CMOS Delay-7 (H.8) Delay Model

20170203

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| References |
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| Some | Figures | from | the | follov | vina | sites |
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[1] http://pages.hmc.edu/harris/cmosvlsi/4e/index.html
 Weste & Harris Book Site

[2] en.wikipedia.org

$$\beta: \text{Device Transconductance Parameter} \\ k: \text{Process Transconductance Parameter} \\ k: \text{Process Transconductance Parameter} \\ \mu: \text{Electron / Hole Mobility} \\ PMOS \quad \beta_{P} = k'_{P} \left(\frac{W}{L}\right)_{P} \qquad k'_{P} = \mu_{P} C_{ox} \quad C_{ox} = \frac{C_{ox}}{C_{ox}} \\ n MOS \quad \beta_{n} = k'_{n} \left(\frac{W}{L}\right)_{n} \qquad k'_{n} = \mu_{n} C_{ox} \quad C_{ox} = \frac{C_{ox}}{C_{ox}} \\ PMOS \quad \beta_{P} = \mu_{P} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{P} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} =$$

Saturation Current $I_{d_{p}} = \frac{\beta_{p}}{2} \left(V_{GSN} - |V_{Tp}| \right)^{2} \qquad V_{Tp} < D$ $I_{d_{n}} = \frac{\beta_{n}}{2} \left(V_{GSN} - V_{Tn} \right)^{3} \qquad V_{Tn} > D$

 $\begin{array}{c} k'_{n} \left(\frac{\omega}{L}\right)_{n} \\ k'_{p} \left(\frac{\omega}{L}\right)_{p} \end{array}$ $\frac{\dot{k_n}}{\dot{k_p}}$ Bn Bp = 2~3 . $\frac{\dot{k'_n}}{\dot{k'_p}} = \frac{\mu_n}{\mu_p} = r$

 $\frac{\beta_{n}}{\beta_{p}} = \frac{k'_{n} \left(\frac{\omega}{L}\right)_{n}}{k'_{p} \left(\frac{\omega}{L}\right)_{p}}$ R $R_n = \frac{1}{\beta_n (V_{pp} - V_{T_n})}$ $R_{p} = \frac{1}{\beta_{n} (V_{pp} - V_{T_{p}})}$ (MJ fall time t_f $T_n = R_n C_{out}$ rise time tr Cp = Rp Cout Cout = Cpara + CL

| fall time | $t_{f} = 2.2 \ C_{n} = l_{n} 9 \ C_{n}$ | $0.9 \ U_{pp} \rightarrow 0.1 \ V_{pp}$ |
|------------------------|---|--|
| rise time | $tr = 2.2 \ C_p = \ln 9 \ C_p$ | $0 \mid \bigvee_{PP} \longrightarrow 0.9 \bigvee_{PD}$ |
| propagation delay time | $t_p = \frac{1}{2} (t_{pf} + t_{pr})$ $= 0.35(t_{pf} + t_{pr})$ | 0.5 Vpp -> 0.5 Vpp |
| propagation fall time | $t_{pf} = 0.7 \tau_n = \ln 2 \tau_n$ | $V_{Pb} \rightarrow 0.5 V_{Pb}$ |
| propagation rise time | tpr = 0.η τρ = ln 2 τρ | 0 → 0.5 Vpb |
| | $T_n = Rn (C_{para} + C_L)$ $T_n = P_n (C_{para} + C_L)$ | • |
| | $C_{p} = R_{p} (C_{pana} + C_{L})$ $C_{out} = C_{pana} + C_{L}$ | |
| | | |
| | | |

$$\begin{pmatrix} \omega \\ \nu \end{pmatrix}_{p} = Y \begin{pmatrix} \omega \\ L \end{pmatrix}_{n}$$

$$Y = \frac{\mu_{n}}{\mu_{p}} = \frac{k_{n}'}{k_{p}'} \neq 1$$

$$R_{n} = R_{p} = R_{m} = \frac{1}{\beta (V_{pp} - V_{T})}$$

$$\begin{cases} U_{but} (t) = V_{pp} (1 - e^{-t/2}) \\ V_{but} (t) = V_{pp} e^{-t/2} \end{cases}$$

$$T = RC_{out} = R (C_{pow} + C_{L})$$

$$Generic Switching Delay$$

$$t_{s} = t_{o} + \alpha C_{L} \Rightarrow t_{s} = t_{r} = t_{f}$$

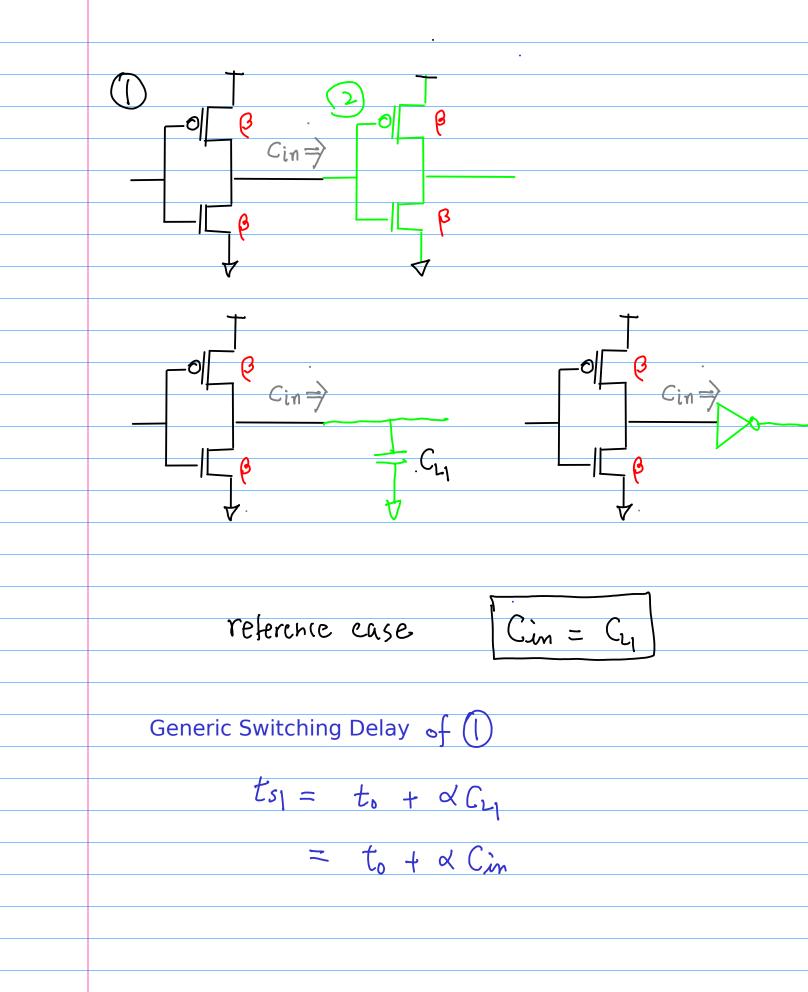
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| Generic Switching Delay |
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| |
| $t_s = t_0 + \alpha C_2$ |
| <u> </u> |
| ts to; zero delan |
| to; zero delay x: slope |
| to |
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| CL |
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| t~rc 1~~ |
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| $\propto \sim $ |
| $\beta(Vpp-V_{T})$ |
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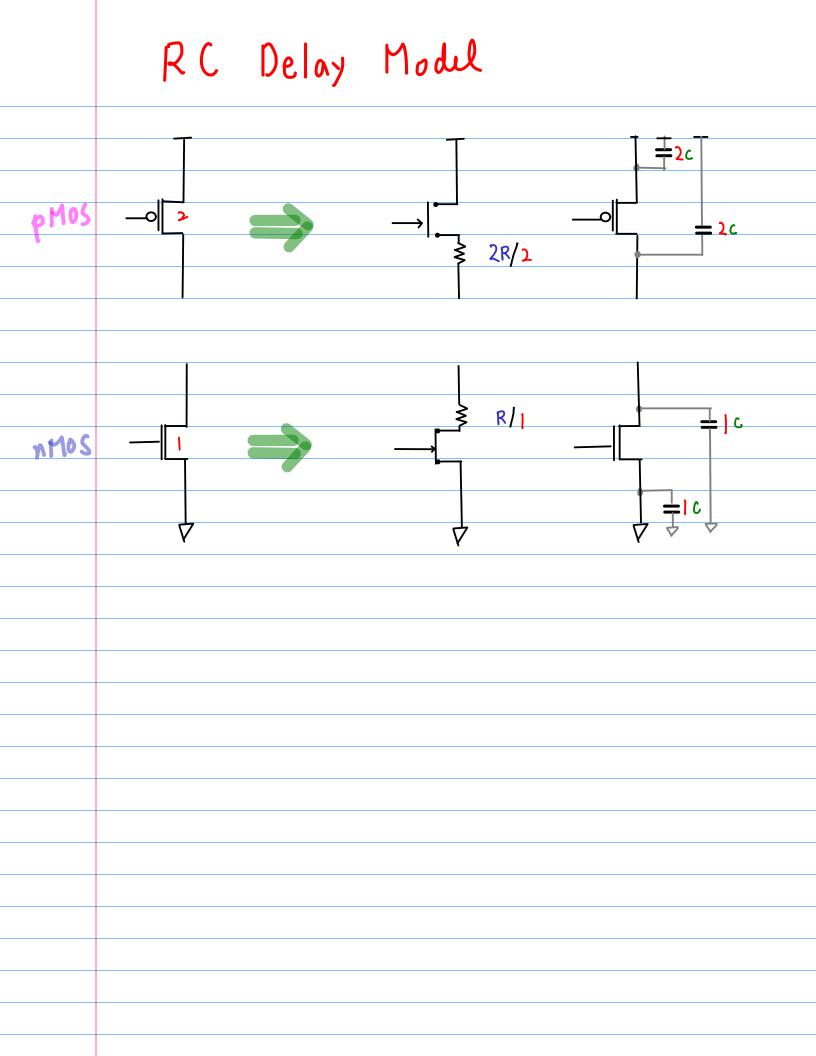


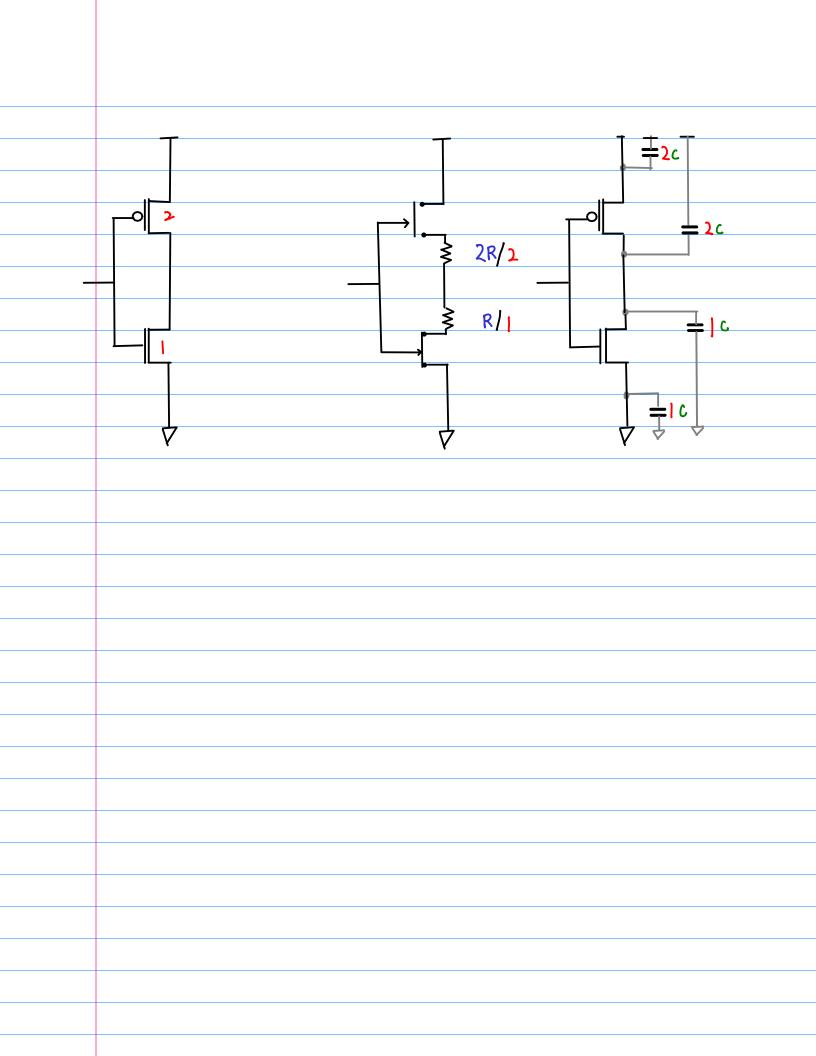


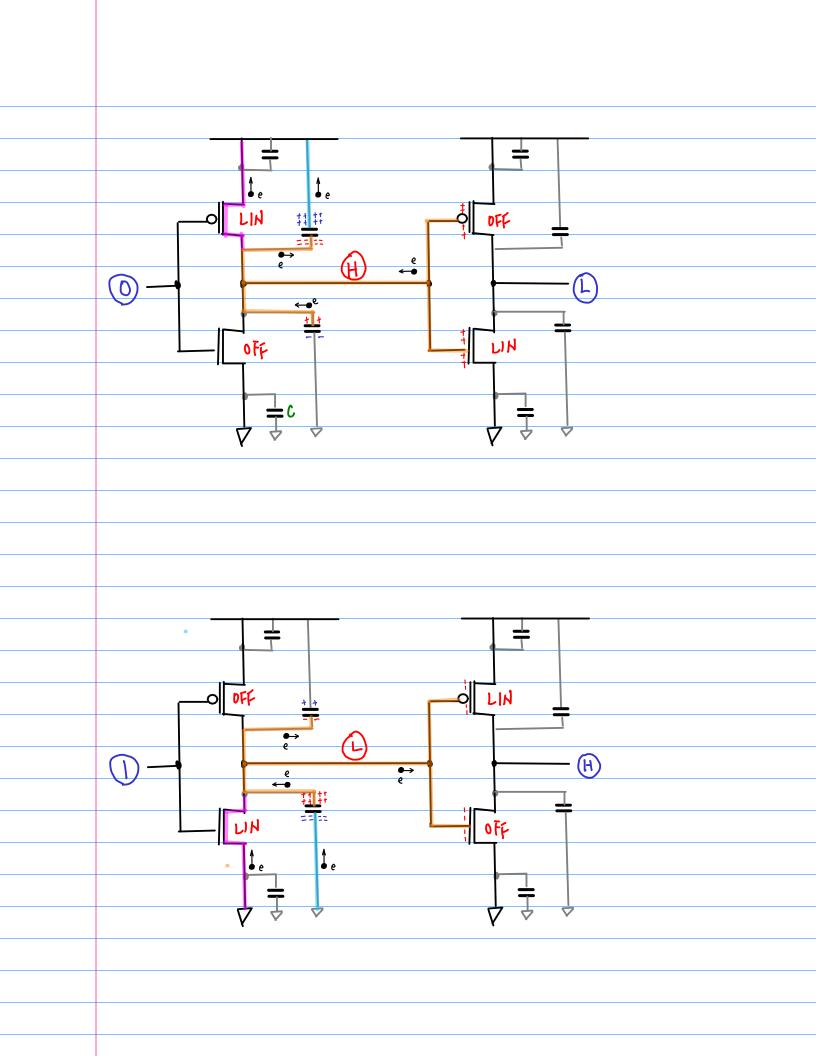
Cin = Can + Cap = Cox (AGn + AGP) Ai gate anea the channel length L assumed Cim = Cox L (Wn + Wp) $= C_{0x}L(W_n + YW_p)$ = $C_{0x} \perp W_{p} \cdot (|+r)$ = $C_{gn}(1+r)$

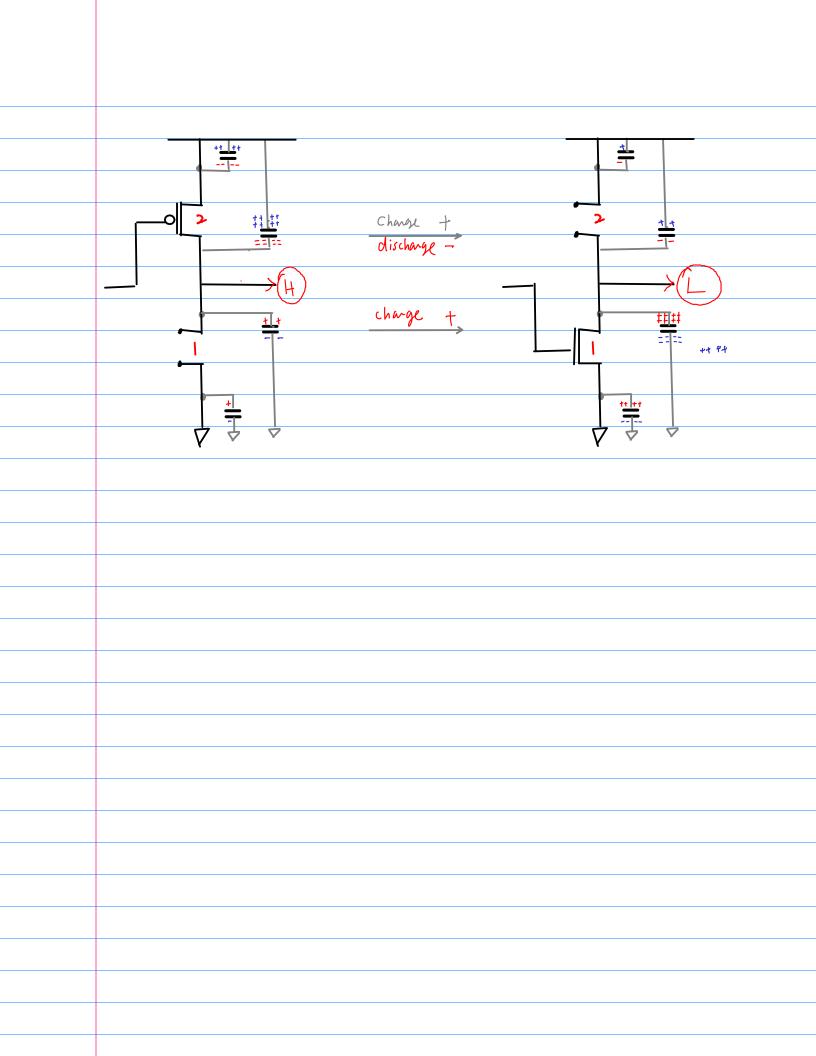
When CL >> Cin -OCin=> ୗ Cin C_{L_1} ß ß B FCL to minimize ts $\forall \downarrow \Rightarrow R \downarrow \Rightarrow \beta \uparrow \Rightarrow bigger size$ speed U.S. anea tradeoff ts = to + dG2 t ~ RC $\propto \propto \frac{1}{\beta(Vpp-V)}$ CL

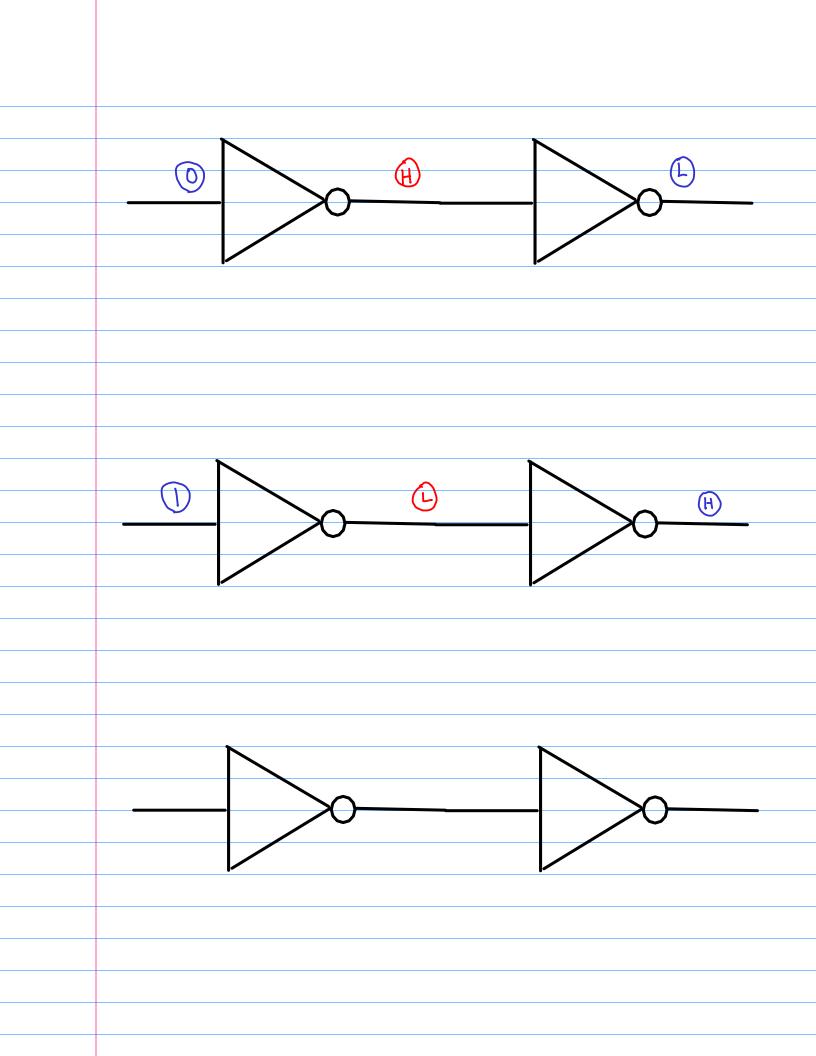
to minimize ts $\mathbb{V} \downarrow \Rightarrow \mathbb{R} \downarrow \Rightarrow \mathbb{B} \uparrow \Rightarrow \text{bigger size}$ speed V.S. anea tradeoff Scaling Factor S. $\beta' = \beta \beta$ $R' = \frac{R}{\sqrt{2}}$ $\alpha' = \alpha'$ $t_s = t_0 + \frac{\alpha}{s} C_L$ Compensation Factor (1) enables a NOT gate drive larger values of (CL) If $C_{L} = 5$ Cin (increased by the scaling factor \$) then the switching time is the same

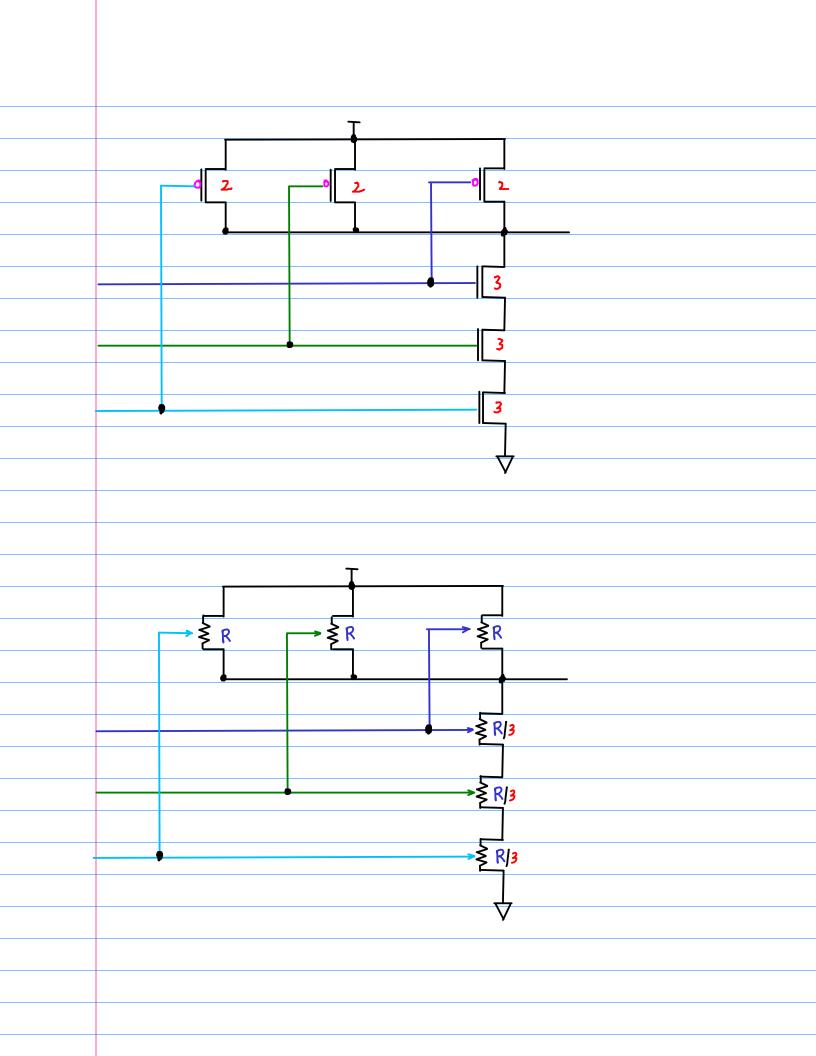


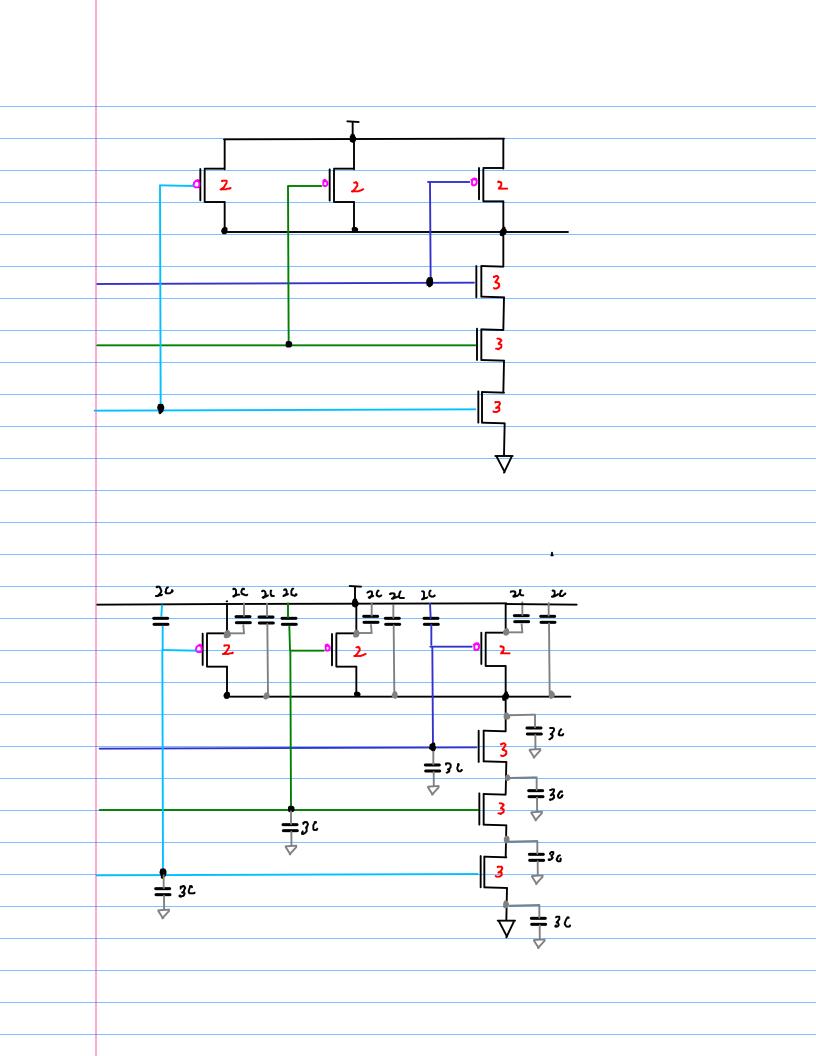


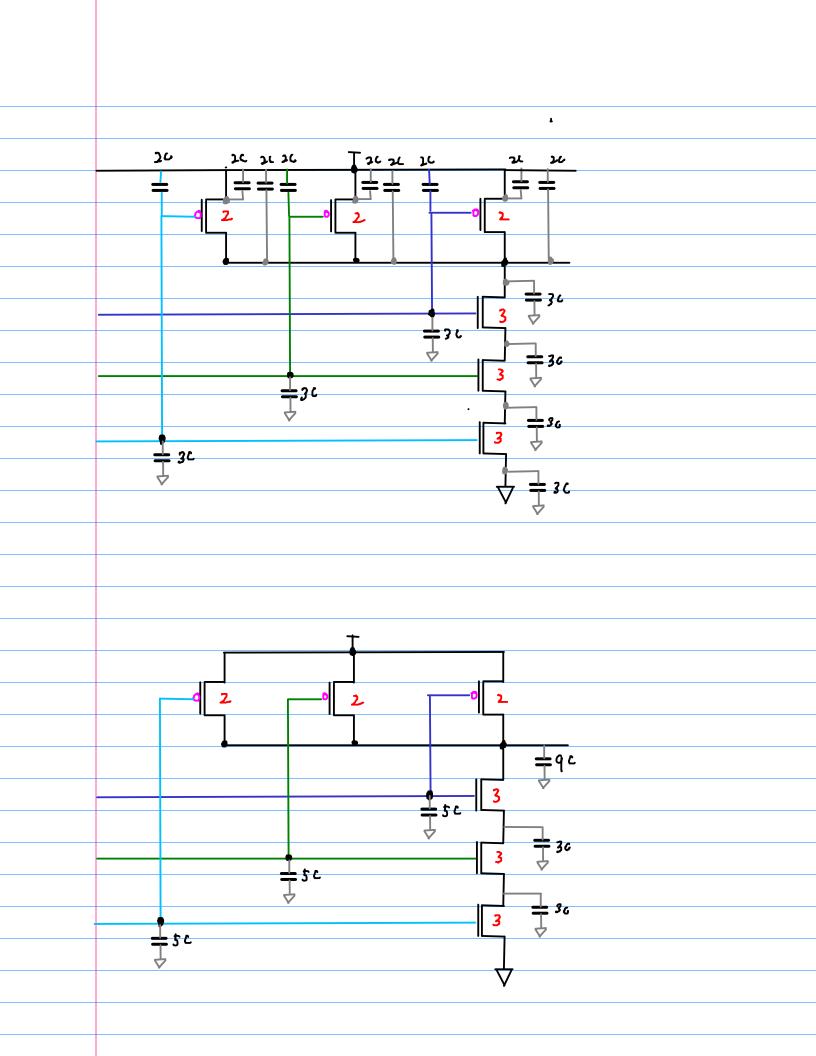


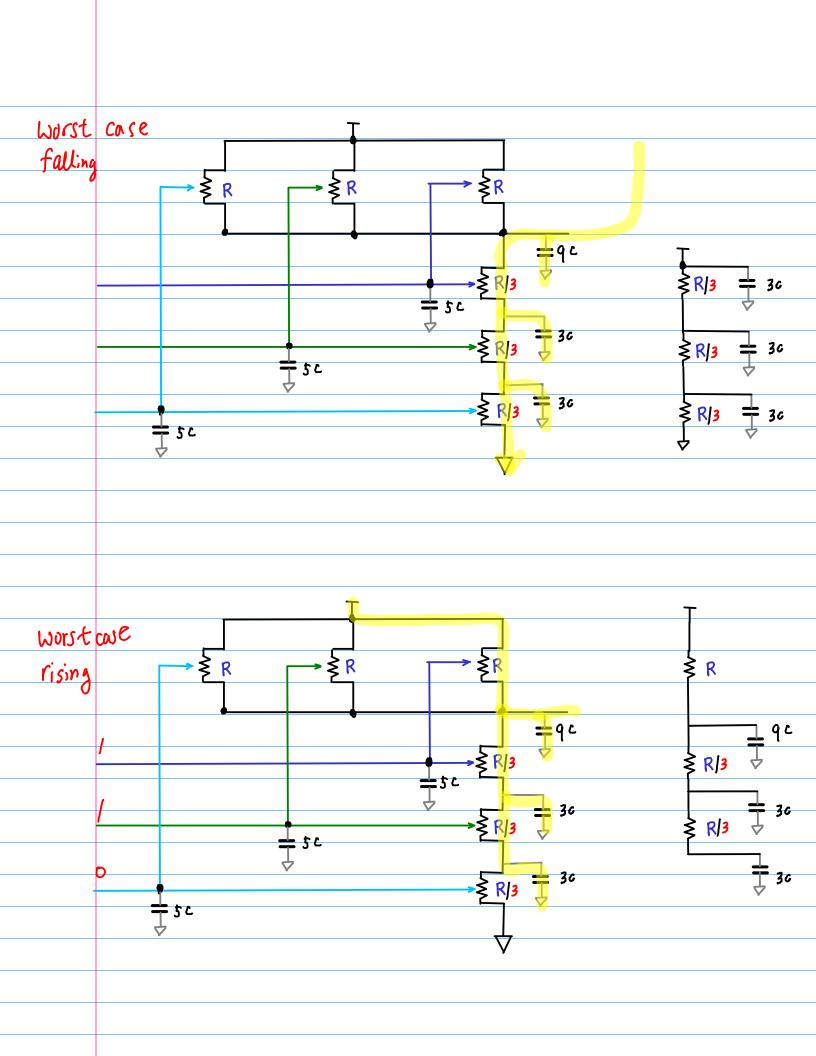


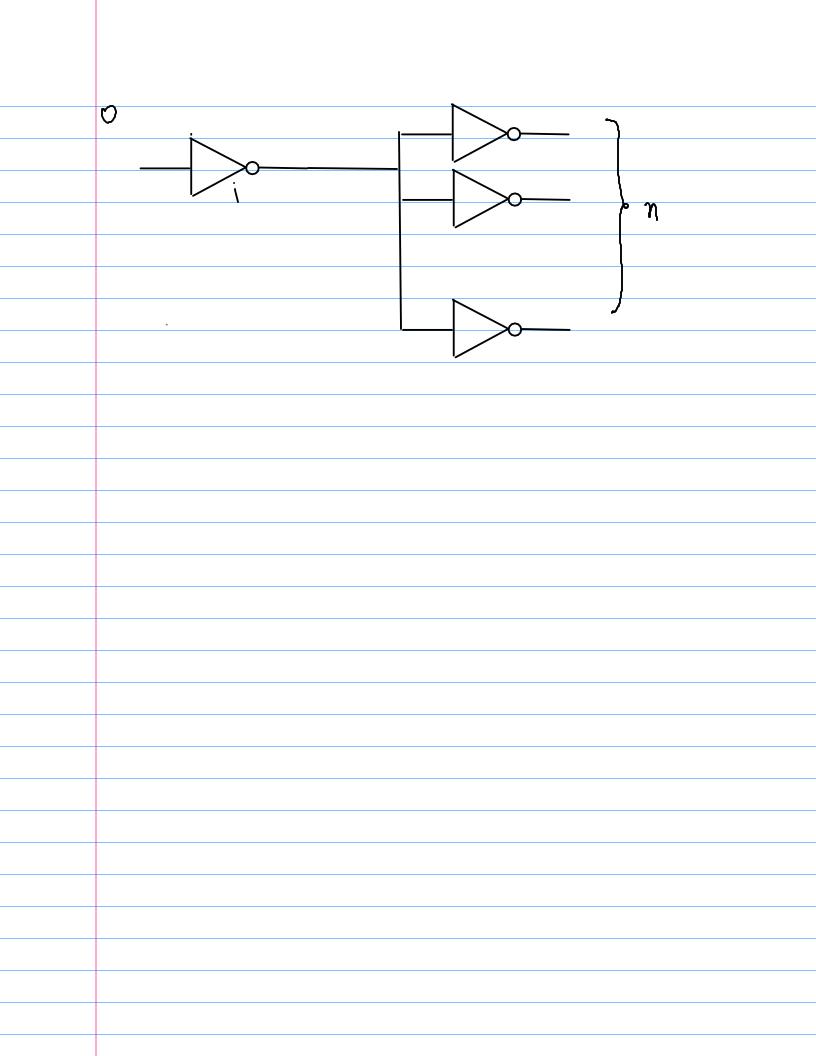


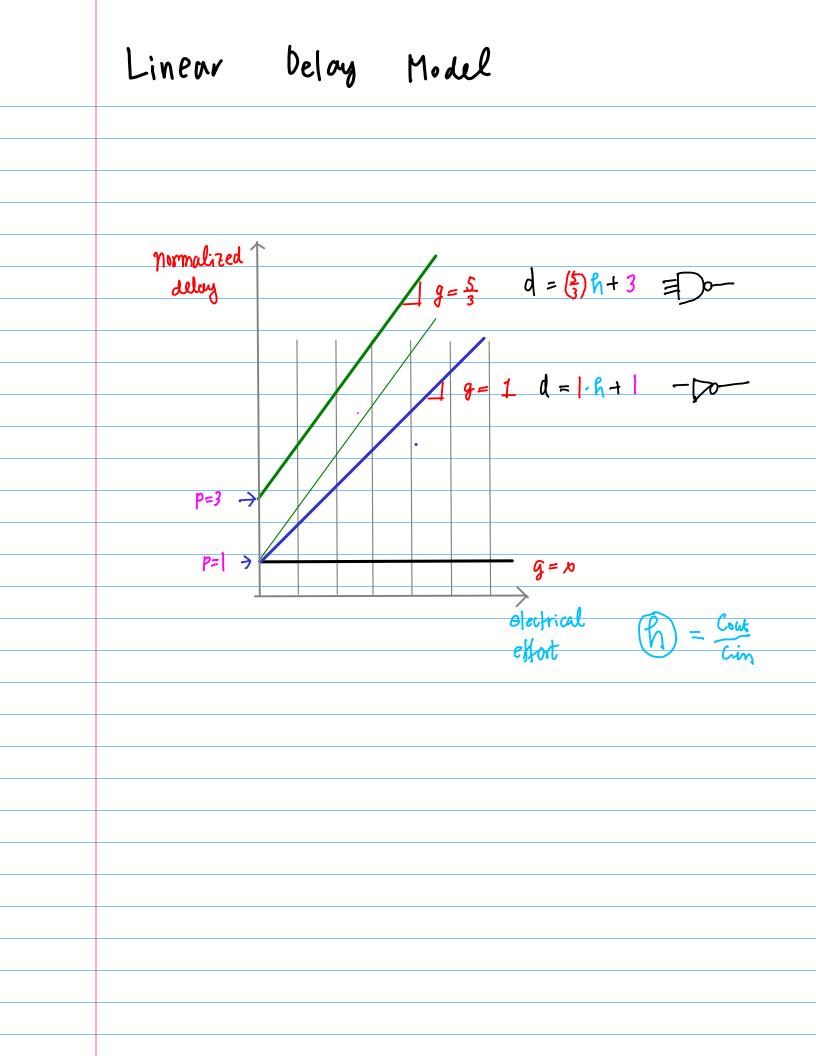


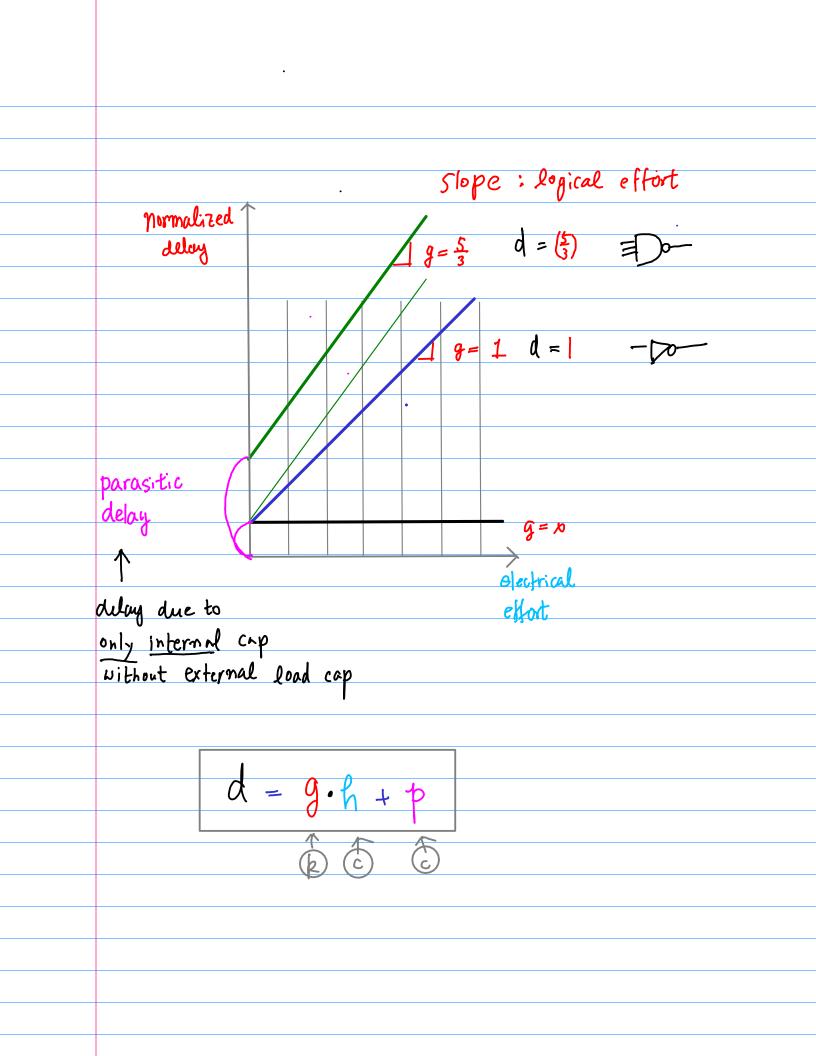


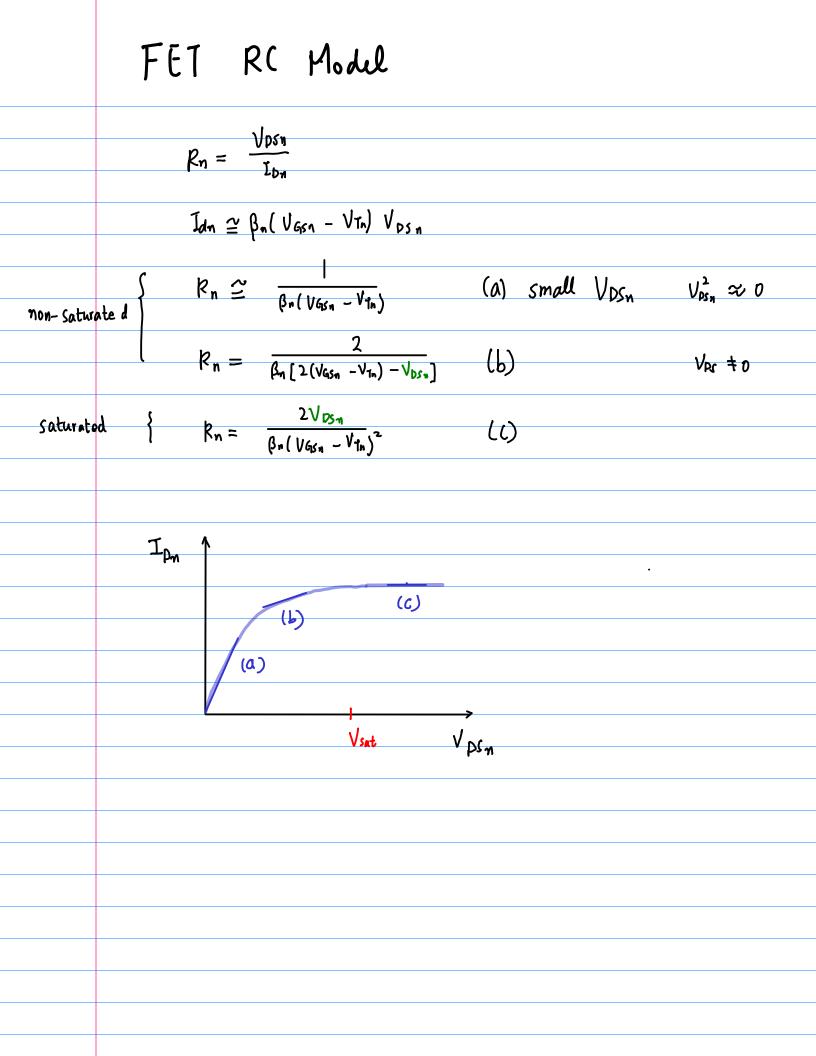












$$R_{n} \propto \frac{1}{\ell_{n}} \qquad (\ell_{n} = k'_{n} \left(\frac{w}{k}\right)_{n}$$

$$R_{n} \approx \frac{\eta}{\ell_{n} \left(\frac{w}{k} + \frac{1}{k}\right)_{n}} \qquad n = 1 - k$$

$$R_{n} = \frac{\eta}{\ell_{n} \left(\frac{w}{k} + \frac{1}{k}\right)_{n}} \qquad n = 1 - k$$

$$R_{n} = \frac{1}{\ell_{n} \left(\frac{w}{k} + \frac{1}{k}\right)_{n}} \qquad g_{n} \qquad \eta = 1$$

$$(a = Cax Aa = Cax WL'$$

$$Cas = \frac{1}{2} Ca$$

$$Cap = \frac{1}{2} Ca$$
April and of p-n junction
$$V_{R}: the revolve bias voltoge$$

