## CMOS Delay-7 (H.8) Delay Model

20170201

Copyright (c) 2015 - 2016 Young W. Lim.

•

Permission is granted to copy, distribute and/or modify this document under the terms of the GNU Free Documentation License, Version 1.2 or any later version published by the Free Software Foundation; with no Invariant Sections, no Front-Cover Texts, and no Back-Cover Texts. A copy of the license is included in the section entitled "GNU Free Documentation License".

References
------------

Some	Figures	from	the	follov	vina	sites
Joine	inguics	110111	CIIC	101101	vii ig	SILCS

[1] http://pages.hmc.edu/harris/cmosvlsi/4e/index.html
 Weste & Harris Book Site

[2] en.wikipedia.org

$$\beta: \text{Device Transconductance Parameter} \\ k: \text{Process Transconductance Parameter} \\ k: \text{Process Transconductance Parameter} \\ \mu: \text{Electron / Hole Mobility} \\ PMOS \quad \beta_{P} = k'_{P} \left(\frac{W}{L}\right)_{P} \qquad k'_{P} = \mu_{P} C_{ox} \quad C_{ox} = \frac{C_{ox}}{C_{ox}} \\ n MOS \quad \beta_{n} = k'_{n} \left(\frac{W}{L}\right)_{n} \qquad k'_{n} = \mu_{n} C_{ox} \quad C_{ox} = \frac{C_{ox}}{C_{ox}} \\ PMOS \quad \beta_{P} = \mu_{P} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{P} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} = \mu_{n} \frac{C_{ox}}{C_{ox}} \left(\frac{W}{L}\right)_{n} \\ n MOS \quad \beta_{n} =$$

Saturation Current  $I_{d_{p}} = \frac{\beta_{p}}{2} \left( V_{GSN} - |V_{Tp}| \right)^{2} \qquad V_{Tp} < D$   $I_{d_{n}} = \frac{\beta_{n}}{2} \left( V_{GSN} - V_{Tn} \right)^{3} \qquad V_{Tn} > D$ 

 $\begin{array}{c} k'_{n} \left(\frac{\omega}{L}\right)_{n} \\ k'_{p} \left(\frac{\omega}{L}\right)_{p} \end{array}$  $\frac{\dot{k_n}}{\dot{k_p}}$ Bn Bp = 2~3 .  $\frac{\dot{k'_n}}{\dot{k'_p}} = \frac{\mu_n}{\mu_p} = r$ 

 $\frac{\beta_{n}}{\beta_{p}} = \frac{k'_{n} \left(\frac{\omega}{L}\right)_{n}}{k'_{p} \left(\frac{\omega}{L}\right)_{p}}$ R  $R_n = \frac{1}{\beta_n (V_{pp} - V_{T_n})}$  $R_{p} = \frac{1}{\beta_{n} (V_{pp} - V_{T_{p}})}$ (MJ fall time  $t_f$   $T_n = R_n C_{out}$ rise time tr Cp = Rp Cout Cout = Cpara + CL

fall time	$t_{f} = 2.2 \ C_{n} = l_{n} 9 \ C_{n}$	$0.9 \ U_{pp} \rightarrow 0.1 \ V_{pp}$
rise time	$tr = 2.2 \ C_p = \ln 9 \ C_p$	$0 \mid \bigvee_{PP} \longrightarrow 0.9 \bigvee_{PD}$
propagation delay time	$t_p = \frac{1}{2} (t_{pf} + t_{pr})$ $= 0.35(t_{pf} + t_{pr})$	0.5 Vpp -> 0.5 Vpp
propagation fall time	$t_{pf} = 0.7  \tau_n = \ln 2  \tau_n$	$V_{Pb} \rightarrow 0.5 V_{Pb}$
propagation rise time	$t_{pr} = 0.\gamma \tau_p = ln 2 \tau_p$	0 → 0.5 Vpb
	$T_n = Rn (C_{para} + C_L)$ $T_n = P_n (C_{para} + C_L)$	•
	$C_{p} = R_{p} (C_{pana} + C_{L})$ $C_{out} = C_{pana} + C_{L}$	

$$\begin{pmatrix} \omega \\ \nu \end{pmatrix}_{p} = Y \begin{pmatrix} \omega \\ L \end{pmatrix}_{n}$$

$$Y = \frac{\mu_{n}}{\mu_{p}} = \frac{k_{n}'}{k_{p}'} \neq 1$$

$$R_{n} = R_{p} = R_{m} = \frac{1}{\beta (V_{pp} - V_{T})}$$

$$\begin{cases} U_{but} (t) = V_{pp} (1 - e^{-t/2}) \\ V_{but} (t) = V_{pp} e^{-t/2} \end{cases}$$

$$T = RC_{out} = R (C_{pow} + C_{L})$$

$$Generic Switching Delay$$

$$t_{s} = t_{o} + \alpha C_{L} \Rightarrow t_{s} = t_{r} = t_{f}$$

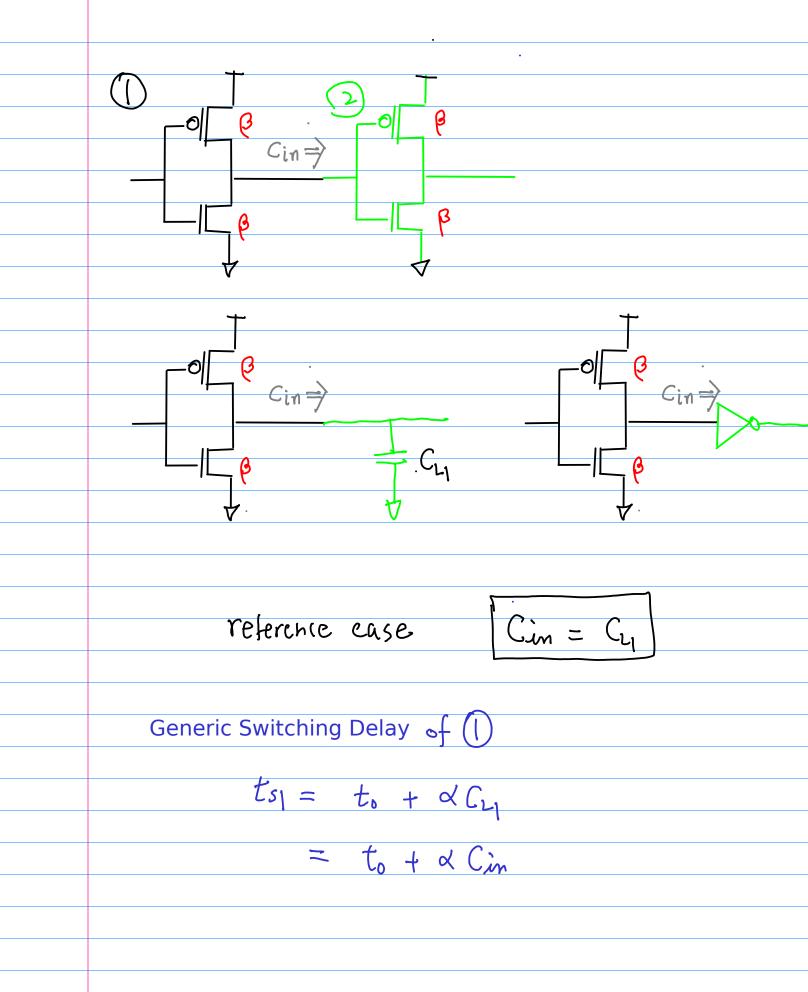
•

•

 Generic Switching Delay
$t_s = t_0 + \alpha C_2$
<u> </u>
ts to; zero delan
to; zero delay x: slope
to
C <sub>L</sub>
 t~ RC
$\propto \sim $
$\beta(Vpp-V_7)$

