

# Correlation



Image source: <http://commons.wikimedia.org/wiki/File:Gnome-power-statistics.svg>, GPL

## Lecture 4

Survey Research & Design in Psychology

James Neill, 2015

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## Overview



1. Covariation
2. Purpose of correlation
3. Linear correlation
4. Types of correlation
5. Interpreting correlation
6. Assumptions / limitations
7. Dealing with several correlations

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## Readings

### Howitt & Cramer (2011/2014)

- Ch 6/7: Relationships between two or more variables: Diagrams and tables
- Ch 7/8: Correlation coefficients: Pearson correlation and Spearman's rho
- Ch 10/11: Statistical significance for the correlation coefficient: A practical introduction to statistical inference
- Ch 14/15: Chi-square: Differences between samples of frequency data
- **Note:** Howitt and Cramer doesn't cover point bi-serial correlation<sup>3</sup>

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## Covariation

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e.g., pollen and bees

e.g., study and grades

e.g., nutrients and growth

The world is made of  
covariations

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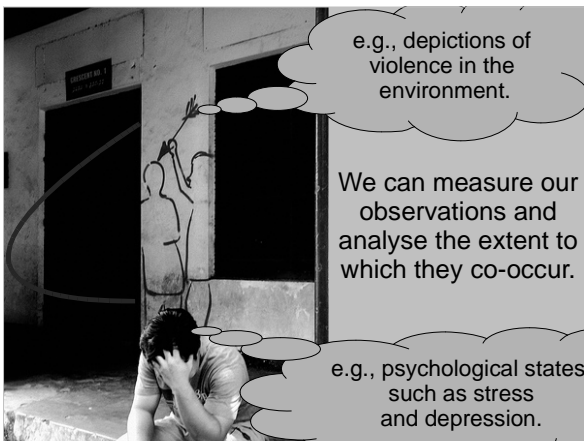
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Covariations are the basis of more complex models.

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**Purpose of correlation**

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**Purpose of correlation**  
The underlying purpose of correlation is to help address the question:  
What is the  
• **relationship** or  
• **association** or  
• **shared variance** or  
• **co-relation**  
between **two variables**?

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## Purpose of correlation

Other ways of expressing the underlying correlational question include:

To what extent do variables

- **covary**?
- **depend** on one another?
- **explain** one another?

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## Linear correlation

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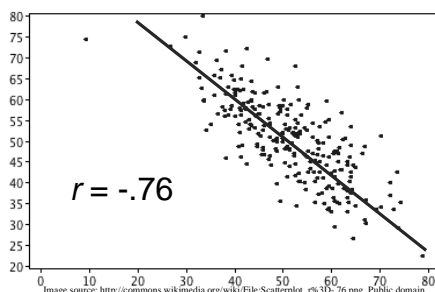
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## Linear correlation

The extent to which two variables have a simple **linear** (straight-line) relationship.



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## Linear correlation

Linear relations between variables are indicated by correlations:

- **Direction:** Correlation sign (+ / -) indicates direction of linear relationship
- **Strength:** Correlation size indicates strength (ranges from -1 to +1)
- **Statistical significance:**  $p$  indicates likelihood that the observed relationship could have occurred by chance

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## What is the linear correlation? Types of answers

- No relationship ( $r = 0$ )  
(X and Y are independent)
- Linear relationship  
(X and Y are dependent)
  - As X ↑s, so does Y ( $r > 0$ )
  - As X ↑s, Y ↓s ( $r < 0$ )
- Non-linear relationship

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## Types of correlation

To decide which type of correlation to use, consider the **levels of measurement** for each variable.

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## Types of correlation

- Nominal by nominal:  
Phi ( $\Phi$ ) / Cramer's  $V$ , Chi-squared
- Ordinal by ordinal:  
Spearman's rank / Kendall's Tau  $b$
- Dichotomous by interval/ratio:  
Point bi-serial  $r_{pb}$
- Interval/ratio by interval/ratio:  
Product-moment or Pearson's  $r$

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## Types of correlation and LOM

|           | Nominal  | Ordinal   | Int/Ratio   |
|-----------|--|---|---|
| Nominal   | Clustered bar-chart,<br>Chi-square,<br>Phi ( $\phi$ ) or<br>Cramer's $V$ | ← Recode  | Scatterplot,<br>bar chart<br>Point bi-serial<br>correlation<br>( $r_{pb}$ ) |
| Ordinal   |  | Scatterplot or<br>clustered bar<br>chart<br>Spearman's<br>Rho or<br>Kendall's Tau | ← ↑ Recode  |
| Int/Ratio |  |   | Scatterplot<br>Product-<br>moment<br>correlation (17)                       |

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## Nominal by nominal

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## Nominal by nominal correlational approaches

- Contingency (or cross-tab) tables
  - Observed
  - Expected
  - Row and/or column %s
  - Marginal totals
- Clustered bar chart
- Chi-square
- Phi/Cramer's V

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## Contingency tables

- Bivariate frequency tables
- Cell frequencies (red)
- Marginal totals (blue)

|         |             | Disease  |       |       |
|---------|-------------|----------|-------|-------|
|         |             | Diseased | Free  |       |
| Exposed | Exposed     | a        | b     | $n_1$ |
|         | Not Exposed | c        | d     | $n_0$ |
|         |             | $m_1$    | $m_0$ | n     |

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## Contingency table: Example

b2 Do you snore? \* b3r Smoker Crosstabulation

| Count            |       | b3r Smoker |       | Total |
|------------------|-------|------------|-------|-------|
|                  |       | 0 No       | 1 Yes |       |
| b2 Do you snore? | 0 yes | 50         | 16    | 66    |
|                  | 1 no  | 111        | 9     | 120   |
| Total            |       | 161        | 25    | 186   |

RED = Contingency cells

BLUE = Marginal totals

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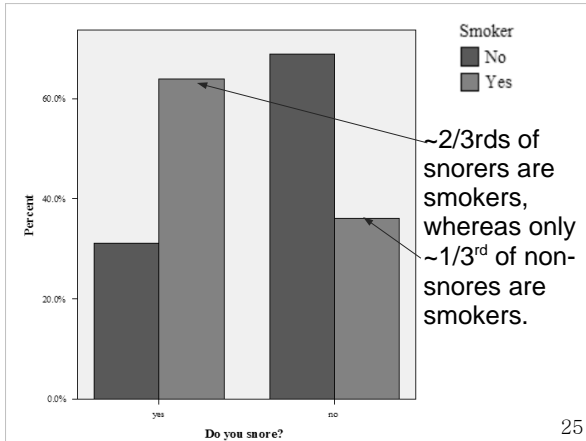
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### Pearson chi-square test

The value of the test-statistic is

$$X^2 = \sum \frac{(O - E)^2}{E},$$

where

- $X^2$  = the test statistic that approaches a  $\chi^2$  distribution.
- $O$  = frequencies observed;
- $E$  = frequencies expected (asserted by the null hypothesis).

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### Pearson chi-square test: Example

|                                    | Value               | df | Asymp. Sig. (2-sided) |
|------------------------------------|---------------------|----|-----------------------|
| Pearson Chi-Square                 | 10.259 <sup>a</sup> | 1  | .001                  |
| Continuity Correction <sup>a</sup> | 8.870               | 1  | .003                  |
| Likelihood Ratio                   | 9.780               | 1  | .002                  |
| Fisher's Exact Test                |                     |    |                       |
| Linear-by-Linear Association       | 10.204              | 1  | .001                  |
| N of Valid Cases                   | 186                 |    |                       |

Write-up:  $\chi^2(1, 186) = 10.26, p = .001$

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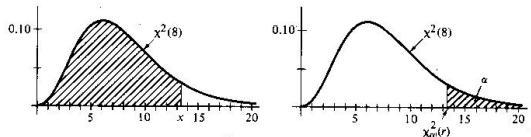
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# Chi-square distribution: Example

The Chi-Square Distribution



$$P(X \leq x) = \int_0^x \frac{1}{\Gamma(r/2)2^{r/2}} w^{r/2-1} e^{-w/2} dw$$

| r | P(X ≤ x)           |                     |                    |                    |                    |                    |                     |                    |
|---|--------------------|---------------------|--------------------|--------------------|--------------------|--------------------|---------------------|--------------------|
|   | 0.010              | 0.025               | 0.050              | 0.100              | 0.900              | 0.950              | 0.975               | 0.990              |
|   | $\chi^2_{0.99}(r)$ | $\chi^2_{0.975}(r)$ | $\chi^2_{0.95}(r)$ | $\chi^2_{0.90}(r)$ | $\chi^2_{0.10}(r)$ | $\chi^2_{0.05}(r)$ | $\chi^2_{0.025}(r)$ | $\chi^2_{0.01}(r)$ |
| 1 | 0.000              | 0.001               | 0.004              | 0.016              | 2.706              | 3.841              | 5.024               | 6.635              |
| 2 | 0.020              | 0.051               | 0.103              | 0.211              | 4.605              | 5.991              | 7.378               | 9.210              |
| 3 | 0.115              | 0.216               | 0.352              | 0.584              | 6.251              | 7.815              | 9.348               | 11.34              |
| 4 | 0.297              | 0.484               | 0.711              | 1.064              | 7.779              | 9.488              | 11.14               | 13.28              |
| 5 | 0.554              | 0.831               | 1.145              | 1.610              | 9.236              | 11.07              | 12.83               | 15.09              |

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## Phi (φ) & Cramer's V

(non-parametric measures of correlation)

### Phi (φ)

- Use for 2x2, 2x3, 3x2 analyses  
e.g., Gender (2) & Pass/Fail (2)

### Cramer's V

- Use for 3x3 or greater analyses  
e.g., Favourite Season (4) x Favourite Sense (5)

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## Phi (φ) & Cramer's V: Example

