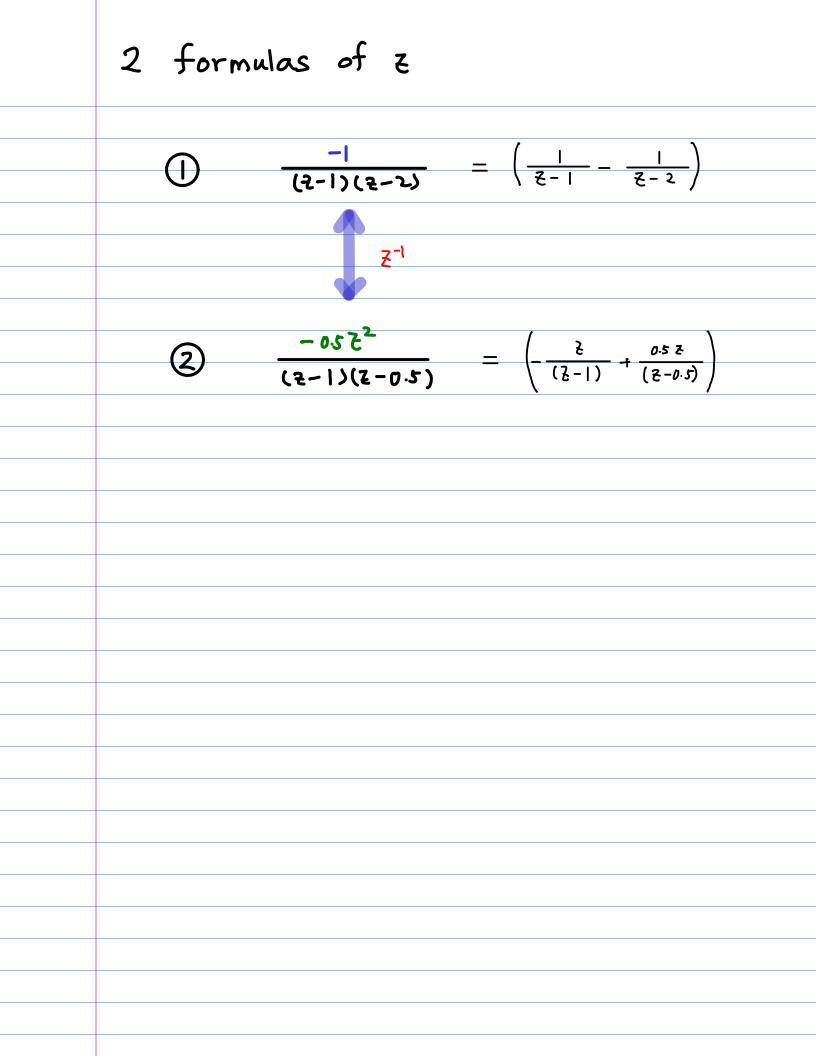
Laurent Series and z-Transform	
- Geometric Series	
Double Pole Examples B	

20180220

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$$\frac{-1}{(2-1)(2-2)} = \left(\frac{1}{(2-1)(2-0.5)}\right)$$

$$\frac{-1}{(2-1)(2-2)} = \left(\frac{1}{(2-1)(2-0.5)}\right)$$

$$\frac{-1}{(2-1)(2-2)} = \left(\frac{1}{(2-1)} - \frac{1}{(2-2)}\right)$$

$$= \left(\frac{1}{(2-1)(2-2)}\right)$$

$$= \left(\frac{1}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-2}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-2}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-2}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-32}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-32}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-32}{(2-1)(2-2)}\right)$$

$$= \left(\frac{-32}{(2-1)(2-2)}\right)$$

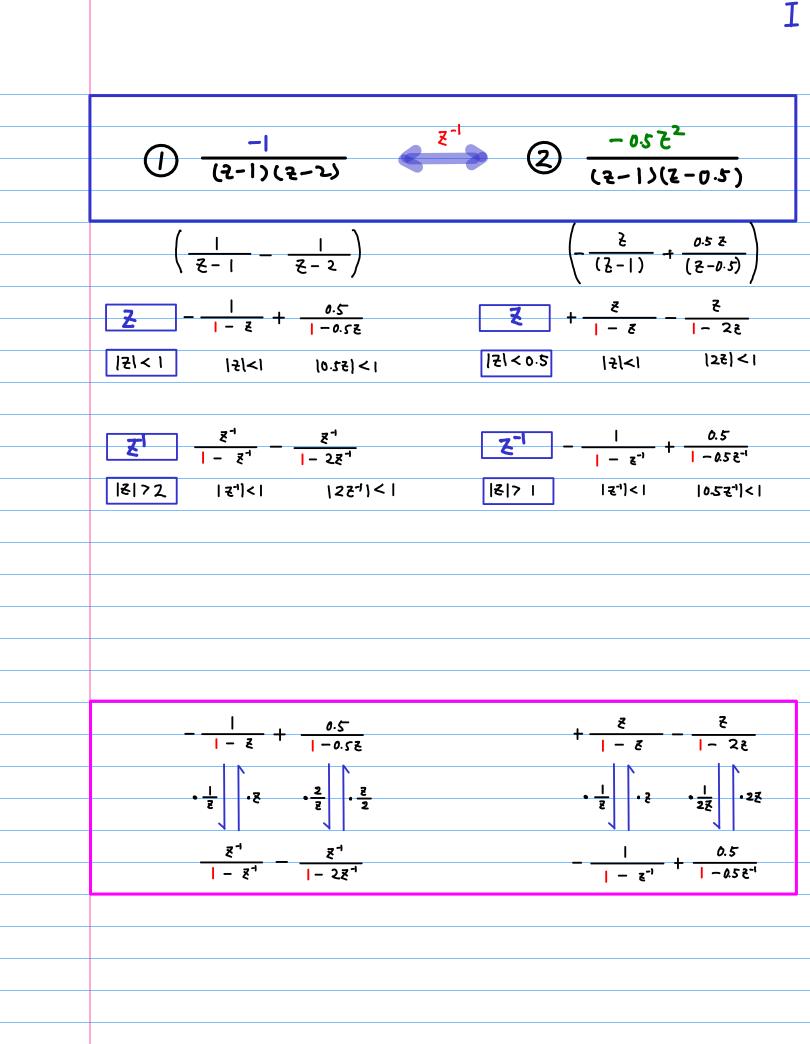
(A) f(z) (B) X(z)

 $(I) \qquad \frac{-1}{(2-1)(2-2)} = \left(\frac{1}{2-1} - \frac{1}{2-2}\right)$ (1 - 4) - (1[(2) $|z| > 2 \qquad f(z) = \frac{z^{-1}}{1-z^{-1}} - \frac{z^{-1}}{1-2z^{-1}} + |z|^{n+1} - (\frac{1}{2})^{n+1} \quad (n < 0)$ $(1 - B) |\xi| < | \qquad \chi(\xi) = -\frac{1}{1 - \xi} + \frac{0.5}{1 - 0.5\xi} - \frac{1^{n-1}}{1 + 2^{n-1}} (n < 1)$ $\frac{\chi(z)}{|z| > 2} \qquad \chi(z) = \frac{z^{-1}}{1 - z^{-1}} - \frac{z^{-1}}{1 - 2z^{-1}} + \frac{|z|^{-1}}{|z|^{-1}} - \frac{|z|^{-1}}{|z|^{-1}}$ $(2) \quad \frac{-0.5 \, z^2}{(z-1)(z-0.5)} = \left(-\frac{z}{(z-1)} + \frac{0.5 \, z}{(z-0.5)}\right)$ 2-A $|\xi| < |$ $f(\xi) = + \frac{\xi}{|-\xi|} - \frac{\xi}{|-\xi|} |^{n-1} - 2^{n-1} (n \ge 1)$ $\frac{f(2)}{|\xi| > 2} \quad \frac{f(2)}{|\xi| > 2} \quad -\frac{|}{|-\epsilon^{-1}|} + \frac{0.5}{|-0.5\epsilon^{-1}|} \quad -|^{n-1} + 2^{n-1} \quad (n < |)$ $2 - B |\xi| < | X(\xi) = + \frac{\xi}{|-\xi|} - \frac{\xi}{|-\xi|} + ||^{n+1} - (\frac{1}{2})^{n+1} (n < 0)$ $\frac{\chi(5)}{|5| > 2} \qquad \chi(5) = -\frac{1}{1 - \epsilon^{-1}} + \frac{0.5}{1 - 0.5\epsilon^{-1}} - |\frac{1}{1 + (\frac{1}{2})^{n+1}} \quad (1) \ge 0)$

$$\frac{\left|\begin{array}{c} 0\right|}{\left(\frac{1}{2}-1\right)\left(\frac{1}{2}-2\right)} & \left(\begin{array}{c} 0\\ \frac{1}{2}-1\right)\left(\frac{1}{2}-2\right)} \\ \hline 0\\ \frac{1}{\left(\frac{1}{2}-1\right)\left(\frac{1}{2}-2\right)} \\ \hline$$

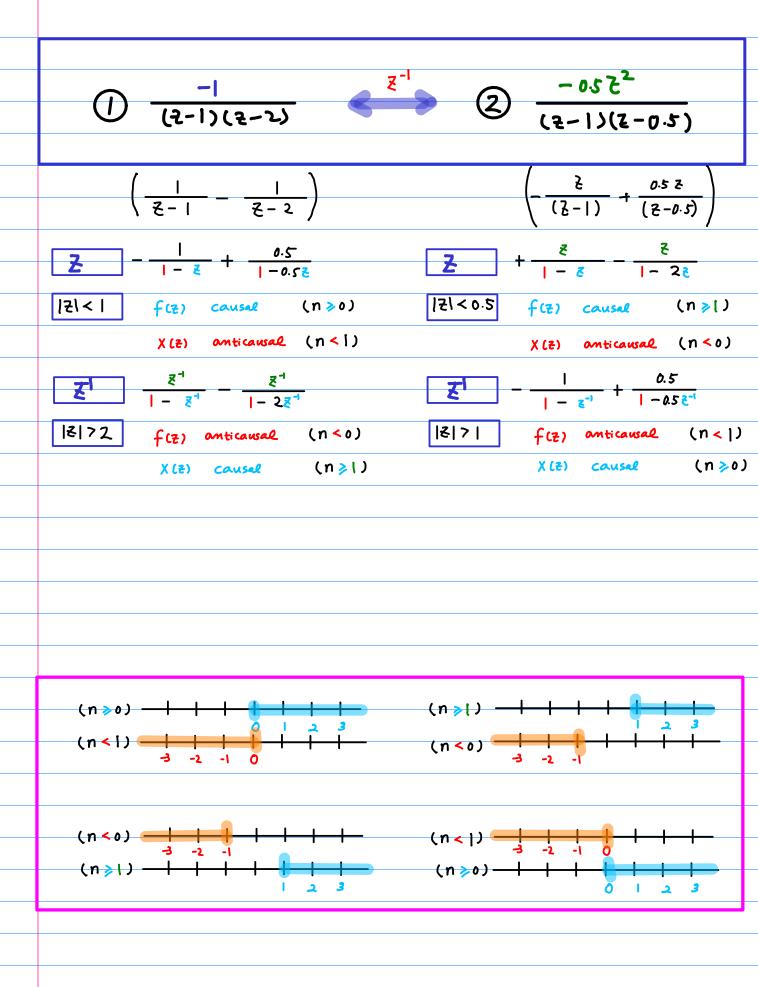
		$\frac{-1}{(2-1)(2-2)}$	$2 \frac{-0.52^{2}}{(2-1)(2-0.5)}$
 z <	f(z)	<u>causal (n≯o)</u>	causal (n>1)
2 > 2	f(2)	anticansal (n <o)< th=""><th>anticansal (n<1)</th></o)<>	anticansal (n<1)
 2 <	X(Z)	Anticansal (n<1)	Anticansal (n<0)
2 > 2	X(Z)	causal (n>1)	causal (n>o)

		() - (2-1)(2-2)	$2 \frac{-0.52^{2}}{(2-1)(2-0.5)}$
2 <	f(z)	<u>causal (n≯o)</u>	causal (nzi)
2 <	X(Z)	articansal (n<1)	anticansal (n <o)< th=""></o)<>
2 > 2	f(z)	Anticansal (n <o)< th=""><th>anticansal (N<1)</th></o)<>	anticansal (N<1)
2 > 2	X(Z)	causal (nzi)	causal (nzo)

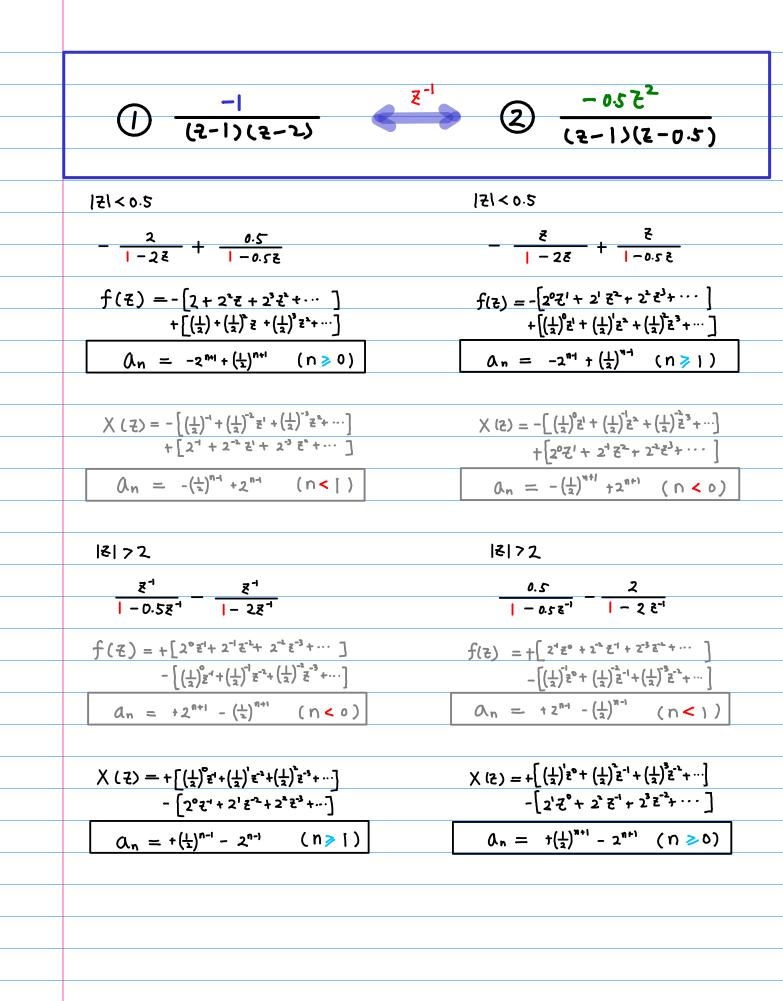


 $\left(-\frac{2}{(2-1)}+\frac{0.5 z}{(2-0.5)}\right)$ $\left(\frac{1}{\xi-1}-\frac{1}{\xi-2}\right)$ $\frac{2}{1-z} - \frac{1}{1-z} + \frac{0.5}{1-0.5z}$ $\frac{2}{1-z} + \frac{z}{1-z} - \frac{z}{1-2z}$ [21<] f(2) causal (n≥0) [Z\<0.5 f(Z) causal (n≥[) $\boxed{\frac{z^{-1}}{1-z^{-1}}} - \frac{z^{-1}}{1-2z^{-1}} - \frac{z^{-1}}{1-z^{-1}} + \frac{0.5}{1-0.5z^{-1}}$ 18172 |そ| 7 | X(Z) causal (n>1) X(z) causal $(n \ge 0)$

I

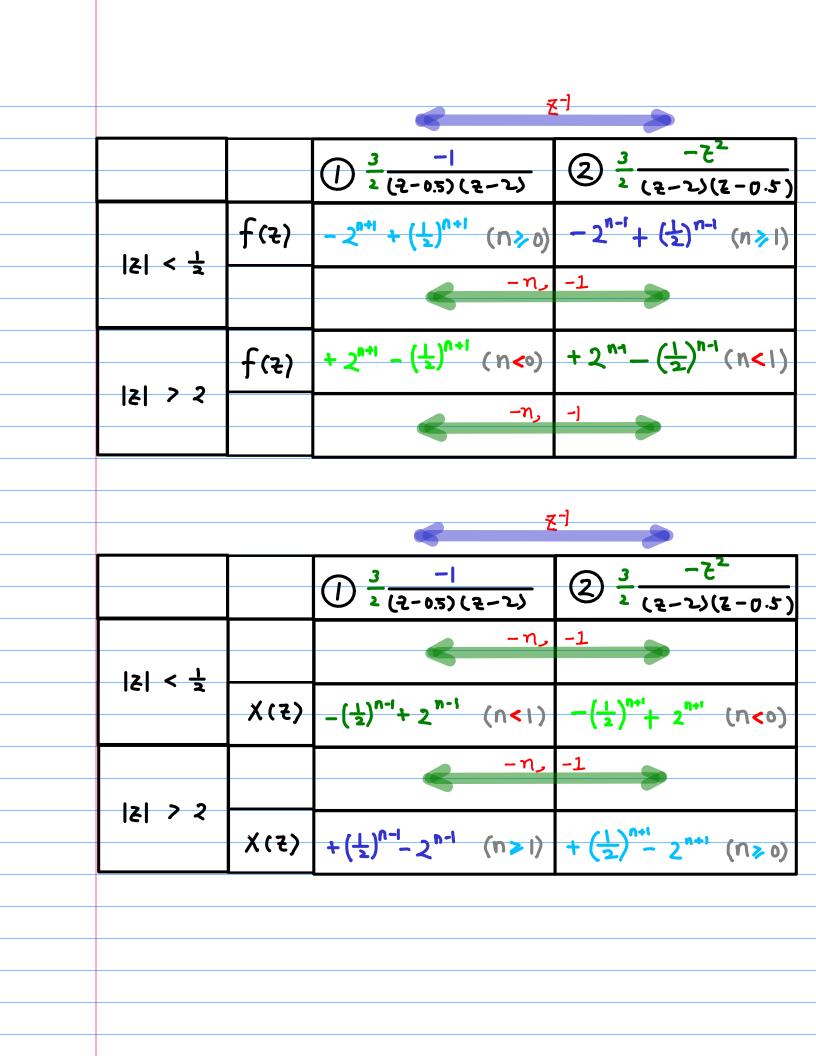


		V
	() - (2-1)(2-2)	$\frac{z^{-1}}{(z-1)(z-0.5)}$
	121 < 0.5	2 < 0.5
	$-\frac{2}{1-2\xi}+\frac{0.5}{1-0.5\xi}$	$-\frac{z}{ -2z}+\frac{z}{ -0.5z}$
	$f(z) = -\left[2 + 2^{3}z' + 2^{3}z' + \cdots\right] -2^{n}$ $+\left[\left(\frac{1}{2}\right) + \left(\frac{1}{2}\right)^{2}z' + \left(\frac{1}{2}\right)^{3}z^{2} + \cdots\right] + \left(\frac{1}{2}\right)^{n+1}$	$f(z) = -\left[2^{0}z' + 2^{1}z^{2} + 2^{2}z^{3} + \cdots\right] -2^{n}$ $+\left[\left(\frac{1}{2}\right)^{0}z' + \left(\frac{1}{2}\right)^{1}z^{2} + \left(\frac{1}{2}\right)^{2}z^{3} + \cdots\right] + \left(\frac{1}{2}\right)^{n-1}$
$\lambda = \left(\frac{1}{2}\right)^{-1}$ $\left(\frac{1}{2}\right) = \lambda^{-1}$	$X (2) = -\left[\left(\frac{1}{2}\right)^{-1} + \left(\frac{1}{2}\right)^{-2} z^{1} + \left(\frac{1}{2}\right)^{-3} z^{2} + \cdots \right] - \left(\frac{1}{2}\right)^{n-1} + \left[2^{-1} + 2^{-2} z^{1} + 2^{-3} z^{2} + \cdots \right] + 2^{n-1}$	$X (2) = -\left[\left(\frac{1}{2} \right)^{0} z^{1} + \left(\frac{1}{2} \right)^{1} z^{2} + \left(\frac{1}{2} \right)^{2} z^{3} + \cdots \right] - \left(\frac{1}{2} \right)^{n+1} + \left[2^{0} z^{1} + 2^{4} z^{2} + 2^{-2} z^{3} + \cdots \right] + 2^{n+1}$
	n= 0 -1 -2 8 72	n= -1 -2 -3 E 72
	$\frac{\overline{\xi}^{-1}}{ -0.5\overline{\xi}^{-1} } = \frac{\overline{\xi}^{-1}}{ -2\overline{\xi}^{-1} }$	$\frac{0.5}{ -0.5\epsilon^{-1}} = \frac{2}{ -2\epsilon^{-1}}$
$2 = \left(\frac{1}{2}\right)^{-1}$ $\left(\frac{1}{2}\right) = 2^{-1}$	$f(z) = + \left[2^{\circ} \overline{z}^{1} + 2^{-1} \overline{z}^{-1} + 2^{-1} \overline{z}^{-3} + \cdots\right] + 2^{n+1} - \left[\left(\frac{1}{2}\right)^{\circ} \overline{z}^{-1} + \left(\frac{1}{2}\right)^{-1} \overline{z}^{-3} + \cdots\right] - \left(\frac{1}{2}\right)^{n+1}$	$f(z) = + \left[2^{4} z^{\circ} + 2^{-2} z^{-1} + 2^{-3} z^{-2} + \cdots \right] + 2^{n-1} - \left[\left(\frac{1}{2} \right)^{-1} z^{\circ} + \left(\frac{1}{2} \right)^{-2} z^{-1} + \left(\frac{1}{2} \right)^{-2} z^{-2} + \cdots \right] - \left(\frac{1}{2} \right)^{N-1}$
	$X (Z) = + \left[\left(\frac{1}{2} \right)^{n} \overline{z}^{1} + \left(\frac{1}{2} \right)^{n} \overline{z}^{-2} + \left(\frac{1}{2} \right)^{n} \overline{z}^{-3} + \cdots \right] + \left(\frac{1}{2} \right)^{n-1} - \left[2^{n} \overline{z}^{-1} + 2^{1} \overline{z}^{-2} + 2^{n} \overline{z}^{-3} + \cdots \right] - 2^{n-1}$	$X (2) = + \left[\left(\frac{1}{2} \right)^{3} \overline{z}^{0} + \left(\frac{1}{2} \right)^{3} \overline{z}^{-1} + \left(\frac{1}{2} \right)^{3} \overline{z}^{-1} + \cdots \right] + \left(\frac{1}{2} \right)^{3+1} - \left[2^{1} \overline{z}^{0} + 2^{2} \overline{z}^{-1} + 2^{3} \overline{z}^{-2} + \cdots \right] - 2^{3+1}$
	n= \ 2 3	n= 0 1 2



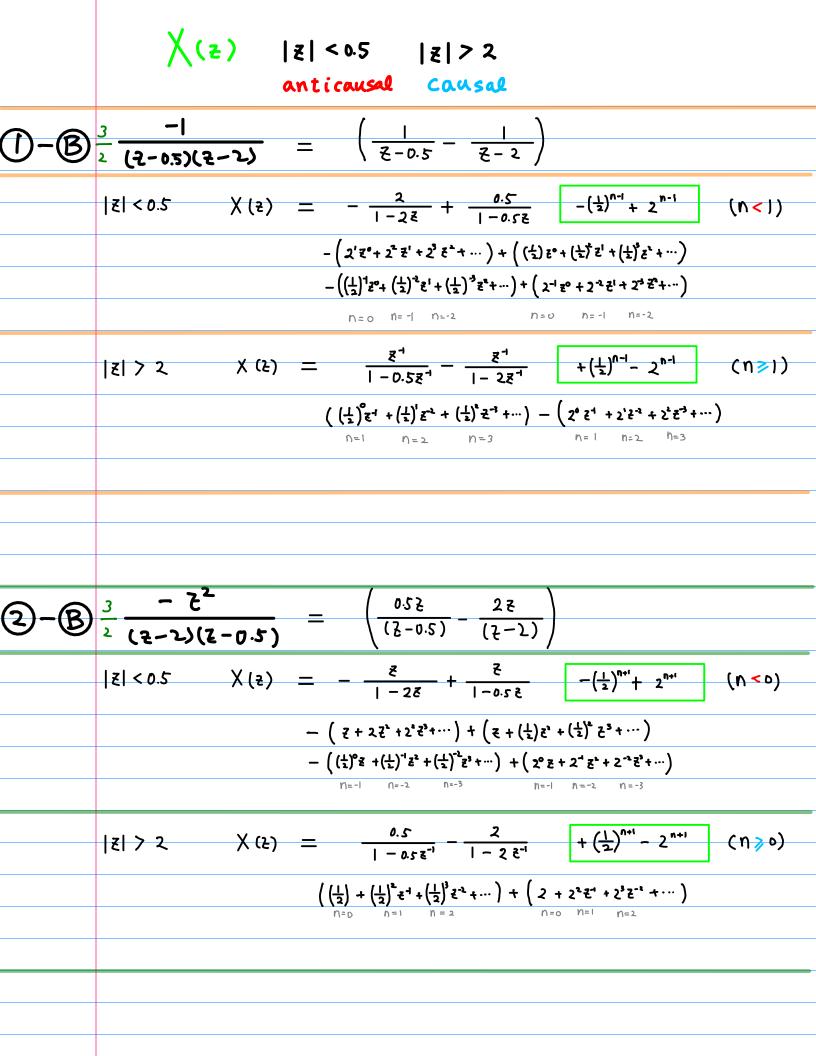
		$(1) \frac{3}{2} \frac{-1}{(2-0.5)(2-2)}$	$2\frac{3}{2}\frac{-2^{2}}{(2-2)(2-0.5)}$
원 < 국	f(z)	$-2^{n+1} + (\frac{1}{2})^{n+1}$ (n>0)	
		-1	-1
2 7 2	f(z)	+ 2 ⁿ⁺¹ - (±) ⁿ⁺¹ (n<0)	$+2^{n_1}-(\frac{1}{2})^{n_1}(n<1)$
		() 3 - I (2-05) (2-2)	$(2) \frac{3}{2} - \frac{-2^2}{2}$
		・ ~ (え-0.5) (そーン)	~ ~ (2-2)(Z-0.5
돈 < 닃	X(₹)	$-(\frac{1}{2})^{n-1}+2^{n-1}$ (n<+)	
 			1-1
2 > 2	X(Z)	$+(\frac{1}{2})^{n-1}-2^{n-1}$ (N>1)	$+ \left(\frac{1}{2}\right)^{n+1} - 2^{n+1} (n \ge 0)$

$$2^{n+1} = \left(\frac{1}{2}\right)^{n-2} = \left(\frac{1}{2}\right)^{n-1} \qquad \left(\frac{1}{2}\right)^{n-1} = 2^{n} \cdot 2 = 2^{n+1} \\ \left(\frac{1}{2}\right)^{n+1} = 2^{n} \cdot \frac{1}{4} = 2^{n-1} \qquad 2^{n-1} = \left(\frac{1}{2}\right)^{n-1} = 2^{n} \cdot 2 = 2^{n+1} \\ \frac{2^{n}}{2} \left(\frac{1}{2}\right)^{n+1} = 2^{n} \cdot \frac{1}{4} = 2^{n-1} \qquad 2^{n-1} = \left(\frac{1}{2}\right)^{n-1} = 2^{n} \cdot 2 = 2^{n+1} \\ \frac{2^{n}}{2} \left(\frac{1}{2}\right)^{n+1} = 2^{n} \cdot \frac{1}{4} = 2^{n-1} \qquad 2^{n-1} = \left(\frac{1}{2}\right)^{n-1} = 2^{n} \cdot 2 = 2^{n} \cdot 2^{n} = 2^{n} \cdot 2^{n} \cdot 2^{n-1} = 2^{n} \cdot 2^{n} \cdot 2^{n-1} = 2^{n} \cdot 2^{n} \cdot 2^{n} \cdot 2^{n-1} = 2^{n} \cdot 2^{n} \cdot 2^{n} \cdot 2^{n-1} = 2^{n} \cdot 2^{n} \cdot 2^{n-1} = 2^{n} \cdot 2^{n} \cdot 2^{n-1} + 2^{n} \cdot 2^{n-1} \cdot 2^{n-1} + 2^{n} \cdot 2^{n-1} \cdot 2^{n-1} \cdot 2^{n-1} + 2^{n} \cdot 2^{n-1} \cdot 2^$$



$ z < \frac{1}{2}$ $ z < \frac{1}{2}$ $\frac{f(z)}{x(z)} - \frac{2^{n+1} + (\frac{1}{2})^{n+1}}{(n < 0)}$ $\frac{f(z)}{x(z)} + \frac{2^{n+1} - (\frac{1}{2})^{n+1}}{(n < 0)}$ $\frac{f(z)}{x(z)} + \frac{(\frac{1}{2})^{n-1} - 2^{n-1}}{(n > 1)}$ $\frac{f(z)}{z(z - 0.5)(z - 2)}$ $\frac{f(z)}{z(z - 0.5)(z - 2)}$ $\frac{f(z)}{x(z)} + \frac{f(z)}{z(z - 0.5)(z - 2)}$ $\frac{f(z)}{z(z - 0.5)(z - 2)}$ $\frac{f(z)}{z(z - 0.5)(z - 2)}$			$\frac{1}{2} \frac{3}{2(2-0.5)(2-2)}$	$2^{\frac{3}{2}} \frac{-2^2}{(2-2)(2-6)}$
$ z < \frac{1}{2}$ $X(z) = -(\frac{1}{2})^{n-1} + 2^{n-1} (n < 1)$ $f(z) + 2^{n+1} - (\frac{1}{2})^{n+1} (n < 0)$ $ z > 2$ $X(z) + (\frac{1}{2})^{n-1} - 2^{n-1} (n > 1)$ $\frac{1}{2} - \frac{1}{2} = \frac{2}{2} - \frac{2^{2}}{2} - \frac{2^{2}}{2$	ــــــــــــــــــــــــــــــــــــــ	f(2)		
$ z > 2$ $X(z) + (\frac{1}{2})^{n-1} - 2^{n-1} (n \ge 1)$ $\frac{1}{2} - \frac{1}{2} (1 \ge \frac{3}{2} - \frac{-2^2}{(2-2)(2-1)}$ $\frac{1}{2} - \frac{1}{2} (2 \ge \frac{3}{2} - \frac{-2^2}{(2-2)(2-1)}$ $\frac{1}{2} - \frac{1}{2} - \frac{1}{2} (n \ge 1)$ $\frac{1}{2} - \frac{1}{2} - \frac{1}{2} (n \ge 1)$	161 1 2	X(Z)	$-(\frac{1}{2})^{n-1}+2^{n-1}$ (n<)	
$\begin{array}{c c} \chi(z) & +\left(\frac{1}{2}\right)^{n-1} - 2^{n-1} & (n \ge 1) \\ \hline & & \\ \hline \\ \hline$		f(2)	+ 2 ⁿ⁺¹ - ([⊥] / ₂) ⁿ⁺¹ (n<0)	
$ z < \frac{1}{2} \qquad f(z) $	121 7 4	X(Z)	$+\left(\frac{7}{7}\right)_{u-1}$ -5_{u-1} $(u \ge 1)$	
$ z < \frac{1}{2}$ $f(z)$ $-2^{n-i} + (\frac{1}{2})^{n-i} (n + 2^{n} + 2^{n}) + 2^{n} (n + 2^{n}) + $		<u> </u>		- 1 - ²
$ z < \frac{1}{2}$ $f(z)$ $-2^{n-i} + (\frac{1}{2})^{n-i} (n)$ $-(\frac{1}{2})^{n+i} + 2^{n+i} (n)$ $f(z)$ $f(z)$ $f(z)$			$\frac{1}{2} \frac{3}{2} \frac{-1}{(2-0.5)(2-2)}$	$2\frac{3}{2}\frac{-2^{-1}}{(2-2)(2-1)}$
$\frac{ z < \frac{1}{2}}{ z > 2} \qquad \frac{\chi(z)}{ z > 2} \qquad -\left(\frac{1}{2}\right)^{n+1} + 2^{n+1} (n) + 2^{n-1} - \left(\frac{1}{2}\right)^{n-1} (n)$		f(z)		$-2^{n-1}+(\frac{1}{2})^{n-1}$ (n
	2 < 호	X(Z)		$-\left(\frac{1}{2}\right)^{n+i} + 2^{n+i}$ (n-
$\frac{1}{2} + \left(\frac{1}{2}\right)^{n+1} - 2^{n+1} (n)$				
		f(z)		$+2^{n_1}-(\frac{1}{2})^{n_1}(n_1)$

$$\begin{aligned}
\int (z) |z| < 0.5 \\
Coursel = \frac{1}{2} \frac{-1}{(z-0.5)(z-2.5)} = \left(\frac{-1}{(z-0.5)} - \frac{1}{(z-2.5)}\right) \\
|z| < 0.5 \\
f(z) = -\frac{2}{1-2z} + \frac{\delta S}{1-\delta r z} - \frac{-2^{s_1}}{(z-2.5)} + \frac{\delta S}{1-\delta r z} \\
|z| < 0.5 \\
f(z) = -\frac{2}{1-2z} + \frac{\delta S}{1-\delta r z} - \frac{-2^{s_1}}{(z-2.5)} + \frac{\delta S}{(z-2.5)} \\
|z| > 2 \\
f(z) = \frac{z^{s_1}}{1-\delta z} - \frac{z^{s_1}}{z^{s_1+1}} - \frac{z^{s_1}}{(z-\delta S z^{s_1}} - \frac{z^{s_1}}{1-2z^{s_1}} + \frac{\delta S}{z^{s_1+1}} - \frac{1}{(z-2.5)} \\
|z| > 2 \\
f(z) = \frac{z^{s_1}}{1-\delta z} - \frac{z^{s_1}}{z^{s_1+1}} - \frac{z^{s_1}}{(z-\delta S z^{s_1}} - \frac{z^{s_1}}{1-2z^{s_1}} + \frac{\delta S}{z^{s_1+1}} - \frac{1}{(z-2.5)} \\
|z| > 2 \\
f(z) = \frac{z^{s_1}}{1-\delta z} - \frac{z^{s_1}}{z^{s_1+1}} - \frac{z^{s_1}}{z^{s_1+1}} + \frac{z^{s_1}}{z^{s_1}} - \frac{1}{(z^{s_1}+z^{s_1}z^{s_1+s_1})} \\
(z^{s_1}z^{s_1}z^{s_2}z^{s_1+s_1}) - (z^{s_1}z^{s_2}z^{s_1+s_1}) \\
(z^{s_1}z^{s_2}z^{s_1}z^{s_2}z^{s_1+s_1}) - (z^{s_1}z^{s_2}z^{s_1+s_1}) \\
(z^{s_1}z^{s_2}z^{s_1}z^{s_2}z^{s_1+s_1}) - (z^{s_1}z^{s_2}z^{s_1+s_1}) \\
(z^{s_1}z^{s_2}z^{s_1+s_1}z^{s_2}z^{s_1+s_1}) - (z^{s_1}z^{s_2}z^{s_1+s_1}z^{s_1+s_1}z^{s_2+s_1}) \\
(z^{s_1}z^{s_2}z^{s_1}z^{s_2+s_1}z^{s_2+s_1}) - (z^{s_1}z^{s_2}z^{s_1+s_1}z^{s_1+s_1}z^{s_2+s_1}z^{s_2+s_1}) \\
(z^{s_1}z^{s_2}z^{s_1+s_2}z^{s_2+s_1}z^{s_1+s_1}z^{s_1+s_1}z^{s_2+s_1+s_1}z^{s_1+s_1}$$



$$\frac{3}{2} \frac{-1}{(2 - 0.5)(2 - 2.)} = \left(\frac{1}{2 - 0.5} - \frac{1}{2 - 2}\right)$$

$$|\xi| < 0.5 \quad f(z) = -\frac{2}{1 - 2\xi} + \frac{6.5}{1 - 0.5\xi} - \frac{2^{\mu_1} + (\frac{1}{2})^{\mu_1}}{1 - 0.5\xi} (n \ge 0)$$

$$-\left(\frac{2^{\mu_1} + 2^{\mu_2} + 2^{\mu_2} + 2^{\mu_2} + \dots\right) + \left(\frac{1}{2}\right)^{\mu_1} + 2^{\mu_1}}{1 - 0.5\xi} (n \ge 0)$$

$$-\left(\frac{2^{\mu_1} + 2^{\mu_1} + 2^{\mu_2} + 2^{\mu_2} + 2^{\mu_2} + \frac{6.5}{1 - 0.5\xi}}{1 - 0.5\xi} - \frac{(\frac{1}{2})^{\mu_1} + 2^{\mu_1}}{1 - 0.5\xi} (n \le 0)$$

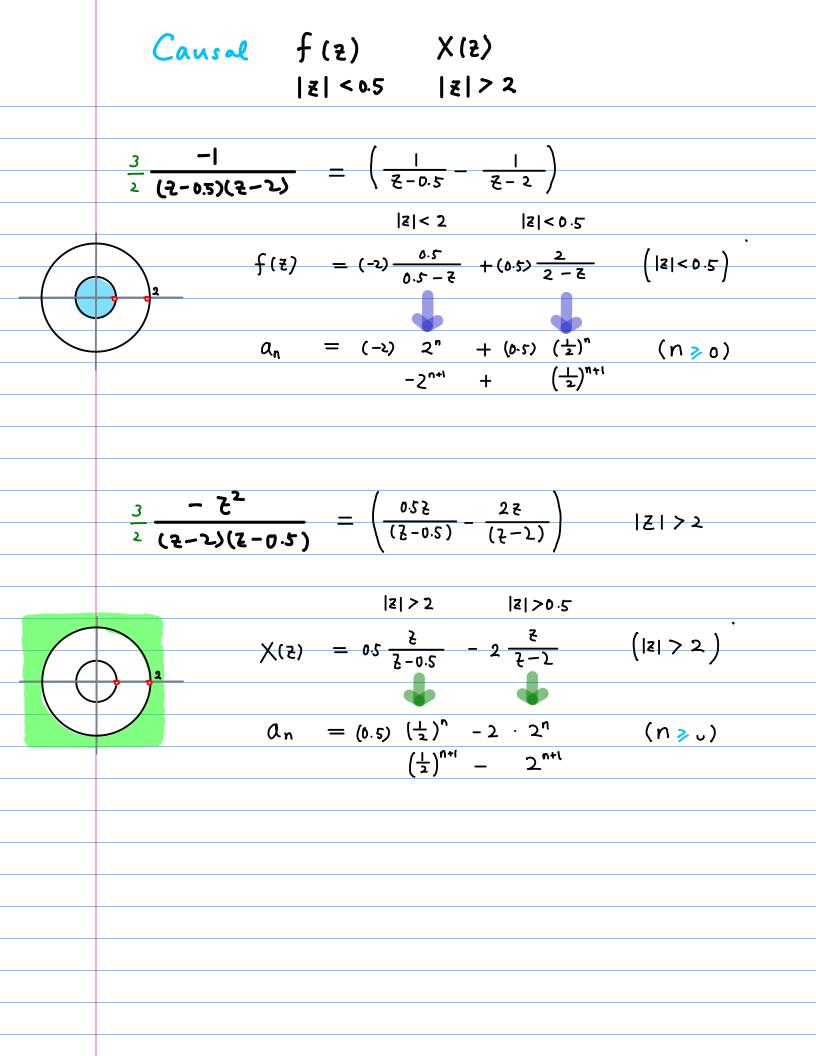
$$-\left(\frac{2^{\mu_1} + 2^{\mu_1} + 2^{\mu_2} + 2^{$$

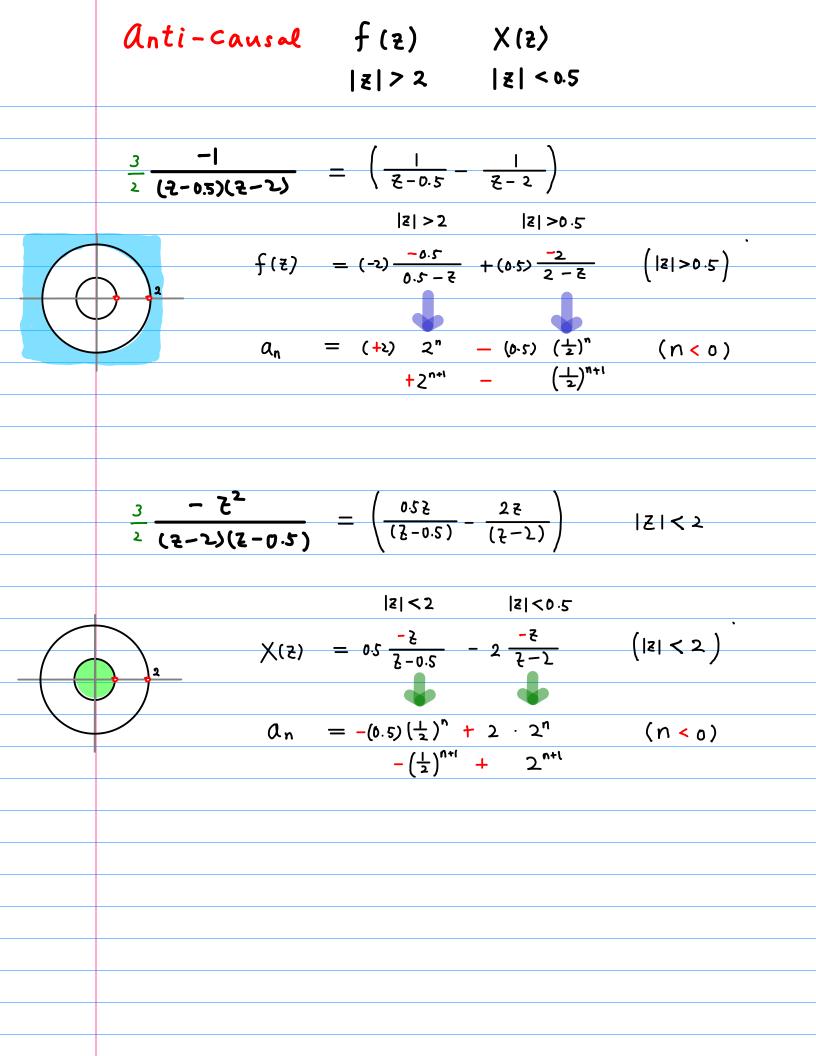
$$Roc \quad f(z) = \sum_{k=0}^{\infty} a^{nk} z^{n} \qquad a^{nk} \qquad n \ge 0 \quad n \ge | \quad n < 0 \quad n < |$$

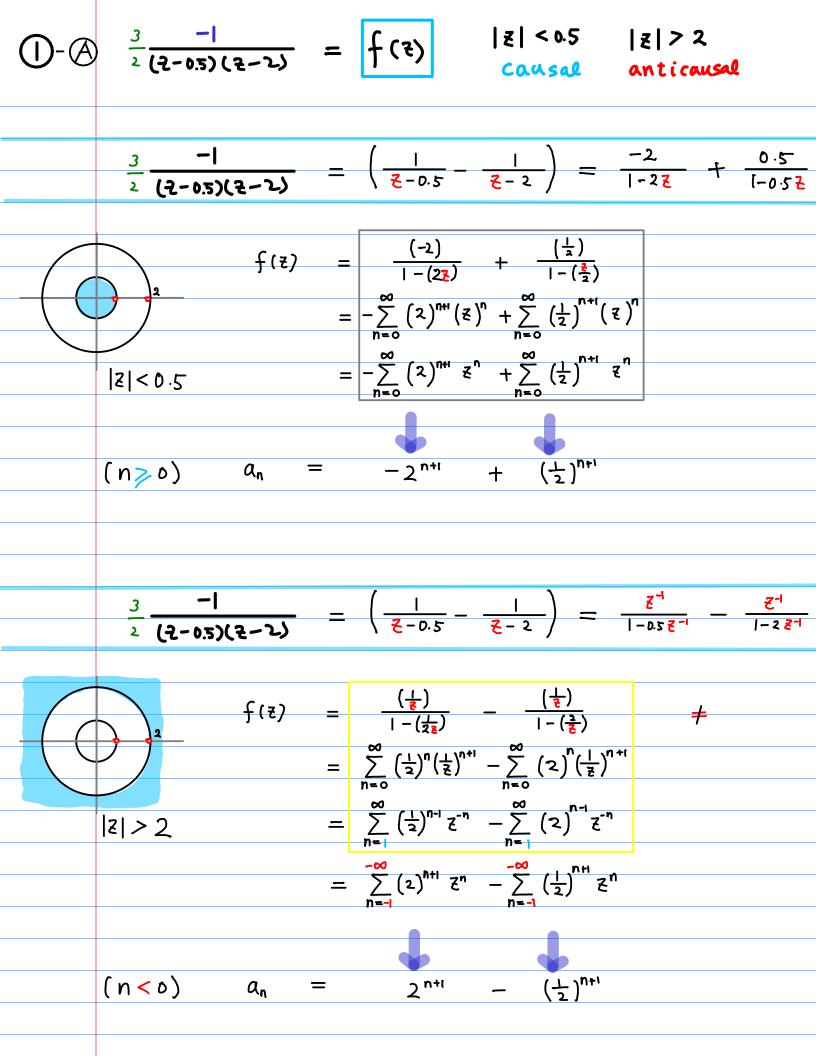
$$Roc \quad f(z) = \sum_{k=0}^{\infty} (a)^{k+1} z^{n} \qquad n < 0 \quad n < | \quad n \ge 0 \quad n \ge |$$

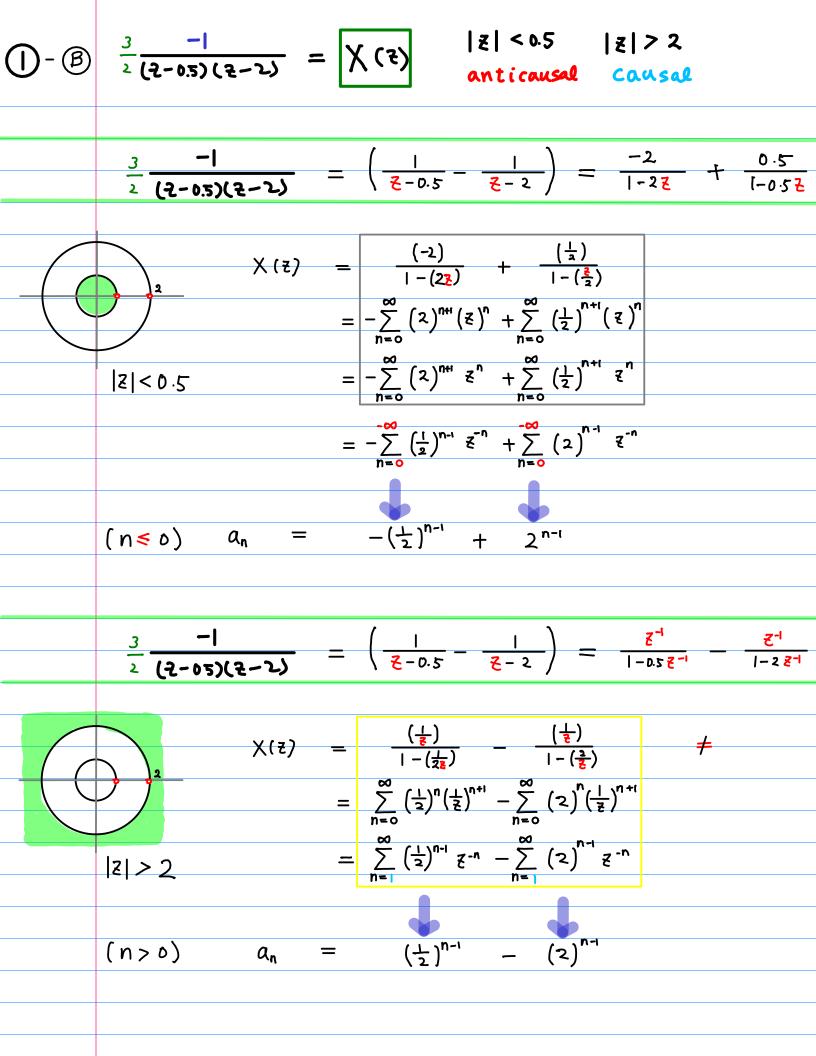
$$Roc \quad \chi(z) = \sum_{k=0}^{\infty} (a)^{k+1} z^{-k} \qquad (\frac{1}{6})^{-nk} \qquad n < 0 \quad n < | \quad n \ge 0 \quad n \ge |$$

$$= a^{n+1}$$









 $(2) - (A) = f(2) \qquad |z| < 0.5 \qquad |z| > 2$ $(2 - 2)(z - 0.5) = f(2) \qquad (ausal anticausal)$ $\frac{3}{2} \frac{-2^{2}}{(2-2)(2-0.5)} = \left(\frac{0.52}{(2-0.5)} - \frac{22}{(2-2)}\right) = -\frac{2}{1-22} + \frac{2}{1-0.52}$ $-\frac{f(z)}{1-(2z)} = -\frac{(z)}{1-(2z)} + \frac{(z)}{1-(\frac{z}{2})} \neq$ $= -\sum_{n=0}^{\infty} (2)^n (z)^{n+1} + \sum_{n=0}^{\infty} (\frac{1}{2})^n (z)^{n+1}$ $= -\sum_{n=1}^{\infty} (2)^{n-1} \vec{z}^n + \sum_{n=1}^{\infty} (\frac{1}{2})^{n-1} \vec{z}^n$ Z | < 0.5 $\frac{3}{2} \frac{-2^{2}}{(2-2)(2-0.5)} = \left(\frac{0.52}{(2-0.5)} - \frac{22}{(2-1)}\right) = \frac{0.5}{1-0.52^{-1}} - \frac{2}{1-22^{-1}}$ $f(\overline{z}) = \frac{\left(\frac{1}{2}\right)}{|-(\frac{1}{2\overline{z}})} - \frac{(2)}{|-(\frac{3}{\overline{z}})}$ 2 $= \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \left(\frac{1}{2}\right)^n - \sum_{n=0}^{\infty} \left(2\right)^{n+1} \left(\frac{1}{2}\right)^n$ $= \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \xi^{-n} - \sum_{n=0}^{\infty} \left(2\right)^{n+1} \xi^{-n}$ |z| > 2 $= \sum_{n=0}^{\infty} (2)^{n-1} \xi^{n} - \sum_{n=0}^{\infty} (\frac{1}{2})^{n-1} \xi^{n}$ $(n \leq 0)$ $a_n = 2^{n-1} - (\frac{1}{2})^{n-1}$

$$(2) - (3) = \frac{3}{2} \frac{-\overline{c}^2}{(\overline{c} - \overline{c})(\overline{c} - 0.5)} = (X, (\overline{c})) = |\overline{z}| < 0.5$$

$$\frac{3}{2} \frac{-\overline{c}^2}{(\overline{c} - \overline{c})(\overline{c} - 0.5)} = (\frac{55}{(\overline{c} - 0.5)} - \frac{2\overline{c}}{(\overline{c} - 1.5)}) = -\frac{\overline{c}}{1 - 2\overline{c}} + \frac{\overline{c}}{1 - 0.5\overline{c}}$$

$$\frac{3}{2} \frac{-\overline{c}^2}{(\overline{c} - \overline{c})(\overline{c} - 0.5)} = (\frac{55}{(\overline{c} - 0.5)} - \frac{2\overline{c}}{(\overline{c} - 1.5)}) = -\frac{\overline{c}}{1 - 2\overline{c}} + \frac{\overline{c}}{1 - 0.5\overline{c}}$$

$$\frac{3}{2} \frac{-\overline{c}^2}{(\overline{c} - \overline{c})(\overline{c} - 0.5)} = (\frac{\overline{c}}{1 - (2\overline{c})}) + \frac{\overline{c}}{1 - (2\overline{c})}) = -\frac{\overline{c}}{1 - 2\overline{c}} + \frac{\overline{c}}{1 - 0.5\overline{c}}$$

$$|\overline{z}| < 0.5 = -\frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n + \frac{\overline{c}}{\overline{c}}(\frac{1}{2})^{n_1}\overline{c}^n$$

$$= -\frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n + \frac{\overline{c}}{\overline{c}}(\frac{1}{2})^{n_1}\overline{c}^n$$

$$= -\frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n + \frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n$$

$$= -\frac{\overline{c}}{\overline{c}}(\frac{1}{\overline{c}})^{n_1}\overline{c}^n + 2^{n_1}$$

$$(n < 0) \qquad 0_n = -(\frac{1}{2})^{n_1}\overline{c}^n - \frac{2\overline{c}}{(\overline{c} - 0.5)} - \frac{2\overline{c}}{1 - 0.5\overline{c}^{n_1}} - \frac{2}{1 - 2\overline{c}^{n_1}}$$

$$\frac{3}{2} \frac{-\overline{c}^2}{(\overline{c} - 0.5)} = (\frac{0.5\overline{c}}{(\overline{c} - 0.5)} - \frac{2\overline{c}}{(\overline{c} - \overline{c})}) = \frac{0.5}{1 - 0.5\overline{c}^{n_1}} - \frac{2}{1 - 2\overline{c}^{n_1}}$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}^2}{(\overline{c} - 0.5)} = (\frac{1}{\overline{c}})^{n_1}\overline{c}^n - \frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}^2}{(\overline{c} - 0.5)} = (\frac{1}{\overline{c}})^{n_1}\overline{c}^n - \frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}^2}{(\overline{c} - 0.5)} = (\frac{1}{\overline{c}})^{n_1}\overline{c}^n - \frac{2\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}^2}{(\overline{c} - 0.5)} = (\frac{1}{\overline{c}})^{n_1}\overline{c}^n - \frac{2\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}}{(\overline{c}})^{n_1}\overline{c}^n - \frac{\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$

$$\frac{3}{\overline{c}} \frac{-\overline{c}}{\overline{c}}(2)^{n_1}\overline{c}^n]$$