

Multiple Random Variables

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February 14, 2019

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Based on
Probability, Random Variables and Random Signal Principles,
P.Z. Peebles,Jr. and B. Shi

Outline

1 Central Limit Theorem

Central Limit Theorem

Definition

the central limit theorem says that the probability distribution function of the sum of large number of random variables approaches a Gaussian distribution.

This theorem is known to apply some cases of statistically independent random variables.

Central Limit Theorem

Unequal Distribution Case

Definition

the sum Y of N independent random variables X_1, X_2, \dots, X_N
Let $Y = X_1 + X_2 + \dots + X_N$, then

$$\bar{Y}_N = \bar{X}_1 + \bar{X}_2 + \dots + \bar{X}_N$$

$$\sigma_{Y_N}^2 = \sigma_{X_1}^2 + \sigma_{X_2}^2 + \dots + \sigma_{X_N}^2$$

the probability distribution of Y asymptotically approaches
to Gaussian distribution function as $N \rightarrow \infty$

Definition

