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////////////////////////////////////
tcl_power2_4ary_i0 R=4 i=0
////////////////////////////////////
quaternary angle tree search (N=12)
theta= atan(pow(2,0) = 0.785398

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.....
* A: the leaf optimal path R=4 i=0
.....
* leaf min node : depth= 11 theta= +2.071228e-07 id=2414597

```

path type : leafmin

dp= 0	th=+0.785398	br= 0	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1	th=-0.463648	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2	th=-0.094314	br= 3	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3	th=-0.000655308	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4	th=+0.00715608	br= 0	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5	th=+0.00129673	br= 0	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6	th=-0.000168116	br= 2	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7	th=-4.60461e-05	br= 2	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8	th=-1.55285e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9	th=+7.35968e-06	br= 0	:	-0.000006	-0.000002	0.000002	0.000006
dp=10	th=+1.63763e-06	br= 0	:	-0.000001	-0.000000	0.000000	0.000001
dp=11	th=+2.07123e-07						

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.....
* B: the global optimal path R=4 i=0
.....
level min node : depth= 0 theta= +7.853982e-01 id=0
level min node : depth= 1 theta= -4.636476e-01 id=1
level min node : depth= 2 theta= -9.431395e-02 id=8
level min node : depth= 3 theta= -6.553079e-04 id=36
level min node : depth= 4 theta= +7.156080e-03 id=147
level min node : depth= 5 theta= +1.296727e-03 id=589
level min node : depth= 6 theta= -1.681164e-04 id=2357
level min node : depth= 7 theta= -4.604608e-05 id=9431
level min node : depth= 8 theta= -1.552850e-05 id=37727
level min node : depth= 9 theta= +7.359680e-06 id=150912
level min node : depth= 10 theta= +1.637634e-06 id=603649
level min node : depth= 11 theta= +2.071228e-07 id=2414597

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* global min node : depth= 11 theta= +2.071228e-07 id=2414597

```

path type : globalmin

dp= 0	th=+0.785398	br= 0	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1	th=-0.463648	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2	th=-0.094314	br= 3	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3	th=-0.000655308	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4	th=+0.00715608	br= 0	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5	th=+0.00129673	br= 0	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6	th=-0.000168116	br= 2	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7	th=-4.60461e-05	br= 2	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8	th=-1.55285e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9	th=+7.35968e-06	br= 0	:	-0.000006	-0.000002	0.000002	0.000006
dp=10	th=+1.63763e-06	br= 0	:	-0.000001	-0.000000	0.000000	0.000001
dp=11	th=+2.07123e-07						

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.....
* C: the cordic path R=4 i=0
.....
* cordic min node : depth= 11 theta= +2.071228e-07 id=2414597

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path type : cordic

dp= 0	th=+0.785398	br= 0	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1	th=-0.463648	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2	th=-0.094314	br= 3	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3	th=-0.000655308	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4	th=+0.00715608	br= 0	:	-0.005859	-0.001953	0.001953	0.005859

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dp= 5 th=+0.00129673      br= 0 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=-0.000168116    br= 2 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-4.60461e-05    br= 2 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=-1.55285e-05    br= 3 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=+7.35968e-06    br= 0 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+1.63763e-06    br= 0 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=+2.07123e-07

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* deallocate nodes in the leafmin path
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path

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////////////////////////////////////
tcl_power2_4ary_i1 R=4 i=1

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////////////////////////////////////
quaternary angle tree search (N=12)

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theta= atan(pow(2,-1) = 0.463648

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.....
* A: the leaf optimal path R=4 i=1

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.....
* leaf min node : depth= 11 theta= -4.286703e-07 id=2817512

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path type : leafmin

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dp= 0 th=+0.463648      br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=+0.141897     br= 1 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0212734    br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=-0.00990559   br= 2 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.0020942    br= 2 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.000141095  br= 2 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000347186  br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-1.90253e-05  br= 2 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.14923e-05  br= 1 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=+3.86286e-06  br= 0 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=-1.85918e-06  br= 3 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-4.2867e-07

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.....
* B: the global optimal path R=4 i=1

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.....
level min node : depth= 0 theta= +4.636476e-01 id=0
level min node : depth= 1 theta= +1.418971e-01 id=2
level min node : depth= 2 theta= +2.127339e-02 id=10
level min node : depth= 3 theta= -9.905591e-03 id=42
level min node : depth= 4 theta= -2.094203e-03 id=171
level min node : depth= 5 theta= -1.410954e-04 id=687
level min node : depth= 6 theta= +3.471856e-04 id=2751
level min node : depth= 7 theta= -1.902532e-05 id=11005
level min node : depth= 8 theta= +1.149226e-05 id=44023
level min node : depth= 9 theta= +3.862864e-06 id=176094
level min node : depth= 10 theta= -1.859182e-06 id=704377
level min node : depth= 11 theta= -4.286703e-07 id=2817512

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* global min node : depth= 11 theta= -4.286703e-07 id=2817512

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path type : globalmin

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```

dp= 0 th=+0.463648      br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=+0.141897     br= 1 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0212734    br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=-0.00990559   br= 2 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.0020942    br= 2 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.000141095  br= 2 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000347186  br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-1.90253e-05  br= 2 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.14923e-05  br= 1 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=+3.86286e-06  br= 0 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=-1.85918e-06  br= 3 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-4.2867e-07

```

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.....

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\* C: the cordic path R=4 i=1  
 .....  
 \* cordic min node : depth= 11 theta= -4.286703e-07 id=2817509

path type : cordic  
 dp= 0 th=+0.463648 br= 1 : -1.249046 -0.321751 0.321751 1.249046  
 dp= 1 th=+0.141897 br= 1 : -0.369334 -0.120624 0.120624 0.369334  
 dp= 2 th=+0.0212734 br= 1 : -0.093659 -0.031179 0.031179 0.093659  
 dp= 3 th=-0.00990559 br= 2 : -0.023436 -0.007811 0.007811 0.023436  
 dp= 4 th=-0.0020942 br= 2 : -0.005859 -0.001953 0.001953 0.005859  
 dp= 5 th=-0.000141095 br= 2 : -0.001465 -0.000488 0.000488 0.001465  
 dp= 6 th=+0.000347186 br= 0 : -0.000366 -0.000122 0.000122 0.000366  
 dp= 7 th=-1.90253e-05 br= 2 : -0.000092 -0.000031 0.000031 0.000092  
 dp= 8 th=+1.14923e-05 br= 1 : -0.000023 -0.000008 0.000008 0.000023  
 dp= 9 th=+3.86286e-06 br= 0 : -0.000006 -0.000002 0.000002 0.000006  
 dp=10 th=-1.85918e-06 br= 3 : -0.000001 -0.000000 0.000000 0.000001  
 dp=11 th=-4.2867e-07

\* deallocate nodes in the leafmin path  
 \* deallocate nodes in the globalmin path  
 \* deallocate nodes in the cordic path  
 ;;  
 tcl\_power2\_4ary\_i2 R=4 i=2  
 ;;  
 quaternary angle tree search (N=12)  
 theta= atan(pow(2,-2) = 0.244979

.....  
 \* A: the leaf optimal path R=4 i=2  
 .....  
 \* leaf min node : depth= 11 theta= +8.036423e-08 id=3055979

path type : leafmin  
 dp= 0 th=+0.244979 br= 1 : -1.249046 -0.321751 0.321751 1.249046  
 dp= 1 th=-0.0767719 br= 2 : -0.369334 -0.120624 0.120624 0.369334  
 dp= 2 th=+0.0438518 br= 1 : -0.093659 -0.031179 0.031179 0.093659  
 dp= 3 th=+0.0126728 br= 1 : -0.023436 -0.007811 0.007811 0.023436  
 dp= 4 th=+0.00486141 br= 0 : -0.005859 -0.001953 0.001953 0.005859  
 dp= 5 th=-0.000997939 br= 3 : -0.001465 -0.000488 0.000488 0.001465  
 dp= 6 th=+0.000466904 br= 0 : -0.000366 -0.000122 0.000122 0.000366  
 dp= 7 th=+0.000100693 br= 0 : -0.000092 -0.000031 0.000031 0.000092  
 dp= 8 th=+9.14027e-06 br= 1 : -0.000023 -0.000008 0.000008 0.000023  
 dp= 9 th=+1.51088e-06 br= 1 : -0.000006 -0.000002 0.000002 0.000006  
 dp=10 th=-3.96473e-07 br= 2 : -0.000001 -0.000000 0.000000 0.000001  
 dp=11 th=+8.03642e-08

.....  
 \* B: the global optimal path R=4 i=2  
 .....  
 level min node : depth= 0 theta= +2.449787e-01 id=0  
 level min node : depth= 1 theta= -7.677189e-02 id=2  
 level min node : depth= 2 theta= +4.385178e-02 id=11  
 level min node : depth= 3 theta= +1.267280e-02 id=46  
 level min node : depth= 4 theta= +4.861413e-03 id=186  
 level min node : depth= 5 theta= -9.979395e-04 id=745  
 level min node : depth= 6 theta= +4.669039e-04 id=2984  
 level min node : depth= 7 theta= +1.006930e-04 id=11937  
 level min node : depth= 8 theta= +9.140270e-06 id=47749  
 level min node : depth= 9 theta= +1.510876e-06 id=190998  
 level min node : depth= 10 theta= -3.964729e-07 id=763994  
 level min node : depth= 11 theta= +8.036423e-08 id=3055979

\* global min node : depth= 11 theta= +8.036423e-08 id=3055979

path type : globalmin  
 dp= 0 th=+0.244979 br= 1 : -1.249046 -0.321751 0.321751 1.249046  
 dp= 1 th=-0.0767719 br= 2 : -0.369334 -0.120624 0.120624 0.369334  
 dp= 2 th=+0.0438518 br= 1 : -0.093659 -0.031179 0.031179 0.093659  
 dp= 3 th=+0.0126728 br= 1 : -0.023436 -0.007811 0.007811 0.023436

```

dp= 4 th=+0.00486141      br= 0 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=-0.000997939    br= 3 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=+0.000466904    br= 0 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+0.000100693    br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=+9.14027e-06    br= 1 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=+1.51088e-06    br= 1 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=-3.96473e-07    br= 2 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=+8.03642e-08

```

```

.....
* C: the cordic path R=4 i=2
.....
* cordic min node : depth= 11 theta= +8.036423e-08 id=3055977

```

```

path type : cordic
dp= 0 th=+0.244979      br= 1 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=-0.0767719    br= 2 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=+0.0438518    br= 1 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=+0.0126728    br= 1 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=+0.00486141    br= 0 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=-0.000997939  br= 3 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=+0.000466904  br= 0 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+0.000100693  br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=+9.14027e-06  br= 1 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=+1.51088e-06  br= 1 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=-3.96473e-07  br= 2 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=+8.03642e-08

```

```

* deallocate nodes in the leafmin path
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path
;;;;;;;;;;;;;
tcl_power2_4ary_i3 R=4 i=3
;;;;;;;;;;;;;
quaternary angle tree search (N=12)
theta= atan(pow(2,-3) = 0.124355

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.....
* A: the leaf optimal path R=4 i=3
.....
* leaf min node : depth= 11 theta= -1.821627e-08 id=3545729

```

```

path type : leafmin
dp= 0 th=+0.124355      br= 2 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=+0.446106      br= 0 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=+0.0767719    br= 0 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=-0.0168868    br= 3 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=+0.00654932    br= 0 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=+0.000689965  br= 1 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=+0.000201684  br= 1 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+7.96136e-05  br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=-1.19391e-05  br= 2 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=-4.30975e-06  br= 3 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=+1.4123e-06   br= 0 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=-1.82163e-08

```

```

.....
* B: the global optimal path R=4 i=3
.....
level min node : depth= 0 theta= +1.243550e-01 id=0
level min node : depth= 1 theta= -1.973956e-01 id=2
level min node : depth= 2 theta= -7.677189e-02 id=11
level min node : depth= 3 theta= -1.688675e-02 id=53
level min node : depth= 4 theta= -6.549318e-03 id=193
level min node : depth= 5 theta= -6.899649e-04 id=776
level min node : depth= 6 theta= -2.016839e-04 id=3107
level min node : depth= 7 theta= -7.961359e-05 id=12431
level min node : depth= 8 theta= -1.193915e-05 id=55401
level min node : depth= 9 theta= -4.309751e-06 id=221607

```

level min node : depth= 10 theta= -1.412295e-06 id=795657
level min node : depth= 11 theta= -1.821627e-08 id=3545729

\* global min node : depth= 11 theta= -1.821627e-08 id=3545729

path type : globalmin

Table with 5 columns: dp, th, br, and two numerical values. Rows represent different path steps from dp=0 to dp=11.

.....

\* C: the cordic path R=4 i=3

.....

\* cordic min node : depth= 11 theta= +1.821627e-08 id=3182629

path type : cordic

Table with 5 columns: dp, th, br, and two numerical values. Rows represent different path steps from dp=0 to dp=11.

\* deallocate nodes in the leafmin path
\* deallocate nodes in the globalmin path
\* deallocate nodes in the cordic path

////////////////////////////////////

tcl\_power2\_4ary\_i4 R=4 i=4

////////////////////////////////////

quaternary angle tree search (N=12)

theta= atan(pow(2,-4) = 0.0624188

.....

\* A: the leaf optimal path R=4 i=4

.....

\* leaf min node : depth= 11 theta= -1.301979e-07 id=3610695

path type : leafmin

Table with 5 columns: dp, th, br, and two numerical values. Rows represent different path steps from dp=0 to dp=11.

.....

\* B: the global optimal path R=4 i=4

.....

```

level min node : depth= 0 theta= +6.241881e-02 id=0
level min node : depth= 1 theta= -2.593317e-01 id=2
level min node : depth= 2 theta= +1.483571e-02 id=13
level min node : depth= 3 theta= -1.634327e-02 id=54
level min node : depth= 4 theta= -7.092800e-03 id=197
level min node : depth= 5 theta= -1.233447e-03 id=792
level min node : depth= 6 theta= -2.313962e-04 id=3525
level min node : depth= 7 theta= -1.093259e-04 id=14103
level min node : depth= 8 theta= -1.777317e-05 id=56416
level min node : depth= 9 theta= -5.115011e-06 id=203045
level min node : depth= 10 theta= -6.070351e-07 id=902673
level min node : depth= 11 theta= -1.301979e-07 id=3610695

```

\* global min node : depth= 11 theta= -1.301979e-07 id=3610695

path type : globalmin

```

dp= 0 th=+0.0624188      br= 2 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=+0.384169      br= 0 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=+0.0148357     br= 1 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=-0.0163433     br= 3 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=+0.0070928     br= 0 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=+0.00123345    br= 0 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=-0.000231396   br= 2 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=-0.000109326   br= 3 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=-1.77732e-05   br= 3 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=+5.11501e-06   br= 0 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=-6.07035e-07   br= 2 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=-1.30198e-07

```

.....

\* C: the cordic path R=4 i=4

.....

\* cordic min node : depth= 11 theta= +1.301979e-07 id=3248737

path type : cordic

```

dp= 0 th=+0.0624188      br= 1 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=-0.259332      br= 3 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=+0.110002      br= 0 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=+0.0163433     br= 0 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=-0.0070928     br= 3 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=-0.00123345    br= 3 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=+0.000231396   br= 1 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+0.000109326   br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=+1.77732e-05   br= 0 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=-5.11501e-06   br= 3 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=+6.07035e-07   br= 1 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=+1.30198e-07

```

```

* deallocate nodes in the leafmin path
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path

```

;;;

tcl\_power2\_4ary\_i5 R=4 i=5

;;;

quaternary angle tree search (N=12)

theta= atan(pow(2,-5) = 0.0312398

.....

\* A: the leaf optimal path R=4 i=5

.....

\* leaf min node : depth= 11 theta= +5.367653e-08 id=3643535

path type : leafmin

```

dp= 0 th=+0.0312398      br= 2 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=+0.35299       br= 0 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=-0.0163433     br= 2 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=+0.0148357     br= 1 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=+0.00702432    br= 0 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=+0.00116497    br= 0 : -0.001465 -0.000488 0.000488 0.001465

```

dp= 6	th=-0.000299877	br= 3	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7	th=+6.6334e-05	br= 0	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8	th=-2.52187e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9	th=-2.33051e-06	br= 2	:	-0.000006	-0.000002	0.000002	0.000006
dp=10	th=-4.23161e-07	br= 2	:	-0.000001	-0.000000	0.000000	0.000001
dp=11	th=+5.36765e-08						

.....  
\* B: the global optimal path R=4 i=5