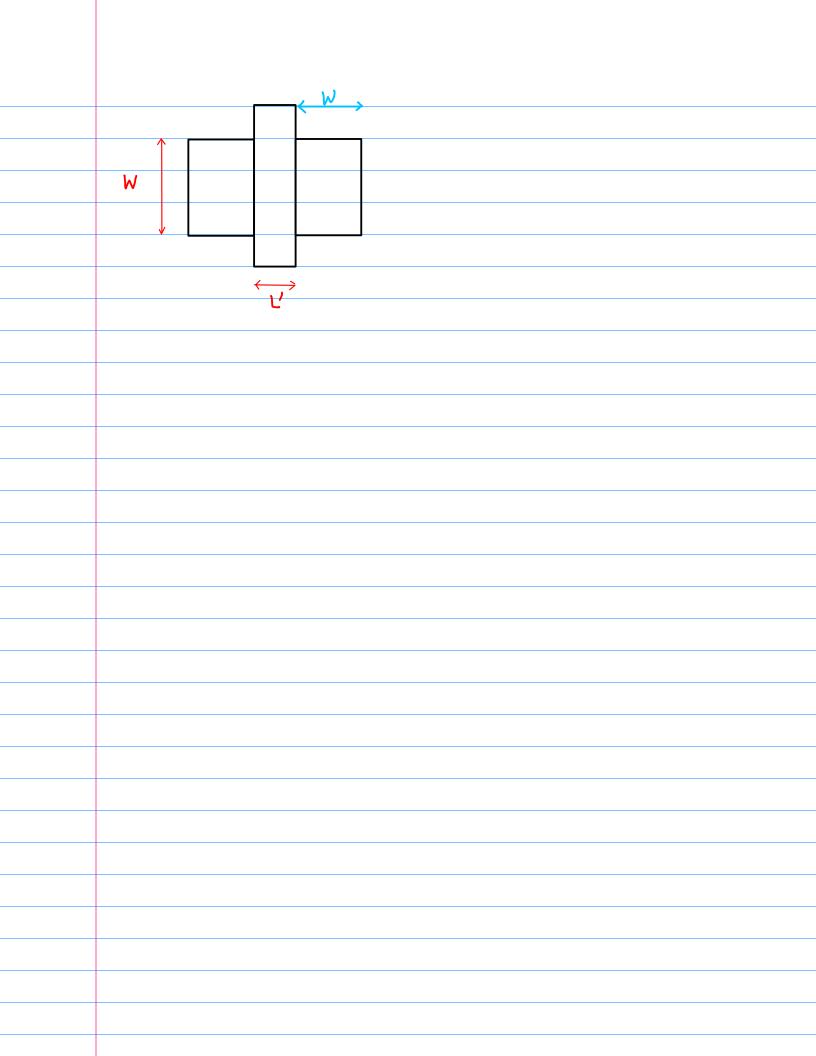
$$C_{0} = C_{j} Apn$$

$$C_{0}: Etro-bias capacitance (V_{R}=0)$$

$$C_{0} = \frac{C_{0}}{(H \frac{V_{R}}{P_{0}})^{m_{j}}}$$

$$f_{0}: built-in potential
$$M_{j}, g_{0} \leftarrow doping \ characteristics$$

$$d_{0} = \left(\frac{kT}{6}\right) Jn \left[\frac{N_{R}N_{R}}{m_{1}^{*}}\right]$$
for an abrupt (step) junction
for a linearly gradud function$$



| $A_{bot} = XW$ |
|---|
| Cbrt = Cj XW |
| $A_{SW} = 2(W \times \chi_{j}) + 2(X + \chi_{j})$ |
| · = Li Psw |
| $P_{SN} = 2(N+X)$ |
| $C_{sw} = C_{jsw} P_{sw}$ |
| $C_{jsw} = C_{j}X_{j}$ |
| |
| X → X + Lo |
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$$C_{\eta} = C_{\mu\nu} + C_{\mu\nu} B_{\mu\nu}$$

$$= C_{\mu} A_{\mu\nu} + C_{\mu\nu} B_{\mu\nu}$$

$$C_{\eta} = \frac{C_{\mu} A_{\mu\nu}}{(1+\frac{\nu}{\mu})^{\nu}} + \frac{C_{\mu\nu} B_{\mu\nu}}{(1+\frac{\nu}{\mu})^{\nu}}$$

$$C_{\mu} = C_{\mu\mu} + C_{\mu\mu}$$

$$C_{\mu} = C_{\mu\nu} + C_{\mu\mu}$$

PFET Characteristics

$$\mathcal{L}_{ox} = \frac{\mathcal{E}_{ox}}{t_{ox}}$$

$$I_{Dp} = \frac{\beta_{p}}{2} \left(\sqrt{s_{\delta p}} - \left| \sqrt{\tau_{p}} \right| \right)^{2}$$

$$\beta_{p} = k_{p}' \left(\frac{W}{L} \right)_{p}$$

$$k_{p}' = \frac{\beta_{p}}{P} C_{ox}$$

$$r = \frac{\beta_{m}}{P} = 2 - 3$$

$$\beta_{m} = k_{m}' \left(\frac{W}{L} \right)_{n}$$

$$\beta_{p} = k_{p}' \left(\frac{W}{L} \right)_{p}$$

$$\sqrt{s_{\delta t}} = \sqrt{s_{\delta p}} - \left| \sqrt{\tau_{p}} \right|$$

$$I_{Dp} = \frac{\beta_{p}}{2} \left[2 \left(\sqrt{s_{\delta p}} - \left| \sqrt{\tau_{p}} \right| \right) \right]^{2}$$

$$R_{p} = \frac{\beta_{p}}{2} \left[\sqrt{s_{\delta p}} - \left| \sqrt{\tau_{p}} \right| \right]^{2}$$

$$R_{p} \propto \frac{1}{\beta_{p}} = \frac{1}{\kappa_{p}' \left(\frac{W}{L} \right)_{p}}$$

$$C_{as} = \frac{1}{2} C_{ap} = C_{ap}$$

$$C_{p} = C_{j} A_{bet} + C_{jsu} P$$

Fall Time Calculation

$$i = -C_{out} \frac{d V_{out}}{dt} = \frac{V_{out}}{R_{\eta}}$$

$$V_{out}(t) = V_{op} e^{-t/Z_{\eta}}$$

$$T_{\eta} = R_{\eta} C_{out}$$

$$t = T_{\eta} L_{\eta} \left(\frac{V_{op}}{V_{out}}\right)$$

$$t_{f} = t_{g} - t_{x} = T_{\eta} l_{\eta} \left(\frac{V_{op}}{R_{\eta} V_{op}}\right) - T_{\eta} L_{\eta} \left(\frac{V_{op}}{\sigma_{\eta} V_{op}}\right)$$

$$= T_{\eta} L_{\eta} (4)$$

$$t_{jul} = t_{f} \cong 3.2 T_{\eta}$$

Rise Time Calculation

$$i = -C_{bbt} \frac{dV_{bct}}{dt} = \frac{U_{00} - V_{aut}}{R_p}$$

$$V_{0at}(t) = V_{pp} [1 - e^{-t/T_p}]$$

$$T_p = R_p C_{aut}$$

$$t = \tau_p L_n \left(\frac{V_{0p}}{V_{aut}}\right)$$

$$t_f = t_p - t_u = \tau_p L_n \left(\frac{V_{0p}}{A_1 V_{uv}}\right) - \tau_n L_n \left(\frac{V_{0p}}{a_1 V_{uv}}\right)$$

$$= \tau_p L_n (9)$$

$$t_{ut} = t_r \approx 2.2 \tau_p$$

Propagation Delay $t_p = \frac{(t_{pf} + t_{pr})}{2}$ $t_{pf} = \ln(2) \cdot \tau_n$ $t_{pr} = ln(2) \cdot \tau_p$ tp ≅ 0.35 (Tn + Tp)

$$C_{out} = C_{FET} + C_{L}$$

$$T_{r} = \sum 2 R_{p} (C_{FT} + C_{L})$$

$$T_{r} = \sum 2 R_{n} (C_{FT} + C_{L})$$

$$T_{r} = t_{ro} + \alpha_{p} C_{L}$$

$$T_{r} = t_{ro} + \alpha_{n} C_{L}$$

$$C_{L} = 0 \Rightarrow T_{r} = t_{ro} \cong 2.1 R_{p} C_{FET}$$

$$C_{L} = 0 \Rightarrow T_{r} = t_{ro} \cong 2.1 R_{p} C_{FET}$$

$$\alpha_{p} = 2.1 R_{p} = \frac{2.2}{\beta_{p} (V_{pp} - |V_{r_{p}}|)}$$

$$\alpha_{n} = 2.1 R_{n} = \frac{2.2}{\beta_{p} (V_{pp} - |V_{r_{p}}|)}$$

$$P_{r} = k'_{p} (\frac{12}{L})_{p}$$

$$P_{n} = k'_{n} (\frac{12}{L})_{n}$$