CMOS Delay-7 (H.8) Delay Model

20170131

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•	References
	ricicies
	Some Figures from the following sites
	[1] http://pages.hmc.edu/harris/cmosvlsi/4e/index.html Weste & Harris Book Site
	[2] on wikingdia org
	[2] en.wikipedia.org

B: Device Transconductance Parameter

k: Process Transconductance Parameter

ル: Electron / Hole Mobility

PMOS
$$\beta_P = k_P' \left(\frac{\omega}{L} \right)_P$$
 $k_P' = \mu_P C_{ox}$ $C_{ox} = \frac{\epsilon_{ox}}{t_{ox}}$

$$n MOS$$
 $\beta_n = k'_n \left(\frac{\omega}{L}\right)_n$ $k'_n = \mu_n C_{ox}$ $C_{ox} = \frac{\varepsilon_{ox}}{t_{ox}}$

PMOS
$$\beta_P = \mu_P \frac{\epsilon_{ox}}{t_{ox}} \left(\frac{\omega}{L}\right)_P$$

$$n MOS$$
 $\beta_n = \mu_n \frac{\epsilon_{ox}}{t_{ox}} \left(\frac{\omega}{L}\right)_n$

Saturation Current

$$I_{dp} = \frac{\beta_p}{2} \left(V_{GSN} - |V_{Tp}| \right)^2 \qquad V_{Tp} < 0$$

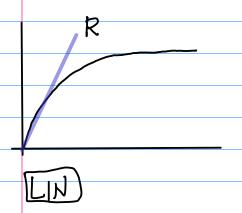
$$I_{dn} = \frac{\rho_n}{2} \left(V_{GSn} - V_{Tn} \right)^2 \qquad V_{Tn} > 0$$

$$\frac{\beta_n}{\beta_p} = \frac{k'_n \left(\frac{\omega}{L}\right)_n}{k'_p \left(\frac{\omega}{L}\right)_p}$$

$$\frac{k'_n}{k'_p} = 2 \sim 3$$

$$\frac{k'_n}{k'_p} - \frac{\mu_n}{\mu_p} = r$$

$$\frac{\beta_{n}}{\beta_{p}} = \frac{k'_{n} \left(\frac{\omega}{\omega}\right)_{n}}{k'_{p} \left(\frac{\omega}{\omega}\right)_{p}}$$



$$R_{n} = \frac{1}{\beta_{n} (V_{pp} - V_{T_{n}})}$$

$$R_{p} = \frac{1}{\beta_{n} (V_{pp} - V_{T_{n}})}$$

Fall time tf
$$T_n = R_n C_{out}$$

rise time tr $T_p = R_p C_{out}$
 $C_{out} = C_{para} + C_L$

fall time	$t_f = 2.2 T_n = \ln 9 T_n$	0.9 Upp -> 0.1 Vpp
rise time	tr = 2.2 Tp = ln 9 Zp	0.1 Vpp -> 0.9 Vpp
propagation delay time	$t_p = \frac{1}{2} (t_{pf} + t_{pr})$ = 0.35(t _{pf} + t _{pr})	0.5 Vpp -> 0.5 Vpp
propagation fall time	tpf = 0.η ζη = ln 2 ζη	Vpb → O.5 Vbb
propagation rise time	tpr = 0.7 Tp = ln 2 Tp	0 → 0.5 V _{Pb}
	$\frac{7_n = Rn(Cpara + C_1)}{T_n = n(C_1 + C_2)}$	
	Tp = Rp (Cpana + CL)	

Cout = Cpara + C1

$$\left(\frac{W}{L}\right)_{p} = \gamma \left(\frac{W}{L}\right)_{n}$$

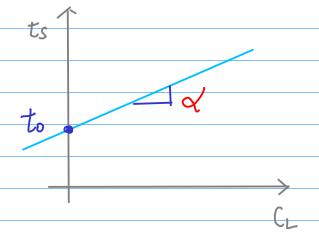
$$\gamma = \frac{\mu_n}{\mu_p} = \frac{k_n}{k_p} > 1$$

$$\begin{cases} V_{\text{out}}(t) = V_{\text{pv}}(1 - e^{-t/z}) \\ V_{\text{out}}(t) = V_{\text{pv}}e^{-t/z} \end{cases}$$

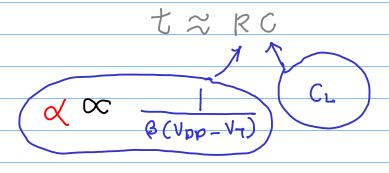
Generic Switching Delay

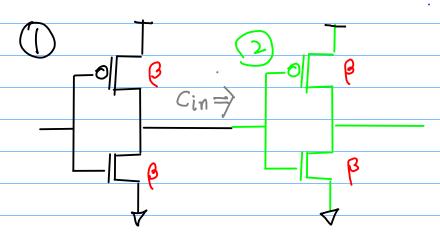
$$ts = t_0 + \alpha C_L \Rightarrow t_s = t_r - t_f$$

