Signal Processing

Young Won Lim 2/22/18 Copyright (c) 2016 – 2018 Young W. Lim.

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Young Won Lim 2/22/18 Signal Processing with Free Software : Practical Experiments F. Auger filter (1)

```
: y = filter (b, a, x)
: [y, sf] = filter (b, a, x, si)
: [y, sf] = filter (b, a, x, [], dim)
: [y, sf] = filter (b, a, x, si, dim)
```

https://octave.sourceforge.io/octave/function/filter.html

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filter (2)

Apply a 1-D digital filter to the data x.

filter returns the solution to the following linear, time-invariant difference equation:

$$\sum_{k=0}^{N} a(k+1) y(n-k) = \sum_{k=0}^{M} b(k+1) x(n-k) \quad for \ 1 \le n \le length(x)$$

where N=length(a)-1 and M=length(b)-1.

$a = [a(1), a(2), \dots, a(N+1)]$	$x = [x(1), x(2), \cdots, x(L+1)]$
$b = [b(1), b(2), \dots, b(M+1)]$	$length(\mathbf{x}) = L + 1$
length(a) = N+1	
$length(\mathbf{b}) = M+1$	$1 \le n \le L+1$

filter (3)

The result is calculated over the **first** non-singleton dimension of x or over **dim** if supplied.

x(1),	x(2),	x(3),		, $x(K)$
x(1, 1),	<i>x</i> (1, 2),	x(1, 3),		x(1,K)
x(2, 1),	x(2, 2),	x(2, 3)	,	, $x(2,K)$
x(3, 1),	x(3, 2),	x(3, 3)	,	, $x(3,K)$
x(L,1),	x(L,2),	x(L,3)	,	, $x(L,K)$
		•		V
x(:,1),	x(:, 2),	x(:, 3)		x(:,K)

https://octave.sourceforge.io/octave/function/filter.html

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filter (4)

$$\sum_{k=0}^{N} a(k+1)y(n-k) = \sum_{k=0}^{M} b(k+1)x(n-k) \quad \text{for } 1 \le n \le \text{length}(x)$$

$$a(1)y(n) + \sum_{k=1}^{N} a(k+1)y(n-k) = \sum_{k=0}^{M} b(k+1)x(n-k)$$

$$a(1)y(n) = -\sum_{k=1}^{N} a(k+1)y(n-k) + \sum_{k=0}^{M} b(k+1)x(n-k)$$

$$y(n) = -\sum_{k=1}^{N} \frac{a(k+1)}{a(1)}y(n-k) + \sum_{k=0}^{M} \frac{b(k+1)}{a(1)}x(n-k)$$

$$y(n) = -\sum_{k=1}^{N} \frac{c(k+1)}{a(1)}y(n-k) + \sum_{k=0}^{M} \frac{d(k+1)}{a(1)}x(n-k) \quad \text{for } 1 \le n \le \text{length}(x)$$

where c = a/a(1) and d = b/a(1).

https://octave.sourceforge.io/octave/function/filter.html

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filter (5)

si : the initial state of the systemsf : the final state

the state vector is a <u>column vector</u> whose length is equal to the length of the <u>longest coefficient</u> vector – 1

No **si** is presented, the <u>zero initial</u> <u>state</u>.

in terms of the z transform, **y** is the result of passing the discrete-time signal **x** through a system characterized by the following rational <u>system function</u>:

$$H(z) = \frac{\sum_{k=0}^{M} d(k+1) z^{-k}}{1 + \sum_{k=1}^{N} c(k+1) z^{-k}}$$

https://octave.sourceforge.io/octave/function/filter.html

Audio Signal Processing freqz (1)

```
: [h, w] = freqz (b, a, n, "whole")
: [h, w] = freqz (b)
: [h, w] = freqz (b, a)
: [h, w] = freqz (b, a, n)
: h = freqz (b, a, w)
: [h, w] = freqz (..., Fs)
: freqz (...)
```

Return the <u>complex frequency response</u> **h** of the rational **IIR** filter with the <u>numerator</u> coefficients **b** and the <u>denominator</u> coefficients **a**

The response is evaluated at **n** angular frequencies between **0** and **2*pi**.

The output value **w** is a <u>vector</u> <u>of the frequencies</u>.

h : the frequency response vector**w** : the frequency vector

If **a** is omitted, the denominator is assumed to be **1** (this corresponds to a simple **FIR** filter).

If n is omitted, a value of 512 is assumed. For fastest computation, n should factor into a small number of small primes.

If the fourth argument, "**whole**", is omitted the response is evaluated at frequencies between **0** and **pi**.

freqz (4)

freqz (b, a, w)

Evaluate the response at the <u>specific</u> <u>frequencies</u> in the vector **w**. The values for **w** are measured in <u>radians</u>.

freqz (...)

<u>Plot</u> the magnitude and phase response of **h** rather than returning them.

freqz (5)

```
[...] = freqz (..., Fs)
```

Return frequencies in <u>Hz</u> instead of <u>radians</u> assuming a <u>sampling</u> <u>rate</u> Fs. If you are evaluating the response at specific frequencies \mathbf{w} , those frequencies should be requested in <u>Hz</u> rather than <u>radians</u>.

```
[h, w] = freqz (b, a, n, "whole", Fs)
[h, w] = freqz (b, Fs)
[h, w] = freqz (b, a, Fs)
[h, w] = freqz (b, a, n, Fs)
h = freqz (b, a, w, Fs)
```

freqz_plot

```
: freqz_plot (w, h)
: freqz_plot (w, h, freq_norm)
```

Plot the magnitude and phase response of **h**.

If the optional freq_norm argument is true, the frequency vector **w** is in units of <u>normalized radians</u>. If freq_norm is false, or not given, then **w** is measured in <u>Hertz</u>.

conv

```
: conv (a, b)
: conv (a, b, shape)
```

Convolve two vectors **a** and **b**.

The output convolution is a vector with length equal to length (\mathbf{a}) + length (\mathbf{b}) - 1. When \mathbf{a} and \mathbf{b} are the coefficient vectors of two polynomials, the convolution represents the coefficient vector of the product polynomial.

```
The optional shape argument may be

shape = "full"
    Return the full convolution. (default)
    shape = "same"
    Return the central part of the convolution with the length(a).
```

fftconv

- : fftconv (x, y)
- : **fftconv** (**x**, **y**, **n**)

Convolve two vectors <u>using</u> the <u>FFT</u> for computation.

c = fftconv (x, y) returns
a vector of length equal to length(x) + length(y) - 1

If \mathbf{x} and \mathbf{y} are the coefficient vectors of two polynomials, the returned value is the coefficient vector of the <u>product polynomial</u>.

The computation uses the FFT by calling the function **fftfilt**.

If the optional argument n is specified, an <u>n-point FFT</u> is used.

: **deconv** (**y**, **a**)

Deconvolve two vectors.

 $[\mathbf{b}, \mathbf{r}] = \mathbf{deconv} (\mathbf{y}, \mathbf{a})$ solves for **b** and **r** such that $\mathbf{y} = \mathbf{conv} (\mathbf{a}, \mathbf{b}) + \mathbf{r}$.

If y and a are polynomial coefficient vectors,
b will contain the coefficients of the polynomial <u>quotient</u> and
r will be a <u>remainder</u> polynomial of lowest order.

Low Pass filter

```
\begin{array}{l} t = 0: 1/100: 1; \\ x = \sin(2*pi*t); \\ x = (x > 0); \\ x = (x - 0.5)*2; \\ xd = [x \ 0 \ 0 \ 0]; \\ \text{for } i=1: \text{length}(x) \\ y(i) = xd(i) + xd(i+1) + xd(i+2) + xd(i+3)) / 4; \\ \text{endfor} \\ \text{hold} \\ plot(t, x) \\ plot(t, y, 'm-'); \end{array}
```

Low Pass filter

```
ir = zeros(1, 44100);
ir(1:2) = 0.5;
irfft = abs(fft(ir));
irfft = irfft(1: 22050);
plot(irfft)
```

```
ir = zeros(1, 44100);
ir(1:3) = 0.333;
irfft = abs(fft(ir));
irfft = irfft(1: 22050);
plot(irfft)
```

```
ir = zeros(1, 44100);
ir(1:4) = 0.25;
irfft = abs(fft(ir));
irfft = irfft(1: 22050);
plot(irfft)
```

DSP for sound engineers (in Korean), J.W. Chae

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```
h0=0.36281; h1= 0.28920; h2 = 0.12082;
sys = zeros(1, 44100);
sys(1)=h2; sys(2) = h1; sys(3)=h0; sys(4)=h1; sys(5)=h2;
sysft = abs( fft(sys) );
sysft = sysft(1: 44100/2);
plot(sysft)
```

High Pass filter

```
ir=zeros(1, 44100);
Ir(1)=0.5;
Ir(2)=-0.5;
irfft=abs(fft(ir));
Irfft = irfft(1: 22050);
plot(irfft);
```

```
h0=0.63719; h1 = 0.28920; h2 = 0.12082;
sys = zeros(1, 44100);
sys(1) = h2; sys(2) =- h1; sys(3) = h0; sys(4)=-h1; sys(5)=h2;
sysft = abs(fft(sys));
sysft = sysft(1: 44100/2);
plot(sysft);
```

 sox --plot gnuplot s6s.wav -n fir 0.1 0.2 0.4 0.3
 >fir1.plt

 sox --plot gnuplot s6s.wav -n fir coeff.txt
 >fir2.plt

 sox --plot gnuplot s6s.wav -n biquad .6 .2 .4 1 -1.5 .6 >fir3.plt

 sox --plot gnuplot s6s.wav -n fir 0.2 0.2 0.2 0.2 0.2

--plot gnuplot | octave



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References

[1] F. Auger, Signal Processing with Free Software : Practical Experiments