

Array Pointers (1A)

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Assumption

assume that

value(c) returns the hexadecimal number that is obtained by `printf("%p", c)`, when the variable `c` contains an address as its value

type(c) can be determined by the warning message of `printf("%d", c)`, when the variable `c` contains an address as its value

```
#include <stdio.h>
int main(void) {
    int c[3];
    printf ("c= %p \n", &c);
}
```

`c= 0x7fffd923487c`

```
#include <stdio.h>
int main(void) {
    int c[3];
    printf ("c= %d \n", &c);
}
```

t.c: In function 'main':
t.c:5:16: warning: format '%d' expects argument of type 'int',
but argument 2 has type 'int (*)[3]' [-Wformat=]
printf ("c= %d \n", &c);

int [4]

array type

int (*) [4]

array pointer type

int *

integer pointer type

int **

integer double pointer type

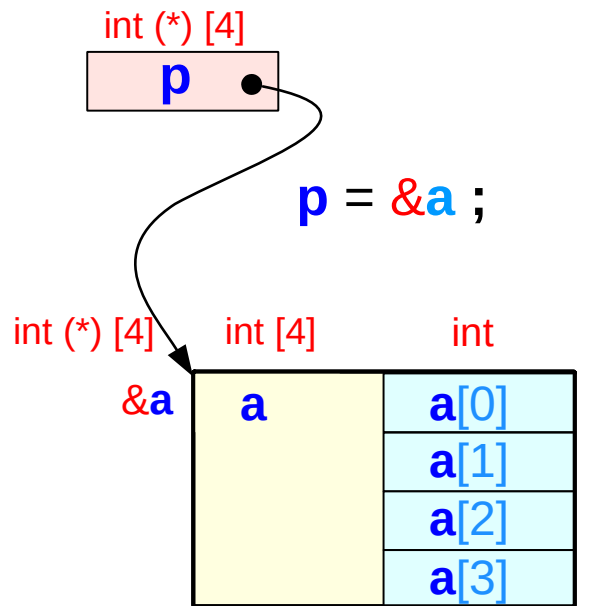
Outside and inside array types (1)

```
int a [4];
```

```
int (*p) [4];
```

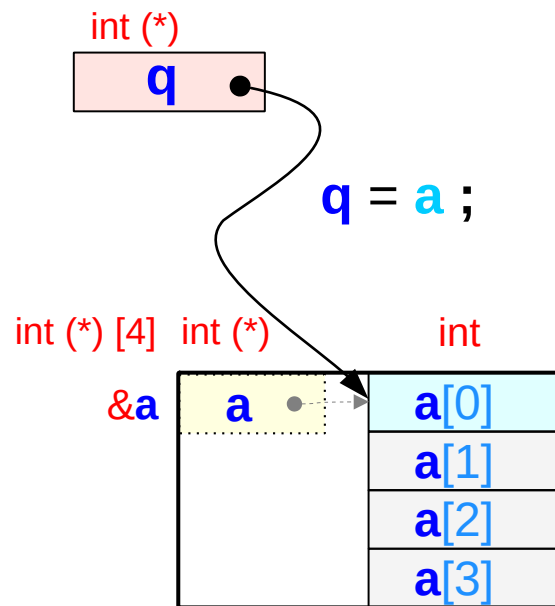
```
int *q ;
```

```
int **r ;
```



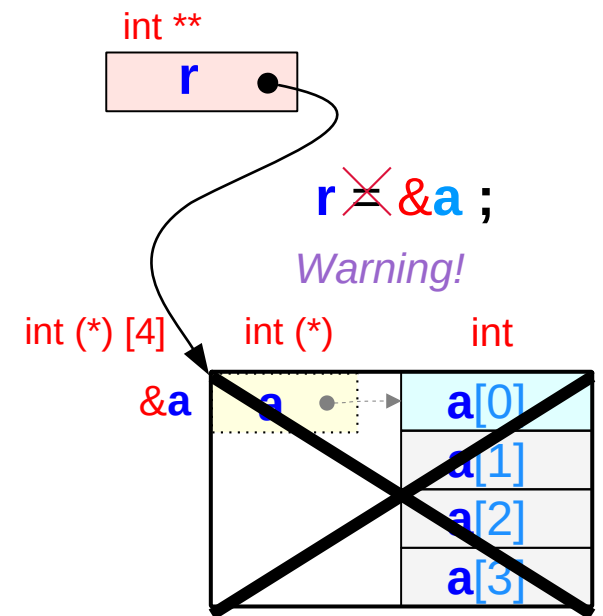
when accessing an array
outside of an array a

type(a) = int [4]
type(&a) = int (*) [4]



when accessing an element
inside of an array a

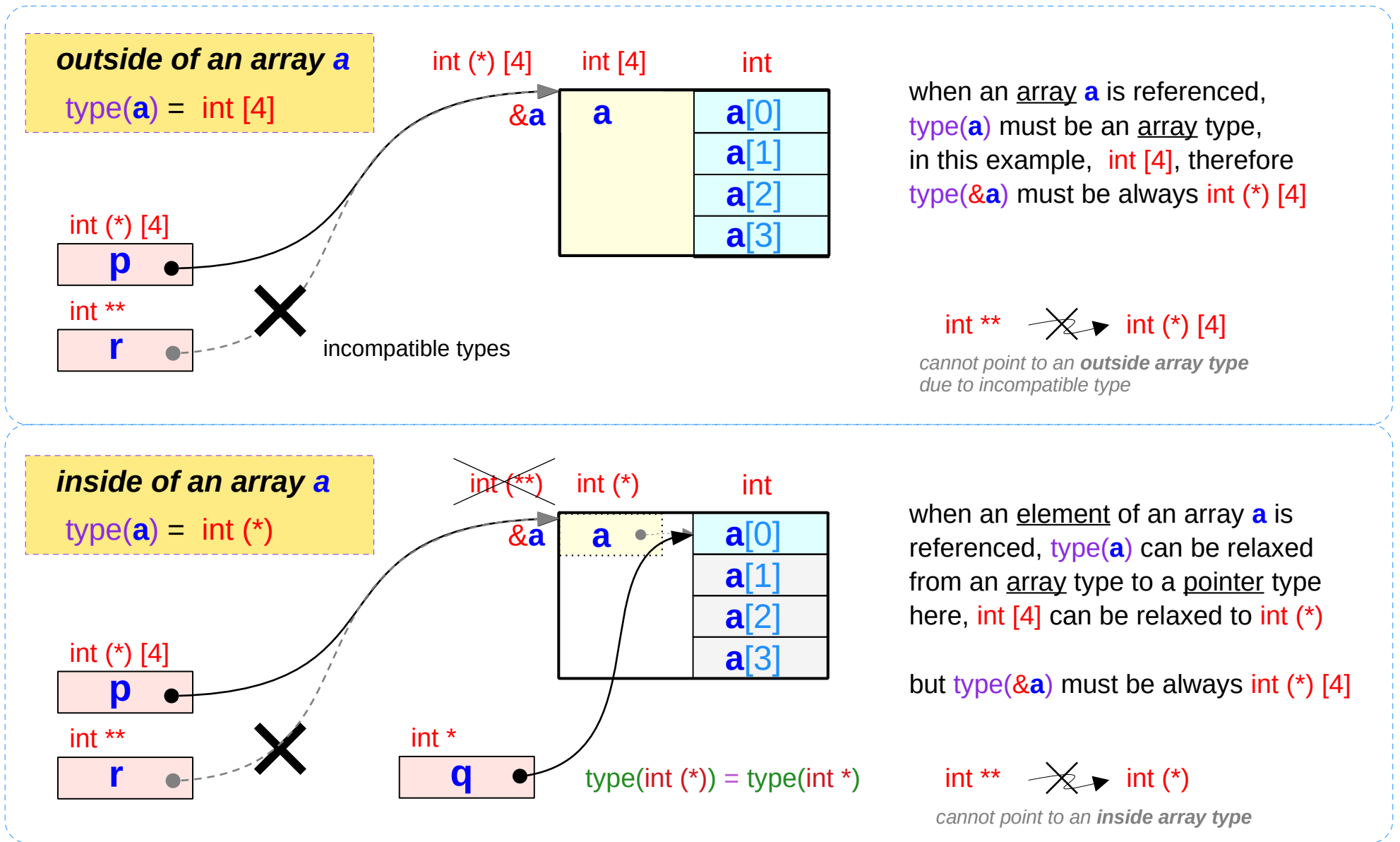
type(a) = int (*)



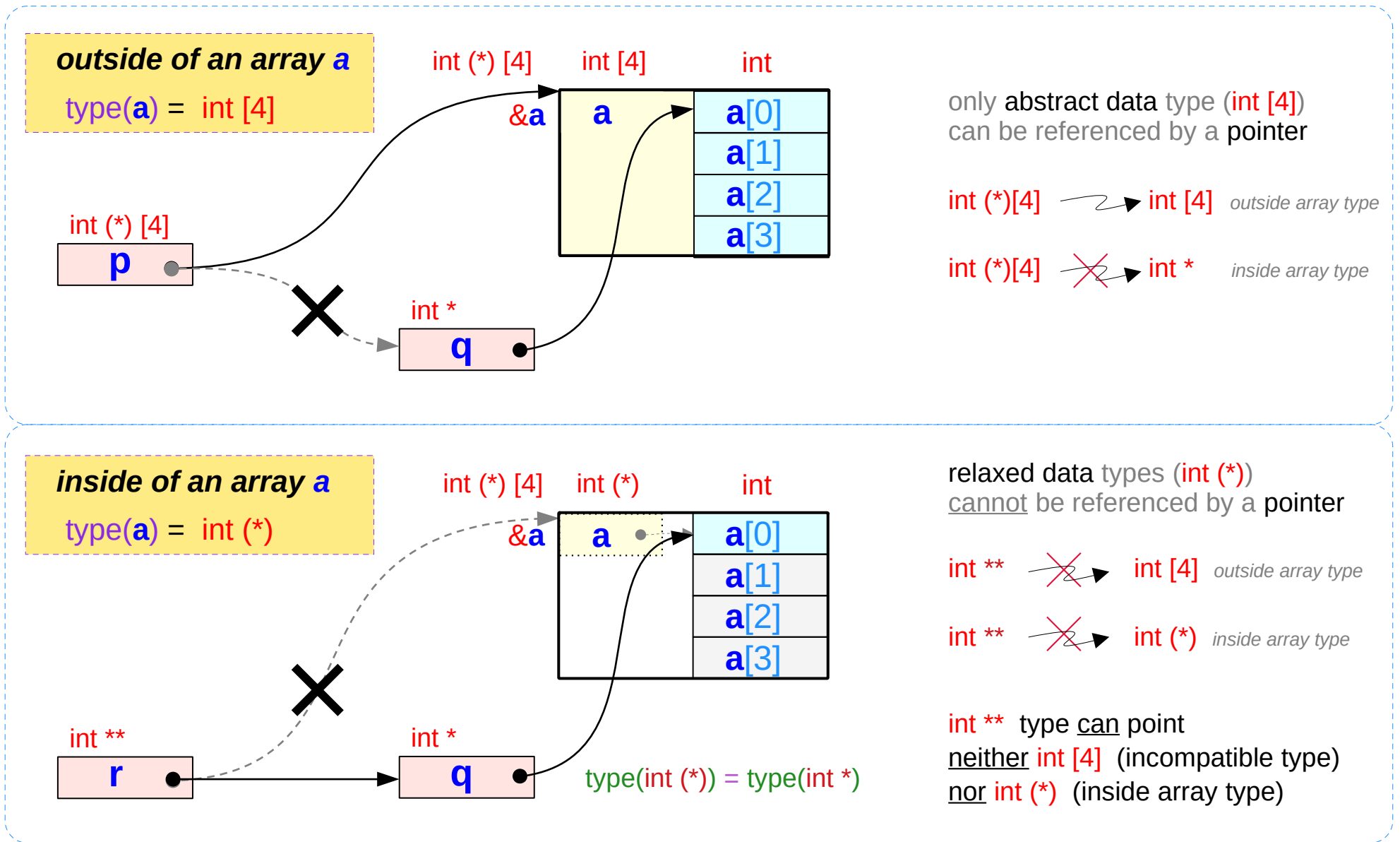
when accessing an array
outside of an array a

type(a) = int [4]
type(&a) = int (*) [4]
type(&a) ≠ int **

Outside and inside array types (2)



Outside and inside array types (3)



int * an integer pointer

int [2] a **1-d** array with 2 integer elements

int [3] a **1-d** array with 3 integer elements

Integer pointer and array types – `int *`, `int [2]`, `int [3]`

`int *a;`



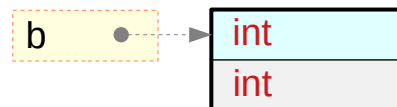
`int b[2];`

`int [2]` outside type



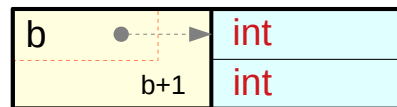
abstract data b – size

`int (*)` inside type



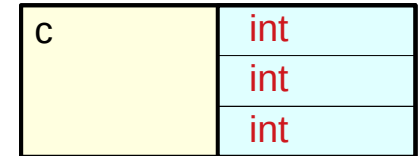
virtual pointer b – address

`int [2]` – size outside type
`int (*)` – address inside type



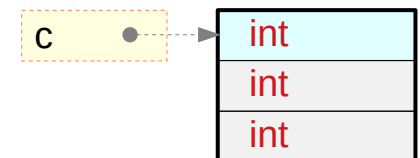
`int c[3];`

`int [3]` outside type



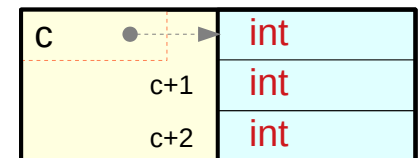
abstract data c – size

`int (*)` inside type



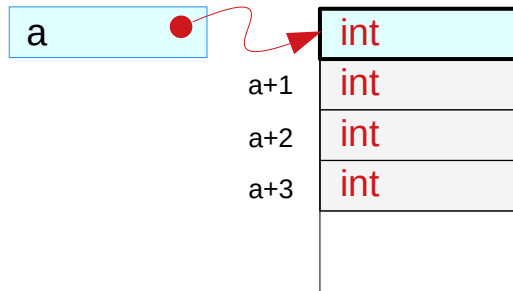
virtual pointer c – address

`int [3]` – size outside type
`int (*)` – address inside type



Incrementing pointers – `int *`, `int [2]`, `int [3]`

`int *a;`

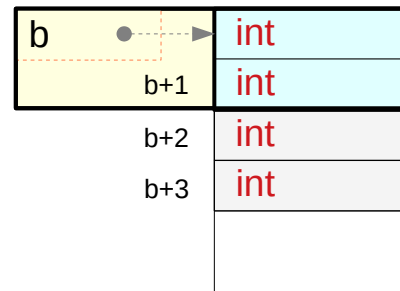


```
a[0] = *a
a[1] = *(a+1)
a[2] = *(a+2)
a[3] = *(a+3)
```

syntactically legitimate

programmers must ensure their validity

`int b[2];`

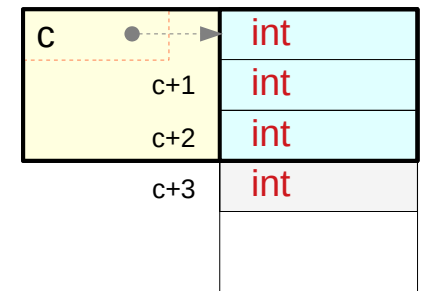


```
b[0] = *b
b[1] = *(b+1)
b[2] = *(b+2)
b[3] = *(b+3)
```

syntactically legitimate

programmers must ensure their validity

`int c[3];`



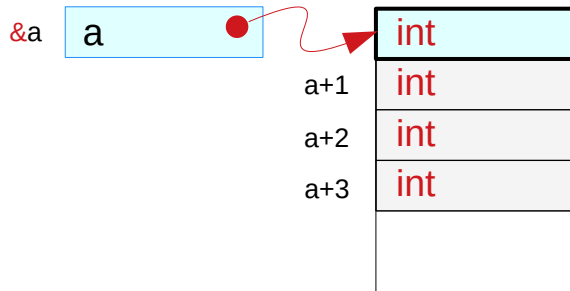
```
c[0] = *c
c[1] = *(c+1)
c[2] = *(c+2)
c[3] = *(c+3)
```

syntactically legitimate

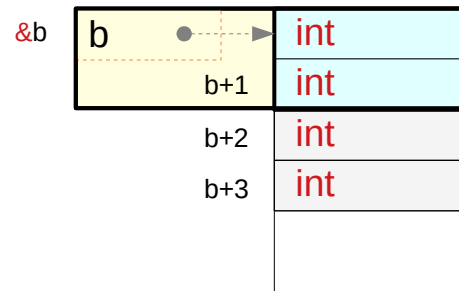
programmers must ensure their validity

Types and sizes – `int *`, `int [2]`, `int [3]`

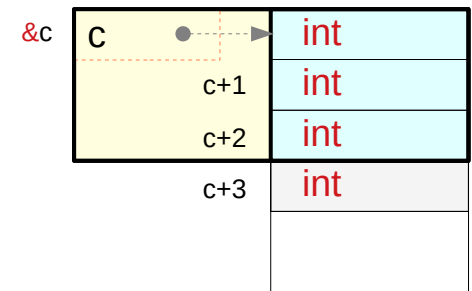
`int *a;`



`int b[2];`



`int c[3];`



`type(&a) = int **`

`type(a) = int *`

`type(*a) = int`

`value(&a) ≠ value(a)`

`sizeof(a)`
 = pointer size
 = `sizeof(int *)`

`type(&b) = int (*) [2]`

`type(b) = int [2] outside type`
`int (*) inside type`

`type(*b) = int`

`value(&b) = value(b)` address replication

`sizeof(b)`
 = `sizeof(*b) * 2`
 = `sizeof(int) * 2`

address replication
 &b and b evaluate the same address
 but have different types and sizes

`type(&c) = int (*) [3]`

`type(c) = int [3] outside type`
`int (*) inside type`

`type(*c) = int`

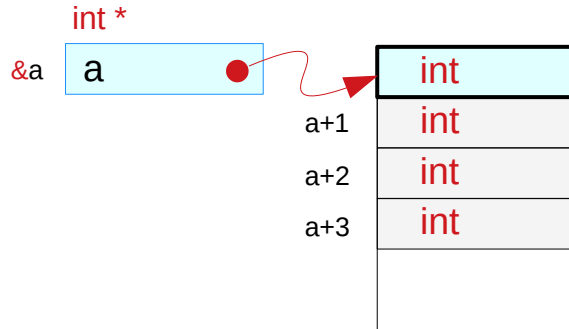
`value(&c) = value(c)` address replication

`sizeof(c)`
 = `sizeof(*c) * 3`
 = `sizeof(int) * 3`

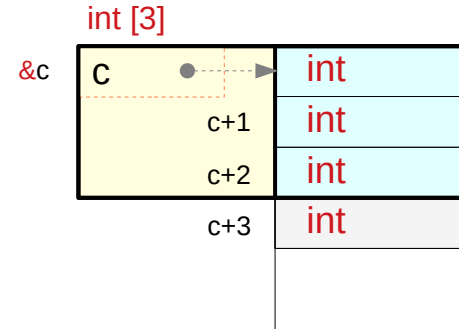
address replication
 &c and c evaluate the same address
 but have different types and sizes

Real pointer and virtual pointer types – `int *`, `int [3]`

`int *a;`



`int c[3];`



`sizeof (a) = pointer size` `int *`

`sizeof (c) = sizeof(*c) * 3` `int [3]`

`value(&a) ≠ value(a)` `int *`

`value(&c) = value(c)` `int (*)`

the address of **pointer** variable `a` is not equal to the pointed address
real memory location for `a`

the starting address of **array** variable `c` is equal to the address of the 1st element **address replication**
no actual memory location for `c`

`type(a) = int *`

`type(c) =` `int [3]` outside type
`int (*)` inside type

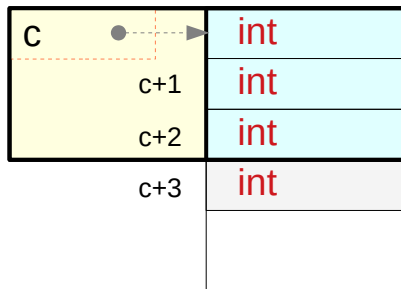
`type(&a) = int **`

`type(&c) = int (*) [3]`

Virtual pointer types of an array– `int [3]`

`int c[3];`

`int [3]` outside type



`sizeof (c) = sizeof(int) * 3`

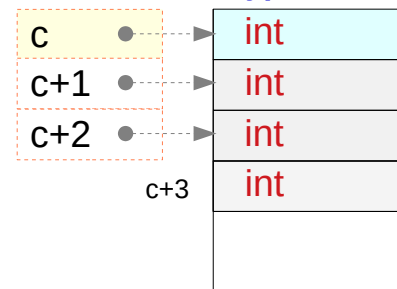
`value(&c) = value(c)` ← address replication →

`type(c) = int [3]` outside type

`type(&c) = int (*) [3]`

`int c[3];`

`int (*)` inside type



`sizeof (c) = sizeof(*c) * 3` ... leading element

`sizeof (c+1) = pointer size`

`sizeof (c+2) = pointer size`

`value(&c) = value(c)` ... leading element

`value(c+1) = value(c) + sizeof(*c) *1`

`value(c+2) = value(c) + sizeof(*c) *2`

`type(c) = int *` inside type

`type(c+1) = int *`

`type(c+2) = int *`

`type(&c) = int (*) [3]`

Array Pointers v.s. Pointer Arrays

Array pointers and pointer arrays

1. **array pointer** `p` – a pointer to an array of `int [4]` type

```
int (*p) [4];
```

2. **pointer array** `x` – an array of pointers of `int *` type

```
int *x [4];
```

Types of array pointer **p** and pointer arrays **y**

array pointer:
a pointer to an array

int **(*p)** **[4]** ;

(*p) is an array with 4 elements
each element is an integer
p is a pointer to such an array

the type of **(*p)** : **int [4]**
the type of **p** : **int (*) [4]**

pointer array:
an array of pointers

int * **y** **[4]** ;

y is an array with 4 elements
each element is an integer pointer

the type of **y** : **int * [4]**

[] has a higher priority than *****

(*p) must be grouped with **[4]**
y must be grouped with **[4]**

Types of array elements $(*p)[i]$ and $y[i]$

array pointer:
a pointer to an array

`int (*p)[4];`

$(*p)[i]$

in a statement

$(*p)$ is an array with 4 elements
 $(*p)[0], (*p)[1], (*p)[2], (*p)[3]$
the type of elements : `int`

pointer array:
an array of pointers

`int *y[4];`

$y[i]$

in a statement

y is an array with 4 elements
 $y[0], y[1], y[2], y[3]$
the type of elements : `int *`

`int *y[4];`

$*y[i]$

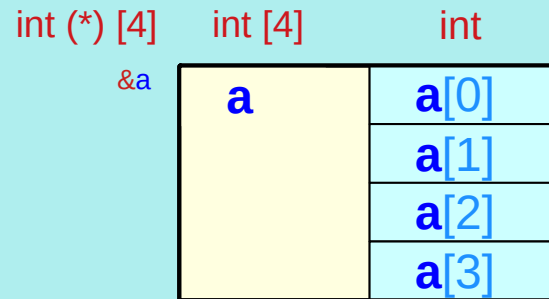
in a statement

y is an array with 4 elements
 $*y[0], *y[1], *y[2], *y[3]$
the type of dereferenced elements : `int`

Array pointer **p**, array ***p**, integer **(*p)[i]**

integer array:
an array of integers

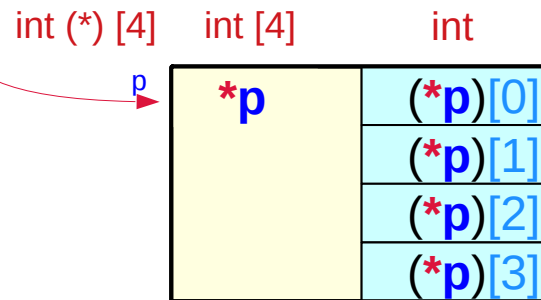
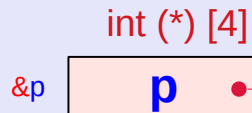
```
int a [4];
```



p = &a; ↓ ***p ≡ a**

array pointer:
a pointer to an array

```
int (*p) [4];
```

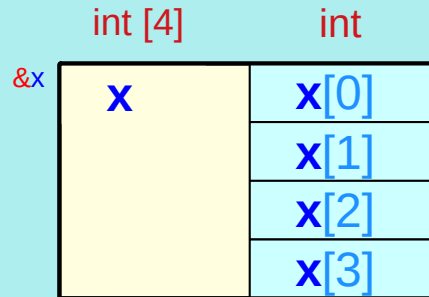


(*p)[i] ≠ *p[i]
parenthesis is necessary

Pointer array **y**, integer pointer **y[i]**, integer ***y[i]**

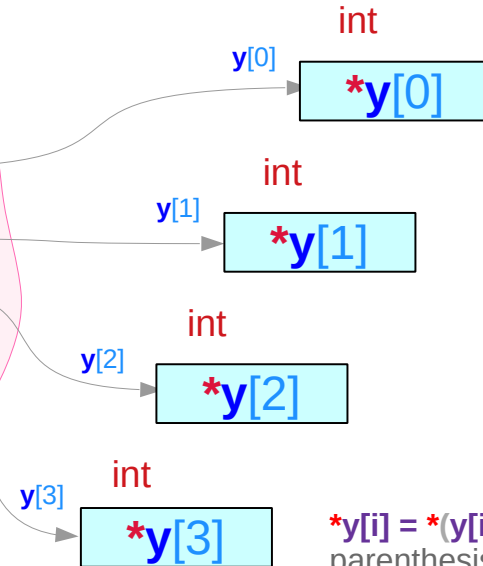
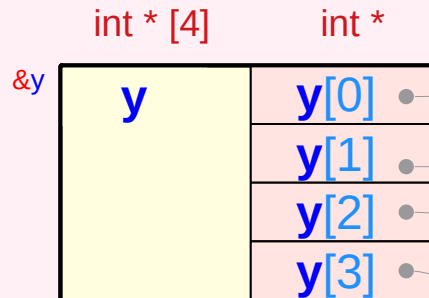
integer array:
an array of integers

```
int x[4];
```



pointer array:
an array of pointers

```
int * y[4];
```



***y[i] = *(y[i])**
parenthesis is not necessary

Array pointers **p** v.s. pointer arrays **y**

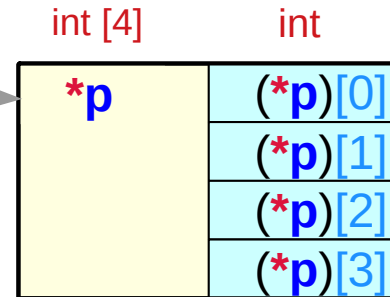
`int (*) [4]`
&p `p`

array pointer:
a pointer to an array

```
int (*p) [4];
```

`p = &x;` `*p ≡ x`

```
int x [4];
```

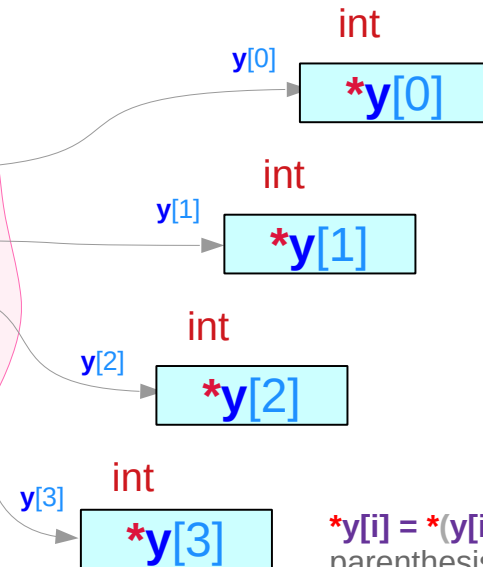


`(*p)[i] ≠ *p[i]`
parenthesis is necessary

pointer array:
an array of pointers

```
int * y [4];
```

| int * [4] | int * |
|----------------|-------------------|
| <code>y</code> | <code>y[0]</code> |
| | <code>y[1]</code> |
| | <code>y[2]</code> |
| | <code>y[3]</code> |



`*y[i] = *(y[i])`
parenthesis is not necessary

Array pointers **p** v.s. array pointer **q**

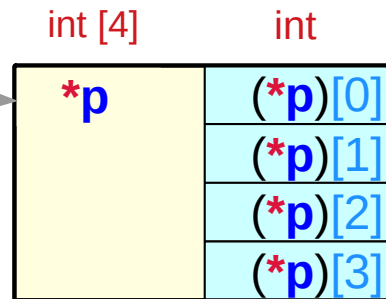
int (*) [4]
&p

p

array pointer:
a pointer to an array

int (*p) [4];

p = &x; *p ≡ x



int x [4];

(*p)[i] ≠ *p[i]
parenthesis is necessary

int * y [4];

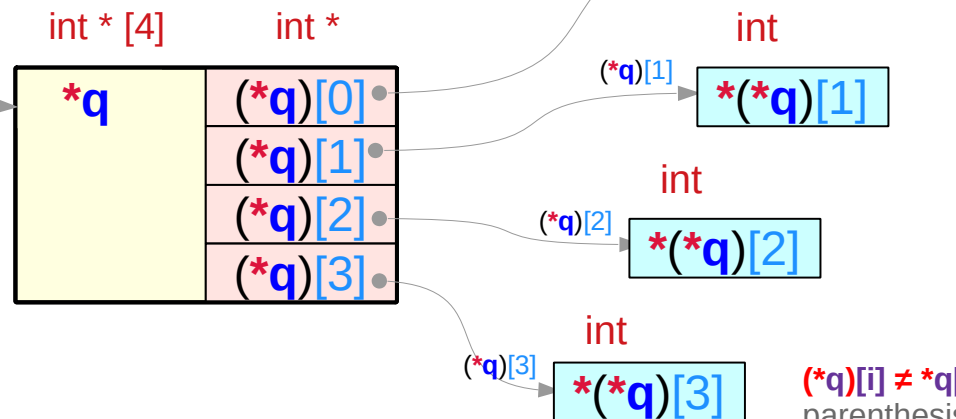
int * (*) [4]
&q

q

array pointer:
a pointer to an array

int * (*q) [4];

q = &y; *q ≡ y



(*q)[i] ≠ *q[i]
parenthesis is necessary

Correspondence of pointer dereference ***n**, ***p**, ***fp**

```
int m ;
```

```
int *n ;
```

an integer pointer **n**

m and ***n** : an integer (**int**)

a and ***p** : a 1-d array (**int [4]**)
with 4 integer elements

f and ***fp** : a function (**int (int, int)**)
taking two integers
returning an integer

```
int a [4] ;
```

```
int (*p) [4] ;
```

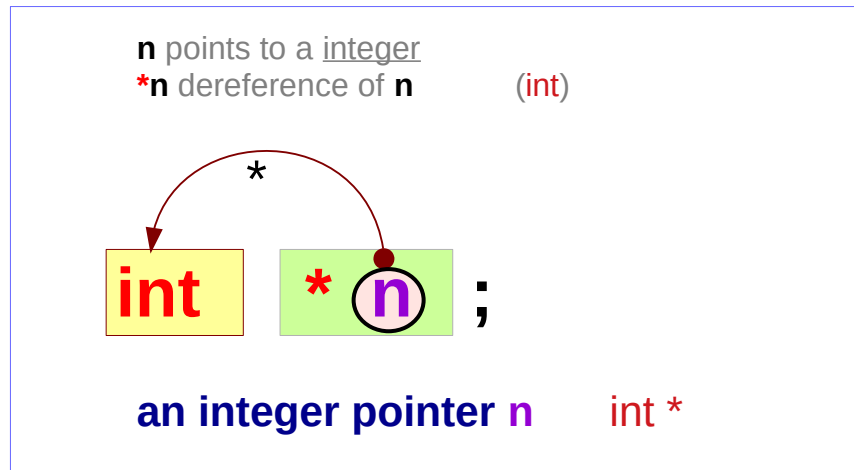
a 1-d array pointer **p**

```
int f (int, int) ;
```

```
int (*fp) (int, int) ;
```

a function pointer **fp**

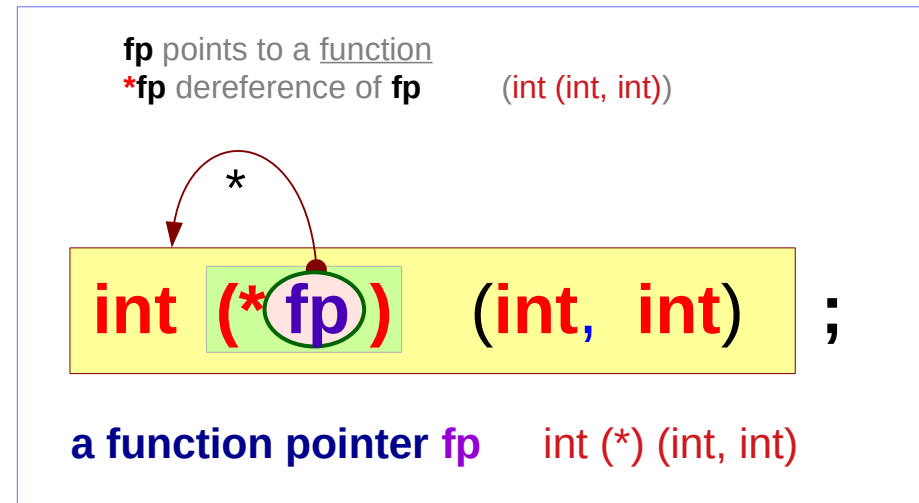
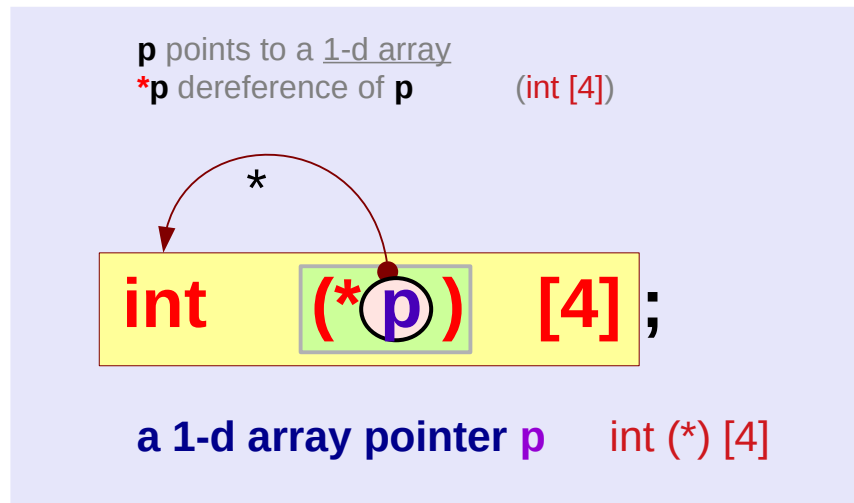
Variables and pointed types



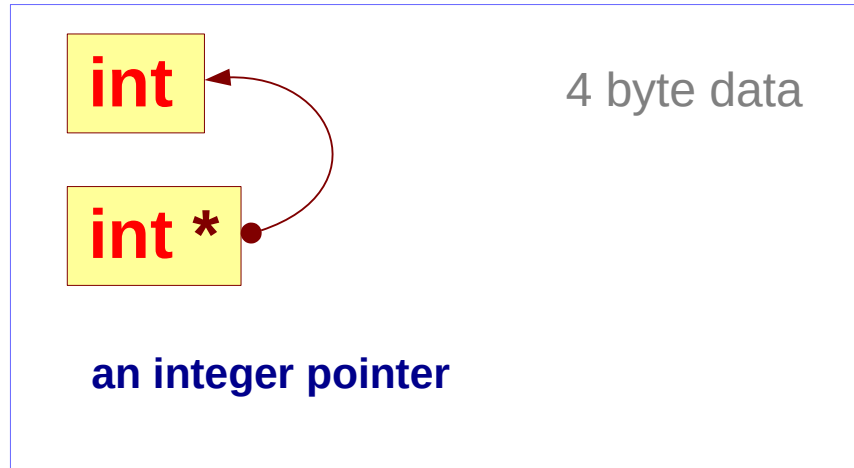
n points to an integer

p points to a 1-d array
that has 4 integer elements

fp points to a function
that takes two integers
returns an integer



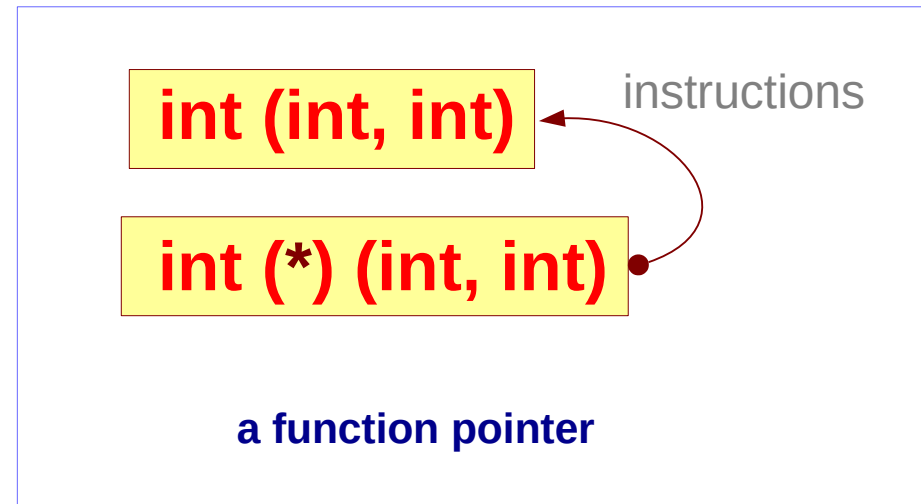
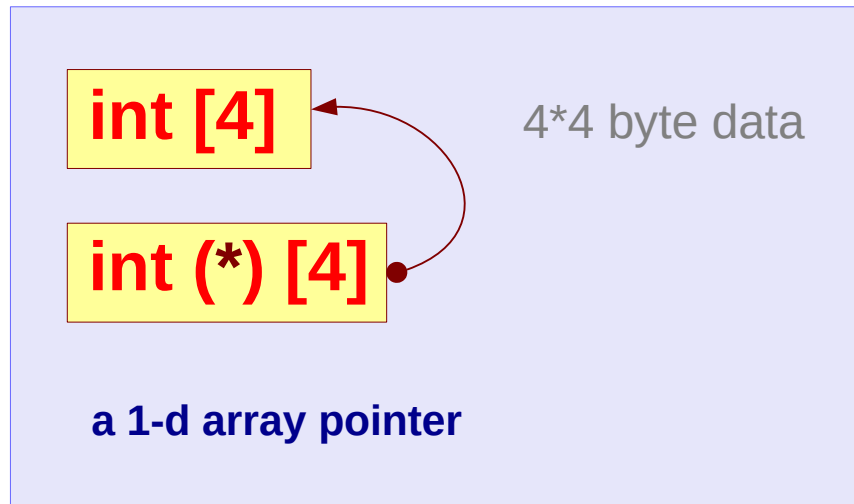
Referring and referenced types



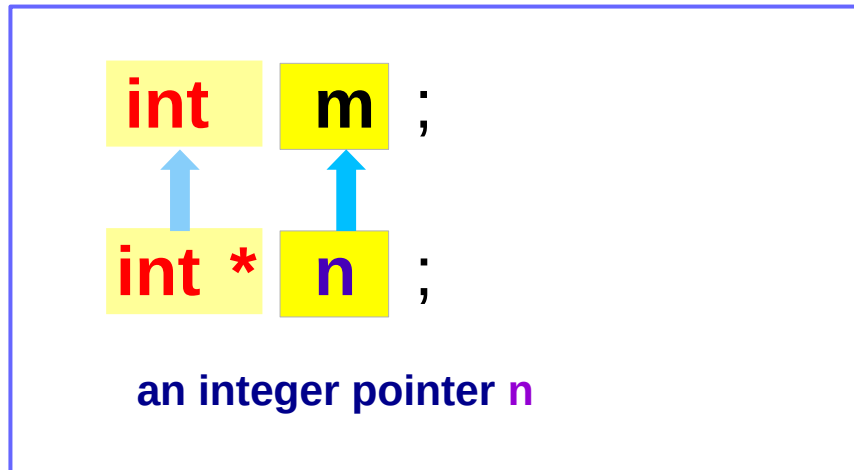
`int *` type variable
points to an `int` type data

`int (*) [4]` type variable
points to an `int [4]` type data

`int (*) (int, int)` type variable
points to an `int (int, int)` type function



Correspondence of pointer reference n , $y[i]$

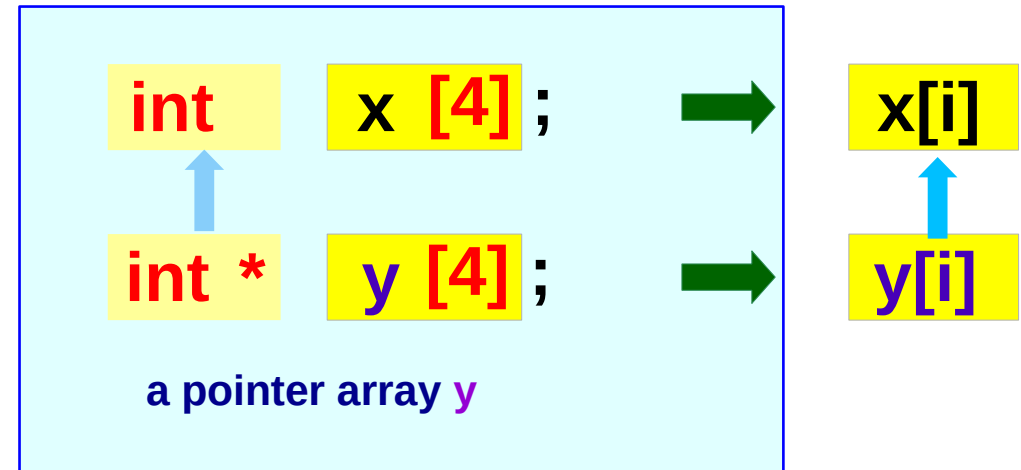


m : an integer

n : an integer pointer

n can point to m

$n = \&m ;$
 $*n \equiv m$



$x[i]$: an integer

$y[i]$: an integer pointer

$y[i]$ can point to $x[i]$

$y[i] = \&x[i] ;$
 $*y[i] \equiv x[i]$

`[]` has a higher priority than `*`

$*y[i] = *(y[i])$ unnecessary parenthesis

Element types of a pointer array y

```
int * y [4];
```

`[]` has a higher priority than `*`

y must be grouped with `[4]`

```
int x [4];
```

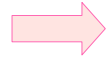


```
x[i]
```

x is a **1-d array** with 4 elements

each element $x[i]$, $i=0, 1, 2, 3$ has the type of an **integer (int)**

```
int * y [4];
```



```
y[i]
```

integer
pointer

y is a **1-d array** with 4 elements

each element $y[i]$, $i=0, 1, 2, 3$ has the type of an **integer pointer (int *)**

```
int *y [4];
```



```
*y[i]
```

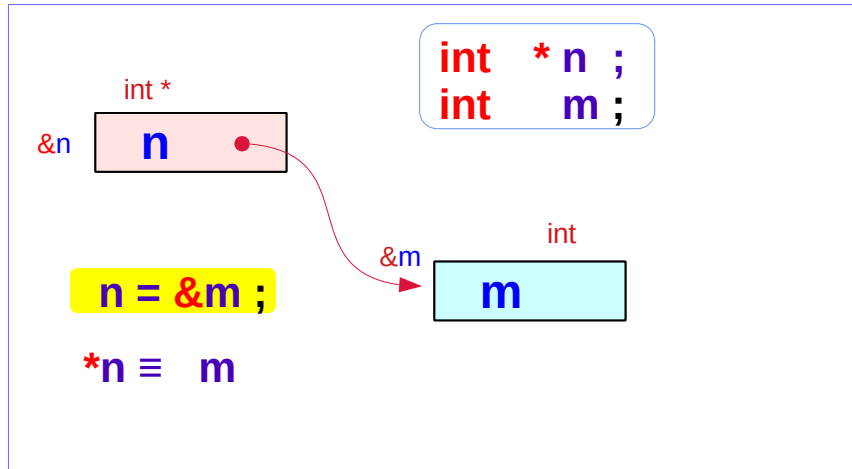
integer

y is a **1-d array** with 4 elements

the **dereference** of each element $*y[i]$, $i=0, 1, 2, 3$ is an **integer**

here, $*y[i] = *(y[i])$

Assigning pointer variables **n**, **p**, **fp**



n : a pointer to an integer

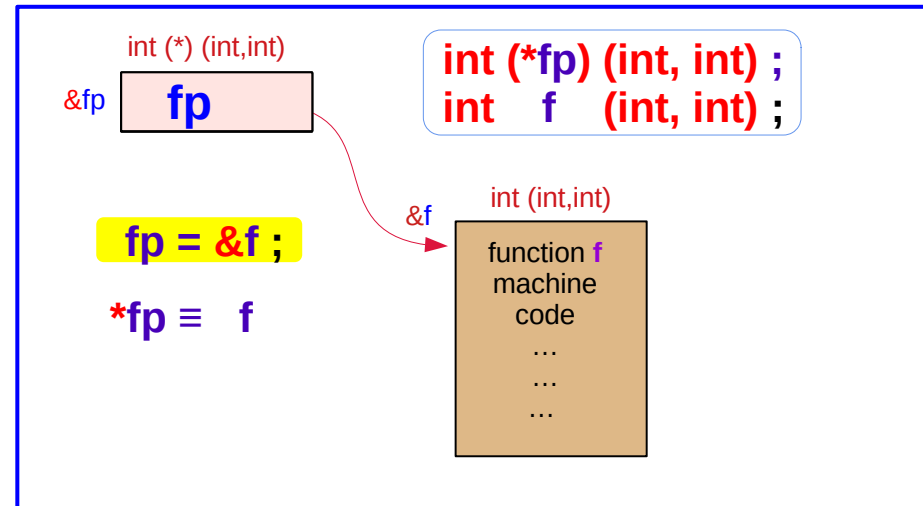
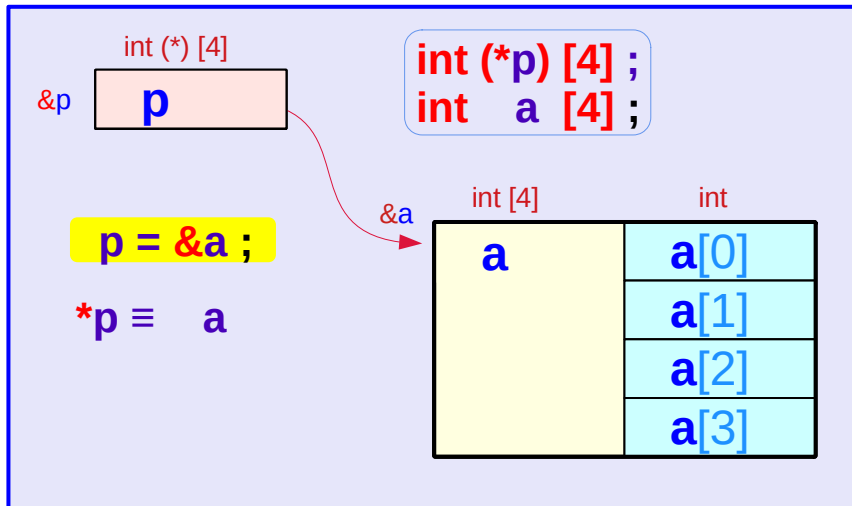
`int *`

p : a pointer to a 1-d array
with 4 integer elements

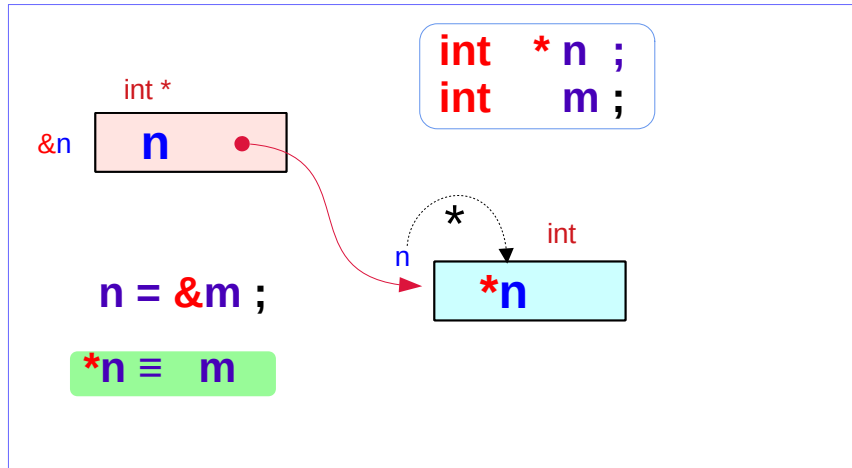
`int (*) [4]`

fp : a pointer to a function
that takes two integers
and returns an integer

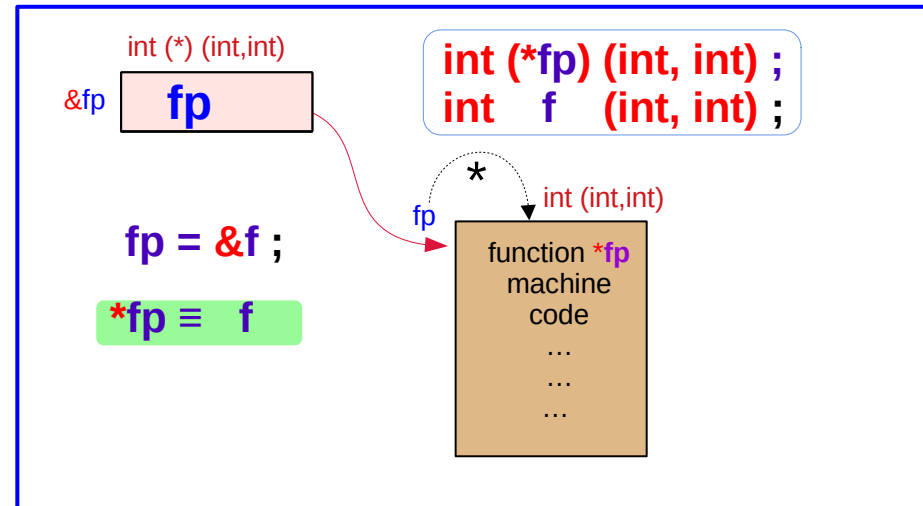
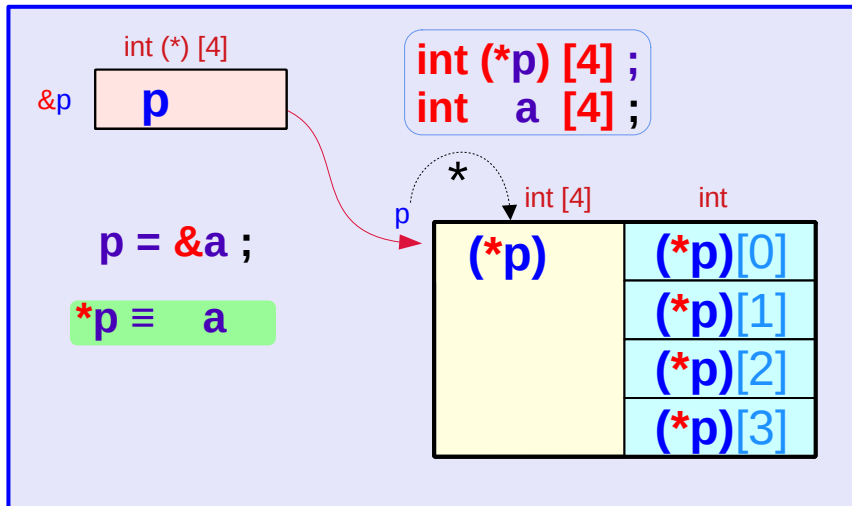
`int (*) (int, int)`



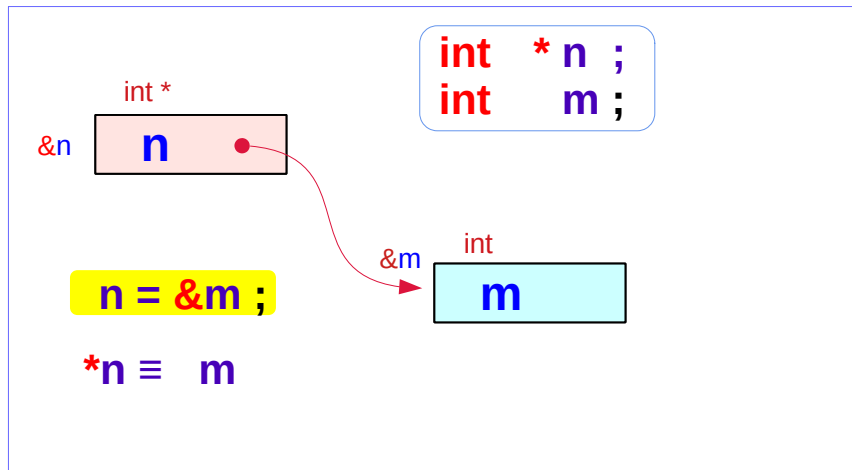
Dereferencing pointer variables **n**, **p**, **fp**



- `*n` : an integer `int`
- `*p` : a 1-d array with 4 integer elements `int [4]`
- `*fp` : a function that takes two integers and returns an integer `int (int, int)`



Assigning pointer variables **n** and **y[i]**



m : an integer

`int`

n : an integer pointer

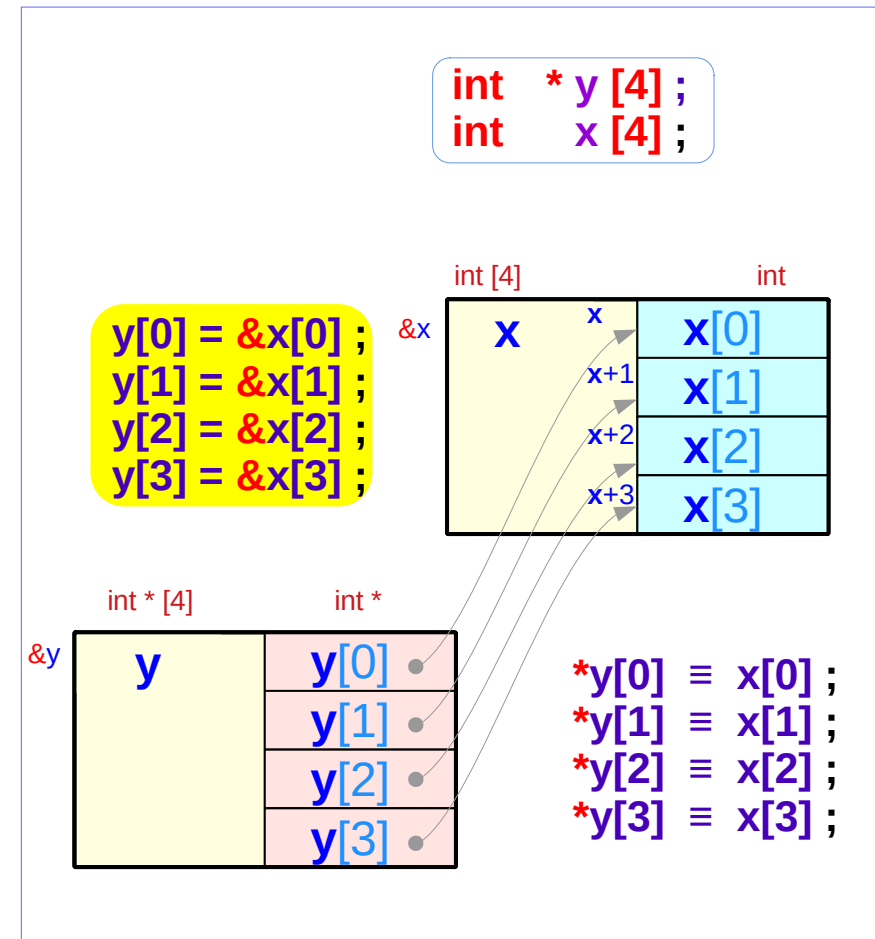
`int *`

x : a 1-d array with
4 integer elements

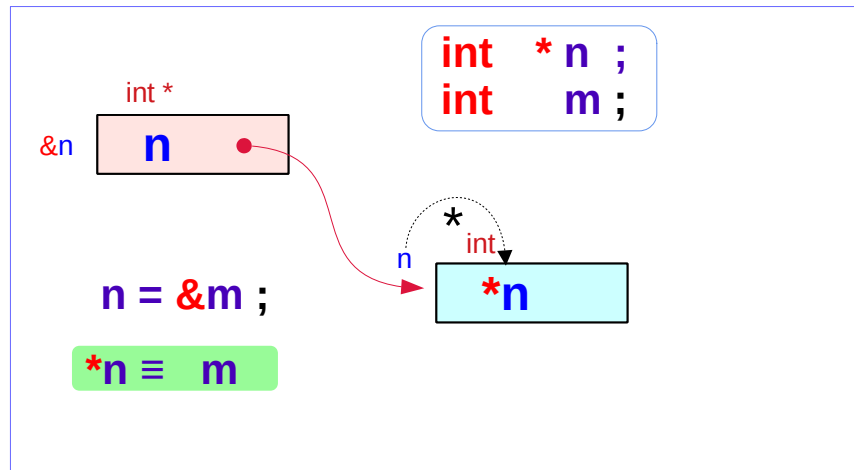
`int [4]`

y : a 1-d array with
4 integer pointer elements

`int * [4]`



Dereferencing pointer variables **n** and **y[i]**



`n` : an integer pointer

`int *`

`*n` : an integer

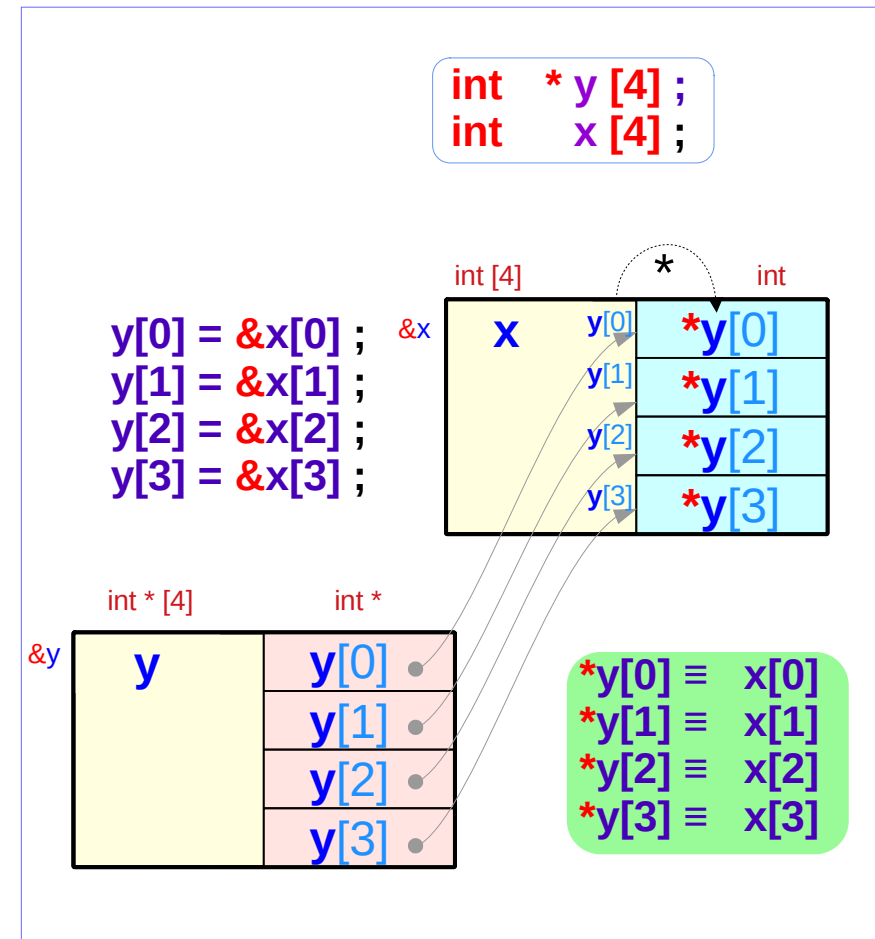
`int`

`y[i]` : an integer pointer

`int *`

`*y[i]` : an integer

`int`



Array pointers

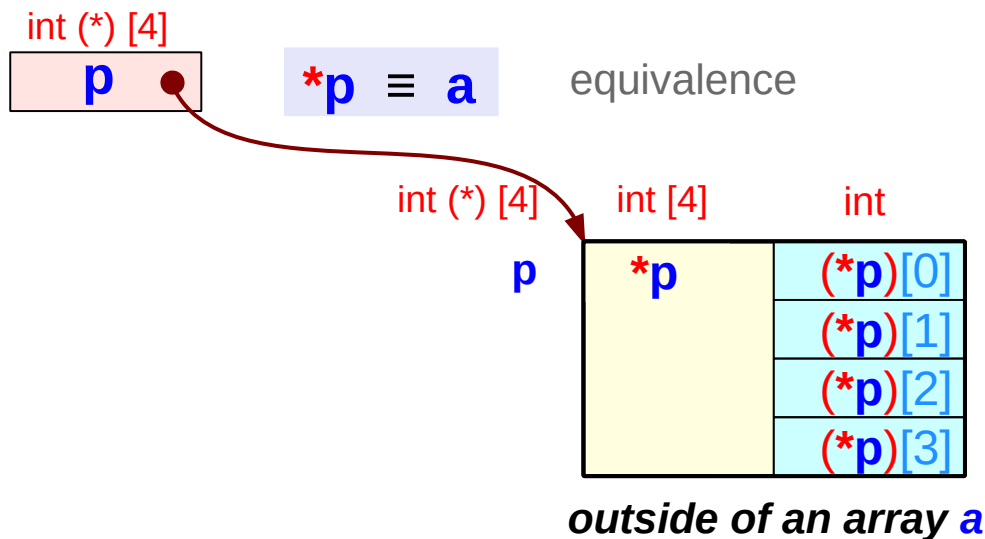
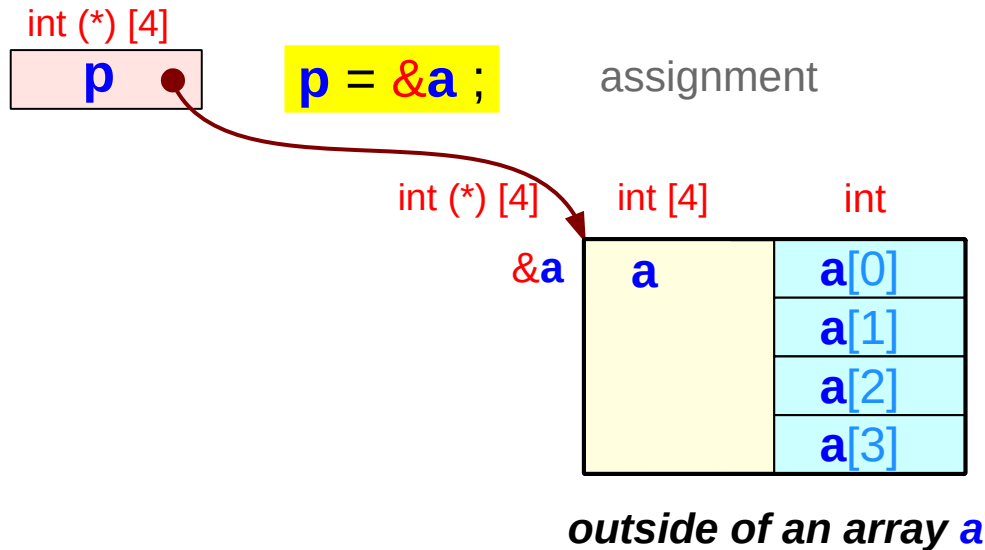
pointer to a **1-d** array **a** and its **0-d** sub-array **a[0]**

```
int (*p) [4];    (1-d array pointer)    int a [4];    (1-d array)
int (*q) ;      (0-d array pointer)
```

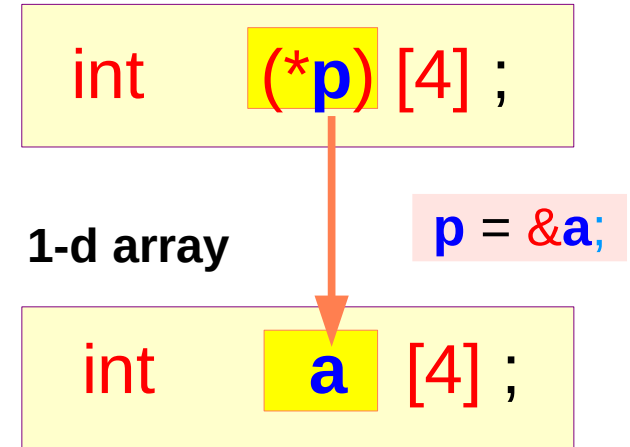
pointer to a **2-d** array **c** and its **1-d** sub-array **c[0]**

```
int (*p) [3][4] ; (2-d array pointer)    int c [3][4]; (2-d array)
int (*q) [4] ;   (1-d array pointer)
```

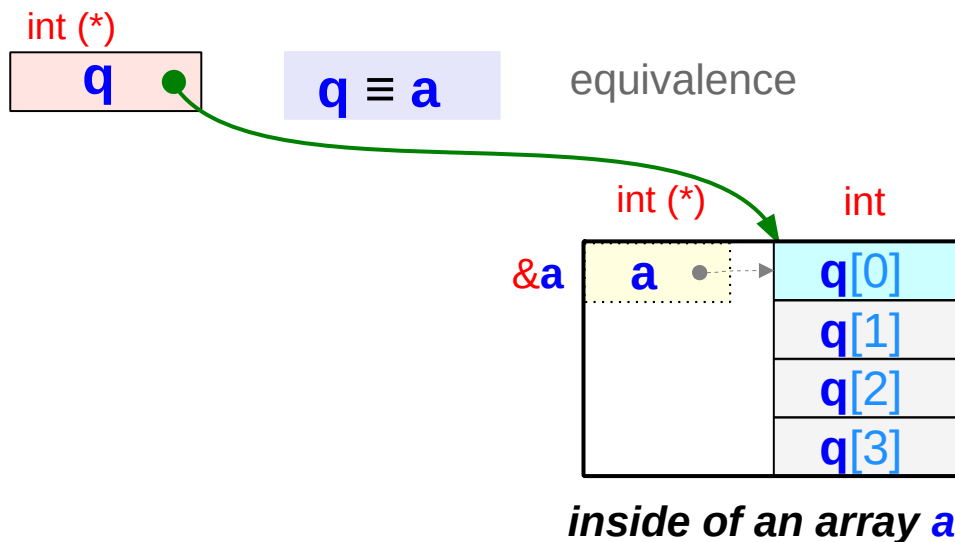
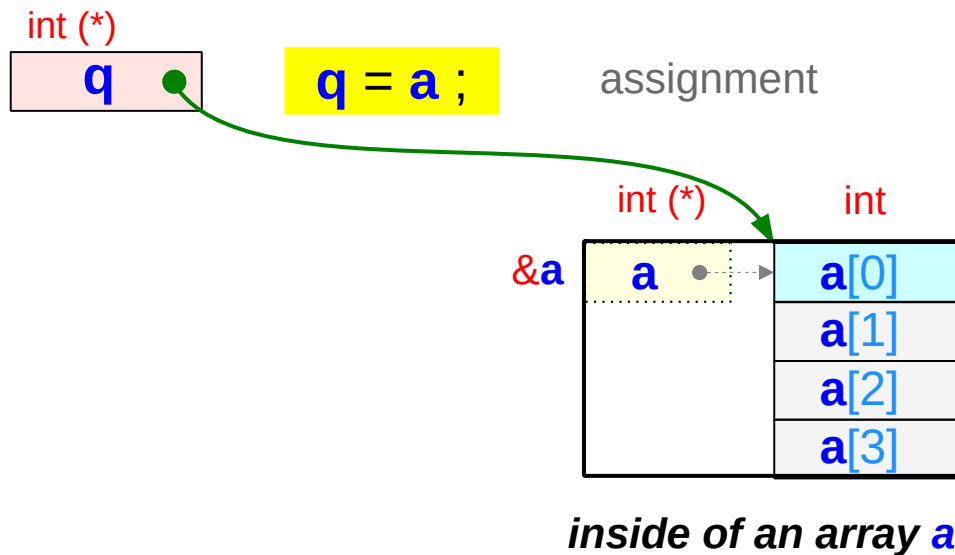
1-d array pointer **p** to a 1-d array **a**



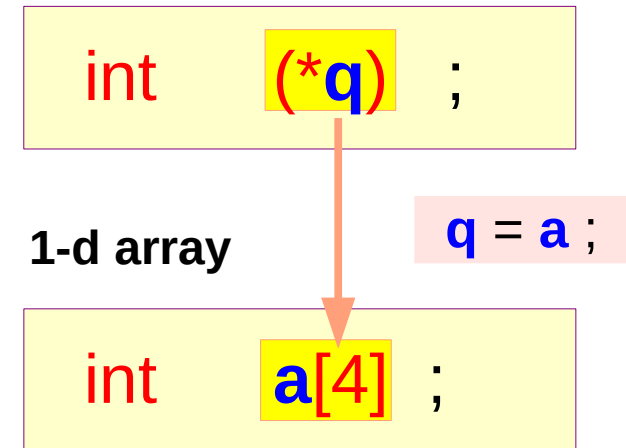
1-d array pointer



0-d array pointer q to a 0-d sub-array $a[0]$



0-d array pointer



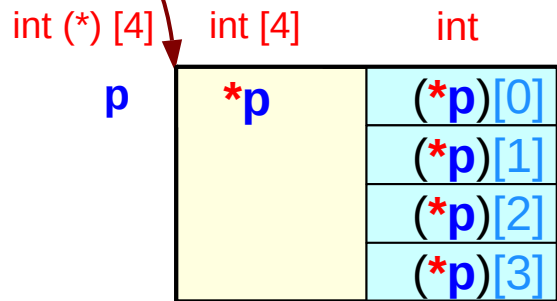
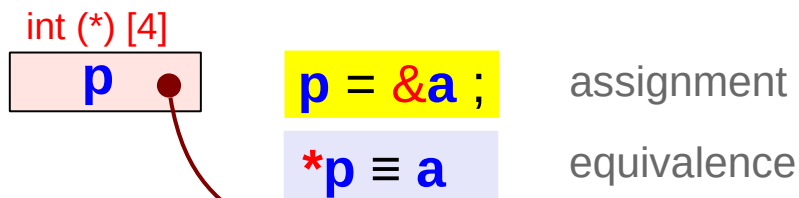
$a[i]$
 $a[0]$

$\&a[0] = \&*(a+0) = a$

1-d array access using **p** and **q**

```
int (*p) [4] = &a;
```

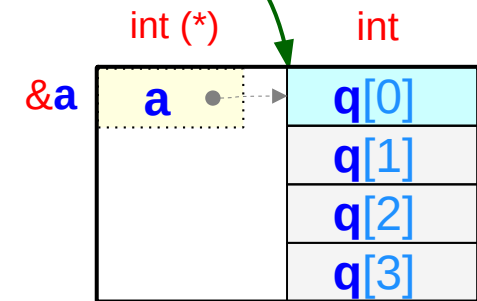
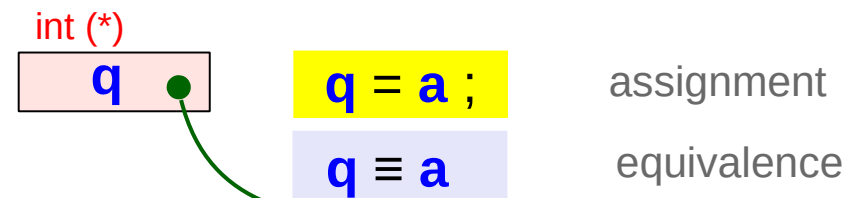
1-d array pointer



outside of an array a

```
int (*q) = a;
```

0-d array pointer

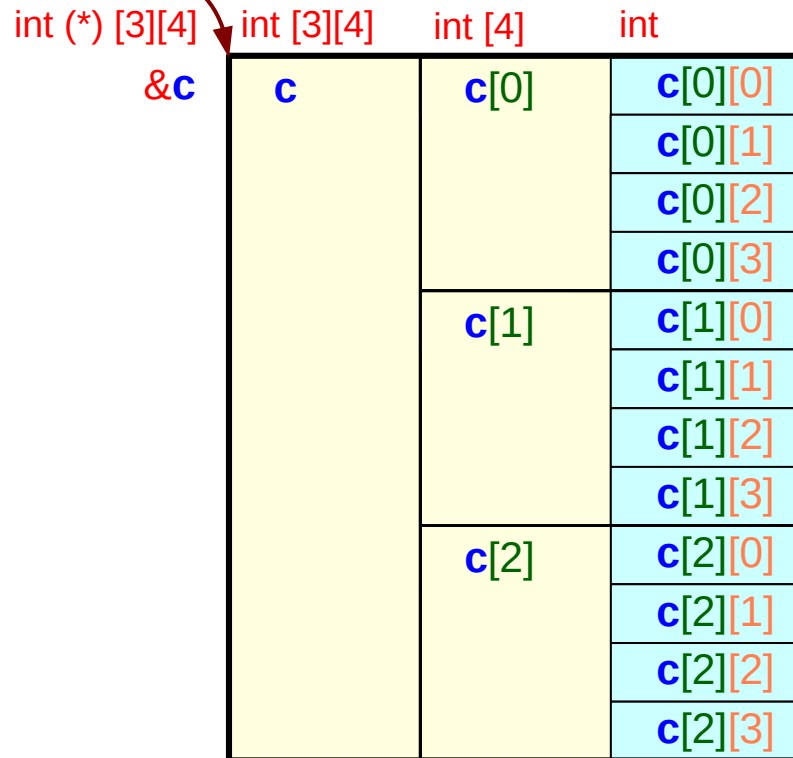


inside of an array a

2-d array pointer **p** to a 2-d array **c** – reference

2-d array pointer

`int (*) [3][4]`
`p` `p = &c ;` assignment



*outside of an array **c***

2-d array pointer

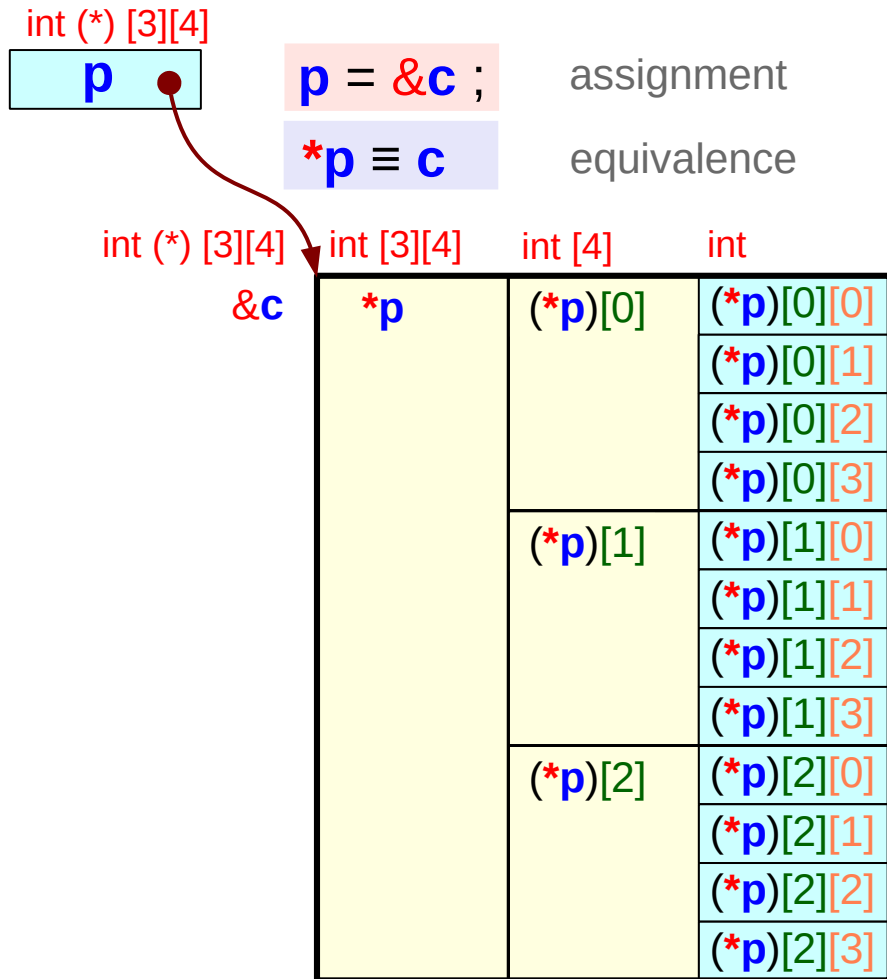
`int (*p) [3][4] ;`

2-d array

`int c [3][4] ;`

2-d array pointer **p** to a 2-d array **c** – dereference

2-d array pointer



*outside of an array **c***

2-d array pointer

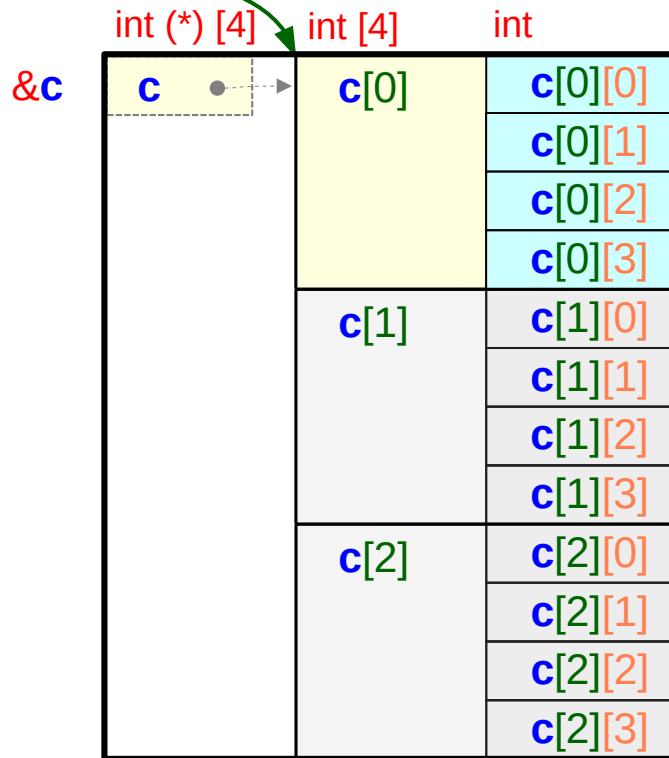
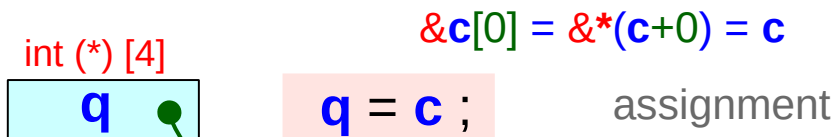
```
int (*p) [3][4] ;
```

2-d array

```
int c [3][4] ;
```

1-d array pointer q to a 1-d subarray $c[0]$ – reference

1-d array pointer



inside of an array c outside of an array $c[0]$

1-d array pointer

$\text{int } (*q) [4];$

1-d subarray

$\text{int } c[3] [4];$

Declaration:

$[3]$ means there are 3 elements

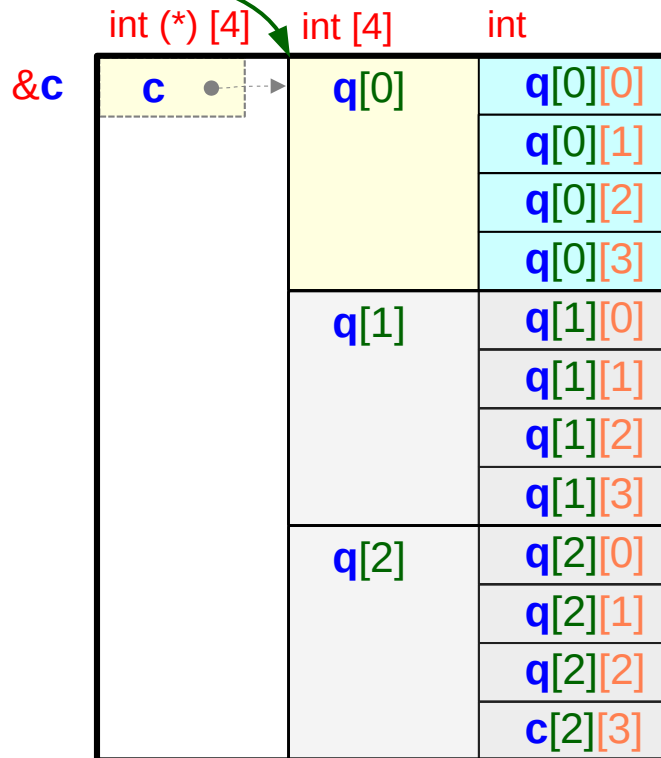
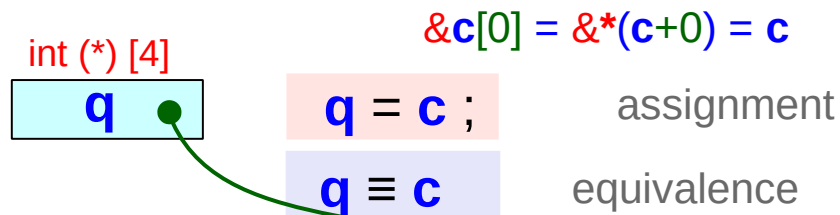
Expression:

$[0], [1], [2]$ are used

among 3 elements $c[0], c[1], c[2]$,
consider the first one $c[0]$

1-d array pointer q to a 1-d subarray $c[0]$ – dereference

1-d array pointer



inside of an array c *outside of an array $c[0]$*

1-d array pointer

```
int (*q) [4] ;
```

1-d subarray

```
int c[3] [4] ;
```

Declaration:

$[3]$ means there are 3 elements

Expression:

$[0], [1], [2]$ are used

among 3 elements $c[0], c[1], c[2]$,
consider the first one $c[0]$

2-d array access using p and q

2-d array pointer

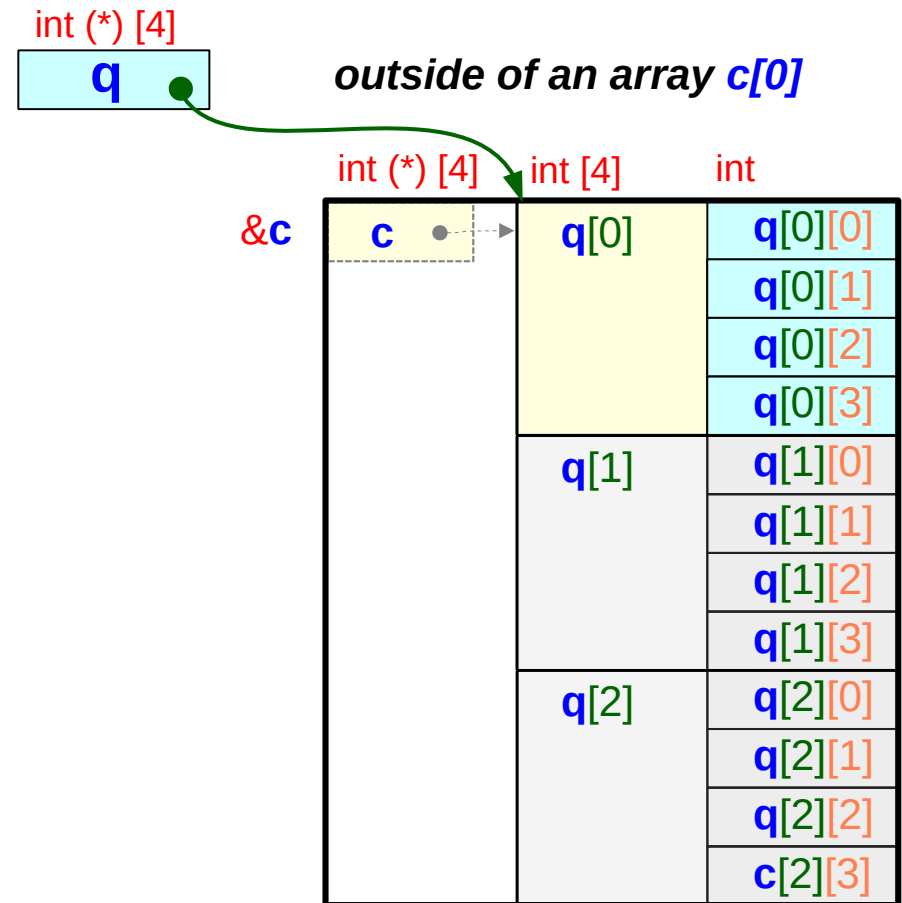
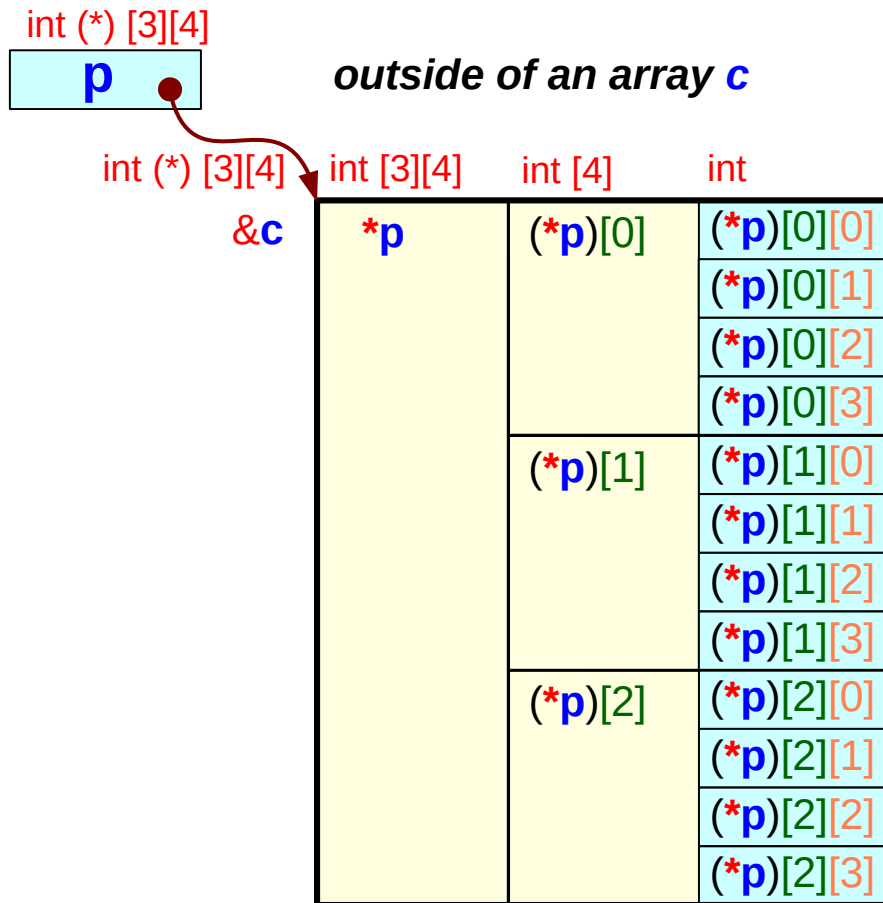
```
int (*p)[3][4] = &c;
```

```
p = &c ;
*p ≡ c
```

1-d array pointer

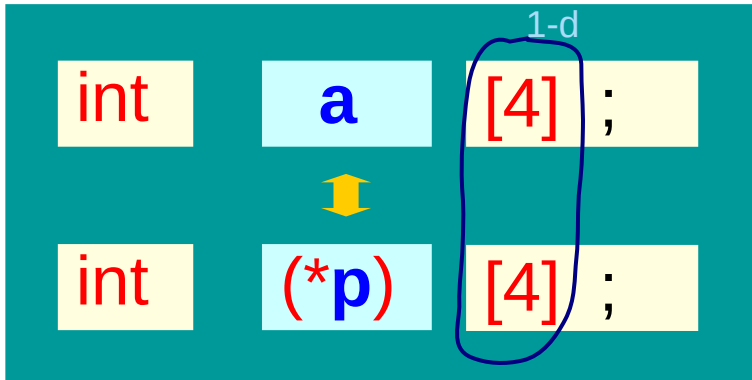
```
int (*q)[4] = c;
```

```
q = &c[0] ;
q ≡ c
```



1-d and 0-d array pointers to an 1-d array

1-d array pointer



int (*) [4]

***p** ≡ **a**

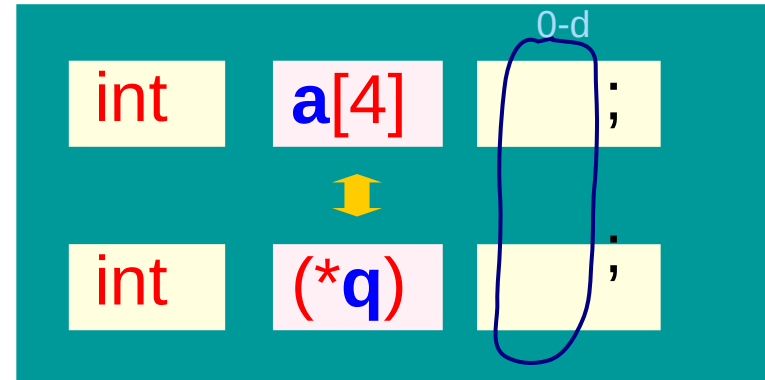
equivalence

p = **&a**;

assignment

(*p)[i] ≡ **a[i]** ≡ **p[0][i]**

0-d array pointer : int pointer



int (*)

***q** ≡ **a[0]**

equivalence

q = **a**;

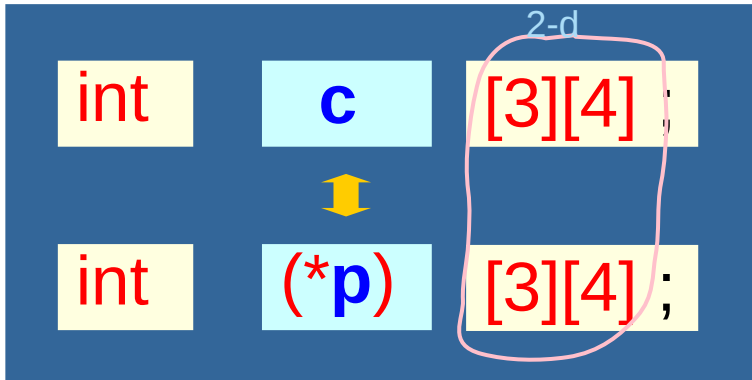
assignment

q[i] ≡ **a[i]** ≡ ***(q+i)**

among 4 elements **a[0]**, **a[1]**, **a[2]**, **a[3]**,
consider the first one **a[0] = *a**

2-d and 1-d array pointers to a 2-d array

2-d array pointer



int (*) [3][4]

***p** ≡ **c**

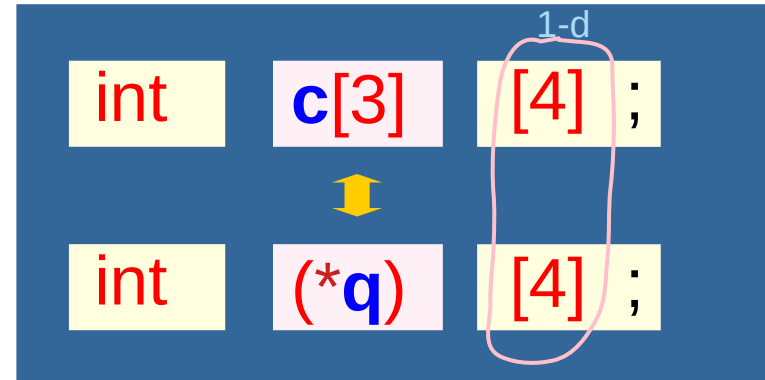
equivalence

p = **&c**;

assignment

(*p)[i][j] ≡ **c[i][j]** ≡ **p[0][i][j]**

1-d array pointer



int (*) [4]

***q** ≡ **c[0]**

equivalence

q = **c**;

assignment

q[i][j] ≡ **c[i][j]** ≡ **(* (q+i))[j]**

among 3 elements **c[0]**, **c[1]**, **c[2]**,
consider the first one **c[0]** = ***c**

Extended references of 1-d & 2-d array pointers

1-d array pointer

```
int (*p) [4];
```



```
int c[4] [4];
```

```
(*p)[j] ≡ c[0][j]  
(*p)
```

minimal
reference

```
p[i][j] ≡ c[i][j]  
(*p+i)
```

extended
reference

2-d array pointer

```
int (*q) [3][4];
```



```
int c [3][4];
```

```
(*q)[i][j] ≡ c[i][j]  
(*q)
```

minimal
reference

```
q[m][i][j]  
(*q+m)
```

extended
reference

Accessing a 2-d array using a 2-d & 1-d array pointers

1-d array pointer

```
int (*p) [4];
```



```
int c[4] [4];
```

```
(*p)[j]
```

1-d array access
minimal

```
p [i][j]
```

2-d array access
extended

2-d array pointer

```
int (*q) [3][4];
```



```
int c [3][4];
```

```
(*q) [i][j]
```

2-d array access
minimal

```
q[m] [i][j]
```

3-d array access
extended

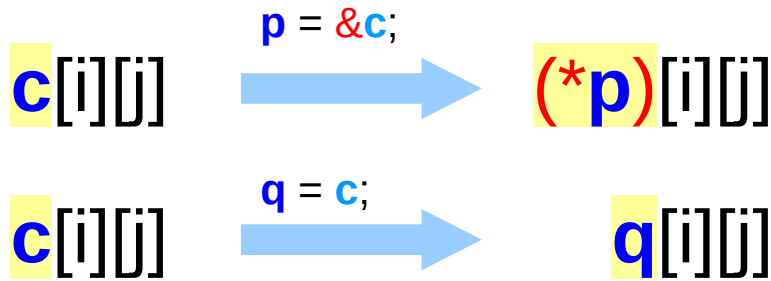
Array pointers to a 2-d array and its sub-array

```
int c [3] [4] ;  
int (*p) [3] [4] = &c ;  
int ( * q ) [4] = &c[0] ; (= c)
```

2-d array **c**

2-d array pointer **p**

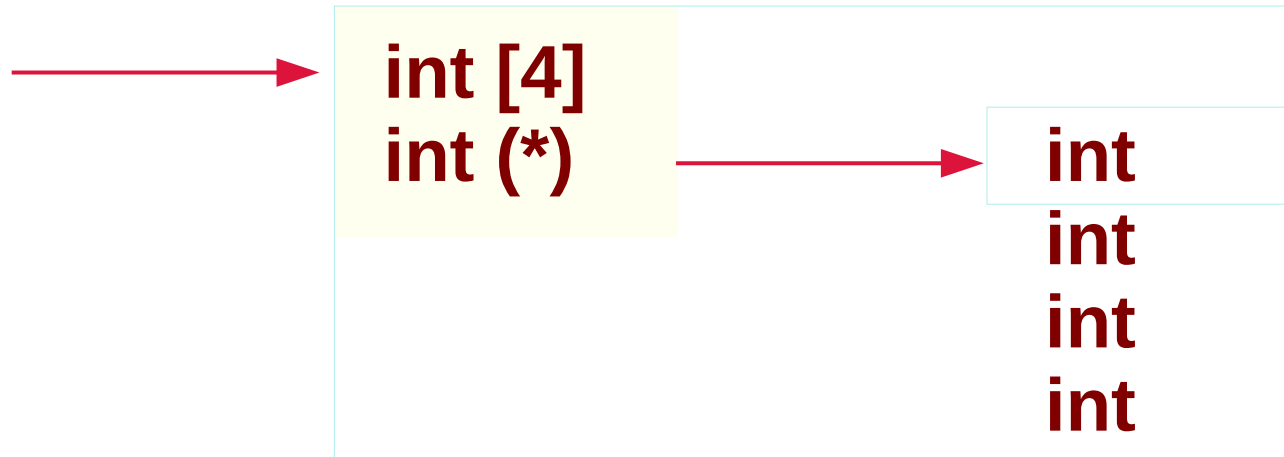
1-d array pointer **q**



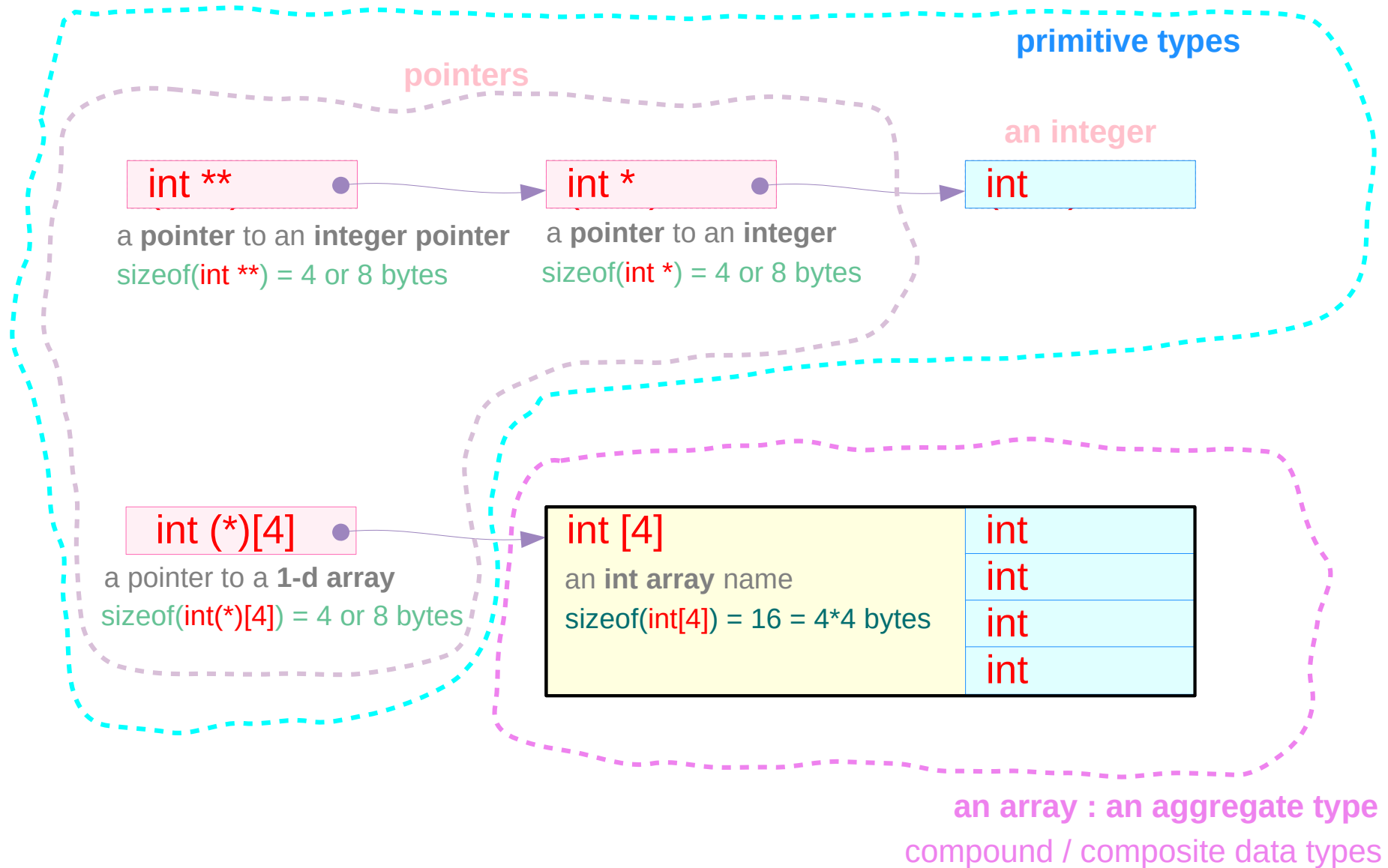
Pointer chains and nested pointers

`int **` \longrightarrow `int *` \longrightarrow `int`

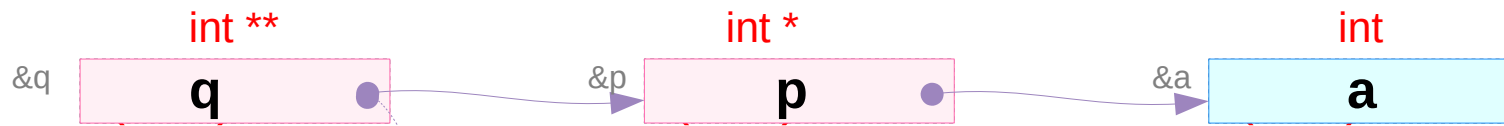
`int (*) [4]`



Types of integer pointers



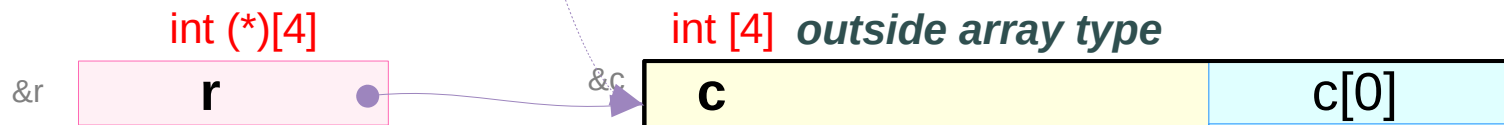
Outside array type `int [4]`



```
int a;  
int *p = &a;  
int *q = &p;
```

`q = &c` *not allowed*
`int **` $\not\rightarrow$ `int [4]` incompatible types

outside array type in rhs
`c :: int [4]`
`&c :: int (*) [4]`

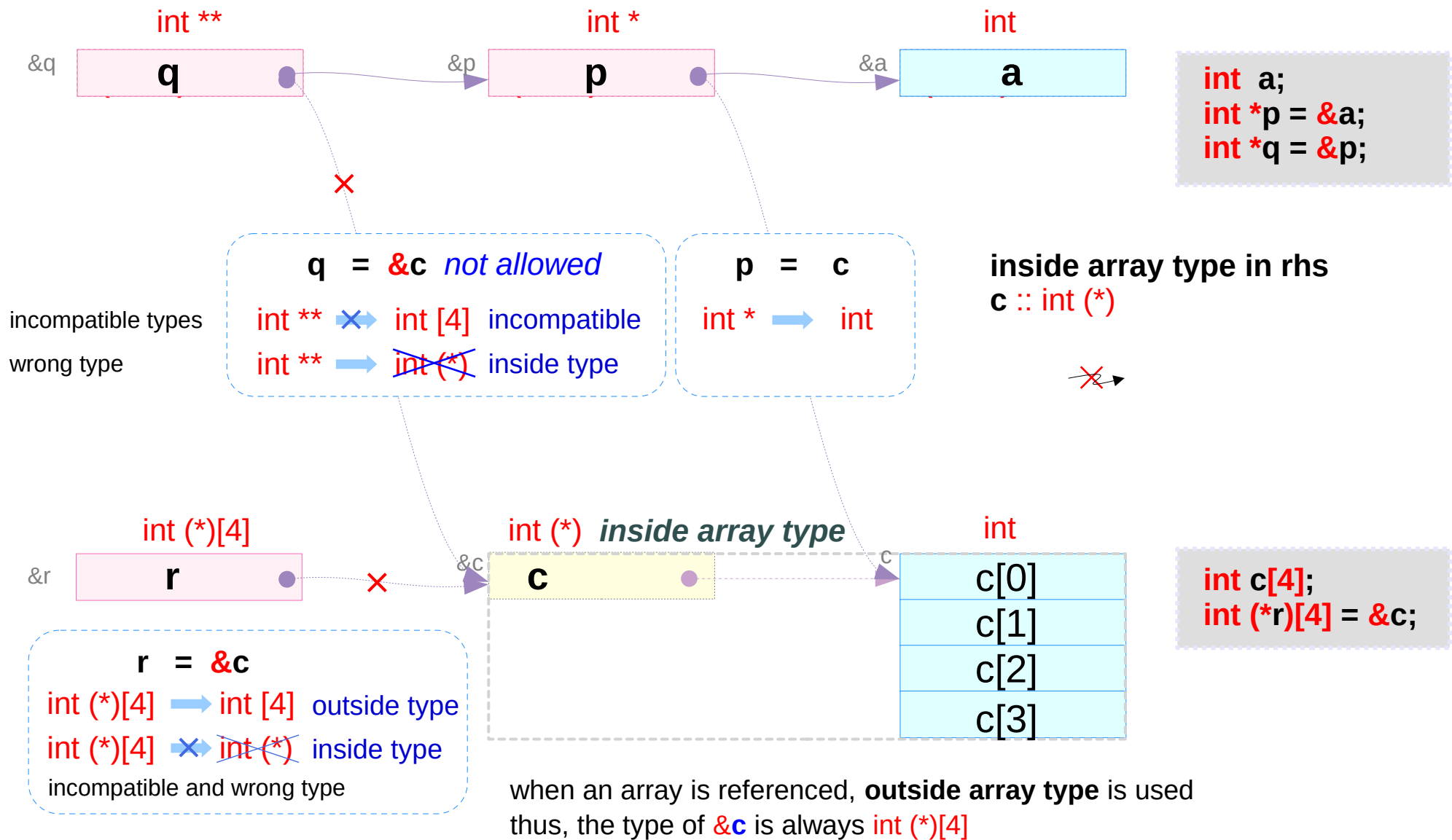


```
int c[4];  
int (*r)[4] = &c;
```

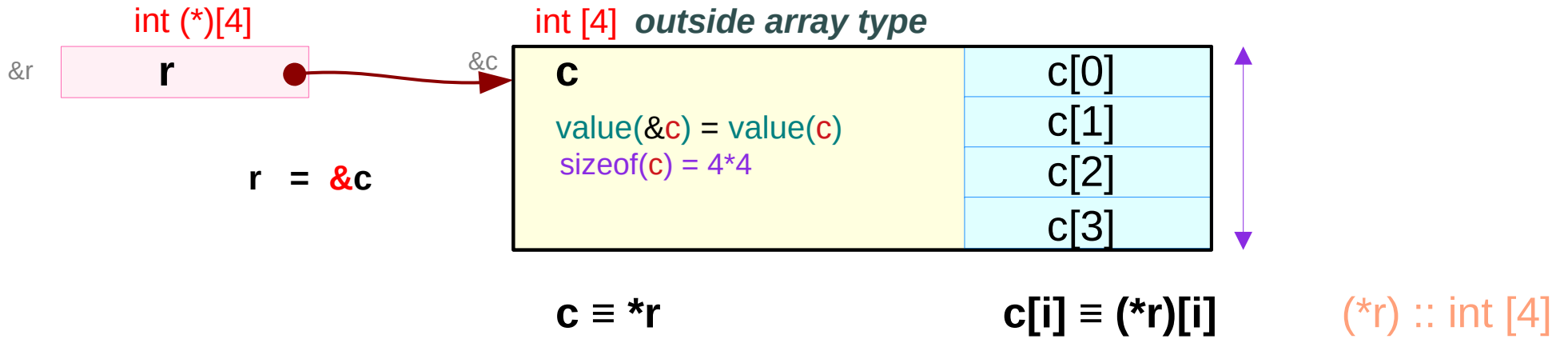
`r = &c`
`int (*)[4]` \rightarrow `int [4]`

| | |
|---------------------------------------|------|
| c | c[0] |
| <code>value(&c) = value(c)</code> | c[1] |
| <code>sizeof(c) = 4*4</code> | c[2] |
| | c[3] |

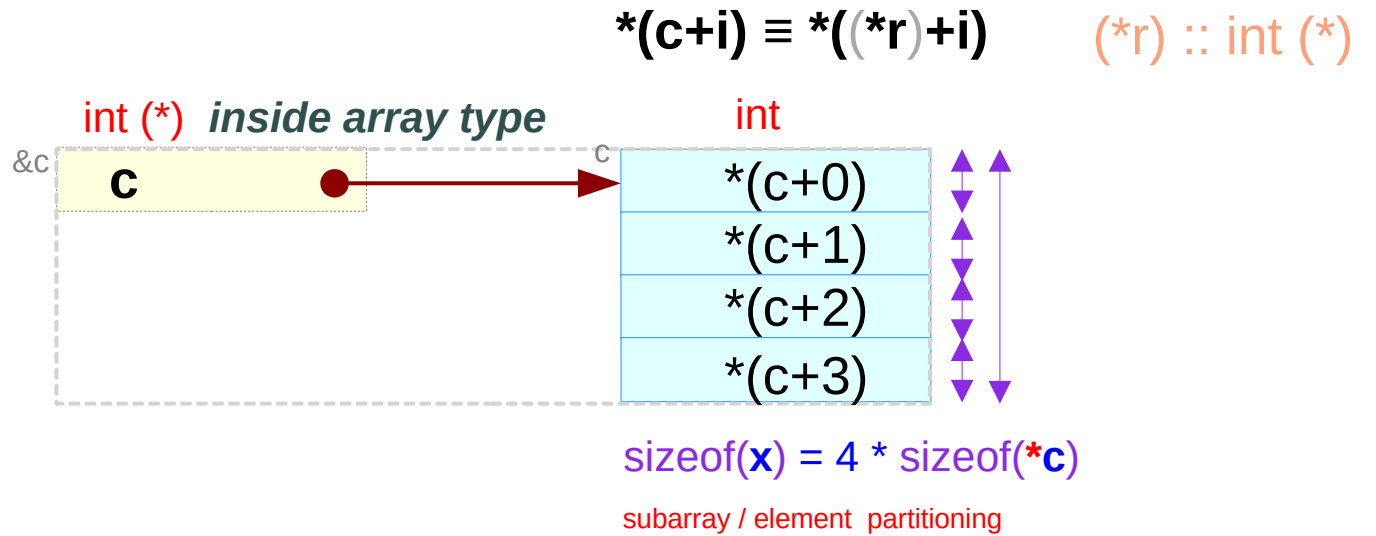
Inside array type `int (*)`



Outside array type `int [4]`



`value(&c) = value(c)`
 address replicating



Explicit and implicit array pointers

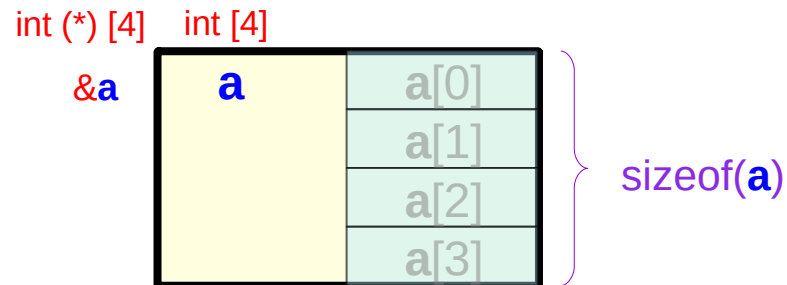
- **Explicit array pointers**
- **Implicit array pointers** in an array

- **Sizes**
- **Types**
- **Values**

Type, size, and value of **a** and **&a** for a 1-d array **a**

```
int a [4] ;
```

*outside of an array a –
a as an abstract data*



abstract data **a**

value(**a**) = value(&a[0])
sizeof(**a**) = 4 * sizeof(int)
type(**a**) = int [4] (outside)
type(**a**) = int (*) (inside)

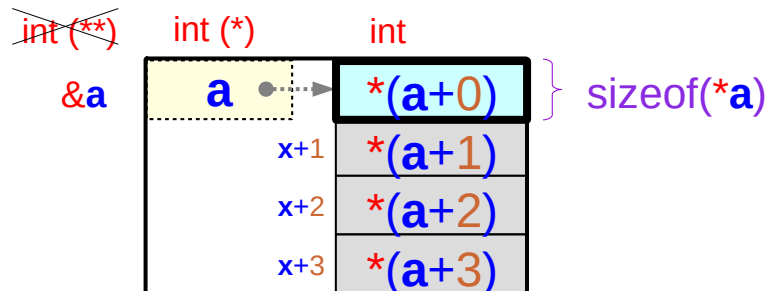
&a : the address of **a**

value(&**a**) = value(**a**)
sizeof(&**a**) = 4 or 8 bytes
type(&**a**) = int (*) [4]

Type, size, and value of `*a` and `a` for a 1-d array `a`

```
int a [4] ;
```

*inside of an array `a` –
`a` as a virtual pointer*



primitive data `*a`

`value(*a) = value(a[0])`

`sizeof(*a) = sizeof(int)`

`type(*a) = int`

`a` : the address of `*a`

`value(a) = value(&a[0])`

`sizeof(a) = 4 * sizeof(int)`

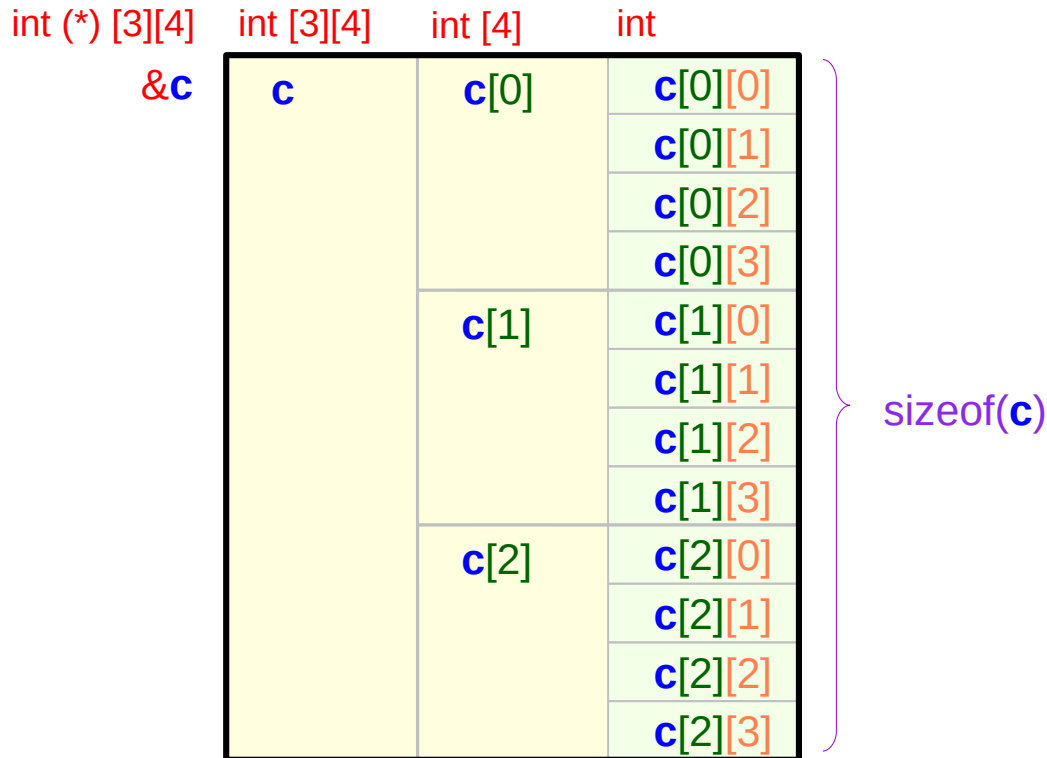
`type(a) = int [4]` (outside)

`type(a) = int (*)` (inside)

Type, size, and value of **c** and **&c** for a 2-d array **c**

```
int c [3][4] ;
```

*outside of an array **c** –
c as an abstract data*



*outside of an array **c***

c : abstract data

$\text{value}(\mathbf{c}) = \text{value}(\&\mathbf{c}[0])$
 $\text{sizeof}(\mathbf{c}) = 3 * 4 * \text{sizeof}(\text{int})$
 $\text{type}(\mathbf{c}) = \text{int } [3][4]$ (outside)
 $\text{type}(\mathbf{c}) = \text{int } (*)[4]$ (inside)

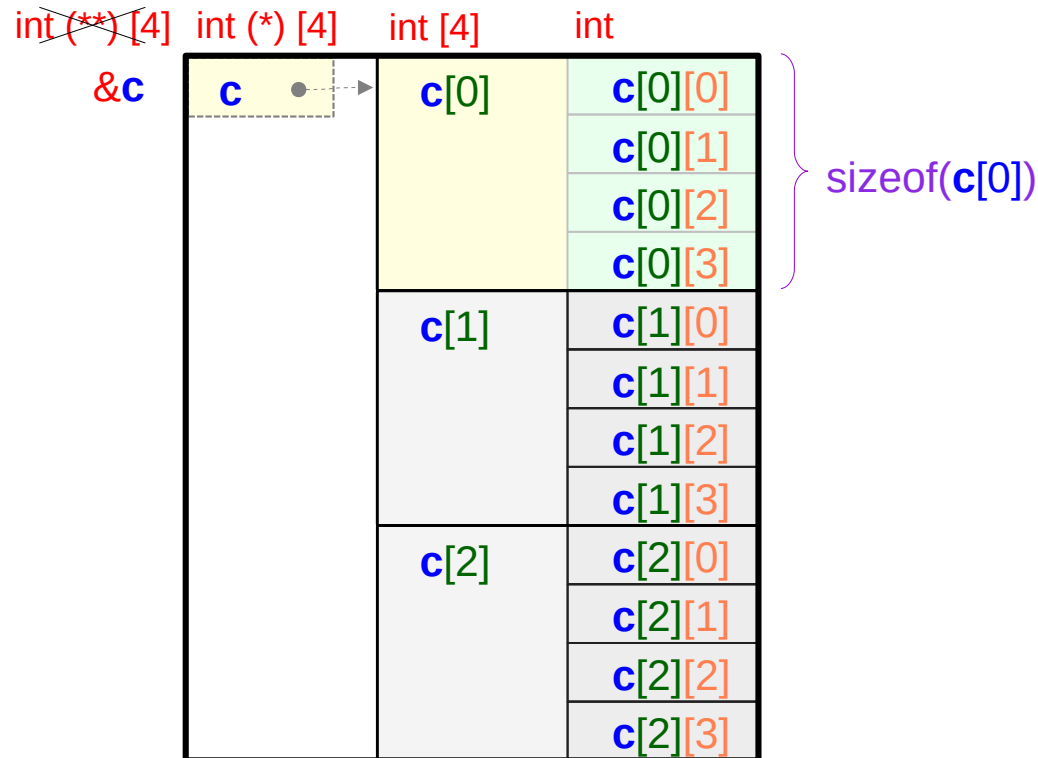
&c : the address of **c**

$\text{value}(\&\mathbf{c}) = \text{value}(\mathbf{c})$
 $\text{sizeof}(\&\mathbf{c}) = 4 \text{ or } 8 \text{ bytes}$
 $\text{type}(\&\mathbf{c}) = \text{int } (*) [3][4]$

Type, size, and value of `c[0]` and `c` for a 2-d array `c`

```
int c [3][4] ;
```

*inside of an array `c` –
`c` as a virtual pointer*



`c[0]` : abstract data `*c`

`value(c[0]) = value(&c[0][0])`
`sizeof(c[0]) = 4 * sizeof(int)`
`type(c[0]) = int [4]` (outside)
`type(c[0]) = int (*)` (inside)

`c` : the address of `c[0]`

`value(c) = value(&c[0])`
`sizeof(c) = 3 * 4 * sizeof(int)`
`type(c) = int [3][4]` (outside)
`type(c) = int (*)[4]` (inside)

outside of an array `c`

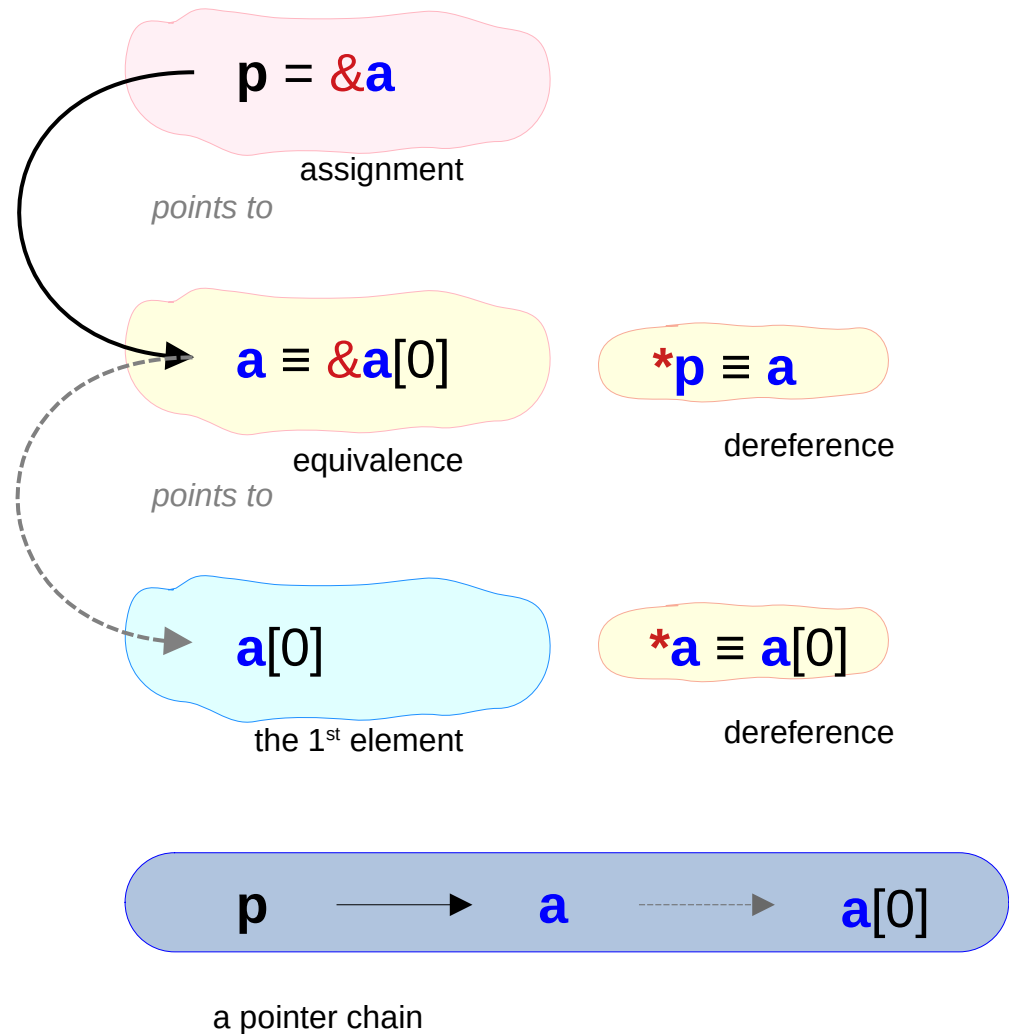
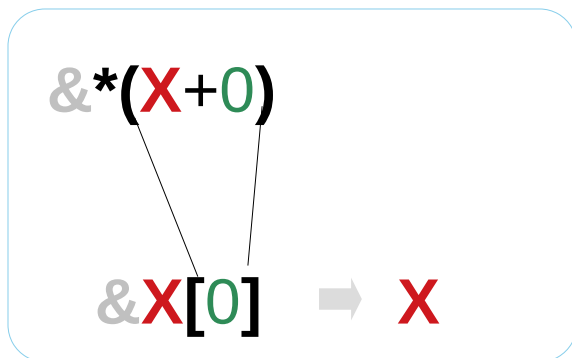
1-d array pointer **p** – (1) pointer chain

1-d array pointer

```
int (*p)[4];
```

1-d array

```
int a[4];
```



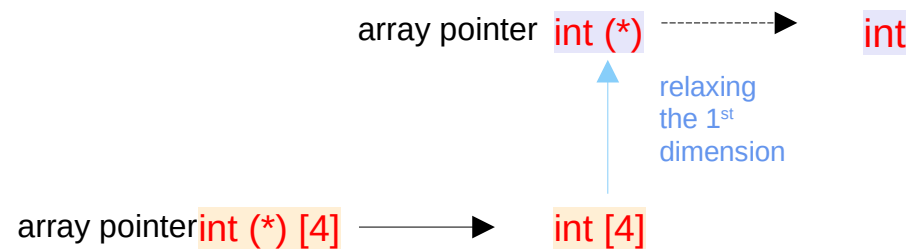
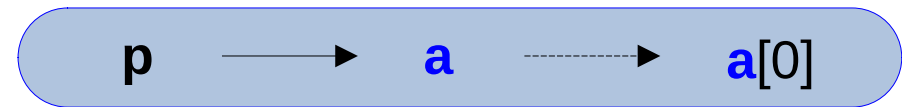
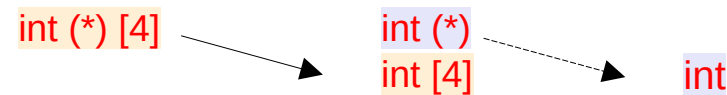
1-d array pointer **p** – (2) types in a pointer chain

1-d array pointer

```
int (*p) [4];
```

1-d array

```
int a [4];
```



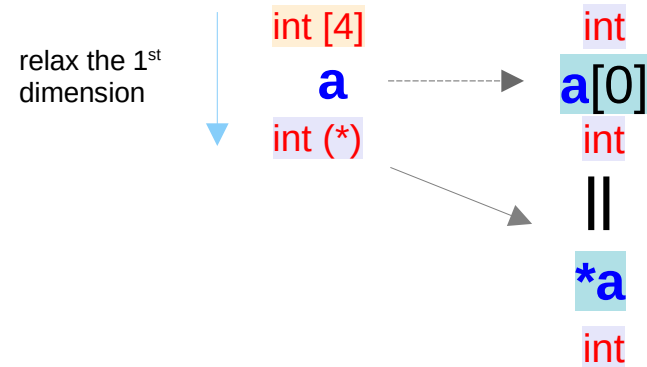
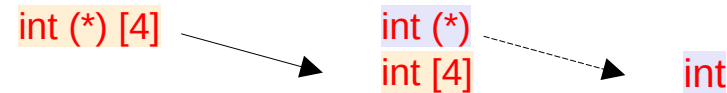
1-d array pointer **p** – (3) relaxing the 1st dimension

1-d array pointer

```
int (*p) [4];
```

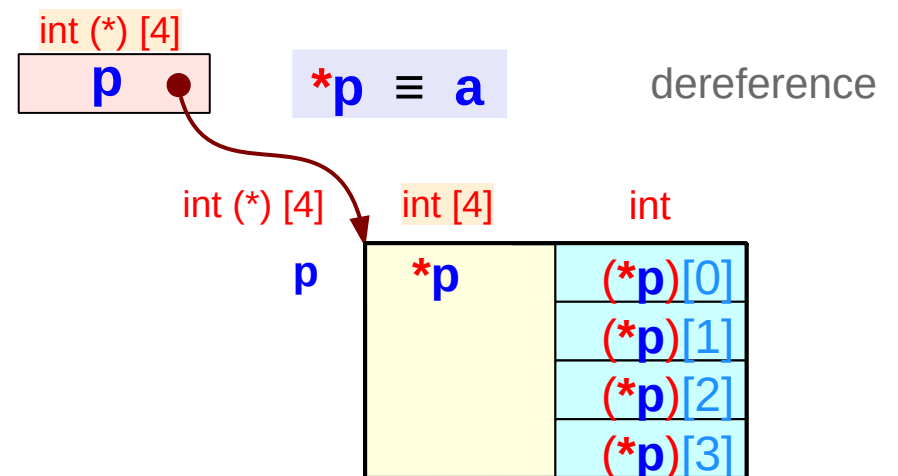
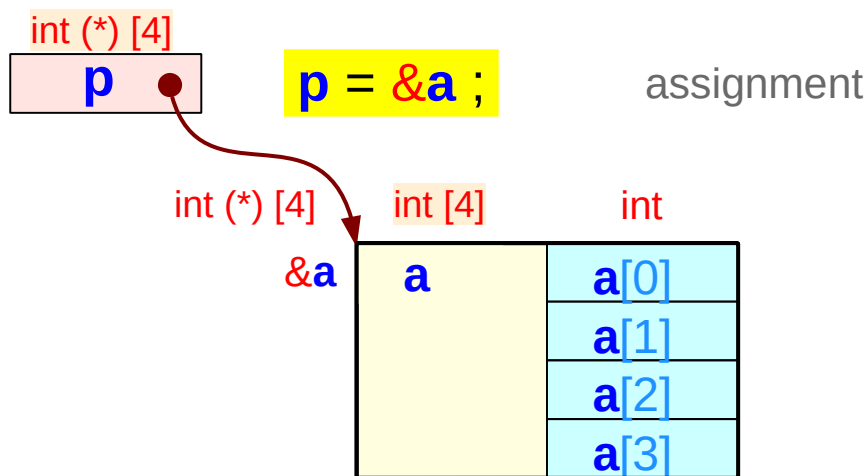
1-d array

```
int a [4];
```



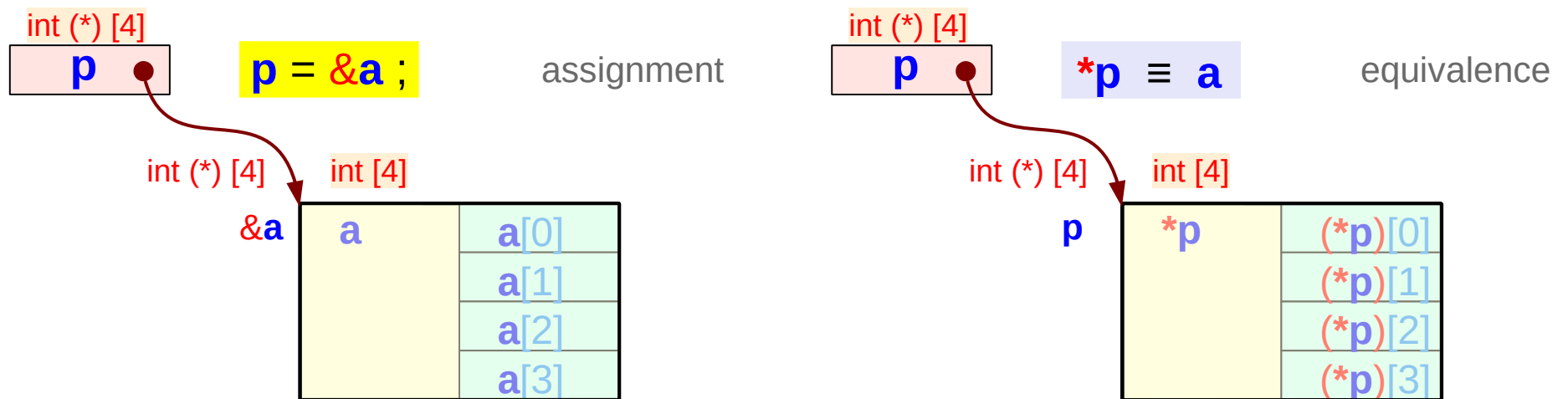
1-d array pointer **p** – (4) assignment and dereference

| | | | | |
|----------------------------|-------------------------|---------------------|----------------------------|------------------------|
| <code>int a [4];</code> | assignment | dereference | equivalence | dereference |
| <code>int (*p) [4];</code> | <code>p = &a</code> | <code>*p ≡ a</code> | <code>a ≡ &a[0]</code> | <code>*a ≡ a[0]</code> |



1-d array pointer **p** – 1-d array **a**

outside of an array **a** (**a** as an abstract data)



`sizeof(&a)` = 4 or 8 bytes size of a pointer

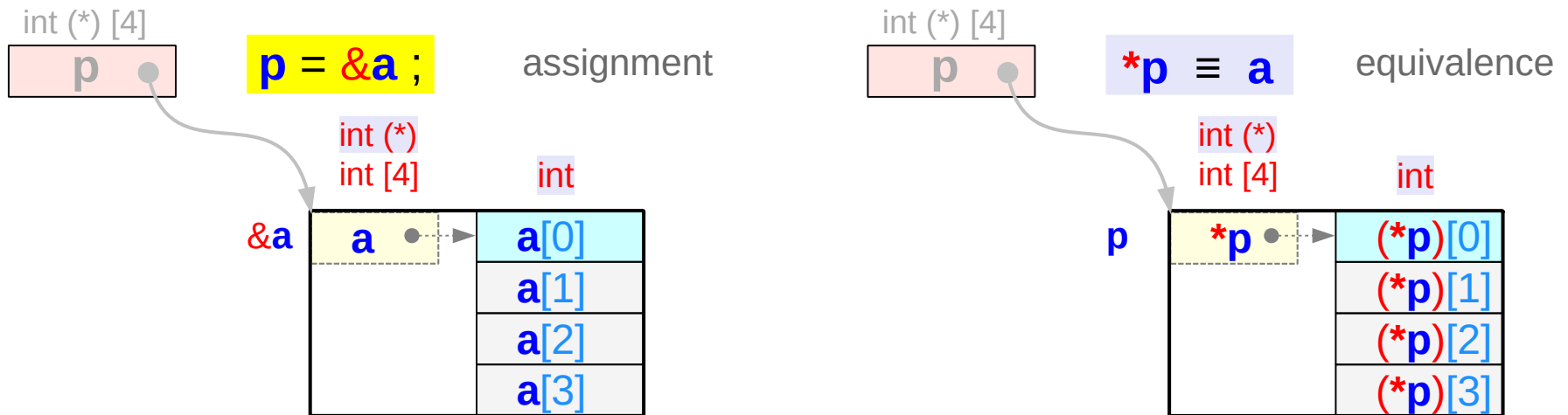
`sizeof(a)` = 4 * `sizeof(int)` size of a 1-d array

`value(&a)` address value of a 1-d array **a**

= `value(a)` data value of a 1-d array **a**

0-d array pointer **a** – 0-d array **a[0]**

inside of an array **a** (**a** as a virtual pointer)



`sizeof(a)` = `4 * sizeof(int)` size of a 1-d array

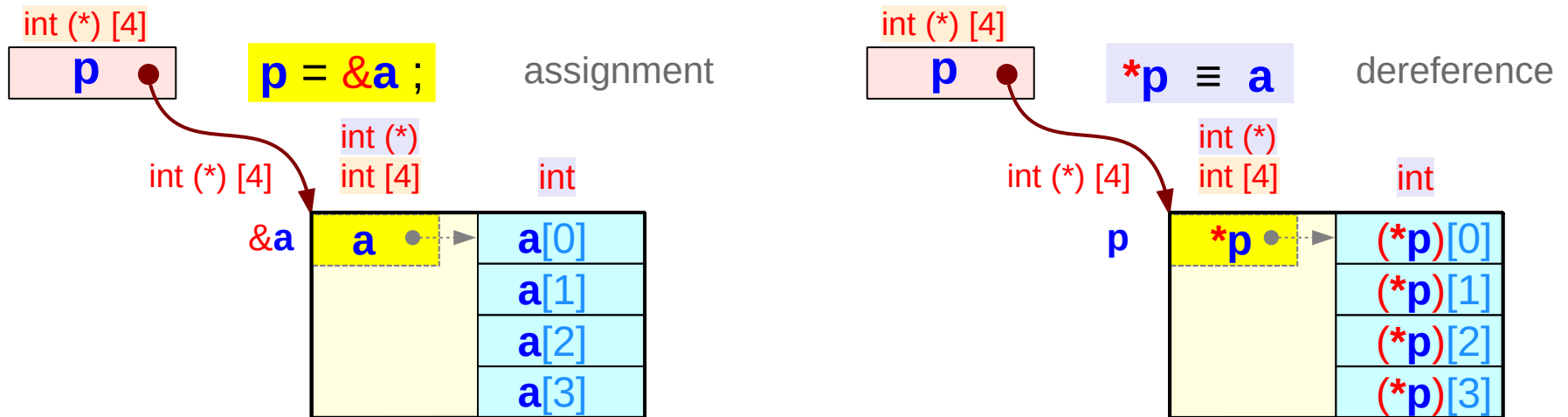
`sizeof(a[0])` = 4 bytes size of an integer

`value(a)` = `value(&a[0])` address value of an integer **a[0]**

`value(a[0])` data value of an integer **a[0]**

Overlaid representation

outside of an array a (a as an abstract data)
inside of an array a (a as a virtual pointer)



not a real pointer `a` `value(&a) = value(a)` = `value(&a[0])`

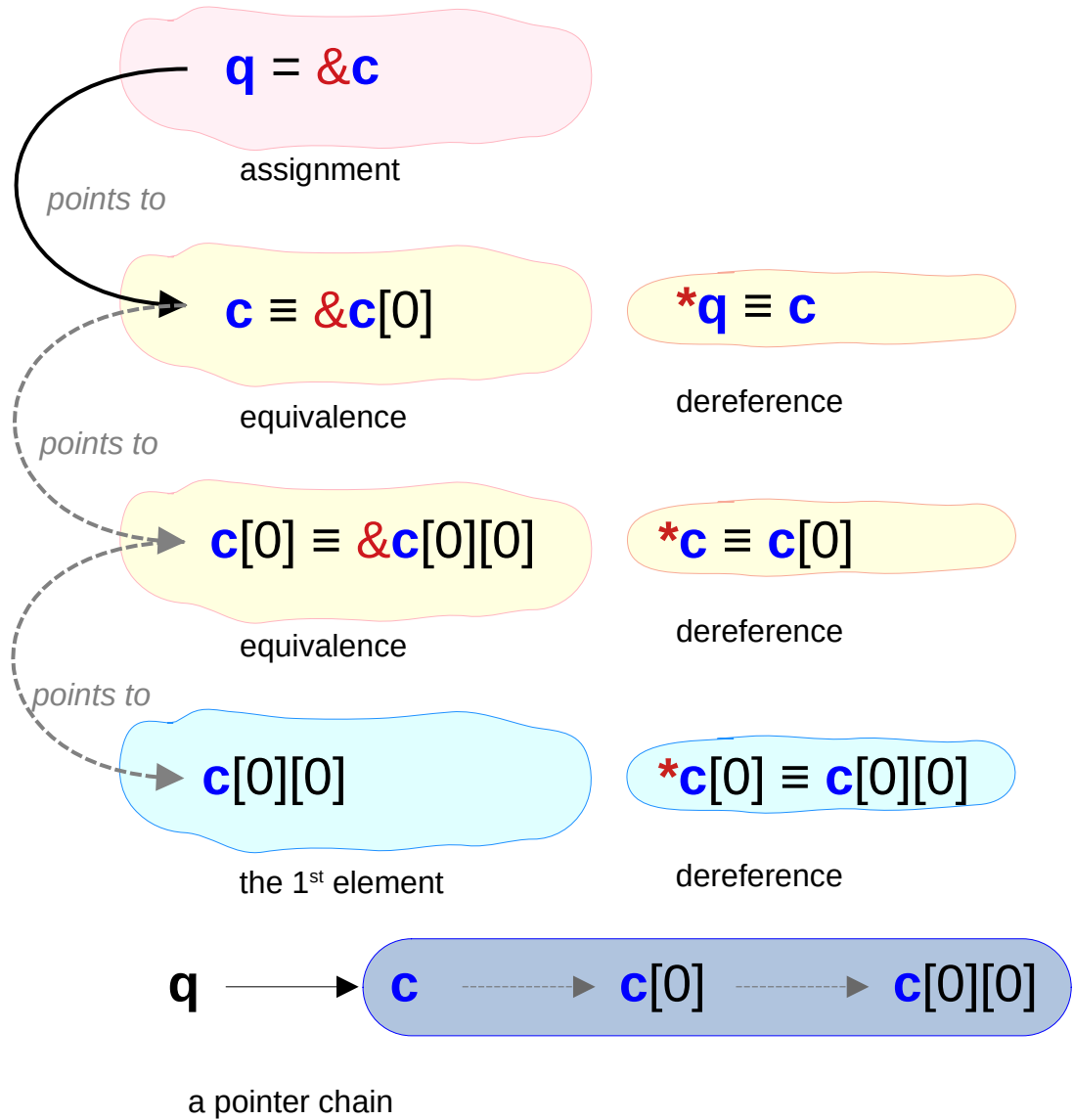
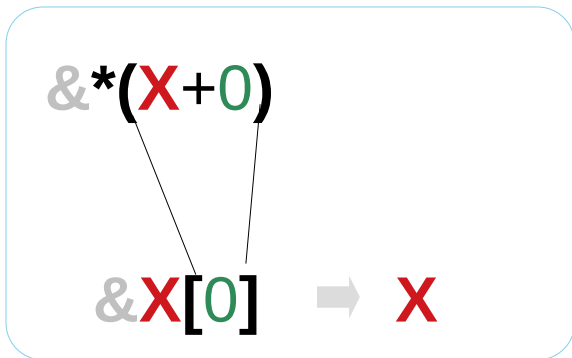
2-d array pointer q – (1) pointer chains

2-d array pointer

```
int (*q)[3][4];
```

2-d array

```
int c[3][4];
```



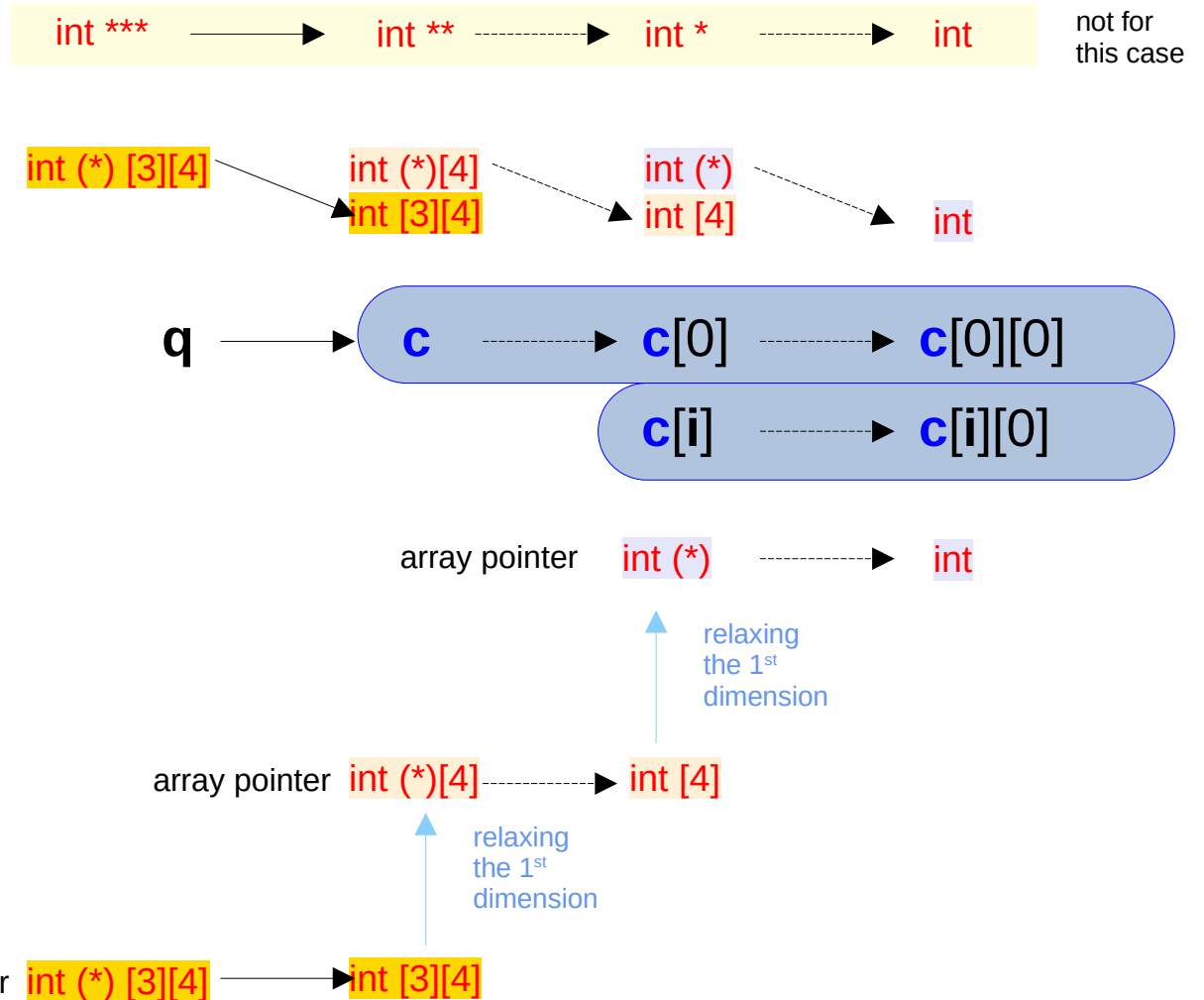
2-d array pointer q – (2) types in a pointer chain

2-d array pointer

```
int (*q) [3][4];
```

2-d array

```
int c [3][4];
```



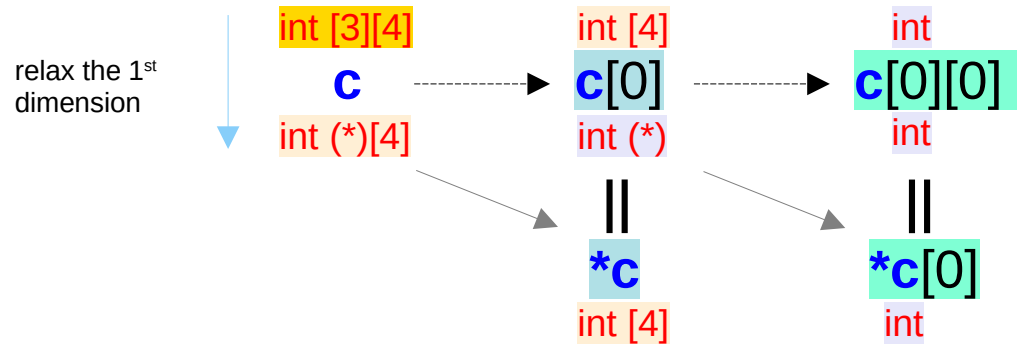
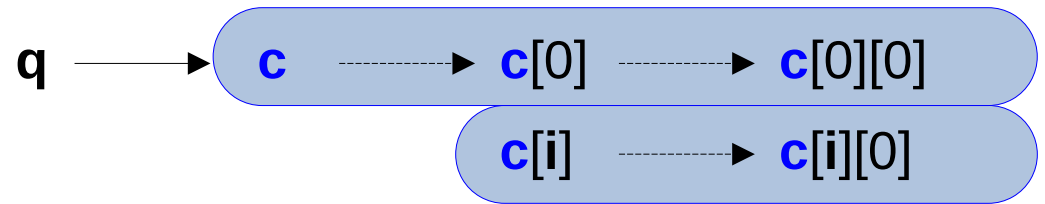
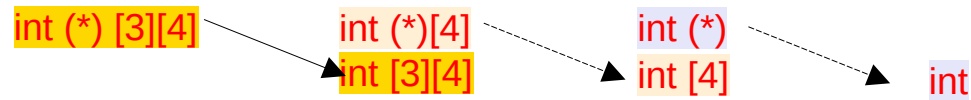
2-d array pointer q – (3) relaxing the 1st dimension

2-d array pointer

```
int (*q) [3][4];
```

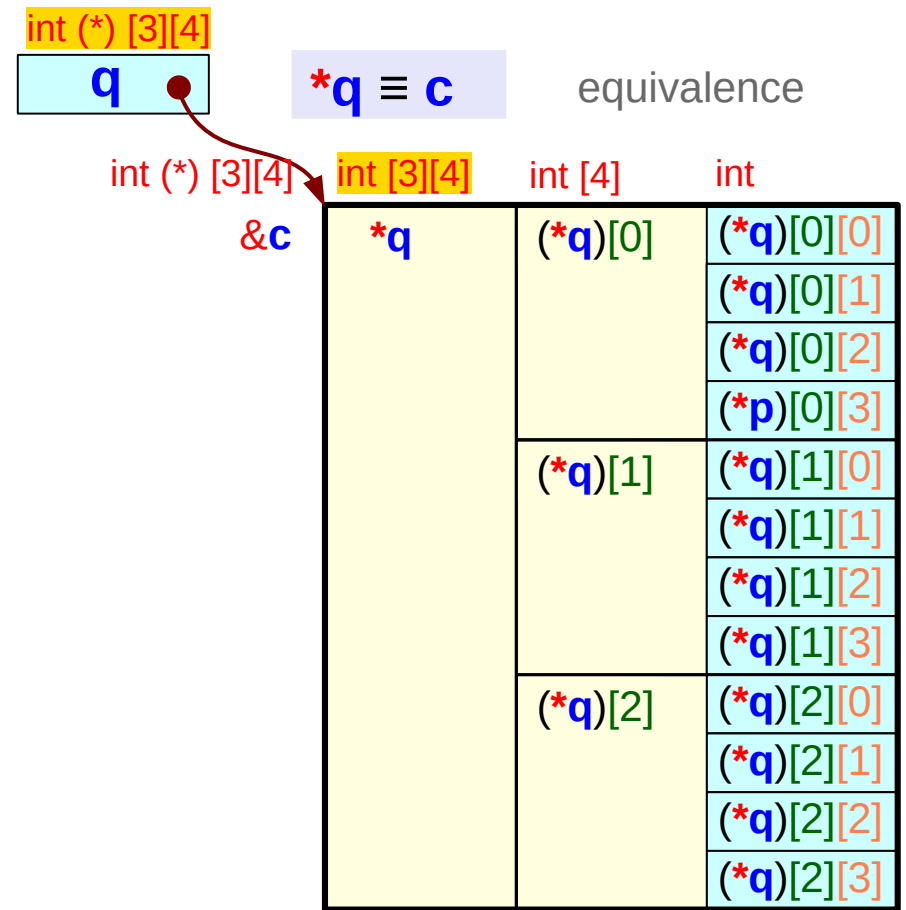
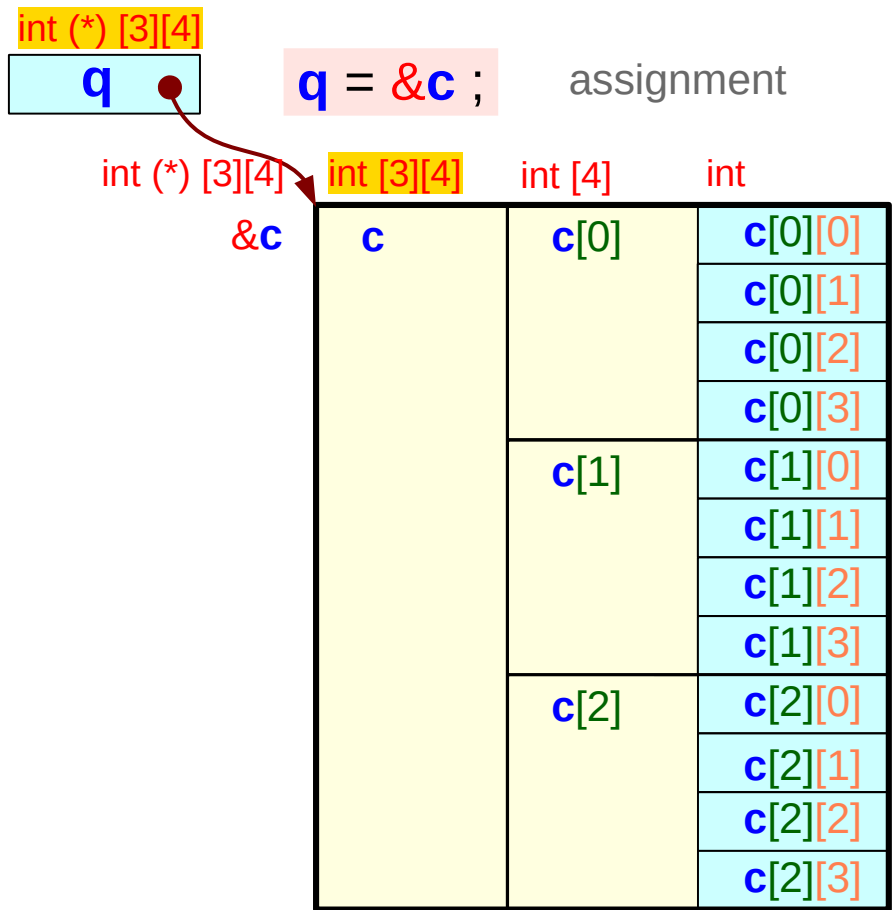
2-d array

```
int c [3][4];
```

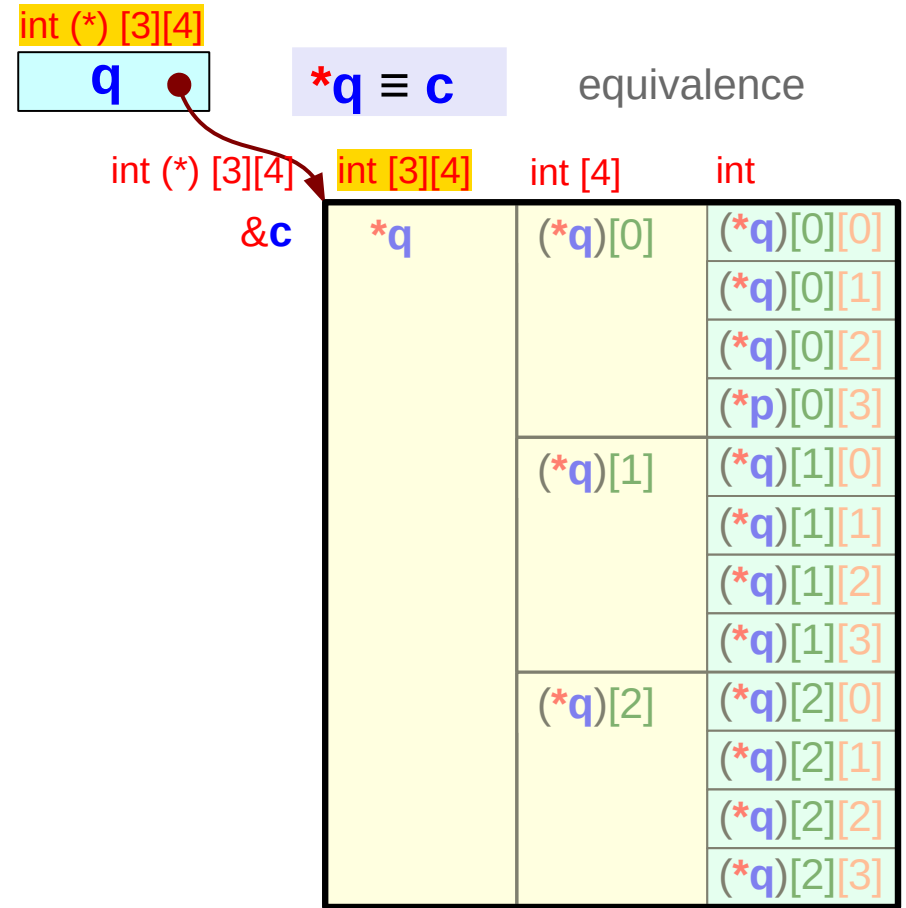
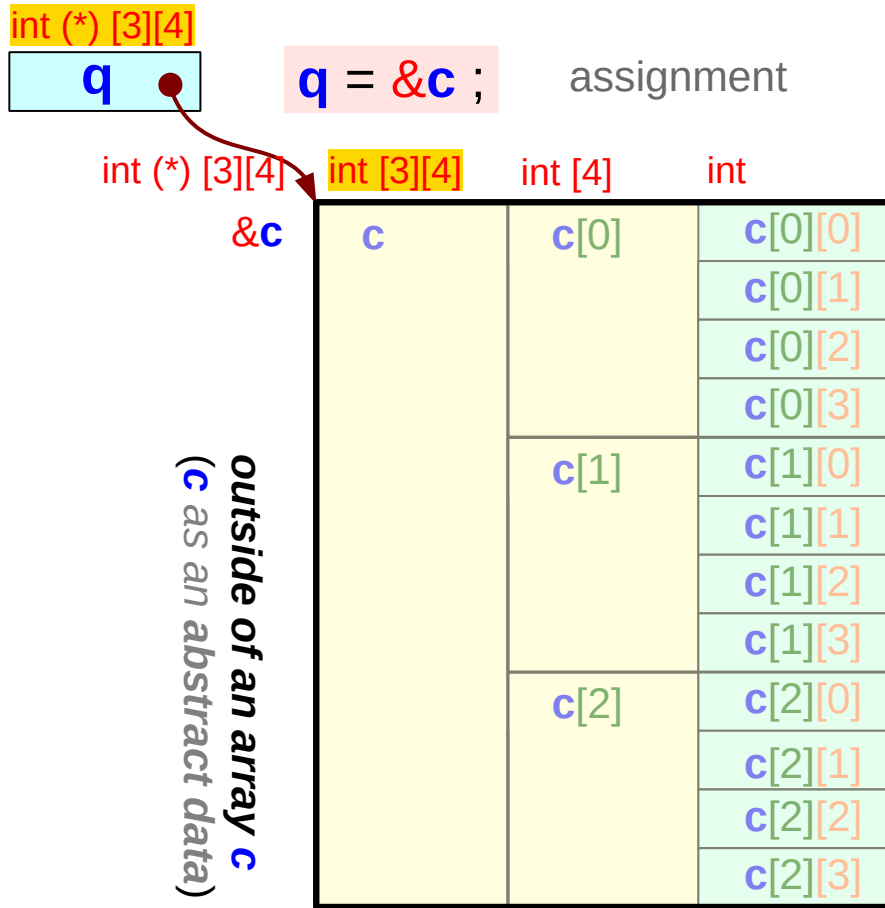


2-d array pointer q – (4) assignment and dereference

| | | | | |
|-------------------------------|-------------------------|---------------------|----------------------------|----------------------------------|
| <code>int c [3][4];</code> | assignment | dereference | equivalence | equivalence |
| <code>int (*q) [3][4];</code> | <code>q = &c</code> | <code>*q ≡ c</code> | <code>c ≡ &c[0]</code> | <code>c[0] ≡ &c[0][0]</code> |



2-d array pointer q – 2-d array c



`sizeof(&c)` = 4 or 8 bytes

size of a pointer

`value(&c)` =

address value of a 2-d array `c`

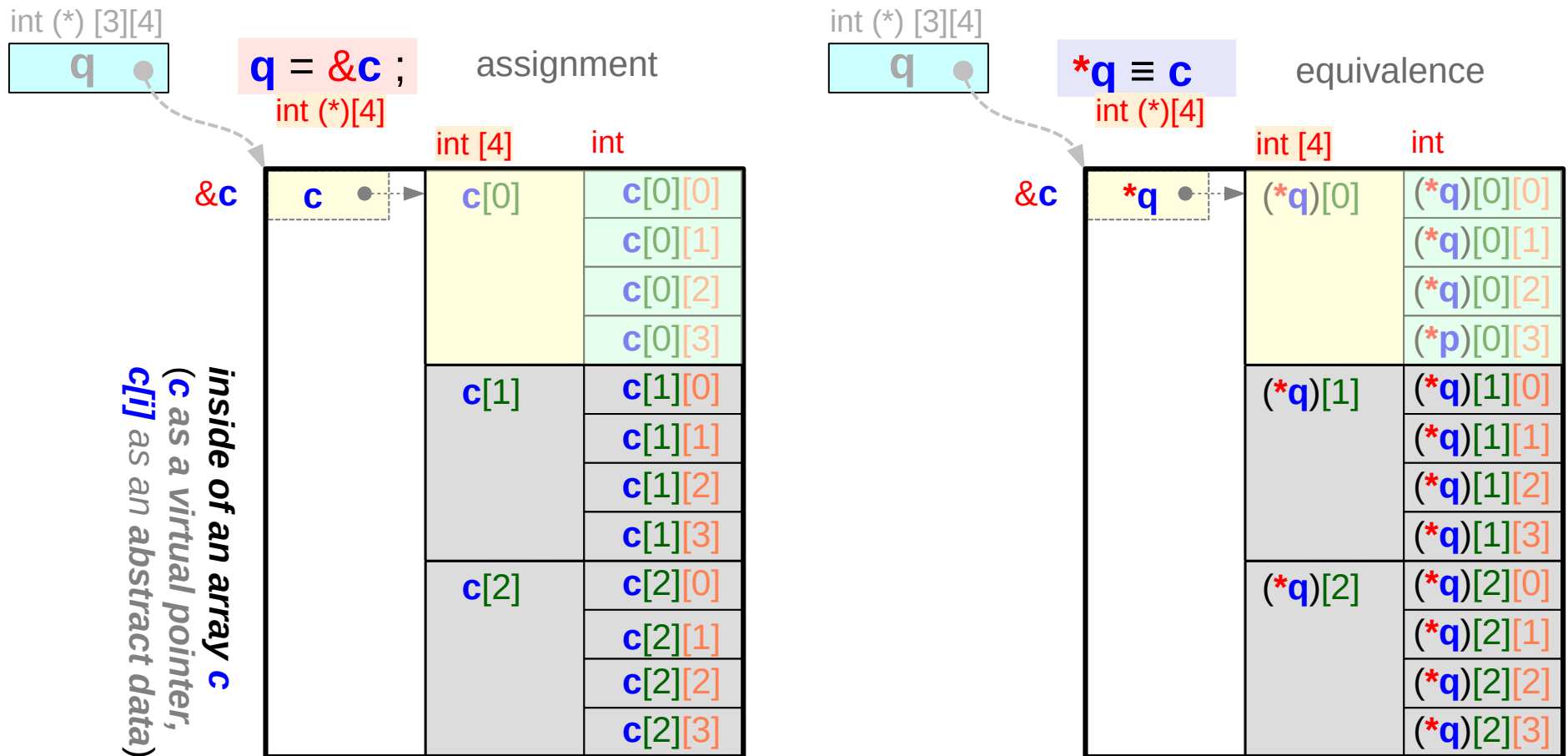
`sizeof(c)` = 3 * 4 * `sizeof(int)`

size of a 2-d array

`value(c)`

data value of a 2-d array `c`

1-d array pointer **c** – 1-d array **c[0]**



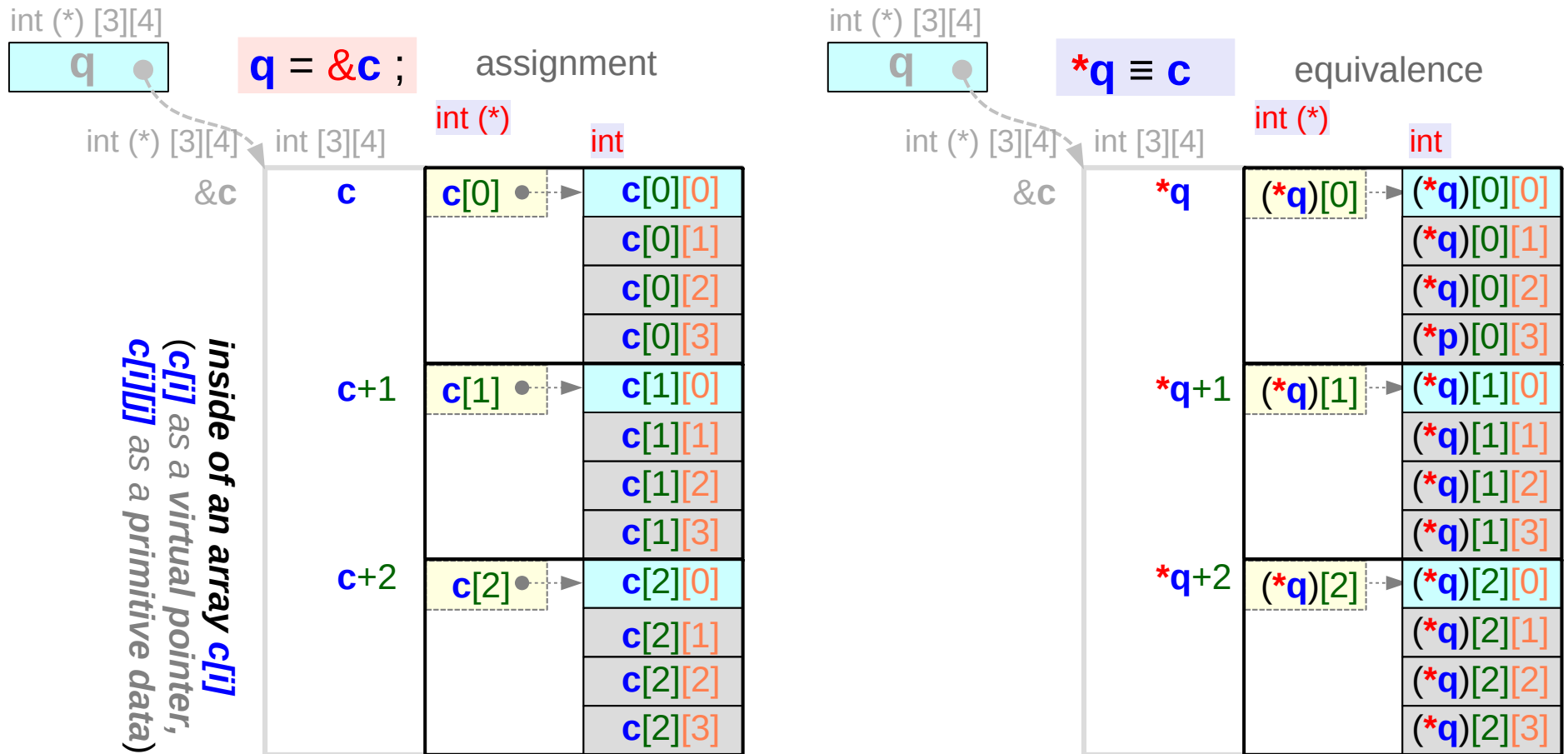
`sizeof(c) = 3 * 4 * sizeof(int)` size of a **2-d** array

`sizeof(c[0]) = 4 * sizeof(int)` size of a **1-d** array

`value(c) =` address value of a **1-d** array **c[0]**

`value(c[0])` data value of a **1-d** array **c[0]**

0-d array pointer $c[i]$ – 0-d array $c[i][0]$



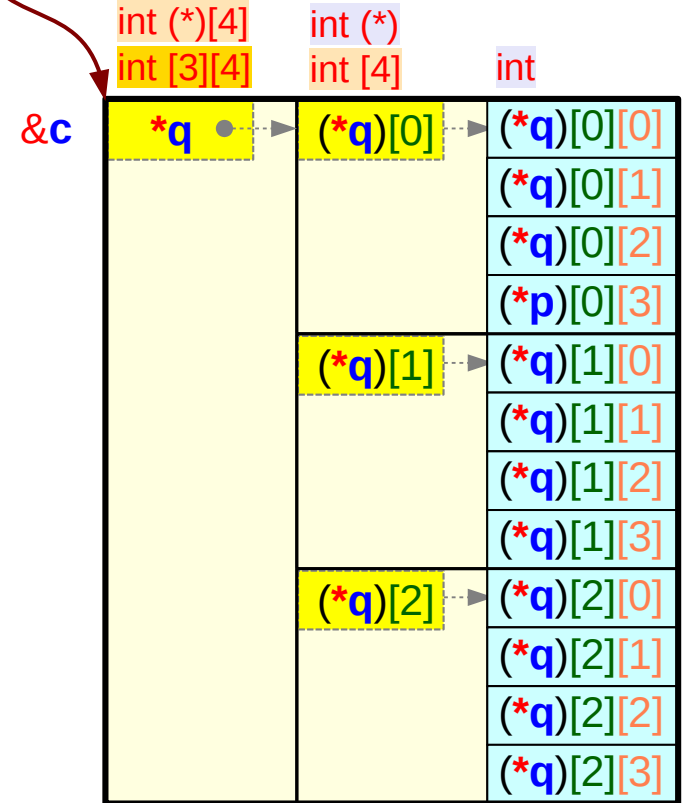
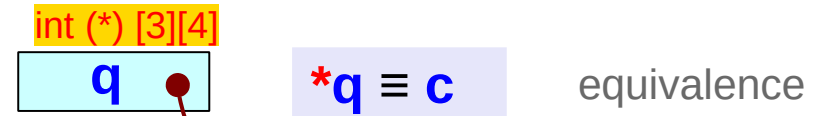
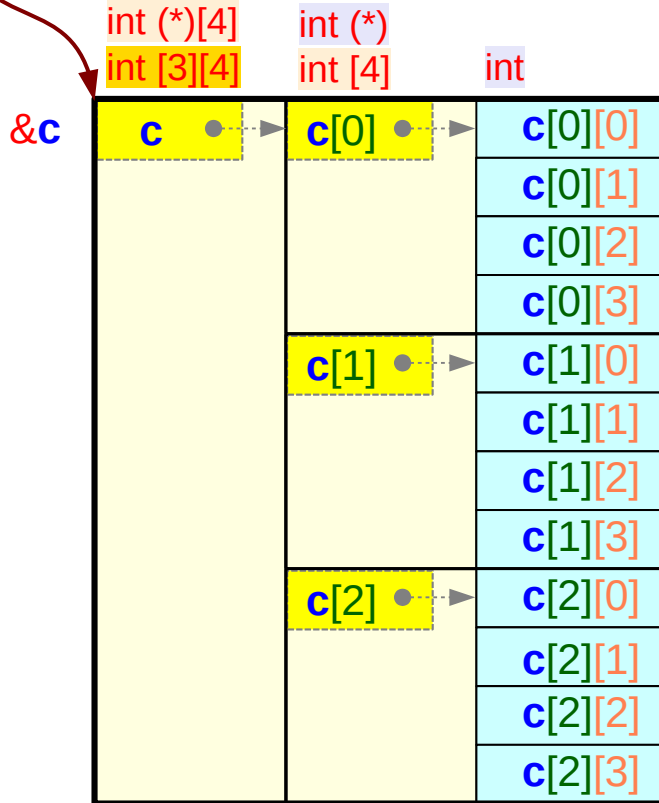
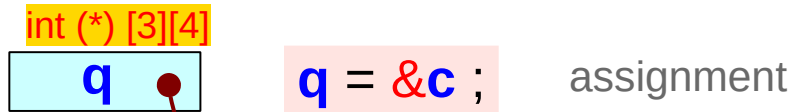
$\text{sizeof}(c[i]) = 4 * \text{sizeof}(\text{int})$ size of a 1-d array

$\text{value}(c[i]) = \text{value}(\&c[i][0])$ address value of an integer $c[i][0]$

$\text{Sizeof}(c[i][0]) = \text{sizeof}(\text{int})$ size of an integer

$\text{value}(c[i][0])$ data value of an integer $c[i][0]$

Overlaid representation



not a real pointer `c`
 not a real pointer `c[i]`

$$\text{value}(\&c) = \text{value}(c)$$

$$= \text{value}(\&c[0]) = \text{value}(c[0])$$

$$\text{value}(\&c[i]) = \text{value}(c[i])$$

$$= \text{value}(\&c[0][0])$$

$$= \text{value}(\&c[i][0])$$

int [4] a **1-d** 4-element integer array

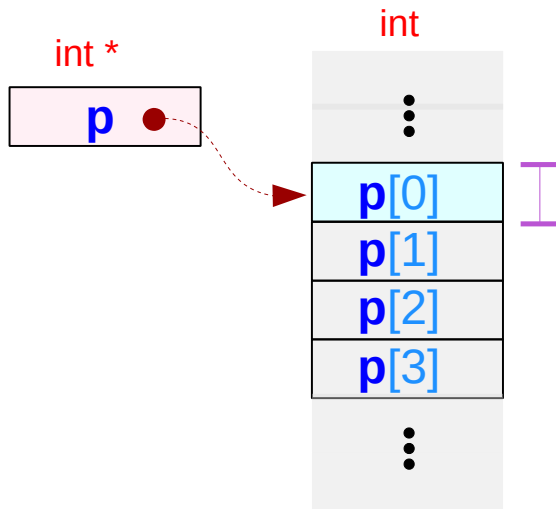
int [] a **1-d** unsized integer array

int (*) a **0-d** integer array pointer (**int ***)

int (*) [4] a **1-d** integer array pointer

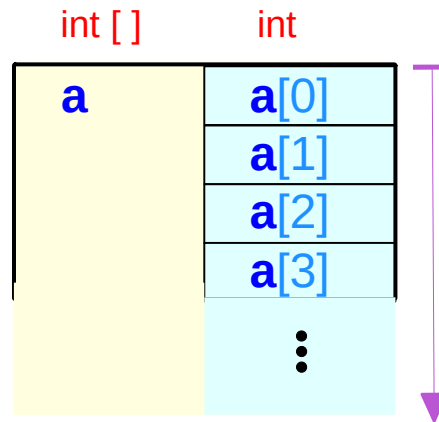
Sizes of `int [4]`, `int []`, `int *` types

`sizeof(int *) = 4 or 8`



an incomplete type

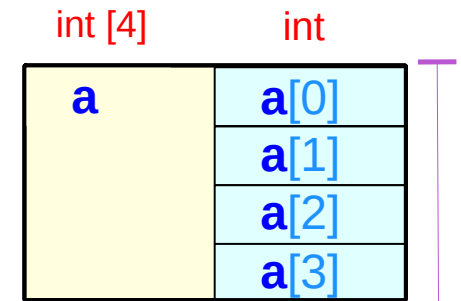
~~undefined size~~
~~`sizeof(int [])`~~



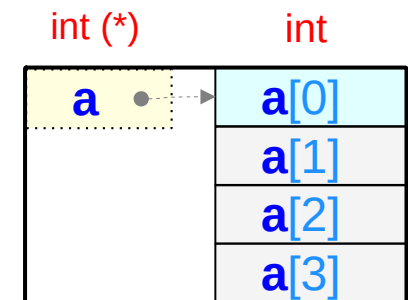
used to pass arrays to a function

`sizeof(int [4]) = sizeof(int) * 4 = 16`

outside array type



inside array type



`&a = value(a)`

`type(int [4]) ⊂ type(int []) ≈ type(int (*)) ≡ int *`

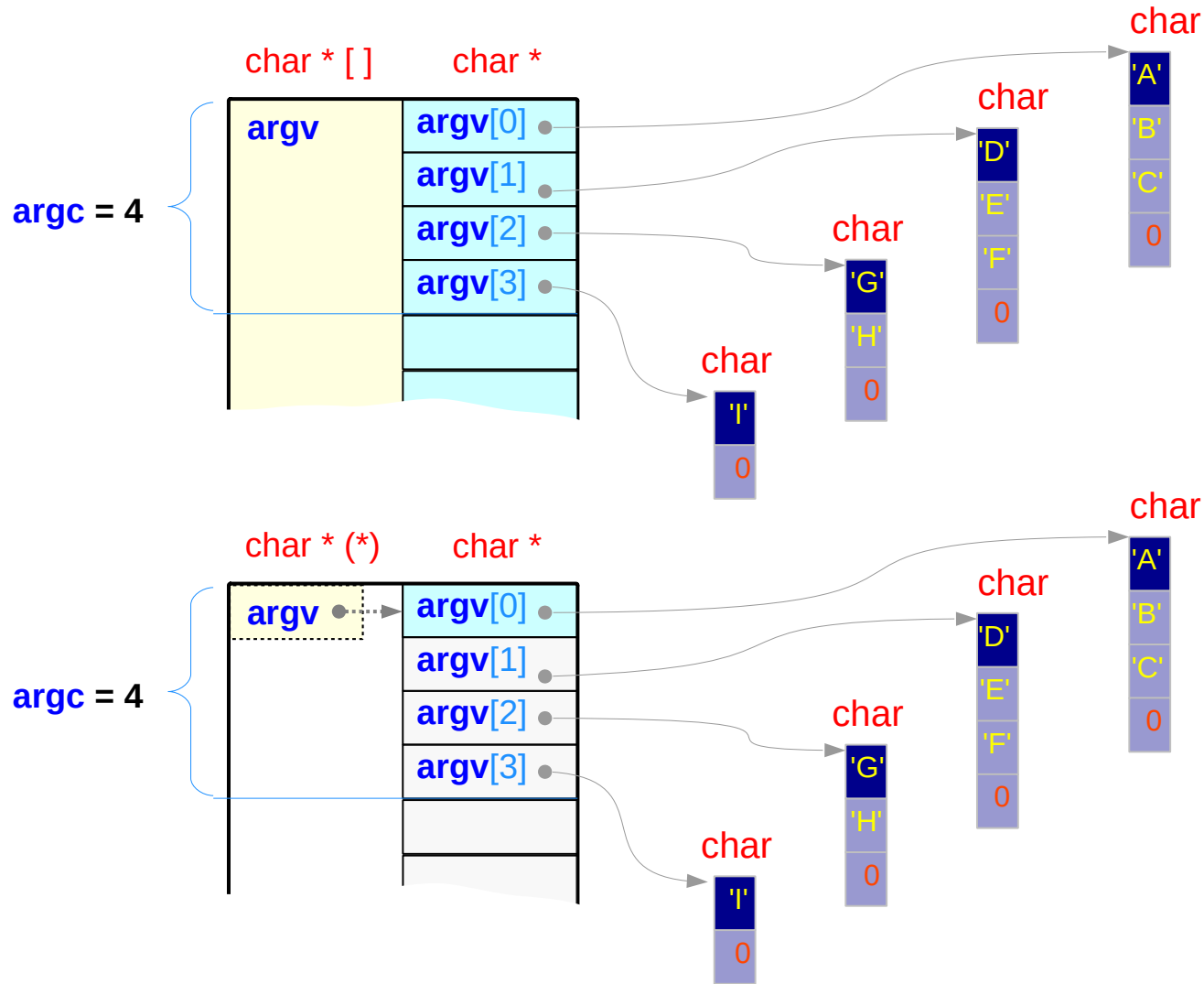
abstract data

relaxed data

0-d array pointer

int pointer

(int argc, char * argv[]) example

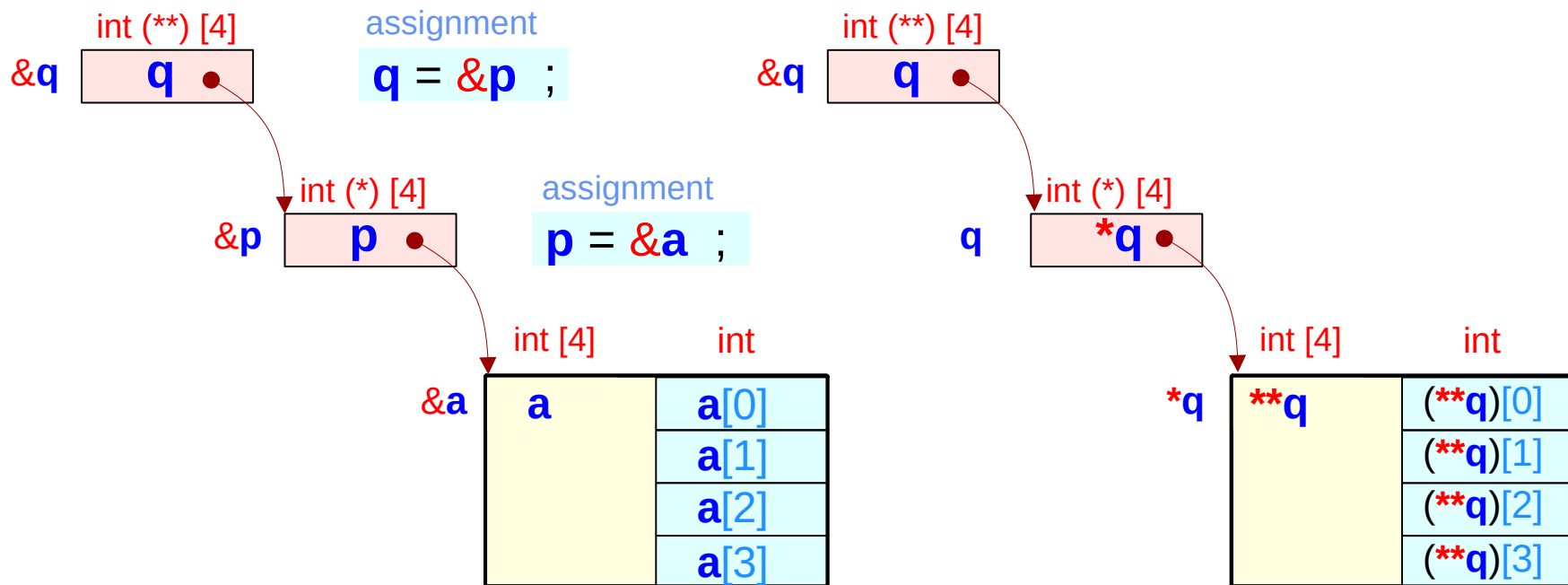


| MSB | | | LSB |
|-----|-----|-----|-----|
| 0 | 'C' | 'B' | 'A' |
| 0 | 'F' | 'E' | 'D' |
| 'I' | 0 | 'H' | 'G' |
| | | | 0 |

`char * []` relaxed 1st dimension
 ↓
`char * (*)` array pointer
`char * *`

Double pointer to a 1-d array – a variable view (p, q)

```
int a [4] ;      int (*p) [4] = &a ;      int (**q) [4] = &p ;
```

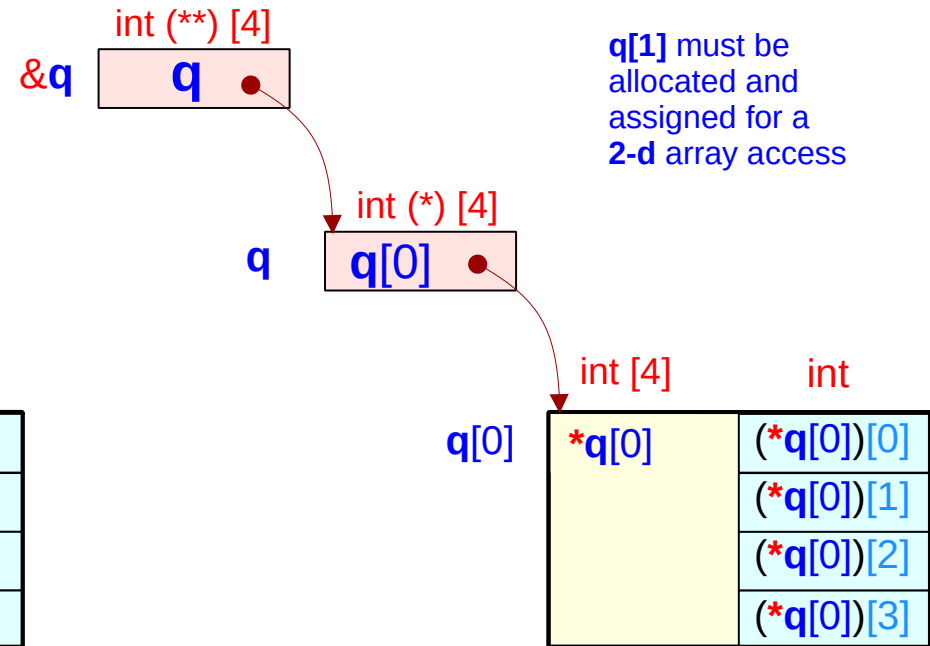
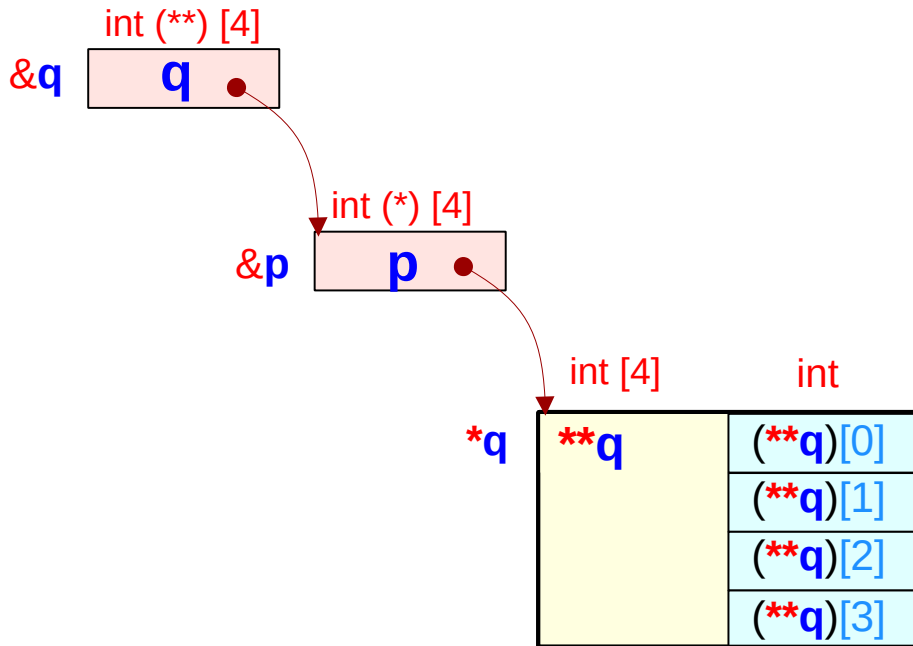


Double array pointer

```
int a[4];
```

1-d array a

```
int (*p)[4] = &a;  
int (**q)[4] = &p;
```

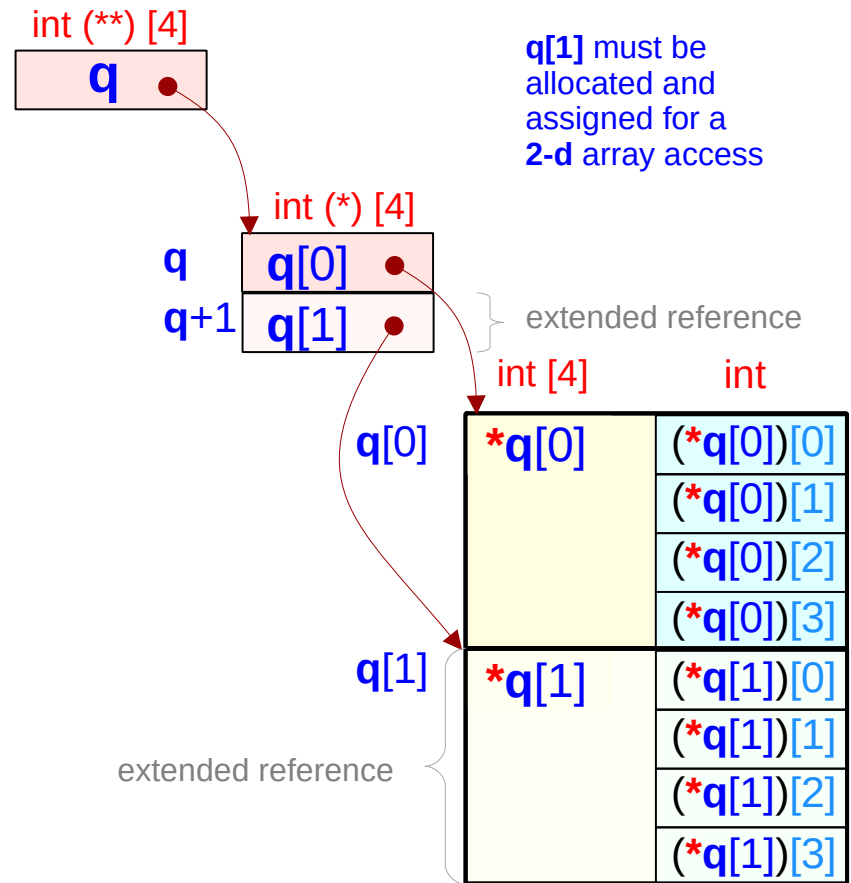
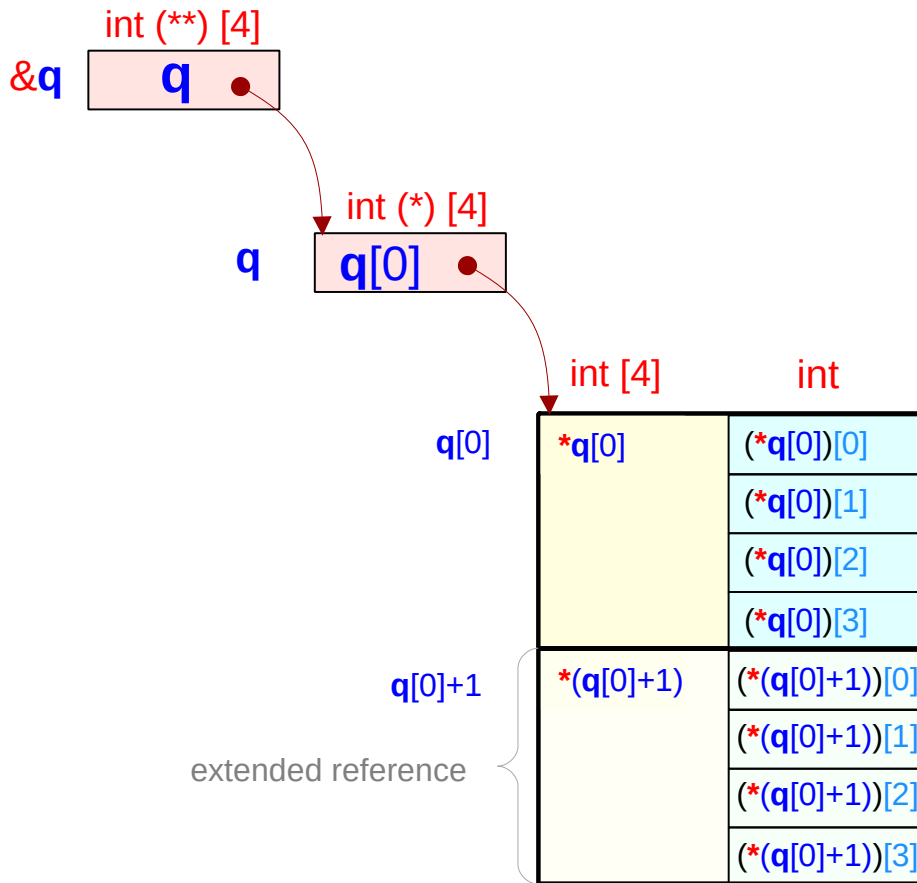


`q[1]` must be allocated and assigned for a 2-d array access

2-d array access with a double array pointer

```
int (*p) [4] = &a ;
int (**q) [4] = &p ;
```

```
int (*p) [4] = &a ;
int (**q) [4] = &p ;
```

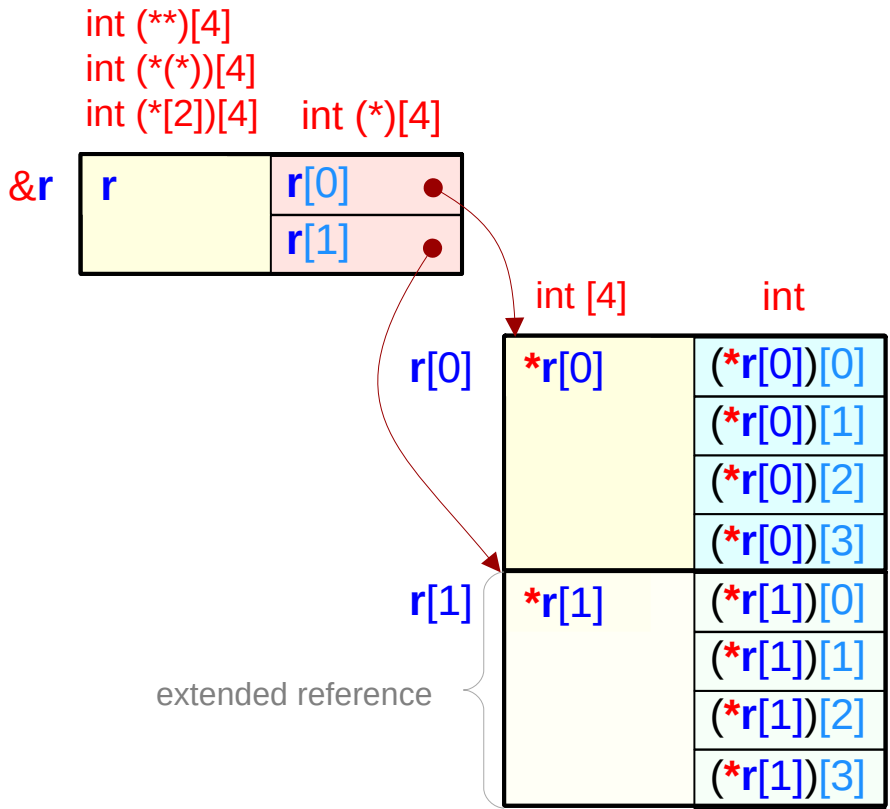


Array pointer and subarray types

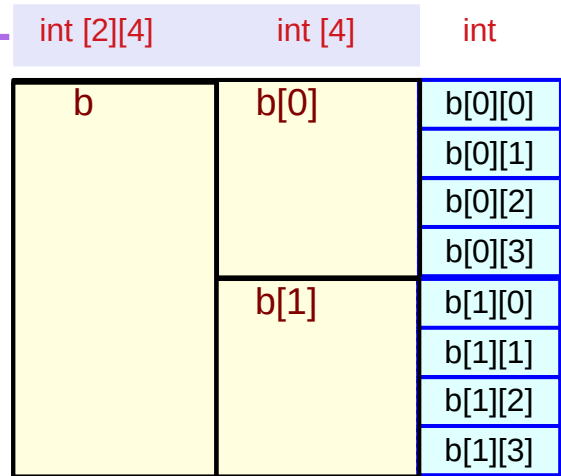
```
int (*r[2])[4] = {&a, &a+1} ;
```

```
int b[2][4];
```

