State Monad – Methods (6B)

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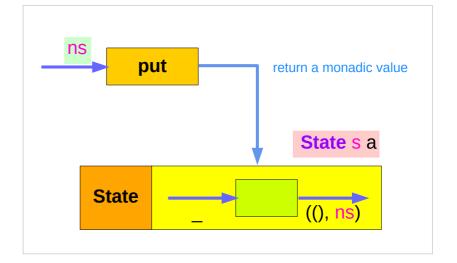
> Young Won Lim 9/10/18

Haskell in 5 steps

https://wiki.haskell.org/Haskell_in_5_steps

Setting the state : put

put :: s -> State s a
put ns = state \$ _ -> ((), ns)



Given a wanted state new State (ns),

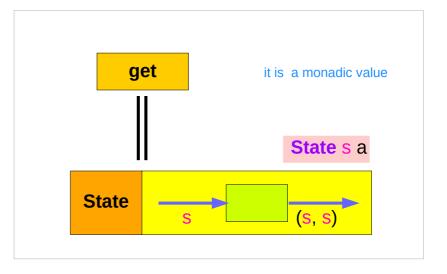
put generates a state processor

- ignores whatever the state it receives,
- <u>updates</u> the state to newState
- doesn't care about the result of this processor
- all we want to do is to change the state
- the tuple will be ((), newState)
- () : the universal placeholder value.

Getting the state : get

get :: State s s

get = state \$ \s -> (s, s)



get generates a state processor

- gives back the state s0
- as a result and as an updated state (s0, s0)
- the state will remain unchanged
- a <u>copy</u> of the state will be made available through the result returned

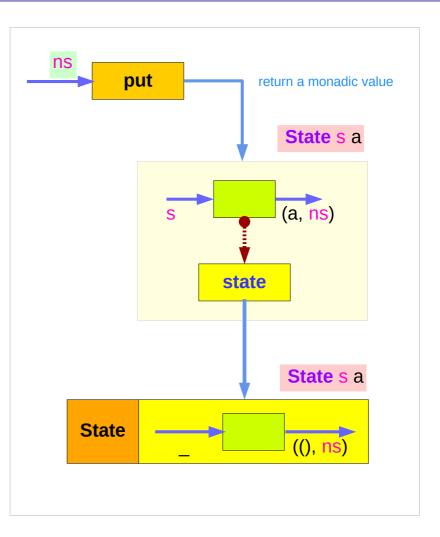
put returns a monadic value

put :: s -> State s a

put s :: State s a

put newState = state \$ _ -> ((), newState)

- -- setting a state to newState
- -- regardless of the old state
- -- setting the result to ()

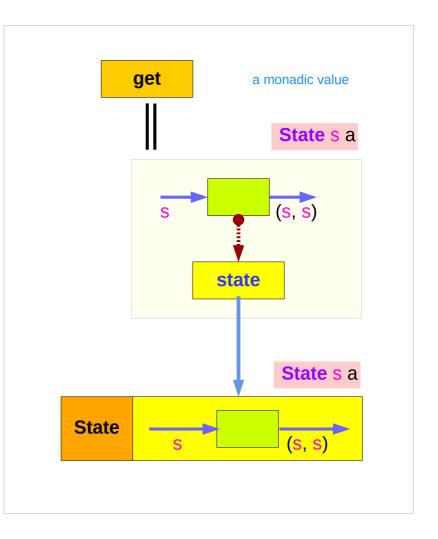


get is a monadic value



get = state \$ \s -> (s, s)

- -- getting the current state s
- -- also setting the result to s



Running put

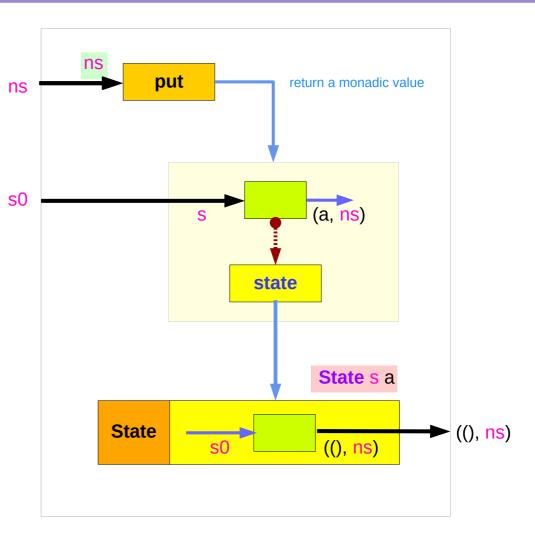
put :: s -> State s a

put s :: State s a

put newState = state \$ _ -> ((), newState)

runState (put ns) s0

runState (put 5) 1 ((),5)



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

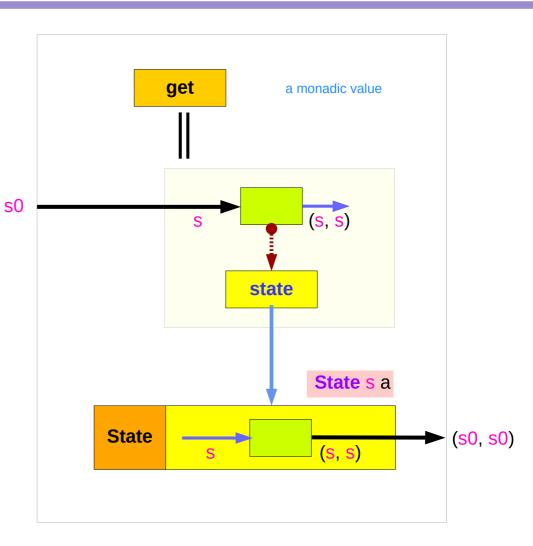
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Running get

get :: State s s get = state \$ \s -> (s, s)

runState (get) s0

runState (get) 1 (1,1)



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

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Example codes

import Control.Monad.Trans.State

```
runState get 1
(1,1)
runState (return 'X') 1
('X',1)
runState get 1
(1,1)
runState (put 5) 1
((),5)
let postincrement = do { x <- get; put (x+1); return x }</pre>
```

```
runState postincrement 1
```

```
(1,2)
```

```
let predecrement = do { x <- get; put (x-1); get }</pre>
```

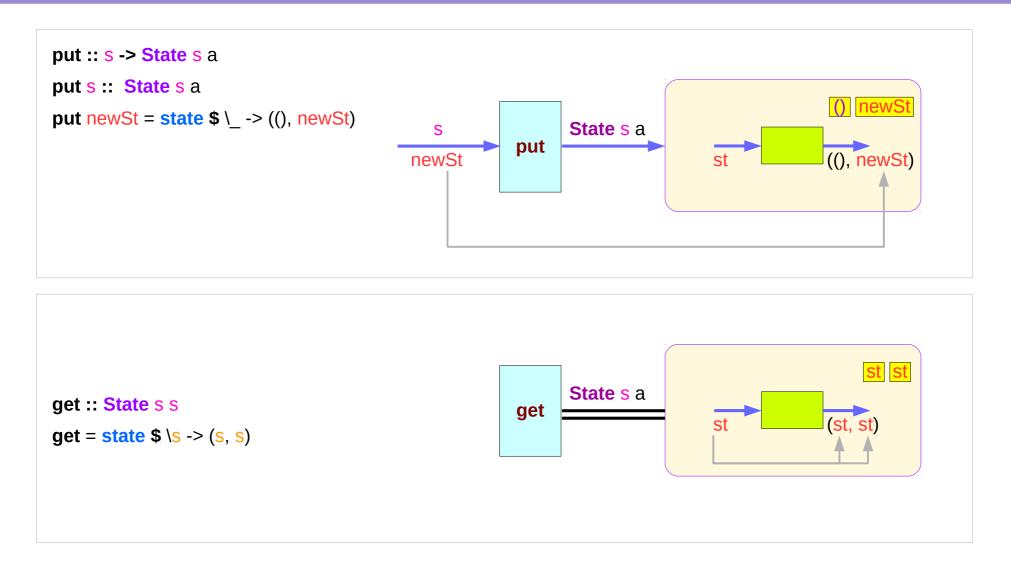
```
runState predecrement 1
```

(0,0)

https://wiki.haskell.org/State_Monad

```
runState (modify (+1)) 1
((),2)
runState (gets (+1)) 1
(2,1)
evalState (gets (+1)) 1
2
execState (gets (+1)) 1
1
```

Simple representation of put and get

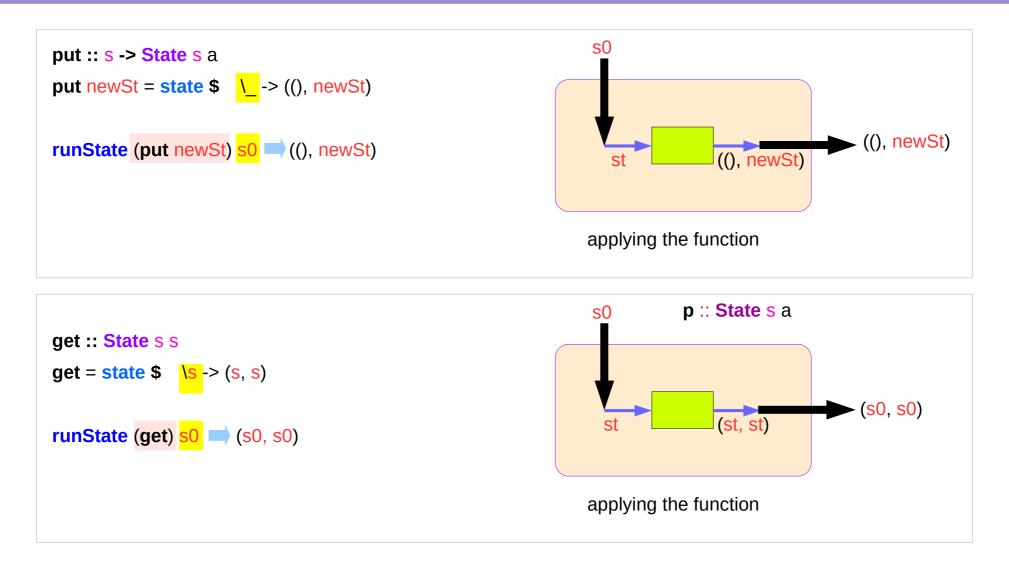


https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

State Monad (6B) Methods

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Executing the state processor



https://en.wikibooks.org/wiki/Haskell/Understanding_monads/State

State Monad (6B) Methods

State Monad Examples – put

runState (put 5) 1 ((),5) put set the result value to () and set the state value.

Comments:

```
put 5 :: State Int ()
runState (put 5) :: Int -> ((),Int)
initial state = 1 :: Int
final value = () :: ()
final state = 5 :: Int
```

put :: s -> State s a

put newState = state \$ _ -> ((), newState)

https://wiki.haskell.org/State_Monad

State Monad Examples – get

runState get 1

(1,1)

get

set the result value to the state and leave the state unchanged.

Comments:

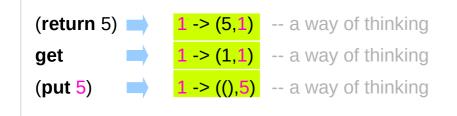
get :: State Int Int
runState get :: Int -> (Int, Int)
initial state = 1 :: Int
final value = 1 :: Int
final state = 1 :: Int

get :: State s s get = state \$ \s -> (s, s)

https://wiki.haskell.org/State_Monad

(1, 1)

Think an unwrapped state processor

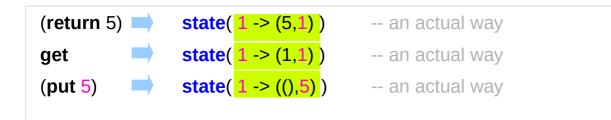


Think an **unwrapped** state processor

a value of type (**State** s a) is a **function** <u>from</u> initial state s <u>to</u> final value a and final state s: (a,s).

these are usually wrapped,

but shown here unwrapped for simplicity.



wrapping the state processor

https://wiki.haskell.org/State_Monad

State Monad Examples – return, get, and put

Return leaves the state unchanged and sets the result:				
ie: (return 5) 📃 🛁	1 -> (5,1)	a way of thinking		
runState (return 5) 1 📫	(5, 1)			

Get leaves state unchanged and sets the result to the state:				
ie: get		1 -> (1,1)	a way of thinking	
runState get 1		(1,1)		

Put sets the result to () ie: (put 5)	and sets the state:	a way of thinking
runState (put 5) 1	((),5)	

https://wiki.haskell.org/State_Monad

State Monad Examples – modify and gets

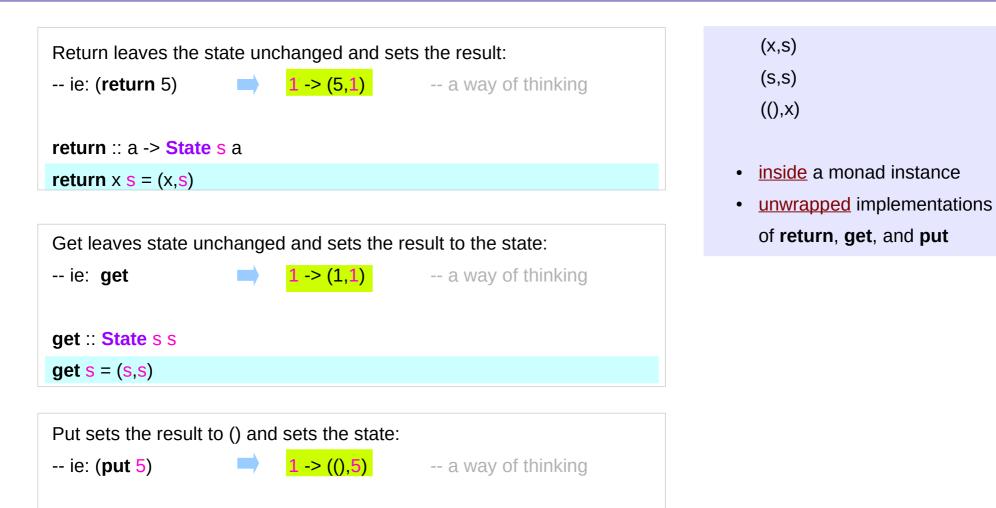
modify :: <mark>(s -> s)</mark> -> State s ()	
modify f = do { x <- get; put (f x) }	
gets :: <mark>(s -> a)</mark> -> State s a	
gets f = do { x <- get; return (f x) }	
runState (modify (+1)) 1	(+1) 1 → 2 :: s
→ ((),2)	
runState (gets (+1)) 1	(+1) 1 → 2 :: a
<u>(2,1)</u>	

evalState (gets (+1)) 1 $\rightarrow :: s \text{ state}$ 2execState (gets (+1)) 1 $\rightarrow :: a \text{ result}$ 1 https://wiki.haskell.org/State_Monad x <- get; put (f x) x <- get; return (f x)

- inside a monad instance
- <u>unwrapped</u> implementations of **modify** and **gets**

State Monad (6B) Methods

Unwrapped Implementation - return, get, and put



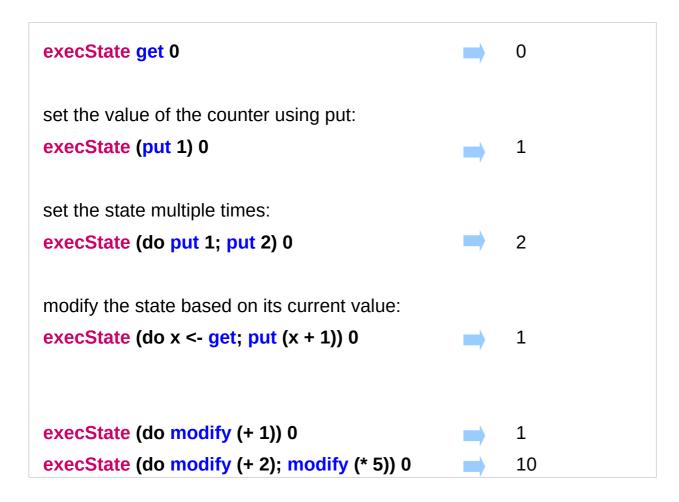
State Monad (6B) Methods

https://wiki.haskell.org/State Monad

put :: s -> State s ()

put x = ((),x)

Counter using State Monad



https://stackoverflow.com/questions/25438575/states-put-and-get-functions

The Result of a Stateful Computation

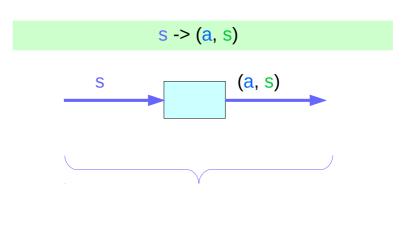


takes some **state** and returns a **value** along with some **new state**.

That function would have the following type:

<mark>s -> (a,s)</mark>

s is the type of the state anda the result of the stateful computation.



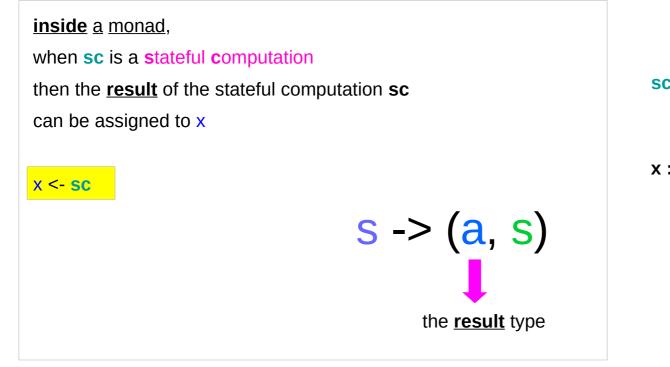
a <u>function</u> is an executable <u>data</u> when <u>executed</u>, a <u>result</u> is produced **action**, **execution**, **result**

s -> (a, s)

http://learnyouahaskell.com/for-a-few-monads-more

State Monad (6B) Methods

Stateful Computations Inside the State Monad



sc :: State s a

x :: a (the execution <u>result</u> of **sc**)

get inside the State Monad

inside the State monad,

get returns the current monad instance

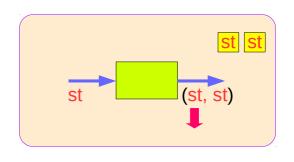
whose type is **State** s a

x <- get

the stateful computation is performed over the <u>current monad instance</u> returned by **get**

the <u>result</u> of the <u>stateful</u> computation is <u>st</u>::s thus x will get the <u>st</u>

x :: a the execution <u>result</u> of **get**



Getting the current state inside the State Monad

inside the State monad,

get returns the current monad instance

whose type is State s a

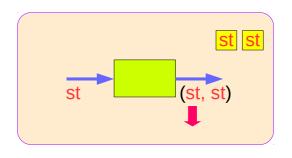
to get the <u>current</u> <u>state</u> st, do

s <- get

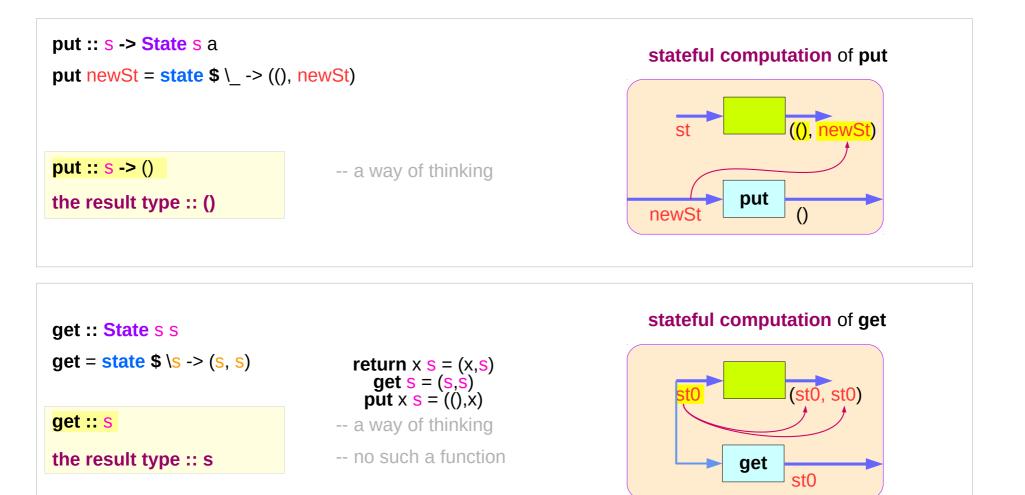
s will have the value of the current state st

this is like evalState is called with the current monad instance

- get
- current monad instance
- stateful computation
- result :: s



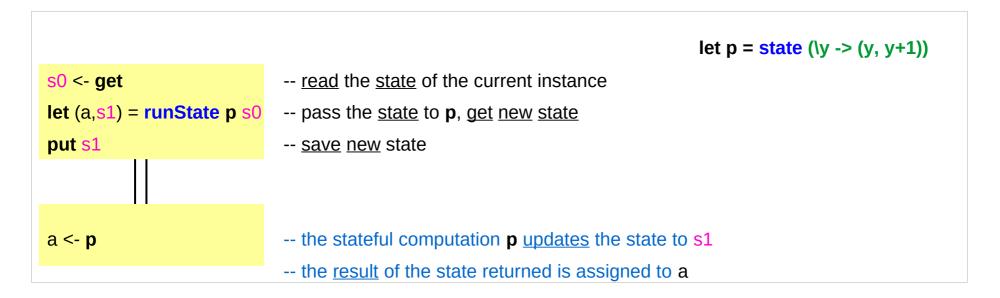
put and get inside State Monad



Inside Functions and runState Functions

Most monads are equipped with some "*run*" functions such as **runState**, **execState**, and so forth.

But, frequent calling such <u>functions</u> inside the <u>monad</u> shows that the functionality of the monad does <u>not fully</u> <u>exploited</u>

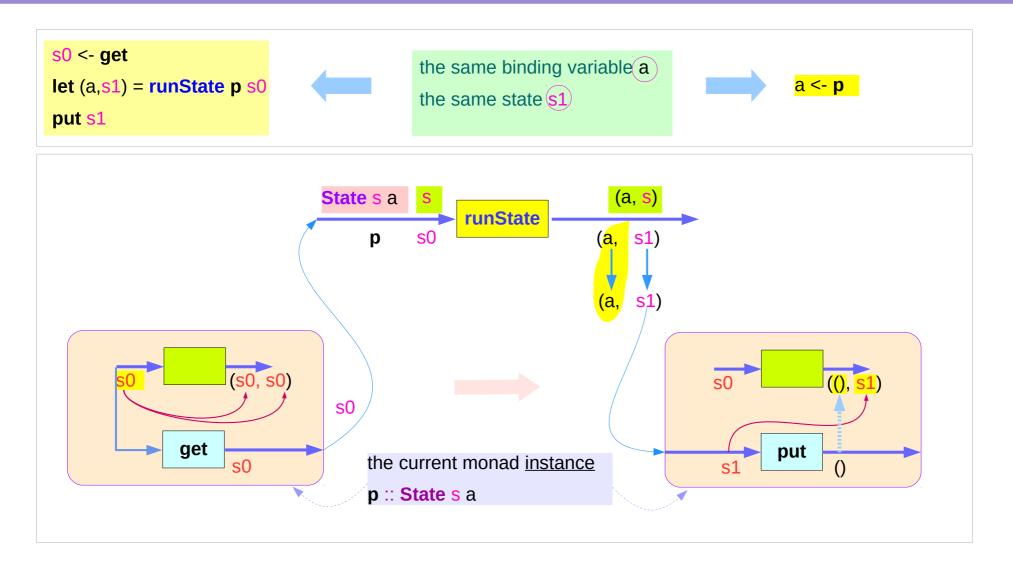


https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods



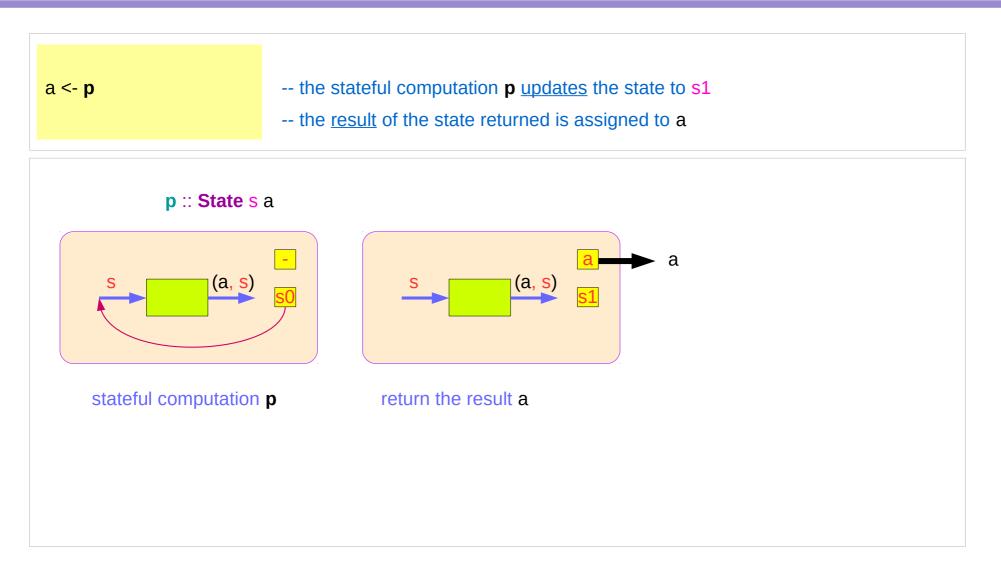
Redundant computation examples (1)



https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

Redundant computation examples (2)



State Monad	(6B)
Methods	

Counter Example

import Control.Monad.State.Lazy

tick :: State Int Int tick = do n <- get put (n+1) return n

plusOne :: Int -> Int
plusOne n = execState tick n

```
plus :: Int -> Int -> Int
```

plus n x = execState (sequence \$ replicate n tick) x

A function to increment a counter.

tick :

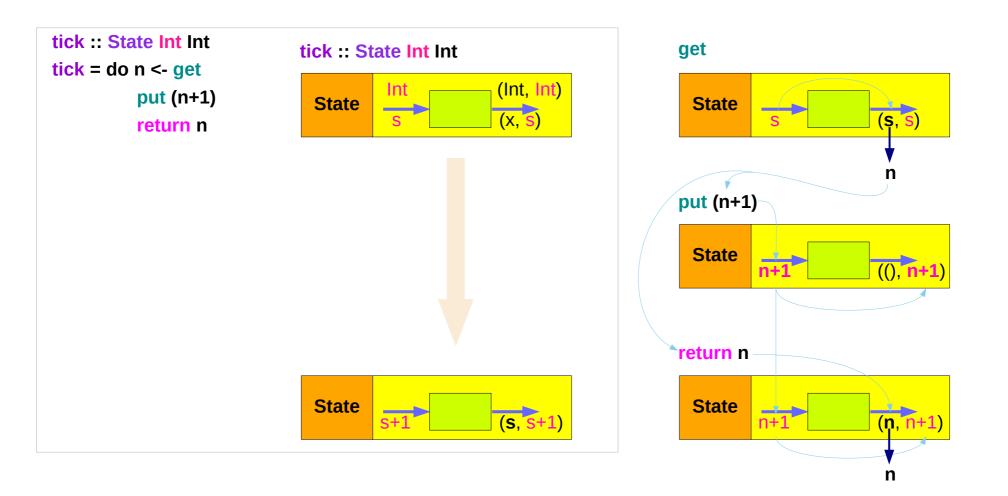
- a monadic value itself

- a function returning a monadic value-

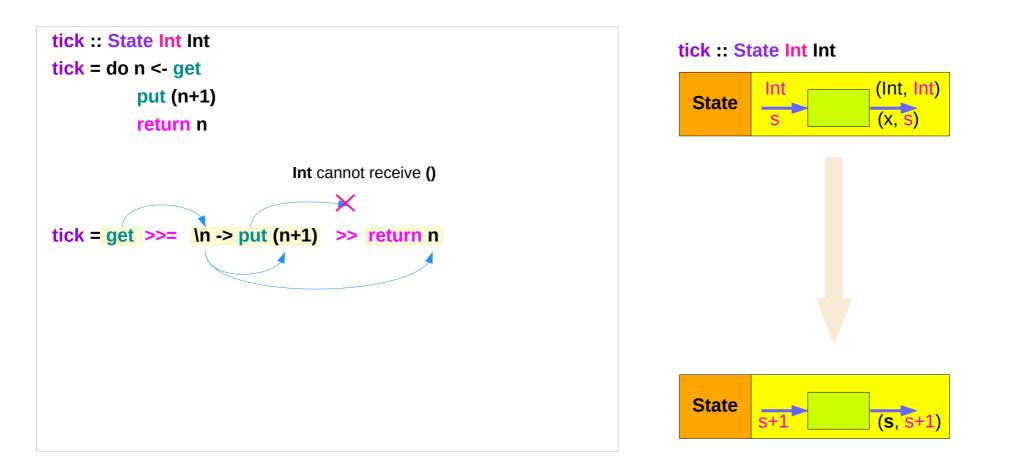
Add one to the given number using the state monad:

A contrived addition example. Works only with positive numbers:

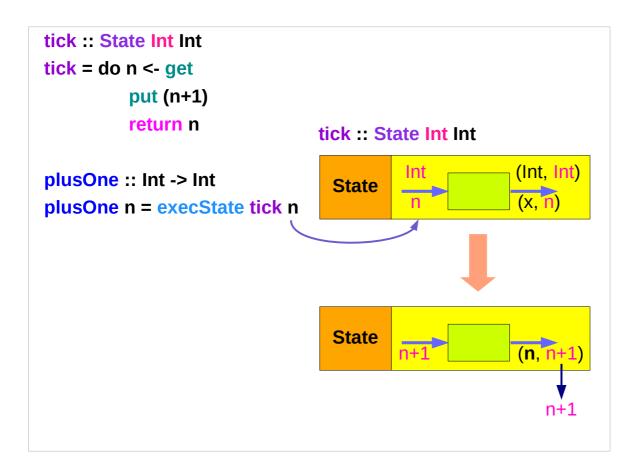
Counter Example – tick



Counter Example – tick without do



Counter Example – incrementing



Counter Example – using sequence

```
plus :: Int -> Int -> Int
plus n x = execState (sequence $ replicate n tick) x
             1
                  2
                         n
sequence $ [tick, tick, ... ,tick]
runState (sequence $ [tick, tick]) 3
                                          ([3,4],5)
runState (sequence $ [tick, tick, tick]) 3 ([3,4,5],6)
execState (sequence $ [tick, tick, tick]) 3
evalState (sequence $ [tick, tick, tick]) 3 
[3,4,5]
```

replicate

replicate :: Int -> a -> [a]

replicate n x is a list of length n with x the value of every element.

replicate 3 5

[5,5,5]

replicate 5 "aa"

["aa","aa","aa","aa","aa"]

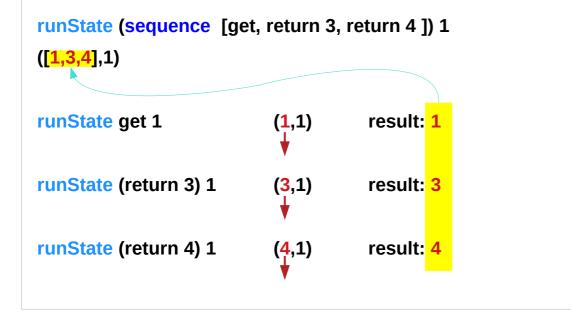
replicate 5 'a'

"aaaaa"

http://zvon.org/other/haskell/Outputprelude/replicate_f.html

sequence

sequence :: Monad m => [m a] -> m [a]
evaluate each action in the sequence from left to right,
and <u>collect</u> the results.



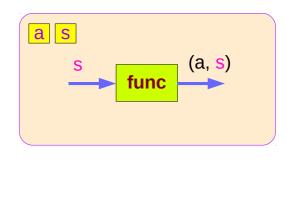
http://derekwyatt.org/2012/01/25/haskell-sequence-over-functions-explained/

Example of collecting returned values

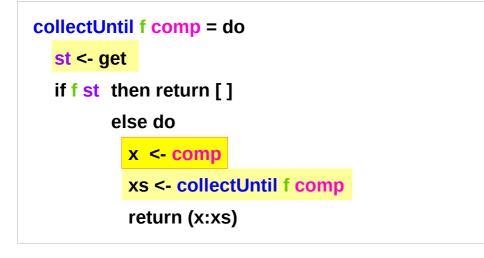
t <- get	Get the current state	st :: s
st then return []	If it satisfies predicate, return	
else do	Otherwise	
x <- comp	Perform the computation s	x :: a
xs <- collectUntil f comp	Perform the rest of the computation	xs ::[a]
return (x:xs)	Collect the results and return them	

```
simpleState = state (\x -> (x,x+1))
```

*Main> evalState (collectUntil (>10) simpleState) 0 [0,1,2,3,4,5,6,7,8,9,10] simpleState :: State s a



Example of collecting – stateful computations



simpleState = state (\x -> (x,x+1))

get	<mark>st</mark> ← 0	comp:	0 → (0, 1)	X ← 0
get	st	comp :	1 → (1, 2)	X ← 1
get	st	comp :	2 → (2, 3)	X ← 2
get	<mark>st</mark>	comp :	3 → (3, 4)	X ← 3
get	<mark>st</mark> ←4	comp:	4 → (4, 5)	X ← 4
get	<mark>st</mark>	comp:	5 → (5, 6)	X ← 5
get	<mark>st</mark> ←6	comp:	6 → (6, 7)	X ← 6
get	st	comp :	7 → (7, 8)	X ← 7
get	<mark>st</mark> ← 8	comp :	8 → (8, 9)	8 → X
get	<mark>st</mark>	comp :	9 → (9, 10)	9 → X
get	<mark>st</mark> ← 10	comp :	$\textbf{10} \rightarrow \textbf{(10, 11)}$	X ← 10

*Main> evalState (collectUntil (>10) simpleState) 0 [0,1,2,3,4,5,6,7,8,9,10]

stateful computation

Example of collecting – the return type

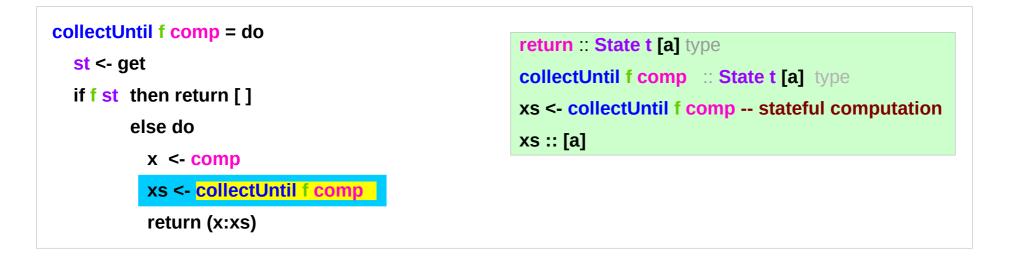


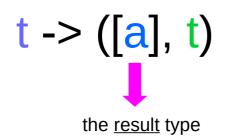
nesting do statements is possible if they are within the same monad

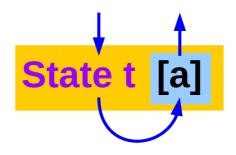
enables **branching** within one do block, as long as <u>both branches</u> of the **if statement**

results in the <u>same monadic</u> type.

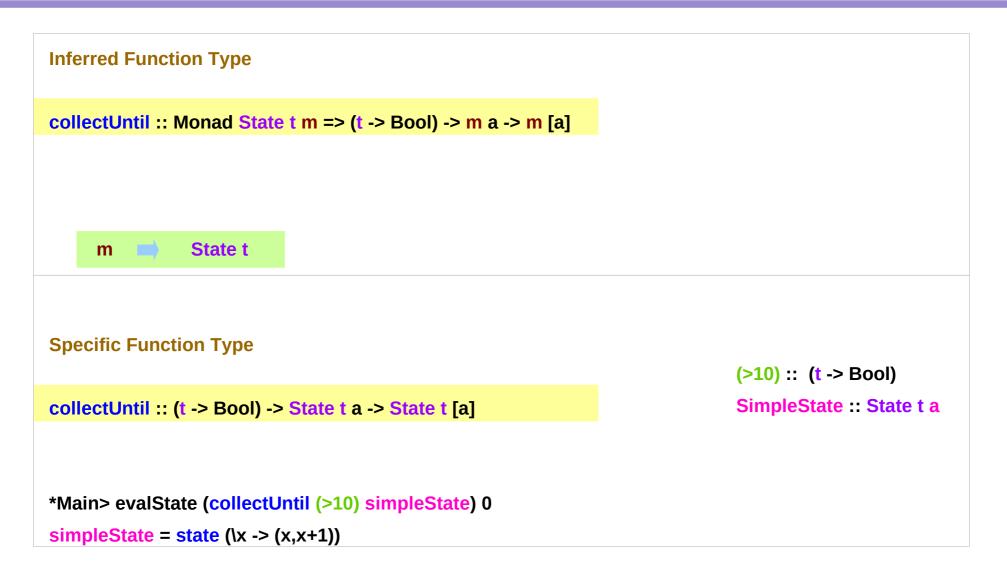
Example of collecting – another stateful compution







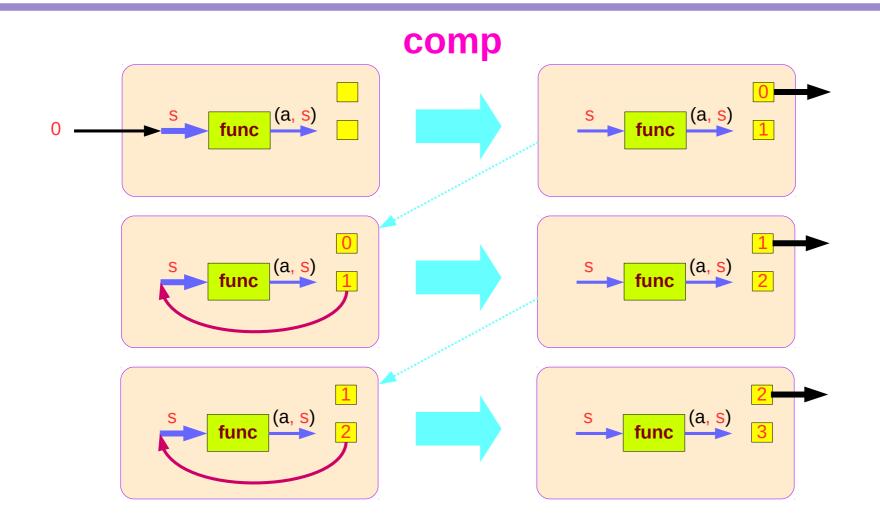
Example of collecting – the function type



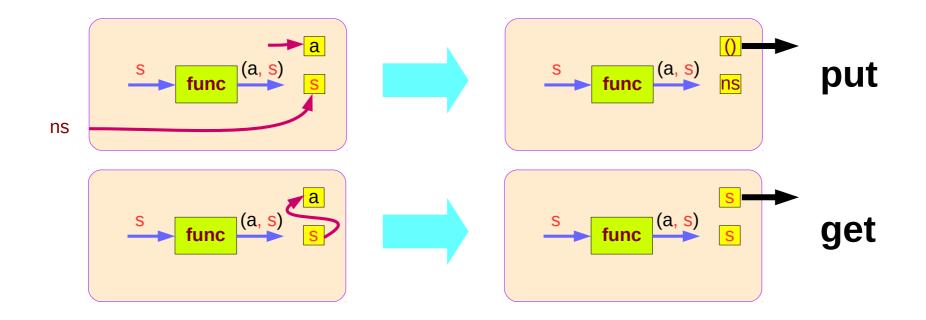
https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

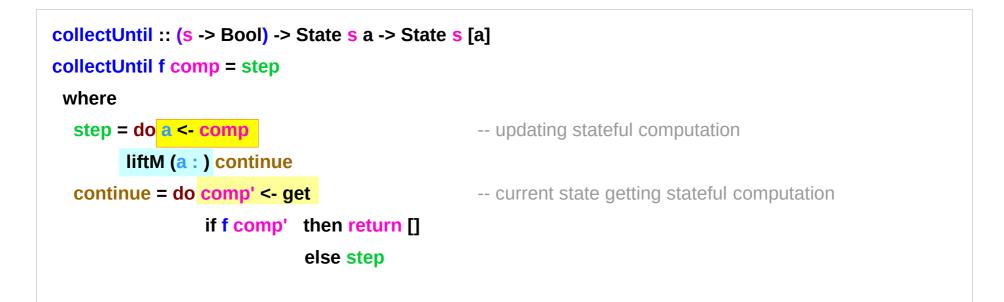
Stateful Computation of **comp**



Stateful Computations of put & get



Another example of collecting returned values



simpleState = state (\x -> (x,x+1))

*Main> evalState (collectUntil (>10) simpleState) 0

[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]

https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

Another example – lifting to merge

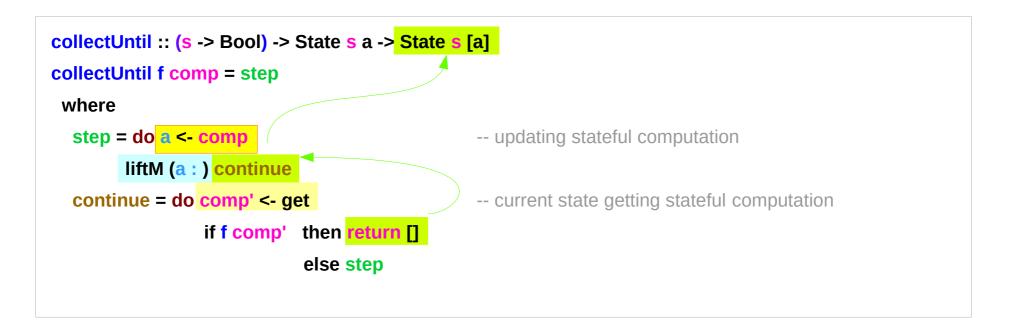
```
collectUntil :: (s -> Bool) -> State s a -> State s [a]
collectUntil f comp = step
where
step = do a <- comp
liftM (a : ) continue
continue = do comp' <- get
if f comp' then return []
else step
```

(:) :: a -> [a] -> [a] (++) :: [a] -> [a] -> [a]

(:) :: a -> [a] -> [a] LiftM (:) :: a -> State s [a] -> State s [a]

(a :) :: [a] -> [a] LiftM (a :) :: State s [a] -> State s [a]

Another example – the return type



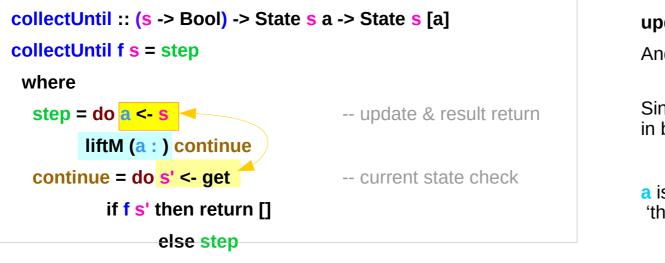


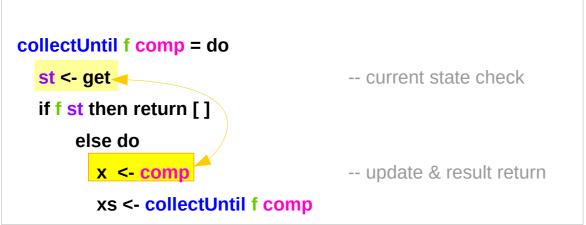
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10]

https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

Another example – sequence comparison





update and check the current state And then merge

Since **a** is part of the result in both branches of the 'if'

a is the common part of both 'then' part and 'else' part

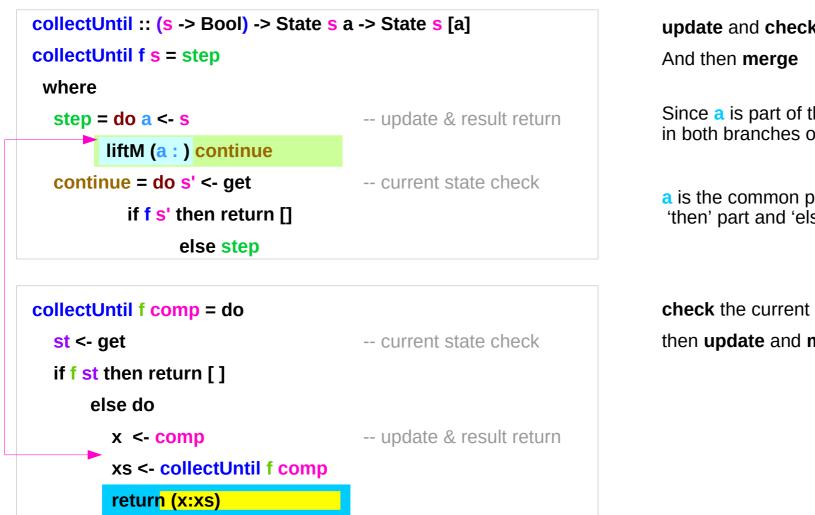
check the current state then update and merge

return (x:xs)

https://stackoverflow.com/questions/11250328/working-with-the-state-monad-in-haskell

State Monad (6B) Methods

Another example – merge comparison



update and check the current state

Since a is part of the result in both branches of the 'if'

a is the common part of both 'then' part and 'else' part

check the current state then update and merge

liftM and mapM

```
liftM :: (Monad m) => (a -> b) -> m a -> m b
mapM :: (Monad m) => (a -> m b) -> [a] -> m [b]
```

```
liftM lifts a function of type a -> b to a monadic counterpart.
mapM applies a function which yields a monadic value to a list of values,
    yielding list of results embedded in the monad.
```

```
> liftM (map toUpper) getLine
Hallo
"HALLO"
> :t mapM return "monad"
mapM return "monad" :: (Monad m) => m [Char]
```

https://stackoverflow.com/questions/5856709/what-is-the-difference-between-liftm-and-mapm-in-haskell

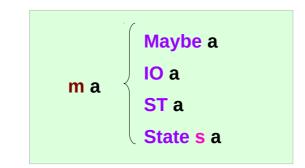
Monad typeclass and Instances

class Monad m where

return :: a -> m a

- (>>=) :: m a -> (a -> m b) -> m b
- (>>) :: m a -> m b -> m b

fail :: String -> m a



instance Monad Maybe where	
return x = Just x	
Nothing >>= f = Nothing	
Just x >>= f = f x	
fail _ = Nothing	

instance Monad IO where	
m >> k = m >>= \> k	
return =	
(>>=) =	
fail s =	

Default Implementations in MonadState s m

class Monad m => MonadState s m | m -> s where

Return the state from the internals of the monad.
get :: m s
<mark>get = state</mark> (\s -> (s, s))
Replace the state inside the monad.
put :: <mark>s</mark> -> m ()
put s = state (\> ((), s))
Embed a simple state action into the monad.
<mark>state</mark> :: (s -> (a, s)) -> m a
state f = do

s <- get let ~(a, s') = f s put s' return a

https://stackoverflow.com/questions/23149318/get-put-and-state-in-monadstate

The mtl package Control.Monad.State.Class module

No dead loop in the default implementation

the definitions of get, put, state in the Monad class declaration

- the default implementations,
- to be overridden in actual instances of the class.

the dead loop in the default definition does not happen:

- put and get in terms of state
- state in terms of put and get

* minimal definition is either both of get and put or just state

get :: m s
get = state (\s -> (s, s))
put :: <mark>s</mark> -> m ()
put s = <mark>state</mark> (\> ((), s))

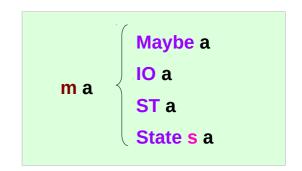
state :: (s -> (a, s)) -> m a
state f = do
s <- get
let ~(a, s') = f s
put s'
return a</pre>

https://stackoverflow.com/questions/23149318/get-put-and-state-in-monadstate

Functional Dependency | (vertical bar)

class Monad m => MonadState s m m -> s where			
functional dependencies to <u>constrain</u> the <u>parameters</u> of type classes.	<mark>s</mark> and <mark>m</mark>		
s can be determined from m , so that s can be the <u>return</u> type but m can <u>not</u> be the <u>return</u> type	m → s State s → s		
in a <u>multi-parameter</u> type class,			
<u>one</u> of the parameters can be <u>determined</u> from the <u>others</u> , so that <u>the parameter</u> determined by the others can be the <u>return type</u> but <u>none</u> of the <u>argument</u> types of some of the methods.			

class Monad m where return :: a -> m a (>>=) :: m a -> (a -> m b) -> m b (>>) :: m a -> m b -> m b fail :: String -> m a



https://stackoverflow.com/questions/23149318/get-put-and-state-in-monadstate

Typeclass MonadState s

class Monad m => MonadState s m m -> s where	
MonadState s a <u>typeclass</u>	:t get :t put
instance MonadState s MM where its <u>type instance</u> itself does not specify <u>values</u>	s ← m functional dependencies
 MonadState s m => can be used as <u>class constraint</u> all the Monad m 	m á State s → s
which supports <i>state operations</i> with state of type s .	state operations defined in the <u>typeclass</u> definition

Types of get and put

:t get ►	get :: MonadState s m => m s	get :: m s
we have a <u>valu</u>	n which supports <i>state operations</i> over state of typ le of <u>type</u> m s - that is, eration which <u>yields</u> the <u>current</u> <u>state</u>	De s,
:t put ►	put :: MonadState s m => s -> m ()	put :: s -> m ()
and returns a p representing ar	takes a <u>value</u> of <u>type</u> s polymorphic value ny <mark>Monad m</mark> s <u>state operations</u> over a state of <u>type</u> s	

Instances of MonadState s m

class Monad m => MonadState s m | m -> s where

The mtl package Control.Monad.State.Class module

instance Monad m => MonadState s (Lazy.StateT s m) where ...

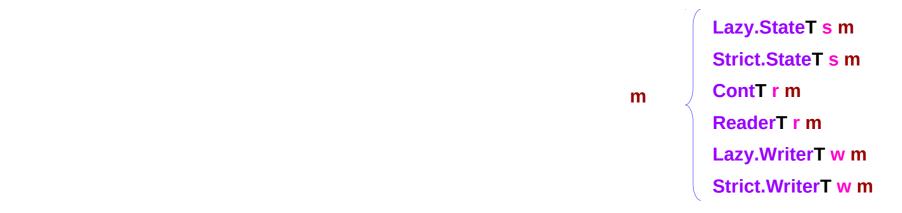
instance Monad m => MonadState s (Strict.StateT s m) where ...

instance MonadState s m => MonadState s (ContT r m) where ...

instance MonadState s m => MonadState s (ReaderT r m) where ...

instance (Monoid w, MonadState s m) => MonadState s (Lazy.WriterT w m) where ...

instance (Monoid w, MonadState s m) => MonadState s (Strict.WriterT w m) where ...



https://stackoverflow.com/questions/23149318/get-put-and-state-in-monadstate

Instances of the typeclass MonadState s

MonadState s is the <u>class</u> of <u>types</u> that are monads with state.

instance MonadState s (State s) where get = Control.Monad.Trans.State.get

put = Control.Monad.Trans.State.put

State s is an instance of that typeclass:

instance MonadState s (StateT s) where get = Control.Monad.Trans.State.get put = Control.Monad.Trans.State.put

StateT s is an <u>instance</u> of that <u>typeclass</u>: (the state monad transformer which adds <u>state</u> to another monad)

Overloading get and put

instance MonadState s (State s) where get = Control.Monad.Trans.State.get

put = Control.Monad.Trans.State.put

This overloading was introduced so that

if you're using a stack of monad transformers,

you do not need to explicitly lift operations

between different transformers.

If you're not doing that,

you can use the simpler operations from transformers.

The **mtl** package provides auto-lifting

Typeclass Constrain MonadState s m (1)

class Monad m => MonadState s m | m -> s where ...

get :: MonadState s m => m s

for some monad **m**

storing some <u>state</u> of type s,

get is an <u>action</u> in m

that returns a value of type s.

Typeclass Constrain MonadState s m (2)

```
class Monad m => MonadState s m | m -> s where ...
```

```
put :: MonadState s m => s -> m ()
```

for some monad **m**

put is an <u>action</u> in m

storing the given <u>state</u> of type s,

but returns nothing ().

References

- [1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
- [2] https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf