

Search (4A)

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Graph Structures and Paths

```
edge(1,2).  
edge(1,4).  
edge(1,3).  
edge(2,3).  
edge(2,5).  
edge(3,4).  
edge(3,5).  
Edge(4,5).
```

```
edge(X,Y) :- edge(Y,X).
```

```
connected(X,Y) :- edge(X,Y) ; edge(Y,X).
```

```
connected(X,Y) :- edge(X,Y).
```

```
connected(X,Y) :- edge(Y,X).
```

Graph Structures and Paths

`path(A, B, Path) :-`

`travel(A, B, [A], Q),`

`reverse(Q, Path).`

`travel(A, B, P, [B|P]) :-`

`connected(A, B).`

`travel(A, B, Visited, Path) :-`

`connected(A, C),`

`C \== B,`

`\+member(C, Visited),`

`travel(C, B, [C|Visited], Path).`

`travel(A, B, [A], Q)`

`travel(A, B, P, [B|P])`

`travel(A, B, Visited, Path)`

`travel(C, B, [C|Visited], Path)`

Graph Structures and Paths

path(A, B, **Path**) :-

travel(A, B, [**A**], **Q**),

reverse(**Q**, **Path**).

travel(A, B, **P**, [**B|P**]) :-

connected(A, B).

travel(A, B, **Visited**, **Path**) :-

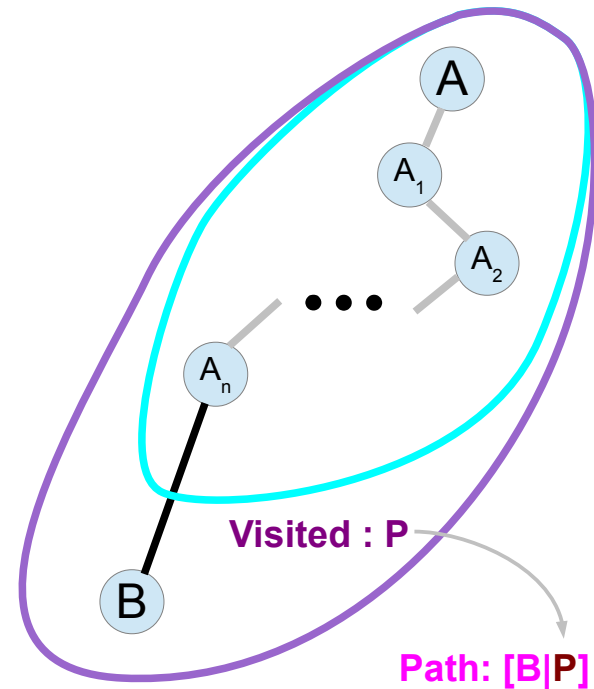
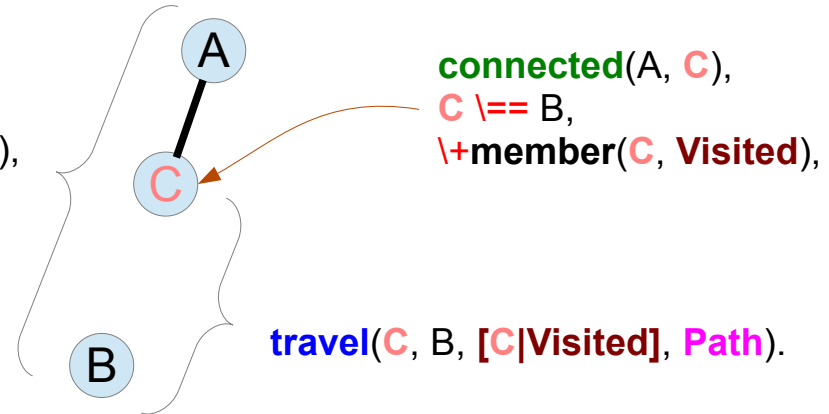
connected(A, **C**),

