

# Haskell Overview III (3A)

---

Copyright (c) 2016 Young W. Lim.

Permission is granted to copy, distribute and/or modify this document under the terms of the GNU Free Documentation License, Version 1.2 or any later version published by the Free Software Foundation; with no Invariant Sections, no Front-Cover Texts, and no Back-Cover Texts. A copy of the license is included in the section entitled "GNU Free Documentation License".

Please send corrections (or suggestions) to [youngwlim@hotmail.com](mailto:youngwlim@hotmail.com).

This document was produced by using OpenOffice.

# Based on

---

Haskell Tutorial, Medak & Navratil

<ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>

Yet Another Haskell Tutorial, Daume

<https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>

# Type Inference

---

```
Prelude> 7 :: Int
```

```
7
```

```
Prelude> 7 :: Double
```

```
7.0
```

usually don't have to declare types

(type inference)

to declare types, use `::` to do it.

[https://wiki.haskell.org/Learn\\_Haskell\\_in\\_10\\_minutes](https://wiki.haskell.org/Learn_Haskell_in_10_minutes)

# Type Information Display

```
Prelude> :t False
```

```
False :: Bool
```

```
Prelude> :t 'A'
```

```
'A' :: Char
```

```
Prelude> :t "Hello, world"
```

```
"Hello, world" :: [Char]
```

`:t` Print type information

[https://wiki.haskell.org/Learn\\_Haskell\\_in\\_10\\_minutes](https://wiki.haskell.org/Learn_Haskell_in_10_minutes)

# Type Classes

```
Prelude> :t 42
```

```
42 :: (Num t) => t
```

```
Prelude> :t 42.0
```

```
42.0 :: (Fractional t) => t
```

```
Prelude> :t gcd 15 20
```

```
gcd 15 20 :: (Integral t) => t
```

42 can be used as any **numeric** type

42.0 can be any **fractional** type

Gcd 15 20 can be any **integral** type

[https://wiki.haskell.org/Learn\\_Haskell\\_in\\_10\\_minutes](https://wiki.haskell.org/Learn_Haskell_in_10_minutes)

# Type Class Constraint

```
Prelude> :t 42
```

```
42 :: (Num t) => t
```

```
Prelude> :t 42.0
```

```
42.0 :: (Fractional t) => t
```

```
Prelude> :t gcd 15 20
```

```
gcd 15 20 :: (Integral t) => t
```

**type  $t$**  belongs to **Num type class**

**type  $t$**  belongs to **Fractional type class**

**type  $t$**  belongs to **Integral type class**

## class constraint

**(Num t) =>**

**(Fractional t) =>**

**(Integral t) =>**

the type  $t$  is *constrained* by the context  
(Num t), (Fractional t), (Integral t)

the **types** of  $t$  must be **Num type class**

the **types** of  $t$  must be **Fractional type class**

the **types** of  $t$  must be **Integral type class**

[https://wiki.haskell.org/Learn\\_Haskell\\_in\\_10\\_minutes](https://wiki.haskell.org/Learn_Haskell_in_10_minutes)

# Instances

## Instances of **Num** type class

### Instances of **Integral** type class

**Int**

an integer with at least *30 bits* of precision.

**Integer**

an integer with *unlimited* precision.

**Float**

a *single* precision floating point number.

**Double**

a *double* precision floating point number.

**Rational**

a *fraction* type, with no rounding error.

### Instances of **Float** type class

**Instances are used as types**

[https://wiki.haskell.org/Learn\\_Haskell\\_in\\_10\\_minutes](https://wiki.haskell.org/Learn_Haskell_in_10_minutes)



# Type Class

a **type class** definition:

specifying  
a set of  
**functions** or **constants**,  
together with their respective types,

Like the Interface in Java

that must be implemented  
for **every type** that *should belong* to the **type class**

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Type Class Definition

the **type class** `Eq` is intended to *include* those **types** that implement **equality** (`==`), (`/=`) functions

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
```

a **type** `a` has an **instance** of the **class** `Eq` if there is an (**overloaded**) operation `==` and `/=` defined.

a **type** `a` *belongs* to the **type class** `Eq` if `(==)` and `(/=)` functions are defined

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Instance of a Class

type class **Eq**

*parameterized type* **a**

