

# Utility Functions Octave Codes (0A)

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Based on  
M.J. Roberts, Fundamentals of Signals and Systems

# Singularity Functions – Continuous Time

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- $u(t)$
- $\text{ramp}(t)$
- $\text{rect}(t)$
- $\text{tri}(t)$
- $\text{drcl}(t)$

# u(t), ramp(t), rect(t), tri(t)

```
# Prevent Octave from thinking that this
# is a function file:
1;

function y = u(t)
    zro = t == 0; pos = t > 0; y = zro/2 + pos;
endfunction

function y = ramp(t)
    y = t.*(t >= 0);
endfunction

function y = rect(t)
    y = u(t+0.5) - u(t-0.5);
endfunction

function y = tri(t)
    y = ramp(t+1) - 2*ramp(t) + ramp(t-1);
endfunction
```

# u(t)

```
function y = u(t)
    zro = t == 0; pos = t > 0; y = zro/2 + pos;
endfunction
```

t > 0 :	zro=0, pos=1	y=1
t = 0 :	zro=1, pos=0	y=0.5
t < 0 :	zro=0, pos=0	y=0

# ramp(t)

```
function y = ramp(t)
    y = t.*(t >= 0);
endfunction
```

(t>=0)

t > 0 :	1	.*	t	t
t = 0 :	1	.*	t	t
t < 0 :	0	.*	t	0

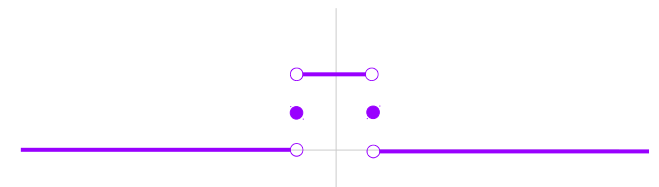
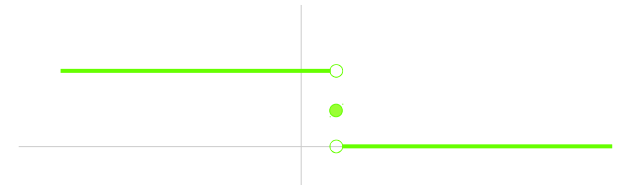
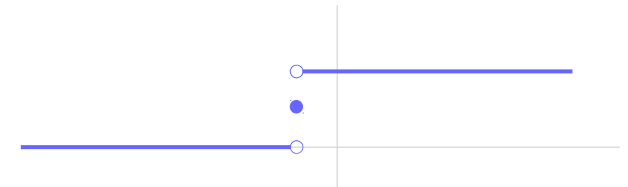
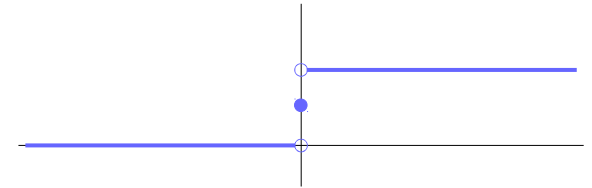
# rect(t)

```
function y = rect(t)
    y = u(t+0.5) - u(t-0.5);
endfunction
```

$t+0.5 > 0$	:	$u(t+0.5) = 1$
$t+0.5 = 0$	:	$u(t+0.5) = 0.5$
$t+0.5 < 0$	:	$u(t+0.5) = 0$

$t-0.5 > 0$	:	$u(t-0.5) = 1$
$t-0.5 = 0$	:	$u(t-0.5) = 0.5$
$t-0.5 < 0$	:	$u(t-0.5) = 0$

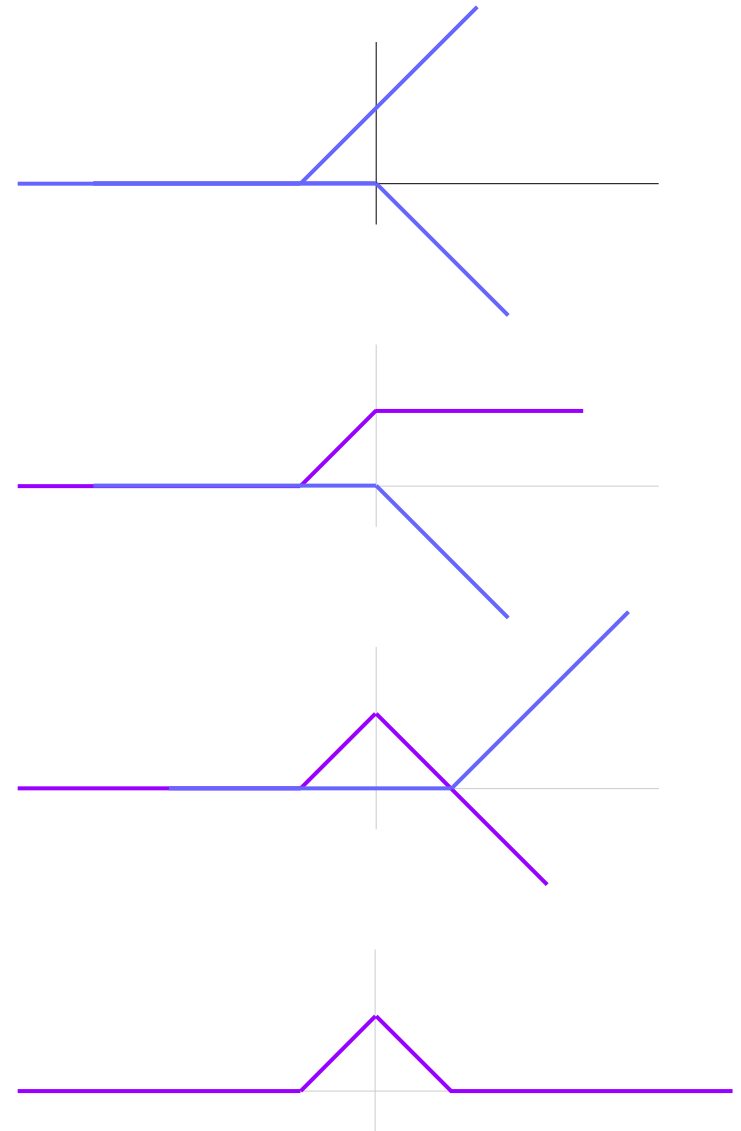
$t > +0.5$	:	$\text{rect}(t) = 0$
$t = +0.5$	:	$\text{rect}(t) = 0.5$
$-0.5 < t < +0.5$	:	$\text{rect}(t) = 1$
$t = -0.5$	:	$\text{rect}(t) = 0.5$
$t < -0.5$	:	$\text{rect}(t) = 0$





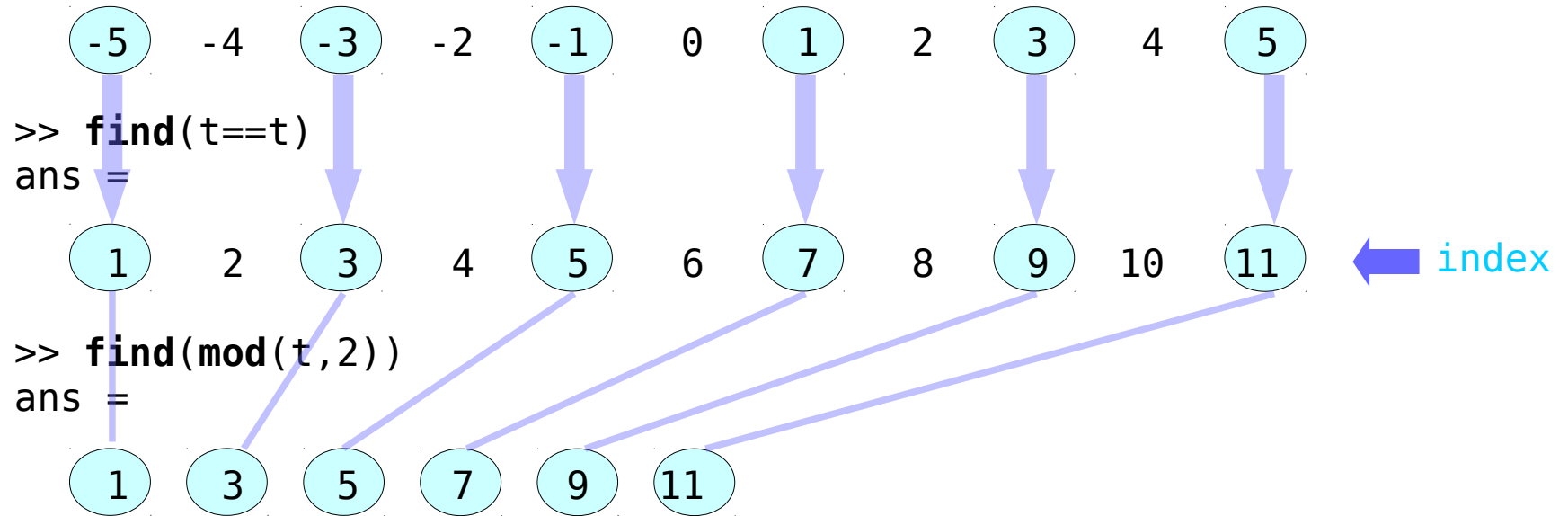
# $u(t)$ , $\text{ramp}(t)$ , $\text{rect}(t)$ , $\text{tri}(t)$

```
function y = tri(t)
    y = ramp(t+1) - 2*ramp(t) + ramp(t-1);
endfunction
```



