

Arrows (1A)

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Based on

aaa

An arrow type

a monadic type $m\ a$:

a computation delivering an **a**

an arrow type $a\ b\ c$:

a computation with input of type **b** delivering a **c**

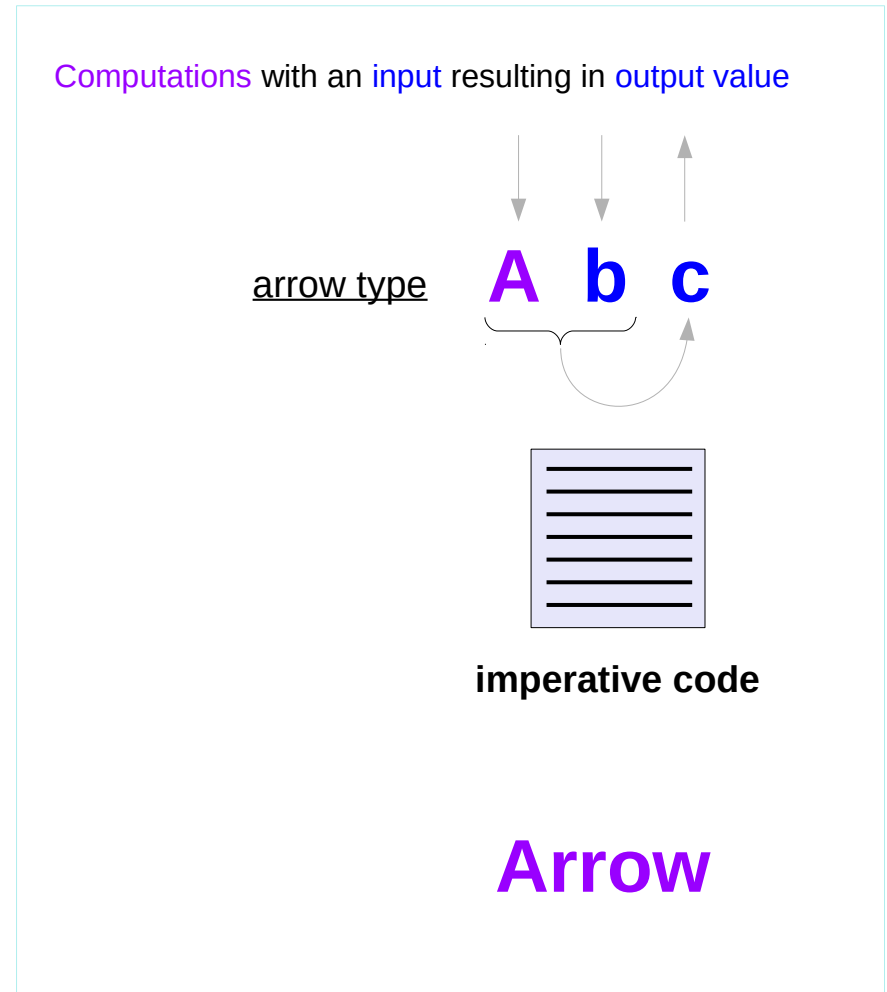
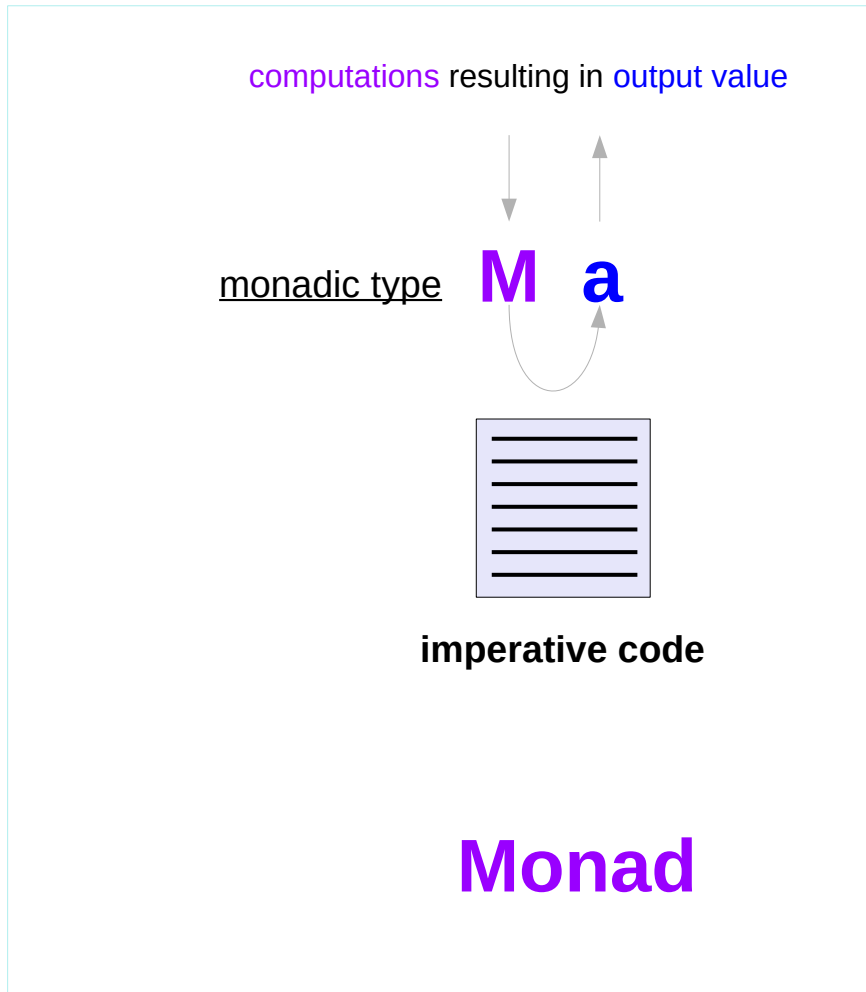
the application of the parameterised type **a**
to the two parameters **b** and **c**