### Symmetric Measures

|                  |            | Value | Approx. Sig. |
|------------------|------------|-------|--------------|
| Nominal by       | Phi        | .235  | .001         |
| Nominal          | Cramer's V | .235  | .001         |
| N of Valid Cases |            | 186   |              |

$$\chi^2 (1, 186) = 10.26, p = .001, \phi = .24$$

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## Ordinal by ordinal

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## Ordinal by ordinal correlational approaches

- Spearman's rho ( $r_s$ )
- Kendall tau ( $\tau$ )
- Alternatively, use nominal by nominal techniques (i.e., recode or treat as lower level of measurement)

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## Graphing ordinal by ordinal data

- Ordinal by ordinal data is difficult to visualise because its non-parametric, yet there may be many points.
- Consider using:
  - Non-parametric approaches (e.g., clustered bar chart)
  - Parametric approaches (e.g., scatterplot with binning)

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**Spearman's rho ( $r_s$ ) or  
Spearman's rank order correlation**

- For ranked (ordinal) data
  - e.g. Olympic Placing correlated with World Ranking
- Uses product-moment correlation formula
- Interpretation is adjusted to consider the underlying ranked scales

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**Kendall's Tau ( $\tau$ )**

- Tau a
  - Does not take joint ranks into account
- Tau b
  - Takes joint ranks into account
  - For square tables
- Tau c
  - Takes joint ranks into account
  - For rectangular tables

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**Dichotomous by  
interval/ratio**

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## Point-biserial correlation ( $r_{pb}$ )

- One dichotomous & one continuous variable  
–e.g., belief in god (yes/no) and amount of international travel
- Calculate as for Pearson's product-moment  $r$ ,
- Adjust interpretation to consider the underlying scales

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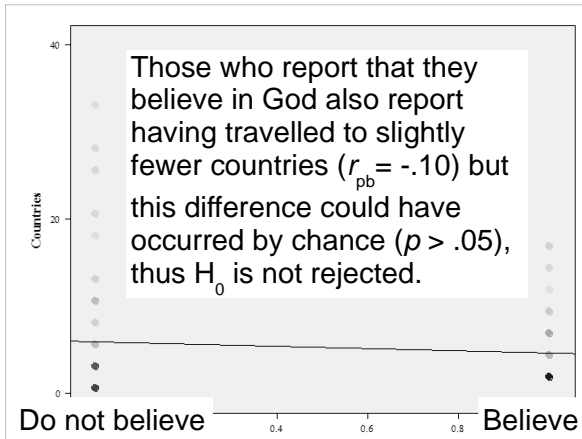
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## Point-biserial correlation ( $r_{pb}$ ): Example

Correlations

|              |                     | b4r God | b8 Countries |
|--------------|---------------------|---------|--------------|
| b4r God      | Pearson Correlation | 1       | -.095        |
|              | Sig. (2-tailed)     |         | .288         |
|              | N                   | 127     | 127          |
| b8 Countries | Pearson Correlation | -.095   | 1            |
|              | Sig. (2-tailed)     | .288    |              |
|              | N                   | 127     | 190          |

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## Interval/ratio by interval/ratio

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## Scatterplot

- Plot each pair of observations (X, Y)
  - x = predictor variable (independent; IV)
  - y = criterion variable (dependent; DV)
- By convention:
  - IV on the x (horizontal) axis
  - DV on the y (vertical) axis
- Direction of relationship:
  - +ve = trend from bottom left to top right
  - -ve r = trend from top left to bottom right

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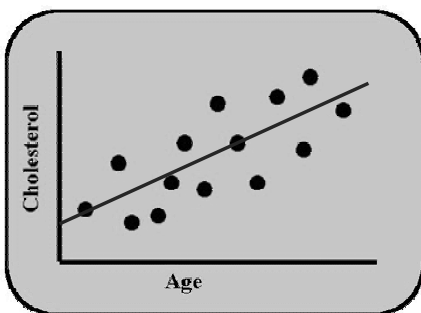
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Scatterplot showing relationship between age & cholesterol with line of best fit



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## Line of best fit

- The correlation between 2 variables is a measure of the degree to which pairs of numbers (points) cluster together around a best-fitting straight line
- Line of best fit:  $y = a + bx$
- Check for:
  - outliers
  - linearity

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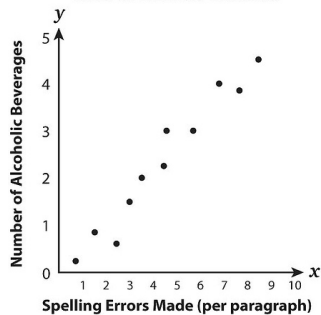
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## What's wrong with this scatterplot?

CORRELATION BETWEEN DRINKING AND SPELLING ERRORS



IV should be treated as X and DV as Y, although this is not always distinct.

