Monad Background (3A)

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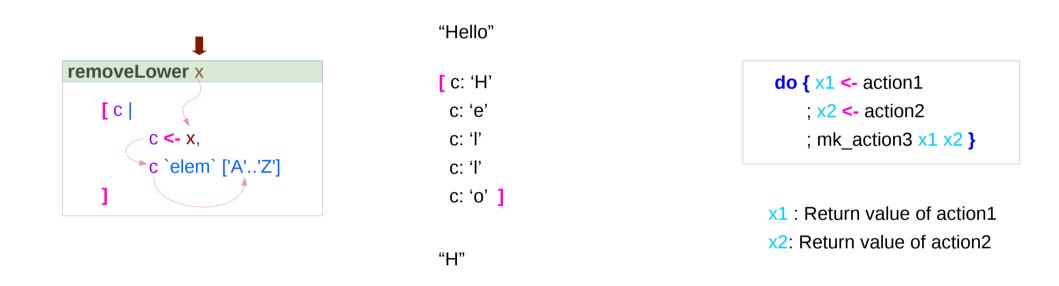
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Young Won Lim 11/6/17 Haskell in 5 steps https://wiki.haskell.org/Haskell_in_5_steps

A List Comprehension Function

let removeLower x = [c | c <- x, c `elem` ['A'..'Z']]

a list comprehension



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https://stackoverflow.com/questions/35198897/does-mean-assigning-a-variable-in-haskell

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Pattern and Predicate

```
let removeLower x = [c | c <- x, c `elem` ['A'..'Z']]
```

a list comprehension

[c | c <- x, c `elem` ['A'..'Z']]

c <- x is a generator

(x : argument of the function removeLower)

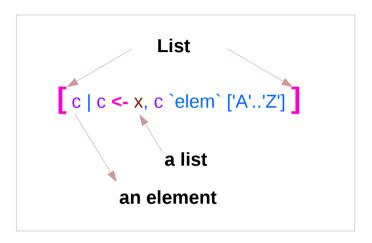
c is a pattern

matching from the **elements** of the **list x** successive binding of c to the **elements** of the **list x**

c `elem` ['A'..'Z']

is a **predicate** which is applied to each successive binding of **c** Only c which <u>passes</u> this predicate will appear in the output list

https://stackoverflow.com/questions/35198897/does-mean-assigning-a-variable-in-haskell



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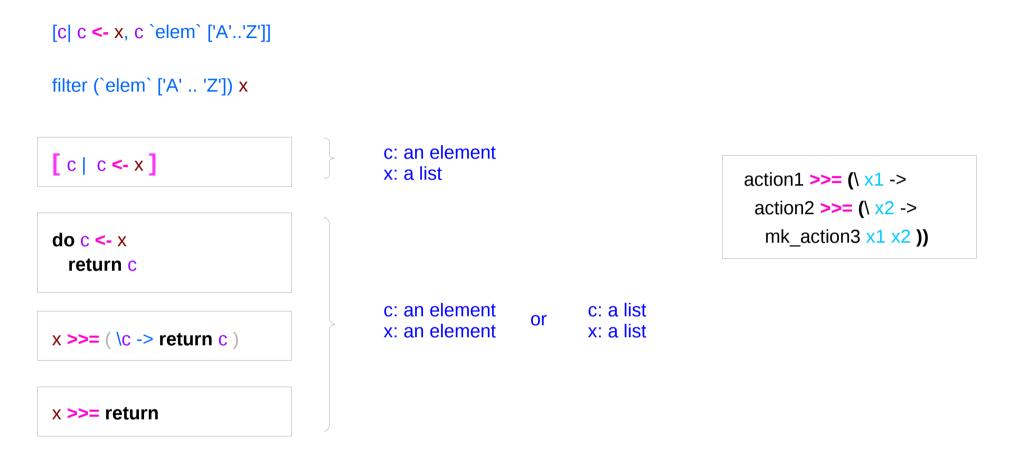
Assignment in Haskell

Assignment in Haskell : <u>declaration</u> with <u>initialization</u>:

- no uninitialized variables,
- must declare with <u>an initial value</u>
- <u>no mutation</u>
- a variable keeps its initial value throughout its scope.

