## State Monad (3D)

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## Based on

Haskell in 5 steps
https://wiki.haskell.org/Haskell_in_5_steps

## State Monad

The Haskell type State describes functions
that take a state
and return both a result and an updated state, which are given back in a tuple.

The state function is wrapped by a data type definition which comes along with a runState accessor no need for pattern matching


```
newtype State s a = State \{ runState :: s-> (s, a) \}
    accessor
```

Control.Monad.Trans.State, transformers package. (focused here)
Control.Monad.State, mtl package.
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

## State Monad

newtype State s a = State \{ runState :: s -> (a, s) \}
$s$ : the type of the state,
a : the type of the produced result
s -> (a, s) : function type

## State String,

State Int,
State SomeLargeDataStructure, and so forth.

Calling the type State is arguably a bit of a misnomer because the wrapped value is not the state itself but a state processor (accessor function: runState)

## State Monad - state function

Control.Monad.Trans.State, transformers package. (focused here) no State constructor
but a state function
state :: (s -> (s, a)) -> State s a

Control.Monad.State, mtl package
Implements the State in somewhat different way

## Instantiating a State Monad

to wrap a function type and give it a name.
for every type s, State s can be made a Monad instance,
the instance is State s, and not just State
(State can't be made an instance of Monad, as it takes two type parameters, rather than one.)

```
newtype State s a = State { runState :: s -> (s, a) }
instance Monad (State s) where
    return
    (>>=);
```

State String, State Int,
State SomeLargeDataStructure, and so forth.

## Instantiating a State Monad

```
instance Monad (State s) where
many different State monads,
one for each possible type of state -
    State String,
    State Int,
    State SomeLargeDataStructure,
    and so forth.
```

only need to write one implementation of
return and
(>>=);
these methods will be able to deal with all choices of $s$.

## State Monad - return method

```
instance Monad (State s) where
return :: a -> State s a
return x = state ( \ s -> (x, s) )
giving a value (x) to return produces a function state
which takes a state (s) and returns it unchanged,
together with value x we want to be returned.
As a finishing step, the function is wrapped up with the state function.
state :: (s -> (a, s)) -> State s a
newtype State s a = State { runState :: s -> (s, a) }
```


## State Monad - binding operator

```
instance Monad (State s) where
(>>=) :: State s a -> (a -> State s b) -> State s b
p >>= k = q where
    p' = runState p -- p' :: s -> (a, s)
    k' = runState . k -- k':: a -> s -> (b, s)
    q' s0 = (y, s2) where -- q':: s -> (b, s)
        (x, s1) = p' s0 -- (x, s1) :: (a, s)
        (y,s2)=\mp@subsup{\mathbf{k}}{}{\prime}xs1 -- (y, s2) :: (b, s)
    q = state q'
```

p >>= k = state \$ $\mathbf{~ s 0 ~ - > ~}$
let $(x, s 1)=$ runState $p$ s0 $\quad-$ running the first processor on s 0 .
in runState $(k x)$ s1 -- running the second processor on s1.
https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

## State Monad - binding operator

instance Monad (State s) where
(>>=) :: State s a -> (a -> State s b) -> State sb
p >>= $\mathbf{k}$ = q where

$$
\begin{array}{ll}
\mathbf{p}^{\prime}=\text { runState } p & --\mathrm{p}^{\prime}:: \mathrm{s}->(\mathrm{a}, \mathrm{~s}) \\
\mathbf{k}^{\prime}=\text { runState } \cdot \mathbf{k} & --\mathrm{k}^{\prime}:: \mathrm{a}->\mathrm{s}->(\mathrm{b}, \mathrm{~s}) \\
\mathbf{q}^{\prime} \text { s0 }=(\mathrm{y}, \text { s2) where } & --\mathrm{q}^{\prime}:: \mathrm{s}->(\mathrm{b}, \mathrm{~s}) \\
\quad(\mathrm{x}, \mathrm{~s} 1)=\mathbf{p}^{\prime} \mathrm{s} 0 & --(\mathrm{x}, \mathrm{~s} 1)::(\mathrm{a}, \mathrm{~s}) \\
\quad(\mathrm{y}, \mathrm{~s} 2)=\mathbf{k}^{\prime} \times \mathrm{s} 1 & --(\mathrm{y}, \mathrm{~s} 2)::(\mathrm{b}, \mathrm{~s}) \\
\mathbf{q}=\text { state } \mathbf{q}^{\prime}
\end{array}
$$

newtype State s a = State \{ runState :: s -> (s, a) \}
state :: (s -> (a, s)) -> State s a


## State Monad - binding operator

```
instance Monad (State s) where
(>>=) :: State s a -> (a -> State s b) -> State s b
p >>= k = q where
    q = state q'
```

```
    \(\mathbf{p}^{\prime}=\) runState \(\mathrm{p} \quad--\mathrm{p}\) ':: s -> \((\mathrm{a}, \mathrm{s})\)
```

    \(\mathbf{p}^{\prime}=\) runState \(\mathrm{p} \quad--\mathrm{p}\) ':: s -> \((\mathrm{a}, \mathrm{s})\)
    \(\mathbf{k}^{\prime}=\) runState . \(\mathbf{k} \quad--k^{\prime}::\) a -> s -> (b, s)
    \(\mathbf{k}^{\prime}=\) runState . \(\mathbf{k} \quad--k^{\prime}::\) a -> s -> (b, s)
    \(\mathbf{q}^{\mathbf{\prime}} \mathbf{~} \mathbf{0}\) = ( \(\mathrm{y}, \mathbf{s} \mathbf{2}\) ) where \(\quad--\mathrm{q}\) ':: s -> (b, s)
    \(\mathbf{q}^{\mathbf{\prime}} \mathbf{~} \mathbf{0}\) = ( \(\mathrm{y}, \mathbf{s} \mathbf{2}\) ) where \(\quad--\mathrm{q}\) ':: s -> (b, s)
        \((x, \mathrm{~s} 1)=\mathbf{p}^{\prime} \mathrm{s} 0 \quad--(\mathrm{x}, \mathrm{s} 1)::(\mathrm{a}, \mathrm{s})\)
        \((x, \mathrm{~s} 1)=\mathbf{p}^{\prime} \mathrm{s} 0 \quad--(\mathrm{x}, \mathrm{s} 1)::(\mathrm{a}, \mathrm{s})\)
        \((y, s 2)=\mathbf{k}^{\prime} x \mathrm{~s} 1 \quad--(\mathrm{y}, \mathrm{s} 2)::(b, s)\)
    ```
        \((y, s 2)=\mathbf{k}^{\prime} x \mathrm{~s} 1 \quad--(\mathrm{y}, \mathrm{s} 2)::(b, s)\)
```



```
newtype State s a = State \{ runState :: s -> (s, a) \}
state :: (s -> (a, s)) -> State s a
```


## References

[1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
[2] https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf


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