# find( )

```
>> t = -5:+5  
t =
```



# drcl(t,N)

```
function x = drcl(t,N)
    num = sin(N*pi*t);
    den = N*sin(pi*t);
    I = find(abs(den) < 100*eps);
    num(I) = cos(N*pi*t(I)); den(I) = cos(pi*t(I));
    x = num ./ den ;
endfunction
```

$$f(t) = \frac{\sin(N\pi t)}{N\sin(\pi t)}$$

$$f(0) = \lim_{t \rightarrow 0} \frac{\sin(N\pi t)}{N\sin(\pi t)} = \lim_{t \rightarrow 0} \frac{N\pi \cos(N\pi t)}{N\pi \cos(\pi t)} = \lim_{t \rightarrow 0} \frac{\cos(N\pi t)}{\cos(\pi t)}$$

100\*eps = 2.2204e-14 : values very close to zero

# The function **eps**

**eps** is the relative spacing between any two adjacent numbers in the machine's floating point system.

system dependent  
IEEE floating point arithmetic

**eps** is approximately  
2.2204e-16 for double precision  
1.1921e-07 for single precision.

**eps** return a scalar with the value **eps** (1.0).

**eps**(x) return the distance between x and the next larger value.

**eps**(n,m, k, ...) matrix dimensions

**eps**(..., "double")

**eps**(..., "single")

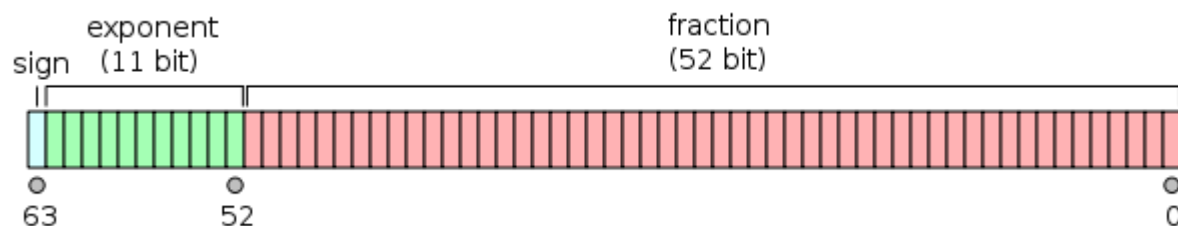
# The function `eps(x)`

```
>> num2hex(1)
ans = 3ff0000000000000
>> num2hex(1+eps(1))
ans = 3ff0000000000001
>> num2hex(eps(1))
ans = 3cb0000000000000
>>
>> hex2dec("3cb") - 1023
ans = -52
```

`1*eps`

```
>> num2hex(10)
ans = 4024000000000000
>> num2hex(10+eps(10))
ans = 4024000000000001
>> num2hex(eps(10))
ans = 3ce0000000000000
>>
>> hex2dec("3ce") - 1023
ans = -49
```

`8*eps`



[https://en.wikipedia.org/wiki/Double-precision\\_floating-point\\_format](https://en.wikipedia.org/wiki/Double-precision_floating-point_format)

