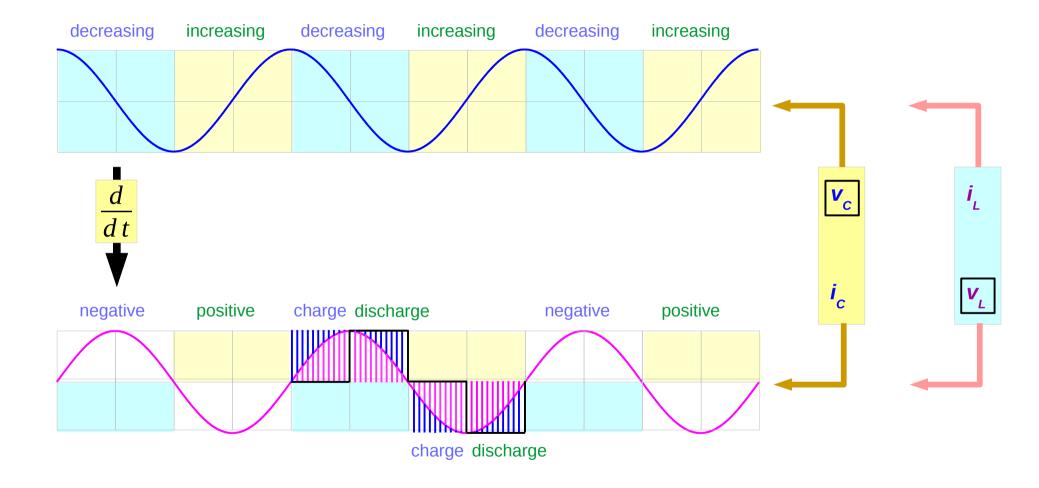
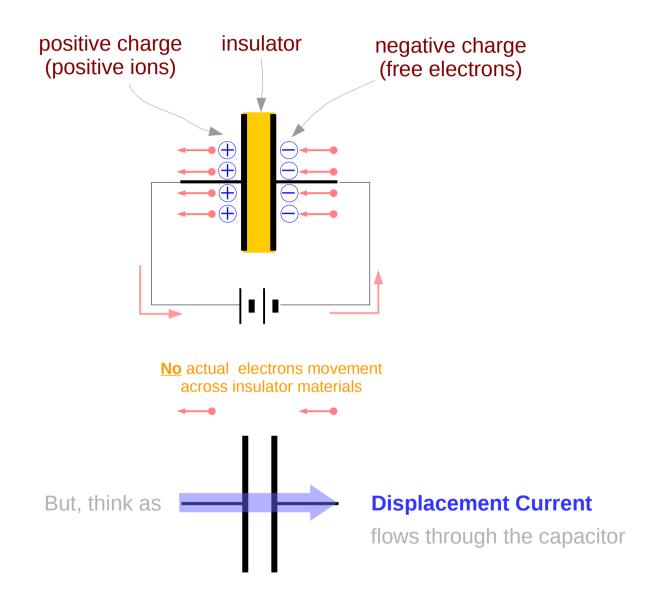
Capacitor in an AC circuit

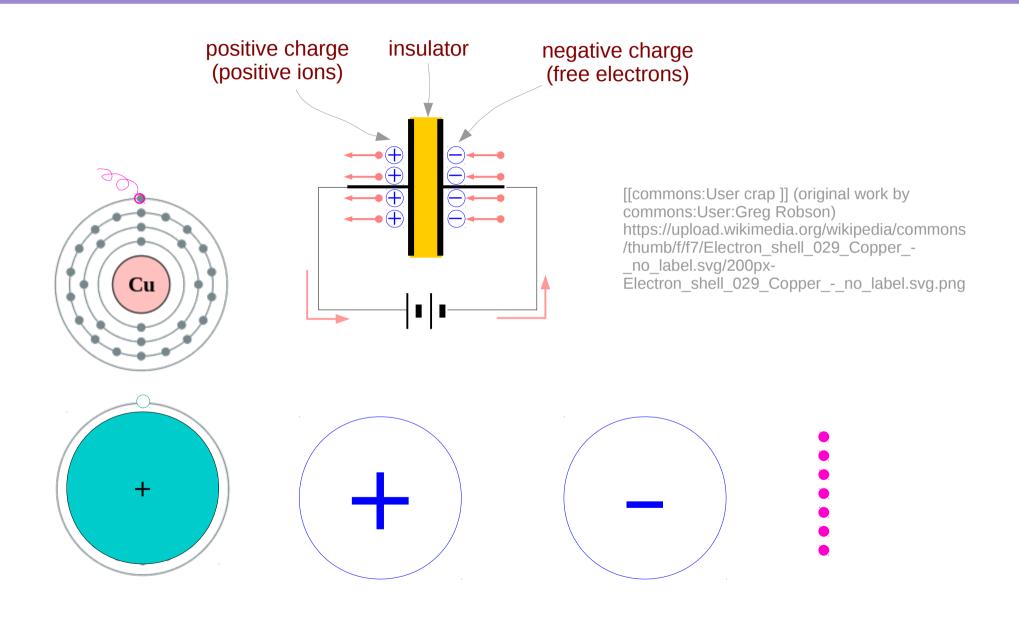
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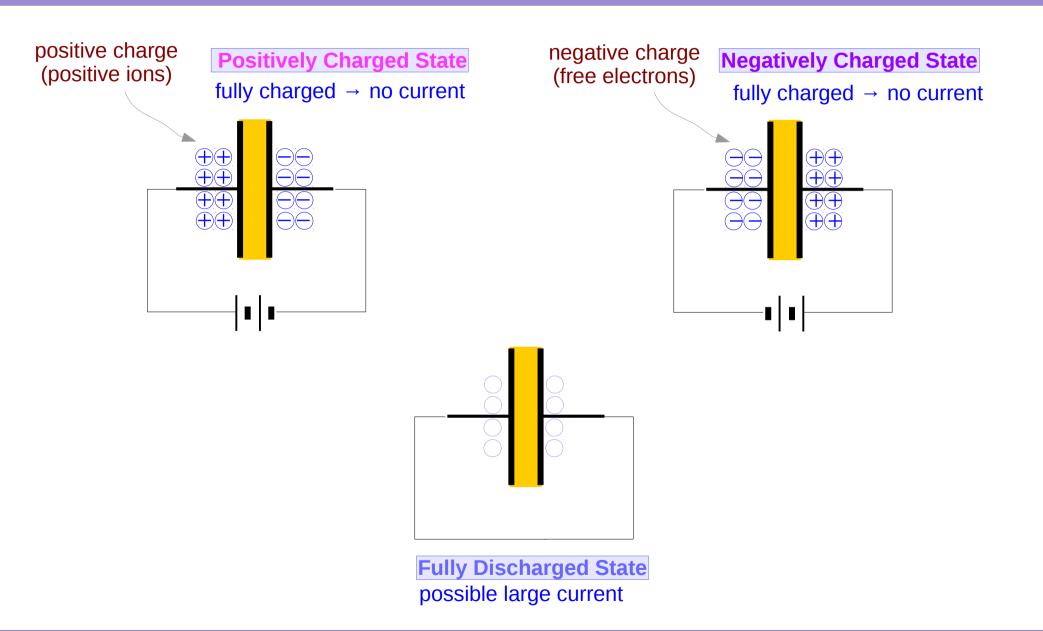
Capacitor Current