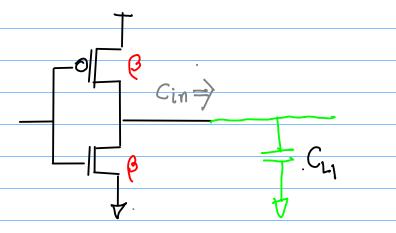
Generic Switching Delay

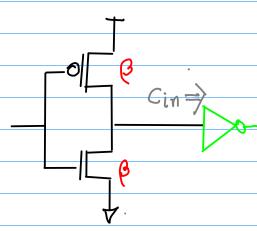


to: zero delay x: slope









reference case

Generic Switching Delay of

$$ts_1 = t_0 + \alpha C_{21}$$

= $t_0 + \alpha C_{in}$

the channel length L assumed

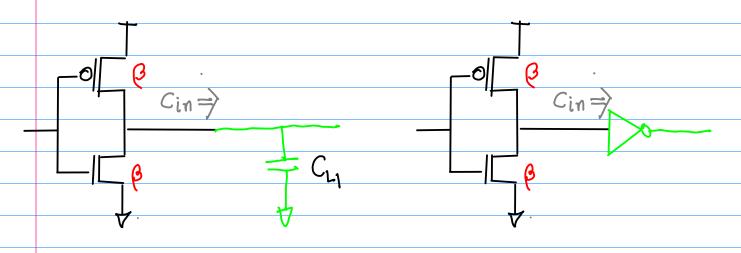
$$Cin = Cox L (W_n + W_p)$$

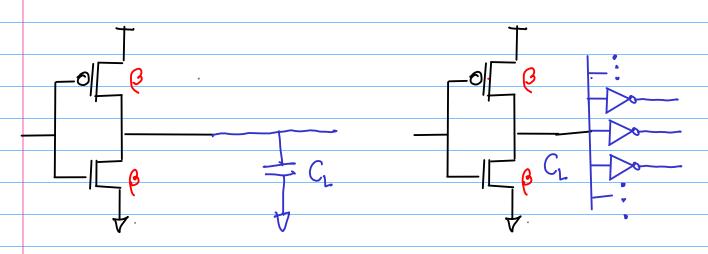
$$= Cox L (W_n + Y W_p)$$

$$= Cox L W_n \cdot (1 + Y)$$

$$= Cox L W_n \cdot (1 + Y)$$

When CL>>> Cin





to minimize ts

Speed V.s. area tradeoff

$$ts = t_0 + \alpha C_L t \approx RC$$

$$\alpha \propto \frac{1}{\beta(V_{pp}-V_T)} C_L$$

to minimize ts

Speed V.s. area tradeoff

Scaling Factor S

$$R' = \frac{R}{\sqrt{3}}$$

$$\alpha' = \alpha$$

$$ts = t_0 + \frac{\alpha}{\beta} C_L$$

Compensation Factor S

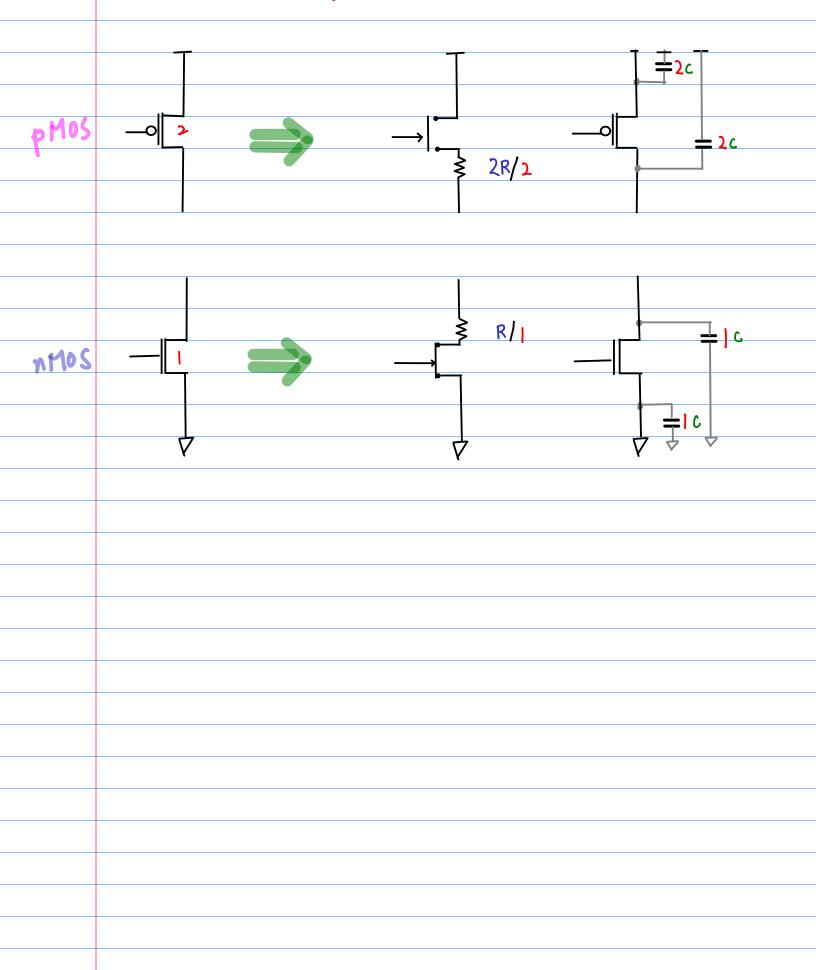


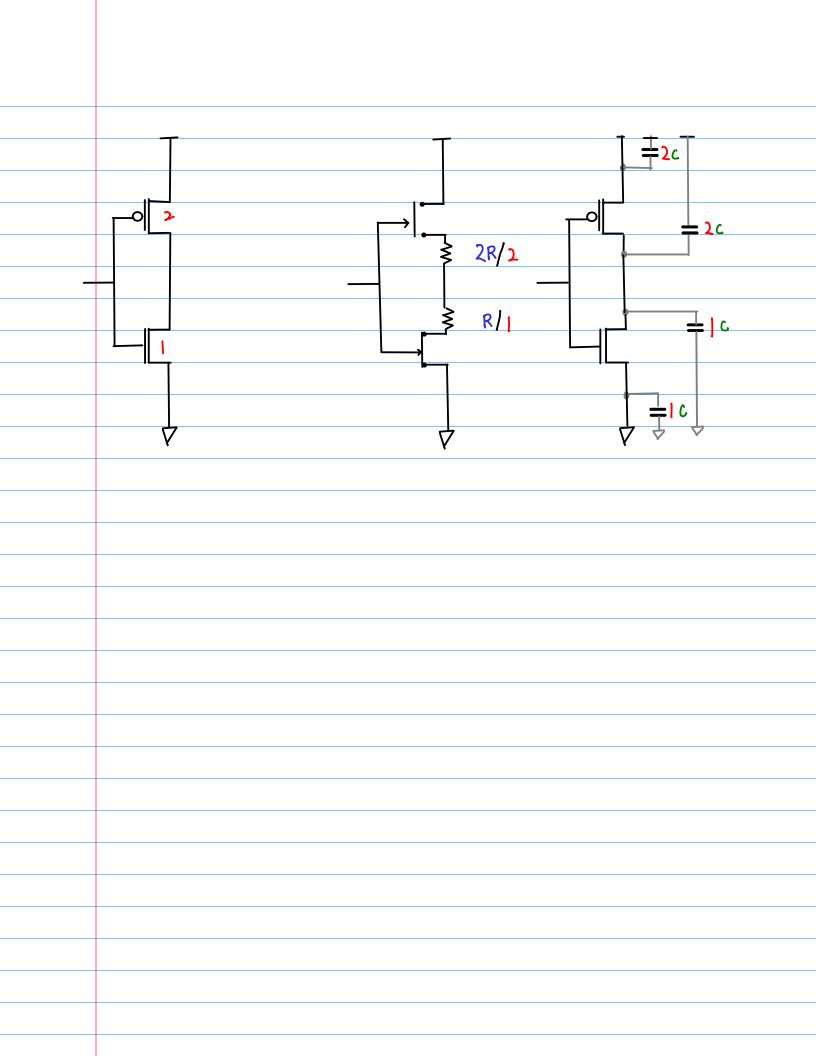
enables a NOT gate drive larger values of CL

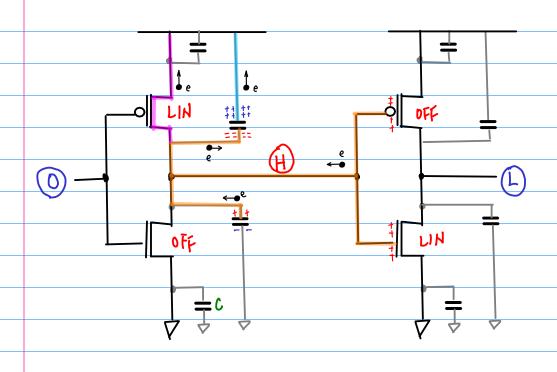
If $C_{L}=5$ Cin (increased by the scaling factor \$)

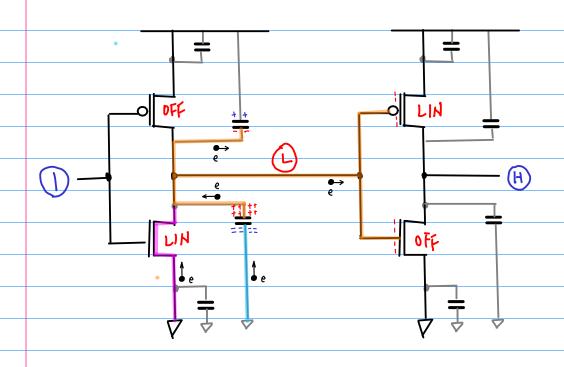
then the switching time is the same

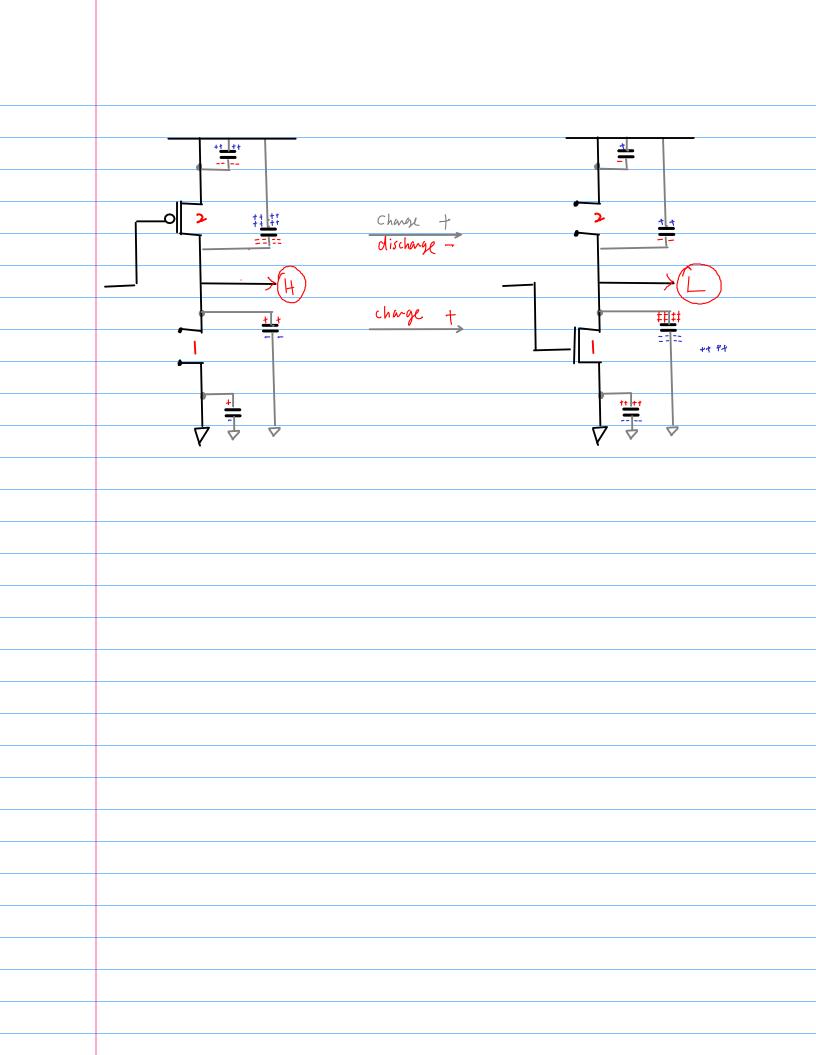
RC Delay Model

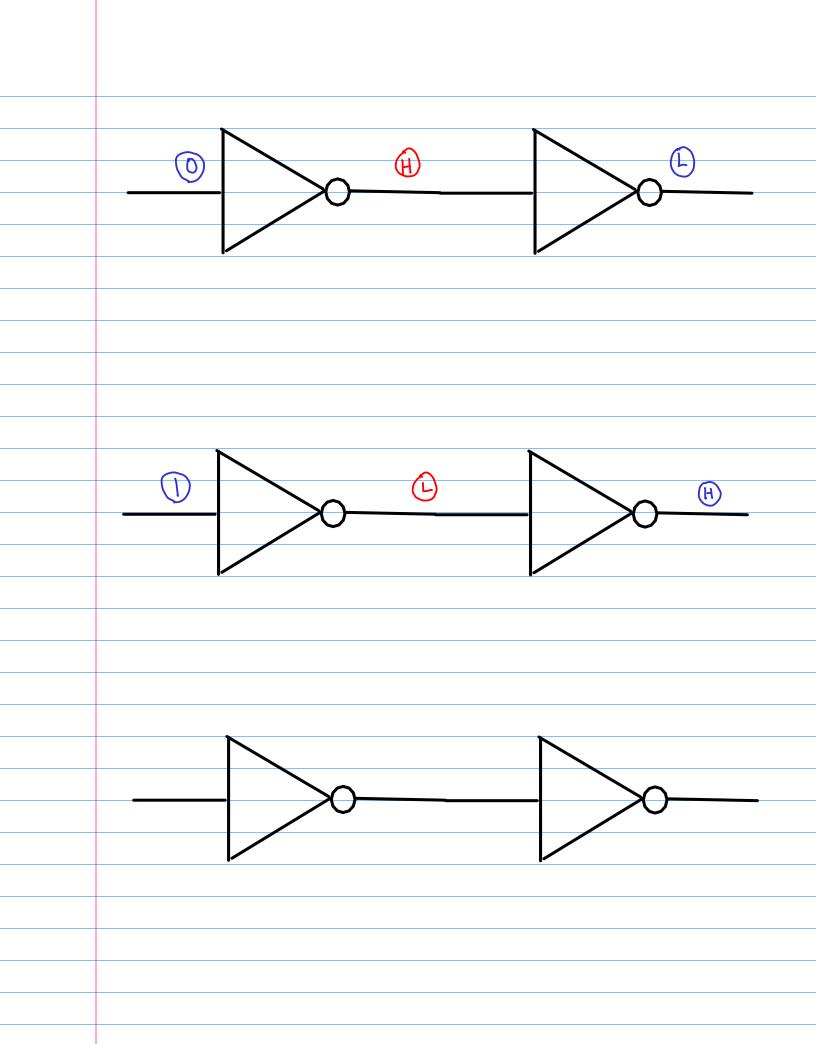


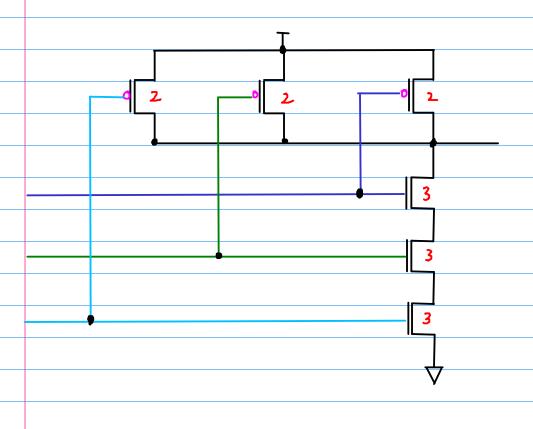


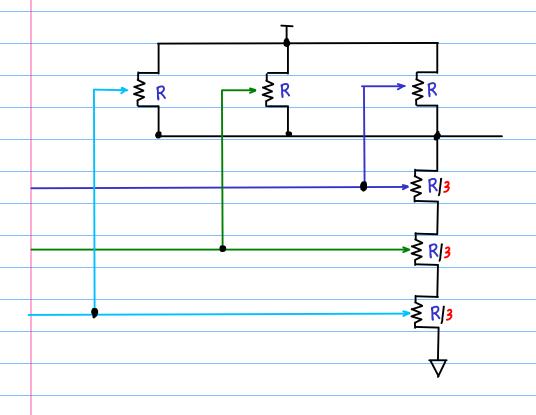


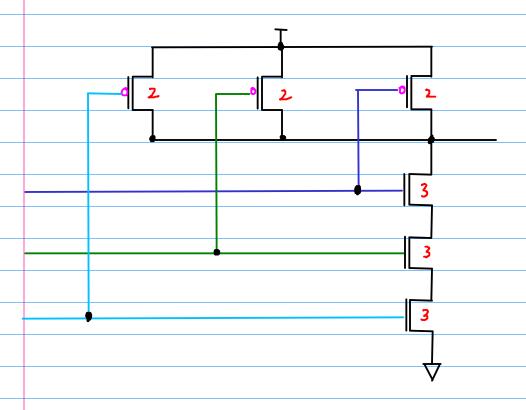


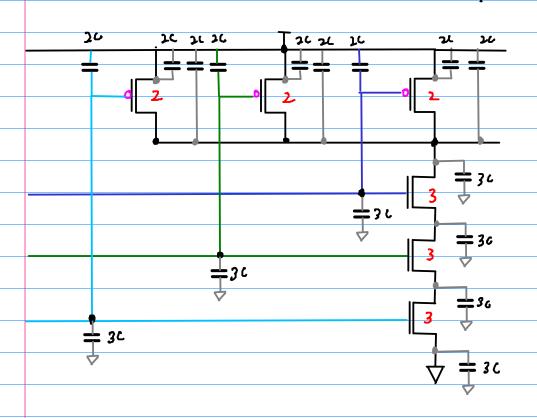


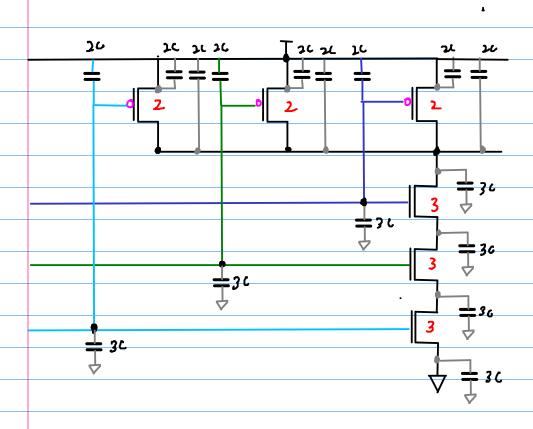


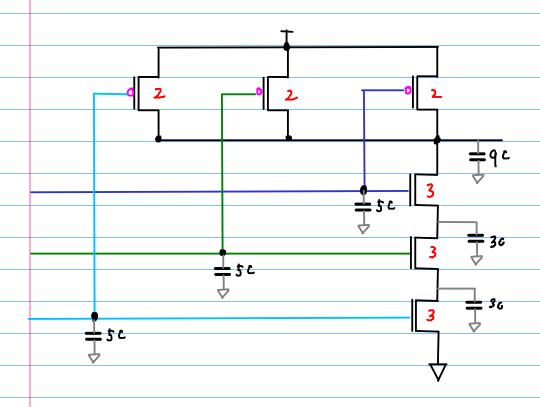


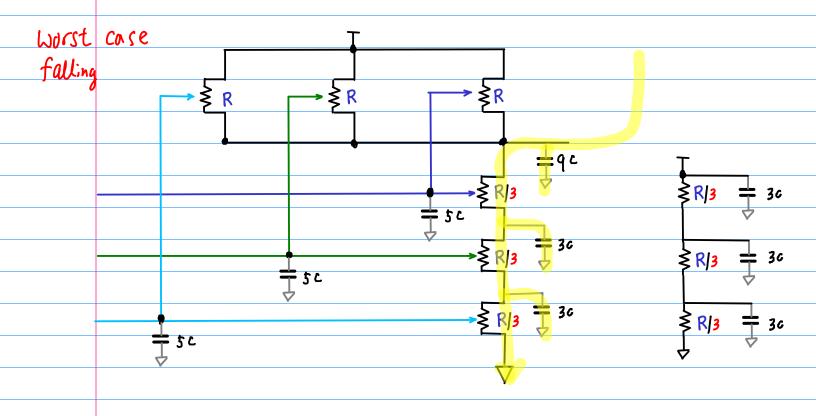


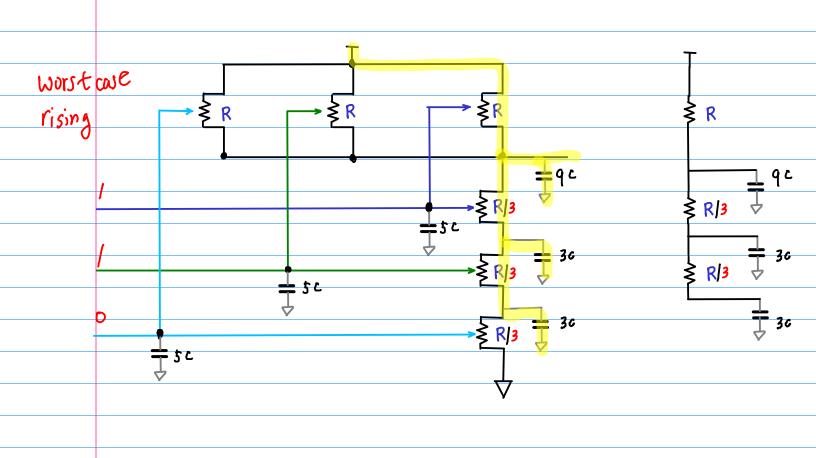


