

Quizbank/Electricity and Magnetism (calculus based)/Equations

- These equations^[1] can be given to students as they take chapter quizzes based on examples in the textbook **OpenStax University Physics**
- A study guide for these quizzes can be found at **Quizbank/Electricity and Magnetism (calculus based)**
- Most solutions for the questions can be found by reading the examples in Unit 2 of the **textbook**. (<https://cnx.org/contents/eg-XcBxE@10.1:Gofkr9Oy@18/Preface>)

Chapter 5

$\epsilon_0 = 8.85 \times 10^{-12}$ F/m = vacuum permittivity.

$e = 1.602 \times 10^{-19}$ C; negative (positive) charge for electrons (protons)

$$\vec{F} = Q\vec{E} \text{ where } \vec{E} = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^N \frac{q_i}{r_{Pi}^2} \hat{r}_{Pi}$$

$$\vec{E} = \int \frac{dq}{r^2} \hat{r} \text{ where } dq = \lambda dl = \sigma da = \rho dV$$

$$E = \frac{\sigma}{2\epsilon_0} = \text{field above an infinite plane of charge.}$$

Chapter 6

$$\Phi = \vec{E} \cdot \vec{A} \rightarrow \int \vec{E} \cdot d\vec{A} = \int \vec{E} \cdot \hat{n} dA = \text{electric flux}$$

$$q_{\text{enclosed}} = \epsilon_0 \oint \vec{E} \cdot d\vec{A}$$

$$d\text{Vol} = dx dy dz = r^2 dr dA \text{ where } dA = r^2 d\phi d\theta$$

$$A_{\text{sphere}} = r^2 \int_0^\pi \sin \theta d\theta \int_0^{2\pi} d\phi = 4\pi r^2$$

Chapter 7

$$\Delta V_{AB} = V_A - V_B = - \int_A^B \vec{E} \cdot d\vec{l} = \text{electric potential}$$

$$\vec{E} = - \frac{\partial V}{\partial x} \hat{i} - \frac{\partial V}{\partial y} \hat{j} - \frac{\partial V}{\partial z} \hat{k} = -\vec{\nabla} V$$

$q\Delta V = \text{change in potential energy}$

Electron (proton) mass = 9.11×10^{-31} kg (1.67×10^{-27} kg).

$$K = \frac{1}{2} m v^2 = \text{kinetic energy. } 1 \text{ eV} = 1.602 \times 10^{-19} \text{ J}$$

$$V(r) = k \frac{q}{r} \text{ near isolated point charge}$$

$$\text{Many charges: } V_P = k \sum_1^N \frac{q_i}{r_i} \rightarrow k \int \frac{dq}{r}$$

Chapter 8

$Q = CV$ defines capacitance.

$C = \epsilon_0 \frac{A}{d}$ where A is area and $d \ll A^{1/2}$ is gap length of parallel plate capacitor

Series: $\frac{1}{C_s} = \sum \frac{1}{C_i}$. **Parallel:** $C_P = \sum C_i$.

$$u = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2} Q^2 = \text{stored energy}$$

$$u_E = \frac{1}{2} \epsilon_0 E^2 = \text{energy density}$$

Chapter 9

Electric current: 1 Amp (A) = 1 Coulomb (C) per second (s)

$$\text{Current} = I = \frac{dQ}{dt} = nqv_d A, \text{ where}$$

(n, q, v_d, A) = (density, charge, speed, Area)

$$I = \int \vec{J} \cdot d\vec{A} \text{ where } \vec{J} = nq\vec{v}_d = \text{current density.}$$

$\vec{E} = \rho\vec{J}$ = electric field where ρ = resistivity

Chapter 10

$V_{terminal} = \varepsilon - Ir_{eq}$ where r_{eq} = internal resistance and $\varepsilon = emf$.

$$R_{series} = \sum_{i=1}^N R_i \text{ and } R_{parallel}^{-1} = \sum_{i=1}^N R_i^{-1}$$

Kirchhoff Loop: $\sum I_{in} = \sum I_{out}$ and Junction: $\sum V = 0$

Chapter 11

$|\vec{a} \times \vec{b}| = ab \sin \theta \Leftrightarrow$

$$(\vec{a} \times \vec{b})_x = (a_y b_z - a_z b_y),$$

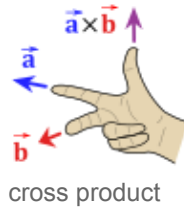
$$(\vec{a} \times \vec{b})_y = (a_z b_x - a_x b_z),$$

$$(\vec{a} \times \vec{b})_z = (a_x b_y - a_y b_x)$$

Magnetic force: $\vec{F} = q\vec{v} \times \vec{B}$,

$$d\vec{F} = I d\vec{\ell} \times \vec{B}.$$

$$\vec{v}_d = \vec{E} \times \vec{B} / B^2 = \text{EXB drift velocity}$$



cross product

$$\rho = \rho_0 [1 + \alpha(T - T_0)], \text{ and } R = R_0 [1 + \alpha\Delta T],$$

where $R = \rho \frac{L}{A}$ is resistance

$$V = IR \text{ and Power} = P = IV = I^2 R = V^2 / R$$

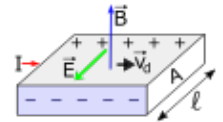
Charging an RC (resistor-capacitor) circuit:
 $q(t) = Q(1 - e^{-t/\tau})$ and $I = I_0 e^{-t/\tau}$ where $\tau = RC$ is RC time, $Q = \varepsilon C$ and $I_0 = \varepsilon / R$.

Discharging an RC circuit: $q(t) = Qe^{-t/\tau}$ and $I(t) = -\frac{Q}{RC}e^{-t/\tau}$

Circular motion (uniform B field): $r = \frac{mB}{qB}$. Period = $T = \frac{2\pi m}{qB}$.

Dipole moment = $\vec{\mu} = NIA\hat{n}$. Torque = $\vec{\tau} = \vec{\mu} \times \vec{B}$. Stored energy = $U = \vec{\mu} \cdot \vec{B}$.

Hall field = $E = V/\ell = Bv_d = \frac{IB}{neA}$



Hall effect

Chapter 12

Free space permeability $\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m/A}$

Force between parallel wires $\frac{F}{\ell} = \frac{\mu_0 I_1 I_2}{2\pi r}$

$$\text{Biot-Savart law } \vec{B} = \frac{\mu_0}{4\pi} \int_{\text{wire}} \frac{I d\vec{\ell} \times \hat{r}}{r^2}$$

(find's field at center of loop)

Ampère's Law: $\oint \vec{B} \cdot d\vec{\ell} = 4\pi\mu_0 I_{enc}$ (for straight wire, solenoid, toroid)

Magnetic field inside solenoid with paramagnetic material = $B = \mu nI$ where $\mu = (1 + \chi)\mu_0 = \text{permeability}$

Chapter 13

Magnetic flux $\Phi_m = \int_S \vec{B} \cdot \hat{n} dA$

Motional $\varepsilon = Blv$ if $\vec{v} \perp \vec{B}$

$$\text{Electromotive "force" (volts) } \varepsilon = -N \frac{d\Phi_m}{dt} = \oint \vec{E} \cdot d\vec{\ell}$$

rotating coil $\varepsilon = NBA\omega \sin \omega t$

Chapter 14

Unit of inductance = Henry (H) = $1 \text{ V}\cdot\text{s/A}$

Mutual inductance: $M \frac{dI_2}{dt} = N_1 \frac{d\Phi_{12}}{dt} = -\varepsilon_1$ where Φ_{12} = flux through 1 due to current in 2. Reciprocity: $M \frac{dI_1}{dt} = -\varepsilon_2$

Self-inductance: $N\Phi_m = LI \rightarrow \epsilon = -L \frac{dI}{dt}$

$I(t) = \frac{\epsilon}{R} (1 - e^{-t/\tau})$ in LR circuit where $\tau = L/R$.

$L_{\text{solenoid}} \approx \mu_0 N^2 A \ell$, $L_{\text{toroid}} \approx \frac{\mu_0 N^2 h}{2\pi} \ln \frac{R_2}{R_1}$, Stored energy = $\frac{1}{2} LI^2$

$q(t) = q_0 \cos(\omega t + \phi)$ in LC circuit where $\omega = \sqrt{\frac{1}{LC}}$

Chapter 15

AC voltage and current $v = V_0 \sin(\omega t - \phi)$ if $i = I_0 \sin \omega t$.

RMS values $I_{rms} = \frac{I_0}{\sqrt{2}}$ and $V_{rms} = \frac{V_0}{\sqrt{2}}$

Impedance $V_0 = I_0 X$

Resistor $V_0 = I_0 X_R$, $\phi = 0$, where $X_R = R$

Capacitor $V_0 = I_0 X_C$, $\phi = -\frac{\pi}{2}$, where $X_C = \frac{1}{\omega C}$

Inductor $V_0 = I_0 X_L$, $\phi = +\frac{\pi}{2}$, where $X_L = \omega L$

RLC series circuit $V_0 = I_0 Z$ where $Z = \sqrt{R^2 + (X_L^2 - X_C^2)}$

and $\phi = \tan^{-1} \frac{X_L - X_C}{R}$

Resonant angular frequency $\omega_0 = \sqrt{\frac{1}{LC}}$

Quality factor $Q = \frac{\omega_0}{\Delta\omega} = \frac{\omega_0 L}{R}$

Average power $P_{ave} = \frac{1}{2} I_0 V_0 \cos \phi = I_{rms} V_{rms} \cos \phi$

Transformer voltages and currents $\frac{V_S}{V_P} = \frac{N_S}{N_P} = \frac{I_P}{I_S}$

Chapter 16

Displacement current $I_d = \epsilon_0 \frac{d\Phi_E}{dt}$ where $\Phi_E = \int \vec{E} \cdot d\vec{A}$ is the electric flux.

Maxwell's equations: $\epsilon_0 \mu_0 = 1/c^2$

$$\oint_S \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} Q_{in}$$

$$\oint_S \vec{B} \cdot d\vec{A} = 0$$

$$\oint_C \vec{E} \cdot d\vec{l} = - \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{A}$$

$$\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I + \epsilon_0 \mu_0 \frac{d\Phi_E}{dt}$$

$$\frac{\partial^2 E_y}{\partial x^2} = \epsilon_0 \mu_0 \frac{\partial^2 E_y}{\partial t^2} \text{ and } \frac{E_0}{B_0} = c$$

Poynting vector $\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$ = energy flux

Average intensity $I = S_{ave} = \frac{c\epsilon_0}{2} E_0^2 = \frac{c}{2\mu_0} B_0^2 = \frac{1}{2\mu_0} E_0 B_0$

Radiation pressure $p = I/c$ (perfect absorber) and $p = 2I/c$ (perfect reflector).

1. transclusions *between* [OpenStax_University_Physics/E&M#Index](https://en.wikiversity.org/wiki/OpenStax_University_Physics/E&M#Index) and [Quizbank/Electricity and Magnetism \(calculus based\)/Equations](https://en.wikiversity.org/wiki/Quizbank/Electricity_and_Magnetism_(calculus_based)/Equations)

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