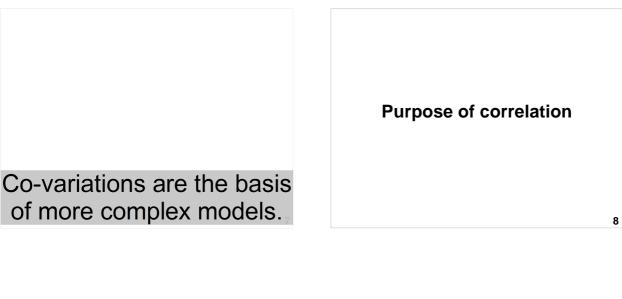
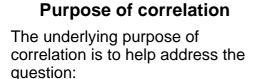


The world is made of co-variations



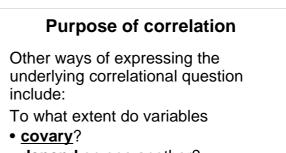


What is the

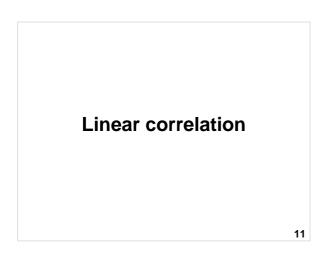
- relationship or
- association or
- shared variance or
- co-relation

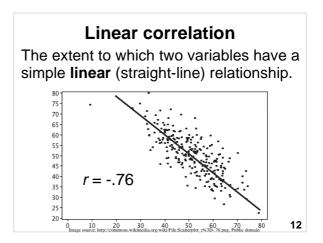
between two variables?

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- depend on one another?
- explain one another?





Linear correlation

Linear relations between variables are indicated by correlations':

- Direction: Sign (+ / -) indicates direction of relationship (+ve or -ve slope)
- Strength: Size indicates strength (values closer to -1 or +1 indicate greater strength)

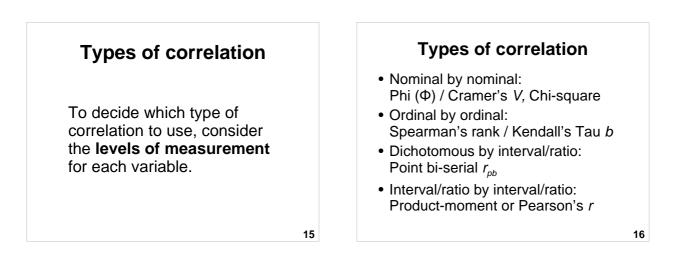
 Statistical significance: p indicates likelihood that the observed relationship could have occurred by chance

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Types of relationships

- No relationship (r = 0)(X and Y are independent)
- Linear relationship (X and Y are dependent) $-As X \uparrow s$, so does Y (r > 0) $-As X \uparrow s, Y \downarrow s (r < 0)$
- Non-linear relationship

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Types of correlation and LOM Ordinal Nominal Int/Ratio Clustered bar Clustered barchart or chart scatterplot Nominal Chi-square, \leftarrow Recode Point bi-serial Phi (φ) or correlation Cramer's V (r_{pb}) Clustered bar chart or scatterplot Ordinal =1[_{Recode} Spearman's Rho or

Kendall's Tau

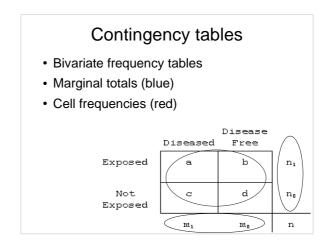
Int/Ratio

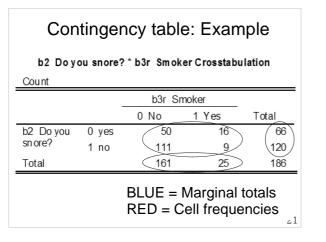
Scatterplot Productmoment correlation (17