```
class Eq a where
  (==) :: a -> a -> Bool
  (/=) :: a -> a -> Bool
```

a **type** **a** can be an **instance** of the **class** **Eq** if there is an (**overloaded**) operation **==** and **/=** defined.

The **type** **Integer** is an **instance** of the **class** **Eq**, whose **method** **==** and **/=** are defined

The **type** **Float** is an **instance** of the **class** **Eq**, whose **method** **==** and **/=** are defined

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Instance Declaration

```
class Eq a where  
  (==) :: a -> a -> Bool
```

type class	type
Eq	a

```
instance Eq Integer where
```

```
x == y = x `integerEq` y
```

type class	instance
Eq	<b>Integer</b>
Eq	<b>Float</b>

```
instance Eq Float where
```

```
x == y = x `floatEq` y
```

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Default Method

```
class Eq a where
  (==), (/=)    :: a -> a -> Bool
  x /= y       = not (x == y)
```

If a method is not defined in an instance declaration, then the default implementation defined in the class declaration, if it exists, is used instead.

overloaded method definition

The default definition can be overloaded in an instance declaration

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Class Constraint

```
elem :: a -> [a] -> Bool
```

the function `elem` has  
the type `a -> [a] -> Bool`

```
elem :: (Eq a) => a -> [a] -> Bool
```

the type `a` is *constrained*  
by the context `(Eq a)`

the **types** of `a` must *belong*  
to the **Eq type class**

`=>` : called as a '**class constraint**'

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

# Class Constraint Example

`elem` function definition

`elem` function determines whether an element is in a list

```
elem :: (Eq a) => a -> [a] -> Bool
```

```
elem y [] = False
```

```
elem y (x:xs) = (x == y) || elem y xs
```

[https://en.wikipedia.org/wiki/Type\\_class](https://en.wikipedia.org/wiki/Type_class)

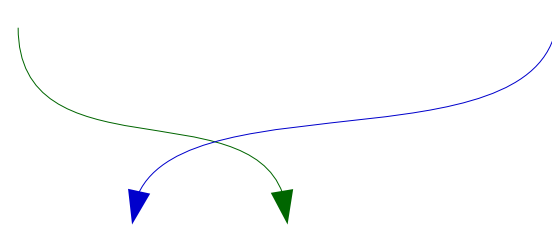
# Enumerated Data Types

Type Constructor

Data Constructor

```
data Bool = True | False
```

The type being defined here is **Bool**, and it has exactly two values: **True** and **False**.



True :: Bool  
False :: Bool

```
var1 :: Bool  
var1 = True  
  
var2 :: Bool  
var2 = False
```

```
data Color = Red | Green | Blue
```



Red :: Color  
Green :: Color  
Blue :: Color

```
var3 :: Color  
var3 = Red  
  
var4 :: Color  
var4 = Green  
  
var5 :: Color  
var5 = Blue
```

<https://www.haskell.org/tutorial/goodies.html>



# Type Names and Constructor Functions

A nullary constructor:  
takes no arguments

A multi-constructor

```
data Bool = True | False
```

Type Constructor

Data Constructor

**Type name** : Bool

The name of new data type

Usually it appears in the linea  
concerning type information  
( :: )

**Constructor function**

: True, False

Usually it appears in the lines  
concerning application ( = )

<https://www.haskell.org/tutorial/goodies.html>

# Data Constructor

---

Data constructors group values together and tag alternatives

Deconstructing data constructors

- What a data constructor does is holding values together
- Have to separate them in order to use them.
- pattern matching ( )

Data constructors are not types but values

<https://wiki.haskell.org/Constructor>

# Parameterized Data Type Definition

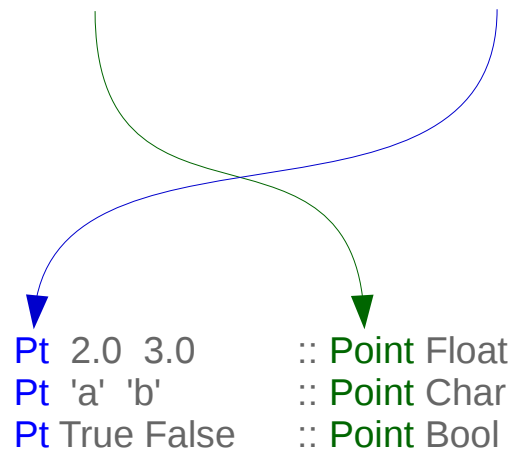
A unary constructor  
(one argument a)

A single constructor

