

Capacitor in an AC circuit

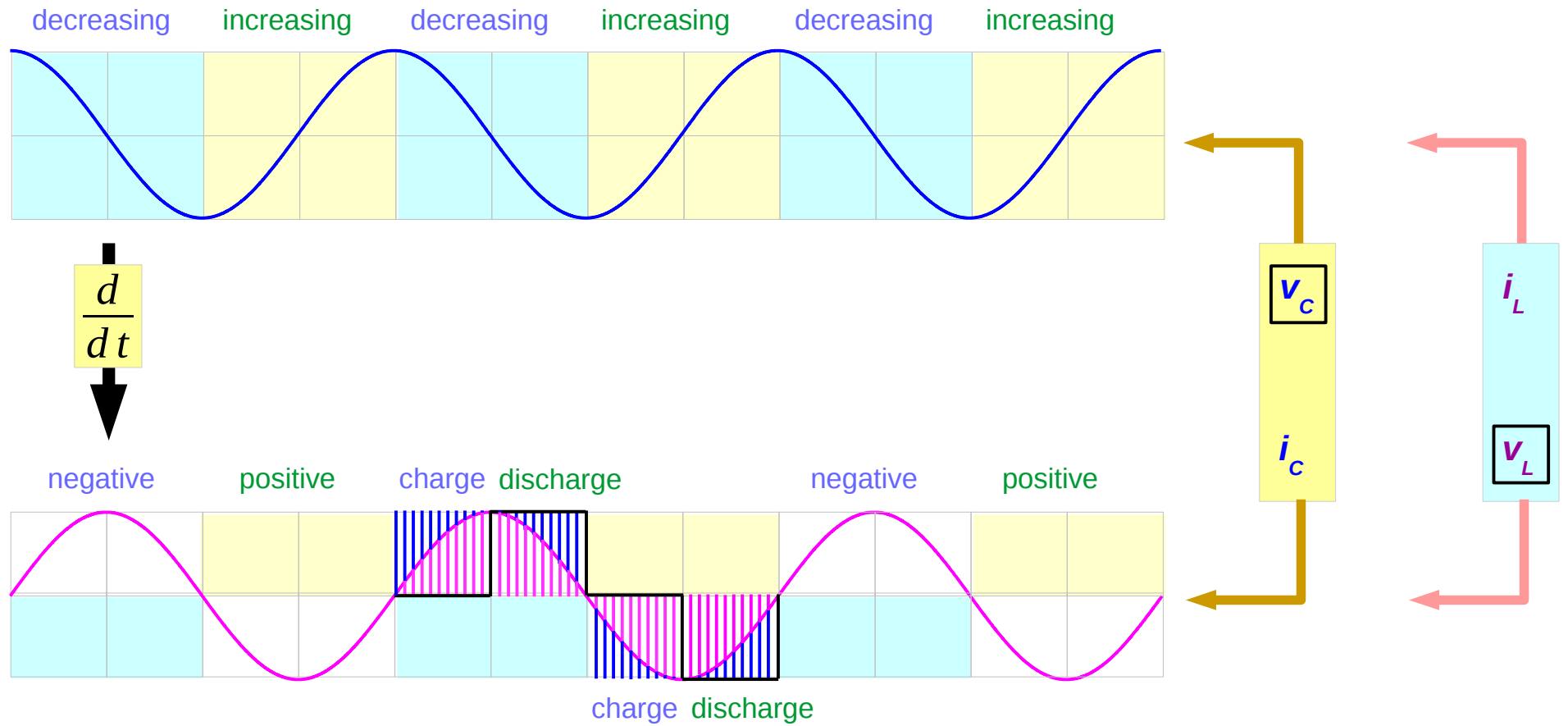
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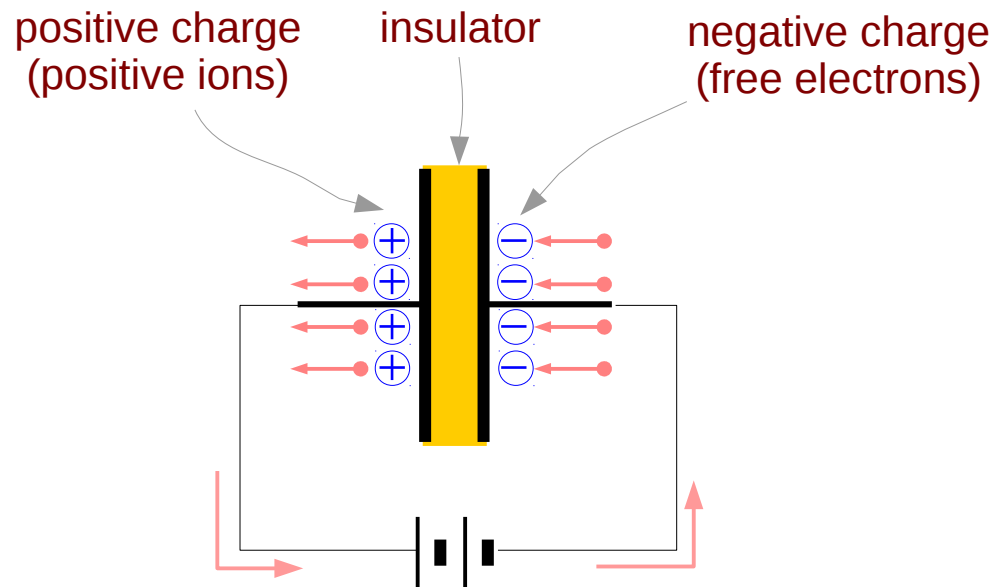
Please send corrections (or suggestions) to youngwlim@hotmail.com.

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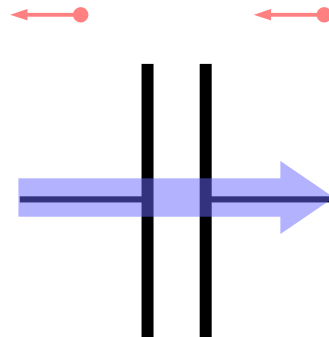
Everchanging signal pairs



Capacitor Current

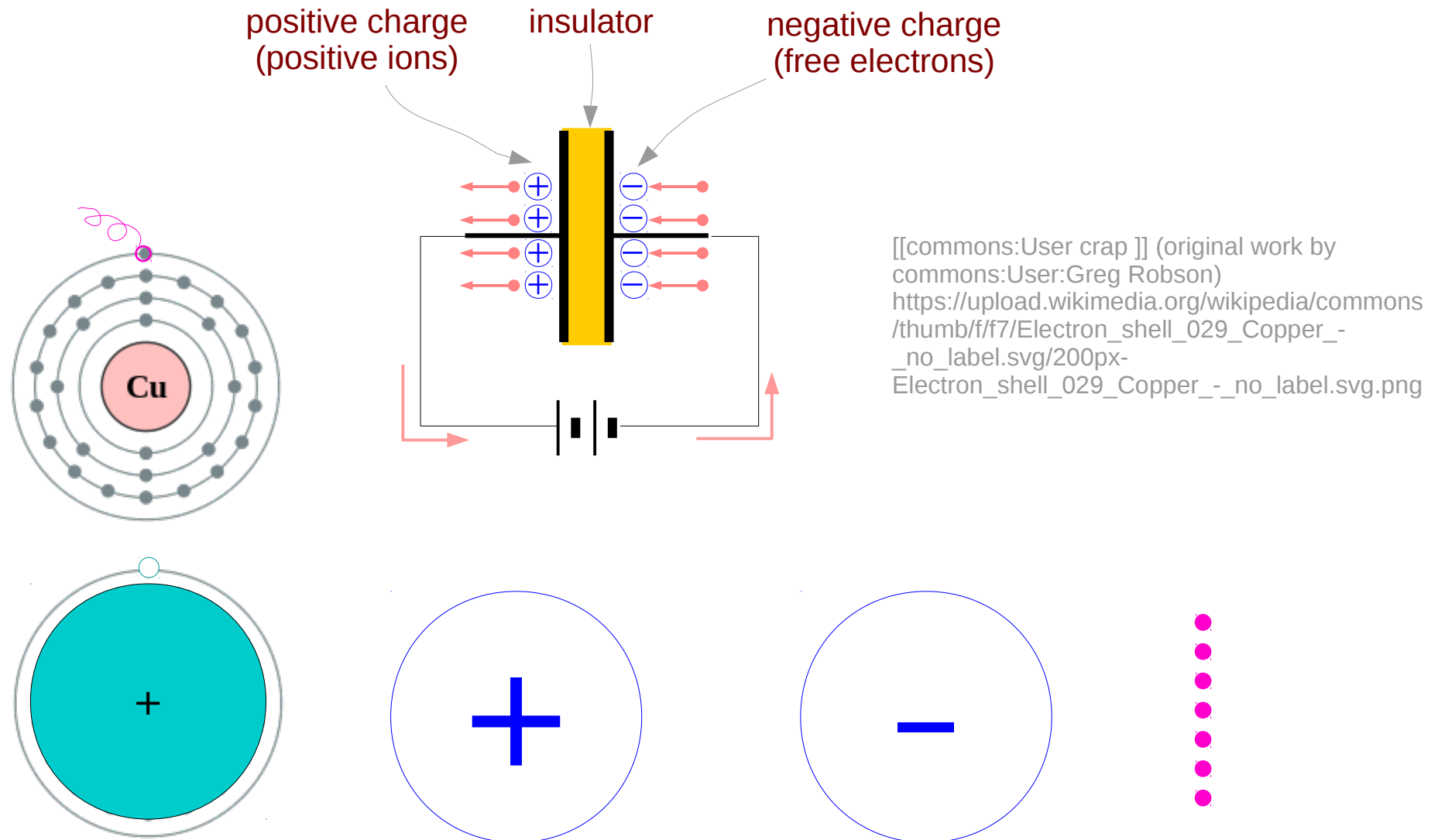


Think as electrons move to the left



Displacement Current

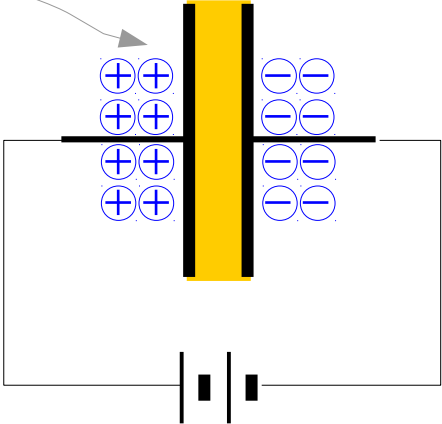
Positive ions and free electrons



Three States

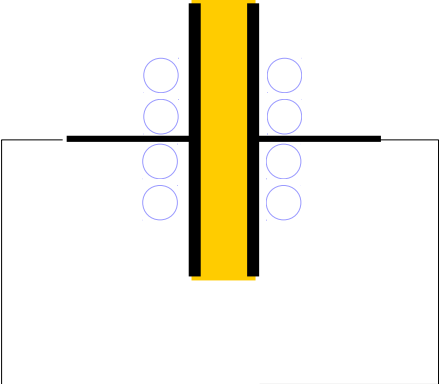
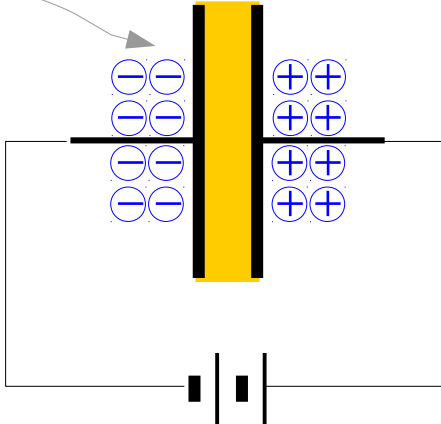
positive charge
(positive ions)

Positive Charged State



negative charge
(free electrons)

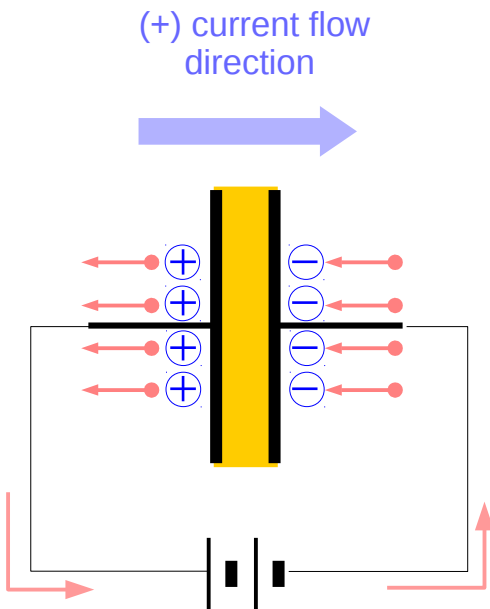
Negative Charged State



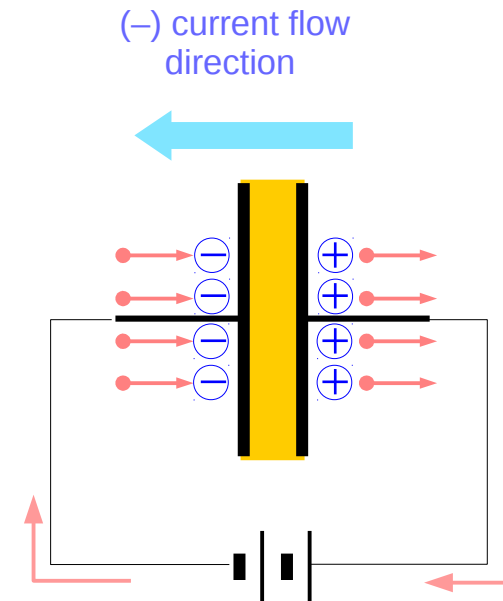
Fully Discharged State

Inter-State Current Flowing

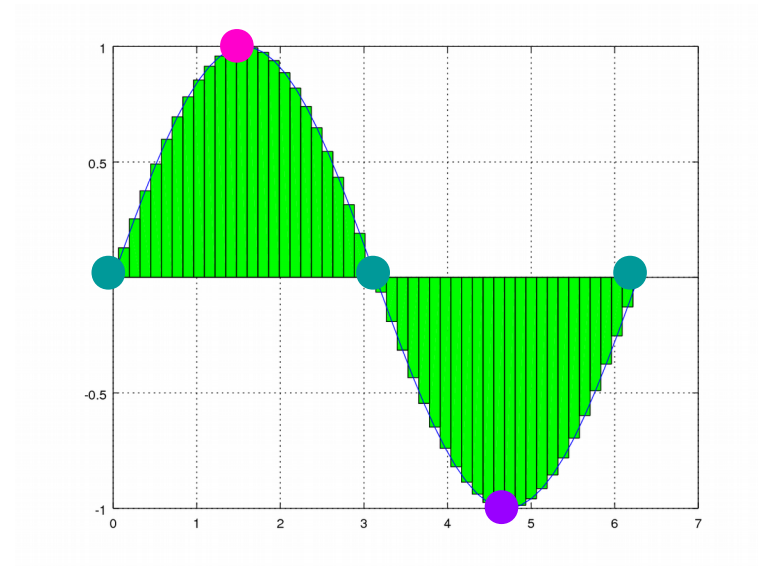
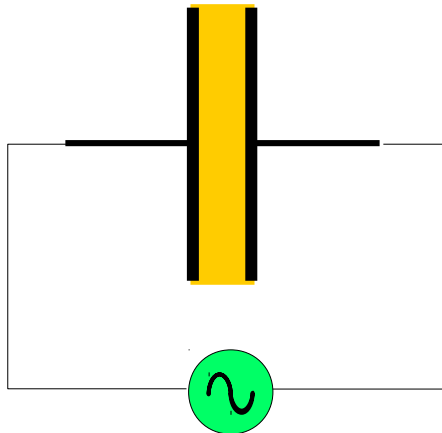
Positive Charging



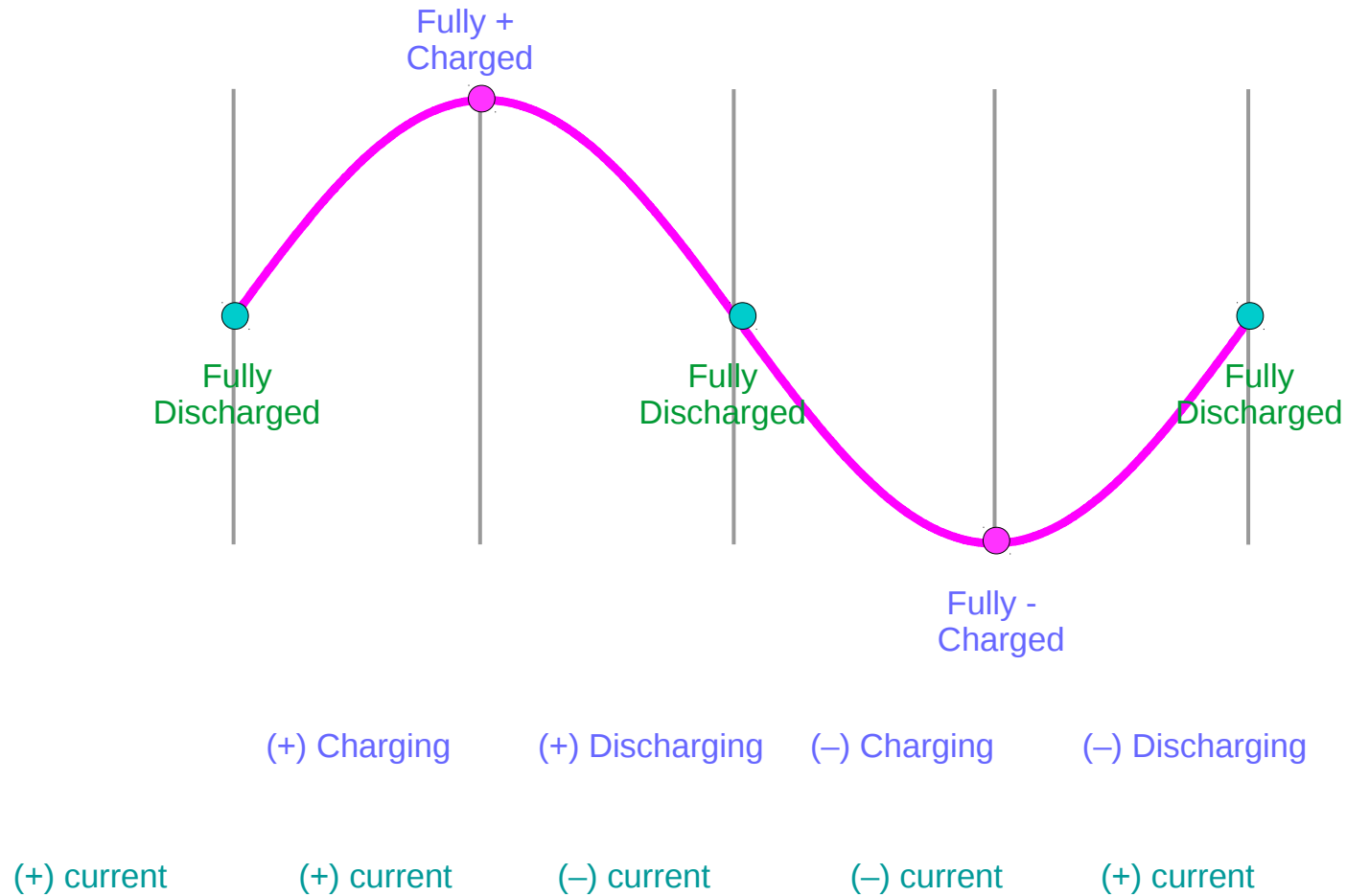
Negative Charging



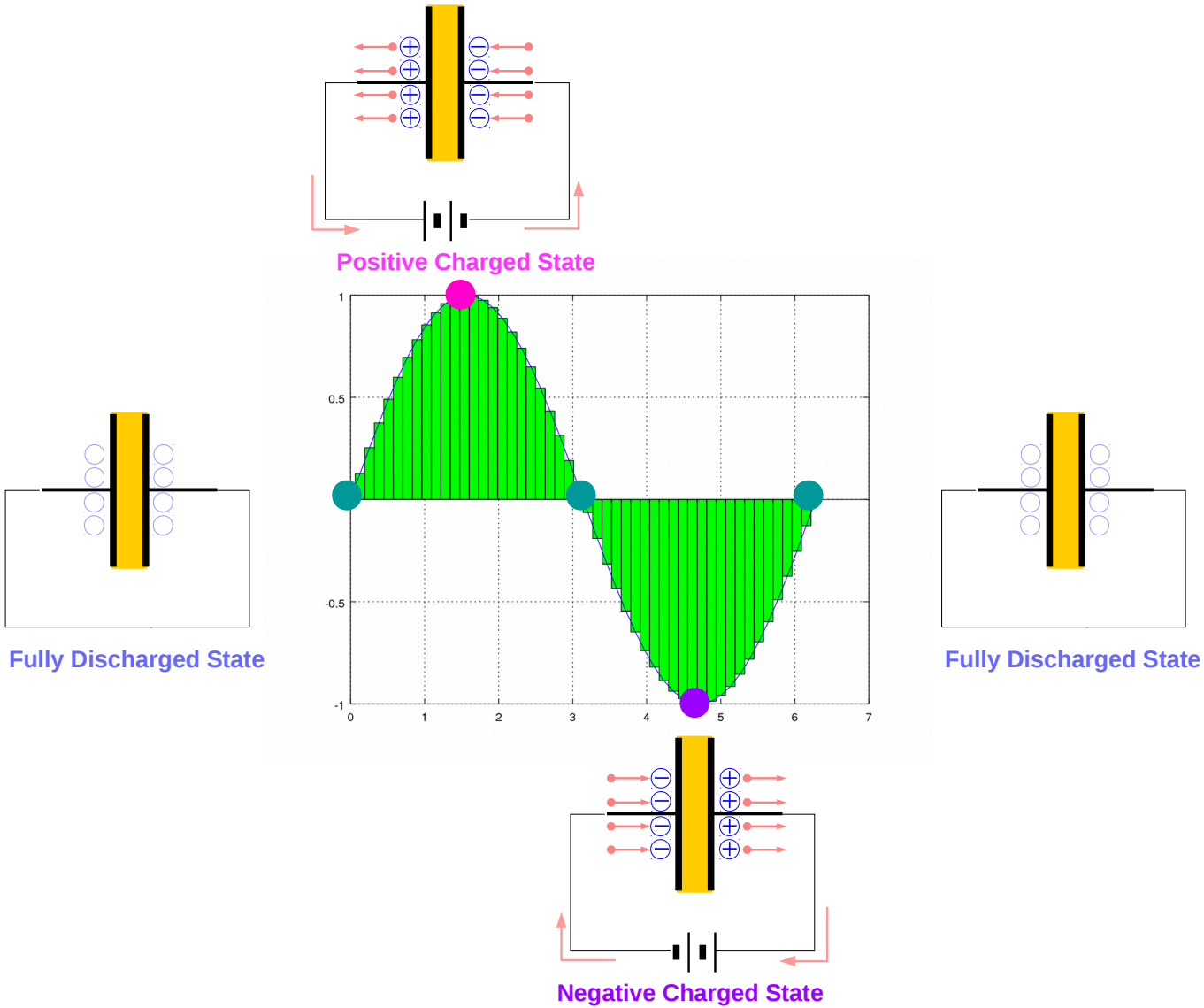
An AC Voltage Source



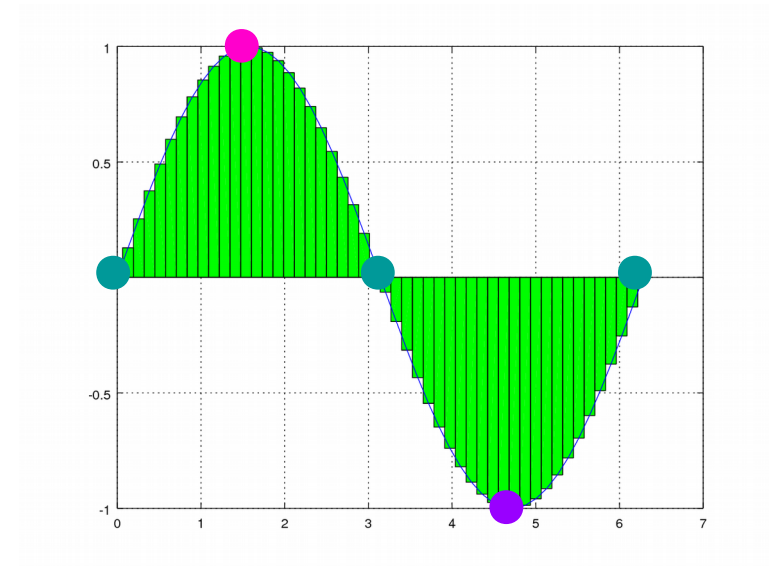
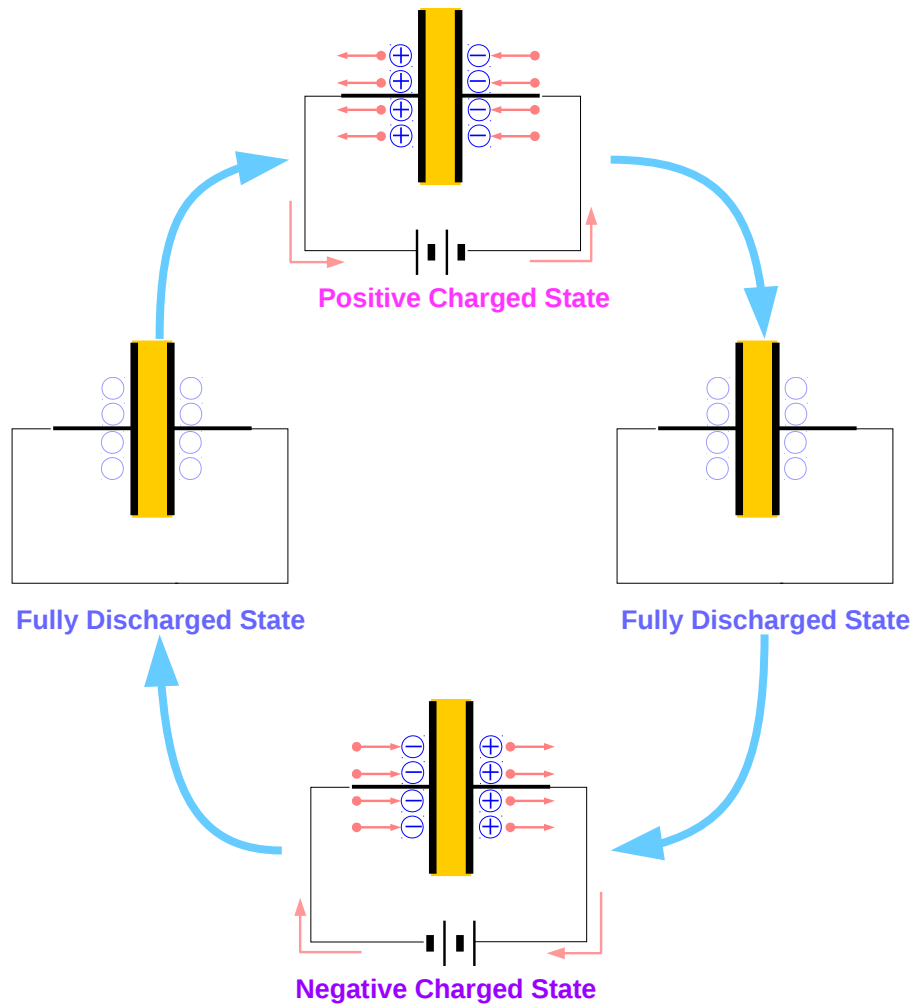
Fully Charged and Fully Discharged



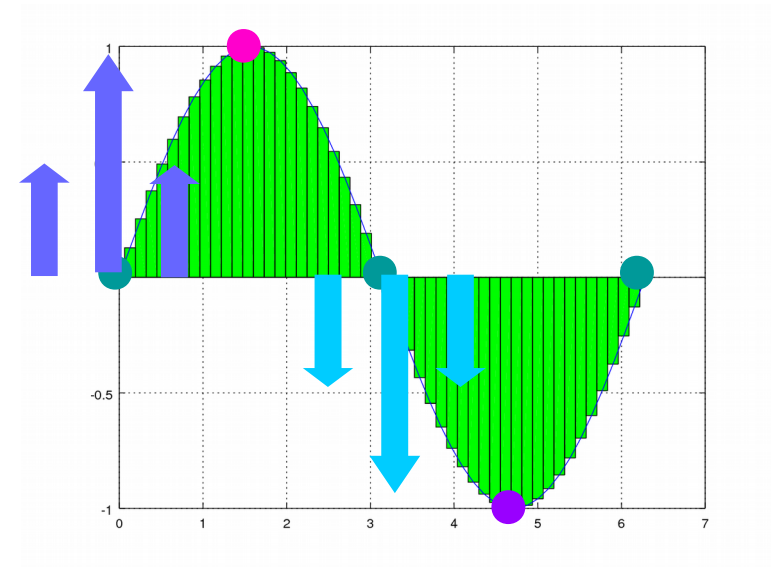
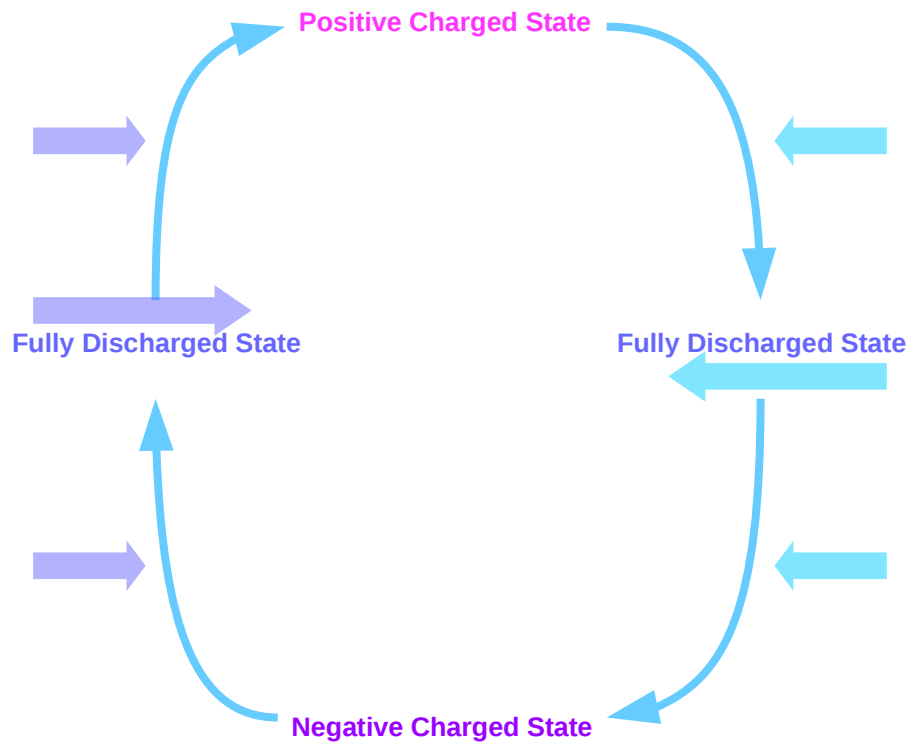
A Cycle



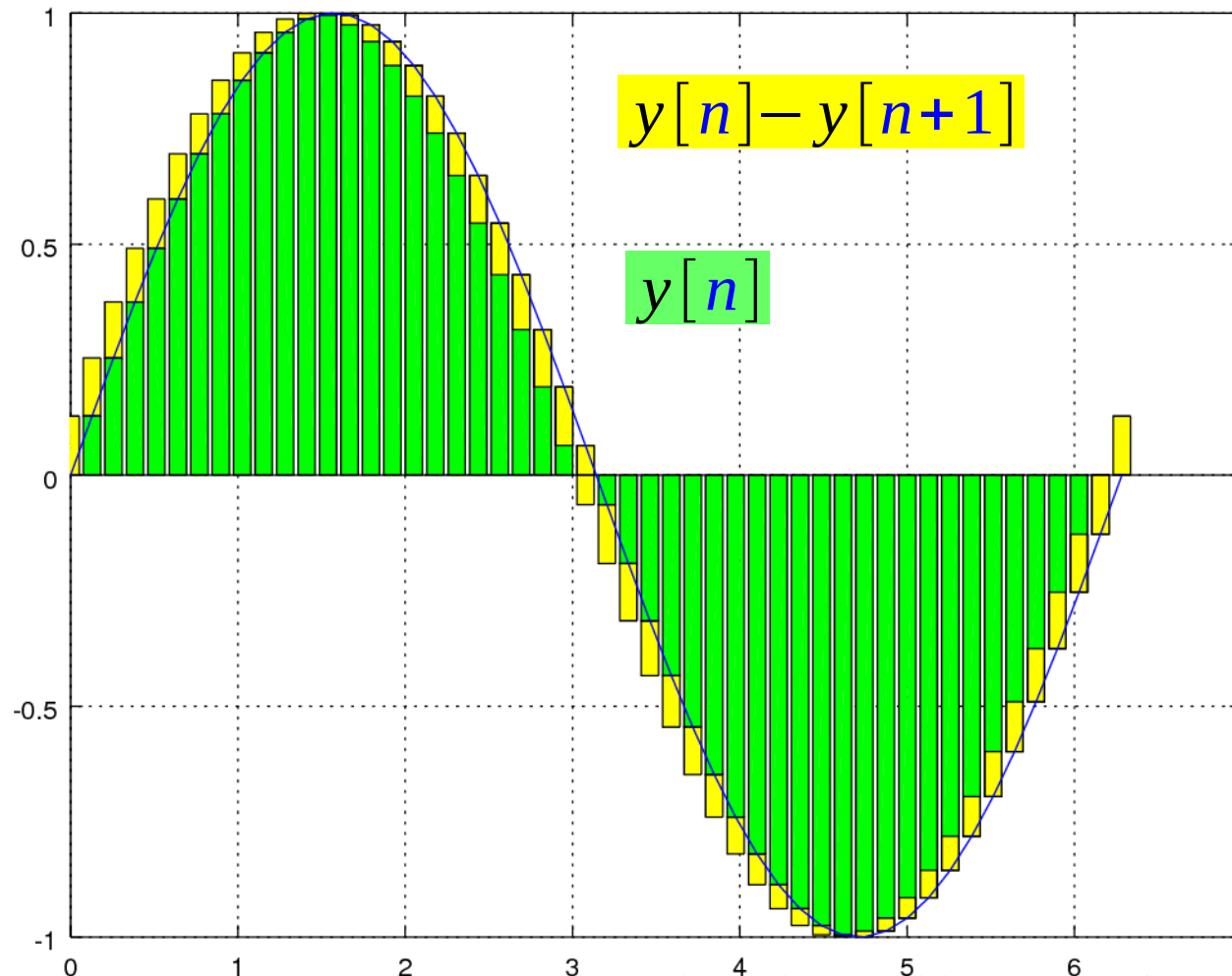
State Transition Diagram



Current Flow



Fully Charged and Fully Discharged



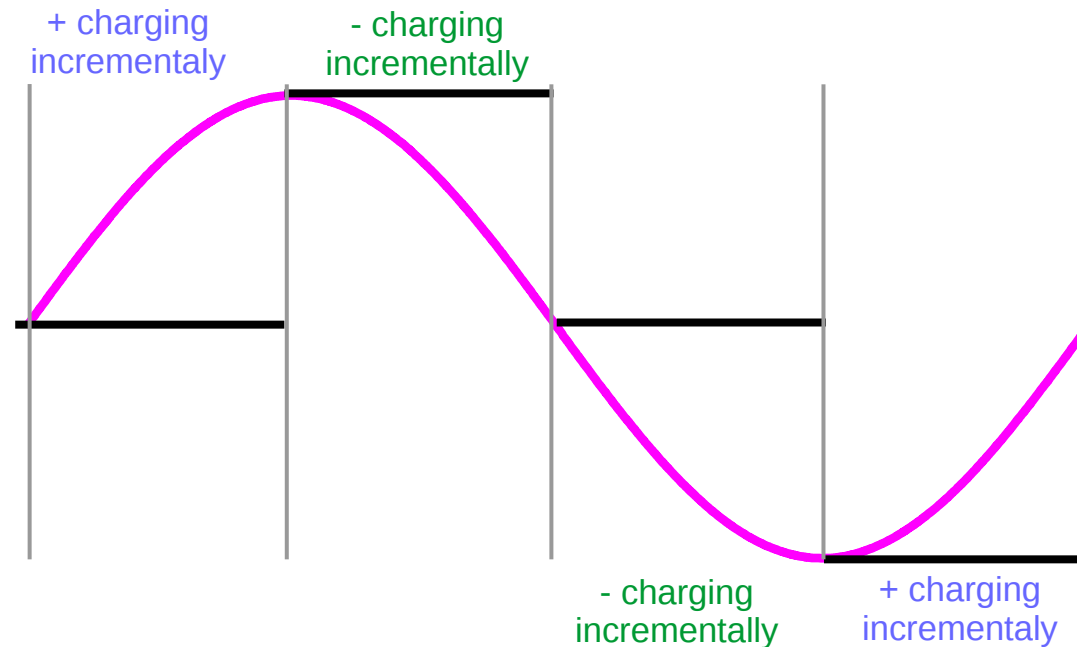
```
h = bar(t1, [y1' y2'],  
"stacked")  
set(h(1), "facecolor", "g");  
set(h(2), "facecolor", "y");  
hold on  
plot(t1, y1)  
axis([0 7 -1 1]);
```

$$y[n] - y[n+1] = y(nT) - y((n+1)T) = \sin(nT) - \sin((n+1)T)$$

Continuous Charging and Discharging Operations

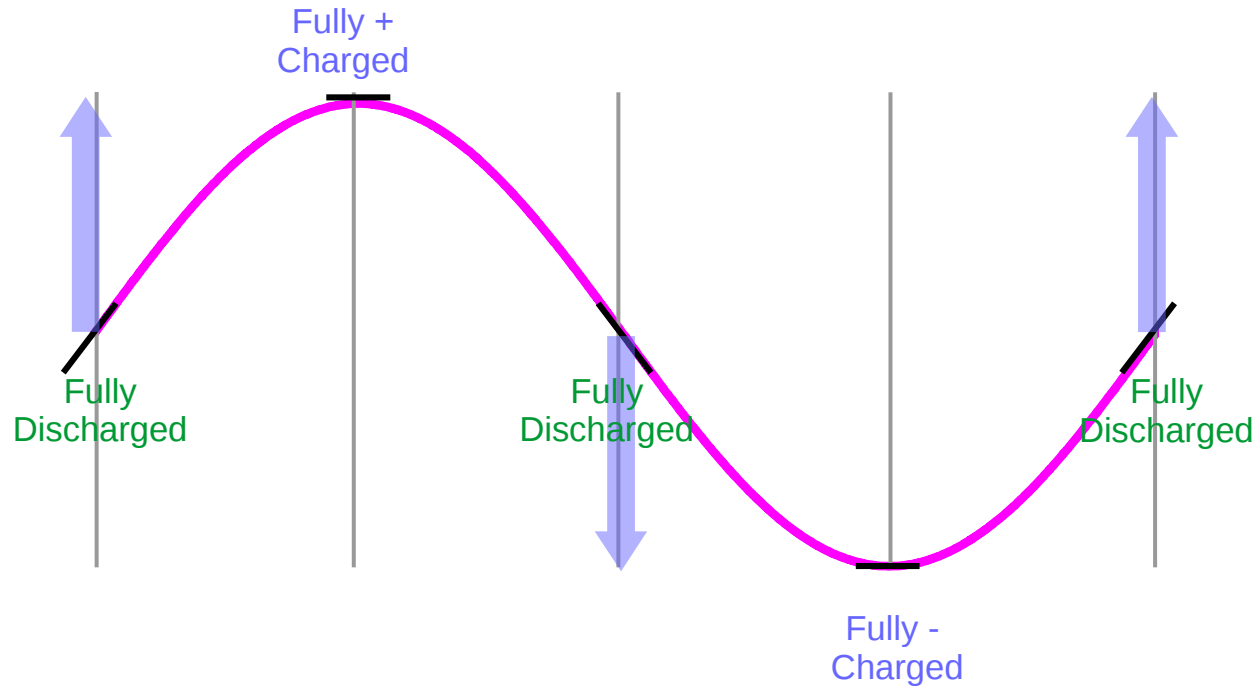
Incremental Voltage Increment \rightarrow + Charging incrementally

Incremental Voltage Decrement \rightarrow - Charging incrementally

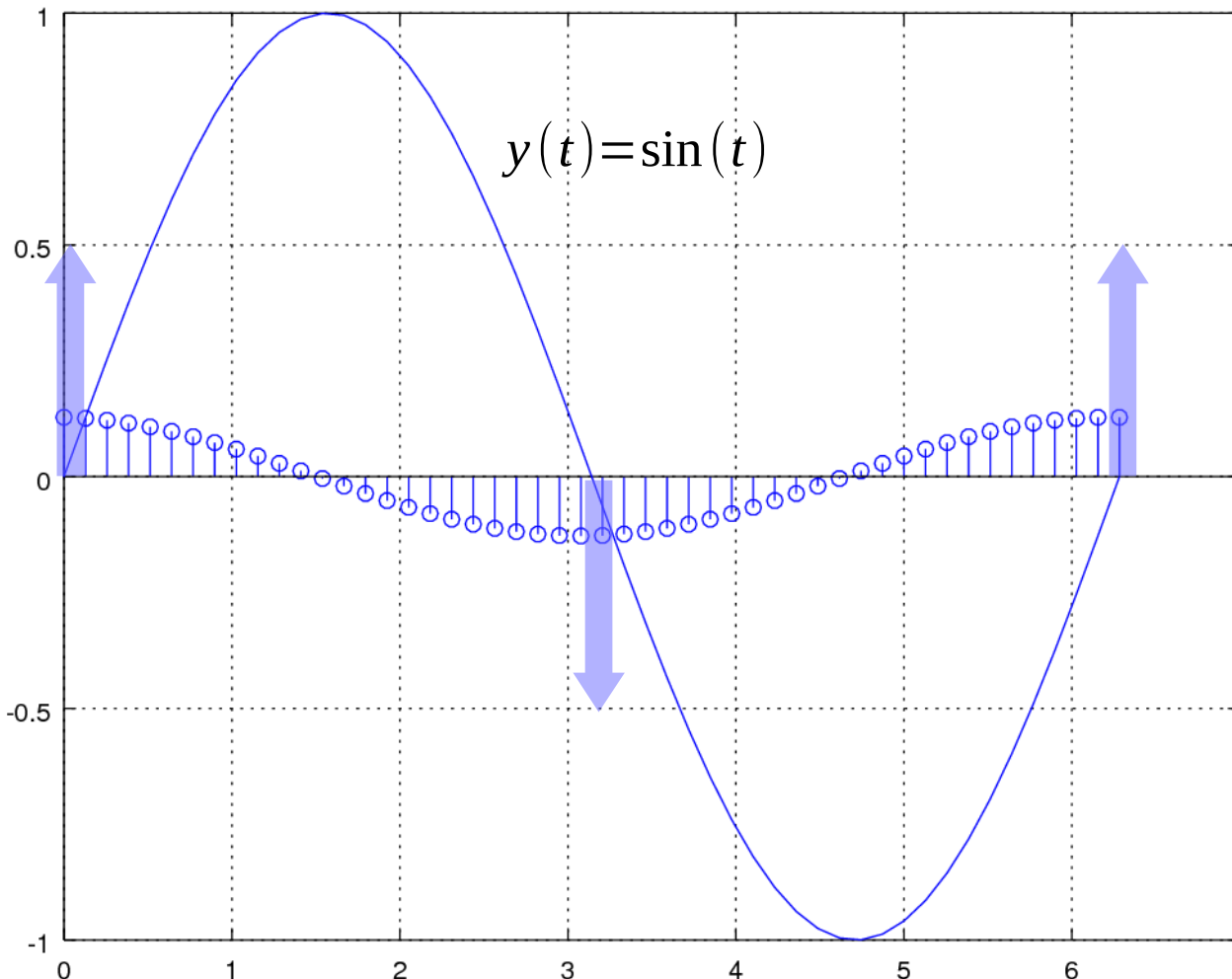


Fully Discharged : Large Current

Incremental Voltage Increment → Continuous Charging
Incremental Voltage Decrement → Continuous Discharging



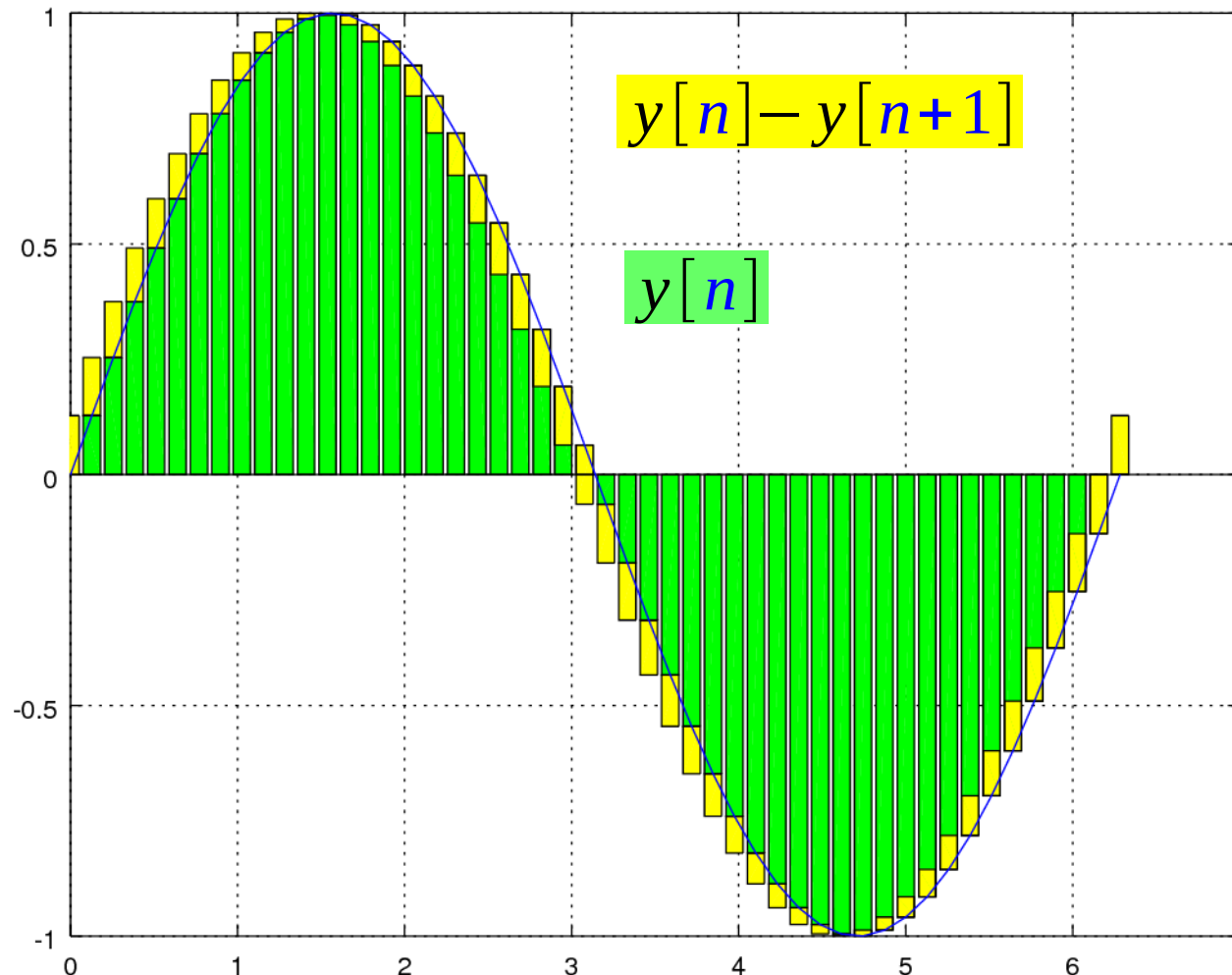
$y[n+1] - y[n]$



```
t = linspace(0, pi*2, 50);  
t1 = t;  
t2 = t + t(2);  
y1 = sin(t1);  
y2 = sin(t2) - sin(t1);  
stem(t1, y2)  
hold on  
plot(t1, y1)
```

$$y[n] - y[n+1] = y(nT) - y((n+1)T) = \sin(nT) - \sin((n+1)T)$$

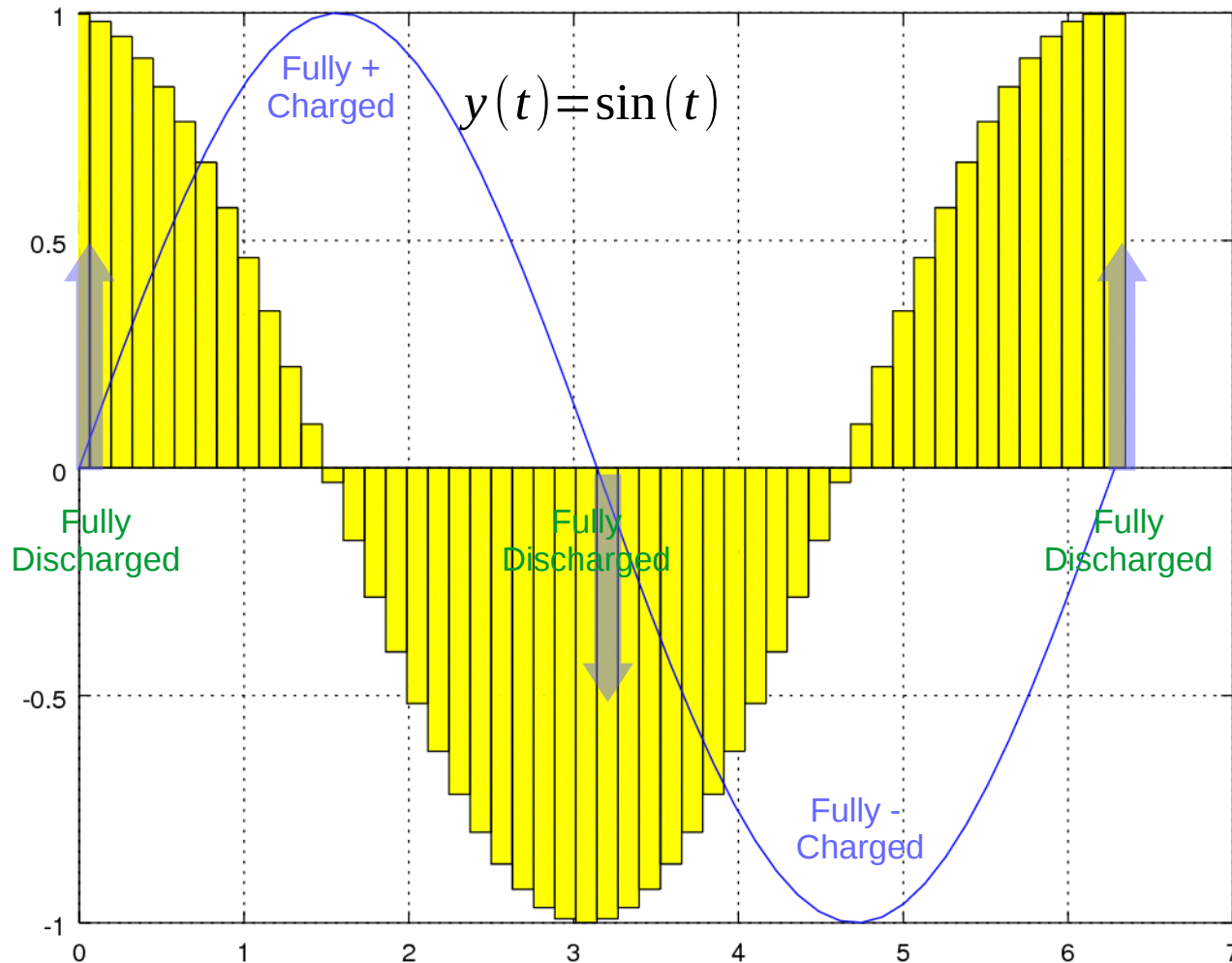
Fully Charged and Fully Discharged



```
h = bar(t1, [y1' y2'],  
"stacked")  
set(h(1), "facecolor", "g");  
set(h(2), "facecolor", "y");  
hold on  
plot(t1, y1)  
axis([0 7 -1 1]);
```

$$y[n] - y[n+1] = y(nT) - y((n+1)T) = \sin(nT) - \sin((n+1)T)$$

Fully Charged and Fully Discharged

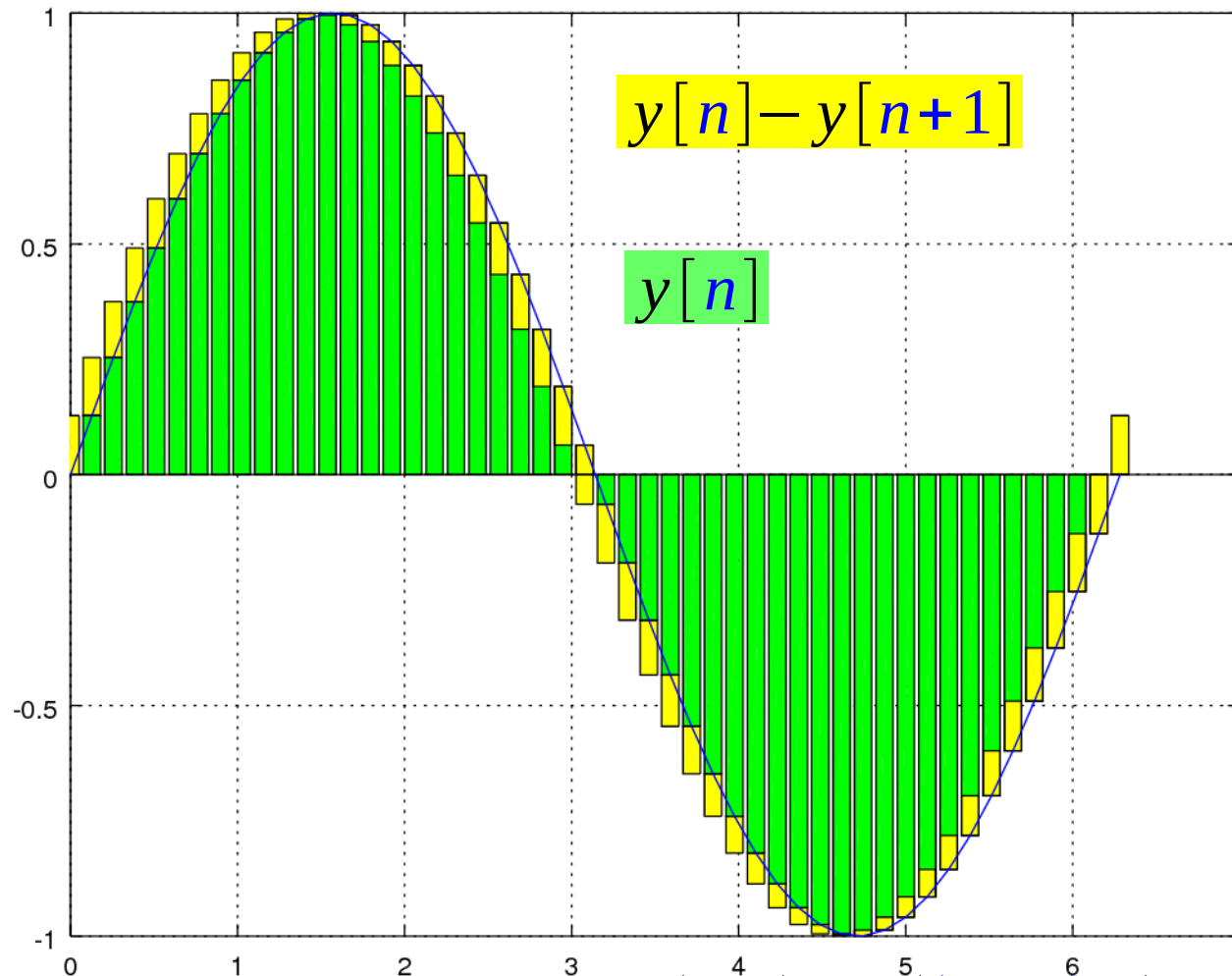


```
h = bar(t1, y2/t(2), "hist")
set(h(1), "facecolor", "y");
hold on
plot(t1, y1)
axis([0 7 -1 1]);
```

$$\frac{y[n] - y[n+1]}{T}$$

$$\propto \frac{dy}{dt}$$

Fully Charged and Fully Discharged

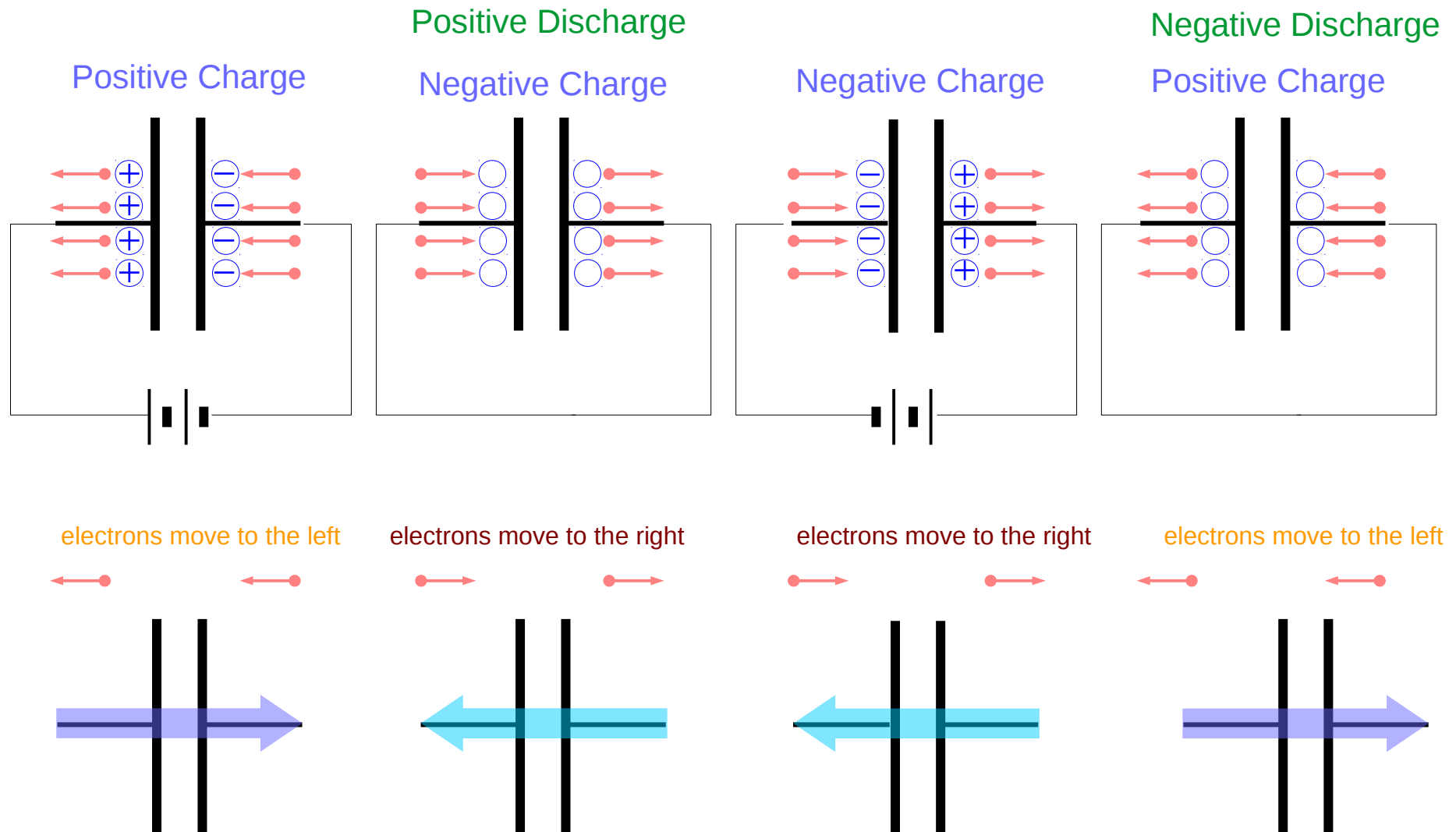


```

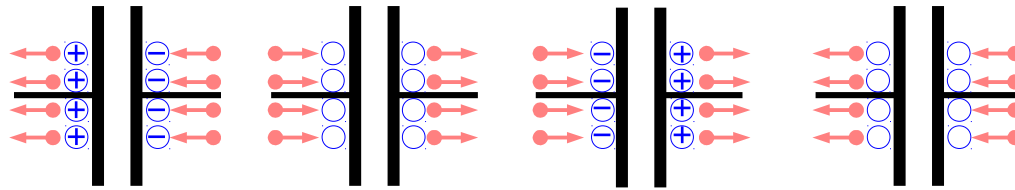
h = bar(t1, [y1' y2'],
"stacked")
set(h(1), "facecolor", "g");
set(h(2), "facecolor", "y");
hold on
plot(t1, y1)
axis([0 pi]);
    
```

$$y[n] - y[n+1] = y(nT) - y((n+1)T) = \sin(nT) - \sin((n+1)T)$$

Everchanging signal pairs

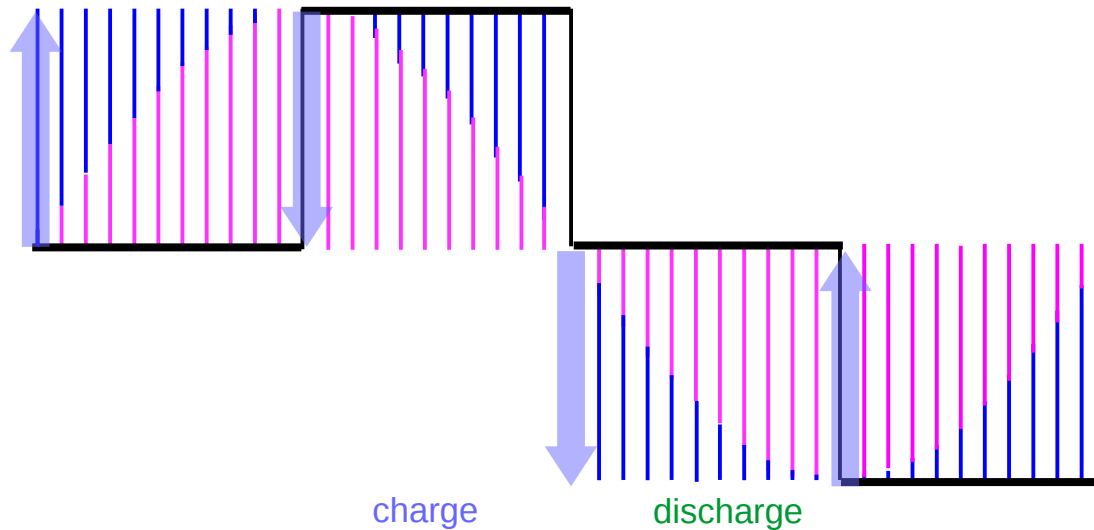


Everchanging signal pairs



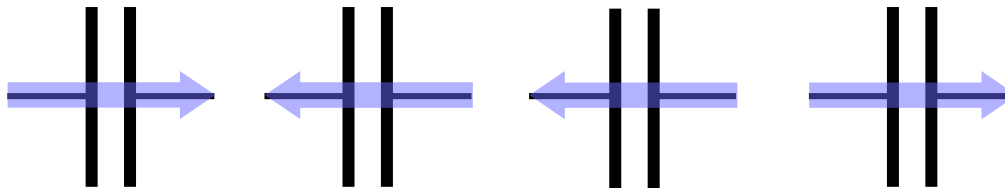
charge

discharge

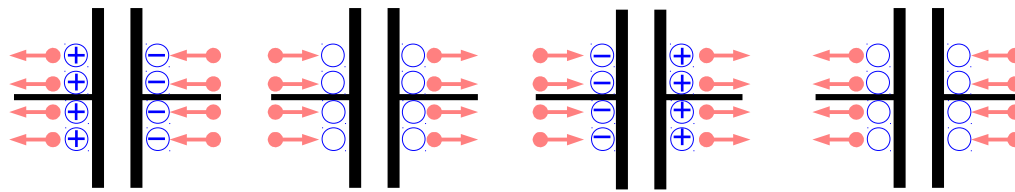


charge

discharge

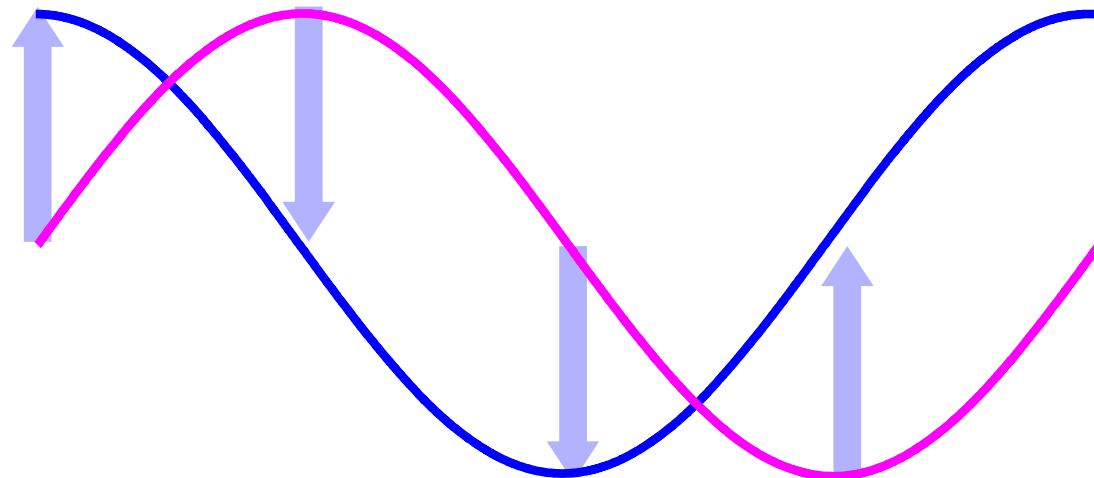


Everchanging signal pairs



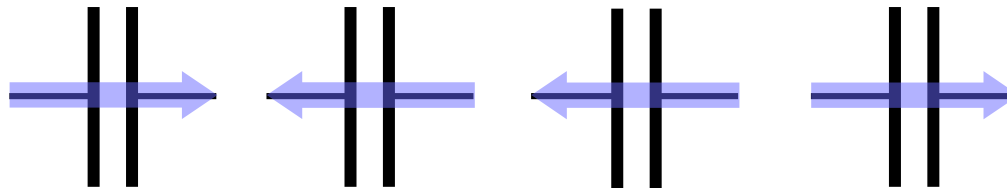
charge

discharge

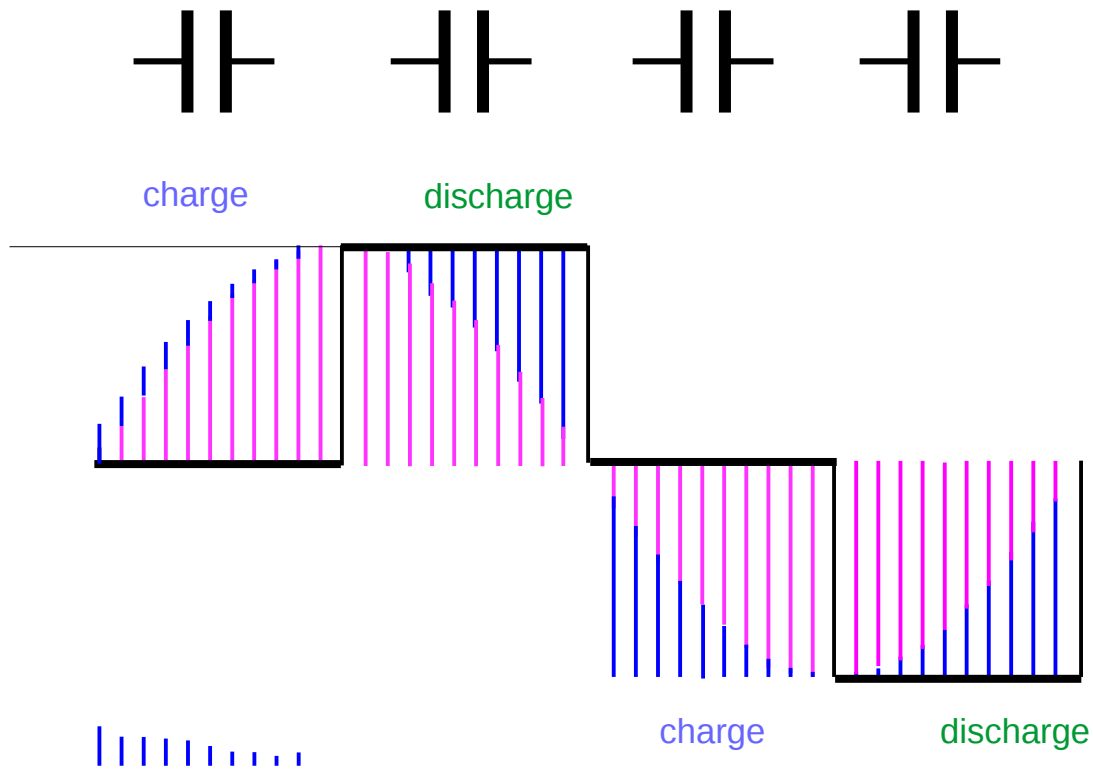


charge

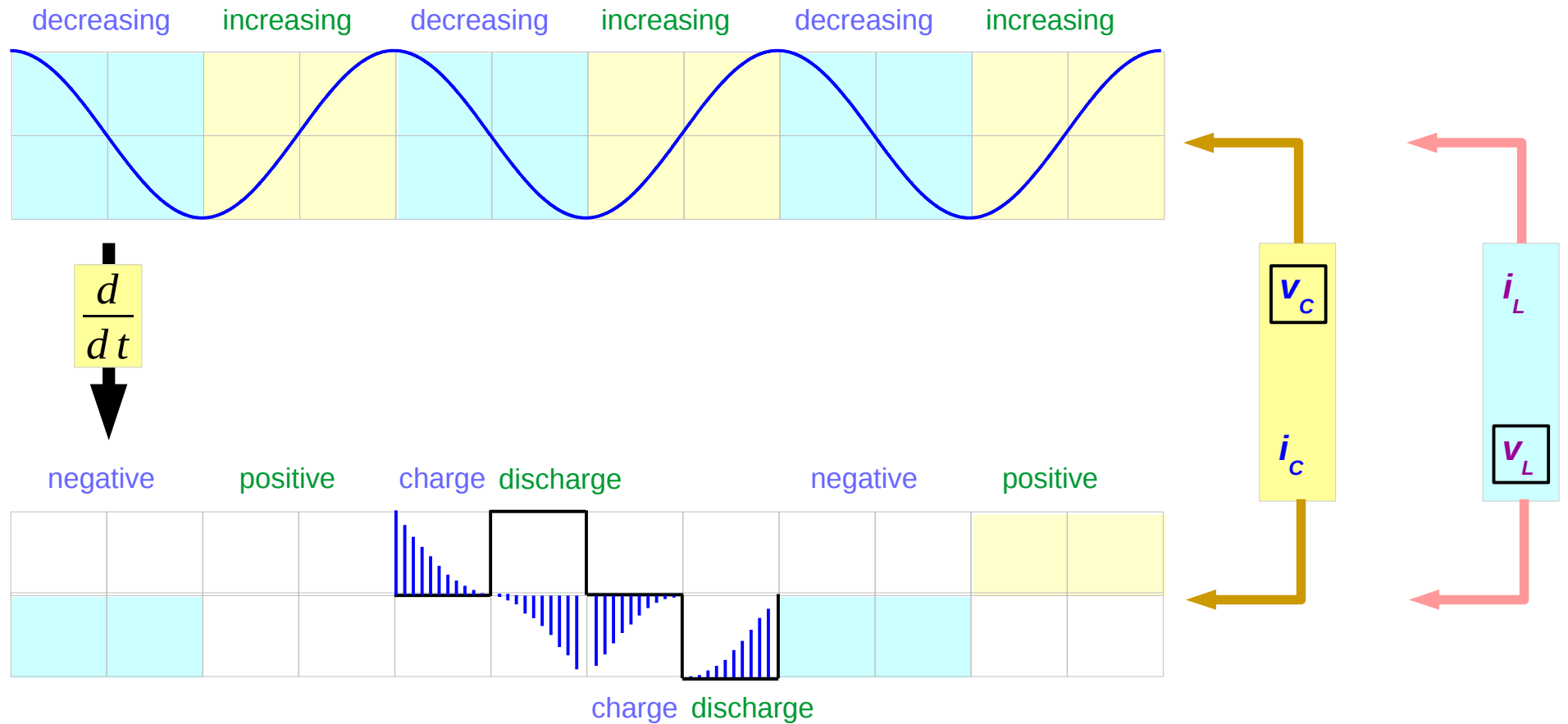
discharge



Everchanging signal pairs

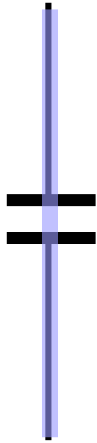


Everchanging signal pairs



I leads V by 90°

*Initial
charge*

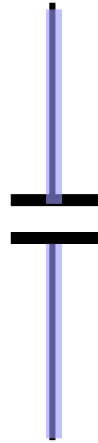


SHORT

V = 0

I : peak

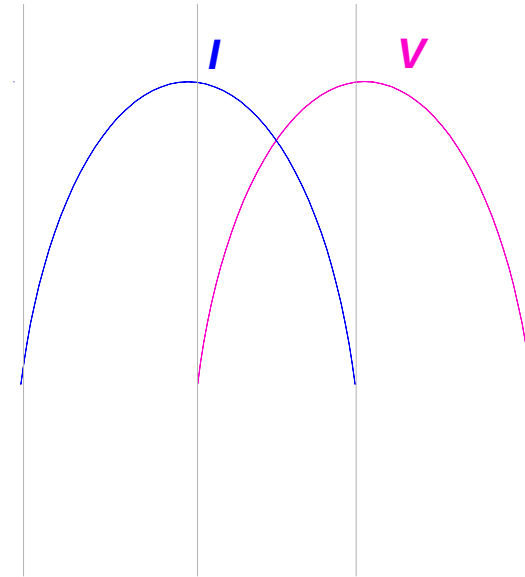
*Full
charge*



OPEN

I = 0

V : peak



References

[1] <http://en.wikipedia.org/>

[2] J.H. McClellan, et al., Signal Processing First, Pearson Prentice Hall, 2003