arrows make the dependence on input explicit

- John Hughes, Generalising Monads to Arrows [1]
Science of Computer Programming 37 (2000)
www.elsevier.nl/locate/scicoGeneralising_monads_to_arrows John Hughes

https://en.wikibooks.org/wiki/Haskell/Understanding_arrows

Monadic and Arrow types



https://en.wikibooks.org/wiki/Haskell/Understanding_arrows

The Arrow

Arrow **a b c**

represents **a** process that
takes as input something of type **b** and
outputs something of type **c**.

the application of the parameterised type **a**
to the two parameters **b** and **c**

a **b** **c**

Function application

a :: Arrow

https://wiki.haskell.org/Arrow_tutorial

arr

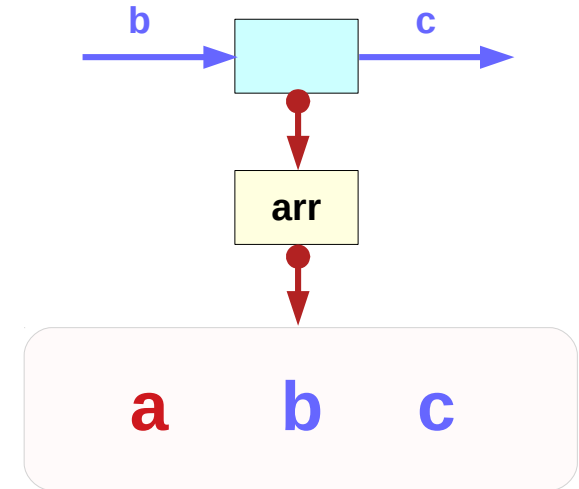
arr builds an arrow out of a **function**.

This function is arrow-specific.

arr :: (Arrow a) => (b -> c) -> a b c

A computation **a** takes inputs of some type **b** and produces outputs of another type **c**.

Each function (**b -> c**) may be treated as a computation



Function application

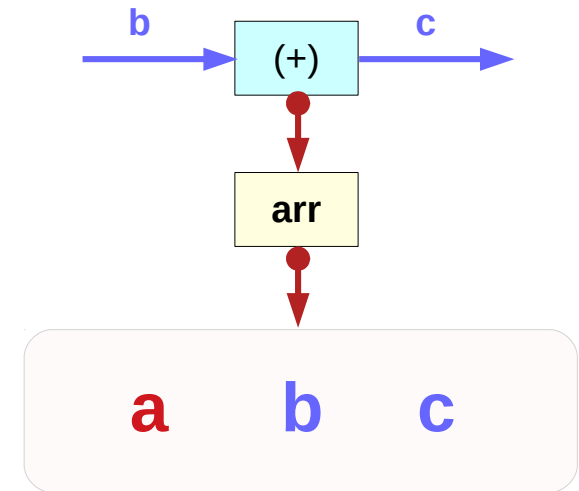
a :: Arrow

https://wiki.haskell.org/Arrow_tutorial

The Arrow

```
Prelude> import Control.Arrow
Prelude Control.Arrow> let a1 = arr (+)
Prelude Control.Arrow> :t a1
a1 :: (Arrow a1, Num a) => a1 a (a -> a)
Prelude Control.Arrow> a1 3 4
7
```

```
Prelude Control.Arrow> let a2 = arr (+3)
Prelude Control.Arrow> a2 4
7
Prelude Control.Arrow> :t a2
a2 :: (Arrow a, Num c) => a c c
```



Function application

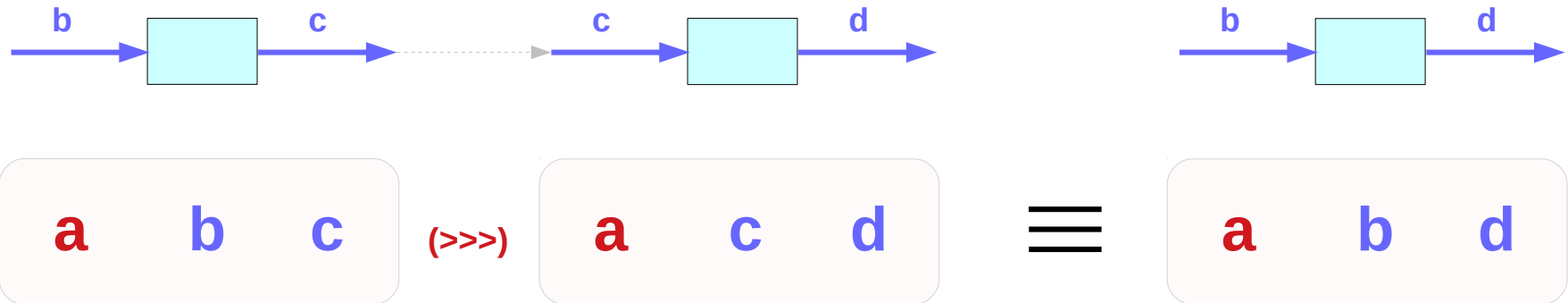
$a :: \text{Arrow}$

<http://tuttlem.github.io/2014/07/26/practical-arrow-usage.html>

The Arrow composition

Arrow composition is achieved with `(>>>)`.
This takes two arrows and **chains** them together,
one after another.
It is also arrow- specific.

`(>>>) :: (Arrow a) => a b c -> a c d -> a b d`



https://wiki.haskell.org/Arrow_tutorial

first and second

First and second make a new arrow out of an existing arrow.

They perform a transformation (given by their argument) on either the first or the second item of a pair.

These definitions are arrow-specific.

first :: (Arrow a) => a b c -> a (b, d) (c, d)

second :: (Arrow a) => a b c -> a (d, b) (d, c)

https://wiki.haskell.org/Arrow_tutorial

first and second

data STRef s a

a value of type **STRef s a** is a mutable variable in state thread **s**, containing a value of type **a**

```
>>> :{  
runST (do  
  ref <- newSTRef "hello"  
  x <- readSTRef ref  
  writeSTRef ref (x ++ "world")  
  readSTRef ref )  
:}  
"helloworld"
```

https://wiki.haskell.org/Arrow_tutorial

References

- [1] <ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf>
- [2] <https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf>