

sketch, and on which he hopes to return in a future communication.

Theorem.—Let $A_1, A_2, \dots A_n$ be any n points (in number odd or even) assumed at pleasure on the n successive sides of a closed polygon $BB_1B_2 \dots B_{n-1}$ (plane or gauche), inscribed in any given surface of the second order. Take any three points, P, Q, R , on that surface, as initial points, and draw from each a system of n successive chords, passing in order through the n assumed points (A), and terminating in three other superficial and final points, P', Q', R' . Then there will be (in general) *another* inscribed and closed polygon, $CC_1C_2 \dots C_{n-1}$, of which the n sides shall pass successively, in the same order, through the same n points (A): and of which the initial point C shall also be connected with the point B of the former polygon, by the relations

$$\frac{ael}{bc} \frac{\beta\gamma}{a\epsilon\lambda} = \frac{a'e'l'}{b'c'} \frac{\beta'\gamma'}{a'\epsilon'\lambda'}$$

$$\frac{bfm}{ca} \frac{\gamma\alpha}{\beta\zeta\mu} = \frac{b'f'm'}{c'a'} \frac{\gamma'\alpha'}{\beta'\zeta'\mu'}$$

$$\frac{cgn}{ab} \frac{\alpha\beta}{\gamma\eta\nu} = \frac{c'g'n'}{a'b'} \frac{\alpha'\beta'}{\gamma'\eta'\nu'}$$

where

$a = QR,$	$b = RP,$	$c = PQ,$
$e = BP,$	$f = BQ,$	$g = BR,$
$l = CP,$	$m = CQ,$	$n = CR,$
$a' = QR',$	$b' = RP',$	$c' = PQ',$
$e' = BP',$	$f' = BQ',$	$g' = BR',$
$l' = CP',$	$m' = CQ',$	$n' = CR';$

while $a\beta\gamma\epsilon\zeta\eta\lambda\mu\nu$, and $a'\beta'\gamma'\epsilon'\zeta'\eta'\lambda'\mu'\nu'$, denote the semidiameters of the surface, respectively parallel to the chords $abcefglmn$, $a'b'c'e'f'g'l'm'n'$.

As a very particular case of this theorem, we may suppose that $PQR'P'Q'R'$ is a plane hexagon in a conic, and BC its Pascal's line.