State Monad – Methods (6B)

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> Young Won Lim 9/18/18

Haskell in 5 steps

https://wiki.haskell.org/Haskell_in_5_steps

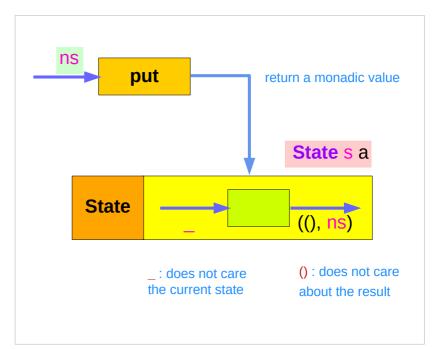
put changes the current state

put :: s -> State s a
put ns = state \$ _ -> ((), ns)

Given a wanted state new State (ns),

put generates a state processor

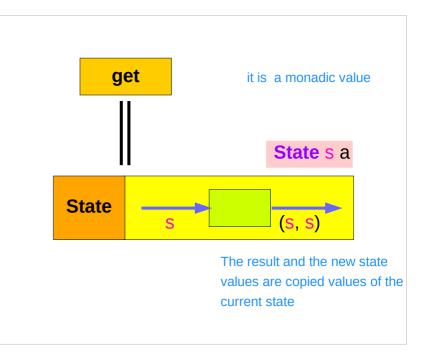
- ignores whatever the state it receives,
- <u>updates</u> the state to ns
- doesn't care about the result of this processor
- all we want to do is to change the state
- the tuple will be ((), ns)
- () : the universal placeholder value.



get gives the current state :

get :: State s s

get = state \$ \s -> (s, s)

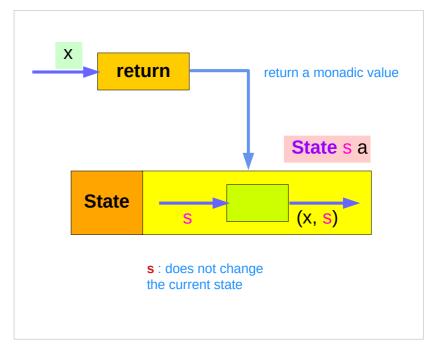


get generates a state processor

- gives back the state s0
- as a result and as an updated state (s0, s0)
- the state will remain unchanged
- a <u>copy</u> of the state will be made available through the result returned

return method

return :: a -> State s a return x = state (\s -> (x, s))



giving a value (x) to **return** results in a **state processor** function

> which <u>takes</u> a state (s) and <u>returns</u> it <u>unchanged</u> (s), together <u>with</u> the value x

finally, the function is <u>wrapped</u> up by state.

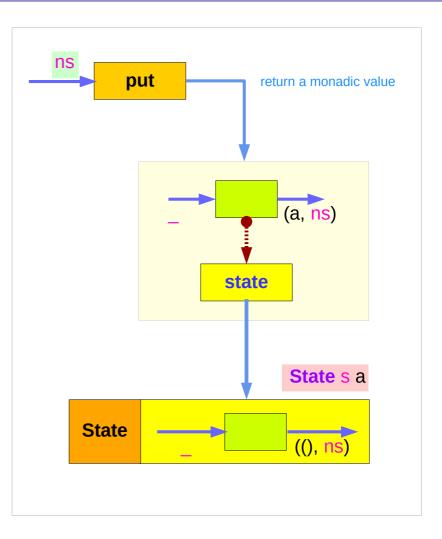
put returns a monadic value by state

put :: s -> State s a

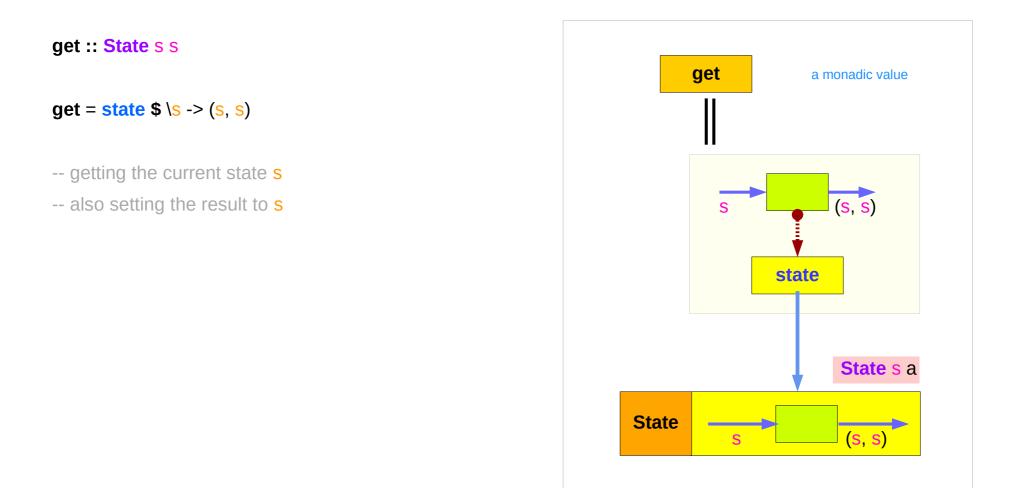
put s :: State s a

put newState = state \$ _ -> ((), newState)

- -- setting a state to newState
- -- regardless of the old state
- -- setting the result to ()



get is a monadic value by state



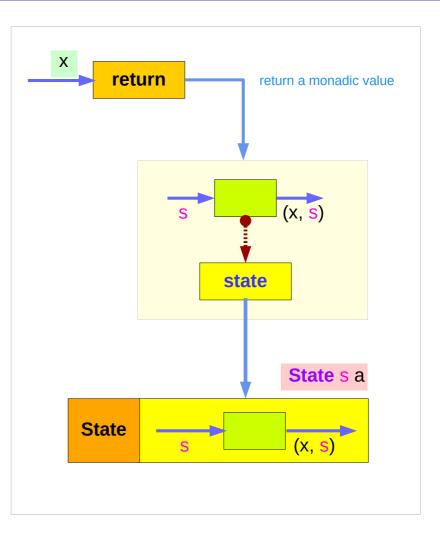
return returns a monadic value by state

return :: s -> State s a return s :: State s a

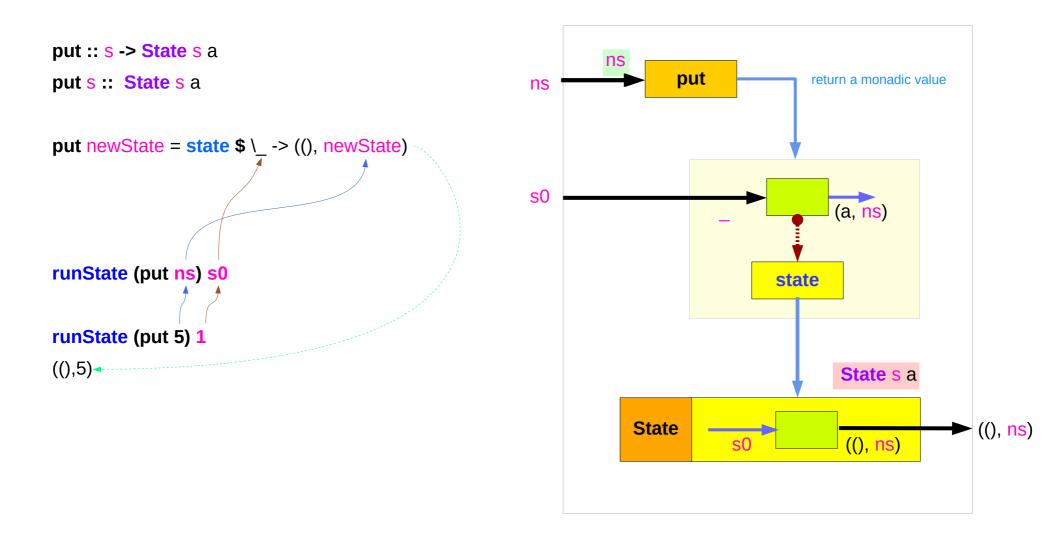
return x = **state** \$ _ -> (x, s)

-- do not change a state s

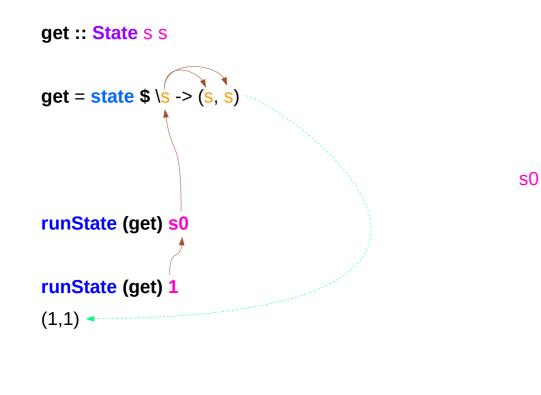
-- setting the result to x

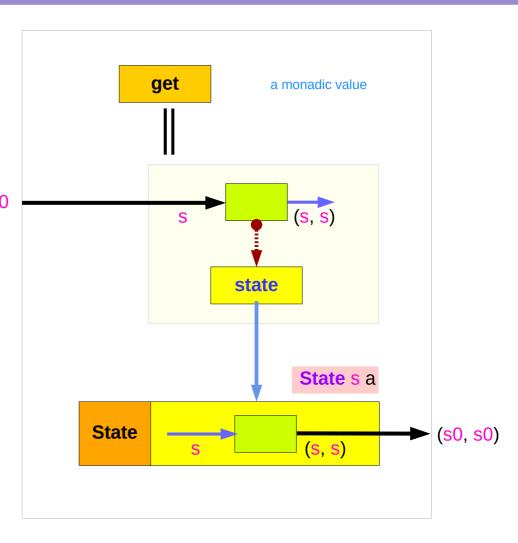


Running put



Running get



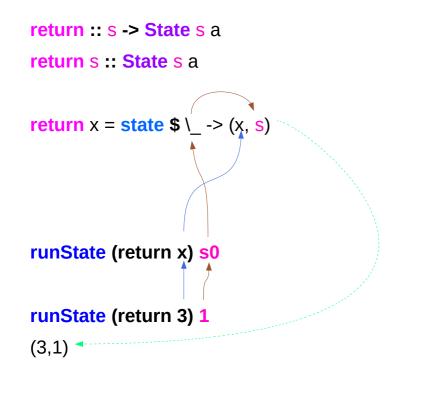


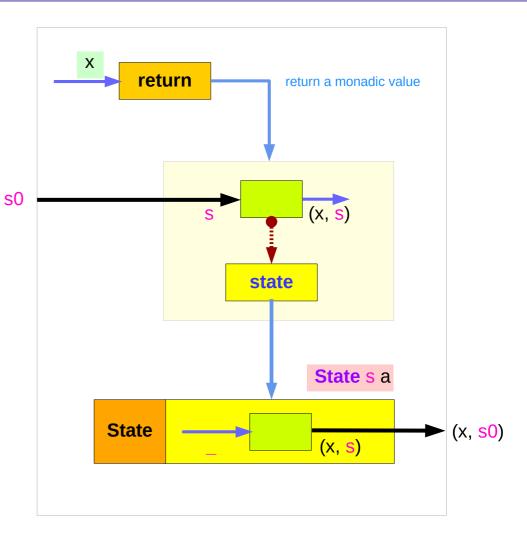
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

State Monad (6B) Methods

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Running return





Example codes (1)

import Control.Monad.Trans.State

runState get 1
(1,1)
runState (return 'X') 1
('X',1)
runState get 1
(1,1)
runState (put 5) 1
((),5)

```
runState (put 1 >> get >> put 2 >> get ) 0
(2,2)
runState (get >>= \n -> put (n+1) >> return n) 0
(0,1)
inc = get >>= (n - put (n+1) >> return n
runState inc 0
(0,1)
runState (inc >> inc) 0
(1,2)
runState (inc >> inc >> inc) 0
(2,3)
```

Example codes (2)

```
import Control.Monad.Trans.State
```

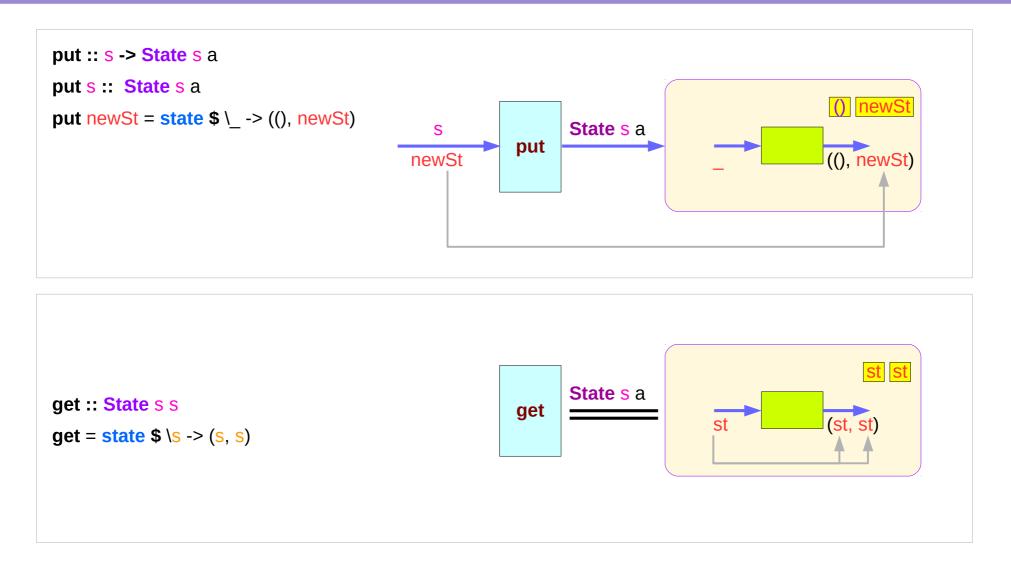
```
let postincrement = do { x <- get; put (x+1); return x }
runState postincrement 1
(1.0)</pre>
```

```
(1,2)
```

```
let predecrement = do { x <- get; put (x-1); get }
runState predecrement 1
(0,0)</pre>
```

```
runState (modify (+1)) 1
((),2)
runState (gets (+1)) 1
(2,1)
evalState (gets (+1)) 1
2
execState (gets (+1)) 1
1
```

Simple representation of put and get

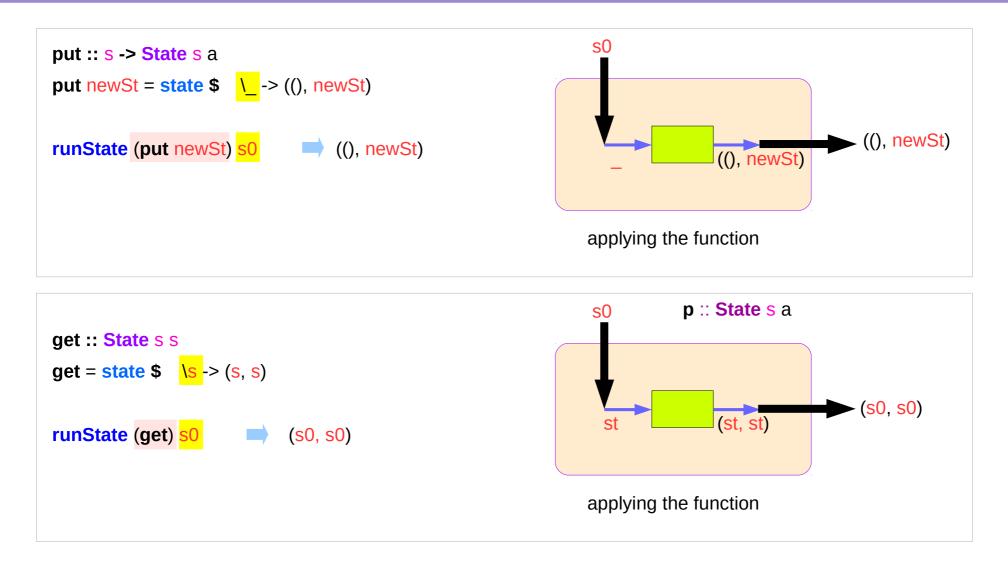


https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

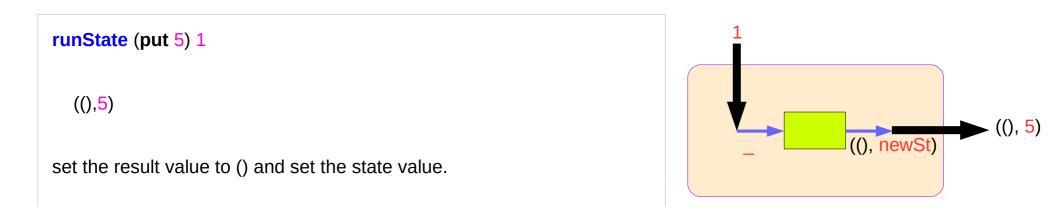
State Monad (6B) Methods

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Executing the state processor



