Multiple Linear Regression II



Lecture 8 Survey Research & Design in Psychology James Neill, 2017 Creative Commons Attribution 4.0

Overview

- 1. Summary of MLR I lecture
- 2. Semi-partial correlations
- 3. Residual analysis
- 4. Interactions
- 5. Analysis of change
- 6. Writing up an MLR
- 7. Summary of MLR II
- 8. MLR II quiz Practice questions 2

Readings

- 1. As per previous lecture, plus
- 2. Howitt & Cramer (2014)
 - Ch 39: Moderator variables and relationships between two variables

Summary of MLR I lecture

Purpose of MLR:

- To examine linear relations between:
 - -two or more predictors (IVs; X) and
 - -a single outcome variable (DV; Y)

Model:

Develop a theoretical model:

- Path diagram and/or Venn diagram
- Express as one hypothesis per IV

3

Summary of MLR I

Check assumptions:

- Level of measurement
- Sample size
- Normality
- Linearity
- Homoscedasticity
- Collinearity
- Multivariate outliers
- Residuals should be normally distributed

5

Summary of MLR I

Choose type:

- Standard
- Hierarchical
- Stepwise, Forward, Backward



6

Summary of MLR I

Interpret output:

Overall:

- -R, R^2 , Adjusted R^2
- -Changes in R^2 (if hierarchical)
- -Significance (F, p)
- · For each IV:
 - Standardised coefficient - size, direction and significance
 - Unstandardised coefficient - report equation (if useful)
 - -Semi-partial correlations (sr²)

Semi-partial correlation

IV1

Venn Diagrams depict variance and shared variance:

- a + b + c + d = variance in DV
- a + b + c = R (variance in the DV
- explained by IV1 and IV2)

7

9

- a + c = uniquely explained variance
 b = non-uniquely explained variance
- D non-uniquely explained variance
- a and c are semi-partial correlations (*sr*):



Semi-partial correlations in MLR

When interpreting MLR coefficients:

- Draw a Path diagram or Venn diagram
- Compare 0-order (r) and semi-partial correlations (sr) for each IV to help understand relations amongst the IVs and the DV:
 - A semi-partial correlation (sr) will be less than or equal to the correlation (r)
 - If a srequals a r, then the IV independently predicts the DV
 - To the extent that a sr is less than the r, the IV's explanation of the DV is shared with other IVs
 An IV exclusion a significant swith the DV but a new piperificant
 - An IV may have a significant r with the DV, but a non-significant sr. This indicates that the unique variance explained by the IV may be 0.
- Compare the relative importance of the predictors using betas and/or *sr*s

Semi-partial correlations (*sr*) in MLR

- SPSS provides semi-partial correlations if selected (labelled "part")
- Square sr to get sr^2 .
- The sr² indicates the % of variance in the DV which is uniquely explained by an IV..
- Compare each *sr*² with the *r*² do they differ why?

10

DV

8

а

С

d

b

Semi-partial correlations for MLR in SPSS

Analyze - Linear Regression - Statistics -Part and partial correlations





Semi-partial correlations for MLR in

Semi-partial correlations (*sr*) indicate the relative importance of each of the predictors; sr^2 indicate the % of variance uniquely explained by each predictorg.

Summary: Semi-partial correlation (sr)

- 1. In MLR, sr is labelled "part" in the regression coefficients table SPSS output
- 2. Square these values to obtain sr^2 , the unique % of DV variance explained by each IV
- 3. Discuss the extent to which the explained variance in the DV is due to unique or shared contributions of the IVs

Semi-partial correlations (sr) in MLR • $R^2 = .34$

• 16% is of the DV variance is uniquely explained by the IVs (sum of sr^2s)

• 18% of the DV

of sr²s)

16% is of the DV		
variance is uniquely	Independent variables	sr ²
explained by the IVs	Not Coping (NC)	.07
(sum of <i>sr</i> ²s)	Somatic Coping (SC)	.06
18% of the DV	Wishful Thinking (WT)	.02
by the combination	Worry (W)	.01
of the IVs (R^2 - sum		

14













Standardized Residual

Regression





Why the big fuss about residuals?

- Standard error formulae (used for confidence intervals and sig. tests) WOrk when residuals are well-behaved.
- If the residuals don't meet assumptions these formulae tend to underestimate coefficient standard errors giving lower *p*-values and more Type I errors.

23

Summary: Residual analysis

- 1. Residuals are the difference between predicted and observed Y values
- 2. MLR assumption is that residuals are normally distributed.
- 3. Examining residuals also helps to assess:
 - 1. Linearity
 - 2. Homoscedasticity

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Interactions

- Additivity when IVs act independently on a DV they do not interact.
- Alternatively, there may be interaction effects - i.e. the magnitude of the effect of one IV on a DV varies as a function of a second IV.

Interactions: Example 2

Physical exercise (IV1)

and Natural environments (IV2)

may provide

multiplicative benefits

in reducing stress e.g.,

Natural env. x Phys. ex. $\rightarrow \downarrow \downarrow \downarrow \downarrow$ Stress

Natural environment $\rightarrow \downarrow$ Stress Physical exercise $\rightarrow \downarrow$ Stress

• Also known as a moderation effect.

26

Interactions: Example 1

Some drugs interact with each other to reduce or enhance other's effects e.g.,

 $\mathsf{Pseudoephedrine} \to \uparrow \mathsf{Arousal}$

Caffeine $\rightarrow \uparrow$ Arousal

Pseudoeph. X Caffeine $\rightarrow \uparrow\uparrow\uparrow$ Arousal





27

Interactions: Example 3

University student satisfaction (IV1) and Level of coping (IV2) may predict level of stress e.g., Satisfaction $\rightarrow \downarrow$ Stress Coping $\rightarrow \downarrow$ Stress Satisfaction x Coping $\rightarrow \downarrow \downarrow \downarrow \downarrow$ Stress (Dissatisfaction x Not coping $\rightarrow \uparrow \uparrow \uparrow$ Stress)

Interactions

Test interactions in MLR by computing a cross-product term e.g.,:

- Pseudoephedrine (IV1)
- Caffeine (IV2)
- Pseudoephedrine x Caffeine (IV3)

Interactions

 $Y = b_1 x_1 + b_2 x_2 + b_{12} x_{12} + a + e$ • b_{12} is the product of the first two slopes $(b_1 x b_2)$

*b*₁₂ can be interpreted as the amount of change in the slope of the regression of Y on *b*₁ when *b*₂ changes by one unit.

Interactions

- Conduct Hierarchical MLR –Step 1:
 - Pseudoephedrine
 - Caffeine
 - -Step 2:
 - Pseudo x Caffeine (cross-product)
- Examine ΔR^2 , to see whether the interaction term explains additional variance above and beyond the additive effects of Pseudo and Caffeine. 32





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	R	R Sa	lare	Adjusted R Square		Std. Error of the Estimate	R Sc Cha	uare
1	5434	11.040	295	. 288		17 34399		295
2	.547 ^b		299	19 289		17.33241		.004
a. Pr	edictors: (Co	nstant)	Caffeir	ne, Ps	eudoepheo	frine		\sim
b. Pr	edictors: (Co	nstant)	Caffeir	ne, Ps	eudoepheo	frine PseudoC	affeine inte	eraction
dodel		Unstandardized Coefficients		Standardized Coefficients				
		В	Std. Error		Beta	t	Sig.	
	(Constant)		57	7 705	5 1 0 2		11.296	.000
(C	onstant)		57					
(Ci Ps	onstant) eudoephedrine		11	1.511	1.510	.464	7.625	.000
(Ci Ps Ca	onstant) eudoephedrine ffeine		11	1.511 4.735	1.510	.464	7.625 2.660	.000 .008
(C) Ps Ca	onstant) eudoephedrine ffeine onstant)		5/ 11 42	1.611 4.735 2.730	1.510 1.780 14.137	.464	7.625 2.660 3.023	.000 .008 .003
(C) Ps Ca (C) Ps	onstant) eudoephedrine ffeine onstant) eudoephedrine		42 11	1.611 1.735 2.730 3.137	1.510 1.780 14.137 6.025	.464 .162	7.625 2.660 3.023 3.010	.000 .008 .003 .003
(Ci Ps Ca (Ci Ps Ca	onstant) eudoephedrine ffeine onstant) eudoephedrine ffeine.		53 11 43 18 10	1.511 4.735 2.730 3.137 0.126	1.510 1.780 14.137 6.025 5.069		7.625 2.660 3.023 3.010 1.998	.000 .008 .003 .003 .047

Interactions

Possible effects of Pseudo and Caffeine on Arousal:

- None
- Pseudo only (↑/↓)
- Caffeine only (↑/↓)
- Pseudo + Caffeine $(\uparrow\uparrow/\downarrow\downarrow)$
- Pseudo x Caffeine (^{↑↑↑} (synergistic))
- Pseudo x Caffeine (\\\ (antagonistic))

33

Interactions

- Cross-product interaction terms may be highly correlated (collinear) with the corresponding simple IVs, creating problems with assessing the relative importance of main effects and interaction effects.
- An alternative approach is to conduct separate regressions for each level of one of the IVs e.g.,
 - What is the effect of caffeine on Arousal without pseudephedrine?
 - What is the effect of caffeine on Arousal with pseudephedrine? 37

Summary: Interactions

- In MLR, IVs may interact to:
 Increase the IVs' effect on DV
 Decrease the IVs' effect on DV
- 2. Model interactions using hierarchical MLR:
 - 1. Step 1: Enter IVs
 - 2. Step 2: Enter cross-product of IVs
 - 3. Examine change in R^2

38



Analysis of change

Example research question: Does the quality of social support (IV2) explain changes in mental health (MH) between the beginning (IV1) and end (DV) of an intervention 2





Analysis of change: Option 2

Hierarchical MLR

• **DV** = Mental health after the intervention

-IV1 = Mental health before the

-IV2 = Support from group members

44

46

Analysis of change: Option 2

Results of interest

- Change in R^2 amount of additional variance in the DV (MH2) explained by the predictor (IV2) added in Step 2 (after having baseline IV1 variance has been accounted for in Step 1)
- Regression coefficients for the predictor (IV2) in Step 2 - indicates variance explained in the DV (MH2) by the IV (SS) after controlling for baseline MH (MH1) in Step 1

45

Summary: Analysis of change

- 1. Analysis of changes over time can be assessed by:
 - 1. Standard regression
 - 1. Calculate difference scores (Post-score minus Pre-score) and use as a DV
 - 2. Hierarchical MLR
 - 1. Step 1: "Partial out" baseline scores 2. Step 2: Enter other IVs to help predict

variance in changes over time.



Writing up an MLR: Intro

- Explain the constructs of interest and why they are important
- Explain how / why the IVs may be related to the DV, drawing on theory and research
- State hypotheses (one per IV) -Null hypothesis or
 - -Directional hypothesis

Writing up an MLR: Results

- Establish the purpose of the analysis
- Provide univariate descriptive statistics (*M*, *SD*, Skewness, Kurtosis) for the IVs and DV
- Describe type of MLR
- Test assumptions
- Examine correlations
- Overall model: R², Adjusted R², F, p
- Explain regression coefficients
- Provide table of correlations and regression coefficients (unstandardised and standardised), *t*, *p*, and *sr*² values

49

Writing up an MLR: Discussion

- Summarise the results in relation to the hypotheses and the overall research question, paying attention to:
 - Direction
 - Size
 - Statistical significance
- Interpret the results in the context of relevant psychological theory and research
- Consider alternative explanations and limitations
- Describe implications and/or recommendations

50

Table of regression coefficients

Table 2

Standard Multiple Linear Regression of Non-productive Coping Strategies on Psychological Distress Reported by Adolescents During Outdoor Education Programs

Variables	PD ^a (DV)	NC	WT	W	SC	В	β	sr ^{2b}
						(unique)		
Not Coping (NC)	.43					.41*	.29	.07
Wishful Thinking (WT)	.38	.36				.15*	.15	.02
Worry (W)	.36	.25	.40			.13*	.13	.01
Somatic Coping (SC)	.42	.22	.30	.38		.26*	.26	.06
Intercept						.60*		

Summary: Writing up an MLR

1. Introduction

- Establish purpose
- 2. Describe model and hypotheses

2. Results

- 1. Univariate descriptive statistics
- 2. Correlations
- 3. Type of MLR and assumptions
- 4. Regression coefficients
- 3. Discussion
 - Summarise and interpret, with limitations
 Implications and recommendations

52



MLR II Quiz – Practice question 1

In an MLR, if the *r* between the two IVs is 1, *R* will equal the *r* between one of the IVs and the DV.

[Hint: Draw a Venn Diagram]

- a) True
- b) False

3

MLR II Quiz – Practice question 2

In MLR, if two IVs are somewhat correlated with the DV and with one another, the *sr*s between the IVs and the DV will be ______ in magnitude than the *r*s:

[Hint: Draw a Venn Diagram]

- a) Equal
- b) Smaller
- c) Larger

d) Impossible to tell

MLR II Quiz – Practice question 3

In MLR, the unique variance in the DV explained by a particular IV is estimated by its:

- a) Zero-order correlation square (r^2)
- b) Multiple correlation coefficient squared (R^2)
- c) Semi-partial correlation squared (sr²)

56

MLR II Quiz – Practice question 4

Interaction effects can be tested in MLR by using IVs that represent:

- a) Cross-products between the IVs and DV in a hierarchical regression
- b) Cross-products of IVs
- c) Semi-partial correlations squared (sr²)

57

55

MLR II Quiz – Practice question 5

To assess the extent to which social support from group members during an intervention program explain changes in mental health (MH) between the beginning and end of an intervention program, what MLR design could be used?

a) Hierarchical with pre-MH in Step 1

b) Hierarchical with cross-products of IVs in Step 2 58

References

- Allen, P. & Bennett, K. (2008). SPSS for the health and behavioural sciences. South Melbourne, Victoria, Australia: Thomson.
- Francis, G. (2007). *Introduction to SPSS for Windows: v. 15.0 and 14.0 with Notes for Studentware* (5th ed.). Sydney: Pearson Education.
- Howell, D. C. (2010). Statistical methods for psychology (7th ed.). Belmont, CA: Wadsworth.
- Howitt, D. & Cramer, D. (2011). Introduction to statistics in psychology (5th ed.). Harlow, UK: Pearson.

59

Next lecture

- Statistical power
- Significance testing
- Inferential decision making
- Effect sizes
- Confidence intervals
- Publication bias
- Academic integrity

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