https://stackoverflow.com/questions/35198897/does-mean-assigning-a-variable-in-haskell

Generator



https://stackoverflow.com/questions/35198897/does-mean-assigning-a-variable-in-haskell

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Anonymous Functions

(\x -> x + 1) 4 5 :: Integer

(\x y -> x + y) 3 5 8 :: Integer

inc1 = \x -> x + 1

incListA lst = map inc2 lst
where inc2 x = x + 1

incListB lst = map $(x \rightarrow x + 1)$ lst

incListC = map (+1)

https://wiki.haskell.org/Anonymous_function

Then Operator (>>) and do Statements

a chain of actions

to <u>sequence</u> input / output operations

the (>>) (then) operator works almost identically in do notation

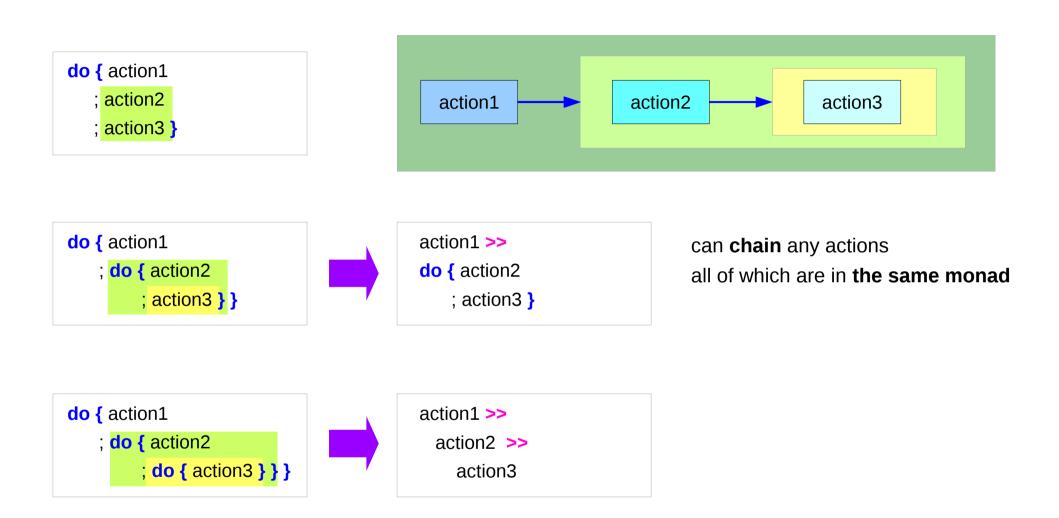
putStr "Hello" >>do { putStr "Hello"putStr "; putStr "Hello"putStr "world!" >>; putStr "world!putStr "\n"; putStr "\n" }
--

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https://en.wikibooks.org/wiki/Haskell/do_notation

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Chaining in **do** and **>>** notations



https://en.wikibooks.org/wiki/Haskell/do_notation

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Bind Operator (>==) and do statements

The bind operator (>>=)

passes a value ->

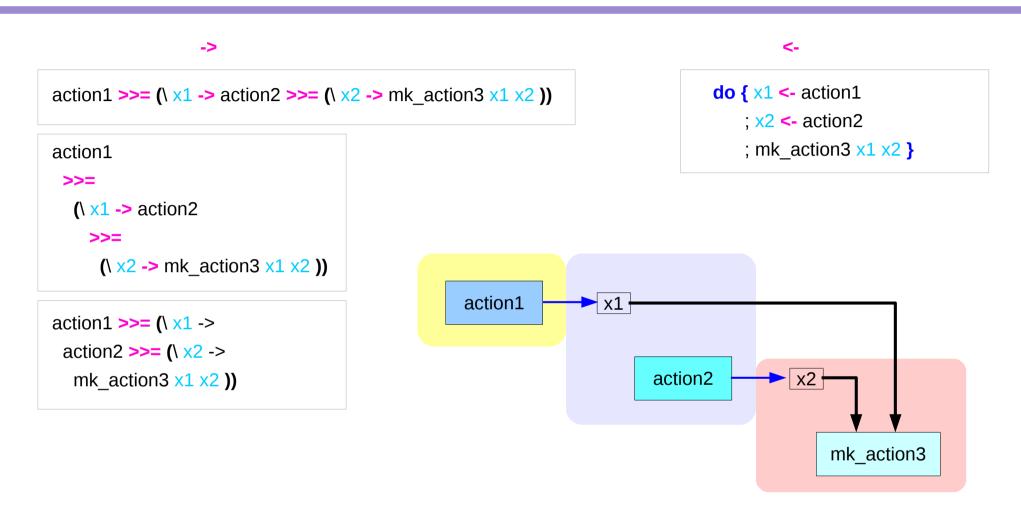
(the result of an action or function), downstream in the binding sequence. **do** notation <u>assigns</u> a variable name to the passed value using the <-

