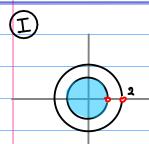
Laurent Series and z-Transform Examples case 3.B

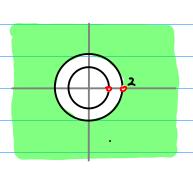
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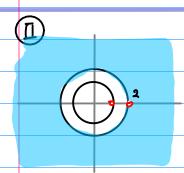
$$\frac{1}{2}(5) = \frac{(5-1)(5-5)}{-1} = \chi(5)$$

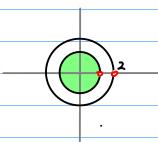




$$Q_n = \begin{cases} \left(\frac{1}{2}\right)^{n_{r_1}} - 1 & (n \geq 0) \\ 0 & (n < 0) \end{cases}$$

$$\chi_{n} = \begin{cases} 1 - 2^{n-1} & (n > 0) \\ 0 & (n < 0) \end{cases}$$

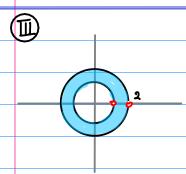


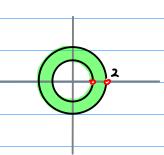


$$Q_n = \begin{cases} Q & (n > 0) \\ (n < 0) \end{cases}$$

$$\chi_{n} = \begin{cases} 0 & (1) > 0 \end{cases}$$

$$\chi_{n} = \begin{cases} 2^{n-1} - 1 & (1) < 0 \end{cases}$$





$$Q_n = \left\{ \begin{array}{c} \left(\frac{1}{2}\right)^{n+1} & (n < 0) \\ 1 & (n < 0) \end{array} \right.$$

$$\mathcal{X}_{n} = \begin{cases} 1 & (n > 0) \\ 2^{n-1} & (n < 0) \end{cases}$$

$$Q_n = \begin{cases} \left(\frac{1}{2}\right)^{n_{r_1}} - 1 & (n \ge 0) \\ 0 & (n < 0) \end{cases}$$

$$\mathcal{I}_{n} = \left\{ \begin{array}{c} 0 \\ \left(\frac{1}{2}\right)^{-n\eta} - 1 \\ \left(\frac{1}{2}\right)^{-n\eta} - 1 \end{array} \right. \quad (n < 0)$$

$$f(\xi) = \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \xi^n - \sum_{n=0}^{\infty} 1. \ \xi^n \qquad \chi(\xi) = \sum_{n=0}^{-\infty} \left(\frac{1}{2}\right)^{-n+1} \xi^{-n} - \sum_{n=0}^{-\infty} 1. \ \xi^{-n}$$

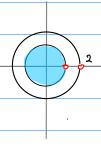
$$X(\xi) = \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \xi^{n} - \sum_{n=0}^{\infty} 1. \xi^{n}$$

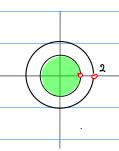
$$= \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \xi^{n} - \sum_{n=0}^{\infty} 1. \xi^{n}$$

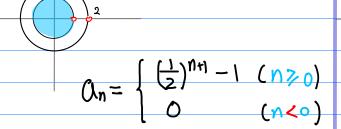
$$= \frac{\left(\frac{1}{2}\right)}{\left|-\left(\frac{2}{2}\right)\right|} = \frac{1}{7-2} + \frac{1}{7-1}$$

$$= \frac{(\xi + 1)(\xi - \xi)}{-1}$$

$$\left|\frac{\xi}{2}\right| < \left|\frac{\xi}{1}\right| < 1$$

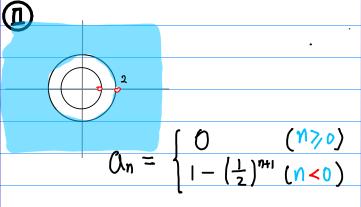




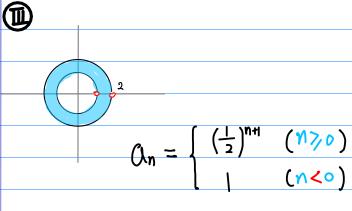


$$f(\xi) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n - \sum_{n=0}^{\infty} 1 \cdot \xi^n$$

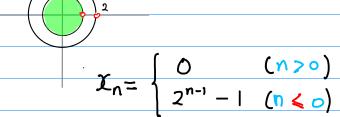
$$f(z) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot z^n - \sum_{n=0}^{\infty} 1 \cdot z^n$$



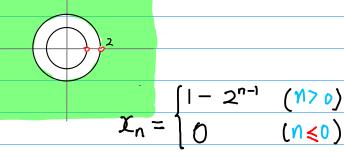
$$f(\xi) = \sum_{n=-1}^{\infty} |\cdot \xi^n| - \sum_{n=-1}^{\infty} 2^{-n-1} \cdot \xi^n$$



$$f(\xi) = \sum_{n=-1}^{-\infty} |\cdot \xi^n| - \sum_{n=0}^{\infty} 2^{-n-1} \cdot z^n$$



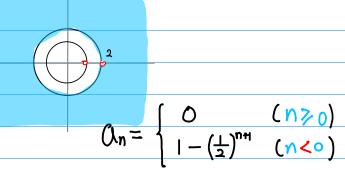
$$\chi(z) = \sum_{n=0}^{-\infty} 2^{n-1} \cdot z^{-n} - \sum_{n=0}^{-\infty} 1 \cdot z^{-n}$$



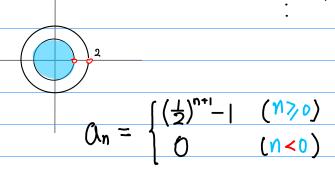
$$\chi(\xi) = \sum_{n=1}^{\infty} |\cdot \xi_n - \sum_{n=1}^{\infty} 2^{n-1} \cdot \xi_{-n}$$

$$\mathcal{I}_{\eta} = \begin{cases} 1 & (1/70) \\ 2^{n-1} & (n \leq 0) \end{cases}$$

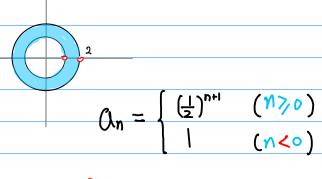
$$X(\xi) = \sum_{n=1}^{\infty} |\cdot \xi^{-n}| - \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^{-n}$$



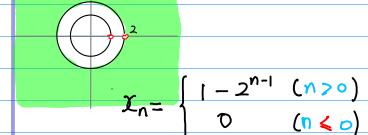
$$f(z) = \sum_{n=-1}^{-1} 1 \cdot z^n - \sum_{n=-1}^{-\infty} 2^{-n-1} z^n$$



$$f(\xi) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n - \sum_{n=0}^{\infty} |\cdot \xi^n|$$

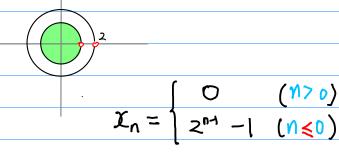


$$f(\xi) = \sum_{n=-1}^{\infty} 1 \cdot \xi^n + \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n$$



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$$\chi(\xi) = \sum_{n=1}^{\infty} |\cdot \xi_n - \sum_{n=1}^{\infty} z_{n-1} \xi_{-n}$$



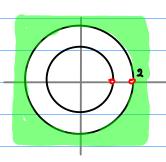
$$X(z) = \sum_{n=0}^{-\infty} 2^{n-1} \cdot z^{-n} - \sum_{n=0}^{-\infty} 1. z^{-n}$$

$$x_n = \begin{cases} 1 & (1/70) \\ 2^{n-1} & (n \le 0) \end{cases}$$

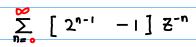
$$X(\xi) = \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^{-n} + \sum_{n=1}^{\infty} |\cdot \xi^{-n}|$$

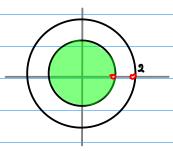
3.B
$$X(2) = \frac{-1}{(2-1)(2-2)}$$

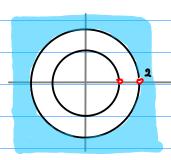
$$\frac{1}{2}(5) = \frac{(5-1)(5-5)}{-1}$$



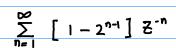
$$\sum_{n=0}^{\infty} \left[\left(\frac{1}{2} \right)^{n+1} - 1 \right] \, \xi^{-n}$$

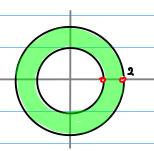


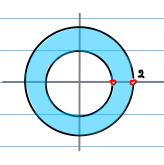




$$\sum_{n=-1}^{-\infty} \left[\left(\frac{1}{2} \right)^{n+1} - 1 \right] Z^{-n}$$





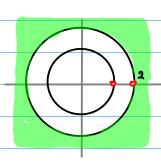


$$-\sum_{\infty}^{n=0} S_{-n} - \sum_{\infty}^{n=-1} J_{-n-1} S_{-n}$$



$$+\sum_{n=1}^{n=1} z_{-n} + \sum_{n=0}^{n=0} z_{n-1} z_{-n}$$

$$\chi(5) = \frac{(5-1)(5-5)}{-1} = \frac{(5-1)}{1} - \frac{(5-5)}{1}$$

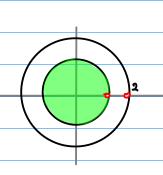


$$+ \frac{\left(\frac{1}{\xi}\right)}{1 - \left(\frac{1}{\xi}\right)} - \frac{\left(\frac{1}{\xi}\right)}{1 - \left(\frac{2}{\xi}\right)}$$

$$= + \sum_{n=0}^{\infty} \left(\frac{1}{\xi}\right) \left(\frac{1}{\xi}\right)^n - \sum_{n=0}^{\infty} \left(\frac{1}{\xi}\right) \left(\frac{2}{\xi}\right)^n$$

$$= \sum_{n=0}^{\infty} \left[1 - 2^n\right] \xi^{-n-1}$$

$$= \sum_{n=1}^{\infty} \left[1 - 2^{n-1}\right] \xi^{-n}$$

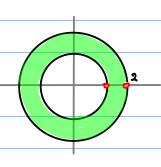


$$-\frac{\left(\frac{1}{1}\right)}{1-\left(\frac{z}{1}\right)} + \frac{\left(\frac{1}{2}\right)}{1-\left(\frac{z}{2}\right)}$$

$$= -\sum_{n=0}^{\infty} (1)\left(\frac{z}{1}\right)^n + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)\left(\frac{z}{2}\right)^n$$

$$= \sum_{n=0}^{\infty} \left[\left(\frac{1}{2}\right)^{n+1} - 1\right] z^n$$

$$= \sum_{n=0}^{\infty} \left[2^{n-1} - 1\right] z^{-n}$$



$$+ \frac{\left(\frac{1}{2}\right)}{1 - \left(\frac{1}{2}\right)} + \frac{\left(\frac{1}{2}\right)}{1 - \left(\frac{2}{2}\right)}$$

$$= + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)^{n} + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right) \left(\frac{z}{2}\right)^{n}$$

$$= + \sum_{n=0}^{\infty} z^{-n-1} + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} z^{n}$$

$$= + \sum_{n=1}^{\infty} z^{-n} + \sum_{n=0}^{\infty} 2^{n-1} z^{-n}$$