```
data Point a = Pt a a
```

Type Constructor

Data Constructor



Pt :: a -> a -> Point a

```
v1 :: Point Float  
v1 = Pt 2.0 3.0  
  
v2 :: Point Char  
v2 = Pt 'a' 'b'  
  
v3 :: Point Bool  
v3 = Pt True False
```

<https://www.haskell.org/tutorial/goodies.html>

Data constructors group values together and tag alternatives

[https://wiki.haskell.org/GADTs\\_for\\_dummies](https://wiki.haskell.org/GADTs_for_dummies)

# Polynom Data Type (1)

**roots** :: (Float, Float, Float) -> (Float, Float)

**roots** (a,b,c) = if d < 0 then error "sorry" else (x1, x2)

where x1 = e + sqrt d / (2 \* a)

x2 = e - sqrt d / (2 \* a)

d = b \* b - 4 \* a \* c

e = - b / (2 \* a)

**real** :: (Float, Float, Float) -> Bool

**real** (a,b,c) = (b\*b - 4\*a\*c) >= 0

p1 = (1.0,2.0,1.0) :: (Float, Float, Float)

p2 = (1.0,1.0,1.0) :: (Float, Float, Float)

ps = [p1,p2]

newPs = filter **real** ps

rootsOfPs = map **roots** newPs

# Polynom Data Type (2)

```
data Polynom = Poly Float Float Float
```

**data** the keyword

**Polynom** the name of the data type

**Poly** the constructor function (:t Poly)

`Poly :: Float -> Float -> Float -> Polynom`

**Float** the three arguments to the Poly constructor

# Polynom Data Type (3)

```
data Polynom = Poly Float Float Float
```

```
roots' :: Float Float Float -> (Float, Float)
```

```
roots' a b c = ... function definition ...
```

```
roots2 :: Polynom -> (Float, Float)
```

```
roots2 (Poly a b c) = ... function definition ...
```

(Float, Float) tuple

(Poly a b c) pattern matching

```
p1, p2 :: Polynom
```

```
p1 = Poly 1.0, 2.0, 3.0
```

```
p2 = Poly 1.0, 3.0, (-5.0)
```

# Recursive Definition of Lists

data [a] = [] | a : [a]

Any type is ok but  
The type of every element in  
the list must be the same

List = [] | (a : List)

an empty  
list

[]

a list with at least  
one element

(x:xs)

<https://www.haskell.org/tutorial/goodies.html>

# List Type Definition : Parameterized & Recursive

Parameter

data

List a = L a (List a) | Empty

Bool  
Int  
Integer  
Float  
Double  
Char  
String

data

List a = L a (List a) | Empty

***Recursive Definition***



# List Type Definition : Constructors

Type Constructor    Data Constructor with two parameters

data

List a = L a (List a) | Empty

Data Constructors

Empty  
L a (List a)

L :: a -> List a -> List a

Head :    Tail :  
element   list

# List Type Definition : Examples

`data List a = L a (List a) | Empty`

`L1, L2, L3 :: List Integer` type constructor List

`L1 = Empty`

`L2 = L 1 L1`

`L3 = L 5 L2`

`L4 = L 1.5 Empty :: List Double` type constructor List

data constructor  
`L a (List a)`

# Tree Data Type : Recursive Definition

```
data Tree a = Leaf a | Branch (Tree a) (Tree a)
```

*Recursive Definition*

**(Tree a) pattern matching**

<https://www.haskell.org/tutorial/goodies.html>

# Tree Data Type : Constructors

data `Tree a` = `Leaf a` | `Branch (Tree a) (Tree a)`

Type Constructor : `Tree a`

Data Constructor 1: `Leaf a`

`Leaf :: a -> Tree a`

Data Constructor 2: `Branch (Tree a) (Tree a)`

`Branch :: Tree a -> Tree a -> Tree a`

`Branch :: (Tree a) -> (Tree a) -> Tree a`

<https://www.haskell.org/tutorial/goodies.html>

# Tree Data Type : Constructors

```
data Tree a = Leaf a | Branch (Tree a) (Tree a)
```

```
fringe      :: Tree a -> [a]
```

```
fringe (Leaf x) = [x]
```

```
fringe (Branch left right) = fringe left ++ fringe right
```

<https://www.haskell.org/tutorial/goodies.html>

# Recursive Data Type Example (1)

```
data Bus = Start | Next (Bus) deriving Show
```

```
myBusA = Start
```

```
myBusB = Next (Next (Next (Start)))
```

```
myBusC = Next myBusB
```

```
plus :: Bus -> Bus -> Bus
```

```
plus a Start = a
```

```
plus a (Next b) = Next (plus a b)
```

(Next b)  
parenthesis for  
pattern matching

```
testBus :: Bus
```

```
testBus = plus myBusC myBusB
```

# Recursive Data Type Example (2)

**data** Bus = Start | Next (Bus) deriving Show

myBusA = Start

myBusB = Next (Next (Next (Start)))

myBusC = Next myBusB

= Next ( Next (Next (Next (Start))) )

**plus** myBusC myBusB

**plus** Next (Next (Next (Start))) Next (Next (Next (Next (Start))))

Next (**plus** Next (Next (Next (Start))) Next (Next (Next (Start))) )

Next (Next (**plus** Next (Next (Next (Start))) Next (Next (Start)) ))

Next (Next (Next (**plus** Next (Next (Next (Start))) Next (Start) )))

Next (Next (Next (Next (**plus** Next (Next (Next (Start))) Start )))

Next (Next (Next (Next (Next (Next (Next (Start))) ))))

**plus** :: Bus -> Bus -> Bus

**plus** a Start = a

**plus** a (Next b) = Next (**plus** a b)

# Recursive Data Type Example (3)

**howFar** :: Bus -> Int

**howFar** Start = 0

**howFar** (Next r) = 1 + **howFar** r

**testInt** :: Int

**testInt** = (+) (**howFar** myBusC) (**howFar** myBusB)



# Recursive Data Type Example (4)

**testInt = (+) (howFar myBusC) (howFar myBusB)**

**howFar myBusC**

**howFar Next (Next (Next (Start)))**

**1 + howFar Next (Next (Start))**

**2 + howFar Next (Start)**

**3 + howFar Start**

**3**

**howFar myBusB**

**howFar Next (Next (Next (Next (Start))))**

**1 + howFar Next (Next (Next (Start)))**

**2 + howFar Next (Next (Start))**

**3 + howFar Next (Start)**

**4 + howFar Start**

**5**

**(+) 3 5**

**8**

**howFar :: Bus -> Int**

**howFar Start = 0**

**howFar (Next r) = 1 + howFar r**

**(Next r) parens for pattern matching**

**(howFar myBusC) (howFar myBusB)  
unnecessary parens in function  
call for readability**

# Anniversary Data Type (1)

```
data Anniversary = Birthday String Int Int Int  
                  | Wedding String String Int Int Int
```

```
Birthday    String  Int    Int    Int  
--          name,  year,   month, day  
Wedding    String          String      Int    Int    Int  
--          spouse name 1, spouse name 2, year,   month, day
```

[https://en.wikibooks.org/wiki/Haskell/Type\\_declarations](https://en.wikibooks.org/wiki/Haskell/Type_declarations)

## Anniversary Data Type (2)

```
johnSmith :: Anniversary
```

```
johnSmith = Birthday "John Smith" 1968 7 3
```

```
smithWedding :: Anniversary
```

```
smithWedding = Wedding "John Smith" "Jane Smith" 1987 3 4
```

```
anniversariesOfJohnSmith :: [Anniversary]
```

```
anniversariesOfJohnSmith = [johnSmith, smithWedding]
```

```
anniversariesOfJohnSmith =
```

```
[Birthday "John Smith" 1968 7 3, Wedding "John Smith" "Jane Smith" 1987 3 4]
```

[https://en.wikibooks.org/wiki/Haskell/Type\\_declarations](https://en.wikibooks.org/wiki/Haskell/Type_declarations)

# Anniversary Data Type (3)

```
showDate :: Int -> Int -> Int -> String
```

```
showDate y m d = show y ++ "-" ++ show m ++ "-" ++ show d
```

```
showAnniversary :: Anniversary -> String
```

```
showAnniversary (Birthday name year month day) =  
  name ++ " born " ++ showDate year month day
```

```
showAnniversary (Wedding name1 name2 year month day) =  
  name1 ++ " married " ++ name2 ++ " on " ++ showDate year month day
```

## Deconstructing Types

( ) around the constructor name and the bound variables are mandatory  
the expression inside ( ) is not a call to the constructor function

[https://en.wikibooks.org/wiki/Haskell/Type\\_declarations](https://en.wikibooks.org/wiki/Haskell/Type_declarations)

# Anniversary Data Type (4)

```
type Name = String
```

```
data Anniversary =  
  Birthday Name Date  
  | Wedding Name Name Date
```

```
data Date = Date Int Int Int -- Year, Month, Day
```

```
johnSmith :: Anniversary  
johnSmith = Birthday "John Smith" (Date 1968 7 3)
```

```
smithWedding :: Anniversary  
smithWedding = Wedding "John Smith" "Jane Smith" (Date 1987 3 4)
```

```
type AnniversaryBook = [Anniversary]
```

```
anniversariesOfJohnSmith :: AnniversaryBook  
anniversariesOfJohnSmith = [johnSmith, smithWedding]
```

```
showDate :: Date -> String  
showDate (Date y m d) = show y ++ "-" ++ show m ++ "-" ++ show d
```

```
showAnniversary :: Anniversary -> String  
showAnniversary (Birthday name date) =  
  name ++ " born " ++ showDate date  
showAnniversary (Wedding name1 name2 date) =  
  name1 ++ " married " ++ name2 ++ " on " ++ showDate date
```

[https://en.wikibooks.org/wiki/Haskell/Type\\_declarations](https://en.wikibooks.org/wiki/Haskell/Type_declarations)

# Polymorphic Type

types that are universally quantified in some way over **all types**  
essentially describe families of types

(forall a) [a] is the family of types consisting of,  
for every type a, the type of lists of a.

- lists of integers (e.g. [1,2,3])
- lists of characters (['a','b','c'])
- lists of lists of integers, etc.
- [2,'b'] is not a valid example

<https://www.haskell.org/tutorial/goodies.html>

# Subset Polymorphism

---

roots :: (Floating a) => (a, a, a) -> (a, a)

<https://www.haskell.org/tutorial/goodies.html>

# Parameterized Polymorphism

```
plus :: a -> a -> a,  
plus :: Int -> Int -> Int,  
plus :: Rat -> Rat -> Rat,
```

```
data List a = L a (List a) | Empty
```

```
listlen :: List a -> Int
```

```
listlen Empty = 0
```

```
listlen (L _ list) = 1 + listlen list
```

(L \_ list) **pattern matching**

\_ : match with any element

<https://www.haskell.org/tutorial/goodies.html>



# ExplicitForAll

**Just** :: a -> Maybe a

**Nothing** :: Maybe a

**reverse** :: [a] -> [a]

**map** :: (a -> b) -> [a] -> [b]

**show** :: (Show a) => a -> String

**Just** :: forall a. a -> Maybe a

**Nothing** :: forall a. Maybe a

**reverse** :: forall a. [a] -> [a]

**map** :: forall a b. (a -> b) -> [a] -> [b]

**show** :: forall a. (Show a) => a -> String

to **explicitly** specify the **universal quantification**

in **polymorphic** type signatures.

<https://www.schoolofhaskell.com/school/to-infinity-and-beyond/pick-of-the-week/guide-to-ghc-extensions/explicit-forall>

# Type function X

```
data Either a b = Left a | Right b
```

```
Left :: a -> Either
```

```
Right :: b -> Either
```

```
isLeft (Left a) = True
```

```
isLeft (Right b) = False
```

```
type X a = Either a a
```

[https://wiki.haskell.org/GADTs\\_for\\_dummies](https://wiki.haskell.org/GADTs_for_dummies)

# First Class Values

```
data Either a b = Left a | Right b
```

Data constructors are **first class values** in Haskell and actually have a **type**.

the type of the **Left** constructor of the **Either** data type is:

```
Left :: forall b a. a -> Either a b
```

first class values:

- may be passed to functions
- may make a list
- may be data elements of other algebraic data types
- and so forth

<https://wiki.haskell.org/Constructor>

# Show Class

---

## Class Show

the instances of Show are those types  
that can be converted to character strings.  
(information about the class)

The function show

`show :: (Show a) => a -> String`

Similar to the `toString()` method in Java

<https://www.haskell.org/tutorial/goodies.html>