CARDS

Carns of andeswelif

With full explanations and illustrations of their construction.

By GEO. R. PHRKINS, LL.D.

UTICA, N. Y. :
D. P, WHITE, PRINTER, 171 GENESEE STRFF
1866.

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## AGE CARDS,

## AND OTHER

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By GEO. R. PERKINS; I,L.D.

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The following pages are the result of a few leisure moments giyen to the preparation of cards for the amusement of some of my friends. As I progressed in my investigations my own interest became increased and I finally concluded to give my results a permanent form, by securing the copyright. And I intend soon to take measures for securing the patent right for the construction and use of all the various cards which I have described and referred to, especially those which I have denominated the Perforated Cards.

Utica, May 3, 1866 GEO. R. PERKINS.


Entered according to Act of Congress in the jear 1866,
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## AGECARDS.

All numbers in the natural series may be produced by the combination of the terms of the geometrical progression, $1,2,4,8,16,32,64$, \&c., by addition as follows:

CASE 1.

$$
\begin{aligned}
1 & =1 \\
2 & =2 \\
3 & =2+1 \\
4 & =4 \\
5 & =4+1 \\
6 & =4+2 \\
7 & =4+2+1 \\
8 & =8 \\
9 & =8+1 \\
10 & =8+2 \\
11 & =8+2+1 \\
12 & =8+4 \\
13 & =8+4+1 \\
14 & =8+4+2 \\
15 & =8+4+2+1 \\
16 & =16 \\
17 & =16+1 \\
18 & =16+2 \\
19 & =16+2+1 \\
20 & =16+4 \\
21 & =16+4+1 \\
22 & =16+4+2 \\
23 & =16+4+2+1
\end{aligned}
$$

The natural series of numbers may also be produced by the combination of the terms of the geometrical progression, 1, 3, 9, 27, 81, \&c., by addition and subtraction, as follows :

CASE II.

$$
\begin{aligned}
& 1=1 \\
& 2=3-1 \\
& 3=5 \\
& 4=3+1 \\
& 5=9-3-1 \\
& 6=9-3 \\
& 7=9-3+1 \\
& 8=9-1 \\
& 9=9 \\
& 10=9+1 \\
& 11=9+3-1 \\
& 12=9+3 \\
& 13=9+3+1
\end{aligned}
$$

$$
14=27-9-8 \times 1
$$

$$
15=27-9-3
$$

$$
16=27-9-3+1
$$

$$
17=27-9-1
$$

$$
18=27-9
$$

$$
19=27-9+1
$$

$$
20=27-9+3-1
$$

$$
21=27-9+3
$$

$$
22=27-9+3+1
$$

$$
23=27-3-1
$$

$$
24=27-3
$$

$$
25=27-3+1
$$

$$
26=27-1
$$

$$
27=27
$$

$$
\begin{aligned}
& 28=27+1 \\
& 29=27+3-1 \\
& 30=27+3 \\
& 31=27+3+1 \\
& 32=27+9-3-1 \\
& 33=27+9-3 \\
& 34=27+9-3+1 \\
& 35=27+9-1 \\
& 36=27+9 \\
& 37=27+9+1 \\
& 38=27+9+3-1 \\
& 39=27+9+3 \\
& 40=27+9+3+1 \\
& 41=81-27-9-3-1 \\
& 42=81-27-9-3 \\
& 43=81-27-9-3+1 \\
& 44=81-27-9-1 \\
& 45=81-27-9 \\
& 46=81-27-9+1 \\
& 47=81-27-9+3-1 \\
& 48=81-27-9+3 \\
& 49=81-27-9+3+1 \\
& 50=81-27-3-1 \\
& 51=81-27-3 \\
& 52=81-27-3+1 \\
& 53=81-27-1 \\
& \& c ., 8 c .
\end{aligned}
$$

These numbers may also be produced by addition and subtraction of the terms of the series, $1,3,5,19,57,171, \& c$.