action1 >>= (\ x1 -> action2 >>= (\ x2 -> mk_action3 x1 x2))

> anonymous function (lambda expression) is used

do { x1 <- action1
 ; x2 <- action2
 ; mk_action3 x1 x2 }</pre>

Chaining >>= and **do** notations



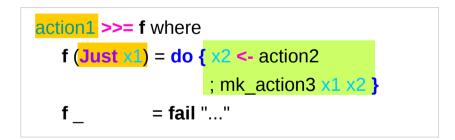
fail method

do {	Just x1 <- action1	
;	x2 <- action2	
;	mk_action3 x1 x2	}

O.K. when action1 returns Just x1

when action1 returns **Nothing** crash with an non-exhaustive patterns error

Handling failure with fail method



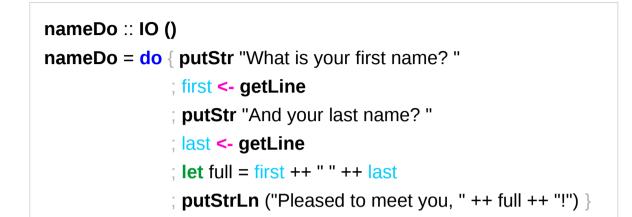
-- A compiler-generated message.

https://en.wikibooks.org/wiki/Haskell/do_notation

do { x1 <- action1	
; x2 <- action2	
; mk_action3 x1 x2 }	

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Example



```
do { x1 <- action1
  ; x2 <- action2
  ; mk_action3 x1 x2 }</pre>
```

using the **do** statement

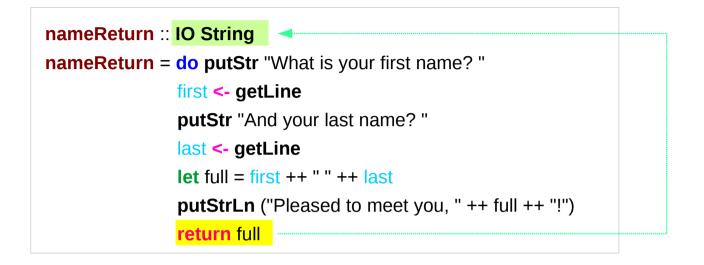
A possible translation into vanilla monadic code:

```
nameLambda :: IO ()
nameLambda = putStr "What is your first name? " >>
    getLine >>= \ first ->
    putStr "And your last name? " >>
    getLine >>= \ last ->
    let full = first ++ " " ++ last
    in putStrLn ("Pleased to meet you, " ++ full ++ "!")
```

https://en.wikibooks.org/wiki/Haskell/do_notation

using then (>>) and Bind (>>=) operators

return method

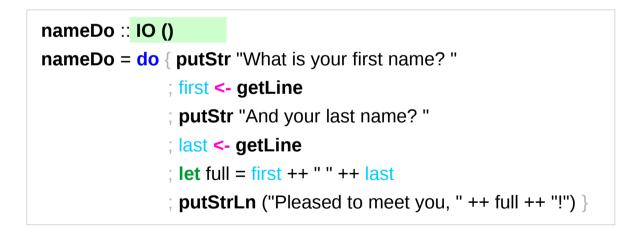


greetAndSeeYou :: IO () greetAndSeeYou = do name <- nameReturn putStrLn ("See you, " ++ name ++ "!")

