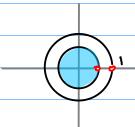
## Laurent Series and z-Transform Examples case 2.A

20171007

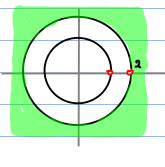
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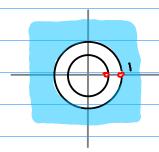
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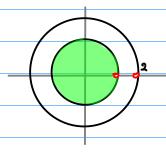
$$\frac{1}{2}(z) = \frac{(5-1)(z-0.5)}{(5-1)(z-0.5)} \longrightarrow \chi(z) = \frac{(3-1)(z-2)}{(3-1)(z-2)}$$

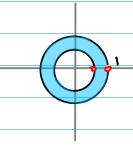


$$\sum_{n=1}^{\infty} \left[1-2^{n-1}\right] \leq n$$

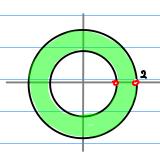








$$\sum_{n=1}^{\infty} 1 \cdot \xi^n + \sum_{n=0}^{\infty} 2^{n-1} \cdot \xi^n$$



L.S. first

$$\begin{array}{c}
D_1 & D_2 \\
\hline
D_2 & D_3
\end{array}$$

$$\begin{array}{c}
\Delta_n? & \Delta_n? & \Delta_n? \\
\parallel & \parallel & \parallel \\
\chi_n & \chi_n & \chi_n
\end{array}$$

$$\begin{array}{c}
\chi_{(2)}? & \chi_{(2)}? & \chi_{(2)}?
\end{array}$$

$$\begin{array}{c}
\chi_{(2)}? & \chi_{(2)}? & \chi_{(2)}?
\end{array}$$

$$f(5) = \frac{(5-1)(5-0.5)}{-0.25}$$

$$\frac{7}{(7-1)(7-0.5)} = \frac{2}{7-1} - \frac{1}{7-0.5}$$

$$= \frac{23-1-2+1}{(7-1)(7-0.5)}$$

$$\frac{-0.5 \ z^2}{(z-1)(z-0.5)} = -0.5 \ \left(\frac{2z}{z-1} - \frac{z}{z-0.5}\right) = \frac{-z}{z-1} + \frac{0.5z}{z-0.5}$$

 $\frac{-\overline{\xi}}{-\overline{\xi}} = \begin{cases} \frac{1 - \left(\frac{\pi}{\xi}\right)}{1 - \left(\frac{\pi}{\xi}\right)} &= -\sum_{\infty}^{N=0} \overline{\xi} \cdot \overline{\xi}_{N} &= -\sum_{\infty}^{N=0} |\cdot \overline{\xi}_{-1}| & \left|\frac{\overline{\xi}}{\xi}\right| < 1 \\ \frac{-1}{\xi} &= -\sum_{\infty}^{N=0} \overline{\xi} \cdot \overline{\xi}_{N} &= -\sum_{\infty}^{N=0} |\cdot \overline{\xi}_{-1}| & \left|\frac{\overline{\xi}}{\xi}\right| < 1 \end{cases}$ 

$$\frac{\frac{0.52}{2-0.5}}{\frac{1}{2-0.5}} = \begin{cases} \frac{-(\frac{2}{1})}{|-(\frac{1}{2})|} &= -\sum_{n=0}^{\infty} (\frac{2}{1})(\frac{22}{1})^n = -\sum_{n=0}^{\infty} 2^n 2^{n+1} \frac{|22|}{|-(\frac{1}{2})|} < |-\frac{1}{2}| < |-\frac{1}{$$

$$f(s) = \frac{(5-1)(5-0.2)}{-0.25_5} \quad \chi(s) = \frac{(5-1)(5-5)}{-1}$$

$$\chi(5) = \frac{(5-1)(5-5)}{-1}$$

L.5. first 
$$(1)-1$$

$$\left( \left| \frac{1}{r} \right| < 1 \right) \qquad \left| \frac{2r}{r} \right| < 1 \right)$$

$$p = 0.5$$

$$p = 1$$

$$|2| < \frac{1}{2}$$

$$f(z) = \frac{-z}{z-1} + \frac{0.5z}{z-0.5}$$

$$=\frac{\left(\frac{2}{l}\right)}{\left(-\left(\frac{2}{l}\right)\right)}+\frac{-\left(\frac{2}{l}\right)}{\left(-\left(\frac{2}{l}\right)\right)}$$

$$= \sum_{n=0}^{\infty} |\cdot \xi^{n+1}| - \sum_{n=0}^{\infty} 2^n \xi^{n+1}$$

$$=\sum_{n=0}^{\infty}\left[\left(-2^{n}\right)\right]\xi^{n+1}$$

$$= \sum_{n=1}^{\infty} \left[ |-2^{n-1}| \right] z^n |z| < \frac{1}{2}$$

$$\chi(z) = \int (z^4) = \sum_{n=1}^{\infty} \left[1 - 2^{n-1}\right] z^{-n} |z| > 2$$

$$= \frac{1}{\left(\frac{1}{5}\right)} - \frac{\left(\frac{1}{5}\right)}{\left(\frac{1}{5}\right)} = \frac{\left(\frac{1}{5}\right)}{\left(\frac{1}{5}\right)}$$

$$= \frac{1}{2-1} - \frac{1}{2-2}$$

$$= \frac{-1}{(z-1)(z-2)}$$

$$f(z) = \frac{-0.5 z^2}{(z-1)(z-0.5)}$$

$$f(\vec{z}') = \frac{-0.5 \, \vec{\epsilon}^2}{(\vec{z}'-1)(\vec{z}'-0.5)} = \frac{-0.5}{(1-\vec{z})(1-0.5\,\vec{z})} = \frac{-1}{(\vec{z}-1)(\vec{z}-2)} = \chi(\vec{z})$$

$$\frac{1}{|z|} = \frac{1}{|z|} = \frac{1$$

$$f(\xi) = \frac{-0.5 \, \xi^2}{(\xi^{-1})(\xi^{-0.5})} = \frac{-0.5 \, \xi^2}{(|-\xi|)(1-0.5)} = \frac{-1}{(|\xi^{-1}|)(\xi^{-1})} = \chi(\xi)$$

$$f(\xi) = \frac{\frac{(\xi^{-1})(\xi^{-0.5})}{(\xi^{-1})(\xi^{-0.5})}}{(\xi^{-1})(\xi^{-0.5})} = \frac{\frac{(\xi^{-1})(\xi^{-2})}{(\xi^{-1})(\xi^{-2})}}{(\xi^{-1})(\xi^{-2})} = \chi(\xi)$$

$$\sum_{i=1}^{n} \frac{x_{i}}{(z-1)(z-0.5)}$$

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