

# Background – Expressions (1D)

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# Guard operator

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**patterns** are a way of making sure a **value** conforms to some **form** and **deconstructing** it

**guards** are a way of **testing** whether some **property** of a **value** (or several of them) are **true** or **false**.

<http://learnyouahaskell.com/syntax-in-functions>

# while and let bindings

**Where bindings** are a **syntactic construct** that let you **bind** to **variables** at the **end** of a function and the whole function can see them, including all the **guards**.

**Let bindings** are **expressions** themselves, let you bind to variables **anywhere**, but are very local, so they don't span across guards. Just like any construct in Haskell that is used to bind values to names, **let bindings** can be used for pattern matching.

<http://learnyouahaskell.com/syntax-in-functions>

# while bindings

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put the keyword **where** after the **guards**  
and define several **names** or **functions**.

all the **names** are aligned at a single column.

These names are visible across the **guards**  
and removes redundancy.

The **names** we define in the where section of a function  
are only visible to that function,  
the namespace of other functions are not contaminated.

**where** bindings aren't shared  
across **function bodies** of **different patterns**.  
If you want several patterns of one function  
to access some shared name, you have to define it **globally**.

You can also use where bindings to **pattern match!**

<http://learnyouahaskell.com/syntax-in-functions>

# let bindings

**let** <bindings> **in** <expression>

The **names** that you define in the **let** part are accessible to the expression after the **in** part.

the **names** are also aligned in a single column

**let** puts the bindings first and the **expression** that uses them later whereas **where** is the other way around.

**let** bindings are **expressions** themselves. **where** bindings are just **syntactic constructs**.

<http://learnyouahaskell.com/syntax-in-functions>

# case expression

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**case** expressions are, well, **expressions**,  
much like **if else expressions** and **let** bindings.

Not only can we evaluate **expressions**  
based on the possible cases of the value of a variable,  
we can also do **pattern matching**

taking a variable,  
pattern matching it,  
evaluating pieces of code based on its value,  
where have we heard this before?

pattern matching on parameters in function definitions!  
Well, that's actually just syntactic sugar for case expressions.

<http://learnyouahaskell.com/syntax-in-functions>

# guard as an expression

```
case () of  
  _ | a >= x    -> 1  
    | a == b    -> 333  
    | otherwise -> 5
```

guard as an expression

```
| a >= x    = 1  
| a == b    = 333  
| otherwise = 5
```

guard

```
if | a >= x    -> 1  
   | a == b    -> 333  
   | otherwise -> 5
```

multi-way if

using the **MultiWayIf** extension

<https://stackoverflow.com/questions/10370346/using-guards-in-let-in-expressions>

# Guard operator

**f x**

| **predicate1** = expression1

| **predicate2** = expression2

| **predicate3** = expression3

Examples)

**absolute x = if (x<0) then (-x) else x**

**absolute x**

| **x<0** = -x

| **otherwise** = x

no equals sign on the first line of the function definition  
but an equals sign after each guard.

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Guard operator – otherwise

The **otherwise** guard should always be last,  
it's like the default in a C switch statement.

**catch all guard**

more readable than **if/then/else**  
for more than two conditional cases

```
score :: Int -> String
```

```
score x
```

```
| x > 90 = show (x) ++ ": A"
```

```
| x > 80 = show (x) ++ ": B"
```

```
| x > 70 = show (x) ++ ": C"
```

```
| otherwise = show(x) ++ ": F"
```

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Guard operator – where

```
holeScore :: Int -> Int -> String
```

```
holeScore strokes par
```

```
| strokes < par      = show (par-strokes) ++ " under par"
```

```
| strokes == par    = "level par"
```

```
| strokes > par      = show(strokes-par) ++ " over par"
```

```
holeScore :: Int -> Int -> String
```

```
holeScore strokes par
```

```
| score < 0        = show (abs score) ++ " under par"
```

```
| score == 0       = "level par"
```

```
| otherwise        = show(score) ++ " over par"
```

```
where score = strokes-par
```

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Case expression

```
data Pet = Cat | Dog | Fish
```

```
hello :: Pet -> String
```

```
hello x =
```

```
case x of
```

```
  Cat  -> "meeow"
```

```
  Dog  -> "woof"
```

```
  Fish -> "bubble"
```

```
case x of
```

```
  pattern -> value
```

```
  pattern -> value
```

```
  pattern -> value
```

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Case expression – a pattern having a variable

```
data Pet = Cat | Dog | Fish | Parrot String
```

```
hello :: Pet -> String
```

```
hello x =
```

```
  case x of
```

```
    Cat  -> "meeow"
```

```
    Dog  -> "woof"
```

```
    Fish -> "bubble"
```

```
    Parrot name -> "pretty" + name
```

```
hello (Parrot "polly")
```

```
"pretty polly"
```

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Case expression – a default pattern

```
data Pet = Cat | Dog | Fish | Parrot String
```

```
hello :: Pet -> String
```

```
hello x =
```

```
  case x of
```

```
    Parrot name -> "pretty " ++ name
```

```
    _           -> "grunt"
```

<https://www.futurelearn.com/courses/functional-programming-haskell/0/steps/27226>

# Select expression

a function implemented in Haskell:

```
select :: a -> [(Bool, a)] -> a  
select def = maybe def snd . List.find fst  
  -- = fromMaybe def . lookup True  
  -- = maybe def id . lookup True
```

```
select exDefault  
  [(cond1, ex1),  
   (cond2, ex2),  
   (cond3, ex3)]
```

Unfortunately this function is not in the **Prelude**.  
It is however in the utility-ht package.

<https://wiki.haskell.org/Case>

# Advantages of **let**

P1

```
f :: s -> (a,s)
f x = y
  where y = ... x ...
```

P2

```
f :: State s a
f = State $ \x -> y
  where y = ... x ...
```

Using Control.Monad.State monad

P2 will not work, because **where** refers to the pattern matching `f =`, where no `x` is in scope.

with **let**, there is no problem.

P3

```
f :: s -> (a,s)
f x =
  let y = ... x ...
  in y
```

P4

```
f :: State s a
f = State $ \x ->
  let y = ... x ...
  in y
```

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

# Advantages of `while`

Because "`where`" blocks are bound to a syntactic construct, they can be used to share bindings between parts of a function that are not syntactically **expressions**.

```
f x
| cond1 x = a
| cond2 x = g a
| otherwise = f (h x a)
where
  a = w x
```

```
f x
= let a = w x
  in case () of
  _ | cond1 x -> a
  | cond2 x -> g a
  | otherwise -> f (h x a)
```

an expression style

```
f x =
  let a = w x
  in select (f (h x a))
    [(cond1 x, a),
     (cond2 x, g a)]
```

a functional equivalent:

```
f x =
  let a = w x
  in if cond1 x
     then a
     else if cond2 x
          then g a
          else f (h x a)
```

a series of if-then-else expressions:

these alternatives are arguably less readable and hide the structure of the function more than simply using `where`

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

# Lambda Lifting

**let** or **where** can often be implemented using **lambda lifting** and **let floating**, incurring at least the cost of introducing a new name.

```
f x
| cond1 x = a
| cond2 x = g a
| otherwise = f (h x a)
where
  a = w x
```

**a** : a free variable

```
f x = f' (w x) x
```

```
f' a x
| cond1 x = a
| cond2 x = g a
| otherwise = f (h x a)
```

**a** : an argument

**lambda lifting:**  
turning free variables  
into arguments

The auxiliary definition can either be a top-level binding, or included in f using **let** or **where**

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

# Let-floating transformation

let-floating transformations:

**floating inwards** moves bindings as far inwards as possible

**let x = y+1**

in case z of

□ -> x\*x

(p:ps) -> 1

case z of

□ -> **let x = y+1**

in x\*x

(p:ps) -> 1

the **full laziness** transformation floats selected bindings outside enclosing lambda abstractions

f = \xs -> letrec

g = \y -> let n = **length xs**

in ...g...n...

in ...g...

f = \xs -> let n = **length xs**

in letrec g = \y -> ...g...n...

in ...g...

**local transformations** fine-tune" the location of bindings

<https://www.microsoft.com/en-us/research/wp-content/uploads/1996/05/float.pdf>

# Eta Conversion

An **eta conversion** ( $\eta$ -conversion) is adding or dropping of **abstraction** over a function.

the following two values are equivalent under  $\eta$ -conversion:

$\lambda x \rightarrow \text{abs } x$

$\text{abs}$

an eta reduction

$\lambda x \rightarrow \text{abs } x \quad \rightarrow \quad \text{abs}$

an eta abstraction (expansion)

$\text{abs} \quad \rightarrow \quad \lambda x \rightarrow \text{abs } x$

Extensive use of  $\eta$ -reduction can lead to **Pointfree** programming.  
It is also typically used in certain **compile-time optimisations**.

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

# Eta Expansion

```
fib = (map fib' [0 ..] !!)
  where
    fib' 0 = 0
    fib' 1 = 1
    fib' n = fib (n - 1) + fib (n - 2)
```

```
fib x = map fib' [0 ..] !! x
  where
    fib' 0 = 0
    fib' 1 = 1
    fib' n = fib (n - 1) + fib (n - 2)
```

the second one runs considerably slower than the first.

You may wonder why simply adding an **explicit argument** to **fib** (known as **eta expansion**) degrades performance so dramatically.

In the first version

**fib'** is a **global constant** that never changes, and you're just indexing into that.

In the second version,

**fib** is a function that constructs a new and different **fib'** for every value of **x**.

```
Prelude> [11, 22, 33, 44, 55] !! 0
11
Prelude> [11, 22, 33, 44, 55] !! 1
22
Prelude> [11, 22, 33, 44, 55] !! 4
55
```

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

# Problems with where (2)

```
fib =  
  let fib' 0 = 0  
      fib' 1 = 1  
      fib' n = fib (n - 1) + fib (n - 2)  
  in (map fib' [0 ..] !!)
```

```
fib x =  
  let fib' 0 = 0  
      fib' 1 = 1  
      fib' n = fib (n - 1) + fib (n - 2)  
  in map fib' [0 ..] !! x
```

In the second case, **fib'** is redefined for every argument **x**  
The compiler cannot know whether you intended this –  
while it increases **time complexity** it may reduce **space complexity**.  
Thus it will not float the definition out from under the binding of **x**.

In contrast, in the first function, **fib'**  
can be moved to the top level by the compiler.  
The **where** clause hid this structure and made the application to **x**  
look like a plain **eta expansion**, which it is not.

[https://wiki.haskell.org/Let\\_vs.\\_Where](https://wiki.haskell.org/Let_vs._Where)

## References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>