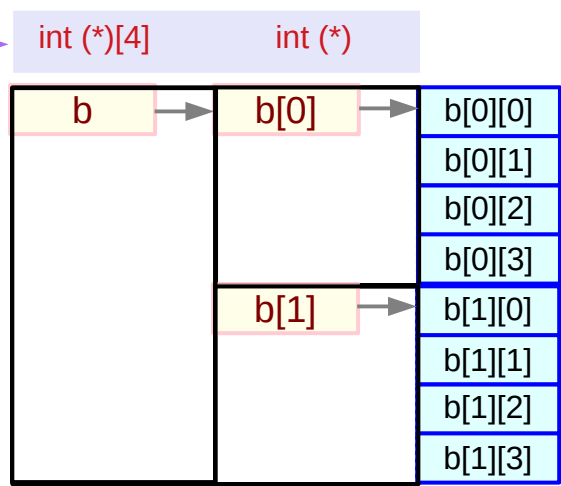
2-d array b



relaxing the 1st dimension



abstract data size view
outside type of each subarray



virtual pointer address view
inside type of each subarray

Relaxing the 1st dimension of an array

Multi-dimensional array types

array types

```
int a [4];
```

```
int b [4][5];
```

```
int c [4][5][6];
```

function calls

```
funa(a);
```

```
funb(b);
```

```
func(c);
```

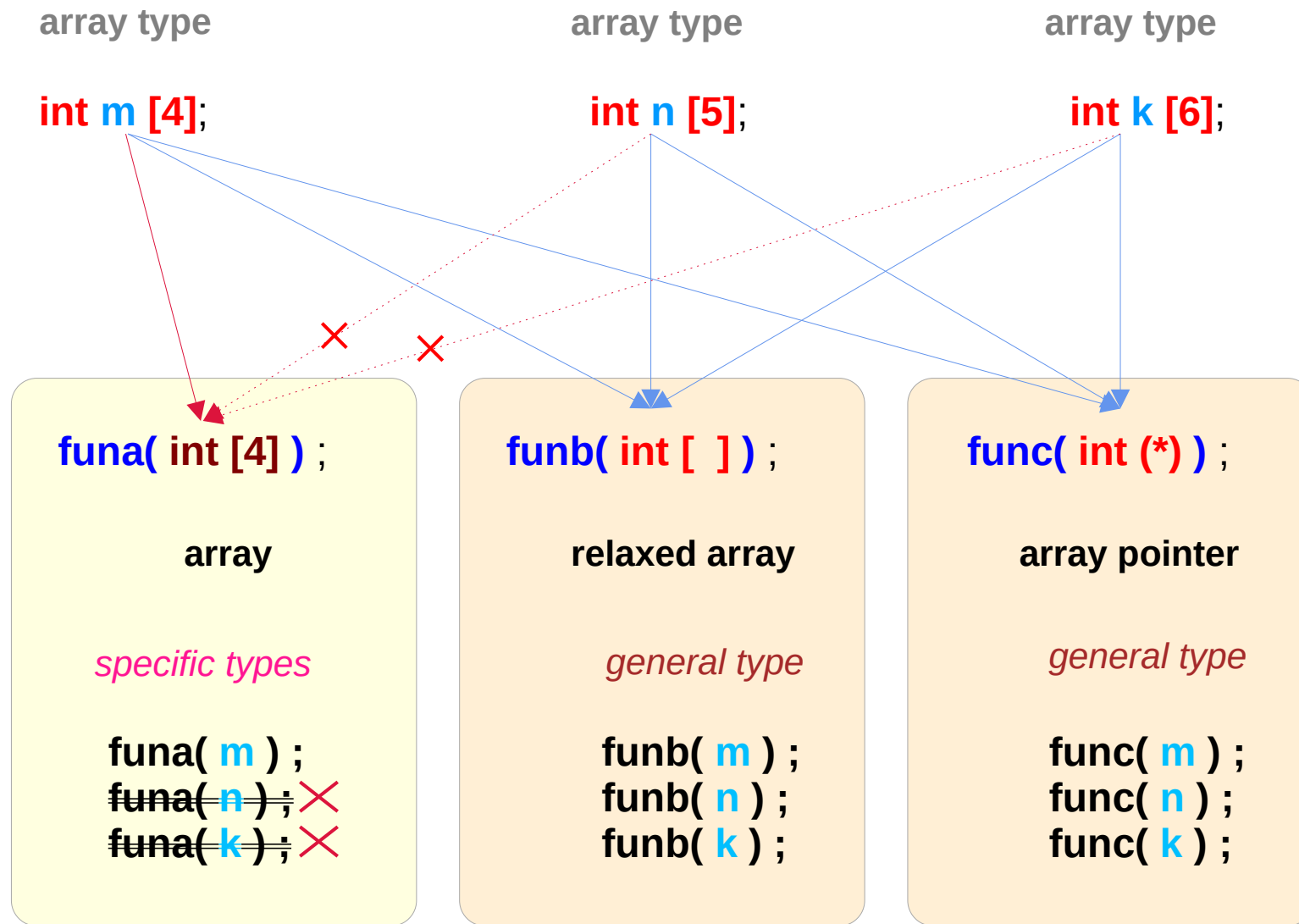
possible function prototypes

| | | |
|-------------------------------|---------------|----------------------|
| <code>funa(int [4]);</code> | array type | <i>specific type</i> |
| <code>funa(int []);</code> | relaxed array | <i>general type</i> |
| <code>funa(int (*));</code> | array pointer | <i>general type</i> |

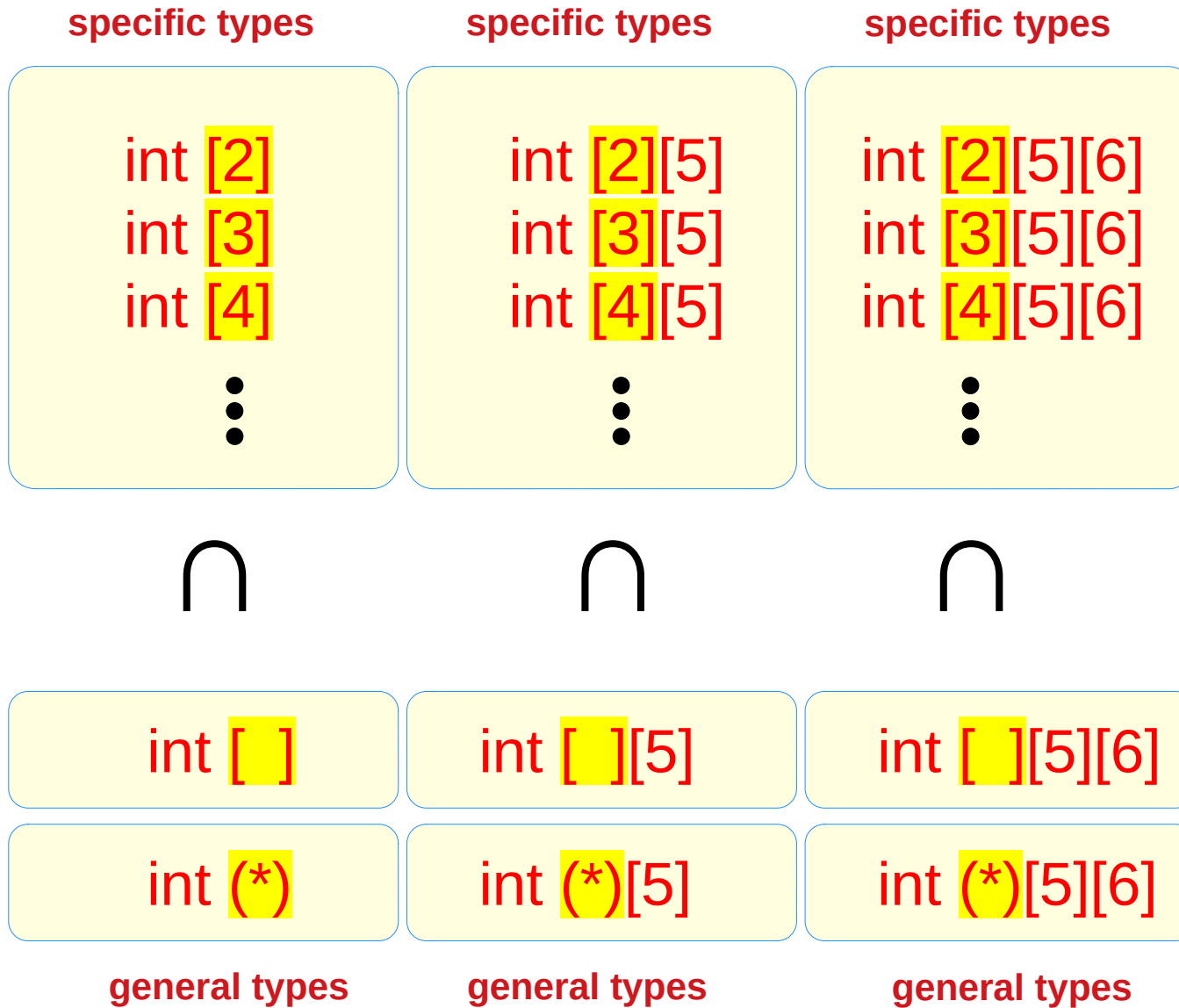
| | | |
|----------------------------------|---------------|----------------------|
| <code>funb(int [4][5]);</code> | array type | <i>specific type</i> |
| <code>funb(int [][5]);</code> | relaxed array | <i>general type</i> |
| <code>funb(int (*)[5]);</code> | array pointer | <i>general type</i> |

| | | |
|-------------------------------------|---------------|----------------------|
| <code>func(int [4][5][6]);</code> | array type | <i>specific type</i> |
| <code>func(int [][5][6]);</code> | relaxed array | <i>general type</i> |
| <code>func(int (*)[5][6]);</code> | array pointer | <i>general type</i> |

Multi-dimensional array types



Super types and sub types



relaxing the 1st dimension

pointer to the sub-array

Relaxing array types

int [3][4][5]

3-d array

int [][4][5]

the 1st dimension
relaxed

int (*)[4][5]

2-d array pointer

int [4][5]

2-d array

int [][5]

the 1st dimension
relaxed

int (*)[5]

1-d array pointer

int [5]

1-d array

int []

the 1st dimension
relaxed

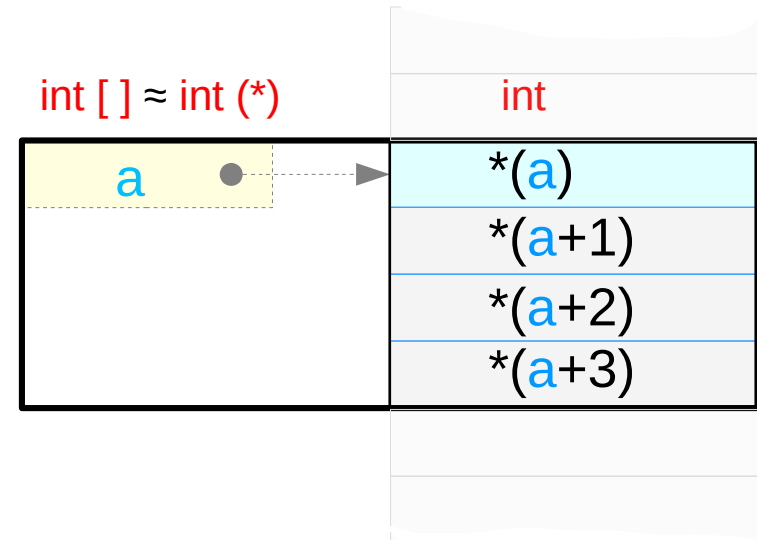
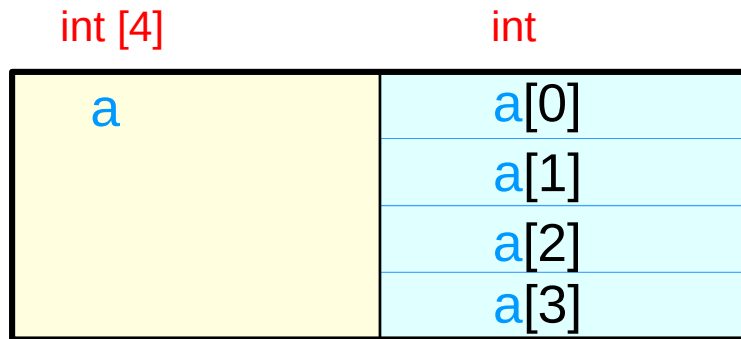
int (*)

0-d array pointer

undefined size

pointer size

Passing an individual element by reference



int [4]



int []
⇔
int (*)
≡
int *

relaxing the 1st dimension

pointer to a 0-d array

pointer to an integer

Passing a *n-d* array pointer

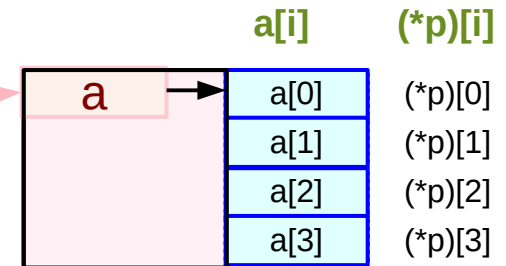
1-d array

```
int a[4];
```



call
`a :: int [4]`
`&a :: int (*) [4]`
`funa(&a, ...);`

prototype
`void funa(int (*p)[4], ...);`
1-d array pointer
`p :: int (*) [4]`



Passing a $(n-1)$ -d array pointer

1-d array

`int a[4];`



call `a :: int[4]`

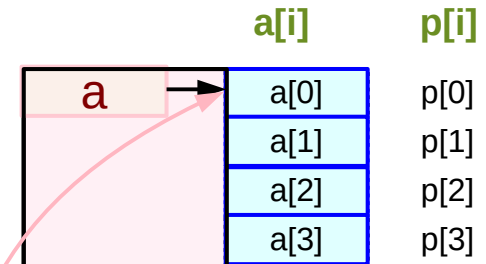
`funa(a, ...);`

prototype

`void funa(int (*p), ...)` {

0-d array pointer

`p :: int(*)`



`int (*p)`
`int p[]`
`int p[4]`

Passing *n*-d array pointers

| | | |
|---|---|---|
| 1-d array <code>int a [4] ;</code> <code>a[i]</code> | call <code>funa(&a, ...);</code> | prototype 1-d array pointer <code>void funa(int (*p)[4], ...);</code> <code>(*p)[i]</code> |
| 2-d array <code>int b [4][2];</code> <code>b[i][j]</code> | call <code>funb(&b, ...);</code> | prototype 2-d array pointer <code>void funb(int (*q)[4][2], ...);</code> <code>(*q)[i][j]</code> |
| 3-d array <code>int c [4][2][3];</code> <code>c[i][j][k]</code> | call <code>func(&c, ...);</code> | prototype 3-d array pointer <code>void func(int (*r)[4][2][3], ...);</code> <code>(*r)[i][j][k]</code> |
| 4-d array <code>int d [4][2][3][4];</code> <code>d[i][j][k][l]</code> | call <code>fund(&d, ...);</code> | prototype 4-d array pointer <code>void fund(int (*s)[4][2][3][4], ...);</code> <code>(*s)[i][j][k][l]</code> |

Passing ($n-1$)-d array pointers

| | | |
|--|------------------------------------|--|
| 1-d array <code>int a[4];</code> <code>a[i]</code> | call <code>funa(a, ...);</code> | prototype 0-d array pointer <code>void funa(int (*p), ...);</code> <code>p[i]</code> |
| 2-d array <code>int b[4][2];</code> <code>b[i][j]</code> | call <code>funb(b, ...);</code> | prototype 1-d array pointer <code>void funb(int (*q)[2], ...);</code> <code>q[i][j]</code> |
| 3-d array <code>int c[4][2][3];</code> <code>c[i][j][k]</code> | call <code>func(c, ...);</code> | prototype 2-d array pointer <code>void func(int (*r)[2][3], ...);</code> <code>r[i][j][k]</code> |
| 4-d array <code>int d[4][2][3][4];</code> <code>d[i][j][k][l]</code> | call <code>fund(d, ...);</code> | prototype 3-d array pointer <code>void fund(int (*s)[2][3][4], ...);</code> <code>s[i][j][k][l]</code> |

Receiving ($n-1$)-d array pointers

1-d array

```
int a [4] ;
```

call `a :: int [4]`

```
funa(a, ...);
```

prototype

```
void funa(int (*p), ...) {
```

```
void funa(int p[ ], ...) {
```

```
void funa(int p[4], ...) {
```

0-d array pointer

`p :: int (*)`

`a[i]`

1-d array, relaxed

`p :: int []`

`a[i]`

1-d array

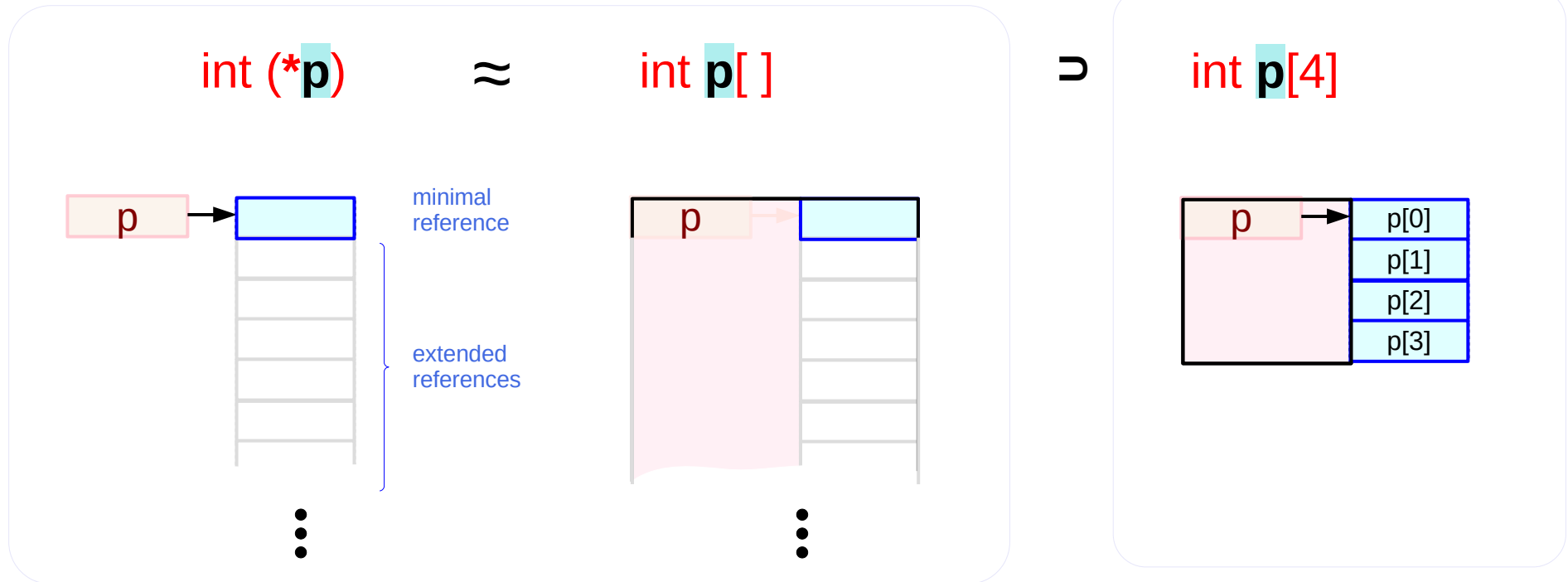
`p :: int [4]`

`a[i]`

int (*) and int [] types

supertype

subtype



`int p[]` unsized array expression is only allowed

- in a function definition
- in an initialization

The 1st dimensions

int **a**[4];

int **(*p)**
int **p**[]
int **p**[4]

p[i]

int **b**[4][2];

int **(*q)**[2]
int **q**[][2]
int **q**[4][2]

q[i][j]

int **c**[4][2][3];

int **(*r)**[2][3]
int **r**[][2][3]
int **r**[4][2][3]

r[i][j][k]

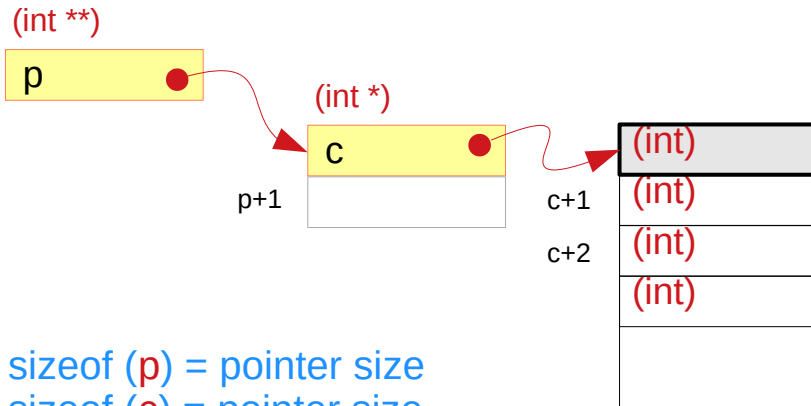
int **d**[4][2][3][4];

int **(*s)**[2][3][4]
int **s**[][2][3][4]
int **s**[4][2][3][4]

s[i][j][k][l]

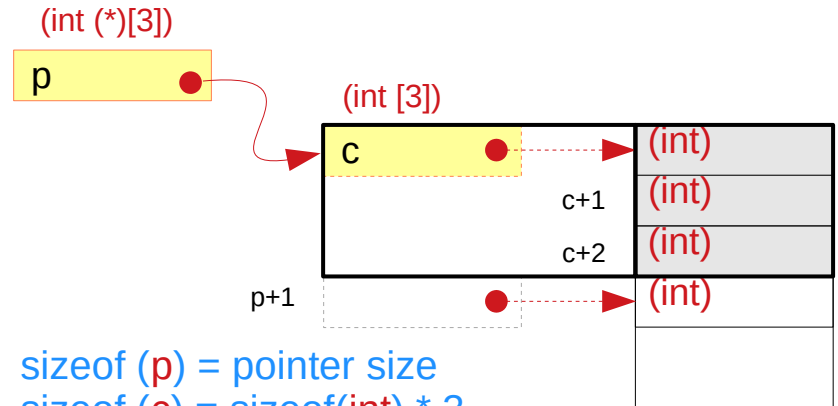
Integer pointer and array types – `int **`, `int (*)[3]`, `int[2][3]`

`int **p;` `int *c;` $v(\&c) \neq v(c)$



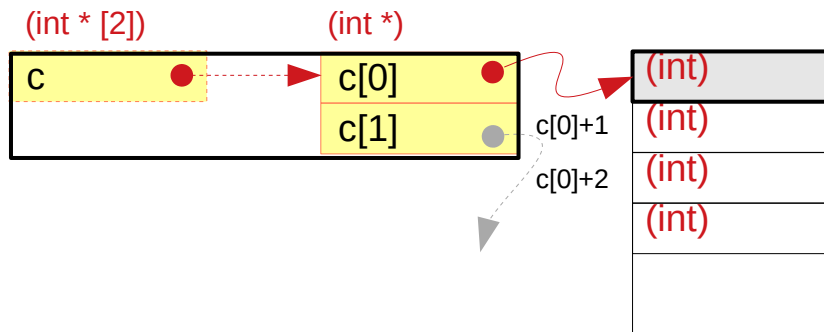
`sizeof (p)` = pointer size
`sizeof (c)` = pointer size

`int (*p)[3];` `int c[3];` $v(\&c) = v(c)$



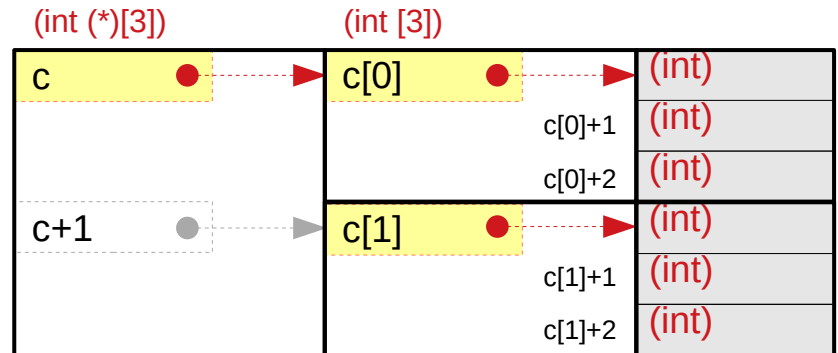
`sizeof (p)` = pointer size
`sizeof (c)` = `sizeof(int) * 3`

`int* c[2];` $v(\&c[0]) \neq v(c[0])$



`sizeof (c)` = pointer size * 2
`sizeof (c[0])` = pointer size

`int c[2][3];` $v(\&c) = v(c) = v(\&c[0]) = v(c[0])$



`sizeof (c)` = `sizeof(int) * 2 * 3`
`sizeof (c[0])` = `sizeof(int) * 3`

Integer pointer types

```
#include <stdio.h>
```

```
void func(int d[ ])
```

```
{  
}  
}
```

```
int main(void) {
```

```
    int a[4];
```

```
    int *b;
```

```
    int **c;
```

```
    int (*p)[4];
```

```
    func(a);
```

```
}
```

```
sizeof(a) = 16 = 4*4
```

```
sizeof(*a) = 4
```

```
// array size
```

```
// int size
```

```
sizeof(b) = 8
```

```
sizeof(*b) = 4
```

```
// pointer size
```

```
// int size
```

```
sizeof(c) = 8
```

```
sizeof(*c) = 8
```

```
sizeof(**c) = 4
```

```
// pointer size
```

```
// pointer size
```

```
// pointer size
```

```
sizeof(d) = 8
```

```
sizeof(*d) = 4
```

```
// pointer size
```

```
// int size
```

```
sizeof(p) = 8
```

```
sizeof(*p) = 16 = 4*4
```

```
// pointer size
```

```
// array size
```

References

- [1] Essential C, Nick Parlante
- [2] Efficient C Programming, Mark A. Weiss
- [3] C A Reference Manual, Samuel P. Harbison & Guy L. Steele Jr.
- [4] C Language Express, I. K. Chun