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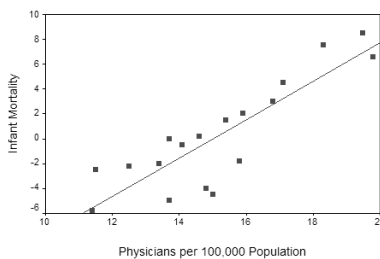
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## Scatterplot example: Strong positive (.81)



Q: Why is infant mortality positively linearly associated with the number of physicians (with the effects of GDP removed)?

A: Because more doctors tend to be deployed to areas with infant mortality (socio-economic status aside).

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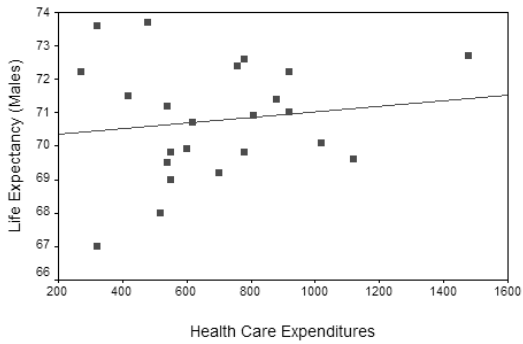
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Scatterplot example:  
Weak positive (.14)



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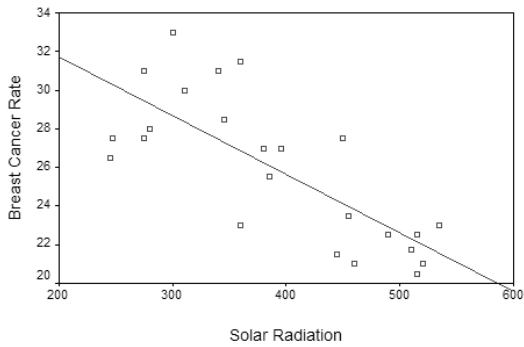
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Scatterplot example:  
Moderately strong negative (-.76)



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**Pearson product-moment correlation ( $r$ )**

- The product-moment correlation is the **standardised covariance**.

$$r_{X,Y} = \frac{\text{cov}(X, Y)}{S_X S_Y}$$

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## Covariance

- Variance shared by 2 variables

$$Cov_{XY} = \frac{\Sigma(X - \bar{X})(Y - \bar{Y})}{N - 1}$$

Cross products

- Covariance reflects the direction of the relationship:
  - +ve cov indicates +ve relationship
  - ve cov indicates -ve relationship

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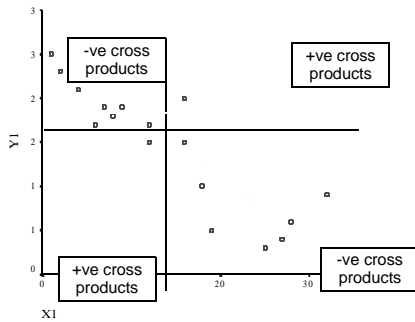
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## Covariance: Cross-products



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## Covariance

- Depends on the measurement scale → Can't compare covariance across different scales of measurement (e.g., age by weight in kilos versus age by weight in grams).
- Therefore, **standardise** covariance (divide by the cross-product of the SDs) → correlation
- Correlation is an effect size – i.e., standardised measure of strength of linear relationship

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### Covariance, SD, and correlation: Example quiz question

For a given set of data the covariance between X and Y is 1.20. The SD of X is 2 and the SD of Y is 3. The resulting correlation is:

- a. .20
- b. .30
- c. .40
- d. 1.20

Answer:  
 $1.20 / 2 \times 3 = .20$

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### Hypothesis testing

Almost all correlations are not 0, therefore the question is:

“What is the **likelihood** that a relationship between variables is a ‘true’ relationship - or could it simply be a result of random sampling variability or ‘chance’?”

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### Significance of correlation

- **Null hypothesis ( $H_0$ ):**  $\rho = 0$ : assumes that there is no ‘true’ relationship (in the population)
- **Alternative hypothesis ( $H_1$ ):**  $\rho \neq 0$ : assumes that the relationship is real (in the population)
- Initially assume  $H_0$  is true, and evaluate whether the data support  $H_1$ .
- **$\rho$  (rho)** = population product-moment correlation coefficient

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## How to test the null hypothesis

- Select a critical value (alpha ( $\alpha$ )); commonly .05
- Can use a 1 or 2-tailed test
- Calculate correlation and its  $p$  value. Compare this to the critical value.
- If  $p <$  critical value, the correlation is statistically significant, i.e., that there is less than a  $x\%$  chance that the relationship being tested is due to random sampling variability.

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## Correlation – SPSS output

| Correlations                            |   |                          |
|---|---|--------------------------|
|   | Cigarette Consumption per Adult per Day | CHD Mortality per 10,000 |
| Cigarette Consumption per Adult per Day | Pearson Correlation                     |                          |
|   | Sig. (2-tailed)                         |                          |
|   | N                                       |                          |
| CHD Mortality per 10,000                | Pearson Correlation                     | .713*                    |
|   | Sig. (2-tailed)                         | .000                     |
|   | N                                       | 21                       |

\*\* . Correlation is significant at the 0.01 level (2-tailed).

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## Imprecision in hypothesis testing

- **Type I error:** rejects  $H_0$  when it is true
- **Type II error:** Accepts  $H_0$  when it is false
- Significance test result will depend on the power of study, which is a function of:
  - Effect size ( $r$ )
  - Sample size ( $N$ )
  - Critical alpha level ( $\alpha_{crit}$ )

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## Significance of correlation

*df*      critical  
 (*N*-2)     $p = .05$

|      |     |   |
|------|-----|---|
| 5    | .67 | The size of correlation required to be significant decreases as <i>N</i> increases – why? |
| 10   | .50 |   |
| 15   | .41 |   |
| 20   | .36 |   |
| 25   | .32 |   |
| 30   | .30 |   |
| 50   | .23 |   |
| 200  | .11 |   |
| 500  | .07 |   |
| 1000 | .05 |   |

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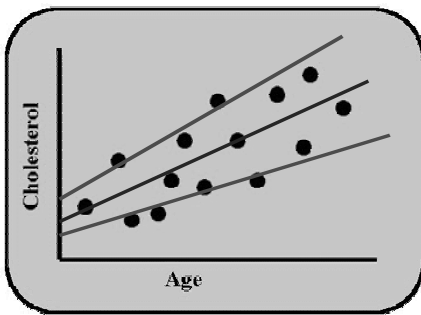
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Scatterplot showing a confidence interval for a line of best fit



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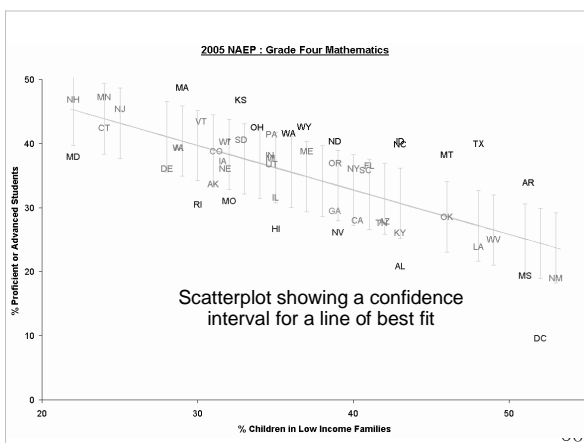
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### Practice quiz question: Significance of correlation

If the correlation between Age and test Performance is statistically significant, it means that:

- a. there is an important relationship between Age and test Performance
- b. the true correlation between Age and Performance in the population is equal to 0
- c. the true correlation between Age and Performance in the population is not equal to 0
- d. getting older causes you to do poorly on tests

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### Interpreting correlation

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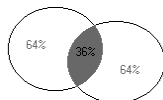
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### Coefficient of Determination ( $r^2$ )

- CoD = The proportion of variance or change in one variable that can be accounted for by another variable.
- e.g.,  $r = .60$ ,  $r^2 = .36$



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### Interpreting correlation (Cohen, 1988)

- A correlation is an **effect size**
- Rule of thumb

| <b>Strength</b> | <b><i>r</i></b> | <b><i>r</i><sup>2</sup></b> |
|-----------------|-----------------|-----------------------------|
| Weak:           | .1 - .3         | 1 - 10%                     |
| Moderate:       | .3 - .5         | 10 - 25%                    |
| Strong:         | >.5             | > 25%                       |

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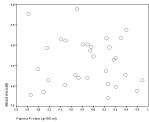
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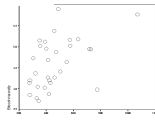
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### Size of correlation (Cohen, 1988)

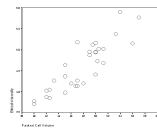
WEAK (.1 - .3)



MODERATE (.3-.5)



STRONG (>.5)




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### Interpreting correlation (Evans, 1996)

| <b>Strength</b> | <b><i>r</i></b> | <b><i>r</i><sup>2</sup></b> |
|-----------------|-----------------|-----------------------------|
| very weak       | 0 - .19         | (0 to 4%)                   |
| weak            | .20 - .39       | (4 to 16%)                  |
| moderate        | .40 - .59       | (16 to 36%)                 |
| strong          | .60 - .79       | (36% to 64%)                |
| very strong     | .80 - 1.00      | (64% to 100%)               |

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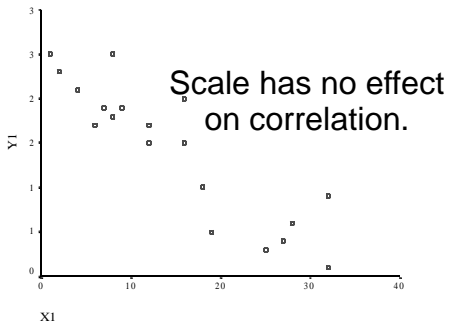
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Correlation of this scatterplot =  $-.9$



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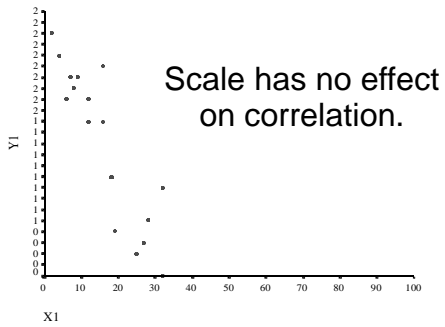
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Correlation of this scatterplot =  $-.9$



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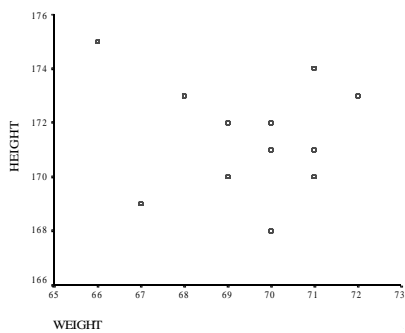
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What do you estimate the correlation of this scatterplot of height and weight to be?

- a.  $-.5$
- b.  $-1$
- c.  $0$
- d.  $.5$
- e.  $1$



69

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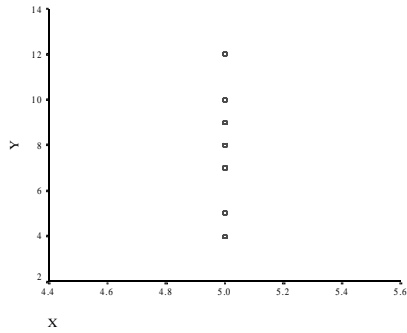
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What do you estimate the correlation of this scatterplot to be?

- a. -.5
- b. -1
- c. 0
- d. .5
- e. 1



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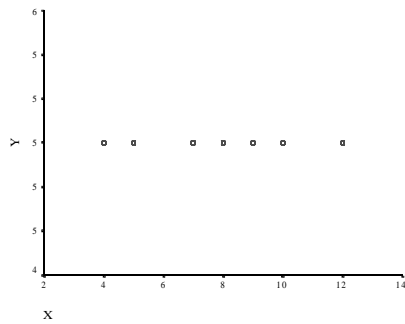
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What do you estimate the correlation of this scatterplot to be?

- a. -.5
- b. -1
- c. 0
- d. .5
- e. 1



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### Write-up: Example

“Number of children and marital satisfaction were inversely related ( $r(48) = -.35, p < .05$ ), such that contentment in marriage tended to be lower for couples with more children. Number of children explained approximately 10% of the variance in marital satisfaction, a small-moderate effect (see Figure 1).”

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**Assumptions and limitations**  
(Pearson product-moment linear correlation)

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**Assumptions and limitations**

1. Levels of measurement
2. Normality
3. Linearity
  1. Effects of outliers
  2. Non-linearity
4. Homoscedasticity
5. No range restriction
6. Homogenous samples
7. Correlation is not causation

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**Normality**

- The X and Y data should be sampled from populations with normal distributions
- Do not overly rely on a single indicator of normality; use histograms, skewness and kurtosis (within -1 and +1)
- Inferential tests of normality (e.g., Shapiro-Wilks) are overly sensitive when sample is large

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## Effect of outliers

- Outliers can disproportionately increase or decrease  $r$ .
- Options
  - compute  $r$  with & without outliers
  - get more data for outlying values
  - recode outliers as having more conservative scores
  - transformation
  - recode variable into lower level of measurement

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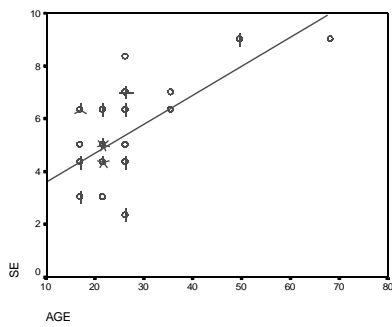
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## Age & self-esteem ( $r = .63$ )



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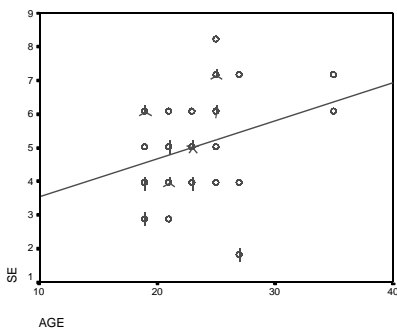
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## Age & self-esteem (outliers removed) $r = .23$



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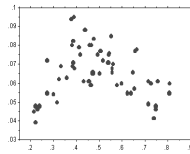
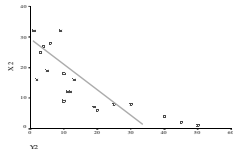
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## Non-linear relationships

Check scatterplot

Can a linear relationship 'capture' the lion's share of the variance?

If so, use  $r$ .



