

Voltage & Current Sources (H.1)

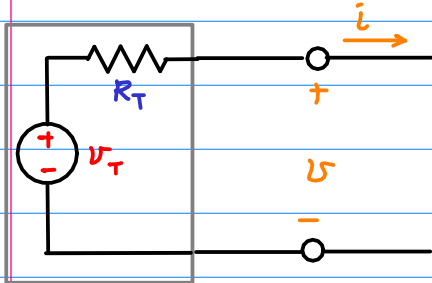
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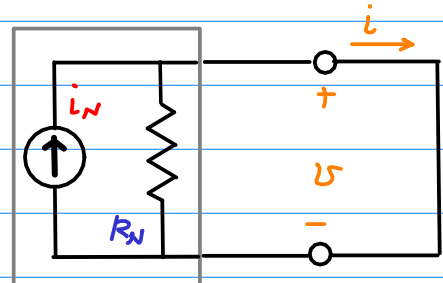
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Source Side Equation R_T

max v $\leftarrow R_L = \infty$

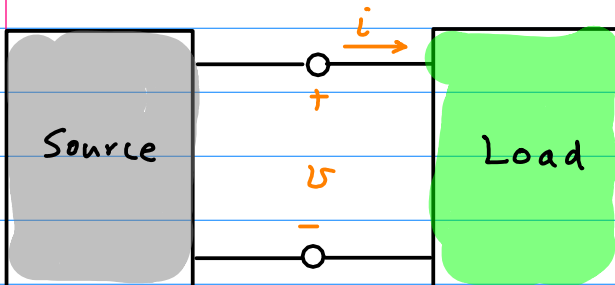


max i $\leftarrow R_L = 0$

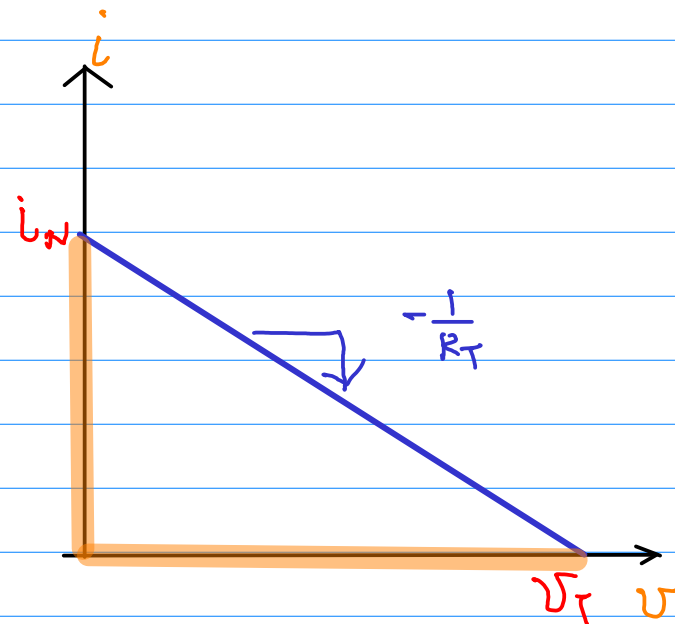


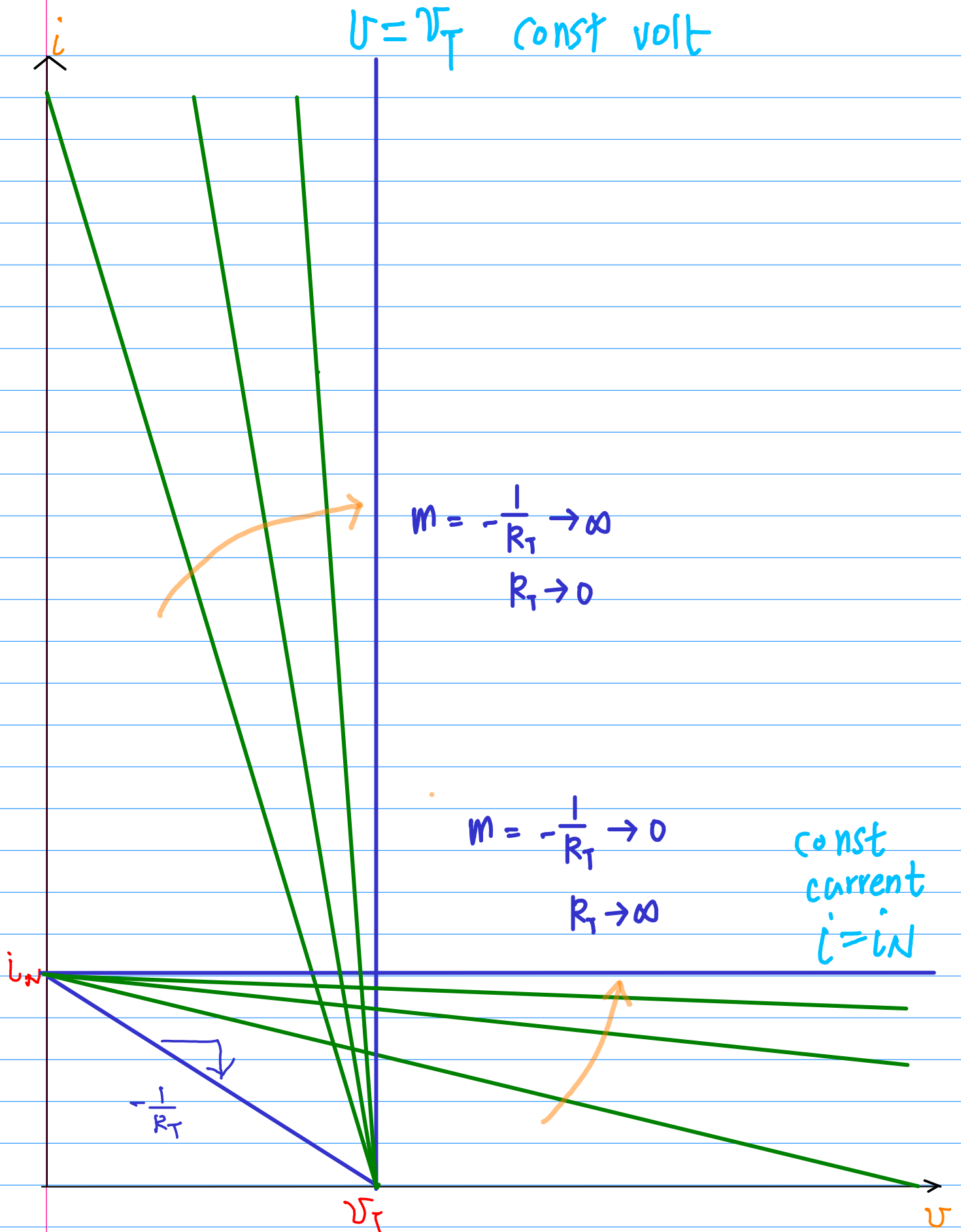
$i < i_N$
 $v < v_T$

$0 < R_L < \infty$

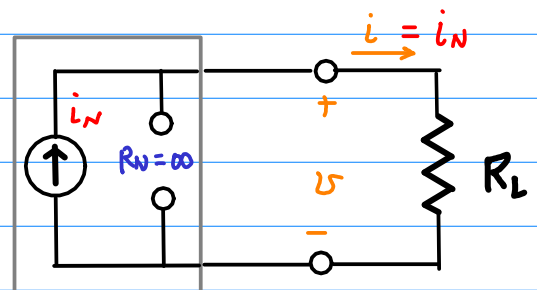
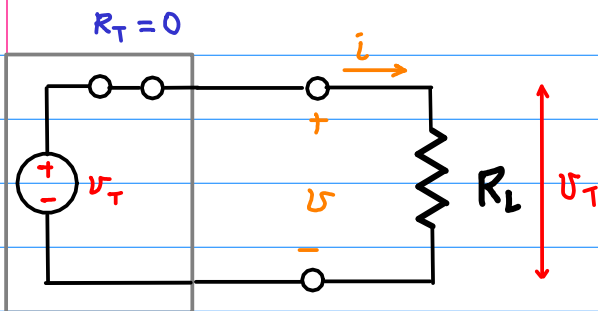
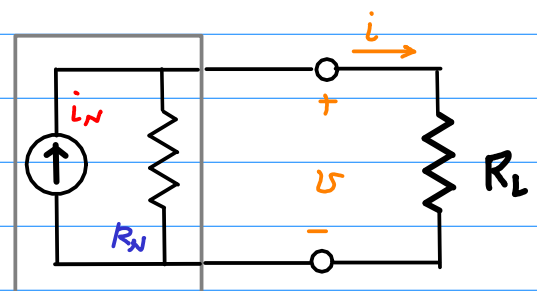
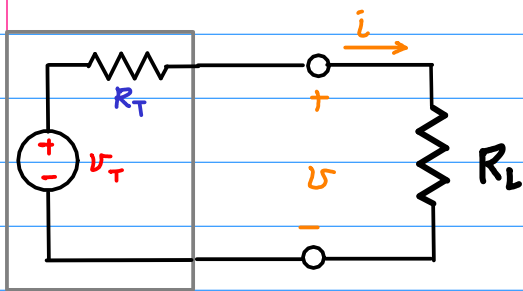


$$i = \frac{1}{R_T} (v_T - v)$$





R_N & R_T for sources

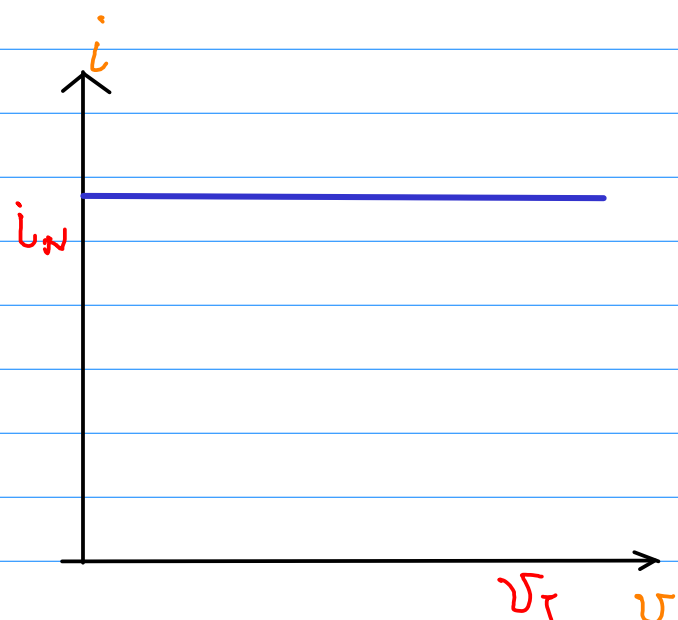
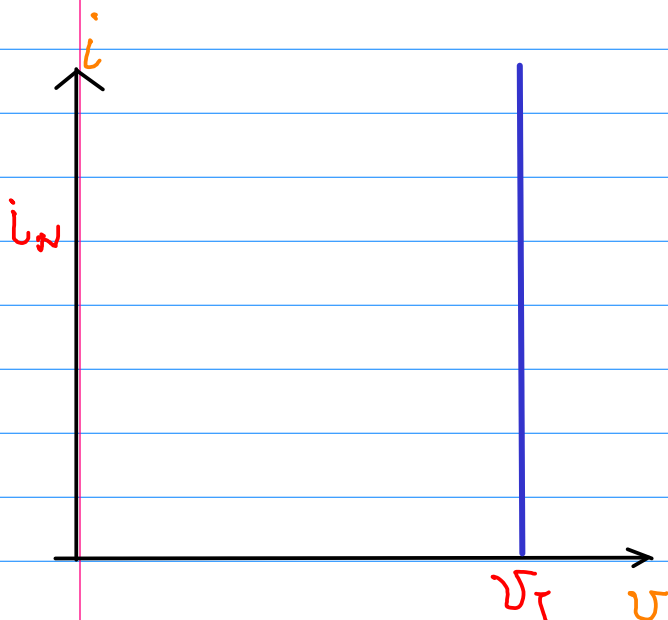


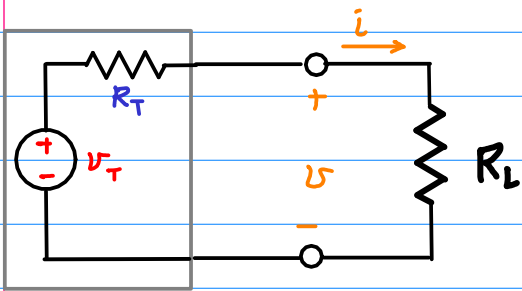
$R_T = 0 \rightarrow U = U_T$
regardless of R_L

* Ideal Voltage Source

$R_N = \infty \rightarrow i = i_T$
regardless of R_L

* Ideal Current Source





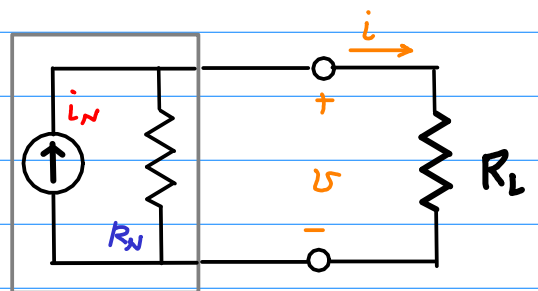
$$U = \frac{R_L}{R_T + R_L} U_T$$

$$R_T \ll R_L$$

$$U \approx \frac{R_L}{R_L} U_T = U_T$$

$$U = \frac{1}{0.01 + 1} U_T$$

$$= \frac{1}{1.01} U_T \approx 0.99 U_T$$



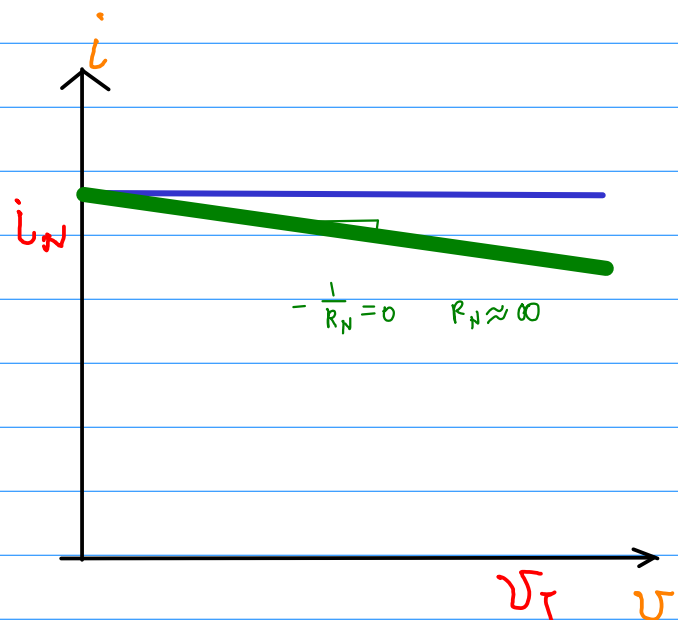
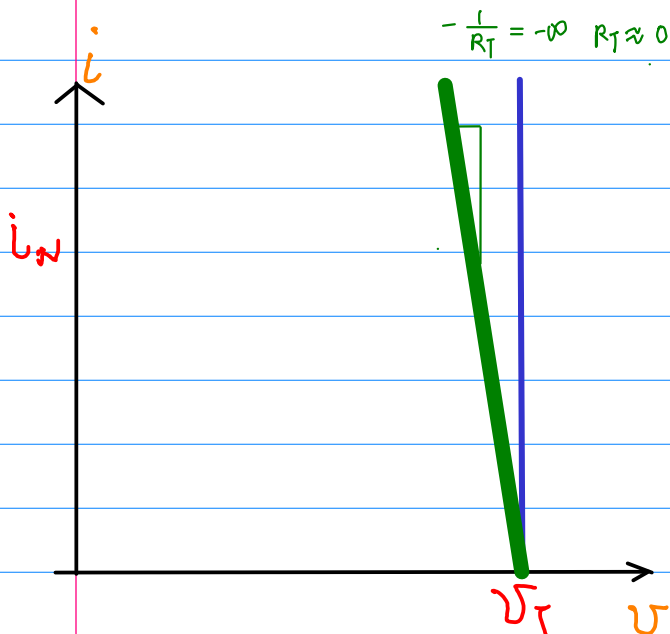
$$i = \frac{R_N}{R_N + R_L} i_N$$

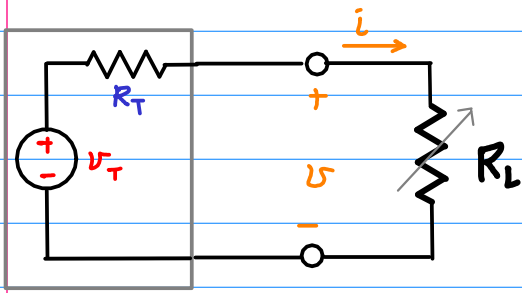
$$R_N \gg R_L$$

$$i = \frac{R_N}{R_N} i_N = i_N$$

$$U = \frac{100}{100 + 1} U_T$$

$$= \frac{100}{101} U_T \approx 0.99 U_T$$

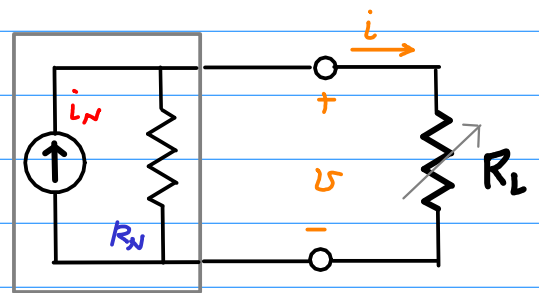




$$U = \frac{R_L}{R_T + R_L} V_T$$

$$= \frac{1}{\frac{R_T}{R_L} + 1} V_T$$

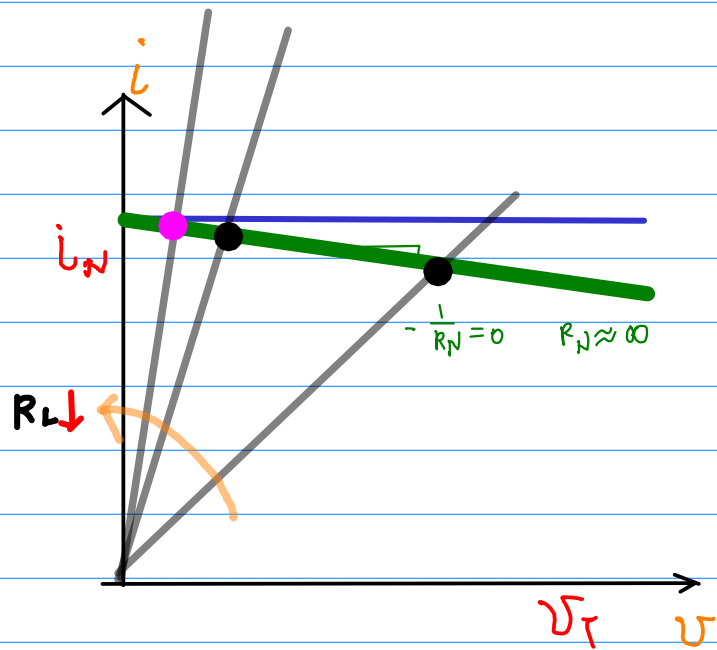
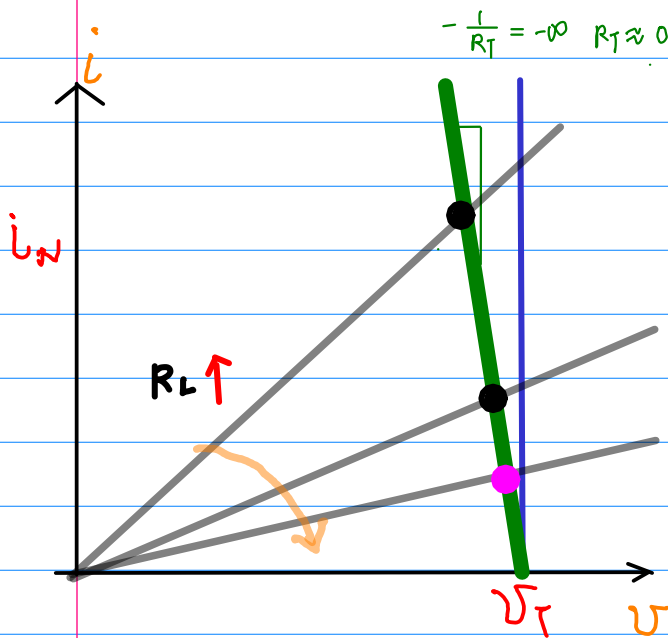
$$R_T \ll R_L$$

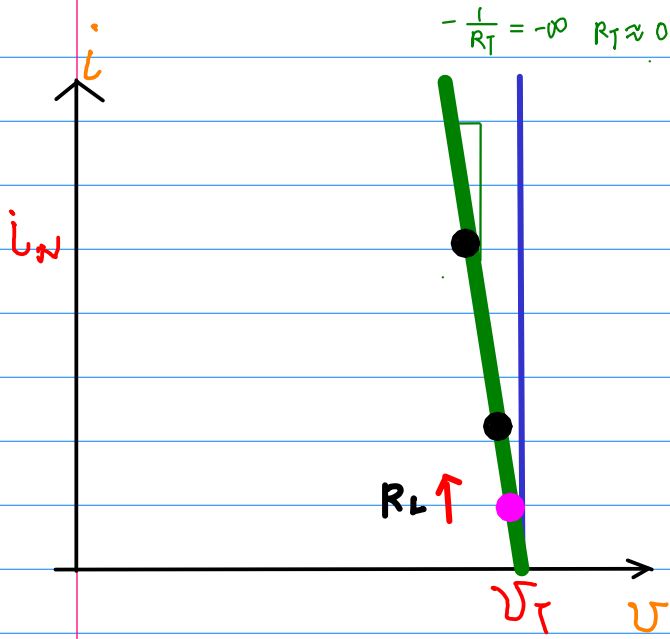


$$i = \frac{R_N}{R_N + R_L} i_N$$

$$= \frac{1}{1 + \frac{R_L}{R_N}} i_N$$

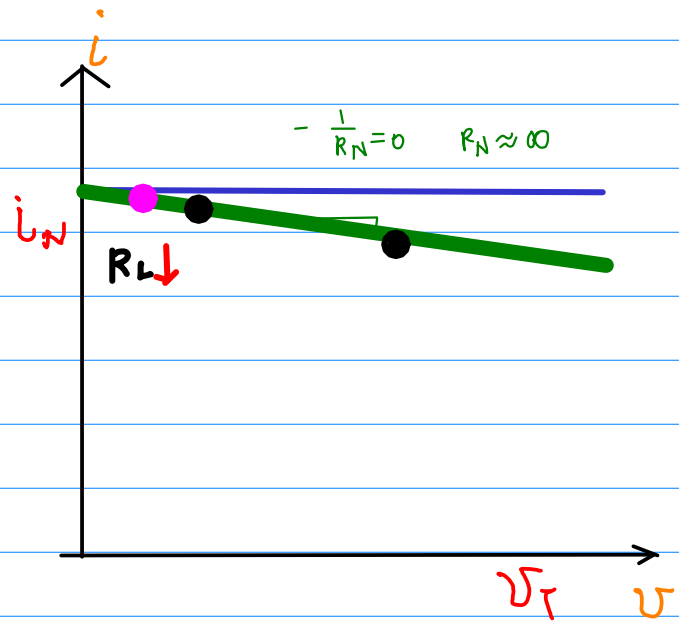
$$R_N \gg R_L$$





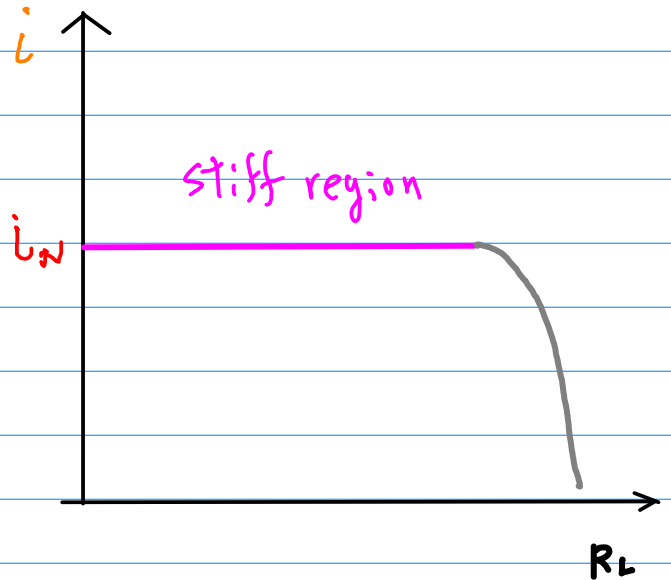
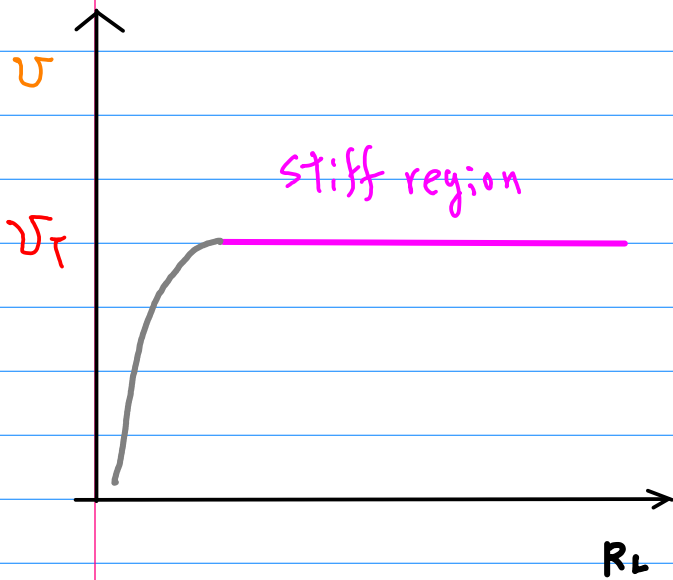
$$U = \frac{1}{\frac{R_T}{R_L} + 1} U_T$$

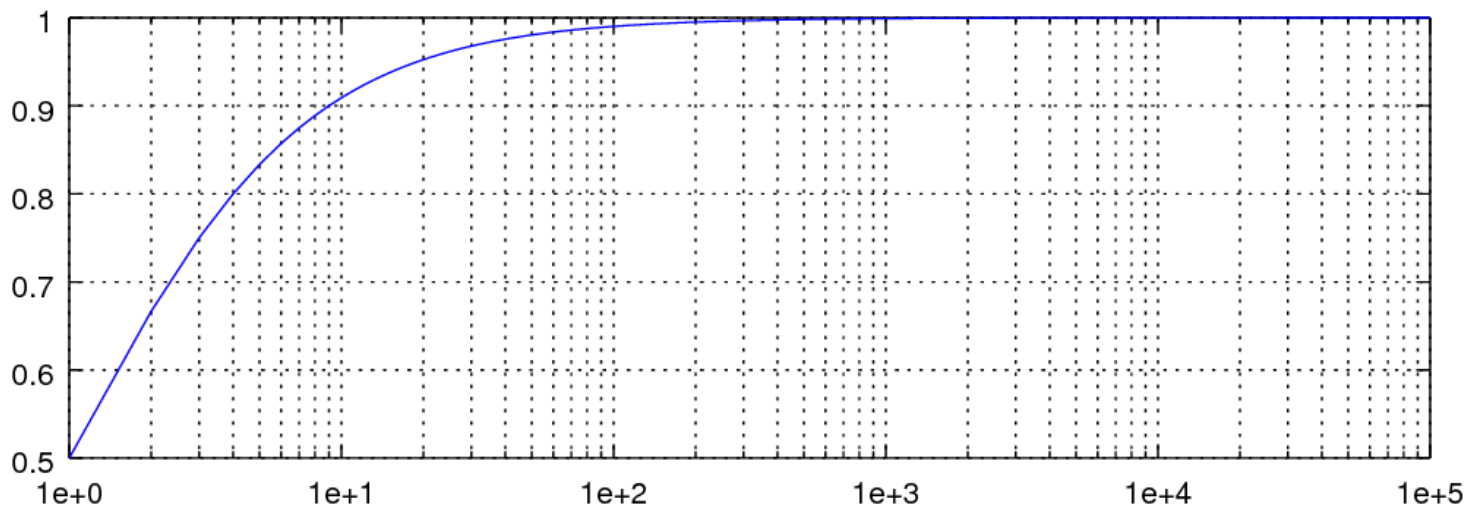
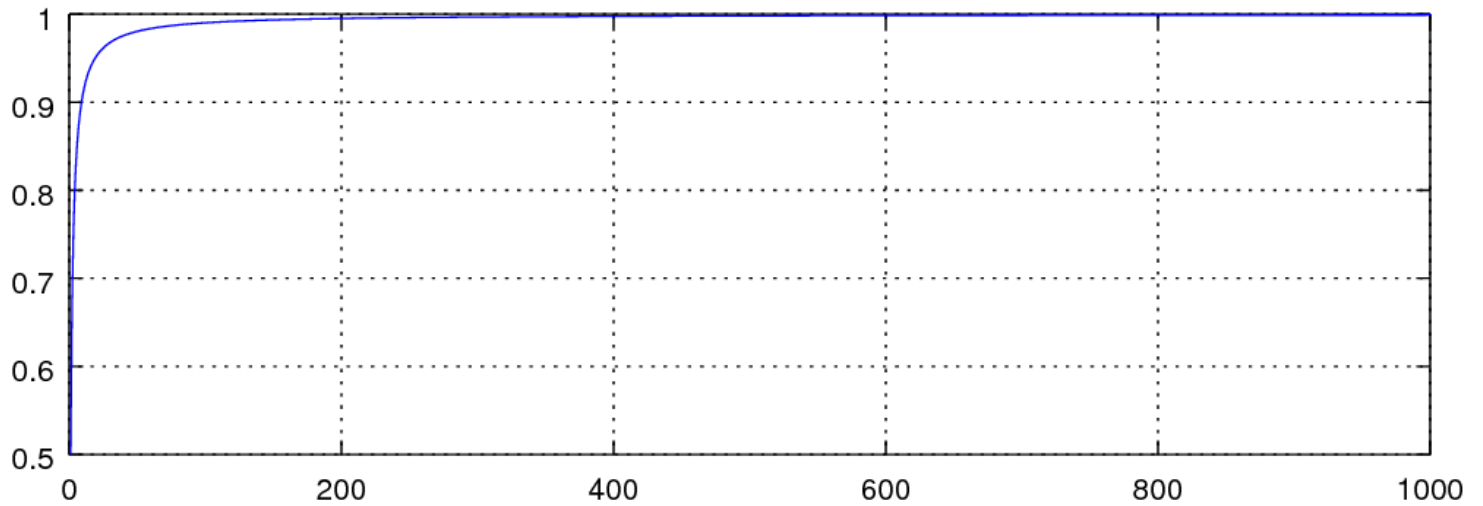
$$R_T \ll R_L$$



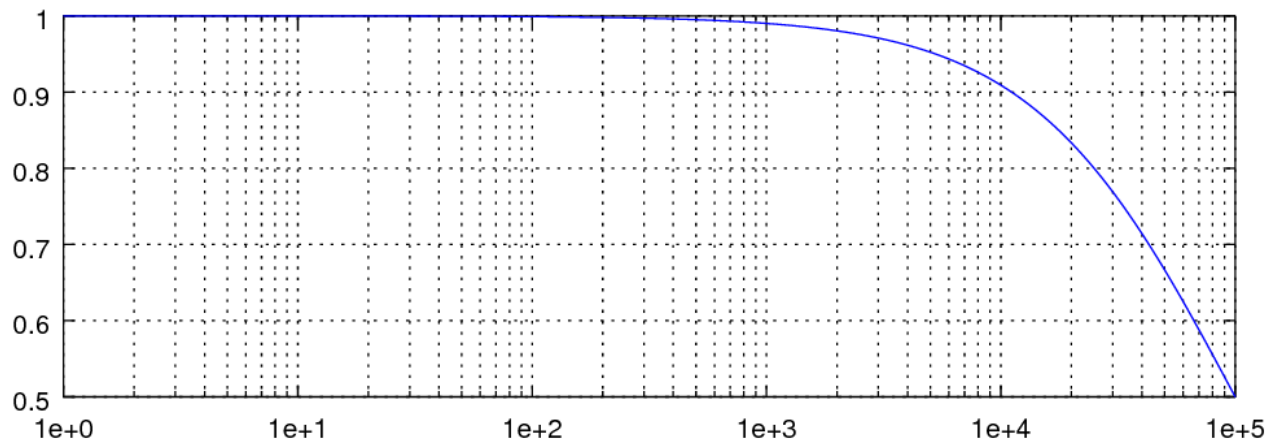
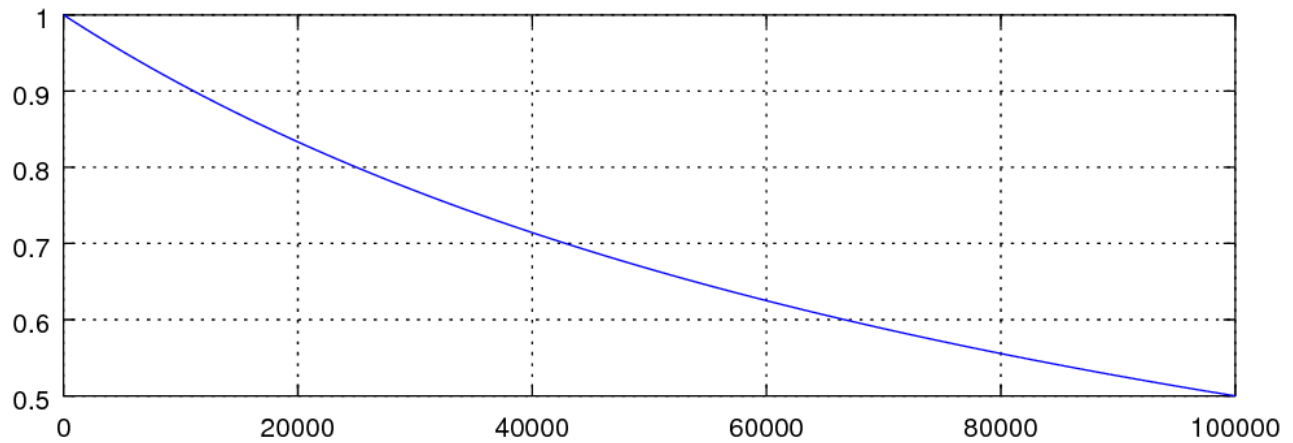
$$i = \frac{1}{1 + \frac{R_L}{R_N}} i_N$$

$$R_N \gg R_L$$



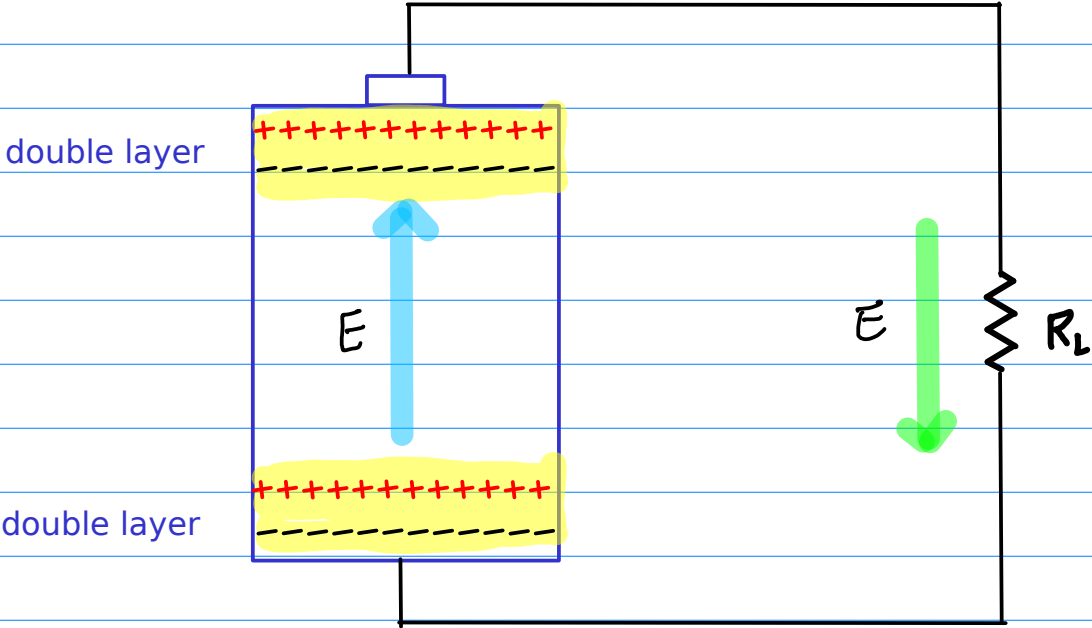
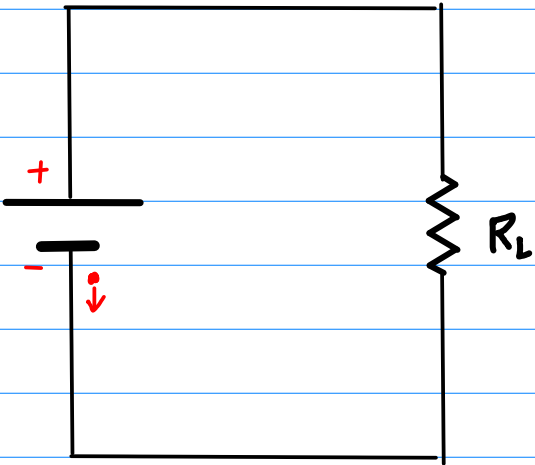


```
>> k = 1 : 100000;  
>> v = k ./ (k+1);  
>> subplot(2, 1, 1)  
>> plot(k,v)  
>> axis([0 1000]);  
>> grid  
>> subplot(2, 1, 2);  
>> semilogx(k, v);  
>> grid
```

```
>> subplot(2, 1, 1);
>> k = 1 : 10000;
>> i = 100000./(100000 +k);
>> plot(k, i);
>> k = 1 : 10: 100000;
>> i = 100000./(100000 +k);
>> plot(k, i);
>> subplot(2, 1, 2);
>> semilogx(k, i);
>> grid
>> subplot(2, 1, 1);
>> grid
```

Electric field inside a battery



Passive Sign Convention

electric power flowing out of an active component
into an pass component

active component - battery - negative power dissipation
passive component - resistor - positive power dissipation

the direction of V and I

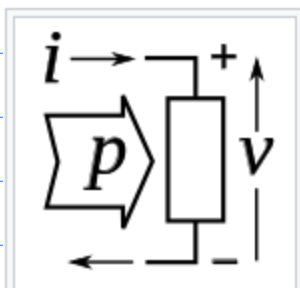


Illustration of the "reference directions" of the current (i), voltage (v), and power (p) variables used in the passive sign convention. If positive current is defined as flowing into the terminal which is defined to have positive voltage, then positive power represents electric power flowing into the device (*big arrow*).

positive current i flowing into the terminal with $+v$

positive power flowing into the device (passive component)

i : defined as entering the device
through the terminal which has $+v$

the power $p = iv$ $r = v/i$

i : defined as entering the device
through the terminal which has $-v$

the power $p = -iv$ $r = -v/i$

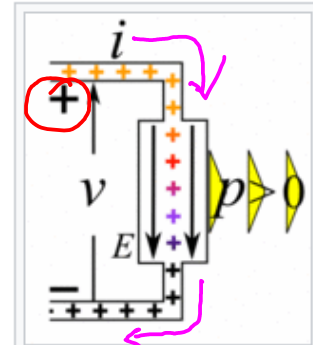
passive components (loads) : $p > 0$, $r > 0$

active components (sources) : $p < 0$, $r < 0$

Active and passive components [edit]

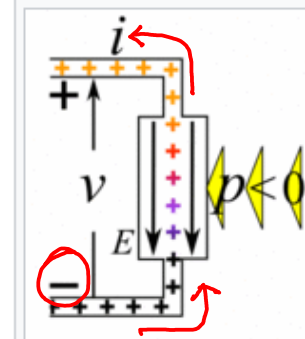
In electrical engineering, **power** represents the rate of electrical energy flowing into or out of a given component or **control volume**. Power is a **signed quantity**; negative power just represents power flowing in the opposite direction from positive power. From the standpoint of power flow, **electrical components** in a circuit can be divided into two types:^[2]

- In a **load** or **passive** component, such as a **light bulb**, **resistor**, or **electric motor**, **electric current** (flow of positive charges) moves through the device under the influence of the **electric field E** in the direction of **lower electric potential**, from the **positive terminal** to the **negative**. So work is done *by* the charges on the component; potential energy flows out of the charges; and electric power flows from the circuit into the component, where it is converted to some other form of energy such as heat or mechanical work.
- In a **source** or **active** component, such as a **battery** or **electric generator**, current is forced to move through the device **in the direction of greater electric potential**, from the **negative** to the **positive voltage terminal**. This increases the potential energy of the electric charges, so electric power flows out of the component into the circuit. **Work** must be done *on* the moving charges by some source of energy in the component, to make them move in this direction against the opposing force of the **electric field E** .



Load (passive component)

dissipation
 $p > 0$



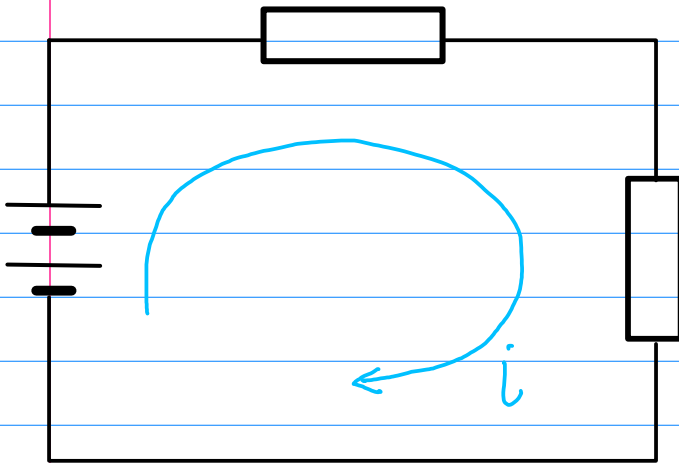
Power source (active component)

generation
 $p < 0$

· Some components can be either a source or a load, depending on the voltage or current through them. For example, a [rechargeable battery](#) acts as a source when it is used to produce power, but as a load when it is being recharged.

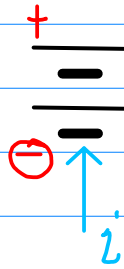
Since it can flow in either direction, there are two possible ways to define electric power; two possible *reference directions*: either power flowing into the circuit, or power flowing out of the circuit, can be defined as positive.^[2] Whichever is defined as positive, the other will be negative. The passive sign convention arbitrarily defines power flowing out of the circuit (into the component) as positive,^[2] so passive components have "positive" power flow.

In an AC ([alternating current](#)) circuit the current and voltage switch direction periodically, but the definitions above still apply; in passive components the current flows from the positive terminal to the negative, while in active components it flows the other direction.

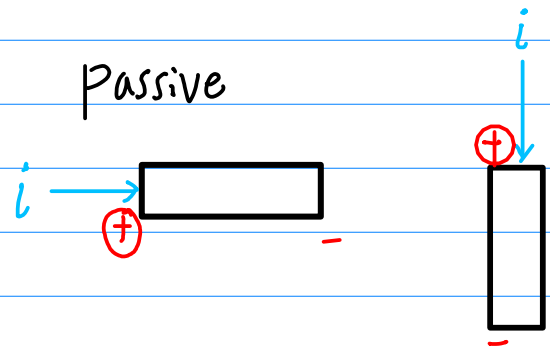


assumed i

Active

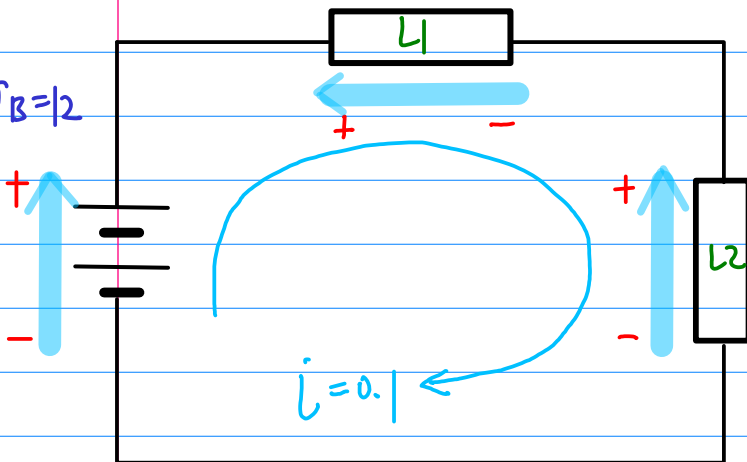


Passive



$$v_1 = 8$$

$$v_B = 12$$



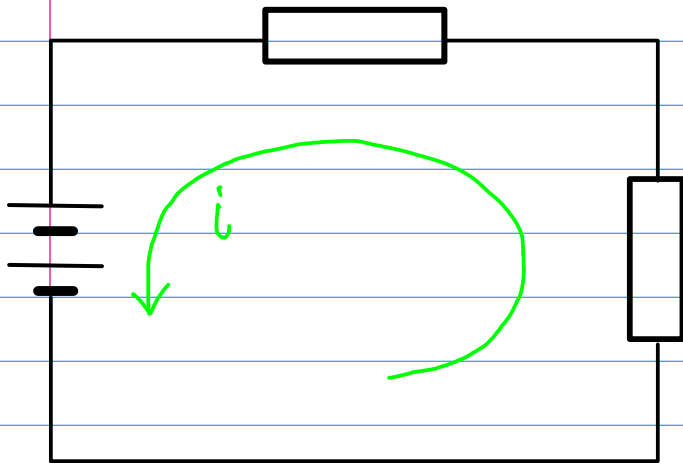
$$P_1 = i \cdot v_1 = 0.1 \times 8 = 0.8$$

$$P_2 = i \cdot v_2 = 0.1 \times 4 = 0.4$$

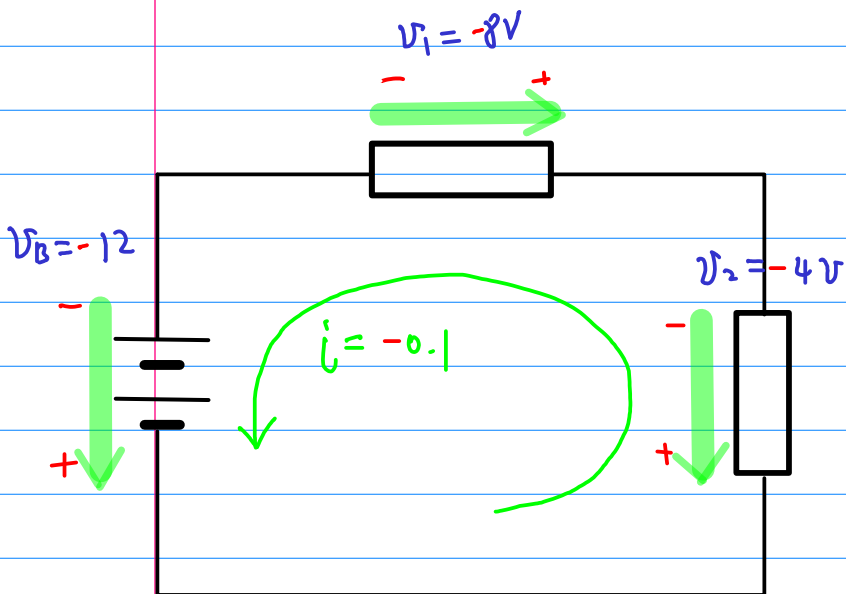
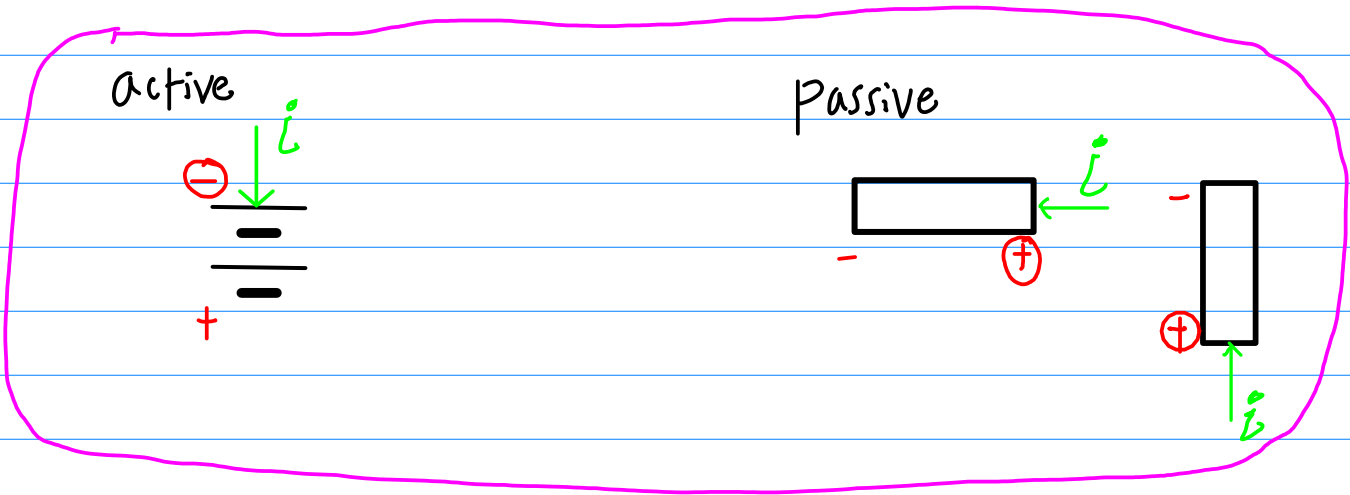
dissipated

$$v_2 = 4 \quad P_B = i \cdot (-v_B) = 0.1 \times (-12) = -1.2$$

generated



assumed i



$$P_1 = i \cdot v_1 = (-0.1) \times (-8) = 0.8$$

$$P_2 = i \cdot v_2 = (-0.1) \times (-4) = 0.4$$

dissipated

$$P_B = i \cdot (-v_B) = (-0.1) \times (+12) = -1.2$$

generated