```

.....
level min node : depth= 0 theta= +3.123983e-02 id=0
level min node : depth= 1 theta= -2.905107e-01 id=2
level min node : depth= 2 theta= -1.634327e-02 id=13
level min node : depth= 3 theta= +1.483571e-02 id=55
level min node : depth= 4 theta= +7.024319e-03 id=222
level min node : depth= 5 theta= +1.164967e-03 id=889
level min node : depth= 6 theta= +2.998769e-04 id=3204
level min node : depth= 7 theta= +6.633404e-05 id=14232
level min node : depth= 8 theta= +2.521869e-05 id=51272
level min node : depth= 9 theta= +2.330509e-06 id=205089
level min node : depth= 10 theta= +4.231606e-07 id=820358
level min node : depth= 11 theta= +5.367653e-08 id=3643535

```

\* global min node : depth= 11 theta= +5.367653e-08 id=3643535

path type : globalmin

dp= 0	th=+0.0312398	br= 2	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1	th=+0.35299	br= 0	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2	th=-0.0163433	br= 2	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3	th=+0.0148357	br= 1	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4	th=+0.00702432	br= 0	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5	th=+0.00116497	br= 0	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6	th=-0.000299877	br= 3	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7	th=+6.6334e-05	br= 0	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8	th=-2.52187e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9	th=-2.33051e-06	br= 2	:	-0.000006	-0.000002	0.000002	0.000006
dp=10	th=-4.23161e-07	br= 2	:	-0.000001	-0.000000	0.000000	0.000001
dp=11	th=+5.36765e-08						

.....  
\* C: the cordic path R=4 i=5

.....  
\* cordic min node : depth= 11 theta= -5.367653e-08 id=3281433

path type : cordic

dp= 0	th=+0.0312398	br= 1	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1	th=-0.290511	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2	th=+0.0788229	br= 0	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3	th=-0.0148357	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4	th=-0.00702432	br= 3	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5	th=-0.00116497	br= 3	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6	th=+0.000299877	br= 0	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7	th=-6.6334e-05	br= 3	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8	th=+2.52187e-05	br= 0	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9	th=+2.33051e-06	br= 1	:	-0.000006	-0.000002	0.000002	0.000006
dp=10	th=+4.23161e-07	br= 1	:	-0.000001	-0.000000	0.000000	0.000001
dp=11	th=-5.36765e-08						

\* deallocate nodes in the leafmin path  
\* deallocate nodes in the globalmin path  
\* deallocate nodes in the cordic path

;;;  
tcl\_power2\_4ary\_i6 R=4 i=6

;;;  
quaternary angle tree search (N=12)  
theta= atan(pow(2,-6) = 0.0156237

.....  
\* A: the leaf optimal path R=4 i=6

.....  
\* leaf min node : depth= 11 theta= +4.826728e-08 id=3659912

path type : leafmin

dp= 0 th=+0.0156237	br= 2	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1 th=+0.337374	br= 0	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2 th=-0.0319594	br= 2	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3 th=-0.000780398	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4 th=+0.00703099	br= 0	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5 th=+0.00117164	br= 0	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6 th=-0.000293207	br= 3	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7 th=+7.30044e-05	br= 0	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8 th=-1.85484e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9 th=+4.3398e-06	br= 0	:	-0.000006	-0.000002	0.000002	0.000006
dp=10 th=-1.38224e-06	br= 3	:	-0.000001	-0.000000	0.000000	0.000001
dp=11 th=+4.82673e-08						

.....  
\* B: the global optimal path R=4 i=6

.....  
level min node : depth= 0 theta= +1.562373e-02 id=0  
level min node : depth= 1 theta= -3.061268e-01 id=2  
level min node : depth= 2 theta= -3.195937e-02 id=13  
level min node : depth= 3 theta= -7.803981e-04 id=55  
level min node : depth= 4 theta= -7.015742e-03 id=200  
level min node : depth= 5 theta= -1.156389e-03 id=804  
level min node : depth= 6 theta= -2.932066e-04 id=3573  
level min node : depth= 7 theta= -5.775673e-05 id=12881  
level min node : depth= 8 theta= -1.854838e-05 id=57185  
level min node : depth= 9 theta= +4.339802e-06 id=228744  
level min node : depth= 10 theta= +1.371077e-06 id=824452  
level min node : depth= 11 theta= +4.826728e-08 id=3659912

\* global min node : depth= 11 theta= +4.826728e-08 id=3659912

path type : globalmin

dp= 0 th=+0.0156237	br= 2	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1 th=+0.337374	br= 0	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2 th=-0.0319594	br= 2	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3 th=-0.000780398	br= 2	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4 th=+0.00703099	br= 0	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5 th=+0.00117164	br= 0	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6 th=-0.000293207	br= 3	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7 th=+7.30044e-05	br= 0	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8 th=-1.85484e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9 th=+4.3398e-06	br= 0	:	-0.000006	-0.000002	0.000002	0.000006
dp=10 th=-1.38224e-06	br= 3	:	-0.000001	-0.000000	0.000000	0.000001
dp=11 th=+4.82673e-08						

.....  
\* C: the cordic path R=4 i=6

.....  
\* cordic min node : depth= 11 theta= -5.943496e-08 id=3297809

path type : cordic

dp= 0 th=+0.0156237	br= 1	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1 th=-0.306127	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2 th=+0.0632068	br= 0	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3 th=-0.0304518	br= 3	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4 th=-0.00701574	br= 3	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5 th=-0.00115639	br= 3	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6 th=+0.000308454	br= 0	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7 th=-5.77567e-05	br= 2	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8 th=-2.72392e-05	br= 3	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9 th=-4.35097e-06	br= 3	:	-0.000006	-0.000002	0.000002	0.000006
dp=10 th=+1.37108e-06	br= 0	:	-0.000001	-0.000000	0.000000	0.000001
dp=11 th=-5.9435e-08						

\* deallocate nodes in the leafmin path