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## Non-linear relationships

If non-linear, consider

- Does a linear relation help?
- Transforming variables to 'create' linear relationship
- Use a non-linear mathematical function to describe the relationship between the variables

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## Scedasticity

- **Homo**scedasticity refers to even spread about a line of best fit
- **Hetero**scedasticity refers to uneven spread about a line of best fit
- Assess visually and with Levene's test

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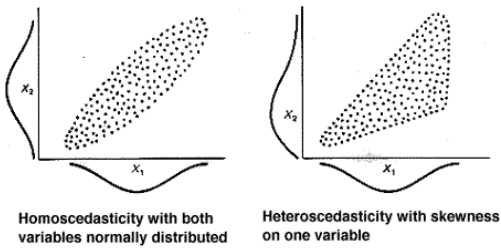
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## Scedasticity



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## Range restriction

- Range restriction is when the sample contains restricted (or truncated) range of scores
  - e.g., level of hormones and age < 18 might have linear relationship
- If range restriction, be cautious in generalising beyond the range for which data is available
  - e.g., level of hormones may not continue to increase linearly with age after age 18

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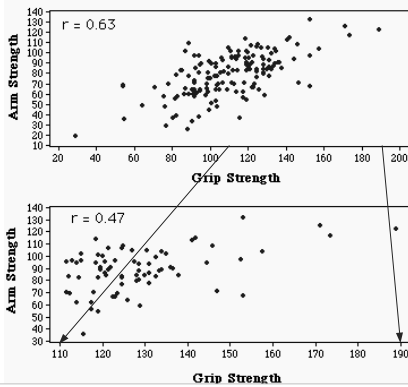
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## Range restriction



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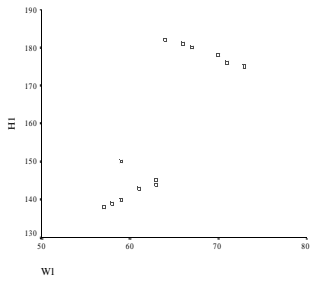
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## Heterogenous samples

- Sub-samples (e.g., males & females) may artificially increase or decrease overall  $r$ .
- Solution - calculate separately for sub-samples & overall, look for differences



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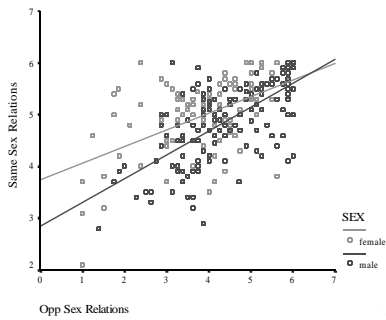
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## Scatterplot of Same-sex & Opposite-sex Relations by Gender

♂  $r = .67$   
 ♀  $r = .52$




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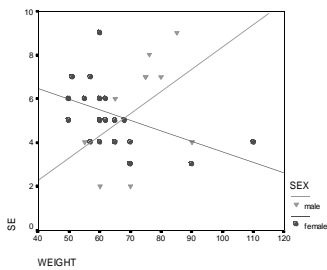
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## Scatterplot of Weight and Self-esteem by Gender

♂  $r = .50$   
 ♀  $r = -.48$



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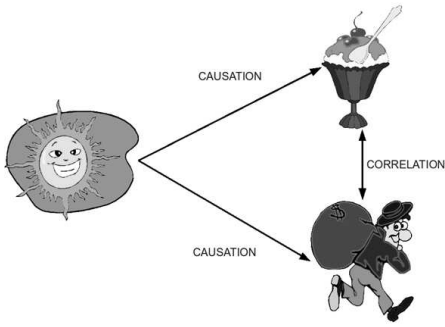
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**Correlation is not causation** e.g.,:  
 correlation between ice cream consumption and crime,  
 but actual cause is temperature




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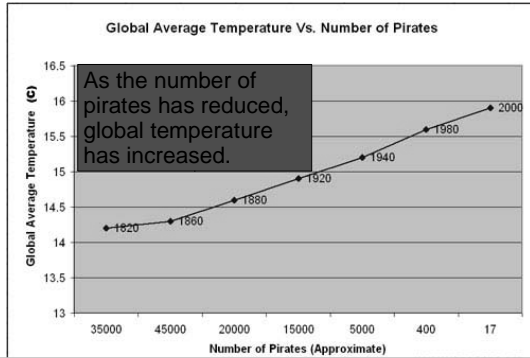
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**Correlation is not causation** e.g.,:  
 Stop global warming: Become a pirate




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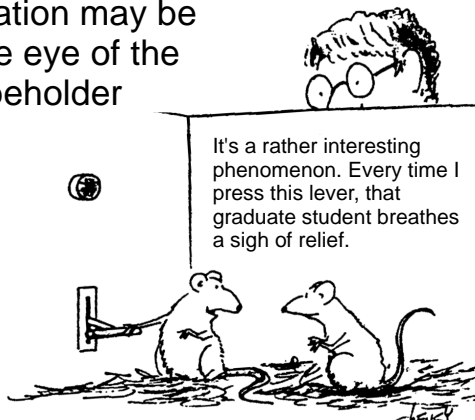
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**Causation may be  
 in the eye of the  
 beholder**




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## Dealing with several correlations

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## Dealing with several correlations

Scatterplot matrices organise scatterplots and correlations amongst several variables at once.

However, they are not sufficiently for over for more than about five variables at a time.

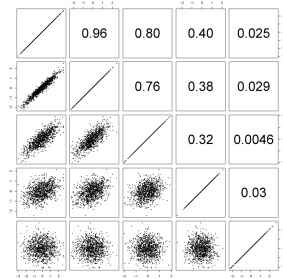


Image source: Unknown

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## Correlation matrix: Example of an APA Style Correlation Table

Table 1.  
*Correlations Between Five Life Effectiveness Factors for Adolescents and Adults (N = 3640)*

|                          | Time Management | Social Competence | Achievement Motivation | Intellectual Flexibility | Task Leadership |
|--------------------------|-----------------|-------------------|------------------------|--------------------------|-----------------|
| Time Management          |                 | .36               | .53                    | .31                      | .42             |
| Social Competence        |                 |                   | .37                    | .32                      | .57             |
| Achievement Motivation   |                 |                   |                        | .42                      | .41             |
| Intellectual Flexibility |                 |                   |                        |                          | .37             |
| Task Leadership          |                 |                   |                        |                          |                 |

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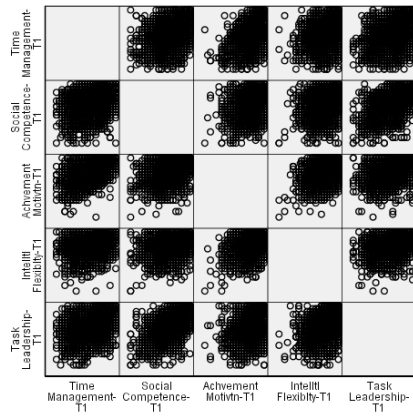
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## Scatterplot matrix



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## Summary

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### Summary: Covariation

1. The world is made of covariations.
2. Covariations are the building blocks of more complex analyses, including
  1. factor analysis
  2. reliability analysis
  3. multiple regression

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**Summary:**

**Purpose of correlation**

1. Correlation is a standardised measure of the extent to which two phenomenon co-relate.
2. Correlation does not prove causation – may be opposite causality, co-causal, or due to other variables.

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**Summary:**

**Types of correlation**

- Nominal by nominal:  
Phi ( $\Phi$ ) / Cramer's  $V$ , Chi-squared
- Ordinal by ordinal:  
Spearman's rank / Kendall's Tau  $b$
- Dichotomous by interval/ratio:  
Point bi-serial  $r_{pb}$
- Interval/ratio by interval/ratio:  
Product-moment or Pearson's  $r$

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**Summary:**

**Correlation steps**

1. Choose measure of correlation and graphs based on levels of measurement.
2. Check graphs (e.g., scatterplot)

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**Summary:**  
**Correlation steps**

- 3. Consider
  - Effect size (e.g.,  $\Phi$ , Cramer's  $V$ ,  $r$ ,  $r^2$ )
  - Direction
  - Inferential test ( $p$ )
- 4. Interpret/Discuss
  - Relate back to hypothesis
  - Size, direction, significance
  - Limitations e.g.,
    - Heterogeneity (sub-samples)
    - Range restriction
    - Causality?

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**Summary:**  
**Interpreting correlation**

- Coefficient of determination
  - Correlation squared
  - Indicates % of shared variance

| <b>Strength</b> | <b><math>r</math></b> | <b><math>r^2</math></b> |
|-----------------|-----------------------|-------------------------|
| Weak:           | .1 - .3               | 1 - 10%                 |
| Moderate:       | .3 - .5               | 10 - 25%                |
| Strong:         | > .5                  | > 25%                   |

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**Summary:**  
**Assumptions & limitations**

1. Levels of measurement
2. Normality
3. Linearity
  1. Effects of outliers
  2. Non-linearity
4. Homoscedasticity
5. No range restriction
6. Homogenous samples
7. Correlation is not causation

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**Summary:**  
**Dealing with several correlations**

- Correlation matrix
- Scatterplot matrix

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**References**

Evans, J. D. (1996). *Straightforward statistics for the behavioral sciences*. Pacific Grove, CA: Brooks/Cole Publishing.

Howell, D. C. (2007). *Fundamental statistics for the behavioral sciences*. Belmont, CA: Wadsworth.

Howell, D. C. (2010). *Statistical methods for psychology* (7th ed.). Belmont, CA: Wadsworth.

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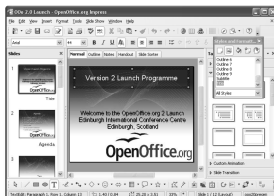
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- Free and open source software.
- <http://www.openoffice.org/product/impress.html>



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