State Monad Examples – put

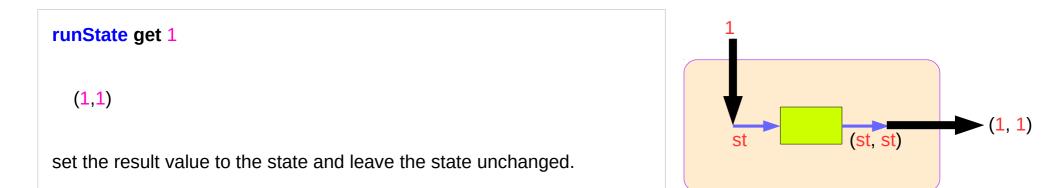


```
put 5 :: State Int ()
runState (put 5) :: Int -> ((),Int)
initial state = 1 :: Int
final value = () :: ()
final state = 5 :: Int
```

put :: s -> State s a

put newState = state \$ _ -> ((), newState)

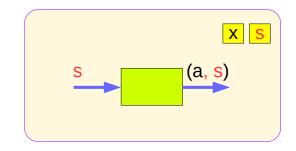
State Monad Examples – get



get :: State Int Int runState get :: Int -> (Int, Int) initial state = 1 :: Int final value = 1 :: Int final state = 1 :: Int get :: State s s get = state \$ \s -> (s, s)

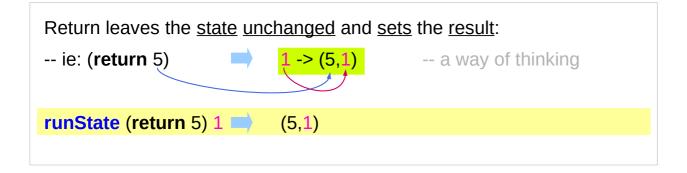
Think an unwrapped state processor

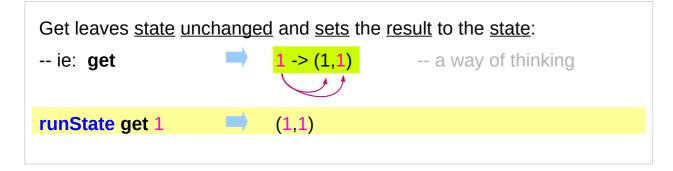


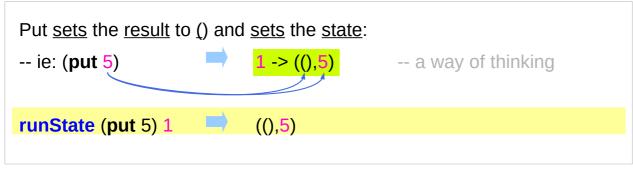


a value of type (State s a) is a function from initial state s (a, s) to final value a and final state s: (a,s). state these are usually wrapped, but shown here unwrapped for simplicity. State s a wrapping the $(return 5) \implies state(1 -> (5,1))$ -- an actual impl state processor (a, s) state(1 -> (1,1))-- an actual impl qet **State** state(1 -> ((), 5))(put 5) -- an actual implementation

State Monad Examples - return, get, and put







https://wiki.haskell.org/State_Monad

State Monad Examples – modify and gets

runState (modify ((+1)) 1	((),2)	modify sta
(+1) 1 → 2 :: s		get state
runState (gets (+1)) 1		(2,1)	evalState
(+1)) 1 → 2 :: a		execState
evalState (modify	(+1)) 1	()	
→ s :: state	fst ((), 2)		(a, s
			(eval, exec
avaaStata (madifu		2	
execState (modify		Ζ	(get, modi
→ a :: result	snd ((), 2)		
evalState (gets (+1	L)) 1	<u>2</u>	
→ s :: state	fst (2, 1)		
execState (gets (+1)) 1		1	
→ a :: result	snd (2, 1)		
	- (/ /		

tate (–, f x) (f x, s) (<mark>a</mark>, s) (a, <mark>s</mark>) е

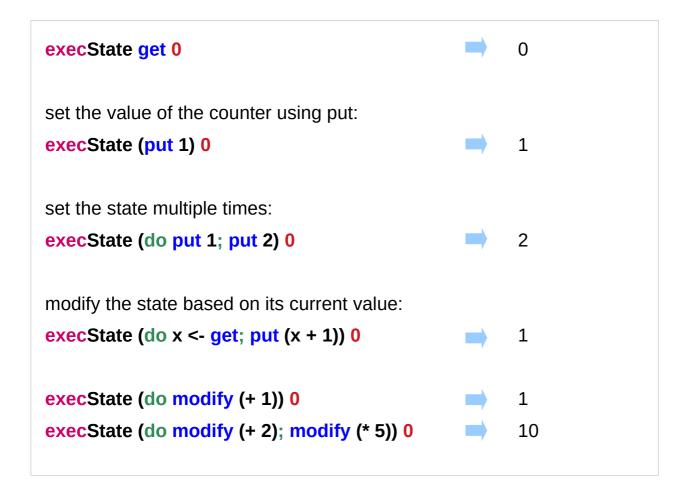
) ec) lify)

Unwrapped Implementation Examples

return :: a -> <mark>State s</mark> a	(x,s)
return x <mark>s</mark> = (x,s)	(S,S)
	((),X)
get :: State s s	
get s = (s,s)	• <u>inside</u>
	• <u>unwr</u>
put :: <mark>s -> State s</mark> ()	of re
put x <mark>s</mark> = ((),x)	
modify :: (<mark>s -> s</mark>) ->	X <
modify f = do { x <- get; put (f x) }	X <
gets :: (<mark>s</mark> -> a) -> <mark>State s</mark> a	• inside
gets f = do { x <- get; return (f x) }	• <u>unwr</u>
	of m e

	(X,S)				
	(S,S)				
	((),X)				
	• inside a monad instance				
	 <u>unwrapped</u> implementations 				
	of return , get , and put				
	x <- get; put (f x) - state				
	x <- get; return (f x) - result				
	• inside a monad instance				
	• <u>unwrapped</u> implementations				
	of modify and gets				

State Monad Examples – put, get, modify



https://stackoverflow.com/questions/25438575/states-put-and-get-functions

A Stateful Computation

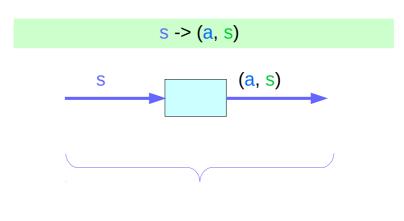
a stateful computation is a function that

takes some **state** and returns a **value** along with some **new state**.

That function would have the following type:

<mark>s -> (a,s)</mark>

s is the type of the state anda the result of the stateful computation.

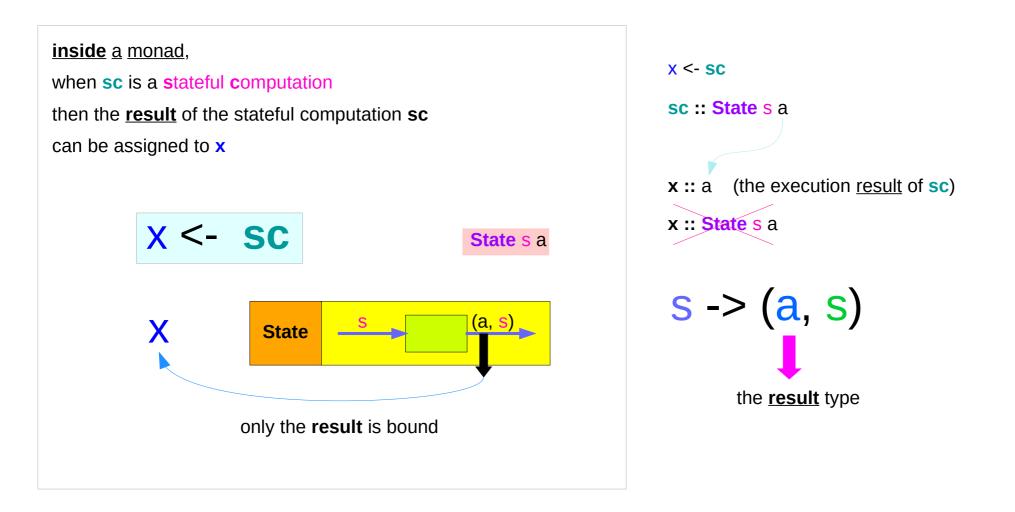


a <u>function</u> is an executable <u>data</u> when <u>executed</u>, a <u>result</u> is produced **action, execution, result**

s -> (a, s)

http://learnyouahaskell.com/for-a-few-monads-more

Stateful Computations inside the State Monad



https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

get inside the State Monad

inside the State monad,

get returns the current monad instance with the type of State s a

x <- get

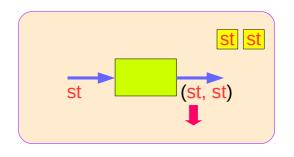
the stateful computation is performed over the <u>current monad instance</u> returned by **get**

the <u>result</u> of the <u>stateful</u> computation of **get** is **st**::s, thus **x** will get the <u>st</u>

this is like evalState is called with the current monad instance

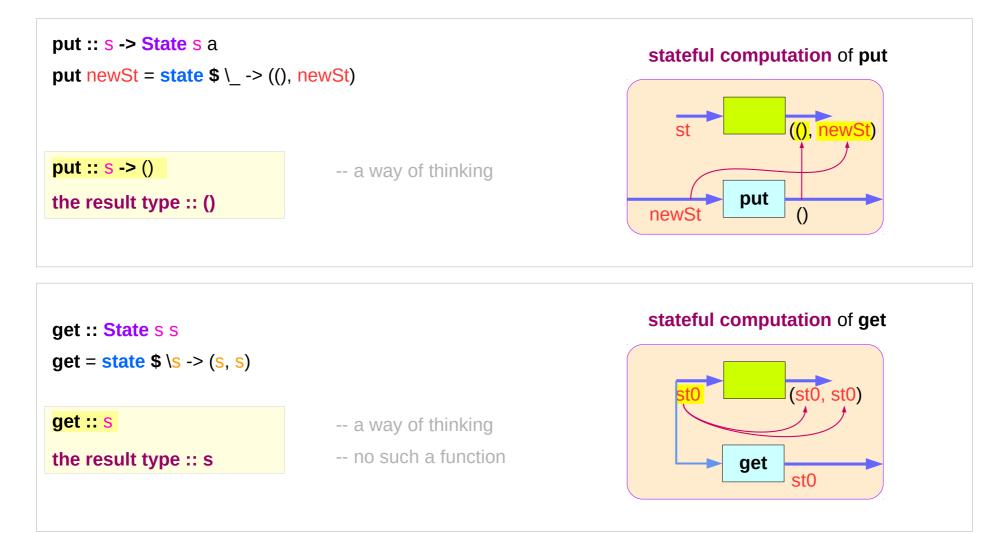
- get executed
- current monad instance
- stateful computation
- result :: s

x :: a the execution <u>result</u> of **get**



https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

put and get inside State Monad



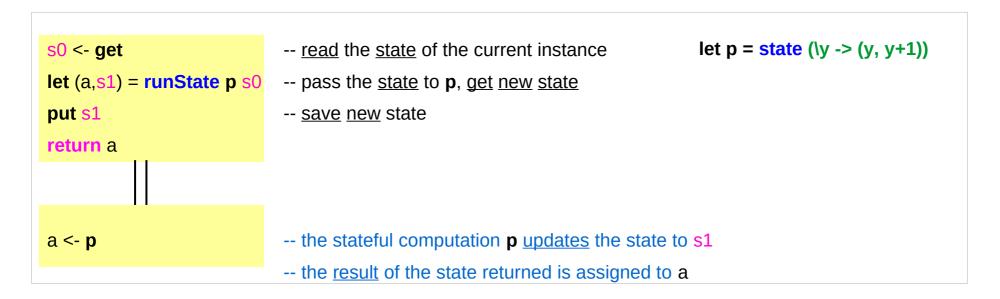
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

run functions inside a Monad

Most monads have some "*run*" functions

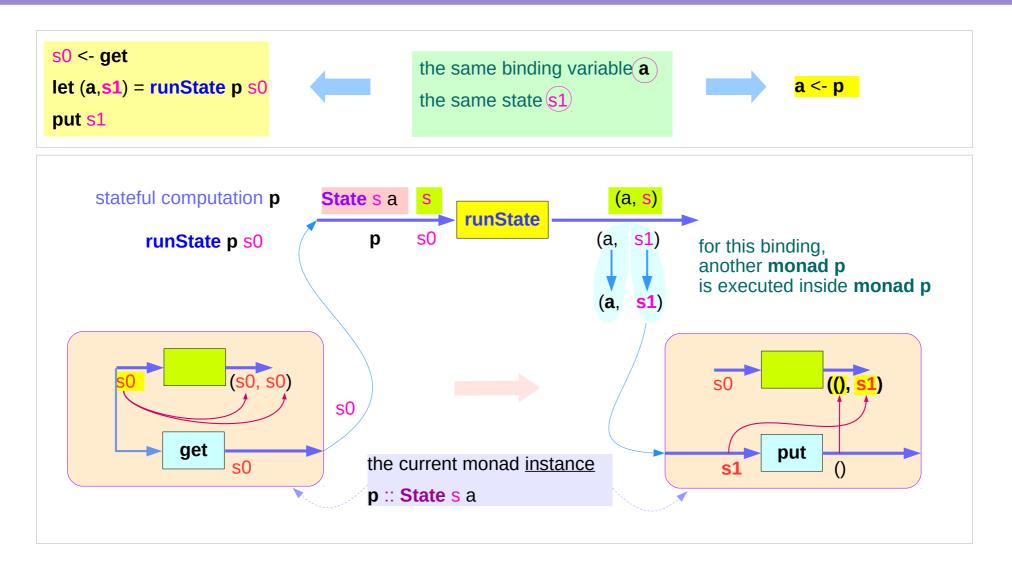
such as **runState**, **execState**, and so forth.

frequent calling such <u>functions</u> <u>inside</u> the <u>monad</u> indicates that the **functionality** of the monad does <u>not</u> <u>fully</u> <u>exploited</u>



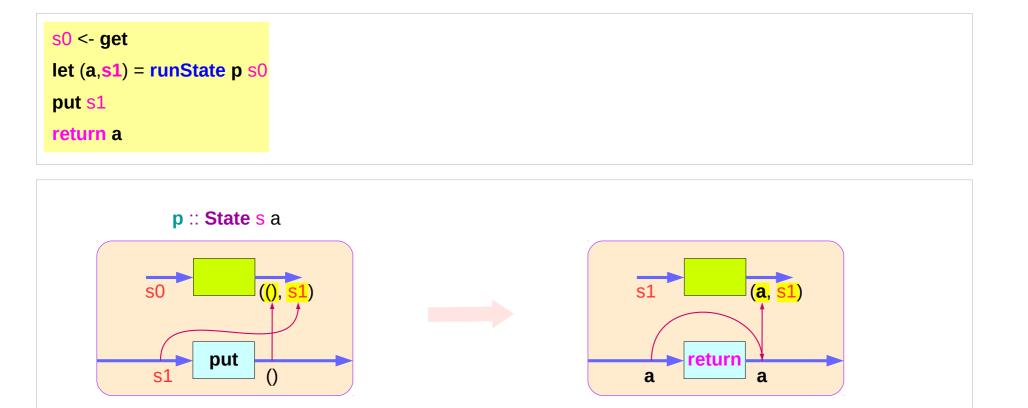
https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

Redundant computation examples (1)



https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

Redundant computation examples (2)



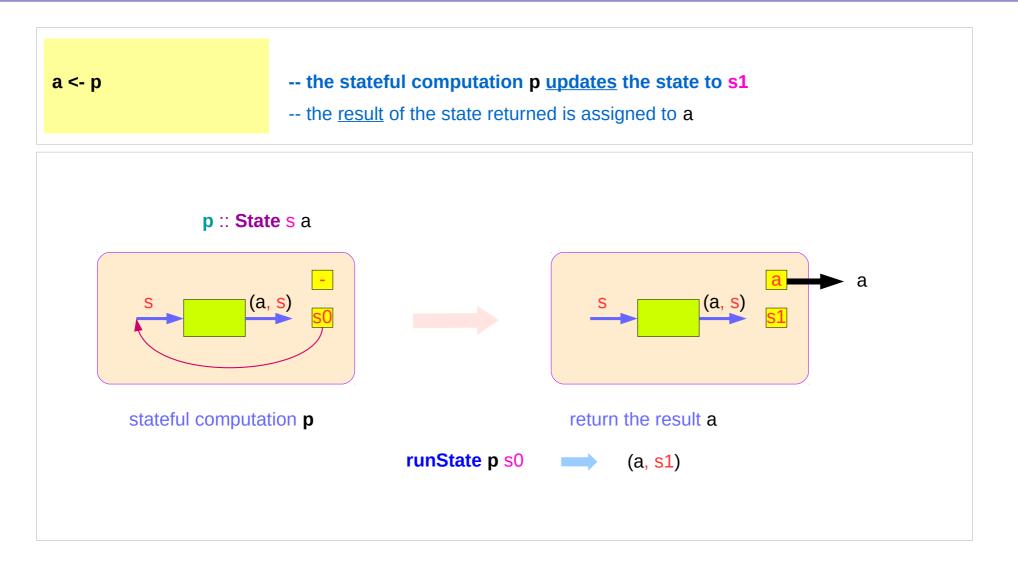
binded name (**a**, **s1**)

https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

put s1

return a

Redundant computation examples (3)



https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad	(6B)
Methods	

Counter Example

import Control.Monad.State.Lazy

tick :: State Int Int tick = do n <- get put (n+1) return n

plusOne :: Int -> Int
plusOne n = execState tick n

```
plus :: Int -> Int -> Int
```

plus n x = execState (sequence \$ replicate n tick) x

A function to increment a counter.