```
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
tcl_power2_4ary_i7 R=4 i=7
;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;;
quaternary angle tree search (N=12)
theta= atan(pow(2,-7) = 0.00781234
```

```
.....
* A: the leaf optimal path R=4 i=7
.....
* leaf min node : depth= 11 theta= +1.672965e-07 id=3668103
```

```
path type : leafmin
dp= 0 th=+0.00781234 br= 2 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=+0.329563 br= 0 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=-0.0397708 br= 2 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=-0.00859179 br= 2 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=-0.000780398 br= 2 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=+0.00117271 br= 0 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=-0.000292134 br= 3 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+7.40771e-05 br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=-1.74757e-05 br= 3 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=+5.41251e-06 br= 0 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=-3.09541e-07 br= 2 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=+1.67297e-07
```

```
.....
* B: the global optimal path R=4 i=7
.....
level min node : depth= 0 theta= +7.812341e-03 id=0
level min node : depth= 1 theta= -3.139382e-01 id=2
level min node : depth= 2 theta= -3.977076e-02 id=13
level min node : depth= 3 theta= -8.591786e-03 id=55
level min node : depth= 4 theta= +7.803981e-04 id=201
level min node : depth= 5 theta= +1.172710e-03 id=895
level min node : depth= 6 theta= +2.921339e-04 id=3228
level min node : depth= 7 theta= +7.407706e-05 id=14328
level min node : depth= 8 theta= +1.747568e-05 id=51656
level min node : depth= 9 theta= +5.412505e-06 id=229256
level min node : depth= 10 theta= +3.095406e-07 id=826504
level min node : depth= 11 theta= +1.672965e-07 id=3668103
```

```
* global min node : depth= 11 theta= +1.672965e-07 id=3668103
```

```
path type : globalmin
dp= 0 th=+0.00781234 br= 2 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=+0.329563 br= 0 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=-0.0397708 br= 2 : -0.093659 -0.031179 0.031179 0.093659
dp= 3 th=-0.00859179 br= 2 : -0.023436 -0.007811 0.007811 0.023436
dp= 4 th=-0.000780398 br= 2 : -0.005859 -0.001953 0.001953 0.005859
dp= 5 th=+0.00117271 br= 0 : -0.001465 -0.000488 0.000488 0.001465
dp= 6 th=-0.000292134 br= 3 : -0.000366 -0.000122 0.000122 0.000366
dp= 7 th=+7.40771e-05 br= 0 : -0.000092 -0.000031 0.000031 0.000092
dp= 8 th=-1.74757e-05 br= 3 : -0.000023 -0.000008 0.000008 0.000023
dp= 9 th=+5.41251e-06 br= 0 : -0.000006 -0.000002 0.000002 0.000006
dp=10 th=-3.09541e-07 br= 2 : -0.000001 -0.000000 0.000000 0.000001
dp=11 th=+1.67297e-07
```

```
.....
* C: the cordic path R=4 i=7
.....
* cordic min node : depth= 11 theta= -1.672965e-07 id=3306017
```

```
path type : cordic
dp= 0 th=+0.00781234 br= 1 : -1.249046 -0.321751 0.321751 1.249046
dp= 1 th=-0.313938 br= 3 : -0.369334 -0.120624 0.120624 0.369334
dp= 2 th=+0.0553954 br= 1 : -0.093659 -0.031179 0.031179 0.093659
```

```

dp= 3 th=+0.0242165      br= 0 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=+0.000780398    br= 1 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.00117271    br= 3 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000292134   br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-7.40771e-05   br= 3 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.74757e-05   br= 0 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=-5.41251e-06   br= 3 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+3.09541e-07   br= 1 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-1.67297e-07

```

```

* deallocate nodes in the leafmin path
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path

```

```

////////////////////////////////////
tcl_power2_4ary_i8 R=4 i=8
////////////////////////////////////
quaternary angle tree search (N=12)
theta= atan(pow(2,-8) = 0.00390623

```

```

.....
* A: the leaf optimal path R=4 i=8
.....
* leaf min node : depth= 11 theta= -6.299368e-08 id=3310114

```

```

path type : leafmin
dp= 0 th=+0.00390623      br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=-0.317844      br= 3 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0514893     br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=+0.0203104     br= 0 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.00312571    br= 2 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.00117261    br= 3 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000292238   br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-7.39728e-05   br= 3 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.758e-05     br= 0 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=-5.3082e-06    br= 3 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+4.13843e-07   br= 1 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-6.29937e-08

```

```

.....
* B: the global optimal path R=4 i=8
.....
level min node : depth= 0 theta= +3.906230e-03 id=0
level min node : depth= 1 theta= -3.178443e-01 id=2
level min node : depth= 2 theta= -4.367687e-02 id=13
level min node : depth= 3 theta= -1.249790e-02 id=55
level min node : depth= 4 theta= -3.125713e-03 id=201
level min node : depth= 5 theta= -1.172605e-03 id=807
level min node : depth= 6 theta= -2.919998e-04 id=3585
level min node : depth= 7 theta= -7.397275e-05 id=12929
level min node : depth= 8 theta= -1.734157e-05 id=57377
level min node : depth= 9 theta= -5.308202e-06 id=206881
level min node : depth= 10 theta= -1.754358e-07 id=918049
level min node : depth= 11 theta= -6.299368e-08 id=3310114

```

```

* global min node : depth= 11 theta= -6.299368e-08 id=3310114

```

```

path type : globalmin
dp= 0 th=+0.00390623      br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=-0.317844      br= 3 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0514893     br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=+0.0203104     br= 0 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.00312571    br= 2 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.00117261    br= 3 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000292238   br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-7.39728e-05   br= 3 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.758e-05     br= 0 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=-5.3082e-06    br= 3 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+4.13843e-07   br= 1 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-6.29937e-08

```

```

.....
* C: the cordic path R=4 i=8
.....
* cordic min node : depth= 11 theta= -6.299368e-08 id=3310113

```

```

path type : cordic
dp= 0 th=+0.00390623    br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=-0.317844    br= 3 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0514893   br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=+0.0203104   br= 0 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.00312571  br= 2 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=-0.00117261  br= 3 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000292238 br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-7.39728e-05 br= 3 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.758e-05   br= 0 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=-5.3082e-06  br= 3 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+4.13843e-07 br= 1 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-6.29937e-08

```

```

* deallocate nodes in the leafmin path
* deallocate nodes in the globalmin path
* deallocate nodes in the cordic path
////////////////////////////////////
tcl_power2_4ary_i9 R=4 i=9
////////////////////////////////////
quaternary angle tree search (N=12)
theta= atan(pow(2,-9) = 0.00195312

```

```

.....
* A: the leaf optimal path R=4 i=9
.....
* leaf min node : depth= 11 theta= -4.995533e-08 id=3312162

```