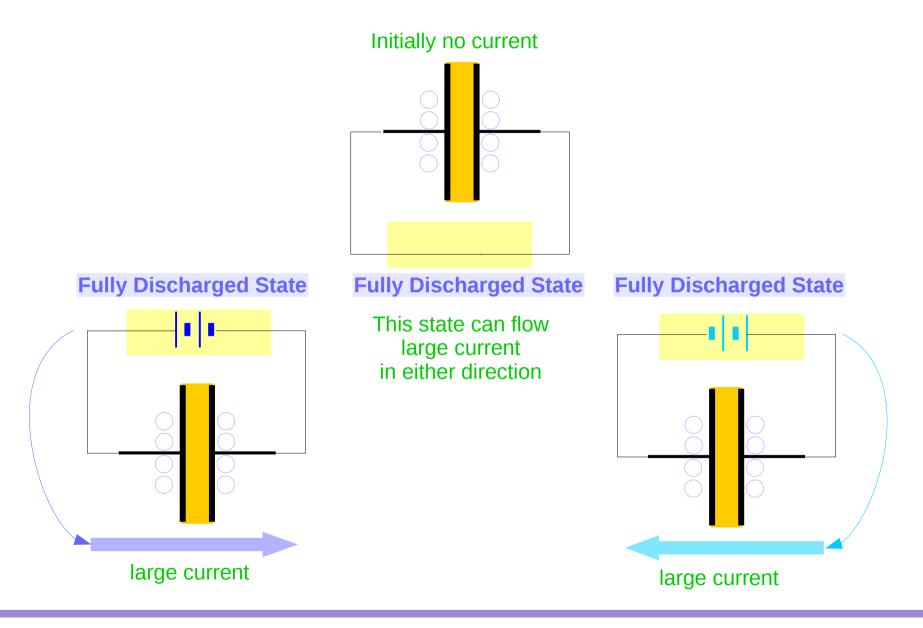
Positive ions and free electrons



Three States



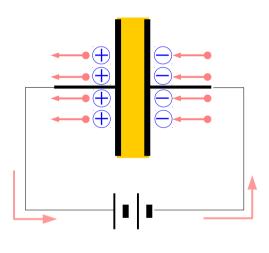
Currents in the Fully Discharged State



Inter-State Current Flowing

Under Positively Charging

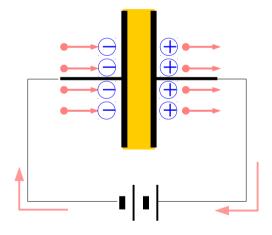




electron flow direction

Under Negatively Charging





electron flow direction

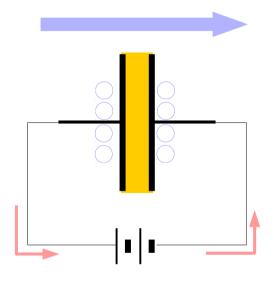
Young Won Lim

07/29/2017

Inter-State Current Flowing

Fully Discharged State

(+) current flow direction

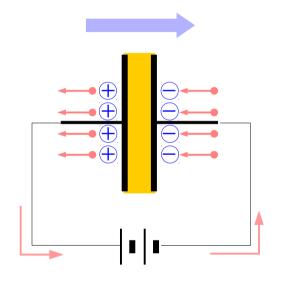


electron flow direction

Initial large current

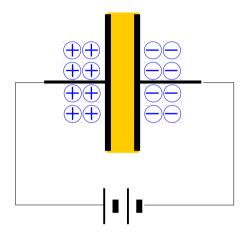
Under Positively Charging

(+) current flow direction



electron flow direction

Positively Charged State



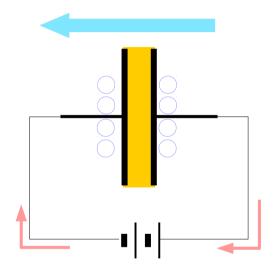
Crowded → No more space

no current

Inter-State Current Flowing

Fully Discharged State

(-) current flow direction

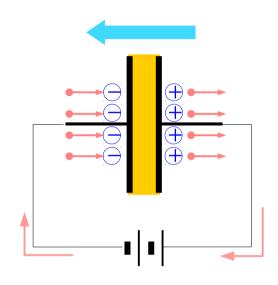


electron flow direction

Initial large current

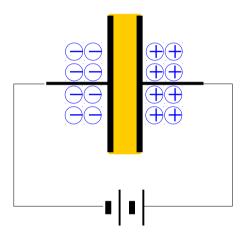
Under Negatively Charging

(-) current flow direction



electron flow direction

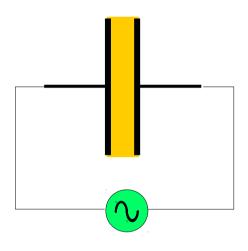
Negatively Charged State

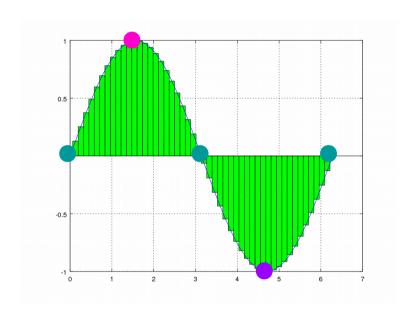


Crowded → No more space

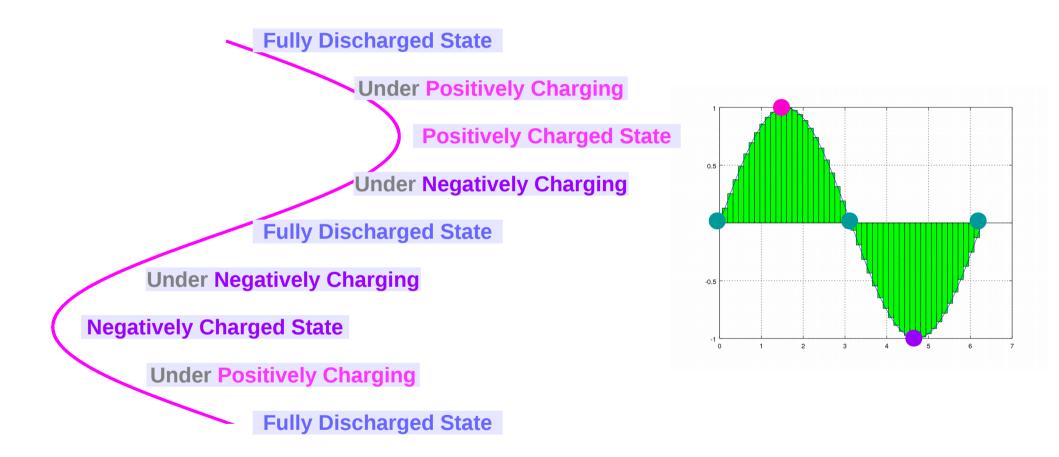
no current

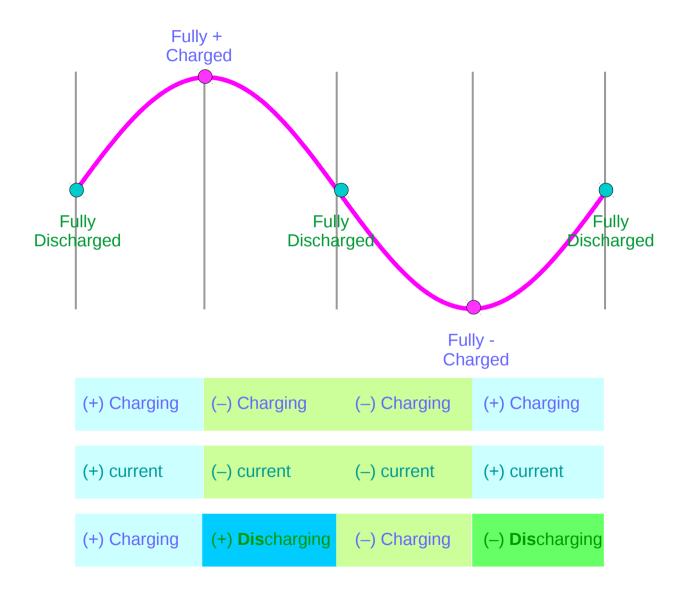
An AC Voltage Source



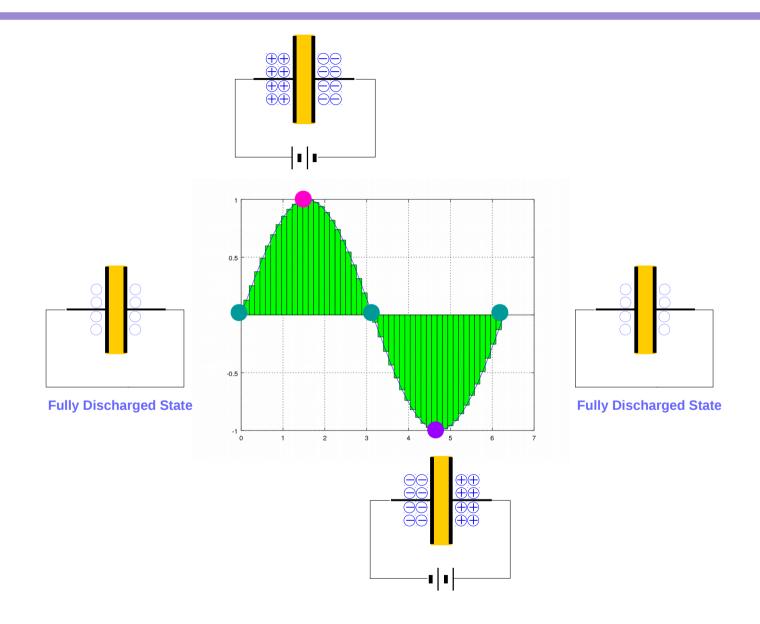


An AC Voltage Source

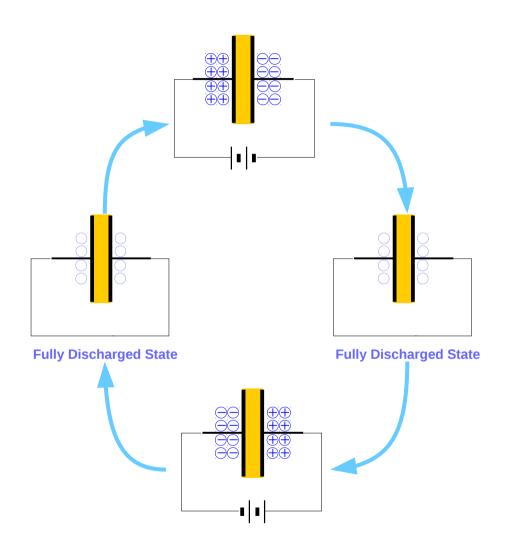


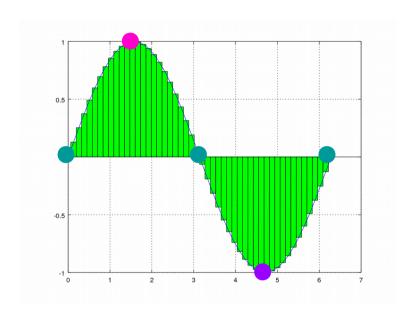


A Cycle

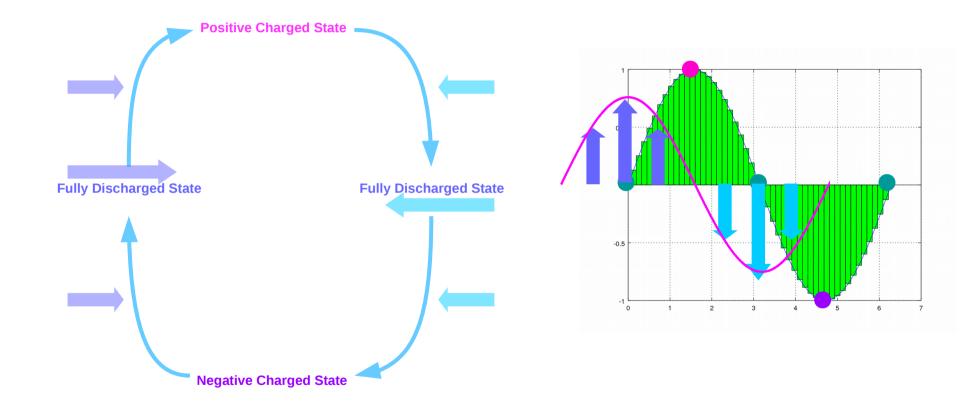


State Transition Diagram



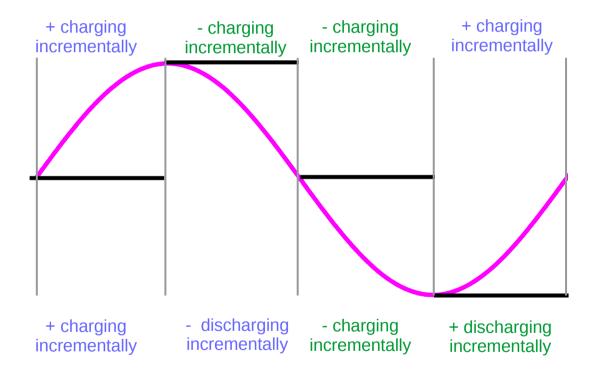


Current Flow



Continuous Charing and Discharging Operations

Incremental Voltage Increment → + Charging incrementally
Incremental Voltage Decrement → - Charging incrementally