# Testing CT Singularity Functions

```
t = -10:0.1:+10;

subplot(5, 1, 1);
plot(t, u(t)); ylabel('u(t)');

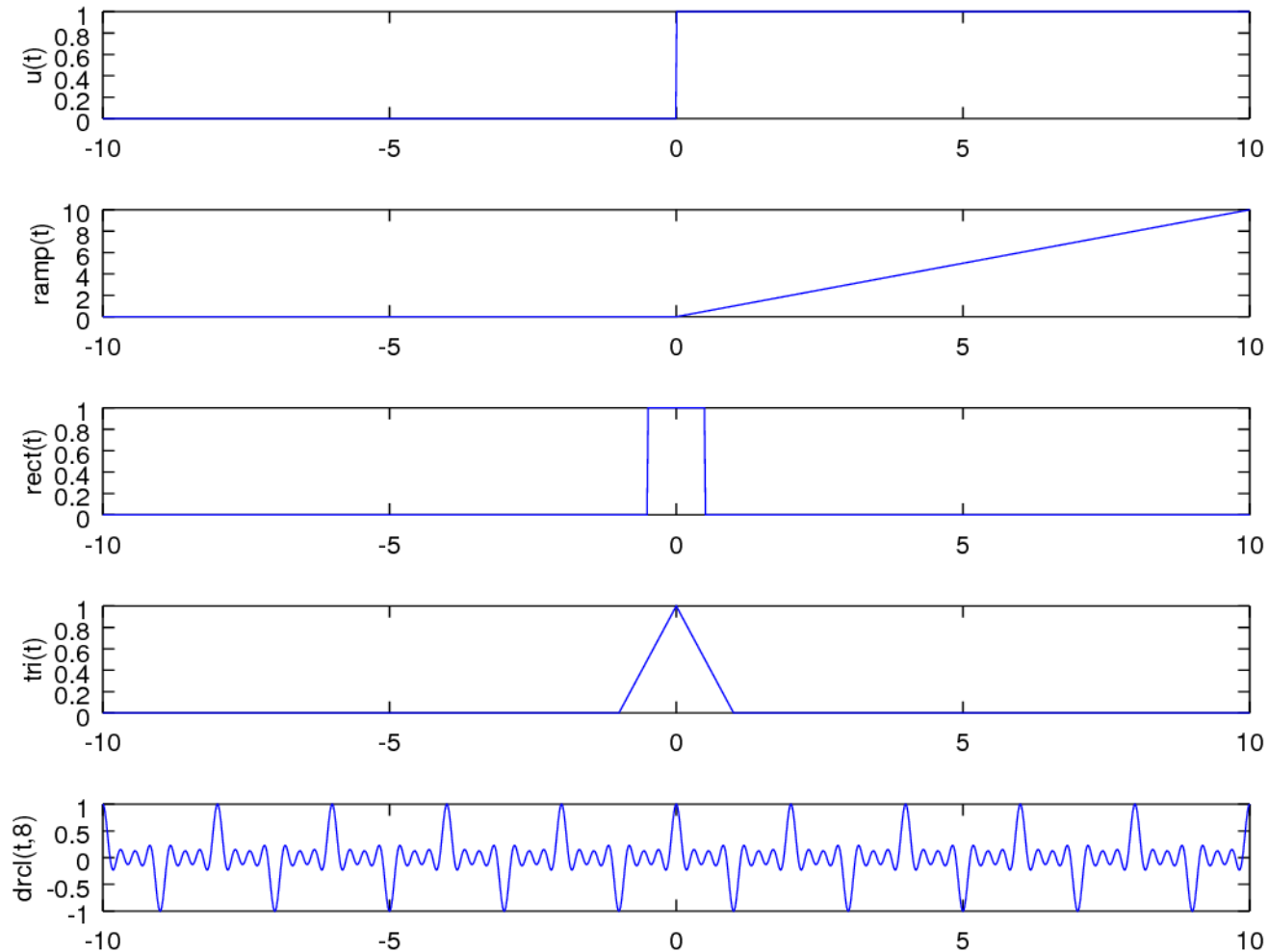
subplot(5, 1, 2);
plot(t, ramp(t)); ylabel('ramp(t)');

subplot(5, 1, 3);
plot(t, rect(t)); ylabel('rect(t)');

subplot(5, 1, 4);
plot(t, tri(t)); ylabel('tri(t)');

subplot(5, 1, 5);
plot(t, drcl(t, 2)); ylabel('drcl(t,2)');
```