```

path type : leafmin
dp= 0 th=+0.00195312    br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=-0.319797    br= 3 : -0.369334 -0.120624  0.120624  0.369334
dp= 2 th=+0.0495362   br= 1 : -0.093659 -0.031179  0.031179  0.093659
dp= 3 th=+0.0183572   br= 0 : -0.023436 -0.007811  0.007811  0.023436
dp= 4 th=-0.00507882  br= 3 : -0.005859 -0.001953  0.001953  0.005859
dp= 5 th=+0.000780532 br= 1 : -0.001465 -0.000488  0.000488  0.001465
dp= 6 th=+0.000292251 br= 0 : -0.000366 -0.000122  0.000122  0.000366
dp= 7 th=-7.39597e-05 br= 3 : -0.000092 -0.000031  0.000031  0.000092
dp= 8 th=+1.7593e-05  br= 0 : -0.000023 -0.000008  0.000008  0.000023
dp= 9 th=-5.29516e-06 br= 3 : -0.000006 -0.000002  0.000002  0.000006
dp=10 th=+4.26882e-07 br= 1 : -0.000001 -0.000000  0.000000  0.000001
dp=11 th=-4.99553e-08

```

```

.....
* B: the global optimal path R=4 i=9
.....
level min node : depth= 0 theta= +1.953123e-03 id=0
level min node : depth= 1 theta= -3.197974e-01 id=2
level min node : depth= 2 theta= -4.562998e-02 id=13
level min node : depth= 3 theta= -1.445100e-02 id=55
level min node : depth= 4 theta= -5.078820e-03 id=201
level min node : depth= 5 theta= -7.802640e-04 id=896
level min node : depth= 6 theta= -2.919830e-04 id=3587
level min node : depth= 7 theta= -7.395971e-05 id=12937
level min node : depth= 8 theta= -1.732481e-05 id=57409
level min node : depth= 9 theta= -5.295164e-06 id=207009
level min node : depth= 10 theta= -1.586722e-07 id=918561
level min node : depth= 11 theta= -4.995533e-08 id=3312162

```

```

* global min node : depth= 11 theta= -4.995533e-08 id=3312162

```

```

path type : globalmin
dp= 0 th=+0.00195312    br= 1 : -1.249046 -0.321751  0.321751  1.249046
dp= 1 th=-0.319797    br= 3 : -0.369334 -0.120624  0.120624  0.369334

```

dp= 2 th=+0.0495362	br= 1	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3 th=+0.0183572	br= 0	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4 th=-0.00507882	br= 3	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5 th=+0.000780532	br= 1	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6 th=+0.000292251	br= 0	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7 th=-7.39597e-05	br= 3	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8 th=+1.7593e-05	br= 0	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9 th=-5.29516e-06	br= 3	:	-0.000006	-0.000002	0.000002	0.000006
dp=10 th=+4.26882e-07	br= 1	:	-0.000001	-0.000000	0.000000	0.000001
dp=11 th=-4.99553e-08						

.....

\* C: the cordic path R=4 i=9

.....

\* cordic min node : depth= 11 theta= -4.995533e-08 id=3312161

path type : cordic

dp= 0 th=+0.00195312	br= 1	:	-1.249046	-0.321751	0.321751	1.249046
dp= 1 th=-0.319797	br= 3	:	-0.369334	-0.120624	0.120624	0.369334
dp= 2 th=+0.0495362	br= 1	:	-0.093659	-0.031179	0.031179	0.093659
dp= 3 th=+0.0183572	br= 0	:	-0.023436	-0.007811	0.007811	0.023436
dp= 4 th=-0.00507882	br= 3	:	-0.005859	-0.001953	0.001953	0.005859
dp= 5 th=+0.000780532	br= 1	:	-0.001465	-0.000488	0.000488	0.001465
dp= 6 th=+0.000292251	br= 0	:	-0.000366	-0.000122	0.000122	0.000366
dp= 7 th=-7.39597e-05	br= 3	:	-0.000092	-0.000031	0.000031	0.000092
dp= 8 th=+1.7593e-05	br= 0	:	-0.000023	-0.000008	0.000008	0.000023
dp= 9 th=-5.29516e-06	br= 3	:	-0.000006	-0.000002	0.000002	0.000006
dp=10 th=+4.26882e-07	br= 1	:	-0.000001	-0.000000	0.000000	0.000001
dp=11 th=-4.99553e-08						

\* deallocate nodes in the leafmin path

\* deallocate nodes in the globalmin path

\* deallocate nodes in the cordic path