

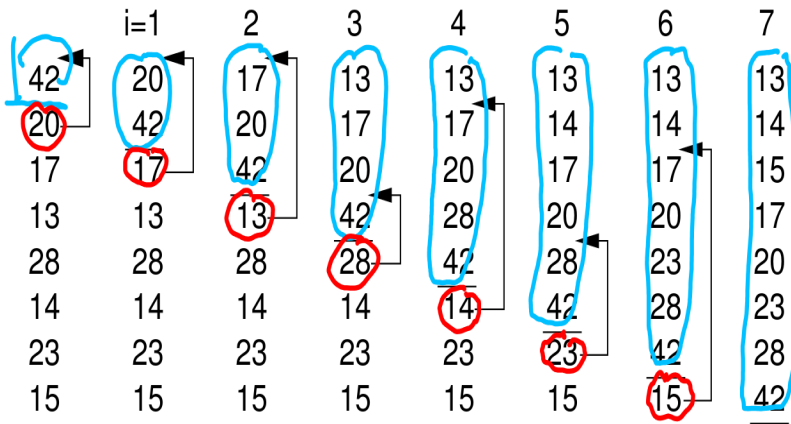
Insertion Sort

20170411

used some pictures and codes from
<http://people.cs.vt.edu/shaffer/Book/C++3elatest.pdf>
Data Structures and Algorithm Analysis
by Clifford A. Schaffer

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42

20

17

13

28

14

23

15

① - A

	$i=1$		$i=2$			$i=3$			
0	42	20	20	20	17	17	17	17	13
1	20	42	42	17	20	20	20	13	17
2	17	17	17	42	42	42	13	20	20
3	13	13	13	13	13	13	42	42	42
4	28	28	28	28	28	28	28	28	28
5	14	14	14	14	14	14	14	14	14
6	23	23	23	23	23	23	23	23	23
7	15	15	15	15	15	15	15	15	15

	$i=4$		$i=5$				
0	13	13	13	13	13	13	13
1	17	17	17	17	17	17	14
2	20	20	20	20	20	14	17
3	42	28	28	28	14	20	20
4	28	42	42	14	28	28	28
5	14	14	14	42	42	42	42
6	23	23	23	23	23	23	23
7	15	15	15	15	15	15	15

② - A

	$i=6$			$i=7$					
0	13	13	13	13	13	13	13	13	13
1	14	14	14	14	14	14	14	14	14
2	17	17	17	17	17	17	17	17	15
3	20	20	20	20	20	20	20	15	17
4	28	28	23	23	23	15	20	20	20
5	42	23	28	28	28	15	23	23	23
6	23	42	42	42	15	28	28	28	28
7	15	15	15	15	42	42	42	42	42

① - B

	$i=1$		$i=2$			$i=3$			
0	42	20	20	17	17	17	17	13	
1	20	42	42	17	20	20	13	17	
2	17	17	17	42	42	13	20	20	
3	13	13	13	13	13	42	42	42	
4	28	28	28	28	28	28	28	28	
5	14	14	14	14	14	14	14	14	
6	23	23	23	23	23	23	23	23	
7	15	15	15	15	15	15	15	15	

	$i=4$		$i=5$				
0	13	13	13	13	13	13	13
1	17	17	17	17	17	17	14
2	20	20	20	20	14	20	17
3	42	28	28	14	28	28	20
4	28	42	42	14	28	28	28
5	14	14	14	42	42	42	42
6	23	23	23	23	23	23	23
7	15	15	15	15	15	15	15

② - B

	$i=6$			$i=7$					
0	13	13	13	13	13	13	13	13	13
1	14	14	14	14	14	14	14	14	14
2	17	17	17	17	17	17	17	17	15
3	20	20	20	20	20	20	20	15	17
4	28	28	23	23	23	23	15	20	20
5	42	23	28	28	28	15	23	23	23
6	23	42	42	42	15	28	28	28	28
7	15	15	15	15	42	42	42	42	42

C++ template

```
#include <stdio.h>
```

```
template <class T>
```

```
T square(T x) {  
    return (x*x);  
}
```

```
int main(void) {
```

```
    int    i2, i=2;  
    float  f2, f=3.0;  
    double d2, d=4.0;
```

```
    i2 = square<int>(i);  
    f2 = square<float>(f);  
    d2 = square<double>(d);
```

```
    printf("i= %d i2= %d \n", i, i2);  
    printf("f= %f f2= %f \n", f, f2);  
    printf("d= %f d2= %f \n", d, d2);
```

```
    return 0;
```

```
}
```

int
float
double

```
template <class T>  
T square(T x) {  
    return (x*x);  
}
```

```
template <typename T>  
T square(T x) {  
    return (x*x);  
}
```

```
square<float>(f);
```

```
int square(float x) {  
    return (x*x);  
}
```

```
square<int>(i);
```

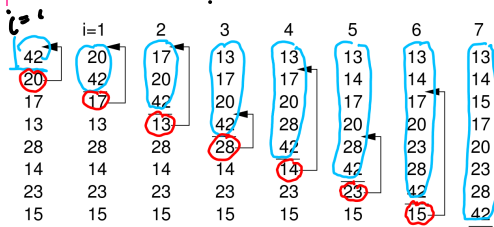
```
int square(int x) {  
    return (x*x);  
}
```

```
square<double>(d);
```

```
double square(double x) {  
    return (x*x);  
}
```

Swap

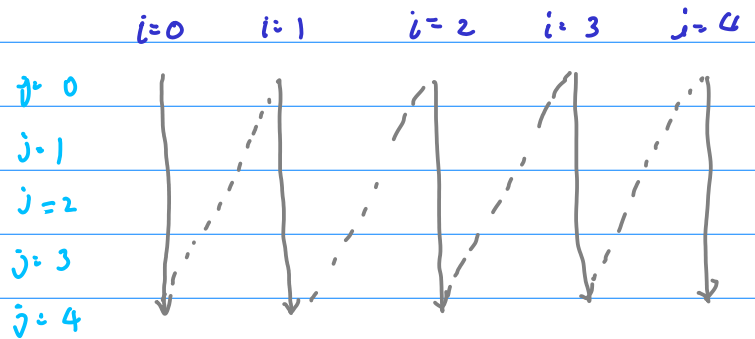
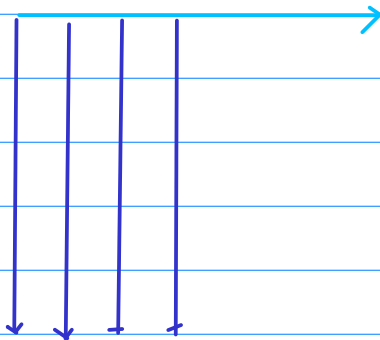
```
// Swap two elements in a generic array
template<typename E>
inline void swap(E A[], int i, int j) {
    E temp = A[i];
    A[i] = A[j];
    A[j] = temp;
}
// Random number generator functions
```

```

template <typename E, typename Comp>
void insert(E A[], int n) { // Insertion Sort
    for (int i=1; i<n; i++) // Insert i'th record
        for (int j=i; (j>0) && (Comp::prior(A[j] < A[j-1])); j--)
            swap(A, j, j-1);
}

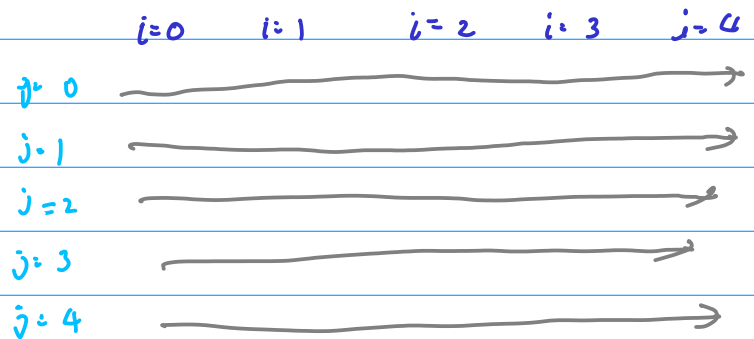
```



```

for (i=0; i<5; ++i)
    for (j=0; j<5; ++j)

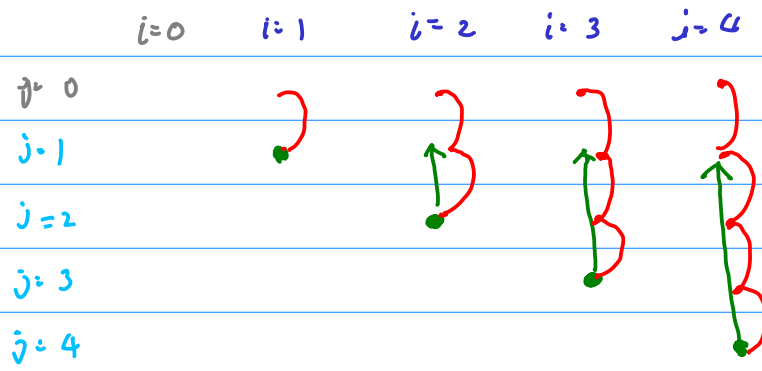
```



```

for (j=0; j<5; ++j)
    for (i=0; i<5; ++i)

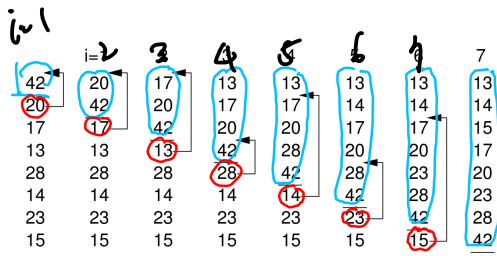
```



```
for (i=1; i<5; ++i)
```

```
  for (j=i; j>0; --j)
```

```
    A[j] < A[j-1]
```



$i=1$ $j=1$

 $i=2$ $j=2$

$i=2$ $j=1$

 $i=3$ $j=3$

$i=3$ $j=2$

$i=3$ $j=1$

 $i=4$ $j=4$

$i=5$ $j=5$

$i=5$ $j=4$

$i=5$ $j=3$

$i=5$ $j=2$

 $i=6$ $j=6$

$i=6$ $j=5$

 $i=7$ $j=7$

$i=7$ $j=6$

$i=7$ $j=5$

$i=7$ $j=4$

$i=7$ $j=3$

for $i = 1$ to N

for $j = 2$ to $(N-1)$

③ do {
 Read $A[i, j]$;
 Write $A[i, j]$;
}

$(N-1) \cdot 2 + 1$

$(N-2) \times 2$

↑
Read
Write

실행되는 명령어의 횟수

└ Read = A

Write A =

Comp A < B >

$$N \times (N-2) \times 2 = 2N^2 - 4N = \underline{O(N^2)}$$

Quadratic time Alg.

```
#define MAX 9000000
```

```
for (i = 1000 to N-20000
```

```
  for (j = 2 to MAX
```

```
    do {
```

```
      Read A[i,j];
```

```
      write A[i,j];
```

```
    }
```

$$N - 20000 - 1000 \\ \approx N - 19000$$

$$9000000 - 2 + 1 \\ \boxed{8999999}$$

$$(N - 19000) \times \underline{8999999} \times 2 = \underline{O(N)}$$

linear time alg.

References

- [1] <http://en.wikipedia.org/>
- [2] <http://people.cs.vt.edu/shaffer/Book/C++3elatest.pdf>