obtained: }\end{aligned}$
    

[^12]:    From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
    

[^13]:     $\mathrm{A}=+7^{\circ} 40^{\prime} .0 \mathrm{~B}=+11^{\circ} \quad 26^{\prime} .5 \quad \mathrm{C}=-1^{\circ} 44^{\prime} .1 \quad \mathrm{~A}=+3^{\circ} 14^{\prime} .4 \quad \mathrm{~B}=+8^{\circ} \quad 26^{\prime} .9 \quad \mathrm{C}=+0^{\circ} 40^{\prime} .4$

[^14]:    a deviation to the West by the sign - Compass to the East is designated by the sign +; $\quad$ a deviation to the West by the sign - . Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
    

[^15]:    a deviation to the West by the sign -.
     deviations are obtained:
    $\mathrm{A}=+9^{\circ}$

[^16]:    From the observations given above, the following values of the coefficients of the
    deviation are obtained:
    $\begin{array}{llll}\mathrm{A}=+4^{\circ} & 21^{\prime} .9 & \mathrm{~B}=+3^{\circ} \cdot 49^{\prime} .1 & \mathrm{C}=+0^{\circ} 12^{\prime} .4\end{array} \begin{aligned} & \text { From the observations given above, the following values of the coefficients of the } \\ & \text { deviations are obtained: }\end{aligned}$
    

[^17]:    A deviation of the North Point of the Compass to the East is designated by the sign +; A deviation of the North Point of the Compass to the East is designated by the sign +; From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the $D=\quad B=\quad \mathrm{E}=\quad \mathrm{C}=$

[^18]:    A deviation of the North Point of the Compass to the East is designated by the sign +; $\quad$ A deviation of the North Point of the Compass to the East is designated by the sign + From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the $\stackrel{29^{\prime} \cdot 3}{=}+6^{\circ} \stackrel{\mathrm{B}}{28^{\prime} \cdot 2}=-\mathrm{r}^{\circ} \stackrel{8^{\prime} \cdot 5}{\mathrm{E}}=-0^{\circ} \mathrm{C}=-3^{\circ} 9^{\prime} \cdot 7$

[^19]:    A deviation of the North Point of the Compass to the East is designated by the sign $+; ~$$\quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign } \\ & \text { deviation to the West by the sign－}\end{aligned}$ ； a deviation to the West by the sign－－
    From the observations given above，the following values of the coefficients of the $\begin{aligned} & \text { a deviation to the west by the sign－－} \\ & \text { From the observations given above，the following values of the coefficients of the } \\ & \text { deviation are obtained：}\end{aligned}$
    

[^20]:    A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to of the West by the sign - . $\quad \begin{aligned} & \text { deviation to the West by the sign }- \text {. }\end{aligned}$ From the observations given above, the following values of the coefficients of the
    From the observations given above, the following values of the coefficients of the
     deviation are obtained:
    $\mathrm{A}=-3^{\circ}$

[^21]:    A deviation of the North Point of the Compass to the East is designated by the sign + ；
    a deviation to the West by the sign - ． From the observations given above，the following values of the coefficients of the $\begin{gathered}\text { These observations exhibit such discordancies among themselves that they do not seem } \\ \text { worth the trouble of reducing．}\end{gathered}$
    

[^22]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; $\quad$ A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to the West by the sign From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the cofficients of the $\mathrm{A}=+2^{\circ} 9^{\prime} .4 \quad \mathrm{~B}=-0^{\circ} \quad 6^{\prime} .0 \quad \mathrm{C}=-0^{\circ} 34^{\prime} \cdot \mathrm{I}$
    

[^23]:    A deviation of the North Point of the Compass to the East is designated by the sign $+; \quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{aligned}+$
    a deviation to the West by the sign From the observations given above, the following values of the coefficients of the $\begin{aligned} & \text { From the observations given above, the following values of the coefficients of the } \\ & \text { Feviations are }\end{aligned}$
    

[^24]:    A deviation of the North Point of the Compass to the East is designated by the sign + ;
    deviation to the West by the sign - deviation to the West by the sign - . From the observations given above, the following values of the coefficients of the
    From the observations given above, the following values of the coefficients of the
    

[^25]:    A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to of the West by the sign - . From the observations given above, the following values of the coefficients of the Fran the observations given above, the following values of the coefficients of the
    deviation are obtained:
    

[^26]:    From the observations given above, the following values of the coefficients of the $\begin{aligned} & \text { a deviation to the West by the sign - From the observations given above, the following values of the coefficients of the } \\ & \text { Fren }\end{aligned}$
     $0-=$
    pau!eqq
    A deviation of the North Point of the Compass to the East is designated by the sign + ; $\quad$ A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to the West by the sign From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
    deviation are obtained $\mathrm{B}=\quad \mathrm{E}=\quad \mathrm{C}=$

    ๘
    $\qquad$

[^27]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; a deviation to the West by the sign -.
    From the observations given above, the following values of the coefficients of the
    

[^28]:    A deviation of the North Point of the Compass to the East is designated by the sign +;
    $\begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{aligned}$;
    deviation to the West by the sign From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
     deviation are obtained:

[^29]:    A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to the West by the sign
    a $\quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{aligned}$, From the observations given above, the following values of the coefficients of the $\begin{aligned} & \text { From the observations given above, the following values of the coefficients of the } \\ & \text { deviation are obtained: }\end{aligned}$
    deviation are obtained:

[^30]:    A deviation of the North Point of the Compass to the East is designated by the sign＋；
    deviation to the West by the sign－deviation to the West From the observations given above，the following values of the coefficients of the From the observations given above，the following values of the coefficients of the
    deviation are obtained： $\stackrel{9^{\prime} \cdot 0}{\mathrm{D}}=+\mathrm{I}^{\mathrm{B}} \underset{56^{\prime} \cdot 5^{\circ}}{4^{\circ}} \stackrel{41^{\prime} \cdot \mathrm{I}}{\mathrm{E}}=+0^{\mathrm{C}}=-3^{\circ}=3^{\circ} 34^{\prime} \cdot 9$

[^31]:    Aeviation to the West by the sign -.
    From the observations given above, the following values of the coefficients of the $\begin{gathered}\text { From the observations given above, the following values of the coefficients of the } \\ \text { deviation are obtained: }\end{gathered}$

[^32]:    

[^33]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; $\quad$ A deviation of the North Point of the Compass to the East is designated by the sign + ; From the observations given above, the following values of the coefficients of the $\begin{gathered}\text { From the observations given above, the following values of the coefficients of the } \\ \text { deviation are obtained }\end{gathered}$
     $\mathrm{D}=\quad \mathrm{B}=$ deviation are obtained

[^34]:    A deviation of the North Point of the Compass to the East is designated by the sign + ; $\quad$ A deviation of the North Point of the Compass to the East is designated by the sign + ;
    a deviation to the West by the sign From the observations given above, the following values of the coefficients of the From the observations given above, the following values of the coefficients of the
    

[^35]:    A deviation of the North Point of the Compass to the East is designated by the sign +; $\begin{gathered}\text { A deviation of the North Point of the Compass to the East is designated by the sign }+ \text {; } \\ \text { a deviation to the West thy the sign - } \\ \text { deve the West by the sign } \\ \text { From the observations given above, the following values of the coefficients of the }\end{gathered}$ From the observations given above, the following values of the coefficients of the
    From the observations given above, the following values of the coefficients of the
    deviation are obtained:
    

[^36]:    $\begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }+ \text {; } \\ & \text { a deviation to the West by the sign -. }\end{aligned} \quad \begin{aligned} & \text { A deviation of the North Point of the Compass to the East is designated by the sign }\end{aligned}+$; From the observations given above, the following values of the coefficients of the $\begin{aligned} & \text { From the observations given above, the following values of the coefficients of the } \\ & \text { deviation are obtained: }\end{aligned}$

