

IO Monad (3C)

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Based on

[Haskell in 5 steps](https://wiki.haskell.org/Haskell_in_5_steps)

https://wiki.haskell.org/Haskell_in_5_steps

<https://www.schoolofhaskell.com/user/EFulmer/currying-and-partial-application>

<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

A Type Monad

Haskell does not have **states**

But its powerful type system enable to construct the **stateful** program flow

Defining a Monad type is like defining a class in an object oriented language

A Monad can do much more than a class:

A Monad is a type that can be used for

- exception handling**

- constructing **parallel program workflow**

- a **parser** generator

<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

Types: rules and data

types are the **rules** associated with the **data**, not the actual data itself.

Object-Oriented Programming enable us

- to use classes/interfaces

 - to define **types**,

 - the **rules (methods)** that interacts with the actual **data**.

- to use **templates**(c++) or **generics**(java)

 - to define more **abstracted rules** that are more reusable

Monad is pretty much like **generic class**.

<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

Monad Rules

A type is just a set of rules, or methods in Object-Oriented terms

A Monad is just yet another type, and the definition of this type is defined by four rules:

- 1) **bind** (`>>=`)
- 2) **then** (`>>`)
- 3) **return**
- 4) **fail**

<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

Monad Applications

1. Exception Handling
2. Accumulate States
3. IO Monad

<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

Monad Class Function >>= & >>

both >>= and >> are functions from the Monad class.

Monad Sequencing Operator with value passing

>>= **passes** the result of the expression on the left
as an argument to the expression on the right,
in a way that respects the context the argument and function use

Monad Sequencing Operator

>> is used to **order** the evaluation of expressions within some context;
it makes evaluation of the right depend on the evaluation of the left

<https://www.quora.com/What-do-the-symbols-and-mean-in-haskell>

Data Constructor

```
data Color = Red | Green | Blue
```

Color is a type

Red is a constructor that contains a value of type **Color**.

Green is a constructor that contains a value of type **Color**.

Blue is a constructor that contains a value of type **Color**.

```
data Color = RGB Int Int Int
```

Color is a type

RGB is not a value but a function taking three Ints and returning a value

```
RGB :: Int -> Int -> Int -> Colour
```

RGB is a **data constructor** that is a function taking three Int values as its arguments, and then uses them to construct a new value.

<https://stackoverflow.com/questions/18204308/haskell-type-vs-data-constructor>

Type Constructor (1)

Consider a binary tree to store **Strings**

```
data SBTree = Leaf String | Branch String SBTree SBTree
```

a type

SBTree is a type

Leaf is a **data constructor** (a function)

Branch is a **data constructor** (a function)

Leaf :: String -> **SBTree**

Branch :: String -> **SBTree** -> **SBTree** -> **SBTree**

Consider a binary tree to store **Bool**

```
data BBTree = Leaf Bool | Branch Bool BBTree BBTree
```

<https://stackoverflow.com/questions/18204308/haskell-type-vs-data-constructor>

Type Constructor (2)

Type constructors

Both **SBTree** and **BBTree** are type constructors

```
data SBTree = Leaf String | Branch String SBTree SBTree
```

```
data BBTree = Leaf Bool | Branch Bool BBTree BBTree
```

```
data BTree a = Leaf a | Branch a (BTree a) (BTree a)
```

Now we introduce a type variable `a` as a parameter to the type constructor.

BTree has become a function.

It takes a type as its argument and it returns a new `tUype`.

<https://stackoverflow.com/questions/18204308/haskell-type-vs-data-constructor>

Monad Definition

A **monad** is defined by

```
a type constructor m;  
a function return;  
an operator (>>=) "bind"
```

The function and operator are methods of the Monad type class and have types

```
return :: a -> m a
```

```
(>>=) :: m a -> (a -> m b) -> m b
```

and are required to obey three laws

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Monad Definition

```
class Monad m where
  return :: a -> m a

  (>>=) :: m a -> (a -> m b) -> m b

  (>>) :: m a -> m b -> m b
  x >> y = x >>= \_ -> y

  fail :: String -> m a
  fail msg = error msg
```

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Maybe Monad

the Maybe monad.

The type constructor is $m = \text{Maybe}$,

$\text{return} :: a \rightarrow \text{Maybe } a$

$\text{return } x = \text{Just } x$

$(\gg=) :: \text{Maybe } a \rightarrow (a \rightarrow \text{Maybe } b) \rightarrow \text{Maybe } b$

$m \gg= g = \text{case } m \text{ of}$
 Nothing \rightarrow Nothing
 Just $x \rightarrow g x$

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Monad Class Function $\gg=$ & \gg

Maybe is the monad
return brings a value into it
by wrapping it with **Just**

$\gg=$ takes

a value $m :: \text{Maybe } a$

a function $g :: a \rightarrow \text{Maybe } b$

if m is **Nothing**,

there is nothing to do and the result is **Nothing**.

Otherwise, in the **Just** x case,

the underlying value x is wrapped in **Just**

g is applied to x , to give a **Maybe** b result.

Note that this result *may* or *may not* be **Nothing**,
depending on what g does to x .

```
(\gg=) :: Maybe a -> (a -> Maybe b) -> Maybe b
m \gg= g = case m of
  Nothing -> Nothing
  Just x   -> g x
```

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Monad Class Function $>>=$ & $>>$

```
(>>=) :: Maybe a -> (a -> Maybe b) -> Maybe b
m >>= g = case m of
    Nothing -> Nothing
    Just x   -> g x
```

if there is an underlying value of type a in m ,
we apply g to it, which brings the underlying value back into the **Maybe** monad.

The key first step to understand how `return` and `(>>=)` work is tracking
which values and arguments are monadic and
which ones aren't.

As in so many other cases, type signatures are our guide to the process.

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Maybe Monad Examples

a family database that provides two functions:

father :: Person -> **Maybe** Person

mother :: Person -> **Maybe** Person

Input the name of someone's father or mother.

If some relevant information is missing in the database

Maybe returns a **Nothing** value
to indicate that the lookup failed,
rather than crashing the program.

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Maybe Monad Examples

functions to query various grandparents.

the following function looks up the maternal grandfather (the father of one's mother):

```
maternalGrandfather :: Person -> Maybe Person
maternalGrandfather p =
  case mother p of
    Nothing -> Nothing
    Just mom -> father mom
```

```
maternalGrandfather p = mother p >>= father
```

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

Maybe Monad Examples

https://en.wikibooks.org/wiki/Haskell/Understanding_monads

```
bothGrandfathers :: Person -> Maybe (Person, Person)
```

```
bothGrandfathers p =
```

```
case father p of
```

```
  Nothing -> Nothing
```

```
  Just dad ->
```

```
    case father dad of
```

```
      Nothing -> Nothing
```

```
      Just gf1 -> -- found first grandfather
```

```
    case mother p of
```

```
      Nothing -> Nothing
```

```
      Just mom ->
```

```
        case father mom of
```

```
          Nothing -> Nothing
```

```
          Just gf2 -> -- found second grandfather
```

```
          Just (gf1, gf2)
```

```
bothGrandfathers p =
```

```
  father p >>=
```

```
    (\dad -> father dad >>=
```

```
      (\gf1 -> mother p >>= -- gf1 is only used in the final return
```

```
        (\mom -> father mom >>=
```

```
          (\gf2 -> return (gf1, gf2) ))))
```

Maybe Monad Examples

```
data Maybe a = Just a  
             | Nothing
```

a type definition: **Maybe a**

a parameter of a type variable a,

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe Monad Examples

```
data Maybe a = Just a
              | Nothing
```

two constructors: **Just a** and **Nothing**

a value of **Maybe a** type must be constructed via either **Just** or **Nothing**
there are no other (non-error) possibilities.

Nothing has no parameter type,
names a constant value that is a member of type **Maybe a** for all types **a**.

Just constructor has a type parameter,
acts like a function from type **a** to **Maybe a**,
i.e. it has the type **a -> Maybe a**

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe Monad Examples

the (data) constructors of a type build a value of that type;

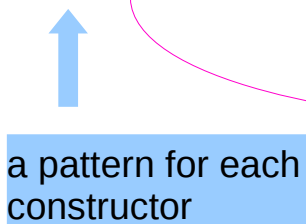
when using that value,
pattern matching can be applied

- Unlike functions, constructors can be used in pattern binding expressions
- **case analysis** of values that belong to types with **more than one constructor**.
- need to provide **a pattern** for each constructor

case maybeVal **of**

```
Nothing -> "There is nothing!"  
Just val -> "There is a value, and it is " ++ (show val)
```

a pattern for each
constructor



<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe

Maybe : Algebraic Data Type (ADT)

Widely used because it effectively extends a type

Integer into a new context in which it has an extra value (Nothing)
that represents a lack of value

Check for that extra value before accessing the possible Integer

Good for debugging

Many other languages have this sort of "no-value" value via NULL references.

The Haskell Maybe type handle this no-value more effectively.

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe as a functor

Functor type class:

- transforming one type to another
- transforming operations of one type to those of another

Maybe has a useful instance of a **functor** type class

Functor provides **fmap** method

maps functions of the *base type* (such as *Integer*)
to *functions* of the *lifted type* (such as *Maybe Integer*).

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe as a functor

A *function* `f` transformed with `fmap`
can work on a Maybe value

case maybeVal of

```
Nothing -> Nothing    -- there is nothing, so just return Nothing
Just val -> Just (f val) -- there is a value, so apply the function to it
```

```
father :: Person -> Maybe Person
mother :: Person -> Maybe Person
```

```
f :: Int -> Int
fmap f :: Maybe Integer -> Maybe Integer
```

a **Maybe Integer** value: `m_x`

```
fmap f m_x
```

In fact, you could apply a whole chain of

lifted Integer -> Integer functions to **Maybe Integer** values

and only have to worry about explicitly checking for **Nothing** once when you're finished.
<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe as a functor

In fact, you could apply a whole chain of **lifted Integer -> Integer** functions to **Maybe Integer** values and only have to worry about explicitly checking for **Nothing** once when you're finished.

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Maybe as a monad

the type signature **IO a** looks remarkably similar to **Maybe a**.

- IO doesn't expose its constructors
- only be "run" by the Haskell runtime system
- a Functor
- a Monad

a Monad is just a special kind of Functor with some extra features

Monads like **IO** *map* types to new types
that represent "computations that result in values"

Can *lift* **functions** into **Monad types**
via a very fmap-like function called **liftM**
that turns a regular function into a
"computation that results in the value obtained by evaluating the function."

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Maybe as a monad

Maybe is also a Monad
represents "computations that could fail to return a value"

Just like with the fmap example,
this lets you do a whole bunch of computations
without having to explicitly check for errors after each step.

And in fact, the way the Monad instance is constructed,
a computation on Maybe values stops as soon as a Nothing is encountered,

an immediate abort or
a valueless return
in the middle of a computation.

<https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell>

Monad – List Comprehension Examples

```
[x*2 | x<-[1..10], odd x]
```

```
do
  x <- [1..10]
  if odd x
    then [x*2]
    else []
```

```
[1..10] >>= (\x -> if odd x then [x*2] else [])
```

<https://stackoverflow.com/questions/44965/what-is-a-monad>

Monad – I/O Examples

```
do
  putStrLn "What is your name?"
  name <- getLine
  putStrLn ("Welcome, " ++ name ++ "!!")
```

<https://stackoverflow.com/questions/44965/what-is-a-monad>

Monad – A Parser Example

```
parseExpr = parseString <|> parseNumber
```

```
parseString = do  
  char ""  
  x <- many (noneOf "\"")  
  char ""  
  return (StringValue x)
```

```
parseNumber = do  
  num <- many1 digit  
  return (NumberValue (read num))
```

<https://stackoverflow.com/questions/44965/what-is-a-monad>

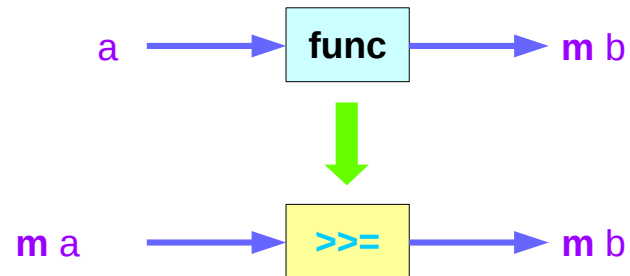
Monad – Asynchronous Examples

```
let AsyncHttp(url:string) =  
    async { let req = WebRequest.Create(url)  
            let! rsp = req.GetResponseAsync()  
            use stream = rsp.GetResponseStream()  
            use reader = new System.IO.StreamReader(stream)  
            return reader.ReadToEnd() }
```

<https://stackoverflow.com/questions/44965/what-is-a-monad>

Monad – Asynchronous Examples

```
class Monad m where  
  (>>=) :: m a -> (a -> m b) -> m b
```



<http://www.idryman.org/blog/2014/01/23/yet-another-monad-tutorial/>

References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>