tick :

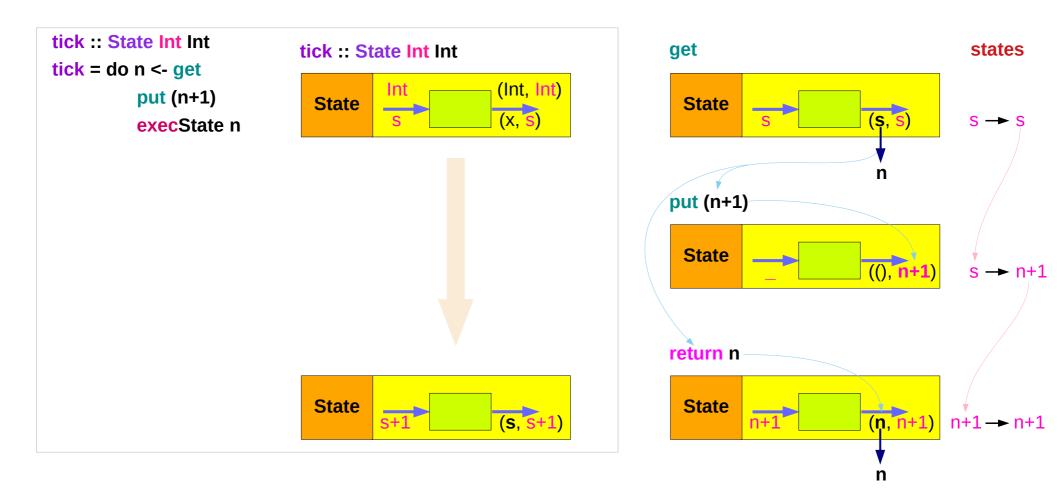
- a monadic value itself

- a function returning a monadic value-

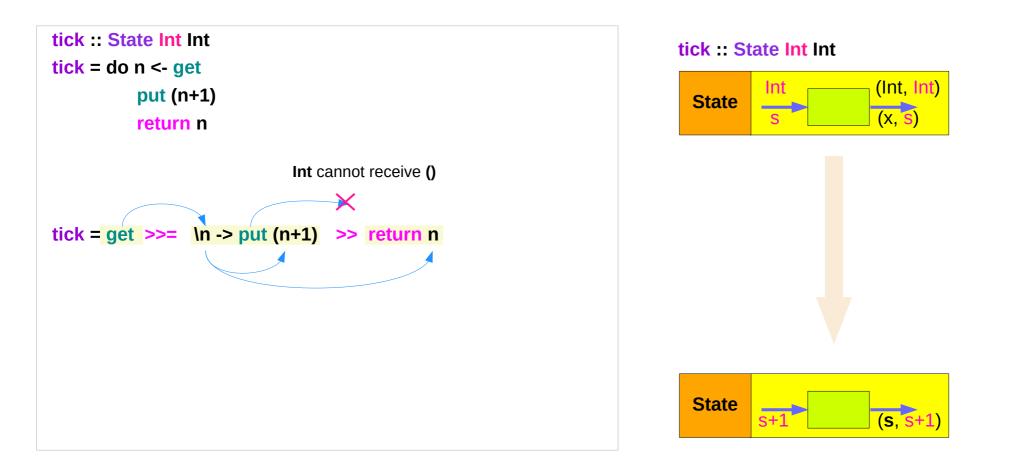
Add one to the given number using the state monad:

A contrived addition example. Works only with positive numbers:

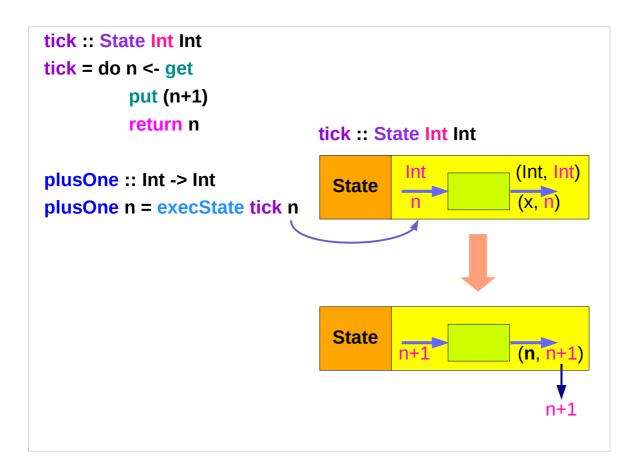
Counter Example – tick



Counter Example – tick without do



Counter Example – incrementing



Counter Example – using sequence

```
plus :: Int -> Int -> Int
plus n x = execState (sequence $ replicate n tick) x
             1
                  2
                         n
sequence $ [tick, tick, ... ,tick]
runState (sequence $ [tick, tick]) 3
                                          ([3,4],5)
runState (sequence $ [tick, tick, tick]) 3 ([3,4,5],6)
execState (sequence $ [tick, tick, tick]) 3
evalState (sequence $ [tick, tick, tick]) 3 
[3,4,5]
```

replicate

replicate :: Int -> a -> [a]

replicate n x is a list of length n with x the value of every element.

replicate 3 5

[5,5,5]

replicate 5 "aa"

["aa","aa","aa","aa","aa"]

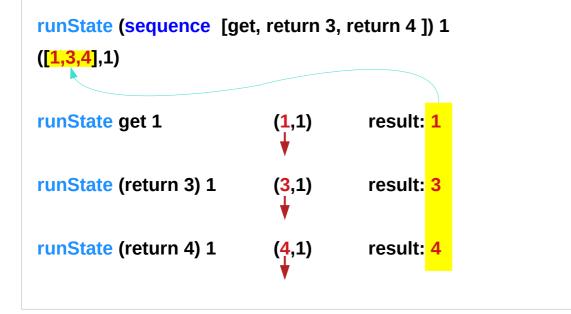
replicate 5 'a'

"aaaaa"

http://zvon.org/other/haskell/Outputprelude/replicate_f.html

sequence

sequence :: Monad m => [m a] -> m [a]
evaluate each action in the sequence from left to right,
and <u>collect</u> the results.

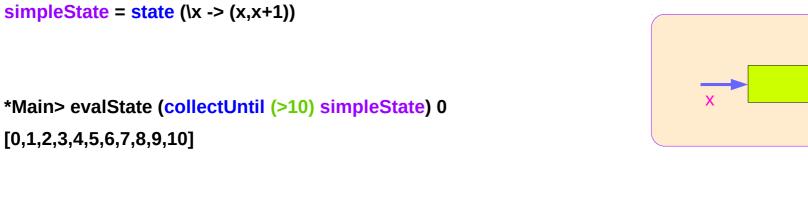


http://derekwyatt.org/2012/01/25/haskell-sequence-over-functions-explained/

Example of collecting returned values

ollectUntil f comp = do		comp :: State s a	
st <- <mark>get</mark>	Get the current state	st :: s	
if f st then return []	If it satisfies predicate, return		
else do	Otherwise		
x <- comp	Perform the computation s		
xs <- collectUntil f comp	Perform the rest of the computation	xs ::[a]	
return (x : xs)	Collect the results and return them		