# Test Results for CT Singularity Functions



# Singularity Functions – Discrete Time

---

- $\text{impD}(n)$
- $\text{uD}(n)$
- $\text{rampD}(n)$
- $\text{rectD}(W,n)$
- $\text{impND}(N,n)$



# impD(n), uD(n), rampD(n)

```
# Prevent Octave from thinking that this
# is a function file:
1;
```

```
function y = impD(n)
  y = double(n == 0);
  ss = find(round(n) ~= n);
  y(ss) = NaN;
endfunction
```

```
function y = uD(n)
  y = double(n >= 0);
  ss = find(round(n) ~= n);
  y(ss) = NaN;
endfunction
```

```
function y = rampD(n)
  pos = double(n>0);
  y = n.*pos;
  ss = find(round(n) ~= n);
  y(ss) = NaN;
endfunction
```

# rectD(W,n), impND(N,n)

```
function y = rectD(W,n);
    if (W == round(W))
        y = double(abs(n) <= abs(W));
        ss = find(round(n) ~= n);
        y(ss) = NaN;
    else
        disp('In rectD, width parameter, W, is not an
integer');
    endif
endfunction
```

```
function y = impND(N, n)
    if (N == round(N))
        y = double(n/N == round(n/N));
        ss = find(round(n) ~= n);
        y(ss) = NaN;
    else
        disp('In impND, period parameter, N, is not an
integer');
    endif
endfunction
```

# impD(n)

```
function y = impD(n)
  y = double(n == 0);
  ss = find(round(n) ~= n);
  y(ss) = NaN;
endfunction
```

n = -1	(n==0) 0	double 0.	round(n)=-1
n = 0	(n==0) 1	double 1.	round(n)= 0
n = +1	(n==0) 0	double 0.	round(n)=+1
n = +1.5	(n==0) 0	NaN	round(n)=+1

# uD(n)

```
function y = uD(n)
  y = double(n >= 0);
  ss = find(round(n) ~= n);
  y(ss) = NaN;
endfunction
```

n = -1	(n>=0) 0	double 0.	round(n)=-1
n = 0	(n>=0) 1	double 1.	round(n)= 0
n = +1	(n>=0) 1	double 1.	round(n)=+1
n = +1.5	(n>=0) 1	NaN	round(n)=+1

# rampD(n)

```
function y = rampD(n)
    pos = double(n>0);
    y = n.*pos;
    ss = find(round(n) ~= n);
    y(ss) = NaN;
endfunction
```

n = -1	(n>0)	0	n * double 0.	round(n)=-1
n = 0	(n>0)	0	n * double 0.	round(n)= 0
n = +1	(n>0)	1	n * double 1.	round(n)=+1
n = +1.5	(n>0)	1	NaN	round(n)=+1

# rectD(W,n)

```
function y = rectD(W,n);  
    if (W == round(W))  
        y = double(abs(n) <= abs(W));  
        ss = find(round(n) ~= n);  
        y(ss) = NaN;  
    else  
        disp('width parameter W is not an integer');  
    endif  
endfunction
```

n = -2	abs(n) 2	abs(W) 1	double 0.	round(n)=-2
n = -1	abs(n) 1	abs(W) 1	double 1.	round(n)=-1
n = 0	abs(n) 0	abs(W) 1	double 1.	round(n)= 0
n = +1	abs(n) 1	abs(W) 1	double 1.	round(n)=+1
n = +2	abs(n) 2	abs(W) 1	double 0.	round(n)=+2