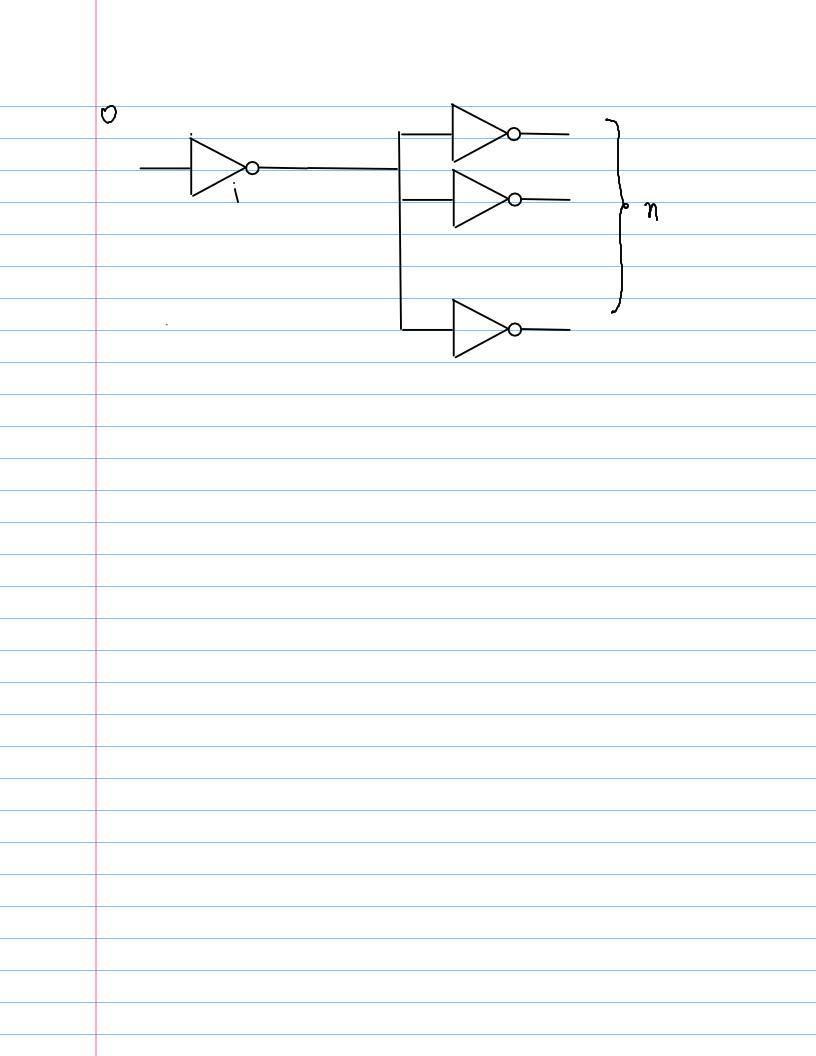




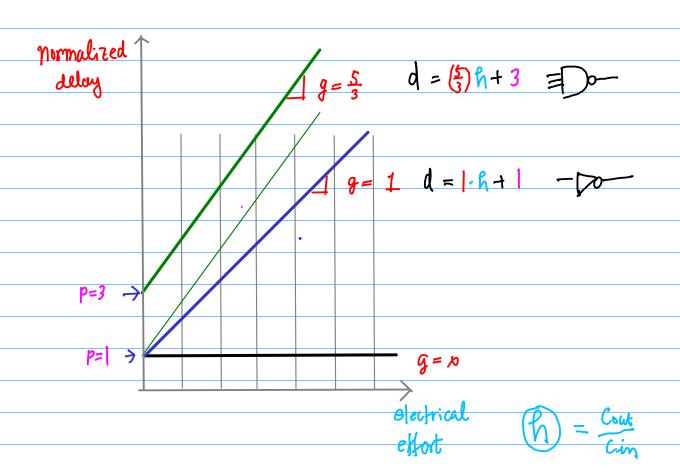


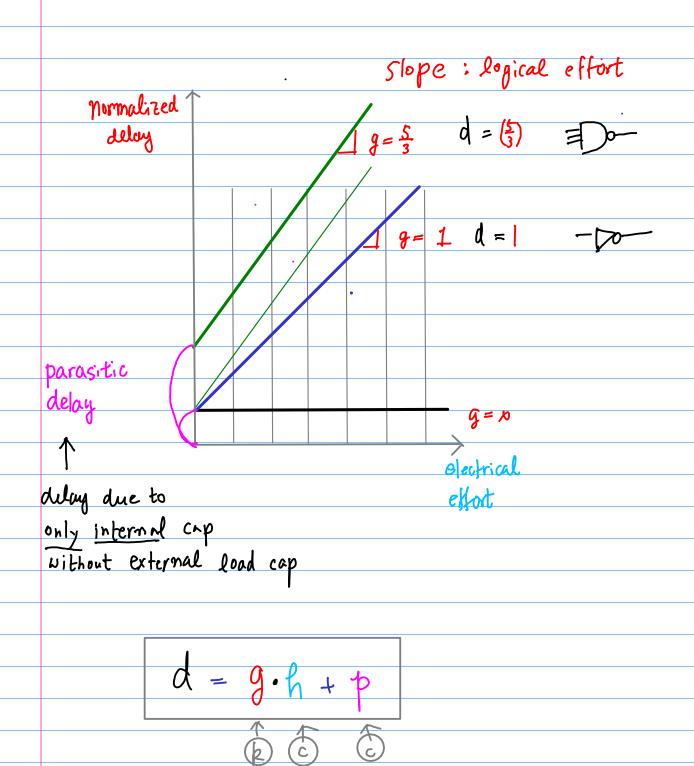






Linear Delay Model





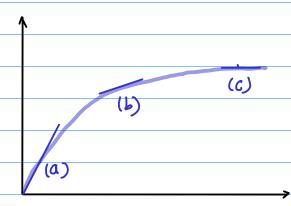


FET RC Model

$$R_n = \frac{\sqrt{psn}}{I_{bn}}$$

$$R_{n} = \frac{2}{\beta_{n} \left[2(V_{GS_{n}} - V_{T_{n}}) - V_{DS_{n}} \right]}$$
 (b)

$$R_n = \frac{2V_{DSn}}{\beta_n (V_{GSn} - V_{fn})^2}$$



$$R_{n} \propto \frac{1}{\beta_{n}}$$

$$R_{n} = k'_{n} \left(\frac{W}{L}\right)_{n}$$

$$R_{n} = \frac{\eta}{\beta_{n}(V_{pv}-V_{Tn})}$$

$$\eta = |$$

$$R_{n} = \frac{1}{\beta_{n}(V_{pv}-V_{Tn})}$$

$$\Omega$$

$$C_{qs} = \frac{1}{2} C_q = C_{qp}$$

$$C = \frac{C_o}{\left(1 + \frac{V_R}{\phi_o}\right)^{m_j}}$$

$$\phi_o = \left(\frac{kT}{g}\right) \ln \left[\frac{N_A N_A}{\eta_{i^2}}\right]$$

$$Asw = 2(W \times X_j) + 2(X + X_j)$$

$$p_{SN} = 2(N+x)$$

$$C_{jsu} = C_{j}x_{j}$$

$$C_{m} = \frac{C_{j} h_{kt}}{\left(\left|+\frac{v}{\phi_{s}}\right|^{h_{j}}} + \frac{C_{jsv} \beta_{sw}}{\left(\left|+\frac{v}{\phi_{slv}}\right|^{m_{jsw}}}\right)$$

$$C_s = C_{qs} + C_{pb}$$

$$C_{p} = C_{qp} + C_{pb}$$

$$i = -C_{out} \frac{dV_{out}}{dt} = \frac{V_{out}}{R_n}$$

$$t = z_n \ln \left(\frac{V_{ob}}{V_{out}} \right)$$

$$t_f = t_y - t_x = 7_{\eta} \ln\left(\frac{V_{DD}}{0.1 V_{DD}}\right) - 7_{\eta} \ln\left(\frac{V_{DD}}{0.9 V_{DD}}\right)$$
$$= 7_{\eta} \ln(9)$$

$$t_{HL} = t_f \cong 2.27\eta$$

$$i = -C_{out} \frac{dV_{out}}{dt} = \frac{V_{DD} - V_{out}}{R_{P}}$$

$$t = \tau_p \ln \left(\frac{V_{ob}}{V_{out}} \right)$$

$$t_f = t_r - t_u = \tau_p \ln\left(\frac{V_{pp}}{o.|V_{pp}}\right) - \tau_n \ln\left(\frac{V_{pp}}{o.9|V_{pp}}\right)$$

$$= \tau_p \ln(9)$$

Propagation Delay

$$t_r = t_{ro} + \alpha_p C_L$$

 $t_f = t_{ro} + \alpha_n C_L$

$$c_1 = 0 \rightarrow t_r = t_{ro} \approx 2.1 \, R_p \, C_{FET}$$
 $c_L = 0 \quad t_f = t_{ro} \approx 2.1 \, R_n \, C_{FET}$

$$\alpha_{p} = 2.1 \, p_{p} = \frac{2.2}{\beta_{p} \left(V_{pp} - |V_{Tp}| \right)}$$

$$\alpha_{n} = 2.1 \, p_{n} = \frac{2.2}{\beta_{n} \left(V_{pp} - |V_{T_{n}}| \right)}$$

$$\beta_n = k'_n \left(\frac{\omega}{L} \right)_n$$