simpleState :: State s a

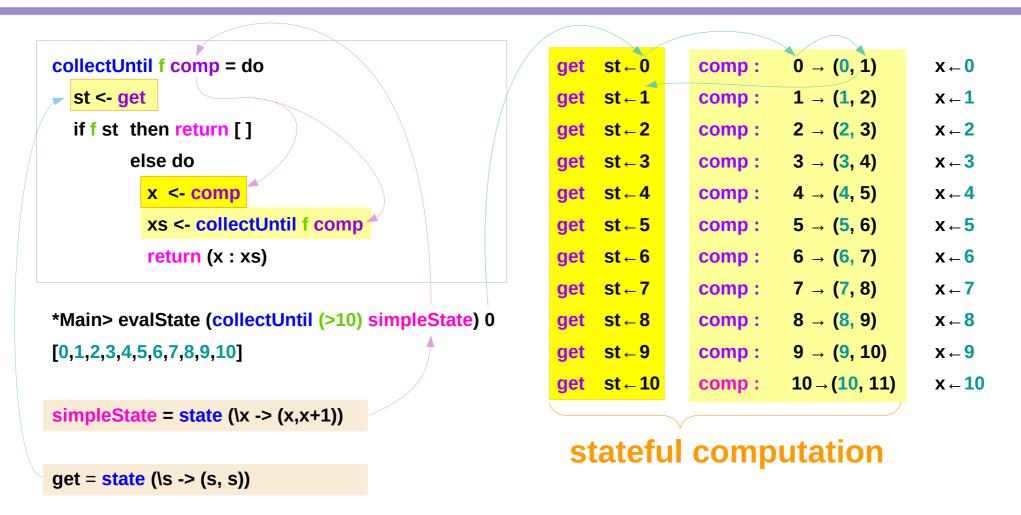


https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

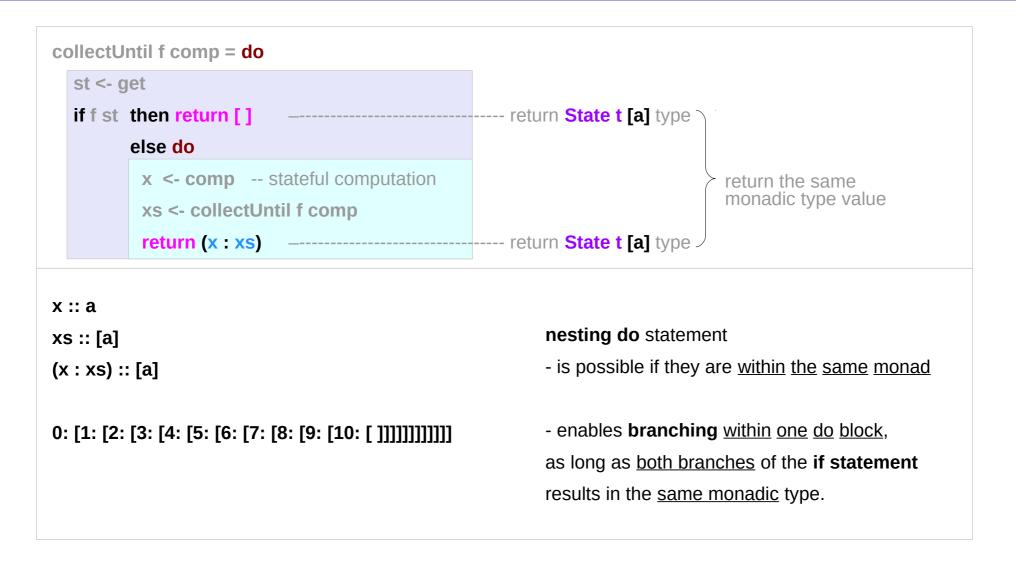
a s

(x, x+1)

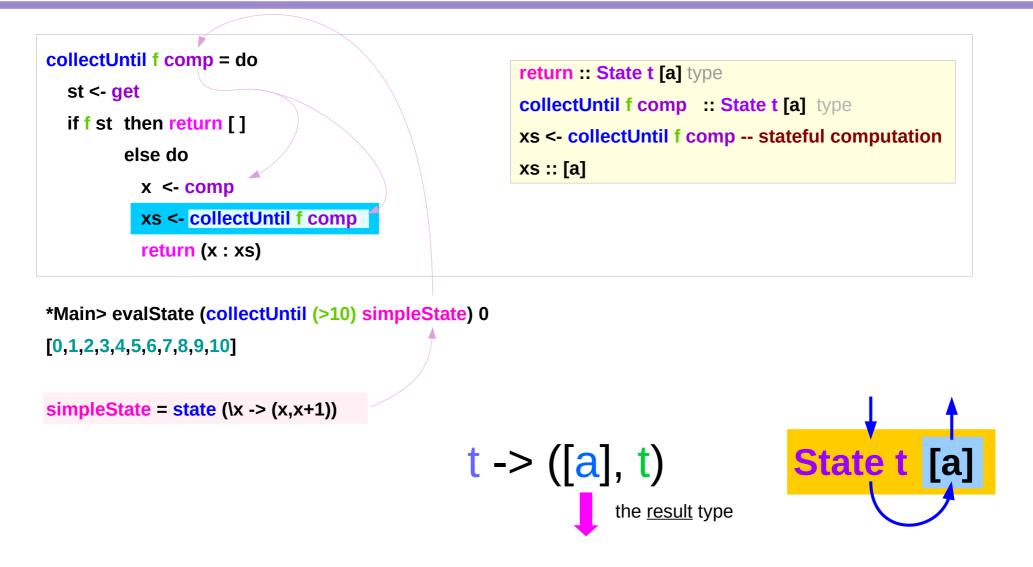
Example of collecting – stateful computations



Example of collecting – the return type



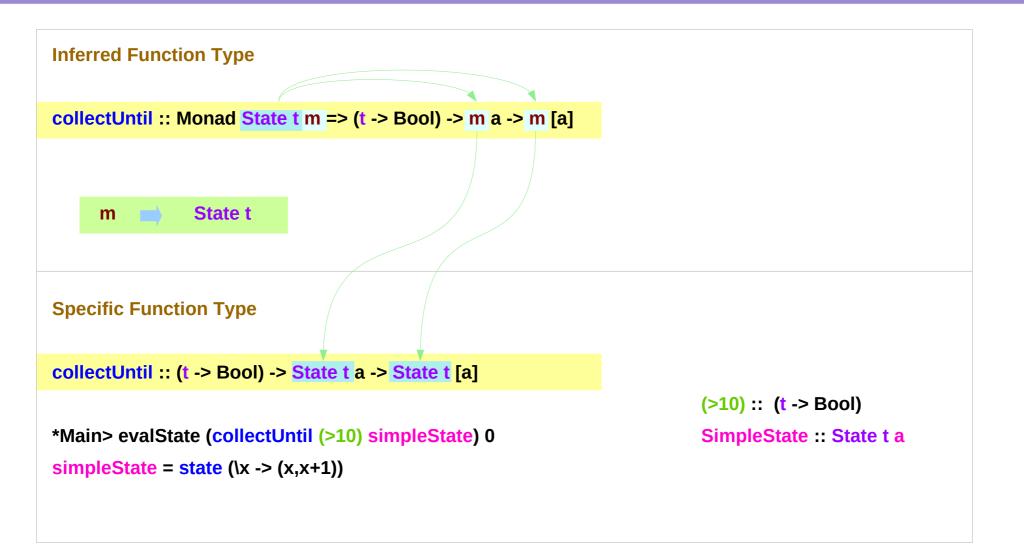
Example of collecting – another stateful compution



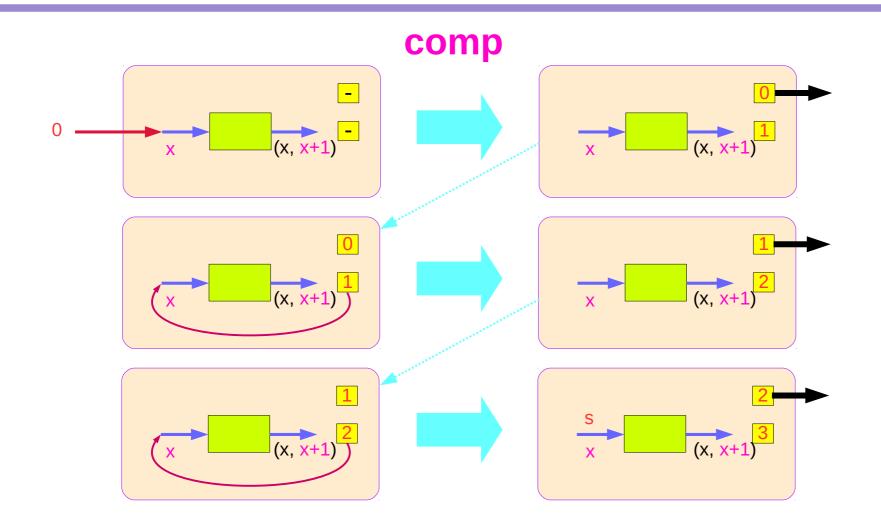
https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

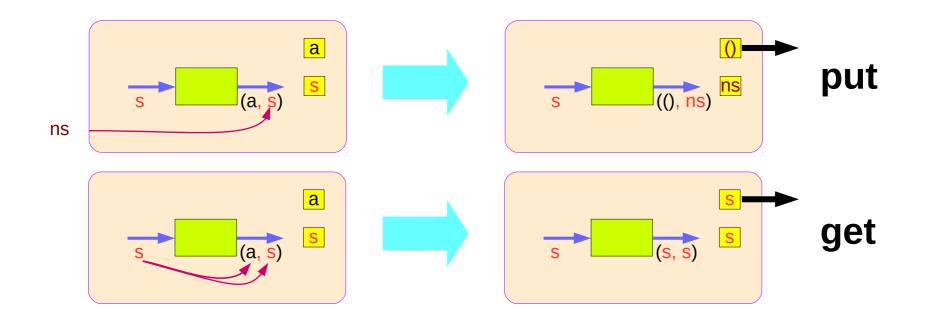
Example of collecting – the function type



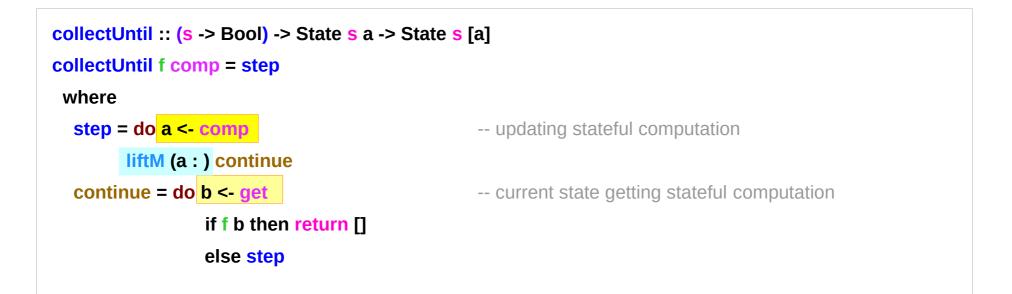
Stateful Computation of comp



Stateful Computations of put & get

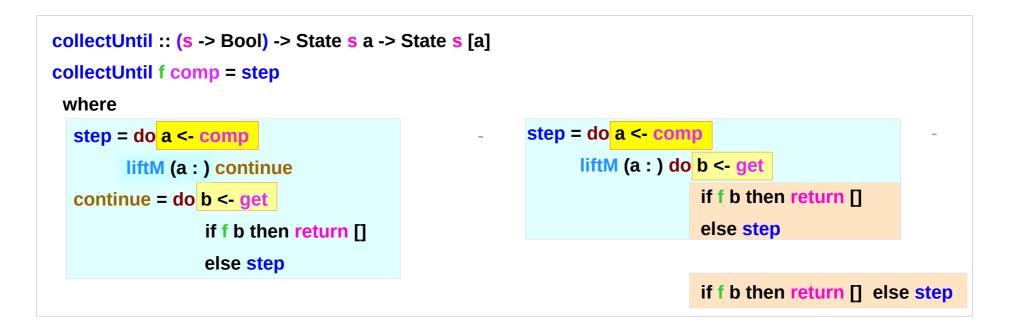


Another example of collecting returned values

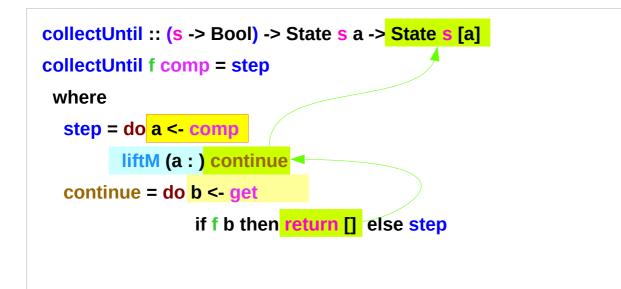


```
*Main> evalState (collectUntil (>10) simpleState) 0
[0,1,2,3,4,5,6,7,8,9,10]
simpleState = state (\x -> (x,x+1))
```

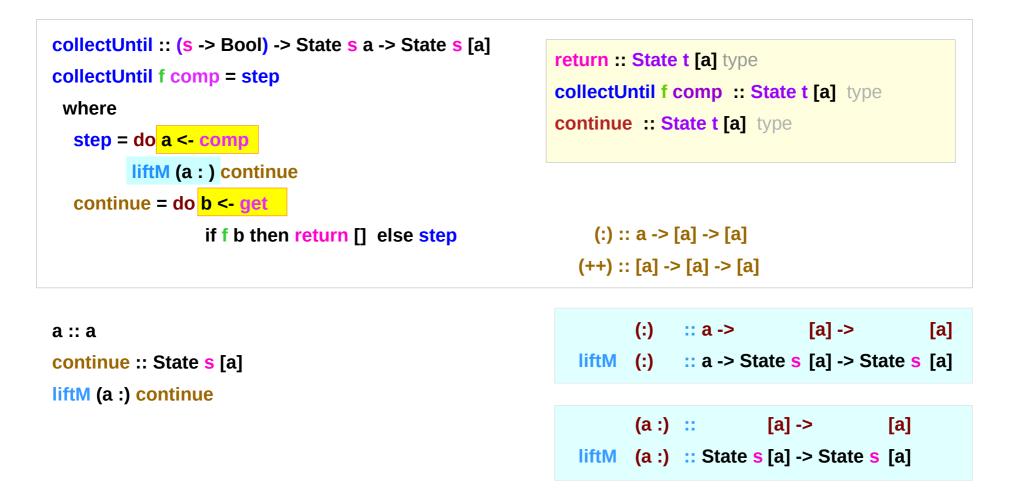
Another example of collecting – other representation



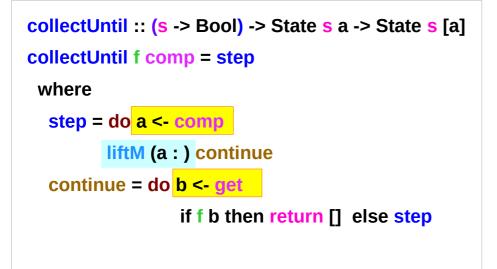
Another example of collecting – the return type



Another example of collecting – liftM to merge



Another example of collecting – stateful computations

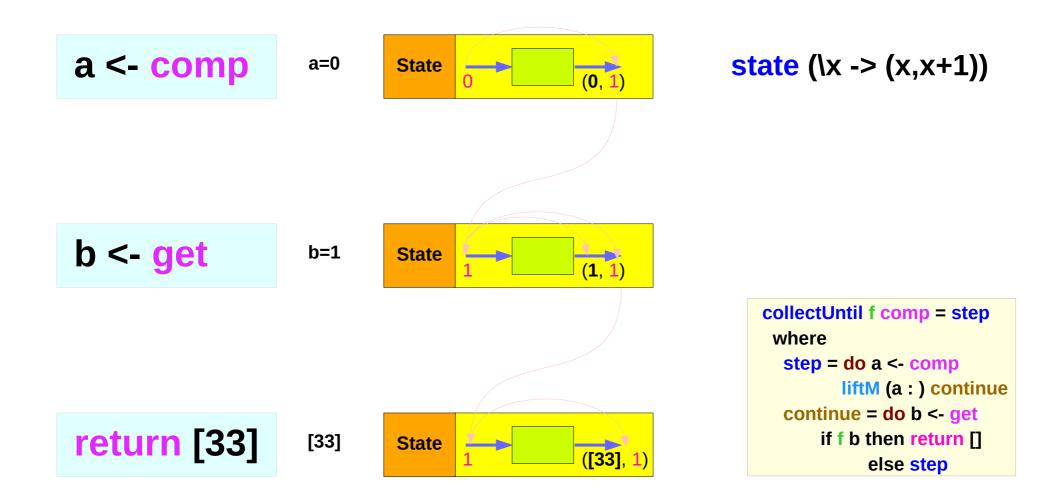


$comp: 0 \rightarrow (0, 1)$	a	get	b ← 1
comp : 1 → (1, 2)	a	get	<mark>b</mark> ← 2
comp : 2 → (2, 3)	a	get	<mark>b</mark>
comp : 3 → (3, 4)	a	get	<mark>b</mark>
comp : 4 → (4, 5)	a	get	<mark>b</mark> ← 5
comp : 5 → (5 , 6)	a	get	b
comp : 6 → (6, 7)	a	get	<mark>b</mark> ← 7
comp : 7 → (7, 8)	a	get	8 → d
comp : 8 → (8, 9)	a	get	<mark>b</mark> ← 9
comp : 9 → (9, 10)	a	get	<mark>b</mark>
comp : $10 \rightarrow (10, 11)$	a	get	<mark>b</mark> ← 11

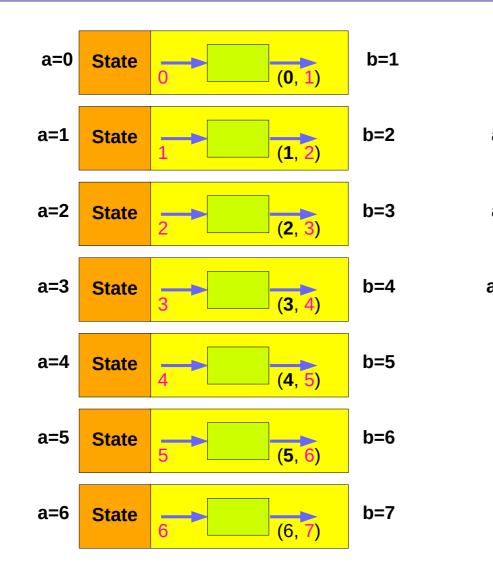
a <- comp b <- get return []

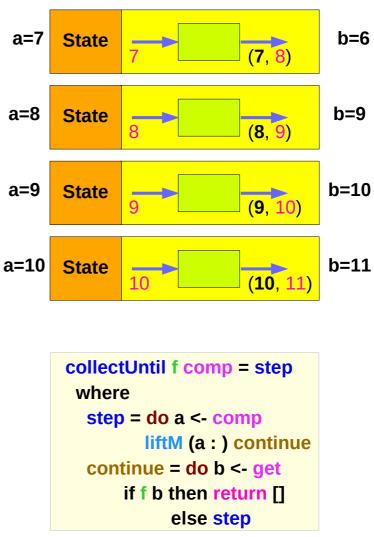
stateful computation

Another example of collecting – comp, get, return

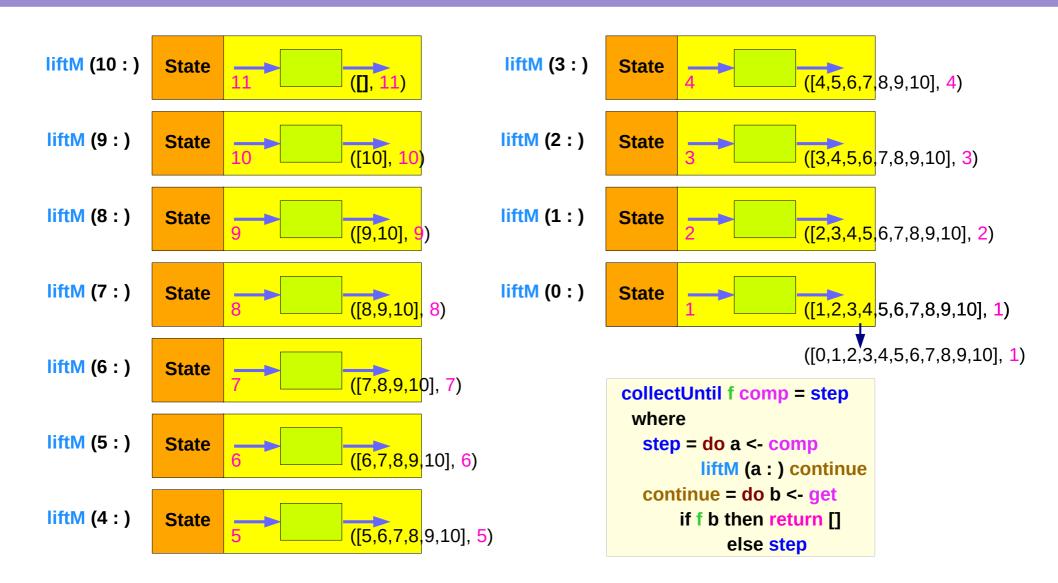


Another example of collecting – **a<-comp**, **b<-get**

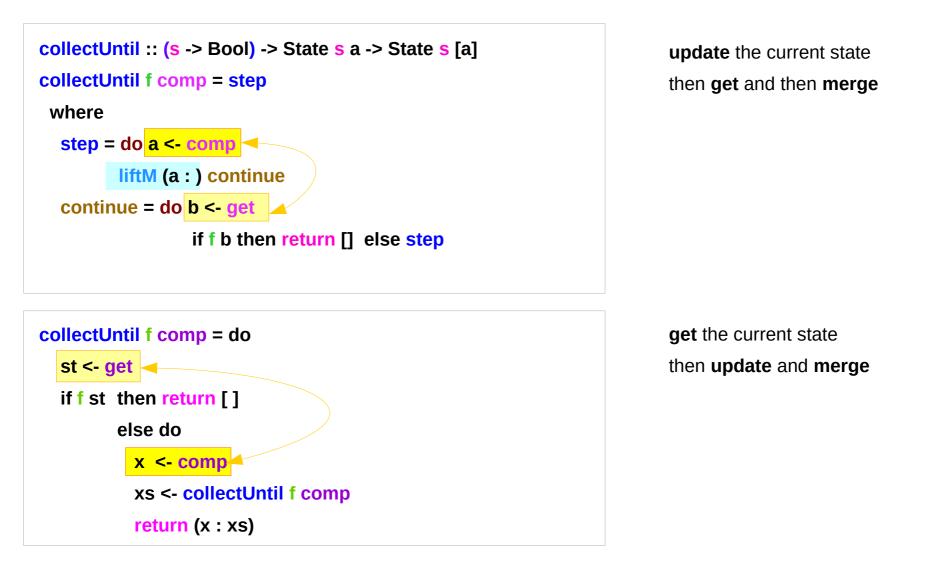




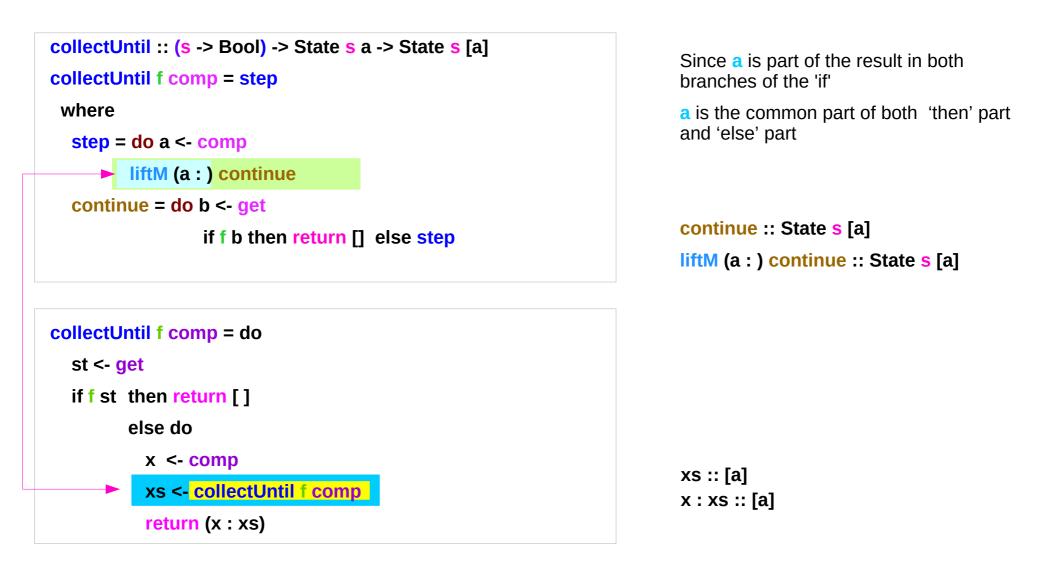
Another example of collecting – liftM (a:) continue



Another example of collecting – sequence comparison



Another example of collecting – merge comparison



Example of collecting – source codes

import Control.Monad.Trans.State	import Control.Monad.Trans.State
	import Control.Monad
collectUntil f comp = do	
st <- get	simpleState :: State Int Int
if f st then return []	simpleState = state \$ \x -> (x,x+1)
else do	
x <- comp	evalState (collectUntil (>10) simpleState) 0
xs <- collectUntil f comp	[0,1,2,3,4,5,6,7,8,9,10]
return (x : xs)	
	collectUntil :: (s -> Bool) -> State s a -> State s [a]
simpleState :: State Int Int	collectUntil f s = step
simpleState = state \$ \x -> (x,x+1)	where
	step = do a <- s
evalState (collectUntil (>10) simpleState) 0	liftM (a:) continue
[0,1,2,3,4,5,6,7,8,9,10]	continue = do s' <- get
	if f s'
	then return []
	else step

liftM and mapM

```
liftM :: (Monad m) => (a -> b) -> m a -> m b
mapM :: (Monad m) => (a -> m b) -> [a] -> m [b]
```

```
liftM lifts a function of type a -> b to a monadic counterpart.
mapM applies a function which yields a monadic value to a list of values,
    yielding list of results embedded in the monad.
```

```
> liftM (map toUpper) getLine
Hallo
"HALLO"
> :t mapM return "monad"
mapM return "monad" :: (Monad m) => m [Char]
```

https://stackoverflow.com/questions/5856709/what-is-the-difference-between-liftm-and-mapm-in-haskell

References

- [1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
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