Nominal by nominal correlational approaches

- Contingency (or cross-tab) tables
 - Observed
 - Expected
 - Row and/or column %s
 - Marginal totals
- Clustered bar chart
- Chi-square
- Phi (**(**) / Cramer's V





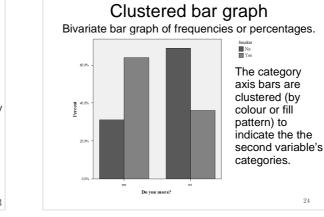
19

			b3r Sm	noker	
			0 No	1 Yes	Total
b2 Do you snore?	0 yes	Count	50	16	(
	\langle	Expected Count	57.1	8.9	66
	1 no	Count	111	9	12
		Expected Count	103.9	16.1	120
Total		Count	161	25	18
		Expected Count	161.0	25.0	186

. . .

. .

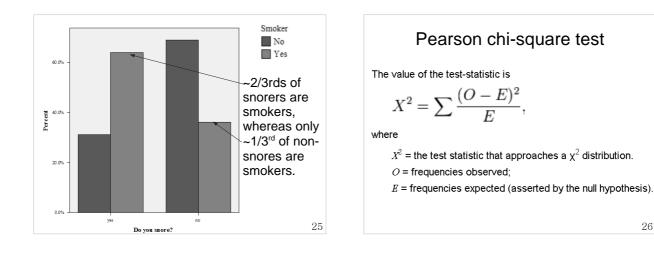
•Chi-square is based on the differences between the actual and expected cell counts. 22



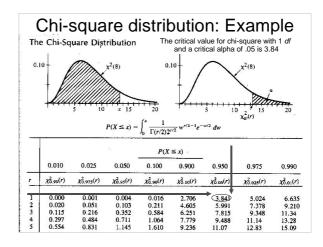
b2 Do you snore? * b3r Smoker Crosstabulation % within b2 Do you snore? b3r Smoker 0 No 1 Yes Total b2 Do you sn ore? 0 yes 75.8% 24.2% 100.0% 92.5% 7.5% 100.0% 1 no Total 86.6% 13.4% 100.0% Row and/or column cell percentages may also

aid interpretation e.g., ~2/3rds of smokers snore, whereas only ~1/3rd of non-smokers snore. b2 Do you snore? * b3r \$moker Crosstabulation

		b3r Siqnoker			
		_0 No	1 Yes	Total	
b2 Do you snore?	0 yes	31.4%	64.0%	35.5%	
	1 no	68.9%	▲36.0%	64.5%	
Total		100.0%	100.0%	100.0%	



Pearson chi-square test: Example				
	Value	df	Asymp. Sig. (2-sided)	
Pearson Chi-Square	10.259	(1)	.001	
Continuity Correction ^a	8.870	1	.003	
Likelih ood Ratio	9.780	1	.002	
Fisher's Exact Test				
Linear-by-Linear Association	10.204	1	.001	
N of Valid Cases	186			
Write-up: χ^2 (1, 186) = 10.26, <i>p</i> = .001				



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Phi (ϕ) & Cramer's V

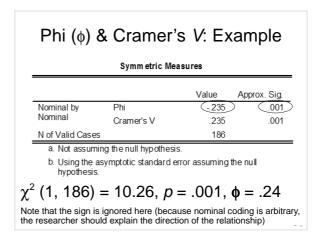
(non-parametric measures of correlation)

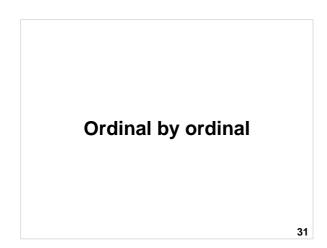
Phi (ø)

• Use for 2 x 2, 2 x 3, 3 x 2 analyses e.g., Gender (2) & Pass/Fail (2)

Cramer's V

• Use for 3 x 3 or greater analyses e.g., Favourite Season (4) x Favourite Sense (5)





Ordinal by ordinal correlational approaches

- Spearman's rho (r)
- Kendall tau (τ)
- Alternatively, use nominal by nominal techniques (i.e., recode the variables or treat them as having a lower level of measurement)

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Graphing ordinal by ordinal data

- Ordinal by ordinal data is difficult to visualise because its non-parametric, with many points.
- Consider using:
 - -Non-parametric approaches (e.g., clustered bar chart)
 - -Parametric approaches (e.g., scatterplot with line of best fit)

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Spearman's rho (*r*_s) or Spearman's rank order correlation

- For ranked (ordinal) data
- –e.g., Olympic Placing correlated with World Ranking
- Uses product-moment correlation formula
- Interpretation is adjusted to consider the underlying ranked scales

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Kendall's Tau (τ)

- Tau a
 - -Does not take joint ranks into account
- Tau b
 - Takes joint ranks into account
 - -For square tables
- Tau c
 - -Takes joint ranks into account
 - -For rectangular tables

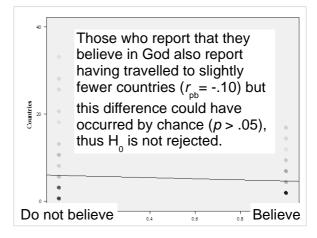
35

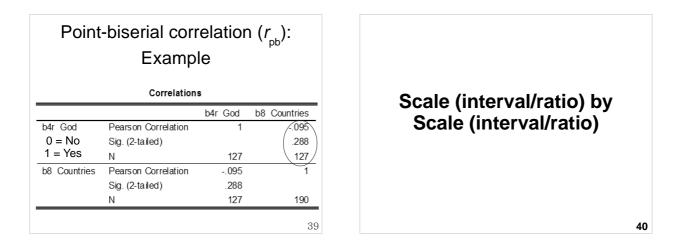
Dichotomous by scale (interval/ratio)

Point-biserial correlation $(r_{\rm nb})$

- One dichotomous & one continuous variable

 –e.g., belief in god (yes/no) and
 - number of countries visited
- Calculate as for Pearson's product-moment *r*
- Adjust interpretation to consider the direction of the dichotomous scales



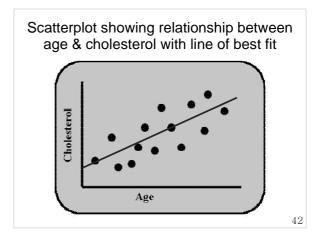


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Scatterplot

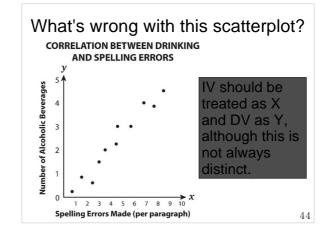
- Plot each pair of observations (X, Y)
 -x = predictor variable (independent; IV)
 - -y = criterion variable (dependent; DV)
- By convention:
 - -IV on the x (horizontal) axis
 - –DV on the y (vertical) axis
- Direction of relationship:
 - -+ve = trend from bottom left to top right

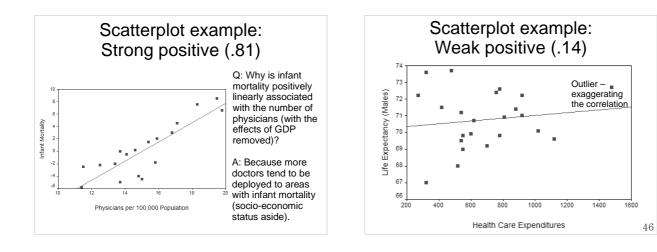
--ve = trend from top left to bottom right

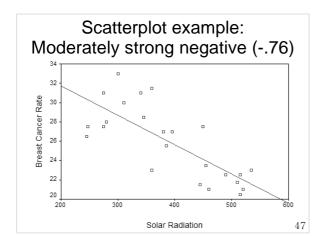


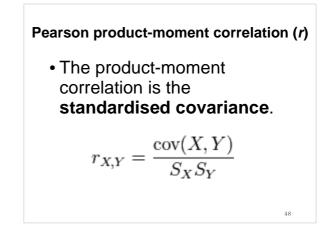
Line of best fit

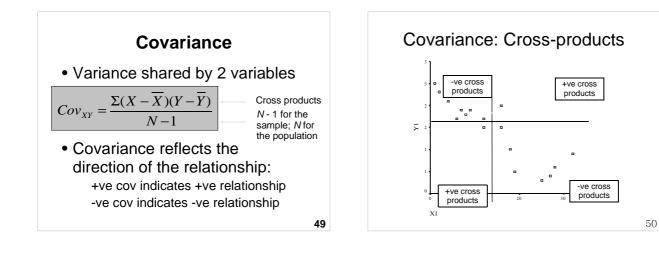
- The correlation between 2 variables is a measure of the degree to which pairs of numbers (points) cluster together around a best-fitting straight line
- Line of best fit: y = a + bx
- Check for:
 - outliers
 - linearity

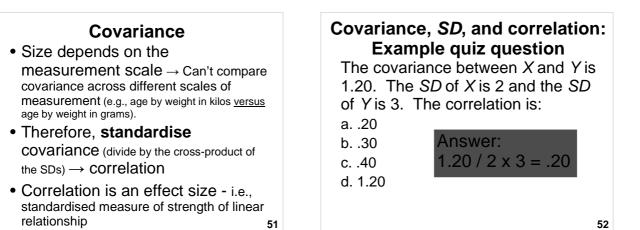












Hypothesis testing

Almost all correlations are not 0, therefore the question is:

"What is the **likelihood** that a relationship between variables is a 'true' relationship - or could it simply be a result of random sampling variability or 'chance'?"

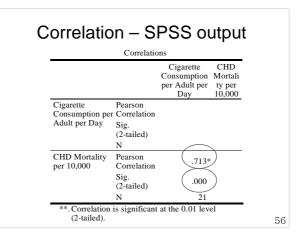
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Significance of correlation

- Null hypothesis (H₀): ρ = 0: assumes that there is no 'true' relationship (in the population)
- Alternative hypothesis (H₁): ρ <> 0: assumes that the relationship is real (in the population)
- Initially assume H₀ is true, and evaluate whether the data support H₁.
- ρ (rho) = population product-moment correlation coefficient

How to test the null hypothesis

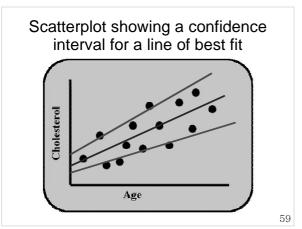
- Select a critical value (alpha (α)); commonly .05
- Can use a 1- or 2-tailed test
- Calculate correlation and its *p* value. Compare this to the critical value.
- If p < critical value, the correlation is statistically significant, i.e., that there is less than a x% chance that the relationship being tested is due to random sampling variability.

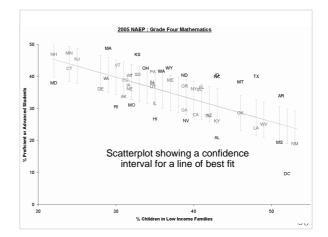


Imprecision in hypothesis testing

- Type I error: rejects H_0 when H_0 is true
- Type II error: accepts H₀ when H₀ is false
- A significance test result depends on the power of study, which is a function of:
 - -Effect size (r)
 - -Sample size (N)
 - -Critical alpha level (α_{crit})

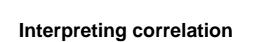
Signific	cance o	of correlation
df	critical	
<u>(N - 2)</u>	<u>p = .05</u>	
5	.67	The size of
10	.50	correlation
15	.41	
20	.36	required to be
25	.32	significant
30	.30	decreases as N
50	.23	increases -
200	.11	
500	.07	why?
1000	.05	58

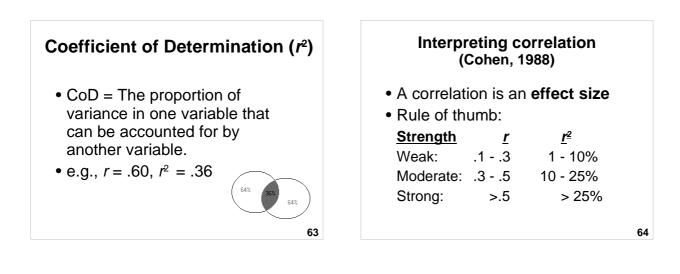


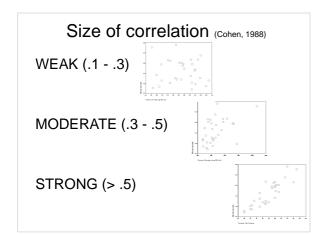


Practice quiz question: Significance of correlation

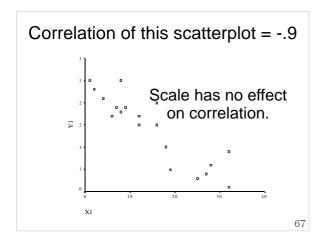
- If the correlation between Age and test Performance is statistically significant, it means that:
- a. there is an important relationship between the variables
- b. the true correlation between the variables in the population is equal to $\ensuremath{0}$
- c. the true correlation between the variables in the population is not equal to 0
- d. getting older causes you to do poorly on tests 61

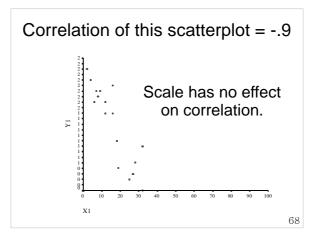


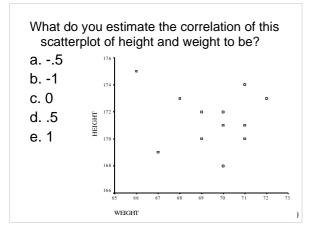


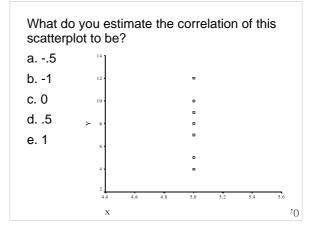


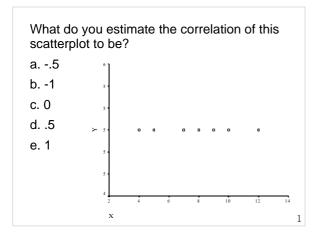
	(Evans, 199	50)
<u>Strength</u>	<u>r</u>	<u>r</u> ²
very weak	019	(0 to 4%)
weak	.2039	(4 to 16%)
moderate	.4059	(16 to 36%)
strong	.6079	(36% to 64%)
very strong	.80 - 1.00	(64% to 100%











Write-up: Example

"Number of children and marital satisfaction were inversely related (r (48) = -.35, p < .05), such that contentment in marriage tended to be lower for couples with more children. Number of children explained approximately 10% of the variance in marital satisfaction, a small-moderate effect."

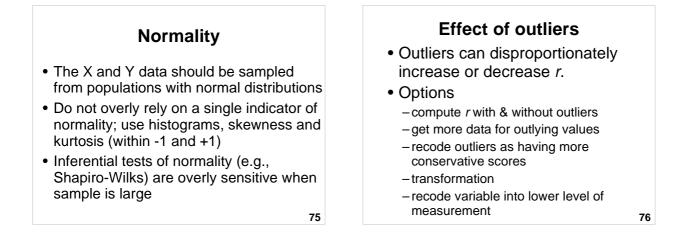
Assumptions and limitations

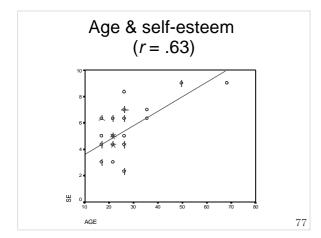
(Pearson product-moment linear correlation)

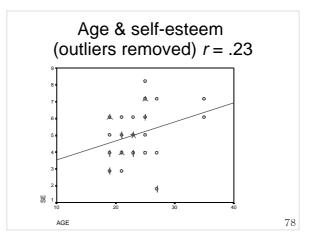
73

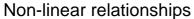
Assumptions and limitations

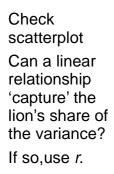
- 1. Levels of measurement
- 2. Normality
- 3. Linearity 1. Effects of outliers
- 2. Non-linearity
- 4. Homoscedasticity
- 5. No range restriction
- 6. Homogenous samples
- 7. Correlation is not causation

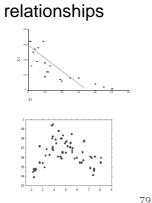










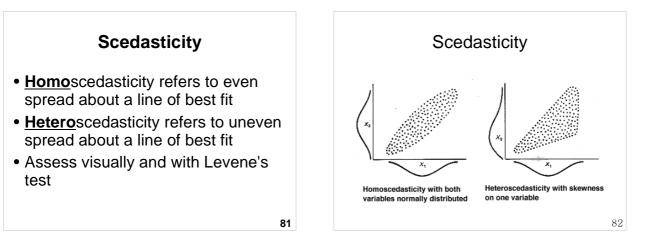


Non-linear relationships

If non-linear, consider

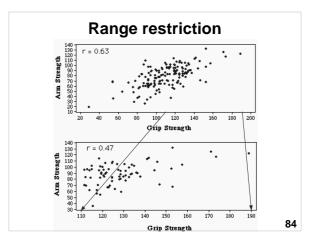
- Does a linear relation help?
- Transforming variables to 'create' linear relationship
- Use a non-linear mathematical function to describe the relationship between the variables

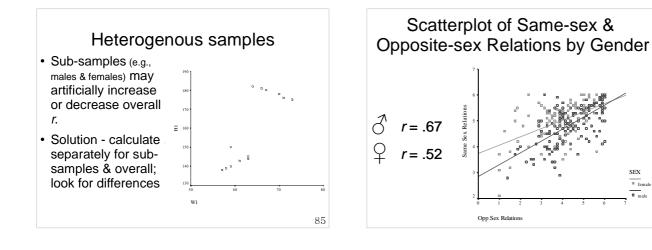


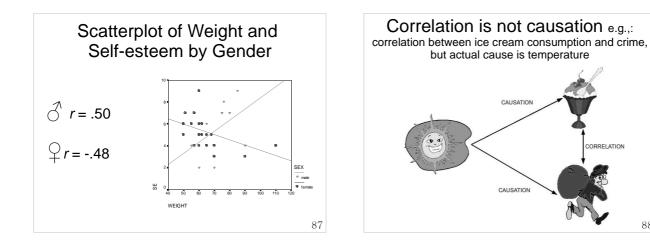


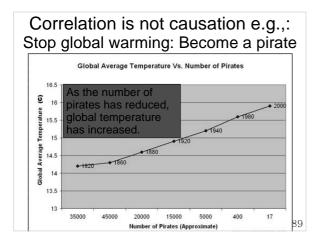
Range restriction

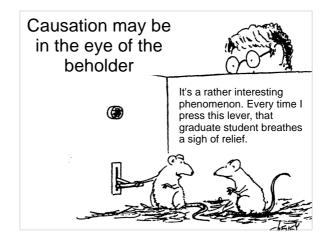
- Range restriction is when the sample contains restricted (or truncated) range of scores
 - -e.g., level of hormone X and age < 18 might have linear relationship
- If range restriction, be cautious in generalising beyond the range for which data is available
 - -e.g., level of hormone X may not continue to increase linearly with age after age 18











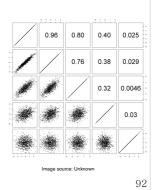
Dealing with several correlations

Dealing with several correlations

Scatterplot matrices organise scatterplots and correlations amongst several variables at once.