Without a return method

nameReturn :: IO String		
<pre>nameReturn = do putStr "What is your first name? "</pre>		
first <- getLine		
putStr "And your last name? "		
last <- getLine		
let full = first ++ " " ++ last		
<pre>putStrLn ("Pleased to meet you, " ++ full ++ "!")</pre>		
return full		

explicit return statement returns **IO String** monad



no return statement returns **empty IO** monad

return method – not a final statement

nameReturnAndCarryOn :: IO ()	_
nameReturnAndCarryOn = do putStr "What is your first name? "	
first <- getLine	
putStr "And your last name? "	
last <- getLine	
let full = first++" "++last	
<pre>putStrLn ("Pleased to meet you, "++full++"!")</pre>	
return full	
putStrLn "I am not finished yet!"	

the return statement does <u>not</u> interrupt the flow the last statements of the sequence returns a value

data Color = Red | Green | Blue

Color	is a type
Red	is a <u>constructor</u> that contains a <u>value</u> of type Color .
Green	is a <u>constructor</u> that contains a <u>value</u> of type Color .
Blue	is a <u>constructor</u> that contains a <u>value</u> of type Color .

data Color = RGB Int Int Int

Color is a typeRGB is not a value but a *function* taking three Int's and *returning a value*

RGB :: Int -> Int -> Int -> Color

RGB is a **data constructor** that is a <u>function</u> taking three Int <u>values</u> as its arguments, and then uses them to <u>construct a new value</u>.

Type Constructor

Consider a binary tree to store Strings

data **SBTree = Leaf String** | **Branch String SBTree SBTree**

a type

SBTree	is a type
Leaf	is a data constructor (a function)
Branch	is a data constructor (a function)

Leaf :: String -> SBTree Branch :: String -> SBTree -> SBTree

Similar Type Constructors

Consider a binary tree to store Strings

data **SBTree = Leaf String** | **Branch String SBTree SBTree**

Consider a binary tree to store **Bool**

data BBTree = Leaf Bool | Branch Bool BBTree BBTree

Consider a binary tree to store a parameter type

data BTree a = Leaf a | Branch a (BTree a) (BTree a)

Type Constructor with a Parameter

Type constructors

Both **SBTree** and **BBTree** are type constructors

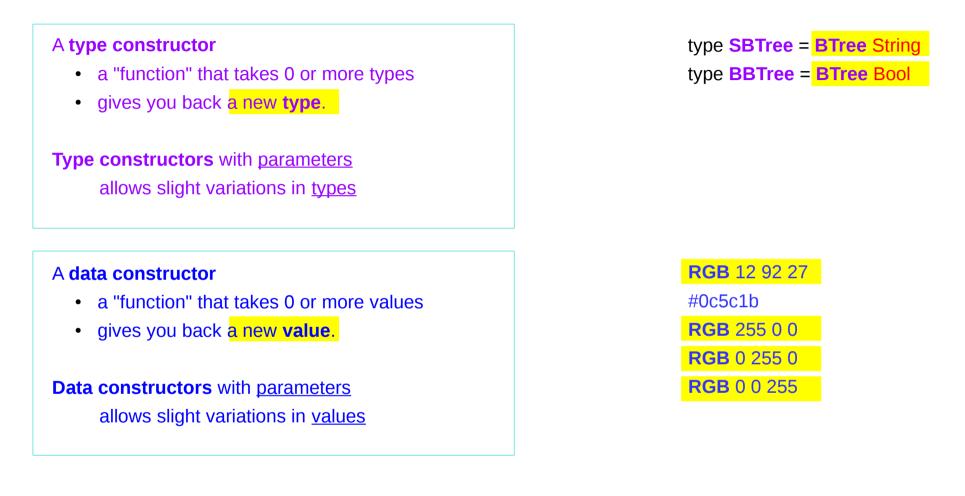
data SBTree = Leaf String |Branch String SBTree SBTreedata BBTree = Leaf Bool |Branch Bool BBTree BBTree

data BTree a = Leaf a | Branch a (BTree a) (BTree a)

Now we introduce a <u>type</u> <u>variable</u> a as a parameter to the type constructor.

BTree has become a <u>function</u>. It takes a type as its argument and it returns a new type.

Type Constructors and Data Constructors



() is both a type and a value.

() is a special **type**, pronounced "unit", has one **value** (), sometimes pronounced "void"

the **unit type** has only one **value** which is called **unit**.

()::()

Type :: Expression

It is the same as the void type void in Java or C/C++.

https://stackoverflow.com/questions/20380465/what-do-parentheses-used-on-their-own-mean

Unit Type

a **unit type** is a type that allows <u>only one value</u> (and thus can hold <u>no information</u>).

It is the same as the void type void in Java or C/C++.

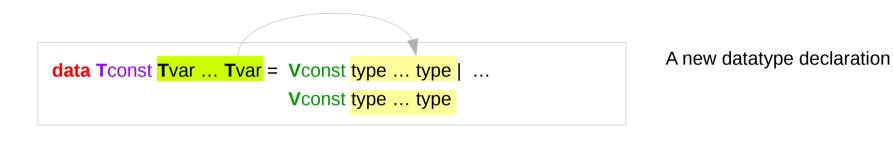
:t Expression :: Type data Unit = Unit

Prelude> :t Unit Unit :: Unit

Prelude> :t () () :: ()

https://stackoverflow.com/questions/20380465/what-do-parentheses-used-on-their-own-mean

Type Language and Expression Language



Tconst (Type Constructor) Vconst (Value Constructor) is added to *the type language* is added to *the expression language* and *its pattern sublanguage must <u>not</u> appear in types*

Argument types in Vconst type ... type are the types given to the arguments (Tconst Tvar ... Tvar) are used in expressions

https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly

Datatype Declaration Examples

data Tree a =	Leaf Node (Tree a) (Tree a)
Tree	(Type Constructor)
Leaf or Node	(Value Constructor)

data Type = Value

data	a () = ()
()	(Type Constructor)
()	(Value Constructor)

the type (), often pronounced "Unit" the value (), sometimes pronounced "void"

the type () containing only one value ()

https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly

Monadic Effect

class Monad m where

return :: a -> m a

(>>=) :: m a -> (a -> m b) -> m b

https://en.wikibooks.org/wiki/Haskell/Understanding_monads/IO https://stackoverflow.com/questions/2488646/why-are-side-effects-modeled-as-monads-in-haskell https://stackoverflow.com/questions/7840126/why-monads-how-does-it-resolve-side-effects https://stackoverflow.com/questions/2488646/why-are-side-effects-modeled-as-monads-in-haskell

https://www.cs.hmc.edu/~adavidso/monads.pdf

IO ()

Monadic operations tend to have types which look like

val-in-type-1 -> ... -> val-in-type-n -> effect-monad val-out-type

where the **return type** is a type application: the function tells you which **effects** are possible and the argument tells you what sort of value is produced by the operation

https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly

IO () - Effect Monad

put :: s -> State s ()

```
put :: s -> (State s) ( )
```

one value input type **s** the **effect-monad State s** the value output type **()**

the operation is used *only for its effect*; the *value* delivered is *uninteresting*

putStr :: String -> IO ()

delivers a string to stdout but does not return anything exciting.

https://stackoverflow.com/questions/16892570/what-is-in-haskell-exactly

Functional & Imperative Languages

Imperative programming:

- variables as changeable locations in a computer's memory
- imperative programs explicitly commands the computer what to do

functional programming

- a way to think in higher-level mathematical terms
- defining how variables relate to one another
- leaving the compiler to translate these
 - to the step-by-step instructions that the computer can process.

Haskell Language Features

Haskell functional programming

- Immutability
- Recursive Definition
- No Data Dependency

Redefinition : not allowed

r = 5 r = 2

imperative programming:

after setting r = 5 and then changing it to r = 2.

Hakell programming:

an error: "multiple declarations of r".

Within a given scope, a variable in Haskell

gets defined only once and cannot change.

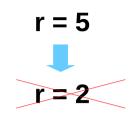
like variables in mathematics.

Immutable: They vary only based on the data we enter into a program.

We can't define r two ways in the same code,

but we could change the value by changing the file

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions



No mutation In Haskell

Variable definition in a file

Var1.hs r = 5	Var2.hs r = 55	(
young@Sys ~ \$ ghci GHCi, version 7.10.3: http://ww Prelude> :load Var1.hs [1 of 1] Compiling Main Ok, modules loaded: Main. *Main> r		
5 *Main> :t r r :: Integer *Main> *Main> :load Var2.hs [1 of 1] Compiling Main Ok, modules loaded: Main. *Main> r 55	(var2.hs, interpreted)	

definition with initialization

No Mutation

Var1.hs r = 5	Var2.hs r = 55	No mutation
*Main> r = 33 <interactive>:12:3: par</interactive>	se error on input '='	
young@Sys ~ \$ ghci GHCi, version 7.10.3: Prelude> r = 333 <interactive>:2:3: pars Prelude></interactive>	http://www.haskell.org/ghc/ :? for hel e error on input '='	lp
let r = 33		

Recursive Definition

r = r + 1

imperative programming:

incrementing the variable r

(updating the value in memory)

Hakell programming:

a recursive definition of r

(defining it in terms of itself)

if r had been defined with any value beforehand,

then r = r + 1 in Haskell would bring an error message.

No Data Dependence

y = x * 2	x = 3
x = 3	y = x * 3

Hakell programming:

because their values of variables do not change within a program

variables can be defined in any order

there is no notion of "x being declared before y" or the other way around.

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

Evaluation

area 5 => { replace the LHS area r = ... by the RHS ... = pi * r^2 } pi * 5 ^ 2 => { replace pi by its numerical value } 3.141592653589793 * 5 ^ 2 => { apply exponentiation (^) } 3.141592653589793 * 25

- => { apply multiplication (*) }
 - 78.53981633974483

replace each function with its definition

calculate the results until a single value remains.

to <u>apply</u> or <u>call</u> <u>a function</u> means

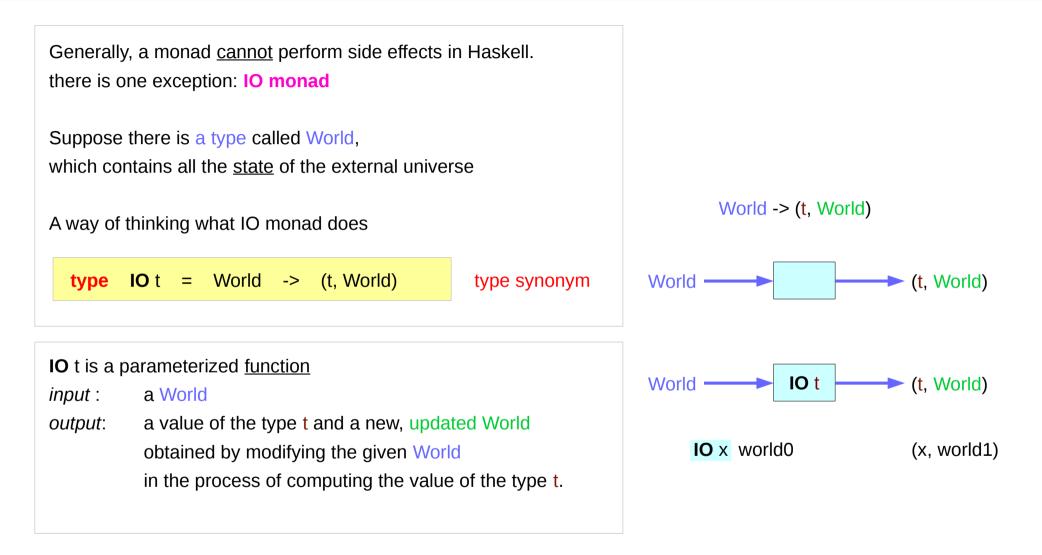
to replace the LHS of its definition by its RHS.

https://en.wikibooks.org/wiki/Haskell/Variables_and_functions

area r = pi * r^2

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Side Effects of IO Monad



Type Synonym IO t

IO t is a parameterized <u>function</u>

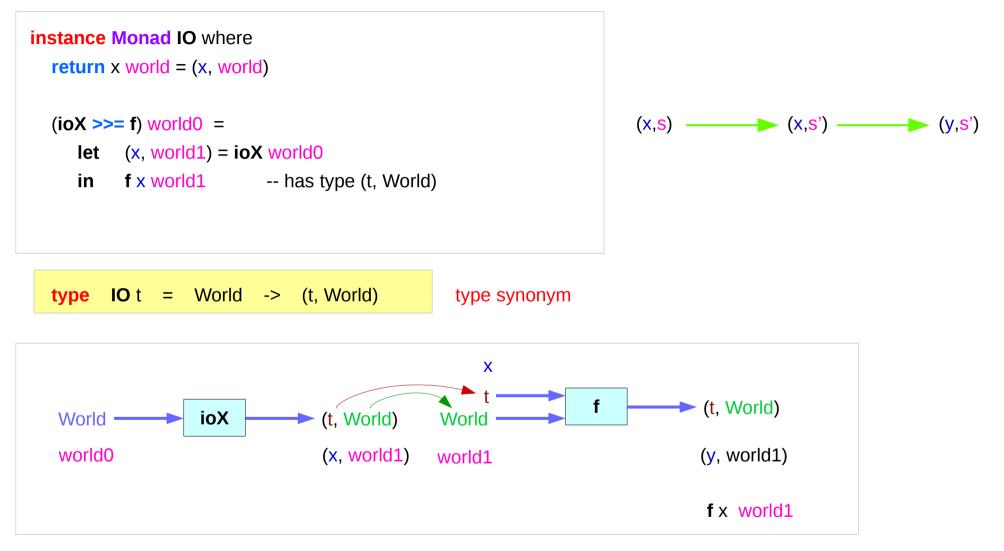
input : a World

output: a value of the type t and a new, updated World obtained by modifying the given World in the process of computing the value of the type t.

It is <u>impossible</u> to store the extra copies of the contents of your hard drive that each of the Worlds contains

given World \rightarrow updated World

IO Monad Implementation



Monad IO and Monad ST

instance Monad IO where return x world = (x, world) (ioX >>= f) world0 = let (x, world1) = ioX world0 in f x world1 -- has type (t, World) instance Monad ST where -- return :: a -> ST a return x = \s -> (x,s) -- (>>=) :: ST a -> (a -> ST b) -> ST b st >>= f = \s -> let (x,s') = st s in f x s'

type IO t = World -> (t, World)

type synonym

State Transformers ST

instance Monad ST where -- return :: a -> ST a return x = \s -> (x,s)

-- (>>=) :: ST a -> (a -> ST b) -> ST b st >>= f = |s -> let (x,s') = st s in f x s'

>>= provides a means of sequencing state transformers: st >>= f applies the state transformer st to an initial state s, then applies the function f to the resulting value x to give a second state transformer (f x), which is then applied to the modified state s' to give the final result: $st >>= f = \langle s -> f \times s' \rangle$ where (x,s') = st s

$$st \gg = f = \langle s \rangle \langle y, s' \rangle$$

where $(x, s') = st s$
 $(y, s') = f x s'$

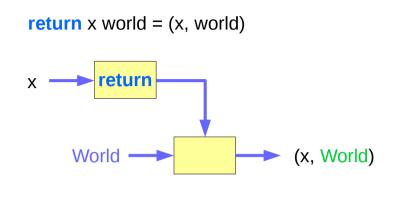
(x,s') = st s

f X S'

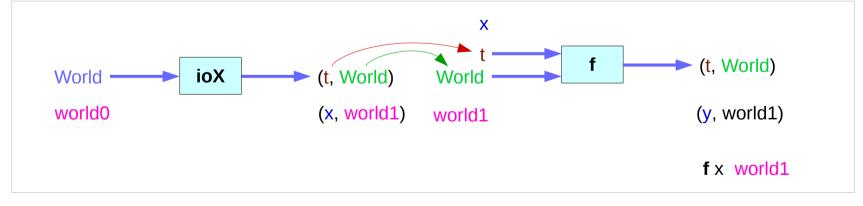
https://cseweb.ucsd.edu/classes/wi13/cse230-a/lectures/monads2.html

Monad IO - return

The **return** function takes x and gives back a <u>function</u> that takes a World and returns x along with the new, updated World (=World) formed by not modifying the World it was given

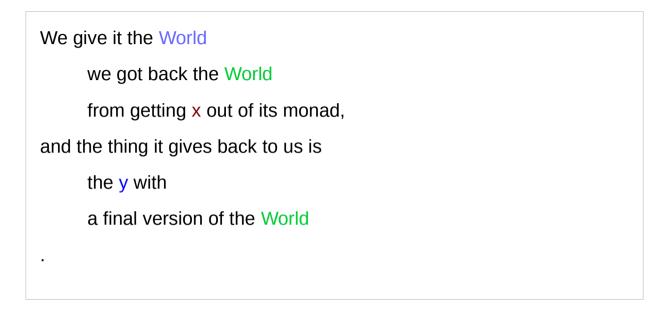






https://www.cs.hmc.edu/~adavidso/monads.pdf

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the implementation of bind

(t,World) (t,World) (t,World) (x,world0) (x,world1) (y,world1)

https://www.cs.hmc.edu/~adavidso/monads.pdf

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Which World was given initially? Which World was updated?

In GHC, a main must be defined somewhere with type IO ()

a program execution <u>starts</u> from the **main** the initial World is contained in the **main** to start everything off the **main** passes the updated World from each **IO** to the next **IO** as its initial World

an **IO** that is <u>not reachable</u> from **main** will <u>never be executed</u> an initial / updated World is not passed to such an **IO** The modification of the World



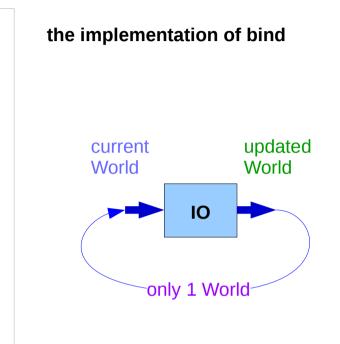
when using **GHCI**, everything is wrapped in **an implicit IO**, since the results get printed out to the screen.

Every time a <u>new command</u> is given to GHCI, GHCI passes the current World,

GHCI gets the *result* of the command back, GHCI request to display the *result* (which updates the World by modifying

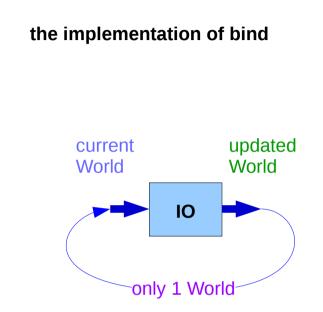
- the contents of the screen or
- the list of defined variables or
- the list of loaded modules or whatever),

and then saves the new World to give to the next command.



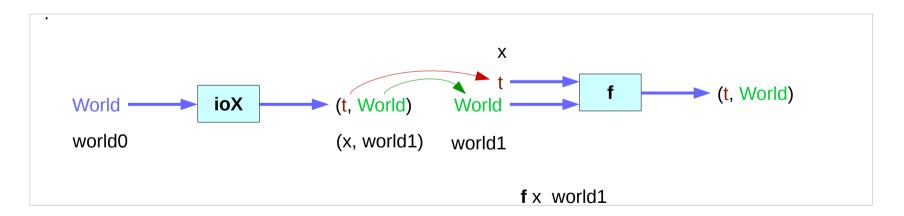
when using **GHCI**, everything is wrapped in **an implicit IO**, since the results get printed out to the screen.

there's only 1 World in existence at any given moment. Each IO takes that one and only World, consumes it, and gives back a single new World. Consequently, there's no way to accidentally run out of Worlds, or have multiple ones running around.



the expression (ioX >>= f) has type World -> (t, World)
a function that takes a World, called world0,
which is used to extract x from its IO monad.
This gets passed to f, resulting in another IO monad,
 which again is a function that takes a World
 and returns a x and a new, updated World.
We give it the World we got back from getting x out of its monad,

and the thing it gives back to us is the t with a final version of the World



https://www.cs.hmc.edu/~adavidso/monads.pdf

the implementation of bind

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References

- [1] ftp://ftp.geoinfo.tuwien.ac.at/navratil/HaskellTutorial.pdf
- [2] https://www.umiacs.umd.edu/~hal/docs/daume02yaht.pdf