

# Wright State University Lake Campus/2018-9/Phy2410/Equation sheet

lintHint

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T1

## 2.5 Electric charges and fields (<https://cnx.org/contents/eg-XcBxE@14.1:Ai7EWArA@5/Introduction>)

$\epsilon_0 = 8.85 \times 10^{-12}$  F/m = vacuum permittivity.

$$\vec{E} = \int \frac{dq}{r^2} \hat{r} \text{ where } dq = \lambda dl = \sigma da = \rho dV$$

$e = 1.602 \times 10^{-19}$  C: negative (positive) charge for electrons (protons)

$$E = \frac{\sigma}{2\epsilon_0} = \text{field above an infinite plane of charge.}$$

$$k_e = \frac{1}{4\pi\epsilon_0} = 8.99 \times 10^9 \text{ m/F}$$

$$\vec{F} = Q\vec{E} \text{ where } \vec{E} = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^N \frac{q_i}{r_i^2} \hat{r}_{Pi}$$

Find E

$$\vec{E}(\vec{r}) = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^N \frac{\widehat{\mathcal{R}}_i Q_i}{|\vec{\mathcal{R}}_i|^2} = \frac{1}{4\pi\epsilon_0} \sum_{i=1}^N \frac{\vec{\mathcal{R}}_i Q_i}{|\vec{\mathcal{R}}_i|^3} \text{ is the electric field at the field point, } \vec{r}, \text{ due to point charges at the source points, } \vec{r}_i, \text{ and } \vec{\mathcal{R}}_i = \vec{r} - \vec{r}_i, \text{ points from source points to the field point.}$$

T2

## 2.6 Gauss's law (<https://cnx.org/contents/eg-XcBxE@14.1:xakXl9gb@5/Introduction>):

$$\Phi = \vec{E} \cdot \vec{A} \rightarrow \int \vec{E} \cdot d\vec{A} = \int \vec{E} \cdot \hat{n} dA = \text{electric flux}$$

$$d \text{Vol} = dx dy dz = r^2 dr dA \text{ where } dA = r^2 d\phi d\theta$$

$$q_{\text{enclosed}} = \epsilon_0 \oint \vec{E} \cdot d\vec{A}$$

$$A_{\text{sphere}} = r^2 \int_0^\pi \sin \theta d\theta \int_0^{2\pi} d\phi = 4\pi r^2$$

Surface Integrals

Calculating  $\int f dA$  and  $\int f dV$  with angular symmetry

Cylindrical:  $dA = 2\pi r dz$ ;  $dV = dA dr$ . Spherical:  $\int dA = 4\pi r^2$ ,  $dV = 4\pi r^2 dr$

More Gauss Law

Calculating  $\int f dA$  and  $\int f dV$  with angular symmetry

Cylindrical:  $dA = 2\pi r dz$ ;  $dV = dA dr$ . Spherical:  $\int dA = 4\pi r^2$ ,  $dV = 4\pi r^2 dr$

T3

**2.7 Electric potential (<https://cnx.org/contents/eg-XcBxE@14.1:bMxnTeM5@6/Introduction>)** The alpha-particle is made up of two protons and two neutrons.

$$\Delta V_{AB} = V_A - V_B = - \int_A^B \vec{E} \cdot d\vec{\ell} = \text{electric potential}$$

$$\vec{E} = -\frac{\partial V}{\partial x} \hat{i} - \frac{\partial V}{\partial y} \hat{j} - \frac{\partial V}{\partial z} \hat{k} = -\vec{\nabla} V$$

$q\Delta V$  = change in potential energy (or simply  $U = qV$ )

$$\text{Power} = \frac{\Delta U}{\Delta t} = \frac{\Delta q}{\Delta t} V = IV = e \frac{\Delta N}{\Delta t}$$

Electron (proton) mass =  $9.11 \times 10^{-31} \text{kg}$  ( $1.67 \times 10^{-27} \text{kg}$ ).  
Elementary charge =  $e = 1.602 \times 10^{-19} \text{C}$ .

$$K = \frac{1}{2} m v^2 = \text{kinetic energy. } 1 \text{ eV} = 1.602 \times 10^{-19} \text{J}$$

$$V(r) = k \frac{q}{r} \text{ near isolated point charge}$$

$$\text{Many charges: } V_P = k \sum_1^N \frac{q_i}{r_i} \rightarrow k \int \frac{dq}{r}$$

**2.8 Capacitance ([https://cnx.org/contents/eg-XcBxE@14.1:FYJxWFC\\_@6/8-1-Capacitors-and-Capacitance](https://cnx.org/contents/eg-XcBxE@14.1:FYJxWFC_@6/8-1-Capacitors-and-Capacitance))**

$Q = CV$  defines capacitance.

$$u = \frac{1}{2} QV = \frac{1}{2} CV^2 = \frac{1}{2C} Q^2 = \text{stored energy}$$

$C = \epsilon_0 \frac{A}{d}$  where A is area and  $d \ll A^{1/2}$  is gap length of parallel plate capacitor

$$u_E = \frac{1}{2} \epsilon_0 E^2 = \text{energy density}$$

Series :  $\frac{1}{C_s} = \sum \frac{1}{C_i}$ . Parallel:  $C_P = \sum C_i$ .

T4

**2.9 Current and resistors (<https://cnx.org/contents/eg-XcBxE@14.10:WS3a1YbB@5/Introduction>)**

Electric current: 1 Amp (A) = 1 Coulomb (C) per second (s)

$$\vec{E} = \rho \vec{J} = \text{electric field where } \rho = \text{resistivity}$$

Current =  $I = dQ/dt = nqv_d A$ , where

$$\rho = \rho_0 [1 + \alpha(T - T_0)], \text{ and } R = R_0 [1 + \alpha \Delta T],$$

$(n, q, v_d, A)$  = (density, charge, speed, Area)

where  $R = \rho \frac{L}{A}$  is resistance

$$I = \int \vec{J} \cdot d\vec{A} \text{ where } \vec{J} = nq\vec{v}_d = \text{current density.}$$

$$V = IR \text{ and Power} = P = IV = I^2 R = V^2 / R$$

**2.10 Direct current circuits (<https://cnx.org/contents/eg-XcBxE@14.1:BRLHpZ5e@6/Introduction>)**

$V_{terminal} = \epsilon - Ir_{eq}$  where  $r_{eq}$  = internal resistance and  $\epsilon = emf$ .

Charging an RC (resistor-capacitor) circuit:  $q(t) = Q (1 - e^{-t/\tau})$   
and  $I = I_0 e^{-t/\tau}$  where  $\tau = RC$  is RC time,  $Q = \epsilon C$  and  $I_0 = \epsilon / R$ .

$$R_{series} = \sum_{i=1}^N R_i \text{ and } R_{parallel}^{-1} = \sum_{i=1}^N R_i^{-1}$$

Kirchhoff Junction:  $\sum I_{in} = \sum I_{out}$  and Loop:  $\sum V = 0$

Discharging an RC circuit:  $q(t) = Q e^{-t/\tau}$  and  $I(t) = -\frac{Q}{RC} e^{-t/\tau}$

T5

**2.11 Magnetic forces and fields (<https://cnx.org/contents/eg-XcBxE@14.1:-cf9Ogkt@5/Introduction>)**

$$|\vec{a} \times \vec{b}| = ab \sin \theta \Leftrightarrow$$

$$(\vec{a} \times \vec{b})_x = (a_y b_z - a_z b_y),$$

$$(\vec{a} \times \vec{b})_y = (a_z b_x - a_x b_z),$$

$$(\vec{a} \times \vec{b})_z = (a_x b_y - a_y b_x)$$

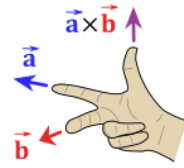
Magnetic force:  $\vec{F} = q\vec{v} \times \vec{B}$ ,

$$d\vec{F} = I d\vec{\ell} \times \vec{B}.$$

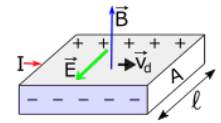
$$\vec{v}_d = \vec{E} \times \vec{B} / B^2 = \text{EXB drift velocity}$$

Circular motion (uniform B field):

$$r = \frac{mv}{qB}, \text{ Period} = T = \frac{2\pi m}{qB}$$



cross product



Hall effect

Dipole moment =  $\vec{\mu} = NIA\hat{n}$ . Torque =

$$\vec{\tau} = \vec{\mu} \times \vec{B}. \text{ Stored energy} = U = \vec{\mu} \cdot \vec{B}$$

$$\text{Hall field} = \vec{E} = V/\ell = Bv_d = \frac{IB}{neA}$$

## 2.12 Sources of magnetic fields (<https://cnx.org/contents/eg-XcBxE@14.1:BDvPdDpp@5/Introduction>)

Free space permeability  $\mu_0 = 4\pi \times 10^{-7} \text{ T}\cdot\text{m}/\text{A}$

$$\text{Force between parallel wires } \frac{F}{\ell} = \frac{\mu_0 I_1 I_2}{2\pi r}$$

$$\text{Biot-Savart law } \vec{B} = \frac{\mu_0}{4\pi} \int_{\text{wire}} \frac{I d\vec{\ell} \times \hat{r}}{r^2}$$

$$\text{Ampère's Law: } \oint \vec{B} \cdot d\vec{\ell} = 4\pi\mu_0 I_{\text{enc}}$$

Magnetic field inside solenoid with paramagnetic material =

$$B = \mu n I \text{ where } \mu = (1 + \chi)\mu_0 = \text{permeability}$$

(we skip T6 because it was a review of previous chapters)

T7

## 2.13 Electromagnetic induction (<https://cnx.org/contents/eg-XcBxE@14.1:az4UJL6l@6/Introduction>)

$$\text{Magnetic flux } \Phi_m = \int_S \vec{B} \cdot \hat{n} dA$$

$$\text{Motional } \varepsilon = Blv \text{ if } \vec{v} \perp \vec{B}$$

$$\text{Electromotive "force" (volts) } \varepsilon = -N \frac{d\Phi_m}{dt} = \oint \vec{E} \cdot d\vec{\ell}$$

$$\text{rotating coil } \varepsilon = NBA\omega \sin \omega t$$

## 2.14 Inductance ([https://cnx.org/contents/eg-XcBxE@14.1:gBxAb\\_6h@6/Introduction](https://cnx.org/contents/eg-XcBxE@14.1:gBxAb_6h@6/Introduction))

Unit of inductance = Henry (H) = 1V·s/A

Mutual inductance:  $M \frac{dI_2}{dt} = N_1 \frac{d\Phi_{12}}{dt} = -\varepsilon_1$  where  $\Phi_{12}$  = flux through 1 due to current in 2. Reciprocity:  $M \frac{dI_1}{dt} = -\varepsilon_2$

Self-inductance:  $N\Phi_m = LI \rightarrow \varepsilon = -L \frac{dI}{dt}$

$$L_{\text{solenoid}} \approx \mu_0 N^2 A \ell, \quad L_{\text{toroid}} \approx \frac{\mu_0 N^2 h}{2\pi} \ln \frac{R_2}{R_1}, \quad \text{Stored energy} = \frac{1}{2} LI^2$$

$$I(t) = \frac{\varepsilon}{R} (1 - e^{-t/\tau}) \text{ in LR circuit where } \tau = L/R$$

$$q(t) = q_0 \cos(\omega t + \phi) \text{ in LC circuit where } \omega = \sqrt{\frac{1}{LC}}$$

## 2.15 Alternating current circuits (<https://cnx.org/contents/eg-XcBxE@14.1:6uMHjFiO@5/Introduction>)

AC voltage and current  $v = V_0 \sin(\omega t - \phi)$  if  $i = I_0 \sin \omega t$ .

$$\text{RMS values } I_{\text{rms}} = \frac{I_0}{\sqrt{2}} \text{ and } V_{\text{rms}} = \frac{V_0}{\sqrt{2}}$$

Impedance  $V_0 = I_0 X$

Resistor  $V_0 = I_0 X_R, \phi = 0$ , where  $X_R = R$

Capacitor  $V_0 = I_0 X_C, \phi = -\frac{\pi}{2}$ , where  $X_C = \frac{1}{\omega C}$