However, they are not sufficiently detailed for more than about five variables at a time.

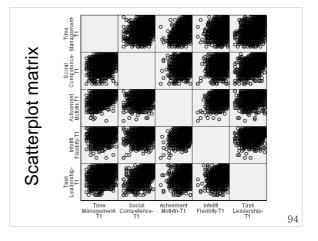
91

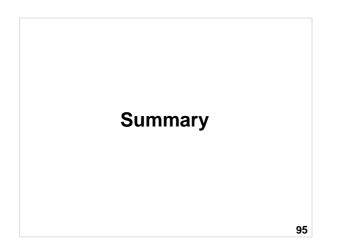


Correlation matrix: Example of an APA Style Correlation Table

Table 1. Correlations Between Five Life Effectiveness Factors for Adolescents and Adults (N = 3640)

	Time Manage- ment	Social Compet- ence	Achieve- ment Motivation	Intellectual Flexibility	Task Leadership
Time Management		.36	.53	.31	.42
Social Competence			.37	.32	.57
Achievement Motivation				.42	.41
Intellectual Flexibility					.37
Task Leadership					
					9





Summary: Covariation

- 1. The world is made of covariations.
- 2. Covariations are the building blocks of more complex relationships which can be analysed through the use of:
 - -factor analysis
 - -reliability analysis
 - -multiple regression

Summary: Purpose of correlation

- 1. Correlation is a standardised measure of the covariance (extent to which two phenomenon corelate).
- 2. Correlation does not prove causation - may be opposite causality, bi-directional, or due to other variables.

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Summary: Types of correlation

- Nominal by nominal: Phi (Φ) / Cramer's V, Chi-squared
- Ordinal by ordinal: Spearman's rank / Kendall's Tau b
- Dichotomous by interval/ratio: Point bi-serial *r*_{pb}
- Interval/ratio by interval/ratio: Product-moment or Pearson's r

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Summary: Correlation steps

- 1. Choose measure of correlation and graphs based on levels of measurement.
- 2. Check graphs (e.g., scatterplot):
 - -Linear or non-linear?
 - -Outliers?
 - -Homoscedasticity?
 - -Range restriction?
 - -Sub-samples to consider?

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Summary: Correlation steps 3. Consider

- -Effect size (e.g., Φ , Cramer's V, r, r²)
- -Direction
- -Inferential test (p)
- 4. Interpret/Discuss
 - -Relate back to hypothesis
 - -Size, direction, significance
 - Limitations e.g.,
 - Heterogeneity (sub-samples)
 - Range restrictionCausality?

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Summary: Interpreting correlation

- Coefficient of determination
 -Correlation squared
 - -Indicates % of shared variance

<u>Strength</u>	<u>r</u>	<u>r</u> ²
Weak:	.13	1 – 10%
Moderate:	.35	10 - 25%
Strong:	> .5	> 25%

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Summary: Asssumptions & limitations

- 1. Levels of measurement
- 2. Normality
- 3. Linearity
- 4. Homoscedasticity
- 5. No range restriction
- 6. Homogenous samples
- 7. Correlation is not causation

Summary: Dealing with several correlations

- Correlation matrix
- Scatterplot matrix

References

Evans, J. D. (1996). *Straightforward statistics for the behavioral sciences*. Pacific Grove, CA: Brooks/Cole Publishing.

Howell, D. C. (2007). *Fundamental statistics for the behavioral sciences*. Belmont, CA: Wadsworth.

Howell, D. C. (2010). *Statistical methods for psychology* (7th ed.). Belmont, CA: Wadsworth. Howitt, D. & Cramer, D. (2011). *Introduction to statistics in psychology* (5th ed.). Harlow, UK: Pearson.

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