This series is partly arithmetical and partly geometrical ; the first three terms $1,3,5$ are in arithmetical progression, the succeeding terms $19,57,171, \& c$., are in geometrical progression. Using these terms we have as follows:

## CASE III.

$$
\begin{aligned}
& 1=1 \\
& 2=3-1 \\
& 3=3 \\
& 4=3+1 \\
& 5=5 \\
& 6=5+1 \\
& 7=5+3-1 \\
& 8=5+3 \\
& 9=5+3+1 \\
& 10=19-5-3-1 \\
& 11=19-5-3 \\
& 12=19-5-3+1 \\
& 13=19-5-1 \\
& 14=19-5 \\
& 15=19-5+1 \\
& 16=19-3 \\
& 17=19-3+1 \\
& 18=19-1 \\
& 19=19 \\
& 20=19+1 \\
& 21=19+3-1 \\
& 22=19+3
\end{aligned}
$$

$$
\begin{aligned}
& 23=19+3+1 \\
& 24=19+5 \\
& 25=19+5+1 \\
& 26=19+5+3-1 \\
& 27=19+5+3 \\
& 28=19+5+3+1 \\
& 29=57-19-5-3-1 \\
& 30=57-19-5-3 \\
& 31=57-19-5-3+1 \\
& 32=57-19-5-1 \\
& 33=57-19-5 \\
& 34=57-19-5+1 \\
& 35=57-19-3 \\
& 36=57-19-3+1 \\
& 37=57-19-1 \\
& 38=57-19 \\
& 39=57-19+1 \\
& 40=57-19+3-1 \\
& 41=57-19+3 \\
& 42=57-19+3+1 \\
& 43=57-19+5 \\
& \quad \& e ., \text { \&c }
\end{aligned}
$$

These numbers may also bo produced by using the terms of the following series, $1,3,5,10,20$, 40 ; \&c., which is partly arithmetical and partly geometrical, in this case, however, the only term to be subtracted is 1 , as follows:

CASE IV.

| $1=1$ | $27=20+5+3-1$ |
| :--- | :--- |
| $2=3-1$ | $28=20+5+3$ |
| $3=3$ | $29=20+5+3+1$ |
| $4=3+1$ | $30=20+10$ |
| $5=5$ | $31=20+10+1$ |
| $6=5+1$ | $32=20+10+3-1$ |
| $7=5+3-1$ | $33=20+10+3$ |
| $8=5+3$ | $34=20+10+3+1$ |
| $9=5+3+1$ | $35=20+10+5$ |
| $10=10$ | $36=20+10+5+1$ |
| $11=10+1$ | $37=20+10+5+3-1$ |
| $12=10+3-1$ | $38=20+10+5+3$ |
| $13=10+3$ | $39=20+10+5+3+1$ |
| $14=10+3+1$ | $40=40$ |
| $15=10+5$ | $41=40+1$ |
| $16=10+5+1$ | $42=40+3-1$ |
| $17=10+5+3-1$ | $43=40+3$ |
| $18=10+5+3$ | $44=40+3+1$ |
| $19=10+5+3+1$ | $45=40+5$ |
| $20=20$ | $46=40+5+1$ |
| $21=20+1$ | $47=40+5+3-1$ |
| $22=20+3-1$ | $48=40+5+3$ |
| $23=20+3$ | $49=40+5+3+1$ |
| $24=20+3+1$ | $50=40+10$ |
| $25=20+5$ | $51=40+10+1$ |
| $26=20+5+1$ |  |

The natural sories of numbers may also bo produced by the addition and subtraction of other chosen terms, but at the present time we propose to confine ourselves to the four cases here exhibited.

## CASER I.

Arranging the numbers according to the elements used in their formation, that is, we group all those numbers together which are formed by the aid of 1 , all those formed by the aid of 2, all those formed by $4, \& c$., as follows:

| $(\Lambda)$ | $(\mathrm{B})$ | $(\mathrm{C})$ | $(\mathrm{D})$ | $(\mathrm{E})$ |
| ---: | ---: | ---: | ---: | ---: |
| 1 | 2 | 4 | 8 | 16 |
| 3 | 3 | 5 | 9 | 17 |
| 5 | 6 | 6 | 10 | 18 |
| 7 | 7 | 7 | 11 | 19 |
| 9 | 10 | 12 | 12 | 20 |
| 11 | 11 | 13 | 13 | 21 |
| 13 | 14 | 14 | 14 | 22 |
| 15 | 15 | 15 | 15 | 23 |
| 17 | 18 | 20 | 24 | 24 |
| 19 | 19 | 21 | 25 | 25 |
| 21 | 22 | 22 | 26 | 26 |
| 23 | 23 | 23 | 27 | 27 |
| 25 | 26 | 28 | 28 | 28 |
| 27 | 27 | 29 | 29 | 29 |
| 29 | 30 | 30 | 30 | 30 |
| 31 | 31 | 31 | 31 | 31 |

These groups designated by the letters A, B, $3, D, E, \& c .$, possess the following property:

Any number which is found in any one or more of these groups, and not in any of the other groups. is obtained by adding the leading or first numbers in the groups. As examples:

The number in groups $A$ and $D$ and not in either of the other groups, is $1+8=9$.

The number in groups $A, C$ and $E$, is $1+4+16=21$; and in like manner for other numbers.

Hence, knowing that a particular number is only in one or more of these groups, we at once know the number.

The above groups when arranged on separate pieces of paper or cards, have been known and published as Age Cards. They usually consist of seven cards, whose leading numbers are 1,2 , $4,8,16,32$ and 64 , and embrace all the series of natural numbers up to 127 .

A person being asked to select such of tho cards as contain the number of years denoting his age, you at once determine this number by adding the top numbers of the selected cards.

## CASE II.

Arranging our groups, or cards, according to the elements, $1,3,9,27,81, \& c$., observing to make a distinct and separate grouping for the negative values of these terms, which we have indicated by the small letters $a, b, c, d$, dc., as follows:

| (A) | (B) | (C) | (D) | (a) | (b) | (c) |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $[1]$ | 2 | 5 | 14 | 2 | 5 | 14 |
| 4 | $[3]$ | 6 | 15 | 5 | 6 | 15 |
| 7 | 4 | 7 | 16 | 8 | 7 | 16 |
| 10 | 11 | 8 | 17 | 11 | 14 | 17 |
| 13 | 12 | $[9]$ | 18 | 14 | 15 | 18 |
| 16 | 13 | 10 | 19 | 17 | 16 | 19 |
| 19 | 20 | 11 | 20 | 20 | 23 | 20 |
| 22 | 21 | 12 | 21 | 23 | 24 | 21 |
| 35 | 22 | 13 | 22 | 26 | 25 | 22 |
| 28 | 29 | 32 | 23 | 29 | 32 |  |
| 31 | 30 | 33 | 24 | 32 | 33 |  |
| 34 | 31 | 34 | 25 | 35 | 34 |  |
| 37 | 38 | 35 | 26 | 38 |  |  |
| 40 | 39 | 36 | $[27]$ |  |  |  |
|  | 40 | 37 | 28 |  |  |  |
|  |  | 38 | 29 |  |  |  |
|  |  | 39 | 30 |  |  |  |
|  |  | 40 | 31 |  |  |  |
|  |  |  | 32 |  |  |  |
|  |  |  | 33 |  |  |  |
|  |  |  | 35 |  |  |  |
|  |  |  | 36 |  |  |  |
|  |  |  | 37 |  |  |  |
|  |  |  | 38 |  |  |  |
|  |  |  | 40 |  |  |  |

To determine in this case the number on the selected cards, we must $a d d$ the numbers on the cards denoted by the capital letters, which are included in the brackets-[ ]-and from the sum subtract the numbers on the cards denoted by the small letters which are in the brackets immediately over the letters. Examples: Suppose the selected cards to be $A, B$ and $D$, the number will be $1+3+27=31$. If the cards are $D, a$ and $c$, the number will be $27-1-9=17$. If the cards are $B, C, D$ and $a$, the number will be $3+9+27-1=38$; and in a similar way for other cases.

By the introduction of two additional cards denoted by (E) and (d) whose values are +81 and -27 , we shall embrace all numbers up to 121.

These nine cards, with a card of explanation, are given on the last pages of this book, two cards being printed on each page, so that they may be readily cut out and used as a Puzzle, independent of the other matter.

In a similar way cards may be formed for the other cases here given.

## CASE III.

Arranging our numbers according to the elements $1,3,5,19,57$, \&c., distinguishing the negative values from the positive as in the preceding case, we have

|  |  |  |  | $[-1][-3][-5]$ |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| (A) | (B) | (C) | (D) | (a) | (b) | (c) |
| [1] | 2 | [5] | 10 | 2 | 10 | 10 |
| 4 | [3] | 6 | 11 | 7 | 11 | 11 |
| 6 | 4 | 7 | 12 | 10 | 12 | 12 |
| 9 | 7 | 8 | 13 | 13 | 16 | 18 |
| 12 | 8 | 9 | 14 | 18 | 17 | 14 |
| 15 | 9 | 24 | 15 | 21 |  | 15 |
| 17 | 21 | 25 | 16 | 26 |  |  |
| 20 | 22 | 26 | 17 |  |  |  |
| 23 | 23 | 27 | 18 |  |  |  |
| 25 | 26 | 28 | [19] |  |  |  |
| 28 | 27 |  | 20 |  |  |  |
|  | 28 |  | 21 |  |  |  |
|  |  |  | 22 |  |  |  |
|  |  |  | 23 |  |  |  |
|  |  |  | 24 |  |  |  |
|  |  |  | 25 |  |  |  |
|  |  |  | 26 |  |  |  |
|  |  |  | 27 |  |  |  |
|  |  |  | 28 |  |  |  |

In this case, if the selected cards are $A$, $D$ and $c$, the number is $1+19-5=15$; if the cards are $D, a, b$ and $c$, the number is $19-1-3-5=10$; and so for other combination of cards.

By the introduction of two cards (E) and (d,) whose values are +57 and -19 , we shall embrace all numbers up to 85 .

## 12

## CASE IV.

Proceeding as in the preceding cases we find:

| $(\mathrm{A})$ | $(\mathrm{B})$ | $(\mathrm{C})$ | $(\mathrm{D})$ | $(\mathrm{E})$ | $(-1]$ |
| :---: | :---: | :---: | :---: | :---: | ---: |
| $[1]$ | 2 | $[5]$ | $[10]$ | $[20]$ | 2 |
| 4 | $[3]$ | 6 | 11 | 21 | 7 |
| 6 | 4 | 7 | 12 | 22 | 12 |
| 9 | 7 | 8 | 13 | 28 | 17 |
| 11 | 8 | 9 | 14 | 24 | 22 |
| 14 | 9 | 15 | 15 | 25 | 27 |
| 16 | 12 | 16 | 16 | 26 | 32 |
| 19 | 13 | 17 | 17 | 27 | 37 |
| 21 | 14 | 18 | 18 | 28 |  |
| 24 | 17 | 19 | 19 | 29 |  |
| 26 | 18 | 25 | 30 | 30 |  |
| 29 | 19 | 26 | 31 | 31 |  |
| 31 | 22 | 27 | 32 | 32 |  |
| 34 | 23 | 28 | 33 | 33 |  |
| 36 | 24 | 29 | 34 | 34 |  |
| 39 | 27 | 35 | 35 | 35 |  |
|  | 28 | 36 | 36 | 36 |  |
|  | 29 | 37 | 37 | 37 |  |
|  | 32 | 38 | 38 | 38 |  |
|  | 33 | 39 | 39 | 39 |  |
|  | 34 |  |  |  |  |
|  | 37 |  |  |  |  |
|  | 38 |  |  |  |  |

If the selected cards are in this case $B, C$ and $a$, we have for the number $3+5-1=7$, if the cards are $C, D$ and $a$, we have $5+10-1=14$, and similarly for other combination of cards.

Introducing another positive card (F) whose value is 40 , we shall embrace all numbers up to 79. In this case, however far we extend our numbers, there will be but one negative card (a) whose value is -1 .

So far as I am aware, cases II, III and IV, which require subtraction as well as addition, have never before been noticed. Case I, is on many accounts the most interesting, it will emhrace more numbers, with fewer cards than in either of the other cases. But as a Puzzle to those not in the secret of the arrangement of the groups of terms, case II is the most remarkable. For, if we omit the letters and the brackets, which we have employed to assist in their explanation, and write simply the numbers, we shall have a set of cards, which would afford considerable amusement.

It is obvious that we might employ instead of these numbers, individual names of things, as the names of distinguished persons, localities, or events, having each individual numbered, so that the particular name selected on any card may be readily determined by means of its corresponding number.

## 14

The following list of the names of 121 Poets are thus arranged alphabetically, and each individual is denoted by the appropriate number as here given:

In this case we have five positive cards, denoted by the capital letters $A, B, C, D$ and $E$, having the corresponding values $1,3,9,27$ and 81 ; and four negative cards, denoted by the small letters $a, b, c$ and $d$, and having the corresponding negative values of $-1,-3,-9$ and -27 .

These nine cards with the Key Card, are correctly arranged and given on the following pages in such a manner as to admit of being cut out and pasted upon card paper so as to save the labor of copying them with the pen.

If an individual is requested to select such cards as contain the name of his laverite Poet, and he should return the cards denoted by $A, C$, and $E$, we should at once have by adding the values of these cards $1+9+81=91$, then referring to our Key Card, we see that Read corresponds to the number 91. Had he returned us the cards $A, E$ and $d$, we should have found $1+81-27=55$ which corresponds to Horace.

Similarly, the cards $D, E, b$ and $c$, give $27+81-3-9=96$, corresponds to Shakespeare. The cards $B, E$ and $c$, give $3+81-9=75$, corresponding to Milton.

## KEY CARD.

| Addison. | 42. Gilman. | 83. Pierpont, |
| :---: | :---: | :---: |
| \%. Akenside, | 43. Glen, | 84. Poe, |
| 3. Aldrich, | 44. Goethe. | $8^{55}$. |
| 4. St. Ambrose, | 45. Goldsmitl:, | 86. Pope. |
| 5. Anecreon, | 46. Gray, | 87. Prentiss, |
| 6. Angelo, | 47. Heber, | 88. Quarles, |
| 7. Baillie, | 48. Hemans, | 89. Raleigh, |
| 8. Barbauld | 49. Herbert, | 90. Ramsey, |
| 9. Baxter, | 50. Herrick, | 91. Read, |
| 10. Beattie, | 51. Hogg, | 92. Rogers, |
| 11. Beaumont, | 5.. Holmes, | 93. Roscoe, |
| 1). Blake, | 53. Homer, | 94. Sappho, |
| 13. Bowles, | 54. Hood, | 95. Scott, |
| 14. Browning, | 55. Horace, | 96. Shakespeare, |
| 15. Burns, | 56. Howitt, | 97. Shelly, |
| 16. Butler, | 57. Hugo | 98. Shenstone, |
| 17. Byron, | 58. Hunt, | 99. Southey. |
| 18. Callistratus, | 59. Ingram, | 100. Spencer, |
| 19. Chatterton, | 60. Sam. Johnson, | 101. Street, |
| 20. Chaucer, | 61. Ben. Jonson, | 102. Suckling, |
| 21. Coleridge, | 69. Keats, | 103. Swift, |
| 2.. Collins, | 63. Keble, | 104. 'Taylor, |
| 23. Cornwall, | 64. Kemble, | 105. Tennyson, |
| 25. Cowper, | $6^{6}$. Kingsley. | 107. Thackeray. |
| 26. Crabbe, | 67. Landor, | 108. Thomson. |
| 27. Croly, | 68. Leonidas. | 1199. Tuckerma |
| 28. Cunningham, | 69. Longfellow, | 110. Uhland, |
| 29. Daniel, | 70. Lover. | 111. Vaughn, |
| 30. Davidson, | 71. Loweli, | 112. Virgil, |
| 31. Dickens, | 72. Luther, | 113. Watts, |
| 32. Doddridge, | 73. Macaulay. | 114. Wesley, |
| 33. Drake, | 74. Marvell. | 115. White, |
| 34. Dryden, | 75. Milton, | 116. Whittier, |
| 35. Eastman, | 76. Montgomery | 117. Willis, |
| 3i. Elliott, <br> 37. Emerson | 77. Moore, | 118. Wilson, |
| 38. Ferguson | 78. Motherwell, | 120. Wordsworth, |
| 39. Mletcher. | 80. Norton, | 121. Zedlitz. |
| 40. Fortunatus, | 81. Ogilvie, |  |
| 41. Gay. | 82. Percival, |  |


| Addison, | Glen, |
| :--- | :--- |
| St. Ambrose, | Gray, |
| Baille, | Herbert, |
| Beattie, | Holmes, |
| Bowles, | Horace, |
| Butler, | Hunt, |
| Chatterton, | Ben. Jonson, |
| Collins, | Kemble, |
| Cowper, | Landor, |
| Cunningham, | Lover, |
| Dickens, | Macaulay, |
| Dryden, | Montgomery, |
| Emerson, | Newton, |
| Fortunatus, | Percival, |

Akenside, Anacreon, Barbauld, Beaumont, Browning, Byron, Chaucer, Cornwall, Crabbe, Daniel, Doddridge, Eastman, Ferguson, Gay,
(a)
(A)

| Glen, | Pollok, |
| :--- | :--- |
| Gray, | Quarles, |
| Herbert, | Read, |
| Holmes, | Sappho, |
| Horace, | SLelly, |
| Hunt, | Spencer, |
| Ben. Jonson, | Swift, |
| Kemble, | Terry, |
| Landor, | Tuckerman, |
| Lover, | Virgil, |
| Macaulay, | White, |
| Montgomery, | Wilson, |
| Newtom, | Zedlitz. |
| Percival, |  |

Goethe,
Heber,
Herrick,
Homer,
Howitt,
Ingram,
Keats,
Kingsley,
Leonidas,
Lowell,
Marvell,
Moore, Norton, Pierpont,

Pope,
Raleigh,
Rogers,
Scott,
Shenstone,
Street,
Taylor,
Thackeray,
Ubland,
Watts,
Whittier,
Wordsworth.

## 17

(B)

| Akonside, | Fortunatus, | Poe, |
| :--- | :--- | :--- |
| Aldrich, | Heber, | Pollok, |
| St. Ambrose, | Hemans, | Rogers, |
| Beaumout, | Herbert, | Roscoe, |
| Blake, | Howitt, | Sappho, |
| Bowles, | Hugo, | Street, |
| Chaucer, | Hunt, | Suckling, |
| Coleridge, | Kingsley, | Swift, |
| Collins, | Lamb, | Uhland, |
| Daniel, | Landor, | Vaughn, |
| Davidson,, | Marvell, | Virgil, |
| Dickens, | Milton, | Wordswortl, |
| Ferguson, | Montgomery, | Young, |
| Fletcher, | Pierpont, | Zedlizz. |

(b)

| Anacreon, | Gilman, | Newton, |
| :--- | :--- | :--- |
| Angelo, | Glen, | Pope, |
| Baillie, | Herrick, | Prentiss, |
| Browning, | Hogg, | Quarles; |
| Burns, | Holmes, | Scott, |
| Butler, | Ingram, | Shakespeare, |
| Cornwall, | Sam. Johnson, Shelly, |  |
| Cowley, | Ben. Jonson, | Taylor, |
| Cowper, | Leonidas, | Tennyson, |
| Doddridge, | Longfellow, | Terry, |
| Drake, | Lover, | Watts, |
| Dryden, | Moore, | Wesley, |
| Gay, | Motherwell, | White. |

Anacreon,
Angelo, Baillie, Barbauld, Baxter. Beattie, Beaumont, Blake, Bowles, Doddridge,
Drake,
Dryden,
Eastman, Elliott,
Emerson,

Ferguson, Fletcher,
Fortunatus, Read,
Ingram, Rogers,
Sam. Johnson, Roscoe,
Ben. Jonson, Sappho,
Keats,
Keble.
Kemble,
Kingsley,
Lamb,
Landor,
Pope,
Prentiss,
Quarles,
(c)

Browning,
Burns,
Butler,
Byron,
Callistratus,
Chatterton,
Chaucer,
Coleridge,
Collins,
Gay,
Gilman.
Glen,

Goethe,
Goldsmith, Gray, Heber, Hemans, Herbert, Leonidas, Longfellow, Lover,
Lowell,
Luther,
Macaulay,

Marvell,
Milton,
Montgomery,
Scott,
Shakespeare,
Shelly,
Shenstone,
Southey,
Spencer,
Street,
Suckling,
Swift.

Raleigh,
Ramsey,

Watts,
Wesley,
White,
Whittier,
Willis,
Wilson,
Wordsworth,
Young,
Zedlitz.
Browning,
Burns,
Butler,
Byron,
Calistratus,
Chatterton.
Chaucer,
Coleridge,
Collins,
Cornwall,
Cowley,
Cowper,
Crabbe,
Croly,
Cunningham,
Daniel,
Davison,
Dickens,

Taylor,
Tennyson,
Terry,
Thackeray,
Thomson,
Tuckerman,
Uhland,
Vaughn,
Virgil,
Watts,
Wesley,
White,
Whittier,
Willis,
Wilson,
Wordsworth,
Young,
Zedlitz.
(d)

| Gay, | Herrick, | Ingram, |
| :---: | :---: | :---: |
| Gilman, | Hogg, | Sam. Johnson, |
| Glen, | Holmes, | Ben. Jonson, |
| Goethe, | Homer, | Keats, |
| Goldsmith, | Hood, | Keble, |
| Gray, | Horace, | Kemble, |
| Heber, | Howitt, | Kingsley, |
| Hemans, | Hugo, | Lamb, |
| Herbert, | Hunt, | Landor, |

(E)

| Gay, | Leonidas, | Scott, |
| :--- | :--- | :--- |
| Gilman, | Longfellow, | Shakespeare, |
| Glen, | Lover, | Shelley, |
| Goethe, | Lowell, | Shenstone, |
| Goldsmith, | Luther, | Southey, |
| Gray, | Macaulay, | Spencer, |
| Heber, | Marvell, | Street, |
| Hemans, | Milton, | Suckling, |
| Herbert, | Montgomery, | Swif, |
| Herrick, | Moore, | Taylor, |
| Hogg, | Motherwell, | Tennyson, |
| Holmes, | Newtol,, | Terry, |
| Homer, | Norton, | Thackeray, |
| Hood, | Ogilvie, | Thomson, |
| Horace, | Percival, | Tuckerman, |
| Howitt, | Pierpont, | Uhland, |
| Hugo, | Poe, | Vaughn, |
| Hunt, | Pollok, | Virgil, |
| Ingram, | Pope, | Watts, |
| Sam. Johnson, | Prentiss, | Weslej, |
| Ben. Jonson, | Quarles, | White, |
| Keats, | Raleigh, | Whittior, |
| Keble, | Ramsey, | Willis, |
| Kemble, | Read, | Wilson, |
| Kingsley, | Rogers, | Wordsworth, |
| Lamb, | Roscoe, | Young, |
| Landor, | Sappho, | Zedlitz. |
|  |  |  |

I will give the following curious mechanical method of performing the addition and subtraction of the terms of the geometrical progression $1,3,9,27,81$, without mental effort.

Prepare 18 square cards of 121 cells each, that is of 11 rows of 11 cells in each row, and locate the 121 numbers in these cells, in numerical order, or in any other order we please, but the same order of location must be observed for the 18 cards.

Cut out the numbers on one of these squares which are given on the card $A$, and denote the square card thus cut or perforated by $A A$. Also make its complimentary perforated card from one of our 18 cards, by cutting out all the numbers except those given on $A$, and call the resulting card AAA. Similarly, cut out from another of our 18 cards, such numbers as are found on the card $a$, and call the result $a \alpha$, also form its complementary card denoted by aaa, by cutting out from one of our 18 cards, all the numbers except those on the card $a$. Proceed in the same way to form the card $B B$, and its complementary card $B B B$; also, $b b$ and $b b b$; also, $C C$ and $C C C$; also, $c c$ and $c c c$; also, $D D$ and $D D D$; also, $d d$ and $d d d$; also, $E E$ and $E E E$.

We shall thus obtain 9 new perforated cards denoted by $A A, a a, B B, b b, C C, c c, D D, d d, E E$, and their 9 corresponding complementary cards $A A A, a a a, B B B, \vee b b, C C C, c c c, D D D, d \dot{d} d, E E E$.

Now if a number is selected which is on the cards $A, B, c$, and $d$, and not on any of the other
cards, we take of the perforated cards, the cards $A A, B B, c c, d d$, and the complementary cards $a a a, b b b, C C C, D D D, E E E$, and placing them together in any order, we have a pack of 9 perforated cards, and we shall find one and only one perforation extending entirely through the pack, and this corresponds with the number sought, and by placing our pack upon a square card which has none of its numbers cut out, the number sought will be revealed through this perforation.

Since by this arrangement, we never superimpose any card on its complementary card, we may combine our 18 perforated cards so as to have only 9 distinct cards, the upper and lower halves of each card being complementary to each other ; and adding to these 9 cards, the corresponding cards denoted by $A, a, B, b, C, c, D, d$ and $E$, we shall have, including the Key Card which contains all the numbers and is not perforated, 10 cards. Each example may be performed by placing the 9 cards together upon the Key Card. The only thing to be careful to observe is to turn over, face downwards, such cards as do not contain the number under consideration.

Such perforated cards would obviously form considerable amusement when exhibited for the first time.

|  | (A) | (a) |  |
| ---: | ---: | ---: | ---: |
| 1 | 64 | 2 | 62 |
| 4 | 67 | 5 | 65 |
| 7 | 70 | 8 | 68 |
| 10 | 73 | 11 | 71 |
| 18 | 76 | 14 | 74 |
| 16 | 79 | 17 | 77 |
| 19 | 82 | 20 | 80 |
| 22 | 85 | 23 | 83 |
| 25 | 88 | 26 | 86 |
| 28 | 91 | 29 | 89 |
| 31 | 94 | 32 | 92 |
| 34 | 97 | 35 | 95 |
| 37 | 100 | 38 | 98 |
| 40 | 103 | 41 | 101 |
| 43 | 106 | 44 | 104 |
| 46 | 109 | 47 | 107 |
| 49 | 112 | 50 | 110 |
| 52 | 115 | 53 | 113 |
| 55 | 118 | 56 | 116 |
| 58 | 121 | 59 | 119 |
| 61 |  |  |  |

25

|  | (B) |  | (b) |  |
| ---: | ---: | ---: | ---: | :---: |
| 2 | 65 | 5 | 61 |  |
| 3 | 66 | 6 | 68 |  |
| 4 | 67 | 7 | 69 |  |
| 11 | 74 | 14 | 70 |  |
| 12 | 75 | 15 | 77 |  |
| 13 | 76 | 16 | 78 |  |
| 20 | 83 | 23 | 79 |  |
| 21 | 84 | 24 | 86 |  |
| 22 | 85 | 25 | 87 |  |
| 29 | 92 | 32 | 88 |  |
| 30 | 93 | 33 | 95 |  |
| 31 | 94 | 34 | 96 |  |
| 38 | 101 | 41 | 97 |  |
| 39 | 102 | 42 | 104 |  |
| 40 | 103 | 43 | 105 |  |
| 47 | 110 | 50 | 106 |  |
| 48 | 111 | 51 | 113 |  |
| 49 | 112 | 52 | 114 |  |
| 56 | 119 | 59 | 115 |  |
| 57 | 120 | 60 |  |  |


|  | (C) |  | (c) |  |
| ---: | ---: | ---: | ---: | :---: |
| 5 | 64 | 14 | 68 |  |
| 6 | 65 | 15 | 69 |  |
| 7 | 66 | 16 | 70 |  |
| 8 | 67 | 17 | 71 |  |
| 9 | 86 | 18 | 72 |  |
| 10 | 87 | 19 | 73 |  |
| 11 | 88 | 20 | 74 |  |
| 12 | 89 | 21 | 75 |  |
| 13 | 90 | 22 | 76 |  |
| 32 | 91 | 41 | 95 |  |
| 33 | 92 | 42 | 96 |  |
| 34 | 93 | 43 | 97 |  |
| 35 | 94 | 44 | 98 |  |
| 36 | 113 | 45 | 99 |  |
| 37 | 114 | 46 | 100 |  |
| 38 | 115 | 47 | 101 |  |
| 39 | 116 | 48 | 102 |  |
| 40 | 117 | 49 | 103 |  |
| 59 | 118 |  |  |  |
| 60 | 119 |  |  |  |
| 61 | 120 |  |  |  |
| 62 | 121 |  |  |  |
| 63 |  |  |  |  |

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29

|  | (D) |  | (d) |  |
| :--- | ---: | :--- | :--- | :--- |
| 14 | 95 | 41 | 54 |  |
| 15 | 96 | 42 | 55 |  |
| 16 | 97 | 43 | 56 |  |
| 17 | 98 | 44 | 57 |  |
| 18 | 99 | 45 | 58 |  |
| 19 | 100 | 46 | 59 |  |
| 20 | 101 | 47 | 60 |  |
| 21 | 102 | 48 | 61 |  |
| 22 | 103 | 49 | 62 |  |
| 23 | 104 | 50 | 63 |  |
| 24 | 105 | 51 | 64 |  |
| 25 | 106 | 52 | 65 |  |
| 26 | 107 | 53 | 66 |  |
| 27 | 108 |  | 67 |  |
| 28 | 109 |  |  |  |
| 29 | 110 |  |  |  |
| 30 | 111 |  |  |  |
| 31 | 112 |  |  |  |
| 32 | 113 |  |  |  |
| 33 | 114 |  |  |  |
| 34 | 115 |  |  |  |
| 35 | 116 |  |  |  |
| 36 | 117 |  |  |  |
| 37 | 118 |  |  |  |
| 38 | 119 |  |  |  |
| 39 | 120 |  |  |  |
| 40 | 121 |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |
|  |  |  |  |  |

## (L)

| 41 | 61 | 81 | 101 |
| ---: | ---: | ---: | ---: |
| 42 | 62 | 82 | 102 |
| 43 | 63 | 83 | 103 |
| 44 | 64 | 84 | 104 |
| 45 | 65 | 85 | 105 |
| 46 | 66 | 86 | 106 |
| 47 | 67 | 87 | 107 |
| 48 | 68 | 88 | 108 |
| 49 | 69 | 89 | 109 |
| 50 | 70 | 90 | 110 |
| 51 | 71 | 91 | 111 |
| 52 | 72 | 92 | 112 |
| 53 | 73 | 93 | 112 |
| 54 | 74 | 94 | 114 |
| 55 | 75 | 95 | 115 |
| 56 | 76 | 96 | 116 |
| 57 | 77 | 97 | 117 |
| 58 | 78 | 98 | 118 |
| 59 | 78 | 99 | 119 |
| 60 | 80 | 100 | 120 |
|  |  |  | 121 |

## EXPLANATION.

The five cards denoted by the capital letters $A$, $B, C, D$ and $E$ all ond with the number 121, and the value of each is positive and requires to be added. These values are as follows:

$$
A=1 ; B=3 ; C=9 ;
$$ $\mathrm{D}=27 ; \mathrm{E}=81$.

The four cards denoted by the small letters $a, b, c$ and $d$ are negative, and their values are to be subtracted. These values are as follows:

$$
\begin{gathered}
\mathrm{a}=-1 ; \quad \mathrm{b}=-3 ; \\
\mathrm{c}=-9 ; \mathrm{d}=-27 .
\end{gathered}
$$

## EXAMPLES.

A, B, C give
$1+3+9=13$ :
A, E, b give
$1+81-3=79$.
B, D, a, c give
$3+27-1-9=20$.
E, a, b, c, d give
$81-1-3-9-27=41$


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