•

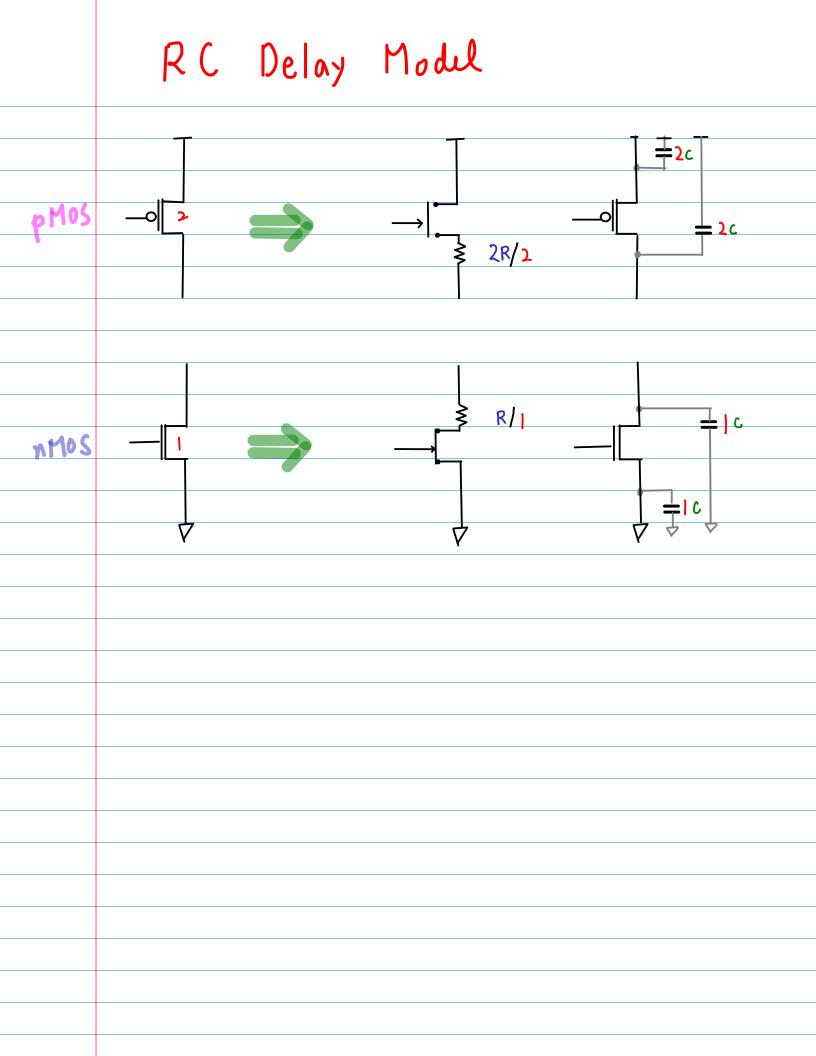


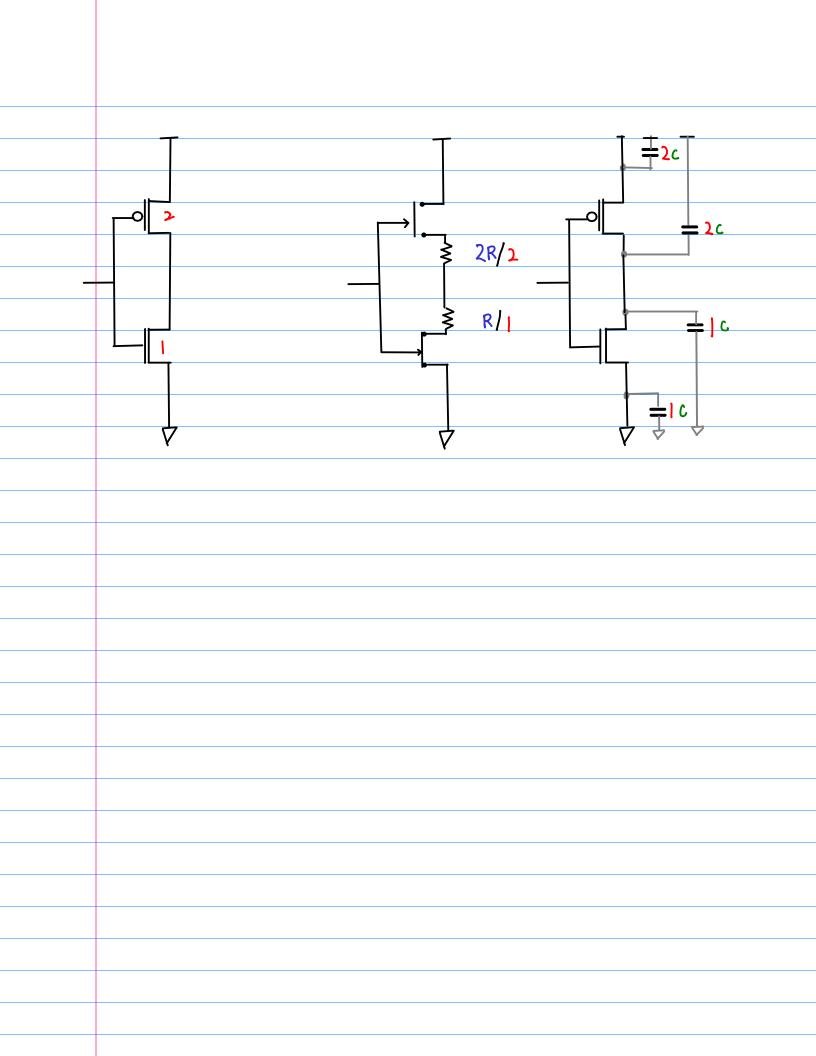


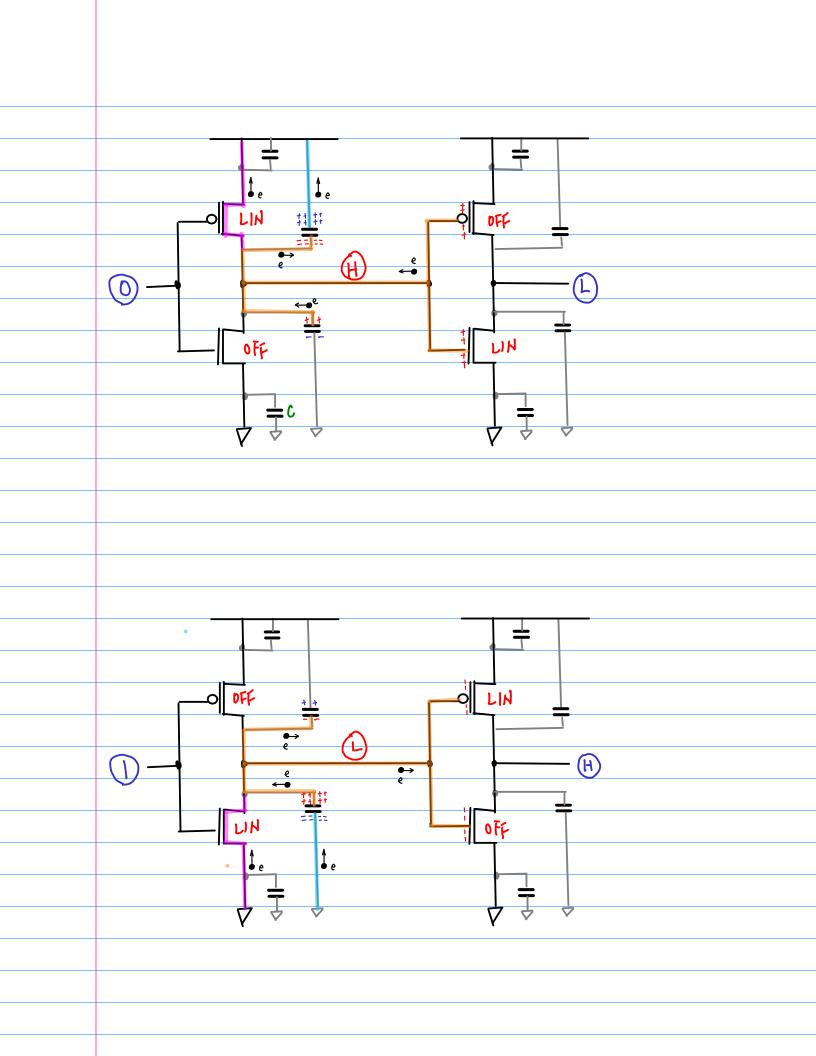
Cin = Can + Cap = Cox (AGn + AGP) Ai gate anea the channel length L assumed Cim = Cox L (Wn + Wp)  $= C_{0x}L(W_n + YW_p)$ =  $C_{0x} \perp W_{p} \cdot (|+r)$ =  $C_{gn}(1+r)$ 

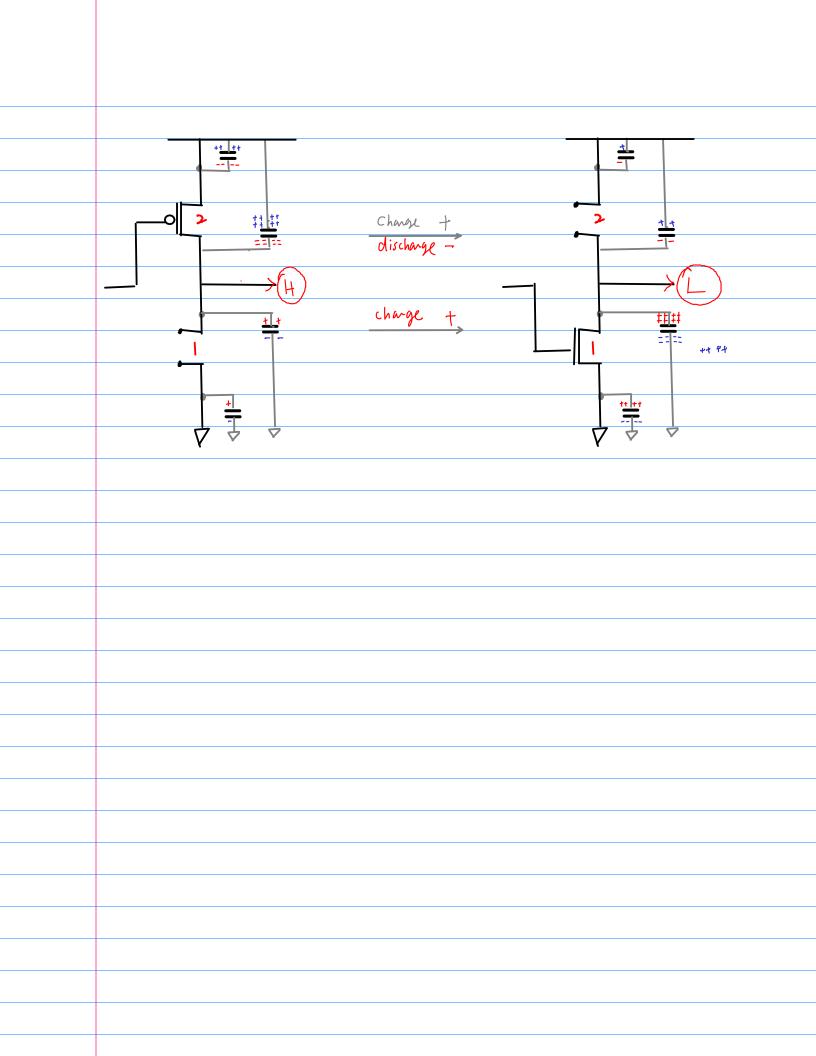
When CL >> Cin -OCin=> ୗ Cin  $C_{L_1}$ ß ß B FCL to minimize ts  $\forall \downarrow \Rightarrow R \downarrow \Rightarrow \beta \uparrow \Rightarrow bigger size$ speed U.S. anea tradeoff ts = to + dG2 t ~ RC  $\propto \propto \frac{1}{\beta(Vpp-V)}$ CL

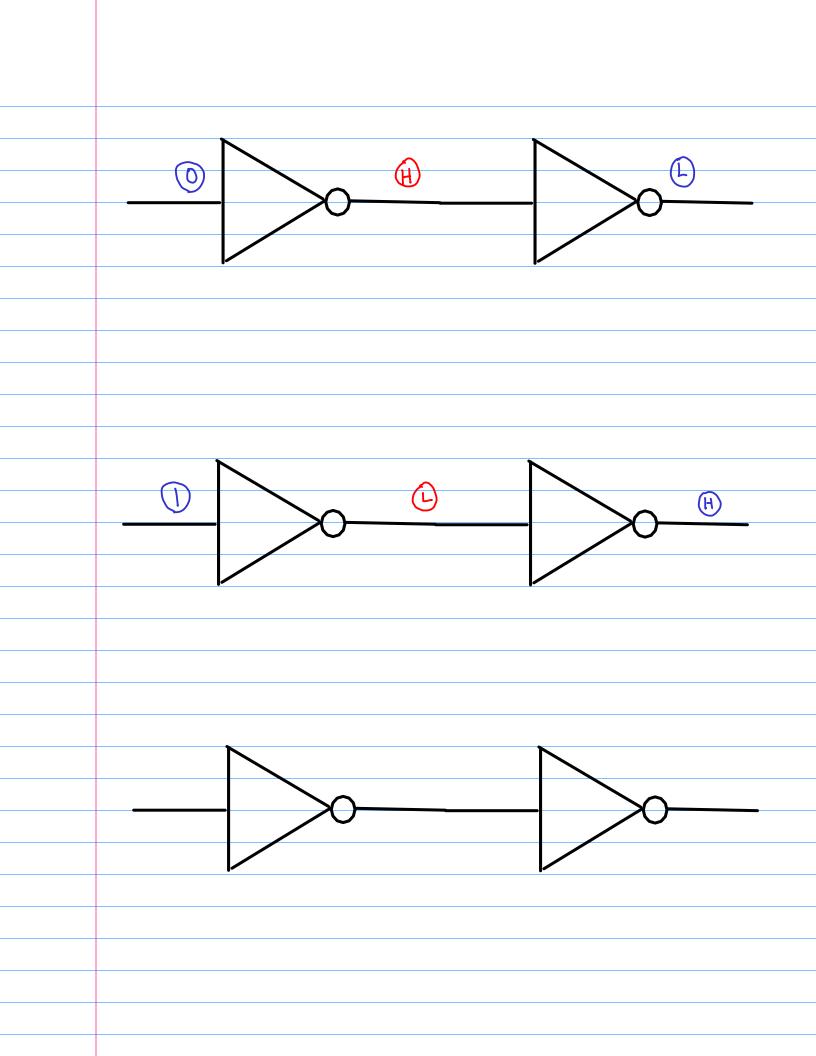
to minimize ts  $\mathbb{V} \downarrow \Rightarrow \mathbb{R} \downarrow \Rightarrow \mathbb{B} \uparrow \Rightarrow \text{bigger size}$ speed V.S. anea tradeoff Scaling Factor S.  $\beta' = \beta \beta$  $R' = \frac{R}{\sqrt{2}}$  $\alpha' = \alpha'$  $t_s = t_0 + \frac{\alpha}{s} C_L$ Compensation Factor (1) enables a NOT gate drive larger values of (CL) If  $C_{L} = 5$  Cin (increased by the scaling factor \$) then the switching time is the same

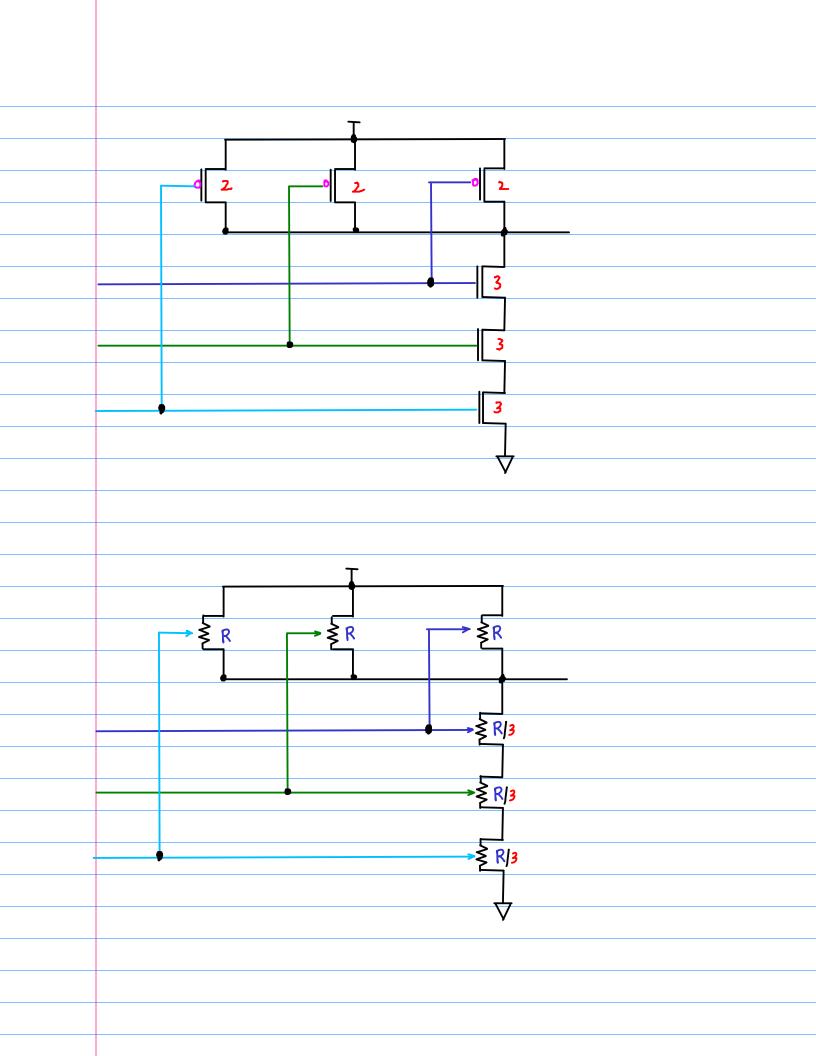


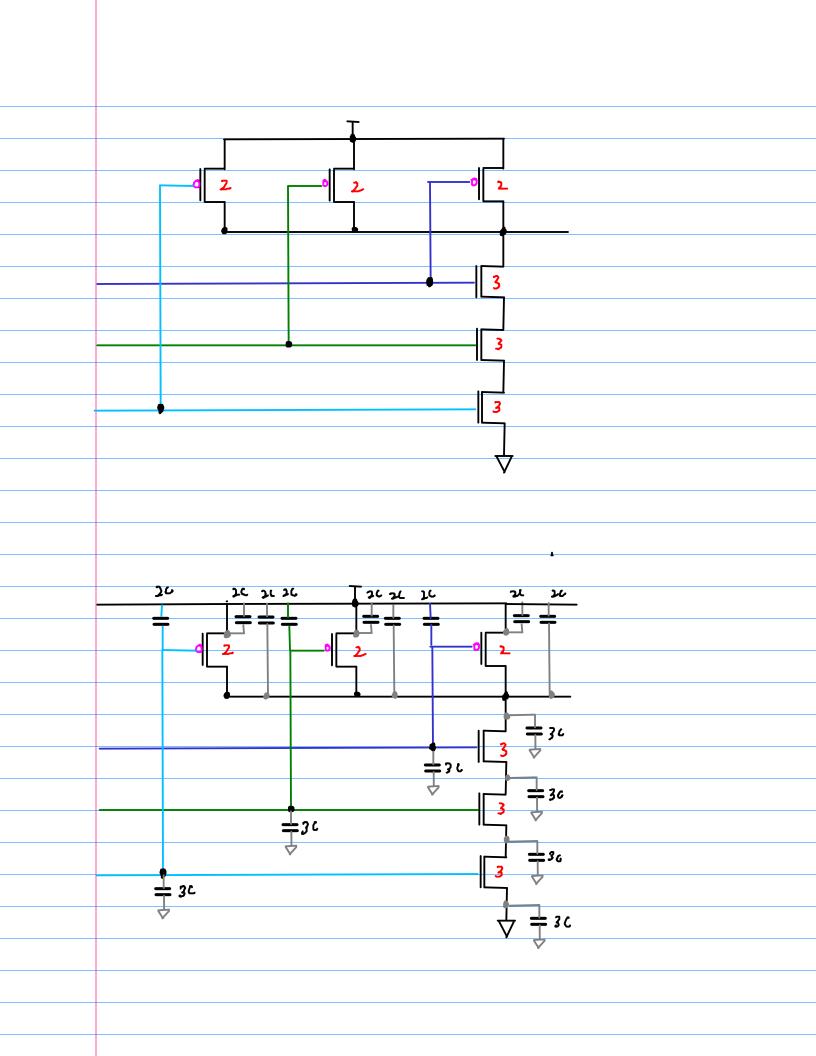


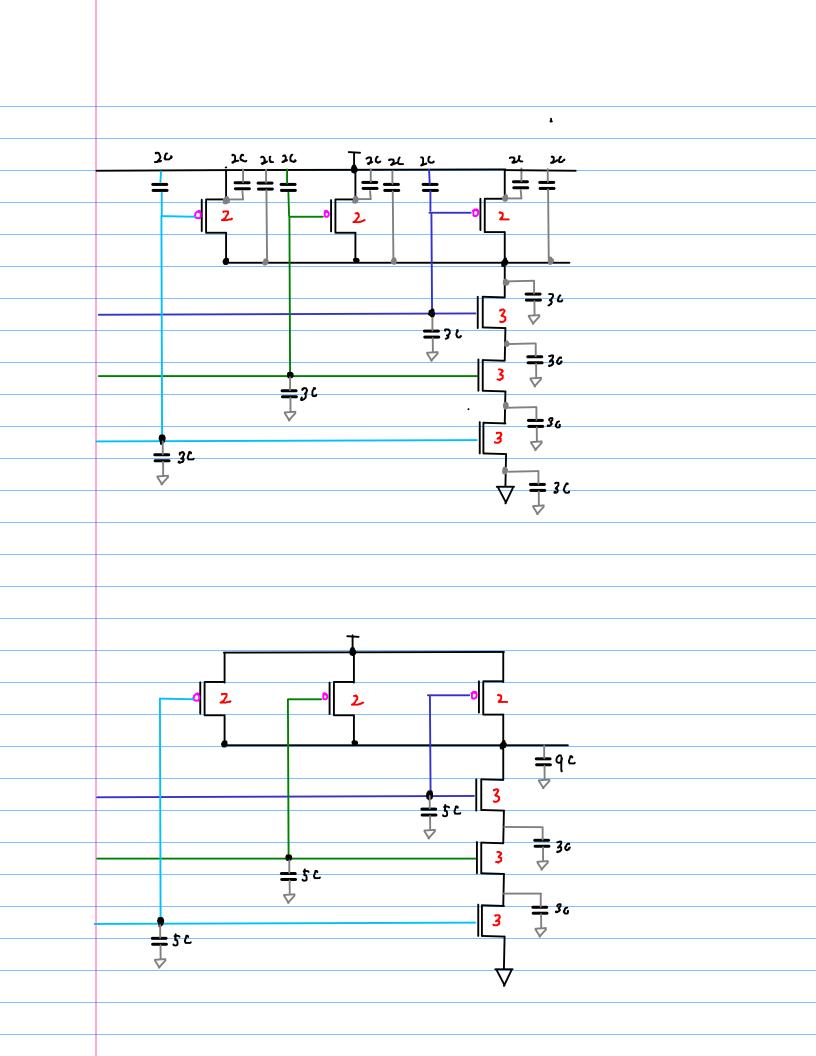


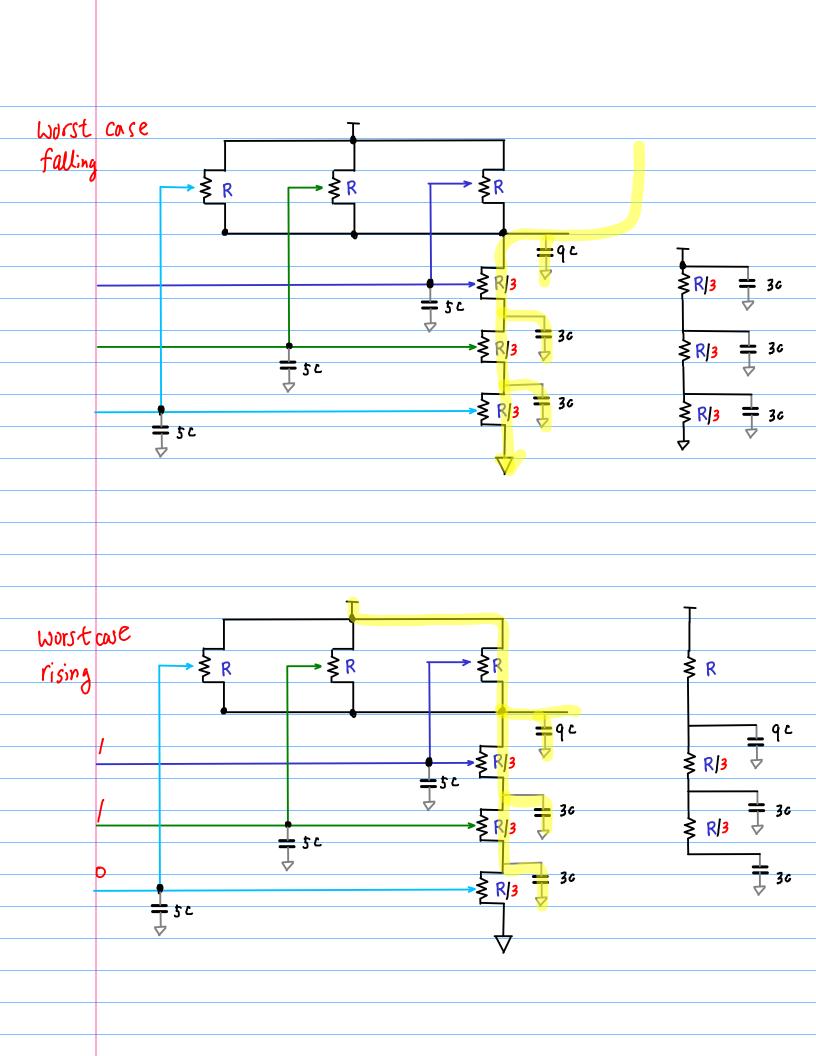


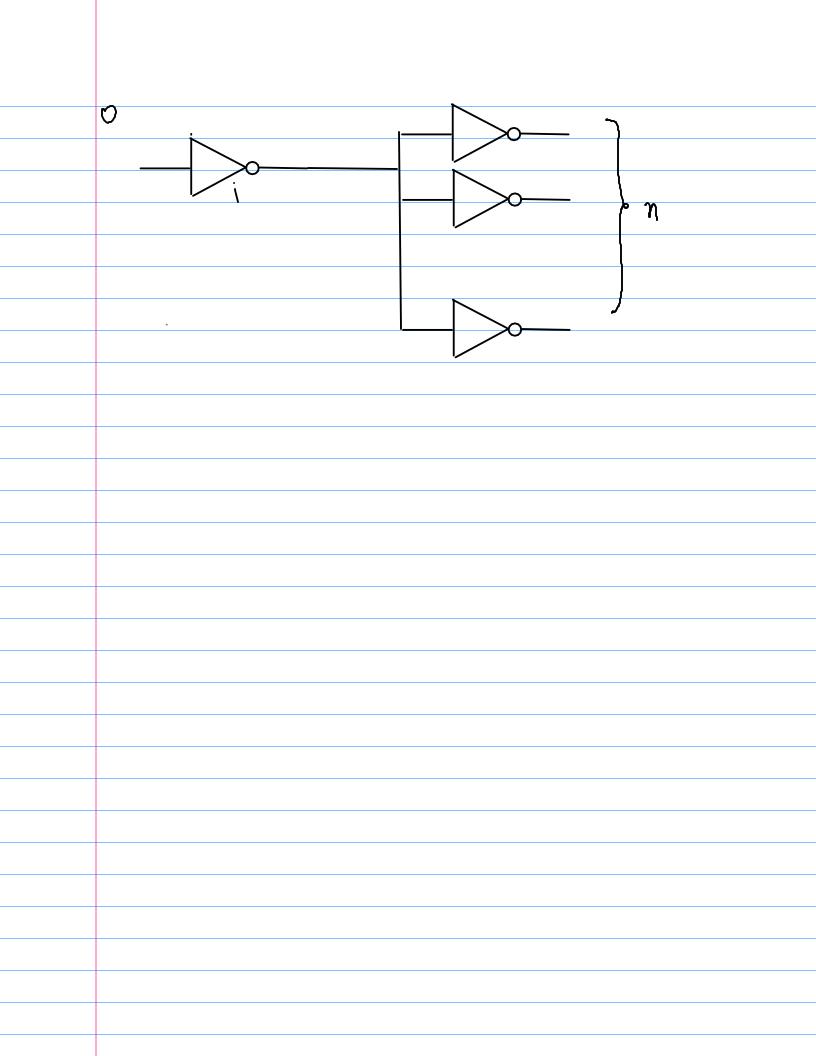


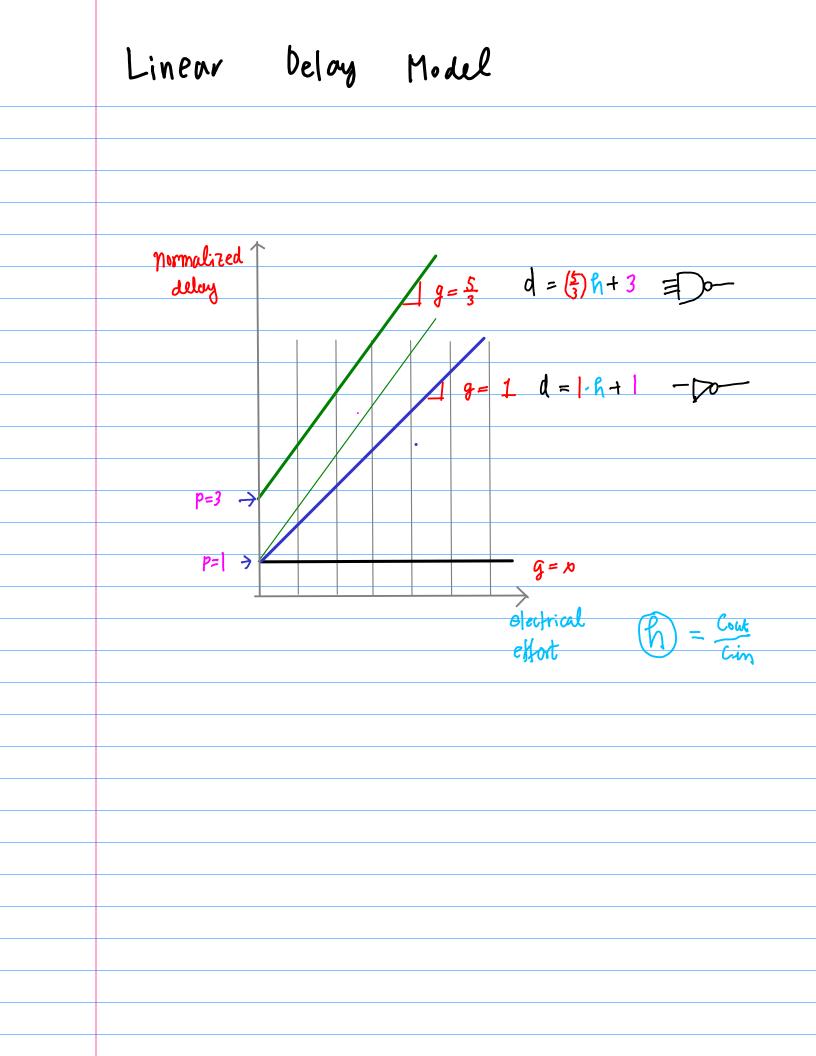


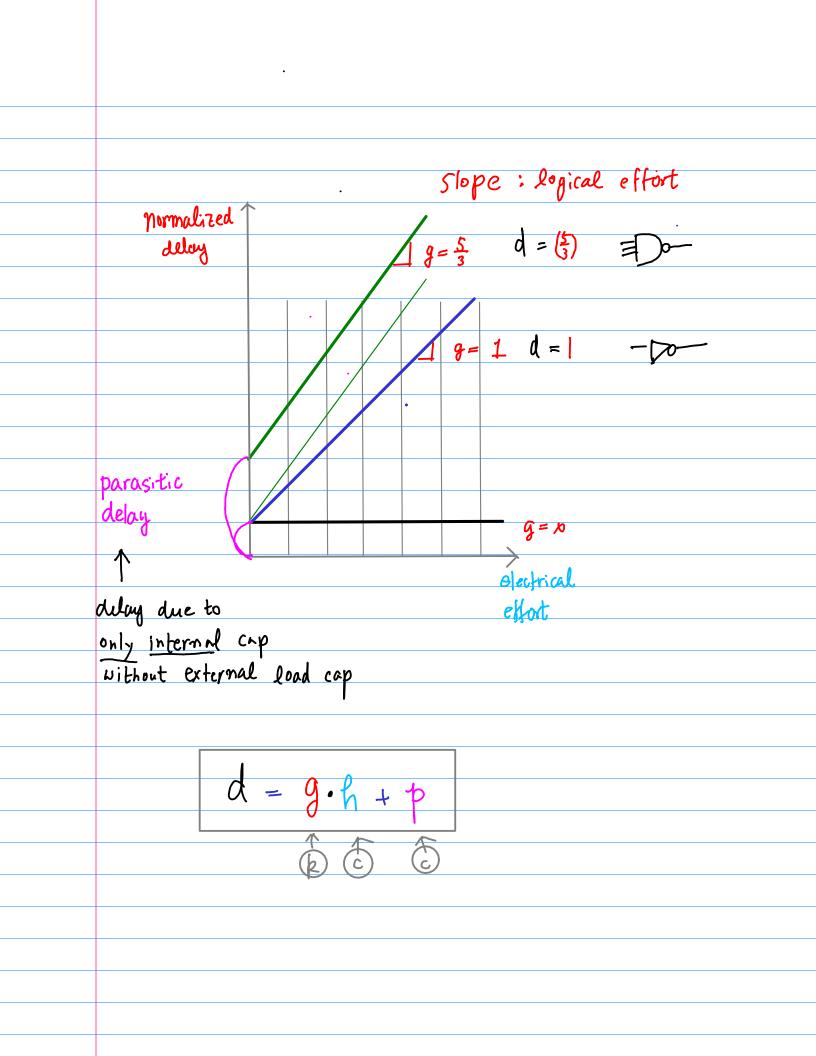


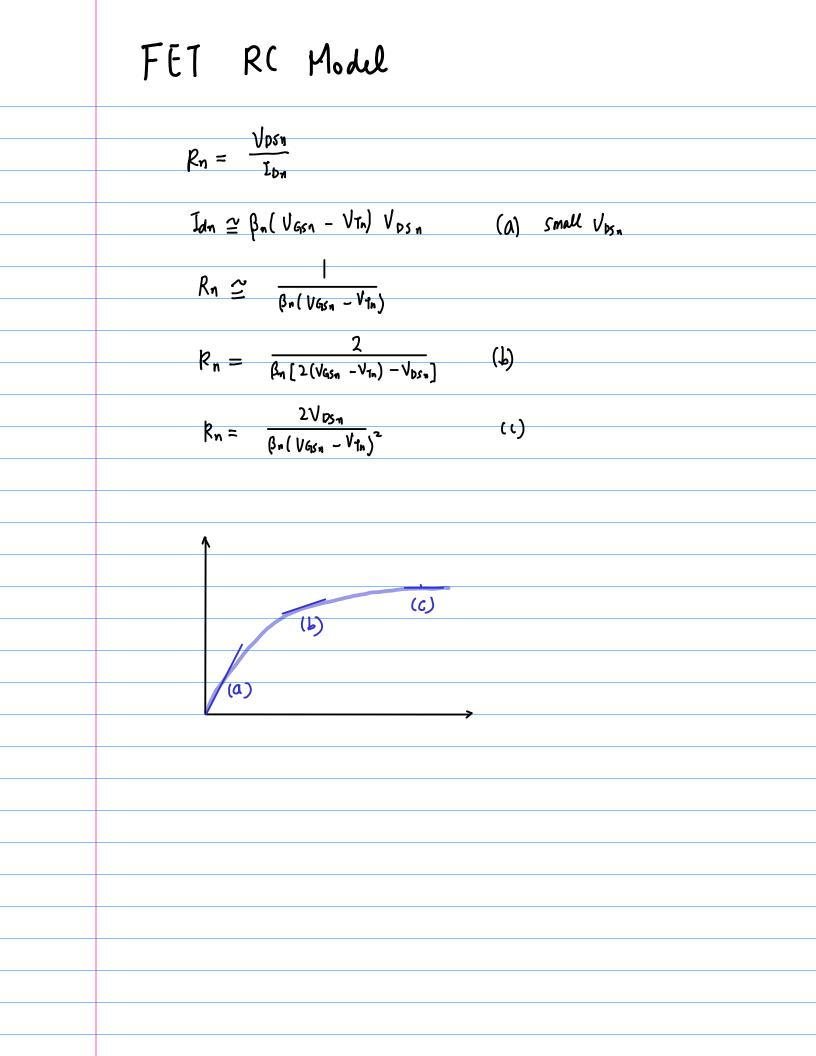


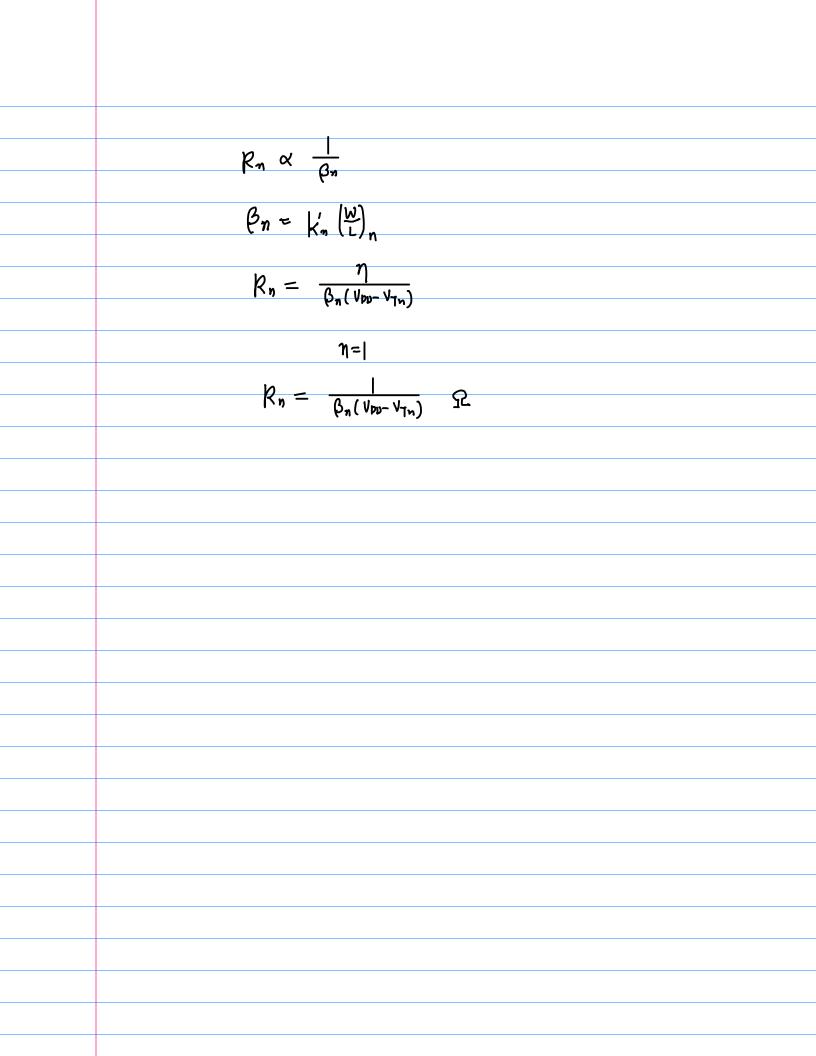












$$(a_{i} = (a_{i} \land A_{i})$$

$$= (a_{i} \lor W')$$

$$(a_{i} = (a_{i} \lor W')$$

$$(a_{i} = C_{i} \land W)$$

$$(a_{i} = (a_{i} \lor W)$$

$$(a_{i} = (a_{i} \lor W)$$

$$(a_{i} = (a_{i} \lor W)$$

$$(a_{i} = C_{i} \lor W)$$

$$(a_{i} = C_{i}$$

$$C_{\eta} = C_{\mu\nu} + C_{\mu\nu} B_{\mu\nu}$$

$$= C_{\mu} A_{\mu\nu} + C_{\mu\nu} B_{\mu\nu}$$

$$C_{\eta} = \frac{C_{\mu} A_{\mu\nu}}{(1+\frac{\nu}{\mu})^{\nu}} + \frac{C_{\mu\nu} B_{\mu\nu}}{(1+\frac{\nu}{\mu})^{\nu}}$$