C \neq B,

\backslash +**member**(**C**, **Visited**),

travel(**C**, B, [**C|Visited**], **Path**).

travel(A, B, [**A**], **Q**),



Search

```
solve(P) :-  
  start(Start),  
  search(Start, [Start], Q),  
  reverse(Q, P).  
  ↓ ↑  
search(S, P, P) :- goal(S), !.      /* done      */  
  ↓ ↑  
search(S, Visited, P) :-  
  next_state(S, Nxt),                /* generate next state */  
  safe_state(Nxt), ↓                 /* check safety      */  
  no_loop(Nxt, Visited), ↑          /* check for loop    */  
  search(Nxt, [Nxt|Visited], P).     /* continue searching... */
```

Search

Start([]).

goal(S) :- length(S,8).

next_state(S, [C|S]) :-
member(C, [1,2,3,4,5,6,7,8]),
not member(C, S).

no_loop(Nxt, Visited) :-

\+member(Nxt, Visited).

Search

```

safe_state([C|S]) :-
    length(S,L),
    Sum is C+L+1,
    Diff is C-L-1,
    safe_state(S, Sum, Diff).

```

```

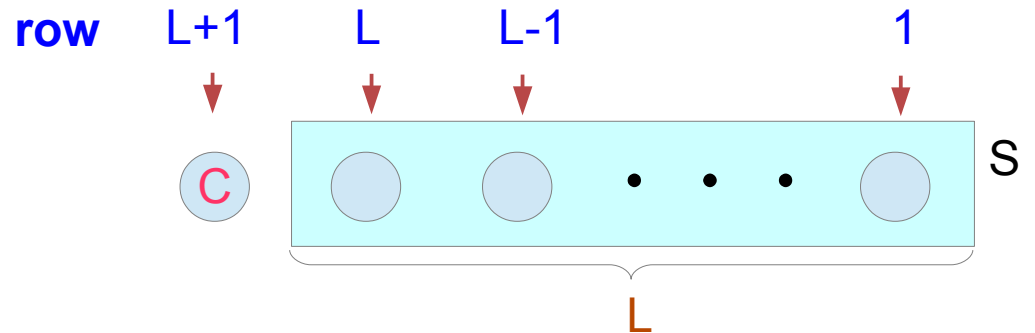
safe_state([],_,_) :- !.

```

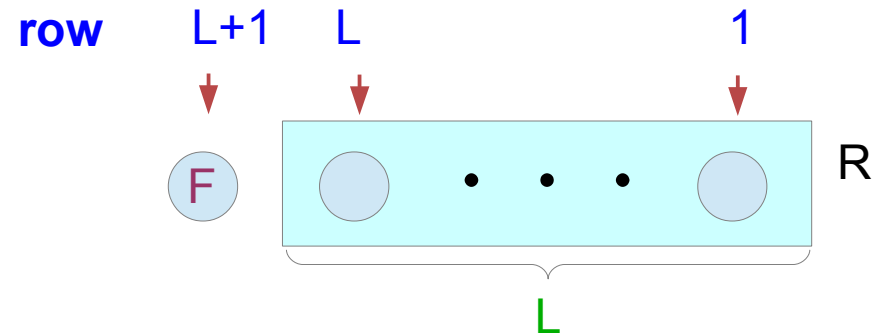
```

safe_state([F|R],Sm,Df) :-
    length(R,L),
    X is F+L+1,
    X \= Sm,
    Y is F-L-1,
    Y \= Df,
    safe_state(R, Sm, Df).

```



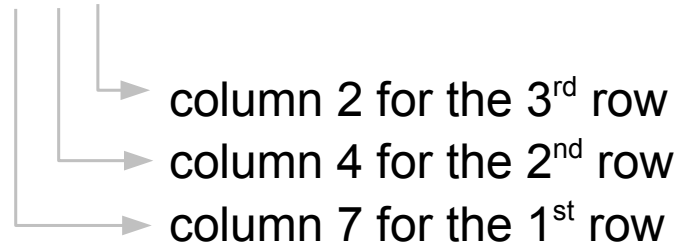
col + row: $C+L+1$
col - row: $C-L-1$



col + row: $F+L+1$
col - row: $F-L-1$

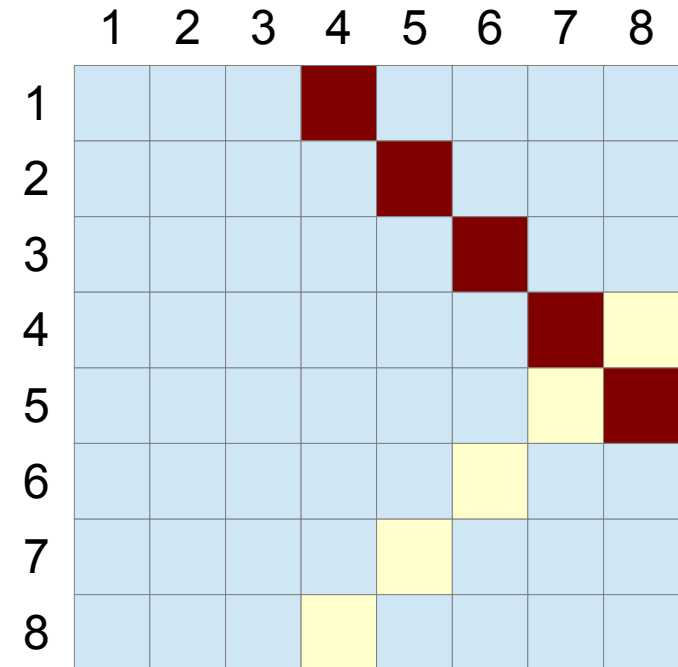
8 Queen Puzzle

$L=[7,4,2]$ already chosen for k rows (length $L = 3$)



$[C|L]$ choosing C for the 1st row

8 Queen Puzzle



□ on the same / diagonal iff
the **sum** of the row and column is the same

■ on the same \ diagonal iff
the **difference** of the row and column is the same

A* Algorithm

```
solve(Start,Soln) :- f_function(Start,0,F),
                    search([Start#0#F#[]],S),
                    reverse(S,Soln).
```

```
f_function(State,D,F) :- h_function(State,H),
                        F is D + H.
```

```
search([State#_#_#Soln | _], Soln) :- goal(State).
search([B|R],S) :- expand(B, Children),
                  insert_all(Children, R, NewOpen),
                  search(NewOpen,S).
```

```
expand(State#D#_#A, All_My_Children) :-
    bagof(Child#D1#F#[Move|A],
         ( D1 is D + 1,
           move(State,Child,Move),
           f_function(Child,D1,F) ),
         All_My_Children).
```

A* Algorithm

```
insert_all([F|R],Open1,Open3) :- insert(F,Open1,Open2),  
                                insert_all(R,Open2,Open3).
```

```
insert_all([],Open,Open).
```

```
insert(B,Open,Open) :- repeat_node(B,Open), ! .
```

```
insert(B,[C|R],[B,C|R]) :- cheaper(B,C), ! .
```

```
insert(B,[B1|R],[B1|S]) :- insert(B,R,S), ! .
```

```
insert(B,[],[B]).
```

```
repeat_node(P#_#_#_ , [P#_#_#_|_]).
```

```
cheaper( _#_#H1#_ , _#_#H2#_ ) :- H1 < H2.
```

References

- [1] en.wikipedia.org
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- [3] U. Endriss, "Lecture Notes : Introduction to Prolog Programming"
- [4] <http://www.learnprolognow.org/> Learn Prolog Now!
- [5] http://www.csupomona.edu/~jrfisher/www/prolog_tutorial
- [6] www.cse.unsw.edu.au/~billw/cs9414/notes/prolog/intro.html
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