

Monad P2: State Monad Methods (2B)

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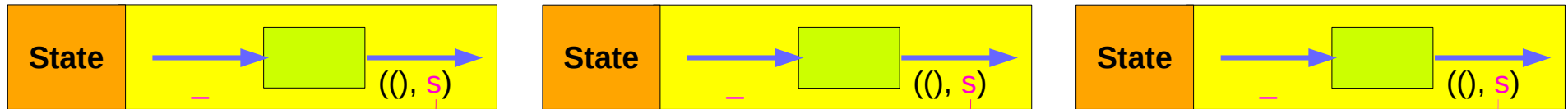
Based on

Haskell in 5 steps

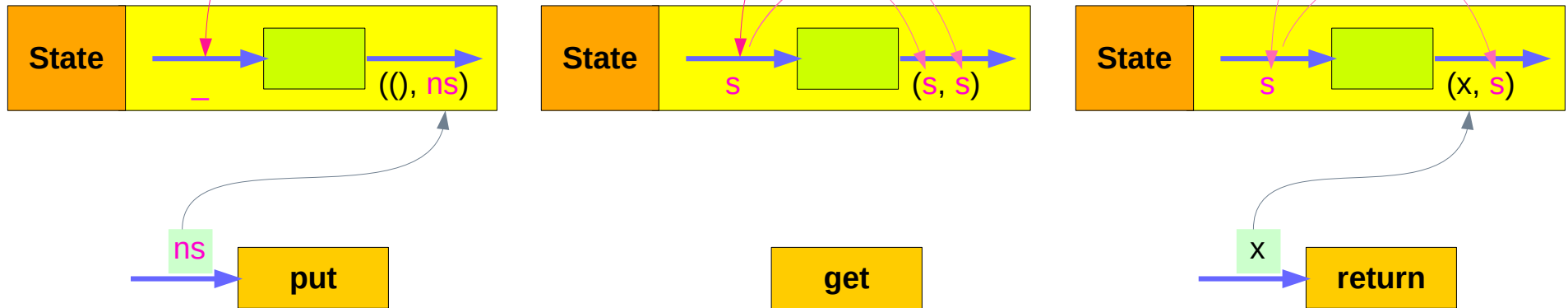
https://wiki.haskell.org/Haskell_in_5_steps

put, get, return methods summary

initial monadic value



return monadic value



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

put changes the current state

`put :: s -> State s a`

`put ns = state $ _ -> ((), ns)`

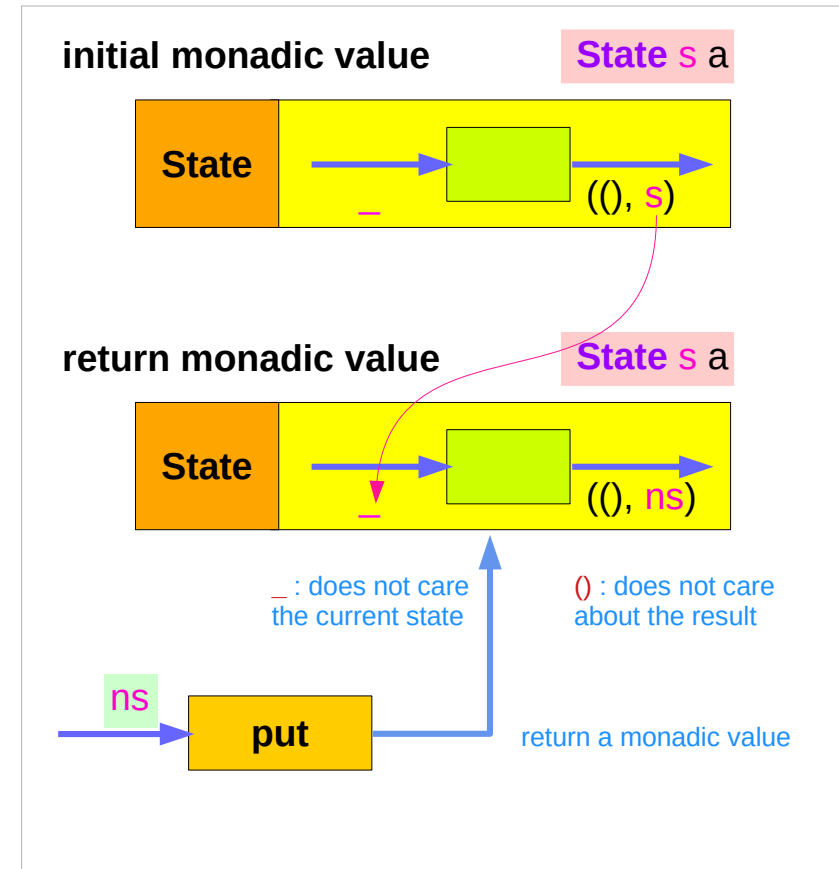
Given a wanted `state new State (ns)`,

`put` generates a `state processor`

- ignores whatever the `state` it receives,
- updates the `state` to `ns`
- doesn't care about the `result` of this processor

- all we want to do is to change the `state`
- the tuple will be `((), ns)`
- `()` : the **universal placeholder value**.

https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State



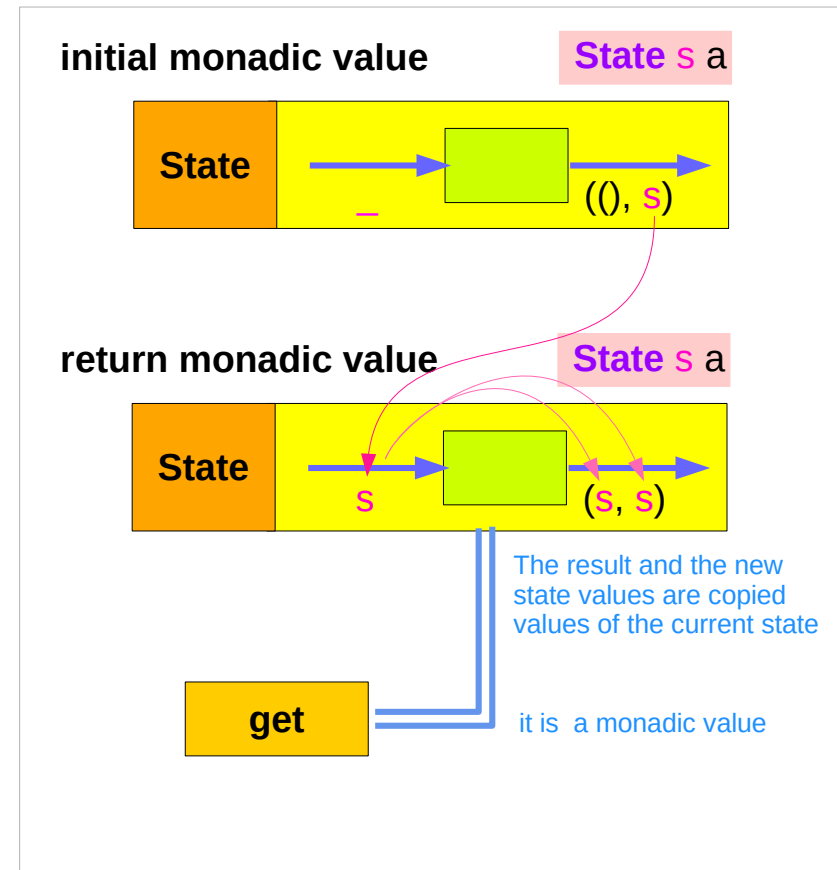
get gives the current state

`get :: State s a`

`get = state $ \s -> (s, s)`

`get` generates a **state processor**

- gives back the **state** `s0`
- as a **result** and as an updated **state** – `(s0, s0)`
- the **state** will remain unchanged
- a copy of the **state** will be made available through the **result** returned



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

return changes the result value

`return` :: $a \rightarrow \text{State } s \ a$

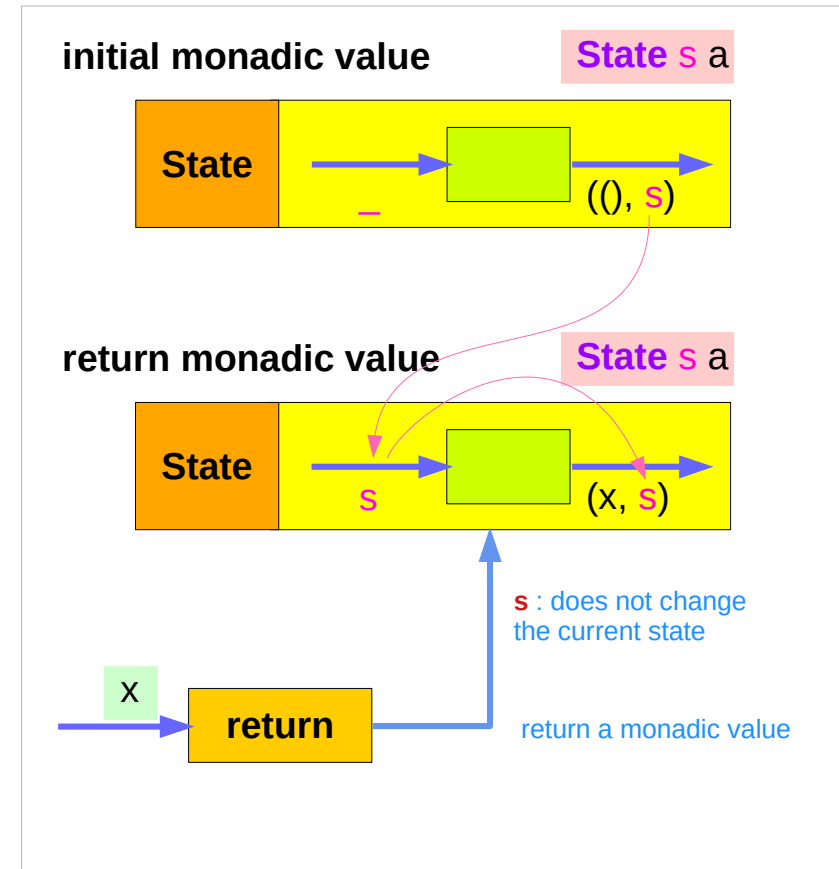
`return` $x = \text{state } (\backslash s \rightarrow (x, s))$

giving a value (x) to `return`

results in a `state processor` function

which takes a state (s) and
returns it unchanged (s),
together with the value x

finally, the function is wrapped up by `state`.



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

put returns a monadic value via state

```
put :: s -> State s a
```

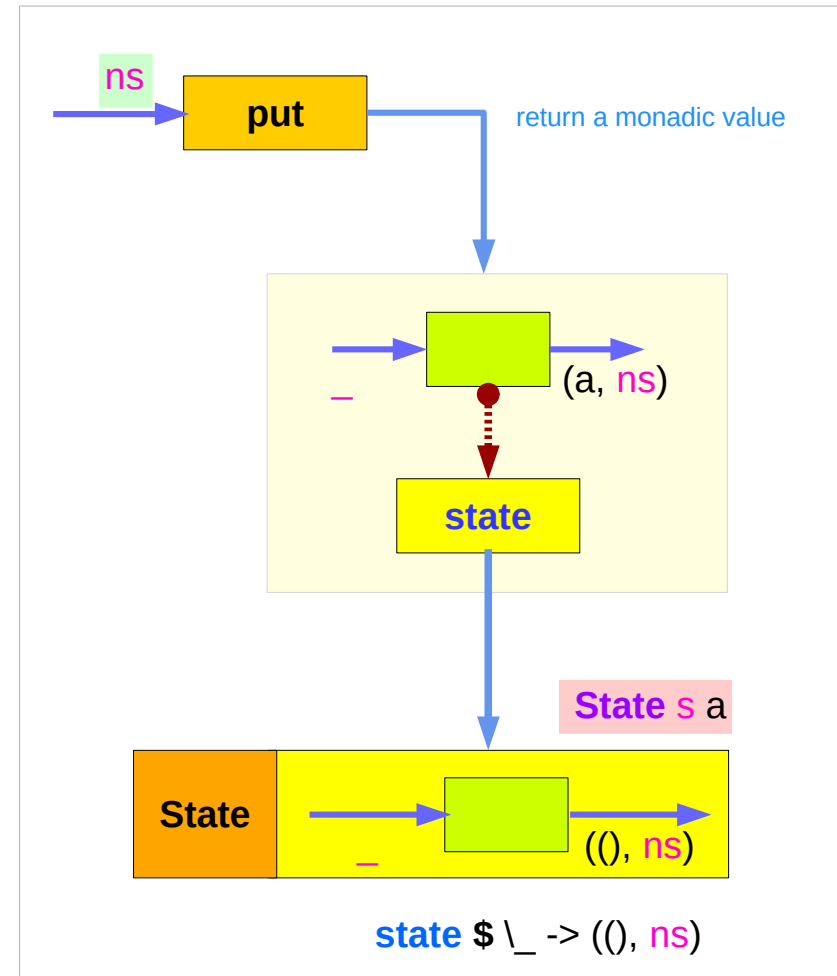
```
put s :: State s a
```

```
put ns = state $ \_ -> ((), ns)
```

```
-- setting a state to ns
```

```
-- regardless of the old state
```

```
-- setting the result to ()
```



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

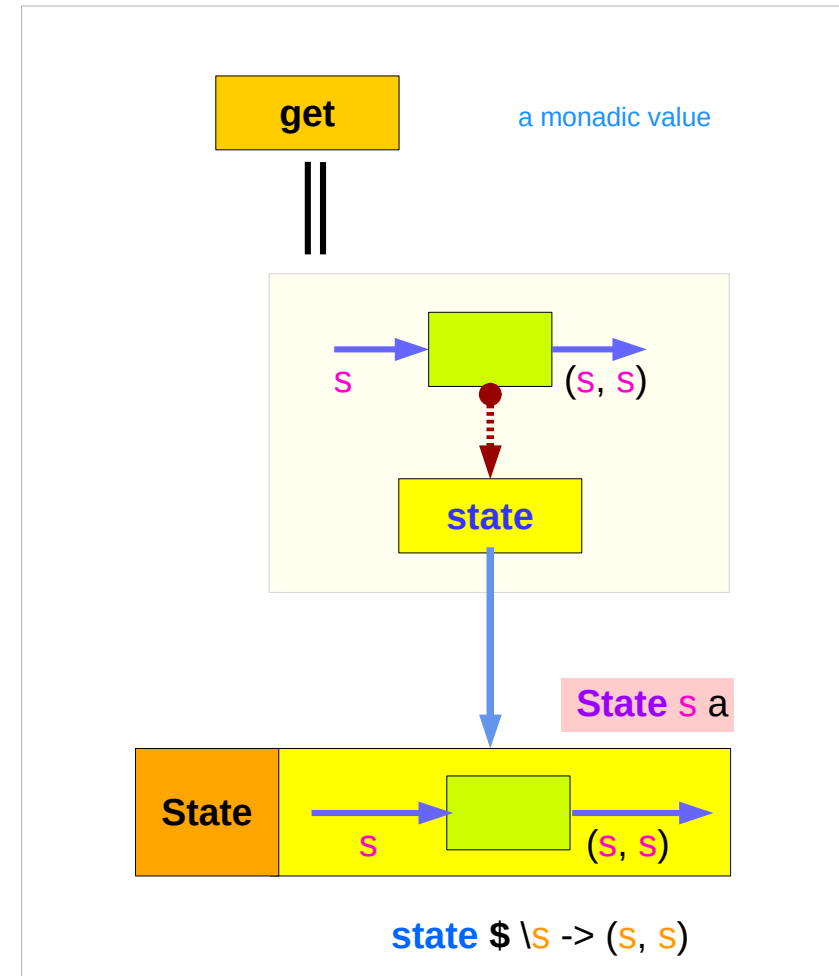
get is a monadic value via state

`get :: State s s`

`get = state $ \s -> (s, s)`

-- getting the current state `s`

-- also setting the result to `s`



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

return returns a monadic value via state

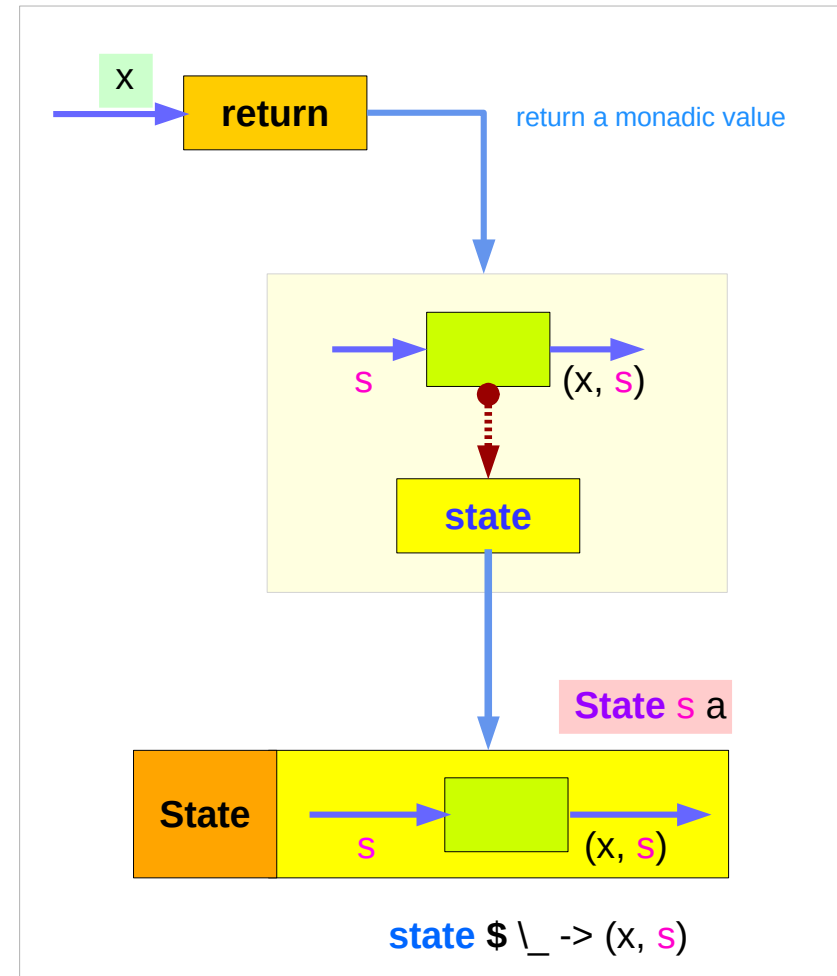
`return :: s -> State s a`

`return s :: State s a`

`return x = state $ _ -> (x, s)`

-- do not change a state s

-- setting the result to x



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Threading `put` via `runState`

`put :: s -> State s a`

`put s :: State s a`

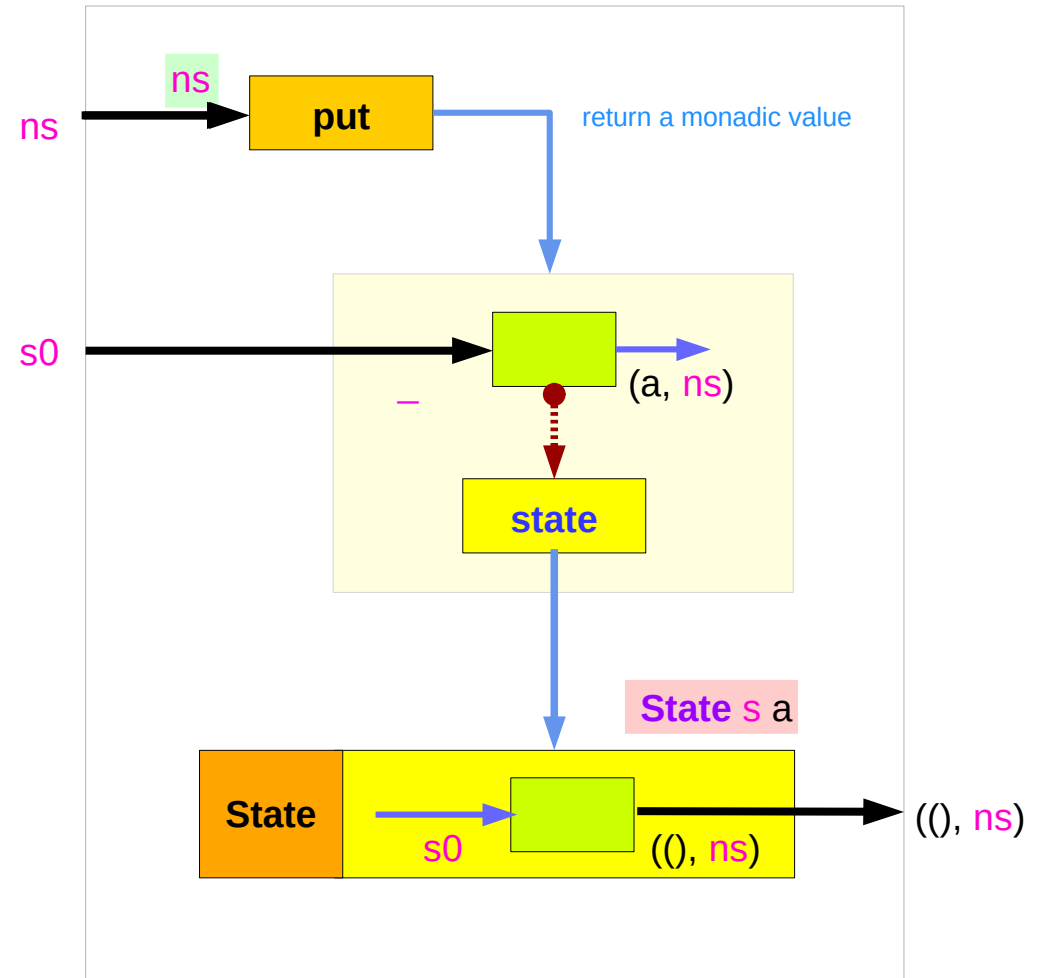
`put newState = state $ _ -> ((), newState)`

`runState (put ns) s0`

`runState (put 5) 1`

`((),5)`

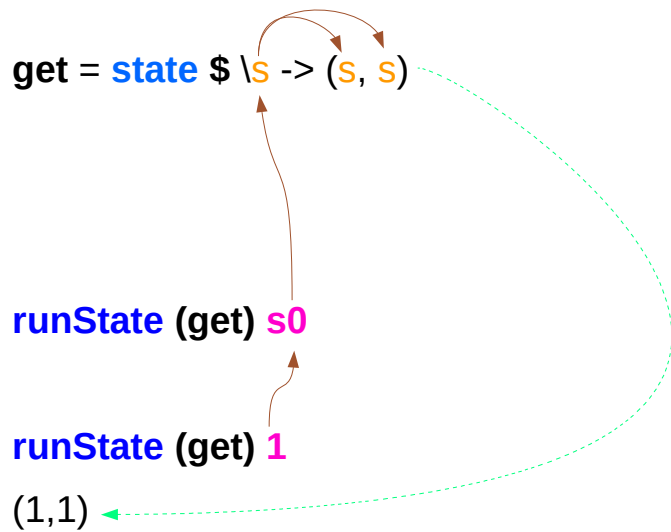
Initial state `s0` can be supplied either by `runState` or by the initial monadic value



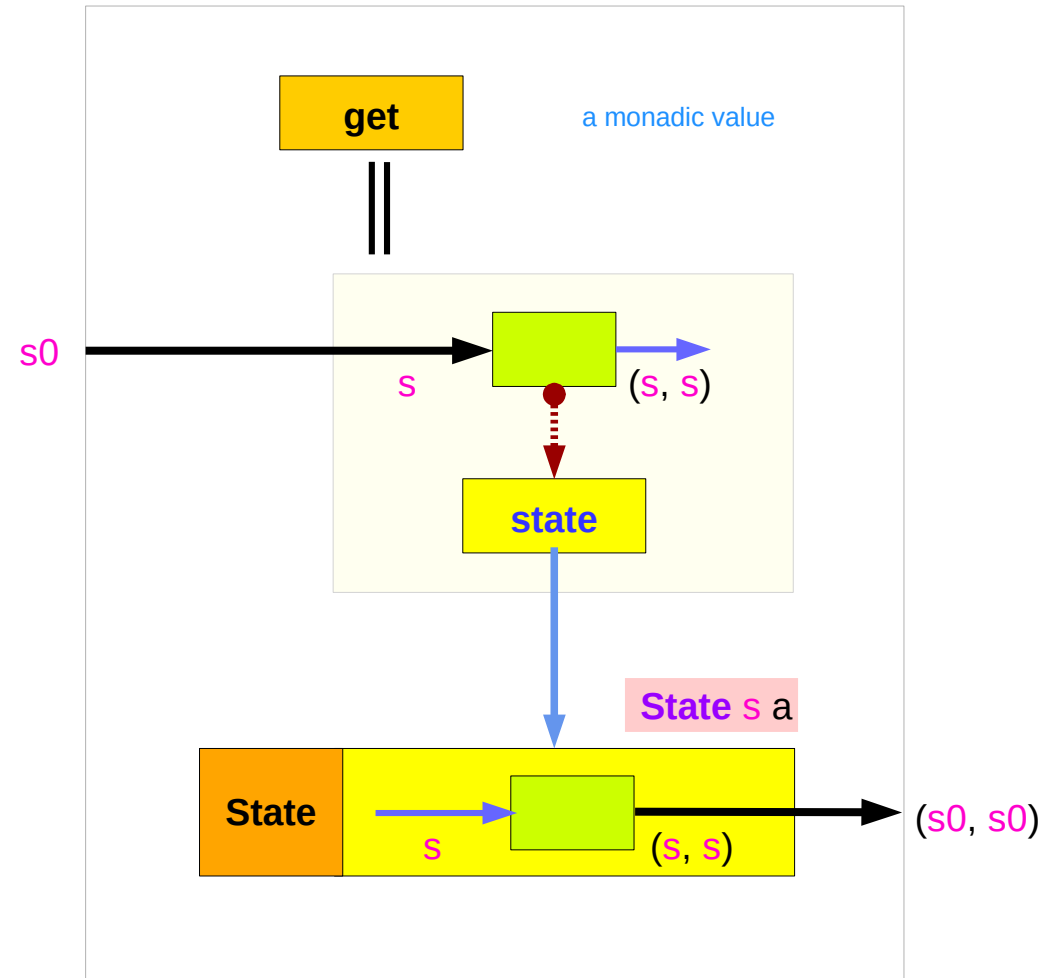
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Running `get` via `runState`

`get :: State s s`



Initial state `s0` can be supplied either by `runState` or by the initial monadic value



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Running `return` via `runState`

`return :: s -> State s a`

`return s :: State s a`

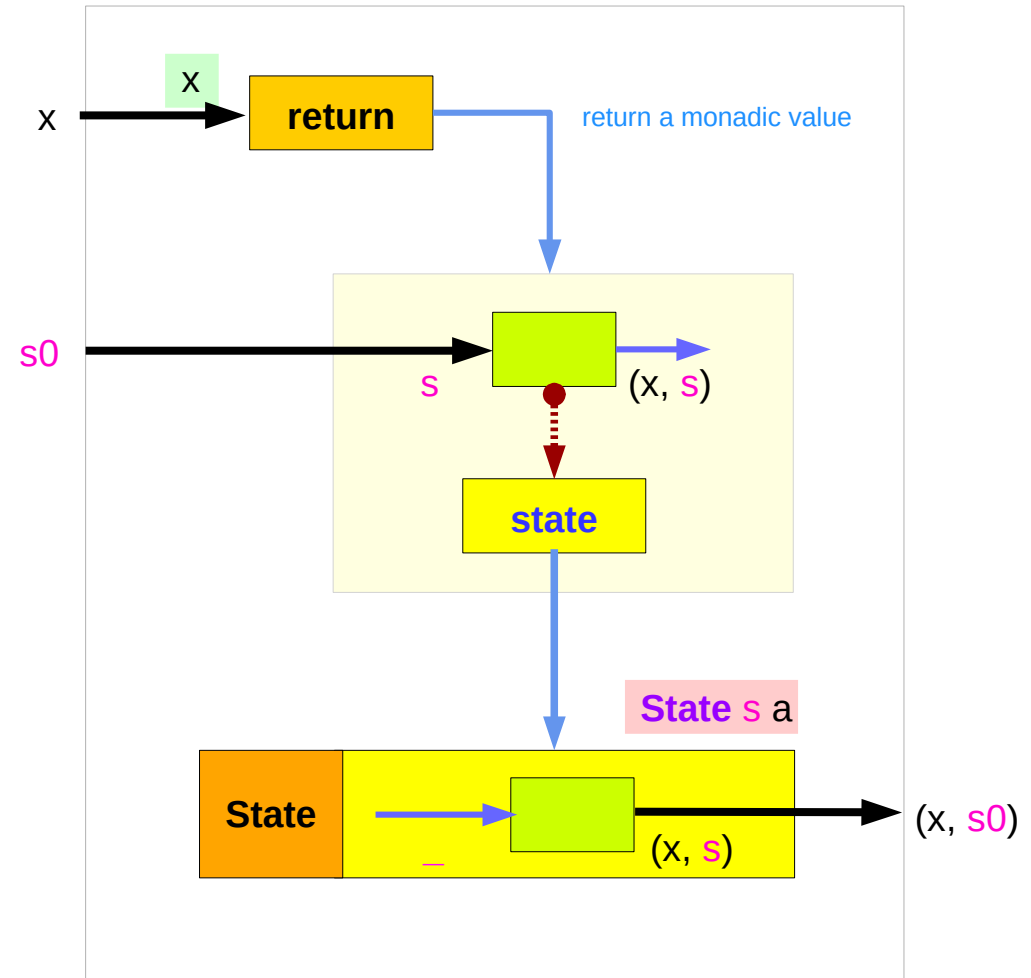
`return x = state $ _ -> (x, s)`

`runState (return x) s0`

`runState (return 3) 1`

`(3,1)`

Initial state `s0` can be supplied either by `runState` or by the initial **monadic value**



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Example codes (1)

```
import Control.Monad.Trans.State
```

```
runState get 1
```

```
(1,1)
```

```
runState (return 'X') 1
```

```
('X',1)
```

```
runState get 1
```

```
(1,1)
```

```
runState (put 5) 1
```

```
((),5)
```

```
runState (put 1 >> get >> put 2 >> get ) 0
```

```
(2,2)
```

```
runState (get >>= \n -> put (n+1) >> return n) 0
```

```
(0,1)
```

```
inc = get >>= \n -> put (n+1) >> return n
```

```
runState inc 0
```

```
(0,1)
```

```
runState (inc >> inc) 0
```

```
(1,2)
```

```
runState (inc >> inc >> inc) 0
```

```
(2,3)
```

https://wiki.haskell.org/State_Monad

Example codes (2)

```
import Control.Monad.Trans.State
```

```
let postincrement = do { x <- get; put (x+1); return x }
```

```
runState postincrement 1
```

```
(1,2)
```

```
get : (1,1) → (1,2)
```

```
let predecrement = do { x <- get; put (x-1); get }
```

```
runState predecrement 1
```

```
(0,0)
```

```
(1,_) → get : (0, 0)
```

```
runState (modify (+1)) 1
```

```
((),2)
```

```
runState (gets (+1)) 1
```

```
(2,1)
```

```
evalState (gets (+1)) 1
```

```
2
```

```
execState (gets (+1)) 1
```

```
1
```

evalState (a, s) computes the result

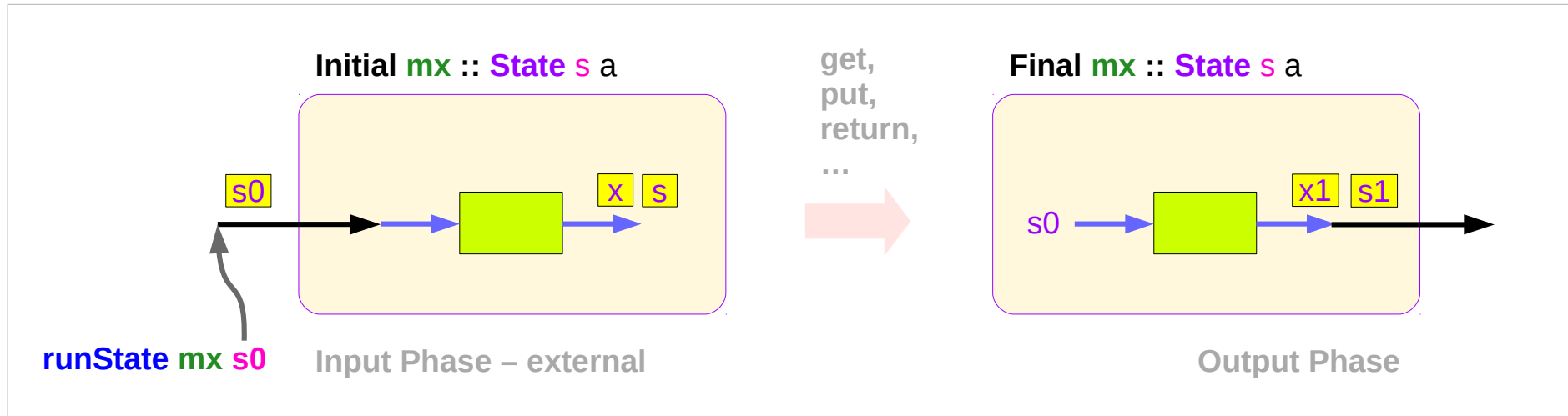
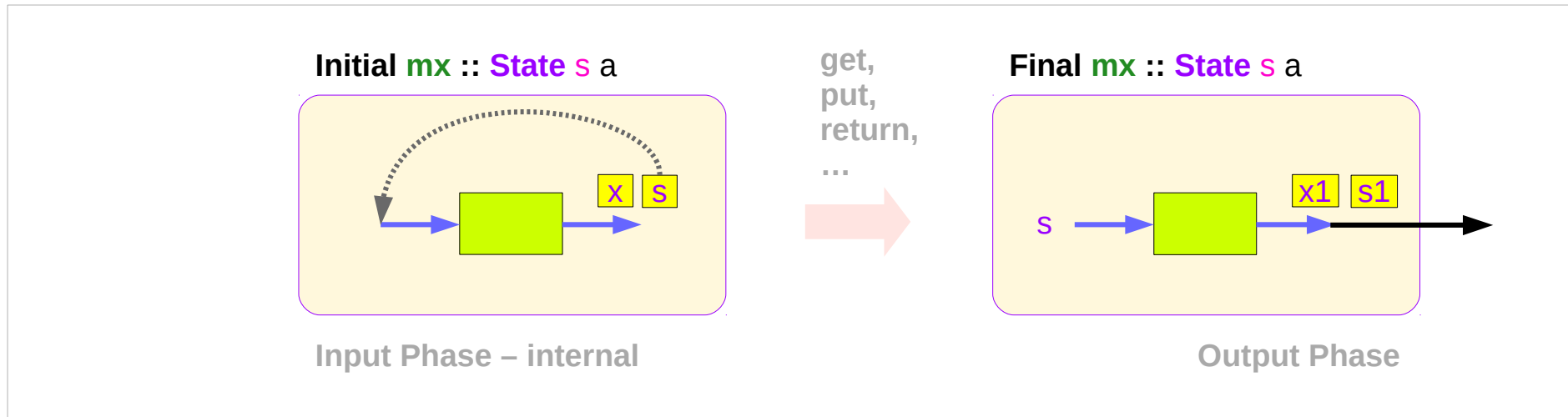
execState (a, s) updates state

modify state ((), f x)

get state (f x, s)

https://wiki.haskell.org/State_Monad

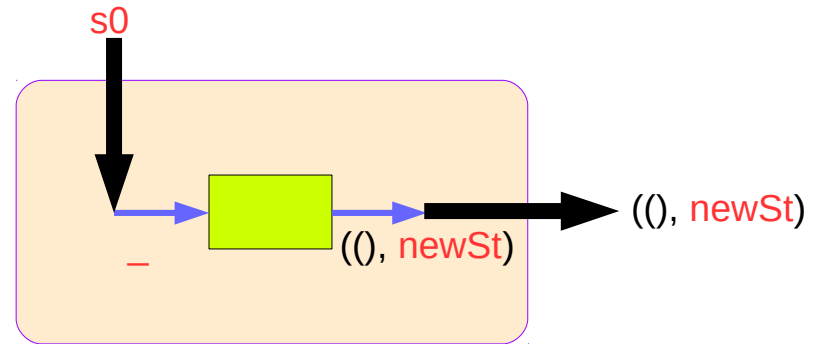
Think two phases (input, output)



Executing the state processor – put

```
put :: s -> State s a
put newSt = state $ \_ -> ((), newSt)

runState (put newSt) s0  →  ((), newSt)
```



applying the function

```
runState (put 5) 1
```

```
((),5)
```

set the result value to () and set the state value.

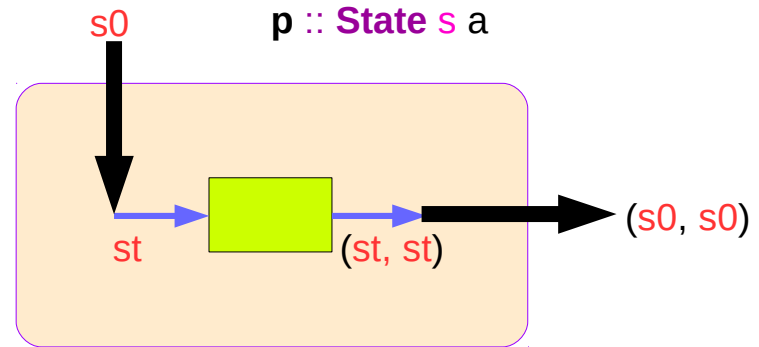
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Executing the state processor – get

`get :: State s s`

`get = state $ \s -> (s, s)`

`runState (get) s0` \rightarrow `(s0, s0)`



applying the function

`runState get 1`

`(1,1)`

set the result value to the state and leave the state unchanged.

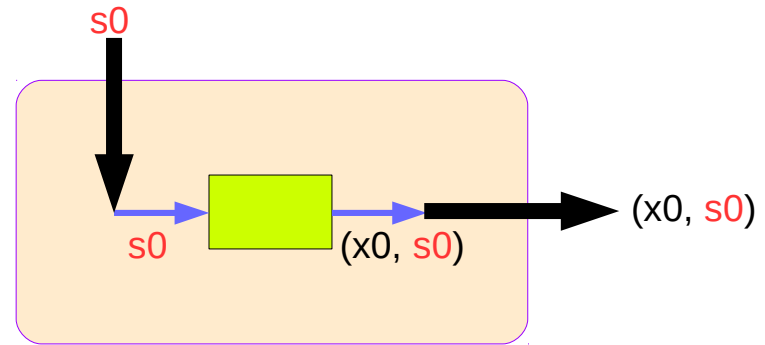
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

Executing the state processor – return

`return :: s -> State s a`

`return x = state $ s -> (x, s)`

`runState (return x0) s0` \rightarrow `(x, s)`



applying the function

`runState return 3 1`

`(3,1)`

set the new result value and leave the state unchanged.

https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

State Monad Examples – put

```
runState (put 5) 1
```

```
((),5)
```

set the result value to () and set the state value.

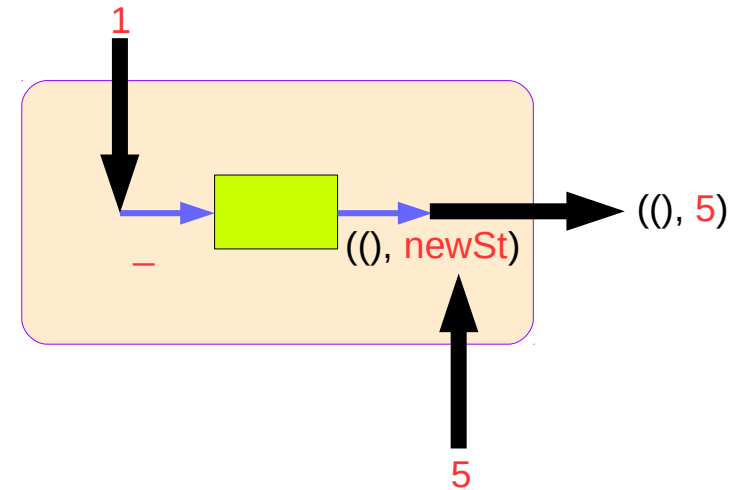
```
put 5 :: State Int ()
```

```
runState (put 5) :: Int -> ((),Int)
```

```
initial state = 1 :: Int
```

```
final value = () :: ()
```

```
final state = 5 :: Int
```



```
put :: s -> State s a
```

```
put newState = state $ \_ -> ((), newState)
```

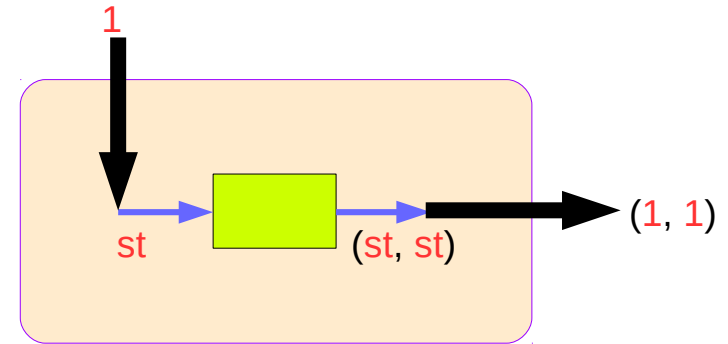
https://wiki.haskell.org/State_Monad

State Monad Examples – get

`runState get 1`

`(1,1)`

set the result value to the state and leave the state unchanged.



```
get :: State Int Int
runState get :: Int -> (Int, Int)
initial state = 1 :: Int
final value = 1 :: Int
final state = 1 :: Int
```

`get :: State s s`

`get = state $ \s -> (s, s)`

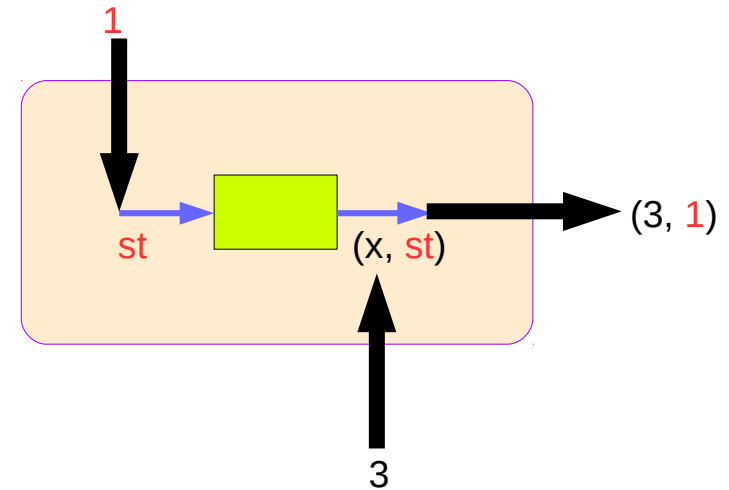
https://wiki.haskell.org/State_Monad

State Monad Examples – return

`runState return 3 1`

`(3,1)`

set the new result value and leave the state unchanged.



`return :: Int -> State Int Int`

`runState return 3 :: Int -> (Int, Int)`

`initial state = 1 :: Int`

`final value = 3 :: Int`

`final state = 1 :: Int`

`return :: s -> State s a`

`return x = state $ s -> (x, s)`

https://wiki.haskell.org/State_Monad

Think an unwrapped state processor

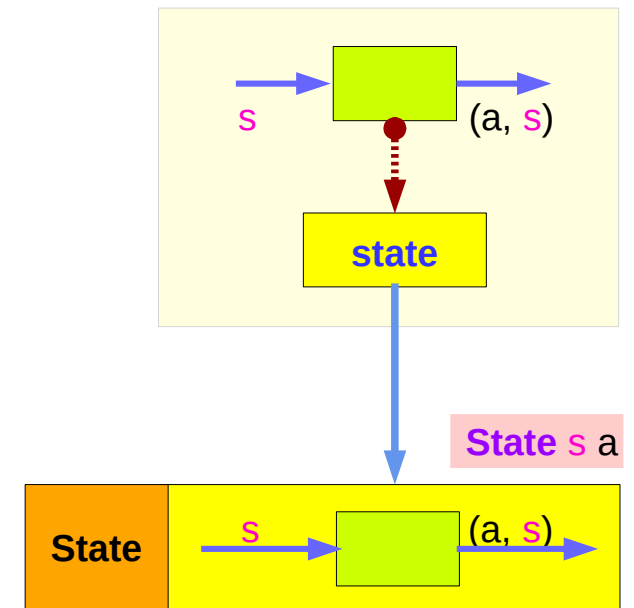
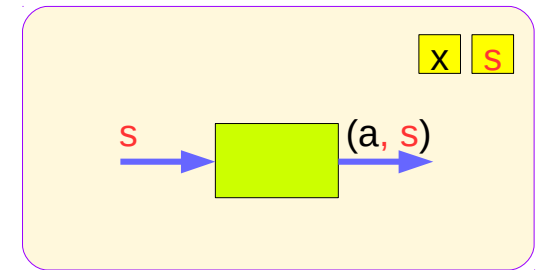
(return 5) \rightarrow `1 -> (5,1)` -- a way of thinking Think an **unwrapped** state processor
get \rightarrow `1 -> (1,1)` -- a way of thinking
(put 5) \rightarrow `1 -> ((),5)` -- a way of thinking

a value of type (`State s a`) is
a **function** from **initial state** `s`
to **final value** `a` and **final state** `s`: `(a,s)`.

these are usually wrapped,
but shown here unwrapped for simplicity.

(return 5) \rightarrow `state(1 -> (5,1))` -- an actual impl **wrapping** the state processor
get \rightarrow `state(1 -> (1,1))` -- an actual impl
(put 5) \rightarrow `state(1 -> ((),5))` -- an actual implementation

https://wiki.haskell.org/State_Monad



Unwrapped Implementation Examples

```
return :: a -> State s a
```

```
return x s = (x,s)
```

```
get :: State s s
```

```
get s = (s,s)
```

```
put :: s -> State s ()
```

```
put x s = ((),x)
```

```
modify :: (s -> s) -> State s ()
```

```
modify f = do { x <- get; put (f x) }
```

```
gets :: (s -> a) -> State s a
```

```
gets f = do { x <- get; return (f x) }
```

- inside a monad instance
- unwrapped implementations

```
return → (x,s)
```

```
get → (s, s)
```

```
put → ((),s)
```

modify

```
x <- get; put (f x) - state
```

gets

```
x <- get; return (f x) - result
```


https://wiki.haskell.org/State_Monad

State Monad Examples – return, get, and put


Return leaves the state unchanged and sets the result:

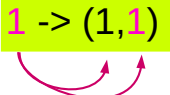
-- ie: (return 5)  1 -> (5,1) -- a way of thinking



runState (return 5) 1  (5,1)

Get leaves state unchanged and sets the result to the state:

-- ie: get  1 -> (1,1) -- a way of thinking




runState get 1  (1,1)

Put sets the result to () and sets the state:

-- ie: (put 5)  1 -> ((),5) -- a way of thinking



runState (put 5) 1  ((),5)

https://wiki.haskell.org/State_Monad

State Monad Examples – modify and gets

```
runState (modify (+1)) 1 → ((), 2)
      (+1) 1 → 2 :: s
```

```
runState (gets (+1)) 1 → (2, 1)
      (+1) 1 → 2 :: a
```

```
evalState (modify (+1)) 1 → ()
      → s :: state      fst ((), 2)
```

```
execState (modify (+1)) 1 → 2
      → a :: result      snd ((), 2)
```

```
evalState (gets (+1)) 1 → 2
      → s :: state      fst (2, 1)
```

```
execState (gets (+1)) 1 → 1
      → a :: result      snd (2, 1)
```

```
modify state  ((), f x)
get state     (f x, s)
```

```
evalState    (a, s)
              computes the result
execState    (a, s)
              updates state
```

```
( a ,  s )
(eval, exec)
(get, modify)
```

https://wiki.haskell.org/State_Monad

State Monad Examples – put, get, modify

`execState get 0`

→ 0

(0,0)

set the value of the counter using put:

`execState (put 1) 0`

→ 1

((),1)

set the state multiple times:

`execState (do put 1; put 2) 0`

→ 2

((),1) → ((), 2)

modify the state based on its current value:

`execState (do x <- get; put (x + 1)) 0`

→ 1

(0,0) → ((),1)

`execState (do modify (+ 1)) 0`

→ 1

((),1)

`execState (do modify (+ 2); modify (* 5)) 0`

→ 10

((),2) → ((),10)

<https://stackoverflow.com/questions/25438575/states-put-and-get-functions>

A Stateful Computation

a **stateful computation** is a **function** that takes some **state** and returns a **value** along with some **new state**.

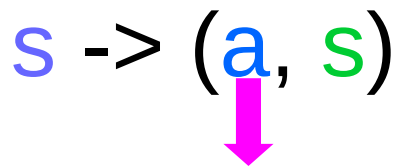
That function would have the following type:

$s \rightarrow (a, s)$

s is the type of the **state** and

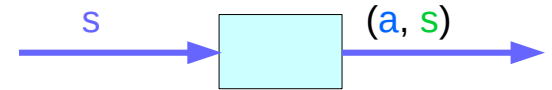
a the **result** of the **stateful computation**.

$s \rightarrow (a, s)$



<http://learnyouahaskell.com/for-a-few-monads-more>

$s \rightarrow (a, s)$



a function is an executable data
when executed, a result is produced
action, execution, result

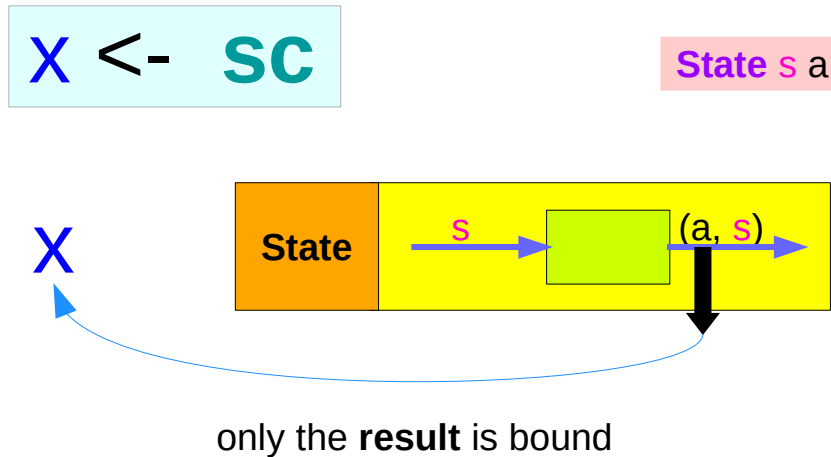
Stateful Computations inside the State Monad

inside a monad,

when `sc` is a **stateful computation**

then the **result** of the stateful computation `sc`

can be assigned to `x`



`x <- sc`

`sc :: State s a`

`x :: a` (the execution result of `sc`)

~~`x :: State s a`~~

`s -> (a, s)`

the result type

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

get inside the State Monad

inside the **State** monad,

get returns **State** monadic value whose new state and result values are the current state value

```
x <- get
```

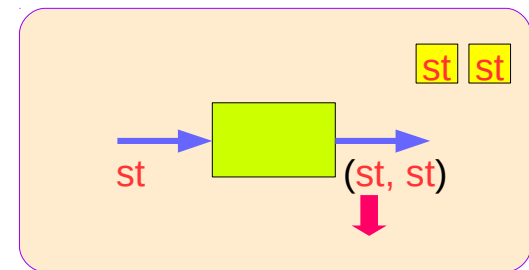
the **stateful computation** is performed over the monadic value returned by **get**

the result of the **stateful computation** of **get** is **st::s**, thus **x** will get the **st**

this is like **evalState** is called with the current monad instance

- **get** executed
- **State monadic value**
- **stateful computation**
- **result :: s**

x :: a the execution result of **get**



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

put inside State Monad

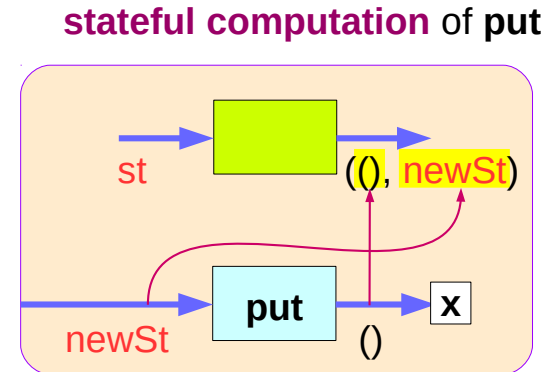
```
put :: s -> State s a  
put newSt = state $ \_ -> ((), newSt)
```

```
in x <- put newSt
```

```
put :: s -> ()
```

```
the result type :: ()
```

-- a way of thinking



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

get inside State Monad

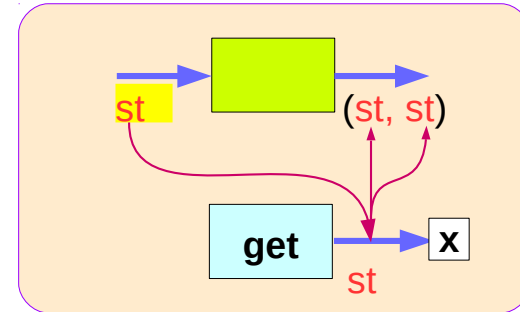
```
get :: State s s  
get = state $ \s -> (s, s)
```

```
in x <- get
```

```
get :: s  
the result type :: s
```

-- a way of thinking

stateful computation of get



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

return inside State Monad

```
put :: s -> State s a  
put newSt = state $ \_ -> ((), newSt)
```

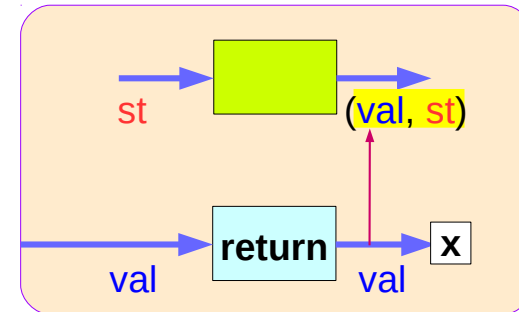
```
in x <- return val
```

```
return :: s -> s
```

```
the result type :: s
```

-- a way of thinking

stateful computation of put



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

run functions inside a Monad

Most monads have some "*run*" functions such as `runState`, `execState`, and so forth.

frequent calling such functions inside the monad indicates that the **functionality** of the monad does not fully exploited

```
s0 <- get                -- read the state of the current instance
let (a,s1) = runState p s0 -- pass the state to p, get new state
put s1                  -- save new state
return a

a <- p                  -- the stateful computation p updates the state to s1
                        -- the result of the state returned is assigned to a
```

`let p = state (ly -> (y, y+1))`

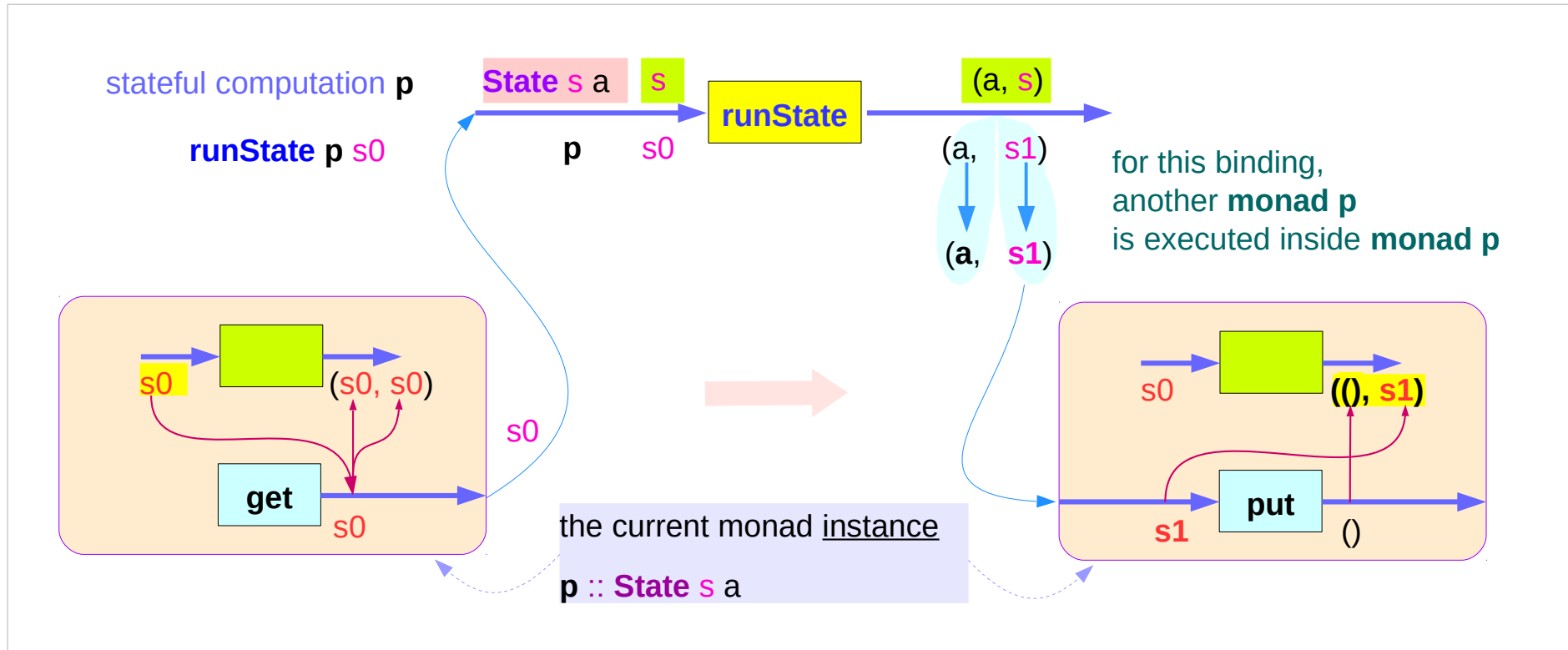
<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Redundant computation examples (1)

```
s0 <- get  
let (a, s1) = runState p s0  
put s1
```

the same binding variable **a**
the same state **s1**

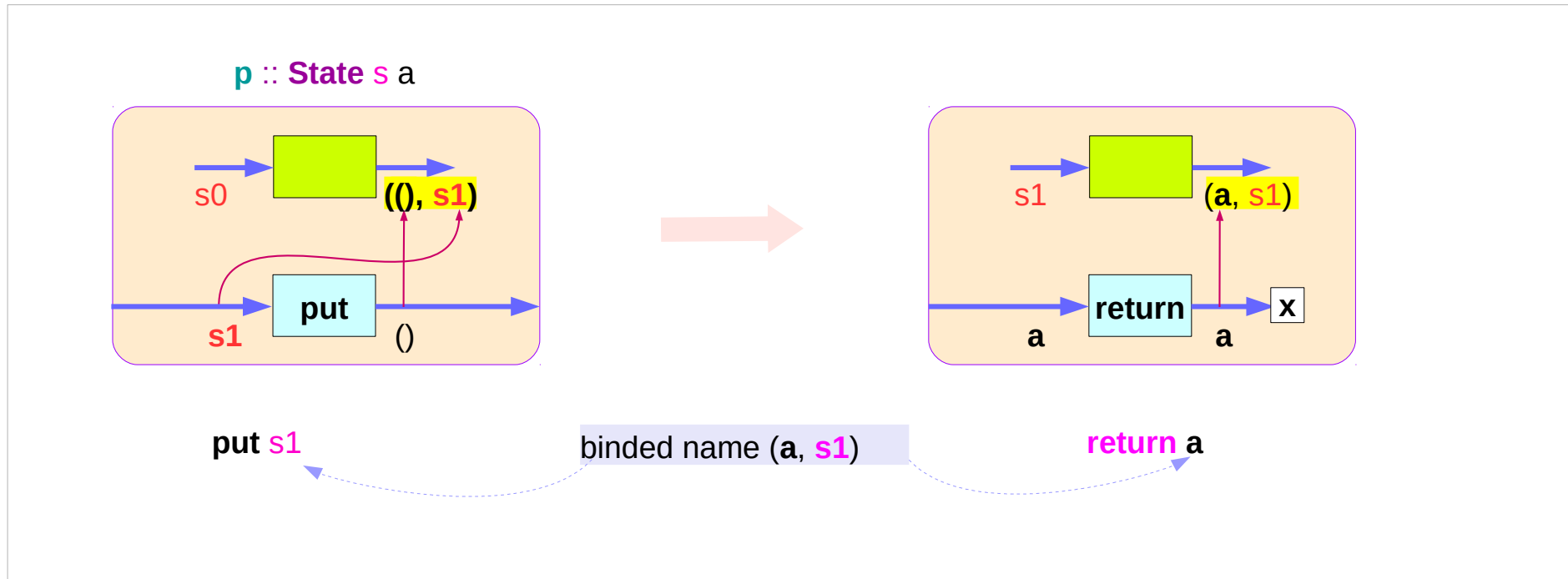
```
a <- p
```



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Redundant computation examples (2)

```
s0 <- get
let (a,s1) = runState p s0
put s1
return a
```



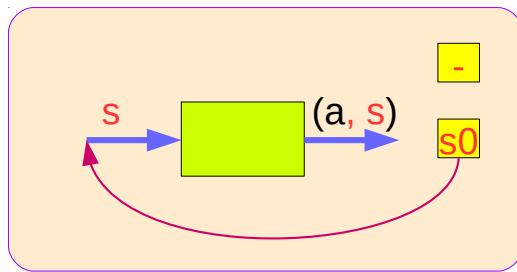
<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Redundant computation examples (3)

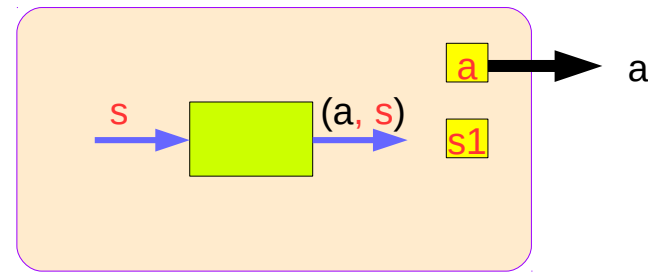
```
a <- p
```

-- the stateful computation **p** updates the state to **s1**
-- the result of the state returned is assigned to **a**

p :: State s a



stateful computation **p**



return the result **a**

runState p s0 → (a, s1)

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Counter Example

```
import Control.Monad.State.Lazy

tick :: State Int Int
tick = do n <- get
         put (n+1)
         return n

plusOne :: Int -> Int
plusOne n = execState tick n

plus :: Int -> Int -> Int
plus n x = execState (sequence $ replicate n tick) x
```

A function to increment a counter.

tick :

- a monadic value itself
- ~~a function returning a monadic value~~

Add one to the given number using the state monad:

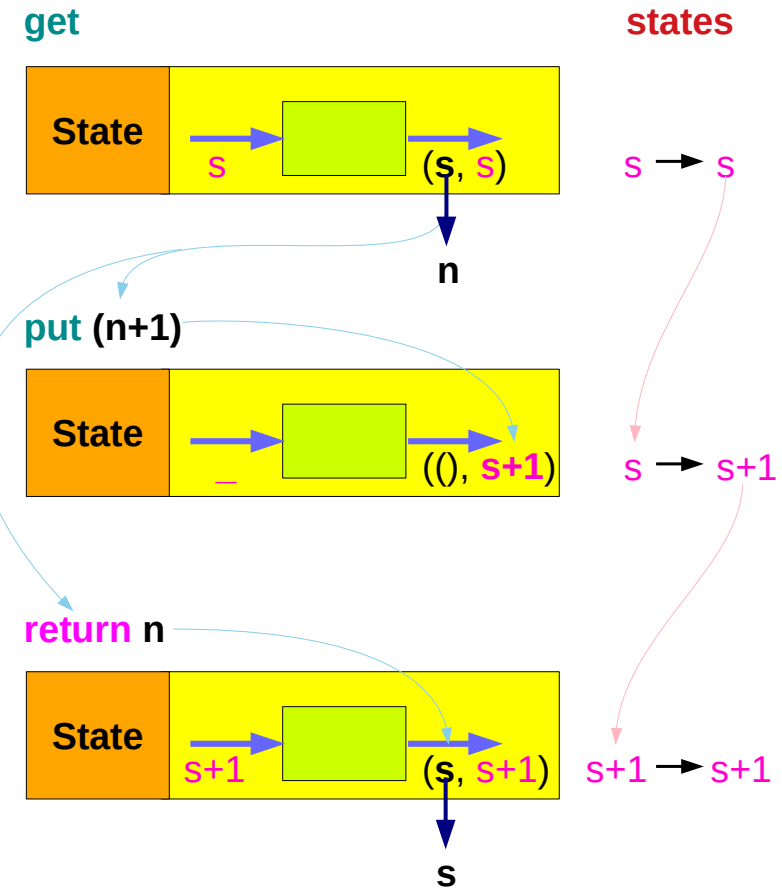
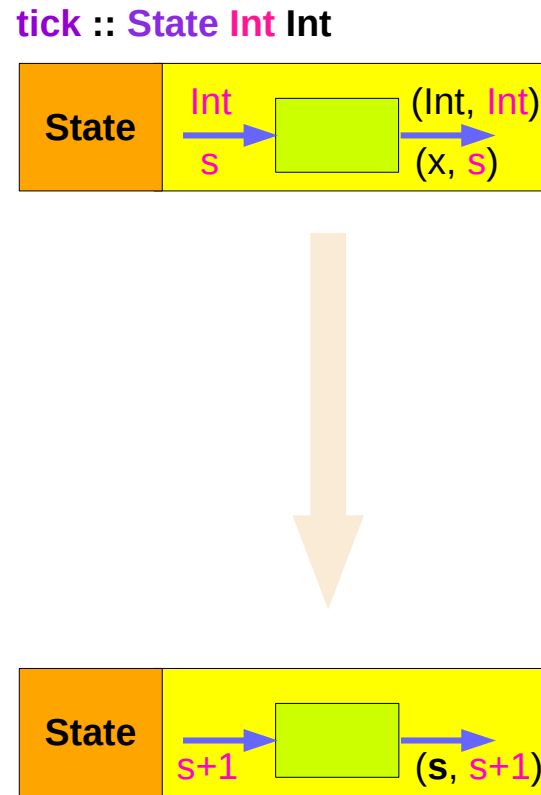
A contrived addition example. Works only with positive numbers:

<https://hackage.haskell.org/package/mtl-2.2.2/docs/Control-Monad-State-Lazy.html>

Counter Example – tick

```

tick :: State Int Int
tick = do n <- get
         put (n+1)
         execState n
    
```

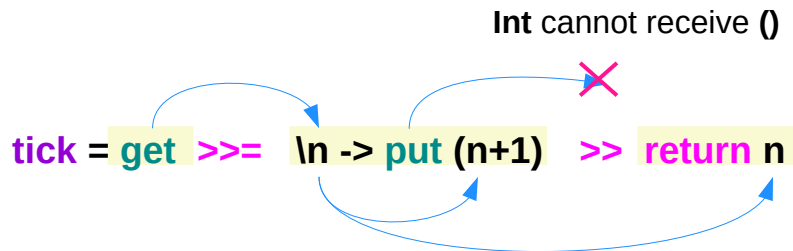


<https://hackage.haskell.org/package/mtl-2.2.2/docs/Control-Monad-State-Lazy.html>

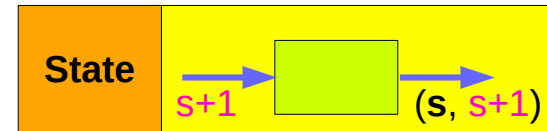
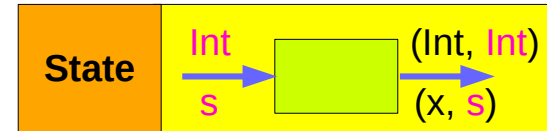
Counter Example – tick without `do`

```
tick :: State Int Int
```

```
tick = do n <- get  
        put (n+1)  
        return n
```



```
tick :: State Int Int
```



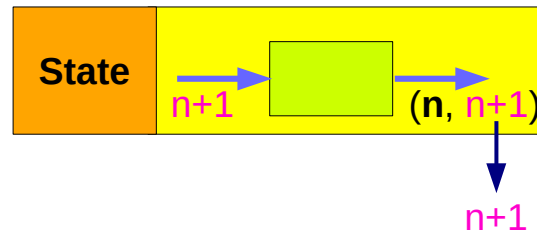
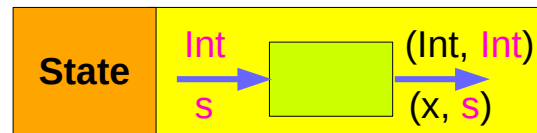
<https://hackage.haskell.org/package/mtl-2.2.2/docs/Control-Monad-State-Lazy.html>

Counter Example – incrementing

```
tick :: State Int Int
tick = do n <- get
         put (n+1)
         return n
```

```
plusOne :: Int -> Int
plusOne n = execState tick n
```

tick :: State Int Int



<https://hackage.haskell.org/package/mtl-2.2.2/docs/Control-Monad-State-Lazy.html>

Counter Example – using sequence

```
plus :: Int -> Int -> Int
```

```
plus n x = execState (sequence $ replicate n tick) x
```

```
sequence $ [tick, tick, ... ,tick]
```

```
runState (sequence $ [tick, tick]) 3 → ([3,4],5)
```

(3,4) → (4, 5)

```
runState (sequence $ [tick, tick, tick]) 3 → ([3,4,5],6)
```

(3,4) → (4,5) → (5,6)

```
execState (sequence $ [tick, tick, tick]) 3 → 6
```

```
evalState (sequence $ [tick, tick, tick]) 3 → [3,4,5]
```

<https://hackage.haskell.org/package/mtl-2.2.2/docs/Control-Monad-State-Lazy.html>

replicate

```
replicate :: Int -> a -> [a]
```

`replicate n x` is a list of length `n` with `x` the value of every element.

```
replicate 3 5
```

```
[5,5,5]
```

```
replicate 5 "aa"
```

```
["aa","aa","aa","aa","aa"]
```

```
replicate 5 'a'
```

```
"aaaaa"
```

http://zvon.org/other/haskell/Outputprelude/replicate_f.html

sequence

`sequence :: Monad m => [m a] -> m [a]`

evaluate **each action** in the sequence from left to right,
and collect the **results**.

`runState (sequence [get, return 3, return 4]) 1`

`([1,3,4],1)`

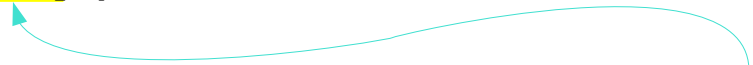
`runState get 1` `(1,1)` `result: 1`



`runState (return 3) 1` `(3,1)` `result: 3`



`runState (return 4) 1` `(4,1)` `result: 4`



<http://derekwyatt.org/2012/01/25/haskell-sequence-over-functions-explained/>

Example of collecting returned values – Method 1

```
collectUntil f comp = do
  st <- get           -- Get the current state
  if f st then return [] -- If it satisfies predicate, return
  else do            -- Otherwise...
    x <- comp         -- Perform the computation s
    xs <- collectUntil f comp -- Perform the rest of the computation
    return (x : xs)   -- Collect the results and return them
```

comp :: State s a

st :: s

f :: s -> Bool

x :: a

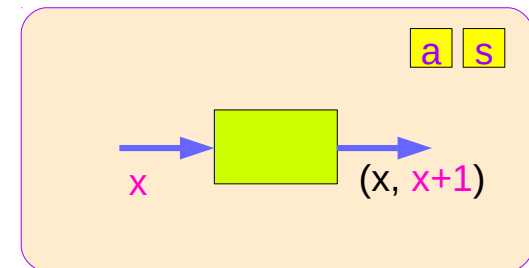
xs :: [a]

```
simpleState = state (\x -> (x,x+1))
```

```
*Main> evalState (collectUntil (>10) simpleState) 0
```

```
[0,1,2,3,4,5,6,7,8,9,10]
```

simpleState :: State s a



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1 and Method 2

```
collectUntil f comp = do
  st <- get
  if f st then return []
  else do
    x <- comp
    xs <- collectUntil f comp
    return (x : xs)
```

Method 1

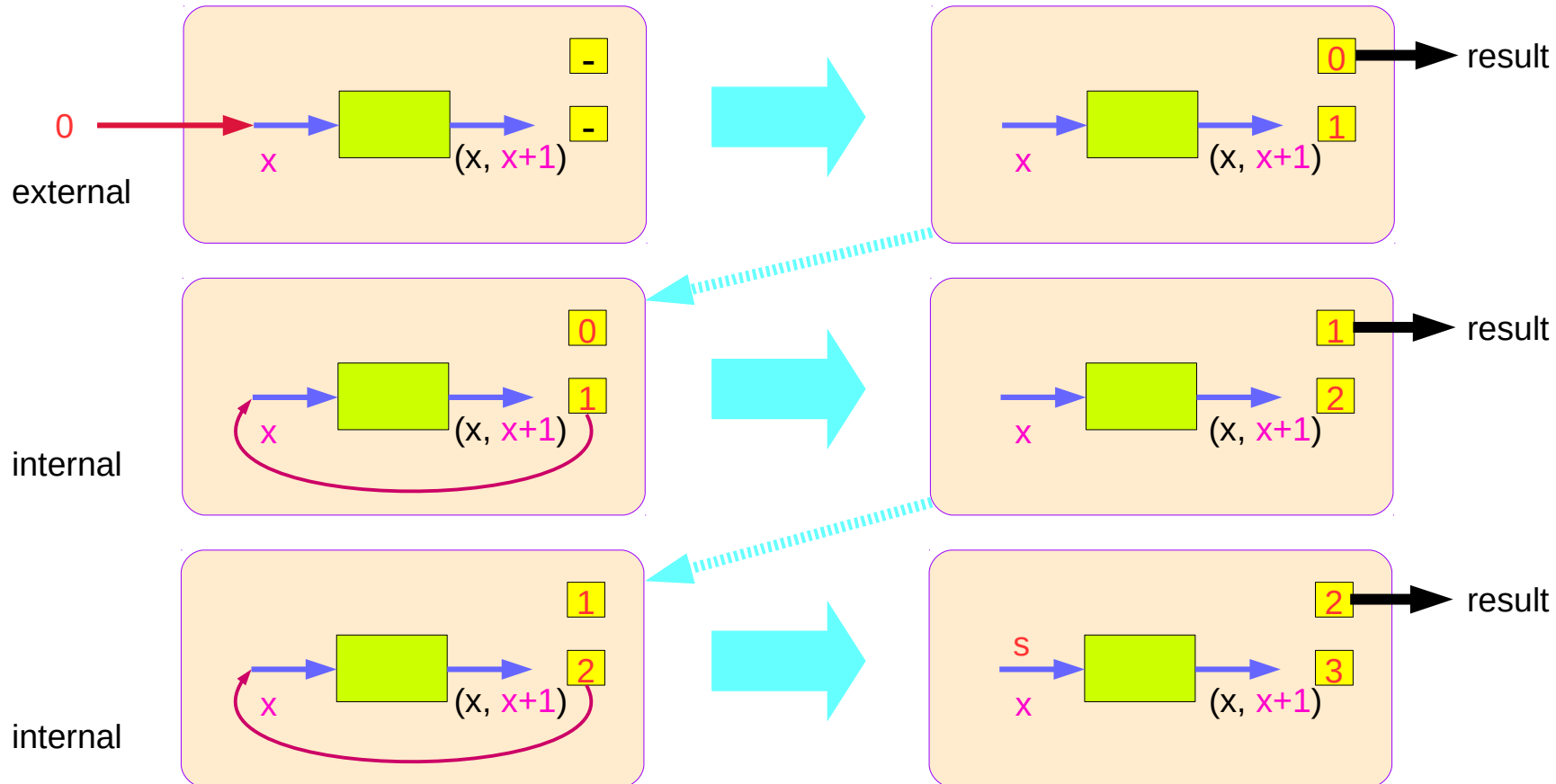
```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
where
  step = do a <- comp
         liftM (a :) continue
  continue = do b <- get
             if f b then return []
             else step
```

Method 2

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

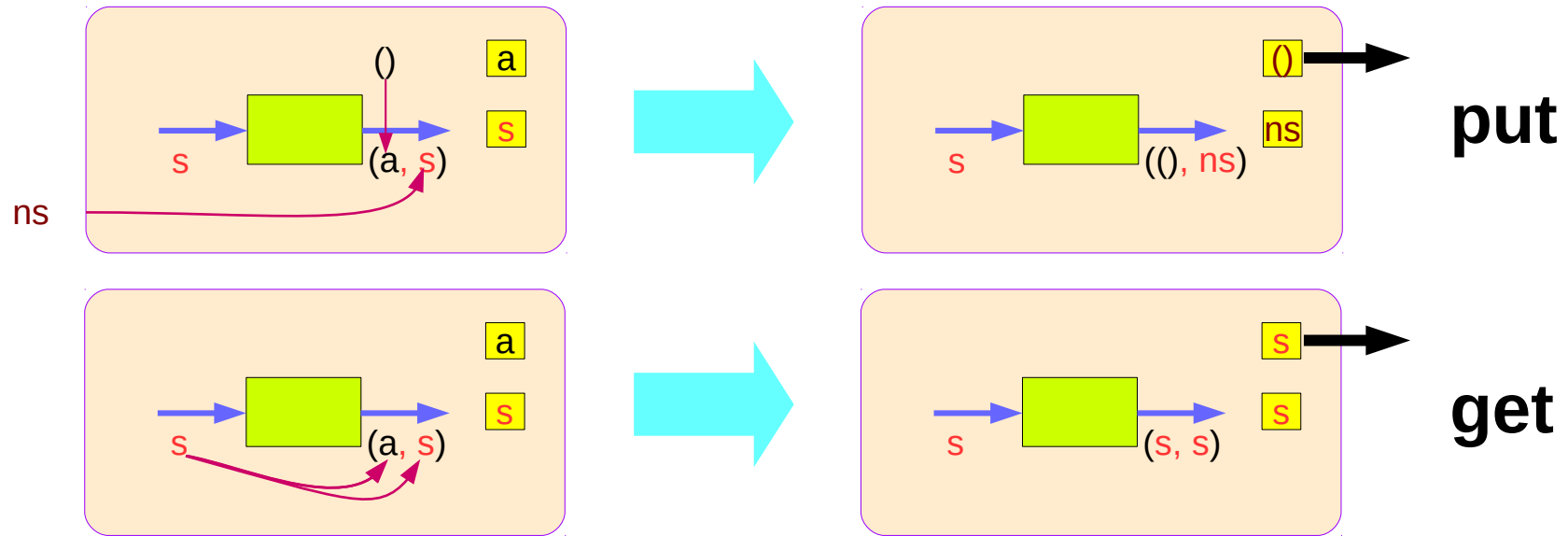
Stateful Computation of **comp**

comp (= simpleState)



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Stateful Computations of **put** & **get**



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: steps of stateful computations

```
collectUntil f comp = do
```

```
  st <- get
```

```
  if f st then return []
```

```
  else do
```

```
    x <- comp
```

```
    xs <- collectUntil f comp
```

```
    return (x : xs)
```

```
*Main> evalState (collectUntil (>10) simpleState) 0  
[0,1,2,3,4,5,6,7,8,9,10]
```

```
simpleState = state (\x -> (x,x+1))
```

```
get = state (\s -> (s, s))
```

```
get st ← 0
```

```
get st ← 1
```

```
get st ← 2
```

```
get st ← 3
```

```
get st ← 4
```

```
get st ← 5
```

```
get st ← 6
```

```
get st ← 7
```

```
get st ← 8
```

```
get st ← 9
```

```
get st ← 10
```

```
comp : 0 → (0, 1)
```

```
comp : 1 → (1, 2)
```

```
comp : 2 → (2, 3)
```

```
comp : 3 → (3, 4)
```

```
comp : 4 → (4, 5)
```

```
comp : 5 → (5, 6)
```

```
comp : 6 → (6, 7)
```

```
comp : 7 → (7, 8)
```

```
comp : 8 → (8, 9)
```

```
comp : 9 → (9, 10)
```

```
comp : 10 → (10, 11)
```

```
x ← 0
```

```
x ← 1
```

```
x ← 2
```

```
x ← 3
```

```
x ← 4
```

```
x ← 5
```

```
x ← 6
```

```
x ← 7
```

```
x ← 8
```

```
x ← 9
```

```
x ← 10
```

stateful computation

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: merge steps of collecting

collectUntil f comp = **do**

```
10 <- get
if f 10 then return [ ]
else do
  10 <- comp
  xs <- collectUntil f comp
  return (10 : xs)  ← 10:[] = [10]
```

collectUntil f comp = **do**

```
11 <- get
if f 11 then return [ ]
else do
  10 <- comp
  xs <- collectUntil f comp
  return (10 : xs)
```

```
0: (1: (2: (3: (4: (5: (6: (7: (8: (9: (10: [ ] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: (8: (9: [10] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: (8: [9,10] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: [8,9,10] )))))))))))
0: (1: (2: (3: (4: (5: (6: [7,8,9,10] )))))))))))
0: (1: (2: (3: (4: (5: [6,7,8,9,10] )))))))))))
0: (1: (2: (3: (4: [5,6,7,8,9,10] )))))))))))
0: (1: (2: (3: [4,5,6,7,8,9,10] )))))))))))
0: (1: (2: [3,4,5,6,7,8,9,10] )))))))))))
0: (1: [2,3,4,5,6,7,8,9,10] )))))))))))
0: [1,2,3,4,5,6,7,8,9,10] )))))))))))
[0, 1,2,3,4,5,6,7,8,9,10]
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: return steps of collecting

```
0: (1: (2: (3: (4: (5: (6: (7: (8: (9: (10: [ ] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: (8: (9: [10] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: (8: [9,10] )))))))))))
0: (1: (2: (3: (4: (5: (6: (7: [8,9,10] )))))))))))
0: (1: (2: (3: (4: (5: (6: [7,8,9,10] )))))))))))
0: (1: (2: (3: (4: (5: [6,7,8,9,10] )))))))))))
0: (1: (2: (3: (4: [5,6,7,8,9,10] )))))))))))
0: (1: (2: (3: [4,5,6,7,8,9,10] )))
0: (1: (2: [3,4,5,6,7,8,9,10] ))
0: [1,2,3,4,5,6,7,8,9,10]
[0, 1,2,3,4,5,6,7,8,9,10]
```

```
return []
return [10]
return [9,10]
return [8,9,10]
return [7,8,9,10]
return [6,7,8,9,10]
return [5,6,7,8,9,10]
return [4,5,6,7,8,9,10]
return [3,4,5,6,7,8,9,10]
return [2,3,4,5,6,7,8,9,10]
return [1,2,3,4,5,6,7,8,9,10]
return [0, 1,2,3,4,5,6,7,8,9,10]
```

```
( [], 11 )
( [10], 11 )
( [9,10], 11 )
( [8,9,10], 11 )
( [7,8,9,10], 11 )
( [6,7,8,9,10], 11 )
( [5,6,7,8,9,10], 11 )
( [4,5,6,7,8,9,10], 11 )
( [3,4,5,6,7,8,9,10], 11 )
( [2,3,4,5,6,7,8,9,10], 11 )
( [1,2,3,4,5,6,7,8,9,10], 11 )
( [0, 1,2,3,4,5,6,7,8,9,10], 11 )
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: branch within a do block

collectUntil f comp = **do**

```
st <- get
```

```
if f st then return []
```

```
else do
```

```
  x <- comp -- stateful computation
```

```
  xs <- collectUntil f comp
```

```
  return (x : xs)
```

----- return **State t [a]** type

----- return **State t [a]** type

} the same return
monadic type value

x :: a

xs :: [a]

(x : xs) :: [a]

0: (1: (2: (3: (4: (5: (6: (7: (8: (9: (10: []))))))))))))

nesting **do statement**

- is possible if they are within the same monad

- enables **branching** within one do block,
as long as both branches of the **if statement**
results in the same monadic type.

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: return stateful computation

```
collectUntil f comp = do
```

```
  st <- get
```

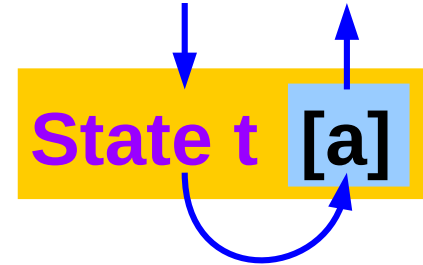
```
  if f st then return []
```

```
  else do
```

```
    x <- comp
```

```
    xs <- collectUntil f comp
```

```
    return (x : xs)
```



```
return :: State t [a] type
```

```
collectUntil f comp :: State t [a] type
```

```
xs <- collectUntil f comp -- stateful computation
```

```
xs :: [a]
```

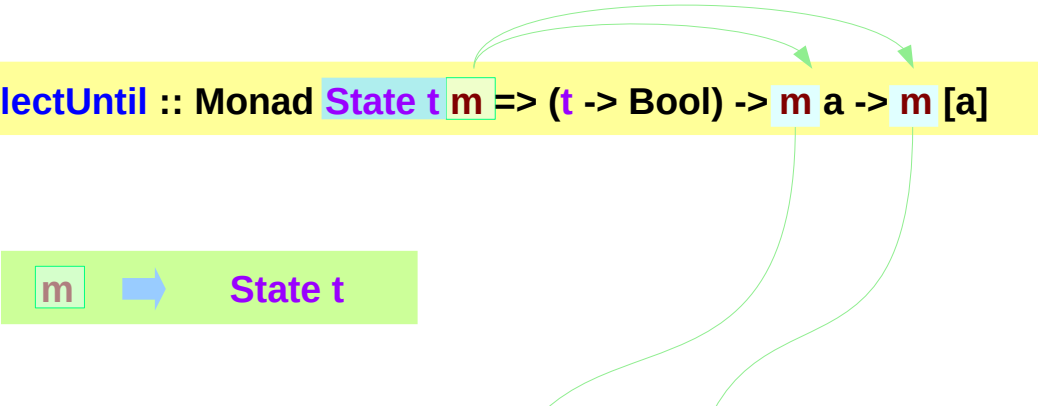
$t \rightarrow ([a], t)$ the result type

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 1: the inferred function type

Inferred Function Type

```
collectUntil :: Monad State t m => (t -> Bool) -> m a -> m [a]
```



A diagram showing the mapping of variables between the general and specific types. A green box labeled 'm' has an arrow pointing to 'State t'. A green box labeled 't' has an arrow pointing to 'State t'. A green box labeled 'a' has an arrow pointing to 'State t'. A green box labeled '[a]' has an arrow pointing to 'State t [a]'. There are also curved arrows at the top of the diagram showing the flow of information from the general type to the specific type.

m → State t

Specific Function Type

```
collectUntil :: (t -> Bool) -> State t a -> State t [a]
```

```
*Main> evalState (collectUntil (>10) simpleState) 0
```

```
simpleState = state (\x -> (x,x+1))
```

```
(>10) :: (t -> Bool)
```

```
simpleState :: State t a
```

```
collectUntil (>10) simpleState :: State t [a]
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Another implementation of collecting returned values

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
```

```
collectUntil f comp = step
```

where

```
step = do a <- comp -- updating stateful computation
```

```
liftM (a :) continue
```

```
continue = do b <- get -- current state getting stateful computation
```

```
if f b then return []
```

```
else step
```

```
*Main> evalState (collectUntil (>10) simpleState) 0
```

```
[0,1,2,3,4,5,6,7,8,9,10]
```

```
simpleState = state (\x -> (x,x+1))
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: other representation

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
```

```
collectUntil f comp = step
```

where

```
step = do a <- comp  
         liftM (a :) continue
```

```
continue = do b <- get  
              if f b then return []  
              else step
```

```
step = do a <- comp  
         liftM (a :) do b <- get  
                       if f b then return []  
                       else step
```

```
step = do a <- comp  
         liftM (a :) do b <- get  
                       if f b then return [] else step
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: the return type

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
where
  step = do a <- comp
           liftM (a :) continue
  continue = do b <- get
              if f b then return [] else step
```

Since **a** is part of the result in both branches of the 'if'

a is the common part of both 'then' part and 'else' part

returns only once at the last iteration

continue :: State s [a]

liftM (a :) continue :: State s [a]

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: liftM to merge

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
  where
    step = do a <- comp
             liftM (a :) continue
    continue = do b <- get
                if f b then return [] else step
```

```
return :: State t [a] type
collectUntil f comp :: State t [a] type
continue :: State t [a] type
```

```
(:) :: a -> [a] -> [a]
(+++) :: [a] -> [a] -> [a]
```

```
a :: a
continue :: State s [a]
liftM (a :) continue :: State s [a]
```

```
(:) :: a -> [a] -> [a]
liftM (:) :: a -> State s [a] -> State s [a]
```

```
(a :) :: [a] -> [a]
liftM (a :) :: State s [a] -> State s [a]
```

```
liftM (a :) continue :: State s [a]
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: steps of stateful computations

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
  where
    step = do a <- comp
             liftM (a :) continue
    continue = do b <- get
                 if f b then return [] else step
```

a <- comp

b <- get

return []

comp : 0 → (0, 1)	a ← 0	get : b ← 1
comp : 1 → (1, 2)	a ← 1	get : b ← 2
comp : 2 → (2, 3)	a ← 2	get : b ← 3
comp : 3 → (3, 4)	a ← 3	get : b ← 4
comp : 4 → (4, 5)	a ← 4	get : b ← 5
comp : 5 → (5, 6)	a ← 5	get : b ← 6
comp : 6 → (6, 7)	a ← 6	get : b ← 7
comp : 7 → (7, 8)	a ← 7	get : b ← 8
comp : 8 → (8, 9)	a ← 8	get : b ← 9
comp : 9 → (9, 10)	a ← 9	get : b ← 10
comp : 10 → (10, 11)	a ← 10	get : b ← 11



stateful computation

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: merge computation steps

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
  where
    step = do 10 <- comp
            liftM (10 :) continue
    continue = do 11 <- get
                if f 11 then return [] else step
```

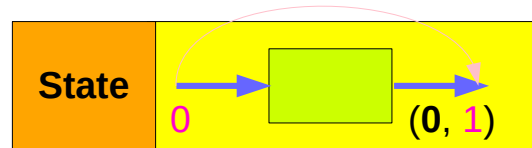
(>10)

```
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) (liftM (6:) (liftM (7:) (liftM (8:) (liftM (9:) (liftM (10:) ([],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) (liftM (6:) (liftM (7:) (liftM (8:) (liftM (9:) ([10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) (liftM (6:) (liftM (7:) (liftM (8:) ([9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) (liftM (6:) (liftM (7:) ([8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) (liftM (6:) ([7,8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) (liftM (5:) ([6,7,8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) (liftM (4:) ([5,6,7,8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) (liftM (3:) ([4,5,6,7,8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) (liftM (2:) ([3,4,5,6,7,8,9,10],11) ))))))))))))
(liftM (0:) (liftM (1:) ([2,3,4,5,6,7,8,9,10],11) ))))))))))))
(liftM (0:) ([1,2,3,4,5,6,7,8,9,10],11) ))))))))))))
[0,1,2,3,4,5,6,7,8,9,10]
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: comp, get, return

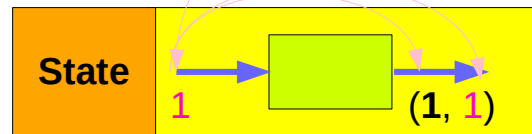
a <- comp



a=0

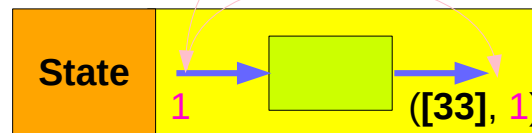
state (\x -> (x,x+1))

b <- get



b=1

return [33]

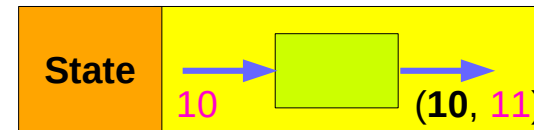
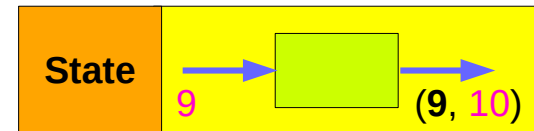
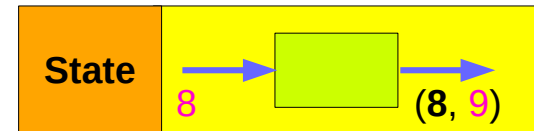
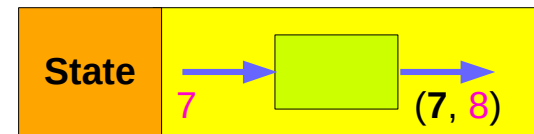
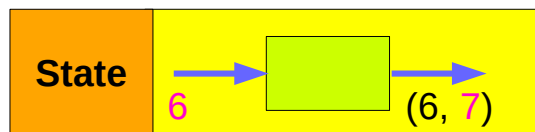
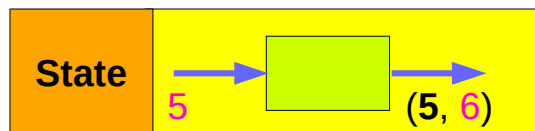
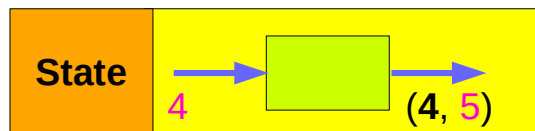
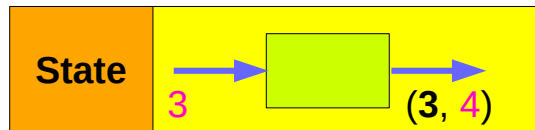
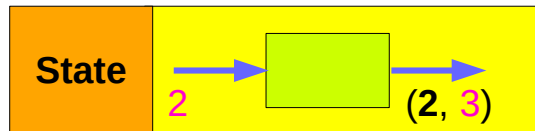
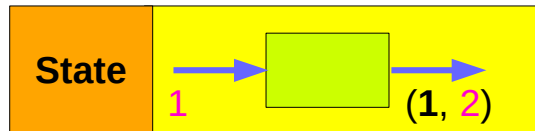
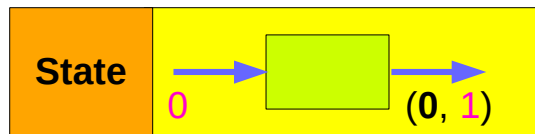


[33]

```
collectUntil f comp = step
where
  step = do a <- comp
         liftM (a :) continue
  continue = do b <- get
              if f b then return []
              else step
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

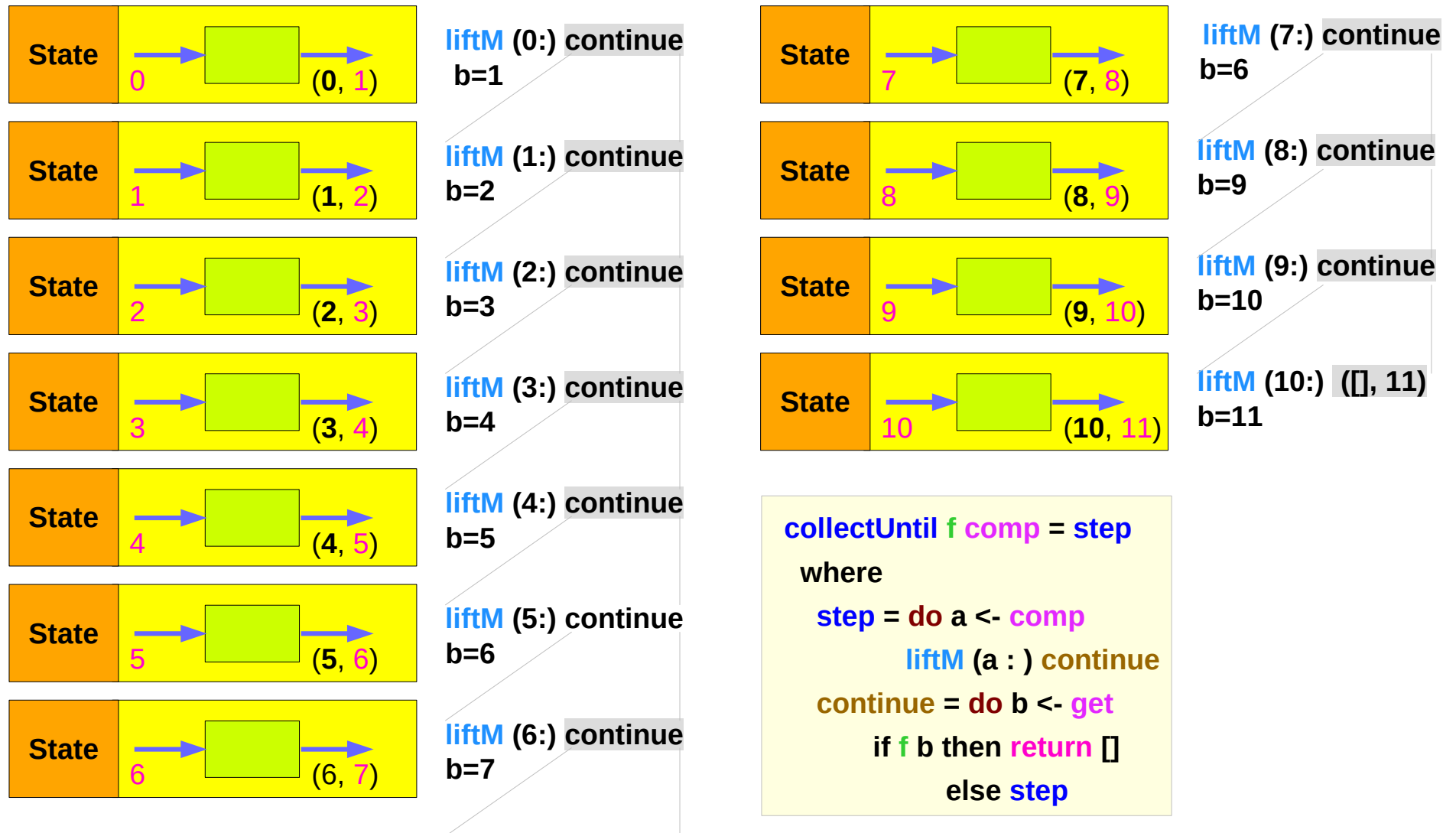
Method 2: steps of a<-comp, b<-get



```
collectUntil f comp = step
  where
    step = do a <- comp
            liftM (a :) continue
    continue = do b <- get
                if f b then return []
                else step
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Method 2: steps of continue



<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Sequence comparison

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
```

```
collectUntil f comp = step
```

where

```
step = do a <- comp
```

```
liftM (a :) continue
```

```
continue = do b <- get
```

```
if f b then return [] else step
```

```
collectUntil f comp = do
```

```
st <- get
```

```
if f st then return []
```

```
else do
```

```
x <- comp
```

```
xs <- collectUntil f comp
```

```
return (x : xs)
```

Method 2

update the current state
then get and then merge

Method 1

get the current state
then update and merge

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Merge comparison

```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
  where
    step = do a <- comp
           liftM (a :) continue
    continue = do b <- get
                if f b then return [] else step
```

```
collectUntil f comp = do
  st <- get
  if f st then return []
  else do
    x <- comp
    xs <- collectUntil f comp
    return (x : xs)
```

Method 2

Since **a** is part of the result in both branches of the 'if'

a is the common part of both 'then' part and 'else' part

continue :: State s [a]

liftM (a :) continue :: State s [a]

Method 1

xs :: [a]

x : xs :: [a]

returns the list of results

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

Example of collecting – source codes

```
import Control.Monad.Trans.State

collectUntil f comp = do
  st <- get
  if f st then return []
  else do
    x <- comp
    xs <- collectUntil f comp
    return (x : xs)

simpleState :: State Int Int
simpleState = state $ \x -> (x,x+1)

-- evalState (collectUntil (>10) simpleState) 0
-- [0,1,2,3,4,5,6,7,8,9,10]
```

```
import Control.Monad.Trans.State
import Control.Monad

simpleState :: State Int Int
simpleState = state $ \x -> (x,x+1)

-- evalState (collectUntil (>10) simpleState) 0
-- [0,1,2,3,4,5,6,7,8,9,10]

collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f s = step
  where
    step = do a <- s
              liftM (a:) continue
    continue = do s' <- get
                 if f s'
                 then return []
                 else step
```

<https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell>

liftM and mapM

```
liftM    :: (Monad m) => (a -> b)  -> m a -> m b
mapM     :: (Monad m) => (a -> m b) -> [a]  -> m [b]
```

liftM lifts a function of type `a -> b` to a monadic counterpart.

mapM applies a function which yields a monadic value to a list of values, yielding list of results embedded in the monad.

```
> liftM (map toUpper) getLine
```

```
Hallo
```

```
"HALLO"
```

```
> :t mapM return "monad"
```

```
mapM return "monad" :: (Monad m) => m [Char]
```

<https://stackoverflow.com/questions/5856709/what-is-the-difference-between-liftm-and-mapm-in-haskell>

References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>