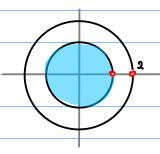
Laurent Series and z-Transform Examples case 0.A

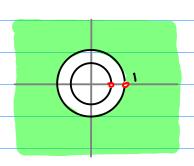
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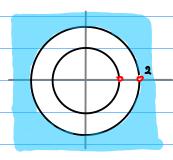
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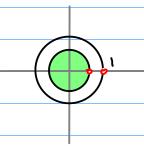
$$\frac{1}{2}(5) = \frac{(5-1)(5-5)}{-1} \longrightarrow \chi(5) = \frac{(5-1)(5-0.5)}{-0.5 \cdot 5^{2}}$$



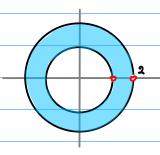


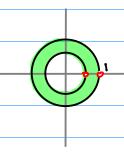
$$\sum_{n=0}^{\infty} \left[\left(\frac{1}{2} \right)^{n+1} - 1 \right] Z^n$$





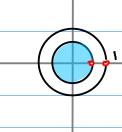
$$\sum_{n=1}^{\infty} \left(\left| - \left(\frac{1}{2} \right)^{n+1} \right) \mathcal{Z}^n$$



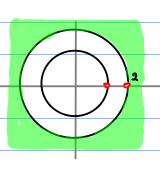


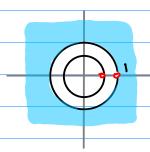
$$\sum_{n=-1}^{\infty} \mathbb{Z}^n + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \mathbb{Z}^n$$

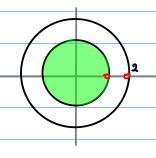
$$\frac{1}{2}(z) = \frac{(5-1)(z-0.5)}{-0.5z^2} \longrightarrow \chi(z) = \frac{(3-1)(3-2)}{-1}$$

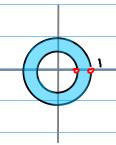


$$\sum_{n=1}^{\infty} \left[1 - 2^{n-1} \right] z^n$$

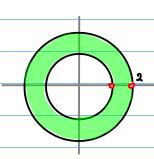




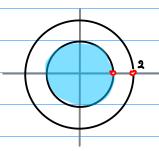


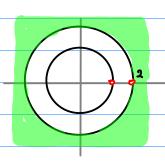


$$\sum_{n=1}^{\infty} 1 \cdot \xi^{n} + \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^{n}$$

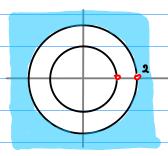


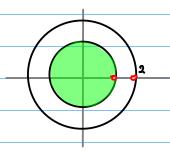
$$\frac{1}{2}(5) = \frac{(5-1)(5-5)}{-1} \longrightarrow \chi(5) = \frac{(5-1)(5-5)}{-1}$$



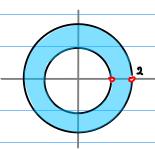


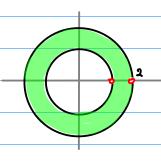
$$\sum_{n=0}^{\infty} \left[\left(\frac{1}{2} \right)^{n+1} - 1 \right] \, \mathcal{Z}^n$$





$$\sum_{n=-1}^{\infty} \left[\left| - \left(\frac{1}{2} \right)^{n+1} \right| \, \mathcal{Z}^n \right]$$

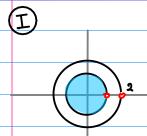


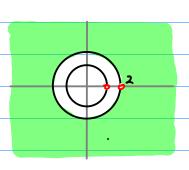


$$\sum_{n=-1}^{\infty} Z^{n} + \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} Z^{n}$$

$$\mathcal{L}_{n} = \begin{cases} \left(\frac{1}{2}\right)^{n+1} - 1 & (n \geq 0) \\ 0 & (n < 0) \end{cases} \qquad \mathcal{L}_{n} = \begin{cases} 1 - 2^{n-1} & (n \geq 0) \\ 0 & (n < 0) \end{cases}$$

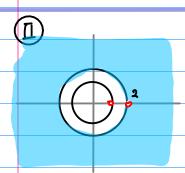
$$\frac{1}{2}(5) = \frac{(5-1)(5-5)}{-1} = \chi(5)$$

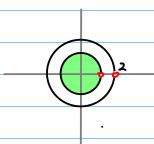




$$Q_n = \begin{cases} \left(\frac{1}{2}\right)^{n_{11}} - 1 & (n \ge 0) \\ 0 & (n < 0) \end{cases}$$

$$\chi_{n} = \begin{cases} 1 - 2^{n-1} & (n > 0) \\ 0 & (n < 0) \end{cases}$$



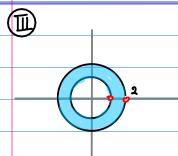


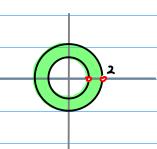
$$Q_n = \begin{cases} Q & (1) > 0 \end{cases}$$

$$1 - \left(\frac{1}{2}\right)^{n+1} \quad (1) < 0$$

$$\mathcal{X}_{n} = \begin{cases} 0 & (1) > 0 \end{cases}$$

$$2^{n+1} - 1 & (1) < 0$$





$$Q_n = \begin{cases} \left(\frac{1}{2}\right)^{n+1} & (n > 0) \\ 1 & (n < 0) \end{cases}$$

$$\mathcal{X}_{n} = \begin{cases} 1 & (n > 0) \\ 2^{n-1} & (n < 0) \end{cases}$$

$$Q_n = \begin{cases} \left(\frac{1}{2}\right)^{n_{r_1}} - 1 & (n \ge 0) \\ 0 & (n < 0) \end{cases}$$

$$\mathcal{I}_{n} = \left\{ \begin{array}{c} 0 \\ \left(\frac{1}{2}\right)^{-n\eta} - 1 \\ \left(\frac{1}{2}\right)^{-n\eta} - 1 \end{array} \right. \quad (n < 0)$$

$$f(\xi) = \sum_{n=0}^{\infty} \left(\frac{1}{2}\right)^{n+1} \xi^n - \sum_{n=0}^{\infty} 1. \ \xi^n \qquad \chi(\xi) = \sum_{n=0}^{-\infty} \left(\frac{1}{2}\right)^{-n+1} \xi^{-n} - \sum_{n=0}^{-\infty} 1. \ \xi^{-n}$$

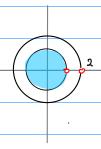
$$X(z) = \sum_{n=0}^{\infty} (\frac{1}{2})^{-n+1} z^{-n} - \sum_{n=0}^{\infty} 1. z^{-n}$$

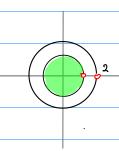
$$= \sum_{n=0}^{\infty} (\frac{1}{2})^{n+1} z^{n} - \sum_{n=0}^{\infty} 1. z^{n}$$

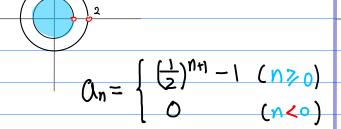
$$=\frac{\left(\frac{1}{2}\right)}{\left|-\left(\frac{2}{2}\right)\right|}$$

$$=\frac{-1}{7-2}+\frac{1}{2-1}$$

$$\left|\frac{\xi}{2}\right| < \left|\frac{\xi}{1}\right| < 1$$

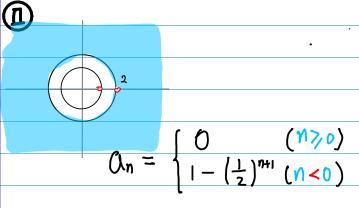




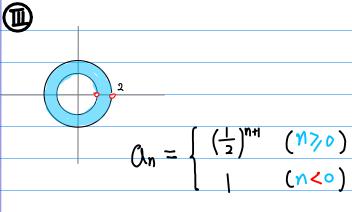


$$f(\xi) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n - \sum_{n=0}^{\infty} 1 \cdot \xi^n$$

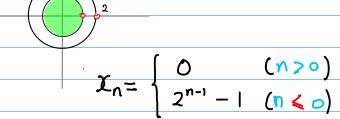
$$f(z) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot z^n - \sum_{n=0}^{\infty} 1 \cdot z^n$$



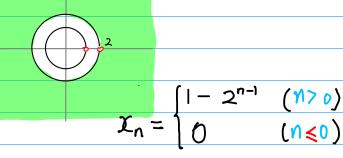
$$f(\xi) = \sum_{n=-1}^{\infty} |\cdot \xi^n| - \sum_{n=-1}^{\infty} 2^{-n-1} \cdot \xi^n$$



$$f(\xi) = \sum_{n=-1}^{-\infty} |\cdot \xi^n| - \sum_{n=0}^{\infty} 2^{-n-1} \cdot z^n$$



$$\chi(z) = \sum_{n=0}^{-\infty} 2^{n-1} \cdot z^{-n} - \sum_{n=0}^{-\infty} 1 \cdot z^{-n}$$



$$\chi(\xi) = \sum_{n=1}^{\infty} |\cdot \xi_n - \sum_{n=1}^{\infty} 2^{n-1} \cdot \xi_{-n}$$

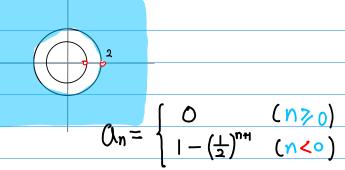
$$\mathcal{I}_{n} = \begin{cases} 1 & (n > 0) \\ 2^{n-1} & (n \leq 0) \end{cases}$$

$$X(\xi) = \sum_{n=1}^{\infty} |\cdot \xi^{-n}| - \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^{-n}$$

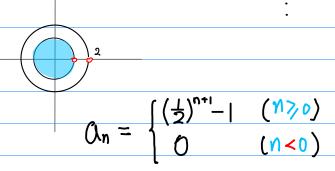
$$f(\xi) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n - \sum_{n=0}^{\infty} 1 \cdot \xi^n \qquad \chi(\xi) = \sum_{n=0}^{-\infty} 2^{n-1} \cdot \xi^{-n} - \sum_{n=0}^{-\infty} 1 \cdot \xi^{-n}$$

$$=\frac{\left(\frac{1}{2}\right)}{1-\left(\frac{2}{2}\right)}-\frac{\left(\frac{1}{1}\right)}{1-\left(\frac{2}{1}\right)}=$$

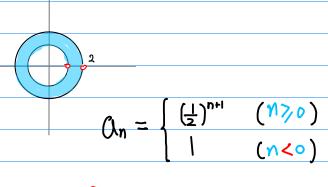
$$=\frac{-1}{\xi-2}+\frac{1}{\xi-1}$$



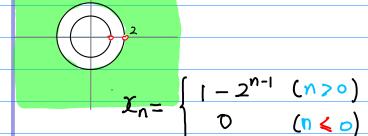
$$f(z) = \sum_{n=-1}^{-1} 1 \cdot z^n - \sum_{n=-1}^{-\infty} 2^{-n-1} z^n$$



$$f(\xi) = \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n - \sum_{n=0}^{\infty} |\cdot \xi^n|$$

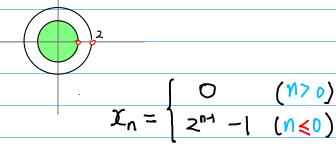


$$f(\xi) = \sum_{n=-1}^{\infty} 1 \cdot \xi^n + \sum_{n=0}^{\infty} 2^{-n-1} \cdot \xi^n$$



囯

$$\chi(\xi) = \sum_{n=1}^{\infty} |\cdot \xi_n - \sum_{n=1}^{\infty} z_{n-1} \xi_n$$



$$\chi(\xi) = \sum_{n=0}^{-\infty} 2^{n-1} \cdot \xi^{-n} - \sum_{n=0}^{-\infty} 1 \cdot \xi^{-n}$$

$$\chi_{n} = \begin{cases} 1 & (1/70) \\ 2^{n-1} & (n \leq 0) \end{cases}$$

$$X(\xi) = \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^{-n} + \sum_{n=1}^{\infty} |\cdot \xi^{-n}|$$



