Functor (1A)

Young Won Lim 7/25/17 Copyright (c) 2016 - 2017 Young W. Lim.

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http://learnyouahaskell.com/making-our-own-types-and-typeclasses#the-functor-typeclass

Haskell in 5 steps https://wiki.haskell.org/Haskell_in_5_steps

Typeclasses

Typeclasses are like interfaces

defines some behavior

comparing for equality comparing for ordering enumeration

Instances of that typeclass types possessing such behavior

Such behavior is defined by function definition type declaration to be implemented

a type is an instance of a typeclass implies the functions defined by the typeclass with that type can be used

No relation with classes in Java or Python



A Typeclass Example

the Eq typeclass

defines the functions == and *I*=

a type Car

comparing two cars c1 and c2 with the equality function ==

The Car type is an instance of Eq typeclass

Instances : various types

Typeclass : a group or a class of these similar types

a type Car	
a type Bag	Eq typeclass
a type Phone	functions
	functions
	== and /=

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Eq Typeclass Example

class Eq a where

- (==) :: a -> a -> Bool a type declaration (I=) :: a -> a -> Bool - a type declaration x == y = not (x /= y) - a function definition $x \neq y = not (x == y)$ - a function definition

data TrafficLight = Red | Yellow | Green

instance Eq TrafficLight where

Red == Red = True Green == Green = True Yellow == Yellow = True = False _ == _

ghci> Red == Red True ghci> Red == Yellow False ghci> Red `elem` [Red, Yellow, Green] True

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class Show a where

show :: a -> String * * *

- a type declaration

data TrafficLight = Red | Yellow | Green

instance Show TrafficLight where

show Red = "Red light"
show Yellow = "Yellow light"
show Green = "Green light"

ghci> [Red, Yellow, Green] [Red light,Yellow light,Green light]

class (Eq a) => Num a where

class Num a where

...

. . .

class constraint on a class declaration only we state that our type a must be an instance of Eq

an instance of **Eq** before being an instance of **Num**

When defining the required function bodies in the class declaration or in instance declarations,

we can safely use == because a is a part of Eq



class constraints in class declarations

to make a typeclass a subclass of another typeclass

class constraints in instance declarations

to express requirements about the contents of some type.

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the **a** : a concrete type

Maybe : <u>not</u> a concrete type

: a type constructor that takes one parameter produces a concrete type.

Maybe a : a concrete type

instance (Eq m) => Eq (Maybe m) where

Just x == Just y = x == y Nothing == Nothing = True _ == _ = False

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the Functor typeclass is basically for things that can be *mapped over*

ex) mapping over lists the list type is part of the Functor typeclass

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class Functor f where fmap :: $(a \rightarrow b) \rightarrow f a \rightarrow f b$

The Functor typeclass <u>defines</u> one function, fmap,

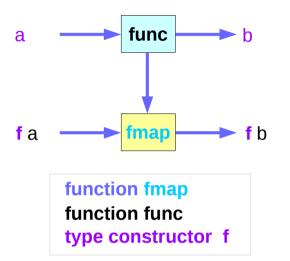
no default implementation

the type variable f

<u>not</u> a concrete type (a concrete type can hold a value) a **type constructor** taking one type parameter

Maybe Int : a concrete type

Maybe : a type constructor that takes one type as the parameter



Function map & fmap

class Functor f where

fmap :: (a -> b) -> **f** a -> **f** b

fmap takes

- a function from one type to another (a -> b)
- a Functor f applied with one type (f a)

fmap returns

• a Functor f applied with another type (f b)

map :: (a -> b) -> [a] -> [b]

map takes

•	a <u>function</u> from one type to another	(* 2)
•	take a list of one type	[1,2,3]
•	returns a list of another type	[2,4,6]

Functor ((1 A)
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List : an instance of Functor typeclass

class Functor f where

fmap :: (a -> b) -> **f** a -> **f** b

map :: (a -> b) -> [a] -> [b]