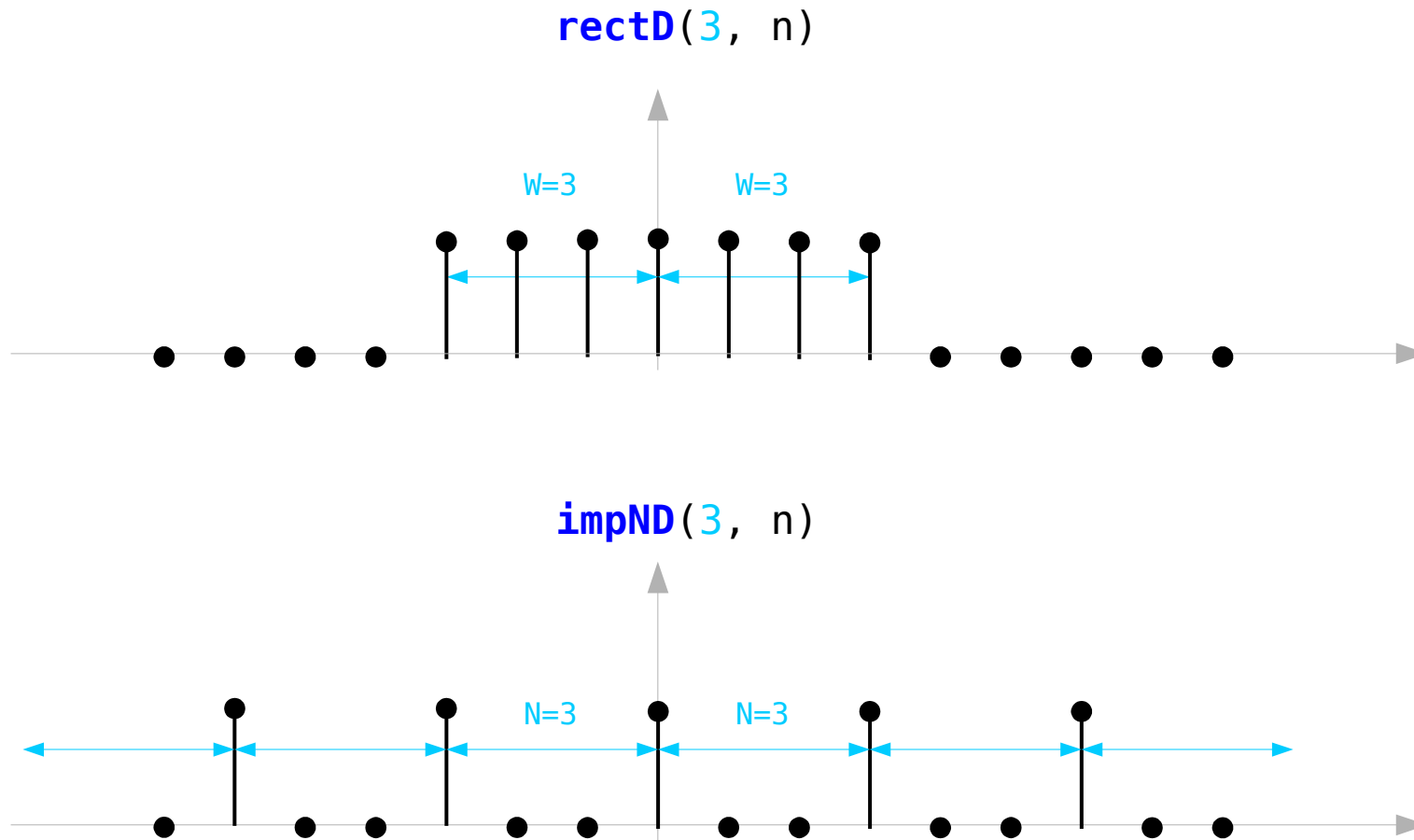
n = +1.5	abs(n) 1.5	abs(W) 1	NaN	round(n)=+1
----------	------------	----------	-----	-------------

# impND(N,n)

```
function y = impND(N, n)
  if (N == round(N)) ----- integer N
    y = double(n/N == round(n/N)); ----- integer (n/N)
    ss = find(round(n) ~= n);
    y(ss) = NaN;
  else
    disp('period parameter N is not an integer');
  endif
endfunction
```

y becomes 1.0 when n is integer multiple of N (n = kN)  
Otherwise y is 0.0

# rectD(3,n) and impND(3,n)





# Testing DT Singularity Functions

```
n = -10: 10;

subplot(5, 1, 1);
stem(n, impD(n)); ylabel('impD(n)');

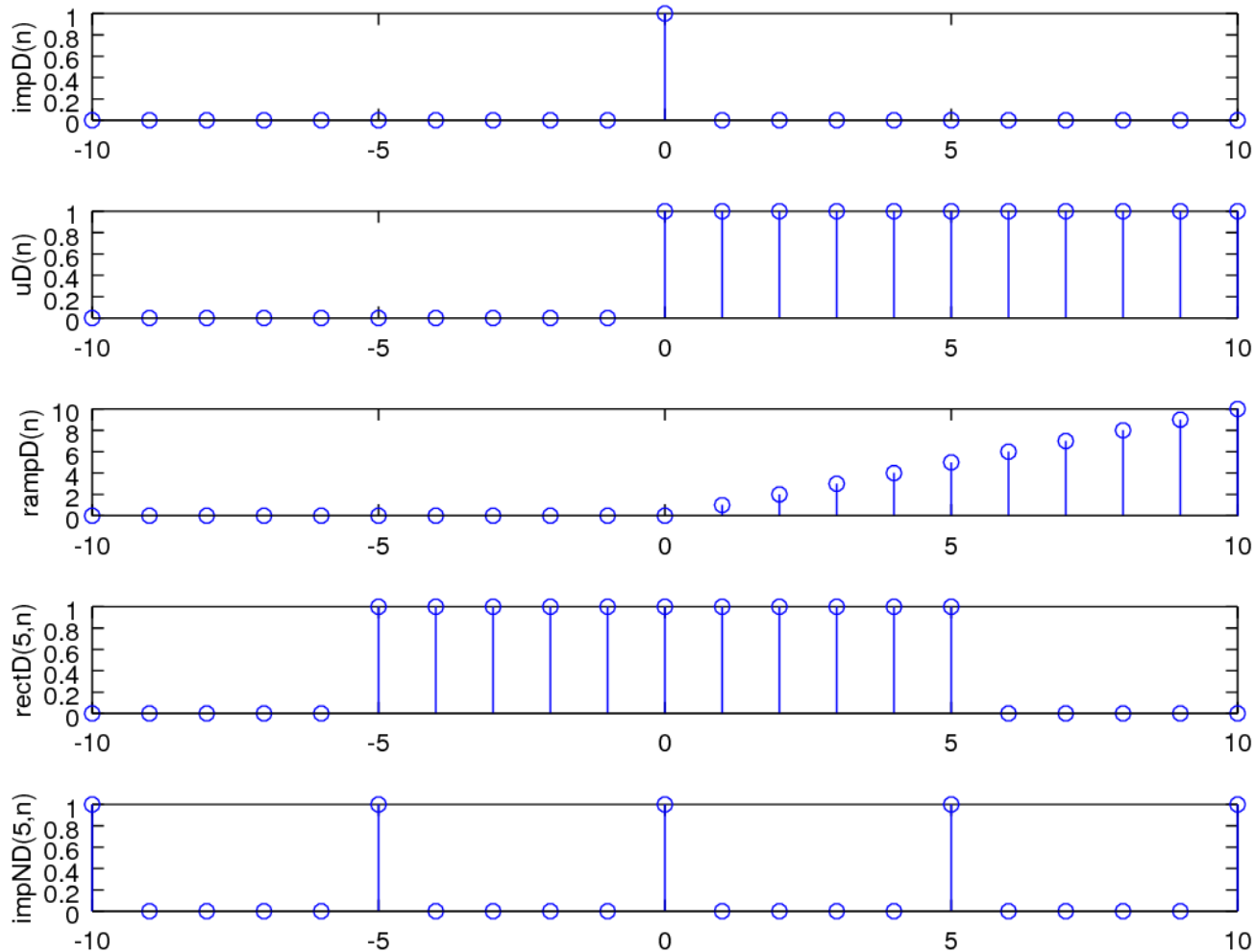
subplot(5, 1, 2);
stem(n, uD(n)); ylabel('uD(n)');

subplot(5, 1, 3);
stem(n, rampD(n)); ylabel('rampD(n)');

subplot(5, 1, 4);
stem(n, rectD(5, n)); ylabel('rectD(5,n)');

subplot(5, 1, 5);
stem(n, impND(5, n)); ylabel('impND(5,n)');
```

# Test Results for DT Singular Functions



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## References

- [1] <http://en.wikipedia.org/>
- [2] J.H. McClellan, et al., Signal Processing First, Pearson Prentice Hall, 2003
- [3] M.J. Roberts, Fundamentals of Signals and Systems
- [4] S.J. Orfanidis, Introduction to Signal Processing
- [5] K. Shin, et al., Fundamentals of Signal Processing for Sound and Vibration Engineerings
  
- [6] A “graphical interpretation” of the DFT and FFT, by Steve Mann