Inductor  $V_0 = I_0 X_L, \phi = +\frac{\pi}{2}$ , where  $X_L = \omega L$

RLC series circuit  $V_0 = I_0 Z$  where  $Z = \sqrt{R^2 + (X_L - X_C)^2}$

$$\text{and } \phi = \tan^{-1} \frac{X_L - X_C}{R}$$

$$\text{Resonant angular frequency } \omega_0 = \sqrt{\frac{1}{LC}}$$

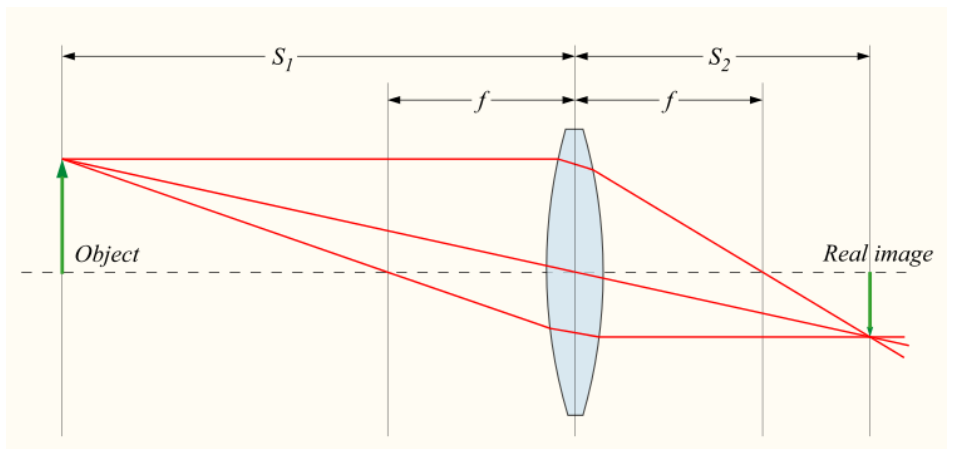
$$\text{Quality factor } Q = \frac{\omega_0}{\Delta\omega} = \frac{\omega_0 L}{R}$$

$$\text{Average power } P_{\text{ave}} = \frac{1}{2} I_0 V_0 \cos \phi = I_{\text{rms}} V_{\text{rms}} \cos \phi$$

$$\text{Transformer voltages and currents } \frac{V_S}{V_P} = \frac{N_S}{N_P} = \frac{I_P}{I_S}$$

### 3.2 Geometric optics and image formation (<https://cnx.org/contents/rydUIGBQ@10.14:-YlrAoNe@5/Introduction>)

$\frac{1}{S_1} + \frac{1}{S_2} = \frac{1}{f}$  relates the focal length  $f$  of the lens, the image distance  $S_1$ , and the object distance  $S_2$ . The figure depicts the situation for which  $(S_1, S_2, f)$  are all positive: (1) The lens is converging (convex); (2) The real image is to the right of the lens; and (3) the object is to the left of the lens. If the lens is diverging (concave), then  $f < 0$ . If the image is to the left of the lens (virtual image), then  $S_2 < 0$ .



### 2.16 Electromagnetic waves (<https://cnx.org/contents/eg-XcBxE@14.10:-LQJwSUO@6/16-1-Maxwell-s-Equations-and-Electromagnetic-Waves>)

Displacement current  $I_d = \epsilon_0 \frac{d\Phi_E}{dt}$  where

$\Phi_E = \int \vec{E} \cdot d\vec{A}$  is the electric flux.

Maxwell's equations:  $\epsilon_0 \mu_0 = 1/c^2$

$$\oint_S \vec{E} \cdot d\vec{A} = \frac{1}{\epsilon_0} Q_{in}$$

$$\oint_S \vec{B} \cdot d\vec{A} = 0$$

$$\oint_C \vec{E} \cdot d\vec{l} = - \int_S \frac{\partial \vec{B}}{\partial t} \cdot d\vec{A}$$

$$\oint_C \vec{B} \cdot d\vec{l} = \mu_0 I + \epsilon_0 \mu_0 \frac{d\Phi_E}{dt}$$

$$\frac{\partial^2 E_y}{\partial x^2} = \epsilon_0 \mu_0 \frac{\partial^2 E_y}{\partial t^2} \text{ and } \frac{E_0}{B_0} = c$$

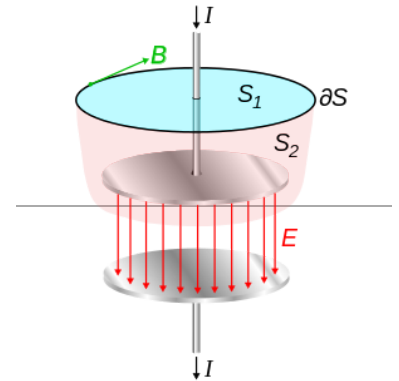
Poynting vector  $\vec{S} = \frac{1}{\mu_0} \vec{E} \times \vec{B}$  = energy flux

Average intensity

$$I = S_{ave} = \frac{c\epsilon_0}{2} E_0^2 = \frac{c}{2\mu_0} B_0^2 = \frac{1}{2\mu_0} E_0 B_0$$

Radiation pressure  $p = I/c$  (perfect absorber)

and  $p = 2I/c$  (perfect reflector).



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