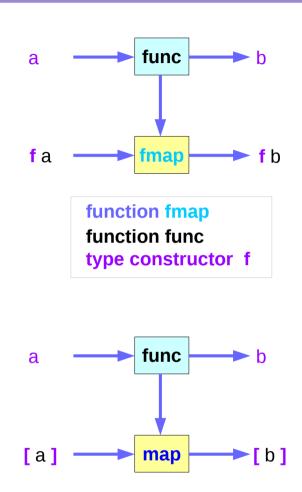
map is just a fmap that works only on lists

a list is an **instance** of the Functor typeclass.

```
instance Functor [ ] where
fmap = map
```

- f: a type constructor that takes one type
- []: a type constructor that takes one type
- [a]: a concrete type ([Int], [String] or [[String]])

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List Examples

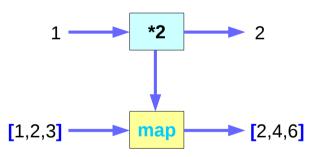
class Functor f where

fmap :: (a -> b) -> **f** a -> **f** b

map :: (a -> b) -> [a] -> [b]

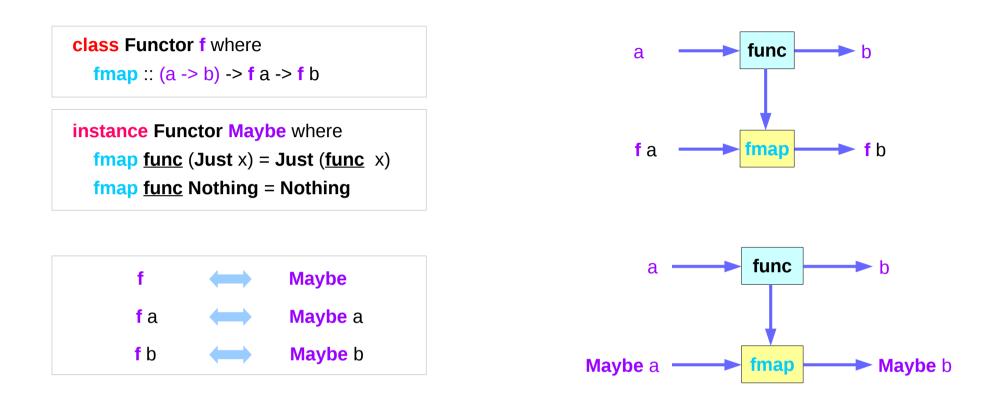
instance Functor [] where
fmap = map

```
map :: (a -> b) -> [a] -> [b]
ghci> fmap (*2) [1..3]
[2,4,6]
ghci> map (*2) [1..3]
[2,4,6]
```



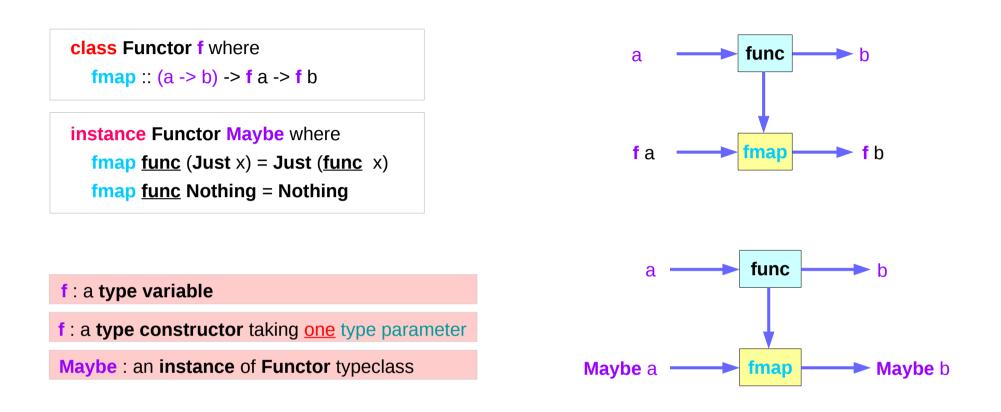
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Maybe : an instance of Functor typeclass



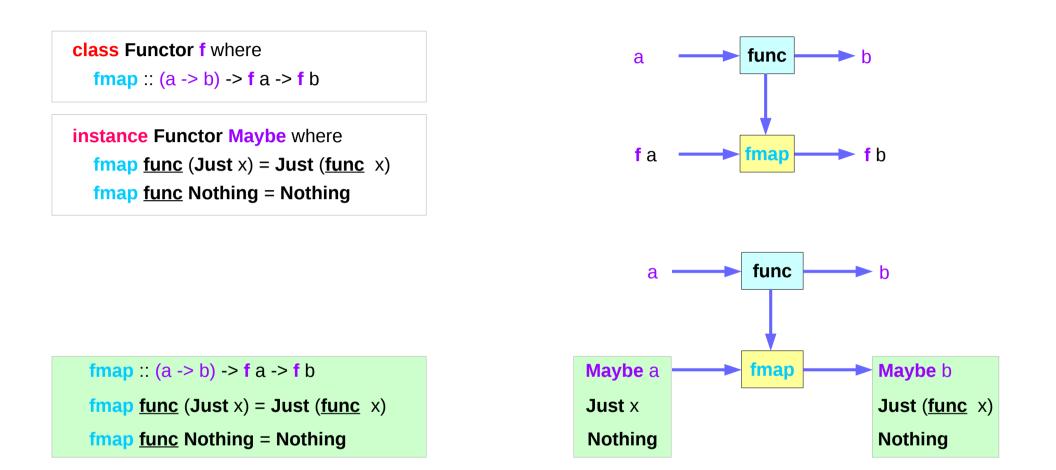
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Maybe : a type constructor



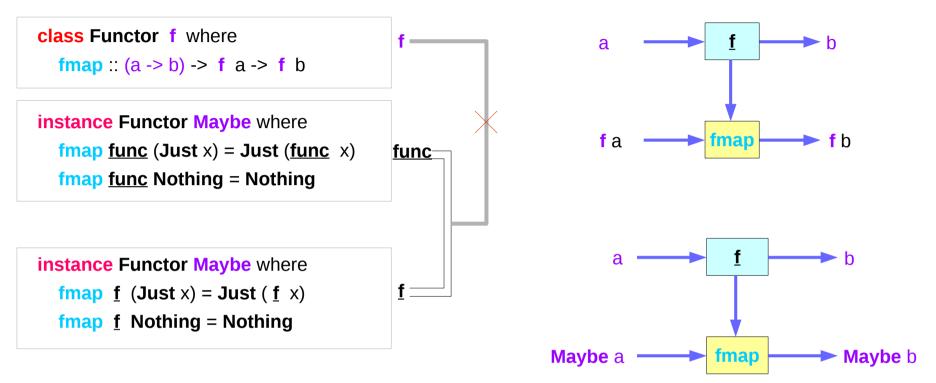
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Maybe : an argument to fmap, together with a



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Maybe : fmap takes a function



 $\underline{\mathbf{f}}$ is different from the type constructor \mathbf{f}

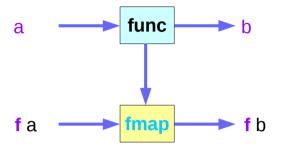
<u>func</u> : a -> b <u>f</u> : a -> b

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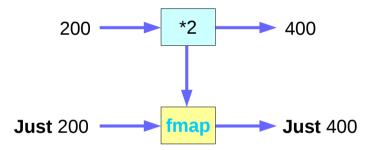
Maybe Examples (1)

class Functor f where fmap :: $(a \rightarrow b) \rightarrow f a \rightarrow f b$

instance Functor Maybe where
fmap f (Just x) = Just (f x)
fmap f Nothing = Nothing



ghci> fmap (*2) (Just 200) Just 400 ghci> fmap (*2) Nothing Nothing

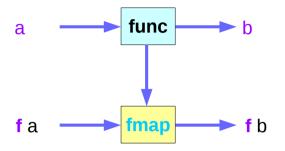


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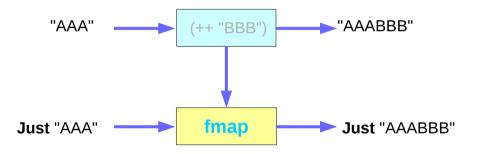
Maybe Examples (2)

class Functor f where fmap :: $(a \rightarrow b) \rightarrow f a \rightarrow f b$

instance Functor Maybe where
fmap f (Just x) = Just (f x)
fmap f Nothing = Nothing



ghci> fmap (++ "BBB") (Just "AAA") Just "AAABBB" ghci> fmap (++ "BBB") Nothing Nothing



Functor	(1A)
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Maybe as a functor

Functor typeclass:

- transforming one type to another
- transforming operations of one type to those of another

Maybe a is an instance of a functor type class

Functor provides fmap method

maps functions of the base type (such as Integer) to *functions* of the lifted type (such as Maybe Integer).

https://stackoverflow.com/questions/18808258/what-does-thejust-syntax-mean-in-haskell

Maybe as a functor

A *function* **f** transformed with **fmap** can work on a **Maybe** value

case maybeVal ofNothing -> NothingJust val -> Just (f val)-- there is a value, so apply the function to it

father :: Person -> Maybe Person mother :: Person -> Maybe Person

f :: Int -> Int fmap f :: Maybe Integer -> Maybe Integer

a Maybe Integer value: m_x

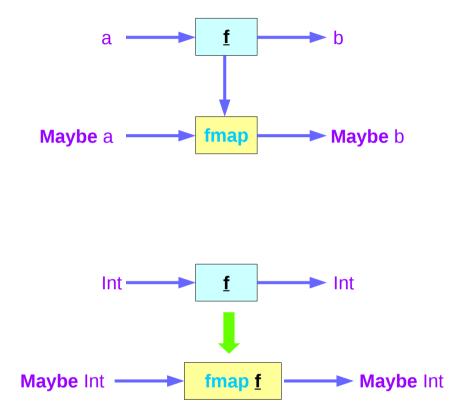
fmap f m_x

https://stackoverflow.com/questions/18808258/what-does-thejust-syntax-mean-in-haskell

Transforming operations

Functor provides fmap method

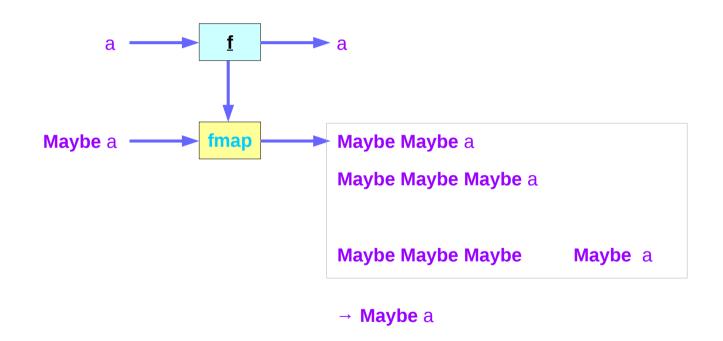
maps functions of the base type (such as Integer) to *functions* of the lifted type (such as Maybe Integer).



https://stackoverflow.com/questions/18808258/what-does-the-just-syntax-mean-in-haskell

Maybe as a functor

In fact, you could apply a whole chain of **lifted Integer** -> **Integer** functions to **Maybe Integer** values and only have to worry about explicitly checking for **Nothing** once when you're finished.



https://stackoverflow.com/questions/18808258/what-does-thejust-syntax-mean-in-haskell

Then Operator (>>) and **do** Statements

putStr "Hello" >> putStr " " >> putStr "world!" >> putStr "\n"

do { putStr "Hello"

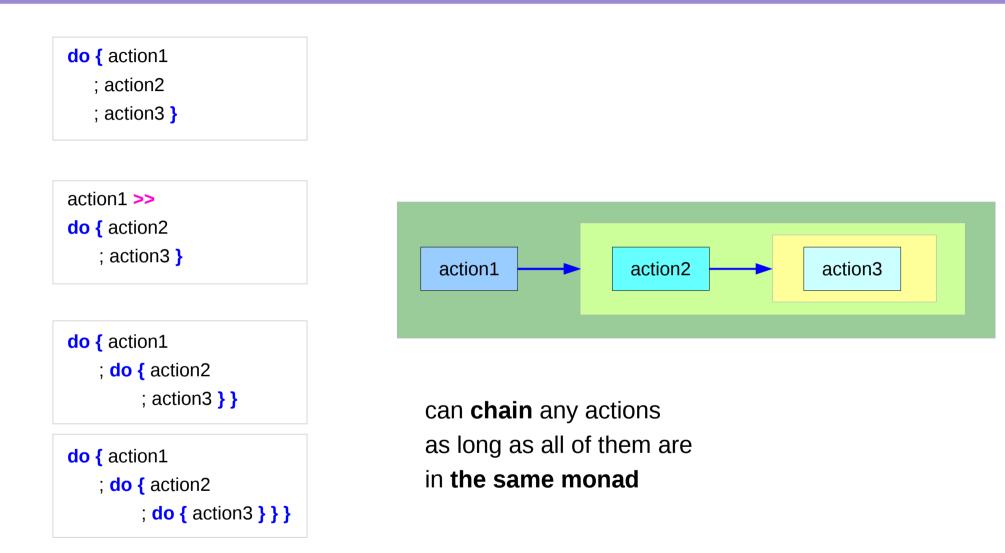
; putStr " "

; putStr "world!"

; putStr "\n" }

https://en.wikibooks.org/wiki/Haskell/do_notation

Translating in do notation



https://en.wikibooks.org/wiki/Haskell/do_notation

Bind Operator (>==) and **do** statements

The bind operator (>>=)

passes a value (the result of an action or function), downstream in the binding sequence.

action1 >>= (\ x1 -> action2 >>= (\ x2 -> mk action3 x1 x2))

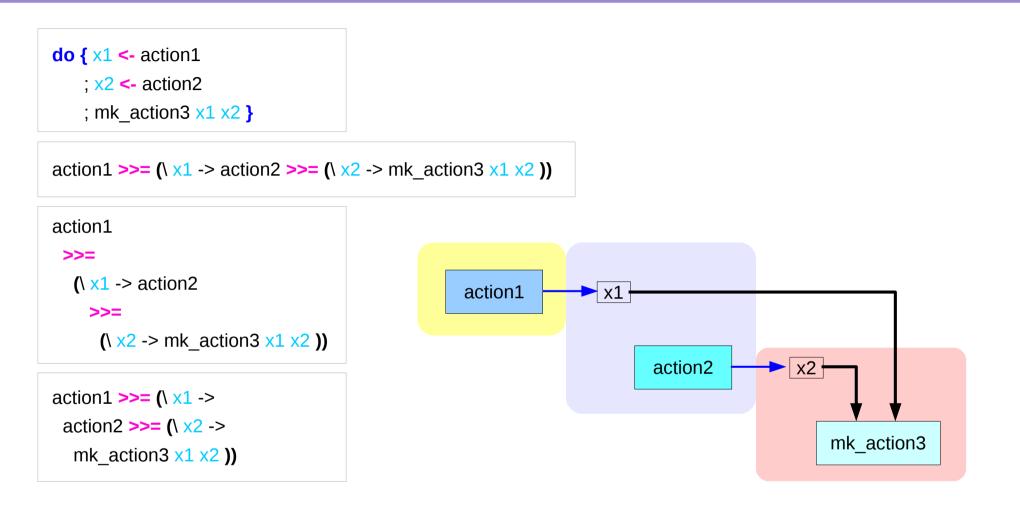
anonymous function (lambda expression) is used

do notation <u>assigns</u> a variable name to the passed value using the <-

do { x1 <- action1
 ; x2 <- action2
 ; mk_action3 x1 x2 }</pre>

https://en.wikibooks.org/wiki/Haskell/do_notation

Translation using the bind operator (>>=)

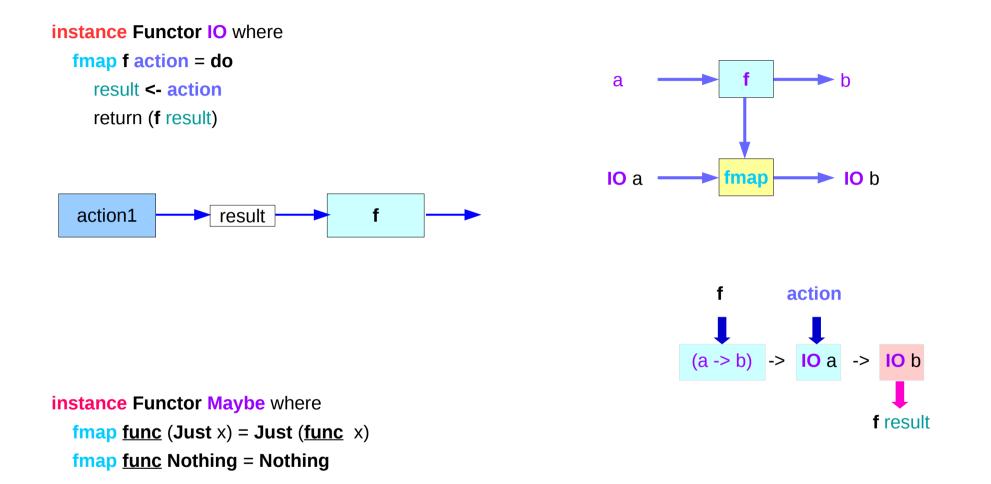


https://en.wikibooks.org/wiki/Haskell/do_notation

Anonymous Function

x -> x + 1	
(\ x -> x + 1) 4	
5 :: Integer	
(\ x y -> x + y) 3 5	
8 :: Integer	
	Lambda Expression
addOne = \x -> x + 1	

https://wiki.haskell.org/Anonymous_function



http://learnyouahaskell.com/functors-applicative-functors-and-monoids

Functor	(1A)
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main = do line <- getLine

let line' = reverse line
putStrLn \$ "You said " ++ line' ++ " backwards!"
putStrLn \$ "Yes, you really said" ++ line' ++ " backwards!"

main = do line <- fmap reverse getLine

putStrLn \$ "You said " ++ line ++ " backwards!" putStrLn \$ "Yes, you really said" ++ line ++ " backwards!"

instance Functor IO where

fmap f action = do
 result <- action
 return (f result)</pre>

fmap reverse getLine = do
 result <- getLine
 return (reverse result)</pre>

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\$ Operator

\$ operator to avoid parentheses

Anything appearing after \$ will take precedence over anything that comes before.

putStrLn (show (1 + 1))

putStrLn (show \$ 1 + 1)
putStrLn \$ show (1 + 1)
putStrLn \$ show \$ 1 + 1

https://stackoverflow.com/questions/940382/haskell-difference-between-dot-and-dollar-sign

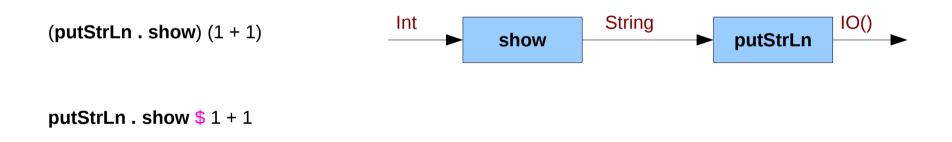


. Operator

. operator to chain functions

putStrLn (show (1 + 1))

(1 + 1) is not a function, so the . operator cannot be applied show can take an Int and return a String.putStrLn can take a String and return an IO().



https://stackoverflow.com/questions/940382/haskell-difference-between-dot-and-dollar-sign

Functor	(1A)
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instance Functor ((->) r) where
fmap f g = (\x -> f (g x))

A function takes any thing and returns any thing

g ∷ a -> b

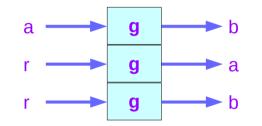
g ∷ r -> a

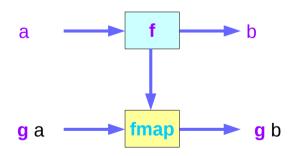
fmap :: (a -> b) -> f a -> f b fmap :: (a -> b) -> ((->) r a) -> ((->) r b) fmap :: (a -> b) -> (r -> a) -> (r -> b)

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Functor (1A)

instance Functor Maybe where
fmap f (Just x) = Just (f x)
fmap f Nothing = Nothing

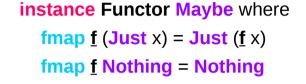


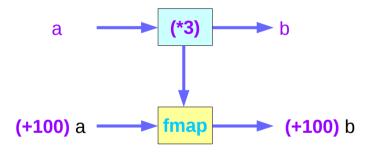


instance Functor ((->) r) where
fmap f g = (\x -> f (g x))

```
instance Functor ((->) r) where
fmap = (.)
```

```
ghci> :t fmap (*3) (+100)
fmap (*3) (+100) :: (Num a) => a -> a
ghci> fmap (*3) (+100) 1
303
ghci> (*3) `fmap` (+100) $ 1
303
ghci> (*3) . (+100) $ 1
303
ghci> fmap (show . (*3)) (*100) 1
"300"
```





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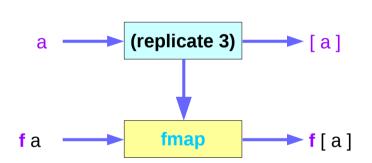
ghci> :t fmap (*2) fmap (*2) :: (Num a, Functor f) => f a -> f a

f a <u>fmap</u>

a

ghci> :t fmap (replicate 3) fmap (replicate 3) :: (Functor f) => f a -> f [a]

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(*2)

a

fa

ghci> fmap (replicate 3) [1,2,3,4] [[1,1,1],[2,2,2],[3,3,3],[4,4,4]]

```
ghci> fmap (replicate 3) (Just 4)
Just [4,4,4]
```

```
ghci> fmap (replicate 3) (Right "blah")
Right ["blah","blah","blah"]
```

```
ghci> fmap (replicate 3) Nothing
Nothing
```

```
ghci> fmap (replicate 3) (Left "foo")
Left "foo"
```

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Functor Laws

fmap id = id

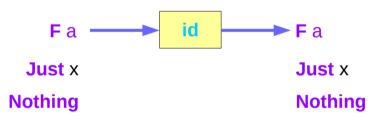
id :: a -> a id x = x a **id** a Fa **fmap** Fa

instance Functor Maybe where
fmap func (Just x) = Just (func x)
fmap func Nothing = Nothing

instance Functor Maybe where
fmap f (Just x) = Just (f x)
fmap f Nothing = Nothing

instance Functor Maybe where
fmap id (Just x) = Just (id x)
fmap id Nothing = Nothing

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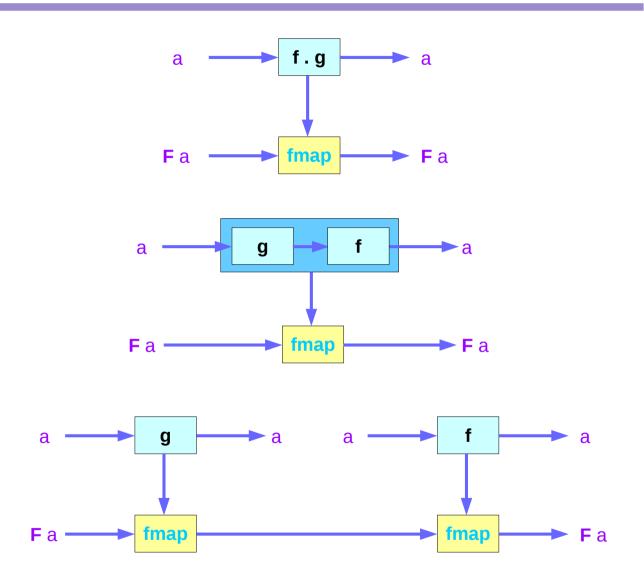
```
ghci> fmap id (Just 3)
Just 3
ghci> id (Just 3)
Just 3
ghci> fmap id [1..5]
[1,2,3,4,5]
ghci> id [1..5]
[1,2,3,4,5]
ghci> fmap id []
[]
ghci> fmap id Nothing
Nothing
```

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Functor Laws

fmap $(f \cdot g) = fmap f \cdot fmap g$

fmap (f . g) F = fmap f (fmap g F)



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Functor Laws

fmap (f . g) = fmap f . fmap g
fmap (f . g) F = fmap f (fmap g F)

```
instance Functor Maybe where
fmap f (Just x) = Just (f x)
fmap f Nothing = Nothing
```

```
fmap (f . g) Nothing = Nothing
fmap f (fmap g Nothing) = Nothing
```

fmap (f . g) (Just x) = Just ((f . g) x) = Just (f (g x)) fmap f (fmap g (Just x)) = fmap f (Just (g x)) = Just (f (g x))

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References

- [1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
- [2] https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf