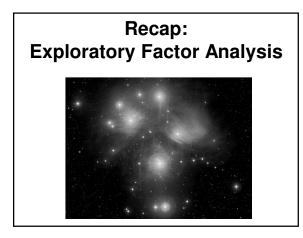
Overview 1 Recap: Exploratory factor analysis 2 Concepts & their measurement 3 Measurement error 4 Psychometrics 5 Reliability & validity 6 Composite scores 7 Writing up instrument development



What is factor analysis?

- · Factor analysis is:
 - a *family* of multivariate correlational methods used to identify clusters of covariance (called factors)
- Two main purposes:
 - -Theoretical (PAF)
- Data reduction (PC)
 Two main types (extraction methods):
 - -Exploratory factor analysis (EFA)
 - -Confirmatory factor analysis (CFA)

EFA steps

1 Test assumptions

- Sample size
 - 5+ cases x no. of variables (min.)
 - 20+ cases x no. of variables (ideal)
- Another guideline: N > 200
- Outliers & linearity
- Factorability Use any of:
 - Correlation matrix: Some > .3?
 - Anti-image correlation matrix diags > .5
 Measures of Sampling Adequacy:
 - Measures of Sampling Adequation
 KMO > ~ .5 to 6
 - Bartlett's sig?

5

EFA steps

2 Select type of analysis

- Extraction
- Principal Components (PC)
- Principal Axis Factoring (PAF)
- Rotation
- Orthogonal (Varimax)
- Oblique (Oblimin)

4

EFA steps

- 3. Determine no. of factors
 - Theory?
 - Kaiser's criterion?
 - Eigen Values and Scree plot?
 % variance explained?
 - Interpretability of weakest factor?

EFA steps

Select items

- Use factor loadings to help identify which items belong in which factor
- Drop items one at a time if they don't belong to any factor e.g., consider any items for which
 - primary (highest) loading is low? (< .5 ?)
 - cross- (other) loading(s) are high? (> .3 ?)
 - item wording doesn't match the meaning of the factor

EFA steps

5 Name and describe factors

6 Examine correlations amongst factors

7 Analyse internal reliability

8 Compute composite scores | Covered in 9 Check factor structure across | this lecture sub-groups

9

EFA example 4: University student motivation

Example EFA: University student motivation

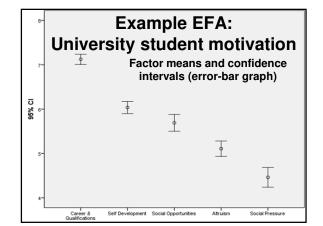
- 271 UC students responded to 24 student motivation statements in 2008
- . 8-point Likert scale (False to True)
- For example:
 - "I study at university ... "
 - to enhance my job prospects.
- because other people have told me I should.
- EFA PC Oblimin revealed 5 factors

This is a pattern matrix 914 779 showing factor tiv25 loading€shows a simple Example EFA: Pattern matrix .955 factor structure. Primary loadings .912 for each item are .885 .765 above .5 notiv22 -.884 notiv17 -.883 -.876 -.734 notiv12 notiv03 - 725 Cross-loadings motiv23 .862 .847 are all below .3. notiv1 motiv21 .767 notiv02 .740 -.248 12

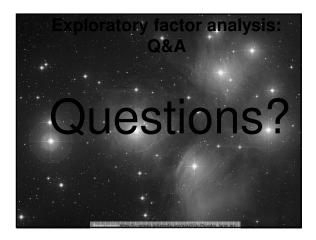
Example EFA: University student motivation 1. Career & Qualifications (6 items; $\alpha = .92$) 2. Self Development (5 items; $\alpha = .81$) 3. Social Opportunities (3 items; $\alpha = .90$) 4. Altruism (5 items; $\alpha = .90$) 5. Social Pressure

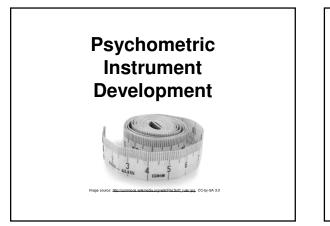
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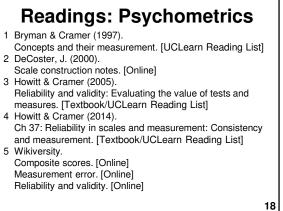
(5 items; $\alpha = .94$)

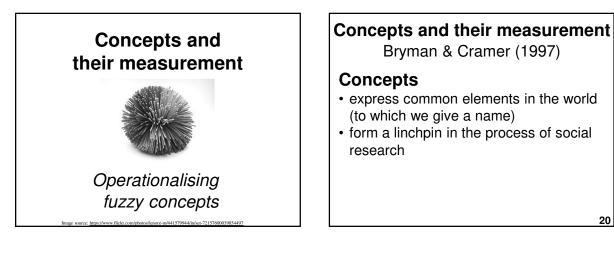


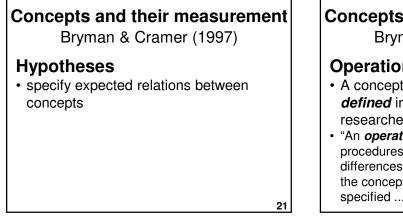
Example EFA: University student motivation Factor correlations										
Motivation	Self Develop ment	Social Enjoyme nt	Altruism	Social Pressure						
Career & Qualifications	.26	.25	.24	.06						
Self Development		.33	.55	18						
Social Enjoyment			.26	.33						
Altruism				.11						
				15						











Concepts and their measurement

Bryman & Cramer (1997)

Operationalisation

- A concept needs to be operationally *defined* in order to be systematically researched.
- "An operational definition specifies the procedures (operations) that will permit differences between individuals in respect of the concept(s) concerned to be precisely specified ..." 22

Concepts and their measurement Bryman & Cramer (1997)

"... What we are in reality talking about here is *measurement*, that is, the assignment of numbers to the units of analysis - be they people, organizations, or nations - to which a

concept refers."



Operationalisation . The act of making a fuzzy concept measurable.

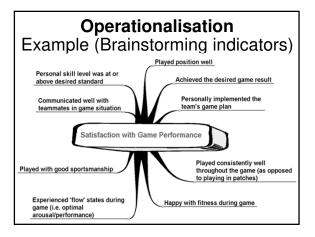
 Social science often uses multi-item measures to assess related but distinct aspects of a fuzzy concept.

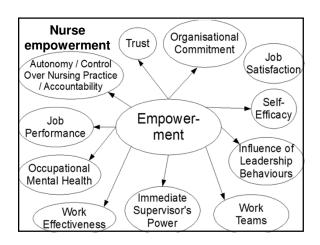


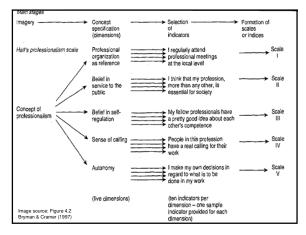


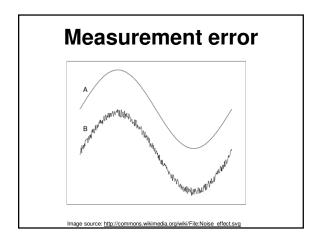
- 1 Brainstorm indicators of a concept
- 2 Define the concept
- 3 Draft measurement items
- 4 Pre-test and pilot test
- 5 Examine psychometric properties
- how precise are the measures?

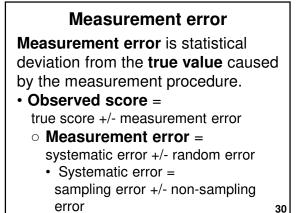
6 Redraft/refine and re-test





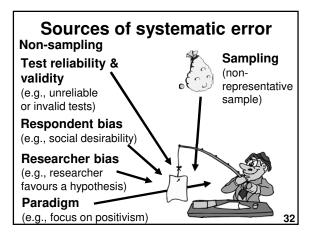






Systematic error – e.g., bathroom scales aren't calibrated properly, and every measurement is 0.5kg too high. This error occurs for each measurement.

Random error – e.g., measure your weight 3 times using the same scales but get three slightly different readings. The amount of error differs for each measurement.



Measurement precision & noise The lower the measurement precision, the more participants are needed to make up for the "noise" in the measurements. Even with a larger sample, noisy data can be hard to interpret. Especially when testing and assessing

 Especially when testing and assessing individual clients, special care is needed when interpreting results of noisy tests.

http://www.sportsci.org/resource/stats/precision.htm

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Minimising measurement error

- Standardise administration conditions with clear instructions and questions
- Minimise potential demand characteristics (e.g., train interviewers)
- Use multiple indicators for fuzzy constructs

Minimising measurement error

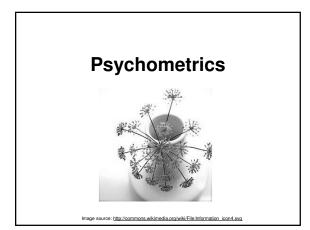
- Obtain a representative sample:
 - Use probability-sampling, if possible
 For non-probability sampling, use
 - strategies to minimise selection bias
- Maximise response rate: -Pre-survey contact
 - -Pre-survey contact
 - -Minimise length / time / hassle
 - -Rewards / incentives
 - -Coloured paper -Call backs / reminders

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Minimising measurement error Ensure administrative accuracy: Set up efficient coding, with well-labelled variables Check data (double-check at least a portion of the data)

36

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Psychometrics: Goal

To validly measure differences between individuals and groups in psychosocial qualities such as attitudes and personality.

Psychometrics: Tasks

- Develop approaches and procedures (theory and practice) for measuring psychological phenomena
- Design and test psychological measurement instrumentation (e.g., examine and improve reliability and validity of psychological tests)

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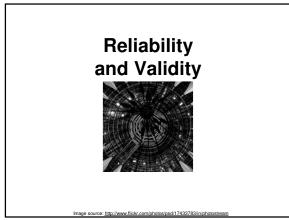
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Psychometrics: In demand

"Psychometrics, one of the most obscure, esoteric and cerebral professions in America, is now also one of the hottest." <u>As test-taking grows, test-makers grow rarer</u>, David M. Herszenhor, May 5, 2006, New York Times Psychometricians are in demand due to

increased testing of educational and psychological capacity and performance.

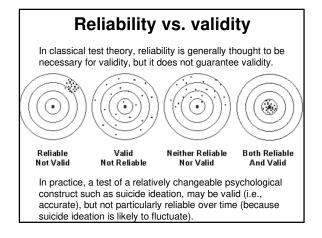
Psychometrics: Methods • Factor analysis – Exploratory – Confirmatory • Classical test theory –Reliability –Validity

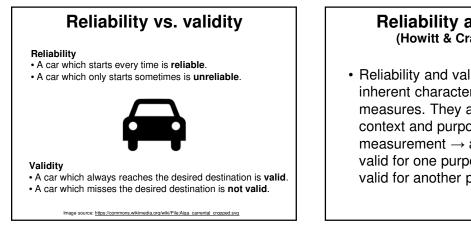


Reliability and validity (Howitt & Cramer, 2005)

Reliability and validity ("classical test theory") are ways of evaluating the accuracy of psychological tests and measures.

- · Reliability is about consistency of - items within the measure
 - the measure over time
- Validity is about whether the measure actually measures what it is intended to measure.

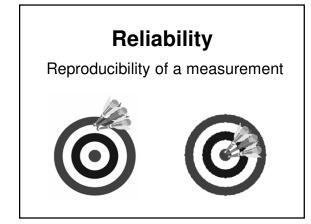




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Reliability and validity (Howitt & Cramer, 2005)

· Reliability and validity are not inherent characteristics of measures. They are affected by the context and purpose of the measurement \rightarrow a measure that is valid for one purpose may not be valid for another purpose.



Reliability: Types

- Internal consistency: Correlation among multiple items in a factor - Cronbach's Alpha (α)
- Test-retest reliability: Correlation between test at one time and another - Product-moment correlation (r)
- Inter-rater reliability: Correlation between one observer and another: – Kappa

48

Reliability: Rule of thumb

< .6 = Unreliable

.6 = OK

- .7 = Good
- .8 = Very good, strong
- .9 = Excellent

> .95 = may be overly reliable or

redundant – this is subjective and depends on the nature what is being measured

Reliability: Rule of thumb

Table 7 Fabrigar et al. (1999)	Perse and	nal of onality Social hology	Ap	rnal of plied chology
Variable	Ν	%	N	%
Average reliability of variables				
Less than .60	3	1.9	2	3.4
.60–.69	6	3.8	5	8.6
.70–.79	33	20.8	9	15.5
.8089	33	20.8	11	19.0
.90-1.00	14	8.8	9	15.5
Unknown	70	44.0	22	37.9

Internal consistency (or internal reliability)

Internal consistency refers to:

- How well multiple items combine as a measure of a single concept
- The extent to which responses to multiple items are consistent with one another

Internal consistency can measured

- by:
- Split-half reliability
- Odd-even reliability
- Cronbach's Alpha (α)

Internal consistency (recoding)

If dealing with a mixture of positively and negatively scored items, remember to recode so that all items are measured i the same direction.

Internal consistency: Split-half reliability

- Sum the scores for the first half (e.g., 1, 2, 3) of the items.
- Sum the scores for the second half (e.g., 4, 5, 6) of the items.
- Compute a correlation between the sums of the two halves.

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Internal consistency: Odd-even reliability

- Sum the scores for odd items (e.g.,1, 3, 5)
- Sum the scores for even items (e.g., 2, 4, 6)
- Compute a correlation between the sums of the two halves.

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Internal consistency: Cronbach's alpha (α)

- Averages all possible split-half reliability coefficients.
- Akin to a single score which represents the degree of intercorrelation amongst the items.
- Most commonly used indicator of internal reliability.

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How many items per factor?

- More items → greater reliability (The more items, the more "rounded" the measure)
- Minimum items to create a factor is 1.
 No maximum. Law of diminishing
- returns = each additional item will add less and less to the reliability.
- Typically ~ 3 to 10 items per factor are used.
- Final decision is subjective and depends on research context

Internal reliability example Student-rated quality of maths teaching

- 10-item scale measuring students' assessment of the educational quality of their maths classes
- 4-point Likert scale ranging from: strongly disagree to strongly agree

Internal reliability example Quality of mathematics teaching

- 1. My maths teacher is friendly and cares about me.
- 2. The work we do in our maths class is well organised.
- My maths teacher expects high standards of work from everyone.
- 4. My maths teacher helps me to learn.
- 5. I enjoy the work I do in maths classes.

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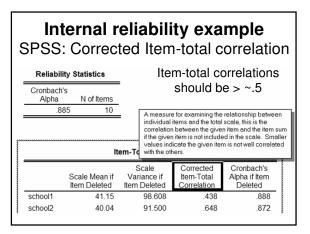
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+ 5 more

56

Internal reliability example Quality of maths teaching

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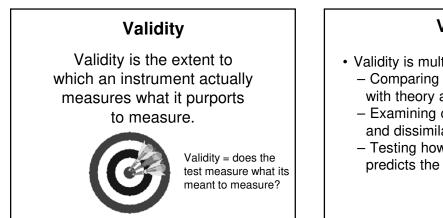


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	Reliabili	ty Statistics		nbach's α d" is highe	if item er than the				
	Cronbach's Alpha N of Items		α, cons	α, consider removing item.					
:	.88	ir C	ndividual items and	iining the relationsh the total scale, this or the remaining iten in the scale.	is the value of				
	Item-Total Statistics								
		Scale Mean if Item Deleted	Scale Variance if Item Deleted	Corrected Item-Total Correlation	Cronbach's Alpha if Item Deleted				
	school1	41.15	98.608	.438	.888				
	school2	40.04	91.500	.648	.872				

Internal reliability example Item-total Statistics SPSS: Reliability output									
	Scale	Scale	Corrected						
	Mean	Variance	Item-	Alpha					
	if Item	if Item	Total	if					
Item									
	Deleted	Deleted	Correlation						
Deleted									
MATHS1 -	25.2749	25.5752	.6614	.8629					
MATHS2	25.0333	26.5322	6235	8661					
MATHS3	25.0192	30.5174	.0996	.9021					
MATHS4	24.9786	25.8671	.7255	.8589					
MATHS5	25.4664	25.6455	.6707	.8622					
MATHS6	25.0813	24.9830	.7114	.8587					
MATHS7	25.0909	26.4215	.6208	.8662					
MATHS8	25.8699	25,7345	.6513	.8637					
MATHS9	25.0340	26.120	movesthic	itom. 8623					
MATHS10	25.4642	25.7578	emovesthis	110-11- ₈₆₃₈					
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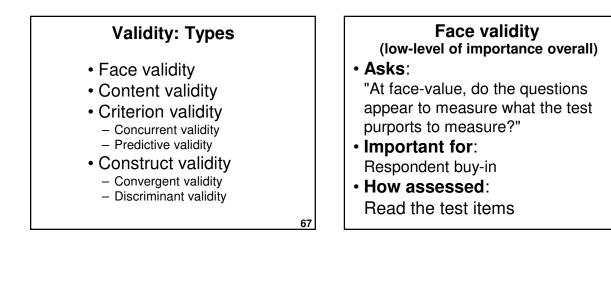
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Item-total S	statistics	SPSS: F	Reliability	output				
	Scale	Scale	Corrected					
	Mean	Variance	Item-	Alpha				
	if Item	if Item	Total	if				
Item								
	Deleted	Deleted	Correlation					
Deleted								
MATHS1	22.2694	24.0699	.6821	.8907				
MATHS2	22.0280	25.2710	.6078	.8961				
MATHS4	21.9727	24.4372	.7365	.8871				
MATHS5	22.4605	24.2235	.6801	.8909				
MATHS6	22.0753	23.5423	.7255	.8873				
MATHS7	22.0849	25.0777	.6166	.8955				
MATHS8	22.8642	24.3449	.6562	.8927				
MATHS9	22.0280	24.5812	.7015	.8895				
MATHS10	22.4590	24.3859	.6524	.8930				
N of Cases =	1355.0	Alpha improves						
Alpha =	. 9024	/		6				

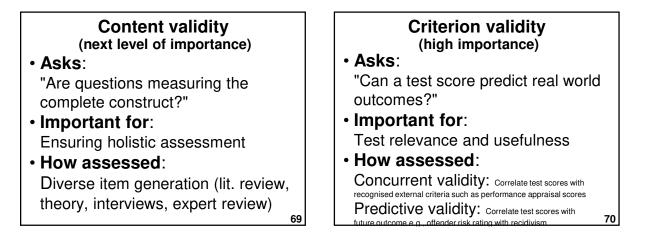
Motivation the required effort into action to attain it. Active Initiative* Initiating action in new situations. .73 .81 Emotional Control Maintaining emotional control when faced .75 .87 with potentially stressful situations. .73 .81 Intellectual Adapting thinking and accommodating new .60 .78 Intellectual information from changing conditions and different perspectives. .73 .84 Self Confidence* Confidence in abilities and the success of .73 .84 actions. Social Competence Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement. .81 .82	LEQ 8-factor model	Description	3 items p	er scale
Motivation the required effort into action to attain it. Active Initiative* Initiating action in new situations. .73 .81 Emotional Control Maintaining emotional control when faced .75 .87 Intellectual Adapting thinking and accommodating new .60 .78 Intellectual Adapting thinking and accommodating new .60 .78 Self Confidence * Confidence in abilities and the success of .73 .84 Social Competence Ability in and success of social .75 .86 Task Leadership Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement. .81 .82				Alpha
Emotional Control Maintaining entroit when faced .75 .87 with potentially stressful situations. Intellectual Adapting thinking and accommodating new .60 .78 information from changing conditions and different perspectives. Self Confidence ' Confidence in abilities and the success of .73 .84 actions. Social Competence Ability in and success of social .75 .86 interactions. Task Leadership Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement.			.68	.87
with potentially stressful situations. .60 .78 Intellectual Adapting thinking and accommodating new .60 .78 Flexibility information from changing conditions and different perspectives. .73 .84 Self Confidence * Confidence in abilities and the success of .73 .84 Social Competence Ability in and success of social .75 .86 Interactions. .75 .86 .81 .82 When a task needs to be done and productivity is the primary requirement. .81 .82	Active Initiative *	Initiating action in new situations.	.73	.81
Flexibility information from changing conditions and different perspectives. Self Confidence Confidence in abilities and the success of .73 .84 actions. Social Competence Ability in and success of social .75 .86 interactions. Task Leadership Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement.	Emotional Control		.75	.87
Self Confidence 'n confidence in abilities and the success of .73 .84 actions. .73 .84 Social Competence Ability in and success of social .75 .86 interactions. .75 .86 Task Leadership Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement. .81		information from changing conditions and	.60	.78
interactions. Task Leadership Ability to lead other people effectively .81 .82 when a task needs to be done and productivity is the primary requirement.	Self Confidence *	Confidence in abilities and the success of	.73	.84
when a task needs to be done and productivity is the primary requirement.	Social Competence		.75	.86
	Task Leadership	when a task needs to be done and	.81	.82
	Time Management		.75	.84
	N		.67	.93

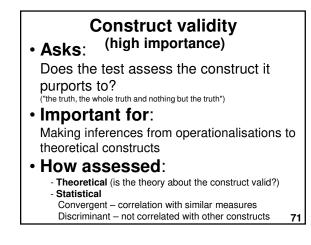


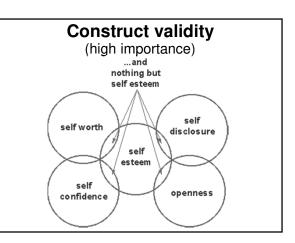
Validity
alidity is multifaceted and includes:
 Comparing wording of the items with theory and expert opinion
- Examining correlations with similar
and dissimilar measures

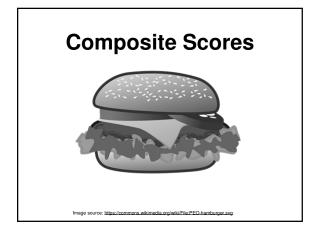
 Testing how well the measure predicts the future







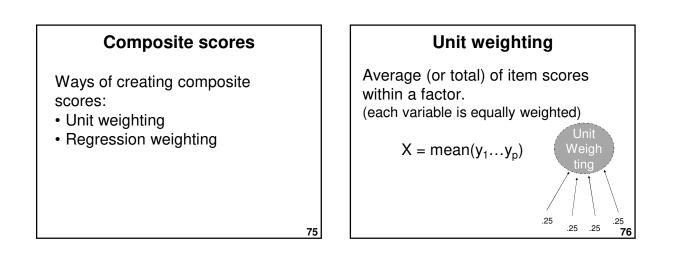




Composite scores Combine item-scores into an overall factor score which represents individual differences for the target construct. The new composite score can then

The new composite score can then be used for:

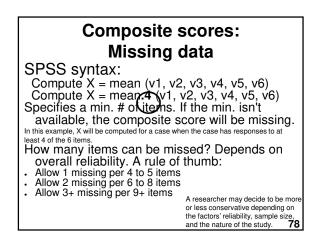
- · Descriptive statistics and histograms
- Correlations
- As IVs and/or DVs in inferential analyses such as MLR and ANOVA

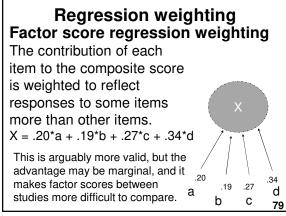


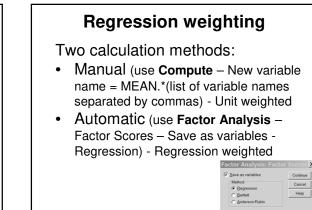
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Composite scores: Missing data

To maximise the sample size, consider computing composite scores in a way that allows for some missing data.







Variat	ole vi	ew: o	f varia	DN W bles ai				ugh
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64 FAC1_	1 Nume	eric	11 5		REGR fact	tor score	for analysi	is 1 N
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66 FAC3_	1 Nume	eric	11 5		REGR fact	tor score	6 for analysi	is 1 N
67 FAC4_	1 Nume	eric	11 5		REGR fact	tor score	for analysi	is 1 N
68 FAC5_	1 Nume	eric	11 5		REGR fact	tor score	o for analysi	is 1 N
69 FAC6_	1 Nume	eric	11 5		REGR fact	tor score 6	for analysi	is 1 N
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-1.34	-1.90		-1.06	10	1.95	-1.39	.66	08
36	02	1.61	-1.27	-2.05	-1.77	74	.72	1.00
.51	09		.56	1.05	72	93	1.06	17
.30	54		2.65	54	.11	1.82	.53	1.23
01	1.18		26	1.35	-1.36	58	-1.06	63
-1.91	-1.74	1.73	36	-2.47	1.34	.37	.86	38



Writing up instrument development

- Introduction
 - Review previous literature about the construct's underlying factors – consider both theory and research
 - -Generate a research question e.g., "What are the underlying factors of X?".
 - -Could also make a hypothesis about the number of factors and what they will represent.

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Writing up instrument development

Method

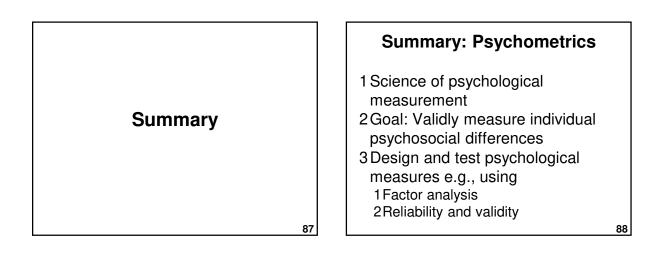
- Materials – summarise the design and development of the measures and the expected factor structure e.g., present a table of the expected factors and their operational definitions.

Writing up instrument development

- Results
 - -Factor analysis
 - Assumption testing
 - Extraction method & rotation
 - \bullet # of factors, with names and definitions
 - # of items removed and rationale
 - Item factor loadings & communalities
 - Factor correlations
 - -Reliability for each factor
 - -Composite scores for each factor
 - -Correlations between factors

Writing up instrument development

- Discussion
- Theoretical underpinning Was it supported by the data? What adaptations should be made to the theory?
- Quality / usefulness of measure Provide an objective, critical assessment, reflecting the measures' strengths and weaknesses
- Recommendations for further improvement
- Writing up a factor analysis
 Download examples: <u>http://goo.gl/fD2qby</u>

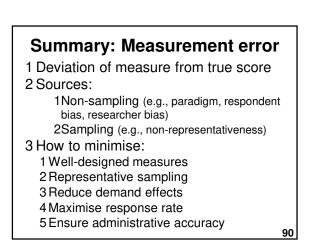


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Summary: Concepts & their measurement

- 1 Concepts name common elements
- 2 Hypotheses identify relations between concepts
- 3 Brainstorm indicators of a concept
- 4 Define the concept
- 5 Draft measurement items
- 6 Pre-test and pilot test
- 7 Examine psychometric properties
- 8 Redraft/refine and re-test



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Summary: Reliability

1 Consistency or reproducibility 2 Types 1 Internal consistency 2Test-retest reliability 3 Rule of thumb 1 > .6 OK 2>.8 Very good 4 Internal consistency 1 Split-half 2 Odd-even 3 Cronbach's Alpha

Summary: Validity 1 Extent to which a measure measures what it is intended to measure 2 Multifaceted 1 Compare with theory and expert opinion 2 Correlations with similar and dissimilar measures **3 Predicts future**

Summary: Composite scores

Ways of creating composite (factor) scores:

1. Unit weighting

1.Total of items or 2. Average of items (recommended for lab report)

2. Regression weighting 1. Each item is weighted by its importance to measuring the underlying

factor (based on regression weights)

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Summary: Writing up instrument development

1. Introduction

- 1. Review constructs & previous structures
- 2. Generate research question or hypothesis
- 2. Method
 - 1. Explain measures and their development

3. Results

- 1. Factor analysis
- 2. Reliability of factors
- 3. Descriptive statistics for composite scores 4. Correlations between factors

4. Discussion

1. Theory? / Measure? / Recommendations?

References

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 Fabrigar, L. R., Wegener, D. T., MacCallum, R. C., & Strahan, E. J. (1999). Evaluating the use of exploratory factor analysis in psychological research. Psychological Methods, 4(3), 272-299.
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- 6 Howitt, D. & Cramer, D. (2005). Reliability and validity: Evaluating the value of tests and measures (Ch. 13). In Introduction to research methods in psychology (pp. 218-231). Harlow, Essex: Pearson. UCLearn Reading List.

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Next lecture

Multiple linear regression I

- Correlation (Review)
- Simple linear regression
- Multiple linear regression