$$C_{\mu} = C_{\mu\mu} + C_{\mu\mu}$$

$$C_{\mu} = C_{\mu\nu} + C_{\mu\mu}$$

PFET Characteristics

$$C_{\sigma x} = \frac{\mathcal{E}_{\sigma x}}{t_{\sigma x}}$$

$$I_{Dp} = \frac{\beta_{T}}{2} \left( \sqrt{s_{\delta p}} - \sqrt{\gamma_{p}} \right)^{2}$$

$$\beta_{P} = k_{P}' \left( \frac{W}{L} \right)_{P}$$

$$k_{P}' = \frac{\beta_{P}}{P} C_{\sigma x}$$

$$r = \frac{\beta_{P}}{\beta_{P}} = 2 - 3$$

$$\beta_{n} = k_{n}' \left( \frac{W}{L} \right)_{n}$$

$$\beta_{P} = k_{P}' \left( \frac{W}{L} \right)_{P}$$

$$\sqrt{s_{\delta t}} = \sqrt{s_{\delta p}} - \sqrt{\gamma_{p}}$$

$$I_{Dp} = \frac{\beta_{P}}{2} \left[ 2\sqrt{s_{\delta p}} - \sqrt{\gamma_{p}} \right]$$

$$I_{Dp} = \frac{\beta_{P}}{2} \left[ \sqrt{s_{\delta p}} - \sqrt{\gamma_{p}} \right]^{2}$$

$$\beta_{P} = \frac{1}{\beta_{P} (\sqrt{p_{P}} - \sqrt{\gamma_{p}})}$$

$$R_{P} \propto \frac{1}{\beta_{P}} = \frac{1}{k_{P}' (\frac{W}{L})_{P}}$$

$$C_{\delta p} = C_{\sigma x} \left( \frac{W}{L} \right)_{P}$$

$$C_{a_{u}} = \frac{1}{2} C_{a_{p}} = C_{a_{p}}$$

$$C_{p} = C_{j} A_{bet} + C_{jsu} P$$

Fall Time Calculation  

$$i = -C_{out} \frac{d V_{mt}}{dt} = \frac{V_{mt}}{R_{\eta}}$$

$$V_{out}(t) = V_{pp} e^{-t/T_{\eta}}$$

$$T_{\eta} = R_{\eta} C_{out}$$

$$t = T_{\eta} L_{\eta} \left(\frac{V_{pp}}{V_{out}}\right)$$

$$T_{f} = t_{g} - t_{x} = T_{\eta} l_{\eta} \left(\frac{V_{pp}}{R_{\eta} V_{pp}}\right) - T_{\eta} L_{\eta} \left(\frac{V_{pp}}{e_{\eta} V_{pp}}\right)$$

$$= T_{\eta} L_{\eta} (4)$$

$$t_{pL} = t_{f} \cong 2.2T_{\eta}$$

\_\_\_\_\_

\_\_\_\_\_

\_\_\_\_\_

Rise Time Calculation  

$$i = -C_{bbt} \frac{dV_{bct}}{dt} = \frac{U_{00} - V_{aut}}{R_p}$$

$$V_{0at}(t) = V_{pp} [1 - e^{-t/T_p}]$$

$$T_p = R_p C_{aut}$$

$$t = \tau_p L_n \left(\frac{V_{0p}}{V_{aut}}\right)$$

$$t_f = t_p - t_u = \tau_p L_n \left(\frac{V_{0p}}{A_1 V_{uv}}\right) - \tau_n L_n \left(\frac{V_{0p}}{a_1 V_{uv}}\right)$$

$$= \tau_p L_n (9)$$

$$t_{ut} = t_r \approx 2.2 \tau_p$$

Propagation Delay  $t_p = \frac{(t_{pf} + t_{pr})}{2}$  $t_{pf} = \ln(2) \cdot \tau_n$  $t_{pr} = ln(2) \cdot \tau_p$ tp ≅ 0.35 (Tn + Tp)

$$C_{out} = C_{FET} + C_{L}$$

$$T_{r} = \sum 2 R_{p} (C_{FT} + C_{L})$$

$$T_{r} = \sum 2 R_{n} (C_{FT} + C_{L})$$

$$T_{r} = t_{ro} + \alpha_{p} C_{L}$$

$$T_{r} = t_{ro} + \alpha_{n} C_{L}$$

$$C_{L} = 0 \Rightarrow T_{r} = t_{ro} \cong 2.1 R_{p} C_{FET}$$

$$C_{L} = 0 \Rightarrow T_{r} = t_{ro} \cong 2.1 R_{p} C_{FET}$$

$$\alpha_{p} = 2.1 R_{p} = \frac{2.2}{\beta_{p} (V_{pp} - |V_{r_{p}}|)}$$

$$\alpha_{n} = 2.1 R_{n} = \frac{2.2}{\beta_{p} (V_{pp} - |V_{r_{p}}|)}$$

$$P_{r} = k'_{p} (\frac{12}{L})_{p}$$

$$P_{n} = k'_{n} (\frac{12}{L})_{n}$$