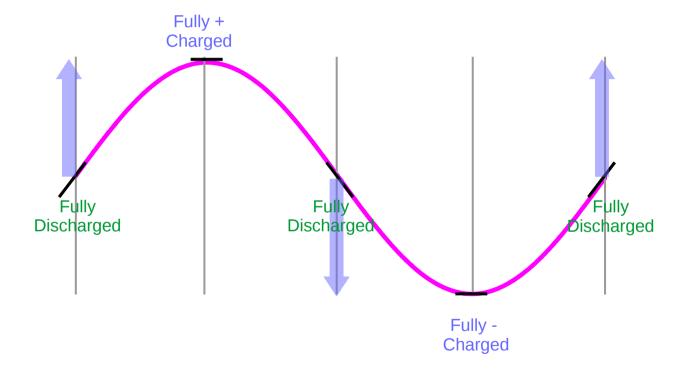


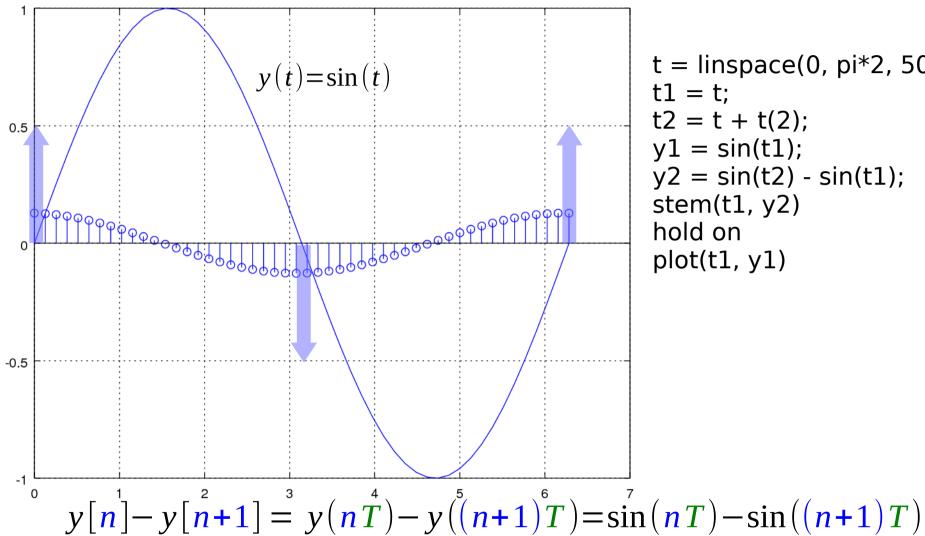
Fully Discharged : Large Current

Incremental Voltage Increment

→ Continuous Charging

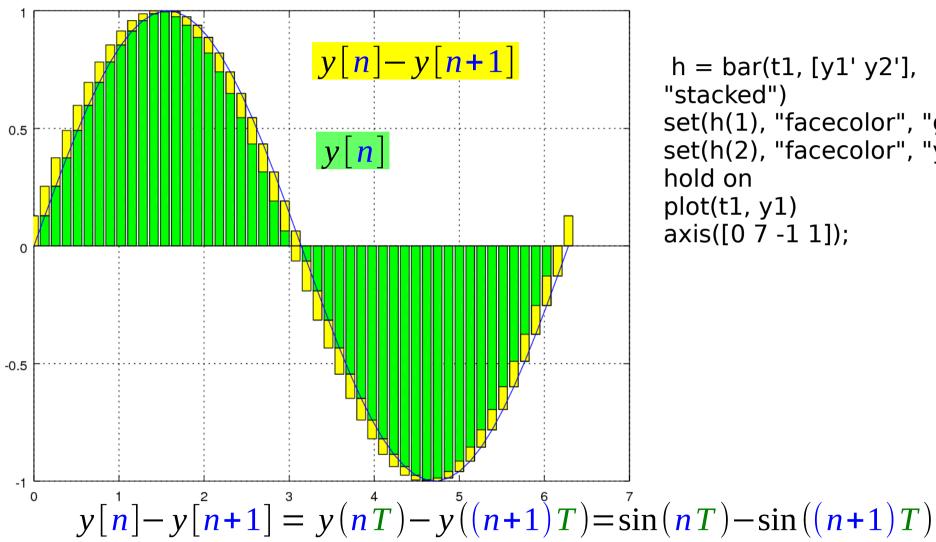
Incremental Voltage Decrement
→ Continuous Discharging





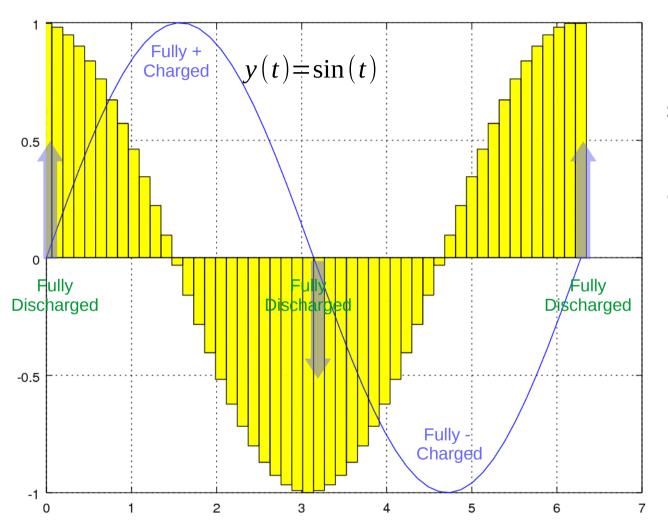
```
t = linspace(0, pi*2, 50);
t1 = t;
t2 = t + t(2);
y1 = \sin(t1);
y2 = \sin(t2) - \sin(t1);
stem(t1, y2)
hold on
plot(t1, y1)
```

$$\sin^{7}(nT) - \sin((n+1)T)$$



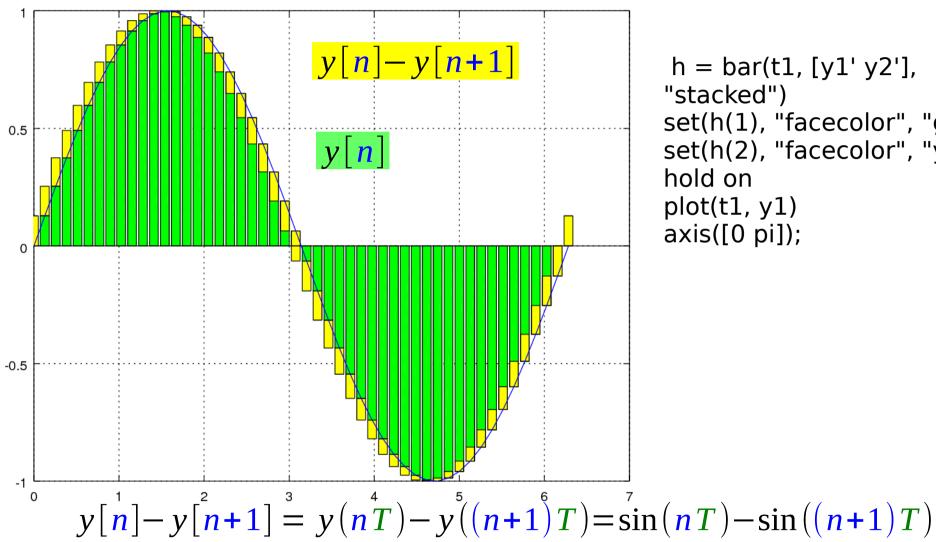
```
h = bar(t1, [y1' y2'],
"stacked")
set(h(1), "facecolor", "g");
set(h(2), "facecolor", "y");
hold on
plot(t1, y1)
axis([0 7 -1 1]);
```

$$\sin(nT) - \sin((n+1)T)$$



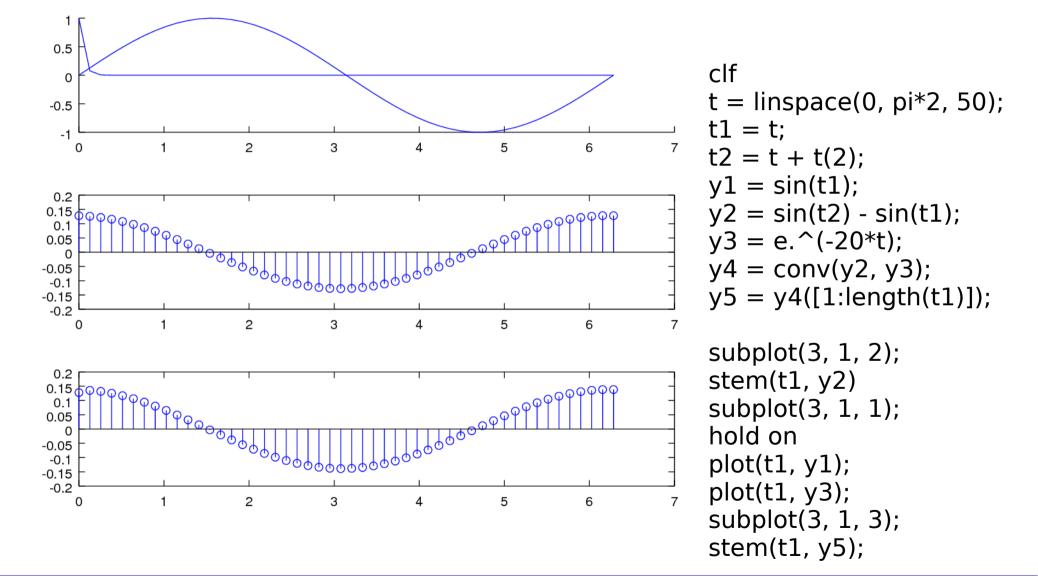
$$\frac{y[n]-y[n+1]}{T}$$

$$\propto \frac{dy}{dt}$$

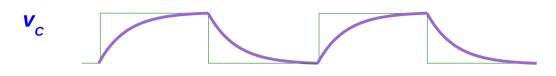


```
h = bar(t1, [y1' y2'],
"stacked")
set(h(1), "facecolor", "g");
set(h(2), "facecolor", "y");
hold on
plot(t1, y1)
axis([0 pi]);
```

$$\sin(nT) - \sin((n+1)T)$$



Pulse



 i_c

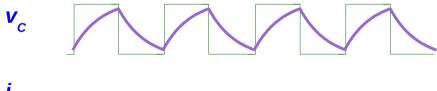


$$i_C = C \frac{d v_C}{d t}$$



 i_c



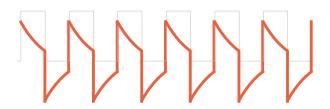


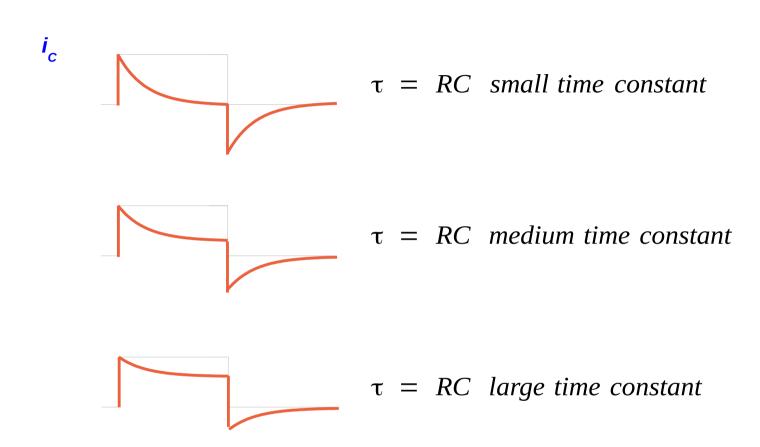
C



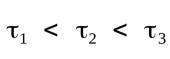


C





i

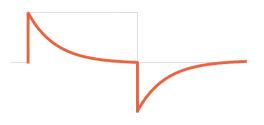


$$a_1 > a_2 > a_3$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}} = e^{-at}$$

$$\tau = RC = \frac{1}{a}$$

 i_c



$$\tau = RC$$

$$\tau = RC$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$



$$\tau = RC$$

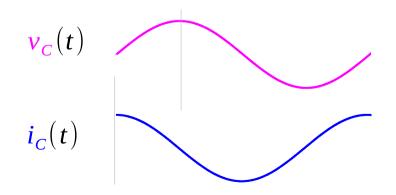
$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$

small τ

small C

large
$$\frac{1}{\omega C} \gg R$$

Fully Capacitative

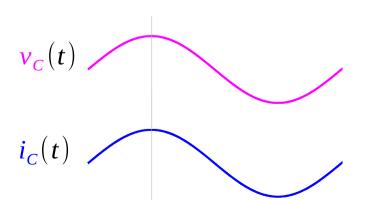


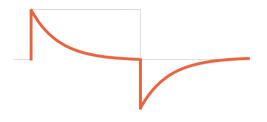
large τ

large C

small
$$\frac{1}{\omega C} \ll R$$

Fully Resistive





$$\tau = RC$$

$$\tau = RC$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$



$$\tau = RC$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$

small
$$\tau$$

small C

large
$$\frac{1}{\omega C} \gg R$$

Fully Capacitative

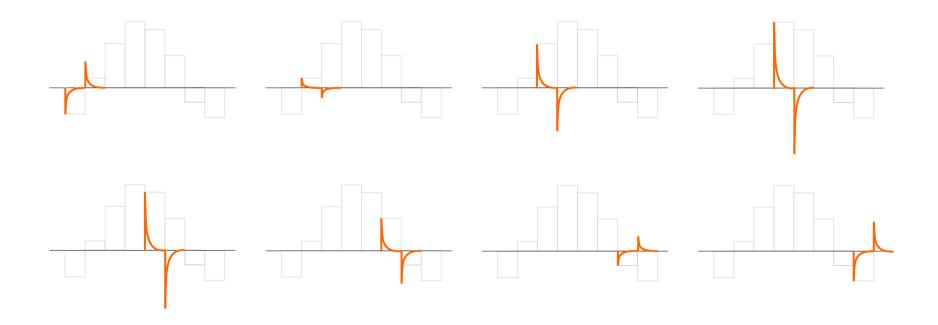
large
$$\tau$$

large C

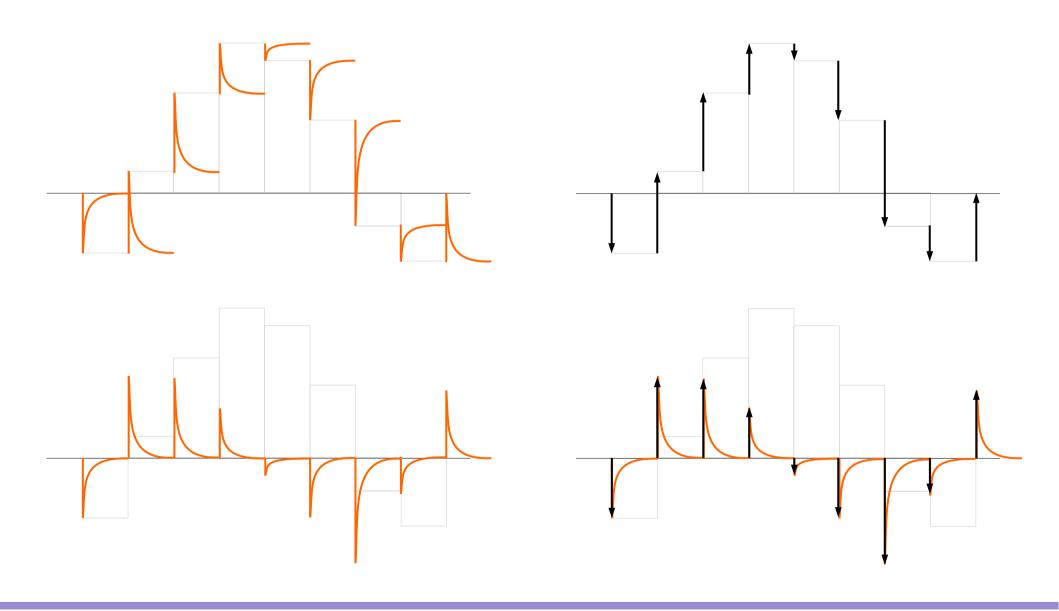
small
$$\frac{1}{\omega C} \ll R$$

Fully Resistive

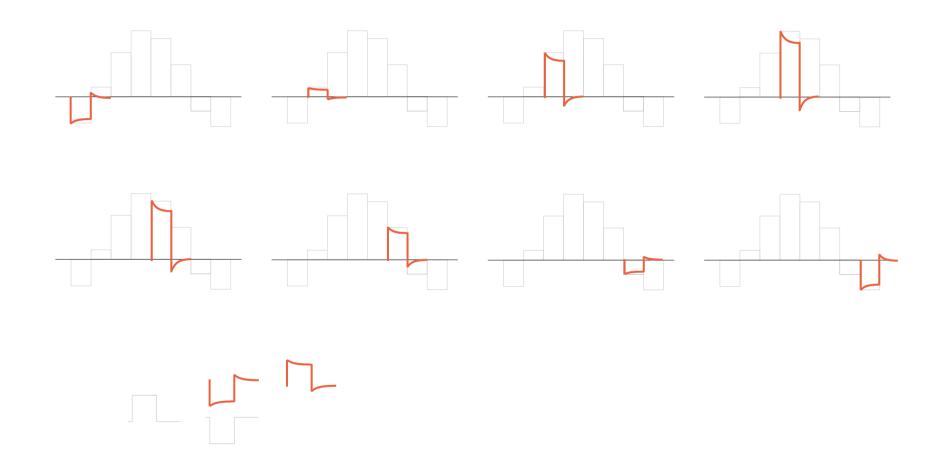
Superposition - Small Time Constant



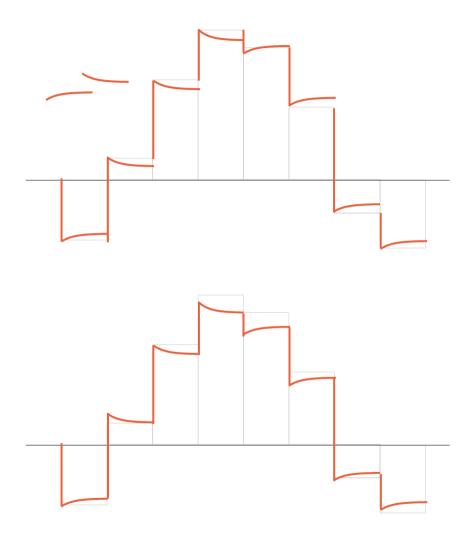
Small Time Constants

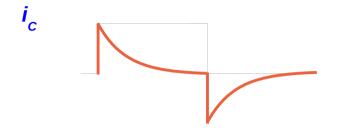


Superposition – Large Time Constant



Large Time Constants





$$\tau = RC$$

$$\tau = RC$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$



$$\tau = RC$$

$$\tau = RC$$

$$e^{-\frac{t}{\tau}} = e^{-\frac{t}{RC}}$$

small τ

small C

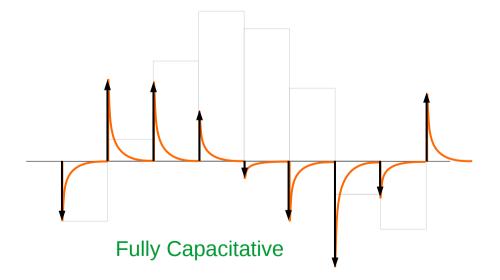
Capacitor - AC

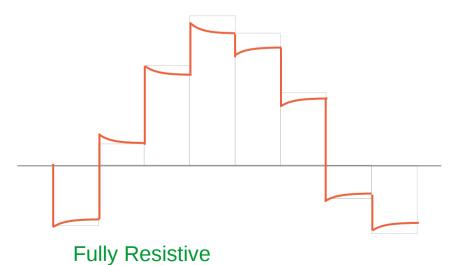
large
$$\frac{1}{\omega C} \gg R$$



large C

small
$$\frac{1}{\omega C} \ll R$$





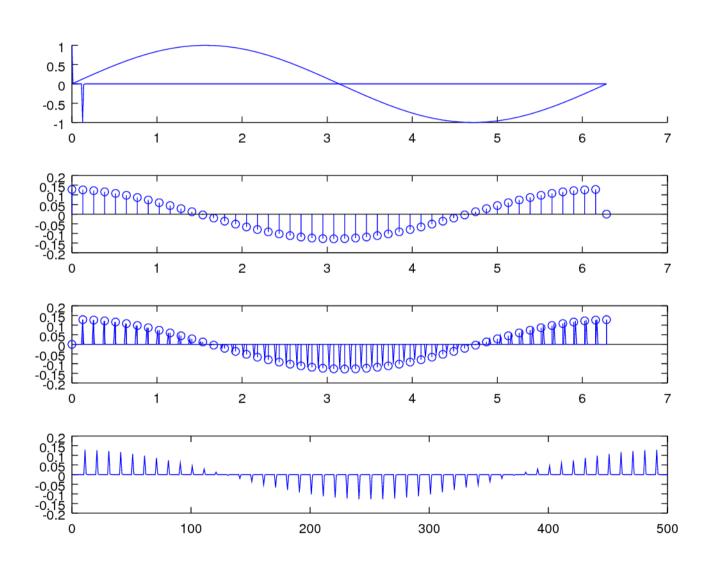
Plotting superposition results

```
clf
t = linspace(0, pi*2, 50);
tt = linspace(0, pi*2, 500);
N = length(t);
NN= length(tt);
t1 = t:
t2 = [t(2:N), t(N)];
y1 = \sin(t1);
y2 = \sin(t2) - \sin(t1);
yy = [y1; zeros(NN/N-1, N)];
yy2 = yy(:)';
a = 1/300:
yy3 = e.^{(-a*tt)};
yy3 = yy3 - [zeros(1, NN/N),
e.^{(-a*tt)}(1:NN):
```

```
svec = zeros(1, NN);
for i = 1:NN;
  tvec = zeros(1, NN);
  tvec = [zeros(1, i-1), yy3];
  tvec = yy2(i) * tvec(1:NN);
  svec = svec + tvec;
endfor
  yy4 = svec;
% yy4= conv(yy2, yy3);
y5 = yy4([1:NN/N:NN]);
yy5= yy4([1:NN]);
```

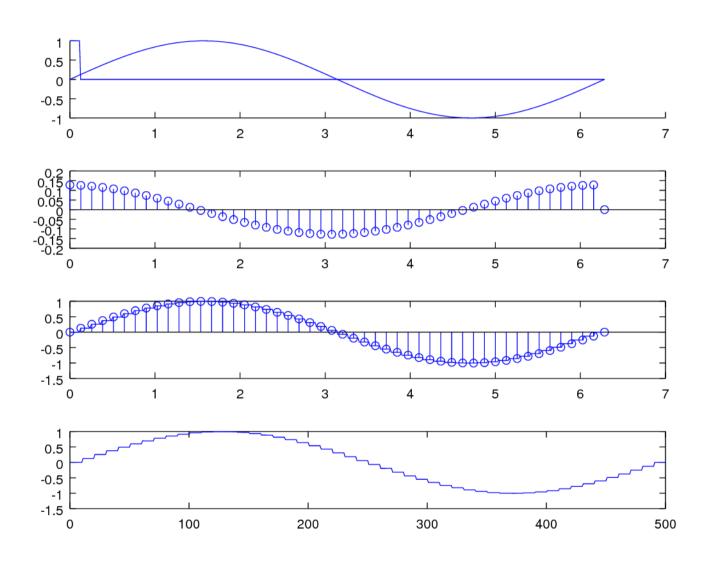
```
subplot(4, 1, 2);
stem(t1, y2)
subplot(4, 1, 1);
hold on
plot(t1, y1);
plot(tt, yy3);
subplot(4, 1, 3);
stem(t1, y5); hold on
plot(tt, yy5)
subplot(4, 1, 4);
plot(yy4);
```

Small Time Constant

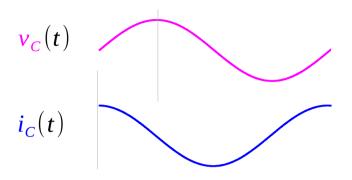


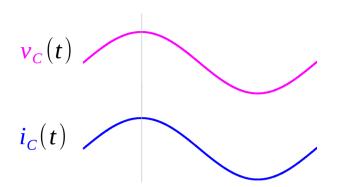
```
yy = [y1;
zeros(NN/N-1, N)];
yy2= yy(:)';
a = 300;
yy3 = e.^{(-a*tt)};
yy3 = yy3 -
[zeros(1, NN/N),
e.^(-a*tt)](1:NN);
\tau = RC
small \tau
small C
large \frac{1}{\omega C}
```

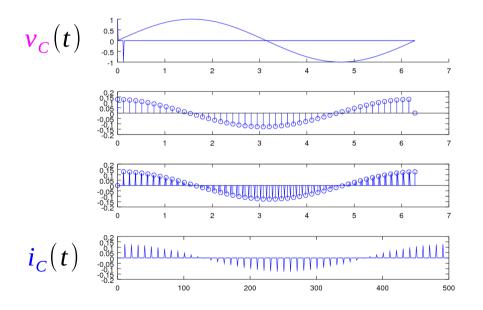
Large Time Constant

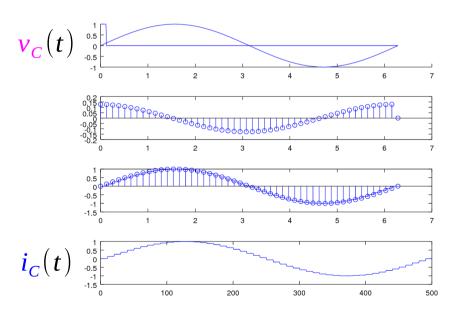


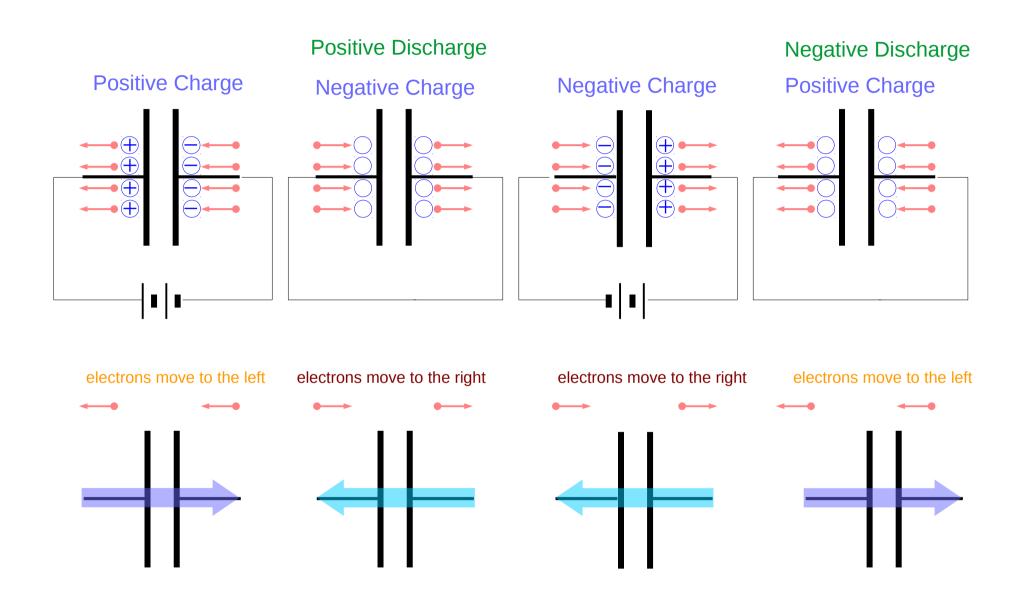
```
yy = [y1;
zeros(NN/N-1, N)];
yy2= yy(:)';
a = 1/300;
yy3 = e.^{(-a*tt)};
yy3 = yy3 -
[zeros(1, NN/N),
e.^(-a*tt)](1:NN);
\tau = RC
large τ
large C
small \frac{1}{\omega C}
```

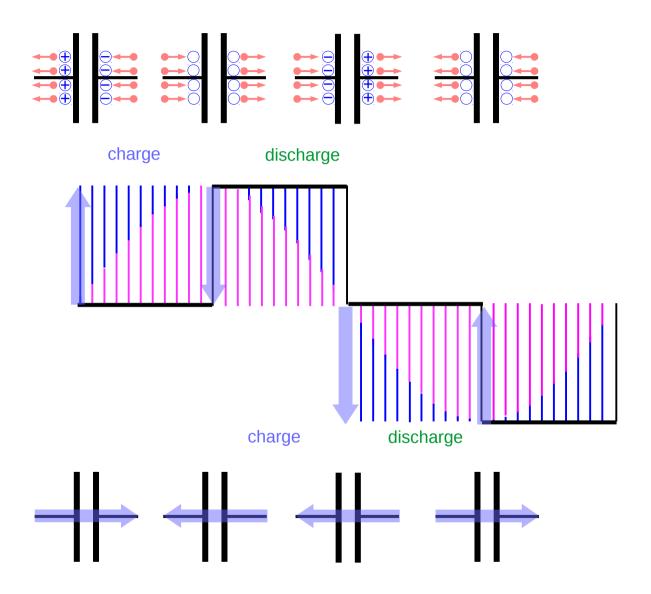


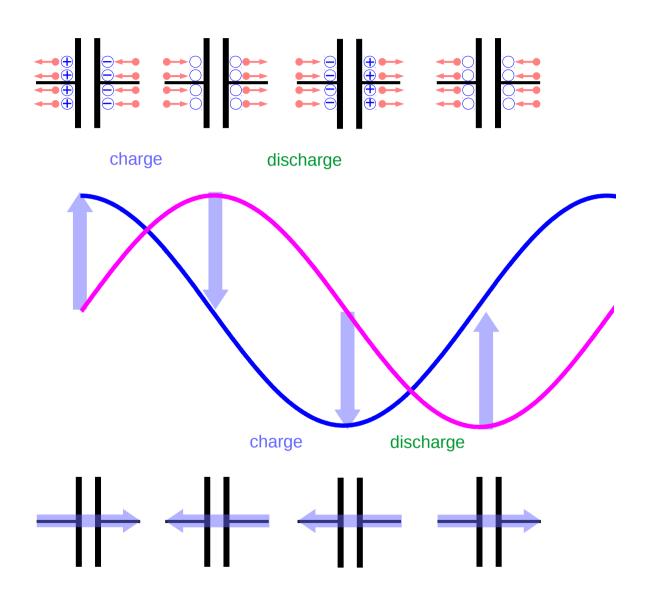


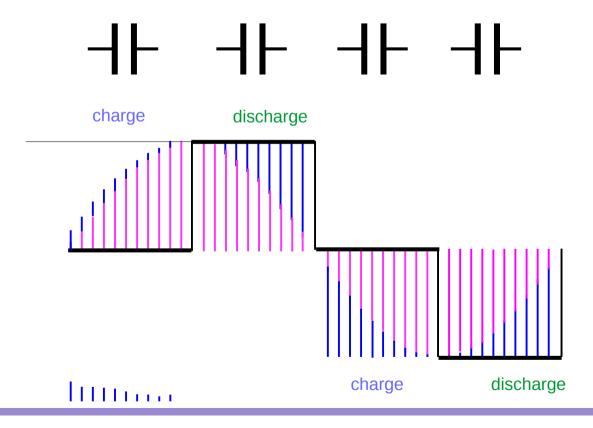


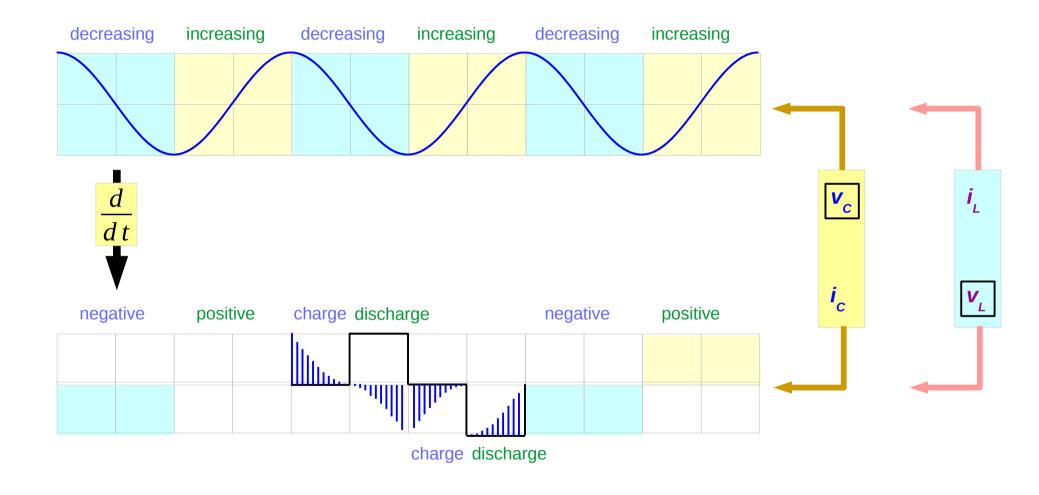




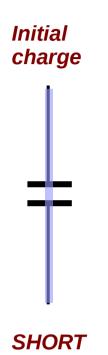






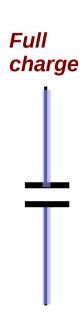


I leads V by 90°



V = 0

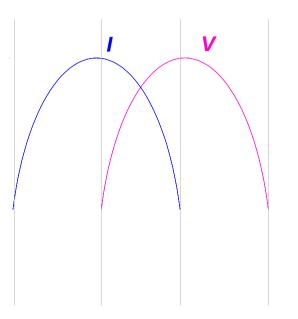
I: peak



OPEN

I = 0

V : peak



References

- [1] http://en.wikipedia.org/
- [2] J.H. McClellan, et al., Signal Processing First, Pearson Prentice Hall, 2003