# R Functions for Probability Distributions 

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2018-03-22 Thr

## Outline

(1) R Functions for Probability Distributions

- Based on
- R Functions
- Signal with noise


## Based on

## "Probability with R: An Introduction with Computer Science Applications" Jane Horgan

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## R Functions

|  | cdf | i cdf | pdf | rv |
| :--- | :--- | :--- | :--- | :--- |
|  | probability | quantile | density | random |
| Beta | pbeta | qbeta | dbeta | rbeta |
| Binomial | pbinom | qbinom | dbinom | rbinom |
| Cauchy | pcauchy | qcauchy | dcauchy | rcauchy |
| Chi-Square | pchisq | qchisq | dchisq | rchisq |
| Exponential | pexp | qexp | dexp | rexp |
| Gamma | pgamma | qgamma | dgamma | rgamma |
| Geometric | pgeom | qgeom | dgeom | rgeom |
| Hypergeometric | phyper | qhyper | dhyper | rhyper |
| Log Normal | plnorm | qlnorm | dlnorm | rlnorm |
| Negative Binomial | pnbinom | qnbinom | dnbinom | rnbinom |
| Normal | pnorm | qnorm | dnorm | rnorm |
| Poisson | ppois | qpois | dpois | rpois |
| Uniform | punif | qunif | dunif | runif |

## Finite Populations

```
sample(1:100)
    # a random permutation of the numbers 1 to 100
sample(x,10,replace=F)
    # a random sample of size N=10
    # drawn from the elements of x without replacement
sample(1:6,10,replace=T,prob=c(1/7,1/7,1/7,1/7,1/7, 2/7))
    # a random sample of size 10 from the digits 1 to 6
    # with unequal probabilities of selection
    # eg. a loaded die
```

http://people.reed.edu/~jones/141/sim1.html

## Bernoulli(p) Trials

- Bernoulli trials are sequences of independent dichotomous trials
- each with probability $p$ of success.
- The sample space consists of the two possible outcomes.
- For example, the results of 10 successive (independent) tosses of a fair coin would constitute 10 Bernoulli(1/2) trials. In R:
- $\operatorname{rbinom}(\mathrm{N}, 1, \mathrm{p})$
- generates a sequence of N trials, each with probability p of success.
http://people.reed.edu/~jones/141/sim1.html


## Binomial $(n, p)$ Trials

- this arises from a sequence of $n$ independent Bernoulli trials
- each with probability $p$ of success.
- Since the number of successes in $n$ trials can range from 0 to $n$
- the sample space is just the integers $0,1,2, \ldots n$.
- the number of heads that occur in 20 independent tosses of a fair coin has a Binomial $(20, .5)$ distribution.
- rbinom( $\mathrm{N}, \mathrm{n}, \mathrm{p}$ )
- generates N independent samples from a binomial( $\mathrm{n}, \mathrm{p}$ ) distribution.
http://people.reed.edu/~jones/141/sim1.html


## Geometric(p) Trials (1)

- The geometric distribution models the number of failures
- until the first success in a sequence of independent Bernoulli trials,
- each with probability $p$ of success.
- the geometric is sometimes defined to be the number of trials including the first success.
- R uses the number of failures.
http://people.reed.edu/~jones/141/sim1.html


## Geometric(p) Trials (2)

- Since we might have to repeat the experiment arbitrarily many times before the first success,
- the sample space is the non-negative integers: $0,1,2, \ldots$
- if we roll a fair die, and count the number of rolls before the first " 6 "appears, we have a geometric distribution with $p=1 / 6$.
- In other words, if the sequence of rolls yields $\{4,2,4,5,6, \ldots\}$, then we had 4 rolls before the first 6 .
- rgeom(N,p)
- generates N geometric $(\mathrm{p})$ counts.
http://people.reed.edu/~jones/141/sim1.html


## Poisson(m) Trials (1)

- The Poisson distibution arises as an approximation to the binomial( $n, p$ ) for large $n$ and small $p$,
- hence the common reference to modelling "rare events".
- the sample space for the Poisson distribution is the non-negative integers
- the number of phone calls arriving at a switchboard in a given time interval is likely to be approximately Poisson.
- The parameter $m$ is the mean count.
- rpois(N,m)
- generates N values from a poisson( m ) distribution.
http://people.reed.edu/~jones/141/sim1.html


## Poisson(m) Trials (2)

- To compare the poisson distribution to a similar binomial distribution, set $m=n * p$.
- You can either directly compare the probabilities for each possible outcome,
- or you could plot the cumulative distribution functions against each other.
- The sample space for a binomial( $\mathrm{n}, \mathrm{p}$ ) distribution is $0: \mathrm{n}$;
- let's try it for a binomial(20,.1) and the poisson(2) distributions:

```
k <- 0:20
bin <- dbinom(k,20,.1)
pois <- dpois(k,2)
plot(k,bin)
points(k,pois,pch="+")
```

http://people.reed.edu/~jones/141/sim1.html

## Poisson(m) Trials (3)

- Analogous to a quantile-quantile plot, we can plot the cumulative relative frequencies of the two distributions against each other:
- If the two distributions agreed exactly, the plotted points would lie on a straight line.
- The abline function adds a line with the given intercept and slope, in this case 0 and 1 respectively.

```
k <- 0:20
bin <- pbinom(k,20,.1)
pois <- ppois(k,2)
plot(bin,pois)
abline(0,1)
```

http://people.reed.edu/~jones/141/sim1.html

## Normal distribution noise

```
x <- seq(0, 2*pi, 0.01)
y <- sin(x)
noise <- rnorm(length(x), 0.0, 0.1)
plot(x, y+noise, "l")
```



## Normal distribution noise



```
x <- seq(0, 2*pi, 0.01)
y<- sin(x)
num <- 100
noise <- rep(0, length(x))
for (i in 1:num) {
    set.seed(i)
        noise <- noise +
        rnorm(length(x), 0.0, 0.1)
}
noise <- noise / num
plot(x, y+noise, "l")
```


## Uniform distribution noise

```
x <- seq(0, 2*pi, 0.01)
y <- sin(x)
noise <- runif(length(x), -0.1, +0.1)
plot(x, y+noise, "l")
```



