

Side Effects (3B)

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Based on

[Haskell in 5 steps](https://wiki.haskell.org/Haskell_in_5_steps)

https://wiki.haskell.org/Haskell_in_5_steps

Variables

Imperative programming:

- **variables** as **changeable locations** in a computer's memory
- imperative programs **explicitly commands**
the computer what to do

functional programming

- a way to think in higher-level **mathematical terms**
- defining how **variables relate** to one another
- leaving the **compiler** to **translate** these
to the step-by-step **instructions**
that the computer can process.

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Haskell Language Features

Haskell Functional Programming

- **Immutability**
- **Recursive Definition**
- **No Data Dependency**

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Redefinition : not allowed

imperative programming:

r = 5

after setting **r = 5** and then changing it to **r = 2**.

r = 2

Haskell programming:

an error: "multiple declarations of **r**".

Within a given scope, a **variable** in Haskell gets defined **only once** and **cannot change**, like variables in mathematics.

r = 5



~~**r = 2**~~

**No mutation
In Haskell**

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Variables in a file

Immutable:

they can change only based on
the data we enter to run the program.

We cannot define `r` two ways in the same code,
but we could change the value **by changing the file**

Vars.hs

```
a = 100
```

```
r = 5
```

```
pi = 3.14159
```

```
e = 2.7818
```

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Loading a variable definition file

```
$ ghci
GHCi, version 7.10.3: http://www.haskell.org/ghc/ :? for help
Prelude> :load Var1.hs
[1 of 1] Compiling Main          ( var.hs, interpreted )
Ok, modules loaded: Main.
*Main> r
5
*Main> :t r
r :: Integer
*Main>

*Main> :load Var2.hs
[1 of 1] Compiling Main          ( var2.hs, interpreted )
Ok, modules loaded: Main.
*Main> r
55
```

:load **Var1.hs**

:load **Var1.hs**

definition with initialization

Var1.hs

r = 5

Var2.hs

r = 55

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

No Mutation

```
*Main> r = 33
```

```
<interactive>:12:3: parse error on input '='
```

```
$ ghci
```

```
GHCi, version 7.10.3: http://www.haskell.org/ghc/ :? for help
```

```
Prelude> r = 333
```

```
<interactive>:2:3: parse error on input '='
```

```
Prelude>
```

No mutation, Immutable

```
let r = 33
```

```
let r = 33
```

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Recursive Definition

imperative programming:

$r = r + 1$

incrementing the variable r

(**updating** the value in memory)

Haskell programming:

a **recursive definition** of r

(defining it in terms of itself)

Side effect, Stateful computation

if r had been defined with any value beforehand,
then $r = r + 1$ in Haskell would bring an error message.

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

No Data Dependence

$y = x * 2$

$x = 3$



$x = 3$

$y = x * 3$



Haskell programming:

because the values of variables do not change

variables can be defined in any order

no mandatory : "x being declared before y"

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Evaluation

area 5

=> { replace the LHS $\text{area } r = \dots$ by the RHS $\dots = \pi * r^2$ }

$\pi * 5^2$

=> { replace π by its numerical value }

$3.141592653589793 * 5^2$

=> { apply exponentiation (^) }

$3.141592653589793 * 25$

=> { apply multiplication (*) }

78.53981633974483

$\text{area } r = \pi * r^2$

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Translation to instructions

functional programming

- leaving the **compiler** to **translate** these to the step-by-step **instructions** that the computer can process.

replace each **function** and **variable** with its **definition**
repeatedly replace the results **until a single value remains**.

to apply or call a function means

to **replace the LHS** of its **definition** by **its RHS**.

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Side Effects Definition

a **function** or **expression** is said to have a **side effect** if it modifies some state outside its scope or has an observable interaction with its calling functions or the outside world besides returning a value.

a particular function might

- modify a **global** variable or **static** variable,
- modify one of its **arguments**,
- raise an **exception**,
- write data to a **display** or **file**,
- read data from a **keyboard** or **file**, or
- call *other side-effecting functions*.

[https://en.wikipedia.org/wiki/Side_effect_\(computer_science\)](https://en.wikipedia.org/wiki/Side_effect_(computer_science))

History, Order, and Context

In the presence of **side effects**,
a program's behaviour may depend on **history**;

the **order** of **evaluation** matters.
the **context** and **histories**

Imperative programming : frequent utilization of **side effects**.
functional programming : **side effects** are rarely used.

The lack of side effects makes it easier
to do **formal verifications** of a program

[https://en.wikipedia.org/wiki/Side_effect_\(computer_science\)](https://en.wikipedia.org/wiki/Side_effect_(computer_science))

Side Effects Examples in C

```
int i, j;  
i = j = 3;  
  
i = (j = 3);    // j = 3 returns 3, which then gets assigned to i
```

```
// The assignment function returns 10  
// which automatically casts to "true"  
// so the loop conditional always evaluates to true  
  
while (b = 10) { }
```

[https://en.wikipedia.org/wiki/Side_effect_\(computer_science\)](https://en.wikipedia.org/wiki/Side_effect_(computer_science))

Pure Languages

Haskell is a **pure** language

programs are made of **functions**

that can't change

any global state or variables,

they can only do

some computations and return them results.

every variable's value does not change in time

However, some problems are inherently stateful

in that they rely on some state that changes over time.

~~st1 = 10~~

s -> (x,s)

st1 (v,10)

a bit tedious to model

Haskell has the **state monad** features

<http://learnyouahaskell.com/for-a-few-monads-more>

Side Effects in Haskell

The functional language Haskell expresses side effects
such as **I/O** and
other **stateful computations**
using **monadic actions**
state monad

[https://en.wikipedia.org/wiki/Side_effect_\(computer_science\)](https://en.wikipedia.org/wiki/Side_effect_(computer_science))

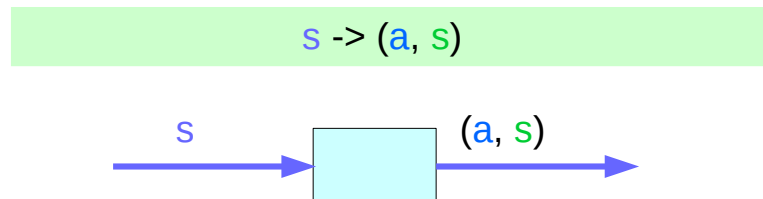
Stateful Computation

a **stateful computation** is a **function** that
takes some **state** and
returns a **value** along with some **new state**.

That function would have the following type:

```
s -> (a,s)
```

s is the type of the **state** and
a the **result** of the **stateful computation**.



<http://learnyouahaskell.com/for-a-few-monads-more>

Assignment

Assignment in an imperative language :

will assign the value 5 to the variable x

will have the value 5 as an *expression*

Assignment in a functional language

as a **function** that

takes a **state** and

returns a **result** and a **new state**

x = 5

<http://learnyouahaskell.com/for-a-few-monads-more>

Assignment as a stateful computation

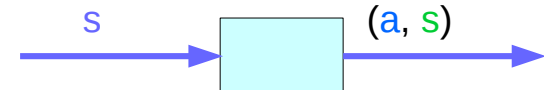
Assignment in a functional language
as a **function** that
takes a **state** and
returns a **result** and a **new state**

an input **state** :
all the variables that have been assigned previously
a **result** : 5
a **new state** :
all the previous variable mappings plus
the newly assigned variable.

<http://learnyouahaskell.com/for-a-few-monads-more>

x = 5

$s \rightarrow (a, s)$



all the variables
that have been
assigned
previously

a = 1
b = 2

all the previous
variable mappings
plus the newly
assigned variable

a result : 5

a = 1
b = 2
x = 5

A value with a context

The **stateful computation**:

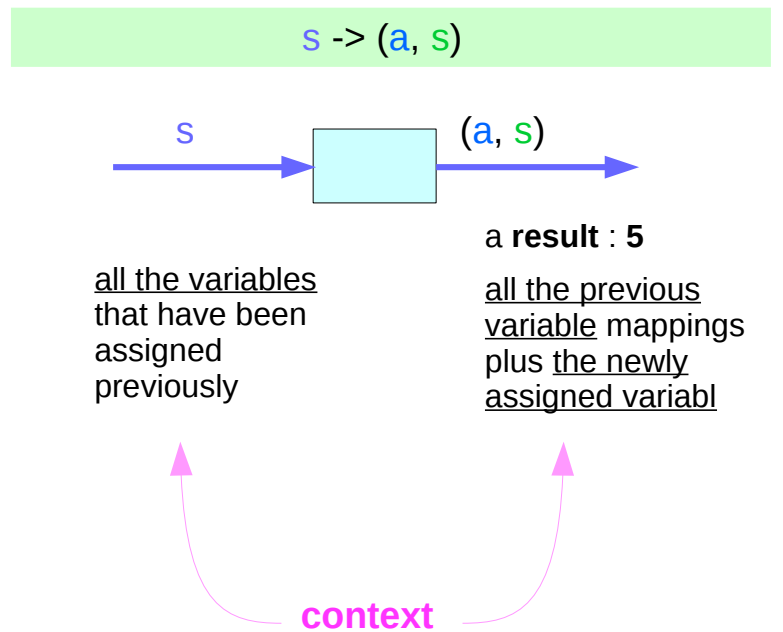
- a **function** that
 - takes a **state** and
 - returns a **result** and a **new state**
- can be considered as **a value with a context**

the actual **value** is

the **result**

the **context** is

that we have to provide an **initial state** to get the result and that apart from getting the result we also get a **new state**.



<http://learnyouahaskell.com/for-a-few-monads-more>

Monadic Effect

```
class Monad m where
  return :: a -> m a
  (>>=) :: m a -> (a -> m b) -> m b
```

https://en.wikibooks.org/wiki/Haskell/Understanding_monads/IO
<https://stackoverflow.com/questions/2488646/why-are-side-effects-modeled-as-monads-in-haskell>
<https://stackoverflow.com/questions/7840126/why-monads-how-does-it-resolve-side-effects>
<https://stackoverflow.com/questions/2488646/why-are-side-effects-modeled-as-monads-in-haskell>

<https://www.cs.hmc.edu/~adavidso/monads.pdf>

Monadic Operation

Monadic operations tend to have types which look like

```
val-in-type-1 -> ... -> val-in-type-n -> effect-monad val-out-type
```

where the **return type** is a type application:

```
effect-monad val-out-type
```

the function tells you
which **effects** are possible

the argument tells you (val-out-type)
what sort of **value** is produced **by the operation**

```
put :: s -> (State s) ()
```

```
putStr :: String -> IO ()
```

```
IO ()
```

function: effect-monad

argument: val-out-type

<https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly>

Monadic Operation – put, putStr

```
put :: s -> State s ()
```

```
put :: s -> (State s) ()
```

one value input type **s**
the effect-monad **State s**
the value output type **()**

the operation is used *only for its effect*;
the *value delivered* is *uninteresting*

```
putStr :: String -> IO ()
```

delivers a string to stdout but does not return anything exciting.

<https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly>

Side Effects of IO Monad

Generally, a monad cannot perform **side effects** in Haskell.
there is one exception: **IO monad**

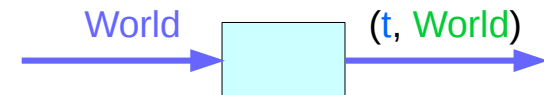
Suppose there is a type called **World**,
which contains all the state of the external universe

A way of thinking what **IO monad** does

```
type IO t = World -> (t, World)    type synonym
```

```
putStr :: String -> IO ()
```

World -> (t, World)



<https://www.cs.hmc.edu/~adavidso/monads.pdf>

Type Synonym **IO t**

IO t is a **parameterized function**

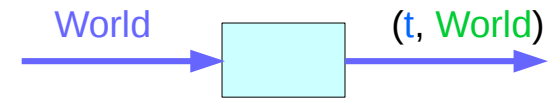
input : a **World**

output: a value of the type **t** and a new **updated World**
obtained by modifying the given **World**
in the process of computing the value of the type **t**.

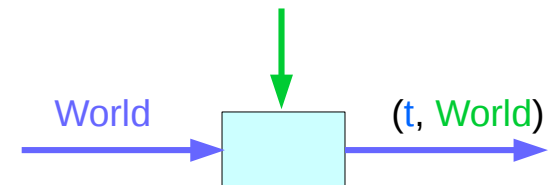
```
type IO t = World -> (t, World)
```

type synonym

World -> (t, World)



IO t



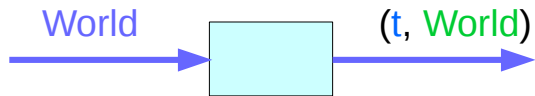
<https://www.cs.hmc.edu/~adavidso/monads.pdf>

A Parameterized Function of IO Monad

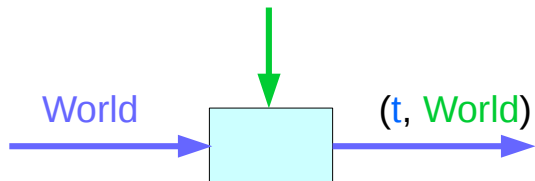
```
type IO t = World -> (t, World)
```

type synonym

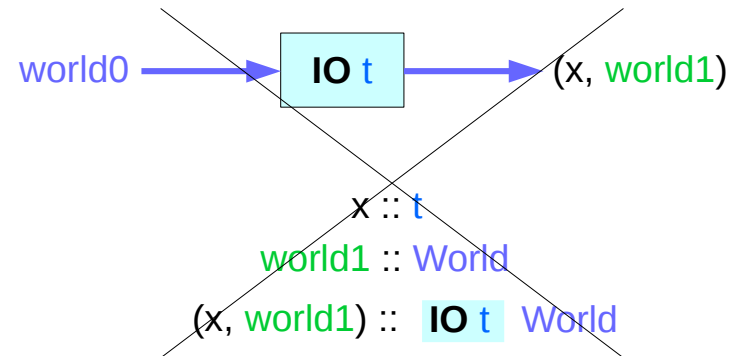
```
World -> (t, World)
```



```
IO t
```



<https://www.cs.hmc.edu/~adavidso/monads.pdf>



Implementation of IO t

It is impossible

to store the extra copies of the contents of your hard drive
that each of the Worlds contains

given World → updated World

<https://www.cs.hmc.edu/~adavidso/monads.pdf>

IO Monad

We give **IO** the **World**

we got back the **World**

from getting **x** out of its monad,

and the thing **IO** gives back to us is

the **y** with

a final version of the **World**

world0 :: **World**

world1 :: **World**

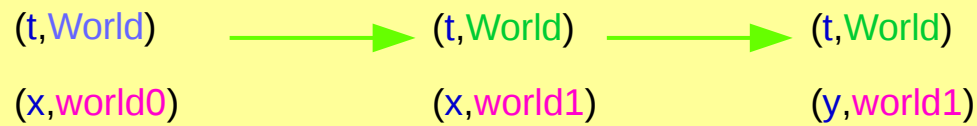
x :: **t**

y :: **t**

world1 :: **World**

.

the implementation of bind



<https://www.cs.hmc.edu/~adavidso/monads.pdf>

IO Monad in GHC

Which World was given initially?

Which World was updated?

In **GHC**, a **main** must be defined somewhere with type **IO ()**

a program execution starts from the **main**

the **initial World** is contained in the **main** to start everything off

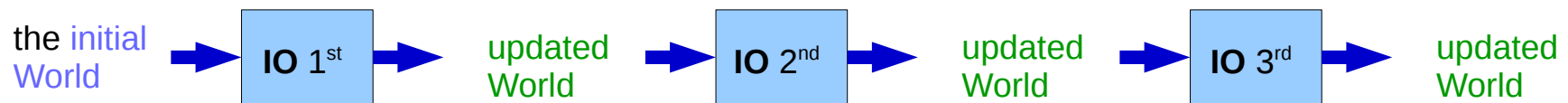
the **main** passes the **updated World** from each **IO**

to the next **IO** as its **initial World**

an **IO** that is not reachable from **main** will never be executed

an **initial / updated World** is not passed to such an **IO**

The modification of the World



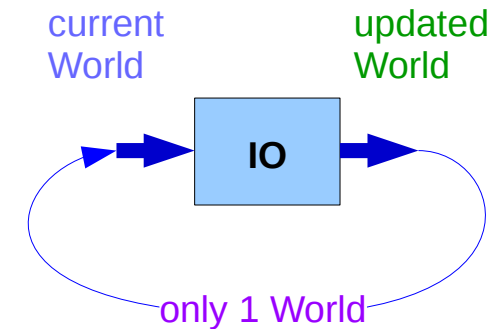
<https://www.cs.hmc.edu/~adavidso/monads.pdf>

IO Monad in GHCi

when using **GHCI**,
everything is wrapped in **an implicit IO**,
since the results get printed out to the screen.

there's **only 1 World** in existence at any given moment.
Each IO takes that **one and only World**, consumes it,
and gives back a single new World.
Consequently, there's no way to accidentally run out of Worlds,
or have multiple ones running around.

the implementation of bind



<https://www.cs.hmc.edu/~adavidso/monads.pdf>

Every time a new command is given to **GHCI**,
GHCI passes *the current World* to **IO**,
GHCI gets the *result* of the command back,
GHCI request to display the *result*

(which *updates the World* by modifying

- the contents of the screen or
- the list of defined variables or
- the list of loaded modules or whatever),

GHCI saves *the new World* to process the next command.

the implementation of bind

<https://www.cs.hmc.edu/~adavidso/monads.pdf>

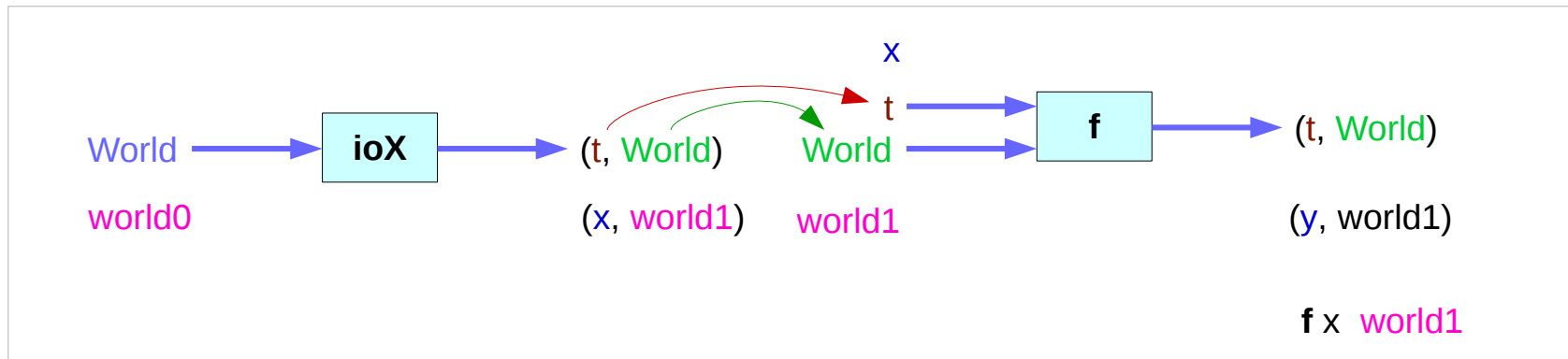
IO Monad Implementation

```
instance Monad IO where  
  return x world = (x, world)
```

```
(ioX >>= f) world0 =  
  let (x, world1) = ioX world0  
  in f x world1      -- has type (t, World)
```

$(x, s) \longrightarrow (x, s') \longrightarrow (y, s')$

```
type IO t = World -> (t, World)      type synonym
```



<https://www.cs.hmc.edu/~adavidso/monads.pdf>

Monad IO and Monad ST

instance Monad IO where

```
return x world = (x, world)
```

```
(ioX >>= f) world0 =
```

```
  let (x, world1) = ioX world0
```

```
  in  f x world1      -- has type (t, World)
```

instance Monad ST where

```
-- return :: a -> ST a
```

```
return x = \s -> (x,s)
```

```
-- (>>=) :: ST a -> (a -> ST b) -> ST b
```

```
st >>= f = \s -> let (x,s') = st s
                  in f x s'
```

```
type IO t = World -> (t, World)
```

type synonym

<https://www.cs.hmc.edu/~adavidso/monads.pdf>

State Transformers ST

instance **Monad ST** where

```
-- return :: a -> ST a
```

```
return x = \s -> (x,s)
```

```
-- (>>=) :: ST a -> (a -> ST b) -> ST b
```

```
st >>= f = \s -> let (x,s') = st s in f x s'
```

>>= provides a means of sequencing **state transformers**:

st >>= f applies the **state transformer st** to an initial state **s**,

then applies the function **f** to the resulting value **x**

to give a second **state transformer (f x)**,

which is then applied to the modified state **s'** to give the final result:

```
st >>= f = \s -> f x s'
```

```
where (x,s') = st s
```

```
st >>= f = \s -> (y,s')
```

```
where (x,s') = st s
```

```
(y,s') = f x s'
```

```
(x,s') = st s
```

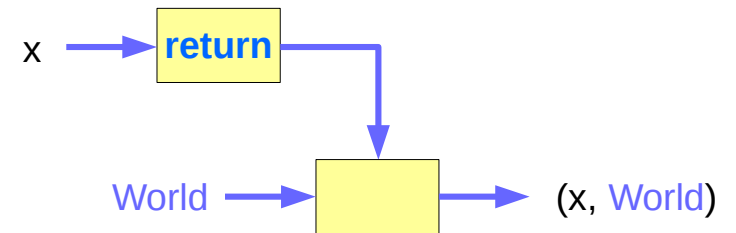
```
f x s'
```

<https://cseweb.ucsd.edu/classes/wi13/cse230-a/lectures/monads2.html>

Monad IO - return

The **return** function takes x
and gives back a function
that takes a **World**
and returns x along with the new, **updated World (=World)**
formed by not modifying the **World** it was given

return x world = (x, world)



<https://www.cs.hmc.edu/~adavidso/monads.pdf>

References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>